

Key

Drill prob. # 3.2)

$$s_{AM}(t) = A_c [1 + K_a m(t)] \cos 2\pi f_c t$$

where $m(t) = A_m \cos 2\pi f_m t$ sinusoidal modulating wave

$$s_{AM}(t) = A_c [1 + K_a A_m \cos 2\pi f_m t] \cos 2\pi f_c t \quad f_c \gg f_m$$

$$K_a A_m = 20\% = 0.2 \Rightarrow$$

$$s_{AM}(t) = A_c [1 + 0.2 \cos 2\pi f_m t] \cos 2\pi f_c t$$

$$= A_c \cos 2\pi f_c t + A_c M \cos 2\pi f_c t \cos 2\pi f_m t$$

$$= \underbrace{A_c \cos 2\pi f_c t}_{\text{carrier}} + \frac{A_c M}{2} \left\{ \underbrace{\cos[2\pi(f_c + f_m)t]}_{\text{U.S.B}} + \underbrace{\cos[2\pi(f_c - f_m)t]}_{\text{L.S.B}} \right\}$$

Thus: $P_c = \frac{A_c^2}{2}$

$$P_{USB} = P_{LSB} = \frac{\left(\frac{A_c M}{2}\right)^2}{2} = \frac{A_c^2 M^2}{8} = \frac{A_c^2 (0.2)^2}{8} = \frac{A_c^2}{200}$$

That is carrier has 98% of total power and each sideband has 1% the total power.

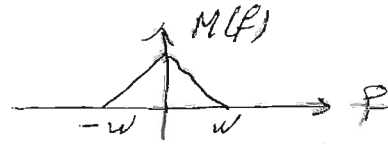
Drill prob. # 3.4)

$$a) \quad v_1(t) = A_c \cos 2\pi f_c t + m(t) \quad (1)$$

$$v_2(t) = a_1 v_1(t) + a_2 v_1^2(t) \quad (2)$$

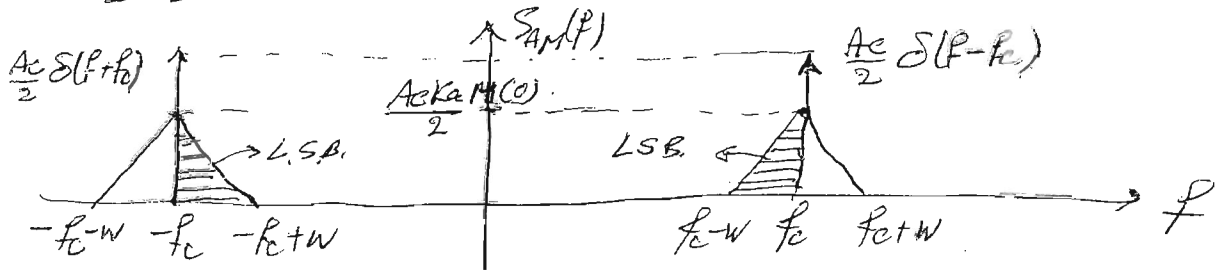
$$\Rightarrow v_2(t) = a_1 (A_c \cos 2\pi f_c t + m(t)) + a_2 (A_c \cos 2\pi f_c t + m(t))^2$$

Mill prob. # 3.3) Assume



In general $s_{AM}(t) = A_c [1 + K_a m(t)] \cos 2\pi f_c t$

$$S_{AM}(f) = \frac{A_c}{2} [\delta(f-f_c) + \delta(f+f_c)] + \frac{A_c K_a}{2} [M(f-f_c) + M(f+f_c)]$$



From the plot of $S_{AM}(f)$ we see that to avoid the overlapping of L.S.B frequencies it must

$$f_c - w > 0 \Rightarrow f_c > w$$

3.18)

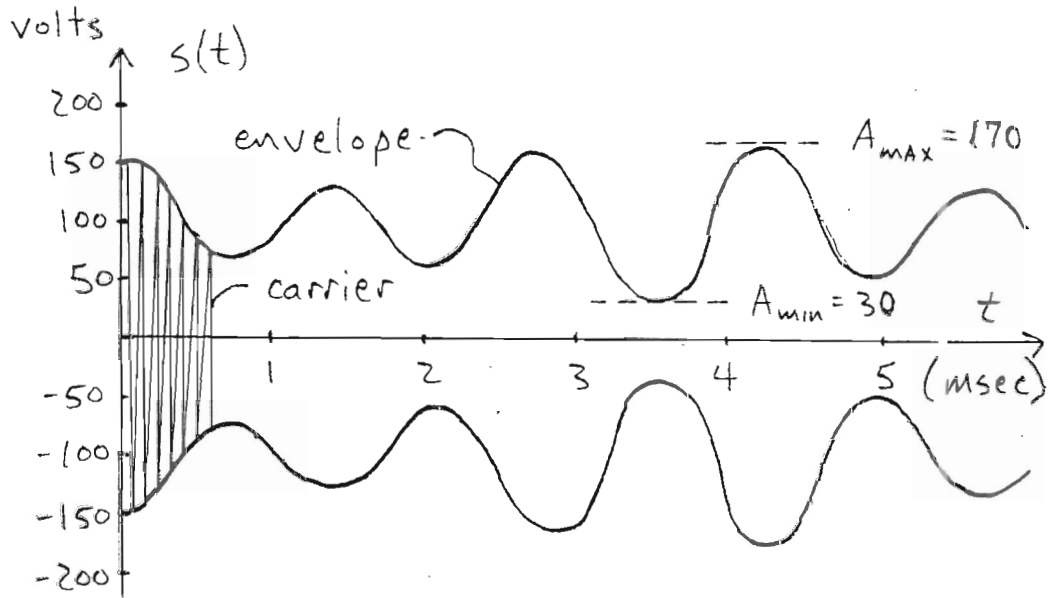
Given:

$$\begin{cases} m(t) = 20 \cos(2\pi t) \text{ volts} \\ c(t) = 50 \cos(100\pi t) \text{ volts} \\ \mu = A_m K_a = 75\% = 0.75 \\ R = 100 \Omega \end{cases}$$

$$\begin{aligned} b) \quad s_{AM}(t) &= A_c [1 + K_a m(t)] \cos 2\pi f_c t = 50 [1 + \underbrace{K_a \cdot 20}_{\mu} \cos 2\pi t] \cos 100\pi t \\ &= 50 \cos(100\pi t) + 50 \times 0.75 \cos(100\pi t) \cos(2\pi t) \\ &= 50 \cos(100\pi t) + \frac{37.5}{2} \{ \cos(102\pi t) + \cos(98\pi t) \} \end{aligned}$$

$$P_{tot} = \frac{(50)^2}{2R} + 2 \times \frac{(\frac{37.5}{2})^2}{2R} = \frac{2500}{200} + \frac{1406.25}{400} = 16.0156 \text{ watts}$$

5-2. (a.) Cont'd



$$(b.) \quad \frac{170 - 30}{2(100)} (100) = \underline{\underline{70\% \text{ modulation}}}$$

$$(c.) \quad G(f) = \delta(f) + m(f)$$

$$= \delta(f) - j \frac{(0.2)}{2} [\delta(f-f_1) - \delta(f+f_1)]$$

$$+ \frac{(0.5)}{2} [\delta(f-f_2) + \delta(f+f_2)]$$

$$S(f) = \frac{A_c}{2} [G(f-f_c) + G^*(-f-f_c)]$$

