MAE91 Summer 2004 – Quiz 3 Dr. H. Susan Zhou

Closed book and notes - 20 minutes

Name: NASSER ABBASI ID:

For each of the following processes draw a P-v and T-v diagrams. If there is a stop in the problem, assume that the process hits the stop and continues. Diagrams all show initial or ambient state. (1 point per diagram)







Bonus Problem (2 points per diagram)



Multi-Stage Process

- Piston is pushed down to bottom stop while maintaining constant T.
- When piston reaches bottom stop force ceases and LARGE amount of heat is added to system.
- Pressure is now greater than initial pressure and pressure after compression.
- Piston then cools back to ambient conditions.



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Discussion Questions – Set #2

5.47

1. Problem Statement:

An insulated cylinder fitted with a piston contains R-12 at 25°C with a quality of 90% and a volume of 45 L. The piston is allowed to move, and the R-12 expands until it exists as saturated vapor. During this process the R-12 does 7.0 kJ of work against the piston. Determine the final temperature, assuming the process is adiabatic.



2. Assumptions and Givens:

Take C.V. to be the R-12 Process is adiabatic

<u>State 1:</u> T_1, x_1, V_1

<u>Process:</u> W_2 Work is done

State 2: x_2

Find: T_2

3. Fundamental Laws:

Continuity: $m_1 = m_2 = m$

Energy Equation (First Law):

$$U_2 - U_1 + \frac{m(\vec{V}_2^2 - \vec{V}_1^2)}{2} + mg(Z_2 - Z_1) = {}_1Q_2 - {}_1W_2$$

$$v = \frac{V}{m}$$
$$v = v_f + xv_{fg}$$
$$u = u_f + xu_{fg}$$

4. Steps:

This is an adiabatic process, with no change in kinetic or potential energy. So: $U_2 - U_1 = W_2$ $m(u_2 - u_1) = W_2$

Using Table B.1.1 and State 1:

$$T_{1}, x_{1} \Rightarrow v_{f1}, v_{g1}, v_{fg1}, u_{f1}, u_{g1}, u_{fg}$$

$$v_{1} = v_{f1} + x_{1}v_{fg1}$$

$$m = \frac{V_{1}}{v_{1}}$$

$$u_{1} = u_{f1} + x_{1}u_{fg1}$$

For State 2 we only know 1 independent property: so we apply the energy equation:

$$m(u_2 - u_1) = W_2 \Longrightarrow u_2$$
$$u_2 = u_g \text{ because } x_2 = 1$$

Now we have two independent properties so we can use table B.2.1 to find T_2

5. Numerical Substitution:

State 1: (T, x) Tabel B.3.1 => $v_1 = 0.000763 \pm 0.9 \times 0.02609 = 0.024244 \text{ m}^3/\text{kg}$ $m = V_1/v_1 = 0.045/0.024244 = 1.856 \text{ kg}$ $u_1 = 59.21 \pm 0.9 \times 121.03 = 168.137 \text{ kJ/kg}$

State 2: (x = 1, ?) We need one property information. $_1Q_2 = \emptyset = m(u_2 - u_1) + {}_1W_2 = 1.856 \times (u_2 - 168.137) + 7.0$ $=> u_2 = 164.365 \text{ kJ/kg} = u_g \text{ at } T_2$ Table B.3.1 gives u_g at different temperatures: $T_2 \cong -15^{\circ}\text{C}$ 5.57

1. Problem Statement:

A cylinder having a piston restrained by a linear spring (of spring constant 15 kN/m) contains 0.5 kg of saturated vapor water at 120° C, as shown in Fig. P5.57. Heat is transferred to the water, causing the piston to rise. If the piston cross-sectional area is 0.05 m^2 , and the pressure varies linearly with volume until a final pressure of 500 kPa is reached. Find the final temperature in the cylinder and the heat transfer for the process.



2. Assumptions and Givens:

C.V. is water in the cylinder <u>State 1:</u> T_1, x_1, k_s, A_p

 P_2

Process: Heat is transferred and the piston moves

State 2:

Find: $T_{2,1}Q_{2}$

3. Fundamental Laws:

Continuity: $m_1 = m_2 = m$

Energy Equation (First Law):

$$U_2 - U_1 + \frac{m(\bar{V}_2^2 - \bar{V}_1^2)}{2} + mg(Z_2 - Z_1) = Q_2 - W_2$$

4. Steps:

We can simplify the energy equation knowing that there is no KE or PE. $U_2 - U_1 = Q_2 - W_2$ $m(u_2 - u_1) = Q_2 - W_2$ Using Table B.1.1 and knowing two independent properties we can find: $T_1, x_1 \Rightarrow v_1 = v_{g1}, u_1 = u_{g1}$

From previous problems we know that for a spring attached to a piston:

$$P_2 = P_1 + \frac{k_s m}{A_p^2} (v_2 - v_1) \Longrightarrow v_2$$

Now we have two independent properties of state 2: $P_2, v_2 \Rightarrow v_1 = T_2, u_2$

Now that we have the final temperature to find the heat transfer we use the energy equation. In this case since the relationship between P and V is linear we can use the following to calculate the work:

$$_{1}W_{2} = |PdV = \frac{1}{2}(P_{1} + P_{2})m(v_{2} - v_{1})|$$

Therefore, we now have all the information to find the heat transfer: $_1Q_2 = m(u_2 - u_1) + _1W_2$

5. Numerical Substitution:

State 1: (T, x) Table B.1.1 => $v_1 = 0.89186 \text{ m}^3/\text{kg}$, $u_1 = 2529.2 \text{ kJ/kg}$ Process: $P_2 = P_1 + \frac{k_s m}{A_p^2} (v_2 - v_1) = 198.5 + \frac{15 \times 0.5}{(0.05)^2} (v_2 - 0.89186)$ State 2: $P_2 = 500 \text{ kPa}$ and on the process curve (see above equation). => $v_2 = 0.89186 \div (500 - 198.5) \times (0.05^2/7.5) = 0.9924 \text{ m}^3/\text{kg}$ (P, v) Table B.1.3 => $T_2 = 803^{\circ}\text{C}$; $u_2 = 3668 \text{ kJ/kg}$ $W_{12} = \int PdV = \left(\frac{P_1 + P_2}{2}\right) m(v_2 - v_1)$ $= \left(\frac{198.5 \pm 500}{2}\right) \times 0.5 \times (0.9924 - 0.89186) = 17.56 \text{ kJ}$

 ${}_{1}Q_{2} = m(u_{2} - u_{1}) + {}_{1}W_{2} = 0.5 \times (3668 - 2529.2) + 17.56 = 587 \text{ kJ}$

1. Problem Statement:

The cylinder volume below the constant loaded piston has two compartments A and B filled with water. A has 0.5 kg at 200 kPa, 150°C and B has 400 kPa with a quality of 50% and a volume of 0.1 m³. The valve is opened and heat is transferred so the water comes to a uniform state with a total volume of 1.006 m³.

- a) Find the total mass of water and the total initial volume.
- b) Find the work in the process
- c) Find the process heat transfer.



FIGURE PS.69

2. Assumptions and Givens:

CV is water in A and B

State 1A: State 1B: Process:	m_{1A}, P_{1A}, T_{1A} P_{1B}, x_{1B}, V_{1B} Heat is transferred and value is opened		

State 2: V_2

Find: See Problem statement

3. Fundamental Laws:

Continuity: $m_{1A} + m_{1B} = m_2 = m$

Energy Equation (First Law):

5.69

$$U_{2} - U_{1} + \frac{m(\vec{V}_{2}^{2} - \vec{V}_{1}^{2})}{2} + mg(Z_{2} - Z_{1}) = Q_{2} + W_{2}$$

$$v = \frac{V}{m}$$

$$v = v_{f} + xv_{fg}$$

$$u = u_{f} + xu_{fg}$$

4. Steps:

Simplifying the Energy equation gives us: $U_2 - U_1 = Q_2 - W_2$ $m_2 u_2 - (m_{1A}u_{1A} + m_{1B}u_{1B}) = Q_2 - W_2$ $m_2 u_2 - m_{1A}u_{1A} - m_{1B}u_{1B} = Q_2 - W_2$

a) If $V_2 > V_B$ then the piston will never hit the stops and P is constant.

Using Table B.1.3 we can find the properties of State 1A: $T_{1A}, P_{1A} \Rightarrow v_{1A}, u_{1A}$ $V_{1A} = m_{1A}v_{1A}$ $\therefore V_1 = V_{1A} + V_{1B}$ Now we can compare V_1 to V_2

Using Table B.1.2 we can find the properties of State 1B: $P_{1B}, x_{1B} \Rightarrow v_{1A}, u_{1A}$ using quality relationships $m_{1B} = V_{1B} / v_{1B}$ $\therefore m_{tot} = m_{1A} + m_{1B} = m_2$

 $\therefore v_2 = V_2 / m_2$

Now we can find out all the information about State 2, using table B.1.3 $P_2, v_2 \Rightarrow T_2, u_2$

b) Since the final volume is bigger than the initial volume, that means the piston floats so it is constant pressure. There the work is:

$$W_2 = |PdV = P\Delta V = P_{float}\Delta V = P_2(V_2 - V_1)$$

c) Finally, using the energy equation we solve for heat. $_1Q_2 = _1W_2 + m_2u_2 - m_{1A}u_{1A} - m_{1B}u_{1B}$

5. Numerical Substitution:

State A1: Sup. vap. Table B.1.3 $v = 0.95964 \text{ m}^3/\text{kg}$, u = 2576.9 kJ/kg $\Rightarrow V = mv = 0.5 \times 0.95964 = 0.47982$ State B1: Table B.1.2 $v = (1-x) \times 0.001084 + x \times 0.4625 = 0.2318 \text{ m}^3/\text{kg}$ $\Rightarrow m = V/v = 0.4314 \text{ kg}$ $u = 604.29 + 0.5 \times 1949.3 = 1578.9 \text{ kJ/kg}$ State 2: 200 kPa, $v_2 = V_2/m = 1.006/0.9314 = 1.0801 \text{ m}^3/\text{kg}$

Table B.1.3
$$\Rightarrow$$
 close to T₂ = 200°C and u₂ = 2654.4 kJ/kg

So now

$$V_1 = 0.47982 \pm 0.1 = 0.5798 \text{ m}^3$$
, $m_1 = 0.5 \pm 0.4314 = 0.9314 \text{ kg}$

Since volume at state 2 is larger than initial volume piston goes up and the pressure then is constant (200 kPa which floats piston).

$$W_2 = \int P dV = P_{\text{lift}} (V_2 - V_1) = 200 (1.006 - 0.57982) = 85.24 \text{ kJ}$$

$$\label{eq:Q2} \begin{split} _1 Q_2 &= m_2 u_2 - m_{1A} u_{1A} - m_{1B} u_{1B} + {}_1 W_2 \\ &= 0.9314 \times 2654.4 - 0.5 \times 2576.9 - 0.4314 \times 1578.9 + 85.24 = 588 \ kJ \end{split}$$