Computer algebra independent integration tests

Summer 2022 edition

8-Special-functions/204-8.1-Error-functions

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Contents

Chapter 1

Introduction

Local contents

This report gives the result of running the computer algebra independent integration test.

The download section in the appendix contains links to download the problems in plain text format used for all CAS systems.

The number of integrals in this report is [311]. This is test number [204].

1.1 Listing of CAS systems tested

The following are the CAS systems tested:

1. Mathematica 13.1 (June 29, 2022) on windows 10.
2. Rubi 4.16.1 (Dec 19, 2018) on Mathematica 13.0.1 on windows 10.
3. Maple 2022.1 (June 1, 2022) on windows 10.
4. Maxima 5.46 (April 13, 2022) using Lisp SBCL 2.1.11.debian on Linux via sagemath 9.6.
5. Fricas 1.3.8 (June 21, 2022) based on sbcl 2.1.11.debian on Linux via sagemath 9.6.
6. Giac/Xcas 1.9.0-13 (July 3, 2022) on Linux via sagemath 9.6.
7. Sympy 1.10.1 (March 20, 2022) Using Python 3.10.4 on Linux.
8. Mupad using Matlab 2021a with Symbolic Math Toolbox Version 8.7 on windows 10.

Maxima and Fricas and Giac are called using Sagemath. This was done using Sagemath `integrate` command by changing the name of the algorithm to use the different CAS systems.

Sympy was called directly from Python.

1.2 Results

Important note: A number of problems in this test suite have no antiderivative in closed form. This means the antiderivative of these integrals can not be expressed in terms of elementary, special functions or `Hypergeometric2F1` functions. `RootSum` and `RootOf` are not allowed.

If a CAS returns the above integral unevaluated within the time limit, then the result is counted as passed and assigned an A grade.

However, if CAS times out, then it is assigned an F grade even if the integral is not integrable, as this implies CAS could not determine that the integral is not integrable in the time limit.

If a CAS returns an antiderivative to such an integral, it is assigned an A grade automatically and this special result is listed in the introduction section of each individual test report to make it easy to identify as this can be important result to investigate.

The results given in in the table below reflects the above.

System	% solved	% Failed
Rubi	100.00 (311)	0.00 (0)
Mathematica	96.46 (300)	3.54 (11)
Fricas	82.96 (258)	17.04 (53)
Mupad	65.27 (203)	34.73 (108)
Sympy	63.67 (198)	36.33 (113)
Maple	57.56 (179)	42.44 (132)
Maxima	45.02 (140)	54.98 (171)
Giac	42.12 (131)	57.88 (180)

Table 1.1: Percentage solved for each CAS

The table below gives additional break down of the grading of quality of the antiderivatives generated by each CAS. The grading is given using the letters A,B,C and F with A being the best quality. The grading is accomplished by comparing the antiderivative generated with the optimal antiderivatives included in the test suite. The following table describes the meaning of these grades.

grade	description
A	Integral was solved and antiderivative is optimal in quality and leaf size.
B	Integral was solved and antiderivative is optimal in quality but leaf size is larger than twice the optimal antiderivatives leaf size.
C	Integral was solved and antiderivative is non-optimal in quality. This can be due to one or more of the following reasons 1. antiderivative contains a hypergeometric function and the optimal antiderivative does not. 2. antiderivative contains a special function and the optimal antiderivative does not. 3. antiderivative contains the imaginary unit and the optimal antiderivative does not.
F	Integral was not solved. Either the integral was returned unevaluated within the time limit, or it timed out, or CAS hanged or crashed or an exception was raised.

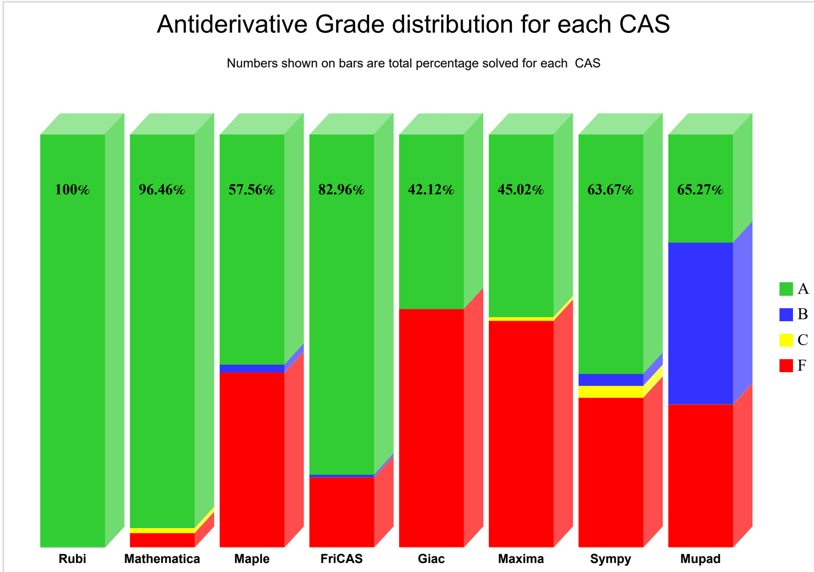
Table 1.2: Description of grading applied to integration result

Grading is implemented for all CAS systems. Based on the above, the following table summarizes the grading for this test suite.

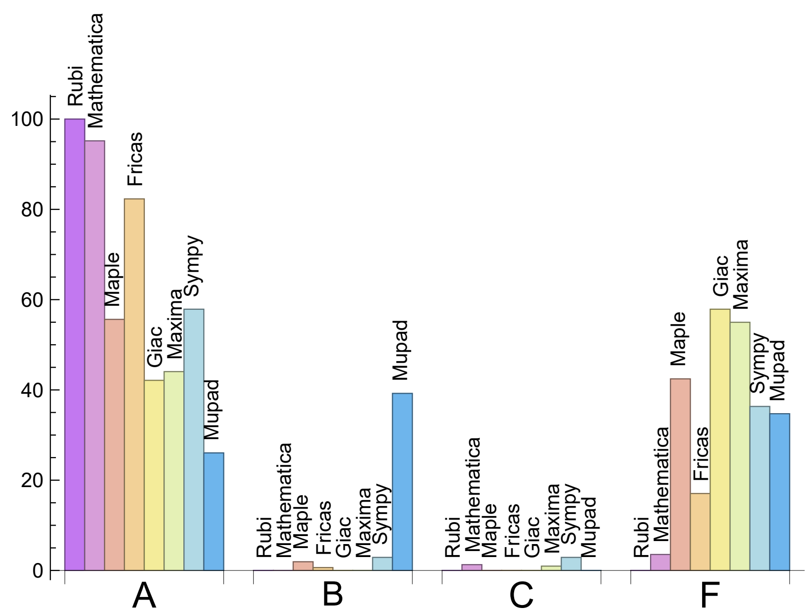
System	% A grade	% B grade	% C grade	% F grade
Rubi	100.00	0.00	0.00	0.00
Mathematica	95.18	0.00	1.29	3.54
Fricas	82.32	0.64	0.00	17.04
Sympy	57.88	2.89	2.89	36.33
Maple	55.63	1.93	0.00	42.44
Maxima	44.05	0.00	0.96	54.98
Giac	42.12	0.00	0.00	57.88
Mupad	N/A	39.23	0.00	34.73

Table 1.3: Antiderivative Grade distribution of each CAS

The following is a Bar chart illustration of the data in the above table.



The figure below compares the CAS systems for each grade level.



The following table shows the distribution of the different types of failure for each CAS. There are 3 types of reasons why it can fail. The first is when CAS returns back the input within the time limit, which means it could not solve it. This the typical normal failure **F** .

The second is due to time out. CAS could not solve the integral within the 3 minutes time limit which is assigned **F(-1)**.

The third is due to an exception generated. Assigned **F(-2)**. This most likely indicates an interface problem between sagemath and the CAS (applicable only to FriCAS, Maxima and

Giac) or it could be an indication of an internal error in CAS. This type of error requires more investigations to determine the cause.

System	Number failed	Percentage normal failure	Percentage timeout failure	Percentage exception failure
Rubi	0	0.00 %	0.00 %	0.00 %
Mathematica	11	100.00 %	0.00 %	0.00 %
Maple	132	100.00 %	0.00 %	0.00 %
Fricas	53	100.00 %	0.00 %	0.00 %
Giac	180	100.00 %	0.00 %	0.00 %
Maxima	171	100.00 %	0.00 %	0.00 %
Sympy	113	91.15 %	7.96 %	0.88 %
Mupad	108	100.00 %	0.00 %	0.00 %

Table 1.4: Failure statistics for each CAS

1.3 Time and leaf size Performance

The table below summarizes the performance of each CAS system in terms of time used and leaf size of results.

Mean size is the average leaf size produced by the CAS (before any normalization). The Normalized mean is relative to the mean size of the optimal anti-derivative given in the input files.

For example, if CAS has **Normalized mean** of 3, then the mean size of its leaf size is 3 times as large as the mean size of the optimal leaf size.

Median size is value of leaf size where half the values are larger than this and half are smaller (before any normalization). i.e. The Middle value.

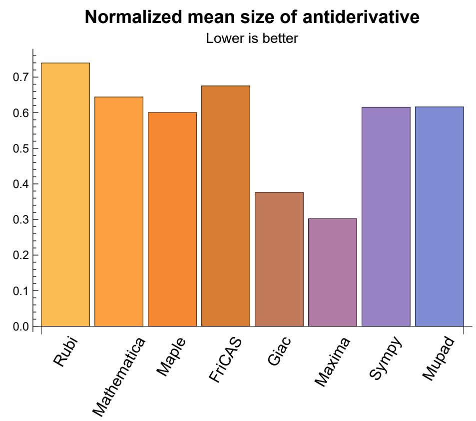
Similarly the **Normalized median** is relative to the median leaf size of the optimal.

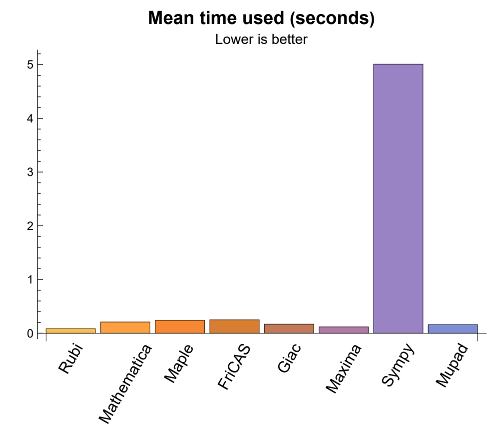
For example, if a CAS has Normalized median of 1.2, then its median is 1.2 as large as the median leaf size of the optimal.

System	Mean time (sec)	Mean size	Normalized mean	Median size	Normalized median
Rubi	0.08	68.68	0.74	59.00	1.00
Mathematica	0.21	56.41	0.64	51.00	0.77
Maple	0.24	56.07	0.60	26.00	0.81
Maxima	0.12	16.39	0.30	0.00	0.00
Fricas	0.25	64.41	0.68	51.00	0.76
Sympy	5.01	51.16	0.62	24.00	0.81
Giac	0.17	41.14	0.38	0.00	0.00
Mupad	0.16	52.44	0.62	24.00	0.77

Table 1.5: Time and leaf size performance for each CAS

The following are bar charts for the normalized leafsize and time used from the above table.


Normalized mean size of antiderivative
Lower is better
0.0
0.1
0.2
0.3
0.4
0.5
0.6
0.7
Rubi
Mathematica
Maple
FriCAS
Giac
Maxima
Sympy
Mupad


Mean time used (seconds)
Lower is better
0
1
2
3
4
5
Rubi
Mathematica
Maple
FriCAS
Giac
Maxima
Sympy
Mupad

1.4 list of integrals that has no closed form antiderivative

$\{19, 20, 21, 25, 32, 33, 34, 38, 39, 56, 57, 58, 59, 60, 61, 62, 63, 78, 79, 80, 88, 89, 90, 91, 92, 93, 94, 122, 123, 124, 128, 135, 136, 137, 141, 142, 159, 160, 161, 162, 163, 164, 165, 166, 181, 182, 183, 191, 192, 193, 194, 195, 196, 197, 225, 226, 227, 231, 238, 239, 240, 244, 245, 262, 263, 264, 265, 266, 267, 268, 269, 286, 287, 288, 296, 297, 298, 299, 300, 301, 302\}$

1.5 List of integrals solved by CAS but has no known antiderivative

Rubi {}

Mathematica {}

Maple {}

Maxima {}

Fricas {}

Sympy {}

Giac {}

Mupad {}

1.6 list of integrals solved by CAS but failed verification

The following are integrals solved by CAS but the verification phase failed to verify the anti-derivative produced is correct. This does not mean necessarily that the anti-derivative is wrong, as additional methods of verification might be needed, or more time is needed (3 minutes time limit was used). These integrals are listed here to make it easier to do further investigation to determine why it was not possible to verify the result produced.

Rubi $\{\}$

Mathematica $\{276, 277, 278, 280, 281, 282\}$

Maple Verification phase not implemented yet.

Maxima Verification phase not implemented yet.

Fricas Verification phase not implemented yet.

Sympy Verification phase not implemented yet.

Giac Verification phase not implemented yet.

Mupad Verification phase not implemented yet.

1.7 Timing

The command `AbsoluteTiming[]` was used in Mathematica to obtain the elapsed time for each integrate call. In Maple, the command `Usage` was used as in the following example

```
cpu_time := Usage(assign ('result_of_int',int(expr,x)),output='realtime'
```

For all other CAS systems, the elapsed time to complete each integral was found by taking the difference between the time after the call completed from the time before the call was made. This was done using Python's `time.time()` call.

All elapsed times shown are in seconds. A time limit of 3 CPU minutes was used for each integral. If the integrate command did not complete within this time limit, the integral was aborted and considered to have failed and assigned an F grade. The time used by failed integrals due to time out was not counted in the final statistics.

1.8 Verification

A verification phase was applied on the result of integration for `Rubi` and `Mathematica`.

Future version of this report will implement verification for the other CAS systems. For the integrals whose result was not run through a verification phase, it is assumed that the antiderivative was correct.

Verification phase also had 3 minutes time out. An integral whose result was not verified could still be correct, but further investigation is needed on those integrals. These integrals were marked in the summary table below and also in each integral separate section so they are easy to identify and locate.

1.9 Important notes about some of the results

1.9.1 Important note about Maxima results

Since tests were run in a batch mode, and using an automated script, then any integral where Maxima needed an interactive response from the user to answer a question during the evaluation of the integral will fail.

The exception raised is `ValueError`. Therefore Maxima results is lower than what would result if Maxima was run directly and each question was answered correctly.

The percentage of such failures were not counted for each test file, but for an example, for the `Timofeev` test file, there were about 14 such integrals out of total 705, or about 2 percent. This percentage can be higher or lower depending on the specific input test file.

Such integrals can be identified by looking at the output of the integration in each section for Maxima. The exception message will indicate the cause of error.

Maxima integrate was run using SageMath with the following settings set by default

```
'besselexpand : true'
'display2d : false'
'domain : complex'
'keepfloat : true'
'load(to_poly_solve)'
'load(simplify_sum)'
'load(abs_integrate)' 'load(diag)'
```

SageMath automatic loading of Maxima `abs_integrate` was found to cause some problems. So the following code was added to disable this effect.

```
from sage.interfaces.maxima_lib import maxima_lib
maxima_lib.set('extra_definite_integration_methods', '[]')
```

```
maxima_lib.set('extra_integration_methods', '[]')
```

See `https://ask.sagemath.org/question/43088/integrate-results-that-are-different-from-using-maxima/` for reference.

1.9.2 Important note about FriCAS result

There were few integrals which failed due to SageMath interface and not because FriCAS system could not do the integration.

These will fail With error `Exception raised: NotImplementedError`.

The number of such cases seems to be very small. About 1 or 2 percent of all integrals. These can be identified by looking at the exception message given in the result.

1.9.3 Important note about finding leaf size of antiderivative

For Mathematica, Rubi, and Maple, the builtin system function `LeafSize` was used to find the leaf size of each antiderivative.

The other CAS systems (SageMath and Sympy) do not have special builtin function for this purpose at this time. Therefore the leaf size for Fricas and Sympy antiderivative was determined using the following function, thanks to user `slelievre` at `https://ask.sagemath.org/question/57123/could-we-have-a-leaf_count-function-in-base-sagemath/`

```
def tree_size(expr):
    r"""
    Return the tree size of this expression.
    """
    if expr not in SR:
        # deal with lists, tuples, vectors
        return 1 + sum(tree_size(a) for a in expr)
    expr = SR(expr)
    x, aa = expr.operator(), expr.operands()
    if x is None:
        return 1
    else:
        return 1 + sum(tree_size(a) for a in aa)
```

For Sympy, which was called directly from Python, the following code was used to obtain the leafsize of its result

```
try:
  # 1.7 is a fudge factor since it is low side from actual leaf count
  leafCount = round(1.7*count_ops(anti))

  except Exception as ee:
        leafCount =1
```

1.9.4 Important note about Mupad results

Matlab's symbolic toolbox does not have a leaf count function to measure the size of the antiderivative. Maple was used to determine the leaf size of Mupad output by post processing Mupad result.

Currently no grading of the antiderivative for Mupad is implemented. If it can integrate the problem, it was assigned a B grade automatically as a placeholder. In the future, when grading function is implemented for Mupad, the tests will be rerun again.

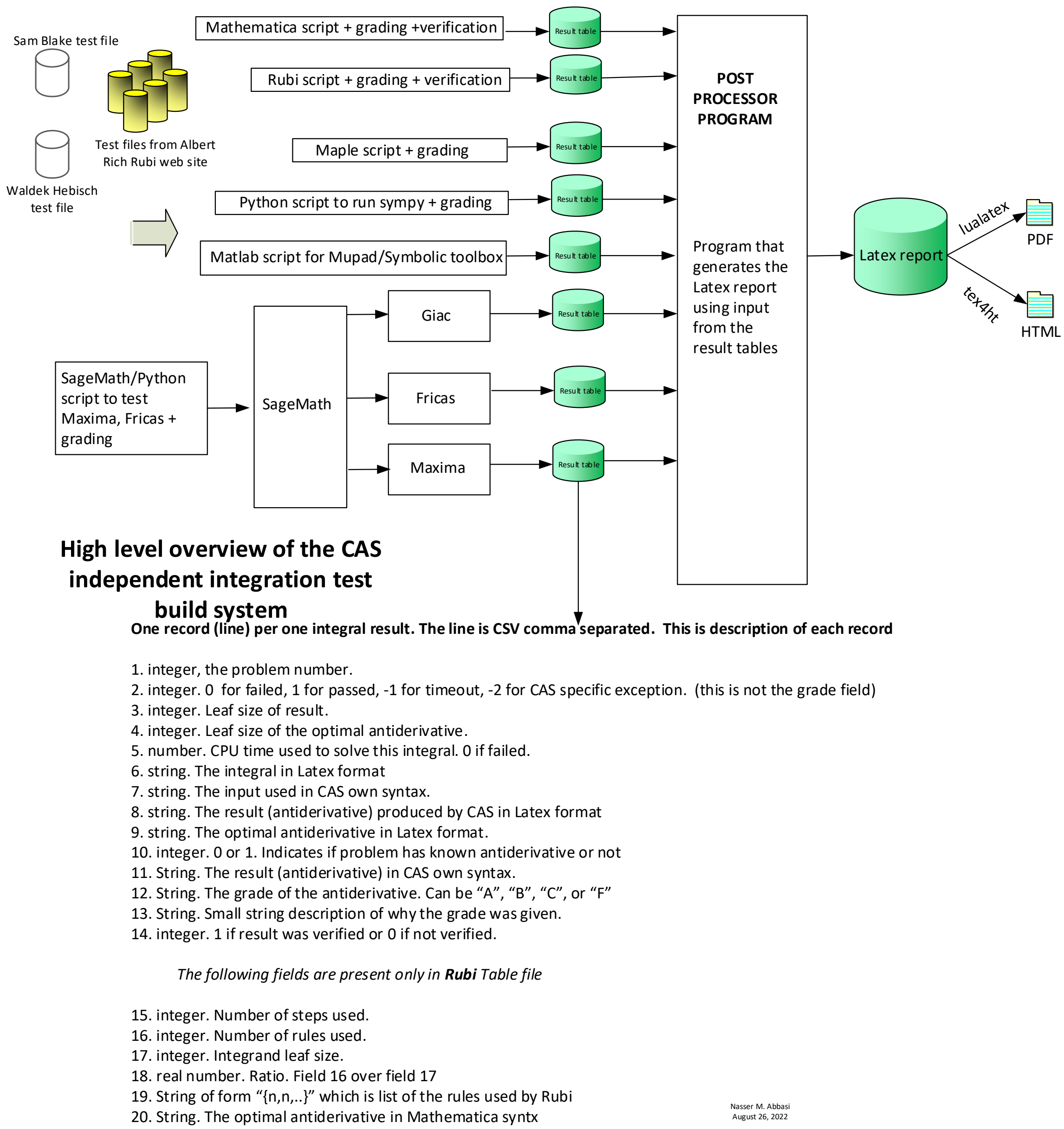
The following is an example of using Matlab's symbolic toolbox (Mupad) to solve an integral

```
integrand = evalin(symengine,'cos(x)*sin(x)')
the_variable = evalin(symengine,'x')
anti = int(integrand,the_variable)
```

Which gives `sin(x)^2/2`

1.10 Design of the test system

The following diagram gives a high level view of the current test build system.



Chapter 2

detailed summary tables of results

Local contents

2.1 List of integrals sorted by grade for each CAS

Local contents

2.1.1 Rubi

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227, 228, 229, 230, 231, 232, 233, 234, 235, 236, 237, 238, 239, 240, 241, 242, 243, 244, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 286, 287, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 299, 300, 301, 302, 303, 304, 305, 306, 307, 308, 309, 310, 311 }

B grade: { }

C grade: { }

F grade: { }

2.1.2 Mathematica

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227, 228, 229, 230, 231, 232, 233, 234, 235, 236, 237, 238, 239, 240, 243, 244, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 283, 284, 285, 286, 287, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 299, 300, 301, 302, 303, 308, 309, 310, 311 }

B grade: { }

C grade: { 242, 280, 281, 282 }

F grade: { 72, 98, 99, 175, 201, 202, 241, 304, 305, 306, 307 }

2.1.3 Maple

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 25, 29, 30, 31, 32, 33, 34, 37, 38, 39, 43, 47, 48, 50, 51, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 75, 76, 77, 78, 79, 80, 83, 87, 88, 89, 90, 91, 92, 93, 94, 95, 104, 105, 106, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 120, 121, 122, 123, 124, 128, 132, 133, 134, 135, 136, 137, 140, 141, 142, 146, 151, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 178, 179, 180, 181, 182, 183, 186, 191, 192, 193, 194, 195, 196, 197, 198, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 223, 224, 225, 226, 227, 231, 238, 239, 240, 244, 245, 249, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 286, 287, 288, 296, 297, 298, 299, 300, 301, 302, 303 }

B grade: { 118, 119, 150, 190, 221, 222 }

C grade: { }

F grade: { 22, 23, 24, 26, 27, 28, 35, 36, 40, 41, 42, 44, 45, 46, 49, 52, 67, 68, 69, 70, 71, 72, 73, 74, 81, 82, 84, 85, 86, 96, 97, 98, 99, 100, 101, 102, 103, 107, 125, 126, 127, 129, 130, 131, 138, 139, 143, 144, 145, 147, 148, 149, 152, 153, 154, 155, 170, 171, 172, 173, 174, 175, 176, 177, 184, 185, 187, 188, 189, 199, 200, 201, 202, 203, 204, 205, 206, 228, 229, 230, 232, 233, 234, 235, 236, 237, 241, 242, 243, 246, 247, 248, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 289, 290, 291, 292, 293, 294, 295, 304, 305, 306, 307, 308, 309, 310, 311 }

2.1.4 Maxima

A grade: { 1, 2, 3, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 18, 19, 20, 21, 25, 31, 32, 33, 34, 38, 39, 43, 47, 48, 49, 50, 51, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 77, 78, 79, 80, 83, 87, 88, 89, 90, 91, 92, 93, 94, 104, 105, 106, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 121, 122, 123, 124, 128, 135, 136, 137, 141, 142, 146, 159, 160, 161, 162, 163, 164, 165, 166, 181, 182, 183, 186, 191, 192, 193, 194, 195, 196, 197, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 224, 225, 226, 227, 231, 238, 239, 240, 244, 245, 249, 262, 263, 264, 265, 266, 267, 268, 269, 286, 287, 288, 296, 297, 298, 299, 300, 301, 302 }

B grade: { }

C grade: { 207, 208, 209 }

F grade: { 4, 15, 16, 17, 22, 23, 24, 26, 27, 28, 29, 30, 35, 36, 37, 40, 41, 42, 44, 45, 46, 52, 53, 54, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 81, 82, 84, 85, 86, 95, 96, 97, 98, 99, 100, 101, 102, 103, 107, 118, 119, 120, 125, 126, 127, 129, 130, 131, 132, 133, 134, 138, 139, 140, 143, 144, 145, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 184, 185, 187, 188, 189, 190, 198, 199, 200, 201, 202, 203, 204, 205, 206, 210, 221, 222, 223, 228, 229, 230, 232, 233, 234, 235, 236, 237, 241, 242, 243, 246, 247, 248, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 289, 290, 291, 292, 293, 294, 295, 303, 304, 305, 306, 307, 308, 309, 310, 311 }

2.1.5 FriCAS

A grade: { 1, 2, 3, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 104, 105, 106, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 141, 142, 143, 144, 145, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 207, 208, 209, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227, 228, 229, 230, 231, 232, 233, 234, 235, 236, 237, 238, 239, 240, 241, 242, 243, 244, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 283, 284, 285, 286, 287, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 299, 300, 301, 302, 303 }

B grade: { 140, 146 }

C grade: { }

F grade: { 4, 67, 68, 69, 70, 71, 72, 73, 74, 96, 97, 98, 99, 100, 101, 102, 103, 107, 170, 171, 172, 173, 174, 175, 176, 177, 199, 200, 201, 202, 203, 204, 205, 206, 210, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 304, 305, 306, 307, 308, 309, 310, 311 }

2.1.6 Sympy

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 17, 18, 19, 20, 21, 22, 23, 24, 25, 32, 33, 34, 38, 39, 47, 48, 49, 50, 51, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 71, 72, 73, 78, 79, 80, 81, 82, 83, 88, 89, 91, 92, 93, 94, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 120, 121, 122, 123, 124, 125, 126, 127, 128, 135, 136, 137, 141, 142, 150, 151, 152, 153, 154, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 177, 181, 182, 183, 184, 185, 186, 191, 192, 194, 195, 196, 197, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 223, 224, 225, 226, 227, 228, 229, 230, 231, 238, 239, 240, 244, 245, 253, 254, 255, 256, 257, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 278, 279, 280, 286, 287, 288, 289, 290, 291, 296, 297, 299, 300, 301, 302, 303 }

B grade: { 15, 16, 52, 118, 119, 155, 221, 222, 258 }

C grade: { 74, 174, 175, 176, 218, 219, 220, 281, 282 }

F grade: { 26, 27, 28, 29, 30, 31, 35, 36, 37, 40, 41, 42, 43, 44, 45, 46, 53, 54, 55, 69, 70, 75, 76, 77, 84, 85, 86, 87, 90, 95, 96, 97, 98, 99, 100, 101, 102, 103, 129, 130, 131, 132, 133, 134, 138, 139, 140, 143, 144, 145, 146, 147, 148, 149, 156, 157, 158, 172, 173, 178, 179, 180, 187, 188, 189, 190, 193, 198, 199, 200, 201, 202, 203, 204, 205, 206, 232, 233, 234, 235, 236, 237, 241, 242, 243, 246, 247, 248, 249, 250, 251, 252, 259, 260, 261, 276, 277, 283, 284, 285, 292, 293, 294, 295, 298, 304, 305, 306, 307, 308, 309, 310, 311 }

2.1.7 Giac

A grade: { 1, 2, 3, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 25, 29, 30, 31, 32, 33, 34, 38, 39, 40, 41, 42, 43, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 75, 76, 77, 78, 79, 80, 86, 87, 88, 89, 90, 91, 92, 93, 94, 104, 105, 106, 111, 112, 113, 114, 118, 119, 120, 121, 122, 123, 124, 128, 132, 133, 134, 135, 136, 137, 141, 142, 143, 144, 145, 146, 159, 160, 161, 162, 163, 164, 165, 166, 181, 182, 183, 191, 192, 193, 194, 195, 196, 197, 225, 226, 227, 231, 238, 239, 240, 244, 245, 262, 263, 264, 265, 266, 267, 268, 269, 286, 287, 288, 296, 297, 298, 299, 300, 301, 302 }

B grade: { }

C grade: { }

F grade: { 4, 5, 6, 7, 22, 23, 24, 26, 27, 28, 35, 36, 37, 44, 45, 46, 47, 48, 49, 50, 51, 52, 67, 68, 69, 70, 71, 72, 73, 74, 81, 82, 83, 84, 85, 95, 96, 97, 98, 99, 100, 101, 102, 103, 107, 108, 109, 110, 115, 116, 117, 125, 126, 127, 129, 130, 131, 138, 139, 140, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 184, 185, 186, 187, 188, 189, 190, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 228, 229, 230, 232, 233, 234, 235, 236, 237, 241, 242, 243, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 289, 290, 291, 292, 293, 294, 295, 303, 304, 305, 306, 307, 308, 309, 310, 311 }

2.1.8 Mupad

A grade: { 19, 20, 21, 25, 32, 33, 34, 38, 39, 56, 57, 58, 59, 60, 61, 62, 63, 78, 79, 80, 88, 89, 90, 91, 92, 93, 94, 122, 123, 124, 128, 135, 136, 137, 141, 142, 159, 160, 161, 162, 163, 164, 165, 166, 181, 182, 183, 191, 192, 193, 194, 195, 196, 197, 225, 226, 227, 231, 238, 239, 240, 244, 245, 262, 263, 264, 265, 266, 267, 268, 269, 286, 287, 288, 296, 297, 298, 299, 300, 301, 302 }

B grade: { 1, 2, 3, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 22, 23, 24, 29, 30, 31, 35, 36, 37, 43, 47, 48, 49, 50, 51, 52, 53, 54, 55, 64, 65, 66, 75, 76, 77, 81, 82, 83, 86, 87, 95, 104, 105, 106, 108, 109, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 125, 126, 127, 146, 150, 151, 152, 153, 154, 155, 167, 168, 169, 184, 185, 186, 207, 208, 209, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 228, 229, 230, 249, 253, 254, 255, 256, 257, 258, 259, 260, 261, 270, 271, 272, 283, 284, 285, 289, 290, 291, 294, 295, 303 }

C grade: { }

F grade: { 4, 26, 27, 28, 40, 41, 42, 44, 45, 46, 67, 68, 69, 70, 71, 72, 73, 74, 84, 85, 96, 97, 98, 99, 100, 101, 102, 103, 107, 110, 129, 130, 131, 132, 133, 134, 138, 139, 140, 143, 144, 145, 147, 148, 149, 156, 157, 158, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 187, 188, 189, 190, 198, 199, 200, 201, 202, 203, 204, 205, 206, 210, 232, 233, 234, 235, 236, 237, 241, 242, 243, 246, 247, 248, 250, 251, 252, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 292, 293, 304, 305, 306, 307, 308, 309, 310, 311 }

2.2 Detailed conclusion table per each integral for all CAS systems

Detailed conclusion table per each integral is given by table below. The elapsed time is in seconds. For failed result it is given as F(-1) if the failure was due to timeout. It is given as F(-2) if the failure was due to an exception being raised, which could indicate a bug in the system. If the failure was due to integral not being evaluated within the time limit, then it is given just an F.

In this table,the column `N.S.` in the table below, which stands for **normalized size** is defined as $\frac{\text{antiderivative leaf size}}{\text{optimal antiderivative leaf size}}$. To help make the table fit, **Mathematica** was abbreviated to **MMA**.

Problem 1	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	96	96	72	83	63	63	88	64	108
N.S.	1	1.00	0.75	0.86	0.66	0.66	0.92	0.67	1.12
time (sec)	N/A	0.062	0.019	0.230	0.263	0.379	0.509	0.409	0.471

Problem 2	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	63	65	55	55	65	56	88
N.S.	1	1.00	0.89	0.92	0.77	0.77	0.92	0.79	1.24
time (sec)	N/A	0.043	0.017	0.207	0.262	0.370	0.288	0.410	0.099

Problem 3	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	46	46	42	47	44	42	39	44	48
N.S.	1	1.00	0.91	1.02	0.96	0.91	0.85	0.96	1.04
time (sec)	N/A	0.024	0.024	0.224	0.253	0.349	0.180	0.404	0.171

Problem 4	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	32	23	0	0	26	0	-1
N.S.	1	1.00	1.00	0.72	0.00	0.00	0.81	0.00	-0.03
time (sec)	N/A	0.010	0.013	0.192	0.000	0.000	0.288	0.000	0.000

Problem 5	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	42	42	42	50	35	41	36	0	67
N.S.	1	1.00	1.00	1.19	0.83	0.98	0.86	0.00	1.60
time (sec)	N/A	0.025	0.028	0.196	0.293	0.360	0.213	0.000	0.145

Problem 6	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	63	69	35	55	60	0	88
N.S.	1	1.00	0.89	0.97	0.49	0.77	0.85	0.00	1.24
time (sec)	N/A	0.041	0.015	0.201	0.290	0.380	0.359	0.000	0.111

Problem 7	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	96	96	73	87	35	62	87	0	113
N.S.	1	1.00	0.76	0.91	0.36	0.65	0.91	0.00	1.18
time (sec)	N/A	0.057	0.018	0.229	0.291	0.342	0.654	0.000	0.160

Problem 8	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	109	109	72	90	52	59	99	52	52
N.S.	1	1.00	0.66	0.83	0.48	0.54	0.91	0.48	0.48
time (sec)	N/A	0.066	0.014	0.231	0.259	0.346	0.719	0.408	0.145

Problem 9	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	66	72	44	51	75	44	44
N.S.	1	1.00	0.79	0.86	0.52	0.61	0.89	0.52	0.52
time (sec)	N/A	0.047	0.013	0.210	0.265	0.347	0.376	0.409	0.126

Problem 10	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	59	59	41	54	36	43	51	36	36
N.S.	1	1.00	0.69	0.92	0.61	0.73	0.86	0.61	0.61
time (sec)	N/A	0.031	0.018	0.378	0.260	0.380	0.218	0.413	0.089

Problem 11	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	26	26	26	26	25	29	24	23	23
N.S.	1	1.00	1.00	1.00	0.96	1.12	0.92	0.88	0.88
time (sec)	N/A	0.003	0.007	0.208	0.258	0.378	0.150	0.400	0.083

Problem 12	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	26	26	26	30	24	30	24	24	24
N.S.	1	1.00	1.00	1.15	0.92	1.15	0.92	0.92	0.92
time (sec)	N/A	0.021	0.011	0.555	0.294	0.381	0.539	0.412	0.153

Problem 13	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	47	53	27	48	54	51	45
N.S.	1	1.00	0.84	0.95	0.48	0.86	0.96	0.91	0.80
time (sec)	N/A	0.034	0.035	0.273	0.287	0.357	1.048	0.413	0.183

Problem 14	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	62	71	27	60	76	68	65
N.S.	1	1.00	0.77	0.88	0.33	0.74	0.94	0.84	0.80
time (sec)	N/A	0.050	0.027	0.312	0.298	0.366	1.946	0.403	0.205

Problem 15	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	289	289	248	467	0	265	746	400	337
N.S.	1	1.00	0.86	1.62	0.00	0.92	2.58	1.38	1.17
time (sec)	N/A	0.220	0.185	0.789	0.000	0.378	2.059	0.443	1.091

Problem 16	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	192	192	138	285	0	163	398	270	204
N.S.	1	1.00	0.72	1.48	0.00	0.85	2.07	1.41	1.06
time (sec)	N/A	0.141	0.143	0.741	0.000	0.353	1.034	0.415	0.716

Problem 17	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	118	118	88	112	0	91	178	149	126
N.S.	1	1.00	0.75	0.95	0.00	0.77	1.51	1.26	1.07
time (sec)	N/A	0.085	0.065	0.426	0.000	0.366	0.540	0.412	0.450

Problem 18	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	35	32	31	47	53	59	48
N.S.	1	1.00	0.97	0.89	0.86	1.31	1.47	1.64	1.33
time (sec)	N/A	0.005	0.029	0.248	0.250	0.341	0.312	0.403	0.221

Problem 19	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	17	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.06
time (sec)	N/A	0.009	0.840	0.157	0.000	0.000	0.000	0.000	0.000

Problem 20	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	52	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.027	0.635	0.240	0.000	0.000	0.000	0.000	0.000

Problem 21	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	107	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.057	1.612	0.205	0.000	0.000	0.000	0.000	0.000

Problem 22	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	178	178	106	0	0	98	168	0	142
N.S.	1	1.00	0.60	0.00	0.00	0.55	0.94	0.00	0.80
time (sec)	N/A	0.187	0.031	0.022	0.000	0.331	0.764	0.000	0.299

Problem 23	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	126	126	90	0	0	81	117	0	101
N.S.	1	1.00	0.71	0.00	0.00	0.64	0.93	0.00	0.80
time (sec)	N/A	0.112	0.027	0.023	0.000	0.353	0.409	0.000	0.205

Problem 24	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	64	0	0	59	65	0	67
N.S.	1	1.00	0.90	0.00	0.00	0.83	0.92	0.00	0.94
time (sec)	N/A	0.058	0.030	0.021	0.000	0.347	0.252	0.000	0.167

Problem 25	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	13	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.08
time (sec)	N/A	0.012	0.021	0.020	0.000	0.000	0.000	0.000	0.000

Problem 26	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	63	0	0	65	0	0	-1
N.S.	1	1.00	0.94	0.00	0.00	0.97	0.00	0.00	-0.01
time (sec)	N/A	0.064	0.022	0.026	0.000	0.342	0.000	0.000	0.000

Problem 27	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	125	125	97	0	0	94	0	0	-1
N.S.	1	1.00	0.78	0.00	0.00	0.75	0.00	0.00	-0.01
time (sec)	N/A	0.117	0.060	0.023	0.000	0.384	0.000	0.000	0.000

Problem 28	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	177	177	133	0	0	114	0	0	-1
N.S.	1	1.00	0.75	0.00	0.00	0.64	0.00	0.00	-0.01
time (sec)	N/A	0.187	0.029	0.023	0.000	0.329	0.000	0.000	0.000

Problem 29	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	165	165	106	131	0	111	0	170	131
N.S.	1	1.00	0.64	0.79	0.00	0.67	0.00	1.03	0.79
time (sec)	N/A	0.165	0.073	0.244	0.000	0.338	0.000	0.433	0.207

Problem 30	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	113	113	88	95	0	90	0	111	90
N.S.	1	1.00	0.78	0.84	0.00	0.80	0.00	0.98	0.80
time (sec)	N/A	0.090	0.051	0.388	0.000	0.380	0.000	0.413	0.172

Problem 31	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	56	48	62	63	0	48	44
N.S.	1	1.00	1.00	0.86	1.11	1.12	0.00	0.86	0.79
time (sec)	N/A	0.036	0.022	0.251	0.475	0.355	0.000	0.432	0.159

Problem 32	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	13	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.08
time (sec)	N/A	0.011	0.026	0.026	0.000	0.000	0.000	0.000	0.000

Problem 33	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	13	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.08
time (sec)	N/A	0.011	0.026	0.023	0.000	0.000	0.000	0.000	0.000

Problem 34	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	13	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.08
time (sec)	N/A	0.011	0.026	0.023	0.000	0.000	0.000	0.000	0.000

Problem 35	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	375	375	226	0	0	281	0	0	359
N.S.	1	1.00	0.60	0.00	0.00	0.75	0.00	0.00	0.96
time (sec)	N/A	0.275	0.696	0.147	0.000	0.377	0.000	0.000	0.443

Problem 36	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	188	188	132	0	0	171	0	0	186
N.S.	1	1.00	0.70	0.00	0.00	0.91	0.00	0.00	0.99
time (sec)	N/A	0.125	0.285	0.031	0.000	0.336	0.000	0.000	0.263

Problem 37	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	66	59	0	91	0	0	79
N.S.	1	1.00	0.93	0.83	0.00	1.28	0.00	0.00	1.11
time (sec)	N/A	0.124	0.008	0.255	0.000	0.368	0.000	0.000	0.130

Problem 38	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	19	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.015	0.037	0.176	0.000	0.000	0.000	0.000	0.000

Problem 39	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	19	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.015	0.076	0.156	0.000	0.000	0.000	0.000	0.000

Problem 40	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	102	102	88	0	0	125	0	85	-1
N.S.	1	1.00	0.86	0.00	0.00	1.23	0.00	0.83	-0.01
time (sec)	N/A	0.114	0.267	0.077	0.000	0.387	0.000	0.591	0.000

Problem 41	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	94	94	84	0	0	121	0	83	-1
N.S.	1	1.00	0.89	0.00	0.00	1.29	0.00	0.88	-0.01
time (sec)	N/A	0.100	0.210	0.077	0.000	0.399	0.000	0.763	0.000

Problem 42	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	93	93	80	0	0	122	0	79	-1
N.S.	1	1.00	0.86	0.00	0.00	1.31	0.00	0.85	-0.01
time (sec)	N/A	0.087	0.193	0.046	0.000	0.399	0.000	0.512	0.000

Problem 43	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	79	62	58	119	0	67	121
N.S.	1	1.00	1.22	0.95	0.89	1.83	0.00	1.03	1.86
time (sec)	N/A	0.032	0.099	1.016	0.262	0.346	0.000	0.410	0.477

Problem 44	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	80	0	0	126	0	0	-1
N.S.	1	1.00	0.87	0.00	0.00	1.37	0.00	0.00	-0.01
time (sec)	N/A	0.109	0.195	0.118	0.000	0.357	0.000	0.000	0.000

Problem 45	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	95	77	0	0	124	0	0	-1
N.S.	1	1.00	0.81	0.00	0.00	1.31	0.00	0.00	-0.01
time (sec)	N/A	0.104	0.189	0.125	0.000	0.369	0.000	0.000	0.000

Problem 46	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	125	125	127	0	0	175	0	0	-1
N.S.	1	1.00	1.02	0.00	0.00	1.40	0.00	0.00	-0.01
time (sec)	N/A	0.151	0.370	0.046	0.000	0.374	0.000	0.000	0.000

Problem 47	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	17	16	16	19	0	16
N.S.	1	1.00	1.00	0.81	0.76	0.76	0.90	0.00	0.76
time (sec)	N/A	0.021	0.008	0.184	0.270	0.345	0.414	0.000	0.111

Problem 48	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	17	16	16	19	0	93
N.S.	1	1.00	1.00	0.81	0.76	0.76	0.90	0.00	4.43
time (sec)	N/A	0.013	0.005	0.221	0.257	0.339	0.163	0.000	0.424

Problem 49	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	20	0	15	15	17	0	15
N.S.	1	1.00	1.00	0.00	0.75	0.75	0.85	0.00	0.75
time (sec)	N/A	0.020	0.009	180.000	0.258	0.365	0.195	0.000	0.155

Problem 50	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	17	16	16	17	0	16
N.S.	1	1.00	1.00	0.81	0.76	0.76	0.81	0.00	0.76
time (sec)	N/A	0.018	0.006	0.176	0.263	0.428	0.312	0.000	0.135

Problem 51	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	17	16	16	19	0	16
N.S.	1	1.00	1.00	0.81	0.76	0.76	0.90	0.00	0.76
time (sec)	N/A	0.018	0.006	0.191	0.260	0.358	0.516	0.000	0.119

Problem 52	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	B	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	28	0	0	24	63	0	23
N.S.	1	1.00	1.00	0.00	0.00	0.86	2.25	0.00	0.82
time (sec)	N/A	0.025	0.009	0.037	0.000	0.418	1.726	0.000	0.164

Problem 53	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	285	285	138	312	0	260	0	270	244
N.S.	1	1.00	0.48	1.09	0.00	0.91	0.00	0.95	0.86
time (sec)	N/A	0.293	0.322	0.427	0.000	0.365	0.000	0.425	0.771

Problem 54	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	155	155	99	168	0	149	0	141	131
N.S.	1	1.00	0.64	1.08	0.00	0.96	0.00	0.91	0.85
time (sec)	N/A	0.107	0.212	0.501	0.000	0.369	0.000	0.421	0.526

Problem 55	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	51	67	47	62	0	48	47
N.S.	1	1.00	0.89	1.18	0.82	1.09	0.00	0.84	0.82
time (sec)	N/A	0.026	0.028	0.441	0.262	0.383	0.000	0.399	0.198

Problem 56	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	20	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.025	0.106	0.072	0.000	0.000	0.000	0.000	0.000

Problem 57	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	101	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.100	0.144	0.228	0.000	0.000	0.000	0.000	0.000

Problem 58	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	231	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.224	0.181	0.180	0.000	0.000	0.000	0.000	0.000

Problem 59	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	186	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.163	0.206	0.066	0.000	0.000	0.000	0.000	0.000

Problem 60	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	84	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.063	0.156	0.131	0.000	0.000	0.000	0.000	0.000

Problem 61	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	17	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.06
time (sec)	N/A	0.010	0.021	0.065	0.000	0.000	0.000	0.000	0.000

Problem 62	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	62	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.076	0.147	0.073	0.000	0.000	0.000	0.000	0.000

Problem 63	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	155	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.188	0.225	0.180	0.000	0.000	0.000	0.000	0.000

Problem 64	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	118	118	73	88	82	74	119	118	91
N.S.	1	1.00	0.62	0.75	0.69	0.63	1.01	1.00	0.77
time (sec)	N/A	0.089	0.035	0.314	0.259	0.352	44.082	0.398	0.297

Problem 65	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	79	79	57	66	59	55	76	71	65
N.S.	1	1.00	0.72	0.84	0.75	0.70	0.96	0.90	0.82
time (sec)	N/A	0.053	0.025	0.533	0.259	0.404	8.599	0.414	0.204

Problem 66	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	37	37	34	51	34	35	34	31	31
N.S.	1	1.00	0.92	1.38	0.92	0.95	0.92	0.84	0.84
time (sec)	N/A	0.022	0.016	0.095	0.265	0.335	1.540	0.428	0.097

Problem 67	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	32	0	0	0	26	0	-1
N.S.	1	1.00	1.00	0.00	0.00	0.00	0.81	0.00	-0.03
time (sec)	N/A	0.029	0.061	0.071	0.000	0.000	5.964	0.000	0.000

Problem 68	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	34	0	0	0	29	0	-1
N.S.	1	1.00	0.48	0.00	0.00	0.00	0.41	0.00	-0.01
time (sec)	N/A	0.058	0.092	0.157	0.000	0.000	28.610	0.000	0.000

Problem 69	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	115	115	36	0	0	0	0	0	-1
N.S.	1	1.00	0.31	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.092	0.099	0.166	0.000	0.000	0.000	0.000	0.000

Problem 70	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	119	119	100	0	0	0	0	0	-1
N.S.	1	1.00	0.84	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.079	0.210	0.072	0.000	0.000	0.000	0.000	0.000

Problem 71	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	76	76	80	0	0	0	24	0	-1
N.S.	1	1.00	1.05	0.00	0.00	0.00	0.32	0.00	-0.01
time (sec)	N/A	0.045	0.149	0.124	0.000	0.000	31.764	0.000	0.000

Problem 72	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	F	F	F	F	A	F	F
verified	N/A	Yes	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	29	29	0	0	0	0	22	0	-1
N.S.	1	1.00	0.00	0.00	0.00	0.00	0.76	0.00	-0.03
time (sec)	N/A	0.013	0.016	0.071	0.000	0.000	4.417	0.000	0.000

Problem 73	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	74	0	0	0	46	0	-1
N.S.	1	1.00	1.12	0.00	0.00	0.00	0.70	0.00	-0.02
time (sec)	N/A	0.044	0.138	0.072	0.000	0.000	11.331	0.000	0.000

Problem 74	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	115	115	100	0	0	0	24	0	-1
N.S.	1	1.00	0.87	0.00	0.00	0.00	0.21	0.00	-0.01
time (sec)	N/A	0.078	0.242	0.169	0.000	0.000	83.056	0.000	0.000

Problem 75	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	135	135	86	119	0	97	0	153	192
N.S.	1	1.00	0.64	0.88	0.00	0.72	0.00	1.13	1.42
time (sec)	N/A	0.139	0.055	0.329	0.000	0.335	0.000	0.410	0.453

Problem 76	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	90	90	68	83	0	76	0	94	106
N.S.	1	1.00	0.76	0.92	0.00	0.84	0.00	1.04	1.18
time (sec)	N/A	0.079	0.034	0.585	0.000	0.357	0.000	0.422	0.451

Problem 77	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	39	39	34	43	0	35	43
N.S.	1	1.00	0.91	0.91	0.79	1.00	0.00	0.81	1.00
time (sec)	N/A	0.024	0.013	0.322	0.459	0.381	0.000	0.401	0.177

Problem 78	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	21	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.022	0.061	0.042	0.000	0.000	0.000	0.000	0.000

Problem 79	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	88	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.063	0.099	0.144	0.000	0.000	0.000	0.000	0.000

Problem 80	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	161	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.130	0.116	0.158	0.000	0.000	0.000	0.000	0.000

Problem 81	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	112	112	85	0	0	74	109	0	90
N.S.	1	1.00	0.76	0.00	0.00	0.66	0.97	0.00	0.80
time (sec)	N/A	0.095	0.023	0.119	0.000	0.381	6.299	0.000	0.749

Problem 82	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	56	0	0	52	60	0	80
N.S.	1	1.00	0.89	0.00	0.00	0.83	0.95	0.00	1.27
time (sec)	N/A	0.046	0.030	0.111	0.000	0.354	1.222	0.000	0.302

Problem 83	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	18	15	14	14	15	0	41
N.S.	1	1.00	1.00	0.83	0.78	0.78	0.83	0.00	2.28
time (sec)	N/A	0.012	0.007	0.224	0.250	0.350	0.325	0.000	0.197

Problem 84	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	52	52	52	0	0	53	0	0	-1
N.S.	1	1.00	1.00	0.00	0.00	1.02	0.00	0.00	-0.02
time (sec)	N/A	0.051	0.013	0.128	0.000	0.349	0.000	0.000	0.000

Problem 85	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	108	108	85	0	0	84	0	0	-1
N.S.	1	1.00	0.79	0.00	0.00	0.78	0.00	0.00	-0.01
time (sec)	N/A	0.105	0.048	0.150	0.000	0.357	0.000	0.000	0.000

Problem 86	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F(-1)	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	342	342	240	0	0	267	0	288	386
N.S.	1	1.00	0.70	0.00	0.00	0.78	0.00	0.84	1.13
time (sec)	N/A	0.360	3.190	0.181	0.000	0.392	0.000	0.439	1.162

Problem 87	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	86	86	82	134	84	100	0	87	89
N.S.	1	1.00	0.95	1.56	0.98	1.16	0.00	1.01	1.03
time (sec)	N/A	0.038	0.074	0.643	0.262	0.395	0.000	0.411	0.181

Problem 88	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	22	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.025	0.147	0.062	0.000	0.000	0.000	0.000	0.000

Problem 89	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	185	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.277	0.272	0.192	0.000	0.000	0.000	0.000	0.000

Problem 90	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	F(-1)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	527	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.657	0.353	0.080	0.000	0.000	0.000	0.000	0.000

Problem 91	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	164	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.130	0.283	0.145	0.000	0.000	0.000	0.000	0.000

Problem 92	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	19	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.011	0.029	0.069	0.000	0.000	0.000	0.000	0.000

Problem 93	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	83	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.148	0.285	0.083	0.000	0.000	0.000	0.000	0.000

Problem 94	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	355	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.607	0.385	0.194	0.000	0.000	0.000	0.000	0.000

Problem 95	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	62	62	62	67	0	66	0	0	52
N.S.	1	1.00	1.00	1.08	0.00	1.06	0.00	0.00	0.84
time (sec)	N/A	0.102	0.070	0.701	0.000	0.350	0.000	0.000	0.217

Problem 96	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	69	0	0	0	0	0	-1
N.S.	1	1.00	1.05	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.043	0.056	0.080	0.000	0.000	0.000	0.000	0.000

Problem 97	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	67	0	0	0	0	0	-1
N.S.	1	1.00	1.02	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.041	0.047	0.072	0.000	0.000	0.000	0.000	0.000

Problem 98	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	F	F	F	F	F	F	F
verified	N/A	Yes	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	62	62	0	0	0	0	0	0	-1
N.S.	1	1.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.037	0.434	0.261	0.000	0.000	0.000	0.000	0.000

Problem 99	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	F	F	F	F	F	F	F
verified	N/A	Yes	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	62	62	0	0	0	0	0	0	-1
N.S.	1	1.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.038	0.444	0.226	0.000	0.000	0.000	0.000	0.000

Problem 100	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	57	0	0	0	0	0	-1
N.S.	1	1.00	1.02	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.038	0.031	0.061	0.000	0.000	0.000	0.000	0.000

Problem 101	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	61	0	0	0	0	0	-1
N.S.	1	1.00	1.09	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.036	0.029	0.059	0.000	0.000	0.000	0.000	0.000

Problem 102	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	93	0	0	0	0	0	-1
N.S.	1	1.00	1.66	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.034	0.184	0.232	0.000	0.000	0.000	0.000	0.000

Problem 103	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	91	0	0	0	0	0	-1
N.S.	1	1.00	1.62	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.036	0.080	0.236	0.000	0.000	0.000	0.000	0.000

Problem 104	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	96	96	62	83	63	71	92	69	78
N.S.	1	1.00	0.65	0.86	0.66	0.74	0.96	0.72	0.81
time (sec)	N/A	0.062	0.043	0.104	0.257	0.343	0.519	0.421	0.267

Problem 105	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	54	65	55	63	68	61	58
N.S.	1	1.00	0.76	0.92	0.77	0.89	0.96	0.86	0.82
time (sec)	N/A	0.042	0.040	0.085	0.265	0.353	0.292	0.414	0.145

Problem 106	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	46	46	43	46	44	50	42	49	38
N.S.	1	1.00	0.93	1.00	0.96	1.09	0.91	1.07	0.83
time (sec)	N/A	0.024	0.030	0.087	0.252	0.363	0.182	0.429	0.116

Problem 107	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	45	0	0	0	36	0	-1
N.S.	1	1.00	1.29	0.00	0.00	0.00	1.03	0.00	-0.03
time (sec)	N/A	0.017	0.019	0.024	0.000	0.000	0.365	0.000	0.000

Problem 108	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	40	40	40	51	35	43	34	0	38
N.S.	1	1.00	1.00	1.28	0.88	1.08	0.85	0.00	0.95
time (sec)	N/A	0.025	0.039	0.085	0.301	0.353	0.224	0.000	0.130

Problem 109	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	53	69	35	58	60	0	71
N.S.	1	1.00	0.75	0.97	0.49	0.82	0.85	0.00	1.00
time (sec)	N/A	0.041	0.027	0.091	0.305	0.354	0.363	0.000	0.191

Problem 110	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	96	96	62	87	35	66	87	0	-1
N.S.	1	1.00	0.65	0.91	0.36	0.69	0.91	0.00	-0.01
time (sec)	N/A	0.058	0.035	0.089	0.302	0.366	0.665	0.000	0.000

Problem 111	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	109	109	73	90	52	68	102	57	90
N.S.	1	1.00	0.67	0.83	0.48	0.62	0.94	0.52	0.83
time (sec)	N/A	0.064	0.015	0.083	0.267	0.352	0.733	0.411	0.286

Problem 112	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	84	84	66	72	44	60	78	49	70
N.S.	1	1.00	0.79	0.86	0.52	0.71	0.93	0.58	0.83
time (sec)	N/A	0.047	0.014	0.100	0.252	0.363	0.388	0.417	0.230

Problem 113	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	59	59	42	54	36	52	54	41	50
N.S.	1	1.00	0.71	0.92	0.61	0.88	0.92	0.69	0.85
time (sec)	N/A	0.035	0.020	0.313	0.264	0.375	0.226	0.433	0.147

Problem 114	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	27	27	27	27	26	35	24	26	24
N.S.	1	1.00	1.00	1.00	0.96	1.30	0.89	0.96	0.89
time (sec)	N/A	0.004	0.003	0.178	0.253	0.353	0.151	0.397	0.104

Problem 115	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	27	27	27	29	25	32	20	0	25
N.S.	1	1.00	1.00	1.07	0.93	1.19	0.74	0.00	0.93
time (sec)	N/A	0.020	0.013	0.459	0.289	0.346	0.652	0.000	0.154

Problem 116	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	49	53	27	51	48	0	46
N.S.	1	1.00	0.88	0.95	0.48	0.91	0.86	0.00	0.82
time (sec)	N/A	0.034	0.029	0.210	0.290	0.349	1.151	0.000	0.182

Problem 117	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	73	71	27	62	70	0	66
N.S.	1	1.00	0.90	0.88	0.33	0.77	0.86	0.00	0.81
time (sec)	N/A	0.050	0.018	0.201	0.302	0.384	2.026	0.000	0.188

Problem 118	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	292	292	268	729	0	314	746	435	352
N.S.	1	1.00	0.92	2.50	0.00	1.08	2.55	1.49	1.21
time (sec)	N/A	0.201	0.239	0.436	0.000	0.366	2.340	0.548	0.391

Problem 119	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F	A	B	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	194	194	159	429	0	197	398	280	220
N.S.	1	1.00	0.82	2.21	0.00	1.02	2.05	1.44	1.13
time (sec)	N/A	0.131	0.193	0.408	0.000	0.336	1.152	0.514	0.306

Problem 120	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	119	119	104	124	0	110	178	158	119
N.S.	1	1.00	0.87	1.04	0.00	0.92	1.50	1.33	1.00
time (sec)	N/A	0.082	0.083	0.265	0.000	0.336	0.560	0.480	0.222

Problem 121	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	37	37	42	33	32	53	53	60	49
N.S.	1	1.00	1.14	0.89	0.86	1.43	1.43	1.62	1.32
time (sec)	N/A	0.006	0.029	0.184	0.258	0.328	0.303	0.415	0.114

Problem 122	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	17	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.06
time (sec)	N/A	0.011	0.088	0.169	0.000	0.000	0.000	0.000	0.000

Problem 123	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	52	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.028	0.340	0.216	0.000	0.000	0.000	0.000	0.000

Problem 124	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	105	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.054	0.652	0.221	0.000	0.000	0.000	0.000	0.000

Problem 125	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	178	178	173	0	0	149	172	0	143
N.S.	1	1.00	0.97	0.00	0.00	0.84	0.97	0.00	0.80
time (sec)	N/A	0.186	0.270	0.023	0.000	0.377	0.784	0.000	0.324

Problem 126	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	126	126	149	0	0	124	121	0	102
N.S.	1	1.00	1.18	0.00	0.00	0.98	0.96	0.00	0.81
time (sec)	N/A	0.118	0.262	0.021	0.000	0.376	0.422	0.000	0.239

Problem 127	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	72	72	99	0	0	91	68	0	68
N.S.	1	1.00	1.38	0.00	0.00	1.26	0.94	0.00	0.94
time (sec)	N/A	0.058	0.097	0.023	0.000	0.343	0.256	0.000	0.197

Problem 128	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	13	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.08
time (sec)	N/A	0.012	0.096	0.023	0.000	0.000	0.000	0.000	0.000

Problem 129	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	63	0	0	98	0	0	-1
N.S.	1	1.00	0.94	0.00	0.00	1.46	0.00	0.00	-0.01
time (sec)	N/A	0.064	0.025	0.022	0.000	0.356	0.000	0.000	0.000

Problem 130	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	125	125	97	0	0	141	0	0	-1
N.S.	1	1.00	0.78	0.00	0.00	1.13	0.00	0.00	-0.01
time (sec)	N/A	0.123	0.061	0.023	0.000	0.357	0.000	0.000	0.000

Problem 131	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	177	177	133	0	0	168	0	0	-1
N.S.	1	1.00	0.75	0.00	0.00	0.95	0.00	0.00	-0.01
time (sec)	N/A	0.206	0.034	0.026	0.000	0.359	0.000	0.000	0.000

Problem 132	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	165	165	108	205	0	154	0	218	-1
N.S.	1	1.00	0.65	1.24	0.00	0.93	0.00	1.32	-0.01
time (sec)	N/A	0.163	0.109	0.192	0.000	0.365	0.000	0.466	0.000

Problem 133	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	113	113	88	151	0	123	0	151	-1
N.S.	1	1.00	0.78	1.34	0.00	1.09	0.00	1.34	-0.01
time (sec)	N/A	0.094	0.065	0.331	0.000	0.352	0.000	0.463	0.000

Problem 134	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	56	56	56	48	0	85	0	73	-1
N.S.	1	1.00	1.00	0.86	0.00	1.52	0.00	1.30	-0.02
time (sec)	N/A	0.034	0.032	0.187	0.000	0.330	0.000	0.442	0.000

Problem 135	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	13	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.08
time (sec)	N/A	0.012	0.096	0.020	0.000	0.000	0.000	0.000	0.000

Problem 136	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	13	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.08
time (sec)	N/A	0.012	0.104	0.023	0.000	0.000	0.000	0.000	0.000

Problem 137	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	13	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.08
time (sec)	N/A	0.012	0.108	0.028	0.000	0.000	0.000	0.000	0.000

Problem 138	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	375	375	610	0	0	472	0	0	-1
N.S.	1	1.00	1.63	0.00	0.00	1.26	0.00	0.00	-0.00
time (sec)	N/A	0.268	3.197	0.138	0.000	0.353	0.000	0.000	0.000

Problem 139	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	189	189	301	0	0	273	0	0	-1
N.S.	1	1.00	1.59	0.00	0.00	1.44	0.00	0.00	-0.01
time (sec)	N/A	0.118	1.414	0.033	0.000	0.339	0.000	0.000	0.000

Problem 140	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	B	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	66	59	0	141	0	0	-1
N.S.	1	1.00	0.93	0.83	0.00	1.99	0.00	0.00	-0.01
time (sec)	N/A	0.112	0.067	0.254	0.000	0.343	0.000	0.000	0.000

Problem 141	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	19	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.016	0.412	0.149	0.000	0.000	0.000	0.000	0.000

Problem 142	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	19	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.015	0.248	0.183	0.000	0.000	0.000	0.000	0.000

Problem 143	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	102	102	87	0	0	130	0	90	-1
N.S.	1	1.00	0.85	0.00	0.00	1.27	0.00	0.88	-0.01
time (sec)	N/A	0.102	0.250	0.076	0.000	0.345	0.000	0.482	0.000

Problem 144	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	94	94	80	0	0	126	0	88	-1
N.S.	1	1.00	0.85	0.00	0.00	1.34	0.00	0.94	-0.01
time (sec)	N/A	0.087	0.220	0.073	0.000	0.357	0.000	0.518	0.000

Problem 145	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	92	92	77	0	0	123	0	82	-1
N.S.	1	1.00	0.84	0.00	0.00	1.34	0.00	0.89	-0.01
time (sec)	N/A	0.078	0.196	0.095	0.000	0.381	0.000	0.478	0.000

Problem 146	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	B	F	A	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	93	63	59	128	0	83	100
N.S.	1	1.00	1.41	0.95	0.89	1.94	0.00	1.26	1.52
time (sec)	N/A	0.031	0.103	0.944	0.253	0.347	0.000	0.401	0.447

Problem 147	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	93	93	81	0	0	128	0	0	-1
N.S.	1	1.00	0.87	0.00	0.00	1.38	0.00	0.00	-0.01
time (sec)	N/A	0.100	0.211	0.121	0.000	0.407	0.000	0.000	0.000

Problem 148	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	95	79	0	0	125	0	0	-1
N.S.	1	1.00	0.83	0.00	0.00	1.32	0.00	0.00	-0.01
time (sec)	N/A	0.097	0.211	0.120	0.000	0.366	0.000	0.000	0.000

Problem 149	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	126	126	126	0	0	186	0	0	-1
N.S.	1	1.00	1.00	0.00	0.00	1.48	0.00	0.00	-0.01
time (sec)	N/A	0.131	0.371	0.056	0.000	0.372	0.000	0.000	0.000

Problem 150	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	43	0	31	24	0	16
N.S.	1	1.00	1.00	2.05	0.00	1.48	1.14	0.00	0.76
time (sec)	N/A	0.020	0.009	0.349	0.000	0.365	0.417	0.000	0.153

Problem 151	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	30	0	23	24	0	16
N.S.	1	1.00	1.00	1.43	0.00	1.10	1.14	0.00	0.76
time (sec)	N/A	0.013	0.006	0.262	0.000	0.346	0.161	0.000	0.148

Problem 152	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	20	0	0	17	24	0	15
N.S.	1	1.00	1.00	0.00	0.00	0.85	1.20	0.00	0.75
time (sec)	N/A	0.019	0.010	0.046	0.000	0.372	0.245	0.000	0.183

Problem 153	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	0	0	19	20	0	16
N.S.	1	1.00	1.00	0.00	0.00	0.90	0.95	0.00	0.76
time (sec)	N/A	0.019	0.007	0.076	0.000	0.389	0.433	0.000	0.164

Problem 154	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	0	0	26	22	0	16
N.S.	1	1.00	1.00	0.00	0.00	1.24	1.05	0.00	0.76
time (sec)	N/A	0.019	0.007	0.207	0.000	0.374	0.745	0.000	0.092

Problem 155	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	B	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	28	0	0	30	60	0	23
N.S.	1	1.00	1.00	0.00	0.00	1.07	2.14	0.00	0.82
time (sec)	N/A	0.023	0.010	0.068	0.000	0.360	1.743	0.000	0.201

Problem 156	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	283	283	184	376	0	356	0	0	-1
N.S.	1	1.00	0.65	1.33	0.00	1.26	0.00	0.00	-0.00
time (sec)	N/A	0.247	0.918	0.420	0.000	0.374	0.000	0.000	0.000

Problem 157	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	155	155	99	206	0	190	0	0	-1
N.S.	1	1.00	0.64	1.33	0.00	1.23	0.00	0.00	-0.01
time (sec)	N/A	0.102	0.233	0.502	0.000	0.343	0.000	0.000	0.000

Problem 158	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	50	92	0	70	0	0	-1
N.S.	1	1.00	0.88	1.61	0.00	1.23	0.00	0.00	-0.02
time (sec)	N/A	0.026	0.027	0.442	0.000	0.356	0.000	0.000	0.000

Problem 159	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	20	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.025	0.358	0.090	0.000	0.000	0.000	0.000	0.000

Problem 160	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	99	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.094	0.450	0.242	0.000	0.000	0.000	0.000	0.000

Problem 161	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	231	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.213	0.529	0.227	0.000	0.000	0.000	0.000	0.000

Problem 162	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	186	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.157	0.576	0.068	0.000	0.000	0.000	0.000	0.000

Problem 163	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	84	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.060	0.448	0.135	0.000	0.000	0.000	0.000	0.000

Problem 164	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	17	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.06
time (sec)	N/A	0.010	0.022	0.065	0.000	0.000	0.000	0.000	0.000

Problem 165	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	63	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.074	0.470	0.075	0.000	0.000	0.000	0.000	0.000

Problem 166	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	155	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.171	0.588	0.164	0.000	0.000	0.000	0.000	0.000

Problem 167	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	118	118	73	135	0	97	126	0	94
N.S.	1	1.00	0.62	1.14	0.00	0.82	1.07	0.00	0.80
time (sec)	N/A	0.082	0.034	0.264	0.000	0.366	45.395	0.000	0.311

Problem 168	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	80	80	58	99	0	68	83	0	63
N.S.	1	1.00	0.72	1.24	0.00	0.85	1.04	0.00	0.79
time (sec)	N/A	0.051	0.025	0.467	0.000	0.352	8.787	0.000	0.163

Problem 169	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	36	36	36	51	0	38	41	0	30
N.S.	1	1.00	1.00	1.42	0.00	1.06	1.14	0.00	0.83
time (sec)	N/A	0.021	0.016	0.089	0.000	0.390	1.610	0.000	0.175

Problem 170	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	48	48	45	0	0	0	39	0	-1
N.S.	1	1.00	0.94	0.00	0.00	0.00	0.81	0.00	-0.02
time (sec)	N/A	0.067	0.094	0.083	0.000	0.000	6.165	0.000	0.000

Problem 171	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	88	88	65	0	0	0	61	0	-1
N.S.	1	1.00	0.74	0.00	0.00	0.00	0.69	0.00	-0.01
time (sec)	N/A	0.100	0.148	0.207	0.000	0.000	33.786	0.000	0.000

Problem 172	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	134	134	83	0	0	0	0	0	-1
N.S.	1	1.00	0.62	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.128	0.155	0.217	0.000	0.000	0.000	0.000	0.000

Problem 173	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	138	138	147	0	0	0	0	0	-1
N.S.	1	1.00	1.07	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.090	0.260	0.068	0.000	0.000	0.000	0.000	0.000

Problem 174	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	95	104	0	0	0	65	0	-1
N.S.	1	1.00	1.09	0.00	0.00	0.00	0.68	0.00	-0.01
time (sec)	N/A	0.057	0.218	0.118	0.000	0.000	32.904	0.000	0.000

Problem 175	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	F	F	F	F	C	F	F
verified	N/A	Yes	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	50	50	0	0	0	0	44	0	-1
N.S.	1	1.00	0.00	0.00	0.00	0.00	0.88	0.00	-0.02
time (sec)	N/A	0.027	0.058	0.072	0.000	0.000	4.610	0.000	0.000

Problem 176	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	80	80	99	0	0	0	80	0	-1
N.S.	1	1.00	1.24	0.00	0.00	0.00	1.00	0.00	-0.01
time (sec)	N/A	0.056	0.186	0.069	0.000	0.000	11.386	0.000	0.000

Problem 177	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	134	134	151	0	0	0	22	0	-1
N.S.	1	1.00	1.13	0.00	0.00	0.00	0.16	0.00	-0.01
time (sec)	N/A	0.088	0.307	0.136	0.000	0.000	90.787	0.000	0.000

Problem 178	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	135	135	87	172	0	121	0	0	-1
N.S.	1	1.00	0.64	1.27	0.00	0.90	0.00	0.00	-0.01
time (sec)	N/A	0.132	0.095	0.253	0.000	0.351	0.000	0.000	0.000

Problem 179	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	90	90	69	118	0	90	0	0	-1
N.S.	1	1.00	0.77	1.31	0.00	1.00	0.00	0.00	-0.01
time (sec)	N/A	0.073	0.068	0.579	0.000	0.342	0.000	0.000	0.000

Problem 180	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	43	43	39	53	0	47	0	0	-1
N.S.	1	1.00	0.91	1.23	0.00	1.09	0.00	0.00	-0.02
time (sec)	N/A	0.024	0.019	0.352	0.000	0.361	0.000	0.000	0.000

Problem 181	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	21	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.023	0.147	0.076	0.000	0.000	0.000	0.000	0.000

Problem 182	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	86	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.065	0.207	0.224	0.000	0.000	0.000	0.000	0.000

Problem 183	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	162	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.127	0.196	0.217	0.000	0.000	0.000	0.000	0.000

Problem 184	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	112	112	112	0	0	97	112	0	90
N.S.	1	1.00	1.00	0.00	0.00	0.87	1.00	0.00	0.80
time (sec)	N/A	0.094	0.096	0.129	0.000	0.349	7.532	0.000	0.202

Problem 185	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	79	0	0	66	63	0	49
N.S.	1	1.00	1.25	0.00	0.00	1.05	1.00	0.00	0.78
time (sec)	N/A	0.044	0.085	0.124	0.000	0.355	1.361	0.000	0.191

Problem 186	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	18	18	18	22	14	21	17	0	14
N.S.	1	1.00	1.00	1.22	0.78	1.17	0.94	0.00	0.78
time (sec)	N/A	0.011	0.005	0.138	0.258	0.351	0.343	0.000	0.072

Problem 187	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	53	0	0	77	0	0	-1
N.S.	1	1.00	1.00	0.00	0.00	1.45	0.00	0.00	-0.02
time (sec)	N/A	0.046	0.012	0.141	0.000	0.353	0.000	0.000	0.000

Problem 188	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	108	108	85	0	0	122	0	0	-1
N.S.	1	1.00	0.79	0.00	0.00	1.13	0.00	0.00	-0.01
time (sec)	N/A	0.104	0.049	0.184	0.000	0.373	0.000	0.000	0.000

Problem 189	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	342	342	256	0	0	328	0	0	-1
N.S.	1	1.00	0.75	0.00	0.00	0.96	0.00	0.00	-0.00
time (sec)	N/A	0.314	3.379	0.181	0.000	0.362	0.000	0.000	0.000

Problem 190	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	86	86	81	175	0	108	0	0	-1
N.S.	1	1.00	0.94	2.03	0.00	1.26	0.00	0.00	-0.01
time (sec)	N/A	0.038	0.087	0.655	0.000	0.377	0.000	0.000	0.000

Problem 191	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	22	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.026	0.505	0.085	0.000	0.000	0.000	0.000	0.000

Problem 192	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	183	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.266	0.655	0.237	0.000	0.000	0.000	0.000	0.000

Problem 193	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	F(-1)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	527	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.631	0.785	0.076	0.000	0.000	0.000	0.000	0.000

Problem 194	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	164	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.121	0.597	0.146	0.000	0.000	0.000	0.000	0.000

Problem 195	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	19	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.010	0.031	0.087	0.000	0.000	0.000	0.000	0.000

Problem 196	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	83	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.141	0.682	0.092	0.000	0.000	0.000	0.000	0.000

Problem 197	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	355	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.595	0.797	0.203	0.000	0.000	0.000	0.000	0.000

Problem 198	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	60	60	60	84	0	71	0	0	-1
N.S.	1	1.00	1.00	1.40	0.00	1.18	0.00	0.00	-0.02
time (sec)	N/A	0.098	0.050	0.806	0.000	0.367	0.000	0.000	0.000

Problem 199	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	91	91	94	0	0	0	0	0	-1
N.S.	1	1.00	1.03	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.055	0.292	0.128	0.000	0.000	0.000	0.000	0.000

Problem 200	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	91	91	101	0	0	0	0	0	-1
N.S.	1	1.00	1.11	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.052	0.292	0.122	0.000	0.000	0.000	0.000	0.000

Problem 201	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	F	F	F	F	F	F	F
verified	N/A	Yes	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	85	85	0	0	0	0	0	0	-1
N.S.	1	1.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.053	1.129	0.408	0.000	0.000	0.000	0.000	0.000

Problem 202	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	F	F	F	F	F	F	F
verified	N/A	Yes	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	85	85	0	0	0	0	0	0	-1
N.S.	1	1.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.054	1.265	0.406	0.000	0.000	0.000	0.000	0.000

Problem 203	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	75	75	83	0	0	0	0	0	-1
N.S.	1	1.00	1.11	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.048	0.112	0.138	0.000	0.000	0.000	0.000	0.000

Problem 204	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	77	77	84	0	0	0	0	0	-1
N.S.	1	1.00	1.09	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.050	0.107	0.122	0.000	0.000	0.000	0.000	0.000

Problem 205	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	75	75	114	0	0	0	0	0	-1
N.S.	1	1.00	1.52	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.049	0.093	0.464	0.000	0.000	0.000	0.000	0.000

Problem 206	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	77	77	117	0	0	0	0	0	-1
N.S.	1	1.00	1.52	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.049	0.083	0.434	0.000	0.000	0.000	0.000	0.000

Problem 207	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	93	93	64	77	63	62	88	0	108
N.S.	1	1.00	0.69	0.83	0.68	0.67	0.95	0.00	1.16
time (sec)	N/A	0.055	0.022	0.108	0.265	0.357	0.423	0.000	0.122

Problem 208	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	51	61	55	53	65	0	89
N.S.	1	1.00	0.74	0.88	0.80	0.77	0.94	0.00	1.29
time (sec)	N/A	0.038	0.023	0.105	0.265	0.382	0.188	0.000	0.088

Problem 209	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	C	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	45	45	39	45	44	41	39	0	43
N.S.	1	1.00	0.87	1.00	0.98	0.91	0.87	0.00	0.96
time (sec)	N/A	0.022	0.020	0.100	0.269	0.350	0.081	0.000	0.188

Problem 210	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	31	31	31	22	0	0	24	0	-1
N.S.	1	1.00	1.00	0.71	0.00	0.00	0.77	0.00	-0.03
time (sec)	N/A	0.009	0.011	0.071	0.000	0.000	0.293	0.000	0.000

Problem 211	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	40	40	37	47	39	40	34	0	69
N.S.	1	1.00	0.92	1.18	0.98	1.00	0.85	0.00	1.72
time (sec)	N/A	0.024	0.017	0.131	0.286	0.409	0.191	0.000	0.115

Problem 212	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	51	65	39	52	60	0	89
N.S.	1	1.00	0.74	0.94	0.57	0.75	0.87	0.00	1.29
time (sec)	N/A	0.041	0.019	0.134	0.293	0.364	0.337	0.000	0.080

Problem 213	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	93	93	64	81	39	61	87	0	108
N.S.	1	1.00	0.69	0.87	0.42	0.66	0.94	0.00	1.16
time (sec)	N/A	0.053	0.018	0.100	0.302	0.343	0.661	0.000	0.121

Problem 214	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	105	105	57	82	51	59	99	0	51
N.S.	1	1.00	0.54	0.78	0.49	0.56	0.94	0.00	0.49
time (sec)	N/A	0.062	0.027	0.119	0.255	0.378	0.643	0.000	0.134

Problem 215	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	81	81	49	64	43	51	75	0	43
N.S.	1	1.00	0.60	0.79	0.53	0.63	0.93	0.00	0.53
time (sec)	N/A	0.045	0.021	0.104	0.254	0.383	0.270	0.000	0.105

Problem 216	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	41	50	35	43	49	0	35
N.S.	1	1.00	0.72	0.88	0.61	0.75	0.86	0.00	0.61
time (sec)	N/A	0.032	0.020	0.365	0.265	0.365	0.116	0.000	0.153

Problem 217	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	26	26	26	26	25	29	22	0	23
N.S.	1	1.00	1.00	1.00	0.96	1.12	0.85	0.00	0.88
time (sec)	N/A	0.004	0.006	0.214	0.268	0.360	0.059	0.000	0.052

Problem 218	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	25	25	25	31	23	29	32	0	23
N.S.	1	1.00	1.00	1.24	0.92	1.16	1.28	0.00	0.92
time (sec)	N/A	0.021	0.011	0.618	0.299	0.361	0.555	0.000	0.181

Problem 219	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	54	54	50	52	28	48	63	0	43
N.S.	1	1.00	0.93	0.96	0.52	0.89	1.17	0.00	0.80
time (sec)	N/A	0.035	0.017	0.302	0.303	0.358	1.201	0.000	0.219

Problem 220	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	C	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	78	78	61	68	28	58	85	0	62
N.S.	1	1.00	0.78	0.87	0.36	0.74	1.09	0.00	0.79
time (sec)	N/A	0.048	0.022	0.339	0.356	0.351	1.973	0.000	0.220

Problem 221	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F	A	B	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	279	279	237	703	0	263	746	0	357
N.S.	1	1.00	0.85	2.52	0.00	0.94	2.67	0.00	1.28
time (sec)	N/A	0.189	0.175	0.774	0.000	0.387	2.089	0.000	0.644

Problem 222	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	B	F	A	B	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	186	186	142	415	0	161	398	0	190
N.S.	1	1.00	0.76	2.23	0.00	0.87	2.14	0.00	1.02
time (sec)	N/A	0.119	0.114	0.863	0.000	0.371	0.905	0.000	0.365

Problem 223	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	115	115	78	117	0	89	178	0	106
N.S.	1	1.00	0.68	1.02	0.00	0.77	1.55	0.00	0.92
time (sec)	N/A	0.075	0.057	0.354	0.000	0.370	0.378	0.000	0.331

Problem 224	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	35	35	33	31	30	45	51	0	46
N.S.	1	1.00	0.94	0.89	0.86	1.29	1.46	0.00	1.31
time (sec)	N/A	0.004	0.020	0.229	0.258	0.374	0.137	0.000	0.136

Problem 225	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	17	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.06
time (sec)	N/A	0.010	0.756	0.153	0.000	0.000	0.000	0.000	0.000

Problem 226	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	50	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.025	0.564	0.164	0.000	0.000	0.000	0.000	0.000

Problem 227	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	102	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.052	0.596	0.191	0.000	0.000	0.000	0.000	0.000

Problem 228	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	175	175	99	0	0	97	168	0	139
N.S.	1	1.00	0.57	0.00	0.00	0.55	0.96	0.00	0.79
time (sec)	N/A	0.174	0.029	0.018	0.000	0.340	0.642	0.000	0.303

Problem 229	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	124	124	82	0	0	79	116	0	100
N.S.	1	1.00	0.66	0.00	0.00	0.64	0.94	0.00	0.81
time (sec)	N/A	0.109	0.024	0.024	0.000	0.430	0.287	0.000	0.219

Problem 230	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	63	0	0	58	63	0	66
N.S.	1	1.00	0.89	0.00	0.00	0.82	0.89	0.00	0.93
time (sec)	N/A	0.051	0.013	0.023	0.000	0.344	0.121	0.000	0.184

Problem 231	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	13	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.08
time (sec)	N/A	0.011	0.020	0.017	0.000	0.000	0.000	0.000	0.000

Problem 232	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	60	0	0	64	0	0	-1
N.S.	1	1.00	0.92	0.00	0.00	0.98	0.00	0.00	-0.02
time (sec)	N/A	0.058	0.018	0.019	0.000	0.356	0.000	0.000	0.000

Problem 233	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	123	123	97	0	0	93	0	0	-1
N.S.	1	1.00	0.79	0.00	0.00	0.76	0.00	0.00	-0.01
time (sec)	N/A	0.111	0.021	0.019	0.000	0.385	0.000	0.000	0.000

Problem 234	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	174	174	114	0	0	113	0	0	-1
N.S.	1	1.00	0.66	0.00	0.00	0.65	0.00	0.00	-0.01
time (sec)	N/A	0.180	0.029	0.019	0.000	0.377	0.000	0.000	0.000

Problem 235	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	162	162	105	0	0	110	0	0	-1
N.S.	1	1.00	0.65	0.00	0.00	0.68	0.00	0.00	-0.01
time (sec)	N/A	0.155	0.033	0.017	0.000	0.368	0.000	0.000	0.000

Problem 236	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	111	111	87	0	0	91	0	0	-1
N.S.	1	1.00	0.78	0.00	0.00	0.82	0.00	0.00	-0.01
time (sec)	N/A	0.086	0.022	0.018	0.000	0.357	0.000	0.000	0.000

Problem 237	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	54	54	54	0	0	61	0	0	-1
N.S.	1	1.00	1.00	0.00	0.00	1.13	0.00	0.00	-0.02
time (sec)	N/A	0.032	0.010	0.019	0.000	0.365	0.000	0.000	0.000

Problem 238	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	13	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.08
time (sec)	N/A	0.011	0.027	0.018	0.000	0.000	0.000	0.000	0.000

Problem 239	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	13	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.08
time (sec)	N/A	0.011	0.028	0.026	0.000	0.000	0.000	0.000	0.000

Problem 240	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	13	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.08
time (sec)	N/A	0.011	0.025	0.026	0.000	0.000	0.000	0.000	0.000

Problem 241	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	F	F	F	A	F	F	F
verified	N/A	Yes	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	366	366	0	0	0	278	0	0	-1
N.S.	1	1.00	0.00	0.00	0.00	0.76	0.00	0.00	-0.00
time (sec)	N/A	0.242	0.345	0.222	0.000	0.382	0.000	0.000	0.000

Problem 242	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	184	184	189	0	0	167	0	0	-1
N.S.	1	1.00	1.03	0.00	0.00	0.91	0.00	0.00	-0.01
time (sec)	N/A	0.106	0.965	0.041	0.000	0.346	0.000	0.000	0.000

Problem 243	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	68	68	64	0	0	90	0	0	-1
N.S.	1	1.00	0.94	0.00	0.00	1.32	0.00	0.00	-0.01
time (sec)	N/A	0.095	0.023	0.021	0.000	0.412	0.000	0.000	0.000

Problem 244	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	19	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.015	0.043	0.222	0.000	0.000	0.000	0.000	0.000

Problem 245	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	19	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.014	0.071	0.217	0.000	0.000	0.000	0.000	0.000

Problem 246	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	102	102	90	0	0	125	0	0	-1
N.S.	1	1.00	0.88	0.00	0.00	1.23	0.00	0.00	-0.01
time (sec)	N/A	0.113	0.232	0.134	0.000	0.379	0.000	0.000	0.000

Problem 247	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	93	93	81	0	0	121	0	0	-1
N.S.	1	1.00	0.87	0.00	0.00	1.30	0.00	0.00	-0.01
time (sec)	N/A	0.098	0.217	0.132	0.000	0.380	0.000	0.000	0.000

Problem 248	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	91	91	78	0	0	122	0	0	-1
N.S.	1	1.00	0.86	0.00	0.00	1.34	0.00	0.00	-0.01
time (sec)	N/A	0.091	0.186	0.056	0.000	0.359	0.000	0.000	0.000

Problem 249	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	A	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	64	64	83	61	58	117	0	0	112
N.S.	1	1.00	1.30	0.95	0.91	1.83	0.00	0.00	1.75
time (sec)	N/A	0.026	0.056	1.598	0.254	0.372	0.000	0.000	0.452

Problem 250	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	94	94	82	0	0	126	0	0	-1
N.S.	1	1.00	0.87	0.00	0.00	1.34	0.00	0.00	-0.01
time (sec)	N/A	0.108	0.207	0.200	0.000	0.372	0.000	0.000	0.000

Problem 251	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	95	95	80	0	0	124	0	0	-1
N.S.	1	1.00	0.84	0.00	0.00	1.31	0.00	0.00	-0.01
time (sec)	N/A	0.106	0.208	0.199	0.000	0.370	0.000	0.000	0.000

Problem 252	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	126	126	126	0	0	175	0	0	-1
N.S.	1	1.00	1.00	0.00	0.00	1.39	0.00	0.00	-0.01
time (sec)	N/A	0.182	0.316	0.082	0.000	0.391	0.000	0.000	0.000

Problem 253	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	0	0	16	19	0	16
N.S.	1	1.00	1.00	0.00	0.00	0.76	0.90	0.00	0.76
time (sec)	N/A	0.018	0.008	0.045	0.000	0.396	0.421	0.000	0.097

Problem 254	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	0	0	16	19	0	91
N.S.	1	1.00	1.00	0.00	0.00	0.76	0.90	0.00	4.33
time (sec)	N/A	0.012	0.005	0.102	0.000	0.348	0.154	0.000	0.447

Problem 255	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	20	20	20	0	0	15	24	0	15
N.S.	1	1.00	1.00	0.00	0.00	0.75	1.20	0.00	0.75
time (sec)	N/A	0.018	0.010	0.058	0.000	0.337	0.191	0.000	0.171

Problem 256	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	0	0	16	24	0	16
N.S.	1	1.00	1.00	0.00	0.00	0.76	1.14	0.00	0.76
time (sec)	N/A	0.017	0.006	0.049	0.000	0.385	0.449	0.000	0.096

Problem 257	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	0	0	16	26	0	16
N.S.	1	1.00	1.00	0.00	0.00	0.76	1.24	0.00	0.76
time (sec)	N/A	0.018	0.006	0.041	0.000	0.331	0.817	0.000	0.145

Problem 258	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	B	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	28	28	28	0	0	24	63	0	23
N.S.	1	1.00	1.00	0.00	0.00	0.86	2.25	0.00	0.82
time (sec)	N/A	0.021	0.009	0.044	0.000	0.362	1.788	0.000	0.186

Problem 259	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	257	257	131	0	0	255	0	0	232
N.S.	1	1.00	0.51	0.00	0.00	0.99	0.00	0.00	0.90
time (sec)	N/A	0.284	0.199	0.109	0.000	0.399	0.000	0.000	0.769

Problem 260	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	142	142	91	0	0	151	0	0	128
N.S.	1	1.00	0.64	0.00	0.00	1.06	0.00	0.00	0.90
time (sec)	N/A	0.104	0.123	0.240	0.000	0.360	0.000	0.000	0.593

Problem 261	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	53	53	47	0	0	61	0	0	51
N.S.	1	1.00	0.89	0.00	0.00	1.15	0.00	0.00	0.96
time (sec)	N/A	0.026	0.014	0.237	0.000	0.353	0.000	0.000	0.174

Problem 262	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	20	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.025	0.095	0.076	0.000	0.000	0.000	0.000	0.000

Problem 263	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	93	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.093	0.137	0.266	0.000	0.000	0.000	0.000	0.000

Problem 264	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	212	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.207	0.167	0.286	0.000	0.000	0.000	0.000	0.000

Problem 265	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	171	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.150	0.199	0.100	0.000	0.000	0.000	0.000	0.000

Problem 266	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	79	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.061	0.156	0.211	0.000	0.000	0.000	0.000	0.000

Problem 267	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	17	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.06
time (sec)	N/A	0.011	0.018	0.102	0.000	0.000	0.000	0.000	0.000

Problem 268	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	59	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.073	0.136	0.110	0.000	0.000	0.000	0.000	0.000

Problem 269	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	144	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.172	0.204	0.273	0.000	0.000	0.000	0.000	0.000

Problem 270	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	107	107	68	103	0	79	99	0	82
N.S.	1	1.00	0.64	0.96	0.00	0.74	0.93	0.00	0.77
time (sec)	N/A	0.074	0.033	0.397	0.000	0.392	138.687	0.000	0.248

Problem 271	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	71	71	51	72	0	59	63	0	56
N.S.	1	1.00	0.72	1.01	0.00	0.83	0.89	0.00	0.79
time (sec)	N/A	0.046	0.022	0.177	0.000	0.387	21.181	0.000	0.182

Problem 272	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	32	32	32	41	0	40	27	0	27
N.S.	1	1.00	1.00	1.28	0.00	1.25	0.84	0.00	0.84
time (sec)	N/A	0.019	0.013	0.126	0.000	0.367	3.151	0.000	0.049

Problem 273	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	30	30	30	0	0	0	24	0	-1
N.S.	1	1.00	1.00	0.00	0.00	0.00	0.80	0.00	-0.03
time (sec)	N/A	0.024	0.015	0.048	0.000	0.000	3.440	0.000	0.000

Problem 274	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	65	65	32	0	0	0	27	0	-1
N.S.	1	1.00	0.49	0.00	0.00	0.00	0.42	0.00	-0.02
time (sec)	N/A	0.050	0.014	0.183	0.000	0.000	7.910	0.000	0.000

Problem 275	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	105	105	34	0	0	0	32	0	-1
N.S.	1	1.00	0.32	0.00	0.00	0.00	0.30	0.00	-0.01
time (sec)	N/A	0.076	0.014	0.601	0.000	0.000	45.486	0.000	0.000

Problem 276	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	148	148	52	0	0	0	0	0	-1
N.S.	1	1.00	0.35	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.094	0.019	0.395	0.000	0.000	0.000	0.000	0.000

Problem 277	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	109	109	43	0	0	0	0	0	-1
N.S.	1	1.00	0.39	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.064	0.016	0.246	0.000	0.000	0.000	0.000	0.000

Problem 278	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	A	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	70	70	36	0	0	0	22	0	-1
N.S.	1	1.00	0.51	0.00	0.00	0.00	0.31	0.00	-0.01
time (sec)	N/A	0.037	0.013	0.096	0.000	0.000	30.589	0.000	0.000

Problem 279	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	A	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	27	27	27	0	0	0	20	0	-1
N.S.	1	1.00	1.00	0.00	0.00	0.00	0.74	0.00	-0.04
time (sec)	N/A	0.011	0.009	0.062	0.000	0.000	4.593	0.000	0.000

Problem 280	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	A	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	60	60	26	0	0	0	41	0	-1
N.S.	1	1.00	0.43	0.00	0.00	0.00	0.68	0.00	-0.02
time (sec)	N/A	0.035	0.015	0.119	0.000	0.000	3.631	0.000	0.000

Problem 281	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	C	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	105	105	29	0	0	0	24	0	-1
N.S.	1	1.00	0.28	0.00	0.00	0.00	0.23	0.00	-0.01
time (sec)	N/A	0.063	0.016	0.335	0.000	0.000	22.787	0.000	0.000

Problem 282	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	C	F	F	F	C	F	F
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD	TBD
size	144	144	29	0	0	0	24	0	-1
N.S.	1	1.00	0.20	0.00	0.00	0.00	0.17	0.00	-0.01
time (sec)	N/A	0.093	0.019	0.624	0.000	0.000	175.456	0.000	0.000

Problem 283	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	144	144	95	0	0	102	0	0	206
N.S.	1	1.00	0.66	0.00	0.00	0.71	0.00	0.00	1.43
time (sec)	N/A	0.157	0.045	0.102	0.000	0.363	0.000	0.000	0.560

Problem 284	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	97	97	77	0	0	82	0	0	117
N.S.	1	1.00	0.79	0.00	0.00	0.85	0.00	0.00	1.21
time (sec)	N/A	0.079	0.030	0.142	0.000	0.353	0.000	0.000	0.440

Problem 285	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	47	47	42	0	0	46	0	0	50
N.S.	1	1.00	0.89	0.00	0.00	0.98	0.00	0.00	1.06
time (sec)	N/A	0.027	0.009	0.129	0.000	0.352	0.000	0.000	0.279

Problem 286	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	22	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.026	0.071	0.045	0.000	0.000	0.000	0.000	0.000

Problem 287	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	93	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.077	0.112	0.152	0.000	0.000	0.000	0.000	0.000

Problem 288	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	174	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.149	0.148	0.158	0.000	0.000	0.000	0.000	0.000

Problem 289	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	121	121	78	0	0	74	124	0	126
N.S.	1	1.00	0.64	0.00	0.00	0.61	1.02	0.00	1.04
time (sec)	N/A	0.106	0.029	0.064	0.000	0.360	1.834	0.000	0.505

Problem 290	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	69	69	58	0	0	53	68	0	86
N.S.	1	1.00	0.84	0.00	0.00	0.77	0.99	0.00	1.25
time (sec)	N/A	0.050	0.013	0.127	0.000	0.342	0.509	0.000	0.324

Problem 291	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	21	21	21	0	0	16	19	0	91
N.S.	1	1.00	1.00	0.00	0.00	0.76	0.90	0.00	4.33
time (sec)	N/A	0.012	0.005	0.026	0.000	0.337	0.155	0.000	0.307

Problem 292	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	59	59	56	0	0	55	0	0	-1
N.S.	1	1.00	0.95	0.00	0.00	0.93	0.00	0.00	-0.02
time (sec)	N/A	0.054	0.017	0.074	0.000	0.343	0.000	0.000	0.000

Problem 293	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	118	118	91	0	0	85	0	0	-1
N.S.	1	1.00	0.77	0.00	0.00	0.72	0.00	0.00	-0.01
time (sec)	N/A	0.116	0.026	0.153	0.000	0.356	0.000	0.000	0.000

Problem 294	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	304	304	206	0	0	262	0	0	336
N.S.	1	1.00	0.68	0.00	0.00	0.86	0.00	0.00	1.11
time (sec)	N/A	0.318	1.483	0.156	0.000	0.343	0.000	0.000	1.135

Problem 295	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	A	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	78	78	73	0	0	100	0	0	79
N.S.	1	1.00	0.94	0.00	0.00	1.28	0.00	0.00	1.01
time (sec)	N/A	0.037	0.051	0.149	0.000	0.372	0.000	0.000	0.251

Problem 296	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	22	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.025	0.126	0.051	0.000	0.000	0.000	0.000	0.000

Problem 297	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	167	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.265	0.220	0.184	0.000	0.000	0.000	0.000	0.000

Problem 298	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	F(-1)	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	468	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.619	0.346	0.065	0.000	0.000	0.000	0.000	0.000

Problem 299	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	149	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.116	0.260	0.129	0.000	0.000	0.000	0.000	0.000

Problem 300	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	19	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.05
time (sec)	N/A	0.010	0.026	0.063	0.000	0.000	0.000	0.000	0.000

Problem 301	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	79	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.136	0.243	0.079	0.000	0.000	0.000	0.000	0.000

Problem 302	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	N/A	A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	323	0	0	0	0	0	0	0	-1
N.S.	1	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.581	0.329	0.189	0.000	0.000	0.000	0.000	0.000

Problem 303	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	A	F	A	A	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	33	33	33	41	0	39	53	0	28
N.S.	1	1.00	1.00	1.24	0.00	1.18	1.61	0.00	0.85
time (sec)	N/A	0.079	0.037	0.177	0.000	0.372	11.080	0.000	0.173

Problem 304	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	F	F	F	F	F	F	F
verified	N/A	Yes	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	0	0	0	0	0	0	-1
N.S.	1	1.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.040	0.391	0.056	0.000	0.000	0.000	0.000	0.000

Problem 305	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	F	F	F	F	F	F	F
verified	N/A	Yes	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	67	67	0	0	0	0	0	0	-1
N.S.	1	1.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.038	0.377	0.072	0.000	0.000	0.000	0.000	0.000

Problem 306	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	F	F	F	F	F	F	F
verified	N/A	Yes	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	0	0	0	0	0	0	-1
N.S.	1	1.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.036	0.379	0.155	0.000	0.000	0.000	0.000	0.000

Problem 307	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	F	F	F	F	F	F	F
verified	N/A	Yes	N/A	TBD	TBD	TBD	TBD	TBD	TBD
size	63	63	0	0	0	0	0	0	-1
N.S.	1	1.00	0.00	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.036	0.406	0.151	0.000	0.000	0.000	0.000	0.000

Problem 308	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	74	0	0	0	0	0	-1
N.S.	1	1.00	1.30	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.037	0.900	0.058	0.000	0.000	0.000	0.000	0.000

Problem 309	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	72	0	0	0	0	0	-1
N.S.	1	1.00	1.26	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.034	0.558	0.061	0.000	0.000	0.000	0.000	0.000

Problem 310	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	74	0	0	0	0	0	-1
N.S.	1	1.00	1.30	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.036	7.535	0.171	0.000	0.000	0.000	0.000	0.000

Problem 311	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	57	57	72	0	0	0	0	0	-1
N.S.	1	1.00	1.26	0.00	0.00	0.00	0.00	0.00	-0.02
time (sec)	N/A	0.036	1.178	0.151	0.000	0.000	0.000	0.000	0.000

2.3 Detailed conclusion table specific for Rubi results

The following table is specific to Rubi. It gives additional statistics for each integral. the column **steps** is the number of steps used by Rubi to obtain the antiderivative. The **rules** column is the number of unique rules used. The **integrand size** column is the leaf size of the integrand. Finally the ratio $\frac{\text{number of rules}}{\text{integrand size}}$ is given. The larger this ratio is, the harder the integral was to solve. In this test, problem number [95] had the largest ratio of [40]

Table 2.1: Rubi specific breakdown of results for each integral

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1	A	5	3	1.00	8	0.375
2	A	4	3	1.00	8	0.375
3	A	3	3	1.00	6	0.500
4	A	1	1	1.00	8	0.125
5	A	3	3	1.00	8	0.375
6	A	4	3	1.00	8	0.375
7	A	5	3	1.00	8	0.375
8	A	5	3	1.00	8	0.375
9	A	4	3	1.00	8	0.375
10	A	3	3	1.00	8	0.375
11	A	1	1	1.00	4	0.250
12	A	2	2	1.00	8	0.250
13	A	3	3	1.00	8	0.375
14	A	4	3	1.00	8	0.375
15	A	12	5	1.00	14	0.357
16	A	9	5	1.00	14	0.357
17	A	7	5	1.00	12	0.417
18	A	1	1	1.00	6	0.167
19	A	0	0	0.00	0	0.000
20	A	0	0	0.00	0	0.000
21	A	0	0	0.00	0	0.000
22	A	12	6	1.00	10	0.600
23	A	8	6	1.00	10	0.600
24	A	5	5	1.00	8	0.625
25	A	0	0	0.00	0	0.000

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
26	A	5	5	1.00	10	0.500
27	A	8	6	1.00	10	0.600
28	A	12	6	1.00	10	0.600
29	A	10	5	1.00	10	0.500
30	A	6	5	1.00	10	0.500
31	A	4	4	1.00	6	0.667
32	A	0	0	0.00	0	0.000
33	A	0	0	0.00	0	0.000
34	A	0	0	0.00	0	0.000
35	A	16	10	1.00	16	0.625
36	A	10	9	1.00	14	0.643
37	A	4	3	1.00	8	0.375
38	A	0	0	0.00	0	0.000
39	A	0	0	0.00	0	0.000
40	A	5	5	1.00	17	0.294
41	A	5	5	1.00	15	0.333
42	A	5	5	1.00	13	0.385
43	A	3	1	1.00	17	0.059
44	A	5	5	1.00	17	0.294
45	A	5	5	1.00	17	0.294
46	A	5	5	1.00	19	0.263
47	A	2	2	1.00	19	0.105
48	A	2	2	1.00	17	0.118
49	A	2	2	1.00	19	0.105
50	A	2	2	1.00	19	0.105
51	A	2	2	1.00	19	0.105
52	A	2	2	1.00	19	0.105
53	A	9	4	1.00	17	0.235
54	A	5	4	1.00	17	0.235
55	A	2	2	1.00	15	0.133
56	A	0	0	0.00	0	0.000
57	A	0	0	0.00	0	0.000
58	A	0	0	0.00	0	0.000
59	A	0	0	0.00	0	0.000
60	A	0	0	0.00	0	0.000

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
61	A	0	0	0.00	0	0.000
62	A	0	0	0.00	0	0.000
63	A	0	0	0.00	0	0.000
64	A	8	5	1.00	19	0.263
65	A	5	5	1.00	19	0.263
66	A	2	2	1.00	17	0.118
67	A	1	1	1.00	19	0.053
68	A	4	4	1.00	19	0.210
69	A	7	4	1.00	19	0.210
70	A	7	4	1.00	19	0.210
71	A	4	4	1.00	19	0.210
72	A	1	1	1.00	16	0.062
73	A	4	4	1.00	19	0.210
74	A	7	5	1.00	19	0.263
75	A	9	4	1.00	18	0.222
76	A	5	4	1.00	18	0.222
77	A	2	2	1.00	16	0.125
78	A	0	0	0.00	0	0.000
79	A	0	0	0.00	0	0.000
80	A	0	0	0.00	0	0.000
81	A	7	5	1.00	18	0.278
82	A	4	4	1.00	18	0.222
83	A	2	2	1.00	15	0.133
84	A	4	4	1.00	18	0.222
85	A	7	5	1.00	18	0.278
86	A	10	6	1.00	19	0.316
87	A	3	3	1.00	17	0.176
88	A	0	0	0.00	0	0.000
89	A	0	0	0.00	0	0.000
90	A	0	0	0.00	0	0.000
91	A	0	0	0.00	0	0.000
92	A	0	0	0.00	0	0.000
93	A	0	0	0.00	0	0.000
94	A	0	0	0.00	0	0.000
95	A	4	3	1.00	40	0.075

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
96	A	4	4	1.00	18	0.222
97	A	4	4	1.00	18	0.222
98	A	4	4	1.00	18	0.222
99	A	4	4	1.00	18	0.222
100	A	4	4	1.00	15	0.267
101	A	4	4	1.00	16	0.250
102	A	4	4	1.00	15	0.267
103	A	4	4	1.00	16	0.250
104	A	5	3	1.00	8	0.375
105	A	4	3	1.00	8	0.375
106	A	3	3	1.00	6	0.500
107	A	2	2	1.00	8	0.250
108	A	3	3	1.00	8	0.375
109	A	4	3	1.00	8	0.375
110	A	5	3	1.00	8	0.375
111	A	5	3	1.00	8	0.375
112	A	4	3	1.00	8	0.375
113	A	3	3	1.00	8	0.375
114	A	1	1	1.00	4	0.250
115	A	2	2	1.00	8	0.250
116	A	3	3	1.00	8	0.375
117	A	4	3	1.00	8	0.375
118	A	12	5	1.00	14	0.357
119	A	9	5	1.00	14	0.357
120	A	7	5	1.00	12	0.417
121	A	1	1	1.00	6	0.167
122	A	0	0	0.00	0	0.000
123	A	0	0	0.00	0	0.000
124	A	0	0	0.00	0	0.000
125	A	12	6	1.00	10	0.600
126	A	8	6	1.00	10	0.600
127	A	5	5	1.00	8	0.625
128	A	0	0	0.00	0	0.000
129	A	5	5	1.00	10	0.500
130	A	8	6	1.00	10	0.600

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
131	A	12	6	1.00	10	0.600
132	A	10	5	1.00	10	0.500
133	A	6	5	1.00	10	0.500
134	A	4	4	1.00	6	0.667
135	A	0	0	0.00	0	0.000
136	A	0	0	0.00	0	0.000
137	A	0	0	0.00	0	0.000
138	A	16	10	1.00	16	0.625
139	A	10	9	1.00	14	0.643
140	A	4	3	1.00	8	0.375
141	A	0	0	0.00	0	0.000
142	A	0	0	0.00	0	0.000
143	A	5	5	1.00	17	0.294
144	A	5	5	1.00	15	0.333
145	A	5	5	1.00	13	0.385
146	A	3	1	1.00	17	0.059
147	A	5	5	1.00	17	0.294
148	A	5	5	1.00	17	0.294
149	A	5	5	1.00	19	0.263
150	A	2	2	1.00	19	0.105
151	A	2	2	1.00	17	0.118
152	A	2	2	1.00	19	0.105
153	A	2	2	1.00	19	0.105
154	A	2	2	1.00	19	0.105
155	A	2	2	1.00	19	0.105
156	A	9	4	1.00	17	0.235
157	A	5	4	1.00	17	0.235
158	A	2	2	1.00	15	0.133
159	A	0	0	0.00	0	0.000
160	A	0	0	0.00	0	0.000
161	A	0	0	0.00	0	0.000
162	A	0	0	0.00	0	0.000
163	A	0	0	0.00	0	0.000
164	A	0	0	0.00	0	0.000
165	A	0	0	0.00	0	0.000

Continued on next page

Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
166	A	0	0	0.00	0	0.000
167	A	8	5	1.00	19	0.263
168	A	5	5	1.00	19	0.263
169	A	2	2	1.00	17	0.118
170	A	3	3	1.00	19	0.158
171	A	6	6	1.00	19	0.316
172	A	9	6	1.00	19	0.316
173	A	9	6	1.00	19	0.316
174	A	6	6	1.00	19	0.316
175	A	3	3	1.00	16	0.188
176	A	6	6	1.00	19	0.316
177	A	9	7	1.00	19	0.368
178	A	9	4	1.00	18	0.222
179	A	5	4	1.00	18	0.222
180	A	2	2	1.00	16	0.125
181	A	0	0	0.00	0	0.000
182	A	0	0	0.00	0	0.000
183	A	0	0	0.00	0	0.000
184	A	7	5	1.00	18	0.278
185	A	4	4	1.00	18	0.222
186	A	2	2	1.00	15	0.133
187	A	4	4	1.00	18	0.222
188	A	7	5	1.00	18	0.278
189	A	10	6	1.00	19	0.316
190	A	3	3	1.00	17	0.176
191	A	0	0	0.00	0	0.000
192	A	0	0	0.00	0	0.000
193	A	0	0	0.00	0	0.000
194	A	0	0	0.00	0	0.000
195	A	0	0	0.00	0	0.000
196	A	0	0	0.00	0	0.000
197	A	0	0	0.00	0	0.000
198	A	4	3	1.00	40	0.075
199	A	6	6	1.00	18	0.333
200	A	6	6	1.00	18	0.333

Continued on next page

Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
201	A	6	6	1.00	18	0.333
202	A	6	6	1.00	18	0.333
203	A	6	6	1.00	15	0.400
204	A	6	6	1.00	16	0.375
205	A	6	6	1.00	15	0.400
206	A	6	6	1.00	16	0.375
207	A	5	3	1.00	8	0.375
208	A	4	3	1.00	8	0.375
209	A	3	3	1.00	6	0.500
210	A	1	1	1.00	8	0.125
211	A	3	3	1.00	8	0.375
212	A	4	3	1.00	8	0.375
213	A	5	3	1.00	8	0.375
214	A	5	3	1.00	8	0.375
215	A	4	3	1.00	8	0.375
216	A	3	3	1.00	8	0.375
217	A	1	1	1.00	4	0.250
218	A	2	2	1.00	8	0.250
219	A	3	3	1.00	8	0.375
220	A	4	3	1.00	8	0.375
221	A	12	5	1.00	14	0.357
222	A	9	5	1.00	14	0.357
223	A	7	5	1.00	12	0.417
224	A	1	1	1.00	6	0.167
225	A	0	0	0.00	0	0.000
226	A	0	0	0.00	0	0.000
227	A	0	0	0.00	0	0.000
228	A	12	6	1.00	10	0.600
229	A	8	6	1.00	10	0.600
230	A	5	5	1.00	8	0.625
231	A	0	0	0.00	0	0.000
232	A	5	5	1.00	10	0.500
233	A	8	6	1.00	10	0.600
234	A	12	6	1.00	10	0.600
235	A	10	5	1.00	10	0.500

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
236	A	6	5	1.00	10	0.500
237	A	4	4	1.00	6	0.667
238	A	0	0	0.00	0	0.000
239	A	0	0	0.00	0	0.000
240	A	0	0	0.00	0	0.000
241	A	16	10	1.00	16	0.625
242	A	10	9	1.00	14	0.643
243	A	4	3	1.00	8	0.375
244	A	0	0	0.00	0	0.000
245	A	0	0	0.00	0	0.000
246	A	5	5	1.00	17	0.294
247	A	5	5	1.00	15	0.333
248	A	5	5	1.00	13	0.385
249	A	3	1	1.00	17	0.059
250	A	5	5	1.00	17	0.294
251	A	5	5	1.00	17	0.294
252	A	5	5	1.00	19	0.263
253	A	2	2	1.00	18	0.111
254	A	2	2	1.00	16	0.125
255	A	2	2	1.00	18	0.111
256	A	2	2	1.00	18	0.111
257	A	2	2	1.00	18	0.111
258	A	2	2	1.00	18	0.111
259	A	9	4	1.00	17	0.235
260	A	5	4	1.00	17	0.235
261	A	2	2	1.00	15	0.133
262	A	0	0	0.00	0	0.000
263	A	0	0	0.00	0	0.000
264	A	0	0	0.00	0	0.000
265	A	0	0	0.00	0	0.000
266	A	0	0	0.00	0	0.000
267	A	0	0	0.00	0	0.000
268	A	0	0	0.00	0	0.000
269	A	0	0	0.00	0	0.000
270	A	6	4	1.00	18	0.222

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
271	A	4	4	1.00	18	0.222
272	A	2	2	1.00	16	0.125
273	A	1	1	1.00	18	0.056
274	A	3	3	1.00	18	0.167
275	A	5	3	1.00	18	0.167
276	A	7	3	1.00	18	0.167
277	A	5	3	1.00	18	0.167
278	A	3	3	1.00	18	0.167
279	A	1	1	1.00	15	0.067
280	A	3	3	1.00	18	0.167
281	A	5	4	1.00	18	0.222
282	A	7	4	1.00	18	0.222
283	A	9	4	1.00	19	0.210
284	A	5	4	1.00	19	0.210
285	A	2	2	1.00	17	0.118
286	A	0	0	0.00	0	0.000
287	A	0	0	0.00	0	0.000
288	A	0	0	0.00	0	0.000
289	A	7	5	1.00	19	0.263
290	A	4	4	1.00	19	0.210
291	A	2	2	1.00	16	0.125
292	A	4	4	1.00	19	0.210
293	A	7	5	1.00	19	0.263
294	A	10	6	1.00	19	0.316
295	A	3	3	1.00	17	0.176
296	A	0	0	0.00	0	0.000
297	A	0	0	0.00	0	0.000
298	A	0	0	0.00	0	0.000
299	A	0	0	0.00	0	0.000
300	A	0	0	0.00	0	0.000
301	A	0	0	0.00	0	0.000
302	A	0	0	0.00	0	0.000
303	A	5	3	1.00	40	0.075
304	A	4	4	1.00	18	0.222
305	A	4	4	1.00	18	0.222

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
306	A	4	4	1.00	18	0.222
307	A	4	4	1.00	18	0.222
308	A	4	4	1.00	15	0.267
309	A	4	4	1.00	16	0.250
310	A	4	4	1.00	15	0.267
311	A	4	4	1.00	16	0.250

Chapter 3

Listing of integrals

Local contents

3.1 $\int x^5 \mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=96

$$\frac{5e^{-b^2x^2}x}{8b^5\sqrt{\pi}}+\frac{5e^{-b^2x^2}x^3}{12b^3\sqrt{\pi}}+\frac{e^{-b^2x^2}x^5}{6b\sqrt{\pi}}-\frac{5\mathrm{Erf}(bx)}{16b^6}+\frac{1}{6}x^6\mathrm{Erf}(bx)$$

```
[Out] -5/16*erf(b*x)/b^6+1/6*x^6*erf(b*x)+5/8*x/b^5/exp(b^2*x^2)/Pi^(1/2)+5/12*x^
3/b^3/exp(b^2*x^2)/Pi^(1/2)+1/6*x^5/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.06, antiderivative size = 96, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.375, Rules used = {6496, 2243, 2236}

$$-\frac{5\mathrm{Erf}(bx)}{16b^6}+\frac{x^5e^{-b^2x^2}}{6\sqrt{\pi}\,b}+\frac{5xe^{-b^2x^2}}{8\sqrt{\pi}\,b^5}+\frac{5x^3e^{-b^2x^2}}{12\sqrt{\pi}\,b^3}+\frac{1}{6}x^6\mathrm{Erf}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x^5*Erf[b*x],x]
```

```
[Out] (5*x)/(8*b^5*E^(b^2*x^2)*Sqrt[Pi]) + (5*x^3)/(12*b^3*E^(b^2*x^2)*Sqrt[Pi])
+ x^5/(6*b*E^(b^2*x^2)*Sqrt[Pi]) - (5*Erf[b*x])/(16*b^6) + (x^6*Erf[b*x])/6
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6496

```
Int[Erf[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(
c + d*x)^(m + 1)*(Erf[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(m
+ 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d, m
}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int x^5\text{erf}(bx)\,dx &= \frac{1}{6}x^6\text{erf}(bx)-\frac{b\int e^{-b^2x^2}x^6\,dx}{3\sqrt{\pi}}\\
&= \frac{e^{-b^2x^2}x^5}{6b\sqrt{\pi}}+\frac{1}{6}x^6\text{erf}(bx)-\frac{5\int e^{-b^2x^2}x^4\,dx}{6b\sqrt{\pi}}\\
&= \frac{5e^{-b^2x^2}x^3}{12b^3\sqrt{\pi}}+\frac{e^{-b^2x^2}x^5}{6b\sqrt{\pi}}+\frac{1}{6}x^6\text{erf}(bx)-\frac{5\int e^{-b^2x^2}x^2\,dx}{4b^3\sqrt{\pi}}\\
&= \frac{5e^{-b^2x^2}x}{8b^5\sqrt{\pi}}+\frac{5e^{-b^2x^2}x^3}{12b^3\sqrt{\pi}}+\frac{e^{-b^2x^2}x^5}{6b\sqrt{\pi}}+\frac{1}{6}x^6\text{erf}(bx)-\frac{5\int e^{-b^2x^2}\,dx}{8b^5\sqrt{\pi}}\\
&= \frac{5e^{-b^2x^2}x}{8b^5\sqrt{\pi}}+\frac{5e^{-b^2x^2}x^3}{12b^3\sqrt{\pi}}+\frac{e^{-b^2x^2}x^5}{6b\sqrt{\pi}}-\frac{5\text{erf}(bx)}{16b^6}+\frac{1}{6}x^6\text{erf}(bx)
\end{aligned}
$$

Mathematica [A]
time = 0.02, size = 72, normalized size = 0.75

$$
\frac{e^{-b^2x^2}\left(30bx+20b^3x^3+8b^5x^5+e^{b^2x^2}\sqrt{\pi}\,(-15+8b^6x^6)\,\text{Erf}(bx)\right)}{48b^6\sqrt{\pi}}
$$

Antiderivative was successfully verified.

```
[In] Integrate[x^5*Erf[b*x],x]
[Out] (30*b*x + 20*b^3*x^3 + 8*b^5*x^5 + E^(b^2*x^2)*Sqrt[Pi]*(-15 + 8*b^6*x^6)*E
rf[b*x])/(48*b^6*E^(b^2*x^2)*Sqrt[Pi])
```

Maple [A]
time = 0.23, size = 83, normalized size = 0.86

method	result	size
meijerg	$\frac{\frac{xb\left(28b^4x^4+70b^2x^2+105\right)e^{-b^2x^2}}{84}-\frac{\left(-56b^6x^6+105\right)\text{erf}(bx)\sqrt{\pi}}{168}}{2b^6\sqrt{\pi}}$	60
derivativedivides	$\frac{\frac{\text{erf}(bx)b^6x^6}{6}-\frac{-\frac{e^{-b^2x^2}b^5x^5}{2}-\frac{5b^3x^3e^{-b^2x^2}}{4}-\frac{15e^{-b^2x^2}bx}{8}+\frac{15\,\text{erf}(bx)\sqrt{\pi}}{16}}{3\sqrt{\pi}}}{b^6}$	83
default	$\frac{\frac{\text{erf}(bx)b^6x^6}{6}-\frac{-\frac{e^{-b^2x^2}b^5x^5}{2}-\frac{5b^3x^3e^{-b^2x^2}}{4}-\frac{15e^{-b^2x^2}bx}{8}+\frac{15\,\text{erf}(bx)\sqrt{\pi}}{16}}{3\sqrt{\pi}}}{b^6}$	83

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*erf(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b^6*(1/6*erf(b*x)*b^6*x^6-1/3/Pi^(1/2)*(-1/2/exp(b^2*x^2)*b^5*x^5-5/4*b^3
*x^3/exp(b^2*x^2)-15/8*b*x/exp(b^2*x^2)+15/16*erf(b*x)*Pi^(1/2)))
```

Maxima [A]
time = 0.26, size = 63, normalized size = 0.66

$$\frac{1}{6}\,x^6\operatorname{erf}\left(bx\right)+\frac{b\left(\frac{2\,\left(4\,b^4x^5+10\,b^2x^3+15\,x\right)e^{\left(-b^2x^2\right)}}{b^6}-\frac{15\,\sqrt{\pi}\,\operatorname{erf}(bx)}{b^7}\right)}{48\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erf(b*x),x, algorithm="maxima")
```

```
[Out] 1/6*x^6*erf(b*x) + 1/48*b*(2*(4*b^4*x^5 + 10*b^2*x^3 + 15*x)*e^(-b^2*x^2)/b
^6 - 15*sqrt(pi)*erf(b*x)/b^7)/sqrt(pi)
```

Fricas [A]
time = 0.38, size = 63, normalized size = 0.66

$$\frac{2\,\sqrt{\pi}\,(4\,b^5x^5+10\,b^3x^3+15\,bx)e^{\left(-b^2x^2\right)}-(15\,\pi-8\,\pi b^6x^6)\operatorname{erf}\left(bx\right)}{48\,\pi b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erf(b*x),x, algorithm="fricas")
```

```
[Out] 1/48*(2*sqrt(pi)*(4*b^5*x^5 + 10*b^3*x^3 + 15*b*x)*e^(-b^2*x^2) - (15*pi -
8*pi*b^6*x^6)*erf(b*x))/(pi*b^6)
```

Sympy [A]
time = 0.51, size = 88, normalized size = 0.92

$$\begin{cases}\frac{x^6\operatorname{erf}\left(bx\right)}{6}+\frac{x^5e^{-b^2x^2}}{6\sqrt{\pi}\,b}+\frac{5x^3e^{-b^2x^2}}{12\sqrt{\pi}\,b^3}+\frac{5xe^{-b^2x^2}}{8\sqrt{\pi}\,b^5}-\frac{5\operatorname{erf}\left(bx\right)}{16b^6} & \text{for } b\neq 0\\ 0 & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**5*erf(b*x),x)
```

```
[Out] Piecewise((x**6*erf(b*x)/6 + x**5*exp(-b**2*x**2)/(6*sqrt(pi)*b) + 5*x**3*e
xp(-b**2*x**2)/(12*sqrt(pi)*b**3) + 5*x*exp(-b**2*x**2)/(8*sqrt(pi)*b**5) -
 5*erf(b*x)/(16*b**6), Ne(b, 0)), (0, True))
```

Giac [A]
time = 0.41, size = 64, normalized size = 0.67

$$\frac{1}{6}\,x^6\operatorname{erf}\left(bx\right)+\frac{b\left(\frac{2\,\left(4\,b^4x^5+10\,b^2x^3+15\,x\right)e^{\left(-b^2x^2\right)}}{b^6}+\frac{15\,\sqrt{\pi}\,\operatorname{erf}(-bx)}{b^7}\right)}{48\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erf(b*x),x, algorithm="giac")
```

```
[Out] 1/6*x^6*erf(b*x) + 1/48*b*(2*(4*b^4*x^5 + 10*b^2*x^3 + 15*x)*e^(-b^2*x^2)/b
^6 + 15*sqrt(pi)*erf(-b*x)/b^7)/sqrt(pi)
```

Mupad [B]
time = 0.47, size = 108, normalized size = 1.12

$$\frac{x^6\,\mathrm{erf}(b\,x)}{6}-\frac{5\,b\,x^7}{16\,{\left(b^2\,x^2\right)}^{7/2}}+\frac{x^5\,\mathrm{e}^{-b^2\,x^2}}{6\,b\,\sqrt{\pi}}+\frac{5\,x^3\,\mathrm{e}^{-b^2\,x^2}}{12\,b^3\,\sqrt{\pi}}+\frac{5\,x\,\mathrm{e}^{-b^2\,x^2}}{8\,b^5\,\sqrt{\pi}}+\frac{5\,b\,x^7\,\mathrm{erfc}\left(\sqrt{b^2\,x^2}\right)}{16\,{\left(b^2\,x^2\right)}^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*erf(b*x),x)
```

```
[Out] (x^6*erf(b*x))/6 - (5*b*x^7)/(16*(b^2*x^2)^(7/2)) + (x^5*exp(-b^2*x^2))/(6*
b*pi^(1/2)) + (5*x^3*exp(-b^2*x^2))/(12*b^3*pi^(1/2)) + (5*x*exp(-b^2*x^2))
/(8*b^5*pi^(1/2)) + (5*b*x^7*erfc((b^2*x^2)^(1/2)))/(16*(b^2*x^2)^(7/2))
```

3.2 $\int x^3 \mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=71

$$\frac{3e^{-b^2x^2}x}{8b^3\sqrt{\pi}}+\frac{e^{-b^2x^2}x^3}{4b\sqrt{\pi}}-\frac{3\text{Erf}(bx)}{16b^4}+\frac{1}{4}x^4\text{Erf}(bx)$$

```
[Out] -3/16*erf(b*x)/b^4+1/4*x^4*erf(b*x)+3/8*x/b^3/exp(b^2*x^2)/Pi^(1/2)+1/4*x^3
/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.04, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}}=0.375$, Rules used = {6496, 2243, 2236}

$$-\frac{3\text{Erf}(bx)}{16b^4}+\frac{x^3e^{-b^2x^2}}{4\sqrt{\pi}\,b}+\frac{3xe^{-b^2x^2}}{8\sqrt{\pi}\,b^3}+\frac{1}{4}x^4\text{Erf}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x^3*Erf[b*x],x]
```

```
[Out] (3*x)/(8*b^3*E^(b^2*x^2)*Sqrt[Pi]) + x^3/(4*b*E^(b^2*x^2)*Sqrt[Pi]) - (3*Er
f[b*x])/(16*b^4) + (x^4*Erf[b*x])/4
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6496

```
Int[Erf[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(
c + d*x)^(m + 1)*(Erf[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(m
+ 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d, m
}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int x^3 \operatorname{erf}(bx)\,dx &= \frac{1}{4}x^4\operatorname{erf}(bx) - \frac{b\int e^{-b^2x^2}x^4\,dx}{2\sqrt{\pi}}\\
&= \frac{e^{-b^2x^2}x^3}{4b\sqrt{\pi}} + \frac{1}{4}x^4\operatorname{erf}(bx) - \frac{3\int e^{-b^2x^2}x^2\,dx}{4b\sqrt{\pi}}\\
&= \frac{3e^{-b^2x^2}x}{8b^3\sqrt{\pi}} + \frac{e^{-b^2x^2}x^3}{4b\sqrt{\pi}} + \frac{1}{4}x^4\operatorname{erf}(bx) - \frac{3\int e^{-b^2x^2}\,dx}{8b^3\sqrt{\pi}}\\
&= \frac{3e^{-b^2x^2}x}{8b^3\sqrt{\pi}} + \frac{e^{-b^2x^2}x^3}{4b\sqrt{\pi}} - \frac{3\operatorname{erf}(bx)}{16b^4} + \frac{1}{4}x^4\operatorname{erf}(bx)
\end{aligned}$$

Mathematica [A]
time = 0.02, size = 63, normalized size = 0.89

$$e^{-b^2x^2}\left(\frac{3x}{8b^3\sqrt{\pi}} + \frac{x^3}{4b\sqrt{\pi}}\right) - \frac{3\operatorname{Erf}(bx)}{16b^4} + \frac{1}{4}x^4\operatorname{Erf}(bx)$$

Antiderivative was successfully verified.

```
[In] Integrate[x^3*Erf[b*x],x]
```

```
[Out] ((3*x)/(8*b^3*Sqrt[Pi]) + x^3/(4*b*Sqrt[Pi]))/E^(b^2*x^2) - (3*Erf[b*x])/(1
6*b^4) + (x^4*Erf[b*x])/4
```

Maple [A]
time = 0.21, size = 65, normalized size = 0.92

method	result	size
meijerg	$\frac{\frac{xb(10b^2x^2+15)e^{-b^2x^2}}{20}-\frac{(-20b^4x^4+15)\operatorname{erf}(bx)\sqrt{\pi}}{40}}{2b^4\sqrt{\pi}}$	52
derivativedivides	$\frac{\frac{\operatorname{erf}(bx)b^4x^4}{4}-\frac{-\frac{b^3x^3e^{-b^2x^2}}{2}-\frac{3e^{-b^2x^2}bx}{4}+\frac{3\operatorname{erf}(bx)\sqrt{\pi}}{8}}{2\sqrt{\pi}}}{b^4}$	65
default	$\frac{\frac{\operatorname{erf}(bx)b^4x^4}{4}-\frac{-\frac{b^3x^3e^{-b^2x^2}}{2}-\frac{3e^{-b^2x^2}bx}{4}+\frac{3\operatorname{erf}(bx)\sqrt{\pi}}{8}}{2\sqrt{\pi}}}{b^4}$	65

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erf(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b^4*(1/4*erf(b*x)*b^4*x^4-1/2/Pi^(1/2)*(-1/2*b^3*x^3/exp(b^2*x^2)-3/4*b*x
/exp(b^2*x^2)+3/8*erf(b*x)*Pi^(1/2)))
```

Maxima [A]
time = 0.26, size = 55, normalized size = 0.77

$$\frac{1}{4}\,x^{4}\,\mathrm{erf}\left(bx\right)+\frac{b\left(\frac{2\,\left(2\,b^{2}x^{3}+3\,x\right)e^{\left(-b^{2}x^{2}\right)}}{b^{4}}-\frac{3\,\sqrt{\pi}\,\mathrm{erf}\left(bx\right)}{b^{5}}\right)}{16\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erf(b*x),x, algorithm="maxima")
```

```
[Out] 1/4*x^4*erf(b*x) + 1/16*b*(2*(2*b^2*x^3 + 3*x)*e^(-b^2*x^2)/b^4 - 3*sqrt(pi
)*erf(b*x)/b^5)/sqrt(pi)
```

Fricas [A]
time = 0.37, size = 55, normalized size = 0.77

$$\frac{2\,\sqrt{\pi}\,\left(2\,b^{3}x^{3}+3\,bx\right)e^{\left(-b^{2}x^{2}\right)}-\left(3\,\pi-4\,\pi b^{4}x^{4}\right)\mathrm{erf}\left(bx\right)}{16\,\pi b^{4}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erf(b*x),x, algorithm="fricas")
```

```
[Out] 1/16*(2*sqrt(pi)*(2*b^3*x^3 + 3*b*x)*e^(-b^2*x^2) - (3*pi - 4*pi*b^4*x^4)*e
rf(b*x))/(pi*b^4)
```

Sympy [A]
time = 0.29, size = 65, normalized size = 0.92

$$\begin{cases}\frac{x^{4}\,\mathrm{erf}\left(bx\right)}{4}+\frac{x^{3}e^{-b^{2}x^{2}}}{4\sqrt{\pi}\,b}+\frac{3xe^{-b^{2}x^{2}}}{8\sqrt{\pi}\,b^{3}}-\frac{3\,\mathrm{erf}\left(bx\right)}{16b^{4}} & \text{for}\ b\neq 0\\ 0 & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3*erf(b*x),x)
```

```
[Out] Piecewise((x**4*erf(b*x)/4 + x**3*exp(-b**2*x**2)/(4*sqrt(pi)*b) + 3*x*exp(
-b**2*x**2)/(8*sqrt(pi)*b**3) - 3*erf(b*x)/(16*b**4), Ne(b, 0)), (0, True))
```

Giac [A]
time = 0.41, size = 56, normalized size = 0.79

$$\frac{1}{4}\,x^{4}\,\mathrm{erf}\left(bx\right)+\frac{b\left(\frac{2\,\left(2\,b^{2}x^{3}+3\,x\right)e^{\left(-b^{2}x^{2}\right)}}{b^{4}}+\frac{3\,\sqrt{\pi}\,\mathrm{erf}\left(-bx\right)}{b^{5}}\right)}{16\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erf(b*x),x, algorithm="giac")
```

```
[Out] 1/4*x^4*erf(b*x) + 1/16*b*(2*(2*b^2*x^3 + 3*x)*e^(-b^2*x^2)/b^4 + 3*sqrt(pi
)*erf(-b*x)/b^5)/sqrt(pi)
```

Mupad [B]
time = 0.10, size = 88, normalized size = 1.24

$$\frac{x^4\,\mathrm{erf}(b\,x)}{4}-\frac{3\,b\,x^5}{16\,{\left(b^2\,x^2\right)}^{5/2}}+\frac{x^3\,\mathrm{e}^{-b^2\,x^2}}{4\,b\,\sqrt{\pi}}+\frac{3\,x\,\mathrm{e}^{-b^2\,x^2}}{8\,b^3\,\sqrt{\pi}}+\frac{3\,b\,x^5\,\mathrm{erfc}\left(\sqrt{b^2\,x^2}\right)}{16\,{\left(b^2\,x^2\right)}^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erf(b*x),x)
```

```
[Out] (x^4*erf(b*x))/4 - (3*b*x^5)/(16*(b^2*x^2)^(5/2)) + (x^3*exp(-b^2*x^2))/(4*
b*pi^(1/2)) + (3*x*exp(-b^2*x^2))/(8*b^3*pi^(1/2)) + (3*b*x^5*erfc((b^2*x^2
)^(1/2)))/(16*(b^2*x^2)^(5/2))
```

3.3 $\int x\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=46

$$\frac{e^{-b^2x^2}x}{2b\sqrt{\pi}}-\frac{\text{Erf}(bx)}{4b^2}+\frac{1}{2}x^2\text{Erf}(bx)$$

```
[Out] -1/4*erf(b*x)/b^2+1/2*x^2*erf(b*x)+1/2*x/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.02, antiderivative size = 46, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.500, Rules used = {6496, 2243, 2236}

$$-\frac{\text{Erf}(bx)}{4b^2}+\frac{xe^{-b^2x^2}}{2\sqrt{\pi}\,b}+\frac{1}{2}x^2\text{Erf}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x*Erf[b*x],x]
```

```
[Out] x/(2*b*E^(b^2*x^2)*Sqrt[Pi]) - Erf[b*x]/(4*b^2) + (x^2*Erf[b*x])/2
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6496

```
Int[Erf[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(
c + d*x)^(m + 1)*(Erf[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(m
+ 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d, m
}, x] && NeQ[m, -1]
```

Rubi steps

$$\int x\mathrm{erf}(bx)\,dx = \frac{1}{2}x^2\mathrm{erf}(bx) - \frac{b\int e^{-b^2x^2}x^2\,dx}{\sqrt{\pi}}$$
$$= \frac{e^{-b^2x^2}x}{2b\sqrt{\pi}} + \frac{1}{2}x^2\mathrm{erf}(bx) - \frac{\int e^{-b^2x^2}\,dx}{2b\sqrt{\pi}}$$
$$= \frac{e^{-b^2x^2}x}{2b\sqrt{\pi}} - \frac{\mathrm{erf}(bx)}{4b^2} + \frac{1}{2}x^2\mathrm{erf}(bx)$$

Mathematica [**A**]
time = 0.02, size = 42, normalized size = 0.91

$$\frac{1}{4}\left(\frac{2e^{-b^2x^2}x}{b\sqrt{\pi}} + \left(-\frac{1}{b^2} + 2x^2\right)\mathrm{Erf}(bx)\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x*Erf[b*x],x]
[Out] ((2*x)/(b*E^(b^2*x^2)*Sqrt[Pi]) + (-b^(-2) + 2*x^2)*Erf[b*x])/4
```

Maple [**A**]
time = 0.22, size = 47, normalized size = 1.02

method	result	size
meijerg	$\frac{e^{-b^2x^2}bx - \frac{\left(-6b^2x^2+3\right)\mathrm{erf}(bx)\sqrt{\pi}}{6}}{2b^2\sqrt{\pi}}$	41
derivativedivides	$\frac{\frac{\mathrm{erf}(bx)b^2x^2}{2} - \frac{-\frac{e^{-b^2x^2}bx}{2} + \frac{\mathrm{erf}(bx)\sqrt{\pi}}{4}}{\sqrt{\pi}}}{b^2}$	47
default	$\frac{\frac{\mathrm{erf}(bx)b^2x^2}{2} - \frac{-\frac{e^{-b^2x^2}bx}{2} + \frac{\mathrm{erf}(bx)\sqrt{\pi}}{4}}{\sqrt{\pi}}}{b^2}$	47

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erf(b*x),x,method=_RETURNVERBOSE)
[Out] 1/b^2*(1/2*erf(b*x)*b^2*x^2-1/Pi^(1/2)*(-1/2*b*x/exp(b^2*x^2)+1/4*erf(b*x)*
Pi^(1/2)))
```

Maxima [**A**]
time = 0.25, size = 44, normalized size = 0.96

$$\frac{1}{2}\,x^2\,\mathrm{erf}\left(bx\right) + \frac{b\left(\frac{2\,xe^{\left(-b^2x^2\right)}}{b^2} - \frac{\sqrt{\pi}\,\mathrm{erf}\left(bx\right)}{b^3}\right)}{4\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(b*x),x, algorithm="maxima")
```

```
[Out] 1/2*x^2*erf(b*x) + 1/4*b*(2*x*e^(-b^2*x^2)/b^2 - sqrt(pi)*erf(b*x)/b^3)/sqr
t(pi)
```

Fricas [A]
time = 0.35, size = 42, normalized size = 0.91

$$\frac{2\sqrt{\pi}\,bxe^{\left(-b^2x^2\right)} - \left(\pi - 2\,\pi b^2x^2\right)\operatorname{erf}\left(bx\right)}{4\,\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(b*x),x, algorithm="fricas")
```

```
[Out] 1/4*(2*sqrt(pi)*b*x*e^(-b^2*x^2) - (pi - 2*pi*b^2*x^2)*erf(b*x))/(pi*b^2)
```

Sympy [A]
time = 0.18, size = 39, normalized size = 0.85

$$\begin{cases} \frac{x^2\operatorname{erf}\left(bx\right)}{2} + \frac{xe^{-b^2x^2}}{2\sqrt{\pi}\,b} - \frac{\operatorname{erf}\left(bx\right)}{4b^2} & \text{for}\ b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(b*x),x)
```

```
[Out] Piecewise((x**2*erf(b*x)/2 + x*exp(-b**2*x**2)/(2*sqrt(pi)*b) - erf(b*x)/(4
*b**2), Ne(b, 0)), (0, True))
```

Giac [A]
time = 0.40, size = 44, normalized size = 0.96

$$\frac{1}{2}\,x^2\operatorname{erf}\left(bx\right) + \frac{b\left(\frac{2\,xe^{\left(-b^2x^2\right)}}{b^2} + \frac{\sqrt{\pi}\operatorname{erf}\left(-bx\right)}{b^3}\right)}{4\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(b*x),x, algorithm="giac")
```

```
[Out] 1/2*x^2*erf(b*x) + 1/4*b*(2*x*e^(-b^2*x^2)/b^2 + sqrt(pi)*erf(-b*x)/b^3)/sq
rt(pi)
```

Mupad [B]
time = 0.17, size = 48, normalized size = 1.04

$$\frac{x^2\operatorname{erf}(b\,x)}{2} + \frac{b\operatorname{erfi}\left(x\,\sqrt{-b^2}\right)}{4\left(-b^2\right)^{3/2}} + \frac{x\,\mathrm{e}^{-b^2\,x^2}}{2\,b\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erf(b*x),x)
```

```
[Out] (x^2*erf(b*x))/2 + (b*erfi(x*(-b^2)^(1/2)))/(4*(-b^2)^(3/2)) + (x*exp(-b^2*
x^2))/(2*b*pi^(1/2))
```

3.4 $\int \frac{\mathbf{Erf}(bx)}{x}\,dx$

Optimal. Leaf size=32

$$\frac{2bx\,{}_2F_2\left(\frac{1}{2},\frac{1}{2};\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}$$

```
[Out] 2*b*x*hypergeom([1/2, 1/2],[3/2, 3/2],-b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.01, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = $\{6493\}$

$$\frac{2bx\,{}_2F_2\left(\frac{1}{2},\frac{1}{2};\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]/x,x]
[Out] (2*b*x*HypergeometricPFQ[{1/2, 1/2}, {3/2, 3/2}, -(b^2*x^2)])/Sqrt[Pi]
```

Rule 6493

```
Int[Erf[(b_.)*(x_)]/(x_), x_Symbol] :> Simp[2*b*(x/Sqrt[Pi])*Hypergeometric
PFQ[{1/2, 1/2}, {3/2, 3/2}, (-b^2)*x^2], x] /; FreeQ[b, x]
```

Rubi steps

$$\int \frac{\text{erf}(bx)}{x}\,dx = \frac{2bx\,{}_2F_2\left(\frac{1}{2},\frac{1}{2};\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}$$

Mathematica [A]
time = 0.01, size = 32, normalized size = 1.00

$$\frac{2bx\,{}_2F_2\left(\frac{1}{2},\frac{1}{2};\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]/x,x]
[Out] (2*b*x*HypergeometricPFQ[{1/2, 1/2}, {3/2, 3/2}, -(b^2*x^2)])/Sqrt[Pi]
```

Maple [A]
time = 0.19, size = 23, normalized size = 0.72

method	result	size
meijerg	$\frac{2bx \operatorname{hypergeom}\left(\left[\frac{1}{2},\frac{1}{2}\right],\left[\frac{3}{2},\frac{3}{2}\right],-b^2x^2\right)}{\sqrt{\pi}}$	23

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/x,x,method=_RETURNVERBOSE)
[Out] 2*b*x*hypergeom([1/2,1/2],[3/2,3/2],-b^2*x^2)/Pi^(1/2)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x,x, algorithm="maxima")
[Out] integrate(erf(b*x)/x, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x,x, algorithm="fricas")
[Out] integral(erf(b*x)/x, x)
```

Sympy [A]
time = 0.29, size = 26, normalized size = 0.81

$$\frac{2bx\,{}_2F_2\left(\begin{matrix}\frac{1}{2},\frac{1}{2}\\ \frac{3}{2},\frac{3}{2}\end{matrix}\middle|\,-b^2x^2\right)}{\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x,x)
[Out] 2*b*x*hyper((1/2, 1/2), (3/2, 3/2), -b**2*x**2)/sqrt(pi)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)/x, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{\operatorname{erf}(b\,x)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/x,x)
```

```
[Out] int(erf(b*x)/x, x)
```

3.5 $\int \frac{\mathbf{Erf}(bx)}{x^3}\,dx$

Optimal. Leaf size=42

$$-\frac{be^{-b^2x^2}}{\sqrt{\pi}\,x}-b^2\text{Erf}(bx)-\frac{\text{Erf}(bx)}{2x^2}$$

```
[Out] -b^2*erf(b*x)-1/2*erf(b*x)/x^2-b/exp(b^2*x^2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.02, antiderivative size = 42, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6496, 2245, 2236}

$$b^2(-\text{Erf}(bx))-\frac{be^{-b^2x^2}}{\sqrt{\pi}\,x}-\frac{\text{Erf}(bx)}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]/x^3,x]
```

```
[Out] -(b/(E^(b^2*x^2)*Sqrt[Pi]*x)) - b^2*Erf[b*x] - Erf[b*x]/(2*x^2)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6496

```
Int[Erf[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(
c + d*x)^(m + 1)*(Erf[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(m
+ 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d, m
}, x] && NeQ[m, -1]
```

Rubi steps

$$\int \frac{\operatorname{erf}(bx)}{x^3}\,dx = -\frac{\operatorname{erf}(bx)}{2x^2} + \frac{b\int \frac{e^{-b^2x^2}}{x^2}\,dx}{\sqrt{\pi}}$$
$$= -\frac{be^{-b^2x^2}}{\sqrt{\pi}\,x} - \frac{\operatorname{erf}(bx)}{2x^2} - \frac{(2b^3)\int e^{-b^2x^2}\,dx}{\sqrt{\pi}}$$
$$= -\frac{be^{-b^2x^2}}{\sqrt{\pi}\,x} - b^2\operatorname{erf}(bx) - \frac{\operatorname{erf}(bx)}{2x^2}$$

Mathematica [A]
time = 0.03, size = 42, normalized size = 1.00

$$-\frac{be^{-b^2x^2}}{\sqrt{\pi}\,x} - b^2\operatorname{Erf}(bx) - \frac{\operatorname{Erf}(bx)}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]/x^3,x]
```

```
[Out] -(b/(E^(b^2*x^2)*Sqrt[Pi]*x)) - b^2*Erf[b*x] - Erf[b*x]/(2*x^2)
```

Maple [A]
time = 0.20, size = 50, normalized size = 1.19

method	result	size
derivativedivides	$b^2\left(-\frac{\operatorname{erf}(bx)}{2b^2x^2}+\frac{-\frac{e^{-b^2x^2}}{xb}-\operatorname{erf}(bx)\sqrt{\pi}}{\sqrt{\pi}}\right)$	50
default	$b^2\left(-\frac{\operatorname{erf}(bx)}{2b^2x^2}+\frac{-\frac{e^{-b^2x^2}}{xb}-\operatorname{erf}(bx)\sqrt{\pi}}{\sqrt{\pi}}\right)$	50
meijerg	$\frac{b^2\left(-\frac{2\,e^{-b^2x^2}}{xb}-\frac{(2b^2x^2+1)\operatorname{erf}(bx)\sqrt{\pi}}{x^2b^2}\right)}{2\sqrt{\pi}}$	52

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/x^3,x,method=_RETURNVERBOSE)
```

```
[Out] b^2*(-1/2*erf(b*x)/b^2/x^2+1/Pi^(1/2)*(-1/exp(b^2*x^2)/b/x-erf(b*x)*Pi^(1/2
)))
```

Maxima [A]
time = 0.29, size = 35, normalized size = 0.83

$$-\frac{b^2\sqrt{x^2}\,\Gamma\left(-\frac{1}{2},b^2x^2\right)}{2\sqrt{\pi}\,x} - \frac{\operatorname{erf}(bx)}{2\,x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^3,x, algorithm="maxima")
[Out] -1/2*b^2*sqrt(x^2)*gamma(-1/2, b^2*x^2)/(sqrt(pi)*x) - 1/2*erf(b*x)/x^2
```

Fricas [A]
time = 0.36, size = 41, normalized size = 0.98

$$-\frac{2\sqrt{\pi}\,bxe^{(-b^2x^2)} + (\pi + 2\,\pi b^2x^2)\operatorname{erf}(bx)}{2\,\pi x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^3,x, algorithm="fricas")
[Out] -1/2*(2*sqrt(pi)*b*x*e^(-b^2*x^2) + (pi + 2*pi*b^2*x^2)*erf(b*x))/(pi*x^2)
```

Sympy [A]
time = 0.21, size = 36, normalized size = 0.86

$$-b^2\operatorname{erf}(bx) - \frac{be^{-b^2x^2}}{\sqrt{\pi}\,x} - \frac{\operatorname{erf}(bx)}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x**3,x)
[Out] -b**2*erf(b*x) - b*exp(-b**2*x**2)/(sqrt(pi)*x) - erf(b*x)/(2*x**2)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^3,x, algorithm="giac")
[Out] integrate(erf(b*x)/x^3, x)
```

Mupad [B]
time = 0.15, size = 67, normalized size = 1.60

$$\frac{b\,\mathrm{erfc}\left(\sqrt{b^2\,x^2}\right)\,\sqrt{b^2\,x^2}}{x} - \frac{b\,\sqrt{b^2\,x^2}}{x} - \frac{b\,\mathrm{e}^{-b^2\,x^2}}{x\,\sqrt{\pi}} - \frac{\mathrm{erf}(b\,x)}{2\,x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/x^3,x)
[Out] (b*erfc((b^2*x^2)^(1/2))*(b^2*x^2)^(1/2))/x - (b*(b^2*x^2)^(1/2))/x - (b*ex
p(-b^2*x^2))/(x*pi^(1/2)) - erf(b*x)/(2*x^2)
```

3.6 $\int \frac{\mathbf{Erf}(bx)}{x^5} \, dx$

Optimal. Leaf size=71

$$-\frac{be^{-b^2x^2}}{6\sqrt{\pi}\,x^3}+\frac{b^3e^{-b^2x^2}}{3\sqrt{\pi}\,x}+\frac{1}{3}b^4\mathrm{Erf}(bx)-\frac{\mathrm{Erf}(bx)}{4x^4}$$

```
[Out] 1/3*b^4*erf(b*x)-1/4*erf(b*x)/x^4-1/6*b/exp(b^2*x^2)/x^3/Pi^(1/2)+1/3*b^3/e
xp(b^2*x^2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.04, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6496, 2245, 2236}

$$\frac{1}{3}b^4\mathrm{Erf}(bx)-\frac{be^{-b^2x^2}}{6\sqrt{\pi}\,x^3}+\frac{b^3e^{-b^2x^2}}{3\sqrt{\pi}\,x}-\frac{\mathrm{Erf}(bx)}{4x^4}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]/x^5,x]
```

```
[Out] -1/6*b/(E^(b^2*x^2)*Sqrt[Pi]*x^3) + b^3/(3*E^(b^2*x^2)*Sqrt[Pi]*x) + (b^4*E
rf[b*x])/3 - Erf[b*x]/(4*x^4)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6496

```
Int[Erf[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(
c + d*x)^(m + 1)*(Erf[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(m
+ 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d, m
}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int \frac{\operatorname{erf}(bx)}{x^5}\,dx &= -\frac{\operatorname{erf}(bx)}{4x^4}+\frac{b\int \frac{e^{-b^2x^2}}{x^4}\,dx}{2\sqrt{\pi}}\\
&= -\frac{be^{-b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{\operatorname{erf}(bx)}{4x^4}-\frac{b^3\int \frac{e^{-b^2x^2}}{x^2}\,dx}{3\sqrt{\pi}}\\
&= -\frac{be^{-b^2x^2}}{6\sqrt{\pi}\,x^3}+\frac{b^3e^{-b^2x^2}}{3\sqrt{\pi}\,x}-\frac{\operatorname{erf}(bx)}{4x^4}+\frac{(2b^5)\int e^{-b^2x^2}\,dx}{3\sqrt{\pi}}\\
&= -\frac{be^{-b^2x^2}}{6\sqrt{\pi}\,x^3}+\frac{b^3e^{-b^2x^2}}{3\sqrt{\pi}\,x}+\frac{1}{3}b^4\operatorname{erf}(bx)-\frac{\operatorname{erf}(bx)}{4x^4}
\end{aligned}$$

Mathematica [A]
time = 0.01, size = 63, normalized size = 0.89

$$e^{-b^2x^2}\left(-\frac{b}{6\sqrt{\pi}\,x^3}+\frac{b^3}{3\sqrt{\pi}\,x}\right)+\frac{1}{3}b^4\operatorname{Erf}(bx)-\frac{\operatorname{Erf}(bx)}{4x^4}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]/x^5,x]
```

```
[Out] (-1/6*b/(Sqrt[Pi]*x^3) + b^3/(3*Sqrt[Pi]*x))/E^(b^2*x^2) + (b^4*Erf[b*x])/3
 - Erf[b*x]/(4*x^4)
```

Maple [A]
time = 0.20, size = 69, normalized size = 0.97

method	result	size
meijerg	$\frac{b^4\left(-\frac{4\left(-\frac{b^2x^2}{2}+\frac{1}{4}\right)e^{-b^2x^2}}{3x^3b^3}-\frac{\left(-4b^4x^4+3\right)\operatorname{erf}(bx)\sqrt{\pi}}{6x^4b^4}\right)}{2\sqrt{\pi}}$	62
derivativedivides	$b^4\left(-\frac{\operatorname{erf}(bx)}{4b^4x^4}+\frac{-\frac{e^{-b^2x^2}}{3b^3x^3}+\frac{2e^{-b^2x^2}}{3xb}+\frac{2\operatorname{erf}(bx)\sqrt{\pi}}{3}}{2\sqrt{\pi}}\right)$	69
default	$b^4\left(-\frac{\operatorname{erf}(bx)}{4b^4x^4}+\frac{-\frac{e^{-b^2x^2}}{3b^3x^3}+\frac{2e^{-b^2x^2}}{3xb}+\frac{2\operatorname{erf}(bx)\sqrt{\pi}}{3}}{2\sqrt{\pi}}\right)$	69

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/x^5,x,method=_RETURNVERBOSE)
```

```
[Out] b^4*(-1/4*erf(b*x)/b^4/x^4+1/2/Pi^(1/2)*(-1/3/exp(b^2*x^2)/b^3/x^3+2/3/exp(
b^2*x^2)/b/x+2/3*erf(b*x)*Pi^(1/2)))
```

Maxima [A]
time = 0.29, size = 35, normalized size = 0.49

$$-\frac{b^4 (x^2)^{\frac{3}{2}} \Gamma\left(-\frac{3}{2}, b^2 x^2\right)}{4\sqrt{\pi}\, x^3} - \frac{\operatorname{erf}(bx)}{4\, x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^5,x, algorithm="maxima")
```

```
[Out] -1/4*b^4*(x^2)^(3/2)*gamma(-3/2, b^2*x^2)/(sqrt(pi)*x^3) - 1/4*erf(b*x)/x^4
```

Fricas [A]
time = 0.38, size = 55, normalized size = 0.77

$$\frac{2\sqrt{\pi}\,(2\, b^3 x^3 - bx)e^{(-b^2 x^2)} - (3\,\pi - 4\,\pi b^4 x^4) \operatorname{erf}(bx)}{12\,\pi x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^5,x, algorithm="fricas")
```

```
[Out] 1/12*(2*sqrt(pi)*(2*b^3*x^3 - b*x)*e^(-b^2*x^2) - (3*pi - 4*pi*b^4*x^4)*erf
(b*x))/(pi*x^4)
```

Sympy [A]
time = 0.36, size = 60, normalized size = 0.85

$$\frac{b^4 \operatorname{erf}(bx)}{3} + \frac{b^3 e^{-b^2 x^2}}{3\sqrt{\pi}\, x} - \frac{b e^{-b^2 x^2}}{6\sqrt{\pi}\, x^3} - \frac{\operatorname{erf}(bx)}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x**5,x)
```

```
[Out] b**4*erf(b*x)/3 + b**3*exp(-b**2*x**2)/(3*sqrt(pi)*x) - b*exp(-b**2*x**2)/(
6*sqrt(pi)*x**3) - erf(b*x)/(4*x**4)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^5,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)/x^5, x)
```

Mupad [B]
time = 0.11, size = 88, normalized size = 1.24

$$\frac{b\,{\left(b^2\,x^2\right)}^{3/2}}{3\,x^3}-\frac{\mathrm{erf}\left(b\,x\right)}{4\,x^4}+\frac{b^3\,{\mathrm{e}}^{-b^2\,x^2}}{3\,x\,\sqrt{\pi }}-\frac{b\,{\mathrm{e}}^{-b^2\,x^2}}{6\,x^3\,\sqrt{\pi }}-\frac{b\,\mathrm{erfc}\left(\sqrt{b^2\,x^2}\right)\,{\left(b^2\,x^2\right)}^{3/2}}{3\,x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/x^5,x)
```

```
[Out] (b*(b^2*x^2)^(3/2))/(3*x^3) - erf(b*x)/(4*x^4) + (b^3*exp(-b^2*x^2))/(3*x*p
i^(1/2)) - (b*exp(-b^2*x^2))/(6*x^3*pi^(1/2)) - (b*erfc((b^2*x^2)^(1/2))*(b
^2*x^2)^(3/2))/(3*x^3)
```

3.7 $\int \frac{\mathbf{Erf}(bx)}{x^7}\,dx$

Optimal. Leaf size=96

$$-\frac{be^{-b^2x^2}}{15\sqrt{\pi}\,x^5}+\frac{2b^3e^{-b^2x^2}}{45\sqrt{\pi}\,x^3}-\frac{4b^5e^{-b^2x^2}}{45\sqrt{\pi}\,x}-\frac{4}{45}b^6\mathrm{Erf}(bx)-\frac{\mathrm{Erf}(bx)}{6x^6}$$

```
[Out] -4/45*b^6*erf(b*x)-1/6*erf(b*x)/x^6-1/15*b/exp(b^2*x^2)/x^5/Pi^(1/2)+2/45*b
^3/exp(b^2*x^2)/x^3/Pi^(1/2)-4/45*b^5/exp(b^2*x^2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.06, antiderivative size = 96, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6496, 2245, 2236}

$$-\frac{4}{45}b^6\mathrm{Erf}(bx)-\frac{be^{-b^2x^2}}{15\sqrt{\pi}\,x^5}-\frac{4b^5e^{-b^2x^2}}{45\sqrt{\pi}\,x}+\frac{2b^3e^{-b^2x^2}}{45\sqrt{\pi}\,x^3}-\frac{\mathrm{Erf}(bx)}{6x^6}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]/x^7,x]
```

```
[Out] -1/15*b/(E^(b^2*x^2)*Sqrt[Pi]*x^5) + (2*b^3)/(45*E^(b^2*x^2)*Sqrt[Pi]*x^3)
- (4*b^5)/(45*E^(b^2*x^2)*Sqrt[Pi]*x) - (4*b^6*Erf[b*x])/45 - Erf[b*x]/(6*x
^6)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6496

```
Int[Erf[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(
c + d*x)^(m + 1)*(Erf[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(m
+ 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d, m
```

```
}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int \frac{\operatorname{erf}(bx)}{x^7}\,dx &= -\frac{\operatorname{erf}(bx)}{6x^6}+\frac{b\int \frac{e^{-b^2x^2}}{x^6}\,dx}{3\sqrt{\pi}}\\
&= -\frac{be^{-b^2x^2}}{15\sqrt{\pi}\,x^5}-\frac{\operatorname{erf}(bx)}{6x^6}-\frac{(2b^3)\int \frac{e^{-b^2x^2}}{x^4}\,dx}{15\sqrt{\pi}}\\
&= -\frac{be^{-b^2x^2}}{15\sqrt{\pi}\,x^5}+\frac{2b^3e^{-b^2x^2}}{45\sqrt{\pi}\,x^3}-\frac{\operatorname{erf}(bx)}{6x^6}+\frac{(4b^5)\int \frac{e^{-b^2x^2}}{x^2}\,dx}{45\sqrt{\pi}}\\
&= -\frac{be^{-b^2x^2}}{15\sqrt{\pi}\,x^5}+\frac{2b^3e^{-b^2x^2}}{45\sqrt{\pi}\,x^3}-\frac{4b^5e^{-b^2x^2}}{45\sqrt{\pi}\,x}-\frac{\operatorname{erf}(bx)}{6x^6}-\frac{(8b^7)\int e^{-b^2x^2}\,dx}{45\sqrt{\pi}}\\
&= -\frac{be^{-b^2x^2}}{15\sqrt{\pi}\,x^5}+\frac{2b^3e^{-b^2x^2}}{45\sqrt{\pi}\,x^3}-\frac{4b^5e^{-b^2x^2}}{45\sqrt{\pi}\,x}-\frac{4}{45}b^6\operatorname{erf}(bx)-\frac{\operatorname{erf}(bx)}{6x^6}
\end{aligned}$$

Mathematica [A]
time = 0.02, size = 73, normalized size = 0.76

$$\frac{e^{-b^2x^2}\left(-6bx+4b^3x^3-8b^5x^5-e^{b^2x^2}\sqrt{\pi}\,(15+8b^6x^6)\operatorname{Erf}(bx)\right)}{90\sqrt{\pi}\,x^6}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]/x^7,x]
[Out] (-6*b*x + 4*b^3*x^3 - 8*b^5*x^5 - E^(b^2*x^2)*Sqrt[Pi]*(15 + 8*b^6*x^6)*Erf
[b*x])/(90*E^(b^2*x^2)*Sqrt[Pi]*x^6)
```

Maple [A]
time = 0.23, size = 87, normalized size = 0.91

method	result	size
meijerg	$\dfrac{b^6\left(-\frac{4\left(\frac{2}{9}b^4x^4-\frac{1}{9}b^2x^2+\frac{1}{6}\right)e^{-b^2x^2}}{5x^5b^5}-\frac{\left(8b^6x^6+15\right)\operatorname{erf}(bx)\sqrt{\pi}}{45x^6b^6}\right)}{2\sqrt{\pi}}$	70
derivativedivides	$b^6\left(-\frac{\operatorname{erf}(bx)}{6b^6x^6}+\frac{-\frac{e^{-b^2x^2}}{5b^5x^5}+\frac{2\,e^{-b^2x^2}}{15b^3x^3}-\frac{4\,e^{-b^2x^2}}{15xb}-\frac{4\operatorname{erf}(bx)\sqrt{\pi}}{15}}{3\sqrt{\pi}}\right)$	87

default	$b^6\left(-\frac{\operatorname{erf}(bx)}{6b^6x^6}+\frac{-\frac{e^{-b^2x^2}}{5b^5x^5}+\frac{2\,e^{-b^2x^2}}{15b^3x^3}-\frac{4\,e^{-b^2x^2}}{15xb}-\frac{4\operatorname{erf}(bx)\sqrt{\pi}}{15}}{3\sqrt{\pi}}\right)$	87

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/x^7,x,method=_RETURNVERBOSE)
```

```
[Out] b^6*(-1/6*erf(b*x)/b^6/x^6+1/3/Pi^(1/2)*(-1/5/exp(b^2*x^2)/b^5/x^5+2/15/exp
(b^2*x^2)/b^3/x^3-4/15/exp(b^2*x^2)/b/x-4/15*erf(b*x)*Pi^(1/2)))
```

Maxima [A]
time = 0.29, size = 35, normalized size = 0.36

$$-\frac{b^6(x^2)^{\frac{5}{2}}\Gamma\left(-\frac{5}{2},b^2x^2\right)}{6\sqrt{\pi}\,x^5}-\frac{\operatorname{erf}(bx)}{6\,x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^7,x, algorithm="maxima")
```

```
[Out] -1/6*b^6*(x^2)^(5/2)*gamma(-5/2, b^2*x^2)/(sqrt(pi)*x^5) - 1/6*erf(b*x)/x^6
```

Fricas [A]
time = 0.34, size = 62, normalized size = 0.65

$$-\frac{2\sqrt{\pi}\,(4\,b^5x^5-2\,b^3x^3+3\,bx)e^{(-b^2x^2)}+(15\,\pi+8\,\pi b^6x^6)\operatorname{erf}(bx)}{90\,\pi x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^7,x, algorithm="fricas")
```

```
[Out] -1/90*(2*sqrt(pi)*(4*b^5*x^5 - 2*b^3*x^3 + 3*b*x)*e^(-b^2*x^2) + (15*pi + 8
*pi*b^6*x^6)*erf(b*x))/(pi*x^6)
```

Sympy [A]
time = 0.65, size = 87, normalized size = 0.91

$$-\frac{4b^6\operatorname{erf}(bx)}{45}-\frac{4b^5e^{-b^2x^2}}{45\sqrt{\pi}\,x}+\frac{2b^3e^{-b^2x^2}}{45\sqrt{\pi}\,x^3}-\frac{be^{-b^2x^2}}{15\sqrt{\pi}\,x^5}-\frac{\operatorname{erf}(bx)}{6x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x**7,x)
```

```
[Out] -4*b**6*erf(b*x)/45 - 4*b**5*exp(-b**2*x**2)/(45*sqrt(pi)*x) + 2*b**3*exp(-
b**2*x**2)/(45*sqrt(pi)*x**3) - b*exp(-b**2*x**2)/(15*sqrt(pi)*x**5) - erf(
b*x)/(6*x**6)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^7,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)/x^7, x)
```

Mupad [B]
time = 0.16, size = 113, normalized size = 1.18

$$-\frac{\mathrm{erf}(b\,x)}{6\,x^6}-\frac{3\,b\,\mathrm{e}^{-b^2\,x^2}-2\,b^3\,x^2\,\mathrm{e}^{-b^2\,x^2}+4\,b^5\,x^4\,\mathrm{e}^{-b^2\,x^2}+4\,b^5\,\sqrt{\pi}\,\sqrt{b^2}\,{\left(x^2\right)}^{5/2}-4\,b^5\,\sqrt{\pi}\,\mathrm{erfc}\left(\sqrt{b^2}\,\sqrt{x^2}\right)\,\sqrt{b^2}\,{\left(x^2\right)}^{5/2}}{45\,x^5\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/x^7,x)
```

```
[Out] - erf(b*x)/(6*x^6) - (3*b*exp(-b^2*x^2) - 2*b^3*x^2*exp(-b^2*x^2) + 4*b^5*x
^4*exp(-b^2*x^2) + 4*b^5*pi^(1/2)*(b^2)^(1/2)*(x^2)^(5/2) - 4*b^5*pi^(1/2)*
erfc((b^2)^(1/2)*(x^2)^(1/2))*(b^2)^(1/2)*(x^2)^(5/2))/(45*x^5*pi^(1/2))
```

3.8 $\int x^6 \mathbf{Erf}(bx)\, dx$

Optimal. Leaf size=109

$$\frac{6e^{-b^2x^2}}{7b^7\sqrt{\pi}}+\frac{6e^{-b^2x^2}x^2}{7b^5\sqrt{\pi}}+\frac{3e^{-b^2x^2}x^4}{7b^3\sqrt{\pi}}+\frac{e^{-b^2x^2}x^6}{7b\sqrt{\pi}}+\frac{1}{7}x^7\mathrm{Erf}(bx)$$

```
[Out] 1/7*x^7*erf(b*x)+6/7/b^7/exp(b^2*x^2)/Pi^(1/2)+6/7*x^2/b^5/exp(b^2*x^2)/Pi^
(1/2)+3/7*x^4/b^3/exp(b^2*x^2)/Pi^(1/2)+1/7*x^6/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.07, antiderivative size = 109, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6496, 2243, 2240}

$$\frac{x^6e^{-b^2x^2}}{7\sqrt{\pi}\,b}+\frac{6e^{-b^2x^2}}{7\sqrt{\pi}\,b^7}+\frac{6x^2e^{-b^2x^2}}{7\sqrt{\pi}\,b^5}+\frac{3x^4e^{-b^2x^2}}{7\sqrt{\pi}\,b^3}+\frac{1}{7}x^7\mathrm{Erf}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x^6*Erf[b*x],x]
```

```
[Out] 6/(7*b^7*E^(b^2*x^2)*Sqrt[Pi]) + (6*x^2)/(7*b^5*E^(b^2*x^2)*Sqrt[Pi]) + (3*
x^4)/(7*b^3*E^(b^2*x^2)*Sqrt[Pi]) + x^6/(7*b*E^(b^2*x^2)*Sqrt[Pi]) + (x^7*E
rf[b*x])/7
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6496

```
Int[Erf[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(
c + d*x)^(m + 1)*(Erf[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(m
+ 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d, m
```

```
}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int x^6 \operatorname{erf}(bx)\,dx &= \frac{1}{7}x^7\operatorname{erf}(bx) - \frac{(2b)\int e^{-b^2x^2}x^7\,dx}{7\sqrt{\pi}} \\
&= \frac{e^{-b^2x^2}x^6}{7b\sqrt{\pi}} + \frac{1}{7}x^7\operatorname{erf}(bx) - \frac{6\int e^{-b^2x^2}x^5\,dx}{7b\sqrt{\pi}} \\
&= \frac{3e^{-b^2x^2}x^4}{7b^3\sqrt{\pi}} + \frac{e^{-b^2x^2}x^6}{7b\sqrt{\pi}} + \frac{1}{7}x^7\operatorname{erf}(bx) - \frac{12\int e^{-b^2x^2}x^3\,dx}{7b^3\sqrt{\pi}} \\
&= \frac{6e^{-b^2x^2}x^2}{7b^5\sqrt{\pi}} + \frac{3e^{-b^2x^2}x^4}{7b^3\sqrt{\pi}} + \frac{e^{-b^2x^2}x^6}{7b\sqrt{\pi}} + \frac{1}{7}x^7\operatorname{erf}(bx) - \frac{12\int e^{-b^2x^2}x\,dx}{7b^5\sqrt{\pi}} \\
&= \frac{6e^{-b^2x^2}}{7b^7\sqrt{\pi}} + \frac{6e^{-b^2x^2}x^2}{7b^5\sqrt{\pi}} + \frac{3e^{-b^2x^2}x^4}{7b^3\sqrt{\pi}} + \frac{e^{-b^2x^2}x^6}{7b\sqrt{\pi}} + \frac{1}{7}x^7\operatorname{erf}(bx)
\end{aligned}
$$

Mathematica [A]
time = 0.01, size = 72, normalized size = 0.66

$$\frac{e^{-b^2x^2}\left(6+6b^2x^2+3b^4x^4+b^6x^6+b^7e^{b^2x^2}\sqrt{\pi}\,x^7\operatorname{Erf}(bx)\right)}{7b^7\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^6*Erf[b*x],x]
```

```
[Out] (6 + 6*b^2*x^2 + 3*b^4*x^4 + b^6*x^6 + b^7*E^(b^2*x^2)*Sqrt[Pi]*x^7*Erf[b*x
])/(7*b^7*E^(b^2*x^2)*Sqrt[Pi])
```

Maple [A]
time = 0.23, size = 90, normalized size = 0.83

method	result	size
meijerg	$\frac{-\frac{12}{7}+\frac{\left(4b^6x^6+12b^4x^4+24b^2x^2+24\right)e^{-b^2x^2}}{14}+\frac{2x^7b^7\operatorname{erf}(bx)\sqrt{\pi}}{7}}{2b^7\sqrt{\pi}}$	63
derivativedivides	$\frac{\frac{\operatorname{erf}(bx)b^7x^7}{7}-\frac{2\left(-\frac{e^{-b^2x^2}b^6x^6}{2}-\frac{3b^4x^4e^{-b^2x^2}}{2}-3b^2x^2e^{-b^2x^2}-3e^{-b^2x^2}\right)}{7\sqrt{\pi}}}{b^7}$	90

default	$\frac{\frac{\operatorname{erf}(bx)b^7x^7}{7}-\frac{2\left(-\frac{e^{-b^2x^2}b^6x^6}{2}-\frac{3b^4x^4e^{-b^2x^2}}{2}-3b^2x^2e^{-b^2x^2}-3\,e^{-b^2x^2}\right)}{7\sqrt{\pi}}}{b^7}$	90

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^6*erf(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b^7*(1/7*erf(b*x)*b^7*x^7-2/7/Pi^(1/2)*(-1/2/exp(b^2*x^2)*b^6*x^6-3/2*b^4
*x^4/exp(b^2*x^2)-3*b^2*x^2/exp(b^2*x^2)-3/exp(b^2*x^2)))
```

Maxima [A]
time = 0.26, size = 52, normalized size = 0.48

$$\frac{1}{7}\,x^7\,\operatorname{erf}\left(bx\right)+\frac{\left(b^6x^6+3\,b^4x^4+6\,b^2x^2+6\right)e^{\left(-b^2x^2\right)}}{7\,\sqrt{\pi}\,b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^6*erf(b*x),x, algorithm="maxima")
```

```
[Out] 1/7*x^7*erf(b*x) + 1/7*(b^6*x^6 + 3*b^4*x^4 + 6*b^2*x^2 + 6)*e^(-b^2*x^2)/(
sqrt(pi)*b^7)
```

Fricas [A]
time = 0.35, size = 59, normalized size = 0.54

$$\frac{\pi b^7x^7\operatorname{erf}\left(bx\right)+\sqrt{\pi}\left(b^6x^6+3\,b^4x^4+6\,b^2x^2+6\right)e^{\left(-b^2x^2\right)}}{7\,\pi b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^6*erf(b*x),x, algorithm="fricas")
```

```
[Out] 1/7*(pi*b^7*x^7*erf(b*x) + sqrt(pi)*(b^6*x^6 + 3*b^4*x^4 + 6*b^2*x^2 + 6)*e
^(-b^2*x^2))/(pi*b^7)
```

Sympy [A]
time = 0.72, size = 99, normalized size = 0.91

$$\begin{cases}\frac{x^7\operatorname{erf}\left(bx\right)}{7}+\frac{x^6e^{-b^2x^2}}{7\sqrt{\pi}\,b}+\frac{3x^4e^{-b^2x^2}}{7\sqrt{\pi}\,b^3}+\frac{6x^2e^{-b^2x^2}}{7\sqrt{\pi}\,b^5}+\frac{6e^{-b^2x^2}}{7\sqrt{\pi}\,b^7} & \text{for}\ b\neq 0\\ 0 & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**6*erf(b*x),x)
```

```
[Out] Piecewise((x**7*erf(b*x)/7 + x**6*exp(-b**2*x**2)/(7*sqrt(pi)*b) + 3*x**4*e
xp(-b**2*x**2)/(7*sqrt(pi)*b**3) + 6*x**2*exp(-b**2*x**2)/(7*sqrt(pi)*b**5)
 + 6*exp(-b**2*x**2)/(7*sqrt(pi)*b**7), Ne(b, 0)), (0, True))
```

Giac [A]
time = 0.41, size = 52, normalized size = 0.48

$$\frac{1}{7}\,x^{7}\,\mathrm{erf}\left(bx\right) + \frac{\left(b^{6}x^{6} + 3\,b^{4}x^{4} + 6\,b^{2}x^{2} + 6\right)e^{\left(-b^{2}x^{2}\right)}}{7\,\sqrt{\pi}\,b^{7}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^6*erf(b*x),x, algorithm="giac")
```

```
[Out] 1/7*x^7*erf(b*x) + 1/7*(b^6*x^6 + 3*b^4*x^4 + 6*b^2*x^2 + 6)*e^(-b^2*x^2)/(
sqrt(pi)*b^7)
```

Mupad [B]
time = 0.14, size = 52, normalized size = 0.48

$$\frac{x^{7}\,\mathrm{erf}(b\,x)}{7} + \frac{\mathrm{e}^{-b^{2}\,x^{2}}\,\left(b^{6}\,x^{6} + 3\,b^{4}\,x^{4} + 6\,b^{2}\,x^{2} + 6\right)}{7\,b^{7}\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^6*erf(b*x),x)
```

```
[Out] (x^7*erf(b*x))/7 + (exp(-b^2*x^2)*(6*b^2*x^2 + 3*b^4*x^4 + b^6*x^6 + 6))/(7
*b^7*pi^(1/2))
```

3.9 $\int x^4 \mathbf{Erf}(bx)\, dx$

Optimal. Leaf size=84

$$\frac{2e^{-b^2x^2}}{5b^5\sqrt{\pi}}+\frac{2e^{-b^2x^2}x^2}{5b^3\sqrt{\pi}}+\frac{e^{-b^2x^2}x^4}{5b\sqrt{\pi}}+\frac{1}{5}x^5\mathrm{Erf}(bx)$$

```
[Out] 1/5*x^5*erf(b*x)+2/5/b^5/exp(b^2*x^2)/Pi^(1/2)+2/5*x^2/b^3/exp(b^2*x^2)/Pi^
(1/2)+1/5*x^4/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.05, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6496, 2243, 2240}

$$\frac{x^4e^{-b^2x^2}}{5\sqrt{\pi}\,b}+\frac{2e^{-b^2x^2}}{5\sqrt{\pi}\,b^5}+\frac{2x^2e^{-b^2x^2}}{5\sqrt{\pi}\,b^3}+\frac{1}{5}x^5\mathrm{Erf}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x^4*Erf[b*x],x]
```

```
[Out] 2/(5*b^5*E^(b^2*x^2)*Sqrt[Pi]) + (2*x^2)/(5*b^3*E^(b^2*x^2)*Sqrt[Pi]) + x^4
/(5*b*E^(b^2*x^2)*Sqrt[Pi]) + (x^5*Erf[b*x])/5
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6496

```
Int[Erf[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(
c + d*x)^(m + 1)*(Erf[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(m
+ 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d, m
}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int x^4\text{erf}(bx)\,dx &= \frac{1}{5}x^5\text{erf}(bx) - \frac{(2b)\int e^{-b^2x^2}x^5\,dx}{5\sqrt{\pi}}\\
&= \frac{e^{-b^2x^2}x^4}{5b\sqrt{\pi}} + \frac{1}{5}x^5\text{erf}(bx) - \frac{4\int e^{-b^2x^2}x^3\,dx}{5b\sqrt{\pi}}\\
&= \frac{2e^{-b^2x^2}x^2}{5b^3\sqrt{\pi}} + \frac{e^{-b^2x^2}x^4}{5b\sqrt{\pi}} + \frac{1}{5}x^5\text{erf}(bx) - \frac{4\int e^{-b^2x^2}x\,dx}{5b^3\sqrt{\pi}}\\
&= \frac{2e^{-b^2x^2}}{5b^5\sqrt{\pi}} + \frac{2e^{-b^2x^2}x^2}{5b^3\sqrt{\pi}} + \frac{e^{-b^2x^2}x^4}{5b\sqrt{\pi}} + \frac{1}{5}x^5\text{erf}(bx)
\end{aligned}
$$

Mathematica [**A**]
time = 0.01, size = 66, normalized size = 0.79

$$e^{-b^2x^2}\left(\frac{2}{5b^5\sqrt{\pi}} + \frac{2x^2}{5b^3\sqrt{\pi}} + \frac{x^4}{5b\sqrt{\pi}}\right) + \frac{1}{5}x^5\text{Erf}(bx)$$

Antiderivative was successfully verified.

```
[In] Integrate[x^4*Erf[b*x],x]
```

```
[Out] (2/(5*b^5*Sqrt[Pi]) + (2*x^2)/(5*b^3*Sqrt[Pi]) + x^4/(5*b*Sqrt[Pi]))/E^(b^2
*x^2) + (x^5*Erf[b*x])/5
```

Maple [**A**]
time = 0.21, size = 72, normalized size = 0.86

method	result	size
meijerg	$\frac{-\frac{4}{5}+\frac{2\left(3b^4x^4+6b^2x^2+6\right)e^{-b^2x^2}}{15}+\frac{2b^5x^5\,\text{erf}(bx)\sqrt{\pi}}{5}}{2b^5\sqrt{\pi}}$	55
derivativedivides	$\frac{\frac{\text{erf}(bx)b^5x^5}{5}-\frac{2\left(-\frac{b^4x^4e^{-b^2x^2}}{2}-b^2x^2e^{-b^2x^2}-e^{-b^2x^2}\right)}{5\sqrt{\pi}}}{b^5}$	72
default	$\frac{\frac{\text{erf}(bx)b^5x^5}{5}-\frac{2\left(-\frac{b^4x^4e^{-b^2x^2}}{2}-b^2x^2e^{-b^2x^2}-e^{-b^2x^2}\right)}{5\sqrt{\pi}}}{b^5}$	72

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erf(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b^5*(1/5*erf(b*x)*b^5*x^5-2/5/Pi^(1/2)*(-1/2*b^4*x^4/exp(b^2*x^2)-b^2*x^2
/exp(b^2*x^2)-1/exp(b^2*x^2)))
```

Maxima [A]
time = 0.26, size = 44, normalized size = 0.52

$$\frac{1}{5}\,x^5\operatorname{erf}\left(bx\right)+\frac{\left(b^4x^4+2\,b^2x^2+2\right)e^{\left(-b^2x^2\right)}}{5\,\sqrt{\pi}\,b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erf(b*x),x, algorithm="maxima")
```

```
[Out] 1/5*x^5*erf(b*x) + 1/5*(b^4*x^4 + 2*b^2*x^2 + 2)*e^(-b^2*x^2)/(sqrt(pi)*b^5
)
```

Fricas [A]
time = 0.35, size = 51, normalized size = 0.61

$$\frac{\pi b^5x^5\operatorname{erf}\left(bx\right)+\sqrt{\pi}\,\left(b^4x^4+2\,b^2x^2+2\right)e^{\left(-b^2x^2\right)}}{5\,\pi b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erf(b*x),x, algorithm="fricas")
```

```
[Out] 1/5*(pi*b^5*x^5*erf(b*x) + sqrt(pi)*(b^4*x^4 + 2*b^2*x^2 + 2)*e^(-b^2*x^2))
/(pi*b^5)
```

Sympy [A]
time = 0.38, size = 75, normalized size = 0.89

$$\begin{cases}\frac{x^5\operatorname{erf}\left(bx\right)}{5}+\frac{x^4e^{-b^2x^2}}{5\sqrt{\pi}\,b}+\frac{2x^2e^{-b^2x^2}}{5\sqrt{\pi}\,b^3}+\frac{2e^{-b^2x^2}}{5\sqrt{\pi}\,b^5} & \text{for}\ b\neq 0\\ 0 & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4*erf(b*x),x)
```

```
[Out] Piecewise((x**5*erf(b*x)/5 + x**4*exp(-b**2*x**2)/(5*sqrt(pi)*b) + 2*x**2*e
xp(-b**2*x**2)/(5*sqrt(pi)*b**3) + 2*exp(-b**2*x**2)/(5*sqrt(pi)*b**5), Ne(
b, 0)), (0, True))
```

Giac [A]
time = 0.41, size = 44, normalized size = 0.52

$$\frac{1}{5}\,x^5\operatorname{erf}\left(bx\right)+\frac{\left(b^4x^4+2\,b^2x^2+2\right)e^{\left(-b^2x^2\right)}}{5\,\sqrt{\pi}\,b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erf(b*x),x, algorithm="giac")
```

```
[Out] 1/5*x^5*erf(b*x) + 1/5*(b^4*x^4 + 2*b^2*x^2 + 2)*e^(-b^2*x^2)/(sqrt(pi)*b^5
)
```

<u>**Mupad**</u> [B]
time = 0.13, size = 44, normalized size = 0.52

$$\frac{x^5\,\mathrm{erf}(b\,x)}{5}+\frac{\mathrm{e}^{-b^2\,x^2}\,\left(b^4\,x^4+2\,b^2\,x^2+2\right)}{5\,b^5\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erf(b*x),x)
```

```
[Out] (x^5*erf(b*x))/5 + (exp(-b^2*x^2)*(2*b^2*x^2 + b^4*x^4 + 2))/(5*b^5*pi^(1/2
))
```

3.10 $\int x^2 \mathbf{Erf}(bx)\, dx$

Optimal. Leaf size=59

$$\frac{e^{-b^2x^2}}{3b^3\sqrt{\pi}}+\frac{e^{-b^2x^2}x^2}{3b\sqrt{\pi}}+\frac{1}{3}x^3\mathrm{Erf}(bx)$$

```
[Out] 1/3*x^3*erf(b*x)+1/3/b^3/exp(b^2*x^2)/Pi^(1/2)+1/3*x^2/b/exp(b^2*x^2)/Pi^(1
/2)
```

Rubi [A]
time = 0.03, antiderivative size = 59, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6496, 2243, 2240}

$$\frac{x^2e^{-b^2x^2}}{3\sqrt{\pi}\,b}+\frac{e^{-b^2x^2}}{3\sqrt{\pi}\,b^3}+\frac{1}{3}x^3\mathrm{Erf}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x^2*Erf[b*x],x]
```

```
[Out] 1/(3*b^3*E^(b^2*x^2)*Sqrt[Pi]) + x^2/(3*b*E^(b^2*x^2)*Sqrt[Pi]) + (x^3*Erf[
b*x])/3
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6496

```
Int[Erf[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(
c + d*x)^(m + 1)*(Erf[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(m
+ 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d, m
}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int x^2\text{erf}(bx)\,dx &= \frac{1}{3}x^3\text{erf}(bx) - \frac{(2b)\int e^{-b^2x^2}x^3\,dx}{3\sqrt{\pi}}\\ &= \frac{e^{-b^2x^2}x^2}{3b\sqrt{\pi}} + \frac{1}{3}x^3\text{erf}(bx) - \frac{2\int e^{-b^2x^2}x\,dx}{3b\sqrt{\pi}}\\ &= \frac{e^{-b^2x^2}}{3b^3\sqrt{\pi}} + \frac{e^{-b^2x^2}x^2}{3b\sqrt{\pi}} + \frac{1}{3}x^3\text{erf}(bx)\end{aligned}$$

Mathematica [A]
time = 0.02, size = 41, normalized size = 0.69

$$\frac{1}{3}\left(\frac{e^{-b^2x^2}(1+b^2x^2)}{b^3\sqrt{\pi}} + x^3\text{Erf}(bx)\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*Erf[b*x],x]
[Out] ((1 + b^2*x^2)/(b^3*E^(b^2*x^2)*Sqrt[Pi]) + x^3*Erf[b*x])/3
```

Maple [A]
time = 0.38, size = 54, normalized size = 0.92

method	result	size
meijerg	$\frac{-\frac{2}{3}+\frac{(2b^2x^2+2)e^{-b^2x^2}}{3}+\frac{2b^3x^3\,\text{erf}(bx)\sqrt{\pi}}{3}}{2b^3\sqrt{\pi}}$	47
derivativedivides	$\frac{\frac{\text{erf}(bx)b^3x^3}{3}-\frac{2\left(-\frac{b^2x^2e^{-b^2x^2}}{2}-\frac{e^{-b^2x^2}}{2}\right)}{3\sqrt{\pi}}}{b^3}$	54
default	$\frac{\frac{\text{erf}(bx)b^3x^3}{3}-\frac{2\left(-\frac{b^2x^2e^{-b^2x^2}}{2}-\frac{e^{-b^2x^2}}{2}\right)}{3\sqrt{\pi}}}{b^3}$	54

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erf(b*x),x,method=_RETURNVERBOSE)
[Out] 1/b^3*(1/3*erf(b*x)*b^3*x^3-2/3/Pi^(1/2)*(-1/2*b^2*x^2/exp(b^2*x^2)-1/2/exp
(b^2*x^2)))
```

Maxima [A]
time = 0.26, size = 36, normalized size = 0.61

$$\frac{1}{3}\,x^3\,\mathrm{erf}\,(bx) + \frac{(b^2x^2+1)e^{(-b^2x^2)}}{3\,\sqrt{\pi}\,b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erf(b*x),x, algorithm="maxima")
```

```
[Out] 1/3*x^3*erf(b*x) + 1/3*(b^2*x^2 + 1)*e^(-b^2*x^2)/(sqrt(pi)*b^3)
```

Fricas [A]
time = 0.38, size = 43, normalized size = 0.73

$$\frac{\pi b^3x^3\,\mathrm{erf}\,(bx) + \sqrt{\pi}\,(b^2x^2+1)e^{(-b^2x^2)}}{3\,\pi b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erf(b*x),x, algorithm="fricas")
```

```
[Out] 1/3*(pi*b^3*x^3*erf(b*x) + sqrt(pi)*(b^2*x^2 + 1)*e^(-b^2*x^2))/(pi*b^3)
```

Sympy [A]
time = 0.22, size = 51, normalized size = 0.86

$$\begin{cases} \frac{x^3\,\mathrm{erf}\,(bx)}{3} + \frac{x^2e^{-b^2x^2}}{3\sqrt{\pi}\,b} + \frac{e^{-b^2x^2}}{3\sqrt{\pi}\,b^3} & \text{for}\ b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*erf(b*x),x)
```

```
[Out] Piecewise((x**3*erf(b*x)/3 + x**2*exp(-b**2*x**2)/(3*sqrt(pi)*b) + exp(-b**
2*x**2)/(3*sqrt(pi)*b**3), Ne(b, 0)), (0, True))
```

Giac [A]
time = 0.41, size = 36, normalized size = 0.61

$$\frac{1}{3}\,x^3\,\mathrm{erf}\,(bx) + \frac{(b^2x^2+1)e^{(-b^2x^2)}}{3\,\sqrt{\pi}\,b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erf(b*x),x, algorithm="giac")
```

```
[Out] 1/3*x^3*erf(b*x) + 1/3*(b^2*x^2 + 1)*e^(-b^2*x^2)/(sqrt(pi)*b^3)
```

Mupad [B]
time = 0.09, size = 36, normalized size = 0.61

$$\frac{x^3\,\mathrm{erf}(b\,x)}{3}+\frac{\mathrm{e}^{-b^2\,x^2}\,\left(b^2\,x^2+1\right)}{3\,b^3\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erf(b*x),x)
[Out] (x^3*erf(b*x))/3 + (exp(-b^2*x^2)*(b^2*x^2 + 1))/(3*b^3*pi^(1/2))
```

3.11 $\int \mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=26

$$\frac{e^{-b^2x^2}}{b\sqrt{\pi}}+x\text{Erf}(bx)$$

```
[Out] x*erf(b*x)+1/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.00, antiderivative size = 26, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 4, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.250, Rules used = {6484}

$$\frac{e^{-b^2x^2}}{\sqrt{\pi}\,b}+x\text{Erf}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x],x]
[Out] 1/(b*E^(b^2*x^2)*Sqrt[Pi]) + x*Erf[b*x]
```

Rule 6484

```
Int[Erf[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[(a + b*x)*(Erf[a + b*x]/b),
x] + Simp[1/(b*Sqrt[Pi]*E^(a + b*x)^2), x] /; FreeQ[{a, b}, x]
```

Rubi steps

$$\int \text{erf}(bx)\,dx=\frac{e^{-b^2x^2}}{b\sqrt{\pi}}+x\text{erf}(bx)$$

Mathematica [A]
time = 0.01, size = 26, normalized size = 1.00

$$\frac{e^{-b^2x^2}}{b\sqrt{\pi}}+x\text{Erf}(bx)$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x],x]
[Out] 1/(b*E^(b^2*x^2)*Sqrt[Pi]) + x*Erf[b*x]
```

Maple [A]
time = 0.21, size = 26, normalized size = 1.00

method	result	size
derivativedivides	$\frac{\operatorname{erf}(bx)bx+\frac{e^{-b^2x^2}}{\sqrt{\pi}}}{b}$	26
default	$\frac{\operatorname{erf}(bx)bx+\frac{e^{-b^2x^2}}{\sqrt{\pi}}}{b}$	26
meijerg	$\frac{-2+2\,e^{-b^2x^2}+2bx\operatorname{erf}(bx)\sqrt{\pi}}{2\sqrt{\pi}\,b}$	33

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*(erf(b*x)*b*x+1/Pi^(1/2)*exp(-b^2*x^2))
```

Maxima [A]
time = 0.26, size = 25, normalized size = 0.96

$$\frac{bx\operatorname{erf}(bx)+\frac{e^{(-b^2x^2)}}{\sqrt{\pi}}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x),x, algorithm="maxima")
```

```
[Out] (b*x*erf(b*x) + e^(-b^2*x^2)/sqrt(pi))/b
```

Fricas [A]
time = 0.38, size = 29, normalized size = 1.12

$$\frac{\pi bx\operatorname{erf}(bx)+\sqrt{\pi}\,e^{(-b^2x^2)}}{\pi b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x),x, algorithm="fricas")
```

```
[Out] (pi*b*x*erf(b*x) + sqrt(pi)*e^(-b^2*x^2))/(pi*b)
```

Sympy [A]
time = 0.15, size = 24, normalized size = 0.92

$$\begin{cases} x\operatorname{erf}(bx)+\frac{e^{-b^2x^2}}{\sqrt{\pi}\,b} & \text{for } b\neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x),x)
```

```
[Out] Piecewise((x*erf(b*x) + exp(-b**2*x**2)/(sqrt(pi)*b), Ne(b, 0)), (0, True))
```

Giac [A]
time = 0.40, size = 23, normalized size = 0.88

$$x \operatorname{erf}(bx) + \frac{e^{(-b^2x^2)}}{\sqrt{\pi}\, b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x),x, algorithm="giac")
```

```
[Out] x*erf(b*x) + e^(-b^2*x^2)/(sqrt(pi)*b)
```

Mupad [B]
time = 0.08, size = 23, normalized size = 0.88

$$x \operatorname{erf}(b\,x) + \frac{\mathrm{e}^{-b^2\,x^2}}{b\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x),x)
```

```
[Out] x*erf(b*x) + exp(-b^2*x^2)/(b*pi^(1/2))
```

3.12 $\int \frac{\mathbf{Erf}(bx)}{x^2}\,dx$

Optimal. Leaf size=26

$$-\frac{\text{Erf}(bx)}{x}+\frac{b\text{Ei}(-b^2x^2)}{\sqrt{\pi}}$$

```
[Out] -erf(b*x)/x+b*Ei(-b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.02, antiderivative size = 26, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {6496, 2241}

$$\frac{b\text{Ei}(-b^2x^2)}{\sqrt{\pi}}-\frac{\text{Erf}(bx)}{x}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]/x^2,x]
```

```
[Out] -(Erf[b*x]/x) + (b*ExpIntegralEi[-(b^2*x^2)])/Sqrt[Pi]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 6496

```
Int[Erf[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(
c + d*x)^(m + 1)*(Erf[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(m
+ 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d, m
}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{\text{erf}(bx)}{x^2}\,dx &= -\frac{\text{erf}(bx)}{x}+\frac{(2b)\int \frac{e^{-b^2x^2}}{x}\,dx}{\sqrt{\pi}}\\ &= -\frac{\text{erf}(bx)}{x}+\frac{b\text{Ei}(-b^2x^2)}{\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 26, normalized size = 1.00

$$-\frac{\text{Erf}(bx)}{x}+\frac{b\text{Ei}(-b^2x^2)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]/x^2,x]
```

```
[Out] -(Erf[b*x]/x) + (b*ExpIntegralEi[-(b^2*x^2)])/Sqrt[Pi]
```

Maple [A]
time = 0.56, size = 30, normalized size = 1.15

method	result	size
derivativedivides	$b\left(-\frac{\operatorname{erf}(bx)}{bx}-\frac{\operatorname{expIntegral}\left(1,b^{2}x^{2}\right)}{\sqrt{\pi}}\right)$	30
default	$b\left(-\frac{\operatorname{erf}(bx)}{bx}-\frac{\operatorname{expIntegral}\left(1,b^{2}x^{2}\right)}{\sqrt{\pi}}\right)$	30
meijerg	$\frac{b\left(-\frac{2b^{2}x^{2}\operatorname{hypergeom}\left(\left[1,1,\frac{3}{2}\right],\left[2,2,\frac{5}{2}\right],-b^{2}x^{2}\right)}{3}+2\gamma-4+4\ln(x)+4\ln(b)\right)}{2\sqrt{\pi}}$	45

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/x^2,x,method=_RETURNVERBOSE)
```

```
[Out] b*(-erf(b*x)/b/x-1/Pi^(1/2)*Ei(1,b^2*x^2))
```

Maxima [A]
time = 0.29, size = 24, normalized size = 0.92

$$\frac{b\mathrm{Ei}(-b^{2}x^{2})}{\sqrt{\pi}}-\frac{\operatorname{erf}(bx)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^2,x, algorithm="maxima")
```

```
[Out] b*Ei(-b^2*x^2)/sqrt(pi) - erf(b*x)/x
```

Fricas [A]
time = 0.38, size = 30, normalized size = 1.15

$$\frac{\sqrt{\pi}\,bx\mathrm{Ei}(-b^{2}x^{2})-\pi\operatorname{erf}(bx)}{\pi x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^2,x, algorithm="fricas")
```

```
[Out] (sqrt(pi)*b*x*Ei(-b^2*x^2) - pi*erf(b*x))/(pi*x)
```

Sympy [A]
time = 0.54, size = 24, normalized size = 0.92

$$-\frac{b\,\mathrm{E}_1\left(b^2x^2\right)}{\sqrt{\pi}}+\frac{\operatorname{erfc}\left(bx\right)}{x}-\frac{1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x**2,x)
```

```
[Out] -b*expint(1, b**2*x**2)/sqrt(pi) + erfc(b*x)/x - 1/x
```

Giac [A]
time = 0.41, size = 24, normalized size = 0.92

$$\frac{b\mathrm{Ei}(-b^2x^2)}{\sqrt{\pi}}-\frac{\operatorname{erf}\left(bx\right)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^2,x, algorithm="giac")
```

```
[Out] b*Ei(-b^2*x^2)/sqrt(pi) - erf(b*x)/x
```

Mupad [B]
time = 0.15, size = 24, normalized size = 0.92

$$\frac{b\,\mathrm{ei}(-b^2\,x^2)}{\sqrt{\pi}}-\frac{\operatorname{erf}(b\,x)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/x^2,x)
```

```
[Out] (b*ei(-b^2*x^2))/pi^(1/2) - erf(b*x)/x
```

3.13 $\int \frac{\textbf{Erf}(bx)}{x^4}\,dx$

Optimal. Leaf size=56

$$-\frac{be^{-b^2x^2}}{3\sqrt{\pi}\,x^2}-\frac{\operatorname{Erf}(bx)}{3x^3}-\frac{b^3\operatorname{Ei}(-b^2x^2)}{3\sqrt{\pi}}$$

```
[Out] -1/3*erf(b*x)/x^3-1/3*b/exp(b^2*x^2)/x^2/Pi^(1/2)-1/3*b^3*Ei(-b^2*x^2)/Pi^(
1/2)
```

Rubi [A]
time = 0.03, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6496, 2245, 2241}

$$-\frac{be^{-b^2x^2}}{3\sqrt{\pi}\,x^2}-\frac{b^3\operatorname{Ei}(-b^2x^2)}{3\sqrt{\pi}}-\frac{\operatorname{Erf}(bx)}{3x^3}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]/x^4,x]
```

```
[Out] -1/3*b/(E^(b^2*x^2)*Sqrt[Pi]*x^2) - Erf[b*x]/(3*x^3) - (b^3*ExpIntegralEi[-
(b^2*x^2)])/(3*Sqrt[Pi])
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6496

```
Int[Erf[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(
c + d*x)^(m + 1)*(Erf[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(m
+ 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d, m
}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{\operatorname{erf}(bx)}{x^4}\,dx &= -\frac{\operatorname{erf}(bx)}{3x^3}+\frac{(2b)\int\frac{e^{-b^2x^2}}{x^3}\,dx}{3\sqrt{\pi}}\\
&= -\frac{be^{-b^2x^2}}{3\sqrt{\pi}\,x^2}-\frac{\operatorname{erf}(bx)}{3x^3}-\frac{(2b^3)\int\frac{e^{-b^2x^2}}{x}\,dx}{3\sqrt{\pi}}\\
&= -\frac{be^{-b^2x^2}}{3\sqrt{\pi}\,x^2}-\frac{\operatorname{erf}(bx)}{3x^3}-\frac{b^3\operatorname{Ei}(-b^2x^2)}{3\sqrt{\pi}}
\end{aligned}
$$

Mathematica [A]
time = 0.04, size = 47, normalized size = 0.84

$$
-\frac{\operatorname{Erf}(bx)+\frac{bx\left(e^{-b^2x^2}+b^2x^2\operatorname{Ei}(-b^2x^2)\right)}{\sqrt{\pi}}}{3x^3}
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]/x^4,x]
```

```
[Out] -1/3*(Erf[b*x] + (b*x*(E^(-(b^2*x^2)) + b^2*x^2*ExpIntegralEi[-(b^2*x^2)]))
/Sqrt[Pi])/x^3
```

Maple [A]
time = 0.27, size = 53, normalized size = 0.95

method	result	size
derivativedivides	$b^3\left(-\frac{\operatorname{erf}(bx)}{3b^3x^3}+\frac{-\frac{e^{-b^2x^2}}{3b^2x^2}+\frac{\operatorname{expIntegral}\left(1,b^2x^2\right)}{3}}{\sqrt{\pi}}\right)$	53
default	$b^3\left(-\frac{\operatorname{erf}(bx)}{3b^3x^3}+\frac{-\frac{e^{-b^2x^2}}{3b^2x^2}+\frac{\operatorname{expIntegral}\left(1,b^2x^2\right)}{3}}{\sqrt{\pi}}\right)$	53
meijerg	$\frac{b^3\left(\frac{b^2x^2\,\operatorname{hypergeom}\left(\left[1,1,\frac{5}{2}\right],\left[2,3,\frac{7}{2}\right],-b^2x^2\right)}{5}+\frac{10}{9}-\frac{2\gamma}{3}-\frac{4\ln(x)}{3}-\frac{4\ln(b)}{3}-\frac{2}{b^2x^2}\right)}{2\sqrt{\pi}}$	55

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/x^4,x,method=_RETURNVERBOSE)
```

```
[Out] b^3*(-1/3*erf(b*x)/b^3/x^3+2/3/Pi^(1/2)*(-1/2/exp(b^2*x^2)/b^2/x^2+1/2*Ei(1
,b^2*x^2)))
```

Maxima [A]
time = 0.29, size = 27, normalized size = 0.48

$$-\frac{b^3\Gamma(-1, b^2x^2)}{3\sqrt{\pi}} - \frac{\operatorname{erf}(bx)}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^4,x, algorithm="maxima")
```

```
[Out] -1/3*b^3*gamma(-1, b^2*x^2)/sqrt(pi) - 1/3*erf(b*x)/x^3
```

Fricas [A]
time = 0.36, size = 48, normalized size = 0.86

$$-\frac{\pi\operatorname{erf}(bx) + \sqrt{\pi}\left(b^3x^3\operatorname{Ei}(-b^2x^2) + bxe^{(-b^2x^2)}\right)}{3\pi x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^4,x, algorithm="fricas")
```

```
[Out] -1/3*(pi*erf(b*x) + sqrt(pi)*(b^3*x^3*Ei(-b^2*x^2) + b*x*e^(-b^2*x^2)))/(pi
*x^3)
```

Sympy [A]
time = 1.05, size = 54, normalized size = 0.96

$$\frac{b^3\operatorname{E}_1(b^2x^2)}{3\sqrt{\pi}} - \frac{be^{-b^2x^2}}{3\sqrt{\pi}x^2} + \frac{\operatorname{erfc}(bx)}{3x^3} - \frac{1}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x**4,x)
```

```
[Out] b**3*expint(1, b**2*x**2)/(3*sqrt(pi)) - b*exp(-b**2*x**2)/(3*sqrt(pi)*x**2
) + erfc(b*x)/(3*x**3) - 1/(3*x**3)
```

Giac [A]
time = 0.41, size = 51, normalized size = 0.91

$$-\frac{\operatorname{erf}(bx)}{3x^3} - \frac{b^6x^2\operatorname{Ei}(-b^2x^2) + b^4e^{(-b^2x^2)}}{3\sqrt{\pi}b^3x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^4,x, algorithm="giac")
```

```
[Out] -1/3*erf(b*x)/x^3 - 1/3*(b^6*x^2*Ei(-b^2*x^2) + b^4*e^(-b^2*x^2))/(sqrt(pi)
*b^3*x^2)
```

Mupad [B]
time = 0.18, size = 45, normalized size = 0.80

$$-\frac{\operatorname{erf}(b\,x)}{3\,x^3}-\frac{b^3\,\operatorname{ei}(-b^2\,x^2)}{3\,\sqrt{\pi}}-\frac{b\,\mathrm{e}^{-b^2\,x^2}}{3\,x^2\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/x^4,x)
```

```
[Out] - erf(b*x)/(3*x^3) - (b^3*ei(-b^2*x^2))/(3*pi^(1/2)) - (b*exp(-b^2*x^2))/(3
*x^2*pi^(1/2))
```

3.14 $\int \frac{\textbf{Erf}(bx)}{x^6} \, dx$

Optimal. Leaf size=81

$$-\frac{be^{-b^2x^2}}{10\sqrt{\pi}\,x^4}+\frac{b^3e^{-b^2x^2}}{10\sqrt{\pi}\,x^2}-\frac{\text{Erf}(bx)}{5x^5}+\frac{b^5\text{Ei}(-b^2x^2)}{10\sqrt{\pi}}$$

```
[Out] -1/5*erf(b*x)/x^5-1/10*b/exp(b^2*x^2)/x^4/Pi^(1/2)+1/10*b^3/exp(b^2*x^2)/x^
2/Pi^(1/2)+1/10*b^5*Ei(-b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.05, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6496, 2245, 2241}

$$-\frac{be^{-b^2x^2}}{10\sqrt{\pi}\,x^4}+\frac{b^5\text{Ei}(-b^2x^2)}{10\sqrt{\pi}}+\frac{b^3e^{-b^2x^2}}{10\sqrt{\pi}\,x^2}-\frac{\text{Erf}(bx)}{5x^5}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]/x^6,x]
```

```
[Out] -1/10*b/(E^(b^2*x^2)*Sqrt[Pi]*x^4) + b^3/(10*E^(b^2*x^2)*Sqrt[Pi]*x^2) - Er
f[b*x]/(5*x^5) + (b^5*ExpIntegralEi[-(b^2*x^2)])/(10*Sqrt[Pi])
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6496

```
Int[Erf[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(
c + d*x)^(m + 1)*(Erf[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(m
+ 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d, m
}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{\operatorname{erf}(bx)}{x^6}\,dx &= -\frac{\operatorname{erf}(bx)}{5x^5} + \frac{(2b)\int \frac{e^{-b^2x^2}}{x^5}\,dx}{5\sqrt{\pi}} \\
&= -\frac{be^{-b^2x^2}}{10\sqrt{\pi}\,x^4} - \frac{\operatorname{erf}(bx)}{5x^5} - \frac{b^3\int \frac{e^{-b^2x^2}}{x^3}\,dx}{5\sqrt{\pi}} \\
&= -\frac{be^{-b^2x^2}}{10\sqrt{\pi}\,x^4} + \frac{b^3e^{-b^2x^2}}{10\sqrt{\pi}\,x^2} - \frac{\operatorname{erf}(bx)}{5x^5} + \frac{b^5\int \frac{e^{-b^2x^2}}{x}\,dx}{5\sqrt{\pi}} \\
&= -\frac{be^{-b^2x^2}}{10\sqrt{\pi}\,x^4} + \frac{b^3e^{-b^2x^2}}{10\sqrt{\pi}\,x^2} - \frac{\operatorname{erf}(bx)}{5x^5} + \frac{b^5\operatorname{Ei}(-b^2x^2)}{10\sqrt{\pi}}
\end{aligned}
$$

Mathematica [A]
time = 0.03, size = 62, normalized size = 0.77

$$\frac{be^{-b^2x^2}x(-1+b^2x^2) - 2\sqrt{\pi}\,\operatorname{Erf}(bx) + b^5x^5\operatorname{Ei}(-b^2x^2)}{10\sqrt{\pi}\,x^5}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]/x^6,x]
```

```
[Out] ((b*x*(-1 + b^2*x^2))/E^(b^2*x^2) - 2*Sqrt[Pi]*Erf[b*x] + b^5*x^5*ExpIntegr
alEi[-(b^2*x^2)])/(10*Sqrt[Pi]*x^5)
```

Maple [A]
time = 0.31, size = 71, normalized size = 0.88

method	result	size
meijerg	$\frac{b^5\left(-\frac{b^2x^2\,\mathrm{hypergeom}\left(\left[1,1,\frac{7}{2}\right],\left[2,4,\frac{9}{2}\right],-b^2x^2\right)}{21}-\frac{19}{50}+\frac{\gamma}{5}+\frac{2\ln(x)}{5}+\frac{2\ln(b)}{5}-\frac{1}{b^4x^4}+\frac{2}{3b^2x^2}\right)}{2\sqrt{\pi}}$	63
derivativedivides	$b^5\left(-\frac{\mathrm{erf}(bx)}{5b^5x^5}+\frac{-\frac{\mathrm{e}^{-b^2x^2}}{10b^4x^4}+\frac{\mathrm{e}^{-b^2x^2}}{10b^2x^2}-\frac{\mathrm{expIntegral}\left(1,b^2x^2\right)}{10}}{\sqrt{\pi}}\right)$	71
default	$b^5\left(-\frac{\mathrm{erf}(bx)}{5b^5x^5}+\frac{-\frac{\mathrm{e}^{-b^2x^2}}{10b^4x^4}+\frac{\mathrm{e}^{-b^2x^2}}{10b^2x^2}-\frac{\mathrm{expIntegral}\left(1,b^2x^2\right)}{10}}{\sqrt{\pi}}\right)$	71

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/x^6,x,method=_RETURNVERBOSE)
```

```
[Out] b^5*(-1/5*erf(b*x)/b^5/x^5+2/5/Pi^(1/2)*(-1/4/exp(b^2*x^2)/b^4/x^4+1/4/exp(
b^2*x^2)/b^2/x^2-1/4*Ei(1,b^2*x^2)))
```

Maxima [A]
time = 0.30, size = 27, normalized size = 0.33

$$-\frac{b^5\Gamma(-2, b^2x^2)}{5\sqrt{\pi}}-\frac{\operatorname{erf}(bx)}{5x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^6,x, algorithm="maxima")
```

```
[Out] -1/5*b^5*gamma(-2, b^2*x^2)/sqrt(pi) - 1/5*erf(b*x)/x^5
```

Fricas [A]
time = 0.37, size = 60, normalized size = 0.74

$$-\frac{2\pi\operatorname{erf}(bx)-\sqrt{\pi}\left(b^5x^5\operatorname{Ei}(-b^2x^2)+(b^3x^3-bx)e^{(-b^2x^2)}\right)}{10\pi x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^6,x, algorithm="fricas")
```

```
[Out] -1/10*(2*pi*erf(b*x) - sqrt(pi)*(b^5*x^5*Ei(-b^2*x^2) + (b^3*x^3 - b*x)*e^(
-b^2*x^2)))/(pi*x^5)
```

Sympy [A]
time = 1.95, size = 76, normalized size = 0.94

$$-\frac{b^5\operatorname{E}_1(b^2x^2)}{10\sqrt{\pi}}+\frac{b^3e^{-b^2x^2}}{10\sqrt{\pi}x^2}-\frac{be^{-b^2x^2}}{10\sqrt{\pi}x^4}+\frac{\operatorname{erfc}(bx)}{5x^5}-\frac{1}{5x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x**6,x)
```

```
[Out] -b**5*expint(1, b**2*x**2)/(10*sqrt(pi)) + b**3*exp(-b**2*x**2)/(10*sqrt(pi
)*x**2) - b*exp(-b**2*x**2)/(10*sqrt(pi)*x**4) + erfc(b*x)/(5*x**5) - 1/(5*
x**5)
```

Giac [A]
time = 0.40, size = 68, normalized size = 0.84

$$-\frac{\operatorname{erf}(bx)}{5x^5}+\frac{b^{10}x^4\operatorname{Ei}(-b^2x^2)+b^8x^2e^{(-b^2x^2)}-b^6e^{(-b^2x^2)}}{10\sqrt{\pi}b^5x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/x^6,x, algorithm="giac")
```

```
[Out] -1/5*erf(b*x)/x^5 + 1/10*(b^10*x^4*Ei(-b^2*x^2) + b^8*x^2*e^(-b^2*x^2) - b^
6*e^(-b^2*x^2))/(sqrt(pi)*b^5*x^4)
```

Mupad [B]
time = 0.20, size = 65, normalized size = 0.80

$$\frac{b^5\,\mathrm{ei}\left(-b^2\,x^2\right)}{10\,\sqrt{\pi}}-\frac{\mathrm{erf}\left(b\,x\right)}{5\,x^5}-\frac{\frac{b\,{\mathrm{e}}^{-b^2\,x^2}}{2}-\frac{b^3\,x^2\,{\mathrm{e}}^{-b^2\,x^2}}{2}}{5\,x^4\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/x^6,x)
```

```
[Out] (b^5*ei(-b^2*x^2))/(10*pi^(1/2)) - erf(b*x)/(5*x^5) - ((b*exp(-b^2*x^2))/2
- (b^3*x^2*exp(-b^2*x^2))/2)/(5*x^4*pi^(1/2))
```

3.15 $\int (c+dx)^3 \mathbf{Erf}(a+bx)\,dx$

Optimal. Leaf size=289

$$\frac{d^2(bc-ad)e^{-(a+bx)^2}}{b^4\sqrt{\pi}}+\frac{(bc-ad)^3e^{-(a+bx)^2}}{b^4\sqrt{\pi}}+\frac{3d^3e^{-(a+bx)^2}(a+bx)}{8b^4\sqrt{\pi}}+\frac{3d(bc-ad)^2e^{-(a+bx)^2}(a+bx)}{2b^4\sqrt{\pi}}+\frac{d^2(bc-ad}{}$$

```
[Out] -3/16*d^3*erf(b*x+a)/b^4-3/4*d*(-a*d+b*c)^2*erf(b*x+a)/b^4-1/4*(-a*d+b*c)^4
*erf(b*x+a)/b^4/d+1/4*(d*x+c)^4*erf(b*x+a)/d+d^2*(-a*d+b*c)/b^4/exp((b*x+a)
^2)/Pi^(1/2)+(-a*d+b*c)^3/b^4/exp((b*x+a)^2)/Pi^(1/2)+3/8*d^3*(b*x+a)/b^4/e
xp((b*x+a)^2)/Pi^(1/2)+3/2*d*(-a*d+b*c)^2*(b*x+a)/b^4/exp((b*x+a)^2)/Pi^(1/
2)+d^2*(-a*d+b*c)*(b*x+a)^2/b^4/exp((b*x+a)^2)/Pi^(1/2)+1/4*d^3*(b*x+a)^3/b
^4/exp((b*x+a)^2)/Pi^(1/2)
```

Rubi [A]

time = 0.22, antiderivative size = 289, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 5, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.357$, Rules used = {6496, 2258, 2236, 2240, 2243}

$$\frac{d^2e^{-(a+bx)^2}(a+bx)^2(bc-ad)}{\sqrt{\pi}\,b^4}+\frac{d^2e^{-(a+bx)^2}(bc-ad)}{\sqrt{\pi}\,b^4}-\frac{(bc-ad)^4\text{Erf}(a+bx)}{4b^4d}-\frac{3d(bc-ad)^2\text{Erf}(a+bx)}{4b^4}+\frac{e^{-(a+bx)^2}(bc-ad)^3}{\sqrt{\pi}\,b^4}+\frac{3de^{-(a+bx)^2}(a+bx)(bc-ad)^2}{2\sqrt{\pi}\,b^4}-\frac{3d^3\text{Erf}(a+bx)}{16b^4}+\frac{d^3e^{-(a+bx)^2}(a+bx)^3}{4\sqrt{\pi}\,b^4}+\frac{3d^3e^{-(a+bx)^2}(a+bx)}{8\sqrt{\pi}\,b^4}+\frac{(c+dx)^4\text{Erf}(a+bx)}{4d}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)^3*Erf[a + b*x],x]
```

```
[Out] (d^2*(b*c - a*d))/(b^4*E^(a + b*x)^2*Sqrt[Pi]) + (b*c - a*d)^3/(b^4*E^(a +
b*x)^2*Sqrt[Pi]) + (3*d^3*(a + b*x))/(8*b^4*E^(a + b*x)^2*Sqrt[Pi]) + (3*d*
(b*c - a*d)^2*(a + b*x))/(2*b^4*E^(a + b*x)^2*Sqrt[Pi]) + (d^2*(b*c - a*d)*
(a + b*x)^2)/(b^4*E^(a + b*x)^2*Sqrt[Pi]) + (d^3*(a + b*x)^3)/(4*b^4*E^(a +
 b*x)^2*Sqrt[Pi]) - (3*d^3*Erf[a + b*x])/(16*b^4) - (3*d*(b*c - a*d)^2*Erf[
a + b*x])/(4*b^4) - ((b*c - a*d)^4*Erf[a + b*x])/(4*b^4*d) + ((c + d*x)^4*E
rf[a + b*x])/(4*d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 2258

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*(u_), x_Symbol] :> Int[E
xpandLinearProduct[F^(a + b*(c + d*x)^n), u, c, d, x], x] /; FreeQ[{F, a, b
, c, d, n}, x] && PolynomialQ[u, x]
```

Rule 6496

```
Int[Erf[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(
c + d*x)^(m + 1)*(Erf[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(m
+ 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d, m
}, x] && NeQ[m, -1]
```

Rubi steps

$$\int (c+dx)^3\operatorname{erf}(a+bx)\,dx = \frac{(c+dx)^4\operatorname{erf}(a+bx)}{4d} - \frac{b\int e^{-(a+bx)^2}(c+dx)^4\,dx}{2d\sqrt{\pi}}$$

$$= \frac{(c+dx)^4\operatorname{erf}(a+bx)}{4d} - \frac{b\int\left(\frac{(bc-ad)^4e^{-(a+bx)^2}}{b^4} + \frac{4d(bc-ad)^3e^{-(a+bx)^2}(a+bx)}{b^4} + \frac{6d^2(bc-ad}{}\right.}{}$$

$$= \frac{(c+dx)^4\operatorname{erf}(a+bx)}{4d} - \frac{d^3\int e^{-(a+bx)^2}(a+bx)^4\,dx}{2b^3\sqrt{\pi}} - \frac{(2d^2(bc-ad))\int e^{-(a+bx)^2}}{b^3\sqrt{\pi}}$$

$$= \frac{(bc-ad)^3e^{-(a+bx)^2}}{b^4\sqrt{\pi}} + \frac{3d(bc-ad)^2e^{-(a+bx)^2}(a+bx)}{2b^4\sqrt{\pi}} + \frac{d^2(bc-ad)e^{-(a+bx)^2}(a}{b^4\sqrt{\pi}}$$

$$= \frac{d^2(bc-ad)e^{-(a+bx)^2}}{b^4\sqrt{\pi}} + \frac{(bc-ad)^3e^{-(a+bx)^2}}{b^4\sqrt{\pi}} + \frac{3d^3e^{-(a+bx)^2}(a+bx)}{8b^4\sqrt{\pi}} + \frac{3d(bc-a}{}$$

$$= \frac{d^2(bc-ad)e^{-(a+bx)^2}}{b^4\sqrt{\pi}} + \frac{(bc-ad)^3e^{-(a+bx)^2}}{b^4\sqrt{\pi}} + \frac{3d^3e^{-(a+bx)^2}(a+bx)}{8b^4\sqrt{\pi}} + \frac{3d(bc-a}{}$$

Mathematica [A]
time = 0.19, size = 248, normalized size = 0.86

$$\frac{e^{-(a+bx)^2}\left(-2a(5+2a^2)d^3+2bd^2(8(1+a^2)c+(3+2a^2)dx)-4ab^2d(6c^2+4cdx+d^2x^2)+4b^3(4c^3+6c^2dx+4cd^2x^2+d^3x^3)-e^{(a+bx)^2}\sqrt{\pi}(12b^2c^2d-16a^3bcd^2+3d^3+4a^4d^3-8a(2b^3c^3+3bcd^2)+12a^2(2b^2c^2d+d^3)-4b^4x(4c^3+6c^2dx+4cd^2x^2+d^3x^3))\operatorname{Erf}(a+bx)\right)}{16b^4\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^3*Erf[a + b*x],x]
```

```
[Out] (-2*a*(5 + 2*a^2)*d^3 + 2*b*d^2*(8*(1 + a^2)*c + (3 + 2*a^2)*d*x) - 4*a*b^2
*d*(6*c^2 + 4*c*d*x + d^2*x^2) + 4*b^3*(4*c^3 + 6*c^2*d*x + 4*c*d^2*x^2 + d
^3*x^3) - E^(a + b*x)^2*Sqrt[Pi]*(12*b^2*c^2*d - 16*a^3*b*c*d^2 + 3*d^3 + 4
*a^4*d^3 - 8*a*(2*b^3*c^3 + 3*b*c*d^2) + 12*a^2*(2*b^2*c^2*d + d^3) - 4*b^4
*x*(4*c^3 + 6*c^2*d*x + 4*c*d^2*x^2 + d^3*x^3))*Erf[a + b*x])/(16*b^4*E^(a
+ b*x)^2*Sqrt[Pi])
```

Maple [A]
time = 0.79, size = 467, normalized size = 1.62

method	result
derivativedivides	$\frac{\frac{\operatorname{erf}(bx+a)(ad-cb-d(bx+a))^4}{4b^3d}-\frac{\frac{a^4d^4\sqrt{\pi}\,\operatorname{erf}(bx+a)}{2}+\frac{b^4c^4\sqrt{\pi}\,\operatorname{erf}(bx+a)}{2}+d^4\left(-\frac{e^{-(bx+a)^2}(bx+a)^3}{2}-\frac{3(bx+a)e^{-(bx+a)^2}}{4}+\frac{3\sqrt{}}{}\right.}{}}{}$
default	$\frac{\frac{\operatorname{erf}(bx+a)(ad-cb-d(bx+a))^4}{4b^3d}-\frac{\frac{a^4d^4\sqrt{\pi}\,\operatorname{erf}(bx+a)}{2}+\frac{b^4c^4\sqrt{\pi}\,\operatorname{erf}(bx+a)}{2}+d^4\left(-\frac{e^{-(bx+a)^2}(bx+a)^3}{2}-\frac{3(bx+a)e^{-(bx+a)^2}}{4}+\frac{3\sqrt{}}{}\right.}{}}{}$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^3*erf(b*x+a),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*(1/4*erf(b*x+a)*(a*d-c*b-d*(b*x+a))^4/b^3/d-1/2/Pi^(1/2)/b^3/d*(1/2*a^4
*d^4*Pi^(1/2)*erf(b*x+a)+1/2*b^4*c^4*Pi^(1/2)*erf(b*x+a)+d^4*(-1/2/exp((b*x
+a)^2)*(b*x+a)^3-3/4*(b*x+a)/exp((b*x+a)^2)+3/8*Pi^(1/2)*erf(b*x+a))-4*a*d^
4*(-1/2/exp((b*x+a)^2)*(b*x+a)^2-1/2/exp((b*x+a)^2))+6*a^2*d^4*(-1/2*(b*x+a
)/exp((b*x+a)^2)+1/4*Pi^(1/2)*erf(b*x+a))+2*a^3*d^4/exp((b*x+a)^2)-2*a*b^3*
c^3*d*Pi^(1/2)*erf(b*x+a)+3*a^2*b^2*c^2*d^2*Pi^(1/2)*erf(b*x+a)-2*a^3*b*c*d
^3*Pi^(1/2)*erf(b*x+a)+4*b*c*d^3*(-1/2/exp((b*x+a)^2)*(b*x+a)^2-1/2/exp((b*
x+a)^2))+6*b^2*c^2*d^2*(-1/2*(b*x+a)/exp((b*x+a)^2)+1/4*Pi^(1/2)*erf(b*x+a)
)-2*b^3*c^3*d/exp((b*x+a)^2)-12*a*b*c*d^3*(-1/2*(b*x+a)/exp((b*x+a)^2)+1/4*
Pi^(1/2)*erf(b*x+a))+6*a*b^2*c^2*d^2/exp((b*x+a)^2)-6*a^2*b*c*d^3/exp((b*x+
a)^2)))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^3*erf(b*x+a),x, algorithm="maxima")
```

```
[Out] 1/4*(d^3*x^4 + 4*c*d^2*x^3 + 6*c^2*d*x^2 + 4*c^3*x)*erf(b*x + a) - 1/2*inte
grate((b*d^3*x^4 + 4*b*c*d^2*x^3 + 6*b*c^2*d*x^2 + 4*b*c^3*x)*e^(-b^2*x^2 -
 2*a*b*x - a^2), x)/sqrt(pi)
```

Fricas [A]
time = 0.38, size = 265, normalized size = 0.92

$$\frac{2\sqrt{\pi}\left(2b^3d^3x^3+8b^3c^3-12ab^2c^2d+8(a^2+1)bcd^2-(2a^3+5a)d^3+2(4b^3cd^2-ab^2d^3)x^2+(12b^3c^2d-8ab^2cd^2+(2a^2+3)bd^3)x\right)e^{(-b^2x^2-2abx-a^2)}+\left(4\pi b^4d^3x^4+16\pi b^4cd^2x^3+24\pi b^4c^2dx^2+16\pi b^4c^3x+\pi(16ab^3c^3-12(2a^2+1)b^2c^2d+8(2a^3+3a)bcd^2-(4a^4+12a^2+3)d^3)\right)\operatorname{erf}(bx+a)}{16\pi b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^3*erf(b*x+a),x, algorithm="fricas")
```

```
[Out] 1/16*(2*sqrt(pi)*(2*b^3*d^3*x^3 + 8*b^3*c^3 - 12*a*b^2*c^2*d + 8*(a^2 + 1)*
b*c*d^2 - (2*a^3 + 5*a)*d^3 + 2*(4*b^3*c*d^2 - a*b^2*d^3)*x^2 + (12*b^3*c^2
*d - 8*a*b^2*c*d^2 + (2*a^2 + 3)*b*d^3)*x)*e^(-b^2*x^2 - 2*a*b*x - a^2) + (
4*pi*b^4*d^3*x^4 + 16*pi*b^4*c*d^2*x^3 + 24*pi*b^4*c^2*d*x^2 + 16*pi*b^4*c^
3*x + pi*(16*a*b^3*c^3 - 12*(2*a^2 + 1)*b^2*c^2*d + 8*(2*a^3 + 3*a)*b*c*d^2
 - (4*a^4 + 12*a^2 + 3)*d^3))*erf(b*x + a))/(pi*b^4)
```

Sympy [B] Leaf count of result is larger than twice the leaf count of optimal. 746 vs. $2(258) = 516$.
time = 2.06, size = 746, normalized size = 2.58

$$\begin{cases} -\frac{a^4d^3\operatorname{erf}(a+bx)}{4b^4}+\frac{a^3cd^2\operatorname{erf}(a+bx)}{b^3}-\frac{a^3d^3e^{-a^2}e^{-b^2x^2}e^{-2abx}}{4\sqrt{\pi}b^4}-\frac{3a^2c^2d\operatorname{erf}(a+bx)}{2b^2}+\frac{a^2cd^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}b^3}+\frac{a^2d^3xe^{-a^2}e^{-b^2x^2}e^{-2abx}}{4\sqrt{\pi}b^3}-\frac{3a^2d^3\operatorname{erf}(a+bx)}{4b^4}+\frac{ac^3\operatorname{erf}(a+bx)}{b}-\frac{3ac^2de^{-a^2}e^{-b^2x^2}e^{-2abx}}{2\sqrt{\pi}b^2}-\frac{acd^2xe^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}b^2}-\frac{ad^3x^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{4\sqrt{\pi}b^2}+\frac{3acd^2\operatorname{erf}(a+bx)}{2b^3}-\frac{5ad^3e^{-a^2}e^{-b^2x^2}e^{-2abx}}{8\sqrt{\pi}b^4}+c^3x\operatorname{erf}(a+bx)+\frac{3c^2dx^2\operatorname{erf}(a+bx)}{2}+cd^2x^3\operatorname{erf}(a+bx)+\frac{d^3x^4\operatorname{erf}(a+bx)}{4}+\frac{c^3e^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}b}+\frac{3c^2dxe^{-a^2}e^{-b^2x^2}e^{-2abx}}{2\sqrt{\pi}b}+\frac{cd^2x^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}b}+\frac{d^3x^3e^{-a^2}e^{-b^2x^2}e^{-2abx}}{4\sqrt{\pi}b}-\frac{3c^2d\operatorname{erf}(a+bx)}{4b^2}+\frac{cd^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}b^3}+\frac{3d^3xe^{-a^2}e^{-b^2x^2}e^{-2abx}}{8\sqrt{\pi}b^3}-\frac{3d^3\operatorname{erf}(a+bx)}{16b^4} & \text{for}\ b\neq 0 \\ \left(c^3x+\frac{3c^2dx^2}{2}+cd^2x^3+\frac{d^3x^4}{4}\right)\operatorname{erf}(a) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**3*erf(b*x+a),x)
```

```
[Out] Piecewise((-a**4*d**3*erf(a + b*x)/(4*b**4) + a**3*c*d**2*erf(a + b*x)/b**3
 - a**3*d**3*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(4*sqrt(pi)*b**4) - 3
*a**2*c**2*d*erf(a + b*x)/(2*b**2) + a**2*c*d**2*exp(-a**2)*exp(-b**2*x**2)
*exp(-2*a*b*x)/(sqrt(pi)*b**3) + a**2*d**3*x*exp(-a**2)*exp(-b**2*x**2)*exp
(-2*a*b*x)/(4*sqrt(pi)*b**3) - 3*a**2*d**3*erf(a + b*x)/(4*b**4) + a*c**3*e
rf(a + b*x)/b - 3*a*c**2*d*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(2*sqrt
(pi)*b**2) - a*c*d**2*x*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(sqrt(pi)*
b**2) - a*d**3*x**2*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(4*sqrt(pi)*b*
*2) + 3*a*c*d**2*erf(a + b*x)/(2*b**3) - 5*a*d**3*exp(-a**2)*exp(-b**2*x**2
)*exp(-2*a*b*x)/(8*sqrt(pi)*b**4) + c**3*x*erf(a + b*x) + 3*c**2*d*x**2*erf
(a + b*x)/2 + c*d**2*x**3*erf(a + b*x) + d**3*x**4*erf(a + b*x)/4 + c**3*ex
p(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(sqrt(pi)*b) + 3*c**2*d*x*exp(-a**2)
*exp(-b**2*x**2)*exp(-2*a*b*x)/(2*sqrt(pi)*b) + c*d**2*x**2*exp(-a**2)*exp(
-b**2*x**2)*exp(-2*a*b*x)/(sqrt(pi)*b) + d**3*x**3*exp(-a**2)*exp(-b**2*x**
2)*exp(-2*a*b*x)/(4*sqrt(pi)*b) - 3*c**2*d*erf(a + b*x)/(4*b**2) + c*d**2*e
xp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(sqrt(pi)*b**3) + 3*d**3*x*exp(-a**
2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(8*sqrt(pi)*b**3) - 3*d**3*erf(a + b*x)/(1
6*b**4), Ne(b, 0)), ((c**3*x + 3*c**2*d*x**2/2 + c*d**2*x**3 + d**3*x**4/4)
*erf(a), True))
```

Giac [A]
time = 0.44, size = 400, normalized size = 1.38

$$\frac{(dx+c)^4\operatorname{erf}(bx+a)}{4d}+\frac{4\pi c^4\operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)-16\sqrt{\pi}\left(\frac{\sqrt{\pi}a\operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b}-\frac{e^{\left(-b^2x^2-2abx-a^2\right)}}{b}\right)c^3d+\frac{12\sqrt{\pi}\left(\frac{\sqrt{\pi}(2a^2+1)\operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b}+\frac{2\left(b\left(x+\frac{a}{b}\right)-2a\right)e^{\left(-b^2x^2-2abx-a^2\right)}}{b}\right)c^2d^2}{b}-\frac{8\sqrt{\pi}\left(\frac{\sqrt{\pi}(2a^3+3a)\operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b}-\frac{2\left(b^2\left(x+\frac{a}{b}\right)^2-3ab\left(x+\frac{a}{b}\right)+3a^2+1\right)e^{\left(-b^2x^2-2abx-a^2\right)}}{b}\right)cd^3}{b^2}+\frac{\sqrt{\pi}\left(\frac{\sqrt{\pi}(4a^4+12a^2+3)\operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b}+\frac{2\left(2b^3\left(x+\frac{a}{b}\right)^3-8ab^2\left(x+\frac{a}{b}\right)^2+12a^2b\left(x+\frac{a}{b}\right)-8a^3+3b\left(x+\frac{a}{b}\right)-8a\right)e^{\left(-b^2x^2-2abx-a^2\right)}}{b}\right)d^4}{b^3}}{16\pi d}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^3*erf(b*x+a),x, algorithm="giac")
```

```
[Out] 1/4*(d*x + c)^4*erf(b*x + a)/d + 1/16*(4*pi*c^4*erf(-b*(x + a/b)) - 16*sqrt
(pi)*(sqrt(pi)*a*erf(-b*(x + a/b))/b - e^(-b^2*x^2 - 2*a*b*x - a^2)/b)*c^3*
d + 12*sqrt(pi)*(sqrt(pi)*(2*a^2 + 1)*erf(-b*(x + a/b))/b + 2*(b*(x + a/b)
- 2*a)*e^(-b^2*x^2 - 2*a*b*x - a^2)/b)*c^2*d^2/b - 8*sqrt(pi)*(sqrt(pi)*(2*
a^3 + 3*a)*erf(-b*(x + a/b))/b - 2*(b^2*(x + a/b)^2 - 3*a*b*(x + a/b) + 3*a
^2 + 1)*e^(-b^2*x^2 - 2*a*b*x - a^2)/b)*c*d^3/b^2 + sqrt(pi)*(sqrt(pi)*(4*a
^4 + 12*a^2 + 3)*erf(-b*(x + a/b))/b + 2*(2*b^3*(x + a/b)^3 - 8*a*b^2*(x +
a/b)^2 + 12*a^2*b*(x + a/b) - 8*a^3 + 3*b*(x + a/b) - 8*a)*e^(-b^2*x^2 - 2*
a*b*x - a^2)/b)*d^4/b^3)/(pi*d)
```

Mupad [B]
time = 1.09, size = 337, normalized size = 1.17

$$\mathrm{erf}(a+b\,x)\,\left(c^3\,x+\frac{3\,c^2\,d\,x^2}{2}+c\,d^2\,x^3+\frac{d^3\,x^4}{4}\right)-\frac{\frac{{\mathrm{e}}^{-a^2-2\,a\,b\,x-b^2\,x^2}\,\left(\frac{5\,a\,d^3}{4}+\frac{a^3\,d^3}{2}-2\,b^3\,c^3-b\,\left(2\,c\,a^2\,d^2+2\,c\,d^2\right)+3\,a\,b^2\,c^2\,d\right)}{b^4}-\frac{x\,{\mathrm{e}}^{-a^2-2\,a\,b\,x-b^2\,x^2}\,\left(2\,a^2\,d^3-8\,a\,b\,c\,d^2+12\,b^2\,c^2\,d+3\,d^3\right)}{4\,b^3}-\frac{d^3\,x^3\,{\mathrm{e}}^{-a^2-2\,a\,b\,x-b^2\,x^2}}{2\,b}+\frac{x^2\,{\mathrm{e}}^{-a^2-2\,a\,b\,x-b^2\,x^2}\,\left(a\,d^3-4\,b\,c\,d^2\right)}{2\,b^2}}{2\,\sqrt{\pi }}+\frac{\mathrm{erfi}(a\,1{}\mathrm{i}+b\,x\,1{}\mathrm{i})\,\left(4\,a^4\,d^3-16\,a^3\,b\,c\,d^2+24\,a^2\,b^2\,c^2\,d+12\,a^2\,d^3-16\,a\,b^3\,c^3-24\,a\,b\,c\,d^2+12\,b^2\,c^2\,d+3\,d^3\right)\,1{}\mathrm{i}}{16\,b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(a + b*x)*(c + d*x)^3,x)
```

```
[Out] erf(a + b*x)*(c^3*x + (d^3*x^4)/4 + (3*c^2*d*x^2)/2 + c*d^2*x^3) - ((exp(-
a^2 - b^2*x^2 - 2*a*b*x)*((5*a*d^3)/4 + (a^3*d^3)/2 - 2*b^3*c^3 - b*(2*c*d^
2 + 2*a^2*c*d^2) + 3*a*b^2*c^2*d))/b^4 - (x*exp(- a^2 - b^2*x^2 - 2*a*b*x)*
(3*d^3 + 2*a^2*d^3 + 12*b^2*c^2*d - 8*a*b*c*d^2))/(4*b^3) - (d^3*x^3*exp(-
a^2 - b^2*x^2 - 2*a*b*x))/(2*b) + (x^2*exp(- a^2 - b^2*x^2 - 2*a*b*x)*(a*d^
3 - 4*b*c*d^2))/(2*b^2))/(2*pi^(1/2)) + (erfi(a*1i + b*x*1i)*(3*d^3 + 12*a^
2*d^3 + 4*a^4*d^3 - 16*a*b^3*c^3 + 12*b^2*c^2*d + 24*a^2*b^2*c^2*d - 24*a*b
*c*d^2 - 16*a^3*b*c*d^2)*1i)/(16*b^4)
```

3.16 $\int (c+dx)^2 \mathbf{Erf}(a+bx)\,dx$

Optimal. Leaf size=192

$$\frac{d^2 e^{-(a+bx)^2}}{3b^3\sqrt{\pi}}+\frac{(bc-ad)^2 e^{-(a+bx)^2}}{b^3\sqrt{\pi}}+\frac{d(bc-ad)e^{-(a+bx)^2}(a+bx)}{b^3\sqrt{\pi}}+\frac{d^2 e^{-(a+bx)^2}(a+bx)^2}{3b^3\sqrt{\pi}}-\frac{d(bc-ad)\mathrm{Erf}(a+bx}{2b^3}$$

```
[Out] -1/2*d*(-a*d+b*c)*erf(b*x+a)/b^3-1/3*(-a*d+b*c)^3*erf(b*x+a)/b^3/d+1/3*(d*x
+c)^3*erf(b*x+a)/d+1/3*d^2/b^3/exp((b*x+a)^2)/Pi^(1/2)+(-a*d+b*c)^2/b^3/exp
((b*x+a)^2)/Pi^(1/2)+d*(-a*d+b*c)*(b*x+a)/b^3/exp((b*x+a)^2)/Pi^(1/2)+1/3*d
^2*(b*x+a)^2/b^3/exp((b*x+a)^2)/Pi^(1/2)
```

Rubi [A]
time = 0.14, antiderivative size = 192, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 5, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.357$, Rules used = {6496, 2258, 2236, 2240, 2243}

$$-\frac{(bc-ad)^3\mathrm{Erf}(a+bx)}{3b^3d}-\frac{d(bc-ad)\mathrm{Erf}(a+bx)}{2b^3}+\frac{e^{-(a+bx)^2}(bc-ad)^2}{\sqrt{\pi}\,b^3}+\frac{de^{-(a+bx)^2}(a+bx)(bc-ad)}{\sqrt{\pi}\,b^3}+\frac{d^2e^{-(a+bx)^2}(a+bx)^2}{3\sqrt{\pi}\,b^3}+\frac{d^2e^{-(a+bx)^2}}{3\sqrt{\pi}\,b^3}+\frac{(c+dx)^3\mathrm{Erf}(a+bx)}{3d}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)^2*Erf[a + b*x],x]
```

```
[Out] d^2/(3*b^3*E^(a + b*x)^2*Sqrt[Pi]) + (b*c - a*d)^2/(b^3*E^(a + b*x)^2*Sqrt[
Pi]) + (d*(b*c - a*d)*(a + b*x))/(b^3*E^(a + b*x)^2*Sqrt[Pi]) + (d^2*(a + b
*x)^2)/(3*b^3*E^(a + b*x)^2*Sqrt[Pi]) - (d*(b*c - a*d)*Erf[a + b*x])/(2*b^3
) - ((b*c - a*d)^3*Erf[a + b*x])/(3*b^3*d) + ((c + d*x)^3*Erf[a + b*x])/(3*
d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
```

```
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 2258

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*(u_), x_Symbol] :> Int[E
xpandLinearProduct[F^(a + b*(c + d*x)^n), u, c, d, x], x] /; FreeQ[{F, a, b
, c, d, n}, x] && PolynomialQ[u, x]
```

Rule 6496

```
Int[Erf[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(
c + d*x)^(m + 1)*(Erf[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(m
+ 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d, m
}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int (c+dx)^2\operatorname{erf}(a+bx)\,dx &= \frac{(c+dx)^3\operatorname{erf}(a+bx)}{3d} - \frac{(2b)\int e^{-(a+bx)^2}(c+dx)^3\,dx}{3d\sqrt{\pi}} \\
&= \frac{(c+dx)^3\operatorname{erf}(a+bx)}{3d} - \frac{(2b)\int \left(\frac{(bc-ad)^3e^{-(a+bx)^2}}{b^3} + \frac{3d(bc-ad)^2e^{-(a+bx)^2}(a+bx)}{b^3} + \frac{3d^2(bc-\cdots}{\cdots}\right.}{3d\sqrt{\pi}} \\
&= \frac{(c+dx)^3\operatorname{erf}(a+bx)}{3d} - \frac{(2d^2)\int e^{-(a+bx)^2}(a+bx)^3\,dx}{3b^2\sqrt{\pi}} - \frac{(2d(bc-ad))\int e^{-(a+bx)^2\cdots}}{b^2\sqrt{\pi}} \\
&= \frac{(bc-ad)^2e^{-(a+bx)^2}}{b^3\sqrt{\pi}} + \frac{d(bc-ad)e^{-(a+bx)^2}(a+bx)}{b^3\sqrt{\pi}} + \frac{d^2e^{-(a+bx)^2}(a+bx)^2}{3b^3\sqrt{\pi}} - \frac{(bc\cdots}{\cdots} \\
&= \frac{d^2e^{-(a+bx)^2}}{3b^3\sqrt{\pi}} + \frac{(bc-ad)^2e^{-(a+bx)^2}}{b^3\sqrt{\pi}} + \frac{d(bc-ad)e^{-(a+bx)^2}(a+bx)}{b^3\sqrt{\pi}} + \frac{d^2e^{-(a+bx)^2}(a\cdots}{3b^3\sqrt{\pi}}
\end{aligned}$$

Mathematica [A]
time = 0.14, size = 138, normalized size = 0.72

$$\frac{\frac{2e^{-(a+bx)^2}\left((1+a^2)d^2-abd(3c+dx)+b^2(3c^2+3cdx+d^2x^2)\right)}{\sqrt{\pi}} + \left(-3bcd-6a^2bcd+2a^3d^2+3a(2b^2c^2+d^2)+2b^3x(3c^2+3cdx+d^2x^2)\right)\operatorname{Erf}(a+bx)}{6b^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^2*Erf[a + b*x],x]
[Out] ((2*((1 + a^2)*d^2 - a*b*d*(3*c + d*x) + b^2*(3*c^2 + 3*c*d*x + d^2*x^2)))/
(E^(a + b*x)^2*Sqrt[Pi]) + (-3*b*c*d - 6*a^2*b*c*d + 2*a^3*d^2 + 3*a*(2*b^2
*c^2 + d^2) + 2*b^3*x*(3*c^2 + 3*c*d*x + d^2*x^2))*Erf[a + b*x])/(6*b^3)
```

Maple [A]
time = 0.74, size = 285, normalized size = 1.48

method	result
derivativedivides	$-\frac{\operatorname{erf}(bx+a)(ad-cb-d(bx+a))^3}{3b^2d}+\frac{a^3d^3\sqrt{\pi}\,\operatorname{erf}(bx+a)}{3}-\frac{b^3c^3\sqrt{\pi}\,\operatorname{erf}(bx+a)}{3}-\frac{2d^3\left(-\frac{e^{-(bx+a)^2}(bx+a)^2}{2}-\frac{e^{-(bx+a)^2}}{2}\right)}{3}+2a$
default	$-\frac{\operatorname{erf}(bx+a)(ad-cb-d(bx+a))^3}{3b^2d}+\frac{a^3d^3\sqrt{\pi}\,\operatorname{erf}(bx+a)}{3}-\frac{b^3c^3\sqrt{\pi}\,\operatorname{erf}(bx+a)}{3}-\frac{2d^3\left(-\frac{e^{-(bx+a)^2}(bx+a)^2}{2}-\frac{e^{-(bx+a)^2}}{2}\right)}{3}+2a$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^2*erf(b*x+a),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*(-1/3*erf(b*x+a)*(a*d-c*b-d*(b*x+a))^3/b^2/d+2/3/Pi^(1/2)/b^2/d*(1/2*a^
3*d^3*Pi^(1/2)*erf(b*x+a)-1/2*b^3*c^3*Pi^(1/2)*erf(b*x+a)-d^3*(-1/2/exp((b*
x+a)^2)*(b*x+a)^2-1/2/exp((b*x+a)^2))+3*a*d^3*(-1/2*(b*x+a)/exp((b*x+a)^2)+
1/4*Pi^(1/2)*erf(b*x+a))+3/2*a^2*d^3/exp((b*x+a)^2)+3/2*a*b^2*c^2*d*Pi^(1/2
)*erf(b*x+a)-3/2*a^2*b*c*d^2*Pi^(1/2)*erf(b*x+a)-3*b*c*d^2*(-1/2*(b*x+a)/ex
p((b*x+a)^2)+1/4*Pi^(1/2)*erf(b*x+a))+3/2*b^2*c^2*d/exp((b*x+a)^2)-3*a*b*c*
d^2/exp((b*x+a)^2)))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erf(b*x+a),x, algorithm="maxima")
```

```
[Out] 1/3*(d^2*x^3 + 3*c*d*x^2 + 3*c^2*x)*erf(b*x + a) - 1/3*integrate(2*(b*d^2*x
^3 + 3*b*c*d*x^2 + 3*b*c^2*x)*e^(-b^2*x^2 - 2*a*b*x - a^2), x)/sqrt(pi)
```

Fricas [A]
time = 0.35, size = 163, normalized size = 0.85

$$\frac{2\sqrt{\pi}\,(b^2d^2x^2+3\,b^2c^2-3\,abcd+(a^2+1)d^2+(3\,b^2cd-abd^2)x)e^{(-b^2x^2-2\,abx-a^2)}+(2\,\pi b^3d^2x^3+6\,\pi b^3cdx^2+6\,\pi b^3c^2x+\pi(6\,ab^2c^2-3\,(2\,a^2+1)bcd+(2\,a^3+3\,a)d^2))\operatorname{erf}(bx+a)}{6\,\pi b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erf(b*x+a),x, algorithm="fricas")
```

```
[Out] 1/6*(2*sqrt(pi)*(b^2*d^2*x^2 + 3*b^2*c^2 - 3*a*b*c*d + (a^2 + 1)*d^2 + (3*b
^2*c*d - a*b*d^2)*x)*e^(-b^2*x^2 - 2*a*b*x - a^2) + (2*pi*b^3*d^2*x^3 + 6*p
```

```
i*b^3*c*d*x^2 + 6*pi*b^3*c^2*x + pi*(6*a*b^2*c^2 - 3*(2*a^2 + 1)*b*c*d + (2
*a^3 + 3*a)*d^2))*erf(b*x + a))/(pi*b^3)
```

Sympy [B] Leaf count of result is larger than twice the leaf count of optimal. 398 vs. $2(165) = 330$.
time = 1.03, size = 398, normalized size = 2.07

$$\begin{cases} \frac{a^3d^2 \operatorname{erf}(a+bx)}{3b^3} - \frac{a^2cd \operatorname{erf}(a+bx)}{b^2} + \frac{a^2d^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{3\sqrt{\pi}\,b^3} + \frac{ac^2 \operatorname{erf}(a+bx)}{b} - \frac{acde^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}\,b^2} - \frac{ad^2xe^{-a^2}e^{-b^2x^2}e^{-2abx}}{3\sqrt{\pi}\,b^2} + \frac{ad^2 \operatorname{erf}(a+bx)}{2b^3} + c^2x \operatorname{erf}(a+bx) + cdx^2 \operatorname{erf}(a+bx) + \frac{d^2x^3 \operatorname{erf}(a+bx)}{3} + \frac{c^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}\,b} + \frac{cdxe^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}\,b} + \frac{d^2x^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{3\sqrt{\pi}\,b} - \frac{cd \operatorname{erf}(a+bx)}{2b^2} + \frac{d^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{3\sqrt{\pi}\,b^3} & \text{for}\ b \neq 0 \\ \left(c^2x + cdx^2 + \frac{d^2x^3}{3}\right) \operatorname{erf}(a) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**2*erf(b*x+a),x)
```

```
[Out] Piecewise((a**3*d**2*erf(a + b*x)/(3*b**3) - a**2*c*d*erf(a + b*x)/b**2 + a
**2*d**2*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(3*sqrt(pi)*b**3) + a*c**
2*erf(a + b*x)/b - a*c*d*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(sqrt(pi)
*b**2) - a*d**2*x*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(3*sqrt(pi)*b**2
) + a*d**2*erf(a + b*x)/(2*b**3) + c**2*x*erf(a + b*x) + c*d*x**2*erf(a + b
*x) + d**2*x**3*erf(a + b*x)/3 + c**2*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b
*x)/(sqrt(pi)*b) + c*d*x*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(sqrt(pi)
*b) + d**2*x**2*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(3*sqrt(pi)*b) - c
*d*erf(a + b*x)/(2*b**2) + d**2*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(3
*sqrt(pi)*b**3), Ne(b, 0)), ((c**2*x + c*d*x**2 + d**2*x**3/3)*erf(a), True
))
```

Giac [A]
time = 0.41, size = 270, normalized size = 1.41

$$\frac{(dx+c)^3 \operatorname{erf}(bx+a)}{3\,d} + \frac{2\,\pi c^3 \operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right) - 6\,\sqrt{\pi}\left(\frac{\sqrt{\pi}\,a \operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b} - \frac{e^{\left(-b^2x^2-2\,abx-a^2\right)}}{b}\right)c^2d + \frac{3\,\sqrt{\pi}\left(\frac{\sqrt{\pi}\,\left(2\,a^2+1\right) \operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b} + \frac{2\,\left(b\left(x+\frac{a}{b}\right)-2\,a\right)e^{\left(-b^2x^2-2\,abx-a^2\right)}}{b}\right)cd^2}{b} - \frac{\sqrt{\pi}\left(\frac{\sqrt{\pi}\,\left(2\,a^3+3\,a\right) \operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b} - \frac{2\,\left(b^2\left(x+\frac{a}{b}\right)^2-3\,ab\left(x+\frac{a}{b}\right)+3\,a^2+1\right)e^{\left(-b^2x^2-2\,abx-a^2\right)}}{b}\right)d^3}{b^2}}{6\,\pi d}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erf(b*x+a),x, algorithm="giac")
```

```
[Out] 1/3*(d*x + c)^3*erf(b*x + a)/d + 1/6*(2*pi*c^3*erf(-b*(x + a/b)) - 6*sqrt(p
i)*(sqrt(pi)*a*erf(-b*(x + a/b))/b - e^(-b^2*x^2 - 2*a*b*x - a^2)/b)*c^2*d
+ 3*sqrt(pi)*(sqrt(pi)*(2*a^2 + 1)*erf(-b*(x + a/b))/b + 2*(b*(x + a/b) - 2
*a)*e^(-b^2*x^2 - 2*a*b*x - a^2)/b)*c*d^2/b - sqrt(pi)*(sqrt(pi)*(2*a^3 + 3
*a)*erf(-b*(x + a/b))/b - 2*(b^2*(x + a/b)^2 - 3*a*b*(x + a/b) + 3*a^2 + 1)
*e^(-b^2*x^2 - 2*a*b*x - a^2)/b)*d^3/b^2)/(pi*d)
```

Mupad [B]
time = 0.72, size = 204, normalized size = 1.06

$$\frac{\frac{{\mathrm{e}}^{-a^2-2\,a\,b\,x-b^2\,x^2}\,\left(a^2\,d^2-3\,a\,b\,c\,d+3\,b^2\,c^2+d^2\right)}{b^3}+\frac{d^2\,x^2\,{\mathrm{e}}^{-a^2-2\,a\,b\,x-b^2\,x^2}}{b}-\frac{x\,{\mathrm{e}}^{-a^2-2\,a\,b\,x-b^2\,x^2}\,\left(a\,d^2-3\,b\,c\,d\right)}{b^2}}{3\,\sqrt{\pi}}+\mathrm{erf}\left(a+b\,x\right)\,\left(c^2\,x+c\,d\,x^2+\frac{d^2\,x^3}{3}\right)-\frac{\mathrm{erfi}\left(a\,1{}\mathrm{i}+b\,x\,1{}\mathrm{i}\right)\,\left(2\,a^3\,d^2-6\,a^2\,b\,c\,d+6\,a\,b^2\,c^2+3\,a\,d^2-3\,b\,c\,d\right)\,1{}\mathrm{i}}{6\,b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(a + b*x)*(c + d*x)^2,x)
```

```
[Out] ((exp(- a^2 - b^2*x^2 - 2*a*b*x)*(d^2 + a^2*d^2 + 3*b^2*c^2 - 3*a*b*c*d))/b
^3 + (d^2*x^2*exp(- a^2 - b^2*x^2 - 2*a*b*x))/b - (x*exp(- a^2 - b^2*x^2 -
2*a*b*x)*(a*d^2 - 3*b*c*d))/b^2)/(3*pi^(1/2)) + erf(a + b*x)*(c^2*x + (d^2*
x^3)/3 + c*d*x^2) - (erfi(a*1i + b*x*1i)*(3*a*d^2 + 2*a^3*d^2 + 6*a*b^2*c^2
 - 3*b*c*d - 6*a^2*b*c*d)*1i)/(6*b^3)
```

3.17 $\int (c+dx)\mathbf{Erf}(a+bx)\,dx$

Optimal. Leaf size=118

$$\frac{(bc-ad)e^{-(a+bx)^2}}{b^2\sqrt{\pi}}+\frac{de^{-(a+bx)^2}(a+bx)}{2b^2\sqrt{\pi}}-\frac{d\mathrm{Erf}(a+bx)}{4b^2}-\frac{(bc-ad)^2\mathrm{Erf}(a+bx)}{2b^2d}+\frac{(c+dx)^2\mathrm{Erf}(a+bx)}{2d}$$

```
[Out] -1/4*d*erf(b*x+a)/b^2-1/2*(-a*d+b*c)^2*erf(b*x+a)/b^2/d+1/2*(d*x+c)^2*erf(b
*x+a)/d+(-a*d+b*c)/b^2/exp((b*x+a)^2)/Pi^(1/2)+1/2*d*(b*x+a)/b^2/exp((b*x+a
)^2)/Pi^(1/2)
```

Rubi [A]
time = 0.08, antiderivative size = 118, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.417$, Rules used = {6496, 2258, 2236, 2240, 2243}

$$-\frac{(bc-ad)^2\mathrm{Erf}(a+bx)}{2b^2d}+\frac{e^{-(a+bx)^2}(bc-ad)}{\sqrt{\pi}\,b^2}-\frac{d\mathrm{Erf}(a+bx)}{4b^2}+\frac{de^{-(a+bx)^2}(a+bx)}{2\sqrt{\pi}\,b^2}+\frac{(c+dx)^2\mathrm{Erf}(a+bx)}{2d}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)*Erf[a + b*x],x]
```

```
[Out] (b*c - a*d)/(b^2*E^(a + b*x)^2*Sqrt[Pi]) + (d*(a + b*x))/(2*b^2*E^(a + b*x)
^2*Sqrt[Pi]) - (d*Erf[a + b*x])/(4*b^2) - ((b*c - a*d)^2*Erf[a + b*x])/(2*b
^2*d) + ((c + d*x)^2*Erf[a + b*x])/(2*d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
```

```
0])
```

Rule 2258

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*(u_), x_Symbol] :> Int[E
xpandLinearProduct[F^(a + b*(c + d*x)^n), u, c, d, x], x] /; FreeQ[{F, a, b
, c, d, n}, x] && PolynomialQ[u, x]
```

Rule 6496

```
Int[Erf[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[(
c + d*x)^(m + 1)*(Erf[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(m
+ 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d, m
}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int (c+dx)\mathrm{erf}(a+bx)\,dx &= \frac{(c+dx)^2\mathrm{erf}(a+bx)}{2d} - \frac{b\int e^{-(a+bx)^2}(c+dx)^2\,dx}{d\sqrt{\pi}}\\ &= \frac{(c+dx)^2\mathrm{erf}(a+bx)}{2d} - \frac{b\int \left(\frac{(bc-ad)^2e^{-(a+bx)^2}}{b^2} + \frac{2d(bc-ad)e^{-(a+bx)^2}(a+bx)}{b^2} + \frac{d^2e^{-(a+bx)^2}}{b^2}\right.}{d\sqrt{\pi}}\\ &= \frac{(c+dx)^2\mathrm{erf}(a+bx)}{2d} - \frac{d\int e^{-(a+bx)^2}(a+bx)^2\,dx}{b\sqrt{\pi}} - \frac{(2(bc-ad))\int e^{-(a+bx)^2}(a+}{b\sqrt{\pi}}\\ &= \frac{(bc-ad)e^{-(a+bx)^2}}{b^2\sqrt{\pi}} + \frac{de^{-(a+bx)^2}(a+bx)}{2b^2\sqrt{\pi}} - \frac{(bc-ad)^2\mathrm{erf}(a+bx)}{2b^2d} + \frac{(c+dx)^2\mathrm{erf}}{2d}\\ &= \frac{(bc-ad)e^{-(a+bx)^2}}{b^2\sqrt{\pi}} + \frac{de^{-(a+bx)^2}(a+bx)}{2b^2\sqrt{\pi}} - \frac{d\mathrm{erf}(a+bx)}{4b^2} - \frac{(bc-ad)^2\mathrm{erf}(a+bx)}{2b^2d}\end{aligned}$$

Mathematica [A]
time = 0.06, size = 88, normalized size = 0.75

$$\frac{e^{-(a+bx)^2}\left(4bc-2ad+2bdx-e^{(a+bx)^2}\sqrt{\pi}\left(-4abc+d+2a^2d-4b^2cx-2b^2dx^2\right)\mathrm{Erf}(a+bx)\right)}{4b^2\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)*Erf[a + b*x],x]
```

```
[Out] (4*b*c - 2*a*d + 2*b*d*x - E^(a + b*x)^2*Sqrt[Pi]*(-4*a*b*c + d + 2*a^2*d -
 4*b^2*c*x - 2*b^2*d*x^2)*Erf[a + b*x])/(4*b^2*E^(a + b*x)^2*Sqrt[Pi])
```

Maple [A]
time = 0.43, size = 112, normalized size = 0.95

method	result	s
derivativedivides	$\frac{-\frac{\operatorname{erf}(bx+a)\left(da(bx+a)-cb(bx+a)-\frac{d(bx+a)^2}{2}\right)}{b}+\frac{-d\left(-\frac{(bx+a)\mathrm{e}^{-(bx+a)^2}}{2}+\frac{\sqrt{\pi}\,\operatorname{erf}(bx+a)}{4}\right)+\mathrm{e}^{-(bx+a)^2}bc-da\,\mathrm{e}^{-(bx+a)^2}}{\sqrt{\pi}\,b}}{b}$	1
default	$\frac{-\frac{\operatorname{erf}(bx+a)\left(da(bx+a)-cb(bx+a)-\frac{d(bx+a)^2}{2}\right)}{b}+\frac{-d\left(-\frac{(bx+a)\mathrm{e}^{-(bx+a)^2}}{2}+\frac{\sqrt{\pi}\,\operatorname{erf}(bx+a)}{4}\right)+\mathrm{e}^{-(bx+a)^2}bc-da\,\mathrm{e}^{-(bx+a)^2}}{\sqrt{\pi}\,b}}{b}$	1

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)*erf(b*x+a),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*(-erf(b*x+a)/b*(d*a*(b*x+a)-c*b*(b*x+a)-1/2*d*(b*x+a)^2)+1/Pi^(1/2)/b*(
-d*(-1/2*(b*x+a)/exp((b*x+a)^2)+1/4*Pi^(1/2)*erf(b*x+a))+c*b/exp((b*x+a)^2)
-d*a/exp((b*x+a)^2)))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erf(b*x+a),x, algorithm="maxima")
```

```
[Out] 1/2*(d*x^2 + 2*c*x)*erf(b*x + a) - integrate((b*d*x^2 + 2*b*c*x)*e^(-b^2*x^
2 - 2*a*b*x - a^2), x)/sqrt(pi)
```

Fricas [A]
time = 0.37, size = 91, normalized size = 0.77

$$\frac{2\sqrt{\pi}\,(bdx+2\,bc-ad)e^{\left(-b^2x^2-2\,abx-a^2\right)}+\left(2\,\pi b^2dx^2+4\,\pi b^2cx+\pi(4\,abc-(2\,a^2+1)d)\right)\operatorname{erf}(bx+a)}{4\,\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erf(b*x+a),x, algorithm="fricas")
```

```
[Out] 1/4*(2*sqrt(pi)*(b*d*x + 2*b*c - a*d)*e^(-b^2*x^2 - 2*a*b*x - a^2) + (2*pi*
b^2*d*x^2 + 4*pi*b^2*c*x + pi*(4*a*b*c - (2*a^2 + 1)*d))*erf(b*x + a))/(pi*
b^2)
```

Sympy [A]
time = 0.54, size = 178, normalized size = 1.51

$$\begin{cases} -\frac{a^2d\operatorname{erf}(a+bx)}{2b^2}+\frac{ac\operatorname{erf}(a+bx)}{b}-\frac{ade^{-a^2}e^{-b^2x^2}e^{-2abx}}{2\sqrt{\pi}\,b^2}+cx\operatorname{erf}(a+bx)+\frac{dx^2\operatorname{erf}(a+bx)}{2}+\frac{ce^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}\,b}+\frac{dxe^{-a^2}e^{-b^2x^2}e^{-2abx}}{2\sqrt{\pi}\,b}-\frac{d\operatorname{erf}(a+bx)}{4b^2} & \text{for } b\neq 0 \\ \left(cx+\frac{dx^2}{2}\right)\operatorname{erf}(a) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erf(b*x+a),x)
```

```
[Out] Piecewise((-a**2*d*erf(a + b*x)/(2*b**2) + a*c*erf(a + b*x)/b - a*d*exp(-a*
*2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(2*sqrt(pi)*b**2) + c*x*erf(a + b*x) + d*
x**2*erf(a + b*x)/2 + c*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(sqrt(pi)*
b) + d*x*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(2*sqrt(pi)*b) - d*erf(a
+ b*x)/(4*b**2), Ne(b, 0)), ((c*x + d*x**2/2)*erf(a), True))
```

Giac [A]
time = 0.41, size = 149, normalized size = 1.26

$$\frac{1}{2}\left(dx^2+2\,cx\right)\operatorname{erf}\left(bx+a\right)-\frac{4\,\sqrt{\pi}\left(\frac{\sqrt{\pi}\,a\operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b}-\frac{e^{\left(-b^2x^2-2\,abx-a^2\right)}}{b}\right)c-\frac{\sqrt{\pi}\left(\frac{\sqrt{\pi}\,\left(2\,a^2+1\right)\operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b}+\frac{2\left(b\left(x+\frac{a}{b}\right)-2\,a\right)e^{\left(-b^2x^2-2\,abx-a^2\right)}}{b}\right)d}{b}}{4\,\pi}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erf(b*x+a),x, algorithm="giac")
```

```
[Out] 1/2*(d*x^2 + 2*c*x)*erf(b*x + a) - 1/4*(4*sqrt(pi)*(sqrt(pi)*a*erf(-b*(x +
a/b))/b - e^(-b^2*x^2 - 2*a*b*x - a^2)/b)*c - sqrt(pi)*(sqrt(pi)*(2*a^2 + 1
)*erf(-b*(x + a/b))/b + 2*(b*(x + a/b) - 2*a)*e^(-b^2*x^2 - 2*a*b*x - a^2)/
b)*d/b)/pi
```

Mupad [B]
time = 0.45, size = 126, normalized size = 1.07

$$\operatorname{erf}(a+b\,x)\,\left(\frac{d\,x^2}{2}+c\,x\right)-\frac{\frac{\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}\,\left(\frac{a\,d}{2}-b\,c\right)}{b^2}-\frac{d\,x\,\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}}{2\,b}}{\sqrt{\pi}}+\frac{\sqrt{\pi}\,\operatorname{erfi}(a\,1\mathrm{i}+b\,x\,1\mathrm{i})\,\left(\frac{2\,d\,a^2+d}{2\,\sqrt{\pi}}-\frac{2\,a\,b\,c}{\sqrt{\pi}}\right)\,1\mathrm{i}}{2\,b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(a + b*x)*(c + d*x),x)
```

```
[Out] erf(a + b*x)*(c*x + (d*x^2)/2) - ((exp(- a^2 - b^2*x^2 - 2*a*b*x)*((a*d)/2
- b*c))/b^2 - (d*x*exp(- a^2 - b^2*x^2 - 2*a*b*x))/(2*b))/pi^(1/2) + (pi^(1
/2)*erfi(a*1i + b*x*1i)*((d + 2*a^2*d)/(2*pi^(1/2)) - (2*a*b*c)/pi^(1/2))*1
i)/(2*b^2)
```

3.18 $\int \mathbf{Erf}(a+bx)\,dx$

Optimal. Leaf size=36

$$\frac{e^{-(a+bx)^2}}{b\sqrt{\pi}}+\frac{(a+bx)\mathrm{Erf}(a+bx)}{b}$$

```
[Out] (b*x+a)*erf(b*x+a)/b+1/b/exp((b*x+a)^2)/Pi^(1/2)
```

Rubi [A]
time = 0.01, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.167, Rules used = {6484}

$$\frac{(a+bx)\mathrm{Erf}(a+bx)}{b}+\frac{e^{-(a+bx)^2}}{\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[a + b*x],x]
```

```
[Out] 1/(b*E^(a + b*x)^2*Sqrt[Pi]) + ((a + b*x)*Erf[a + b*x])/b
```

Rule 6484

```
Int[Erf[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[(a + b*x)*(Erf[a + b*x]/b),
x] + Simp[1/(b*Sqrt[Pi]*E^(a + b*x)^2), x] /; FreeQ[{a, b}, x]
```

Rubi steps

$$\int \mathrm{erf}(a+bx)\,dx=\frac{e^{-(a+bx)^2}}{b\sqrt{\pi}}+\frac{(a+bx)\mathrm{erf}(a+bx)}{b}$$

Mathematica [A]
time = 0.03, size = 35, normalized size = 0.97

$$\frac{e^{-(a+bx)^2}}{b\sqrt{\pi}}+\left(\frac{a}{b}+x\right)\mathrm{Erf}(a+bx)$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[a + b*x],x]
```

```
[Out] 1/(b*E^(a + b*x)^2*Sqrt[Pi]) + (a/b + x)*Erf[a + b*x]
```

Maple [A]
time = 0.25, size = 32, normalized size = 0.89

method	result	size
derivativedivides	$\frac{\mathrm{erf}(bx+a)(bx+a)+\frac{\mathrm{e}^{-(bx+a)^2}}{\sqrt{\pi}}}{b}$	32
default	$\frac{\mathrm{erf}(bx+a)(bx+a)+\frac{\mathrm{e}^{-(bx+a)^2}}{\sqrt{\pi}}}{b}$	32

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x+a),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*(erf(b*x+a)*(b*x+a)+1/Pi^(1/2)*exp(-(b*x+a)^2))
```

Maxima [A]
time = 0.25, size = 31, normalized size = 0.86

$$\frac{(bx+a)\,\mathrm{erf}\,(bx+a)+\frac{e^{\left(-(bx+a)^2\right)}}{\sqrt{\pi}}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a),x, algorithm="maxima")
```

```
[Out] ((b*x + a)*erf(b*x + a) + e^(-(b*x + a)^2)/sqrt(pi))/b
```

Fricas [A]
time = 0.34, size = 47, normalized size = 1.31

$$\frac{(\pi bx+\pi a)\,\mathrm{erf}\,(bx+a)+\sqrt{\pi}\,e^{\left(-b^2x^2-2\,abx-a^2\right)}}{\pi b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a),x, algorithm="fricas")
```

```
[Out] ((pi*b*x + pi*a)*erf(b*x + a) + sqrt(pi)*e^(-b^2*x^2 - 2*a*b*x - a^2))/(pi*
b)
```

Sympy [A]
time = 0.31, size = 53, normalized size = 1.47

$$\begin{cases} \frac{a\,\mathrm{erf}\,(a+bx)}{b}+x\,\mathrm{erf}\,(a+bx)+\frac{e^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}\,b} & \text{for}\ b\neq 0\\ x\,\mathrm{erf}\,(a) & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a),x)
```

```
[Out] Piecewise((a*erf(a + b*x)/b + x*erf(a + b*x) + exp(-a**2)*exp(-b**2*x**2)*e
xp(-2*a*b*x)/(sqrt(pi)*b), Ne(b, 0)), (x*erf(a), True))
```

Giac [A]
time = 0.40, size = 59, normalized size = 1.64

$$x\,\mathrm{erf}\left(bx+a\right)-\frac{\frac{\sqrt{\pi}\,a\,\mathrm{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b}-\frac{e^{\left(-b^2x^2-2\,abx-a^2\right)}}{b}}{\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a),x, algorithm="giac")
```

```
[Out] x*erf(b*x + a) - (sqrt(pi)*a*erf(-b*(x + a/b))/b - e^(-b^2*x^2 - 2*a*b*x -
a^2)/b)/sqrt(pi)
```

Mupad [B]
time = 0.22, size = 48, normalized size = 1.33

$$x\,\mathrm{erf}(a+b\,x)+\frac{a\,\mathrm{erf}(a+b\,x)}{b}+\frac{\mathrm{e}^{-b^2\,x^2}\,\mathrm{e}^{-a^2}\,\mathrm{e}^{-2\,a\,b\,x}}{b\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(a + b*x),x)
```

```
[Out] x*erf(a + b*x) + (a*erf(a + b*x))/b + (exp(-b^2*x^2)*exp(-a^2)*exp(-2*a*b*x
))/(b*pi^(1/2))
```

3.19 $\int \frac{\mathbf{Erf}(a+bx)}{c+dx}\,dx$

Optimal. Leaf size=17

$$\text{Int}\left(\frac{\text{Erf}(a+bx)}{c+dx},x\right)$$

```
[Out] Unintegrable(erf(b*x+a)/(d*x+c),x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\text{Erf}(a+bx)}{c+dx}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erf[a + b*x]/(c + d*x),x]
```

```
[Out] Defer[Int][Erf[a + b*x]/(c + d*x), x]
```

Rubi steps

$$\int \frac{\text{erf}(a+bx)}{c+dx}\,dx = \int \frac{\text{erf}(a+bx)}{c+dx}\,dx$$

Mathematica [A]
time = 0.84, size = 0, normalized size = 0.00

$$\int \frac{\text{Erf}(a+bx)}{c+dx}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erf[a + b*x]/(c + d*x),x]
```

```
[Out] Integrate[Erf[a + b*x]/(c + d*x), x]
```

Maple [A]
time = 0.16, size = 0, normalized size = 0.00

$$\int \frac{\text{erf}\,(bx+a)}{dx+c}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x+a)/(d*x+c),x)
[Out] int(erf(b*x+a)/(d*x+c),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)/(d*x+c),x, algorithm="maxima")
[Out] integrate(erf(b*x + a)/(d*x + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)/(d*x+c),x, algorithm="fricas")
[Out] integral(erf(b*x + a)/(d*x + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}\left(a+bx\right)}{c+dx}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)/(d*x+c),x)
[Out] Integral(erf(a + b*x)/(c + d*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)/(d*x+c),x, algorithm="giac")
[Out] integrate(erf(b*x + a)/(d*x + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.06

$$\int \frac{\operatorname{erf}(a+b\,x)}{c+d\,x}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(a + b*x)/(c + d*x),x)
[Out] int(erf(a + b*x)/(c + d*x), x)
```

3.20 $\int \frac{\mathbf{Erf}(a+bx)}{(c+dx)^2}\,dx$

Optimal. Leaf size=52

$$-\frac{\operatorname{Erf}(a+bx)}{d(c+dx)}+\frac{2b\operatorname{Int}\left(\frac{e^{-(a+bx)^2}}{c+dx},x\right)}{d\sqrt{\pi}}$$

[Out] -erf(b*x+a)/d/(d*x+c)+2*b*Unintegrable(1/exp((b*x+a)^2)/(d*x+c),x)/d/Pi^(1/2)

Rubi [A]
time = 0.03, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.000, Rules used = {}

$$\int \frac{\operatorname{Erf}(a+bx)}{(c+dx)^2}\,dx$$

Verification is not applicable to the result.

[In] Int[Erf[a + b*x]/(c + d*x)^2,x]

[Out] -(Erf[a + b*x]/(d*(c + d*x))) + (2*b*Defer[Int][1/(E^(a + b*x)^2*(c + d*x)), x])/(d*Sqrt[Pi])

Rubi steps

$$\int \frac{\operatorname{erf}(a+bx)}{(c+dx)^2}\,dx=-\frac{\operatorname{erf}(a+bx)}{d(c+dx)}+\frac{(2b)\int \frac{e^{-(a+bx)^2}}{c+dx}\,dx}{d\sqrt{\pi}}$$

Mathematica [A]
time = 0.63, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{Erf}(a+bx)}{(c+dx)^2}\,dx$$

Verification is not applicable to the result.

[In] Integrate[Erf[a + b*x]/(c + d*x)^2,x]

[Out] Integrate[Erf[a + b*x]/(c + d*x)^2, x]

Maple [A]
time = 0.24, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}(bx+a)}{(dx+c)^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x+a)/(d*x+c)^2,x)
```

```
[Out] int(erf(b*x+a)/(d*x+c)^2,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)/(d*x+c)^2,x, algorithm="maxima")
```

```
[Out] 2*b*integrate(e^(-b^2*x^2 - 2*a*b*x)/(sqrt(pi)*d^2*x*e^(a^2) + sqrt(pi)*c*d
*e^(a^2)), x) - erf(b*x + a)/(d^2*x + c*d)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)/(d*x+c)^2,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x + a)/(d^2*x^2 + 2*c*d*x + c^2), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}{\left(a + bx \right)}}{\left(c + dx\right)^{2}}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)/(d*x+c)**2,x)
```

```
[Out] Integral(erf(a + b*x)/(c + d*x)**2, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)/(d*x+c)^2,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x + a)/(d*x + c)^2, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\operatorname{erf}(a+b\,x)}{(c+d\,x)^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(a + b*x)/(c + d*x)^2,x)
[Out] int(erf(a + b*x)/(c + d*x)^2, x)
```

3.21 $\int \frac{\mathbf{Erf}(a+bx)}{(c+dx)^3}\,dx$

Optimal. Leaf size=107

$$-\frac{be^{-(a+bx)^2}}{d^2\sqrt{\pi}\,(c+dx)}-\frac{b^2\mathrm{Erf}(a+bx)}{d^3}-\frac{\mathrm{Erf}(a+bx)}{2d(c+dx)^2}+\frac{2b^2(bc-ad)\mathrm{Int}\left(\frac{e^{-(a+bx)^2}}{c+dx},x\right)}{d^3\sqrt{\pi}}$$

```
[Out] -b^2*erf(b*x+a)/d^3-1/2*erf(b*x+a)/d/(d*x+c)^2-b/d^2/exp((b*x+a)^2)/(d*x+c)
/Pi^(1/2)+2*b^2*(-a*d+b*c)*Unintegrable(1/exp((b*x+a)^2)/(d*x+c),x)/d^3/Pi^
(1/2)
```

Rubi [A]
time = 0.06, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.000, Rules used = {}

$$\int \frac{\mathrm{Erf}(a+bx)}{(c+dx)^3}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erf[a + b*x]/(c + d*x)^3,x]
```

```
[Out] -(b/(d^2*E^(a + b*x)^2*Sqrt[Pi]*(c + d*x))) - (b^2*Erf[a + b*x])/d^3 - Erf[
a + b*x]/(2*d*(c + d*x)^2) + (2*b^2*(b*c - a*d)*Defer[Int][1/(E^(a + b*x)^2
*(c + d*x)), x])/(d^3*Sqrt[Pi])
```

Rubi steps

$$\begin{aligned}
\int \frac{\mathrm{erf}(a+bx)}{(c+dx)^3}\,dx &= -\frac{\mathrm{erf}(a+bx)}{2d(c+dx)^2}+\frac{b\int \frac{e^{-(a+bx)^2}}{(c+dx)^2}\,dx}{d\sqrt{\pi}}\\
&= -\frac{be^{-(a+bx)^2}}{d^2\sqrt{\pi}\,(c+dx)}-\frac{\mathrm{erf}(a+bx)}{2d(c+dx)^2}-\frac{\left(2b^3\right)\int e^{-(a+bx)^2}\,dx}{d^3\sqrt{\pi}}+\frac{\left(2b^2(bc-ad)\right)\int \frac{e^{-(a+bx)^2}}{c+dx}\,dx}{d^3\sqrt{\pi}}\\
&= -\frac{be^{-(a+bx)^2}}{d^2\sqrt{\pi}\,(c+dx)}-\frac{b^2\mathrm{erf}(a+bx)}{d^3}-\frac{\mathrm{erf}(a+bx)}{2d(c+dx)^2}+\frac{\left(2b^2(bc-ad)\right)\int \frac{e^{-(a+bx)^2}}{c+dx}\,dx}{d^3\sqrt{\pi}}
\end{aligned}$$

Mathematica [A]
time = 1.61, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{Erf}(a+bx)}{(c+dx)^3}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erf[a + b*x]/(c + d*x)^3,x]
```

```
[Out] Integrate[Erf[a + b*x]/(c + d*x)^3, x]
```

Maple [A]
time = 0.20, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}\left(bx+a\right)}{\left(dx+c\right)^{3}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x+a)/(d*x+c)^3,x)
```

```
[Out] int(erf(b*x+a)/(d*x+c)^3,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)/(d*x+c)^3,x, algorithm="maxima")
```

```
[Out] b*integrate(e^(-b^2*x^2 - 2*a*b*x)/(sqrt(pi)*d^3*x^2*e^(a^2) + 2*sqrt(pi)*c
*d^2*x*e^(a^2) + sqrt(pi)*c^2*d*e^(a^2)), x) - 1/2*erf(b*x + a)/(d^3*x^2 +
2*c*d^2*x + c^2*d)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)/(d*x+c)^3,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x + a)/(d^3*x^3 + 3*c*d^2*x^2 + 3*c^2*d*x + c^3), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}\left(a+bx\right)}{\left(c+dx\right)^{3}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)/(d*x+c)**3,x)
```

```
[Out] Integral(erf(a + b*x)/(c + d*x)**3, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)/(d*x+c)^3,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x + a)/(d*x + c)^3, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erf}(a+b\,x)}{{(c+d\,x)}^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(a + b*x)/(c + d*x)^3,x)
```

```
[Out] int(erf(a + b*x)/(c + d*x)^3, x)
```

3.22 $\int x^5 \mathbf{Erf}(bx)^2 \, dx$

Optimal. Leaf size=178

$$\frac{11e^{-2b^2x^2}}{12b^6\pi}+\frac{7e^{-2b^2x^2}x^2}{12b^4\pi}+\frac{e^{-2b^2x^2}x^4}{6b^2\pi}+\frac{5e^{-b^2x^2}x\text{Erf}(bx)}{4b^5\sqrt{\pi}}+\frac{5e^{-b^2x^2}x^3\text{Erf}(bx)}{6b^3\sqrt{\pi}}+\frac{e^{-b^2x^2}x^5\text{Erf}(bx)}{3b\sqrt{\pi}}-\frac{5\text{Erf}(bx)^2}{16b^6}+\frac{1}{6}x^6\text{Er}$$

```
[Out] 11/12/b^6/exp(2*b^2*x^2)/Pi+7/12*x^2/b^4/exp(2*b^2*x^2)/Pi+1/6*x^4/b^2/exp(
2*b^2*x^2)/Pi-5/16*erf(b*x)^2/b^6+1/6*x^6*erf(b*x)^2+5/4*x*erf(b*x)/b^5/exp
(b^2*x^2)/Pi^(1/2)+5/6*x^3*erf(b*x)/b^3/exp(b^2*x^2)/Pi^(1/2)+1/3*x^5*erf(b
*x)/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.19, antiderivative size = 178, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.600, Rules used = {6499, 6520, 6508, 30, 2240, 2243}

$$-\frac{5\text{Erf}(bx)^2}{16b^6}+\frac{x^5e^{-b^2x^2}\text{Erf}(bx)}{3\sqrt{\pi}\,b}+\frac{x^4e^{-2b^2x^2}}{6\pi b^2}+\frac{11e^{-2b^2x^2}}{12\pi b^6}+\frac{5xe^{-b^2x^2}\text{Erf}(bx)}{4\sqrt{\pi}\,b^5}+\frac{7x^2e^{-2b^2x^2}}{12\pi b^4}+\frac{5x^3e^{-b^2x^2}\text{Erf}(bx)}{6\sqrt{\pi}\,b^3}+\frac{1}{6}x^6\text{Erf}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[x^5*Erf[b*x]^2,x]
```

```
[Out] 11/(12*b^6*E^(2*b^2*x^2)*Pi) + (7*x^2)/(12*b^4*E^(2*b^2*x^2)*Pi) + x^4/(6*b
^2*E^(2*b^2*x^2)*Pi) + (5*x*Erf[b*x])/(4*b^5*E^(b^2*x^2)*Sqrt[Pi]) + (5*x^3
*Erf[b*x])/(6*b^3*E^(b^2*x^2)*Sqrt[Pi]) + (x^5*Erf[b*x])/(3*b*E^(b^2*x^2)*S
qrt[Pi]) - (5*Erf[b*x]^2)/(16*b^6) + (x^6*Erf[b*x]^2)/6
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
```

```
0])
```

Rule 6499

```
Int[Erf[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erf[b*x]^2/(
m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erf[b*x])/E^(b^
2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int x^5\operatorname{erf}(bx)^2\,dx &= \frac{1}{6}x^6\operatorname{erf}(bx)^2-\frac{(2b)\int e^{-b^2x^2}x^6\operatorname{erf}(bx)\,dx}{3\sqrt{\pi}}\\ &= \frac{e^{-b^2x^2}x^5\operatorname{erf}(bx)}{3b\sqrt{\pi}}+\frac{1}{6}x^6\operatorname{erf}(bx)^2-\frac{2\int e^{-2b^2x^2}x^5\,dx}{3\pi}-\frac{5\int e^{-b^2x^2}x^4\operatorname{erf}(bx)\,dx}{3b\sqrt{\pi}}\\ &= \frac{e^{-2b^2x^2}x^4}{6b^2\pi}+\frac{5e^{-b^2x^2}x^3\operatorname{erf}(bx)}{6b^3\sqrt{\pi}}+\frac{e^{-b^2x^2}x^5\operatorname{erf}(bx)}{3b\sqrt{\pi}}+\frac{1}{6}x^6\operatorname{erf}(bx)^2-\frac{2\int e^{-2b^2x^2}x^3\,dx}{3b^2\pi}-\frac{5\int e\\ &= \frac{7e^{-2b^2x^2}x^2}{12b^4\pi}+\frac{e^{-2b^2x^2}x^4}{6b^2\pi}+\frac{5e^{-b^2x^2}x\operatorname{erf}(bx)}{4b^5\sqrt{\pi}}+\frac{5e^{-b^2x^2}x^3\operatorname{erf}(bx)}{6b^3\sqrt{\pi}}+\frac{e^{-b^2x^2}x^5\operatorname{erf}(bx)}{3b\sqrt{\pi}}+\frac{1}{6}x^6\mathrm{er}\\ &= \frac{11e^{-2b^2x^2}}{12b^6\pi}+\frac{7e^{-2b^2x^2}x^2}{12b^4\pi}+\frac{e^{-2b^2x^2}x^4}{6b^2\pi}+\frac{5e^{-b^2x^2}x\operatorname{erf}(bx)}{4b^5\sqrt{\pi}}+\frac{5e^{-b^2x^2}x^3\operatorname{erf}(bx)}{6b^3\sqrt{\pi}}+\frac{e^{-b^2x^2}x^5\mathrm{erf}(}{3b\sqrt{\pi}}\\ &= \frac{11e^{-2b^2x^2}}{12b^6\pi}+\frac{7e^{-2b^2x^2}x^2}{12b^4\pi}+\frac{e^{-2b^2x^2}x^4}{6b^2\pi}+\frac{5e^{-b^2x^2}x\operatorname{erf}(bx)}{4b^5\sqrt{\pi}}+\frac{5e^{-b^2x^2}x^3\operatorname{erf}(bx)}{6b^3\sqrt{\pi}}+\frac{e^{-b^2x^2}x^5\mathrm{erf}(}{3b\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.03, size = 106, normalized size = 0.60

$$\frac{e^{-2b^2x^2}\left(44+28b^2x^2+8b^4x^4+4be^{b^2x^2}\sqrt{\pi}\,x(15+10b^2x^2+4b^4x^4)\operatorname{Erf}(bx)+e^{2b^2x^2}\pi(-15+8b^6x^6)\operatorname{Erf}(bx)^2\right)}{48b^6\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^5*Erf[b*x]^2,x]
```

```
[Out] (44 + 28*b^2*x^2 + 8*b^4*x^4 + 4*b*E^(b^2*x^2)*Sqrt[Pi]*x*(15 + 10*b^2*x^2
+ 4*b^4*x^4)*Erf[b*x] + E^(2*b^2*x^2)*Pi*(-15 + 8*b^6*x^6)*Erf[b*x]^2)/(48*
b^6*E^(2*b^2*x^2)*Pi)
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int x^5 \operatorname{erf}(bx)^2 \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*erf(b*x)^2,x)
```

```
[Out] int(x^5*erf(b*x)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erf(b*x)^2,x, algorithm="maxima")
```

```
[Out] -1/6*integrate((4*b^4*x^5 + 10*b^2*x^3 + 15*x)*e^(-2*b^2*x^2), x)/(pi*b^4)
+ 1/48*((8*sqrt(pi)*b^6*x^6 - 15*sqrt(pi))*erf(b*x)^2 + 4*(4*b^5*x^5 + 10*b
^3*x^3 + 15*b*x)*erf(b*x)*e^(-b^2*x^2))/(sqrt(pi)*b^6)
```

Fricas [A]
time = 0.33, size = 98, normalized size = 0.55

$$\frac{4\sqrt{\pi}\left(4\,b^5x^5+10\,b^3x^3+15\,bx\right)\operatorname{erf}(bx)\,e^{\left(-b^2x^2\right)}-\left(15\,\pi-8\,\pi b^6x^6\right)\operatorname{erf}(bx)^2+4\left(2\,b^4x^4+7\,b^2x^2+11\right)e^{\left(-2\,b^2x^2\right)}}{48\,\pi b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erf(b*x)^2,x, algorithm="fricas")
```

```
[Out] 1/48*(4*sqrt(pi)*(4*b^5*x^5 + 10*b^3*x^3 + 15*b*x)*erf(b*x)*e^(-b^2*x^2) -
(15*pi - 8*pi*b^6*x^6)*erf(b*x)^2 + 4*(2*b^4*x^4 + 7*b^2*x^2 + 11)*e^(-2*b^
2*x^2))/(pi*b^6)
```

Sympy [A]
time = 0.76, size = 168, normalized size = 0.94

$$\begin{cases} \frac{x^6\operatorname{erf}^2(bx)}{6}+\frac{x^5e^{-b^2x^2}\operatorname{erf}(bx)}{3\sqrt{\pi}\,b}+\frac{x^4e^{-2b^2x^2}}{6\pi b^2}+\frac{5x^3e^{-b^2x^2}\operatorname{erf}(bx)}{6\sqrt{\pi}\,b^3}+\frac{7x^2e^{-2b^2x^2}}{12\pi b^4}+\frac{5xe^{-b^2x^2}\operatorname{erf}(bx)}{4\sqrt{\pi}\,b^5}-\frac{5\operatorname{erf}^2(bx)}{16b^6}+\frac{11e^{-2b^2x^2}}{12\pi b^6} & \text{for } b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**5*erf(b*x)**2,x)
```

```
[Out] Piecewise((x**6*erf(b*x)**2/6 + x**5*exp(-b**2*x**2)*erf(b*x)/(3*sqrt(pi)*b
) + x**4*exp(-2*b**2*x**2)/(6*pi*b**2) + 5*x**3*exp(-b**2*x**2)*erf(b*x)/(6
*sqrt(pi)*b**3) + 7*x**2*exp(-2*b**2*x**2)/(12*pi*b**4) + 5*x*exp(-b**2*x**
2)*erf(b*x)/(4*sqrt(pi)*b**5) - 5*erf(b*x)**2/(16*b**6) + 11*exp(-2*b**2*x*
*2)/(12*pi*b**6), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erf(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(x^5*erf(b*x)^2, x)
```

Mupad [B]
time = 0.30, size = 142, normalized size = 0.80

$$\frac{x^6\,\mathrm{erf}(b\,x)^2}{6}+\frac{\frac{11\,\mathrm{e}^{-2\,b^2\,x^2}}{12}-\frac{5\,\pi\,\mathrm{erf}(b\,x)^2}{16}+\frac{7\,b^2\,x^2\,\mathrm{e}^{-2\,b^2\,x^2}}{12}+\frac{b^4\,x^4\,\mathrm{e}^{-2\,b^2\,x^2}}{6}+\frac{5\,b^3\,x^3\,\sqrt{\pi}\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erf}(b\,x)}{6}+\frac{b^5\,x^5\,\sqrt{\pi}\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erf}(b\,x)}{3}+\frac{5\,b\,x\,\sqrt{\pi}\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erf}(b\,x)}{4}}{b^6\,\pi}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*erf(b*x)^2,x)
```

```
[Out] (x^6*erf(b*x)^2)/6 + ((11*exp(-2*b^2*x^2))/12 - (5*pi*erf(b*x)^2)/16 + (7*b
^2*x^2*exp(-2*b^2*x^2))/12 + (b^4*x^4*exp(-2*b^2*x^2))/6 + (5*b^3*x^3*pi^(1
/2)*exp(-b^2*x^2)*erf(b*x))/6 + (b^5*x^5*pi^(1/2)*exp(-b^2*x^2)*erf(b*x))/3
 + (5*b*x*pi^(1/2)*exp(-b^2*x^2)*erf(b*x))/4)/(b^6*pi)
```

3.23 $\int x^3\mathbf{Erf}(bx)^2\,dx$

Optimal. Leaf size=126

$$\frac{e^{-2b^2x^2}}{2b^4\pi}+\frac{e^{-2b^2x^2}x^2}{4b^2\pi}+\frac{3e^{-b^2x^2}x\mathrm{Erf}(bx)}{4b^3\sqrt{\pi}}+\frac{e^{-b^2x^2}x^3\mathrm{Erf}(bx)}{2b\sqrt{\pi}}-\frac{3\mathrm{Erf}(bx)^2}{16b^4}+\frac{1}{4}x^4\mathrm{Erf}(bx)^2$$

```
[Out] 1/2/b^4/exp(2*b^2*x^2)/Pi+1/4*x^2/b^2/exp(2*b^2*x^2)/Pi-3/16*erf(b*x)^2/b^4
+1/4*x^4*erf(b*x)^2+3/4*x*erf(b*x)/b^3/exp(b^2*x^2)/Pi^(1/2)+1/2*x^3*erf(b*
x)/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.11, antiderivative size = 126, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}}=0.600$, Rules used = {6499, 6520, 6508, 30, 2240, 2243}

$$-\frac{3\mathrm{Erf}(bx)^2}{16b^4}+\frac{x^3e^{-b^2x^2}\mathrm{Erf}(bx)}{2\sqrt{\pi}\,b}+\frac{x^2e^{-2b^2x^2}}{4\pi b^2}+\frac{e^{-2b^2x^2}}{2\pi b^4}+\frac{3xe^{-b^2x^2}\mathrm{Erf}(bx)}{4\sqrt{\pi}\,b^3}+\frac{1}{4}x^4\mathrm{Erf}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[x^3*Erf[b*x]^2,x]
```

```
[Out] 1/(2*b^4*E^(2*b^2*x^2)*Pi) + x^2/(4*b^2*E^(2*b^2*x^2)*Pi) + (3*x*Erf[b*x])/
(4*b^3*E^(b^2*x^2)*Sqrt[Pi]) + (x^3*Erf[b*x])/(2*b*E^(b^2*x^2)*Sqrt[Pi]) -
(3*Erf[b*x]^2)/(16*b^4) + (x^4*Erf[b*x]^2)/4
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6499

```
Int[Erf[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erf[b*x]^2/(
m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erf[b*x])/E^(b^
2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int x^3\operatorname{erf}(bx)^2\,dx &= \frac{1}{4}x^4\operatorname{erf}(bx)^2 - \frac{b\int e^{-b^2x^2}x^4\operatorname{erf}(bx)\,dx}{\sqrt{\pi}}\\
&= \frac{e^{-b^2x^2}x^3\operatorname{erf}(bx)}{2b\sqrt{\pi}} + \frac{1}{4}x^4\operatorname{erf}(bx)^2 - \frac{\int e^{-2b^2x^2}x^3\,dx}{\pi} - \frac{3\int e^{-b^2x^2}x^2\operatorname{erf}(bx)\,dx}{2b\sqrt{\pi}}\\
&= \frac{e^{-2b^2x^2}x^2}{4b^2\pi} + \frac{3e^{-b^2x^2}x\operatorname{erf}(bx)}{4b^3\sqrt{\pi}} + \frac{e^{-b^2x^2}x^3\operatorname{erf}(bx)}{2b\sqrt{\pi}} + \frac{1}{4}x^4\operatorname{erf}(bx)^2 - \frac{\int e^{-2b^2x^2}x\,dx}{2b^2\pi} - \frac{3\int e^{-2b}}{2b}\\
&= \frac{e^{-2b^2x^2}}{2b^4\pi} + \frac{e^{-2b^2x^2}x^2}{4b^2\pi} + \frac{3e^{-b^2x^2}x\operatorname{erf}(bx)}{4b^3\sqrt{\pi}} + \frac{e^{-b^2x^2}x^3\operatorname{erf}(bx)}{2b\sqrt{\pi}} + \frac{1}{4}x^4\operatorname{erf}(bx)^2 - \frac{3\operatorname{Subst}(\int x\,dx}{8b^4}\\
&= \frac{e^{-2b^2x^2}}{2b^4\pi} + \frac{e^{-2b^2x^2}x^2}{4b^2\pi} + \frac{3e^{-b^2x^2}x\operatorname{erf}(bx)}{4b^3\sqrt{\pi}} + \frac{e^{-b^2x^2}x^3\operatorname{erf}(bx)}{2b\sqrt{\pi}} - \frac{3\operatorname{erf}(bx)^2}{16b^4} + \frac{1}{4}x^4\operatorname{erf}(bx)^2
\end{aligned}$$

Mathematica [A]
time = 0.03, size = 90, normalized size = 0.71

$$\frac{e^{-2b^2x^2}\left(8+4b^2x^2+4be^{b^2x^2}\sqrt{\pi}\,x(3+2b^2x^2)\operatorname{Erf}(bx)+e^{2b^2x^2}\pi(-3+4b^4x^4)\operatorname{Erf}(bx)^2\right)}{16b^4\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^3*Erf[b*x]^2,x]
```

```
[Out] (8 + 4*b^2*x^2 + 4*b*E^(b^2*x^2)*Sqrt[Pi]*x*(3 + 2*b^2*x^2)*Erf[b*x] + E^(2
*b^2*x^2)*Pi*(-3 + 4*b^4*x^4)*Erf[b*x]^2)/(16*b^4*E^(2*b^2*x^2)*Pi)
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int x^3 \operatorname{erf}(bx)^2 \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erf(b*x)^2,x)
[Out] int(x^3*erf(b*x)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erf(b*x)^2,x, algorithm="maxima")
[Out] -1/2*integrate((2*b^2*x^3 + 3*x)*e^(-2*b^2*x^2), x)/(pi*b^2) - 1/16*((3*pi
- 4*pi*b^4*x^4)*erf(b*x)^2 - 4*(2*sqrt(pi)*b^3*x^3 + 3*sqrt(pi)*b*x)*erf(b*
x)*e^(-b^2*x^2))/(pi*b^4)
```

Fricas [A]
time = 0.35, size = 81, normalized size = 0.64

$$\frac{4\sqrt{\pi}\,(2\,b^3x^3 + 3\,bx)\operatorname{erf}(bx)\,e^{(-b^2x^2)} - (3\,\pi - 4\,\pi b^4x^4)\operatorname{erf}(bx)^2 + 4\,(b^2x^2 + 2)e^{(-2\,b^2x^2)}}{16\,\pi b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erf(b*x)^2,x, algorithm="fricas")
[Out] 1/16*(4*sqrt(pi)*(2*b^3*x^3 + 3*b*x)*erf(b*x)*e^(-b^2*x^2) - (3*pi - 4*pi*b
^4*x^4)*erf(b*x)^2 + 4*(b^2*x^2 + 2)*e^(-2*b^2*x^2))/(pi*b^4)
```

Sympy [A]
time = 0.41, size = 117, normalized size = 0.93

$$\begin{cases} \frac{x^4 \operatorname{erf}^2(bx)}{4} + \frac{x^3 e^{-b^2x^2} \operatorname{erf}(bx)}{2\sqrt{\pi}\,b} + \frac{x^2 e^{-2b^2x^2}}{4\pi b^2} + \frac{3xe^{-b^2x^2} \operatorname{erf}(bx)}{4\sqrt{\pi}\,b^3} - \frac{3\operatorname{erf}^2(bx)}{16b^4} + \frac{e^{-2b^2x^2}}{2\pi b^4} & \text{for}\ b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3*erf(b*x)**2,x)
```

```
[Out] Piecewise((x**4*erf(b*x)**2/4 + x**3*exp(-b**2*x**2)*erf(b*x)/(2*sqrt(pi)*b
) + x**2*exp(-2*b**2*x**2)/(4*pi*b**2) + 3*x*exp(-b**2*x**2)*erf(b*x)/(4*sq
rt(pi)*b**3) - 3*erf(b*x)**2/(16*b**4) + exp(-2*b**2*x**2)/(2*pi*b**4), Ne(
b, 0)), (0, True))
```

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erf(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(x^3*erf(b*x)^2, x)
```

Mupad [**B**]
time = 0.21, size = 101, normalized size = 0.80

$$\frac{x^4\,\mathrm{erf}(b\,x)^2}{4}+\frac{\frac{\mathrm{e}^{-2\,b^2\,x^2}}{2}-\frac{3\,\pi\,\mathrm{erf}(b\,x)^2}{16}+\frac{b^2\,x^2\,\mathrm{e}^{-2\,b^2\,x^2}}{4}+\frac{b^3\,x^3\,\sqrt{\pi}\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erf}(b\,x)}{2}+\frac{3\,b\,x\,\sqrt{\pi}\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erf}(b\,x)}{4}}{b^4\,\pi}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erf(b*x)^2,x)
```

```
[Out] (x^4*erf(b*x)^2)/4 + (exp(-2*b^2*x^2)/2 - (3*pi*erf(b*x)^2)/16 + (b^2*x^2*e
xp(-2*b^2*x^2))/4 + (b^3*x^3*pi^(1/2)*exp(-b^2*x^2)*erf(b*x))/2 + (3*b*x*pi
^(1/2)*exp(-b^2*x^2)*erf(b*x))/4)/(b^4*pi)
```

3.24 $\int x\mathbf{Erf}(bx)^2\,dx$

Optimal. Leaf size=71

$$\frac{e^{-2b^2x^2}}{2b^2\pi}+\frac{e^{-b^2x^2}x\text{Erf}(bx)}{b\sqrt{\pi}}-\frac{\text{Erf}(bx)^2}{4b^2}+\frac{1}{2}x^2\text{Erf}(bx)^2$$

```
[Out] 1/2/b^2/exp(2*b^2*x^2)/Pi-1/4*erf(b*x)^2/b^2+1/2*x^2*erf(b*x)^2+x*erf(b*x)/
b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.06, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.625, Rules used = {6499, 6520, 6508, 30, 2240}

$$\frac{xe^{-b^2x^2}\text{Erf}(bx)}{\sqrt{\pi}\,b}-\frac{\text{Erf}(bx)^2}{4b^2}+\frac{e^{-2b^2x^2}}{2\pi b^2}+\frac{1}{2}x^2\text{Erf}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[x*Erf[b*x]^2,x]
```

```
[Out] 1/(2*b^2*E^(2*b^2*x^2)*Pi) + (x*Erf[b*x])/(b*E^(b^2*x^2)*Sqrt[Pi]) - Erf[b*
x]^2/(4*b^2) + (x^2*Erf[b*x]^2)/2
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 6499

```
Int[Erf[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erf[b*x]^2/(
m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erf[b*x])/E^(b^
2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
```

```
x] && EqQ[d, -b^2]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int x\operatorname{erf}(bx)^2\,dx &= \frac{1}{2}x^2\operatorname{erf}(bx)^2-\frac{(2b)\int e^{-b^2x^2}x^2\operatorname{erf}(bx)\,dx}{\sqrt{\pi}}\\ &= \frac{e^{-b^2x^2}x\operatorname{erf}(bx)}{b\sqrt{\pi}}+\frac{1}{2}x^2\operatorname{erf}(bx)^2-\frac{2\int e^{-2b^2x^2}x\,dx}{\pi}-\frac{\int e^{-b^2x^2}\operatorname{erf}(bx)\,dx}{b\sqrt{\pi}}\\ &= \frac{e^{-2b^2x^2}}{2b^2\pi}+\frac{e^{-b^2x^2}x\operatorname{erf}(bx)}{b\sqrt{\pi}}+\frac{1}{2}x^2\operatorname{erf}(bx)^2-\frac{\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erf}(bx)\right)}{2b^2}\\ &= \frac{e^{-2b^2x^2}}{2b^2\pi}+\frac{e^{-b^2x^2}x\operatorname{erf}(bx)}{b\sqrt{\pi}}-\frac{\operatorname{erf}(bx)^2}{4b^2}+\frac{1}{2}x^2\operatorname{erf}(bx)^2\end{aligned}$$

Mathematica [A]
time = 0.03, size = 64, normalized size = 0.90

$$\frac{2e^{-2b^2x^2}+4be^{-b^2x^2}\sqrt{\pi}\,x\operatorname{Erf}(bx)+\pi\left(-1+2b^2x^2\right)\operatorname{Erf}(bx)^2}{4b^2\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[x*Erf[b*x]^2,x]
[Out] (2/E^(2*b^2*x^2) + (4*b*Sqrt[Pi]*x*Erf[b*x])/E^(b^2*x^2) + Pi*(-1 + 2*b^2*x
^2)*Erf[b*x]^2)/(4*b^2*Pi)
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int x\operatorname{erf}\left(bx\right)^2\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erf(b*x)^2,x)
```

```
[Out] int(x*erf(b*x)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(b*x)^2,x, algorithm="maxima")
```

```
[Out] -2*integrate(x*e^(-2*b^2*x^2), x)/pi + 1/4*(4*b*x*erf(b*x)*e^(-b^2*x^2) + (
2*sqrt(pi)*b^2*x^2 - sqrt(pi))*erf(b*x)^2)/(sqrt(pi)*b^2)
```

Fricas [A]
time = 0.35, size = 59, normalized size = 0.83

$$\frac{4\sqrt{\pi}\,bx\,\mathrm{erf}\left(bx\right)e^{\left(-b^2x^2\right)} - \left(\pi - 2\,\pi b^2x^2\right)\mathrm{erf}\left(bx\right)^2 + 2\,e^{\left(-2\,b^2x^2\right)}}{4\,\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(b*x)^2,x, algorithm="fricas")
```

```
[Out] 1/4*(4*sqrt(pi)*b*x*erf(b*x)*e^(-b^2*x^2) - (pi - 2*pi*b^2*x^2)*erf(b*x)^2
+ 2*e^(-2*b^2*x^2))/(pi*b^2)
```

Sympy [A]
time = 0.25, size = 65, normalized size = 0.92

$$\begin{cases} \frac{x^2\,\mathrm{erf}^2\left(bx\right)}{2} + \frac{xe^{-b^2x^2}\,\mathrm{erf}\left(bx\right)}{\sqrt{\pi}\,b} - \frac{\mathrm{erf}^2\left(bx\right)}{4b^2} + \frac{e^{-2b^2x^2}}{2\pi b^2} & \text{for}\ b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(b*x)**2,x)
```

```
[Out] Piecewise((x**2*erf(b*x)**2/2 + x*exp(-b**2*x**2)*erf(b*x)/(sqrt(pi)*b) - e
rf(b*x)**2/(4*b**2) + exp(-2*b**2*x**2)/(2*pi*b**2), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(x*erf(b*x)^2, x)
```

Mupad [B]
time = 0.17, size = 67, normalized size = 0.94

$$\frac{\frac{e^{-2\,b^2\,x^2}}{2}+b\,x\,\sqrt{\pi }\,e^{-b^2\,x^2}\,\mathrm{erf}\left(b\,x\right)}{b^2\,\pi }-\frac{\frac{{\mathrm{erf}\left(b\,x\right)}^2}{4}-\frac{b^2\,x^2\,{\mathrm{erf}\left(b\,x\right)}^2}{2}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erf(b*x)^2,x)
```

```
[Out] (exp(-2*b^2*x^2)/2 + b*x*pi^(1/2)*exp(-b^2*x^2)*erf(b*x))/(b^2*pi) - (erf(b
*x)^2/4 - (b^2*x^2*erf(b*x)^2)/2)/b^2
```

3.25 $\int \frac{\mathbf{Erf}(bx)^2}{x}\,dx$

Optimal. Leaf size=13

$$\operatorname{Int}\left(\frac{\operatorname{Erf}(bx)^2}{x},x\right)$$

```
[Out] Unintegrable(erf(b*x)^2/x,x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\operatorname{Erf}(bx)^2}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erf[b*x]^2/x,x]
[Out] Defer[Int][Erf[b*x]^2/x, x]
```

Rubi steps

$$\int \frac{\operatorname{erf}(bx)^2}{x}\,dx = \int \frac{\operatorname{erf}(bx)^2}{x}\,dx$$

Mathematica [A]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{Erf}(bx)^2}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erf[b*x]^2/x,x]
[Out] Integrate[Erf[b*x]^2/x, x]
```

Maple [A]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}\left(bx\right)^2}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2/x,x)
```

```
[Out] int(erf(b*x)^2/x,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)^2/x, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x)^2/x, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}^{2}\left(bx\right)}{x}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)**2/x,x)
```

```
[Out] Integral(erf(b*x)**2/x, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)^2/x, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.08

$$\int \frac{{\mathrm{erf}\left(b\,x\right)}^2}{x} \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2/x,x)
```

```
[Out] int(erf(b*x)^2/x, x)
```

3.26 $\int \frac{\mathbf{Erf}(bx)^2}{x^3}\,dx$

Optimal. Leaf size=67

$$-\frac{2be^{-b^2x^2}\operatorname{Erf}(bx)}{\sqrt{\pi}\,x}-b^2\operatorname{Erf}(bx)^2-\frac{\operatorname{Erf}(bx)^2}{2x^2}+\frac{2b^2\operatorname{Ei}(-2b^2x^2)}{\pi}$$

```
[Out] 2*b^2*Ei(-2*b^2*x^2)/Pi-b^2*erf(b*x)^2-1/2*erf(b*x)^2/x^2-2*b*erf(b*x)/exp(
b^2*x^2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.06, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules used = {6499, 6526, 6508, 30, 2241}

$$-\frac{2be^{-b^2x^2}\operatorname{Erf}(bx)}{\sqrt{\pi}\,x}+b^2\left(-\operatorname{Erf}(bx)^2\right)+\frac{2b^2\operatorname{Ei}(-2b^2x^2)}{\pi}-\frac{\operatorname{Erf}(bx)^2}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]^2/x^3,x]
```

```
[Out] (-2*b*Erf[b*x])/(E^(b^2*x^2)*Sqrt[Pi]*x) - b^2*Erf[b*x]^2 - Erf[b*x]^2/(2*x
^2) + (2*b^2*ExpIntegralEi[-2*b^2*x^2])/Pi
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 6499

```
Int[Erf[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erf[b*x]^2/(
m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erf[b*x])/E^(b^
2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6526

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m + 1)*E^(c + d*x^2)*(Erf[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(m
+ 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[2*(b/((m + 1
)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x])
 /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int \frac{\operatorname{erf}(bx)^2}{x^3}\,dx &= -\frac{\operatorname{erf}(bx)^2}{2x^2}+\frac{(2b)\int \frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{2be^{-b^2x^2}\operatorname{erf}(bx)}{\sqrt{\pi}\,x}-\frac{\operatorname{erf}(bx)^2}{2x^2}+\frac{(4b^2)\int \frac{e^{-2b^2x^2}}{x}\,dx}{\pi}-\frac{(4b^3)\int e^{-b^2x^2}\operatorname{erf}(bx)\,dx}{\sqrt{\pi}}\\
&= -\frac{2be^{-b^2x^2}\operatorname{erf}(bx)}{\sqrt{\pi}\,x}-\frac{\operatorname{erf}(bx)^2}{2x^2}+\frac{2b^2\operatorname{Ei}(-2b^2x^2)}{\pi}-(2b^2)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erf}(bx)\right)\\
&= -\frac{2be^{-b^2x^2}\operatorname{erf}(bx)}{\sqrt{\pi}\,x}-b^2\operatorname{erf}(bx)^2-\frac{\operatorname{erf}(bx)^2}{2x^2}+\frac{2b^2\operatorname{Ei}(-2b^2x^2)}{\pi}
\end{aligned}$$

Mathematica [A]
time = 0.02, size = 63, normalized size = 0.94

$$-\frac{2be^{-b^2x^2}\operatorname{Erf}(bx)}{\sqrt{\pi}\,x}+\left(-b^2-\frac{1}{2x^2}\right)\operatorname{Erf}(bx)^2+\frac{2b^2\operatorname{Ei}(-2b^2x^2)}{\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]^2/x^3,x]
[Out] (-2*b*Erf[b*x])/(E^(b^2*x^2)*Sqrt[Pi]*x) + (-b^2 - 1/(2*x^2))*Erf[b*x]^2 +
(2*b^2*ExpIntegralEi[-2*b^2*x^2])/Pi
```

Maple [F]
time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}\left(bx\right)^2}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2/x^3,x)
[Out] int(erf(b*x)^2/x^3,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^3,x, algorithm="maxima")
[Out] 2*b*integrate(erf(b*x)*e^(-b^2*x^2)/x^2, x)/sqrt(pi) - 1/2*erf(b*x)^2/x^2
```

Fricas [A]
time = 0.34, size = 65, normalized size = 0.97

$$\frac{4\,b^2x^2\mathrm{Ei}(-2\,b^2x^2) - 4\,\sqrt{\pi}\,bx\,\mathrm{erf}\,(bx)\,e^{(-b^2x^2)} - (\pi + 2\,\pi b^2x^2)\,\mathrm{erf}\,(bx)^2}{2\,\pi x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^3,x, algorithm="fricas")
[Out] 1/2*(4*b^2*x^2*Ei(-2*b^2*x^2) - 4*sqrt(pi)*b*x*erf(b*x)*e^(-b^2*x^2) - (pi
+ 2*pi*b^2*x^2)*erf(b*x)^2)/(pi*x^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{erf}^2\,(bx)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)**2/x**3,x)
[Out] Integral(erf(b*x)**2/x**3, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^3,x, algorithm="giac")
[Out] integrate(erf(b*x)^2/x^3, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erf}(b\,x)^2}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2/x^3,x)
[Out] int(erf(b*x)^2/x^3, x)
```

3.27 $\int \frac{\mathbf{Erf}(bx)^2}{x^5}\,dx$

Optimal. Leaf size=125

$$-\frac{b^2e^{-2b^2x^2}}{3\pi x^2}-\frac{be^{-b^2x^2}\text{Erf}(bx)}{3\sqrt{\pi}\,x^3}+\frac{2b^3e^{-b^2x^2}\text{Erf}(bx)}{3\sqrt{\pi}\,x}+\frac{1}{3}b^4\text{Erf}(bx)^2-\frac{\text{Erf}(bx)^2}{4x^4}-\frac{4b^4\text{Ei}(-2b^2x^2)}{3\pi}$$

```
[Out] -1/3*b^2/exp(2*b^2*x^2)/Pi/x^2-4/3*b^4*Ei(-2*b^2*x^2)/Pi+1/3*b^4*erf(b*x)^2
-1/4*erf(b*x)^2/x^4-1/3*b*erf(b*x)/exp(b^2*x^2)/x^3/Pi^(1/2)+2/3*b^3*erf(b*
x)/exp(b^2*x^2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.12, antiderivative size = 125, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.600$, Rules used = {6499, 6526, 6508, 30, 2241, 2245}

$$\frac{1}{3}b^4\text{Erf}(bx)^2-\frac{be^{-b^2x^2}\text{Erf}(bx)}{3\sqrt{\pi}\,x^3}-\frac{b^2e^{-2b^2x^2}}{3\pi x^2}-\frac{4b^4\text{Ei}(-2b^2x^2)}{3\pi}+\frac{2b^3e^{-b^2x^2}\text{Erf}(bx)}{3\sqrt{\pi}\,x}-\frac{\text{Erf}(bx)^2}{4x^4}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]^2/x^5,x]
```

```
[Out] -1/3*b^2/(E^(2*b^2*x^2)*Pi*x^2) - (b*Erf[b*x])/(3*E^(b^2*x^2)*Sqrt[Pi]*x^3)
 + (2*b^3*Erf[b*x])/(3*E^(b^2*x^2)*Sqrt[Pi]*x) + (b^4*Erf[b*x]^2)/3 - Erf[b
*x]^2/(4*x^4) - (4*b^4*ExpIntegralEi[-2*b^2*x^2])/(3*Pi)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6499

```
Int[Erf[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erf[b*x]^2/(
m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erf[b*x])/E^(b^
2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6526

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m + 1)*E^(c + d*x^2)*(Erf[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(m
+ 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[2*(b/((m + 1
)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x])
 /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{\operatorname{erf}(bx)^2}{x^5}\,dx &= -\frac{\operatorname{erf}(bx)^2}{4x^4}+\frac{b\int \frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x^4}\,dx}{\sqrt{\pi}}\\
&= -\frac{be^{-b^2x^2}\operatorname{erf}(bx)}{3\sqrt{\pi}\,x^3}-\frac{\operatorname{erf}(bx)^2}{4x^4}+\frac{(2b^2)\int \frac{e^{-2b^2x^2}}{x^3}\,dx}{3\pi}-\frac{(2b^3)\int \frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x^2}\,dx}{3\sqrt{\pi}}\\
&= -\frac{b^2e^{-2b^2x^2}}{3\pi x^2}-\frac{be^{-b^2x^2}\operatorname{erf}(bx)}{3\sqrt{\pi}\,x^3}+\frac{2b^3e^{-b^2x^2}\operatorname{erf}(bx)}{3\sqrt{\pi}\,x}-\frac{\operatorname{erf}(bx)^2}{4x^4}-2\frac{(4b^4)\int \frac{e^{-2b^2x^2}}{x}\,dx}{3\pi}+\frac{(4b^5)\int
\end{aligned}
$$

$$
\begin{aligned}
&= -\frac{b^2e^{-2b^2x^2}}{3\pi x^2}-\frac{be^{-b^2x^2}\operatorname{erf}(bx)}{3\sqrt{\pi}\,x^3}+\frac{2b^3e^{-b^2x^2}\operatorname{erf}(bx)}{3\sqrt{\pi}\,x}-\frac{\operatorname{erf}(bx)^2}{4x^4}-\frac{4b^4\operatorname{Ei}(-2b^2x^2)}{3\pi}+\frac{1}{3}(2b^4)\operatorname{Sub}\\
&= -\frac{b^2e^{-2b^2x^2}}{3\pi x^2}-\frac{be^{-b^2x^2}\operatorname{erf}(bx)}{3\sqrt{\pi}\,x^3}+\frac{2b^3e^{-b^2x^2}\operatorname{erf}(bx)}{3\sqrt{\pi}\,x}+\frac{1}{3}b^4\operatorname{erf}(bx)^2-\frac{\operatorname{erf}(bx)^2}{4x^4}-\frac{4b^4\operatorname{Ei}(-2b^2x^2)}{3\pi}
\end{aligned}
$$

Mathematica [A]
time = 0.06, size = 97, normalized size = 0.78

$$
\frac{\frac{4be^{-b^2x^2}x(-1+2b^2x^2)\operatorname{Erf}(bx)}{\sqrt{\pi}}+(-3+4b^4x^4)\operatorname{Erf}(bx)^2-\frac{4b^2x^2\left(e^{-2b^2x^2}+4b^2x^2\operatorname{Ei}(-2b^2x^2)\right)}{\pi}}{12x^4}
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]^2/x^5,x]
```

```
[Out] ((4*b*x*(-1 + 2*b^2*x^2)*Erf[b*x])/(E^(b^2*x^2)*Sqrt[Pi]) + (-3 + 4*b^4*x^4
)*Erf[b*x]^2 - (4*b^2*x^2*(E^(-2*b^2*x^2) + 4*b^2*x^2*ExpIntegralEi[-2*b^2*
x^2]))/Pi)/(12*x^4)
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}(bx)^2}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2/x^5,x)
```

```
[Out] int(erf(b*x)^2/x^5,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^5,x, algorithm="maxima")
```

```
[Out] b*integrate(erf(b*x)*e^(-b^2*x^2)/x^4, x)/sqrt(pi) - 1/4*erf(b*x)^2/x^4
```

Fricas [A]
time = 0.38, size = 94, normalized size = 0.75

$$-\frac{16\,b^4x^4\mathrm{Ei}(-2\,b^2x^2)+4\,b^2x^2e^{(-2\,b^2x^2)}-4\,\sqrt{\pi}\,(2\,b^3x^3-bx)\operatorname{erf}(bx)\,e^{(-b^2x^2)}+(3\,\pi-4\,\pi b^4x^4)\operatorname{erf}(bx)^2}{12\,\pi x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^5,x, algorithm="fricas")
```

```
[Out] -1/12*(16*b^4*x^4*Ei(-2*b^2*x^2) + 4*b^2*x^2*e^(-2*b^2*x^2) - 4*sqrt(pi)*(2
*b^3*x^3 - b*x)*erf(b*x)*e^(-b^2*x^2) + (3*pi - 4*pi*b^4*x^4)*erf(b*x)^2)/(
pi*x^4)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}^2(bx)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)**2/x**5,x)
```

```
[Out] Integral(erf(b*x)**2/x**5, x)
```

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^5,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)^2/x^5, x)
```

Mupad [**F**]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erf}(b\,x)^2}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2/x^5,x)
```

```
[Out] int(erf(b*x)^2/x^5, x)
```

3.28 $\int \frac{\mathbf{Erf}(bx)^2}{x^7}\,dx$

Optimal. Leaf size=177

$$-\frac{b^2e^{-2b^2x^2}}{15\pi x^4}+\frac{2b^4e^{-2b^2x^2}}{9\pi x^2}-\frac{2be^{-b^2x^2}\mathrm{Erf}(bx)}{15\sqrt{\pi}\,x^5}+\frac{4b^3e^{-b^2x^2}\mathrm{Erf}(bx)}{45\sqrt{\pi}\,x^3}-\frac{8b^5e^{-b^2x^2}\mathrm{Erf}(bx)}{45\sqrt{\pi}\,x}-\frac{4}{45}b^6\mathrm{Erf}(bx)^2-\frac{\mathrm{Erf}(bx)^2}{6x^6}+\frac{28}{}$$

```
[Out] -1/15*b^2/exp(2*b^2*x^2)/Pi/x^4+2/9*b^4/exp(2*b^2*x^2)/Pi/x^2+28/45*b^6*Ei(
-2*b^2*x^2)/Pi-4/45*b^6*erf(b*x)^2-1/6*erf(b*x)^2/x^6-2/15*b*erf(b*x)/exp(b
^2*x^2)/x^5/Pi^(1/2)+4/45*b^3*erf(b*x)/exp(b^2*x^2)/x^3/Pi^(1/2)-8/45*b^5*e
rf(b*x)/exp(b^2*x^2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.19, antiderivative size = 177, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.600$, Rules used = {6499, 6526, 6508, 30, 2241, 2245}

$$-\frac{4}{45}b^6\mathrm{Erf}(bx)^2-\frac{2be^{-b^2x^2}\mathrm{Erf}(bx)}{15\sqrt{\pi}\,x^5}-\frac{b^2e^{-2b^2x^2}}{15\pi x^4}+\frac{28b^6\mathrm{Ei}(-2b^2x^2)}{45\pi}-\frac{8b^5e^{-b^2x^2}\mathrm{Erf}(bx)}{45\sqrt{\pi}\,x}+\frac{2b^4e^{-2b^2x^2}}{9\pi x^2}+\frac{4b^3e^{-b^2x^2}\mathrm{Erf}(bx)}{45\sqrt{\pi}\,x^3}-\frac{\mathrm{Erf}(bx)^2}{6x^6}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]^2/x^7,x]
```

```
[Out] -1/15*b^2/(E^(2*b^2*x^2)*Pi*x^4) + (2*b^4)/(9*E^(2*b^2*x^2)*Pi*x^2) - (2*b*
Erf[b*x])/(15*E^(b^2*x^2)*Sqrt[Pi]*x^5) + (4*b^3*Erf[b*x])/(45*E^(b^2*x^2)*
Sqrt[Pi]*x^3) - (8*b^5*Erf[b*x])/(45*E^(b^2*x^2)*Sqrt[Pi]*x) - (4*b^6*Erf[b
*x]^2)/45 - Erf[b*x]^2/(6*x^6) + (28*b^6*ExpIntegralEi[-2*b^2*x^2])/(45*Pi)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
```

```
] && LeQ[-n, m + 1]))
```

Rule 6499

```
Int[Erf[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erf[b*x]^2/(
m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erf[b*x])/E^(b^
2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6526

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m + 1)*E^(c + d*x^2)*(Erf[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(m
+ 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[2*(b/((m + 1
)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x])
 /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{\operatorname{erf}(bx)^2}{x^7}\,dx &= -\frac{\operatorname{erf}(bx)^2}{6x^6} + \frac{(2b)\int \frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x^6}\,dx}{3\sqrt{\pi}} \\
&= -\frac{2be^{-b^2x^2}\operatorname{erf}(bx)}{15\sqrt{\pi}\,x^5} - \frac{\operatorname{erf}(bx)^2}{6x^6} + \frac{(4b^2)\int \frac{e^{-2b^2x^2}}{x^5}\,dx}{15\pi} - \frac{(4b^3)\int \frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x^4}\,dx}{15\sqrt{\pi}} \\
&= -\frac{b^2e^{-2b^2x^2}}{15\pi x^4} - \frac{2be^{-b^2x^2}\operatorname{erf}(bx)}{15\sqrt{\pi}\,x^5} + \frac{4b^3e^{-b^2x^2}\operatorname{erf}(bx)}{45\sqrt{\pi}\,x^3} - \frac{\operatorname{erf}(bx)^2}{6x^6} - \frac{(8b^4)\int \frac{e^{-2b^2x^2}}{x^3}\,dx}{45\pi} - \frac{(4b^4)\int \cdots}{\cdots} \\
&= -\frac{b^2e^{-2b^2x^2}}{15\pi x^4} + \frac{2b^4e^{-2b^2x^2}}{9\pi x^2} - \frac{2be^{-b^2x^2}\operatorname{erf}(bx)}{15\sqrt{\pi}\,x^5} + \frac{4b^3e^{-b^2x^2}\operatorname{erf}(bx)}{45\sqrt{\pi}\,x^3} - \frac{8b^5e^{-b^2x^2}\operatorname{erf}(bx)}{45\sqrt{\pi}\,x} - \frac{\operatorname{erf}(bx\cdots}{6x^6} \\
&= -\frac{b^2e^{-2b^2x^2}}{15\pi x^4} + \frac{2b^4e^{-2b^2x^2}}{9\pi x^2} - \frac{2be^{-b^2x^2}\operatorname{erf}(bx)}{15\sqrt{\pi}\,x^5} + \frac{4b^3e^{-b^2x^2}\operatorname{erf}(bx)}{45\sqrt{\pi}\,x^3} - \frac{8b^5e^{-b^2x^2}\operatorname{erf}(bx)}{45\sqrt{\pi}\,x} - \frac{\operatorname{erf}(bx\cdots}{6x^6} \\
&= -\frac{b^2e^{-2b^2x^2}}{15\pi x^4} + \frac{2b^4e^{-2b^2x^2}}{9\pi x^2} - \frac{2be^{-b^2x^2}\operatorname{erf}(bx)}{15\sqrt{\pi}\,x^5} + \frac{4b^3e^{-b^2x^2}\operatorname{erf}(bx)}{45\sqrt{\pi}\,x^3} - \frac{8b^5e^{-b^2x^2}\operatorname{erf}(bx)}{45\sqrt{\pi}\,x} - \frac{4}{45}b^6\mathrm{e}\cdots
\end{aligned}
$$

Mathematica [A]
time = 0.03, size = 133, normalized size = 0.75

$$
\frac{e^{-2b^2x^2}\left(-6b^2x^2+20b^4x^4-4be^{b^2x^2}\sqrt{\pi}\,x(3-2b^2x^2+4b^4x^4)\operatorname{Erf}(bx)-e^{2b^2x^2}\pi(15+8b^6x^6)\operatorname{Erf}(bx)^2+56b^6e^{2b^2x^2}x^6\operatorname{Ei}(-2b^2x^2)\right)}{90\pi x^6}
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]^2/x^7,x]
```

```
[Out] (-6*b^2*x^2 + 20*b^4*x^4 - 4*b*E^(b^2*x^2)*Sqrt[Pi]*x*(3 - 2*b^2*x^2 + 4*b^
4*x^4)*Erf[b*x] - E^(2*b^2*x^2)*Pi*(15 + 8*b^6*x^6)*Erf[b*x]^2 + 56*b^6*E^(
2*b^2*x^2)*x^6*ExpIntegralEi[-2*b^2*x^2])/(90*E^(2*b^2*x^2)*Pi*x^6)
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{erf}\left(bx\right)^{2}}{x^{7}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2/x^7,x)
```

```
[Out] int(erf(b*x)^2/x^7,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^7,x, algorithm="maxima")
```

```
[Out] 2/3*b*integrate(erf(b*x)*e^(-b^2*x^2)/x^6, x)/sqrt(pi) - 1/6*erf(b*x)^2/x^6
```

Fricas [A]
time = 0.33, size = 114, normalized size = 0.64

$$\frac{56\,b^{6}x^{6}\mathrm{Ei}\left(-2\,b^{2}x^{2}\right) - 4\,\sqrt{\pi}\,\left(4\,b^{5}x^{5} - 2\,b^{3}x^{3} + 3\,bx\right)\mathrm{erf}\left(bx\right)e^{\left(-b^{2}x^{2}\right)} - \left(15\,\pi + 8\,\pi b^{6}x^{6}\right)\mathrm{erf}\left(bx\right)^{2} + 2\,\left(10\,b^{4}x^{4} - 3\,b^{2}x^{2}\right)e^{\left(-2\,b^{2}x^{2}\right)}}{90\,\pi x^{6}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^7,x, algorithm="fricas")
```

```
[Out] 1/90*(56*b^6*x^6*Ei(-2*b^2*x^2) - 4*sqrt(pi)*(4*b^5*x^5 - 2*b^3*x^3 + 3*b*x
)*erf(b*x)*e^(-b^2*x^2) - (15*pi + 8*pi*b^6*x^6)*erf(b*x)^2 + 2*(10*b^4*x^4
 - 3*b^2*x^2)*e^(-2*b^2*x^2))/(pi*x^6)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{erf}^{2}\left(bx\right)}{x^{7}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)**2/x**7,x)
```

```
[Out] Integral(erf(b*x)**2/x**7, x)
```

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^7,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)^2/x^7, x)
```

Mupad [**F**]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erf}(b\,x)^2}{x^7}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2/x^7,x)
```

```
[Out] int(erf(b*x)^2/x^7, x)
```

3.29 $\int x^4 \mathbf{Erf}(bx)^2\,dx$

Optimal. Leaf size=165

$$\frac{11e^{-2b^2x^2}x}{20b^4\pi}+\frac{e^{-2b^2x^2}x^3}{5b^2\pi}+\frac{4e^{-b^2x^2}\mathrm{Erf}(bx)}{5b^5\sqrt{\pi}}+\frac{4e^{-b^2x^2}x^2\mathrm{Erf}(bx)}{5b^3\sqrt{\pi}}+\frac{2e^{-b^2x^2}x^4\mathrm{Erf}(bx)}{5b\sqrt{\pi}}+\frac{1}{5}x^5\mathrm{Erf}(bx)^2-\frac{43\mathrm{Erf}\left(\sqrt{2}\,bx\right)}{40b^5\sqrt{2\pi}}$$

```
[Out] 11/20*x/b^4/exp(2*b^2*x^2)/Pi+1/5*x^3/b^2/exp(2*b^2*x^2)/Pi+1/5*x^5*erf(b*x
)^2+4/5*erf(b*x)/b^5/exp(b^2*x^2)/Pi^(1/2)+4/5*x^2*erf(b*x)/b^3/exp(b^2*x^2
)/Pi^(1/2)+2/5*x^4*erf(b*x)/b/exp(b^2*x^2)/Pi^(1/2)-43/80*erf(b*x*2^(1/2))/
b^5*2^(1/2)/Pi^(1/2)
```

Rubi [A]
time = 0.17, antiderivative size = 165, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules used = {6499, 6520, 6517, 2236, 2243}

$$-\frac{43\mathrm{Erf}\left(\sqrt{2}\,bx\right)}{40\sqrt{2\pi}\,b^5}+\frac{2x^4e^{-b^2x^2}\mathrm{Erf}(bx)}{5\sqrt{\pi}\,b}+\frac{x^3e^{-2b^2x^2}}{5\pi b^2}+\frac{4e^{-b^2x^2}\mathrm{Erf}(bx)}{5\sqrt{\pi}\,b^5}+\frac{11xe^{-2b^2x^2}}{20\pi b^4}+\frac{4x^2e^{-b^2x^2}\mathrm{Erf}(bx)}{5\sqrt{\pi}\,b^3}+\frac{1}{5}x^5\mathrm{Erf}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[x^4*Erf[b*x]^2,x]
```

```
[Out] (11*x)/(20*b^4*E^(2*b^2*x^2)*Pi) + x^3/(5*b^2*E^(2*b^2*x^2)*Pi) + (4*Erf[b*
x])/(5*b^5*E^(b^2*x^2)*Sqrt[Pi]) + (4*x^2*Erf[b*x])/(5*b^3*E^(b^2*x^2)*Sqrt
[Pi]) + (2*x^4*Erf[b*x])/(5*b*E^(b^2*x^2)*Sqrt[Pi]) + (x^5*Erf[b*x]^2)/5 -
(43*Erf[Sqrt[2]*b*x])/(40*b^5*Sqrt[2*Pi])
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6499

```
Int[Erf[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erf[b*x]^2/(
m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erf[b*x])/E^(b^
```

```
2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int x^4\operatorname{erf}(bx)^2\,dx &= \frac{1}{5}x^5\operatorname{erf}(bx)^2-\frac{(4b)\int e^{-b^2x^2}x^5\operatorname{erf}(bx)\,dx}{5\sqrt{\pi}}\\
&= \frac{2e^{-b^2x^2}x^4\operatorname{erf}(bx)}{5b\sqrt{\pi}}+\frac{1}{5}x^5\operatorname{erf}(bx)^2-\frac{4\int e^{-2b^2x^2}x^4\,dx}{5\pi}-\frac{8\int e^{-b^2x^2}x^3\operatorname{erf}(bx)\,dx}{5b\sqrt{\pi}}\\
&= \frac{e^{-2b^2x^2}x^3}{5b^2\pi}+\frac{4e^{-b^2x^2}x^2\operatorname{erf}(bx)}{5b^3\sqrt{\pi}}+\frac{2e^{-b^2x^2}x^4\operatorname{erf}(bx)}{5b\sqrt{\pi}}+\frac{1}{5}x^5\operatorname{erf}(bx)^2-\frac{3\int e^{-2b^2x^2}x^2\,dx}{5b^2\pi}-\frac{8\int
\\
&= \frac{11e^{-2b^2x^2}x}{20b^4\pi}+\frac{e^{-2b^2x^2}x^3}{5b^2\pi}+\frac{4e^{-b^2x^2}\operatorname{erf}(bx)}{5b^5\sqrt{\pi}}+\frac{4e^{-b^2x^2}x^2\operatorname{erf}(bx)}{5b^3\sqrt{\pi}}+\frac{2e^{-b^2x^2}x^4\operatorname{erf}(bx)}{5b\sqrt{\pi}}+\frac{1}{5}x^5\mathrm{er}
\\
&= \frac{11e^{-2b^2x^2}x}{20b^4\pi}+\frac{e^{-2b^2x^2}x^3}{5b^2\pi}+\frac{4e^{-b^2x^2}\operatorname{erf}(bx)}{5b^5\sqrt{\pi}}+\frac{4e^{-b^2x^2}x^2\operatorname{erf}(bx)}{5b^3\sqrt{\pi}}+\frac{2e^{-b^2x^2}x^4\operatorname{erf}(bx)}{5b\sqrt{\pi}}+\frac{1}{5}x^5\mathrm{er}
\end{aligned}$$

Mathematica [A]
time = 0.07, size = 106, normalized size = 0.64

$$\frac{4be^{-2b^2x^2}x(11+4b^2x^2)+32e^{-b^2x^2}\sqrt{\pi}\,(2+2b^2x^2+b^4x^4)\operatorname{Erf}(bx)+16b^5\pi x^5\operatorname{Erf}(bx)^2-43\sqrt{2\pi}\operatorname{Erf}\left(\sqrt{2}\,bx\right)}{80b^5\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^4*Erf[b*x]^2,x]
```

```
[Out] ((4*b*x*(11 + 4*b^2*x^2))/E^(2*b^2*x^2) + (32*Sqrt[Pi]*(2 + 2*b^2*x^2 + b^4
*x^4)*Erf[b*x])/E^(b^2*x^2) + 16*b^5*Pi*x^5*Erf[b*x]^2 - 43*Sqrt[2*Pi]*Erf[
Sqrt[2]*b*x])/(80*b^5*Pi)
```

Maple [A]
time = 0.24, size = 131, normalized size = 0.79

method	result
derivativedivides	$\frac{\frac{\mathrm{erf}(bx)^2 b^5 x^5}{5}-\frac{4\,\mathrm{erf}(bx)\left(-\frac{b^4x^4\mathrm{e}^{-b^2x^2}}{2}-b^2x^2\mathrm{e}^{-b^2x^2}-\mathrm{e}^{-b^2x^2}\right)}{5\sqrt{\pi}}+\frac{-\frac{43\sqrt{2}\,\sqrt{\pi}\,\mathrm{erf}\left(bx\sqrt{2}\right)}{80}+\frac{11\,\mathrm{e}^{-2b^2x^2}bx}{20}+\frac{\mathrm{e}^{-2b^2x^2}b^3x^3}{5}}{\pi}}{b^5}$
default	$\frac{\frac{\mathrm{erf}(bx)^2 b^5 x^5}{5}-\frac{4\,\mathrm{erf}(bx)\left(-\frac{b^4x^4\mathrm{e}^{-b^2x^2}}{2}-b^2x^2\mathrm{e}^{-b^2x^2}-\mathrm{e}^{-b^2x^2}\right)}{5\sqrt{\pi}}+\frac{-\frac{43\sqrt{2}\,\sqrt{\pi}\,\mathrm{erf}\left(bx\sqrt{2}\right)}{80}+\frac{11\,\mathrm{e}^{-2b^2x^2}bx}{20}+\frac{\mathrm{e}^{-2b^2x^2}b^3x^3}{5}}{\pi}}{b^5}$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erf(b*x)^2,x,method=_RETURNVERBOSE)
```

```
[Out] 1/b^5*(1/5*erf(b*x)^2*b^5*x^5-4/5*erf(b*x)/Pi^(1/2)*(-1/2/exp(b^2*x^2)*b^4*
x^4-b^2*x^2/exp(b^2*x^2)-1/exp(b^2*x^2))+4/5/Pi*(-43/64*2^(1/2)*Pi^(1/2)*er
f(b*x*2^(1/2))+11/16/exp(b^2*x^2)^2*b*x+1/4/exp(b^2*x^2)^2*b^3*x^3))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erf(b*x)^2,x, algorithm="maxima")
```

```
[Out] -1/5*integrate(4*(b^4*x^4 + 2*b^2*x^2 + 2)*e^(-2*b^2*x^2), x)/(pi*b^4) + 1/
5*(sqrt(pi)*b^5*x^5*erf(b*x)^2 + 2*(b^4*x^4 + 2*b^2*x^2 + 2)*erf(b*x)*e^(-b
^2*x^2))/(sqrt(pi)*b^5)
```

Fricas [A]
time = 0.34, size = 111, normalized size = 0.67

$$\frac{16\,\pi b^6x^5\,\mathrm{erf}\,(bx)^2+32\,\sqrt{\pi}\,(b^5x^4+2\,b^3x^2+2\,b)\,\mathrm{erf}\,(bx)\,e^{(-b^2x^2)}-43\,\sqrt{2}\,\sqrt{\pi}\,\sqrt{b^2}\,\mathrm{erf}\left(\sqrt{2}\,\sqrt{b^2}\,x\right)+4\,(4\,b^4x^3+11\,b^2x)e^{(-2\,b^2x^2)}}{80\,\pi b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erf(b*x)^2,x, algorithm="fricas")
```

```
[Out] 1/80*(16*pi*b^6*x^5*erf(b*x)^2 + 32*sqrt(pi)*(b^5*x^4 + 2*b^3*x^2 + 2*b)*er
f(b*x)*e^(-b^2*x^2) - 43*sqrt(2)*sqrt(pi)*sqrt(b^2)*erf(sqrt(2)*sqrt(b^2)*x
) + 4*(4*b^4*x^3 + 11*b^2*x)*e^(-2*b^2*x^2))/(pi*b^6)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x^4\,\mathrm{erf}^2\,(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4*erf(b*x)**2,x)
```

```
[Out] Integral(x**4*erf(b*x)**2, x)
```

Giac [A]
time = 0.43, size = 170, normalized size = 1.03

$$\frac{1}{5}\,x^{5}\operatorname{erf}\left(bx\right)^{2}+\frac{b\left(\frac{32\,\left(b^{4}x^{4}+2\,b^{2}x^{2}+2\right)\operatorname{erf}\left(bx\right)e^{\left(-b^{2}x^{2}\right)}}{b^{6}}+\frac{b^{4}\left(\frac{4\,\left(4\,b^{2}x^{3}+3\,x\right)e^{\left(-2\,b^{2}x^{2}\right)}}{b^{4}}+\frac{3\,\sqrt{2}\,\sqrt{\pi}\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{b^{5}}\right)+8\,b^{2}\left(\frac{4\,xe^{\left(-2\,b^{2}x^{2}\right)}}{b^{2}}+\frac{\sqrt{2}\,\sqrt{\pi}\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{b^{3}}\right)+\frac{32\,\sqrt{2}\,\sqrt{\pi}\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{b}}{\sqrt{\pi}\,b^{5}}\right)}{80\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erf(b*x)^2,x, algorithm="giac")
```

```
[Out] 1/5*x^5*erf(b*x)^2 + 1/80*b*(32*(b^4*x^4 + 2*b^2*x^2 + 2)*erf(b*x)*e^(-b^2*
x^2)/b^6 + (b^4*(4*(4*b^2*x^3 + 3*x)*e^(-2*b^2*x^2)/b^4 + 3*sqrt(2)*sqrt(pi
)*erf(-sqrt(2)*b*x)/b^5) + 8*b^2*(4*x*e^(-2*b^2*x^2)/b^2 + sqrt(2)*sqrt(pi)
*erf(-sqrt(2)*b*x)/b^3) + 32*sqrt(2)*sqrt(pi)*erf(-sqrt(2)*b*x)/b)/(sqrt(pi
)*b^5))/sqrt(pi)
```

Mupad [B]
time = 0.21, size = 131, normalized size = 0.79

$$\frac{x^5\,\mathrm{erf}\left(b\,x\right)^2}{5}+\frac{\frac{4\,\sqrt{\pi }\,{\mathrm{e}}^{-b^2\,x^2}\,\mathrm{erf}\left(b\,x\right)}{5}+\frac{b^3\,x^3\,{\mathrm{e}}^{-2\,b^2\,x^2}}{5}-\frac{43\,\sqrt{2}\,\sqrt{\pi }\,\mathrm{erf}\left(\sqrt{2}\,b\,x\right)}{80}+\frac{11\,b\,x\,{\mathrm{e}}^{-2\,b^2\,x^2}}{20}+\frac{4\,b^2\,x^2\,\sqrt{\pi }\,{\mathrm{e}}^{-b^2\,x^2}\,\mathrm{erf}\left(b\,x\right)}{5}+\frac{2\,b^4\,x^4\,\sqrt{\pi }\,{\mathrm{e}}^{-b^2\,x^2}\,\mathrm{erf}\left(b\,x\right)}{5}}{b^5\,\pi }$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erf(b*x)^2,x)
```

```
[Out] (x^5*erf(b*x)^2)/5 + ((4*pi^(1/2)*exp(-b^2*x^2)*erf(b*x))/5 + (b^3*x^3*exp(
-2*b^2*x^2))/5 - (43*2^(1/2)*pi^(1/2)*erf(2^(1/2)*b*x))/80 + (11*b*x*exp(-2
*b^2*x^2))/20 + (4*b^2*x^2*pi^(1/2)*exp(-b^2*x^2)*erf(b*x))/5 + (2*b^4*x^4*
pi^(1/2)*exp(-b^2*x^2)*erf(b*x))/5)/(b^5*pi)
```

3.30 $\int x^2 \mathbf{Erf}(bx)^2 \, dx$

Optimal. Leaf size=113

$$\frac{e^{-2b^2x^2}x}{3b^2\pi}+\frac{2e^{-b^2x^2}\mathrm{Erf}(bx)}{3b^3\sqrt{\pi}}+\frac{2e^{-b^2x^2}x^2\mathrm{Erf}(bx)}{3b\sqrt{\pi}}+\frac{1}{3}x^3\mathrm{Erf}(bx)^2-\frac{5\mathrm{Erf}\left(\sqrt{2}\,bx\right)}{6b^3\sqrt{2\pi}}$$

```
[Out] 1/3*x/b^2/exp(2*b^2*x^2)/Pi+1/3*x^3*erf(b*x)^2+2/3*erf(b*x)/b^3/exp(b^2*x^2
)/Pi^(1/2)+2/3*x^2*erf(b*x)/b/exp(b^2*x^2)/Pi^(1/2)-5/12*erf(b*x*2^(1/2))/b
^3*2^(1/2)/Pi^(1/2)
```

Rubi [A]
time = 0.09, antiderivative size = 113, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$,
Rules used = {6499, 6520, 6517, 2236, 2243}

$$-\frac{5\mathrm{Erf}\left(\sqrt{2}\,bx\right)}{6\sqrt{2\pi}\,b^3}+\frac{2x^2e^{-b^2x^2}\mathrm{Erf}(bx)}{3\sqrt{\pi}\,b}+\frac{xe^{-2b^2x^2}}{3\pi b^2}+\frac{2e^{-b^2x^2}\mathrm{Erf}(bx)}{3\sqrt{\pi}\,b^3}+\frac{1}{3}x^3\mathrm{Erf}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[x^2*Erf[b*x]^2,x]
```

```
[Out] x/(3*b^2*E^(2*b^2*x^2)*Pi) + (2*Erf[b*x])/(3*b^3*E^(b^2*x^2)*Sqrt[Pi]) + (2
*x^2*Erf[b*x])/(3*b*E^(b^2*x^2)*Sqrt[Pi]) + (x^3*Erf[b*x]^2)/3 - (5*Erf[Sqr
t[2]*b*x])/(6*b^3*Sqrt[2*Pi])
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6499

```
Int[Erf[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erf[b*x]^2/(
m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erf[b*x])/E^(b^
```

```
2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int x^2\text{erf}(bx)^2\,dx &= \frac{1}{3}x^3\text{erf}(bx)^2 - \frac{(4b)\int e^{-b^2x^2}x^3\text{erf}(bx)\,dx}{3\sqrt{\pi}} \\
&= \frac{2e^{-b^2x^2}x^2\text{erf}(bx)}{3b\sqrt{\pi}} + \frac{1}{3}x^3\text{erf}(bx)^2 - \frac{4\int e^{-2b^2x^2}x^2\,dx}{3\pi} - \frac{4\int e^{-b^2x^2}x\text{erf}(bx)\,dx}{3b\sqrt{\pi}} \\
&= \frac{e^{-2b^2x^2}x}{3b^2\pi} + \frac{2e^{-b^2x^2}\text{erf}(bx)}{3b^3\sqrt{\pi}} + \frac{2e^{-b^2x^2}x^2\text{erf}(bx)}{3b\sqrt{\pi}} + \frac{1}{3}x^3\text{erf}(bx)^2 - \frac{\int e^{-2b^2x^2}\,dx}{3b^2\pi} - \frac{4\int e^{-2b^2x^2}}{3b^2\pi} \\
&= \frac{e^{-2b^2x^2}x}{3b^2\pi} + \frac{2e^{-b^2x^2}\text{erf}(bx)}{3b^3\sqrt{\pi}} + \frac{2e^{-b^2x^2}x^2\text{erf}(bx)}{3b\sqrt{\pi}} + \frac{1}{3}x^3\text{erf}(bx)^2 - \frac{\sqrt{\frac{2}{\pi}}\,\text{erf}\left(\sqrt{2}\,bx\right)}{3b^3} - \frac{\text{erf}(}{6b}
\end{aligned}$$

Mathematica [A]
time = 0.05, size = 88, normalized size = 0.78

$$\frac{4be^{-2b^2x^2}x + 8e^{-b^2x^2}\sqrt{\pi}\,(1+b^2x^2)\,\text{Erf}(bx) + 4b^3\pi x^3\text{Erf}(bx)^2 - 5\sqrt{2\pi}\,\text{Erf}\left(\sqrt{2}\,bx\right)}{12b^3\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*Erf[b*x]^2,x]
```

```
[Out] ((4*b*x)/E^(2*b^2*x^2) + (8*Sqrt[Pi]*(1 + b^2*x^2)*Erf[b*x])/E^(b^2*x^2) +
4*b^3*Pi*x^3*Erf[b*x]^2 - 5*Sqrt[2*Pi]*Erf[Sqrt[2]*b*x])/(12*b^3*Pi)
```

Maple [A]
time = 0.39, size = 95, normalized size = 0.84

method	result	size
derivativedivides	$\frac{\frac{\operatorname{erf}(bx)^{2} b^{3} x^{3}}{3}-\frac{4 \operatorname{erf}(bx)\left(-\frac{b^{2} x^{2} \mathrm{e}^{-b^{2} x^{2}}}{2}-\frac{\mathrm{e}^{-b^{2} x^{2}}}{2}\right)}{3 \sqrt{\pi}}+\frac{-\frac{5 \sqrt{2}\, \sqrt{\pi}\, \operatorname{erf}\left(b x \sqrt{2}\right)}{12}+\frac{\mathrm{e}^{-2 b^{2} x^{2}} b x}{3}}{\pi}}{b^{3}}$	95
default	$\frac{\frac{\operatorname{erf}(bx)^{2} b^{3} x^{3}}{3}-\frac{4 \operatorname{erf}(bx)\left(-\frac{b^{2} x^{2} \mathrm{e}^{-b^{2} x^{2}}}{2}-\frac{\mathrm{e}^{-b^{2} x^{2}}}{2}\right)}{3 \sqrt{\pi}}+\frac{-\frac{5 \sqrt{2}\, \sqrt{\pi}\, \operatorname{erf}\left(b x \sqrt{2}\right)}{12}+\frac{\mathrm{e}^{-2 b^{2} x^{2}} b x}{3}}{\pi}}{b^{3}}$	95

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erf(b*x)^2,x,method=_RETURNVERBOSE)
```

```
[Out] 1/b^3*(1/3*erf(b*x)^2*b^3*x^3-4/3*erf(b*x)/Pi^(1/2)*(-1/2*b^2*x^2/exp(b^2*x
^2)-1/2/exp(b^2*x^2))+4/3/Pi*(-5/16*2^(1/2)*Pi^(1/2)*erf(b*x*2^(1/2))+1/4/e
xp(b^2*x^2)^2*b*x))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erf(b*x)^2,x, algorithm="maxima")
```

```
[Out] -1/3*integrate(4*(b^2*x^2 + 1)*e^(-2*b^2*x^2), x)/(pi*b^2) + 1/3*(pi*b^3*x^
3*erf(b*x)^2 + 2*(sqrt(pi)*b^2*x^2 + sqrt(pi))*erf(b*x)*e^(-b^2*x^2))/(pi*b
^3)
```

Fricas [A]
time = 0.38, size = 90, normalized size = 0.80

$$\frac{4\,\pi b^{4} x^{3} \operatorname{erf}\left(bx\right)^{2} + 4\,b^{2} x e^{\left(-2\,b^{2} x^{2}\right)} + 8\,\sqrt{\pi}\,\left(b^{3} x^{2} + b\right) \operatorname{erf}\left(bx\right) e^{\left(-b^{2} x^{2}\right)} - 5\,\sqrt{2}\,\sqrt{\pi}\,\sqrt{b^{2}}\,\operatorname{erf}\left(\sqrt{2}\,\sqrt{b^{2}}\,x\right)}{12\,\pi b^{4}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erf(b*x)^2,x, algorithm="fricas")
```

```
[Out] 1/12*(4*pi*b^4*x^3*erf(b*x)^2 + 4*b^2*x*e^(-2*b^2*x^2) + 8*sqrt(pi)*(b^3*x^
2 + b)*erf(b*x)*e^(-b^2*x^2) - 5*sqrt(2)*sqrt(pi)*sqrt(b^2)*erf(sqrt(2)*sqr
t(b^2)*x))/(pi*b^4)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x^{2} \operatorname{erf}^{2}\left(bx\right)\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*erf(b*x)**2,x)
```

```
[Out] Integral(x**2*erf(b*x)**2, x)
```

Giac [A]
time = 0.41, size = 111, normalized size = 0.98

$$\frac{1}{3}\,x^{3}\operatorname{erf}\left(bx\right)^{2}+\frac{b\left(\frac{8\,\left(b^{2}x^{2}+1\right)\operatorname{erf}\left(bx\right)e^{\left(-b^{2}x^{2}\right)}}{b^{4}}+\frac{b^{2}\left(\frac{4\,xe^{\left(-2\,b^{2}x^{2}\right)}}{b^{2}}+\frac{\sqrt{2}\,\sqrt{\pi}\,\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{b^{3}}\right)+\frac{4\,\sqrt{2}\,\sqrt{\pi}\,\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{b}}{\sqrt{\pi}\,b^{3}}\right)}{12\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erf(b*x)^2,x, algorithm="giac")
```

```
[Out] 1/3*x^3*erf(b*x)^2 + 1/12*b*(8*(b^2*x^2 + 1)*erf(b*x)*e^(-b^2*x^2)/b^4 + (b
^2*(4*x*e^(-2*b^2*x^2)/b^2 + sqrt(2)*sqrt(pi)*erf(-sqrt(2)*b*x)/b^3) + 4*sq
rt(2)*sqrt(pi)*erf(-sqrt(2)*b*x)/b)/(sqrt(pi)*b^3))/sqrt(pi)
```

Mupad [B]
time = 0.17, size = 90, normalized size = 0.80

$$\frac{x^{3}\operatorname{erf}(b\,x)^{2}}{3}+\frac{\frac{2\,\sqrt{\pi}\,\mathrm{e}^{-b^{2}\,x^{2}}\,\operatorname{erf}(b\,x)}{3}-\frac{5\,\sqrt{2}\,\sqrt{\pi}\,\operatorname{erf}\left(\sqrt{2}\,b\,x\right)}{12}+\frac{b\,x\,\mathrm{e}^{-2\,b^{2}\,x^{2}}}{3}+\frac{2\,b^{2}\,x^{2}\,\sqrt{\pi}\,\mathrm{e}^{-b^{2}\,x^{2}}\,\operatorname{erf}(b\,x)}{3}}{b^{3}\,\pi}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erf(b*x)^2,x)
```

```
[Out] (x^3*erf(b*x)^2)/3 + ((2*pi^(1/2)*exp(-b^2*x^2)*erf(b*x))/3 - (5*2^(1/2)*pi
^(1/2)*erf(2^(1/2)*b*x))/12 + (b*x*exp(-2*b^2*x^2))/3 + (2*b^2*x^2*pi^(1/2)
*exp(-b^2*x^2)*erf(b*x))/3)/(b^3*pi)
```

3.31 $\int \mathbf{Erf}(bx)^2\,dx$

Optimal. Leaf size=56

$$\frac{2e^{-b^2x^2}\text{Erf}(bx)}{b\sqrt{\pi}} + x\text{Erf}(bx)^2 - \frac{\sqrt{\frac{2}{\pi}}\,\text{Erf}\left(\sqrt{2}\,bx\right)}{b}$$

```
[Out] x*erf(b*x)^2-erf(b*x*2^(1/2))*2^(1/2)/Pi^(1/2)/b+2*erf(b*x)/b/exp(b^2*x^2)/
Pi^(1/2)
```

Rubi [A]
time = 0.04, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.667$, Rules used = {6487, 12, 6517, 2236}

$$\frac{2e^{-b^2x^2}\text{Erf}(bx)}{\sqrt{\pi}\,b} + x\text{Erf}(bx)^2 - \frac{\sqrt{\frac{2}{\pi}}\,\text{Erf}\left(\sqrt{2}\,bx\right)}{b}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]^2,x]
```

```
[Out] (2*Erf[b*x])/(b*E^(b^2*x^2)*Sqrt[Pi]) + x*Erf[b*x]^2 - (Sqrt[2/Pi]*Erf[Sqrt
[2]*b*x])/b
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 6487

```
Int[Erf[(a_.) + (b_.)*(x_)]^2, x_Symbol] :> Simp[(a + b*x)*(Erf[a + b*x]^2/
b), x] - Dist[4/Sqrt[Pi], Int[(a + b*x)*(Erf[a + b*x]/E^(a + b*x)^2), x], x
] /; FreeQ[{a, b}, x]
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
```

```
+ c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\begin{aligned}
\int \operatorname{erf}(bx)^2\,dx &= x\operatorname{erf}(bx)^2 - \frac{4\int be^{-b^2x^2}x\operatorname{erf}(bx)\,dx}{\sqrt{\pi}}\\
&= x\operatorname{erf}(bx)^2 - \frac{(4b)\int e^{-b^2x^2}x\operatorname{erf}(bx)\,dx}{\sqrt{\pi}}\\
&= \frac{2e^{-b^2x^2}\operatorname{erf}(bx)}{b\sqrt{\pi}} + x\operatorname{erf}(bx)^2 - \frac{4\int e^{-2b^2x^2}\,dx}{\pi}\\
&= \frac{2e^{-b^2x^2}\operatorname{erf}(bx)}{b\sqrt{\pi}} + x\operatorname{erf}(bx)^2 - \frac{\sqrt{\frac{2}{\pi}}\operatorname{erf}\left(\sqrt{2}\,bx\right)}{b}
\end{aligned}$$

Mathematica [A]
time = 0.02, size = 56, normalized size = 1.00

$$\frac{2e^{-b^2x^2}\operatorname{Erf}(bx)}{b\sqrt{\pi}} + x\operatorname{Erf}(bx)^2 - \frac{\sqrt{\frac{2}{\pi}}\operatorname{Erf}\left(\sqrt{2}\,bx\right)}{b}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]^2,x]
```

```
[Out] (2*Erf[b*x])/(b*E^(b^2*x^2)*Sqrt[Pi]) + x*Erf[b*x]^2 - (Sqrt[2/Pi]*Erf[Sqrt
[2]*b*x])/b
```

Maple [A]
time = 0.25, size = 48, normalized size = 0.86

method	result	size
derivativedivides	$\frac{\operatorname{erf}(bx)^2 bx+\frac{2\operatorname{erf}(bx)e^{-b^2x^2}}{\sqrt{\pi}}-\frac{\sqrt{2}\operatorname{erf}\left(bx\sqrt{2}\right)}{\sqrt{\pi}}}{b}$	48
default	$\frac{\operatorname{erf}(bx)^2 bx+\frac{2\operatorname{erf}(bx)e^{-b^2x^2}}{\sqrt{\pi}}-\frac{\sqrt{2}\operatorname{erf}\left(bx\sqrt{2}\right)}{\sqrt{\pi}}}{b}$	48

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2,x,method=_RETURNVERBOSE)
```

[Out] 1/b*(erf(b*x)^2*b*x+2*erf(b*x)/Pi^(1/2)*exp(-b^2*x^2)-1/Pi^(1/2)*2^(1/2)*erf(b*x*2^(1/2)))

Maxima [A]
time = 0.47, size = 62, normalized size = 1.11

$$\frac{\left(\sqrt{\pi}\,bx\,\mathrm{erf}\,(bx)^2\,e^{(b^2x^2)}+2\,\mathrm{erf}\,(bx)\right)e^{(-b^2x^2)}}{\sqrt{\pi}\,b}-\frac{\sqrt{2}\,\mathrm{erf}\left(\sqrt{2}\,bx\right)}{\sqrt{\pi}\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(erf(b*x)^2,x, algorithm="maxima")

[Out] (sqrt(pi)*b*x*erf(b*x)^2*e^(b^2*x^2) + 2*erf(b*x))*e^(-b^2*x^2)/(sqrt(pi)*b) - sqrt(2)*erf(sqrt(2)*b*x)/(sqrt(pi)*b)

Fricas [A]
time = 0.36, size = 63, normalized size = 1.12

$$\frac{\pi b^2x\,\mathrm{erf}\,(bx)^2+2\,\sqrt{\pi}\,b\,\mathrm{erf}\,(bx)\,e^{(-b^2x^2)}-\sqrt{2}\,\sqrt{\pi}\,\sqrt{b^2}\,\mathrm{erf}\left(\sqrt{2}\,\sqrt{b^2}\,x\right)}{\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(erf(b*x)^2,x, algorithm="fricas")

[Out] (pi*b^2*x*erf(b*x)^2 + 2*sqrt(pi)*b*erf(b*x)*e^(-b^2*x^2) - sqrt(2)*sqrt(pi)*sqrt(b^2)*erf(sqrt(2)*sqrt(b^2)*x))/(pi*b^2)

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \mathrm{erf}^2\,(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(erf(b*x)**2,x)

[Out] Integral(erf(b*x)**2, x)

Giac [A]
time = 0.43, size = 48, normalized size = 0.86

$$x\,\mathrm{erf}\,(bx)^2+\frac{b\left(\frac{2\,\mathrm{erf}(bx)e^{\left(-b^2x^2\right)}}{b^2}+\frac{\sqrt{2}\,\mathrm{erf}\left(-\sqrt{2}\,bx\right)}{b^2}\right)}{\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2,x, algorithm="giac")
```

```
[Out] x*erf(b*x)^2 + b*(2*erf(b*x)*e^(-b^2*x^2)/b^2 + sqrt(2)*erf(-sqrt(2)*b*x)/b
^2)/sqrt(pi)
```

Mupad [B]
time = 0.16, size = 44, normalized size = 0.79

$$x\,\mathrm{erf}(b\,x)^2+\frac{2\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erf}(b\,x)-\sqrt{2}\,\mathrm{erf}\left(\sqrt{2}\,b\,x\right)}{b\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2,x)
```

```
[Out] x*erf(b*x)^2 + (2*exp(-b^2*x^2)*erf(b*x) - 2^(1/2)*erf(2^(1/2)*b*x))/(b*pi^
(1/2))
```

3.32 $\int \frac{\text{Erf}(bx)^2}{x^2} \, dx$

Optimal. Leaf size=13

$$\text{Int}\left(\frac{\text{Erf}(bx)^2}{x^2}, x\right)$$

```
[Out] Unintegrable(erf(b*x)^2/x^2,x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\text{Erf}(bx)^2}{x^2} \, dx$$

Verification is not applicable to the result.

```
[In] Int[Erf[b*x]^2/x^2,x]
[Out] Defer[Int][Erf[b*x]^2/x^2, x]
```

Rubi steps

$$\int \frac{\text{erf}(bx)^2}{x^2} \, dx = \int \frac{\text{erf}(bx)^2}{x^2} \, dx$$

Mathematica [A]
time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{\text{Erf}(bx)^2}{x^2} \, dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erf[b*x]^2/x^2,x]
[Out] Integrate[Erf[b*x]^2/x^2, x]
```

Maple [A]
time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{\text{erf}\left(bx\right)^2}{x^2} \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2/x^2,x)
[Out] int(erf(b*x)^2/x^2,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^2,x, algorithm="maxima")
[Out] 4*b*integrate(erf(b*x)*e^(-b^2*x^2)/x, x)/sqrt(pi) - erf(b*x)^2/x
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^2,x, algorithm="fricas")
[Out] integral(erf(b*x)^2/x^2, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}^{2}(bx)}{x^{2}}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)**2/x**2,x)
[Out] Integral(erf(b*x)**2/x**2, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^2,x, algorithm="giac")
[Out] integrate(erf(b*x)^2/x^2, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.08

$$\int \frac{\operatorname{erf}(b\,x)^2}{x^2}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2/x^2,x)
[Out] int(erf(b*x)^2/x^2, x)
```

3.33 $\int \frac{\text{Erf}(bx)^2}{x^4} \, dx$

Optimal. Leaf size=13

$$\text{Int}\left(\frac{\text{Erf}(bx)^2}{x^4},x\right)$$

```
[Out] Unintegrable(erf(b*x)^2/x^4,x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\text{Erf}(bx)^2}{x^4} \, dx$$

Verification is not applicable to the result.

```
[In] Int[Erf[b*x]^2/x^4,x]
```

```
[Out] Defer[Int][Erf[b*x]^2/x^4, x]
```

Rubi steps

$$\int \frac{\text{erf}(bx)^2}{x^4} \, dx = \int \frac{\text{erf}(bx)^2}{x^4} \, dx$$

Mathematica [A]
time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{\text{Erf}(bx)^2}{x^4} \, dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erf[b*x]^2/x^4,x]
```

```
[Out] Integrate[Erf[b*x]^2/x^4, x]
```

Maple [A]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\text{erf}\,(bx)^2}{x^4} \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2/x^4,x)
```

```
[Out] int(erf(b*x)^2/x^4,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^4,x, algorithm="maxima")
```

```
[Out] 4/3*b*integrate(erf(b*x)*e^(-b^2*x^2)/x^3, x)/sqrt(pi) - 1/3*erf(b*x)^2/x^3
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^4,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x)^2/x^4, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}^{2}(bx)}{x^{4}}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)**2/x**4,x)
```

```
[Out] Integral(erf(b*x)**2/x**4, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^4,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)^2/x^4, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.08

$$\int \frac{\mathrm{erf}(b\,x)^2}{x^4}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2/x^4,x)
```

```
[Out] int(erf(b*x)^2/x^4, x)
```

3.34 $\int \frac{\mathbf{Erf}(bx)^2}{x^6}\,dx$

Optimal. Leaf size=13

$$\operatorname{Int}\left(\frac{\operatorname{Erf}(bx)^2}{x^6},x\right)$$

```
[Out] Unintegrable(erf(b*x)^2/x^6,x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\operatorname{Erf}(bx)^2}{x^6}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erf[b*x]^2/x^6,x]
```

```
[Out] Defer[Int][Erf[b*x]^2/x^6, x]
```

Rubi steps

$$\int \frac{\operatorname{erf}(bx)^2}{x^6}\,dx = \int \frac{\operatorname{erf}(bx)^2}{x^6}\,dx$$

Mathematica [A]
time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{Erf}(bx)^2}{x^6}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erf[b*x]^2/x^6,x]
```

```
[Out] Integrate[Erf[b*x]^2/x^6, x]
```

Maple [A]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}\left(bx\right)^2}{x^6}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2/x^6,x)
[Out] int(erf(b*x)^2/x^6,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^6,x, algorithm="maxima")
[Out] 4/5*b*integrate(erf(b*x)*e^(-b^2*x^2)/x^5, x)/sqrt(pi) - 1/5*erf(b*x)^2/x^5
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^6,x, algorithm="fricas")
[Out] integral(erf(b*x)^2/x^6, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}^{2}(bx)}{x^{6}}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)**2/x**6,x)
[Out] Integral(erf(b*x)**2/x**6, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)^2/x^6,x, algorithm="giac")
[Out] integrate(erf(b*x)^2/x^6, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.08

$$\int \frac{{\mathrm{erf}\left(b\,x\right)}^2}{x^6} \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)^2/x^6,x)
```

```
[Out] int(erf(b*x)^2/x^6, x)
```

3.35 $\int (c+dx)^2 \mathbf{Erf}(a+bx)^2 \, dx$

Optimal. Leaf size=375

$$\frac{d(bc-ad)e^{-2(a+bx)^2}}{b^3\pi}+\frac{d^2e^{-2(a+bx)^2}(a+bx)}{3b^3\pi}+\frac{2d^2e^{-(a+bx)^2}\mathrm{Erf}(a+bx)}{3b^3\sqrt{\pi}}+\frac{2(bc-ad)^2e^{-(a+bx)^2}\mathrm{Erf}(a+bx)}{b^3\sqrt{\pi}}+2d($$

```
[Out] d*(-a*d+b*c)/b^3/exp(2*(b*x+a)^2)/Pi+1/3*d^2*(b*x+a)/b^3/exp(2*(b*x+a)^2)/P
i-1/2*d*(-a*d+b*c)*erf(b*x+a)^2/b^3+(-a*d+b*c)^2*(b*x+a)*erf(b*x+a)^2/b^3+d
*(-a*d+b*c)*(b*x+a)^2*erf(b*x+a)^2/b^3+1/3*d^2*(b*x+a)^3*erf(b*x+a)^2/b^3-(
-a*d+b*c)^2*erf((b*x+a)*2^(1/2))*2^(1/2)/Pi^(1/2)/b^3+2/3*d^2*erf(b*x+a)/b^
3/exp((b*x+a)^2)/Pi^(1/2)+2*(-a*d+b*c)^2*erf(b*x+a)/b^3/exp((b*x+a)^2)/Pi^(
1/2)+2*d*(-a*d+b*c)*(b*x+a)*erf(b*x+a)/b^3/exp((b*x+a)^2)/Pi^(1/2)+2/3*d^2*
(b*x+a)^2*erf(b*x+a)/b^3/exp((b*x+a)^2)/Pi^(1/2)-5/12*d^2*erf((b*x+a)*2^(1/
2))/b^3*2^(1/2)/Pi^(1/2)
```

Rubi [A]
time = 0.28, antiderivative size = 375, normalized size of antiderivative = 1.00, number of steps used = 16, number of rules used = 10, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {6502, 6487, 6517, 2236, 6499, 6520, 6508, 30, 2240, 2243}

$$\frac{d(a+bx)^2(bc-ad)\mathrm{Erf}(a+bx)^2}{b^3}+\frac{(a+bx)(bc-ad)^2\mathrm{Erf}(a+bx)^2}{b^3}+\frac{2de^{-(a+bx)^2}(a+bx)(bc-ad)\mathrm{Erf}(a+bx)}{\sqrt{\pi}b^3}-\frac{d(bc-ad)\mathrm{Erf}(a+bx)^2}{2b^3}+\frac{2e^{-(a+bx)^2}(bc-ad)^2\mathrm{Erf}(a+bx)}{\sqrt{\pi}b^3}-\frac{\sqrt{\frac{2}{\pi}}(bc-ad)^2\mathrm{Erf}\left(\sqrt{2}(a+bx)\right)}{b^3}+\frac{de^{-2(a+bx)^2}(bc-ad)}{\pi b^3}+\frac{d^2(a+bx)^3\mathrm{Erf}(a+bx)^2}{3b^3}+\frac{2d^2e^{-(a+bx)^2}(a+bx)^2\mathrm{Erf}(a+bx)}{3\sqrt{\pi}b^3}+\frac{2d^2e^{-(a+bx)^2}\mathrm{Erf}(a+bx)}{3\sqrt{\pi}b^3}-\frac{5d^2\mathrm{Erf}\left(\sqrt{2}(a+bx)\right)}{6\sqrt{2\pi}b^3}+\frac{d^2e^{-2(a+bx)^2}(a+bx)}{3\pi b^3}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)^2*Erf[a + b*x]^2,x]
```

```
[Out] (d*(b*c - a*d))/(b^3*E^(2*(a + b*x)^2)*Pi) + (d^2*(a + b*x))/(3*b^3*E^(2*(a
 + b*x)^2)*Pi) + (2*d^2*Erf[a + b*x])/(3*b^3*E^(a + b*x)^2*Sqrt[Pi]) + (2*(
b*c - a*d)^2*Erf[a + b*x])/(b^3*E^(a + b*x)^2*Sqrt[Pi]) + (2*d*(b*c - a*d)*
(a + b*x)*Erf[a + b*x])/(b^3*E^(a + b*x)^2*Sqrt[Pi]) + (2*d^2*(a + b*x)^2*E
rf[a + b*x])/(3*b^3*E^(a + b*x)^2*Sqrt[Pi]) - (d*(b*c - a*d)*Erf[a + b*x]^2
)/(2*b^3) + ((b*c - a*d)^2*(a + b*x)*Erf[a + b*x]^2)/b^3 + (d*(b*c - a*d)*(
a + b*x)^2*Erf[a + b*x]^2)/b^3 + (d^2*(a + b*x)^3*Erf[a + b*x]^2)/(3*b^3) -
 ((b*c - a*d)^2*Sqrt[2/Pi]*Erf[Sqrt[2]*(a + b*x)])/b^3 - (5*d^2*Erf[Sqrt[2]
*(a + b*x)])/(6*b^3*Sqrt[2*Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
```

```
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6487

```
Int[Erf[(a_.) + (b_.)*(x_)]^2, x_Symbol] :> Simp[(a + b*x)*(Erf[a + b*x]^2/
b), x] - Dist[4/Sqrt[Pi], Int[(a + b*x)*(Erf[a + b*x]/E^(a + b*x)^2), x], x
] /; FreeQ[{a, b}, x]
```

Rule 6499

```
Int[Erf[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erf[b*x]^2/(
m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erf[b*x])/E^(b^
2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6502

```
Int[Erf[(a_) + (b_.)*(x_)]^2*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Dist[
1/b^(m + 1), Subst[Int[ExpandIntegrand[Erf[x]^2, (b*c - a*d + d*x)^m, x], x
], x, a + b*x], x] /; FreeQ[{a, b, c, d}, x] && IGtQ[m, 0]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
```

```
+ c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$
\begin{aligned}
\int (c+dx)^2\operatorname{erf}(a+bx)^2\,dx &= \frac{\operatorname{Subst}\left(\int \left(b^2c^2\left(1+\frac{ad(-2bc+ad)}{b^2c^2}\right)\operatorname{erf}(x)^2+2bcd\left(1-\frac{ad}{bc}\right)x\operatorname{erf}(x)^2+d^2x^2\operatorname{erf}(x)^2\right.\right.}{b^3} \\
&= \frac{d^2\operatorname{Subst}\left(\int x^2\operatorname{erf}(x)^2\,dx,x,a+bx\right)}{b^3}+\frac{(2d(bc-ad))\operatorname{Subst}\left(\int x\operatorname{erf}(x)^2\,dx,x,a+\right.}{b^3} \\
&= \frac{(bc-ad)^2(a+bx)\operatorname{erf}(a+bx)^2}{b^3}+\frac{d(bc-ad)(a+bx)^2\operatorname{erf}(a+bx)^2}{b^3}+\frac{d^2(a+b}{} \\
&= \frac{2(bc-ad)^2e^{-(a+bx)^2}\operatorname{erf}(a+bx)}{b^3\sqrt{\pi}}+\frac{2d(bc-ad)e^{-(a+bx)^2}(a+bx)\operatorname{erf}(a+bx)}{b^3\sqrt{\pi}}+ \\
&= \frac{d(bc-ad)e^{-2(a+bx)^2}}{b^3\pi}+\frac{d^2e^{-2(a+bx)^2}(a+bx)}{3b^3\pi}+\frac{2d^2e^{-(a+bx)^2}\operatorname{erf}(a+bx)}{3b^3\sqrt{\pi}}+\frac{2(bc}{} \\
&= \frac{d(bc-ad)e^{-2(a+bx)^2}}{b^3\pi}+\frac{d^2e^{-2(a+bx)^2}(a+bx)}{3b^3\pi}+\frac{2d^2e^{-(a+bx)^2}\operatorname{erf}(a+bx)}{3b^3\sqrt{\pi}}+\frac{2(bc}{}
\end{aligned}
$$

Mathematica [A]
time = 0.70, size = 226, normalized size = 0.60

$$
\frac{\frac{4de^{-2(a+bx)^2}(3bc-2ad+bdx)}{\pi}+\frac{8e^{-(a+bx)^2}\left((1+a^2)d^2-abd(3c+dx)+b^2(3c^2+3cdx+d^2x^2)\right)\operatorname{Erf}(a+bx)}{\sqrt{\pi}}+2(-3bcd-6a^2bcd+2a^3d^2+3a(2b^2c^2+d^2)+2b^3x(3c^2+3cdx+d^2x^2))\operatorname{Erf}(a+bx)^2-(12b^2c^2-24abcd+(5+12a^2)d^2)\sqrt{\frac{2}{\pi}}\operatorname{Erf}\left(\sqrt{2}(a+bx)\right)}{12b^3}
$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^2*Erf[a + b*x]^2,x]
[Out] ((4*d*(3*b*c - 2*a*d + b*d*x))/(E^(2*(a + b*x)^2)*Pi) + (8*((1 + a^2)*d^2 -
 a*b*d*(3*c + d*x) + b^2*(3*c^2 + 3*c*d*x + d^2*x^2))*Erf[a + b*x])/(E^(a +
 b*x)^2*Sqrt[Pi]) + 2*(-3*b*c*d - 6*a^2*b*c*d + 2*a^3*d^2 + 3*a*(2*b^2*c^2
+ d^2) + 2*b^3*x*(3*c^2 + 3*c*d*x + d^2*x^2))*Erf[a + b*x]^2 - (12*b^2*c^2
```

```
- 24*a*b*c*d + (5 + 12*a^2)*d^2)*Sqrt[2/Pi]*Erf[Sqrt[2]*(a + b*x)])/(12*b^3
)
```

Maple [F]
time = 0.15, size = 0, normalized size = 0.00

$$\int (dx+c)^2 \operatorname{erf}(bx+a)^2 \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^2*erf(b*x+a)^2,x)
```

```
[Out] int((d*x+c)^2*erf(b*x+a)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erf(b*x+a)^2,x, algorithm="maxima")
```

```
[Out] 1/3*(d^2*x^3 + 3*c*d*x^2 + 3*c^2*x)*erf(b*x + a)^2 - 1/3*integrate(4*(b*d^2
*x^3 + 3*b*c*d*x^2 + 3*b*c^2*x)*erf(b*x + a)*e^(-b^2*x^2 - 2*a*b*x - a^2),
x)/sqrt(pi)
```

Fricas [A]
time = 0.38, size = 281, normalized size = 0.75

$$-\frac{\sqrt{2}\,\sqrt{\pi}\,(12\,b^2c^2 - 24\,abcd + (12\,a^2+5)d^2)\sqrt{b^2}\operatorname{erf}\left(\frac{\sqrt{2}\,\sqrt{b^2}\,(bx+a)}{b}\right) - 8\,\sqrt{\pi}\,(b^3d^2x^2 + 3\,b^3c^2 - 3\,ab^2cd + (a^2+1)bd^2 + (3\,b^3cd - ab^2d^2)x)\operatorname{erf}(bx+a)\,e^{(-b^2x^2-2\,abx-a^2)} - 2\,(2\,\pi b^4d^2x^3 + 6\,\pi b^4cdx^2 + 6\,\pi b^4c^2x + \pi(6\,ab^3c^2 - 3\,(2\,a^2+1)b^2cd + (2\,a^3+3\,a)bd^2))\operatorname{erf}(bx+a)^2 - 4\,(b^2d^2x + 3\,b^2cd - 2\,abd^2)e^{(-2\,b^2x^2-4\,abx-2\,a^2)}}{12\,\pi b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erf(b*x+a)^2,x, algorithm="fricas")
```

```
[Out] -1/12*(sqrt(2)*sqrt(pi)*(12*b^2*c^2 - 24*a*b*c*d + (12*a^2 + 5)*d^2)*sqrt(b
^2)*erf(sqrt(2)*sqrt(b^2)*(b*x + a)/b) - 8*sqrt(pi)*(b^3*d^2*x^2 + 3*b^3*c^
2 - 3*a*b^2*c*d + (a^2 + 1)*b*d^2 + (3*b^3*c*d - a*b^2*d^2)*x)*erf(b*x + a)
*e^(-b^2*x^2 - 2*a*b*x - a^2) - 2*(2*pi*b^4*d^2*x^3 + 6*pi*b^4*c*d*x^2 + 6*
pi*b^4*c^2*x + pi*(6*a*b^3*c^2 - 3*(2*a^2 + 1)*b^2*c*d + (2*a^3 + 3*a)*b*d^
2))*erf(b*x + a)^2 - 4*(b^2*d^2*x + 3*b^2*c*d - 2*a*b*d^2)*e^(-2*b^2*x^2 -
4*a*b*x - 2*a^2))/(pi*b^4)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int (c+dx)^2 \operatorname{erf}^2(a+bx)\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)**2*erf(b*x+a)**2,x)

[Out] Integral((c + d*x)**2*erf(a + b*x)**2, x)

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((d*x+c)^2*erf(b*x+a)^2,x, algorithm="giac")

[Out] integrate((d*x + c)^2*erf(b*x + a)^2, x)

Mupad [B]
time = 0.44, size = 359, normalized size = 0.96

$$\frac{\mathrm{erf}(a+b\,x)^2\,\left(\frac{a\,d^2}{2}-b\,\left(c\,d\,a^2+\frac{c\,d}{2}\right)+\frac{a^3\,d^2}{3}+a\,b^2\,c^2\right)}{b^3}+c^2\,x\,\mathrm{erf}(a+b\,x)^2+\frac{d^2\,x^3\,\mathrm{erf}(a+b\,x)^2}{3}-\frac{\mathrm{e}^{-2\,a^2-4\,a\,b\,x-2\,b^2\,x^2}\,\left(2\,a\,d^2-3\,b\,c\,d\right)}{3\,b^3\,\pi}+c\,d\,x^2\,\mathrm{erf}(a+b\,x)^2+\frac{2\,\mathrm{erf}(a+b\,x)\,\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}\,\left(a^2\,d^2-3\,a\,b\,c\,d+3\,b^2\,c^2+d^2\right)}{3\,b^3\,\sqrt{\pi}}-\frac{\sqrt{2}\,\mathrm{erf}\left(\sqrt{2}\,\left(a+b\,x\right)\right)\,\left(12\,a^2\,d^2-24\,a\,b\,c\,d+12\,b^2\,c^2+5\,d^2\right)}{12\,b^3\,\sqrt{\pi}}+\frac{d^2\,x\,\mathrm{e}^{-2\,a^2-4\,a\,b\,x-2\,b^2\,x^2}}{3\,b^2\,\pi}+\frac{2\,d^2\,x^2\,\mathrm{erf}(a+b\,x)\,\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}}{3\,b\,\sqrt{\pi}}-\frac{2\,x\,\mathrm{erf}(a+b\,x)\,\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}\,\left(a\,d^2-3\,b\,c\,d\right)}{3\,b^2\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(erf(a + b*x)^2*(c + d*x)^2,x)

[Out] (erf(a + b*x)^2*((a*d^2)/2 - b*((c*d)/2 + a^2*c*d) + (a^3*d^2)/3 + a*b^2*c^2))/b^3 + c^2*x*erf(a + b*x)^2 + (d^2*x^3*erf(a + b*x)^2)/3 - (exp(- 2*a^2 - 2*b^2*x^2 - 4*a*b*x)*(2*a*d^2 - 3*b*c*d))/(3*b^3*pi) + c*d*x^2*erf(a + b*x)^2 + (2*erf(a + b*x)*exp(- a^2 - b^2*x^2 - 2*a*b*x)*(d^2 + a^2*d^2 + 3*b^2*c^2 - 3*a*b*c*d))/(3*b^3*pi^(1/2)) - (2^(1/2)*erf(2^(1/2)*(a + b*x))*(5*d^2 + 12*a^2*d^2 + 12*b^2*c^2 - 24*a*b*c*d))/(12*b^3*pi^(1/2)) + (d^2*x*exp(- 2*a^2 - 2*b^2*x^2 - 4*a*b*x))/(3*b^2*pi) + (2*d^2*x^2*erf(a + b*x)*exp(- a^2 - b^2*x^2 - 2*a*b*x))/(3*b*pi^(1/2)) - (2*x*erf(a + b*x)*exp(- a^2 - b^2*x^2 - 2*a*b*x)*(a*d^2 - 3*b*c*d))/(3*b^2*pi^(1/2))

3.36 $\int (c+dx)\mathbf{Erf}(a+bx)^2\,dx$

Optimal. Leaf size=188

$$\frac{de^{-2(a+bx)^2}}{2b^2\pi}+\frac{2(bc-ad)e^{-(a+bx)^2}\mathrm{Erf}(a+bx)}{b^2\sqrt{\pi}}+\frac{de^{-(a+bx)^2}(a+bx)\mathrm{Erf}(a+bx)}{b^2\sqrt{\pi}}-\frac{d\mathrm{Erf}(a+bx)^2}{4b^2}+\frac{(bc-ad)(a+}{b}$$

```
[Out] 1/2*d/b^2/exp(2*(b*x+a)^2)/Pi-1/4*d*erf(b*x+a)^2/b^2+(-a*d+b*c)*(b*x+a)*erf
(b*x+a)^2/b^2+1/2*d*(b*x+a)^2*erf(b*x+a)^2/b^2-(-a*d+b*c)*erf((b*x+a)*2^(1/
2))*2^(1/2)/Pi^(1/2)/b^2+2*(-a*d+b*c)*erf(b*x+a)/b^2/exp((b*x+a)^2)/Pi^(1/2
)+d*(b*x+a)*erf(b*x+a)/b^2/exp((b*x+a)^2)/Pi^(1/2)
```

Rubi [A]
time = 0.12, antiderivative size = 188, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 9, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.643$, Rules used = {6502, 6487, 6517, 2236, 6499, 6520, 6508, 30, 2240}

$$\frac{(a+bx)(bc-ad)\mathrm{Erf}(a+bx)^2}{b^2}+\frac{2e^{-(a+bx)^2}(bc-ad)\mathrm{Erf}(a+bx)}{\sqrt{\pi}\,b^2}-\frac{\sqrt{\frac{2}{\pi}}\,(bc-ad)\mathrm{Erf}\left(\sqrt{2}\,(a+bx)\right)}{b^2}+\frac{d(a+bx)^2\mathrm{Erf}(a+bx)^2}{2b^2}-\frac{d\mathrm{Erf}(a+bx)^2}{4b^2}+\frac{de^{-(a+bx)^2}(a+bx)\mathrm{Erf}(a+bx)}{\sqrt{\pi}\,b^2}+\frac{de^{-2(a+bx)^2}}{2\pi b^2}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)*Erf[a + b*x]^2,x]
```

```
[Out] d/(2*b^2*E^(2*(a + b*x)^2)*Pi) + (2*(b*c - a*d)*Erf[a + b*x])/(b^2*E^(a + b
*x)^2*Sqrt[Pi]) + (d*(a + b*x)*Erf[a + b*x])/(b^2*E^(a + b*x)^2*Sqrt[Pi]) -
 (d*Erf[a + b*x]^2)/(4*b^2) + ((b*c - a*d)*(a + b*x)*Erf[a + b*x]^2)/b^2 +
(d*(a + b*x)^2*Erf[a + b*x]^2)/(2*b^2) - ((b*c - a*d)*Sqrt[2/Pi]*Erf[Sqrt[2
]*(a + b*x)])/b^2
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 6487

```
Int[Erf[(a_.) + (b_.)*(x_)]^2, x_Symbol] :> Simp[(a + b*x)*(Erf[a + b*x]^2/
b), x] - Dist[4/Sqrt[Pi], Int[(a + b*x)*(Erf[a + b*x]/E^(a + b*x)^2), x], x
] /; FreeQ[{a, b}, x]
```

Rule 6499

```
Int[Erf[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erf[b*x]^2/(
m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erf[b*x])/E^(b^
2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6502

```
Int[Erf[(a_) + (b_.)*(x_)]^2*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Dist[
1/b^(m + 1), Subst[Int[ExpandIntegrand[Erf[x]^2, (b*c - a*d + d*x)^m, x], x
], x, a + b*x], x] /; FreeQ[{a, b, c, d}, x] && IGtQ[m, 0]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\int (c+dx)\mathrm{erf}(a+bx)^2\,dx = \frac{\mathrm{Subst}\left(\int \left(bc\left(1-\frac{ad}{bc}\right)\mathrm{erf}(x)^2+dx\mathrm{erf}(x)^2\right)\,dx,x,a+bx\right)}{b^2}$$

$$= \frac{d\mathrm{Subst}\left(\int x\mathrm{erf}(x)^2\,dx,x,a+bx\right)}{b^2}+\frac{(bc-ad)\mathrm{Subst}\left(\int \mathrm{erf}(x)^2\,dx,x,a+bx\right)}{b^2}$$

$$= \frac{(bc-ad)(a+bx)\mathrm{erf}(a+bx)^2}{b^2}+\frac{d(a+bx)^2\mathrm{erf}(a+bx)^2}{2b^2}-\frac{(2d)\mathrm{Subst}\left(\int e^{-x^2}x^2\mathrm{e}\right.}{b^2\sqrt{}}$$

$$= \frac{2(bc-ad)e^{-(a+bx)^2}\mathrm{erf}(a+bx)}{b^2\sqrt{\pi}}+\frac{de^{-(a+bx)^2}(a+bx)\mathrm{erf}(a+bx)}{b^2\sqrt{\pi}}+\frac{(bc-ad)(a+}{}$$

$$= \frac{de^{-2(a+bx)^2}}{2b^2\pi}+\frac{2(bc-ad)e^{-(a+bx)^2}\mathrm{erf}(a+bx)}{b^2\sqrt{\pi}}+\frac{de^{-(a+bx)^2}(a+bx)\mathrm{erf}(a+bx)}{b^2\sqrt{\pi}}+$$

$$= \frac{de^{-2(a+bx)^2}}{2b^2\pi}+\frac{2(bc-ad)e^{-(a+bx)^2}\mathrm{erf}(a+bx)}{b^2\sqrt{\pi}}+\frac{de^{-(a+bx)^2}(a+bx)\mathrm{erf}(a+bx)}{b^2\sqrt{\pi}}-$$

Mathematica [A]
time = 0.28, size = 132, normalized size = 0.70

$$\frac{2de^{-2(a+bx)^2}+4e^{-(a+bx)^2}\sqrt{\pi}\,(2bc-ad+bdx)\mathrm{Erf}(a+bx)+\pi(4abc-d-2a^2d+4b^2cx+2b^2dx^2)\,\mathrm{Erf}(a+bx)^2+4(-bc+ad)\sqrt{2\pi}\,\mathrm{Erf}\left(\sqrt{2}\,(a+bx)\right)}{4b^2\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)*Erf[a + b*x]^2,x]
```

```
[Out] ((2*d)/E^(2*(a + b*x)^2) + (4*Sqrt[Pi]*(2*b*c - a*d + b*d*x)*Erf[a + b*x])/
E^(a + b*x)^2 + Pi*(4*a*b*c - d - 2*a^2*d + 4*b^2*c*x + 2*b^2*d*x^2)*Erf[a
+ b*x]^2 + 4*(-(b*c) + a*d)*Sqrt[2*Pi]*Erf[Sqrt[2]*(a + b*x)])/(4*b^2*Pi)
```

Maple [F]
time = 0.03, size = 0, normalized size = 0.00

$$\int (dx+c)\,\mathrm{erf}\,(bx+a)^2\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)*erf(b*x+a)^2,x)
```

```
[Out] int((d*x+c)*erf(b*x+a)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erf(b*x+a)^2,x, algorithm="maxima")
```

```
[Out] 1/2*(d*x^2 + 2*c*x)*erf(b*x + a)^2 - integrate(2*(b*d*x^2 + 2*b*c*x)*erf(b*
x + a)*e^(-b^2*x^2 - 2*a*b*x - a^2), x)/sqrt(pi)
```

Fricas [A]
time = 0.34, size = 171, normalized size = 0.91

$$-\frac{4\sqrt{2}\sqrt{\pi}\sqrt{b^2}\,(bc-ad)\operatorname{erf}\left(\frac{\sqrt{2}\sqrt{b^2}\,(bx+a)}{b}\right)-4\sqrt{\pi}\,(b^2dx+2b^2c-abd)\operatorname{erf}(bx+a)\,e^{(-b^2x^2-2abx-a^2)}-(2\pi b^3dx^2+4\pi b^3cx+\pi(4ab^2c-(2a^2+1)bd))\operatorname{erf}(bx+a)^2-2bde^{(-2b^2x^2-4abx-2a^2)}}{4\pi b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erf(b*x+a)^2,x, algorithm="fricas")
```

```
[Out] -1/4*(4*sqrt(2)*sqrt(pi)*sqrt(b^2)*(b*c - a*d)*erf(sqrt(2)*sqrt(b^2)*(b*x +
 a)/b) - 4*sqrt(pi)*(b^2*d*x + 2*b^2*c - a*b*d)*erf(b*x + a)*e^(-b^2*x^2 -
2*a*b*x - a^2) - (2*pi*b^3*d*x^2 + 4*pi*b^3*c*x + pi*(4*a*b^2*c - (2*a^2 +
1)*b*d))*erf(b*x + a)^2 - 2*b*d*e^(-2*b^2*x^2 - 4*a*b*x - 2*a^2))/(pi*b^3)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int (c+dx)\operatorname{erf}^2(a+bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erf(b*x+a)**2,x)
```

```
[Out] Integral((c + d*x)*erf(a + b*x)**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erf(b*x+a)^2,x, algorithm="giac")
```

```
[Out] integrate((d*x + c)*erf(b*x + a)^2, x)
```

Mupad [B]
time = 0.26, size = 186, normalized size = 0.99

$$\frac{d\,x^2\operatorname{erf}(a+b\,x)^2}{2}-\frac{\operatorname{erf}(a+b\,x)^2\,(2\,d\,a^2-4\,b\,c\,a+d)}{4\,b^2}+c\,x\operatorname{erf}(a+b\,x)^2+\frac{d\,\mathrm{e}^{-2\,a^2-4\,a\,b\,x-2\,b^2\,x^2}}{2\,b^2\,\pi}-\frac{\operatorname{erf}(a+b\,x)\,\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}\,(a\,d-2\,b\,c)}{b^2\,\sqrt{\pi}}+\frac{\sqrt{2}\operatorname{erf}\left(\sqrt{2}\,(a+b\,x)\right)\,(a\,d-b\,c)}{b^2\,\sqrt{\pi}}+\frac{d\,x\operatorname{erf}(a+b\,x)\,\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}}{b\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(a + b*x)^2*(c + d*x),x)
```

```
[Out] (d*x^2*erf(a + b*x)^2)/2 - (erf(a + b*x)^2*(d + 2*a^2*d - 4*a*b*c))/(4*b^2)
 + c*x*erf(a + b*x)^2 + (d*exp(- 2*a^2 - 2*b^2*x^2 - 4*a*b*x))/(2*b^2*pi) -
 (erf(a + b*x)*exp(- a^2 - b^2*x^2 - 2*a*b*x)*(a*d - 2*b*c))/(b^2*pi^(1/2))
 + (2^(1/2)*erf(2^(1/2)*(a + b*x))*(a*d - b*c))/(b^2*pi^(1/2)) + (d*x*erf(a
 + b*x)*exp(- a^2 - b^2*x^2 - 2*a*b*x))/(b*pi^(1/2))
```

3.37 $\int \mathbf{Erf}(a+bx)^2\,dx$

Optimal. Leaf size=71

$$\frac{2e^{-(a+bx)^2}\operatorname{Erf}(a+bx)}{b\sqrt{\pi}}+\frac{(a+bx)\operatorname{Erf}(a+bx)^2}{b}-\frac{\sqrt{\frac{2}{\pi}}\operatorname{Erf}\left(\sqrt{2}\,(a+bx)\right)}{b}$$

```
[Out] (b*x+a)*erf(b*x+a)^2/b-erf((b*x+a)*2^(1/2))*2^(1/2)/Pi^(1/2)/b+2*erf(b*x+a)
/b/exp((b*x+a)^2)/Pi^(1/2)
```

Rubi [A]
time = 0.12, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.375, Rules used = {6487, 6517, 2236}

$$\frac{(a+bx)\operatorname{Erf}(a+bx)^2}{b}+\frac{2e^{-(a+bx)^2}\operatorname{Erf}(a+bx)}{\sqrt{\pi}\,b}-\frac{\sqrt{\frac{2}{\pi}}\operatorname{Erf}\left(\sqrt{2}\,(a+bx)\right)}{b}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[a + b*x]^2,x]
```

```
[Out] (2*Erf[a + b*x])/(b*E^(a + b*x)^2*Sqrt[Pi]) + ((a + b*x)*Erf[a + b*x]^2)/b
- (Sqrt[2/Pi]*Erf[Sqrt[2]*(a + b*x)])/b
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 6487

```
Int[Erf[(a_.) + (b_.)*(x_)]^2, x_Symbol] :> Simp[(a + b*x)*(Erf[a + b*x]^2/
b), x] - Dist[4/Sqrt[Pi], Int[(a + b*x)*(Erf[a + b*x]/E^(a + b*x)^2), x], x
] /; FreeQ[{a, b}, x]
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$
\begin{aligned}
\int \operatorname{erf}(a+bx)^2\,dx &= \frac{(a+bx)\operatorname{erf}(a+bx)^2}{b} - \frac{4\int e^{-(a+bx)^2}(a+bx)\operatorname{erf}(a+bx)\,dx}{\sqrt{\pi}} \\
&= \frac{(a+bx)\operatorname{erf}(a+bx)^2}{b} - \frac{4\text{Subst}\left(\int e^{-x^2}x\operatorname{erf}(x)\,dx, x, a+bx\right)}{b\sqrt{\pi}} \\
&= \frac{2e^{-(a+bx)^2}\operatorname{erf}(a+bx)}{b\sqrt{\pi}} + \frac{(a+bx)\operatorname{erf}(a+bx)^2}{b} - \frac{4\text{Subst}\left(\int e^{-2x^2}\,dx, x, a+bx\right)}{b\pi} \\
&= \frac{2e^{-(a+bx)^2}\operatorname{erf}(a+bx)}{b\sqrt{\pi}} + \frac{(a+bx)\operatorname{erf}(a+bx)^2}{b} - \frac{\sqrt{\frac{2}{\pi}}\operatorname{erf}\left(\sqrt{2}\,(a+bx)\right)}{b}
\end{aligned}
$$

Mathematica [A]
time = 0.01, size = 66, normalized size = 0.93

$$
\frac{\frac{2e^{-(a+bx)^2}\text{Erf}(a+bx)}{\sqrt{\pi}} + (a+bx)\text{Erf}(a+bx)^2 - \sqrt{\frac{2}{\pi}}\,\text{Erf}\left(\sqrt{2}\,(a+bx)\right)}{b}
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[a + b*x]^2,x]
```

```
[Out] ((2*Erf[a + b*x])/(E^(a + b*x)^2*Sqrt[Pi]) + (a + b*x)*Erf[a + b*x]^2 - Sqr
t[2/Pi]*Erf[Sqrt[2]*(a + b*x)])/b
```

Maple [A]
time = 0.26, size = 59, normalized size = 0.83

method	result	size
derivativedivides	$\frac{\operatorname{erf}(bx+a)^2(bx+a)+\frac{2\operatorname{erf}(bx+a)\mathrm{e}^{-(bx+a)^2}}{\sqrt{\pi}}-\frac{\sqrt{2}\,\operatorname{erf}\left((bx+a)\sqrt{2}\right)}{\sqrt{\pi}}}{b}$	59
default	$\frac{\operatorname{erf}(bx+a)^2(bx+a)+\frac{2\operatorname{erf}(bx+a)\mathrm{e}^{-(bx+a)^2}}{\sqrt{\pi}}-\frac{\sqrt{2}\,\operatorname{erf}\left((bx+a)\sqrt{2}\right)}{\sqrt{\pi}}}{b}$	59

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x+a)^2,x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*(erf(b*x+a)^2*(b*x+a)+2*erf(b*x+a)/Pi^(1/2)*exp(-(b*x+a)^2)-1/Pi^(1/2)*
2^(1/2)*erf((b*x+a)*2^(1/2)))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)^2,x, algorithm="maxima")
```

```
[Out] x*erf(b*x + a)^2 - 4*b*integrate(x*erf(b*x + a)*e^(-b^2*x^2 - 2*a*b*x - a^2
), x)/sqrt(pi)
```

Fricas [A]
time = 0.37, size = 91, normalized size = 1.28

$$\frac{2\sqrt{\pi}\,b\operatorname{erf}\left(bx+a\right)e^{\left(-b^2x^2-2\,abx-a^2\right)}+\left(\pi b^2x+\pi ab\right)\operatorname{erf}\left(bx+a\right)^2-\sqrt{2}\,\sqrt{\pi}\,\sqrt{b^2}\,\operatorname{erf}\left(\frac{\sqrt{2}\,\sqrt{b^2}\,(bx+a)}{b}\right)}{\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)^2,x, algorithm="fricas")
```

```
[Out] (2*sqrt(pi)*b*erf(b*x + a)*e^(-b^2*x^2 - 2*a*b*x - a^2) + (pi*b^2*x + pi*a*
b)*erf(b*x + a)^2 - sqrt(2)*sqrt(pi)*sqrt(b^2)*erf(sqrt(2)*sqrt(b^2)*(b*x +
 a)/b))/(pi*b^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \operatorname{erf}^2\left(a+bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)**2,x)
```

```
[Out] Integral(erf(a + b*x)**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)^2,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x + a)^2, x)
```

Mupad [B]
time = 0.13, size = 79, normalized size = 1.11

$$x\,\mathrm{erf}(a+b\,x)^2+\frac{a\,\mathrm{erf}(a+b\,x)^2}{b}-\frac{\sqrt{2}\,\mathrm{erf}\left(\sqrt{2}\,(a+b\,x)\right)}{b\,\sqrt{\pi}}+\frac{2\,\mathrm{erf}(a+b\,x)\,\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}}{b\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(a + b*x)^2,x)
```

```
[Out] x*erf(a + b*x)^2 + (a*erf(a + b*x)^2)/b - (2^(1/2)*erf(2^(1/2)*(a + b*x)))/
(b*pi^(1/2)) + (2*erf(a + b*x)*exp(- a^2 - b^2*x^2 - 2*a*b*x))/(b*pi^(1/2))
```

3.38 $\int \frac{\textbf{Erf}(a+bx)^2}{c+dx}\,dx$

Optimal. Leaf size=19

$$\text{Int}\left(\frac{\text{Erf}(a+bx)^2}{c+dx},x\right)$$

```
[Out] Unintegrable(erf(b*x+a)^2/(d*x+c),x)
```

Rubi [A]
time = 0.02, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\text{Erf}(a+bx)^2}{c+dx}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erf[a + b*x]^2/(c + d*x),x]
```

```
[Out] Defer[Int][Erf[a + b*x]^2/(c + d*x), x]
```

Rubi steps

$$\int \frac{\text{erf}(a+bx)^2}{c+dx}\,dx = \int \frac{\text{erf}(a+bx)^2}{c+dx}\,dx$$

Mathematica [A]
time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{\text{Erf}(a+bx)^2}{c+dx}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erf[a + b*x]^2/(c + d*x),x]
```

```
[Out] Integrate[Erf[a + b*x]^2/(c + d*x), x]
```

Maple [A]
time = 0.18, size = 0, normalized size = 0.00

$$\int \frac{\text{erf}\left(bx+a\right)^2}{dx+c}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x+a)^2/(d*x+c),x)
[Out] int(erf(b*x+a)^2/(d*x+c),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)^2/(d*x+c),x, algorithm="maxima")
[Out] integrate(erf(b*x + a)^2/(d*x + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)^2/(d*x+c),x, algorithm="fricas")
[Out] integral(erf(b*x + a)^2/(d*x + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}^2(a+bx)}{c+dx}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)**2/(d*x+c),x)
[Out] Integral(erf(a + b*x)**2/(c + d*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)^2/(d*x+c),x, algorithm="giac")
[Out] integrate(erf(b*x + a)^2/(d*x + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{\operatorname{erf}(a+b\,x)^2}{c+d\,x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(a + b*x)^2/(c + d*x),x)
```

```
[Out] int(erf(a + b*x)^2/(c + d*x), x)
```

3.39 $\int \frac{\mathbf{Erf}(a+bx)^2}{(c+dx)^2}\,dx$

Optimal. Leaf size=19

$$\operatorname{Int}\left(\frac{\operatorname{Erf}(a+bx)^2}{(c+dx)^2},x\right)$$

[Out] Unintegrable(erf(b*x+a)^2/(d*x+c)^2,x)

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\operatorname{Erf}(a+bx)^2}{(c+dx)^2}\,dx$$

Verification is not applicable to the result.

[In] Int[Erf[a + b*x]^2/(c + d*x)^2,x]

[Out] Defer[Int][Erf[a + b*x]^2/(c + d*x)^2, x]

Rubi steps

$$\int \frac{\operatorname{erf}(a+bx)^2}{(c+dx)^2}\,dx = \int \frac{\operatorname{erf}(a+bx)^2}{(c+dx)^2}\,dx$$

Mathematica [A]
time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{Erf}(a+bx)^2}{(c+dx)^2}\,dx$$

Verification is not applicable to the result.

[In] Integrate[Erf[a + b*x]^2/(c + d*x)^2,x]

[Out] Integrate[Erf[a + b*x]^2/(c + d*x)^2, x]

Maple [A]
time = 0.16, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}\left(bx+a\right)^2}{\left(dx+c\right)^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x+a)^2/(d*x+c)^2,x)
```

```
[Out] int(erf(b*x+a)^2/(d*x+c)^2,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)^2/(d*x+c)^2,x, algorithm="maxima")
```

```
[Out] 4*b*integrate(erf(b*x + a)*e^(-b^2*x^2 - 2*a*b*x)/(sqrt(pi)*d^2*x*e^(a^2) +
 sqrt(pi)*c*d*e^(a^2)), x) - erf(b*x + a)^2/(d^2*x + c*d)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)^2/(d*x+c)^2,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x + a)^2/(d^2*x^2 + 2*c*d*x + c^2), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}^2(a+bx)}{(c+dx)^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)**2/(d*x+c)**2,x)
```

```
[Out] Integral(erf(a + b*x)**2/(c + d*x)**2, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x+a)^2/(d*x+c)^2,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x + a)^2/(d*x + c)^2, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{\operatorname{erf}(a+b\,x)^2}{(c+d\,x)^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(a + b*x)^2/(c + d*x)^2,x)
```

```
[Out] int(erf(a + b*x)^2/(c + d*x)^2, x)
```

3.40 $\int x^2 \mathbf{Erf}(d(a+b\log(cx^n)))\,dx$

Optimal. Leaf size=102

$$\frac{1}{3}x^3\operatorname{Erf}(d(a+b\log(cx^n)))-\frac{1}{3}e^{\frac{9-12abd^2n}{4b^2d^2n^2}}x^3(cx^n)^{-3/n}\operatorname{Erf}\left(\frac{2abd^2-\frac{3}{n}+2b^2d^2\log(cx^n)}{2bd}\right)$$

```
[Out] 1/3*x^3*erf(d*(a+b*ln(c*x^n)))-1/3*exp(1/4*(-12*a*b*d^2*n+9)/b^2/d^2/n^2)*x
^3*erf(1/2*(2*a*b*d^2-3/n+2*b^2*d^2*ln(c*x^n))/b/d)/((c*x^n)^(3/n))
```

Rubi [A]
time = 0.11, antiderivative size = 102, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.294$, Rules used = {6536, 2314, 2308, 2266, 2236}

$$\frac{1}{3}x^3\operatorname{Erf}(d(a+b\log(cx^n)))-\frac{1}{3}x^3(cx^n)^{-3/n}e^{\frac{9-12abd^2n}{4b^2d^2n^2}}\operatorname{Erf}\left(\frac{2abd^2+2b^2d^2\log(cx^n)-\frac{3}{n}}{2bd}\right)$$

Antiderivative was successfully verified.

```
[In] Int[x^2*Erf[d*(a + b*Log[c*x^n])],x]
```

```
[Out] (x^3*Erf[d*(a + b*Log[c*x^n])])/3 - (E^((9 - 12*a*b*d^2*n)/(4*b^2*d^2*n^2))
*x^3*Erf[(2*a*b*d^2 - 3/n + 2*b^2*d^2*Log[c*x^n])/(2*b*d)])/(3*(c*x^n)^(3/n
))
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2314

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^m*((c*(d + e*x)^n)^(2
*a*b*f*Log[F])/(d + e*x)^(m + 2*a*b*f*n*Log[F])), Int[(d + e*x)^(m + 2*a*b*
f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2), x], x] /; FreeQ[{F, a,
b, c, d, e, f, g, h, m, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 6536

```
Int[Erf[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_))^(m_.), x_
Symbol] :> Simp[(e*x)^(m + 1)*(Erf[d*(a + b*Log[c*x^n])]/(e*(m + 1))), x] -
 Dist[2*b*d*(n/(Sqrt[Pi]*(m + 1))), Int[(e*x)^m/E^(d*(a + b*Log[c*x^n]))^2,
 x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int x^2\operatorname{erf}(d(a+b\log(cx^n)))\,dx &= \frac{1}{3}x^3\operatorname{erf}(d(a+b\log(cx^n))) - \frac{(2bdn)\int e^{-d^2(a+b\log(cx^n))^2}x^2\,dx}{3\sqrt{\pi}} \\
&= \frac{1}{3}x^3\operatorname{erf}(d(a+b\log(cx^n))) - \frac{(2bdn)\int \exp\left(-a^2d^2-2abd^2\log(cx^n)-b^2d^2\,\mathrm{l}\cdots\right.}{3\sqrt{\pi}} \\
&= \frac{1}{3}x^3\operatorname{erf}(d(a+b\log(cx^n))) - \frac{(2bdn)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}x^2(cx^n)^{-2abd^2}\,dx}{3\sqrt{\pi}} \\
&= \frac{1}{3}x^3\operatorname{erf}(d(a+b\log(cx^n))) - \frac{\left(2bdnx^{2abd^2n}(cx^n)^{-2abd^2}\right)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}\cdots}{3\sqrt{\pi}} \\
&= \frac{1}{3}x^3\operatorname{erf}(d(a+b\log(cx^n))) - \frac{\left(2bdx^3(cx^n)^{-2abd^2-\frac{3-2abd^2n}{n}}\right)\operatorname{Subst}\left(\int\exp\left(-\cdots\right.\right.}{3\sqrt{\cdots}} \\
&= \frac{1}{3}x^3\operatorname{erf}(d(a+b\log(cx^n))) - \frac{\left(2bde^{\frac{9-12abd^2n}{4b^2d^2n^2}}x^3(cx^n)^{-2abd^2-\frac{3-2abd^2n}{n}}\right)\operatorname{Subst}\left(\cdots\right.}{3\sqrt{\cdots}} \\
&= \frac{1}{3}x^3\operatorname{erf}(d(a+b\log(cx^n))) - \frac{1}{3}e^{\frac{9-12abd^2n}{4b^2d^2n^2}}x^3(cx^n)^{-3/n}\operatorname{erf}\left(\frac{2abd^2-\frac{3}{n}+2b^2d^2\,\cdots}{2bd}\right.
\end{aligned}
$$

Mathematica [A]
time = 0.27, size = 88, normalized size = 0.86

$$
\frac{1}{3}\left(x^3\operatorname{Erf}(d(a+b\log(cx^n))) - e^{-\frac{3\left(\frac{-\frac{3}{d^2}+4abn}{b^2}+4n\log(cx^n)\right)}{4n^2}}x^3\operatorname{Erf}\left(ad-\frac{3}{2bdn}+bd\log(cx^n)\right)\right)
$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*Erf[d*(a + b*Log[c*x^n])],x]
```

```
[Out] (x^3*Erf[d*(a + b*Log[c*x^n])] - (x^3*Erf[a*d - 3/(2*b*d*n) + b*d*Log[c*x^n
]])/E^((3*((-3/d^2 + 4*a*b*n)/b^2 + 4*n*Log[c*x^n]))/(4*n^2)))/3
```

Maple [F]
time = 0.08, size = 0, normalized size = 0.00

$$\int x^{2} \operatorname{erf}\left(d(a+b\ln\left(c\,x^{n}\right))\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erf(d*(a+b*ln(c*x^n))),x)
```

```
[Out] int(x^2*erf(d*(a+b*ln(c*x^n))),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erf(d*(a+b*log(c*x^n))),x, algorithm="maxima")
```

```
[Out] 1/3*x^3*erf(b*d*log(x^n) + (b*log(c) + a)*d) - 2/3*b*d*n*integrate(x^2*e^(-
b^2*d^2*log(c)^2 - 2*b^2*d^2*log(c)*log(x^n) - b^2*d^2*log(x^n)^2 - 2*a*b*d
^2*log(x^n) - a^2*d^2), x)/(sqrt(pi)*c^(2*a*b*d^2))
```

Fricas [A]
time = 0.39, size = 125, normalized size = 1.23

$$\frac{1}{3}\,x^{3}\operatorname{erf}\left(bd\log\left(cx^{n}\right)+ad\right)-\frac{1}{3}\,\sqrt{b^{2}d^{2}n^{2}}\,\operatorname{erf}\left(\frac{\left(2\,b^{2}d^{2}n^{2}\log\left(x\right)+2\,b^{2}d^{2}n\log\left(c\right)+2\,abd^{2}n-3\right)\sqrt{b^{2}d^{2}n^{2}}}{2\,b^{2}d^{2}n^{2}}\right)e^{\left(-\frac{3\,\left(4\,b^{2}d^{2}n\log(c)+4\,abd^{2}n-3\right)}{4\,b^{2}d^{2}n^{2}}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erf(d*(a+b*log(c*x^n))),x, algorithm="fricas")
```

```
[Out] 1/3*x^3*erf(b*d*log(c*x^n) + a*d) - 1/3*sqrt(b^2*d^2*n^2)*erf(1/2*(2*b^2*d^
2*n^2*log(x) + 2*b^2*d^2*n*log(c) + 2*a*b*d^2*n - 3)*sqrt(b^2*d^2*n^2)/(b^2
*d^2*n^2))*e^(-3/4*(4*b^2*d^2*n*log(c) + 4*a*b*d^2*n - 3)/(b^2*d^2*n^2))
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x^{2}\operatorname{erf}\left(ad+bd\log\left(cx^{n}\right)\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*erf(d*(a+b*ln(c*x**n))),x)
```

```
[Out] Integral(x**2*erf(a*d + b*d*log(c*x**n)), x)
```

Giac [A]
time = 0.59, size = 85, normalized size = 0.83

$$\frac{1}{3}\,x^3\,\mathrm{erf}\left(bdn\log\left(x\right)+bd\log\left(c\right)+ad\right)+\frac{\mathrm{erf}\left(-bdn\log\left(x\right)-bd\log\left(c\right)-ad+\frac{3}{2\,bdn}\right)e^{\left(-\frac{3\,a}{bn}+\frac{9}{4\,b^2d^2n^2}\right)}}{3\,c^{\frac{3}{n}}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erf(d*(a+b*log(c*x^n))),x, algorithm="giac")
```

```
[Out] 1/3*x^3*erf(b*d*n*log(x) + b*d*log(c) + a*d) + 1/3*erf(-b*d*n*log(x) - b*d*
log(c) - a*d + 3/2/(b*d*n))*e^(-3*a/(b*n) + 9/4/(b^2*d^2*n^2))/c^(3/n)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^2\,\mathrm{erf}(d\,(a+b\,\ln\left(c\,x^n\right)))\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erf(d*(a + b*log(c*x^n))),x)
```

```
[Out] int(x^2*erf(d*(a + b*log(c*x^n))), x)
```

3.41 $\int x\mathbf{Erf}(d(a+b\log(cx^n)))\,dx$

Optimal. Leaf size=94

$$\frac{1}{2}x^2\mathrm{Erf}(d(a+b\log(cx^n)))-\frac{1}{2}e^{\frac{1-2abd^2n}{b^2d^2n^2}}x^2(cx^n)^{-2/n}\,\mathrm{Erf}\left(\frac{abd^2-\frac{1}{n}+b^2d^2\log(cx^n)}{bd}\right)$$

```
[Out] 1/2*x^2*erf(d*(a+b*ln(c*x^n)))-1/2*exp((-2*a*b*d^2*n+1)/b^2/d^2/n^2)*x^2*er
f((a*b*d^2-1/n+b^2*d^2*ln(c*x^n))/b/d)/((c*x^n)^(2/n))
```

Rubi [A]
time = 0.10, antiderivative size = 94, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}}=0.333$, Rules used = {6536, 2314, 2308, 2266, 2236}

$$\frac{1}{2}x^2\mathrm{Erf}(d(a+b\log(cx^n)))-\frac{1}{2}x^2(cx^n)^{-2/n}\,e^{\frac{1-2abd^2n}{b^2d^2n^2}}\,\mathrm{Erf}\left(\frac{abd^2+b^2d^2\log(cx^n)-\frac{1}{n}}{bd}\right)$$

Antiderivative was successfully verified.

```
[In] Int[x*Erf[d*(a + b*Log[c*x^n])],x]
```

```
[Out] (x^2*Erf[d*(a + b*Log[c*x^n])])/2 - (E^((1 - 2*a*b*d^2*n)/(b^2*d^2*n^2))*x^
2*Erf[(a*b*d^2 - n^(-1) + b^2*d^2*Log[c*x^n])/(b*d)])/(2*(c*x^n)^(2/n))
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2314

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^m*((c*(d + e*x)^n)^(2
```

```
*a*b*f*Log[F])/(d + e*x)^(m + 2*a*b*f*n*Log[F])), Int[(d + e*x)^(m + 2*a*b*
f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2), x], x] /; FreeQ[{F, a,
b, c, d, e, f, g, h, m, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 6536

```
Int[Erf[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_))^(m_.), x_
Symbol] :> Simp[(e*x)^(m + 1)*(Erf[d*(a + b*Log[c*x^n])]/(e*(m + 1))), x] -
 Dist[2*b*d*(n/(Sqrt[Pi]*(m + 1))), Int[(e*x)^m/E^(d*(a + b*Log[c*x^n]))^2,
 x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int x\mathrm{erf}(d(a+b\log(cx^n)))\,dx &= \frac{1}{2}x^2\mathrm{erf}(d(a+b\log(cx^n))) - \frac{(bdn)\int e^{-d^2(a+b\log(cx^n))^2}x\,dx}{\sqrt{\pi}}\\
&= \frac{1}{2}x^2\mathrm{erf}(d(a+b\log(cx^n))) - \frac{(bdn)\int \exp\left(-a^2d^2-2abd^2\log(cx^n)-b^2d^2\log\right.}{\sqrt{\pi}}\\
&= \frac{1}{2}x^2\mathrm{erf}(d(a+b\log(cx^n))) - \frac{(bdn)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}x(cx^n)^{-2abd^2}\,dx}{\sqrt{\pi}}\\
&= \frac{1}{2}x^2\mathrm{erf}(d(a+b\log(cx^n))) - \frac{\left(bdnx^{2abd^2n}(cx^n)^{-2abd^2}\right)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}x^{1-}}{\sqrt{\pi}}\\
&= \frac{1}{2}x^2\mathrm{erf}(d(a+b\log(cx^n))) - \frac{\left(bdx^2(cx^n)^{-2abd^2-\frac{2-2abd^2n}{n}}\right)\mathrm{Subst}\left(\int\exp\left(-a^2\right.\right.}{\sqrt{\pi}}\\
&= \frac{1}{2}x^2\mathrm{erf}(d(a+b\log(cx^n))) - \frac{\left(bde^{\frac{1-2abd^2n}{b^2d^2n^2}}x^2(cx^n)^{-2abd^2-\frac{2-2abd^2n}{n}}\right)\mathrm{Subst}\left(\int e\right.}{\sqrt{\pi}}\\
&= \frac{1}{2}x^2\mathrm{erf}(d(a+b\log(cx^n))) - \frac{1}{2}e^{\frac{1-2abd^2n}{b^2d^2n^2}}x^2(cx^n)^{-2/n}\,\mathrm{erf}\left(\frac{abd^2-\frac{1}{n}+b^2d^2\log(}{bd}\right.
\end{aligned}$$

Mathematica [A]
time = 0.21, size = 84, normalized size = 0.89

$$\frac{1}{2}\left(x^2\mathrm{Erf}(d(a+b\log(cx^n))) - e^{-\frac{\frac{-\frac{1}{d^2}+2abn}{b^2}+2n\log(cx^n)}{n^2}}x^2\mathrm{Erf}\left(ad-\frac{1}{bdn}+bd\log(cx^n)\right)\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x*Erf[d*(a + b*Log[c*x^n])],x]
```

```
[Out] (x^2*Erf[d*(a + b*Log[c*x^n])] - (x^2*Erf[a*d - 1/(b*d*n) + b*d*Log[c*x^n]]
)/E^(((-d^(-2) + 2*a*b*n)/b^2 + 2*n*Log[c*x^n])/n^2))/2
```

Maple [F]
time = 0.08, size = 0, normalized size = 0.00

$$\int x \operatorname{erf}\left(d(a+b\ln\left(c\,x^{n}\right))\right) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erf(d*(a+b*ln(c*x^n))),x)
```

```
[Out] int(x*erf(d*(a+b*ln(c*x^n))),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(d*(a+b*log(c*x^n))),x, algorithm="maxima")
```

```
[Out] 1/2*x^2*erf(b*d*log(x^n) + (b*log(c) + a)*d) - b*d*n*integrate(x*e^(-b^2*d^
2*log(c)^2 - 2*b^2*d^2*log(c)*log(x^n) - b^2*d^2*log(x^n)^2 - 2*a*b*d^2*log
(x^n) - a^2*d^2), x)/(sqrt(pi)*c^(2*a*b*d^2))
```

Fricas [A]
time = 0.40, size = 121, normalized size = 1.29

$$\frac{1}{2}\,x^{2} \operatorname{erf}\left(bd\log\left(cx^{n}\right)+ad\right)-\frac{1}{2}\,\sqrt{b^{2}d^{2}n^{2}}\,\operatorname{erf}\left(\frac{\left(b^{2}d^{2}n^{2}\log\left(x\right)+b^{2}d^{2}n\log\left(c\right)+abd^{2}n-1\right)\sqrt{b^{2}d^{2}n^{2}}}{b^{2}d^{2}n^{2}}\right)e^{\left(-\frac{2\,b^{2}d^{2}n\log\left(c\right)+2\,abd^{2}n-1}{b^{2}d^{2}n^{2}}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(d*(a+b*log(c*x^n))),x, algorithm="fricas")
```

```
[Out] 1/2*x^2*erf(b*d*log(c*x^n) + a*d) - 1/2*sqrt(b^2*d^2*n^2)*erf((b^2*d^2*n^2*
log(x) + b^2*d^2*n*log(c) + a*b*d^2*n - 1)*sqrt(b^2*d^2*n^2)/(b^2*d^2*n^2))
*e^(-(2*b^2*d^2*n*log(c) + 2*a*b*d^2*n - 1)/(b^2*d^2*n^2))
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x \operatorname{erf}\left(ad+bd\log\left(cx^{n}\right)\right) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(d*(a+b*ln(c*x**n))),x)
```

```
[Out] Integral(x*erf(a*d + b*d*log(c*x**n)), x)
```

Giac [A]
time = 0.76, size = 83, normalized size = 0.88

$$\frac{1}{2}\,x^{2}\,\mathrm{erf}\left(bdn\log\left(x\right)+bd\log\left(c\right)+ad\right)+\frac{\mathrm{erf}\left(-bdn\log\left(x\right)-bd\log\left(c\right)-ad+\frac{1}{bdn}\right)e^{\left(-\frac{2\,a}{bn}+\frac{1}{b^{2}d^{2}n^{2}}\right)}}{2\,c^{\frac{2}{n}}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(d*(a+b*log(c*x^n))),x, algorithm="giac")
```

```
[Out] 1/2*x^2*erf(b*d*n*log(x) + b*d*log(c) + a*d) + 1/2*erf(-b*d*n*log(x) - b*d*
log(c) - a*d + 1/(b*d*n))*e^(-2*a/(b*n) + 1/(b^2*d^2*n^2))/c^(2/n)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x\,\mathrm{erf}(d\,(a+b\,\ln\left(c\,x^n\right)))\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erf(d*(a + b*log(c*x^n))),x)
```

```
[Out] int(x*erf(d*(a + b*log(c*x^n))), x)
```

3.42 $\int \mathbf{Erf}(d(a+b\log(cx^n)))\,dx$

Optimal. Leaf size=93

$$x\mathrm{Erf}(d(a+b\log(cx^n)))-e^{\frac{1-4abd^2n}{4b^2d^2n^2}}x(cx^n)^{-1/n}\,\mathrm{Erf}\left(\frac{2abd^2-\frac{1}{n}+2b^2d^2\log(cx^n)}{2bd}\right)$$

```
[Out] x*erf(d*(a+b*ln(c*x^n)))-exp(1/4*(-4*a*b*d^2*n+1)/b^2/d^2/n^2)*x*erf(1/2*(2
*a*b*d^2-1/n+2*b^2*d^2*ln(c*x^n))/b/d)/((c*x^n)^(1/n))
```

Rubi [A]
time = 0.09, antiderivative size = 93, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}}=0.385$, Rules used = {6532, 2312, 2308, 2266, 2236}

$$x\mathrm{Erf}(d(a+b\log(cx^n)))-x(cx^n)^{-1/n}\,e^{\frac{1-4abd^2n}{4b^2d^2n^2}}\,\mathrm{Erf}\left(\frac{2abd^2+2b^2d^2\log(cx^n)-\frac{1}{n}}{2bd}\right)$$

Antiderivative was successfully verified.

```
[In] Int[Erf[d*(a + b*Log[c*x^n])],x]
```

```
[Out] x*Erf[d*(a + b*Log[c*x^n])] - (E^((1 - 4*a*b*d^2*n)/(4*b^2*d^2*n^2))*x*Erf[
(2*a*b*d^2 - n^(-1) + 2*b^2*d^2*Log[c*x^n])/(2*b*d)])/(c*x^n)^n^(-1)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2312

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.)), x
_Symbol] :> Dist[(c*(d + e*x)^n)^(2*a*b*f*Log[F])/(d + e*x)^(2*a*b*f*n*Log[
```

```
F]), Int[(d + e*x)^(2*a*b*f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2
), x], x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] &&  !IntegerQ[2*a*b*f*Log[F
]]
```

Rule 6532

```
Int[Erf[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)], x_Symbol] :> Simp[x*E
rf[d*(a + b*Log[c*x^n])], x] - Dist[2*b*d*(n/Sqrt[Pi]), Int[1/E^(d*(a + b*L
og[c*x^n]))^2, x], x] /; FreeQ[{a, b, c, d, n}, x]
```

Rubi steps

$$\begin{aligned}
\int \operatorname{erf}(d(a+b\log(cx^n)))\,dx &= x\operatorname{erf}(d(a+b\log(cx^n))) - \frac{(2bdn)\int e^{-d^2(a+b\log(cx^n))^2}\,dx}{\sqrt{\pi}} \\
&= x\operatorname{erf}(d(a+b\log(cx^n))) - \frac{(2bdn)\int \exp\left(-a^2d^2-2abd^2\log(cx^n)-b^2d^2\log^2(\right.}{\sqrt{\pi}} \\
&= x\operatorname{erf}(d(a+b\log(cx^n))) - \frac{(2bdn)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}(cx^n)^{-2abd^2}\,dx}{\sqrt{\pi}} \\
&= x\operatorname{erf}(d(a+b\log(cx^n))) - \frac{\left(2bdnx^{2abd^2n}(cx^n)^{-2abd^2}\right)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}x^{-2ab}}{\sqrt{\pi}} \\
&= x\operatorname{erf}(d(a+b\log(cx^n))) - \frac{\left(2bdx(cx^n)^{-2abd^2-\frac{1-2abd^2n}{n}}\right)\operatorname{Subst}\left(\int \exp\left(-a^2d^2+\right.\right.}{\sqrt{\pi}} \\
&= x\operatorname{erf}(d(a+b\log(cx^n))) - \frac{\left(2bde^{\frac{1-4abd^2n}{4b^2d^2n^2}}x(cx^n)^{-2abd^2-\frac{1-2abd^2n}{n}}\right)\operatorname{Subst}\left(\int \exp\left(\right.\right.}{\sqrt{\pi}} \\
&= x\operatorname{erf}(d(a+b\log(cx^n))) - e^{\frac{1-4abd^2n}{4b^2d^2n^2}}x(cx^n)^{-1/n}\operatorname{erf}\left(\frac{2abd^2-\frac{1}{n}+2b^2d^2\log(cx^n)}{2bd}\right.
\end{aligned}$$

Mathematica [A]
time = 0.19, size = 80, normalized size = 0.86

$$x\operatorname{Erf}(d(a+b\log(cx^n))) - e^{-\frac{\frac{-\frac{1}{d^2}+4abn}{b^2}+4n\log(cx^n)}{4n^2}}x\operatorname{Erf}\left(ad-\frac{1}{2bdn}+bd\log(cx^n)\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[d*(a + b*Log[c*x^n])],x]
```

```
[Out] x*Erf[d*(a + b*Log[c*x^n])] - (x*Erf[a*d - 1/(2*b*d*n) + b*d*Log[c*x^n]])/E
^(((-d^(-2) + 4*a*b*n)/b^2 + 4*n*Log[c*x^n])/(4*n^2))
```

Maple [F]
time = 0.05, size = 0, normalized size = 0.00

$$\int \operatorname{erf}\left(d(a+b\ln\left(c\,x^{n}\right))\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(d*(a+b*ln(c*x^n))),x)
```

```
[Out] int(erf(d*(a+b*ln(c*x^n))),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*log(c*x^n))),x, algorithm="maxima")
```

```
[Out] -2*b*d*n*integrate(e^(-b^2*d^2*log(c)^2 - 2*b^2*d^2*log(c)*log(x^n) - b^2*d
^2*log(x^n)^2 - 2*a*b*d^2*log(x^n) - a^2*d^2), x)/(sqrt(pi)*c^(2*a*b*d^2))
+ x*erf(b*d*log(x^n) + (b*log(c) + a)*d)
```

Fricas [A]
time = 0.40, size = 122, normalized size = 1.31

$$-\sqrt{b^{2}d^{2}n^{2}}\,\operatorname{erf}\left(\frac{\left(2\,b^{2}d^{2}n^{2}\log\left(x\right)+2\,b^{2}d^{2}n\log\left(c\right)+2\,abd^{2}n-1\right)\sqrt{b^{2}d^{2}n^{2}}}{2\,b^{2}d^{2}n^{2}}\right)e^{\left(-\frac{4\,b^{2}d^{2}n\log\left(c\right)+4\,abd^{2}n-1}{4\,b^{2}d^{2}n^{2}}\right)}+x\operatorname{erf}\left(bd\log\left(cx^{n}\right)+ad\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*log(c*x^n))),x, algorithm="fricas")
```

```
[Out] -sqrt(b^2*d^2*n^2)*erf(1/2*(2*b^2*d^2*n^2*log(x) + 2*b^2*d^2*n*log(c) + 2*a
*b*d^2*n - 1)*sqrt(b^2*d^2*n^2)/(b^2*d^2*n^2))*e^(-1/4*(4*b^2*d^2*n*log(c)
+ 4*a*b*d^2*n - 1)/(b^2*d^2*n^2)) + x*erf(b*d*log(c*x^n) + a*d)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \operatorname{erf}\left(d\left(a+b\log\left(cx^{n}\right)\right)\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*ln(c*x**n))),x)
```

```
[Out] Integral(erf(d*(a + b*log(c*x**n))), x)
```

Giac [A]
time = 0.51, size = 79, normalized size = 0.85

$$x \operatorname{erf}\left(bdn \log\left(x\right) + bd \log\left(c\right) + ad\right) + \frac{\operatorname{erf}\left(-bdn \log\left(x\right) - bd \log\left(c\right) - ad + \frac{1}{2 \, bdn}\right) e^{\left(-\frac{a}{bn} + \frac{1}{4 \, b^{2} d^{2} n^{2}}\right)}}{c^{\left(\frac{1}{n}\right)}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*log(c*x^n))),x, algorithm="giac")
```

```
[Out] x*erf(b*d*n*log(x) + b*d*log(c) + a*d) + erf(-b*d*n*log(x) - b*d*log(c) - a
*d + 1/2/(b*d*n))*e^(-a/(b*n) + 1/4/(b^2*d^2*n^2))/c^(1/n)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \operatorname{erf}(d\,(a+b\,\ln\left(c\,x^n\right)))\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(d*(a + b*log(c*x^n))),x)
```

```
[Out] int(erf(d*(a + b*log(c*x^n))), x)
```

3.43 $\int \frac{\mathbf{Erf}(d(a+b\log(cx^n)))}{x}\,dx$

Optimal. Leaf size=65

$$\frac{e^{-d^2(a+b\log(cx^n))^2}}{bdn\sqrt{\pi}}+\frac{\operatorname{Erf}(d(a+b\log(cx^n)))(a+b\log(cx^n))}{bn}$$

```
[Out] erf(d*(a+b*ln(c*x^n)))*(a+b*ln(c*x^n))/b/n+1/b/d/exp(d^2*(a+b*ln(c*x^n))^2)
/n/Pi^(1/2)
```

Rubi [A]
time = 0.03, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.059, Rules used = {6484}

$$\frac{e^{-d^2(a+b\log(cx^n))^2}}{\sqrt{\pi}\,bdn}+\frac{(a+b\log(cx^n))\operatorname{Erf}(d(a+b\log(cx^n)))}{bn}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[d*(a + b*Log[c*x^n])]/x,x]
```

```
[Out] 1/(b*d*E^(d^2*(a + b*Log[c*x^n])^2)*n*Sqrt[Pi]) + (Erf[d*(a + b*Log[c*x^n])
]*(a + b*Log[c*x^n]))/(b*n)
```

Rule 6484

```
Int[Erf[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[(a + b*x)*(Erf[a + b*x]/b),
x] + Simp[1/(b*Sqrt[Pi]*E^(a + b*x)^2), x] /; FreeQ[{a, b}, x]
```

Rubi steps

$$\begin{aligned}\int \frac{\operatorname{erf}(d(a+b\log(cx^n)))}{x}\,dx &= \frac{\operatorname{Subst}\left(\int \operatorname{erf}(d(a+bx))\,dx,x,\log(cx^n)\right)}{n}\\ &= \frac{\operatorname{Subst}\left(\int \operatorname{erf}(x)\,dx,x,ad+bd\log(cx^n)\right)}{bdn}\\ &= \frac{e^{-(ad+bd\log(cx^n))^2}}{bdn\sqrt{\pi}}+\frac{\operatorname{erf}(ad+bd\log(cx^n))(a+b\log(cx^n))}{bn}\end{aligned}$$

Mathematica [A]
time = 0.10, size = 79, normalized size = 1.22

$$\frac{\frac{e^{-d^2\left(a^2+b^2\log^2(cx^n)\right)}(cx^n)^{-2abd^2}}{bd\sqrt{\pi}}+\operatorname{Erf}(d(a+b\log(cx^n)))\left(\frac{a}{b}+\log(cx^n)\right)}{n}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[d*(a + b*Log[c*x^n])]/x,x]
```

```
[Out] (1/(b*d*E^(d^2*(a^2 + b^2*Log[c*x^n]^2))*Sqrt[Pi]*(c*x^n)^(2*a*b*d^2)) + Er
f[d*(a + b*Log[c*x^n])]*(a/b + Log[c*x^n]))/n
```

Maple [A]
time = 1.02, size = 62, normalized size = 0.95

method	result	size
derivativedivides	$\frac{\operatorname{erf}(ad+bd\ln(c\,x^n))(ad+bd\ln(c\,x^n))+\frac{\mathrm{e}^{-(ad+bd\ln(c\,x^n))^2}}{\sqrt{\pi}}}{nbd}$	62
default	$\frac{\operatorname{erf}(ad+bd\ln(c\,x^n))(ad+bd\ln(c\,x^n))+\frac{\mathrm{e}^{-(ad+bd\ln(c\,x^n))^2}}{\sqrt{\pi}}}{nbd}$	62

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(d*(a+b*ln(c*x^n)))/x,x,method=_RETURNVERBOSE)
```

```
[Out] 1/n/b/d*(erf(a*d+b*d*ln(c*x^n))*(a*d+b*d*ln(c*x^n))+1/Pi^(1/2)*exp(-(a*d+b*
d*ln(c*x^n))^2))
```

Maxima [A]
time = 0.26, size = 58, normalized size = 0.89

$$\frac{(b\log(cx^n)+a)d\operatorname{erf}((b\log(cx^n)+a)d)+\frac{e^{\left(-(b\log(cx^n)+a)^2d^2\right)}}{\sqrt{\pi}}}{bdn}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*log(c*x^n)))/x,x, algorithm="maxima")
```

```
[Out] ((b*log(c*x^n) + a)*d*erf((b*log(c*x^n) + a)*d) + e^(-(b*log(c*x^n) + a)^2*
d^2)/sqrt(pi))/(b*d*n)
```

Fricas [A]
time = 0.35, size = 119, normalized size = 1.83

$$\frac{(\pi bdn\log(x)+\pi bd\log(c)+\pi ad)\operatorname{erf}(bd\log(cx^n)+ad)+\sqrt{\pi}\,e^{\left(-b^2d^2n^2\log(x)^2-b^2d^2\log(c)^2-2\,abd^2\log(c)-a^2d^2-2\,(b^2d^2n\log(c)+abd^2n)\log(x)\right)}}{\pi bdn}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*log(c*x^n)))/x,x, algorithm="fricas")
```

```
[Out] ((pi*b*d*n*log(x) + pi*b*d*log(c) + pi*a*d)*erf(b*d*log(c*x^n) + a*d) + sqr
t(pi)*e^(-b^2*d^2*n^2*log(x)^2 - b^2*d^2*log(c)^2 - 2*a*b*d^2*log(c) - a^2*
d^2 - 2*(b^2*d^2*n*log(c) + a*b*d^2*n)*log(x)))/(pi*b*d*n)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}\left(ad+bd\log\left(cx^{n}\right)\right)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*ln(c*x**n)))/x,x)
```

```
[Out] Integral(erf(a*d + b*d*log(c*x**n))/x, x)
```

Giac [A]
time = 0.41, size = 67, normalized size = 1.03

$$\frac{\left(bdn\log\left(x\right)+bd\log\left(c\right)+ad\right)\operatorname{erf}\left(bdn\log\left(x\right)+bd\log\left(c\right)+ad\right)+\frac{e^{\left(-\left(bdn\log\left(x\right)+bd\log\left(c\right)+ad\right)^{2}\right)}}{\sqrt{\pi}}}{bdn}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*log(c*x^n)))/x,x, algorithm="giac")
```

```
[Out] ((b*d*n*log(x) + b*d*log(c) + a*d)*erf(b*d*n*log(x) + b*d*log(c) + a*d) + e
^(-(b*d*n*log(x) + b*d*log(c) + a*d)^2)/sqrt(pi))/(b*d*n)
```

Mupad [B]
time = 0.48, size = 121, normalized size = 1.86

$$\frac{\ln\left(c\,x^n\right)\,\mathrm{erf}\left(a\,d+b\,d\,\ln\left(c\,x^n\right)\right)}{n}+\frac{a\,d\,\mathrm{erfi}\left(a\,\sqrt{-d^2}+b\,\ln\left(c\,x^n\right)\,\sqrt{-d^2}\right)}{b\,n\,\sqrt{-d^2}}+\frac{{\mathrm{e}}^{-b^2\,d^2\,{\ln\left(c\,x^n\right)}^2}\,{\mathrm{e}}^{-a^2\,d^2}}{b\,d\,n\,\sqrt{\pi}\,{\left(c\,x^n\right)}^{2\,a\,b\,d^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(d*(a + b*log(c*x^n)))/x,x)
```

```
[Out] (log(c*x^n)*erf(a*d + b*d*log(c*x^n)))/n + (a*d*erfi(a*(-d^2)^(1/2) + b*log
(c*x^n)*(-d^2)^(1/2)))/(b*n*(-d^2)^(1/2)) + (exp(-b^2*d^2*log(c*x^n)^2)*exp
(-a^2*d^2))/(b*d*n*pi^(1/2)*(c*x^n)^(2*a*b*d^2))
```

3.44 $\int \frac{\operatorname{Erf}(d(a+b\log(cx^n)))}{x^2}\,dx$

Optimal. Leaf size=92

$$-\frac{\operatorname{Erf}(d(a+b\log(cx^n)))}{x}+\frac{e^{\frac{1}{4b^2d^2n^2}+\frac{a}{bn}}(cx^n)^{\frac{1}{n}}\operatorname{Erf}\left(\frac{2abd^2+\frac{1}{n}+2b^2d^2\log(cx^n)}{2bd}\right)}{x}$$

```
[Out] -erf(d*(a+b*ln(c*x^n)))/x+exp(1/4/b^2/d^2/n^2+a/b/n)*(c*x^n)^(1/n)*erf(1/2*
(2*a*b*d^2+1/n+2*b^2*d^2*ln(c*x^n))/b/d)/x
```

Rubi [A]
time = 0.11, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.294, Rules used = {6536, 2314, 2308, 2266, 2236}

$$\frac{(cx^n)^{\frac{1}{n}}e^{\frac{a}{bn}+\frac{1}{4b^2d^2n^2}}\operatorname{Erf}\left(\frac{2abd^2+2b^2d^2\log(cx^n)+\frac{1}{n}}{2bd}\right)}{x}-\frac{\operatorname{Erf}(d(a+b\log(cx^n)))}{x}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[d*(a + b*Log[c*x^n])]/x^2,x]
```

```
[Out] -(Erf[d*(a + b*Log[c*x^n])]/x) + (E^(1/(4*b^2*d^2*n^2) + a/(b*n))*(c*x^n)^n
^(-1)*Erf[(2*a*b*d^2 + n^(-1) + 2*b^2*d^2*Log[c*x^n])/(2*b*d)])/x
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2314

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^m*((c*(d + e*x)^n)^(2
*a*b*f*Log[F])/(d + e*x)^(m + 2*a*b*f*n*Log[F])), Int[(d + e*x)^(m + 2*a*b*
f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2), x], x] /; FreeQ[{F, a,
b, c, d, e, f, g, h, m, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 6536

```
Int[Erf[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_))^(m_.), x_
Symbol] :> Simp[(e*x)^(m + 1)*(Erf[d*(a + b*Log[c*x^n])]/(e*(m + 1))), x] -
 Dist[2*b*d*(n/(Sqrt[Pi]*(m + 1))), Int[(e*x)^m/E^(d*(a + b*Log[c*x^n]))^2,
 x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int \frac{\operatorname{erf}(d(a+b\log(cx^n)))}{x^2}\,dx &= -\frac{\operatorname{erf}(d(a+b\log(cx^n)))}{x}+\frac{(2bdn)\int\frac{e^{-d^2(a+b\log(cx^n))^2}}{x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{\operatorname{erf}(d(a+b\log(cx^n)))}{x}+\frac{(2bdn)\int\frac{\exp\left(-a^2d^2-2abd^2\log(cx^n)-b^2d^2\log^2(cx^n)\right)}{x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{\operatorname{erf}(d(a+b\log(cx^n)))}{x}+\frac{(2bdn)\int\frac{e^{-a^2d^2-b^2d^2\log^2(cx^n)}(cx^n)^{-2abd^2}}{x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{\operatorname{erf}(d(a+b\log(cx^n)))}{x}+\frac{\left(2bdnx^{2abd^2n}(cx^n)^{-2abd^2}\right)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}x^{-}}{\sqrt{\pi}}\\
&= -\frac{\operatorname{erf}(d(a+b\log(cx^n)))}{x}+\frac{\left(2bd(cx^n)^{-2abd^2-\frac{-1-2abd^2n}{n}}\right)\operatorname{Subst}\left(\int\exp\left(-a^2d^2\right.\right.}{\sqrt{\pi}\,x}\\
&= -\frac{\operatorname{erf}(d(a+b\log(cx^n)))}{x}+\frac{\left(2bde^{\frac{1}{4b^2d^2n^2}+\frac{a}{bn}}(cx^n)^{-2abd^2-\frac{-1-2abd^2n}{n}}\right)\operatorname{Subst}\left(\int e\right.}{\sqrt{\pi}\,x}\\
&= -\frac{\operatorname{erf}(d(a+b\log(cx^n)))}{x}+\frac{e^{\frac{1}{4b^2d^2n^2}+\frac{a}{bn}}(cx^n)^{\frac{1}{n}}\operatorname{erf}\left(\frac{2abd^2+\frac{1}{n}+2b^2d^2\log(cx^n)}{2bd}\right)}{x}
\end{aligned}$$

Mathematica [A]
time = 0.20, size = 80, normalized size = 0.87

$$\frac{-\operatorname{Erf}(d(a+b\log(cx^n)))+e^{\frac{\frac{\frac{1}{d^2}+4abn}{b^2}+4n\log(cx^n)}{4n^2}}\operatorname{Erf}\left(ad+\frac{1}{2bdn}+bd\log(cx^n)\right)}{x}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[d*(a + b*Log[c*x^n])]/x^2,x]
```

```
[Out] (-Erf[d*(a + b*Log[c*x^n])] + E^(((d^(-2) + 4*a*b*n)/b^2 + 4*n*Log[c*x^n])/
(4*n^2))*Erf[a*d + 1/(2*b*d*n) + b*d*Log[c*x^n]])/x
```

Maple [F]
time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}\left(d(a+b\ln\left(c\,x^{n}\right))\right)}{x^{2}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(d*(a+b*ln(c*x^n)))/x^2,x)
```

```
[Out] int(erf(d*(a+b*ln(c*x^n)))/x^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*log(c*x^n)))/x^2,x, algorithm="maxima")
```

```
[Out] 2*b*d*n*integrate(e^(-b^2*d^2*log(c)^2 - 2*b^2*d^2*log(c)*log(x^n) - b^2*d^
2*log(x^n)^2 - 2*a*b*d^2*log(x^n) - a^2*d^2)/x^2, x)/(sqrt(pi)*c^(2*a*b*d^2
)) - erf(b*d*log(x^n) + (b*log(c) + a)*d)/x
```

Fricas [A]
time = 0.36, size = 126, normalized size = 1.37

$$\frac{\sqrt{b^{2}d^{2}n^{2}}\,x\operatorname{erf}\left(\frac{\left(2\,b^{2}d^{2}n^{2}\log\left(x\right)+2\,b^{2}d^{2}n\log\left(c\right)+2\,abd^{2}n+1\right)\sqrt{b^{2}d^{2}n^{2}}}{2\,b^{2}d^{2}n^{2}}\right)e^{\left(\frac{4\,b^{2}d^{2}n\log\left(c\right)+4\,abd^{2}n+1}{4\,b^{2}d^{2}n^{2}}\right)}-\operatorname{erf}\left(bd\log\left(cx^{n}\right)+ad\right)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*log(c*x^n)))/x^2,x, algorithm="fricas")
```

```
[Out] (sqrt(b^2*d^2*n^2)*x*erf(1/2*(2*b^2*d^2*n^2*log(x) + 2*b^2*d^2*n*log(c) + 2
*a*b*d^2*n + 1)*sqrt(b^2*d^2*n^2)/(b^2*d^2*n^2))*e^(1/4*(4*b^2*d^2*n*log(c)
 + 4*a*b*d^2*n + 1)/(b^2*d^2*n^2)) - erf(b*d*log(c*x^n) + a*d))/x
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}\left(ad+bd\log\left(cx^{n}\right)\right)}{x^{2}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*ln(c*x**n)))/x**2,x)
```

```
[Out] Integral(erf(a*d + b*d*log(c*x**n))/x**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*log(c*x^n)))/x^2,x, algorithm="giac")
```

```
[Out] integrate(erf((b*log(c*x^n) + a)*d)/x^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erf}(d\,(a+b\,\ln\left(c\,x^n\right)))}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(d*(a + b*log(c*x^n)))/x^2,x)
```

```
[Out] int(erf(d*(a + b*log(c*x^n)))/x^2, x)
```

3.45 $\int \frac{\mathbf{Erf}(d(a+b\log(cx^n)))}{x^3}\,dx$

Optimal. Leaf size=95

$$-\frac{\operatorname{Erf}(d(a+b\log(cx^n)))}{2x^2}+\frac{e^{\frac{1+2abd^2n}{b^2d^2n^2}}(cx^n)^{2/n}\operatorname{Erf}\left(\frac{1+abd^2n+b^2d^2n\log(cx^n)}{bdn}\right)}{2x^2}$$

```
[Out] -1/2*erf(d*(a+b*ln(c*x^n)))/x^2+1/2*exp((2*a*b*d^2*n+1)/b^2/d^2/n^2)*(c*x^n
)^(2/n)*erf((1+a*b*d^2*n+b^2*d^2*n*ln(c*x^n))/b/d/n)/x^2
```

Rubi [A]
time = 0.10, antiderivative size = 95, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.294, Rules used = {6536, 2314, 2308, 2266, 2236}

$$\frac{(cx^n)^{2/n}e^{\frac{2abd^2n+1}{b^2d^2n^2}}\operatorname{Erf}\left(\frac{abd^2n+b^2d^2n\log(cx^n)+1}{bdn}\right)}{2x^2}-\frac{\operatorname{Erf}(d(a+b\log(cx^n)))}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[d*(a + b*Log[c*x^n])]/x^3,x]
```

```
[Out] -1/2*Erf[d*(a + b*Log[c*x^n])]/x^2 + (E^((1 + 2*a*b*d^2*n)/(b^2*d^2*n^2))*(
c*x^n)^(2/n)*Erf[(1 + a*b*d^2*n + b^2*d^2*n*Log[c*x^n])/(b*d*n)])/(2*x^2)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2314

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^m*((c*(d + e*x)^n)^(2
*a*b*f*Log[F])/(d + e*x)^(m + 2*a*b*f*n*Log[F])), Int[(d + e*x)^(m + 2*a*b*
f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2), x], x] /; FreeQ[{F, a,
b, c, d, e, f, g, h, m, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 6536

```
Int[Erf[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_))^(m_.), x_
Symbol] :> Simp[(e*x)^(m + 1)*(Erf[d*(a + b*Log[c*x^n])]/(e*(m + 1))), x] -
 Dist[2*b*d*(n/(Sqrt[Pi]*(m + 1))), Int[(e*x)^m/E^(d*(a + b*Log[c*x^n]))^2,
 x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rubi steps

$$\int \frac{\operatorname{erf}(d(a+b\log(cx^n)))}{x^3}\,dx = -\frac{\operatorname{erf}(d(a+b\log(cx^n)))}{2x^2} + \frac{(bdn)\int \frac{e^{-d^2(a+b\log(cx^n))^2}}{x^3}\,dx}{\sqrt{\pi}}$$

$$= -\frac{\operatorname{erf}(d(a+b\log(cx^n)))}{2x^2} + \frac{(bdn)\int \frac{\exp\left(-a^2d^2-2abd^2\log(cx^n)-b^2d^2\log^2(cx^n)\right)}{x^3}\,dx}{\sqrt{\pi}}$$

$$= -\frac{\operatorname{erf}(d(a+b\log(cx^n)))}{2x^2} + \frac{(bdn)\int \frac{e^{-a^2d^2-b^2d^2\log^2(cx^n)}(cx^n)^{-2abd^2}}{x^3}\,dx}{\sqrt{\pi}}$$

$$= -\frac{\operatorname{erf}(d(a+b\log(cx^n)))}{2x^2} + \frac{\left(bdnx^{2abd^2n}(cx^n)^{-2abd^2}\right)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}x^{-3-}}{\sqrt{\pi}}$$

$$= -\frac{\operatorname{erf}(d(a+b\log(cx^n)))}{2x^2} + \frac{\left(bd(cx^n)^{-2abd^2-\frac{-2-2abd^2n}{n}}\right)\operatorname{Subst}\left(\int \exp\left(-a^2d^2\right.\right.}{\sqrt{\pi}\,x^2}$$

$$= -\frac{\operatorname{erf}(d(a+b\log(cx^n)))}{2x^2} + \frac{\left(bde^{\frac{1+2abd^2n}{b^2d^2n^2}}(cx^n)^{-2abd^2-\frac{-2-2abd^2n}{n}}\right)\operatorname{Subst}\left(\int \exp\right.}{\sqrt{\pi}\,x^2}$$

$$= -\frac{\operatorname{erf}(d(a+b\log(cx^n)))}{2x^2} + \frac{e^{\frac{1+2abd^2n}{b^2d^2n^2}}(cx^n)^{2/n}\operatorname{erf}\left(\frac{1+abd^2n+b^2d^2n\log(cx^n)}{bdn}\right)}{2x^2}$$

Mathematica [A]
time = 0.19, size = 77, normalized size = 0.81

$$\frac{-\operatorname{Erf}(d(a+b\log(cx^n))) + e^{\frac{\frac{\frac{1}{d^2}+2abn}{b^2}+2n\log(cx^n)}{n^2}}\operatorname{Erf}\left(ad+\frac{1}{bdn}+bd\log(cx^n)\right)}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[d*(a + b*Log[c*x^n])]/x^3,x]
```

```
[Out] (-Erf[d*(a + b*Log[c*x^n])] + E^(((d^(-2) + 2*a*b*n)/b^2 + 2*n*Log[c*x^n])/
n^2)*Erf[a*d + 1/(b*d*n) + b*d*Log[c*x^n]])/(2*x^2)
```

Maple [F]
time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}\left(d\left(a+b\ln\left(c\,x^{n}\right)\right)\right)}{x^{3}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(d*(a+b*ln(c*x^n)))/x^3,x)
```

```
[Out] int(erf(d*(a+b*ln(c*x^n)))/x^3,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*log(c*x^n)))/x^3,x, algorithm="maxima")
```

```
[Out] b*d*n*integrate(e^(-b^2*d^2*log(c)^2 - 2*b^2*d^2*log(c)*log(x^n) - b^2*d^2*
log(x^n)^2 - 2*a*b*d^2*log(x^n) - a^2*d^2)/x^3, x)/(sqrt(pi)*c^(2*a*b*d^2))
 - 1/2*erf(b*d*log(x^n) + (b*log(c) + a)*d)/x^2
```

Fricas [A]
time = 0.37, size = 124, normalized size = 1.31

$$\frac{\sqrt{b^{2}d^{2}n^{2}}\,x^{2}\operatorname{erf}\left(\frac{\left(b^{2}d^{2}n^{2}\log\left(x\right)+b^{2}d^{2}n\log\left(c\right)+abd^{2}n+1\right)\sqrt{b^{2}d^{2}n^{2}}}{b^{2}d^{2}n^{2}}\right)e^{\left(\frac{2\,b^{2}d^{2}n\log\left(c\right)+2\,abd^{2}n+1}{b^{2}d^{2}n^{2}}\right)}-\operatorname{erf}\left(bd\log\left(cx^{n}\right)+ad\right)}{2\,x^{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*log(c*x^n)))/x^3,x, algorithm="fricas")
```

```
[Out] 1/2*(sqrt(b^2*d^2*n^2)*x^2*erf((b^2*d^2*n^2*log(x) + b^2*d^2*n*log(c) + a*b
*d^2*n + 1)*sqrt(b^2*d^2*n^2)/(b^2*d^2*n^2))*e^((2*b^2*d^2*n*log(c) + 2*a*b
*d^2*n + 1)/(b^2*d^2*n^2)) - erf(b*d*log(c*x^n) + a*d))/x^2
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}\left(ad+bd\log\left(cx^{n}\right)\right)}{x^{3}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*ln(c*x**n)))/x**3,x)
```

```
[Out] Integral(erf(a*d + b*d*log(c*x**n))/x**3, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(d*(a+b*log(c*x^n)))/x^3,x, algorithm="giac")
```

```
[Out] integrate(erf((b*log(c*x^n) + a)*d)/x^3, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erf}(d\,(a+b\,\ln(c\,x^n)))}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(d*(a + b*log(c*x^n)))/x^3,x)
```

```
[Out] int(erf(d*(a + b*log(c*x^n)))/x^3, x)
```

3.46 $\int (ex)^m \mathbf{Erf}(d(a+b\log(cx^n)))\,dx$

Optimal. Leaf size=125

$$\frac{(ex)^{1+m}\mathrm{Erf}(d(a+b\log(cx^n)))}{e(1+m)}+\frac{e^{\frac{(1+m)\left(1+m-4abd^2n\right)}{4b^2d^2n^2}}x(ex)^m(cx^n)^{-\frac{1+m}{n}}\mathrm{Erf}\left(\frac{1+m-2abd^2n-2b^2d^2n\log(cx^n)}{2bdn}\right)}{1+m}$$

```
[Out] (e*x)^(1+m)*erf(d*(a+b*ln(c*x^n)))/e/(1+m)+exp(1/4*(1+m)*(-4*a*b*d^2*n+m+1)
/b^2/d^2/n^2)*x*(e*x)^m*erf(1/2*(1+m-2*a*b*d^2*n-2*b^2*d^2*n*ln(c*x^n))/b/d
/n)/(1+m)/((c*x^n)^((1+m)/n))
```

Rubi [A]
time = 0.15, antiderivative size = 125, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {6536, 2314, 2308, 2266, 2236}

$$\frac{x(ex)^m(cx^n)^{-\frac{m+1}{n}}\exp\left(\frac{(m+1)(-4abd^2n+m+1)}{4b^2d^2n^2}\right)\mathrm{Erf}\left(\frac{-2abd^2n-2b^2d^2n\log(cx^n)+m+1}{2bdn}\right)}{m+1}+\frac{(ex)^{m+1}\mathrm{Erf}(d(a+b\log(cx^n)))}{e(m+1)}$$

Antiderivative was successfully verified.

```
[In] Int[(e*x)^m*Erf[d*(a + b*Log[c*x^n])],x]
```

```
[Out] ((e*x)^(1 + m)*Erf[d*(a + b*Log[c*x^n])])/(e*(1 + m)) + (E^(((1 + m)*(1 + m
 - 4*a*b*d^2*n))/(4*b^2*d^2*n^2))*x*(e*x)^m*Erf[(1 + m - 2*a*b*d^2*n - 2*b^
2*d^2*n*Log[c*x^n])/(2*b*d*n)])/((1 + m)*(c*x^n)^((1 + m)/n))
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2314

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^m*((c*(d + e*x)^n)^(2
*a*b*f*Log[F])/(d + e*x)^(m + 2*a*b*f*n*Log[F])), Int[(d + e*x)^(m + 2*a*b*
f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2), x], x] /; FreeQ[{F, a,
b, c, d, e, f, g, h, m, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 6536

```
Int[Erf[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_))^(m_.), x_
Symbol] :> Simp[(e*x)^(m + 1)*(Erf[d*(a + b*Log[c*x^n])]/(e*(m + 1))), x] -
 Dist[2*b*d*(n/(Sqrt[Pi]*(m + 1))), Int[(e*x)^m/E^(d*(a + b*Log[c*x^n]))^2,
 x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int (ex)^m \operatorname{erf}(d(a+b\log(cx^n)))\,dx &= \frac{(ex)^{1+m}\operatorname{erf}(d(a+b\log(cx^n)))}{e(1+m)} - \frac{(2bdn)\int e^{-d^2(a+b\log(cx^n))^2}(ex)^m\,dx}{(1+m)\sqrt{\pi}} \\
&= \frac{(ex)^{1+m}\operatorname{erf}(d(a+b\log(cx^n)))}{e(1+m)} - \frac{(2bdn)\int \exp\left(-a^2d^2-2abd^2\log(cx^n\right.}{(1+m)\sqrt{}} \\
&= \frac{(ex)^{1+m}\operatorname{erf}(d(a+b\log(cx^n)))}{e(1+m)} - \frac{(2bdn)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}(ex)^m\,(cx^{\cdots}}{(1+m)\sqrt{\pi}} \\
&= \frac{(ex)^{1+m}\operatorname{erf}(d(a+b\log(cx^n)))}{e(1+m)} - \frac{\left(2bdnx^{2abd^2n}(cx^n)^{-2abd^2}\right)\int e^{-a^2d^2-b^2\cdots}}{(1+m)\sqrt{\pi}} \\
&= \frac{(ex)^{1+m}\operatorname{erf}(d(a+b\log(cx^n)))}{e(1+m)} - \frac{\left(2bdnx^{-m+2abd^2n}(ex)^m\,(cx^n)^{-2abd^2}\right)\int\cdots}{(1+m)\cdots} \\
&= \frac{(ex)^{1+m}\operatorname{erf}(d(a+b\log(cx^n)))}{e(1+m)} - \frac{\left(2bdx(ex)^m\,(cx^n)^{-2abd^2-\frac{1+m-2abd^2n}{n}}\right)\cdots}{\cdots} \\
&= \frac{(ex)^{1+m}\operatorname{erf}(d(a+b\log(cx^n)))}{e(1+m)} - \frac{\left(2bd\exp\left(\frac{(1+m)(1+m-4abd^2n)}{4b^2d^2n^2}\right)x(ex)^{m}\cdots\right.}{\cdots} \\
&= \frac{(ex)^{1+m}\operatorname{erf}(d(a+b\log(cx^n)))}{e(1+m)} + \frac{\exp\left(\frac{(1+m)(1+m-4abd^2n)}{4b^2d^2n^2}\right)x(ex)^m\,(cx^n\cdots}{1+\cdots}
\end{aligned}
$$

Mathematica [A]

time = 0.37, size = 127, normalized size = 1.02

$$\frac{(ex)^m\left(x\text{Erf}(d(a+b\log(cx^n)))-e^{\frac{(1+m)\left(1+m-4abd^2n+4b^2d^2n^2\log(x)-4b^2d^2n\log(cx^n)\right)}{4b^2d^2n^2}}x^{-m}\text{Erf}\left(ad-\frac{1+m-2b^2d^2n\log(cx^n)}{2bdn}\right)\right)}{1+m}$$

Antiderivative was successfully verified.

```
[In] Integrate[(e*x)^m*Erf[d*(a + b*Log[c*x^n])],x]
```

```
[Out] ((e*x)^m*(x*Erf[d*(a + b*Log[c*x^n])] - (E^(((1 + m)*(1 + m - 4*a*b*d^2*n +
 4*b^2*d^2*n^2*Log[x] - 4*b^2*d^2*n*Log[c*x^n]))/(4*b^2*d^2*n^2))*Erf[a*d -
 (1 + m - 2*b^2*d^2*n*Log[c*x^n])/(2*b*d*n)])/x^m))/(1 + m)
```

Maple [F]
time = 0.05, size = 0, normalized size = 0.00

$$\int (ex)^m \operatorname{erf}\left(d(a+b\ln(c\,x^n))\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*erf(d*(a+b*ln(c*x^n))),x)
```

```
[Out] int((e*x)^m*erf(d*(a+b*ln(c*x^n))),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*erf(d*(a+b*log(c*x^n))),x, algorithm="maxima")
```

```
[Out] x*erf(b*d*log(x^n) + (b*log(c) + a)*d)*e^(m*log(x) + m)/(m + 1) - 2*b*d*n*i
ntegrate(e^(-b^2*d^2*log(c)^2 - 2*b^2*d^2*log(c)*log(x^n) - b^2*d^2*log(x^n
)^2 - 2*a*b*d^2*log(x^n) - a^2*d^2 + m*log(x) + m), x)/(sqrt(pi)*c^(2*a*b*d
^2)*(m + 1))
```

Fricas [A]
time = 0.37, size = 175, normalized size = 1.40

$$\frac{x\operatorname{erf}\left(bd\log\left(cx^n\right)+ad\right)e^{(m\log(x)+m)}-\sqrt{b^2d^2n^2}\operatorname{erf}\left(\frac{\left(2\,b^2d^2n^2\log(x)+2\,b^2d^2n\log(c)+2\,abd^2n-m-1\right)\sqrt{b^2d^2n^2}}{2\,b^2d^2n^2}\right)e^{\left(\frac{4\,b^2d^2mn^2-4\,\left(b^2d^2m+b^2d^2\right)n\log(c)+m^2-4\,\left(abd^2m+abd^2\right)n+2\,m+1}{4\,b^2d^2n^2}\right)}}{m+1}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*erf(d*(a+b*log(c*x^n))),x, algorithm="fricas")
```

```
[Out] (x*erf(b*d*log(c*x^n) + a*d)*e^(m*log(x) + m) - sqrt(b^2*d^2*n^2)*erf(1/2*(
2*b^2*d^2*n^2*log(x) + 2*b^2*d^2*n*log(c) + 2*a*b*d^2*n - m - 1)*sqrt(b^2*d
^2*n^2)/(b^2*d^2*n^2))*e^(1/4*(4*b^2*d^2*m*n^2 - 4*(b^2*d^2*m + b^2*d^2)*n*
log(c) + m^2 - 4*(a*b*d^2*m + a*b*d^2)*n + 2*m + 1)/(b^2*d^2*n^2)))/(m + 1)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int (ex)^m \operatorname{erf}(ad + bd\log(cx^n))\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*erf(d*(a+b*ln(c*x**n))),x)
[Out] Integral((e*x)**m*erf(a*d + b*d*log(c*x**n)), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*erf(d*(a+b*log(c*x^n))),x, algorithm="giac")
[Out] integrate((e*x)^m*erf((b*log(c*x^n) + a)*d), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \operatorname{erf}(d\,(a + b\,\ln(c\,x^n)))\,(e\,x)^m\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(d*(a + b*log(c*x^n)))*(e*x)^m,x)
[Out] int(erf(d*(a + b*log(c*x^n)))*(e*x)^m, x)
```

3.47 $\int e^{c-b^2x^2}\textbf{Erf}(bx)^2\,dx$

Optimal. Leaf size=21

$$\frac{e^c\sqrt{\pi}\,\text{Erf}(bx)^3}{6b}$$

```
[Out] 1/6*exp(c)*erf(b*x)^3*Pi^(1/2)/b
```

Rubi [A]
time = 0.02, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {6508, 30}

$$\frac{\sqrt{\pi}\,e^c\text{Erf}(bx)^3}{6b}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c - b^2*x^2)*Erf[b*x]^2,x]
```

```
[Out] (E^c*Sqrt[Pi]*Erf[b*x]^3)/(6*b)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rubi steps

$$\begin{aligned}\int e^{c-b^2x^2}\text{erf}(bx)^2\,dx &= \frac{\left(e^c\sqrt{\pi}\right)\text{Subst}\left(\int x^2\,dx, x, \text{erf}(bx)\right)}{2b}\\ &= \frac{e^c\sqrt{\pi}\,\text{erf}(bx)^3}{6b}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 21, normalized size = 1.00

$$\frac{e^c\sqrt{\pi}\,\text{Erf}(bx)^3}{6b}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c - b^2*x^2)*Erf[b*x]^2,x]
```

```
[Out] (E^c*Sqrt[Pi]*Erf[b*x]^3)/(6*b)
```

Maple [A]
time = 0.18, size = 17, normalized size = 0.81

method	result	size
default	$\frac{\mathrm{e}^{c}\,\mathrm{erf}(bx)^{3}\sqrt{\pi}}{6b}$	17

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(-b^2*x^2+c)*erf(b*x)^2,x,method=_RETURNVERBOSE)
```

```
[Out] 1/6*exp(c)*erf(b*x)^3*Pi^(1/2)/b
```

Maxima [A]
time = 0.27, size = 16, normalized size = 0.76

$$\frac{\sqrt{\pi}\,\operatorname{erf}(bx)^{3}e^{c}}{6\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erf(b*x)^2,x, algorithm="maxima")
```

```
[Out] 1/6*sqrt(pi)*erf(b*x)^3*e^c/b
```

Fricas [A]
time = 0.34, size = 16, normalized size = 0.76

$$\frac{\sqrt{\pi}\,\operatorname{erf}(bx)^{3}e^{c}}{6\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erf(b*x)^2,x, algorithm="fricas")
```

```
[Out] 1/6*sqrt(pi)*erf(b*x)^3*e^c/b
```

Sympy [A]
time = 0.41, size = 19, normalized size = 0.90

$$\begin{cases} \frac{\sqrt{\pi}\,e^{c}\operatorname{erf}^{3}(bx)}{6b} & \text{for}\ b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b**2*x**2+c)*erf(b*x)**2,x)
[Out] Piecewise((sqrt(pi)*exp(c)*erf(b*x)**3/(6*b), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erf(b*x)^2,x, algorithm="giac")
[Out] integrate(erf(b*x)^2*e^(-b^2*x^2 + c), x)
```

Mupad [B]
time = 0.11, size = 16, normalized size = 0.76

$$\frac{\sqrt{\pi}\,\mathrm{e}^c\,\mathrm{erf}(b\,x)^3}{6\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c - b^2*x^2)*erf(b*x)^2,x)
[Out] (pi^(1/2)*exp(c)*erf(b*x)^3)/(6*b)
```

3.48 $\int e^{c-b^2x^2}\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=21

$$\frac{e^c\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{4b}$$

[Out] 1/4*exp(c)*erf(b*x)^2*Pi^(1/2)/b

Rubi [A]
time = 0.01, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.118, Rules used = {6508, 30}

$$\frac{\sqrt{\pi}\,e^c\mathrm{Erf}(bx)^2}{4b}$$

Antiderivative was successfully verified.

[In] Int[E^(c - b^2*x^2)*Erf[b*x],x]

[Out] (E^c*Sqrt[Pi]*Erf[b*x]^2)/(4*b)

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rubi steps

$$\begin{aligned}\int e^{c-b^2x^2}\operatorname{erf}(bx)\,dx &= \frac{\left(e^c\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erf}(bx)\right)}{2b}\\ &= \frac{e^c\sqrt{\pi}\operatorname{erf}(bx)^2}{4b}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 21, normalized size = 1.00

$$\frac{e^c\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{4b}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c - b^2*x^2)*Erf[b*x],x]
```

```
[Out] (E^c*Sqrt[Pi]*Erf[b*x]^2)/(4*b)
```

Maple [A]
time = 0.22, size = 17, normalized size = 0.81

method	result	size
default	$\frac{\mathrm{e}^{c}\,\mathrm{erf}(bx)^{2}\sqrt{\pi}}{4b}$	17

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(-b^2*x^2+c)*erf(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/4*exp(c)*erf(b*x)^2*Pi^(1/2)/b
```

Maxima [A]
time = 0.26, size = 16, normalized size = 0.76

$$\frac{\sqrt{\pi}\,\operatorname{erf}(bx)^{2}\,e^{c}}{4\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erf(b*x),x, algorithm="maxima")
```

```
[Out] 1/4*sqrt(pi)*erf(b*x)^2*e^c/b
```

Fricas [A]
time = 0.34, size = 16, normalized size = 0.76

$$\frac{\sqrt{\pi}\,\operatorname{erf}(bx)^{2}\,e^{c}}{4\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erf(b*x),x, algorithm="fricas")
```

```
[Out] 1/4*sqrt(pi)*erf(b*x)^2*e^c/b
```

Sympy [A]
time = 0.16, size = 19, normalized size = 0.90

$$\begin{cases} \frac{\sqrt{\pi}\,e^{c}\operatorname{erf}^{2}(bx)}{4b} & \text{for}\ b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b**2*x**2+c)*erf(b*x),x)
```

```
[Out] Piecewise((sqrt(pi)*exp(c)*erf(b*x)**2/(4*b), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erf(b*x),x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(-b^2*x^2 + c), x)
```

Mupad [B]
time = 0.42, size = 93, normalized size = 4.43

$$\frac{\sqrt{\pi}\,\mathrm{erf}\left(x\sqrt{b^2}\right)^2\mathrm{e}^c}{4\,b}-\frac{\sqrt{\pi}\,\mathrm{e}^c\,\mathrm{erfi}\left(\frac{b^2\,x}{\sqrt{-b^2}}\right)\,\mathrm{erf}(b\,x)}{2\,\sqrt{-b^2}}+\frac{b\,\sqrt{\pi}\,\mathrm{erf}\left(x\,\sqrt{b^2}\right)\,\mathrm{e}^c\,\mathrm{erfi}\left(\frac{b^2\,x}{\sqrt{-b^2}}\right)}{2\,\sqrt{b^2}\,\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c - b^2*x^2)*erf(b*x),x)
```

```
[Out] (pi^(1/2)*erf(x*(b^2)^(1/2))^2*exp(c))/(4*b) - (pi^(1/2)*exp(c)*erfi((b^2*x
)/(-b^2)^(1/2))*erf(b*x))/(2*(-b^2)^(1/2)) + (b*pi^(1/2)*erf(x*(b^2)^(1/2))
*exp(c)*erfi((b^2*x)/(-b^2)^(1/2)))/(2*(b^2)^(1/2)*(-b^2)^(1/2))
```

3.49 $\int \frac{e^{c-b^2x^2}}{\mathbf{Erf}(bx)}\,dx$

Optimal. Leaf size=20

$$\frac{e^c\sqrt{\pi}\,\log(\mathrm{Erf}(bx))}{2b}$$

```
[Out] 1/2*exp(c)*ln(erf(b*x))*Pi^(1/2)/b
```

Rubi [A]
time = 0.02, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {6508, 29}

$$\frac{\sqrt{\pi}\,e^c\log(\mathrm{Erf}(bx))}{2b}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c - b^2*x^2)/Erf[b*x],x]
```

```
[Out] (E^c*Sqrt[Pi]*Log[Erf[b*x]])/(2*b)
```

Rule 29

```
Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c-b^2x^2}}{\mathrm{erf}(bx)}\,dx &= \frac{\left(e^c\sqrt{\pi}\right)\mathrm{Subst}\left(\int \frac{1}{x}\,dx, x, \mathrm{erf}(bx)\right)}{2b}\\ &= \frac{e^c\sqrt{\pi}\,\log(\mathrm{erf}(bx))}{2b}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 20, normalized size = 1.00

$$\frac{e^c\sqrt{\pi}\,\log(\mathrm{Erf}(bx))}{2b}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c - b^2*x^2)/Erf[b*x],x]
```

```
[Out] (E^c*Sqrt[Pi]*Log[Erf[b*x]])/(2*b)
```

Maple [F]
time = 180.00, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{-b^2x^2+c}}{\mathrm{erf}\left(bx\right)}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(-b^2*x^2+c)/erf(b*x),x)
```

```
[Out] int(exp(-b^2*x^2+c)/erf(b*x),x)
```

Maxima [A]
time = 0.26, size = 15, normalized size = 0.75

$$\frac{\sqrt{\pi}\, e^c \log\left(\mathrm{erf}\left(bx\right)\right)}{2\, b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erf(b*x),x, algorithm="maxima")
```

```
[Out] 1/2*sqrt(pi)*e^c*log(erf(b*x))/b
```

Fricas [A]
time = 0.36, size = 15, normalized size = 0.75

$$\frac{\sqrt{\pi}\, e^c \log\left(\mathrm{erf}\left(bx\right)\right)}{2\, b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erf(b*x),x, algorithm="fricas")
```

```
[Out] 1/2*sqrt(pi)*e^c*log(erf(b*x))/b
```

Sympy [A]
time = 0.19, size = 17, normalized size = 0.85

$$\frac{\sqrt{\pi}\, e^c \log\left(\mathrm{erf}\left(bx\right)\right)}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b**2*x**2+c)/erf(b*x),x)
```

```
[Out] sqrt(pi)*exp(c)*log(erf(b*x))/(2*b)
```

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erf(b*x),x, algorithm="giac")
[Out] integrate(e^(-b^2*x^2 + c)/erf(b*x), x)
```

Mupad [**B**]
time = 0.16, size = 15, normalized size = 0.75

$$\frac{\sqrt{\pi}\ \ln\left(\mathrm{erf}(b\,x)\right)\,\mathrm{e}^c}{2\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c - b^2*x^2)/erf(b*x),x)
[Out] (pi^(1/2)*log(erf(b*x))*exp(c))/(2*b)
```

3.50 $\int \frac{e^{c-b^2x^2}}{\mathbf{Erf}(bx)^2}\,dx$

Optimal. Leaf size=21

$$-\frac{e^c\sqrt{\pi}}{2b\text{Erf}(bx)}$$

```
[Out] -1/2*exp(c)*Pi^(1/2)/b/erf(b*x)
```

Rubi [A]
time = 0.02, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = $\{6508, 30\}$

$$-\frac{\sqrt{\pi}\,e^c}{2b\text{Erf}(bx)}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c - b^2*x^2)/Erf[b*x]^2,x]
```

```
[Out] -1/2*(E^c*Sqrt[Pi])/(b*Erf[b*x])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c-b^2x^2}}{\text{erf}(bx)^2}\,dx &= \frac{\left(e^c\sqrt{\pi}\right)\text{Subst}\left(\int \frac{1}{x^2}\,dx, x, \text{erf}(bx)\right)}{2b}\\ &= -\frac{e^c\sqrt{\pi}}{2b\text{erf}(bx)}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 21, normalized size = 1.00

$$-\frac{e^c\sqrt{\pi}}{2b\text{Erf}(bx)}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c - b^2*x^2)/Erf[b*x]^2,x]
```

```
[Out] -1/2*(E^c*Sqrt[Pi])/(b*Erf[b*x])
```

Maple [A]
time = 0.18, size = 17, normalized size = 0.81

method	result	size
default	$-\frac{\mathrm{e}^{c}\sqrt{\pi}}{2b\,\mathrm{erf}(bx)}$	17

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(-b^2*x^2+c)/erf(b*x)^2,x,method=_RETURNVERBOSE)
```

```
[Out] -1/2*exp(c)*Pi^(1/2)/b/erf(b*x)
```

Maxima [A]
time = 0.26, size = 16, normalized size = 0.76

$$-\frac{\sqrt{\pi}\, e^{c}}{2\, b \operatorname{erf}\left(b x\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erf(b*x)^2,x, algorithm="maxima")
```

```
[Out] -1/2*sqrt(pi)*e^c/(b*erf(b*x))
```

Fricas [A]
time = 0.43, size = 16, normalized size = 0.76

$$-\frac{\sqrt{\pi}\, e^{c}}{2\, b \operatorname{erf}\left(b x\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erf(b*x)^2,x, algorithm="fricas")
```

```
[Out] -1/2*sqrt(pi)*e^c/(b*erf(b*x))
```

Sympy [A]
time = 0.31, size = 17, normalized size = 0.81

$$-\frac{\sqrt{\pi}\, e^{c}}{2b \operatorname{erf}\left(b x\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b**2*x**2+c)/erf(b*x)**2,x)
```

```
[Out] -sqrt(pi)*exp(c)/(2*b*erf(b*x))
```

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erf(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(e^(-b^2*x^2 + c)/erf(b*x)^2, x)
```

Mupad [**B**]
time = 0.14, size = 16, normalized size = 0.76

$$-\frac{\sqrt{\pi}\ \mathrm{e}^c}{2\,b\,\mathrm{erf}\left(b\,x\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c - b^2*x^2)/erf(b*x)^2,x)
```

```
[Out] -(pi^(1/2)*exp(c))/(2*b*erf(b*x))
```

3.51 $\int \frac{e^{c-b^2x^2}}{\mathbf{Erf}(bx)^3}\,dx$

Optimal. Leaf size=21

$$-\frac{e^c\sqrt{\pi}}{4b\text{Erf}(bx)^2}$$

```
[Out] -1/4*exp(c)*Pi^(1/2)/b/erf(b*x)^2
```

Rubi [A]
time = 0.02, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {6508, 30}

$$-\frac{\sqrt{\pi}\,e^c}{4b\text{Erf}(bx)^2}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c - b^2*x^2)/Erf[b*x]^3,x]
```

```
[Out] -1/4*(E^c*Sqrt[Pi])/(b*Erf[b*x]^2)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c-b^2x^2}}{\text{erf}(bx)^3}\,dx &= \frac{\left(e^c\sqrt{\pi}\right)\text{Subst}\left(\int \frac{1}{x^3}\,dx, x, \text{erf}(bx)\right)}{2b}\\ &= -\frac{e^c\sqrt{\pi}}{4b\text{erf}(bx)^2}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 21, normalized size = 1.00

$$-\frac{e^c\sqrt{\pi}}{4b\text{Erf}(bx)^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c - b^2*x^2)/Erf[b*x]^3,x]
```

```
[Out] -1/4*(E^c*Sqrt[Pi])/(b*Erf[b*x]^2)
```

Maple [A]
time = 0.19, size = 17, normalized size = 0.81

method	result	size
default	$-\frac{e^{c} \sqrt{\pi}}{4 b \operatorname{erf}\left(b x \right)^{2}}$	17

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(-b^2*x^2+c)/erf(b*x)^3,x,method=_RETURNVERBOSE)
```

```
[Out] -1/4*exp(c)*Pi^(1/2)/b/erf(b*x)^2
```

Maxima [A]
time = 0.26, size = 16, normalized size = 0.76

$$-\frac{\sqrt{\pi}\, e^{c}}{4\, b \operatorname{erf}\left(b x\right)^{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erf(b*x)^3,x, algorithm="maxima")
```

```
[Out] -1/4*sqrt(pi)*e^c/(b*erf(b*x)^2)
```

Fricas [A]
time = 0.36, size = 16, normalized size = 0.76

$$-\frac{\sqrt{\pi}\, e^{c}}{4\, b \operatorname{erf}\left(b x\right)^{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erf(b*x)^3,x, algorithm="fricas")
```

```
[Out] -1/4*sqrt(pi)*e^c/(b*erf(b*x)^2)
```

Sympy [A]
time = 0.52, size = 19, normalized size = 0.90

$$-\frac{\sqrt{\pi}\, e^{c}}{4 b \operatorname{erf}^{2}\left(b x\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b**2*x**2+c)/erf(b*x)**3,x)
[Out] -sqrt(pi)*exp(c)/(4*b*erf(b*x)**2)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erf(b*x)^3,x, algorithm="giac")
[Out] integrate(e^(-b^2*x^2 + c)/erf(b*x)^3, x)
```

Mupad [B]
time = 0.12, size = 16, normalized size = 0.76

$$-\frac{\sqrt{\pi}\ \mathrm{e}^{c}}{4\,b\,\mathrm{erf}\left(b\,x\right)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c - b^2*x^2)/erf(b*x)^3,x)
[Out] -(pi^(1/2)*exp(c))/(4*b*erf(b*x)^2)
```

3.52 $\int e^{c-b^2x^2}\mathbf{Erf}(bx)^n\,dx$

Optimal. Leaf size=28

$$\frac{e^c\sqrt{\pi}\,\mathrm{Erf}(bx)^{1+n}}{2b(1+n)}$$

```
[Out] 1/2*exp(c)*erf(b*x)^(1+n)*Pi^(1/2)/b/(1+n)
```

Rubi [A]

time = 0.02, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {6508, 30}

$$\frac{\sqrt{\pi}\,e^c\mathrm{Erf}(bx)^{n+1}}{2b(n+1)}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c - b^2*x^2)*Erf[b*x]^n,x]
```

```
[Out] (E^c*Sqrt[Pi]*Erf[b*x]^(1 + n))/(2*b*(1 + n))
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rubi steps

$$\begin{aligned}\int e^{c-b^2x^2}\mathrm{erf}(bx)^n\,dx &= \frac{\left(e^c\sqrt{\pi}\right)\mathrm{Subst}\left(\int x^n\,dx,x,\mathrm{erf}(bx)\right)}{2b}\\ &= \frac{e^c\sqrt{\pi}\,\mathrm{erf}(bx)^{1+n}}{2b(1+n)}\end{aligned}$$

Mathematica [A]

time = 0.01, size = 28, normalized size = 1.00

$$\frac{e^c\sqrt{\pi}\,\mathrm{Erf}(bx)^{1+n}}{2b(1+n)}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c - b^2*x^2)*Erf[b*x]^n,x]
```

```
[Out] (E^c*Sqrt[Pi]*Erf[b*x]^(1 + n))/(2*b*(1 + n))
```

Maple [F]
time = 0.04, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{-b^2x^2+c} \operatorname{erf}(bx)^n \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(-b^2*x^2+c)*erf(b*x)^n,x)
```

```
[Out] int(exp(-b^2*x^2+c)*erf(b*x)^n,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erf(b*x)^n,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)^n*e^(-b^2*x^2 + c), x)
```

Fricas [A]
time = 0.42, size = 24, normalized size = 0.86

$$\frac{\sqrt{\pi} \operatorname{erf}(bx)^n \operatorname{erf}(bx) e^c}{2(bn+b)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erf(b*x)^n,x, algorithm="fricas")
```

```
[Out] 1/2*sqrt(pi)*erf(b*x)^n*erf(b*x)*e^c/(b*n + b)
```

Sympy [B] Leaf count of result is larger than twice the leaf count of optimal. 63 vs. $2(22) = 44$.
time = 1.73, size = 63, normalized size = 2.25

$$\begin{cases} \tilde{\infty} x e^c & \text{for } b = 0 \wedge n = -1 \\ 0^n x e^c & \text{for } b = 0 \\ \frac{\sqrt{\pi} e^c \log(\operatorname{erf}(bx))}{2b} & \text{for } n = -1 \\ \frac{\sqrt{\pi} e^c \operatorname{erf}(bx) \operatorname{erf}^n(bx)}{2bn+2b} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b**2*x**2+c)*erf(b*x)**n,x)
```

```
[Out] Piecewise((zoo*x*exp(c), Eq(b, 0) & Eq(n, -1)), (0**n*x*exp(c), Eq(b, 0)),
(sqrt(pi)*exp(c)*log(erf(b*x))/(2*b), Eq(n, -1)), (sqrt(pi)*exp(c)*erf(b*x)
*erf(b*x)**n/(2*b*n + 2*b), True))
```

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erf(b*x)^n,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)^n*e^(-b^2*x^2 + c), x)
```

Mupad [**B**]
time = 0.16, size = 23, normalized size = 0.82

$$\frac{\sqrt{\pi}\,\mathrm{e}^c\,\mathrm{erf}(b\,x)^{n+1}}{2\,b\,(n+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c - b^2*x^2)*erf(b*x)^n,x)
```

```
[Out] (pi^(1/2)*exp(c)*erf(b*x)^(n + 1))/(2*b*(n + 1))
```

3.53 $\int e^{c+dx^2} x^5 \mathbf{Erf}(bx)\, dx$

Optimal. Leaf size=285

$$-\frac{be^{c-(b^2-d)x^2}x}{(b^2-d)\,d^2\sqrt{\pi}}+\frac{3be^{c-(b^2-d)x^2}x}{4\,(b^2-d)^2\,d\sqrt{\pi}}+\frac{be^{c-(b^2-d)x^2}x^3}{2\,(b^2-d)\,d\sqrt{\pi}}+\frac{e^{c+dx^2}\mathrm{Erf}(bx)}{d^3}-\frac{e^{c+dx^2}x^2\mathrm{Erf}(bx)}{d^2}+\frac{e^{c+dx^2}x^4\mathrm{Erf}(bx)}{2d}-\frac{b}{-}$$

```
[Out] exp(d*x^2+c)*erf(b*x)/d^3-exp(d*x^2+c)*x^2*erf(b*x)/d^2+1/2*exp(d*x^2+c)*x^
4*erf(b*x)/d+1/2*b*exp(c)*erf(x*(b^2-d)^(1/2))/(b^2-d)^(3/2)/d^2-3/8*b*exp(
c)*erf(x*(b^2-d)^(1/2))/(b^2-d)^(5/2)/d-b*exp(c)*erf(x*(b^2-d)^(1/2))/d^3/(
b^2-d)^(1/2)-b*exp(c-(b^2-d)*x^2)*x/(b^2-d)/d^2/Pi^(1/2)+3/4*b*exp(c-(b^2-d
)*x^2)*x/(b^2-d)^2/d/Pi^(1/2)+1/2*b*exp(c-(b^2-d)*x^2)*x^3/(b^2-d)/d/Pi^(1/
2)
```

Rubi [A]
time = 0.29, antiderivative size = 285, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {6520, 6517, 2236, 2243}

$$-\frac{be^c\mathrm{Erf}\left(x\sqrt{b^2-d}\right)}{d^3\sqrt{b^2-d}}+\frac{be^c\mathrm{Erf}\left(x\sqrt{b^2-d}\right)}{2d^2\,(b^2-d)^{3/2}}-\frac{bxe^{c-x^2(b^2-d)}}{\sqrt{\pi}\,d^2\,(b^2-d)}-\frac{3be^c\mathrm{Erf}\left(x\sqrt{b^2-d}\right)}{8d\,(b^2-d)^{5/2}}+\frac{3bxe^{c-x^2(b^2-d)}}{4\sqrt{\pi}\,d\,(b^2-d)^2}+\frac{bx^3e^{c-x^2(b^2-d)}}{2\sqrt{\pi}\,d\,(b^2-d)}+\frac{\mathrm{Erf}(bx)e^{c+dx^2}}{d^3}-\frac{x^2\mathrm{Erf}(bx)e^{c+dx^2}}{d^2}+\frac{x^4\mathrm{Erf}(bx)e^{c+dx^2}}{2d}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + d*x^2)*x^5*Erf[b*x],x]
```

```
[Out] -((b*E^(c - (b^2 - d)*x^2)*x)/((b^2 - d)*d^2*Sqrt[Pi])) + (3*b*E^(c - (b^2
- d)*x^2)*x)/(4*(b^2 - d)^2*d*Sqrt[Pi]) + (b*E^(c - (b^2 - d)*x^2)*x^3)/(2*
(b^2 - d)*d*Sqrt[Pi]) + (E^(c + d*x^2)*Erf[b*x])/d^3 - (E^(c + d*x^2)*x^2*E
rf[b*x])/d^2 + (E^(c + d*x^2)*x^4*Erf[b*x])/(2*d) - (b*E^c*Erf[Sqrt[b^2 - d
]*x])/(Sqrt[b^2 - d]*d^3) + (b*E^c*Erf[Sqrt[b^2 - d]*x])/(2*(b^2 - d)^(3/2)
*d^2) - (3*b*E^c*Erf[Sqrt[b^2 - d]*x])/(8*(b^2 - d)^(5/2)*d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int e^{c+dx^2}x^5\operatorname{erf}(bx)\,dx &= \frac{e^{c+dx^2}x^4\operatorname{erf}(bx)}{2d} - \frac{2\int e^{c+dx^2}x^3\operatorname{erf}(bx)\,dx}{d} - \frac{b\int e^{c-(b^2-d)x^2}x^4\,dx}{d\sqrt{\pi}}\\
&= \frac{be^{c-(b^2-d)x^2}x^3}{2(b^2-d)\,d\sqrt{\pi}} - \frac{e^{c+dx^2}x^2\operatorname{erf}(bx)}{d^2} + \frac{e^{c+dx^2}x^4\operatorname{erf}(bx)}{2d} + \frac{2\int e^{c+dx^2}x\operatorname{erf}(bx)\,dx}{d^2} + \frac{(2b}{}\\
&= -\frac{be^{c-(b^2-d)x^2}x}{(b^2-d)\,d^2\sqrt{\pi}} + \frac{3be^{c-(b^2-d)x^2}x}{4(b^2-d)^2\,d\sqrt{\pi}} + \frac{be^{c-(b^2-d)x^2}x^3}{2(b^2-d)\,d\sqrt{\pi}} + \frac{e^{c+dx^2}\operatorname{erf}(bx)}{d^3} - \frac{e^{c+dx^2}x^2}{d}\\
&= -\frac{be^{c-(b^2-d)x^2}x}{(b^2-d)\,d^2\sqrt{\pi}} + \frac{3be^{c-(b^2-d)x^2}x}{4(b^2-d)^2\,d\sqrt{\pi}} + \frac{be^{c-(b^2-d)x^2}x^3}{2(b^2-d)\,d\sqrt{\pi}} + \frac{e^{c+dx^2}\operatorname{erf}(bx)}{d^3} - \frac{e^{c+dx^2}x^2}{d}
\end{aligned}$$

Mathematica [A]
time = 0.32, size = 138, normalized size = 0.48

$$\frac{e^c\left(\frac{2bde^{(-b^2+d)x^2}x(d(7-2dx^2)+2b^2(-2+dx^2))}{(b^2-d)^2\sqrt{\pi}}+4e^{dx^2}(2-2dx^2+d^2x^4)\operatorname{Erf}(bx)+\frac{b(-8b^4+20b^2d-15d^2)\operatorname{Erfi}\left(\sqrt{-b^2+d}\,x\right)}{(-b^2+d)^{5/2}}\right)}{8d^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + d*x^2)*x^5*Erf[b*x],x]
```

```
[Out] (E^c*((2*b*d*E^((-b^2 + d)*x^2)*x*(d*(7 - 2*d*x^2) + 2*b^2*(-2 + d*x^2)))/(
(b^2 - d)^2*Sqrt[Pi]) + 4*E^(d*x^2)*(2 - 2*d*x^2 + d^2*x^4)*Erf[b*x] + (b*(
-8*b^4 + 20*b^2*d - 15*d^2)*Erfi[Sqrt[-b^2 + d]*x])/(-b^2 + d)^(5/2)))/(8*d
^3)
```

Maple [A]
time = 0.43, size = 312, normalized size = 1.09

method	result
default	$\dfrac{\dfrac{\operatorname{erf}(bx)\mathrm{e}^{c}\left(\frac{\mathrm{e}^{d x^2} b^6 x^4}{2d} - \frac{2b^2\left(\frac{b^4x^2\mathrm{e}^{dx^2}}{2d} - \frac{b^4 \mathrm{e}^{dx^2}}{2d^2}\right)}{d}\right)}{b^5} - \dfrac{\mathrm{e}^c\left(\frac{b^2\left(\frac{b^3x^3 \mathrm{e}^{\left(-1+\frac{d}{b^2}\right)b^2x^2}}{-2+\frac{2d}{b^2}} - \frac{3\left(\frac{bx\, \mathrm{e}^{\left(-1+\frac{d}{b^2}\right)b^2x^2}}{-2+\frac{2d}{b^2}} - \frac{\sqrt{\pi}\operatorname{erf}\left(\sqrt{1-\frac{d}{b^2}}\,bx\right)}{4\left(-1+\frac{d}{b^2}\right)\sqrt{1-\frac{d}{b^2}}}\right)}{2\left(-1+\frac{d}{b^2}\right)}\right)}{d}\right)}{}}{b}$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^5*erf(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] (erf(b*x)/b^5*exp(c)*(1/2*exp(d*x^2)*b^6*x^4/d-2/d*b^2*(1/2/d*b^4*x^2*exp(d
*x^2)-1/2/d^2*b^4*exp(d*x^2)))-1/Pi^(1/2)/b^5*exp(c)*(1/d*b^2*(1/2/(-1+d/b^
2)*b^3*x^3*exp((-1+d/b^2)*b^2*x^2)-3/2/(-1+d/b^2)*(1/2/(-1+d/b^2)*b*x*exp((
-1+d/b^2)*b^2*x^2)-1/4/(-1+d/b^2)*Pi^(1/2)/(1-d/b^2)^(1/2)*erf((1-d/b^2)^(1
/2)*b*x)))+1/d^3*b^6*Pi^(1/2)/(1-d/b^2)^(1/2)*erf((1-d/b^2)^(1/2)*b*x)-2/d^
2*b^4*(1/2/(-1+d/b^2)*b*x*exp((-1+d/b^2)*b^2*x^2)-1/4/(-1+d/b^2)*Pi^(1/2)/(
1-d/b^2)^(1/2)*erf((1-d/b^2)^(1/2)*b*x))))/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^5*erf(b*x),x, algorithm="maxima")
```

```
[Out] 1/2*(d^2*x^4*e^c - 2*d*x^2*e^c + 2*e^c)*erf(b*x)*e^(d*x^2)/d^3 - integrate(
(b*d^2*x^4*e^c - 2*b*d*x^2*e^c + 2*b*e^c)*e^(-b^2*x^2 + d*x^2), x)/(sqrt(pi
)*d^3)
```

Fricas [A]
time = 0.36, size = 260, normalized size = 0.91

$$-\frac{\pi(8\,b^5-20\,b^3d+15\,bd^2)\sqrt{b^2-d}\,\operatorname{erf}\left(\sqrt{b^2-d}\,x\right)e^c-4\,(\pi(b^6d^2-3\,b^4d^3+3\,b^2d^4-d^5)x^4-2\,\pi(b^6d-3\,b^4d^2+3\,b^2d^3-d^4)x^2+2\,\pi(b^6-3\,b^4d+3\,b^2d^2-d^3))\operatorname{erf}(bx)\,e^{(dx^2+c)}-2\,\sqrt{\pi}\,(2\,(b^5d^2-2\,b^3d^3+bd^4)x^3-(4\,b^5d-11\,b^3d^2+7\,bd^3)x)e^{(-b^2x^2+dx^2+c)}}{8\,\pi(b^6d^3-3\,b^4d^4+3\,b^2d^5-d^6)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^5*erf(b*x),x, algorithm="fricas")
```

```
[Out] -1/8*(pi*(8*b^5 - 20*b^3*d + 15*b*d^2)*sqrt(b^2 - d)*erf(sqrt(b^2 - d)*x)*e
^c - 4*(pi*(b^6*d^2 - 3*b^4*d^3 + 3*b^2*d^4 - d^5)*x^4 - 2*pi*(b^6*d - 3*b^
4*d^2 + 3*b^2*d^3 - d^4)*x^2 + 2*pi*(b^6 - 3*b^4*d + 3*b^2*d^2 - d^3))*erf(
b*x)*e^(d*x^2 + c) - 2*sqrt(pi)*(2*(b^5*d^2 - 2*b^3*d^3 + b*d^4)*x^3 - (4*b
^5*d - 11*b^3*d^2 + 7*b*d^3)*x)*e^(-b^2*x^2 + d*x^2 + c))/(pi*(b^6*d^3 - 3*
b^4*d^4 + 3*b^2*d^5 - d^6))
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int x^{5}e^{dx^{2}}\operatorname{erf}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**5*erf(b*x),x)
```

```
[Out] exp(c)*Integral(x**5*exp(d*x**2)*erf(b*x), x)
```

Giac [A]
time = 0.43, size = 270, normalized size = 0.95

$$\frac{1}{2}\left(\frac{c^{2}e^{\left(dx^{2}+c\right)}}{d^{3}}-\frac{\left(2\,dx^{2}-\left(dx^{2}+c\right)^{2}+2\,\left(dx^{2}+c\right)c-2\right)e^{\left(dx^{2}+c\right)}}{d^{3}}\right)\operatorname{erf}\left(bx\right)+\frac{\sqrt{\pi}\,bd^{2}\left(\frac{2\,\left(2\,b^{2}x^{3}-2\,dx^{3}+3\,x\right)e^{\left(-b^{2}x^{2}+dx^{2}+c\right)}}{b^{4}-2\,b^{2}d+d^{2}}+\frac{3\,\sqrt{\pi}\operatorname{erf}\left(-\sqrt{b^{2}-d}\,x\right)e^{c}}{\left(b^{4}-2\,b^{2}d+d^{2}\right)\sqrt{b^{2}-d}}\right)-4\,\sqrt{\pi}\,bd\left(\frac{2\,xe^{\left(-b^{2}x^{2}+dx^{2}+c\right)}}{b^{2}-d}+\frac{\sqrt{\pi}\operatorname{erf}\left(-\sqrt{b^{2}-d}\,x\right)e^{c}}{\left(b^{2}-d\right)^{\frac{3}{2}}}\right)+\frac{8\,\pi b\operatorname{erf}\left(-\sqrt{b^{2}-d}\,x\right)e^{c}}{\sqrt{b^{2}-d}}}{8\,\pi d^{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^5*erf(b*x),x, algorithm="giac")
```

```
[Out] 1/2*(c^2*e^(d*x^2 + c)/d^3 - (2*d*x^2 - (d*x^2 + c)^2 + 2*(d*x^2 + c)*c - 2
)*e^(d*x^2 + c)/d^3)*erf(b*x) + 1/8*(sqrt(pi)*b*d^2*(2*(2*b^2*x^3 - 2*d*x^3
 + 3*x)*e^(-b^2*x^2 + d*x^2 + c)/(b^4 - 2*b^2*d + d^2) + 3*sqrt(pi)*erf(-sq
rt(b^2 - d)*x)*e^c/((b^4 - 2*b^2*d + d^2)*sqrt(b^2 - d))) - 4*sqrt(pi)*b*d*
(2*x*e^(-b^2*x^2 + d*x^2 + c)/(b^2 - d) + sqrt(pi)*erf(-sqrt(b^2 - d)*x)*e^
c/(b^2 - d)^(3/2)) + 8*pi*b*erf(-sqrt(b^2 - d)*x)*e^c/sqrt(b^2 - d))/(pi*d^
3)
```

Mupad [B]
time = 0.77, size = 244, normalized size = 0.86

$$\operatorname{erf}(b\,x)\,\left(\frac{\mathrm{e}^{d\,x^2+c}}{d^3}-\frac{x^2\,\mathrm{e}^{d\,x^2+c}}{d^2}+\frac{x^4\,\mathrm{e}^{d\,x^2+c}}{2\,d}\right)-\frac{b\,\mathrm{e}^c\,\mathrm{erf}\left(x\,\sqrt{b^2-d}\right)}{d^3\,\sqrt{b^2-d}}-\frac{b\,\mathrm{e}^c\,\mathrm{erfi}\left(x\,\sqrt{d-b^2}\right)}{2\,d^2\,{\left(d-b^2\right)}^{3/2}}+\frac{b\,x\,\mathrm{e}^{-b^2\,x^2+d\,x^2+c}}{d^2\,\sqrt{\pi}\,\left(d-b^2\right)}+\frac{b\,x^5\,\mathrm{e}^c\,\left(\mathrm{e}^{d\,x^2-b^2\,x^2}\,\left(\frac{3\,\sqrt{-x^2\,\left(d-b^2\right)}}{2}+{\left(-x^2\,\left(d-b^2\right)\right)}^{3/2}\right)-\frac{3\,\sqrt{\pi}}{4}+\frac{3\,\sqrt{\pi}\,\mathrm{erfc}\left(\sqrt{-x^2\,\left(d-b^2\right)}\right)}{4}\right)}{2\,d\,\sqrt{\pi}\,{\left(-x^2\,\left(d-b^2\right)\right)}^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*exp(c + d*x^2)*erf(b*x),x)
```

```
[Out] erf(b*x)*(exp(c + d*x^2)/d^3 - (x^2*exp(c + d*x^2))/d^2 + (x^4*exp(c + d*x^
2))/(2*d)) - (b*exp(c)*erf(x*(b^2 - d)^(1/2)))/(d^3*(b^2 - d)^(1/2)) - (b*e
xp(c)*erfi(x*(d - b^2)^(1/2)))/(2*d^2*(d - b^2)^(3/2)) + (b*x*exp(c + d*x^2
 - b^2*x^2))/(d^2*pi^(1/2)*(d - b^2)) + (b*x^5*exp(c)*(exp(d*x^2 - b^2*x^2)
*((3*(-x^2*(d - b^2))^(1/2))/2 + (-x^2*(d - b^2))^(3/2)) - (3*pi^(1/2))/4 +
 (3*pi^(1/2)*erfc((-x^2*(d - b^2))^(1/2)))/4))/(2*d*pi^(1/2)*(-x^2*(d - b^2
))^(5/2))
```

3.54 $\int e^{c+dx^2}x^3\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=155

$$\frac{be^{c-(b^2-d)x^2}x}{2\,(b^2-d)\,d\sqrt{\pi}}-\frac{e^{c+dx^2}\text{Erf}(bx)}{2d^2}+\frac{e^{c+dx^2}x^2\text{Erf}(bx)}{2d}+\frac{be^c\text{Erf}\left(\sqrt{b^2-d}\,x\right)}{2\sqrt{b^2-d}\,d^2}-\frac{be^c\text{Erf}\left(\sqrt{b^2-d}\,x\right)}{4\,(b^2-d)^{3/2}\,d}$$

```
[Out] -1/2*exp(d*x^2+c)*erf(b*x)/d^2+1/2*exp(d*x^2+c)*x^2*erf(b*x)/d-1/4*b*exp(c)
*erf(x*(b^2-d)^(1/2))/(b^2-d)^(3/2)/d+1/2*b*exp(c)*erf(x*(b^2-d)^(1/2))/d^2
/(b^2-d)^(1/2)+1/2*b*exp(c-(b^2-d)*x^2)*x/(b^2-d)/d/Pi^(1/2)
```

Rubi [A]
time = 0.11, antiderivative size = 155, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.235, Rules used = {6520, 6517, 2236, 2243}

$$\frac{be^c\text{Erf}\left(x\sqrt{b^2-d}\right)}{2d^2\sqrt{b^2-d}}-\frac{be^c\text{Erf}\left(x\sqrt{b^2-d}\right)}{4d\,(b^2-d)^{3/2}}+\frac{bxe^{c-x^2(b^2-d)}}{2\sqrt{\pi}\,d\,(b^2-d)}-\frac{\text{Erf}(bx)e^{c+dx^2}}{2d^2}+\frac{x^2\text{Erf}(bx)e^{c+dx^2}}{2d}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + d*x^2)*x^3*Erf[b*x],x]
```

```
[Out] (b*E^(c - (b^2 - d)*x^2)*x)/(2*(b^2 - d)*d*Sqrt[Pi]) - (E^(c + d*x^2)*Erf[b
*x])/(2*d^2) + (E^(c + d*x^2)*x^2*Erf[b*x])/(2*d) + (b*E^c*Erf[Sqrt[b^2 - d
]*x])/(2*Sqrt[b^2 - d]*d^2) - (b*E^c*Erf[Sqrt[b^2 - d]*x])/(4*(b^2 - d)^(3/
2)*d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
```

```
 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{c+dx^2}x^3\mathrm{erf}(bx)\,dx &= \frac{e^{c+dx^2}x^2\mathrm{erf}(bx)}{2d}-\frac{\int e^{c+dx^2}x\mathrm{erf}(bx)\,dx}{d}-\frac{b\int e^{c-(b^2-d)x^2}x^2\,dx}{d\sqrt{\pi}}\\ &= \frac{be^{c-(b^2-d)x^2}x}{2(b^2-d)d\sqrt{\pi}}-\frac{e^{c+dx^2}\mathrm{erf}(bx)}{2d^2}+\frac{e^{c+dx^2}x^2\mathrm{erf}(bx)}{2d}+\frac{b\int e^{c-(b^2-d)x^2}\,dx}{d^2\sqrt{\pi}}-\frac{b\int e^{c+(-b^2-}}{2(b^2-d)}\\ &= \frac{be^{c-(b^2-d)x^2}x}{2(b^2-d)d\sqrt{\pi}}-\frac{e^{c+dx^2}\mathrm{erf}(bx)}{2d^2}+\frac{e^{c+dx^2}x^2\mathrm{erf}(bx)}{2d}+\frac{be^c\mathrm{erf}\left(\sqrt{b^2-d}\,x\right)}{2\sqrt{b^2-d}\,d^2}-\frac{be^c\mathrm{erf}\left(\sqrt{\right.}}{4(b^2-}\end{aligned}$$

Mathematica [A]
time = 0.21, size = 99, normalized size = 0.64

$$\frac{e^c\left(\frac{2bde^{\left(-b^2+d\right)x^2}x}{(b^2-d)\sqrt{\pi}}+2e^{dx^2}\left(-1+dx^2\right)\mathrm{Erf}(bx)+\frac{b(-2b^2+3d)\mathrm{Erfi}\left(\sqrt{-b^2+d}\,x\right)}{(-b^2+d)^{3/2}}\right)}{4d^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + d*x^2)*x^3*Erf[b*x],x]
```

```
[Out] (E^c*((2*b*d*E^((-b^2 + d)*x^2)*x)/((b^2 - d)*Sqrt[Pi]) + 2*E^(d*x^2)*(-1 +
 d*x^2)*Erf[b*x] + (b*(-2*b^2 + 3*d)*Erfi[Sqrt[-b^2 + d]*x])/(-b^2 + d)^(3/
2)))/(4*d^2)
```

Maple [A]
time = 0.50, size = 168, normalized size = 1.08

method	result	size

default	$$\frac{\frac{\operatorname{erf}(bx)\,\mathrm{e}^{c}\left(\frac{b^4 x^2 \mathrm{e}^{d\,x^2}}{2d}-\frac{b^4 \mathrm{e}^{d\,x^2}}{2d^2}\right)}{b^3}-\frac{\mathrm{e}^{c}\left(\frac{b^2\left(\frac{bx\,\mathrm{e}^{\left(-1+\frac{d}{b^2}\right)b^2x^2}}{-2+\frac{2d}{b^2}}-\frac{\sqrt{\pi}\,\operatorname{erf}\left(\sqrt{1-\frac{d}{b^2}}\,bx\right)}{4\left(-1+\frac{d}{b^2}\right)\sqrt{1-\frac{d}{b^2}}}\right)}{d}-\frac{b^4\sqrt{\pi}\,\operatorname{erf}\left(\sqrt{1-\frac{d}{b^2}}\,bx\right)}{2d^2\sqrt{1-\frac{d}{b^2}}}\right)}{\sqrt{\pi}\,b^3}}{b}$$	16

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^3*erf(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] (erf(b*x)/b^3*exp(c)*(1/2/d*b^4*x^2*exp(d*x^2)-1/2/d^2*b^4*exp(d*x^2))-1/Pi
^(1/2)/b^3*exp(c)*(1/d*b^2*(1/2/(-1+d/b^2)*b*x*exp((-1+d/b^2)*b^2*x^2)-1/4/
(-1+d/b^2)*Pi^(1/2)/(1-d/b^2)^(1/2)*erf((1-d/b^2)^(1/2)*b*x))-1/2/d^2*b^4*P
i^(1/2)/(1-d/b^2)^(1/2)*erf((1-d/b^2)^(1/2)*b*x)))/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erf(b*x),x, algorithm="maxima")
```

```
[Out] 1/2*(d*x^2*e^c - e^c)*erf(b*x)*e^(d*x^2)/d^2 - integrate((b*d*x^2*e^c - b*e
^c)*e^(-b^2*x^2 + d*x^2), x)/(sqrt(pi)*d^2)
```

Fricas [A]
time = 0.37, size = 149, normalized size = 0.96

$$\frac{\pi(2\,b^3-3\,bd)\sqrt{b^2-d}\,\operatorname{erf}\left(\sqrt{b^2-d}\,x\right)e^c+2\,\sqrt{\pi}\,(b^3d-bd^2)xe^{(-b^2x^2+dx^2+c)}+2\,(\pi(b^4d-2\,b^2d^2+d^3)x^2-\pi(b^4-2\,b^2d+d^2))\operatorname{erf}(bx)\,e^{(dx^2+c)}}{4\,\pi(b^4d^2-2\,b^2d^3+d^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erf(b*x),x, algorithm="fricas")
```

```
[Out] 1/4*(pi*(2*b^3 - 3*b*d)*sqrt(b^2 - d)*erf(sqrt(b^2 - d)*x)*e^c + 2*sqrt(pi)
*(b^3*d - b*d^2)*x*e^(-b^2*x^2 + d*x^2 + c) + 2*(pi*(b^4*d - 2*b^2*d^2 + d^
3)*x^2 - pi*(b^4 - 2*b^2*d + d^2))*erf(b*x)*e^(d*x^2 + c))/(pi*(b^4*d^2 - 2
*b^2*d^3 + d^4))
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int x^{3}e^{dx^{2}}\operatorname{erf}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**3*erf(b*x),x)
```

```
[Out] exp(c)*Integral(x**3*exp(d*x**2)*erf(b*x), x)
```

Giac [A]
time = 0.42, size = 141, normalized size = 0.91

$$\frac{1}{2}\left(\frac{(dx^2+c-1)e^{(dx^2+c)}}{d^2}-\frac{ce^{(dx^2+c)}}{d^2}\right)\operatorname{erf}(bx)+\frac{bd\left(\frac{2xe^{(-b^2x^2+dx^2+c)}}{b^2-d}+\frac{\sqrt{\pi}\operatorname{erf}\left(-\sqrt{b^2-d}\,x\right)e^c}{(b^2-d)^{\frac{3}{2}}}\right)-\frac{2\sqrt{\pi}\,b\operatorname{erf}\left(-\sqrt{b^2-d}\,x\right)e^c}{\sqrt{b^2-d}}}{4\sqrt{\pi}\,d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erf(b*x),x, algorithm="giac")
```

```
[Out] 1/2*((d*x^2 + c - 1)*e^(d*x^2 + c)/d^2 - c*e^(d*x^2 + c)/d^2)*erf(b*x) + 1/
4*(b*d*(2*x*e^(-b^2*x^2 + d*x^2 + c)/(b^2 - d) + sqrt(pi)*erf(-sqrt(b^2 - d
)*x)*e^c/(b^2 - d)^(3/2)) - 2*sqrt(pi)*b*erf(-sqrt(b^2 - d)*x)*e^c/sqrt(b^2
 - d))/(sqrt(pi)*d^2)
```

Mupad [B]
time = 0.53, size = 131, normalized size = 0.85

$$\frac{b\,x\,\mathrm{e}^{-b^2\,x^2+d\,x^2+c}}{2\,\sqrt{\pi}\,\left(b^2\,d-d^2\right)}-\operatorname{erf}(b\,x)\,\left(\frac{\mathrm{e}^{d\,x^2+c}}{2\,d^2}-\frac{x^2\,\mathrm{e}^{d\,x^2+c}}{2\,d}\right)+\frac{b\,\mathrm{e}^c\,\operatorname{erf}\left(x\,\sqrt{b^2-d}\right)}{2\,d^2\,\sqrt{b^2-d}}+\frac{b\,\mathrm{e}^c\,\operatorname{erfi}\left(x\,\sqrt{d-b^2}\right)}{4\,d\,{\left(d-b^2\right)}^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*exp(c + d*x^2)*erf(b*x),x)
```

```
[Out] (b*x*exp(c + d*x^2 - b^2*x^2))/(2*pi^(1/2)*(b^2*d - d^2)) - erf(b*x)*(exp(c
 + d*x^2)/(2*d^2) - (x^2*exp(c + d*x^2))/(2*d)) + (b*exp(c)*erf(x*(b^2 - d)
^(1/2)))/(2*d^2*(b^2 - d)^(1/2)) + (b*exp(c)*erfi(x*(d - b^2)^(1/2)))/(4*d*
(d - b^2)^(3/2))
```

3.55 $\int e^{c+dx^2} x \mathbf{Erf}(bx)\, dx$

Optimal. Leaf size=57

$$\frac{e^{c+dx^2}\text{Erf}(bx)}{2d}-\frac{be^c\text{Erf}\left(\sqrt{b^2-d}\,x\right)}{2\sqrt{b^2-d}\,d}$$

```
[Out] 1/2*exp(d*x^2+c)*erf(b*x)/d-1/2*b*exp(c)*erf(x*(b^2-d)^(1/2))/d/(b^2-d)^(1/
2)
```

Rubi [A]
time = 0.03, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {6517, 2236}

$$\frac{\text{Erf}(bx)e^{c+dx^2}}{2d}-\frac{be^c\text{Erf}\left(x\sqrt{b^2-d}\right)}{2d\sqrt{b^2-d}}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + d*x^2)*x*Erf[b*x],x]
```

```
[Out] (E^(c + d*x^2)*Erf[b*x])/(2*d) - (b*E^c*Erf[Sqrt[b^2 - d]*x])/(2*Sqrt[b^2 -
 d]*d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\begin{aligned}\int e^{c+dx^2}x\text{erf}(bx)\,dx&=\frac{e^{c+dx^2}\text{erf}(bx)}{2d}-\frac{b\int e^{c-(b^2-d)x^2}\,dx}{d\sqrt{\pi}}\\&=\frac{e^{c+dx^2}\text{erf}(bx)}{2d}-\frac{be^c\text{erf}\left(\sqrt{b^2-d}\,x\right)}{2\sqrt{b^2-d}\,d}\end{aligned}$$

Mathematica [A]
time = 0.03, size = 51, normalized size = 0.89

$$\frac{e^c\left(e^{dx^2}\operatorname{Erf}(bx)-\frac{b\operatorname{Erfi}\left(\sqrt{-b^2+d}\,x\right)}{\sqrt{-b^2+d}}\right)}{2d}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + d*x^2)*x*Erf[b*x],x]
```

```
[Out] (E^c*(E^(d*x^2)*Erf[b*x] - (b*Erfi[Sqrt[-b^2 + d]*x])/Sqrt[-b^2 + d]))/(2*d
)
```

Maple [A]
time = 0.44, size = 67, normalized size = 1.18

method	result	size
default	$\frac{\frac{\operatorname{erf}(bx)b\,e^{\frac{b^2dx^2+b^2c}{b^2}}}{2d}-\frac{b\,e^c\operatorname{erf}\left(\sqrt{1-\frac{d}{b^2}}\,bx\right)}{2d\sqrt{1-\frac{d}{b^2}}}}{b}$	67

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x*erf(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] (1/2*erf(b*x)*b*exp((b^2*d*x^2+b^2*c)/b^2)/d-1/2*b/d*exp(c)/(1-d/b^2)^(1/2)
*erf((1-d/b^2)^(1/2)*b*x))/b
```

Maxima [A]
time = 0.26, size = 47, normalized size = 0.82

$$-\frac{b\operatorname{erf}\left(\sqrt{b^2-d}\,x\right)e^c}{2\sqrt{b^2-d}\,d}+\frac{\operatorname{erf}(bx)\,e^{\left(dx^2+c\right)}}{2\,d}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erf(b*x),x, algorithm="maxima")
```

```
[Out] -1/2*b*erf(sqrt(b^2 - d)*x)*e^c/(sqrt(b^2 - d)*d) + 1/2*erf(b*x)*e^(d*x^2 +
 c)/d
```

Fricas [A]
time = 0.38, size = 62, normalized size = 1.09

$$-\frac{\sqrt{b^2-d}\,b\operatorname{erf}\left(\sqrt{b^2-d}\,x\right)e^c-\left(b^2-d\right)\operatorname{erf}(bx)\,e^{\left(dx^2+c\right)}}{2\left(b^2d-d^2\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erf(b*x),x, algorithm="fricas")
```

```
[Out] -1/2*(sqrt(b^2 - d)*b*erf(sqrt(b^2 - d)*x)*e^c - (b^2 - d)*erf(b*x)*e^(d*x^
2 + c))/(b^2*d - d^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int xe^{dx^{2}}\operatorname{erf}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x*erf(b*x),x)
```

```
[Out] exp(c)*Integral(x*exp(d*x**2)*erf(b*x), x)
```

Giac [A]
time = 0.40, size = 48, normalized size = 0.84

$$\frac{b\operatorname{erf}\left(-\sqrt{b^{2}-d}\,x\right)e^{c}}{2\sqrt{b^{2}-d}\,d}+\frac{\operatorname{erf}\left(bx\right)e^{\left(dx^{2}+c\right)}}{2\,d}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erf(b*x),x, algorithm="giac")
```

```
[Out] 1/2*b*erf(-sqrt(b^2 - d)*x)*e^c/(sqrt(b^2 - d)*d) + 1/2*erf(b*x)*e^(d*x^2 +
 c)/d
```

Mupad [B]
time = 0.20, size = 47, normalized size = 0.82

$$\frac{\mathrm{e}^{d\,x^{2}}\,\mathrm{e}^{c}\,\mathrm{erf}(b\,x)}{2\,d}-\frac{b\,\mathrm{e}^{c}\,\mathrm{erf}\left(x\,\sqrt{b^{2}-d}\right)}{2\,d\,\sqrt{b^{2}-d}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*exp(c + d*x^2)*erf(b*x),x)
```

```
[Out] (exp(d*x^2)*exp(c)*erf(b*x))/(2*d) - (b*exp(c)*erf(x*(b^2 - d)^(1/2)))/(2*d
*(b^2 - d)^(1/2))
```

3.56 $\int \frac{e^{c+dx^2}\mathbf{Erf}(bx)}{x}\,dx$

Optimal. Leaf size=20

$$\mathrm{Int}\left(\frac{e^{c+dx^2}\mathrm{Erf}(bx)}{x},x\right)$$

```
[Out] Unintegrable(exp(d*x^2+c)*erf(b*x)/x,x)
```

Rubi [A]
time = 0.02, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\mathrm{Erf}(bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erf[b*x])/x,x]
[Out] Defer[Int][(E^(c + d*x^2)*Erf[b*x])/x, x]
```

Rubi steps

$$\int \frac{e^{c+dx^2}\mathrm{erf}(bx)}{x}\,dx = \int \frac{e^{c+dx^2}\mathrm{erf}(bx)}{x}\,dx$$

Mathematica [A]
time = 0.11, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\mathrm{Erf}(bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erf[b*x])/x,x]
[Out] Integrate[(E^(c + d*x^2)*Erf[b*x])/x, x]
```

Maple [A]
time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\,\mathrm{erf}\,(bx)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erf(b*x)/x,x)
```

```
[Out] int(exp(d*x^2+c)*erf(b*x)/x,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x)/x,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)*e^(d*x^2 + c)/x, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x)/x,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x)*e^(d*x^2 + c)/x, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int\frac{e^{dx^{2}}\operatorname{erf}{\left(bx\right)}}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erf(b*x)/x,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erf(b*x)/x, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x)/x,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(d*x^2 + c)/x, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{e^{d\,x^2+c}\,\mathrm{erf}\left(b\,x\right)}{x} \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + d*x^2)*erf(b*x))/x,x)
```

```
[Out] int((exp(c + d*x^2)*erf(b*x))/x, x)
```

3.57 $\int \frac{e^{c+dx^2}\textbf{Erf}(bx)}{x^3}\,dx$

Optimal. Leaf size=101

$$-\frac{be^{c-(b^2-d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\mathrm{Erf}(bx)}{2x^2}-b\sqrt{b^2-d}\,e^c\mathrm{Erf}\left(\sqrt{b^2-d}\,x\right)+d\mathrm{Int}\left(\frac{e^{c+dx^2}\mathrm{Erf}(bx)}{x},x\right)$$

```
[Out] -1/2*exp(d*x^2+c)*erf(b*x)/x^2-b*exp(c)*erf(x*(b^2-d)^(1/2))*(b^2-d)^(1/2)-
b*exp(c-(b^2-d)*x^2)/x/Pi^(1/2)+d*Unintegrable(exp(d*x^2+c)*erf(b*x)/x,x)
```

Rubi [A]
time = 0.10, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}}=0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\mathrm{Erf}(bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erf[b*x])/x^3,x]
```

```
[Out] -((b*E^(c - (b^2 - d)*x^2))/(Sqrt[Pi]*x)) - (E^(c + d*x^2)*Erf[b*x])/(2*x^2
) - b*Sqrt[b^2 - d]*E^c*Erf[Sqrt[b^2 - d]*x] + d*Defer[Int][(E^(c + d*x^2)*
Erf[b*x])/x, x]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+dx^2}\mathrm{erf}(bx)}{x^3}\,dx &= -\frac{e^{c+dx^2}\mathrm{erf}(bx)}{2x^2}+d\int \frac{e^{c+dx^2}\mathrm{erf}(bx)}{x}\,dx+\frac{b\int \frac{e^{c-\left(b^2-d\right)x^2}}{x^2}\,dx}{\sqrt{\pi}}\\ &= -\frac{be^{c-(b^2-d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\mathrm{erf}(bx)}{2x^2}+d\int \frac{e^{c+dx^2}\mathrm{erf}(bx)}{x}\,dx-\frac{\left(2b(b^2-d)\right)\int e^{c+(-b^2+d)x^2}\,dx}{\sqrt{\pi}}\\ &= -\frac{be^{c-(b^2-d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\mathrm{erf}(bx)}{2x^2}-b\sqrt{b^2-d}\,e^c\mathrm{erf}\left(\sqrt{b^2-d}\,x\right)+d\int \frac{e^{c+dx^2}\mathrm{erf}(bx)}{x}\,dx\end{aligned}$$

Mathematica [A]
time = 0.14, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\mathrm{Erf}(bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erf[b*x])/x^3,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erf[b*x])/x^3, x]
```

Maple [A]
time = 0.23, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\operatorname{erf}(bx)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erf(b*x)/x^3,x)
```

```
[Out] int(exp(d*x^2+c)*erf(b*x)/x^3,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x)/x^3,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)*e^(d*x^2 + c)/x^3, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x)/x^3,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x)*e^(d*x^2 + c)/x^3, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^2}\operatorname{erf}(bx)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erf(b*x)/x**3,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erf(b*x)/x**3, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x)/x^3,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(d*x^2 + c)/x^3, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{e^{d\,x^2+c}\,\mathrm{erf}(b\,x)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + d*x^2)*erf(b*x))/x^3,x)
```

```
[Out] int((exp(c + d*x^2)*erf(b*x))/x^3, x)
```

3.58 $\int \frac{e^{c+dx^2}\mathbf{Erf}(bx)}{x^5}\,dx$

Optimal. Leaf size=231

$$-\frac{be^{c-(b^2-d)x^2}}{6\sqrt{\pi}\,x^3}+\frac{b(b^2-d)\,e^{c-(b^2-d)x^2}}{3\sqrt{\pi}\,x}-\frac{bde^{c-(b^2-d)x^2}}{2\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\mathrm{Erf}(bx)}{4x^4}-\frac{de^{c+dx^2}\mathrm{Erf}(bx)}{4x^2}+\frac{1}{3}b\left(b^2-d\right)^{3/2}e^c\mathrm{Erf}\left(\sqrt{b\right.$$

```
[Out] -1/4*exp(d*x^2+c)*erf(b*x)/x^4-1/4*d*exp(d*x^2+c)*erf(b*x)/x^2+1/3*b*(b^2-d
)^(3/2)*exp(c)*erf(x*(b^2-d)^(1/2))-1/2*b*d*exp(c)*erf(x*(b^2-d)^(1/2))*(b^
2-d)^(1/2)-1/6*b*exp(c-(b^2-d)*x^2)/x^3/Pi^(1/2)+1/3*b*(b^2-d)*exp(c-(b^2-d
)*x^2)/x/Pi^(1/2)-1/2*b*d*exp(c-(b^2-d)*x^2)/x/Pi^(1/2)+1/2*d^2*Unintegrabl
e(exp(d*x^2+c)*erf(b*x)/x,x)
```

Rubi [A]
time = 0.22, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\mathrm{Erf}(bx)}{x^5}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erf[b*x])/x^5,x]
```

```
[Out] -1/6*(b*E^(c - (b^2 - d)*x^2))/(Sqrt[Pi]*x^3) + (b*(b^2 - d)*E^(c - (b^2 -
d)*x^2))/(3*Sqrt[Pi]*x) - (b*d*E^(c - (b^2 - d)*x^2))/(2*Sqrt[Pi]*x) - (E^(
c + d*x^2)*Erf[b*x])/(4*x^4) - (d*E^(c + d*x^2)*Erf[b*x])/(4*x^2) + (b*(b^2
 - d)^(3/2)*E^c*Erf[Sqrt[b^2 - d]*x])/3 - (b*Sqrt[b^2 - d]*d*E^c*Erf[Sqrt[b
^2 - d]*x])/2 + (d^2*Defer[Int][(E^(c + d*x^2)*Erf[b*x])/x, x])/2
```

Rubi steps

$$\begin{aligned}
\int \frac{e^{c+dx^2}\mathrm{erf}(bx)}{x^5}\,dx &= -\frac{e^{c+dx^2}\mathrm{erf}(bx)}{4x^4}+\frac{1}{2}d\int \frac{e^{c+dx^2}\mathrm{erf}(bx)}{x^3}\,dx+\frac{b\int \frac{e^{c-\left(b^2-d\right)x^2}}{x^4}\,dx}{2\sqrt{\pi}}\\
&= -\frac{be^{c-(b^2-d)x^2}}{6\sqrt{\pi}\,x^3}-\frac{e^{c+dx^2}\mathrm{erf}(bx)}{4x^4}-\frac{de^{c+dx^2}\mathrm{erf}(bx)}{4x^2}+\frac{1}{2}d^2\int \frac{e^{c+dx^2}\mathrm{erf}(bx)}{x}\,dx-\frac{(b(b^2-d)}{}\\
&= -\frac{be^{c-(b^2-d)x^2}}{6\sqrt{\pi}\,x^3}+\frac{b(b^2-d)\,e^{c-(b^2-d)x^2}}{3\sqrt{\pi}\,x}-\frac{bde^{c-(b^2-d)x^2}}{2\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\mathrm{erf}(bx)}{4x^4}-\frac{de^{c+dx^2}\mathrm{erf}(bx)}{4x^2}\\
&= -\frac{be^{c-(b^2-d)x^2}}{6\sqrt{\pi}\,x^3}+\frac{b(b^2-d)\,e^{c-(b^2-d)x^2}}{3\sqrt{\pi}\,x}-\frac{bde^{c-(b^2-d)x^2}}{2\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\mathrm{erf}(bx)}{4x^4}-\frac{de^{c+dx^2}\mathrm{erf}(bx)}{4x^2}
\end{aligned}$$

Mathematica [A]
time = 0.18, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\operatorname{Erf}(bx)}{x^5}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erf[b*x])/x^5,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erf[b*x])/x^5, x]
```

Maple [A]
time = 0.18, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\operatorname{erf}\left(bx\right)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erf(b*x)/x^5,x)
```

```
[Out] int(exp(d*x^2+c)*erf(b*x)/x^5,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x)/x^5,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)*e^(d*x^2 + c)/x^5, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x)/x^5,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x)*e^(d*x^2 + c)/x^5, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^2}\operatorname{erf}\left(bx\right)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erf(b*x)/x**5,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erf(b*x)/x**5, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x)/x^5,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(d*x^2 + c)/x^5, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\,\mathrm{erf}(b\,x)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + d*x^2)*erf(b*x))/x^5,x)
```

```
[Out] int((exp(c + d*x^2)*erf(b*x))/x^5, x)
```

3.59 $\int e^{c+dx^2} x^4 \mathbf{Erf}(bx)\, dx$

Optimal. Leaf size=186

$$-\frac{3be^{c-(b^2-d)x^2}}{4(b^2-d)\,d^2\sqrt{\pi}}+\frac{be^{c-(b^2-d)x^2}}{2(b^2-d)^2\,d\sqrt{\pi}}+\frac{be^{c-(b^2-d)x^2}x^2}{2(b^2-d)\,d\sqrt{\pi}}-\frac{3e^{c+dx^2}x\mathrm{Erf}(bx)}{4d^2}+\frac{e^{c+dx^2}x^3\mathrm{Erf}(bx)}{2d}+\frac{3\mathrm{Int}\left(e^{c+dx^2}\mathrm{E}\right.}{4d^2}$$

```
[Out] -3/4*exp(d*x^2+c)*x*erf(b*x)/d^2+1/2*exp(d*x^2+c)*x^3*erf(b*x)/d-3/4*b*exp(
c-(b^2-d)*x^2)/(b^2-d)/d^2/Pi^(1/2)+1/2*b*exp(c-(b^2-d)*x^2)/(b^2-d)^2/d/Pi
^(1/2)+1/2*b*exp(c-(b^2-d)*x^2)*x^2/(b^2-d)/d/Pi^(1/2)+3/4*Unintegrable(exp
(d*x^2+c)*erf(b*x),x)/d^2
```

Rubi [A]
time = 0.16, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int e^{c+dx^2} x^4 \mathrm{Erf}(bx)\, dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*x^4*Erf[b*x],x]
```

```
[Out] (-3*b*E^(c - (b^2 - d)*x^2))/(4*(b^2 - d)*d^2*Sqrt[Pi]) + (b*E^(c - (b^2 -
d)*x^2))/(2*(b^2 - d)^2*d*Sqrt[Pi]) + (b*E^(c - (b^2 - d)*x^2)*x^2)/(2*(b^2
 - d)*d*Sqrt[Pi]) - (3*E^(c + d*x^2)*x*Erf[b*x])/(4*d^2) + (E^(c + d*x^2)*x
^3*Erf[b*x])/(2*d) + (3*Defer[Int][E^(c + d*x^2)*Erf[b*x], x])/(4*d^2)
```

Rubi steps

$$\begin{aligned}\int e^{c+dx^2} x^4 \mathrm{erf}(bx)\, dx &= \frac{e^{c+dx^2}x^3\mathrm{erf}(bx)}{2d}-\frac{3\int e^{c+dx^2}x^2\mathrm{erf}(bx)\,dx}{2d}-\frac{b\int e^{c-(b^2-d)x^2}x^3\,dx}{d\sqrt{\pi}}\\ &= \frac{be^{c-(b^2-d)x^2}x^2}{2(b^2-d)\,d\sqrt{\pi}}-\frac{3e^{c+dx^2}x\mathrm{erf}(bx)}{4d^2}+\frac{e^{c+dx^2}x^3\mathrm{erf}(bx)}{2d}+\frac{3\int e^{c+dx^2}\mathrm{erf}(bx)\,dx}{4d^2}+\frac{(3b)}{}\\ &= -\frac{3be^{c-(b^2-d)x^2}}{4(b^2-d)\,d^2\sqrt{\pi}}+\frac{be^{c-(b^2-d)x^2}}{2(b^2-d)^2\,d\sqrt{\pi}}+\frac{be^{c-(b^2-d)x^2}x^2}{2(b^2-d)\,d\sqrt{\pi}}-\frac{3e^{c+dx^2}x\mathrm{erf}(bx)}{4d^2}+\frac{e^{c+}}{}\end{aligned}$$

Mathematica [A]
time = 0.21, size = 0, normalized size = 0.00

$$\int e^{c+dx^2} x^4 \mathrm{Erf}(bx)\, dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*x^4*Erf[b*x],x]
```

```
[Out] Integrate[E^(c + d*x^2)*x^4*Erf[b*x], x]
```

Maple [A]
time = 0.07, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^2+c} x^4 \,\mathrm{erf}\left(b x\right)\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^4*erf(b*x),x)
```

```
[Out] int(exp(d*x^2+c)*x^4*erf(b*x),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erf(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x^4*erf(b*x)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erf(b*x),x, algorithm="fricas")
```

```
[Out] integral(x^4*erf(b*x)*e^(d*x^2 + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c} \int x^{4} e^{d x^{2}} \operatorname{erf}{\left(b x \right)}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**4*erf(b*x),x)
```

```
[Out] exp(c)*Integral(x**4*exp(d*x**2)*erf(b*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erf(b*x),x, algorithm="giac")
[Out] integrate(x^4*erf(b*x)*e^(d*x^2 + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^4\,\mathrm{e}^{d\,x^2+c}\,\mathrm{erf}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*exp(c + d*x^2)*erf(b*x),x)
[Out] int(x^4*exp(c + d*x^2)*erf(b*x), x)
```

3.60 $\int e^{c+dx^2}x^2\textbf{Erf}(bx)\,dx$

Optimal. Leaf size=84

$$\frac{be^{c-(b^2-d)x^2}}{2(b^2-d)\,d\sqrt{\pi}}+\frac{e^{c+dx^2}x\text{Erf}(bx)}{2d}-\frac{\text{Int}\left(e^{c+dx^2}\text{Erf}(bx),x\right)}{2d}$$

```
[Out] 1/2*exp(d*x^2+c)*x*erf(b*x)/d+1/2*b*exp(c-(b^2-d)*x^2)/(b^2-d)/d/Pi^(1/2)-1
/2*Unintegrable(exp(d*x^2+c)*erf(b*x),x)/d
```

Rubi [A]
time = 0.06, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.000, Rules used = {}

$$\int e^{c+dx^2}x^2\text{Erf}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*x^2*Erf[b*x],x]
[Out] (b*E^(c - (b^2 - d)*x^2))/(2*(b^2 - d)*d*Sqrt[Pi]) + (E^(c + d*x^2)*x*Erf[b
*x])/(2*d) - Defer[Int][E^(c + d*x^2)*Erf[b*x], x]/(2*d)
```

Rubi steps

$$\begin{aligned}\int e^{c+dx^2}x^2\text{erf}(bx)\,dx&=\frac{e^{c+dx^2}x\text{erf}(bx)}{2d}-\frac{\int e^{c+dx^2}\text{erf}(bx)\,dx}{2d}-\frac{b\int e^{c-(b^2-d)x^2}x\,dx}{d\sqrt{\pi}}\\&=\frac{be^{c-(b^2-d)x^2}}{2(b^2-d)\,d\sqrt{\pi}}+\frac{e^{c+dx^2}x\text{erf}(bx)}{2d}-\frac{\int e^{c+dx^2}\text{erf}(bx)\,dx}{2d}\end{aligned}$$

Mathematica [A]
time = 0.16, size = 0, normalized size = 0.00

$$\int e^{c+dx^2}x^2\text{Erf}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*x^2*Erf[b*x],x]
[Out] Integrate[E^(c + d*x^2)*x^2*Erf[b*x], x]
```

Maple [A]
time = 0.13, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^2+c} x^2 \,\mathrm{erf}\left(b x\right)\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^2*erf(b*x),x)
[Out] int(exp(d*x^2+c)*x^2*erf(b*x),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erf(b*x),x, algorithm="maxima")
[Out] integrate(x^2*erf(b*x)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erf(b*x),x, algorithm="fricas")
[Out] integral(x^2*erf(b*x)*e^(d*x^2 + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c} \int x^{2} e^{d x^{2}} \operatorname{erf}{\left(b x \right)}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**2*erf(b*x),x)
[Out] exp(c)*Integral(x**2*exp(d*x**2)*erf(b*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erf(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^2*erf(b*x)*e^(d*x^2 + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^2\,e^{d\,x^2+c}\,\mathrm{erf}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*exp(c + d*x^2)*erf(b*x),x)
```

```
[Out] int(x^2*exp(c + d*x^2)*erf(b*x), x)
```

3.61 $\int e^{c+dx^2}\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=17

$$\mathrm{Int}\left(e^{c+dx^2}\mathrm{Erf}(bx),x\right)$$

```
[Out] Unintegrable(exp(d*x^2+c)*erf(b*x),x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int e^{c+dx^2}\mathrm{Erf}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*Erf[b*x],x]
[Out] Defer[Int][E^(c + d*x^2)*Erf[b*x], x]
```

Rubi steps

$$\int e^{c+dx^2}\mathrm{erf}(bx)\,dx=\int e^{c+dx^2}\mathrm{erf}(bx)\,dx$$

Mathematica [A]
time = 0.02, size = 0, normalized size = 0.00

$$\int e^{c+dx^2}\mathrm{Erf}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*Erf[b*x],x]
[Out] Integrate[E^(c + d*x^2)*Erf[b*x], x]
```

Maple [A]
time = 0.06, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^2+c}\,\mathrm{erf}\left(bx\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erf(b*x),x)
[Out] int(exp(d*x^2+c)*erf(b*x),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x),x, algorithm="maxima")
[Out] integrate(erf(b*x)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x),x, algorithm="fricas")
[Out] integral(erf(b*x)*e^(d*x^2 + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int e^{dx^{2}}\operatorname{erf}{\left(bx\right)}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erf(b*x),x)
[Out] exp(c)*Integral(exp(d*x**2)*erf(b*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x),x, algorithm="giac")
[Out] integrate(erf(b*x)*e^(d*x^2 + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.06

$$\int \mathrm{e}^{d\,x^2+c}\,\mathrm{erf}\left(b\,x\right) \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c + d*x^2)*erf(b*x),x)
```

```
[Out] int(exp(c + d*x^2)*erf(b*x), x)
```

3.62 $\int \frac{e^{c+dx^2}\mathbf{Erf}(bx)}{x^2}\,dx$

Optimal. Leaf size=62

$$-\frac{e^{c+dx^2}\mathrm{Erf}(bx)}{x}+\frac{be^c\mathrm{Ei}(-((b^2-d)\,x^2))}{\sqrt{\pi}}+2d\mathrm{Int}\left(e^{c+dx^2}\mathrm{Erf}(bx),x\right)$$

```
[Out] -exp(d*x^2+c)*erf(b*x)/x+b*exp(c)*Ei(-(b^2-d)*x^2)/Pi^(1/2)+2*d*Unintegrabl
e(exp(d*x^2+c)*erf(b*x),x)
```

Rubi [A]
time = 0.08, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\mathrm{Erf}(bx)}{x^2}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erf[b*x])/x^2,x]
```

```
[Out] -((E^(c + d*x^2)*Erf[b*x])/x) + (b*E^c*ExpIntegralEi[-((b^2 - d)*x^2)])/Sqr
t[Pi] + 2*d*Defer[Int][E^(c + d*x^2)*Erf[b*x], x]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+dx^2}\mathrm{erf}(bx)}{x^2}\,dx &= -\frac{e^{c+dx^2}\mathrm{erf}(bx)}{x}+(2d)\int e^{c+dx^2}\mathrm{erf}(bx)\,dx+\frac{(2b)\int \frac{e^{c-\left(b^2-d\right)x^2}}{x}\,dx}{\sqrt{\pi}}\\ &= -\frac{e^{c+dx^2}\mathrm{erf}(bx)}{x}+\frac{be^c\mathrm{Ei}(-(b^2-d)\,x^2)}{\sqrt{\pi}}+(2d)\int e^{c+dx^2}\mathrm{erf}(bx)\,dx\end{aligned}$$

Mathematica [A]
time = 0.15, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\mathrm{Erf}(bx)}{x^2}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erf[b*x])/x^2,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erf[b*x])/x^2, x]
```

Maple [A]
time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\operatorname{erf}\left(bx\right)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erf(b*x)/x^2,x)
```

```
[Out] int(exp(d*x^2+c)*erf(b*x)/x^2,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x)/x^2,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)*e^(d*x^2 + c)/x^2, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x)/x^2,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x)*e^(d*x^2 + c)/x^2, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^{2}}\operatorname{erf}{\left(bx \right)}}{x^{2}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erf(b*x)/x**2,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erf(b*x)/x**2, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x)/x^2,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(d*x^2 + c)/x^2, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{e^{d x^2+c} \operatorname{erf}(b x)}{x^2} \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + d*x^2)*erf(b*x))/x^2,x)
```

```
[Out] int((exp(c + d*x^2)*erf(b*x))/x^2, x)
```

3.63 $\int \frac{e^{c+dx^2}\mathbf{Erf}(bx)}{x^4}\,dx$

Optimal. Leaf size=155

$$-\frac{be^{c-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2}-\frac{e^{c+dx^2}\text{Erf}(bx)}{3x^3}-\frac{2de^{c+dx^2}\text{Erf}(bx)}{3x}-\frac{b(b^2-d)\,e^c\text{Ei}(-((b^2-d)\,x^2))}{3\sqrt{\pi}}+\frac{2bde^c\text{Ei}(-((b^2-d)\,x^2))}{3\sqrt{\pi}}+$$

```
[Out] -1/3*exp(d*x^2+c)*erf(b*x)/x^3-2/3*d*exp(d*x^2+c)*erf(b*x)/x-1/3*b*exp(c-(b
^2-d)*x^2)/x^2/Pi^(1/2)-1/3*b*(b^2-d)*exp(c)*Ei(-(b^2-d)*x^2)/Pi^(1/2)+2/3*
b*d*exp(c)*Ei(-(b^2-d)*x^2)/Pi^(1/2)+4/3*d^2*Unintegrable(exp(d*x^2+c)*erf(
b*x),x)
```

Rubi [A]
time = 0.19, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\text{Erf}(bx)}{x^4}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erf[b*x])/x^4,x]
```

```
[Out] -1/3*(b*E^(c - (b^2 - d)*x^2))/(Sqrt[Pi]*x^2) - (E^(c + d*x^2)*Erf[b*x])/(3
*x^3) - (2*d*E^(c + d*x^2)*Erf[b*x])/(3*x) - (b*(b^2 - d)*E^c*ExpIntegralEi
[-((b^2 - d)*x^2)])/(3*Sqrt[Pi]) + (2*b*d*E^c*ExpIntegralEi[-((b^2 - d)*x^2
)])/(3*Sqrt[Pi]) + (4*d^2*Defer[Int][E^(c + d*x^2)*Erf[b*x], x])/3
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+dx^2}\text{erf}(bx)}{x^4}\,dx &= -\frac{e^{c+dx^2}\text{erf}(bx)}{3x^3}+\frac{1}{3}(2d)\int \frac{e^{c+dx^2}\text{erf}(bx)}{x^2}\,dx+\frac{(2b)\int \frac{e^{c-(b^2-d)x^2}}{x^3}\,dx}{3\sqrt{\pi}}\\ &= -\frac{be^{c-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2}-\frac{e^{c+dx^2}\text{erf}(bx)}{3x^3}-\frac{2de^{c+dx^2}\text{erf}(bx)}{3x}+\frac{1}{3}(4d^2)\int e^{c+dx^2}\text{erf}(bx)\,dx-\frac{(2b(}{}\\ &= -\frac{be^{c-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2}-\frac{e^{c+dx^2}\text{erf}(bx)}{3x^3}-\frac{2de^{c+dx^2}\text{erf}(bx)}{3x}-\frac{b(b^2-d)\,e^c\text{Ei}(-(b^2-d)\,x^2)}{3\sqrt{\pi}}+\frac{2b}{}\end{aligned}$$

Mathematica [A]
time = 0.22, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\text{Erf}(bx)}{x^4}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erf[b*x])/x^4,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erf[b*x])/x^4, x]
```

Maple [A]
time = 0.18, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^{2}+c}\operatorname{erf}\left(b x\right)}{x^{4}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erf(b*x)/x^4,x)
```

```
[Out] int(exp(d*x^2+c)*erf(b*x)/x^4,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x)/x^4,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)*e^(d*x^2 + c)/x^4, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x)/x^4,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x)*e^(d*x^2 + c)/x^4, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^{2}}\operatorname{erf}\left(bx\right)}{x^{4}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erf(b*x)/x**4,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erf(b*x)/x**4, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x)/x^4,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(d*x^2 + c)/x^4, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{e^{d\,x^2+c}\,\mathrm{erf}(b\,x)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + d*x^2)*erf(b*x))/x^4,x)
```

```
[Out] int((exp(c + d*x^2)*erf(b*x))/x^4, x)
```

3.64 $\int e^{c+b^2x^2} x^5 \mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=118

$$-\frac{2e^c x}{b^5\sqrt{\pi}}+\frac{2e^c x^3}{3b^3\sqrt{\pi}}-\frac{e^c x^5}{5b\sqrt{\pi}}+\frac{e^{c+b^2x^2}\text{Erf}(bx)}{b^6}-\frac{e^{c+b^2x^2}x^2\text{Erf}(bx)}{b^4}+\frac{e^{c+b^2x^2}x^4\text{Erf}(bx)}{2b^2}$$

```
[Out] exp(b^2*x^2+c)*erf(b*x)/b^6-exp(b^2*x^2+c)*x^2*erf(b*x)/b^4+1/2*exp(b^2*x^2
+c)*x^4*erf(b*x)/b^2-2*exp(c)*x/b^5/Pi^(1/2)+2/3*exp(c)*x^3/b^3/Pi^(1/2)-1/
5*exp(c)*x^5/b/Pi^(1/2)
```

Rubi [A]
time = 0.09, antiderivative size = 118, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {6520, 6517, 8, 12, 30}

$$-\frac{2e^c x}{\sqrt{\pi}\,b^5}+\frac{2e^c x^3}{3\sqrt{\pi}\,b^3}+\frac{x^4e^{b^2x^2+c}\text{Erf}(bx)}{2b^2}+\frac{e^{b^2x^2+c}\text{Erf}(bx)}{b^6}-\frac{x^2e^{b^2x^2+c}\text{Erf}(bx)}{b^4}-\frac{e^c x^5}{5\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*x^5*Erf[b*x],x]
```

```
[Out] (-2*E^c*x)/(b^5*Sqrt[Pi]) + (2*E^c*x^3)/(3*b^3*Sqrt[Pi]) - (E^c*x^5)/(5*b*S
qrt[Pi]) + (E^(c + b^2*x^2)*Erf[b*x])/b^6 - (E^(c + b^2*x^2)*x^2*Erf[b*x])/
b^4 + (E^(c + b^2*x^2)*x^4*Erf[b*x])/(2*b^2)
```

Rule 8

```
Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{c+b^2x^2}x^5\operatorname{erf}(bx)\,dx &= \frac{e^{c+b^2x^2}x^4\operatorname{erf}(bx)}{2b^2}-\frac{2\int e^{c+b^2x^2}x^3\operatorname{erf}(bx)\,dx}{b^2}-\frac{\int e^cx^4\,dx}{b\sqrt{\pi}}\\ &= -\frac{e^{c+b^2x^2}x^2\operatorname{erf}(bx)}{b^4}+\frac{e^{c+b^2x^2}x^4\operatorname{erf}(bx)}{2b^2}+\frac{2\int e^{c+b^2x^2}x\operatorname{erf}(bx)\,dx}{b^4}+\frac{2\int e^cx^2\,dx}{b^3\sqrt{\pi}}-\cdots\\ &= -\frac{e^cx^5}{5b\sqrt{\pi}}+\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{b^6}-\frac{e^{c+b^2x^2}x^2\operatorname{erf}(bx)}{b^4}+\frac{e^{c+b^2x^2}x^4\operatorname{erf}(bx)}{2b^2}-\frac{2\int e^c\,dx}{b^5\sqrt{\pi}}+\cdots\\ &= -\frac{2e^cx}{b^5\sqrt{\pi}}+\frac{2e^cx^3}{3b^3\sqrt{\pi}}-\frac{e^cx^5}{5b\sqrt{\pi}}+\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{b^6}-\frac{e^{c+b^2x^2}x^2\operatorname{erf}(bx)}{b^4}+\frac{e^{c+b^2x^2}x^4\operatorname{erf}(bx)}{2b^2}\end{aligned}$$

Mathematica [A]
time = 0.03, size = 73, normalized size = 0.62

$$\frac{e^c\left(-60bx+20b^3x^3-6b^5x^5+15e^{b^2x^2}\sqrt{\pi}\,(2-2b^2x^2+b^4x^4)\operatorname{Erf}(bx)\right)}{30b^6\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*x^5*Erf[b*x],x]
[Out] (E^c*(-60*b*x + 20*b^3*x^3 - 6*b^5*x^5 + 15*E^(b^2*x^2)*Sqrt[Pi]*(2 - 2*b^2
*x^2 + b^4*x^4)*Erf[b*x]))/(30*b^6*Sqrt[Pi])
```

Maple [A]
time = 0.31, size = 88, normalized size = 0.75

method	result	size
default	$\frac{\frac{\operatorname{erf}(bx)e^c\left(\frac{e^{b^2x^2}b^4x^4}{2}-b^2x^2e^{b^2x^2}+e^{b^2x^2}\right)}{b^5}-\frac{e^c\left(\frac{1}{5}b^5x^5-\frac{2}{3}b^3x^3+2bx\right)}{\sqrt{\pi}\,b^5}}{b}$	88

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*x^5*erf(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] (erf(b*x)/b^5*exp(c)*(1/2*exp(b^2*x^2)*b^4*x^4-b^2*x^2*exp(b^2*x^2)+exp(b^2
*x^2))-1/Pi^(1/2)/b^5*exp(c)*(1/5*b^5*x^5-2/3*b^3*x^3+2*b*x))/b
```

Maxima [A]
time = 0.26, size = 82, normalized size = 0.69

$$-\frac{6\,b^5x^5e^c-20\,b^3x^3e^c-15\left(\sqrt{\pi}\,b^4x^4e^c-2\,\sqrt{\pi}\,b^2x^2e^c+2\,\sqrt{\pi}\,e^c\right)\operatorname{erf}(bx)\,e^{\left(b^2x^2\right)}+60\,bxe^c}{30\,\sqrt{\pi}\,b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^5*erf(b*x),x, algorithm="maxima")
```

```
[Out] -1/30*(6*b^5*x^5*e^c - 20*b^3*x^3*e^c - 15*(sqrt(pi)*b^4*x^4*e^c - 2*sqrt(p
i)*b^2*x^2*e^c + 2*sqrt(pi)*e^c)*erf(b*x)*e^(b^2*x^2) + 60*b*x*e^c)/(sqrt(p
i)*b^6)
```

Fricas [A]
time = 0.35, size = 74, normalized size = 0.63

$$\frac{15\left(2\,\pi+\pi b^4x^4-2\,\pi b^2x^2\right)\operatorname{erf}(bx)\,e^{\left(b^2x^2+c\right)}-2\,\sqrt{\pi}\,\left(3\,b^5x^5-10\,b^3x^3+30\,bx\right)e^c}{30\,\pi b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^5*erf(b*x),x, algorithm="fricas")
```

```
[Out] 1/30*(15*(2*pi + pi*b^4*x^4 - 2*pi*b^2*x^2)*erf(b*x)*e^(b^2*x^2 + c) - 2*sq
rt(pi)*(3*b^5*x^5 - 10*b^3*x^3 + 30*b*x)*e^c)/(pi*b^6)
```

Sympy [A]
time = 44.08, size = 119, normalized size = 1.01

$$\begin{cases}-\frac{x^5e^c}{5\sqrt{\pi}\,b}+\frac{x^4e^ce^{b^2x^2}\operatorname{erf}(bx)}{2b^2}+\frac{2x^3e^c}{3\sqrt{\pi}\,b^3}-\frac{x^2e^ce^{b^2x^2}\operatorname{erf}(bx)}{b^4}-\frac{2xe^c}{\sqrt{\pi}\,b^5}+\frac{e^ce^{b^2x^2}\operatorname{erf}(bx)}{b^6} & \text{for } b\neq 0\\ 0 & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*x**5*erf(b*x),x)
```

```
[Out] Piecewise((-x**5*exp(c)/(5*sqrt(pi)*b) + x**4*exp(c)*exp(b**2*x**2)*erf(b*x
)/(2*b**2) + 2*x**3*exp(c)/(3*sqrt(pi)*b**3) - x**2*exp(c)*exp(b**2*x**2)*e
rf(b*x)/b**4 - 2*x*exp(c)/(sqrt(pi)*b**5) + exp(c)*exp(b**2*x**2)*erf(b*x)/
b**6, Ne(b, 0)), (0, True))
```

Giac [A]
time = 0.40, size = 118, normalized size = 1.00

$$\frac{1}{2}\left(\frac{c^2e^{\left(b^2x^2+c\right)}}{b^6}-\frac{\left(2\,b^2x^2-\left(b^2x^2+c\right)^2+2\left(b^2x^2+c\right)c-2\right)e^{\left(b^2x^2+c\right)}}{b^6}\right)\operatorname{erf}(bx)-\frac{3\,\sqrt{\pi}\,b^4x^5e^c-10\,\sqrt{\pi}\,b^2x^3e^c+30\,\sqrt{\pi}\,xe^c}{15\,\pi b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^5*erf(b*x),x, algorithm="giac")
```

```
[Out] 1/2*(c^2*e^(b^2*x^2 + c)/b^6 - (2*b^2*x^2 - (b^2*x^2 + c)^2 + 2*(b^2*x^2 +
c)*c - 2)*e^(b^2*x^2 + c)/b^6)*erf(b*x) - 1/15*(3*sqrt(pi)*b^4*x^5*e^c - 10
*sqrt(pi)*b^2*x^3*e^c + 30*sqrt(pi)*x*e^c)/(pi*b^5)
```

Mupad [B]
time = 0.30, size = 91, normalized size = 0.77

$$\mathrm{erf}(b\,x)\,\left(\frac{{\mathrm{e}}^{b^2\,x^2+c}}{b^6}+\frac{x^4\,{\mathrm{e}}^{b^2\,x^2+c}}{2\,b^2}-\frac{x^2\,{\mathrm{e}}^{b^2\,x^2+c}}{b^4}\right)-\frac{3\,{\mathrm{e}}^c\,b^4\,x^5-10\,{\mathrm{e}}^c\,b^2\,x^3+30\,{\mathrm{e}}^c\,x}{15\,b^5\,\sqrt{\pi }}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*exp(c + b^2*x^2)*erf(b*x),x)
```

```
[Out] erf(b*x)*(exp(c + b^2*x^2)/b^6 + (x^4*exp(c + b^2*x^2))/(2*b^2) - (x^2*exp(
c + b^2*x^2))/b^4) - (30*x*exp(c) - 10*b^2*x^3*exp(c) + 3*b^4*x^5*exp(c))/(
15*b^5*pi^(1/2))
```

3.65 $\int e^{c+b^2x^2}x^3\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=79

$$\frac{e^c x}{b^3\sqrt{\pi}}-\frac{e^c x^3}{3b\sqrt{\pi}}-\frac{e^{c+b^2x^2}\operatorname{Erf}(bx)}{2b^4}+\frac{e^{c+b^2x^2}x^2\operatorname{Erf}(bx)}{2b^2}$$

```
[Out] -1/2*exp(b^2*x^2+c)*erf(b*x)/b^4+1/2*exp(b^2*x^2+c)*x^2*erf(b*x)/b^2+exp(c)
*x/b^3/Pi^(1/2)-1/3*exp(c)*x^3/b/Pi^(1/2)
```

Rubi [A]
time = 0.05, antiderivative size = 79, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.263, Rules used = {6520, 6517, 8, 12, 30}

$$\frac{e^c x}{\sqrt{\pi}\,b^3}+\frac{x^2e^{b^2x^2+c}\operatorname{Erf}(bx)}{2b^2}-\frac{e^{b^2x^2+c}\operatorname{Erf}(bx)}{2b^4}-\frac{e^c x^3}{3\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*x^3*Erf[b*x],x]
```

```
[Out] (E^c*x)/(b^3*Sqrt[Pi]) - (E^c*x^3)/(3*b*Sqrt[Pi]) - (E^(c + b^2*x^2)*Erf[b*
x])/(2*b^4) + (E^(c + b^2*x^2)*x^2*Erf[b*x])/(2*b^2)
```

Rule 8

```
Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{c+b^2x^2}x^3\text{erf}(bx)\,dx &= \frac{e^{c+b^2x^2}x^2\text{erf}(bx)}{2b^2}-\frac{\int e^{c+b^2x^2}x\text{erf}(bx)\,dx}{b^2}-\frac{\int e^cx^2\,dx}{b\sqrt{\pi}}\\ &= -\frac{e^{c+b^2x^2}\text{erf}(bx)}{2b^4}+\frac{e^{c+b^2x^2}x^2\text{erf}(bx)}{2b^2}+\frac{\int e^c\,dx}{b^3\sqrt{\pi}}-\frac{e^c\int x^2\,dx}{b\sqrt{\pi}}\\ &= \frac{e^cx}{b^3\sqrt{\pi}}-\frac{e^cx^3}{3b\sqrt{\pi}}-\frac{e^{c+b^2x^2}\text{erf}(bx)}{2b^4}+\frac{e^{c+b^2x^2}x^2\text{erf}(bx)}{2b^2}\end{aligned}$$

Mathematica [A]
time = 0.02, size = 57, normalized size = 0.72

$$\frac{e^c\left(6bx-2b^3x^3+3e^{b^2x^2}\sqrt{\pi}\left(-1+b^2x^2\right)\text{Erf}(bx)\right)}{6b^4\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*x^3*Erf[b*x],x]
```

```
[Out] (E^c*(6*b*x - 2*b^3*x^3 + 3*E^(b^2*x^2)*Sqrt[Pi]*(-1 + b^2*x^2)*Erf[b*x]))/
(6*b^4*Sqrt[Pi])
```

Maple [A]
time = 0.53, size = 66, normalized size = 0.84

method	result	size
default	$\frac{\frac{\text{erf}(bx)\,\mathrm{e}^{c}\left(\frac{b^{2}x^{2}\mathrm{e}^{b^{2}x^{2}}}{2}-\frac{\mathrm{e}^{b^{2}x^{2}}}{2}\right)}{b^{3}}-\frac{\mathrm{e}^{c}\left(\frac{1}{3}b^{3}x^{3}-bx\right)}{\sqrt{\pi}\,b^{3}}}{b}$	66

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*x^3*erf(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] (erf(b*x)/b^3*exp(c)*(1/2*b^2*x^2*exp(b^2*x^2)-1/2*exp(b^2*x^2))-1/Pi^(1/2)
/b^3*exp(c)*(1/3*b^3*x^3-b*x))/b
```

Maxima [A]
time = 0.26, size = 59, normalized size = 0.75

$$-\frac{2\,b^3x^3e^c - 3\left(\sqrt{\pi}\,b^2x^2e^c - \sqrt{\pi}\,e^c\right)\operatorname{erf}(bx)\,e^{\left(b^2x^2\right)} - 6\,bxe^c}{6\,\sqrt{\pi}\,b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^3*erf(b*x),x, algorithm="maxima")
```

```
[Out] -1/6*(2*b^3*x^3*e^c - 3*(sqrt(pi)*b^2*x^2*e^c - sqrt(pi)*e^c)*erf(b*x)*e^(b
^2*x^2) - 6*b*x*e^c)/(sqrt(pi)*b^4)
```

Fricas [A]
time = 0.40, size = 55, normalized size = 0.70

$$-\frac{3\left(\pi - \pi b^2x^2\right)\operatorname{erf}(bx)\,e^{\left(b^2x^2+c\right)} + 2\,\sqrt{\pi}\,(b^3x^3 - 3\,bx)e^c}{6\,\pi b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^3*erf(b*x),x, algorithm="fricas")
```

```
[Out] -1/6*(3*(pi - pi*b^2*x^2)*erf(b*x)*e^(b^2*x^2 + c) + 2*sqrt(pi)*(b^3*x^3 -
3*b*x)*e^c)/(pi*b^4)
```

Sympy [A]
time = 8.60, size = 76, normalized size = 0.96

$$\begin{cases} -\frac{x^3e^c}{3\sqrt{\pi}\,b} + \frac{x^2e^ce^{b^2x^2}\operatorname{erf}(bx)}{2b^2} + \frac{xe^c}{\sqrt{\pi}\,b^3} - \frac{e^ce^{b^2x^2}\operatorname{erf}(bx)}{2b^4} & \text{for}\ b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*x**3*erf(b*x),x)
```

```
[Out] Piecewise((-x**3*exp(c)/(3*sqrt(pi)*b) + x**2*exp(c)*exp(b**2*x**2)*erf(b*x
)/(2*b**2) + x*exp(c)/(sqrt(pi)*b**3) - exp(c)*exp(b**2*x**2)*erf(b*x)/(2*b
**4), Ne(b, 0)), (0, True))
```

Giac [A]
time = 0.41, size = 71, normalized size = 0.90

$$\frac{1}{2}\left(\frac{(b^2x^2 + c - 1)e^{\left(b^2x^2+c\right)}}{b^4} - \frac{ce^{\left(b^2x^2+c\right)}}{b^4}\right)\operatorname{erf}(bx) - \frac{b^2x^3e^c - 3\,xe^c}{3\,\sqrt{\pi}\,b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^3*erf(b*x),x, algorithm="giac")
```

```
[Out] 1/2*((b^2*x^2 + c - 1)*e^(b^2*x^2 + c)/b^4 - c*e^(b^2*x^2 + c)/b^4)*erf(b*x
) - 1/3*(b^2*x^3*e^c - 3*x*e^c)/(sqrt(pi)*b^3)
```

Mupad [B]
time = 0.20, size = 65, normalized size = 0.82

$$\frac{3\,x\,\mathrm{e}^c-b^2\,x^3\,\mathrm{e}^c}{3\,b^3\,\sqrt{\pi}}-\mathrm{erf}(b\,x)\,\left(\frac{\mathrm{e}^{b^2\,x^2+c}}{2\,b^4}-\frac{x^2\,\mathrm{e}^{b^2\,x^2+c}}{2\,b^2}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*exp(c + b^2*x^2)*erf(b*x),x)
```

```
[Out] (3*x*exp(c) - b^2*x^3*exp(c))/(3*b^3*pi^(1/2)) - erf(b*x)*(exp(c + b^2*x^2)
/(2*b^4) - (x^2*exp(c + b^2*x^2))/(2*b^2))
```

3.66 $\int e^{c+b^2x^2} x\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=37

$$-\frac{e^c x}{b\sqrt{\pi}}+\frac{e^{c+b^2x^2}\mathrm{Erf}(bx)}{2b^2}$$

[Out] 1/2*exp(b^2*x^2+c)*erf(b*x)/b^2-exp(c)*x/b/Pi^(1/2)

Rubi [A]
time = 0.02, antiderivative size = 37, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.118, Rules used = {6517, 8}

$$\frac{e^{b^2x^2+c}\mathrm{Erf}(bx)}{2b^2}-\frac{e^c x}{\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

[In] Int[E^(c + b^2*x^2)*x*Erf[b*x],x]

[Out] -((E^c*x)/(b*Sqrt[Pi])) + (E^(c + b^2*x^2)*Erf[b*x])/(2*b^2)

Rule 8

```
Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\begin{aligned}\int e^{c+b^2x^2} x\mathrm{erf}(bx)\,dx &= \frac{e^{c+b^2x^2}\mathrm{erf}(bx)}{2b^2}-\frac{\int e^c\,dx}{b\sqrt{\pi}}\\ &= -\frac{e^c x}{b\sqrt{\pi}}+\frac{e^{c+b^2x^2}\mathrm{erf}(bx)}{2b^2}\end{aligned}$$

Mathematica [A]
time = 0.02, size = 34, normalized size = 0.92

$$\frac{e^c\left(-\frac{2bx}{\sqrt{\pi}}+e^{b^2x^2}\mathrm{Erf}(bx)\right)}{2b^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*x*Erf[b*x],x]
```

```
[Out] (E^c*((-2*b*x)/Sqrt[Pi] + E^(b^2*x^2)*Erf[b*x]))/(2*b^2)
```

Maple [A]
time = 0.10, size = 51, normalized size = 1.38

method	result	size
default	$\frac{-2\,{\mathrm e}^{b^{2} x^{2}+c} {\mathrm e}^{-b^{2} x^{2}} x b+{\mathrm e}^{b^{2} x^{2}+c} \operatorname{erf}\left(b x \right) \sqrt{\pi}}{2 b^{2} \sqrt{\pi}}$	51

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*x*erf(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/2*(-2*exp(b^2*x^2+c)*exp(-b^2*x^2)*x*b+exp(b^2*x^2+c)*erf(b*x)*Pi^(1/2))/
b^2/Pi^(1/2)
```

Maxima [A]
time = 0.26, size = 34, normalized size = 0.92

$$-\frac{2\,bxe^{c}-\sqrt{\pi}\,\operatorname{erf}\left(bx\right)e^{\left(b^{2}x^{2}+c\right)}}{2\,\sqrt{\pi}\,b^{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x*erf(b*x),x, algorithm="maxima")
```

```
[Out] -1/2*(2*b*x*e^c - sqrt(pi)*erf(b*x)*e^(b^2*x^2 + c))/(sqrt(pi)*b^2)
```

Fricas [A]
time = 0.33, size = 35, normalized size = 0.95

$$-\frac{2\,\sqrt{\pi}\,bxe^{c}-\pi\operatorname{erf}\left(bx\right)e^{\left(b^{2}x^{2}+c\right)}}{2\,\pi b^{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x*erf(b*x),x, algorithm="fricas")
```

```
[Out] -1/2*(2*sqrt(pi)*b*x*e^c - pi*erf(b*x)*e^(b^2*x^2 + c))/(pi*b^2)
```

Sympy [A]
time = 1.54, size = 34, normalized size = 0.92

$$\begin{cases} -\frac{xe^{c}}{\sqrt{\pi}\,b}+\frac{e^{c}e^{b^{2}x^{2}}\operatorname{erf}\left(bx\right)}{2b^{2}} & \text{for}\ b\neq 0\\ 0 & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*x*erf(b*x),x)
```

```
[Out] Piecewise((-x*exp(c)/(sqrt(pi)*b) + exp(c)*exp(b**2*x**2)*erf(b*x)/(2*b**2)
, Ne(b, 0)), (0, True))
```

Giac [A]
time = 0.43, size = 31, normalized size = 0.84

$$-\frac{xe^c}{\sqrt{\pi}\,b} + \frac{\operatorname{erf}(bx)\,e^{\left(b^2x^2+c\right)}}{2\,b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x*erf(b*x),x, algorithm="giac")
```

```
[Out] -x*e^c/(sqrt(pi)*b) + 1/2*erf(b*x)*e^(b^2*x^2 + c)/b^2
```

Mupad [B]
time = 0.10, size = 31, normalized size = 0.84

$$\frac{\mathrm{e}^{b^2\,x^2}\,\mathrm{e}^c\,\mathrm{erf}(b\,x)}{2\,b^2} - \frac{x\,\mathrm{e}^c}{b\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*exp(c + b^2*x^2)*erf(b*x),x)
```

```
[Out] (exp(b^2*x^2)*exp(c)*erf(b*x))/(2*b^2) - (x*exp(c))/(b*pi^(1/2))
```

3.67 $\int \frac{e^{c+b^2x^2}\mathbf{Erf}(bx)}{x}\,dx$

Optimal. Leaf size=32

$$\frac{2be^c x\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}$$

[Out] 2*b*exp(c)*x*hypergeom([1/2, 1],[3/2, 3/2],b^2*x^2)/Pi^(1/2)

Rubi [A]
time = 0.03, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.053$, Rules used = {6523}

$$\frac{2be^c x\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

[In] Int[(E^(c + b^2*x^2)*Erf[b*x])/x,x]

[Out] (2*b*E^c*x*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, b^2*x^2])/Sqrt[Pi]

Rule 6523

```
Int[(E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)])/(x_), x_Symbol] :> Simp[2*b*
E^c*(x/Sqrt[Pi])*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, b^2*x^2], x] /; Fr
eeQ[{b, c, d}, x] && EqQ[d, b^2]
```

Rubi steps

$$\int \frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{x}\,dx = \frac{2be^c x\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}$$

Mathematica [A]
time = 0.06, size = 32, normalized size = 1.00

$$\frac{2be^c x\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

[In] Integrate[(E^(c + b^2*x^2)*Erf[b*x])/x,x]

[Out] (2*b*E^c*x*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, b^2*x^2])/Sqrt[Pi]

Maple [F]
time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{b^2x^2+c}\,\mathrm{erf}\left(bx\right)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erf(b*x)/x,x)
```

```
[Out] int(exp(b^2*x^2+c)*erf(b*x)/x,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x)/x,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)*e^(b^2*x^2 + c)/x, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x)/x,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x)*e^(b^2*x^2 + c)/x, x)
```

Sympy [A]
time = 5.96, size = 26, normalized size = 0.81

$$\frac{2bxe^{c}{}_{2}F_{2}\left(\begin{matrix} \frac{1}{2}, 1 \\ \frac{3}{2}, \frac{3}{2} \end{matrix}\middle|{b^{2}x^{2}}\right)}{\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erf(b*x)/x,x)
```

```
[Out] 2*b*x*exp(c)*hyper((1/2, 1), (3/2, 3/2), b**2*x**2)/sqrt(pi)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x)/x,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(b^2*x^2 + c)/x, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{e^{b^2 x^2+c} \operatorname{erf}(b x)}{x} \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + b^2*x^2)*erf(b*x))/x,x)
```

```
[Out] int((exp(c + b^2*x^2)*erf(b*x))/x, x)
```

3.68 $\int \frac{e^{c+b^2x^2}\mathbf{Erf}(bx)}{x^3}\,dx$

Optimal. Leaf size=71

$$-\frac{be^c}{\sqrt{\pi}\,x}-\frac{e^{c+b^2x^2}\mathrm{Erf}(bx)}{2x^2}+\frac{2b^3e^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}$$

```
[Out] -1/2*exp(b^2*x^2+c)*erf(b*x)/x^2-b*exp(c)/x/Pi^(1/2)+2*b^3*exp(c)*x*hyperge
om([1/2, 1],[3/2, 3/2],b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.06, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {6526, 6523, 12, 30}

$$\frac{2b^3e^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}-\frac{e^{b^2x^2+c}\mathrm{Erf}(bx)}{2x^2}-\frac{be^c}{\sqrt{\pi}\,x}$$

Antiderivative was successfully verified.

```
[In] Int[(E^(c + b^2*x^2)*Erf[b*x])/x^3,x]
```

```
[Out] -((b*E^c)/(Sqrt[Pi]*x)) - (E^(c + b^2*x^2)*Erf[b*x])/(2*x^2) + (2*b^3*E^c*x
*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, b^2*x^2])/Sqrt[Pi]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6523

```
Int[(E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)])/(x_), x_Symbol] :> Simp[2*b*
E^c*(x/Sqrt[Pi])*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, b^2*x^2], x] /; Fr
eeQ[{b, c, d}, x] && EqQ[d, b^2]
```

Rule 6526

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m + 1)*E^(c + d*x^2)*(Erf[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(m
+ 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[2*(b/((m + 1
)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x])
```

```
/; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{x^3}\,dx &= -\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{2x^2}+b^2\int \frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{x}\,dx+\frac{b\int \frac{e^c}{x^2}\,dx}{\sqrt{\pi}}\\ &= -\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{2x^2}+\frac{2b^3e^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}+\frac{(be^c)\int \frac{1}{x^2}\,dx}{\sqrt{\pi}}\\ &= -\frac{be^c}{\sqrt{\pi}\,x}-\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{2x^2}+\frac{2b^3e^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.09, size = 34, normalized size = 0.48

$$-\frac{2be^c\,{}_2F_2\left(-\frac{1}{2},1;\frac{1}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}\,x}$$

Antiderivative was successfully verified.

```
[In] Integrate[(E^(c + b^2*x^2)*Erf[b*x])/x^3,x]
[Out] (-2*b*E^c*HypergeometricPFQ[{-1/2, 1}, {1/2, 3/2}, b^2*x^2])/(Sqrt[Pi]*x)
```

Maple [F]
time = 0.16, size = 0, normalized size = 0.00

$$\int \frac{e^{b^2x^2+c}\operatorname{erf}(bx)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erf(b*x)/x^3,x)
[Out] int(exp(b^2*x^2+c)*erf(b*x)/x^3,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x)/x^3,x, algorithm="maxima")
[Out] integrate(erf(b*x)*e^(b^2*x^2 + c)/x^3, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x)/x^3,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x)*e^(b^2*x^2 + c)/x^3, x)
```

Sympy [A]
time = 28.61, size = 29, normalized size = 0.41

$$-\frac{2be^c{}_2F_2\left(\begin{matrix} -\frac{1}{2}, 1 \\ \frac{1}{2}, \frac{3}{2} \end{matrix}\middle| b^2x^2\right)}{\sqrt{\pi}\, x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erf(b*x)/x**3,x)
```

```
[Out] -2*b*exp(c)*hyper((-1/2, 1), (1/2, 3/2), b**2*x**2)/(sqrt(pi)*x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x)/x^3,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(b^2*x^2 + c)/x^3, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{b^2\,x^2+c}\,\mathrm{erf}(b\,x)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + b^2*x^2)*erf(b*x))/x^3,x)
```

```
[Out] int((exp(c + b^2*x^2)*erf(b*x))/x^3, x)
```

3.69 $\int \frac{e^{c+b^2x^2}\mathbf{Erf}(bx)}{x^5}\,dx$

Optimal. Leaf size=115

$$-\frac{be^c}{6\sqrt{\pi}\,x^3}-\frac{b^3e^c}{2\sqrt{\pi}\,x}-\frac{e^{c+b^2x^2}\mathrm{Erf}(bx)}{4x^4}-\frac{b^2e^{c+b^2x^2}\mathrm{Erf}(bx)}{4x^2}+\frac{b^5e^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}$$

```
[Out] -1/4*exp(b^2*x^2+c)*erf(b*x)/x^4-1/4*b^2*exp(b^2*x^2+c)*erf(b*x)/x^2-1/6*b*
exp(c)/x^3/Pi^(1/2)-1/2*b^3*exp(c)/x/Pi^(1/2)+b^5*exp(c)*x*hypergeom([1/2,
1],[3/2, 3/2],b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.09, antiderivative size = 115, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {6526, 6523, 12, 30}

$$\frac{b^5e^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}-\frac{b^3e^c}{2\sqrt{\pi}\,x}-\frac{b^2e^{b^2x^2+c}\mathrm{Erf}(bx)}{4x^2}-\frac{e^{b^2x^2+c}\mathrm{Erf}(bx)}{4x^4}-\frac{be^c}{6\sqrt{\pi}\,x^3}$$

Antiderivative was successfully verified.

```
[In] Int[(E^(c + b^2*x^2)*Erf[b*x])/x^5,x]
```

```
[Out] -1/6*(b*E^c)/(Sqrt[Pi]*x^3) - (b^3*E^c)/(2*Sqrt[Pi]*x) - (E^(c + b^2*x^2)*E
rf[b*x])/(4*x^4) - (b^2*E^(c + b^2*x^2)*Erf[b*x])/(4*x^2) + (b^5*E^c*x*Hype
rgeometricPFQ[{1/2, 1}, {3/2, 3/2}, b^2*x^2])/Sqrt[Pi]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6523

```
Int[(E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)])/(x_), x_Symbol] :> Simp[2*b*
E^c*(x/Sqrt[Pi])*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, b^2*x^2], x] /; Fr
eeQ[{b, c, d}, x] && EqQ[d, b^2]
```

Rule 6526

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m + 1)*E^(c + d*x^2)*(Erf[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(m
```

```
+ 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[2*(b/((m + 1
)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x])
 /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{x^5}\,dx &= -\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{4x^4}+\frac{1}{2}b^2\int \frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{x^3}\,dx+\frac{b\int \frac{e^c}{x^4}\,dx}{2\sqrt{\pi}}\\ &= -\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{4x^4}-\frac{b^2e^{c+b^2x^2}\operatorname{erf}(bx)}{4x^2}+\frac{1}{2}b^4\int \frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{x}\,dx+\frac{b^3\int \frac{e^c}{x^2}\,dx}{2\sqrt{\pi}}+\frac{(be^c)\int \frac{1}{x}\\ &= -\frac{be^c}{6\sqrt{\pi}\,x^3}-\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{4x^4}-\frac{b^2e^{c+b^2x^2}\operatorname{erf}(bx)}{4x^2}+\frac{b^5e^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}+\frac{(b^3e^c)\int}{2\sqrt{\pi}\\ &= -\frac{be^c}{6\sqrt{\pi}\,x^3}-\frac{b^3e^c}{2\sqrt{\pi}\,x}-\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{4x^4}-\frac{b^2e^{c+b^2x^2}\operatorname{erf}(bx)}{4x^2}+\frac{b^5e^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.10, size = 36, normalized size = 0.31

$$-\frac{2be^c\,{}_2F_2\left(-\frac{3}{2},1;-\frac{1}{2},\frac{3}{2};b^2x^2\right)}{3\sqrt{\pi}\,x^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[(E^(c + b^2*x^2)*Erf[b*x])/x^5,x]
[Out] (-2*b*E^c*HypergeometricPFQ[{-3/2, 1}, {-1/2, 3/2}, b^2*x^2])/(3*Sqrt[Pi]*x
^3)
```

Maple [F]
time = 0.17, size = 0, normalized size = 0.00

$$\int \frac{e^{b^2x^2+c}\operatorname{erf}(bx)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erf(b*x)/x^5,x)
[Out] int(exp(b^2*x^2+c)*erf(b*x)/x^5,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x)/x^5,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)*e^(b^2*x^2 + c)/x^5, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x)/x^5,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x)*e^(b^2*x^2 + c)/x^5, x)
```

Sympy [F(-1)] Timed out
time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erf(b*x)/x**5,x)
```

```
[Out] Timed out
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x)/x^5,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(b^2*x^2 + c)/x^5, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{b^2\,x^2+c}\,\mathrm{erf}(b\,x)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + b^2*x^2)*erf(b*x))/x^5,x)
```

```
[Out] int((exp(c + b^2*x^2)*erf(b*x))/x^5, x)
```

3.70 $\int e^{c+b^2x^2} x^4 \textbf{Erf}(bx)\,dx$

Optimal. Leaf size=119

$$\frac{3e^c x^2}{4b^3\sqrt{\pi}} - \frac{e^c x^4}{4b\sqrt{\pi}} - \frac{3e^{c+b^2x^2} x\mathrm{Erf}(bx)}{4b^4} + \frac{e^{c+b^2x^2} x^3\mathrm{Erf}(bx)}{2b^2} + \frac{3e^c x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{4b^3\sqrt{\pi}}$$

```
[Out] -3/4*exp(b^2*x^2+c)*x*erf(b*x)/b^4+1/2*exp(b^2*x^2+c)*x^3*erf(b*x)/b^2+3/4*
exp(c)*x^2/b^3/Pi^(1/2)-1/4*exp(c)*x^4/b/Pi^(1/2)+3/4*exp(c)*x^2*hypergeom(
[1, 1],[3/2, 2],b^2*x^2)/b^3/Pi^(1/2)
```

Rubi [A]
time = 0.08, antiderivative size = 119, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {6520, 6511, 12, 30}

$$\frac{3e^c x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{4\sqrt{\pi}\,b^3} + \frac{3e^c x^2}{4\sqrt{\pi}\,b^3} + \frac{x^3 e^{b^2x^2+c}\mathrm{Erf}(bx)}{2b^2} - \frac{3xe^{b^2x^2+c}\mathrm{Erf}(bx)}{4b^4} - \frac{e^c x^4}{4\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*x^4*Erf[b*x],x]
```

```
[Out] (3*E^c*x^2)/(4*b^3*Sqrt[Pi]) - (E^c*x^4)/(4*b*Sqrt[Pi]) - (3*E^(c + b^2*x^2
)*x*Erf[b*x])/(4*b^4) + (E^(c + b^2*x^2)*x^3*Erf[b*x])/(2*b^2) + (3*E^c*x^2
*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2])/(4*b^3*Sqrt[Pi])
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
```

```
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{c+b^2x^2}x^4\operatorname{erf}(bx)\,dx &= \frac{e^{c+b^2x^2}x^3\operatorname{erf}(bx)}{2b^2}-\frac{3\int e^{c+b^2x^2}x^2\operatorname{erf}(bx)\,dx}{2b^2}-\frac{\int e^cx^3\,dx}{b\sqrt{\pi}}\\ &= -\frac{3e^{c+b^2x^2}x\operatorname{erf}(bx)}{4b^4}+\frac{e^{c+b^2x^2}x^3\operatorname{erf}(bx)}{2b^2}+\frac{3\int e^{c+b^2x^2}\operatorname{erf}(bx)\,dx}{4b^4}+\frac{3\int e^cx\,dx}{2b^3\sqrt{\pi}}-\frac{e^c\int x}{b\sqrt{}}\\ &= -\frac{e^cx^4}{4b\sqrt{\pi}}-\frac{3e^{c+b^2x^2}x\operatorname{erf}(bx)}{4b^4}+\frac{e^{c+b^2x^2}x^3\operatorname{erf}(bx)}{2b^2}+\frac{3e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{4b^3\sqrt{\pi}}+\frac{(3e^{c}}{2b}\\ &= \frac{3e^cx^2}{4b^3\sqrt{\pi}}-\frac{e^cx^4}{4b\sqrt{\pi}}-\frac{3e^{c+b^2x^2}x\operatorname{erf}(bx)}{4b^4}+\frac{e^{c+b^2x^2}x^3\operatorname{erf}(bx)}{2b^2}+\frac{3e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x\right.}{4b^3\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.21, size = 100, normalized size = 0.84

$$\frac{e^c\left(6b^2x^2-2b^4x^4+2be^{b^2x^2}\sqrt{\pi}\,x(-3+2b^2x^2)\operatorname{Erf}(bx)+3\pi\operatorname{Erf}(bx)\operatorname{Erfi}(bx)-6b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)\right)}{8b^5\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*x^4*Erf[b*x],x]
```

```
[Out] (E^c*(6*b^2*x^2 - 2*b^4*x^4 + 2*b*E^(b^2*x^2)*Sqrt[Pi]*x*(-3 + 2*b^2*x^2)*E
rf[b*x] + 3*Pi*Erf[b*x]*Erfi[b*x] - 6*b^2*x^2*HypergeometricPFQ[{1, 1}, {3/
2, 2}, -(b^2*x^2)]))/(8*b^5*Sqrt[Pi])
```

Maple [F]
time = 0.07, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{b^2x^2+c}x^4\operatorname{erf}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*x^4*erf(b*x),x)
```

```
[Out] int(exp(b^2*x^2+c)*x^4*erf(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^4*erf(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x^4*erf(b*x)*e^(b^2*x^2 + c), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^4*erf(b*x),x, algorithm="fricas")
```

```
[Out] integral(x^4*erf(b*x)*e^(b^2*x^2 + c), x)
```

Sympy [F(-1)] Timed out
time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*x**4*erf(b*x),x)
```

```
[Out] Timed out
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^4*erf(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^4*erf(b*x)*e^(b^2*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^4\,\mathrm{e}^{b^2\,x^2+c}\,\mathrm{erf}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*exp(c + b^2*x^2)*erf(b*x),x)
```

```
[Out] int(x^4*exp(c + b^2*x^2)*erf(b*x), x)
```

3.71 $\int e^{c+b^2x^2}x^2\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=76

$$-\frac{e^cx^2}{2b\sqrt{\pi}}+\frac{e^{c+b^2x^2}x\text{Erf}(bx)}{2b^2}-\frac{e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2b\sqrt{\pi}}$$

```
[Out] 1/2*exp(b^2*x^2+c)*x*erf(b*x)/b^2-1/2*exp(c)*x^2/b/Pi^(1/2)-1/2*exp(c)*x^2*
hypergeom([1, 1],[3/2, 2],b^2*x^2)/b/Pi^(1/2)
```

Rubi [A]
time = 0.04, antiderivative size = 76, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.210, Rules used = {6520, 6511, 12, 30}

$$-\frac{e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}\,b}+\frac{xe^{b^2x^2+c}\text{Erf}(bx)}{2b^2}-\frac{e^cx^2}{2\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*x^2*Erf[b*x],x]
```

```
[Out] -1/2*(E^c*x^2)/(b*Sqrt[Pi]) + (E^(c + b^2*x^2)*x*Erf[b*x])/(2*b^2) - (E^c*x
^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2])/(2*b*Sqrt[Pi])
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
```

```
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{c+b^2x^2}x^2\text{erf}(bx)\,dx &= \frac{e^{c+b^2x^2}x\text{erf}(bx)}{2b^2}-\frac{\int e^{c+b^2x^2}\text{erf}(bx)\,dx}{2b^2}-\frac{\int e^c x\,dx}{b\sqrt{\pi}}\\ &= \frac{e^{c+b^2x^2}x\text{erf}(bx)}{2b^2}-\frac{e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2b\sqrt{\pi}}-\frac{e^c\int x\,dx}{b\sqrt{\pi}}\\ &= -\frac{e^cx^2}{2b\sqrt{\pi}}+\frac{e^{c+b^2x^2}x\text{erf}(bx)}{2b^2}-\frac{e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2b\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.15, size = 80, normalized size = 1.05

$$\frac{e^c\left(-2b^2x^2+\text{Erf}(bx)\left(2be^{b^2x^2}\sqrt{\pi}\,x-\pi\text{Erfi}(bx)\right)+2b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)\right)}{4b^3\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*x^2*Erf[b*x],x]
```

```
[Out] (E^c*(-2*b^2*x^2 + Erf[b*x]*(2*b*E^(b^2*x^2)*Sqrt[Pi]*x - Pi*Erfi[b*x]) + 2
*b^2*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, -(b^2*x^2)]))/(4*b^3*Sqrt[Pi])
```

Maple [F]
time = 0.12, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{b^2x^2+c}x^2\,\text{erf}\left(bx\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*x^2*erf(b*x),x)
```

```
[Out] int(exp(b^2*x^2+c)*x^2*erf(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^2*erf(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x^2*erf(b*x)*e^(b^2*x^2 + c), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^2*erf(b*x),x, algorithm="fricas")
[Out] integral(x^2*erf(b*x)*e^(b^2*x^2 + c), x)
```

Sympy [A]
time = 31.76, size = 24, normalized size = 0.32

$$\frac{bx^4e^c{}_2F_2\left(\begin{matrix}1,2\\ \frac{3}{2},3\end{matrix}\middle|b^2x^2\right)}{2\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*x**2*erf(b*x),x)
[Out] b*x**4*exp(c)*hyper((1, 2), (3/2, 3), b**2*x**2)/(2*sqrt(pi))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^2*erf(b*x),x, algorithm="giac")
[Out] integrate(x^2*erf(b*x)*e^(b^2*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^2\,\mathrm{e}^{b^2\,x^2+c}\,\mathrm{erf}(b\,x)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*exp(c + b^2*x^2)*erf(b*x),x)
[Out] int(x^2*exp(c + b^2*x^2)*erf(b*x), x)
```

3.72 $\int e^{c+b^2x^2}\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=29

$$\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{\sqrt{\pi}}$$

```
[Out] b*exp(c)*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.01, antiderivative size = 29, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.062$, Rules used = $\{6511\}$

$$\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*Erf[b*x],x]
```

```
[Out] (b*E^c*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2])/Sqrt[Pi]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rubi steps

$$\int e^{c+b^2x^2}\operatorname{erf}(bx)\,dx = \frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{\sqrt{\pi}}$$

Mathematica [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int e^{c+b^2x^2}\operatorname{Erf}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + b^2*x^2)*Erf[b*x],x]
```

```
[Out] Integrate[E^(c + b^2*x^2)*Erf[b*x], x]
```

Maple [F]
time = 0.07, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{b^2x^2+c}\operatorname{erf}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erf(b*x),x)
[Out] int(exp(b^2*x^2+c)*erf(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x),x, algorithm="maxima")
[Out] integrate(erf(b*x)*e^(b^2*x^2 + c), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x),x, algorithm="fricas")
[Out] integral(erf(b*x)*e^(b^2*x^2 + c), x)
```

Sympy [A]
time = 4.42, size = 22, normalized size = 0.76

$$\frac{bx^2e^c{}_2F_2\left(\begin{matrix}1,1\\ \frac{3}{2},2\end{matrix}\middle|b^2x^2\right)}{\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erf(b*x),x)
[Out] b*x**2*exp(c)*hyper((1, 1), (3/2, 2), b**2*x**2)/sqrt(pi)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x),x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(b^2*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.03

$$\int e^{b^2 x^2+c} \operatorname{erf}(b x) \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c + b^2*x^2)*erf(b*x),x)
```

```
[Out] int(exp(c + b^2*x^2)*erf(b*x), x)
```

3.73 $\int \frac{e^{c+b^2x^2}\mathbf{Erf}(bx)}{x^2}\,dx$

Optimal. Leaf size=66

$$-\frac{e^{c+b^2x^2}\operatorname{Erf}(bx)}{x}+\frac{2b^3e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{\sqrt{\pi}}+\frac{2be^c\log(x)}{\sqrt{\pi}}$$

```
[Out] -exp(b^2*x^2+c)*erf(b*x)/x+2*b^3*exp(c)*x^2*hypergeom([1, 1],[3/2, 2],b^2*x
^2)/Pi^(1/2)+2*b*exp(c)*ln(x)/Pi^(1/2)
```

Rubi [A]
time = 0.04, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {6526, 6511, 12, 29}

$$\frac{2b^3e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{\sqrt{\pi}}-\frac{e^{b^2x^2+c}\operatorname{Erf}(bx)}{x}+\frac{2be^c\log(x)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[(E^(c + b^2*x^2)*Erf[b*x])/x^2,x]
```

```
[Out] -((E^(c + b^2*x^2)*Erf[b*x])/x) + (2*b^3*E^c*x^2*HypergeometricPFQ[{1, 1},
{3/2, 2}, b^2*x^2])/Sqrt[Pi] + (2*b*E^c*Log[x])/Sqrt[Pi]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 29

```
Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6526

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m + 1)*E^(c + d*x^2)*(Erf[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(m
+ 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[2*(b/((m + 1
)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x])
```

```
/; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{x^2}\,dx &= -\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{x}+\left(2b^2\right)\int e^{c+b^2x^2}\operatorname{erf}(bx)\,dx+\frac{(2b)\int \frac{e^c}{x}\,dx}{\sqrt{\pi}}\\ &= -\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{x}+\frac{2b^3e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{\sqrt{\pi}}+\frac{(2be^c)\int \frac{1}{x}\,dx}{\sqrt{\pi}}\\ &= -\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{x}+\frac{2b^3e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{\sqrt{\pi}}+\frac{2be^c\log(x)}{\sqrt{\pi}}\end{aligned}$$

Mathematica [**A**]
time = 0.14, size = 74, normalized size = 1.12

$$\frac{e^c\left(\operatorname{Erf}(bx)\left(-e^{b^2x^2}\sqrt{\pi}+b\pi x\operatorname{Erfi}(bx)\right)-2b^3x^3\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)+2bx\log(x)\right)}{\sqrt{\pi}\,x}$$

Antiderivative was successfully verified.

```
[In] Integrate[(E^(c + b^2*x^2)*Erf[b*x])/x^2,x]
```

```
[Out] (E^c*(Erf[b*x]*(-(E^(b^2*x^2)*Sqrt[Pi]) + b*Pi*x*Erfi[b*x]) - 2*b^3*x^3*Hyp
ergeometricPFQ[{1, 1}, {3/2, 2}, -(b^2*x^2)] + 2*b*x*Log[x]))/(Sqrt[Pi]*x)
```

Maple [**F**]
time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{e^{b^2x^2+c}\operatorname{erf}(bx)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erf(b*x)/x^2,x)
```

```
[Out] int(exp(b^2*x^2+c)*erf(b*x)/x^2,x)
```

Maxima [**F**]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x)/x^2,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)*e^(b^2*x^2 + c)/x^2, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x)/x^2,x, algorithm="fricas")
[Out] integral(erf(b*x)*e^(b^2*x^2 + c)/x^2, x)
```

Sympy [A]
time = 11.33, size = 46, normalized size = 0.70

$$\frac{2b^3x^2e^c{}_2F_2\left(\begin{matrix}1,1\\2,\frac{5}{2}\end{matrix}\middle|b^2x^2\right)}{3\sqrt{\pi}}+\frac{be^c\log\left(b^2x^2\right)}{\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erf(b*x)/x**2,x)
[Out] 2*b**3*x**2*exp(c)*hyper((1, 1), (2, 5/2), b**2*x**2)/(3*sqrt(pi)) + b*exp(
c)*log(b**2*x**2)/sqrt(pi)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x)/x^2,x, algorithm="giac")
[Out] integrate(erf(b*x)*e^(b^2*x^2 + c)/x^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\mathrm{e}^{b^2\,x^2+c}\,\mathrm{erf}\left(b\,x\right)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + b^2*x^2)*erf(b*x))/x^2,x)
[Out] int((exp(c + b^2*x^2)*erf(b*x))/x^2, x)
```

3.74 $\int \frac{e^{c+b^2x^2}\mathbf{Erf}(bx)}{x^4}\,dx$

Optimal. Leaf size=115

$$-\frac{be^c}{3\sqrt{\pi}\,x^2}-\frac{e^{c+b^2x^2}\mathrm{Erf}(bx)}{3x^3}-\frac{2b^2e^{c+b^2x^2}\mathrm{Erf}(bx)}{3x}+\frac{4b^5e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{3\sqrt{\pi}}+\frac{4b^3e^c\log(x)}{3\sqrt{\pi}}$$

```
[Out] -1/3*exp(b^2*x^2+c)*erf(b*x)/x^3-2/3*b^2*exp(b^2*x^2+c)*erf(b*x)/x-1/3*b*ex
p(c)/x^2/Pi^(1/2)+4/3*b^5*exp(c)*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/Pi^
(1/2)+4/3*b^3*exp(c)*ln(x)/Pi^(1/2)
```

Rubi [A]
time = 0.08, antiderivative size = 115, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {6526, 6511, 12, 29, 30}

$$\frac{4b^5e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{3\sqrt{\pi}}+\frac{4b^3e^c\log(x)}{3\sqrt{\pi}}-\frac{2b^2e^{b^2x^2+c}\mathrm{Erf}(bx)}{3x}-\frac{e^{b^2x^2+c}\mathrm{Erf}(bx)}{3x^3}-\frac{be^c}{3\sqrt{\pi}\,x^2}$$

Antiderivative was successfully verified.

```
[In] Int[(E^(c + b^2*x^2)*Erf[b*x])/x^4,x]
```

```
[Out] -1/3*(b*E^c)/(Sqrt[Pi]*x^2) - (E^(c + b^2*x^2)*Erf[b*x])/(3*x^3) - (2*b^2*E
^(c + b^2*x^2)*Erf[b*x])/(3*x) + (4*b^5*E^c*x^2*HypergeometricPFQ[{1, 1}, {
3/2, 2}, b^2*x^2])/(3*Sqrt[Pi]) + (4*b^3*E^c*Log[x])/(3*Sqrt[Pi])
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 29

```
Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6526

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m + 1)*E^(c + d*x^2)*(Erf[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(m
+ 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[2*(b/((m + 1
)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x])
 /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{x^4}\,dx &= -\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{3x^3}+\frac{1}{3}\left(2b^2\right)\int \frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{x^2}\,dx+\frac{(2b)\int \frac{e^c}{x^3}\,dx}{3\sqrt{\pi}}\\ &= -\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{3x^3}-\frac{2b^2e^{c+b^2x^2}\operatorname{erf}(bx)}{3x}+\frac{1}{3}\left(4b^4\right)\int e^{c+b^2x^2}\operatorname{erf}(bx)\,dx+\frac{\left(4b^3\right)\int \frac{e^c}{x}\,dx}{3\sqrt{\pi}}+\\ &= -\frac{be^c}{3\sqrt{\pi}\,x^2}-\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{3x^3}-\frac{2b^2e^{c+b^2x^2}\operatorname{erf}(bx)}{3x}+\frac{4b^5e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{3\sqrt{\pi}}+\frac{\left(4b^3\right.}{}\\ &= -\frac{be^c}{3\sqrt{\pi}\,x^2}-\frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{3x^3}-\frac{2b^2e^{c+b^2x^2}\operatorname{erf}(bx)}{3x}+\frac{4b^5e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{3\sqrt{\pi}}+\frac{4b^3e}{3}\end{aligned}$$

Mathematica [A]
time = 0.24, size = 100, normalized size = 0.87

$$-\frac{e^c\left(bx+e^{b^2x^2}\sqrt{\pi}\left(1+2b^2x^2\right)\operatorname{Erf}(bx)-2b^3\pi x^3\operatorname{Erf}(bx)\operatorname{Erfi}(bx)+4b^5x^5\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)-4b^3x^3\log(x)\right)}{3\sqrt{\pi}\,x^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[(E^(c + b^2*x^2)*Erf[b*x])/x^4,x]
```

```
[Out] -1/3*(E^c*(b*x + E^(b^2*x^2)*Sqrt[Pi]*(1 + 2*b^2*x^2)*Erf[b*x] - 2*b^3*Pi*x
^3*Erf[b*x]*Erfi[b*x] + 4*b^5*x^5*HypergeometricPFQ[{1, 1}, {3/2, 2}, -(b^2
*x^2)] - 4*b^3*x^3*Log[x]))/(Sqrt[Pi]*x^3)
```

Maple [F]
time = 0.17, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{b^2x^2+c}\operatorname{erf}\left(bx\right)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erf(b*x)/x^4,x)
```

```
[Out] int(exp(b^2*x^2+c)*erf(b*x)/x^4,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x)/x^4,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)*e^(b^2*x^2 + c)/x^4, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x)/x^4,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x)*e^(b^2*x^2 + c)/x^4, x)
```

Sympy [C] Result contains complex when optimal does not.
time = 83.06, size = 24, normalized size = 0.21

$$\frac{b^3 G_{3,2}^{1,2}\left(\begin{matrix} 2,1 & \frac{5}{2} \\ 2 & 0 \end{matrix} \middle| \frac{e^{-i\pi}}{b^2x^2}\right)e^c}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erf(b*x)/x**4,x)
```

```
[Out] b**3*meijerg(((2, 1), (5/2,)), ((2,), (0,)), exp_polar(-I*pi)/(b**2*x**2))*
exp(c)/2
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erf(b*x)/x^4,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(b^2*x^2 + c)/x^4, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{b^2\,x^2+c}\,\mathrm{erf}\left(b\,x\right)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + b^2*x^2)*erf(b*x))/x^4,x)
[Out] int((exp(c + b^2*x^2)*erf(b*x))/x^4, x)
```

3.75 $\int e^{-b^2x^2}x^5\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=135

$$-\frac{11e^{-2b^2x^2}x}{16b^5\sqrt{\pi}}-\frac{e^{-2b^2x^2}x^3}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}\mathrm{Erf}(bx)}{b^6}-\frac{e^{-b^2x^2}x^2\mathrm{Erf}(bx)}{b^4}-\frac{e^{-b^2x^2}x^4\mathrm{Erf}(bx)}{2b^2}+\frac{43\mathrm{Erf}\left(\sqrt{2}\,bx\right)}{32\sqrt{2}\,b^6}$$

```
[Out] -erf(b*x)/b^6/exp(b^2*x^2)-x^2*erf(b*x)/b^4/exp(b^2*x^2)-1/2*x^4*erf(b*x)/b
^2/exp(b^2*x^2)+43/64*erf(b*x*2^(1/2))/b^6*2^(1/2)-11/16*x/b^5/exp(2*b^2*x^
2)/Pi^(1/2)-1/4*x^3/b^3/exp(2*b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.14, antiderivative size = 135, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.222, Rules used = {6520, 6517, 2236, 2243}

$$\frac{43\mathrm{Erf}\left(\sqrt{2}\,bx\right)}{32\sqrt{2}\,b^6}-\frac{x^4e^{-b^2x^2}\mathrm{Erf}(bx)}{2b^2}-\frac{e^{-b^2x^2}\mathrm{Erf}(bx)}{b^6}-\frac{11xe^{-2b^2x^2}}{16\sqrt{\pi}\,b^5}-\frac{x^2e^{-b^2x^2}\mathrm{Erf}(bx)}{b^4}-\frac{x^3e^{-2b^2x^2}}{4\sqrt{\pi}\,b^3}$$

Antiderivative was successfully verified.

```
[In] Int[(x^5*Erf[b*x])/E^(b^2*x^2),x]
```

```
[Out] (-11*x)/(16*b^5*E^(2*b^2*x^2)*Sqrt[Pi]) - x^3/(4*b^3*E^(2*b^2*x^2)*Sqrt[Pi]
) - Erf[b*x]/(b^6*E^(b^2*x^2)) - (x^2*Erf[b*x])/(b^4*E^(b^2*x^2)) - (x^4*Er
f[b*x])/(2*b^2*E^(b^2*x^2)) + (43*Erf[Sqrt[2]*b*x])/(32*Sqrt[2]*b^6)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
```

```
 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{-b^2x^2}x^5\text{erf}(bx)\,dx &= -\frac{e^{-b^2x^2}x^4\text{erf}(bx)}{2b^2}+\frac{2\int e^{-b^2x^2}x^3\text{erf}(bx)\,dx}{b^2}+\frac{\int e^{-2b^2x^2}x^4\,dx}{b\sqrt{\pi}}\\ &= -\frac{e^{-2b^2x^2}x^3}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^2\text{erf}(bx)}{b^4}-\frac{e^{-b^2x^2}x^4\text{erf}(bx)}{2b^2}+\frac{2\int e^{-b^2x^2}x\text{erf}(bx)\,dx}{b^4}+\frac{3\int e^{-2b^2}}{4b^3}\\ &= -\frac{11e^{-2b^2x^2}x}{16b^5\sqrt{\pi}}-\frac{e^{-2b^2x^2}x^3}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}\text{erf}(bx)}{b^6}-\frac{e^{-b^2x^2}x^2\text{erf}(bx)}{b^4}-\frac{e^{-b^2x^2}x^4\text{erf}(bx)}{2b^2}+\frac{3}{}\\ &= -\frac{11e^{-2b^2x^2}x}{16b^5\sqrt{\pi}}-\frac{e^{-2b^2x^2}x^3}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}\text{erf}(bx)}{b^6}-\frac{e^{-b^2x^2}x^2\text{erf}(bx)}{b^4}-\frac{e^{-b^2x^2}x^4\text{erf}(bx)}{2b^2}+\frac{43}{}\end{aligned}$$

Mathematica [A]
time = 0.05, size = 86, normalized size = 0.64

$$\frac{-\frac{4be^{-2b^2x^2}x(11+4b^2x^2)}{\sqrt{\pi}}-32e^{-b^2x^2}(2+2b^2x^2+b^4x^4)\,\text{Erf}(bx)+43\sqrt{2}\,\text{Erf}\left(\sqrt{2}\,bx\right)}{64b^6}$$

Antiderivative was successfully verified.

```
[In] Integrate[(x^5*Erf[b*x])/E^(b^2*x^2),x]
```

```
[Out] ((-4*b*x*(11 + 4*b^2*x^2))/(E^(2*b^2*x^2)*Sqrt[Pi]) - (32*(2 + 2*b^2*x^2 +
b^4*x^4)*Erf[b*x])/E^(b^2*x^2) + 43*Sqrt[2]*Erf[Sqrt[2]*b*x])/(64*b^6)
```

Maple [A]
time = 0.33, size = 119, normalized size = 0.88

method	result	size

default	$\frac{\frac{\operatorname{erf}(bx)\left(-\frac{b^4x^4\mathrm{e}^{-b^2x^2}}{2}-b^2x^2\mathrm{e}^{-b^2x^2}-\mathrm{e}^{-b^2x^2}\right)}{b^5}-\frac{-\frac{43\sqrt{2}\,\sqrt{\pi}\,\operatorname{erf}\left(bx\sqrt{2}\right)}{64}+\frac{\mathrm{e}^{-2b^2x^2}b^3x^3}{4}+\frac{11\,\mathrm{e}^{-2b^2x^2}bx}{16}}{\sqrt{\pi}\,b^5}}{b}$	119

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*erf(b*x)/exp(b^2*x^2),x,method=_RETURNVERBOSE)
```

```
[Out] (erf(b*x)/b^5*(-1/2*b^4*x^4/exp(b^2*x^2)-b^2*x^2/exp(b^2*x^2)-1/exp(b^2*x^2
))-1/Pi^(1/2)/b^5*(-43/64*2^(1/2)*Pi^(1/2)*erf(b*x*2^(1/2))+1/4/exp(b^2*x^2
)^2*b^3*x^3+11/16/exp(b^2*x^2)^2*b*x))/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erf(b*x)/exp(b^2*x^2),x, algorithm="maxima")
```

```
[Out] -1/2*(b^4*x^4 + 2*b^2*x^2 + 2)*erf(b*x)*e^(-b^2*x^2)/b^6 + integrate((b^4*x
^4 + 2*b^2*x^2 + 2)*e^(-2*b^2*x^2), x)/(sqrt(pi)*b^5)
```

Fricas [A]
time = 0.33, size = 97, normalized size = 0.72

$$\frac{43\sqrt{2}\,\pi\sqrt{b^2}\,\operatorname{erf}\left(\sqrt{2}\,\sqrt{b^2}\,x\right)-32\left(\pi b^5x^4+2\,\pi b^3x^2+2\,\pi b\right)\operatorname{erf}\left(bx\right)e^{\left(-b^2x^2\right)}-4\,\sqrt{\pi}\,\left(4\,b^4x^3+11\,b^2x\right)e^{\left(-2\,b^2x^2\right)}}{64\,\pi b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erf(b*x)/exp(b^2*x^2),x, algorithm="fricas")
```

```
[Out] 1/64*(43*sqrt(2)*pi*sqrt(b^2)*erf(sqrt(2)*sqrt(b^2)*x) - 32*(pi*b^5*x^4 + 2
*pi*b^3*x^2 + 2*pi*b)*erf(b*x)*e^(-b^2*x^2) - 4*sqrt(pi)*(4*b^4*x^3 + 11*b^
2*x)*e^(-2*b^2*x^2))/(pi*b^7)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x^5e^{-b^2x^2}\operatorname{erf}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**5*erf(b*x)/exp(b**2*x**2),x)
```

```
[Out] Integral(x**5*exp(-b**2*x**2)*erf(b*x), x)
```

Giac [A]
time = 0.41, size = 153, normalized size = 1.13

$$-\frac{\left(b^4x^4+2\,b^2x^2+2\right)\operatorname{erf}\left(bx\right)e^{\left(-b^2x^2\right)}}{2\,b^6}-\frac{b^4\left(\frac{4\,\left(4\,b^2x^3+3\,x\right)e^{\left(-2\,b^2x^2\right)}}{b^4}+\frac{3\,\sqrt{2}\,\sqrt{\pi}\,\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{b^5}\right)+8\,b^2\left(\frac{4\,xe^{\left(-2\,b^2x^2\right)}}{b^2}+\frac{\sqrt{2}\,\sqrt{\pi}\,\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{b^3}\right)+\frac{32\,\sqrt{2}\,\sqrt{\pi}\,\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{b}}{64\,\sqrt{\pi}\,b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erf(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] -1/2*(b^4*x^4 + 2*b^2*x^2 + 2)*erf(b*x)*e^(-b^2*x^2)/b^6 - 1/64*(b^4*(4*(4*
b^2*x^3 + 3*x)*e^(-2*b^2*x^2)/b^4 + 3*sqrt(2)*sqrt(pi)*erf(-sqrt(2)*b*x)/b^
5) + 8*b^2*(4*x*e^(-2*b^2*x^2)/b^2 + sqrt(2)*sqrt(pi)*erf(-sqrt(2)*b*x)/b^3
) + 32*sqrt(2)*sqrt(pi)*erf(-sqrt(2)*b*x)/b)/(sqrt(pi)*b^5)
```

Mupad [B]
time = 0.45, size = 192, normalized size = 1.42

$$\frac{\sqrt{2}\,\operatorname{erf}\left(\sqrt{2}\,x\,\sqrt{b^2}\right)}{2\,b\,{\left(b^2\right)}^{5/2}}-\frac{\operatorname{erfi}\left(x\,\sqrt{-2\,b^2}\right)}{2\,b^3\,{\left(-2\,b^2\right)}^{3/2}}-\frac{x^3\,{\mathrm{e}}^{-2\,b^2\,x^2}}{4\,b^3\,\sqrt{\pi}}-\operatorname{erf}(b\,x)\,\left(\frac{{\mathrm{e}}^{-b^2\,x^2}}{b^6}+\frac{x^4\,{\mathrm{e}}^{-b^2\,x^2}}{2\,b^2}+\frac{x^2\,{\mathrm{e}}^{-b^2\,x^2}}{b^4}\right)-\frac{11\,x\,{\mathrm{e}}^{-2\,b^2\,x^2}}{16\,b^5\,\sqrt{\pi}}+\frac{3\,\sqrt{2}\,x^5}{64\,b\,{\left(b^2\,x^2\right)}^{5/2}}-\frac{3\,\sqrt{2}\,x^5\,\operatorname{erfc}\left(\sqrt{2\,b^2\,x^2}\right)}{64\,b\,{\left(b^2\,x^2\right)}^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*exp(-b^2*x^2)*erf(b*x),x)
```

```
[Out] (2^(1/2)*erf(2^(1/2)*x*(b^2)^(1/2)))/(2*b*(b^2)^(5/2)) - erfi(x*(-2*b^2)^(1
/2))/(2*b^3*(-2*b^2)^(3/2)) - (x^3*exp(-2*b^2*x^2))/(4*b^3*pi^(1/2)) - erf(
b*x)*(exp(-b^2*x^2)/b^6 + (x^4*exp(-b^2*x^2))/(2*b^2) + (x^2*exp(-b^2*x^2))
/b^4) - (11*x*exp(-2*b^2*x^2))/(16*b^5*pi^(1/2)) + (3*2^(1/2)*x^5)/(64*b*(b
^2*x^2)^(5/2)) - (3*2^(1/2)*x^5*erfc((2*b^2*x^2)^(1/2)))/(64*b*(b^2*x^2)^(5
/2))
```

3.76 $\int e^{-b^2x^2}x^3\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=90

$$-\frac{e^{-2b^2x^2}x}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}\mathrm{Erf}(bx)}{2b^4}-\frac{e^{-b^2x^2}x^2\mathrm{Erf}(bx)}{2b^2}+\frac{5\mathrm{Erf}\left(\sqrt{2}\,bx\right)}{8\sqrt{2}\,b^4}$$

```
[Out] -1/2*erf(b*x)/b^4/exp(b^2*x^2)-1/2*x^2*erf(b*x)/b^2/exp(b^2*x^2)+5/16*erf(b
*x*2^(1/2))/b^4*2^(1/2)-1/4*x/b^3/exp(2*b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.08, antiderivative size = 90, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}}=0.222$, Rules used = {6520, 6517, 2236, 2243}

$$\frac{5\mathrm{Erf}\left(\sqrt{2}\,bx\right)}{8\sqrt{2}\,b^4}-\frac{x^2e^{-b^2x^2}\mathrm{Erf}(bx)}{2b^2}-\frac{e^{-b^2x^2}\mathrm{Erf}(bx)}{2b^4}-\frac{xe^{-2b^2x^2}}{4\sqrt{\pi}\,b^3}$$

Antiderivative was successfully verified.

```
[In] Int[(x^3*Erf[b*x])/E^(b^2*x^2),x]
```

```
[Out] -1/4*x/(b^3*E^(2*b^2*x^2)*Sqrt[Pi]) - Erf[b*x]/(2*b^4*E^(b^2*x^2)) - (x^2*E
rf[b*x])/(2*b^2*E^(b^2*x^2)) + (5*Erf[Sqrt[2]*b*x])/(8*Sqrt[2]*b^4)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{-b^2x^2}x^3\operatorname{erf}(bx)\,dx &= -\frac{e^{-b^2x^2}x^2\operatorname{erf}(bx)}{2b^2}+\frac{\int e^{-b^2x^2}x\operatorname{erf}(bx)\,dx}{b^2}+\frac{\int e^{-2b^2x^2}x^2\,dx}{b\sqrt{\pi}}\\ &= -\frac{e^{-2b^2x^2}x}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}\operatorname{erf}(bx)}{2b^4}-\frac{e^{-b^2x^2}x^2\operatorname{erf}(bx)}{2b^2}+\frac{\int e^{-2b^2x^2}\,dx}{4b^3\sqrt{\pi}}+\frac{\int e^{-2b^2x^2}\,dx}{b^3\sqrt{\pi}}\\ &= -\frac{e^{-2b^2x^2}x}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}\operatorname{erf}(bx)}{2b^4}-\frac{e^{-b^2x^2}x^2\operatorname{erf}(bx)}{2b^2}+\frac{5\operatorname{erf}\left(\sqrt{2}\,bx\right)}{8\sqrt{2}\,b^4}\end{aligned}$$

Mathematica [A]
time = 0.03, size = 68, normalized size = 0.76

$$\frac{-\frac{4be^{-2b^2x^2}x}{\sqrt{\pi}}-8e^{-b^2x^2}(1+b^2x^2)\operatorname{Erf}(bx)+5\sqrt{2}\operatorname{Erf}\left(\sqrt{2}\,bx\right)}{16b^4}$$

Antiderivative was successfully verified.

```
[In] Integrate[(x^3*Erf[b*x])/E^(b^2*x^2),x]
[Out] ((-4*b*x)/(E^(2*b^2*x^2)*Sqrt[Pi]) - (8*(1 + b^2*x^2)*Erf[b*x])/E^(b^2*x^2)
 + 5*Sqrt[2]*Erf[Sqrt[2]*b*x])/(16*b^4)
```

Maple [A]
time = 0.58, size = 83, normalized size = 0.92

method	result	size
default	$\frac{\frac{\operatorname{erf}(bx)\left(-\frac{b^2x^2e^{-b^2x^2}}{2}-\frac{e^{-b^2x^2}}{2}\right)}{b^3}-\frac{-\frac{5\sqrt{2}\,\sqrt{\pi}\,\operatorname{erf}\left(bx\sqrt{2}\right)}{16}+\frac{e^{-2b^2x^2}bx}{4}}{\sqrt{\pi}\,b^3}}{b}$	83

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erf(b*x)/exp(b^2*x^2),x,method=_RETURNVERBOSE)
```

```
[Out] (erf(b*x)/b^3*(-1/2*b^2*x^2/exp(b^2*x^2)-1/2/exp(b^2*x^2))-1/Pi^(1/2)/b^3*(
-5/16*2^(1/2)*Pi^(1/2)*erf(b*x*2^(1/2))+1/4/exp(b^2*x^2)^2*b*x))/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erf(b*x)/exp(b^2*x^2),x, algorithm="maxima")
```

```
[Out] -1/2*(b^2*x^2 + 1)*erf(b*x)*e^(-b^2*x^2)/b^4 + integrate((b^2*x^2 + 1)*e^(-
2*b^2*x^2), x)/(sqrt(pi)*b^3)
```

Fricas [A]
time = 0.36, size = 76, normalized size = 0.84

$$-\frac{4\sqrt{\pi}\,b^2xe^{\left(-2\,b^2x^2\right)}-5\sqrt{2}\,\pi\sqrt{b^2}\,\operatorname{erf}\left(\sqrt{2}\,\sqrt{b^2}\,x\right)+8\left(\pi b^3x^2+\pi b\right)\operatorname{erf}\left(bx\right)e^{\left(-b^2x^2\right)}}{16\,\pi b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erf(b*x)/exp(b^2*x^2),x, algorithm="fricas")
```

```
[Out] -1/16*(4*sqrt(pi)*b^2*x*e^(-2*b^2*x^2) - 5*sqrt(2)*pi*sqrt(b^2)*erf(sqrt(2)
*sqrt(b^2)*x) + 8*(pi*b^3*x^2 + pi*b)*erf(b*x)*e^(-b^2*x^2))/(pi*b^5)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x^3e^{-b^2x^2}\operatorname{erf}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3*erf(b*x)/exp(b**2*x**2),x)
```

```
[Out] Integral(x**3*exp(-b**2*x**2)*erf(b*x), x)
```

Giac [A]
time = 0.42, size = 94, normalized size = 1.04

$$-\frac{\left(b^2x^2+1\right)\operatorname{erf}\left(bx\right)e^{\left(-b^2x^2\right)}}{2\,b^4}-\frac{b^2\left(\frac{4\,xe^{\left(-2\,b^2x^2\right)}}{b^2}+\frac{\sqrt{2}\,\sqrt{\pi}\,\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{b^3}\right)+\frac{4\,\sqrt{2}\,\sqrt{\pi}\,\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{b}}{16\,\sqrt{\pi}\,b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erf(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] -1/2*(b^2*x^2 + 1)*erf(b*x)*e^(-b^2*x^2)/b^4 - 1/16*(b^2*(4*x*e^(-2*b^2*x^2
)/b^2 + sqrt(2)*sqrt(pi)*erf(-sqrt(2)*b*x)/b^3) + 4*sqrt(2)*sqrt(pi)*erf(-s
qrt(2)*b*x)/b)/(sqrt(pi)*b^3)
```

Mupad [B]
time = 0.45, size = 106, normalized size = 1.18

$$\frac{\sqrt{2}\,\operatorname{erf}\left(\sqrt{2}\,x\,\sqrt{b^2}\right)}{4\,b\,{\left(b^2\right)}^{3/2}}-\frac{\operatorname{erfi}\left(\sqrt{2}\,x\,\sqrt{-b^2}\right)}{4\,b\,{\left(-2\,b^2\right)}^{3/2}}-\operatorname{erf}(b\,x)\,\left(\frac{{\mathrm{e}}^{-b^2\,x^2}}{2\,b^4}+\frac{x^2\,{\mathrm{e}}^{-b^2\,x^2}}{2\,b^2}\right)-\frac{x\,{\mathrm{e}}^{-2\,b^2\,x^2}}{4\,b^3\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*exp(-b^2*x^2)*erf(b*x),x)
```

```
[Out] (2^(1/2)*erf(2^(1/2)*x*(b^2)^(1/2)))/(4*b*(b^2)^(3/2)) - erfi(2^(1/2)*x*(-b
^2)^(1/2))/(4*b*(-2*b^2)^(3/2)) - erf(b*x)*(exp(-b^2*x^2)/(2*b^4) + (x^2*ex
p(-b^2*x^2))/(2*b^2)) - (x*exp(-2*b^2*x^2))/(4*b^3*pi^(1/2))
```

3.77 $\int e^{-b^2x^2}x\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=43

$$-\frac{e^{-b^2x^2}\operatorname{Erf}(bx)}{2b^2}+\frac{\operatorname{Erf}\left(\sqrt{2}\,bx\right)}{2\sqrt{2}\,b^2}$$

```
[Out] -1/2*erf(b*x)/b^2/exp(b^2*x^2)+1/4*erf(b*x*2^(1/2))/b^2*2^(1/2)
```

Rubi [A]
time = 0.02, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}}=0.125$, Rules used = {6517, 2236}

$$\frac{\operatorname{Erf}\left(\sqrt{2}\,bx\right)}{2\sqrt{2}\,b^2}-\frac{e^{-b^2x^2}\operatorname{Erf}(bx)}{2b^2}$$

Antiderivative was successfully verified.

```
[In] Int[(x*Erf[b*x])/E^(b^2*x^2),x]
```

```
[Out] -1/2*Erf[b*x]/(b^2*E^(b^2*x^2)) + Erf[Sqrt[2]*b*x]/(2*Sqrt[2]*b^2)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\begin{aligned}\int e^{-b^2x^2}x\operatorname{erf}(bx)\,dx&=-\frac{e^{-b^2x^2}\operatorname{erf}(bx)}{2b^2}+\frac{\int e^{-2b^2x^2}\,dx}{b\sqrt{\pi}}\\&=-\frac{e^{-b^2x^2}\operatorname{erf}(bx)}{2b^2}+\frac{\operatorname{erf}\left(\sqrt{2}\,bx\right)}{2\sqrt{2}\,b^2}\end{aligned}$$

Mathematica [**A**]
time = 0.01, size = 39, normalized size = 0.91

$$\frac{-2e^{-b^2x^2}\operatorname{Erf}(bx)+\sqrt{2}\operatorname{Erf}\left(\sqrt{2}\,bx\right)}{4b^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[(x*Erf[b*x])/E^(b^2*x^2),x]
[Out] ((-2*Erf[b*x])/E^(b^2*x^2) + Sqrt[2]*Erf[Sqrt[2]*b*x])/(4*b^2)
```

Maple [**A**]
time = 0.32, size = 39, normalized size = 0.91

method	result	size
default	$\frac{-\frac{\operatorname{erf}(bx)\mathrm{e}^{-b^2x^2}}{2b}+\frac{\sqrt{2}\,\operatorname{erf}\left(bx\sqrt{2}\right)}{4b}}{b}$	39

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erf(b*x)/exp(b^2*x^2),x,method=_RETURNVERBOSE)
[Out] (-1/2*erf(b*x)/b*exp(-b^2*x^2)+1/4/b*2^(1/2)*erf(b*x*2^(1/2)))/b
```

Maxima [**A**]
time = 0.46, size = 34, normalized size = 0.79

$$-\frac{\operatorname{erf}\left(bx\right)e^{\left(-b^2x^2\right)}}{2\,b^2}+\frac{\sqrt{2}\,\operatorname{erf}\left(\sqrt{2}\,bx\right)}{4\,b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(b*x)/exp(b^2*x^2),x, algorithm="maxima")
[Out] -1/2*erf(b*x)*e^(-b^2*x^2)/b^2 + 1/4*sqrt(2)*erf(sqrt(2)*b*x)/b^2
```

Fricas [**A**]
time = 0.38, size = 43, normalized size = 1.00

$$-\frac{2\,b\operatorname{erf}\left(bx\right)e^{\left(-b^2x^2\right)}-\sqrt{2}\,\sqrt{b^2}\,\operatorname{erf}\left(\sqrt{2}\,\sqrt{b^2}\,x\right)}{4\,b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(b*x)/exp(b^2*x^2),x, algorithm="fricas")
[Out] -1/4*(2*b*erf(b*x)*e^(-b^2*x^2) - sqrt(2)*sqrt(b^2)*erf(sqrt(2)*sqrt(b^2)*x
))/b^3
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int xe^{-b^2x^2}\operatorname{erf}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(b*x)/exp(b**2*x**2),x)
```

```
[Out] Integral(x*exp(-b**2*x**2)*erf(b*x), x)
```

Giac [A]
time = 0.40, size = 35, normalized size = 0.81

$$-\frac{\operatorname{erf}(bx)\,e^{\left(-b^2x^2\right)}}{2\,b^2}-\frac{\sqrt{2}\,\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{4\,b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erf(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] -1/2*erf(b*x)*e^(-b^2*x^2)/b^2 - 1/4*sqrt(2)*erf(-sqrt(2)*b*x)/b^2
```

Mupad [B]
time = 0.18, size = 43, normalized size = 1.00

$$\frac{\sqrt{2}\,\operatorname{erf}\left(\sqrt{2}\,x\,\sqrt{b^2}\right)}{4\,b\,\sqrt{b^2}}-\frac{\mathrm{e}^{-b^2\,x^2}\,\operatorname{erf}(b\,x)}{2\,b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*exp(-b^2*x^2)*erf(b*x),x)
```

```
[Out] (2^(1/2)*erf(2^(1/2)*x*(b^2)^(1/2)))/(4*b*(b^2)^(1/2)) - (exp(-b^2*x^2)*erf
(b*x))/(2*b^2)
```

3.78 $\int \frac{e^{-b^2x^2}\mathbf{Erf}(bx)}{x}\,dx$

Optimal. Leaf size=21

$$\mathrm{Int}\left(\frac{e^{-b^2x^2}\mathrm{Erf}(bx)}{x},x\right)$$

```
[Out] Unintegrable(erf(b*x)/exp(b^2*x^2)/x,x)
```

Rubi [A]
time = 0.02, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{-b^2x^2}\mathrm{Erf}(bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erf[b*x]/(E^(b^2*x^2)*x),x]
[Out] Defer[Int][Erf[b*x]/(E^(b^2*x^2)*x), x]
```

Rubi steps

$$\int \frac{e^{-b^2x^2}\mathrm{erf}(bx)}{x}\,dx = \int \frac{e^{-b^2x^2}\mathrm{erf}(bx)}{x}\,dx$$

Mathematica [A]
time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{e^{-b^2x^2}\mathrm{Erf}(bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erf[b*x]/(E^(b^2*x^2)*x),x]
[Out] Integrate[Erf[b*x]/(E^(b^2*x^2)*x), x]
```

Maple [A]
time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{erf}\left(bx\right)\mathrm{e}^{-b^2x^2}}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/exp(b^2*x^2)/x,x)
```

```
[Out] int(erf(b*x)/exp(b^2*x^2)/x,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)*e^(-b^2*x^2)/x, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x)*e^(-b^2*x^2)/x, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b**2*x**2)/x,x)
```

```
[Out] Integral(exp(-b**2*x**2)*erf(b*x)/x, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(-b^2*x^2)/x, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{\mathrm{e}^{-b^2\,x^2}\,\mathrm{erf}(b\,x)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erf(b*x))/x,x)
```

```
[Out] int((exp(-b^2*x^2)*erf(b*x))/x, x)
```

3.79 $\int \frac{e^{-b^2x^2}\mathbf{Erf}(bx)}{x^3}\,dx$

Optimal. Leaf size=88

$$-\frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\text{Erf}(bx)}{2x^2}-\sqrt{2}\,b^2\text{Erf}\left(\sqrt{2}\,bx\right)-b^2\text{Int}\left(\frac{e^{-b^2x^2}\text{Erf}(bx)}{x},x\right)$$

```
[Out] -1/2*erf(b*x)/exp(b^2*x^2)/x^2-b^2*erf(b*x*2^(1/2))*2^(1/2)-b/exp(2*b^2*x^2
)/x/Pi^(1/2)-b^2*Unintegrable(erf(b*x)/exp(b^2*x^2)/x,x)
```

Rubi [A]
time = 0.06, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}}=0.000$, Rules used = {}

$$\int \frac{e^{-b^2x^2}\text{Erf}(bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erf[b*x]/(E^(b^2*x^2)*x^3),x]
```

```
[Out] -(b/(E^(2*b^2*x^2)*Sqrt[Pi]*x)) - Erf[b*x]/(2*E^(b^2*x^2)*x^2) - Sqrt[2]*b^
2*Erf[Sqrt[2]*b*x] - b^2*Defer[Int][Erf[b*x]/(E^(b^2*x^2)*x), x]
```

Rubi steps

$$\begin{aligned}
\int \frac{e^{-b^2x^2}\text{erf}(bx)}{x^3}\,dx &= -\frac{e^{-b^2x^2}\text{erf}(bx)}{2x^2}-b^2\int \frac{e^{-b^2x^2}\text{erf}(bx)}{x}\,dx+\frac{b\int \frac{e^{-2b^2x^2}}{x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\text{erf}(bx)}{2x^2}-b^2\int \frac{e^{-b^2x^2}\text{erf}(bx)}{x}\,dx-\frac{(4b^3)\int e^{-2b^2x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\text{erf}(bx)}{2x^2}-\sqrt{2}\,b^2\text{erf}\left(\sqrt{2}\,bx\right)-b^2\int \frac{e^{-b^2x^2}\text{erf}(bx)}{x}\,dx
\end{aligned}$$

Mathematica [A]
time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{e^{-b^2x^2}\text{Erf}(bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erf[b*x]/(E^(b^2*x^2)*x^3),x]
```

```
[Out] Integrate[Erf[b*x]/(E^(b^2*x^2)*x^3), x]
```

Maple [A]
time = 0.14, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}\left(bx\right) \mathrm{e}^{-b^{2} x^{2}}}{x^{3}}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/exp(b^2*x^2)/x^3,x)
```

```
[Out] int(erf(b*x)/exp(b^2*x^2)/x^3,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x^3,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)*e^(-b^2*x^2)/x^3, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x^3,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x)*e^(-b^2*x^2)/x^3, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{e^{- b^{2} x^{2}} \operatorname{erf}{\left(bx \right)}}{x^{3}}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b**2*x**2)/x**3,x)
```

```
[Out] Integral(exp(-b**2*x**2)*erf(b*x)/x**3, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x^3,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(-b^2*x^2)/x^3, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{-b^2\,x^2}\,\mathrm{erf}(b\,x)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erf(b*x))/x^3,x)
```

```
[Out] int((exp(-b^2*x^2)*erf(b*x))/x^3, x)
```

3.80 $\int \frac{e^{-b^2x^2}\textbf{Erf}(bx)}{x^5}\,dx$

Optimal. Leaf size=161

$$-\frac{be^{-2b^2x^2}}{6\sqrt{\pi}\,x^3}+\frac{7b^3e^{-2b^2x^2}}{6\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\text{Erf}(bx)}{4x^4}+\frac{b^2e^{-b^2x^2}\text{Erf}(bx)}{4x^2}+\frac{b^4\text{Erf}\left(\sqrt{2}\,bx\right)}{\sqrt{2}}+\frac{2}{3}\sqrt{2}\,b^4\text{Erf}\left(\sqrt{2}\,bx\right)+\frac{1}{2}b^4\text{Int}\left(\frac{e^{-}}{}\right.$$

```
[Out] -1/4*erf(b*x)/exp(b^2*x^2)/x^4+1/4*b^2*erf(b*x)/exp(b^2*x^2)/x^2+7/6*b^4*er
f(b*x*2^(1/2))*2^(1/2)-1/6*b/exp(2*b^2*x^2)/x^3/Pi^(1/2)+7/6*b^3/exp(2*b^2*
x^2)/x/Pi^(1/2)+1/2*b^4*Unintegrable(erf(b*x)/exp(b^2*x^2)/x,x)
```

Rubi [A]
time = 0.13, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{-b^2x^2}\text{Erf}(bx)}{x^5}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erf[b*x]/(E^(b^2*x^2)*x^5),x]
```

```
[Out] -1/6*b/(E^(2*b^2*x^2)*Sqrt[Pi]*x^3) + (7*b^3)/(6*E^(2*b^2*x^2)*Sqrt[Pi]*x)
- Erf[b*x]/(4*E^(b^2*x^2)*x^4) + (b^2*Erf[b*x])/(4*E^(b^2*x^2)*x^2) + (b^4*
Erf[Sqrt[2]*b*x])/Sqrt[2] + (2*Sqrt[2]*b^4*Erf[Sqrt[2]*b*x])/3 + (b^4*Defer
[Int][Erf[b*x]/(E^(b^2*x^2)*x), x])/2
```

Rubi steps

$$\begin{aligned}
\int \frac{e^{-b^2x^2}\text{erf}(bx)}{x^5}\,dx &= -\frac{e^{-b^2x^2}\text{erf}(bx)}{4x^4}-\frac{1}{2}b^2\int \frac{e^{-b^2x^2}\text{erf}(bx)}{x^3}\,dx+\frac{b\int \frac{e^{-2b^2x^2}}{x^4}\,dx}{2\sqrt{\pi}}\\
&= -\frac{be^{-2b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{e^{-b^2x^2}\text{erf}(bx)}{4x^4}+\frac{b^2e^{-b^2x^2}\text{erf}(bx)}{4x^2}+\frac{1}{2}b^4\int \frac{e^{-b^2x^2}\text{erf}(bx)}{x}\,dx-\frac{b^3\int \frac{e^{-2b^2x^2}}{x^2}\,d}{2\sqrt{\pi}}\\
&= -\frac{be^{-2b^2x^2}}{6\sqrt{\pi}\,x^3}+\frac{7b^3e^{-2b^2x^2}}{6\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\text{erf}(bx)}{4x^4}+\frac{b^2e^{-b^2x^2}\text{erf}(bx)}{4x^2}+\frac{1}{2}b^4\int \frac{e^{-b^2x^2}\text{erf}(bx)}{x}\,dx+\\
&= -\frac{be^{-2b^2x^2}}{6\sqrt{\pi}\,x^3}+\frac{7b^3e^{-2b^2x^2}}{6\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\text{erf}(bx)}{4x^4}+\frac{b^2e^{-b^2x^2}\text{erf}(bx)}{4x^2}+\frac{b^4\text{erf}\left(\sqrt{2}\,bx\right)}{\sqrt{2}}+\frac{2}{3}\sqrt{2}\,b
\end{aligned}$$

Mathematica [A]
time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{e^{-b^2x^2}\text{Erf}(bx)}{x^5}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erf[b*x]/(E^(b^2*x^2)*x^5),x]
```

```
[Out] Integrate[Erf[b*x]/(E^(b^2*x^2)*x^5), x]
```

Maple [A]
time = 0.16, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}(bx)\, \mathrm{e}^{-b^2x^2}}{x^5}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/exp(b^2*x^2)/x^5,x)
```

```
[Out] int(erf(b*x)/exp(b^2*x^2)/x^5,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x^5,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)*e^(-b^2*x^2)/x^5, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x^5,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x)*e^(-b^2*x^2)/x^5, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{e^{-b^2x^2} \operatorname{erf}(bx)}{x^5}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b**2*x**2)/x**5,x)
```

```
[Out] Integral(exp(-b**2*x**2)*erf(b*x)/x**5, x)
```

Giac [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x^5,x, algorithm="giac")
[Out] integrate(erf(b*x)*e^(-b^2*x^2)/x^5, x)
```

Mupad [**A**]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{e^{-b^2 x^2} \operatorname{erf}(b x)}{x^5} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erf(b*x))/x^5,x)
[Out] int((exp(-b^2*x^2)*erf(b*x))/x^5, x)
```

3.81 $\int e^{-b^2x^2}x^4\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=112

$$-\frac{e^{-2b^2x^2}}{2b^5\sqrt{\pi}}-\frac{e^{-2b^2x^2}x^2}{4b^3\sqrt{\pi}}-\frac{3e^{-b^2x^2}x\mathrm{Erf}(bx)}{4b^4}-\frac{e^{-b^2x^2}x^3\mathrm{Erf}(bx)}{2b^2}+\frac{3\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{16b^5}$$

```
[Out] -3/4*x*erf(b*x)/b^4/exp(b^2*x^2)-1/2*x^3*erf(b*x)/b^2/exp(b^2*x^2)-1/2/b^5/
exp(2*b^2*x^2)/Pi^(1/2)-1/4*x^2/b^3/exp(2*b^2*x^2)/Pi^(1/2)+3/16*erf(b*x)^2
*Pi^(1/2)/b^5
```

Rubi [A]
time = 0.09, antiderivative size = 112, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}}=0.278$, Rules used = {6520, 6508, 30, 2240, 2243}

$$\frac{3\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{16b^5}-\frac{x^3e^{-b^2x^2}\mathrm{Erf}(bx)}{2b^2}-\frac{e^{-2b^2x^2}}{2\sqrt{\pi}\,b^5}-\frac{3xe^{-b^2x^2}\mathrm{Erf}(bx)}{4b^4}-\frac{x^2e^{-2b^2x^2}}{4\sqrt{\pi}\,b^3}$$

Antiderivative was successfully verified.

```
[In] Int[(x^4*Erf[b*x])/E^(b^2*x^2),x]
```

```
[Out] -1/2*1/(b^5*E^(2*b^2*x^2)*Sqrt[Pi]) - x^2/(4*b^3*E^(2*b^2*x^2)*Sqrt[Pi]) -
(3*x*Erf[b*x])/(4*b^4*E^(b^2*x^2)) - (x^3*Erf[b*x])/(2*b^2*E^(b^2*x^2)) + (
3*Sqrt[Pi]*Erf[b*x]^2)/(16*b^5)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{-b^2x^2}x^4\text{erf}(bx)\,dx &= -\frac{e^{-b^2x^2}x^3\text{erf}(bx)}{2b^2}+\frac{3\int e^{-b^2x^2}x^2\text{erf}(bx)\,dx}{2b^2}+\frac{\int e^{-2b^2x^2}x^3\,dx}{b\sqrt{\pi}}\\ &= -\frac{e^{-2b^2x^2}x^2}{4b^3\sqrt{\pi}}-\frac{3e^{-b^2x^2}x\text{erf}(bx)}{4b^4}-\frac{e^{-b^2x^2}x^3\text{erf}(bx)}{2b^2}+\frac{3\int e^{-b^2x^2}\text{erf}(bx)\,dx}{4b^4}+\frac{\int e^{-2b^2x^2}}{2b^3\sqrt{\pi}}\\ &= -\frac{e^{-2b^2x^2}}{2b^5\sqrt{\pi}}-\frac{e^{-2b^2x^2}x^2}{4b^3\sqrt{\pi}}-\frac{3e^{-b^2x^2}x\text{erf}(bx)}{4b^4}-\frac{e^{-b^2x^2}x^3\text{erf}(bx)}{2b^2}+\frac{(3\sqrt{\pi})\,\text{Subst}(\int x\,dx}{8b^5}\\ &= -\frac{e^{-2b^2x^2}}{2b^5\sqrt{\pi}}-\frac{e^{-2b^2x^2}x^2}{4b^3\sqrt{\pi}}-\frac{3e^{-b^2x^2}x\text{erf}(bx)}{4b^4}-\frac{e^{-b^2x^2}x^3\text{erf}(bx)}{2b^2}+\frac{3\sqrt{\pi}\,\text{erf}(bx)^2}{16b^5}\end{aligned}$$

Mathematica [A]
time = 0.02, size = 85, normalized size = 0.76

$$\frac{e^{-2b^2x^2}\left(-4(2+b^2x^2)-4be^{b^2x^2}\sqrt{\pi}\,x(3+2b^2x^2)\,\text{Erf}(bx)+3e^{2b^2x^2}\pi\text{Erf}(bx)^2\right)}{16b^5\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(x^4*Erf[b*x])/E^(b^2*x^2),x]
[Out] (-4*(2 + b^2*x^2) - 4*b*E^(b^2*x^2)*Sqrt[Pi]*x*(3 + 2*b^2*x^2)*Erf[b*x] + 3
*E^(2*b^2*x^2)*Pi*Erf[b*x]^2)/(16*b^5*E^(2*b^2*x^2)*Sqrt[Pi])
```

Maple [F]
time = 0.12, size = 0, normalized size = 0.00

$$\int x^4\,\text{erf}\,(bx)\,\mathrm{e}^{-b^2x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erf(b*x)/exp(b^2*x^2),x)
```

```
[Out] int(x^4*erf(b*x)/exp(b^2*x^2),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erf(b*x)/exp(b^2*x^2),x, algorithm="maxima")
```

```
[Out] 1/2*integrate((2*b^2*x^3 + 3*x)*e^(-2*b^2*x^2), x)/(sqrt(pi)*b^3) - 1/16*(4
*(2*b^3*x^3 + 3*b*x)*erf(b*x)*e^(-b^2*x^2) - 3*sqrt(pi)*erf(b*x)^2)/b^5
```

Fricas [A]
time = 0.38, size = 74, normalized size = 0.66

$$-\frac{4\,(2\,\pi b^3x^3+3\,\pi bx)\,\mathrm{erf}\,(bx)\,e^{\left(-b^2x^2\right)}-\sqrt{\pi}\,\left(3\,\pi\,\mathrm{erf}\,(bx)^2-4\,(b^2x^2+2)e^{\left(-2\,b^2x^2\right)}\right)}{16\,\pi b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erf(b*x)/exp(b^2*x^2),x, algorithm="fricas")
```

```
[Out] -1/16*(4*(2*pi*b^3*x^3 + 3*pi*b*x)*erf(b*x)*e^(-b^2*x^2) - sqrt(pi)*(3*pi*e
rf(b*x)^2 - 4*(b^2*x^2 + 2)*e^(-2*b^2*x^2)))/(pi*b^5)
```

Sympy [A]
time = 6.30, size = 109, normalized size = 0.97

$$\begin{cases} -\frac{x^3e^{-b^2x^2}\,\mathrm{erf}\,(bx)}{2b^2}-\frac{x^2e^{-2b^2x^2}}{4\sqrt{\pi}\,b^3}-\frac{3xe^{-b^2x^2}\,\mathrm{erf}\,(bx)}{4b^4}+\frac{3\sqrt{\pi}\,\mathrm{erf}^2\,(bx)}{16b^5}-\frac{e^{-2b^2x^2}}{2\sqrt{\pi}\,b^5} & \text{for } b\neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4*erf(b*x)/exp(b**2*x**2),x)
```

```
[Out] Piecewise((-x**3*exp(-b**2*x**2)*erf(b*x)/(2*b**2) - x**2*exp(-2*b**2*x**2)
/(4*sqrt(pi)*b**3) - 3*x*exp(-b**2*x**2)*erf(b*x)/(4*b**4) + 3*sqrt(pi)*erf
(b*x)**2/(16*b**5) - exp(-2*b**2*x**2)/(2*sqrt(pi)*b**5), Ne(b, 0)), (0, Tr
ue))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erf(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(x^4*erf(b*x)*e^(-b^2*x^2), x)
```

Mupad [B]
time = 0.75, size = 90, normalized size = 0.80

$$-\frac{8\,\mathrm{e}^{-2\,b^2\,x^2}-3\,\pi\,\mathrm{erf}\left(b\,x\right)^2}{16\,b^5\,\sqrt{\pi}}-\frac{x^2\,\mathrm{e}^{-2\,b^2\,x^2}}{4\,b^3\,\sqrt{\pi}}-\frac{3\,x\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erf}\left(b\,x\right)}{4\,b^4}-\frac{x^3\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erf}\left(b\,x\right)}{2\,b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*exp(-b^2*x^2)*erf(b*x),x)
```

```
[Out] - (8*exp(-2*b^2*x^2) - 3*pi*erf(b*x)^2)/(16*b^5*pi^(1/2)) - (x^2*exp(-2*b^2
*x^2))/(4*b^3*pi^(1/2)) - (3*x*exp(-b^2*x^2)*erf(b*x))/(4*b^4) - (x^3*exp(-
b^2*x^2)*erf(b*x))/(2*b^2)
```

3.82 $\int e^{-b^2x^2}x^2\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=63

$$-\frac{e^{-2b^2x^2}}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x\mathrm{Erf}(bx)}{2b^2}+\frac{\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{8b^3}$$

```
[Out] -1/2*x*erf(b*x)/b^2/exp(b^2*x^2)-1/4/b^3/exp(2*b^2*x^2)/Pi^(1/2)+1/8*erf(b*
x)^2*Pi^(1/2)/b^3
```

Rubi [A]
time = 0.05, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.222, Rules used = {6520, 6508, 30, 2240}

$$\frac{\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{8b^3}-\frac{xe^{-b^2x^2}\mathrm{Erf}(bx)}{2b^2}-\frac{e^{-2b^2x^2}}{4\sqrt{\pi}\,b^3}$$

Antiderivative was successfully verified.

```
[In] Int[(x^2*Erf[b*x])/E^(b^2*x^2),x]
```

```
[Out] -1/4*1/(b^3*E^(2*b^2*x^2)*Sqrt[Pi]) - (x*Erf[b*x])/(2*b^2*E^(b^2*x^2)) + (S
qrt[Pi]*Erf[b*x]^2)/(8*b^3)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
```

```
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{-b^2x^2}x^2\operatorname{erf}(bx)\,dx &= -\frac{e^{-b^2x^2}x\operatorname{erf}(bx)}{2b^2}+\frac{\int e^{-b^2x^2}\operatorname{erf}(bx)\,dx}{2b^2}+\frac{\int e^{-2b^2x^2}x\,dx}{b\sqrt{\pi}}\\ &= -\frac{e^{-2b^2x^2}}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x\operatorname{erf}(bx)}{2b^2}+\frac{\sqrt{\pi}\,\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erf}(bx)\right)}{4b^3}\\ &= -\frac{e^{-2b^2x^2}}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x\operatorname{erf}(bx)}{2b^2}+\frac{\sqrt{\pi}\,\operatorname{erf}(bx)^2}{8b^3}\end{aligned}$$

Mathematica [A]
time = 0.03, size = 56, normalized size = 0.89

$$-\frac{\frac{2e^{-2b^2x^2}}{\sqrt{\pi}}+4be^{-b^2x^2}x\operatorname{Erf}(bx)-\sqrt{\pi}\,\operatorname{Erf}(bx)^2}{8b^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[(x^2*Erf[b*x])/E^(b^2*x^2),x]
[Out] -1/8*(2/(E^(2*b^2*x^2)*Sqrt[Pi]) + (4*b*x*Erf[b*x])/E^(b^2*x^2) - Sqrt[Pi]*
Erf[b*x]^2)/b^3
```

Maple [F]
time = 0.11, size = 0, normalized size = 0.00

$$\int x^2\operatorname{erf}(bx)\,\mathrm{e}^{-b^2x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erf(b*x)/exp(b^2*x^2),x)
[Out] int(x^2*erf(b*x)/exp(b^2*x^2),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erf(b*x)/exp(b^2*x^2),x, algorithm="maxima")
```

```
[Out] integrate(x*e^(-2*b^2*x^2), x)/(sqrt(pi)*b) - 1/8*(4*b*x*erf(b*x)*e^(-b^2*x
^2) - sqrt(pi)*erf(b*x)^2)/b^3
```

Fricas [A]
time = 0.35, size = 52, normalized size = 0.83

$$-\frac{4\,\pi bx\,\mathrm{erf}\left(bx\right)e^{\left(-b^{2}x^{2}\right)}-\sqrt{\pi}\left(\pi\,\mathrm{erf}\left(bx\right)^{2}-2\,e^{\left(-2\,b^{2}x^{2}\right)}\right)}{8\,\pi b^{3}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erf(b*x)/exp(b^2*x^2),x, algorithm="fricas")
```

```
[Out] -1/8*(4*pi*b*x*erf(b*x)*e^(-b^2*x^2) - sqrt(pi)*(pi*erf(b*x)^2 - 2*e^(-2*b^
2*x^2)))/(pi*b^3)
```

Sympy [A]
time = 1.22, size = 60, normalized size = 0.95

$$\begin{cases}-\frac{xe^{-b^{2}x^{2}}\,\mathrm{erf}\left(bx\right)}{2b^{2}}+\frac{\sqrt{\pi}\,\mathrm{erf}^{2}\left(bx\right)}{8b^{3}}-\frac{e^{-2b^{2}x^{2}}}{4\sqrt{\pi}\,b^{3}} & \text{for}\ b\neq 0\\ 0 & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*erf(b*x)/exp(b**2*x**2),x)
```

```
[Out] Piecewise((-x*exp(-b**2*x**2)*erf(b*x)/(2*b**2) + sqrt(pi)*erf(b*x)**2/(8*b
**3) - exp(-2*b**2*x**2)/(4*sqrt(pi)*b**3), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erf(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(x^2*erf(b*x)*e^(-b^2*x^2), x)
```

Mupad [B]
time = 0.30, size = 80, normalized size = 1.27

$$-\mathrm{erf}(b\,x)\,\left(\frac{\sqrt{\pi}\,\mathrm{erfi}\left(x\,\sqrt{-b^2}\right)}{4\,{\left(-b^2\right)}^{3/2}}+\frac{x\,\mathrm{e}^{-b^2\,x^2}}{2\,b^2}\right)-\frac{2\,\mathrm{e}^{-2\,b^2\,x^2}-\pi\,{\mathrm{erfi}\left(x\,\sqrt{-b^2}\right)}^2}{8\,b^3\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*exp(-b^2*x^2)*erf(b*x),x)
```

```
[Out] - erf(b*x)*((pi^(1/2)*erfi(x*(-b^2)^(1/2)))/(4*(-b^2)^(3/2)) + (x*exp(-b^2*
x^2))/(2*b^2)) - (2*exp(-2*b^2*x^2) - pi*erfi(x*(-b^2)^(1/2))^2)/(8*b^3*pi^
(1/2))
```

3.83 $\int e^{-b^2x^2}\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=18

$$\frac{\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{4b}$$

[Out] 1/4*erf(b*x)^2*Pi^(1/2)/b

Rubi [A]
time = 0.01, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = $\{6508, 30\}$

$$\frac{\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{4b}$$

Antiderivative was successfully verified.

[In] Int[Erf[b*x]/E^(b^2*x^2),x]

[Out] (Sqrt[Pi]*Erf[b*x]^2)/(4*b)

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rubi steps

$$\begin{aligned}\int e^{-b^2x^2}\mathrm{erf}(bx)\,dx &= \frac{\sqrt{\pi}\,\mathrm{Subst}\left(\int x\,dx, x, \mathrm{erf}(bx)\right)}{2b}\\ &= \frac{\sqrt{\pi}\,\mathrm{erf}(bx)^2}{4b}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 18, normalized size = 1.00

$$\frac{\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{4b}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]/E^(b^2*x^2),x]
```

```
[Out] (Sqrt[Pi]*Erf[b*x]^2)/(4*b)
```

Maple [A]
time = 0.22, size = 15, normalized size = 0.83

method	result	size
default	$\frac{\operatorname{erf}(bx)^{2}\sqrt{\pi}}{4b}$	15

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/exp(b^2*x^2),x,method=_RETURNVERBOSE)
```

```
[Out] 1/4*erf(b*x)^2*Pi^(1/2)/b
```

Maxima [A]
time = 0.25, size = 14, normalized size = 0.78

$$\frac{\sqrt{\pi}\,\operatorname{erf}(bx)^{2}}{4\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2),x, algorithm="maxima")
```

```
[Out] 1/4*sqrt(pi)*erf(b*x)^2/b
```

Fricas [A]
time = 0.35, size = 14, normalized size = 0.78

$$\frac{\sqrt{\pi}\,\operatorname{erf}(bx)^{2}}{4\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2),x, algorithm="fricas")
```

```
[Out] 1/4*sqrt(pi)*erf(b*x)^2/b
```

Sympy [A]
time = 0.32, size = 15, normalized size = 0.83

$$\begin{cases} \frac{\sqrt{\pi}\,\operatorname{erf}^{2}(bx)}{4b} & \text{for}\ b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b**2*x**2),x)
```

```
[Out] Piecewise((sqrt(pi)*erf(b*x)**2/(4*b), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(-b^2*x^2), x)
```

Mupad [B]
time = 0.20, size = 41, normalized size = 2.28

$$\frac{\sqrt{\pi}\ \mathrm{erf}\left(x\sqrt{b^2}\right)\ \mathrm{erf}(b\,x)}{2\sqrt{b^2}}-\frac{\sqrt{\pi}\ \mathrm{erf}\left(x\sqrt{b^2}\right)^2}{4\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(-b^2*x^2)*erf(b*x),x)
```

```
[Out] (pi^(1/2)*erf(x*(b^2)^(1/2))*erf(b*x))/(2*(b^2)^(1/2)) - (pi^(1/2)*erf(x*(b
^2)^(1/2))^2)/(4*b)
```

3.84 $\int \frac{e^{-b^2x^2}\mathbf{Erf}(bx)}{x^2}\,dx$

Optimal. Leaf size=52

$$-\frac{e^{-b^2x^2}\operatorname{Erf}(bx)}{x}-\frac{1}{2}b\sqrt{\pi}\operatorname{Erf}(bx)^2+\frac{b\operatorname{Ei}(-2b^2x^2)}{\sqrt{\pi}}$$

```
[Out] -erf(b*x)/exp(b^2*x^2)/x+b*Ei(-2*b^2*x^2)/Pi^(1/2)-1/2*b*erf(b*x)^2*Pi^(1/2
)
```

Rubi [A]
time = 0.05, antiderivative size = 52, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.222, Rules used = {6526, 6508, 30, 2241}

$$-\frac{e^{-b^2x^2}\operatorname{Erf}(bx)}{x}+\frac{b\operatorname{Ei}(-2b^2x^2)}{\sqrt{\pi}}-\frac{1}{2}\sqrt{\pi}\,b\operatorname{Erf}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]/(E^(b^2*x^2)*x^2),x]
```

```
[Out] -(Erf[b*x]/(E^(b^2*x^2)*x)) - (b*Sqrt[Pi]*Erf[b*x]^2)/2 + (b*ExpIntegralEi[
-2*b^2*x^2])/Sqrt[Pi]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6526

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m + 1)*E^(c + d*x^2)*(Erf[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(m
+ 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[2*(b/((m + 1
```

```
)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x])
 /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int \frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x^2}\,dx &= -\frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x} - (2b^2)\int e^{-b^2x^2}\operatorname{erf}(bx)\,dx + \frac{(2b)\int \frac{e^{-2b^2x^2}}{x}\,dx}{\sqrt{\pi}} \\
&= -\frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x} + \frac{b\operatorname{Ei}(-2b^2x^2)}{\sqrt{\pi}} - \left(b\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx, x, \operatorname{erf}(bx)\right) \\
&= -\frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x} - \frac{1}{2}b\sqrt{\pi}\operatorname{erf}(bx)^2 + \frac{b\operatorname{Ei}(-2b^2x^2)}{\sqrt{\pi}}
\end{aligned}$$

Mathematica [**A**]
time = 0.01, size = 52, normalized size = 1.00

$$-\frac{e^{-b^2x^2}\operatorname{Erf}(bx)}{x} - \frac{1}{2}b\sqrt{\pi}\operatorname{Erf}(bx)^2 + \frac{b\operatorname{Ei}(-2b^2x^2)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]/(E^(b^2*x^2)*x^2),x]
[Out] -(Erf[b*x]/(E^(b^2*x^2)*x)) - (b*Sqrt[Pi]*Erf[b*x]^2)/2 + (b*ExpIntegralEi[
-2*b^2*x^2])/Sqrt[Pi]
```

Maple [**F**]
time = 0.13, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erf}(bx)\,\mathrm{e}^{-b^2x^2}}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/exp(b^2*x^2)/x^2,x)
[Out] int(erf(b*x)/exp(b^2*x^2)/x^2,x)
```

Maxima [**F**]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x^2,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)*e^(-b^2*x^2)/x^2, x)
```

Fricas [A]
time = 0.35, size = 53, normalized size = 1.02

$$-\frac{2\,\pi\,\mathrm{erf}\left(bx\right)e^{\left(-b^2x^2\right)}+\sqrt{\pi}\left(\pi bx\,\mathrm{erf}\left(bx\right)^2-2\,bx\mathrm{Ei}\left(-2\,b^2x^2\right)\right)}{2\,\pi x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x^2,x, algorithm="fricas")
```

```
[Out] -1/2*(2*pi*erf(b*x)*e^(-b^2*x^2) + sqrt(pi)*(pi*b*x*erf(b*x)^2 - 2*b*x*Ei(-
2*b^2*x^2)))/(pi*x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int\frac{e^{-b^2x^2}\,\mathrm{erf}\left(bx\right)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b**2*x**2)/x**2,x)
```

```
[Out] Integral(exp(-b**2*x**2)*erf(b*x)/x**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x^2,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(-b^2*x^2)/x^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int\frac{\mathrm{e}^{-b^2\,x^2}\,\mathrm{erf}\left(b\,x\right)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erf(b*x))/x^2,x)
```

```
[Out] int((exp(-b^2*x^2)*erf(b*x))/x^2, x)
```

3.85 $\int \frac{e^{-b^2x^2}\mathbf{Erf}(bx)}{x^4}\,dx$

Optimal. Leaf size=108

$$-\frac{be^{-2b^2x^2}}{3\sqrt{\pi}\,x^2}-\frac{e^{-b^2x^2}\operatorname{Erf}(bx)}{3x^3}+\frac{2b^2e^{-b^2x^2}\operatorname{Erf}(bx)}{3x}+\frac{1}{3}b^3\sqrt{\pi}\operatorname{Erf}(bx)^2-\frac{4b^3\operatorname{Ei}(-2b^2x^2)}{3\sqrt{\pi}}$$

```
[Out] -1/3*erf(b*x)/exp(b^2*x^2)/x^3+2/3*b^2*erf(b*x)/exp(b^2*x^2)/x-1/3*b/exp(2*
b^2*x^2)/x^2/Pi^(1/2)-4/3*b^3*Ei(-2*b^2*x^2)/Pi^(1/2)+1/3*b^3*erf(b*x)^2*Pi
^(1/2)
```

Rubi [A]
time = 0.11, antiderivative size = 108, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.278$, Rules used = $\{6526, 6508, 30, 2241, 2245\}$

$$\frac{1}{3}\sqrt{\pi}\,b^3\operatorname{Erf}(bx)^2+\frac{2b^2e^{-b^2x^2}\operatorname{Erf}(bx)}{3x}-\frac{e^{-b^2x^2}\operatorname{Erf}(bx)}{3x^3}-\frac{be^{-2b^2x^2}}{3\sqrt{\pi}\,x^2}-\frac{4b^3\operatorname{Ei}(-2b^2x^2)}{3\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]/(E^(b^2*x^2)*x^4),x]
```

```
[Out] -1/3*b/(E^(2*b^2*x^2)*Sqrt[Pi]*x^2) - Erf[b*x]/(3*E^(b^2*x^2)*x^3) + (2*b^2
*Erf[b*x])/(3*E^(b^2*x^2)*x) + (b^3*Sqrt[Pi]*Erf[b*x]^2)/3 - (4*b^3*ExpInte
gralEi[-2*b^2*x^2])/(3*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6526

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m + 1)*E^(c + d*x^2)*(Erf[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(m
+ 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[2*(b/((m + 1
)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x])
 /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x^4}\,dx &= -\frac{e^{-b^2x^2}\operatorname{erf}(bx)}{3x^3} - \frac{1}{3}\left(2b^2\right)\int \frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x^2}\,dx + \frac{(2b)\int \frac{e^{-2b^2x^2}}{x^3}\,dx}{3\sqrt{\pi}} \\
&= -\frac{be^{-2b^2x^2}}{3\sqrt{\pi}\,x^2} - \frac{e^{-b^2x^2}\operatorname{erf}(bx)}{3x^3} + \frac{2b^2e^{-b^2x^2}\operatorname{erf}(bx)}{3x} + \frac{1}{3}\left(4b^4\right)\int e^{-b^2x^2}\operatorname{erf}(bx)\,dx - 2\frac{\left(4b^3\right)\int
\end{aligned}
$$

$$
\begin{aligned}
&= -\frac{be^{-2b^2x^2}}{3\sqrt{\pi}\,x^2} - \frac{e^{-b^2x^2}\operatorname{erf}(bx)}{3x^3} + \frac{2b^2e^{-b^2x^2}\operatorname{erf}(bx)}{3x} - \frac{4b^3\operatorname{Ei}\left(-2b^2x^2\right)}{3\sqrt{\pi}} + \frac{1}{3}\left(2b^3\sqrt{\pi}\right)\operatorname{Subst}(\\
&= -\frac{be^{-2b^2x^2}}{3\sqrt{\pi}\,x^2} - \frac{e^{-b^2x^2}\operatorname{erf}(bx)}{3x^3} + \frac{2b^2e^{-b^2x^2}\operatorname{erf}(bx)}{3x} + \frac{1}{3}b^3\sqrt{\pi}\operatorname{erf}(bx)^2 - \frac{4b^3\operatorname{Ei}\left(-2b^2x^2\right)}{3\sqrt{\pi}}
\end{aligned}
$$

Mathematica [A]
time = 0.05, size = 85, normalized size = 0.79

$$
\frac{1}{3}\left(\frac{e^{-b^2x^2}\left(-1+2b^2x^2\right)\operatorname{Erf}(bx)}{x^3} + b^3\sqrt{\pi}\operatorname{Erf}(bx)^2 + \frac{b\left(-\frac{e^{-2b^2x^2}}{x^2} - 4b^2\operatorname{Ei}\left(-2b^2x^2\right)\right)}{\sqrt{\pi}}\right)
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]/(E^(b^2*x^2)*x^4),x]
```

```
[Out] (((-1 + 2*b^2*x^2)*Erf[b*x])/(E^(b^2*x^2)*x^3) + b^3*Sqrt[Pi]*Erf[b*x]^2 +
(b*(-(1/(E^(2*b^2*x^2)*x^2)) - 4*b^2*ExpIntegralEi[-2*b^2*x^2]))/Sqrt[Pi])/
3
```

Maple [F]
time = 0.15, size = 0, normalized size = 0.00

$$
\int \frac{\operatorname{erf}\left(bx\right)\mathrm{e}^{-b^2x^2}}{x^4}\,dx
$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/exp(b^2*x^2)/x^4,x)
```

```
[Out] int(erf(b*x)/exp(b^2*x^2)/x^4,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x^4,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x)*e^(-b^2*x^2)/x^4, x)
```

Fricas [A]
time = 0.36, size = 84, normalized size = 0.78

$$-\frac{(\pi - 2\,\pi b^2x^2)\operatorname{erf}(bx)\,e^{(-b^2x^2)} - \sqrt{\pi}\left(\pi b^3x^3\operatorname{erf}(bx)^2 - 4\,b^3x^3\operatorname{Ei}(-2\,b^2x^2) - bxe^{(-2\,b^2x^2)}\right)}{3\,\pi x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x^4,x, algorithm="fricas")
```

```
[Out] -1/3*((pi - 2*pi*b^2*x^2)*erf(b*x)*e^(-b^2*x^2) - sqrt(pi)*(pi*b^3*x^3*erf(
b*x)^2 - 4*b^3*x^3*Ei(-2*b^2*x^2) - b*x*e^(-2*b^2*x^2)))/(pi*x^3)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b**2*x**2)/x**4,x)
```

```
[Out] Integral(exp(-b**2*x**2)*erf(b*x)/x**4, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x^4,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*e^(-b^2*x^2)/x^4, x)
```

Mupad [**F**]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{e^{-b^2 x^2} \operatorname{erf}(b x)}{x^4} \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erf(b*x))/x^4,x)
[Out] int((exp(-b^2*x^2)*erf(b*x))/x^4, x)
```

3.86 $\int e^{c+dx^2} x^3 \mathbf{Erf}(a+bx)\,dx$

Optimal. Leaf size=342

$$-\frac{ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{2\left(b^2-d\right)^2 d\sqrt{\pi}}+\frac{be^{-a^2+c-2abx-(b^2-d)x^2}x}{2\left(b^2-d\right) d\sqrt{\pi}}-\frac{e^{c+dx^2}\operatorname{Erf}(a+bx)}{2d^2}+\frac{e^{c+dx^2}x^2\operatorname{Erf}(a+bx)}{2d}+\frac{be^{c+\frac{a^2d}{b^2-d}}\operatorname{Erf}\left(\frac{ab\cdots}{\sqrt{\cdots}}\right.}{2\sqrt{b^2-d\cdots}}$$

```
[Out] -1/2*exp(d*x^2+c)*erf(b*x+a)/d^2+1/2*exp(d*x^2+c)*x^2*erf(b*x+a)/d-1/2*a^2*
b^3*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)/(b^2-d)^(1/2))/(b^2-d)^(5/2)/d
-1/4*b*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)/(b^2-d)^(1/2))/(b^2-d)^(3/2
)/d+1/2*b*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)/(b^2-d)^(1/2))/d^2/(b^2-
d)^(1/2)-1/2*a*b^2*exp(-a^2+c-2*a*b*x-(b^2-d)*x^2)/(b^2-d)^2/d/Pi^(1/2)+1/2
*b*exp(-a^2+c-2*a*b*x-(b^2-d)*x^2)*x/(b^2-d)/d/Pi^(1/2)
```

Rubi [A]
time = 0.36, antiderivative size = 342, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {6520, 6517, 2266, 2236, 2273, 2272}

$$\frac{be^{\frac{a^2d}{b^2-d}+c}\operatorname{Erf}\left(\frac{ab+x(b^2-d)}{\sqrt{b^2-d}}\right)}{2d^2\sqrt{b^2-d}}-\frac{be^{\frac{a^2d}{b^2-d}+c}\operatorname{Erf}\left(\frac{ab+x(b^2-d)}{\sqrt{b^2-d}}\right)}{4d\left(b^2-d\right)^{3/2}}-\frac{ab^2e^{-a^2-2abx-x^2(b^2-d)+c}}{2\sqrt{\pi}\,d\left(b^2-d\right)^2}+\frac{bxe^{-a^2-2abx-x^2(b^2-d)+c}}{2\sqrt{\pi}\,d\left(b^2-d\right)}-\frac{a^2b^3e^{\frac{a^2d}{b^2-d}+c}\operatorname{Erf}\left(\frac{ab+x(b^2-d)}{\sqrt{b^2-d}}\right)}{2d\left(b^2-d\right)^{5/2}}-\frac{e^{c+dx^2}\operatorname{Erf}(a+bx)}{2d^2}+\frac{x^2e^{c+dx^2}\operatorname{Erf}(a+bx)}{2d}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + d*x^2)*x^3*Erf[a + b*x],x]
```

```
[Out] -1/2*(a*b^2*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/((b^2 - d)^2*d*Sqrt[Pi]
) + (b*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2)*x)/(2*(b^2 - d)*d*Sqrt[Pi]) -
 (E^(c + d*x^2)*Erf[a + b*x])/(2*d^2) + (E^(c + d*x^2)*x^2*Erf[a + b*x])/(2
*d) + (b*E^(c + (a^2*d)/(b^2 - d))*Erf[(a*b + (b^2 - d)*x)/Sqrt[b^2 - d]])/
(2*Sqrt[b^2 - d]*d^2) - (a^2*b^3*E^(c + (a^2*d)/(b^2 - d))*Erf[(a*b + (b^2
- d)*x)/Sqrt[b^2 - d]])/(2*(b^2 - d)^(5/2)*d) - (b*E^(c + (a^2*d)/(b^2 - d)
)*Erf[(a*b + (b^2 - d)*x)/Sqrt[b^2 - d]])/(4*(b^2 - d)^(3/2)*d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2272

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)*((d_.) + (e_.)*(x_)), x_Symbol
] :> Simp[e*(F^(a + b*x + c*x^2)/(2*c*Log[F])), x] - Dist[(b*e - 2*c*d)/(2*
c), Int[F^(a + b*x + c*x^2), x], x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[
b*e - 2*c*d, 0]
```

Rule 2273

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)*((d_.) + (e_.)*(x_))^(m_), x_S
ymbol] :> Simp[e*(d + e*x)^(m - 1)*(F^(a + b*x + c*x^2)/(2*c*Log[F])), x] +
 (-Dist[(b*e - 2*c*d)/(2*c), Int[(d + e*x)^(m - 1)*F^(a + b*x + c*x^2), x],
 x] - Dist[(m - 1)*(e^2/(2*c*Log[F])), Int[(d + e*x)^(m - 2)*F^(a + b*x + c
*x^2), x], x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[b*e - 2*c*d, 0] && Gt
Q[m, 1]
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6520

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m - 1)*E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/(2
*d), Int[x^(m - 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[b/(d*Sqrt[Pi])
, Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ[{a
, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\int e^{c+dx^2}x^3\text{erf}(a+bx)\,dx = \frac{e^{c+dx^2}x^2\text{erf}(a+bx)}{2d} - \frac{\int e^{c+dx^2}x\text{erf}(a+bx)\,dx}{d} - \frac{b\int e^{-a^2+c-2abx+(-b^2+d)x^2}x^2\,dx}{d\sqrt{\pi}}$$

$$= \frac{be^{-a^2+c-2abx-(b^2-d)x^2}x}{2(b^2-d)\,d\sqrt{\pi}} - \frac{e^{c+dx^2}\text{erf}(a+bx)}{2d^2} + \frac{e^{c+dx^2}x^2\text{erf}(a+bx)}{2d} + \frac{b\int e^{-a^2+c-2a}}{d^2}$$

$$= -\frac{ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2\,d\sqrt{\pi}} + \frac{be^{-a^2+c-2abx-(b^2-d)x^2}x}{2(b^2-d)\,d\sqrt{\pi}} - \frac{e^{c+dx^2}\text{erf}(a+bx)}{2d^2} + \frac{e^{c+dx^2}x}{}$$

$$= -\frac{ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2\,d\sqrt{\pi}} + \frac{be^{-a^2+c-2abx-(b^2-d)x^2}x}{2(b^2-d)\,d\sqrt{\pi}} - \frac{e^{c+dx^2}\text{erf}(a+bx)}{2d^2} + \frac{e^{c+dx^2}x}{}$$

$$= -\frac{ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2\,d\sqrt{\pi}} + \frac{be^{-a^2+c-2abx-(b^2-d)x^2}x}{2(b^2-d)\,d\sqrt{\pi}} - \frac{e^{c+dx^2}\text{erf}(a+bx)}{2d^2} + \frac{e^{c+dx^2}x}{}$$

Mathematica [A]
time = 3.19, size = 240, normalized size = 0.70

$$\frac{e^c\left(2e^{dx^2}(-1+dx^2)\,\text{Erf}(a+bx) - \frac{bde^{-a^2-2abx+(-b^2+d)x^2}\left(2(b^2-d)(ab+(-b^2+d)x)+\sqrt{b^2-d}\,((1+2a^2)b^2-d)e^{\frac{(ab+(b^2-d)x)^2}{b^2-d}}\sqrt{\pi}\,\text{Erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)\right)}{(b^2-d)^3\sqrt{\pi}} + \frac{2be^{\frac{a^2d}{b^2-d}}\text{Erfi}\left(\frac{-ab+(-b^2+d)x}{\sqrt{-b^2+d}}\right)}{\sqrt{-b^2+d}}\right)}{4d^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + d*x^2)*x^3*Erf[a + b*x],x]
```

```
[Out] (E^c*(2*E^(d*x^2)*(-1 + d*x^2)*Erf[a + b*x] - (b*d*E^(-a^2 - 2*a*b*x + (-b^
2 + d)*x^2)*(2*(b^2 - d)*(a*b + (-b^2 + d)*x) + Sqrt[b^2 - d]*((1 + 2*a^2)*
b^2 - d)*E^((a*b + (b^2 - d)*x)^2/(b^2 - d))*Sqrt[Pi]*Erf[(a*b + (b^2 - d)*
x)/Sqrt[b^2 - d]]))/((b^2 - d)^3*Sqrt[Pi]) + (2*b*E^((a^2*d)/(b^2 - d))*Erf
i[(-(a*b) + (-b^2 + d)*x)/Sqrt[-b^2 + d]])/Sqrt[-b^2 + d]))/(4*d^2)
```

Maple [F]
time = 0.18, size = 0, normalized size = 0.00

$$\int e^{d\,x^2+c}x^3\,\text{erf}\,(bx+a)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^3*erf(b*x+a),x)
```

```
[Out] int(exp(d*x^2+c)*x^3*erf(b*x+a),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erf(b*x+a),x, algorithm="maxima")
```

```
[Out] 1/2*(d*x^2*e^c - e^c)*erf(b*x + a)*e^(d*x^2)/d^2 - integrate((b*d*x^2*e^c -
 b*e^c)*e^(-b^2*x^2 - 2*a*b*x + d*x^2 - a^2), x)/(sqrt(pi)*d^2)
```

Fricas [A]
time = 0.39, size = 267, normalized size = 0.78

$$\frac{\pi(2\,b^5-(2\,a^2+5)b^3d+3\,bd^2)\sqrt{b^2-d}\,\operatorname{erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)e^{\left(\frac{b^2c+(a^2-c)d}{b^2-d}\right)}+2\,(\pi(b^6d-3\,b^4d^2+3\,b^2d^3-d^4)x^2-\pi(b^6-3\,b^4d+3\,b^2d^2-d^3))\operatorname{erf}(bx+a)\,e^{(dx^2+c)}-2\,\sqrt{\pi}\,(ab^4d-ab^2d^2-(b^5d-2\,b^3d^2+bd^3)x)e^{(-b^2x^2-2\,abx+dx^2-a^2+c)}}{4\,\pi(b^6d^2-3\,b^4d^3+3\,b^2d^4-d^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erf(b*x+a),x, algorithm="fricas")
```

```
[Out] 1/4*(pi*(2*b^5 - (2*a^2 + 5)*b^3*d + 3*b*d^2)*sqrt(b^2 - d)*erf((a*b + (b^2
 - d)*x)/sqrt(b^2 - d))*e^((b^2*c + (a^2 - c)*d)/(b^2 - d)) + 2*(pi*(b^6*d
- 3*b^4*d^2 + 3*b^2*d^3 - d^4)*x^2 - pi*(b^6 - 3*b^4*d + 3*b^2*d^2 - d^3))*
erf(b*x + a)*e^(d*x^2 + c) - 2*sqrt(pi)*(a*b^4*d - a*b^2*d^2 - (b^5*d - 2*b
^3*d^2 + b*d^3)*x)*e^(-b^2*x^2 - 2*a*b*x + d*x^2 - a^2 + c))/(pi*(b^6*d^2 -
 3*b^4*d^3 + 3*b^2*d^4 - d^5))
```

Sympy [F(-1)] Timed out
time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**3*erf(b*x+a),x)
```

```
[Out] Timed out
```

Giac [A]
time = 0.44, size = 288, normalized size = 0.84

$$\frac{1}{2}\left(\frac{(dx^2+c-1)e^{(dx^2+c)}}{d^2}-\frac{ce^{(dx^2+c)}}{d^2}\right)\operatorname{erf}(bx+a)-\frac{\frac{2\sqrt{\pi}\,b\operatorname{erf}\left(-\sqrt{b^2-d}\left(\frac{ab}{b^2-d}+x\right)\right)e^{\left(\frac{b^2c+a^2d-cd}{b^2-d}\right)}}{\sqrt{b^2-d}}-\frac{\left(\frac{\sqrt{\pi}\,(2\,a^2b^2+b^2-d)\operatorname{erf}\left(-\sqrt{b^2-d}\left(\frac{ab}{b^2-d}+x\right)\right)e^{\left(\frac{b^2c+a^2d-cd}{b^2-d}\right)}}{\sqrt{b^2-d}}+2\left(\left(\frac{ab}{b^2-d}+x\right)b^2-2\,ab-\left(\frac{ab}{b^2-d}+x\right)d\right)e^{(-b^2x^2-2\,abx+dx^2-a^2+c)}\right)bd}{b^4-2\,b^2d+d^2}}{4\sqrt{\pi}\,d^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erf(b*x+a),x, algorithm="giac")
```

```
[Out] 1/2*((d*x^2 + c - 1)*e^(d*x^2 + c)/d^2 - c*e^(d*x^2 + c)/d^2)*erf(b*x + a)
- 1/4*(2*sqrt(pi)*b*erf(-sqrt(b^2 - d)*(a*b/(b^2 - d) + x))*e^((b^2*c + a^2
*d - c*d)/(b^2 - d))/sqrt(b^2 - d) - (sqrt(pi)*(2*a^2*b^2 + b^2 - d)*erf(-s
qrt(b^2 - d)*(a*b/(b^2 - d) + x))*e^((b^2*c + a^2*d - c*d)/(b^2 - d))/sqrt(
b^2 - d) + 2*((a*b/(b^2 - d) + x)*b^2 - 2*a*b - (a*b/(b^2 - d) + x)*d)*e^(-
b^2*x^2 - 2*a*b*x + d*x^2 - a^2 + c))*b*d/(b^4 - 2*b^2*d + d^2))/(sqrt(pi)*
d^2)
```

Mupad [B]
time = 1.16, size = 386, normalized size = 1.13

$$\frac{\mathrm{erfi}\left(\frac{a\,b-x\,(d-b^2)}{\sqrt{d-b^2}}\right)\,\left(b^3\,\mathrm{e}^{\frac{c\,d}{d-b^2}-\frac{a^2\,d}{d-b^2}-\frac{b^2\,c}{d-b^2}}+2\,a^2\,b^3\,\mathrm{e}^{\frac{c\,d}{d-b^2}-\frac{a^2\,d}{d-b^2}-\frac{b^2\,c}{d-b^2}}-b\,d\,\mathrm{e}^{\frac{c\,d}{d-b^2}-\frac{a^2\,d}{d-b^2}-\frac{b^2\,c}{d-b^2}}\right)}{4\,d\,{(d-b^2)}^{5/2}}-\frac{\frac{a\,b^2\,\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2+d\,x^2+c}}{2\,{(d-b^2)}^2}+\frac{b\,x\,\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2+d\,x^2+c}}{2\,(d-b^2)}}{d\,\sqrt{\pi}}-\mathrm{erf}(a+b\,x)\,\left(\frac{\mathrm{e}^{d\,x^2+c}}{2\,d^2}-\frac{x^2\,\mathrm{e}^{d\,x^2+c}}{2\,d}\right)+\frac{b\,\mathrm{erf}\left(\frac{a\,b\,1\mathrm{i}-x\,(d-b^2)\,1\mathrm{i}}{\sqrt{d-b^2}}\right)\,\mathrm{e}^{c-a^2-\frac{a^2\,b^2}{d-b^2}}\,1\mathrm{i}}{2\,d^2\,\sqrt{d-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erf(a + b*x)*exp(c + d*x^2),x)
```

```
[Out] (erfi((a*b - x*(d - b^2))/(d - b^2)^(1/2))*(b^3*exp((c*d)/(d - b^2) - (a^2*
d)/(d - b^2) - (b^2*c)/(d - b^2)) + 2*a^2*b^3*exp((c*d)/(d - b^2) - (a^2*d)
/(d - b^2) - (b^2*c)/(d - b^2)) - b*d*exp((c*d)/(d - b^2) - (a^2*d)/(d - b^
2) - (b^2*c)/(d - b^2))))/(4*d*(d - b^2)^(5/2)) - ((a*b^2*exp(c + d*x^2 - a
^2 - b^2*x^2 - 2*a*b*x))/(2*(d - b^2)^2) + (b*x*exp(c + d*x^2 - a^2 - b^2*x
^2 - 2*a*b*x))/(2*(d - b^2)))/(d*pi^(1/2)) - erf(a + b*x)*(exp(c + d*x^2)/(
2*d^2) - (x^2*exp(c + d*x^2))/(2*d)) + (b*erf((a*b*1i - x*(d - b^2)*1i)/(d
- b^2)^(1/2))*exp(c - a^2 - (a^2*b^2)/(d - b^2))*1i)/(2*d^2*(d - b^2)^(1/2)
)
```

3.87 $\int e^{c+dx^2} x \mathbf{Erf}(a+bx)\,dx$

Optimal. Leaf size=86

$$\frac{e^{c+dx^2}\text{Erf}(a+bx)}{2d}-\frac{be^{c+\frac{a^2d}{b^2-d}}\text{Erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)}{2\sqrt{b^2-d}\,d}$$

```
[Out] 1/2*exp(d*x^2+c)*erf(b*x+a)/d-1/2*b*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x
)/(b^2-d)^(1/2))/d/(b^2-d)^(1/2)
```

Rubi [A]

time = 0.04, antiderivative size = 86, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}}=0.176$, Rules used = {6517, 2266, 2236}

$$\frac{e^{c+dx^2}\text{Erf}(a+bx)}{2d}-\frac{be^{\frac{a^2d}{b^2-d}+c}\text{Erf}\left(\frac{ab+x(b^2-d)}{\sqrt{b^2-d}}\right)}{2d\sqrt{b^2-d}}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + d*x^2)*x*Erf[a + b*x],x]
```

```
[Out] (E^(c + d*x^2)*Erf[a + b*x])/(2*d) - (b*E^(c + (a^2*d)/(b^2 - d))*Erf[(a*b
+ (b^2 - d)*x)/Sqrt[b^2 - d]])/(2*Sqrt[b^2 - d]*d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 6517

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Sim
p[E^(c + d*x^2)*(Erf[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(-a^2
 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\int e^{c+dx^2}x\text{erf}(a+bx)\,dx=\frac{e^{c+dx^2}\text{erf}(a+bx)}{2d}-\frac{b\int e^{-a^2+c-2abx-(b^2-d)x^2}\,dx}{d\sqrt{\pi}}$$
$$=\frac{e^{c+dx^2}\text{erf}(a+bx)}{2d}-\frac{\left(be^{\frac{b^2c+a^2d-cd}{b^2-d}}\right)\int\exp\left(\frac{(-2ab+2(-b^2+d)x)^2}{4(-b^2+d)}\right)dx}{d\sqrt{\pi}}$$
$$=\frac{e^{c+dx^2}\text{erf}(a+bx)}{2d}-\frac{be^{\frac{b^2c+a^2d-cd}{b^2-d}}\text{erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)}{2\sqrt{b^2-d}\,d}$$

Mathematica [A]
time = 0.07, size = 82, normalized size = 0.95

$$\frac{e^c\left(e^{dx^2}\text{Erf}(a+bx)-\frac{be^{\frac{a^2d}{b^2-d}}\text{Erfi}\left(\frac{-ab+(-b^2+d)x}{\sqrt{-b^2+d}}\right)}{\sqrt{-b^2+d}}\right)}{2d}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + d*x^2)*x*Erf[a + b*x],x]
```

```
[Out] (E^c*(E^(d*x^2)*Erf[a + b*x] - (b*E^((a^2*d)/(b^2 - d))*Erfi[(-(a*b) + (-b^
2 + d)*x)/Sqrt[-b^2 + d]])/Sqrt[-b^2 + d]))/(2*d)
```

Maple [A]
time = 0.64, size = 134, normalized size = 1.56

method	result	size
default	$\frac{\frac{\text{erf}(bx+a)b\,e^{\frac{a^2d}{b^2}-\frac{2ad(bx+a)}{b^2}+c+\frac{d(bx+a)^2}{b^2}}}{2d}-\frac{b\,e^{\frac{a^2d}{b^2}+c-\frac{a^2d^2}{b^4\left(-1+\frac{d}{b^2}\right)}}\text{erf}\left(\sqrt{1-\frac{d}{b^2}}\,(bx+a)+\frac{ad}{b^2\sqrt{1-\frac{d}{b^2}}}\right)}{2d\sqrt{1-\frac{d}{b^2}}}}{b}$	134

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x*erf(b*x+a),x,method=_RETURNVERBOSE)
```

```
[Out] (1/2*erf(b*x+a)*b/d*exp(1/b^2*a^2*d-2/b^2*a*d*(b*x+a)+c+1/b^2*d*(b*x+a)^2)-
1/2*b/d*exp(1/b^2*a^2*d+c-a^2*d^2/b^4/(-1+d/b^2))/(1-d/b^2)^(1/2)*erf((1-d/
b^2)^(1/2)*(b*x+a)+a*d/b^2/(1-d/b^2)^(1/2)))/b
```

Maxima [A]
time = 0.26, size = 84, normalized size = 0.98

$$-\frac{b\,\mathrm{erf}\left(\frac{ab}{\sqrt{b^2-d}}+\sqrt{b^2-d}\,x\right)e^{\left(\frac{a^2b^2}{b^2-d}-a^2+c\right)}}{2\sqrt{b^2-d}\,d}+\frac{\mathrm{erf}\left(bx+a\right)e^{\left(dx^2+c\right)}}{2\,d}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erf(b*x+a),x, algorithm="maxima")
```

```
[Out] -1/2*b*erf(a*b/sqrt(b^2 - d) + sqrt(b^2 - d)*x)*e^(a^2*b^2/(b^2 - d) - a^2
+ c)/(sqrt(b^2 - d)*d) + 1/2*erf(b*x + a)*e^(d*x^2 + c)/d
```

Fricas [A]
time = 0.40, size = 100, normalized size = 1.16

$$-\frac{\sqrt{b^2-d}\,b\,\mathrm{erf}\left(\frac{ab+\left(b^2-d\right)x}{\sqrt{b^2-d}}\right)e^{\left(\frac{b^2c+\left(a^2-c\right)d}{b^2-d}\right)}-\left(b^2-d\right)\mathrm{erf}\left(bx+a\right)e^{\left(dx^2+c\right)}}{2\left(b^2d-d^2\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erf(b*x+a),x, algorithm="fricas")
```

```
[Out] -1/2*(sqrt(b^2 - d)*b*erf((a*b + (b^2 - d)*x)/sqrt(b^2 - d))*e^((b^2*c + (a
^2 - c)*d)/(b^2 - d)) - (b^2 - d)*erf(b*x + a)*e^(d*x^2 + c))/(b^2*d - d^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int xe^{dx^2}\,\mathrm{erf}\left(a+bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x*erf(b*x+a),x)
```

```
[Out] exp(c)*Integral(x*exp(d*x**2)*erf(a + b*x), x)
```

Giac [A]
time = 0.41, size = 87, normalized size = 1.01

$$\frac{b\,\mathrm{erf}\left(-\sqrt{b^2-d}\left(\frac{ab}{b^2-d}+x\right)\right)e^{\left(\frac{b^2c+a^2d-cd}{b^2-d}\right)}}{2\sqrt{b^2-d}\,d}+\frac{\mathrm{erf}\left(bx+a\right)e^{\left(dx^2+c\right)}}{2\,d}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erf(b*x+a),x, algorithm="giac")
```

```
[Out] 1/2*b*erf(-sqrt(b^2 - d)*(a*b/(b^2 - d) + x))*e^((b^2*c + a^2*d - c*d)/(b^2
 - d))/(sqrt(b^2 - d)*d) + 1/2*erf(b*x + a)*e^(d*x^2 + c)/d
```

Mupad [B]
time = 0.18, size = 89, normalized size = 1.03

$$\frac{\mathrm{erf}(a+b\,x)\,\mathrm{e}^{d\,x^2+c}}{2\,d}-\frac{b\,\mathrm{erf}\left(\frac{a\,b\,1\mathrm{i}-x\,\left(d-b^2\right)\,1\mathrm{i}}{\sqrt{d-b^2}}\right)\,\mathrm{e}^{c-a^2-\frac{a^2\,b^2}{d-b^2}}\,1\mathrm{i}}{2\,d\,\sqrt{d-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erf(a + b*x)*exp(c + d*x^2),x)
```

```
[Out] (erf(a + b*x)*exp(c + d*x^2))/(2*d) - (b*erf((a*b*1i - x*(d - b^2)*1i)/(d -
 b^2)^(1/2))*exp(c - a^2 - (a^2*b^2)/(d - b^2))*1i)/(2*d*(d - b^2)^(1/2))
```

3.88 $\int \frac{e^{c+dx^2}\mathbf{Erf}(a+bx)}{x}\,dx$

Optimal. Leaf size=22

$$\text{Int}\left(\frac{e^{c+dx^2}\text{Erf}(a+bx)}{x},x\right)$$

```
[Out] Unintegrable(exp(d*x^2+c)*erf(b*x+a)/x,x)
```

Rubi [A]
time = 0.03, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\text{Erf}(a+bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erf[a + b*x])/x,x]
```

```
[Out] Defer[Int][(E^(c + d*x^2)*Erf[a + b*x])/x, x]
```

Rubi steps

$$\int \frac{e^{c+dx^2}\text{erf}(a+bx)}{x}\,dx = \int \frac{e^{c+dx^2}\text{erf}(a+bx)}{x}\,dx$$

Mathematica [A]
time = 0.15, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\text{Erf}(a+bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erf[a + b*x])/x,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erf[a + b*x])/x, x]
```

Maple [A]
time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{e^{d\,x^2+c}\,\text{erf}\,(bx+a)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erf(b*x+a)/x,x)
```

```
[Out] int(exp(d*x^2+c)*erf(b*x+a)/x,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x+a)/x,x, algorithm="maxima")
```

```
[Out] integrate(erf(b*x + a)*e^(d*x^2 + c)/x, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x+a)/x,x, algorithm="fricas")
```

```
[Out] integral(erf(b*x + a)*e^(d*x^2 + c)/x, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int\frac{e^{dx^{2}}\operatorname{erf}\left(a+bx\right)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erf(b*x+a)/x,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erf(a + b*x)/x, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x+a)/x,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x + a)*e^(d*x^2 + c)/x, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{\mathrm{erf}(a+b\,x)\,\mathrm{e}^{d\,x^2+c}}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((erf(a + b*x)*exp(c + d*x^2))/x,x)
[Out] int((erf(a + b*x)*exp(c + d*x^2))/x, x)
```

3.89 $\int \frac{e^{c+dx^2}\mathbf{Erf}(a+bx)}{x^3}\,dx$

Optimal. Leaf size=185

$$-\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\mathrm{Erf}(a+bx)}{2x^2}-b\sqrt{b^2-d}\,e^{c+\frac{a^2d}{b^2-d}}\mathrm{Erf}\left(\frac{ab+(b^2-d)\,x}{\sqrt{b^2-d}}\right)-\frac{2ab^2\mathrm{Int}\left(\frac{e^{-a^2+c-2abx+(-b}}{x}\right.}{\sqrt{\pi}}$$

```
[Out] -1/2*exp(d*x^2+c)*erf(b*x+a)/x^2-b*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)
/(b^2-d)^(1/2))*(b^2-d)^(1/2)-b*exp(-a^2+c-2*a*b*x-(b^2-d)*x^2)/x/Pi^(1/2)-
2*a*b^2*Unintegrable(exp(-a^2+c-2*a*b*x+(-b^2+d)*x^2)/x,x)/Pi^(1/2)+d*Unint
egrable(exp(d*x^2+c)*erf(b*x+a)/x,x)
```

Rubi [A]

time = 0.28, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\mathrm{Erf}(a+bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erf[a + b*x])/x^3,x]
```

```
[Out] -((b*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/(Sqrt[Pi]*x)) - (E^(c + d*x^2)
*Erf[a + b*x])/(2*x^2) - b*Sqrt[b^2 - d]*E^(c + (a^2*d)/(b^2 - d))*Erf[(a*b
 + (b^2 - d)*x)/Sqrt[b^2 - d]] - (2*a*b^2*Defer[Int][E^(-a^2 + c - 2*a*b*x
+ (-b^2 + d)*x^2)/x, x])/Sqrt[Pi] + d*Defer[Int][(E^(c + d*x^2)*Erf[a + b*x
])/x, x]
```

Rubi steps

$$\begin{aligned}
\int \frac{e^{c+dx^2}\mathrm{erf}(a+bx)}{x^3}\,dx &= -\frac{e^{c+dx^2}\mathrm{erf}(a+bx)}{2x^2}+d\int \frac{e^{c+dx^2}\mathrm{erf}(a+bx)}{x}\,dx+\frac{b\int \frac{e^{-a^2+c-2abx+\left(-b^2+d\right)x^2}}{x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\mathrm{erf}(a+bx)}{2x^2}+d\int \frac{e^{c+dx^2}\mathrm{erf}(a+bx)}{x}\,dx-\frac{(2ab^2)\int}{}\\
&= -\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\mathrm{erf}(a+bx)}{2x^2}+d\int \frac{e^{c+dx^2}\mathrm{erf}(a+bx)}{x}\,dx-\frac{(2ab^2)\int}{}\\
&= -\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\mathrm{erf}(a+bx)}{2x^2}-b\sqrt{b^2-d}\,e^{\frac{b^2c+a^2d-cd}{b^2-d}}\mathrm{erf}\left(\frac{ab+(b^2-}{\sqrt{b^2-d}}\right.
\end{aligned}$$

Mathematica [A]
time = 0.27, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\text{Erf}(a+bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erf[a + b*x])/x^3,x]
[Out] Integrate[(E^(c + d*x^2)*Erf[a + b*x])/x^3, x]
```

Maple [A]
time = 0.19, size = 0, normalized size = 0.00

$$\int \frac{e^{d\,x^2+c}\,\text{erf}\,(bx+a)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erf(b*x+a)/x^3,x)
[Out] int(exp(d*x^2+c)*erf(b*x+a)/x^3,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x+a)/x^3,x, algorithm="maxima")
[Out] integrate(erf(b*x + a)*e^(d*x^2 + c)/x^3, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x+a)/x^3,x, algorithm="fricas")
[Out] integral(erf(b*x + a)*e^(d*x^2 + c)/x^3, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^2}\,\text{erf}\,(a+bx)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erf(b*x+a)/x**3,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erf(a + b*x)/x**3, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x+a)/x^3,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x + a)*e^(d*x^2 + c)/x^3, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erf}(a+b\,x)\,\mathrm{e}^{d\,x^2+c}}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((erf(a + b*x)*exp(c + d*x^2))/x^3,x)
```

```
[Out] int((erf(a + b*x)*exp(c + d*x^2))/x^3, x)
```

3.90 $\int e^{c+dx^2}x^4\mathbf{Erf}(a+bx)\,dx$

Optimal. Leaf size=527

$$-\frac{3be^{-a^2+c-2abx-(b^2-d)x^2}}{4(b^2-d)\,d^2\sqrt{\pi}}+\frac{a^2b^3e^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^3\,d\sqrt{\pi}}+\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2\,d\sqrt{\pi}}-\frac{ab^2e^{-a^2+c-2abx-(b^2-d)x^2}x}{2(b^2-d)^2\,d\sqrt{\pi}}+\frac{be^{-a^2+}}{2(}$$

```
[Out] -3/4*exp(d*x^2+c)*x*erf(b*x+a)/d^2+1/2*exp(d*x^2+c)*x^3*erf(b*x+a)/d-3/4*a*
b^2*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)/(b^2-d)^(1/2))/(b^2-d)^(3/2)/d
^2+1/2*a^3*b^4*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)/(b^2-d)^(1/2))/(b^2
-d)^(7/2)/d+3/4*a*b^2*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)/(b^2-d)^(1/2
))/(b^2-d)^(5/2)/d-3/4*b*exp(-a^2+c-2*a*b*x-(b^2-d)*x^2)/(b^2-d)/d^2/Pi^(1/
2)+1/2*a^2*b^3*exp(-a^2+c-2*a*b*x-(b^2-d)*x^2)/(b^2-d)^3/d/Pi^(1/2)+1/2*b*e
xp(-a^2+c-2*a*b*x-(b^2-d)*x^2)/(b^2-d)^2/d/Pi^(1/2)-1/2*a*b^2*exp(-a^2+c-2*
a*b*x-(b^2-d)*x^2)*x/(b^2-d)^2/d/Pi^(1/2)+1/2*b*exp(-a^2+c-2*a*b*x-(b^2-d)*
x^2)*x^2/(b^2-d)/d/Pi^(1/2)+3/4*Unintegrable(exp(d*x^2+c)*erf(b*x+a),x)/d^2
```

Rubi [A]
time = 0.66, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int e^{c+dx^2}x^4\text{Erf}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*x^4*Erf[a + b*x],x]
```

```
[Out] (-3*b*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/(4*(b^2 - d)*d^2*Sqrt[Pi]) +
(a^2*b^3*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/(2*(b^2 - d)^3*d*Sqrt[Pi])
 + (b*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/(2*(b^2 - d)^2*d*Sqrt[Pi]) -
(a*b^2*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2)*x)/(2*(b^2 - d)^2*d*Sqrt[Pi])
 + (b*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2)*x^2)/(2*(b^2 - d)*d*Sqrt[Pi])
- (3*E^(c + d*x^2)*x*Erf[a + b*x])/(4*d^2) + (E^(c + d*x^2)*x^3*Erf[a + b*x
])/(2*d) - (3*a*b^2*E^(c + (a^2*d)/(b^2 - d))*Erf[(a*b + (b^2 - d)*x)/Sqrt[
b^2 - d]])/(4*(b^2 - d)^(3/2)*d^2) + (a^3*b^4*E^(c + (a^2*d)/(b^2 - d))*Erf
[(a*b + (b^2 - d)*x)/Sqrt[b^2 - d]])/(2*(b^2 - d)^(7/2)*d) + (3*a*b^2*E^(c
+ (a^2*d)/(b^2 - d))*Erf[(a*b + (b^2 - d)*x)/Sqrt[b^2 - d]])/(4*(b^2 - d)^(
5/2)*d) + (3*Defer[Int][E^(c + d*x^2)*Erf[a + b*x], x])/(4*d^2)
```

Rubi steps

$$\int e^{c+dx^2}x^4\text{erf}(a+bx)\,dx = \frac{e^{c+dx^2}x^3\text{erf}(a+bx)}{2d} - \frac{3\int e^{c+dx^2}x^2\text{erf}(a+bx)\,dx}{2d} - \frac{b\int e^{-a^2+c-2abx+(-b^2+d)x^2}x^3\,d\ldots}{d\sqrt{\pi}}$$
$$= \frac{be^{-a^2+c-2abx-(b^2-d)x^2}x^2}{2(b^2-d)\,d\sqrt{\pi}} - \frac{3e^{c+dx^2}x\text{erf}(a+bx)}{4d^2} + \frac{e^{c+dx^2}x^3\text{erf}(a+bx)}{2d} + \frac{3\int e^{c+dx}\ldots}{\ldots}$$
$$= -\frac{3be^{-a^2+c-2abx-(b^2-d)x^2}}{4(b^2-d)\,d^2\sqrt{\pi}} + \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2\,d\sqrt{\pi}} - \frac{ab^2e^{-a^2+c-2abx-(b^2-d)x^2}x}{2(b^2-d)^2\,d\sqrt{\pi}} + \frac{be\ldots}{\ldots}$$
$$= -\frac{3be^{-a^2+c-2abx-(b^2-d)x^2}}{4(b^2-d)\,d^2\sqrt{\pi}} + \frac{a^2b^3e^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^3\,d\sqrt{\pi}} + \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2\,d\sqrt{\pi}} - \frac{ab\ldots}{\ldots}$$
$$= -\frac{3be^{-a^2+c-2abx-(b^2-d)x^2}}{4(b^2-d)\,d^2\sqrt{\pi}} + \frac{a^2b^3e^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^3\,d\sqrt{\pi}} + \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2\,d\sqrt{\pi}} - \frac{ab\ldots}{\ldots}$$
$$= -\frac{3be^{-a^2+c-2abx-(b^2-d)x^2}}{4(b^2-d)\,d^2\sqrt{\pi}} + \frac{a^2b^3e^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^3\,d\sqrt{\pi}} + \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2\,d\sqrt{\pi}} - \frac{ab\ldots}{\ldots}$$

Mathematica [A]
time = 0.35, size = 0, normalized size = 0.00

$$\int e^{c+dx^2}x^4\text{Erf}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*x^4*Erf[a + b*x],x]
[Out] Integrate[E^(c + d*x^2)*x^4*Erf[a + b*x], x]
```

Maple [A]
time = 0.08, size = 0, normalized size = 0.00

$$\int e^{d\,x^2+c}x^4\,\text{erf}\,(bx+a)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^4*erf(b*x+a),x)
[Out] int(exp(d*x^2+c)*x^4*erf(b*x+a),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erf(b*x+a),x, algorithm="maxima")
```

```
[Out] integrate(x^4*erf(b*x + a)*e^(d*x^2 + c), x)
```

Fricas [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erf(b*x+a),x, algorithm="fricas")
```

```
[Out] integral(x^4*erf(b*x + a)*e^(d*x^2 + c), x)
```

Sympy [**F(-1)**] Timed out
time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**4*erf(b*x+a),x)
```

```
[Out] Timed out
```

Giac [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erf(b*x+a),x, algorithm="giac")
```

```
[Out] integrate(x^4*erf(b*x + a)*e^(d*x^2 + c), x)
```

Mupad [**A**]
time = 0.00, size = -1, normalized size = -0.00

$$\int x^4 \operatorname{erf}(a+b\,x)\ \mathrm{e}^{d\,x^2+c}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erf(a + b*x)*exp(c + d*x^2),x)
```

```
[Out] int(x^4*erf(a + b*x)*exp(c + d*x^2), x)
```

3.91 $\int e^{c+dx^2}x^2\mathbf{Erf}(a+bx)\,dx$

Optimal. Leaf size=164

$$\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)\,d\sqrt{\pi}}+\frac{e^{c+dx^2}x\text{Erf}(a+bx)}{2d}+\frac{ab^2e^{c+\frac{a^2d}{b^2-d}}\text{Erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)}{2(b^2-d)^{3/2}d}-\frac{\text{Int}\left(e^{c+dx^2}\text{Erf}(a+bx),x\right)}{2d}$$

```
[Out] 1/2*exp(d*x^2+c)*x*erf(b*x+a)/d+1/2*a*b^2*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^
2-d)*x)/(b^2-d)^(1/2))/(b^2-d)^(3/2)/d+1/2*b*exp(-a^2+c-2*a*b*x-(b^2-d)*x^2
)/(b^2-d)/d/Pi^(1/2)-1/2*Unintegrable(exp(d*x^2+c)*erf(b*x+a),x)/d
```

Rubi [A]
time = 0.13, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int e^{c+dx^2}x^2\text{Erf}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*x^2*Erf[a + b*x],x]
```

```
[Out] (b*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/(2*(b^2 - d)*d*Sqrt[Pi]) + (E^(c
 + d*x^2)*x*Erf[a + b*x])/(2*d) + (a*b^2*E^(c + (a^2*d)/(b^2 - d))*Erf[(a*b
 + (b^2 - d)*x)/Sqrt[b^2 - d]])/(2*(b^2 - d)^(3/2)*d) - Defer[Int][E^(c + d
*x^2)*Erf[a + b*x], x]/(2*d)
```

Rubi steps

$$\begin{aligned}\int e^{c+dx^2}x^2\text{erf}(a+bx)\,dx &= \frac{e^{c+dx^2}x\text{erf}(a+bx)}{2d}-\frac{\int e^{c+dx^2}\text{erf}(a+bx)\,dx}{2d}-\frac{b\int e^{-a^2+c-2abx+(-b^2+d)x^2}x\,dx}{d\sqrt{\pi}}\\ &= \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)\,d\sqrt{\pi}}+\frac{e^{c+dx^2}x\text{erf}(a+bx)}{2d}-\frac{\int e^{c+dx^2}\text{erf}(a+bx)\,dx}{2d}+\frac{(ab^2)\int e^{-}}{(}\\ &= \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)\,d\sqrt{\pi}}+\frac{e^{c+dx^2}x\text{erf}(a+bx)}{2d}-\frac{\int e^{c+dx^2}\text{erf}(a+bx)\,dx}{2d}+\frac{\left(ab^2e^{\frac{b^2c+}{b}}\right.}{}\\ &= \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)\,d\sqrt{\pi}}+\frac{e^{c+dx^2}x\text{erf}(a+bx)}{2d}+\frac{ab^2e^{\frac{b^2c+a^2d-cd}{b^2-d}}\text{erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)}{2(b^2-d)^{3/2}d}-\frac{\int}{}\end{aligned}$$

Mathematica [A]
time = 0.28, size = 0, normalized size = 0.00

$$\int e^{c+dx^2}x^2\mathrm{Erf}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*x^2*Erf[a + b*x],x]
[Out] Integrate[E^(c + d*x^2)*x^2*Erf[a + b*x], x]
```

Maple [A]
time = 0.14, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^2+c}x^2\,\mathrm{erf}\,(bx+a)\,\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^2*erf(b*x+a),x)
[Out] int(exp(d*x^2+c)*x^2*erf(b*x+a),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erf(b*x+a),x, algorithm="maxima")
[Out] integrate(x^2*erf(b*x + a)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erf(b*x+a),x, algorithm="fricas")
[Out] integral(x^2*erf(b*x + a)*e^(d*x^2 + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int x^{2}e^{dx^{2}}\,\mathrm{erf}\,(a+bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**2*erf(b*x+a),x)
```

```
[Out] exp(c)*Integral(x**2*exp(d*x**2)*erf(a + b*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erf(b*x+a),x, algorithm="giac")
```

```
[Out] integrate(x^2*erf(b*x + a)*e^(d*x^2 + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^2\,\mathrm{erf}(a+b\,x)\;\mathrm{e}^{d\,x^2+c}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erf(a + b*x)*exp(c + d*x^2),x)
```

```
[Out] int(x^2*erf(a + b*x)*exp(c + d*x^2), x)
```

3.92 $\int e^{c+dx^2}\mathbf{Erf}(a+bx)\,dx$

Optimal. Leaf size=19

$$\operatorname{Int}\left(e^{c+dx^2}\operatorname{Erf}(a+bx),x\right)$$

```
[Out] Unintegrable(exp(d*x^2+c)*erf(b*x+a),x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int e^{c+dx^2}\operatorname{Erf}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*Erf[a + b*x],x]
[Out] Defer[Int][E^(c + d*x^2)*Erf[a + b*x], x]
```

Rubi steps

$$\int e^{c+dx^2}\operatorname{erf}(a+bx)\,dx = \int e^{c+dx^2}\operatorname{erf}(a+bx)\,dx$$

Mathematica [A]
time = 0.03, size = 0, normalized size = 0.00

$$\int e^{c+dx^2}\operatorname{Erf}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*Erf[a + b*x],x]
[Out] Integrate[E^(c + d*x^2)*Erf[a + b*x], x]
```

Maple [A]
time = 0.07, size = 0, normalized size = 0.00

$$\int e^{d\,x^2+c}\operatorname{erf}\left(bx+a\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erf(b*x+a),x)
[Out] int(exp(d*x^2+c)*erf(b*x+a),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x+a),x, algorithm="maxima")
[Out] integrate(erf(b*x + a)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x+a),x, algorithm="fricas")
[Out] integral(erf(b*x + a)*e^(d*x^2 + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int e^{dx^{2}}\operatorname{erf}{\left(a+bx\right)}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erf(b*x+a),x)
[Out] exp(c)*Integral(exp(d*x**2)*erf(a + b*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x+a),x, algorithm="giac")
[Out] integrate(erf(b*x + a)*e^(d*x^2 + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \mathrm{erf}(a+b\,x)\,\mathrm{e}^{d\,x^2+c}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(a + b*x)*exp(c + d*x^2),x)
```

```
[Out] int(erf(a + b*x)*exp(c + d*x^2), x)
```

3.93 $\int \frac{e^{c+dx^2}\mathbf{Erf}(a+bx)}{x^2}\,dx$

Optimal. Leaf size=83

$$-\frac{e^{c+dx^2}\mathrm{Erf}(a+bx)}{x}+\frac{2b\mathrm{Int}\left(\frac{e^{-a^2+c-2abx+\left(-b^2+d\right)x^2}}{x},x\right)}{\sqrt{\pi}}+2d\mathrm{Int}\left(e^{c+dx^2}\mathrm{Erf}(a+bx),x\right)$$

```
[Out] -exp(d*x^2+c)*erf(b*x+a)/x+2*b*Unintegrable(exp(-a^2+c-2*a*b*x+(-b^2+d)*x^2
)/x,x)/Pi^(1/2)+2*d*Unintegrable(exp(d*x^2+c)*erf(b*x+a),x)
```

Rubi [A]
time = 0.15, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\mathrm{Erf}(a+bx)}{x^2}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erf[a + b*x])/x^2,x]
```

```
[Out] -((E^(c + d*x^2)*Erf[a + b*x])/x) + (2*b*Defer[Int][E^(-a^2 + c - 2*a*b*x +
 (-b^2 + d)*x^2)/x, x])/Sqrt[Pi] + 2*d*Defer[Int][E^(c + d*x^2)*Erf[a + b*x
], x]
```

Rubi steps

$$\int \frac{e^{c+dx^2}\mathrm{erf}(a+bx)}{x^2}\,dx=-\frac{e^{c+dx^2}\mathrm{erf}(a+bx)}{x}+(2d)\int e^{c+dx^2}\mathrm{erf}(a+bx)\,dx+\frac{(2b)\int \frac{e^{-a^2+c-2abx+\left(-b^2+d\right)x^2}}{x}\,dx}{\sqrt{\pi}}$$

Mathematica [A]
time = 0.29, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\mathrm{Erf}(a+bx)}{x^2}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erf[a + b*x])/x^2,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erf[a + b*x])/x^2, x]
```

Maple [A]
time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^{2}+c}\,\mathrm{erf}\left(bx+a\right)}{x^{2}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erf(b*x+a)/x^2,x)
[Out] int(exp(d*x^2+c)*erf(b*x+a)/x^2,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x+a)/x^2,x, algorithm="maxima")
[Out] integrate(erf(b*x + a)*e^(d*x^2 + c)/x^2, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x+a)/x^2,x, algorithm="fricas")
[Out] integral(erf(b*x + a)*e^(d*x^2 + c)/x^2, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^{2}}\,\mathrm{erf}\left(a+bx\right)}{x^{2}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erf(b*x+a)/x**2,x)
[Out] exp(c)*Integral(exp(d*x**2)*erf(a + b*x)/x**2, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x+a)/x^2,x, algorithm="giac")
```

```
[Out] integrate(erf(b*x + a)*e^(d*x^2 + c)/x^2, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erf}(a+b\,x)\,\mathrm{e}^{d\,x^2+c}}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((erf(a + b*x)*exp(c + d*x^2))/x^2,x)
```

```
[Out] int((erf(a + b*x)*exp(c + d*x^2))/x^2, x)
```

3.94 $\int \frac{e^{c+dx^2}\textbf{Erf}(a+bx)}{x^4}\,dx$

Optimal. Leaf size=355

$$-\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2}+\frac{2ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\mathrm{Erf}(a+bx)}{3x^3}-\frac{2de^{c+dx^2}\mathrm{Erf}(a+bx)}{3x}+\frac{2}{3}ab^2\sqrt{b^2-d}$$

```
[Out] -1/3*exp(d*x^2+c)*erf(b*x+a)/x^3-2/3*d*exp(d*x^2+c)*erf(b*x+a)/x+2/3*a*b^2*
exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)/(b^2-d)^(1/2))*(b^2-d)^(1/2)-1/3*b
*exp(-a^2+c-2*a*b*x-(b^2-d)*x^2)/x^2/Pi^(1/2)+2/3*a*b^2*exp(-a^2+c-2*a*b*x-
(b^2-d)*x^2)/x/Pi^(1/2)+4/3*a^2*b^3*Unintegrable(exp(-a^2+c-2*a*b*x+(-b^2+d
)*x^2)/x,x)/Pi^(1/2)-2/3*b*(b^2-d)*Unintegrable(exp(-a^2+c-2*a*b*x+(-b^2+d)
*x^2)/x,x)/Pi^(1/2)+4/3*b*d*Unintegrable(exp(-a^2+c-2*a*b*x+(-b^2+d)*x^2)/x
,x)/Pi^(1/2)+4/3*d^2*Unintegrable(exp(d*x^2+c)*erf(b*x+a),x)
```

Rubi [A]
time = 0.61, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\mathrm{Erf}(a+bx)}{x^4}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erf[a + b*x])/x^4,x]
```

```
[Out] -1/3*(b*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/(Sqrt[Pi]*x^2) + (2*a*b^2*E
^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/(3*Sqrt[Pi]*x) - (E^(c + d*x^2)*Erf[
a + b*x])/(3*x^3) - (2*d*E^(c + d*x^2)*Erf[a + b*x])/(3*x) + (2*a*b^2*Sqrt[
b^2 - d]*E^(c + (a^2*d)/(b^2 - d))*Erf[(a*b + (b^2 - d)*x)/Sqrt[b^2 - d]])/
3 + (4*a^2*b^3*Defer[Int][E^(-a^2 + c - 2*a*b*x + (-b^2 + d)*x^2)/x, x])/(3
*Sqrt[Pi]) - (2*b*(b^2 - d)*Defer[Int][E^(-a^2 + c - 2*a*b*x + (-b^2 + d)*x
^2)/x, x])/(3*Sqrt[Pi]) + (4*b*d*Defer[Int][E^(-a^2 + c - 2*a*b*x + (-b^2 +
 d)*x^2)/x, x])/(3*Sqrt[Pi]) + (4*d^2*Defer[Int][E^(c + d*x^2)*Erf[a + b*x]
, x])/3
```

Rubi steps

$$\int \frac{e^{c+dx^2}\operatorname{erf}(a+bx)}{x^4}\,dx = -\frac{e^{c+dx^2}\operatorname{erf}(a+bx)}{3x^3} + \frac{1}{3}(2d)\int \frac{e^{c+dx^2}\operatorname{erf}(a+bx)}{x^2}\,dx + \frac{(2b)\int \frac{e^{-a^2+c-2abx+\left(-b^2+d\right)x^2}}{x^3}\,d}{3\sqrt{\pi}}$$

$$= -\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2} - \frac{e^{c+dx^2}\operatorname{erf}(a+bx)}{3x^3} - \frac{2de^{c+dx^2}\operatorname{erf}(a+bx)}{3x} + \frac{1}{3}\left(4d^2\right)\int e^{c+}$$

$$= -\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2} + \frac{2ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x} - \frac{e^{c+dx^2}\operatorname{erf}(a+bx)}{3x^3} - \frac{2de^{c+dx^2}}{}$$

$$= -\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2} + \frac{2ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x} - \frac{e^{c+dx^2}\operatorname{erf}(a+bx)}{3x^3} - \frac{2de^{c+dx^2}}{}$$

$$= -\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2} + \frac{2ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x} - \frac{e^{c+dx^2}\operatorname{erf}(a+bx)}{3x^3} - \frac{2de^{c+dx^2}}{}$$

Mathematica [A]
time = 0.38, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\operatorname{Erf}(a+bx)}{x^4}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erf[a + b*x])/x^4,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erf[a + b*x])/x^4, x]
```

Maple [A]
time = 0.19, size = 0, normalized size = 0.00

$$\int \frac{e^{d\,x^2+c}\operatorname{erf}\left(bx+a\right)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erf(b*x+a)/x^4,x)
```

```
[Out] int(exp(d*x^2+c)*erf(b*x+a)/x^4,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x+a)/x^4,x, algorithm="maxima")
[Out] integrate(erf(b*x + a)*e^(d*x^2 + c)/x^4, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x+a)/x^4,x, algorithm="fricas")
[Out] integral(erf(b*x + a)*e^(d*x^2 + c)/x^4, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int\frac{e^{dx^{2}}\operatorname{erf}\left(a+bx\right)}{x^{4}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erf(b*x+a)/x**4,x)
[Out] exp(c)*Integral(exp(d*x**2)*erf(a + b*x)/x**4, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erf(b*x+a)/x^4,x, algorithm="giac")
[Out] integrate(erf(b*x + a)*e^(d*x^2 + c)/x^4, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.00

$$\int\frac{\mathrm{erf}\left(a+b\,x\right)\,{\mathrm{e}}^{d\,x^2+c}}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((erf(a + b*x)*exp(c + d*x^2))/x^4,x)
[Out] int((erf(a + b*x)*exp(c + d*x^2))/x^4, x)
```

3.95 $\int \left(\frac{e^{-b^2x^2}\mathbf{Erf}(bx)}{x^3} + \frac{b^2e^{-b^2x^2}\mathbf{Erf}(bx)}{x}\right) dx$

Optimal. Leaf size=62

$$-\frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x} - \frac{e^{-b^2x^2}\mathrm{Erf}(bx)}{2x^2} - \sqrt{2}\,b^2\mathrm{Erf}\left(\sqrt{2}\,bx\right)$$

```
[Out] -1/2*erf(b*x)/exp(b^2*x^2)/x^2-b^2*erf(b*x*2^(1/2))*2^(1/2)-b/exp(2*b^2*x^2
)/x/Pi^(1/2)
```

Rubi [A]
time = 0.10, antiderivative size = 62, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 40, $\frac{\text{number of rules}}{\text{integrand size}} = 0.075$, Rules used = {6526, 2245, 2236}

$$-\frac{e^{-b^2x^2}\mathrm{Erf}(bx)}{2x^2} - \sqrt{2}\,b^2\mathrm{Erf}\left(\sqrt{2}\,bx\right) - \frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]/(E^(b^2*x^2)*x^3) + (b^2*Erf[b*x])/(E^(b^2*x^2)*x),x]
```

```
[Out] -(b/(E^(2*b^2*x^2)*Sqrt[Pi]*x)) - Erf[b*x]/(2*E^(b^2*x^2)*x^2) - Sqrt[2]*b^
2*Erf[Sqrt[2]*b*x]
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6526

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol] :
> Simp[x^(m + 1)*E^(c + d*x^2)*(Erf[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(m
+ 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erf[a + b*x], x], x] - Dist[2*(b/((m + 1
)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x])
```

```
/; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \left(\frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x^3}+\frac{b^2e^{-b^2x^2}\operatorname{erf}(bx)}{x}\right)dx &= b^2\int \frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x}\,dx+\int \frac{e^{-b^2x^2}\operatorname{erf}(bx)}{x^3}\,dx\\
&= -\frac{e^{-b^2x^2}\operatorname{erf}(bx)}{2x^2}+\frac{b\int \frac{e^{-2b^2x^2}}{x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\operatorname{erf}(bx)}{2x^2}-\frac{(4b^3)\int e^{-2b^2x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\operatorname{erf}(bx)}{2x^2}-\sqrt{2}\,b^2\operatorname{erf}\left(\sqrt{2}\,bx\right)
\end{aligned}
$$

Mathematica [A]
time = 0.07, size = 62, normalized size = 1.00

$$
-\frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\operatorname{Erf}(bx)}{2x^2}-\sqrt{2}\,b^2\operatorname{Erf}\left(\sqrt{2}\,bx\right)
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]/(E^(b^2*x^2)*x^3) + (b^2*Erf[b*x])/(E^(b^2*x^2)*x),x]
```

```
[Out] -(b/(E^(2*b^2*x^2)*Sqrt[Pi]*x)) - Erf[b*x]/(2*E^(b^2*x^2)*x^2) - Sqrt[2]*b^
2*Erf[Sqrt[2]*b*x]
```

Maple [A]
time = 0.70, size = 67, normalized size = 1.08

method	result	size
default	$\frac{-\frac{\operatorname{erf}(bx)b\,e^{-b^2x^2}}{2x^2}+\frac{b^3\left(-\frac{e^{-2b^2x^2}}{bx}-\sqrt{2}\,\sqrt{\pi}\,\operatorname{erf}\left(bx\sqrt{2}\right)\right)}{\sqrt{\pi}}}{b}$	67

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)/exp(b^2*x^2)/x^3+b^2*erf(b*x)/exp(b^2*x^2)/x,x,method=_RETURNV
ERBOSE)
```

```
[Out] (-1/2*erf(b*x)*b/exp(b^2*x^2)/x^2+1/Pi^(1/2)*b^3*(-1/exp(b^2*x^2)^2/b/x-2^(
1/2)*Pi^(1/2)*erf(b*x*2^(1/2))))/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x^3+b^2*erf(b*x)/exp(b^2*x^2)/x,x, algorith
m="maxima")
```

```
[Out] b*integrate(e^(-2*b^2*x^2)/x^2, x)/sqrt(pi) - 1/2*erf(b*x)*e^(-b^2*x^2)/x^2
```

Fricas [A]
time = 0.35, size = 66, normalized size = 1.06

$$-\frac{2\sqrt{2}\,\pi\sqrt{b^2}\,bx^2\operatorname{erf}\left(\sqrt{2}\,\sqrt{b^2}\,x\right)+2\sqrt{\pi}\,bxe^{\left(-2\,b^2x^2\right)}+\pi\operatorname{erf}\left(bx\right)e^{\left(-b^2x^2\right)}}{2\,\pi x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x^3+b^2*erf(b*x)/exp(b^2*x^2)/x,x, algorith
m="fricas")
```

```
[Out] -1/2*(2*sqrt(2)*pi*sqrt(b^2)*b*x^2*erf(sqrt(2)*sqrt(b^2)*x) + 2*sqrt(pi)*b*
x*e^(-2*b^2*x^2) + pi*erf(b*x)*e^(-b^2*x^2))/(pi*x^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int\frac{\left(b^2x^2+1\right)e^{-b^2x^2}\operatorname{erf}\left(bx\right)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b**2*x**2)/x**3+b**2*erf(b*x)/exp(b**2*x**2)/x,x)
```

```
[Out] Integral((b**2*x**2 + 1)*exp(-b**2*x**2)*erf(b*x)/x**3, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)/exp(b^2*x^2)/x^3+b^2*erf(b*x)/exp(b^2*x^2)/x,x, algorith
m="giac")
```

```
[Out] integrate(b^2*erf(b*x)*e^(-b^2*x^2)/x + erf(b*x)*e^(-b^2*x^2)/x^3, x)
```

Mupad [B]
time = 0.22, size = 52, normalized size = 0.84

$$-\frac{\frac{e^{-b^2 x^2}\,\mathrm{erf}(b\,x)}{2}+\frac{b\,x\,e^{-2\,b^2\,x^2}}{\sqrt{\pi}}}{x^2}-\sqrt{2}\,b^2\,\mathrm{erf}\left(\sqrt{2}\,b\,x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erf(b*x))/x^3 + (b^2*exp(-b^2*x^2)*erf(b*x))/x,x)
[Out] - ((exp(-b^2*x^2)*erf(b*x))/2 + (b*x*exp(-2*b^2*x^2))/pi^(1/2))/x^2 - 2^(1/
2)*b^2*erf(2^(1/2)*b*x)
```

3.96 $\int \mathbf{Erf}(bx)\sin\left(c+ib^2x^2\right)\,dx$

Optimal. Leaf size=66

$$-\frac{ie^{ic}\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{8b}+\frac{ibe^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] 1/2*I*b*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/exp(I*c)/Pi^(1/2)-1/8*I*exp(
I*c)*erf(b*x)^2*Pi^(1/2)/b
```

Rubi [A]
time = 0.04, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.222, Rules used = {6539, 6511, 6508, 30}

$$\frac{ibe^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}-\frac{i\sqrt{\pi}\,e^{ic}\mathrm{Erf}(bx)^2}{8b}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]*Sin[c + I*b^2*x^2],x]
```

```
[Out] ((-1/8*I)*E^(I*c)*Sqrt[Pi]*Erf[b*x]^2)/b + ((I/2)*b*x^2*HypergeometricPFQ[{
1, 1}, {3/2, 2}, b^2*x^2])/(E^(I*c)*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6539

```
Int[Erf[(b_.)*(x_)]*Sin[(c_.) + (d_.)*(x_)^2], x_Symbol] :> Dist[I/2, Int[E
^((-I)*c - I*d*x^2)*Erf[b*x], x], x] - Dist[I/2, Int[E^(I*c + I*d*x^2)*Erf[
b*x], x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, -b^4]
```

Rubi steps

$$
\begin{aligned}
\int \operatorname{erf}(bx)\sin\left(c+ib^2x^2\right)\,dx &= -\left(\frac{1}{2}i\int e^{ic-b^2x^2}\operatorname{erf}(bx)\,dx\right)+\frac{1}{2}i\int e^{-ic+b^2x^2}\operatorname{erf}(bx)\,dx\\
&= \frac{ibe^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}-\frac{\left(ie^{ic}\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erf}(bx)\right)}{4b}\\
&= -\frac{ie^{ic}\sqrt{\pi}\operatorname{erf}(bx)^2}{8b}+\frac{ibe^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}
\end{aligned}
$$

Mathematica [A]
time = 0.06, size = 69, normalized size = 1.05

$$
\frac{(\cos(c)-i\sin(c))\left(4ib^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)+\pi\operatorname{Erf}(bx)^2(-i\cos(2c)+\sin(2c))\right)}{8b\sqrt{\pi}}
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]*Sin[c + I*b^2*x^2],x]
[Out] ((Cos[c] - I*Sin[c])*((4*I)*b^2*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2
*x^2] + Pi*Erf[b*x]^2*((-I)*Cos[2*c] + Sin[2*c])))/(8*b*Sqrt[Pi])
```

Maple [F]
time = 0.08, size = 0, normalized size = 0.00

$$
\int \operatorname{erf}(bx)\sin\left(ib^2x^2+c\right)\,dx
$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)*sin(c+I*b^2*x^2),x)
[Out] int(erf(b*x)*sin(c+I*b^2*x^2),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)*sin(c+I*b^2*x^2),x, algorithm="maxima")
[Out] -1/8*I*sqrt(pi)*cos(c)*erf(b*x)^2/b + 1/8*sqrt(pi)*erf(b*x)^2*sin(c)/b + 1/
2*I*cos(c)*integrate(erf(b*x)*e^(b^2*x^2), x) + 1/2*integrate(erf(b*x)*e^(b
^2*x^2), x)*sin(c)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)*sin(c+I*b^2*x^2),x, algorithm="fricas")
```

```
[Out] integral(1/2*(-I*erf(b*x)*e^(-2*b^2*x^2 + 2*I*c) + I*erf(b*x))*e^(b^2*x^2 -
 I*c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \sin\left(ib^2x^2+c\right)\operatorname{erf}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)*sin(c+I*b**2*x**2),x)
```

```
[Out] Integral(sin(I*b**2*x**2 + c)*erf(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)*sin(c+I*b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(erf(b*x)*sin(I*b^2*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \sin\left(b^2\,x^2\,1{}\mathrm{i}+c\right)\,\mathrm{erf}\left(b\,x\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(sin(c + b^2*x^2*1i)*erf(b*x),x)
```

```
[Out] int(sin(c + b^2*x^2*1i)*erf(b*x), x)
```

3.97 $\int \mathbf{Erf}(bx)\sin\left(c - ib^2x^2\right)\,dx$

Optimal. Leaf size=66

$$\frac{ie^{-ic}\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{8b} - \frac{ibe^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] -1/2*I*b*exp(I*c)*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/Pi^(1/2)+1/8*I*erf
(b*x)^2*Pi^(1/2)/b/exp(I*c)
```

Rubi [A]
time = 0.04, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {6539, 6508, 30, 6511}

$$\frac{i\sqrt{\pi}\,e^{-ic}\mathrm{Erf}(bx)^2}{8b} - \frac{ibe^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]*Sin[c - I*b^2*x^2],x]
```

```
[Out] ((I/8)*Sqrt[Pi]*Erf[b*x]^2)/(b*E^(I*c)) - ((I/2)*b*E^(I*c)*x^2*Hypergeometr
icPFQ[{1, 1}, {3/2, 2}, b^2*x^2])/Sqrt[Pi]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6539

```
Int[Erf[(b_.)*(x_)]*Sin[(c_.) + (d_.)*(x_)^2], x_Symbol] :> Dist[I/2, Int[E
^((-I)*c - I*d*x^2)*Erf[b*x], x], x] - Dist[I/2, Int[E^(I*c + I*d*x^2)*Erf[
b*x], x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, -b^4]
```

Rubi steps

$$\int \operatorname{erf}(bx)\sin\left(c-ib^2x^2\right)\,dx = \frac{1}{2}i\int e^{-ic-b^2x^2}\operatorname{erf}(bx)\,dx - \frac{1}{2}i\int e^{ic+b^2x^2}\operatorname{erf}(bx)\,dx$$
$$= -\frac{ibe^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}} + \frac{\left(ie^{-ic}\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erf}(bx)\right)}{4b}$$
$$= \frac{ie^{-ic}\sqrt{\pi}\operatorname{erf}(bx)^2}{8b} - \frac{ibe^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

Mathematica [A]
time = 0.05, size = 67, normalized size = 1.02

$$\frac{(i\cos(c)+\sin(c))\left(\pi\operatorname{Erf}(bx)^2-4b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)(\cos(2c)+i\sin(2c))\right)}{8b\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]*Sin[c - I*b^2*x^2],x]
```

```
[Out] ((I*Cos[c] + Sin[c])*(Pi*Erf[b*x]^2 - 4*b^2*x^2*HypergeometricPFQ[{1, 1}, {
3/2, 2}, b^2*x^2]*(Cos[2*c] + I*Sin[2*c])))/(8*b*Sqrt[Pi])
```

Maple [F]
time = 0.07, size = 0, normalized size = 0.00

$$\int -\operatorname{erf}(bx)\sin\left(ib^2x^2-c\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(-erf(b*x)*sin(-c+I*b^2*x^2),x)
```

```
[Out] int(-erf(b*x)*sin(-c+I*b^2*x^2),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erf(b*x)*sin(-c+I*b^2*x^2),x, algorithm="maxima")
```

```
[Out] 1/8*I*sqrt(pi)*cos(c)*erf(b*x)^2/b + 1/8*sqrt(pi)*erf(b*x)^2*sin(c)/b - 1/2
*I*cos(c)*integrate(erf(b*x)*e^(b^2*x^2), x) + 1/2*integrate(erf(b*x)*e^(b^
2*x^2), x)*sin(c)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erf(b*x)*sin(-c+I*b^2*x^2),x, algorithm="fricas")
[Out] integral(1/2*(I*erf(b*x)*e^(-2*b^2*x^2 - 2*I*c) - I*erf(b*x))*e^(b^2*x^2 +
I*c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$-\int \sin\left(ib^2x^2 - c\right)\operatorname{erf}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erf(b*x)*sin(-c+I*b**2*x**2),x)
[Out] -Integral(sin(I*b**2*x**2 - c)*erf(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erf(b*x)*sin(-c+I*b^2*x^2),x, algorithm="giac")
[Out] integrate(-erf(b*x)*sin(I*b^2*x^2 - c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \sin\left(c - b^2\,x^2\,1{}\mathrm{i}\right)\,\mathrm{erf}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(sin(c - b^2*x^2*1i)*erf(b*x),x)
[Out] int(sin(c - b^2*x^2*1i)*erf(b*x), x)
```

3.98 $\int \cos(c + ib^2x^2)\,\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=62

$$\frac{e^{ic}\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{8b}+\frac{be^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] 1/2*b*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/exp(I*c)/Pi^(1/2)+1/8*exp(I*c)
*erf(b*x)^2*Pi^(1/2)/b
```

Rubi [A]
time = 0.04, antiderivative size = 62, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {6542, 6511, 6508, 30}

$$\frac{be^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}+\frac{\sqrt{\pi}\,e^{ic}\mathrm{Erf}(bx)^2}{8b}$$

Antiderivative was successfully verified.

```
[In] Int[Cos[c + I*b^2*x^2]*Erf[b*x],x]
```

```
[Out] (E^(I*c)*Sqrt[Pi]*Erf[b*x]^2)/(8*b) + (b*x^2*HypergeometricPFQ[{1, 1}, {3/2
, 2}, b^2*x^2])/(2*E^(I*c)*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6542

```
Int[Cos[(c_.) + (d_.)*(x_)^2]*Erf[(b_.)*(x_)], x_Symbol] :> Dist[1/2, Int[E
^((-I)*c - I*d*x^2)*Erf[b*x], x], x] + Dist[1/2, Int[E^(I*c + I*d*x^2)*Erf[
b*x], x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, -b^4]
```

Rubi steps

$$\begin{aligned}\int \cos\left(c+ib^2x^2\right)\operatorname{erf}(bx)\,dx &= \frac{1}{2}\int e^{ic-b^2x^2}\operatorname{erf}(bx)\,dx+\frac{1}{2}\int e^{-ic+b^2x^2}\operatorname{erf}(bx)\,dx\\ &= \frac{be^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}+\frac{\left(e^{ic}\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erf}(bx)\right)}{4b}\\ &= \frac{e^{ic}\sqrt{\pi}\operatorname{erf}(bx)^2}{8b}+\frac{be^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}\end{aligned}$$

Mathematica [F]
time = 0.43, size = 0, normalized size = 0.00

$$\int \cos\left(c+ib^2x^2\right)\operatorname{Erf}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Cos[c + I*b^2*x^2]*Erf[b*x],x]
[Out] Integrate[Cos[c + I*b^2*x^2]*Erf[b*x], x]
```

Maple [F]
time = 0.26, size = 0, normalized size = 0.00

$$\int \cos\left(ib^2x^2+c\right)\operatorname{erf}\left(bx\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cos(c+I*b^2*x^2)*erf(b*x),x)
[Out] int(cos(c+I*b^2*x^2)*erf(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(c+I*b^2*x^2)*erf(b*x),x, algorithm="maxima")
[Out] 1/8*sqrt(pi)*cos(c)*erf(b*x)^2/b + 1/8*I*sqrt(pi)*erf(b*x)^2*sin(c)/b + 1/2
*cos(c)*integrate(erf(b*x)*e^(b^2*x^2), x) - 1/2*I*integrate(erf(b*x)*e^(b^
2*x^2), x)*sin(c)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(c+I*b^2*x^2)*erf(b*x),x, algorithm="fricas")
[Out] integral(1/2*(erf(b*x)*e^(-2*b^2*x^2 + 2*I*c) + erf(b*x))*e^(b^2*x^2 - I*c)
, x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \cos\left(ib^2x^2 + c\right)\operatorname{erf}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(c+I*b**2*x**2)*erf(b*x),x)
[Out] Integral(cos(I*b**2*x**2 + c)*erf(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(c+I*b^2*x^2)*erf(b*x),x, algorithm="giac")
[Out] integrate(cos(I*b^2*x^2 + c)*erf(b*x), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \cos\left(b^2\,x^2\,1\mathrm{i}+c\right)\,\mathrm{erf}(b\,x)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cos(c + b^2*x^2*1i)*erf(b*x),x)
[Out] int(cos(c + b^2*x^2*1i)*erf(b*x), x)
```

3.99 $\int \cos(c - ib^2x^2)\, \mathbf{Erf}(bx)\, dx$

Optimal. Leaf size=62

$$\frac{e^{-ic}\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{8b} + \frac{be^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] 1/2*b*exp(I*c)*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/Pi^(1/2)+1/8*erf(b*x)
^2*Pi^(1/2)/b/exp(I*c)
```

Rubi [A]
time = 0.04, antiderivative size = 62, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {6542, 6508, 30, 6511}

$$\frac{be^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}} + \frac{\sqrt{\pi}\,e^{-ic}\mathrm{Erf}(bx)^2}{8b}$$

Antiderivative was successfully verified.

```
[In] Int[Cos[c - I*b^2*x^2]*Erf[b*x],x]
```

```
[Out] (Sqrt[Pi]*Erf[b*x]^2)/(8*b*E^(I*c)) + (b*E^(I*c)*x^2*HypergeometricPFQ[{1,
1}, {3/2, 2}, b^2*x^2])/(2*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6542

```
Int[Cos[(c_.) + (d_.)*(x_)^2]*Erf[(b_.)*(x_)], x_Symbol] :> Dist[1/2, Int[E
^((-I)*c - I*d*x^2)*Erf[b*x], x], x] + Dist[1/2, Int[E^(I*c + I*d*x^2)*Erf[
b*x], x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, -b^4]
```

Rubi steps

$$\begin{aligned}\int \cos\left(c-ib^2x^2\right)\operatorname{erf}(bx)\,dx&=\frac{1}{2}\int e^{-ic-b^2x^2}\operatorname{erf}(bx)\,dx+\frac{1}{2}\int e^{ic+b^2x^2}\operatorname{erf}(bx)\,dx\\&=\frac{be^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}+\frac{\left(e^{-ic}\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erf}(bx)\right)}{4b}\\&=\frac{e^{-ic}\sqrt{\pi}\operatorname{erf}(bx)^2}{8b}+\frac{be^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}\end{aligned}$$

Mathematica [F]
time = 0.44, size = 0, normalized size = 0.00

$$\int \cos\left(c-ib^2x^2\right)\operatorname{Erf}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Cos[c - I*b^2*x^2]*Erf[b*x],x]
[Out] Integrate[Cos[c - I*b^2*x^2]*Erf[b*x], x]
```

Maple [F]
time = 0.23, size = 0, normalized size = 0.00

$$\int \cos\left(ib^2x^2-c\right)\operatorname{erf}\left(bx\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cos(-c+I*b^2*x^2)*erf(b*x),x)
[Out] int(cos(-c+I*b^2*x^2)*erf(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(-c+I*b^2*x^2)*erf(b*x),x, algorithm="maxima")
[Out] 1/8*sqrt(pi)*cos(c)*erf(b*x)^2/b - 1/8*I*sqrt(pi)*erf(b*x)^2*sin(c)/b + 1/2
*cos(c)*integrate(erf(b*x)*e^(b^2*x^2), x) + 1/2*I*integrate(erf(b*x)*e^(b^
2*x^2), x)*sin(c)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(-c+I*b^2*x^2)*erf(b*x),x, algorithm="fricas")
```

```
[Out] integral(1/2*(erf(b*x)*e^(-2*b^2*x^2 - 2*I*c) + erf(b*x))*e^(b^2*x^2 + I*c)
, x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \cos\left(ib^2x^2 - c\right)\operatorname{erf}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(-c+I*b**2*x**2)*erf(b*x),x)
```

```
[Out] Integral(cos(I*b**2*x**2 - c)*erf(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(-c+I*b^2*x^2)*erf(b*x),x, algorithm="giac")
```

```
[Out] integrate(cos(I*b^2*x^2 - c)*erf(b*x), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \cos\left(c - b^2\,x^2\,1{}\mathrm{i}\right)\,\mathrm{erf}(b\,x)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cos(c - b^2*x^2*1i)*erf(b*x),x)
```

```
[Out] int(cos(c - b^2*x^2*1i)*erf(b*x), x)
```

3.100 $\int \mathbf{Erf}(bx)\sinh\left(c+b^2x^2\right)\,dx$

Optimal. Leaf size=56

$$-\frac{e^{-c}\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{8b}+\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] 1/2*b*exp(c)*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/Pi^(1/2)-1/8*erf(b*x)^2
*Pi^(1/2)/b/exp(c)
```

Rubi [A]
time = 0.04, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.267$, Rules used = {6545, 6511, 6508, 30}

$$\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}-\frac{\sqrt{\pi}\,e^{-c}\mathrm{Erf}(bx)^2}{8b}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]*Sinh[c + b^2*x^2],x]
```

```
[Out] -1/8*(Sqrt[Pi]*Erf[b*x]^2)/(b*E^c) + (b*E^c*x^2*HypergeometricPFQ[{1, 1}, {
3/2, 2}, b^2*x^2])/(2*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6545

```
Int[Erf[(b_.)*(x_)]*Sinh[(c_.) + (d_.)*(x_)^2], x_Symbol] :> Dist[1/2, Int[
E^(c + d*x^2)*Erf[b*x], x], x] - Dist[1/2, Int[E^(-c - d*x^2)*Erf[b*x], x],
 x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, b^4]
```

Rubi steps

$$\begin{aligned}\int \operatorname{erf}(bx)\sinh\left(c+b^2x^2\right)\,dx &= -\left(\frac{1}{2}\int e^{-c-b^2x^2}\operatorname{erf}(bx)\,dx\right)+\frac{1}{2}\int e^{c+b^2x^2}\operatorname{erf}(bx)\,dx\\ &= \frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}-\frac{\left(e^{-c}\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erf}(bx)\right)}{4b}\\ &= -\frac{e^{-c}\sqrt{\pi}\operatorname{erf}(bx)^2}{8b}+\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.03, size = 57, normalized size = 1.02

$$\frac{\pi\operatorname{Erf}(bx)^2(-\cosh(c)+\sinh(c))+4b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)(\cosh(c)+\sinh(c))}{8b\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]*Sinh[c + b^2*x^2],x]
[Out] (Pi*Erf[b*x]^2*(-Cosh[c] + Sinh[c]) + 4*b^2*x^2*HypergeometricPFQ[{1, 1}, {
3/2, 2}, b^2*x^2]*(Cosh[c] + Sinh[c]))/(8*b*Sqrt[Pi])
```

Maple [F]
time = 0.06, size = 0, normalized size = 0.00

$$\int \operatorname{erf}(bx)\sinh\left(b^2x^2+c\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erf(b*x)*sinh(b^2*x^2+c),x)
[Out] int(erf(b*x)*sinh(b^2*x^2+c),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)*sinh(b^2*x^2+c),x, algorithm="maxima")
[Out] -1/8*sqrt(pi)*erf(b*x)^2*e^(-c)/b + 1/2*integrate(erf(b*x)*e^(b^2*x^2 + c),
 x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)*sinh(b^2*x^2+c),x, algorithm="fricas")
[Out] integral(erf(b*x)*sinh(b^2*x^2 + c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \sinh\left(b^{2}x^{2}+c\right)\operatorname{erf}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)*sinh(b**2*x**2+c),x)
[Out] Integral(sinh(b**2*x**2 + c)*erf(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erf(b*x)*sinh(b^2*x^2+c),x, algorithm="giac")
[Out] integrate(erf(b*x)*sinh(b^2*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \sinh\left(b^2\,x^2+c\right)\,\mathrm{erf}\left(b\,x\right) \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(sinh(c + b^2*x^2)*erf(b*x),x)
[Out] int(sinh(c + b^2*x^2)*erf(b*x), x)
```

3.101 $\int \mathbf{Erf}(bx)\sinh\left(c-b^2x^2\right)\,dx$

Optimal. Leaf size=56

$$\frac{e^c\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{8b}-\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] -1/2*b*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/exp(c)/Pi^(1/2)+1/8*exp(c)*er
f(b*x)^2*Pi^(1/2)/b
```

Rubi [A]
time = 0.04, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}}=0.250$, Rules used = {6545, 6508, 30, 6511}

$$\frac{\sqrt{\pi}\,e^c\mathrm{Erf}(bx)^2}{8b}-\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[Erf[b*x]*Sinh[c - b^2*x^2],x]
```

```
[Out] (E^c*Sqrt[Pi]*Erf[b*x]^2)/(8*b) - (b*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}
, b^2*x^2])/(2*E^c*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6545

```
Int[Erf[(b_.)*(x_)]*Sinh[(c_.) + (d_.)*(x_)^2], x_Symbol] :> Dist[1/2, Int[
E^(c + d*x^2)*Erf[b*x], x], x] - Dist[1/2, Int[E^(-c - d*x^2)*Erf[b*x], x],
 x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, b^4]
```

Rubi steps

$$\begin{aligned}
\int \operatorname{erf}(bx)\sinh\left(c-b^2x^2\right)\,dx &= \frac{1}{2}\int e^{c-b^2x^2}\operatorname{erf}(bx)\,dx-\frac{1}{2}\int e^{-c+b^2x^2}\operatorname{erf}(bx)\,dx\\
&= -\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}+\frac{\left(e^c\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erf}(bx)\right)}{4b}\\
&= \frac{e^c\sqrt{\pi}\operatorname{erf}(bx)^2}{8b}-\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}
\end{aligned}$$

Mathematica [A]
time = 0.03, size = 61, normalized size = 1.09

$$\frac{(\cosh(c)-\sinh(c))\left(-4b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)+\pi\operatorname{Erf}(bx)^2(\cosh(2c)+\sinh(2c))\right)}{8b\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erf[b*x]*Sinh[c - b^2*x^2],x]
[Out] ((Cosh[c] - Sinh[c])*(-4*b^2*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^
2] + Pi*Erf[b*x]^2*(Cosh[2*c] + Sinh[2*c])))/(8*b*Sqrt[Pi])
```

Maple [F]
time = 0.06, size = 0, normalized size = 0.00

$$\int -\operatorname{erf}\left(bx\right)\sinh\left(b^2x^2-c\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(-erf(b*x)*sinh(b^2*x^2-c),x)
[Out] int(-erf(b*x)*sinh(b^2*x^2-c),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erf(b*x)*sinh(b^2*x^2-c),x, algorithm="maxima")
[Out] 1/8*sqrt(pi)*erf(b*x)^2*e^c/b - 1/2*integrate(erf(b*x)*e^(b^2*x^2 - c), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erf(b*x)*sinh(b^2*x^2-c),x, algorithm="fricas")
[Out] integral(-erf(b*x)*sinh(b^2*x^2 - c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$-\int \sinh\left(b^2x^2 - c\right)\operatorname{erf}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erf(b*x)*sinh(b**2*x**2-c),x)
[Out] -Integral(sinh(b**2*x**2 - c)*erf(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erf(b*x)*sinh(b^2*x^2-c),x, algorithm="giac")
[Out] integrate(-erf(b*x)*sinh(b^2*x^2 - c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \mathrm{sinh}\left(c-b^2\,x^2\right)\,\mathrm{erf}\left(b\,x\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(sinh(c - b^2*x^2)*erf(b*x),x)
[Out] int(sinh(c - b^2*x^2)*erf(b*x), x)
```

3.102 $\int \cosh\left(c+b^2x^2\right)\mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=56

$$\frac{e^{-c}\sqrt{\pi}\,\text{Erf}(bx)^2}{8b}+\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] 1/2*b*exp(c)*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/Pi^(1/2)+1/8*erf(b*x)^2
*Pi^(1/2)/b/exp(c)
```

Rubi [A]
time = 0.03, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}}=0.267$, Rules used = {6548, 6511, 6508, 30}

$$\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}+\frac{\sqrt{\pi}\,e^{-c}\text{Erf}(bx)^2}{8b}$$

Antiderivative was successfully verified.

```
[In] Int[Cosh[c + b^2*x^2]*Erf[b*x],x]
```

```
[Out] (Sqrt[Pi]*Erf[b*x]^2)/(8*b*E^c) + (b*E^c*x^2*HypergeometricPFQ[{1, 1}, {3/2
, 2}, b^2*x^2])/(2*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6548

```
Int[Cosh[(c_.) + (d_.)*(x_)^2]*Erf[(b_.)*(x_)], x_Symbol] :> Dist[1/2, Int[
E^(c + d*x^2)*Erf[b*x], x], x] + Dist[1/2, Int[E^(-c - d*x^2)*Erf[b*x], x],
 x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, b^4]
```

Rubi steps

$$\begin{aligned}
\int \cosh\left(c+b^2x^2\right)\operatorname{erf}(bx)\,dx &= \frac{1}{2}\int e^{-c-b^2x^2}\operatorname{erf}(bx)\,dx+\frac{1}{2}\int e^{c+b^2x^2}\operatorname{erf}(bx)\,dx\\
&= \frac{be^c x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}+\frac{\left(e^{-c}\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erf}(bx)\right)}{4b}\\
&= \frac{e^{-c}\sqrt{\pi}\operatorname{erf}(bx)^2}{8b}+\frac{be^c x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}
\end{aligned}$$

Mathematica [**A**]
time = 0.18, size = 93, normalized size = 1.66

$$\frac{-4b^2x^2\cosh(c)\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)+\pi\operatorname{Erf}(bx)(2\cosh(c)\operatorname{Erfi}(bx)+\operatorname{Erf}(bx)(\cosh(c)-\sinh(c)))+4b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)\sinh(c)}{8b\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Cosh[c + b^2*x^2]*Erf[b*x],x]
[Out] (-4*b^2*x^2*Cosh[c]*HypergeometricPFQ[{1, 1}, {3/2, 2}, -(b^2*x^2)] + Pi*Er
f[b*x]*(2*Cosh[c]*Erfi[b*x] + Erf[b*x]*(Cosh[c] - Sinh[c])) + 4*b^2*x^2*Hyp
ergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2]*Sinh[c])/(8*b*Sqrt[Pi])
```

Maple [**F**]
time = 0.23, size = 0, normalized size = 0.00

$$\int \cosh\left(b^2x^2+c\right)\operatorname{erf}\left(bx\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cosh(b^2*x^2+c)*erf(b*x),x)
[Out] int(cosh(b^2*x^2+c)*erf(b*x),x)
```

Maxima [**F**]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2+c)*erf(b*x),x, algorithm="maxima")
[Out] 1/8*sqrt(pi)*erf(b*x)^2*e^(-c)/b + 1/2*integrate(erf(b*x)*e^(b^2*x^2 + c),
x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2+c)*erf(b*x),x, algorithm="fricas")
[Out] integral(cosh(b^2*x^2 + c)*erf(b*x), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \cosh\left(b^{2}x^{2}+c\right)\operatorname{erf}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b**2*x**2+c)*erf(b*x),x)
[Out] Integral(cosh(b**2*x**2 + c)*erf(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2+c)*erf(b*x),x, algorithm="giac")
[Out] integrate(cosh(b^2*x^2 + c)*erf(b*x), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \cosh\left(b^2\,x^2+c\right)\,\mathrm{erf}\left(b\,x\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cosh(c + b^2*x^2)*erf(b*x),x)
[Out] int(cosh(c + b^2*x^2)*erf(b*x), x)
```

3.103 $\int \cosh\left(c-b^2x^2\right) \mathbf{Erf}(bx)\,dx$

Optimal. Leaf size=56

$$\frac{e^c\sqrt{\pi}\,\mathrm{Erf}(bx)^2}{8b}+\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] 1/2*b*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/exp(c)/Pi^(1/2)+1/8*exp(c)*erf
(b*x)^2*Pi^(1/2)/b
```

Rubi [A]
time = 0.04, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {6548, 6508, 30, 6511}

$$\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}+\frac{\sqrt{\pi}\,e^c\mathrm{Erf}(bx)^2}{8b}$$

Antiderivative was successfully verified.

```
[In] Int[Cosh[c - b^2*x^2]*Erf[b*x],x]
```

```
[Out] (E^c*Sqrt[Pi]*Erf[b*x]^2)/(8*b) + (b*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}
, b^2*x^2])/(2*E^c*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6508

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*(
Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erf[b*x]], x] /; FreeQ[{b, c, d, n},
 x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6548

```
Int[Cosh[(c_.) + (d_.)*(x_)^2]*Erf[(b_.)*(x_)], x_Symbol] :> Dist[1/2, Int[
E^(c + d*x^2)*Erf[b*x], x], x] + Dist[1/2, Int[E^(-c - d*x^2)*Erf[b*x], x],
 x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, b^4]
```

Rubi steps

$$\begin{aligned}\int \cosh\left(c-b^2x^2\right)\operatorname{erf}(bx)\,dx &= \frac{1}{2}\int e^{c-b^2x^2}\operatorname{erf}(bx)\,dx+\frac{1}{2}\int e^{-c+b^2x^2}\operatorname{erf}(bx)\,dx\\ &= \frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}+\frac{\left(e^c\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erf}(bx)\right)}{4b}\\ &= \frac{e^c\sqrt{\pi}\operatorname{erf}(bx)^2}{8b}+\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}\end{aligned}$$

Mathematica [**A**]
time = 0.08, size = 91, normalized size = 1.62

$$\frac{-4b^2x^2\cosh(c)\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)-4b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)\sinh(c)+\pi\operatorname{Erf}(bx)(2\cosh(c)\operatorname{Erfi}(bx)+\operatorname{Erf}(bx)(\cosh(c)+\sinh(c)))}{8b\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Cosh[c - b^2*x^2]*Erf[b*x],x]
```

```
[Out] (-4*b^2*x^2*Cosh[c]*HypergeometricPFQ[{1, 1}, {3/2, 2}, -(b^2*x^2)] - 4*b^2
*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2]*Sinh[c] + Pi*Erf[b*x]*(2*
Cosh[c]*Erfi[b*x] + Erf[b*x]*(Cosh[c] + Sinh[c])))/(8*b*Sqrt[Pi])
```

Maple [**F**]
time = 0.24, size = 0, normalized size = 0.00

$$\int \cosh\left(b^2x^2-c\right)\operatorname{erf}\left(bx\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cosh(b^2*x^2-c)*erf(b*x),x)
```

```
[Out] int(cosh(b^2*x^2-c)*erf(b*x),x)
```

Maxima [**F**]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2-c)*erf(b*x),x, algorithm="maxima")
```

```
[Out] 1/8*sqrt(pi)*erf(b*x)^2*e^c/b + 1/2*integrate(erf(b*x)*e^(b^2*x^2 - c), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2-c)*erf(b*x),x, algorithm="fricas")
[Out] integral(cosh(b^2*x^2 - c)*erf(b*x), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \cosh\left(b^2x^2 - c\right)\operatorname{erf}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b**2*x**2-c)*erf(b*x),x)
[Out] Integral(cosh(b**2*x**2 - c)*erf(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2-c)*erf(b*x),x, algorithm="giac")
[Out] integrate(cosh(b^2*x^2 - c)*erf(b*x), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \cosh\left(c-b^2\,x^2\right)\,\mathrm{erf}\left(b\,x\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cosh(c - b^2*x^2)*erf(b*x),x)
[Out] int(cosh(c - b^2*x^2)*erf(b*x), x)
```

3.104 $\int x^5 \mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=96

$$-\frac{5e^{-b^2x^2}x}{8b^5\sqrt{\pi}}-\frac{5e^{-b^2x^2}x^3}{12b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^5}{6b\sqrt{\pi}}+\frac{5\mathrm{Erf}(bx)}{16b^6}+\frac{1}{6}x^6\mathrm{Erfc}(bx)$$

```
[Out] 5/16*erf(b*x)/b^6+1/6*x^6*erfc(b*x)-5/8*x/b^5/exp(b^2*x^2)/Pi^(1/2)-5/12*x^
3/b^3/exp(b^2*x^2)/Pi^(1/2)-1/6*x^5/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.06, antiderivative size = 96, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6497, 2243, 2236}

$$\frac{5\mathrm{Erf}(bx)}{16b^6}-\frac{x^5e^{-b^2x^2}}{6\sqrt{\pi}\,b}-\frac{5xe^{-b^2x^2}}{8\sqrt{\pi}\,b^5}-\frac{5x^3e^{-b^2x^2}}{12\sqrt{\pi}\,b^3}+\frac{1}{6}x^6\mathrm{Erfc}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x^5*Erfc[b*x],x]
```

```
[Out] (-5*x)/(8*b^5*E^(b^2*x^2)*Sqrt[Pi]) - (5*x^3)/(12*b^3*E^(b^2*x^2)*Sqrt[Pi])
 - x^5/(6*b*E^(b^2*x^2)*Sqrt[Pi]) + (5*Erf[b*x])/(16*b^6) + (x^6*Erfc[b*x])
/6
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6497

```
Int[Erfc[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfc[a + b*x]/(d*(m + 1))), x] + Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int x^5\text{erfc}(bx)\,dx &= \frac{1}{6}x^6\text{erfc}(bx)+\frac{b\int e^{-b^2x^2}x^6\,dx}{3\sqrt{\pi}}\\
&= -\frac{e^{-b^2x^2}x^5}{6b\sqrt{\pi}}+\frac{1}{6}x^6\text{erfc}(bx)+\frac{5\int e^{-b^2x^2}x^4\,dx}{6b\sqrt{\pi}}\\
&= -\frac{5e^{-b^2x^2}x^3}{12b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^5}{6b\sqrt{\pi}}+\frac{1}{6}x^6\text{erfc}(bx)+\frac{5\int e^{-b^2x^2}x^2\,dx}{4b^3\sqrt{\pi}}\\
&= -\frac{5e^{-b^2x^2}x}{8b^5\sqrt{\pi}}-\frac{5e^{-b^2x^2}x^3}{12b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^5}{6b\sqrt{\pi}}+\frac{1}{6}x^6\text{erfc}(bx)+\frac{5\int e^{-b^2x^2}\,dx}{8b^5\sqrt{\pi}}\\
&= -\frac{5e^{-b^2x^2}x}{8b^5\sqrt{\pi}}-\frac{5e^{-b^2x^2}x^3}{12b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^5}{6b\sqrt{\pi}}+\frac{5\text{erf}(bx)}{16b^6}+\frac{1}{6}x^6\text{erfc}(bx)
\end{aligned}
$$

Mathematica [**A**]
time = 0.04, size = 62, normalized size = 0.65

$$
\frac{1}{48}\left(-\frac{2e^{-b^2x^2}x(15+10b^2x^2+4b^4x^4)}{b^5\sqrt{\pi}}+\frac{15\text{Erf}(bx)}{b^6}+8x^6\text{Erfc}(bx)\right)
$$

Antiderivative was successfully verified.

```
[In] Integrate[x^5*Erfc[b*x],x]
```

```
[Out] ((-2*x*(15 + 10*b^2*x^2 + 4*b^4*x^4))/(b^5*E^(b^2*x^2)*Sqrt[Pi]) + (15*Erf[
b*x])/b^6 + 8*x^6*Erfc[b*x])/48
```

Maple [**A**]
time = 0.10, size = 83, normalized size = 0.86

method	result	size
derivativedivides	$\frac{\frac{b^6x^6\text{erfc}(bx)}{6}+\frac{-\frac{b^5x^5\,\mathrm{e}^{-b^2x^2}}{2}-\frac{5b^3x^3\,\mathrm{e}^{-b^2x^2}}{4}-\frac{15\,\mathrm{e}^{-b^2x^2}bx}{8}+\frac{15\,\text{erf}(bx)\sqrt{\pi}}{16}}{3\sqrt{\pi}}}{b^6}$	83
default	$\frac{\frac{b^6x^6\text{erfc}(bx)}{6}+\frac{-\frac{b^5x^5\,\mathrm{e}^{-b^2x^2}}{2}-\frac{5b^3x^3\,\mathrm{e}^{-b^2x^2}}{4}-\frac{15\,\mathrm{e}^{-b^2x^2}bx}{8}+\frac{15\,\text{erf}(bx)\sqrt{\pi}}{16}}{3\sqrt{\pi}}}{b^6}$	83

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*erfc(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b^6*(1/6*b^6*x^6*erfc(b*x)+1/3/Pi^(1/2)*(-1/2*b^5*x^5/exp(b^2*x^2)-5/4*b^
3*x^3/exp(b^2*x^2)-15/8*b*x/exp(b^2*x^2)+15/16*Pi^(1/2)*erf(b*x)))
```

Maxima [A]
time = 0.26, size = 63, normalized size = 0.66

$$\frac{1}{6}\,x^{6}\,\mathrm{erfc}\left(bx\right)-\frac{b\left(\frac{2\,\left(4\,b^{4}x^{5}+10\,b^{2}x^{3}+15\,x\right)e^{\left(-b^{2}x^{2}\right)}}{b^{6}}-\frac{15\,\sqrt{\pi}\,\mathrm{erf}(bx)}{b^{7}}\right)}{48\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfc(b*x),x, algorithm="maxima")
```

```
[Out] 1/6*x^6*erfc(b*x) - 1/48*b*(2*(4*b^4*x^5 + 10*b^2*x^3 + 15*x)*e^(-b^2*x^2)/
b^6 - 15*sqrt(pi)*erf(b*x)/b^7)/sqrt(pi)
```

Fricas [A]
time = 0.34, size = 71, normalized size = 0.74

$$\frac{8\,\pi b^{6}x^{6}-2\,\sqrt{\pi}\,\left(4\,b^{5}x^{5}+10\,b^{3}x^{3}+15\,bx\right)e^{\left(-b^{2}x^{2}\right)}+\left(15\,\pi-8\,\pi b^{6}x^{6}\right)\mathrm{erf}\left(bx\right)}{48\,\pi b^{6}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfc(b*x),x, algorithm="fricas")
```

```
[Out] 1/48*(8*pi*b^6*x^6 - 2*sqrt(pi)*(4*b^5*x^5 + 10*b^3*x^3 + 15*b*x)*e^(-b^2*x
^2) + (15*pi - 8*pi*b^6*x^6)*erf(b*x))/(pi*b^6)
```

Sympy [A]
time = 0.52, size = 92, normalized size = 0.96

$$\begin{cases}\frac{x^{6}\,\mathrm{erfc}\left(bx\right)}{6}-\frac{x^{5}e^{-b^{2}x^{2}}}{6\sqrt{\pi}\,b}-\frac{5x^{3}e^{-b^{2}x^{2}}}{12\sqrt{\pi}\,b^{3}}-\frac{5xe^{-b^{2}x^{2}}}{8\sqrt{\pi}\,b^{5}}-\frac{5\,\mathrm{erfc}\left(bx\right)}{16b^{6}} & \text{for}\ b\neq 0\\ \frac{x^{6}}{6} & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**5*erfc(b*x),x)
```

```
[Out] Piecewise((x**6*erfc(b*x)/6 - x**5*exp(-b**2*x**2)/(6*sqrt(pi)*b) - 5*x**3*
exp(-b**2*x**2)/(12*sqrt(pi)*b**3) - 5*x*exp(-b**2*x**2)/(8*sqrt(pi)*b**5)
- 5*erfc(b*x)/(16*b**6), Ne(b, 0)), (x**6/6, True))
```

Giac [A]
time = 0.42, size = 69, normalized size = 0.72

$$-\frac{1}{6}\,x^{6}\,\mathrm{erf}\left(bx\right)+\frac{1}{6}\,x^{6}-\frac{b\left(\frac{2\,\left(4\,b^{4}x^{5}+10\,b^{2}x^{3}+15\,x\right)e^{\left(-b^{2}x^{2}\right)}}{b^{6}}+\frac{15\,\sqrt{\pi}\,\mathrm{erf}(-bx)}{b^{7}}\right)}{48\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfc(b*x),x, algorithm="giac")
```

```
[Out] -1/6*x^6*erf(b*x) + 1/6*x^6 - 1/48*b*(2*(4*b^4*x^5 + 10*b^2*x^3 + 15*x)*e^(
-b^2*x^2)/b^6 + 15*sqrt(pi)*erf(-b*x)/b^7)/sqrt(pi)
```

Mupad [B]
time = 0.27, size = 78, normalized size = 0.81

$$\frac{x^6\,\mathrm{erfc}(b\,x)}{6}-\frac{\frac{5\,\mathrm{erfc}(b\,x)}{16}+\frac{5\,b^3\,x^3\,\mathrm{e}^{-b^2\,x^2}}{12\,\sqrt{\pi}}+\frac{b^5\,x^5\,\mathrm{e}^{-b^2\,x^2}}{6\,\sqrt{\pi}}+\frac{5\,b\,x\,\mathrm{e}^{-b^2\,x^2}}{8\,\sqrt{\pi}}}{b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*erfc(b*x),x)
```

```
[Out] (x^6*erfc(b*x))/6 - ((5*erfc(b*x))/16 + (5*b^3*x^3*exp(-b^2*x^2))/(12*pi^(1
/2)) + (b^5*x^5*exp(-b^2*x^2))/(6*pi^(1/2)) + (5*b*x*exp(-b^2*x^2))/(8*pi^(
1/2)))/b^6
```

3.105 $\int x^3 \mathbf{Erfc}(bx)\, dx$

Optimal. Leaf size=71

$$-\frac{3e^{-b^2x^2}x}{8b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^3}{4b\sqrt{\pi}}+\frac{3\mathrm{Erf}(bx)}{16b^4}+\frac{1}{4}x^4\mathrm{Erfc}(bx)$$

```
[Out] 3/16*erf(b*x)/b^4+1/4*x^4*erfc(b*x)-3/8*x/b^3/exp(b^2*x^2)/Pi^(1/2)-1/4*x^3
/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.04, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6497, 2243, 2236}

$$\frac{3\mathrm{Erf}(bx)}{16b^4}-\frac{x^3e^{-b^2x^2}}{4\sqrt{\pi}\,b}-\frac{3xe^{-b^2x^2}}{8\sqrt{\pi}\,b^3}+\frac{1}{4}x^4\mathrm{Erfc}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x^3*Erfc[b*x],x]
```

```
[Out] (-3*x)/(8*b^3*E^(b^2*x^2)*Sqrt[Pi]) - x^3/(4*b*E^(b^2*x^2)*Sqrt[Pi]) + (3*E
rf[b*x])/(16*b^4) + (x^4*Erfc[b*x])/4
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6497

```
Int[Erfc[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfc[a + b*x]/(d*(m + 1))), x] + Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int x^3\operatorname{erfc}(bx)\,dx &= \frac{1}{4}x^4\operatorname{erfc}(bx)+\frac{b\int e^{-b^2x^2}x^4\,dx}{2\sqrt{\pi}}\\
&= -\frac{e^{-b^2x^2}x^3}{4b\sqrt{\pi}}+\frac{1}{4}x^4\operatorname{erfc}(bx)+\frac{3\int e^{-b^2x^2}x^2\,dx}{4b\sqrt{\pi}}\\
&= -\frac{3e^{-b^2x^2}x}{8b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^3}{4b\sqrt{\pi}}+\frac{1}{4}x^4\operatorname{erfc}(bx)+\frac{3\int e^{-b^2x^2}\,dx}{8b^3\sqrt{\pi}}\\
&= -\frac{3e^{-b^2x^2}x}{8b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^3}{4b\sqrt{\pi}}+\frac{3\operatorname{erf}(bx)}{16b^4}+\frac{1}{4}x^4\operatorname{erfc}(bx)
\end{aligned}
$$

Mathematica [A]
time = 0.04, size = 54, normalized size = 0.76

$$
\frac{1}{16}\left(-\frac{2e^{-b^2x^2}x(3+2b^2x^2)}{b^3\sqrt{\pi}}+\frac{3\operatorname{Erf}(bx)}{b^4}+4x^4\operatorname{Erfc}(bx)\right)
$$

Antiderivative was successfully verified.

```
[In] Integrate[x^3*Erfc[b*x],x]
```

```
[Out] ((-2*x*(3 + 2*b^2*x^2))/(b^3*E^(b^2*x^2)*Sqrt[Pi]) + (3*Erf[b*x])/b^4 + 4*x
^4*Erfc[b*x])/16
```

Maple [A]
time = 0.08, size = 65, normalized size = 0.92

method	result	size
derivativedivides	$\frac{\frac{b^4x^4\operatorname{erfc}(bx)}{4}+\frac{-\frac{b^3x^3\mathrm{e}^{-b^2x^2}}{2}-\frac{3\,\mathrm{e}^{-b^2x^2}bx}{4}+\frac{3\operatorname{erf}(bx)\sqrt{\pi}}{8}}{2\sqrt{\pi}}}{b^4}$	65
default	$\frac{\frac{b^4x^4\operatorname{erfc}(bx)}{4}+\frac{-\frac{b^3x^3\mathrm{e}^{-b^2x^2}}{2}-\frac{3\,\mathrm{e}^{-b^2x^2}bx}{4}+\frac{3\operatorname{erf}(bx)\sqrt{\pi}}{8}}{2\sqrt{\pi}}}{b^4}$	65

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erfc(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b^4*(1/4*b^4*x^4*erfc(b*x)+1/2/Pi^(1/2)*(-1/2*b^3*x^3/exp(b^2*x^2)-3/4*b*
x/exp(b^2*x^2)+3/8*Pi^(1/2)*erf(b*x)))
```

Maxima [A]
time = 0.27, size = 55, normalized size = 0.77

$$\frac{1}{4}\,x^4\,\mathrm{erfc}\left(bx\right) - \frac{b\left(\frac{2\,\left(2\,b^2x^3+3\,x\right)e^{\left(-b^2x^2\right)}}{b^4} - \frac{3\,\sqrt{\pi}\,\mathrm{erf}\left(bx\right)}{b^5}\right)}{16\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfc(b*x),x, algorithm="maxima")
```

```
[Out] 1/4*x^4*erfc(b*x) - 1/16*b*(2*(2*b^2*x^3 + 3*x)*e^(-b^2*x^2)/b^4 - 3*sqrt(p
i)*erf(b*x)/b^5)/sqrt(pi)
```

Fricas [A]
time = 0.35, size = 63, normalized size = 0.89

$$\frac{4\,\pi b^4x^4 - 2\,\sqrt{\pi}\,\left(2\,b^3x^3 + 3\,bx\right)e^{\left(-b^2x^2\right)} + \left(3\,\pi - 4\,\pi b^4x^4\right)\mathrm{erf}\left(bx\right)}{16\,\pi b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfc(b*x),x, algorithm="fricas")
```

```
[Out] 1/16*(4*pi*b^4*x^4 - 2*sqrt(pi)*(2*b^3*x^3 + 3*b*x)*e^(-b^2*x^2) + (3*pi -
4*pi*b^4*x^4)*erf(b*x))/(pi*b^4)
```

Sympy [A]
time = 0.29, size = 68, normalized size = 0.96

$$\begin{cases} \frac{x^4\,\mathrm{erfc}\left(bx\right)}{4} - \frac{x^3e^{-b^2x^2}}{4\sqrt{\pi}\,b} - \frac{3xe^{-b^2x^2}}{8\sqrt{\pi}\,b^3} - \frac{3\,\mathrm{erfc}\left(bx\right)}{16b^4} & \text{for}\ b \neq 0 \\ \frac{x^4}{4} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3*erfc(b*x),x)
```

```
[Out] Piecewise((x**4*erfc(b*x)/4 - x**3*exp(-b**2*x**2)/(4*sqrt(pi)*b) - 3*x*exp
(-b**2*x**2)/(8*sqrt(pi)*b**3) - 3*erfc(b*x)/(16*b**4), Ne(b, 0)), (x**4/4,
 True))
```

Giac [A]
time = 0.41, size = 61, normalized size = 0.86

$$-\frac{1}{4}\,x^4\,\mathrm{erf}\left(bx\right) + \frac{1}{4}\,x^4 - \frac{b\left(\frac{2\,\left(2\,b^2x^3+3\,x\right)e^{\left(-b^2x^2\right)}}{b^4} + \frac{3\,\sqrt{\pi}\,\mathrm{erf}\left(-bx\right)}{b^5}\right)}{16\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfc(b*x),x, algorithm="giac")
```

```
[Out] -1/4*x^4*erf(b*x) + 1/4*x^4 - 1/16*b*(2*(2*b^2*x^3 + 3*x)*e^(-b^2*x^2)/b^4
+ 3*sqrt(pi)*erf(-b*x)/b^5)/sqrt(pi)
```

Mupad [B]
time = 0.14, size = 58, normalized size = 0.82

$$\frac{x^4\,\mathrm{erfc}(b\,x)}{4}-\frac{\frac{3\,\mathrm{erfc}(b\,x)}{16}+\frac{b^3\,x^3\,\mathrm{e}^{-b^2\,x^2}}{4\,\sqrt{\pi}}+\frac{3\,b\,x\,\mathrm{e}^{-b^2\,x^2}}{8\,\sqrt{\pi}}}{b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erfc(b*x),x)
```

```
[Out] (x^4*erfc(b*x))/4 - ((3*erfc(b*x))/16 + (b^3*x^3*exp(-b^2*x^2))/(4*pi^(1/2)
) + (3*b*x*exp(-b^2*x^2))/(8*pi^(1/2)))/b^4
```

3.106 $\int x\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=46

$$-\frac{e^{-b^2x^2}x}{2b\sqrt{\pi}}+\frac{\text{Erf}(bx)}{4b^2}+\frac{1}{2}x^2\text{Erfc}(bx)$$

```
[Out] 1/4*erf(b*x)/b^2+1/2*x^2*erfc(b*x)-1/2*x/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.02, antiderivative size = 46, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}}=0.500$, Rules used = {6497, 2243, 2236}

$$\frac{\text{Erf}(bx)}{4b^2}-\frac{xe^{-b^2x^2}}{2\sqrt{\pi}\,b}+\frac{1}{2}x^2\text{Erfc}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x*Erfc[b*x],x]
```

```
[Out] -1/2*x/(b*E^(b^2*x^2)*Sqrt[Pi]) + Erf[b*x]/(4*b^2) + (x^2*Erfc[b*x])/2
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6497

```
Int[Erfc[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfc[a + b*x]/(d*(m + 1))), x] + Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int x\text{erfc}(bx)\,dx &= \frac{1}{2}x^2\text{erfc}(bx) + \frac{b\int e^{-b^2x^2}x^2\,dx}{\sqrt{\pi}} \\
&= -\frac{e^{-b^2x^2}x}{2b\sqrt{\pi}} + \frac{1}{2}x^2\text{erfc}(bx) + \frac{\int e^{-b^2x^2}\,dx}{2b\sqrt{\pi}} \\
&= -\frac{e^{-b^2x^2}x}{2b\sqrt{\pi}} + \frac{\text{erf}(bx)}{4b^2} + \frac{1}{2}x^2\text{erfc}(bx)
\end{aligned}
$$

Mathematica [A]
time = 0.03, size = 43, normalized size = 0.93

$$
\frac{1}{4}\left(\frac{\text{Erf}(bx)}{b^2} + 2x\left(-\frac{e^{-b^2x^2}}{b\sqrt{\pi}} + x\text{Erfc}(bx)\right)\right)
$$

Antiderivative was successfully verified.

```
[In] Integrate[x*Erfc[b*x],x]
```

```
[Out] (Erf[b*x]/b^2 + 2*x*(-(1/(b*E^(b^2*x^2)*Sqrt[Pi])) + x*Erfc[b*x]))/4
```

Maple [A]
time = 0.09, size = 46, normalized size = 1.00

method	result	size
derivativedivides	$\frac{\frac{b^2x^2\text{erfc}(bx)}{2} + \frac{-\frac{e^{-b^2x^2}bx}{2} + \frac{\text{erf}(bx)\sqrt{\pi}}{4}}{\sqrt{\pi}}}{b^2}$	46
default	$\frac{\frac{b^2x^2\text{erfc}(bx)}{2} + \frac{-\frac{e^{-b^2x^2}bx}{2} + \frac{\text{erf}(bx)\sqrt{\pi}}{4}}{\sqrt{\pi}}}{b^2}$	46

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfc(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b^2*(1/2*b^2*x^2*erfc(b*x)+1/Pi^(1/2)*(-1/2*b*x/exp(b^2*x^2)+1/4*Pi^(1/2)
*erf(b*x)))
```

Maxima [A]
time = 0.25, size = 44, normalized size = 0.96

$$
\frac{1}{2}\,x^2\,\text{erfc}\,(bx) - \frac{b\left(\frac{2\,xe^{\left(-b^2x^2\right)}}{b^2} - \frac{\sqrt{\pi}\,\text{erf}(bx)}{b^3}\right)}{4\,\sqrt{\pi}}
$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(b*x),x, algorithm="maxima")
```

```
[Out] 1/2*x^2*erfc(b*x) - 1/4*b*(2*x*e^(-b^2*x^2)/b^2 - sqrt(pi)*erf(b*x)/b^3)/sq
rt(pi)
```

Fricas [A]
time = 0.36, size = 50, normalized size = 1.09

$$\frac{2\,\pi b^2x^2 - 2\,\sqrt{\pi}\,bxe^{\left(-b^2x^2\right)} + \left(\pi - 2\,\pi b^2x^2\right)\operatorname{erf}\left(bx\right)}{4\,\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(b*x),x, algorithm="fricas")
```

```
[Out] 1/4*(2*pi*b^2*x^2 - 2*sqrt(pi)*b*x*e^(-b^2*x^2) + (pi - 2*pi*b^2*x^2)*erf(b
*x))/(pi*b^2)
```

Sympy [A]
time = 0.18, size = 42, normalized size = 0.91

$$\begin{cases} \frac{x^2\operatorname{erfc}\left(bx\right)}{2} - \frac{xe^{-b^2x^2}}{2\sqrt{\pi}\,b} - \frac{\operatorname{erfc}\left(bx\right)}{4b^2} & \text{for}\ b \neq 0 \\ \frac{x^2}{2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(b*x),x)
```

```
[Out] Piecewise((x**2*erfc(b*x)/2 - x*exp(-b**2*x**2)/(2*sqrt(pi)*b) - erfc(b*x)/
(4*b**2), Ne(b, 0)), (x**2/2, True))
```

Giac [A]
time = 0.43, size = 49, normalized size = 1.07

$$-\frac{1}{2}\,x^2\operatorname{erf}\left(bx\right) + \frac{1}{2}\,x^2 - \frac{b\left(\frac{2\,xe^{\left(-b^2x^2\right)}}{b^2} + \frac{\sqrt{\pi}\,\operatorname{erf}\left(-bx\right)}{b^3}\right)}{4\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(b*x),x, algorithm="giac")
```

```
[Out] -1/2*x^2*erf(b*x) + 1/2*x^2 - 1/4*b*(2*x*e^(-b^2*x^2)/b^2 + sqrt(pi)*erf(-b
*x)/b^3)/sqrt(pi)
```

Mupad [B]
time = 0.12, size = 38, normalized size = 0.83

$$\frac{x^2\,\mathrm{erfc}(b\,x)}{2}-\frac{\frac{\mathrm{erfc}(b\,x)}{4}+\frac{b\,x\,\mathrm{e}^{-b^2\,x^2}}{2\,\sqrt{\pi}}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfc(b*x),x)
```

```
[Out] (x^2*erfc(b*x))/2 - (erfc(b*x)/4 + (b*x*exp(-b^2*x^2))/(2*pi^(1/2)))/b^2
```

3.107 $\int \frac{\textbf{Erfc}(bx)}{x} \, dx$

Optimal. Leaf size=35

$$-\frac{2bx\,{}_2F_2\left(\frac{1}{2},\frac{1}{2};\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}+\log(x)$$

```
[Out] ln(x)-2*b*x*hypergeom([1/2, 1/2],[3/2, 3/2],-b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.02, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {6494, 6493}

$$\log(x)-\frac{2bx\,{}_2F_2\left(\frac{1}{2},\frac{1}{2};\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]/x,x]
```

```
[Out] (-2*b*x*HypergeometricPFQ[{1/2, 1/2}, {3/2, 3/2}, -(b^2*x^2)])/Sqrt[Pi] + L
og[x]
```

Rule 6493

```
Int[Erf[(b_.)*(x_)]/(x_), x_Symbol] :> Simp[2*b*(x/Sqrt[Pi])*Hypergeometric
PFQ[{1/2, 1/2}, {3/2, 3/2}, (-b^2)*x^2], x] /; FreeQ[b, x]
```

Rule 6494

```
Int[Erfc[(b_.)*(x_)]/(x_), x_Symbol] :> Simp[Log[x], x] - Int[Erf[b*x]/x, x
] /; FreeQ[b, x]
```

Rubi steps

$$\begin{aligned}\int \frac{\operatorname{erfc}(bx)}{x}\,dx &= \log(x)-\int \frac{\operatorname{erf}(bx)}{x}\,dx\\ &= -\frac{2bx\,{}_2F_2\left(\frac{1}{2},\frac{1}{2};\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}+\log(x)\end{aligned}$$

Mathematica [A]
time = 0.02, size = 45, normalized size = 1.29

$$-\frac{2bx\,{}_2F_2\left(\frac{1}{2},\frac{1}{2};\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}+(\operatorname{Erf}(bx)+\operatorname{Erfc}(bx))\log(x)$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]/x,x]
```

```
[Out] (-2*b*x*HypergeometricPFQ[{1/2, 1/2}, {3/2, 3/2}, -(b^2*x^2)])/Sqrt[Pi] + (
Erf[b*x] + Erfc[b*x])*Log[x]
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}(bx)}{x}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/x,x)
```

```
[Out] int(erfc(b*x)/x,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)/x, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x,x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x) - 1)/x, x)
```

Sympy [A]
time = 0.37, size = 36, normalized size = 1.03

$$-\frac{2bx\,{}_{2}F_{2}\left(\begin{matrix}\frac{1}{2},\frac{1}{2}\\ \frac{3}{2},\frac{3}{2}\end{matrix}\middle|\,-b^{2}x^{2}\right)}{\sqrt{\pi}}+\frac{\log\left(b^{2}x^{2}\right)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x,x)
```

```
[Out] -2*b*x*hyper((1/2, 1/2), (3/2, 3/2), -b**2*x**2)/sqrt(pi) + log(b**2*x**2)/
2
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)/x, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{\mathrm{erfc}(b\,x)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/x,x)
```

```
[Out] int(erfc(b*x)/x, x)
```

3.108 $\int \frac{\mathbf{Erfc}(bx)}{x^3} \, dx$

Optimal. Leaf size=40

$$\frac{be^{-b^2x^2}}{\sqrt{\pi}\, x} + b^2\mathrm{Erf}(bx) - \frac{\mathrm{Erfc}(bx)}{2x^2}$$

```
[Out] b^2*erf(b*x)-1/2*erfc(b*x)/x^2+b/exp(b^2*x^2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.02, antiderivative size = 40, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6497, 2245, 2236}

$$b^2\mathrm{Erf}(bx) + \frac{be^{-b^2x^2}}{\sqrt{\pi}\, x} - \frac{\mathrm{Erfc}(bx)}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]/x^3,x]
```

```
[Out] b/(E^(b^2*x^2)*Sqrt[Pi]*x) + b^2*Erf[b*x] - Erfc[b*x]/(2*x^2)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6497

```
Int[Erfc[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfc[a + b*x]/(d*(m + 1))), x] + Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{\operatorname{erfc}(bx)}{x^3}\,dx &= -\frac{\operatorname{erfc}(bx)}{2x^2} - \frac{b\int \frac{e^{-b^2x^2}}{x^2}\,dx}{\sqrt{\pi}} \\ &= \frac{be^{-b^2x^2}}{\sqrt{\pi}\,x} - \frac{\operatorname{erfc}(bx)}{2x^2} + \frac{(2b^3)\int e^{-b^2x^2}\,dx}{\sqrt{\pi}} \\ &= \frac{be^{-b^2x^2}}{\sqrt{\pi}\,x} + b^2\operatorname{erf}(bx) - \frac{\operatorname{erfc}(bx)}{2x^2}\end{aligned}$$

Mathematica [A]
time = 0.04, size = 40, normalized size = 1.00

$$\frac{be^{-b^2x^2}}{\sqrt{\pi}\,x} + b^2\operatorname{Erf}(bx) - \frac{\operatorname{Erfc}(bx)}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]/x^3,x]
```

```
[Out] b/(E^(b^2*x^2)*Sqrt[Pi]*x) + b^2*Erf[b*x] - Erfc[b*x]/(2*x^2)
```

Maple [A]
time = 0.08, size = 51, normalized size = 1.28

method	result	size
derivativedivides	$b^2\left(-\frac{\operatorname{erfc}(bx)}{2b^2x^2} - \frac{-\frac{e^{-b^2x^2}}{xb} - \operatorname{erf}(bx)\sqrt{\pi}}{\sqrt{\pi}}\right)$	51
default	$b^2\left(-\frac{\operatorname{erfc}(bx)}{2b^2x^2} - \frac{-\frac{e^{-b^2x^2}}{xb} - \operatorname{erf}(bx)\sqrt{\pi}}{\sqrt{\pi}}\right)$	51

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/x^3,x,method=_RETURNVERBOSE)
```

```
[Out] b^2*(-1/2/b^2/x^2*erfc(b*x)-1/Pi^(1/2)*(-1/exp(b^2*x^2)/b/x-Pi^(1/2)*erf(b*
x)))
```

Maxima [A]
time = 0.30, size = 35, normalized size = 0.88

$$\frac{b^2\sqrt{x^2}\,\Gamma\left(-\frac{1}{2}, b^2x^2\right)}{2\sqrt{\pi}\,x} - \frac{\operatorname{erfc}(bx)}{2\,x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(erfc(b*x)/x^3,x, algorithm="maxima")

[Out] 1/2*b^2*sqrt(x^2)*gamma(-1/2, b^2*x^2)/(sqrt(pi)*x) - 1/2*erfc(b*x)/x^2

Fricas [A]
time = 0.35, size = 43, normalized size = 1.08

$$-\frac{\pi - 2\sqrt{\pi}\, bxe^{\left(-b^2x^2\right)} - \left(\pi + 2\,\pi b^2x^2\right)\operatorname{erf}\left(bx\right)}{2\,\pi x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(erfc(b*x)/x^3,x, algorithm="fricas")

[Out] -1/2*(pi - 2*sqrt(pi)*b*x*e^(-b^2*x^2) - (pi + 2*pi*b^2*x^2)*erf(b*x))/(pi*x^2)

Sympy [A]
time = 0.22, size = 34, normalized size = 0.85

$$-b^2\operatorname{erfc}\left(bx\right) + \frac{be^{-b^2x^2}}{\sqrt{\pi}\,x} - \frac{\operatorname{erfc}\left(bx\right)}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(erfc(b*x)/x**3,x)

[Out] -b**2*erfc(b*x) + b*exp(-b**2*x**2)/(sqrt(pi)*x) - erfc(b*x)/(2*x**2)

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(erfc(b*x)/x^3,x, algorithm="giac")

[Out] integrate(erfc(b*x)/x^3, x)

Mupad [B]
time = 0.13, size = 38, normalized size = 0.95

$$-b^2\operatorname{erfc}(b\,x) - \frac{\frac{\operatorname{erfc}(b\,x)}{2} - \frac{b\,x\,\mathrm{e}^{-b^2\,x^2}}{\sqrt{\pi}}}{x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(erfc(b*x)/x^3,x)

[Out] - b^2*erfc(b*x) - (erfc(b*x)/2 - (b*x*exp(-b^2*x^2))/pi^(1/2))/x^2

3.109 $\int \frac{\text{Erfc}(bx)}{x^5}\,dx$

Optimal. Leaf size=71

$$\frac{be^{-b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{b^3e^{-b^2x^2}}{3\sqrt{\pi}\,x}-\frac{1}{3}b^4\text{Erf}(bx)-\frac{\text{Erfc}(bx)}{4x^4}$$

```
[Out] -1/3*b^4*erf(b*x)-1/4*erfc(b*x)/x^4+1/6*b/exp(b^2*x^2)/x^3/Pi^(1/2)-1/3*b^3
/exp(b^2*x^2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.04, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6497, 2245, 2236}

$$-\frac{1}{3}b^4\text{Erf}(bx)+\frac{be^{-b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{b^3e^{-b^2x^2}}{3\sqrt{\pi}\,x}-\frac{\text{Erfc}(bx)}{4x^4}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]/x^5,x]
```

```
[Out] b/(6*E^(b^2*x^2)*Sqrt[Pi]*x^3) - b^3/(3*E^(b^2*x^2)*Sqrt[Pi]*x) - (b^4*Erf[
b*x])/3 - Erfc[b*x]/(4*x^4)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6497

```
Int[Erfc[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfc[a + b*x]/(d*(m + 1))), x] + Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{\operatorname{erfc}(bx)}{x^5}\,dx &= -\frac{\operatorname{erfc}(bx)}{4x^4} - \frac{b\int \frac{e^{-b^2x^2}}{x^4}\,dx}{2\sqrt{\pi}}\\
&= \frac{be^{-b^2x^2}}{6\sqrt{\pi}\,x^3} - \frac{\operatorname{erfc}(bx)}{4x^4} + \frac{b^3\int \frac{e^{-b^2x^2}}{x^2}\,dx}{3\sqrt{\pi}}\\
&= \frac{be^{-b^2x^2}}{6\sqrt{\pi}\,x^3} - \frac{b^3e^{-b^2x^2}}{3\sqrt{\pi}\,x} - \frac{\operatorname{erfc}(bx)}{4x^4} - \frac{(2b^5)\int e^{-b^2x^2}\,dx}{3\sqrt{\pi}}\\
&= \frac{be^{-b^2x^2}}{6\sqrt{\pi}\,x^3} - \frac{b^3e^{-b^2x^2}}{3\sqrt{\pi}\,x} - \frac{1}{3}b^4\operatorname{erf}(bx) - \frac{\operatorname{erfc}(bx)}{4x^4}
\end{aligned}
$$

Mathematica [A]
time = 0.03, size = 53, normalized size = 0.75

$$
\frac{1}{12}\left(\frac{2e^{-b^2x^2}(b-2b^3x^2)}{\sqrt{\pi}\,x^3} - 4b^4\operatorname{Erf}(bx) - \frac{3\operatorname{Erfc}(bx)}{x^4}\right)
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]/x^5,x]
```

```
[Out] ((2*(b - 2*b^3*x^2))/(E^(b^2*x^2)*Sqrt[Pi]*x^3) - 4*b^4*Erf[b*x] - (3*Erfc[
b*x])/x^4)/12
```

Maple [A]
time = 0.09, size = 69, normalized size = 0.97

method	result	size
derivativedivides	$b^4\left(-\frac{\operatorname{erfc}(bx)}{4b^4x^4} - \frac{-\frac{\mathrm{e}^{-b^2x^2}}{3b^3x^3} + \frac{2\,\mathrm{e}^{-b^2x^2}}{3xb} + \frac{2\operatorname{erf}(bx)\sqrt{\pi}}{3}}{2\sqrt{\pi}}\right)$	69
default	$b^4\left(-\frac{\operatorname{erfc}(bx)}{4b^4x^4} - \frac{-\frac{\mathrm{e}^{-b^2x^2}}{3b^3x^3} + \frac{2\,\mathrm{e}^{-b^2x^2}}{3xb} + \frac{2\operatorname{erf}(bx)\sqrt{\pi}}{3}}{2\sqrt{\pi}}\right)$	69

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/x^5,x,method=_RETURNVERBOSE)
```

```
[Out] b^4*(-1/4/b^4/x^4*erfc(b*x)-1/2/Pi^(1/2)*(-1/3/exp(b^2*x^2)/b^3/x^3+2/3/exp
(b^2*x^2)/b/x+2/3*Pi^(1/2)*erf(b*x)))
```

Maxima [A]
time = 0.31, size = 35, normalized size = 0.49

$$\frac{b^4(x^2)^{\frac{3}{2}}\Gamma\left(-\frac{3}{2}, b^2x^2\right)}{4\sqrt{\pi}\,x^3} - \frac{\operatorname{erfc}(bx)}{4\,x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x^5,x, algorithm="maxima")
```

```
[Out] 1/4*b^4*(x^2)^(3/2)*gamma(-3/2, b^2*x^2)/(sqrt(pi)*x^3) - 1/4*erfc(b*x)/x^4
```

Fricas [A]
time = 0.35, size = 58, normalized size = 0.82

$$-\frac{3\,\pi + 2\,\sqrt{\pi}\,(2\,b^3x^3 - bx)e^{(-b^2x^2)} - (3\,\pi - 4\,\pi b^4x^4)\operatorname{erf}(bx)}{12\,\pi x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x^5,x, algorithm="fricas")
```

```
[Out] -1/12*(3*pi + 2*sqrt(pi)*(2*b^3*x^3 - b*x)*e^(-b^2*x^2) - (3*pi - 4*pi*b^4*
x^4)*erf(b*x))/(pi*x^4)
```

Sympy [A]
time = 0.36, size = 60, normalized size = 0.85

$$\frac{b^4\operatorname{erfc}(bx)}{3} - \frac{b^3e^{-b^2x^2}}{3\sqrt{\pi}\,x} + \frac{be^{-b^2x^2}}{6\sqrt{\pi}\,x^3} - \frac{\operatorname{erfc}(bx)}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x**5,x)
```

```
[Out] b**4*erfc(b*x)/3 - b**3*exp(-b**2*x**2)/(3*sqrt(pi)*x) + b*exp(-b**2*x**2)/
(6*sqrt(pi)*x**3) - erfc(b*x)/(4*x**4)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x^5,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)/x^5, x)
```

Mupad [B]
time = 0.19, size = 71, normalized size = 1.00

$$-\frac{\frac{\mathrm{erfc}(b\,x)}{4}+\frac{b^3\,x^3\,\mathrm{e}^{-b^2\,x^2}}{3\,\sqrt{\pi}}-\frac{b\,x\,\mathrm{e}^{-b^2\,x^2}}{6\,\sqrt{\pi}}}{x^4}-\frac{b^5\,\mathrm{erfi}\left(x\,\sqrt{-b^2}\right)}{3\,\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/x^5,x)
[Out] - (erfc(b*x)/4 + (b^3*x^3*exp(-b^2*x^2))/(3*pi^(1/2)) - (b*x*exp(-b^2*x^2))
/(6*pi^(1/2)))/x^4 - (b^5*erfi(x*(-b^2)^(1/2)))/(3*(-b^2)^(1/2))
```

3.110 $\int \frac{\textbf{Erfc}(bx)}{x^7}\,dx$

Optimal. Leaf size=96

$$\frac{be^{-b^2x^2}}{15\sqrt{\pi}\,x^5}-\frac{2b^3e^{-b^2x^2}}{45\sqrt{\pi}\,x^3}+\frac{4b^5e^{-b^2x^2}}{45\sqrt{\pi}\,x}+\frac{4}{45}b^6\mathrm{Erf}(bx)-\frac{\mathrm{Erfc}(bx)}{6x^6}$$

```
[Out] 4/45*b^6*erf(b*x)-1/6*erfc(b*x)/x^6+1/15*b/exp(b^2*x^2)/x^5/Pi^(1/2)-2/45*b
^3/exp(b^2*x^2)/x^3/Pi^(1/2)+4/45*b^5/exp(b^2*x^2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.06, antiderivative size = 96, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.375, Rules used = {6497, 2245, 2236}

$$\frac{4}{45}b^6\mathrm{Erf}(bx)+\frac{be^{-b^2x^2}}{15\sqrt{\pi}\,x^5}+\frac{4b^5e^{-b^2x^2}}{45\sqrt{\pi}\,x}-\frac{2b^3e^{-b^2x^2}}{45\sqrt{\pi}\,x^3}-\frac{\mathrm{Erfc}(bx)}{6x^6}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]/x^7,x]
```

```
[Out] b/(15*E^(b^2*x^2)*Sqrt[Pi]*x^5) - (2*b^3)/(45*E^(b^2*x^2)*Sqrt[Pi]*x^3) + (
4*b^5)/(45*E^(b^2*x^2)*Sqrt[Pi]*x) + (4*b^6*Erf[b*x])/45 - Erfc[b*x]/(6*x^6
)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6497

```
Int[Erfc[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfc[a + b*x]/(d*(m + 1))), x] + Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
```

```
m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{\operatorname{erfc}(bx)}{x^7}\,dx &= -\frac{\operatorname{erfc}(bx)}{6x^6} - \frac{b\int \frac{e^{-b^2x^2}}{x^6}\,dx}{3\sqrt{\pi}}\\
&= \frac{be^{-b^2x^2}}{15\sqrt{\pi}\,x^5} - \frac{\operatorname{erfc}(bx)}{6x^6} + \frac{(2b^3)\int \frac{e^{-b^2x^2}}{x^4}\,dx}{15\sqrt{\pi}}\\
&= \frac{be^{-b^2x^2}}{15\sqrt{\pi}\,x^5} - \frac{2b^3e^{-b^2x^2}}{45\sqrt{\pi}\,x^3} - \frac{\operatorname{erfc}(bx)}{6x^6} - \frac{(4b^5)\int \frac{e^{-b^2x^2}}{x^2}\,dx}{45\sqrt{\pi}}\\
&= \frac{be^{-b^2x^2}}{15\sqrt{\pi}\,x^5} - \frac{2b^3e^{-b^2x^2}}{45\sqrt{\pi}\,x^3} + \frac{4b^5e^{-b^2x^2}}{45\sqrt{\pi}\,x} - \frac{\operatorname{erfc}(bx)}{6x^6} + \frac{(8b^7)\int e^{-b^2x^2}\,dx}{45\sqrt{\pi}}\\
&= \frac{be^{-b^2x^2}}{15\sqrt{\pi}\,x^5} - \frac{2b^3e^{-b^2x^2}}{45\sqrt{\pi}\,x^3} + \frac{4b^5e^{-b^2x^2}}{45\sqrt{\pi}\,x} + \frac{4}{45}b^6\operatorname{erf}(bx) - \frac{\operatorname{erfc}(bx)}{6x^6}
\end{aligned}
$$

Mathematica [A]
time = 0.04, size = 62, normalized size = 0.65

$$\frac{1}{90}\left(\frac{2be^{-b^2x^2}(3-2b^2x^2+4b^4x^4)}{\sqrt{\pi}\,x^5}+8b^6\operatorname{Erf}(bx)-\frac{15\operatorname{Erfc}(bx)}{x^6}\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]/x^7,x]
[Out] ((2*b*(3 - 2*b^2*x^2 + 4*b^4*x^4))/(E^(b^2*x^2)*Sqrt[Pi]*x^5) + 8*b^6*Erf[b
*x] - (15*Erfc[b*x])/x^6)/90
```

Maple [A]
time = 0.09, size = 87, normalized size = 0.91

method	result	size
derivativedivides	$b^6\left(-\frac{\operatorname{erfc}(bx)}{6b^6x^6}-\frac{-\frac{e^{-b^2x^2}}{5b^5x^5}+\frac{2e^{-b^2x^2}}{15b^3x^3}-\frac{4e^{-b^2x^2}}{15xb}-\frac{4\operatorname{erf}(bx)\sqrt{\pi}}{15}}{3\sqrt{\pi}}\right)$	87
default	$b^6\left(-\frac{\operatorname{erfc}(bx)}{6b^6x^6}-\frac{-\frac{e^{-b^2x^2}}{5b^5x^5}+\frac{2e^{-b^2x^2}}{15b^3x^3}-\frac{4e^{-b^2x^2}}{15xb}-\frac{4\operatorname{erf}(bx)\sqrt{\pi}}{15}}{3\sqrt{\pi}}\right)$	87

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/x^7,x,method=_RETURNVERBOSE)
```

```
[Out] b^6*(-1/6/b^6/x^6*erfc(b*x)-1/3/Pi^(1/2)*(-1/5/exp(b^2*x^2)/b^5/x^5+2/15/ex
p(b^2*x^2)/b^3/x^3-4/15/exp(b^2*x^2)/b/x-4/15*Pi^(1/2)*erf(b*x)))
```

Maxima [A]
time = 0.30, size = 35, normalized size = 0.36

$$\frac{b^6(x^2)^{\frac{5}{2}}\Gamma\left(-\frac{5}{2},b^2x^2\right)}{6\sqrt{\pi}\,x^5}-\frac{\operatorname{erfc}(bx)}{6\,x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x^7,x, algorithm="maxima")
```

```
[Out] 1/6*b^6*(x^2)^(5/2)*gamma(-5/2, b^2*x^2)/(sqrt(pi)*x^5) - 1/6*erfc(b*x)/x^6
```

Fricas [A]
time = 0.37, size = 66, normalized size = 0.69

$$-\frac{15\,\pi-2\,\sqrt{\pi}\,(4\,b^5x^5-2\,b^3x^3+3\,bx)e^{(-b^2x^2)}-(15\,\pi+8\,\pi b^6x^6)\operatorname{erf}(bx)}{90\,\pi x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x^7,x, algorithm="fricas")
```

```
[Out] -1/90*(15*pi - 2*sqrt(pi)*(4*b^5*x^5 - 2*b^3*x^3 + 3*b*x)*e^(-b^2*x^2) - (1
5*pi + 8*pi*b^6*x^6)*erf(b*x))/(pi*x^6)
```

Sympy [A]
time = 0.67, size = 87, normalized size = 0.91

$$-\frac{4b^6\operatorname{erfc}(bx)}{45}+\frac{4b^5e^{-b^2x^2}}{45\sqrt{\pi}\,x}-\frac{2b^3e^{-b^2x^2}}{45\sqrt{\pi}\,x^3}+\frac{be^{-b^2x^2}}{15\sqrt{\pi}\,x^5}-\frac{\operatorname{erfc}(bx)}{6x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x**7,x)
```

```
[Out] -4*b**6*erfc(b*x)/45 + 4*b**5*exp(-b**2*x**2)/(45*sqrt(pi)*x) - 2*b**3*exp(
-b**2*x**2)/(45*sqrt(pi)*x**3) + b*exp(-b**2*x**2)/(15*sqrt(pi)*x**5) - erf
c(b*x)/(6*x**6)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x^7,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)/x^7, x)
```

Mupad [**F**]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\operatorname{erfc}(b\,x)}{x^7}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/x^7,x)
```

```
[Out] int(erfc(b*x)/x^7, x)
```

3.111 $\int x^6 \mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=109

$$-\frac{6e^{-b^2x^2}}{7b^7\sqrt{\pi}}-\frac{6e^{-b^2x^2}x^2}{7b^5\sqrt{\pi}}-\frac{3e^{-b^2x^2}x^4}{7b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^6}{7b\sqrt{\pi}}+\frac{1}{7}x^7\mathrm{Erfc}(bx)$$

```
[Out] 1/7*x^7*erfc(b*x)-6/7/b^7/exp(b^2*x^2)/Pi^(1/2)-6/7*x^2/b^5/exp(b^2*x^2)/Pi
^(1/2)-3/7*x^4/b^3/exp(b^2*x^2)/Pi^(1/2)-1/7*x^6/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.06, antiderivative size = 109, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6497, 2243, 2240}

$$-\frac{x^6e^{-b^2x^2}}{7\sqrt{\pi}\,b}-\frac{6e^{-b^2x^2}}{7\sqrt{\pi}\,b^7}-\frac{6x^2e^{-b^2x^2}}{7\sqrt{\pi}\,b^5}-\frac{3x^4e^{-b^2x^2}}{7\sqrt{\pi}\,b^3}+\frac{1}{7}x^7\mathrm{Erfc}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x^6*Erfc[b*x],x]
```

```
[Out] -6/(7*b^7*E^(b^2*x^2)*Sqrt[Pi]) - (6*x^2)/(7*b^5*E^(b^2*x^2)*Sqrt[Pi]) - (3
*x^4)/(7*b^3*E^(b^2*x^2)*Sqrt[Pi]) - x^6/(7*b*E^(b^2*x^2)*Sqrt[Pi]) + (x^7*
Erfc[b*x])/7
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6497

```
Int[Erfc[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfc[a + b*x]/(d*(m + 1))), x] + Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
```

```
m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int x^6 \operatorname{erfc}(bx)\,dx &= \frac{1}{7}x^7\operatorname{erfc}(bx)+\frac{(2b)\int e^{-b^2x^2}x^7\,dx}{7\sqrt{\pi}}\\
&= -\frac{e^{-b^2x^2}x^6}{7b\sqrt{\pi}}+\frac{1}{7}x^7\operatorname{erfc}(bx)+\frac{6\int e^{-b^2x^2}x^5\,dx}{7b\sqrt{\pi}}\\
&= -\frac{3e^{-b^2x^2}x^4}{7b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^6}{7b\sqrt{\pi}}+\frac{1}{7}x^7\operatorname{erfc}(bx)+\frac{12\int e^{-b^2x^2}x^3\,dx}{7b^3\sqrt{\pi}}\\
&= -\frac{6e^{-b^2x^2}x^2}{7b^5\sqrt{\pi}}-\frac{3e^{-b^2x^2}x^4}{7b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^6}{7b\sqrt{\pi}}+\frac{1}{7}x^7\operatorname{erfc}(bx)+\frac{12\int e^{-b^2x^2}x\,dx}{7b^5\sqrt{\pi}}\\
&= -\frac{6e^{-b^2x^2}}{7b^7\sqrt{\pi}}-\frac{6e^{-b^2x^2}x^2}{7b^5\sqrt{\pi}}-\frac{3e^{-b^2x^2}x^4}{7b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^6}{7b\sqrt{\pi}}+\frac{1}{7}x^7\operatorname{erfc}(bx)
\end{aligned}
$$

Mathematica [A]
time = 0.02, size = 73, normalized size = 0.67

$$\frac{e^{-b^2x^2}\left(-6-6b^2x^2-3b^4x^4-b^6x^6+b^7e^{b^2x^2}\sqrt{\pi}\,x^7\operatorname{Erfc}(bx)\right)}{7b^7\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^6*Erfc[b*x],x]
[Out] (-6 - 6*b^2*x^2 - 3*b^4*x^4 - b^6*x^6 + b^7*E^(b^2*x^2)*Sqrt[Pi]*x^7*Erfc[b
*x])/(7*b^7*E^(b^2*x^2)*Sqrt[Pi])
```

Maple [A]
time = 0.08, size = 90, normalized size = 0.83

method	result	size
derivativedivides	$\frac{\frac{b^7x^7\operatorname{erfc}(bx)}{7}+\frac{-\frac{e^{-b^2x^2}b^6x^6}{7}-\frac{3b^4x^4e^{-b^2x^2}}{7}-\frac{6b^2x^2e^{-b^2x^2}}{7}-\frac{6\,e^{-b^2x^2}}{7}}{\sqrt{\pi}}}{b^7}$	90
default	$\frac{\frac{b^7x^7\operatorname{erfc}(bx)}{7}+\frac{-\frac{e^{-b^2x^2}b^6x^6}{7}-\frac{3b^4x^4e^{-b^2x^2}}{7}-\frac{6b^2x^2e^{-b^2x^2}}{7}-\frac{6\,e^{-b^2x^2}}{7}}{\sqrt{\pi}}}{b^7}$	90

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^6*erfc(b*x),x,method=_RETURNVERBOSE)
```

[Out] 1/b^7*(1/7*b^7*x^7*erfc(b*x)+2/7/Pi^(1/2)*(-1/2*b^6*x^6/exp(b^2*x^2)-3/2*b^4*x^4/exp(b^2*x^2)-3*b^2*x^2/exp(b^2*x^2)-3/exp(b^2*x^2)))

Maxima [A]
time = 0.27, size = 52, normalized size = 0.48

$$\frac{1}{7}\,x^7\,\mathrm{erfc}\left(bx\right)-\frac{(b^6x^6+3\,b^4x^4+6\,b^2x^2+6)e^{(-b^2x^2)}}{7\,\sqrt{\pi}\,b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*erfc(b*x),x, algorithm="maxima")

[Out] 1/7*x^7*erfc(b*x) - 1/7*(b^6*x^6 + 3*b^4*x^4 + 6*b^2*x^2 + 6)*e^(-b^2*x^2)/(sqrt(pi)*b^7)

Fricas [A]
time = 0.35, size = 68, normalized size = 0.62

$$-\frac{\pi b^7x^7\,\mathrm{erf}\left(bx\right)-\pi b^7x^7+\sqrt{\pi}\,(b^6x^6+3\,b^4x^4+6\,b^2x^2+6)e^{(-b^2x^2)}}{7\,\pi b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^6*erfc(b*x),x, algorithm="fricas")

[Out] -1/7*(pi*b^7*x^7*erf(b*x) - pi*b^7*x^7 + sqrt(pi)*(b^6*x^6 + 3*b^4*x^4 + 6*b^2*x^2 + 6)*e^(-b^2*x^2))/(pi*b^7)

Sympy [A]
time = 0.73, size = 102, normalized size = 0.94

$$\begin{cases}\frac{x^7\,\mathrm{erfc}\,(bx)}{7}-\frac{x^6e^{-b^2x^2}}{7\sqrt{\pi}\,b}-\frac{3x^4e^{-b^2x^2}}{7\sqrt{\pi}\,b^3}-\frac{6x^2e^{-b^2x^2}}{7\sqrt{\pi}\,b^5}-\frac{6e^{-b^2x^2}}{7\sqrt{\pi}\,b^7} & \text{for}\ b\neq 0\\ \frac{x^7}{7} & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**6*erfc(b*x),x)

[Out] Piecewise((x**7*erfc(b*x)/7 - x**6*exp(-b**2*x**2)/(7*sqrt(pi)*b) - 3*x**4*exp(-b**2*x**2)/(7*sqrt(pi)*b**3) - 6*x**2*exp(-b**2*x**2)/(7*sqrt(pi)*b**5) - 6*exp(-b**2*x**2)/(7*sqrt(pi)*b**7), Ne(b, 0)), (x**7/7, True))

Giac [A]
time = 0.41, size = 57, normalized size = 0.52

$$-\frac{1}{7}\,x^7\,\mathrm{erf}\left(bx\right)+\frac{1}{7}\,x^7-\frac{(b^6x^6+3\,b^4x^4+6\,b^2x^2+6)e^{(-b^2x^2)}}{7\,\sqrt{\pi}\,b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^6*erfc(b*x),x, algorithm="giac")
```

```
[Out] -1/7*x^7*erf(b*x) + 1/7*x^7 - 1/7*(b^6*x^6 + 3*b^4*x^4 + 6*b^2*x^2 + 6)*e^(
-b^2*x^2)/(sqrt(pi)*b^7)
```

Mupad [B]
time = 0.29, size = 90, normalized size = 0.83

$$\frac{x^7\,\mathrm{erfc}(b\,x)}{7}-\frac{\frac{6\,\mathrm{e}^{-b^2\,x^2}}{7\,\sqrt{\pi}}+\frac{6\,b^2\,x^2\,\mathrm{e}^{-b^2\,x^2}}{7\,\sqrt{\pi}}+\frac{3\,b^4\,x^4\,\mathrm{e}^{-b^2\,x^2}}{7\,\sqrt{\pi}}+\frac{b^6\,x^6\,\mathrm{e}^{-b^2\,x^2}}{7\,\sqrt{\pi}}}{b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^6*erfc(b*x),x)
```

```
[Out] (x^7*erfc(b*x))/7 - ((6*exp(-b^2*x^2))/(7*pi^(1/2)) + (6*b^2*x^2*exp(-b^2*x
^2))/(7*pi^(1/2)) + (3*b^4*x^4*exp(-b^2*x^2))/(7*pi^(1/2)) + (b^6*x^6*exp(-
b^2*x^2))/(7*pi^(1/2)))/b^7
```

3.112 $\int x^4 \mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=84

$$-\frac{2e^{-b^2x^2}}{5b^5\sqrt{\pi}}-\frac{2e^{-b^2x^2}x^2}{5b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^4}{5b\sqrt{\pi}}+\frac{1}{5}x^5\mathrm{Erfc}(bx)$$

```
[Out] 1/5*x^5*erfc(b*x)-2/5/b^5/exp(b^2*x^2)/Pi^(1/2)-2/5*x^2/b^3/exp(b^2*x^2)/Pi
^(1/2)-1/5*x^4/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.05, antiderivative size = 84, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.375, Rules used = {6497, 2243, 2240}

$$-\frac{x^4e^{-b^2x^2}}{5\sqrt{\pi}\,b}-\frac{2e^{-b^2x^2}}{5\sqrt{\pi}\,b^5}-\frac{2x^2e^{-b^2x^2}}{5\sqrt{\pi}\,b^3}+\frac{1}{5}x^5\mathrm{Erfc}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x^4*Erfc[b*x],x]
```

```
[Out] -2/(5*b^5*E^(b^2*x^2)*Sqrt[Pi]) - (2*x^2)/(5*b^3*E^(b^2*x^2)*Sqrt[Pi]) - x^
4/(5*b*E^(b^2*x^2)*Sqrt[Pi]) + (x^5*Erfc[b*x])/5
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6497

```
Int[Erfc[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfc[a + b*x]/(d*(m + 1))), x] + Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int x^4\text{erfc}(bx)\,dx &= \frac{1}{5}x^5\text{erfc}(bx) + \frac{(2b)\int e^{-b^2x^2}x^5\,dx}{5\sqrt{\pi}}\\
&= -\frac{e^{-b^2x^2}x^4}{5b\sqrt{\pi}} + \frac{1}{5}x^5\text{erfc}(bx) + \frac{4\int e^{-b^2x^2}x^3\,dx}{5b\sqrt{\pi}}\\
&= -\frac{2e^{-b^2x^2}x^2}{5b^3\sqrt{\pi}} - \frac{e^{-b^2x^2}x^4}{5b\sqrt{\pi}} + \frac{1}{5}x^5\text{erfc}(bx) + \frac{4\int e^{-b^2x^2}x\,dx}{5b^3\sqrt{\pi}}\\
&= -\frac{2e^{-b^2x^2}}{5b^5\sqrt{\pi}} - \frac{2e^{-b^2x^2}x^2}{5b^3\sqrt{\pi}} - \frac{e^{-b^2x^2}x^4}{5b\sqrt{\pi}} + \frac{1}{5}x^5\text{erfc}(bx)
\end{aligned}
$$

Mathematica [A]
time = 0.01, size = 66, normalized size = 0.79

$$e^{-b^2x^2}\left(-\frac{2}{5b^5\sqrt{\pi}} - \frac{2x^2}{5b^3\sqrt{\pi}} - \frac{x^4}{5b\sqrt{\pi}}\right) + \frac{1}{5}x^5\text{Erfc}(bx)$$

Antiderivative was successfully verified.

```
[In] Integrate[x^4*Erfc[b*x],x]
[Out] (-2/(5*b^5*Sqrt[Pi]) - (2*x^2)/(5*b^3*Sqrt[Pi]) - x^4/(5*b*Sqrt[Pi]))/E^(b^
2*x^2) + (x^5*Erfc[b*x])/5
```

Maple [A]
time = 0.10, size = 72, normalized size = 0.86

method	result	size
derivativedivides	$\frac{\frac{b^5x^5\text{erfc}(bx)}{5}+\frac{-\frac{b^4x^4\text{e}^{-b^2x^2}}{5}-\frac{2b^2x^2\text{e}^{-b^2x^2}}{5}-\frac{2\,\text{e}^{-b^2x^2}}{5}}{\sqrt{\pi}}}{b^5}$	72
default	$\frac{\frac{b^5x^5\text{erfc}(bx)}{5}+\frac{-\frac{b^4x^4\text{e}^{-b^2x^2}}{5}-\frac{2b^2x^2\text{e}^{-b^2x^2}}{5}-\frac{2\,\text{e}^{-b^2x^2}}{5}}{\sqrt{\pi}}}{b^5}$	72

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erfc(b*x),x,method=_RETURNVERBOSE)
[Out] 1/b^5*(1/5*b^5*x^5*erfc(b*x)+2/5/Pi^(1/2)*(-1/2*b^4*x^4/exp(b^2*x^2)-b^2*x^
2/exp(b^2*x^2)-1/exp(b^2*x^2)))
```

Maxima [A]
time = 0.25, size = 44, normalized size = 0.52

$$\frac{1}{5}\,x^5\,\text{erfc}\left(bx\right) - \frac{(b^4x^4 + 2\,b^2x^2 + 2)e^{(-b^2x^2)}}{5\,\sqrt{\pi}\,b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfc(b*x),x, algorithm="maxima")
```

```
[Out] 1/5*x^5*erfc(b*x) - 1/5*(b^4*x^4 + 2*b^2*x^2 + 2)*e^(-b^2*x^2)/(sqrt(pi)*b^
5)
```

Fricas [A]
time = 0.36, size = 60, normalized size = 0.71

$$-\frac{\pi b^5 x^5 \operatorname{erf}(bx) - \pi b^5 x^5 + \sqrt{\pi}\,(b^4 x^4 + 2\,b^2 x^2 + 2)e^{(-b^2 x^2)}}{5\,\pi b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfc(b*x),x, algorithm="fricas")
```

```
[Out] -1/5*(pi*b^5*x^5*erf(b*x) - pi*b^5*x^5 + sqrt(pi)*(b^4*x^4 + 2*b^2*x^2 + 2)
*e^(-b^2*x^2))/(pi*b^5)
```

Sympy [A]
time = 0.39, size = 78, normalized size = 0.93

$$\begin{cases} \frac{x^5 \operatorname{erfc}(bx)}{5} - \frac{x^4 e^{-b^2x^2}}{5\sqrt{\pi}\,b} - \frac{2x^2 e^{-b^2x^2}}{5\sqrt{\pi}\,b^3} - \frac{2e^{-b^2x^2}}{5\sqrt{\pi}\,b^5} & \text{for } b \neq 0 \\ \frac{x^5}{5} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4*erfc(b*x),x)
```

```
[Out] Piecewise((x**5*erfc(b*x)/5 - x**4*exp(-b**2*x**2)/(5*sqrt(pi)*b) - 2*x**2*
exp(-b**2*x**2)/(5*sqrt(pi)*b**3) - 2*exp(-b**2*x**2)/(5*sqrt(pi)*b**5), Ne
(b, 0)), (x**5/5, True))
```

Giac [A]
time = 0.42, size = 49, normalized size = 0.58

$$-\frac{1}{5}\,x^5 \operatorname{erf}(bx) + \frac{1}{5}\,x^5 - \frac{(b^4x^4 + 2\,b^2x^2 + 2)e^{(-b^2x^2)}}{5\,\sqrt{\pi}\,b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfc(b*x),x, algorithm="giac")
```

```
[Out] -1/5*x^5*erf(b*x) + 1/5*x^5 - 1/5*(b^4*x^4 + 2*b^2*x^2 + 2)*e^(-b^2*x^2)/(s
qrt(pi)*b^5)
```

Mupad [B]
time = 0.23, size = 70, normalized size = 0.83

$$\frac{x^5\,\mathrm{erfc}(b\,x)}{5}-\frac{\frac{2\,\mathrm{e}^{-b^2\,x^2}}{5\,\sqrt{\pi}}+\frac{2\,b^2\,x^2\,\mathrm{e}^{-b^2\,x^2}}{5\,\sqrt{\pi}}+\frac{b^4\,x^4\,\mathrm{e}^{-b^2\,x^2}}{5\,\sqrt{\pi}}}{b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erfc(b*x),x)
```

```
[Out] (x^5*erfc(b*x))/5 - ((2*exp(-b^2*x^2))/(5*pi^(1/2)) + (2*b^2*x^2*exp(-b^2*x
^2))/(5*pi^(1/2)) + (b^4*x^4*exp(-b^2*x^2))/(5*pi^(1/2)))/b^5
```

3.113 $\int x^2 \mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=59

$$-\frac{e^{-b^2x^2}}{3b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^2}{3b\sqrt{\pi}}+\frac{1}{3}x^3\operatorname{Erfc}(bx)$$

```
[Out] 1/3*x^3*erfc(b*x)-1/3/b^3/exp(b^2*x^2)/Pi^(1/2)-1/3*x^2/b/exp(b^2*x^2)/Pi^(
1/2)
```

Rubi [A]
time = 0.03, antiderivative size = 59, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.375, Rules used = {6497, 2243, 2240}

$$-\frac{x^2e^{-b^2x^2}}{3\sqrt{\pi}\,b}-\frac{e^{-b^2x^2}}{3\sqrt{\pi}\,b^3}+\frac{1}{3}x^3\operatorname{Erfc}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x^2*Erfc[b*x],x]
```

```
[Out] -1/3*1/(b^3*E^(b^2*x^2)*Sqrt[Pi]) - x^2/(3*b*E^(b^2*x^2)*Sqrt[Pi]) + (x^3*E
rfc[b*x])/3
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6497

```
Int[Erfc[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfc[a + b*x]/(d*(m + 1))), x] + Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int x^2\text{erfc}(bx)\,dx &= \frac{1}{3}x^3\text{erfc}(bx)+\frac{(2b)\int e^{-b^2x^2}x^3\,dx}{3\sqrt{\pi}}\\
&= -\frac{e^{-b^2x^2}x^2}{3b\sqrt{\pi}}+\frac{1}{3}x^3\text{erfc}(bx)+\frac{2\int e^{-b^2x^2}x\,dx}{3b\sqrt{\pi}}\\
&= -\frac{e^{-b^2x^2}}{3b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^2}{3b\sqrt{\pi}}+\frac{1}{3}x^3\text{erfc}(bx)
\end{aligned}
$$

Mathematica [**A**]
time = 0.02, size = 42, normalized size = 0.71

$$\frac{1}{3}\left(-\frac{e^{-b^2x^2}(1+b^2x^2)}{b^3\sqrt{\pi}}+x^3\text{Erfc}(bx)\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*Erfc[b*x],x]
```

```
[Out] (-((1 + b^2*x^2)/(b^3*E^(b^2*x^2)*Sqrt[Pi])) + x^3*Erfc[b*x])/3
```

Maple [**A**]
time = 0.31, size = 54, normalized size = 0.92

method	result	size
derivativedivides	$\frac{\frac{b^3x^3\text{erfc}(bx)}{3}+\frac{-\frac{b^2x^2\mathrm{e}^{-b^2x^2}}{3}-\frac{\mathrm{e}^{-b^2x^2}}{3}}{\sqrt{\pi}}}{b^3}$	54
default	$\frac{\frac{b^3x^3\text{erfc}(bx)}{3}+\frac{-\frac{b^2x^2\mathrm{e}^{-b^2x^2}}{3}-\frac{\mathrm{e}^{-b^2x^2}}{3}}{\sqrt{\pi}}}{b^3}$	54

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfc(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b^3*(1/3*b^3*x^3*erfc(b*x)+2/3/Pi^(1/2)*(-1/2*b^2*x^2/exp(b^2*x^2)-1/2/ex
p(b^2*x^2)))
```

Maxima [**A**]
time = 0.26, size = 36, normalized size = 0.61

$$\frac{1}{3}\,x^3\,\text{erfc}\,(bx)-\frac{(b^2x^2+1)e^{(-b^2x^2)}}{3\,\sqrt{\pi}\,b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfc(b*x),x, algorithm="maxima")
```

```
[Out] 1/3*x^3*erfc(b*x) - 1/3*(b^2*x^2 + 1)*e^(-b^2*x^2)/(sqrt(pi)*b^3)
```

Fricas [A]
time = 0.38, size = 52, normalized size = 0.88

$$-\frac{\pi b^3 x^3 \operatorname{erf}(bx) - \pi b^3 x^3 + \sqrt{\pi}\,(b^2x^2+1)e^{(-b^2x^2)}}{3\,\pi b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfc(b*x),x, algorithm="fricas")
```

```
[Out] -1/3*(pi*b^3*x^3*erf(b*x) - pi*b^3*x^3 + sqrt(pi)*(b^2*x^2 + 1)*e^(-b^2*x^2
))/(pi*b^3)
```

Sympy [A]
time = 0.23, size = 54, normalized size = 0.92

$$\begin{cases} \frac{x^3 \operatorname{erfc}(bx)}{3} - \frac{x^2 e^{-b^2x^2}}{3\sqrt{\pi}\,b} - \frac{e^{-b^2x^2}}{3\sqrt{\pi}\,b^3} & \text{for } b \neq 0 \\ \frac{x^3}{3} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*erfc(b*x),x)
```

```
[Out] Piecewise((x**3*erfc(b*x)/3 - x**2*exp(-b**2*x**2)/(3*sqrt(pi)*b) - exp(-b*
*2*x**2)/(3*sqrt(pi)*b**3), Ne(b, 0)), (x**3/3, True))
```

Giac [A]
time = 0.43, size = 41, normalized size = 0.69

$$-\frac{1}{3}\,x^3 \operatorname{erf}(bx) + \frac{1}{3}\,x^3 - \frac{(b^2x^2+1)e^{(-b^2x^2)}}{3\,\sqrt{\pi}\,b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfc(b*x),x, algorithm="giac")
```

```
[Out] -1/3*x^3*erf(b*x) + 1/3*x^3 - 1/3*(b^2*x^2 + 1)*e^(-b^2*x^2)/(sqrt(pi)*b^3)
```

Mupad [B]
time = 0.15, size = 50, normalized size = 0.85

$$\frac{x^3\,\mathrm{erfc}(b\,x)}{3} - \frac{\frac{\mathrm{e}^{-b^2\,x^2}}{3\,\sqrt{\pi}} + \frac{b^2\,x^2\,\mathrm{e}^{-b^2\,x^2}}{3\,\sqrt{\pi}}}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfc(b*x),x)
```

```
[Out] (x^3*erfc(b*x))/3 - (exp(-b^2*x^2)/(3*pi^(1/2)) + (b^2*x^2*exp(-b^2*x^2))/(
3*pi^(1/2)))/b^3
```

3.114 $\int \mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=27

$$-\frac{e^{-b^2x^2}}{b\sqrt{\pi}}+x\text{Erfc}(bx)$$

[Out] x*erfc(b*x)-1/b/exp(b^2*x^2)/Pi^(1/2)

Rubi [A]
time = 0.00, antiderivative size = 27, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 4, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.250, Rules used = {6485}

$$x\text{Erfc}(bx)-\frac{e^{-b^2x^2}}{\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

[In] Int[Erfc[b*x],x]

[Out] -(1/(b*E^(b^2*x^2)*Sqrt[Pi])) + x*Erfc[b*x]

Rule 6485

```
Int[Erfc[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[(a + b*x)*(Erfc[a + b*x]/b)
, x] - Simp[1/(b*Sqrt[Pi]*E^(a + b*x)^2), x] /; FreeQ[{a, b}, x]
```

Rubi steps

$$\int \text{erfc}(bx)\,dx=-\frac{e^{-b^2x^2}}{b\sqrt{\pi}}+x\text{erfc}(bx)$$

Mathematica [A]
time = 0.00, size = 27, normalized size = 1.00

$$-\frac{e^{-b^2x^2}}{b\sqrt{\pi}}+x\text{Erfc}(bx)$$

Antiderivative was successfully verified.

[In] Integrate[Erfc[b*x],x]

[Out] -(1/(b*E^(b^2*x^2)*Sqrt[Pi])) + x*Erfc[b*x]

Maple [A]
time = 0.18, size = 27, normalized size = 1.00

method	result	size
derivativedivides	$\frac{bx\,\mathrm{erfc}(bx)-\frac{\mathrm{e}^{-b^2x^2}}{\sqrt{\pi}}}{b}$	27
default	$\frac{bx\,\mathrm{erfc}(bx)-\frac{\mathrm{e}^{-b^2x^2}}{\sqrt{\pi}}}{b}$	27

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*(b*x*erfc(b*x)-1/Pi^(1/2)*exp(-b^2*x^2))
```

Maxima [A]
time = 0.25, size = 26, normalized size = 0.96

$$\frac{bx\,\mathrm{erfc}\,(bx)-\frac{e^{\left(-b^2x^2\right)}}{\sqrt{\pi}}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x),x, algorithm="maxima")
```

```
[Out] (b*x*erfc(b*x) - e^(-b^2*x^2)/sqrt(pi))/b
```

Fricas [A]
time = 0.35, size = 35, normalized size = 1.30

$$-\frac{\pi bx\,\mathrm{erf}\,(bx)-\pi bx+\sqrt{\pi}\,e^{\left(-b^2x^2\right)}}{\pi b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x),x, algorithm="fricas")
```

```
[Out] -(pi*b*x*erf(b*x) - pi*b*x + sqrt(pi)*e^(-b^2*x^2))/(pi*b)
```

Sympy [A]
time = 0.15, size = 24, normalized size = 0.89

$$\begin{cases} x\,\mathrm{erfc}\,(bx)-\frac{e^{-b^2x^2}}{\sqrt{\pi}\,b} & \text{for}\ b\neq 0\\ x & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x),x)
```

```
[Out] Piecewise((x*erfc(b*x) - exp(-b**2*x**2)/(sqrt(pi)*b), Ne(b, 0)), (x, True)
)
```

Giac [A]
time = 0.40, size = 26, normalized size = 0.96

$$-x\,\mathrm{erf}\left(bx\right) + x - \frac{e^{\left(-b^2x^2\right)}}{\sqrt{\pi}\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x),x, algorithm="giac")
```

```
[Out] -x*erf(b*x) + x - e^(-b^2*x^2)/(sqrt(pi)*b)
```

Mupad [B]
time = 0.10, size = 24, normalized size = 0.89

$$x\,\mathrm{erfc}(b\,x) - \frac{\mathrm{e}^{-b^2\,x^2}}{b\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x),x)
```

```
[Out] x*erfc(b*x) - exp(-b^2*x^2)/(b*pi^(1/2))
```

3.115 $\int \frac{\mathbf{Erfc}(bx)}{x^2}\,dx$

Optimal. Leaf size=27

$$-\frac{\text{Erfc}(bx)}{x}-\frac{b\text{Ei}(-b^2x^2)}{\sqrt{\pi}}$$

```
[Out] -erfc(b*x)/x-b*Ei(-b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.02, antiderivative size = 27, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.250$, Rules used = {6497, 2241}

$$-\frac{b\text{Ei}(-b^2x^2)}{\sqrt{\pi}}-\frac{\text{Erfc}(bx)}{x}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]/x^2,x]
[Out] -(Erfc[b*x]/x) - (b*ExpIntegralEi[-(b^2*x^2)])/Sqrt[Pi]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 6497

```
Int[Erfc[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfc[a + b*x]/(d*(m + 1))), x] + Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{\text{erfc}(bx)}{x^2}\,dx &= -\frac{\text{erfc}(bx)}{x}-\frac{(2b)\int \frac{e^{-b^2x^2}}{x}\,dx}{\sqrt{\pi}}\\ &= -\frac{\text{erfc}(bx)}{x}-\frac{b\text{Ei}(-b^2x^2)}{\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 27, normalized size = 1.00

$$-\frac{\text{Erfc}(bx)}{x}-\frac{b\text{Ei}(-b^2x^2)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]/x^2,x]
```

```
[Out] -(Erfc[b*x]/x) - (b*ExpIntegralEi[-(b^2*x^2)])/Sqrt[Pi]
```

Maple [A]
time = 0.46, size = 29, normalized size = 1.07

method	result	size
derivativedivides	$b\left(-\frac{\operatorname{erfc}(bx)}{bx}+\frac{\operatorname{expIntegral}(1,b^2x^2)}{\sqrt{\pi}}\right)$	29
default	$b\left(-\frac{\operatorname{erfc}(bx)}{bx}+\frac{\operatorname{expIntegral}(1,b^2x^2)}{\sqrt{\pi}}\right)$	29

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/x^2,x,method=_RETURNVERBOSE)
```

```
[Out] b*(-1/b/x*erfc(b*x)+1/Pi^(1/2)*Ei(1,b^2*x^2))
```

Maxima [A]
time = 0.29, size = 25, normalized size = 0.93

$$-\frac{b\mathrm{Ei}(-b^2x^2)}{\sqrt{\pi}}-\frac{\operatorname{erfc}(bx)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x^2,x, algorithm="maxima")
```

```
[Out] -b*Ei(-b^2*x^2)/sqrt(pi) - erfc(b*x)/x
```

Fricas [A]
time = 0.35, size = 32, normalized size = 1.19

$$-\frac{\pi+\sqrt{\pi}\,bx\mathrm{Ei}(-b^2x^2)-\pi\operatorname{erf}(bx)}{\pi x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x^2,x, algorithm="fricas")
```

```
[Out] -(pi + sqrt(pi)*b*x*Ei(-b^2*x^2) - pi*erf(b*x))/(pi*x)
```

Sympy [A]
time = 0.65, size = 20, normalized size = 0.74

$$\frac{b\,\mathrm{E}_1\left(b^2x^2\right)}{\sqrt{\pi}}-\frac{\operatorname{erfc}(bx)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x**2,x)
```

```
[Out] b*expint(1, b**2*x**2)/sqrt(pi) - erfc(b*x)/x
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x^2,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)/x^2, x)
```

Mupad [B]
time = 0.15, size = 25, normalized size = 0.93

$$-\frac{\mathrm{erfc}(b\,x)}{x}-\frac{b\,\mathrm{ei}(-b^2\,x^2)}{\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/x^2,x)
```

```
[Out] - erfc(b*x)/x - (b*ei(-b^2*x^2))/pi^(1/2)
```

3.116 $\int \frac{\text{Erfc}(bx)}{x^4} dx$

Optimal. Leaf size=56

$$\frac{be^{-b^2x^2}}{3\sqrt{\pi}\,x^2} - \frac{\text{Erfc}(bx)}{3x^3} + \frac{b^3\text{Ei}(-b^2x^2)}{3\sqrt{\pi}}$$

```
[Out] -1/3*erfc(b*x)/x^3+1/3*b/exp(b^2*x^2)/x^2/Pi^(1/2)+1/3*b^3*Ei(-b^2*x^2)/Pi^
(1/2)
```

Rubi [A]
time = 0.03, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6497, 2245, 2241}

$$\frac{be^{-b^2x^2}}{3\sqrt{\pi}\,x^2} + \frac{b^3\text{Ei}(-b^2x^2)}{3\sqrt{\pi}} - \frac{\text{Erfc}(bx)}{3x^3}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]/x^4,x]
```

```
[Out] b/(3*E^(b^2*x^2)*Sqrt[Pi]*x^2) - Erfc[b*x]/(3*x^3) + (b^3*ExpIntegralEi[-(b
^2*x^2)])/(3*Sqrt[Pi])
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6497

```
Int[Erfc[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfc[a + b*x]/(d*(m + 1))), x] + Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{\operatorname{erfc}(bx)}{x^4}\,dx &= -\frac{\operatorname{erfc}(bx)}{3x^3} - \frac{(2b)\int \frac{e^{-b^2x^2}}{x^3}\,dx}{3\sqrt{\pi}}\\ &= \frac{be^{-b^2x^2}}{3\sqrt{\pi}\,x^2} - \frac{\operatorname{erfc}(bx)}{3x^3} + \frac{(2b^3)\int \frac{e^{-b^2x^2}}{x}\,dx}{3\sqrt{\pi}}\\ &= \frac{be^{-b^2x^2}}{3\sqrt{\pi}\,x^2} - \frac{\operatorname{erfc}(bx)}{3x^3} + \frac{b^3\operatorname{Ei}(-b^2x^2)}{3\sqrt{\pi}}\end{aligned}$$

Mathematica [**A**]
time = 0.03, size = 49, normalized size = 0.88

$$\frac{1}{3}\left(-\frac{\operatorname{Erfc}(bx)}{x^3} + \frac{b\left(\frac{e^{-b^2x^2}}{x^2} + b^2\operatorname{Ei}(-b^2x^2)\right)}{\sqrt{\pi}}\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]/x^4,x]
```

```
[Out] (-(Erfc[b*x]/x^3) + (b*(1/(E^(b^2*x^2)*x^2) + b^2*ExpIntegralEi[-(b^2*x^2)]
))/Sqrt[Pi])/3
```

Maple [**A**]
time = 0.21, size = 53, normalized size = 0.95

method	result	size
derivativedivides	$b^3\left(-\frac{\operatorname{erfc}(bx)}{3b^3x^3} - \frac{2\left(-\frac{e^{-b^2x^2}}{2b^2x^2} + \frac{\operatorname{expIntegral}\left(1,b^2x^2\right)}{2}\right)}{3\sqrt{\pi}}\right)$	53
default	$b^3\left(-\frac{\operatorname{erfc}(bx)}{3b^3x^3} - \frac{2\left(-\frac{e^{-b^2x^2}}{2b^2x^2} + \frac{\operatorname{expIntegral}\left(1,b^2x^2\right)}{2}\right)}{3\sqrt{\pi}}\right)$	53

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/x^4,x,method=_RETURNVERBOSE)
```

```
[Out] b^3*(-1/3/b^3/x^3*erfc(b*x)-2/3/Pi^(1/2)*(-1/2/exp(b^2*x^2)/b^2/x^2+1/2*Ei(
1,b^2*x^2)))
```

Maxima [A]
time = 0.29, size = 27, normalized size = 0.48

$$\frac{b^3\Gamma(-1,b^2x^2)}{3\sqrt{\pi}}-\frac{\operatorname{erfc}(bx)}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x^4,x, algorithm="maxima")
```

```
[Out] 1/3*b^3*gamma(-1, b^2*x^2)/sqrt(pi) - 1/3*erfc(b*x)/x^3
```

Fricas [A]
time = 0.35, size = 51, normalized size = 0.91

$$-\frac{\pi-\pi\operatorname{erf}(bx)-\sqrt{\pi}\left(b^3x^3\operatorname{Ei}(-b^2x^2)+bxe^{(-b^2x^2)}\right)}{3\,\pi x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x^4,x, algorithm="fricas")
```

```
[Out] -1/3*(pi - pi*erf(b*x) - sqrt(pi)*(b^3*x^3*Ei(-b^2*x^2) + b*x*e^(-b^2*x^2))
)/(pi*x^3)
```

Sympy [A]
time = 1.15, size = 48, normalized size = 0.86

$$-\frac{b^3\operatorname{E}_1(b^2x^2)}{3\sqrt{\pi}}+\frac{be^{-b^2x^2}}{3\sqrt{\pi}\,x^2}-\frac{\operatorname{erfc}(bx)}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x**4,x)
```

```
[Out] -b**3*expint(1, b**2*x**2)/(3*sqrt(pi)) + b*exp(-b**2*x**2)/(3*sqrt(pi)*x**
2) - erfc(b*x)/(3*x**3)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x^4,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)/x^4, x)
```

Mupad [B]
time = 0.18, size = 46, normalized size = 0.82

$$\frac{b^3 \operatorname{ei}(-b^2 x^2)}{3 \sqrt{\pi}} - \frac{\frac{\operatorname{erfc}(b x)}{3} - \frac{b x e^{-b^2 x^2}}{3 \sqrt{\pi}}}{x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/x^4,x)
```

```
[Out] (b^3*ei(-b^2*x^2))/(3*pi^(1/2)) - (erfc(b*x)/3 - (b*x*exp(-b^2*x^2))/(3*pi^
(1/2)))/x^3
```

3.117 $\int \frac{\mathbf{Erfc}(bx)}{x^6} dx$

Optimal. Leaf size=81

$$\frac{be^{-b^2x^2}}{10\sqrt{\pi}\,x^4}-\frac{b^3e^{-b^2x^2}}{10\sqrt{\pi}\,x^2}-\frac{\text{Erfc}(bx)}{5x^5}-\frac{b^5\text{Ei}(-b^2x^2)}{10\sqrt{\pi}}$$

```
[Out] -1/5*erfc(b*x)/x^5+1/10*b/exp(b^2*x^2)/x^4/Pi^(1/2)-1/10*b^3/exp(b^2*x^2)/x
^2/Pi^(1/2)-1/10*b^5*Ei(-b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.05, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6497, 2245, 2241}

$$\frac{be^{-b^2x^2}}{10\sqrt{\pi}\,x^4}-\frac{b^5\text{Ei}(-b^2x^2)}{10\sqrt{\pi}}-\frac{b^3e^{-b^2x^2}}{10\sqrt{\pi}\,x^2}-\frac{\text{Erfc}(bx)}{5x^5}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]/x^6,x]
```

```
[Out] b/(10*E^(b^2*x^2)*Sqrt[Pi]*x^4) - b^3/(10*E^(b^2*x^2)*Sqrt[Pi]*x^2) - Erfc[
b*x]/(5*x^5) - (b^5*ExpIntegralEi[-(b^2*x^2)])/(10*Sqrt[Pi])
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6497

```
Int[Erfc[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfc[a + b*x]/(d*(m + 1))), x] + Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{\mathrm{erfc}(bx)}{x^6}\,dx &= -\frac{\mathrm{erfc}(bx)}{5x^5}-\frac{(2b)\int \frac{e^{-b^2x^2}}{x^5}\,dx}{5\sqrt{\pi}}\\
&=\frac{be^{-b^2x^2}}{10\sqrt{\pi}\,x^4}-\frac{\mathrm{erfc}(bx)}{5x^5}+\frac{b^3\int \frac{e^{-b^2x^2}}{x^3}\,dx}{5\sqrt{\pi}}\\
&=\frac{be^{-b^2x^2}}{10\sqrt{\pi}\,x^4}-\frac{b^3e^{-b^2x^2}}{10\sqrt{\pi}\,x^2}-\frac{\mathrm{erfc}(bx)}{5x^5}-\frac{b^5\int \frac{e^{-b^2x^2}}{x}\,dx}{5\sqrt{\pi}}\\
&=\frac{be^{-b^2x^2}}{10\sqrt{\pi}\,x^4}-\frac{b^3e^{-b^2x^2}}{10\sqrt{\pi}\,x^2}-\frac{\mathrm{erfc}(bx)}{5x^5}-\frac{b^5\mathrm{Ei}(-b^2x^2)}{10\sqrt{\pi}}
\end{aligned}
$$

Mathematica [A]
time = 0.02, size = 73, normalized size = 0.90

$$
e^{-b^2x^2}\left(\frac{b}{10\sqrt{\pi}\,x^4}-\frac{b^3}{10\sqrt{\pi}\,x^2}\right)-\frac{\mathrm{Erfc}(bx)}{5x^5}-\frac{b^5\mathrm{Ei}(-b^2x^2)}{10\sqrt{\pi}}
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]/x^6,x]
```

```
[Out] (b/(10*Sqrt[Pi]*x^4) - b^3/(10*Sqrt[Pi]*x^2))/E^(b^2*x^2) - Erfc[b*x]/(5*x^
5) - (b^5*ExpIntegralEi[-(b^2*x^2)])/(10*Sqrt[Pi])
```

Maple [A]
time = 0.20, size = 71, normalized size = 0.88

method	result	size
derivativedivides	$b^5\left(-\frac{\mathrm{erfc}(bx)}{5b^5x^5}-\frac{2\left(-\frac{\mathrm{e}^{-b^2x^2}}{4b^4x^4}+\frac{\mathrm{e}^{-b^2x^2}}{4b^2x^2}-\frac{\mathrm{expIntegral}\left(1,b^2x^2\right)}{4}\right)}{5\sqrt{\pi}}\right)$	71
default	$b^5\left(-\frac{\mathrm{erfc}(bx)}{5b^5x^5}-\frac{2\left(-\frac{\mathrm{e}^{-b^2x^2}}{4b^4x^4}+\frac{\mathrm{e}^{-b^2x^2}}{4b^2x^2}-\frac{\mathrm{expIntegral}\left(1,b^2x^2\right)}{4}\right)}{5\sqrt{\pi}}\right)$	71

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/x^6,x,method=_RETURNVERBOSE)
```

```
[Out] b^5*(-1/5/b^5/x^5*erfc(b*x)-2/5/Pi^(1/2)*(-1/4/exp(b^2*x^2)/b^4/x^4+1/4/exp
(b^2*x^2)/b^2/x^2-1/4*Ei(1,b^2*x^2)))
```

Maxima [A]
time = 0.30, size = 27, normalized size = 0.33

$$\frac{b^5\Gamma(-2,b^2x^2)}{5\sqrt{\pi}} - \frac{\operatorname{erfc}(bx)}{5\,x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x^6,x, algorithm="maxima")
```

```
[Out] 1/5*b^5*gamma(-2, b^2*x^2)/sqrt(pi) - 1/5*erfc(b*x)/x^5
```

Fricas [A]
time = 0.38, size = 62, normalized size = 0.77

$$-\frac{2\,\pi - 2\,\pi\operatorname{erf}(bx) + \sqrt{\pi}\left(b^5x^5\operatorname{Ei}(-b^2x^2) + (b^3x^3 - bx)e^{(-b^2x^2)}\right)}{10\,\pi x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x^6,x, algorithm="fricas")
```

```
[Out] -1/10*(2*pi - 2*pi*erf(b*x) + sqrt(pi)*(b^5*x^5*Ei(-b^2*x^2) + (b^3*x^3 - b
*x)*e^(-b^2*x^2)))/(pi*x^5)
```

Sympy [A]
time = 2.03, size = 70, normalized size = 0.86

$$\frac{b^5\operatorname{E}_1(b^2x^2)}{10\sqrt{\pi}} - \frac{b^3e^{-b^2x^2}}{10\sqrt{\pi}\,x^2} + \frac{be^{-b^2x^2}}{10\sqrt{\pi}\,x^4} - \frac{\operatorname{erfc}(bx)}{5x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x**6,x)
```

```
[Out] b**5*expint(1, b**2*x**2)/(10*sqrt(pi)) - b**3*exp(-b**2*x**2)/(10*sqrt(pi)
*x**2) + b*exp(-b**2*x**2)/(10*sqrt(pi)*x**4) - erfc(b*x)/(5*x**5)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/x^6,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)/x^6, x)
```

Mupad [B]
time = 0.19, size = 66, normalized size = 0.81

$$-\frac{\frac{\mathrm{erfc}(b\,x)}{5}+\frac{b^3\,x^3\,\mathrm{e}^{-b^2\,x^2}}{10\,\sqrt{\pi}}-\frac{b\,x\,\mathrm{e}^{-b^2\,x^2}}{10\,\sqrt{\pi}}}{x^5}-\frac{b^5\,\mathrm{ei}\left(-b^2\,x^2\right)}{10\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/x^6,x)
```

```
[Out] - (erfc(b*x)/5 + (b^3*x^3*exp(-b^2*x^2))/(10*pi^(1/2)) - (b*x*exp(-b^2*x^2)
)/(10*pi^(1/2)))/x^5 - (b^5*ei(-b^2*x^2))/(10*pi^(1/2))
```

3.118 $\int (c+dx)^3 \mathbf{Erfc}(a+bx)\,dx$

Optimal. Leaf size=292

$$-\frac{d^2(bc-ad)e^{-(a+bx)^2}}{b^4\sqrt{\pi}}-\frac{(bc-ad)^3e^{-(a+bx)^2}}{b^4\sqrt{\pi}}-\frac{3d^3e^{-(a+bx)^2}(a+bx)}{8b^4\sqrt{\pi}}-\frac{3d(bc-ad)^2e^{-(a+bx)^2}(a+bx)}{2b^4\sqrt{\pi}}-\frac{d^2(bc-}{}$$

```
[Out] 3/16*d^3*erf(b*x+a)/b^4+3/4*d*(-a*d+b*c)^2*erf(b*x+a)/b^4+1/4*(-a*d+b*c)^4*
erf(b*x+a)/b^4/d+1/4*(d*x+c)^4*erfc(b*x+a)/d-d^2*(-a*d+b*c)/b^4/exp((b*x+a)
^2)/Pi^(1/2)-(-a*d+b*c)^3/b^4/exp((b*x+a)^2)/Pi^(1/2)-3/8*d^3*(b*x+a)/b^4/e
xp((b*x+a)^2)/Pi^(1/2)-3/2*d*(-a*d+b*c)^2*(b*x+a)/b^4/exp((b*x+a)^2)/Pi^(1/
2)-d^2*(-a*d+b*c)*(b*x+a)^2/b^4/exp((b*x+a)^2)/Pi^(1/2)-1/4*d^3*(b*x+a)^3/b
^4/exp((b*x+a)^2)/Pi^(1/2)
```

Rubi [A]
time = 0.20, antiderivative size = 292, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 5, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.357$, Rules used = {6497, 2258, 2236, 2240, 2243}

$$-\frac{d^2e^{-(a+bx)^2}(a+bx)^2(bc-ad)}{\sqrt{\pi}\,b^4}-\frac{d^2e^{-(a+bx)^2}(bc-ad)}{\sqrt{\pi}\,b^4}+\frac{(bc-ad)^4\text{Erf}(a+bx)}{4b^4d}+\frac{3d(bc-ad)^2\text{Erf}(a+bx)}{4b^4}-\frac{e^{-(a+bx)^2}(bc-ad)^3}{\sqrt{\pi}\,b^4}-\frac{3de^{-(a+bx)^2}(a+bx)(bc-ad)^2}{2\sqrt{\pi}\,b^4}+\frac{3d^3\text{Erf}(a+bx)}{16b^4}-\frac{d^3e^{-(a+bx)^2}(a+bx)^3}{4\sqrt{\pi}\,b^4}-\frac{3d^3e^{-(a+bx)^2}(a+bx)}{8\sqrt{\pi}\,b^4}+\frac{(c+dx)^4\text{Erfc}(a+bx)}{4d}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)^3*Erfc[a + b*x],x]
```

```
[Out] -((d^2*(b*c - a*d))/(b^4*E^(a + b*x)^2*Sqrt[Pi])) - (b*c - a*d)^3/(b^4*E^(a
 + b*x)^2*Sqrt[Pi]) - (3*d^3*(a + b*x))/(8*b^4*E^(a + b*x)^2*Sqrt[Pi]) - (3
*d*(b*c - a*d)^2*(a + b*x))/(2*b^4*E^(a + b*x)^2*Sqrt[Pi]) - (d^2*(b*c - a*
d)*(a + b*x)^2)/(b^4*E^(a + b*x)^2*Sqrt[Pi]) - (d^3*(a + b*x)^3)/(4*b^4*E^(
a + b*x)^2*Sqrt[Pi]) + (3*d^3*Erf[a + b*x])/(16*b^4) + (3*d*(b*c - a*d)^2*E
rf[a + b*x])/(4*b^4) + ((b*c - a*d)^4*Erf[a + b*x])/(4*b^4*d) + ((c + d*x)^
4*Erfc[a + b*x])/(4*d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 2258

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*(u_), x_Symbol] :> Int[E
xpandLinearProduct[F^(a + b*(c + d*x)^n), u, c, d, x], x] /; FreeQ[{F, a, b
, c, d, n}, x] && PolynomialQ[u, x]
```

Rule 6497

```
Int[Erfc[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfc[a + b*x]/(d*(m + 1))), x] + Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$\int (c+dx)^3\text{erfc}(a+bx)\,dx = \frac{(c+dx)^4\text{erfc}(a+bx)}{4d}+\frac{b\int e^{-(a+bx)^2}(c+dx)^4\,dx}{2d\sqrt{\pi}}$$

$$= \frac{(c+dx)^4\text{erfc}(a+bx)}{4d}+\frac{b\int\left(\frac{(bc-ad)^4e^{-(a+bx)^2}}{b^4}+\frac{4d(bc-ad)^3e^{-(a+bx)^2}(a+bx)}{b^4}+\frac{6d^2(bc-\cdots}{\cdots}\right.}{\cdots}$$

$$= \frac{(c+dx)^4\text{erfc}(a+bx)}{4d}+\frac{d^3\int e^{-(a+bx)^2}(a+bx)^4\,dx}{2b^3\sqrt{\pi}}+\frac{\left(2d^2(bc-ad)\right)\int e^{-(a+bx}\cdots}{b^3\sqrt{\pi}}$$

$$= -\frac{(bc-ad)^3e^{-(a+bx)^2}}{b^4\sqrt{\pi}}-\frac{3d(bc-ad)^2e^{-(a+bx)^2}(a+bx)}{2b^4\sqrt{\pi}}-\frac{d^2(bc-ad)e^{-(a+bx)^2}}{b^4\sqrt{\pi}}\cdots$$

$$= -\frac{d^2(bc-ad)e^{-(a+bx)^2}}{b^4\sqrt{\pi}}-\frac{(bc-ad)^3e^{-(a+bx)^2}}{b^4\sqrt{\pi}}-\frac{3d^3e^{-(a+bx)^2}(a+bx)}{8b^4\sqrt{\pi}}-\frac{3d(bc\cdots}{\cdots}$$

$$= -\frac{d^2(bc-ad)e^{-(a+bx)^2}}{b^4\sqrt{\pi}}-\frac{(bc-ad)^3e^{-(a+bx)^2}}{b^4\sqrt{\pi}}-\frac{3d^3e^{-(a+bx)^2}(a+bx)}{8b^4\sqrt{\pi}}-\frac{3d(bc\cdots}{\cdots}$$

Mathematica [A]
time = 0.24, size = 268, normalized size = 0.92

$$\frac{e^{-(a+bx)^2}\left(2a(5+2a^2)\,d^3-2bd^2(8(1+a^2)\,c+(3+2a^2)\,dx)+4ab^2d(6c^2+4cdx+d^2x^2)-4b^3(4c^3+6c^2dx+4cd^2x^2+d^3x^3)+(-16a^3bcd^2+4a^4d^3-8a(2b^3c^3+3bcd^2)+12a^2(2b^2c^2d+d^3)+3(4b^2c^2d+d^3))\,e^{(a+bx)^2}\sqrt{\pi}\,\text{Erf}(a+bx)+4b^4e^{(a+bx)^2}\sqrt{\pi}\,x(4c^3+6c^2dx+4cd^2x^2+d^3x^3)\,\text{Erfc}(a+bx)\right)}{16b^4\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^3*Erfc[a + b*x],x]
```

```
[Out] (2*a*(5 + 2*a^2)*d^3 - 2*b*d^2*(8*(1 + a^2)*c + (3 + 2*a^2)*d*x) + 4*a*b^2*
d*(6*c^2 + 4*c*d*x + d^2*x^2) - 4*b^3*(4*c^3 + 6*c^2*d*x + 4*c*d^2*x^2 + d^
3*x^3) + (-16*a^3*b*c*d^2 + 4*a^4*d^3 - 8*a*(2*b^3*c^3 + 3*b*c*d^2) + 12*a^
2*(2*b^2*c^2*d + d^3) + 3*(4*b^2*c^2*d + d^3))*E^(a + b*x)^2*Sqrt[Pi]*Erf[a
 + b*x] + 4*b^4*E^(a + b*x)^2*Sqrt[Pi]*x*(4*c^3 + 6*c^2*d*x + 4*c*d^2*x^2 +
 d^3*x^3)*Erfc[a + b*x])/(16*b^4*E^(a + b*x)^2*Sqrt[Pi])
```

Maple [B] Leaf count of result is larger than twice the leaf count of optimal. 728 vs. $2(260) = 520$.
time = 0.44, size = 729, normalized size = 2.50 Too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^3*erfc(b*x+a),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*(1/4/b^3*d^3*erfc(b*x+a)*a^4-1/b^2*d^2*erfc(b*x+a)*a^3*c-1/b^3*d^3*erfc
(b*x+a)*a^3*(b*x+a)+3/2/b*d*erfc(b*x+a)*a^2*c^2+3/b^2*d^2*erfc(b*x+a)*a^2*c
*(b*x+a)+3/2/b^3*d^3*erfc(b*x+a)*a^2*(b*x+a)^2-erfc(b*x+a)*a*c^3-3/b*d*erfc
(b*x+a)*a*c^2*(b*x+a)-3/b^2*d^2*erfc(b*x+a)*a*c*(b*x+a)^2-1/b^3*d^3*erfc(b*
x+a)*a*(b*x+a)^3+1/4*b/d*erfc(b*x+a)*c^4+erfc(b*x+a)*c^3*(b*x+a)+3/2/b*d*er
fc(b*x+a)*c^2*(b*x+a)^2+1/b^2*d^2*erfc(b*x+a)*c*(b*x+a)^3+1/4/b^3*d^3*erfc(
b*x+a)*(b*x+a)^4+1/2/b^3/d/Pi^(1/2)*(1/2*a^4*d^4*Pi^(1/2)*erf(b*x+a)+1/2*b^
4*c^4*Pi^(1/2)*erf(b*x+a)+d^4*(-1/2/exp((b*x+a)^2)*(b*x+a)^3-3/4*(b*x+a)/ex
p((b*x+a)^2)+3/8*Pi^(1/2)*erf(b*x+a))-4*a*d^4*(-1/2/exp((b*x+a)^2)*(b*x+a)^
2-1/2/exp((b*x+a)^2))+6*a^2*d^4*(-1/2*(b*x+a)/exp((b*x+a)^2)+1/4*Pi^(1/2)*e
rf(b*x+a))+2*a^3*d^4/exp((b*x+a)^2)-2*a*b^3*c^3*d*Pi^(1/2)*erf(b*x+a)+3*a^2
*b^2*c^2*d^2*Pi^(1/2)*erf(b*x+a)-2*a^3*b*c*d^3*Pi^(1/2)*erf(b*x+a)+4*b*c*d^
3*(-1/2/exp((b*x+a)^2)*(b*x+a)^2-1/2/exp((b*x+a)^2))+6*b^2*c^2*d^2*(-1/2*(b
*x+a)/exp((b*x+a)^2)+1/4*Pi^(1/2)*erf(b*x+a))-2*b^3*c^3*d/exp((b*x+a)^2)-12
*a*b*c*d^3*(-1/2*(b*x+a)/exp((b*x+a)^2)+1/4*Pi^(1/2)*erf(b*x+a))+6*a*b^2*c^
2*d^2/exp((b*x+a)^2)-6*a^2*b*c*d^3/exp((b*x+a)^2)))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^3*erfc(b*x+a),x, algorithm="maxima")
```

```
[Out] integrate((d*x + c)^3*erfc(b*x + a), x)
```

Fricas [A]
time = 0.37, size = 314, normalized size = 1.08

$$\frac{4\pi b^4d^3x^4 + 16\pi b^4cd^2x^3 + 24\pi b^4c^2dx^2 + 16\pi b^4c^3x - 2\sqrt{\pi}\,(2b^3d^3x^3 + 8b^3c^3 - 12ab^2c^2d + 8(a^2+1)bcd^2 - (2a^3+5a)d^3 + 2(4b^3cd^2 - ab^2d^3)x^2 + (12b^3c^2d - 8ab^2cd^2 + (2a^2+3)bd^3)x)e^{(-b^2x^2-2abx-a^2)} - (4\pi b^4d^3x^4 + 16\pi b^4cd^2x^3 + 24\pi b^4c^2dx^2 + 16\pi b^4c^3x + \pi(16ab^3c^3 - 12(2a^2+1)b^2c^2d + 8(2a^3+3a)bcd^2 - (4a^4+12a^2+3)d^3))\operatorname{erf}(bx+a)}{16\pi b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^3*erfc(b*x+a),x, algorithm="fricas")
```

```
[Out] 1/16*(4*pi*b^4*d^3*x^4 + 16*pi*b^4*c*d^2*x^3 + 24*pi*b^4*c^2*d*x^2 + 16*pi*
b^4*c^3*x - 2*sqrt(pi)*(2*b^3*d^3*x^3 + 8*b^3*c^3 - 12*a*b^2*c^2*d + 8*(a^2
 + 1)*b*c*d^2 - (2*a^3 + 5*a)*d^3 + 2*(4*b^3*c*d^2 - a*b^2*d^3)*x^2 + (12*b
^3*c^2*d - 8*a*b^2*c*d^2 + (2*a^2 + 3)*b*d^3)*x)*e^(-b^2*x^2 - 2*a*b*x - a^
2) - (4*pi*b^4*d^3*x^4 + 16*pi*b^4*c*d^2*x^3 + 24*pi*b^4*c^2*d*x^2 + 16*pi*
b^4*c^3*x + pi*(16*a*b^3*c^3 - 12*(2*a^2 + 1)*b^2*c^2*d + 8*(2*a^3 + 3*a)*b
*c*d^2 - (4*a^4 + 12*a^2 + 3)*d^3))*erf(b*x + a))/(pi*b^4)
```

Sympy [B] Leaf count of result is larger than twice the leaf count of optimal. 746 vs. $2(258) = 516$.
time = 2.34, size = 746, normalized size = 2.55

$$\begin{cases} -\frac{a^4d^3\operatorname{erfc}(a+bx)}{4b^4} + \frac{a^3cd^2\operatorname{erfc}(a+bx)}{b^3} + \frac{a^3d^3e^{-a^2}e^{-b^2x^2}e^{-2abx}}{4\sqrt{\pi}\,b^4} - \frac{3a^2c^2d\operatorname{erfc}(a+bx)}{2b^2} - \frac{a^2cd^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}\,b^3} - \frac{a^2d^3xe^{-a^2}e^{-b^2x^2}e^{-2abx}}{4\sqrt{\pi}\,b^3} - \frac{3a^2d^3\operatorname{erfc}(a+bx)}{4b^4} + \frac{ac^3\operatorname{erfc}(a+bx)}{b} + \frac{3ac^2de^{-a^2}e^{-b^2x^2}e^{-2abx}}{2\sqrt{\pi}\,b^2} + \frac{acd^2xe^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}\,b^2} + \frac{ad^3x^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{4\sqrt{\pi}\,b^2} + \frac{3acd^2\operatorname{erfc}(a+bx)}{2b^3} + \frac{5ad^3e^{-a^2}e^{-b^2x^2}e^{-2abx}}{8\sqrt{\pi}\,b^4} + c^3x\operatorname{erfc}(a+bx) + \frac{3c^2dx^2\operatorname{erfc}(a+bx)}{2} + cd^2x^3\operatorname{erfc}(a+bx) + \frac{d^3x^4\operatorname{erfc}(a+bx)}{4} - \frac{c^3e^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}\,b} - \frac{3c^2dxe^{-a^2}e^{-b^2x^2}e^{-2abx}}{2\sqrt{\pi}\,b} - \frac{cd^2x^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}\,b} - \frac{d^3x^3e^{-a^2}e^{-b^2x^2}e^{-2abx}}{4\sqrt{\pi}\,b} - \frac{3c^2d\operatorname{erfc}(a+bx)}{4b^2} - \frac{cd^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}\,b^3} - \frac{3d^3xe^{-a^2}e^{-b^2x^2}e^{-2abx}}{8\sqrt{\pi}\,b^3} - \frac{3d^3\operatorname{erfc}(a+bx)}{16b^4} & \text{for}\ b \neq 0 \\ \left(c^3x + \frac{3c^2dx^2}{2} + cd^2x^3 + \frac{d^3x^4}{4}\right)\operatorname{erfc}(a) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**3*erfc(b*x+a),x)
```

```
[Out] Piecewise((-a**4*d**3*erfc(a + b*x)/(4*b**4) + a**3*c*d**2*erfc(a + b*x)/b*
*3 + a**3*d**3*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(4*sqrt(pi)*b**4) -
 3*a**2*c**2*d*erfc(a + b*x)/(2*b**2) - a**2*c*d**2*exp(-a**2)*exp(-b**2*x*
*2)*exp(-2*a*b*x)/(sqrt(pi)*b**3) - a**2*d**3*x*exp(-a**2)*exp(-b**2*x**2)*
exp(-2*a*b*x)/(4*sqrt(pi)*b**3) - 3*a**2*d**3*erfc(a + b*x)/(4*b**4) + a*c*
*3*erfc(a + b*x)/b + 3*a*c**2*d*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(2
*sqrt(pi)*b**2) + a*c*d**2*x*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(sqrt
(pi)*b**2) + a*d**3*x**2*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(4*sqrt(p
i)*b**2) + 3*a*c*d**2*erfc(a + b*x)/(2*b**3) + 5*a*d**3*exp(-a**2)*exp(-b**
2*x**2)*exp(-2*a*b*x)/(8*sqrt(pi)*b**4) + c**3*x*erfc(a + b*x) + 3*c**2*d*x
**2*erfc(a + b*x)/2 + c*d**2*x**3*erfc(a + b*x) + d**3*x**4*erfc(a + b*x)/4
 - c**3*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(sqrt(pi)*b) - 3*c**2*d*x*
exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(2*sqrt(pi)*b) - c*d**2*x**2*exp(-
a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(sqrt(pi)*b) - d**3*x**3*exp(-a**2)*exp
(-b**2*x**2)*exp(-2*a*b*x)/(4*sqrt(pi)*b) - 3*c**2*d*erfc(a + b*x)/(4*b**2)
 - c*d**2*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(sqrt(pi)*b**3) - 3*d**3
*x*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(8*sqrt(pi)*b**3) - 3*d**3*erfc
(a + b*x)/(16*b**4), Ne(b, 0)), ((c**3*x + 3*c**2*d*x**2/2 + c*d**2*x**3 +
d**3*x**4/4)*erfc(a), True))
```

Giac [A]
time = 0.55, size = 435, normalized size = 1.49

$$\frac{1}{4}d^3x^4 + cd^2x^3 + \frac{3}{2}c^2dx^2 - \left(x\operatorname{erf}(bx+a) - \frac{\frac{\sqrt{\pi}\,a\operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b} - \frac{e^{\left(-b^2x^2-2\,abx-a^2\right)}}{b}}{\sqrt{\pi}}\right)c^3 - \frac{3}{4}\left(2\,x^2\operatorname{erf}(bx+a) + \frac{\frac{\sqrt{\pi}\,(2\,a^2+1)\operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b} + \frac{2\left(b\left(x+\frac{a}{b}\right)-2\,a\right)e^{\left(-b^2x^2-2\,abx-a^2\right)}}{b}}{\sqrt{\pi}\,b}\right)c^2d - \frac{1}{2}\left(2\,x^3\operatorname{erf}(bx+a) - \frac{\frac{\sqrt{\pi}\,(2\,a^3+3\,a)\operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b} - \frac{2\left(b^2\left(x+\frac{a}{b}\right)^2-3\,ab\left(x+\frac{a}{b}\right)+3\,a^2+1\right)e^{\left(-b^2x^2-2\,abx-a^2\right)}}{b}}{\sqrt{\pi}\,b^2}\right)cd^2 - \frac{1}{16}\left(4\,x^4\operatorname{erf}(bx+a) + \frac{\frac{\sqrt{\pi}\,(4\,a^4+12\,a^2+3)\operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b} + \frac{2\left(2\,b^3\left(x+\frac{a}{b}\right)^3-8\,ab^2\left(x+\frac{a}{b}\right)^2+12\,a^2b\left(x+\frac{a}{b}\right)-8\,a^3+3\,b\left(x+\frac{a}{b}\right)-8\,a\right)e^{\left(-b^2x^2-2\,abx-a^2\right)}}{b}}{\sqrt{\pi}\,b^3}\right)d^3 + c^3x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^3*erfc(b*x+a),x, algorithm="giac")
```

```
[Out] 1/4*d^3*x^4 + c*d^2*x^3 + 3/2*c^2*d*x^2 - (x*erf(b*x + a) - (sqrt(pi)*a*erf
(-b*(x + a/b))/b - e^(-b^2*x^2 - 2*a*b*x - a^2)/b)/sqrt(pi))*c^3 - 3/4*(2*x
^2*erf(b*x + a) + (sqrt(pi)*(2*a^2 + 1)*erf(-b*(x + a/b))/b + 2*(b*(x + a/b
) - 2*a)*e^(-b^2*x^2 - 2*a*b*x - a^2)/b)/(sqrt(pi)*b))*c^2*d - 1/2*(2*x^3*e
rf(b*x + a) - (sqrt(pi)*(2*a^3 + 3*a)*erf(-b*(x + a/b))/b - 2*(b^2*(x + a/b
)^2 - 3*a*b*(x + a/b) + 3*a^2 + 1)*e^(-b^2*x^2 - 2*a*b*x - a^2)/b)/(sqrt(pi
)*b^2))*c*d^2 - 1/16*(4*x^4*erf(b*x + a) + (sqrt(pi)*(4*a^4 + 12*a^2 + 3)*e
rf(-b*(x + a/b))/b + 2*(2*b^3*(x + a/b)^3 - 8*a*b^2*(x + a/b)^2 + 12*a^2*b*
(x + a/b) - 8*a^3 + 3*b*(x + a/b) - 8*a)*e^(-b^2*x^2 - 2*a*b*x - a^2)/b)/(s
qrt(pi)*b^3))*d^3 + c^3*x
```

Mupad [B]
time = 0.39, size = 352, normalized size = 1.21

$$\frac{d^3\,x^4\,\mathrm{erfc}(a+b\,x)}{4}-\frac{\mathrm{erfc}(a+b\,x)\,\left(b^2\,\left(\frac{3\,d\,a^2\,c^2}{2}+\frac{3\,d\,c^2}{4}\right)-b\,\left(c\,a^3\,d^2+\frac{3\,c\,a\,d^2}{2}\right)+\frac{3\,d^3}{16}+\frac{3\,a^2\,d^3}{4}+\frac{a^4\,d^3}{4}-a\,b^3\,c^3\right)}{b^4}+c^3\,x\,\mathrm{erfc}(a+b\,x)+\frac{\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}\,\left(2\,a^3\,d^3-8\,a^2\,b\,c\,d^2+12\,a\,b^2\,c^2\,d+5\,a\,d^3-8\,b^3\,c^3-8\,b\,c\,d^2\right)}{8\,b^4\,\sqrt{\pi}}+\frac{3\,c^2\,d\,x^2\,\mathrm{erfc}(a+b\,x)}{2}+c\,d^2\,x^3\,\mathrm{erfc}(a+b\,x)-\frac{x\,\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}\,\left(2\,a^2\,d^3-8\,a\,b\,c\,d^2+12\,b^2\,c^2\,d+3\,d^3\right)}{8\,b^3\,\sqrt{\pi}}-\frac{d^3\,x^3\,\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}}{4\,b\,\sqrt{\pi}}+\frac{x^2\,\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}\,\left(a\,d^3-4\,b\,c\,d^2\right)}{4\,b^2\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(a + b*x)*(c + d*x)^3,x)
```

```
[Out] (d^3*x^4*erfc(a + b*x))/4 - (erfc(a + b*x)*(b^2*((3*c^2*d)/4 + (3*a^2*c^2*d
)/2) - b*(a^3*c*d^2 + (3*a*c*d^2)/2) + (3*d^3)/16 + (3*a^2*d^3)/4 + (a^4*d^
3)/4 - a*b^3*c^3))/b^4 + c^3*x*erfc(a + b*x) + (exp(- a^2 - b^2*x^2 - 2*a*b
*x)*(5*a*d^3 + 2*a^3*d^3 - 8*b^3*c^3 - 8*b*c*d^2 + 12*a*b^2*c^2*d - 8*a^2*b
*c*d^2))/(8*b^4*pi^(1/2)) + (3*c^2*d*x^2*erfc(a + b*x))/2 + c*d^2*x^3*erfc(
a + b*x) - (x*exp(- a^2 - b^2*x^2 - 2*a*b*x)*(3*d^3 + 2*a^2*d^3 + 12*b^2*c^
2*d - 8*a*b*c*d^2))/(8*b^3*pi^(1/2)) - (d^3*x^3*exp(- a^2 - b^2*x^2 - 2*a*b
*x))/(4*b*pi^(1/2)) + (x^2*exp(- a^2 - b^2*x^2 - 2*a*b*x)*(a*d^3 - 4*b*c*d^
2))/(4*b^2*pi^(1/2))
```

3.119 $\int (c+dx)^2 \mathbf{Erfc}(a+bx)\,dx$

Optimal. Leaf size=194

$$-\frac{d^2e^{-(a+bx)^2}}{3b^3\sqrt{\pi}}-\frac{(bc-ad)^2e^{-(a+bx)^2}}{b^3\sqrt{\pi}}-\frac{d(bc-ad)e^{-(a+bx)^2}(a+bx)}{b^3\sqrt{\pi}}-\frac{d^2e^{-(a+bx)^2}(a+bx)^2}{3b^3\sqrt{\pi}}+\frac{d(bc-ad)\mathrm{Erf}(a+}{2b^3}$$

```
[Out] 1/2*d*(-a*d+b*c)*erf(b*x+a)/b^3+1/3*(-a*d+b*c)^3*erf(b*x+a)/b^3/d+1/3*(d*x+
c)^3*erfc(b*x+a)/d-1/3*d^2/b^3/exp((b*x+a)^2)/Pi^(1/2)-(-a*d+b*c)^2/b^3/exp
((b*x+a)^2)/Pi^(1/2)-d*(-a*d+b*c)*(b*x+a)/b^3/exp((b*x+a)^2)/Pi^(1/2)-1/3*d
^2*(b*x+a)^2/b^3/exp((b*x+a)^2)/Pi^(1/2)
```

Rubi [A]

time = 0.13, antiderivative size = 194, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 5, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.357$, Rules used = {6497, 2258, 2236, 2240, 2243}

$$\frac{(bc-ad)^3\mathrm{Erf}(a+bx)}{3b^3d}+\frac{d(bc-ad)\mathrm{Erf}(a+bx)}{2b^3}-\frac{e^{-(a+bx)^2}(bc-ad)^2}{\sqrt{\pi}\,b^3}-\frac{de^{-(a+bx)^2}(a+bx)(bc-ad)}{\sqrt{\pi}\,b^3}-\frac{d^2e^{-(a+bx)^2}(a+bx)^2}{3\sqrt{\pi}\,b^3}-\frac{d^2e^{-(a+bx)^2}}{3\sqrt{\pi}\,b^3}+\frac{(c+dx)^3\mathrm{Erfc}(a+bx)}{3d}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)^2*Erfc[a + b*x],x]
```

```
[Out] -1/3*d^2/(b^3*E^(a + b*x)^2*Sqrt[Pi]) - (b*c - a*d)^2/(b^3*E^(a + b*x)^2*Sq
rt[Pi]) - (d*(b*c - a*d)*(a + b*x))/(b^3*E^(a + b*x)^2*Sqrt[Pi]) - (d^2*(a
+ b*x)^2)/(3*b^3*E^(a + b*x)^2*Sqrt[Pi]) + (d*(b*c - a*d)*Erf[a + b*x])/(2*
b^3) + ((b*c - a*d)^3*Erf[a + b*x])/(3*b^3*d) + ((c + d*x)^3*Erfc[a + b*x])
/(3*d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
```

```
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 2258

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*(u_), x_Symbol] :> Int[E
xpandLinearProduct[F^(a + b*(c + d*x)^n), u, c, d, x], x] /; FreeQ[{F, a, b
, c, d, n}, x] && PolynomialQ[u, x]
```

Rule 6497

```
Int[Erfc[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfc[a + b*x]/(d*(m + 1))), x] + Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int (c+dx)^2\operatorname{erfc}(a+bx)\,dx &= \frac{(c+dx)^3\operatorname{erfc}(a+bx)}{3d}+\frac{(2b)\int e^{-(a+bx)^2}(c+dx)^3\,dx}{3d\sqrt{\pi}}\\ &= \frac{(c+dx)^3\operatorname{erfc}(a+bx)}{3d}+\frac{(2b)\int \left(\frac{(bc-ad)^3e^{-(a+bx)^2}}{b^3}+\frac{3d(bc-ad)^2e^{-(a+bx)^2}(a+bx)}{b^3}+\frac{3d^2(b\cdots}{\cdots}\right.}{3d\sqrt{\pi}}\\ &= \frac{(c+dx)^3\operatorname{erfc}(a+bx)}{3d}+\frac{(2d^2)\int e^{-(a+bx)^2}(a+bx)^3\,dx}{3b^2\sqrt{\pi}}+\frac{(2d(bc-ad))\int e^{-(a+b\cdots}}{b^2\sqrt{\pi}}\\ &= -\frac{(bc-ad)^2e^{-(a+bx)^2}}{b^3\sqrt{\pi}}-\frac{d(bc-ad)e^{-(a+bx)^2}(a+bx)}{b^3\sqrt{\pi}}-\frac{d^2e^{-(a+bx)^2}(a+bx)^2}{3b^3\sqrt{\pi}}+\cdots\\ &= -\frac{d^2e^{-(a+bx)^2}}{3b^3\sqrt{\pi}}-\frac{(bc-ad)^2e^{-(a+bx)^2}}{b^3\sqrt{\pi}}-\frac{d(bc-ad)e^{-(a+bx)^2}(a+bx)}{b^3\sqrt{\pi}}-\frac{d^2e^{-(a+bx\cdots}}{3b^3\cdots}\end{aligned}$$

Mathematica [A]
time = 0.19, size = 159, normalized size = 0.82

$$\frac{-((-3bcd-6a^2bcd+2a^3d^2+3a(2b^2c^2+d^2))\operatorname{Erf}(a+bx))+\frac{2e^{-(a+bx)^2}\left(-((1+a^2)d^2)+abd(3c+dx)-b^2(3c^2+3cdx+d^2x^2)+b^3e^{(a+bx)^2}\sqrt{\pi}\,x(3c^2+3cdx+d^2x^2)\operatorname{Erfc}(a+bx)\right)}{\sqrt{\pi}}}{6b^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^2*Erfc[a + b*x],x]
```

```
[Out] (-((-3*b*c*d - 6*a^2*b*c*d + 2*a^3*d^2 + 3*a*(2*b^2*c^2 + d^2))*Erf[a + b*x
]) + (2*(-((1 + a^2)*d^2) + a*b*d*(3*c + d*x) - b^2*(3*c^2 + 3*c*d*x + d^2*
```

```
x^2) + b^3*E^(a + b*x)^2*Sqrt[Pi]*x*(3*c^2 + 3*c*d*x + d^2*x^2)*Erfc[a + b*
x]))/(E^(a + b*x)^2*Sqrt[Pi]))/(6*b^3)
```

Maple [B] Leaf count of result is larger than twice the leaf count of optimal. 428 vs. $2(172) = 344$.
time = 0.41, size = 429, normalized size = 2.21

method	result
derivativedivides	$\frac{-\frac{d^2 \operatorname{erfc}(bx+a)a^3}{3b^2}+\frac{d \operatorname{erfc}(bx+a)a^2c}{b}+\frac{d^2 \operatorname{erfc}(bx+a)a^2(bx+a)}{b^2}-\operatorname{erfc}(bx+a)a\,c^2-\frac{2d \operatorname{erfc}(bx+a)ac(bx+a)}{b}-\frac{d^2 \operatorname{erfc}(bx+a)a(bx+a)^2}{b^2}}{}$
default	$\frac{-\frac{d^2 \operatorname{erfc}(bx+a)a^3}{3b^2}+\frac{d \operatorname{erfc}(bx+a)a^2c}{b}+\frac{d^2 \operatorname{erfc}(bx+a)a^2(bx+a)}{b^2}-\operatorname{erfc}(bx+a)a\,c^2-\frac{2d \operatorname{erfc}(bx+a)ac(bx+a)}{b}-\frac{d^2 \operatorname{erfc}(bx+a)a(bx+a)^2}{b^2}}{}$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^2*erfc(b*x+a),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*(-1/3/b^2*d^2*erfc(b*x+a)*a^3+1/b*d*erfc(b*x+a)*a^2*c+1/b^2*d^2*erfc(b*
x+a)*a^2*(b*x+a)-erfc(b*x+a)*a*c^2-2/b*d*erfc(b*x+a)*a*c*(b*x+a)-1/b^2*d^2*
erfc(b*x+a)*a*(b*x+a)^2+1/3*b/d*erfc(b*x+a)*c^3+erfc(b*x+a)*c^2*(b*x+a)+1/b
*d*erfc(b*x+a)*c*(b*x+a)^2+1/3/b^2*d^2*erfc(b*x+a)*(b*x+a)^3-2/3/b^2/d/Pi^(
1/2)*(1/2*a^3*d^3*Pi^(1/2)*erf(b*x+a)-1/2*b^3*c^3*Pi^(1/2)*erf(b*x+a)-d^3*(
-1/2/exp((b*x+a)^2)*(b*x+a)^2-1/2/exp((b*x+a)^2))+3*a*d^3*(-1/2*(b*x+a)/exp
((b*x+a)^2)+1/4*Pi^(1/2)*erf(b*x+a))+3/2*a^2*d^3/exp((b*x+a)^2)+3/2*a*b^2*c
^2*d*Pi^(1/2)*erf(b*x+a)-3/2*a^2*b*c*d^2*Pi^(1/2)*erf(b*x+a)-3*b*c*d^2*(-1/
2*(b*x+a)/exp((b*x+a)^2)+1/4*Pi^(1/2)*erf(b*x+a))+3/2*b^2*c^2*d/exp((b*x+a)
^2)-3*a*b*c*d^2/exp((b*x+a)^2)))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erfc(b*x+a),x, algorithm="maxima")
```

```
[Out] integrate((d*x + c)^2*erfc(b*x + a), x)
```

Fricas [A]
time = 0.34, size = 197, normalized size = 1.02

$$\frac{2\,\pi b^3 d^2 x^3+6\,\pi b^3 c d x^2+6\,\pi b^3 c^2 x-2\,\sqrt{\pi}\,(b^2 d^2 x^2+3\,b^2 c^2-3\,abcd+(a^2+1)d^2+(3\,b^2 cd-abd^2)x)e^{(-b^2x^2-2\,abx-a^2)}-(2\,\pi b^3 d^2 x^3+6\,\pi b^3 c d x^2+6\,\pi b^3 c^2 x+\pi(6\,ab^2c^2-3\,(2\,a^2+1)bcd+(2\,a^3+3\,a)d^2))\operatorname{erf}(bx+a)}{6\,\pi b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erfc(b*x+a),x, algorithm="fricas")
```

```
[Out] 1/6*(2*pi*b^3*d^2*x^3 + 6*pi*b^3*c*d*x^2 + 6*pi*b^3*c^2*x - 2*sqrt(pi)*(b^2
*d^2*x^2 + 3*b^2*c^2 - 3*a*b*c*d + (a^2 + 1)*d^2 + (3*b^2*c*d - a*b*d^2)*x)
*e^(-b^2*x^2 - 2*a*b*x - a^2) - (2*pi*b^3*d^2*x^3 + 6*pi*b^3*c*d*x^2 + 6*pi
*b^3*c^2*x + pi*(6*a*b^2*c^2 - 3*(2*a^2 + 1)*b*c*d + (2*a^3 + 3*a)*d^2))*er
f(b*x + a))/(pi*b^3)
```

Sympy [B] Leaf count of result is larger than twice the leaf count of optimal. 398 vs. $2(165) = 330$.
time = 1.15, size = 398, normalized size = 2.05

$$\begin{cases} \frac{a^3d^2 \operatorname{erfc}(a+bx)}{3b^3} - \frac{a^2cd \operatorname{erfc}(a+bx)}{b^2} - \frac{a^2d^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{3\sqrt{\pi}b^3} + \frac{ac^2 \operatorname{erfc}(a+bx)}{b} + \frac{acde^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}b^2} + \frac{ad^2xe^{-a^2}e^{-b^2x^2}e^{-2abx}}{3\sqrt{\pi}b^2} + \frac{ad^2 \operatorname{erfc}(a+bx)}{2b^3} + c^2x \operatorname{erfc}(a+bx) + cdx^2 \operatorname{erfc}(a+bx) + \frac{d^2x^3 \operatorname{erfc}(a+bx)}{3} - \frac{c^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}b} - \frac{cdxe^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}b} - \frac{d^2x^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{3\sqrt{\pi}b} - \frac{cd \operatorname{erfc}(a+bx)}{2b^2} - \frac{d^2e^{-a^2}e^{-b^2x^2}e^{-2abx}}{3\sqrt{\pi}b^3} & \text{for}\ b \neq 0 \\ \left(c^2x + cdx^2 + \frac{d^2x^3}{3}\right) \operatorname{erfc}(a) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**2*erfc(b*x+a),x)
```

```
[Out] Piecewise((a**3*d**2*erfc(a + b*x)/(3*b**3) - a**2*c*d*erfc(a + b*x)/b**2 -
 a**2*d**2*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(3*sqrt(pi)*b**3) + a*c
**2*erfc(a + b*x)/b + a*c*d*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(sqrt(
pi)*b**2) + a*d**2*x*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(3*sqrt(pi)*b
**2) + a*d**2*erfc(a + b*x)/(2*b**3) + c**2*x*erfc(a + b*x) + c*d*x**2*erfc
(a + b*x) + d**2*x**3*erfc(a + b*x)/3 - c**2*exp(-a**2)*exp(-b**2*x**2)*exp
(-2*a*b*x)/(sqrt(pi)*b) - c*d*x*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(s
qrt(pi)*b) - d**2*x**2*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(3*sqrt(pi)
*b) - c*d*erfc(a + b*x)/(2*b**2) - d**2*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a
*b*x)/(3*sqrt(pi)*b**3), Ne(b, 0)), ((c**2*x + c*d*x**2 + d**2*x**3/3)*erfc
(a), True))
```

Giac [A]
time = 0.51, size = 280, normalized size = 1.44

$$\frac{1}{3}d^2x^3 + cdx^2 - \left(x \operatorname{erf}(bx+a) - \frac{\frac{\sqrt{\pi}a \operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b} - \frac{e^{\left(-b^2x^2-2abx-a^2\right)}}{b}}{\sqrt{\pi}}\right)c^2 - \frac{1}{2}\left(2x^2 \operatorname{erf}(bx+a) + \frac{\frac{\sqrt{\pi}\left(2a^2+1\right) \operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b} + \frac{2\left(b\left(x+\frac{a}{b}\right)-2a\right)e^{\left(-b^2x^2-2abx-a^2\right)}}{b}}{\sqrt{\pi}b}\right)cd - \frac{1}{6}\left(2x^3 \operatorname{erf}(bx+a) - \frac{\frac{\sqrt{\pi}\left(2a^3+3a\right) \operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b} - \frac{2\left(b^2\left(x+\frac{a}{b}\right)^2-3ab\left(x+\frac{a}{b}\right)+3a^2+1\right)e^{\left(-b^2x^2-2abx-a^2\right)}}{b}}{\sqrt{\pi}b^2}\right)d^2 + c^2x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erfc(b*x+a),x, algorithm="giac")
```

```
[Out] 1/3*d^2*x^3 + c*d*x^2 - (x*erf(b*x + a) - (sqrt(pi)*a*erf(-b*(x + a/b))/b -
 e^(-b^2*x^2 - 2*a*b*x - a^2)/b)/sqrt(pi))*c^2 - 1/2*(2*x^2*erf(b*x + a) +
(sqrt(pi)*(2*a^2 + 1)*erf(-b*(x + a/b))/b + 2*(b*(x + a/b) - 2*a)*e^(-b^2*x
^2 - 2*a*b*x - a^2)/b)/(sqrt(pi)*b))*c*d - 1/6*(2*x^3*erf(b*x + a) - (sqrt(
pi)*(2*a^3 + 3*a)*erf(-b*(x + a/b))/b - 2*(b^2*(x + a/b)^2 - 3*a*b*(x + a/b
) + 3*a^2 + 1)*e^(-b^2*x^2 - 2*a*b*x - a^2)/b)/(sqrt(pi)*b^2))*d^2 + c^2*x
```

Mupad [B]
time = 0.31, size = 220, normalized size = 1.13

$$\frac{d^2\,x^3\,\mathrm{erfc}(a+b\,x)}{3} - \frac{\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}\,\left(\frac{b^2\,c^2}{\sqrt{\pi}} - \frac{a\,d\,b\,c}{\sqrt{\pi}} + \frac{a^2\,d^2+d^2}{3\,\sqrt{\pi}}\right)}{b^3} + \frac{\mathrm{erfc}(a+b\,x)\,\left(\frac{a\,d^2}{2} - b\,\left(c\,d\,a^2 + \frac{c\,d}{2}\right) + \frac{a^3\,d^2}{3} + a\,b^2\,c^2\right)}{b^3} + c^2\,x\,\mathrm{erfc}(a+b\,x) + c\,d\,x^2\,\mathrm{erfc}(a+b\,x) + \frac{x\,\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}\,(a\,d^2 - 3\,b\,c\,d)}{3\,b^2\,\sqrt{\pi}} - \frac{d^2\,x^2\,\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}}{3\,b\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(a + b*x)*(c + d*x)^2,x)
```

```
[Out] (d^2*x^3*erfc(a + b*x))/3 - (exp(- a^2 - b^2*x^2 - 2*a*b*x)*((d^2 + a^2*d^2
)/(3*pi^(1/2)) + (b^2*c^2)/pi^(1/2) - (a*b*c*d)/pi^(1/2)))/b^3 + (erfc(a +
b*x)*((a*d^2)/2 - b*((c*d)/2 + a^2*c*d) + (a^3*d^2)/3 + a*b^2*c^2))/b^3 + c
^2*x*erfc(a + b*x) + c*d*x^2*erfc(a + b*x) + (x*exp(- a^2 - b^2*x^2 - 2*a*b
*x)*(a*d^2 - 3*b*c*d))/(3*b^2*pi^(1/2)) - (d^2*x^2*exp(- a^2 - b^2*x^2 - 2*
a*b*x))/(3*b*pi^(1/2))
```

3.120 $\int (c+dx)\mathrm{\bf Erfc}(a+bx)\,dx$

Optimal. Leaf size=119

$$-\frac{(bc-ad)e^{-(a+bx)^2}}{b^2\sqrt{\pi}}-\frac{de^{-(a+bx)^2}(a+bx)}{2b^2\sqrt{\pi}}+\frac{d\mathrm{Erf}(a+bx)}{4b^2}+\frac{(bc-ad)^2\mathrm{Erf}(a+bx)}{2b^2d}+\frac{(c+dx)^2\mathrm{Erfc}(a+bx)}{2d}$$

```
[Out] 1/4*d*erf(b*x+a)/b^2+1/2*(-a*d+b*c)^2*erf(b*x+a)/b^2/d+1/2*(d*x+c)^2*erfc(b
*x+a)/d+(a*d-b*c)/b^2/exp((b*x+a)^2)/Pi^(1/2)-1/2*d*(b*x+a)/b^2/exp((b*x+a)
^2)/Pi^(1/2)
```

Rubi [A]
time = 0.08, antiderivative size = 119, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.417$, Rules used = {6497, 2258, 2236, 2240, 2243}

$$\frac{(bc-ad)^2\mathrm{Erf}(a+bx)}{2b^2d}-\frac{e^{-(a+bx)^2}(bc-ad)}{\sqrt{\pi}\,b^2}+\frac{d\mathrm{Erf}(a+bx)}{4b^2}-\frac{de^{-(a+bx)^2}(a+bx)}{2\sqrt{\pi}\,b^2}+\frac{(c+dx)^2\mathrm{Erfc}(a+bx)}{2d}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)*Erfc[a + b*x],x]
```

```
[Out] -((b*c - a*d)/(b^2*E^(a + b*x)^2*Sqrt[Pi])) - (d*(a + b*x))/(2*b^2*E^(a + b
*x)^2*Sqrt[Pi]) + (d*Erf[a + b*x])/(4*b^2) + ((b*c - a*d)^2*Erf[a + b*x])/(
2*b^2*d) + ((c + d*x)^2*Erfc[a + b*x])/(2*d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
```

```
0])
```

Rule 2258

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*(u_), x_Symbol] :> Int[E
xpandLinearProduct[F^(a + b*(c + d*x)^n), u, c, d, x], x] /; FreeQ[{F, a, b
, c, d, n}, x] && PolynomialQ[u, x]
```

Rule 6497

```
Int[Erfc[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfc[a + b*x]/(d*(m + 1))), x] + Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)/E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int (c+dx)\operatorname{erfc}(a+bx)\,dx &= \frac{(c+dx)^2\operatorname{erfc}(a+bx)}{2d}+\frac{b\int e^{-(a+bx)^2}(c+dx)^2\,dx}{d\sqrt{\pi}}\\
&= \frac{(c+dx)^2\operatorname{erfc}(a+bx)}{2d}+\frac{b\int \left(\frac{(bc-ad)^2e^{-(a+bx)^2}}{b^2}+\frac{2d(bc-ad)e^{-(a+bx)^2}(a+bx)}{b^2}+\frac{d^2e^{-(a+b
\end{aligned}$$

$$= \frac{(c+dx)^2\operatorname{erfc}(a+bx)}{2d}+\frac{d\int e^{-(a+bx)^2}(a+bx)^2\,dx}{b\sqrt{\pi}}+\frac{(2(bc-ad))\int e^{-(a+bx)^2}(a$$

$$= -\frac{(bc-ad)e^{-(a+bx)^2}}{b^2\sqrt{\pi}}-\frac{de^{-(a+bx)^2}(a+bx)}{2b^2\sqrt{\pi}}+\frac{(bc-ad)^2\operatorname{erf}(a+bx)}{2b^2d}+\frac{(c+dx)^2$$

$$= -\frac{(bc-ad)e^{-(a+bx)^2}}{b^2\sqrt{\pi}}-\frac{de^{-(a+bx)^2}(a+bx)}{2b^2\sqrt{\pi}}+\frac{d\operatorname{erf}(a+bx)}{4b^2}+\frac{(bc-ad)^2\operatorname{erf}(a+$$

Mathematica [A]
time = 0.08, size = 104, normalized size = 0.87

$$\frac{e^{-(a+bx)^2}\left(-4bc+2ad-2bdx+(-4abc+d+2a^2d)\,e^{(a+bx)^2}\sqrt{\pi}\operatorname{Erf}(a+bx)+2b^2e^{(a+bx)^2}\sqrt{\pi}\,x(2c+dx)\operatorname{Erfc}(a+bx)\right)}{4b^2\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)*Erfc[a + b*x],x]
```

```
[Out] (-4*b*c + 2*a*d - 2*b*d*x + (-4*a*b*c + d + 2*a^2*d)*E^(a + b*x)^2*Sqrt[Pi]
*Erf[a + b*x] + 2*b^2*E^(a + b*x)^2*Sqrt[Pi]*x*(2*c + d*x)*Erfc[a + b*x])/(
4*b^2*E^(a + b*x)^2*Sqrt[Pi])
```

Maple [A]
time = 0.26, size = 124, normalized size = 1.04

method	result
derivativedivides	$\frac{-\frac{\operatorname{erfc}(bx+a)da(bx+a)}{b}+\operatorname{erfc}(bx+a)c(bx+a)+\frac{\operatorname{erfc}(bx+a)d(bx+a)^2}{2b}-\frac{-d\left(-\frac{(bx+a)e^{-(bx+a)^2}}{2}+\frac{\sqrt{\pi}\operatorname{erf}(bx+a)}{4}\right)+e^{-(bx+a)^2}bc}{b\sqrt{\pi}}}{b}$
default	$\frac{-\frac{\operatorname{erfc}(bx+a)da(bx+a)}{b}+\operatorname{erfc}(bx+a)c(bx+a)+\frac{\operatorname{erfc}(bx+a)d(bx+a)^2}{2b}-\frac{-d\left(-\frac{(bx+a)e^{-(bx+a)^2}}{2}+\frac{\sqrt{\pi}\operatorname{erf}(bx+a)}{4}\right)+e^{-(bx+a)^2}bc}{b\sqrt{\pi}}}{b}$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)*erfc(b*x+a),x,method=_RETURNVERBOSE)
[Out] 1/b*(-1/b*erfc(b*x+a)*d*a*(b*x+a)+erfc(b*x+a)*c*(b*x+a)+1/2/b*erfc(b*x+a)*d
*(b*x+a)^2-1/b/Pi^(1/2)*(-d*(-1/2*(b*x+a)/exp((b*x+a)^2)+1/4*Pi^(1/2)*erf(b
*x+a))+c*b/exp((b*x+a)^2)-d*a/exp((b*x+a)^2)))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfc(b*x+a),x, algorithm="maxima")
[Out] integrate((d*x + c)*erfc(b*x + a), x)
```

Fricas [A]
time = 0.34, size = 110, normalized size = 0.92

$$\frac{2\,\pi b^2dx^2+4\,\pi b^2cx-2\,\sqrt{\pi}\,(bdx+2\,bc-ad)e^{\left(-b^2x^2-2\,abx-a^2\right)}-\left(2\,\pi b^2dx^2+4\,\pi b^2cx+\pi(4\,abc-(2\,a^2+1)d)\right)\operatorname{erf}(bx+a)}{4\,\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfc(b*x+a),x, algorithm="fricas")
[Out] 1/4*(2*pi*b^2*d*x^2 + 4*pi*b^2*c*x - 2*sqrt(pi)*(b*d*x + 2*b*c - a*d)*e^(-b
^2*x^2 - 2*a*b*x - a^2) - (2*pi*b^2*d*x^2 + 4*pi*b^2*c*x + pi*(4*a*b*c - (2
*a^2 + 1)*d))*erf(b*x + a))/(pi*b^2)
```

Sympy [A]
time = 0.56, size = 178, normalized size = 1.50

$$\begin{cases} -\frac{a^2d\operatorname{erfc}(a+bx)}{2b^2}+\frac{ac\operatorname{erfc}(a+bx)}{b}+\frac{ade^{-a^2}e^{-b^2x^2}e^{-2abx}}{2\sqrt{\pi}\,b^2}+cx\operatorname{erfc}(a+bx)+\frac{dx^2\operatorname{erfc}(a+bx)}{2}-\frac{ce^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}\,b}-\frac{dxe^{-a^2}e^{-b^2x^2}e^{-2abx}}{2\sqrt{\pi}\,b}-\frac{d\operatorname{erfc}(a+bx)}{4b^2} & \text{for}\ b\neq 0 \\ \left(cx+\frac{dx^2}{2}\right)\operatorname{erfc}(a) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfc(b*x+a),x)
```

```
[Out] Piecewise((-a**2*d*erfc(a + b*x)/(2*b**2) + a*c*erfc(a + b*x)/b + a*d*exp(-
a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(2*sqrt(pi)*b**2) + c*x*erfc(a + b*x) +
 d*x**2*erfc(a + b*x)/2 - c*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(sqrt(
pi)*b) - d*x*exp(-a**2)*exp(-b**2*x**2)*exp(-2*a*b*x)/(2*sqrt(pi)*b) - d*er
fc(a + b*x)/(4*b**2), Ne(b, 0)), ((c*x + d*x**2/2)*erfc(a), True))
```

Giac [A]
time = 0.48, size = 158, normalized size = 1.33

$$\frac{1}{2}\,dx^2-\left(x\,\mathrm{erf}\left(bx+a\right)-\frac{\frac{\sqrt{\pi}\,a\,\mathrm{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b}-\frac{e^{\left(-b^2x^2-2\,abx-a^2\right)}}{b}}{\sqrt{\pi}}\right)c-\frac{1}{4}\left(2\,x^2\,\mathrm{erf}\left(bx+a\right)+\frac{\frac{\sqrt{\pi}\,\left(2\,a^2+1\right)\mathrm{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b}+\frac{2\left(b\left(x+\frac{a}{b}\right)-2\,a\right)e^{\left(-b^2x^2-2\,abx-a^2\right)}}{b}}{\sqrt{\pi}\,b}\right)d+cx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfc(b*x+a),x, algorithm="giac")
```

```
[Out] 1/2*d*x^2 - (x*erf(b*x + a) - (sqrt(pi)*a*erf(-b*(x + a/b))/b - e^(-b^2*x^2
 - 2*a*b*x - a^2)/b)/sqrt(pi))*c - 1/4*(2*x^2*erf(b*x + a) + (sqrt(pi)*(2*a
^2 + 1)*erf(-b*(x + a/b))/b + 2*(b*(x + a/b) - 2*a)*e^(-b^2*x^2 - 2*a*b*x -
 a^2)/b)/(sqrt(pi)*b))*d + c*x
```

Mupad [B]
time = 0.22, size = 119, normalized size = 1.00

$$c\,x\,\mathrm{erfc}(a+b\,x)-\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}\,\left(\frac{c}{b\,\sqrt{\pi}}-\frac{a\,d}{2\,b^2\,\sqrt{\pi}}\right)-\frac{\mathrm{erfc}(a+b\,x)\,\left(\frac{d\,a^2}{2}-b\,c\,a+\frac{d}{4}\right)}{b^2}+\frac{d\,x^2\,\mathrm{erfc}(a+b\,x)}{2}-\frac{d\,x\,\mathrm{e}^{-a^2-2\,a\,b\,x-b^2\,x^2}}{2\,b\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(a + b*x)*(c + d*x),x)
```

```
[Out] c*x*erfc(a + b*x) - exp(- a^2 - b^2*x^2 - 2*a*b*x)*(c/(b*pi^(1/2)) - (a*d)/
(2*b^2*pi^(1/2))) - (erfc(a + b*x)*(d/4 + (a^2*d)/2 - a*b*c))/b^2 + (d*x^2*
erfc(a + b*x))/2 - (d*x*exp(- a^2 - b^2*x^2 - 2*a*b*x))/(2*b*pi^(1/2))
```

3.121 $\int \text{Erfc}(a+bx)\,dx$

Optimal. Leaf size=37

$$-\frac{e^{-(a+bx)^2}}{b\sqrt{\pi}}+\frac{(a+bx)\text{Erfc}(a+bx)}{b}$$

```
[Out] (b*x+a)*erfc(b*x+a)/b-1/b/exp((b*x+a)^2)/Pi^(1/2)
```

Rubi [A]
time = 0.01, antiderivative size = 37, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.167, Rules used = {6485}

$$\frac{(a+bx)\text{Erfc}(a+bx)}{b}-\frac{e^{-(a+bx)^2}}{\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[a + b*x],x]
[Out] -(1/(b*E^(a + b*x)^2*Sqrt[Pi])) + ((a + b*x)*Erfc[a + b*x])/b
```

Rule 6485

```
Int[Erfc[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[(a + b*x)*(Erfc[a + b*x]/b)
, x] - Simp[1/(b*Sqrt[Pi]*E^(a + b*x)^2), x] /; FreeQ[{a, b}, x]
```

Rubi steps

$$\int \text{erfc}(a+bx)\,dx=-\frac{e^{-(a+bx)^2}}{b\sqrt{\pi}}+\frac{(a+bx)\text{erfc}(a+bx)}{b}$$

Mathematica [A]
time = 0.03, size = 42, normalized size = 1.14

$$-\frac{e^{-(a+bx)^2}}{b\sqrt{\pi}}-\frac{a\text{Erf}(a+bx)}{b}+x\text{Erfc}(a+bx)$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[a + b*x],x]
[Out] -(1/(b*E^(a + b*x)^2*Sqrt[Pi])) - (a*Erf[a + b*x])/b + x*Erfc[a + b*x]
```

Maple [A]
time = 0.18, size = 33, normalized size = 0.89

method	result	size
derivativedivides	$\frac{(bx+a)\operatorname{erfc}(bx+a)-\frac{\mathrm{e}^{-(bx+a)^2}}{\sqrt{\pi}}}{b}$	33
default	$\frac{(bx+a)\operatorname{erfc}(bx+a)-\frac{\mathrm{e}^{-(bx+a)^2}}{\sqrt{\pi}}}{b}$	33

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x+a),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*((b*x+a)*erfc(b*x+a)-1/Pi^(1/2)*exp(-(b*x+a)^2))
```

Maxima [A]
time = 0.26, size = 32, normalized size = 0.86

$$\frac{(bx+a)\operatorname{erfc}(bx+a)-\frac{e^{\left(-(bx+a)^2\right)}}{\sqrt{\pi}}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a),x, algorithm="maxima")
```

```
[Out] ((b*x + a)*erfc(b*x + a) - e^(-(b*x + a)^2)/sqrt(pi))/b
```

Fricas [A]
time = 0.33, size = 53, normalized size = 1.43

$$\frac{\pi bx-(\pi bx+\pi a)\operatorname{erf}(bx+a)-\sqrt{\pi}\,e^{\left(-b^2x^2-2\,abx-a^2\right)}}{\pi b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a),x, algorithm="fricas")
```

```
[Out] (pi*b*x - (pi*b*x + pi*a)*erf(b*x + a) - sqrt(pi)*e^(-b^2*x^2 - 2*a*b*x - a
^2))/(pi*b)
```

Sympy [A]
time = 0.30, size = 53, normalized size = 1.43

$$\begin{cases} \frac{a\operatorname{erfc}(a+bx)}{b}+x\operatorname{erfc}(a+bx)-\frac{e^{-a^2}e^{-b^2x^2}e^{-2abx}}{\sqrt{\pi}\,b} & \text{for}\ b\neq 0 \\ x\operatorname{erfc}(a) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a),x)
```

```
[Out] Piecewise((a*erfc(a + b*x)/b + x*erfc(a + b*x) - exp(-a**2)*exp(-b**2*x**2)
*exp(-2*a*b*x)/(sqrt(pi)*b), Ne(b, 0)), (x*erfc(a), True))
```

Giac [A]
time = 0.42, size = 60, normalized size = 1.62

$$-x\operatorname{erf}\left(bx+a\right)+x+\frac{\frac{\sqrt{\pi}\,a\operatorname{erf}\left(-b\left(x+\frac{a}{b}\right)\right)}{b}-\frac{e^{\left(-b^2x^2-2\,abx-a^2\right)}}{b}}{\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a),x, algorithm="giac")
```

```
[Out] -x*erf(b*x + a) + x + (sqrt(pi)*a*erf(-b*(x + a/b))/b - e^(-b^2*x^2 - 2*a*b
*x - a^2)/b)/sqrt(pi)
```

Mupad [B]
time = 0.11, size = 49, normalized size = 1.32

$$x\operatorname{erfc}(a+b\,x)+\frac{a\operatorname{erfc}(a+b\,x)}{b}-\frac{\mathrm{e}^{-b^2\,x^2}\,\mathrm{e}^{-a^2}\,\mathrm{e}^{-2\,a\,b\,x}}{b\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(a + b*x),x)
```

```
[Out] x*erfc(a + b*x) + (a*erfc(a + b*x))/b - (exp(-b^2*x^2)*exp(-a^2)*exp(-2*a*b
*x))/(b*pi^(1/2))
```

3.122 $\int \frac{\text{Erfc}(a+bx)}{c+dx} \, dx$

Optimal. Leaf size=17

$$\text{Int}\left(\frac{\text{Erfc}(a+bx)}{c+dx},x\right)$$

```
[Out] Unintegrable(erfc(b*x+a)/(d*x+c),x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\text{Erfc}(a+bx)}{c+dx} \, dx$$

Verification is not applicable to the result.

```
[In] Int[Erfc[a + b*x]/(c + d*x),x]
```

```
[Out] Defer[Int][Erfc[a + b*x]/(c + d*x), x]
```

Rubi steps

$$\int \frac{\text{erfc}(a+bx)}{c+dx} \, dx = \int \frac{\text{erfc}(a+bx)}{c+dx} \, dx$$

Mathematica [A]
time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{\text{Erfc}(a+bx)}{c+dx} \, dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfc[a + b*x]/(c + d*x),x]
```

```
[Out] Integrate[Erfc[a + b*x]/(c + d*x), x]
```

Maple [A]
time = 0.17, size = 0, normalized size = 0.00

$$\int \frac{\text{erfc}(bx+a)}{dx+c} \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x+a)/(d*x+c),x)
```

```
[Out] int(erfc(b*x+a)/(d*x+c),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)/(d*x+c),x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x + a)/(d*x + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)/(d*x+c),x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x + a) - 1)/(d*x + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}\left(a + bx\right)}{c + dx}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)/(d*x+c),x)
```

```
[Out] Integral(erfc(a + b*x)/(c + d*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)/(d*x+c),x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x + a)/(d*x + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.06

$$\int \frac{\mathrm{erfc}(a+b\,x)}{c+d\,x} \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(a + b*x)/(c + d*x),x)
```

```
[Out] int(erfc(a + b*x)/(c + d*x), x)
```

3.123 $\int \frac{\mathbf{Erfc}(a+bx)}{(c+dx)^2}\,dx$

Optimal. Leaf size=52

$$-\frac{\operatorname{Erfc}(a+bx)}{d(c+dx)}-\frac{2b\operatorname{Int}\left(\frac{e^{-(a+bx)^2}}{c+dx},x\right)}{d\sqrt{\pi}}$$

```
[Out] -erfc(b*x+a)/d/(d*x+c)-2*b*Unintegrable(1/exp((b*x+a)^2)/(d*x+c),x)/d/Pi^(1
/2)
```

Rubi [A]
time = 0.03, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\operatorname{Erfc}(a+bx)}{(c+dx)^2}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erfc[a + b*x]/(c + d*x)^2,x]
```

```
[Out] -(Erfc[a + b*x]/(d*(c + d*x))) - (2*b*Defer[Int][1/(E^(a + b*x)^2*(c + d*x)
), x])/(d*Sqrt[Pi])
```

Rubi steps

$$\int \frac{\operatorname{erfc}(a+bx)}{(c+dx)^2}\,dx=-\frac{\operatorname{erfc}(a+bx)}{d(c+dx)}-\frac{(2b)\int \frac{e^{-(a+bx)^2}}{c+dx}\,dx}{d\sqrt{\pi}}$$

Mathematica [A]
time = 0.34, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{Erfc}(a+bx)}{(c+dx)^2}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfc[a + b*x]/(c + d*x)^2,x]
```

```
[Out] Integrate[Erfc[a + b*x]/(c + d*x)^2, x]
```

Maple [A]
time = 0.22, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}(bx+a)}{(dx+c)^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x+a)/(d*x+c)^2,x)
```

```
[Out] int(erfc(b*x+a)/(d*x+c)^2,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)/(d*x+c)^2,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x + a)/(d*x + c)^2, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)/(d*x+c)^2,x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x + a) - 1)/(d^2*x^2 + 2*c*d*x + c^2), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}(a+bx)}{(c+dx)^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)/(d*x+c)**2,x)
```

```
[Out] Integral(erfc(a + b*x)/(c + d*x)**2, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)/(d*x+c)^2,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x + a)/(d*x + c)^2, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\operatorname{erfc}(a+b\,x)}{(c+d\,x)^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(a + b*x)/(c + d*x)^2,x)
```

```
[Out] int(erfc(a + b*x)/(c + d*x)^2, x)
```

3.124 $\int \frac{\mathbf{Erfc}(a+bx)}{(c+dx)^3}\,dx$

Optimal. Leaf size=105

$$\frac{be^{-(a+bx)^2}}{d^2\sqrt{\pi}\,(c+dx)}+\frac{b^2\mathrm{Erf}(a+bx)}{d^3}-\frac{\mathrm{Erfc}(a+bx)}{2d(c+dx)^2}-\frac{2b^2(bc-ad)\mathrm{Int}\left(\frac{e^{-(a+bx)^2}}{c+dx},x\right)}{d^3\sqrt{\pi}}$$

```
[Out] b^2*erf(b*x+a)/d^3-1/2*erfc(b*x+a)/d/(d*x+c)^2+b/d^2/exp((b*x+a)^2)/(d*x+c)
/Pi^(1/2)-2*b^2*(-a*d+b*c)*Unintegrable(1/exp((b*x+a)^2)/(d*x+c),x)/d^3/Pi^
(1/2)
```

Rubi [A]
time = 0.05, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\mathrm{Erfc}(a+bx)}{(c+dx)^3}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erfc[a + b*x]/(c + d*x)^3,x]
```

```
[Out] b/(d^2*E^(a + b*x)^2*Sqrt[Pi]*(c + d*x)) + (b^2*Erf[a + b*x])/d^3 - Erfc[a
+ b*x]/(2*d*(c + d*x)^2) - (2*b^2*(b*c - a*d)*Defer[Int][1/(E^(a + b*x)^2*(
c + d*x)), x])/(d^3*Sqrt[Pi])
```

Rubi steps

$$\begin{aligned}
\int \frac{\mathrm{erfc}(a+bx)}{(c+dx)^3}\,dx &= -\frac{\mathrm{erfc}(a+bx)}{2d(c+dx)^2}-\frac{b\int \frac{e^{-(a+bx)^2}}{(c+dx)^2}\,dx}{d\sqrt{\pi}}\\
&= \frac{be^{-(a+bx)^2}}{d^2\sqrt{\pi}\,(c+dx)}-\frac{\mathrm{erfc}(a+bx)}{2d(c+dx)^2}+\frac{(2b^3)\int e^{-(a+bx)^2}\,dx}{d^3\sqrt{\pi}}-\frac{(2b^2(bc-ad))\int \frac{e^{-(a+bx)^2}}{c+dx}\,dx}{d^3\sqrt{\pi}}\\
&= \frac{be^{-(a+bx)^2}}{d^2\sqrt{\pi}\,(c+dx)}+\frac{b^2\mathrm{erf}(a+bx)}{d^3}-\frac{\mathrm{erfc}(a+bx)}{2d(c+dx)^2}-\frac{(2b^2(bc-ad))\int \frac{e^{-(a+bx)^2}}{c+dx}\,dx}{d^3\sqrt{\pi}}
\end{aligned}$$

Mathematica [A]
time = 0.65, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{Erfc}(a+bx)}{(c+dx)^3}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfc[a + b*x]/(c + d*x)^3,x]
```

```
[Out] Integrate[Erfc[a + b*x]/(c + d*x)^3, x]
```

Maple [A]
time = 0.22, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}(bx+a)}{(dx+c)^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x+a)/(d*x+c)^3,x)
```

```
[Out] int(erfc(b*x+a)/(d*x+c)^3,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)/(d*x+c)^3,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x + a)/(d*x + c)^3, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)/(d*x+c)^3,x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x + a) - 1)/(d^3*x^3 + 3*c*d^2*x^2 + 3*c^2*d*x + c^3), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}{\left(a + bx \right)}}{\left(c + dx\right)^{3}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)/(d*x+c)**3,x)
```

```
[Out] Integral(erfc(a + b*x)/(c + d*x)**3, x)
```

Giac [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)/(d*x+c)^3,x, algorithm="giac")
[Out] integrate(erfc(b*x + a)/(d*x + c)^3, x)
```

Mupad [**A**]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erfc}(a+b\,x)}{(c+d\,x)^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(a + b*x)/(c + d*x)^3,x)
[Out] int(erfc(a + b*x)/(c + d*x)^3, x)
```

3.125 $\int x^5 \mathbf{Erfc}(bx)^2\, dx$

Optimal. Leaf size=178

$$\frac{11e^{-2b^2x^2}}{12b^6\pi}+\frac{7e^{-2b^2x^2}x^2}{12b^4\pi}+\frac{e^{-2b^2x^2}x^4}{6b^2\pi}-\frac{5e^{-b^2x^2}x\mathrm{Erfc}(bx)}{4b^5\sqrt{\pi}}-\frac{5e^{-b^2x^2}x^3\mathrm{Erfc}(bx)}{6b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^5\mathrm{Erfc}(bx)}{3b\sqrt{\pi}}-\frac{5\mathrm{Erfc}(bx)^2}{16b^6}+\frac{1}{6}$$

```
[Out] 11/12/b^6/exp(2*b^2*x^2)/Pi+7/12*x^2/b^4/exp(2*b^2*x^2)/Pi+1/6*x^4/b^2/exp(
2*b^2*x^2)/Pi-5/16*erfc(b*x)^2/b^6+1/6*x^6*erfc(b*x)^2-5/4*x*erfc(b*x)/b^5/
exp(b^2*x^2)/Pi^(1/2)-5/6*x^3*erfc(b*x)/b^3/exp(b^2*x^2)/Pi^(1/2)-1/3*x^5*e
rfc(b*x)/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.19, antiderivative size = 178, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.600$, Rules used = {6500, 6521, 6509, 30, 2240, 2243}

$$-\frac{5\mathrm{Erfc}(bx)^2}{16b^6}-\frac{x^5e^{-b^2x^2}\mathrm{Erfc}(bx)}{3\sqrt{\pi}\,b}+\frac{x^4e^{-2b^2x^2}}{6\pi b^2}+\frac{11e^{-2b^2x^2}}{12\pi b^6}-\frac{5xe^{-b^2x^2}\mathrm{Erfc}(bx)}{4\sqrt{\pi}\,b^5}+\frac{7x^2e^{-2b^2x^2}}{12\pi b^4}-\frac{5x^3e^{-b^2x^2}\mathrm{Erfc}(bx)}{6\sqrt{\pi}\,b^3}+\frac{1}{6}x^6\mathrm{Erfc}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[x^5*Erfc[b*x]^2,x]
```

```
[Out] 11/(12*b^6*E^(2*b^2*x^2)*Pi) + (7*x^2)/(12*b^4*E^(2*b^2*x^2)*Pi) + x^4/(6*b
^2*E^(2*b^2*x^2)*Pi) - (5*x*Erfc[b*x])/(4*b^5*E^(b^2*x^2)*Sqrt[Pi]) - (5*x^
3*Erfc[b*x])/(6*b^3*E^(b^2*x^2)*Sqrt[Pi]) - (x^5*Erfc[b*x])/(3*b*E^(b^2*x^2
)*Sqrt[Pi]) - (5*Erfc[b*x]^2)/(16*b^6) + (x^6*Erfc[b*x]^2)/6
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
```

```
0])
```

Rule 6500

```
Int[Erfc[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfc[b*x]^2
/(m + 1)), x] + Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erfc[b*x])/E^
(b^2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$
\begin{aligned}
\int x^5\operatorname{erfc}(bx)^2\,dx &= \frac{1}{6}x^6\operatorname{erfc}(bx)^2+\frac{(2b)\int e^{-b^2x^2}x^6\operatorname{erfc}(bx)\,dx}{3\sqrt{\pi}}\\
&= -\frac{e^{-b^2x^2}x^5\operatorname{erfc}(bx)}{3b\sqrt{\pi}}+\frac{1}{6}x^6\operatorname{erfc}(bx)^2-\frac{2\int e^{-2b^2x^2}x^5\,dx}{3\pi}+\frac{5\int e^{-b^2x^2}x^4\operatorname{erfc}(bx)\,dx}{3b\sqrt{\pi}}\\
&= \frac{e^{-2b^2x^2}x^4}{6b^2\pi}-\frac{5e^{-b^2x^2}x^3\operatorname{erfc}(bx)}{6b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^5\operatorname{erfc}(bx)}{3b\sqrt{\pi}}+\frac{1}{6}x^6\operatorname{erfc}(bx)^2-\frac{2\int e^{-2b^2x^2}x^3\,dx}{3b^2\pi}-\\
&= \frac{7e^{-2b^2x^2}x^2}{12b^4\pi}+\frac{e^{-2b^2x^2}x^4}{6b^2\pi}-\frac{5e^{-b^2x^2}x\operatorname{erfc}(bx)}{4b^5\sqrt{\pi}}-\frac{5e^{-b^2x^2}x^3\operatorname{erfc}(bx)}{6b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^5\operatorname{erfc}(bx)}{3b\sqrt{\pi}}+\frac{1}{6}\\
&= \frac{11e^{-2b^2x^2}}{12b^6\pi}+\frac{7e^{-2b^2x^2}x^2}{12b^4\pi}+\frac{e^{-2b^2x^2}x^4}{6b^2\pi}-\frac{5e^{-b^2x^2}x\operatorname{erfc}(bx)}{4b^5\sqrt{\pi}}-\frac{5e^{-b^2x^2}x^3\operatorname{erfc}(bx)}{6b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^5}{3b\sqrt{}}\\
&= \frac{11e^{-2b^2x^2}}{12b^6\pi}+\frac{7e^{-2b^2x^2}x^2}{12b^4\pi}+\frac{e^{-2b^2x^2}x^4}{6b^2\pi}-\frac{5e^{-b^2x^2}x\operatorname{erfc}(bx)}{4b^5\sqrt{\pi}}-\frac{5e^{-b^2x^2}x^3\operatorname{erfc}(bx)}{6b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^5}{3b\sqrt{}}
\end{aligned}
$$

Mathematica [A]
time = 0.27, size = 173, normalized size = 0.97

$$
\frac{1}{24}\left(4x^6-\frac{2e^{-b^2x^2}x\left(15+10b^2x^2+4b^4x^4\right)}{b^5\sqrt{\pi}}+\left(\frac{15}{b^6}-8x^6\right)\operatorname{Erf}(bx)+4x^6\operatorname{Erf}(bx)^2+\frac{e^{-2b^2x^2}\left(44+28b^2x^2+8b^4x^4+4be^{b^2x^2}\sqrt{\pi}\,x\left(15+10b^2x^2+4b^4x^4\right)\operatorname{Erf}(bx)-15e^{2b^2x^2}\pi\operatorname{Erf}(bx)^2\right)}{2b^6\pi}\right)
$$

Antiderivative was successfully verified.

```
[In] Integrate[x^5*Erfc[b*x]^2,x]
```

```
[Out] (4*x^6 - (2*x*(15 + 10*b^2*x^2 + 4*b^4*x^4))/(b^5*E^(b^2*x^2)*Sqrt[Pi]) + (
15/b^6 - 8*x^6)*Erf[b*x] + 4*x^6*Erf[b*x]^2 + (44 + 28*b^2*x^2 + 8*b^4*x^4
+ 4*b*E^(b^2*x^2)*Sqrt[Pi]*x*(15 + 10*b^2*x^2 + 4*b^4*x^4)*Erf[b*x] - 15*E^
(2*b^2*x^2)*Pi*Erf[b*x]^2)/(2*b^6*E^(2*b^2*x^2)*Pi))/24
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int x^5 \mathrm{erfc}(bx)^2\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*erfc(b*x)^2,x)
```

```
[Out] int(x^5*erfc(b*x)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfc(b*x)^2,x, algorithm="maxima")
```

```
[Out] integrate(x^5*erfc(b*x)^2, x)
```

Fricas [A]
time = 0.38, size = 149, normalized size = 0.84

$$\frac{8\,\pi b^6 x^6 - (15\,\pi - 8\,\pi b^6 x^6)\,\mathrm{erf}\,(bx)^2 - 4\,\sqrt{\pi}\,(4\,b^5x^5 + 10\,b^3x^3 + 15\,bx - (4\,b^5x^5 + 10\,b^3x^3 + 15\,bx)\,\mathrm{erf}\,(bx))e^{(-b^2x^2)} + 2\,(15\,\pi - 8\,\pi b^6x^6)\,\mathrm{erf}\,(bx) + 4\,(2\,b^4x^4 + 7\,b^2x^2 + 11)e^{(-2\,b^2x^2)}}{48\,\pi b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfc(b*x)^2,x, algorithm="fricas")
```

```
[Out] 1/48*(8*pi*b^6*x^6 - (15*pi - 8*pi*b^6*x^6)*erf(b*x)^2 - 4*sqrt(pi)*(4*b^5*
x^5 + 10*b^3*x^3 + 15*b*x - (4*b^5*x^5 + 10*b^3*x^3 + 15*b*x)*erf(b*x))*e^(
-b^2*x^2) + 2*(15*pi - 8*pi*b^6*x^6)*erf(b*x) + 4*(2*b^4*x^4 + 7*b^2*x^2 +
11)*e^(-2*b^2*x^2))/(pi*b^6)
```

Sympy [A]
time = 0.78, size = 172, normalized size = 0.97

$$\begin{cases} \frac{x^6 \operatorname{erfc}^2(bx)}{6} - \frac{x^5 e^{-b^2x^2} \operatorname{erfc}(bx)}{3\sqrt{\pi}\, b} + \frac{x^4 e^{-2b^2x^2}}{6\pi b^2} - \frac{5x^3 e^{-b^2x^2} \operatorname{erfc}(bx)}{6\sqrt{\pi}\, b^3} + \frac{7x^2 e^{-2b^2x^2}}{12\pi b^4} - \frac{5x e^{-b^2x^2} \operatorname{erfc}(bx)}{4\sqrt{\pi}\, b^5} - \frac{5 \operatorname{erfc}^2(bx)}{16 b^6} + \frac{11 e^{-2b^2x^2}}{12\pi b^6} & \text{for}\ b \neq 0 \\ \frac{x^6}{6} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**5*erfc(b*x)**2,x)
```

```
[Out] Piecewise((x**6*erfc(b*x)**2/6 - x**5*exp(-b**2*x**2)*erfc(b*x)/(3*sqrt(pi)
*b) + x**4*exp(-2*b**2*x**2)/(6*pi*b**2) - 5*x**3*exp(-b**2*x**2)*erfc(b*x)
/(6*sqrt(pi)*b**3) + 7*x**2*exp(-2*b**2*x**2)/(12*pi*b**4) - 5*x*exp(-b**2*
x**2)*erfc(b*x)/(4*sqrt(pi)*b**5) - 5*erfc(b*x)**2/(16*b**6) + 11*exp(-2*b*
*2*x**2)/(12*pi*b**6), Ne(b, 0)), (x**6/6, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfc(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(x^5*erfc(b*x)^2, x)
```

Mupad [B]
time = 0.32, size = 143, normalized size = 0.80

$$\frac{x^6\,\mathrm{erfc}(b\,x)^2}{6}-\frac{\frac{5\,\pi\,\mathrm{erfc}(b\,x)^2}{16}-\frac{11\,\mathrm{e}^{-2\,b^2\,x^2}}{12}-\frac{7\,b^2\,x^2\,\mathrm{e}^{-2\,b^2\,x^2}}{12}-\frac{b^4\,x^4\,\mathrm{e}^{-2\,b^2\,x^2}}{6}+\frac{5\,b^3\,x^3\,\sqrt{\pi}\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfc}(b\,x)}{6}+\frac{b^5\,x^5\,\sqrt{\pi}\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfc}(b\,x)}{3}+\frac{5\,b\,x\,\sqrt{\pi}\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfc}(b\,x)}{4}}{b^6\,\pi}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*erfc(b*x)^2,x)
```

```
[Out] (x^6*erfc(b*x)^2)/6 - ((5*pi*erfc(b*x)^2)/16 - (11*exp(-2*b^2*x^2))/12 - (7
*b^2*x^2*exp(-2*b^2*x^2))/12 - (b^4*x^4*exp(-2*b^2*x^2))/6 + (5*b^3*x^3*pi^
(1/2)*exp(-b^2*x^2)*erfc(b*x))/6 + (b^5*x^5*pi^(1/2)*exp(-b^2*x^2)*erfc(b*x
))/3 + (5*b*x*pi^(1/2)*exp(-b^2*x^2)*erfc(b*x))/4)/(b^6*pi)
```

3.126 $\int x^3 \mathbf{Erfc}(bx)^2 \, dx$

Optimal. Leaf size=126

$$\frac{e^{-2b^2x^2}}{2b^4\pi}+\frac{e^{-2b^2x^2}x^2}{4b^2\pi}-\frac{3e^{-b^2x^2}x\text{Erfc}(bx)}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^3\text{Erfc}(bx)}{2b\sqrt{\pi}}-\frac{3\text{Erfc}(bx)^2}{16b^4}+\frac{1}{4}x^4\text{Erfc}(bx)^2$$

```
[Out] 1/2/b^4/exp(2*b^2*x^2)/Pi+1/4*x^2/b^2/exp(2*b^2*x^2)/Pi-3/16*erfc(b*x)^2/b^
4+1/4*x^4*erfc(b*x)^2-3/4*x*erfc(b*x)/b^3/exp(b^2*x^2)/Pi^(1/2)-1/2*x^3*erf
c(b*x)/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]

time = 0.12, antiderivative size = 126, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.600, Rules used = {6500, 6521, 6509, 30, 2240, 2243}

$$-\frac{3\text{Erfc}(bx)^2}{16b^4}-\frac{x^3e^{-b^2x^2}\text{Erfc}(bx)}{2\sqrt{\pi}\,b}+\frac{x^2e^{-2b^2x^2}}{4\pi b^2}+\frac{e^{-2b^2x^2}}{2\pi b^4}-\frac{3xe^{-b^2x^2}\text{Erfc}(bx)}{4\sqrt{\pi}\,b^3}+\frac{1}{4}x^4\text{Erfc}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[x^3*Erfc[b*x]^2,x]
```

```
[Out] 1/(2*b^4*E^(2*b^2*x^2)*Pi) + x^2/(4*b^2*E^(2*b^2*x^2)*Pi) - (3*x*Erfc[b*x])
/(4*b^3*E^(b^2*x^2)*Sqrt[Pi]) - (x^3*Erfc[b*x])/(2*b*E^(b^2*x^2)*Sqrt[Pi])
- (3*Erfc[b*x]^2)/(16*b^4) + (x^4*Erfc[b*x]^2)/4
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6500

```
Int[Erfc[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfc[b*x]^2
/(m + 1)), x] + Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erfc[b*x])/E^
(b^2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$
\begin{aligned}
\int x^3 \operatorname{erfc}(bx)^2\,dx &= \frac{1}{4}x^4\operatorname{erfc}(bx)^2 + \frac{b\int e^{-b^2x^2}x^4\operatorname{erfc}(bx)\,dx}{\sqrt{\pi}} \\
&= -\frac{e^{-b^2x^2}x^3\operatorname{erfc}(bx)}{2b\sqrt{\pi}} + \frac{1}{4}x^4\operatorname{erfc}(bx)^2 - \frac{\int e^{-2b^2x^2}x^3\,dx}{\pi} + \frac{3\int e^{-b^2x^2}x^2\operatorname{erfc}(bx)\,dx}{2b\sqrt{\pi}} \\
&= \frac{e^{-2b^2x^2}x^2}{4b^2\pi} - \frac{3e^{-b^2x^2}x\operatorname{erfc}(bx)}{4b^3\sqrt{\pi}} - \frac{e^{-b^2x^2}x^3\operatorname{erfc}(bx)}{2b\sqrt{\pi}} + \frac{1}{4}x^4\operatorname{erfc}(bx)^2 - \frac{\int e^{-2b^2x^2}x\,dx}{2b^2\pi} - 3\int \\
&= \frac{e^{-2b^2x^2}}{2b^4\pi} + \frac{e^{-2b^2x^2}x^2}{4b^2\pi} - \frac{3e^{-b^2x^2}x\operatorname{erfc}(bx)}{4b^3\sqrt{\pi}} - \frac{e^{-b^2x^2}x^3\operatorname{erfc}(bx)}{2b\sqrt{\pi}} + \frac{1}{4}x^4\operatorname{erfc}(bx)^2 - 3\mathrm{Subst}(\int \\
&= \frac{e^{-2b^2x^2}}{2b^4\pi} + \frac{e^{-2b^2x^2}x^2}{4b^2\pi} - \frac{3e^{-b^2x^2}x\operatorname{erfc}(bx)}{4b^3\sqrt{\pi}} - \frac{e^{-b^2x^2}x^3\operatorname{erfc}(bx)}{2b\sqrt{\pi}} - \frac{3\operatorname{erfc}(bx)^2}{16b^4} + \frac{1}{4}x^4\operatorname{erfc}(bx)
\end{aligned}
$$

Mathematica [A]
time = 0.26, size = 149, normalized size = 1.18

$$
\frac{1}{8}\left(2x^4 - \frac{2e^{-b^2x^2}x(3+2b^2x^2)}{b^3\sqrt{\pi}} + \left(\frac{3}{b^4} - 4x^4\right)\mathrm{Erf}(bx) + 2x^4\mathrm{Erf}(bx)^2 + \frac{e^{-2b^2x^2}\left(8 + 4b^2x^2 + 4be^{b^2x^2}\sqrt{\pi}\,x(3+2b^2x^2)\,\mathrm{Erf}(bx) - 3e^{2b^2x^2}\pi\mathrm{Erf}(bx)^2\right)}{2b^4\pi}\right)
$$

Antiderivative was successfully verified.

```
[In] Integrate[x^3*Erfc[b*x]^2,x]
```

```
[Out] (2*x^4 - (2*x*(3 + 2*b^2*x^2))/(b^3*E^(b^2*x^2)*Sqrt[Pi]) + (3/b^4 - 4*x^4)
*Erf[b*x] + 2*x^4*Erf[b*x]^2 + (8 + 4*b^2*x^2 + 4*b*E^(b^2*x^2)*Sqrt[Pi]*x*
(3 + 2*b^2*x^2)*Erf[b*x] - 3*E^(2*b^2*x^2)*Pi*Erf[b*x]^2)/(2*b^4*E^(2*b^2*x
^2)*Pi))/8
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int x^3 \operatorname{erfc}(bx)^2 \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erfc(b*x)^2,x)
```

```
[Out] int(x^3*erfc(b*x)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfc(b*x)^2,x, algorithm="maxima")
```

```
[Out] integrate(x^3*erfc(b*x)^2, x)
```

Fricas [A]
time = 0.38, size = 124, normalized size = 0.98

$$\frac{4\,\pi b^4 x^4 - (3\,\pi - 4\,\pi b^4 x^4)\operatorname{erf}(bx)^2 - 4\,\sqrt{\pi}\,(2\,b^3x^3 + 3\,bx - (2\,b^3x^3 + 3\,bx)\operatorname{erf}(bx))e^{(-b^2x^2)} + 2\,(3\,\pi - 4\,\pi b^4x^4)\operatorname{erf}(bx) + 4\,(b^2x^2 + 2)e^{(-2\,b^2x^2)}}{16\,\pi b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfc(b*x)^2,x, algorithm="fricas")
```

```
[Out] 1/16*(4*pi*b^4*x^4 - (3*pi - 4*pi*b^4*x^4)*erf(b*x)^2 - 4*sqrt(pi)*(2*b^3*x
^3 + 3*b*x - (2*b^3*x^3 + 3*b*x)*erf(b*x))*e^(-b^2*x^2) + 2*(3*pi - 4*pi*b^
4*x^4)*erf(b*x) + 4*(b^2*x^2 + 2)*e^(-2*b^2*x^2))/(pi*b^4)
```

Sympy [A]
time = 0.42, size = 121, normalized size = 0.96

$$\begin{cases} \frac{x^4 \operatorname{erfc}^2(bx)}{4} - \frac{x^3 e^{-b^2x^2} \operatorname{erfc}(bx)}{2\sqrt{\pi}\,b} + \frac{x^2 e^{-2b^2x^2}}{4\pi b^2} - \frac{3x e^{-b^2x^2} \operatorname{erfc}(bx)}{4\sqrt{\pi}\,b^3} - \frac{3\operatorname{erfc}^2(bx)}{16b^4} + \frac{e^{-2b^2x^2}}{2\pi b^4} & \text{for}\ b \neq 0 \\ \frac{x^4}{4} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3*erfc(b*x)**2,x)
```

```
[Out] Piecewise((x**4*erfc(b*x)**2/4 - x**3*exp(-b**2*x**2)*erfc(b*x)/(2*sqrt(pi)
*b) + x**2*exp(-2*b**2*x**2)/(4*pi*b**2) - 3*x*exp(-b**2*x**2)*erfc(b*x)/(4
*sqrt(pi)*b**3) - 3*erfc(b*x)**2/(16*b**4) + exp(-2*b**2*x**2)/(2*pi*b**4),
 Ne(b, 0)), (x**4/4, True))
```

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfc(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(x^3*erfc(b*x)^2, x)
```

Mupad [**B**]
time = 0.24, size = 102, normalized size = 0.81

$$\frac{x^4\,\mathrm{erfc}(b\,x)^2}{4}-\frac{\frac{3\,\pi\,\mathrm{erfc}(b\,x)^2}{16}-\frac{\mathrm{e}^{-2\,b^2\,x^2}}{2}-\frac{b^2\,x^2\,\mathrm{e}^{-2\,b^2\,x^2}}{4}+\frac{b^3\,x^3\,\sqrt{\pi}\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfc}(b\,x)}{2}+\frac{3\,b\,x\,\sqrt{\pi}\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfc}(b\,x)}{4}}{b^4\,\pi}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erfc(b*x)^2,x)
```

```
[Out] (x^4*erfc(b*x)^2)/4 - ((3*pi*erfc(b*x)^2)/16 - exp(-2*b^2*x^2)/2 - (b^2*x^2
*exp(-2*b^2*x^2))/4 + (b^3*x^3*pi^(1/2)*exp(-b^2*x^2)*erfc(b*x))/2 + (3*b*x
*pi^(1/2)*exp(-b^2*x^2)*erfc(b*x))/4)/(b^4*pi)
```

3.127 $\int x\mathbf{Erfc}(bx)^2\,dx$

Optimal. Leaf size=72

$$\frac{e^{-2b^2x^2}}{2b^2\pi}-\frac{e^{-b^2x^2}x\mathrm{Erfc}(bx)}{b\sqrt{\pi}}-\frac{\mathrm{Erfc}(bx)^2}{4b^2}+\frac{1}{2}x^2\mathrm{Erfc}(bx)^2$$

```
[Out] 1/2/b^2/exp(2*b^2*x^2)/Pi-1/4*erfc(b*x)^2/b^2+1/2*x^2*erfc(b*x)^2-x*erfc(b*
x)/b/exp(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.06, antiderivative size = 72, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {6500, 6521, 6509, 30, 2240}

$$-\frac{xe^{-b^2x^2}\mathrm{Erfc}(bx)}{\sqrt{\pi}\,b}-\frac{\mathrm{Erfc}(bx)^2}{4b^2}+\frac{e^{-2b^2x^2}}{2\pi b^2}+\frac{1}{2}x^2\mathrm{Erfc}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[x*Erfc[b*x]^2,x]
```

```
[Out] 1/(2*b^2*E^(2*b^2*x^2)*Pi) - (x*Erfc[b*x])/(b*E^(b^2*x^2)*Sqrt[Pi]) - Erfc[
b*x]^2/(4*b^2) + (x^2*Erfc[b*x]^2)/2
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 6500

```
Int[Erfc[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfc[b*x]^2
/(m + 1)), x] + Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erfc[b*x])/E^
(b^2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
```

```
, n}, x] && EqQ[d, -b^2]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int x\text{erfc}(bx)^2\,dx &= \frac{1}{2}x^2\text{erfc}(bx)^2+\frac{(2b)\int e^{-b^2x^2}x^2\text{erfc}(bx)\,dx}{\sqrt{\pi}} \\
&= -\frac{e^{-b^2x^2}x\text{erfc}(bx)}{b\sqrt{\pi}}+\frac{1}{2}x^2\text{erfc}(bx)^2-\frac{2\int e^{-2b^2x^2}x\,dx}{\pi}+\frac{\int e^{-b^2x^2}\text{erfc}(bx)\,dx}{b\sqrt{\pi}} \\
&= \frac{e^{-2b^2x^2}}{2b^2\pi}-\frac{e^{-b^2x^2}x\text{erfc}(bx)}{b\sqrt{\pi}}+\frac{1}{2}x^2\text{erfc}(bx)^2-\frac{\text{Subst}(\int x\,dx,x,\text{erfc}(bx))}{2b^2} \\
&= \frac{e^{-2b^2x^2}}{2b^2\pi}-\frac{e^{-b^2x^2}x\text{erfc}(bx)}{b\sqrt{\pi}}-\frac{\text{erfc}(bx)^2}{4b^2}+\frac{1}{2}x^2\text{erfc}(bx)^2
\end{aligned}$$

Mathematica [A]
time = 0.10, size = 99, normalized size = 1.38

$$\frac{2e^{-2b^2x^2}\left(-1+be^{b^2x^2}\sqrt{\pi}\,x\right)^2+\left(4be^{-b^2x^2}\sqrt{\pi}\,x+\pi(2-4b^2x^2)\right)\text{Erf}(bx)+\pi(-1+2b^2x^2)\,\text{Erf}(bx)^2}{4b^2\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[x*Erfc[b*x]^2,x]
```

```
[Out] ((2*(-1 + b*E^(b^2*x^2)*Sqrt[Pi]*x)^2)/E^(2*b^2*x^2) + ((4*b*Sqrt[Pi]*x)/E^
(b^2*x^2) + Pi*(2 - 4*b^2*x^2))*Erf[b*x] + Pi*(-1 + 2*b^2*x^2)*Erf[b*x]^2)/
(4*b^2*Pi)
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int x\text{erfc}(bx)^2\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfc(b*x)^2,x)
```

```
[Out] int(x*erfc(b*x)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(b*x)^2,x, algorithm="maxima")
```

```
[Out] integrate(x*erfc(b*x)^2, x)
```

Fricas [A]
time = 0.34, size = 91, normalized size = 1.26

$$\frac{2\,\pi b^2x^2 - (\pi - 2\,\pi b^2x^2)\operatorname{erf}(bx)^2 + 4\,\sqrt{\pi}\,(bx\operatorname{erf}(bx) - bx)e^{(-b^2x^2)} + 2\,(\pi - 2\,\pi b^2x^2)\operatorname{erf}(bx) + 2\,e^{(-2\,b^2x^2)}}{4\,\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(b*x)^2,x, algorithm="fricas")
```

```
[Out] 1/4*(2*pi*b^2*x^2 - (pi - 2*pi*b^2*x^2)*erf(b*x)^2 + 4*sqrt(pi)*(b*x*erf(b*
x) - b*x)*e^(-b^2*x^2) + 2*(pi - 2*pi*b^2*x^2)*erf(b*x) + 2*e^(-2*b^2*x^2))
/(pi*b^2)
```

Sympy [A]
time = 0.26, size = 68, normalized size = 0.94

$$\begin{cases} \frac{x^2\operatorname{erfc}^2(bx)}{2} - \frac{xe^{-b^2x^2}\operatorname{erfc}(bx)}{\sqrt{\pi}\,b} - \frac{\operatorname{erfc}^2(bx)}{4b^2} + \frac{e^{-2b^2x^2}}{2\pi b^2} & \text{for } b \neq 0 \\ \frac{x^2}{2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(b*x)**2,x)
```

```
[Out] Piecewise((x**2*erfc(b*x)**2/2 - x*exp(-b**2*x**2)*erfc(b*x)/(sqrt(pi)*b) -
 erfc(b*x)**2/(4*b**2) + exp(-2*b**2*x**2)/(2*pi*b**2), Ne(b, 0)), (x**2/2,
 True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(x*erfc(b*x)^2, x)
```

Mupad [B]
time = 0.20, size = 68, normalized size = 0.94

$$\frac{\frac{\mathrm{e}^{-2\,b^2\,x^2}}{2}-b\,x\,\sqrt{\pi}\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfc}(b\,x)}{b^2\,\pi}-\frac{\frac{\mathrm{erfc}(b\,x)^2}{4}-\frac{b^2\,x^2\,\mathrm{erfc}(b\,x)^2}{2}}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfc(b*x)^2,x)
```

```
[Out] (exp(-2*b^2*x^2)/2 - b*x*pi^(1/2)*exp(-b^2*x^2)*erfc(b*x))/(b^2*pi) - (erfc
(b*x)^2/4 - (b^2*x^2*erfc(b*x)^2)/2)/b^2
```

3.128 $\int \frac{\mathbf{Erfc}(bx)^2}{x}\,dx$

Optimal. Leaf size=13

$$\mathrm{Int}\left(\frac{\mathrm{Erfc}(bx)^2}{x},x\right)$$

```
[Out] Unintegrable(erfc(b*x)^2/x,x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\mathrm{Erfc}(bx)^2}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erfc[b*x]^2/x,x]
```

```
[Out] Defer[Int][Erfc[b*x]^2/x, x]
```

Rubi steps

$$\int \frac{\mathrm{erfc}(bx)^2}{x}\,dx = \int \frac{\mathrm{erfc}(bx)^2}{x}\,dx$$

Mathematica [A]
time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{Erfc}(bx)^2}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfc[b*x]^2/x,x]
```

```
[Out] Integrate[Erfc[b*x]^2/x, x]
```

Maple [A]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{erfc}(bx)^2}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2/x,x)
```

```
[Out] int(erfc(b*x)^2/x,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)^2/x, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x,x, algorithm="fricas")
```

```
[Out] integral((erf(b*x)^2 - 2*erf(b*x) + 1)/x, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}^{2}(bx)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)**2/x,x)
```

```
[Out] Integral(erfc(b*x)**2/x, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)^2/x, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.08

$$\int \frac{\operatorname{erfc}(b\,x)^2}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2/x,x)
```

```
[Out] int(erfc(b*x)^2/x, x)
```

3.129 $\int \frac{\text{Erfc}(bx)^2}{x^3}\,dx$

Optimal. Leaf size=67

$$\frac{2be^{-b^2x^2}\text{Erfc}(bx)}{\sqrt{\pi}\,x}-b^2\text{Erfc}(bx)^2-\frac{\text{Erfc}(bx)^2}{2x^2}+\frac{2b^2\text{Ei}(-2b^2x^2)}{\pi}$$

```
[Out] 2*b^2*Ei(-2*b^2*x^2)/Pi-b^2*erfc(b*x)^2-1/2*erfc(b*x)^2/x^2+2*b*erfc(b*x)/e
xp(b^2*x^2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.06, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}}=0.500$, Rules used = {6500, 6527, 6509, 30, 2241}

$$\frac{2be^{-b^2x^2}\text{Erfc}(bx)}{\sqrt{\pi}\,x}+b^2\left(-\text{Erfc}(bx)^2\right)+\frac{2b^2\text{Ei}(-2b^2x^2)}{\pi}-\frac{\text{Erfc}(bx)^2}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]^2/x^3,x]
```

```
[Out] (2*b*Erfc[b*x])/(E^(b^2*x^2)*Sqrt[Pi]*x) - b^2*Erfc[b*x]^2 - Erfc[b*x]^2/(2
*x^2) + (2*b^2*ExpIntegralEi[-2*b^2*x^2])/Pi
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 6500

```
Int[Erfc[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfc[b*x]^2
/(m + 1)), x] + Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erfc[b*x])/E^
(b^2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6527

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x],
x]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{\operatorname{erfc}(bx)^2}{x^3}\,dx &= -\frac{\operatorname{erfc}(bx)^2}{2x^2} - \frac{(2b)\int \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x^2}\,dx}{\sqrt{\pi}} \\
&= \frac{2be^{-b^2x^2}\operatorname{erfc}(bx)}{\sqrt{\pi}\,x} - \frac{\operatorname{erfc}(bx)^2}{2x^2} + \frac{(4b^2)\int \frac{e^{-2b^2x^2}}{x}\,dx}{\pi} + \frac{(4b^3)\int e^{-b^2x^2}\operatorname{erfc}(bx)\,dx}{\sqrt{\pi}} \\
&= \frac{2be^{-b^2x^2}\operatorname{erfc}(bx)}{\sqrt{\pi}\,x} - \frac{\operatorname{erfc}(bx)^2}{2x^2} + \frac{2b^2\operatorname{Ei}(-2b^2x^2)}{\pi} - (2b^2)\operatorname{Subst}\left(\int x\,dx, x, \operatorname{erfc}(bx)\right) \\
&= \frac{2be^{-b^2x^2}\operatorname{erfc}(bx)}{\sqrt{\pi}\,x} - b^2\operatorname{erfc}(bx)^2 - \frac{\operatorname{erfc}(bx)^2}{2x^2} + \frac{2b^2\operatorname{Ei}(-2b^2x^2)}{\pi}
\end{aligned}
$$

Mathematica [A]
time = 0.02, size = 63, normalized size = 0.94

$$\frac{2be^{-b^2x^2}\operatorname{Erfc}(bx)}{\sqrt{\pi}\,x} + \left(-b^2 - \frac{1}{2x^2}\right)\operatorname{Erfc}(bx)^2 + \frac{2b^2\operatorname{Ei}(-2b^2x^2)}{\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]^2/x^3,x]
[Out] (2*b*Erfc[b*x])/(E^(b^2*x^2)*Sqrt[Pi]*x) + (-b^2 - 1/(2*x^2))*Erfc[b*x]^2 +
 (2*b^2*ExpIntegralEi[-2*b^2*x^2])/Pi
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}(bx)^2}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2/x^3,x)
[Out] int(erfc(b*x)^2/x^3,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^3,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)^2/x^3, x)
```

Fricas [A]
time = 0.36, size = 98, normalized size = 1.46

$$-\frac{\pi - 4\,\pi\sqrt{b^2}\,bx^2\,\mathrm{erf}\left(\sqrt{b^2}\,x\right) - 4\,b^2x^2\mathrm{Ei}(-2\,b^2x^2) + (\pi + 2\,\pi b^2x^2)\,\mathrm{erf}\,(bx)^2 + 4\,\sqrt{\pi}\,(bx\,\mathrm{erf}\,(bx) - bx)e^{(-b^2x^2)} - 2\,\pi\,\mathrm{erf}\,(bx)}{2\,\pi x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^3,x, algorithm="fricas")
```

```
[Out] -1/2*(pi - 4*pi*sqrt(b^2)*b*x^2*erf(sqrt(b^2)*x) - 4*b^2*x^2*Ei(-2*b^2*x^2)
 + (pi + 2*pi*b^2*x^2)*erf(b*x)^2 + 4*sqrt(pi)*(b*x*erf(b*x) - b*x)*e^(-b^2
*x^2) - 2*pi*erf(b*x))/(pi*x^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{erfc}^2\,(bx)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)**2/x**3,x)
```

```
[Out] Integral(erfc(b*x)**2/x**3, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^3,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)^2/x^3, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erfc}(b\,x)^2}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2/x^3,x)
```

```
[Out] int(erfc(b*x)^2/x^3, x)
```

3.130 $\int \frac{\text{Erfc}(bx)^2}{x^5} \, dx$

Optimal. Leaf size=125

$$-\frac{b^2 e^{-2b^2x^2}}{3\pi x^2}+\frac{be^{-b^2x^2}\text{Erfc}(bx)}{3\sqrt{\pi}\,x^3}-\frac{2b^3e^{-b^2x^2}\text{Erfc}(bx)}{3\sqrt{\pi}\,x}+\frac{1}{3}b^4\text{Erfc}(bx)^2-\frac{\text{Erfc}(bx)^2}{4x^4}-\frac{4b^4\text{Ei}(-2b^2x^2)}{3\pi}$$

```
[Out] -1/3*b^2/exp(2*b^2*x^2)/Pi/x^2-4/3*b^4*Ei(-2*b^2*x^2)/Pi+1/3*b^4*erfc(b*x)^
2-1/4*erfc(b*x)^2/x^4+1/3*b*erfc(b*x)/exp(b^2*x^2)/x^3/Pi^(1/2)-2/3*b^3*erf
c(b*x)/exp(b^2*x^2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.12, antiderivative size = 125, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.600$, Rules used = {6500, 6527, 6509, 30, 2241, 2245}

$$\frac{1}{3}b^4\text{Erfc}(bx)^2+\frac{be^{-b^2x^2}\text{Erfc}(bx)}{3\sqrt{\pi}\,x^3}-\frac{b^2e^{-2b^2x^2}}{3\pi x^2}-\frac{4b^4\text{Ei}(-2b^2x^2)}{3\pi}-\frac{2b^3e^{-b^2x^2}\text{Erfc}(bx)}{3\sqrt{\pi}\,x}-\frac{\text{Erfc}(bx)^2}{4x^4}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]^2/x^5,x]
```

```
[Out] -1/3*b^2/(E^(2*b^2*x^2)*Pi*x^2) + (b*Erfc[b*x])/(3*E^(b^2*x^2)*Sqrt[Pi]*x^3
) - (2*b^3*Erfc[b*x])/(3*E^(b^2*x^2)*Sqrt[Pi]*x) + (b^4*Erfc[b*x]^2)/3 - Er
fc[b*x]^2/(4*x^4) - (4*b^4*ExpIntegralEi[-2*b^2*x^2])/(3*Pi)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6500

```
Int[Erfc[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfc[b*x]^2
/(m + 1)), x] + Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erfc[b*x])/E^
(b^2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6527

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x],
x]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{\operatorname{erfc}(bx)^2}{x^5}\,dx &= -\frac{\operatorname{erfc}(bx)^2}{4x^4}-\frac{b\int \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x^4}\,dx}{\sqrt{\pi}}\\
&= \frac{be^{-b^2x^2}\operatorname{erfc}(bx)}{3\sqrt{\pi}\,x^3}-\frac{\operatorname{erfc}(bx)^2}{4x^4}+\frac{(2b^2)\int \frac{e^{-2b^2x^2}}{x^3}\,dx}{3\pi}+\frac{(2b^3)\int \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x^2}\,dx}{3\sqrt{\pi}}\\
&= -\frac{b^2e^{-2b^2x^2}}{3\pi x^2}+\frac{be^{-b^2x^2}\operatorname{erfc}(bx)}{3\sqrt{\pi}\,x^3}-\frac{2b^3e^{-b^2x^2}\operatorname{erfc}(bx)}{3\sqrt{\pi}\,x}-\frac{\operatorname{erfc}(bx)^2}{4x^4}-2\frac{(4b^4)\int \frac{e^{-2b^2x^2}}{x}\,dx}{3\pi}-\frac{(4b^5\\
&= -\frac{b^2e^{-2b^2x^2}}{3\pi x^2}+\frac{be^{-b^2x^2}\operatorname{erfc}(bx)}{3\sqrt{\pi}\,x^3}-\frac{2b^3e^{-b^2x^2}\operatorname{erfc}(bx)}{3\sqrt{\pi}\,x}-\frac{\operatorname{erfc}(bx)^2}{4x^4}-\frac{4b^4\operatorname{Ei}(-2b^2x^2)}{3\pi}+\frac{1}{3}(2b^4)\,\mathrm{S}\\
&= -\frac{b^2e^{-2b^2x^2}}{3\pi x^2}+\frac{be^{-b^2x^2}\operatorname{erfc}(bx)}{3\sqrt{\pi}\,x^3}-\frac{2b^3e^{-b^2x^2}\operatorname{erfc}(bx)}{3\sqrt{\pi}\,x}+\frac{1}{3}b^4\operatorname{erfc}(bx)^2-\frac{\operatorname{erfc}(bx)^2}{4x^4}-\frac{4b^4\operatorname{Ei}(-2b}{3\pi}\end{aligned}$$

Mathematica [A]
time = 0.06, size = 97, normalized size = 0.78

$$\frac{-\frac{4be^{-b^2x^2}x(-1+2b^2x^2)\operatorname{Erfc}(bx)}{\sqrt{\pi}}+(-3+4b^4x^4)\operatorname{Erfc}(bx)^2-\frac{4b^2x^2\left(e^{-2b^2x^2}+4b^2x^2\operatorname{Ei}(-2b^2x^2)\right)}{\pi}}{12x^4}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]^2/x^5,x]
```

```
[Out] ((-4*b*x*(-1 + 2*b^2*x^2)*Erfc[b*x])/(E^(b^2*x^2)*Sqrt[Pi]) + (-3 + 4*b^4*x
^4)*Erfc[b*x]^2 - (4*b^2*x^2*(E^(-2*b^2*x^2) + 4*b^2*x^2*ExpIntegralEi[-2*b
^2*x^2]))/Pi)/(12*x^4)
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}(bx)^2}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2/x^5,x)
```

```
[Out] int(erfc(b*x)^2/x^5,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^5,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)^2/x^5, x)
```

Fricas [A]
time = 0.36, size = 141, normalized size = 1.13

$$-\frac{3\,\pi + 8\,\pi\sqrt{b^2}\,b^3x^4\operatorname{erf}\left(\sqrt{b^2}\,x\right) + 16\,b^4x^4\operatorname{Ei}(-2\,b^2x^2) + 4\,b^2x^2e^{(-2\,b^2x^2)} + (3\,\pi - 4\,\pi b^4x^4)\operatorname{erf}(bx)^2 + 4\,\sqrt{\pi}\,(2\,b^3x^3 - bx - (2\,b^3x^3 - bx)\operatorname{erf}(bx))e^{(-b^2x^2)} - 6\,\pi\operatorname{erf}(bx)}{12\,\pi x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^5,x, algorithm="fricas")
```

```
[Out] -1/12*(3*pi + 8*pi*sqrt(b^2)*b^3*x^4*erf(sqrt(b^2)*x) + 16*b^4*x^4*Ei(-2*b^
2*x^2) + 4*b^2*x^2*e^(-2*b^2*x^2) + (3*pi - 4*pi*b^4*x^4)*erf(b*x)^2 + 4*sq
rt(pi)*(2*b^3*x^3 - b*x - (2*b^3*x^3 - b*x)*erf(b*x))*e^(-b^2*x^2) - 6*pi*e
rf(b*x))/(pi*x^4)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}^2(bx)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)**2/x**5,x)
```

```
[Out] Integral(erfc(b*x)**2/x**5, x)
```

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^5,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)^2/x^5, x)
```

Mupad [**F**]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erfc}(b\,x)^2}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2/x^5,x)
```

```
[Out] int(erfc(b*x)^2/x^5, x)
```

3.131 $\int \frac{\mathbf{Erfc}(bx)^2}{x^7}\,dx$

Optimal. Leaf size=177

$$-\frac{b^2e^{-2b^2x^2}}{15\pi x^4}+\frac{2b^4e^{-2b^2x^2}}{9\pi x^2}+\frac{2be^{-b^2x^2}\mathrm{Erfc}(bx)}{15\sqrt{\pi}\,x^5}-\frac{4b^3e^{-b^2x^2}\mathrm{Erfc}(bx)}{45\sqrt{\pi}\,x^3}+\frac{8b^5e^{-b^2x^2}\mathrm{Erfc}(bx)}{45\sqrt{\pi}\,x}-\frac{4}{45}b^6\mathrm{Erfc}(bx)^2-\frac{\mathrm{Erfc}(bx}{6x^6}$$

```
[Out] -1/15*b^2/exp(2*b^2*x^2)/Pi/x^4+2/9*b^4/exp(2*b^2*x^2)/Pi/x^2+28/45*b^6*Ei(
-2*b^2*x^2)/Pi-4/45*b^6*erfc(b*x)^2-1/6*erfc(b*x)^2/x^6+2/15*b*erfc(b*x)/ex
p(b^2*x^2)/x^5/Pi^(1/2)-4/45*b^3*erfc(b*x)/exp(b^2*x^2)/x^3/Pi^(1/2)+8/45*b
^5*erfc(b*x)/exp(b^2*x^2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.21, antiderivative size = 177, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.600$, Rules used = {6500, 6527, 6509, 30, 2241, 2245}

$$-\frac{4}{45}b^6\mathrm{Erfc}(bx)^2+\frac{2be^{-b^2x^2}\mathrm{Erfc}(bx)}{15\sqrt{\pi}\,x^5}-\frac{b^2e^{-2b^2x^2}}{15\pi x^4}+\frac{28b^6\mathrm{Ei}(-2b^2x^2)}{45\pi}+\frac{8b^5e^{-b^2x^2}\mathrm{Erfc}(bx)}{45\sqrt{\pi}\,x}+\frac{2b^4e^{-2b^2x^2}}{9\pi x^2}-\frac{4b^3e^{-b^2x^2}\mathrm{Erfc}(bx)}{45\sqrt{\pi}\,x^3}-\frac{\mathrm{Erfc}(bx)^2}{6x^6}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]^2/x^7,x]
```

```
[Out] -1/15*b^2/(E^(2*b^2*x^2)*Pi*x^4) + (2*b^4)/(9*E^(2*b^2*x^2)*Pi*x^2) + (2*b*
Erfc[b*x])/(15*E^(b^2*x^2)*Sqrt[Pi]*x^5) - (4*b^3*Erfc[b*x])/(45*E^(b^2*x^2
)*Sqrt[Pi]*x^3) + (8*b^5*Erfc[b*x])/(45*E^(b^2*x^2)*Sqrt[Pi]*x) - (4*b^6*Er
fc[b*x]^2)/45 - Erfc[b*x]^2/(6*x^6) + (28*b^6*ExpIntegralEi[-2*b^2*x^2])/(4
5*Pi)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
```

```
] && LeQ[-n, m + 1]))
```

Rule 6500

```
Int[Erfc[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfc[b*x]^2
/(m + 1)), x] + Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erfc[b*x])/E^
(b^2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6527

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x],
x]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int \frac{\operatorname{erfc}(bx)^2}{x^7}\,dx &= -\frac{\operatorname{erfc}(bx)^2}{6x^6} - \frac{(2b)\int \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x^6}\,dx}{3\sqrt{\pi}} \\
&= \frac{2be^{-b^2x^2}\operatorname{erfc}(bx)}{15\sqrt{\pi}\,x^5} - \frac{\operatorname{erfc}(bx)^2}{6x^6} + \frac{(4b^2)\int \frac{e^{-2b^2x^2}}{x^5}\,dx}{15\pi} + \frac{(4b^3)\int \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x^4}\,dx}{15\sqrt{\pi}} \\
&= -\frac{b^2e^{-2b^2x^2}}{15\pi x^4} + \frac{2be^{-b^2x^2}\operatorname{erfc}(bx)}{15\sqrt{\pi}\,x^5} - \frac{4b^3e^{-b^2x^2}\operatorname{erfc}(bx)}{45\sqrt{\pi}\,x^3} - \frac{\operatorname{erfc}(bx)^2}{6x^6} - \frac{(8b^4)\int \frac{e^{-2b^2x^2}}{x^3}\,dx}{45\pi} - \frac{(4b^4 \\
&= -\frac{b^2e^{-2b^2x^2}}{15\pi x^4} + \frac{2b^4e^{-2b^2x^2}}{9\pi x^2} + \frac{2be^{-b^2x^2}\operatorname{erfc}(bx)}{15\sqrt{\pi}\,x^5} - \frac{4b^3e^{-b^2x^2}\operatorname{erfc}(bx)}{45\sqrt{\pi}\,x^3} + \frac{8b^5e^{-b^2x^2}\operatorname{erfc}(bx)}{45\sqrt{\pi}\,x} - \operatorname{erf} \\
&= -\frac{b^2e^{-2b^2x^2}}{15\pi x^4} + \frac{2b^4e^{-2b^2x^2}}{9\pi x^2} + \frac{2be^{-b^2x^2}\operatorname{erfc}(bx)}{15\sqrt{\pi}\,x^5} - \frac{4b^3e^{-b^2x^2}\operatorname{erfc}(bx)}{45\sqrt{\pi}\,x^3} + \frac{8b^5e^{-b^2x^2}\operatorname{erfc}(bx)}{45\sqrt{\pi}\,x} - \operatorname{erf} \\
&= -\frac{b^2e^{-2b^2x^2}}{15\pi x^4} + \frac{2b^4e^{-2b^2x^2}}{9\pi x^2} + \frac{2be^{-b^2x^2}\operatorname{erfc}(bx)}{15\sqrt{\pi}\,x^5} - \frac{4b^3e^{-b^2x^2}\operatorname{erfc}(bx)}{45\sqrt{\pi}\,x^3} + \frac{8b^5e^{-b^2x^2}\operatorname{erfc}(bx)}{45\sqrt{\pi}\,x} - \frac{4}{45}
\end{aligned}$$

Mathematica [A]
time = 0.03, size = 133, normalized size = 0.75

$$\frac{e^{-2b^2x^2}\left(-6b^2x^2+20b^4x^4+4be^{b^2x^2}\sqrt{\pi}\,x(3-2b^2x^2+4b^4x^4)\operatorname{Erfc}(bx)-e^{2b^2x^2}\pi(15+8b^6x^6)\operatorname{Erfc}(bx)^2+56b^6e^{2b^2x^2}x^6\operatorname{Ei}(-2b^2x^2)\right)}{90\pi x^6}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]^2/x^7,x]
```

```
[Out] (-6*b^2*x^2 + 20*b^4*x^4 + 4*b*E^(b^2*x^2)*Sqrt[Pi]*x*(3 - 2*b^2*x^2 + 4*b^
4*x^4)*Erfc[b*x] - E^(2*b^2*x^2)*Pi*(15 + 8*b^6*x^6)*Erfc[b*x]^2 + 56*b^6*E
^(2*b^2*x^2)*x^6*ExpIntegralEi[-2*b^2*x^2])/(90*E^(2*b^2*x^2)*Pi*x^6)
```

Maple [F]
time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}(bx)^2}{x^7}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2/x^7,x)
```

```
[Out] int(erfc(b*x)^2/x^7,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^7,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)^2/x^7, x)
```

Fricas [A]
time = 0.36, size = 168, normalized size = 0.95

$$-\frac{15\,\pi - 16\,\pi\sqrt{b^2}\,b^5x^6\operatorname{erf}\left(\sqrt{b^2}\,x\right) - 56\,b^6x^6\operatorname{Ei}(-2\,b^2x^2) + (15\,\pi + 8\,\pi b^6x^6)\operatorname{erf}(bx)^2 - 4\,\sqrt{\pi}\,(4\,b^5x^5 - 2\,b^3x^3 + 3\,bx - (4\,b^5x^5 - 2\,b^3x^3 + 3\,bx)\operatorname{erf}(bx))e^{(-b^2x^2)} - 30\,\pi\operatorname{erf}(bx) - 2\,(10\,b^4x^4 - 3\,b^2x^2)e^{(-2\,b^2x^2)}}{90\,\pi x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^7,x, algorithm="fricas")
```

```
[Out] -1/90*(15*pi - 16*pi*sqrt(b^2)*b^5*x^6*erf(sqrt(b^2)*x) - 56*b^6*x^6*Ei(-2*
b^2*x^2) + (15*pi + 8*pi*b^6*x^6)*erf(b*x)^2 - 4*sqrt(pi)*(4*b^5*x^5 - 2*b^
3*x^3 + 3*b*x - (4*b^5*x^5 - 2*b^3*x^3 + 3*b*x)*erf(b*x))*e^(-b^2*x^2) - 30
*pi*erf(b*x) - 2*(10*b^4*x^4 - 3*b^2*x^2)*e^(-2*b^2*x^2))/(pi*x^6)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}^2(bx)}{x^7}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)**2/x**7,x)
```

```
[Out] Integral(erfc(b*x)**2/x**7, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^7,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)^2/x^7, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erfc}(b\,x)^2}{x^7}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2/x^7,x)
```

```
[Out] int(erfc(b*x)^2/x^7, x)
```

3.132 $\int x^4 \mathbf{Erfc}(bx)^2\,dx$

Optimal. Leaf size=165

$$\frac{11e^{-2b^2x^2}x}{20b^4\pi}+\frac{e^{-2b^2x^2}x^3}{5b^2\pi}-\frac{43\mathrm{Erf}\left(\sqrt{2}\,bx\right)}{40b^5\sqrt{2\pi}}-\frac{4e^{-b^2x^2}\mathrm{Erfc}(bx)}{5b^5\sqrt{\pi}}-\frac{4e^{-b^2x^2}x^2\mathrm{Erfc}(bx)}{5b^3\sqrt{\pi}}-\frac{2e^{-b^2x^2}x^4\mathrm{Erfc}(bx)}{5b\sqrt{\pi}}+\frac{1}{5}x^5\mathrm{Erfc}$$

```
[Out] 11/20*x/b^4/exp(2*b^2*x^2)/Pi+1/5*x^3/b^2/exp(2*b^2*x^2)/Pi+1/5*x^5*erfc(b*
x)^2-4/5*erfc(b*x)/b^5/exp(b^2*x^2)/Pi^(1/2)-4/5*x^2*erfc(b*x)/b^3/exp(b^2*
x^2)/Pi^(1/2)-2/5*x^4*erfc(b*x)/b/exp(b^2*x^2)/Pi^(1/2)-43/80*erf(b*x*2^(1/
2))/b^5*2^(1/2)/Pi^(1/2)
```

Rubi [A]

time = 0.16, antiderivative size = 165, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.500, Rules used = {6500, 6521, 6518, 2236, 2243}

$$-\frac{43\mathrm{Erf}\left(\sqrt{2}\,bx\right)}{40\sqrt{2\pi}\,b^5}-\frac{2x^4e^{-b^2x^2}\mathrm{Erfc}(bx)}{5\sqrt{\pi}\,b}+\frac{x^3e^{-2b^2x^2}}{5\pi b^2}-\frac{4e^{-b^2x^2}\mathrm{Erfc}(bx)}{5\sqrt{\pi}\,b^5}+\frac{11xe^{-2b^2x^2}}{20\pi b^4}-\frac{4x^2e^{-b^2x^2}\mathrm{Erfc}(bx)}{5\sqrt{\pi}\,b^3}+\frac{1}{5}x^5\mathrm{Erfc}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[x^4*Erfc[b*x]^2,x]
```

```
[Out] (11*x)/(20*b^4*E^(2*b^2*x^2)*Pi) + x^3/(5*b^2*E^(2*b^2*x^2)*Pi) - (43*Erf[S
qrt[2]*b*x])/(40*b^5*Sqrt[2*Pi]) - (4*Erfc[b*x])/(5*b^5*E^(b^2*x^2)*Sqrt[Pi
]) - (4*x^2*Erfc[b*x])/(5*b^3*E^(b^2*x^2)*Sqrt[Pi]) - (2*x^4*Erfc[b*x])/(5*
b*E^(b^2*x^2)*Sqrt[Pi]) + (x^5*Erfc[b*x]^2)/5
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6500

```
Int[Erfc[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfc[b*x]^2
/(m + 1)), x] + Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erfc[b*x])/E^
```

```
(b^2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int x^4\operatorname{erfc}(bx)^2\,dx &= \frac{1}{5}x^5\operatorname{erfc}(bx)^2+\frac{(4b)\int e^{-b^2x^2}x^5\operatorname{erfc}(bx)\,dx}{5\sqrt{\pi}}\\
&= -\frac{2e^{-b^2x^2}x^4\operatorname{erfc}(bx)}{5b\sqrt{\pi}}+\frac{1}{5}x^5\operatorname{erfc}(bx)^2-\frac{4\int e^{-2b^2x^2}x^4\,dx}{5\pi}+\frac{8\int e^{-b^2x^2}x^3\operatorname{erfc}(bx)\,dx}{5b\sqrt{\pi}}\\
&= \frac{e^{-2b^2x^2}x^3}{5b^2\pi}-\frac{4e^{-b^2x^2}x^2\operatorname{erfc}(bx)}{5b^3\sqrt{\pi}}-\frac{2e^{-b^2x^2}x^4\operatorname{erfc}(bx)}{5b\sqrt{\pi}}+\frac{1}{5}x^5\operatorname{erfc}(bx)^2-\frac{3\int e^{-2b^2x^2}x^2\,dx}{5b^2\pi}-\\
&= \frac{11e^{-2b^2x^2}x}{20b^4\pi}+\frac{e^{-2b^2x^2}x^3}{5b^2\pi}-\frac{4e^{-b^2x^2}\operatorname{erfc}(bx)}{5b^5\sqrt{\pi}}-\frac{4e^{-b^2x^2}x^2\operatorname{erfc}(bx)}{5b^3\sqrt{\pi}}-\frac{2e^{-b^2x^2}x^4\operatorname{erfc}(bx)}{5b\sqrt{\pi}}+\frac{1}{5}x\\
&= \frac{11e^{-2b^2x^2}x}{20b^4\pi}+\frac{e^{-2b^2x^2}x^3}{5b^2\pi}-\frac{2\sqrt{\frac{2}{\pi}}\operatorname{erf}\left(\sqrt{2}\,bx\right)}{5b^5}-\frac{11\operatorname{erf}\left(\sqrt{2}\,bx\right)}{40b^5\sqrt{2\pi}}-\frac{4e^{-b^2x^2}\operatorname{erfc}(bx)}{5b^5\sqrt{\pi}}-4e^{-}
\end{aligned}$$

Mathematica [A]
time = 0.11, size = 108, normalized size = 0.65

$$\frac{-43\sqrt{2\pi}\,\mathrm{Erf}\left(\sqrt{2}\,bx\right)+4\left(be^{-2b^2x^2}x(11+4b^2x^2)-8e^{-b^2x^2}\sqrt{\pi}\,(2+2b^2x^2+b^4x^4)\,\mathrm{Erfc}(bx)+4b^5\pi x^5\mathrm{Erfc}(bx)^2\right)}{80b^5\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^4*Erfc[b*x]^2,x]
```

```
[Out] (-43*Sqrt[2*Pi]*Erf[Sqrt[2]*b*x] + 4*((b*x*(11 + 4*b^2*x^2))/E^(2*b^2*x^2)
- (8*Sqrt[Pi]*(2 + 2*b^2*x^2 + b^4*x^4)*Erfc[b*x])/E^(b^2*x^2) + 4*b^5*Pi*x
^5*Erfc[b*x]^2))/(80*b^5*Pi)
```

Maple [A]
time = 0.19, size = 205, normalized size = 1.24

method	result
derivativedivides	$\frac{\frac{b^{5} x^{5}}{5}-\frac{2 \operatorname{erf}(b x) b^{5} x^{5}}{5}+\frac{-\frac{2 b^{4} x^{4} \mathrm{e}^{-b^{2} x^{2}}}{5}-\frac{4 b^{2} x^{2} \mathrm{e}^{-b^{2} x^{2}}}{5}-\frac{4 \,\mathrm{e}^{-b^{2} x^{2}}}{5}}{\sqrt{\pi}}+\frac{\operatorname{erf}(b x)^{2} b^{5} x^{5}}{5}-\frac{4 \operatorname{erf}(b x) \big(-\frac{b^{4} x^{4} \mathrm{e}^{-b^{2} x^{2}}}{2}-b^{2} x^{2} \mathrm{e}^{-b^{2} x^{2}}-\mathrm{e}^{-b}}{5 \sqrt{\pi}}}{b^{5}}$
default	$\frac{\frac{b^{5} x^{5}}{5}-\frac{2 \operatorname{erf}(b x) b^{5} x^{5}}{5}+\frac{-\frac{2 b^{4} x^{4} \mathrm{e}^{-b^{2} x^{2}}}{5}-\frac{4 b^{2} x^{2} \mathrm{e}^{-b^{2} x^{2}}}{5}-\frac{4 \,\mathrm{e}^{-b^{2} x^{2}}}{5}}{\sqrt{\pi}}+\frac{\operatorname{erf}(b x)^{2} b^{5} x^{5}}{5}-\frac{4 \operatorname{erf}(b x) \big(-\frac{b^{4} x^{4} \mathrm{e}^{-b^{2} x^{2}}}{2}-b^{2} x^{2} \mathrm{e}^{-b^{2} x^{2}}-\mathrm{e}^{-b}}{5 \sqrt{\pi}}}{b^{5}}$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erfc(b*x)^2,x,method=_RETURNVERBOSE)
```

```
[Out] 1/b^5*(1/5*b^5*x^5-2/5*erf(b*x)*b^5*x^5+4/5/Pi^(1/2)*(-1/2/exp(b^2*x^2)*b^4
*x^4-b^2*x^2/exp(b^2*x^2)-1/exp(b^2*x^2))+1/5*erf(b*x)^2*b^5*x^5-4/5*erf(b*
x)/Pi^(1/2)*(-1/2/exp(b^2*x^2)*b^4*x^4-b^2*x^2/exp(b^2*x^2)-1/exp(b^2*x^2))
+4/5/Pi*(-43/64*2^(1/2)*Pi^(1/2)*erf(b*x*2^(1/2))+11/16/exp(b^2*x^2)^2*b*x+
1/4/exp(b^2*x^2)^2*b^3*x^3))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfc(b*x)^2,x, algorithm="maxima")
```

```
[Out] integrate(x^4*erfc(b*x)^2, x)
```

Fricas [A]
time = 0.37, size = 154, normalized size = 0.93

$$\frac{16 \pi b^{6} x^{5} \operatorname{erf}(b x)^{2}-32 \pi b^{6} x^{5} \operatorname{erf}(b x)+16 \pi b^{6} x^{5}-43 \sqrt{2} \sqrt{\pi} \sqrt{b^{2}} \operatorname{erf}\left(\sqrt{2} \sqrt{b^{2}} x\right)-32 \sqrt{\pi}\left(b^{5} x^{4}+2 b^{3} x^{2}-\left(b^{5} x^{4}+2 b^{3} x^{2}+2 b\right) \operatorname{erf}(b x)+2 b\right) e^{\left(-b^{2} x^{2}\right)}+4\left(4 b^{4} x^{3}+11 b^{2} x\right) e^{\left(-2 b^{2} x^{2}\right)}}{80 \pi b^{6}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfc(b*x)^2,x, algorithm="fricas")
```

```
[Out] 1/80*(16*pi*b^6*x^5*erf(b*x)^2 - 32*pi*b^6*x^5*erf(b*x) + 16*pi*b^6*x^5 - 4
3*sqrt(2)*sqrt(pi)*sqrt(b^2)*erf(sqrt(2)*sqrt(b^2)*x) - 32*sqrt(pi)*(b^5*x^
4 + 2*b^3*x^2 - (b^5*x^4 + 2*b^3*x^2 + 2*b)*erf(b*x) + 2*b)*e^(-b^2*x^2) +
4*(4*b^4*x^3 + 11*b^2*x)*e^(-2*b^2*x^2))/(pi*b^6)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x^4 \operatorname{erfc}^2(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4*erfc(b*x)**2,x)
```

```
[Out] Integral(x**4*erfc(b*x)**2, x)
```

Giac [A]
time = 0.47, size = 218, normalized size = 1.32

$$\frac{1}{5}x^5\operatorname{erf}(bx)^2 - \frac{2}{5}x^5\operatorname{erf}(bx) + \frac{1}{5}x^5 + \frac{b\left(\frac{32\,(b^4x^4+2\,b^2x^2+2)\operatorname{erf}(bx)e^{\left(-b^2x^2\right)}}{b^6} + \frac{b^4\left(\frac{4\,(4\,b^2x^3+3\,x)e^{\left(-2\,b^2x^2\right)}}{b^4} + \frac{3\,\sqrt{2}\,\sqrt{\pi}\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{b^5}\right) + 8\,b^2\left(\frac{4\,xe^{\left(-2\,b^2x^2\right)}}{b^2} + \frac{\sqrt{2}\,\sqrt{\pi}\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{b^3}\right) + \frac{32\,\sqrt{2}\,\sqrt{\pi}\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{b}}{\sqrt{\pi}\,b^5}\right)}{80\,\sqrt{\pi}} - \frac{2\,(b^4x^4+2\,b^2x^2+2)e^{\left(-b^2x^2\right)}}{5\,\sqrt{\pi}\,b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfc(b*x)^2,x, algorithm="giac")
```

```
[Out] 1/5*x^5*erf(b*x)^2 - 2/5*x^5*erf(b*x) + 1/5*x^5 + 1/80*b*(32*(b^4*x^4 + 2*b
^2*x^2 + 2)*erf(b*x)*e^(-b^2*x^2)/b^6 + (b^4*(4*(4*b^2*x^3 + 3*x)*e^(-2*b^2
*x^2)/b^4 + 3*sqrt(2)*sqrt(pi)*erf(-sqrt(2)*b*x)/b^5) + 8*b^2*(4*x*e^(-2*b^
2*x^2)/b^2 + sqrt(2)*sqrt(pi)*erf(-sqrt(2)*b*x)/b^3) + 32*sqrt(2)*sqrt(pi)*
erf(-sqrt(2)*b*x)/b)/(sqrt(pi)*b^5))/sqrt(pi) - 2/5*(b^4*x^4 + 2*b^2*x^2 +
2)*e^(-b^2*x^2)/(sqrt(pi)*b^5)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^4\,{\mathrm{erfc}\left(b\,x\right)}^2 \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erfc(b*x)^2,x)
```

```
[Out] int(x^4*erfc(b*x)^2, x)
```

3.133 $\int x^2 \mathbf{Erfc}(bx)^2\, dx$

Optimal. Leaf size=113

$$\frac{e^{-2b^2x^2}x}{3b^2\pi}-\frac{5\mathrm{Erf}\left(\sqrt{2}\,bx\right)}{6b^3\sqrt{2\pi}}-\frac{2e^{-b^2x^2}\mathrm{Erfc}(bx)}{3b^3\sqrt{\pi}}-\frac{2e^{-b^2x^2}x^2\mathrm{Erfc}(bx)}{3b\sqrt{\pi}}+\frac{1}{3}x^3\mathrm{Erfc}(bx)^2$$

```
[Out] 1/3*x/b^2/exp(2*b^2*x^2)/Pi+1/3*x^3*erfc(b*x)^2-2/3*erfc(b*x)/b^3/exp(b^2*x
^2)/Pi^(1/2)-2/3*x^2*erfc(b*x)/b/exp(b^2*x^2)/Pi^(1/2)-5/12*erf(b*x*2^(1/2)
)/b^3*2^(1/2)/Pi^(1/2)
```

Rubi [A]
time = 0.09, antiderivative size = 113, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules used = {6500, 6521, 6518, 2236, 2243}

$$-\frac{5\mathrm{Erf}\left(\sqrt{2}\,bx\right)}{6\sqrt{2\pi}\,b^3}-\frac{2x^2e^{-b^2x^2}\mathrm{Erfc}(bx)}{3\sqrt{\pi}\,b}+\frac{xe^{-2b^2x^2}}{3\pi b^2}-\frac{2e^{-b^2x^2}\mathrm{Erfc}(bx)}{3\sqrt{\pi}\,b^3}+\frac{1}{3}x^3\mathrm{Erfc}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[x^2*Erfc[b*x]^2,x]
```

```
[Out] x/(3*b^2*E^(2*b^2*x^2)*Pi) - (5*Erf[Sqrt[2]*b*x])/(6*b^3*Sqrt[2*Pi]) - (2*E
rfc[b*x])/(3*b^3*E^(b^2*x^2)*Sqrt[Pi]) - (2*x^2*Erfc[b*x])/(3*b*E^(b^2*x^2)
*Sqrt[Pi]) + (x^3*Erfc[b*x]^2)/3
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6500

```
Int[Erfc[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfc[b*x]^2
/(m + 1)), x] + Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erfc[b*x])/E^
```

```
(b^2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int x^2\operatorname{erfc}(bx)^2\,dx &= \frac{1}{3}x^3\operatorname{erfc}(bx)^2+\frac{(4b)\int e^{-b^2x^2}x^3\operatorname{erfc}(bx)\,dx}{3\sqrt{\pi}}\\
&= -\frac{2e^{-b^2x^2}x^2\operatorname{erfc}(bx)}{3b\sqrt{\pi}}+\frac{1}{3}x^3\operatorname{erfc}(bx)^2-\frac{4\int e^{-2b^2x^2}x^2\,dx}{3\pi}+\frac{4\int e^{-b^2x^2}x\operatorname{erfc}(bx)\,dx}{3b\sqrt{\pi}}\\
&= \frac{e^{-2b^2x^2}x}{3b^2\pi}-\frac{2e^{-b^2x^2}\operatorname{erfc}(bx)}{3b^3\sqrt{\pi}}-\frac{2e^{-b^2x^2}x^2\operatorname{erfc}(bx)}{3b\sqrt{\pi}}+\frac{1}{3}x^3\operatorname{erfc}(bx)^2-\frac{\int e^{-2b^2x^2}\,dx}{3b^2\pi}-\frac{4\int e^{-2}}{3b^2}\\
&= \frac{e^{-2b^2x^2}x}{3b^2\pi}-\frac{\sqrt{\frac{2}{\pi}}\operatorname{erf}\left(\sqrt{2}\,bx\right)}{3b^3}-\frac{\operatorname{erf}\left(\sqrt{2}\,bx\right)}{6b^3\sqrt{2\pi}}-\frac{2e^{-b^2x^2}\operatorname{erfc}(bx)}{3b^3\sqrt{\pi}}-\frac{2e^{-b^2x^2}x^2\operatorname{erfc}(bx)}{3b\sqrt{\pi}}+\frac{1}{3}
\end{aligned}$$

Mathematica [A]
time = 0.06, size = 88, normalized size = 0.78

$$\frac{4be^{-2b^2x^2}x-5\sqrt{2\pi}\operatorname{Erf}\left(\sqrt{2}\,bx\right)-8e^{-b^2x^2}\sqrt{\pi}\,(1+b^2x^2)\operatorname{Erfc}(bx)+4b^3\pi x^3\operatorname{Erfc}(bx)^2}{12b^3\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*Erfc[b*x]^2,x]
[Out] ((4*b*x)/E^(2*b^2*x^2) - 5*Sqrt[2*Pi]*Erf[Sqrt[2]*b*x] - (8*Sqrt[Pi]*(1 + b
^2*x^2)*Erfc[b*x])/E^(b^2*x^2) + 4*b^3*Pi*x^3*Erfc[b*x]^2)/(12*b^3*Pi)
```

Maple [A]
time = 0.33, size = 151, normalized size = 1.34

method	result
derivativedivides	$\frac{\frac{b^3x^3}{3}-\frac{2\operatorname{erf}(bx)b^3x^3}{3}+\frac{-\frac{2b^2x^2\mathrm{e}^{-b^2x^2}}{3}-\frac{2\,\mathrm{e}^{-b^2x^2}}{3}}{\sqrt{\pi}}+\frac{\operatorname{erf}(bx)^2b^3x^3}{3}-\frac{4\operatorname{erf}(bx)\left(-\frac{b^2x^2\mathrm{e}^{-b^2x^2}}{2}-\frac{\mathrm{e}^{-b^2x^2}}{2}\right)}{3\sqrt{\pi}}+\frac{-\frac{5\sqrt{2}\sqrt{\pi}\operatorname{erf}(}{12}}{}}{b^3}$
default	$\frac{\frac{b^3x^3}{3}-\frac{2\operatorname{erf}(bx)b^3x^3}{3}+\frac{-\frac{2b^2x^2\mathrm{e}^{-b^2x^2}}{3}-\frac{2\,\mathrm{e}^{-b^2x^2}}{3}}{\sqrt{\pi}}+\frac{\operatorname{erf}(bx)^2b^3x^3}{3}-\frac{4\operatorname{erf}(bx)\left(-\frac{b^2x^2\mathrm{e}^{-b^2x^2}}{2}-\frac{\mathrm{e}^{-b^2x^2}}{2}\right)}{3\sqrt{\pi}}+\frac{-\frac{5\sqrt{2}\sqrt{\pi}\operatorname{erf}(}{12}}{}}{b^3}$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfc(b*x)^2,x,method=_RETURNVERBOSE)
```

```
[Out] 1/b^3*(1/3*b^3*x^3-2/3*erf(b*x)*b^3*x^3+4/3/Pi^(1/2)*(-1/2*b^2*x^2/exp(b^2*
x^2)-1/2/exp(b^2*x^2))+1/3*erf(b*x)^2*b^3*x^3-4/3*erf(b*x)/Pi^(1/2)*(-1/2*b
^2*x^2/exp(b^2*x^2)-1/2/exp(b^2*x^2))+4/3/Pi*(-5/16*2^(1/2)*Pi^(1/2)*erf(b*
x*2^(1/2))+1/4/exp(b^2*x^2)^2*b*x))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfc(b*x)^2,x, algorithm="maxima")
```

```
[Out] integrate(x^2*erfc(b*x)^2, x)
```

Fricas [A]
time = 0.35, size = 123, normalized size = 1.09

$$\frac{4\,\pi b^4x^3\operatorname{erf}(bx)^2-8\,\pi b^4x^3\operatorname{erf}(bx)+4\,\pi b^4x^3+4\,b^2xe^{(-2\,b^2x^2)}-5\,\sqrt{2}\,\sqrt{\pi}\,\sqrt{b^2}\,\operatorname{erf}\left(\sqrt{2}\,\sqrt{b^2}\,x\right)-8\,\sqrt{\pi}\,(b^3x^2-(b^3x^2+b)\operatorname{erf}(bx)+b)e^{(-b^2x^2)}}{12\,\pi b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfc(b*x)^2,x, algorithm="fricas")
```

```
[Out] 1/12*(4*pi*b^4*x^3*erf(b*x)^2 - 8*pi*b^4*x^3*erf(b*x) + 4*pi*b^4*x^3 + 4*b^
2*x*e^(-2*b^2*x^2) - 5*sqrt(2)*sqrt(pi)*sqrt(b^2)*erf(sqrt(2)*sqrt(b^2)*x)
- 8*sqrt(pi)*(b^3*x^2 - (b^3*x^2 + b)*erf(b*x) + b)*e^(-b^2*x^2))/(pi*b^4)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x^2\operatorname{erfc}^2(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*erfc(b*x)**2,x)
```

```
[Out] Integral(x**2*erfc(b*x)**2, x)
```

Giac [A]
time = 0.46, size = 151, normalized size = 1.34

$$\frac{1}{3}x^3\operatorname{erf}(bx)^2-\frac{2}{3}x^3\operatorname{erf}(bx)+\frac{1}{3}x^3+\frac{b\left(\frac{8\,(b^2x^2+1)\operatorname{erf}(bx)e^{\left(-b^2x^2\right)}}{b^4}+\frac{b^2\left(\frac{4\,xe^{\left(-2\,b^2x^2\right)}}{b^2}+\frac{\sqrt{2}\sqrt{\pi}\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{b^3}\right)+\frac{4\,\sqrt{2}\sqrt{\pi}\operatorname{erf}\left(-\sqrt{2}\,bx\right)}{b}}{\sqrt{\pi}\,b^3}\right)}{12\,\sqrt{\pi}}-\frac{2\,(b^2x^2+1)e^{\left(-b^2x^2\right)}}{3\,\sqrt{\pi}\,b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfc(b*x)^2,x, algorithm="giac")
```

```
[Out] 1/3*x^3*erf(b*x)^2 - 2/3*x^3*erf(b*x) + 1/3*x^3 + 1/12*b*(8*(b^2*x^2 + 1)*e
rf(b*x)*e^(-b^2*x^2)/b^4 + (b^2*(4*x*e^(-2*b^2*x^2)/b^2 + sqrt(2)*sqrt(pi)*
erf(-sqrt(2)*b*x)/b^3) + 4*sqrt(2)*sqrt(pi)*erf(-sqrt(2)*b*x)/b)/(sqrt(pi)*
b^3))/sqrt(pi) - 2/3*(b^2*x^2 + 1)*e^(-b^2*x^2)/(sqrt(pi)*b^3)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^2\,\operatorname{erfc}(b\,x)^2\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfc(b*x)^2,x)
```

```
[Out] int(x^2*erfc(b*x)^2, x)
```

3.134 $\int \mathrm{Erfc}(bx)^2\,dx$

Optimal. Leaf size=56

$$-\frac{\sqrt{\frac{2}{\pi}}\,\mathrm{Erf}\left(\sqrt{2}\,bx\right)}{b}-\frac{2e^{-b^2x^2}\mathrm{Erfc}(bx)}{b\sqrt{\pi}}+x\mathrm{Erfc}(bx)^2$$

```
[Out] x*erfc(b*x)^2-erf(b*x*2^(1/2))*2^(1/2)/Pi^(1/2)/b-2*erfc(b*x)/b/exp(b^2*x^2
)/Pi^(1/2)
```

Rubi [A]
time = 0.03, antiderivative size = 56, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.667$, Rules used = {6488, 12, 6518, 2236}

$$-\frac{2e^{-b^2x^2}\mathrm{Erfc}(bx)}{\sqrt{\pi}\,b}-\frac{\sqrt{\frac{2}{\pi}}\,\mathrm{Erf}\left(\sqrt{2}\,bx\right)}{b}+x\mathrm{Erfc}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]^2,x]
```

```
[Out] -((Sqrt[2/Pi]*Erf[Sqrt[2]*b*x])/b) - (2*Erfc[b*x])/(b*E^(b^2*x^2)*Sqrt[Pi])
 + x*Erfc[b*x]^2
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 6488

```
Int[Erfc[(a_.) + (b_.)*(x_)]^2, x_Symbol] :> Simp[(a + b*x)*(Erfc[a + b*x]^
2/b), x] + Dist[4/Sqrt[Pi], Int[(a + b*x)*(Erfc[a + b*x]/E^(a + b*x)^2), x]
, x] /; FreeQ[{a, b}, x]
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
```

```
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\begin{aligned}\int \operatorname{erfc}(bx)^2\,dx &= x\operatorname{erfc}(bx)^2 + \frac{4\int be^{-b^2x^2}x\operatorname{erfc}(bx)\,dx}{\sqrt{\pi}}\\ &= x\operatorname{erfc}(bx)^2 + \frac{(4b)\int e^{-b^2x^2}x\operatorname{erfc}(bx)\,dx}{\sqrt{\pi}}\\ &= -\frac{2e^{-b^2x^2}\operatorname{erfc}(bx)}{b\sqrt{\pi}} + x\operatorname{erfc}(bx)^2 - \frac{4\int e^{-2b^2x^2}\,dx}{\pi}\\ &= -\frac{\sqrt{\frac{2}{\pi}}\operatorname{erf}\left(\sqrt{2}\,bx\right)}{b} - \frac{2e^{-b^2x^2}\operatorname{erfc}(bx)}{b\sqrt{\pi}} + x\operatorname{erfc}(bx)^2\end{aligned}$$

Mathematica [A]
time = 0.03, size = 56, normalized size = 1.00

$$-\frac{\sqrt{\frac{2}{\pi}}\operatorname{Erf}\left(\sqrt{2}\,bx\right)}{b} - \frac{2e^{-b^2x^2}\operatorname{Erfc}(bx)}{b\sqrt{\pi}} + x\operatorname{Erfc}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]^2,x]
[Out] -((Sqrt[2/Pi]*Erf[Sqrt[2]*b*x])/b) - (2*Erfc[b*x])/(b*E^(b^2*x^2)*Sqrt[Pi])
 + x*Erfc[b*x]^2
```

Maple [A]
time = 0.19, size = 48, normalized size = 0.86

method	result	size
derivativedivides	$\frac{\operatorname{erf}(bx)^2 bx+\frac{2\operatorname{erf}(bx)e^{-b^2x^2}}{\sqrt{\pi}}-\frac{\sqrt{2}\,\operatorname{erf}\left(bx\sqrt{2}\right)}{\sqrt{\pi}}}{b}$	48
default	$\frac{\operatorname{erf}(bx)^2 bx+\frac{2\operatorname{erf}(bx)e^{-b^2x^2}}{\sqrt{\pi}}-\frac{\sqrt{2}\,\operatorname{erf}\left(bx\sqrt{2}\right)}{\sqrt{\pi}}}{b}$	48

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2,x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*(erf(b*x)^2*b*x+2*erf(b*x)/Pi^(1/2)*exp(-b^2*x^2)-1/Pi^(1/2)*2^(1/2)*er
f(b*x*2^(1/2)))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)^2, x)
```

Fricas [A]
time = 0.33, size = 85, normalized size = 1.52

$$\frac{\pi b^2 x \operatorname{erf}(bx)^2 - 2\pi b^2 x \operatorname{erf}(bx) + \pi b^2 x - \sqrt{2}\sqrt{\pi}\sqrt{b^2}\operatorname{erf}\left(\sqrt{2}\sqrt{b^2}x\right) + 2\sqrt{\pi}(b\operatorname{erf}(bx) - b)e^{(-b^2x^2)}}{\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2,x, algorithm="fricas")
```

```
[Out] (pi*b^2*x*erf(b*x)^2 - 2*pi*b^2*x*erf(b*x) + pi*b^2*x - sqrt(2)*sqrt(pi)*sq
rt(b^2)*erf(sqrt(2)*sqrt(b^2)*x) + 2*sqrt(pi)*(b*erf(b*x) - b)*e^(-b^2*x^2)
)/(pi*b^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \operatorname{erfc}^2(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)**2,x)
```

```
[Out] Integral(erfc(b*x)**2, x)
```

Giac [A]
time = 0.44, size = 73, normalized size = 1.30

$$x\operatorname{erf}(bx)^2 - 2x\operatorname{erf}(bx) + \frac{b\left(\frac{2\operatorname{erf}(bx)e^{(-b^2x^2)}}{b^2} + \frac{\sqrt{2}\operatorname{erf}\left(-\sqrt{2}bx\right)}{b^2}\right)}{\sqrt{\pi}} + x - \frac{2e^{(-b^2x^2)}}{\sqrt{\pi}b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2,x, algorithm="giac")
```

```
[Out] x*erf(b*x)^2 - 2*x*erf(b*x) + b*(2*erf(b*x)*e^(-b^2*x^2)/b^2 + sqrt(2)*erf(
-sqrt(2)*b*x)/b^2)/sqrt(pi) + x - 2*e^(-b^2*x^2)/(sqrt(pi)*b)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \mathrm{erfc}(b\,x)^2\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2,x)
```

```
[Out] int(erfc(b*x)^2, x)
```

3.135 $\int \frac{\text{Erfc}(bx)^2}{x^2} dx$

Optimal. Leaf size=13

$$\text{Int}\left(\frac{\text{Erfc}(bx)^2}{x^2}, x\right)$$

```
[Out] Unintegrable(erfc(b*x)^2/x^2,x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.000, Rules used = {}

$$\int \frac{\text{Erfc}(bx)^2}{x^2} dx$$

Verification is not applicable to the result.

```
[In] Int[Erfc[b*x]^2/x^2,x]
[Out] Defer[Int][Erfc[b*x]^2/x^2, x]
```

Rubi steps

$$\int \frac{\text{erfc}(bx)^2}{x^2} dx = \int \frac{\text{erfc}(bx)^2}{x^2} dx$$

Mathematica [A]
time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{\text{Erfc}(bx)^2}{x^2} dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfc[b*x]^2/x^2,x]
[Out] Integrate[Erfc[b*x]^2/x^2, x]
```

Maple [A]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\text{erfc}(bx)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2/x^2,x)
```

```
[Out] int(erfc(b*x)^2/x^2,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^2,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)^2/x^2, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^2,x, algorithm="fricas")
```

```
[Out] integral((erf(b*x)^2 - 2*erf(b*x) + 1)/x^2, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}^2(bx)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)**2/x**2,x)
```

```
[Out] Integral(erfc(b*x)**2/x**2, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^2,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)^2/x^2, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.08

$$\int \frac{\operatorname{erfc}(b\,x)^2}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2/x^2,x)
```

```
[Out] int(erfc(b*x)^2/x^2, x)
```

3.136 $\int \frac{\text{Erfc}(bx)^2}{x^4} \, dx$

Optimal. Leaf size=13

$$\text{Int}\left(\frac{\text{Erfc}(bx)^2}{x^4}, x\right)$$

```
[Out] Unintegrable(erfc(b*x)^2/x^4,x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\text{Erfc}(bx)^2}{x^4} \, dx$$

Verification is not applicable to the result.

```
[In] Int[Erfc[b*x]^2/x^4,x]
```

```
[Out] Defer[Int][Erfc[b*x]^2/x^4, x]
```

Rubi steps

$$\int \frac{\text{erfc}(bx)^2}{x^4} \, dx = \int \frac{\text{erfc}(bx)^2}{x^4} \, dx$$

Mathematica [A]
time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{\text{Erfc}(bx)^2}{x^4} \, dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfc[b*x]^2/x^4,x]
```

```
[Out] Integrate[Erfc[b*x]^2/x^4, x]
```

Maple [A]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\text{erfc}(bx)^2}{x^4} \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2/x^4,x)
```

```
[Out] int(erfc(b*x)^2/x^4,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^4,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)^2/x^4, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^4,x, algorithm="fricas")
```

```
[Out] integral((erf(b*x)^2 - 2*erf(b*x) + 1)/x^4, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}^2(bx)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)**2/x**4,x)
```

```
[Out] Integral(erfc(b*x)**2/x**4, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^4,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)^2/x^4, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.08

$$\int \frac{\operatorname{erfc}(b\,x)^2}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2/x^4,x)
```

```
[Out] int(erfc(b*x)^2/x^4, x)
```

3.137 $\int \frac{\textbf{Erfc}(bx)^2}{x^6} dx$

Optimal. Leaf size=13

$$\text{Int}\left(\frac{\text{Erfc}(bx)^2}{x^6}, x\right)$$

[Out] Unintegrable(erfc(b*x)^2/x^6,x)

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\text{Erfc}(bx)^2}{x^6} dx$$

Verification is not applicable to the result.

[In] Int[Erfc[b*x]^2/x^6,x]

[Out] Defer[Int][Erfc[b*x]^2/x^6, x]

Rubi steps

$$\int \frac{\text{erfc}(bx)^2}{x^6} dx = \int \frac{\text{erfc}(bx)^2}{x^6} dx$$

Mathematica [A]
time = 0.11, size = 0, normalized size = 0.00

$$\int \frac{\text{Erfc}(bx)^2}{x^6} dx$$

Verification is not applicable to the result.

[In] Integrate[Erfc[b*x]^2/x^6,x]

[Out] Integrate[Erfc[b*x]^2/x^6, x]

Maple [A]
time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{\text{erfc}(bx)^2}{x^6} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2/x^6,x)
```

```
[Out] int(erfc(b*x)^2/x^6,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^6,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)^2/x^6, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^6,x, algorithm="fricas")
```

```
[Out] integral((erf(b*x)^2 - 2*erf(b*x) + 1)/x^6, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}^{2}(bx)}{x^{6}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)**2/x**6,x)
```

```
[Out] Integral(erfc(b*x)**2/x**6, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)^2/x^6,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)^2/x^6, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.08

$$\int \frac{\operatorname{erfc}(b\,x)^2}{x^6}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)^2/x^6,x)
```

```
[Out] int(erfc(b*x)^2/x^6, x)
```

3.138 $\int (c+dx)^2 \mathbf{Erfc}(a+bx)^2\,dx$

Optimal. Leaf size=375

$$\frac{d(bc-ad)e^{-2(a+bx)^2}}{b^3\pi}+\frac{d^2e^{-2(a+bx)^2}(a+bx)}{3b^3\pi}-\frac{(bc-ad)^2\sqrt{\frac{2}{\pi}}\,\mathrm{Erf}\left(\sqrt{2}\,(a+bx)\right)}{b^3}-\frac{5d^2\mathrm{Erf}\left(\sqrt{2}\,(a+bx)\right)}{6b^3\sqrt{2\pi}}-2d^2$$

```
[Out] d*(-a*d+b*c)/b^3/exp(2*(b*x+a)^2)/Pi+1/3*d^2*(b*x+a)/b^3/exp(2*(b*x+a)^2)/P
i-1/2*d*(-a*d+b*c)*erfc(b*x+a)^2/b^3+(-a*d+b*c)^2*(b*x+a)*erfc(b*x+a)^2/b^3
+d*(-a*d+b*c)*(b*x+a)^2*erfc(b*x+a)^2/b^3+1/3*d^2*(b*x+a)^3*erfc(b*x+a)^2/b
^3-(-a*d+b*c)^2*erf((b*x+a)*2^(1/2))*2^(1/2)/Pi^(1/2)/b^3-2/3*d^2*erfc(b*x+
a)/b^3/exp((b*x+a)^2)/Pi^(1/2)-2*(-a*d+b*c)^2*erfc(b*x+a)/b^3/exp((b*x+a)^2
)/Pi^(1/2)-2*d*(-a*d+b*c)*(b*x+a)*erfc(b*x+a)/b^3/exp((b*x+a)^2)/Pi^(1/2)-2
/3*d^2*(b*x+a)^2*erfc(b*x+a)/b^3/exp((b*x+a)^2)/Pi^(1/2)-5/12*d^2*erf((b*x+
a)*2^(1/2))/b^3*2^(1/2)/Pi^(1/2)
```

Rubi [A]

time = 0.27, antiderivative size = 375, normalized size of antiderivative = 1.00, number of steps used = 16, number of rules used = 10, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {6503, 6488, 6518, 2236, 6500, 6521, 6509, 30, 2240, 2243}

$$-\frac{\sqrt{\frac{2}{\pi}}(bc-ad)^2\mathrm{Erf}\left(\sqrt{2}\,(a+bx)\right)}{b^3}+\frac{d(a+bx)^2(bc-ad)\mathrm{Erfc}(a+bx)^2}{b^3}+\frac{(a+bx)(bc-ad)^2\mathrm{Erfc}(a+bx)^2}{b^3}-\frac{2de^{-(a+bx)^2}(a+bx)(bc-ad)\mathrm{Erfc}(a+bx)}{\sqrt{\pi}\,b^3}-\frac{d(bc-ad)\mathrm{Erfc}(a+bx)^2}{2b^3}-\frac{2e^{-(a+bx)^2}(bc-ad)^2\mathrm{Erfc}(a+bx)}{\sqrt{\pi}\,b^3}+\frac{de^{-2(a+bx)^2}(bc-ad)}{\pi b^3}-\frac{5d^2\mathrm{Erf}\left(\sqrt{2}\,(a+bx)\right)}{6\sqrt{2\pi}\,b^3}+\frac{d^2(a+bx)^3\mathrm{Erfc}(a+bx)^2}{3b^3}-\frac{2d^2e^{-(a+bx)^2}(a+bx)^2\mathrm{Erfc}(a+bx)}{3\sqrt{\pi}\,b^3}-\frac{2d^2e^{-(a+bx)^2}\mathrm{Erfc}(a+bx)}{3\sqrt{\pi}\,b^3}+\frac{d^2e^{-2(a+bx)^2}(a+bx)}{3\pi b^3}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)^2*Erfc[a + b*x]^2,x]
```

```
[Out] (d*(b*c - a*d))/(b^3*E^(2*(a + b*x)^2)*Pi) + (d^2*(a + b*x))/(3*b^3*E^(2*(a
 + b*x)^2)*Pi) - ((b*c - a*d)^2*Sqrt[2/Pi]*Erf[Sqrt[2]*(a + b*x)])/b^3 - (5
*d^2*Erf[Sqrt[2]*(a + b*x)])/(6*b^3*Sqrt[2*Pi]) - (2*d^2*Erfc[a + b*x])/(3*
b^3*E^(a + b*x)^2*Sqrt[Pi]) - (2*(b*c - a*d)^2*Erfc[a + b*x])/(b^3*E^(a + b
*x)^2*Sqrt[Pi]) - (2*d*(b*c - a*d)*(a + b*x)*Erfc[a + b*x])/(b^3*E^(a + b*x
)^2*Sqrt[Pi]) - (2*d^2*(a + b*x)^2*Erfc[a + b*x])/(3*b^3*E^(a + b*x)^2*Sqrt
[Pi]) - (d*(b*c - a*d)*Erfc[a + b*x]^2)/(2*b^3) + ((b*c - a*d)^2*(a + b*x)*
Erfc[a + b*x]^2)/b^3 + (d*(b*c - a*d)*(a + b*x)^2*Erfc[a + b*x]^2)/b^3 + (d
^2*(a + b*x)^3*Erfc[a + b*x]^2)/(3*b^3)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
```

```
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6488

```
Int[Erfc[(a_.) + (b_.)*(x_)]^2, x_Symbol] :> Simp[(a + b*x)*(Erfc[a + b*x]^
2/b), x] + Dist[4/Sqrt[Pi], Int[(a + b*x)*(Erfc[a + b*x]/E^(a + b*x)^2), x]
, x] /; FreeQ[{a, b}, x]
```

Rule 6500

```
Int[Erfc[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfc[b*x]^2
/(m + 1)), x] + Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erfc[b*x])/E^
(b^2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6503

```
Int[Erfc[(a_) + (b_.)*(x_)]^2*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Dist
[1/b^(m + 1), Subst[Int[ExpandIntegrand[Erfc[x]^2, (b*c - a*d + d*x)^m, x],
 x], x, a + b*x], x] /; FreeQ[{a, b, c, d}, x] && IGtQ[m, 0]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
```

```
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\int (c+dx)^2\text{erfc}(a+bx)^2\,dx = \frac{\text{Subst}\Big(\int \Big(b^2c^2\Big(1+\frac{ad(-2bc+ad)}{b^2c^2}\Big)\,\text{erfc}(x)^2 + 2bcd\big(1-\frac{ad}{bc}\big)\,x\text{erfc}(x)^2 + d^2x^2\text{erfc}(}{b^3}$$

$$= \frac{d^2\text{Subst}\big(\int x^2\text{erfc}(x)^2\,dx, x, a+bx\big)}{b^3} + \frac{(2d(bc-ad))\text{Subst}\big(\int x\text{erfc}(x)^2\,dx, x, a}{b^3}$$

$$= \frac{(bc-ad)^2(a+bx)\text{erfc}(a+bx)^2}{b^3} + \frac{d(bc-ad)(a+bx)^2\text{erfc}(a+bx)^2}{b^3} + \frac{d^2(a+}{}$$

$$= -\frac{2(bc-ad)^2e^{-(a+bx)^2}\text{erfc}(a+bx)}{b^3\sqrt{\pi}} - \frac{2d(bc-ad)e^{-(a+bx)^2}(a+bx)\text{erfc}(a+bx)}{b^3\sqrt{\pi}}$$

$$= \frac{d(bc-ad)e^{-2(a+bx)^2}}{b^3\pi} + \frac{d^2e^{-2(a+bx)^2}(a+bx)}{3b^3\pi} - \frac{(bc-ad)^2\sqrt{\frac{2}{\pi}}\,\text{erf}\Big(\sqrt{2}\,(a+bx}{b^3}$$

$$= \frac{d(bc-ad)e^{-2(a+bx)^2}}{b^3\pi} + \frac{d^2e^{-2(a+bx)^2}(a+bx)}{3b^3\pi} - \frac{d^2\sqrt{\frac{2}{\pi}}\,\text{erf}\Big(\sqrt{2}\,(a+bx)\Big)}{3b^3} - \frac{(b}{}$$

Mathematica [A]
time = 3.20, size = 610, normalized size = 1.63

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^2*Erfc[a + b*x]^2,x]
```

```
[Out] (-12*b^2*Sqrt[Pi]*(c + d*x)^2*(Sqrt[2]*Erf[Sqrt[2]*(a + b*x)] + Erfc[a + b*
x]*(2/E^(a + b*x)^2 - Sqrt[Pi]*(a + b*x)*Erfc[a + b*x])) + 6*b*d*(c + d*x)*
(2/E^(2*(a + b*x)^2) + (4*Sqrt[Pi]*(a + b*x))/E^(a + b*x)^2 - 2*Pi*(a + b*x
)^2 - 2*Pi*Erf[a + b*x] - (4*Sqrt[Pi]*(a + b*x)*Erf[a + b*x])/E^(a + b*x)^2
```

```
 + 4*Pi*(a + b*x)^2*Erf[a + b*x] + Pi*Erf[a + b*x]^2 - 2*Pi*(a + b*x)^2*Erf
[a + b*x]^2 + 4*a*Sqrt[2*Pi]*Erf[Sqrt[2]*(a + b*x)] + 4*b*Sqrt[2*Pi]*x*Erf[
Sqrt[2]*(a + b*x)] + 2*Pi*(2 + Erfc[-a - b*x]*Erfc[a + b*x]) - 4*Sqrt[Pi]*(
a + b*x)*ExpIntegralE[1/2, (a + b*x)^2]) + d^2*((24*Sqrt[Pi])/E^(a + b*x)^2
 - 36*b*Pi*x + 12*a^2*b*Pi*x + 12*a*b^2*Pi*x^2 + 4*b^3*Pi*x^3 - (8*(a + b*x
))/E^(2*(a + b*x)^2) - (8*Sqrt[Pi]*(1 + (a + b*x)^2))/E^(a + b*x)^2 + 12*a*
Pi*Erf[a + b*x] + 12*b*Pi*x*Erf[a + b*x] - 8*Pi*(a + b*x)^3*Erf[a + b*x] +
(8*Sqrt[Pi]*(1 + (a + b*x)^2)*Erf[a + b*x])/E^(a + b*x)^2 + 6*Pi*(a + b*x)*
Erf[a + b*x]^2 + 4*Pi*(a + b*x)^3*Erf[a + b*x]^2 - 5*Sqrt[2*Pi]*Erf[Sqrt[2]
*(a + b*x)] - 12*a^2*Sqrt[2*Pi]*Erf[Sqrt[2]*(a + b*x)] - 12*b*Sqrt[2*Pi]*x*
(2*a + b*x)*Erf[Sqrt[2]*(a + b*x)] - 12*Sqrt[Pi]*ExpIntegralE[3/2, (a + b*x
)^2]))/(12*b^3*Pi)
```

Maple [**F**]
time = 0.14, size = 0, normalized size = 0.00

$$\int (dx+c)^2 \operatorname{erfc}(bx+a)^2 \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^2*erfc(b*x+a)^2,x)
```

```
[Out] int((d*x+c)^2*erfc(b*x+a)^2,x)
```

Maxima [**F**]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erfc(b*x+a)^2,x, algorithm="maxima")
```

```
[Out] integrate((d*x + c)^2*erfc(b*x + a)^2, x)
```

Fricas [**A**]
time = 0.35, size = 472, normalized size = 1.26

$$\frac{4\,\pi b^4 d^2 x^3 + 12\,\pi b^4 c d x^2 + 12\,\pi b^4 c^2 x - \sqrt{2}\,\sqrt{\pi}\,(12\,b^2c^2 - 24\,abcd + (12\,a^2+5)d^2)\sqrt{b^2}\,\operatorname{erf}\left(\frac{\sqrt{2}\,\sqrt{b^2}\,(bx+a)}{b}\right) - 4\,\pi(6\,ab^2c^2 - 3\,(2\,a^2+1)bcd + (2\,a^3+3\,a)d^2)\sqrt{b^2}\,\operatorname{erf}\left(\frac{\sqrt{b^2}\,(bx+a)}{b}\right) + 2\,(2\,\pi b^4d^2x^3 + 6\,\pi b^4cdx^2 + 6\,\pi b^4c^2x + \pi(6\,ab^3c^2 - 3\,(2\,a^2+1)b^2cd + (2\,a^3+3\,a)bd^2))\operatorname{erf}(bx+a)^2 - 8\,\sqrt{\pi}\,(b^3d^2x^2 + 3\,b^3c^2 - 3\,ab^2cd + (a^2+1)bd^2 + (3\,b^3cd - ab^2d^2)x - (b^3d^2x^2 + 3\,b^3c^2 - 3\,ab^2cd + (a^2+1)bd^2 + (3\,b^3cd - ab^2d^2)x)\operatorname{erf}(bx+a))e^{(-b^2x^2-2\,abx-a^2)} - 8\,(\pi b^4d^2x^3 + 3\,\pi b^4cdx^2 + 3\,\pi b^4c^2x)\operatorname{erf}(bx+a) + 4\,(b^2d^2x + 3\,b^2cd - 2\,abd^2)e^{(-2\,b^2x^2-4\,abx-2\,a^2)}}{12\,\pi b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erfc(b*x+a)^2,x, algorithm="fricas")
```

```
[Out] 1/12*(4*pi*b^4*d^2*x^3 + 12*pi*b^4*c*d*x^2 + 12*pi*b^4*c^2*x - sqrt(2)*sqrt
(pi)*(12*b^2*c^2 - 24*a*b*c*d + (12*a^2 + 5)*d^2)*sqrt(b^2)*erf(sqrt(2)*sqr
t(b^2)*(b*x + a)/b) - 4*pi*(6*a*b^2*c^2 - 3*(2*a^2 + 1)*b*c*d + (2*a^3 + 3*
a)*d^2)*sqrt(b^2)*erf(sqrt(b^2)*(b*x + a)/b) + 2*(2*pi*b^4*d^2*x^3 + 6*pi*b
```

```
^4*c*d*x^2 + 6*pi*b^4*c^2*x + pi*(6*a*b^3*c^2 - 3*(2*a^2 + 1)*b^2*c*d + (2*
a^3 + 3*a)*b*d^2))*erf(b*x + a)^2 - 8*sqrt(pi)*(b^3*d^2*x^2 + 3*b^3*c^2 - 3
*a*b^2*c*d + (a^2 + 1)*b*d^2 + (3*b^3*c*d - a*b^2*d^2)*x - (b^3*d^2*x^2 + 3
*b^3*c^2 - 3*a*b^2*c*d + (a^2 + 1)*b*d^2 + (3*b^3*c*d - a*b^2*d^2)*x)*erf(b
*x + a))*e^(-b^2*x^2 - 2*a*b*x - a^2) - 8*(pi*b^4*d^2*x^3 + 3*pi*b^4*c*d*x^
2 + 3*pi*b^4*c^2*x)*erf(b*x + a) + 4*(b^2*d^2*x + 3*b^2*c*d - 2*a*b*d^2)*e^
(-2*b^2*x^2 - 4*a*b*x - 2*a^2))/(pi*b^4)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int (c+dx)^2 \operatorname{erfc}^2(a+bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**2*erfc(b*x+a)**2,x)
[Out] Integral((c + d*x)**2*erfc(a + b*x)**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erfc(b*x+a)^2,x, algorithm="giac")
[Out] integrate((d*x + c)^2*erfc(b*x + a)^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.00

$$\int \operatorname{erfc}(a+b\,x)^2\,(c+d\,x)^2\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(a + b*x)^2*(c + d*x)^2,x)
[Out] int(erfc(a + b*x)^2*(c + d*x)^2, x)
```

3.139 $\int (c+dx)\mathbf{Erfc}(a+bx)^2\,dx$

Optimal. Leaf size=189

$$\frac{de^{-2(a+bx)^2}}{2b^2\pi}-\frac{(bc-ad)\sqrt{\frac{2}{\pi}}\,\mathrm{Erf}\left(\sqrt{2}\,(a+bx)\right)}{b^2}-\frac{2(bc-ad)e^{-(a+bx)^2}\mathrm{Erfc}(a+bx)}{b^2\sqrt{\pi}}-\frac{de^{-(a+bx)^2}(a+bx)\mathrm{Erfc}(a$$

```
[Out] 1/2*d/b^2/exp(2*(b*x+a)^2)/Pi-1/4*d*erfc(b*x+a)^2/b^2+(-a*d+b*c)*(b*x+a)*er
fc(b*x+a)^2/b^2+1/2*d*(b*x+a)^2*erfc(b*x+a)^2/b^2-(-a*d+b*c)*erf((b*x+a)*2^
(1/2))*2^(1/2)/Pi^(1/2)/b^2-2*(-a*d+b*c)*erfc(b*x+a)/b^2/exp((b*x+a)^2)/Pi^
(1/2)-d*(b*x+a)*erfc(b*x+a)/b^2/exp((b*x+a)^2)/Pi^(1/2)
```

Rubi [A]
time = 0.12, antiderivative size = 189, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 9, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.643$, Rules used = {6503, 6488, 6518, 2236, 6500, 6521, 6509, 30, 2240}

$$-\frac{\sqrt{\frac{2}{\pi}}(bc-ad)\mathrm{Erf}\left(\sqrt{2}\,(a+bx)\right)}{b^2}+\frac{(a+bx)(bc-ad)\mathrm{Erfc}(a+bx)^2}{b^2}-\frac{2e^{-(a+bx)^2}(bc-ad)\mathrm{Erfc}(a+bx)}{\sqrt{\pi}\,b^2}+\frac{d(a+bx)^2\mathrm{Erfc}(a+bx)^2}{2b^2}-\frac{d\mathrm{Erfc}(a+bx)^2}{4b^2}-\frac{de^{-(a+bx)^2}(a+bx)\mathrm{Erfc}(a+bx)}{\sqrt{\pi}\,b^2}+\frac{de^{-2(a+bx)^2}}{2\pi b^2}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)*Erfc[a + b*x]^2,x]
```

```
[Out] d/(2*b^2*E^(2*(a + b*x)^2)*Pi) - ((b*c - a*d)*Sqrt[2/Pi]*Erf[Sqrt[2]*(a + b
*x)])/b^2 - (2*(b*c - a*d)*Erfc[a + b*x])/(b^2*E^(a + b*x)^2*Sqrt[Pi]) - (d
*(a + b*x)*Erfc[a + b*x])/(b^2*E^(a + b*x)^2*Sqrt[Pi]) - (d*Erfc[a + b*x]^2
)/(4*b^2) + ((b*c - a*d)*(a + b*x)*Erfc[a + b*x]^2)/b^2 + (d*(a + b*x)^2*Er
fc[a + b*x]^2)/(2*b^2)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 6488

```
Int[Erfc[(a_.) + (b_.)*(x_)]^2, x_Symbol] :> Simp[(a + b*x)*(Erfc[a + b*x]^
2/b), x] + Dist[4/Sqrt[Pi], Int[(a + b*x)*(Erfc[a + b*x]/E^(a + b*x)^2), x]
, x] /; FreeQ[{a, b}, x]
```

Rule 6500

```
Int[Erfc[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfc[b*x]^2
/(m + 1)), x] + Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[(x^(m + 1)*Erfc[b*x])/E^
(b^2*x^2), x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6503

```
Int[Erfc[(a_) + (b_.)*(x_)]^2*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Dist
[1/b^(m + 1), Subst[Int[ExpandIntegrand[Erfc[x]^2, (b*c - a*d + d*x)^m, x],
 x], x, a + b*x], x] /; FreeQ[{a, b, c, d}, x] && IGtQ[m, 0]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$
\begin{aligned}
\int (c+dx)\text{erfc}(a+bx)^2\,dx &= \frac{\text{Subst}\left(\int \left(bc\left(1-\frac{ad}{bc}\right)\text{erfc}(x)^2+dx\text{erfc}(x)^2\right)\,dx,x,a+bx\right)}{b^2} \\
&= \frac{d\text{Subst}\left(\int x\text{erfc}(x)^2\,dx,x,a+bx\right)}{b^2}+\frac{(bc-ad)\text{Subst}\left(\int \text{erfc}(x)^2\,dx,x,a+bx\right)}{b^2} \\
&= \frac{(bc-ad)(a+bx)\text{erfc}(a+bx)^2}{b^2}+\frac{d(a+bx)^2\text{erfc}(a+bx)^2}{2b^2}+\frac{(2d)\text{Subst}\left(\int e^{-x}\right.}{} \\
&= -\frac{2(bc-ad)e^{-(a+bx)^2}\text{erfc}(a+bx)}{b^2\sqrt{\pi}}-\frac{de^{-(a+bx)^2}(a+bx)\text{erfc}(a+bx)}{b^2\sqrt{\pi}}+\frac{(bc-a}{} \\
&= \frac{de^{-2(a+bx)^2}}{2b^2\pi}-\frac{(bc-ad)\sqrt{\frac{2}{\pi}}\,\text{erf}\left(\sqrt{2}\,(a+bx)\right)}{b^2}-\frac{2(bc-ad)e^{-(a+bx)^2}\text{erfc}(a+}{b^2\sqrt{\pi}} \\
&= \frac{de^{-2(a+bx)^2}}{2b^2\pi}-\frac{(bc-ad)\sqrt{\frac{2}{\pi}}\,\text{erf}\left(\sqrt{2}\,(a+bx)\right)}{b^2}-\frac{2(bc-ad)e^{-(a+bx)^2}\text{erfc}(a+}{b^2\sqrt{\pi}}
\end{aligned}
$$

Mathematica [A]
time = 1.41, size = 301, normalized size = 1.59

$$
\frac{4b(c+dx)\left(-\sqrt{\frac{2}{\pi}}\,\text{Erf}\left(\sqrt{2}\,(a+bx)\right)+\text{Erfc}(a+bx)\left(-\frac{2e^{-(a+bx)^2}}{\sqrt{\pi}}+(a+bx)\text{Erfc}(a+bx)\right)\right)+\frac{d\left(2e^{-2(a+bx)^2}+4e^{-(a+bx)^2}\sqrt{\pi}\,(a+bx)-2\pi(a+bx)^2-2\pi\text{Erf}(a+bx)-4e^{-(a+bx)^2}\sqrt{\pi}\,(a+bx)\text{Erf}(a+bx)+4\pi(a+bx)^2\text{Erf}(a+bx)+\pi\text{Erf}(a+bx)^2-2\pi(a+bx)^2\text{Erf}(a+bx)^2+4a\sqrt{2\pi}\,\text{Erf}\left(\sqrt{2}\,(a+bx)\right)+4b\sqrt{2\pi}\,x\text{Erf}\left(\sqrt{2}\,(a+bx)\right)+2\pi(2+\text{Erfc}(-a-bx)\text{Erfc}(a+bx))-4\sqrt{\pi}\,(a+bx)E_{\frac{1}{2}}((a+bx)^2)\right)}{\pi}}{4b^2}
$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)*Erfc[a + b*x]^2,x]
```

```
[Out] (4*b*(c + d*x)*(-(Sqrt[2/Pi]*Erf[Sqrt[2]*(a + b*x)]) + Erfc[a + b*x]*(-2/(E
^(a + b*x)^2*Sqrt[Pi]) + (a + b*x)*Erfc[a + b*x])) + (d*(2/E^(2*(a + b*x)^2
) + (4*Sqrt[Pi]*(a + b*x))/E^(a + b*x)^2 - 2*Pi*(a + b*x)^2 - 2*Pi*Erf[a +
b*x] - (4*Sqrt[Pi]*(a + b*x)*Erf[a + b*x])/E^(a + b*x)^2 + 4*Pi*(a + b*x)^2
*Erf[a + b*x] + Pi*Erf[a + b*x]^2 - 2*Pi*(a + b*x)^2*Erf[a + b*x]^2 + 4*a*S
qrt[2*Pi]*Erf[Sqrt[2]*(a + b*x)] + 4*b*Sqrt[2*Pi]*x*Erf[Sqrt[2]*(a + b*x)]
+ 2*Pi*(2 + Erfc[-a - b*x]*Erfc[a + b*x]) - 4*Sqrt[Pi]*(a + b*x)*ExpIntegra
lE[1/2, (a + b*x)^2]))/Pi)/(4*b^2)
```

Maple [F]
time = 0.03, size = 0, normalized size = 0.00

$$
\int \left(dx+c\right)\text{erfc}\left(bx+a\right)^{2}\,dx
$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)*erfc(b*x+a)^2,x)
```

```
[Out] int((d*x+c)*erfc(b*x+a)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfc(b*x+a)^2,x, algorithm="maxima")
```

```
[Out] integrate((d*x + c)*erfc(b*x + a)^2, x)
```

Fricas [A]
time = 0.34, size = 273, normalized size = 1.44

$$\frac{2\,\pi b^3dx^2 + 4\,\pi b^3cx - 4\,\sqrt{2}\,\sqrt{\pi}\,\sqrt{b^2}\,(bc - ad)\operatorname{erf}\left(\frac{\sqrt{2}\,\sqrt{b^2}\,(bx+a)}{b}\right) - 2\,\pi(4\,abc - (2\,a^2+1)d)\sqrt{b^2}\operatorname{erf}\left(\frac{\sqrt{b^2}\,(bx+a)}{b}\right) + (2\,\pi b^3dx^2 + 4\,\pi b^3cx + \pi(4\,ab^2c - (2\,a^2+1)bd))\operatorname{erf}\left(bx+a\right)^2 + 2\,bde^{\left(-2\,b^2x^2-4\,abx-2\,a^2\right)} - 4\,\sqrt{\pi}\,(b^2dx + 2\,b^2c - abd - (b^2dx + 2\,b^2c - abd)\operatorname{erf}\left(bx+a\right))e^{\left(-b^2x^2-2\,abx-a^2\right)} - 4\,(\pi b^3dx^2 + 2\,\pi b^3cx)\operatorname{erf}\left(bx+a\right)}{4\,\pi b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfc(b*x+a)^2,x, algorithm="fricas")
```

```
[Out] 1/4*(2*pi*b^3*d*x^2 + 4*pi*b^3*c*x - 4*sqrt(2)*sqrt(pi)*sqrt(b^2)*(b*c - a*
d)*erf(sqrt(2)*sqrt(b^2)*(b*x + a)/b) - 2*pi*(4*a*b*c - (2*a^2 + 1)*d)*sqrt
(b^2)*erf(sqrt(b^2)*(b*x + a)/b) + (2*pi*b^3*d*x^2 + 4*pi*b^3*c*x + pi*(4*a
*b^2*c - (2*a^2 + 1)*b*d))*erf(b*x + a)^2 + 2*b*d*e^(-2*b^2*x^2 - 4*a*b*x -
 2*a^2) - 4*sqrt(pi)*(b^2*d*x + 2*b^2*c - a*b*d - (b^2*d*x + 2*b^2*c - a*b*
d)*erf(b*x + a))*e^(-b^2*x^2 - 2*a*b*x - a^2) - 4*(pi*b^3*d*x^2 + 2*pi*b^3*
c*x)*erf(b*x + a))/(pi*b^3)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int (c + dx)\operatorname{erfc}^{2}\left(a + bx\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfc(b*x+a)**2,x)
```

```
[Out] Integral((c + d*x)*erfc(a + b*x)**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfc(b*x+a)^2,x, algorithm="giac")
```

```
[Out] integrate((d*x + c)*erfc(b*x + a)^2, x)
```

Mupad [**F**]
time = 0.00, size = -1, normalized size = -0.01

$$\int \mathrm{erfc}(a+b\,x)^2\,(c+d\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(a + b*x)^2*(c + d*x),x)
```

```
[Out] int(erfc(a + b*x)^2*(c + d*x), x)
```

3.140 $\int \mathbf{Erfc}(a+bx)^2\,dx$

Optimal. Leaf size=71

$$-\frac{\sqrt{\frac{2}{\pi}}\,\mathrm{Erf}\left(\sqrt{2}\,(a+bx)\right)}{b}-\frac{2e^{-(a+bx)^2}\mathrm{Erfc}(a+bx)}{b\sqrt{\pi}}+\frac{(a+bx)\mathrm{Erfc}(a+bx)^2}{b}$$

```
[Out] (b*x+a)*erfc(b*x+a)^2/b-erf((b*x+a)*2^(1/2))*2^(1/2)/Pi^(1/2)/b-2*erfc(b*x+
a)/b/exp((b*x+a)^2)/Pi^(1/2)
```

Rubi [A]
time = 0.11, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6488, 6518, 2236}

$$-\frac{\sqrt{\frac{2}{\pi}}\,\mathrm{Erf}\left(\sqrt{2}\,(a+bx)\right)}{b}+\frac{(a+bx)\mathrm{Erfc}(a+bx)^2}{b}-\frac{2e^{-(a+bx)^2}\mathrm{Erfc}(a+bx)}{\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[a + b*x]^2,x]
```

```
[Out] -((Sqrt[2/Pi]*Erf[Sqrt[2]*(a + b*x)])/b) - (2*Erfc[a + b*x])/(b*E^(a + b*x)
^2*Sqrt[Pi]) + ((a + b*x)*Erfc[a + b*x]^2)/b
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 6488

```
Int[Erfc[(a_.) + (b_.)*(x_)]^2, x_Symbol] :> Simp[(a + b*x)*(Erfc[a + b*x]^
2/b), x] + Dist[4/Sqrt[Pi], Int[(a + b*x)*(Erfc[a + b*x]/E^(a + b*x)^2), x]
, x] /; FreeQ[{a, b}, x]
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$
\begin{aligned}
\int \operatorname{erfc}(a+bx)^2\,dx &= \frac{(a+bx)\operatorname{erfc}(a+bx)^2}{b}+\frac{4\int e^{-(a+bx)^2}(a+bx)\operatorname{erfc}(a+bx)\,dx}{\sqrt{\pi}}\\
&= \frac{(a+bx)\operatorname{erfc}(a+bx)^2}{b}+\frac{4\text{Subst}\left(\int e^{-x^2}x\operatorname{erfc}(x)\,dx,x,a+bx\right)}{b\sqrt{\pi}}\\
&= -\frac{2e^{-(a+bx)^2}\operatorname{erfc}(a+bx)}{b\sqrt{\pi}}+\frac{(a+bx)\operatorname{erfc}(a+bx)^2}{b}-\frac{4\text{Subst}\left(\int e^{-2x^2}\,dx,x,a+bx\right)}{b\pi}\\
&= -\frac{\sqrt{\frac{2}{\pi}}\operatorname{erf}\left(\sqrt{2}\,(a+bx)\right)}{b}-\frac{2e^{-(a+bx)^2}\operatorname{erfc}(a+bx)}{b\sqrt{\pi}}+\frac{(a+bx)\operatorname{erfc}(a+bx)^2}{b}
\end{aligned}
$$

Mathematica [A]
time = 0.07, size = 66, normalized size = 0.93

$$
\frac{-\sqrt{\frac{2}{\pi}}\operatorname{Erf}\left(\sqrt{2}\,(a+bx)\right)+\operatorname{Erfc}(a+bx)\left(-\frac{2e^{-(a+bx)^2}}{\sqrt{\pi}}+(a+bx)\operatorname{Erfc}(a+bx)\right)}{b}
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[a + b*x]^2,x]
```

```
[Out] (-(Sqrt[2/Pi]*Erf[Sqrt[2]*(a + b*x)]) + Erfc[a + b*x]*(-2/(E^(a + b*x)^2*Sq
rt[Pi]) + (a + b*x)*Erfc[a + b*x]))/b
```

Maple [A]
time = 0.25, size = 59, normalized size = 0.83

method	result	size
derivativedivides	$\frac{\operatorname{erf}(bx+a)^2(bx+a)+\frac{2\operatorname{erf}(bx+a)e^{-(bx+a)^2}}{\sqrt{\pi}}-\frac{\sqrt{2}\,\operatorname{erf}\left((bx+a)\sqrt{2}\right)}{\sqrt{\pi}}}{b}$	59
default	$\frac{\operatorname{erf}(bx+a)^2(bx+a)+\frac{2\operatorname{erf}(bx+a)e^{-(bx+a)^2}}{\sqrt{\pi}}-\frac{\sqrt{2}\,\operatorname{erf}\left((bx+a)\sqrt{2}\right)}{\sqrt{\pi}}}{b}$	59

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x+a)^2,x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*(erf(b*x+a)^2*(b*x+a)+2*erf(b*x+a)/Pi^(1/2)*exp(-(b*x+a)^2)-1/Pi^(1/2)*
2^(1/2)*erf((b*x+a)*2^(1/2)))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)^2,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x + a)^2, x)
```

Fricas [B] Leaf count of result is larger than twice the leaf count of optimal. 141 vs. $2(63) = 126$.
time = 0.34, size = 141, normalized size = 1.99

$$-\frac{2\pi b^2 x \operatorname{erf}(bx+a) - \pi b^2 x + 2\pi a\sqrt{b^2}\operatorname{erf}\left(\frac{\sqrt{b^2}(bx+a)}{b}\right) - (\pi b^2 x + \pi ab)\operatorname{erf}(bx+a)^2 + \sqrt{2}\sqrt{\pi}\sqrt{b^2}\operatorname{erf}\left(\frac{\sqrt{2}\sqrt{b^2}(bx+a)}{b}\right) - 2\sqrt{\pi}(b\operatorname{erf}(bx+a) - b)e^{(-b^2x^2-2abx-a^2)}}{\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)^2,x, algorithm="fricas")
```

```
[Out] -(2*pi*b^2*x*erf(b*x + a) - pi*b^2*x + 2*pi*a*sqrt(b^2)*erf(sqrt(b^2)*(b*x
+ a)/b) - (pi*b^2*x + pi*a*b)*erf(b*x + a)^2 + sqrt(2)*sqrt(pi)*sqrt(b^2)*e
rf(sqrt(2)*sqrt(b^2)*(b*x + a)/b) - 2*sqrt(pi)*(b*erf(b*x + a) - b)*e^(-b^2
*x^2 - 2*a*b*x - a^2))/(pi*b^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \operatorname{erfc}^2(a+bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)**2,x)
```

```
[Out] Integral(erfc(a + b*x)**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)^2,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x + a)^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \operatorname{erfc}(a+b\,x)^2\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(a + b*x)^2,x)
```

```
[Out] int(erfc(a + b*x)^2, x)
```

3.141 $\int \frac{\text{Erfc}(a+bx)^2}{c+dx} dx$

Optimal. Leaf size=19

$$\text{Int}\left(\frac{\text{Erfc}(a+bx)^2}{c+dx}, x\right)$$

```
[Out] Unintegrable(erfc(b*x+a)^2/(d*x+c),x)
```

Rubi [A]
time = 0.02, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\text{Erfc}(a+bx)^2}{c+dx} dx$$

Verification is not applicable to the result.

```
[In] Int[Erfc[a + b*x]^2/(c + d*x),x]
```

```
[Out] Defer[Int][Erfc[a + b*x]^2/(c + d*x), x]
```

Rubi steps

$$\int \frac{\text{erfc}(a+bx)^2}{c+dx} dx = \int \frac{\text{erfc}(a+bx)^2}{c+dx} dx$$

Mathematica [A]
time = 0.41, size = 0, normalized size = 0.00

$$\int \frac{\text{Erfc}(a+bx)^2}{c+dx} dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfc[a + b*x]^2/(c + d*x),x]
```

```
[Out] Integrate[Erfc[a + b*x]^2/(c + d*x), x]
```

Maple [A]
time = 0.15, size = 0, normalized size = 0.00

$$\int \frac{\text{erfc}(bx+a)^2}{dx+c} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x+a)^2/(d*x+c),x)
```

```
[Out] int(erfc(b*x+a)^2/(d*x+c),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)^2/(d*x+c),x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x + a)^2/(d*x + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)^2/(d*x+c),x, algorithm="fricas")
```

```
[Out] integral((erf(b*x + a)^2 - 2*erf(b*x + a) + 1)/(d*x + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}^{2}\left(a+bx\right)}{c+dx}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)**2/(d*x+c),x)
```

```
[Out] Integral(erfc(a + b*x)**2/(c + d*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)^2/(d*x+c),x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x + a)^2/(d*x + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{\operatorname{erfc}(a+b\,x)^2}{c+d\,x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(a + b*x)^2/(c + d*x),x)
[Out] int(erfc(a + b*x)^2/(c + d*x), x)
```

3.142 $\int \frac{\mathrm{Erfc}(a+bx)^2}{(c+dx)^2} \, dx$

Optimal. Leaf size=19

$$\mathrm{Int}\left(\frac{\mathrm{Erfc}(a+bx)^2}{(c+dx)^2}, x\right)$$

```
[Out] Unintegrable(erfc(b*x+a)^2/(d*x+c)^2,x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\mathrm{Erfc}(a+bx)^2}{(c+dx)^2} \, dx$$

Verification is not applicable to the result.

```
[In] Int[Erfc[a + b*x]^2/(c + d*x)^2,x]
```

```
[Out] Defer[Int][Erfc[a + b*x]^2/(c + d*x)^2, x]
```

Rubi steps

$$\int \frac{\mathrm{erfc}(a+bx)^2}{(c+dx)^2} \, dx = \int \frac{\mathrm{erfc}(a+bx)^2}{(c+dx)^2} \, dx$$

Mathematica [A]
time = 0.25, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{Erfc}(a+bx)^2}{(c+dx)^2} \, dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfc[a + b*x]^2/(c + d*x)^2,x]
```

```
[Out] Integrate[Erfc[a + b*x]^2/(c + d*x)^2, x]
```

Maple [A]
time = 0.18, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{erfc}(bx+a)^2}{(dx+c)^2} \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x+a)^2/(d*x+c)^2,x)
```

```
[Out] int(erfc(b*x+a)^2/(d*x+c)^2,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)^2/(d*x+c)^2,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x + a)^2/(d*x + c)^2, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)^2/(d*x+c)^2,x, algorithm="fricas")
```

```
[Out] integral((erf(b*x + a)^2 - 2*erf(b*x + a) + 1)/(d^2*x^2 + 2*c*d*x + c^2), x
)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}^2(a + bx)}{(c + dx)^2}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)**2/(d*x+c)**2,x)
```

```
[Out] Integral(erfc(a + b*x)**2/(c + d*x)**2, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x+a)^2/(d*x+c)^2,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x + a)^2/(d*x + c)^2, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{\operatorname{erfc}(a+b\,x)^2}{(c+d\,x)^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(a + b*x)^2/(c + d*x)^2,x)
[Out] int(erfc(a + b*x)^2/(c + d*x)^2, x)
```

3.143 $\int x^2 \mathbf{Erfc}(d(a+b\log(cx^n)))\,dx$

Optimal. Leaf size=102

$$\frac{1}{3}e^{\frac{9-12abd^2n}{4b^2d^2n^2}}x^3(cx^n)^{-3/n}\,\mathrm{Erf}\left(\frac{2abd^2-\frac{3}{n}+2b^2d^2\log(cx^n)}{2bd}\right)+\frac{1}{3}x^3\mathrm{Erfc}(d(a+b\log(cx^n)))$$

```
[Out] 1/3*exp(1/4*(-12*a*b*d^2*n+9)/b^2/d^2/n^2)*x^3*erf(1/2*(2*a*b*d^2-3/n+2*b^2
*d^2*ln(c*x^n))/b/d)/((c*x^n)^(3/n))+1/3*x^3*erfc(d*(a+b*ln(c*x^n)))
```

Rubi [A]
time = 0.10, antiderivative size = 102, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.294$, Rules used = {6537, 2314, 2308, 2266, 2236}

$$\frac{1}{3}x^3(cx^n)^{-3/n}\,e^{\frac{9-12abd^2n}{4b^2d^2n^2}}\,\mathrm{Erf}\left(\frac{2abd^2+2b^2d^2\log(cx^n)-\frac{3}{n}}{2bd}\right)+\frac{1}{3}x^3\mathrm{Erfc}(d(a+b\log(cx^n)))$$

Antiderivative was successfully verified.

```
[In] Int[x^2*Erfc[d*(a + b*Log[c*x^n])],x]
```

```
[Out] (E^((9 - 12*a*b*d^2*n)/(4*b^2*d^2*n^2))*x^3*Erf[(2*a*b*d^2 - 3/n + 2*b^2*d^
2*Log[c*x^n])/(2*b*d)])/(3*(c*x^n)^(3/n)) + (x^3*Erfc[d*(a + b*Log[c*x^n])]
)/3
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2314

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^m*((c*(d + e*x)^n)^(2
*a*b*f*Log[F])/(d + e*x)^(m + 2*a*b*f*n*Log[F])), Int[(d + e*x)^(m + 2*a*b*
f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2), x], x] /; FreeQ[{F, a,
b, c, d, e, f, g, h, m, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 6537

```
Int[Erfc[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_))^(m_.), x
_Symbol] :> Simp[(e*x)^(m + 1)*(Erfc[d*(a + b*Log[c*x^n])]/(e*(m + 1))), x]
 + Dist[2*b*d*(n/(Sqrt[Pi]*(m + 1))), Int[(e*x)^m/E^(d*(a + b*Log[c*x^n]))^
2, x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rubi steps

$$\int x^2\operatorname{erfc}(d(a+b\log(cx^n)))\,dx = \frac{1}{3}x^3\operatorname{erfc}(d(a+b\log(cx^n))) + \frac{(2bdn)\int e^{-d^2(a+b\log(cx^n))^2}x^2\,dx}{3\sqrt{\pi}}$$

$$= \frac{1}{3}x^3\operatorname{erfc}(d(a+b\log(cx^n))) + \frac{(2bdn)\int \exp\left(-a^2d^2-2abd^2\log(cx^n)-b^2\right.}{3\sqrt{\pi}}$$

$$= \frac{1}{3}x^3\operatorname{erfc}(d(a+b\log(cx^n))) + \frac{(2bdn)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}x^2(cx^n)^{-2abd^2}\,d}{3\sqrt{\pi}}$$

$$= \frac{1}{3}x^3\operatorname{erfc}(d(a+b\log(cx^n))) + \frac{\left(2bdnx^{2abd^2n}(cx^n)^{-2abd^2}\right)\int e^{-a^2d^2-b^2d^2\log^2(c}}{3\sqrt{\pi}}$$

$$= \frac{1}{3}x^3\operatorname{erfc}(d(a+b\log(cx^n))) + \frac{\left(2bdx^3(cx^n)^{-2abd^2-\frac{3-2abd^2n}{n}}\right)\operatorname{Subst}\left(\int \exp\right.}{}$$

$$= \frac{1}{3}x^3\operatorname{erfc}(d(a+b\log(cx^n))) + \frac{\left(2bde^{\frac{9-12abd^2n}{4b^2d^2n^2}}x^3(cx^n)^{-2abd^2-\frac{3-2abd^2n}{n}}\right)\operatorname{Subs}}{}$$

$$= \frac{1}{3}e^{\frac{9-12abd^2n}{4b^2d^2n^2}}x^3(cx^n)^{-3/n}\operatorname{erf}\left(\frac{2abd^2-\frac{3}{n}+2b^2d^2\log(cx^n)}{2bd}\right) + \frac{1}{3}x^3\operatorname{erfc}(d(a$$

Mathematica [A]
time = 0.25, size = 87, normalized size = 0.85

$$\frac{1}{3}\left(e^{\frac{3\left(\frac{\frac{3}{d^2}-4abn}{b^2}-4n\log(cx^n)\right)}{4n^2}}x^3\operatorname{Erf}\left(ad-\frac{3}{2bdn}+bd\log(cx^n)\right)+x^3\operatorname{Erfc}(d(a+b\log(cx^n)))\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*Erfc[d*(a + b*Log[c*x^n])],x]
[Out] (E^((3*((3/d^2 - 4*a*b*n)/b^2 - 4*n*Log[c*x^n]))/(4*n^2))*x^3*Erf[a*d - 3/(
2*b*d*n) + b*d*Log[c*x^n]] + x^3*Erfc[d*(a + b*Log[c*x^n])])/3
```

Maple [F]
time = 0.08, size = 0, normalized size = 0.00

$$\int x^{2}\operatorname{erfc}(d(a+b\ln(c\,x^{n})))\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfc(d*(a+b*ln(c*x^n))),x)
[Out] int(x^2*erfc(d*(a+b*ln(c*x^n))),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfc(d*(a+b*log(c*x^n))),x, algorithm="maxima")
[Out] integrate(x^2*erfc((b*log(c*x^n) + a)*d), x)
```

Fricas [A]
time = 0.35, size = 130, normalized size = 1.27

$$-\frac{1}{3}\,x^{3}\operatorname{erf}\left(bd\log\left(cx^{n}\right)+ad\right)+\frac{1}{3}\,x^{3}+\frac{1}{3}\,\sqrt{b^{2}d^{2}n^{2}}\,\operatorname{erf}\left(\frac{\left(2\,b^{2}d^{2}n^{2}\log\left(x\right)+2\,b^{2}d^{2}n\log\left(c\right)+2\,abd^{2}n-3\right)\sqrt{b^{2}d^{2}n^{2}}}{2\,b^{2}d^{2}n^{2}}\right)e^{\left(-\frac{3\,\left(4\,b^{2}d^{2}n\log(c)+4\,abd^{2}n-3\right)}{4\,b^{2}d^{2}n^{2}}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfc(d*(a+b*log(c*x^n))),x, algorithm="fricas")
[Out] -1/3*x^3*erf(b*d*log(c*x^n) + a*d) + 1/3*x^3 + 1/3*sqrt(b^2*d^2*n^2)*erf(1/
2*(2*b^2*d^2*n^2*log(x) + 2*b^2*d^2*n*log(c) + 2*a*b*d^2*n - 3)*sqrt(b^2*d^
2*n^2)/(b^2*d^2*n^2))*e^(-3/4*(4*b^2*d^2*n*log(c) + 4*a*b*d^2*n - 3)/(b^2*d
^2*n^2))
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x^{2}\operatorname{erfc}\left(ad+bd\log\left(cx^{n}\right)\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*erfc(d*(a+b*ln(c*x**n))),x)
```

```
[Out] Integral(x**2*erfc(a*d + b*d*log(c*x**n)), x)
```

Giac [A]
time = 0.48, size = 90, normalized size = 0.88

$$-\frac{1}{3}x^3\operatorname{erf}\left(bdn\log\left(x\right)+bd\log\left(c\right)+ad\right)+\frac{1}{3}x^3-\frac{\operatorname{erf}\left(-bdn\log\left(x\right)-bd\log\left(c\right)-ad+\frac{3}{2\,bdn}\right)e^{\left(-\frac{3\,a}{bn}+\frac{9}{4\,b^2d^2n^2}\right)}}{3\,c^{\frac{3}{n}}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfc(d*(a+b*log(c*x^n))),x, algorithm="giac")
```

```
[Out] -1/3*x^3*erf(b*d*n*log(x) + b*d*log(c) + a*d) + 1/3*x^3 - 1/3*erf(-b*d*n*lo
g(x) - b*d*log(c) - a*d + 3/2/(b*d*n))*e^(-3*a/(b*n) + 9/4/(b^2*d^2*n^2))/c
^(3/n)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^2\,\mathrm{erfc}(d\,\left(a+b\,\ln\left(c\,x^n\right)\right))\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfc(d*(a + b*log(c*x^n))),x)
```

```
[Out] int(x^2*erfc(d*(a + b*log(c*x^n))), x)
```

3.144 $\int x\mathbf{Erfc}(d(a+b\log(cx^n)))\,dx$

Optimal. Leaf size=94

$$\frac{1}{2}e^{\frac{1-2abd^2n}{b^2d^2n^2}}x^2(cx^n)^{-2/n}\operatorname{Erf}\left(\frac{abd^2-\frac{1}{n}+b^2d^2\log(cx^n)}{bd}\right)+\frac{1}{2}x^2\operatorname{Erfc}(d(a+b\log(cx^n)))$$

```
[Out] 1/2*exp((-2*a*b*d^2*n+1)/b^2/d^2/n^2)*x^2*erf((a*b*d^2-1/n+b^2*d^2*ln(c*x^n
))/b/d)/((c*x^n)^(2/n))+1/2*x^2*erfc(d*(a+b*ln(c*x^n)))
```

Rubi [A]

time = 0.09, antiderivative size = 94, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.333, Rules used = {6537, 2314, 2308, 2266, 2236}

$$\frac{1}{2}x^2(cx^n)^{-2/n}e^{\frac{1-2abd^2n}{b^2d^2n^2}}\operatorname{Erf}\left(\frac{abd^2+b^2d^2\log(cx^n)-\frac{1}{n}}{bd}\right)+\frac{1}{2}x^2\operatorname{Erfc}(d(a+b\log(cx^n)))$$

Antiderivative was successfully verified.

```
[In] Int[x*Erfc[d*(a + b*Log[c*x^n])],x]
```

```
[Out] (E^((1 - 2*a*b*d^2*n)/(b^2*d^2*n^2))*x^2*Erf[(a*b*d^2 - n^(-1) + b^2*d^2*Lo
g[c*x^n])/(b*d)])/(2*(c*x^n)^(2/n)) + (x^2*Erfc[d*(a + b*Log[c*x^n])])/2
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2314

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^m*((c*(d + e*x)^n)^(2
```

```
*a*b*f*Log[F])/(d + e*x)^(m + 2*a*b*f*n*Log[F])), Int[(d + e*x)^(m + 2*a*b*
f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2), x], x] /; FreeQ[{F, a,
b, c, d, e, f, g, h, m, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 6537

```
Int[Erfc[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_))^(m_.), x
_Symbol] :> Simp[(e*x)^(m + 1)*(Erfc[d*(a + b*Log[c*x^n])]/(e*(m + 1))), x]
 + Dist[2*b*d*(n/(Sqrt[Pi]*(m + 1))), Int[(e*x)^m/E^(d*(a + b*Log[c*x^n]))^
2, x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int x\text{erfc}(d(a+b\log(cx^n)))\,dx &= \frac{1}{2}x^2\text{erfc}(d(a+b\log(cx^n)))+\frac{(bdn)\int e^{-d^2(a+b\log(cx^n))^2}x\,dx}{\sqrt{\pi}}\\ &= \frac{1}{2}x^2\text{erfc}(d(a+b\log(cx^n)))+\frac{(bdn)\int \exp\left(-a^2d^2-2abd^2\log(cx^n)-b^2d^2\right.}{\sqrt{\pi}}\\ &= \frac{1}{2}x^2\text{erfc}(d(a+b\log(cx^n)))+\frac{(bdn)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}x(cx^n)^{-2abd^2}\,dx}{\sqrt{\pi}}\\ &= \frac{1}{2}x^2\text{erfc}(d(a+b\log(cx^n)))+\frac{\left(bdnx^{2abd^2n}(cx^n)^{-2abd^2}\right)\int e^{-a^2d^2-b^2d^2\log^2(cx^n}}{\sqrt{\pi}}\\ &= \frac{1}{2}x^2\text{erfc}(d(a+b\log(cx^n)))+\frac{\left(bdx^2(cx^n)^{-2abd^2-\frac{2-2abd^2n}{n}}\right)\text{Subst}\left(\int\exp\left(-\right.\right.}{}\\ &= \frac{1}{2}x^2\text{erfc}(d(a+b\log(cx^n)))+\frac{\left(bde^{\frac{1-2abd^2n}{b^2d^2n^2}}x^2(cx^n)^{-2abd^2-\frac{2-2abd^2n}{n}}\right)\text{Subst}\left(\right.}{}\\ &= \frac{1}{2}e^{\frac{1-2abd^2n}{b^2d^2n^2}}x^2(cx^n)^{-2/n}\text{erf}\left(\frac{abd^2-\frac{1}{n}+b^2d^2\log(cx^n)}{bd}\right)+\frac{1}{2}x^2\text{erfc}(d(a+b\,\text{l}\end{aligned}$$

Mathematica [A]
time = 0.22, size = 80, normalized size = 0.85

$$\frac{1}{2}\left(e^{\frac{\frac{\frac{1}{d^2}-2abn}{b^2}-2n\log(cx^n)}{n^2}}x^2\text{Erf}\left(ad-\frac{1}{bdn}+bd\log(cx^n)\right)+x^2\text{Erfc}(d(a+b\log(cx^n)))\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x*Erfc[d*(a + b*Log[c*x^n])],x]
```

```
[Out] (E^(((d^(-2) - 2*a*b*n)/b^2 - 2*n*Log[c*x^n])/n^2)*x^2*Erf[a*d - 1/(b*d*n)
+ b*d*Log[c*x^n]] + x^2*Erfc[d*(a + b*Log[c*x^n])])/2
```

Maple [F]
time = 0.07, size = 0, normalized size = 0.00

$$\int x\,\mathrm{erfc}(d(a+b\ln(c\,x^{n})))\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfc(d*(a+b*ln(c*x^n))),x)
```

```
[Out] int(x*erfc(d*(a+b*ln(c*x^n))),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(d*(a+b*log(c*x^n))),x, algorithm="maxima")
```

```
[Out] integrate(x*erfc((b*log(c*x^n) + a)*d), x)
```

Fricas [A]
time = 0.36, size = 126, normalized size = 1.34

$$-\frac{1}{2}\,x^{2}\,\mathrm{erf}\left(bd\log\left(cx^{n}\right)+ad\right)+\frac{1}{2}\,\sqrt{b^{2}d^{2}n^{2}}\,\mathrm{erf}\left(\frac{\left(b^{2}d^{2}n^{2}\log\left(x\right)+b^{2}d^{2}n\log\left(c\right)+abd^{2}n-1\right)\sqrt{b^{2}d^{2}n^{2}}}{b^{2}d^{2}n^{2}}\right)e^{\left(-\frac{2\,b^{2}d^{2}n\log(c)+2\,abd^{2}n-1}{b^{2}d^{2}n^{2}}\right)}+\frac{1}{2}\,x^{2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(d*(a+b*log(c*x^n))),x, algorithm="fricas")
```

```
[Out] -1/2*x^2*erf(b*d*log(c*x^n) + a*d) + 1/2*sqrt(b^2*d^2*n^2)*erf((b^2*d^2*n^2
*log(x) + b^2*d^2*n*log(c) + a*b*d^2*n - 1)*sqrt(b^2*d^2*n^2)/(b^2*d^2*n^2)
)*e^(-(2*b^2*d^2*n*log(c) + 2*a*b*d^2*n - 1)/(b^2*d^2*n^2)) + 1/2*x^2
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x\,\mathrm{erfc}\left(ad+bd\log\left(cx^{n}\right)\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(d*(a+b*ln(c*x**n))),x)
```

```
[Out] Integral(x*erfc(a*d + b*d*log(c*x**n)), x)
```

Giac [A]
time = 0.52, size = 88, normalized size = 0.94

$$-\frac{1}{2}\,x^{2}\operatorname{erf}\left(bdn\log\left(x\right)+bd\log\left(c\right)+ad\right)+\frac{1}{2}\,x^{2}-\frac{\operatorname{erf}\left(-bdn\log\left(x\right)-bd\log\left(c\right)-ad+\frac{1}{bdn}\right)e^{\left(-\frac{2\,a}{bn}+\frac{1}{b^{2}d^{2}n^{2}}\right)}}{2\,c^{\frac{2}{n}}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(d*(a+b*log(c*x^n))),x, algorithm="giac")
```

```
[Out] -1/2*x^2*erf(b*d*n*log(x) + b*d*log(c) + a*d) + 1/2*x^2 - 1/2*erf(-b*d*n*lo
g(x) - b*d*log(c) - a*d + 1/(b*d*n))*e^(-2*a/(b*n) + 1/(b^2*d^2*n^2))/c^(2/
n)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x\,\mathrm{erfc}(d\,\left(a+b\,\ln\left(c\,x^n\right)\right))\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfc(d*(a + b*log(c*x^n))),x)
```

```
[Out] int(x*erfc(d*(a + b*log(c*x^n))), x)
```

3.145 $\int \textbf{Erfc}(d(a+b\log(cx^n)))\,dx$

Optimal. Leaf size=92

$$e^{\frac{1-4abd^2n}{4b^2d^2n^2}}x(cx^n)^{-1/n}\operatorname{Erf}\left(\frac{2abd^2-\frac{1}{n}+2b^2d^2\log(cx^n)}{2bd}\right)+x\operatorname{Erfc}(d(a+b\log(cx^n)))$$

```
[Out] exp(1/4*(-4*a*b*d^2*n+1)/b^2/d^2/n^2)*x*erf(1/2*(2*a*b*d^2-1/n+2*b^2*d^2*ln
(c*x^n))/b/d)/((c*x^n)^(1/n))+x*erfc(d*(a+b*ln(c*x^n)))
```

Rubi [A]
time = 0.08, antiderivative size = 92, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.385, Rules used = {6533, 2312, 2308, 2266, 2236}

$$x(cx^n)^{-1/n}e^{\frac{1-4abd^2n}{4b^2d^2n^2}}\operatorname{Erf}\left(\frac{2abd^2+2b^2d^2\log(cx^n)-\frac{1}{n}}{2bd}\right)+x\operatorname{Erfc}(d(a+b\log(cx^n)))$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[d*(a + b*Log[c*x^n])],x]
```

```
[Out] (E^((1 - 4*a*b*d^2*n)/(4*b^2*d^2*n^2))*x*Erf[(2*a*b*d^2 - n^(-1) + 2*b^2*d^
2*Log[c*x^n])/(2*b*d)])/(c*x^n)^n^(-1) + x*Erfc[d*(a + b*Log[c*x^n])]
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2312

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.)), x
_Symbol] :> Dist[(c*(d + e*x)^n)^(2*a*b*f*Log[F])/(d + e*x)^(2*a*b*f*n*Log[
```

```
F]), Int[(d + e*x)^(2*a*b*f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2
), x], x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] &&  !IntegerQ[2*a*b*f*Log[F
]]
```

Rule 6533

```
Int[Erfc[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)], x_Symbol] :> Simp[x*
Erfc[d*(a + b*Log[c*x^n])], x] + Dist[2*b*d*(n/Sqrt[Pi]), Int[1/E^(d*(a + b
*Log[c*x^n]))^2, x], x] /; FreeQ[{a, b, c, d, n}, x]
```

Rubi steps

$$\int \operatorname{erfc}(d(a+b\log(cx^n)))\,dx = x\operatorname{erfc}(d(a+b\log(cx^n))) + \frac{(2bdn)\int e^{-d^2(a+b\log(cx^n))^2}\,dx}{\sqrt{\pi}}$$

$$= x\operatorname{erfc}(d(a+b\log(cx^n))) + \frac{(2bdn)\int \exp\left(-a^2d^2-2abd^2\log(cx^n)-b^2d^2\log \cdots\right.}{\sqrt{\pi}}$$

$$= x\operatorname{erfc}(d(a+b\log(cx^n))) + \frac{(2bdn)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}(cx^n)^{-2abd^2}\,dx}{\sqrt{\pi}}$$

$$= x\operatorname{erfc}(d(a+b\log(cx^n))) + \frac{\left(2bdnx^{2abd^2n}(cx^n)^{-2abd^2}\right)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}x^{\cdots}}{\sqrt{\pi}}$$

$$= x\operatorname{erfc}(d(a+b\log(cx^n))) + \frac{\left(2bdx(cx^n)^{-2abd^2-\frac{1-2abd^2n}{n}}\right)\operatorname{Subst}\left(\int\exp\left(-a^2 \cdots\right.\right.}{\sqrt{\pi}}$$

$$= x\operatorname{erfc}(d(a+b\log(cx^n))) + \frac{\left(2bde^{\frac{1-4abd^2n}{4b^2d^2n^2}}x(cx^n)^{-2abd^2-\frac{1-2abd^2n}{n}}\right)\operatorname{Subst}\left(\int \cdots\right.}{\sqrt{\pi}}$$

$$= e^{\frac{1-4abd^2n}{4b^2d^2n^2}}x(cx^n)^{-1/n}\operatorname{erf}\left(\frac{2abd^2-\frac{1}{n}+2b^2d^2\log(cx^n)}{2bd}\right)+x\operatorname{erfc}(d(a+b\log \cdots$$

Mathematica [A]
time = 0.20, size = 77, normalized size = 0.84

$$e^{\frac{\frac{\frac{1}{d^2}-4abn}{b^2}-4n\log(cx^n)}{4n^2}}x\operatorname{Erf}\left(ad-\frac{1}{2bdn}+bd\log(cx^n)\right)+x\operatorname{Erfc}(d(a+b\log(cx^n)))$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[d*(a + b*Log[c*x^n])],x]
```

```
[Out] E^(((d^(-2) - 4*a*b*n)/b^2 - 4*n*Log[c*x^n])/(4*n^2))*x*Erf[a*d - 1/(2*b*d*
n) + b*d*Log[c*x^n]] + x*Erfc[d*(a + b*Log[c*x^n])]
```

Maple [F]
time = 0.10, size = 0, normalized size = 0.00

$$\int \operatorname{erfc}(d(a+b\ln(c\,x^{n})))\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(d*(a+b*ln(c*x^n))),x)
```

```
[Out] int(erfc(d*(a+b*ln(c*x^n))),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*log(c*x^n))),x, algorithm="maxima")
```

```
[Out] integrate(erfc((b*log(c*x^n) + a)*d), x)
```

Fricas [A]
time = 0.38, size = 123, normalized size = 1.34

$$\sqrt{b^2d^2n^2}\,\operatorname{erf}\left(\frac{\left(2\,b^2d^2n^2\log\left(x\right)+2\,b^2d^2n\log\left(c\right)+2\,abd^2n-1\right)\sqrt{b^2d^2n^2}}{2\,b^2d^2n^2}\right)e^{\left(-\frac{4\,b^2d^2n\log(c)+4\,abd^2n-1}{4\,b^2d^2n^2}\right)}-x\operatorname{erf}\left(bd\log\left(cx^n\right)+ad\right)+x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*log(c*x^n))),x, algorithm="fricas")
```

```
[Out] sqrt(b^2*d^2*n^2)*erf(1/2*(2*b^2*d^2*n^2*log(x) + 2*b^2*d^2*n*log(c) + 2*a*
b*d^2*n - 1)*sqrt(b^2*d^2*n^2)/(b^2*d^2*n^2))*e^(-1/4*(4*b^2*d^2*n*log(c) +
 4*a*b*d^2*n - 1)/(b^2*d^2*n^2)) - x*erf(b*d*log(c*x^n) + a*d) + x
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \operatorname{erfc}\left(d\left(a+b\log\left(cx^{n}\right)\right)\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*ln(c*x**n))),x)
```

```
[Out] Integral(erfc(d*(a + b*log(c*x**n))), x)
```

Giac [A]
time = 0.48, size = 82, normalized size = 0.89

$$-x\,\mathrm{erf}\left(bdn\log\left(x\right)+bd\log\left(c\right)+ad\right)+x-\frac{\mathrm{erf}\left(-bdn\log\left(x\right)-bd\log\left(c\right)-ad+\frac{1}{2\,bdn}\right)e^{\left(-\frac{a}{bn}+\frac{1}{4\,b^{2}d^{2}n^{2}}\right)}}{c^{\left(\frac{1}{n}\right)}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*log(c*x^n))),x, algorithm="giac")
```

```
[Out] -x*erf(b*d*n*log(x) + b*d*log(c) + a*d) + x - erf(-b*d*n*log(x) - b*d*log(c
) - a*d + 1/2/(b*d*n))*e^(-a/(b*n) + 1/4/(b^2*d^2*n^2))/c^(1/n)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \mathrm{erfc}(d\,(a+b\,\ln\left(c\,x^n\right)))\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(d*(a + b*log(c*x^n))),x)
```

```
[Out] int(erfc(d*(a + b*log(c*x^n))), x)
```

3.146 $\int \frac{\mathbf{Erfc}(d(a+b\log(cx^n)))}{x}\,dx$

Optimal. Leaf size=66

$$-\frac{e^{-d^2(a+b\log(cx^n))^2}}{bdn\sqrt{\pi}}+\frac{\operatorname{Erfc}(d(a+b\log(cx^n)))(a+b\log(cx^n))}{bn}$$

```
[Out] erfc(d*(a+b*ln(c*x^n)))*(a+b*ln(c*x^n))/b/n-1/b/d/exp(d^2*(a+b*ln(c*x^n))^2
)/n/Pi^(1/2)
```

Rubi [A]
time = 0.03, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.059, Rules used = {6485}

$$\frac{(a+b\log(cx^n))\operatorname{Erfc}(d(a+b\log(cx^n)))}{bn}-\frac{e^{-d^2(a+b\log(cx^n))^2}}{\sqrt{\pi}\,bdn}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[d*(a + b*Log[c*x^n])]/x,x]
```

```
[Out] -(1/(b*d*E^(d^2*(a + b*Log[c*x^n])^2)*n*Sqrt[Pi])) + (Erfc[d*(a + b*Log[c*x
^n])]*(a + b*Log[c*x^n]))/(b*n)
```

Rule 6485

```
Int[Erfc[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[(a + b*x)*(Erfc[a + b*x]/b)
, x] - Simp[1/(b*Sqrt[Pi]*E^(a + b*x)^2), x] /; FreeQ[{a, b}, x]
```

Rubi steps

$$\begin{aligned}\int \frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{x}\,dx &= \frac{\operatorname{Subst}\left(\int \operatorname{erfc}(d(a+bx))\,dx,x,\log(cx^n)\right)}{n}\\ &= \frac{\operatorname{Subst}\left(\int \operatorname{erfc}(x)\,dx,x,ad+bd\log(cx^n)\right)}{bdn}\\ &= -\frac{e^{-(ad+bd\log(cx^n))^2}}{bdn\sqrt{\pi}}+\frac{\operatorname{erfc}(ad+bd\log(cx^n))(a+b\log(cx^n))}{bn}\end{aligned}$$

Mathematica [A]
time = 0.10, size = 93, normalized size = 1.41

$$\frac{-\frac{e^{-d^2\left(a^2+b^2\log^2(cx^n)\right)}(cx^n)^{-2abd^2}}{bd\sqrt{\pi}}-\frac{a\operatorname{Erf}(d(a+b\log(cx^n)))}{b}+\operatorname{Erfc}(d(a+b\log(cx^n)))\log(cx^n)}{n}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[d*(a + b*Log[c*x^n])]/x,x]
```

```
[Out] (-(1/(b*d*E^(d^2*(a^2 + b^2*Log[c*x^n]^2))*Sqrt[Pi]*(c*x^n)^(2*a*b*d^2))) -
 (a*Erf[d*(a + b*Log[c*x^n])])/b + Erfc[d*(a + b*Log[c*x^n])]*Log[c*x^n])/n
```

Maple [A]
time = 0.94, size = 63, normalized size = 0.95

method	result	size
derivativedivides	$\frac{(ad+bd\ln(c\,x^{n}))\mathrm{erfc}(ad+bd\ln(c\,x^{n}))-\frac{\mathrm{e}^{-(ad+bd\ln(c\,x^{n}))^{2}}}{\sqrt{\pi}}}{nbd}$	63
default	$\frac{(ad+bd\ln(c\,x^{n}))\mathrm{erfc}(ad+bd\ln(c\,x^{n}))-\frac{\mathrm{e}^{-(ad+bd\ln(c\,x^{n}))^{2}}}{\sqrt{\pi}}}{nbd}$	63

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(d*(a+b*ln(c*x^n)))/x,x,method=_RETURNVERBOSE)
```

```
[Out] 1/n/b/d*((a*d+b*d*ln(c*x^n))*erfc(a*d+b*d*ln(c*x^n))-1/Pi^(1/2)*exp(-(a*d+b
*d*ln(c*x^n))^2))
```

Maxima [A]
time = 0.25, size = 59, normalized size = 0.89

$$\frac{(b\log\left(cx^{n}\right)+a)d\,\mathrm{erfc}\left((b\log\left(cx^{n}\right)+a)d\right)-\frac{e^{\left(-(b\log(cx^{n})+a)^{2}d^{2}\right)}}{\sqrt{\pi}}}{bdn}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*log(c*x^n)))/x,x, algorithm="maxima")
```

```
[Out] ((b*log(c*x^n) + a)*d*erfc((b*log(c*x^n) + a)*d) - e^(-(b*log(c*x^n) + a)^2
*d^2)/sqrt(pi))/(b*d*n)
```

Fricas [B] Leaf count of result is larger than twice the leaf count of optimal. 128 vs. 2(63) = 126.
time = 0.35, size = 128, normalized size = 1.94

$$\frac{\pi bdn\log\left(x\right)-\left(\pi bdn\log\left(x\right)+\pi bd\log\left(c\right)+\pi ad\right)\mathrm{erf}\left(bd\log\left(cx^{n}\right)+ad\right)-\sqrt{\pi}\,e^{\left(-b^{2}d^{2}n^{2}\log(x)^{2}-b^{2}d^{2}\log(c)^{2}-2\,abd^{2}\log(c)-a^{2}d^{2}-2\,\left(b^{2}d^{2}n\log(c)+abd^{2}n\right)\log(x)\right)}}{\pi bdn}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*log(c*x^n)))/x,x, algorithm="fricas")
```

```
[Out] (pi*b*d*n*log(x) - (pi*b*d*n*log(x) + pi*b*d*log(c) + pi*a*d)*erf(b*d*log(c
*x^n) + a*d) - sqrt(pi)*e^(-b^2*d^2*n^2*log(x)^2 - b^2*d^2*log(c)^2 - 2*a*b
```

```
*d^2*log(c) - a^2*d^2 - 2*(b^2*d^2*n*log(c) + a*b*d^2*n)*log(x)))/(pi*b*d*n
)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}\left(ad + bd \log\left(cx^{n}\right)\right)}{x}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*ln(c*x**n)))/x,x)
```

```
[Out] Integral(erfc(a*d + b*d*log(c*x**n))/x, x)
```

Giac [A]
time = 0.40, size = 83, normalized size = 1.26

$$\frac{bdn\log\left(x\right) + bd\log\left(c\right) + ad - \left(bdn\log\left(x\right) + bd\log\left(c\right) + ad\right)\operatorname{erf}\left(bdn\log\left(x\right) + bd\log\left(c\right) + ad\right) - \frac{e^{\left(-\left(bdn\log\left(x\right) + bd\log\left(c\right) + ad\right)^{2}\right)}}{\sqrt{\pi}}}{bdn}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*log(c*x^n)))/x,x, algorithm="giac")
```

```
[Out] (b*d*n*log(x) + b*d*log(c) + a*d - (b*d*n*log(x) + b*d*log(c) + a*d)*erf(b*
d*n*log(x) + b*d*log(c) + a*d) - e^(-(b*d*n*log(x) + b*d*log(c) + a*d)^2)/s
qrt(pi))/(b*d*n)
```

Mupad [B]
time = 0.45, size = 100, normalized size = 1.52

$$\frac{\mathrm{erfc}(d\left(a+b\,\ln\left(c\,x^n\right)\right))\,\ln\left(c\,x^n\right)}{n}+\frac{a\,\mathrm{erfc}(d\left(a+b\,\ln\left(c\,x^n\right)\right))}{b\,n}-\frac{{\mathrm{e}}^{-b^2\,d^2\,{\ln\left(c\,x^n\right)}^2}\,{\mathrm{e}}^{-a^2\,d^2}}{b\,d\,n\,\sqrt{\pi}\,{\left(c\,x^n\right)}^{2\,a\,b\,d^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(d*(a + b*log(c*x^n)))/x,x)
```

```
[Out] (erfc(d*(a + b*log(c*x^n)))*log(c*x^n))/n + (a*erfc(d*(a + b*log(c*x^n))))/
(b*n) - (exp(-b^2*d^2*log(c*x^n)^2)*exp(-a^2*d^2))/(b*d*n*pi^(1/2)*(c*x^n)^
(2*a*b*d^2))
```

3.147 $\int \frac{\operatorname{Erfc}(d(a+b\log(cx^n)))}{x^2}\,dx$

Optimal. Leaf size=93

$$-\frac{e^{\frac{1}{4b^2d^2n^2}+\frac{a}{bn}}(cx^n)^{\frac{1}{n}}\operatorname{Erf}\left(\frac{2abd^2+\frac{1}{n}+2b^2d^2\log(cx^n)}{2bd}\right)}{x}-\frac{\operatorname{Erfc}(d(a+b\log(cx^n)))}{x}$$

```
[Out] -exp(1/4/b^2/d^2/n^2+a/b/n)*(c*x^n)^(1/n)*erf(1/2*(2*a*b*d^2+1/n+2*b^2*d^2*
ln(c*x^n))/b/d)/x-erfc(d*(a+b*ln(c*x^n)))/x
```

Rubi [A]
time = 0.10, antiderivative size = 93, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.294$, Rules used = {6537, 2314, 2308, 2266, 2236}

$$-\frac{(cx^n)^{\frac{1}{n}}e^{\frac{a}{bn}+\frac{1}{4b^2d^2n^2}}\operatorname{Erf}\left(\frac{2abd^2+2b^2d^2\log(cx^n)+\frac{1}{n}}{2bd}\right)}{x}-\frac{\operatorname{Erfc}(d(a+b\log(cx^n)))}{x}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[d*(a + b*Log[c*x^n])]/x^2,x]
```

```
[Out] -((E^(1/(4*b^2*d^2*n^2) + a/(b*n))*(c*x^n)^n^(-1)*Erf[(2*a*b*d^2 + n^(-1) +
 2*b^2*d^2*Log[c*x^n])/(2*b*d)])/x) - Erfc[d*(a + b*Log[c*x^n])]/x
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2314

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^m*((c*(d + e*x)^n)^(2
*a*b*f*Log[F])/(d + e*x)^(m + 2*a*b*f*n*Log[F])), Int[(d + e*x)^(m + 2*a*b*
f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2), x], x] /; FreeQ[{F, a,
b, c, d, e, f, g, h, m, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 6537

```
Int[Erfc[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_))^(m_.), x
_Symbol] :> Simp[(e*x)^(m + 1)*(Erfc[d*(a + b*Log[c*x^n])]/(e*(m + 1))), x]
 + Dist[2*b*d*(n/(Sqrt[Pi]*(m + 1))), Int[(e*x)^m/E^(d*(a + b*Log[c*x^n]))^
2, x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int \frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{x^2}\,dx &= -\frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{x} - \frac{(2bdn)\int \frac{e^{-d^2(a+b\log(cx^n))^2}}{x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{x} - \frac{(2bdn)\int \frac{\exp\left(-a^2d^2-2abd^2\log(cx^n)-b^2d^2\log^2(cx^n)\right)}{x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{x} - \frac{(2bdn)\int \frac{e^{-a^2d^2-b^2d^2\log^2(cx^n)}(cx^n)^{-2abd^2}}{x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{x} - \frac{\left(2bdnx^{2abd^2n}(cx^n)^{-2abd^2}\right)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}x^{-}}{\sqrt{\pi}}\\
&= -\frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{x} - \frac{\left(2bd(cx^n)^{-2abd^2-\frac{-1-2abd^2n}{n}}\right)\operatorname{Subst}\left(\int \exp\left(-a^2d\right.\right.}{\sqrt{\pi}\,x}\\
&= -\frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{x} - \frac{\left(2bde^{\frac{1}{4b^2d^2n^2}+\frac{a}{bn}}(cx^n)^{-2abd^2-\frac{-1-2abd^2n}{n}}\right)\operatorname{Subst}\left(\int\right.}{\sqrt{\pi}}\\
&= -\frac{e^{\frac{1}{4b^2d^2n^2}+\frac{a}{bn}}(cx^n)^{\frac{1}{n}}\operatorname{erf}\left(\frac{2abd^2+\frac{1}{n}+2b^2d^2\log(cx^n)}{2bd}\right)}{x} - \frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{x}
\end{aligned}$$

Mathematica [A]
time = 0.21, size = 81, normalized size = 0.87

$$-\frac{e^{\frac{1+4abd^2n}{4b^2d^2n^2}}(cx^n)^{\frac{1}{n}}\operatorname{Erf}\left(ad+\frac{1}{2bdn}+bd\log(cx^n)\right)+\operatorname{Erfc}(d(a+b\log(cx^n)))}{x}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[d*(a + b*Log[c*x^n])]/x^2,x]
```

```
[Out] -((E^((1 + 4*a*b*d^2*n)/(4*b^2*d^2*n^2))*(c*x^n)^n^(-1)*Erf[a*d + 1/(2*b*d*
n) + b*d*Log[c*x^n]] + Erfc[d*(a + b*Log[c*x^n])])/x)
```

Maple [F]
time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}(d(a+b\ln(c\,x^n)))}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(d*(a+b*ln(c*x^n)))/x^2,x)
```

```
[Out] int(erfc(d*(a+b*ln(c*x^n)))/x^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*log(c*x^n)))/x^2,x, algorithm="maxima")
```

```
[Out] integrate(erfc((b*log(c*x^n) + a)*d)/x^2, x)
```

Fricas [A]
time = 0.41, size = 128, normalized size = 1.38

$$-\frac{\sqrt{b^2d^2n^2}\,x\operatorname{erf}\left(\frac{(2\,b^2d^2n^2\log(x)+2\,b^2d^2n\log(c)+2\,abd^2n+1)\sqrt{b^2d^2n^2}}{2\,b^2d^2n^2}\right)e^{\left(\frac{4\,b^2d^2n\log(c)+4\,abd^2n+1}{4\,b^2d^2n^2}\right)}-\operatorname{erf}\left(bd\log\left(cx^n\right)+ad\right)+1}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*log(c*x^n)))/x^2,x, algorithm="fricas")
```

```
[Out] -(sqrt(b^2*d^2*n^2)*x*erf(1/2*(2*b^2*d^2*n^2*log(x) + 2*b^2*d^2*n*log(c) +
2*a*b*d^2*n + 1)*sqrt(b^2*d^2*n^2)/(b^2*d^2*n^2))*e^(1/4*(4*b^2*d^2*n*log(c
) + 4*a*b*d^2*n + 1)/(b^2*d^2*n^2)) - erf(b*d*log(c*x^n) + a*d) + 1)/x
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}\left(ad+bd\log\left(cx^n\right)\right)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*ln(c*x**n)))/x**2,x)
```

```
[Out] Integral(erfc(a*d + b*d*log(c*x**n))/x**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*log(c*x^n)))/x^2,x, algorithm="giac")
```

```
[Out] integrate(erfc((b*log(c*x^n) + a)*d)/x^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erfc}(d\,(a+b\,\ln\left(c\,x^n\right)))}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(d*(a + b*log(c*x^n)))/x^2,x)
```

```
[Out] int(erfc(d*(a + b*log(c*x^n)))/x^2, x)
```

3.148 $\int \frac{\mathbf{Erfc}(d(a+b\log(cx^n)))}{x^3}\,dx$

Optimal. Leaf size=95

$$-\frac{e^{\frac{1+2abd^2n}{b^2d^2n^2}}(cx^n)^{2/n}\operatorname{Erf}\left(\frac{1+abd^2n+b^2d^2n\log(cx^n)}{bdn}\right)}{2x^2}-\frac{\operatorname{Erfc}(d(a+b\log(cx^n)))}{2x^2}$$

```
[Out] -1/2*exp((2*a*b*d^2*n+1)/b^2/d^2/n^2)*(c*x^n)^(2/n)*erf((1+a*b*d^2*n+b^2*d^
2*n*ln(c*x^n))/b/d/n)/x^2-1/2*erfc(d*(a+b*ln(c*x^n)))/x^2
```

Rubi [A]
time = 0.10, antiderivative size = 95, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.294$, Rules used = {6537, 2314, 2308, 2266, 2236}

$$-\frac{(cx^n)^{2/n}e^{\frac{2abd^2n+1}{b^2d^2n^2}}\operatorname{Erf}\left(\frac{abd^2n+b^2d^2n\log(cx^n)+1}{bdn}\right)}{2x^2}-\frac{\operatorname{Erfc}(d(a+b\log(cx^n)))}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[d*(a + b*Log[c*x^n])]/x^3,x]
```

```
[Out] -1/2*(E^((1 + 2*a*b*d^2*n)/(b^2*d^2*n^2))*(c*x^n)^(2/n)*Erf[(1 + a*b*d^2*n
+ b^2*d^2*n*Log[c*x^n])/(b*d*n)])/x^2 - Erfc[d*(a + b*Log[c*x^n])]/(2*x^2)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2314

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^m*((c*(d + e*x)^n)^(2
*a*b*f*Log[F])/(d + e*x)^(m + 2*a*b*f*n*Log[F])), Int[(d + e*x)^(m + 2*a*b*
f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2), x], x] /; FreeQ[{F, a,
b, c, d, e, f, g, h, m, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 6537

```
Int[Erfc[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_))^(m_.), x
_Symbol] :> Simp[(e*x)^(m + 1)*(Erfc[d*(a + b*Log[c*x^n])]/(e*(m + 1))), x]
 + Dist[2*b*d*(n/(Sqrt[Pi]*(m + 1))), Int[(e*x)^m/E^(d*(a + b*Log[c*x^n]))^
2, x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{x^3}\,dx &= -\frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{2x^2}-\frac{(bdn)\int \frac{e^{-d^2(a+b\log(cx^n))^2}}{x^3}\,dx}{\sqrt{\pi}}\\
&= -\frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{2x^2}-\frac{(bdn)\int \frac{\exp\left(-a^2d^2-2abd^2\log(cx^n)-b^2d^2\log^2(cx^n)\right)}{x^3}\,dx}{\sqrt{\pi}}\\
&= -\frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{2x^2}-\frac{(bdn)\int \frac{e^{-a^2d^2-b^2d^2\log^2(cx^n)}(cx^n)^{-2abd^2}}{x^3}\,dx}{\sqrt{\pi}}\\
&= -\frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{2x^2}-\frac{\left(bdnx^{2abd^2n}(cx^n)^{-2abd^2}\right)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}x^{-3}}{\sqrt{\pi}}\\
&= -\frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{2x^2}-\frac{\left(bd(cx^n)^{-2abd^2-\frac{-2-2abd^2n}{n}}\right)\operatorname{Subst}\left(\int \exp\left(-a^2d^2\right.\right.}{\sqrt{\pi}\,x^2}\\
&= -\frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{2x^2}-\frac{\left(bde^{\frac{1+2abd^2n}{b^2d^2n^2}}(cx^n)^{-2abd^2-\frac{-2-2abd^2n}{n}}\right)\operatorname{Subst}\left(\int \exp\right.}{\sqrt{\pi}\,x^2}\\
&= -\frac{e^{\frac{1+2abd^2n}{b^2d^2n^2}}(cx^n)^{2/n}\operatorname{erf}\left(\frac{1+abd^2n+b^2d^2n\log(cx^n)}{bdn}\right)}{2x^2}-\frac{\operatorname{erfc}(d(a+b\log(cx^n)))}{2x^2}
\end{aligned}
$$

Mathematica [A]
time = 0.21, size = 79, normalized size = 0.83

$$
-\frac{e^{\frac{1+2abd^2n}{b^2d^2n^2}}(cx^n)^{2/n}\operatorname{Erf}\left(ad+\frac{1}{bdn}+bd\log(cx^n)\right)+\operatorname{Erfc}(d(a+b\log(cx^n)))}{2x^2}
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[d*(a + b*Log[c*x^n])]/x^3,x]
```

```
[Out] -1/2*(E^((1 + 2*a*b*d^2*n)/(b^2*d^2*n^2))*(c*x^n)^(2/n)*Erf[a*d + 1/(b*d*n)
 + b*d*Log[c*x^n]] + Erfc[d*(a + b*Log[c*x^n])])/x^2
```

Maple [F]
time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}(d(a+b\ln(c\,x^n)))}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(d*(a+b*ln(c*x^n)))/x^3,x)
```

```
[Out] int(erfc(d*(a+b*ln(c*x^n)))/x^3,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*log(c*x^n)))/x^3,x, algorithm="maxima")
```

```
[Out] integrate(erfc((b*log(c*x^n) + a)*d)/x^3, x)
```

Fricas [A]
time = 0.37, size = 125, normalized size = 1.32

$$-\frac{\sqrt{b^2d^2n^2}\,x^2\operatorname{erf}\left(\frac{(b^2d^2n^2\log(x)+b^2d^2n\log(c)+abd^2n+1)\sqrt{b^2d^2n^2}}{b^2d^2n^2}\right)e^{\left(\frac{2\,b^2d^2n\log(c)+2\,abd^2n+1}{b^2d^2n^2}\right)}-\operatorname{erf}\left(bd\log\left(cx^n\right)+ad\right)+1}{2\,x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*log(c*x^n)))/x^3,x, algorithm="fricas")
```

```
[Out] -1/2*(sqrt(b^2*d^2*n^2)*x^2*erf((b^2*d^2*n^2*log(x) + b^2*d^2*n*log(c) + a*
b*d^2*n + 1)*sqrt(b^2*d^2*n^2)/(b^2*d^2*n^2))*e^((2*b^2*d^2*n*log(c) + 2*a*
b*d^2*n + 1)/(b^2*d^2*n^2)) - erf(b*d*log(c*x^n) + a*d) + 1)/x^2
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}\left(ad+bd\log\left(cx^n\right)\right)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*ln(c*x**n)))/x**3,x)
```

```
[Out] Integral(erfc(a*d + b*d*log(c*x**n))/x**3, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(d*(a+b*log(c*x^n)))/x^3,x, algorithm="giac")
```

```
[Out] integrate(erfc((b*log(c*x^n) + a)*d)/x^3, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erfc}(d\,(a+b\,\ln\left(c\,x^n\right)))}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(d*(a + b*log(c*x^n)))/x^3,x)
```

```
[Out] int(erfc(d*(a + b*log(c*x^n)))/x^3, x)
```

3.149 $\int (ex)^m \mathbf{Erfc}(d(a+b\log(cx^n)))\,dx$

Optimal. Leaf size=126

$$-\frac{e^{\frac{(1+m)\left(1+m-4abd^2n\right)}{4b^2d^2n^2}}x(ex)^m\left(cx^n\right)^{-\frac{1+m}{n}}\operatorname{Erf}\left(\frac{1+m-2abd^2n-2b^2d^2n\log(cx^n)}{2bdn}\right)}{1+m}+\frac{(ex)^{1+m}\operatorname{Erfc}(d(a+b\log(cx^n)))}{e(1+m)}$$

```
[Out] -exp(1/4*(1+m)*(-4*a*b*d^2*n+m+1)/b^2/d^2/n^2)*x*(e*x)^m*erf(1/2*(1+m-2*a*b
*d^2*n-2*b^2*d^2*n*ln(c*x^n))/b/d/n)/(1+m)/((c*x^n)^((1+m)/n))+(e*x)^(1+m)*
erfc(d*(a+b*ln(c*x^n)))/e/(1+m)
```

Rubi [A]
time = 0.13, antiderivative size = 126, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {6537, 2314, 2308, 2266, 2236}

$$\frac{(ex)^{m+1}\operatorname{Erfc}(d(a+b\log(cx^n)))}{e(m+1)}-\frac{x(ex)^m\left(cx^n\right)^{-\frac{m+1}{n}}\exp\left(\frac{(m+1)(-4abd^2n+m+1)}{4b^2d^2n^2}\right)\operatorname{Erf}\left(\frac{-2abd^2n-2b^2d^2n\log(cx^n)+m+1}{2bdn}\right)}{m+1}$$

Antiderivative was successfully verified.

```
[In] Int[(e*x)^m*Erfc[d*(a + b*Log[c*x^n])],x]
```

```
[Out] -((E^(((1 + m)*(1 + m - 4*a*b*d^2*n))/(4*b^2*d^2*n^2))*x*(e*x)^m*Erf[(1 + m
 - 2*a*b*d^2*n - 2*b^2*d^2*n*Log[c*x^n])/(2*b*d*n)])/((1 + m)*(c*x^n)^((1 +
 m)/n))) + ((e*x)^(1 + m)*Erfc[d*(a + b*Log[c*x^n])])/(e*(1 + m))
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2314

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^m*((c*(d + e*x)^n)^(2
*a*b*f*Log[F])/(d + e*x)^(m + 2*a*b*f*n*Log[F])), Int[(d + e*x)^(m + 2*a*b*
f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2), x], x] /; FreeQ[{F, a,
b, c, d, e, f, g, h, m, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 6537

```
Int[Erfc[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_))^(m_.), x
_Symbol] :> Simp[(e*x)^(m + 1)*(Erfc[d*(a + b*Log[c*x^n])]/(e*(m + 1))), x]
 + Dist[2*b*d*(n/(Sqrt[Pi]*(m + 1))), Int[(e*x)^m/E^(d*(a + b*Log[c*x^n]))^
2, x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int (ex)^m \operatorname{erfc}(d(a+b\log(cx^n)))\,dx &= \frac{(ex)^{1+m}\operatorname{erfc}(d(a+b\log(cx^n)))}{e(1+m)} + \frac{(2bdn)\int e^{-d^2(a+b\log(cx^n))^2}(ex)^m\,dx}{(1+m)\sqrt{\pi}} \\
&= \frac{(ex)^{1+m}\operatorname{erfc}(d(a+b\log(cx^n)))}{e(1+m)} + \frac{(2bdn)\int \exp\left(-a^2d^2-2abd^2\log(cx\right.}{(1+m)\sqrt{}} \\
&= \frac{(ex)^{1+m}\operatorname{erfc}(d(a+b\log(cx^n)))}{e(1+m)} + \frac{(2bdn)\int e^{-a^2d^2-b^2d^2\log^2(cx^n)}(ex)^m\,(cx}{(1+m)\sqrt{\pi}} \\
&= \frac{(ex)^{1+m}\operatorname{erfc}(d(a+b\log(cx^n)))}{e(1+m)} + \frac{\left(2bdnx^{2abd^2n}(cx^n)^{-2abd^2}\right)\int e^{-a^2d^2-b^2}}{(1+m)\sqrt{\pi}} \\
&= \frac{(ex)^{1+m}\operatorname{erfc}(d(a+b\log(cx^n)))}{e(1+m)} + \frac{\left(2bdnx^{-m+2abd^2n}(ex)^m\,(cx^n)^{-2abd^2}\right)}{(1+m)} \\
&= \frac{(ex)^{1+m}\operatorname{erfc}(d(a+b\log(cx^n)))}{e(1+m)} + \frac{\left(2bdx(ex)^m\,(cx^n)^{-2abd^2-\frac{1+m-2abd^2n}{n}}\right)}{} \\
&= \frac{(ex)^{1+m}\operatorname{erfc}(d(a+b\log(cx^n)))}{e(1+m)} + \frac{\left(2bd\exp\left(\frac{(1+m)(1+m-4abd^2n)}{4b^2d^2n^2}\right)x(ex)^{}\right.}{} \\
&= -\frac{\exp\left(\frac{(1+m)(1+m-4abd^2n)}{4b^2d^2n^2}\right)x(ex)^m\,(cx^n)^{-\frac{1+m}{n}}\operatorname{erf}\left(\frac{1+m-2abd^2n-2b^2d^2n\log(cx}{2bdn}\right.}{1+m}
\end{aligned}
$$

Mathematica [A]

time = 0.37, size = 126, normalized size = 1.00

$$\frac{(ex)^m \left(e^{\frac{(1+m)\left(1+m-4abd^2n+4b^2d^2n^2\log(x)-4b^2d^2n\log(cx^n)\right)}{4b^2d^2n^2}} x^{-m}\mathrm{Erf}\left(ad-\frac{1+m-2b^2d^2n\log(cx^n)}{2bdn}\right)+x\mathrm{Erfc}(d(a+b\log(cx^n)))\right)}{1+m}$$

Antiderivative was successfully verified.

```
[In] Integrate[(e*x)^m*Erfc[d*(a + b*Log[c*x^n])],x]
```

```
[Out] ((e*x)^m*((E^(((1 + m)*(1 + m - 4*a*b*d^2*n + 4*b^2*d^2*n^2*Log[x] - 4*b^2*
d^2*n*Log[c*x^n]))/(4*b^2*d^2*n^2))*Erf[a*d - (1 + m - 2*b^2*d^2*n*Log[c*x^
n])/(2*b*d*n)])/x^m + x*Erfc[d*(a + b*Log[c*x^n])]))/(1 + m)
```

Maple [F]
time = 0.06, size = 0, normalized size = 0.00

$$\int (ex)^m \operatorname{erfc}(d(a+b\ln(c\,x^n)))\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*erfc(d*(a+b*ln(c*x^n))),x)
```

```
[Out] int((e*x)^m*erfc(d*(a+b*ln(c*x^n))),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*erfc(d*(a+b*log(c*x^n))),x, algorithm="maxima")
```

```
[Out] integrate((x*e)^m*erfc((b*log(c*x^n) + a)*d), x)
```

Fricas [A]
time = 0.37, size = 186, normalized size = 1.48

$$-\frac{x\operatorname{erf}\left(bd\log\left(cx^n\right)+ad\right)e^{(m\log(x)+m)}-\sqrt{b^2d^2n^2}\operatorname{erf}\left(\frac{(2\,b^2d^2n^2\log(x)+2\,b^2d^2n\log(c)+2\,abd^2n-m-1)\sqrt{b^2d^2n^2}}{2\,b^2d^2n^2}\right)e^{\left(\frac{4\,b^2d^2mn^2-4\left(b^2d^2m+b^2d^2\right)n\log(c)+m^2-4\left(abd^2m+abd^2\right)n+2\,m+1}{4\,b^2d^2n^2}\right)}-xe^{(m\log(x)+m)}}{m+1}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*erfc(d*(a+b*log(c*x^n))),x, algorithm="fricas")
```

```
[Out] -(x*erf(b*d*log(c*x^n) + a*d)*e^(m*log(x) + m) - sqrt(b^2*d^2*n^2)*erf(1/2*
(2*b^2*d^2*n^2*log(x) + 2*b^2*d^2*n*log(c) + 2*a*b*d^2*n - m - 1)*sqrt(b^2*
d^2*n^2)/(b^2*d^2*n^2))*e^(1/4*(4*b^2*d^2*m*n^2 - 4*(b^2*d^2*m + b^2*d^2)*n
```

```
*log(c) + m^2 - 4*(a*b*d^2*m + a*b*d^2)*n + 2*m + 1)/(b^2*d^2*n^2)) - x*e^(
m*log(x) + m))/(m + 1)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int (ex)^m \operatorname{erfc}\left(ad + bd\log\left(cx^n\right)\right) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*erfc(d*(a+b*ln(c*x**n))),x)
[Out] Integral((e*x)**m*erfc(a*d + b*d*log(c*x**n)), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*erfc(d*(a+b*log(c*x^n))),x, algorithm="giac")
[Out] integrate((e*x)^m*erfc((b*log(c*x^n) + a)*d), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \operatorname{erfc}(d\,(a + b\,\ln\left(c\,x^n\right)))\,\left(e\,x\right)^m\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(d*(a + b*log(c*x^n)))*(e*x)^m,x)
[Out] int(erfc(d*(a + b*log(c*x^n)))*(e*x)^m, x)
```

3.150 $\int e^{c-b^2x^2}\mathbf{Erfc}(bx)^2\,dx$

Optimal. Leaf size=21

$$-\frac{e^c\sqrt{\pi}\,\text{Erfc}(bx)^3}{6b}$$

[Out] -1/6*exp(c)*erfc(b*x)^3*Pi^(1/2)/b

Rubi [A]
time = 0.02, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = $\{6509, 30\}$

$$-\frac{\sqrt{\pi}\,e^c\text{Erfc}(bx)^3}{6b}$$

Antiderivative was successfully verified.

[In] Int[E^(c - b^2*x^2)*Erfc[b*x]^2,x]

[Out] -1/6*(E^c*Sqrt[Pi]*Erfc[b*x]^3)/b

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rubi steps

$$\begin{aligned}\int e^{c-b^2x^2}\text{erfc}(bx)^2\,dx &= -\frac{\left(e^c\sqrt{\pi}\right)\text{Subst}\left(\int x^2\,dx, x, \text{erfc}(bx)\right)}{2b}\\ &= -\frac{e^c\sqrt{\pi}\,\text{erfc}(bx)^3}{6b}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 21, normalized size = 1.00

$$-\frac{e^c\sqrt{\pi}\,\text{Erfc}(bx)^3}{6b}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c - b^2*x^2)*Erfc[b*x]^2,x]
```

```
[Out] -1/6*(E^c*Sqrt[Pi]*Erfc[b*x]^3)/b
```

Maple [B] Leaf count of result is larger than twice the leaf count of optimal. 42 vs. $2(16) = 32$.
time = 0.35, size = 43, normalized size = 2.05

method	result	size
default	$\frac{\frac{e^{c}\sqrt{\pi}\,\operatorname{erf}(bx)}{2}-\frac{e^{c}\sqrt{\pi}\,\operatorname{erf}(bx)^{2}}{2}+\frac{e^{c}\sqrt{\pi}\,\operatorname{erf}(bx)^{3}}{6}}{b}$	43

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(-b^2*x^2+c)*erfc(b*x)^2,x,method=_RETURNVERBOSE)
```

```
[Out] (1/2*exp(c)*Pi^(1/2)*erf(b*x)-1/2*exp(c)*Pi^(1/2)*erf(b*x)^2+1/6*exp(c)*Pi^
(1/2)*erf(b*x)^3)/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erfc(b*x)^2,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)^2*e^(-b^2*x^2 + c), x)
```

Fricas [A]
time = 0.37, size = 31, normalized size = 1.48

$$\frac{\sqrt{\pi}\left(\operatorname{erf}\left(bx\right)^{3}-3\operatorname{erf}\left(bx\right)^{2}+3\operatorname{erf}\left(bx\right)\right)e^{c}}{6\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erfc(b*x)^2,x, algorithm="fricas")
```

```
[Out] 1/6*sqrt(pi)*(erf(b*x)^3 - 3*erf(b*x)^2 + 3*erf(b*x))*e^c/b
```

Sympy [A]
time = 0.42, size = 24, normalized size = 1.14

$$\begin{cases} -\frac{\sqrt{\pi}\,e^{c}\operatorname{erfc}^{3}(bx)}{6b} & \text{for}\ b \neq 0 \\ xe^{c} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b**2*x**2+c)*erfc(b*x)**2,x)
```

```
[Out] Piecewise((-sqrt(pi)*exp(c)*erfc(b*x)**3/(6*b), Ne(b, 0)), (x*exp(c), True)
)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erfc(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)^2*e^(-b^2*x^2 + c), x)
```

Mupad [B]
time = 0.15, size = 16, normalized size = 0.76

$$-\frac{\sqrt{\pi}\,\mathrm{e}^{c}\,\mathrm{erfc}(b\,x)^3}{6\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c - b^2*x^2)*erfc(b*x)^2,x)
```

```
[Out] -(pi^(1/2)*exp(c)*erfc(b*x)^3)/(6*b)
```

3.151 $\int e^{c-b^2x^2}\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=21

$$-\frac{e^c\sqrt{\pi}\,\text{Erfc}(bx)^2}{4b}$$

```
[Out] -1/4*exp(c)*erfc(b*x)^2*Pi^(1/2)/b
```

Rubi [A]
time = 0.01, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {6509, 30}

$$-\frac{\sqrt{\pi}\,e^c\text{Erfc}(bx)^2}{4b}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c - b^2*x^2)*Erfc[b*x],x]
```

```
[Out] -1/4*(E^c*Sqrt[Pi]*Erfc[b*x]^2)/b
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rubi steps

$$\begin{aligned}\int e^{c-b^2x^2}\text{erfc}(bx)\,dx &= -\frac{\left(e^c\sqrt{\pi}\right)\text{Subst}\left(\int x\,dx, x, \text{erfc}(bx)\right)}{2b}\\ &= -\frac{e^c\sqrt{\pi}\,\text{erfc}(bx)^2}{4b}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 21, normalized size = 1.00

$$-\frac{e^c\sqrt{\pi}\,\text{Erfc}(bx)^2}{4b}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c - b^2*x^2)*Erfc[b*x],x]
```

```
[Out] -1/4*(E^c*Sqrt[Pi]*Erfc[b*x]^2)/b
```

Maple [A]
time = 0.26, size = 30, normalized size = 1.43

method	result	size
default	$\frac{\frac{e^{c}\sqrt{\pi}\ \mathrm{erf}(bx)}{2}-\frac{e^{c}\sqrt{\pi}\ \mathrm{erf}(bx)^{2}}{4}}{b}$	30

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(-b^2*x^2+c)*erfc(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] (1/2*exp(c)*Pi^(1/2)*erf(b*x)-1/4*exp(c)*Pi^(1/2)*erf(b*x)^2)/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erfc(b*x),x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)*e^(-b^2*x^2 + c), x)
```

Fricas [A]
time = 0.35, size = 23, normalized size = 1.10

$$-\frac{\sqrt{\pi}\left(\mathrm{erf}\left(bx\right)^{2}-2\ \mathrm{erf}\left(bx\right)\right)e^{c}}{4\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erfc(b*x),x, algorithm="fricas")
```

```
[Out] -1/4*sqrt(pi)*(erf(b*x)^2 - 2*erf(b*x))*e^c/b
```

Sympy [A]
time = 0.16, size = 24, normalized size = 1.14

$$\begin{cases} -\frac{\sqrt{\pi}\ e^{c}\ \mathrm{erfc}^{2}\left(bx\right)}{4b} & \text{for}\ b\neq 0 \\ xe^{c} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b**2*x**2+c)*erfc(b*x),x)
```

```
[Out] Piecewise((-sqrt(pi)*exp(c)*erfc(b*x)**2/(4*b), Ne(b, 0)), (x*exp(c), True)
)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erfc(b*x),x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(-b^2*x^2 + c), x)
```

Mupad [B]
time = 0.15, size = 16, normalized size = 0.76

$$-\frac{\sqrt{\pi}\,\mathrm{e}^c\,\mathrm{erfc}(b\,x)^2}{4\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c - b^2*x^2)*erfc(b*x),x)
```

```
[Out] -(pi^(1/2)*exp(c)*erfc(b*x)^2)/(4*b)
```

3.152 $\int \frac{e^{c-b^2x^2}}{\textbf{Erfc}(bx)}\,dx$

Optimal. Leaf size=20

$$-\frac{e^c\sqrt{\pi}\,\log(\mathrm{Erfc}(bx))}{2b}$$

```
[Out] -1/2*exp(c)*ln(erfc(b*x))*Pi^(1/2)/b
```

Rubi [A]
time = 0.02, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {6509, 29}

$$-\frac{\sqrt{\pi}\,e^c\log(\mathrm{Erfc}(bx))}{2b}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c - b^2*x^2)/Erfc[b*x],x]
```

```
[Out] -1/2*(E^c*Sqrt[Pi]*Log[Erfc[b*x]])/b
```

Rule 29

```
Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c-b^2x^2}}{\mathrm{erfc}(bx)}\,dx &= -\frac{\left(e^c\sqrt{\pi}\right)\mathrm{Subst}\left(\int \frac{1}{x}\,dx, x, \mathrm{erfc}(bx)\right)}{2b}\\ &= -\frac{e^c\sqrt{\pi}\,\log(\mathrm{erfc}(bx))}{2b}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 20, normalized size = 1.00

$$-\frac{e^c\sqrt{\pi}\,\log(\mathrm{Erfc}(bx))}{2b}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c - b^2*x^2)/Erfc[b*x],x]
```

```
[Out] -1/2*(E^c*Sqrt[Pi]*Log[Erfc[b*x]])/b
```

Maple [**F**]
time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{-b^{2} x^{2}+c}}{\operatorname{erfc}\left(b x\right)}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(-b^2*x^2+c)/erfc(b*x),x)
```

```
[Out] int(exp(-b^2*x^2+c)/erfc(b*x),x)
```

Maxima [**F**]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erfc(b*x),x, algorithm="maxima")
```

```
[Out] integrate(e^(-b^2*x^2 + c)/erfc(b*x), x)
```

Fricas [**A**]
time = 0.37, size = 17, normalized size = 0.85

$$-\frac{\sqrt{\pi}\, e^{c} \log\left(\operatorname{erf}\left(b x\right) - 1\right)}{2\, b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erfc(b*x),x, algorithm="fricas")
```

```
[Out] -1/2*sqrt(pi)*e^c*log(erf(b*x) - 1)/b
```

Sympy [**A**]
time = 0.25, size = 24, normalized size = 1.20

$$\begin{cases} - \frac{\sqrt{\pi} e^{c} \log{\left(\operatorname{erfc}{\left(b x \right)} \right)}}{2 b} & \text{for}\: b \neq 0 \\ x e^{c} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b**2*x**2+c)/erfc(b*x),x)
```

```
[Out] Piecewise((-sqrt(pi)*exp(c)*log(erfc(b*x))/(2*b), Ne(b, 0)), (x*exp(c), Tru
e))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erfc(b*x),x, algorithm="giac")
```

```
[Out] integrate(e^(-b^2*x^2 + c)/erfc(b*x), x)
```

Mupad [B]
time = 0.18, size = 15, normalized size = 0.75

$$-\frac{\sqrt{\pi}\,\ln\left(\mathrm{erfc}(b\,x)\right)\,\mathrm{e}^{c}}{2\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c - b^2*x^2)/erfc(b*x),x)
```

```
[Out] -(pi^(1/2)*log(erfc(b*x))*exp(c))/(2*b)
```

3.153 $\int \frac{e^{c-b^2x^2}}{\textbf{Erfc}(bx)^2}\,dx$

Optimal. Leaf size=21

$$\frac{e^c\sqrt{\pi}}{2b\mathrm{Erfc}(bx)}$$

```
[Out] 1/2*exp(c)*Pi^(1/2)/b/erfc(b*x)
```

Rubi [A]
time = 0.02, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {6509, 30}

$$\frac{\sqrt{\pi}\,e^c}{2b\mathrm{Erfc}(bx)}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c - b^2*x^2)/Erfc[b*x]^2,x]
```

```
[Out] (E^c*Sqrt[Pi])/(2*b*Erfc[b*x])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c-b^2x^2}}{\mathrm{erfc}(bx)^2}\,dx &= -\frac{\left(e^c\sqrt{\pi}\right)\mathrm{Subst}\left(\int \frac{1}{x^2}\,dx, x, \mathrm{erfc}(bx)\right)}{2b}\\ &= \frac{e^c\sqrt{\pi}}{2b\mathrm{erfc}(bx)}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 21, normalized size = 1.00

$$\frac{e^c\sqrt{\pi}}{2b\mathrm{Erfc}(bx)}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c - b^2*x^2)/Erfc[b*x]^2,x]
[Out] (E^c*Sqrt[Pi])/(2*b*Erfc[b*x])
```

Maple [F]
time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{-b^2x^2+c}}{\mathrm{erfc}\,(bx)^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(-b^2*x^2+c)/erfc(b*x)^2,x)
[Out] int(exp(-b^2*x^2+c)/erfc(b*x)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erfc(b*x)^2,x, algorithm="maxima")
[Out] integrate(e^(-b^2*x^2 + c)/erfc(b*x)^2, x)
```

Fricas [A]
time = 0.39, size = 19, normalized size = 0.90

$$-\frac{\sqrt{\pi}\,e^c}{2\,(b\,\mathrm{erf}\,(bx)-b)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erfc(b*x)^2,x, algorithm="fricas")
[Out] -1/2*sqrt(pi)*e^c/(b*erf(b*x) - b)
```

Sympy [A]
time = 0.43, size = 20, normalized size = 0.95

$$\begin{cases} \frac{\sqrt{\pi}\,e^c}{2b\,\mathrm{erfc}\,(bx)} & \text{for } b \neq 0 \\ xe^c & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b**2*x**2+c)/erfc(b*x)**2,x)
```

```
[Out] Piecewise((sqrt(pi)*exp(c)/(2*b*erfc(b*x)), Ne(b, 0)), (x*exp(c), True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erfc(b*x)^2,x, algorithm="giac")
[Out] integrate(e^(-b^2*x^2 + c)/erfc(b*x)^2, x)
```

Mupad [B]
time = 0.16, size = 16, normalized size = 0.76

$$\frac{\sqrt{\pi}\,\mathrm{e}^{c}}{2\,b\,\mathrm{erfc}\left(b\,x\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c - b^2*x^2)/erfc(b*x)^2,x)
[Out] (pi^(1/2)*exp(c))/(2*b*erfc(b*x))
```

3.154 $\int \frac{e^{c-b^2x^2}}{\mathbf{Erfc}(bx)^3}\,dx$

Optimal. Leaf size=21

$$\frac{e^c\sqrt{\pi}}{4b\mathrm{Erfc}(bx)^2}$$

```
[Out] 1/4*exp(c)*Pi^(1/2)/b/erfc(b*x)^2
```

Rubi [A]
time = 0.02, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {6509, 30}

$$\frac{\sqrt{\pi}\,e^c}{4b\mathrm{Erfc}(bx)^2}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c - b^2*x^2)/Erfc[b*x]^3,x]
```

```
[Out] (E^c*Sqrt[Pi])/(4*b*Erfc[b*x]^2)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c-b^2x^2}}{\mathrm{erfc}(bx)^3}\,dx &= -\frac{\left(e^c\sqrt{\pi}\right)\mathrm{Subst}\left(\int \frac{1}{x^3}\,dx, x, \mathrm{erfc}(bx)\right)}{2b}\\ &= \frac{e^c\sqrt{\pi}}{4b\mathrm{erfc}(bx)^2}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 21, normalized size = 1.00

$$\frac{e^c\sqrt{\pi}}{4b\mathrm{Erfc}(bx)^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c - b^2*x^2)/Erfc[b*x]^3,x]
```

```
[Out] (E^c*Sqrt[Pi])/(4*b*Erfc[b*x]^2)
```

Maple [F]
time = 0.21, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{-b^{2} x^{2}+c}}{\operatorname{erfc}\left(b x\right)^{3}}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(-b^2*x^2+c)/erfc(b*x)^3,x)
```

```
[Out] int(exp(-b^2*x^2+c)/erfc(b*x)^3,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erfc(b*x)^3,x, algorithm="maxima")
```

```
[Out] integrate(e^(-b^2*x^2 + c)/erfc(b*x)^3, x)
```

Fricas [A]
time = 0.37, size = 26, normalized size = 1.24

$$\frac{\sqrt{\pi} e^{c}}{4 \, {\left(b \operatorname{erf}\left(b x\right)^{2} - 2 \, b \operatorname{erf}\left(b x\right) + b\right)}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erfc(b*x)^3,x, algorithm="fricas")
```

```
[Out] 1/4*sqrt(pi)*e^c/(b*erf(b*x)^2 - 2*b*erf(b*x) + b)
```

Sympy [A]
time = 0.74, size = 22, normalized size = 1.05

$$\begin{cases} \frac{\sqrt{\pi} e^{c}}{4 b \operatorname{erfc}^{2}{\left(b x \right)}} & \text{for}\: b \neq 0 \\ x e^{c} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b**2*x**2+c)/erfc(b*x)**3,x)
[Out] Piecewise((sqrt(pi)*exp(c)/(4*b*erfc(b*x)**2), Ne(b, 0)), (x*exp(c), True))
```

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)/erfc(b*x)^3,x, algorithm="giac")
[Out] integrate(e^(-b^2*x^2 + c)/erfc(b*x)^3, x)
```

Mupad [**B**]
time = 0.09, size = 16, normalized size = 0.76

$$\frac{\sqrt{\pi}\ \mathrm{e}^{c}}{4\,b\,\mathrm{erfc}\left(b\,x\right)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c - b^2*x^2)/erfc(b*x)^3,x)
[Out] (pi^(1/2)*exp(c))/(4*b*erfc(b*x)^2)
```

3.155 $\int e^{c-b^2x^2}\mathbf{Erfc}(bx)^n\,dx$

Optimal. Leaf size=28

$$-\frac{e^c\sqrt{\pi}\,\mathrm{Erfc}(bx)^{1+n}}{2b(1+n)}$$

```
[Out] -1/2*exp(c)*erfc(b*x)^(1+n)*Pi^(1/2)/b/(1+n)
```

Rubi [A]
time = 0.02, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.105$, Rules used = {6509, 30}

$$-\frac{\sqrt{\pi}\,e^c\mathrm{Erfc}(bx)^{n+1}}{2b(n+1)}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c - b^2*x^2)*Erfc[b*x]^n,x]
```

```
[Out] -1/2*(E^c*Sqrt[Pi]*Erfc[b*x]^(1 + n))/(b*(1 + n))
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rubi steps

$$\begin{aligned}\int e^{c-b^2x^2}\mathrm{erfc}(bx)^n\,dx &= -\frac{\left(e^c\sqrt{\pi}\right)\mathrm{Subst}\left(\int x^n\,dx, x, \mathrm{erfc}(bx)\right)}{2b}\\ &= -\frac{e^c\sqrt{\pi}\,\mathrm{erfc}(bx)^{1+n}}{2b(1+n)}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 28, normalized size = 1.00

$$-\frac{e^c\sqrt{\pi}\,\mathrm{Erfc}(bx)^{1+n}}{2b(1+n)}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c - b^2*x^2)*Erfc[b*x]^n,x]
```

```
[Out] -1/2*(E^c*Sqrt[Pi]*Erfc[b*x]^(1 + n))/(b*(1 + n))
```

Maple [F]
time = 0.07, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{-b^{2} x^{2}+c} \operatorname{erfc}(bx)^{n}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(-b^2*x^2+c)*erfc(b*x)^n,x)
```

```
[Out] int(exp(-b^2*x^2+c)*erfc(b*x)^n,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erfc(b*x)^n,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)^n*e^(-b^2*x^2 + c), x)
```

Fricas [A]
time = 0.36, size = 30, normalized size = 1.07

$$\frac{\sqrt{\pi}\left(-\operatorname{erf}\left(bx\right)+1\right)^{n}\left(\operatorname{erf}\left(bx\right)-1\right)e^{c}}{2\left(bn+b\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erfc(b*x)^n,x, algorithm="fricas")
```

```
[Out] 1/2*sqrt(pi)*(-erf(b*x) + 1)^n*(erf(b*x) - 1)*e^c/(b*n + b)
```

Sympy [B] Leaf count of result is larger than twice the leaf count of optimal. 60 vs. 2(24) = 48.
time = 1.74, size = 60, normalized size = 2.14

$$\begin{cases} xe^{c} & \text{for}\ b = 0 \wedge \left(b = 0 \vee n = -1\right) \\ -\frac{\sqrt{\pi}\, e^{c} \log\left(\operatorname{erfc}\left(bx\right)\right)}{2b} & \text{for}\ n = -1 \\ -\frac{\sqrt{\pi}\, e^{c} \operatorname{erfc}\left(bx\right) \operatorname{erfc}^{n}\left(bx\right)}{2bn+2b} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b**2*x**2+c)*erfc(b*x)**n,x)
```

```
[Out] Piecewise((x*exp(c), Eq(b, 0) & (Eq(b, 0) | Eq(n, -1))), (-sqrt(pi)*exp(c)*
log(erfc(b*x))/(2*b), Eq(n, -1)), (-sqrt(pi)*exp(c)*erfc(b*x)*erfc(b*x)**n/
(2*b*n + 2*b), True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(-b^2*x^2+c)*erfc(b*x)^n,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)^n*e^(-b^2*x^2 + c), x)
```

Mupad [B]
time = 0.20, size = 23, normalized size = 0.82

$$-\frac{\sqrt{\pi}\ \mathrm{e}^c\,\mathrm{erfc}(b\,x)^{n+1}}{2\,b\,\left(n+1\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c - b^2*x^2)*erfc(b*x)^n,x)
```

```
[Out] -(pi^(1/2)*exp(c)*erfc(b*x)^(n + 1))/(2*b*(n + 1))
```

3.156 $\int e^{c+dx^2}x^5\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=283

$$\frac{be^{c-(b^2-d)x^2}x}{(b^2-d)\,d^2\sqrt{\pi}}-\frac{3be^{c-(b^2-d)x^2}x}{4\,(b^2-d)^2\,d\sqrt{\pi}}-\frac{be^{c-(b^2-d)x^2}x^3}{2\,(b^2-d)\,d\sqrt{\pi}}+\frac{be^c\mathrm{Erf}\left(\sqrt{b^2-d}\,x\right)}{\sqrt{b^2-d}\,d^3}-\frac{be^c\mathrm{Erf}\left(\sqrt{b^2-d}\,x\right)}{2\,(b^2-d)^{3/2}\,d^2}+\frac{3be^c\mathrm{Erf}\left(\cdots\right.}{8\,(b^2-\cdots}$$

```
[Out] -1/2*b*exp(c)*erf(x*(b^2-d)^(1/2))/(b^2-d)^(3/2)/d^2+3/8*b*exp(c)*erf(x*(b^
2-d)^(1/2))/(b^2-d)^(5/2)/d+exp(d*x^2+c)*erfc(b*x)/d^3-exp(d*x^2+c)*x^2*erf
c(b*x)/d^2+1/2*exp(d*x^2+c)*x^4*erfc(b*x)/d+b*exp(c)*erf(x*(b^2-d)^(1/2))/d
^3/(b^2-d)^(1/2)+b*exp(c-(b^2-d)*x^2)*x/(b^2-d)/d^2/Pi^(1/2)-3/4*b*exp(c-(b
^2-d)*x^2)*x/(b^2-d)^2/d/Pi^(1/2)-1/2*b*exp(c-(b^2-d)*x^2)*x^3/(b^2-d)/d/Pi
^(1/2)
```

Rubi [A]

time = 0.25, antiderivative size = 283, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {6521, 6518, 2236, 2243}

$$\frac{be^c\mathrm{Erf}\left(x\sqrt{b^2-d}\right)}{d^3\sqrt{b^2-d}}-\frac{be^c\mathrm{Erf}\left(x\sqrt{b^2-d}\right)}{2d^2\,(b^2-d)^{3/2}}+\frac{bxe^{c-x^2(b^2-d)}}{\sqrt{\pi}\,d^2\,(b^2-d)}+\frac{3be^c\mathrm{Erf}\left(x\sqrt{b^2-d}\right)}{8d\,(b^2-d)^{5/2}}-\frac{3bxe^{c-x^2(b^2-d)}}{4\sqrt{\pi}\,d\,(b^2-d)^2}-\frac{bx^3e^{c-x^2(b^2-d)}}{2\sqrt{\pi}\,d\,(b^2-d)}+\frac{\mathrm{Erfc}(bx)e^{c+dx^2}}{d^3}-\frac{x^2\mathrm{Erfc}(bx)e^{c+dx^2}}{d^2}+\frac{x^4\mathrm{Erfc}(bx)e^{c+dx^2}}{2d}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + d*x^2)*x^5*Erfc[b*x],x]
```

```
[Out] (b*E^(c - (b^2 - d)*x^2)*x)/((b^2 - d)*d^2*Sqrt[Pi]) - (3*b*E^(c - (b^2 - d
)*x^2)*x)/(4*(b^2 - d)^2*d*Sqrt[Pi]) - (b*E^(c - (b^2 - d)*x^2)*x^3)/(2*(b^
2 - d)*d*Sqrt[Pi]) + (b*E^c*Erf[Sqrt[b^2 - d]*x])/(Sqrt[b^2 - d]*d^3) - (b*
E^c*Erf[Sqrt[b^2 - d]*x])/(2*(b^2 - d)^(3/2)*d^2) + (3*b*E^c*Erf[Sqrt[b^2 -
 d]*x])/(8*(b^2 - d)^(5/2)*d) + (E^(c + d*x^2)*Erfc[b*x])/d^3 - (E^(c + d*x
^2)*x^2*Erfc[b*x])/d^2 + (E^(c + d*x^2)*x^4*Erfc[b*x])/(2*d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{c+dx^2}x^5\operatorname{erfc}(bx)\,dx &= \frac{e^{c+dx^2}x^4\operatorname{erfc}(bx)}{2d}-\frac{2\int e^{c+dx^2}x^3\operatorname{erfc}(bx)\,dx}{d}+\frac{b\int e^{c-(b^2-d)x^2}x^4\,dx}{d\sqrt{\pi}}\\ &= -\frac{be^{c-(b^2-d)x^2}x^3}{2\left(b^2-d\right)d\sqrt{\pi}}-\frac{e^{c+dx^2}x^2\operatorname{erfc}(bx)}{d^2}+\frac{e^{c+dx^2}x^4\operatorname{erfc}(bx)}{2d}+\frac{2\int e^{c+dx^2}x\operatorname{erfc}(bx)\,dx}{d^2}-\\ &= \frac{be^{c-(b^2-d)x^2}x}{\left(b^2-d\right)d^2\sqrt{\pi}}-\frac{3be^{c-(b^2-d)x^2}x}{4\left(b^2-d\right)^2d\sqrt{\pi}}-\frac{be^{c-(b^2-d)x^2}x^3}{2\left(b^2-d\right)d\sqrt{\pi}}+\frac{e^{c+dx^2}\operatorname{erfc}(bx)}{d^3}-\frac{e^{c+dx^2}x^2\mathrm{e}}{d^2}\\ &= \frac{be^{c-(b^2-d)x^2}x}{\left(b^2-d\right)d^2\sqrt{\pi}}-\frac{3be^{c-(b^2-d)x^2}x}{4\left(b^2-d\right)^2d\sqrt{\pi}}-\frac{be^{c-(b^2-d)x^2}x^3}{2\left(b^2-d\right)d\sqrt{\pi}}+\frac{be^c\operatorname{erf}\left(\sqrt{b^2-d}\,x\right)}{\sqrt{b^2-d}\,d^3}-\frac{be^c\mathrm{e}}{2}\end{aligned}$$

Mathematica [A]
time = 0.92, size = 184, normalized size = 0.65

$$\frac{e^c\left(4e^{dx^2}\left(2-2dx^2+d^2x^4\right)-\frac{2bde^{\left(-b^2+d\right)x^2}x\left(d\left(7-2dx^2\right)+2b^2\left(-2+dx^2\right)\right)}{\left(b^2-d\right)^2\sqrt{\pi}}-4e^{dx^2}\left(2-2dx^2+d^2x^4\right)\operatorname{Erf}(bx)-\frac{b\left(4b^2-7d\right)d\operatorname{Erf}\left(\sqrt{b^2-d}\,x\right)}{\left(b^2-d\right)^{5/2}}+\frac{8b\operatorname{Erfi}\left(\sqrt{-b^2+d}\,x\right)}{\sqrt{-b^2+d}}\right)}{8d^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + d*x^2)*x^5*Erfc[b*x],x]
```

```
[Out] (E^c*(4*E^(d*x^2)*(2 - 2*d*x^2 + d^2*x^4) - (2*b*d*E^((-b^2 + d)*x^2)*x*(d*
(7 - 2*d*x^2) + 2*b^2*(-2 + d*x^2)))/((b^2 - d)^2*Sqrt[Pi]) - 4*E^(d*x^2)*(
2 - 2*d*x^2 + d^2*x^4)*Erf[b*x] - (b*(4*b^2 - 7*d)*d*Erf[Sqrt[b^2 - d]*x])/
(b^2 - d)^(5/2) + (8*b*Erfi[Sqrt[-b^2 + d]*x])/Sqrt[-b^2 + d]))/(8*d^3)
```

Maple [A]
time = 0.42, size = 376, normalized size = 1.33

method	result
default	$\frac{\frac{e^{c}\left(\frac{e^{d\,x^{2}}b^{6}x^{4}}{2d}-\frac{2b^{2}\left(\frac{b^{4}x^{2}e^{d\,x^{2}}}{2d}-\frac{b^{4}e^{d\,x^{2}}}{2d^{2}}\right)}{d}\right)}{b^{5}}-\frac{\mathrm{erf}(bx)e^{c}\left(\frac{e^{d\,x^{2}}b^{6}x^{4}}{2d}-\frac{2b^{2}\left(\frac{b^{4}x^{2}e^{d\,x^{2}}}{2d}-\frac{b^{4}e^{d\,x^{2}}}{2d^{2}}\right)}{d}\right)}{b^{5}}+e^{c}\left(b^{2}\left(\frac{b^{3}x^{3}e^{\left(-1+\frac{d}{b^{2}}\right)b^{2}x^{2}}}{-2+\frac{2d}{b^{2}}}-3\left(bx\,e\right.\right.\right.}{}$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^5*erfc(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] (1/b^5*exp(c)*(1/2*exp(d*x^2)*b^6*x^4/d-2/d*b^2*(1/2/d*b^4*x^2*exp(d*x^2)-1
/2/d^2*b^4*exp(d*x^2)))-erf(b*x)/b^5*exp(c)*(1/2*exp(d*x^2)*b^6*x^4/d-2/d*b
^2*(1/2/d*b^4*x^2*exp(d*x^2)-1/2/d^2*b^4*exp(d*x^2)))+1/Pi^(1/2)/b^5*exp(c)
*(1/d*b^2*(1/2/(-1+d/b^2)*b^3*x^3*exp((-1+d/b^2)*b^2*x^2)-3/2/(-1+d/b^2)*(1
/2/(-1+d/b^2)*b*x*exp((-1+d/b^2)*b^2*x^2)-1/4/(-1+d/b^2)*Pi^(1/2)/(1-d/b^2)
^(1/2)*erf((1-d/b^2)^(1/2)*b*x)))+1/d^3*b^6*Pi^(1/2)/(1-d/b^2)^(1/2)*erf((1
-d/b^2)^(1/2)*b*x)-2/d^2*b^4*(1/2/(-1+d/b^2)*b*x*exp((-1+d/b^2)*b^2*x^2)-1/
4/(-1+d/b^2)*Pi^(1/2)/(1-d/b^2)^(1/2)*erf((1-d/b^2)^(1/2)*b*x))))/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^5*erfc(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x^5*erfc(b*x)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.37, size = 356, normalized size = 1.26

$$\frac{\pi(8\,b^{5}-20\,b^{3}d+15\,bd^{2})\sqrt{b^{2}-d}\,\mathrm{erf}\left(\sqrt{b^{2}-d}\,x\right)e^{c}-2\,\sqrt{\pi}\,(2\,(b^{5}d^{2}-2\,b^{3}d^{3}+bd^{4})x^{3}-(4\,b^{5}d-11\,b^{3}d^{2}+7\,bd^{3})x)e^{(-b^{2}x^{2}+dx^{2}+c)}+4\,(\pi(b^{6}d^{2}-3\,b^{4}d^{3}+3\,b^{2}d^{4}-d^{5})x^{4}-2\,\pi(b^{6}d-3\,b^{4}d^{2}+3\,b^{2}d^{3}-d^{4})x^{2}+2\,\pi(b^{6}-3\,b^{4}d+3\,b^{2}d^{2}-d^{3})-(\pi(b^{6}d^{2}-3\,b^{4}d^{3}+3\,b^{2}d^{4}-d^{5})x^{4}-2\,\pi(b^{6}d-3\,b^{4}d^{2}+3\,b^{2}d^{3}-d^{4})x^{2}+2\,\pi(b^{6}-3\,b^{4}d+3\,b^{2}d^{2}-d^{3}))\,\mathrm{erf}\,(bx))e^{(dx^{2}+c)}}{8\,\pi(b^{6}d^{3}-3\,b^{4}d^{4}+3\,b^{2}d^{5}-d^{6})}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^5*erfc(b*x),x, algorithm="fricas")
```

```
[Out] 1/8*(pi*(8*b^5 - 20*b^3*d + 15*b*d^2)*sqrt(b^2 - d)*erf(sqrt(b^2 - d)*x)*e^
c - 2*sqrt(pi)*(2*(b^5*d^2 - 2*b^3*d^3 + b*d^4)*x^3 - (4*b^5*d - 11*b^3*d^2
 + 7*b*d^3)*x)*e^(-b^2*x^2 + d*x^2 + c) + 4*(pi*(b^6*d^2 - 3*b^4*d^3 + 3*b^
2*d^4 - d^5)*x^4 - 2*pi*(b^6*d - 3*b^4*d^2 + 3*b^2*d^3 - d^4)*x^2 + 2*pi*(b
^6 - 3*b^4*d + 3*b^2*d^2 - d^3) - (pi*(b^6*d^2 - 3*b^4*d^3 + 3*b^2*d^4 - d^
5)*x^4 - 2*pi*(b^6*d - 3*b^4*d^2 + 3*b^2*d^3 - d^4)*x^2 + 2*pi*(b^6 - 3*b^4
*d + 3*b^2*d^2 - d^3))*erf(b*x))*e^(d*x^2 + c))/(pi*(b^6*d^3 - 3*b^4*d^4 +
3*b^2*d^5 - d^6))
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int x^{5}e^{dx^{2}}\operatorname{erfc}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**5*erfc(b*x),x)
```

```
[Out] exp(c)*Integral(x**5*exp(d*x**2)*erfc(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^5*erfc(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^5*erfc(b*x)*e^(d*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.00

$$\int x^5\,{\mathrm{e}}^{d\,x^2+c}\,\mathrm{erfc}\left(b\,x\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*exp(c + d*x^2)*erfc(b*x),x)
```

```
[Out] int(x^5*exp(c + d*x^2)*erfc(b*x), x)
```

3.157 $\int e^{c+dx^2} x^3 \textbf{Erfc}(bx)\,dx$

Optimal. Leaf size=155

$$-\frac{be^{c-(b^2-d)x^2}x}{2(b^2-d)d\sqrt{\pi}}-\frac{be^c\text{Erf}\left(\sqrt{b^2-d}\,x\right)}{2\sqrt{b^2-d}\,d^2}+\frac{be^c\text{Erf}\left(\sqrt{b^2-d}\,x\right)}{4(b^2-d)^{3/2}d}-\frac{e^{c+dx^2}\text{Erfc}(bx)}{2d^2}+\frac{e^{c+dx^2}x^2\text{Erfc}(bx)}{2d}$$

```
[Out] 1/4*b*exp(c)*erf(x*(b^2-d)^(1/2))/(b^2-d)^(3/2)/d-1/2*exp(d*x^2+c)*erfc(b*x
)/d^2+1/2*exp(d*x^2+c)*x^2*erfc(b*x)/d-1/2*b*exp(c)*erf(x*(b^2-d)^(1/2))/d^
2/(b^2-d)^(1/2)-1/2*b*exp(c-(b^2-d)*x^2)*x/(b^2-d)/d/Pi^(1/2)
```

Rubi [A]
time = 0.10, antiderivative size = 155, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {6521, 6518, 2236, 2243}

$$-\frac{be^c\text{Erf}\left(x\sqrt{b^2-d}\right)}{2d^2\sqrt{b^2-d}}+\frac{be^c\text{Erf}\left(x\sqrt{b^2-d}\right)}{4d(b^2-d)^{3/2}}-\frac{bxe^{c-x^2(b^2-d)}}{2\sqrt{\pi}\,d(b^2-d)}-\frac{\text{Erfc}(bx)e^{c+dx^2}}{2d^2}+\frac{x^2\text{Erfc}(bx)e^{c+dx^2}}{2d}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + d*x^2)*x^3*Erfc[b*x],x]
```

```
[Out] -1/2*(b*E^(c - (b^2 - d)*x^2)*x)/((b^2 - d)*d*Sqrt[Pi]) - (b*E^c*Erf[Sqrt[b
^2 - d]*x])/(2*Sqrt[b^2 - d]*d^2) + (b*E^c*Erf[Sqrt[b^2 - d]*x])/(4*(b^2 -
d)^(3/2)*d) - (E^(c + d*x^2)*Erfc[b*x])/(2*d^2) + (E^(c + d*x^2)*x^2*Erfc[b
*x])/(2*d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
```

```
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{c+dx^2}x^3\mathrm{erfc}(bx)\,dx &= \frac{e^{c+dx^2}x^2\mathrm{erfc}(bx)}{2d}-\frac{\int e^{c+dx^2}x\mathrm{erfc}(bx)\,dx}{d}+\frac{b\int e^{c-(b^2-d)x^2}x^2\,dx}{d\sqrt{\pi}}\\ &=-\frac{be^{c-(b^2-d)x^2}x}{2(b^2-d)d\sqrt{\pi}}-\frac{e^{c+dx^2}\mathrm{erfc}(bx)}{2d^2}+\frac{e^{c+dx^2}x^2\mathrm{erfc}(bx)}{2d}-\frac{b\int e^{c-(b^2-d)x^2}\,dx}{d^2\sqrt{\pi}}+\frac{b\int e^{c-}}{2(b^2}\\ &=-\frac{be^{c-(b^2-d)x^2}x}{2(b^2-d)d\sqrt{\pi}}-\frac{be^c\mathrm{erf}\left(\sqrt{b^2-d}\,x\right)}{2\sqrt{b^2-d}\,d^2}+\frac{be^c\mathrm{erf}\left(\sqrt{b^2-d}\,x\right)}{4(b^2-d)^{3/2}d}-\frac{e^{c+dx^2}\mathrm{erfc}(bx)}{2d^2}+\frac{e}{}\end{aligned}$$

Mathematica [A]
time = 0.23, size = 99, normalized size = 0.64

$$\frac{e^c\left(\frac{2bde^{(-b^2+d)x^2}x}{(-b^2+d)\sqrt{\pi}}+2e^{dx^2}(-1+dx^2)\,\mathrm{Erfc}(bx)+\frac{(2b^3-3bd)\mathrm{Erfi}\left(\sqrt{-b^2+d}\,x\right)}{(-b^2+d)^{3/2}}\right)}{4d^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + d*x^2)*x^3*Erfc[b*x],x]
```

```
[Out] (E^c*((2*b*d*E^((-b^2 + d)*x^2)*x)/((-b^2 + d)*Sqrt[Pi]) + 2*E^(d*x^2)*(-1
+ d*x^2)*Erfc[b*x] + ((2*b^3 - 3*b*d)*Erfi[Sqrt[-b^2 + d]*x])/(-b^2 + d)^(3
/2)))/(4*d^2)
```

Maple [A]
time = 0.50, size = 206, normalized size = 1.33

method	result

default	$\frac{\frac{e^{c}\left(\frac{b^{4}x^{2}e^{d\,x^{2}}}{2d}-\frac{b^{4}e^{d\,x^{2}}}{2d^{2}}\right)}{b^{3}}-\frac{\operatorname{erf}(bx)e^{c}\left(\frac{b^{4}x^{2}e^{d\,x^{2}}}{2d}-\frac{b^{4}e^{d\,x^{2}}}{2d^{2}}\right)}{b^{3}}+\frac{e^{c}\left(\frac{b^{2}\left(\frac{bx\,e^{\left(-1+\frac{d}{b^{2}}\right)b^{2}x^{2}}}{-2+\frac{2d}{b^{2}}}-\frac{\sqrt{\pi}\,\operatorname{erf}\left(\sqrt{1-\frac{d}{b^{2}}}\,bx\right)}{4\left(-1+\frac{d}{b^{2}}\right)\sqrt{1-\frac{d}{b^{2}}}}\right)}{d}-\frac{b^{4}\sqrt{\pi}\,\operatorname{erf}\left(\cdots\right.}{2d^{2}\sqrt{\cdots}}\right.}{\sqrt{\pi}\,b^{3}}}{b}$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^3*erfc(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] (1/b^3*exp(c)*(1/2/d*b^4*x^2*exp(d*x^2)-1/2/d^2*b^4*exp(d*x^2))-erf(b*x)/b^
3*exp(c)*(1/2/d*b^4*x^2*exp(d*x^2)-1/2/d^2*b^4*exp(d*x^2))+1/Pi^(1/2)/b^3*e
xp(c)*(1/d*b^2*(1/2/(-1+d/b^2)*b*x*exp((-1+d/b^2)*b^2*x^2)-1/4/(-1+d/b^2)*P
i^(1/2)/(1-d/b^2)^(1/2)*erf((1-d/b^2)^(1/2)*b*x))-1/2/d^2*b^4*Pi^(1/2)/(1-d
/b^2)^(1/2)*erf((1-d/b^2)^(1/2)*b*x)))/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erfc(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x^3*erfc(b*x)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.34, size = 190, normalized size = 1.23

$$-\frac{\pi(2\,b^{3}-3\,bd)\sqrt{b^{2}-d}\,\operatorname{erf}\left(\sqrt{b^{2}-d}\,x\right)e^{c}+2\,\sqrt{\pi}\,(b^{3}d-bd^{2})xe^{(-b^{2}x^{2}+dx^{2}+c)}-2\,(\pi(b^{4}d-2\,b^{2}d^{2}+d^{3})x^{2}-\pi(b^{4}-2\,b^{2}d+d^{2})-(\pi(b^{4}d-2\,b^{2}d^{2}+d^{3})x^{2}-\pi(b^{4}-2\,b^{2}d+d^{2}))\operatorname{erf}(bx))e^{(dx^{2}+c)}}{4\,\pi(b^{4}d^{2}-2\,b^{2}d^{3}+d^{4})}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erfc(b*x),x, algorithm="fricas")
```

```
[Out] -1/4*(pi*(2*b^3 - 3*b*d)*sqrt(b^2 - d)*erf(sqrt(b^2 - d)*x)*e^c + 2*sqrt(pi
)*(b^3*d - b*d^2)*x*e^(-b^2*x^2 + d*x^2 + c) - 2*(pi*(b^4*d - 2*b^2*d^2 + d
^3)*x^2 - pi*(b^4 - 2*b^2*d + d^2) - (pi*(b^4*d - 2*b^2*d^2 + d^3)*x^2 - pi
*(b^4 - 2*b^2*d + d^2))*erf(b*x))*e^(d*x^2 + c))/(pi*(b^4*d^2 - 2*b^2*d^3 +
 d^4))
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int x^{3}e^{dx^{2}}\operatorname{erfc}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**3*erfc(b*x),x)
```

```
[Out] exp(c)*Integral(x**3*exp(d*x**2)*erfc(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erfc(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^3*erfc(b*x)*e^(d*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^{3}\,\mathrm{e}^{d\,x^{2}+c}\,\mathrm{erfc}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*exp(c + d*x^2)*erfc(b*x),x)
```

```
[Out] int(x^3*exp(c + d*x^2)*erfc(b*x), x)
```

3.158 $\int e^{c+dx^2} x\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=57

$$\frac{be^c\text{Erf}\left(\sqrt{b^2-d}\,x\right)}{2\sqrt{b^2-d}\,d}+\frac{e^{c+dx^2}\text{Erfc}(bx)}{2d}$$

```
[Out] 1/2*exp(d*x^2+c)*erfc(b*x)/d+1/2*b*exp(c)*erf(x*(b^2-d)^(1/2))/d/(b^2-d)^(1
/2)
```

Rubi [A]
time = 0.03, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {6518, 2236}

$$\frac{be^c\text{Erf}\left(x\sqrt{b^2-d}\right)}{2d\sqrt{b^2-d}}+\frac{\text{Erfc}(bx)e^{c+dx^2}}{2d}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + d*x^2)*x*Erfc[b*x],x]
```

```
[Out] (b*E^c*Erf[Sqrt[b^2 - d]*x])/(2*Sqrt[b^2 - d]*d) + (E^(c + d*x^2)*Erfc[b*x]
)/(2*d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\begin{aligned}\int e^{c+dx^2}x\text{erfc}(bx)\,dx &= \frac{e^{c+dx^2}\text{erfc}(bx)}{2d}+\frac{b\int e^{c-(b^2-d)x^2}\,dx}{d\sqrt{\pi}}\\ &= \frac{be^c\text{erf}\left(\sqrt{b^2-d}\,x\right)}{2\sqrt{b^2-d}\,d}+\frac{e^{c+dx^2}\text{erfc}(bx)}{2d}\end{aligned}$$

Mathematica [A]
time = 0.03, size = 50, normalized size = 0.88

$$\frac{e^c\left(e^{dx^2}\text{Erfc}(bx)+\frac{b\text{Erfi}\left(\sqrt{-b^2+d}\,x\right)}{\sqrt{-b^2+d}}\right)}{2d}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + d*x^2)*x*Erfc[b*x],x]
```

```
[Out] (E^c*(E^(d*x^2)*Erfc[b*x] + (b*Erfi[Sqrt[-b^2 + d]*x])/Sqrt[-b^2 + d]))/(2*
d)
```

Maple [A]
time = 0.44, size = 92, normalized size = 1.61

method	result	size
default	$\frac{\frac{b\,e^{\frac{b^2 d\,x^2+b^2 c}{b^2}}}{2d}-\frac{\mathrm{erf}(bx)\,b\,e^{\frac{b^2 d\,x^2+b^2 c}{b^2}}}{2d}+\frac{b\,e^{c}\,\mathrm{erf}\left(\sqrt{1-\frac{d}{b^2}}\,bx\right)}{2d\sqrt{1-\frac{d}{b^2}}}}{b}$	92

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x*erfc(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] (1/2*b*exp((b^2*d*x^2+b^2*c)/b^2)/d-1/2*erf(b*x)*b*exp((b^2*d*x^2+b^2*c)/b^
2)/d+1/2*b/d*exp(c)/(1-d/b^2)^(1/2)*erf((1-d/b^2)^(1/2)*b*x))/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erfc(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x*erfc(b*x)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.36, size = 70, normalized size = 1.23

$$\frac{\sqrt{b^2-d}\,b\,\mathrm{erf}\left(\sqrt{b^2-d}\,x\right)e^c+\left(b^2-\left(b^2-d\right)\mathrm{erf}\left(bx\right)-d\right)e^{\left(dx^2+c\right)}}{2\left(b^2d-d^2\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erfc(b*x),x, algorithm="fricas")
```

```
[Out] 1/2*(sqrt(b^2 - d)*b*erf(sqrt(b^2 - d)*x)*e^c + (b^2 - (b^2 - d)*erf(b*x) -
 d)*e^(d*x^2 + c))/(b^2*d - d^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int xe^{dx^{2}}\operatorname{erfc}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x*erfc(b*x),x)
```

```
[Out] exp(c)*Integral(x*exp(d*x**2)*erfc(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erfc(b*x),x, algorithm="giac")
```

```
[Out] integrate(x*erfc(b*x)*e^(d*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int x\,\mathrm{e}^{d\,x^2+c}\,\mathrm{erfc}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*exp(c + d*x^2)*erfc(b*x),x)
```

```
[Out] int(x*exp(c + d*x^2)*erfc(b*x), x)
```

3.159 $\int \frac{e^{c+dx^2}\mathbf{Erfc}(bx)}{x}\,dx$

Optimal. Leaf size=20

$$\operatorname{Int}\left(\frac{e^{c+dx^2}\operatorname{Erfc}(bx)}{x},x\right)$$

```
[Out] Unintegrable(exp(d*x^2+c)*erfc(b*x)/x,x)
```

Rubi [A]
time = 0.02, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\operatorname{Erfc}(bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfc[b*x])/x,x]
```

```
[Out] Defer[Int][(E^(c + d*x^2)*Erfc[b*x])/x, x]
```

Rubi steps

$$\int \frac{e^{c+dx^2}\operatorname{erfc}(bx)}{x}\,dx = \int \frac{e^{c+dx^2}\operatorname{erfc}(bx)}{x}\,dx$$

Mathematica [A]
time = 0.36, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\operatorname{Erfc}(bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfc[b*x])/x,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erfc[b*x])/x, x]
```

Maple [A]
time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\operatorname{erfc}(bx)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfc(b*x)/x,x)
```

```
[Out] int(exp(d*x^2+c)*erfc(b*x)/x,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x)/x,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)*e^(d*x^2 + c)/x, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x)/x,x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x) - 1)*e^(d*x^2 + c)/x, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int\frac{e^{dx^{2}}\operatorname{erfc}\left(bx\right)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfc(b*x)/x,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erfc(b*x)/x, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x)/x,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(d*x^2 + c)/x, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{e^{d\,x^2+c}\,\mathrm{erfc}(b\,x)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + d*x^2)*erfc(b*x))/x,x)
```

```
[Out] int((exp(c + d*x^2)*erfc(b*x))/x, x)
```

3.160 $\int \frac{e^{c+dx^2}\mathbf{Erfc}(bx)}{x^3}\,dx$

Optimal. Leaf size=99

$$\frac{be^{c-(b^2-d)x^2}}{\sqrt{\pi}\,x}+b\sqrt{b^2-d}\,e^c\mathrm{Erf}\left(\sqrt{b^2-d}\,x\right)-\frac{e^{c+dx^2}\mathrm{Erfc}(bx)}{2x^2}+d\mathrm{Int}\left(\frac{e^{c+dx^2}\mathrm{Erfc}(bx)}{x},x\right)$$

```
[Out] -1/2*exp(d*x^2+c)*erfc(b*x)/x^2+b*exp(c)*erf(x*(b^2-d)^(1/2))*(b^2-d)^(1/2)
+b*exp(c-(b^2-d)*x^2)/x/Pi^(1/2)+d*Unintegrable(exp(d*x^2+c)*erfc(b*x)/x,x)
```

Rubi [A]
time = 0.09, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}}=0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\mathrm{Erfc}(bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfc[b*x])/x^3,x]
```

```
[Out] (b*E^(c - (b^2 - d)*x^2))/(Sqrt[Pi]*x) + b*Sqrt[b^2 - d]*E^c*Erf[Sqrt[b^2 -
 d]*x] - (E^(c + d*x^2)*Erfc[b*x])/(2*x^2) + d*Defer[Int][(E^(c + d*x^2)*Er
fc[b*x])/x, x]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+dx^2}\mathrm{erfc}(bx)}{x^3}\,dx &= -\frac{e^{c+dx^2}\mathrm{erfc}(bx)}{2x^2}+d\int \frac{e^{c+dx^2}\mathrm{erfc}(bx)}{x}\,dx-\frac{b\int \frac{e^{c-\left(b^2-d\right)x^2}}{x^2}\,dx}{\sqrt{\pi}}\\ &= \frac{be^{c-(b^2-d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\mathrm{erfc}(bx)}{2x^2}+d\int \frac{e^{c+dx^2}\mathrm{erfc}(bx)}{x}\,dx+\frac{(2b(b^2-d))\int e^{c+(-b^2+d)x^2}\,d}{\sqrt{\pi}}\\ &= \frac{be^{c-(b^2-d)x^2}}{\sqrt{\pi}\,x}+b\sqrt{b^2-d}\,e^c\mathrm{erf}\left(\sqrt{b^2-d}\,x\right)-\frac{e^{c+dx^2}\mathrm{erfc}(bx)}{2x^2}+d\int \frac{e^{c+dx^2}\mathrm{erfc}(bx)}{x}\,dx\end{aligned}$$

Mathematica [A]
time = 0.45, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\mathrm{Erfc}(bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfc[b*x])/x^3,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erfc[b*x])/x^3, x]
```

Maple [A]
time = 0.24, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\mathrm{erfc}(bx)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfc(b*x)/x^3,x)
```

```
[Out] int(exp(d*x^2+c)*erfc(b*x)/x^3,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x)/x^3,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)*e^(d*x^2 + c)/x^3, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x)/x^3,x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x) - 1)*e^(d*x^2 + c)/x^3, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^{2}}\operatorname{erfc}{\left(bx \right)}}{x^{3}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfc(b*x)/x**3,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erfc(b*x)/x**3, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x)/x^3,x, algorithm="giac")
[Out] integrate(erfc(b*x)*e^(d*x^2 + c)/x^3, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{d\,x^2+c}\,\mathrm{erfc}(b\,x)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + d*x^2)*erfc(b*x))/x^3,x)
[Out] int((exp(c + d*x^2)*erfc(b*x))/x^3, x)
```

3.161 $\int \frac{e^{c+dx^2}\textbf{Erfc}(bx)}{x^5}\,dx$

Optimal. Leaf size=231

$$\frac{be^{c-(b^2-d)x^2}}{6\sqrt{\pi}\,x^3}-\frac{b(b^2-d)\,e^{c-(b^2-d)x^2}}{3\sqrt{\pi}\,x}+\frac{bde^{c-(b^2-d)x^2}}{2\sqrt{\pi}\,x}-\frac{1}{3}b\left(b^2-d\right)^{3/2}e^c\mathrm{Erf}\left(\sqrt{b^2-d}\,x\right)+\frac{1}{2}b\sqrt{b^2-d}\,de^c\mathrm{Erf}\left(\sqrt{b^2\right.$$

```
[Out] -1/3*b*(b^2-d)^(3/2)*exp(c)*erf(x*(b^2-d)^(1/2))-1/4*exp(d*x^2+c)*erfc(b*x)
/x^4-1/4*d*exp(d*x^2+c)*erfc(b*x)/x^2+1/2*b*d*exp(c)*erf(x*(b^2-d)^(1/2))*(
b^2-d)^(1/2)+1/6*b*exp(c-(b^2-d)*x^2)/x^3/Pi^(1/2)-1/3*b*(b^2-d)*exp(c-(b^2
-d)*x^2)/x/Pi^(1/2)+1/2*b*d*exp(c-(b^2-d)*x^2)/x/Pi^(1/2)+1/2*d^2*Unintegra
ble(exp(d*x^2+c)*erfc(b*x)/x,x)
```

Rubi [A]
time = 0.21, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\mathrm{Erfc}(bx)}{x^5}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfc[b*x])/x^5,x]
```

```
[Out] (b*E^(c - (b^2 - d)*x^2))/(6*Sqrt[Pi]*x^3) - (b*(b^2 - d)*E^(c - (b^2 - d)*
x^2))/(3*Sqrt[Pi]*x) + (b*d*E^(c - (b^2 - d)*x^2))/(2*Sqrt[Pi]*x) - (b*(b^2
 - d)^(3/2)*E^c*Erf[Sqrt[b^2 - d]*x])/3 + (b*Sqrt[b^2 - d]*d*E^c*Erf[Sqrt[b
^2 - d]*x])/2 - (E^(c + d*x^2)*Erfc[b*x])/(4*x^4) - (d*E^(c + d*x^2)*Erfc[b
*x])/(4*x^2) + (d^2*Defer[Int][(E^(c + d*x^2)*Erfc[b*x])/x, x])/2
```

Rubi steps

$$\begin{aligned}
\int \frac{e^{c+dx^2}\mathrm{erfc}(bx)}{x^5}\,dx &= -\frac{e^{c+dx^2}\mathrm{erfc}(bx)}{4x^4}+\frac{1}{2}d\int \frac{e^{c+dx^2}\mathrm{erfc}(bx)}{x^3}\,dx-\frac{b\int \frac{e^{c-\left(b^2-d\right)x^2}}{x^4}\,dx}{2\sqrt{\pi}}\\
&= \frac{be^{c-(b^2-d)x^2}}{6\sqrt{\pi}\,x^3}-\frac{e^{c+dx^2}\mathrm{erfc}(bx)}{4x^4}-\frac{de^{c+dx^2}\mathrm{erfc}(bx)}{4x^2}+\frac{1}{2}d^2\int \frac{e^{c+dx^2}\mathrm{erfc}(bx)}{x}\,dx+\frac{(b(b^2-\right.}{}\\
&= \frac{be^{c-(b^2-d)x^2}}{6\sqrt{\pi}\,x^3}-\frac{b(b^2-d)\,e^{c-(b^2-d)x^2}}{3\sqrt{\pi}\,x}+\frac{bde^{c-(b^2-d)x^2}}{2\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\mathrm{erfc}(bx)}{4x^4}-\frac{de^{c+dx^2}\mathrm{erfc}(bx}{4x^2}\\
&= \frac{be^{c-(b^2-d)x^2}}{6\sqrt{\pi}\,x^3}-\frac{b(b^2-d)\,e^{c-(b^2-d)x^2}}{3\sqrt{\pi}\,x}+\frac{bde^{c-(b^2-d)x^2}}{2\sqrt{\pi}\,x}-\frac{1}{3}b\left(b^2-d\right)^{3/2}e^c\mathrm{erf}\left(\sqrt{b^2-d}\,x\right)
\end{aligned}$$

Mathematica [A]
time = 0.53, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\mathrm{Erfc}(bx)}{x^5}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfc[b*x])/x^5,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erfc[b*x])/x^5, x]
```

Maple [A]
time = 0.23, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\mathrm{erfc}(bx)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfc(b*x)/x^5,x)
```

```
[Out] int(exp(d*x^2+c)*erfc(b*x)/x^5,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x)/x^5,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)*e^(d*x^2 + c)/x^5, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x)/x^5,x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x) - 1)*e^(d*x^2 + c)/x^5, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^c \int \frac{e^{dx^2}\,\mathrm{erfc}\,(bx)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfc(b*x)/x**5,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erfc(b*x)/x**5, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x)/x^5,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(d*x^2 + c)/x^5, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\,\mathrm{erfc}(b\,x)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + d*x^2)*erfc(b*x))/x^5,x)
```

```
[Out] int((exp(c + d*x^2)*erfc(b*x))/x^5, x)
```

3.162 $\int e^{c+dx^2} x^4 \mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=186

$$\frac{3be^{c-(b^2-d)x^2}}{4(b^2-d)d^2\sqrt{\pi}}-\frac{be^{c-(b^2-d)x^2}}{2(b^2-d)^2d\sqrt{\pi}}-\frac{be^{c-(b^2-d)x^2}x^2}{2(b^2-d)d\sqrt{\pi}}-\frac{3e^{c+dx^2}x\text{Erfc}(bx)}{4d^2}+\frac{e^{c+dx^2}x^3\text{Erfc}(bx)}{2d}+\frac{3\text{Int}\left(e^{c+dx^2}\text{E}\right.}{4d^2}$$

```
[Out] -3/4*exp(d*x^2+c)*x*erfc(b*x)/d^2+1/2*exp(d*x^2+c)*x^3*erfc(b*x)/d+3/4*b*ex
p(c-(b^2-d)*x^2)/(b^2-d)/d^2/Pi^(1/2)-1/2*b*exp(c-(b^2-d)*x^2)/(b^2-d)^2/d/
Pi^(1/2)-1/2*b*exp(c-(b^2-d)*x^2)*x^2/(b^2-d)/d/Pi^(1/2)+3/4*Unintegrable(e
xp(d*x^2+c)*erfc(b*x),x)/d^2
```

Rubi [A]
time = 0.16, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int e^{c+dx^2} x^4 \text{Erfc}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*x^4*Erfc[b*x],x]
```

```
[Out] (3*b*E^(c - (b^2 - d)*x^2))/(4*(b^2 - d)*d^2*Sqrt[Pi]) - (b*E^(c - (b^2 - d
)*x^2))/(2*(b^2 - d)^2*d*Sqrt[Pi]) - (b*E^(c - (b^2 - d)*x^2)*x^2)/(2*(b^2
- d)*d*Sqrt[Pi]) - (3*E^(c + d*x^2)*x*Erfc[b*x])/(4*d^2) + (E^(c + d*x^2)*x
^3*Erfc[b*x])/(2*d) + (3*Defer[Int][E^(c + d*x^2)*Erfc[b*x], x])/(4*d^2)
```

Rubi steps

$$\begin{aligned}\int e^{c+dx^2} x^4 \text{erfc}(bx)\,dx &= \frac{e^{c+dx^2}x^3\text{erfc}(bx)}{2d}-\frac{3\int e^{c+dx^2}x^2\text{erfc}(bx)\,dx}{2d}+\frac{b\int e^{c-(b^2-d)x^2}x^3\,dx}{d\sqrt{\pi}}\\ &=-\frac{be^{c-(b^2-d)x^2}x^2}{2(b^2-d)d\sqrt{\pi}}-\frac{3e^{c+dx^2}x\text{erfc}(bx)}{4d^2}+\frac{e^{c+dx^2}x^3\text{erfc}(bx)}{2d}+\frac{3\int e^{c+dx^2}\text{erfc}(bx)\,dx}{4d^2}\\ &=\frac{3be^{c-(b^2-d)x^2}}{4(b^2-d)d^2\sqrt{\pi}}-\frac{be^{c-(b^2-d)x^2}}{2(b^2-d)^2d\sqrt{\pi}}-\frac{be^{c-(b^2-d)x^2}x^2}{2(b^2-d)d\sqrt{\pi}}-\frac{3e^{c+dx^2}x\text{erfc}(bx)}{4d^2}+\frac{e^{c+}}{}\end{aligned}$$

Mathematica [A]
time = 0.58, size = 0, normalized size = 0.00

$$\int e^{c+dx^2} x^4 \text{Erfc}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*x^4*Erfc[b*x],x]
```

```
[Out] Integrate[E^(c + d*x^2)*x^4*Erfc[b*x], x]
```

Maple [A]
time = 0.07, size = 0, normalized size = 0.00

$$\int e^{d\,x^{2}+c} x^{4} \operatorname{erfc}(b x)\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^4*erfc(b*x),x)
```

```
[Out] int(exp(d*x^2+c)*x^4*erfc(b*x),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erfc(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x^4*erfc(b*x)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erfc(b*x),x, algorithm="fricas")
```

```
[Out] integral(-(x^4*erf(b*x) - x^4)*e^(d*x^2 + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c} \int x^{4} e^{d x^{2}} \operatorname{erfc}{\left(b x \right)}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**4*erfc(b*x),x)
```

```
[Out] exp(c)*Integral(x**4*exp(d*x**2)*erfc(b*x), x)
```

<u>Giac</u> [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erfc(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^4*erfc(b*x)*e^(d*x^2 + c), x)
```

<u>Mupad</u> [**A**]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^4\,\mathrm{e}^{d\,x^2+c}\,\mathrm{erfc}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*exp(c + d*x^2)*erfc(b*x),x)
```

```
[Out] int(x^4*exp(c + d*x^2)*erfc(b*x), x)
```

3.163 $\int e^{c+dx^2}x^2\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=84

$$-\frac{be^{c-(b^2-d)x^2}}{2\left(b^2-d\right)d\sqrt{\pi}}+\frac{e^{c+dx^2}x\text{Erfc}(bx)}{2d}-\frac{\text{Int}\left(e^{c+dx^2}\text{Erfc}(bx),x\right)}{2d}$$

```
[Out] 1/2*exp(d*x^2+c)*x*erfc(b*x)/d-1/2*b*exp(c-(b^2-d)*x^2)/(b^2-d)/d/Pi^(1/2)-
1/2*Unintegrable(exp(d*x^2+c)*erfc(b*x),x)/d
```

Rubi [A]
time = 0.06, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.000, Rules used = {}

$$\int e^{c+dx^2}x^2\text{Erfc}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*x^2*Erfc[b*x],x]
```

```
[Out] -1/2*(b*E^(c - (b^2 - d)*x^2))/((b^2 - d)*d*Sqrt[Pi]) + (E^(c + d*x^2)*x*Er
fc[b*x])/(2*d) - Defer[Int][E^(c + d*x^2)*Erfc[b*x], x]/(2*d)
```

Rubi steps

$$\begin{aligned}\int e^{c+dx^2}x^2\text{erfc}(bx)\,dx&=\frac{e^{c+dx^2}x\text{erfc}(bx)}{2d}-\frac{\int e^{c+dx^2}\text{erfc}(bx)\,dx}{2d}+\frac{b\int e^{c-(b^2-d)x^2}x\,dx}{d\sqrt{\pi}}\\&=-\frac{be^{c-(b^2-d)x^2}}{2\left(b^2-d\right)d\sqrt{\pi}}+\frac{e^{c+dx^2}x\text{erfc}(bx)}{2d}-\frac{\int e^{c+dx^2}\text{erfc}(bx)\,dx}{2d}\end{aligned}$$

Mathematica [A]
time = 0.45, size = 0, normalized size = 0.00

$$\int e^{c+dx^2}x^2\text{Erfc}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*x^2*Erfc[b*x],x]
```

```
[Out] Integrate[E^(c + d*x^2)*x^2*Erfc[b*x], x]
```

Maple [A]
time = 0.14, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^2+c} x^2 \mathrm{erfc}(bx)\; dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^2*erfc(b*x),x)
[Out] int(exp(d*x^2+c)*x^2*erfc(b*x),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erfc(b*x),x, algorithm="maxima")
[Out] integrate(x^2*erfc(b*x)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erfc(b*x),x, algorithm="fricas")
[Out] integral(-(x^2*erf(b*x) - x^2)*e^(d*x^2 + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c} \int x^{2} e^{dx^{2}} \operatorname{erfc}{\left(bx \right)}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**2*erfc(b*x),x)
[Out] exp(c)*Integral(x**2*exp(d*x**2)*erfc(b*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erfc(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^2*erfc(b*x)*e^(d*x^2 + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^2\,\mathrm{e}^{d\,x^2+c}\,\mathrm{erfc}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*exp(c + d*x^2)*erfc(b*x),x)
```

```
[Out] int(x^2*exp(c + d*x^2)*erfc(b*x), x)
```

3.164 $\int e^{c+dx^2}\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=17

$$\operatorname{Int}\left(e^{c+dx^2}\operatorname{Erfc}(bx),x\right)$$

```
[Out] Unintegrable(exp(d*x^2+c)*erfc(b*x),x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int e^{c+dx^2}\operatorname{Erfc}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*Erfc[b*x],x]
[Out] Defer[Int][E^(c + d*x^2)*Erfc[b*x], x]
```

Rubi steps

$$\int e^{c+dx^2}\operatorname{erfc}(bx)\,dx = \int e^{c+dx^2}\operatorname{erfc}(bx)\,dx$$

Mathematica [A]
time = 0.02, size = 0, normalized size = 0.00

$$\int e^{c+dx^2}\operatorname{Erfc}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*Erfc[b*x],x]
[Out] Integrate[E^(c + d*x^2)*Erfc[b*x], x]
```

Maple [A]
time = 0.06, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^{2}+c}\operatorname{erfc}(bx)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfc(b*x),x)
[Out] int(exp(d*x^2+c)*erfc(b*x),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x),x, algorithm="maxima")
[Out] integrate(erfc(b*x)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x),x, algorithm="fricas")
[Out] integral(-(erf(b*x) - 1)*e^(d*x^2 + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int e^{dx^{2}}\operatorname{erfc}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfc(b*x),x)
[Out] exp(c)*Integral(exp(d*x**2)*erfc(b*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x),x, algorithm="giac")
[Out] integrate(erfc(b*x)*e^(d*x^2 + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.06

$$\int \mathrm{e}^{d\,x^2+c}\,\mathrm{erfc}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c + d*x^2)*erfc(b*x),x)
```

```
[Out] int(exp(c + d*x^2)*erfc(b*x), x)
```

3.165 $\int \frac{e^{c+dx^2}\mathbf{Erfc}(bx)}{x^2}\,dx$

Optimal. Leaf size=63

$$-\frac{e^{c+dx^2}\text{Erfc}(bx)}{x}-\frac{be^c\text{Ei}\left(-\left(\left(b^2-d\right)x^2\right)\right)}{\sqrt{\pi}}+2d\text{Int}\left(e^{c+dx^2}\text{Erfc}(bx),x\right)$$

```
[Out] -exp(d*x^2+c)*erfc(b*x)/x-b*exp(c)*Ei(-(b^2-d)*x^2)/Pi^(1/2)+2*d*Unintegrab
le(exp(d*x^2+c)*erfc(b*x),x)
```

Rubi [A]
time = 0.07, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\text{Erfc}(bx)}{x^2}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfc[b*x])/x^2,x]
```

```
[Out] -((E^(c + d*x^2)*Erfc[b*x])/x) - (b*E^c*ExpIntegralEi[-((b^2 - d)*x^2)])/Sq
rt[Pi] + 2*d*Defer[Int][E^(c + d*x^2)*Erfc[b*x], x]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+dx^2}\text{erfc}(bx)}{x^2}\,dx &= -\frac{e^{c+dx^2}\text{erfc}(bx)}{x}+(2d)\int e^{c+dx^2}\text{erfc}(bx)\,dx-\frac{(2b)\int \frac{e^{c-\left(b^2-d\right)x^2}}{x}\,dx}{\sqrt{\pi}}\\ &= -\frac{e^{c+dx^2}\text{erfc}(bx)}{x}-\frac{be^c\text{Ei}\left(-\left(b^2-d\right)x^2\right)}{\sqrt{\pi}}+(2d)\int e^{c+dx^2}\text{erfc}(bx)\,dx\end{aligned}$$

Mathematica [A]
time = 0.47, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\text{Erfc}(bx)}{x^2}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfc[b*x])/x^2,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erfc[b*x])/x^2, x]
```

Maple [A]
time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\mathrm{erfc}(bx)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfc(b*x)/x^2,x)
```

```
[Out] int(exp(d*x^2+c)*erfc(b*x)/x^2,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x)/x^2,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)*e^(d*x^2 + c)/x^2, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x)/x^2,x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x) - 1)*e^(d*x^2 + c)/x^2, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^{2}}\operatorname{erfc}{\left(bx \right)}}{x^{2}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfc(b*x)/x**2,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erfc(b*x)/x**2, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x)/x^2,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(d*x^2 + c)/x^2, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{e^{d\,x^2+c}\,\mathrm{erfc}(b\,x)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + d*x^2)*erfc(b*x))/x^2,x)
```

```
[Out] int((exp(c + d*x^2)*erfc(b*x))/x^2, x)
```

3.166 $\int \frac{e^{c+dx^2}\mathbf{Erfc}(bx)}{x^4}\,dx$

Optimal. Leaf size=155

$$\frac{be^{c-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2}-\frac{e^{c+dx^2}\text{Erfc}(bx)}{3x^3}-\frac{2de^{c+dx^2}\text{Erfc}(bx)}{3x}+\frac{b(b^2-d)\,e^c\text{Ei}(-((b^2-d)\,x^2))}{3\sqrt{\pi}}-\frac{2bde^c\text{Ei}(-((b^2-d)\,x^2))}{3\sqrt{\pi}}+$$

```
[Out] -1/3*exp(d*x^2+c)*erfc(b*x)/x^3-2/3*d*exp(d*x^2+c)*erfc(b*x)/x+1/3*b*exp(c-
(b^2-d)*x^2)/x^2/Pi^(1/2)+1/3*b*(b^2-d)*exp(c)*Ei(-(b^2-d)*x^2)/Pi^(1/2)-2/
3*b*d*exp(c)*Ei(-(b^2-d)*x^2)/Pi^(1/2)+4/3*d^2*Unintegrable(exp(d*x^2+c)*er
fc(b*x),x)
```

Rubi [A]
time = 0.17, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\text{Erfc}(bx)}{x^4}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfc[b*x])/x^4,x]
```

```
[Out] (b*E^(c - (b^2 - d)*x^2))/(3*Sqrt[Pi]*x^2) - (E^(c + d*x^2)*Erfc[b*x])/(3*x
^3) - (2*d*E^(c + d*x^2)*Erfc[b*x])/(3*x) + (b*(b^2 - d)*E^c*ExpIntegralEi[
-((b^2 - d)*x^2)])/(3*Sqrt[Pi]) - (2*b*d*E^c*ExpIntegralEi[-((b^2 - d)*x^2)
])/(3*Sqrt[Pi]) + (4*d^2*Defer[Int][E^(c + d*x^2)*Erfc[b*x], x])/3
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+dx^2}\text{erfc}(bx)}{x^4}\,dx &= -\frac{e^{c+dx^2}\text{erfc}(bx)}{3x^3}+\frac{1}{3}(2d)\int \frac{e^{c+dx^2}\text{erfc}(bx)}{x^2}\,dx-\frac{(2b)\int \frac{e^{c-(b^2-d)x^2}}{x^3}\,dx}{3\sqrt{\pi}}\\ &= \frac{be^{c-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2}-\frac{e^{c+dx^2}\text{erfc}(bx)}{3x^3}-\frac{2de^{c+dx^2}\text{erfc}(bx)}{3x}+\frac{1}{3}\left(4d^2\right)\int e^{c+dx^2}\text{erfc}(bx)\,dx+\frac{(2\\ &= \frac{be^{c-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2}-\frac{e^{c+dx^2}\text{erfc}(bx)}{3x^3}-\frac{2de^{c+dx^2}\text{erfc}(bx)}{3x}+\frac{b(b^2-d)\,e^c\text{Ei}(-(b^2-d)\,x^2)}{3\sqrt{\pi}}-\frac{2\end{aligned}$$

Mathematica [A]
time = 0.59, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\text{Erfc}(bx)}{x^4}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfc[b*x])/x^4,x]
[Out] Integrate[(E^(c + d*x^2)*Erfc[b*x])/x^4, x]
```

Maple [A]
time = 0.16, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\mathrm{erfc}(bx)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfc(b*x)/x^4,x)
[Out] int(exp(d*x^2+c)*erfc(b*x)/x^4,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x)/x^4,x, algorithm="maxima")
[Out] integrate(erfc(b*x)*e^(d*x^2 + c)/x^4, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x)/x^4,x, algorithm="fricas")
[Out] integral(-(erf(b*x) - 1)*e^(d*x^2 + c)/x^4, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^{2}}\operatorname{erfc}{\left(bx \right)}}{x^{4}}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfc(b*x)/x**4,x)
[Out] exp(c)*Integral(exp(d*x**2)*erfc(b*x)/x**4, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x)/x^4,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(d*x^2 + c)/x^4, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{d\,x^2+c}\,\mathrm{erfc}(b\,x)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + d*x^2)*erfc(b*x))/x^4,x)
```

```
[Out] int((exp(c + d*x^2)*erfc(b*x))/x^4, x)
```

3.167 $\int e^{c+b^2x^2} x^5 \mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=118

$$\frac{2e^cx}{b^5\sqrt{\pi}}-\frac{2e^cx^3}{3b^3\sqrt{\pi}}+\frac{e^cx^5}{5b\sqrt{\pi}}+\frac{e^{c+b^2x^2}\mathrm{Erfc}(bx)}{b^6}-\frac{e^{c+b^2x^2}x^2\mathrm{Erfc}(bx)}{b^4}+\frac{e^{c+b^2x^2}x^4\mathrm{Erfc}(bx)}{2b^2}$$

```
[Out] exp(b^2*x^2+c)*erfc(b*x)/b^6-exp(b^2*x^2+c)*x^2*erfc(b*x)/b^4+1/2*exp(b^2*x
^2+c)*x^4*erfc(b*x)/b^2+2*exp(c)*x/b^5/Pi^(1/2)-2/3*exp(c)*x^3/b^3/Pi^(1/2)
+1/5*exp(c)*x^5/b/Pi^(1/2)
```

Rubi [A]
time = 0.08, antiderivative size = 118, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.263, Rules used = {6521, 6518, 8, 12, 30}

$$\frac{2e^cx}{\sqrt{\pi}\,b^5}-\frac{2e^cx^3}{3\sqrt{\pi}\,b^3}+\frac{x^4e^{b^2x^2+c}\mathrm{Erfc}(bx)}{2b^2}+\frac{e^{b^2x^2+c}\mathrm{Erfc}(bx)}{b^6}-\frac{x^2e^{b^2x^2+c}\mathrm{Erfc}(bx)}{b^4}+\frac{e^cx^5}{5\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*x^5*Erfc[b*x],x]
```

```
[Out] (2*E^c*x)/(b^5*Sqrt[Pi]) - (2*E^c*x^3)/(3*b^3*Sqrt[Pi]) + (E^c*x^5)/(5*b*Sq
rt[Pi]) + (E^(c + b^2*x^2)*Erfc[b*x])/b^6 - (E^(c + b^2*x^2)*x^2*Erfc[b*x])
/b^4 + (E^(c + b^2*x^2)*x^4*Erfc[b*x])/(2*b^2)
```

Rule 8

```
Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int e^{c+b^2x^2}x^5\operatorname{erfc}(bx)\,dx &= \frac{e^{c+b^2x^2}x^4\operatorname{erfc}(bx)}{2b^2} - \frac{2\int e^{c+b^2x^2}x^3\operatorname{erfc}(bx)\,dx}{b^2} + \frac{\int e^cx^4\,dx}{b\sqrt{\pi}} \\
&= -\frac{e^{c+b^2x^2}x^2\operatorname{erfc}(bx)}{b^4} + \frac{e^{c+b^2x^2}x^4\operatorname{erfc}(bx)}{2b^2} + \frac{2\int e^{c+b^2x^2}x\operatorname{erfc}(bx)\,dx}{b^4} - \frac{2\int e^cx^2\,dx}{b^3\sqrt{\pi}} + \\
&= \frac{e^cx^5}{5b\sqrt{\pi}} + \frac{e^{c+b^2x^2}\operatorname{erfc}(bx)}{b^6} - \frac{e^{c+b^2x^2}x^2\operatorname{erfc}(bx)}{b^4} + \frac{e^{c+b^2x^2}x^4\operatorname{erfc}(bx)}{2b^2} + \frac{2\int e^c\,dx}{b^5\sqrt{\pi}} - \\
&= \frac{2e^cx}{b^5\sqrt{\pi}} - \frac{2e^cx^3}{3b^3\sqrt{\pi}} + \frac{e^cx^5}{5b\sqrt{\pi}} + \frac{e^{c+b^2x^2}\operatorname{erfc}(bx)}{b^6} - \frac{e^{c+b^2x^2}x^2\operatorname{erfc}(bx)}{b^4} + \frac{e^{c+b^2x^2}x^4\operatorname{erfc}}{2b^2}
\end{aligned}$$

Mathematica [A]
time = 0.03, size = 73, normalized size = 0.62

$$\frac{e^c\left(60bx - 20b^3x^3 + 6b^5x^5 + 15e^{b^2x^2}\sqrt{\pi}\left(2 - 2b^2x^2 + b^4x^4\right)\operatorname{Erfc}(bx)\right)}{30b^6\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*x^5*Erfc[b*x],x]
```

```
[Out] (E^c*(60*b*x - 20*b^3*x^3 + 6*b^5*x^5 + 15*E^(b^2*x^2)*Sqrt[Pi]*(2 - 2*b^2*
x^2 + b^4*x^4)*Erfc[b*x]))/(30*b^6*Sqrt[Pi])
```

Maple [A]
time = 0.26, size = 135, normalized size = 1.14

method	result	size
default	$\dfrac{\frac{e^{c}\left(\frac{e^{b^2x^2}b^4x^4}{2}-b^2x^2e^{b^2x^2}+e^{b^2x^2}\right)}{b^5}-\frac{\operatorname{erf}(bx)e^{c}\left(\frac{e^{b^2x^2}b^4x^4}{2}-b^2x^2e^{b^2x^2}+e^{b^2x^2}\right)}{b^5}+\frac{e^{c}\left(\frac{1}{5}b^5x^5-\frac{2}{3}b^3x^3+2bx\right)}{\sqrt{\pi}\,b^5}}{b}$	135

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*x^5*erfc(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] (1/b^5*exp(c)*(1/2*exp(b^2*x^2)*b^4*x^4-b^2*x^2*exp(b^2*x^2)+exp(b^2*x^2))-
erf(b*x)/b^5*exp(c)*(1/2*exp(b^2*x^2)*b^4*x^4-b^2*x^2*exp(b^2*x^2)+exp(b^2*
x^2))+1/Pi^(1/2)/b^5*exp(c)*(1/5*b^5*x^5-2/3*b^3*x^3+2*b*x))/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^5*erfc(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x^5*erfc(b*x)*e^(b^2*x^2 + c), x)
```

Fricas [A]
time = 0.37, size = 97, normalized size = 0.82

$$\frac{2\sqrt{\pi}\,(3\,b^5x^5 - 10\,b^3x^3 + 30\,bx)e^c + 15\,(2\,\pi + \pi b^4x^4 - 2\,\pi b^2x^2 - (2\,\pi + \pi b^4x^4 - 2\,\pi b^2x^2)\,\mathrm{erf}\,(bx))e^{(b^2x^2+c)}}{30\,\pi b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^5*erfc(b*x),x, algorithm="fricas")
```

```
[Out] 1/30*(2*sqrt(pi)*(3*b^5*x^5 - 10*b^3*x^3 + 30*b*x)*e^c + 15*(2*pi + pi*b^4*
x^4 - 2*pi*b^2*x^2 - (2*pi + pi*b^4*x^4 - 2*pi*b^2*x^2)*erf(b*x))*e^(b^2*x^
2 + c))/(pi*b^6)
```

Sympy [A]
time = 45.39, size = 126, normalized size = 1.07

$$\begin{cases} \frac{x^5e^c}{5\sqrt{\pi}\,b} + \frac{x^4e^ce^{b^2x^2}\,\mathrm{erfc}\,(bx)}{2b^2} - \frac{2x^3e^c}{3\sqrt{\pi}\,b^3} - \frac{x^2e^ce^{b^2x^2}\,\mathrm{erfc}\,(bx)}{b^4} + \frac{2xe^c}{\sqrt{\pi}\,b^5} + \frac{e^ce^{b^2x^2}\,\mathrm{erfc}\,(bx)}{b^6} & \text{for } b \neq 0 \\ \frac{x^6e^c}{6} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*x**5*erfc(b*x),x)
```

```
[Out] Piecewise((x**5*exp(c)/(5*sqrt(pi)*b) + x**4*exp(c)*exp(b**2*x**2)*erfc(b*x
)/(2*b**2) - 2*x**3*exp(c)/(3*sqrt(pi)*b**3) - x**2*exp(c)*exp(b**2*x**2)*e
rfc(b*x)/b**4 + 2*x*exp(c)/(sqrt(pi)*b**5) + exp(c)*exp(b**2*x**2)*erfc(b*x
)/b**6, Ne(b, 0)), (x**6*exp(c)/6, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^5*erfc(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^5*erfc(b*x)*e^(b^2*x^2 + c), x)
```

Mupad [B]
time = 0.31, size = 94, normalized size = 0.80

$$\frac{e^c \left(60\,b\,x-20\,b^3\,x^3+6\,b^5\,x^5+30\,\sqrt{\pi}\,e^{b^2\,x^2}\,\mathrm{erfc}(b\,x)-30\,b^2\,x^2\,\sqrt{\pi}\,e^{b^2\,x^2}\,\mathrm{erfc}(b\,x)+15\,b^4\,x^4\,\sqrt{\pi}\,e^{b^2\,x^2}\,\mathrm{erfc}(b\,x)\right)}{30\,b^6\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*exp(c + b^2*x^2)*erfc(b*x),x)
```

```
[Out] (exp(c)*(60*b*x - 20*b^3*x^3 + 6*b^5*x^5 + 30*pi^(1/2)*exp(b^2*x^2)*erfc(b*
x) - 30*b^2*x^2*pi^(1/2)*exp(b^2*x^2)*erfc(b*x) + 15*b^4*x^4*pi^(1/2)*exp(b
^2*x^2)*erfc(b*x)))/(30*b^6*pi^(1/2))
```

3.168 $\int e^{c+b^2x^2}x^3\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=80

$$-\frac{e^c x}{b^3\sqrt{\pi}}+\frac{e^c x^3}{3b\sqrt{\pi}}-\frac{e^{c+b^2x^2}\text{Erfc}(bx)}{2b^4}+\frac{e^{c+b^2x^2}x^2\text{Erfc}(bx)}{2b^2}$$

```
[Out] -1/2*exp(b^2*x^2+c)*erfc(b*x)/b^4+1/2*exp(b^2*x^2+c)*x^2*erfc(b*x)/b^2-exp(
c)*x/b^3/Pi^(1/2)+1/3*exp(c)*x^3/b/Pi^(1/2)
```

Rubi [A]

time = 0.05, antiderivative size = 80, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}=0.263$, Rules used = {6521, 6518, 8, 12, 30}

$$-\frac{e^c x}{\sqrt{\pi}\,b^3}+\frac{x^2e^{b^2x^2+c}\text{Erfc}(bx)}{2b^2}-\frac{e^{b^2x^2+c}\text{Erfc}(bx)}{2b^4}+\frac{e^c x^3}{3\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*x^3*Erfc[b*x],x]
```

```
[Out] -((E^c*x)/(b^3*Sqrt[Pi])) + (E^c*x^3)/(3*b*Sqrt[Pi]) - (E^(c + b^2*x^2)*Erf
c[b*x])/(2*b^4) + (E^(c + b^2*x^2)*x^2*Erfc[b*x])/(2*b^2)
```

Rule 8

```
Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{c+b^2x^2}x^3\mathrm{erfc}(bx)\,dx &= \frac{e^{c+b^2x^2}x^2\mathrm{erfc}(bx)}{2b^2}-\frac{\int e^{c+b^2x^2}x\mathrm{erfc}(bx)\,dx}{b^2}+\frac{\int e^cx^2\,dx}{b\sqrt{\pi}}\\ &= -\frac{e^{c+b^2x^2}\mathrm{erfc}(bx)}{2b^4}+\frac{e^{c+b^2x^2}x^2\mathrm{erfc}(bx)}{2b^2}-\frac{\int e^c\,dx}{b^3\sqrt{\pi}}+\frac{e^c\int x^2\,dx}{b\sqrt{\pi}}\\ &= -\frac{e^cx}{b^3\sqrt{\pi}}+\frac{e^cx^3}{3b\sqrt{\pi}}-\frac{e^{c+b^2x^2}\mathrm{erfc}(bx)}{2b^4}+\frac{e^{c+b^2x^2}x^2\mathrm{erfc}(bx)}{2b^2}\end{aligned}$$

Mathematica [A]
time = 0.03, size = 58, normalized size = 0.72

$$\frac{e^c\left(2bx(-3+b^2x^2)+3e^{b^2x^2}\sqrt{\pi}\,(-1+b^2x^2)\,\mathrm{Erfc}(bx)\right)}{6b^4\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*x^3*Erfc[b*x],x]
```

```
[Out] (E^c*(2*b*x*(-3 + b^2*x^2) + 3*E^(b^2*x^2)*Sqrt[Pi]*(-1 + b^2*x^2)*Erfc[b*x
]))/(6*b^4*Sqrt[Pi])
```

Maple [A]
time = 0.47, size = 99, normalized size = 1.24

method	result	size
default	$\frac{\frac{e^c\left(\frac{b^2x^2e^{b^2x^2}}{2}-\frac{e^{b^2x^2}}{2}\right)}{b^3}-\frac{\mathrm{erf}(bx)e^c\left(\frac{b^2x^2e^{b^2x^2}}{2}-\frac{e^{b^2x^2}}{2}\right)}{b^3}+\frac{e^c\left(\frac{1}{3}b^3x^3-bx\right)}{\sqrt{\pi}\,b^3}}{b}$	99

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*x^3*erfc(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] (1/b^3*exp(c)*(1/2*b^2*x^2*exp(b^2*x^2)-1/2*exp(b^2*x^2))-erf(b*x)/b^3*exp(
c)*(1/2*b^2*x^2*exp(b^2*x^2)-1/2*exp(b^2*x^2))+1/Pi^(1/2)/b^3*exp(c)*(1/3*b
^3*x^3-b*x))/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^3*erfc(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x^3*erfc(b*x)*e^(b^2*x^2 + c), x)
```

Fricas [A]
time = 0.35, size = 68, normalized size = 0.85

$$\frac{2\sqrt{\pi}\,(b^3x^3 - 3\,bx)e^c - 3\,(\pi - \pi b^2x^2 - (\pi - \pi b^2x^2)\operatorname{erf}(bx))e^{(b^2x^2+c)}}{6\,\pi b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^3*erfc(b*x),x, algorithm="fricas")
```

```
[Out] 1/6*(2*sqrt(pi)*(b^3*x^3 - 3*b*x)*e^c - 3*(pi - pi*b^2*x^2 - (pi - pi*b^2*x
^2)*erf(b*x))*e^(b^2*x^2 + c))/(pi*b^4)
```

Sympy [A]
time = 8.79, size = 83, normalized size = 1.04

$$\begin{cases} \frac{x^3e^c}{3\sqrt{\pi}\,b} + \frac{x^2e^ce^{b^2x^2}\operatorname{erfc}(bx)}{2b^2} - \frac{xe^c}{\sqrt{\pi}\,b^3} - \frac{e^ce^{b^2x^2}\operatorname{erfc}(bx)}{2b^4} & \text{for } b \neq 0 \\ \frac{x^4e^c}{4} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*x**3*erfc(b*x),x)
```

```
[Out] Piecewise((x**3*exp(c)/(3*sqrt(pi)*b) + x**2*exp(c)*exp(b**2*x**2)*erfc(b*x
)/(2*b**2) - x*exp(c)/(sqrt(pi)*b**3) - exp(c)*exp(b**2*x**2)*erfc(b*x)/(2*
b**4), Ne(b, 0)), (x**4*exp(c)/4, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^3*erfc(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^3*erfc(b*x)*e^(b^2*x^2 + c), x)
```

Mupad [B]
time = 0.16, size = 63, normalized size = 0.79

$$-\frac{e^c\left(6\,b\,x-2\,b^3\,x^3+3\,\sqrt{\pi}\,e^{b^2\,x^2}\,\mathrm{erfc}(b\,x)-3\,b^2\,x^2\,\sqrt{\pi}\,e^{b^2\,x^2}\,\mathrm{erfc}(b\,x)\right)}{6\,b^4\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*exp(c + b^2*x^2)*erfc(b*x),x)
```

```
[Out] -(exp(c)*(6*b*x - 2*b^3*x^3 + 3*pi^(1/2)*exp(b^2*x^2)*erfc(b*x) - 3*b^2*x^2
*pi^(1/2)*exp(b^2*x^2)*erfc(b*x)))/(6*b^4*pi^(1/2))
```

3.169 $\int e^{c+b^2x^2} x\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=36

$$\frac{e^c x}{b\sqrt{\pi}} + \frac{e^{c+b^2x^2}\text{Erfc}(bx)}{2b^2}$$

```
[Out] 1/2*exp(b^2*x^2+c)*erfc(b*x)/b^2+exp(c)*x/b/Pi^(1/2)
```

Rubi [A]
time = 0.02, antiderivative size = 36, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.118$, Rules used = {6518, 8}

$$\frac{e^{b^2x^2+c}\text{Erfc}(bx)}{2b^2} + \frac{e^c x}{\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*x*Erfc[b*x],x]
[Out] (E^c*x)/(b*Sqrt[Pi]) + (E^(c + b^2*x^2)*Erfc[b*x])/(2*b^2)
```

Rule 8

```
Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\begin{aligned}\int e^{c+b^2x^2} x\text{erfc}(bx)\,dx &= \frac{e^{c+b^2x^2}\text{erfc}(bx)}{2b^2} + \frac{\int e^c\,dx}{b\sqrt{\pi}}\\ &= \frac{e^c x}{b\sqrt{\pi}} + \frac{e^{c+b^2x^2}\text{erfc}(bx)}{2b^2}\end{aligned}$$

Mathematica [A]
time = 0.02, size = 36, normalized size = 1.00

$$\frac{e^c x}{b\sqrt{\pi}} + \frac{e^{c+b^2x^2}\text{Erfc}(bx)}{2b^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*x*Erfc[b*x],x]
```

```
[Out] (E^c*x)/(b*Sqrt[Pi]) + (E^(c + b^2*x^2)*Erfc[b*x])/(2*b^2)
```

Maple [A]
time = 0.09, size = 51, normalized size = 1.42

method	result	size
default	$\frac{2\,\mathrm{e}^{b^2x^2+c}\mathrm{e}^{-b^2x^2}xb+\mathrm{e}^{b^2x^2+c}\mathrm{erfc}(bx)\sqrt{\pi}}{2\sqrt{\pi}\,b^2}$	51

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*x*erfc(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/2*(2*exp(b^2*x^2+c)*exp(-b^2*x^2)*x*b+exp(b^2*x^2+c)*erfc(b*x)*Pi^(1/2))/
Pi^(1/2)/b^2
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x*erfc(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x*erfc(b*x)*e^(b^2*x^2 + c), x)
```

Fricas [A]
time = 0.39, size = 38, normalized size = 1.06

$$\frac{2\sqrt{\pi}\,bxe^{c} + (\pi - \pi\,\mathrm{erf}\,(bx))e^{(b^2x^2+c)}}{2\,\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x*erfc(b*x),x, algorithm="fricas")
```

```
[Out] 1/2*(2*sqrt(pi)*b*x*e^c + (pi - pi*erf(b*x))*e^(b^2*x^2 + c))/(pi*b^2)
```

Sympy [A]
time = 1.61, size = 41, normalized size = 1.14

$$\begin{cases} \frac{xe^{c}}{\sqrt{\pi}\,b} + \frac{e^{c}e^{b^2x^2}\,\mathrm{erfc}\,(bx)}{2b^2} & \text{for } b \neq 0 \\ \frac{x^2e^{c}}{2} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*x*erfc(b*x),x)
```

```
[Out] Piecewise((x*exp(c)/(sqrt(pi)*b) + exp(c)*exp(b**2*x**2)*erfc(b*x)/(2*b**2)
, Ne(b, 0)), (x**2*exp(c)/2, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x*erfc(b*x),x, algorithm="giac")
```

```
[Out] integrate(x*erfc(b*x)*e^(b^2*x^2 + c), x)
```

Mupad [B]
time = 0.17, size = 30, normalized size = 0.83

$$\frac{x\,\mathrm{e}^c}{b\,\sqrt{\pi}}+\frac{\mathrm{e}^{b^2\,x^2}\,\mathrm{e}^c\,\mathrm{erfc}(b\,x)}{2\,b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*exp(c + b^2*x^2)*erfc(b*x),x)
```

```
[Out] (x*exp(c))/(b*pi^(1/2)) + (exp(b^2*x^2)*exp(c)*erfc(b*x))/(2*b^2)
```

3.170 $\int \frac{e^{c+b^2x^2}\textbf{Erfc}(bx)}{x}\,dx$

Optimal. Leaf size=48

$$\frac{1}{2}e^c\text{Ei}\left(b^2x^2\right)-\frac{2be^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}$$

```
[Out] 1/2*exp(c)*Ei(b^2*x^2)-2*b*exp(c)*x*hypergeom([1/2, 1],[3/2, 3/2],b^2*x^2)/
Pi^(1/2)
```

Rubi [A]
time = 0.07, antiderivative size = 48, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.158, Rules used = {6524, 2241, 6523}

$$\frac{1}{2}e^c\text{Ei}\left(b^2x^2\right)-\frac{2be^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[(E^(c + b^2*x^2)*Erfc[b*x])/x,x]
```

```
[Out] (E^c*ExpIntegralEi[b^2*x^2])/2 - (2*b*E^c*x*HypergeometricPFQ[{1/2, 1}, {3/
2, 3/2}, b^2*x^2])/Sqrt[Pi]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 6523

```
Int[(E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)])/(x_), x_Symbol] :> Simp[2*b*
E^c*(x/Sqrt[Pi])*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, b^2*x^2], x] /; Fr
eeQ[{b, c, d}, x] && EqQ[d, b^2]
```

Rule 6524

```
Int[(E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)])/(x_), x_Symbol] :> Int[E^(c
 + d*x^2)/x, x] - Int[E^(c + d*x^2)*(Erf[b*x]/x), x] /; FreeQ[{b, c, d}, x]
 && EqQ[d, b^2]
```

Rubi steps

$$\int \frac{e^{c+b^2x^2}\operatorname{erfc}(bx)}{x}\,dx = \int \frac{e^{c+b^2x^2}}{x}\,dx - \int \frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{x}\,dx$$
$$= \frac{1}{2}e^c\operatorname{Ei}\left(b^2x^2\right) - \frac{2be^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}$$

Mathematica [**A**]
time = 0.09, size = 45, normalized size = 0.94

$$\frac{1}{2}e^c\left(\operatorname{Ei}\left(b^2x^2\right) - \frac{4bx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[(E^(c + b^2*x^2)*Erfc[b*x])/x,x]
```

```
[Out] (E^c*(ExpIntegralEi[b^2*x^2] - (4*b*x*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2
}, b^2*x^2])/Sqrt[Pi]))/2
```

Maple [**F**]
time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{b^2x^2+c}\operatorname{erfc}(bx)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erfc(b*x)/x,x)
```

```
[Out] int(exp(b^2*x^2+c)*erfc(b*x)/x,x)
```

Maxima [**F**]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x)/x,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)*e^(b^2*x^2 + c)/x, x)
```

Fricas [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x)/x,x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x) - 1)*e^(b^2*x^2 + c)/x, x)
```

Sympy [A]
time = 6.16, size = 39, normalized size = 0.81

$$-\frac{2bxe^{c}{}_{2}F_{2}\left(\begin{matrix} \frac{1}{2}, 1 \\ \frac{3}{2}, \frac{3}{2} \end{matrix}\middle| b^{2}x^{2}\right)}{\sqrt{\pi}}+\frac{e^{c}\operatorname{Ei}\left(b^{2}x^{2}\right)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erfc(b*x)/x,x)
```

```
[Out] -2*b*x*exp(c)*hyper((1/2, 1), (3/2, 3/2), b**2*x**2)/sqrt(pi) + exp(c)*Ei(b
**2*x**2)/2
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x)/x,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(b^2*x^2 + c)/x, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\mathrm{e}^{b^2\,x^2+c}\,\mathrm{erfc}\left(b\,x\right)}{x} \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + b^2*x^2)*erfc(b*x))/x,x)
```

```
[Out] int((exp(c + b^2*x^2)*erfc(b*x))/x, x)
```

3.171 $\int \frac{e^{c+b^2x^2}\mathbf{Erfc}(bx)}{x^3}\,dx$

Optimal. Leaf size=88

$$\frac{be^c}{\sqrt{\pi}\,x}-\frac{e^{c+b^2x^2}\mathrm{Erfc}(bx)}{2x^2}+\frac{1}{2}b^2e^c\mathrm{Ei}\left(b^2x^2\right)-\frac{2b^3e^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}$$

```
[Out] 1/2*b^2*exp(c)*Ei(b^2*x^2)-1/2*exp(b^2*x^2+c)*erfc(b*x)/x^2+b*exp(c)/x/Pi^(
1/2)-2*b^3*exp(c)*x*hypergeom([1/2, 1],[3/2, 3/2],b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.10, antiderivative size = 88, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.316, Rules used = {6527, 6524, 2241, 6523, 12, 30}

$$-\frac{2b^3e^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}-\frac{e^{b^2x^2+c}\mathrm{Erfc}(bx)}{2x^2}+\frac{1}{2}b^2e^c\mathrm{Ei}\left(b^2x^2\right)+\frac{be^c}{\sqrt{\pi}\,x}$$

Antiderivative was successfully verified.

```
[In] Int[(E^(c + b^2*x^2)*Erfc[b*x])/x^3,x]
```

```
[Out] (b*E^c)/(Sqrt[Pi]*x) - (E^(c + b^2*x^2)*Erfc[b*x])/(2*x^2) + (b^2*E^c*ExpIn
tegralEi[b^2*x^2])/2 - (2*b^3*E^c*x*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2},
 b^2*x^2])/Sqrt[Pi]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 6523

```
Int[(E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)])/(x_), x_Symbol] :> Simp[2*b*
E^c*(x/Sqrt[Pi])*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, b^2*x^2], x] /; Fr
```

```
eeQ[{b, c, d}, x] && EqQ[d, b^2]
```

Rule 6524

```
Int[(E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)])/(x_), x_Symbol] :> Int[E^(c
 + d*x^2)/x, x] - Int[E^(c + d*x^2)*(Erf[b*x]/x), x] /; FreeQ[{b, c, d}, x]
 && EqQ[d, b^2]
```

Rule 6527

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x],
x]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+b^2x^2}\operatorname{erfc}(bx)}{x^3}\,dx &= -\frac{e^{c+b^2x^2}\operatorname{erfc}(bx)}{2x^2}+b^2\int \frac{e^{c+b^2x^2}\operatorname{erfc}(bx)}{x}\,dx-\frac{b\int \frac{e^c}{x^2}\,dx}{\sqrt{\pi}}\\ &= -\frac{e^{c+b^2x^2}\operatorname{erfc}(bx)}{2x^2}+b^2\int \frac{e^{c+b^2x^2}}{x}\,dx-b^2\int \frac{e^{c+b^2x^2}\operatorname{erf}(bx)}{x}\,dx-\frac{(be^c)\int \frac{1}{x^2}\,dx}{\sqrt{\pi}}\\ &= \frac{be^c}{\sqrt{\pi}\,x}-\frac{e^{c+b^2x^2}\operatorname{erfc}(bx)}{2x^2}+\frac{1}{2}b^2e^c\operatorname{Ei}\left(b^2x^2\right)-\frac{2b^3e^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.15, size = 65, normalized size = 0.74

$$-\frac{e^c\left(e^{b^2x^2}-b^2x^2\operatorname{Ei}(b^2x^2)-\frac{4bx\,{}_2F_2\left(-\frac{1}{2},1;\frac{1}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}\right)}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[(E^(c + b^2*x^2)*Erfc[b*x])/x^3,x]
```

```
[Out] -1/2*(E^c*(E^(b^2*x^2) - b^2*x^2*ExpIntegralEi[b^2*x^2] - (4*b*x*Hypergeome
tricPFQ[{-1/2, 1}, {1/2, 3/2}, b^2*x^2])/Sqrt[Pi]))/x^2
```

Maple [F]
time = 0.21, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{b^2x^2+c}\operatorname{erfc}(bx)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erfc(b*x)/x^3,x)
```

```
[Out] int(exp(b^2*x^2+c)*erfc(b*x)/x^3,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x)/x^3,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)*e^(b^2*x^2 + c)/x^3, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x)/x^3,x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x) - 1)*e^(b^2*x^2 + c)/x^3, x)
```

Sympy [A]
time = 33.79, size = 61, normalized size = 0.69

$$\frac{b^{2} e^{c} \operatorname{Ei}\left(b^{2} x^{2}\right)}{2} + \frac{2 b e^{c} {}_{2}F_{2}\left(\begin{matrix} - \frac{1}{2}, 1 \\ \frac{1}{2}, \frac{3}{2} \end{matrix}\middle| {b^{2} x^{2}} \right)}{\sqrt{\pi} x} - \frac{e^{c} e^{b^{2} x^{2}}}{2 x^{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erfc(b*x)/x**3,x)
```

```
[Out] b**2*exp(c)*Ei(b**2*x**2)/2 + 2*b*exp(c)*hyper((-1/2, 1), (1/2, 3/2), b**2*
x**2)/(sqrt(pi)*x) - exp(c)*exp(b**2*x**2)/(2*x**2)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x)/x^3,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(b^2*x^2 + c)/x^3, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{e^{b^2 x^2+c} \operatorname{erfc}(b x)}{x^3} \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + b^2*x^2)*erfc(b*x))/x^3,x)
[Out] int((exp(c + b^2*x^2)*erfc(b*x))/x^3, x)
```

3.172 $\int \frac{e^{c+b^2x^2}\mathbf{Erfc}(bx)}{x^5}\,dx$

Optimal. Leaf size=134

$$\frac{be^c}{6\sqrt{\pi}\,x^3}+\frac{b^3e^c}{2\sqrt{\pi}\,x}-\frac{e^{c+b^2x^2}\text{Erfc}(bx)}{4x^4}-\frac{b^2e^{c+b^2x^2}\text{Erfc}(bx)}{4x^2}+\frac{1}{4}b^4e^c\text{Ei}\left(b^2x^2\right)-\frac{b^5e^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}$$

```
[Out] 1/4*b^4*exp(c)*Ei(b^2*x^2)-1/4*exp(b^2*x^2+c)*erfc(b*x)/x^4-1/4*b^2*exp(b^2
*x^2+c)*erfc(b*x)/x^2+1/6*b*exp(c)/x^3/Pi^(1/2)+1/2*b^3*exp(c)/x/Pi^(1/2)-b
^5*exp(c)*x*hypergeom([1/2, 1],[3/2, 3/2],b^2*x^2)/Pi^(1/2)
```

Rubi [A]

time = 0.13, antiderivative size = 134, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {6527, 6524, 2241, 6523, 12, 30}

$$-\frac{b^5e^cx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}+\frac{b^3e^c}{2\sqrt{\pi}\,x}-\frac{b^2e^{b^2x^2+c}\text{Erfc}(bx)}{4x^2}-\frac{e^{b^2x^2+c}\text{Erfc}(bx)}{4x^4}+\frac{1}{4}b^4e^c\text{Ei}\left(b^2x^2\right)+\frac{be^c}{6\sqrt{\pi}\,x^3}$$

Antiderivative was successfully verified.

```
[In] Int[(E^(c + b^2*x^2)*Erfc[b*x])/x^5,x]
```

```
[Out] (b*E^c)/(6*Sqrt[Pi]*x^3) + (b^3*E^c)/(2*Sqrt[Pi]*x) - (E^(c + b^2*x^2)*Erfc
[b*x])/(4*x^4) - (b^2*E^(c + b^2*x^2)*Erfc[b*x])/(4*x^2) + (b^4*E^c*ExpInte
gralEi[b^2*x^2])/4 - (b^5*E^c*x*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, b^2
*x^2])/Sqrt[Pi]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 6523

```
Int[(E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)])/(x_), x_Symbol] :> Simp[2*b*
E^c*(x/Sqrt[Pi])*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, b^2*x^2], x] /; Fr
```

```
eeQ[{b, c, d}, x] && EqQ[d, b^2]
```

Rule 6524

```
Int[(E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)])/(x_), x_Symbol] :> Int[E^(c
 + d*x^2)/x, x] - Int[E^(c + d*x^2)*(Erf[b*x]/x), x] /; FreeQ[{b, c, d}, x]
 && EqQ[d, b^2]
```

Rule 6527

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x],
x]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+b^2x^2}\mathrm{erfc}(bx)}{x^5}\,dx &= -\frac{e^{c+b^2x^2}\mathrm{erfc}(bx)}{4x^4}+\frac{1}{2}b^2\int \frac{e^{c+b^2x^2}\mathrm{erfc}(bx)}{x^3}\,dx-\frac{b\int \frac{e^c}{x^4}\,dx}{2\sqrt{\pi}}\\ &= -\frac{e^{c+b^2x^2}\mathrm{erfc}(bx)}{4x^4}-\frac{b^2e^{c+b^2x^2}\mathrm{erfc}(bx)}{4x^2}+\frac{1}{2}b^4\int \frac{e^{c+b^2x^2}\mathrm{erfc}(bx)}{x}\,dx-\frac{b^3\int \frac{e^c}{x^2}\,dx}{2\sqrt{\pi}}-\frac{(be\\ &= \frac{be^c}{6\sqrt{\pi}\,x^3}-\frac{e^{c+b^2x^2}\mathrm{erfc}(bx)}{4x^4}-\frac{b^2e^{c+b^2x^2}\mathrm{erfc}(bx)}{4x^2}+\frac{1}{2}b^4\int \frac{e^{c+b^2x^2}}{x}\,dx-\frac{1}{2}b^4\int \frac{e^{c+b^2x^2}e}{x}\\ &= \frac{be^c}{6\sqrt{\pi}\,x^3}+\frac{b^3e^c}{2\sqrt{\pi}\,x}-\frac{e^{c+b^2x^2}\mathrm{erfc}(bx)}{4x^4}-\frac{b^2e^{c+b^2x^2}\mathrm{erfc}(bx)}{4x^2}+\frac{1}{4}b^4e^c\mathrm{Ei}\left(b^2x^2\right)-\frac{b^5e^cx\,{}_2}{}\end{aligned}$$

Mathematica [A]
time = 0.15, size = 83, normalized size = 0.62

$$-\frac{e^c\left(3\sqrt{\pi}\left(e^{b^2x^2}(1+b^2x^2)-b^4x^4\mathrm{Ei}(b^2x^2)\right)-8bx\,{}_2F_2\left(-\frac{3}{2},1;-\frac{1}{2},\frac{3}{2};b^2x^2\right)\right)}{12\sqrt{\pi}\,x^4}$$

Antiderivative was successfully verified.

```
[In] Integrate[(E^(c + b^2*x^2)*Erfc[b*x])/x^5,x]
```

```
[Out] -1/12*(E^c*(3*Sqrt[Pi]*(E^(b^2*x^2)*(1 + b^2*x^2) - b^4*x^4*ExpIntegralEi[b
^2*x^2]) - 8*b*x*HypergeometricPFQ[{-3/2, 1}, {-1/2, 3/2}, b^2*x^2]))/(Sqrt
[Pi]*x^4)
```

Maple [F]
time = 0.22, size = 0, normalized size = 0.00

$$\int \frac{e^{b^2x^2+c}\mathrm{erfc}(bx)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erfc(b*x)/x^5,x)
[Out] int(exp(b^2*x^2+c)*erfc(b*x)/x^5,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x)/x^5,x, algorithm="maxima")
[Out] integrate(erfc(b*x)*e^(b^2*x^2 + c)/x^5, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x)/x^5,x, algorithm="fricas")
[Out] integral(-(erf(b*x) - 1)*e^(b^2*x^2 + c)/x^5, x)
```

Sympy [F(-1)] Timed out
time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erfc(b*x)/x**5,x)
[Out] Timed out
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x)/x^5,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(b^2*x^2 + c)/x^5, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{b^2\,x^2+c}\,\mathrm{erfc}(b\,x)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + b^2*x^2)*erfc(b*x))/x^5,x)
```

```
[Out] int((exp(c + b^2*x^2)*erfc(b*x))/x^5, x)
```

3.173 $\int e^{c+b^2x^2}x^4\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=138

$$-\frac{3e^cx^2}{4b^3\sqrt{\pi}}+\frac{e^cx^4}{4b\sqrt{\pi}}-\frac{3e^{c+b^2x^2}x\operatorname{Erfc}(bx)}{4b^4}+\frac{e^{c+b^2x^2}x^3\operatorname{Erfc}(bx)}{2b^2}+\frac{3e^c\sqrt{\pi}\operatorname{Erfi}(bx)}{8b^5}-\frac{3e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{4b^3\sqrt{\pi}}$$

```
[Out] -3/4*exp(b^2*x^2+c)*x*erfc(b*x)/b^4+1/2*exp(b^2*x^2+c)*x^3*erfc(b*x)/b^2-3/
4*exp(c)*x^2/b^3/Pi^(1/2)+1/4*exp(c)*x^4/b/Pi^(1/2)-3/4*exp(c)*x^2*hypergeo
m([1, 1],[3/2, 2],b^2*x^2)/b^3/Pi^(1/2)+3/8*exp(c)*erfi(b*x)*Pi^(1/2)/b^5
```

Rubi [A]
time = 0.09, antiderivative size = 138, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {6521, 6512, 2235, 6511, 12, 30}

$$-\frac{3e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{4\sqrt{\pi}\,b^3}+\frac{3\sqrt{\pi}\,e^c\operatorname{Erfi}(bx)}{8b^5}-\frac{3e^cx^2}{4\sqrt{\pi}\,b^3}+\frac{x^3e^{b^2x^2+c}\operatorname{Erfc}(bx)}{2b^2}-\frac{3xe^{b^2x^2+c}\operatorname{Erfc}(bx)}{4b^4}+\frac{e^cx^4}{4\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*x^4*Erfc[b*x],x]
```

```
[Out] (-3*E^c*x^2)/(4*b^3*Sqrt[Pi]) + (E^c*x^4)/(4*b*Sqrt[Pi]) - (3*E^(c + b^2*x^
2)*x*Erfc[b*x])/(4*b^4) + (E^(c + b^2*x^2)*x^3*Erfc[b*x])/(2*b^2) + (3*E^c*
Sqrt[Pi]*Erfi[b*x])/(8*b^5) - (3*E^c*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}
, b^2*x^2])/(4*b^3*Sqrt[Pi])
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
```

```
d}, x] && EqQ[d, b^2]
```

Rule 6512

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)], x_Symbol] :> Int[E^(c + d*x^
2), x] - Int[E^(c + d*x^2)*Erf[b*x], x] /; FreeQ[{b, c, d}, x] && EqQ[d, b^
2]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{c+b^2x^2}x^4\text{erfc}(bx)\,dx &= \frac{e^{c+b^2x^2}x^3\text{erfc}(bx)}{2b^2} - \frac{3\int e^{c+b^2x^2}x^2\text{erfc}(bx)\,dx}{2b^2} + \frac{\int e^cx^3\,dx}{b\sqrt{\pi}}\\ &= -\frac{3e^{c+b^2x^2}x\text{erfc}(bx)}{4b^4} + \frac{e^{c+b^2x^2}x^3\text{erfc}(bx)}{2b^2} + \frac{3\int e^{c+b^2x^2}\text{erfc}(bx)\,dx}{4b^4} - \frac{3\int e^cx\,dx}{2b^3\sqrt{\pi}} + \\ &= \frac{e^cx^4}{4b\sqrt{\pi}} - \frac{3e^{c+b^2x^2}x\text{erfc}(bx)}{4b^4} + \frac{e^{c+b^2x^2}x^3\text{erfc}(bx)}{2b^2} + \frac{3\int e^{c+b^2x^2}\,dx}{4b^4} - \frac{3\int e^{c+b^2x^2}\text{erf}(}{4b^4}\\ &= -\frac{3e^cx^2}{4b^3\sqrt{\pi}} + \frac{e^cx^4}{4b\sqrt{\pi}} - \frac{3e^{c+b^2x^2}x\text{erfc}(bx)}{4b^4} + \frac{e^{c+b^2x^2}x^3\text{erfc}(bx)}{2b^2} + \frac{3e^c\sqrt{\pi}\,\text{erfi}(bx)}{8b^5} - \end{aligned}$$

Mathematica [A]
time = 0.26, size = 147, normalized size = 1.07

$$-\frac{e^c\left(6be^{b^2x^2}\sqrt{\pi}\,x+6b^2x^2-4b^3e^{b^2x^2}\sqrt{\pi}\,x^3-2b^4x^4+2be^{b^2x^2}\sqrt{\pi}\,x(-3+2b^2x^2)\,\text{Erf}(bx)-3\pi\text{Erfi}(bx)+3\pi\text{Erf}(bx)\text{Erfi}(bx)-6b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)\right)}{8b^5\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*x^4*Erfc[b*x],x]
```

```
[Out] -1/8*(E^c*(6*b*E^(b^2*x^2)*Sqrt[Pi]*x + 6*b^2*x^2 - 4*b^3*E^(b^2*x^2)*Sqrt[
Pi]*x^3 - 2*b^4*x^4 + 2*b*E^(b^2*x^2)*Sqrt[Pi]*x*(-3 + 2*b^2*x^2)*Erf[b*x]
- 3*Pi*Erfi[b*x] + 3*Pi*Erf[b*x]*Erfi[b*x] - 6*b^2*x^2*HypergeometricPFQ[{1
, 1}, {3/2, 2}, -(b^2*x^2)]))/(b^5*Sqrt[Pi])
```

Maple [F]
time = 0.07, size = 0, normalized size = 0.00

$$\int e^{b^2x^2+c}x^4\mathrm{erfc}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*x^4*erfc(b*x),x)
[Out] int(exp(b^2*x^2+c)*x^4*erfc(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^4*erfc(b*x),x, algorithm="maxima")
[Out] integrate(x^4*erfc(b*x)*e^(b^2*x^2 + c), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^4*erfc(b*x),x, algorithm="fricas")
[Out] integral(-(x^4*erf(b*x) - x^4)*e^(b^2*x^2 + c), x)
```

Sympy [F(-1)] Timed out
time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*x**4*erfc(b*x),x)
[Out] Timed out
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^4*erfc(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^4*erfc(b*x)*e^(b^2*x^2 + c), x)
```

Mupad [**F**]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^4\,\mathrm{e}^{b^2\,x^2+c}\,\mathrm{erfc}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*exp(c + b^2*x^2)*erfc(b*x),x)
```

```
[Out] int(x^4*exp(c + b^2*x^2)*erfc(b*x), x)
```

3.174 $\int e^{c+b^2x^2}x^2\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=95

$$\frac{e^cx^2}{2b\sqrt{\pi}}+\frac{e^{c+b^2x^2}x\mathrm{Erfc}(bx)}{2b^2}-\frac{e^c\sqrt{\pi}\,\mathrm{Erfi}(bx)}{4b^3}+\frac{e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2b\sqrt{\pi}}$$

```
[Out] 1/2*exp(b^2*x^2+c)*x*erfc(b*x)/b^2+1/2*exp(c)*x^2/b/Pi^(1/2)+1/2*exp(c)*x^2
*hypergeom([1, 1],[3/2, 2],b^2*x^2)/b/Pi^(1/2)-1/4*exp(c)*erfi(b*x)*Pi^(1/2
)/b^3
```

Rubi [A]
time = 0.06, antiderivative size = 95, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {6521, 6512, 2235, 6511, 12, 30}

$$\frac{e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}\,b}-\frac{\sqrt{\pi}\,e^c\mathrm{Erfi}(bx)}{4b^3}+\frac{xe^{b^2x^2+c}\mathrm{Erfc}(bx)}{2b^2}+\frac{e^cx^2}{2\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*x^2*Erfc[b*x],x]
```

```
[Out] (E^c*x^2)/(2*b*Sqrt[Pi]) + (E^(c + b^2*x^2)*x*Erfc[b*x])/(2*b^2) - (E^c*Sqr
t[Pi]*Erfi[b*x])/(4*b^3) + (E^c*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2
*x^2])/(2*b*Sqrt[Pi])
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
```

```
d}, x] && EqQ[d, b^2]
```

Rule 6512

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)], x_Symbol] :> Int[E^(c + d*x^
2), x] - Int[E^(c + d*x^2)*Erf[b*x], x] /; FreeQ[{b, c, d}, x] && EqQ[d, b^
2]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{c+b^2x^2}x^2\mathrm{erfc}(bx)\,dx &= \frac{e^{c+b^2x^2}x\mathrm{erfc}(bx)}{2b^2}-\frac{\int e^{c+b^2x^2}\mathrm{erfc}(bx)\,dx}{2b^2}+\frac{\int e^cx\,dx}{b\sqrt{\pi}}\\ &= \frac{e^{c+b^2x^2}x\mathrm{erfc}(bx)}{2b^2}-\frac{\int e^{c+b^2x^2}\,dx}{2b^2}+\frac{\int e^{c+b^2x^2}\mathrm{erf}(bx)\,dx}{2b^2}+\frac{e^c\int x\,dx}{b\sqrt{\pi}}\\ &= \frac{e^cx^2}{2b\sqrt{\pi}}+\frac{e^{c+b^2x^2}x\mathrm{erfc}(bx)}{2b^2}-\frac{e^c\sqrt{\pi}\,\mathrm{erfi}(bx)}{4b^3}+\frac{e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2b\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.22, size = 104, normalized size = 1.09

$$-\frac{e^c\left(-2be^{b^2x^2}\sqrt{\pi}\,x-2b^2x^2+\pi\mathrm{Erfi}(bx)+\mathrm{Erf}(bx)\left(2be^{b^2x^2}\sqrt{\pi}\,x-\pi\mathrm{Erfi}(bx)\right)+2b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)\right)}{4b^3\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*x^2*Erfc[b*x],x]
```

```
[Out] -1/4*(E^c*(-2*b*E^(b^2*x^2)*Sqrt[Pi]*x - 2*b^2*x^2 + Pi*Erfi[b*x] + Erf[b*x
]*(2*b*E^(b^2*x^2)*Sqrt[Pi]*x - Pi*Erfi[b*x]) + 2*b^2*x^2*HypergeometricPFQ
[{1, 1}, {3/2, 2}, -(b^2*x^2)]))/(b^3*Sqrt[Pi])
```

Maple [F]
time = 0.12, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{b^2x^2+c}x^2\mathrm{erfc}(bx)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*x^2*erfc(b*x),x)
```

```
[Out] int(exp(b^2*x^2+c)*x^2*erfc(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^2*erfc(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x^2*erfc(b*x)*e^(b^2*x^2 + c), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^2*erfc(b*x),x, algorithm="fricas")
```

```
[Out] integral(-(x^2*erf(b*x) - x^2)*e^(b^2*x^2 + c), x)
```

Sympy [C] Result contains complex when optimal does not.
time = 32.90, size = 65, normalized size = 0.68

$$-\frac{bx^4e^c{}_2F_2\left(\begin{matrix}1,2\\ \frac{3}{2},3\end{matrix}\middle|b^2x^2\right)}{2\sqrt{\pi}}+\frac{xe^ce^{b^2x^2}}{2b^2}+\frac{i\sqrt{\pi}\,e^c\operatorname{erf}(ibx)}{4b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*x**2*erfc(b*x),x)
```

```
[Out] -b*x**4*exp(c)*hyper((1, 2), (3/2, 3), b**2*x**2)/(2*sqrt(pi)) + x*exp(c)*e
xp(b**2*x**2)/(2*b**2) + I*sqrt(pi)*exp(c)*erf(I*b*x)/(4*b**3)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^2*erfc(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^2*erfc(b*x)*e^(b^2*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^2\,\mathrm{e}^{b^2\,x^2+c}\,\mathrm{erfc}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*exp(c + b^2*x^2)*erfc(b*x),x)
```

```
[Out] int(x^2*exp(c + b^2*x^2)*erfc(b*x), x)
```

3.175 $\int e^{c+b^2x^2}\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=50

$$\frac{e^c\sqrt{\pi}\,\mathrm{Erfi}(bx)}{2b}-\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{\sqrt{\pi}}$$

```
[Out] -b*exp(c)*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/Pi^(1/2)+1/2*exp(c)*erfi(b
*x)*Pi^(1/2)/b
```

Rubi [A]
time = 0.03, antiderivative size = 50, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.188, Rules used = {6512, 2235, 6511}

$$\frac{\sqrt{\pi}\,e^c\mathrm{Erfi}(bx)}{2b}-\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*Erfc[b*x],x]
```

```
[Out] (E^c*Sqrt[Pi]*Erfi[b*x])/(2*b) - (b*E^c*x^2*HypergeometricPFQ[{1, 1}, {3/2,
 2}, b^2*x^2])/Sqrt[Pi]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6512

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)], x_Symbol] :> Int[E^(c + d*x^
2), x] - Int[E^(c + d*x^2)*Erf[b*x], x] /; FreeQ[{b, c, d}, x] && EqQ[d, b^
2]
```

Rubi steps

$$\int e^{c+b^2x^2}\text{erfc}(bx)\,dx = \int e^{c+b^2x^2}\,dx - \int e^{c+b^2x^2}\text{erf}(bx)\,dx$$
$$= \frac{e^c\sqrt{\pi}\,\text{erfi}(bx)}{2b} - \frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{\sqrt{\pi}}$$

Mathematica [F]
time = 0.06, size = 0, normalized size = 0.00

$$\int e^{c+b^2x^2}\text{Erfc}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + b^2*x^2)*Erfc[b*x],x]
```

```
[Out] Integrate[E^(c + b^2*x^2)*Erfc[b*x], x]
```

Maple [F]
time = 0.07, size = 0, normalized size = 0.00

$$\int e^{b^2x^2+c}\text{erfc}(bx)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erfc(b*x),x)
```

```
[Out] int(exp(b^2*x^2+c)*erfc(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x),x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)*e^(b^2*x^2 + c), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x),x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x) - 1)*e^(b^2*x^2 + c), x)
```

Sympy [C] Result contains complex when optimal does not.
time = 4.61, size = 44, normalized size = 0.88

$$-\frac{bx^2e^c{}_2F_2\left(\begin{matrix}1,1\\ \frac{3}{2},2\end{matrix}\middle|b^2x^2\right)}{\sqrt{\pi}}-\frac{i\sqrt{\pi}\,e^c\operatorname{erf}(ibx)}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erfc(b*x),x)
```

```
[Out] -b*x**2*exp(c)*hyper((1, 1), (3/2, 2), b**2*x**2)/sqrt(pi) - I*sqrt(pi)*exp
(c)*erf(I*b*x)/(2*b)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x),x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(b^2*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \mathrm{e}^{b^2\,x^2+c}\,\mathrm{erfc}(b\,x)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c + b^2*x^2)*erfc(b*x),x)
```

```
[Out] int(exp(c + b^2*x^2)*erfc(b*x), x)
```

3.176 $\int \frac{e^{c+b^2x^2}\mathbf{Erfc}(bx)}{x^2}\,dx$

Optimal. Leaf size=80

$$-\frac{e^{c+b^2x^2}\operatorname{Erfc}(bx)}{x}+be^c\sqrt{\pi}\operatorname{Erfi}(bx)-\frac{2b^3e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{\sqrt{\pi}}-\frac{2be^c\log(x)}{\sqrt{\pi}}$$

```
[Out] -exp(b^2*x^2+c)*erfc(b*x)/x-2*b^3*exp(c)*x^2*hypergeom([1, 1],[3/2, 2],b^2*
x^2)/Pi^(1/2)-2*b*exp(c)*ln(x)/Pi^(1/2)+b*exp(c)*erfi(b*x)*Pi^(1/2)
```

Rubi [A]

time = 0.06, antiderivative size = 80, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.316, Rules used = {6527, 6512, 2235, 6511, 12, 29}

$$-\frac{2b^3e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{\sqrt{\pi}}-\frac{e^{b^2x^2+c}\operatorname{Erfc}(bx)}{x}+\sqrt{\pi}\,be^c\operatorname{Erfi}(bx)-\frac{2be^c\log(x)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[(E^(c + b^2*x^2)*Erfc[b*x])/x^2,x]
```

```
[Out] -((E^(c + b^2*x^2)*Erfc[b*x])/x) + b*E^c*Sqrt[Pi]*Erfi[b*x] - (2*b^3*E^c*x^
2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2])/Sqrt[Pi] - (2*b*E^c*Log[x])
/Sqrt[Pi]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 29

```
Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6512

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)], x_Symbol] :> Int[E^(c + d*x^
2), x] - Int[E^(c + d*x^2)*Erf[b*x], x] /; FreeQ[{b, c, d}, x] && EqQ[d, b^
2]
```

Rule 6527

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x],
x]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+b^2x^2}\text{erfc}(bx)}{x^2}\,dx &= -\frac{e^{c+b^2x^2}\text{erfc}(bx)}{x}+\left(2b^2\right)\int e^{c+b^2x^2}\text{erfc}(bx)\,dx-\frac{(2b)\int \frac{e^c}{x}\,dx}{\sqrt{\pi}}\\ &= -\frac{e^{c+b^2x^2}\text{erfc}(bx)}{x}+\left(2b^2\right)\int e^{c+b^2x^2}\,dx-\left(2b^2\right)\int e^{c+b^2x^2}\text{erf}(bx)\,dx-\frac{(2be^c)\int \frac{1}{x}\,dx}{\sqrt{\pi}}\\ &= -\frac{e^{c+b^2x^2}\text{erfc}(bx)}{x}+be^c\sqrt{\pi}\,\text{erfi}(bx)-\frac{2b^3e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{\sqrt{\pi}}-\frac{2be^c\log(x)}{\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.19, size = 99, normalized size = 1.24

$$-\frac{e^c\left(e^{b^2x^2}\sqrt{\pi}-b\pi x\text{Erfi}(bx)+\text{Erf}(bx)\left(-e^{b^2x^2}\sqrt{\pi}+b\pi x\text{Erfi}(bx)\right)-2b^3x^3\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)+2bx\log(x)\right)}{\sqrt{\pi}\,x}$$

Antiderivative was successfully verified.

```
[In] Integrate[(E^(c + b^2*x^2)*Erfc[b*x])/x^2,x]
```

```
[Out] -((E^c*(E^(b^2*x^2)*Sqrt[Pi] - b*Pi*x*Erfi[b*x] + Erf[b*x]*(-(E^(b^2*x^2)*S
qrt[Pi]) + b*Pi*x*Erfi[b*x]) - 2*b^3*x^3*HypergeometricPFQ[{1, 1}, {3/2, 2}
, -(b^2*x^2)] + 2*b*x*Log[x]))/(Sqrt[Pi]*x))
```

Maple [F]
time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{b^2x^2+c}\text{erfc}(bx)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erfc(b*x)/x^2,x)
```

```
[Out] int(exp(b^2*x^2+c)*erfc(b*x)/x^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x)/x^2,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)*e^(b^2*x^2 + c)/x^2, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x)/x^2,x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x) - 1)*e^(b^2*x^2 + c)/x^2, x)
```

Sympy [C] Result contains complex when optimal does not.
time = 11.39, size = 80, normalized size = 1.00

$$-\frac{2b^3x^2e^c{}_2F_2\left(\begin{matrix}1,1\\2,\frac{5}{2}\end{matrix}\middle|b^2x^2\right)}{3\sqrt{\pi}}-\frac{be^c\log\left(b^2x^2\right)}{\sqrt{\pi}}-i\sqrt{\pi}\,be^c\operatorname{erf}\left(ibx\right)-\frac{e^ce^{b^2x^2}}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erfc(b*x)/x**2,x)
```

```
[Out] -2*b**3*x**2*exp(c)*hyper((1, 1), (2, 5/2), b**2*x**2)/(3*sqrt(pi)) - b*exp
(c)*log(b**2*x**2)/sqrt(pi) - I*sqrt(pi)*b*exp(c)*erf(I*b*x) - exp(c)*exp(b
**2*x**2)/x
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x)/x^2,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(b^2*x^2 + c)/x^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{e^{b^2\,x^2+c}\,\mathrm{erfc}(b\,x)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + b^2*x^2)*erfc(b*x))/x^2,x)
```

```
[Out] int((exp(c + b^2*x^2)*erfc(b*x))/x^2, x)
```

3.177 $\int \frac{e^{c+b^2x^2}\mathbf{Erfc}(bx)}{x^4}\,dx$

Optimal. Leaf size=134

$$\frac{be^c}{3\sqrt{\pi}\,x^2}-\frac{e^{c+b^2x^2}\text{Erfc}(bx)}{3x^3}-\frac{2b^2e^{c+b^2x^2}\text{Erfc}(bx)}{3x}+\frac{2}{3}b^3e^c\sqrt{\pi}\,\text{Erfi}(bx)-\frac{4b^5e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{3\sqrt{\pi}}-\frac{4b^3e^c\log(}{3\sqrt{\pi}}$$

```
[Out] -1/3*exp(b^2*x^2+c)*erfc(b*x)/x^3-2/3*b^2*exp(b^2*x^2+c)*erfc(b*x)/x+1/3*b*
exp(c)/x^2/Pi^(1/2)-4/3*b^5*exp(c)*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/P
i^(1/2)-4/3*b^3*exp(c)*ln(x)/Pi^(1/2)+2/3*b^3*exp(c)*erfi(b*x)*Pi^(1/2)
```

Rubi [A]
time = 0.09, antiderivative size = 134, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 7, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.368$, Rules used = {6527, 6512, 2235, 6511, 12, 29, 30}

$$-\frac{4b^5e^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{3\sqrt{\pi}}+\frac{2}{3}\sqrt{\pi}\,b^3e^c\text{Erfi}(bx)-\frac{4b^3e^c\log(x)}{3\sqrt{\pi}}-\frac{2b^2e^{b^2x^2+c}\text{Erfc}(bx)}{3x}-\frac{e^{b^2x^2+c}\text{Erfc}(bx)}{3x^3}+\frac{be^c}{3\sqrt{\pi}\,x^2}$$

Antiderivative was successfully verified.

```
[In] Int[(E^(c + b^2*x^2)*Erfc[b*x])/x^4,x]
```

```
[Out] (b*E^c)/(3*Sqrt[Pi]*x^2) - (E^(c + b^2*x^2)*Erfc[b*x])/(3*x^3) - (2*b^2*E^(
c + b^2*x^2)*Erfc[b*x])/(3*x) + (2*b^3*E^c*Sqrt[Pi]*Erfi[b*x])/3 - (4*b^5*E
^c*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2])/(3*Sqrt[Pi]) - (4*b^3*
E^c*Log[x])/(3*Sqrt[Pi])
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 29

```
Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6512

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)], x_Symbol] :> Int[E^(c + d*x^
2), x] - Int[E^(c + d*x^2)*Erf[b*x], x] /; FreeQ[{b, c, d}, x] && EqQ[d, b^
2]
```

Rule 6527

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x],
x]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+b^2x^2}\operatorname{erfc}(bx)}{x^4}\,dx &= -\frac{e^{c+b^2x^2}\operatorname{erfc}(bx)}{3x^3}+\frac{1}{3}\left(2b^2\right)\int \frac{e^{c+b^2x^2}\operatorname{erfc}(bx)}{x^2}\,dx-\frac{(2b)\int \frac{e^c}{x^3}\,dx}{3\sqrt{\pi}}\\ &= -\frac{e^{c+b^2x^2}\operatorname{erfc}(bx)}{3x^3}-\frac{2b^2e^{c+b^2x^2}\operatorname{erfc}(bx)}{3x}+\frac{1}{3}\left(4b^4\right)\int e^{c+b^2x^2}\operatorname{erfc}(bx)\,dx-\frac{\left(4b^3\right)\int \frac{e^c}{x}\,dx}{3\sqrt{\pi}}\\ &= \frac{be^c}{3\sqrt{\pi}\,x^2}-\frac{e^{c+b^2x^2}\operatorname{erfc}(bx)}{3x^3}-\frac{2b^2e^{c+b^2x^2}\operatorname{erfc}(bx)}{3x}+\frac{1}{3}\left(4b^4\right)\int e^{c+b^2x^2}\,dx-\frac{1}{3}\left(4b^4\right)\int e^{c}\\ &= \frac{be^c}{3\sqrt{\pi}\,x^2}-\frac{e^{c+b^2x^2}\operatorname{erfc}(bx)}{3x^3}-\frac{2b^2e^{c+b^2x^2}\operatorname{erfc}(bx)}{3x}+\frac{2}{3}b^3e^c\sqrt{\pi}\operatorname{erfi}(bx)-\frac{4b^5e^cx^2\,{}_2F_2(1,}{3\sqrt{}}\end{aligned}$$

Mathematica [A]
time = 0.31, size = 151, normalized size = 1.13

$$\frac{e^c\left(-e^{b^2x^2}\sqrt{\pi}+bx-2b^2e^{b^2x^2}\sqrt{\pi}\,x^2+e^{b^2x^2}\sqrt{\pi}\left(1+2b^2x^2\right)\operatorname{Erf}(bx)+2b^3\pi x^3\operatorname{Erfi}(bx)-2b^3\pi x^3\operatorname{Erf}(bx)\operatorname{Erfi}(bx)+4b^5x^5\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)-4b^3x^3\log(x)\right)}{3\sqrt{\pi}\,x^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[(E^(c + b^2*x^2)*Erfc[b*x])/x^4,x]
```

```
[Out] (E^c*(-(E^(b^2*x^2)*Sqrt[Pi]) + b*x - 2*b^2*E^(b^2*x^2)*Sqrt[Pi]*x^2 + E^(b
^2*x^2)*Sqrt[Pi]*(1 + 2*b^2*x^2)*Erf[b*x] + 2*b^3*Pi*x^3*Erfi[b*x] - 2*b^3*
```

```
Pi*x^3*Erf[b*x]*Erfi[b*x] + 4*b^5*x^5*HypergeometricPFQ[{1, 1}, {3/2, 2}, -
(b^2*x^2)] - 4*b^3*x^3*Log[x]))/(3*Sqrt[Pi]*x^3)
```

Maple [F]
time = 0.14, size = 0, normalized size = 0.00

$$\int \frac{e^{b^2x^2+c}\operatorname{erfc}(bx)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erfc(b*x)/x^4,x)
[Out] int(exp(b^2*x^2+c)*erfc(b*x)/x^4,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x)/x^4,x, algorithm="maxima")
[Out] integrate(erfc(b*x)*e^(b^2*x^2 + c)/x^4, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x)/x^4,x, algorithm="fricas")
[Out] integral(-(erf(b*x) - 1)*e^(b^2*x^2 + c)/x^4, x)
```

Sympy [A]
time = 90.79, size = 22, normalized size = 0.16

$$-\frac{b^3 G_{3,2}^{1,3}\left(\begin{matrix} 2, \frac{5}{2}, 1 & \\ 2 & 0 \end{matrix} \middle| \frac{1}{b^2x^2}\right) e^c}{2\pi}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erfc(b*x)/x**4,x)
[Out] -b**3*meijerg(((2, 5/2, 1), ()), ((2,), (0,)), 1/(b**2*x**2))*exp(c)/(2*pi)
```

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfc(b*x)/x^4,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(b^2*x^2 + c)/x^4, x)
```

Mupad [**F**]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{b^2\,x^2+c}\,\mathrm{erfc}(b\,x)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + b^2*x^2)*erfc(b*x))/x^4,x)
```

```
[Out] int((exp(c + b^2*x^2)*erfc(b*x))/x^4, x)
```

3.178 $\int e^{-b^2x^2}x^5\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=135

$$\frac{11e^{-2b^2x^2}x}{16b^5\sqrt{\pi}}+\frac{e^{-2b^2x^2}x^3}{4b^3\sqrt{\pi}}-\frac{43\text{Erf}\left(\sqrt{2}\,bx\right)}{32\sqrt{2}\,b^6}-\frac{e^{-b^2x^2}\text{Erfc}(bx)}{b^6}-\frac{e^{-b^2x^2}x^2\text{Erfc}(bx)}{b^4}-\frac{e^{-b^2x^2}x^4\text{Erfc}(bx)}{2b^2}$$

```
[Out] -erfc(b*x)/b^6/exp(b^2*x^2)-x^2*erfc(b*x)/b^4/exp(b^2*x^2)-1/2*x^4*erfc(b*x
)/b^2/exp(b^2*x^2)-43/64*erf(b*x*2^(1/2))/b^6*2^(1/2)+11/16*x/b^5/exp(2*b^2
*x^2)/Pi^(1/2)+1/4*x^3/b^3/exp(2*b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.13, antiderivative size = 135, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {6521, 6518, 2236, 2243}

$$-\frac{43\text{Erf}\left(\sqrt{2}\,bx\right)}{32\sqrt{2}\,b^6}-\frac{x^4e^{-b^2x^2}\text{Erfc}(bx)}{2b^2}-\frac{e^{-b^2x^2}\text{Erfc}(bx)}{b^6}+\frac{11xe^{-2b^2x^2}}{16\sqrt{\pi}\,b^5}-\frac{x^2e^{-b^2x^2}\text{Erfc}(bx)}{b^4}+\frac{x^3e^{-2b^2x^2}}{4\sqrt{\pi}\,b^3}$$

Antiderivative was successfully verified.

```
[In] Int[(x^5*Erfc[b*x])/E^(b^2*x^2),x]
```

```
[Out] (11*x)/(16*b^5*E^(2*b^2*x^2)*Sqrt[Pi]) + x^3/(4*b^3*E^(2*b^2*x^2)*Sqrt[Pi])
 - (43*Erf[Sqrt[2]*b*x])/(32*Sqrt[2]*b^6) - Erfc[b*x]/(b^6*E^(b^2*x^2)) - (
x^2*Erfc[b*x])/(b^4*E^(b^2*x^2)) - (x^4*Erfc[b*x])/(2*b^2*E^(b^2*x^2))
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
```

```
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{-b^2x^2}x^5\mathrm{erfc}(bx)\,dx &= -\frac{e^{-b^2x^2}x^4\mathrm{erfc}(bx)}{2b^2}+\frac{2\int e^{-b^2x^2}x^3\mathrm{erfc}(bx)\,dx}{b^2}-\frac{\int e^{-2b^2x^2}x^4\,dx}{b\sqrt{\pi}}\\ &= \frac{e^{-2b^2x^2}x^3}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x^2\mathrm{erfc}(bx)}{b^4}-\frac{e^{-b^2x^2}x^4\mathrm{erfc}(bx)}{2b^2}+\frac{2\int e^{-b^2x^2}x\mathrm{erfc}(bx)\,dx}{b^4}-\frac{3\int e^{-2}}{4b^3}\\ &= \frac{11e^{-2b^2x^2}x}{16b^5\sqrt{\pi}}+\frac{e^{-2b^2x^2}x^3}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}\mathrm{erfc}(bx)}{b^6}-\frac{e^{-b^2x^2}x^2\mathrm{erfc}(bx)}{b^4}-\frac{e^{-b^2x^2}x^4\mathrm{erfc}(bx)}{2b^2}-3\\ &= \frac{11e^{-2b^2x^2}x}{16b^5\sqrt{\pi}}+\frac{e^{-2b^2x^2}x^3}{4b^3\sqrt{\pi}}-\frac{43\mathrm{erf}\left(\sqrt{2}\,bx\right)}{32\sqrt{2}\,b^6}-\frac{e^{-b^2x^2}\mathrm{erfc}(bx)}{b^6}-\frac{e^{-b^2x^2}x^2\mathrm{erfc}(bx)}{b^4}-e^{-}\end{aligned}$$

Mathematica [A]
time = 0.09, size = 87, normalized size = 0.64

$$\frac{-43\sqrt{2}\,\mathrm{Erf}\left(\sqrt{2}\,bx\right)+4e^{-2b^2x^2}\left(\frac{bx(11+4b^2x^2)}{\sqrt{\pi}}-8e^{b^2x^2}(2+2b^2x^2+b^4x^4)\,\mathrm{Erfc}(bx)\right)}{64b^6}$$

Antiderivative was successfully verified.

```
[In] Integrate[(x^5*Erfc[b*x])/E^(b^2*x^2),x]
```

```
[Out] (-43*Sqrt[2]*Erf[Sqrt[2]*b*x] + (4*((b*x*(11 + 4*b^2*x^2))/Sqrt[Pi] - 8*E^(
b^2*x^2)*(2 + 2*b^2*x^2 + b^4*x^4)*Erfc[b*x]))/E^(2*b^2*x^2))/(64*b^6)
```

Maple [A]
time = 0.25, size = 172, normalized size = 1.27

method	result

default	$\frac{\frac{-\frac{b^4x^4\mathrm{e}^{-b^2x^2}}{2}-b^2x^2\mathrm{e}^{-b^2x^2}-\mathrm{e}^{-b^2x^2}}{b^5}-\frac{\mathrm{erf}(bx)\left(-\frac{b^4x^4\mathrm{e}^{-b^2x^2}}{2}-b^2x^2\mathrm{e}^{-b^2x^2}-\mathrm{e}^{-b^2x^2}\right)}{b^5}+\frac{-\frac{43\sqrt{2}\,\sqrt{\pi}\,\mathrm{erf}\left(bx\sqrt{2}\right)}{64}+\frac{\mathrm{e}^{-2b^2x^2}b^3x^3}{4}+}{\sqrt{\pi}\,b^5}}{b}$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*erfc(b*x)/exp(b^2*x^2),x,method=_RETURNVERBOSE)
```

```
[Out] (1/b^5*(-1/2*b^4*x^4/exp(b^2*x^2)-b^2*x^2/exp(b^2*x^2)-1/exp(b^2*x^2))-erf(
b*x)/b^5*(-1/2*b^4*x^4/exp(b^2*x^2)-b^2*x^2/exp(b^2*x^2)-1/exp(b^2*x^2))+1/
Pi^(1/2)/b^5*(-43/64*2^(1/2)*Pi^(1/2)*erf(b*x*2^(1/2))+1/4/exp(b^2*x^2)^2*b
^3*x^3+11/16/exp(b^2*x^2)^2*b*x))/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfc(b*x)/exp(b^2*x^2),x, algorithm="maxima")
```

```
[Out] integrate(x^5*erfc(b*x)*e^(-b^2*x^2), x)
```

Fricas [A]
time = 0.35, size = 121, normalized size = 0.90

$$-\frac{43\sqrt{2}\,\pi\sqrt{b^2}\,\operatorname{erf}\left(\sqrt{2}\,\sqrt{b^2}\,x\right)-4\sqrt{\pi}\,(4\,b^4x^3+11\,b^2x)e^{(-2\,b^2x^2)}+32\,(\pi b^5x^4+2\,\pi b^3x^2+2\,\pi b-(\pi b^5x^4+2\,\pi b^3x^2+2\,\pi b)\operatorname{erf}(bx))e^{(-b^2x^2)}}{64\,\pi b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfc(b*x)/exp(b^2*x^2),x, algorithm="fricas")
```

```
[Out] -1/64*(43*sqrt(2)*pi*sqrt(b^2)*erf(sqrt(2)*sqrt(b^2)*x) - 4*sqrt(pi)*(4*b^4
*x^3 + 11*b^2*x)*e^(-2*b^2*x^2) + 32*(pi*b^5*x^4 + 2*pi*b^3*x^2 + 2*pi*b -
(pi*b^5*x^4 + 2*pi*b^3*x^2 + 2*pi*b)*erf(b*x))*e^(-b^2*x^2))/(pi*b^7)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x^5e^{-b^2x^2}\operatorname{erfc}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**5*erfc(b*x)/exp(b**2*x**2),x)
```

```
[Out] Integral(x**5*exp(-b**2*x**2)*erfc(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfc(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(x^5*erfc(b*x)*e^(-b^2*x^2), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^5 \, \mathrm{e}^{-b^2 x^2} \, \mathrm{erfc}(b\, x) \; dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*exp(-b^2*x^2)*erfc(b*x),x)
```

```
[Out] int(x^5*exp(-b^2*x^2)*erfc(b*x), x)
```

3.179 $\int e^{-b^2x^2}x^3\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=90

$$\frac{e^{-2b^2x^2}x}{4b^3\sqrt{\pi}}-\frac{5\text{Erf}\left(\sqrt{2}\,bx\right)}{8\sqrt{2}\,b^4}-\frac{e^{-b^2x^2}\text{Erfc}(bx)}{2b^4}-\frac{e^{-b^2x^2}x^2\text{Erfc}(bx)}{2b^2}$$

```
[Out] -1/2*erfc(b*x)/b^4/exp(b^2*x^2)-1/2*x^2*erfc(b*x)/b^2/exp(b^2*x^2)-5/16*erf
(b*x*2^(1/2))/b^4*2^(1/2)+1/4*x/b^3/exp(2*b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.07, antiderivative size = 90, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}}=0.222$, Rules used = {6521, 6518, 2236, 2243}

$$-\frac{5\text{Erf}\left(\sqrt{2}\,bx\right)}{8\sqrt{2}\,b^4}-\frac{x^2e^{-b^2x^2}\text{Erfc}(bx)}{2b^2}-\frac{e^{-b^2x^2}\text{Erfc}(bx)}{2b^4}+\frac{xe^{-2b^2x^2}}{4\sqrt{\pi}\,b^3}$$

Antiderivative was successfully verified.

```
[In] Int[(x^3*Erfc[b*x])/E^(b^2*x^2),x]
```

```
[Out] x/(4*b^3*E^(2*b^2*x^2)*Sqrt[Pi]) - (5*Erf[Sqrt[2]*b*x])/(8*Sqrt[2]*b^4) - E
rfc[b*x]/(2*b^4*E^(b^2*x^2)) - (x^2*Erfc[b*x])/(2*b^2*E^(b^2*x^2))
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int e^{-b^2x^2}x^3\text{erfc}(bx)\,dx &= -\frac{e^{-b^2x^2}x^2\text{erfc}(bx)}{2b^2}+\frac{\int e^{-b^2x^2}x\text{erfc}(bx)\,dx}{b^2}-\frac{\int e^{-2b^2x^2}x^2\,dx}{b\sqrt{\pi}}\\
&= \frac{e^{-2b^2x^2}x}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}\text{erfc}(bx)}{2b^4}-\frac{e^{-b^2x^2}x^2\text{erfc}(bx)}{2b^2}-\frac{\int e^{-2b^2x^2}\,dx}{4b^3\sqrt{\pi}}-\frac{\int e^{-2b^2x^2}\,dx}{b^3\sqrt{\pi}}\\
&= \frac{e^{-2b^2x^2}x}{4b^3\sqrt{\pi}}-\frac{5\text{erf}\left(\sqrt{2}\,bx\right)}{8\sqrt{2}\,b^4}-\frac{e^{-b^2x^2}\text{erfc}(bx)}{2b^4}-\frac{e^{-b^2x^2}x^2\text{erfc}(bx)}{2b^2}
\end{aligned}$$

Mathematica [A]
time = 0.07, size = 69, normalized size = 0.77

$$\frac{-5\sqrt{2}\,\text{Erf}\left(\sqrt{2}\,bx\right)+4e^{-2b^2x^2}\left(\frac{bx}{\sqrt{\pi}}-2e^{b^2x^2}(1+b^2x^2)\,\text{Erfc}(bx)\right)}{16b^4}$$

Antiderivative was successfully verified.

```
[In] Integrate[(x^3*Erfc[b*x])/E^(b^2*x^2),x]
[Out] (-5*Sqrt[2]*Erf[Sqrt[2]*b*x] + (4*((b*x)/Sqrt[Pi] - 2*E^(b^2*x^2)*(1 + b^2*
x^2)*Erfc[b*x]))/E^(2*b^2*x^2))/(16*b^4)
```

Maple [A]
time = 0.58, size = 118, normalized size = 1.31

method	result	size
default	$\frac{\frac{-\frac{b^2x^2\mathrm{e}^{-b^2x^2}}{2}-\frac{\mathrm{e}^{-b^2x^2}}{2}}{b^3}-\frac{\mathrm{erf}(bx)\left(-\frac{b^2x^2\mathrm{e}^{-b^2x^2}}{2}-\frac{\mathrm{e}^{-b^2x^2}}{2}\right)}{b^3}+\frac{-\frac{5\sqrt{2}\,\sqrt{\pi}\,\mathrm{erf}\left(bx\sqrt{2}\right)}{16}+\frac{\mathrm{e}^{-2b^2x^2}bx}{4}}{\sqrt{\pi}\,b^3}}{b}$	118

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erfc(b*x)/exp(b^2*x^2),x,method=_RETURNVERBOSE)
```

```
[Out] (1/b^3*(-1/2*b^2*x^2/exp(b^2*x^2)-1/2/exp(b^2*x^2))-erf(b*x)/b^3*(-1/2*b^2*
x^2/exp(b^2*x^2)-1/2/exp(b^2*x^2))+1/Pi^(1/2)/b^3*(-5/16*2^(1/2)*Pi^(1/2)*e
rf(b*x*2^(1/2))+1/4/exp(b^2*x^2)^2*b*x))/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfc(b*x)/exp(b^2*x^2),x, algorithm="maxima")
```

```
[Out] integrate(x^3*erfc(b*x)*e^(-b^2*x^2), x)
```

Fricas [A]
time = 0.34, size = 90, normalized size = 1.00

$$\frac{4\sqrt{\pi}\,b^2xe^{(-2\,b^2x^2)}-5\,\sqrt{2}\,\pi\sqrt{b^2}\,\operatorname{erf}\left(\sqrt{2}\,\sqrt{b^2}\,x\right)-8\,(\pi b^3x^2+\pi b-(\pi b^3x^2+\pi b)\operatorname{erf}(bx))e^{(-b^2x^2)}}{16\,\pi b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfc(b*x)/exp(b^2*x^2),x, algorithm="fricas")
```

```
[Out] 1/16*(4*sqrt(pi)*b^2*x*e^(-2*b^2*x^2) - 5*sqrt(2)*pi*sqrt(b^2)*erf(sqrt(2)*
sqrt(b^2)*x) - 8*(pi*b^3*x^2 + pi*b - (pi*b^3*x^2 + pi*b)*erf(b*x))*e^(-b^2
*x^2))/(pi*b^5)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x^3e^{-b^2x^2}\operatorname{erfc}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3*erfc(b*x)/exp(b**2*x**2),x)
```

```
[Out] Integral(x**3*exp(-b**2*x**2)*erfc(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfc(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(x^3*erfc(b*x)*e^(-b^2*x^2), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^3\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfc}(b\,x)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*exp(-b^2*x^2)*erfc(b*x),x)
[Out] int(x^3*exp(-b^2*x^2)*erfc(b*x), x)
```

3.180 $\int e^{-b^2x^2} x\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=43

$$-\frac{\text{Erf}\left(\sqrt{2}\,bx\right)}{2\sqrt{2}\,b^2}-\frac{e^{-b^2x^2}\text{Erfc}(bx)}{2b^2}$$

```
[Out] -1/2*erfc(b*x)/b^2/exp(b^2*x^2)-1/4*erf(b*x*2^(1/2))/b^2*2^(1/2)
```

Rubi [A]
time = 0.02, antiderivative size = 43, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {6518, 2236}

$$-\frac{\text{Erf}\left(\sqrt{2}\,bx\right)}{2\sqrt{2}\,b^2}-\frac{e^{-b^2x^2}\text{Erfc}(bx)}{2b^2}$$

Antiderivative was successfully verified.

```
[In] Int[(x*Erfc[b*x])/E^(b^2*x^2),x]
```

```
[Out] -1/2*Erf[Sqrt[2]*b*x]/(Sqrt[2]*b^2) - Erfc[b*x]/(2*b^2*E^(b^2*x^2))
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\begin{aligned}\int e^{-b^2x^2}x\text{erfc}(bx)\,dx&=-\frac{e^{-b^2x^2}\text{erfc}(bx)}{2b^2}-\frac{\int e^{-2b^2x^2}\,dx}{b\sqrt{\pi}}\\&=-\frac{\text{erf}\left(\sqrt{2}\,bx\right)}{2\sqrt{2}\,b^2}-\frac{e^{-b^2x^2}\text{erfc}(bx)}{2b^2}\end{aligned}$$

Mathematica [A]
time = 0.02, size = 39, normalized size = 0.91

$$-\frac{\sqrt{2}\,\mathrm{Erf}\left(\sqrt{2}\,bx\right)+2e^{-b^2x^2}\mathrm{Erfc}(bx)}{4b^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[(x*Erfc[b*x])/E^(b^2*x^2),x]
```

```
[Out] -1/4*(Sqrt[2]*Erf[Sqrt[2]*b*x] + (2*Erfc[b*x])/E^(b^2*x^2))/b^2
```

Maple [A]
time = 0.35, size = 53, normalized size = 1.23

method	result	size
default	$\frac{-\frac{\mathrm{e}^{-b^2x^2}}{2b}+\frac{\mathrm{erf}(bx)\mathrm{e}^{-b^2x^2}}{2b}-\frac{\sqrt{2}\,\mathrm{erf}\left(bx\sqrt{2}\right)}{4b}}{b}$	53

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfc(b*x)/exp(b^2*x^2),x,method=_RETURNVERBOSE)
```

```
[Out] (-1/2/b*exp(-b^2*x^2)+1/2*erf(b*x)/b*exp(-b^2*x^2)-1/4/b*2^(1/2)*erf(b*x*2^
(1/2)))/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(b*x)/exp(b^2*x^2),x, algorithm="maxima")
```

```
[Out] integrate(x*erfc(b*x)*e^(-b^2*x^2), x)
```

Fricas [A]
time = 0.36, size = 47, normalized size = 1.09

$$-\frac{\sqrt{2}\,\sqrt{b^2}\,\mathrm{erf}\left(\sqrt{2}\,\sqrt{b^2}\,x\right)-2\,(b\,\mathrm{erf}\,(bx)-b)e^{(-b^2x^2)}}{4\,b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(b*x)/exp(b^2*x^2),x, algorithm="fricas")
```

```
[Out] -1/4*(sqrt(2)*sqrt(b^2)*erf(sqrt(2)*sqrt(b^2)*x) - 2*(b*erf(b*x) - b)*e^(-b
^2*x^2))/b^3
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int xe^{-b^2x^2}\operatorname{erfc}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(b*x)/exp(b**2*x**2),x)
```

```
[Out] Integral(x*exp(-b**2*x**2)*erfc(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfc(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(x*erfc(b*x)*e^(-b^2*x^2), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int x\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfc}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*exp(-b^2*x^2)*erfc(b*x),x)
```

```
[Out] int(x*exp(-b^2*x^2)*erfc(b*x), x)
```

3.181 $\int \frac{e^{-b^2x^2}\textbf{Erfc}(bx)}{x}\,dx$

Optimal. Leaf size=21

$$\operatorname{Int}\left(\frac{e^{-b^2x^2}\operatorname{Erfc}(bx)}{x},x\right)$$

[Out] Unintegrable(erfc(b*x)/exp(b^2*x^2)/x,x)

Rubi [A]
time = 0.02, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{-b^2x^2}\operatorname{Erfc}(bx)}{x}\,dx$$

Verification is not applicable to the result.

[In] Int[Erfc[b*x]/(E^(b^2*x^2)*x),x]

[Out] Defer[Int][Erfc[b*x]/(E^(b^2*x^2)*x), x]

Rubi steps

$$\int \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x}\,dx = \int \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x}\,dx$$

Mathematica [A]
time = 0.15, size = 0, normalized size = 0.00

$$\int \frac{e^{-b^2x^2}\operatorname{Erfc}(bx)}{x}\,dx$$

Verification is not applicable to the result.

[In] Integrate[Erfc[b*x]/(E^(b^2*x^2)*x),x]

[Out] Integrate[Erfc[b*x]/(E^(b^2*x^2)*x), x]

Maple [A]
time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}(bx)\,\mathrm{e}^{-b^2x^2}}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/exp(b^2*x^2)/x,x)
```

```
[Out] int(erfc(b*x)/exp(b^2*x^2)/x,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)*e^(-b^2*x^2)/x, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x,x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x) - 1)*e^(-b^2*x^2)/x, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b**2*x**2)/x,x)
```

```
[Out] Integral(exp(-b**2*x**2)*erfc(b*x)/x, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(-b^2*x^2)/x, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{\mathrm{e}^{-b^2 x^2} \operatorname{erfc}(b x)}{x} \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erfc(b*x))/x,x)
[Out] int((exp(-b^2*x^2)*erfc(b*x))/x, x)
```

3.182 $\int \frac{e^{-b^2x^2}\mathbf{Erfc}(bx)}{x^3}\,dx$

Optimal. Leaf size=86

$$\frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x}+\sqrt{2}\,b^2\mathrm{Erf}\left(\sqrt{2}\,bx\right)-\frac{e^{-b^2x^2}\mathrm{Erfc}(bx)}{2x^2}-b^2\mathrm{Int}\left(\frac{e^{-b^2x^2}\mathrm{Erfc}(bx)}{x},x\right)$$

```
[Out] -1/2*erfc(b*x)/exp(b^2*x^2)/x^2+b^2*erf(b*x*2^(1/2))*2^(1/2)+b/exp(2*b^2*x^
2)/x/Pi^(1/2)-b^2*Unintegrable(erfc(b*x)/exp(b^2*x^2)/x,x)
```

Rubi [A]
time = 0.06, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}}=0.000$, Rules used = {}

$$\int \frac{e^{-b^2x^2}\mathrm{Erfc}(bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erfc[b*x]/(E^(b^2*x^2)*x^3),x]
```

```
[Out] b/(E^(2*b^2*x^2)*Sqrt[Pi]*x) + Sqrt[2]*b^2*Erf[Sqrt[2]*b*x] - Erfc[b*x]/(2*
E^(b^2*x^2)*x^2) - b^2*Defer[Int][Erfc[b*x]/(E^(b^2*x^2)*x), x]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{-b^2x^2}\mathrm{erfc}(bx)}{x^3}\,dx&=-\frac{e^{-b^2x^2}\mathrm{erfc}(bx)}{2x^2}-b^2\int \frac{e^{-b^2x^2}\mathrm{erfc}(bx)}{x}\,dx-\frac{b\int \frac{e^{-2b^2x^2}}{x^2}\,dx}{\sqrt{\pi}}\\&=\frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\mathrm{erfc}(bx)}{2x^2}-b^2\int \frac{e^{-b^2x^2}\mathrm{erfc}(bx)}{x}\,dx+\frac{\left(4b^3\right)\int e^{-2b^2x^2}\,dx}{\sqrt{\pi}}\\&=\frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x}+\sqrt{2}\,b^2\mathrm{erf}\left(\sqrt{2}\,bx\right)-\frac{e^{-b^2x^2}\mathrm{erfc}(bx)}{2x^2}-b^2\int \frac{e^{-b^2x^2}\mathrm{erfc}(bx)}{x}\,dx\end{aligned}$$

Mathematica [A]
time = 0.21, size = 0, normalized size = 0.00

$$\int \frac{e^{-b^2x^2}\mathrm{Erfc}(bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfc[b*x]/(E^(b^2*x^2)*x^3),x]
```

```
[Out] Integrate[Erfc[b*x]/(E^(b^2*x^2)*x^3), x]
```

Maple [A]
time = 0.22, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}(bx)\,\mathrm{e}^{-b^2x^2}}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/exp(b^2*x^2)/x^3,x)
[Out] int(erfc(b*x)/exp(b^2*x^2)/x^3,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x^3,x, algorithm="maxima")
[Out] integrate(erfc(b*x)*e^(-b^2*x^2)/x^3, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x^3,x, algorithm="fricas")
[Out] integral(-(erf(b*x) - 1)*e^(-b^2*x^2)/x^3, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b**2*x**2)/x**3,x)
[Out] Integral(exp(-b**2*x**2)*erfc(b*x)/x**3, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x^3,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(-b^2*x^2)/x^3, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfc}(b\,x)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erfc(b*x))/x^3,x)
```

```
[Out] int((exp(-b^2*x^2)*erfc(b*x))/x^3, x)
```

3.183 $\int \frac{e^{-b^2x^2}\mathbf{Erfc}(bx)}{x^5}\,dx$

Optimal. Leaf size=162

$$\frac{be^{-2b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{7b^3e^{-2b^2x^2}}{6\sqrt{\pi}\,x}-\frac{b^4\text{Erf}\left(\sqrt{2}\,bx\right)}{\sqrt{2}}-\frac{2}{3}\sqrt{2}\,b^4\text{Erf}\left(\sqrt{2}\,bx\right)-\frac{e^{-b^2x^2}\text{Erfc}(bx)}{4x^4}+\frac{b^2e^{-b^2x^2}\text{Erfc}(bx)}{4x^2}+\frac{1}{2}b^4\text{Int}\left(\frac{e^{-b}}{}\right.$$

```
[Out] -1/4*erfc(b*x)/exp(b^2*x^2)/x^4+1/4*b^2*erfc(b*x)/exp(b^2*x^2)/x^2-7/6*b^4*
erf(b*x*2^(1/2))*2^(1/2)+1/6*b/exp(2*b^2*x^2)/x^3/Pi^(1/2)-7/6*b^3/exp(2*b^
2*x^2)/x/Pi^(1/2)+1/2*b^4*Unintegrable(erfc(b*x)/exp(b^2*x^2)/x,x)
```

Rubi [A]
time = 0.13, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{-b^2x^2}\text{Erfc}(bx)}{x^5}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erfc[b*x]/(E^(b^2*x^2)*x^5),x]
```

```
[Out] b/(6*E^(2*b^2*x^2)*Sqrt[Pi]*x^3) - (7*b^3)/(6*E^(2*b^2*x^2)*Sqrt[Pi]*x) - (
b^4*Erf[Sqrt[2]*b*x])/Sqrt[2] - (2*Sqrt[2]*b^4*Erf[Sqrt[2]*b*x])/3 - Erfc[b
*x]/(4*E^(b^2*x^2)*x^4) + (b^2*Erfc[b*x])/(4*E^(b^2*x^2)*x^2) + (b^4*Defer[
Int][Erfc[b*x]/(E^(b^2*x^2)*x), x])/2
```

Rubi steps

$$\begin{aligned}
\int \frac{e^{-b^2x^2}\text{erfc}(bx)}{x^5}\,dx &= -\frac{e^{-b^2x^2}\text{erfc}(bx)}{4x^4}-\frac{1}{2}b^2\int \frac{e^{-b^2x^2}\text{erfc}(bx)}{x^3}\,dx-\frac{b\int \frac{e^{-2b^2x^2}}{x^4}\,dx}{2\sqrt{\pi}}\\
&= \frac{be^{-2b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{e^{-b^2x^2}\text{erfc}(bx)}{4x^4}+\frac{b^2e^{-b^2x^2}\text{erfc}(bx)}{4x^2}+\frac{1}{2}b^4\int \frac{e^{-b^2x^2}\text{erfc}(bx)}{x}\,dx+\frac{b^3\int \frac{e^{-2b^2x^2}}{x^2}}{2\sqrt{\pi}}\\
&= \frac{be^{-2b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{7b^3e^{-2b^2x^2}}{6\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\text{erfc}(bx)}{4x^4}+\frac{b^2e^{-b^2x^2}\text{erfc}(bx)}{4x^2}+\frac{1}{2}b^4\int \frac{e^{-b^2x^2}\text{erfc}(bx)}{x}\,dx\\
&= \frac{be^{-2b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{7b^3e^{-2b^2x^2}}{6\sqrt{\pi}\,x}-\frac{b^4\text{erf}\left(\sqrt{2}\,bx\right)}{\sqrt{2}}-\frac{2}{3}\sqrt{2}\,b^4\text{erf}\left(\sqrt{2}\,bx\right)-\frac{e^{-b^2x^2}\text{erfc}(bx)}{4x^4}+\frac{b^2e}{}
\end{aligned}$$

Mathematica [A]
time = 0.20, size = 0, normalized size = 0.00

$$\int \frac{e^{-b^2x^2}\text{Erfc}(bx)}{x^5}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfc[b*x]/(E^(b^2*x^2)*x^5),x]
```

```
[Out] Integrate[Erfc[b*x]/(E^(b^2*x^2)*x^5), x]
```

Maple [A]
time = 0.22, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}(bx)\,\mathrm{e}^{-b^2x^2}}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/exp(b^2*x^2)/x^5,x)
```

```
[Out] int(erfc(b*x)/exp(b^2*x^2)/x^5,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x^5,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)*e^(-b^2*x^2)/x^5, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x^5,x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x) - 1)*e^(-b^2*x^2)/x^5, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b**2*x**2)/x**5,x)
```

```
[Out] Integral(exp(-b**2*x**2)*erfc(b*x)/x**5, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x^5,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(-b^2*x^2)/x^5, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{e^{-b^2 x^2} \operatorname{erfc}(b x)}{x^5} \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erfc(b*x))/x^5,x)
```

```
[Out] int((exp(-b^2*x^2)*erfc(b*x))/x^5, x)
```

3.184 $\int e^{-b^2x^2}x^4\textbf{Erfc}(bx)\,dx$

Optimal. Leaf size=112

$$\frac{e^{-2b^2x^2}}{2b^5\sqrt{\pi}}+\frac{e^{-2b^2x^2}x^2}{4b^3\sqrt{\pi}}-\frac{3e^{-b^2x^2}x\text{Erfc}(bx)}{4b^4}-\frac{e^{-b^2x^2}x^3\text{Erfc}(bx)}{2b^2}-\frac{3\sqrt{\pi}\,\text{Erfc}(bx)^2}{16b^5}$$

```
[Out] -3/4*x*erfc(b*x)/b^4/exp(b^2*x^2)-1/2*x^3*erfc(b*x)/b^2/exp(b^2*x^2)+1/2/b^
5/exp(2*b^2*x^2)/Pi^(1/2)+1/4*x^2/b^3/exp(2*b^2*x^2)/Pi^(1/2)-3/16*erfc(b*x
)^2*Pi^(1/2)/b^5
```

Rubi [A]
time = 0.09, antiderivative size = 112, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}}=0.278$, Rules used = {6521, 6509, 30, 2240, 2243}

$$-\frac{3\sqrt{\pi}\,\text{Erfc}(bx)^2}{16b^5}-\frac{x^3e^{-b^2x^2}\text{Erfc}(bx)}{2b^2}+\frac{e^{-2b^2x^2}}{2\sqrt{\pi}\,b^5}-\frac{3xe^{-b^2x^2}\text{Erfc}(bx)}{4b^4}+\frac{x^2e^{-2b^2x^2}}{4\sqrt{\pi}\,b^3}$$

Antiderivative was successfully verified.

```
[In] Int[(x^4*Erfc[b*x])/E^(b^2*x^2),x]
```

```
[Out] 1/(2*b^5*E^(2*b^2*x^2)*Sqrt[Pi]) + x^2/(4*b^3*E^(2*b^2*x^2)*Sqrt[Pi]) - (3*
x*Erfc[b*x])/(4*b^4*E^(b^2*x^2)) - (x^3*Erfc[b*x])/(2*b^2*E^(b^2*x^2)) - (3
*Sqrt[Pi]*Erfc[b*x]^2)/(16*b^5)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$
\begin{aligned}
\int e^{-b^2x^2}x^4\operatorname{erfc}(bx)\,dx &= -\frac{e^{-b^2x^2}x^3\operatorname{erfc}(bx)}{2b^2}+\frac{3\int e^{-b^2x^2}x^2\operatorname{erfc}(bx)\,dx}{2b^2}-\frac{\int e^{-2b^2x^2}x^3\,dx}{b\sqrt{\pi}}\\
&= \frac{e^{-2b^2x^2}x^2}{4b^3\sqrt{\pi}}-\frac{3e^{-b^2x^2}x\operatorname{erfc}(bx)}{4b^4}-\frac{e^{-b^2x^2}x^3\operatorname{erfc}(bx)}{2b^2}+\frac{3\int e^{-b^2x^2}\operatorname{erfc}(bx)\,dx}{4b^4}-\frac{\int e^{-2b^2x^2}\cdots}{2b^3\sqrt{\cdots}}\\
&= \frac{e^{-2b^2x^2}}{2b^5\sqrt{\pi}}+\frac{e^{-2b^2x^2}x^2}{4b^3\sqrt{\pi}}-\frac{3e^{-b^2x^2}x\operatorname{erfc}(bx)}{4b^4}-\frac{e^{-b^2x^2}x^3\operatorname{erfc}(bx)}{2b^2}-\frac{\left(3\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx\cdots\right)}{8b^5}\\
&= \frac{e^{-2b^2x^2}}{2b^5\sqrt{\pi}}+\frac{e^{-2b^2x^2}x^2}{4b^3\sqrt{\pi}}-\frac{3e^{-b^2x^2}x\operatorname{erfc}(bx)}{4b^4}-\frac{e^{-b^2x^2}x^3\operatorname{erfc}(bx)}{2b^2}-\frac{3\sqrt{\pi}\operatorname{erfc}(bx)^2}{16b^5}
\end{aligned}
$$

Mathematica [A]
time = 0.10, size = 112, normalized size = 1.00

$$
-\frac{-4e^{-2b^2x^2}(2+b^2x^2)+4be^{-b^2x^2}\sqrt{\pi}\,x(3+2b^2x^2)-6\pi\operatorname{Erf}(bx)-4be^{-b^2x^2}\sqrt{\pi}\,x(3+2b^2x^2)\operatorname{Erf}(bx)+3\pi\operatorname{Erf}(bx)^2}{16b^5\sqrt{\pi}}
$$

Antiderivative was successfully verified.

```
[In] Integrate[(x^4*Erfc[b*x])/E^(b^2*x^2),x]
```

```
[Out] -1/16*((-4*(2 + b^2*x^2))/E^(2*b^2*x^2) + (4*b*Sqrt[Pi]*x*(3 + 2*b^2*x^2))/
E^(b^2*x^2) - 6*Pi*Erf[b*x] - (4*b*Sqrt[Pi]*x*(3 + 2*b^2*x^2)*Erf[b*x])/E^(
b^2*x^2) + 3*Pi*Erf[b*x]^2)/(b^5*Sqrt[Pi])
```

Maple [F]
time = 0.13, size = 0, normalized size = 0.00

$$
\int x^4\operatorname{erfc}(bx)\,\mathrm{e}^{-b^2x^2}\,dx
$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erfc(b*x)/exp(b^2*x^2),x)
```

```
[Out] int(x^4*erfc(b*x)/exp(b^2*x^2),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfc(b*x)/exp(b^2*x^2),x, algorithm="maxima")
```

```
[Out] integrate(x^4*erfc(b*x)*e^(-b^2*x^2), x)
```

Fricas [A]
time = 0.35, size = 97, normalized size = 0.87

$$-\frac{4\,(2\,\pi b^3x^3+3\,\pi bx-(2\,\pi b^3x^3+3\,\pi bx)\operatorname{erf}(bx))e^{(-b^2x^2)}+\sqrt{\pi}\left(3\,\pi\operatorname{erf}(bx)^2-6\,\pi\operatorname{erf}(bx)-4\,(b^2x^2+2)e^{(-2\,b^2x^2)}\right)}{16\,\pi b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfc(b*x)/exp(b^2*x^2),x, algorithm="fricas")
```

```
[Out] -1/16*(4*(2*pi*b^3*x^3 + 3*pi*b*x - (2*pi*b^3*x^3 + 3*pi*b*x)*erf(b*x))*e^(
-b^2*x^2) + sqrt(pi)*(3*pi*erf(b*x)^2 - 6*pi*erf(b*x) - 4*(b^2*x^2 + 2)*e^(
-2*b^2*x^2)))/(pi*b^5)
```

Sympy [A]
time = 7.53, size = 112, normalized size = 1.00

$$\begin{cases} -\frac{x^3e^{-b^2x^2}\operatorname{erfc}(bx)}{2b^2}+\frac{x^2e^{-2b^2x^2}}{4\sqrt{\pi}\,b^3}-\frac{3xe^{-b^2x^2}\operatorname{erfc}(bx)}{4b^4}-\frac{3\sqrt{\pi}\operatorname{erfc}^2(bx)}{16b^5}+\frac{e^{-2b^2x^2}}{2\sqrt{\pi}\,b^5} & \text{for } b\neq 0\\ \frac{x^5}{5} & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4*erfc(b*x)/exp(b**2*x**2),x)
```

```
[Out] Piecewise((-x**3*exp(-b**2*x**2)*erfc(b*x)/(2*b**2) + x**2*exp(-2*b**2*x**2
)/(4*sqrt(pi)*b**3) - 3*x*exp(-b**2*x**2)*erfc(b*x)/(4*b**4) - 3*sqrt(pi)*e
rfc(b*x)**2/(16*b**5) + exp(-2*b**2*x**2)/(2*sqrt(pi)*b**5), Ne(b, 0)), (x*
*5/5, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfc(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(x^4*erfc(b*x)*e^(-b^2*x^2), x)
```

Mupad [B]
time = 0.20, size = 90, normalized size = 0.80

$$\frac{8\,\mathrm{e}^{-2\,b^2\,x^2}-3\,\pi\,\mathrm{erfc}(b\,x)^2}{16\,b^5\,\sqrt{\pi}}+\frac{x^2\,\mathrm{e}^{-2\,b^2\,x^2}}{4\,b^3\,\sqrt{\pi}}-\frac{3\,x\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfc}(b\,x)}{4\,b^4}-\frac{x^3\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfc}(b\,x)}{2\,b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*exp(-b^2*x^2)*erfc(b*x),x)
```

```
[Out] (8*exp(-2*b^2*x^2) - 3*pi*erfc(b*x)^2)/(16*b^5*pi^(1/2)) + (x^2*exp(-2*b^2*
x^2))/(4*b^3*pi^(1/2)) - (3*x*exp(-b^2*x^2)*erfc(b*x))/(4*b^4) - (x^3*exp(-
b^2*x^2)*erfc(b*x))/(2*b^2)
```

3.185 $\int e^{-b^2x^2}x^2\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=63

$$\frac{e^{-2b^2x^2}}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x\mathrm{Erfc}(bx)}{2b^2}-\frac{\sqrt{\pi}\,\mathrm{Erfc}(bx)^2}{8b^3}$$

```
[Out] -1/2*x*erfc(b*x)/b^2/exp(b^2*x^2)+1/4/b^3/exp(2*b^2*x^2)/Pi^(1/2)-1/8*erfc(
b*x)^2*Pi^(1/2)/b^3
```

Rubi [A]
time = 0.04, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {6521, 6509, 30, 2240}

$$-\frac{\sqrt{\pi}\,\mathrm{Erfc}(bx)^2}{8b^3}-\frac{xe^{-b^2x^2}\mathrm{Erfc}(bx)}{2b^2}+\frac{e^{-2b^2x^2}}{4\sqrt{\pi}\,b^3}$$

Antiderivative was successfully verified.

```
[In] Int[(x^2*Erfc[b*x])/E^(b^2*x^2),x]
```

```
[Out] 1/(4*b^3*E^(2*b^2*x^2)*Sqrt[Pi]) - (x*Erfc[b*x])/(2*b^2*E^(b^2*x^2)) - (Sqr
t[Pi]*Erfc[b*x]^2)/(8*b^3)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
```

```
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int e^{-b^2x^2}x^2\operatorname{erfc}(bx)\,dx &= -\frac{e^{-b^2x^2}x\operatorname{erfc}(bx)}{2b^2}+\frac{\int e^{-b^2x^2}\operatorname{erfc}(bx)\,dx}{2b^2}-\frac{\int e^{-2b^2x^2}x\,dx}{b\sqrt{\pi}}\\
&= \frac{e^{-2b^2x^2}}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x\operatorname{erfc}(bx)}{2b^2}-\frac{\sqrt{\pi}\,\operatorname{Subst}(\int x\,dx,x,\operatorname{erfc}(bx))}{4b^3}\\
&= \frac{e^{-2b^2x^2}}{4b^3\sqrt{\pi}}-\frac{e^{-b^2x^2}x\operatorname{erfc}(bx)}{2b^2}-\frac{\sqrt{\pi}\,\operatorname{erfc}(bx)^2}{8b^3}
\end{aligned}$$

Mathematica [A]
time = 0.08, size = 79, normalized size = 1.25

$$\frac{2e^{-2b^2x^2}\left(\frac{1}{\sqrt{\pi}}-2be^{b^2x^2}x\right)+\left(2\sqrt{\pi}+4be^{-b^2x^2}x\right)\operatorname{Erf}(bx)-\sqrt{\pi}\operatorname{Erf}(bx)^2}{8b^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[(x^2*Erfc[b*x])/E^(b^2*x^2),x]
```

```
[Out] ((2*(1/Sqrt[Pi] - 2*b*E^(b^2*x^2)*x))/E^(2*b^2*x^2) + (2*Sqrt[Pi] + (4*b*x)
/E^(b^2*x^2))*Erf[b*x] - Sqrt[Pi]*Erf[b*x]^2)/(8*b^3)
```

Maple [F]
time = 0.12, size = 0, normalized size = 0.00

$$\int x^2\operatorname{erfc}(bx)\,\mathrm{e}^{-b^2x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfc(b*x)/exp(b^2*x^2),x)
```

```
[Out] int(x^2*erfc(b*x)/exp(b^2*x^2),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfc(b*x)/exp(b^2*x^2),x, algorithm="maxima")
```

```
[Out] integrate(x^2*erfc(b*x)*e^(-b^2*x^2), x)
```

Fricas [A]
time = 0.35, size = 66, normalized size = 1.05

$$\frac{4\,(\pi bx\,\mathrm{erf}\,(bx) - \pi bx)e^{(-b^2x^2)} - \sqrt{\pi}\,\left(\pi\,\mathrm{erf}\,(bx)^2 - 2\,\pi\,\mathrm{erf}\,(bx) - 2\,e^{(-2\,b^2x^2)}\right)}{8\,\pi b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfc(b*x)/exp(b^2*x^2),x, algorithm="fricas")
```

```
[Out] 1/8*(4*(pi*b*x*erf(b*x) - pi*b*x)*e^(-b^2*x^2) - sqrt(pi)*(pi*erf(b*x)^2 -
2*pi*erf(b*x) - 2*e^(-2*b^2*x^2)))/(pi*b^3)
```

Sympy [A]
time = 1.36, size = 63, normalized size = 1.00

$$\begin{cases} -\frac{xe^{-b^2x^2}\,\mathrm{erfc}\,(bx)}{2b^2} - \frac{\sqrt{\pi}\,\mathrm{erfc}^2\,(bx)}{8b^3} + \frac{e^{-2b^2x^2}}{4\sqrt{\pi}\,b^3} & \text{for } b \neq 0 \\ \frac{x^3}{3} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*erfc(b*x)/exp(b**2*x**2),x)
```

```
[Out] Piecewise((-x*exp(-b**2*x**2)*erfc(b*x)/(2*b**2) - sqrt(pi)*erfc(b*x)**2/(8
*b**3) + exp(-2*b**2*x**2)/(4*sqrt(pi)*b**3), Ne(b, 0)), (x**3/3, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfc(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(x^2*erfc(b*x)*e^(-b^2*x^2), x)
```

Mupad [B]
time = 0.19, size = 49, normalized size = 0.78

$$\frac{2\,\mathrm{e}^{-2\,b^2\,x^2} - \pi\,\mathrm{erfc}(b\,x)^2}{8\,b^3\,\sqrt{\pi}} - \frac{x\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfc}(b\,x)}{2\,b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*exp(-b^2*x^2)*erfc(b*x),x)
```

```
[Out] (2*exp(-2*b^2*x^2) - pi*erfc(b*x)^2)/(8*b^3*pi^(1/2)) - (x*exp(-b^2*x^2)*er
fc(b*x))/(2*b^2)
```

3.186 $\int e^{-b^2x^2}\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=18

$$-\frac{\sqrt{\pi}\,\mathrm{Erfc}(bx)^2}{4b}$$

```
[Out] -1/4*erfc(b*x)^2*Pi^(1/2)/b
```

Rubi [A]
time = 0.01, antiderivative size = 18, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.133$, Rules used = {6509, 30}

$$-\frac{\sqrt{\pi}\,\mathrm{Erfc}(bx)^2}{4b}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]/E^(b^2*x^2),x]
```

```
[Out] -1/4*(Sqrt[Pi]*Erfc[b*x]^2)/b
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rubi steps

$$\begin{aligned}\int e^{-b^2x^2}\mathrm{erfc}(bx)\,dx &= -\frac{\sqrt{\pi}\,\mathrm{Subst}\left(\int x\,dx, x, \mathrm{erfc}(bx)\right)}{2b}\\ &= -\frac{\sqrt{\pi}\,\mathrm{erfc}(bx)^2}{4b}\end{aligned}$$

Mathematica [A]
time = 0.00, size = 18, normalized size = 1.00

$$-\frac{\sqrt{\pi}\,\mathrm{Erfc}(bx)^2}{4b}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]/E^(b^2*x^2),x]
```

```
[Out] -1/4*(Sqrt[Pi]*Erfc[b*x]^2)/b
```

Maple [A]
time = 0.14, size = 22, normalized size = 1.22

method	result	size
default	$\frac{\sqrt{\pi}\,\left(-\frac{\operatorname{erf}(bx)^2}{2}+\operatorname{erf}(bx)\right)}{2b}$	22

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/exp(b^2*x^2),x,method=_RETURNVERBOSE)
```

```
[Out] 1/2*Pi^(1/2)/b*(-1/2*erf(b*x)^2+erf(b*x))
```

Maxima [A]
time = 0.26, size = 14, normalized size = 0.78

$$-\frac{\sqrt{\pi}\,\operatorname{erfc}\left(bx\right)^2}{4\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2),x, algorithm="maxima")
```

```
[Out] -1/4*sqrt(pi)*erfc(b*x)^2/b
```

Fricas [A]
time = 0.35, size = 21, normalized size = 1.17

$$-\frac{\sqrt{\pi}\,\left(\operatorname{erf}\left(bx\right)^2-2\,\operatorname{erf}\left(bx\right)\right)}{4\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2),x, algorithm="fricas")
```

```
[Out] -1/4*sqrt(pi)*(erf(b*x)^2 - 2*erf(b*x))/b
```

Sympy [A]
time = 0.34, size = 17, normalized size = 0.94

$$\begin{cases} -\frac{\sqrt{\pi}\,\operatorname{erfc}^{2}\left(bx\right)}{4b} & \text{for}\ b\neq 0\\ x & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b**2*x**2),x)
```

```
[Out] Piecewise((-sqrt(pi)*erfc(b*x)**2/(4*b), Ne(b, 0)), (x, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(-b^2*x^2), x)
```

Mupad [B]
time = 0.07, size = 14, normalized size = 0.78

$$-\frac{\sqrt{\pi}\,\mathrm{erfc}(b\,x)^2}{4\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(-b^2*x^2)*erfc(b*x),x)
```

```
[Out] -(pi^(1/2)*erfc(b*x)^2)/(4*b)
```

3.187 $\int \frac{e^{-b^2x^2}\mathbf{Erfc}(bx)}{x^2}\,dx$

Optimal. Leaf size=53

$$-\frac{e^{-b^2x^2}\text{Erfc}(bx)}{x}+\frac{1}{2}b\sqrt{\pi}\,\text{Erfc}(bx)^2-\frac{b\text{Ei}(-2b^2x^2)}{\sqrt{\pi}}$$

```
[Out] -erfc(b*x)/exp(b^2*x^2)/x-b*Ei(-2*b^2*x^2)/Pi^(1/2)+1/2*b*erfc(b*x)^2*Pi^(1
/2)
```

Rubi [A]
time = 0.05, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.222, Rules used = {6527, 6509, 30, 2241}

$$-\frac{e^{-b^2x^2}\text{Erfc}(bx)}{x}-\frac{b\text{Ei}(-2b^2x^2)}{\sqrt{\pi}}+\frac{1}{2}\sqrt{\pi}\,b\text{Erfc}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]/(E^(b^2*x^2)*x^2),x]
```

```
[Out] -(Erfc[b*x]/(E^(b^2*x^2)*x)) + (b*Sqrt[Pi]*Erfc[b*x]^2)/2 - (b*ExpIntegralE
i[-2*b^2*x^2])/Sqrt[Pi]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6527

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[2*(b/((m
```

```
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x],
x]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x^2}\,dx &= -\frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x} - \left(2b^2\right)\int e^{-b^2x^2}\operatorname{erfc}(bx)\,dx - \frac{(2b)\int \frac{e^{-2b^2x^2}}{x}\,dx}{\sqrt{\pi}} \\
&= -\frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x} - \frac{b\operatorname{Ei}\left(-2b^2x^2\right)}{\sqrt{\pi}} + \left(b\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx, x, \operatorname{erfc}(bx)\right) \\
&= -\frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x} + \frac{1}{2}b\sqrt{\pi}\operatorname{erfc}(bx)^2 - \frac{b\operatorname{Ei}\left(-2b^2x^2\right)}{\sqrt{\pi}}
\end{aligned}
$$

Mathematica [A]
time = 0.01, size = 53, normalized size = 1.00

$$
-\frac{e^{-b^2x^2}\operatorname{Erfc}(bx)}{x} + \frac{1}{2}b\sqrt{\pi}\operatorname{Erfc}(bx)^2 - \frac{b\operatorname{Ei}\left(-2b^2x^2\right)}{\sqrt{\pi}}
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]/(E^(b^2*x^2)*x^2),x]
[Out] -(Erfc[b*x]/(E^(b^2*x^2)*x)) + (b*Sqrt[Pi]*Erfc[b*x]^2)/2 - (b*ExpIntegralE
i[-2*b^2*x^2])/Sqrt[Pi]
```

Maple [F]
time = 0.14, size = 0, normalized size = 0.00

$$
\int \frac{\operatorname{erfc}(bx)\,\mathrm{e}^{-b^2x^2}}{x^2}\,dx
$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/exp(b^2*x^2)/x^2,x)
[Out] int(erfc(b*x)/exp(b^2*x^2)/x^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x^2,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)*e^(-b^2*x^2)/x^2, x)
```

Fricas [A]
time = 0.35, size = 77, normalized size = 1.45

$$-\frac{2\,\pi^{\frac{3}{2}}\sqrt{b^2}\,x\,\mathrm{erf}\left(\sqrt{b^2}\,x\right)+2\,(\pi-\pi\,\mathrm{erf}\,(bx))e^{\left(-b^2x^2\right)}-\sqrt{\pi}\,\left(\pi bx\,\mathrm{erf}\,(bx)^2-2\,bx\mathrm{Ei}(-2\,b^2x^2)\right)}{2\,\pi x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x^2,x, algorithm="fricas")
```

```
[Out] -1/2*(2*pi^(3/2)*sqrt(b^2)*x*erf(sqrt(b^2)*x) + 2*(pi - pi*erf(b*x))*e^(-b^
2*x^2) - sqrt(pi)*(pi*b*x*erf(b*x)^2 - 2*b*x*Ei(-2*b^2*x^2)))/(pi*x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int\frac{e^{-b^2x^2}\,\mathrm{erfc}\,(bx)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b**2*x**2)/x**2,x)
```

```
[Out] Integral(exp(-b**2*x**2)*erfc(b*x)/x**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x^2,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(-b^2*x^2)/x^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int\frac{\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfc}(b\,x)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erfc(b*x))/x^2,x)
```

```
[Out] int((exp(-b^2*x^2)*erfc(b*x))/x^2, x)
```

3.188 $\int \frac{e^{-b^2x^2}\mathbf{Erfc}(bx)}{x^4}\,dx$

Optimal. Leaf size=108

$$\frac{be^{-2b^2x^2}}{3\sqrt{\pi}\,x^2}-\frac{e^{-b^2x^2}\text{Erfc}(bx)}{3x^3}+\frac{2b^2e^{-b^2x^2}\text{Erfc}(bx)}{3x}-\frac{1}{3}b^3\sqrt{\pi}\,\text{Erfc}(bx)^2+\frac{4b^3\text{Ei}(-2b^2x^2)}{3\sqrt{\pi}}$$

```
[Out] -1/3*erfc(b*x)/exp(b^2*x^2)/x^3+2/3*b^2*erfc(b*x)/exp(b^2*x^2)/x+1/3*b/exp(
2*b^2*x^2)/x^2/Pi^(1/2)+4/3*b^3*Ei(-2*b^2*x^2)/Pi^(1/2)-1/3*b^3*erfc(b*x)^2
*Pi^(1/2)
```

Rubi [A]
time = 0.10, antiderivative size = 108, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.278$, Rules used = {6527, 6509, 30, 2241, 2245}

$$-\frac{1}{3}\sqrt{\pi}\,b^3\text{Erfc}(bx)^2+\frac{2b^2e^{-b^2x^2}\text{Erfc}(bx)}{3x}-\frac{e^{-b^2x^2}\text{Erfc}(bx)}{3x^3}+\frac{be^{-2b^2x^2}}{3\sqrt{\pi}\,x^2}+\frac{4b^3\text{Ei}(-2b^2x^2)}{3\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]/(E^(b^2*x^2)*x^4),x]
```

```
[Out] b/(3*E^(2*b^2*x^2)*Sqrt[Pi]*x^2) - Erfc[b*x]/(3*E^(b^2*x^2)*x^3) + (2*b^2*E
rfc[b*x])/(3*E^(b^2*x^2)*x) - (b^3*Sqrt[Pi]*Erfc[b*x]^2)/3 + (4*b^3*ExpInte
gralEi[-2*b^2*x^2])/(3*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6527

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x],
x]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x^4}\,dx &= -\frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{3x^3} - \frac{1}{3}(2b^2)\int \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x^2}\,dx - \frac{(2b)\int \frac{e^{-2b^2x^2}}{x^3}\,dx}{3\sqrt{\pi}}\\ &= \frac{be^{-2b^2x^2}}{3\sqrt{\pi}\,x^2} - \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{3x^3} + \frac{2b^2e^{-b^2x^2}\operatorname{erfc}(bx)}{3x} + \frac{1}{3}(4b^4)\int e^{-b^2x^2}\operatorname{erfc}(bx)\,dx + 2\frac{(4b^3\\ &= \frac{be^{-2b^2x^2}}{3\sqrt{\pi}\,x^2} - \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{3x^3} + \frac{2b^2e^{-b^2x^2}\operatorname{erfc}(bx)}{3x} + \frac{4b^3\operatorname{Ei}(-2b^2x^2)}{3\sqrt{\pi}} - \frac{1}{3}(2b^3\sqrt{\pi})\,\text{Subst}\\ &= \frac{be^{-2b^2x^2}}{3\sqrt{\pi}\,x^2} - \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{3x^3} + \frac{2b^2e^{-b^2x^2}\operatorname{erfc}(bx)}{3x} - \frac{1}{3}b^3\sqrt{\pi}\operatorname{erfc}(bx)^2 + \frac{4b^3\operatorname{Ei}(-2b^2x^2)}{3\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.05, size = 85, normalized size = 0.79

$$\frac{1}{3}\left(\frac{e^{-b^2x^2}(-1+2b^2x^2)\operatorname{Erfc}(bx)}{x^3} - b^3\sqrt{\pi}\operatorname{Erfc}(bx)^2 + \frac{b\left(\frac{e^{-2b^2x^2}}{x^2}+4b^2\operatorname{Ei}(-2b^2x^2)\right)}{\sqrt{\pi}}\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]/(E^(b^2*x^2)*x^4),x]
```

```
[Out] (((-1 + 2*b^2*x^2)*Erfc[b*x])/(E^(b^2*x^2)*x^3) - b^3*Sqrt[Pi]*Erfc[b*x]^2
+ (b*(1/(E^(2*b^2*x^2)*x^2) + 4*b^2*ExpIntegralEi[-2*b^2*x^2]))/Sqrt[Pi])/3
```

Maple [F]
time = 0.18, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfc}(bx)\,\mathrm{e}^{-b^2x^2}}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/exp(b^2*x^2)/x^4,x)
```

```
[Out] int(erfc(b*x)/exp(b^2*x^2)/x^4,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x^4,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x)*e^(-b^2*x^2)/x^4, x)
```

Fricas [A]
time = 0.37, size = 122, normalized size = 1.13

$$\frac{2\,\pi^{\frac{3}{2}}\sqrt{b^2}\,b^2x^3\,\mathrm{erf}\left(\sqrt{b^2}\,x\right) - (\pi - 2\,\pi b^2x^2 - (\pi - 2\,\pi b^2x^2)\,\mathrm{erf}\,(bx))e^{(-b^2x^2)} - \sqrt{\pi}\left(\pi b^3x^3\,\mathrm{erf}\,(bx)^2 - 4\,b^3x^3\mathrm{Ei}(-2\,b^2x^2) - bxe^{(-2\,b^2x^2)}\right)}{3\,\pi x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x^4,x, algorithm="fricas")
```

```
[Out] 1/3*(2*pi^(3/2)*sqrt(b^2)*b^2*x^3*erf(sqrt(b^2)*x) - (pi - 2*pi*b^2*x^2 - (
pi - 2*pi*b^2*x^2)*erf(b*x))*e^(-b^2*x^2) - sqrt(pi)*(pi*b^3*x^3*erf(b*x)^2
 - 4*b^3*x^3*Ei(-2*b^2*x^2) - b*x*e^(-2*b^2*x^2)))/(pi*x^3)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{e^{-b^2x^2}\,\mathrm{erfc}\,(bx)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b**2*x**2)/x**4,x)
```

```
[Out] Integral(exp(-b**2*x**2)*erfc(b*x)/x**4, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x^4,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*e^(-b^2*x^2)/x^4, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfc}(b\,x)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erfc(b*x))/x^4,x)
[Out] int((exp(-b^2*x^2)*erfc(b*x))/x^4, x)
```

3.189 $\int e^{c+dx^2}x^3\mathbf{Erfc}(a+bx)\,dx$

Optimal. Leaf size=342

$$\frac{ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2d\sqrt{\pi}}-\frac{be^{-a^2+c-2abx-(b^2-d)x^2}x}{2(b^2-d)d\sqrt{\pi}}-\frac{be^{c+\frac{a^2d}{b^2-d}}\mathrm{Erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)}{2\sqrt{b^2-d}\,d^2}+\frac{a^2b^3e^{c+\frac{a^2d}{b^2-d}}\mathrm{Erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)}{2(b^2-d)^{5/2}d}+\frac{be}{}$$

```
[Out] 1/2*a^2*b^3*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)/(b^2-d)^(1/2))/(b^2-d)
^(5/2)/d+1/4*b*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)/(b^2-d)^(1/2))/(b^2
-d)^(3/2)/d-1/2*exp(d*x^2+c)*erfc(b*x+a)/d^2+1/2*exp(d*x^2+c)*x^2*erfc(b*x+
a)/d-1/2*b*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)/(b^2-d)^(1/2))/d^2/(b^2
-d)^(1/2)+1/2*a*b^2*exp(-a^2+c-2*a*b*x-(b^2-d)*x^2)/(b^2-d)^2/d/Pi^(1/2)-1/
2*b*exp(-a^2+c-2*a*b*x-(b^2-d)*x^2)*x/(b^2-d)/d/Pi^(1/2)
```

Rubi [A]
time = 0.31, antiderivative size = 342, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {6521, 6518, 2266, 2236, 2273, 2272}

$$-\frac{be^{\frac{a^2d}{b^2-d}+c}\mathrm{Erf}\left(\frac{ab+x(b^2-d)}{\sqrt{b^2-d}}\right)}{2d^2\sqrt{b^2-d}}+\frac{be^{\frac{a^2d}{b^2-d}+c}\mathrm{Erf}\left(\frac{ab+x(b^2-d)}{\sqrt{b^2-d}}\right)}{4d(b^2-d)^{3/2}}+\frac{ab^2e^{-a^2-2abx-x^2(b^2-d)+c}}{2\sqrt{\pi}d(b^2-d)^2}-\frac{bxe^{-a^2-2abx-x^2(b^2-d)+c}}{2\sqrt{\pi}d(b^2-d)}+\frac{a^2b^3e^{\frac{a^2d}{b^2-d}+c}\mathrm{Erf}\left(\frac{ab+x(b^2-d)}{\sqrt{b^2-d}}\right)}{2d(b^2-d)^{5/2}}-\frac{e^{c+dx^2}\mathrm{Erfc}(a+bx)}{2d^2}+\frac{x^2e^{c+dx^2}\mathrm{Erfc}(a+bx)}{2d}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + d*x^2)*x^3*Erfc[a + b*x],x]
```

```
[Out] (a*b^2*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/(2*(b^2 - d)^2*d*Sqrt[Pi]) -
 (b*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2)*x)/(2*(b^2 - d)*d*Sqrt[Pi]) - (b
*E^(c + (a^2*d)/(b^2 - d))*Erf[(a*b + (b^2 - d)*x)/Sqrt[b^2 - d]])/(2*Sqrt[
b^2 - d]*d^2) + (a^2*b^3*E^(c + (a^2*d)/(b^2 - d))*Erf[(a*b + (b^2 - d)*x)/
Sqrt[b^2 - d]])/(2*(b^2 - d)^(5/2)*d) + (b*E^(c + (a^2*d)/(b^2 - d))*Erf[(a
*b + (b^2 - d)*x)/Sqrt[b^2 - d]])/(4*(b^2 - d)^(3/2)*d) - (E^(c + d*x^2)*Er
fc[a + b*x])/(2*d^2) + (E^(c + d*x^2)*x^2*Erfc[a + b*x])/(2*d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2272

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)*((d_.) + (e_.)*(x_)), x_Symbol
] :> Simp[e*(F^(a + b*x + c*x^2)/(2*c*Log[F])), x] - Dist[(b*e - 2*c*d)/(2*
c), Int[F^(a + b*x + c*x^2), x], x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[
b*e - 2*c*d, 0]
```

Rule 2273

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)*((d_.) + (e_.)*(x_))^(m_), x_S
ymbol] :> Simp[e*(d + e*x)^(m - 1)*(F^(a + b*x + c*x^2)/(2*c*Log[F])), x] +
 (-Dist[(b*e - 2*c*d)/(2*c), Int[(d + e*x)^(m - 1)*F^(a + b*x + c*x^2), x],
 x] - Dist[(m - 1)*(e^2/(2*c*Log[F])), Int[(d + e*x)^(m - 2)*F^(a + b*x + c
*x^2), x], x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[b*e - 2*c*d, 0] && Gt
Q[m, 1]
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6521

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x]) /; FreeQ
[{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$
\begin{aligned}
\int e^{c+dx^2}x^3\operatorname{erfc}(a+bx)\,dx &= \frac{e^{c+dx^2}x^2\operatorname{erfc}(a+bx)}{2d} - \frac{\int e^{c+dx^2}x\operatorname{erfc}(a+bx)\,dx}{d} + \frac{b\int e^{-a^2+c-2abx+(-b^2+d)x^2}x^2\,d}{d\sqrt{\pi}} \\
&= -\frac{be^{-a^2+c-2abx-(b^2-d)x^2}x}{2(b^2-d)d\sqrt{\pi}} - \frac{e^{c+dx^2}\operatorname{erfc}(a+bx)}{2d^2} + \frac{e^{c+dx^2}x^2\operatorname{erfc}(a+bx)}{2d} - \frac{b\int e^{-a^2}}{} \\
&= \frac{ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2d\sqrt{\pi}} - \frac{be^{-a^2+c-2abx-(b^2-d)x^2}x}{2(b^2-d)d\sqrt{\pi}} - \frac{e^{c+dx^2}\operatorname{erfc}(a+bx)}{2d^2} + \frac{e^{c+dx^2}}{} \\
&= \frac{ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2d\sqrt{\pi}} - \frac{be^{-a^2+c-2abx-(b^2-d)x^2}x}{2(b^2-d)d\sqrt{\pi}} - \frac{be^{\frac{b^2c+a^2d-cd}{b^2-d}}\operatorname{erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)}{2\sqrt{b^2-d}\,d^2} \\
&= \frac{ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2d\sqrt{\pi}} - \frac{be^{-a^2+c-2abx-(b^2-d)x^2}x}{2(b^2-d)d\sqrt{\pi}} - \frac{be^{\frac{b^2c+a^2d-cd}{b^2-d}}\operatorname{erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)}{2\sqrt{b^2-d}\,d^2}
\end{aligned}
$$

Mathematica [A]
time = 3.38, size = 256, normalized size = 0.75

$$
-\frac{e^c\left(-2e^{dx^2}(-1+dx^2)+2e^{dx^2}(-1+dx^2)\operatorname{Erf}(a+bx)-\frac{bde^{-a^2-2abx+(-b^2+d)x^2}\left(2(b^2-d)(ab+(-b^2+d)x)+\sqrt{b^2-d}\,((1+2a^2)b^2-d)e^{\frac{(ab+(b^2-d)x)^2}{b^2-d}}\sqrt{\pi}\operatorname{Erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)\right)}{(b^2-d)^3\sqrt{\pi}}+\frac{2be^{\frac{a^2d}{b^2-d}}\operatorname{Erfi}\left(\frac{-ab+(-b^2+d)x}{\sqrt{-b^2+d}}\right)}{\sqrt{-b^2+d}}\right)}{4d^2}
$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + d*x^2)*x^3*Erfc[a + b*x],x]
```

```
[Out] -1/4*(E^c*(-2*E^(d*x^2)*(-1 + d*x^2) + 2*E^(d*x^2)*(-1 + d*x^2)*Erf[a + b*x
] - (b*d*E^(-a^2 - 2*a*b*x + (-b^2 + d)*x^2)*(2*(b^2 - d)*(a*b + (-b^2 + d)
*x) + Sqrt[b^2 - d]*((1 + 2*a^2)*b^2 - d)*E^((a*b + (b^2 - d)*x)^2/(b^2 - d
))*Sqrt[Pi]*Erf[(a*b + (b^2 - d)*x)/Sqrt[b^2 - d]]))/((b^2 - d)^3*Sqrt[Pi])
 + (2*b*E^((a^2*d)/(b^2 - d))*Erfi[(-(a*b) + (-b^2 + d)*x)/Sqrt[-b^2 + d]])
/Sqrt[-b^2 + d]))/d^2
```

Maple [F]
time = 0.18, size = 0, normalized size = 0.00

$$
\int \mathrm{e}^{d\,x^2+c}x^3\operatorname{erfc}(bx+a)\;dx
$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^3*erfc(b*x+a),x)
```

```
[Out] int(exp(d*x^2+c)*x^3*erfc(b*x+a),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erfc(b*x+a),x, algorithm="maxima")
```

```
[Out] integrate(x^3*erfc(b*x + a)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.36, size = 328, normalized size = 0.96

$$-\frac{\pi(2\,b^5-(2\,a^2+5)b^3d+3\,bd^2)\sqrt{b^2-d}\,\operatorname{erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)e^{\left(\frac{b^2c+\left(a^2-c\right)d}{b^2-d}\right)}-2\,\sqrt{\pi}\,(ab^4d-ab^2d^2-(b^5d-2\,b^3d^2+bd^3)x)e^{(-b^2x^2-2\,abx+dx^2-a^2+c)}-2\,(\pi(b^6d-3\,b^4d^2+3\,b^2d^3-d^4)x^2-\pi(b^6-3\,b^4d+3\,b^2d^2-d^3)-(\pi(b^6d-3\,b^4d^2+3\,b^2d^3-d^4)x^2-\pi(b^6-3\,b^4d+3\,b^2d^2-d^3))\operatorname{erf}(bx+a))e^{(dx^2+c)}}{4\,\pi(b^6d^2-3\,b^4d^3+3\,b^2d^4-d^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erfc(b*x+a),x, algorithm="fricas")
```

```
[Out] -1/4*(pi*(2*b^5 - (2*a^2 + 5)*b^3*d + 3*b*d^2)*sqrt(b^2 - d)*erf((a*b + (b^
2 - d)*x)/sqrt(b^2 - d))*e^((b^2*c + (a^2 - c)*d)/(b^2 - d)) - 2*sqrt(pi)*(
a*b^4*d - a*b^2*d^2 - (b^5*d - 2*b^3*d^2 + b*d^3)*x)*e^(-b^2*x^2 - 2*a*b*x
+ d*x^2 - a^2 + c) - 2*(pi*(b^6*d - 3*b^4*d^2 + 3*b^2*d^3 - d^4)*x^2 - pi*(
b^6 - 3*b^4*d + 3*b^2*d^2 - d^3) - (pi*(b^6*d - 3*b^4*d^2 + 3*b^2*d^3 - d^4
)*x^2 - pi*(b^6 - 3*b^4*d + 3*b^2*d^2 - d^3))*erf(b*x + a))*e^(d*x^2 + c))/
(pi*(b^6*d^2 - 3*b^4*d^3 + 3*b^2*d^4 - d^5))
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int x^{3}e^{dx^{2}}\operatorname{erfc}\left(a+bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**3*erfc(b*x+a),x)
```

```
[Out] exp(c)*Integral(x**3*exp(d*x**2)*erfc(a + b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erfc(b*x+a),x, algorithm="giac")
```

```
[Out] integrate(x^3*erfc(b*x + a)*e^(d*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.00

$$\int x^3 \operatorname{erfc}(a + b\,x)\,\mathrm{e}^{d\,x^2+c}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erfc(a + b*x)*exp(c + d*x^2),x)
```

```
[Out] int(x^3*erfc(a + b*x)*exp(c + d*x^2), x)
```

3.190 $\int e^{c+dx^2} x \mathbf{Erfc}(a+bx)\,dx$

Optimal. Leaf size=86

$$\frac{be^{c+\frac{a^2d}{b^2-d}}\operatorname{Erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)}{2\sqrt{b^2-d}\,d}+\frac{e^{c+dx^2}\operatorname{Erfc}(a+bx)}{2d}$$

```
[Out] 1/2*exp(d*x^2+c)*erfc(b*x+a)/d+1/2*b*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*
x)/(b^2-d)^(1/2))/d/(b^2-d)^(1/2)
```

Rubi [A]
time = 0.04, antiderivative size = 86, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {6518, 2266, 2236}

$$\frac{be^{\frac{a^2d}{b^2-d}+c}\operatorname{Erf}\left(\frac{ab+x(b^2-d)}{\sqrt{b^2-d}}\right)}{2d\sqrt{b^2-d}}+\frac{e^{c+dx^2}\operatorname{Erfc}(a+bx)}{2d}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + d*x^2)*x*Erfc[a + b*x],x]
```

```
[Out] (b*E^(c + (a^2*d)/(b^2 - d))*Erf[(a*b + (b^2 - d)*x)/Sqrt[b^2 - d]])/(2*Sqr
t[b^2 - d]*d) + (E^(c + d*x^2)*Erfc[a + b*x])/(2*d)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 6518

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfc[a + b*x]/(2*d)), x] + Dist[b/(d*Sqrt[Pi]), Int[E^(-a
^2 + c - 2*a*b*x - (b^2 - d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\int e^{c+dx^2} x \operatorname{erfc}(a+bx)\,dx = \frac{e^{c+dx^2}\operatorname{erfc}(a+bx)}{2d} + \frac{b\int e^{-a^2+c-2abx-(b^2-d)x^2}\,dx}{d\sqrt{\pi}}$$

$$= \frac{e^{c+dx^2}\operatorname{erfc}(a+bx)}{2d} + \frac{\left(be^{\frac{b^2c+a^2d-cd}{b^2-d}}\right)\int \exp\left(\frac{(-2ab+2(-b^2+d)x)^2}{4(-b^2+d)}\right)\,dx}{d\sqrt{\pi}}$$

$$= \frac{be^{\frac{b^2c+a^2d-cd}{b^2-d}}\operatorname{erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)}{2\sqrt{b^2-d}\,d} + \frac{e^{c+dx^2}\operatorname{erfc}(a+bx)}{2d}$$

Mathematica [A]
time = 0.09, size = 81, normalized size = 0.94

$$\frac{e^c\left(e^{dx^2}\operatorname{Erfc}(a+bx)+\frac{be^{\frac{a^2d}{b^2-d}}\operatorname{Erfi}\left(\frac{-ab+(-b^2+d)x}{\sqrt{-b^2+d}}\right)}{\sqrt{-b^2+d}}\right)}{2d}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + d*x^2)*x*Erfc[a + b*x],x]
```

```
[Out] (E^c*(E^(d*x^2)*Erfc[a + b*x] + (b*E^((a^2*d)/(b^2 - d))*Erfi[(-(a*b) + (-b
^2 + d)*x)/Sqrt[-b^2 + d]])/Sqrt[-b^2 + d]))/(2*d)
```

Maple [B] Leaf count of result is larger than twice the leaf count of optimal. 174 vs. $2(76) = 152$.
time = 0.66, size = 175, normalized size = 2.03

method	result
default	$\frac{\frac{b\,e^{\frac{a^2d}{b^2}-\frac{2ad(bx+a)}{b^2}+c+\frac{d(bx+a)^2}{b^2}}}{2d}-\frac{\operatorname{erf}(bx+a)\,b\,e^{\frac{a^2d}{b^2}-\frac{2ad(bx+a)}{b^2}+c+\frac{d(bx+a)^2}{b^2}}}{2d}+\frac{b\,e^{\frac{a^2d}{b^2}+c-\frac{a^2d^2}{b^4\left(-1+\frac{d}{b^2}\right)}}\operatorname{erf}\left(\sqrt{1-\frac{d}{b^2}}\,(bx+a)+\right.}{2d\sqrt{1-\frac{d}{b^2}}}}{b}$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x*erfc(b*x+a),x,method=_RETURNVERBOSE)
```

```
[Out] (1/2*b/d*exp(1/b^2*a^2*d-2/b^2*a*d*(b*x+a)+c+1/b^2*d*(b*x+a)^2)-1/2*erf(b*x
+a)*b/d*exp(1/b^2*a^2*d-2/b^2*a*d*(b*x+a)+c+1/b^2*d*(b*x+a)^2)+1/2*b/d*exp(
```

```
1/b^2*a^2*d+c-a^2*d^2/b^4/(-1+d/b^2))/(1-d/b^2)^(1/2)*erf((1-d/b^2)^(1/2)*(
b*x+a)+a*d/b^2/(1-d/b^2)^(1/2)))/b
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erfc(b*x+a),x, algorithm="maxima")
[Out] integrate(x*erfc(b*x + a)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.38, size = 108, normalized size = 1.26

$$\frac{\sqrt{b^2-d}\,b\operatorname{erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)e^{\left(\frac{b^2c+\left(a^2-c\right)d}{b^2-d}\right)}+\left(b^2-\left(b^2-d\right)\operatorname{erf}\left(bx+a\right)-d\right)e^{\left(dx^2+c\right)}}{2\left(b^2d-d^2\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erfc(b*x+a),x, algorithm="fricas")
[Out] 1/2*(sqrt(b^2 - d)*b*erf((a*b + (b^2 - d)*x)/sqrt(b^2 - d))*e^((b^2*c + (a^
2 - c)*d)/(b^2 - d)) + (b^2 - (b^2 - d)*erf(b*x + a) - d)*e^(d*x^2 + c))/(b
^2*d - d^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int xe^{dx^{2}}\operatorname{erfc}\left(a+bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x*erfc(b*x+a),x)
[Out] exp(c)*Integral(x*exp(d*x**2)*erfc(a + b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erfc(b*x+a),x, algorithm="giac")
```

```
[Out] integrate(x*erfc(b*x + a)*e^(d*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x\,\mathrm{erfc}(a+b\,x)\,\mathrm{e}^{d\,x^2+c}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfc(a + b*x)*exp(c + d*x^2),x)
[Out] int(x*erfc(a + b*x)*exp(c + d*x^2), x)
```

3.191 $\int \frac{e^{c+dx^2}\mathbf{Erfc}(a+bx)}{x}\,dx$

Optimal. Leaf size=22

$$\operatorname{Int}\left(\frac{e^{c+dx^2}\operatorname{Erfc}(a+bx)}{x},x\right)$$

```
[Out] Unintegrable(exp(d*x^2+c)*erfc(b*x+a)/x,x)
```

Rubi [A]
time = 0.03, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\operatorname{Erfc}(a+bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfc[a + b*x])/x,x]
[Out] Defer[Int][(E^(c + d*x^2)*Erfc[a + b*x])/x, x]
```

Rubi steps

$$\int \frac{e^{c+dx^2}\operatorname{erfc}(a+bx)}{x}\,dx = \int \frac{e^{c+dx^2}\operatorname{erfc}(a+bx)}{x}\,dx$$

Mathematica [A]
time = 0.51, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\operatorname{Erfc}(a+bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfc[a + b*x])/x,x]
[Out] Integrate[(E^(c + d*x^2)*Erfc[a + b*x])/x, x]
```

Maple [A]
time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\operatorname{erfc}(bx+a)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfc(b*x+a)/x,x)
```

```
[Out] int(exp(d*x^2+c)*erfc(b*x+a)/x,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x+a)/x,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x + a)*e^(d*x^2 + c)/x, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x+a)/x,x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x + a) - 1)*e^(d*x^2 + c)/x, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^{2}}\operatorname{erfc}\left(a+bx\right)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfc(b*x+a)/x,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erfc(a + b*x)/x, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x+a)/x,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x + a)*e^(d*x^2 + c)/x, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{\operatorname{erfc}(a + b\,x)\ \mathrm{e}^{d\,x^2+c}}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((erfc(a + b*x)*exp(c + d*x^2))/x,x)
```

```
[Out] int((erfc(a + b*x)*exp(c + d*x^2))/x, x)
```

3.192 $\int \frac{e^{c+dx^2}\mathbf{Erfc}(a+bx)}{x^3}\,dx$

Optimal. Leaf size=183

$$\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{\sqrt{\pi}\,x}+b\sqrt{b^2-d}\,e^{c+\frac{a^2d}{b^2-d}}\text{Erf}\left(\frac{ab+(b^2-d)\,x}{\sqrt{b^2-d}}\right)-\frac{e^{c+dx^2}\text{Erfc}(a+bx)}{2x^2}+\frac{2ab^2\text{Int}\left(\frac{e^{-a^2+c-2abx+(-b^2}}{x}\right.}{\sqrt{\pi}}$$

```
[Out] -1/2*exp(d*x^2+c)*erfc(b*x+a)/x^2+b*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x
)/(b^2-d)^(1/2))*(b^2-d)^(1/2)+b*exp(-a^2+c-2*a*b*x-(b^2-d)*x^2)/x/Pi^(1/2)
+2*a*b^2*Unintegrable(exp(-a^2+c-2*a*b*x+(-b^2+d)*x^2)/x,x)/Pi^(1/2)+d*Unin
tegrable(exp(d*x^2+c)*erfc(b*x+a)/x,x)
```

Rubi [A]
time = 0.27, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$,
Rules used = {}

$$\int \frac{e^{c+dx^2}\text{Erfc}(a+bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfc[a + b*x])/x^3,x]
```

```
[Out] (b*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/(Sqrt[Pi]*x) + b*Sqrt[b^2 - d]*E
^(c + (a^2*d)/(b^2 - d))*Erf[(a*b + (b^2 - d)*x)/Sqrt[b^2 - d]] - (E^(c + d
*x^2)*Erfc[a + b*x])/(2*x^2) + (2*a*b^2*Defer[Int][E^(-a^2 + c - 2*a*b*x +
(-b^2 + d)*x^2)/x, x])/Sqrt[Pi] + d*Defer[Int][(E^(c + d*x^2)*Erfc[a + b*x]
)/x, x]
```

Rubi steps

$$\begin{aligned}
\int \frac{e^{c+dx^2}\text{erfc}(a+bx)}{x^3}\,dx &= -\frac{e^{c+dx^2}\text{erfc}(a+bx)}{2x^2}+d\int \frac{e^{c+dx^2}\text{erfc}(a+bx)}{x}\,dx-\frac{b\int \frac{e^{-a^2+c-2abx+(-b^2+d)x^2}}{x^2}\,dx}{\sqrt{\pi}}\\
&= \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\text{erfc}(a+bx)}{2x^2}+d\int \frac{e^{c+dx^2}\text{erfc}(a+bx)}{x}\,dx+\frac{(2ab^2)}{}\\
&= \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\text{erfc}(a+bx)}{2x^2}+d\int \frac{e^{c+dx^2}\text{erfc}(a+bx)}{x}\,dx+\frac{(2ab^2)}{}\\
&= \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{\sqrt{\pi}\,x}+b\sqrt{b^2-d}\,e^{\frac{b^2c+a^2d-cd}{b^2-d}}\text{erf}\left(\frac{ab+(b^2-d)\,x}{\sqrt{b^2-d}}\right)-\frac{e^{c+dx^2}\text{erfc}(a}{2x^2}
\end{aligned}$$

Mathematica [**A**]
time = 0.65, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\text{Erfc}(a+bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfc[a + b*x])/x^3,x]
[Out] Integrate[(E^(c + d*x^2)*Erfc[a + b*x])/x^3, x]
```

Maple [**A**]
time = 0.24, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\text{erfc}(bx+a)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfc(b*x+a)/x^3,x)
[Out] int(exp(d*x^2+c)*erfc(b*x+a)/x^3,x)
```

Maxima [**A**]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x+a)/x^3,x, algorithm="maxima")
[Out] integrate(erfc(b*x + a)*e^(d*x^2 + c)/x^3, x)
```

Fricas [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x+a)/x^3,x, algorithm="fricas")
[Out] integral(-(erf(b*x + a) - 1)*e^(d*x^2 + c)/x^3, x)
```

Sympy [**A**]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^2}\,\text{erfc}\,(a+bx)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfc(b*x+a)/x**3,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erfc(a + b*x)/x**3, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x+a)/x^3,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x + a)*e^(d*x^2 + c)/x^3, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erfc}(a+b\,x)\,\mathrm{e}^{d\,x^2+c}}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((erfc(a + b*x)*exp(c + d*x^2))/x^3,x)
```

```
[Out] int((erfc(a + b*x)*exp(c + d*x^2))/x^3, x)
```

3.193 $\int e^{c+dx^2}x^4\textbf{Erfc}(a+bx)\,dx$

Optimal. Leaf size=527

$$\frac{3be^{-a^2+c-2abx-(b^2-d)x^2}}{4\left(b^2-d\right)d^2\sqrt{\pi}}-\frac{a^2b^3e^{-a^2+c-2abx-(b^2-d)x^2}}{2\left(b^2-d\right)^3d\sqrt{\pi}}-\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2\left(b^2-d\right)^2d\sqrt{\pi}}+\frac{ab^2e^{-a^2+c-2abx-(b^2-d)x^2}x}{2\left(b^2-d\right)^2d\sqrt{\pi}}-\frac{be^{-a^2+c\cdots}}{2\left(b^2\cdots\right.}$$

```
[Out] 3/4*a*b^2*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)/(b^2-d)^(1/2))/(b^2-d)^(
3/2)/d^2-1/2*a^3*b^4*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)/(b^2-d)^(1/2)
)/(b^2-d)^(7/2)/d-3/4*a*b^2*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)/(b^2-d
)^(1/2))/(b^2-d)^(5/2)/d-3/4*exp(d*x^2+c)*x*erfc(b*x+a)/d^2+1/2*exp(d*x^2+c
)*x^3*erfc(b*x+a)/d+3/4*b*exp(-a^2+c-2*a*b*x-(b^2-d)*x^2)/(b^2-d)/d^2/Pi^(1
/2)-1/2*a^2*b^3*exp(-a^2+c-2*a*b*x-(b^2-d)*x^2)/(b^2-d)^3/d/Pi^(1/2)-1/2*b*
exp(-a^2+c-2*a*b*x-(b^2-d)*x^2)/(b^2-d)^2/d/Pi^(1/2)+1/2*a*b^2*exp(-a^2+c-2
*a*b*x-(b^2-d)*x^2)*x/(b^2-d)^2/d/Pi^(1/2)-1/2*b*exp(-a^2+c-2*a*b*x-(b^2-d)
*x^2)*x^2/(b^2-d)/d/Pi^(1/2)+3/4*Unintegrable(exp(d*x^2+c)*erfc(b*x+a),x)/d
^2
```

Rubi [A]
time = 0.63, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int e^{c+dx^2}x^4\text{Erfc}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*x^4*Erfc[a + b*x],x]
```

```
[Out] (3*b*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/(4*(b^2 - d)*d^2*Sqrt[Pi]) - (
a^2*b^3*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/(2*(b^2 - d)^3*d*Sqrt[Pi])
- (b*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/(2*(b^2 - d)^2*d*Sqrt[Pi]) + (
a*b^2*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2)*x)/(2*(b^2 - d)^2*d*Sqrt[Pi])
- (b*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2)*x^2)/(2*(b^2 - d)*d*Sqrt[Pi]) +
 (3*a*b^2*E^(c + (a^2*d)/(b^2 - d))*Erf[(a*b + (b^2 - d)*x)/Sqrt[b^2 - d]])
/(4*(b^2 - d)^(3/2)*d^2) - (a^3*b^4*E^(c + (a^2*d)/(b^2 - d))*Erf[(a*b + (b
^2 - d)*x)/Sqrt[b^2 - d]])/(2*(b^2 - d)^(7/2)*d) - (3*a*b^2*E^(c + (a^2*d)/
(b^2 - d))*Erf[(a*b + (b^2 - d)*x)/Sqrt[b^2 - d]])/(4*(b^2 - d)^(5/2)*d) -
(3*E^(c + d*x^2)*x*Erfc[a + b*x])/(4*d^2) + (E^(c + d*x^2)*x^3*Erfc[a + b*x
])/(2*d) + (3*Defer[Int][E^(c + d*x^2)*Erfc[a + b*x], x])/(4*d^2)
```

Rubi steps

$$\int e^{c+dx^2}x^4\text{erfc}(a+bx)\,dx = \frac{e^{c+dx^2}x^3\text{erfc}(a+bx)}{2d} - \frac{3\int e^{c+dx^2}x^2\text{erfc}(a+bx)\,dx}{2d} + \frac{b\int e^{-a^2+c-2abx+(-b^2+d)x^2}x}{d\sqrt{\pi}}$$

$$= -\frac{be^{-a^2+c-2abx-(b^2-d)x^2}x^2}{2(b^2-d)\,d\sqrt{\pi}} - \frac{3e^{c+dx^2}x\text{erfc}(a+bx)}{4d^2} + \frac{e^{c+dx^2}x^3\text{erfc}(a+bx)}{2d} + 3\int$$

$$= \frac{3be^{-a^2+c-2abx-(b^2-d)x^2}}{4(b^2-d)\,d^2\sqrt{\pi}} - \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2\,d\sqrt{\pi}} + \frac{ab^2e^{-a^2+c-2abx-(b^2-d)x^2}x}{2(b^2-d)^2\,d\sqrt{\pi}} - be$$

$$= \frac{3be^{-a^2+c-2abx-(b^2-d)x^2}}{4(b^2-d)\,d^2\sqrt{\pi}} - \frac{a^2b^3e^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^3\,d\sqrt{\pi}} - \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2\,d\sqrt{\pi}} + ab^2$$

$$= \frac{3be^{-a^2+c-2abx-(b^2-d)x^2}}{4(b^2-d)\,d^2\sqrt{\pi}} - \frac{a^2b^3e^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^3\,d\sqrt{\pi}} - \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2\,d\sqrt{\pi}} + ab^2$$

$$= \frac{3be^{-a^2+c-2abx-(b^2-d)x^2}}{4(b^2-d)\,d^2\sqrt{\pi}} - \frac{a^2b^3e^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^3\,d\sqrt{\pi}} - \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)^2\,d\sqrt{\pi}} + ab^2$$

Mathematica [A]
time = 0.79, size = 0, normalized size = 0.00

$$\int e^{c+dx^2}x^4\text{Erfc}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*x^4*Erfc[a + b*x],x]
[Out] Integrate[E^(c + d*x^2)*x^4*Erfc[a + b*x], x]
```

Maple [A]
time = 0.08, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^2+c}x^4\text{erfc}(bx+a)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^4*erfc(b*x+a),x)
[Out] int(exp(d*x^2+c)*x^4*erfc(b*x+a),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erfc(b*x+a),x, algorithm="maxima")
```

```
[Out] integrate(x^4*erfc(b*x + a)*e^(d*x^2 + c), x)
```

Fricas [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erfc(b*x+a),x, algorithm="fricas")
```

```
[Out] integral(-(x^4*erf(b*x + a) - x^4)*e^(d*x^2 + c), x)
```

Sympy [**F(-1)**] Timed out
time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**4*erfc(b*x+a),x)
```

```
[Out] Timed out
```

Giac [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erfc(b*x+a),x, algorithm="giac")
```

```
[Out] integrate(x^4*erfc(b*x + a)*e^(d*x^2 + c), x)
```

Mupad [**A**]
time = 0.00, size = -1, normalized size = -0.00

$$\int x^4\,\mathrm{erfc}(a+b\,x)\,\mathrm{e}^{d\,x^2+c}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erfc(a + b*x)*exp(c + d*x^2),x)
```

```
[Out] int(x^4*erfc(a + b*x)*exp(c + d*x^2), x)
```

3.194 $\int e^{c+dx^2}x^2\mathbf{Erfc}(a+bx)\,dx$

Optimal. Leaf size=164

$$-\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)d\sqrt{\pi}}-\frac{ab^2e^{c+\frac{a^2d}{b^2-d}}\text{Erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)}{2(b^2-d)^{3/2}d}+\frac{e^{c+dx^2}x\text{Erfc}(a+bx)}{2d}-\frac{\text{Int}\left(e^{c+dx^2}\text{Erfc}(a+bx),x\right)}{2d}$$

```
[Out] -1/2*a*b^2*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)/(b^2-d)^(1/2))/(b^2-d)^
(3/2)/d+1/2*exp(d*x^2+c)*x*erfc(b*x+a)/d-1/2*b*exp(-a^2+c-2*a*b*x-(b^2-d)*x
^2)/(b^2-d)/d/Pi^(1/2)-1/2*Unintegrable(exp(d*x^2+c)*erfc(b*x+a),x)/d
```

Rubi [A]
time = 0.12, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int e^{c+dx^2}x^2\text{Erfc}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*x^2*Erfc[a + b*x],x]
```

```
[Out] -1/2*(b*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/((b^2 - d)*d*Sqrt[Pi]) - (a
*b^2*E^(c + (a^2*d)/(b^2 - d))*Erf[(a*b + (b^2 - d)*x)/Sqrt[b^2 - d]])/(2*(
b^2 - d)^(3/2)*d) + (E^(c + d*x^2)*x*Erfc[a + b*x])/(2*d) - Defer[Int][E^(c
 + d*x^2)*Erfc[a + b*x], x]/(2*d)
```

Rubi steps

$$\int e^{c+dx^2}x^2\text{erfc}(a+bx)\,dx=\frac{e^{c+dx^2}x\text{erfc}(a+bx)}{2d}-\frac{\int e^{c+dx^2}\text{erfc}(a+bx)\,dx}{2d}+\frac{b\int e^{-a^2+c-2abx+(-b^2+d)x^2}x\,dx}{d\sqrt{\pi}}$$

$$=-\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)d\sqrt{\pi}}+\frac{e^{c+dx^2}x\text{erfc}(a+bx)}{2d}-\frac{\int e^{c+dx^2}\text{erfc}(a+bx)\,dx}{2d}-\frac{(ab^2)}{}$$

$$=-\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)d\sqrt{\pi}}+\frac{e^{c+dx^2}x\text{erfc}(a+bx)}{2d}-\frac{\int e^{c+dx^2}\text{erfc}(a+bx)\,dx}{2d}-\frac{\left(ab^2\right.}{}$$

$$=-\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{2(b^2-d)d\sqrt{\pi}}-\frac{ab^2e^{\frac{b^2c+a^2d-cd}{b^2-d}}\text{erf}\left(\frac{ab+(b^2-d)x}{\sqrt{b^2-d}}\right)}{2(b^2-d)^{3/2}d}+\frac{e^{c+dx^2}x\text{erfc}(a+bx)}{2d}-$$

Mathematica [A]
time = 0.60, size = 0, normalized size = 0.00

$$\int e^{c+dx^2}x^2\text{Erfc}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*x^2*Erfc[a + b*x],x]
[Out] Integrate[E^(c + d*x^2)*x^2*Erfc[a + b*x], x]
```

Maple [A]
time = 0.15, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^2+c}x^2\text{erfc}(bx+a)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^2*erfc(b*x+a),x)
[Out] int(exp(d*x^2+c)*x^2*erfc(b*x+a),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erfc(b*x+a),x, algorithm="maxima")
[Out] integrate(x^2*erfc(b*x + a)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erfc(b*x+a),x, algorithm="fricas")
[Out] integral(-(x^2*erf(b*x + a) - x^2)*e^(d*x^2 + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int x^{2}e^{dx^{2}}\operatorname{erfc}{\left(a+bx\right)}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**2*erfc(b*x+a),x)
```

```
[Out] exp(c)*Integral(x**2*exp(d*x**2)*erfc(a + b*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erfc(b*x+a),x, algorithm="giac")
```

```
[Out] integrate(x^2*erfc(b*x + a)*e^(d*x^2 + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^2\,\mathrm{erfc}(a+b\,x)\,\mathrm{e}^{d\,x^2+c}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfc(a + b*x)*exp(c + d*x^2),x)
```

```
[Out] int(x^2*erfc(a + b*x)*exp(c + d*x^2), x)
```

3.195 $\int e^{c+dx^2}\mathbf{Erfc}(a+bx)\,dx$

Optimal. Leaf size=19

$$\mathrm{Int}\left(e^{c+dx^2}\mathrm{Erfc}(a+bx),x\right)$$

```
[Out] Unintegrable(exp(d*x^2+c)*erfc(b*x+a),x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int e^{c+dx^2}\mathrm{Erfc}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*Erfc[a + b*x],x]
```

```
[Out] Defer[Int][E^(c + d*x^2)*Erfc[a + b*x], x]
```

Rubi steps

$$\int e^{c+dx^2}\mathrm{erfc}(a+bx)\,dx=\int e^{c+dx^2}\mathrm{erfc}(a+bx)\,dx$$

Mathematica [A]
time = 0.03, size = 0, normalized size = 0.00

$$\int e^{c+dx^2}\mathrm{Erfc}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*Erfc[a + b*x],x]
```

```
[Out] Integrate[E^(c + d*x^2)*Erfc[a + b*x], x]
```

Maple [A]
time = 0.09, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^{2}+c}\mathrm{erfc}(bx+a)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfc(b*x+a),x)
[Out] int(exp(d*x^2+c)*erfc(b*x+a),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x+a),x, algorithm="maxima")
[Out] integrate(erfc(b*x + a)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x+a),x, algorithm="fricas")
[Out] integral(-(erf(b*x + a) - 1)*e^(d*x^2 + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int e^{dx^{2}}\operatorname{erfc}\left(a+bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfc(b*x+a),x)
[Out] exp(c)*Integral(exp(d*x**2)*erfc(a + b*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x+a),x, algorithm="giac")
[Out] integrate(erfc(b*x + a)*e^(d*x^2 + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \operatorname{erfc}(a+b\,x)\;\mathrm{e}^{d\,x^2+c}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(a + b*x)*exp(c + d*x^2),x)
[Out] int(erfc(a + b*x)*exp(c + d*x^2), x)
```

3.196 $\int \frac{e^{c+dx^2}\text{Erfc}(a+bx)}{x^2}\,dx$

Optimal. Leaf size=83

$$-\frac{e^{c+dx^2}\text{Erfc}(a+bx)}{x}-\frac{2b\text{Int}\left(\frac{e^{-a^2+c-2abx+(-b^2+d)x^2}}{x},x\right)}{\sqrt{\pi}}+2d\text{Int}\left(e^{c+dx^2}\text{Erfc}(a+bx),x\right)$$

```
[Out] -exp(d*x^2+c)*erfc(b*x+a)/x-2*b*Unintegrable(exp(-a^2+c-2*a*b*x+(-b^2+d)*x^
2)/x,x)/Pi^(1/2)+2*d*Unintegrable(exp(d*x^2+c)*erfc(b*x+a),x)
```

Rubi [A]
time = 0.14, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\text{Erfc}(a+bx)}{x^2}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfc[a + b*x])/x^2,x]
```

```
[Out] -((E^(c + d*x^2)*Erfc[a + b*x])/x) - (2*b*Defer[Int][E^(-a^2 + c - 2*a*b*x
+ (-b^2 + d)*x^2)/x, x])/Sqrt[Pi] + 2*d*Defer[Int][E^(c + d*x^2)*Erfc[a + b
*x], x]
```

Rubi steps

$$\int \frac{e^{c+dx^2}\text{erfc}(a+bx)}{x^2}\,dx=-\frac{e^{c+dx^2}\text{erfc}(a+bx)}{x}+(2d)\int e^{c+dx^2}\text{erfc}(a+bx)\,dx-\frac{(2b)\int \frac{e^{-a^2+c-2abx+(-b^2+d)x^2}}{x}\,d}{\sqrt{\pi}}$$

Mathematica [A]
time = 0.68, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\text{Erfc}(a+bx)}{x^2}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfc[a + b*x])/x^2,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erfc[a + b*x])/x^2, x]
```

Maple [A]
time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\mathrm{erfc}(bx+a)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfc(b*x+a)/x^2,x)
[Out] int(exp(d*x^2+c)*erfc(b*x+a)/x^2,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x+a)/x^2,x, algorithm="maxima")
[Out] integrate(erfc(b*x + a)*e^(d*x^2 + c)/x^2, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x+a)/x^2,x, algorithm="fricas")
[Out] integral(-(erf(b*x + a) - 1)*e^(d*x^2 + c)/x^2, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^{2}}\operatorname{erfc}{\left(a+bx\right)}}{x^{2}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfc(b*x+a)/x**2,x)
[Out] exp(c)*Integral(exp(d*x**2)*erfc(a + b*x)/x**2, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x+a)/x^2,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x + a)*e^(d*x^2 + c)/x^2, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\operatorname{erfc}(a+b\,x)\,\,\mathrm{e}^{d\,x^2+c}}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((erfc(a + b*x)*exp(c + d*x^2))/x^2,x)
```

```
[Out] int((erfc(a + b*x)*exp(c + d*x^2))/x^2, x)
```

3.197 $\int \frac{e^{c+dx^2}\mathbf{Erfc}(a+bx)}{x^4}\,dx$

Optimal. Leaf size=355

$$\frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2}-\frac{2ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x}-\frac{2}{3}ab^2\sqrt{b^2-d}\,e^{c+\frac{a^2d}{b^2-d}}\mathrm{Erf}\left(\frac{ab+(b^2-d)\,x}{\sqrt{b^2-d}}\right)-\frac{e^{c+dx^2}\mathrm{Erfc}(a$$

```
[Out] -1/3*exp(d*x^2+c)*erfc(b*x+a)/x^3-2/3*d*exp(d*x^2+c)*erfc(b*x+a)/x-2/3*a*b^
2*exp(c+a^2*d/(b^2-d))*erf((a*b+(b^2-d)*x)/(b^2-d)^(1/2))*(b^2-d)^(1/2)+1/3
*b*exp(-a^2+c-2*a*b*x-(b^2-d)*x^2)/x^2/Pi^(1/2)-2/3*a*b^2*exp(-a^2+c-2*a*b*
x-(b^2-d)*x^2)/x/Pi^(1/2)-4/3*a^2*b^3*Unintegrable(exp(-a^2+c-2*a*b*x+(-b^2
+d)*x^2)/x,x)/Pi^(1/2)+2/3*b*(b^2-d)*Unintegrable(exp(-a^2+c-2*a*b*x+(-b^2+
d)*x^2)/x,x)/Pi^(1/2)-4/3*b*d*Unintegrable(exp(-a^2+c-2*a*b*x+(-b^2+d)*x^2)
/x,x)/Pi^(1/2)+4/3*d^2*Unintegrable(exp(d*x^2+c)*erfc(b*x+a),x)
```

Rubi [A]
time = 0.59, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\mathrm{Erfc}(a+bx)}{x^4}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfc[a + b*x])/x^4,x]
```

```
[Out] (b*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/(3*Sqrt[Pi]*x^2) - (2*a*b^2*E^(-
a^2 + c - 2*a*b*x - (b^2 - d)*x^2))/(3*Sqrt[Pi]*x) - (2*a*b^2*Sqrt[b^2 - d]
*E^(c + (a^2*d)/(b^2 - d))*Erf[(a*b + (b^2 - d)*x)/Sqrt[b^2 - d]])/3 - (E^(
c + d*x^2)*Erfc[a + b*x])/(3*x^3) - (2*d*E^(c + d*x^2)*Erfc[a + b*x])/(3*x)
 - (4*a^2*b^3*Defer[Int][E^(-a^2 + c - 2*a*b*x + (-b^2 + d)*x^2)/x, x])/(3*
Sqrt[Pi]) + (2*b*(b^2 - d)*Defer[Int][E^(-a^2 + c - 2*a*b*x + (-b^2 + d)*x^
2)/x, x])/(3*Sqrt[Pi]) - (4*b*d*Defer[Int][E^(-a^2 + c - 2*a*b*x + (-b^2 +
d)*x^2)/x, x])/(3*Sqrt[Pi]) + (4*d^2*Defer[Int][E^(c + d*x^2)*Erfc[a + b*x]
, x])/3
```

Rubi steps

$$\int \frac{e^{c+dx^2}\text{erfc}(a+bx)}{x^4}\,dx = -\frac{e^{c+dx^2}\text{erfc}(a+bx)}{3x^3} + \frac{1}{3}(2d)\int \frac{e^{c+dx^2}\text{erfc}(a+bx)}{x^2}\,dx - \frac{(2b)\int \frac{e^{-a^2+c-2abx+\left(-b^2+d\right)x}}{x^3}}{3\sqrt{\pi}}$$

$$= \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2} - \frac{e^{c+dx^2}\text{erfc}(a+bx)}{3x^3} - \frac{2de^{c+dx^2}\text{erfc}(a+bx)}{3x} + \frac{1}{3}(4d^2)\int e^{c}$$

$$= \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2} - \frac{2ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x} - \frac{e^{c+dx^2}\text{erfc}(a+bx)}{3x^3} - \frac{2de^{c+dx^2}}{}$$

$$= \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2} - \frac{2ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x} - \frac{e^{c+dx^2}\text{erfc}(a+bx)}{3x^3} - \frac{2de^{c+dx^2}}{}$$

$$= \frac{be^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x^2} - \frac{2ab^2e^{-a^2+c-2abx-(b^2-d)x^2}}{3\sqrt{\pi}\,x} - \frac{2}{3}ab^2\sqrt{b^2-d}\,e^{\frac{b^2c+a^2d-cd}{b^2-d}}\text{erf}\Big(\frac{a}{}$$

Mathematica [A]
time = 0.80, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\text{Erfc}(a+bx)}{x^4}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfc[a + b*x])/x^4,x]
[Out] Integrate[(E^(c + d*x^2)*Erfc[a + b*x])/x^4, x]
```

Maple [A]
time = 0.20, size = 0, normalized size = 0.00

$$\int \frac{e^{d\,x^2+c}\text{erfc}(bx+a)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfc(b*x+a)/x^4,x)
[Out] int(exp(d*x^2+c)*erfc(b*x+a)/x^4,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x+a)/x^4,x, algorithm="maxima")
```

```
[Out] integrate(erfc(b*x + a)*e^(d*x^2 + c)/x^4, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x+a)/x^4,x, algorithm="fricas")
```

```
[Out] integral(-(erf(b*x + a) - 1)*e^(d*x^2 + c)/x^4, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int\frac{e^{dx^{2}}\operatorname{erfc}\left(a+bx\right)}{x^{4}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfc(b*x+a)/x**4,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erfc(a + b*x)/x**4, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfc(b*x+a)/x^4,x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x + a)*e^(d*x^2 + c)/x^4, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.00

$$\int\frac{\mathrm{erfc}(a+b\,x)\,\mathrm{e}^{d\,x^2+c}}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((erfc(a + b*x)*exp(c + d*x^2))/x^4,x)
```

```
[Out] int((erfc(a + b*x)*exp(c + d*x^2))/x^4, x)
```

3.198 $\int \left(\frac{e^{-b^2x^2}\mathbf{Erfc}(bx)}{x^3} + \frac{b^2e^{-b^2x^2}\mathbf{Erfc}(bx)}{x}\right) dx$

Optimal. Leaf size=60

$$\frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x} + \sqrt{2}\,b^2\mathrm{Erf}\left(\sqrt{2}\,bx\right) - \frac{e^{-b^2x^2}\mathrm{Erfc}(bx)}{2x^2}$$

```
[Out] -1/2*erfc(b*x)/exp(b^2*x^2)/x^2+b^2*erf(b*x*2^(1/2))*2^(1/2)+b/exp(2*b^2*x^
2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.10, antiderivative size = 60, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 40, $\frac{\text{number of rules}}{\text{integrand size}} = 0.075$, Rules used = {6527, 2245, 2236}

$$\sqrt{2}\,b^2\mathrm{Erf}\left(\sqrt{2}\,bx\right) - \frac{e^{-b^2x^2}\mathrm{Erfc}(bx)}{2x^2} + \frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]/(E^(b^2*x^2)*x^3) + (b^2*Erfc[b*x])/(E^(b^2*x^2)*x),x]
```

```
[Out] b/(E^(2*b^2*x^2)*Sqrt[Pi]*x) + Sqrt[2]*b^2*Erf[Sqrt[2]*b*x] - Erfc[b*x]/(2*
E^(b^2*x^2)*x^2)
```

Rule 2236

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erf[(c + d*x)*Rt[(-b)*Log[F], 2]]/(2*d*Rt[(-b)*Log[F], 2])), x] /; Fr
eeQ[{F, a, b, c, d}, x] && NegQ[b]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6527

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfc[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfc[a + b*x], x], x] + Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(-a^2 + c - 2*a*b*x - (b^2 - d)*x^2), x],
```

```
x]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \left(\frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x^3}+\frac{b^2e^{-b^2x^2}\operatorname{erfc}(bx)}{x}\right)dx &= b^2\int \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x}\,dx+\int \frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{x^3}\,dx\\ &= -\frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{2x^2}-\frac{b\int \frac{e^{-2b^2x^2}}{x^2}\,dx}{\sqrt{\pi}}\\ &= \frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{2x^2}+\frac{(4b^3)\int e^{-2b^2x^2}\,dx}{\sqrt{\pi}}\\ &= \frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x}+\sqrt{2}\,b^2\operatorname{erf}\left(\sqrt{2}\,bx\right)-\frac{e^{-b^2x^2}\operatorname{erfc}(bx)}{2x^2}\end{aligned}$$

Mathematica [A]
time = 0.05, size = 60, normalized size = 1.00

$$\frac{be^{-2b^2x^2}}{\sqrt{\pi}\,x}+\sqrt{2}\,b^2\mathrm{Erf}\left(\sqrt{2}\,bx\right)-\frac{e^{-b^2x^2}\mathrm{Erfc}(bx)}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]/(E^(b^2*x^2)*x^3) + (b^2*Erfc[b*x])/(E^(b^2*x^2)*x),x]
```

```
[Out] b/(E^(2*b^2*x^2)*Sqrt[Pi]*x) + Sqrt[2]*b^2*Erf[Sqrt[2]*b*x] - Erfc[b*x]/(2*
E^(b^2*x^2)*x^2)
```

Maple [A]
time = 0.81, size = 84, normalized size = 1.40

method	result	size
default	$\frac{-\frac{b\,e^{-b^2x^2}}{2x^2}+\frac{\operatorname{erf}(bx)b\,e^{-b^2x^2}}{2x^2}-\frac{b^3\left(-\frac{e^{-2b^2x^2}}{bx}-\sqrt{2}\,\sqrt{\pi}\,\operatorname{erf}\left(bx\sqrt{2}\right)\right)}{\sqrt{\pi}}}{b}$	84

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)/exp(b^2*x^2)/x^3+b^2*erfc(b*x)/exp(b^2*x^2)/x,x,method=_RETUR
NVERBOSE)
```

```
[Out] (-1/2*b/exp(b^2*x^2)/x^2+1/2*erf(b*x)*b/exp(b^2*x^2)/x^2-1/Pi^(1/2)*b^3*(-1
/exp(b^2*x^2)^2/b/x-2^(1/2)*Pi^(1/2)*erf(b*x*2^(1/2))))/b
```

Maximà [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x^3+b^2*erfc(b*x)/exp(b^2*x^2)/x,x, algori
thm="maxima")
```

```
[Out] integrate(b^2*erfc(b*x)*e^(-b^2*x^2)/x + erfc(b*x)*e^(-b^2*x^2)/x^3, x)
```

Fricas [A]
time = 0.37, size = 71, normalized size = 1.18

$$\frac{2\sqrt{2}\,\pi\sqrt{b^2}\,bx^2\operatorname{erf}\left(\sqrt{2}\,\sqrt{b^2}\,x\right)+2\sqrt{\pi}\,bxe^{\left(-2\,b^2x^2\right)}-(\pi-\pi\operatorname{erf}(bx))e^{\left(-b^2x^2\right)}}{2\,\pi x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x^3+b^2*erfc(b*x)/exp(b^2*x^2)/x,x, algori
thm="fricas")
```

```
[Out] 1/2*(2*sqrt(2)*pi*sqrt(b^2)*b*x^2*erf(sqrt(2)*sqrt(b^2)*x) + 2*sqrt(pi)*b*x
*e^(-2*b^2*x^2) - (pi - pi*erf(b*x))*e^(-b^2*x^2))/(pi*x^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int\frac{\left(b^2x^2+1\right)e^{-b^2x^2}\operatorname{erfc}(bx)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b**2*x**2)/x**3+b**2*erfc(b*x)/exp(b**2*x**2)/x,x)
```

```
[Out] Integral((b**2*x**2 + 1)*exp(-b**2*x**2)*erfc(b*x)/x**3, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)/exp(b^2*x^2)/x^3+b^2*erfc(b*x)/exp(b^2*x^2)/x,x, algori
thm="giac")
```

```
[Out] integrate(b^2*erfc(b*x)*e^(-b^2*x^2)/x + erfc(b*x)*e^(-b^2*x^2)/x^3, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{e^{-b^2 x^2} \operatorname{erfc}(b x)}{x^3} + \frac{b^2 e^{-b^2 x^2} \operatorname{erfc}(b x)}{x} \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erfc(b*x))/x^3 + (b^2*exp(-b^2*x^2)*erfc(b*x))/x,x)
[Out] int((exp(-b^2*x^2)*erfc(b*x))/x^3 + (b^2*exp(-b^2*x^2)*erfc(b*x))/x, x)
```

3.199 $\int \mathbf{Erfc}(bx)\sin\left(c+ib^2x^2\right)\,dx$

Optimal. Leaf size=91

$$\frac{ie^{ic}\sqrt{\pi}\,\mathrm{Erfc}(bx)^2}{8b}+\frac{ie^{-ic}\sqrt{\pi}\,\mathrm{Erfi}(bx)}{4b}-\frac{ibe^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] -1/2*I*b*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/exp(I*c)/Pi^(1/2)+1/8*I*exp
(I*c)*erfc(b*x)^2*Pi^(1/2)/b+1/4*I*erfi(b*x)*Pi^(1/2)/b/exp(I*c)
```

Rubi [A]
time = 0.06, antiderivative size = 91, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.333, Rules used = {6540, 6512, 2235, 6511, 6509, 30}

$$-\frac{ibe^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}+\frac{i\sqrt{\pi}\,e^{ic}\mathrm{Erfc}(bx)^2}{8b}+\frac{i\sqrt{\pi}\,e^{-ic}\mathrm{Erfi}(bx)}{4b}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]*Sin[c + I*b^2*x^2],x]
```

```
[Out] ((I/8)*E^(I*c)*Sqrt[Pi]*Erfc[b*x]^2)/b + ((I/4)*Sqrt[Pi]*Erfi[b*x])/(b*E^(I
*c)) - ((I/2)*b*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2])/(E^(I*c)*
Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
```

```
d}, x] && EqQ[d, b^2]
```

Rule 6512

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)], x_Symbol] :> Int[E^(c + d*x^
2), x] - Int[E^(c + d*x^2)*Erf[b*x], x] /; FreeQ[{b, c, d}, x] && EqQ[d, b^
2]
```

Rule 6540

```
Int[Erfc[(b_.)*(x_)]*Sin[(c_.) + (d_.)*(x_)^2], x_Symbol] :> Dist[I/2, Int[
E^((-I)*c - I*d*x^2)*Erfc[b*x], x], x] - Dist[I/2, Int[E^(I*c + I*d*x^2)*Er
fc[b*x], x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, -b^4]
```

Rubi steps

$$
\begin{aligned}
\int \operatorname{erfc}(bx)\sin\left(c+ib^2x^2\right)\,dx &= -\left(\frac{1}{2}i\int e^{ic-b^2x^2}\operatorname{erfc}(bx)\,dx\right)+\frac{1}{2}i\int e^{-ic+b^2x^2}\operatorname{erfc}(bx)\,dx \\
&= \frac{1}{2}i\int e^{-ic+b^2x^2}\,dx-\frac{1}{2}i\int e^{-ic+b^2x^2}\operatorname{erf}(bx)\,dx+\frac{\left(ie^{ic}\sqrt{\pi}\right)\operatorname{Subst}(\int x\,dx,x,\mathrm{e}}{4b} \\
&= \frac{ie^{ic}\sqrt{\pi}\operatorname{erfc}(bx)^2}{8b}+\frac{ie^{-ic}\sqrt{\pi}\operatorname{erfi}(bx)}{4b}-\frac{ibe^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}
\end{aligned}
$$

Mathematica [A]
time = 0.29, size = 94, normalized size = 1.03

$$\frac{(i\cos(c)+\sin(c))\left(-4b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)+\pi(2\operatorname{Erfi}(bx)-2\operatorname{Erf}(bx)(\cos(2c)+i\sin(2c))+\operatorname{Erf}(bx)^2(\cos(2c)+i\sin(2c)))\right)}{8b\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]*Sin[c + I*b^2*x^2],x]
```

```
[Out] ((I*Cos[c] + Sin[c])*(-4*b^2*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^
2] + Pi*(2*Erfi[b*x] - 2*Erf[b*x]*(Cos[2*c] + I*Sin[2*c]) + Erf[b*x]^2*(Cos
[2*c] + I*Sin[2*c]))))/(8*b*Sqrt[Pi])
```

Maple [F]
time = 0.13, size = 0, normalized size = 0.00

$$\int \operatorname{erfc}(bx)\sin\left(ib^2x^2+c\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)*sin(c+I*b^2*x^2),x)
```

```
[Out] int(erfc(b*x)*sin(c+I*b^2*x^2),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)*sin(c+I*b^2*x^2),x, algorithm="maxima")
```

```
[Out] 1/8*I*sqrt(pi)*cos(c)*erfc(b*x)^2/b - 1/8*sqrt(pi)*erfc(b*x)^2*sin(c)/b + 1
/2*I*cos(c)*integrate(erfc(b*x)*e^(b^2*x^2), x) + 1/2*integrate(erfc(b*x)*e
^(b^2*x^2), x)*sin(c)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)*sin(c+I*b^2*x^2),x, algorithm="fricas")
```

```
[Out] integral(1/2*((I*erf(b*x) - I)*e^(-2*b^2*x^2 + 2*I*c) - I*erf(b*x) + I)*e^(
b^2*x^2 - I*c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \sin\left(ib^2x^2 + c\right)\operatorname{erfc}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)*sin(c+I*b**2*x**2),x)
```

```
[Out] Integral(sin(I*b**2*x**2 + c)*erfc(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)*sin(c+I*b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(erfc(b*x)*sin(I*b^2*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \sin \left(b^2 x^2 1\mathrm{i} + c\right) \operatorname{erfc}(b x) \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(sin(c + b^2*x^2*1i)*erfc(b*x),x)
[Out] int(sin(c + b^2*x^2*1i)*erfc(b*x), x)
```

3.200 $\int \textbf{Erfc}(bx)\sin\left(c-ib^2x^2\right)\,dx$

Optimal. Leaf size=91

$$-\frac{ie^{-ic}\sqrt{\pi}\,\mathrm{Erfc}(bx)^2}{8b}-\frac{ie^{ic}\sqrt{\pi}\,\mathrm{Erfi}(bx)}{4b}+\frac{ibe^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] 1/2*I*b*exp(I*c)*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/Pi^(1/2)-1/8*I*erfc
(b*x)^2*Pi^(1/2)/b/exp(I*c)-1/4*I*exp(I*c)*erfi(b*x)*Pi^(1/2)/b
```

Rubi [A]
time = 0.05, antiderivative size = 91, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}}=0.333$, Rules used = {6540, 6509, 30, 6512, 2235, 6511}

$$\frac{ibe^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}-\frac{i\sqrt{\pi}\,e^{-ic}\mathrm{Erfc}(bx)^2}{8b}-\frac{i\sqrt{\pi}\,e^{ic}\mathrm{Erfi}(bx)}{4b}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]*Sin[c - I*b^2*x^2],x]
```

```
[Out] ((-1/8*I)*Sqrt[Pi]*Erfc[b*x]^2)/(b*E^(I*c)) - ((I/4)*E^(I*c)*Sqrt[Pi]*Erfi[
b*x])/b + ((I/2)*b*E^(I*c)*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2]
)/Sqrt[Pi]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
```

```
d}, x] && EqQ[d, b^2]
```

Rule 6512

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)], x_Symbol] :> Int[E^(c + d*x^
2), x] - Int[E^(c + d*x^2)*Erf[b*x], x] /; FreeQ[{b, c, d}, x] && EqQ[d, b^
2]
```

Rule 6540

```
Int[Erfc[(b_.)*(x_)]*Sin[(c_.) + (d_.)*(x_)^2], x_Symbol] :> Dist[I/2, Int[
E^((-I)*c - I*d*x^2)*Erfc[b*x], x], x] - Dist[I/2, Int[E^(I*c + I*d*x^2)*Er
fc[b*x], x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, -b^4]
```

Rubi steps

$$\begin{aligned}\int \operatorname{erfc}(bx)\sin\left(c-ib^2x^2\right)\,dx &= \frac{1}{2}i\int e^{-ic-b^2x^2}\operatorname{erfc}(bx)\,dx-\frac{1}{2}i\int e^{ic+b^2x^2}\operatorname{erfc}(bx)\,dx\\ &= -\left(\frac{1}{2}i\int e^{ic+b^2x^2}\,dx\right)+\frac{1}{2}i\int e^{ic+b^2x^2}\operatorname{erf}(bx)\,dx-\frac{\left(ie^{-ic}\sqrt{\pi}\right)\operatorname{Subst}(\int x\,dx,\\ &= -\frac{ie^{-ic}\sqrt{\pi}\operatorname{erfc}(bx)^2}{8b}-\frac{ie^{ic}\sqrt{\pi}\operatorname{erfi}(bx)}{4b}+\frac{ibe^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.29, size = 101, normalized size = 1.11

$$\frac{1}{2}i\left(-\frac{\sqrt{\pi}\left(-2\text{Erf}(bx)(\cos(c)-i\sin(c))+\text{Erf}(bx)^2(\cos(c)-i\sin(c))+2\text{Erfi}(bx)(\cos(c)+i\sin(c))\right)}{4b}+\frac{bx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)(\cos(c)+i\sin(c))}{\sqrt{\pi}}\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]*Sin[c - I*b^2*x^2],x]
```

```
[Out] (I/2)*(-1/4*(Sqrt[Pi]*(-2*Erf[b*x]*(Cos[c] - I*Sin[c]) + Erf[b*x]^2*(Cos[c]
 - I*Sin[c]) + 2*Erfi[b*x]*(Cos[c] + I*Sin[c])))/b + (b*x^2*HypergeometricP
FQ[{1, 1}, {3/2, 2}, b^2*x^2]*(Cos[c] + I*Sin[c]))/Sqrt[Pi])
```

Maple [F]
time = 0.12, size = 0, normalized size = 0.00

$$\int -\operatorname{erfc}(bx)\sin\left(ib^2x^2-c\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(-erfc(b*x)*sin(-c+I*b^2*x^2),x)
```

```
[Out] int(-erfc(b*x)*sin(-c+I*b^2*x^2),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfc(b*x)*sin(-c+I*b^2*x^2),x, algorithm="maxima")
```

```
[Out] -1/8*I*sqrt(pi)*cos(c)*erfc(b*x)^2/b - 1/8*sqrt(pi)*erfc(b*x)^2*sin(c)/b -
1/2*I*cos(c)*integrate(erfc(b*x)*e^(b^2*x^2), x) + 1/2*integrate(erfc(b*x)*
e^(b^2*x^2), x)*sin(c)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfc(b*x)*sin(-c+I*b^2*x^2),x, algorithm="fricas")
```

```
[Out] integral(1/2*((-I*erf(b*x) + I)*e^(-2*b^2*x^2 - 2*I*c) + I*erf(b*x) - I)*e^
(b^2*x^2 + I*c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$-\int \sin\left(ib^2x^2 - c\right)\operatorname{erfc}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfc(b*x)*sin(-c+I*b**2*x**2),x)
```

```
[Out] -Integral(sin(I*b**2*x**2 - c)*erfc(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfc(b*x)*sin(-c+I*b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(-erfc(b*x)*sin(I*b^2*x^2 - c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \sin \left(c - b^2 x^2 \, 1\mathrm{i}\right) \operatorname{erfc}(b\,x) \,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(sin(c - b^2*x^2*1i)*erfc(b*x),x)
[Out] int(sin(c - b^2*x^2*1i)*erfc(b*x), x)
```

3.201 $\int \cos\left(c + ib^2x^2\right) \mathbf{Erfc}(bx)\, dx$

Optimal. Leaf size=85

$$-\frac{e^{ic}\sqrt{\pi}\,\mathrm{Erfc}(bx)^2}{8b}+\frac{e^{-ic}\sqrt{\pi}\,\mathrm{Erfi}(bx)}{4b}-\frac{be^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] -1/2*b*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/exp(I*c)/Pi^(1/2)-1/8*exp(I*c
)*erfc(b*x)^2*Pi^(1/2)/b+1/4*erfi(b*x)*Pi^(1/2)/b/exp(I*c)
```

Rubi [A]
time = 0.05, antiderivative size = 85, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {6543, 6512, 2235, 6511, 6509, 30}

$$-\frac{be^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}-\frac{\sqrt{\pi}\,e^{ic}\mathrm{Erfc}(bx)^2}{8b}+\frac{\sqrt{\pi}\,e^{-ic}\mathrm{Erfi}(bx)}{4b}$$

Antiderivative was successfully verified.

```
[In] Int[Cos[c + I*b^2*x^2]*Erfc[b*x],x]
```

```
[Out] -1/8*(E^(I*c)*Sqrt[Pi]*Erfc[b*x]^2)/b + (Sqrt[Pi]*Erfi[b*x])/(4*b*E^(I*c))
- (b*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2])/(2*E^(I*c)*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6512

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)], x_Symbol] :> Int[E^(c + d*x^
2), x] - Int[E^(c + d*x^2)*Erf[b*x], x] /; FreeQ[{b, c, d}, x] && EqQ[d, b^
2]
```

Rule 6543

```
Int[Cos[(c_.) + (d_.)*(x_)^2]*Erfc[(b_.)*(x_)], x_Symbol] :> Dist[1/2, Int[
E^((-I)*c - I*d*x^2)*Erfc[b*x], x], x] + Dist[1/2, Int[E^(I*c + I*d*x^2)*Er
fc[b*x], x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, -b^4]
```

Rubi steps

$$\begin{aligned}\int \cos\left(c+ib^2x^2\right)\operatorname{erfc}(bx)\,dx &= \frac{1}{2}\int e^{ic-b^2x^2}\operatorname{erfc}(bx)\,dx+\frac{1}{2}\int e^{-ic+b^2x^2}\operatorname{erfc}(bx)\,dx\\ &= \frac{1}{2}\int e^{-ic+b^2x^2}\,dx-\frac{1}{2}\int e^{-ic+b^2x^2}\operatorname{erf}(bx)\,dx-\frac{\left(e^{ic}\sqrt{\pi}\right)\operatorname{Subst}(\int x\,dx,x,\operatorname{erfc}\\ &= -\frac{e^{ic}\sqrt{\pi}\operatorname{erfc}(bx)^2}{8b}+\frac{e^{-ic}\sqrt{\pi}\operatorname{erfi}(bx)}{4b}-\frac{be^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}\end{aligned}$$

Mathematica [F]
time = 1.13, size = 0, normalized size = 0.00

$$\int \cos\left(c+ib^2x^2\right)\operatorname{Erfc}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Cos[c + I*b^2*x^2]*Erfc[b*x],x]
[Out] Integrate[Cos[c + I*b^2*x^2]*Erfc[b*x], x]
```

Maple [F]
time = 0.41, size = 0, normalized size = 0.00

$$\int \cos\left(ib^2x^2+c\right)\operatorname{erfc}(bx)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cos(c+I*b^2*x^2)*erfc(b*x),x)
[Out] int(cos(c+I*b^2*x^2)*erfc(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(c+I*b^2*x^2)*erfc(b*x),x, algorithm="maxima")
```

```
[Out] -1/8*sqrt(pi)*cos(c)*erfc(b*x)^2/b - 1/8*I*sqrt(pi)*erfc(b*x)^2*sin(c)/b +
1/2*cos(c)*integrate(erfc(b*x)*e^(b^2*x^2), x) - 1/2*I*integrate(erfc(b*x)*
e^(b^2*x^2), x)*sin(c)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(c+I*b^2*x^2)*erfc(b*x),x, algorithm="fricas")
```

```
[Out] integral(-1/2*((erf(b*x) - 1)*e^(-2*b^2*x^2 + 2*I*c) + erf(b*x) - 1)*e^(b^2
*x^2 - I*c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \cos\left(ib^2x^2 + c\right)\operatorname{erfc}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(c+I*b**2*x**2)*erfc(b*x),x)
```

```
[Out] Integral(cos(I*b**2*x**2 + c)*erfc(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(c+I*b^2*x^2)*erfc(b*x),x, algorithm="giac")
```

```
[Out] integrate(cos(I*b^2*x^2 + c)*erfc(b*x), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \cos\left(b^2\,x^2\,1\mathrm{i}+c\right)\,\mathrm{erfc}(b\,x)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cos(c + b^2*x^2*1i)*erfc(b*x),x)
```

```
[Out] int(cos(c + b^2*x^2*1i)*erfc(b*x), x)
```

3.202 $\int \cos(c - ib^2x^2)\,\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=85

$$-\frac{e^{-ic}\sqrt{\pi}\,\mathrm{Erfc}(bx)^2}{8b}+\frac{e^{ic}\sqrt{\pi}\,\mathrm{Erfi}(bx)}{4b}-\frac{be^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] -1/2*b*exp(I*c)*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/Pi^(1/2)-1/8*erfc(b*
x)^2*Pi^(1/2)/b/exp(I*c)+1/4*exp(I*c)*erfi(b*x)*Pi^(1/2)/b
```

Rubi [A]
time = 0.05, antiderivative size = 85, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {6543, 6509, 30, 6512, 2235, 6511}

$$-\frac{be^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}-\frac{\sqrt{\pi}\,e^{-ic}\mathrm{Erfc}(bx)^2}{8b}+\frac{\sqrt{\pi}\,e^{ic}\mathrm{Erfi}(bx)}{4b}$$

Antiderivative was successfully verified.

```
[In] Int[Cos[c - I*b^2*x^2]*Erfc[b*x],x]
```

```
[Out] -1/8*(Sqrt[Pi]*Erfc[b*x]^2)/(b*E^(I*c)) + (E^(I*c)*Sqrt[Pi]*Erfi[b*x])/(4*b
) - (b*E^(I*c)*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2])/(2*Sqrt[Pi
])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
```

```
d}, x] && EqQ[d, b^2]
```

Rule 6512

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)], x_Symbol] :> Int[E^(c + d*x^
2), x] - Int[E^(c + d*x^2)*Erf[b*x], x] /; FreeQ[{b, c, d}, x] && EqQ[d, b^
2]
```

Rule 6543

```
Int[Cos[(c_.) + (d_.)*(x_)^2]*Erfc[(b_.)*(x_)], x_Symbol] :> Dist[1/2, Int[
E^((-I)*c - I*d*x^2)*Erfc[b*x], x], x] + Dist[1/2, Int[E^(I*c + I*d*x^2)*Er
fc[b*x], x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, -b^4]
```

Rubi steps

$$\begin{aligned}\int \cos\left(c-ib^2x^2\right)\operatorname{erfc}(bx)\,dx &= \frac{1}{2}\int e^{-ic-b^2x^2}\operatorname{erfc}(bx)\,dx+\frac{1}{2}\int e^{ic+b^2x^2}\operatorname{erfc}(bx)\,dx\\ &= \frac{1}{2}\int e^{ic+b^2x^2}\,dx-\frac{1}{2}\int e^{ic+b^2x^2}\operatorname{erf}(bx)\,dx-\frac{\left(e^{-ic}\sqrt{\pi}\right)\operatorname{Subst}(\int x\,dx,x,\operatorname{erfc}(\\ &= -\frac{e^{-ic}\sqrt{\pi}\operatorname{erfc}(bx)^2}{8b}+\frac{e^{ic}\sqrt{\pi}\operatorname{erfi}(bx)}{4b}-\frac{be^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}\end{aligned}$$

Mathematica [F]
time = 1.27, size = 0, normalized size = 0.00

$$\int \cos\left(c-ib^2x^2\right)\operatorname{Erfc}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Cos[c - I*b^2*x^2]*Erfc[b*x],x]
[Out] Integrate[Cos[c - I*b^2*x^2]*Erfc[b*x], x]
```

Maple [F]
time = 0.41, size = 0, normalized size = 0.00

$$\int \cos\left(ib^2x^2-c\right)\operatorname{erfc}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cos(-c+I*b^2*x^2)*erfc(b*x),x)
```

```
[Out] int(cos(-c+I*b^2*x^2)*erfc(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(-c+I*b^2*x^2)*erfc(b*x),x, algorithm="maxima")
```

```
[Out] -1/8*sqrt(pi)*cos(c)*erfc(b*x)^2/b + 1/8*I*sqrt(pi)*erfc(b*x)^2*sin(c)/b +
1/2*cos(c)*integrate(erfc(b*x)*e^(b^2*x^2), x) + 1/2*I*integrate(erfc(b*x)*
e^(b^2*x^2), x)*sin(c)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(-c+I*b^2*x^2)*erfc(b*x),x, algorithm="fricas")
```

```
[Out] integral(-1/2*((erf(b*x) - 1)*e^(-2*b^2*x^2 - 2*I*c) + erf(b*x) - 1)*e^(b^2
*x^2 + I*c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \cos\left(ib^2x^2 - c\right) \operatorname{erfc}\left(bx\right) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(-c+I*b**2*x**2)*erfc(b*x),x)
```

```
[Out] Integral(cos(I*b**2*x**2 - c)*erfc(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(-c+I*b^2*x^2)*erfc(b*x),x, algorithm="giac")
```

```
[Out] integrate(cos(I*b^2*x^2 - c)*erfc(b*x), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \cos\left(c - b^2\,x^2\,1\mathrm{i}\right)\,\mathrm{erfc}(b\,x)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cos(c - b^2*x^2*1i)*erfc(b*x),x)
```

```
[Out] int(cos(c - b^2*x^2*1i)*erfc(b*x), x)
```

3.203 $\int \mathbf{Erfc}(bx)\sinh\left(c+b^2x^2\right)\,dx$

Optimal. Leaf size=75

$$\frac{e^{-c}\sqrt{\pi}\,\mathrm{Erfc}(bx)^2}{8b}+\frac{e^c\sqrt{\pi}\,\mathrm{Erfi}(bx)}{4b}-\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] -1/2*b*exp(c)*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/Pi^(1/2)+1/8*erfc(b*x)
^2*Pi^(1/2)/b/exp(c)+1/4*exp(c)*erfi(b*x)*Pi^(1/2)/b
```

Rubi [A]
time = 0.05, antiderivative size = 75, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}}=0.400$, Rules used = {6546, 6512, 2235, 6511, 6509, 30}

$$-\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}+\frac{\sqrt{\pi}\,e^{-c}\mathrm{Erfc}(bx)^2}{8b}+\frac{\sqrt{\pi}\,e^c\mathrm{Erfi}(bx)}{4b}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]*Sinh[c + b^2*x^2],x]
```

```
[Out] (Sqrt[Pi]*Erfc[b*x]^2)/(8*b*E^c) + (E^c*Sqrt[Pi]*Erfi[b*x])/(4*b) - (b*E^c*
x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2])/(2*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6512

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)], x_Symbol] :> Int[E^(c + d*x^
2), x] - Int[E^(c + d*x^2)*Erf[b*x], x] /; FreeQ[{b, c, d}, x] && EqQ[d, b^
2]
```

Rule 6546

```
Int[Erfc[(b_.)*(x_)]*Sinh[(c_.) + (d_.)*(x_)^2], x_Symbol] :> Dist[1/2, Int
[E^(c + d*x^2)*Erfc[b*x], x], x] - Dist[1/2, Int[E^(-c - d*x^2)*Erfc[b*x],
x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, b^4]
```

Rubi steps

$$\begin{aligned}\int \operatorname{erfc}(bx)\sinh\left(c+b^2x^2\right)\,dx &= -\left(\frac{1}{2}\int e^{-c-b^2x^2}\operatorname{erfc}(bx)\,dx\right)+\frac{1}{2}\int e^{c+b^2x^2}\operatorname{erfc}(bx)\,dx\\ &= \frac{1}{2}\int e^{c+b^2x^2}\,dx-\frac{1}{2}\int e^{c+b^2x^2}\operatorname{erf}(bx)\,dx+\frac{\left(e^{-c}\sqrt{\pi}\right)\operatorname{Subst}(\int x\,dx,x,\operatorname{erfc}(b
}{4b}\\ &= \frac{e^{-c}\sqrt{\pi}\operatorname{erfc}(bx)^2}{8b}+\frac{e^c\sqrt{\pi}\operatorname{erfi}(bx)}{4b}-\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.11, size = 83, normalized size = 1.11

$$\frac{-4b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)(\cosh(c)+\sinh(c))+\pi(-2\operatorname{Erf}(bx)(\cosh(c)-\sinh(c))+\operatorname{Erf}(bx)^2(\cosh(c)-\sinh(c))+2\operatorname{Erfi}(bx)(\cosh(c)+\sinh(c)))}{8b\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]*Sinh[c + b^2*x^2],x]
[Out] (-4*b^2*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2]*(Cosh[c] + Sinh[c]
) + Pi*(-2*Erf[b*x]*(Cosh[c] - Sinh[c]) + Erf[b*x]^2*(Cosh[c] - Sinh[c]) +
2*Erfi[b*x]*(Cosh[c] + Sinh[c])))/(8*b*Sqrt[Pi])
```

Maple [F]
time = 0.14, size = 0, normalized size = 0.00

$$\int \operatorname{erfc}(bx)\sinh\left(b^2x^2+c\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfc(b*x)*sinh(b^2*x^2+c),x)
[Out] int(erfc(b*x)*sinh(b^2*x^2+c),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)*sinh(b^2*x^2+c),x, algorithm="maxima")
[Out] integrate(erfc(b*x)*sinh(b^2*x^2 + c), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)*sinh(b^2*x^2+c),x, algorithm="fricas")
[Out] integral(-(erf(b*x) - 1)*sinh(b^2*x^2 + c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \sinh\left(b^2x^2+c\right)\operatorname{erfc}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)*sinh(b**2*x**2+c),x)
[Out] Integral(sinh(b**2*x**2 + c)*erfc(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfc(b*x)*sinh(b^2*x^2+c),x, algorithm="giac")
[Out] integrate(erfc(b*x)*sinh(b^2*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \sinh\left(b^2\,x^2+c\right)\,\mathrm{erfc}\left(b\,x\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(sinh(c + b^2*x^2)*erfc(b*x),x)
[Out] int(sinh(c + b^2*x^2)*erfc(b*x), x)
```

3.204 $\int \mathbf{Erfc}(bx)\sinh\left(c-b^2x^2\right)\,dx$

Optimal. Leaf size=77

$$-\frac{e^c\sqrt{\pi}\,\mathrm{Erfc}(bx)^2}{8b}-\frac{e^{-c}\sqrt{\pi}\,\mathrm{Erfi}(bx)}{4b}+\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] 1/2*b*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/exp(c)/Pi^(1/2)-1/8*exp(c)*erf
c(b*x)^2*Pi^(1/2)/b-1/4*erfi(b*x)*Pi^(1/2)/b/exp(c)
```

Rubi [A]
time = 0.05, antiderivative size = 77, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.375, Rules used = {6546, 6509, 30, 6512, 2235, 6511}

$$\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}-\frac{\sqrt{\pi}\,e^c\mathrm{Erfc}(bx)^2}{8b}-\frac{\sqrt{\pi}\,e^{-c}\mathrm{Erfi}(bx)}{4b}$$

Antiderivative was successfully verified.

```
[In] Int[Erfc[b*x]*Sinh[c - b^2*x^2],x]
```

```
[Out] -1/8*(E^c*Sqrt[Pi]*Erfc[b*x]^2)/b - (Sqrt[Pi]*Erfi[b*x])/(4*b*E^c) + (b*x^2
*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2])/(2*E^c*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6512

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)], x_Symbol] :> Int[E^(c + d*x^
2), x] - Int[E^(c + d*x^2)*Erf[b*x], x] /; FreeQ[{b, c, d}, x] && EqQ[d, b^
2]
```

Rule 6546

```
Int[Erfc[(b_.)*(x_)]*Sinh[(c_.) + (d_.)*(x_)^2], x_Symbol] :> Dist[1/2, Int
[E^(c + d*x^2)*Erfc[b*x], x], x] - Dist[1/2, Int[E^(-c - d*x^2)*Erfc[b*x],
x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, b^4]
```

Rubi steps

$$\begin{aligned}\int \operatorname{erfc}(bx)\sinh\left(c-b^2x^2\right)\,dx &= \frac{1}{2}\int e^{c-b^2x^2}\operatorname{erfc}(bx)\,dx-\frac{1}{2}\int e^{-c+b^2x^2}\operatorname{erfc}(bx)\,dx\\ &= -\left(\frac{1}{2}\int e^{-c+b^2x^2}\,dx\right)+\frac{1}{2}\int e^{-c+b^2x^2}\operatorname{erf}(bx)\,dx-\frac{\left(e^c\sqrt{\pi}\right)\operatorname{Subst}(\int x\,dx,x,e\\ &= -\frac{e^c\sqrt{\pi}\operatorname{erfc}(bx)^2}{8b}-\frac{e^{-c}\sqrt{\pi}\operatorname{erfi}(bx)}{4b}+\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.11, size = 84, normalized size = 1.09

$$-\frac{(\cosh(c)-\sinh(c))\left(-4b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)+\pi(2\operatorname{Erfi}(bx)-2\operatorname{Erf}(bx)(\cosh(2c)+\sinh(2c))+\operatorname{Erf}(bx)^2(\cosh(2c)+\sinh(2c)))\right)}{8b\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfc[b*x]*Sinh[c - b^2*x^2],x]
[Out] -1/8*((Cosh[c] - Sinh[c])*(-4*b^2*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b
^2*x^2] + Pi*(2*Erfi[b*x] - 2*Erf[b*x]*(Cosh[2*c] + Sinh[2*c]) + Erf[b*x]^2
*(Cosh[2*c] + Sinh[2*c]))))/(b*Sqrt[Pi])
```

Maple [F]
time = 0.12, size = 0, normalized size = 0.00

$$\int -\operatorname{erfc}(bx)\sinh\left(b^2x^2-c\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(-erfc(b*x)*sinh(b^2*x^2-c),x)
```

```
[Out] int(-erfc(b*x)*sinh(b^2*x^2-c),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfc(b*x)*sinh(b^2*x^2-c),x, algorithm="maxima")
[Out] -integrate(erfc(b*x)*sinh(b^2*x^2 - c), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfc(b*x)*sinh(b^2*x^2-c),x, algorithm="fricas")
[Out] integral((erf(b*x) - 1)*sinh(b^2*x^2 - c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$-\int \sinh\left(b^2x^2-c\right)\operatorname{erfc}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfc(b*x)*sinh(b**2*x**2-c),x)
[Out] -Integral(sinh(b**2*x**2 - c)*erfc(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfc(b*x)*sinh(b^2*x^2-c),x, algorithm="giac")
[Out] integrate(-erfc(b*x)*sinh(b^2*x^2 - c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \sinh\left(c-b^2\,x^2\right)\,\mathrm{erfc}\left(b\,x\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(sinh(c - b^2*x^2)*erfc(b*x),x)
[Out] int(sinh(c - b^2*x^2)*erfc(b*x), x)
```

3.205 $\int \cosh(c+b^2x^2)\,\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=75

$$-\frac{e^{-c}\sqrt{\pi}\,\mathrm{Erfc}(bx)^2}{8b}+\frac{e^{c}\sqrt{\pi}\,\mathrm{Erfi}(bx)}{4b}-\frac{be^{c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] -1/2*b*exp(c)*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/Pi^(1/2)-1/8*erfc(b*x)
^2*Pi^(1/2)/b/exp(c)+1/4*exp(c)*erfi(b*x)*Pi^(1/2)/b
```

Rubi [A]
time = 0.05, antiderivative size = 75, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.400, Rules used = {6549, 6512, 2235, 6511, 6509, 30}

$$-\frac{be^{c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}-\frac{\sqrt{\pi}\,e^{-c}\mathrm{Erfc}(bx)^2}{8b}+\frac{\sqrt{\pi}\,e^{c}\mathrm{Erfi}(bx)}{4b}$$

Antiderivative was successfully verified.

```
[In] Int[Cosh[c + b^2*x^2]*Erfc[b*x],x]
```

```
[Out] -1/8*(Sqrt[Pi]*Erfc[b*x]^2)/(b*E^c) + (E^c*Sqrt[Pi]*Erfi[b*x])/(4*b) - (b*E
^c*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2])/(2*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6512

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)], x_Symbol] :> Int[E^(c + d*x^
2), x] - Int[E^(c + d*x^2)*Erf[b*x], x] /; FreeQ[{b, c, d}, x] && EqQ[d, b^
2]
```

Rule 6549

```
Int[Cosh[(c_.) + (d_.)*(x_)^2]*Erfc[(b_.)*(x_)], x_Symbol] :> Dist[1/2, Int
[E^(c + d*x^2)*Erfc[b*x], x], x] + Dist[1/2, Int[E^(-c - d*x^2)*Erfc[b*x],
x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, b^4]
```

Rubi steps

$$\begin{aligned}\int \cosh\left(c+b^2x^2\right)\operatorname{erfc}(bx)\,dx &= \frac{1}{2}\int e^{-c-b^2x^2}\operatorname{erfc}(bx)\,dx+\frac{1}{2}\int e^{c+b^2x^2}\operatorname{erfc}(bx)\,dx\\ &= \frac{1}{2}\int e^{c+b^2x^2}\,dx-\frac{1}{2}\int e^{c+b^2x^2}\operatorname{erf}(bx)\,dx-\frac{\left(e^{-c}\sqrt{\pi}\right)\operatorname{Subst}(\int x\,dx,x,\operatorname{erfc}(bx\\ &= -\frac{e^{-c}\sqrt{\pi}\operatorname{erfc}(bx)^2}{8b}+\frac{e^{c}\sqrt{\pi}\operatorname{erfi}(bx)}{4b}-\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.09, size = 114, normalized size = 1.52

$$\frac{4b^2x^2\cosh(c)\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)-4b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)\sinh(c)+\pi(\operatorname{Erf}(bx)^2(-\cosh(c)+\sinh(c))+2\operatorname{Erfi}(bx)(\cosh(c)+\sinh(c))-2\operatorname{Erf}(bx)(-\cosh(c)+\cosh(c)\operatorname{Erfi}(bx)+\sinh(c)))}{8b\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Cosh[c + b^2*x^2]*Erfc[b*x],x]
```

```
[Out] (4*b^2*x^2*Cosh[c]*HypergeometricPFQ[{1, 1}, {3/2, 2}, -(b^2*x^2)] - 4*b^2*
x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2]*Sinh[c] + Pi*(Erf[b*x]^2*(
-Cosh[c] + Sinh[c]) + 2*Erfi[b*x]*(Cosh[c] + Sinh[c]) - 2*Erf[b*x]*(-Cosh[c
] + Cosh[c]*Erfi[b*x] + Sinh[c])))/(8*b*Sqrt[Pi])
```

Maple [F]
time = 0.46, size = 0, normalized size = 0.00

$$\int \cosh\left(b^2x^2+c\right)\operatorname{erfc}(bx)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cosh(b^2*x^2+c)*erfc(b*x),x)
```

```
[Out] int(cosh(b^2*x^2+c)*erfc(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2+c)*erfc(b*x),x, algorithm="maxima")
[Out] integrate(cosh(b^2*x^2 + c)*erfc(b*x), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2+c)*erfc(b*x),x, algorithm="fricas")
[Out] integral(-cosh(b^2*x^2 + c)*erf(b*x) + cosh(b^2*x^2 + c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \cosh\left(b^{2}x^{2}+c\right)\operatorname{erfc}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b**2*x**2+c)*erfc(b*x),x)
[Out] Integral(cosh(b**2*x**2 + c)*erfc(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2+c)*erfc(b*x),x, algorithm="giac")
[Out] integrate(cosh(b^2*x^2 + c)*erfc(b*x), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \cosh\left(b^2\,x^2+c\right)\,\mathrm{erfc}\left(b\,x\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cosh(c + b^2*x^2)*erfc(b*x),x)
[Out] int(cosh(c + b^2*x^2)*erfc(b*x), x)
```

3.206 $\int \cosh\left(c-b^2x^2\right)\mathbf{Erfc}(bx)\,dx$

Optimal. Leaf size=77

$$-\frac{e^c\sqrt{\pi}\,\mathrm{Erfc}(bx)^2}{8b}+\frac{e^{-c}\sqrt{\pi}\,\mathrm{Erfi}(bx)}{4b}-\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] -1/2*b*x^2*hypergeom([1, 1],[3/2, 2],b^2*x^2)/exp(c)/Pi^(1/2)-1/8*exp(c)*er
fc(b*x)^2*Pi^(1/2)/b+1/4*erfi(b*x)*Pi^(1/2)/b/exp(c)
```

Rubi [A]
time = 0.05, antiderivative size = 77, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 6, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}}=0.375$, Rules used = {6549, 6509, 30, 6512, 2235, 6511}

$$-\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}-\frac{\sqrt{\pi}\,e^c\mathrm{Erfc}(bx)^2}{8b}+\frac{\sqrt{\pi}\,e^{-c}\mathrm{Erfi}(bx)}{4b}$$

Antiderivative was successfully verified.

```
[In] Int[Cosh[c - b^2*x^2]*Erfc[b*x],x]
```

```
[Out] -1/8*(E^c*Sqrt[Pi]*Erfc[b*x]^2)/b + (Sqrt[Pi]*Erfi[b*x])/(4*b*E^c) - (b*x^2
*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2])/(2*E^c*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6509

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[(-E^
c)*(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfc[b*x]], x] /; FreeQ[{b, c, d
, n}, x] && EqQ[d, -b^2]
```

Rule 6511

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erf[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2/
Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2], x] /; FreeQ[{b, c,
d}, x] && EqQ[d, b^2]
```

Rule 6512

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfc[(b_.)*(x_)], x_Symbol] :> Int[E^(c + d*x^
2), x] - Int[E^(c + d*x^2)*Erf[b*x], x] /; FreeQ[{b, c, d}, x] && EqQ[d, b^
2]
```

Rule 6549

```
Int[Cosh[(c_.) + (d_.)*(x_)^2]*Erfc[(b_.)*(x_)], x_Symbol] :> Dist[1/2, Int
[E^(c + d*x^2)*Erfc[b*x], x], x] + Dist[1/2, Int[E^(-c - d*x^2)*Erfc[b*x],
x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, b^4]
```

Rubi steps

$$\begin{aligned}\int \cosh\left(c-b^2x^2\right)\operatorname{erfc}(bx)\,dx &= \frac{1}{2}\int e^{c-b^2x^2}\operatorname{erfc}(bx)\,dx+\frac{1}{2}\int e^{-c+b^2x^2}\operatorname{erfc}(bx)\,dx\\ &= \frac{1}{2}\int e^{-c+b^2x^2}\,dx-\frac{1}{2}\int e^{-c+b^2x^2}\operatorname{erf}(bx)\,dx-\frac{\left(e^c\sqrt{\pi}\right)\operatorname{Subst}(\int x\,dx,x,\operatorname{erfc}(bx\\ &= -\frac{e^c\sqrt{\pi}\operatorname{erfc}(bx)^2}{8b}+\frac{e^{-c}\sqrt{\pi}\operatorname{erfi}(bx)}{4b}-\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)}{2\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.08, size = 117, normalized size = 1.52

$$\frac{4b^2x^2\cosh(c)\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)+4b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)\sinh(c)-\pi(2\operatorname{Erf}(bx)(-\cosh(c)+\cosh(c)\operatorname{Erfi}(bx)-\sinh(c))+2\operatorname{Erfi}(bx)(-\cosh(c)+\sinh(c))+\operatorname{Erf}(bx)^2(\cosh(c)+\sinh(c)))}{8b\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Cosh[c - b^2*x^2]*Erfc[b*x],x]
```

```
[Out] (4*b^2*x^2*Cosh[c]*HypergeometricPFQ[{1, 1}, {3/2, 2}, -(b^2*x^2)] + 4*b^2*
x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2]*Sinh[c] - Pi*(2*Erf[b*x]*(
-Cosh[c] + Cosh[c]*Erfi[b*x] - Sinh[c]) + 2*Erfi[b*x]*(-Cosh[c] + Sinh[c])
+ Erf[b*x]^2*(Cosh[c] + Sinh[c])))/(8*b*Sqrt[Pi])
```

Maple [F]
time = 0.43, size = 0, normalized size = 0.00

$$\int \cosh\left(b^2x^2-c\right)\operatorname{erfc}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cosh(b^2*x^2-c)*erfc(b*x),x)
```

```
[Out] int(cosh(b^2*x^2-c)*erfc(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2-c)*erfc(b*x),x, algorithm="maxima")
[Out] integrate(cosh(b^2*x^2 - c)*erfc(b*x), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2-c)*erfc(b*x),x, algorithm="fricas")
[Out] integral(-cosh(b^2*x^2 - c)*erf(b*x) + cosh(b^2*x^2 - c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \cosh\left(b^{2}x^{2}-c\right)\operatorname{erfc}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b**2*x**2-c)*erfc(b*x),x)
[Out] Integral(cosh(b**2*x**2 - c)*erfc(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2-c)*erfc(b*x),x, algorithm="giac")
[Out] integrate(cosh(b^2*x^2 - c)*erfc(b*x), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \cosh\left(c-b^{2}\,x^{2}\right)\,\operatorname{erfc}(b\,x)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cosh(c - b^2*x^2)*erfc(b*x),x)
[Out] int(cosh(c - b^2*x^2)*erfc(b*x), x)
```

3.207 $\int x^5 \mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=93

$$-\frac{5e^{b^2x^2}x}{8b^5\sqrt{\pi}}+\frac{5e^{b^2x^2}x^3}{12b^3\sqrt{\pi}}-\frac{e^{b^2x^2}x^5}{6b\sqrt{\pi}}+\frac{5\mathrm{Erfi}(bx)}{16b^6}+\frac{1}{6}x^6\mathrm{Erfi}(bx)$$

```
[Out] 5/16*erfi(b*x)/b^6+1/6*x^6*erfi(b*x)-5/8*exp(b^2*x^2)*x/b^5/Pi^(1/2)+5/12*e
xp(b^2*x^2)*x^3/b^3/Pi^(1/2)-1/6*exp(b^2*x^2)*x^5/b/Pi^(1/2)
```

Rubi [A]
time = 0.06, antiderivative size = 93, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6498, 2243, 2235}

$$\frac{5\mathrm{Erfi}(bx)}{16b^6}-\frac{x^5e^{b^2x^2}}{6\sqrt{\pi}\,b}-\frac{5xe^{b^2x^2}}{8\sqrt{\pi}\,b^5}+\frac{5x^3e^{b^2x^2}}{12\sqrt{\pi}\,b^3}+\frac{1}{6}x^6\mathrm{Erfi}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x^5*Erfi[b*x],x]
```

```
[Out] (-5*E^(b^2*x^2)*x)/(8*b^5*Sqrt[Pi]) + (5*E^(b^2*x^2)*x^3)/(12*b^3*Sqrt[Pi])
 - (E^(b^2*x^2)*x^5)/(6*b*Sqrt[Pi]) + (5*Erfi[b*x])/(16*b^6) + (x^6*Erfi[b*
x])/6
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6498

```
Int[Erfi[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfi[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)*E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int x^5\text{erfi}(bx)\,dx &= \frac{1}{6}x^6\text{erfi}(bx)-\frac{b\int e^{b^2x^2}x^6\,dx}{3\sqrt{\pi}}\\
&= -\frac{e^{b^2x^2}x^5}{6b\sqrt{\pi}}+\frac{1}{6}x^6\text{erfi}(bx)+\frac{5\int e^{b^2x^2}x^4\,dx}{6b\sqrt{\pi}}\\
&= \frac{5e^{b^2x^2}x^3}{12b^3\sqrt{\pi}}-\frac{e^{b^2x^2}x^5}{6b\sqrt{\pi}}+\frac{1}{6}x^6\text{erfi}(bx)-\frac{5\int e^{b^2x^2}x^2\,dx}{4b^3\sqrt{\pi}}\\
&= -\frac{5e^{b^2x^2}x}{8b^5\sqrt{\pi}}+\frac{5e^{b^2x^2}x^3}{12b^3\sqrt{\pi}}-\frac{e^{b^2x^2}x^5}{6b\sqrt{\pi}}+\frac{1}{6}x^6\text{erfi}(bx)+\frac{5\int e^{b^2x^2}\,dx}{8b^5\sqrt{\pi}}\\
&= -\frac{5e^{b^2x^2}x}{8b^5\sqrt{\pi}}+\frac{5e^{b^2x^2}x^3}{12b^3\sqrt{\pi}}-\frac{e^{b^2x^2}x^5}{6b\sqrt{\pi}}+\frac{5\text{erfi}(bx)}{16b^6}+\frac{1}{6}x^6\text{erfi}(bx)
\end{aligned}
$$

Mathematica [A]
time = 0.02, size = 64, normalized size = 0.69

$$\frac{-2be^{b^2x^2}x(15-10b^2x^2+4b^4x^4)+\sqrt{\pi}\,(15+8b^6x^6)\,\text{Erfi}(bx)}{48b^6\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^5*Erfi[b*x],x]
```

```
[Out] (-2*b*E^(b^2*x^2)*x*(15 - 10*b^2*x^2 + 4*b^4*x^4) + Sqrt[Pi]*(15 + 8*b^6*x^
6)*Erfi[b*x])/(48*b^6*Sqrt[Pi])
```

Maple [A]
time = 0.11, size = 77, normalized size = 0.83

method	result	size
meijerg	$\frac{i\left(\frac{ixb\left(28b^4x^4-70b^2x^2+105\right)e^{b^2x^2}}{84}-\frac{i\left(56b^6x^6+105\right)\text{erfi}(bx)\sqrt{\pi}}{168}\right)}{2b^6\sqrt{\pi}}$	62
derivativedivides	$\frac{\frac{b^6x^6\,\text{erfi}(bx)}{6}-\frac{\frac{b^5x^5e^{b^2x^2}}{2}-\frac{5b^3x^3e^{b^2x^2}}{4}+\frac{15\,e^{b^2x^2}bx}{8}-\frac{15\,\text{erfi}(bx)\sqrt{\pi}}{16}}{3\sqrt{\pi}}}{b^6}$	77
default	$\frac{\frac{b^6x^6\,\text{erfi}(bx)}{6}-\frac{\frac{b^5x^5e^{b^2x^2}}{2}-\frac{5b^3x^3e^{b^2x^2}}{4}+\frac{15\,e^{b^2x^2}bx}{8}-\frac{15\,\text{erfi}(bx)\sqrt{\pi}}{16}}{3\sqrt{\pi}}}{b^6}$	77

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*erfi(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b^6*(1/6*b^6*x^6*erfi(b*x)-1/3/Pi^(1/2)*(1/2*b^5*x^5*exp(b^2*x^2)-5/4*b^3
*x^3*exp(b^2*x^2)+15/8*exp(b^2*x^2)*b*x-15/16*erfi(b*x)*Pi^(1/2)))
```

Maxima [C] Result contains complex when optimal does not.
time = 0.27, size = 63, normalized size = 0.68

$$\frac{1}{6}\,x^{6}\,\mathrm{erfi}\left(bx\right)-\frac{b\left(\frac{2\,\left(4\,b^{4}x^{5}-10\,b^{2}x^{3}+15\,x\right)e^{\left(b^{2}x^{2}\right)}}{b^{6}}+\frac{15i\,\sqrt{\pi}\,\mathrm{erf}(i\,bx)}{b^{7}}\right)}{48\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfi(b*x),x, algorithm="maxima")
```

```
[Out] 1/6*x^6*erfi(b*x) - 1/48*b*(2*(4*b^4*x^5 - 10*b^2*x^3 + 15*x)*e^(b^2*x^2)/b
^6 + 15*I*sqrt(pi)*erf(I*b*x)/b^7)/sqrt(pi)
```

Fricas [A]
time = 0.36, size = 62, normalized size = 0.67

$$-\frac{2\,\sqrt{\pi}\,\left(4\,b^{5}x^{5}-10\,b^{3}x^{3}+15\,bx\right)e^{\left(b^{2}x^{2}\right)}-\left(15\,\pi+8\,\pi b^{6}x^{6}\right)\mathrm{erfi}\left(bx\right)}{48\,\pi b^{6}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfi(b*x),x, algorithm="fricas")
```

```
[Out] -1/48*(2*sqrt(pi)*(4*b^5*x^5 - 10*b^3*x^3 + 15*b*x)*e^(b^2*x^2) - (15*pi +
8*pi*b^6*x^6)*erfi(b*x))/(pi*b^6)
```

Sympy [A]
time = 0.42, size = 88, normalized size = 0.95

$$\begin{cases}\frac{x^{6}\,\mathrm{erfi}\left(bx\right)}{6}-\frac{x^{5}e^{b^{2}x^{2}}}{6\sqrt{\pi}\,b}+\frac{5x^{3}e^{b^{2}x^{2}}}{12\sqrt{\pi}\,b^{3}}-\frac{5xe^{b^{2}x^{2}}}{8\sqrt{\pi}\,b^{5}}+\frac{5\,\mathrm{erfi}\left(bx\right)}{16b^{6}} & \text{for}\ b\neq 0\\ 0 & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**5*erfi(b*x),x)
```

```
[Out] Piecewise((x**6*erfi(b*x)/6 - x**5*exp(b**2*x**2)/(6*sqrt(pi)*b) + 5*x**3*e
xp(b**2*x**2)/(12*sqrt(pi)*b**3) - 5*x*exp(b**2*x**2)/(8*sqrt(pi)*b**5) + 5
*erfi(b*x)/(16*b**6), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfi(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^5*erfi(b*x), x)
```

Mupad [B]
time = 0.12, size = 108, normalized size = 1.16

$$\frac{x^6\,\mathrm{erfi}(b\,x)}{6}-\frac{5\,b\,x^7}{16\,{\left(-b^2\,x^2\right)}^{7/2}}-\frac{x^5\,{\mathrm{e}}^{b^2\,x^2}}{6\,b\,\sqrt{\pi }}+\frac{5\,x^3\,{\mathrm{e}}^{b^2\,x^2}}{12\,b^3\,\sqrt{\pi }}-\frac{5\,x\,{\mathrm{e}}^{b^2\,x^2}}{8\,b^5\,\sqrt{\pi }}+\frac{5\,b\,x^7\,\mathrm{erfc}\left(\sqrt{-b^2\,x^2}\right)}{16\,{\left(-b^2\,x^2\right)}^{7/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*erfi(b*x),x)
```

```
[Out] (x^6*erfi(b*x))/6 - (5*b*x^7)/(16*(-b^2*x^2)^(7/2)) - (x^5*exp(b^2*x^2))/(6
*b*pi^(1/2)) + (5*x^3*exp(b^2*x^2))/(12*b^3*pi^(1/2)) - (5*x*exp(b^2*x^2))/
(8*b^5*pi^(1/2)) + (5*b*x^7*erfc((-b^2*x^2)^(1/2)))/(16*(-b^2*x^2)^(7/2))
```

3.208 $\int x^3\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=69

$$\frac{3e^{b^2x^2}x}{8b^3\sqrt{\pi}}-\frac{e^{b^2x^2}x^3}{4b\sqrt{\pi}}-\frac{3\text{Erfi}(bx)}{16b^4}+\frac{1}{4}x^4\text{Erfi}(bx)$$

```
[Out] -3/16*erfi(b*x)/b^4+1/4*x^4*erfi(b*x)+3/8*exp(b^2*x^2)*x/b^3/Pi^(1/2)-1/4*e
xp(b^2*x^2)*x^3/b/Pi^(1/2)
```

Rubi [A]
time = 0.04, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}}=0.375$, Rules used = {6498, 2243, 2235}

$$-\frac{3\text{Erfi}(bx)}{16b^4}-\frac{x^3e^{b^2x^2}}{4\sqrt{\pi}\,b}+\frac{3xe^{b^2x^2}}{8\sqrt{\pi}\,b^3}+\frac{1}{4}x^4\text{Erfi}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x^3*Erfi[b*x],x]
```

```
[Out] (3*E^(b^2*x^2)*x)/(8*b^3*Sqrt[Pi]) - (E^(b^2*x^2)*x^3)/(4*b*Sqrt[Pi]) - (3*
Erfi[b*x])/(16*b^4) + (x^4*Erfi[b*x])/4
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6498

```
Int[Erfi[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfi[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)*E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int x^3\text{erfi}(bx)\,dx &= \frac{1}{4}x^4\text{erfi}(bx) - \frac{b\int e^{b^2x^2}x^4\,dx}{2\sqrt{\pi}}\\ &= -\frac{e^{b^2x^2}x^3}{4b\sqrt{\pi}} + \frac{1}{4}x^4\text{erfi}(bx) + \frac{3\int e^{b^2x^2}x^2\,dx}{4b\sqrt{\pi}}\\ &= \frac{3e^{b^2x^2}x}{8b^3\sqrt{\pi}} - \frac{e^{b^2x^2}x^3}{4b\sqrt{\pi}} + \frac{1}{4}x^4\text{erfi}(bx) - \frac{3\int e^{b^2x^2}\,dx}{8b^3\sqrt{\pi}}\\ &= \frac{3e^{b^2x^2}x}{8b^3\sqrt{\pi}} - \frac{e^{b^2x^2}x^3}{4b\sqrt{\pi}} - \frac{3\text{erfi}(bx)}{16b^4} + \frac{1}{4}x^4\text{erfi}(bx)\end{aligned}$$

Mathematica [A]
time = 0.02, size = 51, normalized size = 0.74

$$\frac{-\frac{2be^{b^2x^2}x(-3+2b^2x^2)}{\sqrt{\pi}} + (-3+4b^4x^4)\,\text{Erfi}(bx)}{16b^4}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^3*Erfi[b*x],x]
[Out] ((-2*b*E^(b^2*x^2)*x*(-3 + 2*b^2*x^2))/Sqrt[Pi] + (-3 + 4*b^4*x^4)*Erfi[b*x
])/(16*b^4)
```

Maple [A]
time = 0.10, size = 61, normalized size = 0.88

method	result	size
meijerg	$-\frac{i\left(\frac{ixb\left(-10b^2x^2+15\right)e^{b^2x^2}}{20}-\frac{i\left(-20b^4x^4+15\right)\text{erfi}(bx)\sqrt{\pi}}{40}\right)}{2b^4\sqrt{\pi}}$	54
derivativedivides	$\frac{\frac{b^4x^4\,\text{erfi}(bx)}{4}-\frac{\frac{b^3x^3e^{b^2x^2}}{2}-\frac{3\,e^{b^2x^2}bx}{4}+\frac{3\,\text{erfi}(bx)\sqrt{\pi}}{8}}{2\sqrt{\pi}}}{b^4}$	61
default	$\frac{\frac{b^4x^4\,\text{erfi}(bx)}{4}-\frac{\frac{b^3x^3e^{b^2x^2}}{2}-\frac{3\,e^{b^2x^2}bx}{4}+\frac{3\,\text{erfi}(bx)\sqrt{\pi}}{8}}{2\sqrt{\pi}}}{b^4}$	61

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erfi(b*x),x,method=_RETURNVERBOSE)
```

[Out] 1/b^4*(1/4*b^4*x^4*erfi(b*x)-1/2/Pi^(1/2)*(1/2*b^3*x^3*exp(b^2*x^2)-3/4*exp(b^2*x^2)*b*x+3/8*erfi(b*x)*Pi^(1/2)))

Maxima [C] Result contains complex when optimal does not.
time = 0.27, size = 55, normalized size = 0.80

$$\frac{1}{4}\,x^4\,\mathrm{erfi}\left(bx\right)-\frac{b\left(\frac{2\,(2\,b^2x^3-3\,x)e^{\left(b^2x^2\right)}}{b^4}-\frac{3i\,\sqrt{\pi}\,\mathrm{erf}(i\,bx)}{b^5}\right)}{16\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfi(b*x),x, algorithm="maxima")
```

```
[Out] 1/4*x^4*erfi(b*x) - 1/16*b*(2*(2*b^2*x^3 - 3*x)*e^(b^2*x^2)/b^4 - 3*I*sqrt(pi)*erf(I*b*x)/b^5)/sqrt(pi)
```

Fricas [A]
time = 0.38, size = 53, normalized size = 0.77

$$-\frac{2\,\sqrt{\pi}\,(2\,b^3x^3-3\,bx)e^{\left(b^2x^2\right)}+(3\,\pi-4\,\pi b^4x^4)\,\mathrm{erfi}\left(bx\right)}{16\,\pi b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfi(b*x),x, algorithm="fricas")
```

```
[Out] -1/16*(2*sqrt(pi)*(2*b^3*x^3 - 3*b*x)*e^(b^2*x^2) + (3*pi - 4*pi*b^4*x^4)*erfi(b*x))/(pi*b^4)
```

Sympy [A]
time = 0.19, size = 65, normalized size = 0.94

$$\begin{cases}\frac{x^4\,\mathrm{erfi}\,(bx)}{4}-\frac{x^3e^{b^2x^2}}{4\sqrt{\pi}\,b}+\frac{3xe^{b^2x^2}}{8\sqrt{\pi}\,b^3}-\frac{3\,\mathrm{erfi}\,(bx)}{16b^4} & \text{for } b\neq 0\\ 0 & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3*erfi(b*x),x)
```

```
[Out] Piecewise((x**4*erfi(b*x)/4 - x**3*exp(b**2*x**2)/(4*sqrt(pi)*b) + 3*x*exp(b**2*x**2)/(8*sqrt(pi)*b**3) - 3*erfi(b*x)/(16*b**4), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfi(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^3*erfi(b*x), x)
```

Mupad [B]
time = 0.09, size = 89, normalized size = 1.29

$$\frac{x^4\,\mathrm{erfi}(b\,x)}{4}-\frac{3\,b\,x^5}{16\,{\left(-b^2\,x^2\right)}^{5/2}}-\frac{x^3\,{\mathrm{e}}^{b^2\,x^2}}{4\,b\,\sqrt{\pi }}+\frac{3\,x\,{\mathrm{e}}^{b^2\,x^2}}{8\,b^3\,\sqrt{\pi }}+\frac{3\,b\,x^5\,\mathrm{erfc}\left(\sqrt{-b^2\,x^2}\right)}{16\,{\left(-b^2\,x^2\right)}^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erfi(b*x),x)
```

```
[Out] (x^4*erfi(b*x))/4 - (3*b*x^5)/(16*(-b^2*x^2)^(5/2)) - (x^3*exp(b^2*x^2))/(4
*b*pi^(1/2)) + (3*x*exp(b^2*x^2))/(8*b^3*pi^(1/2)) + (3*b*x^5*erfc((-b^2*x^
2)^(1/2)))/(16*(-b^2*x^2)^(5/2))
```

3.209 $\int x\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=45

$$-\frac{e^{b^2x^2}x}{2b\sqrt{\pi}}+\frac{\text{Erfi}(bx)}{4b^2}+\frac{1}{2}x^2\text{Erfi}(bx)$$

```
[Out] 1/4*erfi(b*x)/b^2+1/2*x^2*erfi(b*x)-1/2*exp(b^2*x^2)*x/b/Pi^(1/2)
```

Rubi [A]
time = 0.02, antiderivative size = 45, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.500, Rules used = {6498, 2243, 2235}

$$\frac{\text{Erfi}(bx)}{4b^2}-\frac{xe^{b^2x^2}}{2\sqrt{\pi}\,b}+\frac{1}{2}x^2\text{Erfi}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x*Erfi[b*x],x]
```

```
[Out] -1/2*(E^(b^2*x^2)*x)/(b*Sqrt[Pi]) + Erfi[b*x]/(4*b^2) + (x^2*Erfi[b*x])/2
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6498

```
Int[Erfi[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfi[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)*E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int x\mathrm{erfi}(bx)\,dx &= \frac{1}{2}x^2\mathrm{erfi}(bx)-\frac{b\int e^{b^2x^2}x^2\,dx}{\sqrt{\pi}}\\&=-\frac{e^{b^2x^2}x}{2b\sqrt{\pi}}+\frac{1}{2}x^2\mathrm{erfi}(bx)+\frac{\int e^{b^2x^2}\,dx}{2b\sqrt{\pi}}\\&=-\frac{e^{b^2x^2}x}{2b\sqrt{\pi}}+\frac{\mathrm{erfi}(bx)}{4b^2}+\frac{1}{2}x^2\mathrm{erfi}(bx)\end{aligned}$$

Mathematica [A]
time = 0.02, size = 39, normalized size = 0.87

$$\frac{1}{4}\left(-\frac{2e^{b^2x^2}x}{b\sqrt{\pi}}+\left(\frac{1}{b^2}+2x^2\right)\mathrm{Erfi}(bx)\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x*Erfi[b*x],x]
[Out] ((-2*E^(b^2*x^2)*x)/(b*Sqrt[Pi]) + (b^(-2) + 2*x^2)*Erfi[b*x])/4
```

Maple [A]
time = 0.10, size = 45, normalized size = 1.00

method	result	size
meijerg	$\frac{i\left(ixb\,\mathrm{e}^{b^2x^2}-\frac{i\left(6b^2x^2+3\right)\mathrm{erfi}(bx)\sqrt{\pi}}{6}\right)}{2\sqrt{\pi}\,b^2}$	44
derivativedivides	$\frac{\frac{b^2x^2\,\mathrm{erfi}(bx)}{2}-\frac{\frac{\mathrm{e}^{b^2x^2}bx}{2}-\frac{\mathrm{erfi}(bx)\sqrt{\pi}}{4}}{\sqrt{\pi}}}{b^2}$	45
default	$\frac{\frac{b^2x^2\,\mathrm{erfi}(bx)}{2}-\frac{\frac{\mathrm{e}^{b^2x^2}bx}{2}-\frac{\mathrm{erfi}(bx)\sqrt{\pi}}{4}}{\sqrt{\pi}}}{b^2}$	45

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfi(b*x),x,method=_RETURNVERBOSE)
[Out] 1/b^2*(1/2*b^2*x^2*erfi(b*x)-1/Pi^(1/2)*(1/2*exp(b^2*x^2)*b*x-1/4*erfi(b*x)
*Pi^(1/2)))
```

Maxima [C] Result contains complex when optimal does not.
time = 0.27, size = 44, normalized size = 0.98

$$\frac{1}{2}\,x^2\,\mathrm{erfi}\left(bx\right)-\frac{b\left(\frac{2\,xe^{\left(b^2x^2\right)}}{b^2}+\frac{i\,\sqrt{\pi}\,\mathrm{erf}\left(i\,bx\right)}{b^3}\right)}{4\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(b*x),x, algorithm="maxima")
```

```
[Out] 1/2*x^2*erfi(b*x) - 1/4*b*(2*x*e^(b^2*x^2)/b^2 + I*sqrt(pi)*erf(I*b*x)/b^3)
/sqrt(pi)
```

Fricas [A]
time = 0.35, size = 41, normalized size = 0.91

$$-\frac{2\sqrt{\pi}\,bxe^{(b^2x^2)} - (\pi + 2\,\pi b^2x^2)\operatorname{erfi}(bx)}{4\,\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(b*x),x, algorithm="fricas")
```

```
[Out] -1/4*(2*sqrt(pi)*b*x*e^(b^2*x^2) - (pi + 2*pi*b^2*x^2)*erfi(b*x))/(pi*b^2)
```

Sympy [A]
time = 0.08, size = 39, normalized size = 0.87

$$\begin{cases} \frac{x^2\operatorname{erfi}(bx)}{2} - \frac{xe^{b^2x^2}}{2\sqrt{\pi}\,b} + \frac{\operatorname{erfi}(bx)}{4b^2} & \text{for } b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(b*x),x)
```

```
[Out] Piecewise((x**2*erfi(b*x)/2 - x*exp(b**2*x**2)/(2*sqrt(pi)*b) + erfi(b*x)/(
4*b**2), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(b*x),x, algorithm="giac")
```

```
[Out] integrate(x*erfi(b*x), x)
```

Mupad [B]
time = 0.19, size = 43, normalized size = 0.96

$$\frac{x^2\operatorname{erfi}(b\,x)}{2} + \frac{b\operatorname{erfi}\left(x\,\sqrt{b^2}\right)}{4\,(b^2)^{3/2}} - \frac{x\,e^{b^2\,x^2}}{2\,b\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfi(b*x),x)
```

```
[Out] (x^2*erfi(b*x))/2 + (b*erfi(x*(b^2)^(1/2)))/(4*(b^2)^(3/2)) - (x*exp(b^2*x^
2))/(2*b*pi^(1/2))
```

3.210 $\int \frac{\mathbf{Erfi}(bx)}{x} \, dx$

Optimal. Leaf size=31

$$\frac{2bx\,{}_2F_2\left(\frac{1}{2},\frac{1}{2};\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}$$

```
[Out] 2*b*x*hypergeom([1/2, 1/2],[3/2, 3/2],b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.01, antiderivative size = 31, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = $\{6495\}$

$$\frac{2bx\,{}_2F_2\left(\frac{1}{2},\frac{1}{2};\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]/x,x]
```

```
[Out] (2*b*x*HypergeometricPFQ[{1/2, 1/2}, {3/2, 3/2}, b^2*x^2])/Sqrt[Pi]
```

Rule 6495

```
Int[Erfi[(b_.)*(x_)]/(x_), x_Symbol] :> Simp[2*b*(x/Sqrt[Pi])*Hypergeometri
cPFQ[{1/2, 1/2}, {3/2, 3/2}, b^2*x^2], x] /; FreeQ[b, x]
```

Rubi steps

$$\int \frac{\text{erfi}(bx)}{x} \, dx = \frac{2bx\,{}_2F_2\left(\frac{1}{2},\frac{1}{2};\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}$$

Mathematica [A]
time = 0.01, size = 31, normalized size = 1.00

$$\frac{2bx\,{}_2F_2\left(\frac{1}{2},\frac{1}{2};\frac{3}{2},\frac{3}{2};b^2x^2\right)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]/x,x]
```

```
[Out] (2*b*x*HypergeometricPFQ[{1/2, 1/2}, {3/2, 3/2}, b^2*x^2])/Sqrt[Pi]
```

Maple [A]
time = 0.07, size = 22, normalized size = 0.71

method	result	size
meijerg	$\frac{2bx\,\mathrm{hypergeom}\left(\left[\frac{1}{2},\frac{1}{2}\right],\left[\frac{3}{2},\frac{3}{2}\right],b^2x^2\right)}{\sqrt{\pi}}$	22

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/x,x,method=_RETURNVERBOSE)
```

```
[Out] 2*b*x*hypergeom([1/2,1/2],[3/2,3/2],b^2*x^2)/Pi^(1/2)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)/x, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x)/x, x)
```

Sympy [A]
time = 0.29, size = 24, normalized size = 0.77

$$\frac{2bx{}_2F_2\left(\begin{matrix}\frac{1}{2},\frac{1}{2}\\ \frac{3}{2},\frac{3}{2}\end{matrix}\middle|b^2x^2\right)}{\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x,x)
```

```
[Out] 2*b*x*hyper((1/2, 1/2), (3/2, 3/2), b**2*x**2)/sqrt(pi)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)/x, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{\operatorname{erfi}(b\,x)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/x,x)
```

```
[Out] int(erfi(b*x)/x, x)
```

3.211 $\int \frac{\text{Erfi}(bx)}{x^3} dx$

Optimal. Leaf size=40

$$-\frac{be^{b^2x^2}}{\sqrt{\pi}\,x}+b^2\text{Erfi}(bx)-\frac{\text{Erfi}(bx)}{2x^2}$$

```
[Out] b^2*erfi(b*x)-1/2*erfi(b*x)/x^2-b*exp(b^2*x^2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.02, antiderivative size = 40, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6498, 2245, 2235}

$$b^2\text{Erfi}(bx)-\frac{be^{b^2x^2}}{\sqrt{\pi}\,x}-\frac{\text{Erfi}(bx)}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]/x^3,x]
```

```
[Out] -((b*E^(b^2*x^2))/(Sqrt[Pi]*x)) + b^2*Erfi[b*x] - Erfi[b*x]/(2*x^2)
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6498

```
Int[Erfi[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfi[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)*E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$\int \frac{\operatorname{erfi}(bx)}{x^3} dx = -\frac{\operatorname{erfi}(bx)}{2x^2} + \frac{b \int \frac{e^{b^2x^2}}{x^2} dx}{\sqrt{\pi}}$$
$$= -\frac{be^{b^2x^2}}{\sqrt{\pi}\, x} - \frac{\operatorname{erfi}(bx)}{2x^2} + \frac{(2b^3) \int e^{b^2x^2} dx}{\sqrt{\pi}}$$
$$= -\frac{be^{b^2x^2}}{\sqrt{\pi}\, x} + b^2 \operatorname{erfi}(bx) - \frac{\operatorname{erfi}(bx)}{2x^2}$$

Mathematica [A]
time = 0.02, size = 37, normalized size = 0.92

$$-\frac{be^{b^2x^2}}{\sqrt{\pi}\, x} + \left(b^2 - \frac{1}{2x^2}\right) \operatorname{Erfi}(bx)$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]/x^3,x]
[Out] -((b*E^(b^2*x^2))/(Sqrt[Pi]*x)) + (b^2 - 1/(2*x^2))*Erfi[b*x]
```

Maple [A]
time = 0.13, size = 47, normalized size = 1.18

method	result	size
derivativedivides	$b^2 \left(-\frac{\operatorname{erfi}(bx)}{2b^2x^2} + \frac{-\frac{e^{b^2x^2}}{bx} + \operatorname{erfi}(bx)\sqrt{\pi}}{\sqrt{\pi}}\right)$	47
default	$b^2 \left(-\frac{\operatorname{erfi}(bx)}{2b^2x^2} + \frac{-\frac{e^{b^2x^2}}{bx} + \operatorname{erfi}(bx)\sqrt{\pi}}{\sqrt{\pi}}\right)$	47
meijerg	$\frac{i b^2 \left(\frac{2i e^{b^2x^2}}{xb} + \frac{i\left(-2b^2x^2+1\right) \operatorname{erfi}(bx)\sqrt{\pi}}{x^2b^2}\right)}{2\sqrt{\pi}}$	54

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/x^3,x,method=_RETURNVERBOSE)
[Out] b^2*(-1/2/b^2/x^2*erfi(b*x)+1/Pi^(1/2)*(-exp(b^2*x^2)/b/x+erfi(b*x)*Pi^(1/2
)))
```

Maxima [A]
time = 0.29, size = 39, normalized size = 0.98

$$-\frac{\sqrt{-b^2x^2}\, b\Gamma\left(-\frac{1}{2}, -b^2x^2\right)}{2\sqrt{\pi}\, x} - \frac{\operatorname{erfi}(bx)}{2\,x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^3,x, algorithm="maxima")
[Out] -1/2*sqrt(-b^2*x^2)*b*gamma(-1/2, -b^2*x^2)/(sqrt(pi)*x) - 1/2*erfi(b*x)/x^
2
```

Fricas [A]
time = 0.41, size = 40, normalized size = 1.00

$$-\frac{2\sqrt{\pi}\,bxe^{\left(b^2x^2\right)} + \left(\pi - 2\,\pi b^2x^2\right)\operatorname{erfi}\left(bx\right)}{2\,\pi x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^3,x, algorithm="fricas")
[Out] -1/2*(2*sqrt(pi)*b*x*e^(b^2*x^2) + (pi - 2*pi*b^2*x^2)*erfi(b*x))/(pi*x^2)
```

Sympy [A]
time = 0.19, size = 34, normalized size = 0.85

$$b^2\operatorname{erfi}\left(bx\right) - \frac{be^{b^2x^2}}{\sqrt{\pi}\,x} - \frac{\operatorname{erfi}\left(bx\right)}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x**3,x)
[Out] b**2*erfi(b*x) - b*exp(b**2*x**2)/(sqrt(pi)*x) - erfi(b*x)/(2*x**2)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^3,x, algorithm="giac")
[Out] integrate(erfi(b*x)/x^3, x)
```

Mupad [B]
time = 0.11, size = 69, normalized size = 1.72

$$\frac{b\operatorname{erfc}\left(\sqrt{-b^2\,x^2}\right)\,\sqrt{-b^2\,x^2}}{x} - \frac{b\,\sqrt{-b^2\,x^2}}{x} - \frac{b\,\mathrm{e}^{b^2\,x^2}}{x\,\sqrt{\pi}} - \frac{\operatorname{erfi}(b\,x)}{2\,x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/x^3,x)
[Out] (b*erfc((-b^2*x^2)^(1/2))*(-b^2*x^2)^(1/2))/x - (b*(-b^2*x^2)^(1/2))/x - (b
*exp(b^2*x^2))/(x*pi^(1/2)) - erfi(b*x)/(2*x^2)
```

3.212 $\int \frac{\mathbf{Erfi}(bx)}{x^5}\,dx$

Optimal. Leaf size=69

$$-\frac{be^{b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{b^3e^{b^2x^2}}{3\sqrt{\pi}\,x}+\frac{1}{3}b^4\mathrm{Erfi}(bx)-\frac{\mathrm{Erfi}(bx)}{4x^4}$$

```
[Out] 1/3*b^4*erfi(b*x)-1/4*erfi(b*x)/x^4-1/6*b*exp(b^2*x^2)/x^3/Pi^(1/2)-1/3*b^3
*exp(b^2*x^2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.04, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6498, 2245, 2235}

$$\frac{1}{3}b^4\mathrm{Erfi}(bx)-\frac{be^{b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{b^3e^{b^2x^2}}{3\sqrt{\pi}\,x}-\frac{\mathrm{Erfi}(bx)}{4x^4}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]/x^5,x]
```

```
[Out] -1/6*(b*E^(b^2*x^2))/(Sqrt[Pi]*x^3) - (b^3*E^(b^2*x^2))/(3*Sqrt[Pi]*x) + (b
^4*Erfi[b*x])/3 - Erfi[b*x]/(4*x^4)
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6498

```
Int[Erfi[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfi[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)*E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{\operatorname{erfi}(bx)}{x^5}\,dx &= -\frac{\operatorname{erfi}(bx)}{4x^4}+\frac{b\int \frac{e^{b^2x^2}}{x^4}\,dx}{2\sqrt{\pi}}\\
&= -\frac{be^{b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{\operatorname{erfi}(bx)}{4x^4}+\frac{b^3\int \frac{e^{b^2x^2}}{x^2}\,dx}{3\sqrt{\pi}}\\
&= -\frac{be^{b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{b^3e^{b^2x^2}}{3\sqrt{\pi}\,x}-\frac{\operatorname{erfi}(bx)}{4x^4}+\frac{(2b^5)\int e^{b^2x^2}\,dx}{3\sqrt{\pi}}\\
&= -\frac{be^{b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{b^3e^{b^2x^2}}{3\sqrt{\pi}\,x}+\frac{1}{3}b^4\operatorname{erfi}(bx)-\frac{\operatorname{erfi}(bx)}{4x^4}
\end{aligned}
$$

Mathematica [A]
time = 0.02, size = 51, normalized size = 0.74

$$
\frac{-\frac{2be^{b^2x^2}x(1+2b^2x^2)}{\sqrt{\pi}}+(-3+4b^4x^4)\operatorname{Erfi}(bx)}{12x^4}
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]/x^5,x]
```

```
[Out] ((-2*b*E^(b^2*x^2)*x*(1 + 2*b^2*x^2))/Sqrt[Pi] + (-3 + 4*b^4*x^4)*Erfi[b*x]
)/(12*x^4)
```

Maple [A]
time = 0.13, size = 65, normalized size = 0.94

method	result	size
meijerg	$-\frac{i b^4\left(-\frac{4i\left(\frac{b^2x^2}{2}+\frac{1}{4}\right)e^{b^2x^2}}{3x^3b^3}-\frac{i\left(-4b^4x^4+3\right)\operatorname{erfi}(bx)\sqrt{\pi}}{6x^4b^4}\right)}{2\sqrt{\pi}}$	64
derivativedivides	$b^4\left(-\frac{\operatorname{erfi}(bx)}{4b^4x^4}+\frac{-\frac{e^{b^2x^2}}{3b^3x^3}-\frac{2e^{b^2x^2}}{3bx}+\frac{2\operatorname{erfi}(bx)\sqrt{\pi}}{3}}{2\sqrt{\pi}}\right)$	65
default	$b^4\left(-\frac{\operatorname{erfi}(bx)}{4b^4x^4}+\frac{-\frac{e^{b^2x^2}}{3b^3x^3}-\frac{2e^{b^2x^2}}{3bx}+\frac{2\operatorname{erfi}(bx)\sqrt{\pi}}{3}}{2\sqrt{\pi}}\right)$	65

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/x^5,x,method=_RETURNVERBOSE)
```

```
[Out] b^4*(-1/4/b^4/x^4*erfi(b*x)+1/2/Pi^(1/2)*(-1/3*exp(b^2*x^2)/b^3/x^3-2/3*exp
(b^2*x^2)/b/x+2/3*erfi(b*x)*Pi^(1/2)))
```

Maxima [A]
time = 0.29, size = 39, normalized size = 0.57

$$-\frac{\left(-b^2x^2\right)^{\frac{3}{2}} b\Gamma\left(-\frac{3}{2},-b^2x^2\right)}{4\sqrt{\pi}\,x^3}-\frac{\operatorname{erfi}\left(bx\right)}{4\,x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^5,x, algorithm="maxima")
```

```
[Out] -1/4*(-b^2*x^2)^(3/2)*b*gamma(-3/2, -b^2*x^2)/(sqrt(pi)*x^3) - 1/4*erfi(b*x
)/x^4
```

Fricas [A]
time = 0.36, size = 52, normalized size = 0.75

$$-\frac{2\sqrt{\pi}\left(2\,b^3x^3+bx\right)e^{\left(b^2x^2\right)}+\left(3\,\pi-4\,\pi b^4x^4\right)\operatorname{erfi}\left(bx\right)}{12\,\pi x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^5,x, algorithm="fricas")
```

```
[Out] -1/12*(2*sqrt(pi)*(2*b^3*x^3 + b*x)*e^(b^2*x^2) + (3*pi - 4*pi*b^4*x^4)*erf
i(b*x))/(pi*x^4)
```

Sympy [A]
time = 0.34, size = 60, normalized size = 0.87

$$\frac{b^4\operatorname{erfi}\left(bx\right)}{3}-\frac{b^3e^{b^2x^2}}{3\sqrt{\pi}\,x}-\frac{be^{b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{\operatorname{erfi}\left(bx\right)}{4x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x**5,x)
```

```
[Out] b**4*erfi(b*x)/3 - b**3*exp(b**2*x**2)/(3*sqrt(pi)*x) - b*exp(b**2*x**2)/(6
*sqrt(pi)*x**3) - erfi(b*x)/(4*x**4)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^5,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)/x^5, x)
```

Mupad [B]
time = 0.08, size = 89, normalized size = 1.29

$$\frac{b\,{\left(-b^2\,x^2\right)}^{3/2}}{3\,x^3}-\frac{\mathrm{erfi}\left(b\,x\right)}{4\,x^4}-\frac{b^3\,{\mathrm{e}}^{b^2\,x^2}}{3\,x\,\sqrt{\pi }}-\frac{b\,{\mathrm{e}}^{b^2\,x^2}}{6\,x^3\,\sqrt{\pi }}-\frac{b\,\mathrm{erfc}\left(\sqrt{-b^2\,x^2}\right)\,{\left(-b^2\,x^2\right)}^{3/2}}{3\,x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/x^5,x)
```

```
[Out] (b*(-b^2*x^2)^(3/2))/(3*x^3) - erfi(b*x)/(4*x^4) - (b^3*exp(b^2*x^2))/(3*x*
pi^(1/2)) - (b*exp(b^2*x^2))/(6*x^3*pi^(1/2)) - (b*erfc((-b^2*x^2)^(1/2))*(
-b^2*x^2)^(3/2))/(3*x^3)
```

3.213 $\int \frac{\textbf{Erfi}(bx)}{x^7}\,dx$

Optimal. Leaf size=93

$$-\frac{be^{b^2x^2}}{15\sqrt{\pi}\,x^5}-\frac{2b^3e^{b^2x^2}}{45\sqrt{\pi}\,x^3}-\frac{4b^5e^{b^2x^2}}{45\sqrt{\pi}\,x}+\frac{4}{45}b^6\text{Erfi}(bx)-\frac{\text{Erfi}(bx)}{6x^6}$$

```
[Out] 4/45*b^6*erfi(b*x)-1/6*erfi(b*x)/x^6-1/15*b*exp(b^2*x^2)/x^5/Pi^(1/2)-2/45*
b^3*exp(b^2*x^2)/x^3/Pi^(1/2)-4/45*b^5*exp(b^2*x^2)/x/Pi^(1/2)
```

Rubi [A]
time = 0.05, antiderivative size = 93, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6498, 2245, 2235}

$$\frac{4}{45}b^6\text{Erfi}(bx)-\frac{be^{b^2x^2}}{15\sqrt{\pi}\,x^5}-\frac{4b^5e^{b^2x^2}}{45\sqrt{\pi}\,x}-\frac{2b^3e^{b^2x^2}}{45\sqrt{\pi}\,x^3}-\frac{\text{Erfi}(bx)}{6x^6}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]/x^7,x]
```

```
[Out] -1/15*(b*E^(b^2*x^2))/(Sqrt[Pi]*x^5) - (2*b^3*E^(b^2*x^2))/(45*Sqrt[Pi]*x^3
) - (4*b^5*E^(b^2*x^2))/(45*Sqrt[Pi]*x) + (4*b^6*Erfi[b*x])/45 - Erfi[b*x]/
(6*x^6)
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6498

```
Int[Erfi[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfi[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)*E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
```

```
m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{\operatorname{erfi}(bx)}{x^7}\,dx &= -\frac{\operatorname{erfi}(bx)}{6x^6}+\frac{b\int \frac{e^{b^2x^2}}{x^6}\,dx}{3\sqrt{\pi}}\\
&= -\frac{be^{b^2x^2}}{15\sqrt{\pi}\,x^5}-\frac{\operatorname{erfi}(bx)}{6x^6}+\frac{(2b^3)\int \frac{e^{b^2x^2}}{x^4}\,dx}{15\sqrt{\pi}}\\
&= -\frac{be^{b^2x^2}}{15\sqrt{\pi}\,x^5}-\frac{2b^3e^{b^2x^2}}{45\sqrt{\pi}\,x^3}-\frac{\operatorname{erfi}(bx)}{6x^6}+\frac{(4b^5)\int \frac{e^{b^2x^2}}{x^2}\,dx}{45\sqrt{\pi}}\\
&= -\frac{be^{b^2x^2}}{15\sqrt{\pi}\,x^5}-\frac{2b^3e^{b^2x^2}}{45\sqrt{\pi}\,x^3}-\frac{4b^5e^{b^2x^2}}{45\sqrt{\pi}\,x}-\frac{\operatorname{erfi}(bx)}{6x^6}+\frac{(8b^7)\int e^{b^2x^2}\,dx}{45\sqrt{\pi}}\\
&= -\frac{be^{b^2x^2}}{15\sqrt{\pi}\,x^5}-\frac{2b^3e^{b^2x^2}}{45\sqrt{\pi}\,x^3}-\frac{4b^5e^{b^2x^2}}{45\sqrt{\pi}\,x}+\frac{4}{45}b^6\operatorname{erfi}(bx)-\frac{\operatorname{erfi}(bx)}{6x^6}
\end{aligned}
$$

Mathematica [A]
time = 0.02, size = 64, normalized size = 0.69

$$\frac{-2be^{b^2x^2}x(3+2b^2x^2+4b^4x^4)+\sqrt{\pi}\,(-15+8b^6x^6)\operatorname{Erfi}(bx)}{90\sqrt{\pi}\,x^6}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]/x^7,x]
[Out] (-2*b*E^(b^2*x^2)*x*(3 + 2*b^2*x^2 + 4*b^4*x^4) + Sqrt[Pi]*(-15 + 8*b^6*x^6
)*Erfi[b*x])/(90*Sqrt[Pi]*x^6)
```

Maple [A]
time = 0.10, size = 81, normalized size = 0.87

method	result	size
meijerg	$\frac{ib^6\left(\frac{4i\left(\frac{2}{9}b^4x^4+\frac{1}{9}b^2x^2+\frac{1}{6}\right)e^{b^2x^2}}{5x^5b^5}+\frac{i\left(-8b^6x^6+15\right)\operatorname{erfi}(bx)\sqrt{\pi}}{45x^6b^6}\right)}{2\sqrt{\pi}}$	72
derivativedivides	$b^6\left(-\frac{\operatorname{erfi}(bx)}{6b^6x^6}+\frac{-\frac{e^{b^2x^2}}{5b^5x^5}-\frac{2\,e^{b^2x^2}}{15b^3x^3}-\frac{4\,e^{b^2x^2}}{15bx}+\frac{4\,\operatorname{erfi}(bx)\sqrt{\pi}}{15}}{3\sqrt{\pi}}\right)$	81

default	$b^6\left(-\frac{\operatorname{erfi}(bx)}{6b^6x^6}+\frac{-\frac{e^{b^2x^2}}{5b^5x^5}-\frac{2\,e^{b^2x^2}}{15b^3x^3}-\frac{4\,e^{b^2x^2}}{15bx}+\frac{4\operatorname{erfi}(bx)\sqrt{\pi}}{15}}{3\sqrt{\pi}}\right)$	81

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/x^7,x,method=_RETURNVERBOSE)
```

```
[Out] b^6*(-1/6/b^6/x^6*erfi(b*x)+1/3/Pi^(1/2)*(-1/5*exp(b^2*x^2)/b^5/x^5-2/15*ex
p(b^2*x^2)/b^3/x^3-4/15*exp(b^2*x^2)/b/x+4/15*erfi(b*x)*Pi^(1/2)))
```

Maxima [A]
time = 0.30, size = 39, normalized size = 0.42

$$-\frac{\left(-b^2x^2\right)^{\frac{5}{2}}b\Gamma\left(-\frac{5}{2},-b^2x^2\right)}{6\sqrt{\pi}\,x^5}-\frac{\operatorname{erfi}\left(bx\right)}{6\,x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^7,x, algorithm="maxima")
```

```
[Out] -1/6*(-b^2*x^2)^(5/2)*b*gamma(-5/2, -b^2*x^2)/(sqrt(pi)*x^5) - 1/6*erfi(b*x
)/x^6
```

Fricas [A]
time = 0.34, size = 61, normalized size = 0.66

$$-\frac{2\sqrt{\pi}\left(4\,b^5x^5+2\,b^3x^3+3\,bx\right)e^{\left(b^2x^2\right)}+\left(15\,\pi-8\,\pi b^6x^6\right)\operatorname{erfi}\left(bx\right)}{90\,\pi x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^7,x, algorithm="fricas")
```

```
[Out] -1/90*(2*sqrt(pi)*(4*b^5*x^5 + 2*b^3*x^3 + 3*b*x)*e^(b^2*x^2) + (15*pi - 8*
pi*b^6*x^6)*erfi(b*x))/(pi*x^6)
```

Sympy [A]
time = 0.66, size = 87, normalized size = 0.94

$$\frac{4b^6\operatorname{erfi}\left(bx\right)}{45}-\frac{4b^5e^{b^2x^2}}{45\sqrt{\pi}\,x}-\frac{2b^3e^{b^2x^2}}{45\sqrt{\pi}\,x^3}-\frac{be^{b^2x^2}}{15\sqrt{\pi}\,x^5}-\frac{\operatorname{erfi}\left(bx\right)}{6x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x**7,x)
```

```
[Out] 4*b**6*erfi(b*x)/45 - 4*b**5*exp(b**2*x**2)/(45*sqrt(pi)*x) - 2*b**3*exp(b*
*2*x**2)/(45*sqrt(pi)*x**3) - b*exp(b**2*x**2)/(15*sqrt(pi)*x**5) - erfi(b*
x)/(6*x**6)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^7,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)/x^7, x)
```

Mupad [B]
time = 0.12, size = 108, normalized size = 1.16

$$-\frac{\operatorname{erfi}(b\,x)}{6\,x^6}-\frac{3\,b\,\mathrm{e}^{b^2\,x^2}+2\,b^3\,x^2\,\mathrm{e}^{b^2\,x^2}+4\,b^5\,x^4\,\mathrm{e}^{b^2\,x^2}+4\,b\,\sqrt{\pi}\,{\left(-b^2\,x^2\right)}^{5/2}-4\,b\,\sqrt{\pi}\,\mathrm{erfc}\left(\sqrt{-b^2}\,\sqrt{x^2}\right)\,{\left(-b^2\,x^2\right)}^{5/2}}{45\,x^5\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/x^7,x)
```

```
[Out] - erfi(b*x)/(6*x^6) - (3*b*exp(b^2*x^2) + 2*b^3*x^2*exp(b^2*x^2) + 4*b^5*x^
4*exp(b^2*x^2) + 4*b*pi^(1/2)*(-b^2*x^2)^(5/2) - 4*b*pi^(1/2)*erfc((-b^2)^(
1/2)*(x^2)^(1/2))*(-b^2*x^2)^(5/2))/(45*x^5*pi^(1/2))
```

3.214 $\int x^6 \mathbf{Erfi}(bx)\, dx$

Optimal. Leaf size=105

$$\frac{6e^{b^2x^2}}{7b^7\sqrt{\pi}}-\frac{6e^{b^2x^2}x^2}{7b^5\sqrt{\pi}}+\frac{3e^{b^2x^2}x^4}{7b^3\sqrt{\pi}}-\frac{e^{b^2x^2}x^6}{7b\sqrt{\pi}}+\frac{1}{7}x^7\mathrm{Erfi}(bx)$$

```
[Out] 1/7*x^7*erfi(b*x)+6/7*exp(b^2*x^2)/b^7/Pi^(1/2)-6/7*exp(b^2*x^2)*x^2/b^5/Pi
^(1/2)+3/7*exp(b^2*x^2)*x^4/b^3/Pi^(1/2)-1/7*exp(b^2*x^2)*x^6/b/Pi^(1/2)
```

Rubi [A]
time = 0.06, antiderivative size = 105, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6498, 2243, 2240}

$$-\frac{x^6e^{b^2x^2}}{7\sqrt{\pi}\,b}+\frac{6e^{b^2x^2}}{7\sqrt{\pi}\,b^7}-\frac{6x^2e^{b^2x^2}}{7\sqrt{\pi}\,b^5}+\frac{3x^4e^{b^2x^2}}{7\sqrt{\pi}\,b^3}+\frac{1}{7}x^7\mathrm{Erfi}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x^6*Erfi[b*x],x]
```

```
[Out] (6*E^(b^2*x^2))/(7*b^7*Sqrt[Pi]) - (6*E^(b^2*x^2)*x^2)/(7*b^5*Sqrt[Pi]) + (
3*E^(b^2*x^2)*x^4)/(7*b^3*Sqrt[Pi]) - (E^(b^2*x^2)*x^6)/(7*b*Sqrt[Pi]) + (x
^7*Erfi[b*x])/7
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6498

```
Int[Erfi[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfi[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)*E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
```

```
m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int x^6 \mathrm{erfi}(bx)\,dx &= \frac{1}{7}x^7\mathrm{erfi}(bx) - \frac{(2b)\int e^{b^2x^2}x^7\,dx}{7\sqrt{\pi}} \\
&= -\frac{e^{b^2x^2}x^6}{7b\sqrt{\pi}} + \frac{1}{7}x^7\mathrm{erfi}(bx) + \frac{6\int e^{b^2x^2}x^5\,dx}{7b\sqrt{\pi}} \\
&= \frac{3e^{b^2x^2}x^4}{7b^3\sqrt{\pi}} - \frac{e^{b^2x^2}x^6}{7b\sqrt{\pi}} + \frac{1}{7}x^7\mathrm{erfi}(bx) - \frac{12\int e^{b^2x^2}x^3\,dx}{7b^3\sqrt{\pi}} \\
&= -\frac{6e^{b^2x^2}x^2}{7b^5\sqrt{\pi}} + \frac{3e^{b^2x^2}x^4}{7b^3\sqrt{\pi}} - \frac{e^{b^2x^2}x^6}{7b\sqrt{\pi}} + \frac{1}{7}x^7\mathrm{erfi}(bx) + \frac{12\int e^{b^2x^2}x\,dx}{7b^5\sqrt{\pi}} \\
&= \frac{6e^{b^2x^2}}{7b^7\sqrt{\pi}} - \frac{6e^{b^2x^2}x^2}{7b^5\sqrt{\pi}} + \frac{3e^{b^2x^2}x^4}{7b^3\sqrt{\pi}} - \frac{e^{b^2x^2}x^6}{7b\sqrt{\pi}} + \frac{1}{7}x^7\mathrm{erfi}(bx)
\end{aligned}
$$

Mathematica [A]
time = 0.03, size = 57, normalized size = 0.54

$$\frac{1}{7}\left(\frac{e^{b^2x^2}(6-6b^2x^2+3b^4x^4-b^6x^6)}{b^7\sqrt{\pi}} + x^7\mathrm{Erfi}(bx)\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x^6*Erfi[b*x],x]
```

```
[Out] ((E^(b^2*x^2)*(6 - 6*b^2*x^2 + 3*b^4*x^4 - b^6*x^6))/(b^7*Sqrt[Pi]) + x^7*E
rfi[b*x])/7
```

Maple [A]
time = 0.12, size = 82, normalized size = 0.78

method	result	size
meijerg	$\frac{-\frac{12}{7}+\frac{\left(-4b^6x^6+12b^4x^4-24b^2x^2+24\right)e^{b^2x^2}}{14}+\frac{2x^7b^7\sqrt{\pi}\,\mathrm{erfi}(bx)}{7}}{2b^7\sqrt{\pi}}$	62
derivativedivides	$\frac{\frac{b^7x^7\,\mathrm{erfi}(bx)}{7}-\frac{2\left(\frac{b^6x^6e^{b^2x^2}}{2}-\frac{3\,e^{b^2x^2}b^4x^4}{2}+3b^2x^2e^{b^2x^2}-3\,e^{b^2x^2}\right)}{7\sqrt{\pi}}}{b^7}$	82
default	$\frac{\frac{b^7x^7\,\mathrm{erfi}(bx)}{7}-\frac{2\left(\frac{b^6x^6e^{b^2x^2}}{2}-\frac{3\,e^{b^2x^2}b^4x^4}{2}+3b^2x^2e^{b^2x^2}-3\,e^{b^2x^2}\right)}{7\sqrt{\pi}}}{b^7}$	82

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^6*erfi(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b^7*(1/7*b^7*x^7*erfi(b*x)-2/7/Pi^(1/2)*(1/2*b^6*x^6*exp(b^2*x^2)-3/2*exp
(b^2*x^2)*b^4*x^4+3*b^2*x^2*exp(b^2*x^2)-3*exp(b^2*x^2)))
```

Maxima [A]
time = 0.25, size = 51, normalized size = 0.49

$$\frac{1}{7}\,x^7\,\operatorname{erfi}\left(bx\right)-\frac{(b^6x^6-3\,b^4x^4+6\,b^2x^2-6)e^{(b^2x^2)}}{7\,\sqrt{\pi}\,b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^6*erfi(b*x),x, algorithm="maxima")
```

```
[Out] 1/7*x^7*erfi(b*x) - 1/7*(b^6*x^6 - 3*b^4*x^4 + 6*b^2*x^2 - 6)*e^(b^2*x^2)/(
sqrt(pi)*b^7)
```

Fricas [A]
time = 0.38, size = 59, normalized size = 0.56

$$\frac{\pi b^7x^7\,\operatorname{erfi}\left(bx\right)-\sqrt{\pi}\,(b^6x^6-3\,b^4x^4+6\,b^2x^2-6)e^{(b^2x^2)}}{7\,\pi b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^6*erfi(b*x),x, algorithm="fricas")
```

```
[Out] 1/7*(pi*b^7*x^7*erfi(b*x) - sqrt(pi)*(b^6*x^6 - 3*b^4*x^4 + 6*b^2*x^2 - 6)*
e^(b^2*x^2))/(pi*b^7)
```

Sympy [A]
time = 0.64, size = 99, normalized size = 0.94

$$\begin{cases}\frac{x^7\operatorname{erfi}\left(bx\right)}{7}-\frac{x^6e^{b^2x^2}}{7\sqrt{\pi}\,b}+\frac{3x^4e^{b^2x^2}}{7\sqrt{\pi}\,b^3}-\frac{6x^2e^{b^2x^2}}{7\sqrt{\pi}\,b^5}+\frac{6e^{b^2x^2}}{7\sqrt{\pi}\,b^7} & \text{for}\ b\neq 0\\ 0 & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**6*erfi(b*x),x)
```

```
[Out] Piecewise((x**7*erfi(b*x)/7 - x**6*exp(b**2*x**2)/(7*sqrt(pi)*b) + 3*x**4*e
xp(b**2*x**2)/(7*sqrt(pi)*b**3) - 6*x**2*exp(b**2*x**2)/(7*sqrt(pi)*b**5) +
 6*exp(b**2*x**2)/(7*sqrt(pi)*b**7), Ne(b, 0)), (0, True))
```

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^6*erfi(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^6*erfi(b*x), x)
```

Mupad [**B**]
time = 0.13, size = 51, normalized size = 0.49

$$\frac{x^7\,\mathrm{erfi}(b\,x)}{7}-\frac{\mathrm{e}^{b^2\,x^2}\,\left(b^6\,x^6-3\,b^4\,x^4+6\,b^2\,x^2-6\right)}{7\,b^7\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^6*erfi(b*x),x)
```

```
[Out] (x^7*erfi(b*x))/7 - (exp(b^2*x^2)*(6*b^2*x^2 - 3*b^4*x^4 + b^6*x^6 - 6))/(7
*b^7*pi^(1/2))
```

3.215 $\int x^4 \mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=81

$$-\frac{2e^{b^2x^2}}{5b^5\sqrt{\pi}}+\frac{2e^{b^2x^2}x^2}{5b^3\sqrt{\pi}}-\frac{e^{b^2x^2}x^4}{5b\sqrt{\pi}}+\frac{1}{5}x^5\mathrm{Erfi}(bx)$$

```
[Out] 1/5*x^5*erfi(b*x)-2/5*exp(b^2*x^2)/b^5/Pi^(1/2)+2/5*exp(b^2*x^2)*x^2/b^3/Pi
^(1/2)-1/5*exp(b^2*x^2)*x^4/b/Pi^(1/2)
```

Rubi [A]
time = 0.04, antiderivative size = 81, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6498, 2243, 2240}

$$-\frac{x^4e^{b^2x^2}}{5\sqrt{\pi}\,b}-\frac{2e^{b^2x^2}}{5\sqrt{\pi}\,b^5}+\frac{2x^2e^{b^2x^2}}{5\sqrt{\pi}\,b^3}+\frac{1}{5}x^5\mathrm{Erfi}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x^4*Erfi[b*x],x]
```

```
[Out] (-2*E^(b^2*x^2))/(5*b^5*Sqrt[Pi]) + (2*E^(b^2*x^2)*x^2)/(5*b^3*Sqrt[Pi]) -
(E^(b^2*x^2)*x^4)/(5*b*Sqrt[Pi]) + (x^5*Erfi[b*x])/5
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6498

```
Int[Erfi[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfi[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)*E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int x^4 \operatorname{erfi}(bx)\,dx &= \frac{1}{5}x^5\operatorname{erfi}(bx) - \frac{(2b)\int e^{b^2x^2}x^5\,dx}{5\sqrt{\pi}} \\
&= -\frac{e^{b^2x^2}x^4}{5b\sqrt{\pi}} + \frac{1}{5}x^5\operatorname{erfi}(bx) + \frac{4\int e^{b^2x^2}x^3\,dx}{5b\sqrt{\pi}} \\
&= \frac{2e^{b^2x^2}x^2}{5b^3\sqrt{\pi}} - \frac{e^{b^2x^2}x^4}{5b\sqrt{\pi}} + \frac{1}{5}x^5\operatorname{erfi}(bx) - \frac{4\int e^{b^2x^2}x\,dx}{5b^3\sqrt{\pi}} \\
&= -\frac{2e^{b^2x^2}}{5b^5\sqrt{\pi}} + \frac{2e^{b^2x^2}x^2}{5b^3\sqrt{\pi}} - \frac{e^{b^2x^2}x^4}{5b\sqrt{\pi}} + \frac{1}{5}x^5\operatorname{erfi}(bx)
\end{aligned}
$$

Mathematica [A]
time = 0.02, size = 49, normalized size = 0.60

$$\frac{1}{5}\left(-\frac{e^{b^2x^2}(2-2b^2x^2+b^4x^4)}{b^5\sqrt{\pi}} + x^5\operatorname{Erfi}(bx)\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x^4*Erfi[b*x],x]
[Out] (-((E^(b^2*x^2)*(2 - 2*b^2*x^2 + b^4*x^4))/(b^5*Sqrt[Pi])) + x^5*Erfi[b*x])
/5
```

Maple [A]
time = 0.10, size = 64, normalized size = 0.79

method	result	size
meijerg	$-\frac{-\frac{4}{5}+\frac{2\left(3b^4x^4-6b^2x^2+6\right)e^{b^2x^2}}{15}-\frac{2b^5x^5\sqrt{\pi}\,\operatorname{erfi}(bx)}{5}}{2b^5\sqrt{\pi}}$	54
derivativedivides	$\frac{\frac{b^5x^5\operatorname{erfi}(bx)}{5}-\frac{2\left(\frac{e^{b^2x^2}b^4x^4}{2}-b^2x^2e^{b^2x^2}+e^{b^2x^2}\right)}{5\sqrt{\pi}}}{b^5}$	64
default	$\frac{\frac{b^5x^5\operatorname{erfi}(bx)}{5}-\frac{2\left(\frac{e^{b^2x^2}b^4x^4}{2}-b^2x^2e^{b^2x^2}+e^{b^2x^2}\right)}{5\sqrt{\pi}}}{b^5}$	64

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erfi(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b^5*(1/5*b^5*x^5*erfi(b*x)-2/5/Pi^(1/2)*(1/2*exp(b^2*x^2)*b^4*x^4-b^2*x^2
*exp(b^2*x^2)+exp(b^2*x^2)))
```

Maxima [A]
time = 0.25, size = 43, normalized size = 0.53

$$\frac{1}{5}\,x^5\,\mathrm{erfi}\,(bx) - \frac{(b^4x^4 - 2\,b^2x^2 + 2)e^{(b^2x^2)}}{5\,\sqrt{\pi}\,b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfi(b*x),x, algorithm="maxima")
```

```
[Out] 1/5*x^5*erfi(b*x) - 1/5*(b^4*x^4 - 2*b^2*x^2 + 2)*e^(b^2*x^2)/(sqrt(pi)*b^5
)
```

Fricas [A]
time = 0.38, size = 51, normalized size = 0.63

$$\frac{\pi b^5x^5\,\mathrm{erfi}\,(bx) - \sqrt{\pi}\,(b^4x^4 - 2\,b^2x^2 + 2)e^{(b^2x^2)}}{5\,\pi b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfi(b*x),x, algorithm="fricas")
```

```
[Out] 1/5*(pi*b^5*x^5*erfi(b*x) - sqrt(pi)*(b^4*x^4 - 2*b^2*x^2 + 2)*e^(b^2*x^2))
/(pi*b^5)
```

Sympy [A]
time = 0.27, size = 75, normalized size = 0.93

$$\begin{cases} \frac{x^5\,\mathrm{erfi}\,(bx)}{5} - \frac{x^4e^{b^2x^2}}{5\sqrt{\pi}\,b} + \frac{2x^2e^{b^2x^2}}{5\sqrt{\pi}\,b^3} - \frac{2e^{b^2x^2}}{5\sqrt{\pi}\,b^5} & \text{for } b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4*erfi(b*x),x)
```

```
[Out] Piecewise((x**5*erfi(b*x)/5 - x**4*exp(b**2*x**2)/(5*sqrt(pi)*b) + 2*x**2*e
xp(b**2*x**2)/(5*sqrt(pi)*b**3) - 2*exp(b**2*x**2)/(5*sqrt(pi)*b**5), Ne(b,
 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfi(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^4*erfi(b*x), x)
```

Mupad [B]
time = 0.11, size = 43, normalized size = 0.53

$$\frac{x^5\,\mathrm{erfi}(b\,x)}{5}-\frac{\mathrm{e}^{b^2\,x^2}\,\left(b^4\,x^4-2\,b^2\,x^2+2\right)}{5\,b^5\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erfi(b*x),x)
```

```
[Out] (x^5*erfi(b*x))/5 - (exp(b^2*x^2)*(b^4*x^4 - 2*b^2*x^2 + 2))/(5*b^5*pi^(1/2
))
```

3.216 $\int x^2 \mathbf{Erfi}(bx)\, dx$

Optimal. Leaf size=57

$$\frac{e^{b^2x^2}}{3b^3\sqrt{\pi}}-\frac{e^{b^2x^2}x^2}{3b\sqrt{\pi}}+\frac{1}{3}x^3\text{Erfi}(bx)$$

```
[Out] 1/3*x^3*erfi(b*x)+1/3*exp(b^2*x^2)/b^3/Pi^(1/2)-1/3*exp(b^2*x^2)*x^2/b/Pi^(
1/2)
```

Rubi [A]
time = 0.03, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.375, Rules used = {6498, 2243, 2240}

$$-\frac{x^2e^{b^2x^2}}{3\sqrt{\pi}\,b}+\frac{e^{b^2x^2}}{3\sqrt{\pi}\,b^3}+\frac{1}{3}x^3\text{Erfi}(bx)$$

Antiderivative was successfully verified.

```
[In] Int[x^2*Erfi[b*x],x]
```

```
[Out] E^(b^2*x^2)/(3*b^3*Sqrt[Pi]) - (E^(b^2*x^2)*x^2)/(3*b*Sqrt[Pi]) + (x^3*Erfi
[b*x])/3
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6498

```
Int[Erfi[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfi[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)*E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int x^2\text{erfi}(bx)\,dx &= \frac{1}{3}x^3\text{erfi}(bx) - \frac{(2b)\int e^{b^2x^2}x^3\,dx}{3\sqrt{\pi}} \\
&= -\frac{e^{b^2x^2}x^2}{3b\sqrt{\pi}} + \frac{1}{3}x^3\text{erfi}(bx) + \frac{2\int e^{b^2x^2}x\,dx}{3b\sqrt{\pi}} \\
&= \frac{e^{b^2x^2}}{3b^3\sqrt{\pi}} - \frac{e^{b^2x^2}x^2}{3b\sqrt{\pi}} + \frac{1}{3}x^3\text{erfi}(bx)
\end{aligned}
$$

Mathematica [A]
time = 0.02, size = 41, normalized size = 0.72

$$\frac{1}{3}\left(\frac{e^{b^2x^2}(1-b^2x^2)}{b^3\sqrt{\pi}} + x^3\text{Erfi}(bx)\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*Erfi[b*x],x]
[Out] ((E^(b^2*x^2)*(1 - b^2*x^2))/(b^3*Sqrt[Pi]) + x^3*Erfi[b*x])/3
```

Maple [A]
time = 0.36, size = 50, normalized size = 0.88

method	result	size
meijerg	$\frac{-\frac{2}{3}+\frac{\left(-2b^2x^2+2\right)e^{b^2x^2}}{3}+\frac{2b^3x^3\sqrt{\pi}\ \text{erfi}(bx)}{3}}{2b^3\sqrt{\pi}}$	46
derivativedivides	$\frac{\frac{b^3x^3\ \text{erfi}(bx)}{3}-\frac{2\left(\frac{b^2x^2e^{b^2x^2}}{2}-\frac{e^{b^2x^2}}{2}\right)}{3\sqrt{\pi}}}{b^3}$	50
default	$\frac{\frac{b^3x^3\ \text{erfi}(bx)}{3}-\frac{2\left(\frac{b^2x^2e^{b^2x^2}}{2}-\frac{e^{b^2x^2}}{2}\right)}{3\sqrt{\pi}}}{b^3}$	50

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfi(b*x),x,method=_RETURNVERBOSE)
[Out] 1/b^3*(1/3*b^3*x^3*erfi(b*x)-2/3/Pi^(1/2)*(1/2*b^2*x^2*exp(b^2*x^2)-1/2*exp
(b^2*x^2)))
```

Maxima [A]
time = 0.27, size = 35, normalized size = 0.61

$$\frac{1}{3}\,x^3\,\mathrm{erfi}\,(bx) - \frac{(b^2x^2-1)e^{(b^2x^2)}}{3\,\sqrt{\pi}\,b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfi(b*x),x, algorithm="maxima")
[Out] 1/3*x^3*erfi(b*x) - 1/3*(b^2*x^2 - 1)*e^(b^2*x^2)/(sqrt(pi)*b^3)
```

Fricas [A]
time = 0.36, size = 43, normalized size = 0.75

$$\frac{\pi b^3x^3\,\mathrm{erfi}\,(bx) - \sqrt{\pi}\,(b^2x^2-1)e^{(b^2x^2)}}{3\,\pi b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfi(b*x),x, algorithm="fricas")
[Out] 1/3*(pi*b^3*x^3*erfi(b*x) - sqrt(pi)*(b^2*x^2 - 1)*e^(b^2*x^2))/(pi*b^3)
```

Sympy [A]
time = 0.12, size = 49, normalized size = 0.86

$$\begin{cases} \frac{x^3\,\mathrm{erfi}\,(bx)}{3} - \frac{x^2e^{b^2x^2}}{3\sqrt{\pi}\,b} + \frac{e^{b^2x^2}}{3\sqrt{\pi}\,b^3} & \text{for } b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*erfi(b*x),x)
[Out] Piecewise((x**3*erfi(b*x)/3 - x**2*exp(b**2*x**2)/(3*sqrt(pi)*b) + exp(b**2
*x**2)/(3*sqrt(pi)*b**3), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfi(b*x),x, algorithm="giac")
[Out] integrate(x^2*erfi(b*x), x)
```

Mupad [B]
time = 0.15, size = 35, normalized size = 0.61

$$\frac{x^3\,\mathrm{erfi}(b\,x)}{3}-\frac{\mathrm{e}^{b^2\,x^2}\,\left(b^2\,x^2-1\right)}{3\,b^3\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfi(b*x),x)
```

```
[Out] (x^3*erfi(b*x))/3 - (exp(b^2*x^2)*(b^2*x^2 - 1))/(3*b^3*pi^(1/2))
```

3.217 $\int \mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=26

$$-\frac{e^{b^2x^2}}{b\sqrt{\pi}}+x\text{Erfi}(bx)$$

```
[Out] x*erfi(b*x)-exp(b^2*x^2)/b/Pi^(1/2)
```

Rubi [A]
time = 0.00, antiderivative size = 26, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 4, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.250, Rules used = {6486}

$$x\text{Erfi}(bx)-\frac{e^{b^2x^2}}{\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x],x]
[Out] -(E^(b^2*x^2)/(b*Sqrt[Pi])) + x*Erfi[b*x]
```

Rule 6486

```
Int[Erfi[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[(a + b*x)*(Erfi[a + b*x]/b)
, x] - Simp[E^(a + b*x)^2/(b*Sqrt[Pi]), x] /; FreeQ[{a, b}, x]
```

Rubi steps

$$\int \text{erfi}(bx)\,dx=-\frac{e^{b^2x^2}}{b\sqrt{\pi}}+x\text{erfi}(bx)$$

Mathematica [A]
time = 0.01, size = 26, normalized size = 1.00

$$-\frac{e^{b^2x^2}}{b\sqrt{\pi}}+x\text{Erfi}(bx)$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x],x]
[Out] -(E^(b^2*x^2)/(b*Sqrt[Pi])) + x*Erfi[b*x]
```

Maple [A]
time = 0.21, size = 26, normalized size = 1.00

method	result	size
derivativedivides	$\frac{bx\,\mathrm{erfi}(bx)-\frac{\mathrm{e}^{b^2x^2}}{\sqrt{\pi}}}{b}$	26
default	$\frac{bx\,\mathrm{erfi}(bx)-\frac{\mathrm{e}^{b^2x^2}}{\sqrt{\pi}}}{b}$	26
meijerg	$-\frac{-2+2\,\mathrm{e}^{b^2x^2}-2bx\sqrt{\pi}\,\mathrm{erfi}(bx)}{2\sqrt{\pi}\,b}$	32

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*(b*x*erfi(b*x)-1/Pi^(1/2)*exp(b^2*x^2))
```

Maxima [A]
time = 0.27, size = 25, normalized size = 0.96

$$\frac{bx\,\mathrm{erfi}\left(bx\right)-\frac{e^{\left(b^2x^2\right)}}{\sqrt{\pi}}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x),x, algorithm="maxima")
```

```
[Out] (b*x*erfi(b*x) - e^(b^2*x^2)/sqrt(pi))/b
```

Fricas [A]
time = 0.36, size = 29, normalized size = 1.12

$$\frac{\pi bx\,\mathrm{erfi}\left(bx\right)-\sqrt{\pi}\,e^{\left(b^2x^2\right)}}{\pi b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x),x, algorithm="fricas")
```

```
[Out] (pi*b*x*erfi(b*x) - sqrt(pi)*e^(b^2*x^2))/(pi*b)
```

Sympy [A]
time = 0.06, size = 22, normalized size = 0.85

$$\begin{cases} x\,\mathrm{erfi}\left(bx\right)-\frac{e^{b^2x^2}}{\sqrt{\pi}\,b} & \text{for}\ b\neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x),x)
```

```
[Out] Piecewise((x*erfi(b*x) - exp(b**2*x**2)/(sqrt(pi)*b), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x),x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x), x)
```

Mupad [B]
time = 0.05, size = 23, normalized size = 0.88

$$x\,\mathrm{erfi}(b\,x)-\frac{\mathrm{e}^{b^2\,x^2}}{b\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x),x)
```

```
[Out] x*erfi(b*x) - exp(b^2*x^2)/(b*pi^(1/2))
```

3.218 $\int \frac{\textbf{Erfi}(bx)}{x^2}\,dx$

Optimal. Leaf size=25

$$-\frac{\text{Erfi}(bx)}{x}+\frac{b\text{Ei}(b^2x^2)}{\sqrt{\pi}}$$

```
[Out] -erfi(b*x)/x+b*Ei(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.02, antiderivative size = 25, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.250, Rules used = {6498, 2241}

$$\frac{b\text{Ei}(b^2x^2)}{\sqrt{\pi}}-\frac{\text{Erfi}(bx)}{x}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]/x^2,x]
```

```
[Out] -(Erfi[b*x]/x) + (b*ExpIntegralEi[b^2*x^2])/Sqrt[Pi]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 6498

```
Int[Erfi[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfi[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)*E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{\text{erfi}(bx)}{x^2}\,dx &= -\frac{\text{erfi}(bx)}{x}+\frac{(2b)\int \frac{e^{b^2x^2}}{x}\,dx}{\sqrt{\pi}}\\ &= -\frac{\text{erfi}(bx)}{x}+\frac{b\text{Ei}(b^2x^2)}{\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 25, normalized size = 1.00

$$-\frac{\text{Erfi}(bx)}{x}+\frac{b\text{Ei}(b^2x^2)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]/x^2,x]
```

```
[Out] -(Erfi[b*x]/x) + (b*ExpIntegralEi[b^2*x^2])/Sqrt[Pi]
```

Maple [A]
time = 0.62, size = 31, normalized size = 1.24

method	result	size
derivativedivides	$b\left(-\frac{\operatorname{erfi}(bx)}{bx}-\frac{\operatorname{expIntegral}\left(1,-b^{2}x^{2}\right)}{\sqrt{\pi}}\right)$	31
default	$b\left(-\frac{\operatorname{erfi}(bx)}{bx}-\frac{\operatorname{expIntegral}\left(1,-b^{2}x^{2}\right)}{\sqrt{\pi}}\right)$	31
meijerg	$\frac{b\left(-\frac{2\sqrt{\pi}\,\operatorname{erfi}(bx)}{bx}-2\ln\left(-b^{2}x^{2}\right)-2\operatorname{expIntegral}\left(1,-b^{2}x^{2}\right)+4\ln(x)+4\ln(ib)\right)}{2\sqrt{\pi}}$	57

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/x^2,x,method=_RETURNVERBOSE)
```

```
[Out] b*(-1/b/x*erfi(b*x)-1/Pi^(1/2)*Ei(1,-b^2*x^2))
```

Maxima [A]
time = 0.30, size = 23, normalized size = 0.92

$$\frac{b\operatorname{Ei}(b^2x^2)}{\sqrt{\pi}}-\frac{\operatorname{erfi}(bx)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^2,x, algorithm="maxima")
```

```
[Out] b*Ei(b^2*x^2)/sqrt(pi) - erfi(b*x)/x
```

Fricas [A]
time = 0.36, size = 29, normalized size = 1.16

$$\frac{\sqrt{\pi}\,bx\operatorname{Ei}(b^2x^2)-\pi\operatorname{erfi}(bx)}{\pi x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^2,x, algorithm="fricas")
```

```
[Out] (sqrt(pi)*b*x*Ei(b^2*x^2) - pi*erfi(b*x))/(pi*x)
```

Sympy [C] Result contains complex when optimal does not.
time = 0.56, size = 32, normalized size = 1.28

$$-\frac{b\,\mathrm{E}_{1}\left(b^{2}x^{2}e^{i\pi}\right)}{\sqrt{\pi}}-\frac{i\,\mathrm{erfc}\left(ibx\right)}{x}+\frac{i}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x**2,x)
```

```
[Out] -b*expint(1, b**2*x**2*exp_polar(I*pi))/sqrt(pi) - I*erfc(I*b*x)/x + I/x
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^2,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)/x^2, x)
```

Mupad [B]
time = 0.18, size = 23, normalized size = 0.92

$$\frac{b\,\mathrm{ei}(b^2\,x^2)}{\sqrt{\pi}}-\frac{\mathrm{erfi}(b\,x)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/x^2,x)
```

```
[Out] (b*ei(b^2*x^2))/pi^(1/2) - erfi(b*x)/x
```

3.219 $\int \frac{\mathbf{Erfi}(bx)}{x^4}\,dx$

Optimal. Leaf size=54

$$-\frac{be^{b^2x^2}}{3\sqrt{\pi}\,x^2}-\frac{\mathrm{Erfi}(bx)}{3x^3}+\frac{b^3\mathrm{Ei}(b^2x^2)}{3\sqrt{\pi}}$$

```
[Out] -1/3*erfi(b*x)/x^3-1/3*b*exp(b^2*x^2)/x^2/Pi^(1/2)+1/3*b^3*Ei(b^2*x^2)/Pi^(
1/2)
```

Rubi [A]
time = 0.03, antiderivative size = 54, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6498, 2245, 2241}

$$-\frac{be^{b^2x^2}}{3\sqrt{\pi}\,x^2}+\frac{b^3\mathrm{Ei}(b^2x^2)}{3\sqrt{\pi}}-\frac{\mathrm{Erfi}(bx)}{3x^3}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]/x^4,x]
```

```
[Out] -1/3*(b*E^(b^2*x^2))/(Sqrt[Pi]*x^2) - Erfi[b*x]/(3*x^3) + (b^3*ExpIntegralE
i[b^2*x^2])/(3*Sqrt[Pi])
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6498

```
Int[Erfi[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfi[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)*E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{\operatorname{erfi}(bx)}{x^4}\,dx &= -\frac{\operatorname{erfi}(bx)}{3x^3} + \frac{(2b)\int \frac{e^{b^2x^2}}{x^3}\,dx}{3\sqrt{\pi}} \\
&= -\frac{be^{b^2x^2}}{3\sqrt{\pi}\,x^2} - \frac{\operatorname{erfi}(bx)}{3x^3} + \frac{(2b^3)\int \frac{e^{b^2x^2}}{x}\,dx}{3\sqrt{\pi}} \\
&= -\frac{be^{b^2x^2}}{3\sqrt{\pi}\,x^2} - \frac{\operatorname{erfi}(bx)}{3x^3} + \frac{b^3\operatorname{Ei}(b^2x^2)}{3\sqrt{\pi}}
\end{aligned}
$$

Mathematica [A]
time = 0.02, size = 50, normalized size = 0.93

$$
-\frac{\frac{be^{b^2x^2}x}{\sqrt{\pi}} + \operatorname{Erfi}(bx) - \frac{b^3x^3\operatorname{Ei}(b^2x^2)}{\sqrt{\pi}}}{3x^3}
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]/x^4,x]
```

```
[Out] -1/3*((b*E^(b^2*x^2)*x)/Sqrt[Pi] + Erfi[b*x] - (b^3*x^3*ExpIntegralEi[b^2*x
^2])/Sqrt[Pi])/x^3
```

Maple [A]
time = 0.30, size = 52, normalized size = 0.96

method	result	siz
derivativedivides	$b^3\left(-\frac{\operatorname{erfi}(bx)}{3b^3x^3} + \frac{-\frac{e^{b^2x^2}}{3b^2x^2} - \frac{\operatorname{expIntegral}\left(1,-b^2x^2\right)}{3}}{\sqrt{\pi}}\right)$	52
default	$b^3\left(-\frac{\operatorname{erfi}(bx)}{3b^3x^3} + \frac{-\frac{e^{b^2x^2}}{3b^2x^2} - \frac{\operatorname{expIntegral}\left(1,-b^2x^2\right)}{3}}{\sqrt{\pi}}\right)$	52
meijerg	$-\frac{b^3\left(-\frac{50b^2x^2+90}{45b^2x^2} + \frac{2\,e^{b^2x^2}}{3b^2x^2} + \frac{2\sqrt{\pi}\,\operatorname{erfi}(bx)}{3b^3x^3} + \frac{2\ln\left(-b^2x^2\right)}{3} + \frac{2\operatorname{expIntegral}\left(1,-b^2x^2\right)}{3} + \frac{10}{9} - \frac{4\ln(x)}{3} - \frac{4\ln(ib)}{3} + \frac{2}{b^2x^2}\right)}{2\sqrt{\pi}}$	102

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/x^4,x,method=_RETURNVERBOSE)
```

```
[Out] b^3*(-1/3/b^3/x^3*erfi(b*x)+2/3/Pi^(1/2)*(-1/2*exp(b^2*x^2)/b^2/x^2-1/2*Ei(
1,-b^2*x^2)))
```

Maxima [A]
time = 0.30, size = 28, normalized size = 0.52

$$\frac{b^3\Gamma(-1,-b^2x^2)}{3\sqrt{\pi}}-\frac{\operatorname{erfi}(bx)}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^4,x, algorithm="maxima")
```

```
[Out] 1/3*b^3*gamma(-1, -b^2*x^2)/sqrt(pi) - 1/3*erfi(b*x)/x^3
```

Fricas [A]
time = 0.36, size = 48, normalized size = 0.89

$$-\frac{\pi\operatorname{erfi}(bx)-\sqrt{\pi}\left(b^3x^3\mathrm{Ei}(b^2x^2)-bxe^{(b^2x^2)}\right)}{3\pi x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^4,x, algorithm="fricas")
```

```
[Out] -1/3*(pi*erfi(b*x) - sqrt(pi)*(b^3*x^3*Ei(b^2*x^2) - b*x*e^(b^2*x^2)))/(pi*
x^3)
```

Sympy [C] Result contains complex when optimal does not.
time = 1.20, size = 63, normalized size = 1.17

$$-\frac{b^3\,\mathrm{E}_1\left(b^2x^2e^{i\pi}\right)}{3\sqrt{\pi}}-\frac{be^{b^2x^2}}{3\sqrt{\pi}\,x^2}-\frac{i\operatorname{erfc}(ibx)}{3x^3}+\frac{i}{3x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x**4,x)
```

```
[Out] -b**3*expint(1, b**2*x**2*exp_polar(I*pi))/(3*sqrt(pi)) - b*exp(b**2*x**2)/
(3*sqrt(pi)*x**2) - I*erfc(I*b*x)/(3*x**3) + I/(3*x**3)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^4,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)/x^4, x)
```

Mupad [B]
time = 0.22, size = 43, normalized size = 0.80

$$\frac{b^3\,\mathrm{ei}\left(b^2\,x^2\right)}{3\,\sqrt{\pi}}-\frac{\mathrm{erfi}\left(b\,x\right)}{3\,x^3}-\frac{b\,\mathrm{e}^{b^2\,x^2}}{3\,x^2\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/x^4,x)
```

```
[Out] (b^3*ei(b^2*x^2))/(3*pi^(1/2)) - erfi(b*x)/(3*x^3) - (b*exp(b^2*x^2))/(3*x^
2*pi^(1/2))
```

3.220 $\int \frac{\mathbf{Erfi}(bx)}{x^6}\, dx$

Optimal. Leaf size=78

$$-\frac{be^{b^2x^2}}{10\sqrt{\pi}\,x^4}-\frac{b^3e^{b^2x^2}}{10\sqrt{\pi}\,x^2}-\frac{\mathrm{Erfi}(bx)}{5x^5}+\frac{b^5\mathrm{Ei}(b^2x^2)}{10\sqrt{\pi}}$$

```
[Out] -1/5*erfi(b*x)/x^5-1/10*b*exp(b^2*x^2)/x^4/Pi^(1/2)-1/10*b^3*exp(b^2*x^2)/x
^2/Pi^(1/2)+1/10*b^5*Ei(b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.05, antiderivative size = 78, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6498, 2245, 2241}

$$-\frac{be^{b^2x^2}}{10\sqrt{\pi}\,x^4}+\frac{b^5\mathrm{Ei}(b^2x^2)}{10\sqrt{\pi}}-\frac{b^3e^{b^2x^2}}{10\sqrt{\pi}\,x^2}-\frac{\mathrm{Erfi}(bx)}{5x^5}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]/x^6,x]
```

```
[Out] -1/10*(b*E^(b^2*x^2))/(Sqrt[Pi]*x^4) - (b^3*E^(b^2*x^2))/(10*Sqrt[Pi]*x^2)
- Erfi[b*x]/(5*x^5) + (b^5*ExpIntegralEi[b^2*x^2])/(10*Sqrt[Pi])
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6498

```
Int[Erfi[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfi[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)*E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{\operatorname{erfi}(bx)}{x^6}\,dx &= -\frac{\operatorname{erfi}(bx)}{5x^5}+\frac{(2b)\int \frac{e^{b^2x^2}}{x^5}\,dx}{5\sqrt{\pi}}\\
&= -\frac{be^{b^2x^2}}{10\sqrt{\pi}\,x^4}-\frac{\operatorname{erfi}(bx)}{5x^5}+\frac{b^3\int \frac{e^{b^2x^2}}{x^3}\,dx}{5\sqrt{\pi}}\\
&= -\frac{be^{b^2x^2}}{10\sqrt{\pi}\,x^4}-\frac{b^3e^{b^2x^2}}{10\sqrt{\pi}\,x^2}-\frac{\operatorname{erfi}(bx)}{5x^5}+\frac{b^5\int \frac{e^{b^2x^2}}{x}\,dx}{5\sqrt{\pi}}\\
&= -\frac{be^{b^2x^2}}{10\sqrt{\pi}\,x^4}-\frac{b^3e^{b^2x^2}}{10\sqrt{\pi}\,x^2}-\frac{\operatorname{erfi}(bx)}{5x^5}+\frac{b^5\operatorname{Ei}(b^2x^2)}{10\sqrt{\pi}}
\end{aligned}
$$

Mathematica [A]
time = 0.02, size = 61, normalized size = 0.78

$$\frac{-be^{b^2x^2}x(1+b^2x^2)-2\sqrt{\pi}\operatorname{Erfi}(bx)+b^5x^5\operatorname{Ei}(b^2x^2)}{10\sqrt{\pi}\,x^5}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]/x^6,x]
```

```
[Out] (-(b*E^(b^2*x^2)*x*(1 + b^2*x^2)) - 2*Sqrt[Pi]*Erfi[b*x] + b^5*x^5*ExpInteg
ralEi[b^2*x^2])/(10*Sqrt[Pi]*x^5)
```

Maple [A]
time = 0.34, size = 68, normalized size = 0.87

method	result
derivativedivides	$b^5\left(-\frac{\operatorname{erfi}(bx)}{5b^5x^5}+\frac{-\frac{e^{b^2x^2}}{10b^4x^4}-\frac{e^{b^2x^2}}{10b^2x^2}-\frac{\operatorname{expIntegral}\left(1,-b^2x^2\right)}{10}}{\sqrt{\pi}}\right)$
default	$b^5\left(-\frac{\operatorname{erfi}(bx)}{5b^5x^5}+\frac{-\frac{e^{b^2x^2}}{10b^4x^4}-\frac{e^{b^2x^2}}{10b^2x^2}-\frac{\operatorname{expIntegral}\left(1,-b^2x^2\right)}{10}}{\sqrt{\pi}}\right)$
meijerg	$\frac{b^5\left(\frac{399b^4x^4+700b^2x^2+1050}{1050b^4x^4}-\frac{\left(21b^2x^2+21\right)e^{b^2x^2}}{105b^4x^4}-\frac{2\sqrt{\pi}\operatorname{erfi}(bx)}{5b^5x^5}-\frac{\ln\left(-b^2x^2\right)}{5}-\frac{\operatorname{expIntegral}\left(1,-b^2x^2\right)}{5}-\frac{19}{50}+\frac{2\ln(x)}{5}+\frac{2\ln(ib)}{5}\right.}{2\sqrt{\pi}}$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/x^6,x,method=_RETURNVERBOSE)
```

```
[Out] b^5*(-1/5/b^5/x^5*erfi(b*x)+2/5/Pi^(1/2)*(-1/4*exp(b^2*x^2)/b^4/x^4-1/4*exp
(b^2*x^2)/b^2/x^2-1/4*Ei(1,-b^2*x^2)))
```

Maxima [A]
time = 0.36, size = 28, normalized size = 0.36

$$-\frac{b^5\Gamma(-2,-b^2x^2)}{5\sqrt{\pi}}-\frac{\operatorname{erfi}(bx)}{5x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^6,x, algorithm="maxima")
```

```
[Out] -1/5*b^5*gamma(-2, -b^2*x^2)/sqrt(pi) - 1/5*erfi(b*x)/x^5
```

Fricas [A]
time = 0.35, size = 58, normalized size = 0.74

$$-\frac{2\pi\operatorname{erfi}(bx)-\sqrt{\pi}\left(b^5x^5\operatorname{Ei}(b^2x^2)-(b^3x^3+bx)e^{(b^2x^2)}\right)}{10\pi x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^6,x, algorithm="fricas")
```

```
[Out] -1/10*(2*pi*erfi(b*x) - sqrt(pi)*(b^5*x^5*Ei(b^2*x^2) - (b^3*x^3 + b*x)*e^(
b^2*x^2)))/(pi*x^5)
```

Sympy [C] Result contains complex when optimal does not.
time = 1.97, size = 85, normalized size = 1.09

$$-\frac{b^5\operatorname{E}_1(b^2x^2e^{i\pi})}{10\sqrt{\pi}}-\frac{b^3e^{b^2x^2}}{10\sqrt{\pi}x^2}-\frac{be^{b^2x^2}}{10\sqrt{\pi}x^4}-\frac{i\operatorname{erfc}(ibx)}{5x^5}+\frac{i}{5x^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x**6,x)
```

```
[Out] -b**5*expint(1, b**2*x**2*exp_polar(I*pi))/(10*sqrt(pi)) - b**3*exp(b**2*x*
*2)/(10*sqrt(pi)*x**2) - b*exp(b**2*x**2)/(10*sqrt(pi)*x**4) - I*erfc(I*b*x
)/(5*x**5) + I/(5*x**5)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/x^6,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)/x^6, x)
```

Mupad [B]
time = 0.22, size = 62, normalized size = 0.79

$$\frac{b^5\,\mathrm{ei}(b^2\,x^2)}{10\,\sqrt{\pi}}-\frac{\mathrm{erfi}(b\,x)}{5\,x^5}-\frac{\frac{b\,\mathrm{e}^{b^2\,x^2}}{2}+\frac{b^3\,x^2\,\mathrm{e}^{b^2\,x^2}}{2}}{5\,x^4\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/x^6,x)
```

```
[Out] (b^5*ei(b^2*x^2))/(10*pi^(1/2)) - erfi(b*x)/(5*x^5) - ((b*exp(b^2*x^2))/2 +
 (b^3*x^2*exp(b^2*x^2))/2)/(5*x^4*pi^(1/2))
```

3.221 $\int (c+dx)^3 \textbf{Erfi}(a+bx)\,dx$

Optimal. Leaf size=279

$$\frac{d^2(bc-ad)e^{(a+bx)^2}}{b^4\sqrt{\pi}}-\frac{(bc-ad)^3e^{(a+bx)^2}}{b^4\sqrt{\pi}}+\frac{3d^3e^{(a+bx)^2}(a+bx)}{8b^4\sqrt{\pi}}-\frac{3d(bc-ad)^2e^{(a+bx)^2}(a+bx)}{2b^4\sqrt{\pi}}-\frac{d^2(bc-ad)e^{(a\cdots}}{b^4\sqrt{\cdots}}$$

```
[Out] -3/16*d^3*erfi(b*x+a)/b^4+3/4*d*(-a*d+b*c)^2*erfi(b*x+a)/b^4-1/4*(-a*d+b*c)
^4*erfi(b*x+a)/b^4/d+1/4*(d*x+c)^4*erfi(b*x+a)/d+d^2*(-a*d+b*c)*exp((b*x+a)
^2)/b^4/Pi^(1/2)-(-a*d+b*c)^3*exp((b*x+a)^2)/b^4/Pi^(1/2)+3/8*d^3*exp((b*x+
a)^2)*(b*x+a)/b^4/Pi^(1/2)-3/2*d*(-a*d+b*c)^2*exp((b*x+a)^2)*(b*x+a)/b^4/Pi
^(1/2)-d^2*(-a*d+b*c)*exp((b*x+a)^2)*(b*x+a)^2/b^4/Pi^(1/2)-1/4*d^3*exp((b*
x+a)^2)*(b*x+a)^3/b^4/Pi^(1/2)
```

Rubi [A]
time = 0.19, antiderivative size = 279, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 5, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.357$, Rules used = {6498, 2258, 2235, 2240, 2243}

$$-\frac{d^2e^{(a+bx)^2}(a+bx)^2(bc-ad)}{\sqrt{\pi}\,b^4}+\frac{d^2e^{(a+bx)^2}(bc-ad)}{\sqrt{\pi}\,b^4}-\frac{(bc-ad)^4\text{Erfi}(a+bx)}{4b^4d}+\frac{3d(bc-ad)^2\text{Erfi}(a+bx)}{4b^4}-\frac{e^{(a+bx)^2}(bc-ad)^3}{\sqrt{\pi}\,b^4}-\frac{3de^{(a+bx)^2}(a+bx)(bc-ad)^2}{2\sqrt{\pi}\,b^4}-\frac{3d^3\text{Erfi}(a+bx)}{16b^4}-\frac{d^3e^{(a+bx)^2}(a+bx)^3}{4\sqrt{\pi}\,b^4}+\frac{3d^3e^{(a+bx)^2}(a+bx)}{8\sqrt{\pi}\,b^4}+\frac{(c+dx)^4\text{Erfi}(a+bx)}{4d}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)^3*Erfi[a + b*x],x]
```

```
[Out] (d^2*(b*c - a*d)*E^(a + b*x)^2)/(b^4*Sqrt[Pi]) - ((b*c - a*d)^3*E^(a + b*x)
^2)/(b^4*Sqrt[Pi]) + (3*d^3*E^(a + b*x)^2*(a + b*x))/(8*b^4*Sqrt[Pi]) - (3*
d*(b*c - a*d)^2*E^(a + b*x)^2*(a + b*x))/(2*b^4*Sqrt[Pi]) - (d^2*(b*c - a*d
)*E^(a + b*x)^2*(a + b*x)^2)/(b^4*Sqrt[Pi]) - (d^3*E^(a + b*x)^2*(a + b*x)^
3)/(4*b^4*Sqrt[Pi]) - (3*d^3*Erfi[a + b*x])/(16*b^4) + (3*d*(b*c - a*d)^2*E
rfi[a + b*x])/(4*b^4) - ((b*c - a*d)^4*Erfi[a + b*x])/(4*b^4*d) + ((c + d*x
)^4*Erfi[a + b*x])/(4*d)
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 2258

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*(u_), x_Symbol] :> Int[E
xpandLinearProduct[F^(a + b*(c + d*x)^n), u, c, d, x], x] /; FreeQ[{F, a, b
, c, d, n}, x] && PolynomialQ[u, x]
```

Rule 6498

```
Int[Erfi[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfi[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)*E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int (c+dx)^3\text{erfi}(a+bx)\,dx &= \frac{(c+dx)^4\text{erfi}(a+bx)}{4d} - \frac{b\int e^{(a+bx)^2}(c+dx)^4\,dx}{2d\sqrt{\pi}} \\
&= \frac{(c+dx)^4\text{erfi}(a+bx)}{4d} - \frac{b\int \left(\frac{(bc-ad)^4e^{(a+bx)^2}}{b^4} + \frac{4d(bc-ad)^3e^{(a+bx)^2}(a+bx)}{b^4} + \frac{6d^2(bc-ad)^2e \cdots}{\cdots}\right.}{2\cdots} \\
&= \frac{(c+dx)^4\text{erfi}(a+bx)}{4d} - \frac{d^3\int e^{(a+bx)^2}(a+bx)^4\,dx}{2b^3\sqrt{\pi}} - \frac{(2d^2(bc-ad))\int e^{(a+bx)^2}(a \cdots}{b^3\sqrt{\pi}} \\
&= -\frac{(bc-ad)^3e^{(a+bx)^2}}{b^4\sqrt{\pi}} - \frac{3d(bc-ad)^2e^{(a+bx)^2}(a+bx)}{2b^4\sqrt{\pi}} - \frac{d^2(bc-ad)e^{(a+bx)^2}(a+b \cdots}{b^4\sqrt{\pi}} \\
&= \frac{d^2(bc-ad)e^{(a+bx)^2}}{b^4\sqrt{\pi}} - \frac{(bc-ad)^3e^{(a+bx)^2}}{b^4\sqrt{\pi}} + \frac{3d^3e^{(a+bx)^2}(a+bx)}{8b^4\sqrt{\pi}} - \frac{3d(bc-ad)^2e \cdots}{2b^4 \cdots} \\
&= \frac{d^2(bc-ad)e^{(a+bx)^2}}{b^4\sqrt{\pi}} - \frac{(bc-ad)^3e^{(a+bx)^2}}{b^4\sqrt{\pi}} + \frac{3d^3e^{(a+bx)^2}(a+bx)}{8b^4\sqrt{\pi}} - \frac{3d(bc-ad)^2e \cdots}{2b^4 \cdots}
\end{aligned}
$$

Mathematica [A]
time = 0.17, size = 237, normalized size = 0.85

$$
\frac{-2e^{(a+bx)^2}\left(a\left(5-2a^2\right)d^3+bd^2\left(8\left(-1+a^2\right)c+\left(-3+2a^2\right)dx\right)-2ab^2d\left(6c^2+4cdx+d^2x^2\right)+2b^3\left(4c^3+6c^2dx+4cd^2x^2+d^3x^3\right)\right)+\sqrt{\pi}\left(12b^2c^2d+16a^3bcd^2-3d^3-4a^4d^3+12a^2d\left(-2b^2c^2+d^2\right)+8a\left(2b^3c^3-3bcd^2\right)+4b^4x\left(4c^3+6c^2dx+4cd^2x^2+d^3x^3\right)\right)\text{Erfi}(a+bx)}{16b^4\sqrt{\pi}}
$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^3*Erfi[a + b*x],x]
```

```
[Out] (-2*E^(a + b*x)^2*(a*(5 - 2*a^2)*d^3 + b*d^2*(8*(-1 + a^2)*c + (-3 + 2*a^2)
*d*x) - 2*a*b^2*d*(6*c^2 + 4*c*d*x + d^2*x^2) + 2*b^3*(4*c^3 + 6*c^2*d*x +
4*c*d^2*x^2 + d^3*x^3)) + Sqrt[Pi]*(12*b^2*c^2*d + 16*a^3*b*c*d^2 - 3*d^3 -
 4*a^4*d^3 + 12*a^2*d*(-2*b^2*c^2 + d^2) + 8*a*(2*b^3*c^3 - 3*b*c*d^2) + 4*
b^4*x*(4*c^3 + 6*c^2*d*x + 4*c*d^2*x^2 + d^3*x^3))*Erfi[a + b*x])/(16*b^4*S
qrt[Pi])
```

Maple [B] Leaf count of result is larger than twice the leaf count of optimal. 702 vs. $2(247) = 494$.
time = 0.77, size = 703, normalized size = 2.52 Too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^3*erfi(b*x+a),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*(1/4/b^3*d^3*erfi(b*x+a)*a^4-1/b^2*d^2*erfi(b*x+a)*a^3*c-1/b^3*d^3*erfi
(b*x+a)*a^3*(b*x+a)+3/2/b*d*erfi(b*x+a)*a^2*c^2+3/b^2*d^2*erfi(b*x+a)*a^2*c
*(b*x+a)+3/2/b^3*d^3*erfi(b*x+a)*a^2*(b*x+a)^2-erfi(b*x+a)*a*c^3-3/b*d*erfi
(b*x+a)*a*c^2*(b*x+a)-3/b^2*d^2*erfi(b*x+a)*a*c*(b*x+a)^2-1/b^3*d^3*erfi(b*
x+a)*a*(b*x+a)^3+1/4*b/d*erfi(b*x+a)*c^4+erfi(b*x+a)*c^3*(b*x+a)+3/2/b*d*er
fi(b*x+a)*c^2*(b*x+a)^2+1/b^2*d^2*erfi(b*x+a)*c*(b*x+a)^3+1/4/b^3*d^3*erfi(
b*x+a)*(b*x+a)^4-1/2/b^3/d/Pi^(1/2)*(1/2*a^4*d^4*Pi^(1/2)*erfi(b*x+a)+1/2*b
^4*c^4*Pi^(1/2)*erfi(b*x+a)+d^4*(1/2*exp((b*x+a)^2)*(b*x+a)^3-3/4*(b*x+a)*e
xp((b*x+a)^2)+3/8*Pi^(1/2)*erfi(b*x+a))-4*a*d^4*(1/2*exp((b*x+a)^2)*(b*x+a)
^2-1/2*exp((b*x+a)^2))+6*a^2*d^4*(1/2*(b*x+a)*exp((b*x+a)^2)-1/4*Pi^(1/2)*e
rfi(b*x+a))-2*a^3*d^4*exp((b*x+a)^2)-2*a*b^3*c^3*d*Pi^(1/2)*erfi(b*x+a)+3*a
^2*b^2*c^2*d^2*Pi^(1/2)*erfi(b*x+a)-2*a^3*b*c*d^3*Pi^(1/2)*erfi(b*x+a)+4*b*
c*d^3*(1/2*exp((b*x+a)^2)*(b*x+a)^2-1/2*exp((b*x+a)^2))+6*b^2*c^2*d^2*(1/2*
(b*x+a)*exp((b*x+a)^2)-1/4*Pi^(1/2)*erfi(b*x+a))+2*b^3*c^3*d*exp((b*x+a)^2)
-12*a*b*c*d^3*(1/2*(b*x+a)*exp((b*x+a)^2)-1/4*Pi^(1/2)*erfi(b*x+a))-6*a*b^2
*c^2*d^2*exp((b*x+a)^2)+6*a^2*b*c*d^3*exp((b*x+a)^2)))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^3*erfi(b*x+a),x, algorithm="maxima")
```

```
[Out] integrate((d*x + c)^3*erfi(b*x + a), x)
```

Fricas [A]
time = 0.39, size = 263, normalized size = 0.94

$$-\frac{2\sqrt{\pi}\left(2b^{3}d^{3}x^{3}+8b^{3}c^{3}-12ab^{2}c^{2}d+8(a^{2}-1)bcd^{2}-(2a^{3}-5a)d^{3}+2(4b^{3}cd^{2}-ab^{2}d^{3})x^{2}+(12b^{3}c^{2}d-8ab^{2}cd^{2}+(2a^{2}-3)bd^{3})x\right)e^{\left(b^{2}x^{2}+2abx+a^{2}\right)}-\left(4\pi b^{4}d^{3}x^{4}+16\pi b^{4}cd^{2}x^{3}+24\pi b^{4}c^{2}dx^{2}+16\pi b^{4}c^{3}x+\pi\left(16ab^{3}c^{3}-12(2a^{2}-1)b^{2}c^{2}d+8(2a^{3}-3a)bcd^{2}-(4a^{4}-12a^{2}+3)d^{3}\right)\right)\operatorname{erfi}(bx+a)}{16\pi b^{4}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^3*erfi(b*x+a),x, algorithm="fricas")
```

```
[Out] -1/16*(2*sqrt(pi)*(2*b^3*d^3*x^3 + 8*b^3*c^3 - 12*a*b^2*c^2*d + 8*(a^2 - 1)
*b*c*d^2 - (2*a^3 - 5*a)*d^3 + 2*(4*b^3*c*d^2 - a*b^2*d^3)*x^2 + (12*b^3*c^
2*d - 8*a*b^2*c*d^2 + (2*a^2 - 3)*b*d^3)*x)*e^(b^2*x^2 + 2*a*b*x + a^2) - (
4*pi*b^4*d^3*x^4 + 16*pi*b^4*c*d^2*x^3 + 24*pi*b^4*c^2*d*x^2 + 16*pi*b^4*c^
3*x + pi*(16*a*b^3*c^3 - 12*(2*a^2 - 1)*b^2*c^2*d + 8*(2*a^3 - 3*a)*b*c*d^2
 - (4*a^4 - 12*a^2 + 3)*d^3))*erfi(b*x + a))/(pi*b^4)
```

Sympy [B] Leaf count of result is larger than twice the leaf count of optimal. 746 vs. $2(258) = 516$.
time = 2.09, size = 746, normalized size = 2.67

$$\begin{cases} - \frac{a^{4} d^{3} \operatorname{erfi}{\left(a + b x \right)}}{4 b^{4}} + \frac{a^{3} c d^{2} \operatorname{erfi}{\left(a + b x \right)}}{b^{3}} + \frac{a^{3} d^{3} e^{a^{2}} e^{b^{2} x^{2}} e^{2 a b x}}{4 \sqrt{\pi} b^{4}} - \frac{3 a^{2} c^{2} d \operatorname{erfi}{\left(a + b x \right)}}{2 b^{2}} - \frac{a^{2} c d^{2} e^{a^{2}} e^{b^{2} x^{2}} e^{2 a b x}}{\sqrt{\pi} b^{3}} - \frac{a^{2} d^{3} x e^{a^{2}} e^{b^{2} x^{2}} e^{2 a b x}}{4 \sqrt{\pi} b^{3}} + \frac{3 a^{2} d^{3} \operatorname{erfi}{\left(a + b x \right)}}{4 b^{4}} + \frac{a c^{3} \operatorname{erfi}{\left(a + b x \right)}}{b} + \frac{3 a c^{2} d e^{a^{2}} e^{b^{2} x^{2}} e^{2 a b x}}{2 \sqrt{\pi} b^{2}} + \frac{a c d^{2} x e^{a^{2}} e^{b^{2} x^{2}} e^{2 a b x}}{\sqrt{\pi} b^{2}} + \frac{a d^{3} x^{2} e^{a^{2}} e^{b^{2} x^{2}} e^{2 a b x}}{4 \sqrt{\pi} b^{2}} - \frac{3 a c d^{2} \operatorname{erfi}{\left(a + b x \right)}}{2 b^{3}} - \frac{5 a d^{3} e^{a^{2}} e^{b^{2} x^{2}} e^{2 a b x}}{8 \sqrt{\pi} b^{4}} + c^{3} x \operatorname{erfi}{\left(a + b x \right)} + \frac{3 c^{2} d x^{2} \operatorname{erfi}{\left(a + b x \right)}}{2} + c d^{2} x^{3} \operatorname{erfi}{\left(a + b x \right)} + \frac{d^{3} x^{4} \operatorname{erfi}{\left(a + b x \right)}}{4} - \frac{c^{3} e^{a^{2}} e^{b^{2} x^{2}} e^{2 a b x}}{\sqrt{\pi} b} - \frac{3 c^{2} d x e^{a^{2}} e^{b^{2} x^{2}} e^{2 a b x}}{2 \sqrt{\pi} b} - \frac{c d^{2} x^{2} e^{a^{2}} e^{b^{2} x^{2}} e^{2 a b x}}{\sqrt{\pi} b} - \frac{d^{3} x^{3} e^{a^{2}} e^{b^{2} x^{2}} e^{2 a b x}}{4 \sqrt{\pi} b} + \frac{3 c^{2} d \operatorname{erfi}{\left(a + b x \right)}}{4 b^{2}} + \frac{c d^{2} e^{a^{2}} e^{b^{2} x^{2}} e^{2 a b x}}{\sqrt{\pi} b^{3}} + \frac{3 d^{3} x e^{a^{2}} e^{b^{2} x^{2}} e^{2 a b x}}{8 \sqrt{\pi} b^{3}} - \frac{3 d^{3} \operatorname{erfi}{\left(a + b x \right)}}{16 b^{4}} & \text{for}\: b \neq 0 \\\left(c^{3} x + \frac{3 c^{2} d x^{2}}{2} + c d^{2} x^{3} + \frac{d^{3} x^{4}}{4}\right) \operatorname{erfi}{\left(a \right)} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**3*erfi(b*x+a),x)
```

```
[Out] Piecewise((-a**4*d**3*erfi(a + b*x)/(4*b**4) + a**3*c*d**2*erfi(a + b*x)/b*
*3 + a**3*d**3*exp(a**2)*exp(b**2*x**2)*exp(2*a*b*x)/(4*sqrt(pi)*b**4) - 3*
a**2*c**2*d*erfi(a + b*x)/(2*b**2) - a**2*c*d**2*exp(a**2)*exp(b**2*x**2)*e
xp(2*a*b*x)/(sqrt(pi)*b**3) - a**2*d**3*x*exp(a**2)*exp(b**2*x**2)*exp(2*a*
b*x)/(4*sqrt(pi)*b**3) + 3*a**2*d**3*erfi(a + b*x)/(4*b**4) + a*c**3*erfi(a
 + b*x)/b + 3*a*c**2*d*exp(a**2)*exp(b**2*x**2)*exp(2*a*b*x)/(2*sqrt(pi)*b*
*2) + a*c*d**2*x*exp(a**2)*exp(b**2*x**2)*exp(2*a*b*x)/(sqrt(pi)*b**2) + a*
d**3*x**2*exp(a**2)*exp(b**2*x**2)*exp(2*a*b*x)/(4*sqrt(pi)*b**2) - 3*a*c*d
**2*erfi(a + b*x)/(2*b**3) - 5*a*d**3*exp(a**2)*exp(b**2*x**2)*exp(2*a*b*x)
/(8*sqrt(pi)*b**4) + c**3*x*erfi(a + b*x) + 3*c**2*d*x**2*erfi(a + b*x)/2 +
 c*d**2*x**3*erfi(a + b*x) + d**3*x**4*erfi(a + b*x)/4 - c**3*exp(a**2)*exp
(b**2*x**2)*exp(2*a*b*x)/(sqrt(pi)*b) - 3*c**2*d*x*exp(a**2)*exp(b**2*x**2)
*exp(2*a*b*x)/(2*sqrt(pi)*b) - c*d**2*x**2*exp(a**2)*exp(b**2*x**2)*exp(2*a
*b*x)/(sqrt(pi)*b) - d**3*x**3*exp(a**2)*exp(b**2*x**2)*exp(2*a*b*x)/(4*sqr
t(pi)*b) + 3*c**2*d*erfi(a + b*x)/(4*b**2) + c*d**2*exp(a**2)*exp(b**2*x**2
)*exp(2*a*b*x)/(sqrt(pi)*b**3) + 3*d**3*x*exp(a**2)*exp(b**2*x**2)*exp(2*a*
b*x)/(8*sqrt(pi)*b**3) - 3*d**3*erfi(a + b*x)/(16*b**4), Ne(b, 0)), ((c**3*
x + 3*c**2*d*x**2/2 + c*d**2*x**3 + d**3*x**4/4)*erfi(a), True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^3*erfi(b*x+a),x, algorithm="giac")
```

```
[Out] integrate((d*x + c)^3*erfi(b*x + a), x)
```

Mupad [B]
time = 0.64, size = 357, normalized size = 1.28

$$\mathrm{erfi}(a+b\,x)\,\left(c^3\,x+\frac{3\,c^2\,d\,x^2}{2}+c\,d^2\,x^3+\frac{d^3\,x^4}{4}\right)-\frac{\frac{{\mathrm{e}}^{a^2+2\,a\,b\,x+b^2\,x^2}\,\left(-2\,a^3\,d^3+8\,a^2\,b\,c\,d^2-12\,a\,b^2\,c^2\,d+5\,a\,d^3+8\,b^3\,c^3-8\,b\,c\,d^2\right)}{4\,b^4}+\frac{d^3\,x^3\,{\mathrm{e}}^{a^2+2\,a\,b\,x+b^2\,x^2}}{2\,b}-\frac{x^2\,{\mathrm{e}}^{a^2+2\,a\,b\,x+b^2\,x^2}\,\left(a\,d^3-4\,b\,c\,d^2\right)}{2\,b^2}-\frac{x\,{\mathrm{e}}^{a^2+2\,a\,b\,x+b^2\,x^2}\,\left(b^2\,\left(12\,c^2\,d-72\,a^2\,c^2\,d\right)+b\,\left(48\,a^3\,c\,d^2-8\,a\,c\,d^2\right)-3\,d^3+20\,a^2\,d^3-12\,a^4\,d^3\right)}{b^3\,\left(24\,a^2-4\right)}}{2\,\sqrt{\pi}}-\frac{\mathrm{erfi}(a+b\,x)\,\left(4\,a^4\,d^3-16\,a^3\,b\,c\,d^2+24\,a^2\,b^2\,c^2\,d-12\,a^2\,d^3-16\,a\,b^3\,c^3+24\,a\,b\,c\,d^2-12\,b^2\,c^2\,d+3\,d^3\right)}{16\,b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(a + b*x)*(c + d*x)^3,x)
```

```
[Out] erfi(a + b*x)*(c^3*x + (d^3*x^4)/4 + (3*c^2*d*x^2)/2 + c*d^2*x^3) - ((exp(a
^2 + b^2*x^2 + 2*a*b*x)*(5*a*d^3 - 2*a^3*d^3 + 8*b^3*c^3 - 8*b*c*d^2 - 12*a
*b^2*c^2*d + 8*a^2*b*c*d^2))/(4*b^4) + (d^3*x^3*exp(a^2 + b^2*x^2 + 2*a*b*x
))/(2*b) - (x^2*exp(a^2 + b^2*x^2 + 2*a*b*x)*(a*d^3 - 4*b*c*d^2))/(2*b^2) -
 (x*exp(a^2 + b^2*x^2 + 2*a*b*x)*(b^2*(12*c^2*d - 72*a^2*c^2*d) + b*(48*a^3
*c*d^2 - 8*a*c*d^2) - 3*d^3 + 20*a^2*d^3 - 12*a^4*d^3))/(b^3*(24*a^2 - 4)))
/(2*pi^(1/2)) - (erfi(a + b*x)*(3*d^3 - 12*a^2*d^3 + 4*a^4*d^3 - 16*a*b^3*c
^3 - 12*b^2*c^2*d + 24*a^2*b^2*c^2*d + 24*a*b*c*d^2 - 16*a^3*b*c*d^2))/(16*
b^4)
```

3.222 $\int (c+dx)^2 \mathbf{Erfi}(a+bx)\,dx$

Optimal. Leaf size=186

$$\frac{d^2e^{(a+bx)^2}}{3b^3\sqrt{\pi}}-\frac{(bc-ad)^2e^{(a+bx)^2}}{b^3\sqrt{\pi}}-\frac{d(bc-ad)e^{(a+bx)^2}(a+bx)}{b^3\sqrt{\pi}}-\frac{d^2e^{(a+bx)^2}(a+bx)^2}{3b^3\sqrt{\pi}}+\frac{d(bc-ad)\mathrm{Erfi}(a+bx)}{2b^3}-(bc$$

```
[Out] 1/2*d*(-a*d+b*c)*erfi(b*x+a)/b^3-1/3*(-a*d+b*c)^3*erfi(b*x+a)/b^3/d+1/3*(d*
x+c)^3*erfi(b*x+a)/d+1/3*d^2*exp((b*x+a)^2)/b^3/Pi^(1/2)-(-a*d+b*c)^2*exp((
b*x+a)^2)/b^3/Pi^(1/2)-d*(-a*d+b*c)*exp((b*x+a)^2)*(b*x+a)/b^3/Pi^(1/2)-1/3
*d^2*exp((b*x+a)^2)*(b*x+a)^2/b^3/Pi^(1/2)
```

Rubi [A]
time = 0.12, antiderivative size = 186, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 5, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.357$, Rules used = {6498, 2258, 2235, 2240, 2243}

$$-\frac{(bc-ad)^3\mathrm{Erfi}(a+bx)}{3b^3d}+\frac{d(bc-ad)\mathrm{Erfi}(a+bx)}{2b^3}-\frac{e^{(a+bx)^2}(bc-ad)^2}{\sqrt{\pi}\,b^3}-\frac{de^{(a+bx)^2}(a+bx)(bc-ad)}{\sqrt{\pi}\,b^3}-\frac{d^2e^{(a+bx)^2}(a+bx)^2}{3\sqrt{\pi}\,b^3}+\frac{d^2e^{(a+bx)^2}}{3\sqrt{\pi}\,b^3}+\frac{(c+dx)^3\mathrm{Erfi}(a+bx)}{3d}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)^2*Erfi[a + b*x],x]
```

```
[Out] (d^2*E^(a + b*x)^2)/(3*b^3*Sqrt[Pi]) - ((b*c - a*d)^2*E^(a + b*x)^2)/(b^3*S
qrt[Pi]) - (d*(b*c - a*d)*E^(a + b*x)^2*(a + b*x))/(b^3*Sqrt[Pi]) - (d^2*E^
(a + b*x)^2*(a + b*x)^2)/(3*b^3*Sqrt[Pi]) + (d*(b*c - a*d)*Erfi[a + b*x])/(
2*b^3) - ((b*c - a*d)^3*Erfi[a + b*x])/(3*b^3*d) + ((c + d*x)^3*Erfi[a + b*
x])/(3*d)
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
```

```
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 2258

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*(u_), x_Symbol] :> Int[E
xpandLinearProduct[F^(a + b*(c + d*x)^n), u, c, d, x], x] /; FreeQ[{F, a, b
, c, d, n}, x] && PolynomialQ[u, x]
```

Rule 6498

```
Int[Erfi[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfi[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)*E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$\int (c+dx)^2\mathrm{erfi}(a+bx)\,dx = \frac{(c+dx)^3\mathrm{erfi}(a+bx)}{3d} - \frac{(2b)\int e^{(a+bx)^2}(c+dx)^3\,dx}{3d\sqrt{\pi}}$$

$$= \frac{(c+dx)^3\mathrm{erfi}(a+bx)}{3d} - \frac{(2b)\int\left(\frac{(bc-ad)^3e^{(a+bx)^2}}{b^3} + \frac{3d(bc-ad)^2e^{(a+bx)^2}(a+bx)}{b^3} + \frac{3d^2(bc-}{}\right.}{3d\sqrt{\pi}}$$

$$= \frac{(c+dx)^3\mathrm{erfi}(a+bx)}{3d} - \frac{(2d^2)\int e^{(a+bx)^2}(a+bx)^3\,dx}{3b^2\sqrt{\pi}} - \frac{(2d(bc-ad))\int e^{(a+bx)^2}}{b^2\sqrt{\pi}}$$

$$= -\frac{(bc-ad)^2e^{(a+bx)^2}}{b^3\sqrt{\pi}} - \frac{d(bc-ad)e^{(a+bx)^2}(a+bx)}{b^3\sqrt{\pi}} - \frac{d^2e^{(a+bx)^2}(a+bx)^2}{3b^3\sqrt{\pi}} - \frac{(bc}{}$$

$$= \frac{d^2e^{(a+bx)^2}}{3b^3\sqrt{\pi}} - \frac{(bc-ad)^2e^{(a+bx)^2}}{b^3\sqrt{\pi}} - \frac{d(bc-ad)e^{(a+bx)^2}(a+bx)}{b^3\sqrt{\pi}} - \frac{d^2e^{(a+bx)^2}(a+}{3b^3\sqrt{\pi}}$$

Mathematica [A]
time = 0.11, size = 142, normalized size = 0.76

$$\frac{-2e^{(a+bx)^2}\left((-1+a^2)\,d^2-abd(3c+dx)+b^2(3c^2+3cdx+d^2x^2)\right)+\sqrt{\pi}\,(3bcd-6a^2bcd+2a^3d^2+a(6b^2c^2-3d^2)+2b^3x(3c^2+3cdx+d^2x^2))\,\mathrm{Erfi}(a+bx)}{6b^3\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)^2*Erfi[a + b*x],x]
```

```
[Out] (-2*E^(a + b*x)^2*((-1 + a^2)*d^2 - a*b*d*(3*c + d*x) + b^2*(3*c^2 + 3*c*d*
x + d^2*x^2)) + Sqrt[Pi]*(3*b*c*d - 6*a^2*b*c*d + 2*a^3*d^2 + a*(6*b^2*c^2
```

```
- 3*d^2) + 2*b^3*x*(3*c^2 + 3*c*d*x + d^2*x^2))*Erfi[a + b*x])/(6*b^3*Sqrt[
Pi])
```

Maple [B] Leaf count of result is larger than twice the leaf count of optimal. 414 vs. $2(164) = 328$.
time = 0.86, size = 415, normalized size = 2.23

method	result
derivativedivides	$\frac{-\frac{d^2 \operatorname{erfi}(bx+a)a^3}{3b^2}+\frac{d \operatorname{erfi}(bx+a)a^2 c}{b}+\frac{d^2 \operatorname{erfi}(bx+a)a^2(bx+a)}{b^2}-\operatorname{erfi}(bx+a)a\,c^2-\frac{2d \operatorname{erfi}(bx+a)ac(bx+a)}{b}-\frac{d^2 \operatorname{erfi}(bx+a)a(bx+a)^2}{b^2}+b}{}$
default	$\frac{-\frac{d^2 \operatorname{erfi}(bx+a)a^3}{3b^2}+\frac{d \operatorname{erfi}(bx+a)a^2 c}{b}+\frac{d^2 \operatorname{erfi}(bx+a)a^2(bx+a)}{b^2}-\operatorname{erfi}(bx+a)a\,c^2-\frac{2d \operatorname{erfi}(bx+a)ac(bx+a)}{b}-\frac{d^2 \operatorname{erfi}(bx+a)a(bx+a)^2}{b^2}+b}{}$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^2*erfi(b*x+a),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*(-1/3/b^2*d^2*erfi(b*x+a)*a^3+1/b*d*erfi(b*x+a)*a^2*c+1/b^2*d^2*erfi(b*
x+a)*a^2*(b*x+a)-erfi(b*x+a)*a*c^2-2/b*d*erfi(b*x+a)*a*c*(b*x+a)-1/b^2*d^2*
erfi(b*x+a)*a*(b*x+a)^2+1/3*b/d*erfi(b*x+a)*c^3+erfi(b*x+a)*c^2*(b*x+a)+1/b
*d*erfi(b*x+a)*c*(b*x+a)^2+1/3/b^2*d^2*erfi(b*x+a)*(b*x+a)^3+2/3/b^2/d/Pi^(
1/2)*(1/2*a^3*d^3*Pi^(1/2)*erfi(b*x+a)-1/2*b^3*c^3*Pi^(1/2)*erfi(b*x+a)-d^3
*(1/2*exp((b*x+a)^2)*(b*x+a)^2-1/2*exp((b*x+a)^2))+3*a*d^3*(1/2*(b*x+a)*exp
((b*x+a)^2)-1/4*Pi^(1/2)*erfi(b*x+a))-3/2*a^2*d^3*exp((b*x+a)^2)+3/2*a*b^2*
c^2*d*Pi^(1/2)*erfi(b*x+a)-3/2*a^2*b*c*d^2*Pi^(1/2)*erfi(b*x+a)-3*b*c*d^2*(
1/2*(b*x+a)*exp((b*x+a)^2)-1/4*Pi^(1/2)*erfi(b*x+a))-3/2*b^2*c^2*d*exp((b*x
+a)^2)+3*a*b*c*d^2*exp((b*x+a)^2)))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erfi(b*x+a),x, algorithm="maxima")
```

```
[Out] integrate((d*x + c)^2*erfi(b*x + a), x)
```

Fricas [A]
time = 0.37, size = 161, normalized size = 0.87

$$-\frac{2\sqrt{\pi}\,(b^2d^2x^2+3\,b^2c^2-3\,abcd+(a^2-1)d^2+(3\,b^2cd-abd^2)x)e^{(b^2x^2+2\,abx+a^2)}-(2\,\pi b^3d^2x^3+6\,\pi b^3cdx^2+6\,\pi b^3c^2x+\pi(6\,ab^2c^2-3\,(2\,a^2-1)bcd+(2\,a^3-3\,a)d^2))\operatorname{erfi}(bx+a)}{6\,\pi b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erfi(b*x+a),x, algorithm="fricas")
```

```
[Out] -1/6*(2*sqrt(pi)*(b^2*d^2*x^2 + 3*b^2*c^2 - 3*a*b*c*d + (a^2 - 1)*d^2 + (3*
b^2*c*d - a*b*d^2)*x)*e^(b^2*x^2 + 2*a*b*x + a^2) - (2*pi*b^3*d^2*x^3 + 6*p
i*b^3*c*d*x^2 + 6*pi*b^3*c^2*x + pi*(6*a*b^2*c^2 - 3*(2*a^2 - 1)*b*c*d + (2
*a^3 - 3*a)*d^2))*erfi(b*x + a))/(pi*b^3)
```

Sympy [B] Leaf count of result is larger than twice the leaf count of optimal. 398 vs. $2(165) = 330$.
time = 0.90, size = 398, normalized size = 2.14

$$\begin{cases} \frac{a^3d^2 \operatorname{erfi}(a+bx)}{3b^3} - \frac{a^2cd \operatorname{erfi}(a+bx)}{b^2} - \frac{a^2d^2e^{a^2}e^{b^2x^2}e^{2abx}}{3\sqrt{\pi}\,b^3} + \frac{ac^2 \operatorname{erfi}(a+bx)}{b} + \frac{acde^{a^2}e^{b^2x^2}e^{2abx}}{\sqrt{\pi}\,b^2} + \frac{ad^2xe^{a^2}e^{b^2x^2}e^{2abx}}{3\sqrt{\pi}\,b^2} - \frac{ad^2 \operatorname{erfi}(a+bx)}{2b^3} + c^2x \operatorname{erfi}(a+bx) + cdx^2 \operatorname{erfi}(a+bx) + \frac{d^2x^3 \operatorname{erfi}(a+bx)}{3} - \frac{c^2e^{a^2}e^{b^2x^2}e^{2abx}}{\sqrt{\pi}\,b} - \frac{cdxe^{a^2}e^{b^2x^2}e^{2abx}}{\sqrt{\pi}\,b} - \frac{d^2x^2e^{a^2}e^{b^2x^2}e^{2abx}}{3\sqrt{\pi}\,b} + \frac{cd \operatorname{erfi}(a+bx)}{2b^2} + \frac{d^2e^{a^2}e^{b^2x^2}e^{2abx}}{3\sqrt{\pi}\,b^3} & \text{for}\ b \neq 0 \\ \left(c^2x + cdx^2 + \frac{d^2x^3}{3}\right) \operatorname{erfi}(a) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**2*erfi(b*x+a),x)
```

```
[Out] Piecewise((a**3*d**2*erfi(a + b*x)/(3*b**3) - a**2*c*d*erfi(a + b*x)/b**2 -
 a**2*d**2*exp(a**2)*exp(b**2*x**2)*exp(2*a*b*x)/(3*sqrt(pi)*b**3) + a*c**2
*erfi(a + b*x)/b + a*c*d*exp(a**2)*exp(b**2*x**2)*exp(2*a*b*x)/(sqrt(pi)*b*
*2) + a*d**2*x*exp(a**2)*exp(b**2*x**2)*exp(2*a*b*x)/(3*sqrt(pi)*b**2) - a*
d**2*erfi(a + b*x)/(2*b**3) + c**2*x*erfi(a + b*x) + c*d*x**2*erfi(a + b*x)
 + d**2*x**3*erfi(a + b*x)/3 - c**2*exp(a**2)*exp(b**2*x**2)*exp(2*a*b*x)/(
sqrt(pi)*b) - c*d*x*exp(a**2)*exp(b**2*x**2)*exp(2*a*b*x)/(sqrt(pi)*b) - d*
*2*x**2*exp(a**2)*exp(b**2*x**2)*exp(2*a*b*x)/(3*sqrt(pi)*b) + c*d*erfi(a +
 b*x)/(2*b**2) + d**2*exp(a**2)*exp(b**2*x**2)*exp(2*a*b*x)/(3*sqrt(pi)*b**
3), Ne(b, 0)), ((c**2*x + c*d*x**2 + d**2*x**3/3)*erfi(a), True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erfi(b*x+a),x, algorithm="giac")
```

```
[Out] integrate((d*x + c)^2*erfi(b*x + a), x)
```

Mupad [B]
time = 0.37, size = 190, normalized size = 1.02

$$\frac{\frac{e^{a^2+2\,a\,b\,x+b^2\,x^2}\,\left(-a^2\,d^2+3\,a\,b\,c\,d-3\,b^2\,c^2+d^2\right)}{b^3}+\frac{x\,e^{a^2+2\,a\,b\,x+b^2\,x^2}\,\left(a\,d^2-3\,b\,c\,d\right)}{b^2}-\frac{d^2\,x^2\,e^{a^2+2\,a\,b\,x+b^2\,x^2}}{b}}{3\,\sqrt{\pi}}+\operatorname{erfi}(a+b\,x)\,\left(c^2\,x+c\,d\,x^2+\frac{d^2\,x^3}{3}\right)+\frac{\operatorname{erfi}(a+b\,x)\,\left(2\,a^3\,d^2-6\,a^2\,b\,c\,d+6\,a\,b^2\,c^2-3\,a\,d^2+3\,b\,c\,d\right)}{6\,b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(a + b*x)*(c + d*x)^2,x)
```

```
[Out] ((exp(a^2 + b^2*x^2 + 2*a*b*x)*(d^2 - a^2*d^2 - 3*b^2*c^2 + 3*a*b*c*d))/b^3
 + (x*exp(a^2 + b^2*x^2 + 2*a*b*x)*(a*d^2 - 3*b*c*d))/b^2 - (d^2*x^2*exp(a^
2 + b^2*x^2 + 2*a*b*x))/b)/(3*pi^(1/2)) + erfi(a + b*x)*(c^2*x + (d^2*x^3)/
3 + c*d*x^2) + (erfi(a + b*x)*(2*a^3*d^2 - 3*a*d^2 + 6*a*b^2*c^2 + 3*b*c*d
- 6*a^2*b*c*d))/(6*b^3)
```

3.223 $\int (c+dx)\mathbf{Erfi}(a+bx)\,dx$

Optimal. Leaf size=115

$$-\frac{(bc-ad)e^{(a+bx)^2}}{b^2\sqrt{\pi}}-\frac{de^{(a+bx)^2}(a+bx)}{2b^2\sqrt{\pi}}+\frac{d\text{Erfi}(a+bx)}{4b^2}-\frac{(bc-ad)^2\text{Erfi}(a+bx)}{2b^2d}+\frac{(c+dx)^2\text{Erfi}(a+bx)}{2d}$$

```
[Out] 1/4*d*erfi(b*x+a)/b^2-1/2*(-a*d+b*c)^2*erfi(b*x+a)/b^2/d+1/2*(d*x+c)^2*erfi
(b*x+a)/d-(-a*d+b*c)*exp((b*x+a)^2)/b^2/Pi^(1/2)-1/2*d*exp((b*x+a)^2)*(b*x+
a)/b^2/Pi^(1/2)
```

Rubi [A]
time = 0.07, antiderivative size = 115, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.417$, Rules used = {6498, 2258, 2235, 2240, 2243}

$$-\frac{(bc-ad)^2\text{Erfi}(a+bx)}{2b^2d}-\frac{e^{(a+bx)^2}(bc-ad)}{\sqrt{\pi}b^2}+\frac{d\text{Erfi}(a+bx)}{4b^2}-\frac{de^{(a+bx)^2}(a+bx)}{2\sqrt{\pi}b^2}+\frac{(c+dx)^2\text{Erfi}(a+bx)}{2d}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)*Erfi[a + b*x],x]
```

```
[Out] -(((b*c - a*d)*E^(a + b*x)^2)/(b^2*Sqrt[Pi])) - (d*E^(a + b*x)^2*(a + b*x))
/(2*b^2*Sqrt[Pi]) + (d*Erfi[a + b*x])/(4*b^2) - ((b*c - a*d)^2*Erfi[a + b*x
])/(2*b^2*d) + ((c + d*x)^2*Erfi[a + b*x])/(2*d)
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
```

```
0])
```

Rule 2258

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*(u_), x_Symbol] :> Int[E
xpandLinearProduct[F^(a + b*(c + d*x)^n), u, c, d, x], x] /; FreeQ[{F, a, b
, c, d, n}, x] && PolynomialQ[u, x]
```

Rule 6498

```
Int[Erfi[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[
(c + d*x)^(m + 1)*(Erfi[a + b*x]/(d*(m + 1))), x] - Dist[2*(b/(Sqrt[Pi]*d*(
m + 1))), Int[(c + d*x)^(m + 1)*E^(a + b*x)^2, x], x] /; FreeQ[{a, b, c, d,
 m}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int (c+dx)\text{erfi}(a+bx)\,dx &= \frac{(c+dx)^2\text{erfi}(a+bx)}{2d} - \frac{b\int e^{(a+bx)^2}(c+dx)^2\,dx}{d\sqrt{\pi}} \\
&= \frac{(c+dx)^2\text{erfi}(a+bx)}{2d} - \frac{b\int \left(\frac{(bc-ad)^2e^{(a+bx)^2}}{b^2} + \frac{2d(bc-ad)e^{(a+bx)^2}(a+bx)}{b^2} + \frac{d^2e^{(a+bx)^2}(a+b}{b^2}\right.}{d\sqrt{\pi}} \\
&= \frac{(c+dx)^2\text{erfi}(a+bx)}{2d} - \frac{d\int e^{(a+bx)^2}(a+bx)^2\,dx}{b\sqrt{\pi}} - \frac{(2(bc-ad))\int e^{(a+bx)^2}(a+bx}{b\sqrt{\pi}} \\
&= -\frac{(bc-ad)e^{(a+bx)^2}}{b^2\sqrt{\pi}} - \frac{de^{(a+bx)^2}(a+bx)}{2b^2\sqrt{\pi}} - \frac{(bc-ad)^2\text{erfi}(a+bx)}{2b^2d} + \frac{(c+dx)^2\text{erfi}}{2d} \\
&= -\frac{(bc-ad)e^{(a+bx)^2}}{b^2\sqrt{\pi}} - \frac{de^{(a+bx)^2}(a+bx)}{2b^2\sqrt{\pi}} + \frac{d\text{erfi}(a+bx)}{4b^2} - \frac{(bc-ad)^2\text{erfi}(a+bx)}{2b^2d}
\end{aligned}
$$

Mathematica [A]
time = 0.06, size = 78, normalized size = 0.68

$$
\frac{-2e^{(a+bx)^2}(2bc-ad+bdx)+\sqrt{\pi}\,(4abc+d-2a^2d+4b^2cx+2b^2dx^2)\,\text{Erfi}(a+bx)}{4b^2\sqrt{\pi}}
$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)*Erfi[a + b*x],x]
```

```
[Out] (-2*E^(a + b*x)^2*(2*b*c - a*d + b*d*x) + Sqrt[Pi]*(4*a*b*c + d - 2*a^2*d +
 4*b^2*c*x + 2*b^2*d*x^2)*Erfi[a + b*x])/(4*b^2*Sqrt[Pi])
```

Maple [A]
time = 0.35, size = 117, normalized size = 1.02

method	result
derivativedivides	$\frac{-\frac{\mathrm{erfi}(bx+a)da(bx+a)}{b}+\mathrm{erfi}(bx+a)c(bx+a)+\frac{\mathrm{erfi}(bx+a)d(bx+a)^2}{2b}+\frac{-d\left(\frac{(bx+a)e^{(bx+a)^2}}{2}-\frac{\sqrt{\pi}\,\mathrm{erfi}(bx+a)}{4}\right)-e^{(bx+a)^2}bc+da}{b\sqrt{\pi}}}{b}$
default	$\frac{-\frac{\mathrm{erfi}(bx+a)da(bx+a)}{b}+\mathrm{erfi}(bx+a)c(bx+a)+\frac{\mathrm{erfi}(bx+a)d(bx+a)^2}{2b}+\frac{-d\left(\frac{(bx+a)e^{(bx+a)^2}}{2}-\frac{\sqrt{\pi}\,\mathrm{erfi}(bx+a)}{4}\right)-e^{(bx+a)^2}bc+da}{b\sqrt{\pi}}}{b}$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)*erfi(b*x+a),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*(-1/b*erfi(b*x+a)*d*a*(b*x+a)+erfi(b*x+a)*c*(b*x+a)+1/2/b*erfi(b*x+a)*d
*(b*x+a)^2+1/b/Pi^(1/2)*(-d*(1/2*(b*x+a)*exp((b*x+a)^2)-1/4*Pi^(1/2)*erfi(b
*x+a))-exp((b*x+a)^2)*b*c+d*a*exp((b*x+a)^2)))
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfi(b*x+a),x, algorithm="maxima")
```

```
[Out] integrate((d*x + c)*erfi(b*x + a), x)
```

Fricas [A]
time = 0.37, size = 89, normalized size = 0.77

$$-\frac{2\sqrt{\pi}\,(bdx+2\,bc-ad)e^{\left(b^2x^2+2\,abx+a^2\right)}-\left(2\,\pi b^2dx^2+4\,\pi b^2cx+\pi(4\,abc-(2\,a^2-1)d)\right)\mathrm{erfi}\,(bx+a)}{4\,\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfi(b*x+a),x, algorithm="fricas")
```

```
[Out] -1/4*(2*sqrt(pi)*(b*d*x + 2*b*c - a*d)*e^(b^2*x^2 + 2*a*b*x + a^2) - (2*pi*
b^2*d*x^2 + 4*pi*b^2*c*x + pi*(4*a*b*c - (2*a^2 - 1)*d))*erfi(b*x + a))/(pi
*b^2)
```

Sympy [A]
time = 0.38, size = 178, normalized size = 1.55

$$\begin{cases} -\frac{a^2d\,\mathrm{erfi}\,(a+bx)}{2b^2}+\frac{ac\,\mathrm{erfi}\,(a+bx)}{b}+\frac{ade^{a^2}e^{b^2x^2}e^{2abx}}{2\sqrt{\pi}\,b^2}+cx\,\mathrm{erfi}\,(a+bx)+\frac{dx^2\,\mathrm{erfi}\,(a+bx)}{2}-\frac{ce^{a^2}e^{b^2x^2}e^{2abx}}{\sqrt{\pi}\,b}-\frac{dxe^{a^2}e^{b^2x^2}e^{2abx}}{2\sqrt{\pi}\,b}+\frac{d\,\mathrm{erfi}\,(a+bx)}{4b^2} & \text{for}\ b\neq 0 \\ \left(cx+\frac{dx^2}{2}\right)\mathrm{erfi}\,(a) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfi(b*x+a),x)
```

```
[Out] Piecewise((-a**2*d*erfi(a + b*x)/(2*b**2) + a*c*erfi(a + b*x)/b + a*d*exp(a
**2)*exp(b**2*x**2)*exp(2*a*b*x)/(2*sqrt(pi)*b**2) + c*x*erfi(a + b*x) + d*
x**2*erfi(a + b*x)/2 - c*exp(a**2)*exp(b**2*x**2)*exp(2*a*b*x)/(sqrt(pi)*b)
 - d*x*exp(a**2)*exp(b**2*x**2)*exp(2*a*b*x)/(2*sqrt(pi)*b) + d*erfi(a + b*
x)/(4*b**2), Ne(b, 0)), ((c*x + d*x**2/2)*erfi(a), True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfi(b*x+a),x, algorithm="giac")
```

```
[Out] integrate((d*x + c)*erfi(b*x + a), x)
```

Mupad [B]
time = 0.33, size = 106, normalized size = 0.92

$$\frac{\frac{e^{a^2+2\,a\,b\,x+b^2\,x^2}\,\left(\frac{a\,d}{2}-b\,c\right)}{b^2}-\frac{d\,x\,e^{a^2+2\,a\,b\,x+b^2\,x^2}}{2\,b}}{\sqrt{\pi}}+\mathrm{erfi}(a+b\,x)\,\left(\frac{d\,x^2}{2}+c\,x\right)+\frac{\mathrm{erfi}(a+b\,x)\,\left(-2\,d\,a^2\,b+4\,c\,a\,b^2+d\,b\right)}{4\,b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(a + b*x)*(c + d*x),x)
```

```
[Out] ((exp(a^2 + b^2*x^2 + 2*a*b*x)*((a*d)/2 - b*c))/b^2 - (d*x*exp(a^2 + b^2*x^
2 + 2*a*b*x))/(2*b))/pi^(1/2) + erfi(a + b*x)*(c*x + (d*x^2)/2) + (erfi(a +
 b*x)*(b*d + 4*a*b^2*c - 2*a^2*b*d))/(4*b^3)
```

3.224 $\int \mathbf{Erfi}(a+bx)\,dx$

Optimal. Leaf size=35

$$-\frac{e^{(a+bx)^2}}{b\sqrt{\pi}}+\frac{(a+bx)\text{Erfi}(a+bx)}{b}$$

```
[Out] (b*x+a)*erfi(b*x+a)/b-exp((b*x+a)^2)/b/Pi^(1/2)
```

Rubi [A]
time = 0.00, antiderivative size = 35, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.167, Rules used = {6486}

$$\frac{(a+bx)\text{Erfi}(a+bx)}{b}-\frac{e^{(a+bx)^2}}{\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[a + b*x],x]
[Out] -(E^(a + b*x)^2/(b*Sqrt[Pi])) + ((a + b*x)*Erfi[a + b*x])/b
```

Rule 6486

```
Int[Erfi[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[(a + b*x)*(Erfi[a + b*x]/b)
, x] - Simp[E^(a + b*x)^2/(b*Sqrt[Pi]), x] /; FreeQ[{a, b}, x]
```

Rubi steps

$$\int \text{erfi}(a+bx)\,dx=-\frac{e^{(a+bx)^2}}{b\sqrt{\pi}}+\frac{(a+bx)\text{erfi}(a+bx)}{b}$$

Mathematica [A]
time = 0.02, size = 33, normalized size = 0.94

$$\frac{-\frac{e^{(a+bx)^2}}{\sqrt{\pi}}+(a+bx)\text{Erfi}(a+bx)}{b}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[a + b*x],x]
[Out] (-(E^(a + b*x)^2/Sqrt[Pi]) + (a + b*x)*Erfi[a + b*x])/b
```

Maple [A]
time = 0.23, size = 31, normalized size = 0.89

method	result	size
derivativedivides	$\frac{(bx+a)\,\mathrm{erfi}(bx+a)-\frac{\mathrm{e}^{(bx+a)^2}}{\sqrt{\pi}}}{b}$	31
default	$\frac{(bx+a)\,\mathrm{erfi}(bx+a)-\frac{\mathrm{e}^{(bx+a)^2}}{\sqrt{\pi}}}{b}$	31

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x+a),x,method=_RETURNVERBOSE)
```

```
[Out] 1/b*((b*x+a)*erfi(b*x+a)-1/Pi^(1/2)*exp((b*x+a)^2))
```

Maxima [A]
time = 0.26, size = 30, normalized size = 0.86

$$\frac{(bx+a)\,\mathrm{erfi}\,(bx+a)-\frac{e^{\left((bx+a)^2\right)}}{\sqrt{\pi}}}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a),x, algorithm="maxima")
```

```
[Out] ((b*x + a)*erfi(b*x + a) - e^((b*x + a)^2)/sqrt(pi))/b
```

Fricas [A]
time = 0.37, size = 45, normalized size = 1.29

$$\frac{(\pi bx+\pi a)\,\mathrm{erfi}\,(bx+a)-\sqrt{\pi}\,e^{\left(b^2x^2+2\,abx+a^2\right)}}{\pi b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a),x, algorithm="fricas")
```

```
[Out] ((pi*b*x + pi*a)*erfi(b*x + a) - sqrt(pi)*e^(b^2*x^2 + 2*a*b*x + a^2))/(pi*
b)
```

Sympy [A]
time = 0.14, size = 51, normalized size = 1.46

$$\begin{cases} \frac{a\,\mathrm{erfi}\,(a+bx)}{b}+x\,\mathrm{erfi}\,(a+bx)-\frac{e^{a^2}e^{b^2x^2}e^{2abx}}{\sqrt{\pi}\,b} & \text{for}\ b\neq 0 \\ x\,\mathrm{erfi}\,(a) & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a),x)
```

```
[Out] Piecewise((a*erfi(a + b*x)/b + x*erfi(a + b*x) - exp(a**2)*exp(b**2*x**2)*e
xp(2*a*b*x)/(sqrt(pi)*b), Ne(b, 0)), (x*erfi(a), True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a),x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x + a), x)
```

Mupad [B]
time = 0.14, size = 46, normalized size = 1.31

$$x\,\mathrm{erfi}(a+b\,x)+\frac{a\,\mathrm{erfi}(a+b\,x)}{b}-\frac{\mathrm{e}^{a^2}\,\mathrm{e}^{b^2\,x^2}\,\mathrm{e}^{2\,a\,b\,x}}{b\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(a + b*x),x)
```

```
[Out] x*erfi(a + b*x) + (a*erfi(a + b*x))/b - (exp(a^2)*exp(b^2*x^2)*exp(2*a*b*x)
)/(b*pi^(1/2))
```

3.225 $\int \frac{\mathbf{Erfi}(a+bx)}{c+dx} \, dx$

Optimal. Leaf size=17

$$\text{Int}\left(\frac{\text{Erfi}(a+bx)}{c+dx},x\right)$$

```
[Out] Unintegrable(erfi(b*x+a)/(d*x+c),x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\text{Erfi}(a+bx)}{c+dx} \, dx$$

Verification is not applicable to the result.

```
[In] Int[Erfi[a + b*x]/(c + d*x),x]
[Out] Defer[Int][Erfi[a + b*x]/(c + d*x), x]
```

Rubi steps

$$\int \frac{\text{erfi}(a+bx)}{c+dx} \, dx = \int \frac{\text{erfi}(a+bx)}{c+dx} \, dx$$

Mathematica [A]
time = 0.76, size = 0, normalized size = 0.00

$$\int \frac{\text{Erfi}(a+bx)}{c+dx} \, dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfi[a + b*x]/(c + d*x),x]
[Out] Integrate[Erfi[a + b*x]/(c + d*x), x]
```

Maple [A]
time = 0.15, size = 0, normalized size = 0.00

$$\int \frac{\text{erfi}\,(bx+a)}{dx+c} \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x+a)/(d*x+c),x)
```

```
[Out] int(erfi(b*x+a)/(d*x+c),x)
```

Maxima [**A**]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)/(d*x+c),x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x + a)/(d*x + c), x)
```

Fricas [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)/(d*x+c),x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x + a)/(d*x + c), x)
```

Sympy [**A**]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}\left(a+bx\right)}{c+dx}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)/(d*x+c),x)
```

```
[Out] Integral(erfi(a + b*x)/(c + d*x), x)
```

Giac [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)/(d*x+c),x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x + a)/(d*x + c), x)
```

Mupad [**A**]
time = 0.00, size = -1, normalized size = -0.06

$$\int \frac{\mathrm{erfi}(a+b\,x)}{c+d\,x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(a + b*x)/(c + d*x),x)
```

```
[Out] int(erfi(a + b*x)/(c + d*x), x)
```

3.226 $\int \frac{\mathbf{Erfi}(a+bx)}{(c+dx)^2}\,dx$

Optimal. Leaf size=50

$$-\frac{\mathrm{Erfi}(a+bx)}{d(c+dx)}+\frac{2b\mathrm{Int}\left(\frac{e^{(a+bx)^2}}{c+dx},x\right)}{d\sqrt{\pi}}$$

```
[Out] -erfi(b*x+a)/d/(d*x+c)+2*b*Unintegrable(exp((b*x+a)^2)/(d*x+c),x)/d/Pi^(1/2
)
```

Rubi [A]
time = 0.02, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.000, Rules used = {}

$$\int \frac{\mathrm{Erfi}(a+bx)}{(c+dx)^2}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erfi[a + b*x]/(c + d*x)^2,x]
[Out] -(Erfi[a + b*x]/(d*(c + d*x))) + (2*b*Defer[Int][E^(a + b*x)^2/(c + d*x), x
])/(d*Sqrt[Pi])
```

Rubi steps

$$\int \frac{\mathrm{erfi}(a+bx)}{(c+dx)^2}\,dx=-\frac{\mathrm{erfi}(a+bx)}{d(c+dx)}+\frac{(2b)\int \frac{e^{(a+bx)^2}}{c+dx}\,dx}{d\sqrt{\pi}}$$

Mathematica [A]
time = 0.56, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{Erfi}(a+bx)}{(c+dx)^2}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfi[a + b*x]/(c + d*x)^2,x]
[Out] Integrate[Erfi[a + b*x]/(c + d*x)^2, x]
```

Maple [A]
time = 0.16, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{erfi}\left(bx+a\right)}{\left(dx+c\right)^{2}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x+a)/(d*x+c)^2,x)
```

```
[Out] int(erfi(b*x+a)/(d*x+c)^2,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)/(d*x+c)^2,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x + a)/(d*x + c)^2, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)/(d*x+c)^2,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x + a)/(d^2*x^2 + 2*c*d*x + c^2), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}\left(a + bx\right)}{\left(c + dx\right)^{2}}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)/(d*x+c)**2,x)
```

```
[Out] Integral(erfi(a + b*x)/(c + d*x)**2, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)/(d*x+c)^2,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x + a)/(d*x + c)^2, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\operatorname{erfi}(a+b\,x)}{{\left(c+d\,x\right)}^2} \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(a + b*x)/(c + d*x)^2,x)
```

```
[Out] int(erfi(a + b*x)/(c + d*x)^2, x)
```

3.227 $\int \frac{\text{Erfi}(a+bx)}{(c+dx)^3} \, dx$

Optimal. Leaf size=102

$$-\frac{be^{(a+bx)^2}}{d^2\sqrt{\pi}\,(c+dx)}+\frac{b^2\text{Erfi}(a+bx)}{d^3}-\frac{\text{Erfi}(a+bx)}{2d(c+dx)^2}-\frac{2b^2(bc-ad)\text{Int}\left(\frac{e^{(a+bx)^2}}{c+dx},x\right)}{d^3\sqrt{\pi}}$$

```
[Out] b^2*erfi(b*x+a)/d^3-1/2*erfi(b*x+a)/d/(d*x+c)^2-b*exp((b*x+a)^2)/d^2/(d*x+c
)/Pi^(1/2)-2*b^2*(-a*d+b*c)*Unintegrable(exp((b*x+a)^2)/(d*x+c),x)/d^3/Pi^(
1/2)
```

Rubi [A]
time = 0.05, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\text{Erfi}(a+bx)}{(c+dx)^3}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erfi[a + b*x]/(c + d*x)^3,x]
```

```
[Out] -((b*E^(a + b*x)^2)/(d^2*Sqrt[Pi]*(c + d*x))) + (b^2*Erfi[a + b*x])/d^3 - E
rfi[a + b*x]/(2*d*(c + d*x)^2) - (2*b^2*(b*c - a*d)*Defer[Int][E^(a + b*x)^
2/(c + d*x), x])/(d^3*Sqrt[Pi])
```

Rubi steps

$$\begin{aligned}
\int \frac{\text{erfi}(a+bx)}{(c+dx)^3}\,dx &= -\frac{\text{erfi}(a+bx)}{2d(c+dx)^2}+\frac{b\int \frac{e^{(a+bx)^2}}{(c+dx)^2}\,dx}{d\sqrt{\pi}}\\
&= -\frac{be^{(a+bx)^2}}{d^2\sqrt{\pi}\,(c+dx)}-\frac{\text{erfi}(a+bx)}{2d(c+dx)^2}+\frac{\left(2b^3\right)\int e^{(a+bx)^2}\,dx}{d^3\sqrt{\pi}}-\frac{\left(2b^2(bc-ad)\right)\int \frac{e^{(a+bx)^2}}{c+dx}\,dx}{d^3\sqrt{\pi}}\\
&= -\frac{be^{(a+bx)^2}}{d^2\sqrt{\pi}\,(c+dx)}+\frac{b^2\text{erfi}(a+bx)}{d^3}-\frac{\text{erfi}(a+bx)}{2d(c+dx)^2}-\frac{\left(2b^2(bc-ad)\right)\int \frac{e^{(a+bx)^2}}{c+dx}\,dx}{d^3\sqrt{\pi}}
\end{aligned}$$

Mathematica [A]
time = 0.60, size = 0, normalized size = 0.00

$$\int \frac{\text{Erfi}(a+bx)}{(c+dx)^3}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfi[a + b*x]/(c + d*x)^3,x]
```

```
[Out] Integrate[Erfi[a + b*x]/(c + d*x)^3, x]
```

Maple [A]
time = 0.19, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}\left(bx+a\right)}{\left(dx+c\right)^{3}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x+a)/(d*x+c)^3,x)
```

```
[Out] int(erfi(b*x+a)/(d*x+c)^3,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)/(d*x+c)^3,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x + a)/(d*x + c)^3, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)/(d*x+c)^3,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x + a)/(d^3*x^3 + 3*c*d^2*x^2 + 3*c^2*d*x + c^3), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}\left(a+bx\right)}{\left(c+dx\right)^{3}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)/(d*x+c)**3,x)
```

```
[Out] Integral(erfi(a + b*x)/(c + d*x)**3, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)/(d*x+c)^3,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x + a)/(d*x + c)^3, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erfi}(a+b\,x)}{{(c+d\,x)}^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(a + b*x)/(c + d*x)^3,x)
```

```
[Out] int(erfi(a + b*x)/(c + d*x)^3, x)
```

3.228 $\int x^5 \mathbf{Erfi}(bx)^2 \, dx$

Optimal. Leaf size=175

$$\frac{11e^{2b^2x^2}}{12b^6\pi}-\frac{7e^{2b^2x^2}x^2}{12b^4\pi}+\frac{e^{2b^2x^2}x^4}{6b^2\pi}-\frac{5e^{b^2x^2}x\mathrm{Erfi}(bx)}{4b^5\sqrt{\pi}}+\frac{5e^{b^2x^2}x^3\mathrm{Erfi}(bx)}{6b^3\sqrt{\pi}}-\frac{e^{b^2x^2}x^5\mathrm{Erfi}(bx)}{3b\sqrt{\pi}}+\frac{5\mathrm{Erfi}(bx)^2}{16b^6}+\frac{1}{6}x^6\mathrm{Erfi}(bx$$

```
[Out] 11/12*exp(2*b^2*x^2)/b^6/Pi-7/12*exp(2*b^2*x^2)*x^2/b^4/Pi+1/6*exp(2*b^2*x^
2)*x^4/b^2/Pi+5/16*erfi(b*x)^2/b^6+1/6*x^6*erfi(b*x)^2-5/4*exp(b^2*x^2)*x*e
rfi(b*x)/b^5/Pi^(1/2)+5/6*exp(b^2*x^2)*x^3*erfi(b*x)/b^3/Pi^(1/2)-1/3*exp(b
^2*x^2)*x^5*erfi(b*x)/b/Pi^(1/2)
```

Rubi [A]
time = 0.17, antiderivative size = 175, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.600$, Rules used = {6501, 6522, 6510, 30, 2240, 2243}

$$\frac{5\mathrm{Erfi}(bx)^2}{16b^6}-\frac{x^5e^{b^2x^2}\mathrm{Erfi}(bx)}{3\sqrt{\pi}\,b}+\frac{x^4e^{2b^2x^2}}{6\pi b^2}+\frac{11e^{2b^2x^2}}{12\pi b^6}-\frac{5xe^{b^2x^2}\mathrm{Erfi}(bx)}{4\sqrt{\pi}\,b^5}-\frac{7x^2e^{2b^2x^2}}{12\pi b^4}+\frac{5x^3e^{b^2x^2}\mathrm{Erfi}(bx)}{6\sqrt{\pi}\,b^3}+\frac{1}{6}x^6\mathrm{Erfi}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[x^5*Erfi[b*x]^2,x]
```

```
[Out] (11*E^(2*b^2*x^2))/(12*b^6*Pi) - (7*E^(2*b^2*x^2)*x^2)/(12*b^4*Pi) + (E^(2*
b^2*x^2)*x^4)/(6*b^2*Pi) - (5*E^(b^2*x^2)*x*Erfi[b*x])/(4*b^5*Sqrt[Pi]) + (
5*E^(b^2*x^2)*x^3*Erfi[b*x])/(6*b^3*Sqrt[Pi]) - (E^(b^2*x^2)*x^5*Erfi[b*x])
/(3*b*Sqrt[Pi]) + (5*Erfi[b*x]^2)/(16*b^6) + (x^6*Erfi[b*x]^2)/6
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
```

```
0])
```

Rule 6501

```
Int[Erfi[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfi[b*x]^2
/(m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[x^(m + 1)*E^(b^2*x^2)*Er
fi[b*x], x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int x^5\text{erfi}(bx)^2\,dx &= \frac{1}{6}x^6\text{erfi}(bx)^2 - \frac{(2b)\int e^{b^2x^2}x^6\text{erfi}(bx)\,dx}{3\sqrt{\pi}} \\
&= -\frac{e^{b^2x^2}x^5\text{erfi}(bx)}{3b\sqrt{\pi}} + \frac{1}{6}x^6\text{erfi}(bx)^2 + \frac{2\int e^{2b^2x^2}x^5\,dx}{3\pi} + \frac{5\int e^{b^2x^2}x^4\text{erfi}(bx)\,dx}{3b\sqrt{\pi}} \\
&= \frac{e^{2b^2x^2}x^4}{6b^2\pi} + \frac{5e^{b^2x^2}x^3\text{erfi}(bx)}{6b^3\sqrt{\pi}} - \frac{e^{b^2x^2}x^5\text{erfi}(bx)}{3b\sqrt{\pi}} + \frac{1}{6}x^6\text{erfi}(bx)^2 - \frac{2\int e^{2b^2x^2}x^3\,dx}{3b^2\pi} - \frac{5\int e^{2b^2x^2}}{3b^2} \\
&= -\frac{7e^{2b^2x^2}x^2}{12b^4\pi} + \frac{e^{2b^2x^2}x^4}{6b^2\pi} - \frac{5e^{b^2x^2}x\text{erfi}(bx)}{4b^5\sqrt{\pi}} + \frac{5e^{b^2x^2}x^3\text{erfi}(bx)}{6b^3\sqrt{\pi}} - \frac{e^{b^2x^2}x^5\text{erfi}(bx)}{3b\sqrt{\pi}} + \frac{1}{6}x^6\text{erfi}(b \\
&= \frac{11e^{2b^2x^2}}{12b^6\pi} - \frac{7e^{2b^2x^2}x^2}{12b^4\pi} + \frac{e^{2b^2x^2}x^4}{6b^2\pi} - \frac{5e^{b^2x^2}x\text{erfi}(bx)}{4b^5\sqrt{\pi}} + \frac{5e^{b^2x^2}x^3\text{erfi}(bx)}{6b^3\sqrt{\pi}} - \frac{e^{b^2x^2}x^5\text{erfi}(bx)}{3b\sqrt{\pi}} + \\
&= \frac{11e^{2b^2x^2}}{12b^6\pi} - \frac{7e^{2b^2x^2}x^2}{12b^4\pi} + \frac{e^{2b^2x^2}x^4}{6b^2\pi} - \frac{5e^{b^2x^2}x\text{erfi}(bx)}{4b^5\sqrt{\pi}} + \frac{5e^{b^2x^2}x^3\text{erfi}(bx)}{6b^3\sqrt{\pi}} - \frac{e^{b^2x^2}x^5\text{erfi}(bx)}{3b\sqrt{\pi}} +
\end{aligned}$$

Mathematica [A]
time = 0.03, size = 99, normalized size = 0.57

$$\frac{4e^{2b^2x^2}(11-7b^2x^2+2b^4x^4)-4be^{b^2x^2}\sqrt{\pi}\,x(15-10b^2x^2+4b^4x^4)\,\text{Erfi}(bx)+\pi(15+8b^6x^6)\,\text{Erfi}(bx)^2}{48b^6\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^5*Erfi[b*x]^2,x]
```

```
[Out] (4*E^(2*b^2*x^2)*(11 - 7*b^2*x^2 + 2*b^4*x^4) - 4*b*E^(b^2*x^2)*Sqrt[Pi]*x*
(15 - 10*b^2*x^2 + 4*b^4*x^4)*Erfi[b*x] + Pi*(15 + 8*b^6*x^6)*Erfi[b*x]^2)/
(48*b^6*Pi)
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int x^5 \operatorname{erfi}(bx)^2\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*erfi(b*x)^2,x)
```

```
[Out] int(x^5*erfi(b*x)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfi(b*x)^2,x, algorithm="maxima")
```

```
[Out] integrate(x^5*erfi(b*x)^2, x)
```

Fricas [A]
time = 0.34, size = 97, normalized size = 0.55

$$-\frac{4\sqrt{\pi}\,(4\,b^5x^5-10\,b^3x^3+15\,bx)\operatorname{erfi}(bx)\,e^{(b^2x^2)}-(15\,\pi+8\,\pi b^6x^6)\operatorname{erfi}(bx)^2-4\,(2\,b^4x^4-7\,b^2x^2+11)e^{(2\,b^2x^2)}}{48\,\pi b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfi(b*x)^2,x, algorithm="fricas")
```

```
[Out] -1/48*(4*sqrt(pi)*(4*b^5*x^5 - 10*b^3*x^3 + 15*b*x)*erfi(b*x)*e^(b^2*x^2) -
 (15*pi + 8*pi*b^6*x^6)*erfi(b*x)^2 - 4*(2*b^4*x^4 - 7*b^2*x^2 + 11)*e^(2*b
^2*x^2))/(pi*b^6)
```

Sympy [A]
time = 0.64, size = 168, normalized size = 0.96

$$\begin{cases} \frac{x^6\operatorname{erfi}^2(bx)}{6}-\frac{x^5e^{b^2x^2}\operatorname{erfi}(bx)}{3\sqrt{\pi}\,b}+\frac{x^4e^{2b^2x^2}}{6\pi b^2}+\frac{5x^3e^{b^2x^2}\operatorname{erfi}(bx)}{6\sqrt{\pi}\,b^3}-\frac{7x^2e^{2b^2x^2}}{12\pi b^4}-\frac{5xe^{b^2x^2}\operatorname{erfi}(bx)}{4\sqrt{\pi}\,b^5}+\frac{11e^{2b^2x^2}}{12\pi b^6}+\frac{5\operatorname{erfi}^2(bx)}{16b^6} & \text{for}\ b\neq 0\\ 0 & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**5*erfi(b*x)**2,x)
```

```
[Out] Piecewise((x**6*erfi(b*x)**2/6 - x**5*exp(b**2*x**2)*erfi(b*x)/(3*sqrt(pi)*
b) + x**4*exp(2*b**2*x**2)/(6*pi*b**2) + 5*x**3*exp(b**2*x**2)*erfi(b*x)/(6
*sqrt(pi)*b**3) - 7*x**2*exp(2*b**2*x**2)/(12*pi*b**4) - 5*x*exp(b**2*x**2)
*erfi(b*x)/(4*sqrt(pi)*b**5) + 11*exp(2*b**2*x**2)/(12*pi*b**6) + 5*erfi(b*
x)**2/(16*b**6), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfi(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(x^5*erfi(b*x)^2, x)
```

Mupad [B]
time = 0.30, size = 139, normalized size = 0.79

$$\frac{x^6\,\mathrm{erfi}\left(b\,x\right)^2}{6}+\frac{\frac{11\,\mathrm{e}^{2\,b^2\,x^2}}{12}+\frac{5\,\pi\,\mathrm{erfi}\left(b\,x\right)^2}{16}-\frac{7\,b^2\,x^2\,\mathrm{e}^{2\,b^2\,x^2}}{12}+\frac{b^4\,x^4\,\mathrm{e}^{2\,b^2\,x^2}}{6}+\frac{5\,b^3\,x^3\,\sqrt{\pi}\,\mathrm{e}^{b^2\,x^2}\,\mathrm{erfi}\left(b\,x\right)}{6}-\frac{b^5\,x^5\,\sqrt{\pi}\,\mathrm{e}^{b^2\,x^2}\,\mathrm{erfi}\left(b\,x\right)}{3}-\frac{5\,b\,x\,\sqrt{\pi}\,\mathrm{e}^{b^2\,x^2}\,\mathrm{erfi}\left(b\,x\right)}{4}}{b^6\,\pi}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*erfi(b*x)^2,x)
```

```
[Out] (x^6*erfi(b*x)^2)/6 + ((11*exp(2*b^2*x^2))/12 + (5*pi*erfi(b*x)^2)/16 - (7*
b^2*x^2*exp(2*b^2*x^2))/12 + (b^4*x^4*exp(2*b^2*x^2))/6 + (5*b^3*x^3*pi^(1/
2)*exp(b^2*x^2)*erfi(b*x))/6 - (b^5*x^5*pi^(1/2)*exp(b^2*x^2)*erfi(b*x))/3
- (5*b*x*pi^(1/2)*exp(b^2*x^2)*erfi(b*x))/4)/(b^6*pi)
```

3.229 $\int x^3 \mathbf{Erfi}(bx)^2\,dx$

Optimal. Leaf size=124

$$-\frac{e^{2b^2x^2}}{2b^4\pi}+\frac{e^{2b^2x^2}x^2}{4b^2\pi}+\frac{3e^{b^2x^2}x\text{Erfi}(bx)}{4b^3\sqrt{\pi}}-\frac{e^{b^2x^2}x^3\text{Erfi}(bx)}{2b\sqrt{\pi}}-\frac{3\text{Erfi}(bx)^2}{16b^4}+\frac{1}{4}x^4\text{Erfi}(bx)^2$$

```
[Out] -1/2*exp(2*b^2*x^2)/b^4/Pi+1/4*exp(2*b^2*x^2)*x^2/b^2/Pi-3/16*erfi(b*x)^2/b
^4+1/4*x^4*erfi(b*x)^2+3/4*exp(b^2*x^2)*x*erfi(b*x)/b^3/Pi^(1/2)-1/2*exp(b^
2*x^2)*x^3*erfi(b*x)/b/Pi^(1/2)
```

Rubi [A]
time = 0.11, antiderivative size = 124, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.600$, Rules used = {6501, 6522, 6510, 30, 2240, 2243}

$$-\frac{3\text{Erfi}(bx)^2}{16b^4}-\frac{x^3e^{b^2x^2}\text{Erfi}(bx)}{2\sqrt{\pi}\,b}+\frac{x^2e^{2b^2x^2}}{4\pi b^2}-\frac{e^{2b^2x^2}}{2\pi b^4}+\frac{3xe^{b^2x^2}\text{Erfi}(bx)}{4\sqrt{\pi}\,b^3}+\frac{1}{4}x^4\text{Erfi}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[x^3*Erfi[b*x]^2,x]
```

```
[Out] -1/2*E^(2*b^2*x^2)/(b^4*Pi) + (E^(2*b^2*x^2)*x^2)/(4*b^2*Pi) + (3*E^(b^2*x^
2)*x*Erfi[b*x])/(4*b^3*Sqrt[Pi]) - (E^(b^2*x^2)*x^3*Erfi[b*x])/(2*b*Sqrt[Pi
]) - (3*Erfi[b*x]^2)/(16*b^4) + (x^4*Erfi[b*x]^2)/4
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6501

```
Int[Erfi[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfi[b*x]^2
/(m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[x^(m + 1)*E^(b^2*x^2)*Er
fi[b*x], x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int x^3\text{erfi}(bx)^2\,dx &= \frac{1}{4}x^4\text{erfi}(bx)^2 - \frac{b\int e^{b^2x^2}x^4\text{erfi}(bx)\,dx}{\sqrt{\pi}}\\
&= -\frac{e^{b^2x^2}x^3\text{erfi}(bx)}{2b\sqrt{\pi}} + \frac{1}{4}x^4\text{erfi}(bx)^2 + \frac{\int e^{2b^2x^2}x^3\,dx}{\pi} + \frac{3\int e^{b^2x^2}x^2\text{erfi}(bx)\,dx}{2b\sqrt{\pi}}\\
&= \frac{e^{2b^2x^2}x^2}{4b^2\pi} + \frac{3e^{b^2x^2}x\text{erfi}(bx)}{4b^3\sqrt{\pi}} - \frac{e^{b^2x^2}x^3\text{erfi}(bx)}{2b\sqrt{\pi}} + \frac{1}{4}x^4\text{erfi}(bx)^2 - \frac{\int e^{2b^2x^2}x\,dx}{2b^2\pi} - \frac{3\int e^{2b^2x^2}x\,d}{2b^2\pi}\\
&= -\frac{e^{2b^2x^2}}{2b^4\pi} + \frac{e^{2b^2x^2}x^2}{4b^2\pi} + \frac{3e^{b^2x^2}x\text{erfi}(bx)}{4b^3\sqrt{\pi}} - \frac{e^{b^2x^2}x^3\text{erfi}(bx)}{2b\sqrt{\pi}} + \frac{1}{4}x^4\text{erfi}(bx)^2 - \frac{3\text{Subst}(\int x\,dx, x}{8b^4}\\
&= -\frac{e^{2b^2x^2}}{2b^4\pi} + \frac{e^{2b^2x^2}x^2}{4b^2\pi} + \frac{3e^{b^2x^2}x\text{erfi}(bx)}{4b^3\sqrt{\pi}} - \frac{e^{b^2x^2}x^3\text{erfi}(bx)}{2b\sqrt{\pi}} - \frac{3\text{erfi}(bx)^2}{16b^4} + \frac{1}{4}x^4\text{erfi}(bx)^2
\end{aligned}$$

Mathematica [A]
time = 0.02, size = 82, normalized size = 0.66

$$\frac{4e^{2b^2x^2}(-2+b^2x^2) - 4be^{b^2x^2}\sqrt{\pi}\,x(-3+2b^2x^2)\,\text{Erfi}(bx) + \pi(-3+4b^4x^4)\,\text{Erfi}(bx)^2}{16b^4\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^3*Erfi[b*x]^2,x]
```

```
[Out] (4*E^(2*b^2*x^2)*(-2 + b^2*x^2) - 4*b*E^(b^2*x^2)*Sqrt[Pi]*x*(-3 + 2*b^2*x^
2)*Erfi[b*x] + Pi*(-3 + 4*b^4*x^4)*Erfi[b*x]^2)/(16*b^4*Pi)
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int x^{3} \operatorname{erfi}\left(b x\right)^{2}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erfi(b*x)^2,x)
[Out] int(x^3*erfi(b*x)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfi(b*x)^2,x, algorithm="maxima")
[Out] integrate(x^3*erfi(b*x)^2, x)
```

Fricas [A]
time = 0.43, size = 79, normalized size = 0.64

$$-\frac{4\,\sqrt{\pi}\,\left(2\,b^{3} x^{3} - 3\,b x\right) \operatorname{erfi}\left(b x\right) e^{\left(b^{2} x^{2}\right)} + \left(3\,\pi - 4\,\pi b^{4} x^{4}\right) \operatorname{erfi}\left(b x\right)^{2} - 4\,\left(b^{2} x^{2} - 2\right) e^{\left(2\,b^{2} x^{2}\right)}}{16\,\pi b^{4}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfi(b*x)^2,x, algorithm="fricas")
[Out] -1/16*(4*sqrt(pi)*(2*b^3*x^3 - 3*b*x)*erfi(b*x)*e^(b^2*x^2) + (3*pi - 4*pi*
b^4*x^4)*erfi(b*x)^2 - 4*(b^2*x^2 - 2)*e^(2*b^2*x^2))/(pi*b^4)
```

Sympy [A]
time = 0.29, size = 116, normalized size = 0.94

$$\begin{cases} \frac{x^{4} \operatorname{erfi}^{2}{\left(b x \right)}}{4} - \frac{x^{3} e^{b^{2} x^{2}} \operatorname{erfi}{\left(b x \right)}}{2 \sqrt{\pi} b} + \frac{x^{2} e^{2 b^{2} x^{2}}}{4 \pi b^{2}} + \frac{3 x e^{b^{2} x^{2}} \operatorname{erfi}{\left(b x \right)}}{4 \sqrt{\pi} b^{3}} - \frac{e^{2 b^{2} x^{2}}}{2 \pi b^{4}} - \frac{3 \operatorname{erfi}^{2}{\left(b x \right)}}{16 b^{4}} & \text{for}\: b \neq 0 \\0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3*erfi(b*x)**2,x)
```

```
[Out] Piecewise((x**4*erfi(b*x)**2/4 - x**3*exp(b**2*x**2)*erfi(b*x)/(2*sqrt(pi)*
b) + x**2*exp(2*b**2*x**2)/(4*pi*b**2) + 3*x*exp(b**2*x**2)*erfi(b*x)/(4*sq
rt(pi)*b**3) - exp(2*b**2*x**2)/(2*pi*b**4) - 3*erfi(b*x)**2/(16*b**4), Ne(
b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfi(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(x^3*erfi(b*x)^2, x)
```

Mupad [B]
time = 0.22, size = 100, normalized size = 0.81

$$\frac{x^4\,\mathrm{erfi}(b\,x)^2}{4}-\frac{\frac{\mathrm{e}^{2\,b^2\,x^2}}{2}+\frac{3\,\pi\,\mathrm{erfi}(b\,x)^2}{16}-\frac{b^2\,x^2\,\mathrm{e}^{2\,b^2\,x^2}}{4}+\frac{b^3\,x^3\,\sqrt{\pi}\,\mathrm{e}^{b^2\,x^2}\,\mathrm{erfi}(b\,x)}{2}-\frac{3\,b\,x\,\sqrt{\pi}\,\mathrm{e}^{b^2\,x^2}\,\mathrm{erfi}(b\,x)}{4}}{b^4\,\pi}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erfi(b*x)^2,x)
```

```
[Out] (x^4*erfi(b*x)^2)/4 - (exp(2*b^2*x^2)/2 + (3*pi*erfi(b*x)^2)/16 - (b^2*x^2*
exp(2*b^2*x^2))/4 + (b^3*x^3*pi^(1/2)*exp(b^2*x^2)*erfi(b*x))/2 - (3*b*x*pi
^(1/2)*exp(b^2*x^2)*erfi(b*x))/4)/(b^4*pi)
```

3.230 $\int x\mathbf{Erfi}(bx)^2\,dx$

Optimal. Leaf size=71

$$\frac{e^{2b^2x^2}}{2b^2\pi}-\frac{e^{b^2x^2}x\text{Erfi}(bx)}{b\sqrt{\pi}}+\frac{\text{Erfi}(bx)^2}{4b^2}+\frac{1}{2}x^2\text{Erfi}(bx)^2$$

```
[Out] 1/2*exp(2*b^2*x^2)/b^2/Pi+1/4*erfi(b*x)^2/b^2+1/2*x^2*erfi(b*x)^2-exp(b^2*x
^2)*x*erfi(b*x)/b/Pi^(1/2)
```

Rubi [A]
time = 0.05, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}}=0.625$, Rules used = {6501, 6522, 6510, 30, 2240}

$$-\frac{xe^{b^2x^2}\text{Erfi}(bx)}{\sqrt{\pi}\,b}+\frac{\text{Erfi}(bx)^2}{4b^2}+\frac{e^{2b^2x^2}}{2\pi b^2}+\frac{1}{2}x^2\text{Erfi}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[x*Erfi[b*x]^2,x]
```

```
[Out] E^(2*b^2*x^2)/(2*b^2*Pi) - (E^(b^2*x^2)*x*Erfi[b*x])/(b*Sqrt[Pi]) + Erfi[b*
x]^2/(4*b^2) + (x^2*Erfi[b*x]^2)/2
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 6501

```
Int[Erfi[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfi[b*x]^2
/(m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[x^(m + 1)*E^(b^2*x^2)*Er
fi[b*x], x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
```

```
}, x] && EqQ[d, b^2]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int x\text{erfi}(bx)^2\,dx &= \frac{1}{2}x^2\text{erfi}(bx)^2 - \frac{(2b)\int e^{b^2x^2}x^2\text{erfi}(bx)\,dx}{\sqrt{\pi}}\\
&= -\frac{e^{b^2x^2}x\text{erfi}(bx)}{b\sqrt{\pi}} + \frac{1}{2}x^2\text{erfi}(bx)^2 + \frac{2\int e^{2b^2x^2}x\,dx}{\pi} + \frac{\int e^{b^2x^2}\text{erfi}(bx)\,dx}{b\sqrt{\pi}}\\
&= \frac{e^{2b^2x^2}}{2b^2\pi} - \frac{e^{b^2x^2}x\text{erfi}(bx)}{b\sqrt{\pi}} + \frac{1}{2}x^2\text{erfi}(bx)^2 + \frac{\text{Subst}(\int x\,dx, x, \text{erfi}(bx))}{2b^2}\\
&= \frac{e^{2b^2x^2}}{2b^2\pi} - \frac{e^{b^2x^2}x\text{erfi}(bx)}{b\sqrt{\pi}} + \frac{\text{erfi}(bx)^2}{4b^2} + \frac{1}{2}x^2\text{erfi}(bx)^2
\end{aligned}$$

Mathematica [**A**]
time = 0.01, size = 63, normalized size = 0.89

$$\frac{2e^{2b^2x^2} - 4be^{b^2x^2}\sqrt{\pi}\,x\text{Erfi}(bx) + (\pi + 2b^2\pi x^2)\,\text{Erfi}(bx)^2}{4b^2\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[x*Erfi[b*x]^2,x]
[Out] (2*E^(2*b^2*x^2) - 4*b*E^(b^2*x^2)*Sqrt[Pi]*x*Erfi[b*x] + (Pi + 2*b^2*Pi*x^
2)*Erfi[b*x]^2)/(4*b^2*Pi)
```

Maple [**F**]
time = 0.02, size = 0, normalized size = 0.00

$$\int x\,\text{erfi}\,(bx)^2\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfi(b*x)^2,x)
```

[Out] int(x*erfi(b*x)^2,x)

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(b*x)^2,x, algorithm="maxima")
```

```
[Out] integrate(x*erfi(b*x)^2, x)
```

Fricas [A]
time = 0.34, size = 58, normalized size = 0.82

$$-\frac{4\sqrt{\pi}\,bx\,\mathrm{erfi}\,(bx)\,e^{(b^2x^2)} - (\pi + 2\,\pi b^2x^2)\,\mathrm{erfi}\,(bx)^2 - 2\,e^{(2\,b^2x^2)}}{4\,\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(b*x)^2,x, algorithm="fricas")
```

```
[Out] -1/4*(4*sqrt(pi)*b*x*erfi(b*x)*e^(b^2*x^2) - (pi + 2*pi*b^2*x^2)*erfi(b*x)^
2 - 2*e^(2*b^2*x^2))/(pi*b^2)
```

Sympy [A]
time = 0.12, size = 63, normalized size = 0.89

$$\begin{cases} \frac{x^2\,\mathrm{erfi}^2\,(bx)}{2} - \frac{xe^{b^2x^2}\,\mathrm{erfi}\,(bx)}{\sqrt{\pi}\,b} + \frac{e^{2b^2x^2}}{2\pi b^2} + \frac{\mathrm{erfi}^2\,(bx)}{4b^2} & \text{for}\ b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(b*x)**2,x)
```

```
[Out] Piecewise((x**2*erfi(b*x)**2/2 - x*exp(b**2*x**2)*erfi(b*x)/(sqrt(pi)*b) +
exp(2*b**2*x**2)/(2*pi*b**2) + erfi(b*x)**2/(4*b**2), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(x*erfi(b*x)^2, x)
```

Mupad [B]
time = 0.18, size = 66, normalized size = 0.93

$$\frac{\frac{b^2\,x^2\,\mathrm{erfi}(b\,x)^2}{2}+\frac{\mathrm{erfi}(b\,x)^2}{4}}{b^2}+\frac{\frac{\mathrm{e}^{2\,b^2\,x^2}}{2}-b\,x\,\sqrt{\pi}\,\,\mathrm{e}^{b^2\,x^2}\,\mathrm{erfi}(b\,x)}{b^2\,\pi}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfi(b*x)^2,x)
```

```
[Out] (erfi(b*x)^2/4 + (b^2*x^2*erfi(b*x)^2)/2)/b^2 + (exp(2*b^2*x^2)/2 - b*x*pi^
(1/2)*exp(b^2*x^2)*erfi(b*x))/(b^2*pi)
```

3.231 $\int \frac{\mathbf{Erfi}(bx)^2}{x}\,dx$

Optimal. Leaf size=13

$$\mathrm{Int}\left(\frac{\mathrm{Erfi}(bx)^2}{x},x\right)$$

```
[Out] Unintegrable(erfi(b*x)^2/x,x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\mathrm{Erfi}(bx)^2}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erfi[b*x]^2/x,x]
```

```
[Out] Defer[Int][Erfi[b*x]^2/x, x]
```

Rubi steps

$$\int \frac{\mathrm{erfi}(bx)^2}{x}\,dx = \int \frac{\mathrm{erfi}(bx)^2}{x}\,dx$$

Mathematica [A]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{Erfi}(bx)^2}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfi[b*x]^2/x,x]
```

```
[Out] Integrate[Erfi[b*x]^2/x, x]
```

Maple [A]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{erfi}\left(bx\right)^2}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2/x,x)
```

```
[Out] int(erfi(b*x)^2/x,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)^2/x, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x)^2/x, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}^{2}(bx)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)**2/x,x)
```

```
[Out] Integral(erfi(b*x)**2/x, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)^2/x, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.08

$$\int \frac{\operatorname{erfi}(b\,x)^2}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2/x,x)
```

```
[Out] int(erfi(b*x)^2/x, x)
```

3.232 $\int \frac{\mathbf{Erfi}(bx)^2}{x^3}\,dx$

Optimal. Leaf size=65

$$-\frac{2be^{b^2x^2}\mathrm{Erfi}(bx)}{\sqrt{\pi}\,x}+b^2\mathrm{Erfi}(bx)^2-\frac{\mathrm{Erfi}(bx)^2}{2x^2}+\frac{2b^2\mathrm{Ei}(2b^2x^2)}{\pi}$$

```
[Out] 2*b^2*Ei(2*b^2*x^2)/Pi+b^2*erfi(b*x)^2-1/2*erfi(b*x)^2/x^2-2*b*exp(b^2*x^2)
*erfi(b*x)/x/Pi^(1/2)
```

Rubi [A]

time = 0.06, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules used = {6501, 6528, 6510, 30, 2241}

$$-\frac{2be^{b^2x^2}\mathrm{Erfi}(bx)}{\sqrt{\pi}\,x}+b^2\mathrm{Erfi}(bx)^2+\frac{2b^2\mathrm{Ei}(2b^2x^2)}{\pi}-\frac{\mathrm{Erfi}(bx)^2}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]^2/x^3,x]
```

```
[Out] (-2*b*E^(b^2*x^2)*Erfi[b*x])/(Sqrt[Pi]*x) + b^2*Erfi[b*x]^2 - Erfi[b*x]^2/(
2*x^2) + (2*b^2*ExpIntegralEi[2*b^2*x^2])/Pi
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 6501

```
Int[Erfi[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfi[b*x]^2
/(m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[x^(m + 1)*E^(b^2*x^2)*Er
fi[b*x], x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6528

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x
]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int \frac{\operatorname{erfi}(bx)^2}{x^3}\,dx &= -\frac{\operatorname{erfi}(bx)^2}{2x^2}+\frac{(2b)\int \frac{e^{b^2x^2}\operatorname{erfi}(bx)}{x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{2be^{b^2x^2}\operatorname{erfi}(bx)}{\sqrt{\pi}\,x}-\frac{\operatorname{erfi}(bx)^2}{2x^2}+\frac{(4b^2)\int \frac{e^{2b^2x^2}}{x}\,dx}{\pi}+\frac{(4b^3)\int e^{b^2x^2}\operatorname{erfi}(bx)\,dx}{\sqrt{\pi}}\\
&= -\frac{2be^{b^2x^2}\operatorname{erfi}(bx)}{\sqrt{\pi}\,x}-\frac{\operatorname{erfi}(bx)^2}{2x^2}+\frac{2b^2\operatorname{Ei}(2b^2x^2)}{\pi}+(2b^2)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erfi}(bx)\right)\\
&= -\frac{2be^{b^2x^2}\operatorname{erfi}(bx)}{\sqrt{\pi}\,x}+b^2\operatorname{erfi}(bx)^2-\frac{\operatorname{erfi}(bx)^2}{2x^2}+\frac{2b^2\operatorname{Ei}(2b^2x^2)}{\pi}
\end{aligned}$$

Mathematica [A]
time = 0.02, size = 60, normalized size = 0.92

$$-\frac{2be^{b^2x^2}\operatorname{Erfi}(bx)}{\sqrt{\pi}\,x}+\left(b^2-\frac{1}{2x^2}\right)\operatorname{Erfi}(bx)^2+\frac{2b^2\operatorname{Ei}(2b^2x^2)}{\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]^2/x^3,x]
[Out] (-2*b*E^(b^2*x^2)*Erfi[b*x])/(Sqrt[Pi]*x) + (b^2 - 1/(2*x^2))*Erfi[b*x]^2 +
 (2*b^2*ExpIntegralEi[2*b^2*x^2])/Pi
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}\left(bx\right)^2}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2/x^3,x)
[Out] int(erfi(b*x)^2/x^3,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^3,x, algorithm="maxima")
[Out] integrate(erfi(b*x)^2/x^3, x)
```

Fricas [A]
time = 0.36, size = 64, normalized size = 0.98

$$\frac{4\,b^2x^2\mathrm{Ei}(2\,b^2x^2) - 4\,\sqrt{\pi}\,bx\,\mathrm{erfi}\,(bx)\,e^{(b^2x^2)} - (\pi - 2\,\pi b^2x^2)\,\mathrm{erfi}\,(bx)^2}{2\,\pi x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^3,x, algorithm="fricas")
[Out] 1/2*(4*b^2*x^2*Ei(2*b^2*x^2) - 4*sqrt(pi)*b*x*erfi(b*x)*e^(b^2*x^2) - (pi -
 2*pi*b^2*x^2)*erfi(b*x)^2)/(pi*x^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{erfi}^2\,(bx)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)**2/x**3,x)
[Out] Integral(erfi(b*x)**2/x**3, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^3,x, algorithm="giac")
[Out] integrate(erfi(b*x)^2/x^3, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\mathrm{erfi}(b\,x)^2}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2/x^3,x)
[Out] int(erfi(b*x)^2/x^3, x)
```

3.233 $\int \frac{\text{Erfi}(bx)^2}{x^5}\,dx$

Optimal. Leaf size=123

$$-\frac{b^2e^{2b^2x^2}}{3\pi x^2}-\frac{be^{b^2x^2}\text{Erfi}(bx)}{3\sqrt{\pi}\,x^3}-\frac{2b^3e^{b^2x^2}\text{Erfi}(bx)}{3\sqrt{\pi}\,x}+\frac{1}{3}b^4\text{Erfi}(bx)^2-\frac{\text{Erfi}(bx)^2}{4x^4}+\frac{4b^4\text{Ei}(2b^2x^2)}{3\pi}$$

```
[Out] -1/3*b^2*exp(2*b^2*x^2)/Pi/x^2+4/3*b^4*Ei(2*b^2*x^2)/Pi+1/3*b^4*erfi(b*x)^2
-1/4*erfi(b*x)^2/x^4-1/3*b*exp(b^2*x^2)*erfi(b*x)/x^3/Pi^(1/2)-2/3*b^3*exp(
b^2*x^2)*erfi(b*x)/x/Pi^(1/2)
```

Rubi [A]
time = 0.11, antiderivative size = 123, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.600, Rules used = {6501, 6528, 6510, 30, 2241, 2245}

$$\frac{1}{3}b^4\text{Erfi}(bx)^2-\frac{be^{b^2x^2}\text{Erfi}(bx)}{3\sqrt{\pi}\,x^3}-\frac{b^2e^{2b^2x^2}}{3\pi x^2}+\frac{4b^4\text{Ei}(2b^2x^2)}{3\pi}-\frac{2b^3e^{b^2x^2}\text{Erfi}(bx)}{3\sqrt{\pi}\,x}-\frac{\text{Erfi}(bx)^2}{4x^4}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]^2/x^5,x]
```

```
[Out] -1/3*(b^2*E^(2*b^2*x^2))/(Pi*x^2) - (b*E^(b^2*x^2)*Erfi[b*x])/(3*Sqrt[Pi]*x
^3) - (2*b^3*E^(b^2*x^2)*Erfi[b*x])/(3*Sqrt[Pi]*x) + (b^4*Erfi[b*x]^2)/3 -
Erfi[b*x]^2/(4*x^4) + (4*b^4*ExpIntegralEi[2*b^2*x^2])/(3*Pi)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6501

```
Int[Erfi[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfi[b*x]^2
/(m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[x^(m + 1)*E^(b^2*x^2)*Er
fi[b*x], x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6528

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x
]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int \frac{\operatorname{erfi}(bx)^2}{x^5}\,dx &= -\frac{\operatorname{erfi}(bx)^2}{4x^4}+\frac{b\int \frac{e^{b^2x^2}\operatorname{erfi}(bx)}{x^4}\,dx}{\sqrt{\pi}}\\
&= -\frac{be^{b^2x^2}\operatorname{erfi}(bx)}{3\sqrt{\pi}\,x^3}-\frac{\operatorname{erfi}(bx)^2}{4x^4}+\frac{(2b^2)\int \frac{e^{2b^2x^2}}{x^3}\,dx}{3\pi}+\frac{(2b^3)\int \frac{e^{b^2x^2}\operatorname{erfi}(bx)}{x^2}\,dx}{3\sqrt{\pi}}\\
&= -\frac{b^2e^{2b^2x^2}}{3\pi x^2}-\frac{be^{b^2x^2}\operatorname{erfi}(bx)}{3\sqrt{\pi}\,x^3}-\frac{2b^3e^{b^2x^2}\operatorname{erfi}(bx)}{3\sqrt{\pi}\,x}-\frac{\operatorname{erfi}(bx)^2}{4x^4}+2\frac{(4b^4)\int \frac{e^{2b^2x^2}}{x}\,dx}{3\pi}+\frac{(4b^5)\int e^{b^2x}}{3\sqrt{}}\\
&= -\frac{b^2e^{2b^2x^2}}{3\pi x^2}-\frac{be^{b^2x^2}\operatorname{erfi}(bx)}{3\sqrt{\pi}\,x^3}-\frac{2b^3e^{b^2x^2}\operatorname{erfi}(bx)}{3\sqrt{\pi}\,x}-\frac{\operatorname{erfi}(bx)^2}{4x^4}+\frac{4b^4\operatorname{Ei}(2b^2x^2)}{3\pi}+\frac{1}{3}(2b^4)\operatorname{Subst}(\int\\
&= -\frac{b^2e^{2b^2x^2}}{3\pi x^2}-\frac{be^{b^2x^2}\operatorname{erfi}(bx)}{3\sqrt{\pi}\,x^3}-\frac{2b^3e^{b^2x^2}\operatorname{erfi}(bx)}{3\sqrt{\pi}\,x}+\frac{1}{3}b^4\operatorname{erfi}(bx)^2-\frac{\operatorname{erfi}(bx)^2}{4x^4}+\frac{4b^4\operatorname{Ei}(2b^2x^2)}{3\pi}
\end{aligned}$$

Mathematica [A]
time = 0.02, size = 97, normalized size = 0.79

$$\frac{-4be^{b^2x^2}\sqrt{\pi}\,x(1+2b^2x^2)\operatorname{Erfi}(bx)+\pi(-3+4b^4x^4)\operatorname{Erfi}(bx)^2-4b^2x^2\left(e^{2b^2x^2}-4b^2x^2\operatorname{Ei}(2b^2x^2)\right)}{12\pi x^4}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]^2/x^5,x]
```

```
[Out] (-4*b*E^(b^2*x^2)*Sqrt[Pi]*x*(1 + 2*b^2*x^2)*Erfi[b*x] + Pi*(-3 + 4*b^4*x^4
)*Erfi[b*x]^2 - 4*b^2*x^2*(E^(2*b^2*x^2) - 4*b^2*x^2*ExpIntegralEi[2*b^2*x^
2]))/(12*Pi*x^4)
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}(bx)^2}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2/x^5,x)
```

```
[Out] int(erfi(b*x)^2/x^5,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^5,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)^2/x^5, x)
```

Fricas [A]
time = 0.38, size = 93, normalized size = 0.76

$$\frac{16\,b^4x^4\mathrm{Ei}(2\,b^2x^2) - 4\,b^2x^2e^{(2\,b^2x^2)} - 4\,\sqrt{\pi}\,(2\,b^3x^3 + bx)\operatorname{erfi}(bx)\,e^{(b^2x^2)} - (3\,\pi - 4\,\pi b^4x^4)\operatorname{erfi}(bx)^2}{12\,\pi x^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^5,x, algorithm="fricas")
```

```
[Out] 1/12*(16*b^4*x^4*Ei(2*b^2*x^2) - 4*b^2*x^2*e^(2*b^2*x^2) - 4*sqrt(pi)*(2*b^
3*x^3 + b*x)*erfi(b*x)*e^(b^2*x^2) - (3*pi - 4*pi*b^4*x^4)*erfi(b*x)^2)/(pi
*x^4)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}^2(bx)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)**2/x**5,x)
```

```
[Out] Integral(erfi(b*x)**2/x**5, x)
```

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^5,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)^2/x^5, x)
```

Mupad [**F**]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erfi}(b\,x)^2}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2/x^5,x)
```

```
[Out] int(erfi(b*x)^2/x^5, x)
```

3.234 $\int \frac{\mathbf{Erfi}(bx)^2}{x^7}\,dx$

Optimal. Leaf size=174

$$-\frac{b^2e^{2b^2x^2}}{15\pi x^4}-\frac{2b^4e^{2b^2x^2}}{9\pi x^2}-\frac{2be^{b^2x^2}\mathrm{Erfi}(bx)}{15\sqrt{\pi}\,x^5}-\frac{4b^3e^{b^2x^2}\mathrm{Erfi}(bx)}{45\sqrt{\pi}\,x^3}-\frac{8b^5e^{b^2x^2}\mathrm{Erfi}(bx)}{45\sqrt{\pi}\,x}+\frac{4}{45}b^6\mathrm{Erfi}(bx)^2-\frac{\mathrm{Erfi}(bx)^2}{6x^6}+\frac{28b^6}{}$$

```
[Out] -1/15*b^2*exp(2*b^2*x^2)/Pi/x^4-2/9*b^4*exp(2*b^2*x^2)/Pi/x^2+28/45*b^6*Ei(
2*b^2*x^2)/Pi+4/45*b^6*erfi(b*x)^2-1/6*erfi(b*x)^2/x^6-2/15*b*exp(b^2*x^2)*
erfi(b*x)/x^5/Pi^(1/2)-4/45*b^3*exp(b^2*x^2)*erfi(b*x)/x^3/Pi^(1/2)-8/45*b^
5*exp(b^2*x^2)*erfi(b*x)/x/Pi^(1/2)
```

Rubi [A]
time = 0.18, antiderivative size = 174, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.600$, Rules used = {6501, 6528, 6510, 30, 2241, 2245}

$$\frac{4}{45}b^6\mathrm{Erfi}(bx)^2-\frac{2be^{b^2x^2}\mathrm{Erfi}(bx)}{15\sqrt{\pi}\,x^5}-\frac{b^2e^{2b^2x^2}}{15\pi x^4}+\frac{28b^6\mathrm{Ei}(2b^2x^2)}{45\pi}-\frac{8b^5e^{b^2x^2}\mathrm{Erfi}(bx)}{45\sqrt{\pi}\,x}-\frac{2b^4e^{2b^2x^2}}{9\pi x^2}-\frac{4b^3e^{b^2x^2}\mathrm{Erfi}(bx)}{45\sqrt{\pi}\,x^3}-\frac{\mathrm{Erfi}(bx)^2}{6x^6}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]^2/x^7,x]
```

```
[Out] -1/15*(b^2*E^(2*b^2*x^2))/(Pi*x^4) - (2*b^4*E^(2*b^2*x^2))/(9*Pi*x^2) - (2*
b*E^(b^2*x^2)*Erfi[b*x])/(15*Sqrt[Pi]*x^5) - (4*b^3*E^(b^2*x^2)*Erfi[b*x])/
(45*Sqrt[Pi]*x^3) - (8*b^5*E^(b^2*x^2)*Erfi[b*x])/(45*Sqrt[Pi]*x) + (4*b^6*
Erfi[b*x]^2)/45 - Erfi[b*x]^2/(6*x^6) + (28*b^6*ExpIntegralEi[2*b^2*x^2])/(
45*Pi)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
```

```
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6501

```
Int[Erfi[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfi[b*x]^2
/(m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[x^(m + 1)*E^(b^2*x^2)*Er
fi[b*x], x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6528

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x
]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int \frac{\operatorname{erfi}(bx)^2}{x^7}\,dx &= -\frac{\operatorname{erfi}(bx)^2}{6x^6} + \frac{(2b)\int \frac{e^{b^2x^2}\operatorname{erfi}(bx)}{x^6}\,dx}{3\sqrt{\pi}} \\
&= -\frac{2be^{b^2x^2}\operatorname{erfi}(bx)}{15\sqrt{\pi}\,x^5} - \frac{\operatorname{erfi}(bx)^2}{6x^6} + \frac{(4b^2)\int \frac{e^{2b^2x^2}}{x^5}\,dx}{15\pi} + \frac{(4b^3)\int \frac{e^{b^2x^2}\operatorname{erfi}(bx)}{x^4}\,dx}{15\sqrt{\pi}} \\
&= -\frac{b^2e^{2b^2x^2}}{15\pi x^4} - \frac{2be^{b^2x^2}\operatorname{erfi}(bx)}{15\sqrt{\pi}\,x^5} - \frac{4b^3e^{b^2x^2}\operatorname{erfi}(bx)}{45\sqrt{\pi}\,x^3} - \frac{\operatorname{erfi}(bx)^2}{6x^6} + \frac{(8b^4)\int \frac{e^{2b^2x^2}}{x^3}\,dx}{45\pi} + \frac{(4b^4)\int \frac{e^{2b^2x^2}}{x^3}}{15\pi} \\
&= -\frac{b^2e^{2b^2x^2}}{15\pi x^4} - \frac{2b^4e^{2b^2x^2}}{9\pi x^2} - \frac{2be^{b^2x^2}\operatorname{erfi}(bx)}{15\sqrt{\pi}\,x^5} - \frac{4b^3e^{b^2x^2}\operatorname{erfi}(bx)}{45\sqrt{\pi}\,x^3} - \frac{8b^5e^{b^2x^2}\operatorname{erfi}(bx)}{45\sqrt{\pi}\,x} - \frac{\operatorname{erfi}(bx)^2}{6x^6} + \\
&= -\frac{b^2e^{2b^2x^2}}{15\pi x^4} - \frac{2b^4e^{2b^2x^2}}{9\pi x^2} - \frac{2be^{b^2x^2}\operatorname{erfi}(bx)}{15\sqrt{\pi}\,x^5} - \frac{4b^3e^{b^2x^2}\operatorname{erfi}(bx)}{45\sqrt{\pi}\,x^3} - \frac{8b^5e^{b^2x^2}\operatorname{erfi}(bx)}{45\sqrt{\pi}\,x} - \frac{\operatorname{erfi}(bx)^2}{6x^6} + \\
&= -\frac{b^2e^{2b^2x^2}}{15\pi x^4} - \frac{2b^4e^{2b^2x^2}}{9\pi x^2} - \frac{2be^{b^2x^2}\operatorname{erfi}(bx)}{15\sqrt{\pi}\,x^5} - \frac{4b^3e^{b^2x^2}\operatorname{erfi}(bx)}{45\sqrt{\pi}\,x^3} - \frac{8b^5e^{b^2x^2}\operatorname{erfi}(bx)}{45\sqrt{\pi}\,x} + \frac{4}{45}b^6\operatorname{erfi}(bx
\end{aligned}
$$

Mathematica [A]

time = 0.03, size = 114, normalized size = 0.66

$$\frac{-2b^2e^{2b^2x^2}x^2(3+10b^2x^2)-4be^{b^2x^2}\sqrt{\pi}\,x(3+2b^2x^2+4b^4x^4)\,\mathrm{Erfi}(bx)+\pi(-15+8b^6x^6)\,\mathrm{Erfi}(bx)^2+56b^6x^6\mathrm{Ei}(2b^2x^2)}{90\pi x^6}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]^2/x^7,x]
```

```
[Out] (-2*b^2*E^(2*b^2*x^2)*x^2*(3 + 10*b^2*x^2) - 4*b*E^(b^2*x^2)*Sqrt[Pi]*x*(3
+ 2*b^2*x^2 + 4*b^4*x^4)*Erfi[b*x] + Pi*(-15 + 8*b^6*x^6)*Erfi[b*x]^2 + 56*
b^6*x^6*ExpIntegralEi[2*b^2*x^2])/(90*Pi*x^6)
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{erfi}\left(bx\right)^{2}}{x^{7}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2/x^7,x)
```

```
[Out] int(erfi(b*x)^2/x^7,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^7,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)^2/x^7, x)
```

Fricas [A]
time = 0.38, size = 113, normalized size = 0.65

$$\frac{56\,b^6x^6\mathrm{Ei}(2\,b^2x^2)-4\,\sqrt{\pi}\,(4\,b^5x^5+2\,b^3x^3+3\,bx)\,\mathrm{erfi}\,(bx)\,e^{(b^2x^2)}-(15\,\pi-8\,\pi b^6x^6)\,\mathrm{erfi}\,(bx)^2-2\,(10\,b^4x^4+3\,b^2x^2)e^{(2\,b^2x^2)}}{90\,\pi x^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^7,x, algorithm="fricas")
```

```
[Out] 1/90*(56*b^6*x^6*Ei(2*b^2*x^2) - 4*sqrt(pi)*(4*b^5*x^5 + 2*b^3*x^3 + 3*b*x)
*erfi(b*x)*e^(b^2*x^2) - (15*pi - 8*pi*b^6*x^6)*erfi(b*x)^2 - 2*(10*b^4*x^4
 + 3*b^2*x^2)*e^(2*b^2*x^2))/(pi*x^6)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}^2(bx)}{x^7}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)**2/x**7,x)
```

```
[Out] Integral(erfi(b*x)**2/x**7, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^7,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)^2/x^7, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\operatorname{erfi}(b\,x)^2}{x^7}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2/x^7,x)
```

```
[Out] int(erfi(b*x)^2/x^7, x)
```

3.235 $\int x^4\mathbf{Erfi}(bx)^2\,dx$

Optimal. Leaf size=162

$$-\frac{11e^{2b^2x^2}x}{20b^4\pi}+\frac{e^{2b^2x^2}x^3}{5b^2\pi}-\frac{4e^{b^2x^2}\mathrm{Erfi}(bx)}{5b^5\sqrt{\pi}}+\frac{4e^{b^2x^2}x^2\mathrm{Erfi}(bx)}{5b^3\sqrt{\pi}}-\frac{2e^{b^2x^2}x^4\mathrm{Erfi}(bx)}{5b\sqrt{\pi}}+\frac{1}{5}x^5\mathrm{Erfi}(bx)^2+\frac{43\mathrm{Erfi}\left(\sqrt{2}\,bx\right)}{40b^5\sqrt{2\pi}}$$

```
[Out] -11/20*exp(2*b^2*x^2)*x/b^4/Pi+1/5*exp(2*b^2*x^2)*x^3/b^2/Pi+1/5*x^5*erfi(b
*x)^2-4/5*exp(b^2*x^2)*erfi(b*x)/b^5/Pi^(1/2)+4/5*exp(b^2*x^2)*x^2*erfi(b*x
)/b^3/Pi^(1/2)-2/5*exp(b^2*x^2)*x^4*erfi(b*x)/b/Pi^(1/2)+43/80*erfi(b*x*2^(
1/2))/b^5*2^(1/2)/Pi^(1/2)
```

Rubi [A]
time = 0.15, antiderivative size = 162, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}}=0.500$, Rules used = {6501, 6522, 6519, 2235, 2243}

$$\frac{43\mathrm{Erfi}\left(\sqrt{2}\,bx\right)}{40\sqrt{2\pi}\,b^5}-\frac{2x^4e^{b^2x^2}\mathrm{Erfi}(bx)}{5\sqrt{\pi}\,b}+\frac{x^3e^{2b^2x^2}}{5\pi b^2}-\frac{4e^{b^2x^2}\mathrm{Erfi}(bx)}{5\sqrt{\pi}\,b^5}-\frac{11xe^{2b^2x^2}}{20\pi b^4}+\frac{4x^2e^{b^2x^2}\mathrm{Erfi}(bx)}{5\sqrt{\pi}\,b^3}+\frac{1}{5}x^5\mathrm{Erfi}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[x^4*Erfi[b*x]^2,x]
```

```
[Out] (-11*E^(2*b^2*x^2)*x)/(20*b^4*Pi) + (E^(2*b^2*x^2)*x^3)/(5*b^2*Pi) - (4*E^(
b^2*x^2)*Erfi[b*x])/(5*b^5*Sqrt[Pi]) + (4*E^(b^2*x^2)*x^2*Erfi[b*x])/(5*b^3
*Sqrt[Pi]) - (2*E^(b^2*x^2)*x^4*Erfi[b*x])/(5*b*Sqrt[Pi]) + (x^5*Erfi[b*x]^
2)/5 + (43*Erfi[Sqrt[2]*b*x])/(40*b^5*Sqrt[2*Pi])
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6501

```
Int[Erfi[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfi[b*x]^2
/(m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[x^(m + 1)*E^(b^2*x^2)*Er
```

```
fi[b*x], x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$
\begin{aligned}
\int x^4\operatorname{erfi}(bx)^2\,dx &= \frac{1}{5}x^5\operatorname{erfi}(bx)^2-\frac{(4b)\int e^{b^2x^2}x^5\operatorname{erfi}(bx)\,dx}{5\sqrt{\pi}}\\
&= -\frac{2e^{b^2x^2}x^4\operatorname{erfi}(bx)}{5b\sqrt{\pi}}+\frac{1}{5}x^5\operatorname{erfi}(bx)^2+\frac{4\int e^{2b^2x^2}x^4\,dx}{5\pi}+\frac{8\int e^{b^2x^2}x^3\operatorname{erfi}(bx)\,dx}{5b\sqrt{\pi}}\\
&= \frac{e^{2b^2x^2}x^3}{5b^2\pi}+\frac{4e^{b^2x^2}x^2\operatorname{erfi}(bx)}{5b^3\sqrt{\pi}}-\frac{2e^{b^2x^2}x^4\operatorname{erfi}(bx)}{5b\sqrt{\pi}}+\frac{1}{5}x^5\operatorname{erfi}(bx)^2-\frac{3\int e^{2b^2x^2}x^2\,dx}{5b^2\pi}-\frac{8\int e^{2b^2}}{5b}\\
&= -\frac{11e^{2b^2x^2}x}{20b^4\pi}+\frac{e^{2b^2x^2}x^3}{5b^2\pi}-\frac{4e^{b^2x^2}\operatorname{erfi}(bx)}{5b^5\sqrt{\pi}}+\frac{4e^{b^2x^2}x^2\operatorname{erfi}(bx)}{5b^3\sqrt{\pi}}-\frac{2e^{b^2x^2}x^4\operatorname{erfi}(bx)}{5b\sqrt{\pi}}+\frac{1}{5}x^5\operatorname{erfi}(b\\
&= -\frac{11e^{2b^2x^2}x}{20b^4\pi}+\frac{e^{2b^2x^2}x^3}{5b^2\pi}-\frac{4e^{b^2x^2}\operatorname{erfi}(bx)}{5b^5\sqrt{\pi}}+\frac{4e^{b^2x^2}x^2\operatorname{erfi}(bx)}{5b^3\sqrt{\pi}}-\frac{2e^{b^2x^2}x^4\operatorname{erfi}(bx)}{5b\sqrt{\pi}}+\frac{1}{5}x^5\operatorname{erfi}(b
\end{aligned}
$$

Mathematica [A]
time = 0.03, size = 105, normalized size = 0.65

$$\frac{4be^{2b^2x^2}x(-11+4b^2x^2)-32e^{b^2x^2}\sqrt{\pi}\,(2-2b^2x^2+b^4x^4)\operatorname{Erfi}(bx)+16b^5\pi x^5\operatorname{Erfi}(bx)^2+43\sqrt{2\pi}\operatorname{Erfi}\left(\sqrt{2}\,bx\right)}{80b^5\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^4*Erfi[b*x]^2,x]
```

```
[Out] (4*b*E^(2*b^2*x^2)*x*(-11 + 4*b^2*x^2) - 32*E^(b^2*x^2)*Sqrt[Pi]*(2 - 2*b^2
*x^2 + b^4*x^4)*Erfi[b*x] + 16*b^5*Pi*x^5*Erfi[b*x]^2 + 43*Sqrt[2*Pi]*Erfi[
Sqrt[2]*b*x])/(80*b^5*Pi)
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int x^4 \operatorname{erfi}(bx)^2 \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erfi(b*x)^2,x)
```

```
[Out] int(x^4*erfi(b*x)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfi(b*x)^2,x, algorithm="maxima")
```

```
[Out] integrate(x^4*erfi(b*x)^2, x)
```

Fricas [A]
time = 0.37, size = 110, normalized size = 0.68

$$\frac{16\,\pi b^6 x^5 \operatorname{erfi}(bx)^2 - 32\,\sqrt{\pi}\,(b^5x^4 - 2\,b^3x^2 + 2\,b)\operatorname{erfi}(bx)\,e^{(b^2x^2)} + 43\,\sqrt{2}\,\sqrt{\pi}\,\sqrt{b^2}\,\operatorname{erfi}\left(\sqrt{2}\,\sqrt{b^2}\,x\right) + 4\,(4\,b^4x^3 - 11\,b^2x)e^{(2\,b^2x^2)}}{80\,\pi b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfi(b*x)^2,x, algorithm="fricas")
```

```
[Out] 1/80*(16*pi*b^6*x^5*erfi(b*x)^2 - 32*sqrt(pi)*(b^5*x^4 - 2*b^3*x^2 + 2*b)*e
rfi(b*x)*e^(b^2*x^2) + 43*sqrt(2)*sqrt(pi)*sqrt(b^2)*erfi(sqrt(2)*sqrt(b^2)
*x) + 4*(4*b^4*x^3 - 11*b^2*x)*e^(2*b^2*x^2))/(pi*b^6)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x^4 \operatorname{erfi}^2(bx)\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4*erfi(b*x)**2,x)
```

```
[Out] Integral(x**4*erfi(b*x)**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfi(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(x^4*erfi(b*x)^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^4 \operatorname{erfi}(b\,x)^2\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erfi(b*x)^2,x)
```

```
[Out] int(x^4*erfi(b*x)^2, x)
```

3.236 $\int x^2 \mathbf{Erfi}(bx)^2\, dx$

Optimal. Leaf size=111

$$\frac{e^{2b^2x^2}x}{3b^2\pi}+\frac{2e^{b^2x^2}\text{Erfi}(bx)}{3b^3\sqrt{\pi}}-\frac{2e^{b^2x^2}x^2\text{Erfi}(bx)}{3b\sqrt{\pi}}+\frac{1}{3}x^3\text{Erfi}(bx)^2-\frac{5\text{Erfi}\left(\sqrt{2}\,bx\right)}{6b^3\sqrt{2\pi}}$$

```
[Out] 1/3*exp(2*b^2*x^2)*x/b^2/Pi+1/3*x^3*erfi(b*x)^2+2/3*exp(b^2*x^2)*erfi(b*x)/
b^3/Pi^(1/2)-2/3*exp(b^2*x^2)*x^2*erfi(b*x)/b/Pi^(1/2)-5/12*erfi(b*x*2^(1/2
))/b^3*2^(1/2)/Pi^(1/2)
```

Rubi [A]
time = 0.09, antiderivative size = 111, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.500$, Rules used = {6501, 6522, 6519, 2235, 2243}

$$-\frac{5\text{Erfi}\left(\sqrt{2}\,bx\right)}{6\sqrt{2\pi}\,b^3}-\frac{2x^2e^{b^2x^2}\text{Erfi}(bx)}{3\sqrt{\pi}\,b}+\frac{xe^{2b^2x^2}}{3\pi b^2}+\frac{2e^{b^2x^2}\text{Erfi}(bx)}{3\sqrt{\pi}\,b^3}+\frac{1}{3}x^3\text{Erfi}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[x^2*Erfi[b*x]^2,x]
```

```
[Out] (E^(2*b^2*x^2)*x)/(3*b^2*Pi) + (2*E^(b^2*x^2)*Erfi[b*x])/(3*b^3*Sqrt[Pi]) -
 (2*E^(b^2*x^2)*x^2*Erfi[b*x])/(3*b*Sqrt[Pi]) + (x^3*Erfi[b*x]^2)/3 - (5*Er
fi[Sqrt[2]*b*x])/(6*b^3*Sqrt[2*Pi])
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6501

```
Int[Erfi[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfi[b*x]^2
/(m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[x^(m + 1)*E^(b^2*x^2)*Er
```

```
fi[b*x], x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$
\begin{aligned}
\int x^2\text{erfi}(bx)^2\,dx &= \frac{1}{3}x^3\text{erfi}(bx)^2 - \frac{(4b)\int e^{b^2x^2}x^3\text{erfi}(bx)\,dx}{3\sqrt{\pi}} \\
&= -\frac{2e^{b^2x^2}x^2\text{erfi}(bx)}{3b\sqrt{\pi}} + \frac{1}{3}x^3\text{erfi}(bx)^2 + \frac{4\int e^{2b^2x^2}x^2\,dx}{3\pi} + \frac{4\int e^{b^2x^2}x\text{erfi}(bx)\,dx}{3b\sqrt{\pi}} \\
&= \frac{e^{2b^2x^2}x}{3b^2\pi} + \frac{2e^{b^2x^2}\text{erfi}(bx)}{3b^3\sqrt{\pi}} - \frac{2e^{b^2x^2}x^2\text{erfi}(bx)}{3b\sqrt{\pi}} + \frac{1}{3}x^3\text{erfi}(bx)^2 - \frac{\int e^{2b^2x^2}\,dx}{3b^2\pi} - \frac{4\int e^{2b^2x^2}\,dx}{3b^2\pi} \\
&= \frac{e^{2b^2x^2}x}{3b^2\pi} + \frac{2e^{b^2x^2}\text{erfi}(bx)}{3b^3\sqrt{\pi}} - \frac{2e^{b^2x^2}x^2\text{erfi}(bx)}{3b\sqrt{\pi}} + \frac{1}{3}x^3\text{erfi}(bx)^2 - \frac{\sqrt{\frac{2}{\pi}}\,\text{erfi}\left(\sqrt{2}\,bx\right)}{3b^3} - \frac{\text{erfi}\left(\sqrt{\right.}}{6b^3\sqrt{}}
\end{aligned}
$$

Mathematica [A]
time = 0.02, size = 87, normalized size = 0.78

$$\frac{4be^{2b^2x^2}x - 8e^{b^2x^2}\sqrt{\pi}\,(-1+b^2x^2)\,\text{Erfi}(bx) + 4b^3\pi x^3\text{Erfi}(bx)^2 - 5\sqrt{2\pi}\,\text{Erfi}\left(\sqrt{2}\,bx\right)}{12b^3\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*Erfi[b*x]^2,x]
```

```
[Out] (4*b*E^(2*b^2*x^2)*x - 8*E^(b^2*x^2)*Sqrt[Pi]*(-1 + b^2*x^2)*Erfi[b*x] + 4*
b^3*Pi*x^3*Erfi[b*x]^2 - 5*Sqrt[2*Pi]*Erfi[Sqrt[2]*b*x])/(12*b^3*Pi)
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int x^2 \operatorname{erfi}(bx)^2 \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfi(b*x)^2,x)
```

```
[Out] int(x^2*erfi(b*x)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfi(b*x)^2,x, algorithm="maxima")
```

```
[Out] integrate(x^2*erfi(b*x)^2, x)
```

Fricas [A]
time = 0.36, size = 91, normalized size = 0.82

$$\frac{4\,\pi b^4 x^3 \operatorname{erfi}(bx)^2 + 4\,b^2 x e^{(2\,b^2x^2)} - 8\,\sqrt{\pi}\,(b^3x^2 - b)\operatorname{erfi}(bx)\,e^{(b^2x^2)} - 5\,\sqrt{2}\,\sqrt{\pi}\,\sqrt{b^2}\,\operatorname{erfi}\left(\sqrt{2}\,\sqrt{b^2}\,x\right)}{12\,\pi b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfi(b*x)^2,x, algorithm="fricas")
```

```
[Out] 1/12*(4*pi*b^4*x^3*erfi(b*x)^2 + 4*b^2*x*e^(2*b^2*x^2) - 8*sqrt(pi)*(b^3*x^
2 - b)*erfi(b*x)*e^(b^2*x^2) - 5*sqrt(2)*sqrt(pi)*sqrt(b^2)*erfi(sqrt(2)*sq
rt(b^2)*x))/(pi*b^4)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x^2 \operatorname{erfi}^2(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*erfi(b*x)**2,x)
```

```
[Out] Integral(x**2*erfi(b*x)**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfi(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(x^2*erfi(b*x)^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^2 \operatorname{erfi}(b\,x)^2\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfi(b*x)^2,x)
```

```
[Out] int(x^2*erfi(b*x)^2, x)
```

3.237 $\int \mathbf{Erfi}(bx)^2\,dx$

Optimal. Leaf size=54

$$-\frac{2e^{b^2x^2}\text{Erfi}(bx)}{b\sqrt{\pi}}+x\text{Erfi}(bx)^2+\frac{\sqrt{\frac{2}{\pi}}\,\text{Erfi}\left(\sqrt{2}\,bx\right)}{b}$$

```
[Out] x*erfi(b*x)^2+erfi(b*x*2^(1/2))*2^(1/2)/Pi^(1/2)/b-2*exp(b^2*x^2)*erfi(b*x)
/b/Pi^(1/2)
```

Rubi [A]
time = 0.03, antiderivative size = 54, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.667, Rules used = {6489, 12, 6519, 2235}

$$-\frac{2e^{b^2x^2}\text{Erfi}(bx)}{\sqrt{\pi}\,b}+x\text{Erfi}(bx)^2+\frac{\sqrt{\frac{2}{\pi}}\,\text{Erfi}\left(\sqrt{2}\,bx\right)}{b}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]^2,x]
```

```
[Out] (-2*E^(b^2*x^2)*Erfi[b*x])/(b*Sqrt[Pi]) + x*Erfi[b*x]^2 + (Sqrt[2/Pi]*Erfi[
Sqrt[2]*b*x])/b
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] &&  !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6489

```
Int[Erfi[(a_.) + (b_.)*(x_)]^2, x_Symbol] :> Simp[(a + b*x)*(Erfi[a + b*x]^
2/b), x] - Dist[4/Sqrt[Pi], Int[(a + b*x)*E^(a + b*x)^2*Erfi[a + b*x], x],
x] /; FreeQ[{a, b}, x]
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
```

```
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\int \operatorname{erfi}(bx)^2\,dx = x\operatorname{erfi}(bx)^2 - \frac{4\int be^{b^2x^2}x\operatorname{erfi}(bx)\,dx}{\sqrt{\pi}}$$
$$= x\operatorname{erfi}(bx)^2 - \frac{(4b)\int e^{b^2x^2}x\operatorname{erfi}(bx)\,dx}{\sqrt{\pi}}$$
$$= -\frac{2e^{b^2x^2}\operatorname{erfi}(bx)}{b\sqrt{\pi}} + x\operatorname{erfi}(bx)^2 + \frac{4\int e^{2b^2x^2}\,dx}{\pi}$$
$$= -\frac{2e^{b^2x^2}\operatorname{erfi}(bx)}{b\sqrt{\pi}} + x\operatorname{erfi}(bx)^2 + \frac{\sqrt{\frac{2}{\pi}}\operatorname{erfi}\left(\sqrt{2}\,bx\right)}{b}$$

Mathematica [A]
time = 0.01, size = 54, normalized size = 1.00

$$-\frac{2e^{b^2x^2}\operatorname{Erfi}(bx)}{b\sqrt{\pi}} + x\operatorname{Erfi}(bx)^2 + \frac{\sqrt{\frac{2}{\pi}}\operatorname{Erfi}\left(\sqrt{2}\,bx\right)}{b}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]^2,x]
[Out] (-2*E^(b^2*x^2)*Erfi[b*x])/(b*Sqrt[Pi]) + x*Erfi[b*x]^2 + (Sqrt[2/Pi]*Erfi[
Sqrt[2]*b*x])/b
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int \operatorname{erfi}(bx)^2\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2,x)
[Out] int(erfi(b*x)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)^2, x)
```

Fricas [A]
time = 0.36, size = 61, normalized size = 1.13

$$\frac{\pi b^2 x \operatorname{erfi}(bx)^2 - 2\sqrt{\pi}\, b \operatorname{erfi}(bx)\, e^{(b^2x^2)} + \sqrt{2}\sqrt{\pi}\sqrt{b^2} \operatorname{erfi}\left(\sqrt{2}\sqrt{b^2}\, x\right)}{\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2,x, algorithm="fricas")
```

```
[Out] (pi*b^2*x*erfi(b*x)^2 - 2*sqrt(pi)*b*erfi(b*x)*e^(b^2*x^2) + sqrt(2)*sqrt(p
i)*sqrt(b^2)*erfi(sqrt(2)*sqrt(b^2)*x))/(pi*b^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \operatorname{erfi}^2(bx)\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)**2,x)
```

```
[Out] Integral(erfi(b*x)**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \operatorname{erfi}(b\,x)^2\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2,x)
```

```
[Out] int(erfi(b*x)^2, x)
```

3.238 $\int \frac{\mathrm{Erfi}(bx)^2}{x^2}\,dx$

Optimal. Leaf size=13

$$\mathrm{Int}\left(\frac{\mathrm{Erfi}(bx)^2}{x^2},x\right)$$

```
[Out] Unintegrable(erfi(b*x)^2/x^2,x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\mathrm{Erfi}(bx)^2}{x^2}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erfi[b*x]^2/x^2,x]
```

```
[Out] Defer[Int][Erfi[b*x]^2/x^2, x]
```

Rubi steps

$$\int \frac{\mathrm{erfi}(bx)^2}{x^2}\,dx = \int \frac{\mathrm{erfi}(bx)^2}{x^2}\,dx$$

Mathematica [A]
time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{Erfi}(bx)^2}{x^2}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfi[b*x]^2/x^2,x]
```

```
[Out] Integrate[Erfi[b*x]^2/x^2, x]
```

Maple [A]
time = 0.02, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{erfi}\left(bx\right)^2}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2/x^2,x)
```

```
[Out] int(erfi(b*x)^2/x^2,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^2,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)^2/x^2, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^2,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x)^2/x^2, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}^{2}\left(bx\right)}{x^{2}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)**2/x**2,x)
```

```
[Out] Integral(erfi(b*x)**2/x**2, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^2,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)^2/x^2, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.08

$$\int \frac{{\mathrm{erfi}\left(b\,x\right)}^2}{x^2} \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2/x^2,x)
[Out] int(erfi(b*x)^2/x^2, x)
```

3.239 $\int \frac{\mathbf{Erfi}(bx)^2}{x^4}\,dx$

Optimal. Leaf size=13

$$\text{Int}\left(\frac{\text{Erfi}(bx)^2}{x^4},x\right)$$

```
[Out] Unintegrable(erfi(b*x)^2/x^4,x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\text{Erfi}(bx)^2}{x^4}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erfi[b*x]^2/x^4,x]
```

```
[Out] Defer[Int][Erfi[b*x]^2/x^4, x]
```

Rubi steps

$$\int \frac{\text{erfi}(bx)^2}{x^4}\,dx = \int \frac{\text{erfi}(bx)^2}{x^4}\,dx$$

Mathematica [A]
time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{\text{Erfi}(bx)^2}{x^4}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfi[b*x]^2/x^4,x]
```

```
[Out] Integrate[Erfi[b*x]^2/x^4, x]
```

Maple [A]
time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{\text{erfi}\left(bx\right)^2}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2/x^4,x)
```

```
[Out] int(erfi(b*x)^2/x^4,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^4,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)^2/x^4, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^4,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x)^2/x^4, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}^{2}(bx)}{x^{4}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)**2/x**4,x)
```

```
[Out] Integral(erfi(b*x)**2/x**4, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^4,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)^2/x^4, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.08

$$\int \frac{\mathrm{erfi}(b\,x)^2}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2/x^4,x)
```

```
[Out] int(erfi(b*x)^2/x^4, x)
```

3.240 $\int \frac{\mathbf{Erfi}(bx)^2}{x^6}\,dx$

Optimal. Leaf size=13

$$\operatorname{Int}\left(\frac{\operatorname{Erfi}(bx)^2}{x^6},x\right)$$

```
[Out] Unintegrable(erfi(b*x)^2/x^6,x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\operatorname{Erfi}(bx)^2}{x^6}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erfi[b*x]^2/x^6,x]
```

```
[Out] Defer[Int][Erfi[b*x]^2/x^6, x]
```

Rubi steps

$$\int \frac{\operatorname{erfi}(bx)^2}{x^6}\,dx = \int \frac{\operatorname{erfi}(bx)^2}{x^6}\,dx$$

Mathematica [A]
time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{Erfi}(bx)^2}{x^6}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfi[b*x]^2/x^6,x]
```

```
[Out] Integrate[Erfi[b*x]^2/x^6, x]
```

Maple [A]
time = 0.03, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}\left(bx\right)^2}{x^6}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2/x^6,x)
```

```
[Out] int(erfi(b*x)^2/x^6,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^6,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)^2/x^6, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^6,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x)^2/x^6, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}^{2}(bx)}{x^{6}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)**2/x**6,x)
```

```
[Out] Integral(erfi(b*x)**2/x**6, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)^2/x^6,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)^2/x^6, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.08

$$\int \frac{\operatorname{erfi}(b\,x)^2}{x^6}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)^2/x^6,x)
[Out] int(erfi(b*x)^2/x^6, x)
```

3.241 $\int (c+dx)^2 \mathbf{Erfi}(a+bx)^2\, dx$

Optimal. Leaf size=366

$$\frac{d(bc-ad)e^{2(a+bx)^2}}{b^3\pi}+\frac{d^2e^{2(a+bx)^2}(a+bx)}{3b^3\pi}+\frac{2d^2e^{(a+bx)^2}\mathrm{Erfi}(a+bx)}{3b^3\sqrt{\pi}}-\frac{2(bc-ad)^2e^{(a+bx)^2}\mathrm{Erfi}(a+bx)}{b^3\sqrt{\pi}}-\frac{2d(bc-$$

```
[Out] d*(-a*d+b*c)*exp(2*(b*x+a)^2)/b^3/Pi+1/3*d^2*exp(2*(b*x+a)^2)*(b*x+a)/b^3/P
i+1/2*d*(-a*d+b*c)*erfi(b*x+a)^2/b^3+(-a*d+b*c)^2*(b*x+a)*erfi(b*x+a)^2/b^3
+d*(-a*d+b*c)*(b*x+a)^2*erfi(b*x+a)^2/b^3+1/3*d^2*(b*x+a)^3*erfi(b*x+a)^2/b
^3+(-a*d+b*c)^2*erfi((b*x+a)*2^(1/2))*2^(1/2)/Pi^(1/2)/b^3+2/3*d^2*exp((b*x
+a)^2)*erfi(b*x+a)/b^3/Pi^(1/2)-2*(-a*d+b*c)^2*exp((b*x+a)^2)*erfi(b*x+a)/b
^3/Pi^(1/2)-2*d*(-a*d+b*c)*exp((b*x+a)^2)*(b*x+a)*erfi(b*x+a)/b^3/Pi^(1/2)-
2/3*d^2*exp((b*x+a)^2)*(b*x+a)^2*erfi(b*x+a)/b^3/Pi^(1/2)-5/12*d^2*erfi((b*
x+a)*2^(1/2))/b^3*2^(1/2)/Pi^(1/2)
```

Rubi [A]
time = 0.24, antiderivative size = 366, normalized size of antiderivative = 1.00, number of steps used = 16, number of rules used = 10, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {6504, 6489, 6519, 2235, 6501, 6522, 6510, 30, 2240, 2243}

$$\frac{d(a+bx)^2(bc-ad)\mathrm{Erfi}(a+bx)^2}{b^3}+\frac{(a+bx)(bc-ad)^2\mathrm{Erfi}(a+bx)^2}{b^3}-\frac{2de^{(a+bx)^2}(a+bx)(bc-ad)\mathrm{Erfi}(a+bx)}{\sqrt{\pi}b^3}+\frac{d(bc-ad)\mathrm{Erfi}(a+bx)^2}{2b^3}-\frac{2e^{(a+bx)^2}(bc-ad)^2\mathrm{Erfi}(a+bx)}{\sqrt{\pi}b^3}+\frac{\sqrt{\frac{2}{\pi}}(bc-ad)^2\mathrm{Erfi}\left(\sqrt{2}(a+bx)\right)}{b^3}+\frac{de^{2(a+bx)^2}(bc-ad)}{\pi b^3}+\frac{d^2(a+bx)^3\mathrm{Erfi}(a+bx)^2}{3b^3}-\frac{2d^2e^{(a+bx)^2}(a+bx)^2\mathrm{Erfi}(a+bx)}{3\sqrt{\pi}b^3}+\frac{2d^2e^{(a+bx)^2}\mathrm{Erfi}(a+bx)}{3\sqrt{\pi}b^3}-\frac{5d^2\mathrm{Erfi}\left(\sqrt{2}(a+bx)\right)}{6\sqrt{2\pi}b^3}+\frac{d^2e^{2(a+bx)^2}(a+bx)}{3\pi b^3}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)^2*Erfi[a + b*x]^2,x]
```

```
[Out] (d*(b*c - a*d)*E^(2*(a + b*x)^2))/(b^3*Pi) + (d^2*E^(2*(a + b*x)^2)*(a + b*
x))/(3*b^3*Pi) + (2*d^2*E^(a + b*x)^2*Erfi[a + b*x])/(3*b^3*Sqrt[Pi]) - (2*
(b*c - a*d)^2*E^(a + b*x)^2*Erfi[a + b*x])/(b^3*Sqrt[Pi]) - (2*d*(b*c - a*d
)*E^(a + b*x)^2*(a + b*x)*Erfi[a + b*x])/(b^3*Sqrt[Pi]) - (2*d^2*E^(a + b*x
)^2*(a + b*x)^2*Erfi[a + b*x])/(3*b^3*Sqrt[Pi]) + (d*(b*c - a*d)*Erfi[a + b
*x]^2)/(2*b^3) + ((b*c - a*d)^2*(a + b*x)*Erfi[a + b*x]^2)/b^3 + (d*(b*c -
a*d)*(a + b*x)^2*Erfi[a + b*x]^2)/b^3 + (d^2*(a + b*x)^3*Erfi[a + b*x]^2)/(
3*b^3) + ((b*c - a*d)^2*Sqrt[2/Pi]*Erfi[Sqrt[2]*(a + b*x)])/b^3 - (5*d^2*Er
fi[Sqrt[2]*(a + b*x)])/(6*b^3*Sqrt[2*Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
```

```
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6489

```
Int[Erfi[(a_.) + (b_.)*(x_)]^2, x_Symbol] :> Simp[(a + b*x)*(Erfi[a + b*x]^
2/b), x] - Dist[4/Sqrt[Pi], Int[(a + b*x)*E^(a + b*x)^2*Erfi[a + b*x], x],
x] /; FreeQ[{a, b}, x]
```

Rule 6501

```
Int[Erfi[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfi[b*x]^2
/(m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[x^(m + 1)*E^(b^2*x^2)*Er
fi[b*x], x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6504

```
Int[Erfi[(a_) + (b_.)*(x_)]^2*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Dist
[1/b^(m + 1), Subst[Int[ExpandIntegrand[Erfi[x]^2, (b*c - a*d + d*x)^m, x],
 x], x, a + b*x], x] /; FreeQ[{a, b, c, d}, x] && IGtQ[m, 0]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
```

```
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\int (c+dx)^2 \text{erfi}(a+bx)^2\,dx = \frac{\text{Subst}\left(\int \left(b^2c^2\left(1+\frac{ad(-2bc+ad)}{b^2c^2}\right)\text{erfi}(x)^2+2bcd\left(1-\frac{ad}{bc}\right)x\text{erfi}(x)^2+d^2x^2\text{erfi}(
}{b^3}$$

$$= \frac{d^2\text{Subst}\left(\int x^2\text{erfi}(x)^2\,dx,x,a+bx\right)}{b^3}+\frac{(2d(bc-ad))\text{Subst}\left(\int x\text{erfi}(x)^2\,dx,x,a
}{b^3}$$

$$= \frac{(bc-ad)^2(a+bx)\text{erfi}(a+bx)^2}{b^3}+\frac{d(bc-ad)(a+bx)^2\text{erfi}(a+bx)^2}{b^3}+\frac{d^2(a+
}{}$$

$$= -\frac{2(bc-ad)^2e^{(a+bx)^2}\text{erfi}(a+bx)}{b^3\sqrt{\pi}}-\frac{2d(bc-ad)e^{(a+bx)^2}(a+bx)\text{erfi}(a+bx)}{b^3\sqrt{\pi}}-$$

$$= \frac{d(bc-ad)e^{2(a+bx)^2}}{b^3\pi}+\frac{d^2e^{2(a+bx)^2}(a+bx)}{3b^3\pi}+\frac{2d^2e^{(a+bx)^2}\text{erfi}(a+bx)}{3b^3\sqrt{\pi}}-\frac{2(bc-
}{}$$

$$= \frac{d(bc-ad)e^{2(a+bx)^2}}{b^3\pi}+\frac{d^2e^{2(a+bx)^2}(a+bx)}{3b^3\pi}+\frac{2d^2e^{(a+bx)^2}\text{erfi}(a+bx)}{3b^3\sqrt{\pi}}-\frac{2(bc-
}{}$$

Mathematica [F]
time = 0.35, size = 0, normalized size = 0.00

$$\int (c+dx)^2\text{Erfi}(a+bx)^2\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(c + d*x)^2*Erfi[a + b*x]^2,x]
[Out] Integrate[(c + d*x)^2*Erfi[a + b*x]^2, x]
```

Maple [F]
time = 0.22, size = 0, normalized size = 0.00

$$\int (dx+c)^2\,\text{erfi}\,(bx+a)^2\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)^2*erfi(b*x+a)^2,x)
```

```
[Out] int((d*x+c)^2*erfi(b*x+a)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erfi(b*x+a)^2,x, algorithm="maxima")
```

```
[Out] integrate((d*x + c)^2*erfi(b*x + a)^2, x)
```

Fricas [A]
time = 0.38, size = 278, normalized size = 0.76

$$\frac{\sqrt{2}\,\sqrt{\pi}\,(12\,b^2c^2-24\,abcd+(12\,a^2-5)d^2)\sqrt{b^2}\,\operatorname{erfi}\left(\frac{\sqrt{2}\,\sqrt{b^2}\,(bx+a)}{b}\right)-8\,\sqrt{\pi}\,(b^3d^2x^2+3\,b^3c^2-3\,ab^2cd+(a^2-1)bd^2+(3\,b^3cd-ab^2d^2)x)\operatorname{erfi}\left(bx+a\right)e^{(b^2x^2+2\,abx+a^2)}+2\,(2\,\pi b^4d^2x^3+6\,\pi b^4cdx^2+6\,\pi b^4c^2x+\pi(6\,ab^3c^2-3\,(2\,a^2-1)b^2cd+(2\,a^3-3\,a)bd^2))\operatorname{erfi}\left(bx+a\right)^2+4\,(b^2d^2x+3\,b^2cd-2\,abd^2)e^{(2\,b^2x^2+4\,abx+2\,a^2)}}{12\,\pi b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erfi(b*x+a)^2,x, algorithm="fricas")
```

```
[Out] 1/12*(sqrt(2)*sqrt(pi)*(12*b^2*c^2 - 24*a*b*c*d + (12*a^2 - 5)*d^2)*sqrt(b^
2)*erfi(sqrt(2)*sqrt(b^2)*(b*x + a)/b) - 8*sqrt(pi)*(b^3*d^2*x^2 + 3*b^3*c^
2 - 3*a*b^2*c*d + (a^2 - 1)*b*d^2 + (3*b^3*c*d - a*b^2*d^2)*x)*erfi(b*x + a
)*e^(b^2*x^2 + 2*a*b*x + a^2) + 2*(2*pi*b^4*d^2*x^3 + 6*pi*b^4*c*d*x^2 + 6*
pi*b^4*c^2*x + pi*(6*a*b^3*c^2 - 3*(2*a^2 - 1)*b^2*c*d + (2*a^3 - 3*a)*b*d^
2))*erfi(b*x + a)^2 + 4*(b^2*d^2*x + 3*b^2*c*d - 2*a*b*d^2)*e^(2*b^2*x^2 +
4*a*b*x + 2*a^2))/(pi*b^4)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \left(c+dx\right)^2\operatorname{erfi}^2\left(a+bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)**2*erfi(b*x+a)**2,x)
```

```
[Out] Integral((c + d*x)**2*erfi(a + b*x)**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)^2*erfi(b*x+a)^2,x, algorithm="giac")
```

```
[Out] integrate((d*x + c)^2*erfi(b*x + a)^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.00

$$\int \mathrm{erfi}(a+b\,x)^2\,{(c+d\,x)}^2\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(a + b*x)^2*(c + d*x)^2,x)
```

```
[Out] int(erfi(a + b*x)^2*(c + d*x)^2, x)
```

3.242 $\int (c+dx)\textbf{Erfi}(a+bx)^2\,dx$

Optimal. Leaf size=184

$$\frac{de^{2(a+bx)^2}}{2b^2\pi}-\frac{2(bc-ad)e^{(a+bx)^2}\mathrm{Erfi}(a+bx)}{b^2\sqrt{\pi}}-\frac{de^{(a+bx)^2}(a+bx)\mathrm{Erfi}(a+bx)}{b^2\sqrt{\pi}}+\frac{d\mathrm{Erfi}(a+bx)^2}{4b^2}+\frac{(bc-ad)(a+bx}{b^2}$$

```
[Out] 1/2*d*exp(2*(b*x+a)^2)/b^2/Pi+1/4*d*erfi(b*x+a)^2/b^2+(-a*d+b*c)*(b*x+a)*er
fi(b*x+a)^2/b^2+1/2*d*(b*x+a)^2*erfi(b*x+a)^2/b^2+(-a*d+b*c)*erfi((b*x+a)*2
^(1/2))*2^(1/2)/Pi^(1/2)/b^2-2*(-a*d+b*c)*exp((b*x+a)^2)*erfi(b*x+a)/b^2/Pi
^(1/2)-d*exp((b*x+a)^2)*(b*x+a)*erfi(b*x+a)/b^2/Pi^(1/2)
```

Rubi [A]
time = 0.11, antiderivative size = 184, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 9, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.643$, Rules used = {6504, 6489, 6519, 2235, 6501, 6522, 6510, 30, 2240}

$$\frac{(a+bx)(bc-ad)\mathrm{Erfi}(a+bx)^2}{b^2}-\frac{2e^{(a+bx)^2}(bc-ad)\mathrm{Erfi}(a+bx)}{\sqrt{\pi}\,b^2}+\frac{\sqrt{\frac{2}{\pi}}\,(bc-ad)\mathrm{Erfi}\left(\sqrt{2}\,(a+bx)\right)}{b^2}+\frac{d(a+bx)^2\mathrm{Erfi}(a+bx)^2}{2b^2}+\frac{d\mathrm{Erfi}(a+bx)^2}{4b^2}-\frac{de^{(a+bx)^2}(a+bx)\mathrm{Erfi}(a+bx)}{\sqrt{\pi}\,b^2}+\frac{de^{2(a+bx)^2}}{2\pi b^2}$$

Antiderivative was successfully verified.

```
[In] Int[(c + d*x)*Erfi[a + b*x]^2,x]
```

```
[Out] (d*E^(2*(a + b*x)^2))/(2*b^2*Pi) - (2*(b*c - a*d)*E^(a + b*x)^2*Erfi[a + b*
x])/(b^2*Sqrt[Pi]) - (d*E^(a + b*x)^2*(a + b*x)*Erfi[a + b*x])/(b^2*Sqrt[Pi
]) + (d*Erfi[a + b*x]^2)/(4*b^2) + ((b*c - a*d)*(a + b*x)*Erfi[a + b*x]^2)/
b^2 + (d*(a + b*x)^2*Erfi[a + b*x]^2)/(2*b^2) + ((b*c - a*d)*Sqrt[2/Pi]*Erf
i[Sqrt[2]*(a + b*x)])/b^2
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 6489

```
Int[Erfi[(a_.) + (b_.)*(x_)]^2, x_Symbol] :> Simp[(a + b*x)*(Erfi[a + b*x]^
2/b), x] - Dist[4/Sqrt[Pi], Int[(a + b*x)*E^(a + b*x)^2*Erfi[a + b*x], x],
x] /; FreeQ[{a, b}, x]
```

Rule 6501

```
Int[Erfi[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)*(Erfi[b*x]^2
/(m + 1)), x] - Dist[4*(b/(Sqrt[Pi]*(m + 1))), Int[x^(m + 1)*E^(b^2*x^2)*Er
fi[b*x], x], x] /; FreeQ[b, x] && (IGtQ[m, 0] || ILtQ[(m + 1)/2, 0])
```

Rule 6504

```
Int[Erfi[(a_) + (b_.)*(x_)]^2*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Dist
[1/b^(m + 1), Subst[Int[ExpandIntegrand[Erfi[x]^2, (b*c - a*d + d*x)^m, x],
 x], x, a + b*x], x] /; FreeQ[{a, b, c, d}, x] && IGtQ[m, 0]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\int (c+dx)\text{erfi}(a+bx)^2\,dx = \frac{\text{Subst}\left(\int \left(bc\left(1-\frac{ad}{bc}\right)\text{erfi}(x)^2 + dx\text{erfi}(x)^2\right)\,dx, x, a+bx\right)}{b^2}$$

$$= \frac{d\text{Subst}\left(\int x\text{erfi}(x)^2\,dx, x, a+bx\right)}{b^2} + \frac{(bc-ad)\text{Subst}\left(\int \text{erfi}(x)^2\,dx, x, a+bx\right)}{b^2}$$

$$= \frac{(bc-ad)(a+bx)\text{erfi}(a+bx)^2}{b^2} + \frac{d(a+bx)^2\text{erfi}(a+bx)^2}{2b^2} - \frac{(2d)\text{Subst}\left(\int e^{x^2}x^2 e\right.}{b^2}$$

$$= -\frac{2(bc-ad)e^{(a+bx)^2}\text{erfi}(a+bx)}{b^2\sqrt{\pi}} - \frac{de^{(a+bx)^2}(a+bx)\text{erfi}(a+bx)}{b^2\sqrt{\pi}} + \frac{(bc-ad)(a}{}$$

$$= \frac{de^{2(a+bx)^2}}{2b^2\pi} - \frac{2(bc-ad)e^{(a+bx)^2}\text{erfi}(a+bx)}{b^2\sqrt{\pi}} - \frac{de^{(a+bx)^2}(a+bx)\text{erfi}(a+bx)}{b^2\sqrt{\pi}} + \frac{(b}{}$$

$$= \frac{de^{2(a+bx)^2}}{2b^2\pi} - \frac{2(bc-ad)e^{(a+bx)^2}\text{erfi}(a+bx)}{b^2\sqrt{\pi}} - \frac{de^{(a+bx)^2}(a+bx)\text{erfi}(a+bx)}{b^2\sqrt{\pi}} + \frac{de}{}$$

Mathematica [C] Result contains complex when optimal does not.
time = 0.96, size = 189, normalized size = 1.03

$$\frac{(4abc+d-2a^2d)\,\pi\text{Erfc}(-i(a+bx))\text{Erfc}(i(a+bx)) + 2\left(de^{2(a+bx)^2} + 4abc\pi + d\pi - 2a^2d\pi + 2ibc\sqrt{2\pi} - 2iad\sqrt{2\pi} - 2e^{(a+bx)^2}\sqrt{\pi}\,(2bc-ad+bdx)\text{Erfi}(a+bx) + b^2\pi x(2c+dx)\text{Erfi}(a+bx)^2 + 2(bc-ad)\sqrt{2\pi}\,\text{Erfi}\left(\sqrt{2}\,(a+bx)\right)\right)}{4b^2\pi}$$

Antiderivative was successfully verified.

```
[In] Integrate[(c + d*x)*Erfi[a + b*x]^2,x]
```

```
[Out] ((4*a*b*c + d - 2*a^2*d)*Pi*Erfc[(-I)*(a + b*x)]*Erfc[I*(a + b*x)] + 2*(d*E
^(2*(a + b*x)^2) + 4*a*b*c*Pi + d*Pi - 2*a^2*d*Pi + (2*I)*b*c*Sqrt[2*Pi] -
(2*I)*a*d*Sqrt[2*Pi] - 2*E^(a + b*x)^2*Sqrt[Pi]*(2*b*c - a*d + b*d*x)*Erfi[
a + b*x] + b^2*Pi*x*(2*c + d*x)*Erfi[a + b*x]^2 + 2*(b*c - a*d)*Sqrt[2*Pi]*
Erfi[Sqrt[2]*(a + b*x)]))/(4*b^2*Pi)
```

Maple [F]
time = 0.04, size = 0, normalized size = 0.00

$$\int (dx+c)\,\text{erfi}\,(bx+a)^2\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((d*x+c)*erfi(b*x+a)^2,x)
```

```
[Out] int((d*x+c)*erfi(b*x+a)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfi(b*x+a)^2,x, algorithm="maxima")
```

```
[Out] integrate((d*x + c)*erfi(b*x + a)^2, x)
```

Fricas [A]
time = 0.35, size = 167, normalized size = 0.91

$$\frac{4\sqrt{2}\sqrt{\pi}\sqrt{b^2}(bc-ad)\operatorname{erfi}\left(\frac{\sqrt{2}\sqrt{b^2}(bx+a)}{b}\right)-4\sqrt{\pi}(b^2dx+2b^2c-abd)\operatorname{erfi}(bx+a)e^{(b^2x^2+2abx+a^2)}+(2\pi b^3dx^2+4\pi b^3cx+\pi(4ab^2c-(2a^2-1)bd))\operatorname{erfi}(bx+a)^2+2bde^{(2b^2x^2+4abx+2a^2)}}{4\pi b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfi(b*x+a)^2,x, algorithm="fricas")
```

```
[Out] 1/4*(4*sqrt(2)*sqrt(pi)*sqrt(b^2)*(b*c - a*d)*erfi(sqrt(2)*sqrt(b^2)*(b*x +
 a)/b) - 4*sqrt(pi)*(b^2*d*x + 2*b^2*c - a*b*d)*erfi(b*x + a)*e^(b^2*x^2 +
2*a*b*x + a^2) + (2*pi*b^3*d*x^2 + 4*pi*b^3*c*x + pi*(4*a*b^2*c - (2*a^2 -
1)*b*d))*erfi(b*x + a)^2 + 2*b*d*e^(2*b^2*x^2 + 4*a*b*x + 2*a^2))/(pi*b^3)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int(c+dx)\operatorname{erfi}^2(a+bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfi(b*x+a)**2,x)
```

```
[Out] Integral((c + d*x)*erfi(a + b*x)**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((d*x+c)*erfi(b*x+a)^2,x, algorithm="giac")
```

```
[Out] integrate((d*x + c)*erfi(b*x + a)^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int\operatorname{erfi}(a+b\,x)^2\,(c+d\,x)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(a + b*x)^2*(c + d*x),x)
[Out] int(erfi(a + b*x)^2*(c + d*x), x)
```

3.243 $\int \text{Erfi}(a+bx)^2 \, dx$

Optimal. Leaf size=68

$$-\frac{2e^{(a+bx)^2}\text{Erfi}(a+bx)}{b\sqrt{\pi}}+\frac{(a+bx)\text{Erfi}(a+bx)^2}{b}+\frac{\sqrt{\frac{2}{\pi}}\,\text{Erfi}\left(\sqrt{2}\,(a+bx)\right)}{b}$$

```
[Out] (b*x+a)*erfi(b*x+a)^2/b+erfi((b*x+a)*2^(1/2))*2^(1/2)/Pi^(1/2)/b-2*exp((b*x
+a)^2)*erfi(b*x+a)/b/Pi^(1/2)
```

Rubi [A]
time = 0.09, antiderivative size = 68, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.375$, Rules used = {6489, 6519, 2235}

$$\frac{(a+bx)\text{Erfi}(a+bx)^2}{b}-\frac{2e^{(a+bx)^2}\text{Erfi}(a+bx)}{\sqrt{\pi}\,b}+\frac{\sqrt{\frac{2}{\pi}}\,\text{Erfi}\left(\sqrt{2}\,(a+bx)\right)}{b}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[a + b*x]^2,x]
```

```
[Out] (-2*E^(a + b*x)^2*Erfi[a + b*x])/(b*Sqrt[Pi]) + ((a + b*x)*Erfi[a + b*x]^2)
/b + (Sqrt[2/Pi]*Erfi[Sqrt[2]*(a + b*x)])/b
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6489

```
Int[Erfi[(a_.) + (b_.)*(x_)]^2, x_Symbol] :> Simp[(a + b*x)*(Erfi[a + b*x]^
2/b), x] - Dist[4/Sqrt[Pi], Int[(a + b*x)*E^(a + b*x)^2*Erfi[a + b*x], x],
x] /; FreeQ[{a, b}, x]
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\int \operatorname{erfi}(a+bx)^2\,dx = \frac{(a+bx)\operatorname{erfi}(a+bx)^2}{b} - \frac{4\int e^{(a+bx)^2}(a+bx)\operatorname{erfi}(a+bx)\,dx}{\sqrt{\pi}}$$
$$= \frac{(a+bx)\operatorname{erfi}(a+bx)^2}{b} - \frac{4\mathrm{Subst}\left(\int e^{x^2}x\operatorname{erfi}(x)\,dx,x,a+bx\right)}{b\sqrt{\pi}}$$
$$= -\frac{2e^{(a+bx)^2}\operatorname{erfi}(a+bx)}{b\sqrt{\pi}} + \frac{(a+bx)\operatorname{erfi}(a+bx)^2}{b} + \frac{4\mathrm{Subst}\left(\int e^{2x^2}\,dx,x,a+bx\right)}{b\pi}$$
$$= -\frac{2e^{(a+bx)^2}\operatorname{erfi}(a+bx)}{b\sqrt{\pi}} + \frac{(a+bx)\operatorname{erfi}(a+bx)^2}{b} + \frac{\sqrt{\frac{2}{\pi}}\operatorname{erfi}\left(\sqrt{2}\,(a+bx)\right)}{b}$$

Mathematica [A]
time = 0.02, size = 64, normalized size = 0.94

$$\frac{-2e^{(a+bx)^2}\mathrm{Erfi}(a+bx)+\sqrt{\pi}\,(a+bx)\mathrm{Erfi}(a+bx)^2+\sqrt{2}\,\mathrm{Erfi}\left(\sqrt{2}\,(a+bx)\right)}{b\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[a + b*x]^2,x]
[Out] (-2*E^(a + b*x)^2*Erfi[a + b*x] + Sqrt[Pi]*(a + b*x)*Erfi[a + b*x]^2 + Sqrt
[2]*Erfi[Sqrt[2]*(a + b*x)])/(b*Sqrt[Pi])
```

Maple [F]
time = 0.02, size = 0, normalized size = 0.00

$$\int \operatorname{erfi}(bx+a)^2\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x+a)^2,x)
[Out] int(erfi(b*x+a)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)^2,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x + a)^2, x)
```

Fricas [A]
time = 0.41, size = 90, normalized size = 1.32

$$-\frac{2\sqrt{\pi}\,b\operatorname{erfi}\left(bx+a\right)e^{\left(b^{2}x^{2}+2\,abx+a^{2}\right)}-\left(\pi b^{2}x+\pi ab\right)\operatorname{erfi}\left(bx+a\right)^{2}-\sqrt{2}\,\sqrt{\pi}\,\sqrt{b^{2}}\,\operatorname{erfi}\left(\frac{\sqrt{2}\,\sqrt{b^{2}}\,(bx+a)}{b}\right)}{\pi b^{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)^2,x, algorithm="fricas")
```

```
[Out] -(2*sqrt(pi)*b*erfi(b*x + a)*e^(b^2*x^2 + 2*a*b*x + a^2) - (pi*b^2*x + pi*a
*b)*erfi(b*x + a)^2 - sqrt(2)*sqrt(pi)*sqrt(b^2)*erfi(sqrt(2)*sqrt(b^2)*(b*
x + a)/b))/(pi*b^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \operatorname{erfi}^{2}\left(a+bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)**2,x)
```

```
[Out] Integral(erfi(a + b*x)**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)^2,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x + a)^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \operatorname{erfi}(a+b\,x)^2\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(a + b*x)^2,x)
```

```
[Out] int(erfi(a + b*x)^2, x)
```

3.244 $\int \frac{\mathbf{Erfi}(a+bx)^2}{c+dx}\,dx$

Optimal. Leaf size=19

$$\mathrm{Int}\left(\frac{\mathrm{Erfi}(a+bx)^2}{c+dx},x\right)$$

```
[Out] Unintegrable(erfi(b*x+a)^2/(d*x+c),x)
```

Rubi [A]
time = 0.02, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\mathrm{Erfi}(a+bx)^2}{c+dx}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erfi[a + b*x]^2/(c + d*x),x]
```

```
[Out] Defer[Int][Erfi[a + b*x]^2/(c + d*x), x]
```

Rubi steps

$$\int \frac{\mathrm{erfi}(a+bx)^2}{c+dx}\,dx = \int \frac{\mathrm{erfi}(a+bx)^2}{c+dx}\,dx$$

Mathematica [A]
time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{Erfi}(a+bx)^2}{c+dx}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfi[a + b*x]^2/(c + d*x),x]
```

```
[Out] Integrate[Erfi[a + b*x]^2/(c + d*x), x]
```

Maple [A]
time = 0.22, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{erfi}\left(bx+a\right)^2}{dx+c}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x+a)^2/(d*x+c),x)
[Out] int(erfi(b*x+a)^2/(d*x+c),x)
```

Maxima [**A**]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)^2/(d*x+c),x, algorithm="maxima")
[Out] integrate(erfi(b*x + a)^2/(d*x + c), x)
```

Fricas [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)^2/(d*x+c),x, algorithm="fricas")
[Out] integral(erfi(b*x + a)^2/(d*x + c), x)
```

Sympy [**A**]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}^{2}\left(a + bx\right)}{c + dx}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)**2/(d*x+c),x)
[Out] Integral(erfi(a + b*x)**2/(c + d*x), x)
```

Giac [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)^2/(d*x+c),x, algorithm="giac")
[Out] integrate(erfi(b*x + a)^2/(d*x + c), x)
```

Mupad [**A**]
time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{{\mathrm{erfi}\left(a+b\,x\right)}^2}{c+d\,x} \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(a + b*x)^2/(c + d*x),x)
```

```
[Out] int(erfi(a + b*x)^2/(c + d*x), x)
```

3.245 $\int \frac{\text{Erfi}(a+bx)^2}{(c+dx)^2} dx$

Optimal. Leaf size=19

$$\text{Int}\left(\frac{\text{Erfi}(a+bx)^2}{(c+dx)^2},x\right)$$

```
[Out] Unintegrable(erfi(b*x+a)^2/(d*x+c)^2,x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{\text{Erfi}(a+bx)^2}{(c+dx)^2}\,dx$$

Verification is not applicable to the result.

```
[In] Int[Erfi[a + b*x]^2/(c + d*x)^2,x]
[Out] Defer[Int][Erfi[a + b*x]^2/(c + d*x)^2, x]
```

Rubi steps

$$\int \frac{\text{erfi}(a+bx)^2}{(c+dx)^2}\,dx = \int \frac{\text{erfi}(a+bx)^2}{(c+dx)^2}\,dx$$

Mathematica [A]
time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{\text{Erfi}(a+bx)^2}{(c+dx)^2}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfi[a + b*x]^2/(c + d*x)^2,x]
[Out] Integrate[Erfi[a + b*x]^2/(c + d*x)^2, x]
```

Maple [A]
time = 0.22, size = 0, normalized size = 0.00

$$\int \frac{\text{erfi}\left(bx+a\right)^{2}}{\left(dx+c\right)^{2}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x+a)^2/(d*x+c)^2,x)
```

```
[Out] int(erfi(b*x+a)^2/(d*x+c)^2,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)^2/(d*x+c)^2,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x + a)^2/(d*x + c)^2, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)^2/(d*x+c)^2,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x + a)^2/(d^2*x^2 + 2*c*d*x + c^2), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}^{2}\left(a + bx\right)}{\left(c + dx\right)^{2}}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)**2/(d*x+c)**2,x)
```

```
[Out] Integral(erfi(a + b*x)**2/(c + d*x)**2, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x+a)^2/(d*x+c)^2,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x + a)^2/(d*x + c)^2, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{{\mathrm{erfi}\left(a+b\,x\right)}^2}{{\left(c+d\,x\right)}^2} \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(a + b*x)^2/(c + d*x)^2,x)
[Out] int(erfi(a + b*x)^2/(c + d*x)^2, x)
```

3.246 $\int x^2 \mathbf{Erfi}(d(a+b\log(cx^n)))\,dx$

Optimal. Leaf size=102

$$\frac{1}{3}x^3\text{Erfi}(d(a+b\log(cx^n)))-\frac{1}{3}e^{-\frac{3(3+4abd^2n)}{4b^2d^2n^2}}x^3(cx^n)^{-3/n}\,\text{Erfi}\left(\frac{2abd^2+\frac{3}{n}+2b^2d^2\log(cx^n)}{2bd}\right)$$

```
[Out] 1/3*x^3*erfi(d*(a+b*ln(c*x^n)))-1/3*x^3*erfi(1/2*(2*a*b*d^2+3/n+2*b^2*d^2*l
n(c*x^n))/b/d)/exp(3/4*(4*a*b*d^2*n+3)/b^2/d^2/n^2)/((c*x^n)^(3/n))
```

Rubi [A]
time = 0.11, antiderivative size = 102, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}}=0.294$, Rules used = {6538, 2314, 2308, 2266, 2235}

$$\frac{1}{3}x^3\text{Erfi}(d(a+b\log(cx^n)))-\frac{1}{3}x^3(cx^n)^{-3/n}\,e^{-\frac{3(4abd^2n+3)}{4b^2d^2n^2}}\text{Erfi}\left(\frac{2abd^2+2b^2d^2\log(cx^n)+\frac{3}{n}}{2bd}\right)$$

Antiderivative was successfully verified.

```
[In] Int[x^2*Erfi[d*(a + b*Log[c*x^n])],x]
```

```
[Out] (x^3*Erfi[d*(a + b*Log[c*x^n])])/3 - (x^3*Erfi[(2*a*b*d^2 + 3/n + 2*b^2*d^2
*Log[c*x^n])/(2*b*d)])/(3*E^((3*(3 + 4*a*b*d^2*n))/(4*b^2*d^2*n^2))*(c*x^n)
^(3/n))
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2314

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^m*((c*(d + e*x)^n)^(2
*a*b*f*Log[F])/(d + e*x)^(m + 2*a*b*f*n*Log[F])), Int[(d + e*x)^(m + 2*a*b*
f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2), x], x] /; FreeQ[{F, a,
b, c, d, e, f, g, h, m, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 6538

```
Int[Erfi[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_))^(m_.), x
_Symbol] :> Simp[(e*x)^(m + 1)*(Erfi[d*(a + b*Log[c*x^n])]/(e*(m + 1))), x]
 - Dist[2*b*d*(n/(Sqrt[Pi]*(m + 1))), Int[(e*x)^m*E^(d*(a + b*Log[c*x^n]))^
2, x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int x^2\mathrm{erfi}(d(a+b\log(cx^n)))\,dx &= \frac{1}{3}x^3\mathrm{erfi}(d(a+b\log(cx^n))) - \frac{(2bdn)\int e^{d^2(a+b\log(cx^n))^2}x^2\,dx}{3\sqrt{\pi}}\\ &= \frac{1}{3}x^3\mathrm{erfi}(d(a+b\log(cx^n))) - \frac{(2bdn)\int \exp\left(a^2d^2+2abd^2\log(cx^n)+b^2d^2\right.}{3\sqrt{\pi}}\\ &= \frac{1}{3}x^3\mathrm{erfi}(d(a+b\log(cx^n))) - \frac{(2bdn)\int e^{a^2d^2+b^2d^2\log^2(cx^n)}x^2(cx^n)^{2abd^2}\,dx}{3\sqrt{\pi}}\\ &= \frac{1}{3}x^3\mathrm{erfi}(d(a+b\log(cx^n))) - \frac{\left(2bdnx^{-2abd^2n}(cx^n)^{2abd^2}\right)\int e^{a^2d^2+b^2d^2\log^2(cx^n}}{3\sqrt{\pi}}\\ &= \frac{1}{3}x^3\mathrm{erfi}(d(a+b\log(cx^n))) - \frac{\left(2bdx^3(cx^n)^{2abd^2-\frac{3+2abd^2n}{n}}\right)\mathrm{Subst}\left(\int\exp\left(a\right.\right.}{3\sqrt{}}\\ &= \frac{1}{3}x^3\mathrm{erfi}(d(a+b\log(cx^n))) - \frac{\left(2bde^{-\frac{3(3+4abd^2n)}{4b^2d^2n^2}}x^3(cx^n)^{2abd^2-\frac{3+2abd^2n}{n}}\right)\mathrm{Sub}}{3}\\ &= \frac{1}{3}x^3\mathrm{erfi}(d(a+b\log(cx^n))) - \frac{1}{3}e^{-\frac{3(3+4abd^2n)}{4b^2d^2n^2}}x^3(cx^n)^{-3/n}\,\mathrm{erfi}\left(\frac{2abd^2+\frac{3}{n}+}{2}\right.\end{aligned}$$

Mathematica [A]
time = 0.23, size = 90, normalized size = 0.88

$$\frac{1}{3}\left(x^3\mathrm{Erfi}(d(a+b\log(cx^n))) - e^{-\frac{3(3+4abd^2n)}{4b^2d^2n^2}}x^3(cx^n)^{-3/n}\,\mathrm{Erfi}\left(ad+\frac{3}{2bdn}+bd\log(cx^n)\right)\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*Erfi[d*(a + b*Log[c*x^n])],x]
[Out] (x^3*Erfi[d*(a + b*Log[c*x^n])] - (x^3*Erfi[a*d + 3/(2*b*d*n) + b*d*Log[c*x
^n]])/(E^((3*(3 + 4*a*b*d^2*n))/(4*b^2*d^2*n^2))*(c*x^n)^(3/n)))/3
```

Maple [F]
time = 0.13, size = 0, normalized size = 0.00

$$\int x^2 \operatorname{erfi}\left(d(a+b\ln\left(c\,x^n\right))\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfi(d*(a+b*ln(c*x^n))),x)
[Out] int(x^2*erfi(d*(a+b*ln(c*x^n))),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfi(d*(a+b*log(c*x^n))),x, algorithm="maxima")
[Out] integrate(x^2*erfi((b*log(c*x^n) + a)*d), x)
```

Fricas [A]
time = 0.38, size = 125, normalized size = 1.23

$$\frac{1}{3}\,x^3\operatorname{erfi}\left(bd\log\left(cx^n\right)+ad\right)-\frac{1}{3}\,\sqrt{b^2d^2n^2}\,\operatorname{erfi}\left(\frac{\left(2\,b^2d^2n^2\log\left(x\right)+2\,b^2d^2n\log\left(c\right)+2\,abd^2n+3\right)\sqrt{b^2d^2n^2}}{2\,b^2d^2n^2}\right)e^{\left(-\frac{3\,\left(4\,b^2d^2n\log\left(c\right)+4\,abd^2n+3\right)}{4\,b^2d^2n^2}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfi(d*(a+b*log(c*x^n))),x, algorithm="fricas")
[Out] 1/3*x^3*erfi(b*d*log(c*x^n) + a*d) - 1/3*sqrt(b^2*d^2*n^2)*erfi(1/2*(2*b^2*
d^2*n^2*log(x) + 2*b^2*d^2*n*log(c) + 2*a*b*d^2*n + 3)*sqrt(b^2*d^2*n^2)/(b
^2*d^2*n^2))*e^(-3/4*(4*b^2*d^2*n*log(c) + 4*a*b*d^2*n + 3)/(b^2*d^2*n^2))
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x^2\operatorname{erfi}\left(ad+bd\log\left(cx^n\right)\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*erfi(d*(a+b*ln(c*x**n))),x)
```

```
[Out] Integral(x**2*erfi(a*d + b*d*log(c*x**n)), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfi(d*(a+b*log(c*x^n))),x, algorithm="giac")
[Out] integrate(x^2*erfi((b*log(c*x^n) + a)*d), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^2\,\mathrm{erfi}(d\,(a+b\,\ln(c\,x^n)))\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfi(d*(a + b*log(c*x^n))),x)
[Out] int(x^2*erfi(d*(a + b*log(c*x^n))), x)
```

3.247 $\int x\text{Erfi}(d(a+b\log(cx^n)))\,dx$

Optimal. Leaf size=93

$$\frac{1}{2}x^2\text{Erfi}(d(a+b\log(cx^n)))-\frac{1}{2}e^{-\frac{1+2abd^2n}{b^2d^2n^2}}x^2(cx^n)^{-2/n}\,\text{Erfi}\left(\frac{abd^2+\frac{1}{n}+b^2d^2\log(cx^n)}{bd}\right)$$

[Out] 1/2*x^2*erfi(d*(a+b*ln(c*x^n)))-1/2*x^2*erfi((a*b*d^2+1/n+b^2*d^2*ln(c*x^n))/b/d)/exp((2*a*b*d^2*n+1)/b^2/d^2/n^2)/((c*x^n)^(2/n))

Rubi [A]

time = 0.10, antiderivative size = 93, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.333, Rules used = {6538, 2314, 2308, 2266, 2235}

$$\frac{1}{2}x^2\text{Erfi}(d(a+b\log(cx^n)))-\frac{1}{2}x^2(cx^n)^{-2/n}\,e^{-\frac{2abd^2n+1}{b^2d^2n^2}}\,\text{Erfi}\left(\frac{abd^2+b^2d^2\log(cx^n)+\frac{1}{n}}{bd}\right)$$

Antiderivative was successfully verified.

[In] Int[x*Erfi[d*(a + b*Log[c*x^n])],x]

[Out] (x^2*Erfi[d*(a + b*Log[c*x^n])])/2 - (x^2*Erfi[(a*b*d^2 + n^(-1) + b^2*d^2*Log[c*x^n])/(b*d)])/(2*E^((1 + 2*a*b*d^2*n)/(b^2*d^2*n^2))*(c*x^n)^(2/n))

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2314

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^m*((c*(d + e*x)^n)^(2
```

```
*a*b*f*Log[F])/(d + e*x)^(m + 2*a*b*f*n*Log[F])), Int[(d + e*x)^(m + 2*a*b*
f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2), x], x] /; FreeQ[{F, a,
b, c, d, e, f, g, h, m, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 6538

```
Int[Erfi[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_))^(m_.), x
_Symbol] :> Simp[(e*x)^(m + 1)*(Erfi[d*(a + b*Log[c*x^n])]/(e*(m + 1))), x]
 - Dist[2*b*d*(n/(Sqrt[Pi]*(m + 1))), Int[(e*x)^m*E^(d*(a + b*Log[c*x^n]))^
2, x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int x\text{erfi}(d(a+b\log(cx^n)))\,dx &= \frac{1}{2}x^2\text{erfi}(d(a+b\log(cx^n))) - \frac{(bdn)\int e^{d^2(a+b\log(cx^n))^2}x\,dx}{\sqrt{\pi}} \\
&= \frac{1}{2}x^2\text{erfi}(d(a+b\log(cx^n))) - \frac{(bdn)\int \exp\left(a^2d^2+2abd^2\log(cx^n)+b^2d^2\log\right.}{\sqrt{\pi}} \\
&= \frac{1}{2}x^2\text{erfi}(d(a+b\log(cx^n))) - \frac{(bdn)\int e^{a^2d^2+b^2d^2\log^2(cx^n)}x(cx^n)^{2abd^2}\,dx}{\sqrt{\pi}} \\
&= \frac{1}{2}x^2\text{erfi}(d(a+b\log(cx^n))) - \frac{\left(bdnx^{-2abd^2n}(cx^n)^{2abd^2}\right)\int e^{a^2d^2+b^2d^2\log^2(cx^n)}x}{\sqrt{\pi}} \\
&= \frac{1}{2}x^2\text{erfi}(d(a+b\log(cx^n))) - \frac{\left(bdx^2(cx^n)^{2abd^2-\frac{2+2abd^2n}{n}}\right)\text{Subst}\left(\int \exp\left(a^2d\right.\right.}{\sqrt{\pi}} \\
&= \frac{1}{2}x^2\text{erfi}(d(a+b\log(cx^n))) - \frac{\left(bde^{-\frac{1+2abd^2n}{b^2d^2n^2}}x^2(cx^n)^{2abd^2-\frac{2+2abd^2n}{n}}\right)\text{Subst}\left(\right.}{\sqrt{\pi}} \\
&= \frac{1}{2}x^2\text{erfi}(d(a+b\log(cx^n))) - \frac{1}{2}e^{-\frac{1+2abd^2n}{b^2d^2n^2}}x^2(cx^n)^{-2/n}\text{erfi}\left(\frac{abd^2+\frac{1}{n}+b^2d^2}{bd}\right.
\end{aligned}$$

Mathematica [A]
time = 0.22, size = 81, normalized size = 0.87

$$\frac{1}{2}\left(x^2\text{Erfi}(d(a+b\log(cx^n))) - e^{-\frac{\frac{\frac{1}{d^2}+2abn}{b^2}+2n\log(cx^n)}{n^2}}x^2\text{Erfi}\left(ad+\frac{1}{bdn}+bd\log(cx^n)\right)\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x*Erfi[d*(a + b*Log[c*x^n])],x]
```

```
[Out] (x^2*Erfi[d*(a + b*Log[c*x^n])] - (x^2*Erfi[a*d + 1/(b*d*n) + b*d*Log[c*x^n
]])/E^(((d^(-2) + 2*a*b*n)/b^2 + 2*n*Log[c*x^n])/n^2))/2
```

Maple [F]
time = 0.13, size = 0, normalized size = 0.00

$$\int x \,\mathrm{erfi}\left(d(a+b\ln\left(c\,x^{n}\right))\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfi(d*(a+b*ln(c*x^n))),x)
[Out] int(x*erfi(d*(a+b*ln(c*x^n))),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(d*(a+b*log(c*x^n))),x, algorithm="maxima")
[Out] integrate(x*erfi((b*log(c*x^n) + a)*d), x)
```

Fricas [A]
time = 0.38, size = 121, normalized size = 1.30

$$\frac{1}{2}\,x^{2}\,\mathrm{erfi}\left(bd\log\left(cx^{n}\right)+ad\right)-\frac{1}{2}\,\sqrt{b^{2}d^{2}n^{2}}\,\mathrm{erfi}\left(\frac{\left(b^{2}d^{2}n^{2}\log\left(x\right)+b^{2}d^{2}n\log\left(c\right)+abd^{2}n+1\right)\sqrt{b^{2}d^{2}n^{2}}}{b^{2}d^{2}n^{2}}\right)e^{\left(-\frac{2\,b^{2}d^{2}n\log\left(c\right)+2\,abd^{2}n+1}{b^{2}d^{2}n^{2}}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(d*(a+b*log(c*x^n))),x, algorithm="fricas")
[Out] 1/2*x^2*erfi(b*d*log(c*x^n) + a*d) - 1/2*sqrt(b^2*d^2*n^2)*erfi((b^2*d^2*n^
2*log(x) + b^2*d^2*n*log(c) + a*b*d^2*n + 1)*sqrt(b^2*d^2*n^2)/(b^2*d^2*n^2
))*e^(-(2*b^2*d^2*n*log(c) + 2*a*b*d^2*n + 1)/(b^2*d^2*n^2))
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int x\,\mathrm{erfi}\left(ad+bd\log\left(cx^{n}\right)\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(d*(a+b*ln(c*x**n))),x)
[Out] Integral(x*erfi(a*d + b*d*log(c*x**n)), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(d*(a+b*log(c*x^n))),x, algorithm="giac")
[Out] integrate(x*erfi((b*log(c*x^n) + a)*d), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x\,\mathrm{erfi}(d\,(a+b\,\ln\left(c\,x^n\right)))\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfi(d*(a + b*log(c*x^n))),x)
[Out] int(x*erfi(d*(a + b*log(c*x^n))), x)
```

3.248 $\int \mathbf{Erfi}(d(a+b\log(cx^n)))\,dx$

Optimal. Leaf size=91

$$x\text{Erfi}(d(a+b\log(cx^n)))-e^{-\frac{1+4abd^2n}{4b^2d^2n^2}}x(cx^n)^{-1/n}\,\text{Erfi}\left(\frac{2abd^2+\frac{1}{n}+2b^2d^2\log(cx^n)}{2bd}\right)$$

```
[Out] x*erfi(d*(a+b*ln(c*x^n)))-x*erfi(1/2*(2*a*b*d^2+1/n+2*b^2*d^2*ln(c*x^n))/b/
d)/exp(1/4*(4*a*b*d^2*n+1)/b^2/d^2/n^2)/((c*x^n)^(1/n))
```

Rubi [A]
time = 0.09, antiderivative size = 91, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {6534, 2312, 2308, 2266, 2235}

$$x\text{Erfi}(d(a+b\log(cx^n)))-x(cx^n)^{-1/n}\,e^{-\frac{4abd^2n+1}{4b^2d^2n^2}}\,\text{Erfi}\left(\frac{2abd^2+2b^2d^2\log(cx^n)+\frac{1}{n}}{2bd}\right)$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[d*(a + b*Log[c*x^n])],x]
```

```
[Out] x*Erfi[d*(a + b*Log[c*x^n])] - (x*Erfi[(2*a*b*d^2 + n^(-1) + 2*b^2*d^2*Log[
c*x^n])/(2*b*d)])/(E^((1 + 4*a*b*d^2*n)/(4*b^2*d^2*n^2))*(c*x^n)^n^(-1))
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2312

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.)), x
_Symbol] :> Dist[(c*(d + e*x)^n)^(2*a*b*f*Log[F])/(d + e*x)^(2*a*b*f*n*Log[
```

```
F]), Int[(d + e*x)^(2*a*b*f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2
), x], x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] &&  !IntegerQ[2*a*b*f*Log[F
]]
```

Rule 6534

```
Int[Erfi[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)], x_Symbol] :> Simp[x*
Erfi[d*(a + b*Log[c*x^n])], x] - Dist[2*b*d*(n/Sqrt[Pi]), Int[E^(d*(a + b*L
og[c*x^n]))^2, x], x] /; FreeQ[{a, b, c, d, n}, x]
```

Rubi steps

$$\int \operatorname{erfi}(d(a+b\log(cx^n)))\,dx = x\operatorname{erfi}(d(a+b\log(cx^n))) - \frac{(2bdn)\int e^{d^2(a+b\log(cx^n))^2}\,dx}{\sqrt{\pi}}$$
$$= x\operatorname{erfi}(d(a+b\log(cx^n))) - \frac{(2bdn)\int \exp\left(a^2d^2+2abd^2\log(cx^n)+b^2d^2\log^2(\right.}{\sqrt{\pi}}$$
$$= x\operatorname{erfi}(d(a+b\log(cx^n))) - \frac{(2bdn)\int e^{a^2d^2+b^2d^2\log^2(cx^n)}(cx^n)^{2abd^2}\,dx}{\sqrt{\pi}}$$
$$= x\operatorname{erfi}(d(a+b\log(cx^n))) - \frac{\left(2bdnx^{-2abd^2n}(cx^n)^{2abd^2}\right)\int e^{a^2d^2+b^2d^2\log^2(cx^n)}x^{2abd}}{\sqrt{\pi}}$$
$$= x\operatorname{erfi}(d(a+b\log(cx^n))) - \frac{\left(2bdx(cx^n)^{2abd^2-\frac{1+2abd^2n}{n}}\right)\operatorname{Subst}\left(\int \exp\left(a^2d^2+\right.\right.}{\sqrt{\pi}}$$
$$= x\operatorname{erfi}(d(a+b\log(cx^n))) - \frac{\left(2bde^{-\frac{1+4abd^2n}{4b^2d^2n^2}}x(cx^n)^{2abd^2-\frac{1+2abd^2n}{n}}\right)\operatorname{Subst}\left(\int \exp\right.}{\sqrt{\pi}}$$
$$= x\operatorname{erfi}(d(a+b\log(cx^n))) - e^{-\frac{1+4abd^2n}{4b^2d^2n^2}}x(cx^n)^{-1/n}\operatorname{erfi}\left(\frac{2abd^2+\frac{1}{n}+2b^2d^2\log(}{2bd}\right.$$

Mathematica [A]
time = 0.19, size = 78, normalized size = 0.86

$$x\operatorname{Erfi}(d(a+b\log(cx^n))) - e^{-\frac{\frac{\frac{1}{d^2}+4abn}{b^2}+4n\log(cx^n)}{4n^2}}x\operatorname{Erfi}\left(ad+\frac{1}{2bdn}+bd\log(cx^n)\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[d*(a + b*Log[c*x^n])],x]
```

```
[Out] x*Erfi[d*(a + b*Log[c*x^n])] - (x*Erfi[a*d + 1/(2*b*d*n) + b*d*Log[c*x^n]])
/E^(((d^(-2) + 4*a*b*n)/b^2 + 4*n*Log[c*x^n])/(4*n^2))
```

Maple [F]
time = 0.06, size = 0, normalized size = 0.00

$$\int \operatorname{erfi}\left(d(a+b\ln\left(c\,x^{n}\right))\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(d*(a+b*ln(c*x^n))),x)
```

```
[Out] int(erfi(d*(a+b*ln(c*x^n))),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(d*(a+b*log(c*x^n))),x, algorithm="maxima")
```

```
[Out] integrate(erfi((b*log(c*x^n) + a)*d), x)
```

Fricas [A]
time = 0.36, size = 122, normalized size = 1.34

$$-\sqrt{b^2d^2n^2}\,\operatorname{erfi}\left(\frac{\left(2\,b^2d^2n^2\log\left(x\right)+2\,b^2d^2n\log\left(c\right)+2\,abd^2n+1\right)\sqrt{b^2d^2n^2}}{2\,b^2d^2n^2}\right)e^{\left(-\frac{4\,b^2d^2n\log(c)+4\,abd^2n+1}{4\,b^2d^2n^2}\right)}+x\operatorname{erfi}\left(bd\log\left(cx^n\right)+ad\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(d*(a+b*log(c*x^n))),x, algorithm="fricas")
```

```
[Out] -sqrt(b^2*d^2*n^2)*erfi(1/2*(2*b^2*d^2*n^2*log(x) + 2*b^2*d^2*n*log(c) + 2*
a*b*d^2*n + 1)*sqrt(b^2*d^2*n^2)/(b^2*d^2*n^2))*e^(-1/4*(4*b^2*d^2*n*log(c)
 + 4*a*b*d^2*n + 1)/(b^2*d^2*n^2)) + x*erfi(b*d*log(c*x^n) + a*d)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \operatorname{erfi}\left(d\left(a+b\log\left(cx^{n}\right)\right)\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(d*(a+b*ln(c*x**n))),x)
```

```
[Out] Integral(erfi(d*(a + b*log(c*x**n))), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(d*(a+b*log(c*x^n))),x, algorithm="giac")
[Out] integrate(erfi((b*log(c*x^n) + a)*d), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \mathrm{erfi}(d\,(a+b\,\ln\left(c\,x^n\right)))\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(d*(a + b*log(c*x^n))),x)
[Out] int(erfi(d*(a + b*log(c*x^n))), x)
```

3.249 $\int \frac{\text{Erfi}(d(a+b\log(cx^n)))}{x}\,dx$

Optimal. Leaf size=64

$$-\frac{e^{(ad+bd\log(cx^n))^2}}{bdn\sqrt{\pi}}+\frac{\text{Erfi}(d(a+b\log(cx^n)))(a+b\log(cx^n))}{bn}$$

```
[Out] erfi(d*(a+b*ln(c*x^n)))*(a+b*ln(c*x^n))/b/n-exp((a*d+b*d*ln(c*x^n))^2)/b/d/
n/Pi^(1/2)
```

Rubi [A]
time = 0.03, antiderivative size = 64, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}}=0.059$, Rules used = $\{6486\}$

$$\frac{(a+b\log(cx^n))\,\text{Erfi}(d(a+b\log(cx^n)))}{bn}-\frac{e^{(ad+bd\log(cx^n))^2}}{\sqrt{\pi}\,bdn}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[d*(a + b*Log[c*x^n])]/x,x]
```

```
[Out] -(E^(a*d + b*d*Log[c*x^n])^2/(b*d*n*Sqrt[Pi])) + (Erfi[d*(a + b*Log[c*x^n])
]*(a + b*Log[c*x^n]))/(b*n)
```

Rule 6486

```
Int[Erfi[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[(a + b*x)*(Erfi[a + b*x]/b)
, x] - Simp[E^(a + b*x)^2/(b*Sqrt[Pi]), x] /; FreeQ[{a, b}, x]
```

Rubi steps

$$\begin{aligned}\int \frac{\text{erfi}(d(a+b\log(cx^n)))}{x}\,dx &= \frac{\text{Subst}\left(\int \text{erfi}(d(a+bx))\,dx, x, \log(cx^n)\right)}{n}\\ &= \frac{\text{Subst}\left(\int \text{erfi}(x)\,dx, x, ad+bd\log(cx^n)\right)}{bdn}\\ &= -\frac{e^{(ad+bd\log(cx^n))^2}}{bdn\sqrt{\pi}}+\frac{\text{erfi}(ad+bd\log(cx^n))(a+b\log(cx^n))}{bn}\end{aligned}$$

Mathematica [A]
time = 0.06, size = 83, normalized size = 1.30

$$\frac{-e^{d^2(a^2+b^2\log^2(cx^n))}(cx^n)^{2abd^2}+d\sqrt{\pi}\,\text{Erfi}(d(a+b\log(cx^n)))(a+b\log(cx^n))}{bdn\sqrt{\pi}}$$

Antiderivative was successfully verified.

[In] Integrate[Erfi[d*(a + b*Log[c*x^n])]/x,x]

[Out] (-(E^(d^2*(a^2 + b^2*Log[c*x^n]^2))*(c*x^n)^(2*a*b*d^2)) + d*Sqrt[Pi]*Erfi[d*(a + b*Log[c*x^n])]*(a + b*Log[c*x^n]))/(b*d*n*Sqrt[Pi])

Maple [A]
time = 1.60, size = 61, normalized size = 0.95

method	result	size
derivativedivides	$\frac{(ad+bd\ln(c\,x^{n}))\,\mathrm{erfi}(ad+bd\ln(c\,x^{n}))-\frac{\mathrm{e}^{(ad+bd\ln(c\,x^{n}))^{2}}}{\sqrt{\pi}}}{nbd}$	61
default	$\frac{(ad+bd\ln(c\,x^{n}))\,\mathrm{erfi}(ad+bd\ln(c\,x^{n}))-\frac{\mathrm{e}^{(ad+bd\ln(c\,x^{n}))^{2}}}{\sqrt{\pi}}}{nbd}$	61

Verification of antiderivative is not currently implemented for this CAS.

[In] int(erfi(d*(a+b*ln(c*x^n)))/x,x,method=_RETURNVERBOSE)

[Out] 1/n/b/d*((a*d+b*d*ln(c*x^n))*erfi(a*d+b*d*ln(c*x^n))-1/Pi^(1/2)*exp((a*d+b*d*ln(c*x^n))^2))

Maxima [A]
time = 0.25, size = 58, normalized size = 0.91

$$\frac{(b\log(cx^{n})+a)d\,\mathrm{erfi}\left((b\log(cx^{n})+a)d\right)-\frac{e^{\left((b\log(cx^{n})+a)^{2}d^{2}\right)}}{\sqrt{\pi}}}{bdn}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(erfi(d*(a+b*log(c*x^n)))/x,x, algorithm="maxima")

[Out] ((b*log(c*x^n) + a)*d*erfi((b*log(c*x^n) + a)*d) - e^((b*log(c*x^n) + a)^2*d^2)/sqrt(pi))/(b*d*n)

Fricas [A]
time = 0.37, size = 117, normalized size = 1.83

$$\frac{(\pi bdn\log(x)+\pi bd\log(c)+\pi ad)\,\mathrm{erfi}\left(bd\log(cx^{n})+ad\right)-\sqrt{\pi}\,e^{\left(b^{2}d^{2}n^{2}\log(x)^{2}+b^{2}d^{2}\log(c)^{2}+2\,abd^{2}\log(c)+a^{2}d^{2}+2\,(b^{2}d^{2}n\log(c)+abd^{2}n)\log(x)\right)}}{\pi bdn}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(erfi(d*(a+b*log(c*x^n)))/x,x, algorithm="fricas")

[Out] ((pi*b*d*n*log(x) + pi*b*d*log(c) + pi*a*d)*erfi(b*d*log(c*x^n) + a*d) - sqrt(pi)*e^(b^2*d^2*n^2*log(x)^2 + b^2*d^2*log(c)^2 + 2*a*b*d^2*log(c) + a^2*d^2 + 2*(b^2*d^2*n*log(c) + a*b*d^2*n)*log(x)))/(pi*b*d*n)

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}(ad + bd\log(cx^n))}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(d*(a+b*ln(c*x**n)))/x,x)
```

```
[Out] Integral(erfi(a*d + b*d*log(c*x**n))/x, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(d*(a+b*log(c*x^n)))/x,x, algorithm="giac")
```

```
[Out] integrate(erfi((b*log(c*x^n) + a)*d)/x, x)
```

Mupad [B]
time = 0.45, size = 112, normalized size = 1.75

$$\frac{\ln(c\,x^n)\,\operatorname{erfi}(a\,d+b\,d\,\ln(c\,x^n))}{n}+\frac{a\,d\,\operatorname{erfi}\left(a\,\sqrt{d^2}+b\,\ln(c\,x^n)\,\sqrt{d^2}\right)}{b\,n\,\sqrt{d^2}}-\frac{\mathrm{e}^{b^2\,d^2\,\ln(c\,x^n)^2}\,\mathrm{e}^{a^2\,d^2}\,(c\,x^n)^{2\,a\,b\,d^2}}{b\,d\,n\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(d*(a + b*log(c*x^n)))/x,x)
```

```
[Out] (log(c*x^n)*erfi(a*d + b*d*log(c*x^n)))/n + (a*d*erfi(a*(d^2)^(1/2) + b*log
(c*x^n)*(d^2)^(1/2)))/(b*n*(d^2)^(1/2)) - (exp(b^2*d^2*log(c*x^n)^2)*exp(a^
2*d^2)*(c*x^n)^(2*a*b*d^2))/(b*d*n*pi^(1/2))
```

3.250 $\int \frac{\mathbf{Erfi}(d(a+b\log(cx^n)))}{x^2}\,dx$

Optimal. Leaf size=94

$$-\frac{\operatorname{Erfi}(d(a+b\log(cx^n)))}{x}+\frac{e^{-\frac{1}{4b^2d^2n^2}+\frac{a}{bn}}(cx^n)^{\frac{1}{n}}\operatorname{Erfi}\left(\frac{2abd^2-\frac{1}{n}+2b^2d^2\log(cx^n)}{2bd}\right)}{x}$$

```
[Out] -erfi(d*(a+b*ln(c*x^n)))/x+exp(-1/4/b^2/d^2/n^2+a/b/n)*(c*x^n)^(1/n)*erfi(1
/2*(2*a*b*d^2-1/n+2*b^2*d^2*ln(c*x^n))/b/d)/x
```

Rubi [A]
time = 0.11, antiderivative size = 94, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.294, Rules used = {6538, 2314, 2308, 2266, 2235}

$$\frac{(cx^n)^{\frac{1}{n}}e^{\frac{a}{bn}-\frac{1}{4b^2d^2n^2}}\operatorname{Erfi}\left(\frac{2abd^2+2b^2d^2\log(cx^n)-\frac{1}{n}}{2bd}\right)}{x}-\frac{\operatorname{Erfi}(d(a+b\log(cx^n)))}{x}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[d*(a + b*Log[c*x^n])]/x^2,x]
```

```
[Out] -(Erfi[d*(a + b*Log[c*x^n])]/x) + (E^(-1/4*1/(b^2*d^2*n^2) + a/(b*n))*(c*x^
n)^n^(-1)*Erfi[(2*a*b*d^2 - n^(-1) + 2*b^2*d^2*Log[c*x^n])/(2*b*d)])/x
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2314

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^m*((c*(d + e*x)^n)^(2
*a*b*f*Log[F])/(d + e*x)^(m + 2*a*b*f*n*Log[F])), Int[(d + e*x)^(m + 2*a*b*
f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2), x], x] /; FreeQ[{F, a,
b, c, d, e, f, g, h, m, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 6538

```
Int[Erfi[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_))^(m_.), x
_Symbol] :> Simp[(e*x)^(m + 1)*(Erfi[d*(a + b*Log[c*x^n])]/(e*(m + 1))), x]
 - Dist[2*b*d*(n/(Sqrt[Pi]*(m + 1))), Int[(e*x)^m*E^(d*(a + b*Log[c*x^n]))^
2, x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rubi steps

$$\int \frac{\operatorname{erfi}(d(a+b\log(cx^n)))}{x^2}\,dx = -\frac{\operatorname{erfi}(d(a+b\log(cx^n)))}{x}+\frac{(2bdn)\int \frac{e^{d^2(a+b\log(cx^n))^2}}{x^2}\,dx}{\sqrt{\pi}}$$

$$= -\frac{\operatorname{erfi}(d(a+b\log(cx^n)))}{x}+\frac{(2bdn)\int \frac{\exp\left(a^2d^2+2abd^2\log(cx^n)+b^2d^2\log^2(cx^n)\right)}{x^2}\,dx}{\sqrt{\pi}}$$

$$= -\frac{\operatorname{erfi}(d(a+b\log(cx^n)))}{x}+\frac{(2bdn)\int \frac{e^{a^2d^2+b^2d^2\log^2(cx^n)}(cx^n)^{2abd^2}}{x^2}\,dx}{\sqrt{\pi}}$$

$$= -\frac{\operatorname{erfi}(d(a+b\log(cx^n)))}{x}+\frac{\left(2bdnx^{-2abd^2n}(cx^n)^{2abd^2}\right)\int e^{a^2d^2+b^2d^2\log^2(cx^n)}x^{-2+}}{\sqrt{\pi}}$$

$$= -\frac{\operatorname{erfi}(d(a+b\log(cx^n)))}{x}+\frac{\left(2bd(cx^n)^{2abd^2-\frac{-1+2abd^2n}{n}}\right)\operatorname{Subst}\left(\int \exp\left(a^2d^2+\right.\right.}{\sqrt{\pi}\,x}$$

$$= -\frac{\operatorname{erfi}(d(a+b\log(cx^n)))}{x}+\frac{\left(2bde^{-\frac{1}{4b^2d^2n^2}+\frac{a}{bn}}(cx^n)^{2abd^2-\frac{-1+2abd^2n}{n}}\right)\operatorname{Subst}\left(\int e\right.}{\sqrt{\pi}\,x}$$

$$= -\frac{\operatorname{erfi}(d(a+b\log(cx^n)))}{x}+\frac{e^{-\frac{1}{4b^2d^2n^2}+\frac{a}{bn}}(cx^n)^{\frac{1}{n}}\operatorname{erfi}\left(\frac{2abd^2-\frac{1}{n}+2b^2d^2\log(cx^n)}{2bd}\right)}{x}$$

Mathematica [A]
time = 0.21, size = 82, normalized size = 0.87

$$\frac{-\operatorname{Erfi}(d(a+b\log(cx^n)))+e^{\frac{-1+4abd^2n}{4b^2d^2n^2}}(cx^n)^{\frac{1}{n}}\operatorname{Erfi}\left(ad-\frac{1}{2bdn}+bd\log(cx^n)\right)}{x}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[d*(a + b*Log[c*x^n])]/x^2,x]
```

```
[Out] (-Erfi[d*(a + b*Log[c*x^n])] + E^((-1 + 4*a*b*d^2*n)/(4*b^2*d^2*n^2))*(c*x^
n)^n^(-1)*Erfi[a*d - 1/(2*b*d*n) + b*d*Log[c*x^n]])/x
```

Maple [F]
time = 0.20, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}\left(d(a+b\ln\left(c\,x^{n}\right))\right)}{x^{2}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(d*(a+b*ln(c*x^n)))/x^2,x)
```

```
[Out] int(erfi(d*(a+b*ln(c*x^n)))/x^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(d*(a+b*log(c*x^n)))/x^2,x, algorithm="maxima")
```

```
[Out] integrate(erfi((b*log(c*x^n) + a)*d)/x^2, x)
```

Fricas [A]
time = 0.37, size = 126, normalized size = 1.34

$$\frac{\sqrt{b^{2}d^{2}n^{2}}\,x\operatorname{erfi}\left(\frac{(2\,b^{2}d^{2}n^{2}\log(x)+2\,b^{2}d^{2}n\log(c)+2\,abd^{2}n-1)\sqrt{b^{2}d^{2}n^{2}}}{2\,b^{2}d^{2}n^{2}}\right)e^{\left(\frac{4\,b^{2}d^{2}n\log(c)+4\,abd^{2}n-1}{4\,b^{2}d^{2}n^{2}}\right)}-\operatorname{erfi}\left(bd\log\left(cx^{n}\right)+ad\right)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(d*(a+b*log(c*x^n)))/x^2,x, algorithm="fricas")
```

```
[Out] (sqrt(b^2*d^2*n^2)*x*erfi(1/2*(2*b^2*d^2*n^2*log(x) + 2*b^2*d^2*n*log(c) +
2*a*b*d^2*n - 1)*sqrt(b^2*d^2*n^2)/(b^2*d^2*n^2))*e^(1/4*(4*b^2*d^2*n*log(c
) + 4*a*b*d^2*n - 1)/(b^2*d^2*n^2)) - erfi(b*d*log(c*x^n) + a*d))/x
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}\left(ad+bd\log\left(cx^{n}\right)\right)}{x^{2}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(d*(a+b*ln(c*x**n)))/x**2,x)
```

```
[Out] Integral(erfi(a*d + b*d*log(c*x**n))/x**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(d*(a+b*log(c*x^n)))/x^2,x, algorithm="giac")
```

```
[Out] integrate(erfi((b*log(c*x^n) + a)*d)/x^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erfi}(d\,(a+b\,\ln\left(c\,x^n\right)))}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(d*(a + b*log(c*x^n)))/x^2,x)
```

```
[Out] int(erfi(d*(a + b*log(c*x^n)))/x^2, x)
```

3.251 $\int \frac{\mathbf{Erfi}(d(a+b\log(cx^n)))}{x^3}\,dx$

Optimal. Leaf size=95

$$-\frac{\text{Erfi}(d(a+b\log(cx^n)))}{2x^2}+\frac{e^{-\frac{1-2abd^2n}{b^2d^2n^2}}(cx^n)^{2/n}\,\text{Erfi}\left(\frac{abd^2-\frac{1}{n}+b^2d^2\log(cx^n)}{bd}\right)}{2x^2}$$

```
[Out] -1/2*erfi(d*(a+b*ln(c*x^n)))/x^2+1/2*(c*x^n)^(2/n)*erfi((a*b*d^2-1/n+b^2*d^
2*ln(c*x^n))/b/d)/exp((-2*a*b*d^2*n+1)/b^2/d^2/n^2)/x^2
```

Rubi [A]
time = 0.11, antiderivative size = 95, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.294$, Rules used = {6538, 2314, 2308, 2266, 2235}

$$\frac{(cx^n)^{2/n}\,e^{-\frac{1-2abd^2n}{b^2d^2n^2}}\,\text{Erfi}\left(\frac{abd^2+b^2d^2\log(cx^n)-\frac{1}{n}}{bd}\right)}{2x^2}-\frac{\text{Erfi}(d(a+b\log(cx^n)))}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[d*(a + b*Log[c*x^n])]/x^3,x]
```

```
[Out] -1/2*Erfi[d*(a + b*Log[c*x^n])]/x^2 + ((c*x^n)^(2/n)*Erfi[(a*b*d^2 - n^(-1)
 + b^2*d^2*Log[c*x^n])/(b*d)])/(2*E^((1 - 2*a*b*d^2*n)/(b^2*d^2*n^2))*x^2)
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2314

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^m*((c*(d + e*x)^n)^(2
*a*b*f*Log[F])/(d + e*x)^(m + 2*a*b*f*n*Log[F])), Int[(d + e*x)^(m + 2*a*b*
f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2), x], x] /; FreeQ[{F, a,
b, c, d, e, f, g, h, m, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 6538

```
Int[Erfi[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_))^(m_.), x
_Symbol] :> Simp[(e*x)^(m + 1)*(Erfi[d*(a + b*Log[c*x^n])]/(e*(m + 1))), x]
 - Dist[2*b*d*(n/(Sqrt[Pi]*(m + 1))), Int[(e*x)^m*E^(d*(a + b*Log[c*x^n]))^
2, x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rubi steps

$$\int \frac{\text{erfi}(d(a+b\log(cx^n)))}{x^3}\,dx = -\frac{\text{erfi}(d(a+b\log(cx^n)))}{2x^2} + \frac{(bdn)\int \frac{e^{d^2(a+b\log(cx^n))^2}}{x^3}\,dx}{\sqrt{\pi}}$$

$$= -\frac{\text{erfi}(d(a+b\log(cx^n)))}{2x^2} + \frac{(bdn)\int \frac{\exp\left(a^2d^2+2abd^2\log(cx^n)+b^2d^2\log^2(cx^n)\right)}{x^3}\,dx}{\sqrt{\pi}}$$

$$= -\frac{\text{erfi}(d(a+b\log(cx^n)))}{2x^2} + \frac{(bdn)\int \frac{e^{a^2d^2+b^2d^2\log^2(cx^n)}(cx^n)^{2abd^2}}{x^3}\,dx}{\sqrt{\pi}}$$

$$= -\frac{\text{erfi}(d(a+b\log(cx^n)))}{2x^2} + \frac{\left(bdnx^{-2abd^2n}(cx^n)^{2abd^2}\right)\int e^{a^2d^2+b^2d^2\log^2(cx^n)}x^{-3+2}}{\sqrt{\pi}}$$

$$= -\frac{\text{erfi}(d(a+b\log(cx^n)))}{2x^2} + \frac{\left(bd(cx^n)^{2abd^2-\frac{-2+2abd^2n}{n}}\right)\text{Subst}\left(\int \exp\left(a^2d^2+\frac{(}{}\right.\right.}{\sqrt{\pi}\,x^2}$$

$$= -\frac{\text{erfi}(d(a+b\log(cx^n)))}{2x^2} + \frac{\left(bde^{-\frac{1-2abd^2n}{b^2d^2n^2}}(cx^n)^{2abd^2-\frac{-2+2abd^2n}{n}}\right)\text{Subst}\left(\int \exp\right.}{\sqrt{\pi}\,x^2}$$

$$= -\frac{\text{erfi}(d(a+b\log(cx^n)))}{2x^2} + \frac{e^{-\frac{1-2abd^2n}{b^2d^2n^2}}(cx^n)^{2/n}\,\text{erfi}\left(\frac{abd^2-\frac{1}{n}+b^2d^2\log(cx^n)}{bd}\right)}{2x^2}$$

Mathematica [A]
time = 0.21, size = 80, normalized size = 0.84

$$\frac{-\text{Erfi}(d(a+b\log(cx^n))) + e^{\frac{\frac{-\frac{1}{d^2}+2abn}{b^2}+2n\log(cx^n)}{n^2}}\,\text{Erfi}\left(ad-\frac{1}{bdn}+bd\log(cx^n)\right)}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[d*(a + b*Log[c*x^n])]/x^3,x]
```

```
[Out] (-Erfi[d*(a + b*Log[c*x^n])] + E^(((-d^(-2) + 2*a*b*n)/b^2 + 2*n*Log[c*x^n]
)/n^2)*Erfi[a*d - 1/(b*d*n) + b*d*Log[c*x^n]])/(2*x^2)
```

Maple [F]
time = 0.20, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}\left(d(a+b\ln\left(c\,x^{n}\right))\right)}{x^{3}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(d*(a+b*ln(c*x^n)))/x^3,x)
```

```
[Out] int(erfi(d*(a+b*ln(c*x^n)))/x^3,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(d*(a+b*log(c*x^n)))/x^3,x, algorithm="maxima")
```

```
[Out] integrate(erfi((b*log(c*x^n) + a)*d)/x^3, x)
```

Fricas [A]
time = 0.37, size = 124, normalized size = 1.31

$$\frac{\sqrt{b^2d^2n^2}\,x^2\operatorname{erfi}\left(\frac{(b^2d^2n^2\log(x)+b^2d^2n\log(c)+abd^2n-1)\sqrt{b^2d^2n^2}}{b^2d^2n^2}\right)e^{\left(\frac{2\,b^2d^2n\log(c)+2\,abd^2n-1}{b^2d^2n^2}\right)}-\operatorname{erfi}\left(bd\log\left(cx^n\right)+ad\right)}{2\,x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(d*(a+b*log(c*x^n)))/x^3,x, algorithm="fricas")
```

```
[Out] 1/2*(sqrt(b^2*d^2*n^2)*x^2*erfi((b^2*d^2*n^2*log(x) + b^2*d^2*n*log(c) + a*
b*d^2*n - 1)*sqrt(b^2*d^2*n^2)/(b^2*d^2*n^2))*e^((2*b^2*d^2*n*log(c) + 2*a*
b*d^2*n - 1)/(b^2*d^2*n^2)) - erfi(b*d*log(c*x^n) + a*d))/x^2
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}\left(ad+bd\log\left(cx^{n}\right)\right)}{x^{3}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(d*(a+b*ln(c*x**n)))/x**3,x)
```

```
[Out] Integral(erfi(a*d + b*d*log(c*x**n))/x**3, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(d*(a+b*log(c*x^n)))/x^3,x, algorithm="giac")
```

```
[Out] integrate(erfi((b*log(c*x^n) + a)*d)/x^3, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erfi}(d\,(a+b\,\ln\left(c\,x^n\right)))}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(d*(a + b*log(c*x^n)))/x^3,x)
```

```
[Out] int(erfi(d*(a + b*log(c*x^n)))/x^3, x)
```

3.252 $\int (ex)^m \mathbf{Erfi}(d(a+b\log(cx^n)))\,dx$

Optimal. Leaf size=126

$$\frac{(ex)^{1+m}\mathrm{Erfi}(d(a+b\log(cx^n)))}{e(1+m)}-\frac{e^{-\frac{(1+m)\left(1+m+4abd^2n\right)}{4b^2d^2n^2}}x(ex)^m(cx^n)^{-\frac{1+m}{n}}\,\mathrm{Erfi}\left(\frac{1+m+2abd^2n+2b^2d^2n\log(cx^n)}{2bdn}\right)}{1+m}$$

```
[Out] (e*x)^(1+m)*erfi(d*(a+b*ln(c*x^n)))/e/(1+m)-x*(e*x)^m*erfi(1/2*(1+m+2*a*b*d
^2*n+2*b^2*d^2*n*ln(c*x^n))/b/d/n)/exp(1/4*(1+m)*(4*a*b*d^2*n+m+1)/b^2/d^2/
n^2)/(1+m)/((c*x^n)^((1+m)/n))
```

Rubi [A]

time = 0.18, antiderivative size = 126, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {6538, 2314, 2308, 2266, 2235}

$$\frac{(ex)^{m+1}\mathrm{Erfi}(d(a+b\log(cx^n)))}{e(m+1)}-\frac{x(ex)^m(cx^n)^{-\frac{m+1}{n}}\exp\left(-\frac{(m+1)\left(4abd^2n+m+1\right)}{4b^2d^2n^2}\right)\mathrm{Erfi}\left(\frac{2abd^2n+2b^2d^2n\log(cx^n)+m+1}{2bdn}\right)}{m+1}$$

Antiderivative was successfully verified.

```
[In] Int[(e*x)^m*Erfi[d*(a + b*Log[c*x^n])],x]
```

```
[Out] ((e*x)^(1 + m)*Erfi[d*(a + b*Log[c*x^n])])/(e*(1 + m)) - (x*(e*x)^m*Erfi[(1
 + m + 2*a*b*d^2*n + 2*b^2*d^2*n*Log[c*x^n])/(2*b*d*n)])/(E^(((1 + m)*(1 +
m + 4*a*b*d^2*n))/(4*b^2*d^2*n^2))*(1 + m)*(c*x^n)^((1 + m)/n))
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2308

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]^2*(b_.))*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^(m + 1)/(h*n*(c*(d +
e*x)^n)^((m + 1)/n)), Subst[Int[E^(a*f*Log[F] + ((m + 1)*x)/n + b*f*Log[F]*
x^2), x], x, Log[c*(d + e*x)^n]], x] /; FreeQ[{F, a, b, c, d, e, f, g, h, m
, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 2314

```
Int[(F_)^(((a_.) + Log[(c_.)*((d_.) + (e_.)*(x_))^(n_.)]*(b_.))^2*(f_.))*((
g_.) + (h_.)*(x_))^(m_.), x_Symbol] :> Dist[(g + h*x)^m*((c*(d + e*x)^n)^(2
*a*b*f*Log[F])/(d + e*x)^(m + 2*a*b*f*n*Log[F])), Int[(d + e*x)^(m + 2*a*b*
f*n*Log[F])*F^(a^2*f + b^2*f*Log[c*(d + e*x)^n]^2), x], x] /; FreeQ[{F, a,
b, c, d, e, f, g, h, m, n}, x] && EqQ[e*g - d*h, 0]
```

Rule 6538

```
Int[Erfi[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_))^(m_.), x
_Symbol] :> Simp[(e*x)^(m + 1)*(Erfi[d*(a + b*Log[c*x^n])]/(e*(m + 1))), x]
 - Dist[2*b*d*(n/(Sqrt[Pi]*(m + 1))), Int[(e*x)^m*E^(d*(a + b*Log[c*x^n]))^
2, x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rubi steps

$$
\begin{aligned}
\int (ex)^m \operatorname{erfi}(d(a+b\log(cx^n)))\,dx &= \frac{(ex)^{1+m}\operatorname{erfi}(d(a+b\log(cx^n)))}{e(1+m)} - \frac{(2bdn)\int e^{d^2(a+b\log(cx^n))^2}(ex)^m\,dx}{(1+m)\sqrt{\pi}} \\
&= \frac{(ex)^{1+m}\operatorname{erfi}(d(a+b\log(cx^n)))}{e(1+m)} - \frac{(2bdn)\int \exp\left(a^2d^2+2abd^2\log(cx^n)\right.}{(1+m)\sqrt{\pi}} \\
&= \frac{(ex)^{1+m}\operatorname{erfi}(d(a+b\log(cx^n)))}{e(1+m)} - \frac{(2bdn)\int e^{a^2d^2+b^2d^2\log^2(cx^n)}(ex)^m\,(cx^n)}{(1+m)\sqrt{\pi}} \\
&= \frac{(ex)^{1+m}\operatorname{erfi}(d(a+b\log(cx^n)))}{e(1+m)} - \frac{\left(2bdnx^{-2abd^2n}(cx^n)^{2abd^2}\right)\int e^{a^2d^2+b^2d^2}}{(1+m)\sqrt{\pi}} \\
&= \frac{(ex)^{1+m}\operatorname{erfi}(d(a+b\log(cx^n)))}{e(1+m)} - \frac{\left(2bdnx^{-m-2abd^2n}(ex)^m\,(cx^n)^{2abd^2}\right)\int}{(1+m)\sqrt{}} \\
&= \frac{(ex)^{1+m}\operatorname{erfi}(d(a+b\log(cx^n)))}{e(1+m)} - \frac{\left(2bdx(ex)^m\,(cx^n)^{2abd^2-\frac{1+m+2abd^2n}{n}}\right)\mathrm{Su}}{} \\
&= \frac{(ex)^{1+m}\operatorname{erfi}(d(a+b\log(cx^n)))}{e(1+m)} - \frac{\left(2bd\exp\left(-\frac{(1+m)(1+m+4abd^2n)}{4b^2d^2n^2}\right)x(ex)\right.}{} \\
&= \frac{(ex)^{1+m}\operatorname{erfi}(d(a+b\log(cx^n)))}{e(1+m)} - \frac{\exp\left(-\frac{(1+m)(1+m+4abd^2n)}{4b^2d^2n^2}\right)x(ex)^m\,(cx}{1+}
\end{aligned}
$$

Mathematica [A]

time = 0.32, size = 126, normalized size = 1.00

$$\frac{(ex)^m \left(x\mathrm{Erfi}(d(a+b\log(cx^n))) - e^{-\frac{(1+m)\left(1+m+4abd^2n-4b^2d^2n^2\log(x)+4b^2d^2n\log(cx^n)\right)}{4b^2d^2n^2}} x^{-m}\mathrm{Erfi}\left(\frac{1+m+2abd^2n}{2bdn}+bd\log(cx^n)\right)\right)}{1+m}$$

Antiderivative was successfully verified.

```
[In] Integrate[(e*x)^m*Erfi[d*(a + b*Log[c*x^n])],x]
```

```
[Out] ((e*x)^m*(x*Erfi[d*(a + b*Log[c*x^n])] - Erfi[(1 + m + 2*a*b*d^2*n)/(2*b*d*
n) + b*d*Log[c*x^n]]/(E^(((1 + m)*(1 + m + 4*a*b*d^2*n - 4*b^2*d^2*n^2*Log[
x] + 4*b^2*d^2*n*Log[c*x^n]))/(4*b^2*d^2*n^2))*x^m)))/(1 + m)
```

Maple [F]
time = 0.08, size = 0, normalized size = 0.00

$$\int (ex)^m \operatorname{erfi}(d(a+b\ln(c\,x^n)))\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*erfi(d*(a+b*ln(c*x^n))),x)
```

```
[Out] int((e*x)^m*erfi(d*(a+b*ln(c*x^n))),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*erfi(d*(a+b*log(c*x^n))),x, algorithm="maxima")
```

```
[Out] integrate((x*e)^m*erfi((b*log(c*x^n) + a)*d), x)
```

Fricas [A]
time = 0.39, size = 175, normalized size = 1.39

$$\frac{x\operatorname{erfi}(bd\log(cx^n)+ad)\,e^{(m\log(x)+m)} - \sqrt{b^2d^2n^2}\,\operatorname{erfi}\left(\frac{\left(2\,b^2d^2n^2\log(x)+2\,b^2d^2n\log(c)+2\,abd^2n+m+1\right)\sqrt{b^2d^2n^2}}{2\,b^2d^2n^2}\right)e^{\left(\frac{4\,b^2d^2mn^2-4\,\left(b^2d^2m+b^2d^2\right)n\log(c)-m^2-4\,\left(abd^2m+abd^2\right)n-2\,m-1}{4\,b^2d^2n^2}\right)}}{m+1}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*erfi(d*(a+b*log(c*x^n))),x, algorithm="fricas")
```

```
[Out] (x*erfi(b*d*log(c*x^n) + a*d)*e^(m*log(x) + m) - sqrt(b^2*d^2*n^2)*erfi(1/2
*(2*b^2*d^2*n^2*log(x) + 2*b^2*d^2*n*log(c) + 2*a*b*d^2*n + m + 1)*sqrt(b^2
*d^2*n^2)/(b^2*d^2*n^2))*e^(1/4*(4*b^2*d^2*m*n^2 - 4*(b^2*d^2*m + b^2*d^2)*
```

```
n*log(c) - m^2 - 4*(a*b*d^2*m + a*b*d^2)*n - 2*m - 1)/(b^2*d^2*n^2)))/(m +
1)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int (ex)^m \operatorname{erfi}\left(ad + bd\log\left(cx^n\right)\right) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*erfi(d*(a+b*ln(c*x**n))),x)
[Out] Integral((e*x)**m*erfi(a*d + b*d*log(c*x**n)), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*erfi(d*(a+b*log(c*x^n))),x, algorithm="giac")
[Out] integrate((e*x)^m*erfi((b*log(c*x^n) + a)*d), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \operatorname{erfi}(d\,(a+b\,\ln\left(c\,x^n\right)))\,\left(e\,x\right)^m\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(d*(a + b*log(c*x^n)))*(e*x)^m,x)
[Out] int(erfi(d*(a + b*log(c*x^n)))*(e*x)^m, x)
```

3.253 $\int e^{c+b^2x^2}\textbf{Erfi}(bx)^2\,dx$

Optimal. Leaf size=21

$$\frac{e^c\sqrt{\pi}\,\text{Erfi}(bx)^3}{6b}$$

```
[Out] 1/6*exp(c)*erfi(b*x)^3*Pi^(1/2)/b
```

Rubi [A]
time = 0.02, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {6510, 30}

$$\frac{\sqrt{\pi}\,e^c\text{Erfi}(bx)^3}{6b}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*Erfi[b*x]^2,x]
```

```
[Out] (E^c*Sqrt[Pi]*Erfi[b*x]^3)/(6*b)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rubi steps

$$\begin{aligned}\int e^{c+b^2x^2}\text{erfi}(bx)^2\,dx &= \frac{\left(e^c\sqrt{\pi}\right)\text{Subst}\left(\int x^2\,dx,x,\text{erfi}(bx)\right)}{2b}\\ &= \frac{e^c\sqrt{\pi}\,\text{erfi}(bx)^3}{6b}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 21, normalized size = 1.00

$$\frac{e^c\sqrt{\pi}\,\text{Erfi}(bx)^3}{6b}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*Erfi[b*x]^2,x]
```

```
[Out] (E^c*Sqrt[Pi]*Erfi[b*x]^3)/(6*b)
```

Maple [F]
time = 0.04, size = 0, normalized size = 0.00

$$\int e^{b^2x^2+c} \operatorname{erfi}(bx)^2 \, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erfi(b*x)^2,x)
```

```
[Out] int(exp(b^2*x^2+c)*erfi(b*x)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)^2,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)^2*e^(b^2*x^2 + c), x)
```

Fricas [A]
time = 0.40, size = 16, normalized size = 0.76

$$\frac{\sqrt{\pi} \operatorname{erfi}(bx)^3 e^c}{6 b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)^2,x, algorithm="fricas")
```

```
[Out] 1/6*sqrt(pi)*erfi(b*x)^3*e^c/b
```

Sympy [A]
time = 0.42, size = 19, normalized size = 0.90

$$\begin{cases} \frac{\sqrt{\pi} e^{c} \operatorname{erfi}^{3}(bx)}{6b} & \text{for}\ b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erfi(b*x)**2,x)
```

```
[Out] Piecewise((sqrt(pi)*exp(c)*erfi(b*x)**3/(6*b), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)^2,x, algorithm="giac")
[Out] integrate(erfi(b*x)^2*e^(b^2*x^2 + c), x)
```

Mupad [B]
time = 0.10, size = 16, normalized size = 0.76

$$\frac{\sqrt{\pi}\,\mathrm{e}^c\,\mathrm{erfi}(b\,x)^3}{6\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c + b^2*x^2)*erfi(b*x)^2,x)
[Out] (pi^(1/2)*exp(c)*erfi(b*x)^3)/(6*b)
```

3.254 $\int e^{c+b^2x^2}\textbf{Erfi}(bx)\,dx$

Optimal. Leaf size=21

$$\frac{e^c\sqrt{\pi}\,\mathrm{Erfi}(bx)^2}{4b}$$

[Out] 1/4*exp(c)*erfi(b*x)^2*Pi^(1/2)/b

Rubi [A]

time = 0.01, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {6510, 30}

$$\frac{\sqrt{\pi}\,e^c\mathrm{Erfi}(bx)^2}{4b}$$

Antiderivative was successfully verified.

[In] Int[E^(c + b^2*x^2)*Erfi[b*x],x]

[Out] (E^c*Sqrt[Pi]*Erfi[b*x]^2)/(4*b)

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rubi steps

$$\begin{aligned}\int e^{c+b^2x^2}\mathrm{erfi}(bx)\,dx &= \frac{\left(e^c\sqrt{\pi}\right)\mathrm{Subst}\left(\int x\,dx,x,\mathrm{erfi}(bx)\right)}{2b}\\ &= \frac{e^c\sqrt{\pi}\,\mathrm{erfi}(bx)^2}{4b}\end{aligned}$$

Mathematica [A]

time = 0.01, size = 21, normalized size = 1.00

$$\frac{e^c\sqrt{\pi}\,\mathrm{Erfi}(bx)^2}{4b}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*Erfi[b*x],x]
```

```
[Out] (E^c*Sqrt[Pi]*Erfi[b*x]^2)/(4*b)
```

Maple [F]
time = 0.10, size = 0, normalized size = 0.00

$$\int e^{b^2x^2+c}\,\mathrm{erfi}\left(bx\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erfi(b*x),x)
```

```
[Out] int(exp(b^2*x^2+c)*erfi(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x),x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)*e^(b^2*x^2 + c), x)
```

Fricas [A]
time = 0.35, size = 16, normalized size = 0.76

$$\frac{\sqrt{\pi}\,\mathrm{erfi}\left(bx\right)^{2}e^{c}}{4\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x),x, algorithm="fricas")
```

```
[Out] 1/4*sqrt(pi)*erfi(b*x)^2*e^c/b
```

Sympy [A]
time = 0.15, size = 19, normalized size = 0.90

$$\begin{cases} \frac{\sqrt{\pi}\,e^{c}\,\mathrm{erfi}^{2}\left(bx\right)}{4b} & \text{for}\ b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erfi(b*x),x)
```

```
[Out] Piecewise((sqrt(pi)*exp(c)*erfi(b*x)**2/(4*b), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x),x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)*e^(b^2*x^2 + c), x)
```

Mupad [B]
time = 0.45, size = 91, normalized size = 4.33

$$\frac{\sqrt{\pi}\,\operatorname{erfi}\left(\frac{b^2\,x}{\sqrt{b^2}}\right)\,\mathrm{e}^c\,\operatorname{erfi}(b\,x)}{2\,\sqrt{b^2}}-\frac{\sqrt{\pi}\,\mathrm{e}^c\,\operatorname{erf}\left(x\,\sqrt{-b^2}\right)^2}{4\,b}-\frac{b\,\sqrt{\pi}\,\operatorname{erfi}\left(\frac{b^2\,x}{\sqrt{b^2}}\right)\,\mathrm{e}^c\,\operatorname{erf}\left(x\,\sqrt{-b^2}\right)}{2\,\sqrt{b^2}\,\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c + b^2*x^2)*erfi(b*x),x)
```

```
[Out] (pi^(1/2)*erfi((b^2*x)/(b^2)^(1/2))*exp(c)*erfi(b*x))/(2*(b^2)^(1/2)) - (pi
^(1/2)*exp(c)*erf(x*(-b^2)^(1/2))^2)/(4*b) - (b*pi^(1/2)*erfi((b^2*x)/(b^2)
^(1/2))*exp(c)*erf(x*(-b^2)^(1/2)))/(2*(b^2)^(1/2)*(-b^2)^(1/2))
```

3.255 $\int \frac{e^{c+b^2x^2}}{\mathbf{Erfi}(bx)}\,dx$

Optimal. Leaf size=20

$$\frac{e^c\sqrt{\pi}\,\log(\mathrm{Erfi}(bx))}{2b}$$

```
[Out] 1/2*exp(c)*ln(erfi(b*x))*Pi^(1/2)/b
```

Rubi [A]

time = 0.02, antiderivative size = 20, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = $\{6510, 29\}$

$$\frac{\sqrt{\pi}\,e^c\log(\mathrm{Erfi}(bx))}{2b}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)/Erfi[b*x],x]
```

```
[Out] (E^c*Sqrt[Pi]*Log[Erfi[b*x]])/(2*b)
```

Rule 29

```
Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+b^2x^2}}{\mathrm{erfi}(bx)}\,dx &= \frac{\left(e^c\sqrt{\pi}\right)\mathrm{Subst}\left(\int \frac{1}{x}\,dx, x, \mathrm{erfi}(bx)\right)}{2b}\\ &= \frac{e^c\sqrt{\pi}\,\log(\mathrm{erfi}(bx))}{2b}\end{aligned}$$

Mathematica [A]

time = 0.01, size = 20, normalized size = 1.00

$$\frac{e^c\sqrt{\pi}\,\log(\mathrm{Erfi}(bx))}{2b}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)/Erfi[b*x],x]
```

```
[Out] (E^c*Sqrt[Pi]*Log[Erfi[b*x]])/(2*b)
```

Maple [F]
time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{b^2x^2+c}}{\operatorname{erfi}(bx)}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)/erfi(b*x),x)
```

```
[Out] int(exp(b^2*x^2+c)/erfi(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)/erfi(b*x),x, algorithm="maxima")
```

```
[Out] integrate(e^(b^2*x^2 + c)/erfi(b*x), x)
```

Fricas [A]
time = 0.34, size = 15, normalized size = 0.75

$$\frac{\sqrt{\pi}\,e^c\log\left(\operatorname{erfi}(bx)\right)}{2\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)/erfi(b*x),x, algorithm="fricas")
```

```
[Out] 1/2*sqrt(pi)*e^c*log(erfi(b*x))/b
```

Sympy [A]
time = 0.19, size = 24, normalized size = 1.20

$$\begin{cases} \frac{\sqrt{\pi}\,e^c\log\left(\operatorname{erfi}(bx)\right)}{2b} & \text{for } b \neq 0 \\ \tilde{\infty} x e^c & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)/erfi(b*x),x)
```

```
[Out] Piecewise((sqrt(pi)*exp(c)*log(erfi(b*x))/(2*b), Ne(b, 0)), (zoo*x*exp(c),
True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)/erfi(b*x),x, algorithm="giac")
[Out] integrate(e^(b^2*x^2 + c)/erfi(b*x), x)
```

Mupad [B]
time = 0.17, size = 15, normalized size = 0.75

$$\frac{\sqrt{\pi}\ \ln\left(\mathrm{erfi}(b\,x)\right)\,\mathrm{e}^c}{2\,b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c + b^2*x^2)/erfi(b*x),x)
[Out] (pi^(1/2)*log(erfi(b*x))*exp(c))/(2*b)
```

3.256 $\int \frac{e^{c+b^2x^2}}{\textbf{Erfi}(bx)^2}\,dx$

Optimal. Leaf size=21

$$-\frac{e^c\sqrt{\pi}}{2b\text{Erfi}(bx)}$$

[Out] -1/2*exp(c)*Pi^(1/2)/b/erfi(b*x)

Rubi [A]
time = 0.02, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {6510, 30}

$$-\frac{\sqrt{\pi}\,e^c}{2b\text{Erfi}(bx)}$$

Antiderivative was successfully verified.

[In] Int[E^(c + b^2*x^2)/Erfi[b*x]^2,x]

[Out] -1/2*(E^c*Sqrt[Pi])/(b*Erfi[b*x])

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+b^2x^2}}{\text{erfi}(bx)^2}\,dx &= \frac{\left(e^c\sqrt{\pi}\right)\text{Subst}\left(\int \frac{1}{x^2}\,dx, x, \text{erfi}(bx)\right)}{2b}\\ &= -\frac{e^c\sqrt{\pi}}{2b\text{erfi}(bx)}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 21, normalized size = 1.00

$$-\frac{e^c\sqrt{\pi}}{2b\text{Erfi}(bx)}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)/Erfi[b*x]^2,x]
```

```
[Out] -1/2*(E^c*Sqrt[Pi])/(b*Erfi[b*x])
```

Maple [F]
time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{e^{b^2x^2+c}}{\operatorname{erfi}(bx)^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)/erfi(b*x)^2,x)
```

```
[Out] int(exp(b^2*x^2+c)/erfi(b*x)^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)/erfi(b*x)^2,x, algorithm="maxima")
```

```
[Out] integrate(e^(b^2*x^2 + c)/erfi(b*x)^2, x)
```

Fricas [A]
time = 0.38, size = 16, normalized size = 0.76

$$-\frac{\sqrt{\pi}\,e^c}{2\,b\operatorname{erfi}(bx)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)/erfi(b*x)^2,x, algorithm="fricas")
```

```
[Out] -1/2*sqrt(pi)*e^c/(b*erfi(b*x))
```

Sympy [A]
time = 0.45, size = 24, normalized size = 1.14

$$\begin{cases} -\frac{\sqrt{\pi}\,e^c}{2b\operatorname{erfi}(bx)} & \text{for } b \neq 0 \\ \tilde{\infty} x e^c & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)/erfi(b*x)**2,x)
```

```
[Out] Piecewise((-sqrt(pi)*exp(c)/(2*b*erfi(b*x)), Ne(b, 0)), (zoo*x*exp(c), True
))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)/erfi(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(e^(b^2*x^2 + c)/erfi(b*x)^2, x)
```

Mupad [B]
time = 0.10, size = 16, normalized size = 0.76

$$-\frac{\sqrt{\pi}\ \mathrm{e}^c}{2\,b\,\mathrm{erfi}\left(b\,x\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c + b^2*x^2)/erfi(b*x)^2,x)
```

```
[Out] -(pi^(1/2)*exp(c))/(2*b*erfi(b*x))
```

3.257 $\int \frac{e^{c+b^2x^2}}{\mathbf{Erfi}(bx)^3}\,dx$

Optimal. Leaf size=21

$$-\frac{e^c\sqrt{\pi}}{4b\text{Erfi}(bx)^2}$$

```
[Out] -1/4*exp(c)*Pi^(1/2)/b/erfi(b*x)^2
```

Rubi [A]
time = 0.02, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {6510, 30}

$$-\frac{\sqrt{\pi}\,e^c}{4b\text{Erfi}(bx)^2}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)/Erfi[b*x]^3,x]
```

```
[Out] -1/4*(E^c*Sqrt[Pi])/(b*Erfi[b*x]^2)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+b^2x^2}}{\text{erfi}(bx)^3}\,dx &= \frac{\left(e^c\sqrt{\pi}\right)\text{Subst}\left(\int \frac{1}{x^3}\,dx, x, \text{erfi}(bx)\right)}{2b}\\ &= -\frac{e^c\sqrt{\pi}}{4b\text{erfi}(bx)^2}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 21, normalized size = 1.00

$$-\frac{e^c\sqrt{\pi}}{4b\text{Erfi}(bx)^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)/Erfi[b*x]^3,x]
```

```
[Out] -1/4*(E^c*Sqrt[Pi])/(b*Erfi[b*x]^2)
```

Maple [**F**]
time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{b^{2} x^{2}+c}}{\operatorname{erfi}\left(b x\right)^{3}}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)/erfi(b*x)^3,x)
```

```
[Out] int(exp(b^2*x^2+c)/erfi(b*x)^3,x)
```

Maxima [**F**]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)/erfi(b*x)^3,x, algorithm="maxima")
```

```
[Out] integrate(e^(b^2*x^2 + c)/erfi(b*x)^3, x)
```

Fricas [**A**]
time = 0.33, size = 16, normalized size = 0.76

$$-\frac{\sqrt{\pi}\, e^{c}}{4\, b \operatorname{erfi}\left(b x\right)^{2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)/erfi(b*x)^3,x, algorithm="fricas")
```

```
[Out] -1/4*sqrt(pi)*e^c/(b*erfi(b*x)^2)
```

Sympy [**A**]
time = 0.82, size = 26, normalized size = 1.24

$$\begin{cases} - \frac{\sqrt{\pi} e^{c}}{4 b \operatorname{erfi}^{2}{\left(b x \right)}} & \text{for}\: b \neq 0 \\ \tilde{\infty} x e^{c} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)/erfi(b*x)**3,x)
```

```
[Out] Piecewise((-sqrt(pi)*exp(c)/(4*b*erfi(b*x)**2), Ne(b, 0)), (zoo*x*exp(c), T
rue))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)/erfi(b*x)^3,x, algorithm="giac")
[Out] integrate(e^(b^2*x^2 + c)/erfi(b*x)^3, x)
```

Mupad [B]
time = 0.14, size = 16, normalized size = 0.76

$$-\frac{\sqrt{\pi}\,\mathrm{e}^c}{4\,b\,\mathrm{erfi}\left(b\,x\right)^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c + b^2*x^2)/erfi(b*x)^3,x)
[Out] -(pi^(1/2)*exp(c))/(4*b*erfi(b*x)^2)
```

3.258 $\int e^{c+b^2x^2}\mathbf{Erfi}(bx)^n\,dx$

Optimal. Leaf size=28

$$\frac{e^c\sqrt{\pi}\,\text{Erfi}(bx)^{1+n}}{2b(1+n)}$$

[Out] 1/2*exp(c)*erfi(b*x)^(1+n)*Pi^(1/2)/b/(1+n)

Rubi [A]
time = 0.02, antiderivative size = 28, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$, Rules used = {6510, 30}

$$\frac{\sqrt{\pi}\,e^c\text{Erfi}(bx)^{n+1}}{2b(n+1)}$$

Antiderivative was successfully verified.

[In] Int[E^(c + b^2*x^2)*Erfi[b*x]^n,x]

[Out] (E^c*Sqrt[Pi]*Erfi[b*x]^(1 + n))/(2*b*(1 + n))

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rubi steps

$$\begin{aligned}\int e^{c+b^2x^2}\text{erfi}(bx)^n\,dx &= \frac{\left(e^c\sqrt{\pi}\right)\text{Subst}\left(\int x^n\,dx, x, \text{erfi}(bx)\right)}{2b}\\ &= \frac{e^c\sqrt{\pi}\,\text{erfi}(bx)^{1+n}}{2b(1+n)}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 28, normalized size = 1.00

$$\frac{e^c\sqrt{\pi}\,\text{Erfi}(bx)^{1+n}}{2b(1+n)}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*Erfi[b*x]^n,x]
[Out] (E^c*Sqrt[Pi]*Erfi[b*x]^(1 + n))/(2*b*(1 + n))
```

Maple [F]
time = 0.04, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{b^2x^2+c}\,\mathrm{erfi}\left(bx\right)^n\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erfi(b*x)^n,x)
[Out] int(exp(b^2*x^2+c)*erfi(b*x)^n,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)^n,x, algorithm="maxima")
[Out] integrate(erfi(b*x)^n*e^(b^2*x^2 + c), x)
```

Fricas [A]
time = 0.36, size = 24, normalized size = 0.86

$$\frac{\sqrt{\pi}\,\mathrm{erfi}\left(bx\right)^n\,\mathrm{erfi}\left(bx\right)e^c}{2\left(bn+b\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)^n,x, algorithm="fricas")
[Out] 1/2*sqrt(pi)*erfi(b*x)^n*erfi(b*x)*e^c/(b*n + b)
```

Sympy [B] Leaf count of result is larger than twice the leaf count of optimal. 63 vs. 2(22) = 44.
time = 1.79, size = 63, normalized size = 2.25

$$\begin{cases} \tilde{\infty}xe^c & \text{for } b=0\wedge n=-1 \\ 0^n xe^c & \text{for } b=0 \\ \frac{\sqrt{\pi}\,e^c\log\left(\mathrm{erfi}\left(bx\right)\right)}{2b} & \text{for } n=-1 \\ \frac{\sqrt{\pi}\,e^c\,\mathrm{erfi}\left(bx\right)\mathrm{erfi}^n\left(bx\right)}{2bn+2b} & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erfi(b*x)**n,x)
```

```
[Out] Piecewise((zoo*x*exp(c), Eq(b, 0) & Eq(n, -1)), (0**n*x*exp(c), Eq(b, 0)),
(sqrt(pi)*exp(c)*log(erfi(b*x))/(2*b), Eq(n, -1)), (sqrt(pi)*exp(c)*erfi(b*
x)*erfi(b*x)**n/(2*b*n + 2*b), True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)^n,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)^n*e^(b^2*x^2 + c), x)
```

Mupad [B]
time = 0.19, size = 23, normalized size = 0.82

$$\frac{\sqrt{\pi}\,\mathrm{e}^c\,\mathrm{erfi}(b\,x)^{n+1}}{2\,b\,(n+1)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c + b^2*x^2)*erfi(b*x)^n,x)
```

```
[Out] (pi^(1/2)*exp(c)*erfi(b*x)^(n + 1))/(2*b*(n + 1))
```

3.259 $\int e^{c+dx^2} x^5 \mathbf{Erfi}(bx)\, dx$

Optimal. Leaf size=257

$$\frac{3be^{c+\left(b^2+d\right)x^2}x}{4d\left(b^2+d\right)^2\sqrt{\pi}}+\frac{be^{c+\left(b^2+d\right)x^2}x}{d^2\left(b^2+d\right)\sqrt{\pi}}-\frac{be^{c+\left(b^2+d\right)x^2}x^3}{2d\left(b^2+d\right)\sqrt{\pi}}+\frac{e^{c+dx^2}\text{Erfi}(bx)}{d^3}-\frac{e^{c+dx^2}x^2\text{Erfi}(bx)}{d^2}+\frac{e^{c+dx^2}x^4\text{Erfi}(bx)}{2d}-$$

```
[Out] exp(d*x^2+c)*erfi(b*x)/d^3-exp(d*x^2+c)*x^2*erfi(b*x)/d^2+1/2*exp(d*x^2+c)*
x^4*erfi(b*x)/d-3/8*b*exp(c)*erfi(x*(b^2+d)^(1/2))/d/(b^2+d)^(5/2)-1/2*b*ex
p(c)*erfi(x*(b^2+d)^(1/2))/d^2/(b^2+d)^(3/2)-b*exp(c)*erfi(x*(b^2+d)^(1/2))
/d^3/(b^2+d)^(1/2)+3/4*b*exp(c+(b^2+d)*x^2)*x/d/(b^2+d)^2/Pi^(1/2)+b*exp(c+
(b^2+d)*x^2)*x/d^2/(b^2+d)/Pi^(1/2)-1/2*b*exp(c+(b^2+d)*x^2)*x^3/d/(b^2+d)/
Pi^(1/2)
```

Rubi [A]
time = 0.28, antiderivative size = 257, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {6522, 6519, 2235, 2243}

$$-\frac{be^c\text{Erfi}\left(x\sqrt{b^2+d}\right)}{d^3\sqrt{b^2+d}}-\frac{be^c\text{Erfi}\left(x\sqrt{b^2+d}\right)}{2d^2\left(b^2+d\right)^{3/2}}+\frac{bxe^{x^2\left(b^2+d\right)+c}}{\sqrt{\pi}d^2\left(b^2+d\right)}-\frac{3be^c\text{Erfi}\left(x\sqrt{b^2+d}\right)}{8d\left(b^2+d\right)^{5/2}}+\frac{3bxe^{x^2\left(b^2+d\right)+c}}{4\sqrt{\pi}d\left(b^2+d\right)^2}-\frac{bx^3e^{x^2\left(b^2+d\right)+c}}{2\sqrt{\pi}d\left(b^2+d\right)}+\frac{\text{Erfi}(bx)e^{c+dx^2}}{d^3}-\frac{x^2\text{Erfi}(bx)e^{c+dx^2}}{d^2}+\frac{x^4\text{Erfi}(bx)e^{c+dx^2}}{2d}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + d*x^2)*x^5*Erfi[b*x],x]
```

```
[Out] (3*b*E^(c + (b^2 + d)*x^2)*x)/(4*d*(b^2 + d)^2*Sqrt[Pi]) + (b*E^(c + (b^2 +
 d)*x^2)*x)/(d^2*(b^2 + d)*Sqrt[Pi]) - (b*E^(c + (b^2 + d)*x^2)*x^3)/(2*d*(
b^2 + d)*Sqrt[Pi]) + (E^(c + d*x^2)*Erfi[b*x])/d^3 - (E^(c + d*x^2)*x^2*Erf
i[b*x])/d^2 + (E^(c + d*x^2)*x^4*Erfi[b*x])/(2*d) - (3*b*E^c*Erfi[Sqrt[b^2
+ d]*x])/(8*d*(b^2 + d)^(5/2)) - (b*E^c*Erfi[Sqrt[b^2 + d]*x])/(2*d^2*(b^2
+ d)^(3/2)) - (b*E^c*Erfi[Sqrt[b^2 + d]*x])/(d^3*Sqrt[b^2 + d])
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\int e^{c+dx^2}x^5\text{erfi}(bx)\,dx = \frac{e^{c+dx^2}x^4\text{erfi}(bx)}{2d} - \frac{2\int e^{c+dx^2}x^3\text{erfi}(bx)\,dx}{d} - \frac{b\int e^{c+(b^2+d)x^2}x^4\,dx}{d\sqrt{\pi}}$$

$$= -\frac{be^{c+(b^2+d)x^2}x^3}{2d\left(b^2+d\right)\sqrt{\pi}} - \frac{e^{c+dx^2}x^2\text{erfi}(bx)}{d^2} + \frac{e^{c+dx^2}x^4\text{erfi}(bx)}{2d} + \frac{2\int e^{c+dx^2}x\text{erfi}(bx)\,dx}{d^2} + \cdots$$

$$= \frac{3be^{c+(b^2+d)x^2}x}{4d\left(b^2+d\right)^2\sqrt{\pi}} + \frac{be^{c+(b^2+d)x^2}x}{d^2\left(b^2+d\right)\sqrt{\pi}} - \frac{be^{c+(b^2+d)x^2}x^3}{2d\left(b^2+d\right)\sqrt{\pi}} + \frac{e^{c+dx^2}\text{erfi}(bx)}{d^3} - \frac{e^{c+dx^2}x^2\text{e}\cdots}{d^2}$$

$$= \frac{3be^{c+(b^2+d)x^2}x}{4d\left(b^2+d\right)^2\sqrt{\pi}} + \frac{be^{c+(b^2+d)x^2}x}{d^2\left(b^2+d\right)\sqrt{\pi}} - \frac{be^{c+(b^2+d)x^2}x^3}{2d\left(b^2+d\right)\sqrt{\pi}} + \frac{e^{c+dx^2}\text{erfi}(bx)}{d^3} - \frac{e^{c+dx^2}x^2\text{e}\cdots}{d^2}$$

Mathematica [A]
time = 0.20, size = 131, normalized size = 0.51

$$\frac{e^c\left(-\frac{2bde^{(b^2+d)x^2}x(2b^2(-2+dx^2)+d(-7+2dx^2))}{(b^2+d)^2\sqrt{\pi}} + 4e^{dx^2}(2-2dx^2+d^2x^4)\,\text{Erfi}(bx) - \frac{b(8b^4+20b^2d+15d^2)\text{Erfi}\left(\sqrt{b^2+d}\,x\right)}{(b^2+d)^{5/2}}\right)}{8d^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + d*x^2)*x^5*Erfi[b*x],x]
```

```
[Out] (E^c*((-2*b*d*E^((b^2 + d)*x^2)*x*(2*b^2*(-2 + d*x^2) + d*(-7 + 2*d*x^2)))/
((b^2 + d)^2*Sqrt[Pi]) + 4*E^(d*x^2)*(2 - 2*d*x^2 + d^2*x^4)*Erfi[b*x] - (b
*(8*b^4 + 20*b^2*d + 15*d^2)*Erfi[Sqrt[b^2 + d]*x])/(b^2 + d)^(5/2)))/(8*d^
3)
```

Maple [F]
time = 0.11, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^{2}+c} x^{5} \operatorname{erfi}\left(b x\right)d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^5*erfi(b*x),x)
```

```
[Out] int(exp(d*x^2+c)*x^5*erfi(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^5*erfi(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x^5*erfi(b*x)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.40, size = 255, normalized size = 0.99

$$\frac{\pi (8\,b^{5} + 20\,b^{3} d + 15\,b d^{2}) \sqrt{-b^{2} - d}\,\operatorname{erf}\left(\sqrt{-b^{2} - d}\,x\right) e^{c} + 4\,(\pi (b^{6} d^{2} + 3\,b^{4} d^{3} + 3\,b^{2} d^{4} + d^{5}) x^{4} - 2\,\pi (b^{6} d + 3\,b^{4} d^{2} + 3\,b^{2} d^{3} + d^{4}) x^{2} + 2\,\pi (b^{6} + 3\,b^{4} d + 3\,b^{2} d^{2} + d^{3})) \operatorname{erfi}\left(b x\right) e^{(d x^{2} + c)} - 2\,\sqrt{\pi}\,(2\,(b^{5} d^{2} + 2\,b^{3} d^{3} + b d^{4}) x^{3} - (4\,b^{5} d + 11\,b^{3} d^{2} + 7\,b d^{3}) x) e^{(b^{2} x^{2} + d x^{2} + c)}}{8\,\pi (b^{6} d^{3} + 3\,b^{4} d^{4} + 3\,b^{2} d^{5} + d^{6})}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^5*erfi(b*x),x, algorithm="fricas")
```

```
[Out] 1/8*(pi*(8*b^5 + 20*b^3*d + 15*b*d^2)*sqrt(-b^2 - d)*erf(sqrt(-b^2 - d)*x)*
e^c + 4*(pi*(b^6*d^2 + 3*b^4*d^3 + 3*b^2*d^4 + d^5)*x^4 - 2*pi*(b^6*d + 3*b
^4*d^2 + 3*b^2*d^3 + d^4)*x^2 + 2*pi*(b^6 + 3*b^4*d + 3*b^2*d^2 + d^3))*erf
i(b*x)*e^(d*x^2 + c) - 2*sqrt(pi)*(2*(b^5*d^2 + 2*b^3*d^3 + b*d^4)*x^3 - (4
*b^5*d + 11*b^3*d^2 + 7*b*d^3)*x)*e^(b^2*x^2 + d*x^2 + c))/(pi*(b^6*d^3 + 3
*b^4*d^4 + 3*b^2*d^5 + d^6))
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c} \int x^{5} e^{d x^{2}} \operatorname{erfi}{\left(b x \right)}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**5*erfi(b*x),x)
```

```
[Out] exp(c)*Integral(x**5*exp(d*x**2)*erfi(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^5*erfi(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^5*erfi(b*x)*e^(d*x^2 + c), x)
```

Mupad [B]
time = 0.77, size = 232, normalized size = 0.90

$$\mathrm{erfi}(b\,x)\,\left(\frac{{\mathrm{e}}^{d\,x^2+c}}{d^3}-\frac{x^2\,{\mathrm{e}}^{d\,x^2+c}}{d^2}+\frac{x^4\,{\mathrm{e}}^{d\,x^2+c}}{2\,d}\right)-\frac{b\,\mathrm{erfi}\left(x\,\sqrt{b^2+d}\right)\,{\mathrm{e}}^c}{2\,d^2\,{\left(b^2+d\right)}^{3/2}}-\frac{b\,{\mathrm{e}}^c\,\mathrm{erf}\left(x\,\sqrt{-b^2-d}\right)}{d^3\,\sqrt{-b^2-d}}+\frac{b\,x\,{\mathrm{e}}^{b^2\,x^2+d\,x^2+c}}{d^2\,\sqrt{\pi }\,\left(b^2+d\right)}+\frac{b\,x^5\,{\mathrm{e}}^c\,\left(\frac{3\,\sqrt{\pi }\,\mathrm{erfc}\left(\sqrt{-x^2\,\left(b^2+d\right)}\right)}{4}+{\mathrm{e}}^{b^2\,x^2+d\,x^2}\,\left(\frac{3\,\sqrt{-x^2\,\left(b^2+d\right)}}{2}+{\left(-x^2\,\left(b^2+d\right)\right)}^{3/2}\right)-\frac{3\,\sqrt{\pi }}{4}\right)}{2\,d\,\sqrt{\pi }\,{\left(-x^2\,\left(b^2+d\right)\right)}^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*exp(c + d*x^2)*erfi(b*x),x)
```

```
[Out] erfi(b*x)*(exp(c + d*x^2)/d^3 - (x^2*exp(c + d*x^2))/d^2 + (x^4*exp(c + d*x
^2))/(2*d)) - (b*erfi(x*(d + b^2)^(1/2))*exp(c))/(2*d^2*(d + b^2)^(3/2)) -
(b*exp(c)*erf(x*(- d - b^2)^(1/2)))/(d^3*(- d - b^2)^(1/2)) + (b*x*exp(c +
d*x^2 + b^2*x^2))/(d^2*pi^(1/2)*(d + b^2)) + (b*x^5*exp(c)*((3*pi^(1/2)*erf
c((-x^2*(d + b^2))^(1/2)))/4 + exp(d*x^2 + b^2*x^2)*((3*(-x^2*(d + b^2))^(1
/2))/2 + (-x^2*(d + b^2))^(3/2)) - (3*pi^(1/2))/4))/(2*d*pi^(1/2)*(-x^2*(d
+ b^2))^(5/2))
```

3.260 $\int e^{c+dx^2}x^3\text{Erfi}(bx)\,dx$

Optimal. Leaf size=142

$$-\frac{be^{c+(b^2+d)x^2}x}{2d\,(b^2+d)\,\sqrt{\pi}}-\frac{e^{c+dx^2}\text{Erfi}(bx)}{2d^2}+\frac{e^{c+dx^2}x^2\text{Erfi}(bx)}{2d}+\frac{be^c\text{Erfi}\left(\sqrt{b^2+d}\,x\right)}{4d\,(b^2+d)^{3/2}}+\frac{be^c\text{Erfi}\left(\sqrt{b^2+d}\,x\right)}{2d^2\sqrt{b^2+d}}$$

```
[Out] -1/2*exp(d*x^2+c)*erfi(b*x)/d^2+1/2*exp(d*x^2+c)*x^2*erfi(b*x)/d+1/4*b*exp(
c)*erfi(x*(b^2+d)^(1/2))/d/(b^2+d)^(3/2)+1/2*b*exp(c)*erfi(x*(b^2+d)^(1/2))
/d^2/(b^2+d)^(1/2)-1/2*b*exp(c+(b^2+d)*x^2)*x/d/(b^2+d)/Pi^(1/2)
```

Rubi [A]
time = 0.10, antiderivative size = 142, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.235$, Rules used = {6522, 6519, 2235, 2243}

$$\frac{be^c\text{Erfi}\left(x\sqrt{b^2+d}\right)}{2d^2\sqrt{b^2+d}}+\frac{be^c\text{Erfi}\left(x\sqrt{b^2+d}\right)}{4d\,(b^2+d)^{3/2}}-\frac{bxe^{x^2(b^2+d)+c}}{2\sqrt{\pi}\,d\,(b^2+d)}-\frac{\text{Erfi}(bx)e^{c+dx^2}}{2d^2}+\frac{x^2\text{Erfi}(bx)e^{c+dx^2}}{2d}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + d*x^2)*x^3*Erfi[b*x],x]
```

```
[Out] -1/2*(b*E^(c + (b^2 + d)*x^2)*x)/(d*(b^2 + d)*Sqrt[Pi]) - (E^(c + d*x^2)*Er
fi[b*x])/(2*d^2) + (E^(c + d*x^2)*x^2*Erfi[b*x])/(2*d) + (b*E^c*Erfi[Sqrt[b
^2 + d]*x])/(4*d*(b^2 + d)^(3/2)) + (b*E^c*Erfi[Sqrt[b^2 + d]*x])/(2*d^2*Sq
rt[b^2 + d])
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
```

```
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\int e^{c+dx^2}x^3\text{erfi}(bx)\,dx = \frac{e^{c+dx^2}x^2\text{erfi}(bx)}{2d} - \frac{\int e^{c+dx^2}x\text{erfi}(bx)\,dx}{d} - \frac{b\int e^{c+(b^2+d)x^2}x^2\,dx}{d\sqrt{\pi}}$$

$$= -\frac{be^{c+(b^2+d)x^2}x}{2d\,(b^2+d)\,\sqrt{\pi}} - \frac{e^{c+dx^2}\text{erfi}(bx)}{2d^2} + \frac{e^{c+dx^2}x^2\text{erfi}(bx)}{2d} + \frac{b\int e^{c+(b^2+d)x^2}\,dx}{d^2\sqrt{\pi}} + \frac{b\int e^{c+(}}{2d\,(b^2}$$

$$= -\frac{be^{c+(b^2+d)x^2}x}{2d\,(b^2+d)\,\sqrt{\pi}} - \frac{e^{c+dx^2}\text{erfi}(bx)}{2d^2} + \frac{e^{c+dx^2}x^2\text{erfi}(bx)}{2d} + \frac{be^c\text{erfi}\left(\sqrt{b^2+d}\,x\right)}{4d\,(b^2+d)^{3/2}} + \frac{be^c\text{er}}{2}$$

Mathematica [A]
time = 0.12, size = 91, normalized size = 0.64

$$\frac{e^c\left(-\frac{2bde^{(b^2+d)x^2}x}{(b^2+d)\sqrt{\pi}} + 2e^{dx^2}(-1+dx^2)\,\text{Erfi}(bx) + \frac{(2b^3+3bd)\,\text{Erfi}\left(\sqrt{b^2+d}\,x\right)}{(b^2+d)^{3/2}}\right)}{4d^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + d*x^2)*x^3*Erfi[b*x],x]
```

```
[Out] (E^c*((-2*b*d*E^((b^2 + d)*x^2)*x)/((b^2 + d)*Sqrt[Pi]) + 2*E^(d*x^2)*(-1 +
 d*x^2)*Erfi[b*x] + ((2*b^3 + 3*b*d)*Erfi[Sqrt[b^2 + d]*x])/(b^2 + d)^(3/2)
))/(4*d^2)
```

Maple [F]
time = 0.24, size = 0, normalized size = 0.00

$$\int e^{d\,x^2+c}x^3\,\text{erfi}\left(bx\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^3*erfi(b*x),x)
```

```
[Out] int(exp(d*x^2+c)*x^3*erfi(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erfi(b*x),x, algorithm="maxima")
[Out] integrate(x^3*erfi(b*x)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.36, size = 151, normalized size = 1.06

$$-\frac{\pi(2\,b^3+3\,bd)\sqrt{-b^2-d}\,\operatorname{erf}\left(\sqrt{-b^2-d}\,x\right)e^c+2\,\sqrt{\pi}\,(b^3d+bd^2)xe^{(b^2x^2+dx^2+c)}-2\,(\pi(b^4d+2\,b^2d^2+d^3)x^2-\pi(b^4+2\,b^2d+d^2))\operatorname{erfi}(bx)\,e^{(dx^2+c)}}{4\,\pi(b^4d^2+2\,b^2d^3+d^4)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erfi(b*x),x, algorithm="fricas")
[Out] -1/4*(pi*(2*b^3 + 3*b*d)*sqrt(-b^2 - d)*erf(sqrt(-b^2 - d)*x)*e^c + 2*sqrt(
pi)*(b^3*d + b*d^2)*x*e^(b^2*x^2 + d*x^2 + c) - 2*(pi*(b^4*d + 2*b^2*d^2 +
d^3)*x^2 - pi*(b^4 + 2*b^2*d + d^2))*erfi(b*x)*e^(d*x^2 + c))/(pi*(b^4*d^2
+ 2*b^2*d^3 + d^4))
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int x^{3}e^{dx^{2}}\operatorname{erfi}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**3*erfi(b*x),x)
[Out] exp(c)*Integral(x**3*exp(d*x**2)*erfi(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erfi(b*x),x, algorithm="giac")
[Out] integrate(x^3*erfi(b*x)*e^(d*x^2 + c), x)
```

Mupad [B]
time = 0.59, size = 128, normalized size = 0.90

$$\frac{b\,\mathrm{erfi}\left(x\,\sqrt{b^2+d}\right)\,\mathrm{e}^c}{4\,d\,{\left(b^2+d\right)}^{3/2}}-\mathrm{erfi}(b\,x)\,\left(\frac{\mathrm{e}^{d\,x^2+c}}{2\,d^2}-\frac{x^2\,\mathrm{e}^{d\,x^2+c}}{2\,d}\right)-\frac{b\,x\,\mathrm{e}^{b^2\,x^2+d\,x^2+c}}{2\,\sqrt{\pi}\,\left(b^2\,d+d^2\right)}+\frac{b\,\mathrm{e}^c\,\mathrm{erf}\left(x\,\sqrt{-b^2-d}\right)}{2\,d^2\,\sqrt{-b^2-d}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*exp(c + d*x^2)*erfi(b*x),x)
```

```
[Out] (b*erfi(x*(d + b^2)^(1/2))*exp(c))/(4*d*(d + b^2)^(3/2)) - erfi(b*x)*(exp(c
 + d*x^2)/(2*d^2) - (x^2*exp(c + d*x^2))/(2*d)) - (b*x*exp(c + d*x^2 + b^2*
x^2))/(2*pi^(1/2)*(b^2*d + d^2)) + (b*exp(c)*erf(x*(- d - b^2)^(1/2)))/(2*d
^2*(- d - b^2)^(1/2))
```

3.261 $\int e^{c+dx^2} x \mathbf{Erfi}(bx)\, dx$

Optimal. Leaf size=53

$$\frac{e^{c+dx^2}\text{Erfi}(bx)}{2d}-\frac{be^c\text{Erfi}\left(\sqrt{b^2+d}\,x\right)}{2d\sqrt{b^2+d}}$$

```
[Out] 1/2*exp(d*x^2+c)*erfi(b*x)/d-1/2*b*exp(c)*erfi(x*(b^2+d)^(1/2))/d/(b^2+d)^(
1/2)
```

Rubi [A]
time = 0.03, antiderivative size = 53, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}}=0.133$, Rules used = {6519, 2235}

$$\frac{\text{Erfi}(bx)e^{c+dx^2}}{2d}-\frac{be^c\text{Erfi}\left(x\sqrt{b^2+d}\right)}{2d\sqrt{b^2+d}}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + d*x^2)*x*Erfi[b*x],x]
```

```
[Out] (E^(c + d*x^2)*Erfi[b*x])/(2*d) - (b*E^c*Erfi[Sqrt[b^2 + d]*x])/(2*d*Sqrt[b
^2 + d])
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\begin{aligned}\int e^{c+dx^2}x\text{erfi}(bx)\,dx&=\frac{e^{c+dx^2}\text{erfi}(bx)}{2d}-\frac{b\int e^{c+\left(b^2+d\right)x^2}\,dx}{d\sqrt{\pi}}\\&=\frac{e^{c+dx^2}\text{erfi}(bx)}{2d}-\frac{be^c\text{erfi}\left(\sqrt{b^2+d}\,x\right)}{2d\sqrt{b^2+d}}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 47, normalized size = 0.89

$$\frac{e^c\left(e^{dx^2}\mathrm{Erfi}(bx)-\frac{b\mathrm{Erfi}\left(\sqrt{b^2+d}\,x\right)}{\sqrt{b^2+d}}\right)}{2d}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + d*x^2)*x*Erfi[b*x],x]
```

```
[Out] (E^c*(E^(d*x^2)*Erfi[b*x] - (b*Erfi[Sqrt[b^2 + d]*x])/Sqrt[b^2 + d]))/(2*d)
```

Maple [F]
time = 0.24, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^2+c} x \,\mathrm{erfi}\,(bx)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x*erfi(b*x),x)
```

```
[Out] int(exp(d*x^2+c)*x*erfi(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erfi(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x*erfi(b*x)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.35, size = 61, normalized size = 1.15

$$\frac{\sqrt{-b^2-d}\,b\,\mathrm{erf}\left(\sqrt{-b^2-d}\,x\right)e^c+(b^2+d)\,\mathrm{erfi}\,(bx)\,e^{(dx^2+c)}}{2\,(b^2d+d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erfi(b*x),x, algorithm="fricas")
```

```
[Out] 1/2*(sqrt(-b^2 - d)*b*erf(sqrt(-b^2 - d)*x)*e^c + (b^2 + d)*erfi(b*x)*e^(d*
x^2 + c))/(b^2*d + d^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int xe^{dx^{2}}\operatorname{erfi}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x*erfi(b*x),x)
```

```
[Out] exp(c)*Integral(x*exp(d*x**2)*erfi(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erfi(b*x),x, algorithm="giac")
```

```
[Out] integrate(x*erfi(b*x)*e^(d*x^2 + c), x)
```

Mupad [B]
time = 0.17, size = 51, normalized size = 0.96

$$\frac{\mathrm{e}^{d\,x^2}\,\mathrm{e}^{c}\,\mathrm{erfi}(b\,x)}{2\,d}-\frac{b\,\mathrm{e}^{c}\,\mathrm{erf}\left(x\,\sqrt{-b^2-d}\right)}{2\,d\,\sqrt{-b^2-d}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*exp(c + d*x^2)*erfi(b*x),x)
```

```
[Out] (exp(d*x^2)*exp(c)*erfi(b*x))/(2*d) - (b*exp(c)*erf(x*(- d - b^2)^(1/2)))/(
2*d*(- d - b^2)^(1/2))
```

3.262 $\int \frac{e^{c+dx^2}\mathbf{Erfi}(bx)}{x}\,dx$

Optimal. Leaf size=20

$$\operatorname{Int}\left(\frac{e^{c+dx^2}\operatorname{Erfi}(bx)}{x},x\right)$$

```
[Out] Unintegrable(exp(d*x^2+c)*erfi(b*x)/x,x)
```

Rubi [A]
time = 0.03, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\operatorname{Erfi}(bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfi[b*x])/x,x]
[Out] Defer[Int][(E^(c + d*x^2)*Erfi[b*x])/x, x]
```

Rubi steps

$$\int \frac{e^{c+dx^2}\operatorname{erfi}(bx)}{x}\,dx = \int \frac{e^{c+dx^2}\operatorname{erfi}(bx)}{x}\,dx$$

Mathematica [A]
time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\operatorname{Erfi}(bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfi[b*x])/x,x]
[Out] Integrate[(E^(c + d*x^2)*Erfi[b*x])/x, x]
```

Maple [A]
time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{e^{d\,x^2+c}\operatorname{erfi}(bx)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfi(b*x)/x,x)
```

```
[Out] int(exp(d*x^2+c)*erfi(b*x)/x,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x)/x,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)*e^(d*x^2 + c)/x, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x)/x,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x)*e^(d*x^2 + c)/x, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int\frac{e^{dx^{2}}\operatorname{erfi}\left(bx\right)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfi(b*x)/x,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erfi(b*x)/x, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x)/x,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)*e^(d*x^2 + c)/x, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{e^{d\,x^2+c}\,\mathrm{erfi}(b\,x)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + d*x^2)*erfi(b*x))/x,x)
[Out] int((exp(c + d*x^2)*erfi(b*x))/x, x)
```

3.263 $\int \frac{e^{c+dx^2}\mathbf{Erfi}(bx)}{x^3}\,dx$

Optimal. Leaf size=93

$$-\frac{be^{c+(b^2+d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\text{Erfi}(bx)}{2x^2}+b\sqrt{b^2+d}\,e^c\text{Erfi}\left(\sqrt{b^2+d}\,x\right)+d\text{Int}\left(\frac{e^{c+dx^2}\text{Erfi}(bx)}{x},x\right)$$

```
[Out] -1/2*exp(d*x^2+c)*erfi(b*x)/x^2+b*exp(c)*erfi(x*(b^2+d)^(1/2))*(b^2+d)^(1/2
)-b*exp(c+(b^2+d)*x^2)/x/Pi^(1/2)+d*Unintegrable(exp(d*x^2+c)*erfi(b*x)/x,x
)
```

Rubi [A]
time = 0.09, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\text{Erfi}(bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfi[b*x])/x^3,x]
```

```
[Out] -((b*E^(c + (b^2 + d)*x^2))/(Sqrt[Pi]*x)) - (E^(c + d*x^2)*Erfi[b*x])/(2*x^
2) + b*Sqrt[b^2 + d]*E^c*Erfi[Sqrt[b^2 + d]*x] + d*Defer[Int][(E^(c + d*x^2
)*Erfi[b*x])/x, x]
```

Rubi steps

$$\begin{aligned}
\int \frac{e^{c+dx^2}\text{erfi}(bx)}{x^3}\,dx &= -\frac{e^{c+dx^2}\text{erfi}(bx)}{2x^2}+d\int \frac{e^{c+dx^2}\text{erfi}(bx)}{x}\,dx+\frac{b\int \frac{e^{c+\left(b^2+d\right)x^2}}{x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{be^{c+(b^2+d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\text{erfi}(bx)}{2x^2}+d\int \frac{e^{c+dx^2}\text{erfi}(bx)}{x}\,dx+\frac{(2b(b^2+d))\int e^{c+(b^2+d)x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{be^{c+(b^2+d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\text{erfi}(bx)}{2x^2}+b\sqrt{b^2+d}\,e^c\text{erfi}\left(\sqrt{b^2+d}\,x\right)+d\int \frac{e^{c+dx^2}\text{erfi}(bx)}{x}\,dx
\end{aligned}$$

Mathematica [A]
time = 0.14, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\text{Erfi}(bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfi[b*x])/x^3,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erfi[b*x])/x^3, x]
```

Maple [A]
time = 0.27, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^{2}+c}\,\mathrm{erfi}\left(b x\right)}{x^{3}}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfi(b*x)/x^3,x)
```

```
[Out] int(exp(d*x^2+c)*erfi(b*x)/x^3,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x)/x^3,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)*e^(d*x^2 + c)/x^3, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x)/x^3,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x)*e^(d*x^2 + c)/x^3, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c} \int \frac{e^{dx^{2}} \operatorname{erfi}\left(bx\right)}{x^{3}}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfi(b*x)/x**3,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erfi(b*x)/x**3, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x)/x^3,x, algorithm="giac")
[Out] integrate(erfi(b*x)*e^(d*x^2 + c)/x^3, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{e^{d\,x^2+c}\,\mathrm{erfi}(b\,x)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + d*x^2)*erfi(b*x))/x^3,x)
[Out] int((exp(c + d*x^2)*erfi(b*x))/x^3, x)
```

3.264 $\int \frac{e^{c+dx^2}\mathbf{Erfi}(bx)}{x^5}\,dx$

Optimal. Leaf size=212

$$-\frac{be^{c+(b^2+d)x^2}}{6\sqrt{\pi}\,x^3}-\frac{bde^{c+(b^2+d)x^2}}{2\sqrt{\pi}\,x}-\frac{b(b^2+d)\,e^{c+(b^2+d)x^2}}{3\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\text{Erfi}(bx)}{4x^4}-\frac{de^{c+dx^2}\text{Erfi}(bx)}{4x^2}+\frac{1}{2}bd\sqrt{b^2+d}\,e^c\text{Erfi}\Big(\sqrt{}$$

```
[Out] -1/4*exp(d*x^2+c)*erfi(b*x)/x^4-1/4*d*exp(d*x^2+c)*erfi(b*x)/x^2+1/3*b*(b^2
+d)^(3/2)*exp(c)*erfi(x*(b^2+d)^(1/2))+1/2*b*d*exp(c)*erfi(x*(b^2+d)^(1/2))
*(b^2+d)^(1/2)-1/6*b*exp(c+(b^2+d)*x^2)/x^3/Pi^(1/2)-1/2*b*d*exp(c+(b^2+d)*
x^2)/x/Pi^(1/2)-1/3*b*(b^2+d)*exp(c+(b^2+d)*x^2)/x/Pi^(1/2)+1/2*d^2*Unintegrable(exp(d*x^2+c)*erfi(b*x)/x,x)
```

Rubi [A]
time = 0.21, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\text{Erfi}(bx)}{x^5}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfi[b*x])/x^5,x]
```

```
[Out] -1/6*(b*E^(c + (b^2 + d)*x^2))/(Sqrt[Pi]*x^3) - (b*d*E^(c + (b^2 + d)*x^2))
/(2*Sqrt[Pi]*x) - (b*(b^2 + d)*E^(c + (b^2 + d)*x^2))/(3*Sqrt[Pi]*x) - (E^(
c + d*x^2)*Erfi[b*x])/(4*x^4) - (d*E^(c + d*x^2)*Erfi[b*x])/(4*x^2) + (b*d*
Sqrt[b^2 + d]*E^c*Erfi[Sqrt[b^2 + d]*x])/2 + (b*(b^2 + d)^(3/2)*E^c*Erfi[Sq
rt[b^2 + d]*x])/3 + (d^2*Defer[Int][(E^(c + d*x^2)*Erfi[b*x])/x, x])/2
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+dx^2}\text{erfi}(bx)}{x^5}\,dx &= -\frac{e^{c+dx^2}\text{erfi}(bx)}{4x^4}+\frac{1}{2}d\int \frac{e^{c+dx^2}\text{erfi}(bx)}{x^3}\,dx+\frac{b\int \frac{e^{c+(b^2+d)x^2}}{x^4}\,dx}{2\sqrt{\pi}}\\ &= -\frac{be^{c+(b^2+d)x^2}}{6\sqrt{\pi}\,x^3}-\frac{e^{c+dx^2}\text{erfi}(bx)}{4x^4}-\frac{de^{c+dx^2}\text{erfi}(bx)}{4x^2}+\frac{1}{2}d^2\int \frac{e^{c+dx^2}\text{erfi}(bx)}{x}\,dx+\frac{(bd)\int e}{2}\\ &= -\frac{be^{c+(b^2+d)x^2}}{6\sqrt{\pi}\,x^3}-\frac{bde^{c+(b^2+d)x^2}}{2\sqrt{\pi}\,x}-\frac{b(b^2+d)\,e^{c+(b^2+d)x^2}}{3\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\text{erfi}(bx)}{4x^4}-\frac{de^{c+dx^2}\text{erfi}(bx}{4x^2}\\ &= -\frac{be^{c+(b^2+d)x^2}}{6\sqrt{\pi}\,x^3}-\frac{bde^{c+(b^2+d)x^2}}{2\sqrt{\pi}\,x}-\frac{b(b^2+d)\,e^{c+(b^2+d)x^2}}{3\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\text{erfi}(bx)}{4x^4}-\frac{de^{c+dx^2}\text{erfi}(bx}{4x^2}\end{aligned}$$

Mathematica [A]
time = 0.17, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\mathrm{Erfi}(bx)}{x^5}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfi[b*x])/x^5,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erfi[b*x])/x^5, x]
```

Maple [A]
time = 0.29, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\,\mathrm{erfi}\left(bx\right)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfi(b*x)/x^5,x)
```

```
[Out] int(exp(d*x^2+c)*erfi(b*x)/x^5,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x)/x^5,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)*e^(d*x^2 + c)/x^5, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x)/x^5,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x)*e^(d*x^2 + c)/x^5, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^2}\,\mathrm{erfi}\left(bx\right)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfi(b*x)/x**5,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erfi(b*x)/x**5, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x)/x^5,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)*e^(d*x^2 + c)/x^5, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\,\mathrm{erfi}(b\,x)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + d*x^2)*erfi(b*x))/x^5,x)
```

```
[Out] int((exp(c + d*x^2)*erfi(b*x))/x^5, x)
```

3.265 $\int e^{c+dx^2} x^4 \mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=171

$$\frac{be^{c+(b^2+d)x^2}}{2d(b^2+d)^2\sqrt{\pi}}+\frac{3be^{c+(b^2+d)x^2}}{4d^2(b^2+d)\sqrt{\pi}}-\frac{be^{c+(b^2+d)x^2}x^2}{2d(b^2+d)\sqrt{\pi}}-\frac{3e^{c+dx^2}x\mathrm{Erfi}(bx)}{4d^2}+\frac{e^{c+dx^2}x^3\mathrm{Erfi}(bx)}{2d}+\frac{3\mathrm{Int}\left(e^{c+dx^2}\mathrm{Er}\right.}{4d^2}$$

```
[Out] -3/4*exp(d*x^2+c)*x*erfi(b*x)/d^2+1/2*exp(d*x^2+c)*x^3*erfi(b*x)/d+1/2*b*ex
p(c+(b^2+d)*x^2)/d/(b^2+d)^2/Pi^(1/2)+3/4*b*exp(c+(b^2+d)*x^2)/d^2/(b^2+d)/
Pi^(1/2)-1/2*b*exp(c+(b^2+d)*x^2)*x^2/d/(b^2+d)/Pi^(1/2)+3/4*Unintegrable(e
xp(d*x^2+c)*erfi(b*x),x)/d^2
```

Rubi [A]
time = 0.15, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$,
Rules used = {}

$$\int e^{c+dx^2} x^4 \mathrm{Erfi}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*x^4*Erfi[b*x],x]
```

```
[Out] (b*E^(c + (b^2 + d)*x^2))/(2*d*(b^2 + d)^2*Sqrt[Pi]) + (3*b*E^(c + (b^2 + d
)*x^2))/(4*d^2*(b^2 + d)*Sqrt[Pi]) - (b*E^(c + (b^2 + d)*x^2)*x^2)/(2*d*(b^
2 + d)*Sqrt[Pi]) - (3*E^(c + d*x^2)*x*Erfi[b*x])/(4*d^2) + (E^(c + d*x^2)*x
^3*Erfi[b*x])/(2*d) + (3*Defer[Int][E^(c + d*x^2)*Erfi[b*x], x])/(4*d^2)
```

Rubi steps

$$\begin{aligned}
\int e^{c+dx^2} x^4 \mathrm{erfi}(bx)\,dx &= \frac{e^{c+dx^2}x^3\mathrm{erfi}(bx)}{2d}-\frac{3\int e^{c+dx^2}x^2\mathrm{erfi}(bx)\,dx}{2d}-\frac{b\int e^{c+(b^2+d)x^2}x^3\,dx}{d\sqrt{\pi}}\\
&= -\frac{be^{c+(b^2+d)x^2}x^2}{2d(b^2+d)\sqrt{\pi}}-\frac{3e^{c+dx^2}x\mathrm{erfi}(bx)}{4d^2}+\frac{e^{c+dx^2}x^3\mathrm{erfi}(bx)}{2d}+\frac{3\int e^{c+dx^2}\mathrm{erfi}(bx)\,dx}{4d^2}+\\
&= \frac{be^{c+(b^2+d)x^2}}{2d(b^2+d)^2\sqrt{\pi}}+\frac{3be^{c+(b^2+d)x^2}}{4d^2(b^2+d)\sqrt{\pi}}-\frac{be^{c+(b^2+d)x^2}x^2}{2d(b^2+d)\sqrt{\pi}}-\frac{3e^{c+dx^2}x\mathrm{erfi}(bx)}{4d^2}+\frac{e^{c+d}}{}
\end{aligned}$$

Mathematica [A]
time = 0.20, size = 0, normalized size = 0.00

$$\int e^{c+dx^2} x^4 \mathrm{Erfi}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*x^4*Erfi[b*x],x]
```

```
[Out] Integrate[E^(c + d*x^2)*x^4*Erfi[b*x], x]
```

Maple [A]
time = 0.10, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^2+c} x^4\,\mathrm{erfi}\left(bx\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^4*erfi(b*x),x)
```

```
[Out] int(exp(d*x^2+c)*x^4*erfi(b*x),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erfi(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x^4*erfi(b*x)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erfi(b*x),x, algorithm="fricas")
```

```
[Out] integral(x^4*erfi(b*x)*e^(d*x^2 + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int x^{4} e^{dx^{2}}\,\mathrm{erfi}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**4*erfi(b*x),x)
```

```
[Out] exp(c)*Integral(x**4*exp(d*x**2)*erfi(b*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erfi(b*x),x, algorithm="giac")
[Out] integrate(x^4*erfi(b*x)*e^(d*x^2 + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^4\,\mathrm{e}^{d\,x^2+c}\,\mathrm{erfi}(b\,x)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*exp(c + d*x^2)*erfi(b*x),x)
[Out] int(x^4*exp(c + d*x^2)*erfi(b*x), x)
```

3.266 $\int e^{c+dx^2}x^2\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=79

$$-\frac{be^{c+(b^2+d)x^2}}{2d\,(b^2+d)\,\sqrt{\pi}}+\frac{e^{c+dx^2}x\mathrm{Erfi}(bx)}{2d}-\frac{\mathrm{Int}\left(e^{c+dx^2}\mathrm{Erfi}(bx),x\right)}{2d}$$

```
[Out] 1/2*exp(d*x^2+c)*x*erfi(b*x)/d-1/2*b*exp(c+(b^2+d)*x^2)/d/(b^2+d)/Pi^(1/2)-
1/2*Unintegrable(exp(d*x^2+c)*erfi(b*x),x)/d
```

Rubi [A]
time = 0.06, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}}=0.000$, Rules used = {}

$$\int e^{c+dx^2}x^2\mathrm{Erfi}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*x^2*Erfi[b*x],x]
```

```
[Out] -1/2*(b*E^(c + (b^2 + d)*x^2))/(d*(b^2 + d)*Sqrt[Pi]) + (E^(c + d*x^2)*x*Er
fi[b*x])/(2*d) - Defer[Int][E^(c + d*x^2)*Erfi[b*x], x]/(2*d)
```

Rubi steps

$$\begin{aligned}\int e^{c+dx^2}x^2\mathrm{erfi}(bx)\,dx&=\frac{e^{c+dx^2}x\mathrm{erfi}(bx)}{2d}-\frac{\int e^{c+dx^2}\mathrm{erfi}(bx)\,dx}{2d}-\frac{b\int e^{c+(b^2+d)x^2}x\,dx}{d\sqrt{\pi}}\\&=-\frac{be^{c+(b^2+d)x^2}}{2d\,(b^2+d)\,\sqrt{\pi}}+\frac{e^{c+dx^2}x\mathrm{erfi}(bx)}{2d}-\frac{\int e^{c+dx^2}\mathrm{erfi}(bx)\,dx}{2d}\end{aligned}$$

Mathematica [A]
time = 0.16, size = 0, normalized size = 0.00

$$\int e^{c+dx^2}x^2\mathrm{Erfi}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*x^2*Erfi[b*x],x]
```

```
[Out] Integrate[E^(c + d*x^2)*x^2*Erfi[b*x], x]
```

Maple [A]
time = 0.21, size = 0, normalized size = 0.00

$$\int e^{d\,x^2+c}x^2\,\mathrm{erfi}\left(bx\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^2*erfi(b*x),x)
```

```
[Out] int(exp(d*x^2+c)*x^2*erfi(b*x),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erfi(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x^2*erfi(b*x)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erfi(b*x),x, algorithm="fricas")
```

```
[Out] integral(x^2*erfi(b*x)*e^(d*x^2 + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int x^{2}e^{dx^{2}}\,\mathrm{erfi}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**2*erfi(b*x),x)
```

```
[Out] exp(c)*Integral(x**2*exp(d*x**2)*erfi(b*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erfi(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^2*erfi(b*x)*e^(d*x^2 + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^2\,\mathrm{e}^{d\,x^2+c}\,\mathrm{erfi}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*exp(c + d*x^2)*erfi(b*x),x)
```

```
[Out] int(x^2*exp(c + d*x^2)*erfi(b*x), x)
```

3.267 $\int e^{c+dx^2}\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=17

$$\mathrm{Int}\left(e^{c+dx^2}\mathrm{Erfi}(bx),x\right)$$

```
[Out] Unintegrable(exp(d*x^2+c)*erfi(b*x),x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int e^{c+dx^2}\mathrm{Erfi}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*Erfi[b*x],x]
```

```
[Out] Defer[Int][E^(c + d*x^2)*Erfi[b*x], x]
```

Rubi steps

$$\int e^{c+dx^2}\mathrm{erfi}(bx)\,dx = \int e^{c+dx^2}\mathrm{erfi}(bx)\,dx$$

Mathematica [A]
time = 0.02, size = 0, normalized size = 0.00

$$\int e^{c+dx^2}\mathrm{Erfi}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*Erfi[b*x],x]
```

```
[Out] Integrate[E^(c + d*x^2)*Erfi[b*x], x]
```

Maple [A]
time = 0.10, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^2+c}\,\mathrm{erfi}\left(bx\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfi(b*x),x)
[Out] int(exp(d*x^2+c)*erfi(b*x),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x),x, algorithm="maxima")
[Out] integrate(erfi(b*x)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x),x, algorithm="fricas")
[Out] integral(erfi(b*x)*e^(d*x^2 + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int e^{dx^{2}}\operatorname{erfi}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfi(b*x),x)
[Out] exp(c)*Integral(exp(d*x**2)*erfi(b*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x),x, algorithm="giac")
[Out] integrate(erfi(b*x)*e^(d*x^2 + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.06

$$\int \mathrm{e}^{d\,x^2+c}\,\mathrm{erfi}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c + d*x^2)*erfi(b*x),x)
```

```
[Out] int(exp(c + d*x^2)*erfi(b*x), x)
```

3.268 $\int \frac{e^{c+dx^2}\mathbf{Erfi}(bx)}{x^2}\,dx$

Optimal. Leaf size=59

$$-\frac{e^{c+dx^2}\text{Erfi}(bx)}{x}+\frac{be^c\text{Ei}\left(\left(b^2+d\right)x^2\right)}{\sqrt{\pi}}+2d\text{Int}\left(e^{c+dx^2}\text{Erfi}(bx),x\right)$$

```
[Out] -exp(d*x^2+c)*erfi(b*x)/x+b*exp(c)*Ei((b^2+d)*x^2)/Pi^(1/2)+2*d*Unintegrabl
e(exp(d*x^2+c)*erfi(b*x),x)
```

Rubi [A]
time = 0.07, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\text{Erfi}(bx)}{x^2}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfi[b*x])/x^2,x]
```

```
[Out] -((E^(c + d*x^2)*Erfi[b*x])/x) + (b*E^c*ExpIntegralEi[(b^2 + d)*x^2])/Sqrt[
Pi] + 2*d*Defer[Int][E^(c + d*x^2)*Erfi[b*x], x]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+dx^2}\text{erfi}(bx)}{x^2}\,dx &= -\frac{e^{c+dx^2}\text{erfi}(bx)}{x}+(2d)\int e^{c+dx^2}\text{erfi}(bx)\,dx+\frac{(2b)\int \frac{e^{c+\left(b^2+d\right)x^2}}{x}\,dx}{\sqrt{\pi}}\\ &= -\frac{e^{c+dx^2}\text{erfi}(bx)}{x}+\frac{be^c\text{Ei}\left(\left(b^2+d\right)x^2\right)}{\sqrt{\pi}}+(2d)\int e^{c+dx^2}\text{erfi}(bx)\,dx\end{aligned}$$

Mathematica [A]
time = 0.14, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\text{Erfi}(bx)}{x^2}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfi[b*x])/x^2,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erfi[b*x])/x^2, x]
```

Maple [A]
time = 0.11, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\,\mathrm{erfi}\left(bx\right)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfi(b*x)/x^2,x)
```

```
[Out] int(exp(d*x^2+c)*erfi(b*x)/x^2,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x)/x^2,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)*e^(d*x^2 + c)/x^2, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x)/x^2,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x)*e^(d*x^2 + c)/x^2, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^2}\,\mathrm{erfi}\left(bx\right)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfi(b*x)/x**2,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erfi(b*x)/x**2, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x)/x^2,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)*e^(d*x^2 + c)/x^2, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{e^{d\,x^2+c}\,\mathrm{erfi}(b\,x)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + d*x^2)*erfi(b*x))/x^2,x)
```

```
[Out] int((exp(c + d*x^2)*erfi(b*x))/x^2, x)
```

3.269 $\int \frac{e^{c+dx^2}\mathbf{Erfi}(bx)}{x^4}\,dx$

Optimal. Leaf size=144

$$-\frac{be^{c+(b^2+d)x^2}}{3\sqrt{\pi}\,x^2}-\frac{e^{c+dx^2}\mathrm{Erfi}(bx)}{3x^3}-\frac{2de^{c+dx^2}\mathrm{Erfi}(bx)}{3x}+\frac{2bde^c\mathrm{Ei}\left(\left(b^2+d\right)x^2\right)}{3\sqrt{\pi}}+\frac{b\left(b^2+d\right)e^c\mathrm{Ei}\left(\left(b^2+d\right)x^2\right)}{3\sqrt{\pi}}+\frac{4}{3}d^2\mathrm{In}$$

```
[Out] -1/3*exp(d*x^2+c)*erfi(b*x)/x^3-2/3*d*exp(d*x^2+c)*erfi(b*x)/x-1/3*b*exp(c+
(b^2+d)*x^2)/x^2/Pi^(1/2)+2/3*b*d*exp(c)*Ei((b^2+d)*x^2)/Pi^(1/2)+1/3*b*(b^
2+d)*exp(c)*Ei((b^2+d)*x^2)/Pi^(1/2)+4/3*d^2*Unintegrable(exp(d*x^2+c)*erfi
(b*x),x)
```

Rubi [A]
time = 0.17, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\mathrm{Erfi}(bx)}{x^4}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfi[b*x])/x^4,x]
```

```
[Out] -1/3*(b*E^(c + (b^2 + d)*x^2))/(Sqrt[Pi]*x^2) - (E^(c + d*x^2)*Erfi[b*x])/(
3*x^3) - (2*d*E^(c + d*x^2)*Erfi[b*x])/(3*x) + (2*b*d*E^c*ExpIntegralEi[(b^
2 + d)*x^2])/(3*Sqrt[Pi]) + (b*(b^2 + d)*E^c*ExpIntegralEi[(b^2 + d)*x^2])/
(3*Sqrt[Pi]) + (4*d^2*Defer[Int][E^(c + d*x^2)*Erfi[b*x], x])/3
```

Rubi steps

$$\begin{aligned}
\int \frac{e^{c+dx^2}\mathrm{erfi}(bx)}{x^4}\,dx &= -\frac{e^{c+dx^2}\mathrm{erfi}(bx)}{3x^3}+\frac{1}{3}(2d)\int \frac{e^{c+dx^2}\mathrm{erfi}(bx)}{x^2}\,dx+\frac{(2b)\int \frac{e^{c+\left(b^2+d\right)x^2}}{x^3}\,dx}{3\sqrt{\pi}}\\
&= -\frac{be^{c+(b^2+d)x^2}}{3\sqrt{\pi}\,x^2}-\frac{e^{c+dx^2}\mathrm{erfi}(bx)}{3x^3}-\frac{2de^{c+dx^2}\mathrm{erfi}(bx)}{3x}+\frac{1}{3}\left(4d^2\right)\int e^{c+dx^2}\mathrm{erfi}(bx)\,dx+\frac{(4\\
&= -\frac{be^{c+(b^2+d)x^2}}{3\sqrt{\pi}\,x^2}-\frac{e^{c+dx^2}\mathrm{erfi}(bx)}{3x^3}-\frac{2de^{c+dx^2}\mathrm{erfi}(bx)}{3x}+\frac{2bde^c\mathrm{Ei}\left(\left(b^2+d\right)x^2\right)}{3\sqrt{\pi}}+\frac{b(b^2+d
\end{aligned}$$

Mathematica [A]
time = 0.20, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\mathrm{Erfi}(bx)}{x^4}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfi[b*x])/x^4,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erfi[b*x])/x^4, x]
```

Maple [A]
time = 0.27, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\,\mathrm{erfi}\,(bx)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfi(b*x)/x^4,x)
```

```
[Out] int(exp(d*x^2+c)*erfi(b*x)/x^4,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x)/x^4,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)*e^(d*x^2 + c)/x^4, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x)/x^4,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x)*e^(d*x^2 + c)/x^4, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^2}\,\mathrm{erfi}\,(bx)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfi(b*x)/x**4,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erfi(b*x)/x**4, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x)/x^4,x, algorithm="giac")
[Out] integrate(erfi(b*x)*e^(d*x^2 + c)/x^4, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{d\,x^2+c}\,\mathrm{erfi}(b\,x)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + d*x^2)*erfi(b*x))/x^4,x)
[Out] int((exp(c + d*x^2)*erfi(b*x))/x^4, x)
```

3.270 $\int e^{-b^2x^2}x^5\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=107

$$\frac{2x}{b^5\sqrt{\pi}}+\frac{2x^3}{3b^3\sqrt{\pi}}+\frac{x^5}{5b\sqrt{\pi}}-\frac{e^{-b^2x^2}\text{Erfi}(bx)}{b^6}-\frac{e^{-b^2x^2}x^2\text{Erfi}(bx)}{b^4}-\frac{e^{-b^2x^2}x^4\text{Erfi}(bx)}{2b^2}$$

```
[Out] -erfi(b*x)/b^6/exp(b^2*x^2)-x^2*erfi(b*x)/b^4/exp(b^2*x^2)-1/2*x^4*erfi(b*x
)/b^2/exp(b^2*x^2)+2*x/b^5/Pi^(1/2)+2/3*x^3/b^3/Pi^(1/2)+1/5*x^5/b/Pi^(1/2)
```

Rubi [A]
time = 0.07, antiderivative size = 107, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {6522, 6519, 8, 30}

$$\frac{2x}{\sqrt{\pi}b^5}+\frac{2x^3}{3\sqrt{\pi}b^3}-\frac{x^4e^{-b^2x^2}\text{Erfi}(bx)}{2b^2}-\frac{e^{-b^2x^2}\text{Erfi}(bx)}{b^6}-\frac{x^2e^{-b^2x^2}\text{Erfi}(bx)}{b^4}+\frac{x^5}{5\sqrt{\pi}b}$$

Antiderivative was successfully verified.

```
[In] Int[(x^5*Erfi[b*x])/E^(b^2*x^2),x]
```

```
[Out] (2*x)/(b^5*Sqrt[Pi]) + (2*x^3)/(3*b^3*Sqrt[Pi]) + x^5/(5*b*Sqrt[Pi]) - Erfi
[b*x]/(b^6*E^(b^2*x^2)) - (x^2*Erfi[b*x])/(b^4*E^(b^2*x^2)) - (x^4*Erfi[b*x
])/(2*b^2*E^(b^2*x^2))
```

Rule 8

```
Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
```

```
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$
\begin{aligned}
\int e^{-b^2x^2}x^5\operatorname{erfi}(bx)\,dx &= -\frac{e^{-b^2x^2}x^4\operatorname{erfi}(bx)}{2b^2}+\frac{2\int e^{-b^2x^2}x^3\operatorname{erfi}(bx)\,dx}{b^2}+\frac{\int x^4\,dx}{b\sqrt{\pi}}\\
&= \frac{x^5}{5b\sqrt{\pi}}-\frac{e^{-b^2x^2}x^2\operatorname{erfi}(bx)}{b^4}-\frac{e^{-b^2x^2}x^4\operatorname{erfi}(bx)}{2b^2}+\frac{2\int e^{-b^2x^2}x\operatorname{erfi}(bx)\,dx}{b^4}+\frac{2\int x^2\,dx}{b^3\sqrt{\pi}}\\
&= \frac{2x^3}{3b^3\sqrt{\pi}}+\frac{x^5}{5b\sqrt{\pi}}-\frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{b^6}-\frac{e^{-b^2x^2}x^2\operatorname{erfi}(bx)}{b^4}-\frac{e^{-b^2x^2}x^4\operatorname{erfi}(bx)}{2b^2}+\frac{2\int 1\,dx}{b^5\sqrt{\pi}}\\
&= \frac{2x}{b^5\sqrt{\pi}}+\frac{2x^3}{3b^3\sqrt{\pi}}+\frac{x^5}{5b\sqrt{\pi}}-\frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{b^6}-\frac{e^{-b^2x^2}x^2\operatorname{erfi}(bx)}{b^4}-\frac{e^{-b^2x^2}x^4\operatorname{erfi}(bx)}{2b^2}
\end{aligned}
$$

Mathematica [A]
time = 0.03, size = 68, normalized size = 0.64

$$\frac{\frac{60bx+20b^3x^3+6b^5x^5}{\sqrt{\pi}}-15e^{-b^2x^2}\left(2+2b^2x^2+b^4x^4\right)\operatorname{Erfi}(bx)}{30b^6}$$

Antiderivative was successfully verified.

```
[In] Integrate[(x^5*Erfi[b*x])/E^(b^2*x^2),x]
```

```
[Out] ((60*b*x + 20*b^3*x^3 + 6*b^5*x^5)/Sqrt[Pi] - (15*(2 + 2*b^2*x^2 + b^4*x^4)
*Erfi[b*x])/E^(b^2*x^2))/(30*b^6)
```

Maple [A]
time = 0.40, size = 103, normalized size = 0.96

method	result	size
default	$\frac{\left(6x^5 e^{b^2x^2}b^5-15\operatorname{erfi}(bx)x^4b^4\sqrt{\pi}+20b^3x^3e^{b^2x^2}-30\operatorname{erfi}(bx)\sqrt{\pi}\,b^2x^2+60\,e^{b^2x^2}bx-30\operatorname{erfi}(bx)\sqrt{\pi}\right)e^{-b^2x^2}}{30b^6\sqrt{\pi}}$	103

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*erfi(b*x)/exp(b^2*x^2),x,method=_RETURNVERBOSE)
```

```
[Out] 1/30*(6*x^5*exp(b^2*x^2)*b^5-15*erfi(b*x)*x^4*b^4*Pi^(1/2)+20*b^3*x^3*exp(b
^2*x^2)-30*erfi(b*x)*Pi^(1/2)*b^2*x^2+60*exp(b^2*x^2)*b*x-30*erfi(b*x)*Pi^(
1/2))/b^6/Pi^(1/2)/exp(b^2*x^2)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfi(b*x)/exp(b^2*x^2),x, algorithm="maxima")
```

```
[Out] integrate(x^5*erfi(b*x)*e^(-b^2*x^2), x)
```

Fricas [A]
time = 0.39, size = 79, normalized size = 0.74

$$\frac{\left(2\sqrt{\pi}\,(3\,b^5x^5+10\,b^3x^3+30\,bx)e^{(b^2x^2)}-15\,(2\,\pi+\pi b^4x^4+2\,\pi b^2x^2)\operatorname{erfi}(bx)\right)e^{(-b^2x^2)}}{30\,\pi b^6}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfi(b*x)/exp(b^2*x^2),x, algorithm="fricas")
```

```
[Out] 1/30*(2*sqrt(pi)*(3*b^5*x^5 + 10*b^3*x^3 + 30*b*x)*e^(b^2*x^2) - 15*(2*pi +
 pi*b^4*x^4 + 2*pi*b^2*x^2)*erfi(b*x))*e^(-b^2*x^2)/(pi*b^6)
```

Sympy [A]
time = 138.69, size = 99, normalized size = 0.93

$$\begin{cases} \frac{x^5}{5\sqrt{\pi}\,b}-\frac{x^4e^{-b^2x^2}\operatorname{erfi}(bx)}{2b^2}+\frac{2x^3}{3\sqrt{\pi}\,b^3}-\frac{x^2e^{-b^2x^2}\operatorname{erfi}(bx)}{b^4}+\frac{2x}{\sqrt{\pi}\,b^5}-\frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{b^6} & \text{for } b\neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**5*erfi(b*x)/exp(b**2*x**2),x)
```

```
[Out] Piecewise((x**5/(5*sqrt(pi)*b) - x**4*exp(-b**2*x**2)*erfi(b*x)/(2*b**2) +
2*x**3/(3*sqrt(pi)*b**3) - x**2*exp(-b**2*x**2)*erfi(b*x)/b**4 + 2*x/(sqrt(
pi)*b**5) - exp(-b**2*x**2)*erfi(b*x)/b**6, Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^5*erfi(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(x^5*erfi(b*x)*e^(-b^2*x^2), x)
```

Mupad [B]
time = 0.25, size = 82, normalized size = 0.77

$$\frac{3\,b^4\,x^5+10\,b^2\,x^3+30\,x}{15\,b^5\,\sqrt{\pi}}-\operatorname{erfi}(b\,x)\,\left(\frac{\mathrm{e}^{-b^2\,x^2}}{b^6}+\frac{x^4\,\mathrm{e}^{-b^2\,x^2}}{2\,b^2}+\frac{x^2\,\mathrm{e}^{-b^2\,x^2}}{b^4}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*exp(-b^2*x^2)*erfi(b*x),x)
```

```
[Out] (30*x + 10*b^2*x^3 + 3*b^4*x^5)/(15*b^5*pi^(1/2)) - erfi(b*x)*(exp(-b^2*x^2
)/b^6 + (x^4*exp(-b^2*x^2))/(2*b^2) + (x^2*exp(-b^2*x^2))/b^4)
```

3.271 $\int e^{-b^2x^2}x^3\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=71

$$\frac{x}{b^3\sqrt{\pi}}+\frac{x^3}{3b\sqrt{\pi}}-\frac{e^{-b^2x^2}\mathrm{Erfi}(bx)}{2b^4}-\frac{e^{-b^2x^2}x^2\mathrm{Erfi}(bx)}{2b^2}$$

```
[Out] -1/2*erfi(b*x)/b^4/exp(b^2*x^2)-1/2*x^2*erfi(b*x)/b^2/exp(b^2*x^2)+x/b^3/Pi
^(1/2)+1/3*x^3/b/Pi^(1/2)
```

Rubi [A]
time = 0.05, antiderivative size = 71, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {6522, 6519, 8, 30}

$$\frac{x}{\sqrt{\pi}\,b^3}-\frac{x^2e^{-b^2x^2}\mathrm{Erfi}(bx)}{2b^2}-\frac{e^{-b^2x^2}\mathrm{Erfi}(bx)}{2b^4}+\frac{x^3}{3\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[(x^3*Erfi[b*x])/E^(b^2*x^2),x]
```

```
[Out] x/(b^3*Sqrt[Pi]) + x^3/(3*b*Sqrt[Pi]) - Erfi[b*x]/(2*b^4*E^(b^2*x^2)) - (x^
2*Erfi[b*x])/(2*b^2*E^(b^2*x^2))
```

Rule 8

```
Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}\int e^{-b^2x^2}x^3\text{erfi}(bx)\,dx&=-\frac{e^{-b^2x^2}x^2\text{erfi}(bx)}{2b^2}+\frac{\int e^{-b^2x^2}x\text{erfi}(bx)\,dx}{b^2}+\frac{\int x^2\,dx}{b\sqrt{\pi}}\\&=\frac{x^3}{3b\sqrt{\pi}}-\frac{e^{-b^2x^2}\text{erfi}(bx)}{2b^4}-\frac{e^{-b^2x^2}x^2\text{erfi}(bx)}{2b^2}+\frac{\int 1\,dx}{b^3\sqrt{\pi}}\\&=\frac{x}{b^3\sqrt{\pi}}+\frac{x^3}{3b\sqrt{\pi}}-\frac{e^{-b^2x^2}\text{erfi}(bx)}{2b^4}-\frac{e^{-b^2x^2}x^2\text{erfi}(bx)}{2b^2}\end{aligned}$$

Mathematica [A]
time = 0.02, size = 51, normalized size = 0.72

$$\frac{\frac{2bx(3+b^2x^2)}{\sqrt{\pi}}-3e^{-b^2x^2}(1+b^2x^2)\,\text{Erfi}(bx)}{6b^4}$$

Antiderivative was successfully verified.

```
[In] Integrate[(x^3*Erfi[b*x])/E^(b^2*x^2),x]
[Out] ((2*b*x*(3 + b^2*x^2))/Sqrt[Pi] - (3*(1 + b^2*x^2)*Erfi[b*x])/E^(b^2*x^2))/
(6*b^4)
```

Maple [A]
time = 0.18, size = 72, normalized size = 1.01

method	result	size
default	$\frac{\left(2b^3x^3e^{b^2x^2}-3\,\text{erfi}(bx)\sqrt{\pi}\,b^2x^2+6\,e^{b^2x^2}bx-3\,\text{erfi}(bx)\sqrt{\pi}\right)e^{-b^2x^2}}{6b^4\sqrt{\pi}}$	72

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erfi(b*x)/exp(b^2*x^2),x,method=_RETURNVERBOSE)
[Out] 1/6*(2*b^3*x^3*exp(b^2*x^2)-3*erfi(b*x)*Pi^(1/2)*b^2*x^2+6*exp(b^2*x^2)*b*x
-3*erfi(b*x)*Pi^(1/2))/b^4/Pi^(1/2)/exp(b^2*x^2)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfi(b*x)/exp(b^2*x^2),x, algorithm="maxima")
```

[Out] integrate(x^3*erfi(b*x)*e^(-b^2*x^2), x)

Fricas [A]
time = 0.39, size = 59, normalized size = 0.83

$$\frac{\left(2\sqrt{\pi}\,(b^3x^3+3\,bx)e^{\left(b^2x^2\right)}-3\,(\pi+\pi b^2x^2)\,\mathrm{erfi}\,(bx)\right)e^{\left(-b^2x^2\right)}}{6\,\pi b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfi(b*x)/exp(b^2*x^2),x, algorithm="fricas")
```

```
[Out] 1/6*(2*sqrt(pi)*(b^3*x^3 + 3*b*x)*e^(b^2*x^2) - 3*(pi + pi*b^2*x^2)*erfi(b*
x))*e^(-b^2*x^2)/(pi*b^4)
```

Sympy [A]
time = 21.18, size = 63, normalized size = 0.89

$$\begin{cases}\frac{x^3}{3\sqrt{\pi}\,b}-\frac{x^2e^{-b^2x^2}\,\mathrm{erfi}\,(bx)}{2b^2}+\frac{x}{\sqrt{\pi}\,b^3}-\frac{e^{-b^2x^2}\,\mathrm{erfi}\,(bx)}{2b^4} & \text{for } b\neq 0\\ 0 & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**3*erfi(b*x)/exp(b**2*x**2),x)
```

```
[Out] Piecewise((x**3/(3*sqrt(pi)*b) - x**2*exp(-b**2*x**2)*erfi(b*x)/(2*b**2) +
x/(sqrt(pi)*b**3) - exp(-b**2*x**2)*erfi(b*x)/(2*b**4), Ne(b, 0)), (0, True
))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^3*erfi(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(x^3*erfi(b*x)*e^(-b^2*x^2), x)
```

Mupad [B]
time = 0.18, size = 56, normalized size = 0.79

$$\frac{\frac{b^2\,x^3}{3}+x}{b^3\,\sqrt{\pi}}-\mathrm{erfi}(b\,x)\,\left(\frac{\mathrm{e}^{-b^2\,x^2}}{2\,b^4}+\frac{x^2\,\mathrm{e}^{-b^2\,x^2}}{2\,b^2}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*exp(-b^2*x^2)*erfi(b*x),x)
```

```
[Out] (x + (b^2*x^3)/3)/(b^3*pi^(1/2)) - erfi(b*x)*(exp(-b^2*x^2)/(2*b^4) + (x^2*
exp(-b^2*x^2))/(2*b^2))
```

3.272 $\int e^{-b^2 x^2} x \mathbf{Erfi}(bx) \, dx$

Optimal. Leaf size=32

$$\frac{x}{b\sqrt{\pi}} - \frac{e^{-b^2x^2}\text{Erfi}(bx)}{2b^2}$$

```
[Out] -1/2*erfi(b*x)/b^2/exp(b^2*x^2)+x/b/Pi^(1/2)
```

Rubi [A]
time = 0.02, antiderivative size = 32, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {6519, 8}

$$\frac{x}{\sqrt{\pi}\, b} - \frac{e^{-b^2x^2}\text{Erfi}(bx)}{2b^2}$$

Antiderivative was successfully verified.

```
[In] Int[(x*Erfi[b*x])/E^(b^2*x^2),x]
```

```
[Out] x/(b*Sqrt[Pi]) - Erfi[b*x]/(2*b^2*E^(b^2*x^2))
```

Rule 8

```
Int[a_, x_Symbol] :> Simp[a*x, x] /; FreeQ[a, x]
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\begin{aligned}\int e^{-b^2x^2} x\text{erfi}(bx)\,dx &= -\frac{e^{-b^2x^2}\text{erfi}(bx)}{2b^2} + \frac{\int 1\,dx}{b\sqrt{\pi}}\\ &= \frac{x}{b\sqrt{\pi}} - \frac{e^{-b^2x^2}\text{erfi}(bx)}{2b^2}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 32, normalized size = 1.00

$$\frac{x}{b\sqrt{\pi}} - \frac{e^{-b^2x^2}\text{Erfi}(bx)}{2b^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[(x*Erfi[b*x])/E^(b^2*x^2),x]
[Out] x/(b*Sqrt[Pi]) - Erfi[b*x]/(2*b^2*E^(b^2*x^2))
```

Maple [A]
time = 0.13, size = 41, normalized size = 1.28

method	result	size
default	$\frac{\left(2\,\mathrm{e}^{b^2x^2}bx-\mathrm{erfi}(bx)\sqrt{\pi}\right)\mathrm{e}^{-b^2x^2}}{2\sqrt{\pi}\,b^2}$	41

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfi(b*x)/exp(b^2*x^2),x,method=_RETURNVERBOSE)
[Out] 1/2*(2*exp(b^2*x^2)*b*x-erfi(b*x)*Pi^(1/2))/Pi^(1/2)/b^2/exp(b^2*x^2)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(b*x)/exp(b^2*x^2),x, algorithm="maxima")
[Out] integrate(x*erfi(b*x)*e^(-b^2*x^2), x)
```

Fricas [A]
time = 0.37, size = 40, normalized size = 1.25

$$\frac{\left(2\sqrt{\pi}\,bxe^{\left(b^2x^2\right)}-\pi\,\mathrm{erfi}\left(bx\right)\right)e^{\left(-b^2x^2\right)}}{2\,\pi b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(b*x)/exp(b^2*x^2),x, algorithm="fricas")
[Out] 1/2*(2*sqrt(pi)*b*x*e^(b^2*x^2) - pi*erfi(b*x))*e^(-b^2*x^2)/(pi*b^2)
```

Sympy [A]
time = 3.15, size = 27, normalized size = 0.84

$$\begin{cases}\frac{x}{\sqrt{\pi}\,b}-\frac{e^{-b^2x^2}\,\mathrm{erfi}\left(bx\right)}{2b^2} & \text{for}\ b\neq 0\\ 0 & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(b*x)/exp(b**2*x**2),x)
```

```
[Out] Piecewise((x/(sqrt(pi)*b) - exp(-b**2*x**2)*erfi(b*x)/(2*b**2), Ne(b, 0)),
(0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*erfi(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(x*erfi(b*x)*e^(-b^2*x^2), x)
```

Mupad [B]
time = 0.05, size = 27, normalized size = 0.84

$$\frac{x}{b\sqrt{\pi}}-\frac{\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfi}(b\,x)}{2\,b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*exp(-b^2*x^2)*erfi(b*x),x)
```

```
[Out] x/(b*pi^(1/2)) - (exp(-b^2*x^2)*erfi(b*x))/(2*b^2)
```

3.273 $\int \frac{e^{-b^2x^2}\mathbf{Erfi}(bx)}{x}\,dx$

Optimal. Leaf size=30

$$\frac{2bx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}$$

```
[Out] 2*b*x*hypergeom([1/2, 1],[3/2, 3/2],-b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.02, antiderivative size = 30, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.056$, Rules used = $\{6525\}$

$$\frac{2bx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]/(E^(b^2*x^2)*x),x]
[Out] (2*b*x*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, -(b^2*x^2)])/Sqrt[Pi]
```

Rule 6525

```
Int[(E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)])/(x_), x_Symbol] :> Simp[2*b
*E^c*(x/Sqrt[Pi])*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, (-b^2)*x^2], x] /
; FreeQ[{b, c, d}, x] && EqQ[d, -b^2]
```

Rubi steps

$$\int \frac{e^{-b^2x^2}\text{erfi}(bx)}{x}\,dx = \frac{2bx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}$$

Mathematica [A]
time = 0.02, size = 30, normalized size = 1.00

$$\frac{2bx\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]/(E^(b^2*x^2)*x),x]
[Out] (2*b*x*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, -(b^2*x^2)])/Sqrt[Pi]
```

Maple [F]
time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}(bx)\,\mathrm{e}^{-b^2x^2}}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/exp(b^2*x^2)/x,x)
[Out] int(erfi(b*x)/exp(b^2*x^2)/x,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x,x, algorithm="maxima")
[Out] integrate(erfi(b*x)*e^(-b^2*x^2)/x, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x,x, algorithm="fricas")
[Out] integral(erfi(b*x)*e^(-b^2*x^2)/x, x)
```

Sympy [A]
time = 3.44, size = 24, normalized size = 0.80

$$\frac{2bx\,{}_2F_2\left(\begin{matrix}\frac{1}{2},1\\\frac{3}{2},\frac{3}{2}\end{matrix}\middle|\,-b^2x^2\right)}{\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b**2*x**2)/x,x)
[Out] 2*b*x*hyper((1/2, 1), (3/2, 3/2), -b**2*x**2)/sqrt(pi)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)*e^(-b^2*x^2)/x, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.03

$$\int \frac{\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfi}(b\,x)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erfi(b*x))/x,x)
```

```
[Out] int((exp(-b^2*x^2)*erfi(b*x))/x, x)
```

3.274 $\int \frac{e^{-b^2x^2}\textbf{Erfi}(bx)}{x^3}\,dx$

Optimal. Leaf size=65

$$-\frac{b}{\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\text{Erfi}(bx)}{2x^2}-\frac{2b^3x\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}$$

```
[Out] -1/2*erfi(b*x)/exp(b^2*x^2)/x^2-b/x/Pi^(1/2)-2*b^3*x*hypergeom([1/2, 1],[3/
2, 3/2],-b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.05, antiderivative size = 65, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.167$, Rules used = {6528, 6525, 30}

$$-\frac{2b^3x\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}-\frac{e^{-b^2x^2}\text{Erfi}(bx)}{2x^2}-\frac{b}{\sqrt{\pi}\,x}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]/(E^(b^2*x^2)*x^3),x]
```

```
[Out] -(b/(Sqrt[Pi]*x)) - Erfi[b*x]/(2*E^(b^2*x^2)*x^2) - (2*b^3*x*Hypergeometric
PFQ[{1/2, 1}, {3/2, 3/2}, -(b^2*x^2)])/Sqrt[Pi]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6525

```
Int[(E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)])/(x_), x_Symbol] :> Simp[2*b
*E^c*(x/Sqrt[Pi])*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, (-b^2)*x^2], x] /
; FreeQ[{b, c, d}, x] && EqQ[d, -b^2]
```

Rule 6528

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x
]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\int \frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{x^3}\,dx = -\frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{2x^2} - b^2\int \frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{x}\,dx + \frac{b\int \frac{1}{x^2}\,dx}{\sqrt{\pi}}$$
$$= -\frac{b}{\sqrt{\pi}\,x} - \frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{2x^2} - \frac{2b^3x\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}$$

Mathematica [A]
time = 0.01, size = 32, normalized size = 0.49

$$-\frac{2b\,{}_2F_2\left(-\frac{1}{2},1;\frac{1}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}\,x}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]/(E^(b^2*x^2)*x^3),x]
[Out] (-2*b*HypergeometricPFQ[{-1/2, 1}, {1/2, 3/2}, -(b^2*x^2)])/(Sqrt[Pi]*x)
```

Maple [F]
time = 0.18, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}(bx)\,\mathrm{e}^{-b^2x^2}}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/exp(b^2*x^2)/x^3,x)
[Out] int(erfi(b*x)/exp(b^2*x^2)/x^3,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^3,x, algorithm="maxima")
[Out] integrate(erfi(b*x)*e^(-b^2*x^2)/x^3, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^3,x, algorithm="fricas")
[Out] integral(erfi(b*x)*e^(-b^2*x^2)/x^3, x)
```

Sympy [**A**]
time = 7.91, size = 27, normalized size = 0.42

$$-\frac{2b{}_2F_2\left(\begin{matrix} -\frac{1}{2}, 1 \\ \frac{1}{2}, \frac{3}{2} \end{matrix}\middle| -b^2x^2\right)}{\sqrt{\pi}\,x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b**2*x**2)/x**3,x)
[Out] -2*b*hyper((-1/2, 1), (1/2, 3/2), -b**2*x**2)/(sqrt(pi)*x)
```

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^3,x, algorithm="giac")
[Out] integrate(erfi(b*x)*e^(-b^2*x^2)/x^3, x)
```

Mupad [**F**]
time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{e^{-b^2\,x^2}\,\mathrm{erfi}(b\,x)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erfi(b*x))/x^3,x)
[Out] int((exp(-b^2*x^2)*erfi(b*x))/x^3, x)
```

3.275 $\int \frac{e^{-b^2x^2}\mathbf{Erfi}(bx)}{x^5}\,dx$

Optimal. Leaf size=105

$$-\frac{b}{6\sqrt{\pi}\,x^3}+\frac{b^3}{2\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\mathrm{Erfi}(bx)}{4x^4}+\frac{b^2e^{-b^2x^2}\mathrm{Erfi}(bx)}{4x^2}+\frac{b^5x\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}$$

```
[Out] -1/4*erfi(b*x)/exp(b^2*x^2)/x^4+1/4*b^2*erfi(b*x)/exp(b^2*x^2)/x^2-1/6*b/x^
3/Pi^(1/2)+1/2*b^3/x/Pi^(1/2)+b^5*x*hypergeom([1/2, 1],[3/2, 3/2],-b^2*x^2)
/Pi^(1/2)
```

Rubi [A]
time = 0.08, antiderivative size = 105, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.167, Rules used = {6528, 6525, 30}

$$\frac{b^5x\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}+\frac{b^3}{2\sqrt{\pi}\,x}+\frac{b^2e^{-b^2x^2}\mathrm{Erfi}(bx)}{4x^2}-\frac{e^{-b^2x^2}\mathrm{Erfi}(bx)}{4x^4}-\frac{b}{6\sqrt{\pi}\,x^3}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]/(E^(b^2*x^2)*x^5),x]
```

```
[Out] -1/6*b/(Sqrt[Pi]*x^3) + b^3/(2*Sqrt[Pi]*x) - Erfi[b*x]/(4*E^(b^2*x^2)*x^4)
+ (b^2*Erfi[b*x])/(4*E^(b^2*x^2)*x^2) + (b^5*x*HypergeometricPFQ[{1/2, 1},
{3/2, 3/2}, -(b^2*x^2)])/Sqrt[Pi]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6525

```
Int[(E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)])/(x_), x_Symbol] :> Simp[2*b
*E^c*(x/Sqrt[Pi])*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, (-b^2)*x^2], x] /
; FreeQ[{b, c, d}, x] && EqQ[d, -b^2]
```

Rule 6528

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x
]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\int \frac{e^{-b^2x^2}\text{erfi}(bx)}{x^5}\,dx = -\frac{e^{-b^2x^2}\text{erfi}(bx)}{4x^4} - \frac{1}{2}b^2\int \frac{e^{-b^2x^2}\text{erfi}(bx)}{x^3}\,dx + \frac{b\int \frac{1}{x^4}\,dx}{2\sqrt{\pi}}$$
$$= -\frac{b}{6\sqrt{\pi}\,x^3} - \frac{e^{-b^2x^2}\text{erfi}(bx)}{4x^4} + \frac{b^2e^{-b^2x^2}\text{erfi}(bx)}{4x^2} + \frac{1}{2}b^4\int \frac{e^{-b^2x^2}\text{erfi}(bx)}{x}\,dx - \frac{b^3\int \frac{1}{x^2}\,dx}{2\sqrt{\pi}}$$
$$= -\frac{b}{6\sqrt{\pi}\,x^3} + \frac{b^3}{2\sqrt{\pi}\,x} - \frac{e^{-b^2x^2}\text{erfi}(bx)}{4x^4} + \frac{b^2e^{-b^2x^2}\text{erfi}(bx)}{4x^2} + \frac{b^5x\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}$$

Mathematica [A]
time = 0.01, size = 34, normalized size = 0.32

$$-\frac{2b\,{}_2F_2\left(-\frac{3}{2},1;-\frac{1}{2},\frac{3}{2};-b^2x^2\right)}{3\sqrt{\pi}\,x^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]/(E^(b^2*x^2)*x^5),x]
```

```
[Out] (-2*b*HypergeometricPFQ[{-3/2, 1}, {-1/2, 3/2}, -(b^2*x^2)])/(3*Sqrt[Pi]*x^
3)
```

Maple [F]
time = 0.60, size = 0, normalized size = 0.00

$$\int \frac{\text{erfi}\left(bx\right)\mathrm{e}^{-b^2x^2}}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/exp(b^2*x^2)/x^5,x)
```

```
[Out] int(erfi(b*x)/exp(b^2*x^2)/x^5,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^5,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)*e^(-b^2*x^2)/x^5, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^5,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x)*e^(-b^2*x^2)/x^5, x)
```

Sympy [A]
time = 45.49, size = 32, normalized size = 0.30

$$-\frac{2b\,{}_2F_2\left(\begin{matrix}-\frac{3}{2},1\\ -\frac{1}{2},\frac{3}{2}\end{matrix}\middle|-b^2x^2\right)}{3\sqrt{\pi}\,x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b**2*x**2)/x**5,x)
```

```
[Out] -2*b*hyper((-3/2, 1), (-1/2, 3/2), -b**2*x**2)/(3*sqrt(pi)*x**3)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^5,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)*e^(-b^2*x^2)/x^5, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfi}(b\,x)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erfi(b*x))/x^5,x)
```

```
[Out] int((exp(-b^2*x^2)*erfi(b*x))/x^5, x)
```

3.276 $\int e^{-b^2x^2}x^6\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=148

$$\frac{15x^2}{8b^5\sqrt{\pi}}+\frac{5x^4}{8b^3\sqrt{\pi}}+\frac{x^6}{6b\sqrt{\pi}}-\frac{15e^{-b^2x^2}x\mathrm{Erfi}(bx)}{8b^6}-\frac{5e^{-b^2x^2}x^3\mathrm{Erfi}(bx)}{4b^4}-\frac{e^{-b^2x^2}x^5\mathrm{Erfi}(bx)}{2b^2}+\frac{15x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-\right.}{8b^5\sqrt{\pi}}$$

```
[Out] -15/8*x*erfi(b*x)/b^6/exp(b^2*x^2)-5/4*x^3*erfi(b*x)/b^4/exp(b^2*x^2)-1/2*x
^5*erfi(b*x)/b^2/exp(b^2*x^2)+15/8*x^2/b^5/Pi^(1/2)+5/8*x^4/b^3/Pi^(1/2)+1/
6*x^6/b/Pi^(1/2)+15/8*x^2*hypergeom([1, 1],[3/2, 2],-b^2*x^2)/b^5/Pi^(1/2)
```

Rubi [A]
time = 0.09, antiderivative size = 148, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 3, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.167$, Rules used = {6522, 6513, 30}

$$\frac{15x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{8\sqrt{\pi}\,b^5}+\frac{15x^2}{8\sqrt{\pi}\,b^5}+\frac{5x^4}{8\sqrt{\pi}\,b^3}-\frac{x^5e^{-b^2x^2}\mathrm{Erfi}(bx)}{2b^2}-\frac{15xe^{-b^2x^2}\mathrm{Erfi}(bx)}{8b^6}-\frac{5x^3e^{-b^2x^2}\mathrm{Erfi}(bx)}{4b^4}+\frac{x^6}{6\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[(x^6*Erfi[b*x])/E^(b^2*x^2),x]
```

```
[Out] (15*x^2)/(8*b^5*Sqrt[Pi]) + (5*x^4)/(8*b^3*Sqrt[Pi]) + x^6/(6*b*Sqrt[Pi]) -
 (15*x*Erfi[b*x])/(8*b^6*E^(b^2*x^2)) - (5*x^3*Erfi[b*x])/(4*b^4*E^(b^2*x^2
)) - (x^5*Erfi[b*x])/(2*b^2*E^(b^2*x^2)) + (15*x^2*HypergeometricPFQ[{1, 1}
, {3/2, 2}, -(b^2*x^2)])/(8*b^5*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6513

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2
/Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, (-b^2)*x^2], x] /; FreeQ[{b,
 c, d}, x] && EqQ[d, -b^2]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\int e^{-b^2x^2}x^6\operatorname{erfi}(bx)\,dx = -\frac{e^{-b^2x^2}x^5\operatorname{erfi}(bx)}{2b^2} + \frac{5\int e^{-b^2x^2}x^4\operatorname{erfi}(bx)\,dx}{2b^2} + \frac{\int x^5\,dx}{b\sqrt{\pi}}$$
$$= \frac{x^6}{6b\sqrt{\pi}} - \frac{5e^{-b^2x^2}x^3\operatorname{erfi}(bx)}{4b^4} - \frac{e^{-b^2x^2}x^5\operatorname{erfi}(bx)}{2b^2} + \frac{15\int e^{-b^2x^2}x^2\operatorname{erfi}(bx)\,dx}{4b^4} + \frac{5\int x^3\,d}{2b^3\sqrt{\pi}}$$
$$= \frac{5x^4}{8b^3\sqrt{\pi}} + \frac{x^6}{6b\sqrt{\pi}} - \frac{15e^{-b^2x^2}x\operatorname{erfi}(bx)}{8b^6} - \frac{5e^{-b^2x^2}x^3\operatorname{erfi}(bx)}{4b^4} - \frac{e^{-b^2x^2}x^5\operatorname{erfi}(bx)}{2b^2} + \frac{15}{}$$
$$= \frac{15x^2}{8b^5\sqrt{\pi}} + \frac{5x^4}{8b^3\sqrt{\pi}} + \frac{x^6}{6b\sqrt{\pi}} - \frac{15e^{-b^2x^2}x\operatorname{erfi}(bx)}{8b^6} - \frac{5e^{-b^2x^2}x^3\operatorname{erfi}(bx)}{4b^4} - \frac{e^{-b^2x^2}x^5\operatorname{erfi}}{2b^2}$$

Mathematica [A]
time = 0.02, size = 52, normalized size = 0.35

$$\frac{x^2\left(9+3b^2x^2+4b^4x^4-9\,{}_2F_2\left(1,1;-\frac{3}{2},2;-b^2x^2\right)\right)}{24b^5\sqrt{\pi}}$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[(x^6*Erfi[b*x])/E^(b^2*x^2),x]
[Out] (x^2*(9 + 3*b^2*x^2 + 4*b^4*x^4 - 9*HypergeometricPFQ[{1, 1}, {-3/2, 2}, -(
b^2*x^2)]))/(24*b^5*Sqrt[Pi])
```

Maple [F]
time = 0.40, size = 0, normalized size = 0.00

$$\int x^6\operatorname{erfi}(bx)\,\mathrm{e}^{-b^2x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^6*erfi(b*x)/exp(b^2*x^2),x)
[Out] int(x^6*erfi(b*x)/exp(b^2*x^2),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^6*erfi(b*x)/exp(b^2*x^2),x, algorithm="maxima")
[Out] integrate(x^6*erfi(b*x)*e^(-b^2*x^2), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^6*erfi(b*x)/exp(b^2*x^2),x, algorithm="fricas")
[Out] integral(x^6*erfi(b*x)*e^(-b^2*x^2), x)
```

Sympy [F(-2)]
time = 0.00, size = 0, normalized size = 0.00

Exception raised: SystemError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**6*erfi(b*x)/exp(b**2*x**2),x)
[Out] Exception raised: SystemError >> excessive stack use: stack is 3004 deep
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^6*erfi(b*x)/exp(b^2*x^2),x, algorithm="giac")
[Out] integrate(x^6*erfi(b*x)*e^(-b^2*x^2), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^6\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfi}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^6*exp(-b^2*x^2)*erfi(b*x),x)
[Out] int(x^6*exp(-b^2*x^2)*erfi(b*x), x)
```

3.277 $\int e^{-b^2x^2}x^4\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=109

$$\frac{3x^2}{4b^3\sqrt{\pi}}+\frac{x^4}{4b\sqrt{\pi}}-\frac{3e^{-b^2x^2}x\text{Erfi}(bx)}{4b^4}-\frac{e^{-b^2x^2}x^3\text{Erfi}(bx)}{2b^2}+\frac{3x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{4b^3\sqrt{\pi}}$$

```
[Out] -3/4*x*erfi(b*x)/b^4/exp(b^2*x^2)-1/2*x^3*erfi(b*x)/b^2/exp(b^2*x^2)+3/4*x^
2/b^3/Pi^(1/2)+1/4*x^4/b/Pi^(1/2)+3/4*x^2*hypergeom([1, 1],[3/2, 2],-b^2*x^
2)/b^3/Pi^(1/2)
```

Rubi [A]
time = 0.06, antiderivative size = 109, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.167, Rules used = {6522, 6513, 30}

$$\frac{3x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{4\sqrt{\pi}\,b^3}+\frac{3x^2}{4\sqrt{\pi}\,b^3}-\frac{x^3e^{-b^2x^2}\text{Erfi}(bx)}{2b^2}-\frac{3xe^{-b^2x^2}\text{Erfi}(bx)}{4b^4}+\frac{x^4}{4\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[(x^4*Erfi[b*x])/E^(b^2*x^2),x]
```

```
[Out] (3*x^2)/(4*b^3*Sqrt[Pi]) + x^4/(4*b*Sqrt[Pi]) - (3*x*Erfi[b*x])/(4*b^4*E^(b
^2*x^2)) - (x^3*Erfi[b*x])/(2*b^2*E^(b^2*x^2)) + (3*x^2*HypergeometricPFQ[{
1, 1}, {3/2, 2}, -(b^2*x^2)])/(4*b^3*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6513

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2
/Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, (-b^2)*x^2], x] /; FreeQ[{b,
 c, d}, x] && EqQ[d, -b^2]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\int e^{-b^2x^2}x^4\text{erfi}(bx)\,dx = -\frac{e^{-b^2x^2}x^3\text{erfi}(bx)}{2b^2} + \frac{3\int e^{-b^2x^2}x^2\text{erfi}(bx)\,dx}{2b^2} + \frac{\int x^3\,dx}{b\sqrt{\pi}}$$
$$= \frac{x^4}{4b\sqrt{\pi}} - \frac{3e^{-b^2x^2}x\text{erfi}(bx)}{4b^4} - \frac{e^{-b^2x^2}x^3\text{erfi}(bx)}{2b^2} + \frac{3\int e^{-b^2x^2}\text{erfi}(bx)\,dx}{4b^4} + \frac{3\int x\,dx}{2b^3\sqrt{\pi}}$$
$$= \frac{3x^2}{4b^3\sqrt{\pi}} + \frac{x^4}{4b\sqrt{\pi}} - \frac{3e^{-b^2x^2}x\text{erfi}(bx)}{4b^4} - \frac{e^{-b^2x^2}x^3\text{erfi}(bx)}{2b^2} + \frac{3x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{4b^3\sqrt{\pi}}$$

Mathematica [A]
time = 0.02, size = 43, normalized size = 0.39

$$\frac{x^2\left(1+b^2x^2-\,{}_2F_2\left(1,1;-\frac{1}{2},2;-b^2x^2\right)\right)}{4b^3\sqrt{\pi}}$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[(x^4*Erfi[b*x])/E^(b^2*x^2),x]
[Out] (x^2*(1 + b^2*x^2 - HypergeometricPFQ[{1, 1}, {-1/2, 2}, -(b^2*x^2)]))/(4*b
^3*Sqrt[Pi])
```

Maple [F]
time = 0.25, size = 0, normalized size = 0.00

$$\int x^4\,\text{erfi}\left(bx\right)\text{e}^{-b^2x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erfi(b*x)/exp(b^2*x^2),x)
[Out] int(x^4*erfi(b*x)/exp(b^2*x^2),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfi(b*x)/exp(b^2*x^2),x, algorithm="maxima")
[Out] integrate(x^4*erfi(b*x)*e^(-b^2*x^2), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfi(b*x)/exp(b^2*x^2),x, algorithm="fricas")
```

```
[Out] integral(x^4*erfi(b*x)*e^(-b^2*x^2), x)
```

Sympy [F(-1)] Timed out
time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**4*erfi(b*x)/exp(b**2*x**2),x)
```

```
[Out] Timed out
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^4*erfi(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(x^4*erfi(b*x)*e^(-b^2*x^2), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^4\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfi}(b\,x)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*exp(-b^2*x^2)*erfi(b*x),x)
```

```
[Out] int(x^4*exp(-b^2*x^2)*erfi(b*x), x)
```

3.278 $\int e^{-b^2x^2}x^2\textbf{Erfi}(bx)\,dx$

Optimal. Leaf size=70

$$\frac{x^2}{2b\sqrt{\pi}}-\frac{e^{-b^2x^2}x\text{Erfi}(bx)}{2b^2}+\frac{x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2b\sqrt{\pi}}$$

```
[Out] -1/2*x*erfi(b*x)/b^2/exp(b^2*x^2)+1/2*x^2/b/Pi^(1/2)+1/2*x^2*hypergeom([1,
1],[3/2, 2],-b^2*x^2)/b/Pi^(1/2)
```

Rubi [A]
time = 0.04, antiderivative size = 70, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}}=0.167$, Rules used = {6522, 6513, 30}

$$\frac{x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}\,b}-\frac{xe^{-b^2x^2}\text{Erfi}(bx)}{2b^2}+\frac{x^2}{2\sqrt{\pi}\,b}$$

Antiderivative was successfully verified.

```
[In] Int[(x^2*Erfi[b*x])/E^(b^2*x^2),x]
```

```
[Out] x^2/(2*b*Sqrt[Pi]) - (x*Erfi[b*x])/(2*b^2*E^(b^2*x^2)) + (x^2*Hypergeometri
cPFQ[{1, 1}, {3/2, 2}, -(b^2*x^2)])/(2*b*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6513

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2
/Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, (-b^2)*x^2], x] /; FreeQ[{b,
 c, d}, x] && EqQ[d, -b^2]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\int e^{-b^2x^2}x^2\text{erfi}(bx)\,dx = -\frac{e^{-b^2x^2}x\text{erfi}(bx)}{2b^2} + \frac{\int e^{-b^2x^2}\text{erfi}(bx)\,dx}{2b^2} + \frac{\int x\,dx}{b\sqrt{\pi}}$$
$$= \frac{x^2}{2b\sqrt{\pi}} - \frac{e^{-b^2x^2}x\text{erfi}(bx)}{2b^2} + \frac{x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2b\sqrt{\pi}}$$

Mathematica [A]
time = 0.01, size = 36, normalized size = 0.51

$$\frac{x^2\left(1-\,{}_2F_2\left(1,1;\frac{1}{2},2;-b^2x^2\right)\right)}{2b\sqrt{\pi}}$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[(x^2*Erfi[b*x])/E^(b^2*x^2),x]
[Out] (x^2*(1 - HypergeometricPFQ[{1, 1}, {1/2, 2}, -(b^2*x^2)]))/(2*b*Sqrt[Pi])
```

Maple [F]
time = 0.10, size = 0, normalized size = 0.00

$$\int x^2\,\text{erfi}\,(bx)\,\mathrm{e}^{-b^2x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfi(b*x)/exp(b^2*x^2),x)
[Out] int(x^2*erfi(b*x)/exp(b^2*x^2),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfi(b*x)/exp(b^2*x^2),x, algorithm="maxima")
[Out] integrate(x^2*erfi(b*x)*e^(-b^2*x^2), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfi(b*x)/exp(b^2*x^2),x, algorithm="fricas")
[Out] integral(x^2*erfi(b*x)*e^(-b^2*x^2), x)
```

Sympy [**A**]
time = 30.59, size = 22, normalized size = 0.31

$$\frac{bx^4{}_2F_2\left(\begin{matrix} 1,2 \\ \frac{3}{2},3 \end{matrix}\middle| -b^2x^2\right)}{2\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*erfi(b*x)/exp(b**2*x**2),x)
[Out] b*x**4*hyper((1, 2), (3/2, 3), -b**2*x**2)/(2*sqrt(pi))
```

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*erfi(b*x)/exp(b^2*x^2),x, algorithm="giac")
[Out] integrate(x^2*erfi(b*x)*e^(-b^2*x^2), x)
```

Mupad [**F**]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^2\,\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfi}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*exp(-b^2*x^2)*erfi(b*x),x)
[Out] int(x^2*exp(-b^2*x^2)*erfi(b*x), x)
```

3.279 $\int e^{-b^2x^2}\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=27

$$\frac{bx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{\sqrt{\pi}}$$

```
[Out] b*x^2*hypergeom([1, 1],[3/2, 2],-b^2*x^2)/Pi^(1/2)
```

Rubi [A]
time = 0.01, antiderivative size = 27, normalized size of antiderivative = 1.00, number of steps used = 1, number of rules used = 1, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.067$, Rules used = {6513}

$$\frac{bx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]/E^(b^2*x^2),x]
```

```
[Out] (b*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, -(b^2*x^2)])/Sqrt[Pi]
```

Rule 6513

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2
/Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, (-b^2)*x^2], x] /; FreeQ[{b,
 c, d}, x] && EqQ[d, -b^2]
```

Rubi steps

$$\int e^{-b^2x^2}\operatorname{erfi}(bx)\,dx=\frac{bx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{\sqrt{\pi}}$$

Mathematica [A]
time = 0.01, size = 27, normalized size = 1.00

$$\frac{bx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]/E^(b^2*x^2),x]
```

```
[Out] (b*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, -(b^2*x^2)])/Sqrt[Pi]
```

Maple [F]
time = 0.06, size = 0, normalized size = 0.00

$$\int \operatorname{erfi}(bx)\, \mathrm{e}^{-b^2x^2}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/exp(b^2*x^2),x)
[Out] int(erfi(b*x)/exp(b^2*x^2),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2),x, algorithm="maxima")
[Out] integrate(erfi(b*x)*e^(-b^2*x^2), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2),x, algorithm="fricas")
[Out] integral(erfi(b*x)*e^(-b^2*x^2), x)
```

Sympy [A]
time = 4.59, size = 20, normalized size = 0.74

$$\frac{bx^2{}_2F_2\left(\begin{matrix}1,1\\ \frac{3}{2},2\end{matrix}\middle|\, -b^2x^2\right)}{\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b**2*x**2),x)
[Out] b*x**2*hyper((1, 1), (3/2, 2), -b**2*x**2)/sqrt(pi)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)*e^(-b^2*x^2), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.04

$$\int \mathrm{e}^{-b^2\,x^2}\,\mathrm{erfi}(b\,x)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(-b^2*x^2)*erfi(b*x),x)
```

```
[Out] int(exp(-b^2*x^2)*erfi(b*x), x)
```

3.280 $\int \frac{e^{-b^2x^2}\textbf{Erfi}(bx)}{x^2}\,dx$

Optimal. Leaf size=60

$$-\frac{e^{-b^2x^2}\text{Erfi}(bx)}{x}-\frac{2b^3x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{\sqrt{\pi}}+\frac{2b\log(x)}{\sqrt{\pi}}$$

```
[Out] -erfi(b*x)/exp(b^2*x^2)/x-2*b^3*x^2*hypergeom([1, 1],[3/2, 2],-b^2*x^2)/Pi^
(1/2)+2*b*ln(x)/Pi^(1/2)
```

Rubi [A]
time = 0.04, antiderivative size = 60, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.167, Rules used = {6528, 6513, 29}

$$-\frac{2b^3x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{\sqrt{\pi}}-\frac{e^{-b^2x^2}\text{Erfi}(bx)}{x}+\frac{2b\log(x)}{\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]/(E^(b^2*x^2)*x^2),x]
```

```
[Out] -(Erfi[b*x]/(E^(b^2*x^2)*x)) - (2*b^3*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2
}, -(b^2*x^2)])/Sqrt[Pi] + (2*b*Log[x])/Sqrt[Pi]
```

Rule 29

```
Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]
```

Rule 6513

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2
/Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, (-b^2)*x^2], x] /; FreeQ[{b,
 c, d}, x] && EqQ[d, -b^2]
```

Rule 6528

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x
]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\int \frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{x^2}\,dx = -\frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{x} - (2b^2)\int e^{-b^2x^2}\operatorname{erfi}(bx)\,dx + \frac{(2b)\int \frac{1}{x}\,dx}{\sqrt{\pi}}$$
$$= -\frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{x} - \frac{2b^3x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{\sqrt{\pi}} + \frac{2b\log(x)}{\sqrt{\pi}}$$

Mathematica [C] Result contains higher order function than in optimal. Order 9 vs. order 5 in optimal.
time = 0.01, size = 26, normalized size = 0.43

$$-\frac{1}{2}bG_{2,3}^{2,1}\left(b^2x^2|\begin{array}{c} 0,1 \\ 0,0,-\frac{1}{2} \end{array}\right)$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[Erfi[b*x]/(E^(b^2*x^2)*x^2),x]
[Out] -1/2*(b*MeijerG[{{0}, {1}}, {{0, 0}, {-1/2}}, b^2*x^2])
```

Maple [F]
time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}(bx)\,e^{-b^2x^2}}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/exp(b^2*x^2)/x^2,x)
[Out] int(erfi(b*x)/exp(b^2*x^2)/x^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^2,x, algorithm="maxima")
[Out] integrate(erfi(b*x)*e^(-b^2*x^2)/x^2, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^2,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x)*e^(-b^2*x^2)/x^2, x)
```

Sympy [**A**]
time = 3.63, size = 41, normalized size = 0.68

$$-\frac{2b^3x^2{}_2F_2\left(\begin{matrix}1,1\\2,\frac{5}{2}\end{matrix}\middle|-b^2x^2\right)}{3\sqrt{\pi}}+\frac{b\log\left(b^2x^2\right)}{\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b**2*x**2)/x**2,x)
```

```
[Out] -2*b**3*x**2*hyper((1, 1), (2, 5/2), -b**2*x**2)/(3*sqrt(pi)) + b*log(b**2*
x**2)/sqrt(pi)
```

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^2,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)*e^(-b^2*x^2)/x^2, x)
```

Mupad [**F**]
time = 0.00, size = -1, normalized size = -0.02

$$\int \frac{\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfi}(b\,x)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erfi(b*x))/x^2,x)
```

```
[Out] int((exp(-b^2*x^2)*erfi(b*x))/x^2, x)
```

3.281 $\int \frac{e^{-b^2x^2}\mathbf{Erfi}(bx)}{x^4}\,dx$

Optimal. Leaf size=105

$$-\frac{b}{3\sqrt{\pi}\,x^2}-\frac{e^{-b^2x^2}\mathrm{Erfi}(bx)}{3x^3}+\frac{2b^2e^{-b^2x^2}\mathrm{Erfi}(bx)}{3x}+\frac{4b^5x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{3\sqrt{\pi}}-\frac{4b^3\log(x)}{3\sqrt{\pi}}$$

```
[Out] -1/3*erfi(b*x)/exp(b^2*x^2)/x^3+2/3*b^2*erfi(b*x)/exp(b^2*x^2)/x-1/3*b/x^2/
Pi^(1/2)+4/3*b^5*x^2*hypergeom([1, 1],[3/2, 2],-b^2*x^2)/Pi^(1/2)-4/3*b^3*l
n(x)/Pi^(1/2)
```

Rubi [A]
time = 0.06, antiderivative size = 105, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {6528, 6513, 29, 30}

$$\frac{4b^5x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{3\sqrt{\pi}}-\frac{4b^3\log(x)}{3\sqrt{\pi}}+\frac{2b^2e^{-b^2x^2}\mathrm{Erfi}(bx)}{3x}-\frac{e^{-b^2x^2}\mathrm{Erfi}(bx)}{3x^3}-\frac{b}{3\sqrt{\pi}\,x^2}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]/(E^(b^2*x^2)*x^4),x]
```

```
[Out] -1/3*b/(Sqrt[Pi]*x^2) - Erfi[b*x]/(3*E^(b^2*x^2)*x^3) + (2*b^2*Erfi[b*x])/(
3*E^(b^2*x^2)*x) + (4*b^5*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, -(b^2*x^2
)])/(3*Sqrt[Pi]) - (4*b^3*Log[x])/(3*Sqrt[Pi])
```

Rule 29

```
Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6513

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2
/Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, (-b^2)*x^2], x] /; FreeQ[{b,
 c, d}, x] && EqQ[d, -b^2]
```

Rule 6528

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[2*(b/((m
```

```
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x
]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int \frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{x^4}\,dx &= -\frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{3x^3} - \frac{1}{3}\left(2b^2\right)\int \frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{x^2}\,dx + \frac{(2b)\int \frac{1}{x^3}\,dx}{3\sqrt{\pi}}\\
&= -\frac{b}{3\sqrt{\pi}\,x^2} - \frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{3x^3} + \frac{2b^2e^{-b^2x^2}\operatorname{erfi}(bx)}{3x} + \frac{1}{3}\left(4b^4\right)\int e^{-b^2x^2}\operatorname{erfi}(bx)\,dx - \frac{(4b^3)}{3\sqrt{}}\\
&= -\frac{b}{3\sqrt{\pi}\,x^2} - \frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{3x^3} + \frac{2b^2e^{-b^2x^2}\operatorname{erfi}(bx)}{3x} + \frac{4b^5x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{3\sqrt{\pi}} - \frac{4b^3\,\mathrm{l}}{3\sqrt{}}
\end{aligned}$$

Mathematica [C] Result contains higher order function than in optimal. Order 9 vs. order 5 in optimal.
time = 0.02, size = 29, normalized size = 0.28

$$-\frac{bG_{2,3}^{2,1}\left(b^2x^2\middle|\begin{array}{c}0,2\\0,1,-\frac{1}{2}\end{array}\right)}{2x^2}$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[Erfi[b*x]/(E^(b^2*x^2)*x^4),x]
[Out] -1/2*(b*MeijerG[{{0}, {2}}, {{0, 1}, {-1/2}}, b^2*x^2])/x^2
```

Maple [F]
time = 0.34, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}\left(bx\right)\mathrm{e}^{-b^2x^2}}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/exp(b^2*x^2)/x^4,x)
[Out] int(erfi(b*x)/exp(b^2*x^2)/x^4,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^4,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)*e^(-b^2*x^2)/x^4, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^4,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x)*e^(-b^2*x^2)/x^4, x)
```

Sympy [C] Result contains complex when optimal does not.
time = 22.79, size = 24, normalized size = 0.23

$$-\frac{b^3 G_{3,2}^{1,2}\left(\begin{matrix} 2, 1 & \frac{5}{2} \\ 2 & 0 \end{matrix} \middle| \frac{e^{-2i\pi}}{b^2x^2}\right)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b**2*x**2)/x**4,x)
```

```
[Out] -b**3*meijerg(((2, 1), (5/2,)), ((2,), (0,)), exp_polar(-2*I*pi)/(b**2*x**2
))/2
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^4,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)*e^(-b^2*x^2)/x^4, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfi}(b\,x)}{x^4} \,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erfi(b*x))/x^4,x)
```

```
[Out] int((exp(-b^2*x^2)*erfi(b*x))/x^4, x)
```

3.282 $\int \frac{e^{-b^2x^2}\mathbf{Erfi}(bx)}{x^6}\,dx$

Optimal. Leaf size=144

$$-\frac{b}{10\sqrt{\pi}\,x^4}+\frac{2b^3}{15\sqrt{\pi}\,x^2}-\frac{e^{-b^2x^2}\mathrm{Erfi}(bx)}{5x^5}+\frac{2b^2e^{-b^2x^2}\mathrm{Erfi}(bx)}{15x^3}-\frac{4b^4e^{-b^2x^2}\mathrm{Erfi}(bx)}{15x}-\frac{8b^7x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{15\sqrt{\pi}}$$

```
[Out] -1/5*erfi(b*x)/exp(b^2*x^2)/x^5+2/15*b^2*erfi(b*x)/exp(b^2*x^2)/x^3-4/15*b^
4*erfi(b*x)/exp(b^2*x^2)/x-1/10*b/x^4/Pi^(1/2)+2/15*b^3/x^2/Pi^(1/2)-8/15*b
^7*x^2*hypergeom([1, 1],[3/2, 2],-b^2*x^2)/Pi^(1/2)+8/15*b^5*ln(x)/Pi^(1/2)
```

Rubi [A]

time = 0.09, antiderivative size = 144, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {6528, 6513, 29, 30}

$$-\frac{8b^7x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{15\sqrt{\pi}}+\frac{8b^5\log(x)}{15\sqrt{\pi}}+\frac{2b^3}{15\sqrt{\pi}\,x^2}-\frac{e^{-b^2x^2}\mathrm{Erfi}(bx)}{5x^5}+\frac{2b^2e^{-b^2x^2}\mathrm{Erfi}(bx)}{15x^3}-\frac{4b^4e^{-b^2x^2}\mathrm{Erfi}(bx)}{15x}-\frac{b}{10\sqrt{\pi}\,x^4}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]/(E^(b^2*x^2)*x^6),x]
```

```
[Out] -1/10*b/(Sqrt[Pi]*x^4) + (2*b^3)/(15*Sqrt[Pi]*x^2) - Erfi[b*x]/(5*E^(b^2*x^
2)*x^5) + (2*b^2*Erfi[b*x])/(15*E^(b^2*x^2)*x^3) - (4*b^4*Erfi[b*x])/(15*E^
(b^2*x^2)*x) - (8*b^7*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, -(b^2*x^2)])/
(15*Sqrt[Pi]) + (8*b^5*Log[x])/(15*Sqrt[Pi])
```

Rule 29

```
Int[(x_)^(-1), x_Symbol] :> Simp[Log[x], x]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6513

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2
/Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, (-b^2)*x^2], x] /; FreeQ[{b,
 c, d}, x] && EqQ[d, -b^2]
```

Rule 6528

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
```

```
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x
]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{x^6}\,dx &= -\frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{5x^5} - \frac{1}{5}\left(2b^2\right)\int \frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{x^4}\,dx + \frac{(2b)\int \frac{1}{x^5}\,dx}{5\sqrt{\pi}}\\
&= -\frac{b}{10\sqrt{\pi}\,x^4} - \frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{5x^5} + \frac{2b^2e^{-b^2x^2}\operatorname{erfi}(bx)}{15x^3} + \frac{1}{15}\left(4b^4\right)\int \frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{x^2}\,dx - \frac{(4b^3}{1}\\
&= -\frac{b}{10\sqrt{\pi}\,x^4} + \frac{2b^3}{15\sqrt{\pi}\,x^2} - \frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{5x^5} + \frac{2b^2e^{-b^2x^2}\operatorname{erfi}(bx)}{15x^3} - \frac{4b^4e^{-b^2x^2}\operatorname{erfi}(bx)}{15x} - \frac{1}{15}\\
&= -\frac{b}{10\sqrt{\pi}\,x^4} + \frac{2b^3}{15\sqrt{\pi}\,x^2} - \frac{e^{-b^2x^2}\operatorname{erfi}(bx)}{5x^5} + \frac{2b^2e^{-b^2x^2}\operatorname{erfi}(bx)}{15x^3} - \frac{4b^4e^{-b^2x^2}\operatorname{erfi}(bx)}{15x} - \frac{8b}{}\end{aligned}$$

Mathematica [C] Result contains higher order function than in optimal. Order 9 vs. order 5 in optimal.
time = 0.02, size = 29, normalized size = 0.20

$$-\frac{bG_{2,3}^{2,1}\left(b^2x^2\middle|\begin{array}{c}0,3\\0,2,-\frac{1}{2}\end{array}\right)}{2x^4}$$

Warning: Unable to verify antiderivative.

```
[In] Integrate[Erfi[b*x]/(E^(b^2*x^2)*x^6),x]
[Out] -1/2*(b*MeijerG[{{0}, {3}}, {{0, 2}, {-1/2}}, b^2*x^2])/x^4
```

Maple [F]
time = 0.62, size = 0, normalized size = 0.00

$$\int \frac{\operatorname{erfi}(bx)\,\mathrm{e}^{-b^2x^2}}{x^6}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/exp(b^2*x^2)/x^6,x)
[Out] int(erfi(b*x)/exp(b^2*x^2)/x^6,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^6,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)*e^(-b^2*x^2)/x^6, x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^6,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x)*e^(-b^2*x^2)/x^6, x)
```

Sympy [C] Result contains complex when optimal does not.
time = 175.46, size = 24, normalized size = 0.17

$$-\frac{b^5 G_{3,2}^{1,2}\left(\begin{matrix} 3,1 & \frac{7}{2} \\ 3 & 0 \end{matrix} \middle| \frac{e^{-2i\pi}}{b^2x^2}\right)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b**2*x**2)/x**6,x)
```

```
[Out] -b**5*meijerg(((3, 1), (7/2,)), ((3,), (0,)), exp_polar(-2*I*pi)/(b**2*x**2
))/2
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^6,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)*e^(-b^2*x^2)/x^6, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfi}\left(b\,x\right)}{x^6}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erfi(b*x))/x^6,x)
```

```
[Out] int((exp(-b^2*x^2)*erfi(b*x))/x^6, x)
```

3.283 $\int e^{c+b^2x^2}x^5\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=144

$$\frac{11e^{c+2b^2x^2}x}{16b^5\sqrt{\pi}}-\frac{e^{c+2b^2x^2}x^3}{4b^3\sqrt{\pi}}+\frac{e^{c+b^2x^2}\text{Erfi}(bx)}{b^6}-\frac{e^{c+b^2x^2}x^2\text{Erfi}(bx)}{b^4}+\frac{e^{c+b^2x^2}x^4\text{Erfi}(bx)}{2b^2}-\frac{43e^c\text{Erfi}\left(\sqrt{2}\,bx\right)}{32\sqrt{2}\,b^6}$$

```
[Out] exp(b^2*x^2+c)*erfi(b*x)/b^6-exp(b^2*x^2+c)*x^2*erfi(b*x)/b^4+1/2*exp(b^2*x
^2+c)*x^4*erfi(b*x)/b^2-43/64*exp(c)*erfi(b*x*2^(1/2))/b^6*2^(1/2)+11/16*ex
p(2*b^2*x^2+c)*x/b^5/Pi^(1/2)-1/4*exp(2*b^2*x^2+c)*x^3/b^3/Pi^(1/2)
```

Rubi [A]
time = 0.16, antiderivative size = 144, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {6522, 6519, 2235, 2243}

$$-\frac{43e^c\text{Erfi}\left(\sqrt{2}\,bx\right)}{32\sqrt{2}\,b^6}+\frac{x^4e^{b^2x^2+c}\text{Erfi}(bx)}{2b^2}+\frac{e^{b^2x^2+c}\text{Erfi}(bx)}{b^6}+\frac{11xe^{2b^2x^2+c}}{16\sqrt{\pi}\,b^5}-\frac{x^2e^{b^2x^2+c}\text{Erfi}(bx)}{b^4}-\frac{x^3e^{2b^2x^2+c}}{4\sqrt{\pi}\,b^3}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*x^5*Erfi[b*x],x]
```

```
[Out] (11*E^(c + 2*b^2*x^2)*x)/(16*b^5*Sqrt[Pi]) - (E^(c + 2*b^2*x^2)*x^3)/(4*b^3
*Sqrt[Pi]) + (E^(c + b^2*x^2)*Erfi[b*x])/b^6 - (E^(c + b^2*x^2)*x^2*Erfi[b*
x])/b^4 + (E^(c + b^2*x^2)*x^4*Erfi[b*x])/(2*b^2) - (43*E^c*Erfi[Sqrt[2]*b*
x])/(32*Sqrt[2]*b^6)
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
```

```
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int e^{c+b^2x^2}x^5\text{erfi}(bx)\,dx &= \frac{e^{c+b^2x^2}x^4\text{erfi}(bx)}{2b^2} - \frac{2\int e^{c+b^2x^2}x^3\text{erfi}(bx)\,dx}{b^2} - \frac{\int e^{c+2b^2x^2}x^4\,dx}{b\sqrt{\pi}} \\
&= -\frac{e^{c+2b^2x^2}x^3}{4b^3\sqrt{\pi}} - \frac{e^{c+b^2x^2}x^2\text{erfi}(bx)}{b^4} + \frac{e^{c+b^2x^2}x^4\text{erfi}(bx)}{2b^2} + \frac{2\int e^{c+b^2x^2}x\text{erfi}(bx)\,dx}{b^4} + \frac{3}{} \\
&= \frac{11e^{c+2b^2x^2}x}{16b^5\sqrt{\pi}} - \frac{e^{c+2b^2x^2}x^3}{4b^3\sqrt{\pi}} + \frac{e^{c+b^2x^2}\text{erfi}(bx)}{b^6} - \frac{e^{c+b^2x^2}x^2\text{erfi}(bx)}{b^4} + \frac{e^{c+b^2x^2}x^4\text{erfi}(bx)}{2b^2} \\
&= \frac{11e^{c+2b^2x^2}x}{16b^5\sqrt{\pi}} - \frac{e^{c+2b^2x^2}x^3}{4b^3\sqrt{\pi}} + \frac{e^{c+b^2x^2}\text{erfi}(bx)}{b^6} - \frac{e^{c+b^2x^2}x^2\text{erfi}(bx)}{b^4} + \frac{e^{c+b^2x^2}x^4\text{erfi}(bx)}{2b^2}
\end{aligned}$$

Mathematica [A]
time = 0.04, size = 95, normalized size = 0.66

$$\frac{e^c\left(-4be^{2b^2x^2}x(-11+4b^2x^2)+32e^{b^2x^2}\sqrt{\pi}\,(2-2b^2x^2+b^4x^4)\,\text{Erfi}(bx)-43\sqrt{2\pi}\,\text{Erfi}\left(\sqrt{2}\,bx\right)\right)}{64b^6\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*x^5*Erfi[b*x],x]
```

```
[Out] (E^c*(-4*b*E^(2*b^2*x^2)*x*(-11 + 4*b^2*x^2) + 32*E^(b^2*x^2)*Sqrt[Pi]*(2 -
 2*b^2*x^2 + b^4*x^4)*Erfi[b*x] - 43*Sqrt[2*Pi]*Erfi[Sqrt[2]*b*x]))/(64*b^6
*Sqrt[Pi])
```

Maple [F]
time = 0.10, size = 0, normalized size = 0.00

$$\int e^{b^2x^2+c}x^5\,\text{erfi}\,(bx)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(exp(b^2*x^2+c)*x^5*erfi(b*x),x)

[Out] int(exp(b^2*x^2+c)*x^5*erfi(b*x),x)

Maxima [**F**]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b^2*x^2+c)*x^5*erfi(b*x),x, algorithm="maxima")

[Out] integrate(x^5*erfi(b*x)*e^(b^2*x^2 + c), x)

Fricas [**A**]
time = 0.36, size = 102, normalized size = 0.71

$$-\frac{43\sqrt{2}\,\pi\sqrt{b^2}\,\operatorname{erfi}\left(\sqrt{2}\,\sqrt{b^2}\,x\right)e^c-32\,(\pi b^5x^4-2\,\pi b^3x^2+2\,\pi b)\operatorname{erfi}(bx)\,e^{(b^2x^2+c)}+4\,\sqrt{\pi}\,(4\,b^4x^3-11\,b^2x)e^{(2\,b^2x^2+c)}}{64\,\pi b^7}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b^2*x^2+c)*x^5*erfi(b*x),x, algorithm="fricas")

[Out] -1/64*(43*sqrt(2)*pi*sqrt(b^2)*erfi(sqrt(2)*sqrt(b^2)*x)*e^c - 32*(pi*b^5*x^4 - 2*pi*b^3*x^2 + 2*pi*b)*erfi(b*x)*e^(b^2*x^2 + c) + 4*sqrt(pi)*(4*b^4*x^3 - 11*b^2*x)*e^(2*b^2*x^2 + c))/(pi*b^7)

Sympy [**F**]
time = 0.00, size = 0, normalized size = 0.00

$$e^c\int x^5e^{b^2x^2}\operatorname{erfi}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b**2*x**2+c)*x**5*erfi(b*x),x)

[Out] exp(c)*Integral(x**5*exp(b**2*x**2)*erfi(b*x), x)

Giac [**F**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(exp(b^2*x^2+c)*x^5*erfi(b*x),x, algorithm="giac")

[Out] integrate(x^5*erfi(b*x)*e^(b^2*x^2 + c), x)

Mupad [B]
time = 0.56, size = 206, normalized size = 1.43

$$\mathrm{erfi}(b\,x)\,\left(\frac{\mathrm{e}^{b^2\,x^2+c}}{b^6}+\frac{x^4\,\mathrm{e}^{b^2\,x^2+c}}{2\,b^2}-\frac{x^2\,\mathrm{e}^{b^2\,x^2+c}}{b^4}\right)-\frac{3\,x^5\,\mathrm{e}^c}{8\,b\,{\left(-2\,b^2\,x^2\right)}^{5/2}}+\frac{11\,x\,\mathrm{e}^{2\,b^2\,x^2+c}}{16\,b^5\,\sqrt{\pi}}-\frac{x^3\,\mathrm{e}^{2\,b^2\,x^2+c}}{4\,b^3\,\sqrt{\pi}}-\frac{\sqrt{2}\,\mathrm{e}^c\,\mathrm{erfi}\left(\sqrt{2}\,x\,\sqrt{b^2}\right)}{8\,b^3\,{\left(b^2\right)}^{3/2}}+\frac{3\,x^5\,\mathrm{e}^c\,\mathrm{erfc}\left(\sqrt{-2\,b^2\,x^2}\right)}{8\,b\,{\left(-2\,b^2\,x^2\right)}^{5/2}}-\frac{\sqrt{2}\,\mathrm{erf}\left(\sqrt{2}\,x\,\sqrt{-b^2}\right)\,\mathrm{e}^c}{2\,b\,{\left(-b^2\right)}^{5/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^5*exp(c + b^2*x^2)*erfi(b*x),x)
```

```
[Out] erfi(b*x)*(exp(c + b^2*x^2)/b^6 + (x^4*exp(c + b^2*x^2))/(2*b^2) - (x^2*exp
(c + b^2*x^2))/b^4) - (3*x^5*exp(c))/(8*b*(-2*b^2*x^2)^(5/2)) + (11*x*exp(c
 + 2*b^2*x^2))/(16*b^5*pi^(1/2)) - (x^3*exp(c + 2*b^2*x^2))/(4*b^3*pi^(1/2)
) - (2^(1/2)*exp(c)*erfi(2^(1/2)*x*(b^2)^(1/2)))/(8*b^3*(b^2)^(3/2)) + (3*x
^5*exp(c)*erfc((-2*b^2*x^2)^(1/2)))/(8*b*(-2*b^2*x^2)^(5/2)) - (2^(1/2)*erf
(2^(1/2)*x*(-b^2)^(1/2))*exp(c))/(2*b*(-b^2)^(5/2))
```

3.284 $\int e^{c+b^2x^2}x^3\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=97

$$-\frac{e^{c+2b^2x^2}x}{4b^3\sqrt{\pi}}-\frac{e^{c+b^2x^2}\mathrm{Erfi}(bx)}{2b^4}+\frac{e^{c+b^2x^2}x^2\mathrm{Erfi}(bx)}{2b^2}+\frac{5e^c\mathrm{Erfi}\left(\sqrt{2}\,bx\right)}{8\sqrt{2}\,b^4}$$

```
[Out] -1/2*exp(b^2*x^2+c)*erfi(b*x)/b^4+1/2*exp(b^2*x^2+c)*x^2*erfi(b*x)/b^2+5/16
*exp(c)*erfi(b*x*2^(1/2))/b^4*2^(1/2)-1/4*exp(2*b^2*x^2+c)*x/b^3/Pi^(1/2)
```

Rubi [A]
time = 0.08, antiderivative size = 97, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}=0.210$, Rules used = {6522, 6519, 2235, 2243}

$$\frac{5e^c\mathrm{Erfi}\left(\sqrt{2}\,bx\right)}{8\sqrt{2}\,b^4}+\frac{x^2e^{b^2x^2+c}\mathrm{Erfi}(bx)}{2b^2}-\frac{e^{b^2x^2+c}\mathrm{Erfi}(bx)}{2b^4}-\frac{xe^{2b^2x^2+c}}{4\sqrt{\pi}\,b^3}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*x^3*Erfi[b*x],x]
```

```
[Out] -1/4*(E^(c + 2*b^2*x^2)*x)/(b^3*Sqrt[Pi]) - (E^(c + b^2*x^2)*Erfi[b*x])/(2*
b^4) + (E^(c + b^2*x^2)*x^2*Erfi[b*x])/(2*b^2) + (5*E^c*Erfi[Sqrt[2]*b*x])/
(8*Sqrt[2]*b^4)
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int e^{c+b^2x^2}x^3\operatorname{erfi}(bx)\,dx &= \frac{e^{c+b^2x^2}x^2\operatorname{erfi}(bx)}{2b^2} - \frac{\int e^{c+b^2x^2}x\operatorname{erfi}(bx)\,dx}{b^2} - \frac{\int e^{c+2b^2x^2}x^2\,dx}{b\sqrt{\pi}} \\
&= -\frac{e^{c+2b^2x^2}x}{4b^3\sqrt{\pi}} - \frac{e^{c+b^2x^2}\operatorname{erfi}(bx)}{2b^4} + \frac{e^{c+b^2x^2}x^2\operatorname{erfi}(bx)}{2b^2} + \frac{\int e^{c+2b^2x^2}\,dx}{4b^3\sqrt{\pi}} + \frac{\int e^{c+2b^2x^2}\,dx}{b^3\sqrt{\pi}} \\
&= -\frac{e^{c+2b^2x^2}x}{4b^3\sqrt{\pi}} - \frac{e^{c+b^2x^2}\operatorname{erfi}(bx)}{2b^4} + \frac{e^{c+b^2x^2}x^2\operatorname{erfi}(bx)}{2b^2} + \frac{5e^c\operatorname{erfi}\left(\sqrt{2}\,bx\right)}{8\sqrt{2}\,b^4}
\end{aligned}$$

Mathematica [A]
time = 0.03, size = 77, normalized size = 0.79

$$\frac{e^c\left(-4be^{2b^2x^2}x + 8e^{b^2x^2}\sqrt{\pi}\,(-1+b^2x^2)\operatorname{Erfi}(bx) + 5\sqrt{2\pi}\operatorname{Erfi}\left(\sqrt{2}\,bx\right)\right)}{16b^4\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*x^3*Erfi[b*x],x]
[Out] (E^c*(-4*b*E^(2*b^2*x^2)*x + 8*E^(b^2*x^2)*Sqrt[Pi]*(-1 + b^2*x^2)*Erfi[b*x
] + 5*Sqrt[2*Pi]*Erfi[Sqrt[2]*b*x]))/(16*b^4*Sqrt[Pi])
```

Maple [F]
time = 0.14, size = 0, normalized size = 0.00

$$\int e^{b^2x^2+c}x^3\operatorname{erfi}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*x^3*erfi(b*x),x)
[Out] int(exp(b^2*x^2+c)*x^3*erfi(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^3*erfi(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x^3*erfi(b*x)*e^(b^2*x^2 + c), x)
```

Fricas [A]
time = 0.35, size = 82, normalized size = 0.85

$$-\frac{4\sqrt{\pi}\,b^2xe^{(2\,b^2x^2+c)}-5\sqrt{2}\,\pi\sqrt{b^2}\,\mathrm{erfi}\left(\sqrt{2}\,\sqrt{b^2}\,x\right)e^c-8\left(\pi b^3x^2-\pi b\right)\mathrm{erfi}\left(bx\right)e^{(b^2x^2+c)}}{16\,\pi b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^3*erfi(b*x),x, algorithm="fricas")
```

```
[Out] -1/16*(4*sqrt(pi)*b^2*x*e^(2*b^2*x^2 + c) - 5*sqrt(2)*pi*sqrt(b^2)*erfi(sqr
t(2)*sqrt(b^2)*x)*e^c - 8*(pi*b^3*x^2 - pi*b)*erfi(b*x)*e^(b^2*x^2 + c))/(p
i*b^5)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^c\int x^3e^{b^2x^2}\,\mathrm{erfi}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*x**3*erfi(b*x),x)
```

```
[Out] exp(c)*Integral(x**3*exp(b**2*x**2)*erfi(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^3*erfi(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^3*erfi(b*x)*e^(b^2*x^2 + c), x)
```

Mupad [B]
time = 0.44, size = 117, normalized size = 1.21

$$\frac{\sqrt{2}\,\mathrm{e}^c\,\mathrm{erfi}\left(\sqrt{2}\,x\,\sqrt{b^2}\right)}{16\,b\,{\left(b^2\right)}^{3/2}}-\frac{x\,\mathrm{e}^{2\,b^2\,x^2+c}}{4\,b^3\,\sqrt{\pi}}-\mathrm{erfi}(b\,x)\,\left(\frac{\mathrm{e}^{b^2\,x^2+c}}{2\,b^4}-\frac{x^2\,\mathrm{e}^{b^2\,x^2+c}}{2\,b^2}\right)-\frac{\sqrt{2}\,\mathrm{erf}\left(\sqrt{2}\,x\,\sqrt{-b^2}\right)\,\mathrm{e}^c}{4\,b\,{\left(-b^2\right)}^{3/2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*exp(c + b^2*x^2)*erfi(b*x),x)
```

```
[Out] (2^(1/2)*exp(c)*erfi(2^(1/2)*x*(b^2)^(1/2)))/(16*b*(b^2)^(3/2)) - (x*exp(c
+ 2*b^2*x^2))/(4*b^3*pi^(1/2)) - erfi(b*x)*(exp(c + b^2*x^2)/(2*b^4) - (x^2
*exp(c + b^2*x^2))/(2*b^2)) - (2^(1/2)*erf(2^(1/2)*x*(-b^2)^(1/2))*exp(c))/
(4*b*(-b^2)^(3/2))
```

3.285 $\int e^{c+b^2x^2} x\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=47

$$\frac{e^{c+b^2x^2}\text{Erfi}(bx)}{2b^2}-\frac{e^c\text{Erfi}\left(\sqrt{2}\,bx\right)}{2\sqrt{2}\,b^2}$$

```
[Out] 1/2*exp(b^2*x^2+c)*erfi(b*x)/b^2-1/4*exp(c)*erfi(b*x*2^(1/2))/b^2*2^(1/2)
```

Rubi [A]
time = 0.03, antiderivative size = 47, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}}=0.118$, Rules used = {6519, 2235}

$$\frac{e^{b^2x^2+c}\text{Erfi}(bx)}{2b^2}-\frac{e^c\text{Erfi}\left(\sqrt{2}\,bx\right)}{2\sqrt{2}\,b^2}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*x*Erfi[b*x],x]
```

```
[Out] (E^(c + b^2*x^2)*Erfi[b*x])/(2*b^2) - (E^c*Erfi[Sqrt[2]*b*x])/(2*Sqrt[2]*b^
2)
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\begin{aligned}\int e^{c+b^2x^2}x\text{erfi}(bx)\,dx&=\frac{e^{c+b^2x^2}\text{erfi}(bx)}{2b^2}-\frac{\int e^{c+2b^2x^2}\,dx}{b\sqrt{\pi}}\\&=\frac{e^{c+b^2x^2}\text{erfi}(bx)}{2b^2}-\frac{e^c\text{erfi}\left(\sqrt{2}\,bx\right)}{2\sqrt{2}\,b^2}\end{aligned}$$

Mathematica [A]
time = 0.01, size = 42, normalized size = 0.89

$$\frac{e^c\left(2e^{b^2x^2}\operatorname{Erfi}(bx)-\sqrt{2}\operatorname{Erfi}\left(\sqrt{2}\,bx\right)\right)}{4b^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*x*Erfi[b*x],x]
[Out] (E^c*(2*E^(b^2*x^2)*Erfi[b*x] - Sqrt[2]*Erfi[Sqrt[2]*b*x]))/(4*b^2)
```

Maple [F]
time = 0.13, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{b^2x^2+c}x\operatorname{erfi}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*x*erfi(b*x),x)
[Out] int(exp(b^2*x^2+c)*x*erfi(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x*erfi(b*x),x, algorithm="maxima")
[Out] integrate(x*erfi(b*x)*e^(b^2*x^2 + c), x)
```

Fricas [A]
time = 0.35, size = 46, normalized size = 0.98

$$\frac{2\,b\operatorname{erfi}(bx)\,e^{\left(b^2x^2+c\right)}-\sqrt{2}\,\sqrt{b^2}\,\operatorname{erfi}\left(\sqrt{2}\,\sqrt{b^2}\,x\right)e^c}{4\,b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x*erfi(b*x),x, algorithm="fricas")
[Out] 1/4*(2*b*erfi(b*x)*e^(b^2*x^2 + c) - sqrt(2)*sqrt(b^2)*erfi(sqrt(2)*sqrt(b^
2)*x)*e^c)/b^3
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^c\int xe^{b^2x^2}\operatorname{erfi}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*x*erfi(b*x),x)
```

```
[Out] exp(c)*Integral(x*exp(b**2*x**2)*erfi(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x*erfi(b*x),x, algorithm="giac")
```

```
[Out] integrate(x*erfi(b*x)*e^(b^2*x^2 + c), x)
```

Mupad [B]
time = 0.28, size = 50, normalized size = 1.06

$$\frac{e^{b^2\,x^2}\,e^c\,\mathrm{erfi}(b\,x)}{2\,b^2}-\frac{\sqrt{2}\,\mathrm{erf}\left(\sqrt{2}\,x\,\sqrt{-b^2}\right)\,e^c}{4\,b\,\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*exp(c + b^2*x^2)*erfi(b*x),x)
```

```
[Out] (exp(b^2*x^2)*exp(c)*erfi(b*x))/(2*b^2) - (2^(1/2)*erf(2^(1/2)*x*(-b^2)^(1/
2))*exp(c))/(4*b*(-b^2)^(1/2))
```

3.286 $\int \frac{e^{c+b^2x^2}\mathbf{Erfi}(bx)}{x}\,dx$

Optimal. Leaf size=22

$$\mathrm{Int}\left(\frac{e^{c+b^2x^2}\mathrm{Erfi}(bx)}{x},x\right)$$

```
[Out] Unintegrable(exp(b^2*x^2+c)*erfi(b*x)/x,x)
```

Rubi [A]
time = 0.03, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+b^2x^2}\mathrm{Erfi}(bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + b^2*x^2)*Erfi[b*x])/x,x]
[Out] Defer[Int][(E^(c + b^2*x^2)*Erfi[b*x])/x, x]
```

Rubi steps

$$\int \frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{x}\,dx = \int \frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{x}\,dx$$

Mathematica [A]
time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{e^{c+b^2x^2}\mathrm{Erfi}(bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + b^2*x^2)*Erfi[b*x])/x,x]
[Out] Integrate[(E^(c + b^2*x^2)*Erfi[b*x])/x, x]
```

Maple [A]
time = 0.04, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{b^2x^2+c}\,\mathrm{erfi}\,(bx)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erfi(b*x)/x,x)
```

```
[Out] int(exp(b^2*x^2+c)*erfi(b*x)/x,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)/x,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)*e^(b^2*x^2 + c)/x, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)/x,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x)*e^(b^2*x^2 + c)/x, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int\frac{e^{b^{2}x^{2}}\operatorname{erfi}\left(bx\right)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erfi(b*x)/x,x)
```

```
[Out] exp(c)*Integral(exp(b**2*x**2)*erfi(b*x)/x, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)/x,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)*e^(b^2*x^2 + c)/x, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{e^{b^2 x^2+c} \operatorname{erfi}(b x)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + b^2*x^2)*erfi(b*x))/x,x)
[Out] int((exp(c + b^2*x^2)*erfi(b*x))/x, x)
```

3.287 $\int \frac{e^{c+b^2x^2}\mathbf{Erfi}(bx)}{x^3}\,dx$

Optimal. Leaf size=93

$$-\frac{be^{c+2b^2x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+b^2x^2}\mathrm{Erfi}(bx)}{2x^2}+\sqrt{2}\,b^2e^c\mathrm{Erfi}\left(\sqrt{2}\,bx\right)+b^2\mathrm{Int}\left(\frac{e^{c+b^2x^2}\mathrm{Erfi}(bx)}{x},x\right)$$

```
[Out] -1/2*exp(b^2*x^2+c)*erfi(b*x)/x^2+b^2*exp(c)*erfi(b*x*2^(1/2))*2^(1/2)-b*ex
p(2*b^2*x^2+c)/x/Pi^(1/2)+b^2*Unintegrable(exp(b^2*x^2+c)*erfi(b*x)/x,x)
```

Rubi [A]
time = 0.08, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+b^2x^2}\mathrm{Erfi}(bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + b^2*x^2)*Erfi[b*x])/x^3,x]
```

```
[Out] -((b*E^(c + 2*b^2*x^2))/(Sqrt[Pi]*x)) - (E^(c + b^2*x^2)*Erfi[b*x])/(2*x^2)
 + Sqrt[2]*b^2*E^c*Erfi[Sqrt[2]*b*x] + b^2*Defer[Int][(E^(c + b^2*x^2)*Erfi
[b*x])/x, x]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{x^3}\,dx &= -\frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{2x^2}+b^2\int \frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{x}\,dx+\frac{b\int \frac{e^{c+2b^2x^2}}{x^2}\,dx}{\sqrt{\pi}}\\ &= -\frac{be^{c+2b^2x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{2x^2}+b^2\int \frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{x}\,dx+\frac{(4b^3)\int e^{c+2b^2x^2}\,dx}{\sqrt{\pi}}\\ &= -\frac{be^{c+2b^2x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{2x^2}+\sqrt{2}\,b^2e^c\mathrm{erfi}\left(\sqrt{2}\,bx\right)+b^2\int \frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{x}\,dx\end{aligned}$$

Mathematica [A]
time = 0.11, size = 0, normalized size = 0.00

$$\int \frac{e^{c+b^2x^2}\mathrm{Erfi}(bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + b^2*x^2)*Erfi[b*x])/x^3,x]
[Out] Integrate[(E^(c + b^2*x^2)*Erfi[b*x])/x^3, x]
```

Maple [A]
time = 0.15, size = 0, normalized size = 0.00

$$\int \frac{e^{b^2x^2+c}\,\mathrm{erfi}\,(bx)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erfi(b*x)/x^3,x)
[Out] int(exp(b^2*x^2+c)*erfi(b*x)/x^3,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)/x^3,x, algorithm="maxima")
[Out] integrate(erfi(b*x)*e^(b^2*x^2 + c)/x^3, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)/x^3,x, algorithm="fricas")
[Out] integral(erfi(b*x)*e^(b^2*x^2 + c)/x^3, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{b^2x^2}\,\mathrm{erfi}\,(bx)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erfi(b*x)/x**3,x)
[Out] exp(c)*Integral(exp(b**2*x**2)*erfi(b*x)/x**3, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)/x^3,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)*e^(b^2*x^2 + c)/x^3, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{b^2\,x^2+c}\,\mathrm{erfi}\left(b\,x\right)}{x^3} \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + b^2*x^2)*erfi(b*x))/x^3,x)
```

```
[Out] int((exp(c + b^2*x^2)*erfi(b*x))/x^3, x)
```

3.288 $\int \frac{e^{c+b^2x^2}\mathbf{Erfi}(bx)}{x^5}\,dx$

Optimal. Leaf size=174

$$-\frac{be^{c+2b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{7b^3e^{c+2b^2x^2}}{6\sqrt{\pi}\,x}-\frac{e^{c+b^2x^2}\mathrm{Erfi}(bx)}{4x^4}-\frac{b^2e^{c+b^2x^2}\mathrm{Erfi}(bx)}{4x^2}+\frac{b^4e^c\mathrm{Erfi}\left(\sqrt{2}\,bx\right)}{\sqrt{2}}+\frac{2}{3}\sqrt{2}\,b^4e^c\mathrm{Erfi}\left(\sqrt{2}\,bx\right)+\frac{1}{2}$$

```
[Out] -1/4*exp(b^2*x^2+c)*erfi(b*x)/x^4-1/4*b^2*exp(b^2*x^2+c)*erfi(b*x)/x^2+7/6*
b^4*exp(c)*erfi(b*x*2^(1/2))*2^(1/2)-1/6*b*exp(2*b^2*x^2+c)/x^3/Pi^(1/2)-7/
6*b^3*exp(2*b^2*x^2+c)/x/Pi^(1/2)+1/2*b^4*Unintegrable(exp(b^2*x^2+c)*erfi(
b*x)/x,x)
```

Rubi [A]
time = 0.15, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.000, Rules used = {}

$$\int \frac{e^{c+b^2x^2}\mathrm{Erfi}(bx)}{x^5}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + b^2*x^2)*Erfi[b*x])/x^5,x]
```

```
[Out] -1/6*(b*E^(c + 2*b^2*x^2))/(Sqrt[Pi]*x^3) - (7*b^3*E^(c + 2*b^2*x^2))/(6*Sq
rt[Pi]*x) - (E^(c + b^2*x^2)*Erfi[b*x])/(4*x^4) - (b^2*E^(c + b^2*x^2)*Erfi
[b*x])/(4*x^2) + (b^4*E^c*Erfi[Sqrt[2]*b*x])/Sqrt[2] + (2*Sqrt[2]*b^4*E^c*E
rfi[Sqrt[2]*b*x])/3 + (b^4*Defer[Int][(E^(c + b^2*x^2)*Erfi[b*x])/x, x])/2
```

Rubi steps

$$\begin{aligned}
\int \frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{x^5}\,dx &= -\frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{4x^4}+\frac{1}{2}b^2\int \frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{x^3}\,dx+\frac{b\int \frac{e^{c+2b^2x^2}}{x^4}\,dx}{2\sqrt{\pi}}\\
&= -\frac{be^{c+2b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{4x^4}-\frac{b^2e^{c+b^2x^2}\mathrm{erfi}(bx)}{4x^2}+\frac{1}{2}b^4\int \frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{x}\,dx+\frac{b^3\int e}{2}\\
&= -\frac{be^{c+2b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{7b^3e^{c+2b^2x^2}}{6\sqrt{\pi}\,x}-\frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{4x^4}-\frac{b^2e^{c+b^2x^2}\mathrm{erfi}(bx)}{4x^2}+\frac{1}{2}b^4\int \frac{e^{c+b^2x^2}\mathrm{erfi}(b}{x}\\
&= -\frac{be^{c+2b^2x^2}}{6\sqrt{\pi}\,x^3}-\frac{7b^3e^{c+2b^2x^2}}{6\sqrt{\pi}\,x}-\frac{e^{c+b^2x^2}\mathrm{erfi}(bx)}{4x^4}-\frac{b^2e^{c+b^2x^2}\mathrm{erfi}(bx)}{4x^2}+\frac{b^4e^c\mathrm{erfi}\left(\sqrt{2}\,bx\right)}{\sqrt{2}}+
\end{aligned}$$

Mathematica [A]
time = 0.15, size = 0, normalized size = 0.00

$$\int \frac{e^{c+b^2x^2}\text{Erfi}(bx)}{x^5}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + b^2*x^2)*Erfi[b*x])/x^5,x]
[Out] Integrate[(E^(c + b^2*x^2)*Erfi[b*x])/x^5, x]
```

Maple [A]
time = 0.16, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{b^2x^2+c}\,\text{erfi}\,(bx)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erfi(b*x)/x^5,x)
[Out] int(exp(b^2*x^2+c)*erfi(b*x)/x^5,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)/x^5,x, algorithm="maxima")
[Out] integrate(erfi(b*x)*e^(b^2*x^2 + c)/x^5, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)/x^5,x, algorithm="fricas")
[Out] integral(erfi(b*x)*e^(b^2*x^2 + c)/x^5, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^c \int \frac{e^{b^2x^2}\,\text{erfi}\,(bx)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erfi(b*x)/x**5,x)
[Out] exp(c)*Integral(exp(b**2*x**2)*erfi(b*x)/x**5, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)/x^5,x, algorithm="giac")
[Out] integrate(erfi(b*x)*e^(b^2*x^2 + c)/x^5, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{b^2\,x^2+c}\,\mathrm{erfi}(b\,x)}{x^5}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + b^2*x^2)*erfi(b*x))/x^5,x)
[Out] int((exp(c + b^2*x^2)*erfi(b*x))/x^5, x)
```

3.289 $\int e^{c+b^2x^2}x^4\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=121

$$\frac{e^{c+2b^2x^2}}{2b^5\sqrt{\pi}}-\frac{e^{c+2b^2x^2}x^2}{4b^3\sqrt{\pi}}-\frac{3e^{c+b^2x^2}x\text{Erfi}(bx)}{4b^4}+\frac{e^{c+b^2x^2}x^3\text{Erfi}(bx)}{2b^2}+\frac{3e^c\sqrt{\pi}\,\text{Erfi}(bx)^2}{16b^5}$$

```
[Out] -3/4*exp(b^2*x^2+c)*x*erfi(b*x)/b^4+1/2*exp(b^2*x^2+c)*x^3*erfi(b*x)/b^2+1/
2*exp(2*b^2*x^2+c)/b^5/Pi^(1/2)-1/4*exp(2*b^2*x^2+c)*x^2/b^3/Pi^(1/2)+3/16*
exp(c)*erfi(b*x)^2*Pi^(1/2)/b^5
```

Rubi [A]
time = 0.11, antiderivative size = 121, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {6522, 6510, 30, 2240, 2243}

$$\frac{3\sqrt{\pi}\,e^c\text{Erfi}(bx)^2}{16b^5}+\frac{x^3e^{b^2x^2+c}\text{Erfi}(bx)}{2b^2}+\frac{e^{2b^2x^2+c}}{2\sqrt{\pi}\,b^5}-\frac{3xe^{b^2x^2+c}\text{Erfi}(bx)}{4b^4}-\frac{x^2e^{2b^2x^2+c}}{4\sqrt{\pi}\,b^3}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*x^4*Erfi[b*x],x]
```

```
[Out] E^(c + 2*b^2*x^2)/(2*b^5*Sqrt[Pi]) - (E^(c + 2*b^2*x^2)*x^2)/(4*b^3*Sqrt[Pi
]) - (3*E^(c + b^2*x^2)*x*Erfi[b*x])/(4*b^4) + (E^(c + b^2*x^2)*x^3*Erfi[b*
x])/(2*b^2) + (3*E^c*Sqrt[Pi]*Erfi[b*x]^2)/(16*b^5)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 2243

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m - n + 1)*(F^(a + b*(c + d*x)^n)/(b*d*n*L
og[F])), x] - Dist[(m - n + 1)/(b*n*Log[F]), Int[(c + d*x)^(m - n)*F^(a + b
*(c + d*x)^n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n
)] && LtQ[0, (m + 1)/n, 5] && IntegerQ[n] && (LtQ[0, n, m + 1] || LtQ[m, n,
 0])
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\begin{aligned}
\int e^{c+b^2x^2}x^4\text{erfi}(bx)\,dx &= \frac{e^{c+b^2x^2}x^3\text{erfi}(bx)}{2b^2}-\frac{3\int e^{c+b^2x^2}x^2\text{erfi}(bx)\,dx}{2b^2}-\frac{\int e^{c+2b^2x^2}x^3\,dx}{b\sqrt{\pi}}\\
&= -\frac{e^{c+2b^2x^2}x^2}{4b^3\sqrt{\pi}}-\frac{3e^{c+b^2x^2}x\text{erfi}(bx)}{4b^4}+\frac{e^{c+b^2x^2}x^3\text{erfi}(bx)}{2b^2}+\frac{3\int e^{c+b^2x^2}\text{erfi}(bx)\,dx}{4b^4}+\frac{\int e\cdots}{\cdots}\\
&= \frac{e^{c+2b^2x^2}}{2b^5\sqrt{\pi}}-\frac{e^{c+2b^2x^2}x^2}{4b^3\sqrt{\pi}}-\frac{3e^{c+b^2x^2}x\text{erfi}(bx)}{4b^4}+\frac{e^{c+b^2x^2}x^3\text{erfi}(bx)}{2b^2}+\frac{\left(3e^c\sqrt{\pi}\right)\text{Subst}(\int\cdots}{8b\cdots}\\
&= \frac{e^{c+2b^2x^2}}{2b^5\sqrt{\pi}}-\frac{e^{c+2b^2x^2}x^2}{4b^3\sqrt{\pi}}-\frac{3e^{c+b^2x^2}x\text{erfi}(bx)}{4b^4}+\frac{e^{c+b^2x^2}x^3\text{erfi}(bx)}{2b^2}+\frac{3e^c\sqrt{\pi}\,\text{erfi}(bx)^2}{16b^5}
\end{aligned}$$

Mathematica [A]
time = 0.03, size = 78, normalized size = 0.64

$$\frac{e^c\left(-4e^{2b^2x^2}(-2+b^2x^2)+4be^{b^2x^2}\sqrt{\pi}\,x(-3+2b^2x^2)\,\text{Erfi}(bx)+3\pi\text{Erfi}(bx)^2\right)}{16b^5\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*x^4*Erfi[b*x],x]
[Out] (E^c*(-4*E^(2*b^2*x^2)*(-2 + b^2*x^2) + 4*b*E^(b^2*x^2)*Sqrt[Pi]*x*(-3 + 2*
b^2*x^2)*Erfi[b*x] + 3*Pi*Erfi[b*x]^2))/(16*b^5*Sqrt[Pi])
```

Maple [F]
time = 0.06, size = 0, normalized size = 0.00

$$\int e^{b^2x^2+c}x^4\,\text{erfi}\,(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*x^4*erfi(b*x),x)
```

```
[Out] int(exp(b^2*x^2+c)*x^4*erfi(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^4*erfi(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x^4*erfi(b*x)*e^(b^2*x^2 + c), x)
```

Fricas [A]
time = 0.36, size = 74, normalized size = 0.61

$$\frac{\left(4\,(2\,\pi b^3x^3 - 3\,\pi bx)\operatorname{erfi}(bx)\,e^{(b^2x^2)} + \sqrt{\pi}\left(3\,\pi\operatorname{erfi}(bx)^2 - 4\,(b^2x^2 - 2)e^{(2\,b^2x^2)}\right)\right)e^c}{16\,\pi b^5}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^4*erfi(b*x),x, algorithm="fricas")
```

```
[Out] 1/16*(4*(2*pi*b^3*x^3 - 3*pi*b*x)*erfi(b*x)*e^(b^2*x^2) + sqrt(pi)*(3*pi*er
fi(b*x)^2 - 4*(b^2*x^2 - 2)*e^(2*b^2*x^2)))*e^c/(pi*b^5)
```

Sympy [A]
time = 1.83, size = 124, normalized size = 1.02

$$\begin{cases} \frac{x^3e^ce^{b^2x^2}\operatorname{erfi}(bx)}{2b^2} - \frac{x^2e^ce^{2b^2x^2}}{4\sqrt{\pi}\,b^3} - \frac{3xe^ce^{b^2x^2}\operatorname{erfi}(bx)}{4b^4} + \frac{e^ce^{2b^2x^2}}{2\sqrt{\pi}\,b^5} + \frac{3\sqrt{\pi}\,e^c\operatorname{erfi}^2(bx)}{16b^5} & \text{for } b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*x**4*erfi(b*x),x)
```

```
[Out] Piecewise((x**3*exp(c)*exp(b**2*x**2)*erfi(b*x)/(2*b**2) - x**2*exp(c)*exp(
2*b**2*x**2)/(4*sqrt(pi)*b**3) - 3*x*exp(c)*exp(b**2*x**2)*erfi(b*x)/(4*b**
4) + exp(c)*exp(2*b**2*x**2)/(2*sqrt(pi)*b**5) + 3*sqrt(pi)*exp(c)*erfi(b*x
)**2/(16*b**5), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^4*erfi(b*x),x, algorithm="giac")
```

```
[Out] integrate(x^4*erfi(b*x)*e^(b^2*x^2 + c), x)
```

Mupad [B]
time = 0.50, size = 126, normalized size = 1.04

$$\mathrm{erfi}(b\,x)\,\left(\frac{x^3\,\mathrm{e}^{b^2\,x^2+c}}{2\,b^2}-\frac{3\,x\,\mathrm{e}^{b^2\,x^2+c}}{4\,b^4}+\frac{3\,\sqrt{\pi}\,\mathrm{erfi}\left(\frac{b^2\,x}{\sqrt{b^2}}\right)\,\mathrm{e}^c}{8\,{\left(b^2\right)}^{5/2}}\right)+\frac{8\,\mathrm{e}^{2\,b^2\,x^2+c}-3\,\pi\,\mathrm{erfi}{\left(\frac{b^2\,x}{\sqrt{b^2}}\right)}^2\,\mathrm{e}^c}{16\,b^5\,\sqrt{\pi}}-\frac{x^2\,\mathrm{e}^{2\,b^2\,x^2+c}}{4\,b^3\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*exp(c + b^2*x^2)*erfi(b*x),x)
```

```
[Out] erfi(b*x)*((x^3*exp(c + b^2*x^2))/(2*b^2) - (3*x*exp(c + b^2*x^2))/(4*b^4)
+ (3*pi^(1/2)*erfi((b^2*x)/(b^2)^(1/2))*exp(c))/(8*(b^2)^(5/2))) + (8*exp(c
 + 2*b^2*x^2) - 3*pi*erfi((b^2*x)/(b^2)^(1/2))^2*exp(c))/(16*b^5*pi^(1/2))
- (x^2*exp(c + 2*b^2*x^2))/(4*b^3*pi^(1/2))
```

3.290 $\int e^{c+b^2x^2}x^2\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=69

$$-\frac{e^{c+2b^2x^2}}{4b^3\sqrt{\pi}}+\frac{e^{c+b^2x^2}x\mathrm{Erfi}(bx)}{2b^2}-\frac{e^c\sqrt{\pi}\,\mathrm{Erfi}(bx)^2}{8b^3}$$

```
[Out] 1/2*exp(b^2*x^2+c)*x*erfi(b*x)/b^2-1/4*exp(2*b^2*x^2+c)/b^3/Pi^(1/2)-1/8*ex
p(c)*erfi(b*x)^2*Pi^(1/2)/b^3
```

Rubi [A]
time = 0.05, antiderivative size = 69, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}=0.210$, Rules used = {6522, 6510, 30, 2240}

$$-\frac{\sqrt{\pi}\,e^c\mathrm{Erfi}(bx)^2}{8b^3}+\frac{xe^{b^2x^2+c}\mathrm{Erfi}(bx)}{2b^2}-\frac{e^{2b^2x^2+c}}{4\sqrt{\pi}\,b^3}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + b^2*x^2)*x^2*Erfi[b*x],x]
```

```
[Out] -1/4*E^(c + 2*b^2*x^2)/(b^3*Sqrt[Pi]) + (E^(c + b^2*x^2)*x*Erfi[b*x])/(2*b^
2) - (E^c*Sqrt[Pi]*Erfi[b*x]^2)/(8*b^3)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2240

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((e_.) + (f_.)*(x_))^(m_
.), x_Symbol] :> Simp[(e + f*x)^n*(F^(a + b*(c + d*x)^n)/(b*f*n*(c + d*x)^n
*Log[F])), x] /; FreeQ[{F, a, b, c, d, e, f, n}, x] && EqQ[m, n - 1] && EqQ
[d*e - c*f, 0]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
```

```
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$
\begin{aligned}
\int e^{c+b^2x^2}x^2\operatorname{erfi}(bx)\,dx &= \frac{e^{c+b^2x^2}x\operatorname{erfi}(bx)}{2b^2} - \frac{\int e^{c+b^2x^2}\operatorname{erfi}(bx)\,dx}{2b^2} - \frac{\int e^{c+2b^2x^2}x\,dx}{b\sqrt{\pi}} \\
&= -\frac{e^{c+2b^2x^2}}{4b^3\sqrt{\pi}} + \frac{e^{c+b^2x^2}x\operatorname{erfi}(bx)}{2b^2} - \frac{\left(e^c\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx, x, \operatorname{erfi}(bx)\right)}{4b^3} \\
&= -\frac{e^{c+2b^2x^2}}{4b^3\sqrt{\pi}} + \frac{e^{c+b^2x^2}x\operatorname{erfi}(bx)}{2b^2} - \frac{e^c\sqrt{\pi}\operatorname{erfi}(bx)^2}{8b^3}
\end{aligned}
$$

Mathematica [A]
time = 0.01, size = 58, normalized size = 0.84

$$-\frac{e^c\left(2e^{2b^2x^2} - 4be^{b^2x^2}\sqrt{\pi}\,x\operatorname{Erfi}(bx) + \pi\operatorname{Erfi}(bx)^2\right)}{8b^3\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*x^2*Erfi[b*x],x]
```

```
[Out] -1/8*(E^c*(2*E^(2*b^2*x^2) - 4*b*E^(b^2*x^2)*Sqrt[Pi]*x*Erfi[b*x] + Pi*Erfi
[b*x]^2))/(b^3*Sqrt[Pi])
```

Maple [F]
time = 0.13, size = 0, normalized size = 0.00

$$\int e^{b^2x^2+c}x^2\operatorname{erfi}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*x^2*erfi(b*x),x)
```

```
[Out] int(exp(b^2*x^2+c)*x^2*erfi(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^2*erfi(b*x),x, algorithm="maxima")
[Out] integrate(x^2*erfi(b*x)*e^(b^2*x^2 + c), x)
```

Fricas [A]
time = 0.34, size = 53, normalized size = 0.77

$$\frac{\left(4\,\pi bx\,\mathrm{erfi}\left(bx\right)e^{\left(b^2x^2\right)}-\sqrt{\pi}\left(\pi\,\mathrm{erfi}\left(bx\right)^2+2\,e^{\left(2\,b^2x^2\right)}\right)\right)e^c}{8\,\pi b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^2*erfi(b*x),x, algorithm="fricas")
[Out] 1/8*(4*pi*b*x*erfi(b*x)*e^(b^2*x^2) - sqrt(pi)*(pi*erfi(b*x)^2 + 2*e^(2*b^2
*x^2)))*e^c/(pi*b^3)
```

Sympy [A]
time = 0.51, size = 68, normalized size = 0.99

$$\begin{cases}\frac{xe^ce^{b^2x^2}\,\mathrm{erfi}\left(bx\right)}{2b^2}-\frac{e^ce^{2b^2x^2}}{4\sqrt{\pi}\,b^3}-\frac{\sqrt{\pi}\,e^c\,\mathrm{erfi}^2\left(bx\right)}{8b^3} & \text{for}\ b\neq 0\\ 0 & \text{otherwise}\end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*x**2*erfi(b*x),x)
[Out] Piecewise((x*exp(c)*exp(b**2*x**2)*erfi(b*x)/(2*b**2) - exp(c)*exp(2*b**2*x
**2)/(4*sqrt(pi)*b**3) - sqrt(pi)*exp(c)*erfi(b*x)**2/(8*b**3), Ne(b, 0)),
(0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*x^2*erfi(b*x),x, algorithm="giac")
[Out] integrate(x^2*erfi(b*x)*e^(b^2*x^2 + c), x)
```

Mupad [B]
time = 0.32, size = 86, normalized size = 1.25

$$\mathrm{erfi}(b\,x)\,\left(\frac{x\,\mathrm{e}^{b^2\,x^2+c}}{2\,b^2}-\frac{\sqrt{\pi}\,\mathrm{erfi}\left(\frac{b^2\,x}{\sqrt{b^2}}\right)\,\mathrm{e}^c}{4\,{\left(b^2\right)}^{3/2}}\right)-\frac{2\,\mathrm{e}^{2\,b^2\,x^2+c}-\pi\,\mathrm{erfi}{\left(\frac{b^2\,x}{\sqrt{b^2}}\right)}^2\,\mathrm{e}^c}{8\,b^3\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*exp(c + b^2*x^2)*erfi(b*x),x)
```

```
[Out] erfi(b*x)*((x*exp(c + b^2*x^2))/(2*b^2) - (pi^(1/2)*erfi((b^2*x)/(b^2)^(1/2
))*exp(c))/(4*(b^2)^(3/2))) - (2*exp(c + 2*b^2*x^2) - pi*erfi((b^2*x)/(b^2)
^(1/2))^2*exp(c))/(8*b^3*pi^(1/2))
```

3.291 $\int e^{c+b^2x^2}\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=21

$$\frac{e^c\sqrt{\pi}\,\text{Erfi}(bx)^2}{4b}$$

[Out] 1/4*exp(c)*erfi(b*x)^2*Pi^(1/2)/b

Rubi [A]
time = 0.01, antiderivative size = 21, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {6510, 30}

$$\frac{\sqrt{\pi}\,e^c\text{Erfi}(bx)^2}{4b}$$

Antiderivative was successfully verified.

[In] Int[E^(c + b^2*x^2)*Erfi[b*x],x]

[Out] (E^c*Sqrt[Pi]*Erfi[b*x]^2)/(4*b)

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rubi steps

$$\begin{aligned}\int e^{c+b^2x^2}\text{erfi}(bx)\,dx &= \frac{\left(e^c\sqrt{\pi}\right)\text{Subst}\left(\int x\,dx, x, \text{erfi}(bx)\right)}{2b}\\ &= \frac{e^c\sqrt{\pi}\,\text{erfi}(bx)^2}{4b}\end{aligned}$$

Mathematica [A]
time = 0.00, size = 21, normalized size = 1.00

$$\frac{e^c\sqrt{\pi}\,\text{Erfi}(bx)^2}{4b}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + b^2*x^2)*Erfi[b*x],x]
```

```
[Out] (E^c*Sqrt[Pi]*Erfi[b*x]^2)/(4*b)
```

Maple [F]
time = 0.03, size = 0, normalized size = 0.00

$$\int e^{b^2x^2+c} \operatorname{erfi}(bx)\ dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erfi(b*x),x)
```

```
[Out] int(exp(b^2*x^2+c)*erfi(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x),x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)*e^(b^2*x^2 + c), x)
```

Fricas [A]
time = 0.34, size = 16, normalized size = 0.76

$$\frac{\sqrt{\pi}\ \operatorname{erfi}(bx)^2\, e^c}{4\, b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x),x, algorithm="fricas")
```

```
[Out] 1/4*sqrt(pi)*erfi(b*x)^2*e^c/b
```

Sympy [A]
time = 0.16, size = 19, normalized size = 0.90

$$\begin{cases} \frac{\sqrt{\pi}\ e^c \operatorname{erfi}^2(bx)}{4b} & \text{for}\ b \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erfi(b*x),x)
```

```
[Out] Piecewise((sqrt(pi)*exp(c)*erfi(b*x)**2/(4*b), Ne(b, 0)), (0, True))
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x),x, algorithm="giac")
[Out] integrate(erfi(b*x)*e^(b^2*x^2 + c), x)
```

Mupad [B]
time = 0.31, size = 91, normalized size = 4.33

$$\frac{\sqrt{\pi}\,\mathrm{erfi}\left(\frac{b^2\,x}{\sqrt{b^2}}\right)\,\mathrm{e}^c\,\mathrm{erfi}(b\,x)}{2\,\sqrt{b^2}}-\frac{\sqrt{\pi}\,\mathrm{e}^c\,\mathrm{erf}{\left(x\,\sqrt{-b^2}\right)}^2}{4\,b}-\frac{b\,\sqrt{\pi}\,\mathrm{erfi}\left(\frac{b^2\,x}{\sqrt{b^2}}\right)\,\mathrm{e}^c\,\mathrm{erf}\left(x\,\sqrt{-b^2}\right)}{2\,\sqrt{b^2}\,\sqrt{-b^2}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(c + b^2*x^2)*erfi(b*x),x)
[Out] (pi^(1/2)*erfi((b^2*x)/(b^2)^(1/2))*exp(c)*erfi(b*x))/(2*(b^2)^(1/2)) - (pi
^(1/2)*exp(c)*erf(x*(-b^2)^(1/2))^2)/(4*b) - (b*pi^(1/2)*erfi((b^2*x)/(b^2)
^(1/2))*exp(c)*erf(x*(-b^2)^(1/2)))/(2*(b^2)^(1/2)*(-b^2)^(1/2))
```

3.292 $\int \frac{e^{c+b^2x^2}\textbf{Erfi}(bx)}{x^2}\,dx$

Optimal. Leaf size=59

$$-\frac{e^{c+b^2x^2}\operatorname{Erfi}(bx)}{x}+\frac{1}{2}be^c\sqrt{\pi}\operatorname{Erfi}(bx)^2+\frac{be^c\operatorname{Ei}(2b^2x^2)}{\sqrt{\pi}}$$

```
[Out] -exp(b^2*x^2+c)*erfi(b*x)/x+b*exp(c)*Ei(2*b^2*x^2)/Pi^(1/2)+1/2*b*exp(c)*er
fi(b*x)^2*Pi^(1/2)
```

Rubi [A]
time = 0.05, antiderivative size = 59, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.210$, Rules used = {6528, 6510, 30, 2241}

$$-\frac{e^{b^2x^2+c}\operatorname{Erfi}(bx)}{x}+\frac{be^c\operatorname{Ei}(2b^2x^2)}{\sqrt{\pi}}+\frac{1}{2}\sqrt{\pi}\,be^c\operatorname{Erfi}(bx)^2$$

Antiderivative was successfully verified.

```
[In] Int[(E^(c + b^2*x^2)*Erfi[b*x])/x^2,x]
```

```
[Out] -((E^(c + b^2*x^2)*Erfi[b*x])/x) + (b*E^c*Sqrt[Pi]*Erfi[b*x]^2)/2 + (b*E^c*
ExpIntegralEi[2*b^2*x^2])/Sqrt[Pi]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6528

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[2*(b/((m
```

```
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x
]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}\int \frac{e^{c+b^2x^2}\operatorname{erfi}(bx)}{x^2}\,dx &= -\frac{e^{c+b^2x^2}\operatorname{erfi}(bx)}{x} + (2b^2)\int e^{c+b^2x^2}\operatorname{erfi}(bx)\,dx + \frac{(2b)\int \frac{e^{c+2b^2x^2}}{x}\,dx}{\sqrt{\pi}}\\ &= -\frac{e^{c+b^2x^2}\operatorname{erfi}(bx)}{x} + \frac{be^c\operatorname{Ei}(2b^2x^2)}{\sqrt{\pi}} + \left(be^c\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx, x, \operatorname{erfi}(bx)\right)\\ &= -\frac{e^{c+b^2x^2}\operatorname{erfi}(bx)}{x} + \frac{1}{2}be^c\sqrt{\pi}\operatorname{erfi}(bx)^2 + \frac{be^c\operatorname{Ei}(2b^2x^2)}{\sqrt{\pi}}\end{aligned}$$

Mathematica [A]
time = 0.02, size = 56, normalized size = 0.95

$$\frac{1}{2}e^c\left(-\frac{2e^{b^2x^2}\operatorname{Erfi}(bx)}{x} + b\sqrt{\pi}\operatorname{Erfi}(bx)^2 + \frac{2b\operatorname{Ei}(2b^2x^2)}{\sqrt{\pi}}\right)$$

Antiderivative was successfully verified.

```
[In] Integrate[(E^(c + b^2*x^2)*Erfi[b*x])/x^2,x]
```

```
[Out] (E^c*((-2*E^(b^2*x^2)*Erfi[b*x])/x + b*Sqrt[Pi]*Erfi[b*x]^2 + (2*b*ExpInteg
ralEi[2*b^2*x^2])/Sqrt[Pi]))/2
```

Maple [F]
time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{e^{b^2x^2+c}\operatorname{erfi}(bx)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erfi(b*x)/x^2,x)
```

```
[Out] int(exp(b^2*x^2+c)*erfi(b*x)/x^2,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)/x^2,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)*e^(b^2*x^2 + c)/x^2, x)
```

Fricas [A]
time = 0.34, size = 55, normalized size = 0.93

$$-\frac{\left(2\,\pi\,\mathrm{erfi}\left(bx\right)e^{\left(b^2x^2\right)}-\sqrt{\pi}\,\left(\pi bx\,\mathrm{erfi}\left(bx\right)^2+2\,bx\mathrm{Ei}(2\,b^2x^2)\right)\right)e^c}{2\,\pi x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)/x^2,x, algorithm="fricas")
```

```
[Out] -1/2*(2*pi*erfi(b*x)*e^(b^2*x^2) - sqrt(pi)*(pi*b*x*erfi(b*x)^2 + 2*b*x*Ei(
2*b^2*x^2)))*e^c/(pi*x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^c\int\frac{e^{b^2x^2}\,\mathrm{erfi}\left(bx\right)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erfi(b*x)/x**2,x)
```

```
[Out] exp(c)*Integral(exp(b**2*x**2)*erfi(b*x)/x**2, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)/x^2,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)*e^(b^2*x^2 + c)/x^2, x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int\frac{\mathrm{e}^{b^2\,x^2+c}\,\mathrm{erfi}\left(b\,x\right)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + b^2*x^2)*erfi(b*x))/x^2,x)
```

```
[Out] int((exp(c + b^2*x^2)*erfi(b*x))/x^2, x)
```

3.293 $\int \frac{e^{c+b^2x^2}\mathbf{Erfi}(bx)}{x^4}\,dx$

Optimal. Leaf size=118

$$-\frac{be^{c+2b^2x^2}}{3\sqrt{\pi}\,x^2}-\frac{e^{c+b^2x^2}\mathrm{Erfi}(bx)}{3x^3}-\frac{2b^2e^{c+b^2x^2}\mathrm{Erfi}(bx)}{3x}+\frac{1}{3}b^3e^c\sqrt{\pi}\,\mathrm{Erfi}(bx)^2+\frac{4b^3e^c\mathrm{Ei}(2b^2x^2)}{3\sqrt{\pi}}$$

```
[Out] -1/3*exp(b^2*x^2+c)*erfi(b*x)/x^3-2/3*b^2*exp(b^2*x^2+c)*erfi(b*x)/x-1/3*b*
exp(2*b^2*x^2+c)/x^2/Pi^(1/2)+4/3*b^3*exp(c)*Ei(2*b^2*x^2)/Pi^(1/2)+1/3*b^3
*exp(c)*erfi(b*x)^2*Pi^(1/2)
```

Rubi [A]
time = 0.12, antiderivative size = 118, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}}$ = 0.263, Rules used = {6528, 6510, 30, 2241, 2245}

$$\frac{1}{3}\sqrt{\pi}\,b^3e^c\mathrm{Erfi}(bx)^2-\frac{2b^2e^{b^2x^2+c}\mathrm{Erfi}(bx)}{3x}-\frac{e^{b^2x^2+c}\mathrm{Erfi}(bx)}{3x^3}-\frac{be^{2b^2x^2+c}}{3\sqrt{\pi}\,x^2}+\frac{4b^3e^c\mathrm{Ei}(2b^2x^2)}{3\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[(E^(c + b^2*x^2)*Erfi[b*x])/x^4,x]
```

```
[Out] -1/3*(b*E^(c + 2*b^2*x^2))/(Sqrt[Pi]*x^2) - (E^(c + b^2*x^2)*Erfi[b*x])/(3*
x^3) - (2*b^2*E^(c + b^2*x^2)*Erfi[b*x])/(3*x) + (b^3*E^c*Sqrt[Pi]*Erfi[b*x
]^2)/3 + (4*b^3*E^c*ExpIntegralEi[2*b^2*x^2])/(3*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 2241

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))/((e_.) + (f_.)*(x_)), x_
Symbol] :> Simp[F^a*(ExpIntegralEi[b*(c + d*x)^n*Log[F]]/(f*n)), x] /; Free
Q[{F, a, b, c, d, e, f, n}, x] && EqQ[d*e - c*f, 0]
```

Rule 2245

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^(n_))*((c_.) + (d_.)*(x_))^(m_
.), x_Symbol] :> Simp[(c + d*x)^(m + 1)*(F^(a + b*(c + d*x)^n)/(d*(m + 1)))
, x] - Dist[b*n*(Log[F]/(m + 1)), Int[(c + d*x)^(m + n)*F^(a + b*(c + d*x)^
n), x], x] /; FreeQ[{F, a, b, c, d}, x] && IntegerQ[2*((m + 1)/n)] && LtQ[-
4, (m + 1)/n, 5] && IntegerQ[n] && ((GtQ[n, 0] && LtQ[m, -1]) || (GtQ[-n, 0
] && LeQ[-n, m + 1]))
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6528

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x
]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\begin{aligned}
\int \frac{e^{c+b^2x^2}\operatorname{erfi}(bx)}{x^4}\,dx &= -\frac{e^{c+b^2x^2}\operatorname{erfi}(bx)}{3x^3}+\frac{1}{3}\left(2b^2\right)\int \frac{e^{c+b^2x^2}\operatorname{erfi}(bx)}{x^2}\,dx+\frac{(2b)\int \frac{e^{c+2b^2x^2}}{x^3}\,dx}{3\sqrt{\pi}}\\
&= -\frac{be^{c+2b^2x^2}}{3\sqrt{\pi}\,x^2}-\frac{e^{c+b^2x^2}\operatorname{erfi}(bx)}{3x^3}-\frac{2b^2e^{c+b^2x^2}\operatorname{erfi}(bx)}{3x}+\frac{1}{3}\left(4b^4\right)\int e^{c+b^2x^2}\operatorname{erfi}(bx)\,dx+2\cdots\\
&= -\frac{be^{c+2b^2x^2}}{3\sqrt{\pi}\,x^2}-\frac{e^{c+b^2x^2}\operatorname{erfi}(bx)}{3x^3}-\frac{2b^2e^{c+b^2x^2}\operatorname{erfi}(bx)}{3x}+\frac{4b^3e^c\operatorname{Ei}(2b^2x^2)}{3\sqrt{\pi}}+\frac{1}{3}\left(2b^3e^c\sqrt{\pi}\right)\cdots\\
&= -\frac{be^{c+2b^2x^2}}{3\sqrt{\pi}\,x^2}-\frac{e^{c+b^2x^2}\operatorname{erfi}(bx)}{3x^3}-\frac{2b^2e^{c+b^2x^2}\operatorname{erfi}(bx)}{3x}+\frac{1}{3}b^3e^c\sqrt{\pi}\operatorname{erfi}(bx)^2+\frac{4b^3e^c\operatorname{Ei}(2b\cdots}{3\sqrt{\pi}}
\end{aligned}$$

Mathematica [A]
time = 0.03, size = 91, normalized size = 0.77

$$-\frac{e^c\left(e^{b^2x^2}\sqrt{\pi}\left(1+2b^2x^2\right)\operatorname{Erfi}(bx)-b^3\pi x^3\operatorname{Erfi}(bx)^2+bx\left(e^{2b^2x^2}-4b^2x^2\operatorname{Ei}(2b^2x^2)\right)\right)}{3\sqrt{\pi}\,x^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[(E^(c + b^2*x^2)*Erfi[b*x])/x^4,x]
```

```
[Out] -1/3*(E^c*(E^(b^2*x^2)*Sqrt[Pi]*(1 + 2*b^2*x^2)*Erfi[b*x] - b^3*Pi*x^3*Erfi
[b*x]^2 + b*x*(E^(2*b^2*x^2) - 4*b^2*x^2*ExpIntegralEi[2*b^2*x^2])))/(Sqrt[
Pi]*x^3)
```

Maple [F]
time = 0.15, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{b^2x^2+c}\operatorname{erfi}(bx)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(b^2*x^2+c)*erfi(b*x)/x^4,x)
```

```
[Out] int(exp(b^2*x^2+c)*erfi(b*x)/x^4,x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)/x^4,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x)*e^(b^2*x^2 + c)/x^4, x)
```

Fricas [A]
time = 0.36, size = 85, normalized size = 0.72

$$-\frac{\left((\pi + 2\,\pi b^2x^2)\,\mathrm{erfi}\,(bx)\,e^{(b^2x^2)} - \sqrt{\pi}\,\left(\pi b^3x^3\,\mathrm{erfi}\,(bx)^2 + 4\,b^3x^3\mathrm{Ei}(2\,b^2x^2) - bxe^{(2\,b^2x^2)}\right)\right)e^c}{3\,\pi x^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)/x^4,x, algorithm="fricas")
```

```
[Out] -1/3*((pi + 2*pi*b^2*x^2)*erfi(b*x)*e^(b^2*x^2) - sqrt(pi)*(pi*b^3*x^3*erfi
(b*x)^2 + 4*b^3*x^3*Ei(2*b^2*x^2) - b*x*e^(2*b^2*x^2)))*e^c/(pi*x^3)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^c \int \frac{e^{b^2x^2}\,\mathrm{erfi}\,(bx)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b**2*x**2+c)*erfi(b*x)/x**4,x)
```

```
[Out] exp(c)*Integral(exp(b**2*x**2)*erfi(b*x)/x**4, x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(b^2*x^2+c)*erfi(b*x)/x^4,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)*e^(b^2*x^2 + c)/x^4, x)
```

Mupad [**F**]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{e}^{b^2\,x^2+c}\,\mathrm{erfi}(b\,x)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(c + b^2*x^2)*erfi(b*x))/x^4,x)
[Out] int((exp(c + b^2*x^2)*erfi(b*x))/x^4, x)
```

3.294 $\int e^{c+dx^2}x^3\mathbf{Erfi}(a+bx)\,dx$

Optimal. Leaf size=304

$$\frac{ab^2e^{a^2+c+2abx+(b^2+d)x^2}}{2d\left(b^2+d\right)^2\sqrt{\pi}}-\frac{be^{a^2+c+2abx+(b^2+d)x^2}x}{2d\left(b^2+d\right)\sqrt{\pi}}-\frac{e^{c+dx^2}\text{Erfi}(a+bx)}{2d^2}+\frac{e^{c+dx^2}x^2\text{Erfi}(a+bx)}{2d}-\frac{a^2b^3e^{c+\frac{a^2d}{b^2+d}}\text{Erfi}\left(\frac{ab}{\sqrt{}}\right.}{2d\left(b^2+d\right)^{5}}$$

```
[Out] -1/2*exp(d*x^2+c)*erfi(b*x+a)/d^2+1/2*exp(d*x^2+c)*x^2*erfi(b*x+a)/d-1/2*a^
2*b^3*exp(c+a^2*d/(b^2+d))*erfi((a*b+(b^2+d)*x)/(b^2+d)^(1/2))/d/(b^2+d)^(5
/2)+1/4*b*exp(c+a^2*d/(b^2+d))*erfi((a*b+(b^2+d)*x)/(b^2+d)^(1/2))/d/(b^2+d
)^(3/2)+1/2*b*exp(c+a^2*d/(b^2+d))*erfi((a*b+(b^2+d)*x)/(b^2+d)^(1/2))/d^2/
(b^2+d)^(1/2)+1/2*a*b^2*exp(a^2+c+2*a*b*x+(b^2+d)*x^2)/d/(b^2+d)^2/Pi^(1/2)
-1/2*b*exp(a^2+c+2*a*b*x+(b^2+d)*x^2)*x/d/(b^2+d)/Pi^(1/2)
```

Rubi [A]
time = 0.32, antiderivative size = 304, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 6, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.316$, Rules used = {6522, 6519, 2266, 2235, 2273, 2272}

$$\frac{be^{\frac{a^2d}{b^2+d}+c}\text{Erfi}\left(\frac{ab+x\left(b^2+d\right)}{\sqrt{b^2+d}}\right)}{2d^2\sqrt{b^2+d}}+\frac{be^{\frac{a^2d}{b^2+d}+c}\text{Erfi}\left(\frac{ab+x\left(b^2+d\right)}{\sqrt{b^2+d}}\right)}{4d\left(b^2+d\right)^{3/2}}+\frac{ab^2e^{a^2+2abx+x^2\left(b^2+d\right)+c}}{2\sqrt{\pi}\,d\left(b^2+d\right)^2}-\frac{bxe^{a^2+2abx+x^2\left(b^2+d\right)+c}}{2\sqrt{\pi}\,d\left(b^2+d\right)}-\frac{a^2b^3e^{\frac{a^2d}{b^2+d}+c}\text{Erfi}\left(\frac{ab+x\left(b^2+d\right)}{\sqrt{b^2+d}}\right)}{2d\left(b^2+d\right)^{5/2}}-\frac{e^{c+dx^2}\text{Erfi}(a+bx)}{2d^2}+\frac{x^2e^{c+dx^2}\text{Erfi}(a+bx)}{2d}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + d*x^2)*x^3*Erfi[a + b*x],x]
```

```
[Out] (a*b^2*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2))/(2*d*(b^2 + d)^2*Sqrt[Pi]) -
(b*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2)*x)/(2*d*(b^2 + d)*Sqrt[Pi]) - (E^(
c + d*x^2)*Erfi[a + b*x])/(2*d^2) + (E^(c + d*x^2)*x^2*Erfi[a + b*x])/(2*d)
 - (a^2*b^3*E^(c + (a^2*d)/(b^2 + d))*Erfi[(a*b + (b^2 + d)*x)/Sqrt[b^2 + d
]])/(2*d*(b^2 + d)^(5/2)) + (b*E^(c + (a^2*d)/(b^2 + d))*Erfi[(a*b + (b^2 +
 d)*x)/Sqrt[b^2 + d]])/(4*d*(b^2 + d)^(3/2)) + (b*E^(c + (a^2*d)/(b^2 + d))
*Erfi[(a*b + (b^2 + d)*x)/Sqrt[b^2 + d]])/(2*d^2*Sqrt[b^2 + d])
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 2272

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)*((d_.) + (e_.)*(x_)), x_Symbol
] :> Simp[e*(F^(a + b*x + c*x^2)/(2*c*Log[F])), x] - Dist[(b*e - 2*c*d)/(2*
c), Int[F^(a + b*x + c*x^2), x], x] /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[
b*e - 2*c*d, 0]
```

Rule 2273

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2)*((d_.) + (e_.)*(x_))^(m_), x_S
ymbol] :> Simp[e*(d + e*x)^(m - 1)*(F^(a + b*x + c*x^2)/(2*c*Log[F])), x] +
 (-Dist[(b*e - 2*c*d)/(2*c), Int[(d + e*x)^(m - 1)*F^(a + b*x + c*x^2), x],
 x] - Dist[(m - 1)*(e^2/(2*c*Log[F])), Int[(d + e*x)^(m - 2)*F^(a + b*x + c
*x^2), x], x]) /; FreeQ[{F, a, b, c, d, e}, x] && NeQ[b*e - 2*c*d, 0] && Gt
Q[m, 1]
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 6522

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m - 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] + (-Dist[(m - 1)/
(2*d), Int[x^(m - 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[b/(d*Sqrt[P
i]), Int[x^(m - 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x]) /; FreeQ[
{a, b, c, d}, x] && IGtQ[m, 1]
```

Rubi steps

$$\int e^{c+dx^2}x^3\text{erfi}(a+bx)\,dx = \frac{e^{c+dx^2}x^2\text{erfi}(a+bx)}{2d} - \frac{\int e^{c+dx^2}x\text{erfi}(a+bx)\,dx}{d} - \frac{b\int e^{a^2+c+2abx+(b^2+d)x^2}x^2\,dx}{d\sqrt{\pi}}$$

$$= -\frac{be^{a^2+c+2abx+(b^2+d)x^2}x}{2d(b^2+d)\sqrt{\pi}} - \frac{e^{c+dx^2}\text{erfi}(a+bx)}{2d^2} + \frac{e^{c+dx^2}x^2\text{erfi}(a+bx)}{2d} + \frac{b\int e^{a^2+c+}}{d}$$

$$= \frac{ab^2e^{a^2+c+2abx+(b^2+d)x^2}}{2d(b^2+d)^2\sqrt{\pi}} - \frac{be^{a^2+c+2abx+(b^2+d)x^2}x}{2d(b^2+d)\sqrt{\pi}} - \frac{e^{c+dx^2}\text{erfi}(a+bx)}{2d^2} + \frac{e^{c+dx^2}x^2\text{er}}{2}$$

$$= \frac{ab^2e^{a^2+c+2abx+(b^2+d)x^2}}{2d(b^2+d)^2\sqrt{\pi}} - \frac{be^{a^2+c+2abx+(b^2+d)x^2}x}{2d(b^2+d)\sqrt{\pi}} - \frac{e^{c+dx^2}\text{erfi}(a+bx)}{2d^2} + \frac{e^{c+dx^2}x^2\text{er}}{2}$$

$$= \frac{ab^2e^{a^2+c+2abx+(b^2+d)x^2}}{2d(b^2+d)^2\sqrt{\pi}} - \frac{be^{a^2+c+2abx+(b^2+d)x^2}x}{2d(b^2+d)\sqrt{\pi}} - \frac{e^{c+dx^2}\text{erfi}(a+bx)}{2d^2} + \frac{e^{c+dx^2}x^2\text{er}}{2}$$

Mathematica [A]
time = 1.48, size = 206, normalized size = 0.68

$$\frac{e^c\left(2e^{dx^2}(-1+dx^2)\,\text{Erfi}(a+bx)+\frac{2be^{\frac{a^2d}{b^2+d}}\text{Erfi}\left(\frac{ab+(b^2+d)x}{\sqrt{b^2+d}}\right)}{\sqrt{b^2+d}}-\frac{bde^{\frac{a^2d}{b^2+d}}\left(2(b^2+d)e^{\frac{(ab+(b^2+d)x)^2}{b^2+d}}(-ab+(b^2+d)x)+((-1+2a^2)b^2-d)\sqrt{b^2+d}\,\sqrt{\pi}\,\text{Erfi}\left(\frac{ab+(b^2+d)x}{\sqrt{b^2+d}}\right)\right)}{(b^2+d)^3\sqrt{\pi}}\right)}{4d^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + d*x^2)*x^3*Erfi[a + b*x],x]
```

```
[Out] (E^c*(2*E^(d*x^2)*(-1 + d*x^2)*Erfi[a + b*x] + (2*b*E^((a^2*d)/(b^2 + d))*E
rfi[(a*b + (b^2 + d)*x)/Sqrt[b^2 + d]])/Sqrt[b^2 + d] - (b*d*E^((a^2*d)/(b^
2 + d))*(2*(b^2 + d)*E^((a*b + (b^2 + d)*x)^2/(b^2 + d))*(-(a*b) + (b^2 + d
)*x) + ((-1 + 2*a^2)*b^2 - d)*Sqrt[b^2 + d]*Sqrt[Pi]*Erfi[(a*b + (b^2 + d)*
x)/Sqrt[b^2 + d]]))/((b^2 + d)^3*Sqrt[Pi])))/(4*d^2)
```

Maple [F]
time = 0.16, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^2+c}x^3\,\text{erfi}\left(bx+a\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^3*erfi(b*x+a),x)
```

```
[Out] int(exp(d*x^2+c)*x^3*erfi(b*x+a),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erfi(b*x+a),x, algorithm="maxima")
```

```
[Out] integrate(x^3*erfi(b*x + a)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.34, size = 262, normalized size = 0.86

$$-\frac{\pi(2\,b^5-(2\,a^2-5)b^3d+3\,bd^2)\sqrt{-b^2-d}\,\operatorname{erf}\left(\frac{(ab+(b^2+d)x)\sqrt{-b^2-d}}{b^2+d}\right)e^{\left(\frac{b^2c+(a^2+c)d}{b^2+d}\right)}-2\,(\pi(b^6d+3\,b^4d^2+3\,b^2d^3+d^4)x^2-\pi(b^6+3\,b^4d+3\,b^2d^2+d^3))\operatorname{erfi}(bx+a)\,e^{(dx^2+c)}-2\,\sqrt{\pi}\,(ab^4d+ab^2d^2-(b^5d+2\,b^3d^2+bd^3)x)e^{(b^2x^2+2\,abx+dx^2+a^2+c)}}{4\,\pi(b^6d^2+3\,b^4d^3+3\,b^2d^4+d^5)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erfi(b*x+a),x, algorithm="fricas")
```

```
[Out] -1/4*(pi*(2*b^5 - (2*a^2 - 5)*b^3*d + 3*b*d^2)*sqrt(-b^2 - d)*erf((a*b + (b
^2 + d)*x)*sqrt(-b^2 - d)/(b^2 + d))*e^((b^2*c + (a^2 + c)*d)/(b^2 + d)) -
2*(pi*(b^6*d + 3*b^4*d^2 + 3*b^2*d^3 + d^4)*x^2 - pi*(b^6 + 3*b^4*d + 3*b^2
*d^2 + d^3))*erfi(b*x + a)*e^(d*x^2 + c) - 2*sqrt(pi)*(a*b^4*d + a*b^2*d^2
- (b^5*d + 2*b^3*d^2 + b*d^3)*x)*e^(b^2*x^2 + 2*a*b*x + d*x^2 + a^2 + c))/(
pi*(b^6*d^2 + 3*b^4*d^3 + 3*b^2*d^4 + d^5))
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int x^{3}e^{dx^{2}}\operatorname{erfi}\left(a+bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**3*erfi(b*x+a),x)
```

```
[Out] exp(c)*Integral(x**3*exp(d*x**2)*erfi(a + b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^3*erfi(b*x+a),x, algorithm="giac")
```

```
[Out] integrate(x^3*erfi(b*x + a)*e^(d*x^2 + c), x)
```

Mupad [B]
time = 1.13, size = 336, normalized size = 1.11

$$\frac{\mathrm{erfi}\left(\frac{a\,b+x\,\left(b^2+d\right)}{\sqrt{b^2+d}}\right)\,\left(b^3\,\mathrm{e}^{\frac{c\,d}{b^2+d}+\frac{a^2\,d}{b^2+d}+\frac{b^2\,c}{b^2+d}}-2\,a^2\,b^3\,\mathrm{e}^{\frac{c\,d}{b^2+d}+\frac{a^2\,d}{b^2+d}+\frac{b^2\,c}{b^2+d}}+b\,d\,\mathrm{e}^{\frac{c\,d}{b^2+d}+\frac{a^2\,d}{b^2+d}+\frac{b^2\,c}{b^2+d}}\right)}{4\,d\,{\left(b^2+d\right)}^{5/2}}-\frac{\frac{b\,x\,\mathrm{e}^{a^2+2\,a\,b\,x+b^2\,x^2+d\,x^2+c}}{2\,\left(b^2+d\right)}-\frac{a\,b^2\,\mathrm{e}^{a^2+2\,a\,b\,x+b^2\,x^2+d\,x^2+c}}{2\,{\left(b^2+d\right)}^2}}{d\,\sqrt{\pi }}-\mathrm{erfi}\left(a+b\,x\right)\,\left(\frac{\mathrm{e}^{d\,x^2+c}}{2\,d^2}-\frac{x^2\,\mathrm{e}^{d\,x^2+c}}{2\,d}\right)-\frac{b\,\mathrm{e}^{c+a^2-\frac{a^2\,b^2}{b^2+d}}\,\mathrm{erf}\left(\frac{a\,b\,1{}\mathrm{i}+x\,\left(b^2+d\right)\,1{}\mathrm{i}}{\sqrt{b^2+d}}\right)\,1{}\mathrm{i}}{2\,d^2\,\sqrt{b^2+d}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*erfi(a + b*x)*exp(c + d*x^2),x)
```

```
[Out] (erfi((a*b + x*(d + b^2))/(d + b^2)^(1/2))*(b^3*exp((c*d)/(d + b^2) + (a^2*
d)/(d + b^2) + (b^2*c)/(d + b^2)) - 2*a^2*b^3*exp((c*d)/(d + b^2) + (a^2*d)
/(d + b^2) + (b^2*c)/(d + b^2)) + b*d*exp((c*d)/(d + b^2) + (a^2*d)/(d + b^
2) + (b^2*c)/(d + b^2))))/(4*d*(d + b^2)^(5/2)) - ((b*x*exp(c + d*x^2 + a^2
 + b^2*x^2 + 2*a*b*x))/(2*(d + b^2)) - (a*b^2*exp(c + d*x^2 + a^2 + b^2*x^2
 + 2*a*b*x))/(2*(d + b^2)^2))/(d*pi^(1/2)) - erfi(a + b*x)*(exp(c + d*x^2)/
(2*d^2) - (x^2*exp(c + d*x^2))/(2*d)) - (b*exp(c + a^2 - (a^2*b^2)/(d + b^2
))*erf((a*b*1i + x*(d + b^2)*1i)/(d + b^2)^(1/2))*1i)/(2*d^2*(d + b^2)^(1/2
))
```

3.295 $\int e^{c+dx^2} x \mathbf{Erfi}(a+bx)\, dx$

Optimal. Leaf size=78

$$\frac{e^{c+dx^2}\text{Erfi}(a+bx)}{2d}-\frac{be^{c+\frac{a^2d}{b^2+d}}\text{Erfi}\left(\frac{ab+(b^2+d)x}{\sqrt{b^2+d}}\right)}{2d\sqrt{b^2+d}}$$

```
[Out] 1/2*exp(d*x^2+c)*erfi(b*x+a)/d-1/2*b*exp(c+a^2*d/(b^2+d))*erfi((a*b+(b^2+d)
*x)/(b^2+d)^(1/2))/d/(b^2+d)^(1/2)
```

Rubi [A]

time = 0.04, antiderivative size = 78, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.176$, Rules used = {6519, 2266, 2235}

$$\frac{e^{c+dx^2}\text{Erfi}(a+bx)}{2d}-\frac{be^{\frac{a^2d}{b^2+d}+c}\text{Erfi}\left(\frac{ab+x(b^2+d)}{\sqrt{b^2+d}}\right)}{2d\sqrt{b^2+d}}$$

Antiderivative was successfully verified.

```
[In] Int[E^(c + d*x^2)*x*Erfi[a + b*x],x]
```

```
[Out] (E^(c + d*x^2)*Erfi[a + b*x])/(2*d) - (b*E^(c + (a^2*d)/(b^2 + d))*Erfi[(a*
b + (b^2 + d)*x)/Sqrt[b^2 + d]])/(2*d*Sqrt[b^2 + d])
```

Rule 2235

```
Int[(F_)^((a_.) + (b_.)*((c_.) + (d_.)*(x_))^2), x_Symbol] :> Simp[F^a*Sqrt
[Pi]*(Erfi[(c + d*x)*Rt[b*Log[F], 2]]/(2*d*Rt[b*Log[F], 2])), x] /; FreeQ[{
F, a, b, c, d}, x] && PosQ[b]
```

Rule 2266

```
Int[(F_)^((a_.) + (b_.)*(x_) + (c_.)*(x_)^2), x_Symbol] :> Dist[F^(a - b^2/
(4*c)), Int[F^((b + 2*c*x)^2/(4*c)), x], x] /; FreeQ[{F, a, b, c}, x]
```

Rule 6519

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_), x_Symbol] :> Si
mp[E^(c + d*x^2)*(Erfi[a + b*x]/(2*d)), x] - Dist[b/(d*Sqrt[Pi]), Int[E^(a^
2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\int e^{c+dx^2} x\text{erfi}(a+bx)\,dx = \frac{e^{c+dx^2}\text{erfi}(a+bx)}{2d} - \frac{b\int e^{a^2+c+2abx+(b^2+d)x^2}\,dx}{d\sqrt{\pi}}$$
$$= \frac{e^{c+dx^2}\text{erfi}(a+bx)}{2d} - \frac{\left(be^{c+\frac{a^2d}{b^2+d}}\right)\int e^{\frac{\left(2ab+2\left(b^2+d\right)x\right)^2}{4\left(b^2+d\right)}}\,dx}{d\sqrt{\pi}}$$
$$= \frac{e^{c+dx^2}\text{erfi}(a+bx)}{2d} - \frac{be^{c+\frac{a^2d}{b^2+d}}\text{erfi}\left(\frac{ab+(b^2+d)x}{\sqrt{b^2+d}}\right)}{2d\sqrt{b^2+d}}$$

Mathematica [A]
time = 0.05, size = 73, normalized size = 0.94

$$\frac{e^c\left(e^{dx^2}\text{Erfi}(a+bx) - \frac{be^{\frac{a^2d}{b^2+d}}\text{Erfi}\left(\frac{ab+\left(b^2+d\right)x}{\sqrt{b^2+d}}\right)}{\sqrt{b^2+d}}\right)}{2d}$$

Antiderivative was successfully verified.

```
[In] Integrate[E^(c + d*x^2)*x*Erfi[a + b*x],x]
[Out] (E^c*(E^(d*x^2)*Erfi[a + b*x] - (b*E^((a^2*d)/(b^2 + d))*Erfi[(a*b + (b^2 +
 d)*x)/Sqrt[b^2 + d]])/Sqrt[b^2 + d]))/(2*d)
```

Maple [F]
time = 0.15, size = 0, normalized size = 0.00

$$\int e^{d\,x^2+c} x\,\text{erfi}\,(bx+a)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x*erfi(b*x+a),x)
[Out] int(exp(d*x^2+c)*x*erfi(b*x+a),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erfi(b*x+a),x, algorithm="maxima")
```

```
[Out] integrate(x*erfi(b*x + a)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.37, size = 100, normalized size = 1.28

$$\frac{\sqrt{-b^2-d}\,b\operatorname{erf}\left(\frac{(ab+(b^2+d)x)\sqrt{-b^2-d}}{b^2+d}\right)e^{\left(\frac{b^2c+(a^2+c)d}{b^2+d}\right)}+(b^2+d)\operatorname{erfi}(bx+a)\,e^{(dx^2+c)}}{2\,(b^2d+d^2)}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erfi(b*x+a),x, algorithm="fricas")
```

```
[Out] 1/2*(sqrt(-b^2 - d)*b*erf((a*b + (b^2 + d)*x)*sqrt(-b^2 - d)/(b^2 + d))*e^(
(b^2*c + (a^2 + c)*d)/(b^2 + d)) + (b^2 + d)*erfi(b*x + a)*e^(d*x^2 + c))/(
b^2*d + d^2)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$e^c\int xe^{dx^2}\operatorname{erfi}(a+bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x*erfi(b*x+a),x)
```

```
[Out] exp(c)*Integral(x*exp(d*x**2)*erfi(a + b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x*erfi(b*x+a),x, algorithm="giac")
```

```
[Out] integrate(x*erfi(b*x + a)*e^(d*x^2 + c), x)
```

Mupad [B]
time = 0.25, size = 79, normalized size = 1.01

$$\frac{\operatorname{erfi}(a+b\,x)\;\mathrm{e}^{d\,x^2+c}}{2\,d}+\frac{b\,\mathrm{e}^{c+a^2-\frac{a^2\,b^2}{b^2+d}}\,\operatorname{erf}\left(\frac{a\,b\,1\mathrm{i}+x\,\left(b^2+d\right)\,1\mathrm{i}}{\sqrt{b^2+d}}\right)\,1\mathrm{i}}{2\,d\,\sqrt{b^2+d}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*erfi(a + b*x)*exp(c + d*x^2),x)
```

```
[Out] (erfi(a + b*x)*exp(c + d*x^2))/(2*d) + (b*exp(c + a^2 - (a^2*b^2)/(d + b^2)
)*erf((a*b*1i + x*(d + b^2)*1i)/(d + b^2)^(1/2))*1i)/(2*d*(d + b^2)^(1/2))
```

3.296 $\int \frac{e^{c+dx^2}\mathbf{Erfi}(a+bx)}{x}\,dx$

Optimal. Leaf size=22

$$\mathrm{Int}\left(\frac{e^{c+dx^2}\mathrm{Erfi}(a+bx)}{x},x\right)$$

```
[Out] Unintegrable(exp(d*x^2+c)*erfi(b*x+a)/x,x)
```

Rubi [A]
time = 0.02, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\mathrm{Erfi}(a+bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfi[a + b*x])/x,x]
[Out] Defer[Int][(E^(c + d*x^2)*Erfi[a + b*x])/x, x]
```

Rubi steps

$$\int \frac{e^{c+dx^2}\mathrm{erfi}(a+bx)}{x}\,dx = \int \frac{e^{c+dx^2}\mathrm{erfi}(a+bx)}{x}\,dx$$

Mathematica [A]
time = 0.13, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\mathrm{Erfi}(a+bx)}{x}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfi[a + b*x])/x,x]
[Out] Integrate[(E^(c + d*x^2)*Erfi[a + b*x])/x, x]
```

Maple [A]
time = 0.05, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\,\mathrm{erfi}\,(bx+a)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfi(b*x+a)/x,x)
```

```
[Out] int(exp(d*x^2+c)*erfi(b*x+a)/x,x)
```

Maxima [**A**]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x+a)/x,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x + a)*e^(d*x^2 + c)/x, x)
```

Fricas [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x+a)/x,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x + a)*e^(d*x^2 + c)/x, x)
```

Sympy [**A**]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^{2}}\operatorname{erfi}\left(a+bx\right)}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfi(b*x+a)/x,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erfi(a + b*x)/x, x)
```

Giac [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x+a)/x,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x + a)*e^(d*x^2 + c)/x, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \frac{\mathrm{erfi}(a+b\,x)\,\,\mathrm{e}^{d\,x^2+c}}{x}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((erfi(a + b*x)*exp(c + d*x^2))/x,x)
[Out] int((erfi(a + b*x)*exp(c + d*x^2))/x, x)
```

3.297 $\int \frac{e^{c+dx^2}\text{Erfi}(a+bx)}{x^3}\,dx$

Optimal. Leaf size=167

$$-\frac{be^{a^2+c+2abx+(b^2+d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\text{Erfi}(a+bx)}{2x^2}+b\sqrt{b^2+d}\,e^{c+\frac{a^2d}{b^2+d}}\text{Erfi}\left(\frac{ab+(b^2+d)\,x}{\sqrt{b^2+d}}\right)+\frac{2ab^2\text{Int}\left(\frac{e^{a^2+c+2abx+(b^2\cdots}}{x}\right.}{\sqrt{\pi}}$$

```
[Out] -1/2*exp(d*x^2+c)*erfi(b*x+a)/x^2+b*exp(c+a^2*d/(b^2+d))*erfi((a*b+(b^2+d)*
x)/(b^2+d)^(1/2))*(b^2+d)^(1/2)-b*exp(a^2+c+2*a*b*x+(b^2+d)*x^2)/x/Pi^(1/2)
+2*a*b^2*Unintegrable(exp(a^2+c+2*a*b*x+(b^2+d)*x^2)/x,x)/Pi^(1/2)+d*Uninte
grable(exp(d*x^2+c)*erfi(b*x+a)/x,x)
```

Rubi [A]
time = 0.26, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\text{Erfi}(a+bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfi[a + b*x])/x^3,x]
```

```
[Out] -((b*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2))/(Sqrt[Pi]*x)) - (E^(c + d*x^2)*
Erfi[a + b*x])/(2*x^2) + b*Sqrt[b^2 + d]*E^(c + (a^2*d)/(b^2 + d))*Erfi[(a*
b + (b^2 + d)*x)/Sqrt[b^2 + d]] + (2*a*b^2*Defer[Int][E^(a^2 + c + 2*a*b*x
+ (b^2 + d)*x^2)/x, x])/Sqrt[Pi] + d*Defer[Int][(E^(c + d*x^2)*Erfi[a + b*x
])/x, x]
```

Rubi steps

$$\begin{aligned}
\int \frac{e^{c+dx^2}\text{erfi}(a+bx)}{x^3}\,dx &= -\frac{e^{c+dx^2}\text{erfi}(a+bx)}{2x^2}+d\int \frac{e^{c+dx^2}\text{erfi}(a+bx)}{x}\,dx+\frac{b\int \frac{e^{a^2+c+2abx+(b^2+d)x^2}}{x^2}\,dx}{\sqrt{\pi}}\\
&= -\frac{be^{a^2+c+2abx+(b^2+d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\text{erfi}(a+bx)}{2x^2}+d\int \frac{e^{c+dx^2}\text{erfi}(a+bx)}{x}\,dx+\frac{(2ab^2)\cdots}{}\\
&= -\frac{be^{a^2+c+2abx+(b^2+d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\text{erfi}(a+bx)}{2x^2}+d\int \frac{e^{c+dx^2}\text{erfi}(a+bx)}{x}\,dx+\frac{(2ab^2)\cdots}{}\\
&= -\frac{be^{a^2+c+2abx+(b^2+d)x^2}}{\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\text{erfi}(a+bx)}{2x^2}+b\sqrt{b^2+d}\,e^{c+\frac{a^2d}{b^2+d}}\text{erfi}\left(\frac{ab+(b^2+d\cdots}{\sqrt{b^2+d}}\right.
\end{aligned}$$

Mathematica [A]
time = 0.22, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\text{Erfi}(a+bx)}{x^3}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfi[a + b*x])/x^3,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erfi[a + b*x])/x^3, x]
```

Maple [A]
time = 0.18, size = 0, normalized size = 0.00

$$\int \frac{e^{d\,x^2+c}\,\text{erfi}\left(bx+a\right)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfi(b*x+a)/x^3,x)
```

```
[Out] int(exp(d*x^2+c)*erfi(b*x+a)/x^3,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x+a)/x^3,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x + a)*e^(d*x^2 + c)/x^3, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x+a)/x^3,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x + a)*e^(d*x^2 + c)/x^3, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^2}\,\text{erfi}\left(a+bx\right)}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfi(b*x+a)/x**3,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erfi(a + b*x)/x**3, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x+a)/x^3,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x + a)*e^(d*x^2 + c)/x^3, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erfi}(a+b\,x)\;\mathrm{e}^{d\,x^2+c}}{x^3}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((erfi(a + b*x)*exp(c + d*x^2))/x^3,x)
```

```
[Out] int((erfi(a + b*x)*exp(c + d*x^2))/x^3, x)
```

3.298 $\int e^{c+dx^2}x^4\mathbf{Erfi}(a+bx)\,dx$

Optimal. Leaf size=468

$$-\frac{a^2b^3e^{a^2+c+2abx+(b^2+d)x^2}}{2d\,(b^2+d)^3\sqrt{\pi}}+\frac{be^{a^2+c+2abx+(b^2+d)x^2}}{2d\,(b^2+d)^2\sqrt{\pi}}+\frac{3be^{a^2+c+2abx+(b^2+d)x^2}}{4d^2\,(b^2+d)\sqrt{\pi}}+\frac{ab^2e^{a^2+c+2abx+(b^2+d)x^2}x}{2d\,(b^2+d)^2\sqrt{\pi}}-\frac{be^{a^2+c+2abx+(}}{2d\,(b^2+d}$$

```
[Out] -3/4*exp(d*x^2+c)*x*erfi(b*x+a)/d^2+1/2*exp(d*x^2+c)*x^3*erfi(b*x+a)/d+1/2*
a^3*b^4*exp(c+a^2*d/(b^2+d))*erfi((a*b+(b^2+d)*x)/(b^2+d)^(1/2))/d/(b^2+d)^
(7/2)-3/4*a*b^2*exp(c+a^2*d/(b^2+d))*erfi((a*b+(b^2+d)*x)/(b^2+d)^(1/2))/d/
(b^2+d)^(5/2)-3/4*a*b^2*exp(c+a^2*d/(b^2+d))*erfi((a*b+(b^2+d)*x)/(b^2+d)^(
1/2))/d^2/(b^2+d)^(3/2)-1/2*a^2*b^3*exp(a^2+c+2*a*b*x+(b^2+d)*x^2)/d/(b^2+d
)^3/Pi^(1/2)+1/2*b*exp(a^2+c+2*a*b*x+(b^2+d)*x^2)/d/(b^2+d)^2/Pi^(1/2)+3/4*
b*exp(a^2+c+2*a*b*x+(b^2+d)*x^2)/d^2/(b^2+d)/Pi^(1/2)+1/2*a*b^2*exp(a^2+c+2
*a*b*x+(b^2+d)*x^2)*x/d/(b^2+d)^2/Pi^(1/2)-1/2*b*exp(a^2+c+2*a*b*x+(b^2+d)*
x^2)*x^2/d/(b^2+d)/Pi^(1/2)+3/4*Unintegrable(exp(d*x^2+c)*erfi(b*x+a),x)/d^
2
```

Rubi [A]
time = 0.62, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int e^{c+dx^2}x^4\text{Erfi}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*x^4*Erfi[a + b*x],x]
```

```
[Out] -1/2*(a^2*b^3*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2))/(d*(b^2 + d)^3*Sqrt[Pi
]) + (b*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2))/(2*d*(b^2 + d)^2*Sqrt[Pi]) +
 (3*b*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2))/(4*d^2*(b^2 + d)*Sqrt[Pi]) + (
a*b^2*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2)*x)/(2*d*(b^2 + d)^2*Sqrt[Pi]) -
 (b*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2)*x^2)/(2*d*(b^2 + d)*Sqrt[Pi]) - (
3*E^(c + d*x^2)*x*Erfi[a + b*x])/(4*d^2) + (E^(c + d*x^2)*x^3*Erfi[a + b*x]
)/(2*d) + (a^3*b^4*E^(c + (a^2*d)/(b^2 + d))*Erfi[(a*b + (b^2 + d)*x)/Sqrt[
b^2 + d]])/(2*d*(b^2 + d)^(7/2)) - (3*a*b^2*E^(c + (a^2*d)/(b^2 + d))*Erfi[
(a*b + (b^2 + d)*x)/Sqrt[b^2 + d]])/(4*d*(b^2 + d)^(5/2)) - (3*a*b^2*E^(c +
 (a^2*d)/(b^2 + d))*Erfi[(a*b + (b^2 + d)*x)/Sqrt[b^2 + d]])/(4*d^2*(b^2 +
d)^(3/2)) + (3*Defer[Int][E^(c + d*x^2)*Erfi[a + b*x], x])/(4*d^2)
```

Rubi steps

$$\int e^{c+dx^2}x^4\text{erfi}(a+bx)\,dx = \frac{e^{c+dx^2}x^3\text{erfi}(a+bx)}{2d} - \frac{3\int e^{c+dx^2}x^2\text{erfi}(a+bx)\,dx}{2d} - \frac{b\int e^{a^2+c+2abx+(b^2+d)x^2}x^3\,d}{d\sqrt{\pi}}$$

$$= -\frac{be^{a^2+c+2abx+(b^2+d)x^2}x^2}{2d(b^2+d)\sqrt{\pi}} - \frac{3e^{c+dx^2}x\text{erfi}(a+bx)}{4d^2} + \frac{e^{c+dx^2}x^3\text{erfi}(a+bx)}{2d} + \frac{3\int e^{}}{}$$

$$= \frac{be^{a^2+c+2abx+(b^2+d)x^2}}{2d(b^2+d)^2\sqrt{\pi}} + \frac{3be^{a^2+c+2abx+(b^2+d)x^2}}{4d^2(b^2+d)\sqrt{\pi}} + \frac{ab^2e^{a^2+c+2abx+(b^2+d)x^2}x}{2d(b^2+d)^2\sqrt{\pi}} - \frac{be^{a^2+c}}{2d}$$

$$= -\frac{a^2b^3e^{a^2+c+2abx+(b^2+d)x^2}}{2d(b^2+d)^3\sqrt{\pi}} + \frac{be^{a^2+c+2abx+(b^2+d)x^2}}{2d(b^2+d)^2\sqrt{\pi}} + \frac{3be^{a^2+c+2abx+(b^2+d)x^2}}{4d^2(b^2+d)\sqrt{\pi}} + \frac{ab^2e}{2}$$

$$= -\frac{a^2b^3e^{a^2+c+2abx+(b^2+d)x^2}}{2d(b^2+d)^3\sqrt{\pi}} + \frac{be^{a^2+c+2abx+(b^2+d)x^2}}{2d(b^2+d)^2\sqrt{\pi}} + \frac{3be^{a^2+c+2abx+(b^2+d)x^2}}{4d^2(b^2+d)\sqrt{\pi}} + \frac{ab^2e}{2}$$

$$= -\frac{a^2b^3e^{a^2+c+2abx+(b^2+d)x^2}}{2d(b^2+d)^3\sqrt{\pi}} + \frac{be^{a^2+c+2abx+(b^2+d)x^2}}{2d(b^2+d)^2\sqrt{\pi}} + \frac{3be^{a^2+c+2abx+(b^2+d)x^2}}{4d^2(b^2+d)\sqrt{\pi}} + \frac{ab^2e}{2}$$

Mathematica [A]
time = 0.35, size = 0, normalized size = 0.00

$$\int e^{c+dx^2}x^4\text{Erfi}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*x^4*Erfi[a + b*x],x]
[Out] Integrate[E^(c + d*x^2)*x^4*Erfi[a + b*x], x]
```

Maple [A]
time = 0.06, size = 0, normalized size = 0.00

$$\int e^{d\,x^2+c}x^4\,\text{erfi}\left(bx+a\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^4*erfi(b*x+a),x)
[Out] int(exp(d*x^2+c)*x^4*erfi(b*x+a),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erfi(b*x+a),x, algorithm="maxima")
```

```
[Out] integrate(x^4*erfi(b*x + a)*e^(d*x^2 + c), x)
```

Fricas [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erfi(b*x+a),x, algorithm="fricas")
```

```
[Out] integral(x^4*erfi(b*x + a)*e^(d*x^2 + c), x)
```

Sympy [**F(-1)**] Timed out
time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**4*erfi(b*x+a),x)
```

```
[Out] Timed out
```

Giac [**A**]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^4*erfi(b*x+a),x, algorithm="giac")
```

```
[Out] integrate(x^4*erfi(b*x + a)*e^(d*x^2 + c), x)
```

Mupad [**A**]
time = 0.00, size = -1, normalized size = -0.00

$$\int x^4\,\mathrm{erfi}(a+b\,x)\,\mathrm{e}^{d\,x^2+c}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^4*erfi(a + b*x)*exp(c + d*x^2),x)
```

```
[Out] int(x^4*erfi(a + b*x)*exp(c + d*x^2), x)
```

3.299 $\int e^{c+dx^2} x^2 \mathbf{Erfi}(a+bx)\,dx$

Optimal. Leaf size=149

$$-\frac{be^{a^2+c+2abx+(b^2+d)x^2}}{2d(b^2+d)\sqrt{\pi}}+\frac{e^{c+dx^2}x\mathrm{Erfi}(a+bx)}{2d}+\frac{ab^2e^{c+\frac{a^2d}{b^2+d}}\mathrm{Erfi}\left(\frac{ab+(b^2+d)x}{\sqrt{b^2+d}}\right)}{2d(b^2+d)^{3/2}}-\frac{\mathrm{Int}\left(e^{c+dx^2}\mathrm{Erfi}(a+bx),x\right)}{2d}$$

```
[Out] 1/2*exp(d*x^2+c)*x*erfi(b*x+a)/d+1/2*a*b^2*exp(c+a^2*d/(b^2+d))*erfi((a*b+(
b^2+d)*x)/(b^2+d)^(1/2))/d/(b^2+d)^(3/2)-1/2*b*exp(a^2+c+2*a*b*x+(b^2+d)*x^
2)/d/(b^2+d)/Pi^(1/2)-1/2*Unintegrable(exp(d*x^2+c)*erfi(b*x+a),x)/d
```

Rubi [A]
time = 0.12, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int e^{c+dx^2}x^2\mathrm{Erfi}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*x^2*Erfi[a + b*x],x]
```

```
[Out] -1/2*(b*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2))/(d*(b^2 + d)*Sqrt[Pi]) + (E^
(c + d*x^2)*x*Erfi[a + b*x])/(2*d) + (a*b^2*E^(c + (a^2*d)/(b^2 + d))*Erfi[
(a*b + (b^2 + d)*x)/Sqrt[b^2 + d]])/(2*d*(b^2 + d)^(3/2)) - Defer[Int][E^(c
 + d*x^2)*Erfi[a + b*x], x]/(2*d)
```

Rubi steps

$$\begin{aligned}\int e^{c+dx^2}x^2\mathrm{erfi}(a+bx)\,dx &= \frac{e^{c+dx^2}x\mathrm{erfi}(a+bx)}{2d}-\frac{\int e^{c+dx^2}\mathrm{erfi}(a+bx)\,dx}{2d}-\frac{b\int e^{a^2+c+2abx+(b^2+d)x^2}x\,dx}{d\sqrt{\pi}}\\ &= -\frac{be^{a^2+c+2abx+(b^2+d)x^2}}{2d(b^2+d)\sqrt{\pi}}+\frac{e^{c+dx^2}x\mathrm{erfi}(a+bx)}{2d}-\frac{\int e^{c+dx^2}\mathrm{erfi}(a+bx)\,dx}{2d}+\frac{(ab^2)}{}\\ &= -\frac{be^{a^2+c+2abx+(b^2+d)x^2}}{2d(b^2+d)\sqrt{\pi}}+\frac{e^{c+dx^2}x\mathrm{erfi}(a+bx)}{2d}-\frac{\int e^{c+dx^2}\mathrm{erfi}(a+bx)\,dx}{2d}+\frac{\left(ab^2e\right.}{}\\ &= -\frac{be^{a^2+c+2abx+(b^2+d)x^2}}{2d(b^2+d)\sqrt{\pi}}+\frac{e^{c+dx^2}x\mathrm{erfi}(a+bx)}{2d}+\frac{ab^2e^{c+\frac{a^2d}{b^2+d}}\mathrm{erfi}\left(\frac{ab+(b^2+d)x}{\sqrt{b^2+d}}\right)}{2d(b^2+d)^{3/2}}-\int\end{aligned}$$

Mathematica [A]
time = 0.26, size = 0, normalized size = 0.00

$$\int e^{c+dx^2}x^2\mathrm{Erfi}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*x^2*Erfi[a + b*x],x]
[Out] Integrate[E^(c + d*x^2)*x^2*Erfi[a + b*x], x]
```

Maple [A]
time = 0.13, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^2+c}x^2\,\mathrm{erfi}\left(bx+a\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*x^2*erfi(b*x+a),x)
[Out] int(exp(d*x^2+c)*x^2*erfi(b*x+a),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erfi(b*x+a),x, algorithm="maxima")
[Out] integrate(x^2*erfi(b*x + a)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erfi(b*x+a),x, algorithm="fricas")
[Out] integral(x^2*erfi(b*x + a)*e^(d*x^2 + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int x^{2}e^{dx^{2}}\,\mathrm{erfi}\left(a+bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*x**2*erfi(b*x+a),x)
```

```
[Out] exp(c)*Integral(x**2*exp(d*x**2)*erfi(a + b*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*x^2*erfi(b*x+a),x, algorithm="giac")
```

```
[Out] integrate(x^2*erfi(b*x + a)*e^(d*x^2 + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int x^2\,\mathrm{erfi}(a+b\,x)\;\mathrm{e}^{d\,x^2+c}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*erfi(a + b*x)*exp(c + d*x^2),x)
```

```
[Out] int(x^2*erfi(a + b*x)*exp(c + d*x^2), x)
```

3.300 $\int e^{c+dx^2}\mathbf{Erfi}(a+bx)\,dx$

Optimal. Leaf size=19

$$\mathrm{Int}\left(e^{c+dx^2}\mathrm{Erfi}(a+bx),x\right)$$

```
[Out] Unintegrable(exp(d*x^2+c)*erfi(b*x+a),x)
```

Rubi [A]
time = 0.01, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int e^{c+dx^2}\mathrm{Erfi}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Int[E^(c + d*x^2)*Erfi[a + b*x],x]
[Out] Defer[Int][E^(c + d*x^2)*Erfi[a + b*x], x]
```

Rubi steps

$$\int e^{c+dx^2}\mathrm{erfi}(a+bx)\,dx = \int e^{c+dx^2}\mathrm{erfi}(a+bx)\,dx$$

Mathematica [A]
time = 0.03, size = 0, normalized size = 0.00

$$\int e^{c+dx^2}\mathrm{Erfi}(a+bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[E^(c + d*x^2)*Erfi[a + b*x],x]
[Out] Integrate[E^(c + d*x^2)*Erfi[a + b*x], x]
```

Maple [A]
time = 0.06, size = 0, normalized size = 0.00

$$\int \mathrm{e}^{d\,x^2+c}\,\mathrm{erfi}\left(bx+a\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfi(b*x+a),x)
[Out] int(exp(d*x^2+c)*erfi(b*x+a),x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x+a),x, algorithm="maxima")
[Out] integrate(erfi(b*x + a)*e^(d*x^2 + c), x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x+a),x, algorithm="fricas")
[Out] integral(erfi(b*x + a)*e^(d*x^2 + c), x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int e^{dx^{2}}\operatorname{erfi}\left(a+bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfi(b*x+a),x)
[Out] exp(c)*Integral(exp(d*x**2)*erfi(a + b*x), x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x+a),x, algorithm="giac")
[Out] integrate(erfi(b*x + a)*e^(d*x^2 + c), x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.05

$$\int \mathrm{erfi}(a+b\,x)\,\mathrm{e}^{d\,x^2+c}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(a + b*x)*exp(c + d*x^2),x)
[Out] int(erfi(a + b*x)*exp(c + d*x^2), x)
```

3.301 $\int \frac{e^{c+dx^2}\textbf{Erfi}(a+bx)}{x^2}\,dx$

Optimal. Leaf size=79

$$-\frac{e^{c+dx^2}\mathrm{Erfi}(a+bx)}{x}+\frac{2b\mathrm{Int}\left(\frac{e^{a^2+c+2abx+\left(b^2+d\right)x^2}}{x},x\right)}{\sqrt{\pi}}+2d\mathrm{Int}\left(e^{c+dx^2}\mathrm{Erfi}(a+bx),x\right)$$

```
[Out] -exp(d*x^2+c)*erfi(b*x+a)/x+2*b*Unintegrable(exp(a^2+c+2*a*b*x+(b^2+d)*x^2)
/x,x)/Pi^(1/2)+2*d*Unintegrable(exp(d*x^2+c)*erfi(b*x+a),x)
```

Rubi [A]
time = 0.14, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\mathrm{Erfi}(a+bx)}{x^2}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfi[a + b*x])/x^2,x]
```

```
[Out] -((E^(c + d*x^2)*Erfi[a + b*x])/x) + (2*b*Defer[Int][E^(a^2 + c + 2*a*b*x +
 (b^2 + d)*x^2)/x, x])/Sqrt[Pi] + 2*d*Defer[Int][E^(c + d*x^2)*Erfi[a + b*x
], x]
```

Rubi steps

$$\int \frac{e^{c+dx^2}\mathrm{erfi}(a+bx)}{x^2}\,dx=-\frac{e^{c+dx^2}\mathrm{erfi}(a+bx)}{x}+(2d)\int e^{c+dx^2}\mathrm{erfi}(a+bx)\,dx+\frac{(2b)\int \frac{e^{a^2+c+2abx+\left(b^2+d\right)x^2}}{x}\,dx}{\sqrt{\pi}}$$

Mathematica [A]
time = 0.24, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\mathrm{Erfi}(a+bx)}{x^2}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfi[a + b*x])/x^2,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erfi[a + b*x])/x^2, x]
```

Maple [A]
time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{\mathrm{e}^{d\,x^2+c}\,\mathrm{erfi}\left(bx+a\right)}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfi(b*x+a)/x^2,x)
```

```
[Out] int(exp(d*x^2+c)*erfi(b*x+a)/x^2,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x+a)/x^2,x, algorithm="maxima")
```

```
[Out] integrate(erfi(b*x + a)*e^(d*x^2 + c)/x^2, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x+a)/x^2,x, algorithm="fricas")
```

```
[Out] integral(erfi(b*x + a)*e^(d*x^2 + c)/x^2, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^{2}}\,\mathrm{erfi}\left(a+bx\right)}{x^{2}}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfi(b*x+a)/x**2,x)
```

```
[Out] exp(c)*Integral(exp(d*x**2)*erfi(a + b*x)/x**2, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x+a)/x^2,x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x + a)*e^(d*x^2 + c)/x^2, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{\mathrm{erfi}(a+b\,x)\,\mathrm{e}^{d\,x^2+c}}{x^2}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((erfi(a + b*x)*exp(c + d*x^2))/x^2,x)
```

```
[Out] int((erfi(a + b*x)*exp(c + d*x^2))/x^2, x)
```

3.302 $\int \frac{e^{c+dx^2}\mathbf{Erfi}(a+bx)}{x^4}\,dx$

Optimal. Leaf size=323

$$-\frac{be^{a^2+c+2abx+(b^2+d)x^2}}{3\sqrt{\pi}\,x^2}-\frac{2ab^2e^{a^2+c+2abx+(b^2+d)x^2}}{3\sqrt{\pi}\,x}-\frac{e^{c+dx^2}\mathrm{Erfi}(a+bx)}{3x^3}-\frac{2de^{c+dx^2}\mathrm{Erfi}(a+bx)}{3x}+\frac{2}{3}ab^2\sqrt{b^2+d}\,e^{c+}$$

```
[Out] -1/3*exp(d*x^2+c)*erfi(b*x+a)/x^3-2/3*d*exp(d*x^2+c)*erfi(b*x+a)/x+2/3*a*b^
2*exp(c+a^2*d/(b^2+d))*erfi((a*b+(b^2+d)*x)/(b^2+d)^(1/2))*(b^2+d)^(1/2)-1/
3*b*exp(a^2+c+2*a*b*x+(b^2+d)*x^2)/x^2/Pi^(1/2)-2/3*a*b^2*exp(a^2+c+2*a*b*x
+(b^2+d)*x^2)/x/Pi^(1/2)+4/3*a^2*b^3*Unintegrable(exp(a^2+c+2*a*b*x+(b^2+d)
*x^2)/x,x)/Pi^(1/2)+4/3*b*d*Unintegrable(exp(a^2+c+2*a*b*x+(b^2+d)*x^2)/x,x
)/Pi^(1/2)+2/3*b*(b^2+d)*Unintegrable(exp(a^2+c+2*a*b*x+(b^2+d)*x^2)/x,x)/P
i^(1/2)+4/3*d^2*Unintegrable(exp(d*x^2+c)*erfi(b*x+a),x)
```

Rubi [A]
time = 0.58, antiderivative size = 0, normalized size of antiderivative = 0.00, number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.000$, Rules used = {}

$$\int \frac{e^{c+dx^2}\mathrm{Erfi}(a+bx)}{x^4}\,dx$$

Verification is not applicable to the result.

```
[In] Int[(E^(c + d*x^2)*Erfi[a + b*x])/x^4,x]
```

```
[Out] -1/3*(b*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2))/(Sqrt[Pi]*x^2) - (2*a*b^2*E^
(a^2 + c + 2*a*b*x + (b^2 + d)*x^2))/(3*Sqrt[Pi]*x) - (E^(c + d*x^2)*Erfi[a
 + b*x])/(3*x^3) - (2*d*E^(c + d*x^2)*Erfi[a + b*x])/(3*x) + (2*a*b^2*Sqrt[
b^2 + d]*E^(c + (a^2*d)/(b^2 + d))*Erfi[(a*b + (b^2 + d)*x)/Sqrt[b^2 + d]])
/3 + (4*a^2*b^3*Defer[Int][E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2)/x, x])/(3*
Sqrt[Pi]) + (4*b*d*Defer[Int][E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2)/x, x])/
(3*Sqrt[Pi]) + (2*b*(b^2 + d)*Defer[Int][E^(a^2 + c + 2*a*b*x + (b^2 + d)*x
^2)/x, x])/(3*Sqrt[Pi]) + (4*d^2*Defer[Int][E^(c + d*x^2)*Erfi[a + b*x], x]
)/3
```

Rubi steps

$$\int \frac{e^{c+dx^2}\text{erfi}(a+bx)}{x^4}\,dx = -\frac{e^{c+dx^2}\text{erfi}(a+bx)}{3x^3} + \frac{1}{3}(2d)\int \frac{e^{c+dx^2}\text{erfi}(a+bx)}{x^2}\,dx + \frac{(2b)\int \frac{e^{a^2+c+2abx+\left(b^2+d\right)x^2}}{x^3}}{3\sqrt{\pi}}$$

$$= -\frac{be^{a^2+c+2abx+\left(b^2+d\right)x^2}}{3\sqrt{\pi}\,x^2} - \frac{e^{c+dx^2}\text{erfi}(a+bx)}{3x^3} - \frac{2de^{c+dx^2}\text{erfi}(a+bx)}{3x} + \frac{1}{3}\left(4d^2\right)\int e$$

$$= -\frac{be^{a^2+c+2abx+\left(b^2+d\right)x^2}}{3\sqrt{\pi}\,x^2} - \frac{2ab^2e^{a^2+c+2abx+\left(b^2+d\right)x^2}}{3\sqrt{\pi}\,x} - \frac{e^{c+dx^2}\text{erfi}(a+bx)}{3x^3} - \frac{2de^{c+dx^2}}{}$$

$$= -\frac{be^{a^2+c+2abx+\left(b^2+d\right)x^2}}{3\sqrt{\pi}\,x^2} - \frac{2ab^2e^{a^2+c+2abx+\left(b^2+d\right)x^2}}{3\sqrt{\pi}\,x} - \frac{e^{c+dx^2}\text{erfi}(a+bx)}{3x^3} - \frac{2de^{c+dx^2}}{}$$

$$= -\frac{be^{a^2+c+2abx+\left(b^2+d\right)x^2}}{3\sqrt{\pi}\,x^2} - \frac{2ab^2e^{a^2+c+2abx+\left(b^2+d\right)x^2}}{3\sqrt{\pi}\,x} - \frac{e^{c+dx^2}\text{erfi}(a+bx)}{3x^3} - \frac{2de^{c+dx^2}}{}$$

Mathematica [A]
time = 0.33, size = 0, normalized size = 0.00

$$\int \frac{e^{c+dx^2}\text{Erfi}(a+bx)}{x^4}\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[(E^(c + d*x^2)*Erfi[a + b*x])/x^4,x]
```

```
[Out] Integrate[(E^(c + d*x^2)*Erfi[a + b*x])/x^4, x]
```

Maple [A]
time = 0.19, size = 0, normalized size = 0.00

$$\int \frac{e^{d\,x^2+c}\,\text{erfi}\,(bx+a)}{x^4}\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(exp(d*x^2+c)*erfi(b*x+a)/x^4,x)
```

```
[Out] int(exp(d*x^2+c)*erfi(b*x+a)/x^4,x)
```

Maxima [A]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x+a)/x^4,x, algorithm="maxima")
[Out] integrate(erfi(b*x + a)*e^(d*x^2 + c)/x^4, x)
```

Fricas [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x+a)/x^4,x, algorithm="fricas")
[Out] integral(erfi(b*x + a)*e^(d*x^2 + c)/x^4, x)
```

Sympy [A]
time = 0.00, size = 0, normalized size = 0.00

$$e^{c}\int \frac{e^{dx^{2}} \operatorname{erfi}{\left(a + bx \right)}}{x^{4}}\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x**2+c)*erfi(b*x+a)/x**4,x)
[Out] exp(c)*Integral(exp(d*x**2)*erfi(a + b*x)/x**4, x)
```

Giac [A]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(exp(d*x^2+c)*erfi(b*x+a)/x^4,x, algorithm="giac")
[Out] integrate(erfi(b*x + a)*e^(d*x^2 + c)/x^4, x)
```

Mupad [A]
time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{\mathrm{erfi}(a+b\,x)\,{\mathrm{e}}^{d\,x^2+c}}{x^4} \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((erfi(a + b*x)*exp(c + d*x^2))/x^4,x)
[Out] int((erfi(a + b*x)*exp(c + d*x^2))/x^4, x)
```

3.303 $\int \left(\frac{e^{-b^2x^2}\mathbf{Erfi}(bx)}{x^3}+\frac{b^2e^{-b^2x^2}\mathbf{Erfi}(bx)}{x}\right)\,dx$

Optimal. Leaf size=33

$$-\frac{b}{\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\text{Erfi}(bx)}{2x^2}$$

```
[Out] -1/2*erfi(b*x)/exp(b^2*x^2)/x^2-b/x/Pi^(1/2)
```

Rubi [A]
time = 0.08, antiderivative size = 33, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 40, $\frac{\text{number of rules}}{\text{integrand size}}=0.075$, Rules used = {6528, 6525, 30}

$$-\frac{e^{-b^2x^2}\text{Erfi}(bx)}{2x^2}-\frac{b}{\sqrt{\pi}\,x}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]/(E^(b^2*x^2)*x^3) + (b^2*Erfi[b*x])/(E^(b^2*x^2)*x),x]
```

```
[Out] -(b/(Sqrt[Pi]*x)) - Erfi[b*x]/(2*E^(b^2*x^2)*x^2)
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6525

```
Int[(E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)])/(x_), x_Symbol] :> Simp[2*b
*E^c*(x/Sqrt[Pi])*HypergeometricPFQ[{1/2, 1}, {3/2, 3/2}, (-b^2)*x^2], x] /
; FreeQ[{b, c, d}, x] && EqQ[d, -b^2]
```

Rule 6528

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(a_.) + (b_.)*(x_)]*(x_)^(m_), x_Symbol]
:> Simp[x^(m + 1)*E^(c + d*x^2)*(Erfi[a + b*x]/(m + 1)), x] + (-Dist[2*(d/(
m + 1)), Int[x^(m + 2)*E^(c + d*x^2)*Erfi[a + b*x], x], x] - Dist[2*(b/((m
+ 1)*Sqrt[Pi])), Int[x^(m + 1)*E^(a^2 + c + 2*a*b*x + (b^2 + d)*x^2), x], x
]) /; FreeQ[{a, b, c, d}, x] && ILtQ[m, -1]
```

Rubi steps

$$\int \left(\frac{e^{-b^2x^2}\mathrm{erfi}(bx)}{x^3}+\frac{b^2e^{-b^2x^2}\mathrm{erfi}(bx)}{x}\right)dx = b^2\int \frac{e^{-b^2x^2}\mathrm{erfi}(bx)}{x}dx+\int \frac{e^{-b^2x^2}\mathrm{erfi}(bx)}{x^3}dx$$
$$= -\frac{e^{-b^2x^2}\mathrm{erfi}(bx)}{2x^2}+\frac{2b^3x\,{}_2F_2\left(\frac{1}{2},1;\frac{3}{2},\frac{3}{2};-b^2x^2\right)}{\sqrt{\pi}}-b^2\int \frac{e^{-b^2x^2}\mathrm{erfi}(}{x}$$
$$= -\frac{b}{\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\mathrm{erfi}(bx)}{2x^2}$$

Mathematica [A]
time = 0.04, size = 33, normalized size = 1.00

$$-\frac{b}{\sqrt{\pi}\,x}-\frac{e^{-b^2x^2}\mathrm{Erfi}(bx)}{2x^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]/(E^(b^2*x^2)*x^3) + (b^2*Erfi[b*x])/(E^(b^2*x^2)*x),x]
[Out] -(b/(Sqrt[Pi]*x)) - Erfi[b*x]/(2*E^(b^2*x^2)*x^2)
```

Maple [A]
time = 0.18, size = 41, normalized size = 1.24

method	result	size
default	$\frac{\left(-2\,\mathrm{e}^{b^2x^2}bx-\mathrm{erfi}(bx)\sqrt{\pi}\right)\mathrm{e}^{-b^2x^2}}{2\sqrt{\pi}\,x^2}$	41

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)/exp(b^2*x^2)/x^3+b^2*erfi(b*x)/exp(b^2*x^2)/x,x,method=_RETUR
NVERBOSE)
[Out] 1/2*(-2*exp(b^2*x^2)*b*x-erfi(b*x)*Pi^(1/2))/Pi^(1/2)/exp(b^2*x^2)/x^2
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^3+b^2*erfi(b*x)/exp(b^2*x^2)/x,x, algori
thm="maxima")
[Out] integrate(b^2*erfi(b*x)*e^(-b^2*x^2)/x + erfi(b*x)*e^(-b^2*x^2)/x^3, x)
```

Fricas [A]
time = 0.37, size = 39, normalized size = 1.18

$$-\frac{\left(2\sqrt{\pi}\,bxe^{\left(b^2x^2\right)}+\pi\operatorname{erfi}\left(bx\right)\right)e^{\left(-b^2x^2\right)}}{2\,\pi x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^3+b^2*erfi(b*x)/exp(b^2*x^2)/x,x, algori
thm="fricas")
```

```
[Out] -1/2*(2*sqrt(pi)*b*x*e^(b^2*x^2) + pi*erfi(b*x))*e^(-b^2*x^2)/(pi*x^2)
```

Sympy [A]
time = 11.08, size = 53, normalized size = 1.61

$$\frac{2b^3x\,{}_2F_2\left(\begin{matrix}\frac{1}{2},1\\\frac{3}{2},\frac{3}{2}\end{matrix}\middle|-b^2x^2\right)}{\sqrt{\pi}}-\frac{2b\,{}_2F_2\left(\begin{matrix}-\frac{1}{2},1\\\frac{1}{2},\frac{3}{2}\end{matrix}\middle|-b^2x^2\right)}{\sqrt{\pi}\,x}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b**2*x**2)/x**3+b**2*erfi(b*x)/exp(b**2*x**2)/x,x)
```

```
[Out] 2*b**3*x*hyper((1/2, 1), (3/2, 3/2), -b**2*x**2)/sqrt(pi) - 2*b*hyper((-1/2
, 1), (1/2, 3/2), -b**2*x**2)/(sqrt(pi)*x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)/exp(b^2*x^2)/x^3+b^2*erfi(b*x)/exp(b^2*x^2)/x,x, algori
thm="giac")
```

```
[Out] integrate(b^2*erfi(b*x)*e^(-b^2*x^2)/x + erfi(b*x)*e^(-b^2*x^2)/x^3, x)
```

Mupad [B]
time = 0.17, size = 28, normalized size = 0.85

$$-\frac{\mathrm{e}^{-b^2\,x^2}\,\mathrm{erfi}(b\,x)}{2\,x^2}-\frac{b}{x\,\sqrt{\pi}}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((exp(-b^2*x^2)*erfi(b*x))/x^3 + (b^2*exp(-b^2*x^2)*erfi(b*x))/x,x)
```

```
[Out] - (exp(-b^2*x^2)*erfi(b*x))/(2*x^2) - b/(x*pi^(1/2))
```

3.304 $\int \mathbf{Erfi}(bx) \sin\left(c + ib^2x^2\right) \, dx$

Optimal. Leaf size=67

$$\frac{ie^{-ic}\sqrt{\pi}\,\mathrm{Erfi}(bx)^2}{8b} - \frac{ibe^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] -1/2*I*b*exp(I*c)*x^2*hypergeom([1, 1],[3/2, 2],-b^2*x^2)/Pi^(1/2)+1/8*I*er
fi(b*x)^2*Pi^(1/2)/b/exp(I*c)
```

Rubi [A]
time = 0.04, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {6541, 6510, 30, 6513}

$$\frac{i\sqrt{\pi}\,e^{-ic}\mathrm{Erfi}(bx)^2}{8b} - \frac{ibe^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]*Sin[c + I*b^2*x^2],x]
```

```
[Out] ((I/8)*Sqrt[Pi]*Erfi[b*x]^2)/(b*E^(I*c)) - ((I/2)*b*E^(I*c)*x^2*Hypergeomet
ricPFQ[{1, 1}, {3/2, 2}, -(b^2*x^2)])/Sqrt[Pi]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6513

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2
/Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, (-b^2)*x^2], x] /; FreeQ[{b,
 c, d}, x] && EqQ[d, -b^2]
```

Rule 6541

```
Int[Erfi[(b_.)*(x_)]*Sin[(c_.) + (d_.)*(x_)^2], x_Symbol] :> Dist[I/2, Int[
E^((-I)*c - I*d*x^2)*Erfi[b*x], x], x] - Dist[I/2, Int[E^(I*c + I*d*x^2)*Er
fi[b*x], x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, -b^4]
```

Rubi steps

$$\begin{aligned}
\int \operatorname{erfi}(bx)\sin\left(c+ib^2x^2\right)\,dx &= -\left(\frac{1}{2}i\int e^{ic-b^2x^2}\operatorname{erfi}(bx)\,dx\right)+\frac{1}{2}i\int e^{-ic+b^2x^2}\operatorname{erfi}(bx)\,dx\\
&= -\frac{ibe^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}+\frac{\left(ie^{-ic}\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erfi}(bx)\right)}{4b}\\
&= \frac{ie^{-ic}\sqrt{\pi}\operatorname{erfi}(bx)^2}{8b}-\frac{ibe^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}
\end{aligned}$$

Mathematica [F]
time = 0.39, size = 0, normalized size = 0.00

$$\int \operatorname{Erfi}(bx)\sin\left(c+ib^2x^2\right)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfi[b*x]*Sin[c + I*b^2*x^2],x]
[Out] Integrate[Erfi[b*x]*Sin[c + I*b^2*x^2], x]
```

Maple [F]
time = 0.06, size = 0, normalized size = 0.00

$$\int \operatorname{erfi}(bx)\sin\left(ib^2x^2+c\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)*sin(c+I*b^2*x^2),x)
[Out] int(erfi(b*x)*sin(c+I*b^2*x^2),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)*sin(c+I*b^2*x^2),x, algorithm="maxima")
[Out] 1/8*I*sqrt(pi)*cos(c)*erfi(b*x)^2/b + 1/8*sqrt(pi)*erfi(b*x)^2*sin(c)/b - 1
/2*I*cos(c)*integrate(erfi(b*x)*e^(-b^2*x^2), x) + 1/2*integrate(erfi(b*x)*
e^(-b^2*x^2), x)*sin(c)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)*sin(c+I*b^2*x^2),x, algorithm="fricas")
```

```
[Out] integral(1/2*(-I*erfi(b*x)*e^(-2*b^2*x^2 + 2*I*c) + I*erfi(b*x))*e^(b^2*x^2
 - I*c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \sin\left(ib^2x^2 + c\right)\operatorname{erfi}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)*sin(c+I*b**2*x**2),x)
```

```
[Out] Integral(sin(I*b**2*x**2 + c)*erfi(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)*sin(c+I*b^2*x^2),x, algorithm="giac")
```

```
[Out] integrate(erfi(b*x)*sin(I*b^2*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \sin\left(b^2\,x^2\,1{}\mathrm{i}+c\right)\,\mathrm{erfi}(b\,x)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(sin(c + b^2*x^2*1i)*erfi(b*x),x)
```

```
[Out] int(sin(c + b^2*x^2*1i)*erfi(b*x), x)
```

3.305 $\int \mathbf{Erfi}(bx)\sin\left(c - ib^2x^2\right)\,dx$

Optimal. Leaf size=67

$$-\frac{ie^{ic}\sqrt{\pi}\,\mathrm{Erfi}(bx)^2}{8b}+\frac{ibe^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] 1/2*I*b*x^2*hypergeom([1, 1],[3/2, 2],-b^2*x^2)/exp(I*c)/Pi^(1/2)-1/8*I*exp
(I*c)*erfi(b*x)^2*Pi^(1/2)/b
```

Rubi [A]
time = 0.04, antiderivative size = 67, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {6541, 6513, 6510, 30}

$$\frac{ibe^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}-\frac{i\sqrt{\pi}\,e^{ic}\mathrm{Erfi}(bx)^2}{8b}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]*Sin[c - I*b^2*x^2],x]
```

```
[Out] ((-1/8*I)*E^(I*c)*Sqrt[Pi]*Erfi[b*x]^2)/b + ((I/2)*b*x^2*HypergeometricPFQ[
{1, 1}, {3/2, 2}, -(b^2*x^2)])/(E^(I*c)*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6513

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2
/Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, (-b^2)*x^2], x] /; FreeQ[{b,
 c, d}, x] && EqQ[d, -b^2]
```

Rule 6541

```
Int[Erfi[(b_.)*(x_)]*Sin[(c_.) + (d_.)*(x_)^2], x_Symbol] :> Dist[I/2, Int[
E^((-I)*c - I*d*x^2)*Erfi[b*x], x], x] - Dist[I/2, Int[E^(I*c + I*d*x^2)*Er
fi[b*x], x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, -b^4]
```

Rubi steps

$$\begin{aligned}\int \operatorname{erfi}(bx)\sin\left(c-ib^2x^2\right)\,dx &= \frac{1}{2}i\int e^{-ic-b^2x^2}\operatorname{erfi}(bx)\,dx-\frac{1}{2}i\int e^{ic+b^2x^2}\operatorname{erfi}(bx)\,dx\\ &= \frac{ibe^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}-\frac{\left(ie^{ic}\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erfi}(bx)\right)}{4b}\\ &= -\frac{ie^{ic}\sqrt{\pi}\operatorname{erfi}(bx)^2}{8b}+\frac{ibe^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}\end{aligned}$$

Mathematica [F]
time = 0.38, size = 0, normalized size = 0.00

$$\int \operatorname{Erfi}(bx)\sin\left(c-ib^2x^2\right)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Erfi[b*x]*Sin[c - I*b^2*x^2],x]
[Out] Integrate[Erfi[b*x]*Sin[c - I*b^2*x^2], x]
```

Maple [F]
time = 0.07, size = 0, normalized size = 0.00

$$\int -\operatorname{erfi}(bx)\sin\left(ib^2x^2-c\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(-erfi(b*x)*sin(-c+I*b^2*x^2),x)
[Out] int(-erfi(b*x)*sin(-c+I*b^2*x^2),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfi(b*x)*sin(-c+I*b^2*x^2),x, algorithm="maxima")
[Out] -1/8*I*sqrt(pi)*cos(c)*erfi(b*x)^2/b + 1/8*sqrt(pi)*erfi(b*x)^2*sin(c)/b +
1/2*I*cos(c)*integrate(erfi(b*x)*e^(-b^2*x^2), x) + 1/2*integrate(erfi(b*x)
*e^(-b^2*x^2), x)*sin(c)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfi(b*x)*sin(-c+I*b^2*x^2),x, algorithm="fricas")
[Out] integral(1/2*(I*erfi(b*x)*e^(-2*b^2*x^2 - 2*I*c) - I*erfi(b*x))*e^(b^2*x^2
+ I*c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$-\int \sin\left(ib^2x^2-c\right)\operatorname{erfi}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfi(b*x)*sin(-c+I*b**2*x**2),x)
[Out] -Integral(sin(I*b**2*x**2 - c)*erfi(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfi(b*x)*sin(-c+I*b^2*x^2),x, algorithm="giac")
[Out] integrate(-erfi(b*x)*sin(I*b^2*x^2 - c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.01

$$\int \sin\left(c-b^2\,x^2\,1\mathrm{i}\right)\,\mathrm{erfi}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(sin(c - b^2*x^2*1i)*erfi(b*x),x)
[Out] int(sin(c - b^2*x^2*1i)*erfi(b*x), x)
```

3.306 $\int \cos\left(c + ib^2x^2\right) \mathbf{Erfi}(bx)\, dx$

Optimal. Leaf size=63

$$\frac{e^{-ic}\sqrt{\pi}\,\mathrm{Erfi}(bx)^2}{8b} + \frac{be^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] 1/2*b*exp(I*c)*x^2*hypergeom([1, 1],[3/2, 2],-b^2*x^2)/Pi^(1/2)+1/8*erfi(b*
x)^2*Pi^(1/2)/b/exp(I*c)
```

Rubi [A]
time = 0.04, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = {6544, 6510, 30, 6513}

$$\frac{be^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}} + \frac{\sqrt{\pi}\,e^{-ic}\mathrm{Erfi}(bx)^2}{8b}$$

Antiderivative was successfully verified.

```
[In] Int[Cos[c + I*b^2*x^2]*Erfi[b*x],x]
```

```
[Out] (Sqrt[Pi]*Erfi[b*x]^2)/(8*b*E^(I*c)) + (b*E^(I*c)*x^2*HypergeometricPFQ[{1,
 1}, {3/2, 2}, -(b^2*x^2)])/(2*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6513

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2
/Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, (-b^2)*x^2], x] /; FreeQ[{b,
 c, d}, x] && EqQ[d, -b^2]
```

Rule 6544

```
Int[Cos[(c_.) + (d_.)*(x_)^2]*Erfi[(b_.)*(x_)], x_Symbol] :> Dist[1/2, Int[
E^((-I)*c - I*d*x^2)*Erfi[b*x], x], x] + Dist[1/2, Int[E^(I*c + I*d*x^2)*Er
fi[b*x], x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, -b^4]
```

Rubi steps

$$
\begin{aligned}
\int \cos\left(c+ib^2x^2\right)\operatorname{erfi}(bx)\,dx &= \frac{1}{2}\int e^{ic-b^2x^2}\operatorname{erfi}(bx)\,dx+\frac{1}{2}\int e^{-ic+b^2x^2}\operatorname{erfi}(bx)\,dx\\
&= \frac{be^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}+\frac{\left(e^{-ic}\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erfi}(bx)\right)}{4b}\\
&= \frac{e^{-ic}\sqrt{\pi}\operatorname{erfi}(bx)^2}{8b}+\frac{be^{ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}
\end{aligned}
$$

Mathematica [F]
time = 0.38, size = 0, normalized size = 0.00

$$\int \cos\left(c+ib^2x^2\right)\operatorname{Erfi}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Cos[c + I*b^2*x^2]*Erfi[b*x],x]
[Out] Integrate[Cos[c + I*b^2*x^2]*Erfi[b*x], x]
```

Maple [F]
time = 0.16, size = 0, normalized size = 0.00

$$\int \cos\left(ib^2x^2+c\right)\operatorname{erfi}\left(bx\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cos(c+I*b^2*x^2)*erfi(b*x),x)
[Out] int(cos(c+I*b^2*x^2)*erfi(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(c+I*b^2*x^2)*erfi(b*x),x, algorithm="maxima")
[Out] 1/8*sqrt(pi)*cos(c)*erfi(b*x)^2/b - 1/8*I*sqrt(pi)*erfi(b*x)^2*sin(c)/b + 1
/2*cos(c)*integrate(erfi(b*x)*e^(-b^2*x^2), x) + 1/2*I*integrate(erfi(b*x)*
e^(-b^2*x^2), x)*sin(c)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(c+I*b^2*x^2)*erfi(b*x),x, algorithm="fricas")
```

```
[Out] integral(1/2*(erfi(b*x)*e^(-2*b^2*x^2 + 2*I*c) + erfi(b*x))*e^(b^2*x^2 - I*
c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \cos\left(ib^2x^2 + c\right) \operatorname{erfi}\left(bx\right) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(c+I*b**2*x**2)*erfi(b*x),x)
```

```
[Out] Integral(cos(I*b**2*x**2 + c)*erfi(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(c+I*b^2*x^2)*erfi(b*x),x, algorithm="giac")
```

```
[Out] integrate(cos(I*b^2*x^2 + c)*erfi(b*x), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \cos\left(b^2\,x^2\,1\mathrm{i}+c\right)\,\mathrm{erfi}(b\,x)\;dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cos(c + b^2*x^2*1i)*erfi(b*x),x)
```

```
[Out] int(cos(c + b^2*x^2*1i)*erfi(b*x), x)
```

3.307 $\int \cos\left(c - ib^2x^2\right) \mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=63

$$\frac{e^{ic}\sqrt{\pi}\,\mathrm{Erfi}(bx)^2}{8b} + \frac{be^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] 1/2*b*x^2*hypergeom([1, 1],[3/2, 2],-b^2*x^2)/exp(I*c)/Pi^(1/2)+1/8*exp(I*c
)*erfi(b*x)^2*Pi^(1/2)/b
```

Rubi [A]
time = 0.04, antiderivative size = 63, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 18, $\frac{\text{number of rules}}{\text{integrand size}} = 0.222$, Rules used = $\{6544, 6513, 6510, 30\}$

$$\frac{be^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}} + \frac{\sqrt{\pi}\,e^{ic}\mathrm{Erfi}(bx)^2}{8b}$$

Antiderivative was successfully verified.

```
[In] Int[Cos[c - I*b^2*x^2]*Erfi[b*x],x]
```

```
[Out] (E^(I*c)*Sqrt[Pi]*Erfi[b*x]^2)/(8*b) + (b*x^2*HypergeometricPFQ[{1, 1}, {3/
2, 2}, -(b^2*x^2)])/(2*E^(I*c)*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6513

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2
/Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, (-b^2)*x^2], x] /; FreeQ[{b,
 c, d}, x] && EqQ[d, -b^2]
```

Rule 6544

```
Int[Cos[(c_.) + (d_.)*(x_)^2]*Erfi[(b_.)*(x_)], x_Symbol] :> Dist[1/2, Int[
E^((-I)*c - I*d*x^2)*Erfi[b*x], x], x] + Dist[1/2, Int[E^(I*c + I*d*x^2)*Er
fi[b*x], x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, -b^4]
```

Rubi steps

$$\begin{aligned}\int \cos\left(c-ib^2x^2\right)\operatorname{erfi}(bx)\,dx &= \frac{1}{2}\int e^{-ic-b^2x^2}\operatorname{erfi}(bx)\,dx+\frac{1}{2}\int e^{ic+b^2x^2}\operatorname{erfi}(bx)\,dx\\ &= \frac{be^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}+\frac{\left(e^{ic}\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erfi}(bx)\right)}{4b}\\ &= \frac{e^{ic}\sqrt{\pi}\operatorname{erfi}(bx)^2}{8b}+\frac{be^{-ic}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}\end{aligned}$$

Mathematica [F]
time = 0.41, size = 0, normalized size = 0.00

$$\int \cos\left(c-ib^2x^2\right)\operatorname{Erfi}(bx)\,dx$$

Verification is not applicable to the result.

```
[In] Integrate[Cos[c - I*b^2*x^2]*Erfi[b*x],x]
[Out] Integrate[Cos[c - I*b^2*x^2]*Erfi[b*x], x]
```

Maple [F]
time = 0.15, size = 0, normalized size = 0.00

$$\int \cos\left(ib^2x^2-c\right)\operatorname{erfi}\left(bx\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cos(-c+I*b^2*x^2)*erfi(b*x),x)
[Out] int(cos(-c+I*b^2*x^2)*erfi(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(-c+I*b^2*x^2)*erfi(b*x),x, algorithm="maxima")
[Out] 1/8*sqrt(pi)*cos(c)*erfi(b*x)^2/b + 1/8*I*sqrt(pi)*erfi(b*x)^2*sin(c)/b + 1
/2*cos(c)*integrate(erfi(b*x)*e^(-b^2*x^2), x) - 1/2*I*integrate(erfi(b*x)*
e^(-b^2*x^2), x)*sin(c)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(-c+I*b^2*x^2)*erfi(b*x),x, algorithm="fricas")
```

```
[Out] integral(1/2*(erfi(b*x)*e^(-2*b^2*x^2 - 2*I*c) + erfi(b*x))*e^(b^2*x^2 + I*c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \cos\left(ib^2x^2 - c\right)\operatorname{erfi}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(-c+I*b**2*x**2)*erfi(b*x),x)
```

```
[Out] Integral(cos(I*b**2*x**2 - c)*erfi(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(-c+I*b^2*x^2)*erfi(b*x),x, algorithm="giac")
```

```
[Out] integrate(cos(I*b^2*x^2 - c)*erfi(b*x), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \cos\left(c - b^2\,x^2\,1\mathrm{i}\right)\,\mathrm{erfi}(b\,x)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cos(c - b^2*x^2*1i)*erfi(b*x),x)
```

```
[Out] int(cos(c - b^2*x^2*1i)*erfi(b*x), x)
```

3.308 $\int \mathbf{Erfi}(bx)\sinh\left(c+b^2x^2\right)\,dx$

Optimal. Leaf size=57

$$\frac{e^c\sqrt{\pi}\,\mathrm{Erfi}(bx)^2}{8b}-\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] -1/2*b*x^2*hypergeom([1, 1],[3/2, 2],-b^2*x^2)/exp(c)/Pi^(1/2)+1/8*exp(c)*e
rfi(b*x)^2*Pi^(1/2)/b
```

Rubi [A]
time = 0.04, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}}=0.267$, Rules used = {6547, 6510, 30, 6513}

$$\frac{\sqrt{\pi}\,e^c\mathrm{Erfi}(bx)^2}{8b}-\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]*Sinh[c + b^2*x^2],x]
```

```
[Out] (E^c*Sqrt[Pi]*Erfi[b*x]^2)/(8*b) - (b*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2
}, -(b^2*x^2)])/(2*E^c*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6513

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2
/Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, (-b^2)*x^2], x] /; FreeQ[{b,
 c, d}, x] && EqQ[d, -b^2]
```

Rule 6547

```
Int[Erfi[(b_.)*(x_)]*Sinh[(c_.) + (d_.)*(x_)^2], x_Symbol] :> Dist[1/2, Int
[E^(c + d*x^2)*Erfi[b*x], x], x] - Dist[1/2, Int[E^(-c - d*x^2)*Erfi[b*x],
x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, b^4]
```

Rubi steps

$$
\begin{aligned}
\int \operatorname{erfi}(bx)\sinh\left(c+b^2x^2\right)\,dx &= -\left(\frac{1}{2}\int e^{-c-b^2x^2}\operatorname{erfi}(bx)\,dx\right)+\frac{1}{2}\int e^{c+b^2x^2}\operatorname{erfi}(bx)\,dx\\
&= -\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}+\frac{\left(e^c\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erfi}(bx)\right)}{4b}\\
&= \frac{e^c\sqrt{\pi}\operatorname{erfi}(bx)^2}{8b}-\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}
\end{aligned}
$$

Mathematica [**A**]
time = 0.90, size = 74, normalized size = 1.30

$$
\frac{4b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)(\cosh(c)-\sinh(c))+\pi\operatorname{Erfi}(bx)(-2\operatorname{Erf}(bx)(\cosh(c)-\sinh(c))+\operatorname{Erfi}(bx)(\cosh(c)+\sinh(c)))}{8b\sqrt{\pi}}
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]*Sinh[c + b^2*x^2],x]
[Out] (4*b^2*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2]*(Cosh[c] - Sinh[c])
 + Pi*Erfi[b*x]*(-2*Erf[b*x]*(Cosh[c] - Sinh[c]) + Erfi[b*x]*(Cosh[c] + Sin
h[c])))/(8*b*Sqrt[Pi])
```

Maple [**F**]
time = 0.06, size = 0, normalized size = 0.00

$$
\int \operatorname{erfi}(bx)\sinh\left(b^2x^2+c\right)\,dx
$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(erfi(b*x)*sinh(b^2*x^2+c),x)
[Out] int(erfi(b*x)*sinh(b^2*x^2+c),x)
```

Maxima [**F**]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)*sinh(b^2*x^2+c),x, algorithm="maxima")
[Out] integrate(erfi(b*x)*sinh(b^2*x^2 + c), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)*sinh(b^2*x^2+c),x, algorithm="fricas")
[Out] integral(erfi(b*x)*sinh(b^2*x^2 + c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \sinh \left(b^{2} x^{2} + c\right) \operatorname{erfi}\left(b x\right)\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)*sinh(b**2*x**2+c),x)
[Out] Integral(sinh(b**2*x**2 + c)*erfi(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(erfi(b*x)*sinh(b^2*x^2+c),x, algorithm="giac")
[Out] integrate(erfi(b*x)*sinh(b^2*x^2 + c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \mathrm{sinh}\left(b^2\,x^2+c\right)\,\mathrm{erfi}\left(b\,x\right) \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(sinh(c + b^2*x^2)*erfi(b*x),x)
[Out] int(sinh(c + b^2*x^2)*erfi(b*x), x)
```

3.309 $\int \mathbf{Erfi}(bx)\sinh\left(c-b^2x^2\right)\,dx$

Optimal. Leaf size=57

$$-\frac{e^{-c}\sqrt{\pi}\,\mathrm{Erfi}(bx)^2}{8b}+\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] 1/2*b*exp(c)*x^2*hypergeom([1, 1],[3/2, 2],-b^2*x^2)/Pi^(1/2)-1/8*erfi(b*x)
^2*Pi^(1/2)/b/exp(c)
```

Rubi [A]
time = 0.03, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}}=0.250$, Rules used = $\{6547, 6513, 6510, 30\}$

$$\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}-\frac{\sqrt{\pi}\,e^{-c}\mathrm{Erfi}(bx)^2}{8b}$$

Antiderivative was successfully verified.

```
[In] Int[Erfi[b*x]*Sinh[c - b^2*x^2],x]
```

```
[Out] -1/8*(Sqrt[Pi]*Erfi[b*x]^2)/(b*E^c) + (b*E^c*x^2*HypergeometricPFQ[{1, 1},
{3/2, 2}, -(b^2*x^2)])/(2*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6513

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2
/Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, (-b^2)*x^2], x] /; FreeQ[{b,
 c, d}, x] && EqQ[d, -b^2]
```

Rule 6547

```
Int[Erfi[(b_.)*(x_)]*Sinh[(c_.) + (d_.)*(x_)^2], x_Symbol] :> Dist[1/2, Int
[E^(c + d*x^2)*Erfi[b*x], x], x] - Dist[1/2, Int[E^(-c - d*x^2)*Erfi[b*x],
x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, b^4]
```

Rubi steps

$$
\begin{aligned}
\int \operatorname{erfi}(bx)\sinh\left(c-b^2x^2\right)\,dx &= \frac{1}{2}\int e^{c-b^2x^2}\operatorname{erfi}(bx)\,dx-\frac{1}{2}\int e^{-c+b^2x^2}\operatorname{erfi}(bx)\,dx\\
&= \frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}-\frac{\left(e^{-c}\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erfi}(bx)\right)}{4b}\\
&= -\frac{e^{-c}\sqrt{\pi}\operatorname{erfi}(bx)^2}{8b}+\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}
\end{aligned}
$$

Mathematica [A]
time = 0.56, size = 72, normalized size = 1.26

$$
\frac{-4b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)(\cosh(c)+\sinh(c))+\pi\operatorname{Erfi}(bx)(\operatorname{Erfi}(bx)(-\cosh(c)+\sinh(c))+2\operatorname{Erf}(bx)(\cosh(c)+\sinh(c)))}{8b\sqrt{\pi}}
$$

Antiderivative was successfully verified.

```
[In] Integrate[Erfi[b*x]*Sinh[c - b^2*x^2],x]
```

```
[Out] (-4*b^2*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2]*(Cosh[c] + Sinh[c]
) + Pi*Erfi[b*x]*(Erfi[b*x]*(-Cosh[c] + Sinh[c]) + 2*Erf[b*x]*(Cosh[c] + Si
nh[c])))/(8*b*Sqrt[Pi])
```

Maple [F]
time = 0.06, size = 0, normalized size = 0.00

$$
\int -\operatorname{erfi}(bx)\sinh\left(b^2x^2-c\right)\,dx
$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(-erfi(b*x)*sinh(b^2*x^2-c),x)
```

```
[Out] int(-erfi(b*x)*sinh(b^2*x^2-c),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfi(b*x)*sinh(b^2*x^2-c),x, algorithm="maxima")
```

```
[Out] -integrate(erfi(b*x)*sinh(b^2*x^2 - c), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfi(b*x)*sinh(b^2*x^2-c),x, algorithm="fricas")
[Out] integral(-erfi(b*x)*sinh(b^2*x^2 - c), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$-\int \sinh \left(b^{2} x^{2} - c\right) \operatorname{erfi}\left(b x\right)\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfi(b*x)*sinh(b**2*x**2-c),x)
[Out] -Integral(sinh(b**2*x**2 - c)*erfi(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(-erfi(b*x)*sinh(b^2*x^2-c),x, algorithm="giac")
[Out] integrate(-erfi(b*x)*sinh(b^2*x^2 - c), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \sinh\left(c-b^2\,x^2\right)\,\mathrm{erfi}\left(b\,x\right) \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(sinh(c - b^2*x^2)*erfi(b*x),x)
[Out] int(sinh(c - b^2*x^2)*erfi(b*x), x)
```

3.310 $\int \cosh(c+b^2x^2)\,\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=57

$$\frac{e^c\sqrt{\pi}\,\mathrm{Erfi}(bx)^2}{8b}+\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] 1/2*b*x^2*hypergeom([1, 1],[3/2, 2],-b^2*x^2)/exp(c)/Pi^(1/2)+1/8*exp(c)*er
fi(b*x)^2*Pi^(1/2)/b
```

Rubi [A]
time = 0.04, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}}=0.267$, Rules used = {6550, 6510, 30, 6513}

$$\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}+\frac{\sqrt{\pi}\,e^c\mathrm{Erfi}(bx)^2}{8b}$$

Antiderivative was successfully verified.

```
[In] Int[Cosh[c + b^2*x^2]*Erfi[b*x],x]
```

```
[Out] (E^c*Sqrt[Pi]*Erfi[b*x]^2)/(8*b) + (b*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2
}, -(b^2*x^2)])/(2*E^c*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6513

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2
/Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, (-b^2)*x^2], x] /; FreeQ[{b,
 c, d}, x] && EqQ[d, -b^2]
```

Rule 6550

```
Int[Cosh[(c_.) + (d_.)*(x_)^2]*Erfi[(b_.)*(x_)], x_Symbol] :> Dist[1/2, Int
[E^(c + d*x^2)*Erfi[b*x], x], x] + Dist[1/2, Int[E^(-c - d*x^2)*Erfi[b*x],
x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, b^4]
```

Rubi steps

$$
\begin{aligned}
\int \cosh\left(c+b^2x^2\right)\operatorname{erfi}(bx)\,dx &= \frac{1}{2}\int e^{-c-b^2x^2}\operatorname{erfi}(bx)\,dx+\frac{1}{2}\int e^{c+b^2x^2}\operatorname{erfi}(bx)\,dx\\
&= \frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}+\frac{\left(e^c\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erfi}(bx)\right)}{4b}\\
&= \frac{e^c\sqrt{\pi}\operatorname{erfi}(bx)^2}{8b}+\frac{be^{-c}x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}
\end{aligned}
$$

Mathematica [A]
time = 7.53, size = 74, normalized size = 1.30

$$\frac{4b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)(-\cosh(c)+\sinh(c))+\pi\operatorname{Erfi}(bx)(2\operatorname{Erf}(bx)(\cosh(c)-\sinh(c))+\operatorname{Erfi}(bx)(\cosh(c)+\sinh(c)))}{8b\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Cosh[c + b^2*x^2]*Erfi[b*x],x]
```

```
[Out] (4*b^2*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2]*(-Cosh[c] + Sinh[c]
) + Pi*Erfi[b*x]*(2*Erf[b*x]*(Cosh[c] - Sinh[c]) + Erfi[b*x]*(Cosh[c] + Sin
h[c])))/(8*b*Sqrt[Pi])
```

Maple [F]
time = 0.17, size = 0, normalized size = 0.00

$$\int \cosh\left(b^2x^2+c\right)\operatorname{erfi}\left(bx\right)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cosh(b^2*x^2+c)*erfi(b*x),x)
```

```
[Out] int(cosh(b^2*x^2+c)*erfi(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2+c)*erfi(b*x),x, algorithm="maxima")
```

```
[Out] integrate(cosh(b^2*x^2 + c)*erfi(b*x), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2+c)*erfi(b*x),x, algorithm="fricas")
[Out] integral(cosh(b^2*x^2 + c)*erfi(b*x), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \cosh \left(b^{2} x^{2} + c\right) \operatorname{erfi}\left(b x\right)\, dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b**2*x**2+c)*erfi(b*x),x)
[Out] Integral(cosh(b**2*x**2 + c)*erfi(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2+c)*erfi(b*x),x, algorithm="giac")
[Out] integrate(cosh(b^2*x^2 + c)*erfi(b*x), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \mathrm{cosh}\left(b^2\,x^2+c\right)\,\mathrm{erfi}\left(b\,x\right) \,d x$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cosh(c + b^2*x^2)*erfi(b*x),x)
[Out] int(cosh(c + b^2*x^2)*erfi(b*x), x)
```

3.311 $\int \cosh(c-b^2x^2)\,\mathbf{Erfi}(bx)\,dx$

Optimal. Leaf size=57

$$\frac{e^{-c}\sqrt{\pi}\,\mathrm{Erfi}(bx)^2}{8b}+\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}$$

```
[Out] 1/2*b*exp(c)*x^2*hypergeom([1, 1],[3/2, 2],-b^2*x^2)/Pi^(1/2)+1/8*erfi(b*x)
^2*Pi^(1/2)/b/exp(c)
```

Rubi [A]
time = 0.04, antiderivative size = 57, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}}=0.250$, Rules used = {6550, 6513, 6510, 30}

$$\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}+\frac{\sqrt{\pi}\,e^{-c}\mathrm{Erfi}(bx)^2}{8b}$$

Antiderivative was successfully verified.

```
[In] Int[Cosh[c - b^2*x^2]*Erfi[b*x],x]
```

```
[Out] (Sqrt[Pi]*Erfi[b*x]^2)/(8*b*E^c) + (b*E^c*x^2*HypergeometricPFQ[{1, 1}, {3/
2, 2}, -(b^2*x^2)])/(2*Sqrt[Pi])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6510

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)]^(n_.), x_Symbol] :> Dist[E^c*
(Sqrt[Pi]/(2*b)), Subst[Int[x^n, x], x, Erfi[b*x]], x] /; FreeQ[{b, c, d, n
}, x] && EqQ[d, b^2]
```

Rule 6513

```
Int[E^((c_.) + (d_.)*(x_)^2)*Erfi[(b_.)*(x_)], x_Symbol] :> Simp[b*E^c*(x^2
/Sqrt[Pi])*HypergeometricPFQ[{1, 1}, {3/2, 2}, (-b^2)*x^2], x] /; FreeQ[{b,
 c, d}, x] && EqQ[d, -b^2]
```

Rule 6550

```
Int[Cosh[(c_.) + (d_.)*(x_)^2]*Erfi[(b_.)*(x_)], x_Symbol] :> Dist[1/2, Int
[E^(c + d*x^2)*Erfi[b*x], x], x] + Dist[1/2, Int[E^(-c - d*x^2)*Erfi[b*x],
x], x] /; FreeQ[{b, c, d}, x] && EqQ[d^2, b^4]
```

Rubi steps

$$\begin{aligned}
\int \cosh\left(c-b^2x^2\right)\operatorname{erfi}(bx)\,dx &= \frac{1}{2}\int e^{c-b^2x^2}\operatorname{erfi}(bx)\,dx+\frac{1}{2}\int e^{-c+b^2x^2}\operatorname{erfi}(bx)\,dx\\
&= \frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}+\frac{\left(e^{-c}\sqrt{\pi}\right)\operatorname{Subst}\left(\int x\,dx,x,\operatorname{erfi}(bx)\right)}{4b}\\
&= \frac{e^{-c}\sqrt{\pi}\operatorname{erfi}(bx)^2}{8b}+\frac{be^cx^2\,{}_2F_2\left(1,1;\frac{3}{2},2;-b^2x^2\right)}{2\sqrt{\pi}}
\end{aligned}$$

Mathematica [A]
time = 1.18, size = 72, normalized size = 1.26

$$\frac{-4b^2x^2\,{}_2F_2\left(1,1;\frac{3}{2},2;b^2x^2\right)(\cosh(c)+\sinh(c))+\pi\operatorname{Erfi}(bx)(\operatorname{Erfi}(bx)(\cosh(c)-\sinh(c))+2\operatorname{Erf}(bx)(\cosh(c)+\sinh(c)))}{8b\sqrt{\pi}}$$

Antiderivative was successfully verified.

```
[In] Integrate[Cosh[c - b^2*x^2]*Erfi[b*x],x]
[Out] (-4*b^2*x^2*HypergeometricPFQ[{1, 1}, {3/2, 2}, b^2*x^2]*(Cosh[c] + Sinh[c]
) + Pi*Erfi[b*x]*(Erfi[b*x]*(Cosh[c] - Sinh[c]) + 2*Erf[b*x]*(Cosh[c] + Sin
h[c])))/(8*b*Sqrt[Pi])
```

Maple [F]
time = 0.15, size = 0, normalized size = 0.00

$$\int \cosh\left(b^2x^2-c\right)\operatorname{erfi}(bx)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cosh(b^2*x^2-c)*erfi(b*x),x)
[Out] int(cosh(b^2*x^2-c)*erfi(b*x),x)
```

Maxima [F]
time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2-c)*erfi(b*x),x, algorithm="maxima")
[Out] integrate(cosh(b^2*x^2 - c)*erfi(b*x), x)
```

Fricas [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2-c)*erfi(b*x),x, algorithm="fricas")
[Out] integral(cosh(b^2*x^2 - c)*erfi(b*x), x)
```

Sympy [F]
time = 0.00, size = 0, normalized size = 0.00

$$\int \cosh\left(b^2x^2 - c\right)\operatorname{erfi}\left(bx\right)dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b**2*x**2-c)*erfi(b*x),x)
[Out] Integral(cosh(b**2*x**2 - c)*erfi(b*x), x)
```

Giac [F]
time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cosh(b^2*x^2-c)*erfi(b*x),x, algorithm="giac")
[Out] integrate(cosh(b^2*x^2 - c)*erfi(b*x), x)
```

Mupad [F]
time = 0.00, size = -1, normalized size = -0.02

$$\int \cosh\left(c - b^2\,x^2\right)\,\operatorname{erfi}(b\,x)\,dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(cosh(c - b^2*x^2)*erfi(b*x),x)
[Out] int(cosh(c - b^2*x^2)*erfi(b*x), x)
```

Chapter 4

Appendix

Local contents

4.1 Download section

The following zip files contain the raw integrals used in this test.

Mathematica format Mathematica_syntax.zip

Maple and Mupad format Maple_syntax.zip

Sympy format SYMPY_syntax.zip

Sage math format SAGE_syntax.zip

4.2 Listing of Grading functions

The following are the current version of the grading functions used for grading the quality of the antiderivative with reference to the optimal antiderivative included in the test suite.

There is a version for Maple and for Mathematica/Rubi. There is a version for grading Sympy and version for use with Sagemath.

The following are links to the current source code.

The following are the listings of source code of the grading functions.

4.2.1 Mathematica and Rubi grading function

```
(* Original version thanks to Albert Rich emailed on 03/21/2017 *)
(* ::Package:: *)

(* Nasser: April 7,2022. add second output which gives reason for the grade *)
(*                       Small rewrite of logic in main function to make it*)
(*                       match Maple's logic. No change in functionality otherwise*)

(* ::Subsection:: *)
(*GradeAntiderivative[result,optimal]*)


(* ::Text:: *)
(*If result and optimal are mathematical expressions, *)
(*          GradeAntiderivative[result,optimal] returns*)
(*  "F" if the result fails to integrate an expression that*)
(*      is integrable*)
(*  "C" if result involves higher level functions than necessary*)
(*  "B" if result is more than twice the size of the optimal*)
(*      antiderivative*)
(*  "A" if result can be considered optimal*)
```

```
GradeAntiderivative[result_,optimal_] := Module[{expnResult,expnOptimal,leafCountResult,leafC
    expnResult  = ExpnType[result];
    expnOptimal = ExpnType[optimal];
    leafCountResult = LeafCount[result];
    leafCountOptimal = LeafCount[optimal];

    (*Print["expnResult=",expnResult," expnOptimal=",expnOptimal];*)
    If[expnResult<=expnOptimal,
        If[Not[FreeQ[result,Complex]], (*result contains complex*)
            If[Not[FreeQ[optimal,Complex]], (*optimal contains complex*)
                If[leafCountResult<=2*leafCountOptimal,
                    finalresult={"A","none"}
                    ,(*ELSE*)
                    finalresult={"B","Both result and optimal contain complex but leaf count
                  ]
            ,(*ELSE*)
                finalresult={"C","Result contains complex when optimal does not."}
            ]
        ,(*ELSE*)(*result does not contains complex*)
            If[leafCountResult<=2*leafCountOptimal,
               finalresult={"A","none"}
            ,(*ELSE*)
               finalresult={"B","Leaf count is larger than twice the leaf count of optimal. $
              ]
        ]
    ,(*ELSE*) (*expnResult>expnOptimal*)
        If[FreeQ[result,Integrate] && FreeQ[result,Int],
            finalresult={"C","Result contains higher order function than in optimal. Order "<
            ,
            finalresult={"F","Contains unresolved integral."}
        ]
    ];

    finalresult
]

(* ::Text:: *)
(*The following summarizes the type number assigned an *)
(*expression based on the functions it involves*)
(*1 = rational function*)
(*2 = algebraic function*)
(*3 = elementary function*)
(*4 = special function*)
(*5 = hyperpergeometric function*)
(*6 = appell function*)
(*7 = rootsum function*)
(*8 = integrate function*)
```

```
(*9 = unknown function*)


ExpnType[expn_] :=
  If[AtomQ[expn],
    1,
  If[ListQ[expn],
    Max[Map[ExpnType,expn]],
  If[Head[expn]===Power,
    If[IntegerQ[expn[[2]]],
      ExpnType[expn[[1]]],
    If[Head[expn[[2]]]===Rational,
      If[IntegerQ[expn[[1]]] || Head[expn[[1]]]===Rational,
        1,
      Max[ExpnType[expn[[1]]],2]],
    Max[ExpnType[expn[[1]]],ExpnType[expn[[2]]],3]]],
  If[Head[expn]===Plus || Head[expn]===Times,
    Max[ExpnType[First[expn]],ExpnType[Rest[expn]]],
  If[ElementaryFunctionQ[Head[expn]],
    Max[3,ExpnType[expn[[1]]]],
  If[SpecialFunctionQ[Head[expn]],
    Apply[Max,Append[Map[ExpnType,Apply[List,expn]],4]],
  If[HypergeometricFunctionQ[Head[expn]],
    Apply[Max,Append[Map[ExpnType,Apply[List,expn]],5]],
  If[AppellFunctionQ[Head[expn]],
    Apply[Max,Append[Map[ExpnType,Apply[List,expn]],6]],
  If[Head[expn]===RootSum,
    Apply[Max,Append[Map[ExpnType,Apply[List,expn]],7]],
  If[Head[expn]===Integrate || Head[expn]===Int,
    Apply[Max,Append[Map[ExpnType,Apply[List,expn]],8]],
  9]]]]]]]]]]


ElementaryFunctionQ[func_] :=
  MemberQ[{
  Exp,Log,
  Sin,Cos,Tan,Cot,Sec,Csc,
  ArcSin,ArcCos,ArcTan,ArcCot,ArcSec,ArcCsc,
  Sinh,Cosh,Tanh,Coth,Sech,Csch,
  ArcSinh,ArcCosh,ArcTanh,ArcCoth,ArcSech,ArcCsch
},func]


SpecialFunctionQ[func_] :=
  MemberQ[{
  Erf, Erfc, Erfi,
  FresnelS, FresnelC,
```

```
  ExpIntegralE, ExpIntegralEi, LogIntegral,
  SinIntegral, CosIntegral, SinhIntegral, CoshIntegral,
  Gamma, LogGamma, PolyGamma,
  Zeta, PolyLog, ProductLog,
  EllipticF, EllipticE, EllipticPi
},func]


HypergeometricFunctionQ[func_] :=
  MemberQ[{Hypergeometric1F1,Hypergeometric2F1,HypergeometricPFQ},func]


AppellFunctionQ[func_] :=
  MemberQ[{AppellF1},func]
```

4.2.2 Maple grading function

```
# File: GradeAntiderivative.mpl
# Original version thanks to Albert Rich emailed on 03/21/2017

#Nasser 03/22/2017  Use Maple leaf count instead since buildin
#Nasser 03/23/2017  missing 'ln' for ElementaryFunctionQ added
#Nasser 03/24/2017  corrected the check for complex result
#Nasser 10/27/2017  check for leafsize and do not call ExpnType()
#                   if leaf size is "too large". Set at 500,000
#Nasser 12/22/2019  Added debug flag, added 'dilog' to special functions
#                   see problem 156, file Apostol_Problems
#Nasser 4/07/2022   add second output which gives reason for the grade

GradeAntiderivative := proc(result,optimal)
local leaf_count_result,
        leaf_count_optimal,
        ExpnType_result,
        ExpnType_optimal,
        debug:=false;

        leaf_count_result:=leafcount(result);
        #do NOT call ExpnType() if leaf size is too large. Recursion problem
        if leaf_count_result > 500000 then
            return "B","result has leaf size over 500,000. Avoiding possible recursion issues
        fi;

        leaf_count_optimal := leafcount(optimal);
        ExpnType_result  := ExpnType(result);
        ExpnType_optimal := ExpnType(optimal);
```

```
        if debug then
            print("ExpnType_result",ExpnType_result," ExpnType_optimal=",ExpnType_optimal);
        fi;

# If result and optimal are mathematical expressions,
#  GradeAntiderivative[result,optimal] returns
#   "F" if the result fails to integrate an expression that
#       is integrable
#   "C" if result involves higher level functions than necessary
#   "B" if result is more than twice the size of the optimal
#       antiderivative
#   "A" if result can be considered optimal

    #This check below actually is not needed, since I only
    #call this grading only for passed integrals. i.e. I check
    #for "F" before calling this. But no harm of keeping it here.
    #just in case.


    if not type(result,freeof('int')) then
        return "F","Result contains unresolved integral";
    fi;


    if ExpnType_result<=ExpnType_optimal then
        if debug then
             print("ExpnType_result<=ExpnType_optimal");
        fi;
        if is_contains_complex(result) then
            if is_contains_complex(optimal) then
                if debug then
                        print("both result and optimal complex");
                fi;
                if leaf_count_result<=2*leaf_count_optimal then
                    return "A","";
                else
                   return "B",cat("Both result and optimal contain complex but leaf count of re
                                   convert(leaf_count_result,string)," vs. $2 (",
                                   convert(leaf_count_optimal,string)," ) = ",convert(2*leaf_co
                end if
            else #result contains complex but optimal is not
                if debug then
                        print("result contains complex but optimal is not");
                fi;
                return "C","Result contains complex when optimal does not.";
            fi;
        else # result do not contain complex
```

```
             # this assumes optimal do not as well. No check is needed here.
            if debug then
                   print("result do not contain complex, this assumes optimal do not as well"
            fi;
            if leaf_count_result<=2*leaf_count_optimal then
                if debug then
                    print("leaf_count_result<=2*leaf_count_optimal");
                fi;
                return "A","";
            else
                if debug then
                    print("leaf_count_result>2*leaf_count_optimal");
                fi;
                return "B",cat("Leaf count of result is larger than twice the leaf count of o
                               convert(leaf_count_result,string),"$ vs. $2(",
                               convert(leaf_count_optimal,string),")=",convert(2*leaf_cou
            fi;
        fi;
    else #ExpnType(result) > ExpnType(optimal)
        if debug then
            print("ExpnType(result) > ExpnType(optimal)");
        fi;
        return "C",cat("Result contains higher order function than in optimal. Order ",
                       convert(ExpnType_result,string)," vs. order ",
                       convert(ExpnType_optimal,string),".");
    fi;

end proc:

#
# is_contains_complex(result)
# takes expressions and returns true if it contains "I" else false
#
#Nasser 032417
is_contains_complex:= proc(expression)
  return (has(expression,I));
end proc:

# The following summarizes the type number assigned an expression
# based on the functions it involves
# 1 = rational function
# 2 = algebraic function
# 3 = elementary function
# 4 = special function
# 5 = hyperpergeometric function
# 6 = appell function
# 7 = rootsum function
```

```
# 8 = integrate function
# 9 = unknown function

ExpnType := proc(expn)
  if type(expn,'atomic') then
    1
  elif type(expn,'list') then
    apply(max,map(ExpnType,expn))
  elif type(expn,'sqrt') then
    if type(op(1,expn),'rational') then
       1
    else
       max(2,ExpnType(op(1,expn)))
    end if
  elif type(expn,'`^`') then
    if type(op(2,expn),'integer') then
      ExpnType(op(1,expn))
    elif type(op(2,expn),'rational') then
      if type(op(1,expn),'rational') then
         1
      else
         max(2,ExpnType(op(1,expn)))
      end if
    else
         max(3,ExpnType(op(1,expn)),ExpnType(op(2,expn)))
    end if
  elif type(expn,'`+`') or type(expn,'`*`') then
    max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
  elif ElementaryFunctionQ(op(0,expn)) then
    max(3,ExpnType(op(1,expn)))
  elif SpecialFunctionQ(op(0,expn)) then
    max(4,apply(max,map(ExpnType,[op(expn)])))
  elif HypergeometricFunctionQ(op(0,expn)) then
    max(5,apply(max,map(ExpnType,[op(expn)])))
  elif AppellFunctionQ(op(0,expn)) then
    max(6,apply(max,map(ExpnType,[op(expn)])))
  elif op(0,expn)='int' then
    max(8,apply(max,map(ExpnType,[op(expn)]))) else
  9
  end if
end proc:


ElementaryFunctionQ := proc(func)
  member(func,[
        exp,log,ln,
        sin,cos,tan,cot,sec,csc,
```

```
        arcsin,arccos,arctan,arccot,arcsec,arccsc,
        sinh,cosh,tanh,coth,sech,csch,
        arcsinh,arccosh,arctanh,arccoth,arcsech,arccsch])
end proc:

SpecialFunctionQ := proc(func)
  member(func,[
        erf,erfc,erfi,
        FresnelS,FresnelC,
        Ei,Ei,Li,Si,Ci,Shi,Chi,
        GAMMA,lnGAMMA,Psi,Zeta,polylog,dilog,LambertW,
        EllipticF,EllipticE,EllipticPi])
end proc:

HypergeometricFunctionQ := proc(func)
  member(func,[Hypergeometric1F1,hypergeom,HypergeometricPFQ])
end proc:

AppellFunctionQ := proc(func)
  member(func,[AppellF1])
end proc:

# u is a sum or product.  rest(u) returns all but the
# first term or factor of u.
rest := proc(u) local v;
  if nops(u)=2 then
     op(2,u)
  else
     apply(op(0,u),op(2..nops(u),u))
  end if
end proc:

#leafcount(u) returns the number of nodes in u.
#Nasser 3/23/17  Replaced by build-in leafCount from package in Maple
leafcount := proc(u)
   MmaTranslator[Mma][LeafCount](u);
end proc:
```

4.2.3 Sympy grading function

```
#Dec 24, 2019. Nasser M. Abbasi:
#            Port of original Maple grading function by
#            Albert Rich to use with Sympy/Python
#Dec 27, 2019  Nasser. Added `RootSum`. See problem 177, Timofeev file
#            added 'exp_polar'
from sympy import *

def leaf_count(expr):
   #sympy do not have leaf count function. This is approximation
   return round(1.7*count_ops(expr))

def is_sqrt(expr):
   if isinstance(expr,Pow):
      if expr.args[1] == Rational(1,2):
         return True
      else:
         return False
   else:
      return False

def is_elementary_function(func):
   return func in [exp,log,ln,sin,cos,tan,cot,sec,csc,
         asin,acos,atan,acot,asec,acsc,sinh,cosh,tanh,coth,sech,csch,
         asinh,acosh,atanh,acoth,asech,acsch
      ]

def is_special_function(func):
   return func in [ erf,erfc,erfi,
          fresnels,fresnelc,Ei,Ei,Li,Si,Ci,Shi,Chi,
          gamma,loggamma,digamma,zeta,polylog,LambertW,
          elliptic_f,elliptic_e,elliptic_pi,exp_polar
       ]

def is_hypergeometric_function(func):
   return func in [hyper]

def is_appell_function(func):
   return func in [appellf1]

def is_atom(expn):
   try:
      if expn.isAtom or isinstance(expn,int) or isinstance(expn,float):
        return True
      else:
        return False
```

```
    except AttributeError as error:
        return False

def expnType(expn):
    debug=False
    if debug:
        print("expn=",expn,"type(expn)=",type(expn))

    if is_atom(expn):
       return 1
    elif isinstance(expn,list):
        return max(map(expnType, expn))   #apply(max,map(ExpnType,expn))
    elif  is_sqrt(expn):
        if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
            return 1
        else:
            return max(2,expnType(expn.args[0]))  #max(2,ExpnType(op(1,expn)))
    elif isinstance(expn,Pow):   #type(expn,'`^`')
        if isinstance(expn.args[1],Integer):  #type(op(2,expn),'integer')
            return expnType(expn.args[0])   #ExpnType(op(1,expn))
        elif isinstance(expn.args[1],Rational):  #type(op(2,expn),'rational')
            if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
                return 1
            else:
                return max(2,expnType(expn.args[0]))  #max(2,ExpnType(op(1,expn)))
        else:
            return max(3,expnType(expn.args[0]),expnType(expn.args[1])) #max(3,ExpnType(op(1,expn)),ExpnT
    elif isinstance(expn,Add) or isinstance(expn,Mul): #type(expn,'`+`') or type(expn,'`*`')
        m1 = expnType(expn.args[0])
        m2 = expnType(list(expn.args[1:]))
        return max(m1,m2)  #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
    elif is_elementary_function(expn.func):  #ElementaryFunctionQ(op(0,expn))
        return max(3,expnType(expn.args[0]))  #max(3,ExpnType(op(1,expn)))
    elif is_special_function(expn.func): #SpecialFunctionQ(op(0,expn))
        m1 = max(map(expnType, list(expn.args)))
        return max(4,m1)   #max(4,apply(max,map(ExpnType,[op(expn)])))
    elif is_hypergeometric_function(expn.func): #HypergeometricFunctionQ(op(0,expn))
        m1 = max(map(expnType, list(expn.args)))
        return max(5,m1)   #max(5,apply(max,map(ExpnType,[op(expn)])))
    elif is_appell_function(expn.func):
        m1 = max(map(expnType, list(expn.args)))
        return max(6,m1)   #max(5,apply(max,map(ExpnType,[op(expn)])))
    elif isinstance(expn,RootSum):
        m1 = max(map(expnType, list(expn.args))) #Apply[Max,Append[Map[ExpnType,Apply[List,expn]],7]],
        return max(7,m1)
    elif str(expn).find("Integral") != -1:
```

```
        m1 = max(map(expnType, list(expn.args)))
        return max(8,m1)    #max(5,apply(max,map(ExpnType,[op(expn)])))
    else:
        return 9

#main function
def grade_antiderivative(result,optimal):

    #print ("Enter grade_antiderivative for sagemath")
    #print("Enter grade_antiderivative, result=",result," optimal=",optimal)

    leaf_count_result  = leaf_count(result)
    leaf_count_optimal = leaf_count(optimal)

    #print("leaf_count_result=",leaf_count_result)
    #print("leaf_count_optimal=",leaf_count_optimal)

    expnType_result  = expnType(result)
    expnType_optimal = expnType(optimal)

    if str(result).find("Integral") != -1:
        grade = "F"
        grade_annotation =""
    else:
        if expnType_result <= expnType_optimal:
            if result.has(I):
                if optimal.has(I): #both result and optimal complex
                    if leaf_count_result <= 2*leaf_count_optimal:
                        grade = "A"
                        grade_annotation =""
                    else:
                        grade = "B"
                        grade_annotation ="Both result and optimal contain complex but leaf count of result is larger
                else: #result contains complex but optimal is not
                    grade = "C"
                    grade_annotation ="Result contains complex when optimal does not."
            else: # result do not contain complex, this assumes optimal do not as well
                if leaf_count_result <= 2*leaf_count_optimal:
                    grade = "A"
                    grade_annotation =""
                else:
                    grade = "B"
                    grade_annotation ="Leaf count of result is larger than twice the leaf count of optimal. "+str(lea
        else:
            grade = "C"
            grade_annotation ="Result contains higher order function than in optimal. Order "+str(ExpnType_re
```

```
    #print("Before returning. grade=",grade, " grade_annotation=",grade_annotation)

    return grade, grade_annotation
```

4.2.4 SageMath grading function

```
#Dec 24, 2019. Nasser: Ported original Maple grading function by
#           Albert Rich to use with Sagemath. This is used to
#           grade Fricas, Giac and Maxima results.
#Dec 24, 2019. Nasser: Added 'exp_integral_e' and 'sng', 'sin_integral'
#           'arctan2','floor','abs','log_integral'
#June 4, 2022  Made default grade_annotation "none" instead of "" due
#           issue later when reading the file.
#July 14, 2022. Added ellipticF. This is until they fix sagemath, then remove it.

from sage.all import *
from sage.symbolic.operators import add_vararg, mul_vararg

debug=False;

def tree_size(expr):
    r"""
    Return the tree size of this expression.
    """
    #print("Enter tree_size, expr is ",expr)

    if expr not in SR:
        # deal with lists, tuples, vectors
        return 1 + sum(tree_size(a) for a in expr)
    expr = SR(expr)
    x, aa = expr.operator(), expr.operands()
    if x is None:
        return 1
    else:
        return 1 + sum(tree_size(a) for a in aa)

def is_sqrt(expr):
    if expr.operator() == operator.pow:   #isinstance(expr,Pow):
        if expr.operands()[1]==1/2: #expr.args[1] == Rational(1,2):
            if debug: print ("expr is sqrt")
            return True
        else:
            return False
    else:
        return False
```

```
def is_elementary_function(func):
   #debug=False
   m = func.name() in ['exp','log','ln',
         'sin','cos','tan','cot','sec','csc',
         'arcsin','arccos','arctan','arccot','arcsec','arccsc',
         'sinh','cosh','tanh','coth','sech','csch',
         'arcsinh','arccosh','arctanh','arccoth','arcsech','arccsch','sgn',
      'arctan2','floor','abs'
      ]
   if debug:
      if m:
         print ("func ", func , " is elementary_function")
      else:
         print ("func ", func , " is NOT elementary_function")


   return m

def is_special_function(func):
   #debug=False
   if debug:
      print ("type(func)=", type(func))

   m= func.name() in ['erf','erfc','erfi','fresnel_sin','fresnel_cos','Ei',
        'Ei','Li','Si','sin_integral','Ci','cos_integral','Shi','sinh_integral'
        'Chi','cosh_integral','gamma','log_gamma','psi,zeta',
        'polylog','lambert_w','elliptic_f','elliptic_e','ellipticF',
        'elliptic_pi','exp_integral_e','log_integral']

   if debug:
      print ("m=",m)
      if m:
         print ("func ", func ," is special_function")
      else:
         print ("func ", func ," is NOT special_function")


   return m


def is_hypergeometric_function(func):
   return func.name() in ['hypergeometric','hypergeometric_M','hypergeometric_U']

def is_appell_function(func):
   return func.name() in ['hypergeometric']   #[appellf1] can't find this in sagemath
```

```
def is_atom(expn):

   #debug=False
   if debug:
       print ("Enter is_atom, expn=",expn)

   if not hasattr(expn, 'parent'):
      return False


   #thanks to answer at https://ask.sagemath.org/question/49179/what-is-sagemath-equivalent-to-atomic-
   try:
      if expn.parent() is SR:
         return expn.operator() is None
      if expn.parent() in (ZZ, QQ, AA, QQbar):
         return expn in expn.parent() # Should always return True
      if hasattr(expn.parent(),"base_ring") and hasattr(expn.parent(),"gens"):
         return expn in expn.parent().base_ring() or expn in expn.parent().gens()

      return False

   except AttributeError as error:
      print("Exception,AttributeError in  is_atom")
      print ("cought exception" , type(error).__name__ )
      return False


def expnType(expn):

   if debug:
      print (">>>>>Enter expnType, expn=", expn)
      print (">>>>>is_atom(expn)=", is_atom(expn))

   if is_atom(expn):
      return 1
   elif type(expn)==list:   #isinstance(expn,list):
      return max(map(expnType, expn))    #apply(max,map(ExpnType,expn))
   elif  is_sqrt(expn):
      if  type(expn.operands()[0])==Rational:  #type(isinstance(expn.args[0],Rational):
         return 1
      else:
         return max(2,expnType(expn.operands()[0]))   #max(2,expnType(expn.args[0]))
   elif expn.operator() == operator.pow:    #isinstance(expn,Pow)
      if type(expn.operands()[1])==Integer:   #isinstance(expn.args[1],Integer)
         return expnType(expn.operands()[0])    #expnType(expn.args[0])
      elif type(expn.operands()[1])==Rational:   #isinstance(expn.args[1],Rational)
         if type(expn.operands()[0])==Rational:  #isinstance(expn.args[0],Rational)
```

```
            return 1
        else:
            return max(2,expnType(expn.operands()[0]))   #max(2,expnType(expn.args[0]))
    else:
        return max(3,expnType(expn.operands()[0]),expnType(expn.operands()[1]))  #max(3,expnType(expn.op
elif expn.operator() == add_vararg or expn.operator() == mul_vararg: #isinstance(expn,Add) or isinstan
    m1 = expnType(expn.operands()[0]) #expnType(expn.args[0])
    m2 = expnType(expn.operands()[1:]) #expnType(list(expn.args[1:]))
    return max(m1,m2)   #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
elif is_elementary_function(expn.operator()):   #is_elementary_function(expn.func)
    return max(3,expnType(expn.operands()[0]))
elif is_special_function(expn.operator()): #is_special_function(expn.func)
    m1 = max(map(expnType, expn.operands()))       #max(map(expnType, list(expn.args)))
    return max(4,m1)    #max(4,m1)
elif is_hypergeometric_function(expn.operator()): #is_hypergeometric_function(expn.func)
    m1 = max(map(expnType, expn.operands()))       #max(map(expnType, list(expn.args)))
    return max(5,m1)    #max(5,m1)
elif is_appell_function(expn.operator()):
    m1 = max(map(expnType, expn.operands()))       #max(map(expnType, list(expn.args)))
    return max(6,m1)    #max(6,m1)
elif str(expn).find("Integral") != -1: #this will never happen, since it
        #is checked before calling the grading function that is passed.
        #but kept it here.
    m1 = max(map(expnType, expn.operands()))       #max(map(expnType, list(expn.args)))
    return max(8,m1)    #max(5,apply(max,map(ExpnType,[op(expn)])))
else:
    return 9

#main function
def grade_antiderivative(result,optimal):


    if debug:
        print ("Enter grade_antiderivative for sagemath")
        print("Enter grade_antiderivative, result=",result)
        print("Enter grade_antiderivative, optimal=",optimal)
        print("type(anti)=",type(result))
        print("type(optimal)=",type(optimal))

    leaf_count_result  = tree_size(result) #leaf_count(result)
    leaf_count_optimal = tree_size(optimal) #leaf_count(optimal)

    #if debug: print ("leaf_count_result=", leaf_count_result, "leaf_count_optimal=",leaf_count_optimal)


    expnType_result  = expnType(result)
    expnType_optimal = expnType(optimal)
```

```
if debug: print ("expnType_result=", expnType_result, "expnType_optimal=",expnType_optimal)

if expnType_result <= expnType_optimal:
    if result.has(I):
        if optimal.has(I): #both result and optimal complex
            if leaf_count_result <= 2*leaf_count_optimal:
                grade = "A"
                grade_annotation ="none"
            else:
                grade = "B"
                grade_annotation ="Both result and optimal contain complex but leaf count of result is larger t
        else: #result contains complex but optimal is not
            grade = "C"
            grade_annotation ="Result contains complex when optimal does not."
    else: # result do not contain complex, this assumes optimal do not as well
        if leaf_count_result <= 2*leaf_count_optimal:
            grade = "A"
            grade_annotation ="none"
        else:
            grade = "B"
            grade_annotation ="Leaf count of result is larger than twice the leaf count of optimal. "+str(leaf_
else:
    grade = "C"
    grade_annotation ="Result contains higher order function than in optimal. Order "+str(expnType_resu


print("Before returning. grade=",grade, " grade_annotation=",grade_annotation)

return grade, grade_annotation
```