# HW 4 <br> EE 409 (Linear Systems), CSUF spring 2010 <br> Spring 2010 <br> CSUF 

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Write the state variable equation for the following


Figure 1: System description

## Solution

Let $x_{1}(t)$ and $x_{2}(t)$ be the state variables. Hence from the diagram we see the following

$$
\begin{aligned}
& x_{1}^{\prime}(t)=a x_{1}(t)+u(t) \\
& x_{2}^{\prime}(t)=b x_{2}(t)+u(t)
\end{aligned}
$$

And

$$
y(t)=x_{1}(t)+x_{2}(t)
$$

Hence

$$
\begin{aligned}
\binom{x_{1}^{\prime}(t)}{x_{2}^{\prime}(t)} & =\overbrace{\left(\begin{array}{ll}
a & 0 \\
0 & b
\end{array}\right)}^{A}\binom{x_{1}(t)}{x_{2}(t)}+\overbrace{\binom{1}{1}}^{B} u(t) \\
y(t) & =\overbrace{\left(\begin{array}{ll}
1 & 1
\end{array}\right)}^{C} \begin{array}{l}
\binom{x_{1}(t)}{x_{2}(t)}
\end{array}
\end{aligned}
$$

