HW 4 EE 409 (Linear Systems), CSUF spring 2010 Spring 2010 CSUF

Nasser M. Abbasi

Spring 2010 Compiled on January 31, 2019 at 12:46am

Contents

1 Problem 3.23 (a)

2

Date due and handed in March 18,2010

1 Problem 3.23 (a)

Write the state variable equation for the following

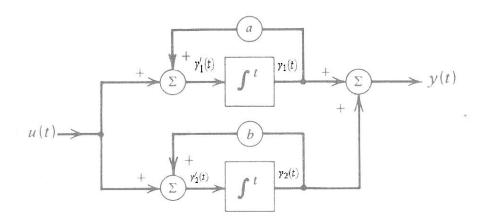


Figure 1: System description

Solution

Let $x_1(t)$ and $x_2(t)$ be the state variables. Hence from the diagram we see the following

$$x'_{1}(t) = ax_{1}(t) + u(t)$$
$$x'_{2}(t) = bx_{2}(t) + u(t)$$

And

$$y\left(t\right) = x_{1}\left(t\right) + x_{2}\left(t\right)$$

Hence

$$\begin{pmatrix} x_1'(t) \\ x_2'(t) \end{pmatrix} = \overbrace{\begin{pmatrix} a & 0 \\ 0 & b \end{pmatrix}}^A \begin{pmatrix} x_1(t) \\ x_2(t) \end{pmatrix} + \overbrace{\begin{pmatrix} 1 \\ 1 \end{pmatrix}}^B u(t)$$
$$y(t) = \overbrace{\begin{pmatrix} 1 & 1 \end{pmatrix}}^C \begin{pmatrix} x_1(t) \\ x_2(t) \end{pmatrix}$$