

Computer Algebra Independent Integration Tests

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October 14, 2017 compiled on — Saturday October 14, 2017 at 02:00 PM [public]

These reports and the web pages themselves are written in \LaTeX using TeXLive distribution on Linux and compiled to HTML using TeX4ht.

Lite CAS integration test applied to compare different versions of same system

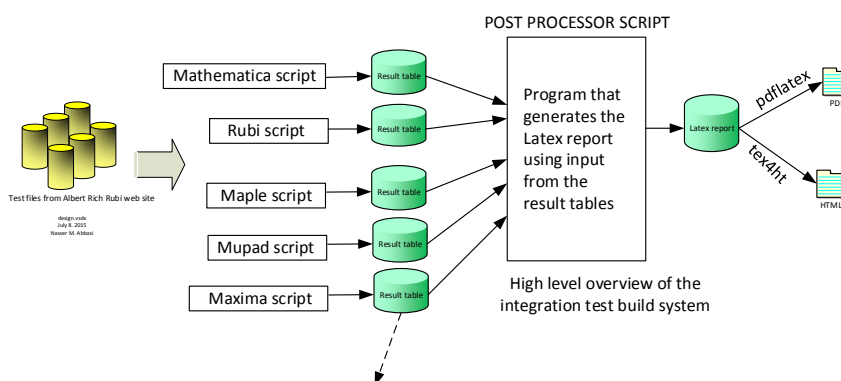
1. Mathematica (In progress) This zip file contains the raw input tests used which was obtained from Rubi web site.
2. Rubi (In progress) Uses same zip file as above for input.
3. Maple (Not started) This zip file contains the raw input tests used which was obtained from Rubi web site.

Full CAS integration test applied to compare different systems on same test

1. Rubi 4.13, Mathematica 11.2, Maple 2017.2 [66746 integrals. Done] Started on Sept 17,2017. Completed on Sept 28, 2017.
2. Rubi 4.11, Mathematica 11.1.1, Maple 2017.1 [63,648 integrals. Done]
Due to slow computation time with sympy and to a lesser extent mupad, I will not be including sympy and mupad for the time being in future builds of the test cases. The build below includes sympy and mupad for the first 16 test cases.
3. Rubi 4.11, Mathematica 11.1, Maple 2017, Mupad 7.0, Sympy 1.0 [9615 integrals. Done]
4. Rubi 4.9.8, Mathematica 11.0, Maple 2016 and Mupad 7.0 (Matlab 2016a) [58,469 integrals. Done]
5. Rubi 4.9, Mathematica 10.4, Maple 2016 and Mupad 7.0 (Matlab 2016a) [58,469 integrals. Done]

1 Note on build system

The following diagram gives a high level view of the current test build system.



One record (line) per one integral result. The line is comma delimited. It contains 12 fields. This is description of each record (line)

1. integer. the problem number.
2. integer. 0 or 1 for failed or passed. (this is not the grade field)
3. integer. Leaf size of result.
4. integer. Leaf size of the optimal antiderivative.
5. number. CPU time used to solve this integral. 0 if failed.
6. string. The integral in Latex format
7. string. The input used in CAS own syntx.
8. string. The result (antiderivative) produced by CAS in Latex format
9. string. The optimal antiderivative in Latex format.
10. integer. 0 or 1. Indicates if problem has known antiderivative or not
11. String. The result (antiderivative) in CAS own syntax.
12. String. The grade of the antiderivative. Can be "A", "B", "C", or "F"

The following are the steps to run one test suite

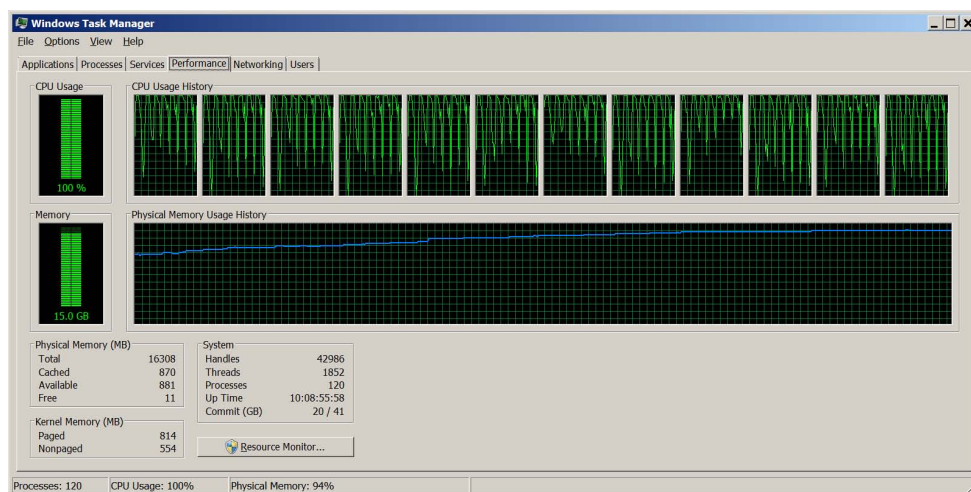
1. open Maple and run `convert_maple_to_sympy.mw` This translates all Maple input files to sympy syntax. This needs to be done once only. This coverts all Maple (177) test files to sympy syntax.

2. load Rubi package
3. open main.nb and definitions.nb. Evaluate definitions.nb. Then in main.nb, increment counter to run the test number (under RUN THE TESTS). This will run both Mathematica and Rubi test and grade and create the result tables in the test folder.
4. In main.nb, increment counter for Rubi rules and run. This will create Rubi rules used for each integral.
5. Now run Maple. open master_file_maple.mw and adjust the counter to same test number and evaluate. This will create Maple result table and will also call grading function to grade the result. This uses `GradeAntiderivative.mpl`
6. remove all comments from Maple input files before the next step, since mupad does not like Maple comments. Use the command

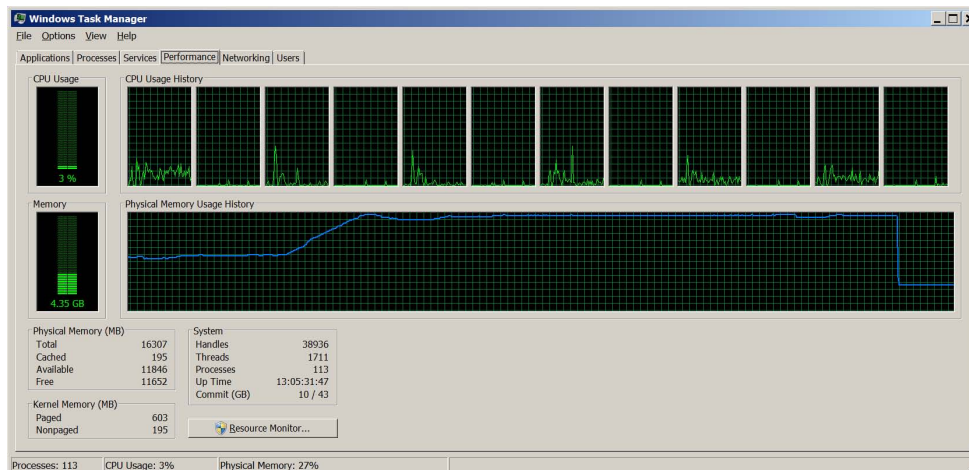

```
grep -v '^ *#' file_name.txt > new_file.txt
mv new_file.txt file_name.txt
```
7. Now open Matlab and load mupad.mn and increment the counter to same test number and run it. This will create mupad result table.
8. Open Maple again and load grade_mupad.mw and adjust the counter to the test number. Before running this, make sure to backup mupad result table file. Now run it. This will read mupad result table and grade it.
9. Edit `sympy_main.py` which is the Python driver to run the sympy tests and adjust the counter, then type (on Linux only) `python sympy_main.py` This will create sympy result table. Wait few days for this to complete.
10. Now go back to main.nb and run command `makeReportLatexDriver[n]` where n is the test number. This will create the test report Latex document. Then run `makeIndexLatexReportDriver[m]` command, where m is the total completed tests so far. This will build the main index latex document.
11. Now compile everything on Linux using the command `CAS_integration_tests>make -I$HOME all`
12. after many hrs it should be done.
13. When build is done, upload to site.

2 My PC during running the tests

I really need a faster PC with much more RAM !



This below shows example of CAS suddenly consuming all RAM in PC, and I had to terminate the process, since it did not time out as instructed, and just hanged.



3 cheat sheet notes

3.1 Fricas

To use Fricas online, go to <http://axiom-wiki.newsynthesis.org/FriCASIntegration> Go to bottom of page, type

```
\begin{axiom}
setSimplifyDenomsFlag(true)
integrate(sin(x),x)
\end{axiom}
```

Then click the preview button
For Fricas, use these commands to get 1D plain text output

```
setSimplifyDenomsFlag(true)
)set output algebra on
ii:=integrate(1/(x*(3*x^2 - 6*x + 4)^(1/3)),x);
unparse(ii::InputForm)
```

Otherwise the output will go to console in 2D. To get Latex output do

```
setSimplifyDenomsFlag(true)
)set output algebra off
)set output tex on
s:=asin(sqrt(1-x^2))/sqrt(1-x^2);
ii:=integrate(s,x)
```

And this will give

$$(19) \quad \frac{\arcsin\left(\sqrt{-x^2+1}\right)^2}{2}$$

To record console session to file, use (from <https://github.com/daly/axiom/blob/master/faq>)

```
)spool filename
starts sending output to the file called filename
)spool )off
stops sending output to the file
```

To send Latex output to file do

```
)set output tex on
)set output tex filename
```

To turn off, just do)set output tex off. Make sure to tex on first. To send back to console, do)set output tex console

To make record

```
)clear prop r
r: Record(a: String,b: Integer)
r:=["hello",10]
```

Some hints below thanks to Waldek Hebisch <http://mathforum.org/kb/message.jspa?messageID=9791385>

copied here so easy for me to get to:

1. How to measure CPU time used from the int call?

(3) ->)set messages time on

(3) -> integrate(x^(3/2)/sqrt(1 + x^5), x)

Type: Union(Expression(Integer),...)

Time: 0.06 (EV) + 0.00 (OT) = 0.06 sec

That is command ')set messages time on' tell FriCAS to print time needed to execute following command. The (EV) part means actual computation (OT) printing and at the end there is total

2. How to measure leaf count/size of result? (Maple and Mathematica have build in function to do this)

That is a bit tricky. FriCAS (like Axiom) has quite different representation of expressions than Maple or Mathematica.

In FriCAS expression is a quotient of two polynomials, with variables being kernels:

(13) -> f := exp(x^3 + 1/x) + 1

(14) -> numer(f)

```
4
x + 1
-----
x
```

(15) -> denom(f)

(16) -> variables(numer(f))

```
4
x + 1
-----
x
```

(16) [%e]

Type: List(Kernel(Expression(Integer)))

Time: 0.00 (OT) = 0.00 sec

From FriCAS point of view natural measure of size is number of monomials in numerator and denominator:

(17) -> numberOfMonomials(numer(f))

(17) 2

(18) -> numberOfMonomials(denom(f))

(18) 1

but this may underestimate size because kernels may be big. Also internally given kernel is stored only once, but in printed output it may appear several times.

It is possible to traverse expression in somewhat tree like manner, so it is possible to give better approximation to say Maple result, but that would require investigating what Maple is doing. I personally never used Maple node count so I do not know if this is simple or if there are some traps.

3. How to check if int passed or failed? Aborted? nil result? etc..

integrate may produce an error (in particular it will do so if it can not decide if integral is elementary). Or may produce unevaluated integral. Or normal result. At programistic level it is possible to catch errors, but a bit tricky, If you look at printed output, than errors are reasonably

easy to match via a regex:

```
(22) -> integrate(1/sqrt(exp(x) - x + 1), x)
integrate: implementation incomplete (constant residues)
```

the '>> Error' part indicates error. Unevaluated integrals always have integral sign at top level. FriCAS never returns partial results, so text match is relatively easy. Or you may use code like:

```
test_int(f) ==
res : Union(Expression Integer, LE)
res := integrate(f, 'x)
res0 : List Expression Integer :=
res case Expression Integer =>
[res::(Expression Integer)]@(List Expression Integer)
res case List Expression Integer =>
res::(List Expression Integer)
error "test_int: impossible 1"
for ri in res0 repeat
#(kernels ri) > 0 and is?(operator first kernels ri, 'integral) =>
print("Unevaluated integral"::OutputForm)
```

Note1: this is part extracted from bigger test script, I did not test it alone.

Note2: FriCAS may either return list of results or a single result. Middle part converts this to have always a list (typically of length 1). The last part is a loop so that all solutions can be examined. If you only want to know if result is evaluated, then loop is not needed: more than one result means that integral is evaluated.

Note3: In FriCAS testsuite I use a bit different test for evaluated integrals. Namely, FriCAS can do useful computations on unevaluated integrals and in particular unevaluated integrals may appear in the argument to integrate. Such unevaluated integrals of course may propagate from input to the output. The test above may misclassify such integral as unevaluated, while better test checks that unevaluated integral came from the input.

4. And most importantly, how to export the result (if it passed) to a plain text file in `_Latex_` format?

```
(24) -> )set output tex on
(24) -> integrate(exp(x)*exp(1/(exp(x)+1)-x), x)
```

Here one has to decide what to do with errors. Without error trapping error will abort currently executing function and propagate to top level (up to command line).

After doing:

```
)set break resume
```

after error FriCAS will continue executing file from next command (but still abort current command). If you need real loop then I can provide error catcher, but it is a bit more complicated than snippets above.

Waldek Hebisch

To get type of value in fricas do `typeOf(r)`

To clear everything do

```
)clear all
```

)clear completely

3.2 sympy

<http://docs.sympy.org/0.7.1/modules/integrals.html>

<http://docs.sympy.org/dev/tutorial/index.html>

To install python package do `conda install package-name` to update do `conda update package`
for example `conda update spyder`

To integrate the command is

```
from sympy import *
```

or

```
import sympy #but now have to add sympy. to each call
```

```
import os
os.getcwd()
os.chdir('X:\\data\\public_html\\my_notes\\CAS_integration_tests\\reports\\rubi_4_11\\code')
os.getcwd()
import math
init_printing()
init_printing(use_unicode=False, wrap_line=False, no_global=True)
x = symbols('x', real=True)
r=integrate(x,x)
r0=latex(r)
text_file = open("python.txt", "w")
text_file.write("%s\n" % r0)
text_file.close()
```

To check if integral fails?

```
r=integrate(f*g, (x, L/2, L))
type(r) is integrals.Integral
```

```
Out[41]: True
```

or

```
isinstance(r, integrals.Integral)
Out[48]: True
```

```
r=integrate(x,x)
type(r) is integrals.Integral
Out[43]: False
```

```
if isinstance(r, integrals.Integral):
    result = 0
else:
    result=1
```

To get cwd

```
os.getcwd()
```

To get list of folder in cwd do

```
os.listdir(os.getcwd())
```

or

```
ls
```

```
Out[85]:
['1_Algebraic_functions',
 '2_Exponentials',
 '3_Logarithms',
 '4_Trig_functions',
 '5_Inverse_trig_functions',
 '6_Hyperbolic_functions',
 '7_Inverse_hyperbolic_functions',
 '8_Special_functions',
```

```
'Independent_test_suites']

f = open('Hebisch_Problems.txt','r')
f.readline()
f.close()
```

how to do timeout? simple timeouts using `signal.alarm` module check <http://stackoverflow.com/questions/492519/timeout-on-a-function-call> for some code. There is also talk about it here <https://groups.google.com/forum/#!topic/sympy/qsPImy6WqcI> code from above is

```
def _timeout(self, function, timeout):
    def callback(x, y):
        signal.alarm(0)
        raise Skipped("Timeout")
    signal.signal(signal.SIGALRM, callback)
    signal.alarm(timeout) # Set an alarm with a given timeout
    function()
    signal.alarm(0) # Disable the alarm
```

elementary functions <http://docs.sympy.org/latest/modules/functions/elementary.html>
and <http://docs.sympy.org/dev/modules/functions/special.html>
and <http://docs.sympy.org/latest/modules/functions/index.html>
Need to change

```
AppellF1 --> #hypergeometric function of two variables
Ellipticpi-->
arctanh -->atanh
arctan --> atan
arccosh->acosh
Pi --> pi.
arcsin -> asin
arccos -> acos
hypergeom -> hyper,
arccoth -> acoth
GAMMA -> uppergamma()
arccsc -> acsc
arcsec -> asec
arccot -> acot,
EllipticF -> elliptic_f
EllipticE -> elliptic_e
Li -> Li
Si -> Si
Ci -> Ci
Ei -> Ei
FresnelS -> fresnels
FresnelC -> fresnelc
```

I also removed 4th field that contains `integrate(...)` in it as it hangs the reading of the input file.

To run python tests do

```
cd /media/data/public_html/my_notes/CAS_integration_tests/reports/rubi_4_11
python sympy_main.py
```

To add new test, or run more tests, edit `sympy_main.py` and change the line

```
for n in range(0,1): #change the last number to the number of tests to do
```

To update conda and python do

```
conda update conda
conda update python
```

To update sympy do

```
pip list | grep sympy
pip install --upgrade sympy
\end{x300}
```

To find version, from inside python, type
\begin{x300}
import sympy
sympy.__version__

from github <https://github.com/sympy/sympy/wiki/SymPy-vs.-Sage>

To obtain a Rational in SymPy, one of these methods must be used:

```
>>> from sympy import Rational
>>> Rational(2, 7)
2/7
```

In python/sympy, to loop using index 1, can use this:

```
>>> for num,val in enumerate(sol,start=1):
...     print("root number {} is {}".format(num,val))
```

For timeout in recent python, on windows, this seems to work

```
from subprocess import STDOUT, check_output
output = check_output('dir', shell=True, stderr=STDOUT, timeout=5)
print(output)
```