### HW 7

## Electronic Communication Systems Fall 2008

## California State University, Fullerson

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#### 0.1 Questions

Book Coash? HW question. Used for HW's 7,8,9,10

ap. 5 Problems

$$(f_c)_{SSB} - f_1 = 7090 \text{ kHz} - 2.225 \text{ kHz} = 7087.775 \text{ kHz}$$

a space frequency (binary 0) of

$$(f_c)_{SSB} - f_2 = 7090 - 2.025 = 7087.975 \text{ kHz}$$

and a carrier frequency of

$$(f_c)_{FSK} = (f_c)_{SSB} - (f_c)_{Bell \ 103} = 7090 - 2.125 = 7087.875 \text{ kHz}$$

Consequently, the SSB transceiver would produce a FSK digital signal with a carrier frequency of 7087.875 kHz.

For the case of alternating data, the spectrum of this FSK signal is given by (5-85) and (5-86), where  $f_c = 7087.875$  kHz. The resulting spectral plot would be like that of Fig. 5-26a, where the spectrum is translated from  $f_c = 1170$  Hz to  $f_c = 7087.875$  kHz. It is also realized that this spectrum appears on the lower sideband of the SSB carrier frequency ( $f_c$ )<sub>SSB</sub> = 7090 kHz. If a DSB-SC transmitter had been used (instead of a LSSB transmitter), the spectrum would be replicated on the upper sideband as well as on the lower sideband, and two redundant FSK signals would be emitted.

For the case of random data, the PSD for the complex envelope is given by (5-90) and shown in Fig. 5-25 for the modulation index of h = 0.7. Using (5-2b), the PSD for the FSK signal is the translation of the PSD for the complex envelope to the carrier frequency of 7087.875 kHz.

- 5-1 An AM broadcast transmitter is tested by feeding the RF output into a 50-Ω (dummy) load. Tone modulation is applied. The carrier frequency is 850 kHz and the FCC licensed power output is 5000 W. The sinusoidal tone of 1000 Hz is set for 90% modulation.
  - (a) Evaluate the FCC power in dBk (dB above 1 kW) units.
  - (b) Write an equation for the voltage that appears across the 50-Ω load, giving numerical values for all constants.
  - (c) Sketch the spectrum of this voltage as it would appear on a calibrated spectrum analyzer.
  - (d) What is the average power that is being dissipated in the dummy load?
  - (e) What is the peak envelope power?
- An AM transmitter is modulated with an audio testing signal given by  $m(t) = 0.2 \sin \omega_1 t + 0.5 \cos \omega_2 t$ , where  $f_1 = 500 \text{ Hz}$ ,  $f_2 = 500 \sqrt{2} \text{ Hz}$ , and  $A_c = 100$ . Assume that the AM signal is fed into a 50- $\Omega$  load.
  - (a) Sketch the AM waveform.
  - (b) What is the modulation percentage?
  - (c) Evaluate and sketch the spectrum of the AM waveform.
- (5-3) For the AM signal given in Prob. 5-2:
  - (a) Evaluate the average power of the AM signal.
  - (b) Evaluate the PEP of the AM signal.
- 5-4 Assume that an AM transmitter is modulated with a video testing signal given by  $m(t) = -0.2 + 0.6 \sin \omega_1 t$  where  $f_1 = 3.57$  MHz. Let  $A_c = 100$ .

14 this Normalized poment

- (a) Sketch the AM waveform.
- (b) What is the percentage of positive and negative modulation?
  - ) Evaluate and sketch the spectrum of the AM waveform about  $f_c$ .

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A 50,000-W AM broadcast transmitter is being evaluated by means of a two-tone te transmitter is connected to a 50- $\Omega$  load and  $m(t) = A_1 \cos \omega_1 t + A_1 \cos 2\omega_1 t$   $f_1 = 500$  Hz. Assume that a perfect AM signal is generated.

- (a) Evaluate the complex envelope for the AM signal in terms of  $A_1$  and  $\omega_1$ .
- (b) Determine the value of  $A_1$  for 90% modulation.

Par = comi-

- (c) Find the values for the peak current and average current into the  $50-\Omega$  load for the  $90^{\circ}$  ulation case.
- 5-6 An AM transmitter uses a two-quadrant multiplier so that the transmitted signal is described. (5-7). Assume that the transmitter is modulated by  $m(t) = A_m \cos \omega_m t$ , where  $A_m$  is adjusted that 120% positive modulation is obtained. Evaluate the spectrum of this AM signal in  $A_c$ ,  $f_c$ , and  $f_m$ . Sketch your result.

A DSB-SC signal is modulated by  $m(t) = \cos \omega_1 t + 2 \cos 2\omega_1 t$  where  $\omega_1$   $f_1 = 500$  Hz, and  $A_c = 1$ .

- (a) Write an expression for the DSB-SC signal and sketch a picture of this waveform.
- (b) Evaluate and sketch the spectrum for this DSB-SC signal.
- (c) Find the value of the average (normalized) power
- (d) Find the value of the PEP (normalized).

Plane

Assume that transmitting circuitry restricts the modulated output signal to a certain persay  $A_p$ , because of power-supply voltages that are used and the peak voltage and current of the components. If a DSB-SC signal with a peak value of  $A_p$  is generated by this circuit that the sideband power of this DSB-SC signal is four times the sideband power of a ble AM signal having the same peak value,  $A_p$ , that could also be generated by this  $A_p$ .

A DSB-SC signal can be generated from two AM signals as shown in Fig. P5-9. Usi matics to describe signals at each point on the figure prove that the output is a DSB-

athenalis

Franky

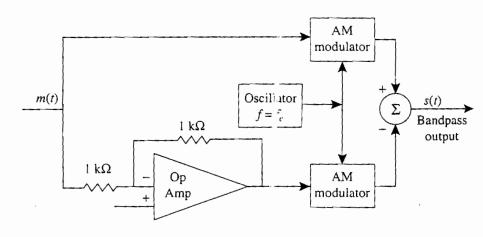


Figure P5-9

- 5-10 Show that the complex envelope  $g(t) = m(t) [\hat{m}(t)]$  produces a lower SSB sign that m(t) is a real signal.
- 5-11 Show that the impulse response of  $3a 90^{\circ}$  phase shift network (i.e., a Hilbert tr  $1/\pi t$ . Hint:

 $\int_{-\infty}^{\infty} -je^{-\alpha f}, \quad f>0$ 

5-12 SSB signals can be generated by the phasing method, Fig. 5-5a; the filter method, Fig. 5-5b; or by the use of Weaver's method as shown in Fig. P5-12. For Weaver's method (Fig. P5-12) where B is the bandwidth of m(t):

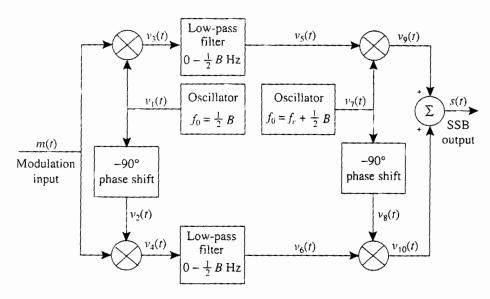
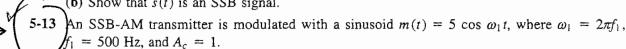


Figure P5-12 Weaver's method for generating SSB.

- (a) Find a mathematical expression that describes the waveform out of each block on the block diagram.
- (b) Show that s(t) is an SSB signal.



- (a) Evaluate  $\hat{m}(t)$ .
- (b) Find the expression for a lower SSB signal.
- (c) Find the rms value of the SSB signal.
- (d) Find the peak value of the SSB signal.
- (e) Find the normalized average power of the SSB signal.
- (f) Find the normalized PEP of the SSB signal.
- 5-14 An SSB-AM transmitter is modulated by a rectangular pulse such that  $m(t) = \Pi(t/T)$  and  $A_c = 1.$ 
  - (a) Prove that

$$\hat{m}(t) = \frac{1}{\pi} \ln \left| \frac{2t + T}{2t - T} \right|$$

as given in Table A-7.

- (b) Find an expression for the SSB-AM signal, s(t), and sketch s(t).
- (c) Find the peak value of s(t).
- **5-15** For Prob. 5-14:
  - (a) Find the expression for the spectrum of a USSB-AM signal.
  - (b) Sketch the magnitude spectrum,  $|S(f)|_4$

5-16 A USSB transmitter is modulated with the pulse



$$m(t) = \frac{\sin \pi at}{\pi at}$$

(a) Prove that

$$\hat{m}(t) = \frac{\sin^2[(\pi a/2)t]}{(\pi a/2)t}$$

- (b) Plot the corresponding USSB signal waveform for the case of  $A_c = 1$ , a = 2, and  $f_c = 20$  Hz.
- 5-17 A USSB-AM signal is modulated by a rectangular pulse train:

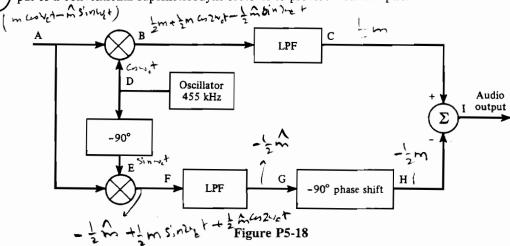
$$m(t) = \sum_{n=-\infty}^{\infty} \Pi[(t - nT_0)/T]$$

where  $T_0 = 2T$ .

- (a) Find the expression for the spectrum of the SSB-AM signal
- (b) Sketch the magnitude spectrum, |S(f)|.



A phasing-type SSB-AM detector is shown in Fig. P5-18. This circuit is attached to the IF output of a conventional superheterodyne receiver to provide SSB reception.



- (a) Determine whether this detector is sensitive to LSSB or USSB signals. How would the detector be changed to receive SSB signals with alternate (opposite type of) sidebands?
- (b) Assume that the signal at point A is a <u>USSB</u> signal with  $f_c = 455$  kHz. Find the mathematical expressions for the signals at points B through I.
- (c) Repeat part (b) for the case of an LSSB-AM signal at poin: A.
- (d) Discuss the IF and LP filter requirements if the SSB signal at point A has a 3-kHz bandwidth.
- 5-19 Can a Costas loop, as shown in Fig. 5-3, be used to demodulate an SSB-AM signal? Demonstrate that your answer is correct by using mathematics.



5-20 A modulated signal is described by the equation

$$s(t) = 10 \cos[(2\pi \times 10^8)t + 10 \cos(2\pi \times 10^3t)]$$

Find each of the following.

- (a) Percentage of AM.
- (b) Normalized power of the modulated signal.
- (c) Maximum phase deviation.
- (d) Maximum frequency deviation.



- 5-21 A sinusoidal signal,  $m(t) = \cos 2\pi f_m t$ , is the input to an angle-modulated transmitter where the carrier frequency is  $f_c = 1$  Hz and  $f_m = f_c/4$ .
  - (a) Plot m(t) and the corresponding PM signal where  $D_p = \pi$ .
  - (b) Plot m(t) and the corresponding FM signal where  $D_f = \pi$ .
- 5-22 A sinusoidal modulating waveform of amplitude 4 V and a frequency of 1 kHz is applied to an FM exciter that has a modulator gain of 50 Hz/V.
  - (a) What is the peak frequency deviation?
  - (b) What is the modulation index?
  - 5-23 An FM signal has sinusoidal modulation with a frequency of  $f_m = 15$  kHz and modulation index of  $\beta = 2.0$ .
    - (a) Find the transmission bandwidth using Carson's rule.
    - (b) What percentage of the total FM signal power lies within the Carson rule bandwidth?
- An FM transmitter has a block diagram as shown in Fig. P5-24. The audio frequency response is flat over the 20-Hz to 15-kHz audio band. The FM output signal is to have a carrier frequency of 103.7 MHz and a peak deviation of 75 kHz.

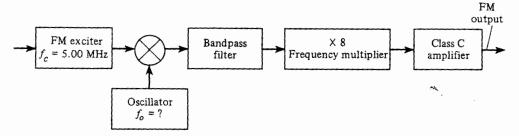


Figure P5-24

- (a) Find the bandwidth and center frequency required for the bandpass filter.
- (b) Calculate the frequency  $f_0$  of the oscillator.
- (c) What is the required peak deviation capability of the FM exciter?
- 5-25 Analyze the performance of the FM circuit of Fig. 5-8b. Assume that the voltage appearing across the reversed-biased diodes, which provide the voltage variable capacitance, is v(t) = 5 + 0.05m(t), where the modulating signal is a test tone,  $m(t) = \cos \omega_1 t$ ,  $\omega_1 = 2\pi f_1$ , and  $f_1 = 1$  kHz. The capacitance of each of the biased diodes is  $C_d = 100/\sqrt{1 + 2v(t)}$  pF. Assume that  $C_0 = 180$  pF and that L is chosen to resonate at 5 MHz.
  - (a) Find the value of L.
  - (b) Show that the resulting oscillator signal is an FM signal. For convenience, assume that the peak level of the oscillator signal is 10 V. Find the parameter  $D_f$ .
- 5-26 A modulated RF waveform is given by 500  $\cos[\omega_c t + 20 \cos \omega_1 t]$ , where  $\omega_1 = 2\pi f_1$ ,  $f_1 = 1$  kHz, and  $f_c = 100$  MHz.
  - (a) If the phase deviation constant is 100 rad/V, find the mathematical expression for the corresponding phase modulation voltage m(t). What is its peak value and its frequency?
  - (b) If the frequency deviation constant is  $1 \times 10^6$  rad/V-s, find the mathematical expression for the corresponding FM voltage, m(t). What is its peak value and its frequency?
  - (c) If the RF waveform appears across a 50- $\Omega$  load, determine the average power and the PEP.

- 5-27 Given the FM signal  $s(t) = 10 \cos \left[\omega_c t + 100 \int_{-\infty}^{t} m(\sigma) d\sigma\right]$ , where m(t) is a polar square wave signal with a duty cycle of 50%, a period of 1 s, and a peak value of 5 V.
  - (a) Sketch the instantaneous frequency waveform and the waveform of the corresponding Fl signal (see Fig. 5-9).
  - (b) Plot the phase deviation  $\theta(t)$  as a function of time.
  - (c) Evaluate the peak frequency deviation.
  - 5-28 A carrier  $s(t) = 100 \cos(2\pi \times 10^9 t)$  of an FM transmitter is modulated with a tone signal. F this transmitter a 1-V (rms) tone produces a deviation of 30 kHz. Determine the amplitude at frequency of all FM signal components (spectral lines) that are greater than 1% of the unmoulated carrier amplitude for the following modulating signals
    - (a)  $m(t) = 2.5 \cos(3\pi \times 10^4 t)$ .
    - **(b)**  $m(t) = 1 \cos(6\pi \times 10^4 t)$ .
  - 5-29 Referring to (5-58), show that

$$J_{-n}(\beta) = (-1)^n J_n(\beta)$$



- 5-30 Consider an FM exciter with the output  $s(t) = 100 \cos [2\pi 1000t + \theta(t)]$ . The modulation  $m(t) = 5 \cos (2\pi 8t)$  and the modulation gain of the exciter is 8 Hz/V. The FM output signal passed through an ideal (brickwall) bandpass filter which has a center frequency of 1000 Hz bandwidth of 56 Hz, and a gain of unity. Determine the normalized average power:
  - (a) At the bandpass filter input.
  - (b) At the bandpass filter output.
- 5-31 A 1-kHz sinusoidal signal phase modulates a carrier at 146.52 MHz with a peak phase dev tion of 45°. Evaluate the exact magnitude spectra of the PM signal if  $A_c = 1$ . Sketch your sult. Using Carson's rule, evaluate the approximate bandwidth of the PM signal and see if it a reasonable number when compared with your spectral plot.
- 5-32 A 1-kHz sinusoidal signal frequency modulates a carrier at 146.52 MHz with a peak deviat of 5 kHz. Evaluate the exact magnitude spectra of the FM signal if  $A_c = 1$ . Sketch your results Carson's rule, evaluate the approximate bandwidth of the FM signal and see if it is a resonable number when compared with your spectral plot.
- 5-33 The calibration of a frequency deviation monitor is to be verified by using a Bessel function to An FM test signal with a calculated frequency deviation is generated by frequency modulat a sine wave onto a carrier. Assume that the sine wave has a frequency of 2 kHz and that amplitude of the sine wave is slowly increased from zero until the discrete carrier term (at of the FM signal reduces to zero, as observed on a spectrum analyzer. What is the peak quency deviation of the FM test signal when the discrete carrier term is zero? Suppose that amplitude of the sine wave is increased further until this discrete carrier term appears, reac a maximum, and then disappears again. What is the peak frequency deviation of the FM test and now?
- 5-34 A frequency modulator has a modulator gain of 10 Hz/V and the modulating waveform is



$$m(t) = \begin{cases} 0, & t < 0 \\ 5, & 0 < t < 1 \\ 15, & 1 < t < 3 \\ 7, & 3 < t < 4 \\ 0, & 4 < t \end{cases}$$

- (a) Plot the frequency deviation in hertz over the time interval 0 < t < 5.
- (b) Plot the phase deviation in radians over the time interval 0 < t < 5.

#### 0.2 Key solution

Drill prob. # 3.2)

$$\begin{array}{llll}
\text{Sprill} & \text{prob.} \# 3.2) \\
\text{Sprill} & \text{Prob.} \# 3.4) \\
\text{Prob.} & \text{Prob.} \# 3.4)

\text{Prob.} & \text{Prob.} & \text{Prob.} \# 3.4)

\text{Prob.} & \text{Prob.} & \text{Prob.} \# 3.4)

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\text{Prob.} & \text$$

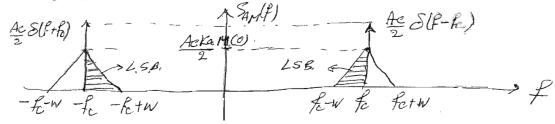
EE 443

HW #7

Mill prob. #3.3) Assure

In general Som (4) = Ac [1+ Ko mit)] Cos 21 fet

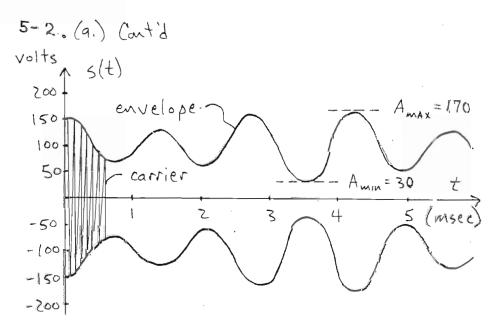
SAM(f) = Ac [S(f-fc)+S(f+fc)]+ Acka [M(f-fc)+M(f+fc)]



From the plot of San(f) we see that to exoid the overlapping of L. S. B frequencies it must - fe-w > 0 => fc > W

b) Som (t) = Ac[1+Ko. m(t)] Cos 211 fet = 50[1+ Ka. 20, Cos 200t] les 10011 = 50 cs (10011) + 50x 0.75 cos (100111) cs (2111) = 50 Was (100171) + 37.5 { es (102171) + Cas (98171)}

 $P_{tot} = \frac{(50)}{90} + 2x \frac{(37.5)^2}{2R} = \frac{2500}{200} + \frac{1406.25}{400} = 16.0156 \text{ walls}$ 



(b.) 
$$\frac{170-30}{2(100)}(100) = \frac{70\%}{0}$$
 modulation

(c.) 
$$G(f) = S(f) + M(f)$$

$$= S(f) - \frac{1}{2} \left[ S(f-f_1) - S(f+f_1) \right] + \frac{(0.5)}{2} \left[ S(f-f_2) + S(f+f_2) \right] + \frac{(0.5)}{2} \left[ S(f-f_2) + S(f+f_2) \right] + \frac{Ac}{2} \left[ G(f-f_2) + G^*(-f-f_2) \right] + \frac{Ac}{2} \left[ G(f-f_2) + G^*(-f-f_2) \right] + \frac{50}{20} +$$

#### 0.3 my graded HW

HW#7 EE 443 Oct 30,2008 Fall 2008

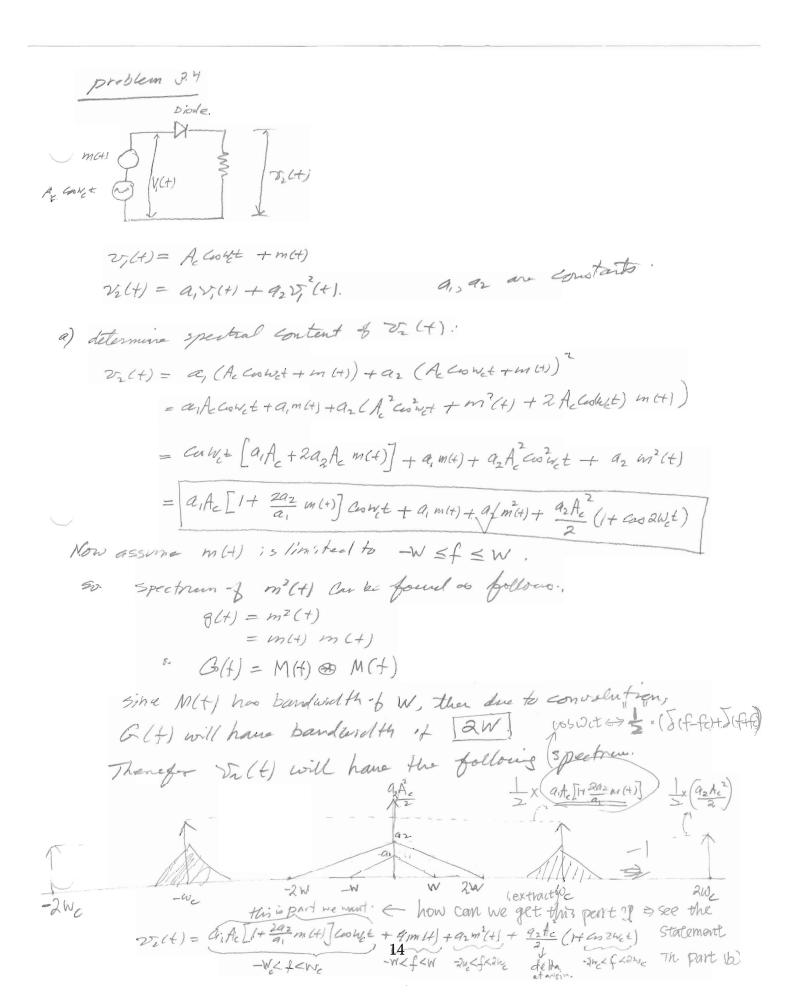
MASSER ABBASI.

Problems 3.2
3.3
3.4
3.18

5.2 (Handont)
(Hard)

problem 3.2 (Book page 110) For particular case of AM using Sinusoidal modulation ware, the percentage modulation is 20%. Calculate average power in (9) the carrier and (6) each side frequency. Arenac in this case m(+) = Am Con (277 funt) c(+) = Ac Cos (2176t) S(t) = Ac[1+ Kam(t)] Coo (21) fc+) and = Ac [It KacAm Coo(27) fruit)] Coo(21) fet) let K. Am = le 51+) = Ac[1+11 Coo(27) fint)] Coo(27) fot). = Ac Cao (27/2t) - AcM. Coo(27/4nt) Coo(27/4t) - 0 but Coolwint) Coo(wet) = 1 ( Coo(wm+we)t + coo(wm-we)t) Es O be come S(+) = Ac Goowet + ACK (Coo (wm+wit + Coo(w-wm)t) lower side appar side Bard. bard So, power in 5(+) = 1 A + 2 (Ack) x2 (a) power in Carrier = [1 Ac] (b) pons in lower side and upps side = \frac{1}{2} \frac{Ac^2 H^2}{4} = \frac{Ac^2 H^2}{0} but 11= 2 , here pour = Ac (12) = Ac /400 Then power in side band to power in carries is 400 + 400 = 1/.

in AM, spectral overlap is said to ochur of lower sideband for positive frequencies overlaps with its image for negative fequences, what conditions must the modulated wave 30 to by if we save to avoid spectral oursless? Consum m(+) is low-pass Kind with band width W. Carried spectrum. I this shape answar Spectrum of m (+) modulated Carried: So to word spectral overlap, we need. or ENW this insures that modulated carrier Side bands do not overlap in the figureen domain



non 25(4) is isputed to Dand-pass filter. then we see that the modulated carries range of frequencies is in the positive side f-W <f < f+W in the nighthe side the above is the rouge of frequencies of the shaded part of the spectrum, which carries the modulated carrier by m(+) signal one ok = That is: aiAc[1+ saz mti] coswit. () after band-pass, we abtain this Range. must be >3W

where 2W are due to m2H) spectrum originals and an addition W comes from the m(+) band width itself.

#3.18 m(t)=20 Coo(27t) botts. and carrier

c(+) = 50 Coo (100 Tt ) volto

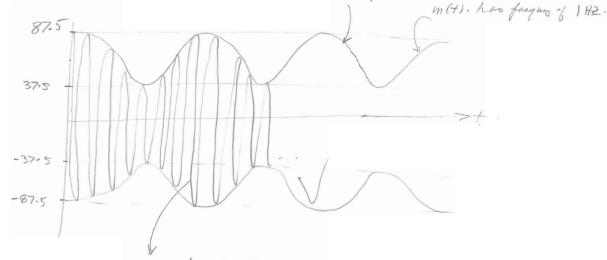
(4) sketch to scale the resulting AM wave for 11= .75 (b) find power developed across would 100 ohms due to this AM wave.

Anone

When Ac = 50 We = 100TT

S(t) = 50[1+ .75 cm271+] cm(1007+)

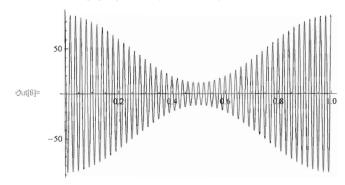
So the emclose will have a max value of [87.5] and a min valer - 6 [37.5 envelope



Carrier, has freg=50HZ. ie 50 fines as mit).

> Please see more accord plat next page.

 $[n[7] = s[t_{-}] := 50 (1 + .75 \cos[2 Pi t]) \cos[100 Pi t]$ Plot[s[t], {t, 0, 1}, PlotRange  $\rightarrow$  All]



So power across [5] from C(+1 is 502 Watt. and power across

12 from side bando i6 2x \(\frac{1}{2}\left(\frac{37.5}{2}\right)^2\) watt \(\chi\) \(\R=100\)Ω.

Total power across 12 is 1,425.78 Watt

So Total power developed in 100 s is 142,500 watt as 142.5 KW

$$\frac{(50)^{2}}{500} + 34 \frac{(\frac{37.5}{2})^{2}}{500} = 16.0156$$

# problem 5.2 from Handont

AM transmitter is modulated with sign m(+)=0.25in w.+7.5642t where fi= 500 HZ and fr= 500 VI HZ, Ac=100. Assum AM Sign in Fed into 50 2 load.

a) Sketh AM wanton

b) what is modulating!!

c) Evaluate and sketch the spectrum of the AM waveform

5(+) = A=[ 1+ Ka Amm (+)] (10 Wet.

Amm(+) = . 2 sin 27/5 + . 5 cm 27/2+

the Largest frequency in m(+) is 500HZ. So fe >W.

let f = 500 HZ

Su 5(t) = 100 [1+ Ka (.2 sin 1000 TI + .5 Coo 1000 V2 TI t)] Coo (1000 TT t)

We need | Kym(+) | < | to award ourmodulation

we can write S(+) as follows

s(+) = 100 [1+ M m(+)] Coowet

where le = Amax-Amin

Amax + Amin.

Where Amax = max value of , 25m w, t + 5 Cooks t and

Anin = min value of

so to finel Amax and Anin we do

d m(+) and set to tow.

OK.

 $\frac{dw(t)}{dt} = (2\cos(\omega, t)) \cdot \omega_1 - (.5 \sin(\omega_2 t)) \omega_2 = g(t)$ 

so g(t) =0 ⇒ (2600 \$600017+) - 1000\$ - (.5 Sin 1000 \$21 +) 1000\$ \$211 =0

So g(t)=0 > .2 cao loco Tt - V2 \frac{1}{2} Sin loco \( \text{loc} \) \\

1. & find where the above has root. that

\[
\text{t will 8've either max or min.}
\]

once the above is done, we can find

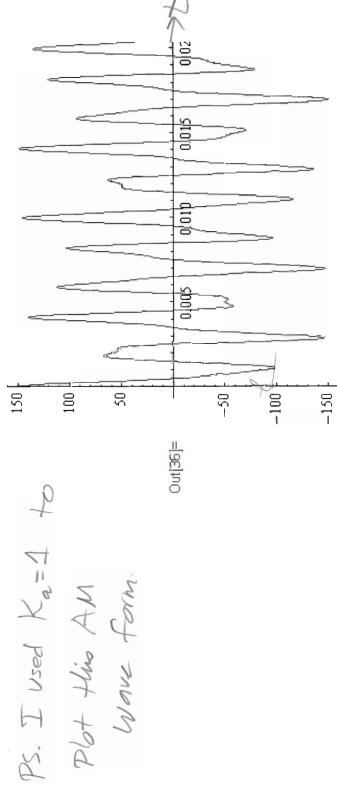
\[
\text{ll.}
\]

a 5 ke the will be as follows:
\[
\text{Conrelep.}
\]

Carries Preg.

Plem see exact
plot on next page

Plot[f[t], {t, 0, .03}, PlotRange - $\ln[35] = \text{f[}t\_\text{]} := 100 (1 + (.2 \sin[2Pi 500 t])$ 150



Part b - b Find. modulation !, this is M.

M= Amax - Amin Amax + Amin

Zs you should find Amax and Amin.

I described to find this exlie. (need to take derivative.
of M(t) Writing and set to Zero to find Amex/Amin).

Dodal not do this on the generated equation is nonlinear and Dam not sure if my approach's Correct at this time.

(c) to find the spectrum.

S(+) = Ac[i+ Ka(.2 Sinw,++.5 Cowz+)] Coswc+

note: There are 2 different Harmonico in M (+).

= AcCooket + AcKa 2 Sink, + Cohet + AcKa 5 Cohet Cohet

 $= A_{c} \left( \operatorname{cool}_{we} + \cdot 2 \operatorname{A_{c}ka} \right) \left( \operatorname{sin} \left( w_{c} + w_{d} \right) + \operatorname{sin} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{d} \right) + + \operatorname{Coo} \left( w_{c} - w_{d} \right) + \right)$   $+ \cdot 5 \operatorname{A_{c}ka} \left( \operatorname{Coo} \left( w_{c} + w_{$ 

-te fetf, -fetf2 6 fet2