Method of Characteristics - Practice Problems

Use the method of characteristics to solve the following initial value problems for t>0 and $-\infty < x < \infty$.

1.
$$u_t + 4u_x = 0$$
, and $u(x, 0) = e^{x^2}$.

2.
$$u_t + (xt)u_x = 0$$
, and $u(x, 0) = 2x$.

3.
$$u_t + (x \sin t)u_x = 0$$
, and $u(x, 0) = 1/(1 + x^2)$.

4.
$$u_t - (tx^2) u_x = 0$$
, and $u(x, 0) = 1 + x$.

5.
$$u_t - u_x = xu$$
, and $u(x, 0) = 2x$.