Physics 3041 (Spring 2021) Homework Set 3 (Due 2/10)

- 1. (a) Problem 5.2.3. (5 points)
- (b) Problem 5.2.4.(iv). (5 points)
- (c) Problem 5.2.5. (10 points)
- (d) Problem 5.3.2. (20 points)
- 2. (a) Problem 5.3.5. (10 points)
- (b) Problem 5.3.6. (10 points)

(c) Find $\int_0^\infty x e^{-ax} \cos kx dx$ using Euler's formula. (10 points)

3. Given the intensity pattern for the N-slit interference with separation d between adjacent slits, show that the pattern becomes that for the single-slit diffraction with slit width a when d goes to zero but with a fixed value of Nd = a. (10 points)

4. (1) Find the roots z_n $(n = 1, 2, \dots, N)$ of the complex equation $z^N = 1$. (5 points)

(2) Find $S_N = \sum_{n=1}^N z_n$ and give a geometric interpretation of the result. (10 points)

(3) Note that $1 - z^N = (1 - z)(1 + z + z^2 + \dots + z^{N-1})$. Relate this result and the roots z_n to the conditions for destructive interference among N slits. (5 points)