

# Kamke differential equations. Mathematica 10.0 and Maple 18.01 and Sage 6.2

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<b>3</b>	<b>Kamke chapter 2. Linear second order</b>	<b>505</b>
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3.9	ODE No. 1009 . . . . .	507
3.10	ODE No. 1010 . . . . .	508
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3.12	ODE No. 1012 . . . . .	508
3.13	ODE No. 1013 . . . . .	509
3.14	ODE No. 1014 . . . . .	509
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7.107	ODE No. 1697	741
7.108	ODE No. 1698	741
7.109	ODE No. 1699	741
7.110	ODE No. 1700	742
7.111	ODE No. 1701	742
7.112	ODE No. 1702	742
7.113	ODE No. 1703	743
7.114	ODE No. 1704	743
7.115	ODE No. 1705	743
7.116	ODE No. 1706	744
7.117	ODE No. 1707	744
7.118	ODE No. 1708	744
7.119	ODE No. 1709	745
7.120	ODE No. 1710	745
7.121	ODE No. 1711	745
7.122	ODE No. 1712	746
7.123	ODE No. 1713	746
7.124	ODE No. 1714	747
7.125	ODE No. 1715	747
7.126	ODE No. 1716	747
7.127	ODE No. 1717	748
7.128	ODE No. 1718	748
7.129	ODE No. 1719	749
7.130	ODE No. 1720	749
7.131	ODE No. 1721	749
7.132	ODE No. 1722	750
7.133	ODE No. 1723	750
7.134	ODE No. 1724	750
7.135	ODE No. 1725	751
7.136	ODE No. 1726	751
7.137	ODE No. 1727	751
7.138	ODE No. 1728	752
7.139	ODE No. 1729	752

7.140	ODE No. 1730	752
7.141	ODE No. 1731	753
7.142	ODE No. 1732	753
7.143	ODE No. 1733	753
7.144	ODE No. 1734	754
7.145	ODE No. 1735	754
7.146	ODE No. 1736	754
7.147	ODE No. 1737	755
7.148	ODE No. 1738	755
7.149	ODE No. 1739	755
7.150	ODE No. 1740	756
7.151	ODE No. 1741	756
7.152	ODE No. 1742	756
7.153	ODE No. 1743	757
7.154	ODE No. 1744	757
7.155	ODE No. 1745	757
7.156	ODE No. 1746	758
7.157	ODE No. 1747	758
7.158	ODE No. 1748	759
7.159	ODE No. 1749	759
7.160	ODE No. 1750	759
7.161	ODE No. 1751	760
7.162	ODE No. 1752	760
7.163	ODE No. 1753	761
7.164	ODE No. 1754	761
7.165	ODE No. 1755	761
7.166	ODE No. 1756	762
7.167	ODE No. 1757	762
7.168	ODE No. 1758	762
7.169	ODE No. 1759	763
7.170	ODE No. 1760	763
7.171	ODE No. 1761	763
7.172	ODE No. 1762	764
7.173	ODE No. 1763	764
7.174	ODE No. 1764	764
7.175	ODE No. 1765	765
7.176	ODE No. 1766	765
7.177	ODE No. 1767	765
7.178	ODE No. 1768	766

7.179	ODE No. 1769	766
7.180	ODE No. 1770	766
7.181	ODE No. 1771	767
7.182	ODE No. 1772	767
7.183	ODE No. 1773	767
7.184	ODE No. 1774	768
7.185	ODE No. 1775	768
7.186	ODE No. 1776	768
7.187	ODE No. 1777	769
7.188	ODE No. 1778	769
7.189	ODE No. 1779	769
7.190	ODE No. 1780	770
7.191	ODE No. 1781	770
7.192	ODE No. 1782	770
7.193	ODE No. 1783	771
7.194	ODE No. 1784	771
7.195	ODE No. 1785	771
7.196	ODE No. 1786	772
7.197	ODE No. 1787	772
7.198	ODE No. 1788	772
7.199	ODE No. 1789	773
7.200	ODE No. 1790	773
7.201	ODE No. 1791	774
7.202	ODE No. 1792	774
7.203	ODE No. 1793	775
7.204	ODE No. 1794	775
7.205	ODE No. 1795	775
7.206	ODE No. 1796	776
7.207	ODE No. 1797	776
7.208	ODE No. 1798	777
7.209	ODE No. 1799	777
7.210	ODE No. 1800	777
7.211	ODE No. 1801	778
7.212	ODE No. 1802	778
7.213	ODE No. 1803	778
7.214	ODE No. 1804	779
7.215	ODE No. 1805	779
7.216	ODE No. 1806	780
7.217	ODE No. 1807	780

7.218	ODE No. 1808	780
7.219	ODE No. 1809	781
7.220	ODE No. 1810	781
7.221	ODE No. 1811	781
7.222	ODE No. 1812	782
7.223	ODE No. 1813	782
7.224	ODE No. 1814	783
7.225	ODE No. 1815	783
7.226	ODE No. 1816	783
7.227	ODE No. 1817	784
7.228	ODE No. 1818	784
7.229	ODE No. 1819	784
7.230	ODE No. 1820	785
7.231	ODE No. 1821	785
7.232	ODE No. 1822	785
7.233	ODE No. 1823	786
7.234	ODE No. 1824	786
7.235	ODE No. 1825	787
7.236	ODE No. 1826	787
7.237	ODE No. 1827	787
7.238	ODE No. 1828	788
7.239	ODE No. 1829	788
7.240	ODE No. 1830	788
7.241	ODE No. 1831	789
7.242	ODE No. 1832	789
7.243	ODE No. 1833	789
7.244	ODE No. 1834	790
7.245	ODE No. 1835	790
7.246	ODE No. 1836	790

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8.1	ODE No. 1837	791
8.2	ODE No. 1838	791
8.3	ODE No. 1839	791
8.4	ODE No. 1840	792
8.5	ODE No. 1841	792
8.6	ODE No. 1842	793
8.7	ODE No. 1843	793
8.8	ODE No. 1844	794



8.9	ODE No. 1845	794
8.10	ODE No. 1846	794
8.11	ODE No. 1847	795
8.12	ODE No. 1848	795
8.13	ODE No. 1849	795
8.14	ODE No. 1850	796
8.15	ODE No. 1851	796
8.16	ODE No. 1852	796
8.17	ODE No. 1853	797
8.18	ODE No. 1854	797
8.19	ODE No. 1855	797
<b>9</b>	<b>Kamke chapter 8. System of linear differential equations</b>	<b>798</b>
9.1	ODE No. 1856	798
9.2	ODE No. 1857	798
9.3	ODE No. 1858	798
9.4	ODE No. 1859	799
9.5	ODE No. 1860	799
9.6	ODE No. 1861	799
9.7	ODE No. 1862	800
9.8	ODE No. 1863	800
9.9	ODE No. 1864	800
9.10	ODE No. 1865	801
9.11	ODE No. 1866	801
9.12	ODE No. 1867	801
9.13	ODE No. 1868	802
9.14	ODE No. 1869	802
9.15	ODE No. 1870	802
9.16	ODE No. 1871	803
9.17	ODE No. 1872	803
9.18	ODE No. 1873	803
9.19	ODE No. 1874	804
9.20	ODE No. 1875	804
9.21	ODE No. 1876	804
9.22	ODE No. 1877	805
9.23	ODE No. 1878	805
9.24	ODE No. 1879	805
9.25	ODE No. 1880	806
9.26	ODE No. 1881	806

9.27	ODE No. 1882	806
9.28	ODE No. 1883	807
9.29	ODE No. 1884	807
9.30	ODE No. 1885	807
9.31	ODE No. 1886	808
9.32	ODE No. 1887	808
9.33	ODE No. 1888	808
9.34	ODE No. 1889	809
9.35	ODE No. 1890	809
9.36	ODE No. 1891	809
9.37	ODE No. 1892	810
9.38	ODE No. 1893	810
9.39	ODE No. 1894	811
9.40	ODE No. 1895	811
9.41	ODE No. 1896	811
9.42	ODE No. 1897	812
9.43	ODE No. 1898	812
9.44	ODE No. 1899	812
9.45	ODE No. 1900	813
9.46	ODE No. 1901	813
9.47	ODE No. 1902	813
9.48	ODE No. 1903	814
9.49	ODE No. 1904	814
9.50	ODE No. 1905	814
9.51	ODE No. 1906	815
9.52	ODE No. 1907	815
9.53	ODE No. 1908	815
9.54	ODE No. 1909	816
9.55	ODE No. 1910	816
9.56	ODE No. 1911	816
9.57	ODE No. 1912	817

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10.1	ODE No. 1913	818
10.2	ODE No. 1914	818
10.3	ODE No. 1915	820
10.4	ODE No. 1916	820
10.5	ODE No. 1917	820
10.6	ODE No. 1918	821

10.7	ODE No. 1919	821
10.8	ODE No. 1920	821
10.9	ODE No. 1921	822
10.10	ODE No. 1922	822
10.11	ODE No. 1923	822
10.12	ODE No. 1924	823
10.13	ODE No. 1925	823
10.14	ODE No. 1926	823
10.15	ODE No. 1927	824
10.16	ODE No. 1928	824
10.17	ODE No. 1929	824
10.18	ODE No. 1930	825
10.19	ODE No. 1931	825
10.20	ODE No. 1932	826
10.21	ODE No. 1933	826
10.22	ODE No. 1934	826
10.23	ODE No. 1935	827
10.24	ODE No. 1936	827
10.25	ODE No. 1937	827
10.26	ODE No. 1938	828
10.27	ODE No. 1939	828
10.28	ODE No. 1940	829

# 1 Introduction and summary of results

This report gives the result of solving the 1,940 Kamke differential equations in Mathematica 10.0.2 and Maple 18.02 on windows 7, 64 bit OS. The PC used is an Intel i7-3930k running at 3.20 GHz with 16 GB memory. Sage 6.2 is currently work in progress and is being added. Currently only the first 70 Kamke differential equations are implemented in Sage.

The command `AboluteTiming[]` was used in Mathematica to obtain the CPU time. In Sage the command `cputime()` was used. In Maple the following command was used for this purpose

```
cpu_time := Usage(assign('result_of_solve',dsolve(ode,y(x))),output='cputime');
```

When Mathematica returned `DifferentialRoot` as a solution to an ODE this was counted as not solved. Similarly, when Maple returned `DESol` this was also counted as not solved.

Table 1 below summarizes the performance of each CAS system

system	% solved	mean CPU time (sec)	mean leaf size of result	total CPU (minutes)	to
Mathematica	79.7423	23.6369	2770.78	609	
Maple	92.2165	0.876531	327.822	26	
Sage	56.5217	2.3	0.	89.7 (sec)	

Table 1: Summary of final results

A number of problems were not solved due to the program hanging. When a program took more than 20 minutes of real time or more (sometimes, the wait was over one hour before terminating the process), only then it was considered as hanged process. Also, when it causes the PC to run of memory while running forcing the termination of the current process, this was counted as hanged process as well. Table 2 shows the percentage that hanged out of all the unsolved problems.

system	% hanged
Mathematica	27.9898
Maple	15.2318
Sage	16.6667

Table 2: Showing how many solution failed due to hanged process

Table 3 summarizes the Kamke equations used

book chapter	kamke book numbering of equations	Numbering in t
Chapter 1, linear first order	1.1—1.576	1—576
Additional non-linear first order	N/A	577—1000
Chapter 2, linear second order	2.1—2.448	1001—1448
Chapter 3, linear third order	3.1—3.85	1449—1533
Chapter 4, linear fourth order	4.1—4.44	1534—1577
Chapter 5, linear fifth and higher order	5.1—5.13	1578—1590
Chapter 6, non-linear second order	6.1—6.246	1591—1836
Chapter 7, non-linear third and higher order	7.1—7.19	1837—1855
Chapter 8, system of ode, first order	8.1—8.57	1856—1912
Chapter 9, system of ode, higher order	9.1—9.28	1913—1940

Table 3: Kamke equation numbering

The following summarizes which equations are solved by each system

**Not solved by Sage** 14, 23, 24, 31, 35, 36, 37, 38, 40, 41, 42, 43, 45, 46, 47, 48, 49, 50, 52, 55, 56, 58, 59, 62, 63, 64, 65, 67, 68, 69

**Not solved by Mathematica** 16, 22, 38, 47, 48, 49, 50, 55, 56, 74, 79, 80, 81, 82, 83, 86, 87, 110, 121, 127, 188, 202, 203, 205, 206, 219, 234, 237, 250, 253, 265, 266, 269, 331, 340, 365, 367, 368, 370, 383, 385, 394, 395, 400, 402, 404, 413, 414, 416, 428, 429, 430, 451, 452, 460, 461, 465, 467, 468, 479, 480, 482, 485, 487, 489, 494, 503, 504, 506, 509, 510, 513, 515, 523, 524, 527, 528, 530, 531, 533, 534, 535, 537, 538, 541, 542, 543, 544, 546, 550, 555, 561, 566, 567, 570, 572, 575, 576, 620, 638, 639, 640, 672, 701, 703, 706, 714, 730, 733, 735, 743, 745, 746, 747, 752, 759, 766, 769, 776, 782, 783, 784, 785, 786, 788, 789, 807, 835, 837, 854, 855, 862, 885, 889, 892, 894, 909, 913, 915, 916, 917, 918, 919, 922, 923, 925, 926, 929, 932, 942, 953, 961, 996, 1000, 1008, 1026, 1036, 1049, 1068, 1073, 1090, 1156, 1212, 1216, 1232, 1233, 1236, 1263, 1278, 1341, 1413, 1418, 1427, 1439, 1441, 1442, 1443, 1444, 1445, 1450, 1457, 1458, 1459, 1460, 1461, 1462, 1463, 1471, 1472, 1473, 1474, 1476, 1482, 1484, 1489, 1500, 1505, 1507, 1510, 1515, 1516, 1520, 1526, 1527, 1529, 1530, 1531, 1540, 1541, 1542, 1543, 1544, 1547, 1552, 1572, 1573, 1574, 1575, 1576, 1581, 1586, 1590, 1593, 1595, 1596, 1598, 1599, 1601, 1603, 1605, 1606, 1608, 1609, 1610, 1611, 1612, 1613, 1614, 1615, 1616, 1617, 1618, 1619, 1620, 1621, 1622, 1623, 1624, 1625, 1626, 1627, 1628, 1629, 1631, 1633, 1634, 1635, 1636, 1637, 1638, 1639, 1640, 1642, 1643, 1644, 1645, 1648, 1649, 1652, 1656, 1658, 1659, 1660, 1662, 1663, 1664, 1665, 1666, 1667, 1672, 1673, 1675, 1677, 1678, 1680, 1681, 1682, 1684, 1685, 1686, 1690,

1691, 1692, 1693, 1695, 1696, 1702, 1704, 1705, 1706, 1708, 1709, 1710, 1713, 1719, 1720, 1721, 1729, 1732, 1734, 1735, 1737, 1738, 1739, 1742, 1746, 1751, 1755, 1757, 1761, 1762, 1776, 1777, 1779, 1780, 1788, 1789, 1797, 1798, 1801, 1802, 1806, 1807, 1809, 1811, 1813, 1815, 1816, 1817, 1818, 1819, 1820, 1821, 1823, 1825, 1827, 1831, 1832, 1833, 1834, 1836, 1837, 1838, 1839, 1840, 1841, 1844, 1845, 1848, 1850, 1851, 1853, 1854, 1855, 1875, 1880, 1885, 1890, 1894, 1905, 1911, 1912, 1915, 1916, 1917, 1918, 1919, 1920, 1921, 1922, 1925, 1926, 1927, 1928, 1929, 1932, 1933, 1934, 1935, 1936, 1937, 1939, 1940

**Not solved by Maple** 38, 47, 48, 49, 50, 55, 56, 74, 79, 82, 87, 110, 121, 202, 203, 205, 206, 219, 234, 237, 250, 253, 265, 269, 286, 331, 340, 367, 368, 370, 383, 395, 452, 460, 461, 480, 482, 484, 485, 503, 506, 507, 510, 531, 537, 543, 572, 575, 576, 733, 788, 789, 790, 835, 837, 885, 894, 920, 1015, 1019, 1026, 1028, 1031, 1038, 1072, 1073, 1075, 1076, 1077, 1081, 1158, 1212, 1216, 1236, 1278, 1457, 1458, 1459, 1460, 1461, 1462, 1463, 1473, 1474, 1476, 1484, 1489, 1510, 1515, 1531, 1540, 1541, 1542, 1543, 1581, 1582, 1586, 1593, 1595, 1596, 1598, 1599, 1606, 1608, 1609, 1616, 1619, 1623, 1625, 1628, 1634, 1642, 1643, 1645, 1649, 1675, 1685, 1698, 1702, 1704, 1705, 1706, 1721, 1729, 1732, 1734, 1735, 1737, 1738, 1739, 1751, 1757, 1761, 1788, 1789, 1797, 1801, 1802, 1807, 1835, 1851, 1854, 1855, 1880, 1890, 1905, 1921, 1922, 1927, 1928, 1940

**Solved by Mathematica but not by Maple** 286, 484, 507, 790, 920, 1015, 1019, 1028, 1031, 1038, 1072, 1075, 1076, 1077, 1081, 1158, 1582, 1698, 1835

**Solved by Maple but not by Mathematica** 16, 22, 80, 81, 83, 86, 127, 188, 266, 365, 385, 394, 400, 402, 404, 413, 414, 416, 428, 429, 430, 451, 465, 467, 468, 479, 487, 489, 494, 504, 509, 513, 515, 523, 524, 527, 528, 530, 533, 534, 535, 538, 541, 542, 544, 546, 550, 555, 561, 566, 567, 570, 620, 638, 639, 640, 672, 701, 703, 706, 714, 730, 735, 743, 745, 746, 747, 752, 759, 766, 769, 776, 782, 783, 784, 785, 786, 807, 854, 855, 862, 889, 892, 909, 913, 915, 916, 917, 918, 919, 922, 923, 925, 926, 929, 932, 942, 953, 961, 996, 1000, 1008, 1036, 1049, 1068, 1090, 1156, 1232, 1233, 1263, 1341, 1413, 1418, 1427, 1439, 1441, 1442, 1443, 1444, 1445, 1450, 1471, 1472, 1482, 1500, 1505, 1507, 1516, 1520, 1526, 1527, 1529, 1530, 1544, 1547, 1552, 1572, 1573, 1574, 1575, 1576, 1590, 1601, 1603, 1605, 1610, 1611, 1612, 1613, 1614, 1615, 1617, 1618, 1620, 1621, 1622, 1624, 1626, 1627, 1629, 1631, 1633, 1635, 1636, 1637, 1638, 1639, 1640, 1644, 1648, 1652, 1656, 1658, 1659, 1660, 1662, 1663, 1664, 1665, 1666, 1667, 1672, 1673, 1677, 1678, 1680, 1681, 1682, 1684, 1686, 1690, 1691, 1692, 1693, 1695, 1696, 1708, 1709, 1710, 1713, 1719, 1720, 1742, 1746, 1755, 1762, 1776, 1777, 1779, 1780, 1798, 1806, 1809, 1811, 1813, 1815, 1816, 1817, 1818, 1819, 1820, 1821, 1823, 1825, 1827, 1831, 1832, 1833, 1834, 1836, 1837, 1838, 1839, 1840, 1841, 1844, 1845, 1848, 1850, 1853, 1875, 1885, 1894, 1911, 1912, 1915, 1916, 1917, 1918,

1919, 1920, 1925, 1926, 1929, 1932, 1933, 1934, 1935, 1936, 1937, 1939

**Solved by both Maple and Mathematica** 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 17, 18, 19, 20, 21, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 39, 40, 41, 42, 43, 44, 45, 46, 51, 52, 53, 54, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 75, 76, 77, 78, 84, 85, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 122, 123, 124, 125, 126, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 201, 204, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 220, 221, 222, 223, 224, 225, 226, 227, 228, 229, 230, 231, 232, 233, 235, 236, 238, 239, 240, 241, 242, 243, 244, 245, 246, 247, 248, 249, 251, 252, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 267, 268, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 287, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 299, 300, 301, 302, 303, 304, 305, 306, 307, 308, 309, 310, 311, 312, 313, 314, 315, 316, 317, 318, 319, 320, 321, 322, 323, 324, 325, 326, 327, 328, 329, 330, 332, 333, 334, 335, 336, 337, 338, 339, 341, 342, 343, 344, 345, 346, 347, 348, 349, 350, 351, 352, 353, 354, 355, 356, 357, 358, 359, 360, 361, 362, 363, 364, 366, 369, 371, 372, 373, 374, 375, 376, 377, 378, 379, 380, 381, 382, 384, 386, 387, 388, 389, 390, 391, 392, 393, 396, 397, 398, 399, 401, 403, 405, 406, 407, 408, 409, 410, 411, 412, 415, 417, 418, 419, 420, 421, 422, 423, 424, 425, 426, 427, 431, 432, 433, 434, 435, 436, 437, 438, 439, 440, 441, 442, 443, 444, 445, 446, 447, 448, 449, 450, 453, 454, 455, 456, 457, 458, 459, 462, 463, 464, 466, 469, 470, 471, 472, 473, 474, 475, 476, 477, 478, 481, 483, 486, 488, 490, 491, 492, 493, 495, 496, 497, 498, 499, 500, 501, 502, 505, 508, 511, 512, 514, 516, 517, 518, 519, 520, 521, 522, 525, 526, 529, 532, 536, 539, 540, 545, 547, 548, 549, 551, 552, 553, 554, 556, 557, 558, 559, 560, 562, 563, 564, 565, 568, 569, 571, 573, 574, 577, 578, 579, 580, 581, 582, 583, 584, 585, 586, 587, 588, 589, 590, 591, 592, 593, 594, 595, 596, 597, 598, 599, 600, 601, 602, 603, 604, 605, 606, 607, 608, 609, 610, 611, 612, 613, 614, 615, 616, 617, 618, 619, 621, 622, 623, 624, 625, 626, 627, 628, 629, 630, 631, 632, 633, 634, 635, 636, 637, 641, 642, 643, 644, 645, 646, 647, 648, 649, 650, 651, 652, 653, 654, 655, 656, 657, 658, 659, 660, 661, 662, 663, 664, 665, 666, 667, 668, 669, 670, 671, 673, 674, 675, 676, 677, 678, 679, 680, 681, 682, 683, 684, 685, 686, 687, 688, 689, 690, 691, 692, 693, 694, 695, 696, 697, 698, 699, 700, 702, 704, 705, 707, 708, 709, 710, 711, 712, 713, 715, 716, 717, 718, 719, 720, 721, 722, 723, 724, 725, 726, 727, 728, 729, 731, 732, 734, 736, 737, 738, 739, 740, 741, 742, 744, 748, 749, 750, 751, 753, 754, 755, 756, 757, 758,

760, 761, 762, 763, 764, 765, 767, 768, 770, 771, 772, 773, 774, 775, 777, 778, 779,  
780, 781, 787, 791, 792, 793, 794, 795, 796, 797, 798, 799, 800, 801, 802, 803, 804,  
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**Both systems unable to solve** 38, 47, 48, 49, 50, 55, 56, 74, 79, 82, 87, 110, 121, 202, 203, 205, 206, 219, 234, 237, 250, 253, 265, 269, 331, 340, 367, 368, 370, 383, 395, 452, 460, 461, 480, 482, 485, 503, 506, 510, 531, 537, 543, 572, 575, 576, 733, 788, 789, 835, 837, 885, 894, 1026, 1073, 1212, 1216, 1236, 1278, 1457, 1458, 1459, 1460, 1461, 1462, 1463, 1473, 1474, 1476, 1484, 1489, 1510, 1515, 1531, 1540, 1541, 1542, 1543, 1581, 1586, 1593, 1595, 1596, 1598, 1599, 1606, 1608, 1609, 1616, 1619, 1623, 1625, 1628, 1634, 1642, 1643, 1645, 1649, 1675, 1685, 1702, 1704, 1705, 1706, 1721, 1729, 1732, 1734, 1735, 1737, 1738, 1739, 1751, 1757, 1761, 1788, 1789, 1797, 1801, 1802, 1807, 1851, 1854, 1855, 1880, 1890, 1905, 1921, 1922, 1927, 1928, 1940

Final conclusion table for each equation is given by table 4 below.

Table 4: Breakdown of results for each Kamke differential equation

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1	K 1.1	✓	2.002	1117	✓	0.062	30	✓
2	K 1.2	✓	0.015	34	✓	0.047	25	✓
3	K 1.3	✓	0.059	40	✓	0.015	37	✓
4	K 1.4	✓	0.009	30	✓	0.015	18	✓
5	K 1.5	✓	3.135	38	✓	0.171	27	✓
6	K 1.6	✓	0.022	18	✓	0.078	15	✓
7	K 1.7	✓	0.023	23	✓	0.0	19	✓
8	K 1.8	✓	0.024	17	✓	0.0	15	✓
9	K 1.9	✓	0.016	19	✓	0.015	16	✓
10	K 1.10	✓	0.008	18	✓	0.015	15	✓
11	K 1.11	✓	0.473	62	✓	0.0	24	✓
12	K 1.12	✓	0.063	34	✓	0.062	8	✓
13	K 1.13	✓	0.052	79	✓	0.125	79	✓
14	K 1.14	✓	0.011	254	✓	0.093	189	✗
15	K 1.15	✓	0.02	25	✓	0.156	38	✓
16	K 1.16	✗	21.387	24	✓	0.093	50	✓
17	K 1.17	✓	0.023	34	✓	0.093	25	✓
18	K 1.18	✓	0.021	50	✓	0.062	47	✓
19	K 1.19	✓	0.009	30	✓	0.047	16	✓
20	K 1.20	✓	0.79	48	✓	0.062	34	✓
21	K 1.21	✓	7.447	69	✓	0.093	25	✓
22	K 1.22	✗	241.061	31	✓	0.468	198	✓
23	K 1.23	✓	0.041	43	✓	0.031	29	✗
24	K 1.24	✓	0.012	277	✓	0.046	214	✗
25	K 1.25	✓	0.237	1835	✓	0.249	378	✓

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
26	K 1.26	✓	0.076	68	✓	0.047	59	✓
27	K 1.27	✓	0.044	120	✓	0.156	71	✓
28	K 1.28	✓	0.047	96	✓	0.078	67	✓
29	K 1.29	✓	0.022	39	✓	0.031	19	✓
30	K 1.30	✓	0.065	230	✓	0.078	81	✓
31	K 1.31	✓	0.06	21	✓	0.031	26	✗
32	K 1.32	✓	0.237	34	✓	0.218	28	✓
33	K 1.33	✓	26.354	157	✓	0.343	57	✓
34	K 1.34	✓	0.507	51	✓	0.031	28	✓
35	K 1.35	✓	0.058	60	✓	0.031	45	✗
36	K 1.36	✓	0.227	195	✓	0.062	62	✗
37	K 1.37	✓	0.679	78	✓	0.062	50	✗
38	K 1.38	✗	8.692	26	✗	0.655	0	✗
39	K 1.39	✓	0.051	54	✓	0.016	30	✓
40	K 1.40	✓	0.242	185	✓	0.062	48	✗
41	K 1.41	✓	0.076	103	✓	0.172	103	✗
42	K 1.42	✓	0.936	485	✓	0.016	40	✗
43	K 1.43	✓	8.686	490	✓	1.263	384	✗
44	K 1.44	✓	0.015	72	✓	0.016	53	✓
45	K 1.45	✓	0.523	133	✓	0.094	123	✗
46	K 1.46	✓	0.228	258	✓	0.062	1052	✗
47	K 1.47	✗	33.169	31	✗	1.248	0	✗
48	K 1.48	✗	36.628	33	✗	1.232	0	✗
49	K 1.49	✗	28.632	52	✗	0.702	0	✗
50	K 1.50	✗	125.836	37	✗	0.265	0	✗
51	K 1.51	✓	0.753	354	✓	0.156	2348	✓
52	K 1.52	✓	116.892	115	✓	0.156	61	✗

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
53	K 1.53	✓	57.745	95	✓	0.062	281	✓
54	K 1.54	✓	0.117	74	✓	0.124	42	✓
55	K 1.55	✗	6.593	29	✗	0.218	0	✗
56	K 1.56	✗	2.268	27	✗	0.202	0	✗
57	K 1.57	✓	101.289	283	✓	0.078	31	✓
58	K 1.58	✓	0.153	119	✓	0.078	68	✗
59	K 1.59	✓	0.177	96	✓	0.032	26	✗
60	K 1.60	✓	0.05	55	✓	0.016	29	✓
61	K 1.61	✓	0.177	75	✓	0.016	50	✓
62	K 1.62	✓	3.808	40	✓	0.297	34	✗(hange
63	K 1.63	✓	558.948	47	✓	0.094	35	✗
64	K 1.64	✓	0.188	269	✓	0.078	124	✗
65	K 1.65	✓	1.551	312	✓	0.063	47	✗(hange
66	K 1.66	✓	877.252	65	✓	0.062	40	✓
67	K 1.67	✓	0.08	14	✓	0.015	32	✗(hange
68	K 1.68	✓	1.109	373	✓	0.047	77	✗(hange
69	K 1.69	✓	53.802	12750	✓	0.109	111	✗(hange
70	K 1.70	✓	159.017	23353	✓	0.110	113	
71	K 1.71	✓	2.352	2237	✓	0.078	113	
72	K 1.72	✓	0.818	87	✓	0.016	64	
73	K 1.73	✓	1.033	733	✓	0.187	91	
74	K 1.74	✗	2.973	39	✗	0.484	0	
75	K 1.75	✓	0.191	20	✓	0.109	20	
76	K 1.76	✓	0.14	116	✓	0.031	54	
77	K 1.77	✓	0.318	124	✓	0.062	65	
78	K 1.78	✓	0.861	1317	✓	0.655	118	
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#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
79	K 1.79	✗	32.093	29	✗	0.748	0	
80	K 1.80	✗	23.832	36	✓	0.811	41	
81	K 1.81	✗	43.305	19	✓	0.827	78	
82	K 1.82	✗	49.921	27	✗	8.471	0	
83	K 1.83	✗	40.401	18	✓	0.297	44	
84	K 1.84	✓	8.757	244	✓	0.031	37	
85	K 1.85	✓	155.677	235	✓	0.359	153	
86	K 1.86	✗(hanged)	0	0	✓	0.312	52	
87	K 1.87	✗	28.157	56	✗	1.154	0	
88	K 1.88	✓	0.287	2831	✓	0.156	420	
89	K 1.89	✓	0.031	48	✓	0.016	56	
90	K 1.90	✓	0.013	24	✓	0.016	17	
91	K 1.91	✓	0.006	15	✓	0.015	11	
92	K 1.92	✓	0.012	15	✓	0.0	13	
93	K 1.93	✓	0.025	16	✓	0.0	14	
94	K 1.94	✓	0.014	25	✓	0.0	23	
95	K 1.95	✓	0.015	32	✓	0.062	40	
96	K 1.96	✓	0.022	33	✓	0.031	11	
97	K 1.97	✓	0.025	46	✓	0.031	31	
98	K 1.98	✓	0.023	442	✓	0.046	38	
99	K 1.99	✓	0.017	244	✓	0.078	237	
100	K 1.100	✓	0.008	157	✓	0.062	59	
101	K 1.101	✓	0.008	18	✓	0.016	16	
102	K 1.102	✓	0.019	36	✓	0.031	24	
103	K 1.103	✓	0.097	90	✓	0.031	29	
104	K 1.104	✓	0.016	43	✓	0.047	63	
105	K 1.105	✓	0.187	473	✓	0.202	844	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
106	K 1.106	✓	0.037	40	✓	0.046	42	
107	K 1.107	✓	0.258	1415	✓	0.156	176	
108	K 1.108	✓	0.011	15	✓	0.0	13	
109	K 1.109	✓	0.011	17	✓	0.015	15	
110	K 1.110	✗	20.764	26	✗	0.093	0	
111	K 1.111	✓	0.273	55	✓	0.125	54	
112	K 1.112	✓	0.022	13	✓	0.031	27	
113	K 1.113	✓	0.023	16	✓	0.015	33	
114	K 1.114	✓	0.02	12	✓	0.936	28	
115	K 1.115	✓	0.123	99	✓	0.156	49	
116	K 1.116	✓	0.411	143	✓	0.156	144	
117	K 1.117	✓	0.025	21	✓	0.078	20	
118	K 1.118	✓	0.011	13	✓	0.047	8	
119	K 1.119	✓	0.03	17	✓	0.047	14	
120	K 1.120	✓	0.049	20	✓	0.125	17	
121	K 1.121	✗	3.055	22	✗	0.982	0	
122	K 1.122	✓	0.072	21	✓	0.297	16	
123	K 1.123	✓	0.059	19	✓	0.047	44	
124	K 1.124	✓	0.027	16	✓	0.015	12	
125	K 1.125	✓	0.039	16	✓	0.047	14	
126	K 1.126	✓	15.029	112	✓	0.016	29	
127	K 1.127	✗(hanged)	0	0	✓	0.078	39	
128	K 1.128	✓	5.143	39	✓	0.203	33	
129	K 1.129	✓	0.028	44	✓	0.032	41	
130	K 1.130	✓	0.006	21	✓	0.0	15	
131	K 1.131	✓	0.018	21	✓	0.141	34	
132	K 1.132	✓	0.011	115	✓	0.031	234	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
133	K 1.133	✓	0.007	27	✓	0.015	16	
134	K 1.134	✓	0.011	27	✓	0.0	17	
135	K 1.135	✓	0.007	14	✓	0.016	11	
136	K 1.136	✓	0.013	28	✓	0.015	18	
137	K 1.137	✓	0.009	16	✓	0.0	15	
138	K 1.138	✓	0.014	13	✓	0.031	11	
139	K 1.139	✓	0.131	821	✓	0.094	296	
140	K 1.140	✓	0.01	17	✓	0.032	23	
141	K 1.141	✓	0.026	67	✓	0.031	64	
142	K 1.142	✓	0.182	113	✓	0.078	61	
143	K 1.143	✓	0.009	51	✓	0.032	49	
144	K 1.144	✓	0.169	1712	✓	0.078	244	
145	K 1.145	✓	0.39	267	✓	0.078	117	
146	K 1.146	✓	0.508	78	✓	0.141	82	
147	K 1.147	✓	0.523	343	✓	0.156	178	
148	K 1.148	✓	0.012	30	✓	0.0	16	
149	K 1.149	✓	0.011	27	✓	0.0	20	
150	K 1.150	✓	0.008	30	✓	0.0	19	
151	K 1.151	✓	0.421	203	✓	0.047	85	
152	K 1.152	✓	0.242	40	✓	0.530	25	
153	K 1.153	✓	0.017	21	✓	0.015	20	
154	K 1.154	✓	0.013	26	✓	0.015	16	
155	K 1.155	✓	0.017	46	✓	0.094	14	
156	K 1.156	✓	0.016	21	✓	0.016	20	
157	K 1.157	✓	0.086	158	✓	0.188	231	
158	K 1.158	✓	0.034	31	✓	0.0	22	
159	K 1.159	✓	0.018	22	✓	0.078	13	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
160	K 1.160	✓	0.02	27	✓	0.015	29	
161	K 1.161	✓	0.013	53	✓	0.016	27	
162	K 1.162	✓	0.261	133	✓	0.125	128	
163	K 1.163	✓	0.011	43	✓	0.031	26	
164	K 1.164	✓	0.082	131	✓	0.156	102	
165	K 1.165	✓	0.017	22	✓	0.015	17	
166	K 1.166	✓	0.083	71	✓	0.109	97	
167	K 1.167	✓	0.022	35	✓	0.031	20	
168	K 1.168	✓	0.093	234	✓	0.140	140	
169	K 1.169	✓	2.096	149	✓	0.141	153	
170	K 1.170	✓	0.022	43	✓	0.016	23	
171	K 1.171	✓	0.01	17	✓	0.0	15	
172	K 1.172	✓	0.041	35	✓	0.203	26	
173	K 1.173	✓	0.016	29	✓	0.031	27	
174	K 1.174	✓	0.006	17	✓	0.0	13	
175	K 1.175	✓	0.02	24	✓	0.031	21	
176	K 1.176	✓	0.124	82	✓	0.078	45	
177	K 1.177	✓	0.016	22	✓	0.015	18	
178	K 1.178	✓	0.068	62	✓	0.110	63	
179	K 1.179	✓	1.567	2816	✓	0.109	145	
180	K 1.180	✓	0.123	132	✓	0.047	58	
181	K 1.181	✓	0.012	347	✓	0.063	30	
182	K 1.182	✓	0.175	96	✓	0.093	18	
183	K 1.183	✓	0.014	22	✓	0.0	18	
184	K 1.184	✓	1.468	704	✓	0.234	846	
185	K 1.185	✓	0.376	123	✓	0.031	63	
186	K 1.186	✓	0.029	19	✓	0.031	17	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
187	K 1.187	✓	0.07	328	✓	0.047	88	
188	K 1.188	✗	21.064	33	✓	0.031	32	
189	K 1.189	✓	59.179	90	✓	0.187	61	
190	K 1.190	✓	0.052	55	✓	0.0	29	
191	K 1.191	✓	0.03	52	✓	0.015	16	
192	K 1.192	✓	0.028	57	✓	0.016	36	
193	K 1.193	✓	0.008	16	✓	0.0	14	
194	K 1.194	✓	0.076	98	✓	0.015	23	
195	K 1.195	✓	0.058	27	✓	0.093	28	
196	K 1.196	✓	0.054	53	✓	0.062	29	
197	K 1.197	✓	0.041	98	✓	0.031	364	
198	K 1.198	✓	0.025	15	✓	0.0	15	
199	K 1.199	✓	0.185	15	✓	0.125	100	
200	K 1.200	✓	0.051	77	✓	0.032	56	
201	K 1.201	✓	0.078	38	✓	0.031	23	
202	K 1.202	✗	20.513	22	✗	0.172	0	
203	K 1.203	✗	3.319	19	✗	1.779	0	
204	K 1.204	✓	0.097	70	✓	0.218	88	
205	K 1.205	✗	24.751	33	✗	0.967	0	
206	K 1.206	✗	30.06	26	✗	0.780	0	
207	K 1.207	✓	0.011	47	✓	0.016	37	
208	K 1.208	✓	0.065	118	✓	0.047	116	
209	K 1.209	✓	0.021	84	✓	0.016	21	
210	K 1.210	✓	0.016	47	✓	0.016	33	
211	K 1.211	✓	38.749	40	✓	0.016	31	
212	K 1.212	✓	22.411	92	✓	0.094	30	
213	K 1.213	✓	0.101	71	✓	0.624	73	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
214	K 1.214	✓	0.109	78	✓	0.125	65	
215	K 1.215	✓	0.119	80	✓	0.125	68	
216	K 1.216	✓	0.102	82	✓	0.125	68	
217	K 1.217	✓	0.019	29	✓	0.047	23	
218	K 1.218	✓	0.103	257	✓	0.140	53	
219	K 1.219	✗(hanged)	0	0	✗	0.873	0	
220	K 1.220	✓	0.012	57	✓	0.016	43	
221	K 1.221	✓	0.018	35	✓	0.047	21	
222	K 1.222	✓	0.057	65	✓	0.047	31	
223	K 1.223	✓	0.025	55	✓	0.109	53	
224	K 1.224	✓	0.018	29	✓	0.047	35	
225	K 1.225	✓	0.016	33	✓	0.031	20	
226	K 1.226	✓	0.016	35	✓	0.047	21	
227	K 1.227	✓	0.011	107	✓	0.109	38	
228	K 1.228	✓	0.196	3357	✓	0.280	377	
229	K 1.229	✓	0.011	121	✓	0.125	33	
230	K 1.230	✓	0.122	96	✓	0.047	104	
231	K 1.231	✓	2.446	252	✓	0.156	206	
232	K 1.232	✓	0.009	56	✓	0.015	39	
233	K 1.233	✓	0.025	38	✓	0.031	30	
234	K 1.234	✗	29.157	33	✗	1.731	0	
235	K 1.235	✓	0.043	40	✓	0.047	30	
236	K 1.236	✓	0.016	114	✓	0.047	147	
237	K 1.237	✗	7.597	24	✗	2.293	0	
238	K 1.238	✓	0.042	192	✓	0.062	146	
239	K 1.239	✓	0.029	54	✓	0.125	59	
240	K 1.240	✓	0.009	41	✓	0.016	33	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
241	K 1.241	✓	0.009	41	✓	0.015	33	
242	K 1.242	✓	0.014	60	✓	0.015	39	
243	K 1.243	✓	8.05	487	✓	0.093	493	
244	K 1.244	✓	7.973	484	✓	0.078	499	
245	K 1.245	✓	0.409	1453	✓	0.218	31	
246	K 1.246	✓	0.032	80	✓	0.047	63	
247	K 1.247	✓	7.982	693	✓	0.156	517	
248	K 1.248	✓	0.013	106	✓	0.016	71	
249	K 1.249	✓	4.955	115	✓	0.156	202	
250	K 1.250	✗(hanged)	0	0	✗	5.741	0	
251	K 1.251	✓	0.012	60	✓	0.032	50	
252	K 1.252	✓	7.836	819	✓	0.562	1623	
253	K 1.253	✗	19.448	28	✗	1.810	0	
254	K 1.254	✓	0.03	99	✓	0.016	59	
255	K 1.255	✓	5.161	31	✓	0.156	74	
256	K 1.256	✓	0.02	21	✓	0.047	31	
257	K 1.257	✓	0.358	38	✓	0.078	98	
258	K 1.258	✓	0.013	43	✓	0.016	33	
259	K 1.259	✓	0.019	50	✓	0.032	51	
260	K 1.260	✓	0.013	80	✓	0.031	59	
261	K 1.261	✓	0.864	33	✓	0.094	18	
262	K 1.262	✓	0.082	101	✓	0.218	74	
263	K 1.263	✓	0.037	121	✓	0.109	207	
264	K 1.264	✓	0.341	680	✓	0.390	574	
265	K 1.265	✗	407.591	48	✗	4.680	0	
266	K 1.266	✗(hanged)	0	0	✓	1.045	59	
267	K 1.267	✓	0.033	36	✓	0.015	32	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
268	K 1.268	✓	1.005	140	✓	0.063	124	
269	K 1.269	✗(hanged)	0	0	✗	2.652	0	
270	K 1.270	✓	0.015	327	✓	0.031	402	
271	K 1.271	✓	0.1	370	✓	0.125	417	
272	K 1.272	✓	0.045	42	✓	0.109	43	
273	K 1.273	✓	0.014	297	✓	0.015	470	
274	K 1.274	✓	0.019	411	✓	0.015	810	
275	K 1.275	✓	0.024	18	✓	0.078	30	
276	K 1.276	✓	0.036	61	✓	0.047	45	
277	K 1.277	✓	0.015	53	✓	0.234	67	
278	K 1.278	✓	0.065	39	✓	0.047	33	
279	K 1.279	✓	0.624	107	✓	0.140	120	
280	K 1.280	✓	0.036	21	✓	0.047	24	
281	K 1.281	✓	0.063	75	✓	0.047	53	
282	K 1.282	✓	0.087	2129	✓	0.156	72	
283	K 1.283	✓	0.046	477	✓	0.047	622	
284	K 1.284	✓	0.033	59	✓	0.094	21	
285	K 1.285	✓	0.029	402	✓	0.047	431	
286	K 1.286	✓	0.184	3501	✗(hanged)	0	0	
287	K 1.287	✓	0.913	77	✓	0.063	56	
288	K 1.288	✓	0.018	534	✓	0.031	587	
289	K 1.289	✓	0.017	115	✓	0.031	115	
290	K 1.290	✓	0.056	831	✓	0.062	1666	
291	K 1.291	✓	0.461	39	✓	0.109	50	
292	K 1.292	✓	54.667	760	✓	0.031	124	
293	K 1.293	✓	0.106	661	✓	0.234	36	
294	K 1.294	✓	0.04	71	✓	0.078	112	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
295	K 1.295	✓	0.037	31	✓	0.141	29	
296	K 1.296	✓	0.571	102	✓	0.562	165	
297	K 1.297	✓	0.058	216	✓	0.219	29	
298	K 1.298	✓	0.009	72	✓	0.015	99	
299	K 1.299	✓	0.017	371	✓	0.125	327	
300	K 1.300	✓	0.01	99	✓	0.015	120	
301	K 1.301	✓	0.039	64	✓	0.156	25	
302	K 1.302	✓	0.016	70	✓	0.109	137	
303	K 1.303	✓	0.044	25	✓	0.125	34	
304	K 1.304	✓	45.176	59	✓	0.156	44	
305	K 1.305	✓	0.018	1277	✓	0.015	21	
306	K 1.306	✓	0.051	201	✓	0.250	391	
307	K 1.307	✓	0.024	149	✓	0.046	125	
308	K 1.308	✓	0.007	55	✓	0.015	37	
309	K 1.309	✓	0.011	151	✓	0.047	113	
310	K 1.310	✓	0.044	159	✓	0.109	125	
311	K 1.311	✓	0.052	2201	✓	0.062	50	
312	K 1.312	✓	0.246	204	✓	1.061	236	
313	K 1.313	✓	0.069	537	✓	0.156	912	
314	K 1.314	✓	0.043	188	✓	0.047	170	
315	K 1.315	✓	0.115	368	✓	0.062	447	
316	K 1.316	✓	0.039	48	✓	0.047	53	
317	K 1.317	✓	0.321	23	✓	0.093	29	
318	K 1.318	✓	0.06	4284	✓	0.016	28	
319	K 1.319	✓	0.024	302	✓	0.031	33	
320	K 1.320	✓	0.057	76	✓	0.078	70	
321	K 1.321	✓	0.181	47	✓	0.125	42	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
322	K 1.322	✓	0.025	2077	✓	0.031	28	
323	K 1.323	✓	0.032	463	✓	0.093	761	
324	K 1.324	✓	0.026	723	✓	0.109	770	
325	K 1.325	✓	0.049	139	✓	0.296	1192	
326	K 1.326	✓	0.272	13289	✓	0.343	160	
327	K 1.327	✓	0.385	669	✓	0.156	583	
328	K 1.328	✓	0.095	42	✓	0.140	33	
329	K 1.329	✓	0.314	102	✓	0.249	78	
330	K 1.330	✓	32.94	49	✓	0.031	22	
331	K 1.331	✗(hanged)	0	0	✗(hanged)	0	0	
332	K 1.332	✓	0.081	24	✓	0.015	31	
333	K 1.333	✓	0.173	72	✓	0.062	32	
334	K 1.334	✓	0.036	39	✓	0.031	19	
335	K 1.335	✓	0.181	75	✓	0.0	50	
336	K 1.336	✓	0.063	53	✓	0.031	41	
337	K 1.337	✓	0.059	52	✓	0.031	28	
338	K 1.338	✓	77.787	17681	✓	0.530	136	
339	K 1.339	✓	0.11	27	✓	0.140	27	
340	K 1.340	✗(hanged)	0	0	✗(hanged)	0	0	
341	K 1.341	✓	0.05	33	✓	0.047	30	
342	K 1.342	✓	0.261	163	✓	0.031	17	
343	K 1.343	✓	0.038	35	✓	0.046	27	
344	K 1.344	✓	0.019	23	✓	0.016	19	
345	K 1.345	✓	0.041	35	✓	0.063	36	
346	K 1.346	✓	0.054	24	✓	0.202	19	
347	K 1.347	✓	0.118	32	✓	0.094	16	
348	K 1.348	✓	0.048	17	✓	0.078	15	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
349	K 1.349	✓	0.039	15	✓	0.031	15	
350	K 1.350	✓	0.544	53	✓	0.718	270	
351	K 1.351	✓	0.367	61	✓	0.343	55	
352	K 1.352	✓	0.132	43	✓	0.188	35	
353	K 1.353	✓	0.02	14	✓	0.047	12	
354	K 1.354	✓	0.064	145	✓	0.047	115	
355	K 1.355	✓	0.048	17	✓	0.062	15	
356	K 1.356	✓	0.062	21	✓	0.078	19	
357	K 1.357	✓	0.318	35	✓	0.406	13	
358	K 1.358	✓	0.044	29	✓	0.062	11	
359	K 1.359	✓	0.056	45	✓	0.047	28	
360	K 1.360	✓	4.99	369	✓	0.124	48	
361	K 1.361	✓	0.213	31	✓	0.172	22	
362	K 1.362	✓	0.07	23	✓	0.110	23	
363	K 1.363	✓	0.035	33	✓	0.062	35	
364	K 1.364	✓	0.064	31	✓	0.078	23	
365	K 1.365	✗(hanged)	0	0	✓	0.218	42	
366	K 1.366	✓	264.973	88	✓	0.046	45	
367	K 1.367	✗	22.563	46	✗	0.874	0	
368	K 1.368	✗(hanged)	0	0	✗(hanged)	0	0	
369	K 1.369	✓	0.047	107	✓	0.514	68	
370	K 1.370	✗	22.439	23	✗	1.404	0	
371	K 1.371	✓	0.026	37	✓	0.468	20	
372	K 1.372	✓	0.004	27	✓	0.499	271	
373	K 1.373	✓	0.109	71	✓	0.187	47	
374	K 1.374	✓	0.062	73	✓	0.406	85	
375	K 1.375	✓	0.063	71	✓	0.468	49	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
376	K 1.376	✓	0.313	110	✓	0.796	215	
377	K 1.377	✓	0.006	19	✓	0.390	25	
378	K 1.378	✓	0.005	18	✓	0.452	32	
379	K 1.379	✓	0.004	18	✓	0.422	27	
380	K 1.380	✓	0.411	1757	✓	0.437	690	
381	K 1.381	✓	0.421	1757	✓	0.405	656	
382	K 1.382	✓	0.255	201	✓	0.390	146	
383	K 1.383	✗(hanged)	0	0	✗(hanged)	0	0	
384	K 1.384	✓	2.056	183	✓	0.468	50	
385	K 1.385	✗(hanged)	0	0	✓	0.562	169	
386	K 1.386	✓	0.205	56	✓	0.655	27	
387	K 1.387	✓	0.536	134	✓	1.202	115	
388	K 1.388	✓	0.67	53	✓	0.499	217	
389	K 1.389	✓	0.074	109	✓	0.811	193	
390	K 1.390	✓	1.796	142	✓	0.655	416	
391	K 1.391	✓	0.006	29	✓	0.0	22	
392	K 1.392	✓	0.255	27	✓	0.312	50	
393	K 1.393	✓	0.073	31	✓	0.858	85	
394	K 1.394	✗	58.133	52	✓	3.822	310	
395	K 1.395	✗	38.766	32	✗	0.968	0	
396	K 1.396	✓	0.014	29	✓	0.016	20	
397	K 1.397	✓	0.432	143	✓	0.671	131	
398	K 1.398	✓	0.737	258	✓	2.402	137	
399	K 1.399	✓	0.004	20	✓	0.515	29	
400	K 1.400	✗(hanged)	0	0	✓	0.624	123	
401	K 1.401	✓	0.354	1093	✓	0.452	656	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
402	K 1.402	<del>X</del> (hanged)	0	0	✓	0.577	121	
403	K 1.403	✓	0.303	116	✓	0.858	197	
404	K 1.404	<del>X</del> (hanged)	0	0	✓	0.686	499	
405	K 1.405	✓	1.014	53	✓	0.593	380	
406	K 1.406	✓	0.864	49	✓	0.577	266	
407	K 1.407	✓	0.021	51	✓	0.499	39	
408	K 1.408	✓	0.532	166	✓	0.514	73	
409	K 1.409	✓	30.78	66	✓	0.468	63	
410	K 1.410	✓	31.056	80	✓	0.546	64	
411	K 1.411	✓	0.559	181	✓	0.531	69	
412	K 1.412	✓	5.287	16145	✓	0.546	146	
413	K 1.413	<del>X</del> (hanged)	0	0	✓	0.640	337	
414	K 1.414	<del>X</del> (hanged)	0	0	✓	0.639	337	
415	K 1.415	✓	0.21	133	✓	0.655	95	
416	K 1.416	<del>X</del> (hanged)	0	0	✓	0.546	136	
417	K 1.417	✓	0.374	430	✓	0.484	33	
418	K 1.418	✓	0.446	165	✓	0.515	55	
419	K 1.419	✓	0.68	9073	✓	0.531	110	
420	K 1.420	✓	1.329	11757	✓	0.546	897	
421	K 1.421	✓	0.032	27	✓	0.437	31	
422	K 1.422	✓	0.047	49	✓	0.515	29	
423	K 1.423	✓	0.079	59	✓	0.515	52	
424	K 1.424	✓	0.378	223	✓	0.546	224	
425	K 1.425	✓	0.27	59	✓	0.562	59	
426	K 1.426	✓	0.392	310	✓	0.546	49	
427	K 1.427	✓	0.635	479	✓	0.452	67	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
428	K 1.428	<del>X</del> (hanged)	0	0	✓	0.546	85	
429	K 1.429	<del>X</del> (hanged)	0	0	✓	0.437	96	
430	K 1.430	<del>X</del> (hanged)	0	0	✓	1.201	9885	
431	K 1.431	✓	0.037	111	✓	0.561	62	
432	K 1.432	✓	1.714	64	✓	7.551	615	
433	K 1.433	✓	0.51	22	✓	0.640	32	
434	K 1.434	✓	0.032	27	✓	0.015	7	
435	K 1.435	✓	0.037	61	✓	0.671	22	
436	K 1.436	✓	0.035	26	✓	1.809	59	
437	K 1.437	✓	0.274	47	✓	0.515	36	
438	K 1.438	✓	0.011	21	✓	0.0	17	
439	K 1.439	✓	0.035	49	✓	0.546	33	
440	K 1.440	✓	0.009	19	✓	0.0	15	
441	K 1.441	✓	0.065	65	✓	1.311	265	
442	K 1.442	✓	0.008	28	✓	0.0	21	
443	K 1.443	✓	0.553	1921	✓	1.638	221	
444	K 1.444	✓	0.144	103	✓	1.045	121	
445	K 1.445	✓	0.009	49	✓	0.016	35	
446	K 1.446	✓	0.491	201	✓	0.577	57	
447	K 1.447	✓	0.016	41	✓	0.468	33	
448	K 1.448	✓	0.092	109	✓	10.858	166	
449	K 1.449	✓	0.01	27	✓	0.0	23	
450	K 1.450	✓	0.453	26	✓	0.795	51	
451	K 1.451	<del>X</del> (hanged)	0	0	✓	0.561	78	
452	K 1.452	<del>X</del> (hanged)	0	0	<del>X</del>	1.779	37	
453	K 1.453	✓	0.573	395	✓	1.170	229	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
454	K 1.454	✓	0.155	118	✓	0.593	138	
455	K 1.455	✓	0.401	123	✓	0.686	66	
456	K 1.456	✓	0.123	79	✓	0.874	33	
457	K 1.457	✓	0.948	410	✓	1.186	135	
458	K 1.458	✓	0.06	139	✓	0.593	90	
459	K 1.459	✓	2.603	271	✓	0.422	65	
460	K 1.460	✗	56.015	28	✗	5.163	0	
461	K 1.461	✗	108.142	49	✗	19.953	0	
462	K 1.462	✓	0.015	43	✓	0.577	27	
463	K 1.463	✓	0.017	47	✓	1.092	50	
464	K 1.464	✓	0.061	52	✓	0.983	71	
465	K 1.465	✗(hanged)	0	0	✓	0.640	209	
466	K 1.466	✓	0.249	145	✓	0.811	71	
467	K 1.467	✗(hanged)	0	0	✓	0.655	148	
468	K 1.468	✗(hanged)	0	0	✓	0.577	181	
469	K 1.469	✓	0.945	317	✓	0.639	242	
470	K 1.470	✓	0.883	454	✓	0.780	87	
471	K 1.471	✓	0.007	47	✓	0.015	33	
472	K 1.472	✓	0.186	127	✓	0.936	119	
473	K 1.473	✓	0.407	165	✓	0.936	78	
474	K 1.474	✓	0.232	135	✓	1.295	154	
475	K 1.475	✓	0.098	205	✓	0.936	69	
476	K 1.476	✓	0.843	454	✓	0.874	87	
477	K 1.477	✓	0.305	146	✓	0.858	929	
478	K 1.478	✓	0.167	141	✓	0.609	88	
479	K 1.479	✗(hanged)	0	0	✓	0.811	929	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
480	K 1.480	✗	30.55	41	✗	2.044	0	
481	K 1.481	✓	0.009	49	✓	0.016	35	
482	K 1.482	✗	65.128	38	✗	1.264	0	
483	K 1.483	✓	0.157	71	✓	0.624	109	
484	K 1.484	✓	0.171	81	✗(hanged)	0	0	
485	K 1.485	✗(hanged)	0	0	✗(hanged)	0	0	
486	K 1.486	✓	0.024	117	✓	0.608	59	
487	K 1.487	✗(hanged)	0	0	✓	0.858	114	
488	K 1.488	✓	0.367	85	✓	0.905	113	
489	K 1.489	✗(hanged)	0	0	✓	2.621	5525	
490	K 1.490	✓	0.601	70	✓	0.920	145	
491	K 1.491	✓	1.033	79	✓	1.107	251	
492	K 1.492	✓	0.283	111	✓	0.905	122	
493	K 1.493	✓	8.601	553	✓	1.341	124	
494	K 1.494	✗(hanged)	0	0	✓	0.764	173	
495	K 1.495	✓	0.11	83	✓	0.905	61	
496	K 1.496	✓	95.092	65	✓	0.718	130	
497	K 1.497	✓	0.174	203	✓	0.889	203	
498	K 1.498	✓	0.104	107	✓	0.749	99	
499	K 1.499	✓	0.334	212	✓	0.702	201	
500	K 1.500	✓	1.323	100	✓	1.232	260	
501	K 1.501	✓	33.601	913	✓	4.259	287	
502	K 1.502	✓	1.718	100	✓	0.890	195	
503	K 1.503	✗(hanged)	0	0	✗	33.103	0	
504	K 1.504	✗(hanged)	0	0	✓	1.201	303	
505	K 1.505	✓	0.013	73	✓	0.032	52	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
506	K 1.506	<del>X</del>	47.848	58	<del>X</del>	1.310	0	
507	K 1.507	✓	29.711	443	<del>X</del> (hanged)	0	0	
508	K 1.508	✓	55.172	47	✓	2.122	60	
509	K 1.509	<del>X</del> (hanged)	0	0	✓	1.622	245	
510	K 1.510	<del>X</del>	60.566	66	<del>X</del>	2.730	0	
511	K 1.511	✓	1.556	229	✓	8.112	199	
512	K 1.512	✓	4.686	725	✓	40.935	135	
513	K 1.513	<del>X</del> (hanged)	0	0	✓	1.748	2402	
514	K 1.514	✓	15.435	605	✓	0.140	87	
515	K 1.515	<del>X</del> (hanged)	0	0	✓	1.888	113	
516	K 1.516	✓	2.612	251	✓	0.827	141	
517	K 1.517	✓	2.739	281	✓	0.812	78	
518	K 1.518	✓	0.801	236	✓	0.156	126	
519	K 1.519	✓	1.828	473	✓	0.250	197	
520	K 1.520	✓	151.473	3323	✓	0.062	245	
521	K 1.521	✓	0.004	14	✓	0.031	33	
522	K 1.522	✓	0.004	20	✓	0.047	46	
523	K 1.523	<del>X</del> (hanged)	0	0	✓	0.046	299	
524	K 1.524	<del>X</del> (hanged)	0	0	✓	0.047	295	
525	K 1.525	✓	0.063	135	✓	0.062	125	
526	K 1.526	✓	0.01	45	✓	0.016	32	
527	K 1.527	<del>X</del> (hanged)	0	0	✓	0.671	43	
528	K 1.528	<del>X</del> (hanged)	0	0	✓	0.078	95	
529	K 1.529	✓	52.152	1758	✓	0.031	1473	
530	K 1.530	<del>X</del> (hanged)	0	0	✓	0.094	421	
531	K 1.531	<del>X</del>	73.501	72	<del>X</del>	1.935	0	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
532	K 1.532	✓	3505.56	1258	✓	0.125	1211	
533	K 1.533	✗(hanged)	0	0	✓	0.032	92	
534	K 1.534	✗(hanged)	0	0	✓	0.062	102	
535	K 1.535	✗(hanged)	0	0	✓	0.046	80	
536	K 1.536	✓	0.024	86	✓	0.016	52	
537	K 1.537	✗(hanged)	0	0	✗(hanged)	0	0	
538	K 1.538	✗(hanged)	0	0	✓	0.608	3181	
539	K 1.539	✓	0.027	45	✓	0.031	32	
540	K 1.540	✓	0.02	69	✓	0.047	109	
541	K 1.541	✗(hanged)	0	0	✓	0.499	103	
542	K 1.542	✗(hanged)	0	0	✓	0.500	107	
543	K 1.543	✗(hanged)	0	0	✗	1.060	325	
544	K 1.544	✗(hanged)	0	0	✓	0.686	7860	
545	K 1.545	✓	0.702	383	✓	0.140	141	
546	K 1.546	✗(hanged)	0	0	✓	0.125	245	
547	K 1.547	✓	1.233	490	✓	0.171	118	
548	K 1.548	✓	1.006	569	✓	0.234	241	
549	K 1.549	✓	0.246	406	✓	0.140	552	
550	K 1.550	✗(hanged)	0	0	✓	0.203	61	
551	K 1.551	✓	0.381	84	✓	0.297	127	
552	K 1.552	✓	0.164	39	✓	0.062	43	
553	K 1.553	✓	0.12	51	✓	0.031	36	
554	K 1.554	✓	0.075	49	✓	0.266	29	
555	K 1.555	✗(hanged)	0	0	✓	0.015	15	
556	K 1.556	✓	6.601	60	✓	0.156	581	
557	K 1.557	✓	0.016	39	✓	0.093	78	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
558	K 1.558	✓	0.587	395	✓	0.140	223	
559	K 1.559	✓	0.351	212	✓	0.234	223	
560	K 1.560	✓	21.647	110	✓	0.671	1512	
561	K 1.561	✗(hanged)	0	0	✓	1.919	50	
562	K 1.562	✓	264.371	119	✓	0.094	3961	
563	K 1.563	✓	0.109	59	✓	0.125	66	
564	K 1.564	✓	0.042	28	✓	0.031	36	
565	K 1.565	✓	0.012	25	✓	0.093	17	
566	K 1.566	✗	0.01	19	✓	0.031	16	
567	K 1.567	✗	0.011	21	✓	0.031	18	
568	K 1.568	✓	0.037	28	✓	0.047	32	
569	K 1.569	✓	0.041	59	✓	0.358	147	
570	K 1.570	✗	0.109	29	✓	0.047	30	
571	K 1.571	✓	0.102	114	✓	0.203	199	
572	K 1.572	✗	0.031	41	✗	0.905	0	
573	K 1.573	✓	0.012	42	✓	0.109	16	
574	K 1.574	✓	0.015	102	✓	0.109	67	
575	K 1.575	✗	0.017	41	✗	0.452	0	
576	K 1.576	✗	0.007	23	✗	0.016	0	
577	K 1.577	✓	12.112	240	✓	0.031	28	
578	K 1.578	✓	16.413	97	✓	0.031	22	
579	K 1.579	✓	13.258	510	✓	0.031	35	
580	K 1.580	✓	24.434	200	✓	0.047	31	
581	K 1.581	✓	40.987	141	✓	0.093	32	
582	K 1.582	✓	16.7	139	✓	0.156	30	
583	K 1.583	✓	41.456	123	✓	0.125	31	
584	K 1.584	✓	18.982	112	✓	0.047	35	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
585	K 1.585	✓	123.304	202	✓	0.406	163	
586	K 1.586	✓	143.313	972	✓	0.203	39	
587	K 1.587	✓	44.026	120	✓	0.109	29	
588	K 1.588	✓	31.941	106	✓	0.109	53	
589	K 1.589	✓	19.556	242	✓	0.124	38	
590	K 1.590	✓	30.944	91	✓	0.125	28	
591	K 1.591	✓	18.189	250	✓	0.140	108	
592	K 1.592	✓	248.172	238	✓	0.156	33	
593	K 1.593	✓	62.104	218	✓	0.265	35	
594	K 1.594	✓	17.878	233	✓	0.140	67	
595	K 1.595	✓	19.349	201	✓	0.124	72	
596	K 1.596	✓	49.763	153	✓	0.093	26	
597	K 1.597	✓	27.164	127	✓	0.296	37	
598	K 1.598	✓	0.077	36	✓	0.032	29	
599	K 1.599	✓	22.629	92	✓	0.093	57	
600	K 1.600	✓	24.087	243	✓	0.141	38	
601	K 1.601	✓	32.152	179	✓	0.125	61	
602	K 1.602	✓	46.097	164	✓	0.125	33	
603	K 1.603	✓	17.469	114	✓	0.124	27	
604	K 1.604	✓	26.277	140	✓	0.141	30	
605	K 1.605	✓	28.542	142	✓	0.125	29	
606	K 1.606	✓	64.107	358	✓	0.655	34	
607	K 1.607	✓	739.416	118	✓	0.078	22	
608	K 1.608	✓	284.31	271	✓	0.125	40	
609	K 1.609	✓	51.408	114	✓	0.140	22	
610	K 1.610	✓	0.063	24	✓	0.016	20	
611	K 1.611	✓	39.069	188	✓	0.078	28	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
612	K 1.612	✓	49.253	196	✓	0.110	27	
613	K 1.613	✓	818.937	223	✓	0.093	23	
614	K 1.614	✓	72.938	171	✓	0.328	59	
615	K 1.615	✓	17.029	74	✓	0.109	26	
616	K 1.616	✓	52.213	174	✓	0.093	26	
617	K 1.617	✓	67.611	612	✓	0.234	47	
618	K 1.618	✓	0.104	25	✓	0.312	34	
619	K 1.619	✓	60.581	327	✓	0.359	81	
620	K 1.620	✗(hanged)	0	0	✓	0.156	37	
621	K 1.621	✓	0.099	445	✓	0.234	59	
622	K 1.622	✓	0.449	134	✓	0.172	83	
623	K 1.623	✓	0.177	77	✓	0.172	51	
624	K 1.624	✓	0.952	9837	✓	0.858	46	
625	K 1.625	✓	0.21	76	✓	0.156	53	
626	K 1.626	✓	0.196	104	✓	0.359	112	
627	K 1.627	✓	0.754	25	✓	0.141	39	
628	K 1.628	✓	0.086	33	✓	0.156	23	
629	K 1.629	✓	0.781	47	✓	0.172	72	
630	K 1.630	✓	0.567	101	✓	0.249	98	
631	K 1.631	✓	0.097	31	✓	0.172	23	
632	K 1.632	✓	0.169	65	✓	0.203	52	
633	K 1.633	✓	0.191	85	✓	0.686	52	
634	K 1.634	✓	0.185	33	✓	0.187	26	
635	K 1.635	✓	0.125	33	✓	0.156	22	
636	K 1.636	✓	0.055	24	✓	0.140	19	
637	K 1.637	✓	9.663	59	✓	1.482	84	
638	K 1.638	✗	2.786	21	✓	0.124	35	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
639	K 1.639	✗	0.364	23	✓	0.172	50	
640	K 1.640	✗	3.866	24	✓	0.203	45	
641	K 1.641	✓	0.177	35	✓	0.172	26	
642	K 1.642	✓	0.145	105	✓	0.187	286	
643	K 1.643	✓	0.119	31	✓	0.172	22	
644	K 1.644	✓	0.275	34	✓	0.265	27	
645	K 1.645	✓	0.039	20	✓	0.110	14	
646	K 1.646	✓	0.181	35	✓	0.202	23	
647	K 1.647	✓	0.423	115	✓	0.218	460	
648	K 1.648	✓	0.351	128	✓	0.437	41	
649	K 1.649	✓	0.181	37	✓	0.187	27	
650	K 1.650	✓	0.246	40	✓	0.187	28	
651	K 1.651	✓	0.038	16	✓	0.047	13	
652	K 1.652	✓	1.924	101	✓	0.124	27	
653	K 1.653	✓	0.182	34	✓	0.172	24	
654	K 1.654	✓	0.165	37	✓	0.203	23	
655	K 1.655	✓	11.359	82	✓	0.920	64	
656	K 1.656	✓	0.043	20	✓	0.062	15	
657	K 1.657	✓	0.19	37	✓	0.171	26	
658	K 1.658	✓	0.248	45	✓	0.218	28	
659	K 1.659	✓	0.441	60	✓	0.187	41	
660	K 1.660	✓	0.265	42	✓	0.188	29	
661	K 1.661	✓	0.421	61	✓	0.218	39	
662	K 1.662	✓	0.197	37	✓	0.188	26	
663	K 1.663	✓	2.294	101	✓	0.125	27	
664	K 1.664	✓	0.191	36	✓	0.171	25	
665	K 1.665	✓	0.272	41	✓	0.343	28	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
666	K 1.666	✓	0.076	29	✓	0.156	24	
667	K 1.667	✓	1.022	90	✓	0.172	83	
668	K 1.668	✓	0.537	78	✓	0.546	58	
669	K 1.669	✓	0.884	264	✓	0.203	72	
670	K 1.670	✓	0.37	99	✓	0.250	70	
671	K 1.671	✓	0.426	192	✓	0.156	237	
672	K 1.672	✗(hanged)	0	0	✓	0.156	36	
673	K 1.673	✓	0.084	23	✓	0.359	17	
674	K 1.674	✓	0.234	40	✓	0.234	27	
675	K 1.675	✓	0.057	48	✓	0.031	46	
676	K 1.676	✓	0.324	144	✓	0.374	43	
677	K 1.677	✓	0.038	80	✓	0.047	64	
678	K 1.678	✓	0.251	101	✓	0.234	37	
679	K 1.679	✓	0.036	59	✓	0.031	37	
680	K 1.680	✓	0.236	39	✓	0.218	28	
681	K 1.681	✓	0.045	84	✓	0.031	57	
682	K 1.682	✓	0.091	39	✓	0.218	28	
683	K 1.683	✓	0.361	84	✓	0.109	166	
684	K 1.684	✓	0.027	20	✓	0.920	30	
685	K 1.685	✓	0.039	87	✓	0.047	48	
686	K 1.686	✓	9.257	68	✓	1.482	85	
687	K 1.687	✓	0.064	130	✓	0.063	39	
688	K 1.688	✓	0.117	78	✓	0.062	61	
689	K 1.689	✓	0.075	60	✓	0.047	25	
690	K 1.690	✓	0.319	127	✓	0.265	40	
691	K 1.691	✓	0.08	21	✓	0.499	17	
692	K 1.692	✓	0.027	20	✓	1.186	30	

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#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
693	K 1.693	✓	0.173	146	✓	0.078	40	
694	K 1.694	✓	0.3	66	✓	0.234	30	
695	K 1.695	✓	0.052	34	✓	0.047	39	
696	K 1.696	✓	121.91	50	✓	0.047	32	
697	K 1.697	✓	0.129	114	✓	0.078	40	
698	K 1.698	✓	0.133	108	✓	0.062	34	
699	K 1.699	✓	0.244	101	✓	0.265	36	
700	K 1.700	✓	0.071	76	✓	0.094	62	
701	K 1.701	✗(hanged)	0	0	✓	4.727	100	
702	K 1.702	✓	197.341	36	✓	0.063	35	
703	K 1.703	✗(hanged)	0	0	✓	0.172	68	
704	K 1.704	✓	240.336	65	✓	0.047	45	
705	K 1.705	✓	0.062	30	✓	0.172	24	
706	K 1.706	✗(hanged)	0	0	✓	0.405	65	
707	K 1.707	✓	480.133	334	✓	0.468	105	
708	K 1.708	✓	0.299	89	✓	0.656	308	
709	K 1.709	✓	5.564	217	✓	0.203	39	
710	K 1.710	✓	1910.258	37	✓	1.685	35	
711	K 1.711	✓	0.074	28	✓	0.109	31	
712	K 1.712	✓	0.296	115	✓	0.265	38	
713	K 1.713	✓	0.135	649	✓	0.297	86	
714	K 1.714	✗(hanged)	0	0	✓	0.327	104	
715	K 1.715	✓	0.273	104	✓	0.249	39	
716	K 1.716	✓	5.77	133	✓	0.249	37	
717	K 1.717	✓	0.338	46	✓	0.281	33	
718	K 1.718	✓	0.13	127	✓	0.063	44	

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#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
719	K 1.719	✓	0.1	49	✓	0.110	57	
720	K 1.720	✓	6.128	314	✓	0.171	48	
721	K 1.721	✓	0.021	27	✓	0.062	19	
722	K 1.722	✓	63.894	491	✓	0.281	96	
723	K 1.723	✓	0.065	663	✓	0.046	864	
724	K 1.724	✓	64.507	420	✓	0.047	18	
725	K 1.725	✓	0.265	19	✓	0.561	25	
726	K 1.726	✓	0.082	625	✓	0.202	83	
727	K 1.727	✓	0.495	29	✓	0.187	25	
728	K 1.728	✓	0.435	72	✓	0.234	50	
729	K 1.729	✓	0.355	327	✓	0.093	497	
730	K 1.730	✗	33.979	55	✓	1.342	49	
731	K 1.731	✓	0.198	47	✓	0.125	42	
732	K 1.732	✓	0.498	110	✓	0.281	43	
733	K 1.733	✗(hanged)	0	0	✗(hanged)	0	0	
734	K 1.734	✓	0.122	37	✓	0.125	39	
735	K 1.735	✗(hanged)	0	0	✓	0.062	104	
736	K 1.736	✓	0.107	31	✓	0.140	47	
737	K 1.737	✓	0.034	36	✓	0.062	29	
738	K 1.738	✓	0.516	1347	✓	0.561	1096	
739	K 1.739	✓	0.132	39	✓	0.140	35	
740	K 1.740	✓	0.068	74	✓	0.093	72	
741	K 1.741	✓	3.706	175	✓	0.749	400	
742	K 1.742	✓	5.755	3913	✓	1.185	259	
743	K 1.743	✗	32.841	43	✓	0.328	269	
744	K 1.744	✓	0.043	510	✓	0.156	621	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
745	K 1.745	<del>X</del> (hanged)	0	0	✓	0.063	104	
746	K 1.746	<del>X</del>	31.24	39	✓	0.312	243	
747	K 1.747	<del>X</del> (hanged)	0	0	✓	0.281	69	
748	K 1.748	✓	0.383	285	✓	0.078	497	
749	K 1.749	✓	0.106	126	✓	0.109	192	
750	K 1.750	✓	0.423	72	✓	0.234	49	
751	K 1.751	✓	0.078	30	✓	0.093	26	
752	K 1.752	<del>X</del>	19.954	39	✓	1.060	874	
753	K 1.753	✓	0.109	41	✓	0.125	38	
754	K 1.754	✓	0.027	47	✓	0.016	26	
755	K 1.755	✓	0.178	2633	✓	0.094	44	
756	K 1.756	✓	0.08	95	✓	0.031	37	
757	K 1.757	✓	0.03	36	✓	0.062	26	
758	K 1.758	✓	1.094	459	✓	0.187	41	
759	K 1.759	<del>X</del>	40.967	46	✓	0.452	315	
760	K 1.760	✓	1.559	112	✓	1.685	475	
761	K 1.761	✓	0.028	33	✓	0.062	18	
762	K 1.762	✓	0.061	26	✓	0.093	22	
763	K 1.763	✓	0.064	22	✓	0.093	14	
764	K 1.764	✓	0.104	50	✓	0.093	36	
765	K 1.765	✓	135.603	128	✓	0.110	106	
766	K 1.766	<del>X</del> (hanged)	0	0	✓	0.234	85	
767	K 1.767	✓	0.753	38	✓	0.062	26	
768	K 1.768	✓	0.977	70	✓	0.062	26	
769	K 1.769	<del>X</del>	42.445	46	✓	0.359	251	
770	K 1.770	✓	0.106	705	✓	0.094	1345	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
771	K 1.771	✓	0.053	46	✓	0.078	84	
772	K 1.772	✓	0.109	21	✓	0.093	18	
773	K 1.773	✓	0.053	61	✓	0.218	48	
774	K 1.774	✓	0.027	45	✓	0.078	50	
775	K 1.775	✓	0.095	943	✓	0.078	60	
776	K 1.776	✗(hanged)	0	0	✓	0.234	92	
777	K 1.777	✓	0.086	39	✓	0.125	51	
778	K 1.778	✓	0.063	95	✓	0.031	37	
779	K 1.779	✓	0.029	57	✓	0.078	50	
780	K 1.780	✓	0.023	15	✓	0.280	27	
781	K 1.781	✓	0.496	82	✓	0.249	61	
782	K 1.782	✗(hanged)	0	0	✓	0.530	92	
783	K 1.783	✗(hanged)	0	0	✓	0.203	69	
784	K 1.784	✗(hanged)	0	0	✓	26.208	24	
785	K 1.785	✗(hanged)	0	0	✓	96.767	24	
786	K 1.786	✗(hanged)	0	0	✓	0.047	39	
787	K 1.787	✓	19.683	487	✓	0.437	191	
788	K 1.788	✗(hanged)	0	0	✗(hanged)	0	0	
789	K 1.789	✗(hanged)	0	0	✗(hanged)	0	0	
790	K 1.790	✓	1267.681	95	✗(hanged)	0	0	
791	K 1.791	✓	1670.398	87	✓	12.699	634	
792	K 1.792	✓	0.	0	✓	0.312	114	
793	K 1.793	✓	13.842	397	✓	0.078	32	
794	K 1.794	✓	0.092	67	✓	0.390	32	
795	K 1.795	✓	0.157	111	✓	0.032	37	
796	K 1.796	✓	9.404	102	✓	1.155	143	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
797	K 1.797	✓	2.028	349	✓	0.141	281	
798	K 1.798	✓	0.552	27	✓	0.109	30	
799	K 1.799	✓	0.301	70	✓	0.234	147	
800	K 1.800	✓	0.176	128	✓	0.015	41	
801	K 1.801	✓	0.101	126	✓	0.047	63	
802	K 1.802	✓	0.076	98	✓	0.125	27	
803	K 1.803	✓	0.08	386	✓	0.327	65	
804	K 1.804	✓	0.493	43	✓	0.827	38	
805	K 1.805	✓	0.056	37	✓	0.422	42	
806	K 1.806	✓	0.27	23	✓	0.468	22	
807	K 1.807	✗	1.853	34	✓	0.468	43	
808	K 1.808	✓	1.138	127	✓	0.062	44	
809	K 1.809	✓	0.153	128	✓	0.015	41	
810	K 1.810	✓	0.015	40	✓	0.062	16	
811	K 1.811	✓	2.217	33	✓	1.544	32	
812	K 1.812	✓	0.327	70	✓	0.312	32	
813	K 1.813	✓	0.493	66	✓	0.327	38	
814	K 1.814	✓	0.014	72	✓	0.016	38	
815	K 1.815	✓	10.173	103	✓	1.326	202	
816	K 1.816	✓	0.141	74	✓	0.624	307	
817	K 1.817	✓	0.384	63	✓	0.500	27	
818	K 1.818	✓	0.047	34	✓	0.109	34	
819	K 1.819	✓	0.23	65	✓	0.265	32	
820	K 1.820	✓	0.341	63	✓	0.530	27	
821	K 1.821	✓	0.034	2093	✓	0.124	27	
822	K 1.822	✓	0.042	32	✓	0.109	25	
823	K 1.823	✓	0.383	39	✓	0.109	38	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
824	K 1.824	✓	0.055	68	✓	0.280	61	
825	K 1.825	✓	0.183	148	✓	0.062	89	
826	K 1.826	✓	0.57	70	✓	0.234	51	
827	K 1.827	✓	0.125	111	✓	0.156	49	
828	K 1.828	✓	0.208	56	✓	0.202	54	
829	K 1.829	✓	0.389	74	✓	0.297	40	
830	K 1.830	✓	0.434	37	✓	0.109	38	
831	K 1.831	✓	4.434	145	✓	0.234	35	
832	K 1.832	✓	0.581	2497	✓	0.125	31	
833	K 1.833	✓	0.119	105	✓	0.125	49	
834	K 1.834	✓	0.696	90	✓	0.234	60	
835	K 1.835	✗	2.56	47	✗	1.638	0	
836	K 1.836	✓	12.339	386	✓	0.156	102	
837	K 1.837	✗	3.086	52	✗	1.700	0	
838	K 1.838	✓	0.027	31	✓	0.078	27	
839	K 1.839	✓	0.068	28	✓	0.062	19	
840	K 1.840	✓	0.096	30	✓	0.063	19	
841	K 1.841	✓	1.256	236	✓	0.234	97	
842	K 1.842	✓	0.122	186	✓	0.047	43	
843	K 1.843	✓	0.124	198	✓	0.015	43	
844	K 1.844	✓	16.574	386	✓	0.140	97	
845	K 1.845	✓	4.914	227	✓	0.187	44	
846	K 1.846	✓	1.357	362	✓	0.141	40	
847	K 1.847	✓	0.365	69	✓	0.265	36	
848	K 1.848	✓	0.109	154	✓	0.405	27	
849	K 1.849	✓	0.324	68	✓	0.265	35	
850	K 1.850	✓	0.197	1478	✓	0.795	32	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
851	K 1.851	✓	0.156	145	✓	0.047	42	
852	K 1.852	✓	0.149	145	✓	0.047	42	
853	K 1.853	✓	0.017	76	✓	0.031	65	
854	K 1.854	✗	0.624	49	✓	0.156	51	
855	K 1.855	✗	0.672	49	✓	0.156	51	
856	K 1.856	✓	0.894	100	✓	0.218	65	
857	K 1.857	✓	0.342	69	✓	0.265	36	
858	K 1.858	✓	0.161	145	✓	0.047	42	
859	K 1.859	✓	1.298	102	✓	0.218	63	
860	K 1.860	✓	0.151	33	✓	1.669	29	
861	K 1.861	✓	1.815	155	✓	0.125	26	
862	K 1.862	✗	1.114	32	✓	0.172	27	
863	K 1.863	✓	0.035	30	✓	2.355	38	
864	K 1.864	✓	0.041	137	✓	0.062	186	
865	K 1.865	✓	150.793	84	✓	0.156	23	
866	K 1.866	✓	0.5	74	✓	0.437	39	
867	K 1.867	✓	0.06	77	✓	0.046	30	
868	K 1.868	✓	0.042	79	✓	0.047	28	
869	K 1.869	✓	0.035	42	✓	0.047	37	
870	K 1.870	✓	1.681	35	✓	0.702	30	
871	K 1.871	✓	0.023	22	✓	0.062	66	
872	K 1.872	✓	0.046	215	✓	0.047	49	
873	K 1.873	✓	0.345	53	✓	0.187	50	
874	K 1.874	✓	0.068	101	✓	0.047	40	
875	K 1.875	✓	0.294	285	✓	0.187	79	
876	K 1.876	✓	0.017	135	✓	0.031	41	
877	K 1.877	✓	0.017	49	✓	0.031	71	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
878	K 1.878	✓	0.263	130	✓	0.359	75	
879	K 1.879	✓	0.153	135	✓	0.172	55	
880	K 1.880	✓	0.128	131	✓	0.063	41	
881	K 1.881	✓	0.018	75	✓	0.047	75	
882	K 1.882	✓	0.068	119	✓	0.047	41	
883	K 1.883	✓	1.403	164	✓	0.592	595	
884	K 1.884	✓	0.365	71	✓	0.265	107	
885	K 1.885	✗	40.742	73	✗	0.858	0	
886	K 1.886	✓	0.055	82	✓	0.016	42	
887	K 1.887	✓	0.049	106	✓	0.046	70	
888	K 1.888	✓	0.02	78	✓	0.031	79	
889	K 1.889	✗(hanged)	0	0	✓	0.858	47	
890	K 1.890	✓	0.141	103	✓	0.686	34	
891	K 1.891	✓	0.021	135	✓	0.047	56	
892	K 1.892	✗(hanged)	0	0	✓	0.452	40	
893	K 1.893	✓	0.048	80	✓	0.031	41	
894	K 1.894	✗	40.655	65	✗	0.734	0	
895	K 1.895	✓	0.023	81	✓	0.047	80	
896	K 1.896	✓	0.201	106	✓	0.296	63	
897	K 1.897	✓	0.027	79	✓	0.062	85	
898	K 1.898	✓	0.022	106	✓	0.031	83	
899	K 1.899	✓	0.062	106	✓	0.015	47	
900	K 1.900	✓	0.091	381	✓	0.063	46	
901	K 1.901	✓	0.09	33	✓	0.343	30	
902	K 1.902	✓	0.11	295	✓	0.171	175	
903	K 1.903	✓	0.05	19	✓	0.047	48	
904	K 1.904	✓	0.052	23	✓	0.031	64	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
905	K 1.905	✓	0.061	85	✓	0.031	46	
906	K 1.906	✓	0.055	326	✓	0.249	33	
907	K 1.907	✓	0.053	22	✓	0.109	22	
908	K 1.908	✓	1.365	1278	✓	0.312	1742	
909	K 1.909	✗	40.684	64	✓	0.390	84	
910	K 1.910	✓	0.058	98	✓	0.016	42	
911	K 1.911	✓	4.338	56	✓	0.374	30	
912	K 1.912	✓	1.4	205	✓	3.026	43	
913	K 1.913	✗(hanged)	0	0	✓	0.047	43	
914	K 1.914	✓	1.504	401	✓	2.247	77	
915	K 1.915	✗(hanged)	0	0	✓	0.046	43	
916	K 1.916	✗	2.07	66	✓	0.219	80	
917	K 1.917	✗	1.227	60	✓	0.172	38	
918	K 1.918	✗(hanged)	0	0	✓	0.858	41	
919	K 1.919	✗(hanged)	0	0	✓	0.140	120	
920	K 1.920	✓	0.245	301	✗(hanged)	0	0	
921	K 1.921	✓	2.719	52	✓	0.093	30	
922	K 1.922	✗(hanged)	0	0	✓	0.110	47	
923	K 1.923	✗(hanged)	0	0	✓	0.156	36	
924	K 1.924	✓	0.801	55	✓	0.094	47	
925	K 1.925	✗(hanged)	0	0	✓	0.188	38	
926	K 1.926	✗(hanged)	0	0	✓	0.032	65	
927	K 1.927	✓	0.14	112	✓	0.078	72	
928	K 1.928	✓	1.366	23	✓	0.265	21	
929	K 1.929	✗(hanged)	0	0	✓	0.031	42	
930	K 1.930	✓	1.568	39	✓	0.436	36	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
931	K 1.931	✓	0.027	80	✓	0.032	73	
932	K 1.932	✗(hanged)	0	0	✓	0.109	54	
933	K 1.933	✓	0.061	99	✓	0.031	39	
934	K 1.934	✓	0.1	102	✓	0.063	39	
935	K 1.935	✓	49.448	246	✓	0.156	55	
936	K 1.936	✓	0.094	99	✓	0.046	39	
937	K 1.937	✓	0.054	124	✓	0.046	79	
938	K 1.938	✓	0.063	108	✓	0.031	39	
939	K 1.939	✓	0.381	136	✓	0.094	70	
940	K 1.940	✓	0.022	80	✓	0.031	63	
941	K 1.941	✓	0.372	53	✓	0.047	35	
942	K 1.942	✗(hanged)	0	0	✓	0.390	43	
943	K 1.943	✓	0.395	53	✓	0.047	40	
944	K 1.944	✓	1.613	233	✓	0.062	47	
945	K 1.945	✓	1.213	213	✓	0.047	41	
946	K 1.946	✓	0.082	150	✓	0.125	100	
947	K 1.947	✓	0.108	30	✓	0.171	36	
948	K 1.948	✓	0.259	39	✓	0.140	68	
949	K 1.949	✓	0.021	76	✓	0.031	97	
950	K 1.950	✓	0.168	141	✓	0.078	42	
951	K 1.951	✓	0.144	140	✓	0.062	41	
952	K 1.952	✓	0.139	189	✓	0.202	65	
953	K 1.953	✗	1.521	97	✓	0.281	145	
954	K 1.954	✓	0.088	115	✓	0.031	53	
955	K 1.955	✓	0.043	112	✓	0.078	111	
956	K 1.956	✓	0.211	28	✓	0.062	197	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
957	K 1.957	✓	0.199	28	✓	0.031	197	
958	K 1.958	✓	0.061	82	✓	0.047	40	
959	K 1.959	✓	0.046	20	✓	0.047	16	
960	K 1.960	✓	0.036	14	✓	0.031	16	
961	K 1.961	✗(hanged)	0	0	✓	0.312	45	
962	K 1.962	✓	5.355	1191	✓	1.092	79	
963	K 1.963	✓	0.112	108	✓	0.156	39	
964	K 1.964	✓	4.81	264	✓	2.012	80	
965	K 1.965	✓	0.056	29	✓	0.093	25	
966	K 1.966	✓	0.44	292	✓	0.484	50	
967	K 1.967	✓	0.129	151	✓	0.062	90	
968	K 1.968	✓	0.085	30	✓	0.109	45	
969	K 1.969	✓	0.059	19	✓	0.125	27	
970	K 1.970	✓	0.475	66	✓	0.562	183	
971	K 1.971	✓	0.101	157	✓	0.187	88	
972	K 1.972	✓	0.032	32	✓	0.062	27	
973	K 1.973	✓	0.164	146	✓	0.234	136	
974	K 1.974	✓	0.01	39	✓	0.031	57	
975	K 1.975	✓	0.012	47	✓	0.032	59	
976	K 1.976	✓	0.076	101	✓	0.172	57	
977	K 1.977	✓	0.172	139	✓	0.141	122	
978	K 1.978	✓	0.048	60	✓	0.125	71	
979	K 1.979	✓	0.011	37	✓	0.047	57	
980	K 1.980	✓	0.012	43	✓	0.016	35	
981	K 1.981	✓	0.018	49	✓	0.016	41	
982	K 1.982	✓	0.105	132	✓	0.312	187	
983	K 1.983	✓	0.255	238	✓	0.203	469	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
984	K 1.984	✓	3.039	426	✓	0.203	40	
985	K 1.985	✓	0.158	103	✓	0.031	43	
986	K 1.986	✓	0.015	44	✓	0.031	36	
987	K 1.987	✓	0.1	40	✓	0.047	26	
988	K 1.988	✓	0.366	104	✓	0.031	29	
989	K 1.989	✓	0.104	55	✓	0.031	35	
990	K 1.990	✓	0.474	49	✓	0.359	46	
991	K 1.991	✓	0.307	101	✓	0.031	31	
992	K 1.992	✓	0.107	42	✓	0.031	25	
993	K 1.993	✓	5232.496	71	✓	0.016	35	
994	K 1.994	✓	0.123	198	✓	0.031	43	
995	K 1.995	✓	0.017	17	✓	0.094	14	
996	K 1.996	✗	56.731	25	✓	0.047	15	
997	K 1.997	✓	0.029	18	✓	0.047	16	
998	K 1.998	✓	0.473	27	✓	0.281	27	
999	K 1.999	✓	0.024	24	✓	0.047	39	
1000	K 1.1000	✗(hanged)	0	0	✓	0.109	19	
1001	K 2.1	✓	0.003	12	✓	0.0	9	
1002	K 2.2	✓	0.004	16	✓	0.031	13	
1003	K 2.3	✓	0.116	45	✓	0.032	26	
1004	K 2.4	✓	0.097	47	✓	0.031	27	
1005	K 2.5	✓	0.532	1163	✓	0.047	82	
1006	K 2.6	✓	0.004	20	✓	0.016	15	
1007	K 2.7	✓	0.057	135	✓	0.016	26	
1008	K 2.8	✗(hanged)	0	0	✓	0.032	39	
1009	K 2.9	✓	0.004	28	✓	0.016	21	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1010	K 2.10	✓	0.006	46	✓	0.062	31	
1011	K 2.11	✓	0.006	33	✓	0.031	23	
1012	K 2.12	✓	0.008	47	✓	0.062	31	
1013	K 2.13	✓	0.02	43	✓	0.031	29	
1014	K 2.14	✓	0.029	170	✓	0.078	65	
1015	K 2.15	✓	0.345	26	✗	0.156	31	
1016	K 2.16	✓	0.126	312	✓	0.141	95	
1017	K 2.17	✓	0.028	46	✓	0.063	17	
1018	K 2.18	✓	0.022	55	✓	0.047	39	
1019	K 2.19	✓	0.78	35	✗	0.531	39	
1020	K 2.20	✓	0.681	180	✓	0.141	61	
1021	K 2.21	✓	0.054	44	✓	0.140	39	
1022	K 2.22	✓	0.027	28	✓	0.156	21	
1023	K 2.23	✓	0.015	44	✓	0.141	29	
1024	K 2.24	✓	0.162	84	✓	0.109	34	
1025	K 2.25	✓	0.954	615	✓	0.140	105	
1026	K 2.26	✗	0.184	27	✗	0.280	33	
1027	K 2.27	✓	0.995	23	✓	0.265	69	
1028	K 2.28	✓	0.258	37	✗	0.172	48	
1029	K 2.29	✓	0.177	24	✓	0.125	22	
1030	K 2.30	✓	0.157	18	✓	0.0	23	
1031	K 2.31	✓	0.127	17	✗	0.0	22	
1032	K 2.32	✓	0.478	71	✓	0.156	53	
1033	K 2.33	✓	0.017	37	✓	0.032	27	
1034	K 2.34	✓	0.011	20	✓	0.015	15	
1035	K 2.35	✓	0.005	58	✓	0.0	45	
1036	K 2.36	✗(hanged)	0	0	✓	0.078	128	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1037	K 2.37	✓	0.03	101	✓	0.078	73	
1038	K 2.38	✓	0.33	23	✗	0.0	28	
1039	K 2.39	✓	0.012	47	✓	0.015	33	
1040	K 2.40	✓	0.03	53	✓	0.031	34	
1041	K 2.41	✓	0.009	55	✓	0.062	47	
1042	K 2.42	✓	0.008	61	✓	0.046	47	
1043	K 2.43	✓	0.045	69	✓	0.140	44	
1044	K 2.44	✓	0.008	39	✓	0.062	35	
1045	K 2.45	✓	0.021	39	✓	0.016	28	
1046	K 2.46	✓	0.007	31	✓	0.063	31	
1047	K 2.47	✓	0.014	27	✓	0.031	22	
1048	K 2.48	✓	0.01	45	✓	0.063	43	
1049	K 2.49	✗(hanged)	0	0	✓	0.125	70	
1050	K 2.50	✓	0.012	23	✓	0.016	18	
1051	K 2.51	✓	0.03	44	✓	0.032	27	
1052	K 2.52	✓	0.021	78	✓	0.063	65	
1053	K 2.53	✓	0.029	57	✓	0.047	35	
1054	K 2.54	✓	0.048	172	✓	0.047	105	
1055	K 2.55	✓	0.155	421	✓	0.172	317	
1056	K 2.56	✓	0.036	66	✓	0.078	48	
1057	K 2.57	✓	0.88	55	✓	0.110	50	
1058	K 2.58	✓	0.9	55	✓	0.093	35	
1059	K 2.59	✓	0.052	72	✓	0.062	55	
1060	K 2.60	✓	0.037	83	✓	0.125	91	
1061	K 2.61	✓	0.076	70	✓	0.062	38	
1062	K 2.62	✓	0.028	35	✓	0.015	23	
1063	K 2.63	✓	0.041	28	✓	0.125	66	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1064	K 2.64	✓	0.564	1400	✓	0.203	129	
1065	K 2.65	✓	0.163	114	✓	0.171	67	
1066	K 2.66	✓	0.035	18	✓	0.063	15	
1067	K 2.67	✓	0.033	21	✓	0.032	17	
1068	K 2.68	✗(hanged)	0	0	✓	0.141	45	
1069	K 2.69	✓	0.036	19	✓	0.063	15	
1070	K 2.70	✓	0.318	143	✓	0.141	67	
1071	K 2.71	✓	0.107	59	✓	0.046	37	
1072	K 2.72	✓	0.282	38	✗	0.250	45	
1073	K 2.73	✗	1.365	129	✗	2.511	109	
1074	K 2.74	✓	26.456	41	✓	0.016	21	
1075	K 2.75	✓	0.179	23	✗	0.0	28	
1076	K 2.76	✓	0.203	31	✗	0.171	36	
1077	K 2.77	✓	0.32	31	✗	0.172	36	
1078	K 2.78	✓	0.073	73	✓	0.031	39	
1079	K 2.79	✓	0.238	135	✓	0.016	37	
1080	K 2.80	✓	0.303	56	✓	0.219	74	
1081	K 2.81	✓	0.81	55	✗	0.561	64	
1082	K 2.82	✓	0.548	73	✓	0.094	85	
1083	K 2.83	✓	0.824	111	✓	0.078	43	
1084	K 2.84	✓	0.86	125	✓	0.078	21	
1085	K 2.85	✓	0.923	118	✓	0.062	29	
1086	K 2.86	✓	0.005	42	✓	0.016	29	
1087	K 2.87	✓	0.008	36	✓	0.062	35	
1088	K 2.88	✓	0.103	180	✓	0.094	36	
1089	K 2.89	✓	0.045	99	✓	0.047	61	
1090	K 2.90	✗(hanged)	0	0	✓	0.032	59	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1091	K 2.91	✓	0.023	41	✓	0.031	35	
1092	K 2.92	✓	0.096	72	✓	0.109	29	
1093	K 2.93	✓	0.005	13	✓	0.016	10	
1094	K 2.94	✓	0.022	41	✓	0.016	29	
1095	K 2.95	✓	0.009	30	✓	0.031	23	
1096	K 2.96	✓	0.012	61	✓	0.109	43	
1097	K 2.97	✓	0.026	46	✓	0.016	31	
1098	K 2.98	✓	0.009	41	✓	0.0	27	
1099	K 2.99	✓	1.066	36	✓	0.031	25	
1100	K 2.100	✓	0.022	44	✓	0.032	23	
1101	K 2.101	✓	0.026	51	✓	0.031	31	
1102	K 2.102	✓	0.006	42	✓	0.031	35	
1103	K 2.103	✓	0.026	64	✓	0.016	35	
1104	K 2.104	✓	0.036	104	✓	0.016	47	
1105	K 2.105	✓	0.021	64	✓	0.031	45	
1106	K 2.106	✓	0.055	447	✓	0.062	77	
1107	K 2.107	✓	0.031	40	✓	0.062	33	
1108	K 2.108	✓	0.035	37	✓	0.062	29	
1109	K 2.109	✓	0.053	45	✓	0.031	40	
1110	K 2.110	✓	0.041	36	✓	0.094	23	
1111	K 2.111	✓	0.018	20	✓	0.031	14	
1112	K 2.112	✓	0.025	30	✓	0.031	22	
1113	K 2.113	✓	0.022	24	✓	0.063	17	
1114	K 2.114	✓	0.05	39	✓	0.031	35	
1115	K 2.115	✓	0.069	76	✓	0.140	55	
1116	K 2.116	✓	0.054	43	✓	0.078	35	
1117	K 2.117	✓	0.098	107	✓	0.094	91	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1118	K 2.118	✓	0.093	51	✓	0.063	43	
1119	K 2.119	✓	0.175	77	✓	0.047	24	
1120	K 2.120	✓	0.065	166	✓	0.140	123	
1121	K 2.121	✓	10.522	40	✓	0.016	26	
1122	K 2.122	✓	10.079	56	✓	0.125	34	
1123	K 2.123	✓	0.012	91	✓	0.047	45	
1124	K 2.124	✓	0.063	65	✓	0.062	29	
1125	K 2.125	✓	0.129	84	✓	0.062	36	
1126	K 2.126	✓	1.204	58	✓	0.047	26	
1127	K 2.127	✓	0.039	36	✓	0.016	31	
1128	K 2.128	✓	0.244	29	✓	0.156	35	
1129	K 2.129	✓	0.038	42	✓	0.047	30	
1130	K 2.130	✓	0.012	46	✓	0.016	31	
1131	K 2.131	✓	0.01	58	✓	0.062	35	
1132	K 2.132	✓	0.011	48	✓	0.063	31	
1133	K 2.133	✓	0.091	92	✓	0.078	47	
1134	K 2.134	✓	0.095	78	✓	0.094	21	
1135	K 2.135	✓	0.01	27	✓	0.0	17	
1136	K 2.136	✓	0.021	30	✓	0.031	20	
1137	K 2.137	✓	0.096	74	✓	0.109	25	
1138	K 2.138	✓	0.031	38	✓	0.062	29	
1139	K 2.139	✓	0.013	74	✓	0.063	43	
1140	K 2.140	✓	0.049	190	✓	0.015	77	
1141	K 2.141	✓	0.108	70	✓	0.047	49	
1142	K 2.142	✓	0.047	108	✓	0.078	59	
1143	K 2.143	✓	0.045	93	✓	0.078	67	
1144	K 2.144	✓	0.04	88	✓	0.063	67	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1145	K 2.145	✓	0.387	398	✓	0.141	287	
1146	K 2.146	✓	0.023	18	✓	0.0	15	
1147	K 2.147	✓	0.016	18	✓	0.015	15	
1148	K 2.148	✓	0.01	77	✓	0.016	35	
1149	K 2.149	✓	0.076	212	✓	0.015	47	
1150	K 2.150	✓	0.009	53	✓	0.063	31	
1151	K 2.151	✓	0.018	129	✓	0.062	43	
1152	K 2.152	✓	0.019	114	✓	0.171	67	
1153	K 2.153	✓	0.034	56	✓	0.031	33	
1154	K 2.154	✓	0.02	88	✓	0.094	57	
1155	K 2.155	✓	0.053	225	✓	0.031	69	
1156	K 2.156	✗	0.207	34	✓	0.093	73	
1157	K 2.157	✓	0.502	46	✓	0.140	32	
1158	K 2.158	✓	8.381	42	✗	0.172	180	
1159	K 2.159	✓	0.015	44	✓	0.016	19	
1160	K 2.160	✓	0.009	30	✓	0.016	23	
1161	K 2.161	✓	0.048	78	✓	0.0	31	
1162	K 2.162	✓	0.057	18	✓	0.0	15	
1163	K 2.163	✓	0.353	70	✓	0.015	50	
1164	K 2.164	✓	0.028	30	✓	0.031	23	
1165	K 2.165	✓	0.055	37	✓	0.016	19	
1166	K 2.166	✓	0.013	23	✓	0.015	18	
1167	K 2.167	✓	0.082	326	✓	0.031	63	
1168	K 2.168	✓	0.005	15	✓	0.016	11	
1169	K 2.169	✓	0.07	236	✓	0.016	51	
1170	K 2.170	✓	0.023	58	✓	0.031	45	
1171	K 2.171	✓	0.054	142	✓	0.093	51	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1172	K 2.172	✓	0.055	158	✓	0.031	57	
1173	K 2.173	✓	0.061	74	✓	0.062	45	
1174	K 2.174	✓	0.018	33	✓	0.031	24	
1175	K 2.175	✓	0.157	38	✓	0.032	33	
1176	K 2.176	✓	0.018	33	✓	0.016	15	
1177	K 2.177	✓	174.646	136	✓	0.062	39	
1178	K 2.178	✓	0.053	74	✓	0.016	28	
1179	K 2.179	✓	0.04	53	✓	0.016	19	
1180	K 2.180	✓	0.231	73	✓	0.047	53	
1181	K 2.181	✓	0.028	37	✓	0.016	25	
1182	K 2.182	✓	0.016	24	✓	0.015	20	
1183	K 2.183	✓	0.024	27	✓	0.0	22	
1184	K 2.184	✓	0.019	38	✓	0.015	29	
1185	K 2.185	✓	0.036	67	✓	0.016	35	
1186	K 2.186	✓	0.03	42	✓	0.015	34	
1187	K 2.187	✓	0.011	99	✓	0.015	53	
1188	K 2.188	✓	0.083	266	✓	0.125	135	
1189	K 2.189	✓	0.07	445	✓	0.031	85	
1190	K 2.190	✓	0.03	122	✓	0.062	41	
1191	K 2.191	✓	0.009	110	✓	0.016	25	
1192	K 2.192	✓	10.168	39	✓	0.109	53	
1193	K 2.193	✓	0.049	44	✓	0.032	40	
1194	K 2.194	✓	0.05	65	✓	0.047	44	
1195	K 2.195	✓	0.028	80	✓	0.078	94	
1196	K 2.196	✓	0.025	37	✓	0.031	27	
1197	K 2.197	✓	0.018	78	✓	0.032	49	
1198	K 2.198	✓	0.03	41	✓	0.031	33	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1199	K 2.199	✓	0.013	41	✓	0.016	32	
1200	K 2.200	✓	0.022	62	✓	0.015	33	
1201	K 2.201	✓	0.054	44	✓	0.015	34	
1202	K 2.202	✓	0.015	22	✓	0.031	15	
1203	K 2.203	✓	0.021	124	✓	0.015	30	
1204	K 2.204	✓	0.019	132	✓	0.031	37	
1205	K 2.205	✓	0.213	29	✓	0.0	30	
1206	K 2.206	✓	0.115	120	✓	0.062	87	
1207	K 2.207	✓	0.124	294	✓	0.156	119	
1208	K 2.208	✓	0.037	59	✓	0.047	40	
1209	K 2.209	✓	0.02	67	✓	0.047	48	
1210	K 2.210	✓	0.266	252	✓	0.421	93	
1211	K 2.211	✓	0.055	68	✓	0.046	41	
1212	K 2.212	✗	0.376	33	✗	0.016	39	
1213	K 2.213	✓	0.072	54	✓	0.047	59	
1214	K 2.214	✓	0.289	260	✓	0.390	73	
1215	K 2.215	✓	0.158	664	✓	0.140	167	
1216	K 2.216	✗	1.452	50	✗	0.546	56	
1217	K 2.217	✓	0.144	30	✓	0.031	27	
1218	K 2.218	✓	0.144	38	✓	0.031	33	
1219	K 2.219	✓	23.117	216	✓	0.062	79	
1220	K 2.220	✓	11.805	96	✓	0.015	51	
1221	K 2.221	✓	0.062	40	✓	0.016	53	
1222	K 2.222	✓	0.02	30	✓	0.015	23	
1223	K 2.223	✓	0.02	25	✓	0.016	39	
1224	K 2.224	✓	0.018	30	✓	0.016	23	
1225	K 2.225	✓	0.032	29	✓	0.016	24	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1226	K 2.226	✓	0.019	30	✓	0.031	25	
1227	K 2.227	✓	0.036	21	✓	0.016	15	
1228	K 2.228	✓	0.015	82	✓	0.047	59	
1229	K 2.229	✓	0.041	48	✓	0.016	41	
1230	K 2.230	✓	0.026	82	✓	0.062	36	
1231	K 2.231	✓	0.075	58	✓	0.047	57	
1232	K 2.232	✗(hanged)	0	0	✓	0.141	418	
1233	K 2.233	✗(hanged)	0	0	✓	0.109	418	
1234	K 2.234	✓	0.028	38	✓	0.125	57	
1235	K 2.235	✓	0.027	50	✓	0.015	43	
1236	K 2.236	✗	0.365	28	✗	0.0	41	
1237	K 2.237	✓	0.01	30	✓	0.031	21	
1238	K 2.238	✓	0.018	36	✓	0.015	34	
1239	K 2.239	✓	0.014	46	✓	0.031	35	
1240	K 2.240	✓	0.017	18	✓	0.031	15	
1241	K 2.241	✓	0.015	30	✓	0.031	29	
1242	K 2.242	✓	0.075	68	✓	0.063	42	
1243	K 2.243	✓	0.029	45	✓	0.031	27	
1244	K 2.244	✓	0.026	42	✓	0.062	35	
1245	K 2.245	✓	0.021	42	✓	0.031	35	
1246	K 2.246	✓	0.021	42	✓	0.094	35	
1247	K 2.247	✓	0.225	97	✓	0.031	27	
1248	K 2.248	✓	2.122	57	✓	0.172	150	
1249	K 2.249	✓	0.175	193	✓	0.062	134	
1250	K 2.250	✓	0.048	41	✓	0.016	52	
1251	K 2.251	✓	0.035	25	✓	0.031	20	
1252	K 2.252	✓	0.162	151	✓	0.032	124	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1253	K 2.253	✓	0.025	34	✓	0.0	16	
1254	K 2.254	✓	0.089	69	✓	0.062	44	
1255	K 2.255	✓	0.205	118	✓	0.031	42	
1256	K 2.256	✓	0.023	26	✓	0.078	51	
1257	K 2.257	✓	0.046	33	✓	0.172	27	
1258	K 2.258	✓	0.162	146	✓	0.031	110	
1259	K 2.259	✓	0.142	120	✓	0.047	92	
1260	K 2.260	✓	0.16	65	✓	0.296	76	
1261	K 2.261	✓	2.667	82	✓	0.171	124	
1262	K 2.262	✓	38.899	87	✓	0.171	55	
1263	K 2.263	✗(hanged)	0	0	✓	0.047	52	
1264	K 2.264	✓	0.064	23	✓	0.031	19	
1265	K 2.265	✓	0.043	64	✓	0.093	97	
1266	K 2.266	✓	0.03	22	✓	0.0	19	
1267	K 2.267	✓	34.197	205	✓	0.046	41	
1268	K 2.268	✓	1.378	55	✓	0.078	39	
1269	K 2.269	✓	0.085	60	✓	0.062	40	
1270	K 2.270	✓	162.566	57	✓	0.125	54	
1271	K 2.271	✓	0.011	27	✓	0.0	17	
1272	K 2.272	✓	0.012	32	✓	0.031	25	
1273	K 2.273	✓	0.017	20	✓	0.062	17	
1274	K 2.274	✓	0.044	38	✓	0.0	19	
1275	K 2.275	✓	0.037	120	✓	0.110	55	
1276	K 2.276	✓	0.047	55	✓	0.063	31	
1277	K 2.277	✓	0.029	51	✓	0.047	29	
1278	K 2.278	✗	0.268	28	✗	0.0	33	
1279	K 2.279	✓	0.163	74	✓	0.094	32	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1280	K 2.280	✓	0.039	52	✓	0.047	41	
1281	K 2.281	✓	0.021	28	✓	0.047	19	
1282	K 2.282	✓	0.024	39	✓	0.047	27	
1283	K 2.283	✓	0.099	90	✓	0.093	52	
1284	K 2.284	✓	0.045	47	✓	0.016	42	
1285	K 2.285	✓	0.336	134	✓	0.079	52	
1286	K 2.286	✓	0.103	101	✓	0.015	32	
1287	K 2.287	✓	0.019	83	✓	0.016	27	
1288	K 2.288	✓	0.039	47	✓	0.016	23	
1289	K 2.289	✓	0.08	53	✓	0.062	35	
1290	K 2.290	✓	0.175	103	✓	0.015	47	
1291	K 2.291	✓	0.078	92	✓	0.031	62	
1292	K 2.292	✓	0.042	53	✓	0.047	31	
1293	K 2.293	✓	0.342	44	✓	0.046	35	
1294	K 2.294	✓	0.07	44	✓	0.047	35	
1295	K 2.295	✓	0.287	310	✓	0.218	113	
1296	K 2.296	✓	0.572	356	✓	0.218	165	
1297	K 2.297	✓	0.034	52	✓	0.016	61	
1298	K 2.298	✓	0.08	162	✓	0.078	143	
1299	K 2.299	✓	0.014	19	✓	0.016	31	
1300	K 2.300	✓	0.016	41	✓	0.046	32	
1301	K 2.301	✓	0.033	31	✓	0.016	22	
1302	K 2.302	✓	0.084	243	✓	0.046	117	
1303	K 2.303	✓	14.511	56	✓	0.140	501	
1304	K 2.304	✓	0.034	50	✓	0.016	41	
1305	K 2.305	✓	0.071	47	✓	0.046	47	
1306	K 2.306	✓	1.002	56	✓	0.109	95	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1307	K 2.307	✓	0.085	54	✓	0.047	38	
1308	K 2.308	✓	0.019	41	✓	0.016	36	
1309	K 2.309	✓	0.081	84	✓	0.078	73	
1310	K 2.310	✓	0.01	31	✓	0.031	20	
1311	K 2.311	✓	0.135	63	✓	0.109	52	
1312	K 2.312	✓	0.026	32	✓	0.015	26	
1313	K 2.313	✓	0.212	87	✓	0.062	39	
1314	K 2.314	✓	0.185	87	✓	0.062	35	
1315	K 2.315	✓	0.028	44	✓	0.015	45	
1316	K 2.316	✓	0.092	38	✓	0.032	18	
1317	K 2.317	✓	0.115	38	✓	0.032	13	
1318	K 2.318	✓	0.294	172	✓	0.094	122	
1319	K 2.319	✓	0.1	118	✓	0.078	37	
1320	K 2.320	✓	0.07	21	✓	0.031	17	
1321	K 2.321	✓	0.026	18	✓	0.015	15	
1322	K 2.322	✓	0.029	44	✓	0.015	44	
1323	K 2.323	✓	0.744	54	✓	0.016	20	
1324	K 2.324	✓	0.029	25	✓	0.047	21	
1325	K 2.325	✓	0.265	52	✓	0.093	103	
1326	K 2.326	✓	0.029	29	✓	0.031	26	
1327	K 2.327	✓	0.168	104	✓	0.094	85	
1328	K 2.328	✓	0.022	36	✓	0.015	32	
1329	K 2.329	✓	6.41	99	✓	0.234	64	
1330	K 2.330	✓	135.163	71	✓	0.780	1147	
1331	K 2.331	✓	0.043	55	✓	0.031	19	
1332	K 2.332	✓	0.024	26	✓	0.015	19	
1333	K 2.333	✓	0.109	70	✓	0.047	45	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1334	K 2.334	✓	0.199	114	✓	0.062	97	
1335	K 2.335	✓	0.305	893	✓	0.031	57	
1336	K 2.336	✓	0.051	70	✓	0.031	50	
1337	K 2.337	✓	0.081	62	✓	0.015	44	
1338	K 2.338	✓	0.067	40	✓	0.016	31	
1339	K 2.339	✓	0.264	66	✓	0.094	89	
1340	K 2.340	✓	0.035	32	✓	0.015	29	
1341	K 2.341	✗(hanged)	0	0	✓	0.125	195	
1342	K 2.342	✓	0.042	51	✓	0.031	31	
1343	K 2.343	✓	0.666	61	✓	0.094	62	
1344	K 2.344	✓	0.56	173	✓	0.031	23	
1345	K 2.345	✓	0.029	52	✓	0.047	32	
1346	K 2.346	✓	0.327	87	✓	0.047	25	
1347	K 2.347	✓	0.077	31	✓	0.031	19	
1348	K 2.348	✓	1.313	58	✓	0.156	101	
1349	K 2.349	✓	0.087	76	✓	0.063	73	
1350	K 2.350	✓	0.01	25	✓	0.0	21	
1351	K 2.351	✓	0.024	50	✓	0.031	30	
1352	K 2.352	✓	0.013	89	✓	0.047	43	
1353	K 2.353	✓	0.108	119	✓	0.141	68	
1354	K 2.354	✓	0.071	108	✓	0.156	32	
1355	K 2.355	✓	0.132	59	✓	0.110	37	
1356	K 2.356	✓	0.288	90	✓	0.063	29	
1357	K 2.357	✓	0.666	288	✓	0.094	103	
1358	K 2.358	✓	0.065	66	✓	0.031	21	
1359	K 2.359	✓	0.102	86	✓	0.063	57	
1360	K 2.360	✓	0.092	68	✓	0.046	47	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1361	K 2.361	✓	0.472	38	✓	0.015	33	
1362	K 2.362	✓	14.233	115	✓	0.172	109	
1363	K 2.363	✓	0.803	236	✓	0.109	171	
1364	K 2.364	✓	0.172	42	✓	0.078	33	
1365	K 2.365	✓	0.094	72	✓	0.031	65	
1366	K 2.366	✓	0.023	31	✓	0.016	24	
1367	K 2.367	✓	2.3	98	✓	0.187	96	
1368	K 2.368	✓	0.027	106	✓	0.062	81	
1369	K 2.369	✓	0.103	75	✓	0.031	61	
1370	K 2.370	✓	0.029	53	✓	0.016	19	
1371	K 2.371	✓	0.022	48	✓	0.047	37	
1372	K 2.372	✓	4.813	93	✓	0.187	120	
1373	K 2.373	✓	2.321	104	✓	0.156	92	
1374	K 2.374	✓	0.036	32	✓	0.032	29	
1375	K 2.375	✓	0.052	54	✓	0.047	39	
1376	K 2.376	✓	0.097	82	✓	0.016	71	
1377	K 2.377	✓	0.236	109	✓	0.078	91	
1378	K 2.378	✓	0.05	65	✓	0.031	50	
1379	K 2.379	✓	0.078	99	✓	0.047	66	
1380	K 2.380	✓	0.297	132	✓	0.047	75	
1381	K 2.381	✓	0.626	589	✓	0.109	219	
1382	K 2.382	✓	0.699	154	✓	0.078	116	
1383	K 2.383	✓	0.138	50	✓	0.047	39	
1384	K 2.384	✓	0.034	110	✓	0.187	73	
1385	K 2.385	✓	0.019	78	✓	0.047	61	
1386	K 2.386	✓	0.089	108	✓	0.046	68	
1387	K 2.387	✓	0.039	50	✓	0.015	36	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1388	K 2.388	✓	0.291	235	✓	0.047	82	
1389	K 2.389	✓	0.379	217	✓	0.047	74	
1390	K 2.390	✓	0.041	51	✓	0.032	25	
1391	K 2.391	✓	0.058	27	✓	0.032	20	
1392	K 2.392	✓	83.233	1763961	✓	0.157	613	
1393	K 2.393	✓	17.23	413606	✓	0.110	299	
1394	K 2.394	✓	0.051	115	✓	0.078	89	
1395	K 2.395	✓	0.161	78	✓	0.063	43	
1396	K 2.396	✓	1.41	211	✓	0.109	189	
1397	K 2.397	✓	0.027	38	✓	0.063	28	
1398	K 2.398	✓	1.453	88	✓	0.124	69	
1399	K 2.399	✓	0.054	72	✓	0.062	46	
1400	K 2.400	✓	0.051	60	✓	0.047	37	
1401	K 2.401	✓	0.013	93	✓	0.047	45	
1402	K 2.402	✓	4.464	127	✓	0.218	69	
1403	K 2.403	✓	97.102	611	✓	0.639	311	
1404	K 2.404	✓	0.023	33	✓	0.031	24	
1405	K 2.405	✓	0.076	77	✓	0.062	47	
1406	K 2.406	✓	276.982	257	✓	0.109	53	
1407	K 2.407	✓	491.009	842	✓	2.074	2907	
1408	K 2.408	✓	59.616	98	✓	7.301	165	
1409	K 2.409	✓	0.023	43	✓	0.016	39	
1410	K 2.410	✓	0.132	481	✓	0.187	253	
1411	K 2.411	✓	0.334	42	✓	0.016	27	
1412	K 2.412	✓	0.016	29	✓	0.0	27	
1413	K 2.413	✗	0.347	37	✓	0.047	12	
1414	K 2.414	✓	1.132	231	✓	0.187	97	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1415	K 2.415	✓	0.841	273	✓	0.109	43	
1416	K 2.416	✓	0.215	46	✓	0.141	31	
1417	K 2.417	✓	0.142	52	✓	0.094	35	
1418	K 2.418	✗	1.249	46	✓	13.588	60	
1419	K 2.419	✓	1.178	53	✓	0.219	13	
1420	K 2.420	✓	0.435	134	✓	0.218	123	
1421	K 2.421	✓	0.248	67	✓	0.063	27	
1422	K 2.422	✓	0.086	64	✓	0.156	57	
1423	K 2.423	✓	0.072	70	✓	0.203	165	
1424	K 2.424	✓	0.171	90	✓	0.203	125	
1425	K 2.425	✓	0.726	232	✓	0.312	99	
1426	K 2.426	✓	6.105	4128	✓	0.390	599	
1427	K 2.427	✗	200.592	57	✓	1.107	262	
1428	K 2.428	✓	0.392	104	✓	0.218	219	
1429	K 2.429	✓	0.057	51	✓	0.031	25	
1430	K 2.430	✓	0.453	22	✓	0.250	122	
1431	K 2.431	✓	0.203	80	✓	0.156	35	
1432	K 2.432	✓	0.091	37	✓	0.046	25	
1433	K 2.433	✓	0.201	46	✓	0.078	32	
1434	K 2.434	✓	99.286	1596424	✓	0.936	559	
1435	K 2.435	✓	0.138	70	✓	0.109	41	
1436	K 2.436	✓	0.54	42	✓	0.203	140	
1437	K 2.437	✓	0.241	44	✓	0.125	29	
1438	K 2.438	✓	0.94	615	✓	0.141	105	
1439	K 2.439	✗	0.765	61	✓	0.671	69	
1440	K 2.440	✓	0.891	86	✓	0.0	94	
1441	K 2.441	✗	1.467	105	✓	340.784	85	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1442	K 2.442	✗	0.213	28	✓	0.063	31	
1443	K 2.443	✗	0.267	36	✓	0.016	39	
1444	K 2.444	✗	1.511	36	✓	0.016	37	
1445	K 2.445	✗	1.327	169	✓	0.203	21	
1446	K 2.446	✓	0.022	33	✓	0.047	28	
1447	K 2.447	✓	0.02	29	✓	0.047	24	
1448	K 2.448	✓	0.323	149	✓	0.063	87	
1449	K 3.1	✓	0.017	53	✓	0.015	53	
1450	K 3.2	✗(hanged)	0	0	✓	0.171	2294	
1451	K 3.3	✓	0.02	168	✓	0.093	114	
1452	K 3.4	✓	0.006	54	✓	0.016	35	
1453	K 3.5	✓	0.593	128	✓	0.094	230	
1454	K 3.6	✓	0.009	79	✓	0.047	55	
1455	K 3.7	✓	0.028	127	✓	0.110	71	
1456	K 3.8	✓	0.034	183	✓	0.047	74	
1457	K 3.9	✗	0.02	30	✗	0.203	37	
1458	K 3.10	✗	0.019	51	✗	0.218	59	
1459	K 3.11	✗	0.018	43	✗	0.297	41	
1460	K 3.12	✗	0.013	34	✗	0.219	39	
1461	K 3.13	✗	0.03	55	✗	1.154	63	
1462	K 3.14	✗	0.022	32	✗	1.264	40	
1463	K 3.15	✗	0.073	26	✗	0.063	24	
1464	K 3.16	✓	0.006	34	✓	0.0	27	
1465	K 3.17	✓	0.081	95	✓	0.031	467	
1466	K 3.18	✓	0.018	46	✓	0.031	36	
1467	K 3.19	✓	0.005	84	✓	0.015	644	
1468	K 3.20	✓	0.087	57	✓	0.062	64	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1469	K 3.21	✓	0.027	72	✓	0.031	37	
1470	K 3.22	✓	75.668	63	✓	0.062	36	
1471	K 3.23	✗	0.08	27	✓	0.156	36	
1472	K 3.24	✗	0.081	34	✓	0.141	33	
1473	K 3.25	✗	0.012	38	✗	0.046	47	
1474	K 3.26	✗	0.015	55	✗	0.110	30	
1475	K 3.27	✓	0.022	38	✓	0.015	26	
1476	K 3.28	✗	0.129	44	✗	0.234	62	
1477	K 3.29	✓	0.171	48	✓	0.031	41	
1478	K 3.30	✓	0.032	104	✓	0.094	48	
1479	K 3.31	✓	0.143	153	✓	0.187	92	
1480	K 3.32	✓	0.21	93	✓	0.219	35	
1481	K 3.33	✓	0.985	431	✓	0.031	44	
1482	K 3.34	✗(hanged)	0	0	✓	0.219	2292	
1483	K 3.35	✓	0.149	112	✓	0.218	37	
1484	K 3.36	✗	63.308	80	✗	0.296	62	
1485	K 3.37	✓	0.119	66	✓	0.297	47	
1486	K 3.38	✓	0.168	65	✓	0.187	50	
1487	K 3.39	✓	114.052	86	✓	0.078	38	
1488	K 3.40	✓	0.546	102	✓	0.390	151	
1489	K 3.41	✗	0.799	54	✗	0.218	36	
1490	K 3.42	✓	0.019	33	✓	0.063	18	
1491	K 3.43	✓	0.046	102	✓	0.063	88	
1492	K 3.44	✓	0.404	43	✓	0.094	39	
1493	K 3.45	✓	7.185	2582	✓	0.265	1849	
1494	K 3.46	✓	0.027	43	✓	0.016	25	
1495	K 3.47	✓	0.018	24	✓	0.015	16	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1496	K 3.48	✓	0.274	63	✓	0.031	67	
1497	K 3.49	✓	0.499	135	✓	0.203	77	
1498	K 3.50	✓	8.482	584	✓	0.234	53	
1499	K 3.51	✓	0.233	97	✓	0.218	25	
1500	K 3.52	✗	47.362	71	✓	0.172	55	
1501	K 3.53	✓	0.187	86	✓	0.203	37	
1502	K 3.54	✓	0.055	98	✓	0.328	109	
1503	K 3.55	✓	0.106	62	✓	0.031	86	
1504	K 3.56	✓	0.108	43	✓	0.171	18	
1505	K 3.57	✗	62.085	69	✓	0.125	79	
1506	K 3.58	✓	30.884	208	✓	0.031	43	
1507	K 3.59	✗	2.447	40	✓	0.468	1421	
1508	K 3.60	✓	0.777	143	✓	0.125	81	
1509	K 3.61	✓	0.011	34	✓	0.047	30	
1510	K 3.62	✗	0.052	60	✗	0.078	74	
1511	K 3.63	✓	0.036	51	✓	0.031	37	
1512	K 3.64	✓	0.038	29	✓	0.016	18	
1513	K 3.65	✓	0.075	25	✓	0.171	20	
1514	K 3.66	✓	0.717	102	✓	0.390	151	
1515	K 3.67	✗	0.121	104	✗(hanged)	0	0	
1516	K 3.68	✗	434.677	71	✓	0.359	263	
1517	K 3.69	✓	0.409	30686	✓	0.327	1770	
1518	K 3.70	✓	0.242	106	✓	0.374	56	
1519	K 3.71	✓	0.03	65	✓	0.124	20	
1520	K 3.72	✗	72.774	167	✓	0.374	279	
1521	K 3.73	✓	0.065	35	✓	0.358	31	
1522	K 3.74	✓	0.02	44	✓	0.032	31	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1523	K 3.75	✓	0.119	74	✓	0.359	26	
1524	K 3.76	✓	0.144	96	✓	0.390	104	
1525	K 3.77	✓	0.44	102	✓	0.437	291	
1526	K 3.78	✗(hanged)	0	0	✓	0.203	20	
1527	K 3.79	✗	135.355	58	✓	0.421	500	
1528	K 3.80	✓	0.495	72	✓	0.078	68	
1529	K 3.81	✗	0.077	42	✓	0.047	43	
1530	K 3.82	✗	0.113	58	✓	0.187	113	
1531	K 3.83	✗	0.034	76	✗	0.125	70	
1532	K 3.84	✓	0.019	103	✓	0.078	58	
1533	K 3.85	✓	0.017	113	✓	0.078	58	
1534	K 4.1	✓	0.003	24	✓	0.141	21	
1535	K 4.2	✓	1.374	265	✓	0.156	36	
1536	K 4.3	✓	0.004	76	✓	0.109	50	
1537	K 4.4	✓	0.829	1722	✓	0.141	67	
1538	K 4.5	✓	0.248	66	✓	0.250	46	
1539	K 4.6	✓	0.007	44	✓	0.015	35	
1540	K 4.7	✗	0.43	67	✗	0.094	44	
1541	K 4.8	✗	80.218	73	✗	0.062	50	
1542	K 4.9	✗	0.029	55	✗	0.561	60	
1543	K 4.10	✗	0.1	47	✗	5.319	59	
1544	K 4.11	✗	0.015	45	✓	0.0	41	
1545	K 4.12	✓	0.165	40	✓	0.046	31	
1546	K 4.13	✓	0.649	301	✓	0.047	81	
1547	K 4.14	✗	0.035	116	✓	0.015	87	
1548	K 4.15	✓	0.099	50	✓	0.047	32	
1549	K 4.16	✓	0.012	34	✓	0.047	26	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1550	K 4.17	✓	7.687	262	✓	0.390	159	
1551	K 4.18	✓	0.444	110	✓	0.110	63	
1552	K 4.19	✗(hanged)	0	0	✓	0.047	89	
1553	K 4.20	✓	0.022	29	✓	0.031	18	
1554	K 4.21	✓	0.022	29	✓	0.0	18	
1555	K 4.22	✓	0.06	156	✓	0.062	69	
1556	K 4.23	✓	0.02	30	✓	0.015	19	
1557	K 4.24	✓	0.063	146	✓	0.047	69	
1558	K 4.25	✓	0.161	319	✓	0.062	93	
1559	K 4.26	✓	0.265	100	✓	0.078	33	
1560	K 4.27	✓	0.02	29	✓	0.016	18	
1561	K 4.28	✓	3.737	400	✓	0.140	77	
1562	K 4.29	✓	1.108	140	✓	0.187	93	
1563	K 4.30	✓	1.852	232	✓	0.110	83	
1564	K 4.31	✓	1.386	230	✓	0.156	156	
1565	K 4.32	✓	0.518	242	✓	0.171	85	
1566	K 4.33	✓	0.62	238	✓	0.156	37	
1567	K 4.34	✓	0.021	30	✓	0.016	19	
1568	K 4.35	✓	0.157	378	✓	0.015	89	
1569	K 4.36	✓	0.152	378	✓	0.218	81	
1570	K 4.37	✓	0.154	470	✓	0.047	57	
1571	K 4.38	✓	0.094	390	✓	0.093	151	
1572	K 4.39	✗	93.273	174	✓	0.203	37	
1573	K 4.40	✗	0.055	59	✓	0.016	65	
1574	K 5.1	✗	0.207	73	✓	0.639	345	
1575	K 5.2	✗	0.067	61	✓	0.265	1277	
1576	K 5.3	✗	0.246	50	✓	0.016	67	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1577	K 5.4	✓	1.266	44	✓	0.016	21	
1578	K 5.5	✓	438.074	139	✓	0.764	92	
1579	K 5.6	✓	0.621	104	✓	0.156	78	
1580	K 5.7	✓	0.839	234	✓	0.375	164	
1581	K 5.8	✗	0.153	61	✗(hanged)	0	0	
1582	K 5.9	✓	0.338	787	✗	0.047	41	
1583	K 5.10	✓	1218.104	117	✓	0.015	40	
1584	K 5.11	✓	2.838	216	✓	0.124	118	
1585	K 5.12	✓	0.247	214	✓	0.016	806	
1586	K 5.13	✗	84.451	148	✗	0.124	119	
1587	K 5.14	✓	0.312	492	✓	0.265	200	
1588	K 5.15	✓	6.345	114	✓	0.078	90	
1589	K 5.16	✓	0.041	670	✓	6.380	27500	
1590	K 5.17	✗	343.291	72	✓(ODESolStruct)	1.794	1258	
1591	K 6.1	✓	0.039	26	✓	0.031	12	
1592	K 6.2	✓	0.03	14	✓	0.016	10	
1593	K 6.3	✗	0.162	20	✗	0.094	0	
1594	K 6.4	✓	0.367	373	✓	0.110	59	
1595	K 6.5	✗	0.336	21	✗	0.124	0	
1596	K 6.6	✗	0.968	23	✗	0.187	0	
1597	K 6.7	✓	2.337	242	✓	0.031	21	
1598	K 6.8	✗	3.346	30	✗	0.234	0	
1599	K 6.9	✗	2.856	27	✗	0.250	0	
1600	K 6.10	✓	2.225	1017	✓	0.063	89	
1601	K 6.11	✗	0.038	20	✓(ODESolStruct)	3.479	184	
1602	K 6.12	✓	81.622	46	✓	0.125	73	
1603	K 6.13	✗	60.656	42	✓	59.530	13291	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1604	K 6.14	✓	0.061	34	✓	0.281	23	
1605	K 6.15	✗	0.52	22	✓ (ODESolStruct)	0.811	109	
1606	K 6.16	✗	1.086	18	✗	0.733	0	
1607	K 6.17	✓	0.108	79	✓	0.078	49	
1608	K 6.18	✗	0.05	23	✗	1.248	0	
1609	K 6.19	✗	0.035	23	✗	0.624	0	
1610	K 6.20	✗(hanged)	0	0	✓	0.203	92	
1611	K 6.21	✗	5.239	27	✓ (ODESolStruct)	0.359	57	
1612	K 6.22	✗	22.519	29	✓ (ODESolStruct)	0.811	57	
1613	K 6.23	✗	2.183	31	✓	0.016	27	
1614	K 6.24	✗	1.49	31	✓	0.047	33	
1615	K 6.25	✗	118.098	50	✓ (ODESolStruct)	3.526	116	
1616	K 6.26	✗	25.262	34	✗	0.889	63	
1617	K 6.27	✗	0.045	26	✓ (ODESolStruct)	0.359	0	
1618	K 6.28	✗	30.684	26	✓ (ODESolStruct)	1.107	56	
1619	K 6.29	✗	0.056	23	✗	0.593	0	
1620	K 6.30	✗	122.323	24	✓	0.078	253	
1621	K 6.31	✗	100.138	28	✓	0.967	8191	
1622	K 6.32	✗	26.601	41	✓	0.219	775	
1623	K 6.33	✗	0.446	50	✗	2.340	0	
1624	K 6.34	✗	1.426	93	✓ (ODESolStruct)	1.263	135	
1625	K 6.35	✗	0.963	82	✗	0.343	0	
1626	K 6.36	✗	52.088	33	✓ (ODESolStruct)	0.156	48	
1627	K 6.37	✗	0.326	35	✓ (ODESolStruct)	0.609	63	
1628	K 6.38	✗	7.278	32	✗	0.0	63	
1629	K 6.39	✗	0.037	34	✓	0.015	38	

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#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1630	K 6.40	✓	11.895	3227	✓	0.405	803	
1631	K 6.41	✗	0.032	35	✓	0.031	38	
1632	K 6.42	✓	0.065	46	✓	0.062	29	
1633	K 6.43	✗	35.438	25	✓	0.188	97	
1634	K 6.44	✗	0.163	24	✗	0.0	0	
1635	K 6.45	✗	101.518	23	✓	0.109	79	
1636	K 6.46	✗	36.576	32	✓ (ODESolStruct)	0.531	59	
1637	K 6.47	✗	30.478	29	✓ (ODESolStruct)	0.359	58	
1638	K 6.48	✗	100.155	24	✓	0.125	126	
1639	K 6.49	✗	41.17	27	✓ (ODESolStruct)	2.246	56	
1640	K 6.50	✗	200.468	25	✓	0.109	70	
1641	K 6.51	✓	2.379	57	✓	0.032	29	
1642	K 6.52	✗	1.082	40	✗	0.203	0	
1643	K 6.53	✗	0.41	34	✗	0.265	0	
1644	K 6.54	✗	62.319	32	✓ (ODESolStruct)	0.374	59	
1645	K 6.55	✗	0.173	34	✗	0.0	0	
1646	K 6.56	✓	10.814	262	✓	0.187	94	
1647	K 6.57	✓	48.123	59	✓	0.312	123	
1648	K 6.58	✗	0.086	27	✓ (ODESolStruct)	1.404	413	
1649	K 6.59	✗	2.647	30	✗	0.0	0	
1650	K 6.60	✓	0.024	30	✓	0.125	18	
1651	K 6.61	✓	0.284	414	✓	0.109	31	
1652	K 6.62	✗	0.834	31	✓	0.203	36	
1653	K 6.63	✓	0.072	75	✓	0.078	55	
1654	K 6.64	✓	0.312	308	✓	0.125	49	
1655	K 6.65	✓	0.887	350	✓	0.140	106	
1656	K 6.66	✗	100.341	33	✓	0.499	771	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1657	K 6.67	✓	0.152	33	✓	0.187	47	
1658	K 6.68	✗	0.131	26	✓ (ODESolStruct)	0.094	117	
1659	K 6.69	✗	12.591	26	✓ (ODESolStruct)	0.063	60	
1660	K 6.70	✗	3.899	39	✓ (ODESolStruct)	0.640	132	
1661	K 6.71	✓	0.034	92	✓	0.062	51	
1662	K 6.72	✗	1.537	22	✓ (ODESolStruct)	0.266	56	
1663	K 6.73	✗	0.037	26	✓ (ODESolStruct)	0.593	151	
1664	K 6.74	✗	0.538	28	✓ (ODESolStruct)	2.355	185	
1665	K 6.75	✗	0.4	25	✓ (ODESolStruct)	0.405	84	
1666	K 6.76	✗	0.594	26	✓ (ODESolStruct)	0.608	93	
1667	K 6.77	✗	0.641	32	✓ (ODESolStruct)	0.983	124	
1668	K 6.78	✓	0.082	60	✓	0.109	24	
1669	K 6.79	✓	103.487	126	✓	0.094	32	
1670	K 6.80	✓	90.651	50	✓	0.281	35	
1671	K 6.81	✓	0.043	59	✓	0.063	35	
1672	K 6.82	✗	19.524	27	✓ (ODESolStruct)	0.702	67	
1673	K 6.83	✗	35.89	23	✓ (ODESolStruct)	0.514	65	
1674	K 6.84	✓	0.066	106	✓	0.047	27	
1675	K 6.85	✗	3.448	47	✗	1.638	0	
1676	K 6.86	✓	54.699	133	✓	0.920	110	
1677	K 6.87	✗	46.987	28	✓ (ODESolStruct)	2.309	101	
1678	K 6.88	✗	1.837	39	✓	1.622	60	
1679	K 6.89	✓	0.042	33	✓	0.826	27	
1680	K 6.90	✗	10.874	31	✓ (ODESolStruct)	1.092	103	
1681	K 6.91	✗	3.482	26	✓	0.780	31	
1682	K 6.92	✗	22.595	35	✓ (ODESolStruct)	1.186	102	

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#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1683	K 6.93	✓	0.069	26	✓	0.796	23	
1684	K 6.94	✗	53.614	52	✓ (ODESolStruct)	1.810	108	
1685	K 6.95	✗	4.994	70	✗	3.650	0	
1686	K 6.96	✗	0.033	23	✓ (ODESolStruct)	0.764	160	
1687	K 6.97	✓	0.07	262	✓	1.544	23	
1688	K 6.98	✓	283.32	166	✓	1.638	32	
1689	K 6.99	✓	0.643	329	✓	1.623	37	
1690	K 6.100	✗	22.744	25	✓ (ODESolStruct)	3.479	97	
1691	K 6.101	✗	61.997	46	✓	0.795	254	
1692	K 6.102	✗	0.083	37	✓ (ODESolStruct)	3.370	165	
1693	K 6.103	✗	0.952	39	✓ (ODESolStruct)	0.218	68	
1694	K 6.104	✓	0.196	115	✓	1.669	55	
1695	K 6.105	✗	25.611	18	✓ (ODESolStruct)	2.090	103	
1696	K 6.106	✗	24.305	20	✓ (ODESolStruct)	1.856	102	
1697	K 6.107	✓	0.063	94	✓	1.669	39	
1698	K 6.108	✓	0.04	72	✗	1.669	0	
1699	K 6.109	✓	0.038	40	✓	1.622	33	
1700	K 6.110	✓	0.073	44	✓	1.669	79	
1701	K 6.111	✓	0.181	97	✓	1.654	79	
1702	K 6.112	✗	5.336	50	✗	3.448	0	
1703	K 6.113	✓	0.095	63	✓	0.047	25	
1704	K 6.114	✗	41.261	62	✗	0.390	0	
1705	K 6.115	✗	0.245	43	✗	0.375	0	
1706	K 6.116	✗	0.483	52	✗	0.390	0	
1707	K 6.117	✓	0.073	31	✓	1.545	39	
1708	K 6.118	✗	46.195	43	✓ (ODESolStruct)	2.106	73	

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#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1709	K 6.119	✗	61.278	56	✓ (ODESolStruct)	2.792	84	
1710	K 6.120	✗	104.391	55	✓ (ODESolStruct)	4.383	91	
1711	K 6.121	✓	635.572	915	✓	0.390	81	
1712	K 6.122	✓	10.804	70	✓	0.063	61	
1713	K 6.123	✗	21.003	56	✓ (ODESolStruct)	0.234	60	
1714	K 6.124	✓	0.061	25	✓	1.513	67	
1715	K 6.125	✓	0.035	26	✓	1.638	25	
1716	K 6.126	✓	0.645	172	✓	1.622	68	
1717	K 6.127	✓	1.554	290	✓	1.716	108	
1718	K 6.128	✓	1.508	744	✓	0.187	158	
1719	K 6.129	✗	41.86	38	✓ (ODESolStruct)	0.374	70	
1720	K 6.130	✗	89.227	38	✓	1.747	174	
1721	K 6.131	✗	0.928	71	✗	1.856	0	
1722	K 6.132	✓	1.927	797	✓	3.339	98	
1723	K 6.133	✓	1.972	1033	✓	1.591	16	
1724	K 6.134	✓	0.199	38	✓	1.919	21	
1725	K 6.135	✓	0.327	75	✓	1.997	105	
1726	K 6.136	✓	0.754	75	✓	0.078	39	
1727	K 6.137	✓	0.173	129	✓	1.716	95	
1728	K 6.138	✓	0.006	31	✓	1.622	24	
1729	K 6.139	✗	0.023	31	✗	0.359	0	
1730	K 6.140	✓	0.483	127	✓	1.669	53	
1731	K 6.141	✓	1.403	359	✓	1.653	63	
1732	K 6.142	✗	1.658	35	✗	1.825	0	
1733	K 6.143	✓	2.552	437	✓	1.560	71	
1734	K 6.144	✗	1.482	37	✗	1.841	0	
1735	K 6.145	✗	1.244	36	✗	1.638	0	

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#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1736	K 6.146	✓	8.596	285	✓	1.654	49	
1737	K 6.147	✗	1.183	48	✗	1.779	0	
1738	K 6.148	✗	0.55	54	✗	1.217	0	
1739	K 6.149	✗	0.051	45	✗	0.265	0	
1740	K 6.150	✓	0.027	16	✓	1.513	13	
1741	K 6.151	✓	0.092	17	✓	1.638	37	
1742	K 6.152	✗	11.134	30	✓ (ODESolStruct)	0.140	60	
1743	K 6.153	✓	18.186	2761	✓	1.638	71	
1744	K 6.154	✓	0.975	173	✓	1.670	95	
1745	K 6.155	✓	0.295	204	✓	1.763	293	
1746	K 6.156	✗	0.041	36	✓	1.903	207	
1747	K 6.157	✓	0.028	20	✓	1.576	17	
1748	K 6.158	✓	0.094	43	✓	1.654	67	
1749	K 6.159	✓	0.547	181	✓	1.684	57	
1750	K 6.160	✓	3.891	2281	✓	1.716	87	
1751	K 6.161	✗	0.743	73	✗	0.483	0	
1752	K 6.162	✓	0.129	26	✓	1.575	33	
1753	K 6.163	✓	0.321	43	✓	1.575	147	
1754	K 6.164	✓	0.034	17	✓	1.544	15	
1755	K 6.165	✗	104.001	46	✓	1.810	1028	
1756	K 6.166	✓	0.662	126	✓	3.074	79	
1757	K 6.167	✗	0.827	59	✗	1.123	0	
1758	K 6.168	✓	0.062	36	✓	1.529	88	
1759	K 6.169	✓	0.037	18	✓	1.498	31	
1760	K 6.170	✓	11.967	104	✓	0.063	114	
1761	K 6.171	✗	1.734	52	✗	2.184	0	
1762	K 6.172	✗	52.686	39	✓ (ODESolStruct)	2.215	106	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1763	K 6.173	✓	0.139	35	✓	1.560	234	
1764	K 6.174	✓	0.065	52	✓	1.638	18	
1765	K 6.175	✓	0.128	24	✓	1.513	31	
1766	K 6.176	✓	0.047	21	✓	1.529	84	
1767	K 6.177	✓	0.076	55	✓	3.182	50	
1768	K 6.178	✓	0.113	87	✓	1.544	43	
1769	K 6.179	✓	0.046	18	✓	1.575	21	
1770	K 6.180	✓	0.792	28	✓	1.560	26	
1771	K 6.181	✓	0.082	21	✓	1.685	21	
1772	K 6.182	✓	0.866	37	✓	1.670	47	
1773	K 6.183	✓	0.19	44	✓	1.638	28	
1774	K 6.184	✓	1.34	93	✓	1.653	155	
1775	K 6.185	✓	0.135	29	✓	1.544	31	
1776	K 6.186	✗(hanged)	0	0	✓	1.825	88	
1777	K 6.187	✗	49.431	41	✓(ODESolStruct)	0.530	83	
1778	K 6.188	✓	0.538	75	✓	1.950	369	
1779	K 6.189	✗	3.996	28	✓	1.872	130	
1780	K 6.190	✗	0.489	32	✓	2.012	172	
1781	K 6.191	✓	0.085	19	✓	1.528	11	
1782	K 6.192	✓	0.088	93	✓	1.638	56	
1783	K 6.193	✓	1.423	26	✓	1.670	23	
1784	K 6.194	✓	0.264	74	✓	2.324	52	
1785	K 6.195	✓	0.364	95	✓	1.810	83	
1786	K 6.196	✓	1.029	95	✓	0.094	59	
1787	K 6.197	✓	36.216	166	✓	0.187	84	
1788	K 6.198	✗	1.565	85	✗	0.219	113	
1789	K 6.199	✗	8.823	110	✗	11.169	0	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1790	K 6.200	✓	21.362	182	✓	0.171	219	
1791	K 6.201	✓	20.225	164	✓	0.249	90	
1792	K 6.202	✓	25.014	222	✓	0.562	192	
1793	K 6.203	✓	1.372	113	✓	1.747	40	
1794	K 6.204	✓	1.296	98	✓	1.669	46	
1795	K 6.205	✓	0.26	116	✓	2.262	793	
1796	K 6.206	✓	0.34	66	✓	1.732	51	
1797	K 6.207	✗	23.56	91	✗	5.881	0	
1798	K 6.208	✗	38.093	37	✓	1.716	166	
1799	K 6.209	✓	1.945	88	✓	1.762	70	
1800	K 6.210	✓	0.521	84	✓	1.607	67	
1801	K 6.211	✗	20.022	32	✗	1.794	0	
1802	K 6.212	✗	0.358	41	✗	1.903	0	
1803	K 6.213	✓	18.332	10387	✓	5.288	230971	
1804	K 6.214	✓	2.998	415	✓	0.031	31	
1805	K 6.215	✓	1.882	436	✓	0.031	34	
1806	K 6.216	✗	18.425	123	✓	3.073	916	
1807	K 6.217	✗	33.962	185	✗	136.267	0	
1808	K 6.218	✓	103.725	172	✓	0.110	72	
1809	K 6.219	✗	43.117	33	✓	0.437	382	
1810	K 6.220	✓	0.06	1677	✓	0.109	55	
1811	K 6.221	✗(hanged)	0	0	✓	3.026	1864	
1812	K 6.222	✓	0.027	29	✓	0.031	19	
1813	K 6.223	✗	100.861	48	✓	0.265	146	
1814	K 6.224	✓	13.254	116	✓	0.125	90	
1815	K 6.225	✗	1.17	45	✓ (ODESolStruct)	0.780	74	
1816	K 6.226	✗	63.61	34	✓ (ODESolStruct)	0.874	46	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1817	K 6.227	✗	14.421	31	✓	0.156	40	
1818	K 6.228	✗	1.403	35	✓	0.265	66	
1819	K 6.229	✗	90.745	26	✓	0.047	42	
1820	K 6.230	✗(hanged)	0	0	✓(ODESolStruct)	0.780	81	
1821	K 6.231	✗	42.478	45	✓(ODESolStruct)	1.529	54	
1822	K 6.232	✓	1.083	371	✓	0.842	295	
1823	K 6.233	✗	0.17	35	✓	0.281	423	
1824	K 6.234	✓	0.353	347	✓	0.717	99	
1825	K 6.235	✗	0.041	27	✓(ODESolStruct)	0.702	50	
1826	K 6.236	✓	0.773	233	✓	0.203	201	
1827	K 6.237	✗	0.768	29	✓	2.169	81	
1828	K 6.238	✓	0.013	32	✓	1.045	20	
1829	K 6.239	✓	0.006	24	✓	0.234	32	
1830	K 6.240	✓	0.029	24	✓	0.390	312	
1831	K 6.241	✗	230.454	90	✓(ODESolStruct)	1.731	191	
1832	K 6.242	✗	0.682	24	✓(ODESolStruct)	0.608	117	
1833	K 6.243	✗(hanged)	0	0	✓	2.465	145	
1834	K 6.244	✗	16.501	53	✓(ODESolStruct)	0.343	86	
1835	K 6.245	✓	0.114	143	✗(hanged)	0	0	
1836	K 6.246	✗	14.719	44	✓(ODESolStruct)	0.297	94	
1837	K 7.1	✗	10.857	35	✓	0.265	95	
1838	K 7.2	✗	0.033	27	✓(ODESolStruct)	0.453	73	
1839	K 7.3	✗	0.03	25	✓(ODESolStruct)	0.655	127	
1840	K 7.4	✗	0.027	19	✓(ODESolStruct)	0.655	129	
1841	K 7.5	✗	0.088	41	✓(ODESolStruct)	0.406	60	
1842	K 7.6	✓	0.167	286	✓	0.421	190	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1843	K 7.7	✓	2.97	409	✓	0.234	77	
1844	K 7.8	✗	0.075	37	✓	0.203	26	
1845	K 7.9	✗	0.074	37	✓	0.187	22	
1846	K 7.10	✓	0.041	51	✓	0.0	28	
1847	K 7.11	✓	0.124	95	✓	0.171	49	
1848	K 7.12	✗	594.053	37	✓	0.843	789	
1849	K 7.13	✓	0.592	426	✓	0.125	337	
1850	K 7.14	✗	0.084	37	✓ (ODESolStruct)	1.092	165	
1851	K 7.15	✗	0.806	141	✗	2.589	0	
1852	K 7.16	✓	0.037	28	✓	0.203	30	
1853	K 7.17	✗	0.074	41	✓	0.515	110	
1854	K 7.18	✗	0.	1	✗	0.515	0	
1855	K 7.19	✗	0.	1	✗	0.515	0	
1856	K 8.1	✓	0.005	22	✓	0.015	19	
1857	K 8.2	✓	0.04	39	✓	0.047	35	
1858	K 8.3	✓	0.011	182	✓	0.047	64	
1859	K 8.4	✓	0.005	51	✓	0.031	37	
1860	K 8.5	✓	0.046	696	✓	0.046	237	
1861	K 8.6	✓	0.011	183	✓	0.062	144	
1862	K 8.7	✓	0.042	52	✓	0.032	42	
1863	K 8.8	✓	0.007	84	✓	0.031	35	
1864	K 8.9	✓	0.013	59	✓	0.031	46	
1865	K 8.10	✓	1.202	2062	✓	0.172	334	
1866	K 8.11	✓	0.027	132	✓	0.032	39	
1867	K 8.12	✓	0.076	124	✓	0.031	42	
1868	K 8.13	✓	0.046	162	✓	0.047	64	
1869	K 8.14	✓	0.088	118	✓	0.031	51	

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#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1870	K 8.15	✓	0.127	122	✓	0.078	47	
1871	K 8.16	✓	0.162	180	✓	0.047	71	
1872	K 8.17	✓	0.06	162	✓	0.047	65	
1873	K 8.18	✓	0.045	322	✓	0.047	52	
1874	K 8.19	✓	0.063	107	✓	0.296	57	
1875	K 8.20	✗	0.007	48	✓	0.670	1633	
1876	K 8.21	✓	0.075	38	✓	0.093	18	
1877	K 8.22	✓	0.005	31	✓	0.032	31	
1878	K 8.23	✓	0.013	39	✓	0.047	39	
1879	K 8.24	✓	0.058	58	✓	0.046	54	
1880	K 8.25	✗	0.022	79	✗(hanged)	0	0	
1881	K 8.26	✓	0.059	44	✓	0.015	48	
1882	K 8.27	✓	0.42	928	✓	0.047	118	
1883	K 8.28	✓	0.59	614	✓	0.094	80	
1884	K 8.29	✓	0.181	226	✓	0.078	69	
1885	K 8.30	✗	0.023	47	✓	0.078	47	
1886	K 8.31	✓	0.021	115	✓	0.062	50	
1887	K 8.32	✓	0.48	5748	✓	0.094	418	
1888	K 8.33	✓	25.511	37858	✓	0.171	634	
1889	K 8.34	✓	0.104	554	✓	0.032	72	
1890	K 8.35	✗	0.01	86	✗	13.666	1445	
1891	K 8.36	✓	0.446	766	✓	0.047	64	
1892	K 8.37	✓	0.371	4815	✓	0.094	868	
1893	K 8.38	✓	369.475	5538	✓	0.858	4516	
1894	K 8.39	✗(hanged)	0	0	✓	0.671	2511	
1895	K 8.40	✓	0.45	7517	✓	0.156	1187	
1896	K 8.41	✓	0.198	1132	✓	0.031	75	

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Table 4 – continued from previous page

#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1897	K 8.42	✓	0.114	284	✓	0.110	98	
1898	K 8.43	✓	0.038	420	✓	0.063	73	
1899	K 8.44	✓	0.011	112	✓	0.078	52	
1900	K 8.45	✓	0.01	94	✓	0.062	50	
1901	K 8.46	✓	0.01	105	✓	0.047	48	
1902	K 8.47	✓	0.014	226	✓	0.047	56	
1903	K 8.48	✓	0.09	1304	✓	0.109	312	
1904	K 8.49	✓	0.065	1445	✓	0.062	312	
1905	K 8.50	✗	0.007	61	✗	0.530	2014	
1906	K 8.51	✓	0.052	278	✓	0.063	128	
1907	K 8.52	✓	0.01	179	✓	0.046	66	
1908	K 8.53	✓	0.02	551	✓	0.468	3207	
1909	K 8.54	✓	0.06	1630	✓	23.774	33085	
1910	K 8.55	✓	0.01	39	✓	0.063	37	
1911	K 8.56	✗	0.038	64	✓	0.110	322	
1912	K 8.57	✗	0.011	122	✓	1.716	11399	
1913	K 9.1	✓	0.032	64	✓	0.109	54	
1914	K 9.2	✓	0.508	201	✓	0.250	92	
1915	K 9.3	✗(hanged)	0	0	✓(ODESolStruct)	13.791	181	
1916	K 9.4	✗(hanged)	0	0	✓	0.359	237	
1917	K 9.5	✗	250.097	35	✓	0.593	109	
1918	K 9.6	✗	0.091	47	✓(ODESolStruct)	1.373	245	
1919	K 9.7	✗	0.107	56	✓(ODESolStruct)	2.278	249	
1920	K 9.8	✗	0.082	52	✓(ODESolStruct)	2.294	250	
1921	K 9.9	✗	2.354	86	✗(hanged)	0	0	
1922	K 9.10	✗	11.113	106	✗(hanged)	0	0	

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#	Kamke	Mathematica			Maple			solved
		solved	cpu	leaf	solved	cpu	leaf	
1923	K 9.11	✓	0.686	53	✓	0.062	35	
1924	K 9.12	✓	0.071	191	✓	0.234	186	
1925	K 9.13	✗	8.4	55	✓	0.219	226	
1926	K 9.14	✗	0.006	46	✓	0.078	96	
1927	K 9.15	✗(hanged)	0	0	✗(hanged)	0	0	
1928	K 9.16	✗	0.007	52	✗(hanged)	0	0	
1929	K 9.17	✗	0.008	110	✓(ODESolStruct)	2.247	116	
1930	K 9.18	✓	0.053	308	✓	0.047	45	
1931	K 9.19	✓	6.038	10101	✓	0.514	1356	
1932	K 9.20	✗	2.252	55	✓	0.686	393	
1933	K 9.21	✗	126.589	55	✓	1.529	17743	
1934	K 9.22	✗	72.632	66	✓	0.904	376	
1935	K 9.23	✗	0.051	67	✓	1.357	741	
1936	K 9.24	✗	0.048	64	✓	0.531	704	
1937	K 9.25	✗	0.267	65	✓(ODESolStruct)	0.608	304	
1938	K 9.26	✓	0.011	137	✓	0.078	101	
1939	K 9.27	✗	0.012	76	✓	1.030	1121	
1940	K 9.28	✗	0.007	118	✗(hanged)	0	0	

## 2 Kamke chapter one. Linear first order

### 2.1 ODE No. 1

$$\frac{d}{dx}y(x) - \frac{1}{\sqrt{a_4 x^4 + a_3 x^3 + a_2 x^2 + a_1 x + a_0}} = 0$$

**Mathematica:** cpu = 2.001754 (sec), leaf count = 1117

$$\left\{ \left\{ y(x) \rightarrow c_1 - \frac{2F\left(\sin^{-1}\left(\sqrt{\frac{(x-\text{Root}[a_4\#1^4+a_3\#1^3+a_2\#1^2+a_1\#1+a_0\&,1])}{(x-\text{Root}[a_4\#1^4+a_3\#1^3+a_2\#1^2+a_1\#1+a_0\&,2])}}\right)}{\sqrt{\frac{(x-\text{Root}[a_4\#1^4+a_3\#1^3+a_2\#1^2+a_1\#1+a_0\&,1])}{(x-\text{Root}[a_4\#1^4+a_3\#1^3+a_2\#1^2+a_1\#1+a_0\&,2])}}}\right)}{\sqrt{\frac{(x-\text{Root}[a_4\#1^4+a_3\#1^3+a_2\#1^2+a_1\#1+a_0\&,1])}{(x-\text{Root}[a_4\#1^4+a_3\#1^3+a_2\#1^2+a_1\#1+a_0\&,2])}}}\right. \right.$$

**Maple:** cpu = 0.062 (sec), leaf count = 30

$$\left\{ y(x) = \int \frac{1}{\sqrt{a_4 x^4 + a_3 x^3 + a_2 x^2 + a_1 x + a_0}} dx + -C1 \right\}$$

**Sage:** cpu = 1.012 (sec), leaf count = 0

$$\left[ c + \int \frac{1}{\sqrt{a_4 x^4 + a_3 x^3 + a_2 x^2 + a_1 x + a_0}} dx, \text{linear} \right]$$

### 2.2 ODE No. 2

$$\frac{d}{dx}y(x) + ay(x) - ce^{bx} = 0$$

**Mathematica:** cpu = 0.014502 (sec), leaf count = 34

$$\left\{ \left\{ y(x) \rightarrow \frac{ce^{x(a+b)-ax}}{a+b} + c_1 e^{-ax} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 25

$$\left\{ y(x) = \left( \frac{ce^{(a+b)x}}{a+b} + -C1 \right) e^{-ax} \right\}$$

**Sage:** cpu = 0.008 (sec), leaf count = 0

$$\left[ \left( c + \frac{ce^{(ax+bx)}}{a+b} \right) e^{(-ax)}, \text{linear} \right]$$

### 2.3 ODE No. 3

$$\frac{d}{dx}y(x) + ay(x) - b \sin(cx) = 0$$

**Mathematica:** cpu = 0.058507 (sec), leaf count = 40

$$\left\{ \left\{ y(x) \rightarrow \frac{b(a \sin(cx) - c \cos(cx))}{a^2 + c^2} + c_1 e^{-ax} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 37

$$\left\{ y(x) = e^{-ax} \_C1 + \frac{b(\sin(cx) a - c \cos(cx))}{a^2 + c^2} \right\}$$

**Sage:** cpu = 0.008 (sec), leaf count = 0

$$\left[ - \left( \frac{(c \cos(cx) - a \sin(cx)) b e^{(ax)}}{a^2 + c^2} - c \right) e^{(-ax)}, \text{linear} \right]$$

### 2.4 ODE No. 4

$$\frac{d}{dx}y(x) + 2xy(x) - xe^{-x^2} = 0$$

**Mathematica:** cpu = 0.009001 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-x^2} + \frac{1}{2} e^{-x^2} x^2 \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 18

$$\left\{ y(x) = \left( \frac{x^2}{2} + \_C1 \right) e^{-x^2} \right\}$$

**Sage:** cpu = 0.008 (sec), leaf count = 0

$$\left[ \frac{1}{2} (x^2 + 2c) e^{(-x^2)}, \text{linear} \right]$$

## 2.5 ODE No. 5

$$\frac{d}{dx}y(x) + y(x) \cos(x) - e^{2x} = 0$$

**Mathematica:** cpu = 3.134898 (sec), leaf count = 38

$$\left\{ \left\{ y(x) \rightarrow e^{-\sin(x)} \int_1^x e^{2K[1]+\sin(K[1])} dK[1] + c_1 e^{-\sin(x)} \right\} \right\}$$

**Maple:** cpu = 0.171 (sec), leaf count = 27

$$\left\{ y(x) = e^{-\sin(x)} \int e^{2x+\sin(x)} dx + e^{-\sin(x)} \_C1 \right\}$$

**Sage:** cpu = 2.088 (sec), leaf count = 0

$$\left[ \left( c + \int e^{(2x+\sin(x))} dx \right) e^{(-\sin(x))}, \mathbf{linear} \right]$$

## 2.6 ODE No. 6

$$\frac{d}{dx}y(x) + y(x) \cos(x) - \frac{1}{2} \sin(2x) = 0$$

**Mathematica:** cpu = 0.022003 (sec), leaf count = 18

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-\sin(x)} + \sin(x) - 1 \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 15

$$\left\{ y(x) = \sin(x) - 1 + e^{-\sin(x)} \_C1 \right\}$$

**Sage:** cpu = 0.008 (sec), leaf count = 0

$$\left[ ((\sin(x) - 1)e^{\sin(x)} + c) e^{(-\sin(x))}, \mathbf{linear} \right]$$

## 2.7 ODE No. 7

$$\frac{d}{dx}y(x) + y(x) \cos(x) - e^{-\sin(x)} = 0$$

**Mathematica:** cpu = 0.022503 (sec), leaf count = 23

$$\{ \{ y(x) \rightarrow c_1 e^{-\sin(x)} + x e^{-\sin(x)} \} \}$$

**Maple:** cpu = 0.0 (sec), leaf count = 19

$$\{ y(x) = e^{-\sin(x)} \_C1 + e^{-\sin(x)} x \}$$

**Sage:** cpu = 0.004 (sec), leaf count = 0

$$[(c + x)e^{-\sin(x)}, \text{linear}]$$

## 2.8 ODE No. 8

$$\frac{d}{dx}y(x) + y(x) \tan(x) - \sin(2x) = 0$$

**Mathematica:** cpu = 0.024003 (sec), leaf count = 17

$$\{ \{ y(x) \rightarrow c_1 \cos(x) - 2 \cos^2(x) \} \}$$

**Maple:** cpu = 0.0 (sec), leaf count = 15

$$\{ y(x) = -2 (\cos(x))^2 + \cos(x) \_C1 \}$$

**Sage:** cpu = 0.004 (sec), leaf count = 0

$$\left[ \frac{c - 2 \cos(x)}{\sec(x)}, \text{linear} \right]$$

## 2.9 ODE No. 9

$$\frac{d}{dx}y(x) - (\sin(\ln(x)) + \cos(\ln(x)) + a)y(x) = 0$$

**Mathematica:** cpu = 0.015502 (sec), leaf count = 19

$$\{ \{ y(x) \rightarrow c_1 e^{ax + x \sin(\log(x))} \} \}$$

**Maple:** cpu = 0.015 (sec), leaf count = 16

$$\{y(x) = \_C1 e^{\sin(\ln(x))x+ax}\}$$

**Sage:** cpu = 0.004 (sec), leaf count = 0

$$\left[ c e^{(ax + \frac{1}{2} x(\cos(\log(x)) + \sin(\log(x))) - \frac{1}{2} x(\cos(\log(x)) - \sin(\log(x))))}, \mathbf{linear} \right]$$

## 2.10 ODE No. 10

$$\frac{d}{dx}y(x) + \left(\frac{d}{dx}f(x)\right)y(x) - f(x)\frac{d}{dx}f(x) = 0$$

**Mathematica:** cpu = 0.007501 (sec), leaf count = 18

$$\{\{y(x) \rightarrow c_1 e^{-f(x)} + f(x) - 1\}\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 15

$$\{y(x) = f(x) - 1 + e^{-f(x)} \_C1\}$$

**Sage:** cpu = 0.06 (sec), leaf count = 0

$$\left[ \left( c + \int e^{f(x)} f(x) D[0](f)(x) dx \right) e^{-f(x)}, \mathbf{linear} \right]$$

## 2.11 ODE No. 11

$$\frac{d}{dx}y(x) + f(x)y(x) - g(x) = 0$$

**Mathematica:** cpu = 0.472560 (sec), leaf count = 62

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\int_1^x -f(K[1]) dK[1]} + e^{\int_1^x -f(K[1]) dK[1]} \int_1^x g(K[2]) e^{-\int_1^{K[2]} -f(K[1]) dK[1]} dK[2] \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 24

$$\left\{ y(x) = \left( \int g(x) e^{\int f(x) dx} dx + \_C1 \right) e^{\int -f(x) dx} \right\}$$

**Sage:** cpu = 0.096 (sec), leaf count = 0

$$\left[ \left( c + \int e^{\int f(x) dx} g(x) dx \right) e^{-\int f(x) dx}, \mathbf{linear} \right]$$

## 2.12 ODE No. 12

$$\frac{d}{dx}y(x) + (y(x))^2 - 1 = 0$$

**Mathematica:** cpu = 0.063008 (sec), leaf count = 34

$$\left\{ \left\{ y(x) \rightarrow \frac{e^{2x} - e^{2c_1}}{e^{2c_1} + e^{2x}} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 8

$$\{y(x) = \tanh(x + \_C1)\}$$

**Sage:** cpu = 0.06 (sec), leaf count = 0

$$\left[ \frac{1}{2} \log(y(x) + 1) - \frac{1}{2} \log(y(x) - 1) = c + x, \text{separable} \right]$$

## 2.13 ODE No. 13

$$\frac{d}{dx}y(x) + (y(x))^2 - ax - b = 0$$

**Mathematica:** cpu = 0.051507 (sec), leaf count = 79

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt[3]{ac_1} \text{Ai}'\left(\frac{b+ax}{a^{2/3}}\right) + \sqrt[3]{a} \text{Bi}'\left(\frac{b+ax}{a^{2/3}}\right)}{-c_1 \text{Ai}\left(\frac{b+ax}{a^{2/3}}\right) - \text{Bi}\left(\frac{b+ax}{a^{2/3}}\right)} \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 79

$$\left\{ y(x) = -i\sqrt[3]{-ia} \left( \text{Ai}^{(1)}\left(- (ax+b) (-ia)^{-\frac{2}{3}}\right) \_C1 + \text{Bi}^{(1)}\left(- (ax+b) (-ia)^{-\frac{2}{3}}\right) \right) \left( \text{Ai}\left(- (ax+b) (-ia)^{-\frac{2}{3}}\right) \right)^{-\frac{2}{3}} \right\}$$

**Sage:** cpu = 2.744 (sec), leaf count = 0

$$\left[ \left[ y(x) = \frac{3a^5cx^5 \left( 4i I_{\frac{4}{3}}\left(\frac{2(ax+b)^{\frac{3}{2}}}{3a}\right) + 4i I_{\frac{2}{3}}\left(\frac{2(ax+b)^{\frac{3}{2}}}{3a}\right) \right) + 3a^4bcx^4 \left( 20i I_{\frac{4}{3}}\left(\frac{2(ax+b)^{\frac{3}{2}}}{3a}\right) + 20i I_{\frac{2}{3}}\left(\frac{2(ax+b)^{\frac{3}{2}}}{3a}\right) \right)}{\dots} \right] \right]$$



## 2.14 ODE No. 14

$$\frac{d}{dx}y(x) + (y(x))^2 + ax^m = 0$$

**Mathematica:** cpu = 0.010501 (sec), leaf count = 254

$$y(x) = -\frac{i\sqrt{-ax}^{\frac{m+2}{2}} \left( c_1 J_{\frac{m+1}{m+2}}(z) - c_1 J_{-\frac{m+3}{m+2}}(z) - 2J_{\frac{1}{m+2}-1}(z) \right) - c_1 J_{-\frac{1}{m+2}}(z)}{2x \left( c_1 J_{-\frac{1}{m+2}}(z) + J_{\frac{1}{m+2}}(z) \right)}$$

Where

$$z = \left( \frac{2i\sqrt{-ax}^{\frac{m}{2}+1}}{m+2} \right)$$

**Maple:** cpu = 0.093 (sec), leaf count = 189

$$\left\{ y(x) = -\frac{1}{x} \left( \sqrt{ax}^{\frac{m}{2}+1} J_{\frac{3+m}{m+2}} \left( 2 \frac{\sqrt{ax}^{m/2+1}}{m+2} \right) - C1 + Y_{\frac{3+m}{m+2}} \left( 2 \frac{\sqrt{ax}^{m/2+1}}{m+2} \right) \sqrt{ax}^{\frac{m}{2}+1} - C1 J_{(m+2)^{-1}} \left( 2 \frac{\sqrt{ax}^{m/2+1}}{m+2} \right) \right) \right.$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.15 ODE No. 15

$$\frac{d}{dx}y(x) + (y(x))^2 - 2x^2y(x) + x^4 - 2x - 1 = 0$$

**Mathematica:** cpu = 0.019502 (sec), leaf count = 25

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{c_1(-e^{2x}) - \frac{1}{2}} + x^2 + 1 \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 38

$$\left\{ y(x) = 1 \left( \frac{x^2 - C1}{(e^x)^2} - x^2 - \frac{C1}{(e^x)^2} - 1 \right) \left( -1 + \frac{C1}{(e^x)^2} \right)^{-1} \right\}$$

**Sage:** cpu = 0.064 (sec), leaf count = 0

$$\left[ \left[ y(x) = \frac{(ce^{(2x)} + 1)x^2 + ce^{(2x)} - 1}{ce^{(2x)} + 1} \right], \text{riccati} \right]$$

## 2.16 ODE No. 16

$$\frac{d}{dx}y(x) + (y(x))^2 + (xy(x) - 1)f(x) = 0$$

**Mathematica:** cpu = 21.387216 (sec), leaf count = 24

$$\text{DSolve}[f(x)(xy(x) - 1) + y'(x) + y(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 0.093 (sec), leaf count = 50

$$\left\{ y(x) = -1e^{\int -\frac{x^2 f(x)+2}{x} dx} \left( -C1 - \int e^{\int -\frac{x^2 f(x)+2}{x} dx} dx \right)^{-1} + x^{-1} \right\}$$

**Sage:** cpu = 0.068 (sec), leaf count = 0

$$[[[y(x) = 0, u f(x) = 0]], \text{riccati}]$$

## 2.17 ODE No. 17

$$\frac{d}{dx}y(x) - (y(x))^2 - 3y(x) + 4 = 0$$

**Mathematica:** cpu = 0.022503 (sec), leaf count = 34

$$\left\{ \left\{ y(x) \rightarrow \frac{-4e^{5c_1+5x} - 1}{e^{5c_1+5x} - 1} \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 25

$$\left\{ y(x) = -\frac{4e^{5x} - C1 + 1}{-1 + e^{5x} - C1} \right\}$$

**Sage:** cpu = 0.052 (sec), leaf count = 0

$$\left[ -\frac{1}{5} \log(y(x) + 4) + \frac{1}{5} \log(y(x) - 1) = c + x, \text{separable} \right]$$

## 2.18 ODE No. 18

$$\frac{d}{dx}y(x) - (y(x))^2 - xy(x) - x + 1 = 0$$

**Mathematica:** cpu = 0.020503 (sec), leaf count = 50

$$\left\{ \left\{ y(x) \rightarrow \frac{e^{\frac{x^2}{2}-2x}}{c_1 - \frac{\sqrt{\frac{\pi}{2}} \operatorname{erfi}\left(\frac{x-2}{\sqrt{2}}\right)}{e^2}} - 1 \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 47

$$\left\{ y(x) = -1 + \frac{1}{-C1 + \frac{i}{2}\sqrt{\pi}e^{-2}\sqrt{2}\operatorname{Erf}\left(\frac{i}{2}\sqrt{2}x - i\sqrt{2}\right)} e^{\frac{x^2}{2}-2x} \right\}$$

**Sage:** cpu = 0.076 (sec), leaf count = 0

$$\left[ \left[ y(x) = -\frac{\sqrt{\pi}ce^2 + \sqrt{\pi}\operatorname{erf}\left(\frac{1}{2}\sqrt{2}(ix - 2i)\right) + i\sqrt{2}e^{\left(\frac{1}{2}(x-2)^2\right)}}{\sqrt{\pi}ce^2 + \sqrt{\pi}\operatorname{erf}\left(\frac{1}{2}\sqrt{2}(ix - 2i)\right)} \right], \text{riccati} \right]$$

## 2.19 ODE No. 19

$$\frac{d}{dx}y(x) - (y(x) + x)^2 = 0$$

**Mathematica:** cpu = 0.009001 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{c_1 e^{2ix} - \frac{i}{2}} - x - i \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 16

$$\{y(x) = -x - \tan(-x + \_C1)\}$$

**Sage:** cpu = 0.052 (sec), leaf count = 0

$$\left[ \left[ \left[ x = c - \arctan(\sqrt{t}), y(x) = -x - \sqrt{t} \right], \left[ x = c + \arctan(\sqrt{t}), y(x) = -x + \sqrt{t} \right] \right], \text{lagrange} \right]$$

## 2.20 ODE No. 20

$$\frac{d}{dx}y(x) - (y(x))^2 + (x^2 + 1)y(x) - 2x = 0$$

**Mathematica:** cpu = 0.789600 (sec), leaf count = 48

$$\left\{ \left\{ y(x) \rightarrow \frac{e^{\frac{x^3}{3}+x}}{c_1 - \int_1^x e^{\frac{K[1]^3}{3}+K[1]} dK[1]} + x^2 + 1 \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 34

$$\left\{ y(x) = x^2 + 1 + 1e^{\frac{x^3}{3}+x} \left( -C1 - \int e^{\frac{x^3}{3}+x} dx \right)^{-1} \right\}$$

**Sage:** cpu = 0.244 (sec), leaf count = 0

$$\left[ \left[ y(x) = \frac{cx^2 + (x^2 + 1) \int e^{\left(\frac{1}{3}x^3+x\right)} dx + c - e^{\left(\frac{1}{3}x^3+x\right)}}{c + \int e^{\left(\frac{1}{3}x^3+x\right)} dx} \right], \text{riccati} \right]$$

## 2.21 ODE No. 21

$$\frac{d}{dx}y(x) - (y(x))^2 + y(x) \sin(x) - \cos(x) = 0$$

**Mathematica:** cpu = 7.447446 (sec), leaf count = 69

$$\left\{ \left\{ y(x) \rightarrow -\frac{c_1(1 - \sin(x)e^{\cos(x)} \left( \int_1^x e^{-\cos(K[1])} dK[1] \right)) - \sin(x)e^{\cos(x)}}{c_1e^{\cos(x)} \int_1^x e^{-\cos(K[1])} dK[1] + e^{\cos(x)}} \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 25

$$\left\{ y(x) = -\frac{e^{-\cos(x)}}{-C1 + \int e^{-\cos(x)} dx} + \sin(x) \right\}$$

**Sage:** cpu = 3.404 (sec), leaf count = 0

$$\left[ \left[ y(x) = \frac{ce^{\cos(x)} \sin(x) + e^{\cos(x)} \int e^{(-\cos(x))} dx \sin(x) - 1}{ce^{\cos(x)} + e^{\cos(x)} \int e^{(-\cos(x))} dx} \right], \text{riccati} \right]$$

## 2.22 ODE No. 22

$$\frac{d}{dx}y(x) - (y(x))^2 - y(x) \sin(2x) - \cos(2x) = 0$$

**Mathematica:** cpu = 241.061111 (sec), leaf count = 31

$$\text{DSolve}[y'(x) - y(x)^2 - y(x) \sin(2x) - \cos(2x) = 0, y(x), x]$$

**Maple:** cpu = 0.468 (sec), leaf count = 198

$$\left\{ y(x) = \left( 2 \frac{-C1 \cos(2x)}{\sqrt{2 \cos(2x) + 2}} \text{HeunCPrime} \left( 1, 1/2, -1/2, -1, \frac{7}{8}, 1/2 \cos(2x) + 1/2 \right) \left( -C1 \text{HeunC} \left( 1, \right. \right. \right.$$

**Sage:** cpu = 0.06 (sec), leaf count = 0

$$[[[y(x) = 0, u \cos(2x) = 0]], \text{riccati}]$$

## 2.23 ODE No. 23

$$\frac{d}{dx}y(x) + a(y(x))^2 - b = 0$$

**Mathematica:** cpu = 0.040505 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt{b} \tanh \left( \sqrt{a} \sqrt{bc_1} + \sqrt{a} \sqrt{bx} \right)}{\sqrt{a}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 29

$$\left\{ y(x) = \frac{1}{a} \tanh \left( -C1 \sqrt{ab} + x \sqrt{ab} \right) \sqrt{ab} \right\}$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.24 ODE No. 24

$$\frac{d}{dx}y(x) + a(y(x))^2 - bx^\nu = 0$$

**Mathematica:** cpu = 0.011501 (sec), leaf count = 277

$$\left\{ \left\{ y(x) \rightarrow - \frac{\sqrt{-a}\sqrt{bx}^{\frac{\nu+2}{2}} \left( c_1 J_{\frac{\nu+1}{\nu+2}} \left( \frac{2\sqrt{-a}\sqrt{bx}^{\frac{\nu+2}{2}}}{\nu+2} \right) - c_1 J_{-\frac{\nu+3}{\nu+2}} \left( \frac{2\sqrt{-a}\sqrt{bx}^{\frac{\nu+2}{2}}}{\nu+2} \right) - 2J_{\frac{1}{\nu+2}-1} \left( \frac{2\sqrt{-a}\sqrt{bx}^{\frac{\nu+2}{2}}}{\nu+2} \right) \right)}{2ax \left( c_1 J_{-\frac{1}{\nu+2}} \left( \frac{2\sqrt{-a}\sqrt{bx}^{\frac{\nu+2}{2}}}{\nu+2} \right) + J_{\frac{1}{\nu+2}} \left( \frac{2\sqrt{-a}\sqrt{bx}^{\frac{\nu+2}{2}}}{\nu+2} \right) \right)} \right\} \right.$$

**Maple:** cpu = 0.046 (sec), leaf count = 214

$$\left\{ y(x) = \frac{1}{ax} \left( -J_{\frac{3+\nu}{\nu+2}} \left( 2 \frac{\sqrt{-abx}^{\nu/2+1}}{\nu+2} \right) \sqrt{-abx}^{\frac{\nu}{2}+1} - C1 - Y_{\frac{3+\nu}{\nu+2}} \left( 2 \frac{\sqrt{-abx}^{\nu/2+1}}{\nu+2} \right) \sqrt{-abx}^{\frac{\nu}{2}+1} + -C1 J_{(\nu+2)} \right) \right.$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.25 ODE No. 25

$$\frac{d}{dx}y(x) + a(y(x))^2 - bx^{2\nu} - cx^{\nu-1} = 0$$

**Mathematica:** cpu = 0.237030 (sec), leaf count = 1835

$$\left\{ \left\{ y(x) \rightarrow - \frac{-2^{2(\nu+1)-1} e^{-\frac{\sqrt{a}\sqrt{bx}^{\nu+1}}{\sqrt{\nu^2+2\nu+1}}} \nu (x^{\nu+1})^{\frac{\nu}{2(\nu+1)}} L^{\frac{\nu}{\nu+1}-1} \frac{\sqrt{a}\sqrt{b\nu c} + \frac{\sqrt{a}\sqrt{bc}}{\sqrt{(\nu+1)^2}} + b\nu}{2(\nu b + b)} \left( \frac{2\sqrt{a}\sqrt{bx}^{\nu+1}}{\sqrt{\nu^2+2\nu+1}} \right) x^{-\frac{\nu}{2}-1} - \frac{\sqrt{a}\sqrt{b} e^{-\frac{\sqrt{a}\sqrt{bx}^{\nu+1}}{\sqrt{\nu^2+2\nu+1}}}}{2^{2(\nu+1)}}}{\dots} \right\} \right.$$

**Maple:** cpu = 0.249 (sec), leaf count = 378

$$\left\{ y(x) = \frac{1}{2ax} \left( \left( 2\sqrt{ax}^{\nu+1} - C1 b^2 - b^{\frac{3}{2}} - C1 \nu + \sqrt{a} - C1 bc \right) W_{-\frac{c}{2\nu+2}\sqrt{a}\frac{1}{\sqrt{b}}, \frac{1}{2\nu+2}} \left( 2 \frac{\sqrt{a}\sqrt{bx}^{\nu+1}}{\nu+1} \right) + (-2b^{\frac{3}{2}}) \right) \right\}$$

**Sage:** cpu = 0.084 (sec), leaf count = 0

$$\left[ \left[ y(x) = 0, (bx^{2\nu} + cx^{\nu-1})a^2u = 0 \right], \text{riccati} \right]$$

## 2.26 ODE No. 26

$$\frac{d}{dx}y(x) - (Ay(x) - a)(By(x) - b) = 0$$

**Mathematica:** cpu = 0.076010 (sec), leaf count = 68

$$\left\{ \left\{ y(x) \rightarrow \frac{ae^{Abc_1+Abx} - be^{aBc_1+aBx}}{Ae^{Abc_1+Abx} - Be^{aBc_1+aBx}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 59

$$\left\{ y(x) = \frac{e^{A-C1 b+Abx-B-C1 a-Bax} a - b}{Ae^{A-C1 b+Abx-B-C1 a-Bax} - B} \right\}$$

**Sage:** cpu = 0.152 (sec), leaf count = 0

$$\left[ \frac{\log(Ay(x) - a) - \log(By(x) - b)}{Ba - Ab} = c + x, \text{separable} \right]$$

## 2.27 ODE No. 27

$$\frac{d}{dx}y(x) + ay(x)(y(x) - x) - 1 = 0$$

**Mathematica:** cpu = 0.044006 (sec), leaf count = 120

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 \left( \sqrt{\frac{\pi}{2}} \sqrt{ax} e^{\frac{ax^2}{2}} \operatorname{erf}\left(\frac{\sqrt{ax}}{\sqrt{2}}\right) + 1 \right) + ax e^{\frac{ax^2}{2}}}{a \left( \frac{\sqrt{\frac{\pi}{2}} c_1 e^{\frac{ax^2}{2}} \operatorname{erf}\left(\frac{\sqrt{ax}}{\sqrt{2}}\right)}{\sqrt{a}} + e^{\frac{ax^2}{2}} \right)} \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 71

$$\left\{ y(x) = 1 \left( \sqrt{\pi} \operatorname{Erf} \left( \frac{\sqrt{2}x}{2} \sqrt{a} \right) \sqrt{2}ax + 2 a^{3/2} - C1 x + 2 \sqrt{a} e^{-1/2 ax^2} \right) \left( \sqrt{\pi} \operatorname{Erf} \left( \frac{\sqrt{2}x}{2} \sqrt{a} \right) \sqrt{2}a + 2 a^{3/2} \right) \right.$$

**Sage:** cpu = 0.068 (sec), leaf count = 0

$$\left[ \left[ y(x) = \frac{2 \sqrt{\frac{1}{2}} a^{\frac{3}{2}} c x e^{\left(\frac{1}{2} a x^2\right)} + \sqrt{\pi} a x \operatorname{erf} \left( \sqrt{\frac{1}{2}} \sqrt{a} x \right) e^{\left(\frac{1}{2} a x^2\right)} + 2 \sqrt{\frac{1}{2}} \sqrt{a}}{2 \sqrt{\frac{1}{2}} a^{\frac{3}{2}} c e^{\left(\frac{1}{2} a x^2\right)} + \sqrt{\pi} a \operatorname{erf} \left( \sqrt{\frac{1}{2}} \sqrt{a} x \right) e^{\left(\frac{1}{2} a x^2\right)}}, \operatorname{riccati} \right] \right]$$

## 2.28 ODE No. 28

$$\frac{d}{dx} y(x) + x(y(x))^2 - x^3 y(x) - 2x = 0$$

**Mathematica:** cpu = 0.047006 (sec), leaf count = 96

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{\frac{x^4}{4}} x^3 + \frac{1}{2} \sqrt{\pi} e^{\frac{x^4}{4}} x^3 \operatorname{erf} \left( \frac{x^2}{2} \right) + x}{x \left( c_1 e^{\frac{x^4}{4}} + \frac{1}{2} \sqrt{\pi} e^{\frac{x^4}{4}} \operatorname{erf} \left( \frac{x^2}{2} \right) \right)} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 67

$$\left\{ y(x) = 2 \frac{e^{-1/4 x^4} - C1}{\sqrt{\pi} \left( \operatorname{Erf} \left( \frac{x^2}{2} \right) - C1 + 1 \right)} + \frac{1}{\sqrt{\pi}} \left( \operatorname{Erf} \left( \frac{x^2}{2} \right) \sqrt{\pi} - C1 x^2 + x^2 \sqrt{\pi} \right) \left( \operatorname{Erf} \left( \frac{x^2}{2} \right) - C1 + 1 \right)^{-1} \right.$$

**Sage:** cpu = 0.096 (sec), leaf count = 0

$$\left[ \left[ y(x) = \frac{\left( \left( \sqrt{\pi} \operatorname{cerf} \left( \frac{1}{2} x^2 \right) + \sqrt{\pi} \right) x^2 e^{\left( \frac{1}{4} x^4 \right)} + 2 c \right) e^{\left( -\frac{1}{4} x^4 \right)}}{\sqrt{\pi} \operatorname{cerf} \left( \frac{1}{2} x^2 \right) + \sqrt{\pi}}, \operatorname{riccati} \right] \right]$$

## 2.29 ODE No. 29

$$\frac{d}{dx} y(x) - x(y(x))^2 - 3xy(x) = 0$$

**Mathematica:** cpu = 0.022003 (sec), leaf count = 39

$$\left\{ \left\{ y(x) \rightarrow -\frac{3e^{3c_1 + \frac{3x^2}{2}}}{e^{3c_1 + \frac{3x^2}{2}} - 1} \right\} \right\}$$



**Maple:** cpu = 0.031 (sec), leaf count = 19

$$\left\{ y(x) = 3 \left( -1 + 3e^{-3/2x^2} - C1 \right)^{-1} \right\}$$

**Sage:** cpu = 0.056 (sec), leaf count = 0

$$\left[ -\frac{1}{3} \log(y(x) + 3) + \frac{1}{3} \log(y(x)) = \frac{1}{2} x^2 + c, \text{separable} \right]$$

### 2.30 ODE No. 30

$$\frac{d}{dx} y(x) + x^{-a-1} (y(x))^2 - x^a = 0$$

**Mathematica:** cpu = 0.065008 (sec), leaf count = 230

$$\left\{ \left\{ y(x) \rightarrow \frac{x^{a+1} \left( c_1 \left( \frac{1}{2} x^{-\frac{a}{2} - \frac{1}{2}} \Gamma(a+1) (I_{a-1}(2\sqrt{x}) + I_{a+1}(2\sqrt{x})) - \frac{1}{2} a x^{-\frac{a}{2} - 1} \Gamma(a+1) I_a(2\sqrt{x}) \right) - \frac{1}{2} (-1) \right)}{c_1 x^{-a/2} \Gamma(a+1) I_a(2\sqrt{x}) + (-1)} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 81

$$\left\{ y(x) = -C1 x^{a+1} K_{a+1}(2\sqrt{x}) \frac{1}{\sqrt{x}} (K_a(2\sqrt{x}) - C1 + I_a(2\sqrt{x}))^{-1} + x^{a+1} I_{a+1}(2\sqrt{x}) \frac{1}{\sqrt{x}} (K_a(2\sqrt{x}) - C1) \right\}$$

**Sage:** cpu = 0.236 (sec), leaf count = 0

$$\left[ \left[ y(x) = -\frac{((c Y_a(2\sqrt{-x}) + J_a(2\sqrt{-x})) a + (c Y_{a+1}(2\sqrt{-x}) - c Y_{a-1}(2\sqrt{-x}) + J_{a+1}(2\sqrt{-x}) - J_{a-1}(2\sqrt{-x}))}{2 (c Y_a(2\sqrt{-x}) + J_a(2\sqrt{-x}))} \right] \right]$$

### 2.31 ODE No. 31

$$\frac{d}{dx} y(x) - a x^n ((y(x))^2 + 1) = 0$$

**Mathematica:** cpu = 0.060008 (sec), leaf count = 21

$$\left\{ \left\{ y(x) \rightarrow \tan \left( \frac{a x^{n+1}}{n+1} + c_1 \right) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 26

$$\left\{ y(x) = \tan \left( \frac{-C1 a n + x^{n+1} a + -C1 a}{n+1} \right) \right\}$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

### 2.32 ODE No. 32

$$\frac{d}{dx}y(x) + (y(x))^2 \sin(x) - 2 \frac{\sin(x)}{(\cos(x))^2} = 0$$

**Mathematica:** cpu = 0.237030 (sec), leaf count = 34

$$\left\{ \left\{ y(x) \rightarrow \frac{\csc(x) (c_1 \tan(x) \sec(x) - 2 \sin(x) \cos(x))}{c_1 \sec(x) + \cos^2(x)} \right\} \right\}$$

**Maple:** cpu = 0.218 (sec), leaf count = 28

$$\left\{ y(x) = -2 \frac{(\cos(x))^3 - C1 + 1}{((\cos(x))^3 - C1 - 2) \cos(x)} \right\}$$

**Sage:** cpu = 0.064 (sec), leaf count = 0

$$\left[ \left[ y(x) = -\frac{(c - 3i) \cosh\left(\frac{3}{2} \log(\cos(x))\right) + (3c - i) \sinh\left(\frac{3}{2} \log(\cos(x))\right)}{2c \cos(x) \cosh\left(\frac{3}{2} \log(\cos(x))\right) - 2i \cos(x) \sinh\left(\frac{3}{2} \log(\cos(x))\right)} \right], \text{riccati} \right]$$

### 2.33 ODE No. 33

$$\frac{d}{dx}y(x) - \frac{\left(\frac{d}{dx}f(x)\right) (y(x))^2}{g(x)} + \frac{\frac{d}{dx}g(x)}{f(x)} = 0$$

**Mathematica:** cpu = 26.354347 (sec), leaf count = 157

$$\text{Solve} \left[ \int_1^{y(x)} \left( \frac{1}{(f(x)K[2] + g(x))^2} - \int_1^x \left( \frac{2(K[2]^2 f(K[1])f'(K[1]) - g(K[1])g'(K[1]))}{g(K[1])(K[2]f(K[1]) + g(K[1]))^3} - \frac{2K[2]}{g(K[1])(K[2]f(K[1]) + g(K[1]))} \right) dx \right) dx \right]$$

**Maple:** cpu = 0.343 (sec), leaf count = 57

$$\left\{ y(x) = -\frac{1}{(f(x))^2} \left( g(x) f(x) \int \frac{\frac{d}{dx}f(x)}{g(x) (f(x))^2} dx + g(x) f(x) - C1 + 1 \right) \left( -C1 + \int \frac{\frac{d}{dx}f(x)}{g(x) (f(x))^2} dx \right) \right\}$$

**Sage:** cpu = 0.1 (sec), leaf count = 0

$$\left[ \left[ \left[ y(x) = 0, -\frac{uD[0](f)(x)^2 D[0](g)(x)}{f(x)g(x)^2} = 0 \right] \right], \text{riccati} \right]$$

### 2.34 ODE No. 34

$$\frac{d}{dx}y(x) + f(x) (y(x))^2 + g(x) y(x) = 0$$

**Mathematica:** cpu = 0.507064 (sec), leaf count = 51

$$\left\{ \left\{ y(x) \rightarrow \frac{e^{\int_1^x -g(K[1]) dK[1]}}{c_1 - \int_1^x f(K[2]) \left( -e^{\int_1^{K[2]} -g(K[1]) dK[1]} \right) dK[2]} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 28

$$\left\{ y(x) = \frac{e^{\int -g(x) dx}}{\int e^{\int -g(x) dx} f(x) dx + \_C1} \right\}$$

**Sage:** cpu = 0.112 (sec), leaf count = 0

$$\left[ \frac{e^{(-\int g(x) dx)}}{c + \int e^{(-\int g(x) dx)} f(x) dx}, \text{bernoulli} \right]$$

### 2.35 ODE No. 35

$$\frac{d}{dx}y(x) + f(x) ((y(x))^2 + 2ay(x) + b) = 0$$

**Mathematica:** cpu = 0.057507 (sec), leaf count = 60

$$\left\{ \left\{ y(x) \rightarrow \sqrt{b-a^2} \tan \left( \sqrt{b-a^2} \int_1^x -f(K[1]) dK[1] + c_1 \sqrt{b-a^2} \right) - a \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 45

$$\left\{ y(x) = \tanh \left( \int f(x) dx \sqrt{a^2 - b} + \_C1 \sqrt{a^2 - b} \right) \sqrt{a^2 - b} - a \right\}$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.36 ODE No. 36

$$\frac{d}{dx}y(x) + (y(x))^3 + ax(y(x))^2 = 0$$

**Mathematica:** cpu = 0.227029 (sec), leaf count = 195

$$\text{Solve} \left[ \frac{\text{Ai}'\left(\frac{\sqrt[3]{-\frac{1}{2}}\sqrt[3]{a}}{y(x)} - \frac{1}{2}\sqrt[3]{-\frac{1}{2}}a^{4/3}x^2\right) - \left(-\frac{1}{2}\right)^{2/3}a^{2/3}x\text{Ai}\left(\frac{\sqrt[3]{-\frac{1}{2}}\sqrt[3]{a}}{y(x)} - \frac{1}{2}\sqrt[3]{-\frac{1}{2}}a^{4/3}x^2\right)}{\text{Bi}'\left(\frac{\sqrt[3]{-\frac{1}{2}}\sqrt[3]{a}}{y(x)} - \frac{1}{2}\sqrt[3]{-\frac{1}{2}}a^{4/3}x^2\right) - \left(-\frac{1}{2}\right)^{2/3}a^{2/3}x\text{Bi}\left(\frac{\sqrt[3]{-\frac{1}{2}}\sqrt[3]{a}}{y(x)} - \frac{1}{2}\sqrt[3]{-\frac{1}{2}}a^{4/3}x^2\right)} + c_1 = 0, y(x) \right]$$

**Maple:** cpu = 0.062 (sec), leaf count = 62

$$\left\{ y(x) = 2 \frac{a}{a^2x^2 + 2 \text{RootOf}\left(\sqrt[3]{-2a^2}\text{Bi}(\_Z)\_C1 x + \sqrt[3]{-2a^2}x\text{Ai}(\_Z) + 2\text{Bi}^{(1)}(\_Z)\_C1 + 2\text{Ai}^{(1)}(\_Z)\right)} \right.$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.37 ODE No. 37

$$\frac{d}{dx}y(x) - (y(x))^3 - ae^x(y(x))^2 = 0$$

**Mathematica:** cpu = 0.679086 (sec), leaf count = 78

$$\text{Solve} \left[ -iae^x = \frac{2e^{\frac{1}{2}\left(-iae^x - \frac{i}{y(x)}\right)^2}}{2c_1 + \sqrt{2\pi}\text{erfi}\left(\frac{-iae^x - \frac{i}{y(x)}}{\sqrt{2}}\right)}, y(x) \right]$$

**Maple:** cpu = 0.062 (sec), leaf count = 50

$$\left\{ -C1 + \frac{1}{ae^x} e^{-\frac{(ae^x + (y(x))^{-1})^2}{2}} + \frac{\sqrt{2}\sqrt{\pi}}{2} \text{Erf}\left(\frac{(ae^x + (y(x))^{-1})\sqrt{2}}{2}\right) = 0 \right\}$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

### 2.38 ODE No. 38

$$\frac{d}{dx}y(x) - a(y(x))^3 - bx^{3/2} = 0$$

**Mathematica:** cpu = 8.692104 (sec), leaf count = 26

$$\text{DSolve}[-ay(x)^3 - bx^{3/2} + y'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.655 (sec), leaf count = 0

could not solve

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

### 2.39 ODE No. 39

$$\frac{d}{dx}y(x) - a^3(y(x))^3 - a^2(y(x))^2 - a^1y(x) - a^0 = 0$$

**Mathematica:** cpu = 0.051007 (sec), leaf count = 54

$$\text{Solve}\left[\text{RootSum}\left[\#1^3a^3 + \#1^2a^2 + \#1a^1 + a^0\&, \frac{\log(y(x) - \#1)}{3\#1^2a^3 + 2\#1a^2 + a^1}\&\right] = c_1 + x, y(x)\right]$$

**Maple:** cpu = 0.016 (sec), leaf count = 30

$$\left\{x - \int^{y(x)} (-a^3a^3 + -a^2a^2 + -a^1a^1 + a^0)^{-1} d_a + -C1 = 0\right\}$$

**Sage:** cpu = 0.228 (sec), leaf count = 0

$$\left[\int \frac{1}{a_3y(x)^3 + a_2y(x)^2 + a_1y(x) + a_0} d(y(x)) = c + x, \text{separable}\right]$$

## 2.40 ODE No. 40

$$\frac{d}{dx}y(x) + 3a(y(x))^3 + 6ax(y(x))^2 = 0$$

**Mathematica:** cpu = 0.241531 (sec), leaf count = 185

$$\text{Solve} \left[ \frac{\sqrt[3]{-3}\sqrt[3]{ax}\text{Ai}\left((-3)^{2/3}a^{2/3}x^2 - \frac{(-1)^{2/3}}{\sqrt[3]{3}\sqrt[3]{ay(x)}}\right) + \text{Ai}'\left((-3)^{2/3}a^{2/3}x^2 - \frac{(-1)^{2/3}}{\sqrt[3]{3}\sqrt[3]{ay(x)}}\right)}{\sqrt[3]{-3}\sqrt[3]{ax}\text{Bi}\left((-3)^{2/3}a^{2/3}x^2 - \frac{(-1)^{2/3}}{\sqrt[3]{3}\sqrt[3]{ay(x)}}\right) + \text{Bi}'\left((-3)^{2/3}a^{2/3}x^2 - \frac{(-1)^{2/3}}{\sqrt[3]{3}\sqrt[3]{ay(x)}}\right)} + c_1 = 0, y(x) \right]$$

**Maple:** cpu = 0.062 (sec), leaf count = 48

$$\left\{ y(x) = \left( 3ax^2 + \text{RootOf}\left(\sqrt[3]{-3}a\text{Bi}(\_Z)\_C1x + \sqrt[3]{-3}ax\text{Ai}(\_Z) + \text{Bi}^{(1)}(\_Z)\_C1 + \text{Ai}^{(1)}(\_Z)\right) \sqrt[3]{-3} \right. \right.$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.41 ODE No. 41

$$\frac{d}{dx}y(x) + ax(y(x))^3 + b(y(x))^2 = 0$$

**Mathematica:** cpu = 0.076010 (sec), leaf count = 103

$$\text{Solve} \left[ \frac{b^2 \left( \frac{2 \tan^{-1} \left( \frac{-2axy(x)-b}{b\sqrt{-\frac{4a}{b^2}-1}} \right)}{\sqrt{-\frac{4a}{b^2}-1}} - \log \left( \frac{a(-x)y(x)(-axy(x)-b)-a}{a^2x^2y(x)^2} \right) \right)}{2a} = c_1 - \frac{b^2 \log(x)}{a}, y(x) \right]$$

**Maple:** cpu = 0.172 (sec), leaf count = 103

$$\left\{ y(x) = \frac{1}{x} e^{\text{RootOf}\left(2\sqrt{b^2+4ab}\text{Artanh}\left(\frac{2ae^{-Z}+b}{\sqrt{b^2+4a}}\right) - \ln(x^2(ae^{-Z}+be^{-Z}-1))b^2+2\_C1b^2+2\_Zb^2-4\ln(x^2(ae^{-Z}+be^{-Z}-1))a+8\_C1\right)}$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.42 ODE No. 42

$$\frac{d}{dx}y(x) - x(x+2)(y(x))^3 - (x+3)(y(x))^2 = 0$$

**Mathematica:** cpu = 0.936119 (sec), leaf count = 485

$$\text{Solve } c_1 = - \frac{i\sqrt{\frac{2}{\pi}}\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}\left(\frac{\sinh\left(\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}\right)-\cosh\left(\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}\right)}{\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}}\right) - \frac{i\sqrt{\frac{2}{\pi}}\left(\frac{x+1}{2}+\frac{1}{2}\right)\sinh\left(\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}\right)}{\sqrt{-i\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}}}}{i\sqrt{\frac{2}{\pi}}\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}\left(i\sinh\left(\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}\right)-\frac{i\cosh\left(\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}\right)}{\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}}\right) - \frac{\sqrt{\frac{2}{\pi}}\left(\frac{x+1}{2}+\frac{1}{2}\right)\cosh\left(\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}\right)}{\sqrt{-i\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}}}$$

**Maple:** cpu = 0.016 (sec), leaf count = 40

$$\left\{ -C1 + \text{Artanh}\left(x\sqrt{y(x)}\frac{1}{\sqrt{x(x+2)y(x)+2}}\right) + \frac{1}{2}\sqrt{x(x+2)y(x)+2}\frac{1}{\sqrt{y(x)}} = 0 \right\}$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.43 ODE No. 43

$$\frac{d}{dx}y(x) + (4a^2x + 3ax^2 + b)(y(x))^3 + 3x(y(x))^2 = 0$$

**Mathematica:** cpu = 8.685603 (sec), leaf count = 490

$$\text{Solve } c_1 = - \frac{i\sqrt{-\frac{4a^3-3b}{4a^3}-\frac{3}{2a^2y(x)}+\frac{(-2a-3x)^2}{4a^2}}J_{\frac{1}{2}\sqrt{\frac{4a^3-3b}{a^3}+1}}\left(-i\sqrt{\frac{(-2a-3x)^2}{4a^2}-\frac{4a^3-3b}{4a^3}-\frac{3}{2a^2y(x)}}\right) + \left(\frac{1}{2}\sqrt{\frac{4a^3-3b}{a^3}}\right)}{i\sqrt{-\frac{4a^3-3b}{4a^3}-\frac{3}{2a^2y(x)}+\frac{(-2a-3x)^2}{4a^2}}Y_{\frac{1}{2}\sqrt{\frac{4a^3-3b}{a^3}+1}}\left(-i\sqrt{\frac{(-2a-3x)^2}{4a^2}-\frac{4a^3-3b}{4a^3}-\frac{3}{2a^2y(x)}}\right) + \left(\frac{1}{2}\sqrt{\frac{4a^3-3b}{a^3}}\right)}$$

**Maple:** cpu = 1.263 (sec), leaf count = 384

$$\left\{ -C1 + 1\left(-\left(\frac{1}{2}\sqrt{\frac{4a^3-3b}{a^3}}-\frac{2a+3x}{2a}\right)K_{\frac{1}{2}\sqrt{\frac{4a^3-3b}{a^3}+1}}\left(-\frac{\sqrt{3}}{2}\sqrt{\frac{4y(x)a^2x+3ax^2y(x)+by(x)-2a}{a^3y(x)}}\right)\right)$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.44 ODE No. 44

$$\frac{d}{dx}y(x) + 2ax^3(y(x))^3 + 2xy(x) = 0$$

**Mathematica:** cpu = 0.014502 (sec), leaf count = 72

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{2}}{\sqrt{-2ax^2 - a + 2c_1e^{2x^2}}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{2}}{\sqrt{-2ax^2 - a + 2c_1e^{2x^2}}} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 53

$$\left\{ y(x) = -2 \frac{1}{\sqrt{-4ax^2 + 4e^{2x^2} - C1 - 2a}}, y(x) = 2 \frac{1}{\sqrt{-4ax^2 + 4e^{2x^2} - C1 - 2a}} \right\}$$

**Sage:** cpu = 0.9 (sec), leaf count = 0

$$\left[ \frac{e^{(-x^2)}}{\sqrt{-\frac{1}{2}(2x^2 + 1)ae^{(-2x^2)} + c}}, \text{bernoulli} \right]$$

## 2.45 ODE No. 45

$$\frac{d}{dx}y(x) + 2(a^2x^3 - b^2x)(y(x))^3 + 3b(y(x))^2 = 0$$

**Mathematica:** cpu = 0.522566 (sec), leaf count = 133

$$\text{Solve} \left[ c_1 = \sqrt[4]{\left(\frac{b}{ax} - \frac{1}{ax^2y(x)}\right)^2 - 1} \left( -\frac{\left(\frac{b}{ax} - \frac{1}{ax^2y(x)}\right) {}_2F_1\left(\frac{1}{2}, \frac{3}{4}; \frac{3}{2}; \left(\frac{b}{ax} - \frac{1}{ax^2y(x)}\right)^2\right)}{2\sqrt[4]{1 - \left(\frac{b}{ax} - \frac{1}{ax^2y(x)}\right)^2}} - \frac{ax}{b} \right), y(x) \right]$$

**Maple:** cpu = 0.094 (sec), leaf count = 123

$$\left\{ -C1 + 1 \sqrt[4]{\left(\frac{ax}{b} + \left(\frac{b^2y(x)}{a} - \frac{b}{ax}\right)^{-1}\right)^2 - 1} \left(\frac{b^2y(x)}{a} - \frac{b}{ax}\right)^{-1} \frac{1}{\sqrt{\frac{ax}{b} + \left(\frac{b^2y(x)}{a} - \frac{b}{ax}\right)^{-1}}} - \int^{\frac{ax^2y(x)}{bxy(x)-1}} 1 \sqrt[4]{\dots} \right\}$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE



## 2.46 ODE No. 46

$$\frac{d}{dx}y(x) - x^a(y(x))^3 + 3(y(x))^2 - x^{-a}y(x) - x^{-2a} + ax^{-a-1} = 0$$

**Mathematica:** cpu = 0.227529 (sec), leaf count = 258

$$\left\{ \left\{ y(x) \rightarrow x^{-a} - \frac{e^{-\frac{2x^{1-a}}{1-a}}}{\sqrt{c_1 - \frac{2x \left( \frac{\frac{a+1}{4} x^{\frac{1-a}}{1-a} \right)^{\frac{2}{a-1}} \Gamma\left(-\frac{2}{a-1}, -\frac{4x^{1-a}}{a-1}\right)}{a-1} + e^{\frac{4x^{1-a}}{a-1}} x^a}{a+1}} \right\} \right\}, \left\{ y(x) \rightarrow \frac{e^{\frac{2x^{1-a}}{1-a}}}{\sqrt{c_1 - \frac{2x \left( \frac{\frac{a+1}{4} x^{\frac{1-a}}{1-a} \right)^{\frac{2}{a-1}} \Gamma\left(-\frac{2}{a-1}, -\frac{4x^{1-a}}{a-1}\right)}{a-1} + e^{\frac{4x^{1-a}}{a-1}} x^a}{a+1}}} \right\} \right.$$

**Maple:** cpu = 0.062 (sec), leaf count = 1052

$$\left\{ y(x) = -1e^{2\frac{x}{(a-1)x^a}} \sqrt{-C1 - 2\frac{1}{1-a}2^{-2\frac{a}{1-a}-2(1-a)^{-1}}((1-a)^{-1})^{-\frac{a}{1-a}-(1-a)^{-1}}\left(\frac{1-a}{-3+a}2^{-3+2\frac{a}{1-a}+2(1-a)^{-1}+2(a-1)^{-1}}\right)^{\frac{2}{a-1}}}\right.$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.47 ODE No. 47

$$\frac{d}{dx}y(x) - a(x^n - x)(y(x))^3 - (y(x))^2 = 0$$

**Mathematica:** cpu = 33.168712 (sec), leaf count = 31

$$\text{DSolve}[-a(x^n - x)y(x)^3 + y'(x) - y(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 1.248 (sec), leaf count = 0

could not solve

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.48 ODE No. 48

$$\frac{d}{dx}y(x) - (ax^n + bx)(y(x))^3 - c(y(x))^2 = 0$$

**Mathematica:** cpu = 36.628151 (sec), leaf count = 33

$$\text{DSolve}[y(x)^3(-(ax^n + bx)) - cy(x)^2 + y'(x) = 0, y(x), x]$$

**Maple:** cpu = 1.232 (sec), leaf count = 0

could not solve

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.49 ODE No. 49

$$\frac{d}{dx}y(x) + a\left(\frac{d}{dx}\phi(x)\right)(y(x))^3 + 6a\phi(x)(y(x))^2 + \frac{(2a+1)y(x)\frac{d^2}{dx^2}\phi(x)}{\frac{d}{dx}\phi(x)} + 2a + 2 = 0$$

**Mathematica:** cpu = 28.631636 (sec), leaf count = 52

$$\text{DSolve}\left[ay(x)^3\phi'(x) + \frac{(2a+1)y(x)\phi''(x)}{\phi'(x)} + 6a\phi(x)y(x)^2 + 2a + y'(x) + 2 = 0, y(x), x\right]$$

**Maple:** cpu = 0.702 (sec), leaf count = 0

could not solve

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.50 ODE No. 50

$$\frac{d}{dx}y(x) - f_3(x)(y(x))^3 - f_2(x)(y(x))^2 - f_1(x)y(x) - f_0(x) = 0$$

**Mathematica:** cpu = 125.836479 (sec), leaf count = 37

$$\text{DSolve}[-f_0(x) - f_1(x)y(x) - f_2(x)y(x)^2 - f_3(x)y(x)^3 + y'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.265 (sec), leaf count = 0

could not solve

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.51 ODE No. 51

$$\frac{d}{dx}y(x) - (y(x) - f(x))(y(x) - g(x)) \left( y(x) - \frac{af(x) + bg(x)}{a + b} \right) h(x) - \frac{\left(\frac{d}{dx}f(x)\right)(y(x) - g(x))}{f(x) - g(x)} - \frac{\left(\frac{d}{dx}g(x)\right)(y(x) - f(x))}{g(x) - f(x)}$$

**Mathematica:** cpu = 0.753096 (sec), leaf count = 354

$$\text{Solve} \left[ -\frac{1}{3}(a - b)^{2/3}(2a + b)^{2/3}(a + 2b)^{2/3} \text{RootSum} \left[ \#1^3(a - b)^{2/3}(2a + b)^{2/3}(a + 2b)^{2/3} - 3\#1a^2 - 3\#1b^2 \right] \right]$$

**Maple:** cpu = 0.156 (sec), leaf count = 2348

$$\left\{ y(x) = -\frac{1}{9a^3 + 18a^2b + 18ab^2 + 9b^3} \left( 2g(x) \text{RootOf} \left( -27 \int^{-Z} \frac{1}{4a^3a^6 + 12a^3a^5b - 3a^3a^4b^2 - 27a^3a^3b^3 + 18a^2a^2b^2 - 18a^2a^2b^2 + 9b^3} dz \right) \right) \right\}$$

**Sage:** cpu = 2.588 (sec), leaf count = 0

$$\left[ (a^2 + ab + b^2) \log \left( 3a^2 + 3ab + 3b^2 - \frac{3(a^3 + 3a^2b + 3ab^2 + b^3)(a^2 + ab - 2b^2) \left( \frac{(2a+b)f(x) + (a+2b)g(x)}{a+b} - 3y(x) \right)}{(a^2 + ab + b^2)} \right) \right]$$

## 2.52 ODE No. 52

$$\frac{d}{dx}y(x) - a(y(x))^n - bx^{\frac{n}{1-n}} = 0$$

**Mathematica:** cpu = 116.892343 (sec), leaf count = 115

$$\text{Solve} \left[ \int_1^{y(x) \left( \frac{ax - \frac{n}{1-n}}{b} \right)^{\frac{1}{n}}} \frac{1}{-K[1] \left( \frac{(-1)^n (n-1)^{-n} b^{1-n}}{a} \right)^{\frac{1}{n}} + K[1]^n + 1} dK[1] = \int_1^x bK[2]^{\frac{n}{1-n}} \left( \frac{aK[2]^{-\frac{n}{1-n}}}{b} \right)^{\frac{1}{n}} dx \right]$$

**Maple:** cpu = 0.156 (sec), leaf count = 61

$$\left\{ - \int_{-b}^{y(x)} 1x^{\frac{n}{n-1}} \left( (ax(n-1) - a^n + a) x^{\frac{n}{n-1}} + b(n-1)x \right)^{-1} dx - a(n-1) + \ln(x) - C1 = 0 \right\}$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.53 ODE No. 53

$$\frac{d}{dx}y(x) - \frac{(f(x))^{1-n} \left( \frac{d}{dx}g(x) \right) (y(x))^n}{(ag(x) + b)^n} - \frac{\left( \frac{d}{dx}f(x) \right) y(x)}{f(x)} - f(x) \frac{d}{dx}g(x) = 0$$

**Mathematica:** cpu = 57.744833 (sec), leaf count = 95

$$\text{Solve} \left[ \int_1^{y(x)(f(x)^{-n}(ag(x)+b)^{-n})^{\frac{1}{n}}} \frac{1}{-(a^n)^{\frac{1}{n}} K[1] + K[1]^n + 1} dK[1] = \frac{f(x)(ag(x) + b) \log(ag(x) + b) (f(x))^{-n}}{a} \right]$$

**Maple:** cpu = 0.062 (sec), leaf count = 281

$$\left\{ y(x) = \frac{(ag(x) + b) f(x)}{a} \text{RootOf} \left( - \int^{-Z} \frac{1}{-a \left( \left( \frac{d}{dx}g(x) \right) (ag(x) + b)^{-n} (f(x))^{1-n} \right)^{-n-1} (f(x) \frac{d}{dx}g(x))} dx \right) \right\}$$

**Sage:** cpu = 69.46 (sec), leaf count = 0

$$\left[ \int - \frac{(ag(x) + b)^n f(x)^n y(x) D[0](f)(x) + y(x)^n f(x)^2 D[0](g)(x) + (ag(x) + b)^n f(x)^{n+2} D[0](g)(x)}{(ag(x) + b)^n a f(x)^{n+1} y(x) - (a f(x)^{n+2} g(x) + b f(x)^{n+2}) (ag(x) + b)^n - (a f(x)^2 g(x) + b f(x)^2)} dx \right]$$

## 2.54 ODE No. 54

$$\frac{d}{dx}y(x) - a^n(f(x))^{1-n} \left( \frac{d}{dx}g(x) \right) (y(x))^n - \frac{\left( \frac{d}{dx}f(x) \right) y(x)}{f(x)} - f(x) \frac{d}{dx}g(x) = 0$$

**Mathematica:** cpu = 0.116515 (sec), leaf count = 74

$$\text{Solve} \left[ y(x) (a^n f(x)^{-n})^{\frac{1}{n}} {}_2F_1 \left( 1, \frac{1}{n}; 1 + \frac{1}{n}; - \left( (a^n f(x)^{-n})^{\frac{1}{n}} y(x) \right)^n \right) = f(x)g(x) (a^n f(x)^{-n})^{\frac{1}{n}} + c_1, y(x) \right]$$

**Maple:** cpu = 0.124 (sec), leaf count = 42

$$\left\{ -C1 + \frac{y(x)}{f(x)} {}_2F_1(1, n^{-1}; \frac{n+1}{n}; - \left( \frac{ay(x)}{f(x)} \right)^n) - g(x) = 0 \right\}$$

**Sage:** cpu = 1.384 (sec), leaf count = 0

$$\left[ \int \frac{a^n y(x)^n f(x)^2 D[0](g)(x) + f(x)^n y(x) D[0](f)(x) + f(x)^{n+2} D[0](g)(x)}{a^n y(x)^n f(x)^2 + f(x)^{n+2}} dx + \int \frac{(a^n y(x)^n f(x) + \dots}{\dots} \right]$$

## 2.55 ODE No. 55

$$\frac{d}{dx}y(x) - f(x) (y(x))^n - g(x) y(x) - h(x) = 0$$

**Mathematica:** cpu = 6.593337 (sec), leaf count = 29

$$\text{DSolve}[-f(x)y(x)^n - g(x)y(x) - h(x) + y'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.218 (sec), leaf count = 0

could not solve

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.56 ODE No. 56

$$\frac{d}{dx}y(x) - f(x)(y(x))^a - g(x)(y(x))^b = 0$$

**Mathematica:** cpu = 2.267788 (sec), leaf count = 27

$$\text{DSolve}[-f(x)y(x)^a - g(x)y(x)^b + y'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.202 (sec), leaf count = 0

could not solve

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.57 ODE No. 57

$$\frac{d}{dx}y(x) - \sqrt{|y(x)|} = 0$$

**Mathematica:** cpu = 101.289362 (sec), leaf count = 283

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\frac{2 \cdot 2^{3/4} (1 - \#1) \sqrt[4]{|\Im(\#1)|} + i(1 - \Re(\#1))(i|\Im(\#1)| - \Re(\#1) + 1) {}_2F_1\left(\frac{1}{4}, \dots\right)}{3 \sqrt[4]{|\Im(\#1)|} (\Im(\#1)^2 + (1 - \Re(\#1))^2)} \right] \right. \right.$$

**Maple:** cpu = 0.078 (sec), leaf count = 31

$$\left\{ x - \begin{cases} -2 \sqrt{-y(x)} & y(x) \leq 0 \\ 2 \sqrt{y(x)} & 0 < y(x) \end{cases} + _C1 = 0 \right\}$$

**Sage:** cpu = 1.08 (sec), leaf count = 0

[c + x, separable]

## 2.58 ODE No. 58

$$\frac{d}{dx}y(x) - a\sqrt{y(x)} - bx = 0$$

**Mathematica:** cpu = 0.153020 (sec), leaf count = 119

$$\text{Solve} \left[ \frac{a^2 \left( -\log \left( a^2 \left( \sqrt{\frac{a^2 y(x)}{b^2 x^2}} + 1 \right) - \frac{2a^2 y(x)}{bx^2} \right) - \frac{2a \tanh^{-1} \left( \frac{a^2 - 4b \sqrt{\frac{a^2 y(x)}{b^2 x^2}}}{a \sqrt{a^2 + 8b}} \right)}{\sqrt{a^2 + 8b}} \right)}{2b} = \frac{a^2 \log(x)}{b} + c_1, y(x) \right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 68

$$\left\{ -\frac{1}{2} \ln \left( \sqrt{y(x)} ax + bx^2 - 2y(x) \right) + a\sqrt{y(x)} \text{Artanh} \left( 1 \left( a\sqrt{y(x)} + 2bx \right) \frac{1}{\sqrt{y(x)(a^2 + 8b)}} \right) \frac{1}{\sqrt{y(x)(a^2 + 8b)}} \right\}$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.59 ODE No. 59

$$\frac{d}{dx}y(x) - a\sqrt{(y(x))^2 + 1} - b = 0$$

**Mathematica:** cpu = 0.176522 (sec), leaf count = 96

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \frac{b \tan^{-1} \left( \frac{\#1b}{\sqrt{\#1^2 + 1} \sqrt{a^2 - b^2}} \right) - \frac{b \tan^{-1} \left( \frac{\#1a}{\sqrt{a^2 - b^2}} \right) + \sinh^{-1}(\#1)}{a} \right] \& [c_1 + x] \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 26

$$\left\{ x - \int^{y(x)} \left( a\sqrt{-a^2 + 1} + b \right)^{-1} d_a + \_C1 = 0 \right\}$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.60 ODE No. 60

$$\frac{d}{dx}y(x) - \frac{\sqrt{(y(x))^2 - 1}}{\sqrt{x^2 - 1}} = 0$$

**Mathematica:** cpu = 0.049506 (sec), leaf count = 55

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( -e^{-c_1} \sqrt{x^2 - 1} + e^{c_1} \sqrt{x^2 - 1} + e^{-c_1} x + e^{c_1} x \right) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 29

$$\left\{ \ln \left( x + \sqrt{x^2 - 1} \right) - \ln \left( y(x) + \sqrt{(y(x))^2 - 1} \right) + \_C1 = 0 \right\}$$

**Sage:** cpu = 1.22 (sec), leaf count = 0

$$\left[ \log \left( 2 \sqrt{y(x)^2 - 1} + 2y(x) \right) = c + \log \left( 2x + 2\sqrt{x^2 - 1} \right), \text{separable} \right]$$

## 2.61 ODE No. 61

$$\frac{d}{dx}y(x) - \frac{\sqrt{x^2 - 1}}{\sqrt{(y(x))^2 - 1}} = 0$$

**Mathematica:** cpu = 0.176522 (sec), leaf count = 75

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \frac{1}{2} \#1 \sqrt{\#1^2 - 1} - \frac{1}{2} \log \left( \sqrt{\#1^2 - 1} + \#1 \right) \right] \& \right\} \left[ c_1 + \frac{1}{2} \sqrt{x^2 - 1} x - \frac{1}{2} \log \left( \sqrt{x^2 - 1} + x \right) \right] \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 50

$$\left\{ \_C1 + x \sqrt{x^2 - 1} - \ln \left( x + \sqrt{x^2 - 1} \right) - y(x) \sqrt{(y(x))^2 - 1} + \ln \left( y(x) + \sqrt{(y(x))^2 - 1} \right) = 0 \right\}$$

**Sage:** cpu = 0.176 (sec), leaf count = 0

$$\left[ \frac{1}{2} \sqrt{y(x)^2 - 1} y(x) - \frac{1}{2} \log \left( 2 \sqrt{y(x)^2 - 1} + 2y(x) \right) = \frac{1}{2} \sqrt{x^2 - 1} x + c - \frac{1}{2} \log \left( 2x + 2\sqrt{x^2 - 1} \right), \text{separable} \right]$$



## 2.62 ODE No. 62

$$\frac{d}{dx}y(x) - \frac{y(x) - x^2\sqrt{x^2 - (y(x))^2}}{xy(x)\sqrt{x^2 - (y(x))^2} + x} = 0$$

**Mathematica:** cpu = 3.807984 (sec), leaf count = 40

$$\text{Solve} \left[ \tan^{-1} \left( \frac{y(x)}{\sqrt{x^2 - y(x)^2}} \right) + \frac{x^2}{2} + \frac{y(x)^2}{2} = c_1, y(x) \right]$$

**Maple:** cpu = 0.297 (sec), leaf count = 34

$$\left\{ \frac{(y(x))^2}{2} + \arctan \left( y(x) \frac{1}{\sqrt{x^2 - (y(x))^2}} \right) + \frac{x^2}{2} - C1 = 0 \right\}$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.63 ODE No. 63

$$\frac{d}{dx}y(x) - \frac{(y(x))^2 + 1}{|y(x) + \sqrt{1 + y(x)}| (1 + x)^{3/2}} = 0$$

**Mathematica:** cpu = 558.947977 (sec), leaf count = 47

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \int_1^{\#1} \frac{|K[1] + \sqrt{K[1] + 1}|}{K[1]^2 + 1} dK[1] \& \right] \left[ c_1 - \frac{2}{\sqrt{x + 1}} \right] \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 35

$$\left\{ -2 \frac{1}{\sqrt{1 + x}} - \int^{y(x)} \frac{1}{-a^2 + 1} | -a + \sqrt{-a + 1} | d_a + C1 = 0 \right\}$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.64 ODE No. 64

$$\frac{d}{dx}y(x) - \sqrt{\frac{a(y(x))^2 + by(x) + c}{ax^2 + bx + c}} = 0$$

**Mathematica:** cpu = 0.187524 (sec), leaf count = 269

$$\left\{ \left\{ y(x) \rightarrow \frac{e^{-\sqrt{ac_1}} (8a^{3/2}ce^{2\sqrt{ac_1}}\sqrt{ax^2 + bx + c} - 8a^{3/2}c\sqrt{ax^2 + bx + c} + 8a^2cx e^{2\sqrt{ac_1}} + 8a^2cx + 2b^3e^{\sqrt{ac_1}})}{\dots} \right. \right.$$

**Maple:** cpu = 0.078 (sec), leaf count = 124

$$\left\{ -1\sqrt{\frac{a(y(x))^2 + by(x) + c}{ax^2 + bx + c}}\sqrt{ax^2 + bx + c} \ln\left(\frac{1}{2}\left(2\sqrt{ax^2 + bx + c}\sqrt{a} + 2ax + b\right)\frac{1}{\sqrt{a}}\right) \frac{1}{\sqrt{a(y(x))^2 + b}} \right.$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.65 ODE No. 65

$$\frac{d}{dx}y(x) - \sqrt{\frac{(y(x))^3 + 1}{x^3 + 1}} = 0$$

**Mathematica:** cpu = 1.550697 (sec), leaf count = 312

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \frac{i(\#1 + 1)\sqrt{1 + \frac{6i}{(\sqrt{3}-3i)(\#1+1)}}\sqrt{\frac{2}{3} - \frac{4i}{(\sqrt{3}+3i)(\#1+1)}}F\left(i \sinh^{-1}\left(\frac{\sqrt{-\frac{6i}{3i+\sqrt{3}}}}{\sqrt{\#1+1}}\right)\right)}{\sqrt{-\frac{i}{\sqrt{3}+3i}}\sqrt{\#1^2 - \#1 + 1}} \right] \right. \right.$$

**Maple:** cpu = 0.063 (sec), leaf count = 47

$$\left\{ \int^{y(x)} \frac{1}{\sqrt{-a^3 + 1}} d_a + \int^x -1\sqrt{\frac{(y(x))^3 + 1}{-a^3 + 1}} \frac{1}{\sqrt{(y(x))^3 + 1}} d_a + \_C1 = 0 \right\}$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.66 ODE No. 66

$$\frac{d}{dx}y(x) - \frac{\sqrt{|y(x)(1-y(x))(1-ay(x))|}}{\sqrt{|x(1-x)(-ax+1)|}} = 0$$

**Mathematica:** cpu = 877.251897 (sec), leaf count = 65

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \int_1^{\#1} \frac{1}{\sqrt{|(1-K[1])K[1](1-aK[1])|}} dK[1] \& \right] \left[ \int_1^x \frac{1}{\sqrt{|(1-K[2])K[2](1-aK[2])|}} dK[2] \right] \right. \right.$$

**Maple:** cpu = 0.062 (sec), leaf count = 40

$$\left\{ \int \frac{1}{\sqrt{|x(x-1)(ax-1)|}} dx - \int^{y(x)} \frac{1}{\sqrt{|_a(_a-1)(_a a-1)|}} d_a + _C1 = 0 \right\}$$

**Sage:** cpu = 1.572 (sec), leaf count = 0

$$[(y(x) - 1)\text{sgn}(y(x) - 1) = (x - 1)\text{sgn}(x - 1) + c, \text{separable}]$$

## 2.67 ODE No. 67

$$\frac{d}{dx}y(x) - \frac{\sqrt{1-(y(x))^4}}{\sqrt{-x^4+1}} = 0$$

**Mathematica:** cpu = 0.080010 (sec), leaf count = 14

$$\{ \{ y(x) \rightarrow \text{sn}(c_1 + F(\sin^{-1}(x) | -1) | -1) \} \}$$

**Maple:** cpu = 0.015 (sec), leaf count = 32

$$\left\{ \int \frac{1}{\sqrt{-x^4+1}} dx - \int^{y(x)} \frac{1}{\sqrt{-_a^4+1}} d_a + _C1 = 0 \right\}$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.68 ODE No. 68

$$\frac{d}{dx}y(x) - \sqrt{\frac{a(y(x))^4 + b(y(x))^2 + 1}{ax^4 + bx^2 + 1}} = 0$$

**Mathematica:** cpu = 1.108641 (sec), leaf count = 373

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\frac{i\sqrt{\frac{2\#1^2a + \sqrt{b^2 - 4a} + b}{\sqrt{b^2 - 4a}}} \sqrt{\frac{2\#1^2a}{b - \sqrt{b^2 - 4a}}} + 1 F\left(i \sinh^{-1}\left(\sqrt{2}\sqrt{\frac{a}{b + \sqrt{b^2 - 4a}}}\#1\right) \mid \frac{b + \sqrt{b^2 - 4a}}{b - \sqrt{b^2 - 4a}}\right)}{\sqrt{2}\sqrt{\frac{a}{\sqrt{b^2 - 4a} + b}}\sqrt{\#1^4a + \#1^2b + 1}} \right] \right. \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 77

$$\left\{ \int^{y(x)} \frac{1}{\sqrt{-a^4a + -a^2b + 1}} d_a + \int^x -1 \sqrt{\frac{a(y(x))^4 + b(y(x))^2 + 1}{-a^4a + -a^2b + 1}} \frac{1}{\sqrt{a(y(x))^4 + b(y(x))^2 + 1}} d_a + \dots \right.$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.69 ODE No. 69

$$\frac{d}{dx}y(x) - \sqrt{(b_4(y(x))^4 + b_3(y(x))^3 + b_2(y(x))^2 + b_1y(x) + b_0)(a_4x^4 + a_3x^3 + a_2x^2 + a_1x + a_0)}$$

**Mathematica:** cpu = 53.802332 (sec), leaf count = 12750

Failed to compile Latex

**Maple:** cpu = 0.109 (sec), leaf count = 111

$$\left\{ \int^{y(x)} \frac{1}{\sqrt{-a^4b_4 + -a^3b_3 + -a^2b_2 + -ab_1 + b_0}} d_a + \int^x -1 \sqrt{(b_4(y(x))^4 + b_3(y(x))^3 + b_2(y(x))^2 + b_1y(x) + b_0)(a_4x^4 + a_3x^3 + a_2x^2 + a_1x + a_0)} \right.$$

**Sage:** cpu = 0 (sec), leaf count = 0

Maxima was unable to solve this ODE

## 2.70 ODE No. 70

$$\frac{d}{dx}y(x) - \sqrt{\frac{a_4 x^4 + a_3 x^3 + a_2 x^2 + a_1 x + a_0}{b_4 (y(x))^4 + b_3 (y(x))^3 + b_2 (y(x))^2 + b_1 y(x) + b_0}} = 0$$

**Mathematica:** cpu = 159.017193 (sec), leaf count = 23353

Unable to compile Latex

**Maple:** cpu = 0.110 (sec), leaf count = 113

$$\left\{ \int^{y(x)} \sqrt{-a^4 b_4 + -a^3 b_3 + -a^2 b_2 + -a b_1 + b_0} d_a + \int^x -\sqrt{\frac{-a^4 a_4 + -a^3 a_3 + -a^2 a_2 + -a a_1 + a_0}{b_4 (y(x))^4 + b_3 (y(x))^3 + b_2 (y(x))^2 + b_1 y(x) + b_0}} d_x \right.$$

## 2.71 ODE No. 71

$$\frac{d}{dx}y(x) - \sqrt{\frac{b_4 (y(x))^4 + b_3 (y(x))^3 + b_2 (y(x))^2 + b_1 y(x) + b_0}{a_4 x^4 + a_3 x^3 + a_2 x^2 + a_1 x + a_0}} = 0$$

**Mathematica:** cpu = 2.352299 (sec), leaf count = 2237

$$\text{Solve} \left[ \frac{2F \left( \sin^{-1} \left( \sqrt{\frac{(\text{Root}[b_4 \#^4 + b_3 \#^3 + b_2 \#^2 + b_1 \# + b_0 \&, 2] - \text{Root}[b_4 \#^4 + b_3 \#^3 + b_2 \#^2 + b_1 \# + b_0 \&, 4]) (y(x) - \text{Root}[b_4 \#^4 + b_3 \#^3 + b_2 \#^2 + b_1 \# + b_0 \&, 4])}{(\text{Root}[b_4 \#^4 + b_3 \#^3 + b_2 \#^2 + b_1 \# + b_0 \&, 1] - \text{Root}[b_4 \#^4 + b_3 \#^3 + b_2 \#^2 + b_1 \# + b_0 \&, 4]) (y(x) - \text{Root}[b_4 \#^4 + b_3 \#^3 + b_2 \#^2 + b_1 \# + b_0 \&, 4])}} \right)}{\dots} \right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 113

$$\left\{ \int^{y(x)} \frac{1}{\sqrt{-a^4 b_4 + -a^3 b_3 + -a^2 b_2 + -a b_1 + b_0}} d_a + \int^x -1 \sqrt{\frac{b_4 (y(x))^4 + b_3 (y(x))^3 + b_2 (y(x))^2 + b_1 y(x) + b_0}{-a^4 a_4 + -a^3 a_3 + -a^2 a_2 + -a a_1 + a_0}} d_x \right.$$

## 2.72 ODE No. 72

$$\frac{d}{dx}y(x) - R1 \left( x, \sqrt{a_4 x^4 + a_3 x^3 + a_2 x^2 + a_1 x + a_0} \right) R2 \left( y(x), \sqrt{b_4 (y(x))^4 + b_3 (y(x))^3 + b_2 (y(x))^2 + b_1 y(x) + b_0} \right)$$

**Mathematica:** cpu = 0.818104 (sec), leaf count = 87

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \int_1^{\#1} \frac{1}{R2 \left( K[1], \sqrt{b_1 K[1] + b_2 K[1]^2 + b_3 K[1]^3 + b_4 K[1]^4 + b_0} \right)} dK[1] \& \right] \right. \right.$$

**Maple:** cpu = 0.016 (sec), leaf count = 64

$$\left\{ \int R1(x, \sqrt{a_4 x^4 + a_3 x^3 + a_2 x^2 + a_1 x + a_0}) dx - \int^{y(x)} \left( R2\left(-a, \sqrt{-a^4 b_4 + -a^3 b_3 + -a^2 b_2 + -a b_1 + b_0}\right) \right) dy = 0 \right.$$

## 2.73 ODE No. 73

$$\frac{d}{dx} y(x) - \left( \frac{a_3 x^3 + a_2 x^2 + a_1 x + a_0}{a_3 (y(x))^3 + a_2 (y(x))^2 + a_1 y(x) + a_0} \right)^{2/3} = 0$$

**Mathematica:** cpu = 1.032631 (sec), leaf count = 733

$$\text{Solve} \left[ \frac{3(a_0 + y(x)(a_1 + y(x)(a_2 + a_3 y(x))))^{2/3} (y(x) - \text{Root}[\#1^3 a_3 + \#1^2 a_2 + \#1 a_1 + a_0 \&, 1]) F_1\left(\frac{5}{3}; -\frac{y(x) - \text{Root}[\#1^3 a_3 + \#1^2 a_2 + \#1 a_1 + a_0 \&, 2]}{\text{Root}[\#1^3 a_3 + \#1^2 a_2 + \#1 a_1 + a_0 \&, 1]} - \text{Root}[\#1^3 a_3 + \#1^2 a_2 + \#1 a_1 + a_0 \&, 1] \right)}{5 \left( \frac{y(x) - \text{Root}[\#1^3 a_3 + \#1^2 a_2 + \#1 a_1 + a_0 \&, 2]}{\text{Root}[\#1^3 a_3 + \#1^2 a_2 + \#1 a_1 + a_0 \&, 1]} - \text{Root}[\#1^3 a_3 + \#1^2 a_2 + \#1 a_1 + a_0 \&, 1] \right)^{2/3}} \right]$$

**Maple:** cpu = 0.187 (sec), leaf count = 91

$$\left\{ \int^{y(x)} (-a^3 a_3 + -a^2 a_2 + -a a_1 + a_0)^{2/3} d_a + \int^x - \left( \frac{-a^3 a_3 + -a^2 a_2 + -a a_1 + a_0}{a_3 (y(x))^3 + a_2 (y(x))^2 + a_1 y(x) + a_0} \right)^{2/3} (a_3 y(x)^3 + a_2 y(x)^2 + a_1 y(x) + a_0) dy = 0 \right.$$

## 2.74 ODE No. 74

$$\frac{d}{dx} y(x) - f(x) (y(x) - g(x)) \sqrt{(y(x) - a)(y(x) - b)} = 0$$

**Mathematica:** cpu = 2.972878 (sec), leaf count = 39

$$\text{DSolve} \left[ y'(x) - f(x)(y(x) - g(x)) \sqrt{(y(x) - a)(y(x) - b)} = 0, y(x), x \right]$$

**Maple:** cpu = 0.484 (sec), leaf count = 0

could not solve

## 2.75 ODE No. 75

$$\frac{d}{dx}y(x) - e^{x-y(x)} + e^x = 0$$

**Mathematica:** cpu = 0.191024 (sec), leaf count = 20

$$\left\{ \left\{ y(x) \rightarrow \log(1 - e^{c_1 - e^x}) \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 20

$$\left\{ y(x) = -e^x + \ln(-1 + e^{e^x + C_1}) - C_1 \right\}$$

## 2.76 ODE No. 76

$$\frac{d}{dx}y(x) - a \cos(y(x)) + b = 0$$

**Mathematica:** cpu = 0.140018 (sec), leaf count = 116

$$\left\{ \left\{ y(x) \rightarrow 2 \tan^{-1} \left( \frac{a \tanh \left( \frac{1}{2} \left( x \sqrt{(a-b)(a+b)} - c_1 \sqrt{(a-b)(a+b)} \right) \right)}{\sqrt{(a-b)(a+b)}} \right) - \frac{b \tanh \left( \frac{1}{2} \left( x \sqrt{(a-b)(a+b)} \right)}{\sqrt{(a-b)(a+b)}} \right)}{\sqrt{(a-b)(a+b)}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 54

$$\left\{ y(x) = 2 \arctan \left( \frac{\tanh(1/2 C_1 \sqrt{a^2 - b^2} + 1/2 x \sqrt{a^2 - b^2}) \sqrt{a^2 - b^2}}{a + b} \right) \right\}$$

## 2.77 ODE No. 77

$$\frac{d}{dx}y(x) - \cos(ay(x) + bx) = 0$$

**Mathematica:** cpu = 0.318040 (sec), leaf count = 124

$$\left\{ \left\{ y(x) \rightarrow \frac{-2 \tan^{-1} \left( \frac{a \tanh \left( \frac{1}{2} \left( c_1 \sqrt{a^2 - b^2} - x \sqrt{a^2 - b^2} \right) \right)}{\sqrt{a^2 - b^2}} \right) + \frac{b \tanh \left( \frac{1}{2} \left( c_1 \sqrt{a^2 - b^2} - x \sqrt{a^2 - b^2} \right) \right)}{\sqrt{a^2 - b^2}} \right) - bx}{a} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 65

$$\left\{ y(x) = -\frac{1}{a} \left( bx + 2 \arctan \left( \frac{\tanh(1/2 C_1 \sqrt{a^2 - b^2} - 1/2 x \sqrt{a^2 - b^2}) \sqrt{a^2 - b^2}}{a - b} \right) \right) \right\}$$

## 2.78 ODE No. 78

$$\frac{d}{dx}y(x) + a \sin(\alpha y(x) + \beta x) + b = 0$$

**Mathematica:** cpu = 0.860609 (sec), leaf count = 1317

$$\left\{ \left\{ y(x) \rightarrow 2 \tan^{-1} \left( \frac{a^2 \sqrt{-(a\alpha + b\alpha - \beta)(a\alpha - b\alpha + \beta)} \tan\left(\frac{1}{2} \left( \frac{a^2 x \alpha^2}{\sqrt{-(a\alpha + b\alpha - \beta)(a\alpha - b\alpha + \beta)}} - \frac{b^2 x \alpha^2}{\sqrt{-(a\alpha + b\alpha - \beta)(a\alpha - b\alpha + \beta)}} - \frac{a^2 c_1 \alpha^2}{\sqrt{-(a\alpha + b\alpha - \beta)(a\alpha - b\alpha + \beta)}} \right)} \right)} \right. \right.$$

**Maple:** cpu = 0.655 (sec), leaf count = 118

$$\left\{ y(x) = \frac{1}{\alpha} \left( -\beta x + 2 \arctan \left( \frac{\tan(1/2 \_C1 \sqrt{-a^2 \alpha^2 + \alpha^2 b^2 - 2 \alpha b \beta + \beta^2} - 1/2 x \sqrt{-a^2 \alpha^2 + \alpha^2 b^2 - 2 \alpha b \beta + \beta^2})}{b\alpha - \beta} \right) \right) \right.$$

## 2.79 ODE No. 79

$$\frac{d}{dx}y(x) + f(x) \cos(\alpha y(x)) + g(x) \sin(\alpha y(x)) + h(x) = 0$$

**Mathematica:** cpu = 32.093075 (sec), leaf count = 29

$$\text{DSolve}[f(x) \cos(\alpha y(x)) + g(x) \sin(\alpha y(x)) + h(x) + y'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.748 (sec), leaf count = 0

could not solve

## 2.80 ODE No. 80

$$\frac{d}{dx}y(x) + f(x) \sin(y(x)) + \left( 1 - \frac{d}{dx}f(x) \right) \cos(y(x)) - \frac{d}{dx}f(x) - 1 = 0$$

**Mathematica:** cpu = 23.831526 (sec), leaf count = 36

$$\text{DSolve}[(1 - f'(x)) \cos(y(x)) - f'(x) + f(x) \sin(y(x)) + y'(x) - 1 = 0, y(x), x]$$

**Maple:** cpu = 0.811 (sec), leaf count = 41

$$\left\{ y(x) = 2 \arctan \left( \frac{-e^{\int f(x) dx} + \int e^{\int f(x) dx} dx f(x) + \_C1 f(x)}{\_C1 + \int e^{\int f(x) dx} dx} \right) \right\}$$



## 2.81 ODE No. 81

$$\frac{d}{dx}y(x) + 2 \tan(y(x)) \tan(x) - 1 = 0$$

**Mathematica:** cpu = 43.305499 (sec), leaf count = 19

$$\text{DSolve}[y'(x) + 2 \tan(x) \tan(y(x)) - 1 = 0, y(x), x]$$

**Maple:** cpu = 0.827 (sec), leaf count = 78

$$\left\{ -C1 + \tan(x) \frac{1}{\sqrt[4]{\frac{(1+(\tan(y(x)))^2)(1+(\tan(x))^2)}{(\tan(y(x))\tan(x)-1)^2}}} + \frac{\tan(y(x)) + \tan(x)}{2 \tan(y(x)) \tan(x) - 2^2} {}_2F_1\left(\frac{1}{2}, \frac{5}{4}; \frac{3}{2}; -\frac{(\tan(y(x)) + \tan(x))}{(\tan(y(x)) \tan(x) - 2^2)}\right) \right\}$$

## 2.82 ODE No. 82

$$\frac{d}{dx}y(x) - a(1 + (\tan(y(x)))^2) + \tan(y(x)) \tan(x) = 0$$

**Mathematica:** cpu = 49.920839 (sec), leaf count = 27

$$\text{DSolve}[-a(\tan^2(y(x)) + 1) + y'(x) + \tan(x) \tan(y(x)) = 0, y(x), x]$$

**Maple:** cpu = 8.471 (sec), leaf count = 0

could not solve

## 2.83 ODE No. 83

$$\frac{d}{dx}y(x) - \tan(xy(x)) = 0$$

**Mathematica:** cpu = 40.401130 (sec), leaf count = 18

$$\text{DSolve}[y'(x) - \tan(xy(x)) = 0, y(x), x]$$

**Maple:** cpu = 0.297 (sec), leaf count = 44

$$\left\{ y(x) = -i \text{RootOf} \left( -\text{Erf} \left( \frac{(-x + \_Z) \sqrt{2}}{2} \right) \sqrt{\pi} - \text{Erf} \left( \frac{\sqrt{2}(x + \_Z)}{2} \right) \sqrt{\pi} + \sqrt{2} \_C1 \right) \right\}$$

## 2.84 ODE No. 84

$$\frac{d}{dx}y(x) - f(ax + by(x)) = 0$$

**Mathematica:** cpu = 8.757112 (sec), leaf count = 244

$$\text{Solve} \left[ \int_1^{y(x)} \frac{bf(bK[2] + ax) \left( \int_1^x \left( \frac{b^2 f'(aK[1] + bK[2])}{bf(aK[1] + bK[2]) + a} - \frac{b^3 f(aK[1] + bK[2]) f'(aK[1] + bK[2])}{(bf(aK[1] + bK[2]) + a)^2} \right) dK[1] \right) + a \int_1^x \left( \frac{b^2 f'(aK[1] + bK[2])}{bf(aK[1] + bK[2]) + a} \right) dK[1]}{bf(bK[2] + ax) + a} \right]$$

**Maple:** cpu = 0.031 (sec), leaf count = 37

$$\left\{ y(x) = \frac{\text{RootOf} \left( \int^{-Z} (f(-ab)b + a)^{-1} d_{-ab} - x + \_C1 \right) b - ax}{b} \right\}$$

## 2.85 ODE No. 85

$$\frac{d}{dx}y(x) - x^{a-1}(y(x))^{1-b} f \left( \frac{x^a}{a} + \frac{(y(x))^b}{b} \right) = 0$$

**Mathematica:** cpu = 155.676769 (sec), leaf count = 235

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x \left( \frac{K[1]^{a-1} K[2]^{b-1} f' \left( \frac{K[1]^a}{a} + \frac{K[2]^b}{b} \right)}{f \left( \frac{K[1]^a}{a} + \frac{K[2]^b}{b} \right) + 1} - \frac{K[1]^{a-1} K[2]^{b-1} f \left( \frac{K[1]^a}{a} + \frac{K[2]^b}{b} \right) f' \left( \frac{K[1]^a}{a} + \frac{K[2]^b}{b} \right)}{\left( f \left( \frac{K[1]^a}{a} + \frac{K[2]^b}{b} \right) + 1 \right)^2} \right) dK[1] \right)$$

**Maple:** cpu = 0.359 (sec), leaf count = 153

$$\left\{ y(x) = \sqrt[b]{-\frac{1}{a} \left( -\text{RootOf} \left( \int^{-Z} \left( (\sqrt[a]{a})^a f \left( \frac{(\sqrt[a]{a})^a b + (\sqrt[b]{-b + \_a})^b a}{ab} \right) (\sqrt[b]{-b + \_a})^{-b} \_a - (\sqrt[a]{a})^a \right) \right)} \right)}$$

## 2.86 ODE No. 86

$$\frac{d}{dx}y(x) - \frac{y(x) - xf(x^2 + a(y(x))^2)}{x + ay(x)f(x^2 + a(y(x))^2)} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.312 (sec), leaf count = 52

$$\left\{ 1 \arctan \left( x\sqrt{a} \frac{1}{\sqrt{a^2(y(x))^2}} \right) \frac{1}{\sqrt{a}} - \frac{1}{2} \int^{(y(x))^2 + \frac{x^2}{a}} \frac{f(-aa)}{-a} d_a - C1 = 0 \right\}$$

## 2.87 ODE No. 87

$$\frac{d}{dx}y(x) - \frac{y(x)af(x^cy(x)) + cx^a(y(x))^b}{xbf(x^cy(x)) - x^a(y(x))^b} = 0$$

**Mathematica:** cpu = 28.157076 (sec), leaf count = 56

$$\text{DSolve} \left[ y'(x) - \frac{cx^ay(x)^b + ay(x)f(x^cy(x))}{bf(x^cy(x)) - x^ay(x)^b} = 0, y(x), x \right]$$

**Maple:** cpu = 1.154 (sec), leaf count = 0

could not solve

## 2.88 ODE No. 88

$$2 \frac{d}{dx}y(x) - 3(y(x))^2 - 4ay(x) - b - ce^{-2ax} = 0$$

**Mathematica:** cpu = 0.287036 (sec), leaf count = 2831

$$\left\{ \left\{ y(x) \rightarrow - \frac{2 \left( -2^{-\frac{a\sqrt{4a^2-3b-2a^2} + \sqrt{4a^4-3a^2b}}{a^2}} + 3^{\frac{a\sqrt{4a^2-3b-2a^2} - \sqrt{4a^4-3a^2b}}{4a^2}} a^{-\frac{a\sqrt{4a^2-3b-2a^2} + \sqrt{4a^4-3a^2b}}{2a^2}} + 1 b^{\frac{a\sqrt{4a^2-3b-2a^2}}{4a^2}} \right)}{\dots} \right. \right.$$

**Maple:** cpu = 0.156 (sec), leaf count = 420

$$\left\{ y(x) = \left( -\frac{\sqrt{3}C1}{3} \sqrt{c} Y_{-\frac{1}{2a}(\sqrt{4a^2-3b-2a^2})} \left( \frac{\sqrt{3}e^{-ax}}{2a} \sqrt{c} \right) \left( Y_{-\frac{1}{2a}\sqrt{4a^2-3b}} \left( \frac{\sqrt{3}e^{-ax}}{2a} \sqrt{c} \right) - C1 + J_{-\frac{1}{2a}\sqrt{4a^2-3b}} \right) \right) \right.$$

## 2.89 ODE No. 89

$$x \frac{d}{dx} y(x) - \sqrt{a^2 - x^2} = 0$$

**Mathematica:** cpu = 0.030504 (sec), leaf count = 48

$$\left\{ \left\{ y(x) \rightarrow \sqrt{a^2 - x^2} - a \log \left( a\sqrt{a^2 - x^2} + a^2 \right) + a \log(x) + c_1 \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 56

$$\left\{ y(x) = \sqrt{a^2 - x^2} - a^2 \ln \left( \frac{1}{x} \left( 2a^2 + 2\sqrt{a^2}\sqrt{a^2 - x^2} \right) \right) \frac{1}{\sqrt{a^2}} + \_C1 \right\}$$

## 2.90 ODE No. 90

$$x \frac{d}{dx} y(x) + y(x) - x \sin(x) = 0$$

**Mathematica:** cpu = 0.012502 (sec), leaf count = 24

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{x} + \frac{\sin(x) - x \cos(x)}{x} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 17

$$\left\{ y(x) = \frac{\sin(x) - \cos(x)x + \_C1}{x} \right\}$$

## 2.91 ODE No. 91

$$x \frac{d}{dx} y(x) - y(x) - \frac{x}{\ln(x)} = 0$$

**Mathematica:** cpu = 0.005501 (sec), leaf count = 15

$$\left\{ \left\{ y(x) \rightarrow c_1 x + x \log(\log(x)) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 11

$$\{ y(x) = (\ln(\ln(x)) + \_C1) x \}$$

## 2.92 ODE No. 92

$$x \frac{d}{dx} y(x) - y(x) - x^2 \sin(x) = 0$$

**Mathematica:** cpu = 0.011501 (sec), leaf count = 15

$$\{ \{ y(x) \rightarrow c_1 x - x \cos(x) \} \}$$

**Maple:** cpu = 0.0 (sec), leaf count = 13

$$\{ y(x) = -\cos(x) x + x\_C1 \}$$

## 2.93 ODE No. 93

$$x \frac{d}{dx} y(x) - y(x) - \frac{x \cos(\ln(\ln(x)))}{\ln(x)} = 0$$

**Mathematica:** cpu = 0.024503 (sec), leaf count = 16

$$\{ \{ y(x) \rightarrow c_1 x + x \sin(\log(\log(x))) \} \}$$

**Maple:** cpu = 0.0 (sec), leaf count = 14

$$\{ y(x) = x \sin(\ln(\ln(x))) + x\_C1 \}$$

## 2.94 ODE No. 94

$$x \frac{d}{dx} y(x) + ay(x) + bx^n = 0$$

**Mathematica:** cpu = 0.013502 (sec), leaf count = 25

$$\left\{ \left\{ y(x) \rightarrow c_1 x^{-a} - \frac{bx^n}{a+n} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 23

$$\left\{ y(x) = -\frac{bx^n}{n+a} + x^{-a} \_C1 \right\}$$

## 2.95 ODE No. 95

$$x \frac{d}{dx} y(x) + (y(x))^2 + x^2 = 0$$

**Mathematica:** cpu = 0.014502 (sec), leaf count = 32

$$\left\{ \left\{ y(x) \rightarrow \frac{x(-c_1 J_1(x) - Y_1(x))}{c_1 J_0(x) + Y_0(x)} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 40

$$\left\{ y(x) = -\frac{-C1 x Y_1(x)}{-C1 Y_0(x) + J_0(x)} - \frac{J_1(x)x}{-C1 Y_0(x) + J_0(x)} \right\}$$

## 2.96 ODE No. 96

$$x \frac{d}{dx} y(x) - (y(x))^2 + 1 = 0$$

**Mathematica:** cpu = 0.022003 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow \frac{1 - e^{2c_1 x^2}}{e^{2c_1 x^2} + 1} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 11

$$\{y(x) = -\tanh(\ln(x) + \_C1)\}$$

## 2.97 ODE No. 97

$$x \frac{d}{dx} y(x) + a(y(x))^2 - y(x) + bx^2 = 0$$

**Mathematica:** cpu = 0.024503 (sec), leaf count = 46

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{bx} \tan\left(\sqrt{a}\sqrt{bx} - \sqrt{a}\sqrt{bc_1}\right)}{\sqrt{a}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 31

$$\left\{ y(x) = -\frac{x}{a} \tan\left(\_C1 \sqrt{ab} + x\sqrt{ab}\right) \sqrt{ab} \right\}$$

**2.98 ODE No. 98**

$$x \frac{d}{dx} y(x) + a(y(x))^2 - by(x) + cx^{2b} = 0$$

**Mathematica:** cpu = 0.022503 (sec), leaf count = 442

$$\left\{ \left\{ y(x) \rightarrow - \frac{\sqrt{-a}\sqrt{-cx^b} \left( \frac{\sqrt{\frac{2}{\pi}} c_1 \sin\left(\frac{\sqrt{-a}\sqrt{-cx^b}}{b}\right)}{\sqrt{\sqrt{-a}\sqrt{-cx^b}}} - \frac{2\sqrt{\frac{2}{\pi}} \cos\left(\frac{\sqrt{-a}\sqrt{-cx^b}}{b}\right)}{\sqrt{\sqrt{-a}\sqrt{-cx^b}}} - \frac{\sqrt{\frac{2}{\pi}} c_1 \left( -\sin\left(\frac{\sqrt{-a}\sqrt{-cx^b}}{b}\right) - \frac{\sqrt{-ab}\sqrt{-cx^{-b}} \cos\left(\frac{\sqrt{-a}\sqrt{-cx^b}}{b}\right)}{\sqrt{\sqrt{-a}\sqrt{-cx^b}}} \right)}{\sqrt{\sqrt{-a}\sqrt{-cx^b}}} \right)}{2a \left( \frac{\sqrt{\frac{2}{\pi}} \sin\left(\frac{\sqrt{-a}\sqrt{-cx^b}}{b}\right)}{\sqrt{\sqrt{-a}\sqrt{-cx^b}}} + \frac{\sqrt{\frac{2}{\pi}} c_1 \cos\left(\frac{\sqrt{-a}\sqrt{-cx^b}}{b}\right)}{\sqrt{\sqrt{-a}\sqrt{-cx^b}}} \right)} \right. \right.$$

**Maple:** cpu = 0.046 (sec), leaf count = 38

$$\left\{ y(x) = -\frac{1}{x^{-b}} \tan\left(\frac{1}{b}(x^b \sqrt{a}\sqrt{c} + C_1 b)\right) \sqrt{c} \frac{1}{\sqrt{a}} \right\}$$

**2.99 ODE No. 99**

$$x \frac{d}{dx} y(x) + a(y(x))^2 - by(x) - cx^\beta = 0$$

**Mathematica:** cpu = 0.017002 (sec), leaf count = 244

$$\left\{ \left\{ y(x) \rightarrow - \frac{\sqrt{-a}\sqrt{cx^{\beta/2}} \left( -2J_{\frac{b}{\beta}-1}\left(\frac{2\sqrt{-a}\sqrt{cx^{\beta/2}}}{\beta}\right) + c_1 J_{1-\frac{b}{\beta}}\left(\frac{2\sqrt{-a}\sqrt{cx^{\beta/2}}}{\beta}\right) - c_1 J_{-\frac{b+\beta}{\beta}}\left(\frac{2\sqrt{-a}\sqrt{cx^{\beta/2}}}{\beta}\right) \right) - bc_1 J_{-\frac{b+\beta}{\beta}}\left(\frac{2\sqrt{-a}\sqrt{cx^{\beta/2}}}{\beta}\right)}{2a \left( J_{\frac{b}{\beta}}\left(\frac{2\sqrt{-a}\sqrt{cx^{\beta/2}}}{\beta}\right) + c_1 J_{-\frac{b}{\beta}}\left(\frac{2\sqrt{-a}\sqrt{cx^{\beta/2}}}{\beta}\right) \right)} \right. \right.$$

**Maple:** cpu = 0.078 (sec), leaf count = 237

$$\left\{ y(x) = -\frac{C_1}{a} \sqrt{-acx}^{\frac{\beta}{2}} Y_{\frac{b+\beta}{\beta}}\left(2 \frac{\sqrt{-acx}^{\beta/2}}{\beta}\right) \left( Y_{\frac{b}{\beta}}\left(2 \frac{\sqrt{-acx}^{\beta/2}}{\beta}\right) - C_1 + J_{\frac{b}{\beta}}\left(2 \frac{\sqrt{-acx}^{\beta/2}}{\beta}\right) \right)^{-1} - \frac{1}{a} \left( J_{-\frac{b+\beta}{\beta}}\left(\frac{2\sqrt{-a}\sqrt{cx^{\beta/2}}}{\beta}\right) \right) \right\}$$

**2.100 ODE No. 100**

$$x \frac{d}{dx} y(x) + x(y(x))^2 + a = 0$$

**Mathematica:** cpu = 0.007501 (sec), leaf count = 157

$$\left\{ \left\{ y(x) \rightarrow -\frac{c_1 J_1(2i\sqrt{-a}\sqrt{x}) + i\sqrt{-a}\sqrt{x}(c_1 J_0(2i\sqrt{-a}\sqrt{x}) - c_1 J_2(2i\sqrt{-a}\sqrt{x}) - 2J_0(2i\sqrt{-a}\sqrt{x}))}{2x (J_1(2i\sqrt{-a}\sqrt{x}) - c_1 J_1(2i\sqrt{-a}\sqrt{x}))} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 59

$$\left\{ y(x) = 1\sqrt{a}(J_0(2\sqrt{a}\sqrt{x}) - C1 + Y_0(2\sqrt{a}\sqrt{x})) \frac{1}{\sqrt{x}} (-C1 J_1(2\sqrt{a}\sqrt{x}) + Y_1(2\sqrt{a}\sqrt{x}))^{-1} \right\}$$

**2.101 ODE No. 101**

$$x \frac{d}{dx} y(x) + x(y(x))^2 - y(x) = 0$$

**Mathematica:** cpu = 0.008001 (sec), leaf count = 18

$$\left\{ \left\{ y(x) \rightarrow \frac{2x}{2c_1 + x^2} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 16

$$\left\{ y(x) = 2 \frac{x}{x^2 + 2 - C1} \right\}$$

**2.102 ODE No. 102**

$$x \frac{d}{dx} y(x) + x(y(x))^2 - y(x) - ax^3 = 0$$

**Mathematica:** cpu = 0.018502 (sec), leaf count = 36

$$\left\{ \left\{ y(x) \rightarrow \sqrt{a}x \tanh \left( \frac{1}{2} (2\sqrt{a}c_1 + \sqrt{a}x^2) \right) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 24

$$\left\{ y(x) = \tanh \left( \frac{x^2}{2} \sqrt{a} + -C1 \sqrt{a} \right) x \sqrt{a} \right\}$$



### 2.103 ODE No. 103

$$x \frac{d}{dx} y(x) + x(y(x))^2 - (2x^2 + 1)y(x) - x^3 = 0$$

**Mathematica:** cpu = 0.097012 (sec), leaf count = 90

$$\left\{ \left\{ y(x) \rightarrow \frac{x \left( e^{2\sqrt{2}c_1} - \sqrt{2}e^{2\sqrt{2}c_1} + e^{\sqrt{2}x^2} + \sqrt{2}e^{\sqrt{2}x^2} \right)}{e^{2\sqrt{2}c_1} + e^{\sqrt{2}x^2}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 29

$$\left\{ y(x) = \frac{\sqrt{2}x}{2} \left( \sqrt{2} + 2 \tanh \left( 1/2 (x^2 + 2\_C1) \sqrt{2} \right) \right) \right\}$$

### 2.104 ODE No. 104

$$x \frac{d}{dx} y(x) + ax(y(x))^2 + 2y(x) + bx = 0$$

**Mathematica:** cpu = 0.015502 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{\frac{b}{a}} \tan \left( ax \sqrt{\frac{b}{a}} - c_1 \right) - \frac{1}{ax} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 63

$$\left\{ y(x) = -\frac{1}{a} \left( -\frac{1}{x} \left( i\sqrt{a}\sqrt{bx} - 1 \right) + 1e^{-2ix\sqrt{a}\sqrt{b}} \left( -C1 - \frac{i}{2} e^{-2ix\sqrt{a}\sqrt{b}} \frac{1}{\sqrt{a}} \frac{1}{\sqrt{b}} \right)^{-1} \right) \right\}$$

### 2.105 ODE No. 105

$$x \frac{d}{dx} y(x) + ax(y(x))^2 + by(x) + cx + d = 0$$

**Mathematica:** cpu = 0.187024 (sec), leaf count = 473

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 \left( i\sqrt{a}e^{-i\sqrt{a}\sqrt{cx}} (b(-\sqrt{c}) - i\sqrt{ad}) U \left( 1 - \frac{-\sqrt{cb} - i\sqrt{ad}}{2\sqrt{c}}, b + 1, 2i\sqrt{a}\sqrt{cx} \right) - i\sqrt{a}\sqrt{c}e^{-i\sqrt{a}\sqrt{cx}} U \left( -\frac{-\sqrt{cb} - i\sqrt{ad}}{2\sqrt{c}} \right) \right)}{a \left( c_1 e^{-i\sqrt{a}\sqrt{cx}} U \left( -\frac{-\sqrt{cb} - i\sqrt{ad}}{2\sqrt{c}} \right) \right)} \right\} \right\}$$

**Maple:** cpu = 0.202 (sec), leaf count = 844

$$\left\{ y(x) = -4c^2 \left( -1/4 \_C1 \left( a^3 c^2 d^2 + a^2 b^2 c^3 - 2(-ac)^{3/2} abcd - 2(-ac)^{5/2} bd \right) U \left( 1/2 \frac{(-ac)^{3/2} d + (2\sqrt{-ac} x)^{3/2}}{\dots} \right) \right) \right.$$

## 2.106 ODE No. 106

$$x \frac{d}{dx} y(x) + x^a (y(x))^2 + 1/2 (a - b) y(x) + x^b = 0$$

**Mathematica:** cpu = 0.036505 (sec), leaf count = 40

$$\left\{ \left\{ y(x) \rightarrow -x^{\frac{b-a}{2}} \tan \left( \frac{2x^{\frac{a+b}{2}}}{a+b} - c_1 \right) \right\} \right\}$$

**Maple:** cpu = 0.046 (sec), leaf count = 42

$$\left\{ y(x) = -1 \tan \left( \frac{1}{a+b} (-C1 a + -C1 b + 2x^{a/2+b/2}) \right) \left( x^{\frac{a}{2}-\frac{b}{2}} \right)^{-1} \right\}$$

## 2.107 ODE No. 107

$$x \frac{d}{dx} y(x) + ax^\alpha (y(x))^2 + by(x) - cx^\beta = 0$$

**Mathematica:** cpu = 0.258033 (sec), leaf count = 1415

$$\left\{ \left\{ y(x) \rightarrow \frac{x^{1-\alpha} \left( (-1)^{\frac{\alpha-b}{\alpha+\beta}} a^{\frac{\alpha-b}{\alpha+\beta} + \frac{1}{2}} \left( \frac{b}{\alpha+\beta} - \frac{\alpha}{\alpha+\beta} \right) (\alpha + \beta)^{\frac{\alpha}{\alpha+\beta} - \frac{b}{\alpha+\beta} + 1} (\alpha^2 + 2\beta\alpha + \beta^2)^{-\frac{\alpha-b}{\alpha+\beta}} \left( \frac{\alpha-b}{\alpha+\beta} + \frac{1}{2} \left( \frac{b}{\alpha+\beta} - \frac{\alpha}{\alpha+\beta} \right) \right) \right)}{\dots} \right\} \right.$$

**Maple:** cpu = 0.156 (sec), leaf count = 176

$$\left\{ y(x) = -\frac{x^{1-\alpha}}{ax} \left( Y_{\frac{b+\beta}{\alpha+\beta}} \left( 2 \frac{\sqrt{-ac} x^{\alpha/2+\beta/2}}{\alpha+\beta} \right) - C1 + J_{\frac{b+\beta}{\alpha+\beta}} \left( 2 \frac{\sqrt{-ac} x^{\alpha/2+\beta/2}}{\alpha+\beta} \right) \right) x^{\frac{\alpha}{2} + \frac{\beta}{2}} \sqrt{-ac} \left( Y_{-\frac{\alpha-b}{\alpha+\beta}} \left( 2 \frac{\sqrt{-ac} x^{\alpha/2+\beta/2}}{\alpha+\beta} \right) \right) \right.$$

**2.108 ODE No. 108**

$$x \frac{d}{dx} y(x) - (y(x))^2 \ln(x) + y(x) = 0$$

**Mathematica:** cpu = 0.010501 (sec), leaf count = 15

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{c_1 x + \log(x) + 1} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 13

$$\{y(x) = (1 + \_C1 x + \ln(x))^{-1}\}$$

**2.109 ODE No. 109**

$$x \frac{d}{dx} y(x) - y(x) (2 y(x) \ln(x) - 1) = 0$$

**Mathematica:** cpu = 0.011001 (sec), leaf count = 17

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{c_1 x + 2 \log(x) + 2} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 15

$$\{y(x) = (2 + \_C1 x + 2 \ln(x))^{-1}\}$$

**2.110 ODE No. 110**

$$x \frac{d}{dx} y(x) + f(x) ((y(x))^2 - x^2) = 0$$

**Mathematica:** cpu = 20.763637 (sec), leaf count = 26

$$\text{DSolve}[f(x) (y(x)^2 - x^2) + xy'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.093 (sec), leaf count = 0

could not solve

### 2.111 ODE No. 111

$$x \frac{d}{dx} y(x) + (y(x))^3 + 3x(y(x))^2 = 0$$

Mathematica: cpu = 0.272535 (sec), leaf count = 55

$$\text{Solve} \left[ -3x = \frac{2e^{\frac{1}{2} \left( \frac{1}{y(x)} - 3x \right)^2}}{2c_1 + \sqrt{2\pi} \operatorname{erfi} \left( \frac{\frac{1}{y(x)} - 3x}{\sqrt{2}} \right)}, y(x) \right]$$

Maple: cpu = 0.125 (sec), leaf count = 54

$$\left\{ -C1 - \frac{i}{3} e^{\frac{(3xy(x)-1)^2}{2(y(x))^2}} + \frac{\sqrt{\pi}\sqrt{2}}{2} \operatorname{Erf} \left( \frac{(-i + 3iy(x)x)\sqrt{2}}{2y(x)} \right) = 0 \right\}$$

### 2.112 ODE No. 112

$$x \frac{d}{dx} y(x) - \sqrt{(y(x))^2 + x^2} - y(x) = 0$$

Mathematica: cpu = 0.021503 (sec), leaf count = 13

$$\{\{y(x) \rightarrow x \sinh(c_1 + \log(x))\}\}$$

Maple: cpu = 0.031 (sec), leaf count = 27

$$\left\{ \frac{1}{x^2} \sqrt{(y(x))^2 + x^2} + \frac{y(x)}{x^2} - C1 = 0 \right\}$$

### 2.113 ODE No. 113

$$x \frac{d}{dx} y(x) + a \sqrt{(y(x))^2 + x^2} - y(x) = 0$$

Mathematica: cpu = 0.022503 (sec), leaf count = 16

$$\{\{y(x) \rightarrow x \sinh(c_1 - a \log(x))\}\}$$

Maple: cpu = 0.015 (sec), leaf count = 33

$$\left\{ \frac{x^a}{x} \sqrt{(y(x))^2 + x^2} + \frac{x^a y(x)}{x} - C1 = 0 \right\}$$

**2.114 ODE No. 114**

$$x \frac{d}{dx} y(x) - x \sqrt{(y(x))^2 + x^2} - y(x) = 0$$

**Mathematica:** cpu = 0.019502 (sec), leaf count = 12

$$\{ \{ y(x) \rightarrow x \sinh(c_1 + x) \} \}$$

**Maple:** cpu = 0.936 (sec), leaf count = 28

$$\left\{ \ln \left( \sqrt{(y(x))^2 + x^2} + y(x) \right) - x - \ln(x) - \_C1 = 0 \right\}$$

**2.115 ODE No. 115**

$$x \frac{d}{dx} y(x) - x(y(x) - x) \sqrt{(y(x))^2 + x^2} - y(x) = 0$$

**Mathematica:** cpu = 0.123016 (sec), leaf count = 99

$$\left\{ \left\{ y(x) \rightarrow \frac{x \left( -2e^{\sqrt{2}c_1 + \frac{x^2}{\sqrt{2}}} + e^{2\sqrt{2}c_1 + \sqrt{2}x^2} - 1 \right)}{2e^{\sqrt{2}c_1 + \frac{x^2}{\sqrt{2}}} + e^{2\sqrt{2}c_1 + \sqrt{2}x^2} - 1} \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 49

$$\left\{ \ln \left( 2 \frac{x \left( \sqrt{2} (y(x))^2 + 2x^2 + y(x) + x \right)}{y(x) - x} \right) + \frac{\sqrt{2}x^2}{2} - \ln(x) - \_C1 = 0 \right\}$$

**2.116 ODE No. 116**

$$x \frac{d}{dx} y(x) - x \sqrt{((y(x))^2 - x^2) ((y(x))^2 - 4x^2)} - y(x) = 0$$

**Mathematica:** cpu = 0.410552 (sec), leaf count = 143

$$\text{Solve} \left[ \frac{2 \left( \frac{y(x)}{x} - 2 \right)^{3/2} \sqrt{-\frac{4}{\frac{y(x)}{x} - 2} - 1} \sqrt{-\frac{3}{\frac{y(x)}{x} - 2} - 1} \sqrt{\frac{1}{\frac{y(x)}{x} - 2} + 1} F \left( \sin^{-1} \left( \frac{\sqrt{-1 - \frac{3}{\frac{y(x)}{x} - 2}}}{\sqrt{2}} \right) \middle| -8 \right)}{\sqrt{\frac{y(x)}{x} - 1} \sqrt{\frac{y(x)}{x} + 1} \sqrt{\frac{y(x)}{x} + 2}} = c_1 + \frac{x^2}{2} \right]$$

**Maple:** cpu = 0.156 (sec), leaf count = 144

$$\left\{ \int_{-b}^x 1 \left( -a \sqrt{4 - a^4 - 5 - a^2 (y(x))^2 + (y(x))^4} + y(x) \right) \frac{1}{\sqrt{4 - a^4 - 5 - a^2 (y(x))^2 + (y(x))^4}} d_a + \int^{y(x)} \right.$$

### 2.117 ODE No. 117

$$x \frac{d}{dx} y(x) - x e^{\frac{y(x)}{x}} - y(x) - x = 0$$

**Mathematica:** cpu = 0.024503 (sec), leaf count = 21

$$\left\{ \left\{ y(x) \rightarrow -x \log \left( \frac{e^{-c_1}}{x} - 1 \right) \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 20

$$\left\{ y(x) = \left( \ln \left( -\frac{x}{-1 + x e^{-C_1}} \right) + -C_1 \right) x \right\}$$

### 2.118 ODE No. 118

$$x \frac{d}{dx} y(x) - y(x) \ln(y(x)) = 0$$

**Mathematica:** cpu = 0.010501 (sec), leaf count = 13

$$\left\{ \left\{ y(x) \rightarrow e^{e^{c_1} x} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 8

$$\left\{ y(x) = e^{-C_1 x} \right\}$$

### 2.119 ODE No. 119

$$x \frac{d}{dx} y(x) - y(x) (\ln(xy(x)) - 1) = 0$$

**Mathematica:** cpu = 0.029504 (sec), leaf count = 17

$$\left\{ \left\{ y(x) \rightarrow \frac{e^{e^{c_1} x}}{x} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 14

$$\left\{ y(x) = \frac{1}{x} e^{-\frac{x}{C_1}} \right\}$$

**2.120 ODE No. 120**

$$x \frac{d}{dx} y(x) - y(x) \left( x \ln \left( \frac{x^2}{y(x)} \right) + 2 \right) = 0$$

**Mathematica:** cpu = 0.048506 (sec), leaf count = 20

$$\left\{ \left\{ y(x) \rightarrow x^2 e^{-2c_1 e^{-x}} \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 17

$$\left\{ y(x) = x^2 \left( e^{-\frac{C1}{e^x}} \right)^{-1} \right\}$$

**2.121 ODE No. 121**

$$x \frac{d}{dx} y(x) - \sin(x - y(x)) = 0$$

**Mathematica:** cpu = 3.054888 (sec), leaf count = 22

$$\text{DSolve}[xy'(x) - \sin(x - y(x)) = 0, y(x), x]$$

**Maple:** cpu = 0.982 (sec), leaf count = 0

could not solve

**2.122 ODE No. 122**

$$x \frac{d}{dx} y(x) + (\sin(y(x)) - 3x^2 \cos(y(x))) \cos(y(x)) = 0$$

**Mathematica:** cpu = 0.071509 (sec), leaf count = 21

$$\left\{ \left\{ y(x) \rightarrow \tan^{-1} \left( \frac{c_1 + 2x^3}{2x} \right) \right\} \right\}$$

**Maple:** cpu = 0.297 (sec), leaf count = 16

$$\left\{ y(x) = \arctan \left( \frac{x^3 + 2\_C1}{x} \right) \right\}$$

**2.123 ODE No. 123**

$$x \frac{d}{dx} y(x) - x \sin \left( \frac{y(x)}{x} \right) - y(x) = 0$$

**Mathematica:** cpu = 0.058507 (sec), leaf count = 19

$$\left\{ \left\{ y(x) \rightarrow 2x \cot^{-1} \left( \frac{e^{-c_1}}{x} \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 44

$$\left\{ y(x) = \arctan \left( 2 \frac{-C1 x}{-C1^2 x^2 + 1}, -\frac{C1^2 x^2 - 1}{-C1^2 x^2 + 1} \right) x \right\}$$

**2.124 ODE No. 124**

$$x \frac{d}{dx} y(x) + x \cos \left( \frac{y(x)}{x} \right) - y(x) + x = 0$$

**Mathematica:** cpu = 0.027003 (sec), leaf count = 16

$$\left\{ \left\{ y(x) \rightarrow 2x \tan^{-1} (c_1 - \log(x)) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 12

$$\{ y(x) = -2 \arctan (\ln (x) + \_C1) x \}$$

**2.125 ODE No. 125**

$$x \frac{d}{dx} y(x) + x \tan \left( \frac{y(x)}{x} \right) - y(x) = 0$$

**Mathematica:** cpu = 0.038505 (sec), leaf count = 16

$$\left\{ \left\{ y(x) \rightarrow x \sin^{-1} \left( \frac{e^{c_1}}{x} \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 14

$$\left\{ y(x) = \arcsin \left( \frac{1}{-C1 x} \right) x \right\}$$



**2.126 ODE No. 126**

$$x \frac{d}{dx} y(x) - y(x) f(xy(x)) = 0$$

**Mathematica:** cpu = 15.028909 (sec), leaf count = 112

$$\text{Solve} \left[ \int_1^{y(x)} \left( \frac{1}{K[2](-f(xK[2]) - 1)} - \int_1^x \left( \frac{f'(K[1]K[2])}{f(K[1]K[2]) + 1} - \frac{f(K[1]K[2])f'(K[1]K[2])}{(f(K[1]K[2]) + 1)^2} \right) dK[1] \right) dK[2] \right]$$

**Maple:** cpu = 0.016 (sec), leaf count = 29

$$\left\{ y(x) = \frac{1}{x} \text{RootOf} \left( -\ln(x) + \_C1 + \int^{-Z} \frac{1}{-a(1+f(-a))} d\_a \right) \right\}$$

**2.127 ODE No. 127**

$$x \frac{d}{dx} y(x) - y(x) f(x^a(y(x))^b) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.078 (sec), leaf count = 39

$$\left\{ \int_{-b}^{y(x)} \frac{1}{-a(f(x^a\_a^b)b+a)} d\_a - \frac{\ln(x)}{b} - \_C1 = 0 \right\}$$

**2.128 ODE No. 128**

$$x \frac{d}{dx} y(x) + ay(x) - f(x) g(x^a y(x)) = 0$$

**Mathematica:** cpu = 5.142653 (sec), leaf count = 39

$$\text{Solve} \left[ \int_1^{x^a y(x)} \frac{1}{g(K[1])} dK[1] = \int_1^x K[2]^{a-1} f(K[2]) dK[2] + c_1, y(x) \right]$$

**Maple:** cpu = 0.203 (sec), leaf count = 33

$$\left\{ y(x) = \frac{\text{RootOf} \left( -\int x^{a-1} f(x) dx + \int^{-Z} (g(-a))^{-1} d\_a + \_C1 \right)}{x^a} \right\}$$

**2.129 ODE No. 129**

$$(1+x) \frac{d}{dx} y(x) + y(x)(y(x)-x) = 0$$

**Mathematica:** cpu = 0.027504 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow -\frac{e^{x+1}}{-ec_1x - ec_1 - x\text{Ei}(x+1) - \text{Ei}(x+1) + e^{x+1}} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 41

$$\left\{ y(x) = -\frac{e^x}{e^{-1}\text{Ei}(1, -1-x)x + e^{-1}\text{Ei}(1, -1-x) - \_C1x + e^x - \_C1} \right\}$$

**2.130 ODE No. 130**

$$2x \frac{d}{dx} y(x) - y(x) - 2x^3 = 0$$

**Mathematica:** cpu = 0.005501 (sec), leaf count = 21

$$\left\{ \left\{ y(x) \rightarrow c_1\sqrt{x} + \frac{2x^3}{5} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 15

$$\left\{ y(x) = \frac{2x^3}{5} + \sqrt{x}\_C1 \right\}$$

**2.131 ODE No. 131**

$$(2x+1) \frac{d}{dx} y(x) - 4e^{-y(x)} + 2 = 0$$

**Mathematica:** cpu = 0.018002 (sec), leaf count = 21

$$\left\{ \left\{ y(x) \rightarrow \log \left( 2 - \frac{e^{c_1}}{2x+1} \right) \right\} \right\}$$

**Maple:** cpu = 0.141 (sec), leaf count = 34

$$\left\{ y(x) = -\ln \left( \frac{2x+1}{-1+4xe^{2-C1} + 2e^{2-C1}} \right) - 2\_C1 \right\}$$

### 2.132 ODE No. 132

$$3x \frac{d}{dx} y(x) - 3x \ln(x) (y(x))^4 - y(x) = 0$$

**Mathematica:** cpu = 0.011001 (sec), leaf count = 115

$$\left\{ \left\{ y(x) \rightarrow \frac{(-2)^{2/3} \sqrt[3]{x}}{\sqrt[3]{4c_1 + 3x^2 - 6x^2 \log(x)}} \right\}, \left\{ y(x) \rightarrow \frac{2^{2/3} \sqrt[3]{x}}{\sqrt[3]{4c_1 + 3x^2 - 6x^2 \log(x)}} \right\}, \left\{ y(x) \rightarrow -\frac{\sqrt[3]{-12^2}}{\sqrt[3]{4c_1 + 3x^2 - 6x^2 \log(x)}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 234

$$\left\{ y(x) = \frac{1}{6x^2 \ln(x) - 3x^2 - 4\_C1} \sqrt[3]{-4x(6x^2 \ln(x) - 3x^2 - 4\_C1)^2}, y(x) = -\frac{1}{12x^2 \ln(x) - 6x^2 - 8\_C1} \right\}$$

### 2.133 ODE No. 133

$$x^2 \frac{d}{dx} y(x) + y(x) - x = 0$$

**Mathematica:** cpu = 0.007001 (sec), leaf count = 27

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{1}{x}} - e^{\frac{1}{x}} \text{Ei}\left(-\frac{1}{x}\right) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 16

$$\left\{ y(x) = (\text{Ei}(1, x^{-1}) + \_C1) e^{x^{-1}} \right\}$$

### 2.134 ODE No. 134

$$x^2 \frac{d}{dx} y(x) - y(x) + x^2 e^{x-x^{-1}} = 0$$

**Mathematica:** cpu = 0.010501 (sec), leaf count = 27

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-1/x} - e^{x-1/x} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 17

$$\left\{ y(x) = (-e^x + \_C1) e^{-x^{-1}} \right\}$$

**2.135 ODE No. 135**

$$x^2 \frac{d}{dx} y(x) - (x - 1) y(x) = 0$$

**Mathematica:** cpu = 0.006501 (sec), leaf count = 14

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{1}{x} x} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 11

$$\left\{ y(x) = \_C1 x e^{x^{-1}} \right\}$$

**2.136 ODE No. 136**

$$x^2 \frac{d}{dx} y(x) + (y(x))^2 + xy(x) + x^2 = 0$$

**Mathematica:** cpu = 0.012502 (sec), leaf count = 28

$$\left\{ \left\{ y(x) \rightarrow \frac{-c_1 x - x + x \log(x)}{c_1 - \log(x)} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 18

$$\left\{ y(x) = -\frac{x(\ln(x) + \_C1 - 1)}{\ln(x) + \_C1} \right\}$$

**2.137 ODE No. 137**

$$x^2 \frac{d}{dx} y(x) - (y(x))^2 - xy(x) = 0$$

**Mathematica:** cpu = 0.008501 (sec), leaf count = 16

$$\left\{ \left\{ y(x) \rightarrow \frac{x}{c_1 - \log(x)} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 15

$$\left\{ y(x) = -\frac{x}{\ln(x) - \_C1} \right\}$$

### 2.138 ODE No. 138

$$x^2 \frac{d}{dx} y(x) - (y(x))^2 - xy(x) - x^2 = 0$$

**Mathematica:** cpu = 0.013502 (sec), leaf count = 13

$$\{ \{ y(x) \rightarrow x \tan(c_1 + \log(x)) \} \}$$

**Maple:** cpu = 0.031 (sec), leaf count = 11

$$\{ y(x) = \tan(\ln(x) + \_C1) x \}$$

### 2.139 ODE No. 139

$$x^2 \left( \frac{d}{dx} y(x) + (y(x))^2 \right) + ax^k - b(b-1) = 0$$

**Mathematica:** cpu = 0.131017 (sec), leaf count = 821

$$\left\{ \left\{ y(x) \rightarrow - \frac{a^{\frac{b}{k} + \frac{1}{2} \left( \frac{1}{k} - \frac{2b}{k} \right)} \left( \frac{b}{k} + \frac{1}{2} \left( \frac{1}{k} - \frac{2b}{k} \right) \right) x^{k-1} (x^k)^{\frac{b}{k} + \frac{1}{2} \left( \frac{1}{k} - \frac{2b}{k} \right) - 1} J_{\frac{2b-1}{k}} \left( \frac{2\sqrt{a}\sqrt{x^k}}{k} \right) \Gamma \left( \frac{2b}{k} - \frac{1}{k} + 1 \right) k^{1-\frac{1}{k}} + \frac{1}{2} a}{\dots} \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 296

$$\left\{ y(x) = - \frac{C1}{x} \sqrt{ax^{\frac{k}{2}}} Y_{\frac{1}{k}} \left( \sqrt{(-1+2b)^2 + k} \right) \left( 2 \frac{\sqrt{ax^{k/2}}}{k} \right) \left( Y_{\frac{1}{k}} \sqrt{(-1+2b)^2} \left( 2 \frac{\sqrt{ax^{k/2}}}{k} \right) - C1 + J_{\frac{1}{k}} \sqrt{(-1+2b)^2} \left( 2 \frac{\sqrt{ax^{k/2}}}{k} \right) \right) \right\}$$

### 2.140 ODE No. 140

$$x^2 \left( \frac{d}{dx} y(x) + (y(x))^2 \right) + 4xy(x) + 2 = 0$$

**Mathematica:** cpu = 0.009501 (sec), leaf count = 17

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{c_1 + x} - \frac{2}{x} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 23

$$\left\{ y(x) = - \frac{2\_C1 - x}{x(-x + \_C1)} \right\}$$

**2.141 ODE No. 141**

$$x^2 \left( \frac{d}{dx} y(x) + (y(x))^2 \right) + axy(x) + b = 0$$

**Mathematica:** cpu = 0.026003 (sec), leaf count = 67

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{a^2 - 2a - 4b + 1} \left( \frac{2c_1}{x\sqrt{a^2 - 2a - 4b + 1} + c_1} - 1 \right) - 1}{2x} - \frac{a}{2x} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 64

$$\left\{ y(x) = \frac{1}{2x} \left( -\tanh \left( -\frac{\ln(x)}{2} \sqrt{a^2 - 2a - 4b + 1} + \frac{C1}{2} \sqrt{a^2 - 2a - 4b + 1} \right) \sqrt{a^2 - 2a - 4b + 1} - a \right) \right\}$$

**2.142 ODE No. 142**

$$x^2 \left( \frac{d}{dx} y(x) - (y(x))^2 \right) - ax^2y(x) + ax + 2 = 0$$

**Mathematica:** cpu = 0.181523 (sec), leaf count = 113

$$\left\{ \left\{ y(x) \rightarrow -\frac{\frac{1}{a^3x^2} + c_1 \left( \frac{e^{ax}(a^2x+a(ax-2))}{x} - \frac{e^{ax}(ax(ax-2)+2)}{x^2} + \frac{ae^{ax}(ax(ax-2)+2)}{x} \right)}{\frac{c_1 e^{ax}(ax(ax-2)+2)}{x} - \frac{1}{a^3x}} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 61

$$\left\{ y(x) = -\frac{(a^3x^3 - a^2x^2 + 2ax - 2)e^{ax} - C1}{x((a^2x^2 - 2ax + 2)e^{ax} + C1)} \right\}$$

**2.143 ODE No. 143**

$$x^2 \left( \frac{d}{dx} y(x) + a(y(x))^2 \right) - b = 0$$

**Mathematica:** cpu = 0.008501 (sec), leaf count = 51

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{4ab + 1} \left( \frac{2c_1}{x\sqrt{4ab + 1} + c_1} - 1 \right) - 1}{2ax} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 49

$$\left\{ y(x) = \frac{1}{2ax} \left( -\tanh \left( -\frac{\ln(x)}{2} \sqrt{4ab + 1} + \frac{C1}{2} \sqrt{4ab + 1} \right) \sqrt{4ab + 1} + 1 \right) \right\}$$

**2.144 ODE No. 144**

$$x^2 \left( \frac{d}{dx} y(x) + a(y(x))^2 \right) + bx^\alpha + c = 0$$

**Mathematica:** cpu = 0.168521 (sec), leaf count = 1712

$$\left\{ \left\{ y(x) \rightarrow \frac{a^{\frac{i\sqrt{4ac-1}\alpha+\alpha}{2\alpha^2}} - \frac{i\sqrt{4ac-1}}{2\alpha} \alpha^{-\frac{i\sqrt{4ac-1}\alpha+\alpha}{\alpha^2}} + \frac{i\sqrt{4ac-1}}{\alpha} + 1 b^{\frac{i\sqrt{4ac-1}\alpha+\alpha}{2\alpha^2}} - \frac{i\sqrt{4ac-1}}{2\alpha} \left( \frac{i\sqrt{4ac-1}\alpha+\alpha}{2\alpha^2} - \frac{i\sqrt{4ac-1}}{2\alpha} \right) (x^\alpha)^{\frac{i\sqrt{4ac-1}}{2\alpha^2}} \right. \right.$$

**Maple:** cpu = 0.078 (sec), leaf count = 244

$$\left\{ y(x) = -\frac{1}{2ax} \left( (-\sqrt{-4ac+1} C1 - C1) Y_{\frac{1}{\alpha}\sqrt{-4ac+1}} \left( 2 \frac{\sqrt{abx^{\alpha/2}}}{\alpha} \right) + 2x^{\alpha/2} Y_{\frac{\sqrt{-4ac+1}}{\alpha}} \left( 2 \frac{\sqrt{abx^{\alpha/2}}}{\alpha} \right) \right) \right.$$

**2.145 ODE No. 145**

$$x^2 \frac{d}{dx} y(x) + a(y(x))^3 - ax^2(y(x))^2 = 0$$

**Mathematica:** cpu = 0.390050 (sec), leaf count = 267

$$\text{Solve} \left[ \frac{\left( -\frac{1}{2^{2/3} a^{2/3} y(x)} - \frac{\sqrt[3]{ax}}{2^{2/3}} \right) \text{Ai} \left( \left( -\frac{\sqrt[3]{ax}}{2^{2/3}} - \frac{1}{2^{2/3} a^{2/3} y(x)} \right)^2 + \frac{1}{\sqrt[3]{2} \sqrt[3]{ax}} \right) + \text{Ai}' \left( \left( -\frac{\sqrt[3]{ax}}{2^{2/3}} - \frac{1}{2^{2/3} a^{2/3} y(x)} \right)^2 + \frac{1}{\sqrt[3]{2} \sqrt[3]{ax}} \right)}{\left( -\frac{1}{2^{2/3} a^{2/3} y(x)} - \frac{\sqrt[3]{ax}}{2^{2/3}} \right) \text{Bi} \left( \left( -\frac{\sqrt[3]{ax}}{2^{2/3}} - \frac{1}{2^{2/3} a^{2/3} y(x)} \right)^2 + \frac{1}{\sqrt[3]{2} \sqrt[3]{ax}} \right) + \text{Bi}' \left( \left( -\frac{\sqrt[3]{ax}}{2^{2/3}} - \frac{1}{2^{2/3} a^{2/3} y(x)} \right)^2 + \frac{1}{\sqrt[3]{2} \sqrt[3]{ax}} \right)} \right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 117

$$\left\{ y(x) = -\left( ax + (-2a)^{\frac{2}{3}} \text{RootOf} \left( \text{Bi} \left( \frac{1}{x} (-Z^2 \sqrt[3]{-2ax} - 1) \frac{1}{\sqrt[3]{-2a}} \right) - C1 - Z + Z \text{Ai} \left( \frac{1}{x} (-Z^2 \sqrt[3]{-2ax} \right) \right) \right) \right.$$

**2.146 ODE No. 146**

$$x^2 \frac{d}{dx} y(x) + x(y(x))^3 + a(y(x))^2 = 0$$

**Mathematica:** cpu = 0.507564 (sec), leaf count = 78

$$\text{Solve} \left[ -\frac{ia}{x} = \frac{2e^{\frac{1}{2} \left( -\frac{ia}{x} - \frac{i}{y(x)} \right)^2}}{2c_1 + \sqrt{2\pi} \operatorname{erfi} \left( \frac{-\frac{ia}{x} - \frac{i}{y(x)}}{\sqrt{2}} \right)}, y(x) \right]$$

**Maple:** cpu = 0.141 (sec), leaf count = 82

$$\left\{ -C1 + \left( x + \frac{a\sqrt{\pi}\sqrt{2}}{2} \operatorname{Erf} \left( \frac{\sqrt{2}(ay(x) + x)}{2xy(x)} \right) e^{\frac{(ay(x)+x)^2}{2x^2(y(x))^2}} \right) e^{-\frac{(a-x)y(x)+x((x+a)y(x)+x)}{2x^2(y(x))^2}} = 0 \right\}$$

**2.147 ODE No. 147**

$$x^2 \frac{d}{dx} y(x) + ax^2(y(x))^3 + b(y(x))^2 = 0$$

**Mathematica:** cpu = 0.523066 (sec), leaf count = 343

$$\text{Solve} \left[ \frac{\left( \frac{b^{2/3}}{2^{2/3} \sqrt[3]{ax}} + \frac{1}{2^{2/3} \sqrt[3]{a} \sqrt[3]{by(x)}} \right) \operatorname{Ai} \left( \left( \frac{b^{2/3}}{2^{2/3} \sqrt[3]{ax}} + \frac{1}{2^{2/3} \sqrt[3]{ay(x)} \sqrt[3]{b}} \right)^2 - \frac{\sqrt[3]{ax}}{\sqrt[3]{2b^{2/3}}} \right) + \operatorname{Ai}' \left( \left( \frac{b^{2/3}}{2^{2/3} \sqrt[3]{ax}} + \frac{1}{2^{2/3} \sqrt[3]{ay(x)} \sqrt[3]{b}} \right)}{\left( \frac{b^{2/3}}{2^{2/3} \sqrt[3]{ax}} + \frac{1}{2^{2/3} \sqrt[3]{a} \sqrt[3]{by(x)}} \right) \operatorname{Bi} \left( \left( \frac{b^{2/3}}{2^{2/3} \sqrt[3]{ax}} + \frac{1}{2^{2/3} \sqrt[3]{ay(x)} \sqrt[3]{b}} \right)^2 - \frac{\sqrt[3]{ax}}{\sqrt[3]{2b^{2/3}}} \right) + \operatorname{Bi}' \left( \left( \frac{b^{2/3}}{2^{2/3} \sqrt[3]{ax}} + \frac{1}{2^{2/3} \sqrt[3]{ay(x)} \sqrt[3]{b}} \right)} \right. \right]$$

**Maple:** cpu = 0.156 (sec), leaf count = 178

$$\left\{ y(x) = -\sqrt[3]{2} abx \left( \sqrt[3]{2} ab^2 - 2 (a^2 b^2)^{2/3} \operatorname{RootOf} \left( \operatorname{Bi} \left( -1/2 \frac{a2^{2/3}x - 2\_Z^2 \sqrt[3]{a^2 b^2}}{\sqrt[3]{a^2 b^2}} \right) - C1\_Z + \_Z \operatorname{Ai} \left( - \right) \right) \right.$$



**2.148 ODE No. 148**

$$(x^2 + 1) \frac{d}{dx}y(x) + xy(x) - 1 = 0$$

**Mathematica:** cpu = 0.012002 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{\sqrt{x^2 + 1}} + \frac{\sinh^{-1}(x)}{\sqrt{x^2 + 1}} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 16

$$\left\{ y(x) = (\text{Arcsinh}(x) + \_C1) \frac{1}{\sqrt{x^2 + 1}} \right\}$$

**2.149 ODE No. 149**

$$(x^2 + 1) \frac{d}{dx}y(x) + xy(x) - x(x^2 + 1) = 0$$

**Mathematica:** cpu = 0.011001 (sec), leaf count = 27

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{\sqrt{x^2 + 1}} + \frac{1}{3}(x^2 + 1) \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 20

$$\left\{ y(x) = \frac{x^2}{3} + \frac{1}{3} + \_C1 \frac{1}{\sqrt{x^2 + 1}} \right\}$$

**2.150 ODE No. 150**

$$(x^2 + 1) \frac{d}{dx}y(x) + 2xy(x) - 2x^2 = 0$$

**Mathematica:** cpu = 0.008001 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{x^2 + 1} + \frac{2x^3}{3(x^2 + 1)} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 19

$$\left\{ y(x) = \frac{1}{x^2 + 1} \left( \frac{2x^3}{3} + \_C1 \right) \right\}$$

**2.151 ODE No. 151**

$$(x^2 + 1) \frac{d}{dx}y(x) + ((y(x))^2 + 1) (2xy(x) - 1) = 0$$

**Mathematica:** cpu = 0.420553 (sec), leaf count = 203

$$\text{Solve} \left[ c_1 = \frac{\frac{1}{2} \left( \frac{1}{\frac{ix}{x^2+1} - \frac{ix^2y(x)}{x^2+1}} + \frac{i}{x} \right) \sqrt[4]{1 - \left( \frac{1}{\frac{ix}{x^2+1} - \frac{ix^2y(x)}{x^2+1}} + \frac{i}{x} \right)^2} {}_2F_1 \left( \frac{1}{2}, \frac{5}{4}; \frac{3}{2}; \left( \frac{1}{\frac{ix}{x^2+1} - \frac{ix^2y(x)}{x^2+1}} + \frac{i}{x} \right)^2 \right) + ix}{\sqrt[4]{-1 + \left( \frac{1}{\frac{ix}{x^2+1} - \frac{ix^2y(x)}{x^2+1}} + \frac{i}{x} \right)^2}}, y(x) \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 85

$$\left\{ -C1 + x \frac{1}{\sqrt[4]{\left(x^{-1} + x^2 \left(\frac{y(x)x^4}{x^2+1} - \frac{x^3}{x^2+1}\right)^{-1}\right)^2} + 1} + \frac{y(x) + x}{2xy(x) - 1} {}_2F_1 \left( \frac{1}{2}, \frac{5}{4}; \frac{3}{2}; -\frac{(y(x) + x)^2}{(xy(x) - 1)^2} \right) = 0 \right\}$$

**2.152 ODE No. 152**

$$(x^2 + 1) \frac{d}{dx}y(x) + x \sin(y(x)) \cos(y(x)) - x(x^2 + 1) (\cos(y(x)))^2 = 0$$

**Mathematica:** cpu = 0.242031 (sec), leaf count = 40

$$\left\{ \left\{ y(x) \rightarrow \tan^{-1} \left( \frac{-6c_1 \sqrt{x^2 + 1} + x^4 + 2x^2 + 1}{3(x^2 + 1)} \right) \right\} \right\}$$

**Maple:** cpu = 0.530 (sec), leaf count = 25

$$\left\{ y(x) = \arctan \left( \frac{1}{3} \left( (x^2 + 1)^{\frac{3}{2}} + 3_{-}C1 \right) \frac{1}{\sqrt{x^2 + 1}} \right) \right\}$$

**2.153 ODE No. 153**

$$(x^2 - 1) \frac{d}{dx} y(x) - xy(x) + a = 0$$

**Mathematica:** cpu = 0.016502 (sec), leaf count = 21

$$\left\{ \left\{ y(x) \rightarrow ax + c_1 \sqrt{x^2 - 1} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 20

$$\left\{ y(x) = \sqrt{1+x} \sqrt{x-1} \_C1 + ax \right\}$$

**2.154 ODE No. 154**

$$(x^2 - 1) \frac{d}{dx} y(x) + 2xy(x) - \cos(x) = 0$$

**Mathematica:** cpu = 0.013002 (sec), leaf count = 26

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{x^2 - 1} + \frac{\sin(x)}{x^2 - 1} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 16

$$\left\{ y(x) = \frac{\sin(x) + \_C1}{x^2 - 1} \right\}$$

**2.155 ODE No. 155**

$$(x^2 - 1) \frac{d}{dx} y(x) + (y(x))^2 - 2xy(x) + 1 = 0$$

**Mathematica:** cpu = 0.017002 (sec), leaf count = 46

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{c_1 + \frac{1}{2} \log(1-x) - \frac{1}{2} \log(x+1)} - \frac{x(1-x^2)}{x^2-1} \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 14

$$\left\{ y(x) = x + (\_C1 - \text{Artanh}(x))^{-1} \right\}$$

**2.156 ODE No. 156**

$$(x^2 - 1) \frac{d}{dx} y(x) - y(x)(y(x) - x) = 0$$

**Mathematica:** cpu = 0.016002 (sec), leaf count = 21

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{c_1 \sqrt{x^2 - 1} + x} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 20

$$\left\{ y(x) = \left( \sqrt{x-1} \sqrt{1+x} C1 + x \right)^{-1} \right\}$$

**2.157 ODE No. 157**

$$(x^2 - 1) \frac{d}{dx} y(x) + a((y(x))^2 - 2xy(x) + 1) = 0$$

**Mathematica:** cpu = 0.086011 (sec), leaf count = 158

$$\left\{ \left\{ y(x) \rightarrow \frac{(x^2 - 1) \left( c_1 \left( ax(x^2 - 1)^{\frac{a}{2}-1} P_{a-1}(x) + (x^2 - 1)^{\frac{a}{2}-1} (aP_a(x) - axP_{a-1}(x)) \right) + ax(x^2 - 1)^{\frac{a}{2}-1} \right)}{a \left( c_1 (x^2 - 1)^{a/2} P_{a-1}(x) + (x^2 - 1)^{a/2} Q_{a-1}(x) \right)} \right\} \right\}$$

**Maple:** cpu = 0.188 (sec), leaf count = 231

$$\left\{ y(x) = \frac{1}{(4 + 4x)a} \left( 8((a - 1/2)x - a/2 + 1/2)(1 + x) C1 \operatorname{HeunC}(0, -2a + 1, 0, 0, a^2 - a + 1/2, 2(1 + x)) \right) \right\}$$

**2.158 ODE No. 158**

$$(x^2 - 1) \frac{d}{dx} y(x) + ax(y(x))^2 + xy(x) = 0$$

**Mathematica:** cpu = 0.034004 (sec), leaf count = 31

$$\left\{ \left\{ y(x) \rightarrow -\frac{e^{c_1}}{ae^{c_1} - \sqrt{x^2 - 1}} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 22

$$\left\{ y(x) = \left( \sqrt{x-1} \sqrt{1+x} C1 - a \right)^{-1} \right\}$$

**2.159 ODE No. 159**

$$(x^2 - 1) \frac{d}{dx} y(x) - 2xy(x) \ln(y(x)) = 0$$

**Mathematica:** cpu = 0.017502 (sec), leaf count = 22

$$\left\{ \left\{ y(x) \rightarrow e^{e^{c_1} x^2 - e^{c_1}} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 13

$$\{y(x) = e^{-C1(x-1)(1+x)}\}$$

**2.160 ODE No. 160**

$$(x^2 - 4) \frac{d}{dx} y(x) + (x + 2) (y(x))^2 - 4y(x) = 0$$

**Mathematica:** cpu = 0.019502 (sec), leaf count = 27

$$\left\{ \left\{ y(x) \rightarrow \frac{2 - x}{(x + 2) (c_1 - \log(x + 2))} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 29

$$\left\{ y(x) = \frac{x - 2}{\ln(x + 2) x + \_C1 x + 2 \ln(x + 2) + 2 \_C1} \right\}$$

**2.161 ODE No. 161**

$$(x^2 - 5x + 6) \frac{d}{dx} y(x) + 3xy(x) - 8y(x) + x^2 = 0$$

**Mathematica:** cpu = 0.013002 (sec), leaf count = 53

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{(2 - x)^2(3 - x)} + \frac{\frac{x^4}{4} - \frac{2x^3}{3}}{(2 - x)^2(3 - x)} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 27

$$\left\{ y(x) = \frac{1}{(x - 2)^2(x - 3)} \left( -\frac{x^4}{4} + \frac{2x^3}{3} + \_C1 \right) \right\}$$

## 2.162 ODE No. 162

$$(x-a)(x-b) \frac{d}{dx} y(x) + (y(x))^2 + k(y(x) + x - a)(y(x) + x - b) = 0$$

**Mathematica:** cpu = 0.260533 (sec), leaf count = 133

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \sqrt{\frac{-a^2 k^2 + 2abk^2 - b^2 k^2}{(k+1)^2}} \tan \left( \frac{(k+1) \sqrt{\frac{-a^2 k^2 + 2abk^2 - b^2 k^2}{(k+1)^2}} (\log(x-b) - \log(x-a))}{2(a-b)} + c_1 \right) \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 128

$$\left\{ y(x) = \frac{k}{k+1} \left( \frac{_{-}C1 (a-x)^k a}{_{-}C1 (a-x)^k + (b-x)^k} - \frac{_{-}C1 (a-x)^k x}{_{-}C1 (a-x)^k + (b-x)^k} + \frac{(b-x)^k b}{_{-}C1 (a-x)^k + (b-x)^k} - \dots \right) \right\}$$

## 2.163 ODE No. 163

$$2x^2 \frac{d}{dx} y(x) - 2(y(x))^2 - xy(x) + 2a^2 x = 0$$

**Mathematica:** cpu = 0.011001 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{-a^2} \sqrt{x} \tan \left( \frac{2\sqrt{-a^2}}{\sqrt{x}} - c_1 \right) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 26

$$\left\{ y(x) = i \tan \left( 1(_{-}C1 \sqrt{x} - 2ia) \frac{1}{\sqrt{x}} \right) \sqrt{xa} \right\}$$

## 2.164 ODE No. 164

$$2x^2 \frac{d}{dx} y(x) - 2(y(x))^2 - 3xy(x) + 2a^2 x = 0$$

**Mathematica:** cpu = 0.082010 (sec), leaf count = 131

$$\left\{ \left\{ y(x) \rightarrow -\frac{x^2 \left( c_1 \left( \frac{ae^{-\frac{2a}{\sqrt{x}}}}{x} + \frac{e^{-\frac{2a}{\sqrt{x}}}}{2\sqrt{x}} \right) - \frac{2a}{4a\sqrt{x}} + \frac{2a}{2x} \right)}{c_1 \sqrt{x} e^{-\frac{2a}{\sqrt{x}}} - \frac{\sqrt{x} e^{\frac{2a}{\sqrt{x}}}}{2a}} \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 102

$$\left\{ y(x) = 1 \left( \left( -2x - C1 \sqrt{-\frac{a^2}{x}} - x \right) \sin \left( 2 \sqrt{-\frac{a^2}{x}} \right) - x \left( -C1 - 2 \sqrt{-\frac{a^2}{x}} \right) \cos \left( 2 \sqrt{-\frac{a^2}{x}} \right) \right) \left( 2 \cos \left( 2 \sqrt{-\frac{a^2}{x}} \right) \right) \right\}$$

## 2.165 ODE No. 165

$$x(2x - 1) \frac{d}{dx} y(x) + (y(x))^2 - (4x + 1)y(x) + 4x = 0$$

**Mathematica:** cpu = 0.016502 (sec), leaf count = 22

$$\left\{ \left\{ y(x) \rightarrow \frac{(1 - 2x)x}{c_1 - x} + 1 \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 17

$$\left\{ y(x) = \frac{2x^2 + -C1}{x + -C1} \right\}$$

## 2.166 ODE No. 166

$$2x(x - 1) \frac{d}{dx} y(x) + (x - 1)(y(x))^2 - x = 0$$

**Mathematica:** cpu = 0.082511 (sec), leaf count = 71

$$\left\{ \left\{ y(x) \rightarrow \frac{2x \left( \frac{c_1(E(x) - K(x))}{\pi x} - G_{2,2}^{2,0} \left( x \left| \begin{array}{l} -\frac{1}{2}, \frac{1}{2} \\ -1, 0 \end{array} \right. \right) \right)}{G_{2,2}^{2,0} \left( x \left| \begin{array}{l} \frac{1}{2}, \frac{3}{2} \\ 0, 0 \end{array} \right. \right) + \frac{2c_1 E(x)}{\pi}} \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 97

$$\left\{ y(x) = \frac{x}{2x - 2} \left( LegendreQ \left( -\frac{1}{2}, 1, \frac{2-x}{x} \right) - C1 - LegendreQ \left( \frac{1}{2}, 1, \frac{2-x}{x} \right) - C1 + LegendreP \left( -\frac{1}{2}, 1, \frac{2-x}{x} \right) \right) \right\}$$

**2.167 ODE No. 167**

$$3x^2 \frac{d}{dx}y(x) - 7(y(x))^2 - 3xy(x) - x^2 = 0$$

**Mathematica:** cpu = 0.022003 (sec), leaf count = 35

$$\left\{ \left\{ y(x) \rightarrow \frac{x \tan\left(\frac{1}{3}(3\sqrt{7}c_1 + \sqrt{7}\log(x))\right)}{\sqrt{7}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 20

$$\left\{ y(x) = \frac{x\sqrt{7}}{7} \tan\left(\frac{(\ln(x) + C1)\sqrt{7}}{3}\right) \right\}$$

**2.168 ODE No. 168**

$$3(x^2 - 4) \frac{d}{dx}y(x) + (y(x))^2 - xy(x) - 3 = 0$$

**Mathematica:** cpu = 0.093012 (sec), leaf count = 234

$$\left\{ \left\{ y(x) \rightarrow \frac{3(x^2 - 4) \left( c_1 \left( \frac{xP_{-\frac{1}{6}}^{\frac{1}{3}}\left(\frac{x}{2}\right)}{6(x^2-4)^{11/12}} + \frac{{}^{12}\sqrt{x^2-4} \left( \frac{1}{2}P_{\frac{5}{6}}^{\frac{1}{3}}\left(\frac{x}{2}\right) - \frac{5}{12}xP_{-\frac{1}{6}}^{\frac{1}{3}}\left(\frac{x}{2}\right) \right)}{2\left(\frac{x^2}{4}-1\right)} \right) + \frac{xQ_{-\frac{1}{6}}^{\frac{1}{3}}\left(\frac{x}{2}\right)}{6(x^2-4)^{11/12}} + \frac{{}^{12}\sqrt{x^2-4} \left( \frac{1}{2}Q_{\frac{5}{6}}^{\frac{1}{3}}\left(\frac{x}{2}\right) - \frac{5}{12}x \right)}{2\left(\frac{x^2}{4}-1\right)} \right)}{c_1 {}^{12}\sqrt{x^2-4} P_{-\frac{1}{6}}^{\frac{1}{3}}\left(\frac{x}{2}\right) + {}^{12}\sqrt{x^2-4} Q_{-\frac{1}{6}}^{\frac{1}{3}}\left(\frac{x}{2}\right)} \right\} \right\}$$

**Maple:** cpu = 0.140 (sec), leaf count = 140

$$\left\{ y(x) = -3(x+2) \left( HeunC\left(0, 4/3, -1/3, 0, \frac{25}{36}, 4(x+2)^{-1}\right) - C1 - 1/3(-x/4 - 1/2)^{4/3} HeunC\left(0, - \right) \right) \right\}$$



**2.169 ODE No. 169**

$$(ax + b)^2 \frac{d}{dx}y(x) + (ax + b)(y(x))^3 + c(y(x))^2 = 0$$

**Mathematica:** cpu = 2.095766 (sec), leaf count = 149

$$\text{Solve} \left[ -\frac{c}{\sqrt{-a(ax+b)^2}} = \frac{2 \exp\left(\frac{1}{2}\left(-\frac{c}{\sqrt{-a(ax+b)^2}} - \frac{\sqrt{-a(ax+b)^2}}{y(x)(-ax-b)}\right)^2\right)}{\sqrt{2\pi} \operatorname{erfi}\left(\frac{-\frac{c}{\sqrt{-a(ax+b)^2}} - \frac{\sqrt{-a(ax+b)^2}}{y(x)(-ax-b)}}{\sqrt{2}}\right)} + 2c_1, y(x) \right]$$

**Maple:** cpu = 0.141 (sec), leaf count = 153

$$\left\{ -C1 + \left( x + \frac{b}{a} + \frac{c\sqrt{\pi}\sqrt{2}}{2} \operatorname{Erf}\left(\frac{\sqrt{2}(a^2x + ab + cy(x))}{2(ax+b)y(x)} \frac{1}{\sqrt{a}}\right) e^{\frac{(a^2x+ab+cy(x))^2}{2(y(x))^2(ax+b)^2a}} a^{-\frac{3}{2}} \right) e^{-\frac{(a^2x+axy(x)+ab+by(x)+cy(x))^2}{2(y(x))^2}} \right\}$$

**2.170 ODE No. 170**

$$x^3 \frac{d}{dx}y(x) - (y(x))^2 - x^4 = 0$$

**Mathematica:** cpu = 0.022003 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow -\frac{x^3\left(-\frac{c_1}{x^2} + \frac{1}{x^2} - \frac{\log(x)}{x^2}\right)}{\frac{c_1}{x} + \frac{\log(x)}{x}} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 23

$$\left\{ y(x) = \frac{x^2(\ln(x) - C1 - 1)}{\ln(x) - C1} \right\}$$

**2.171 ODE No. 171**

$$x^3 \frac{d}{dx} y(x) - (y(x))^2 - x^2 y(x) = 0$$

**Mathematica:** cpu = 0.009501 (sec), leaf count = 17

$$\left\{ \left\{ y(x) \rightarrow \frac{x^2}{c_1 x + 1} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 15

$$\left\{ y(x) = \frac{x^2}{\_C1 x + 1} \right\}$$

**2.172 ODE No. 172**

$$x^3 \frac{d}{dx} y(x) - x^4 (y(x))^2 + x^2 y(x) + 20 = 0$$

**Mathematica:** cpu = 0.040505 (sec), leaf count = 35

$$\left\{ \left\{ y(x) \rightarrow -\frac{5c_1 x^4 - \frac{4}{x^5}}{x (c_1 x^5 + \frac{1}{x^4})} \right\} \right\}$$

**Maple:** cpu = 0.203 (sec), leaf count = 26

$$\left\{ y(x) = \frac{5 x^9 + 4 \_C1}{(-x^9 + \_C1) x^2} \right\}$$

**2.173 ODE No. 173**

$$x^3 \frac{d}{dx} y(x) - x^6 (y(x))^2 - (2x - 3) x^2 y(x) + 3 = 0$$

**Mathematica:** cpu = 0.016002 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{x^3 (c_1 e^{4x} + \frac{1}{4})} - \frac{3}{x^3} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 27

$$\left\{ y(x) = -3 \frac{(e^x)^4 \_C1 + 1}{x^3 ((e^x)^4 \_C1 - 3)} \right\}$$

**2.174 ODE No. 174**

$$x(x^2 + 1) \frac{d}{dx}y(x) + x^2y(x) = 0$$

**Mathematica:** cpu = 0.006001 (sec), leaf count = 17

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{\sqrt{x^2 + 1}} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 13

$$\left\{ y(x) = -C1 \frac{1}{\sqrt{x^2 + 1}} \right\}$$

**2.175 ODE No. 175**

$$x(x^2 - 1) \frac{d}{dx}y(x) - (2x^2 - 1)y(x) + ax^3 = 0$$

**Mathematica:** cpu = 0.020002 (sec), leaf count = 24

$$\left\{ \left\{ y(x) \rightarrow ax + c_1 \sqrt{1 - x^2} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 21

$$\left\{ y(x) = x\sqrt{1+x}\sqrt{x-1} - C1 + ax \right\}$$

**2.176 ODE No. 176**

$$x(x^2 - 1) \frac{d}{dx}y(x) + (x^2 - 1)(y(x))^2 - x^2 = 0$$

**Mathematica:** cpu = 0.123516 (sec), leaf count = 82

$$\left\{ \left\{ y(x) \rightarrow \frac{x \left( \frac{2c_1(E(x^2) - K(x^2))}{\pi x} - 2x G_{2,2}^{2,0} \left( x^2 \mid \begin{matrix} -\frac{1}{2}, \frac{1}{2} \\ -1, 0 \end{matrix} \right) \right)}{G_{2,2}^{2,0} \left( x^2 \mid \begin{matrix} \frac{1}{2}, \frac{3}{2} \\ 0, 0 \end{matrix} \right) + \frac{2c_1 E(x^2)}{\pi}} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 45

$$\left\{ y(x) = -\frac{\text{EllipticK}(x)}{-C1 \text{EllipticCE}(x) - C1 \text{EllipticCK}(x) + \text{EllipticE}(x)} + \frac{-C1 \text{EllipticCE}(x)}{-C1 \text{EllipticCE}(x) - C1 \text{EllipticCK}(x) + \text{EllipticE}(x)} \right\}$$

**2.177 ODE No. 177**

$$x^2(x-1) \frac{d}{dx} y(x) - (y(x))^2 - x(x-2)y(x) = 0$$

**Mathematica:** cpu = 0.016002 (sec), leaf count = 22

$$\left\{ \left\{ y(x) \rightarrow -\frac{x^2}{c_1 x - c_1 - 1} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 18

$$\left\{ y(x) = \frac{x^2}{-C1 x - C1 + 1} \right\}$$

**2.178 ODE No. 178**

$$2x(x^2-1) \frac{d}{dx} y(x) + 2(x^2-1)(y(x))^2 - (3x^2-5)y(x) + x^2 - 3 = 0$$

**Mathematica:** cpu = 0.068009 (sec), leaf count = 62

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt{x}}{\sqrt{1-x^2} \left( c_1 - \frac{2\sqrt{1-\frac{1}{x^2}} x F\left(\sin^{-1}\left(\frac{1}{\sqrt{x}}\right) \middle| -1\right)}{\sqrt{1-x^2}} \right)} + 1 \right\} \right\}$$

**Maple:** cpu = 0.110 (sec), leaf count = 63

$$\left\{ y(x) = 1 - 2 \frac{\sqrt{x}}{\sqrt{x-1}\sqrt{1+x}} \left( -C1 - 2 \frac{\text{EllipticF}(\sqrt{1+x}, 1/2\sqrt{2}) \sqrt{-x}\sqrt{-2x+2\sqrt{2}}}{\sqrt{2x-2}\sqrt{x}} \right)^{-1} \right\}$$

**2.179 ODE No. 179**

$$3x(x^2-1) \frac{d}{dx} y(x) + x(y(x))^2 - (x^2+1)y(x) - 3x = 0$$

**Mathematica:** cpu = 1.566699 (sec), leaf count = 2816

$$\left\{ \left\{ y(x) \rightarrow \frac{3(x^2-1) \left( \frac{e^{\int_1^x \text{Root}[125K[1]^8 - 164K[1]^6 + 70K[1]^4 - 20K[1]^2 + (1296K[1]^{12} - 5184K[1]^{10} + 7776K[1]^8 - 5184K[1]^6 + 1296K[1]^4) \#1^4 + (-3}}{\dots}} \right)}{\dots} \right\} \right\}$$

Maple: cpu = 0.109 (sec), leaf count = 145

$$\left\{ y(x) = \frac{35\_C1 x^4 - 35\_C1 x^2}{8} {}_2F_1\left(\frac{11}{6}, \frac{13}{6}; \frac{7}{3}; x^2\right) \frac{1}{\sqrt[3]{x}} \left( x^{\frac{2}{3}} {}_2F_1\left(\frac{5}{6}, \frac{7}{6}; \frac{4}{3}; x^2\right) - C1 + {}_2F_1\left(\frac{1}{2}, \frac{5}{6}; \frac{2}{3}; x^2\right) \right)^{-1} \right\}$$

## 2.180 ODE No. 180

$$(ax^2 + bx + c) \left( x \frac{d}{dx} y(x) - y(x) \right) - (y(x))^2 + x^2 = 0$$

Mathematica: cpu = 0.123016 (sec), leaf count = 132

$$\left\{ \left\{ y(x) \rightarrow - \frac{x \left( \exp \left( \frac{4 \tan^{-1} \left( \frac{2ax}{\sqrt{4ac-b^2}} + \frac{b}{\sqrt{4ac-b^2}} \right) + 2c_1 \right) - 1 \right)}{\exp \left( \frac{4 \tan^{-1} \left( \frac{2ax}{\sqrt{4ac-b^2}} + \frac{b}{\sqrt{4ac-b^2}} \right) + 2c_1 \right) + 1} \right\} \right\}$$

Maple: cpu = 0.047 (sec), leaf count = 58

$$\left\{ y(x) = - \tanh \left( 1 \left( -C1 \sqrt{4ac - b^2} + 2 \arctan \left( \frac{2ax + b}{\sqrt{4ac - b^2}} \right) \right) \frac{1}{\sqrt{4ac - b^2}} \right) x \right\}$$

## 2.181 ODE No. 181

$$x^4 \left( \frac{d}{dx} y(x) + (y(x))^2 \right) + a = 0$$

Mathematica: cpu = 0.011501 (sec), leaf count = 347

$$\left\{ \left\{ y(x) \rightarrow - \frac{\frac{i\sqrt{\frac{2}{\pi}} c_1 \sinh\left(\frac{\sqrt{-a}}{x}\right)}{\sqrt{-\frac{i\sqrt{-a}}{x}}} + \frac{i\sqrt{-a} \left( -\frac{\sqrt{\frac{2}{\pi}} c_1 \cosh\left(\frac{\sqrt{-a}}{x}\right)}{\sqrt{-\frac{i\sqrt{-a}}{x}}} + \frac{\sqrt{\frac{2}{\pi}} c_1 \left( -\frac{\sqrt{-ax} \sinh\left(\frac{\sqrt{-a}}{x}\right)}{a} - \cosh\left(\frac{\sqrt{-a}}{x}\right) \right)}{\sqrt{-\frac{i\sqrt{-a}}{x}}} \right)}{x} - \frac{2\sqrt{\frac{2}{\pi}} \left( i \sinh\left(\frac{\sqrt{-a}}{x}\right) + \frac{i\sqrt{-a}}{\sqrt{-\frac{i\sqrt{-a}}{x}}} \right)}{\sqrt{-\frac{i\sqrt{-a}}{x}}}}{2x \left( \frac{\sqrt{\frac{2}{\pi}} \cosh\left(\frac{\sqrt{-a}}{x}\right)}{\sqrt{-\frac{i\sqrt{-a}}{x}}} - \frac{i\sqrt{\frac{2}{\pi}} c_1 \sinh\left(\frac{\sqrt{-a}}{x}\right)}{\sqrt{-\frac{i\sqrt{-a}}{x}}} \right)} \right\} \right\}$$

Maple: cpu = 0.063 (sec), leaf count = 30

$$\left\{ y(x) = - \frac{1}{x^2} \left( \tan \left( \frac{-C1 x - 1}{x} \sqrt{a} \right) \sqrt{a} - x \right) \right\}$$

## 2.182 ODE No. 182

$$x(x^3 - 1) \frac{d}{dx} y(x) - 2x(y(x))^2 + y(x) + x^2 = 0$$

**Mathematica:** cpu = 0.175022 (sec), leaf count = 96

$$\left\{ \left\{ y(x) \rightarrow -\frac{(x^3 - 1) \left( \frac{2c_1 x^2}{(1-x^3)^{5/3}} + \frac{x}{(1-x^3)^{2/3}} + \frac{x^4}{(1-x^3)^{5/3}} \right)}{2 \left( \frac{c_1}{(1-x^3)^{2/3}} + \frac{x^2}{2(1-x^3)^{2/3}} \right)} \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 18

$$\left\{ y(x) = \frac{x(x + \_C1)}{\_C1 x^2 + 1} \right\}$$

## 2.183 ODE No. 183

$$(2x^4 - x) \frac{d}{dx} y(x) - 2(x^3 - 1)y(x) = 0$$

**Mathematica:** cpu = 0.014002 (sec), leaf count = 22

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 x^2}{\sqrt[3]{1 - 2x^3}} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 18

$$\left\{ y(x) = \_C1 x^2 \frac{1}{\sqrt[3]{2x^3 - 1}} \right\}$$

## 2.184 ODE No. 184

$$(ax^2 + bx + c)^2 \left( \frac{d}{dx} y(x) + (y(x))^2 \right) + A = 0$$

**Mathematica:** cpu = 1.467686 (sec), leaf count = 704

$$\left\{ \left\{ y(x) \rightarrow -\frac{2a\sqrt{ax^2+bx+c} \exp\left(-\frac{\sqrt{4ac-b^2}\sqrt{1-\frac{4A}{b^2-4ac}} \tan^{-1}\left(\frac{2ax+b}{\sqrt{4ac-b^2}}\right)}{\sqrt{b^2-4ac}}\right)}{(b^2-4ac)\left(\frac{(2ax+b)^2}{4ac-b^2}+1\right)} + \frac{(2ax+b) \exp\left(-\frac{\sqrt{4ac-b^2}\sqrt{1-\frac{4A}{b^2-4ac}} \tan^{-1}\left(\frac{2ax+b}{\sqrt{4ac-b^2}}\right)}{\sqrt{b^2-4ac}}\right)}{2\sqrt{b^2-4ac}\sqrt{1-\frac{4A}{b^2-4ac}}\sqrt{ax^2+bx+c}} \right. \right. \\ \left. \left. c_1 \sqrt{x(ax+b)+c} \left( -\exp\left(\frac{\sqrt{4ac-b^2}\sqrt{1-\frac{4A}{b^2-4ac}} \tan^{-1}\left(\frac{2ax+b}{\sqrt{4ac-b^2}}\right)}{\sqrt{b^2-4ac}}\right)} \right) \right\} \right\}$$

Maple: cpu = 0.234 (sec), leaf count = 846

$$\left\{ y(x) = -2 \frac{a}{\sqrt{-4ac + b^2} (2ax + b + i\sqrt{4ac - b^2}) (i\sqrt{4ac - b^2} - 2ax - b)} \left( -i\sqrt{4ac - b^2} \left( \frac{i\sqrt{4ac - b^2}}{2ax + b + i} \right) \right) \right.$$

## 2.185 ODE No. 185

$$x^7 \frac{d}{dx} y(x) + 2(x^2 + 1)(y(x))^3 + 5x^3(y(x))^2 = 0$$

Mathematica: cpu = 0.375548 (sec), leaf count = 123

$$\text{Solve} \left[ c_1 = \frac{\frac{1}{2} \sqrt[4]{1 - \left( \frac{ix^2}{y(x)} + \frac{i}{x} \right)^2} \left( \frac{ix^2}{y(x)} + \frac{i}{x} \right) {}_2F_1 \left( \frac{1}{2}, \frac{5}{4}, \frac{3}{2}; \left( \frac{ix^2}{y(x)} + \frac{i}{x} \right)^2 \right) + ix}{\sqrt[4]{-1 + \left( \frac{ix^2}{y(x)} + \frac{i}{x} \right)^2}}, y(x) \right]$$

Maple: cpu = 0.031 (sec), leaf count = 63

$$\left\{ -C1 + x \frac{1}{\sqrt[4]{\left(x^{-1} + \frac{x^2}{y(x)}\right)^2 + 1}} + \frac{x^3 + y(x)}{2xy(x)} {}_2F_1 \left( \frac{1}{2}, \frac{5}{4}; \frac{3}{2}; -\frac{(x^3 + y(x))^2}{x^2(y(x))^2} \right) = 0 \right\}$$

## 2.186 ODE No. 186

$$x^n \frac{d}{dx} y(x) + (y(x))^2 - (n-1)x^{n-1}y(x) + x^{2n-2} = 0$$

Mathematica: cpu = 0.029004 (sec), leaf count = 19

$$\{ \{ y(x) \rightarrow x^{n-1} \tan(c_1 - \log(x)) \} \}$$

Maple: cpu = 0.031 (sec), leaf count = 17

$$\{ y(x) = \tan(-\ln(x) + \_C1) x^{n-1} \}$$

**2.187 ODE No. 187**

$$x^n \frac{d}{dx} y(x) - a(y(x))^2 - bx^{2n-2} = 0$$

**Mathematica:** cpu = 0.070009 (sec), leaf count = 328

$$\left\{ \left\{ y(x) \rightarrow - \frac{x^n \left( \frac{1}{2} \sqrt{a} \sqrt{b} c_1 \left( -\frac{n-1}{\sqrt{a}\sqrt{b}} - \sqrt{\frac{(n-1)^2}{ab} - 4} \right) x^{\frac{1}{2} \sqrt{a}\sqrt{b} \left( -\frac{n-1}{\sqrt{a}\sqrt{b}} - \sqrt{\frac{(n-1)^2}{ab} - 4} \right) - 1} + \frac{1}{2} \sqrt{a} \sqrt{b} \left( \sqrt{\frac{(n-1)^2}{ab} - 4} - \frac{n-1}{\sqrt{a}\sqrt{b}} \right) x^{\frac{1}{2} \sqrt{a}\sqrt{b} \left( \sqrt{\frac{(n-1)^2}{ab} - 4} - \frac{n-1}{\sqrt{a}\sqrt{b}} \right) - 1}}{a \left( c_1 x^{\frac{1}{2} \sqrt{a}\sqrt{b} \left( -\frac{n-1}{\sqrt{a}\sqrt{b}} - \sqrt{\frac{(n-1)^2}{ab} - 4} \right) + x^{\frac{1}{2} \sqrt{a}\sqrt{b} \left( \sqrt{\frac{(n-1)^2}{ab} - 4} - \frac{n-1}{\sqrt{a}\sqrt{b}} \right) - 1}} \right)} \right. \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 88

$$\left\{ y(x) = \frac{1}{2a} \left( -x^{n-1} \tan \left( -\frac{\ln(x)}{2} \sqrt{4ab - n^2 + 2n - 1} + \frac{C1}{2} \sqrt{4ab - n^2 + 2n - 1} \right) \sqrt{4ab - n^2 + 2n - 1} \right) \right.$$

**2.188 ODE No. 188**

$$x^{2n+1} \frac{d}{dx} y(x) - a(y(x))^3 - bx^{3n} = 0$$

**Mathematica:** cpu = 21.064175 (sec), leaf count = 33

$$\text{DSolve}[-ay(x)^3 - bnx^3 + x^{2n+1}y'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.031 (sec), leaf count = 32

$$\left\{ y(x) = \text{RootOf} \left( -\ln(x) + \_C1 + \int^{-Z} (\_a^3 a - n\_a + b)^{-1} d\_a \right) x^n \right\}$$

**2.189 ODE No. 189**

$$x^{m(n-1)+n} \frac{d}{dx} y(x) - a(y(x))^n - bx^{n(m+1)} = 0$$

**Mathematica:** cpu = 59.178515 (sec), leaf count = 90

$$\text{Solve} \left[ \int_1^{y(x) \left( \frac{ax^{-(m+1)n}}{b} \right)^{\frac{1}{n}}} \frac{1}{-K[1] \left( \frac{b^{1-n}(m+1)^n}{a} \right)^{\frac{1}{n}} + K[1]^n + 1} dK[1] = bx^{m+1} \log(x) \left( \frac{ax^{-(m+1)n}}{b} \right)^{\frac{1}{n}} + c_1, y \right]$$

**Maple:** cpu = 0.187 (sec), leaf count = 61

$$\left\{ \int_{-b}^{y(x)} \frac{x^{mn} x^n}{-x^n (x^m x b - (m+1) \_a) x^{mn} - \_a^n x^m x a} d\_a + \ln(x) - \_C1 = 0 \right\}$$



**2.190 ODE No. 190**

$$\sqrt{x^2 - 1} \frac{d}{dx} y(x) - \sqrt{(y(x))^2 - 1} = 0$$

**Mathematica:** cpu = 0.052007 (sec), leaf count = 55

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( -e^{-c_1} \sqrt{x^2 - 1} + e^{c_1} \sqrt{x^2 - 1} + e^{-c_1} x + e^{c_1} x \right) \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 29

$$\left\{ \ln \left( x + \sqrt{x^2 - 1} \right) - \ln \left( y(x) + \sqrt{(y(x))^2 - 1} \right) + \_C1 = 0 \right\}$$

**2.191 ODE No. 191**

$$\sqrt{-x^2 + 1} \frac{d}{dx} y(x) - y(x) \sqrt{(y(x))^2 - 1} = 0$$

**Mathematica:** cpu = 0.030004 (sec), leaf count = 52

$$\left\{ \left\{ y(x) \rightarrow \sqrt{\tan^2(c_1 + \sin^{-1}(x)) + 1} (-\cot(c_1 + \sin^{-1}(x))) \right\}, \left\{ y(x) \rightarrow \sqrt{\tan^2(c_1 + \sin^{-1}(x)) + 1} \cot(c_1 + \sin^{-1}(x)) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 16

$$\left\{ \arcsin(x) + \arctan \left( \frac{1}{\sqrt{(y(x))^2 - 1}} \right) + \_C1 = 0 \right\}$$

**2.192 ODE No. 192**

$$\sqrt{a^2 + x^2} \frac{d}{dx} y(x) + y(x) - \sqrt{a^2 + x^2} + x = 0$$

**Mathematica:** cpu = 0.027504 (sec), leaf count = 57

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{\sqrt{a^2 + x^2} + x} + \frac{a^2 \log(\sqrt{a^2 + x^2} + x)}{\sqrt{a^2 + x^2} + x} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 36

$$\left\{ y(x) = 1 \left( a^2 \ln \left( x + \sqrt{a^2 + x^2} \right) + \_C1 \right) \left( x + \sqrt{a^2 + x^2} \right)^{-1} \right\}$$

**2.193 ODE No. 193**

$$x \left( \frac{d}{dx} y(x) \right) \ln(x) + y(x) - ax(\ln(x) + 1) = 0$$

**Mathematica:** cpu = 0.007501 (sec), leaf count = 16

$$\left\{ \left\{ y(x) \rightarrow ax + \frac{c_1}{\log(x)} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 14

$$\left\{ y(x) = ax + \frac{-C1}{\ln(x)} \right\}$$

**2.194 ODE No. 194**

$$x \left( \frac{d}{dx} y(x) \right) \ln(x) - (y(x))^2 \ln(x) - (2(\ln(x))^2 + 1)y(x) - (\ln(x))^3 = 0$$

**Mathematica:** cpu = 0.075510 (sec), leaf count = 98

$$\left\{ \left\{ y(x) \rightarrow - \frac{x \left( \frac{c_1 e^{\frac{\log^2(x)}{2}} \log(x)}{x} + \frac{e^{\frac{\log^2(x)}{2}} \log(x)}{x} + \frac{e^{\frac{\log^2(x)}{2}} \log^3(x)}{2x} \right)}{c_1 e^{\frac{\log^2(x)}{2}} + \frac{1}{2} e^{\frac{\log^2(x)}{2}} \log^2(x)} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 23

$$\left\{ y(x) = - \frac{\ln(x) ((\ln(x))^2 + \_C1 + 2)}{(\ln(x))^2 + \_C1} \right\}$$

**2.195 ODE No. 195**

$$\sin(x) \frac{d}{dx} y(x) - (y(x))^2 (\sin(x))^2 + (\cos(x) - 3 \sin(x)) y(x) + 4 = 0$$

**Mathematica:** cpu = 0.057507 (sec), leaf count = 27

$$\left\{ \left\{ y(x) \rightarrow \frac{\csc(x)}{c_1 e^{5x} + \frac{1}{5}} - 4 \csc(x) \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 28

$$\left\{ y(x) = -4 \frac{(e^x)^5 \_C1 + 1}{\sin(x) ((e^x)^5 \_C1 - 4)} \right\}$$

## 2.196 ODE No. 196

$$\cos(x) \frac{d}{dx} y(x) + y(x) + (1 + \sin(x)) \cos(x) = 0$$

**Mathematica:** cpu = 0.054007 (sec), leaf count = 53

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-2 \tanh^{-1}(\tan(\frac{x}{2}))} + e^{-2 \tanh^{-1}(\tan(\frac{x}{2}))} \left( \sin(x) + 4 \log \left( \cos \left( \frac{x}{2} \right) - \sin \left( \frac{x}{2} \right) \right) \right) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 29

$$\left\{ y(x) = \frac{\sin(x) + 2 \ln(\cos(x)) - 2 \ln(\sec(x) + \tan(x)) + \_C1}{\sec(x) + \tan(x)} \right\}$$

## 2.197 ODE No. 197

$$\cos(x) \frac{d}{dx} y(x) - (y(x))^4 - y(x) \sin(x) = 0$$

**Mathematica:** cpu = 0.041005 (sec), leaf count = 98

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{\sqrt[3]{c_1 \cos^3(x) - \sin(x) - 2 \sin(x) \cos^2(x)}} \right\}, \left\{ y(x) \rightarrow -\frac{\sqrt[3]{-1}}{\sqrt[3]{c_1 \cos^3(x) - \sin(x) - 2 \sin(x) \cos^2(x)}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 364

$$\left\{ y(x) = \frac{1}{\_C1 (\sin(x))^4 + 2 \cos(x) (\sin(x))^3 - 2 \_C1 (\sin(x))^2 - 3 \cos(x) \sin(x) + \_C1 \sqrt[3]{\cos(x) (\_C1 \cos^3(x) - \sin(x) - 2 \sin(x) \cos^2(x))}} \right\}$$

## 2.198 ODE No. 198

$$\sin(x) \cos(x) \frac{d}{dx} y(x) - y(x) - (\sin(x))^3 = 0$$

**Mathematica:** cpu = 0.024503 (sec), leaf count = 15

$$\left\{ \left\{ y(x) \rightarrow c_1 \tan(x) - \sin(x) \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 15

$$\left\{ y(x) = -\cos(x) \tan(x) + \tan(x) \_C1 \right\}$$

**2.199 ODE No. 199**

$$\sin(2x) \frac{d}{dx}y(x) + \sin(2y(x)) = 0$$

**Mathematica:** cpu = 0.185024 (sec), leaf count = 15

$$\left\{ \left\{ y(x) \rightarrow \cot^{-1} \left( e^{-2c_1} \tan(x) \right) \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 100

$$\left\{ y(x) = \frac{1}{2} \arctan \left( 2 \frac{-C1 (2 \sin(2x) + \sin(4x))}{-C1^2 \cos(4x) + C1^2 + 4 \cos(2x) + \cos(4x) + 3}, -\frac{-C1^2 \cos(4x) - C1^2 + 4 \cos(2x) + \cos(4x) + 3}{-C1^2 \cos(4x) + C1^2} \right) \right\}$$

**2.200 ODE No. 200**

$$(a(\sin(x))^2 + b) \frac{d}{dx}y(x) + ay(x) \sin(2x) + Ax(a(\sin(x))^2 + c) = 0$$

**Mathematica:** cpu = 0.050506 (sec), leaf count = 77

$$\left\{ \left\{ y(x) \rightarrow \frac{\frac{1}{2}aAx^2 - \frac{1}{2}aAx \sin(2x) - \frac{1}{4}aA \cos(2x) + Acx^2}{a \cos(2x) - a - 2b} + \frac{c_1}{a \cos(2x) - a - 2b} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 56

$$\left\{ y(x) = \frac{-2A \sin(2x) ax + 2Aax^2 + 4Acx^2 - A \cos(2x) a - 8C1}{4a \cos(2x) - 4a - 8b} \right\}$$

**2.201 ODE No. 201**

$$2f(x) \frac{d}{dx}y(x) + 2f(x)(y(x))^2 - \left( \frac{d}{dx}f(x) \right) y(x) - 2(f(x))^2 = 0$$

**Mathematica:** cpu = 0.077510 (sec), leaf count = 38

$$\left\{ \left\{ y(x) \rightarrow i \sqrt{f(x)} \tan \left( c_1 + i \int_1^x -\sqrt{f(K[1])} dK[1] \right) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 23

$$\left\{ y(x) = i \tan \left( -i \int \sqrt{f(x)} dx + C1 \right) \sqrt{f(x)} \right\}$$

**2.202 ODE No. 202**

$$f(x) \frac{d}{dx}y(x) + g(x) \operatorname{tg}(y(x)) + h(x) = 0$$

**Mathematica:** cpu = 20.512605 (sec), leaf count = 22

$$\text{DSolve}[f(x)y'(x) + g(x)\operatorname{tg}(y(x)) + h(x) = 0, y(x), x]$$

**Maple:** cpu = 0.172 (sec), leaf count = 0

could not solve

**2.203 ODE No. 203**

$$y(x) \frac{d}{dx}y(x) + y(x) + x^3 = 0$$

**Mathematica:** cpu = 3.318922 (sec), leaf count = 19

$$\text{DSolve}[x^3 + y(x)y'(x) + y(x) = 0, y(x), x]$$

**Maple:** cpu = 1.779 (sec), leaf count = 0

could not solve

**2.204 ODE No. 204**

$$y(x) \frac{d}{dx}y(x) + ay(x) + x = 0$$

**Mathematica:** cpu = 0.096512 (sec), leaf count = 70

$$\text{Solve} \left[ \frac{1}{2} \log \left( \frac{ay(x)}{x} + \frac{y(x)^2}{x^2} + 1 \right) - \frac{a \tan^{-1} \left( \frac{a + \frac{2y(x)}{x}}{\sqrt{4-a^2}} \right)}{\sqrt{4-a^2}} = c_1 - \log(x), y(x) \right]$$

**Maple:** cpu = 0.218 (sec), leaf count = 88

$$\left\{ y(x) = \operatorname{RootOf} \left( -Z^2 - e^{\operatorname{RootOf} \left( x^2 \left( \left( \tanh \left( \frac{2-C1+Z+2 \ln(x)}{2a} \sqrt{a^2-4} \right) \right)^2 a^2-4 \left( \tanh \left( 1/2 \frac{\sqrt{a^2-4}(2-C1+Z+2 \ln(x))}{a} \right) \right) \right)^2 - a^2-4} \right) \right.$$

**2.205 ODE No. 205**

$$y(x) \frac{d}{dx} y(x) + ay(x) + 1/4 (a^2 - 1) x + bx^n = 0$$

**Mathematica:** cpu = 24.751143 (sec), leaf count = 33

$$\text{DSolve}\left[\frac{1}{4}(a^2 - 1)x + ay(x) + bx^n + y(x)y'(x) = 0, y(x), x\right]$$

**Maple:** cpu = 0.967 (sec), leaf count = 0

could not solve

**2.206 ODE No. 206**

$$y(x) \frac{d}{dx} y(x) + ay(x) + be^x - 2a = 0$$

**Mathematica:** cpu = 30.060317 (sec), leaf count = 26

$$\text{DSolve}[ay(x) - 2a + be^x + y(x)y'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.780 (sec), leaf count = 0

could not solve

**2.207 ODE No. 207**

$$y(x) \frac{d}{dx} y(x) + (y(x))^2 + 4x(1+x) = 0$$

**Mathematica:** cpu = 0.010501 (sec), leaf count = 47

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{c_1 e^{-2x} - 4x^2} \right\}, \left\{ y(x) \rightarrow \sqrt{c_1 e^{-2x} - 4x^2} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 37

$$\left\{ y(x) = \sqrt{e^{-2x} C1 - 4x^2}, y(x) = -\sqrt{e^{-2x} C1 - 4x^2} \right\}$$

**2.208 ODE No. 208**

$$y(x) \frac{d}{dx} y(x) + a(y(x))^2 - b \cos(x + c) = 0$$

**Mathematica:** cpu = 0.064508 (sec), leaf count = 118

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{4a^2 c_1 e^{-2ax} + 4ab \cos(c+x) + c_1 e^{-2ax} + 2b \sin(c+x)}}{\sqrt{4a^2 + 1}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{4a^2 c_1 e^{-2ax} + 4ab \cos(c+x) + c_1 e^{-2ax} + 2b \sin(c+x)}}{\sqrt{4a^2 + 1}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 116

$$\left\{ y(x) = \frac{1}{4a^2 + 1} \sqrt{(4a^2 + 1)(4e^{-2ax} - C1 a^2 + 4 \cos(x+c) ab + e^{-2ax} - C1 + 2 \sin(x+c) b)}, y(x) = -\frac{1}{4a^2 + 1} \sqrt{(4a^2 + 1)(4e^{-2ax} - C1 a^2 + 4 \cos(x+c) ab + e^{-2ax} - C1 + 2 \sin(x+c) b)} \right\}$$

**2.209 ODE No. 209**

$$y(x) \frac{d}{dx} y(x) - \sqrt{a(y(x))^2 + b} = 0$$

**Mathematica:** cpu = 0.021003 (sec), leaf count = 84

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{2a^2 c_1 x + a^2 c_1^2 + a^2 x^2 - b}}{\sqrt{a}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{2a^2 c_1 x + a^2 c_1^2 + a^2 x^2 - b}}{\sqrt{a}} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 21

$$\left\{ x - \frac{1}{a} \sqrt{a(y(x))^2 + b} + C1 = 0 \right\}$$

**2.210 ODE No. 210**

$$y(x) \frac{d}{dx} y(x) + x(y(x))^2 - 4x = 0$$

**Mathematica:** cpu = 0.015502 (sec), leaf count = 47

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{e^{2c_1 - x^2} + 4} \right\}, \left\{ y(x) \rightarrow \sqrt{e^{2c_1 - x^2} + 4} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 33

$$\left\{ y(x) = \sqrt{e^{-x^2} - C1 + 4}, y(x) = -\sqrt{e^{-x^2} - C1 + 4} \right\}$$

## 2.211 ODE No. 211

$$y(x) \frac{d}{dx} y(x) - x e^{\frac{x}{y(x)}} = 0$$

**Mathematica:** cpu = 38.749421 (sec), leaf count = 40

$$\text{Solve} \left[ \int_1^{\frac{y(x)}{x}} \frac{K[1]}{K[1]^2 - e^{\frac{1}{K[1]}}} dK[1] = c_1 - \log(x), y(x) \right]$$

**Maple:** cpu = 0.016 (sec), leaf count = 31

$$\left\{ y(x) = \text{RootOf} \left( - \int^{-Z} \frac{-a}{-a^2 + e^{-a^{-1}}} d_a + \ln(x) + \_C1 \right) x \right\}$$

## 2.212 ODE No. 212

$$y(x) \frac{d}{dx} y(x) + f((y(x))^2 + x^2) g(x) + x = 0$$

**Mathematica:** cpu = 22.411346 (sec), leaf count = 92

$$\text{Solve} \left[ \int_1^{y(x)} \left( \frac{K[2]}{f(K[2]^2 + x^2)} - \int_1^x - \frac{2K[1]K[2]f'(K[1]^2 + K[2]^2)}{f(K[1]^2 + K[2]^2)} dK[1] \right) dK[2] + \int_1^x \left( \frac{K[1]}{f(K[1]^2 + y(x))} \right) \right]$$

**Maple:** cpu = 0.094 (sec), leaf count = 30

$$\left\{ \int_{-b}^{y(x)} \frac{-a}{f(-a^2 + x^2)} d_a + \int g(x) dx - \_C1 = 0 \right\}$$

## 2.213 ODE No. 213

$$(1 + y(x)) \frac{d}{dx} y(x) - y(x) - x = 0$$

**Mathematica:** cpu = 0.100513 (sec), leaf count = 71

$$\text{Solve} \left[ \frac{1}{2} \log \left( \frac{x^2 - y(x)^2 + (x-3)y(x) - x - 1}{(x-1)^2} \right) + \log(1-x) = c_1 + \frac{\tanh^{-1} \left( \frac{y(x)+2x-1}{\sqrt{5}(y(x)+1)} \right)}{\sqrt{5}}, y(x) \right]$$

**Maple:** cpu = 0.624 (sec), leaf count = 73

$$\left\{ -\frac{1}{2} \ln \left( - \frac{(x-1)^2 - (x-1)(-y(x)-1) - (-y(x)-1)^2}{(x-1)^2} \right) - \frac{\sqrt{5}}{5} \text{Artanh} \left( \frac{(x-3-2y(x))\sqrt{5}}{5x-5} \right) - \ln \left( \right) \right\}$$



## 2.214 ODE No. 214

$$(y(x) + x - 1) \frac{d}{dx} y(x) - y(x) + 2x + 3 = 0$$

**Mathematica:** cpu = 0.109014 (sec), leaf count = 78

$$\text{Solve} \left[ 2\sqrt{2} \tan^{-1} \left( \frac{-y(x) + 2x + 3}{\sqrt{2}(y(x) + x - 1)} \right) = 3c_1 + 2 \log \left( \frac{6x^2 + 3y(x)^2 - 10y(x) + 8x + 11}{(3x + 2)^2} \right) + 4 \log(3x + 2) \right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 65

$$\left\{ y(x) = \frac{5}{3} - \frac{\tan(\text{RootOf}(\sqrt{2} \ln(18(\tan(\_Z))^2 x^2 + 24(\tan(\_Z))^2 x + 8(\tan(\_Z))^2 + 18x^2 + 24x + 11)))}{3} \right.$$

## 2.215 ODE No. 215

$$(y(x) + 2x - 2) \frac{d}{dx} y(x) - y(x) + x + 1 = 0$$

**Mathematica:** cpu = 0.119015 (sec), leaf count = 80

$$\text{Solve} \left[ 6\sqrt{3} \tan^{-1} \left( \frac{4 - 3y(x)}{\sqrt{3}(y(x) + 2x - 2)} \right) = 2c_1 + 3 \log \left( \frac{3x^2 + 3y(x)^2 + 3(x - 3)y(x) - 6x + 7}{(1 - 3x)^2} \right) + 6 \log(3x + 2) \right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 68

$$\left\{ y(x) = \frac{3}{2} - \frac{x}{2} + \frac{\sqrt{3}(3x - 1)}{6} \tan \left( \text{RootOf} \left( \sqrt{3} \ln \left( \frac{27x^2}{4} - \frac{9x}{2} + \frac{3}{4} + \frac{27(\tan(\_Z))^2 x^2}{4} - \frac{9(\tan(\_Z))^2}{2} \right) \right) \right) \right.$$

## 2.216 ODE No. 216

$$(y(x) - 2x + 1) \frac{d}{dx} y(x) + y(x) + x = 0$$

**Mathematica:** cpu = 0.101513 (sec), leaf count = 82

$$\text{Solve} \left[ 6\sqrt{3} \tan^{-1} \left( \frac{3y(x) + 1}{\sqrt{3}(-y(x) + 2x - 1)} \right) = 2c_1 + 3 \log \left( \frac{3x^2 + 3y(x)^2 - 3(x - 1)y(x) - 3x + 1}{(1 - 3x)^2} \right) + 6 \log(3x + 2) \right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 68

$$\left\{ y(x) = -\frac{1}{2} + \frac{x}{2} - \frac{\sqrt{3}(3x - 1)}{6} \tan \left( \text{RootOf} \left( \sqrt{3} \ln \left( \frac{27x^2}{4} - \frac{9x}{2} + \frac{3}{4} + \frac{27(\tan(\_Z))^2 x^2}{4} - \frac{9(\tan(\_Z))^2}{2} \right) \right) \right) \right.$$

**2.217 ODE No. 217**

$$(y(x) - x^2) \frac{d}{dx}y(x) - x = 0$$

**Mathematica:** cpu = 0.018502 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( W \left( -e^{c_1 - 2x^2 - 1} \right) + 1 \right) + x^2 \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 23

$$\left\{ y(x) = x^2 + \frac{\text{lambertW} \left( -4\_C1 e^{-2x^2 - 1} \right)}{2} + \frac{1}{2} \right\}$$

**2.218 ODE No. 218**

$$(y(x) - x^2) \frac{d}{dx}y(x) + 4xy(x) = 0$$

**Mathematica:** cpu = 0.102513 (sec), leaf count = 257

$$\left\{ \left\{ y(x) \rightarrow x^2 + \frac{1}{-\frac{1}{2x^2} - \frac{\frac{1}{2} - \frac{i}{2}}{\sqrt{2x^2} \sqrt{x^2 \sinh\left(\frac{2c_1}{9}\right) + x^2 \cosh\left(\frac{2c_1}{9}\right) - i}}} \right\}, \left\{ y(x) \rightarrow x^2 + \frac{1}{-\frac{1}{2x^2} + \frac{\frac{1}{2} - \frac{i}{2}}{\sqrt{2x^2} \sqrt{x^2 \sinh\left(\frac{2c_1}{9}\right) + x^2 \cosh\left(\frac{2c_1}{9}\right) - i}}} \right\} \right\}$$

**Maple:** cpu = 0.140 (sec), leaf count = 53

$$\left\{ y(x) = \frac{-C1}{2} \left( -C1 - \sqrt{-C1^2 - 4x^2} \right) - x^2, y(x) = \frac{-C1}{2} \left( -C1 + \sqrt{-C1^2 - 4x^2} \right) - x^2 \right\}$$

**2.219 ODE No. 219**

$$(y(x) + g(x)) \frac{d}{dx}y(x) - f_2(x) (y(x))^2 - f_1(x) y(x) - f_0(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.873 (sec), leaf count = 0

could not solve

## 2.220 ODE No. 220

$$2y(x) \frac{d}{dx}y(x) - x(y(x))^2 - x^3 = 0$$

**Mathematica:** cpu = 0.012002 (sec), leaf count = 57

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{c_1 e^{\frac{x^2}{2}} - x^2 - 2} \right\}, \left\{ y(x) \rightarrow \sqrt{c_1 e^{\frac{x^2}{2}} - x^2 - 2} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 43

$$\left\{ y(x) = \sqrt{e^{\frac{x^2}{2}} \_C1 - x^2 - 2}, y(x) = -\sqrt{e^{\frac{x^2}{2}} \_C1 - x^2 - 2} \right\}$$

## 2.221 ODE No. 221

$$(2y(x) + x + 1) \frac{d}{dx}y(x) - 2y(x) - x + 1 = 0$$

**Mathematica:** cpu = 0.017502 (sec), leaf count = 35

$$\left\{ \left\{ y(x) \rightarrow \frac{2}{3} \left( W \left( -e^{c_1 + \frac{9x}{4} - 1} \right) + 1 \right) + \frac{1}{2}(-x - 1) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 21

$$\left\{ y(x) = -\frac{x}{2} + \frac{2}{3} \text{lambertW} \left( \frac{e^{-\frac{1}{4}} \_C1}{4} e^{\frac{9x}{4}} \right) + \frac{1}{6} \right\}$$

## 2.222 ODE No. 222

$$(2y(x) + x + 7) \frac{d}{dx}y(x) - y(x) + 2x + 4 = 0$$

**Mathematica:** cpu = 0.056507 (sec), leaf count = 65

$$\text{Solve} \left[ 5c_1 + 2 \log \left( \frac{4(x^2 + y(x))^2 + 4y(x) + 6x + 13}{5(x+3)^2} \right) + 2 \tan^{-1} \left( \frac{y(x) - 2(x+2)}{2y(x) + x + 7} \right) + 4 \log(x+3) = 0, y \right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 31

$$\{y(x) = -2 - \tan(\text{RootOf}(-\_Z + \ln((\cos(\_Z))^{-2}) + 2 \ln(x+3) + 2\_C1))(x+3)\}$$

**2.223 ODE No. 223**

$$(2y(x) - x) \frac{d}{dx}y(x) - y(x) - 2x = 0$$

**Mathematica:** cpu = 0.025003 (sec), leaf count = 55

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( x - \sqrt{5x^2 - 4e^{c_1}} \right) \right\}, \left\{ y(x) \rightarrow \frac{1}{2} \left( \sqrt{5x^2 - 4e^{c_1}} + x \right) \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 53

$$\left\{ y(x) = \frac{1}{-C1} \left( \frac{-C1 x}{2} - \frac{1}{2} \sqrt{5 - C1^2 x^2 + 4} \right), y(x) = \frac{1}{-C1} \left( \frac{-C1 x}{2} + \frac{1}{2} \sqrt{5 - C1^2 x^2 + 4} \right) \right\}$$

**2.224 ODE No. 224**

$$(2y(x) - 6x) \frac{d}{dx}y(x) - y(x) + 3x + 2 = 0$$

**Mathematica:** cpu = 0.017502 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow 3x - \frac{2}{5} \left( W \left( -e^{c_1 + \frac{25x}{4} - 1} \right) + 1 \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 35

$$\left\{ y(x) = \frac{1}{5} e^{-\text{lambertW} \left( -\frac{e^{-1}}{2} e^{\frac{25x}{4}} e^{-\frac{25-C1}{4}} \right) + \frac{25x}{4} - 1 - \frac{25-C1}{4}} + 3x - \frac{2}{5} \right\}$$

**2.225 ODE No. 225**

$$(4y(x) + 2x + 3) \frac{d}{dx}y(x) - 2y(x) - x - 1 = 0$$

**Mathematica:** cpu = 0.016002 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{8} \left( W \left( -e^{c_1 + 8x - 1} \right) + 1 \right) + \frac{1}{4} (-2x - 3) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 20

$$\left\{ y(x) = -\frac{x}{2} + \frac{\text{lambertW} \left( e^5 (e^x)^8 - C1 \right)}{8} - \frac{5}{8} \right\}$$

**2.226 ODE No. 226**

$$(4y(x) - 2x - 3) \frac{d}{dx}y(x) + 2y(x) - x - 1 = 0$$

**Mathematica:** cpu = 0.016002 (sec), leaf count = 35

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{8}(-W(-e^{c_1+8x-1}) - 1) + \frac{1}{4}(2x + 3) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 21

$$\left\{ y(x) = \frac{x}{2} - \frac{\text{lambertW}(-e^5(e^x)^8 - C1)}{8} + \frac{5}{8} \right\}$$

**2.227 ODE No. 227**

$$(4y(x) - 3x - 5) \frac{d}{dx}y(x) - 3y(x) + 7x + 2 = 0$$

**Mathematica:** cpu = 0.010501 (sec), leaf count = 107

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4}(3x + 5) - \frac{1}{2}i\sqrt{-4c_1 - 2\left(-\frac{7x^2}{2} - 2x\right) - \frac{1}{4}(3x + 5)^2} \right\}, \left\{ y(x) \rightarrow \frac{1}{4}(3x + 5) + \frac{1}{2}i\sqrt{-4c_1 - 2\left(-\frac{7x^2}{2} - 2x\right) - \frac{1}{4}(3x + 5)^2} \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 38

$$\left\{ y(x) = \frac{29}{19} - \frac{1}{38 - C1} \left( -\frac{(57x - 21) - C1}{2} + \frac{1}{2}\sqrt{-19(19x - 7)^2 - C1^2 + 4} \right) \right\}$$

**2.228 ODE No. 228**

$$(4y(x) + 11x - 11) \frac{d}{dx}y(x) - 25y(x) - 8x + 62 = 0$$

**Mathematica:** cpu = 0.196025 (sec), leaf count = 3357

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4} \left( -\frac{81(9x-1) \left( 81 \cosh\left(\frac{3c_1}{8}\right) x^2 + 81 \sinh\left(\frac{3c_1}{8}\right) x^2 - 18 \cosh\left(\frac{3c_1}{8}\right) x - 18 \sinh\left(\frac{3c_1}{8}\right) x + \cosh\left(\frac{3c_1}{8}\right) + \sinh\left(\frac{3c_1}{8}\right) - 1 \right)^3 - 258280}{\dots} \right) \right\} \right\}$$

**Maple:** cpu = 0.280 (sec), leaf count = 377

$$\left\{ y(x) = \frac{22}{9} + 36(9x - 1) \left( -1/27 \sqrt[3]{64 - 8748(9x - 1)^2 - C1} + 108 \sqrt{6561(9x - 1)^4 - C1^2} - 96(9x - 1) \right) \right.$$

## 2.229 ODE No. 229

$$(12y(x) - 5x - 8) \frac{d}{dx}y(x) - 5y(x) + 2x + 3 = 0$$

**Mathematica:** cpu = 0.010501 (sec), leaf count = 121

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{12}(5x + 8) - \frac{i\sqrt{-12c_1 - 24\left(-\frac{x^2}{12} - \frac{x}{4}\right) - \frac{1}{12}(5x + 8)^2}}{2\sqrt{3}} \right\}, \left\{ y(x) \rightarrow \frac{1}{12}(5x + 8) + \frac{i\sqrt{-12c_1 - 24\left(-\frac{x^2}{12} - \frac{x}{4}\right) - \frac{1}{12}(5x + 8)^2}}{2\sqrt{3}} \right\} \right.$$

**Maple:** cpu = 0.125 (sec), leaf count = 33

$$\left\{ y(x) = -1 - \frac{1}{-C1} \left( -\frac{(5x + 20) - C1}{12} + \frac{1}{12} \sqrt{(x + 4)^2 - C1^2 + 24} \right) \right\}$$

## 2.230 ODE No. 230

$$ay(x) \frac{d}{dx}y(x) + b(y(x))^2 + f(x) = 0$$

**Mathematica:** cpu = 0.121515 (sec), leaf count = 96

$$\left\{ \left\{ y(x) \rightarrow -e^{-\frac{bx}{a}} \sqrt{2 \int_1^x -\frac{f(K[1])e^{\frac{2bK[1]}}{a}}{a} dK[1] + c_1} \right\}, \left\{ y(x) \rightarrow e^{-\frac{bx}{a}} \sqrt{2 \int_1^x -\frac{f(K[1])e^{\frac{2bK[1]}}{a}}{a} dK[1] + c_1} \right\} \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 104

$$\left\{ y(x) = \frac{1}{a} \sqrt{-e^{2\frac{bx}{a}} a \left( -C1 a + 2 \int \left( e^{\frac{bx}{a}} \right)^2 f(x) dx \right) \left( e^{2\frac{bx}{a}} \right)^{-1}}, y(x) = -\frac{1}{a} \sqrt{-e^{2\frac{bx}{a}} a \left( -C1 a + 2 \int \left( e^{\frac{bx}{a}} \right)^2 f(x) dx \right) \left( e^{2\frac{bx}{a}} \right)^{-1}} \right.$$

**2.231 ODE No. 231**

$$(ay(x) + bx + c) \frac{d}{dx}y(x) + \alpha y(x) + \beta x + \gamma = 0$$

**Mathematica:** cpu = 2.446311 (sec), leaf count = 252

Solve

$$\left[ (\alpha - b)^2 \left( -\log \left( \frac{(ay(x)+bx+c)^2 \left( -\frac{(\alpha(bx+c)-a(\beta x+\gamma))(a(\alpha-b)y(x)+a(\beta x+\gamma)+b^2(-x)-bc)}{(ay(x)+bx+c)^2} + a\beta - \alpha b \right)}{(\alpha(bx+c)-a(\beta x+\gamma))^2} \right) - \frac{2 \tan^{-1} \left( \frac{2(a(\beta x+\gamma)-ay(x))}{(\alpha-b)\sqrt{\frac{4(a\beta-\alpha^2-2b\alpha-b^2)}{(\alpha-b)^2}}} \right)}{\sqrt{\frac{4(a\beta-\alpha^2-2b\alpha-b^2)}{(\alpha-b)^2}}} \right) \right] \frac{1}{2(a\beta - \alpha b)}$$

**Maple:** cpu = 0.156 (sec), leaf count = 206

$$\left\{ y(x) = \frac{1}{-a\beta + b\alpha} \left( -b\gamma + \beta c + \frac{x(a\beta - b\alpha) + a\gamma - \alpha c}{2a} \left( \sqrt{4a\beta - \alpha^2 - 2b\alpha - b^2} \tan \left( \text{RootOf} \left( \sqrt{4a\beta - \alpha^2 - 2b\alpha - b^2} \right) \right) \right) \right) \right\}$$

**2.232 ODE No. 232**

$$xy(x) \frac{d}{dx}y(x) + (y(x))^2 + x^2 = 0$$

**Mathematica:** cpu = 0.009001 (sec), leaf count = 56

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{2c_1 - x^4}}{\sqrt{2x}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{2c_1 - x^4}}{\sqrt{2x}} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 39

$$\left\{ y(x) = -\frac{1}{2x} \sqrt{-2x^4 + 4\_C1}, y(x) = \frac{1}{2x} \sqrt{-2x^4 + 4\_C1} \right\}$$

**2.233 ODE No. 233**

$$xy(x) \frac{d}{dx}y(x) - (y(x))^2 + ax^3 \cos(x) = 0$$

**Mathematica:** cpu = 0.024503 (sec), leaf count = 38

$$\left\{ \left\{ y(x) \rightarrow -x \sqrt{c_1 - 2a \sin(x)} \right\}, \left\{ y(x) \rightarrow x \sqrt{c_1 - 2a \sin(x)} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 30

$$\left\{ y(x) = \sqrt{-2a \sin(x) + \_C1}x, y(x) = -\sqrt{-2a \sin(x) + \_C1}x \right\}$$

**2.234 ODE No. 234**

$$xy(x) \frac{d}{dx}y(x) - (y(x))^2 + xy(x) + x^3 - 2x^2 = 0$$

**Mathematica:** cpu = 29.157203 (sec), leaf count = 33

$$\text{DSolve}[x^3 - 2x^2 + xy(x)y'(x) + xy(x) - y(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 1.731 (sec), leaf count = 0

could not solve

**2.235 ODE No. 235**

$$(xy(x) + a) \frac{d}{dx}y(x) + by(x) = 0$$

**Mathematica:** cpu = 0.042505 (sec), leaf count = 40

$$\text{Solve} \left[ x = c_1 e^{-\frac{y(x)}{b}} - \frac{a e^{-\frac{y(x)}{b}} \text{Ei} \left( \frac{y(x)}{b} \right)}{b}, y(x) \right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 30

$$\left\{ \_C1 + \left( -e^{\frac{y(x)}{b}} bx + a \text{Ei} \left( 1, -\frac{y(x)}{b} \right) \right)^{-1} = 0 \right\}$$



**2.236 ODE No. 236**

$$x(y(x) + 4) \frac{d}{dx}y(x) - (y(x))^2 - 2y(x) - 2x = 0$$

Mathematica: cpu = 0.015502 (sec), leaf count = 114

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{x \left( \frac{1}{x^2+4x} - \frac{e^{-2\left(\frac{\log(x)}{4} + \frac{3}{4} \log(x+4)\right)}}{\sqrt{c_1 - \frac{4}{x+4}}} \right)} - 4 \right\}, \left\{ y(x) \rightarrow \frac{1}{x \left( \frac{e^{-2\left(\frac{\log(x)}{4} + \frac{3}{4} \log(x+4)\right)}}{\sqrt{c_1 - \frac{4}{x+4}}} + \frac{1}{x^2+4x} \right)} - 4 \right\} \right\}$$

Maple: cpu = 0.047 (sec), leaf count = 147

$$\left\{ y(x) = -1 \left( -(x+4)^{\frac{3}{2}} \sqrt{\frac{-C_1 x + 4 - C_1 - 4}{x+4}} x + 4x^{3/2} + 16\sqrt{x} \right) \left( (x+4)^{\frac{3}{2}} \sqrt{\frac{-C_1 x + 4 - C_1 - 4}{x+4}} + \dots \right) \right\}$$

**2.237 ODE No. 237**

$$x(y(x) + a) \frac{d}{dx}y(x) + by(x) + cx = 0$$

Mathematica: cpu = 7.597465 (sec), leaf count = 24

$$\text{DSolve}[x(a + y(x))y'(x) + by(x) + cx = 0, y(x), x]$$

Maple: cpu = 2.293 (sec), leaf count = 0

could not solve

**2.238 ODE No. 238**

$$(x(y(x) + x) + a) \frac{d}{dx}y(x) - y(x)(y(x) + x) - b = 0$$

Mathematica: cpu = 0.041505 (sec), leaf count = 192

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{x \left( -\frac{x}{(a^2+ax^2+bx^2)^{3/2} \sqrt{c_1 - \frac{1}{(a+b)(a^2+ax^2+bx^2)}}} - \frac{a}{-a^2-ax^2-bx^2} \right)} - \frac{a+x^2}{x} \right\}, \left\{ y(x) \rightarrow \frac{1}{x \left( \frac{x}{(a^2+ax^2+bx^2)^{3/2} \sqrt{c_1 - \frac{1}{(a+b)(a^2+ax^2+bx^2)}}} - \frac{a}{-a^2-ax^2-bx^2} \right)} - \frac{a+x^2}{x} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 146

$$\left\{ y(x) = \frac{1}{-a^2 + \_C1} \left( -abx - \_C1 x + \sqrt{\_C1 a^2 x^2 + 2 \_C1 abx^2 + \_C1 b^2 x^2 + \_C1 a^3 + \_C1 a^2 b - \dots} \right) \right.$$

## 2.239 ODE No. 239

$$(xy(x) - x^2) \frac{d}{dx} y(x) + (y(x))^2 - 3xy(x) - 2x^2 = 0$$

**Mathematica:** cpu = 0.028504 (sec), leaf count = 54

$$\left\{ \left\{ y(x) \rightarrow x - \frac{\sqrt{e^{2c_1} + 2x^4}}{x} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{e^{2c_1} + 2x^4}}{x} + x \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 59

$$\left\{ y(x) = \frac{1}{\_C1 x} \left( x^2 \_C1 - \sqrt{2x^4 \_C1^2 + 1} \right), y(x) = \frac{1}{\_C1 x} \left( x^2 \_C1 + \sqrt{2x^4 \_C1^2 + 1} \right) \right\}$$

## 2.240 ODE No. 240

$$2xy(x) \frac{d}{dx} y(x) - (y(x))^2 + ax = 0$$

**Mathematica:** cpu = 0.008501 (sec), leaf count = 41

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{c_1 x - ax \log(x)} \right\}, \left\{ y(x) \rightarrow \sqrt{c_1 x - ax \log(x)} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 33

$$\left\{ y(x) = \sqrt{-ax \ln(x) + \_C1 x}, y(x) = -\sqrt{-ax \ln(x) + \_C1 x} \right\}$$

## 2.241 ODE No. 241

$$2xy(x) \frac{d}{dx} y(x) - (y(x))^2 + ax^2 = 0$$

**Mathematica:** cpu = 0.009001 (sec), leaf count = 41

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{c_1 x - ax^2} \right\}, \left\{ y(x) \rightarrow \sqrt{c_1 x - ax^2} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 33

$$\left\{ y(x) = \sqrt{-ax^2 + \_C1 x}, y(x) = -\sqrt{-ax^2 + \_C1 x} \right\}$$

**2.242 ODE No. 242**

$$2xy(x) \frac{d}{dx}y(x) + 2(y(x))^2 + 1 = 0$$

**Mathematica:** cpu = 0.013502 (sec), leaf count = 60

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{e^{4c_1} - x^2}}{\sqrt{2}x} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{e^{4c_1} - x^2}}{\sqrt{2}x} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 39

$$\left\{ y(x) = -\frac{1}{2x} \sqrt{-2x^2 + 4\_C1}, y(x) = \frac{1}{2x} \sqrt{-2x^2 + 4\_C1} \right\}$$

**2.243 ODE No. 243**

$$x(2y(x) + x - 1) \frac{d}{dx}y(x) - y(x)(y(x) + 2x + 1) = 0$$

**Mathematica:** cpu = 8.050022 (sec), leaf count = 487

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt[3]{2}x}{\sqrt[3]{-27c_1^2x^2 + \sqrt{108c_1^3x^3 + (27c_1^2x - 27c_1^2x^2)^2} + 27c_1^2x}} + \frac{\sqrt[3]{-27c_1^2x^2 + \sqrt{108c_1^3x^3 + (27c_1^2x - 27c_1^2x^2)^2} + 27c_1^2x}}{3\sqrt[3]{2}c_1} \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 493

$$\left\{ y(x) = \frac{3\sqrt[3]{5}}{40\_C1} \sqrt[3]{x \left( \sqrt{5} \sqrt{\frac{80x^2\_C1 - 160\_C1x + 80\_C1 - x}{\_C1}} + 20x - 20 \right) - C1^2 + \frac{3x^{5/3}}{40} \sqrt[3]{x} \right\}$$

**2.244 ODE No. 244**

$$x(2y(x) - x - 1) \frac{d}{dx}y(x) + y(x)(2x - y(x) - 1) = 0$$

**Mathematica:** cpu = 7.972512 (sec), leaf count = 484

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt[3]{2}x}{\sqrt[3]{27c_1^2x^2 + \sqrt{(27c_1^2x^2 + 27c_1^2x)^2 - 108c_1^3x^3} + 27c_1^2x}} - \frac{\sqrt[3]{27c_1^2x^2 + \sqrt{(27c_1^2x^2 + 27c_1^2x)^2 - 108c_1^3x^3} + 27c_1^2x}}{3\sqrt[3]{2}c_1} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 499

$$\left\{ y(x) = \frac{3 \sqrt[3]{5}}{40 - C1} \sqrt[3]{x \left( \sqrt{5} \sqrt{\frac{80 x^2 - C1 + 160 - C1 x + 80 - C1 - x}{-C1}} - 20 x - 20 \right) - C1^2 + \frac{3 x^{5/3}}{40} \sqrt[3]{x} \right\}$$

## 2.245 ODE No. 245

$$(2xy(x) + 4x^3) \frac{d}{dx}y(x) + (y(x))^2 + 112x^2y(x) = 0$$

**Mathematica:** cpu = 0.408552 (sec), leaf count = 1453

$$\left\{ \left\{ y(x) \rightarrow \text{Root} \left[ -1521681143169024 \#1 x^{22} - 697437190619136 \#1^2 x^{20} - 145299414712320 \#1^3 x^{18} - 18 \right] \right\} \right\}$$

**Maple:** cpu = 0.218 (sec), leaf count = 31

$$\left\{ y(x) = \frac{-C1}{x^{28} (\text{RootOf}(x^{30} - Z^{360} - 24x^{30} - Z^{330} - C1))^{330}} \right\}$$

## 2.246 ODE No. 246

$$x(3y(x) + 2x) \frac{d}{dx}y(x) + 3(y(x) + x)^2 = 0$$

**Mathematica:** cpu = 0.031504 (sec), leaf count = 80

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{6} \left( -\frac{\sqrt{2} \sqrt{3e^{4c_1} - x^4}}{x} - 4x \right) \right\}, \left\{ y(x) \rightarrow \frac{1}{6} \left( \frac{\sqrt{2} \sqrt{3e^{4c_1} - x^4}}{x} - 4x \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 63

$$\left\{ y(x) = \frac{1}{-C1 x} \left( -\frac{2x^2 - C1}{3} - \frac{1}{6} \sqrt{-2x^4 - C1^2 + 6} \right), y(x) = \frac{1}{-C1 x} \left( -\frac{2x^2 - C1}{3} + \frac{1}{6} \sqrt{-2x^4 - C1^2 + 6} \right) \right\}$$

**2.247 ODE No. 247**

$$(3x + 2)(y(x) - 2x - 1) \frac{d}{dx}y(x) - (y(x))^2 + xy(x) - 7x^2 - 9x - 3 = 0$$

**Mathematica:** cpu = 7.981514 (sec), leaf count = 693

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{\sqrt{(-324e^{2c_1}x - 216e^{2c_1} + 1458x^3 + 2916x^2 + 1944x + 432)^2 + 4(-81x^2 - 108x - 36)^3} - 6\sqrt[3]{2}}}{6\sqrt[3]{2}} \right\} \right.$$

**Maple:** cpu = 0.156 (sec), leaf count = 517

$$\left\{ y(x) = -\frac{1}{3} + \frac{3x + 2}{6} \left( 7 \left( -1/4 \sqrt[3]{2(3x + 2) - C1} - 27(3x + 2)^3 - C1^3 + 2\sqrt{-27(3x + 2)^4 - C1^4} \right) \right. \right.$$

**2.248 ODE No. 248**

$$(6xy(x) + x^2 + 3) \frac{d}{dx}y(x) + 3(y(x))^2 + 2xy(x) + 2x = 0$$

**Mathematica:** cpu = 0.013002 (sec), leaf count = 106

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{6c_1x - 2x^3 + \frac{1}{6}(x^2 + 3)^2} - \frac{x^2 + 3}{6x}}{\sqrt{6x}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{6c_1x - 2x^3 + \frac{1}{6}(x^2 + 3)^2} - \frac{x^2 + 3}{6x}}{\sqrt{6x}} \right\} \right.$$

**Maple:** cpu = 0.016 (sec), leaf count = 71

$$\left\{ y(x) = \frac{1}{6x} \left( -x^2 - 3 + \sqrt{x^4 - 12x^3 - 12 - C1x + 6x^2 + 9} \right), y(x) = -\frac{1}{6x} \left( x^2 + \sqrt{x^4 - 12x^3 - 12 - C1x + 6x^2 + 9} \right) \right.$$

**2.249 ODE No. 249**

$$(axy(x) + bx^n) \frac{d}{dx}y(x) + \alpha (y(x))^3 + \beta (y(x))^2 = 0$$

**Mathematica:** cpu = 4.954629 (sec), leaf count = 115

$$\text{Solve} \left[ \frac{(a(-n) + a + \alpha y(x))y(x)^{\frac{a-an}{\beta}-1}(\alpha y(x) + \beta)^{\frac{a(n-1)}{\beta}}}{a^2(n-1)^2(a(n-1) + \beta)} + \frac{x^{1-n} \exp\left(-\frac{a(n-1)(\log(y(x)) - \log(\alpha y(x) + \beta))}{\beta}\right)}{ab(1-n)(n-1)} = c_1, \right.$$

**Maple:** cpu = 0.156 (sec), leaf count = 202

$$\left\{ y(x) = \beta \left( \text{RootOf} \left( -_Z^{\frac{a(n-1)}{\beta}} x^{1-n} a^2 \beta n + \_C1 a^2 b n^2 - \_Z^{\frac{an-a+\beta}{\beta}} \beta a b n + \_Z^{\frac{a(n-1)}{\beta}} x^{1-n} a^2 \beta - \_Z^{\frac{a(n-1)}{\beta}} \right) \right) \right.$$

**2.250 ODE No. 250**

$$(Bxy(x) + Ax^2 + ax + by(x) + c) \frac{d}{dx}y(x) - B(g(x))^2 + Axy(x) + \alpha x + \beta y(x) + \gamma = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 5.741 (sec), leaf count = 0

could not solve

**2.251 ODE No. 251**

$$(x^2y(x) - 1) \frac{d}{dx}y(x) + x(y(x))^2 - 1 = 0$$

**Mathematica:** cpu = 0.011501 (sec), leaf count = 60

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{x^2} - \frac{\sqrt{c_1 x^2 + 2x^3 + 1}}{x^2} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{c_1 x^2 + 2x^3 + 1}}{x^2} + \frac{1}{x^2} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 50

$$\left\{ y(x) = \frac{1}{x^2} \left( 1 + \sqrt{-2x^2\_C1 + 2x^3 + 1} \right), y(x) = -\frac{1}{x^2} \left( -1 + \sqrt{-2x^2\_C1 + 2x^3 + 1} \right) \right\}$$

**2.252 ODE No. 252**

$$(x^2y(x) - 1) \frac{d}{dx}y(x) - x(y(x))^2 + 1 = 0$$

**Mathematica:** cpu = 7.835995 (sec), leaf count = 819

$$\left\{ \left\{ y(x) \rightarrow \frac{6xc_1 - x}{6c_1 - 1} + \frac{\sqrt[3]{-1944c_1^2x^3 + 648c_1x^3 - 54x^3 + 1944c_1^2 - 648c_1 + \sqrt{4(54x^2c_1 - 9x^2)^3 + (-1944c_1^2x^3 + 648c_1x^3 - 54x^3 + 1944c_1^2 - 648c_1)}}{3\sqrt[3]{2}(6c_1 - 1)} \right. \right.$$

**Maple:** cpu = 0.562 (sec), leaf count = 1623

$$\left\{ y(x) = -\frac{1}{4x^2} \left( 63x^3 - 63 \frac{x^2}{-C1x^6 - 80x^6 + 160x^3 - 80} \sqrt[3]{-C1 \left( -1 + 4 \sqrt{-\frac{5x^6 - 10x^3 + 5}{-C1x^6 - 80x^6 + 160x^3 - 80}} \right)} \right) \right.$$

**2.253 ODE No. 253**

$$(x^2y(x) - 1) \frac{d}{dx}y(x) + 8x(y(x))^2 - 8 = 0$$

**Mathematica:** cpu = 19.448470 (sec), leaf count = 28

$$\text{DSolve}[(x^2y(x) - 1) y'(x) + 8xy(x)^2 - 8 = 0, y(x), x]$$

**Maple:** cpu = 1.810 (sec), leaf count = 0

could not solve

**2.254 ODE No. 254**

$$x(xy(x) - 2) \frac{d}{dx}y(x) + x^2(y(x))^3 + x(y(x))^2 - 2y(x) = 0$$

**Mathematica:** cpu = 0.030004 (sec), leaf count = 99

$$\left\{ \left\{ y(x) \rightarrow -\frac{2x}{\frac{\sqrt{2}\sqrt{-2x(c_1 - \log(x)) - \frac{x}{2}}}{\sqrt{-\frac{1}{x^3}}} - x^2} \right. \right\}, \left\{ \left\{ y(x) \rightarrow \frac{2x}{\frac{\sqrt{2}\sqrt{-2x(c_1 - \log(x)) - \frac{x}{2}}}{\sqrt{-\frac{1}{x^3}}} + x^2} \right. \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 59

$$\left\{ y(x) = -\frac{1}{(2 \ln(x) - 2\_C1)x} \left( -1 + \sqrt{1 - 4 \ln(x) + 4\_C1} \right), y(x) = \frac{1}{(2 \ln(x) - 2\_C1)x} \left( 1 + \sqrt{1 - 4 \ln(x) + 4\_C1} \right) \right.$$

**2.255 ODE No. 255**

$$x(xy(x) - 3) \frac{d}{dx}y(x) + x(y(x))^2 - y(x) = 0$$

**Mathematica:** cpu = 5.161155 (sec), leaf count = 31

$$\left\{ \left\{ y(x) \rightarrow -\frac{3W\left(2e^{\frac{9c_1}{2^{2/3}}-1}x^{2/3}\right)}{x} \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 74

$$\left\{ y(x) = -3 \frac{\text{lambertW}\left(2/3 \sqrt[3]{-1/8 x^2 - C1}\right)}{x}, y(x) = -3 \frac{\text{lambertW}\left(1/3 \sqrt[3]{-1/8 x^2 - C1} (i\sqrt{3} - 1)\right)}{x}, y(x) \right\}$$

**2.256 ODE No. 256**

$$x^2(-1 + y(x)) \frac{d}{dx}y(x) + (x - 1)y(x) = 0$$

**Mathematica:** cpu = 0.019502 (sec), leaf count = 21

$$\left\{ \left\{ y(x) \rightarrow -W\left(x\left(-e^{\frac{1}{x}-c_1}\right)\right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 31

$$\left\{ y(x) = e^{\frac{x \ln(x) - \text{lambertW}\left(-x e^{-C1+x^{-1}}\right) x + C1 x + 1}{x}} \right\}$$

**2.257 ODE No. 257**

$$x(xy(x) + x^4 - 1) \frac{d}{dx}y(x) - y(x)(xy(x) - x^4 - 1) = 0$$

**Mathematica:** cpu = 0.358046 (sec), leaf count = 38

$$\text{Solve} \left[ \frac{c_1 + 2xy(x) - 2 \log\left(\frac{1}{1-xy(x)}\right) - 2}{x^2y(x)^2} + \frac{1}{x^4} = 0, y(x) \right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 98

$$\left\{ y(x) = \frac{-C1 + e^{\text{RootOf}\left(-2_Z x^4 (e^{-Z})^2 + 2x^4 (e^{-Z})^2 - 2e^{-Z} C1 x^4 + (e^{-Z})^2 - 2e^{-Z} C1 + C1^2\right)}}{x e^{\text{RootOf}\left(-2_Z x^4 (e^{-Z})^2 + 2x^4 (e^{-Z})^2 - 2e^{-Z} C1 x^4 + (e^{-Z})^2 - 2e^{-Z} C1 + C1^2\right)}} \right\}$$



**2.258 ODE No. 258**

$$2x^2y(x) \frac{d}{dx}y(x) + (y(x))^2 - 2x^3 - x^2 = 0$$

**Mathematica:** cpu = 0.012502 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{c_1 e^{\frac{1}{x}} + x^2} \right\}, \left\{ y(x) \rightarrow \sqrt{c_1 e^{\frac{1}{x}} + x^2} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 33

$$\left\{ y(x) = \sqrt{e^{x^{-1}} C1 + x^2}, y(x) = -\sqrt{e^{x^{-1}} C1 + x^2} \right\}$$

**2.259 ODE No. 259**

$$2x^2y(x) \frac{d}{dx}y(x) - (y(x))^2 - x^2 e^{x-x^{-1}} = 0$$

**Mathematica:** cpu = 0.019002 (sec), leaf count = 50

$$\left\{ \left\{ y(x) \rightarrow -e^{-\frac{1}{2}/x} \sqrt{c_1 + e^x} \right\}, \left\{ y(x) \rightarrow e^{-\frac{1}{2}/x} \sqrt{c_1 + e^x} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 51

$$\left\{ y(x) = \sqrt{e^{-x^{-1}} C1 + e^{\frac{x^2-1}{x}}}, y(x) = -\sqrt{e^{-x^{-1}} C1 + e^{\frac{x^2-1}{x}}} \right\}$$

**2.260 ODE No. 260**

$$(2x^2y(x) + x) \frac{d}{dx}y(x) - x^2(y(x))^3 + 2x(y(x))^2 + y(x) = 0$$

**Mathematica:** cpu = 0.012502 (sec), leaf count = 80

$$\left\{ \left\{ y(x) \rightarrow \frac{x}{\frac{\sqrt{x(c_1 - 2 \log(x) + 4x)}}{\sqrt{\frac{1}{x^3}}} - 2x^2} \right\}, \left\{ y(x) \rightarrow -\frac{x}{\frac{\sqrt{x(c_1 - 2 \log(x) + 4x)}}{\sqrt{\frac{1}{x^3}}} + 2x^2} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 59

$$\left\{ y(x) = \frac{1}{(2 \ln(x) - 2 C1) x} \left( -2 + \sqrt{4 - 2 \ln(x) + 2 C1} \right), y(x) = -\frac{1}{(2 \ln(x) - 2 C1) x} \left( 2 + \sqrt{4 - 2 \ln(x) + 2 C1} \right) \right\}$$

**2.261 ODE No. 261**

$$(2x^2y(x) - x) \frac{d}{dx}y(x) - 2x(y(x))^2 - y(x) = 0$$

**Mathematica:** cpu = 0.864110 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{2xW\left(\frac{2e^{\frac{9c_1}{2^{2/3}}-1}}{x^2}\right)} \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 18

$$\left\{ y(x) = -\frac{1}{2x} \left( \text{lambertW}\left(-\frac{C1}{2x^2}\right) \right)^{-1} \right\}$$

**2.262 ODE No. 262**

$$(2x^2y(x) - x^3) \frac{d}{dx}y(x) + (y(x))^3 - 4x(y(x))^2 + 2x^3 = 0$$

**Mathematica:** cpu = 0.081510 (sec), leaf count = 101

$$\left\{ \left\{ y(x) \rightarrow \frac{2x^3 - \sqrt{e^{4c_1}x^2 - 3e^{2c_1}x^4}}{e^{2c_1} + x^2} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{e^{4c_1}x^2 - 3e^{2c_1}x^4} + 2x^3}{e^{2c_1} + x^2} \right\} \right\}$$

**Maple:** cpu = 0.218 (sec), leaf count = 74

$$\left\{ y(x) = -\frac{x}{x^2 - C1 - 1} \left( -3x^2 - C1 + \sqrt{3x^2 - C1 + 1} + 1 \right) - x, y(x) = \frac{x}{x^2 - C1 - 1} \left( 3x^2 - C1 + \sqrt{3x^2 - C1 + 1} + 1 \right) \right\}$$

**2.263 ODE No. 263**

$$2x^3 + y(x) \frac{d}{dx}y(x) + 3x^2(y(x))^2 + 7 = 0$$

**Mathematica:** cpu = 0.036505 (sec), leaf count = 121

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{c_1 e^{-2x^3} + \frac{20 \cdot 2^{2/3} e^{-2x^3} x \Gamma\left(\frac{1}{3}, -2x^3\right)}{9\sqrt[3]{-x^3}} - \frac{2x}{3}} \right\}, \left\{ y(x) \rightarrow \sqrt{c_1 e^{-2x^3} + \frac{20 \cdot 2^{2/3} e^{-2x^3} x \Gamma\left(\frac{1}{3}, -2x^3\right)}{9\sqrt[3]{-x^3}}} \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 207

$$\left\{ y(x) = -\frac{2^{\frac{2}{3}}}{18\Gamma(2/3)} \sqrt{-3\sqrt[3]{2}\Gamma(2/3)\sqrt[3]{-x^3} \left( -27e^{-2x^3} - C1\Gamma(2/3)\sqrt[3]{2\sqrt[3]{-x^3}} + 80e^{-2x^3}x\pi\sqrt{3} - 120e^{-2x^3} \right)} \right\}$$

**2.264 ODE No. 264**

$$2x(x^3y(x) + 1) \frac{d}{dx}y(x) + (3x^3y(x) - 1)y(x) = 0$$

**Mathematica:** cpu = 0.341043 (sec), leaf count = 680

$$\left\{ \left\{ y(x) \rightarrow \text{Root} \left[ 81\#1^7 e^{\frac{21c_1}{2}} x^{12} + 756\#1^6 e^{\frac{21c_1}{2}} x^9 + 2646\#1^5 e^{\frac{21c_1}{2}} x^6 + 4116\#1^4 e^{\frac{21c_1}{2}} x^3 + 2401\#1^3 e^{\frac{21c_1}{2}} - \right. \right. \right.$$

**Maple:** cpu = 0.390 (sec), leaf count = 574

$$\left\{ y(x) = \frac{-40353607 (\text{RootOf}(9x^7 - Z^{98} - 49\_C1 - Z^{42} + 14\_C1 - Z^{21} - \_C1))^{91} \_C1 + 756315 (\text{RootOf}(9x^7 - Z^{98} - 49\_C1 - Z^{42} + 14\_C1 - Z^{21} - \_C1))^{91} \_C1}{3x^3 (\text{RootOf}(9x^7 - Z^{98} - 49\_C1 - Z^{42} + 14\_C1 - Z^{21} - \_C1))^{91} (5764801 \_C1 (\text{RootOf}(9x^7 - Z^{98} - 49\_C1 - Z^{42} + 14\_C1 - Z^{21} - \_C1))^{91} \_C1 + 756315 (\text{RootOf}(9x^7 - Z^{98} - 49\_C1 - Z^{42} + 14\_C1 - Z^{21} - \_C1))^{91} \_C1)}$$

**2.265 ODE No. 265**

$$(x^{n(n+1)}y(x) - 1) \frac{d}{dx}y(x) + 2(n+1)^2 x^{n-1} (x^{n^2} (y(x))^2 - 1) = 0$$

**Mathematica:** cpu = 407.590757 (sec), leaf count = 48

$$\text{DSolve} \left[ 2(n+1)^2 x^{n-1} (x^{n^2} y(x)^2 - 1) + (x^{n(n+1)} y(x) - 1) y'(x) = 0, y(x), x \right]$$

**Maple:** cpu = 4.680 (sec), leaf count = 0

could not solve

**2.266 ODE No. 266**

$$(y(x) - x) \sqrt{x^2 + 1} \frac{d}{dx}y(x) - a \sqrt{((y(x))^2 + 1)^3} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 1.045 (sec), leaf count = 59

$$\left\{ y(x) = \tan \left( \text{RootOf} \left( -\arctan(x) + \int^{-\arctan(x)+\_Z} -\frac{1}{2a^2 + \cos(2\_a) - 1} \left( \cos(2\_a) - 1 + \sqrt{-2a^2 \cos(2\_a) + 1} \right) \right. \right. \right.$$

**2.267 ODE No. 267**

$$y(x) \left( \frac{d}{dx} y(x) \right) (\sin(x))^2 + (y(x))^2 \cos(x) \sin(x) - 1 = 0$$

**Mathematica:** cpu = 0.033004 (sec), leaf count = 36

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{c_1 + 2x} \csc(x) \right\}, \left\{ y(x) \rightarrow \sqrt{c_1 + 2x} \csc(x) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 32

$$\left\{ y(x) = \frac{1}{\sin(x)} \sqrt{2x + \_C1}, y(x) = -\frac{1}{\sin(x)} \sqrt{2x + \_C1} \right\}$$

**2.268 ODE No. 268**

$$f(x) y(x) \frac{d}{dx} y(x) + g(x) (y(x))^2 + h(x) = 0$$

**Mathematica:** cpu = 1.005128 (sec), leaf count = 140

$$\left\{ \left\{ y(x) \rightarrow -e^{\int_1^x -\frac{g(K[1])}{f(K[1])} dK[1]} \sqrt{2 \int_1^x -\frac{h(K[2]) \exp\left(-2 \int_1^{K[2]} -\frac{g(K[1])}{f(K[1])} dK[1]\right)}{f(K[2])} dK[2] + c_1} \right\}, \left\{ y(x) \rightarrow e^{\int_1^x \dots} \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 124

$$\left\{ y(x) = 1 \sqrt{-e^{2 \int \frac{g(x)}{f(x)} dx} \left( 2 \int \frac{h(x)}{f(x)} \left( e^{\int \frac{g(x)}{f(x)} dx} \right)^2 dx - \_C1 \right) \left( e^{2 \int \frac{g(x)}{f(x)} dx} \right)^{-1}}, y(x) = -1 \sqrt{-e^{2 \int \frac{g(x)}{f(x)} dx} \left( 2 \int \frac{h(x)}{f(x)} \left( e^{\int \frac{g(x)}{f(x)} dx} \right)^2 dx - \_C1 \right) \left( e^{2 \int \frac{g(x)}{f(x)} dx} \right)^{-1}} \right\}$$

**2.269 ODE No. 269**

$$(g1(x) y(x) + g0(x)) \frac{d}{dx} y(x) - f1(x) y(x) - f2(x) (y(x))^2 - f3(x) (y(x))^3 - f0(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 2.652 (sec), leaf count = 0

could not solve

**2.270 ODE No. 270**

$$\boxed{((y(x))^2 - x) \frac{d}{dx}y(x) - y(x) + x^2 = 0}$$

**Mathematica:** cpu = 0.014502 (sec), leaf count = 327

$$\left\{ \left\{ y(x) \rightarrow -\frac{3\sqrt[3]{2}x}{\sqrt[3]{\sqrt{(81c_1 + 27x^3)^2 - 2916x^3 + 81c_1 + 27x^3}}} - \frac{\sqrt[3]{\sqrt{(81c_1 + 27x^3)^2 - 2916x^3 + 81c_1 + 27x^3}}}{3\sqrt[3]{2}} \right. \right.$$

**Maple:** cpu = 0.031 (sec), leaf count = 402

$$\left\{ y(x) = \frac{1}{2} \sqrt[3]{-4x^3 - 12\_C1 + 4\sqrt{x^6 + 6x^3\_C1 - 4x^3 + 9\_C1^2}} + 2 \frac{x}{\sqrt[3]{-4x^3 - 12\_C1 + 4\sqrt{x^6 + 6x^3\_C1 - 4x^3 + 9\_C1^2}}} \right.$$

**2.271 ODE No. 271**

$$\boxed{((y(x))^2 + x^2) \frac{d}{dx}y(x) + 2x(y(x) + 2x) = 0}$$

**Mathematica:** cpu = 0.100013 (sec), leaf count = 370

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{\sqrt{-8e^{3c_1}x^3 + e^{6c_1} + 20x^6 + e^{3c_1} - 4x^3}}}{\sqrt[3]{2}} - \frac{\sqrt[3]{2}x^2}{\sqrt[3]{\sqrt{-8e^{3c_1}x^3 + e^{6c_1} + 20x^6 + e^{3c_1} - 4x^3}}} \right. \right\}, \left\{ y(x) \right.$$

**Maple:** cpu = 0.125 (sec), leaf count = 417

$$\left\{ y(x) = 1 \left( \frac{1}{2} \sqrt[3]{4 - 16x^3\_C1^{3/2} + 4\sqrt{20\_C1^3x^6 - 8x^3\_C1^{3/2} + 1}} - 2 \frac{x^2\_C1}{\sqrt[3]{4 - 16x^3\_C1^{3/2} + 4\sqrt{20\_C1^3x^6 - 8x^3\_C1^{3/2} + 1}}} \right) \right.$$

**2.272 ODE No. 272**

$$\boxed{((y(x))^2 + x^2) \frac{d}{dx}y(x) - (y(x))^2 = 0}$$

**Mathematica:** cpu = 0.044506 (sec), leaf count = 42

$$\text{Solve} \left[ \log\left(\frac{y(x)}{x}\right) + \frac{2 \tan^{-1}\left(\frac{2y(x)-1}{\sqrt{3}}\right)}{\sqrt{3}} = c_1 - \log(x), y(x) \right]$$

**Maple:** cpu = 0.109 (sec), leaf count = 43

$$\left\{ y(x) = e^{\frac{2\sqrt{3}}{3} \text{RootOf}(-\sqrt{3}xe^{-C1} + 3 \tan(_Z)xe^{-C1} + 2\sqrt{3}e^{2/3\sqrt{3}_Z}) - _C1} \right\}$$

## 2.273 ODE No. 273

$$\boxed{((y(x))^2 + x^2 + a) \frac{d}{dx}y(x) + 2xy(x) = 0}$$

**Mathematica:** cpu = 0.014002 (sec), leaf count = 297

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{\sqrt{2916(a+x^2)^3 + 6561c_1^2 + 81c_1}}}{3\sqrt[3]{2}} - \frac{3\sqrt[3]{2}(a+x^2)}{\sqrt[3]{\sqrt{2916(a+x^2)^3 + 6561c_1^2 + 81c_1}}} \right\}, \left\{ y(x) \rightarrow \frac{x^2 + a}{2\sqrt[3]{2}} \right\} \right.$$

**Maple:** cpu = 0.015 (sec), leaf count = 470

$$\left\{ y(x) = \frac{1}{2} \sqrt[3]{-12\_C1 + 4\sqrt{4x^6 + 12ax^4 + 12a^2x^2 + 4a^3 + 9\_C1^2}} - 2 \frac{x^2 + a}{\sqrt[3]{-12\_C1 + 4\sqrt{4x^6 + 12ax^4 + 12a^2x^2 + 4a^3 + 9\_C1^2}}} \right.$$

## 2.274 ODE No. 274

$$\boxed{((y(x))^2 + x^2 + a) \frac{d}{dx}y(x) + 2xy(x) + x^2 + b = 0}$$

**Mathematica:** cpu = 0.018502 (sec), leaf count = 411

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{\sqrt{2916(a+x^2)^3 + (-81bx + 81c_1 - 27x^3)^2 - 81bx + 81c_1 - 27x^3}}}{3\sqrt[3]{2}} - \frac{x^2 + a}{\sqrt[3]{\sqrt{2916(a+x^2)^3 + (-81bx + 81c_1 - 27x^3)^2 - 81bx + 81c_1 - 27x^3}}} \right\}, \left\{ y(x) \rightarrow \frac{x^2 + a}{2\sqrt[3]{2}} \right\} \right.$$

**Maple:** cpu = 0.015 (sec), leaf count = 810

$$\left\{ y(x) = \frac{1}{2} \sqrt[3]{-4x^3 - 12bx - 12\_C1 + 4\sqrt{5x^6 + 12ax^4 + 6x^4b + 6x^3\_C1 + 12a^2x^2 + 9b^2x^2 + 18bx + 4\_C1^2}} - \frac{x^2 + a}{\sqrt[3]{-4x^3 - 12bx - 12\_C1 + 4\sqrt{5x^6 + 12ax^4 + 6x^4b + 6x^3\_C1 + 12a^2x^2 + 9b^2x^2 + 18bx + 4\_C1^2}}} \right.$$

**2.275 ODE No. 275**

$$\left( (y(x))^2 + x^2 + x \right) \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.024003 (sec), leaf count = 18

$$\text{Solve} \left[ y(x) - \tan^{-1} \left( \frac{x}{y(x)} \right) = c_1, y(x) \right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 30

$$\left\{ -C1 + \frac{e^{-2iy(x)}(ix + y(x))}{2iy(x) + 2x} = 0 \right\}$$

**2.276 ODE No. 276**

$$\left( (y(x))^2 - x^2 \right) \frac{d}{dx} y(x) + 2xy(x) = 0$$

**Mathematica:** cpu = 0.036005 (sec), leaf count = 61

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( e^{c_1} - \sqrt{e^{2c_1} - 4x^2} \right) \right\}, \left\{ y(x) \rightarrow \frac{1}{2} \left( \sqrt{e^{2c_1} - 4x^2} + e^{c_1} \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 45

$$\left\{ y(x) = \frac{1}{2\_C1} \left( 1 + \sqrt{-4\_C1^2 x^2 + 1} \right), y(x) = -\frac{1}{2\_C1} \left( -1 + \sqrt{-4\_C1^2 x^2 + 1} \right) \right\}$$

**2.277 ODE No. 277**

$$\left( (y(x))^2 + x^4 \right) \frac{d}{dx} y(x) - 4x^3 y(x) = 0$$

**Mathematica:** cpu = 0.014502 (sec), leaf count = 53

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( c_1 - \sqrt{c_1^2 + 4x^4} \right) \right\}, \left\{ y(x) \rightarrow \frac{1}{2} \left( \sqrt{c_1^2 + 4x^4} + c_1 \right) \right\} \right\}$$

**Maple:** cpu = 0.234 (sec), leaf count = 67

$$\left\{ y(x) = \left( \frac{1}{2x^2} \left( 2x^2 + \_C1 - \sqrt{4x^4 + \_C1^2} \right) - 1 \right) x^2, y(x) = \left( \frac{1}{2x^2} \left( 2x^2 + \_C1 + \sqrt{4x^4 + \_C1^2} \right) - 1 \right) x^2 \right\}$$

**2.278 ODE No. 278**

$$\left( (y(x))^2 + 4 \sin(x) \right) \frac{d}{dx} y(x) - \cos(x) = 0$$

**Mathematica:** cpu = 0.064508 (sec), leaf count = 39

$$\text{Solve} \left[ -\frac{1}{32} e^{-4y(x)} (8y(x)^2 + 4y(x) + 1) - e^{-4y(x)} \sin(x) = c_1, y(x) \right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 33

$$\left\{ -e^{-4y(x)} \sin(x) - \frac{(8(y(x))^2 + 4y(x) + 1) e^{-4y(x)}}{32} + \_C1 = 0 \right\}$$

**2.279 ODE No. 279**

$$\left( (y(x))^2 + 2y(x) + x \right) \frac{d}{dx} y(x) + (y(x) + x)^2 (y(x))^2 + y(x) (1 + y(x)) = 0$$

**Mathematica:** cpu = 0.624079 (sec), leaf count = 107

$$\left\{ \left\{ y(x) \rightarrow \frac{-\sqrt{(-c_1 x + x^2 - 1)^2 + 4(x - c_1)} + c_1 x - x^2 + 1}{2(x - c_1)} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{(-c_1 x + x^2 - 1)^2 + 4(x - c_1)}}{2(x - c_1)} \right\} \right.$$

**Maple:** cpu = 0.140 (sec), leaf count = 120

$$\left\{ y(x) = \frac{1}{2\_C1 - 4x} \left( -\_C1 x + 2x^2 - 2 + \sqrt{-\_C1^2 x^2 - 4x^3 \_C1 + 4x^4 + 4\_C1 x - 8x^2 - 8\_C1 +} \right) \right.$$

**2.280 ODE No. 280**

$$(y(x) + x)^2 \frac{d}{dx} y(x) - a^2 = 0$$

**Mathematica:** cpu = 0.036005 (sec), leaf count = 21

$$\text{Solve} \left[ y(x) - a \tan^{-1} \left( \frac{y(x) + x}{a} \right) = c_1, y(x) \right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 24

$$\{y(x) = a \text{RootOf}(\tan(\_Z) a - \_Z a + \_C1 - x) - \_C1\}$$



**2.281 ODE No. 281**

$$\left( (y(x))^2 + 2xy(x) - x^2 \right) \frac{d}{dx}y(x) - (y(x))^2 + 2xy(x) + x^2 = 0$$

**Mathematica:** cpu = 0.062508 (sec), leaf count = 75

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( e^{c_1} - \sqrt{4e^{c_1}x + e^{2c_1} - 4x^2} \right) \right\}, \left\{ y(x) \rightarrow \frac{1}{2} \left( \sqrt{4e^{c_1}x + e^{2c_1} - 4x^2} + e^{c_1} \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 53

$$\left\{ y(x) = \frac{1}{2\_C1} \left( 1 + \sqrt{-4\_C1^2x^2 + 4\_C1x + 1} \right), y(x) = -\frac{1}{2\_C1} \left( -1 + \sqrt{-4\_C1^2x^2 + 4\_C1x + 1} \right) \right\}$$

**2.282 ODE No. 282**

$$(y(x) + 3x - 1)^2 \frac{d}{dx}y(x) - (2y(x) - 1)(4y(x) + 6x - 3) = 0$$

**Mathematica:** cpu = 0.087011 (sec), leaf count = 2129

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{6}(12x + 4e^{c_1} + 1) - \frac{1}{6} \sqrt{36x^2 + 96e^{c_1}x - 12x - 16e^{c_1} + 16e^{2c_1} + 3 \cdot 2^{2/3} \sqrt[3]{-7776e^{c_1}x^5 + 6480e^{2c_1}x^4 - 1440e^{3c_1}x^3 + 144e^{4c_1}x^2 - 144e^{5c_1}x + 144e^{6c_1}}} \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 72

$$\left\{ 3 \ln \left( \frac{-6y(x) + 3}{6x - 1} \right) - \ln \left( -\frac{6y(x) - 4 + 6x}{6x - 1} \right) - 3 \ln \left( \frac{-6y(x) + 18x}{6x - 1} \right) - \ln(6x - 1) - \_C1 = 0 \right\}$$

**2.283 ODE No. 283**

$$3 \left( (y(x))^2 - x^2 \right) \frac{d}{dx}y(x) + 2(y(x))^3 - 6x(1+x)y(x) - 3e^x = 0$$

**Mathematica:** cpu = 0.046006 (sec), leaf count = 477

$$\left\{ \left\{ y(x) \rightarrow -\frac{e^{-2x} \sqrt[3]{\sqrt{(27c_1e^{4x} - 27e^{7x})^2 - 2916e^{12x}x^6 + 27c_1e^{4x} - 27e^{7x}}}}{3\sqrt[3]{2}} - \frac{3\sqrt[3]{2}}{\sqrt[3]{\sqrt{(27c_1e^{4x} - 27e^{7x})^2 - 2916e^{12x}x^6 + 27c_1e^{4x} - 27e^{7x}}}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 622

$$\left\{ y(x) = \frac{1}{2e^{2x}} \sqrt[3]{\left( 4e^{3x} - 4\_C1 + 4 \sqrt{-4x^6(e^{2x})^2 + (e^{3x})^2 - 2e^{3x}\_C1 + \_C1^2} \right) (e^{2x})^2 + 2 \sqrt[3]{\left( 4e^{3x}x \right)}} \right\}$$

**2.284 ODE No. 284**

$$\boxed{(4(y(x))^2 + x^2) \frac{d}{dx}y(x) - xy(x) = 0}$$

**Mathematica:** cpu = 0.033004 (sec), leaf count = 59

$$\left\{ \left\{ y(x) \rightarrow -\frac{x}{2\sqrt{W\left(\frac{1}{4}e^{-\frac{c_1}{2}}x^2\right)}} \right\}, \left\{ y(x) \rightarrow \frac{x}{2\sqrt{W\left(\frac{1}{4}e^{-\frac{c_1}{2}}x^2\right)}} \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 21

$$\left\{ y(x) = e^{\frac{1}{2}\text{lambertW}\left(\frac{(e^{-C1})^2x^2}{4}\right) - C1} \right\}$$

**2.285 ODE No. 285**

$$\boxed{(4(y(x))^2 + 2xy(x) + 3x^2) \frac{d}{dx}y(x) + (y(x))^2 + 6xy(x) + 2x^2 = 0}$$

**Mathematica:** cpu = 0.029004 (sec), leaf count = 402

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{\sqrt{(432e^{3c_1} + 54x^3)^2 + 3881196x^6} + 432e^{3c_1} + 54x^3}}{12\sqrt[3]{2}} - \frac{33x^2}{2 \cdot 2^{2/3} \sqrt[3]{\sqrt{(432e^{3c_1} + 54x^3)^2 + 3881196x^6} + 432e^{3c_1} + 54x^3}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 431

$$\left\{ y(x) = \frac{1}{-C1} \left( \frac{1}{4} \sqrt[3]{x^3 - C1^3 + 8 + 2\sqrt{333 - C1^6x^6 + 4x^3 - C1^3 + 16}} - \frac{11 - C1^2x^2}{4} \frac{1}{\sqrt[3]{x^3 - C1^3 + 8 + 2\sqrt{333 - C1^6x^6 + 4x^3 - C1^3 + 16}}} \right) \right\}$$

**2.286 ODE No. 286**

$$(2y(x) - 3x + 1)^2 \frac{d}{dx}y(x) - (3y(x) - 2x - 4)^2 = 0$$

**Mathematica:** cpu = 0.183523 (sec), leaf count = 3501

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

**2.287 ODE No. 287**

$$(2y(x) - 4x + 1)^2 \frac{d}{dx}y(x) - (y(x) - 2x)^2 = 0$$

**Mathematica:** cpu = 0.912616 (sec), leaf count = 77

Solve  $\left[ \frac{y(x)}{2} + \frac{1}{196} (14y(x) - (8 - 9\sqrt{2}) \log(-7y(x) + 14x + \sqrt{2} - 4) - (8 + 9\sqrt{2}) \log(7y(x) - 14x + \dots) \right]$

**Maple:** cpu = 0.063 (sec), leaf count = 56

$$\left\{ -\frac{x}{7} + \frac{4y(x)}{7} - \frac{2 \ln(7(y(x) - 2x)^2 + 8y(x) - 16x + 2)}{49} - \frac{9\sqrt{2}}{98} \operatorname{Artanh}\left(\frac{(14y(x) - 28x + 8)\sqrt{2}}{4}\right) \right\} -$$

**2.288 ODE No. 288**

$$(6(y(x))^2 - 3x^2y(x) + 1) \frac{d}{dx}y(x) - 3x(y(x))^2 + x = 0$$

**Mathematica:** cpu = 0.017502 (sec), leaf count = 534

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt[3]{4\sqrt{3}\sqrt{-54c_1x^6 + 648c_1x^2 + 432c_1^2 - 27x^8 + 207x^4 + 32} + 144c_1 - 9x^6 + 108x^2}}{4 \cdot 3^{2/3}} + \frac{1}{3\sqrt[3]{3}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 587

$$\left\{ y(x) = \frac{1}{12} \sqrt[3]{-324x^2 - 432\_C1 + 27x^6 + 12\sqrt{-81x^8 - 162\_C1x^6 + 621x^4 + 1944x^2\_C1 + 1296}} \right\}$$

**2.289 ODE No. 289**

$$(6y(x) - x)^2 \frac{d}{dx}y(x) - 6(y(x))^2 + 2xy(x) + a = 0$$

**Mathematica:** cpu = 0.016502 (sec), leaf count = 115

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{6} \left( \sqrt[3]{-18ax + 18c_1 - x^3} + x \right) \right\}, \left\{ y(x) \rightarrow \frac{x}{6} - \frac{1}{12} (1 - i\sqrt{3}) \sqrt[3]{-18ax + 18c_1 - x^3} \right\}, \left\{ y(x) \right\} \right.$$

**Maple:** cpu = 0.031 (sec), leaf count = 115

$$\left\{ y(x) = \frac{1}{6} \sqrt[3]{-x^3 - 18ax - 18\_C1} + \frac{x}{6}, y(x) = -\frac{1}{12} \sqrt[3]{-x^3 - 18ax - 18\_C1} - \frac{i}{12} \sqrt{3} \sqrt[3]{-x^3 - 18ax - 18\_C1} \right.$$

**2.290 ODE No. 290**

$$(a(y(x))^2 + 2bxy(x) + cx^2) \frac{d}{dx}y(x) + b(y(x))^2 + 2cxy(x) + dx^2 = 0$$

**Mathematica:** cpu = 0.056007 (sec), leaf count = 831

$$\left\{ \left\{ y(x) \rightarrow -\frac{bx}{a} + \frac{\sqrt[3]{-54b^3x^3 + 81abcx^3 - 27a^2dx^3 + 27a^2e^{3c_1} + \sqrt{4(9acx^2 - 9b^2x^2)^3 + (-54b^3x^3 + 81abcx^3 - 27a^2dx^3 + 27a^2e^{3c_1})^2}}{3\sqrt[3]{2a}} \right\} \right.$$

**Maple:** cpu = 0.062 (sec), leaf count = 1666

$$\left\{ y(x) = \frac{1}{\_C1} \left( \frac{1}{2a} \sqrt[3]{-4\_C1^3a^2dx^3 + 12cx^3\_C1^3ba - 8b^3x^3\_C1^3 + 4\sqrt{-C1^6a^2d^2x^6 - 6\_C1^6abcdx^3}} \right) \right.$$

**2.291 ODE No. 291**

$$(b(\beta y(x) + \alpha x)^2 - \beta(ax + by(x))) \frac{d}{dx}y(x) + a(\beta y(x) + \alpha x)^2 - \alpha(ax + by(x)) = 0$$

**Mathematica:** cpu = 0.460558 (sec), leaf count = 39

$$\text{Solve} \left[ \frac{a\beta \left( \log(ax + by(x)) + \frac{1}{\alpha x + \beta y(x)} \right)}{a\beta - \alpha b} = c_1, y(x) \right]$$

**Maple:** cpu = 0.109 (sec), leaf count = 50

$$\left\{ y(x) = \frac{-ax + e^{\text{RootOf}(-C1 a\beta x - C1 \alpha bx - Z a\beta x + Z \alpha bx - C1 \beta e^{-Z} + e^{-Z} Z \beta + b)}}{b} \right\}$$

## 2.292 ODE No. 292

$$(ay(x) + bx + c)^2 \frac{d}{dx}y(x) + (\alpha y(x) + \beta x + \gamma)^2 = 0$$

**Mathematica:** cpu = 54.667442 (sec), leaf count = 760

$$\text{Solve} \left[ (\alpha b - a\beta) \text{RootSum} \left[ \#1^3 a\beta^3 - \#1^3 \alpha b\beta^2 + 2\#1^2 a\alpha\beta^2 y(x) + \#1^2 ab^2\beta y(x) + 3\gamma\#1^2 a\beta^2 - 2\#1^2 \alpha^2 b \right. \right.$$

**Maple:** cpu = 0.031 (sec), leaf count = 124

$$\left\{ y(x) = \frac{1}{-a\beta + b\alpha} \left( -\gamma b + \beta c + \text{RootOf} \left( \int^{-Z} \frac{-a^2 a^2 - 2_a ab + b^2}{-a^3 a^2 - 2_a^2 ab - a^2 \alpha^2 + 2_a \alpha \beta + a b^2 - \beta^2} d_a \right. \right. \right.$$

## 2.293 ODE No. 293

$$x((y(x))^2 - 3x) \frac{d}{dx}y(x) + 2(y(x))^3 - 5xy(x) = 0$$

**Mathematica:** cpu = 0.105513 (sec), leaf count = 661

$$\left\{ \left\{ y(x) \rightarrow \text{Root} \left[ -\#1^{15} - \frac{25\#1^2 e^{\frac{65c_1}{2}}}{x^{26}} + \frac{65e^{\frac{65c_1}{2}}}{x^{25}} \&, 1 \right] \right\}, \left\{ y(x) \rightarrow \text{Root} \left[ -\#1^{15} - \frac{25\#1^2 e^{\frac{65c_1}{2}}}{x^{26}} + \frac{65e^{\frac{65c_1}{2}}}{x^{25}} \right. \right. \right.$$

**Maple:** cpu = 0.234 (sec), leaf count = 36

$$\left\{ \ln(x) - C1 + \frac{6}{13} \ln \left( y(x) \frac{1}{\sqrt{x}} \right) - \frac{2}{65} \ln \left( -\frac{5(y(x))^2 + 13x}{x} \right) = 0 \right\}$$

**2.294 ODE No. 294**

$$x((y(x))^2 + x^2 - a) \frac{d}{dx}y(x) - y(x)((y(x))^2 + x^2 + a) = 0$$

**Mathematica:** cpu = 0.040005 (sec), leaf count = 71

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( c_1 x - \sqrt{-4a + c_1^2 x^2 + 4x^2} \right) \right\}, \left\{ y(x) \rightarrow \frac{1}{2} \left( \sqrt{-4a + c_1^2 x^2 + 4x^2} + c_1 x \right) \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 112

$$\left\{ \left( (y(x))^{-2} - (-x^2 + a)^{-1} \right)^{-1} = -x\sqrt{x^2 - a} \frac{1}{\sqrt{-C1 + 4 \frac{a}{x^2 - a}}} + \frac{x^2}{2} - \frac{a}{2}, \left( (y(x))^{-2} - (-x^2 + a)^{-1} \right)^{-1} = \dots \right\}$$

**2.295 ODE No. 295**

$$x((y(x))^2 + xy(x) - x^2) \frac{d}{dx}y(x) - (y(x))^3 + x(y(x))^2 + x^2y(x) = 0$$

**Mathematica:** cpu = 0.036505 (sec), leaf count = 31

$$\text{Solve} \left[ \frac{x}{y(x)} + \frac{y(x)}{x} + \log \left( \frac{y(x)}{x} \right) = c_1 - 2 \log(x), y(x) \right]$$

**Maple:** cpu = 0.141 (sec), leaf count = 29

$$\left\{ y(x) = e^{\text{RootOf}((e^{-z})^2 + 2e^{-z} \ln(x) + 2e^{-z} - C1 + z e^{-z} + 1)} x \right\}$$

**2.296 ODE No. 296**

$$x((y(x))^2 + x^2y(x) + x^2) \frac{d}{dx}y(x) - 2(y(x))^3 - 2x^2(y(x))^2 + x^4 = 0$$

**Mathematica:** cpu = 0.571072 (sec), leaf count = 102

$$\left\{ \left\{ y(x) \rightarrow -e^{-c_1} x^2 - e^{-c_1} \sqrt{-e^{c_1} x^4 + e^{2c_1} x^2 + x^4} \right\}, \left\{ y(x) \rightarrow e^{-c_1} \sqrt{-e^{c_1} x^4 + e^{2c_1} x^2 + x^4} - e^{-c_1} x^2 \right\} \right\}$$

**Maple:** cpu = 0.562 (sec), leaf count = 165

$$\left\{ y(x) = -x^3(x - 2) \left( \frac{1}{(x - 2)x^2} \left( -C1 x - x^2 - \sqrt{-C1 x^4 + C1^2 x^2 + x^4} \right) - 1 \right) \left( -C1 x - x^2 - \sqrt{-C1 x^4 + C1^2 x^2 + x^4} \right) \right\}$$

**2.297 ODE No. 297**

$$2x((y(x))^2 + 5x^2) \frac{d}{dx}y(x) + (y(x))^3 - x^2y(x) = 0$$

**Mathematica:** cpu = 0.058007 (sec), leaf count = 216

$$\left\{ \left\{ y(x) \rightarrow \text{Root} \left[ -\#1^5 + \frac{\#1^2 e^{3c_1}}{x^{3/2}} + 3e^{3c_1} \sqrt{x} \&, 1 \right] \right\}, \left\{ y(x) \rightarrow \text{Root} \left[ -\#1^5 + \frac{\#1^2 e^{3c_1}}{x^{3/2}} + 3e^{3c_1} \sqrt{x} \&, 2 \right] \right\} \right\}$$

**Maple:** cpu = 0.219 (sec), leaf count = 29

$$\left\{ y(x) = (\text{RootOf}(x^9 \_C1 \_Z^{45} - \_Z^{18} - 6 \_Z^9 - 9))^{\frac{9}{2}} x \right\}$$

**2.298 ODE No. 298**

$$3x(y(x))^2 \frac{d}{dx}y(x) + (y(x))^3 - 2x = 0$$

**Mathematica:** cpu = 0.009001 (sec), leaf count = 72

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{c_1 + x^2}}{\sqrt[3]{x}} \right\}, \left\{ y(x) \rightarrow -\frac{\sqrt[3]{-1} \sqrt[3]{c_1 + x^2}}{\sqrt[3]{x}} \right\}, \left\{ y(x) \rightarrow \frac{(-1)^{2/3} \sqrt[3]{c_1 + x^2}}{\sqrt[3]{x}} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 99

$$\left\{ y(x) = \frac{1}{x} \sqrt[3]{(x^2 + \_C1) x^2}, y(x) = -\frac{1}{2x} \sqrt[3]{(x^2 + \_C1) x^2} - \frac{i\sqrt{3}}{x} \sqrt[3]{(x^2 + \_C1) x^2}, y(x) = -\frac{1}{2x} \sqrt[3]{(x^2 + \_C1) x^2} + \frac{i\sqrt{3}}{x} \sqrt[3]{(x^2 + \_C1) x^2} \right\}$$

**2.299 ODE No. 299**

$$(3x(y(x))^2 - x^2) \frac{d}{dx}y(x) + (y(x))^3 - 2xy(x) = 0$$

**Mathematica:** cpu = 0.017002 (sec), leaf count = 371

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt[3]{\frac{2}{3}x^2}}{\sqrt[3]{9c_1x^2 + \sqrt{3}\sqrt{27c_1^2x^4 - 4x^9}}} - \frac{\sqrt[3]{9c_1x^2 + \sqrt{3}\sqrt{27c_1^2x^4 - 4x^9}}}{\sqrt[3]{23^{2/3}x}} \right\}, \left\{ y(x) \rightarrow \frac{(1 - \sqrt{3}) \sqrt[3]{9c_1x^2 + \sqrt{3}\sqrt{27c_1^2x^4 - 4x^9}}}{2^{2/3} \sqrt[3]{3} \sqrt[3]{9c_1x^2 + \sqrt{3}\sqrt{27c_1^2x^4 - 4x^9}}} \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 327

$$\left\{ y(x) = \frac{1}{6x} \sqrt[3]{\left(12 \sqrt{-12x^5 + 81 \_C1^2} + 108 \_C1\right) x^2} + 2 \frac{x^2}{\sqrt[3]{\left(12 \sqrt{-12x^5 + 81 \_C1^2} + 108 \_C1\right) x^2}}, \left\{ y(x) = \frac{1}{6x} \sqrt[3]{\left(12 \sqrt{-12x^5 + 81 \_C1^2} + 108 \_C1\right) x^2} - 2 \frac{x^2}{\sqrt[3]{\left(12 \sqrt{-12x^5 + 81 \_C1^2} + 108 \_C1\right) x^2}}, \left\{ y(x) = \frac{1}{6x} \sqrt[3]{\left(12 \sqrt{-12x^5 + 81 \_C1^2} + 108 \_C1\right) x^2} - 2 \frac{x^2}{\sqrt[3]{\left(12 \sqrt{-12x^5 + 81 \_C1^2} + 108 \_C1\right) x^2}} \right\} \right\}$$

### 2.300 ODE No. 300

$$6x(y(x))^2 \frac{d}{dx}y(x) + 2(y(x))^3 + x = 0$$

**Mathematica:** cpu = 0.009501 (sec), leaf count = 99

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{4c_1 - x^2}}{2^{2/3}\sqrt[3]{x}} \right\}, \left\{ y(x) \rightarrow -\frac{\sqrt[3]{-1}\sqrt[3]{4c_1 - x^2}}{2^{2/3}\sqrt[3]{x}} \right\}, \left\{ y(x) \rightarrow \frac{(-1)^{2/3}\sqrt[3]{4c_1 - x^2}}{2^{2/3}\sqrt[3]{x}} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 120

$$\left\{ y(x) = \frac{1}{2x} \sqrt[3]{(-2x^2 + 8\_C1)x^2}, y(x) = -\frac{1}{4x} \sqrt[3]{(-2x^2 + 8\_C1)x^2} - \frac{i\sqrt{3}}{x} \sqrt[3]{(-2x^2 + 8\_C1)x^2}, y(x) \right\}$$

### 2.301 ODE No. 301

$$(6x(y(x))^2 + x^2) \frac{d}{dx}y(x) - y(x)(3(y(x))^2 - x) = 0$$

**Mathematica:** cpu = 0.039005 (sec), leaf count = 64

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{x}\sqrt{W\left(\frac{6e^{3c_1}}{x^3}\right)}}{\sqrt{6}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{x}\sqrt{W\left(\frac{6e^{3c_1}}{x^3}\right)}}{\sqrt{6}} \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 25

$$\left\{ y(x) = \frac{1}{x} e^{-\frac{1}{2} \text{lambertW}\left(6 \frac{e^{3-C1}}{x^3}\right) + \frac{3-C1}{2}} \right\}$$

### 2.302 ODE No. 302

$$(x^2(y(x))^2 + x) \frac{d}{dx}y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.016002 (sec), leaf count = 70

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1x - \sqrt{x}\sqrt{c_1^2x + 4}}{2x} \right\}, \left\{ y(x) \rightarrow \frac{c_1x + \sqrt{x}\sqrt{c_1^2x + 4}}{2x} \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 137

$$\left\{ y(x) = -\frac{1}{2\_C1x} \sqrt{-2x\_C1 \left(-2\_C1 - x + \sqrt{4\_C1x + x^2}\right)}, y(x) = \frac{1}{2\_C1x} \sqrt{-2x\_C1 \left(-2\_C1 - x + \sqrt{4\_C1x + x^2}\right)} \right\}$$



### 2.303 ODE No. 303

$$(xy(x) - 1)^2 x \frac{d}{dx}y(x) + (x^2(y(x))^2 + 1)y(x) = 0$$

**Mathematica:** cpu = 0.044006 (sec), leaf count = 25

$$\text{Solve}\left[xy(x) - \frac{1}{xy(x)} - 2\log(y(x)) = c_1, y(x)\right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 34

$$\left\{y(x) = \frac{e^{\text{RootOf}(-2e^{-Z}\ln(x)-e^{2-Z}+2e^{-Z}-C1+2-Ze^{-Z}+1)}}{x}\right\}$$

### 2.304 ODE No. 304

$$(10x^3(y(x))^2 + x^2y(x) + 2x) \frac{d}{dx}y(x) + 5x^2(y(x))^3 + x(y(x))^2 = 0$$

**Mathematica:** cpu = 45.176237 (sec), leaf count = 59

$$\text{Solve}\left[-y(x) \left(\frac{\log(5x^2y(x)^2 + 2)}{2y(x)} + \frac{\tan^{-1}\left(\sqrt{\frac{5}{2}}xy(x)\right)}{\sqrt{10}y(x)}\right) - \log(y(x)) = c_1, y(x)\right]$$

**Maple:** cpu = 0.156 (sec), leaf count = 44

$$\left\{y(x) = \frac{\sqrt{10}}{5x} \tan\left(\text{RootOf}\left(\sqrt{10}\ln\left(\frac{4(\tan(_Z))^2((\tan(_Z))^2 + 1)}{5x^2}\right) + 2\sqrt{10}-C1 + 2-Z\right)\right)\right\}$$

### 2.305 ODE No. 305

$$((y(x))^3 - 3x) \frac{d}{dx}y(x) - 3y(x) + x^2 = 0$$

**Mathematica:** cpu = 0.017502 (sec), leaf count = 1277

$$\left\{\left\{y(x) \rightarrow -\frac{1}{2}\sqrt{\frac{16\sqrt[3]{2}(x^3 + 3c_1)}{\sqrt[3]{104976x^2 - \sqrt{11019960576x^4 - 4(144x^3 + 432c_1)^3}} + \sqrt[3]{104976x^2 - \sqrt{11019960576x^4 - 4(144x^3 + 432c_1)^3}}}}{9\sqrt[3]{2}}}\right\}\right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 21

$$\left\{ \frac{x^3}{3} - 3xy(x) + \frac{(y(x))^4}{4} + \_C1 = 0 \right\}$$

### 2.306 ODE No. 306

$$\left( (y(x))^3 - x^3 \right) \frac{d}{dx} y(x) - x^2 y(x) = 0$$

**Mathematica:** cpu = 0.051007 (sec), leaf count = 201

$$\left\{ \left\{ y(x) \rightarrow \sqrt[3]{x^3 - \sqrt{x^6 - e^{6c_1}}} \right\}, \left\{ y(x) \rightarrow -\sqrt[3]{-1} \sqrt[3]{x^3 - \sqrt{x^6 - e^{6c_1}}} \right\}, \left\{ y(x) \rightarrow (-1)^{2/3} \sqrt[3]{x^3 - \sqrt{x^6 - e^{6c_1}}} \right\} \right\}$$

**Maple:** cpu = 0.250 (sec), leaf count = 391

$$\left\{ y(x) = x \frac{1}{\sqrt[3]{-(x^3\_C1 - \sqrt{-C1^2 x^6 + 1}) x^3\_C1}}, y(x) = x \frac{1}{\sqrt[3]{-(x^3\_C1 + \sqrt{-C1^2 x^6 + 1}) x^3\_C1}}, y(x) = \dots \right\}$$

### 2.307 ODE No. 307

$$\left( (y(x))^2 + x^2 + a \right) y(x) \frac{d}{dx} y(x) + \left( (y(x))^2 + x^2 - a \right) x = 0$$

**Mathematica:** cpu = 0.024003 (sec), leaf count = 149

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{-\sqrt{a^2 + 4ax^2 + 4c_1} - a - x^2} \right\}, \left\{ y(x) \rightarrow \sqrt{-\sqrt{a^2 + 4ax^2 + 4c_1} - a - x^2} \right\}, \left\{ y(x) \rightarrow \dots \right\} \right\}$$

**Maple:** cpu = 0.046 (sec), leaf count = 125

$$\left\{ y(x) = \sqrt{-x^2 - a - \sqrt{4ax^2 + a^2 - 4\_C1}}, y(x) = \sqrt{-x^2 - a + \sqrt{4ax^2 + a^2 - 4\_C1}}, y(x) = -\sqrt{-x^2 - a - \sqrt{4ax^2 + a^2 - 4\_C1}} \right\}$$

**2.308 ODE No. 308**

$$2(y(x))^3 \frac{d}{dx}y(x) + x(y(x))^2 = 0$$

**Mathematica:** cpu = 0.007001 (sec), leaf count = 55

$$\left\{ \left\{ y(x) \rightarrow 0 \right\}, \left\{ y(x) \rightarrow -\frac{\sqrt{4c_1 - x^2}}{\sqrt{2}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{4c_1 - x^2}}{\sqrt{2}} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 37

$$\left\{ y(x) = 0, y(x) = -\frac{1}{2}\sqrt{-2x^2 + 4\_C1}, y(x) = \frac{1}{2}\sqrt{-2x^2 + 4\_C1} \right\}$$

**2.309 ODE No. 309**

$$(2(y(x))^3 + y(x)) \frac{d}{dx}y(x) - 2x^3 - x = 0$$

**Mathematica:** cpu = 0.011001 (sec), leaf count = 151

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{-\sqrt{8c_1 + 4x^4 + 4x^2 + 1} - 1}}{\sqrt{2}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{-\sqrt{8c_1 + 4x^4 + 4x^2 + 1} - 1}}{\sqrt{2}} \right\}, \left\{ y(x) \rightarrow -\sqrt{\sqrt{8c_1 + 4x^4 + 4x^2 + 1} - 1} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 113

$$\left\{ y(x) = -\frac{1}{2}\sqrt{-2 - 2\sqrt{4x^4 + 4x^2 + 8\_C1 + 1}}, y(x) = \frac{1}{2}\sqrt{-2 - 2\sqrt{4x^4 + 4x^2 + 8\_C1 + 1}}, y(x) = -\sqrt{\sqrt{4x^4 + 4x^2 + 8\_C1 + 1} - 1} \right\}$$

**2.310 ODE No. 310**

$$(2(y(x))^3 + 5x^2y(x)) \frac{d}{dx}y(x) + 5x(y(x))^2 + x^3 = 0$$

**Mathematica:** cpu = 0.044006 (sec), leaf count = 159

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{-\sqrt{2e^{4c_1} + 23x^4 - 5x^2}}}{\sqrt{2}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{-\sqrt{2e^{4c_1} + 23x^4 - 5x^2}}}{\sqrt{2}} \right\}, \left\{ y(x) \rightarrow -\frac{\sqrt{\sqrt{2e^{4c_1} + 23x^4 - 5x^2}}}{\sqrt{2}} \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 125

$$\left\{ y(x) = -\frac{1}{2}\sqrt{-10x^2\_C1 - 2\sqrt{23x^4\_C1^2 + 2}}\frac{1}{\sqrt{-C1}}, y(x) = \frac{1}{2}\sqrt{-10x^2\_C1 - 2\sqrt{23x^4\_C1^2 + 2}}\frac{1}{\sqrt{-C1}}, y(x) = -\frac{\sqrt{\sqrt{23x^4\_C1^2 + 2}}}{\sqrt{-C1}} \right\}$$

### 2.311 ODE No. 311

$$(20(y(x))^3 - 3x(y(x))^2 + 6x^2y(x) + 3x^3) \frac{d}{dx}y(x) - (y(x))^3 + 6x(y(x))^2 + 9x^2y(x) + 4x^3 = 0$$

**Mathematica:** cpu = 0.051506 (sec), leaf count = 2201

$$\left\{ \left\{ y(x) \rightarrow \frac{x}{20} + \frac{1}{2} \sqrt{-\frac{39x^2}{100} + \frac{\sqrt[3]{99x^6 + 351e^{c_1x^2} + \sqrt{3}\sqrt{-67037x^{12} + 185406e^{c_1x^8} - 83733e^{2c_1x^4} + 320}}{5\sqrt[3]{23^2/3}}}} \right. \right.$$

**Maple:** cpu = 0.062 (sec), leaf count = 50

$$\left\{ y(x) = \frac{\text{RootOf}(x^4\_C1^4 + 3x^3\_C1^3\_Z + 3\_C1^2\_Z^2x^2 -\_C1\_Z^3x + 5\_Z^4 - 1)}{\_C1} \right\}$$

### 2.312 ODE No. 312

$$\left( \frac{(y(x))^2}{b} + \frac{x^2}{a} \right) \left( y(x) \frac{d}{dx}y(x) + x \right) + \frac{(a-b)(y(x) \frac{d}{dx}y(x) - x)}{a+b} = 0$$

**Mathematica:** cpu = 0.245531 (sec), leaf count = 204

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{b} \sqrt{a^2 + 2a^2 W \left( \frac{c_1(a+b)e^{\frac{bx^2}{2a^2} - \frac{b}{2a} - \frac{x^2}{2b} - \frac{1}{2}} \right) + ab - ax^2 - bx^2}}{\sqrt{a}\sqrt{a+b}} \right. \right\}, \left\{ y(x) \rightarrow -\frac{\sqrt{b} \sqrt{a^2 + 2a^2 W \left( \dots \right)}}{\sqrt{a}\sqrt{a+b}} \right\}$$

**Maple:** cpu = 1.061 (sec), leaf count = 236

$$\left\{ y(x) = \frac{1}{a} \sqrt{a \left( -bx^2 + ab + e^{-\frac{1}{2a^2b}} \left( 2 \text{lambertW} \left( 1/2 \frac{(a+b)e^{-1/2}}{a^2b} e^{-1/2} \frac{x^2}{b} e^{1/2} \frac{bx^2}{a^2} e^{-1/2} \frac{b}{a} \left( e^{-\frac{C1}{ab}} \right)^{-1} \right) a^2b + a^2x^2 - b^2x^2 + a^2b + \dots \right)} \right)}$$

### 2.313 ODE No. 313

$$(2a(y(x))^3 + 3ax(y(x))^2 - bx^3 + cx^2) \frac{d}{dx}y(x) - a(y(x))^3 + c(y(x))^2 + 3bx^2y(x) + 2bx^3 = 0$$

**Mathematica:** cpu = 0.069009 (sec), leaf count = 537

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{2}(3acx + 3ac_1)}{3a\sqrt[3]{\sqrt{(27a^2bx^3 + 27a^2c_1x)^2 + 4(3acx + 3ac_1)^3 + 27a^2bx^3 + 27a^2c_1x}}} - \sqrt[3]{\sqrt{(27a^2bx^3 + 27a^2c_1x)^2 + 4(3acx + 3ac_1)^3 + 27a^2bx^3 + 27a^2c_1x}} \right. \right.$$

**Maple:** cpu = 0.156 (sec), leaf count = 912

$$\left\{ y(x) = \frac{1}{6a} \sqrt[3]{\left( -108bx^3 + 108\_C1x + 12\sqrt{-\frac{-81ab^2x^6 + 162\_C1abx^4 - 12c^3x^3 - 81\_C1^2ax^2 + 3c^2x}{a}} \right)} \right.$$

### 2.314 ODE No. 314

$$x(y(x))^3 \frac{d}{dx}y(x) + (y(x))^4 - x \sin(x) = 0$$

**Mathematica:** cpu = 0.042505 (sec), leaf count = 188

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt[4]{c_1 - 4x^4 \cos(x) + 16x^3 \sin(x) + 48x^2 \cos(x) - 96x \sin(x) - 96 \cos(x)}}{x} \right\}, \left\{ y(x) \rightarrow -\frac{i\sqrt[4]{c_1}}{x} \right\} \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 170

$$\left\{ y(x) = \frac{1}{x} \sqrt[4]{-4x^4 \cos(x) + 16 \sin(x)x^3 + 48x^2 \cos(x) - 96 \cos(x) - 96x \sin(x) + \_C1}, y(x) = \frac{-i}{x} \sqrt[4]{c_1} \right.$$

### 2.315 ODE No. 315

$$(2x(y(x))^3 - x^4) \frac{d}{dx}y(x) - (y(x))^4 + 2x^3y(x) = 0$$

**Mathematica:** cpu = 0.114515 (sec), leaf count = 368

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{\frac{2}{3}e^{c_1x}}}{\sqrt[3]{\sqrt{3}\sqrt{27x^6 - 4e^{3c_1x}x^3 - 9x^3}}} + \frac{\sqrt[3]{\sqrt{3}\sqrt{27x^6 - 4e^{3c_1x}x^3 - 9x^3}}}{\sqrt[3]{23^{2/3}}} \right\}, \left\{ y(x) \rightarrow -\frac{(1+i)}{2^{2/3}\sqrt[3]{3}\sqrt[3]{\sqrt{3}\sqrt{27x^6 - 4e^{3c_1x}x^3 - 9x^3}}} \right\} \right.$$

**Maple:** cpu = 0.062 (sec), leaf count = 447

$$\left\{ y(x) = \frac{\sqrt[3]{12}}{6-C1} \sqrt[3]{x \left( -9x^2 - C1 + \sqrt{3} \sqrt{\frac{x(27x^3 - C1^3 - 4)}{-C1}} \right)} - C1^2 + \frac{x12^{\frac{2}{3}}}{6} \frac{1}{\sqrt[3]{x \left( -9x^2 - C1 + \sqrt{3} \sqrt{\frac{x(27x^3 - C1^3 - 4)}{-C1}} \right)}} \right\}$$

### 2.316 ODE No. 316

$$(2x(y(x))^3 + y(x)) \frac{d}{dx} y(x) + 2(y(x))^2 = 0$$

**Mathematica:** cpu = 0.039005 (sec), leaf count = 48

$$\left\{ \{y(x) \rightarrow 0\}, \text{Solve} \left[ x = c_1 e^{-\frac{1}{2}y(x)^2} - \frac{1}{4} e^{-\frac{1}{2}y(x)^2} \text{Ei} \left( \frac{y(x)^2}{2} \right), y(x) \right] \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 53

$$\left\{ y(x) = 0, y(x) = \sqrt{-2 \text{RootOf}(e^{-Z} \text{Ei}(1, -Z) + 4e^{-Z} - C1 - 4x)}, y(x) = -\sqrt{-2 \text{RootOf}(e^{-Z} \text{Ei}(1, -Z) + 4e^{-Z} - C1 - 4x)} \right\}$$

### 2.317 ODE No. 317

$$(2x(y(x))^3 + xy(x) + x^2) \frac{d}{dx} y(x) + (y(x))^2 - xy(x) = 0$$

**Mathematica:** cpu = 0.320541 (sec), leaf count = 23

$$\text{Solve} \left[ y(x)^2 - \frac{x}{y(x)} + \log(y(x)) + \log(x) = c_1, y(x) \right]$$

**Maple:** cpu = 0.093 (sec), leaf count = 29

$$\left\{ y(x) = e^{\text{RootOf}(-e^{-Z})^3 - e^{-Z} \ln(x) + e^{-Z} - C1 - Z e^{-Z} + x)} \right\}$$

**2.318 ODE No. 318**

$$(3x(y(x))^3 - 4xy(x) + y(x)) \frac{d}{dx}y(x) + (y(x))^2 ((y(x))^2 - 2) = 0$$

**Mathematica:** cpu = 0.060008 (sec), leaf count = 4284

$$\left\{ \left\{ y(x) \rightarrow 0 \right\}, \left\{ y(x) \rightarrow -\sqrt{\frac{4\sqrt[3]{2}x^2}{3\sqrt[3]{16x^6 + 24x^5 - 27c_1^2x^4 + 12x^4 + 2x^3 + 3\sqrt{3}\sqrt{-32c_1^2x^{10} - 48c_1^2x^9 + 27c_1^4x^8}}}} \right\} \right.$$

**Maple:** cpu = 0.016 (sec), leaf count = 28

$$\left\{ x + (y(x))^{-2} - \frac{-C1}{(y(x))^2} \frac{1}{\sqrt{(y(x))^2 - 2}} = 0, y(x) = 0 \right\}$$

**2.319 ODE No. 319**

$$(7x(y(x))^3 + y(x) - 5x) \frac{d}{dx}y(x) + (y(x))^4 - 5y(x) = 0$$

**Mathematica:** cpu = 0.023503 (sec), leaf count = 302

$$\left\{ \left\{ y(x) \rightarrow \text{Root}[10\#1^7x + 2\#1^5 - 100\#1^4x - 25\#1^2 + 250\#1x - 10c_1\&, 1] \right\}, \left\{ y(x) \rightarrow \text{Root}[10\#1^7x + \dots] \right\} \right.$$

**Maple:** cpu = 0.031 (sec), leaf count = 33

$$\left\{ x - \frac{1}{y(x)((y(x))^3 - 5)^2} \left( -\frac{(y(x))^5}{5} + \frac{5(y(x))^2}{2} + -C1 \right) = 0 \right\}$$

**2.320 ODE No. 320**

$$(x^2(y(x))^3 + xy(x)) \frac{d}{dx}y(x) - 1 = 0$$

**Mathematica:** cpu = 0.057007 (sec), leaf count = 76

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{2xW\left(c_1e^{\frac{1}{2x}-1}\right) + 2x - 1}}{\sqrt{x}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{2xW\left(c_1e^{\frac{1}{2x}-1}\right) + 2x - 1}}{\sqrt{x}} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 70

$$\left\{ y(x) = \frac{1}{x} \sqrt{x \left( 2 \operatorname{lambertW} \left( \frac{1}{2} \_C1 e^{-1/2 \frac{2x-1}{x}} \right) x + 2x - 1 \right)}, y(x) = -\frac{1}{x} \sqrt{x \left( 2 \operatorname{lambertW} \left( \frac{1}{2} \_C1 e^{-1/2 \frac{2x-1}{x}} \right) x + 2x - 1 \right)} \right.$$

### 2.321 ODE No. 321

$$(2x^2(y(x))^3 + x^2(y(x))^2 - 2x) \frac{d}{dx}y(x) - 2y(x) - 1 = 0$$

**Mathematica:** cpu = 0.181023 (sec), leaf count = 47

$$\text{Solve} \left[ \frac{1}{64} (-4y(x)^2 + 4y(x) - 2 \log(8y(x) + 4) + 3) - \frac{1}{4x(2y(x) + 1)} = c_1, y(x) \right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 42

$$\left\{ y(x) = \frac{e^{\operatorname{RootOf}(x(e^{-z})^3 - 4x(e^{-z})^2 + 8\_C1 x e^{-z} + 2\_Z x e^{-z} + 3x e^{-z} + 16)}}{2} - \frac{1}{2} \right\}$$

### 2.322 ODE No. 322

$$(10x^2(y(x))^3 - 3(y(x))^2 - 2) \frac{d}{dx}y(x) + 5x(y(x))^4 + x = 0$$

**Mathematica:** cpu = 0.024503 (sec), leaf count = 2077

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{2} \sqrt{\frac{4\sqrt[3]{2}(5x^4 - 10c_1x^2 - 2)}{5x^2\sqrt[3]{2268x^2 - 216c_1} + \sqrt{(2160x^2 + 108(x^2 - 2c_1))^2 - 4(60x^4 - 120c_1x^2 - 24)^3}} + \sqrt[3]{\dots}} \right. \right.$$

**Maple:** cpu = 0.031 (sec), leaf count = 28

$$\left\{ \frac{x^2(5(y(x))^4 + 1)}{2} - (y(x))^3 - 2y(x) + \_C1 = 0 \right\}$$



**2.323 ODE No. 323**

$$(ax(y(x))^3 + c) x \frac{d}{dx}y(x) + (bx^3y(x) + c) y(x) = 0$$

**Mathematica:** cpu = 0.032004 (sec), leaf count = 463

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{54a^2cx^2 + \sqrt{2916a^4c^2x^4 + 108a^3x^3(bx^3 - 2c_1x)^3}}}{3\sqrt[3]{2ax}} - \frac{\sqrt[3]{2}(bx^3 - 2c_1x)}{\sqrt[3]{54a^2cx^2 + \sqrt{2916a^4c^2x^4 + 108a^3x^3(bx^3 - 2c_1x)^3}}} \right. \right.$$

**Maple:** cpu = 0.093 (sec), leaf count = 761

$$\left\{ y(x) = \frac{1}{3ax} \sqrt[3]{\left(27c + 3\sqrt{-\frac{-3b^3x^8 + 18\_C1b^2x^6 - 36\_C1^2bx^4 + 24\_C1^3x^2 - 81c^2a}{a}}\right)} a^2x^2 + x(-$$

**2.324 ODE No. 324**

$$(2x^3(y(x))^3 - x) \frac{d}{dx}y(x) + 2x^3(y(x))^3 - y(x) = 0$$

**Mathematica:** cpu = 0.026003 (sec), leaf count = 723

$$\left\{ \left\{ y(x) \rightarrow -\frac{2x^3 - c_1x^2}{6x^2} + \frac{\sqrt[3]{12c_1x^8 - 6c_1^2x^7 + c_1^3x^6 + 3\sqrt{3}\sqrt{-24c_1x^{12} + 12c_1^2x^{11} - 2c_1^3x^{10} + 16x^{13} + 27c_1^3x^6}}}{6x^2} \right. \right.$$

**Maple:** cpu = 0.109 (sec), leaf count = 770

$$\left\{ y(x) = \frac{1}{6x} \sqrt[3]{(-C1^3x^2 - 6\_C1^2x^3 + 12\_C1x^4 - 8x^5 + 3\sqrt{-6\_C1^3x^2 + 36\_C1^2x^3 - 72\_C1x^4 + 27x^5}}$$

### 2.325 ODE No. 325

$$y(x) \left( (y(x))^3 - 2x^3 \right) \frac{d}{dx} y(x) + (2(y(x))^3 - x^3) x = 0$$

**Mathematica:** cpu = 0.049006 (sec), leaf count = 139

$$\text{Solve} \left[ \frac{1}{7} \text{RootSum} \left[ \#1^4 + \#1^3 + 3\#1^2 + \#1 + 1 \&, \frac{8\#1^3 \log\left(\frac{y(x)}{x} - \#1\right) + 9\#1^2 \log\left(\frac{y(x)}{x} - \#1\right) + 12\#1 \log\left(\frac{y(x)}{x} - \#1\right)}{4\#1^3 + 3\#1^2 + 6\#1 + 1} \right], y(x) \right]$$

**Maple:** cpu = 0.296 (sec), leaf count = 1192

$$\left\{ y(x) = -\frac{\sqrt{3}x}{6} \left( \sqrt{3} - 3 \text{RootOf} \left( 3\_Z - \sqrt{3} - \sqrt{3}\_Z^2 + 4 \tan\left(\frac{7}{6}\sqrt{3} \ln(2)\right) + 3\_Z^3 + 3 \tan\left(\frac{7}{6}\sqrt{3} \ln(2)\right) \_Z^2 \right) \right)$$

### 2.326 ODE No. 326

$$y(x) \left( (ay(x) + bx)^3 + bx^3 \right) \frac{d}{dx} y(x) + x \left( (ay(x) + bx)^3 + a(y(x))^3 \right) = 0$$

**Mathematica:** cpu = 0.272035 (sec), leaf count = 13289

**Maple:** cpu = 0.343 (sec), leaf count = 160

$$\left\{ y(x) = \frac{x(-C1 x - b \text{RootOf}(b^2\_Z^4 - 2bx\_C1\_Z^3 + (a^2x^2\_C1^2 + b^2x^2\_C1^2 + \_C1^2x^2 - a^2)\_Z^2 - a^2)}{a \text{RootOf}(b^2\_Z^4 - 2bx\_C1\_Z^3 + (a^2x^2\_C1^2 + b^2x^2\_C1^2 + \_C1^2x^2 - a^2)\_Z^2 - 2bx\_C1)}$$

**2.327 ODE No. 327**

$$(x(y(x))^4 + 2x^2(y(x))^3 + 2y(x) + x) \frac{d}{dx}y(x) + (y(x))^5 + y(x) = 0$$

**Mathematica:** cpu = 0.384549 (sec), leaf count = 669

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{9c_1^2x^2 + 3\sqrt{3}\sqrt{-4c_1^3x^6 - c_1^4x^4 + 18c_1^2x^4 + 4c_1^3x^2 + 27x^4 + 2c_1^3 + 27x^2}}}{3\sqrt[3]{2x}} - \frac{1}{3x\sqrt[3]{9c_1^2x^2 + 3\sqrt{3}\sqrt{-4c_1^3x^6 - c_1^4x^4 + 18c_1^2x^4 + 4c_1^3x^2 + 27x^4 + 2c_1^3 + 27x^2}}} \right\} \right.$$

**Maple:** cpu = 0.156 (sec), leaf count = 583

$$\left\{ y(x) = \frac{1}{12\_C1 x} \left( \left( -12ix^2\_C1 - i \left( 108\_C1^3x^2 + 12\sqrt{3}\sqrt{27\_C1^4x^2 + 18\_C1^2x^2 + (4x^4 - 4)\_C1} \right) \right) \right)$$

**2.328 ODE No. 328**

$$ax^2(y(x))^n \frac{d}{dx}y(x) - 2x \frac{d}{dx}y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.095012 (sec), leaf count = 42

$$\text{Solve} \left[ \frac{n(\log(x) - \log(-axy(x)^n + n + 2))}{n + 2} - \frac{2n \log(y(x))}{n + 2} = c_1, y(x) \right]$$

**Maple:** cpu = 0.140 (sec), leaf count = 33

$$\left\{ \frac{x^n}{((y(x))^n ax - n - 2)^n ((y(x))^n)^2} - \_C1 = 0 \right\}$$

**2.329 ODE No. 329**

$$(y(x))^m x^n \left( ax \frac{d}{dx}y(x) + by(x) \right) + \alpha x \frac{d}{dx}y(x) + \beta y(x) = 0$$

**Mathematica:** cpu = 0.313540 (sec), leaf count = 102

$$\text{Solve} \left[ \frac{m((a\beta - \alpha b) \log(x^n y(x)^m (bm - an) - \alpha n + \beta m) + \beta \log(x)(bm - an))}{(bm - an)(\beta m - \alpha n)} + \frac{\alpha m \log(\beta m y(x) - \alpha n y(x))}{\beta m - \alpha n} = c_1, y(x) \right]$$

**Maple:** cpu = 0.249 (sec), leaf count = 78

$$\left\{ x^{a\beta mn - b\beta m^2} ((y(x))^m)^{a\alpha n - \alpha bm} ((y(x))^m x^n na - (y(x))^m mx^n b + \alpha n - \beta m)^{-a\beta m + \alpha bm} - \_C1 = 0 \right\}$$

**2.330 ODE No. 330**

$$\left( f(y(x) + x) + 1 \right) \frac{d}{dx} y(x) + f(y(x) + x) = 0$$

**Mathematica:** cpu = 32.940183 (sec), leaf count = 49

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x f'(K[1] + K[2]) dK[1] + f(K[2] + x) + 1 \right) dK[2] + \int_1^x f(K[1] + y(x)) dK[1] = c_1, y(x) \right]$$

**Maple:** cpu = 0.031 (sec), leaf count = 22

$$\left\{ y(x) = -x + \text{RootOf} \left( -x + \int^{-Z} 1 + f(-a) d_a + _C1 \right) \right\}$$

**2.331 ODE No. 331**

$$\left( \frac{d}{dx} y(x) \right) \sum_{\nu=1}^p f_{\nu}(x) (y(x))^{\nu} - \sum_{\nu=1}^q g_{\nu}(x) (y(x))^{\nu} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0 (sec), leaf count = 0

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**2.332 ODE No. 332**

$$\left( \sqrt{xy(x)} - 1 \right) x \frac{d}{dx} y(x) - \left( \sqrt{xy(x)} + 1 \right) y(x) = 0$$

**Mathematica:** cpu = 0.080510 (sec), leaf count = 24

$$\text{Solve} \left[ \frac{2}{\sqrt{xy(x)}} + \log(y(x)) - \log(x) = c_1, y(x) \right]$$

**Maple:** cpu = 0.015 (sec), leaf count = 31

$$\left\{ \ln(x) - _C1 - \frac{1}{2} \left( \ln(xy(x)) \sqrt{xy(x)} + 2 \right) \frac{1}{\sqrt{xy(x)}} = 0 \right\}$$

**2.333 ODE No. 333**

$$\left( 2x^{5/2}(y(x))^{3/2} + x^2y(x) - x \right) \frac{d}{dx}y(x) - x^{3/2}(y(x))^{5/2} + x(y(x))^2 - y(x) = 0$$

**Mathematica:** cpu = 0.173022 (sec), leaf count = 72

$$\text{Solve} \left[ \frac{2\sqrt{xy(x)} \log(y(x))}{\sqrt{x}\sqrt{y(x)}} - \frac{\sqrt{xy(x)}(3x^{3/2}y(x)^{3/2} \log(x) + 6xy(x) - 2)}{3x^2y(x)^2} = c_1, y(x) \right]$$

**Maple:** cpu = 0.062 (sec), leaf count = 32

$$\left\{ \ln(y(x)) - 1 \frac{1}{\sqrt{x}} \frac{1}{\sqrt{y(x)}} + \frac{1}{3}(y(x))^{-\frac{3}{2}} x^{-\frac{3}{2}} - \frac{\ln(x)}{2} - \_C1 = 0 \right\}$$

**2.334 ODE No. 334**

$$\left( \sqrt{y(x) + x + 1} \right) \frac{d}{dx}y(x) + 1 = 0$$

**Mathematica:** cpu = 0.035505 (sec), leaf count = 39

$$\left\{ \{y(x) \rightarrow -2\sqrt{c_1 + x + 1} + c_1 + 2\}, \{y(x) \rightarrow 2\sqrt{c_1 + x + 1} + c_1 + 2\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 19

$$\left\{ -y(x) - 2\sqrt{y(x) + x} - \_C1 = 0 \right\}$$

**2.335 ODE No. 335**

$$\sqrt{(y(x))^2 - 1} \frac{d}{dx}y(x) - \sqrt{x^2 - 1} = 0$$

**Mathematica:** cpu = 0.181023 (sec), leaf count = 75

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \frac{1}{2} \#1 \sqrt{\#1^2 - 1} - \frac{1}{2} \log \left( \sqrt{\#1^2 - 1} + \#1 \right) \right] \& \right\} \left[ c_1 + \frac{1}{2} \sqrt{x^2 - 1} x - \frac{1}{2} \log \left( \sqrt{x^2 - 1} + x \right) \right] \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 50

$$\left\{ \_C1 + x\sqrt{x^2 - 1} - \ln \left( x + \sqrt{x^2 - 1} \right) - y(x) \sqrt{(y(x))^2 - 1} + \ln \left( y(x) + \sqrt{(y(x))^2 - 1} \right) = 0 \right\}$$

**2.336 ODE No. 336**

$$\left( \sqrt{(y(x))^2 + 1} + ax \right) \frac{d}{dx} y(x) + \sqrt{x^2 + 1} + ay(x) = 0$$

**Mathematica:** cpu = 0.063008 (sec), leaf count = 53

$$\text{Solve} \left[ axy(x) + \frac{1}{2} \sqrt{x^2 + 1} x + \frac{1}{2} \left( y(x) \sqrt{y(x)^2 + 1} + \sinh^{-1}(y(x)) \right) + \frac{1}{2} \sinh^{-1}(x) = c_1, y(x) \right]$$

**Maple:** cpu = 0.031 (sec), leaf count = 41

$$\left\{ \frac{x}{2} \sqrt{x^2 + 1} + \frac{\text{Arcsinh}(x)}{2} + axy(x) + \frac{y(x)}{2} \sqrt{(y(x))^2 + 1} + \frac{\text{Arcsinh}(y(x))}{2} + \_C1 = 0 \right\}$$

**2.337 ODE No. 337**

$$\left( \sqrt{(y(x))^2 + x^2} + x \right) \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.059007 (sec), leaf count = 52

$$\left\{ \left\{ y(x) \rightarrow -e^{\frac{c_1}{2}} \sqrt{e^{c_1} + 2x} \right\}, \left\{ y(x) \rightarrow e^{\frac{c_1}{2}} \sqrt{e^{c_1} + 2x} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 28

$$\left\{ -\_C1 + \frac{1}{(y(x))^2} \sqrt{(y(x))^2 + x^2} + \frac{x}{(y(x))^2} = 0 \right\}$$

**2.338 ODE No. 338**

$$\left( y(x) \sqrt{(y(x))^2 + x^2} + ((y(x))^2 - x^2) \sin(\alpha) - 2xy(x) \cos(\alpha) \right) \frac{d}{dx} y(x) + x \sqrt{(y(x))^2 + x^2} + 2xy(x) \sin(\alpha) = 0$$

**Mathematica:** cpu = 77.787378 (sec), leaf count = 17681

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{2} e^{c_1} \sin(\alpha) - \frac{1}{2} \sqrt{e^{2c_1} \sin^2(\alpha) + \frac{1}{6} (4x^2 - 4e^{c_1} \cos(\alpha)x - e^{2c_1} - e^{2c_1} \cos(2\alpha)) + \frac{1}{2} (-4x^2 + 4x^2 \cos(2\alpha) - 4x^2 \sin^2(\alpha))} \right\} \right\}$$

**Maple:** cpu = 0.530 (sec), leaf count = 136

$$\left\{ y(x) = \text{RootOf} \left( -\ln(x) + \int^{-z} -\frac{1}{(\_a^2 + 1) (\cos(2\alpha) \_a^2 + 2 \_a \sin(2\alpha) + \_a^2 - \cos(2\alpha) + 1)} (\cos(2\alpha) \_a^2 + 2 \_a \sin(2\alpha) + \_a^2 - \cos(2\alpha) + 1) \right) \right\}$$

**2.339 ODE No. 339**

$$\left( x\sqrt{x^2 + (y(x))^2 + 1} - y(x) \left( (y(x))^2 + x^2 \right) \right) \frac{d}{dx} y(x) - y(x) \sqrt{x^2 + (y(x))^2 + 1} - x \left( (y(x))^2 + x^2 \right) = 0$$

**Mathematica:** cpu = 0.109514 (sec), leaf count = 27

$$\text{Solve} \left[ \sqrt{x^2 + y(x)^2 + 1} + \tan^{-1} \left( \frac{x}{y(x)} \right) = c_1, y(x) \right]$$

**Maple:** cpu = 0.140 (sec), leaf count = 27

$$\left\{ \arctan \left( \frac{y(x)}{x} \right) - \sqrt{x^2 + (y(x))^2 + 1} - \_C1 = 0 \right\}$$

**2.340 ODE No. 340**

$$\left( \frac{e1(x+a)}{\left( (x+a)^2 + (y(x))^2 \right)^{3/2}} + \frac{e2(x-a)}{\left( (x-a)^2 + (y(x))^2 \right)^{3/2}} \right) \frac{d}{dx} y(x) - y(x) \left( \frac{e1}{\left( (x+a)^2 + (y(x))^2 \right)^{3/2}} + \frac{e2}{\left( (x-a)^2 + (y(x))^2 \right)^{3/2}} \right) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

**2.341 ODE No. 341**

$$\left( xe^{y(x)} + e^x \right) \frac{d}{dx} y(x) + e^{y(x)} + y(x) e^x = 0$$

**Mathematica:** cpu = 0.049506 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-x} - W \left( x e^{c_1 e^{-x} - x} \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 30

$$\left\{ y(x) = -\text{lambertW} \left( \frac{x}{e^x} \left( e^{\frac{c_1}{e^x}} \right)^{-1} \right) - \frac{c_1}{e^x} \right\}$$

### 2.342 ODE No. 342

$$x(3e^{xy(x)} + 2e^{-xy(x)}) \left( x \frac{d}{dx} y(x) + y(x) \right) + 1 = 0$$

**Mathematica:** cpu = 0.261033 (sec), leaf count = 163

$$\left\{ \left\{ y(x) \rightarrow -\frac{\cosh^{-1} \left( \frac{1}{24} \left( -5\sqrt{\log^2 \left( \frac{c_1}{x} \right) + 24} - \log \left( \frac{c_1}{x} \right) \right) \right)}{x} \right\} \right\}, \left\{ y(x) \rightarrow \frac{\cosh^{-1} \left( \frac{1}{24} \left( -5\sqrt{\log^2 \left( \frac{c_1}{x} \right) + 24} \right) \right)}{x} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 17

$$\left\{ y(x) = \frac{1}{x} \ln \left( -\frac{\ln(x)}{5} + \frac{C1}{5} \right) \right\}$$

### 2.343 ODE No. 343

$$(\ln(y(x)) + x) \frac{d}{dx} y(x) - 1 = 0$$

**Mathematica:** cpu = 0.037505 (sec), leaf count = 35

$$\text{Solve}[x = c_1 e^{y(x)} + e^{y(x)} (\text{Ei}(-y(x)) - e^{-y(x)} \log(y(x))), y(x)]$$

**Maple:** cpu = 0.046 (sec), leaf count = 27

$$\left\{ y(x) = e^{\text{RootOf}(-Z-x-\text{Ei}(1,e^{-Z})e^{e^{-Z}}+e^{e^{-Z}}-C1)} \right\}$$

### 2.344 ODE No. 344

$$(\ln(y(x)) + 2x - 1) \frac{d}{dx} y(x) - 2y(x) = 0$$

**Mathematica:** cpu = 0.018502 (sec), leaf count = 23

$$\left\{ \left\{ y(x) \rightarrow -\frac{W(-2c_1 e^{-2x})}{2c_1} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 19

$$\left\{ y(x) = e^{-\text{lambertW}(-2e^{-2x}-C1)-2x} \right\}$$



**2.345 ODE No. 345**

$$x(2x^2y(x)\ln(y(x)) + 1) \frac{d}{dx}y(x) - 2y(x) = 0$$

**Mathematica:** cpu = 0.041005 (sec), leaf count = 35

$$\text{Solve}\left[\frac{y(x)}{x^2} + 2\left(\frac{1}{2}y(x)^2\log(y(x)) - \frac{y(x)^2}{4}\right) = c_1, y(x)\right]$$

**Maple:** cpu = 0.063 (sec), leaf count = 36

$$\left\{y(x) = e^{\text{RootOf}\left(2\_Z x^2(e^{-Z})^2 - x^2(e^{-Z})^2 + 2x^2\_C1 + 2e^{-Z}\right)}\right\}$$

**2.346 ODE No. 346**

$$x(y(x)\ln(xy(x)) + y(x) - ax) \frac{d}{dx}y(x) - y(x)(ax\ln(xy(x)) - y(x) + ax) = 0$$

**Mathematica:** cpu = 0.054007 (sec), leaf count = 24

$$\text{Solve}[ax\log(xy(x)) - y(x)\log(xy(x)) = c_1, y(x)]$$

**Maple:** cpu = 0.202 (sec), leaf count = 19

$$\left\{(xy(x))^{-ax+y(x)} - \_C1 = 0\right\}$$

**2.347 ODE No. 347**

$$\left(\frac{d}{dx}y(x)\right)(1 + \sin(x))\sin(y(x)) + \cos(x)(\cos(y(x)) - 1) = 0$$

**Mathematica:** cpu = 0.117515 (sec), leaf count = 32

$$\left\{\left\{y(x) \rightarrow 0\right\}, \left\{y(x) \rightarrow 2\sin^{-1}\left(\frac{1}{4}c_1\left(\sin\left(\frac{x}{2}\right) + \cos\left(\frac{x}{2}\right)\right)\right)\right\}\right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 16

$$\{y(x) = \pi - \arccos(\sin(x)\_C1 + \_C1 - 1)\}$$

**2.348 ODE No. 348**

$$(x \cos(y(x)) + \sin(x)) \frac{d}{dx} y(x) + y(x) \cos(x) + \sin(y(x)) = 0$$

**Mathematica:** cpu = 0.048006 (sec), leaf count = 17

$$\text{Solve}[x \sin(y(x)) + y(x) \sin(x) = c_1, y(x)]$$

**Maple:** cpu = 0.078 (sec), leaf count = 15

$$\{y(x) \sin(x) + x \sin(y(x)) + \_C1 = 0\}$$

**2.349 ODE No. 349**

$$x \left( \frac{d}{dx} y(x) \right) \cot \left( \frac{y(x)}{x} \right) + 2x \sin \left( \frac{y(x)}{x} \right) - y(x) \cot \left( \frac{y(x)}{x} \right) = 0$$

**Mathematica:** cpu = 0.039005 (sec), leaf count = 15

$$\{ \{y(x) \rightarrow x \csc^{-1}(2(c_1 + \log(x)))\} \}$$

**Maple:** cpu = 0.031 (sec), leaf count = 15

$$\left\{ y(x) = \arcsin \left( \frac{1}{2 \ln(x) + 2 \_C1} \right) x \right\}$$

**2.350 ODE No. 350**

$$\left( \frac{d}{dx} y(x) \right) \cos(y(x)) - \cos(x) (\sin(y(x)))^2 - \sin(y(x)) = 0$$

**Mathematica:** cpu = 0.543569 (sec), leaf count = 53

$$\left\{ \left\{ y(x) \rightarrow \csc^{-1} \left( \frac{1}{2} (-2c_1 e^{-x} - \sin(x) - \cos(x)) \right) \right\}, \left\{ y(x) \rightarrow -\csc^{-1} \left( \frac{1}{2} (2c_1 e^{-x} + \sin(x) + \cos(x)) \right) \right\} \right\}$$

**Maple:** cpu = 0.718 (sec), leaf count = 270

$$\left\{ y(x) = \arctan \left( -2 \frac{e^x}{e^x \cos(x) + e^x \sin(x) + 2 \_C1}, \frac{1}{2 \cos(x) \sin(x) (e^x)^2 + 4 \_C1 \sin(x) e^x + 4 \cos(x)} \right) \right\}$$

### 2.351 ODE No. 351

$$\left(\frac{d}{dx}y(x)\right) \cos(y(x)) + x \sin(y(x)) (\cos(y(x)))^2 - (\sin(y(x)))^3 = 0$$

**Mathematica:** cpu = 0.367047 (sec), leaf count = 61

$$\left\{ \left\{ y(x) \rightarrow -\cot^{-1} \left( \sqrt{e^{x^2} (4c_1 - \sqrt{\pi} \operatorname{erf}(x))} \right) \right\}, \left\{ y(x) \rightarrow \cot^{-1} \left( \sqrt{e^{x^2} (4c_1 - \sqrt{\pi} \operatorname{erf}(x))} \right) \right\} \right\}$$

**Maple:** cpu = 0.343 (sec), leaf count = 55

$$\left\{ y(x) = -\arcsin \left( \frac{1}{\sqrt{1 - \sqrt{\pi} \operatorname{Erf}(x) e^{x^2} - 2\_C1 e^{x^2}}} \right), y(x) = \arcsin \left( \frac{1}{\sqrt{1 - \sqrt{\pi} \operatorname{Erf}(x) e^{x^2} - 2\_C1 e^{x^2}}} \right) \right\}$$

### 2.352 ODE No. 352

$$\left(\frac{d}{dx}y(x)\right) (\cos(y(x)) - \sin(\alpha) \sin(x)) \cos(y(x)) + (\cos(x) - \sin(\alpha) \sin(y(x))) \cos(x) = 0$$

**Mathematica:** cpu = 0.132017 (sec), leaf count = 43

$$\text{Solve} \left[ 4 \sin(\alpha) \sin(x) \sin(y(x)) - 4 \left( \frac{y(x)}{2} + \frac{1}{4} \sin(2y(x)) \right) - 2x - \sin(2x) = c_1, y(x) \right]$$

**Maple:** cpu = 0.188 (sec), leaf count = 35

$$\left\{ -\sin(x) \sin(\alpha) \sin(y(x)) + \frac{\cos(x) \sin(x)}{2} + \frac{x}{2} + \frac{\sin(y(x)) \cos(y(x))}{2} + \frac{y(x)}{2} + \_C1 = 0 \right\}$$

### 2.353 ODE No. 353

$$x \left(\frac{d}{dx}y(x)\right) \cos(y(x)) + \sin(y(x)) = 0$$

**Mathematica:** cpu = 0.020002 (sec), leaf count = 14

$$\left\{ \left\{ y(x) \rightarrow \sin^{-1} \left( \frac{e^{c_1}}{x} \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 12

$$\left\{ y(x) = \arcsin \left( \frac{1}{\_C1 x} \right) \right\}$$

**2.354 ODE No. 354**

$$(x \sin(y(x)) - 1) \frac{d}{dx} y(x) + \cos(y(x)) = 0$$

**Mathematica:** cpu = 0.064008 (sec), leaf count = 145

$$\left\{ \left\{ y(x) \rightarrow -\cos^{-1} \left( \frac{c_1 x - \sqrt{c_1^2 - x^2 + 1}}{c_1^2 + 1} \right) \right\}, \left\{ y(x) \rightarrow \cos^{-1} \left( \frac{c_1 x - \sqrt{c_1^2 - x^2 + 1}}{c_1^2 + 1} \right) \right\}, \left\{ y(x) \rightarrow -\cos^{-1} \left( \frac{c_1 x - \sqrt{c_1^2 - x^2 + 1}}{c_1^2 + 1} \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 115

$$\left\{ y(x) = \arctan \left( \frac{-C1}{-C1^2 + 1} \left( -C1 x + \sqrt{-C1^2 - x^2 + 1} \right) + x, -\frac{1}{-C1^2 + 1} \left( -C1 x + \sqrt{-C1^2 - x^2 + 1} \right) \right) \right\}$$

**2.355 ODE No. 355**

$$(x \cos(y(x)) + \cos(x)) \frac{d}{dx} y(x) - y(x) \sin(x) + \sin(y(x)) = 0$$

**Mathematica:** cpu = 0.048006 (sec), leaf count = 17

$$\text{Solve}[x \sin(y(x)) + y(x) \cos(x) = c_1, y(x)]$$

**Maple:** cpu = 0.062 (sec), leaf count = 15

$$\{y(x) \cos(x) + x \sin(y(x)) + \_C1 = 0\}$$

**2.356 ODE No. 356**

$$(x^2 \cos(y(x)) + 2 y(x) \sin(x)) \frac{d}{dx} y(x) + 2 x \sin(y(x)) + (y(x))^2 \cos(x) = 0$$

**Mathematica:** cpu = 0.061508 (sec), leaf count = 21

$$\text{Solve}[x^2 \sin(y(x)) + y(x)^2 \sin(x) = c_1, y(x)]$$

**Maple:** cpu = 0.078 (sec), leaf count = 19

$$\{(y(x))^2 \sin(x) + \sin(y(x)) x^2 + \_C1 = 0\}$$

**2.357 ODE No. 357**

$$x \left( \frac{d}{dx} y(x) \right) \ln(x) \sin(y(x)) + \cos(y(x)) (1 - x \cos(y(x))) = 0$$

**Mathematica:** cpu = 0.317540 (sec), leaf count = 35

$$\left\{ \left\{ y(x) \rightarrow -\sec^{-1} \left( \frac{x - c_1}{\log(x)} \right) \right\}, \left\{ y(x) \rightarrow \sec^{-1} \left( \frac{x - c_1}{\log(x)} \right) \right\} \right\}$$

**Maple:** cpu = 0.406 (sec), leaf count = 13

$$\left\{ y(x) = \arccos \left( \frac{\ln(x)}{x + \_C1} \right) \right\}$$

**2.358 ODE No. 358**

$$\left( \frac{d}{dx} y(x) \right) \sin(y(x)) \cos(x) + \cos(y(x)) \sin(x) = 0$$

**Mathematica:** cpu = 0.043506 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow -\cos^{-1} \left( \frac{1}{2} c_1 \sec(x) \right) \right\}, \left\{ y(x) \rightarrow \cos^{-1} \left( \frac{1}{2} c_1 \sec(x) \right) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 11

$$\left\{ y(x) = \arccos \left( \frac{\_C1}{\cos(x)} \right) \right\}$$

**2.359 ODE No. 359**

$$3 \left( \frac{d}{dx} y(x) \right) \sin(x) \sin(y(x)) + 5 (\cos(x))^4 y(x) = 0$$

**Mathematica:** cpu = 0.055507 (sec), leaf count = 45

$$\left\{ \left\{ y(x) \rightarrow \text{SinIntegral}^{(-1)} \left( c_1 - \frac{5}{3} \left( \frac{5 \cos(x)}{4} + \frac{1}{12} \cos(3x) + \log \left( \sin \left( \frac{x}{2} \right) \right) - \log \left( \cos \left( \frac{x}{2} \right) \right) \right) \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 28

$$\left\{ \frac{\cos(3x)}{12} + \frac{5 \cos(x)}{4} + \ln(\csc(x) - \cot(x)) + \frac{3 \text{Si}(y(x))}{5} + \_C1 = 0 \right\}$$

**2.360 ODE No. 360**

$$\left( \frac{d}{dx} y(x) \right) \cos(ay(x)) - b(1 - c \cos(ay(x))) \sqrt{(\cos(ay(x)))^2 - 1 + c \cos(ay(x))} = 0$$

**Mathematica:** cpu = 4.990134 (sec), leaf count = 369

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\frac{i(\cos(\#1a) + 1) \sqrt{\frac{2c \cos(\#1a) + \cos(2\#1a) - 1}{(\cos(\#1a) + 1)^2}} \sqrt{\frac{c \tan^2\left(\frac{\#1a}{2}\right) + \sqrt{c^2 + 4} + 2}{\sqrt{c^2 + 4} + 2}} \sqrt{1 - \frac{c \tan^2\left(\frac{\#1a}{2}\right)}{\sqrt{c^2 + 4}}}}{a(c^2 - 1) \sqrt{4 - 2\sqrt{c^2 + 4}}} \right] \right. \right.$$

**Maple:** cpu = 0.124 (sec), leaf count = 48

$$\left\{ x + \int^{y(x)} \frac{\cos(_a a)}{b(c \cos(_a a) - 1) \sqrt{2 \cos(2_a a) - 2 + 4 c \cos(_a a)}} d_a + _C1 = 0 \right\}$$

**2.361 ODE No. 361**

$$(x \sin(xy(x)) + \cos(y(x) + x) - \sin(y(x))) \frac{d}{dx} y(x) + y(x) \sin(xy(x)) + \cos(y(x) + x) + \cos(x) = 0$$

**Mathematica:** cpu = 0.213027 (sec), leaf count = 31

$$\text{Solve}[\cos(y(x)) - \cos(xy(x)) + \sin(x) \cos(y(x)) + \cos(x) \sin(y(x)) + \sin(x) = c_1, y(x)]$$

**Maple:** cpu = 0.172 (sec), leaf count = 22

$$\{-\cos(xy(x)) + \sin(y(x) + x) + \sin(x) + \cos(y(x)) + _C1 = 0\}$$

**2.362 ODE No. 362**

$$(x^2 y(x) \sin(xy(x)) - 4x) \frac{d}{dx} y(x) + x(y(x))^2 \sin(xy(x)) - y(x) = 0$$

**Mathematica:** cpu = 0.070009 (sec), leaf count = 23

$$\text{Solve}[-4 \log(y(x)) - \cos(xy(x)) - \log(x) = c_1, y(x)]$$

**Maple:** cpu = 0.110 (sec), leaf count = 23

$$\left\{ y(x) = \frac{1}{x} \text{RootOf}\left(-_Z + e^{-\frac{\cos(_Z)}{4}} _C1 x^{\frac{3}{4}}\right) \right\}$$

**2.363 ODE No. 363**

$$\left( x \frac{d}{dx} y(x) - y(x) \right) \left( \cos \left( \frac{y(x)}{x} \right) \right)^2 + x = 0$$

**Mathematica:** cpu = 0.035005 (sec), leaf count = 33

$$\text{Solve} \left[ \frac{y(x)}{2x} + \frac{1}{4} \sin \left( \frac{2y(x)}{x} \right) = c_1 - \log(x), y(x) \right]$$

**Maple:** cpu = 0.062 (sec), leaf count = 35

$$\left\{ -\frac{1}{2x} \left( \cos \left( \frac{y(x)}{x} \right) \sin \left( \frac{y(x)}{x} \right) x + y(x) \right) - \ln(x) - \_C1 = 0 \right\}$$

**2.364 ODE No. 364**

$$\left( y(x) \sin \left( \frac{y(x)}{x} \right) - x \cos \left( \frac{y(x)}{x} \right) \right) x \frac{d}{dx} y(x) - \left( x \cos \left( \frac{y(x)}{x} \right) + y(x) \sin \left( \frac{y(x)}{x} \right) \right) y(x) = 0$$

**Mathematica:** cpu = 0.064008 (sec), leaf count = 31

$$\text{Solve} \left[ -\log \left( \frac{y(x)}{x} \right) - \log \left( \cos \left( \frac{y(x)}{x} \right) \right) = c_1 + 2 \log(x), y(x) \right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 23

$$\left\{ y(x) = \frac{\_C1}{\cos(\text{RootOf}(-\_Z x^2 \cos(\_Z) + \_C1)) x} \right\}$$

**2.365 ODE No. 365**

$$(y(x) f((y(x))^2 + x^2) - x) \frac{d}{dx} y(x) + y(x) + x f((y(x))^2 + x^2) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.218 (sec), leaf count = 42

$$\left\{ y(x) = x \left( \tan \left( \text{RootOf} \left( -2\_Z - \int \frac{x^2 ((\tan(\_Z))^2 + 1)}{(\tan(\_Z))^2} \frac{f(\_a)}{\_a} d\_a + 2\_C1 \right) \right) \right)^{-1} \right\}$$

**2.366 ODE No. 366**

$$f(x^2 + a(y(x))^2) \left( ay(x) \frac{d}{dx}y(x) + x \right) - y(x) - x \frac{d}{dx}y(x) = 0$$

**Mathematica:** cpu = 264.973147 (sec), leaf count = 88

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x (1 - 2aK[1]K[2]f'(aK[2]^2 + K[1]^2)) dK[1] - aK[2]f(aK[2]^2 + x^2) + x \right) dK[2] + \dots \right]$$

**Maple:** cpu = 0.046 (sec), leaf count = 45

$$\left\{ -ax(y(x))^2 \frac{1}{\sqrt{a^2(y(x))^2}} - \int^{-\frac{a(y(x))^2 - x^2}{2}} f(-2\_a) d\_a + \_C1 = 0 \right\}$$

**2.367 ODE No. 367**

$$f(x^c y(x)) \left( bx \frac{d}{dx}y(x) - a \right) - x^a (y(x))^b \left( x \frac{d}{dx}y(x) + cy(x) \right) = 0$$

**Mathematica:** cpu = 22.563365 (sec), leaf count = 46

$$\text{DSolve}[f(x^c y(x)) (bx y'(x) - a) - x^a y(x)^b (cy(x) + xy'(x)) = 0, y(x), x]$$

**Maple:** cpu = 0.874 (sec), leaf count = 0

could not solve

**2.368 ODE No. 368**

$$\left( \frac{d}{dx}y(x) \right)^2 + ay(x) + bx^2 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0 (sec), leaf count = 0

hanged



**2.369 ODE No. 369**

$$\left(\frac{d}{dx}y(x)\right)^2 + (y(x))^2 - a^2 = 0$$

**Mathematica:** cpu = 0.046506 (sec), leaf count = 107

$$\left\{ \left\{ y(x) \rightarrow -\frac{a \tan(x - c_1)}{\sqrt{\tan^2(x - c_1) + 1}} \right\}, \left\{ y(x) \rightarrow \frac{a \tan(x - c_1)}{\sqrt{\tan^2(x - c_1) + 1}} \right\}, \left\{ y(x) \rightarrow -\frac{a \tan(c_1 + x)}{\sqrt{\tan^2(c_1 + x) + 1}} \right\} \right\},$$

**Maple:** cpu = 0.514 (sec), leaf count = 68

$$\left\{ y(x) = a, y(x) = \tan(-x + \_C1) \sqrt{\frac{a^2}{(\tan(-x + \_C1))^2 + 1}}, y(x) = -a, y(x) = -\tan(-x + \_C1) \sqrt{\frac{a^2}{(\tan(-x + \_C1))^2 + 1}} \right\}$$

**2.370 ODE No. 370**

$$\left(\frac{d}{dx}y(x)\right)^2 + (y(x))^2 - (f(x))^2 = 0$$

**Mathematica:** cpu = 22.438849 (sec), leaf count = 23

$$\text{DSolve}[-f(x)^2 + y'(x)^2 + y(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 1.404 (sec), leaf count = 0

could not solve

**2.371 ODE No. 371**

$$\left(\frac{d}{dx}y(x)\right)^2 - (y(x))^3 + (y(x))^2 = 0$$

**Mathematica:** cpu = 0.026003 (sec), leaf count = 37

$$\left\{ \left\{ y(x) \rightarrow \tan^2\left(\frac{1}{2}(c_1 - x)\right) + 1 \right\}, \left\{ y(x) \rightarrow \tan^2\left(\frac{1}{2}(c_1 + x)\right) + 1 \right\} \right\}$$

**Maple:** cpu = 0.468 (sec), leaf count = 20

$$\left\{ y(x) = 1, y(x) = \left(\tan\left(-\frac{x}{2} + \frac{\_C1}{2}\right)\right)^2 + 1 \right\}$$

**2.372 ODE No. 372**

$$\left(\frac{d}{dx}y(x)\right)^2 - 4(y(x))^3 + ay(x) + b = 0$$

**Mathematica:** cpu = 0.003501 (sec), leaf count = 27

$$\{\{y(x) \rightarrow \wp(x - c_1; a, b)\}, \{y(x) \rightarrow \wp(x + c_1; a, b)\}\}$$

**Maple:** cpu = 0.499 (sec), leaf count = 271

$$\left\{y(x) = \frac{1}{6}\sqrt[3]{27b + 3\sqrt{-3a^3 + 81b^2}} + \frac{a}{2\sqrt[3]{27b + 3\sqrt{-3a^3 + 81b^2}}}, y(x) = -\frac{1}{12}\sqrt[3]{27b + 3\sqrt{-3a^3 + 81b^2}}\right\}$$

**2.373 ODE No. 373**

$$\left(\frac{d}{dx}y(x)\right)^2 + a^2(y(x))^2((\ln(y(x)))^2 - 1) = 0$$

**Mathematica:** cpu = 0.109014 (sec), leaf count = 71

$$\left\{\left\{y(x) \rightarrow e^{\frac{1}{2}(e^{-c_1+iax}+e^{c_1-iax})}\right\}, \left\{y(x) \rightarrow \exp\left(\frac{1}{2}(e^{-c_1-iax}+e^{c_1+iax})\right)\right\}\right\}$$

**Maple:** cpu = 0.187 (sec), leaf count = 47

$$\left\{y(x) = (e^{\sin(-C1 a-ax)})^{-1}, y(x) = e^{\text{RootOf}(a^2(e^{-Z})^2(-Z^2-1))}, y(x) = e^{\sin(-C1 a-ax)}\right\}$$

**2.374 ODE No. 374**

$$\left(\frac{d}{dx}y(x)\right)^2 - 2\frac{d}{dx}y(x) - (y(x))^2 = 0$$

**Mathematica:** cpu = 0.061508 (sec), leaf count = 73

$$\left\{\left\{y(x) \rightarrow \text{InverseFunction}\left[-\frac{\sqrt{\#1^2+1}}{\#1} - \frac{1}{\#1} + \sinh^{-1}(\#1)\&\right][c_1 - x]\right\}, \left\{y(x) \rightarrow \text{InverseFunction}\left[\frac{\sqrt{\#1^2+1}}{\#1} - \frac{1}{\#1} + \sinh^{-1}(\#1)\&\right][c_1 - x]\right\}\right\}$$

**Maple:** cpu = 0.406 (sec), leaf count = 85

$$\left\{x - (y(x))^{-1} - \frac{1}{y(x)}((y(x))^2 + 1)^{\frac{3}{2}} + y(x)\sqrt{(y(x))^2 + 1} + \text{Arcsinh}(y(x)) - C1 = 0, x - (y(x))^{-1} + \frac{1}{y(x)}((y(x))^2 + 1)^{\frac{3}{2}} - y(x)\sqrt{(y(x))^2 + 1} - \text{Arcsinh}(y(x)) - C1 = 0\right\}$$

**2.375 ODE No. 375**

$$\left(\frac{d}{dx}y(x)\right)^2 + a\frac{d}{dx}y(x) + bx = 0$$

**Mathematica:** cpu = 0.062508 (sec), leaf count = 71

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( -\frac{(a^2 - 4bx)^{3/2}}{6b} - ax \right) + c_1 \right\}, \left\{ y(x) \rightarrow \frac{1}{2} \left( \frac{(a^2 - 4bx)^{3/2}}{6b} - ax \right) + c_1 \right\} \right\}$$

**Maple:** cpu = 0.468 (sec), leaf count = 49

$$\left\{ y(x) = -\frac{ax}{2} - \frac{1}{12b}(a^2 - 4bx)^{3/2} + \_C1, y(x) = -\frac{ax}{2} + \frac{1}{12b}(a^2 - 4bx)^{3/2} + \_C1 \right\}$$

**2.376 ODE No. 376**

$$\left(\frac{d}{dx}y(x)\right)^2 + a\frac{d}{dx}y(x) + by(x) = 0$$

**Mathematica:** cpu = 0.313040 (sec), leaf count = 110

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\frac{\sqrt{a^2 - 4\#1b} + a \log(\sqrt{a^2 - 4\#1b} - a)}{2b} \& \right] \left[ c_1 + \frac{x}{2} \right] \right\}, \left\{ y(x) \rightarrow \text{InverseF}$$

**Maple:** cpu = 0.796 (sec), leaf count = 215

$$\left\{ y(x) = -\frac{1}{4b} e^{-\frac{1}{2a} \left( a \ln\left(-\frac{1}{4b}\right) + 2 a \text{lambertW}\left(2 \frac{e^{-1}}{a} e^{-\frac{C1 b}{a}} \frac{1}{\sqrt{-b-1}} \left(e^{\frac{bx}{a}}\right)^{-1}\right) - 2 \_C1 b + 2 bx + 2 a\right)} \left( e^{-\frac{1}{2a} \left( a \ln\left(-\frac{1}{4b}\right) + 2 a \text{lambertW}\right)} \right) \right\}$$

**2.377 ODE No. 377**

$$\left(\frac{d}{dx}y(x)\right)^2 + (x - 2) \frac{d}{dx}y(x) - y(x) + 1 = 0$$

**Mathematica:** cpu = 0.006001 (sec), leaf count = 19

$$\{ \{ y(x) \rightarrow c_1 x + c_1^2 - 2c_1 + 1 \} \}$$

**Maple:** cpu = 0.390 (sec), leaf count = 25

$$\left\{ y(x) = -\frac{x^2}{4} + x, y(x) = \_C1^2 + \_C1 x - 2 \_C1 + 1 \right\}$$

**2.378 ODE No. 378**

$$\left(\frac{d}{dx}y(x)\right)^2 + (x+a)\frac{d}{dx}y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.004501 (sec), leaf count = 18

$$\{ \{y(x) \rightarrow ac_1 + c_1x + c_1^2\} \}$$

**Maple:** cpu = 0.452 (sec), leaf count = 32

$$\left\{ y(x) = -\frac{x^2}{4} - \frac{ax}{2} - \frac{a^2}{4}, y(x) = \_C1^2 + \_C1 a + \_C1 x \right\}$$

**2.379 ODE No. 379**

$$\left(\frac{d}{dx}y(x)\right)^2 - (1+x)\frac{d}{dx}y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.004000 (sec), leaf count = 18

$$\{ \{y(x) \rightarrow c_1x - c_1^2 + c_1\} \}$$

**Maple:** cpu = 0.422 (sec), leaf count = 27

$$\left\{ y(x) = \frac{x^2}{4} + \frac{x}{2} + \frac{1}{4}, y(x) = -\_C1^2 + \_C1 x + \_C1 \right\}$$

**2.380 ODE No. 380**

$$\left(\frac{d}{dx}y(x)\right)^2 + 2x\frac{d}{dx}y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.410552 (sec), leaf count = 1757

$$\left\{ \left\{ y(x) \rightarrow -\frac{x^2}{4} - \frac{1}{4} \sqrt[3]{x^6 - 20 \cosh(3c_1)x^3 - 20 \sinh(3c_1)x^3 - 8 \cosh(6c_1) - 8 \sinh(6c_1) + 8\sqrt{-\cosh(6c_1) - \sinh(6c_1)}} \right\} \right\}$$

**Maple:** cpu = 0.437 (sec), leaf count = 690

$$\left\{ y(x) = \left( \frac{1}{2} \sqrt[3]{6\_C1 - x^3 + 2\sqrt{-3\_C1 x^3 + 9\_C1^2}} + \frac{x^2}{2} \frac{1}{\sqrt[3]{6\_C1 - x^3 + 2\sqrt{-3\_C1 x^3 + 9\_C1^2}}} \right) \right\}$$

**2.381 ODE No. 381**

$$\left(\frac{d}{dx}y(x)\right)^2 - 2x\frac{d}{dx}y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.420553 (sec), leaf count = 1757

$$\left\{ \left\{ y(x) \rightarrow \frac{x^2}{4} + \frac{1}{4} \sqrt[3]{x^6 - 20 \cosh(3c_1)x^3 - 20 \sinh(3c_1)x^3 - 8 \cosh(6c_1) - 8 \sinh(6c_1) + 8\sqrt{-\cosh(3c_1)}}$$

**Maple:** cpu = 0.405 (sec), leaf count = 656

$$\left\{ y(x) = -\left(\frac{1}{2} \sqrt[3]{-6\_C1 + x^3 + 2\sqrt{-3\_C1x^3 + 9\_C1^2}} + \frac{x^2}{2} \frac{1}{\sqrt[3]{-6\_C1 + x^3 + 2\sqrt{-3\_C1x^3 + 9\_C1^2}}}\right) \right.$$

**2.382 ODE No. 382**

$$\left(\frac{d}{dx}y(x)\right)^2 + ax\frac{d}{dx}y(x) - bx^2 - c = 0$$

**Mathematica:** cpu = 0.255032 (sec), leaf count = 201

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( \frac{1}{2} x \sqrt{a^2x^2 + 4bx^2 + 4c} + \frac{2c \log(\sqrt{a^2 + 4b}\sqrt{a^2x^2 + 4bx^2 + 4c} + a^2x + 4bx)}{\sqrt{a^2 + 4b}} - \frac{ax^2}{2} \right) + c_1 \right\} \right.$$

**Maple:** cpu = 0.390 (sec), leaf count = 146

$$\left\{ y(x) = -\frac{ax^2}{4} - \frac{x}{4} \sqrt{(a^2 + 4b)x^2 + 4c} - c \ln(\sqrt{a^2 + 4b}x + \sqrt{(a^2 + 4b)x^2 + 4c}) \frac{1}{\sqrt{a^2 + 4b}} + \_C1, y(x) \right.$$

**2.383 ODE No. 383**

$$\left(\frac{d}{dx}y(x)\right)^2 + ax\frac{d}{dx}y(x) + by(x) + cx^2 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

**2.384 ODE No. 384**

$$\left(\frac{d}{dx}y(x)\right)^2 + (ax + b)\frac{d}{dx}y(x) - ay(x) + c = 0$$

**Mathematica:** cpu = 2.056261 (sec), leaf count = 183

$$\left\{ \left\{ y(x) \rightarrow \frac{-2\sqrt{-a^4 e^{2c_1} x^2 - 2a^4 e^{2c_1} x + a^4 (-e^{2c_1})} + 2a^3 x + a^3 - 2a^2 b x - ab^2 - a e^{2c_1} + 4ac}{4a^2} \right\}, \left\{ y(x) \rightarrow \dots \right\} \right\}$$

**Maple:** cpu = 0.468 (sec), leaf count = 50

$$\left\{ y(x) = \frac{-a^2 x^2 - 2abx - b^2 + 4c}{4a}, y(x) = \_C1 x + \frac{\_C1^2 + \_C1 b + c}{a} \right\}$$

**2.385 ODE No. 385**

$$\left(\frac{d}{dx}y(x)\right)^2 - 2x^2\frac{d}{dx}y(x) + 2xy(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.562 (sec), leaf count = 169

$$\left\{ y(x) = \frac{x^4 - (RootOf(x^{16} - 12\_Z^2 x^{12} + 16\_Z^3 x^{10} + 30\_Z^4 x^8 - 96\_Z^5 x^6 + 100\_Z^6 x^4 - 48\_Z^7 x^2))}{2x} \right\}$$

**2.386 ODE No. 386**

$$\left(\frac{d}{dx}y(x)\right)^2 + ax^3\frac{d}{dx}y(x) - 2ax^2y(x) = 0$$

**Mathematica:** cpu = 0.204526 (sec), leaf count = 56

$$\left\{ \left\{ y(x) \rightarrow 2ae^{2c_1}(4e^{2c_1} + x^2) \right\}, \left\{ y(x) \rightarrow \frac{e^{2c_1}(e^{2c_1} - 2ax^2)}{8a} \right\} \right\}$$

**Maple:** cpu = 0.655 (sec), leaf count = 27

$$\left\{ y(x) = -\frac{ax^4}{8}, y(x) = x^2\_C1 + 2\frac{\_C1^2}{a} \right\}$$

**2.387 ODE No. 387**

$$\left( \frac{d}{dx} y(x) \right)^2 + \left( \frac{d}{dx} y(x) - y(x) \right) e^x = 0$$

**Mathematica:** cpu = 0.535568 (sec), leaf count = 134

$$\left\{ \text{Solve} \left[ \frac{-e^{x/2} \sqrt{4y(x) + e^x} - 4y(x) \log(\sqrt{4y(x) + e^x} + e^{x/2}) + e^x}{2y(x)} = c_1, y(x) \right], \text{Solve} \left[ 2 \log(y(x)) - \frac{e^x}{2y(x)} = c_2, y(x) \right] \right\}$$

**Maple:** cpu = 1.202 (sec), leaf count = 115

$$\left\{ -\frac{e^x}{2y(x)} + \ln(y(x)) + 2 \operatorname{Artanh}(\sqrt{e^{2x} + 4y(x)e^x}) + \frac{1}{2y(x)} \sqrt{e^{2x} + 4y(x)e^x} - C1 = 0, -2 \operatorname{Arctanh}(\sqrt{e^{2x} + 4y(x)e^x}) - \frac{1}{2y(x)} \sqrt{e^{2x} + 4y(x)e^x} - C2 = 0 \right\}$$

**2.388 ODE No. 388**

$$\left( \frac{d}{dx} y(x) \right)^2 - 2y(x) \frac{d}{dx} y(x) - 2x = 0$$

**Mathematica:** cpu = 0.670085 (sec), leaf count = 53

$$\text{Solve} \left[ \left\{ x = \frac{c_1 \sqrt{K\$1205645^2 + 1}}{\sqrt{K\$1205645^2 + 1}} + \frac{K\$1205645 \sinh^{-1}(K\$1205645)}{2\sqrt{K\$1205645^2 + 1}}, y(x) = \frac{K\$1205645}{2} - \frac{x}{K\$1205645} \right\} \right]$$

**Maple:** cpu = 0.499 (sec), leaf count = 217

$$\left\{ -C1 \left( -2y(x) + 2\sqrt{(y(x))^2 + 2x} \right) \frac{1}{\sqrt{2(y(x))^2 + 2x - 2y(x)} \sqrt{(y(x))^2 + 2x + 1}} + x - \frac{1}{2} \left( -y(x) + \sqrt{(y(x))^2 + 2x} \right) = 0 \right\}$$

**2.389 ODE No. 389**

$$\left( \frac{d}{dx} y(x) \right)^2 - (4y(x) + 1) \frac{d}{dx} y(x) + (4y(x) + 1) y(x) = 0$$

**Mathematica:** cpu = 0.074009 (sec), leaf count = 109

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{4} e^{x-4c_1} (2e^{2c_1} - e^x) \right\}, \left\{ y(x) \rightarrow \frac{1}{4} (\sinh(2c_1 + x) + \cosh(2c_1 + x) - 2) (\sinh(2c_1 + x) + \cosh(2c_1 + x)) \right\} \right\}$$

**Maple:** cpu = 0.811 (sec), leaf count = 193

$$\left\{ y(x) = -\frac{1}{4}, y(x) = -\frac{(e^x)^2}{2\_C1} \left( -\frac{C1}{(e^x)^2} \left( \sqrt{-\frac{C1}{(e^x)^2}} - 2 \right) \frac{1}{\sqrt{-\frac{C1}{(e^x)^2}}} + \frac{C1}{(e^x)^2} + 2 \right), y(x) = \frac{(e^x)^2}{2\_C1} \left( \frac{C1}{(e^x)^2} \right) \right.$$

## 2.390 ODE No. 390

$$\left( \frac{d}{dx} y(x) \right)^2 + ay(x) \frac{d}{dx} y(x) - bx - c = 0$$

**Mathematica:** cpu = 1.795728 (sec), leaf count = 142

$$\text{Solve} \left[ \left\{ x = c_1 e^{b \left( \frac{\log(K\$1206119)}{b} - \frac{\log(b - aK\$1206119^2)}{2b} \right)} + e^{b \left( \frac{\log(K\$1206119)}{b} - \frac{\log(b - aK\$1206119^2)}{2b} \right)} \left( \frac{\tan^{-1} \left( \frac{\sqrt{a}K\$1206119}{\sqrt{b - aK\$1206119^2}} \right)}{\sqrt{a}} \right) \right. \right.$$

**Maple:** cpu = 0.655 (sec), leaf count = 416

$$\left\{ y(x) = 2 \frac{b e^{\text{RootOf}(\sqrt{a\_C1} b e^2 - Z - a e^2 - Z b x + \sqrt{a\_C1} b^2 - e^2 - Z b - a e^2 - Z c + a b^2 x - Z b^2 + a b c)} x}{(e^{2 \text{RootOf}(\sqrt{a\_C1} b e^2 - Z - a e^2 - Z b x + \sqrt{a\_C1} b^2 - e^2 - Z b - a e^2 - Z c + a b^2 x - Z b^2 + a b c)} + b) \sqrt{a}} + 2 \frac{e^{\text{RootOf}(\sqrt{a\_C1} b e^2 - Z - a e^2 - Z b x + \sqrt{a\_C1} b^2 - e^2 - Z b - a e^2 - Z c + a b^2 x - Z b^2 + a b c)}}{(e^{2 \text{RootOf}(\sqrt{a\_C1} b e^2 - Z - a e^2 - Z b x + \sqrt{a\_C1} b^2 - e^2 - Z b - a e^2 - Z c + a b^2 x - Z b^2 + a b c)} + b) \sqrt{a}} \right.$$

## 2.391 ODE No. 391

$$\left( \frac{d}{dx} y(x) \right)^2 + (ay(x) + bx) \frac{d}{dx} y(x) + abxy(x) = 0$$

**Mathematica:** cpu = 0.005501 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-ax} \right\}, \left\{ y(x) \rightarrow c_1 - \frac{bx^2}{2} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 22

$$\left\{ y(x) = \_C1 e^{-ax}, y(x) = -\frac{bx^2}{2} + \_C1 \right\}$$



**2.392 ODE No. 392**

$$\left(\frac{d}{dx}y(x)\right)^2 - xy(x)\frac{d}{dx}y(x) + (y(x))^2 \ln(ay(x)) = 0$$

**Mathematica:** cpu = 0.255032 (sec), leaf count = 27

$$\left\{ \left\{ y(x) \rightarrow \frac{e^{\frac{c_1 x}{2} - \frac{c_1^2}{4}}}{a} \right\} \right\}$$

**Maple:** cpu = 0.312 (sec), leaf count = 50

$$\left\{ y(x) = \frac{1}{a} e^{\frac{x^2}{4}}, y(x) = \frac{1}{e^{-C1^2} e^{-C1 x a}}, y(x) = \frac{e^{-C1 x}}{e^{-C1^2} a} \right\}$$

**2.393 ODE No. 393**

$$\left(\frac{d}{dx}y(x)\right)^2 + 2y(x)\left(\frac{d}{dx}y(x)\right)\cot(x) - (y(x))^2 = 0$$

**Mathematica:** cpu = 0.072509 (sec), leaf count = 31

$$\left\{ \left\{ y(x) \rightarrow c_1 \csc^2\left(\frac{x}{2}\right) \right\}, \left\{ y(x) \rightarrow c_1 \sec^2\left(\frac{x}{2}\right) \right\} \right\}$$

**Maple:** cpu = 0.858 (sec), leaf count = 85

$$\left\{ y(x) = \frac{-C1}{\tan(x)} \sqrt{1 - ((\tan(x))^2 + 1)^{-1}} \sqrt{(\tan(x))^2 + 1} \left(1 + \frac{1}{\sqrt{(\tan(x))^2 + 1}}\right)^{-1}, y(x) = \frac{-C1}{\tan(x)} \left(1 + \frac{1}{\sqrt{(\tan(x))^2 + 1}}\right)^{-1} \right\}$$

**2.394 ODE No. 394**

$$\left(\frac{d}{dx}y(x)\right)^2 + 2f(x)y(x)\frac{d}{dx}y(x) + g(x)(y(x))^2 - (g(x) - (f(x))^2)e^{-2\int_a^x f(xp)dxp} = 0$$

**Mathematica:** cpu = 58.132882 (sec), leaf count = 52

$$\text{DSolve}\left[-(g(x) - f(x)^2)e^{-2\int_a^x f(xp)dxp} + 2f(x)y(x)y'(x) + g(x)y(x)^2 + y'(x)^2 = 0, y(x), x\right]$$

**Maple:** cpu = 3.822 (sec), leaf count = 310

$$\left\{ y(x) = -\tan\left(\frac{1}{2\cos(2) + 2}\left(-2 - C1 \cos(2) + \sqrt{2}\int(e^{\int_a^x f(xp)dxp})^2\sqrt{-\frac{\cos(4)(f(x))^2}{(e^{\int_a^x f(xp)dxp})^4} - 4\frac{\cos(2)(f(x))^2}{(e^{\int_a^x f(xp)dxp})^4}}\right)\right)$$

**2.395 ODE No. 395**

$$\left(\frac{d}{dx}y(x)\right)^2 + 2f(x)y(x)\frac{d}{dx}y(x) + g(x)(y(x))^2 + h(x) = 0$$

**Mathematica:** cpu = 38.765923 (sec), leaf count = 32

$$\text{DSolve}[2f(x)y(x)y'(x) + g(x)y(x)^2 + h(x) + y'(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 0.968 (sec), leaf count = 0

could not solve

**2.396 ODE No. 396**

$$\left(\frac{d}{dx}y(x)\right)^2 + y(x)(y(x) - x)\frac{d}{dx}y(x) - x(y(x))^3 = 0$$

**Mathematica:** cpu = 0.014002 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{x - c_1} \right\}, \left\{ y(x) \rightarrow c_1 e^{\frac{x^2}{2}} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 20

$$\left\{ y(x) = (x + \_C1)^{-1}, y(x) = e^{\frac{x^2}{2}} \_C1 \right\}$$

**2.397 ODE No. 397**

$$\left(\frac{d}{dx}y(x)\right)^2 - 2x^3(y(x))^2\frac{d}{dx}y(x) - 4x^2(y(x))^3 = 0$$

**Mathematica:** cpu = 0.431555 (sec), leaf count = 143

$$\left\{ \text{Solve} \left[ \frac{x\sqrt{x^4y(x) + 4y(x)^{3/2}} \sinh^{-1} \left( \frac{1}{2}x^2\sqrt{y(x)} \right)}{2\sqrt{x^2y(x)^3(x^4y(x) + 4)}} - \frac{1}{4} \log(y(x)) = c_1, y(x) \right], \text{Solve} \left[ \frac{xy(x)^{3/2}\sqrt{x^4y(x)}}{2\sqrt{x^2y(x)}} \right] \right\}$$

**Maple:** cpu = 0.671 (sec), leaf count = 131

$$\left\{ y(x) = -4x^{-4}, y(x) = \frac{(\sqrt{2x^2\_C1} - 2)\_C1^2}{2\_C1^2x^4 - 4}, y(x) = -\frac{(\sqrt{2x^2\_C1} + 2)\_C1^2}{2\_C1^2x^4 - 4}, y(x) = -2\frac{\sqrt{2x^2\_C1}}{\_C1^2(-2)} \right\}$$

**2.398 ODE No. 398**

$$\left( \frac{d}{dx} y(x) \right)^2 - 3x(y(x))^{2/3} \frac{d}{dx} y(x) + 9(y(x))^{5/3} = 0$$

**Mathematica:** cpu = 0.737094 (sec), leaf count = 258

$$\left\{ \text{Solve} \left[ -\frac{\left(x^2 - 4\sqrt[3]{y(x)}\right)^{3/2} y(x)^2 \log(y(x))}{6 \left(\left(x^2 - 4\sqrt[3]{y(x)}\right) y(x)^{4/3}\right)^{3/2}} + \frac{\sqrt{\left(x^2 - 4\sqrt[3]{y(x)}\right) y(x)^{4/3}} \log\left(\sqrt{x^2 - 4\sqrt[3]{y(x)}} + x\right)}{\sqrt{x^2 - 4\sqrt[3]{y(x)}} y(x)^{2/3}} + \dots \right]$$

**Maple:** cpu = 2.402 (sec), leaf count = 137

$$\left\{ \ln(x) + \frac{1}{6} \ln\left(\frac{y(x)}{x^6}\right) - \frac{1}{6} \ln\left(4\sqrt[3]{\frac{y(x)}{x^6}} - 1\right) + 1\sqrt{-4\left(\frac{y(x)}{x^6}\right)^{5/3} + \left(\frac{y(x)}{x^6}\right)^{4/3}} \text{Artanh}\left(\sqrt{-4\sqrt[3]{\frac{y(x)}{x^6}}}\right) \dots \right\}$$

**2.399 ODE No. 399**

$$2\left(\frac{d}{dx} y(x)\right)^2 + (x-1) \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.003500 (sec), leaf count = 20

$$\{\{y(x) \rightarrow c_1 x + 2c_1^2 - c_1\}\}$$

**Maple:** cpu = 0.515 (sec), leaf count = 29

$$\left\{ y(x) = -\frac{x^2}{8} + \frac{x}{4} - \frac{1}{8}, y(x) = 2\_C1^2 + \_C1 x - \_C1 \right\}$$

**2.400 ODE No. 400**

$$2\left(\frac{d}{dx} y(x)\right)^2 - 2x^2 \frac{d}{dx} y(x) + 3xy(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.624 (sec), leaf count = 123

$$\left\{ y(x) = \frac{x^3}{6}, y(x) = -\frac{1}{3\_C1} \left( -\_C1 x^3 - x \left( -x^2 \_C1 + \sqrt{-6\_C1 x} \right) - 3 \right), y(x) = -\frac{1}{3\_C1} \left( -\_C1 x^3 \dots \right) \right\}$$

## 2.401 ODE No. 401

$$3 \left( \frac{d}{dx} y(x) \right)^2 - 2x \frac{d}{dx} y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.353545 (sec), leaf count = 1093

{ {y(x) → Root[-16e<sup>6c1</sup>x<sup>6</sup> + 3#1<sup>4</sup>x<sup>4</sup> + 144e<sup>6c1</sup>#1x<sup>4</sup> - 24#1<sup>5</sup>x<sup>2</sup> - 378e<sup>6c1</sup>#1<sup>2</sup>x<sup>2</sup> + 243e<sup>12c1</sup> + 48#1<sup>6</sup> + 2

**Maple:** cpu = 0.452 (sec), leaf count = 656

$$\left\{ y(x) = -3 \left( 1/6 \sqrt[3]{-54\_C1 + x^3 + 6 \sqrt{-3\_C1 x^3 + 81\_C1^2}} + 1/6 \frac{x^2}{\sqrt[3]{-54\_C1 + x^3 + 6 \sqrt{-3\_C1 x^3 + 81\_C1^2}}} \right) \right.$$

## 2.402 ODE No. 402

$$3 \left( \frac{d}{dx} y(x) \right)^2 + 4x \frac{d}{dx} y(x) - y(x) + x^2 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.577 (sec), leaf count = 121

$$\left\{ y(x) = -\frac{x^2}{3}, y(x) = \frac{-2\_C1 x(-\_C1 x + \sqrt{3}) - 5\_C1^2 x^2 + 3}{12\_C1^2}, y(x) = \frac{2\_C1 x(-\_C1 x + \sqrt{3}) - 5\_C1^2}{12\_C1^2} \right.$$

## 2.403 ODE No. 403

$$a \left( \frac{d}{dx} y(x) \right)^2 + b \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.302538 (sec), leaf count = 116

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \frac{\sqrt{4\#1a + b^2} + b \log(\sqrt{4\#1a + b^2} - b)}{2a} \& \right] \left[ \frac{x}{2a} + c_1 \right] \right\}, \left\{ y(x) \rightarrow \text{InverseFu} \right.$$

**Maple:** cpu = 0.858 (sec), leaf count = 197

$$\left\{ y(x) = \frac{1}{4a} e^{-\frac{1}{2b} \left( b \ln\left(\frac{1}{4a}\right) + 2 \text{blambert}W\left(2 \frac{e^{-1}}{b\sqrt{a-1}} e^{\frac{x}{b}} \left(e^{-\frac{C1}{b}}\right)^{-1}\right) + 2\_C1 + 2b - 2x \right)} \left( e^{-\frac{1}{2b} \left( b \ln\left(\frac{1}{4a}\right) + 2 \text{blambert}W\left(2 \frac{e^{-1}}{b\sqrt{a-1}} e^{\frac{x}{b}} \right)} \right)} \right.$$

**2.404 ODE No. 404**

$$a \left( \frac{d}{dx} y(x) \right)^2 + bx^2 \frac{d}{dx} y(x) + cxy(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.686 (sec), leaf count = 499

$$\left\{ \int_{-b}^x -1 \left( -b - a^2 + \sqrt{-a^4 b^2 - 4 - a a c y(x)} \right) \left( -b - a^3 + \sqrt{-a^4 b^2 - 4 - a a c y(x)} - a - 6 a y(x) \right)^{-1} d - a + \right.$$

**2.405 ODE No. 405**

$$a \left( \frac{d}{dx} y(x) \right)^2 + y(x) \frac{d}{dx} y(x) - x = 0$$

**Mathematica:** cpu = 1.013629 (sec), leaf count = 53

$$\text{Solve} \left[ \left\{ x = \frac{a \text{K\$1210941} \sin^{-1}(\text{K\$1210941})}{\sqrt{1 - \text{K\$1210941}^2}} + \frac{c_1 \text{K\$1210941}}{\sqrt{1 - \text{K\$1210941}^2}}, y(x) = \frac{x}{\text{K\$1210941}} - a \text{K\$1210941} \right\} \right],$$

**Maple:** cpu = 0.593 (sec), leaf count = 380

$$\left\{ -_C1 \left( -y(x) + \sqrt{4ax + (y(x))^2} \right) \frac{1}{\sqrt{\frac{1}{a} \left( -y(x) + \sqrt{4ax + (y(x))^2} + 2a \right)}} \frac{1}{\sqrt{\frac{1}{a} \left( -y(x) + \sqrt{4ax + (y(x))^2} \right)}} \right.$$

**2.406 ODE No. 406**

$$a \left( \frac{d}{dx} y(x) \right)^2 - y(x) \frac{d}{dx} y(x) - x = 0$$

**Mathematica:** cpu = 0.864110 (sec), leaf count = 49

$$\text{Solve} \left[ \left\{ x = \frac{a \text{K\$1211116} \sinh^{-1}(\text{K\$1211116})}{\sqrt{\text{K\$1211116}^2 + 1}} + \frac{c_1 \text{K\$1211116}}{\sqrt{\text{K\$1211116}^2 + 1}}, y(x) = a \text{K\$1211116} - \frac{x}{\text{K\$1211116}} \right\} \right]$$

**Maple:** cpu = 0.577 (sec), leaf count = 266

$$\left\{ -C1 \left( -y(x) + \sqrt{4ax + (y(x))^2} \right) \frac{1}{\sqrt{-\frac{1}{a^2} \left( 2y(x) \sqrt{4ax + (y(x))^2} - 4a^2 - 4ax - 2(y(x))^2 \right)}} + x - \right.$$

## 2.407 ODE No. 407

$$x \left( \frac{d}{dx} y(x) \right)^2 - y(x) = 0$$

**Mathematica:** cpu = 0.020503 (sec), leaf count = 51

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4} (-4c_1 \sqrt{x} + c_1^2 + 4x) \right\}, \left\{ y(x) \rightarrow \frac{1}{4} (4c_1 \sqrt{x} + c_1^2 + 4x) \right\} \right\}$$

**Maple:** cpu = 0.499 (sec), leaf count = 39

$$\left\{ y(x) = 0, y(x) = \frac{1}{x} \left( -x + \sqrt{-C1 x} \right)^2, y(x) = \frac{1}{x} \left( x + \sqrt{-C1 x} \right)^2 \right\}$$

## 2.408 ODE No. 408

$$x \left( \frac{d}{dx} y(x) \right)^2 - 2y(x) + x = 0$$

**Mathematica:** cpu = 0.532068 (sec), leaf count = 166

$$\left\{ \text{Solve} \left[ \frac{\left( \sqrt{\frac{2y(x)}{x} - 1} - 1 \right) \left( \left( \sqrt{\frac{2y(x)}{x} - 1} - 1 \right) \log \left( \sqrt{\frac{2y(x)}{x} - 1} - 1 \right) - 1 \right)}{\sqrt{\frac{2y(x)}{x} - 1} - \frac{y(x)}{x}} = c_1 + \log(x), y(x) \right], \text{Solve} \right.$$

**Maple:** cpu = 0.514 (sec), leaf count = 73

$$\left\{ y(x) = \left( \frac{1}{2} \left( \text{lambertW} \left( \frac{1}{-C1} \sqrt{-C1 x} \right) + 1 \right) \right)^2 \left( \text{lambertW} \left( \frac{1}{-C1} \sqrt{-C1 x} \right) \right)^{-2} + \frac{1}{2} \right\} x, y(x) = \left( \frac{1}{2} \right.$$

**2.409 ODE No. 409**

$$x \left( \frac{d}{dx} y(x) \right)^2 - 2 \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 30.779909 (sec), leaf count = 66

$$\text{Solve} \left[ \left\{ x = \frac{y(\text{K\$1211643}) + 2\text{K\$1211643}}{\text{K\$1211643}^2}, y(x) = c_1 e^{2(\log(\text{K\$1211643}) - \log(1 - \text{K\$1211643}))} + e^{2(\log(\text{K\$1211643}) - \log(1 - \text{K\$1211643}))} \right\} \right]$$

**Maple:** cpu = 0.468 (sec), leaf count = 63

$$\left\{ y(x) = x e^{2 \text{RootOf}(-x e^2 - Z + 2 x e^{-Z} + 2 e^{-Z} + C1 - 2 Z - x)} - 2 e^{\text{RootOf}(-x e^2 - Z + 2 x e^{-Z} + 2 e^{-Z} + C1 - 2 Z - x)} \right\}$$

**2.410 ODE No. 410**

$$x \left( \frac{d}{dx} y(x) \right)^2 + 4 \frac{d}{dx} y(x) - 2 y(x) = 0$$

**Mathematica:** cpu = 31.055944 (sec), leaf count = 80

$$\text{Solve} \left[ \left\{ x = -\frac{2(2\text{K\$1211948} - y(\text{K\$1211948}))}{\text{K\$1211948}^2}, y(x) = c_1 e^{-4\left(\frac{1}{2} \log(2 - \text{K\$1211948}) - \frac{\log(\text{K\$1211948})}{2}\right)} + 4 e^{-4\left(\frac{1}{2} \log(2 - \text{K\$1211948}) - \frac{\log(\text{K\$1211948})}{2}\right)} \right\} \right]$$

**Maple:** cpu = 0.546 (sec), leaf count = 64

$$\left\{ y(x) = \frac{x e^{2 \text{RootOf}(-x e^2 - Z + 4 x e^{-Z} - 4 e^{-Z} + C1 + 8 Z - 4 x)}}{2} + 2 e^{\text{RootOf}(-x e^2 - Z + 4 x e^{-Z} - 4 e^{-Z} + C1 + 8 Z - 4 x)} \right\}$$

**2.411 ODE No. 411**

$$x \left( \frac{d}{dx} y(x) \right)^2 + x \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.558571 (sec), leaf count = 181

$$\left\{ \text{Solve} \left[ \frac{\left( \sqrt{\frac{4y(x)}{x} + 1} - 1 \right) \left( \left( \sqrt{\frac{4y(x)}{x} + 1} - 1 \right) \log \left( \sqrt{\frac{4y(x)}{x} + 1} - 1 \right) - 1 \right)}{2 \left( -\frac{2y(x)}{x} + \sqrt{\frac{4y(x)}{x} + 1} - 1 \right)} = c_1 + \frac{\log(x)}{2}, y(x) \right], \text{Solve} \left[ \dots \right] \right\}$$

**Maple:** cpu = 0.531 (sec), leaf count = 69

$$\left\{ y(x) = \left( \frac{1}{4} \left( \text{lambertW} \left( -\frac{1}{2} \frac{1}{\sqrt{\frac{C1}{x}}} \right) \right) \right)^{-2} + \frac{1}{2} \left( \text{lambertW} \left( -\frac{1}{2} \frac{1}{\sqrt{\frac{C1}{x}}} \right) \right)^{-1} \right) x, y(x) = \left( \frac{1}{4} \left( \text{lambertW} \left( -\frac{1}{2} \frac{1}{\sqrt{\frac{C1}{x}}} \right) \right) \right)^{-2} + \frac{1}{2} \left( \text{lambertW} \left( -\frac{1}{2} \frac{1}{\sqrt{\frac{C1}{x}}} \right) \right)^{-1} \right) x \right\}$$

**2.412 ODE No. 412**

$$x \left( \frac{d}{dx} y(x) \right)^2 + y(x) \frac{d}{dx} y(x) + a = 0$$

**Mathematica:** cpu = 5.287171 (sec), leaf count = 16145

$$\left\{ \left\{ y(x) \rightarrow - \sqrt{-\frac{4ax}{3} - \frac{1}{2} \sqrt{-\frac{64}{9} a^2 x^2 + \frac{\cosh(3c_1)}{81ax} + \frac{\sinh(3c_1)}{81ax} + \sqrt[3]{4529848320a^6 \cosh(6c_1) x^6 + 4529}} \right. \right.$$

**Maple:** cpu = 0.546 (sec), leaf count = 146

$$\left\{ -x^2 \_C1 \left( \frac{1}{x} \left( -y(x) + \sqrt{(y(x))^2 - 4ax} \right) \right)^{\frac{3}{2}} \left( -y(x) + \sqrt{(y(x))^2 - 4ax} \right)^{-2} + x + \frac{4ax^2}{3} \left( -y(x) + \sqrt{(y(x))^2 - 4ax} \right) \right.$$

**2.413 ODE No. 413**

$$x \left( \frac{d}{dx} y(x) \right)^2 + y(x) \frac{d}{dx} y(x) - x^2 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.640 (sec), leaf count = 337

$$\left\{ \int_{-b}^x -\frac{1}{-a} \left( y(x) + \sqrt{4-a^3 + (y(x))^2} \right) \left( \sqrt{4-a^3 + (y(x))^2} + 4y(x) \right)^{-1} d_a + \int^{y(x)} -2 \frac{1}{\sqrt{4x^3 + f^2} +} \right.$$



**2.414 ODE No. 414**

$$x \left( \frac{d}{dx} y(x) \right)^2 + y(x) \frac{d}{dx} y(x) + x^3 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.639 (sec), leaf count = 337

$$\left\{ \int_{-b}^x -\frac{1}{-a} \left( y(x) + \sqrt{-4_a^4 + (y(x))^2} \right) \left( \sqrt{-4_a^4 + (y(x))^2} + 5y(x) \right)^{-1} d_a + \int^{y(x)} 2 \frac{1}{\sqrt{-4x^4 + \dots}} \right.$$

**2.415 ODE No. 415**

$$x \left( \frac{d}{dx} y(x) \right)^2 + y(x) \frac{d}{dx} y(x) - (y(x))^4 = 0$$

**Mathematica:** cpu = 0.210027 (sec), leaf count = 133

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{\tanh^2 \left( \frac{1}{2} (c_1 - \log(x)) \right) - 1}}{2\sqrt{x}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{\tanh^2 \left( \frac{1}{2} (c_1 - \log(x)) \right) - 1}}{2\sqrt{x}} \right\}, \left\{ y(x) \rightarrow -\sqrt{\dots} \right\} \right.$$

**Maple:** cpu = 0.655 (sec), leaf count = 95

$$\left\{ y(x) = -\frac{1}{2} \frac{1}{\sqrt{-x}}, y(x) = \frac{1}{2} \frac{1}{\sqrt{-x}}, y(x) = -\frac{1}{2x} \sqrt{-\left( \tanh \left( -\frac{\ln(x)}{2} + \frac{C1}{2} \right) \right)^2 x + x \left( \tanh \left( -\frac{\ln(x)}{2} \right) \right)^2} \right.$$

**2.416 ODE No. 416**

$$x \left( \frac{d}{dx} y(x) \right)^2 + (y(x) - 3x) \frac{d}{dx} y(x) + y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.546 (sec), leaf count = 136

$$\left\{ -\frac{C1}{x} \left( 5x - y(x) + \sqrt{9x^2 - 10xy(x) + (y(x))^2} \right) \left( \frac{1}{x} \left( 3x - y(x) + \sqrt{9x^2 - 10xy(x) + (y(x))^2} \right) \right) \right.$$

**2.417 ODE No. 417**

$$x \left( \frac{d}{dx} y(x) \right)^2 - y(x) \frac{d}{dx} y(x) + a = 0$$

**Mathematica:** cpu = 0.374047 (sec), leaf count = 430

$$\left\{ \left\{ y(x) \rightarrow -\frac{8a^2}{4a - \sinh(c_1) - \cosh(c_1)} - \frac{\sqrt{16a^3 \sinh(c_1) + 16a^3 \cosh(c_1) - 8a^2 x \sinh(c_1) - 8a^2 x \cosh(c_1)}}{4a - \sinh(c_1) - \cosh(c_1)} \right\} \right.$$

**Maple:** cpu = 0.484 (sec), leaf count = 33

$$\left\{ y(x) = -2\sqrt{ax}, y(x) = 2\sqrt{ax}, y(x) = -C1 x + \frac{a}{-C1} \right\}$$

**2.418 ODE No. 418**

$$x \left( \frac{d}{dx} y(x) \right)^2 - y(x) \frac{d}{dx} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.446057 (sec), leaf count = 165

$$\left\{ \text{Solve} \left[ \frac{\sqrt{\frac{y(x)}{x}} \sqrt{\frac{y(x)}{x}} - 4a - 4a \log \left( \sqrt{\frac{y(x)}{x}} - 4a + \sqrt{\frac{y(x)}{x}} \right) + \frac{y(x)}{x}}{4a} = c_1 + \frac{\log(x)}{2}, y(x) \right], \text{Solve} \left[ \frac{y(x)}{4ax} \right] \right.$$

**Maple:** cpu = 0.515 (sec), leaf count = 55

$$\left\{ y(x) = 0, y(x) = -a^2 x \left( -\text{lambertW} \left( -\frac{xe}{-C1 a} \right) + 1 \right)^2 \left( -\left( -\text{lambertW} \left( -\frac{xe}{-C1 a} \right) + 1 \right) a + a \right)^{-1} \right\}$$

**2.419 ODE No. 419**

$$x \left( \frac{d}{dx} y(x) \right)^2 + 2y(x) \frac{d}{dx} y(x) - x = 0$$

**Mathematica:** cpu = 0.679586 (sec), leaf count = 9073

**Maple:** cpu = 0.531 (sec), leaf count = 110

$$\left\{ x - \frac{C1}{x} \left( -y(x) + \sqrt{(y(x))^2 + x^2} \right) \left( \frac{1}{x^2} \left( 2x^2 + 6(y(x))^2 - 6y(x) \sqrt{(y(x))^2 + x^2} \right) \right)^{-\frac{2}{3}} = 0, \frac{C1}{x} \right\}$$

## 2.420 ODE No. 420

$$x \left( \frac{d}{dx} y(x) \right)^2 - 2y(x) \frac{d}{dx} y(x) + a = 0$$

**Mathematica:** cpu = 1.329169 (sec), leaf count = 11757

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{\frac{16 \sqrt[3]{27a^6 x^{12} - 144a^5 \cosh(3c_1) x^9 - 144a^5 \sinh(3c_1) x^9 + 272a^4 \cosh(6c_1) x^6 + 272a^4 \sinh(6c_1) x^3}}{16 \sqrt[3]{27a^6 x^{12} - 144a^5 \cosh(3c_1) x^9 - 144a^5 \sinh(3c_1) x^9 + 272a^4 \cosh(6c_1) x^6 + 272a^4 \sinh(6c_1) x^3}} \right\} \right\}$$

**Maple:** cpu = 0.546 (sec), leaf count = 897

$$\left\{ y(x) = \frac{x}{2} \left( \frac{1}{6-C1} \sqrt[3]{-36a-C1^2 + 8x^3 + 12\sqrt{a(9a-C1^2 - 4x^3)}-C1} + \frac{2x^2}{3-C1} \sqrt[3]{-36a-C1^2 + 8x^3} \right) \right\}$$

## 2.421 ODE No. 421

$$x \left( \frac{d}{dx} y(x) \right)^2 - 2y(x) \frac{d}{dx} y(x) - x = 0$$

**Mathematica:** cpu = 0.032004 (sec), leaf count = 27

$$\{\{y(x) \rightarrow x \sinh(c_1 - \log(x))\}, \{y(x) \rightarrow x \sinh(c_1 + \log(x))\}\}$$

**Maple:** cpu = 0.437 (sec), leaf count = 31

$$\left\{ y(x) = -ix, y(x) = ix, y(x) = -\frac{C1}{2} \left( -\frac{x^2}{-C1^2} + 1 \right) \right\}$$

**2.422 ODE No. 422**

$$x \left( \frac{d}{dx} y(x) \right)^2 - 2y(x) \frac{d}{dx} y(x) + 4x = 0$$

**Mathematica:** cpu = 0.046506 (sec), leaf count = 49

$$\left\{ \left\{ y(x) \rightarrow 2 \left( 2x \sinh^2 \left( \frac{1}{2}(c_1 - \log(x)) \right) + x \right) \right\}, \left\{ y(x) \rightarrow 2 \left( 2x \sinh^2 \left( \frac{1}{2}(c_1 + \log(x)) \right) + x \right) \right\} \right\}$$

**Maple:** cpu = 0.515 (sec), leaf count = 29

$$\left\{ y(x) = -2x, y(x) = 2x, y(x) = -\frac{C1}{2} \left( -\frac{x^2}{-C1^2} - 4 \right) \right\}$$

**2.423 ODE No. 423**

$$x \left( \frac{d}{dx} y(x) \right)^2 - 2y(x) \frac{d}{dx} y(x) + 2y(x) + x = 0$$

**Mathematica:** cpu = 0.078510 (sec), leaf count = 59

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2}(-2e^{-c_1}x^2 - e^{c_1} + 2x) \right\}, \left\{ y(x) \rightarrow \frac{1}{2}(-e^{c_1}x^2 - 2e^{-c_1} + 2x) \right\} \right\}$$

**Maple:** cpu = 0.515 (sec), leaf count = 52

$$\left\{ y(x) = (1 - \sqrt{2})x, y(x) = (1 + \sqrt{2})x, y(x) = -x \left( \frac{(x + \frac{-C1}{-C1^2})^2}{-C1^2} + 1 \right) \left( -2 \frac{x + \frac{-C1}{-C1}}{-C1} + 2 \right)^{-1} \right\}$$

**2.424 ODE No. 424**

$$x \left( \frac{d}{dx} y(x) \right)^2 + ay(x) \frac{d}{dx} y(x) + bx = 0$$

**Mathematica:** cpu = 0.378048 (sec), leaf count = 223

$$\left\{ \text{Solve} \left[ \frac{-2a \tan^{-1} \left( \frac{ay(x)}{x \sqrt{4b - \frac{a^2 y(x)^2}{x^2}}} \right) + (a+2) \left( 2 \tan^{-1} \left( \frac{(a+2)y(x)}{x \sqrt{4b - \frac{a^2 y(x)^2}{x^2}}} \right) - i \log \left( \frac{(a+1)y(x)^2}{x^2} + b \right) \right)}{8(a+1)} = c_1 + \right. \right.$$

**Maple:** cpu = 0.546 (sec), leaf count = 224

$$\left\{ \frac{-C1}{x} \left( \frac{a}{2x^2} \left( a^2(y(x))^2 + \sqrt{a^2(y(x))^2 - 4bx^2}ay(x) + a(y(x))^2 - 2bx^2 + \sqrt{a^2(y(x))^2 - 4bx^2}y(x) \right) \right) \right\}$$

### 2.425 ODE No. 425

$$(1+x) \left( \frac{d}{dx}y(x) \right)^2 - (y(x)+x) \frac{d}{dx}y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.270034 (sec), leaf count = 59

$$\left\{ \left\{ y(x) \rightarrow -\frac{e^{c_1}(e^{c_1} - 2x)}{2(e^{c_1} + 2)} \right\}, \left\{ y(x) \rightarrow -\frac{2e^{c_1}(2e^{c_1} - x)}{2e^{c_1} + 1} \right\} \right\}$$

**Maple:** cpu = 0.562 (sec), leaf count = 59

$$\left\{ y(x) = \frac{(-C1^2 + C1)x}{-C1 + 1} - \frac{C1^2}{-C1 + 1}, y(x) = x + 2 - 2\sqrt{1+x}, y(x) = x + 2 + 2\sqrt{1+x} \right\}$$

### 2.426 ODE No. 426

$$(3x+1) \left( \frac{d}{dx}y(x) \right)^2 - 3(y(x)+2) \frac{d}{dx}y(x) + 9 = 0$$

**Mathematica:** cpu = 0.392050 (sec), leaf count = 310

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{9x^2 \sinh(c_1) + 9x^2 \cosh(c_1)} - 210x \sinh(c_1) + 6x \sinh(2c_1) - 210x \cosh(c_1) + 6x \cosh(2c_1)}{\sinh(c_1) + \cosh(c_1)} \right\} \right\}$$

**Maple:** cpu = 0.546 (sec), leaf count = 49

$$\left\{ y(x) = -2 - 2\sqrt{3x+1}, y(x) = -2 + 2\sqrt{3x+1}, y(x) = -C1x + \frac{C1^2 - 6C1 + 9}{3 - C1} \right\}$$

**2.427 ODE No. 427**

$$(3x + 5) \left( \frac{d}{dx} y(x) \right)^2 - (3y(x) + x) \frac{d}{dx} y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.634581 (sec), leaf count = 479

$$\left\{ \left\{ y(x) \rightarrow \frac{-\sqrt{5} \sqrt{-144e^{\frac{4c_1}{3}} x^2 - 360e^{\frac{4c_1}{3}} x + 24e^{\frac{8c_1}{3}} x - 225e^{\frac{4c_1}{3}} + 30e^{\frac{8c_1}{3}} - e^{4c_1} + 6e^{\frac{4c_1}{3}} x + 15e^{\frac{4c_1}{3}} - 30x}}{18 \left( e^{\frac{4c_1}{3}} + 5 \right)} \right. \right.$$

**Maple:** cpu = 0.452 (sec), leaf count = 67

$$\left\{ y(x) = \frac{(-3\_C1^2 + \_C1) x}{-3\_C1 + 1} - 5 \frac{\_C1^2}{-3\_C1 + 1}, y(x) = \frac{x}{3} + \frac{10}{9} - \frac{2}{9} \sqrt{15x + 25}, y(x) = \frac{x}{3} + \frac{10}{9} + \frac{2}{9} \sqrt{15x + 25} \right.$$

**2.428 ODE No. 428**

$$ax \left( \frac{d}{dx} y(x) \right)^2 + (bx - ay(x) + c) \frac{d}{dx} y(x) - by(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.546 (sec), leaf count = 85

$$\left\{ y(x) = \frac{1}{a} (-bx + c - 2\sqrt{-bcx}), y(x) = \frac{1}{a} (-bx + c + 2\sqrt{-bcx}), y(x) = -\frac{(a\_C1^2 + \_C1 b) x}{-\_C1 a - b} - \frac{c}{-\_C1 a - b} \right.$$

**2.429 ODE No. 429**

$$ax \left( \frac{d}{dx} y(x) \right)^2 - (ay(x) + bx - a - b) \frac{d}{dx} y(x) + by(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.437 (sec), leaf count = 96

$$\left\{ y(x) = \frac{1}{a} (bx + a + b - 2\sqrt{abx + b^2x}), y(x) = \frac{1}{a} (bx + a + b + 2\sqrt{abx + b^2x}), y(x) = \frac{(-a\_C1^2 + \_C1 b) x}{-\_C1 a + b} + \frac{c}{-\_C1 a + b} \right.$$

**2.430 ODE No. 430**

$$(a_2 x + c_2) \left( \frac{d}{dx} y(x) \right)^2 + (a_1 x + b_1 y(x) + c_1) \frac{d}{dx} y(x) + a_0 x + b_0 y(x) + c_0 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 1.201 (sec), leaf count = 9885

$$\left\{ \frac{-C1}{a_2 x + c_2} \left( -\frac{1}{2 (a_2 x + c_2)^2} \left( 2 a_0 a_2 b_1 x^2 + 2 a_0 b_1 c_2 x + 2 a_2 b_1 c_0 x + a_1 c_1 c_2 + b_0 c_1 c_2 + 2 a_1 c_1 c_0 \right) \right) \right\}$$

**2.431 ODE No. 431**

$$x^2 \left( \frac{d}{dx} y(x) \right)^2 - (y(x))^4 + (y(x))^2 = 0$$

**Mathematica:** cpu = 0.037005 (sec), leaf count = 111

$$\left\{ \left\{ y(x) \rightarrow \sqrt{\tan^2 (c_1 - \log(x)) + 1} (-\cot (c_1 - \log(x))) \right\}, \left\{ y(x) \rightarrow \sqrt{\tan^2 (c_1 - \log(x)) + 1} \cot (c_1 - \log(x)) \right\} \right\}$$

**Maple:** cpu = 0.561 (sec), leaf count = 62

$$\left\{ y(x) = -1, y(x) = 1, y(x) = \frac{1}{\tan (-\ln (x) + \_C1)} \sqrt{(\tan (-\ln (x) + \_C1))^2 + 1}, y(x) = -\frac{1}{\tan (-\ln (x) + \_C1)} \sqrt{(\tan (-\ln (x) + \_C1))^2 + 1} \right\}$$

**2.432 ODE No. 432**

$$\left( x \frac{d}{dx} y(x) + a \right)^2 - 2 a y(x) + x^2 = 0$$

**Mathematica:** cpu = 1.713718 (sec), leaf count = 64

$$\text{Solve} \left[ \left\{ y(x) = \frac{a^2 + 2a \sqrt{K\$1274426x + K\$1274426^2 x^2 + x^2}}{2a}, x = \frac{c_1}{\sqrt{K\$1274426^2 + 1}} - \frac{a \sinh^{-1}(K\$1274426x + K\$1274426^2 x^2 + x^2)}{\sqrt{K\$1274426^2 + 1}} \right\} \right]$$

**Maple:** cpu = 7.551 (sec), leaf count = 615

$$\left\{ y(x) = -\frac{(\text{RootOf}((\text{Arcsinh}(\_Z))^2 a^2 - \_Z^2 x^2 - 2 \text{Arcsinh}(\_Z) \_C1 a + \_C1^2 - x^2))^4 x^2}{-2 (\text{RootOf}((\text{Arcsinh}(\_Z))^2 a^2 - \_Z^2 x^2 - 2 \text{Arcsinh}(\_Z) \_C1 a + \_C1^2 - x^2))^2 a - 2 a} \right\}$$

**2.433 ODE No. 433**

$$\left(x \frac{d}{dx} y(x) + y(x) + 2x\right)^2 - 4xy(x) - 4x^2 - 4a = 0$$

**Mathematica:** cpu = 0.510065 (sec), leaf count = 22

$$\left\{ \left\{ y(x) \rightarrow \frac{-a - 2c_1x + c_1^2}{x} \right\} \right\}$$

**Maple:** cpu = 0.640 (sec), leaf count = 32

$$\left\{ y(x) = -\frac{x^2 + a}{x}, y(x) = -C1 + \frac{1}{x} \left( \frac{-C1^2}{4} - a \right) \right\}$$

**2.434 ODE No. 434**

$$\frac{d}{dx} y(x) - 1 = 0$$

**Mathematica:** cpu = 0.032004 (sec), leaf count = 27

$$\{ \{ y(x) \rightarrow x \sinh(c_1 - \log(x)) \}, \{ y(x) \rightarrow x \sinh(c_1 + \log(x)) \} \}$$

**Maple:** cpu = 0.015 (sec), leaf count = 7

$$\{ y(x) = x + \_C1 \}$$

**2.435 ODE No. 435**

$$x^2 \left( \frac{d}{dx} y(x) \right)^2 - 2xy(x) \frac{d}{dx} y(x) + y(x) (1 + y(x)) - x = 0$$

**Mathematica:** cpu = 0.037005 (sec), leaf count = 61

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4} (c_1^2 x - 4ic_1 \sqrt{x} + 4x - 4) \right\}, \left\{ y(x) \rightarrow \frac{1}{4} (c_1^2 x + 4ic_1 \sqrt{x} + 4x - 4) \right\} \right\}$$

**Maple:** cpu = 0.671 (sec), leaf count = 22

$$\left\{ y(x) = x, y(x) = -C1 \sqrt{x} - \frac{x - C1^2}{4} + x - 1 \right\}$$



**2.436 ODE No. 436**

$$x^2 \left( \frac{d}{dx} y(x) \right)^2 - 2xy(x) \frac{d}{dx} y(x) + (y(x))^2 (-x^2 + 1) - x^4 = 0$$

**Mathematica:** cpu = 0.034504 (sec), leaf count = 26

$$\{ \{y(x) \rightarrow -x \sinh(x - c_1)\}, \{y(x) \rightarrow x \sinh(c_1 + x)\} \}$$

**Maple:** cpu = 1.809 (sec), leaf count = 59

$$\left\{ y(x) = -ix, y(x) = ix, y(x) = -\frac{C1 x}{2 e^x} \left( \frac{(e^x)^2}{-C1^2} - 1 \right), y(x) = \frac{x((e^x)^2 - C1^2 - 1)}{2 e^x - C1} \right\}$$

**2.437 ODE No. 437**

$$x^2 \left( \frac{d}{dx} y(x) \right)^2 - (2xy(x) + a) \frac{d}{dx} y(x) + (y(x))^2 = 0$$

**Mathematica:** cpu = 0.274035 (sec), leaf count = 47

$$\left\{ \left\{ y(x) \rightarrow \frac{x - 2\sqrt{ac_1}}{4c_1^2} \right\}, \left\{ y(x) \rightarrow \frac{2\sqrt{ac_1} + x}{4c_1^2} \right\} \right\}$$

**Maple:** cpu = 0.515 (sec), leaf count = 36

$$\left\{ y(x) = -\frac{a}{4x}, y(x) = -C1 x - \sqrt{-C1 a}, y(x) = -C1 x + \sqrt{-C1 a} \right\}$$

**2.438 ODE No. 438**

$$x^2 \left( \frac{d}{dx} y(x) \right)^2 + 3xy(x) \frac{d}{dx} y(x) + 2(y(x))^2 = 0$$

**Mathematica:** cpu = 0.010501 (sec), leaf count = 21

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{x^2} \right\}, \left\{ y(x) \rightarrow \frac{c_1}{x} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 17

$$\left\{ y(x) = \frac{C1}{x^2}, y(x) = \frac{C1}{x} \right\}$$

**2.439 ODE No. 439**

$$x^2 \left( \frac{d}{dx} y(x) \right)^2 + 3xy(x) \frac{d}{dx} y(x) + 3(y(x))^2 = 0$$

**Mathematica:** cpu = 0.034504 (sec), leaf count = 49

$$\left\{ \left\{ y(x) \rightarrow c_1 x^{\frac{1}{2}(-3-i\sqrt{3})} \right\}, \left\{ y(x) \rightarrow c_1 x^{\frac{1}{2}i(\sqrt{3}+3i)} \right\} \right\}$$

**Maple:** cpu = 0.546 (sec), leaf count = 33

$$\left\{ y(x) = \_C1 x^{-\frac{i}{2}\sqrt{3}} x^{-\frac{3}{2}}, y(x) = \_C1 x^{\frac{i}{2}\sqrt{3}} x^{-\frac{3}{2}} \right\}$$

**2.440 ODE No. 440**

$$x^2 \left( \frac{d}{dx} y(x) \right)^2 + 4xy(x) \frac{d}{dx} y(x) - 5(y(x))^2 = 0$$

**Mathematica:** cpu = 0.009001 (sec), leaf count = 19

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{x^5} \right\}, \left\{ y(x) \rightarrow c_1 x \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 15

$$\left\{ y(x) = \frac{-C1}{x^5}, y(x) = \_C1 x \right\}$$

**2.441 ODE No. 441**

$$x^2 \left( \frac{d}{dx} y(x) \right)^2 - 4x(y(x) + 2) \frac{d}{dx} y(x) + 4y(x)(y(x) + 2) = 0$$

**Mathematica:** cpu = 0.064508 (sec), leaf count = 65

$$\left\{ \left\{ y(x) \rightarrow -e^{-c_1} x \left( 2\sqrt{2} e^{\frac{c_1}{2}} - x \right) \right\}, \left\{ y(x) \rightarrow e^{\frac{c_1}{2}} x \left( e^{\frac{c_1}{2}} x - 2\sqrt{2} \right) \right\} \right\}$$

**Maple:** cpu = 1.311 (sec), leaf count = 265

$$\left\{ y(x) = -2, y(x) = \frac{x^2}{-C1} \left( -2 \frac{\sqrt{2}\sqrt{x^2-C1}}{x^2} + 1 \right), y(x) = \frac{x^2}{-C1} \left( 2 \frac{\sqrt{2}\sqrt{x^2-C1}}{x^2} + 1 \right), y(x) = -\frac{1}{-C1^2} \right\}$$

**2.442 ODE No. 442**

$$x^2 \left( \frac{d}{dx} y(x) \right)^2 + (x^2 y(x) - 2xy(x) + x^3) \frac{d}{dx} y(x) + ((y(x))^2 - x^2 y(x)) (1 - x) = 0$$

**Mathematica:** cpu = 0.007501 (sec), leaf count = 28

$$\{ \{y(x) \rightarrow c_1 e^{-x} x\}, \{y(x) \rightarrow c_1 x - x^2\} \}$$

**Maple:** cpu = 0.0 (sec), leaf count = 21

$$\{y(x) = (-x + \_C1) x, y(x) = \_C1 e^{-x} x\}$$

**2.443 ODE No. 443**

$$x \left( x \frac{d}{dx} y(x) - y(x) \right)^2 - \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.552570 (sec), leaf count = 1921

$$\{ \{y(x) \rightarrow \text{Root}[1024x^{12} - 576e^{12c_1} \#1^4 x^8 - 2176e^{12c_1} \#1^3 x^6 + 81e^{24c_1} \#1^8 x^4 - 1536e^{12c_1} \#1^2 x^4 + 36e^{24c_1} \#1^8, 1]\} \}$$

**Maple:** cpu = 1.638 (sec), leaf count = 221

$$\left\{ y(x) = -\frac{2}{9x^2}, y(x) = \frac{(\text{RootOf}(-729\_C1 x^{12} + \_Z^8 - 12\_Z^7 + 60\_Z^6 - 160\_Z^5 + 240\_Z^4 - 192\_Z^3 + 72\_Z^2 - 9\_Z + 1), \_Z)}{9x^2} \right\}$$

**2.444 ODE No. 444**

$$x^2 \left( \frac{d}{dx} y(x) \right)^2 - y(x) (y(x) - 2x) \frac{d}{dx} y(x) + (y(x))^2 = 0$$

**Mathematica:** cpu = 0.143518 (sec), leaf count = 103

$$\left\{ \left\{ y(x) \rightarrow -\frac{4e^{-2c_1}}{e^{2c_1} x - 2} \right\}, \left\{ y(x) \rightarrow -\frac{4e^{-2c_1}}{e^{2c_1} x + 2} \right\}, \left\{ y(x) \rightarrow -\frac{e^{-2c_1}}{2(2e^{2c_1} x - 1)} \right\}, \left\{ y(x) \rightarrow -\frac{e^{-2c_1}}{2(2e^{2c_1} x + 1)} \right\} \right\}$$

**Maple:** cpu = 1.045 (sec), leaf count = 121

$$\left\{ y(x) = 4x, y(x) = -\frac{\_C1^2(\sqrt{2}\_C1 - 2x)}{2\_C1^2 - 4x^2}, y(x) = -2\frac{\_C1^2(\sqrt{2}\_C1 - x)}{2\_C1^2 - x^2}, y(x) = 2\frac{\_C1^2(\sqrt{2}\_C1 + x)}{2\_C1^2 - x^2} \right\}$$

**2.445 ODE No. 445**

$$x^2 \left( \frac{d}{dx} y(x) \right)^2 + (ax^2(y(x))^3 + b) \frac{d}{dx} y(x) + ab(y(x))^3 = 0$$

**Mathematica:** cpu = 0.009001 (sec), leaf count = 49

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{\sqrt{2ax - 2c_1}} \right\}, \left\{ y(x) \rightarrow \frac{1}{\sqrt{2ax - 2c_1}} \right\}, \left\{ y(x) \rightarrow \frac{b}{x} + c_1 \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 35

$$\left\{ y(x) = \frac{1}{\sqrt{2ax + \_C1}}, y(x) = -\frac{1}{\sqrt{2ax + \_C1}}, y(x) = \frac{b}{x} + \_C1 \right\}$$

**2.446 ODE No. 446**

$$(x^2 + 1) \left( \frac{d}{dx} y(x) \right)^2 - 2xy(x) \frac{d}{dx} y(x) + (y(x))^2 - 1 = 0$$

**Mathematica:** cpu = 0.490562 (sec), leaf count = 201

$$\left\{ \left\{ y(x) \rightarrow \frac{e^{2c_1}x - 2e^{c_1} - x}{e^{2c_1} + 1} \right\}, \left\{ y(x) \rightarrow \frac{e^{2c_1}x + 2e^{c_1} - x}{e^{2c_1} + 1} \right\}, \left\{ y(x) \rightarrow \frac{-e^{4c_1}x - 2\sqrt{-e^{2c_1} + 2e^{4c_1} - e^{6c_1}}}{2e^{2c_1} - e^{4c_1} - 1} \right\} \right\}$$

**Maple:** cpu = 0.577 (sec), leaf count = 57

$$\left\{ y(x) = \sqrt{x^2 + 1}, y(x) = -\sqrt{x^2 + 1}, y(x) = \_C1 x - \sqrt{\_C1^2 + 1}, y(x) = \_C1 x + \sqrt{\_C1^2 + 1} \right\}$$

**2.447 ODE No. 447**

$$(x^2 - 1) \left( \frac{d}{dx} y(x) \right)^2 - 1 = 0$$

**Mathematica:** cpu = 0.015502 (sec), leaf count = 41

$$\left\{ \left\{ y(x) \rightarrow c_1 - \log(\sqrt{x^2 - 1} + x) \right\}, \left\{ y(x) \rightarrow c_1 + \log(\sqrt{x^2 - 1} + x) \right\} \right\}$$

**Maple:** cpu = 0.468 (sec), leaf count = 33

$$\left\{ y(x) = -\ln(x + \sqrt{x^2 - 1}) + \_C1, y(x) = \ln(x + \sqrt{x^2 - 1}) + \_C1 \right\}$$

**2.448 ODE No. 448**

$$(x^2 - 1) \left( \frac{d}{dx} y(x) \right)^2 - (y(x))^2 + 1 = 0$$

**Mathematica:** cpu = 0.091512 (sec), leaf count = 109

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( e^{-c_1} \sqrt{x^2 - 1} - e^{c_1} \sqrt{x^2 - 1} + e^{-c_1} x + e^{c_1} x \right) \right\}, \left\{ y(x) \rightarrow \frac{1}{2} \left( -e^{-c_1} \sqrt{x^2 - 1} + e^{c_1} \sqrt{x^2 - 1} + \right. \right. \right.$$

**Maple:** cpu = 10.858 (sec), leaf count = 166

$$\left. \left\{ 1 \sqrt{(-1 + y(x))(1 + y(x))} \ln \left( y(x) + \sqrt{(y(x))^2 - 1} \right) \frac{1}{\sqrt{-1 + y(x)}} \frac{1}{\sqrt{1 + y(x)}} + \int^x \frac{1}{-a^2 - 1} \sqrt{(-a^2} \right. \right.$$

**2.449 ODE No. 449**

$$(-a^2 + x^2) \left( \frac{d}{dx} y(x) \right)^2 + 2xy(x) \frac{d}{dx} y(x) + (y(x))^2 = 0$$

**Mathematica:** cpu = 0.010001 (sec), leaf count = 27

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{a - x} \right\}, \left\{ y(x) \rightarrow \frac{c_1}{a + x} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 23

$$\left\{ y(x) = \frac{-C1}{a - x}, y(x) = \frac{-C1}{x + a} \right\}$$

**2.450 ODE No. 450**

$$(-a^2 + x^2) \left( \frac{d}{dx} y(x) \right)^2 - 2xy(x) \frac{d}{dx} y(x) - x^2 = 0$$

**Mathematica:** cpu = 0.453058 (sec), leaf count = 26

$$\left\{ \left\{ y(x) \rightarrow \frac{a^2 + c_1^2 - x^2}{2c_1} \right\} \right\}$$

**Maple:** cpu = 0.795 (sec), leaf count = 51

$$\left\{ y(x) = \sqrt{a^2 - x^2}, y(x) = -\sqrt{a^2 - x^2}, y(x) = x^2 - C1 - C1 a^2 - \frac{1}{4 - C1} \right\}$$

**2.451 ODE No. 451**

$$(x^2 + a) \left( \frac{d}{dx} y(x) \right)^2 - 2xy(x) \frac{d}{dx} y(x) + (y(x))^2 + b = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.561 (sec), leaf count = 78

$$\left\{ y(x) = \frac{1}{a} \sqrt{-ab(x^2 + a)}, y(x) = -\frac{1}{a} \sqrt{-ab(x^2 + a)}, y(x) = -C1 x - \sqrt{-a - C1^2 - b}, y(x) = -C1 x + \sqrt{-a - C1^2 - b} \right\}$$

**2.452 ODE No. 452**

$$(2x^2 + 1) \left( \frac{d}{dx} y(x) \right)^2 + ((y(x))^2 + 2xy(x) + x^2 + 2) \frac{d}{dx} y(x) + 2(y(x))^2 + 1 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 1.779 (sec), leaf count = 37

$$\left\{ y(x) = -3x - 2\sqrt{2x^2 + 1}, y(x) = -3x + 2\sqrt{2x^2 + 1} \right\}$$

**2.453 ODE No. 453**

$$(a^2 - 1) x^2 \left( \frac{d}{dx} y(x) \right)^2 + 2xy(x) \frac{d}{dx} y(x) - (y(x))^2 + a^2 x^2 = 0$$

**Mathematica:** cpu = 0.573073 (sec), leaf count = 395

$$\left\{ \text{Solve} \left[ \frac{a \left( -\log \left( \frac{(a^2-1) \left( a \sqrt{a^2 - \frac{y(x)^2}{x^2} - 1} + a^2 - \frac{iy(x)}{x} - 1 \right)}{a^3 \left( \frac{y(x)}{x} - i \right)} \right) + \log \left( -\frac{(a^2-1) \left( a \sqrt{a^2 - \frac{y(x)^2}{x^2} - 1} + a^2 + \frac{iy(x)}{x} - 1 \right)}{a^3 \left( \frac{y(x)}{x} + i \right)} \right) + \log \left( \frac{y(x)}{x} \right)}{2(a^2 - 1)} \right] \right.$$

**Maple:** cpu = 1.170 (sec), leaf count = 229

$$\left\{ \ln(x) - \frac{1}{a} \sqrt{-a^2} \arctan \left( \frac{a^2 y(x)}{x} \frac{1}{\sqrt{-a^2}} \frac{1}{\sqrt{-\frac{a^2 x^2 - x^2 - (y(x))^2}{x^2}}} \right) + \frac{1}{2} \ln \left( \frac{(y(x))^2 + x^2}{x^2} \right) + \frac{1}{a} \ln \left( \frac{1}{x} \left( \sqrt{-a^2} \right) \right) \right\}$$

## 2.454 ODE No. 454

$$ax^2 \left( \frac{d}{dx} y(x) \right)^2 - 2axy(x) \frac{d}{dx} y(x) + (y(x))^2 - a(a-1)x^2 = 0$$

**Mathematica:** cpu = 0.154520 (sec), leaf count = 118

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} e^{-c_1} x^{1 - \frac{\sqrt{a-1}}{\sqrt{a}}} \left( e^{2c_1} - ax \frac{2\sqrt{a-1}}{\sqrt{a}} \right) \right\}, \left\{ y(x) \rightarrow \frac{1}{2} e^{-c_1} x^{1 - \frac{\sqrt{a-1}}{\sqrt{a}}} \left( e^{2c_1} x \frac{2\sqrt{a-1}}{\sqrt{a}} - a \right) \right\} \right\}$$

**Maple:** cpu = 0.593 (sec), leaf count = 138

$$\left\{ y(x) = \sqrt{-ax}, y(x) = \text{RootOf} \left( -\ln(x) - \int^{-Z} \frac{1}{-a^2 a - a^2 + a^2 - a} \sqrt{(-a^2 a - a^2 + a^2 - a) ad - a} + \right) \right\}$$

## 2.455 ODE No. 455

$$x^3 \left( \frac{d}{dx} y(x) \right)^2 + x^2 y(x) \frac{d}{dx} y(x) + a = 0$$

**Mathematica:** cpu = 0.400551 (sec), leaf count = 123

$$\left\{ \left\{ y(x) \rightarrow -\frac{e^{-\frac{c_1}{2}} (2ae^{c_1} + x)}{\sqrt{2x}} \right\}, \left\{ y(x) \rightarrow \frac{e^{-\frac{c_1}{2}} (2ae^{c_1} + x)}{\sqrt{2x}} \right\}, \left\{ y(x) \rightarrow -\frac{e^{-\frac{c_1}{2}} (2ax + e^{c_1})}{\sqrt{2x}} \right\}, \left\{ y(x) \rightarrow \frac{e^{-\frac{c_1}{2}} (2ax + e^{c_1})}{\sqrt{2x}} \right\} \right\}$$

**Maple:** cpu = 0.686 (sec), leaf count = 66

$$\left\{ y(x) = -2 \frac{\sqrt{ax}}{x}, y(x) = 2 \frac{\sqrt{ax}}{x}, y(x) = \frac{C1^2 + 4ax}{2\_C1 x}, y(x) = \frac{C1^2 x + 4a}{2\_C1 x} \right\}$$

**2.456 ODE No. 456**

$$x(x^2 - 1) \left( \frac{d}{dx} y(x) \right)^2 + 2(-x^2 + 1) y(x) \frac{d}{dx} y(x) + x(y(x))^2 - x = 0$$

**Mathematica:** cpu = 0.122516 (sec), leaf count = 79

$$\left\{ \left\{ y(x) \rightarrow x + 2x \sinh^2 \left( \frac{1}{2} \left( c_1 - 2i \tan^{-1} \left( \frac{\sqrt{x-1}}{\sqrt{x+1}} \right) \right) \right) \right\}, \left\{ y(x) \rightarrow x + 2x \sinh^2 \left( \frac{1}{2} \left( c_1 + 2i \tan^{-1} \left( \frac{\sqrt{x-1}}{\sqrt{x+1}} \right) \right) \right) \right\} \right\}$$

**Maple:** cpu = 0.874 (sec), leaf count = 33

$$\left\{ y(x) = x, y(x) = -x, y(x) = \sqrt{-C1^2 + 1} + \sqrt{x^2 - 1} C1 \right\}$$

**2.457 ODE No. 457**

$$x^4 \left( \frac{d}{dx} y(x) \right)^2 - x \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.948120 (sec), leaf count = 410

$$\left\{ \text{Solve} \left[ \frac{x \sqrt{4x^2 y(x) + 1} \left( \log(x) - \log \left( \sqrt{4x^2 y(x) + 1} + 1 \right) \right)}{\sqrt{4x^4 y(x) + x^2}} + \frac{x \sqrt{4x^2 y(x) + 1} \log(y(x)) - x \sqrt{4x^2 y(x)}}{\sqrt{4x^4 y(x) + x^2}} \right] \right\}$$

**Maple:** cpu = 1.186 (sec), leaf count = 135

$$\left\{ y(x) = -\frac{1}{4x^2}, y(x) = \frac{-C1(-C1 - 2ix) - C1^2 - 2x^2}{2C1^2 x^2}, y(x) = \frac{-C1(-C1 + 2ix) - C1^2 - 2x^2}{2C1^2 x^2} \right\}$$

**2.458 ODE No. 458**

$$x^2(-a^2 + x^2) \left( \frac{d}{dx} y(x) \right)^2 - 1 = 0$$

**Mathematica:** cpu = 0.059508 (sec), leaf count = 139

$$\left\{ \left\{ y(x) \rightarrow c_1 - \frac{ix \sqrt{x^2 - a^2} \log \left( \frac{2(\sqrt{x^2 - a^2} - ia)}{x} \right)}{a \sqrt{x^4 - a^2 x^2}} \right\}, \left\{ y(x) \rightarrow c_1 + \frac{ix \sqrt{x^2 - a^2} \log \left( \frac{2(\sqrt{x^2 - a^2} - ia)}{x} \right)}{a \sqrt{x^4 - a^2 x^2}} \right\} \right\}$$

**Maple:** cpu = 0.593 (sec), leaf count = 90

$$\left\{ y(x) = -1 \ln \left( \frac{1}{x} \left( -2a^2 + 2 \sqrt{-a^2} \sqrt{-a^2 + x^2} \right) \right) \frac{1}{\sqrt{-a^2}} + C1, y(x) = 1 \ln \left( \frac{1}{x} \left( -2a^2 + 2 \sqrt{-a^2} \sqrt{-a^2 + x^2} \right) \right) \frac{1}{\sqrt{-a^2}} + C1 \right\}$$



**2.459 ODE No. 459**

$$e^{-2x} \left( \frac{d}{dx} y(x) \right)^2 - \left( \frac{d}{dx} y(x) - 1 \right)^2 + e^{-2y(x)} = 0$$

**Mathematica:** cpu = 2.602831 (sec), leaf count = 271

$$\left\{ \left\{ y(x) \rightarrow \log \left( -\frac{e^{-c_1}(e^x + 1)(e^{2c_1+x} - e^{2c_1} - e^x - 1)}{\sqrt{8e^x + 4e^{2x} + 4}} \right) \right\}, \left\{ y(x) \rightarrow \log \left( \frac{e^{-c_1}(e^x + 1)(e^{2c_1+x} - e^{2c_1} - e^x - 1)}{\sqrt{8e^x + 4e^{2x} + 4}} \right) \right\} \right.$$

**Maple:** cpu = 0.422 (sec), leaf count = 65

$$\left\{ y(x) = x + \ln \left( \frac{1}{e^x} \left( -1 - \sqrt{(e^x)^2 - \frac{(e^x)^2}{(e^{-C_1})^2}} \right) \right) + _-C_1, y(x) = x + \ln \left( \frac{1}{e^x} \left( -1 + \sqrt{(e^x)^2 - \frac{(e^x)^2}{(e^{-C_1})^2}} \right) \right) \right.$$

**2.460 ODE No. 460**

$$\left( \left( \frac{d}{dx} y(x) \right)^2 + (y(x))^2 \right) (\cos(x))^4 - a^2 = 0$$

**Mathematica:** cpu = 56.015113 (sec), leaf count = 28

$$\text{DSolve}[\cos^4(x) (y'(x)^2 + y(x)^2) - a^2 = 0, y(x), x]$$

**Maple:** cpu = 5.163 (sec), leaf count = 0

could not solve

**2.461 ODE No. 461**

$$d_0(x) \left( \frac{d}{dx} y(x) \right)^2 + 2 b_0(x) y(x) \frac{d}{dx} y(x) + c_0(x) (y(x))^2 + 2 d_0(x) \frac{d}{dx} y(x) + 2 e_0(x) y(x) + f_0(x) = 0$$

**Mathematica:** cpu = 108.142232 (sec), leaf count = 49

$$\text{DSolve}[a(x)y'(x)^2 + 2b(x)y(x)y'(x) + c(x)y(x)^2 + 2d(x)y'(x) + 2e(x)y(x) + f(x) = 0, y(x), x]$$

**Maple:** cpu = 19.953 (sec), leaf count = 0

could not solve

**2.462 ODE No. 462**

$$y(x) \left( \frac{d}{dx} y(x) \right)^2 - 1 = 0$$

**Mathematica:** cpu = 0.014502 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow \left( \frac{3}{2} \right)^{2/3} (c_1 - x)^{2/3} \right\}, \left\{ y(x) \rightarrow \left( \frac{3}{2} \right)^{2/3} (c_1 + x)^{2/3} \right\} \right\}$$

**Maple:** cpu = 0.577 (sec), leaf count = 27

$$\left\{ x - \frac{2}{3}(y(x))^{\frac{3}{2}} - \_C1 = 0, x + \frac{2}{3}(y(x))^{\frac{3}{2}} - \_C1 = 0 \right\}$$

**2.463 ODE No. 463**

$$y(x) \left( \frac{d}{dx} y(x) \right)^2 - e^{2x} = 0$$

**Mathematica:** cpu = 0.017002 (sec), leaf count = 47

$$\left\{ \left\{ y(x) \rightarrow \left( \frac{3}{2} \right)^{2/3} (c_1 - e^x)^{2/3} \right\}, \left\{ y(x) \rightarrow \left( \frac{3}{2} \right)^{2/3} (c_1 + e^x)^{2/3} \right\} \right\}$$

**Maple:** cpu = 1.092 (sec), leaf count = 50

$$\left\{ -1\sqrt{y(x)(e^x)^2} \frac{1}{\sqrt{y(x)}} + \frac{2}{3}(y(x))^{\frac{3}{2}} + \_C1 = 0, 1\sqrt{y(x)(e^x)^2} \frac{1}{\sqrt{y(x)}} + \frac{2}{3}(y(x))^{\frac{3}{2}} + \_C1 = 0 \right\}$$

**2.464 ODE No. 464**

$$y(x) \left( \frac{d}{dx} y(x) \right)^2 + 2x \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.061008 (sec), leaf count = 52

$$\left\{ \left\{ y(x) \rightarrow -e^{\frac{c_1}{2}} \sqrt{e^{c_1} - 2x} \right\}, \left\{ y(x) \rightarrow e^{\frac{c_1}{2}} \sqrt{e^{c_1} - 2x} \right\} \right\}$$

**Maple:** cpu = 0.983 (sec), leaf count = 71

$$\left\{ y(x) = \sqrt{\_C1^2 - 2\_C1 x}, y(x) = \sqrt{\_C1^2 + 2\_C1 x}, y(x) = -ix, y(x) = ix, y(x) = -\sqrt{\_C1^2 - 2\_C1 x} \right\}$$

**2.465 ODE No. 465**

$$y(x) \left( \frac{d}{dx} y(x) \right)^2 + 2x \frac{d}{dx} y(x) - 9y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.640 (sec), leaf count = 209

$$\left\{ -\frac{C1 x}{2} \left( -x + \sqrt{x^2 + 9 (y(x))^2} \right) \left( \frac{1}{y(x)} \left( -x + \sqrt{x^2 + 9 (y(x))^2} \right) \right)^{\frac{2}{7}} \left( x \sqrt{x^2 + 9 (y(x))^2} - x^2 - (y(x))^2 \right) \right\}$$

**2.466 ODE No. 466**

$$y(x) \left( \frac{d}{dx} y(x) \right)^2 - 2x \frac{d}{dx} y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.248532 (sec), leaf count = 145

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{-2x \sinh(c_1) - 2x \cosh(c_1) - \sinh(2c_1) - \cosh(2c_1)} \right\}, \left\{ y(x) \rightarrow \sqrt{-2x \sinh(c_1) - 2x \cosh(c_1) - \sinh(2c_1) - \cosh(2c_1)} \right\} \right\}$$

**Maple:** cpu = 0.811 (sec), leaf count = 71

$$\left\{ y(x) = x, y(x) = \sqrt{-C1^2 - 2ix\_C1}, y(x) = \sqrt{-C1^2 + 2ix\_C1}, y(x) = -x, y(x) = -\sqrt{-C1^2 - 2ix\_C1} \right\}$$

**2.467 ODE No. 467**

$$y(x) \left( \frac{d}{dx} y(x) \right)^2 - 4x \frac{d}{dx} y(x) + y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.655 (sec), leaf count = 148

$$\left\{ -\frac{C1 x}{y(x)} \frac{1}{\sqrt[3]{\frac{1}{y(x)} \left( 2x - \sqrt{4x^2 - (y(x))^2} \right)}} \frac{1}{\sqrt[3]{\frac{1}{(y(x))^2} \left( 8x^2 - 4(y(x))^2 - 4x \sqrt{4x^2 - (y(x))^2} \right)}} + x = 0, \right\}$$

**2.468 ODE No. 468**

$$y(x) \left( \frac{d}{dx} y(x) \right)^2 - 4a^2 x \frac{d}{dx} y(x) + a^2 y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.577 (sec), leaf count = 181

$$\left\{ \frac{-C1 x}{ay(x)} \frac{1}{\sqrt[3]{\frac{a}{y(x)} \left( 2ax + \sqrt{4a^2x^2 - (y(x))^2} \right)}} \frac{1}{\sqrt[3]{\frac{a^2}{(y(x))^2} \left( 2a^2x^2 + \sqrt{4a^2x^2 - (y(x))^2} ax - (y(x))^2 \right)}} + x \right.$$

**2.469 ODE No. 469**

$$y(x) \left( \frac{d}{dx} y(x) \right)^2 + ax \frac{d}{dx} y(x) + by(x) = 0$$

**Mathematica:** cpu = 0.945120 (sec), leaf count = 317

$$\left\{ \text{Solve} \left[ \frac{\left( \sqrt{a^2 - \frac{4by(x)^2}{x^2}} - a \right) \left( \sqrt{a^2 - \frac{4by(x)^2}{x^2}} + a + 2b \right) \left( a \log \left( \sqrt{a^2 - \frac{4by(x)^2}{x^2}} - a \right) + (a + 2b) \log \left( \sqrt{a^2 - \frac{4by(x)^2}{x^2}} + a + 2b \right) \right)}{8b(a + b) \left( \sqrt{a^2 - \frac{4by(x)^2}{x^2}} - a - \frac{2y(x)^2}{x^2} \right)} \right]$$

**Maple:** cpu = 0.639 (sec), leaf count = 242

$$\left\{ \frac{-C1 x}{(y(x))^2} \left( -\frac{1}{2y(x)} \left( ax + \sqrt{a^2x^2 - 4b(y(x))^2} \right) \right)^{-\frac{a}{a+b}} \left( ax + \sqrt{a^2x^2 - 4b(y(x))^2} \right) \left( \frac{a}{2(y(x))^2} \left( ax^2 + \right) \right) \right.$$

**2.470 ODE No. 470**

$$y(x) \left( \frac{d}{dx} y(x) \right)^2 + x^3 \frac{d}{dx} y(x) - x^2 y(x) = 0$$

**Mathematica:** cpu = 0.883112 (sec), leaf count = 454

$$\left\{ \text{Solve} \left[ \frac{\sqrt{x^6 + 4x^2 y(x)^2} \log \left( \sqrt{x^4 + 4y(x)^2 + x^2} \right) - x \sqrt{x^4 + 4y(x)^2} \log \left( y(x)^2 \right) + x \sqrt{x^4 + 4y(x)^2} \log \left( y(x)^2 \right)}{2x \sqrt{x^4 + 4y(x)^2}} \right] \right.$$

**Maple:** cpu = 0.780 (sec), leaf count = 87

$$\left\{ y(x) = -\frac{i}{2} x^2, y(x) = \frac{i}{2} x^2, y(x) = -\frac{1}{4} \sqrt{-4x^2\_C1 + \_C1^2}, y(x) = \frac{1}{4} \sqrt{-4x^2\_C1 + \_C1^2}, y(x) = -2 \right.$$

**2.471 ODE No. 471**

$$y(x) \left( \frac{d}{dx} y(x) \right)^2 - (y(x) - x) \frac{d}{dx} y(x) - x = 0$$

**Mathematica:** cpu = 0.007001 (sec), leaf count = 47

$$\left\{ \{y(x) \rightarrow c_1 + x\}, \{y(x) \rightarrow -\sqrt{2c_1 - x^2}\}, \{y(x) \rightarrow \sqrt{2c_1 - x^2}\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 33

$$\left\{ y(x) = \sqrt{-x^2 + \_C1}, y(x) = -\sqrt{-x^2 + \_C1}, y(x) = x + \_C1 \right\}$$

**2.472 ODE No. 472**

$$(y(x) + x) \left( \frac{d}{dx} y(x) \right)^2 + 2x \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.186024 (sec), leaf count = 127

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{3} \left( -2\sqrt{e^{2c_1} - 3e^{c_1} x} - e^{c_1} \right) \right\}, \left\{ y(x) \rightarrow \frac{1}{3} \left( 2\sqrt{e^{2c_1} - 3e^{c_1} x} - e^{c_1} \right) \right\}, \left\{ y(x) \rightarrow e^{c_1} - 2\sqrt{e^{c_1} x} + \right. \right.$$

**Maple:** cpu = 0.936 (sec), leaf count = 119

$$\left\{ \ln(x) - \text{Artanh} \left( \frac{y(x) + 2x}{2x} \frac{1}{\sqrt{\frac{(y(x))^2 + xy(x) + x^2}{x^2}}} \right) + \ln \left( \frac{y(x)}{x} \right) - \_C1 = 0, \ln(x) + \text{Artanh} \left( \frac{y(x) + 2x}{2x} \right. \right.$$

**2.473 ODE No. 473**

$$(y(x) - 2x) \left( \frac{d}{dx} y(x) \right)^2 - 2(x-1) \frac{d}{dx} y(x) + y(x) - 2 = 0$$

**Mathematica:** cpu = 0.407052 (sec), leaf count = 165

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( -\sqrt{-4e^{c_1}x + 4e^{c_1} - e^{2c_1}} - e^{c_1} + 4 \right) \right\}, \left\{ y(x) \rightarrow \frac{1}{2} \left( \sqrt{-4e^{c_1}x + 4e^{c_1} - e^{2c_1}} - e^{c_1} + 4 \right) \right\}, \left\{ \right\} \right\}$$

**Maple:** cpu = 0.936 (sec), leaf count = 78

$$\left\{ y(x) = 2 + \_C1 - \sqrt{-\_C1^2 + 2\_C1(x-1)}, y(x) = 2 + \frac{C1}{2} - \frac{1}{2} \sqrt{-\_C1^2 + 4\_C1(x-1)}, y(x) \right\}$$

**2.474 ODE No. 474**

$$2y(x) \left( \frac{d}{dx} y(x) \right)^2 - (4x-5) \frac{d}{dx} y(x) + 2y(x) = 0$$

**Mathematica:** cpu = 0.232029 (sec), leaf count = 135

$$\left\{ \left\{ y(x) \rightarrow -i\sqrt{2}e^{\frac{c_1}{2}} \sqrt{8e^{c_1} + 4x - 5} \right\}, \left\{ y(x) \rightarrow i\sqrt{2}e^{\frac{c_1}{2}} \sqrt{8e^{c_1} + 4x - 5} \right\}, \left\{ y(x) \rightarrow -\frac{1}{4}ie^{\frac{c_1}{2}} \sqrt{e^{c_1} + 8x - 1} \right\}, \left\{ \right\} \right\}$$

**Maple:** cpu = 1.295 (sec), leaf count = 154

$$\left\{ \ln \left( x - \frac{5}{4} \right) + \frac{1}{2} \ln \left( 16 \frac{(y(x))^2}{(4x-5)^2} - 1 \right) - \sqrt{-16 \frac{(y(x))^2}{(4x-5)^2} + 1} + \text{Artanh} \left( \frac{1}{\sqrt{-16 \frac{(y(x))^2}{(4x-5)^2} + 1}} \right) + \frac{\sqrt{4}}{2} \right\}$$

**2.475 ODE No. 475**

$$4y(x) \left( \frac{d}{dx} y(x) \right)^2 + 2x \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.097512 (sec), leaf count = 205

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{2}e^{2c_1} \sqrt{e^{4c_1} - 2x} \right\}, \left\{ y(x) \rightarrow \frac{1}{2}e^{2c_1} \sqrt{e^{4c_1} - 2x} \right\}, \left\{ y(x) \rightarrow -\frac{1}{2}(\sinh(2c_1) + \cosh(2c_1)) \sqrt{\sin} \right\}, \left\{ \right\} \right\}$$

**Maple:** cpu = 0.936 (sec), leaf count = 69

$$\left\{ y(x) = \sqrt{-C1^2 - C1x}, y(x) = \sqrt{-C1^2 + C1x}, y(x) = -\frac{i}{2}x, y(x) = \frac{i}{2}x, y(x) = -\sqrt{-C1^2 - C1x} \right\}$$

**2.476 ODE No. 476**

$$9y(x) \left( \frac{d}{dx}y(x) \right)^2 + 4x^3 \frac{d}{dx}y(x) - 4x^2y(x) = 0$$

**Mathematica:** cpu = 0.843107 (sec), leaf count = 454

$$\left\{ \text{Solve} \left[ \frac{\sqrt{x^6 + 9x^2y(x)^2} \log \left( \sqrt{x^4 + 9y(x)^2} + x^2 \right) - x\sqrt{x^4 + 9y(x)^2} \log(y(x)^2) + x\sqrt{x^4 + 9y(x)^2} \log}{2x\sqrt{x^4 + 9y(x)^2}} \right] \right.$$

**Maple:** cpu = 0.874 (sec), leaf count = 87

$$\left\{ y(x) = -\frac{i}{3}x^2, y(x) = \frac{i}{3}x^2, y(x) = -\frac{1}{6}\sqrt{-4x^2\_C1 + \_C1^2}, y(x) = \frac{1}{6}\sqrt{-4x^2\_C1 + \_C1^2}, y(x) = -2 \right.$$

**2.477 ODE No. 477**

$$ay(x) \left( \frac{d}{dx}y(x) \right)^2 + (2x - b) \frac{d}{dx}y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.304539 (sec), leaf count = 146

$$\left\{ \left\{ y(x) \rightarrow -\frac{e^{\frac{c_1}{2}} \sqrt{2b + e^{c_1} - 4x}}{2\sqrt{a}} \right\}, \left\{ y(x) \rightarrow \frac{e^{\frac{c_1}{2}} \sqrt{2b + e^{c_1} - 4x}}{2\sqrt{a}} \right\}, \left\{ y(x) \rightarrow -\sqrt{2}e^{\frac{c_1}{2}} \sqrt{2ae^{c_1} - b + 2x} \right\}, \right.$$

**Maple:** cpu = 0.858 (sec), leaf count = 929

$$\left\{ \int_{-b}^x 2 \frac{-2\_a + b + \sqrt{4a(y(x))^2 + 4\_a^2 - 4\_ab + b^2}}{4a(y(x))^2 + \sqrt{4a(y(x))^2 + 4\_a^2 - 4\_ab + b^2}b - 2\sqrt{4a(y(x))^2 + 4\_a^2 - 4\_ab + b^2}\_a + b^2} \right.$$

**2.478 ODE No. 478**

$$(ay(x) + b) \left( \left( \frac{d}{dx}y(x) \right)^2 + 1 \right) - c = 0$$

**Mathematica:** cpu = 0.166521 (sec), leaf count = 141

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \frac{c \tan^{-1} \left( \frac{\sqrt{\#1a+b}}{\sqrt{-\#1a-b+c}} \right) - \sqrt{\#1a+b} \sqrt{-\#1a-b+c}}{a} \& \right] [c_1 - x] \right\}, \left\{ y(x) \rightarrow \right.$$

Maple: cpu = 0.609 (sec), leaf count = 88

$$\left\{ x - \int^{y(x)} \frac{1}{\sqrt{-(aa+b)(aa+b-c)}} da - C1 = 0, x - \int^{y(x)} \frac{-(aa+b)}{\sqrt{-(aa+b)(aa+b-c)}} da - C1 = 0 \right.$$

### 2.479 ODE No. 479

$$(b2 y(x) + a2 x + c2) \left( \frac{d}{dx} y(x) \right)^2 + (a1 x + b1 y(x) + c1) \frac{d}{dx} y(x) + a0 x + b0 y(x) + c0 = 0$$

Mathematica: cpu = 0 (sec), leaf count = 0

Hanged

Maple: cpu = 0.811 (sec), leaf count = 929

$$\left\{ x - e^{\int \frac{1}{2 b2 y(x) + 2 a2 x + 2 c2} (-a1 x - b1 y(x) - c1 + \sqrt{-4 a0 a2 x^2 - 4 a0 b2 xy(x) + a1^2 x^2 + 2 a1 b1 xy(x) - 4 a2 b0 xy(x) - 4 b0 b2 (y(x))^2 + b1^2 (y(x))^2 - 4 a0 c2 x - 4 c2^2}) dx} = 0 \right.$$

### 2.480 ODE No. 480

$$(ay(x) - x^2) \left( \frac{d}{dx} y(x) \right)^2 + 2xy(x) \left( \frac{d}{dx} y(x) \right) - (y(x))^2 = 0$$

Mathematica: cpu = 30.550379 (sec), leaf count = 41

$$\text{DSolve}[(ay(x) - x^2) y'(x)^2 + 2xy(x)y'(x) - y(x)^2 = 0, y(x), x]$$

Maple: cpu = 2.044 (sec), leaf count = 0

could not solve

### 2.481 ODE No. 481

$$xy(x) \left( \frac{d}{dx} y(x) \right)^2 + ((y(x))^2 + x^2) \frac{d}{dx} y(x) + xy(x) = 0$$

Mathematica: cpu = 0.008501 (sec), leaf count = 49

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{x} \right\}, \left\{ y(x) \rightarrow -\sqrt{2c_1 - x^2} \right\}, \left\{ y(x) \rightarrow \sqrt{2c_1 - x^2} \right\} \right\}$$

Maple: cpu = 0.016 (sec), leaf count = 35

$$\left\{ y(x) = \sqrt{-x^2 + C1}, y(x) = \frac{-C1}{x}, y(x) = -\sqrt{-x^2 + C1} \right\}$$



**2.482 ODE No. 482**

$$xy(x) \left( \frac{d}{dx} y(x) \right)^2 + (x^{22} - (y(x))^2 + a) \frac{d}{dx} y(x) - xy(x) = 0$$

**Mathematica:** cpu = 65.128270 (sec), leaf count = 38

$$\text{DSolve}[(a + x^{22} - y(x)^2) y'(x) + xy(x)y'(x)^2 - xy(x) = 0, y(x), x]$$

**Maple:** cpu = 1.264 (sec), leaf count = 0

could not solve

**2.483 ODE No. 483**

$$(2xy(x) - x^2) \left( \frac{d}{dx} y(x) \right)^2 + 2xy(x) \frac{d}{dx} y(x) + 2xy(x) - (y(x))^2 = 0$$

**Mathematica:** cpu = 0.157020 (sec), leaf count = 71

$$\left\{ \left\{ y(x) \rightarrow e^{\frac{c_1}{2}} - \sqrt{2e^{\frac{c_1}{2}} x - x^2} \right\}, \left\{ y(x) \rightarrow \sqrt{2e^{\frac{c_1}{2}} x - x^2} + e^{\frac{c_1}{2}} \right\} \right\}$$

**Maple:** cpu = 0.624 (sec), leaf count = 109

$$\left\{ y(x) = 0, y(x) = \text{RootOf} \left( -2 \ln(x) + \int^{-Z} \frac{1}{-a(-a^2 + 1)} \left( -2 - a^2 + \sqrt{2 - a^3 - 4 - a^2 + 2 - a} \right) d_a + 2 \right) \right\}$$

**2.484 ODE No. 484**

$$(2xy(x) - x^2) \left( \frac{d}{dx} y(x) \right)^2 - 6xy(x) \frac{d}{dx} y(x) - (y(x))^2 + 2xy(x) = 0$$

**Mathematica:** cpu = 0.170522 (sec), leaf count = 81

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{3x^2 - 2e^{\frac{c_1}{2}} x - e^{\frac{c_1}{2}}} + 2x \right\}, \left\{ y(x) \rightarrow \sqrt{3x^2 - 2e^{\frac{c_1}{2}} x - e^{\frac{c_1}{2}}} + 2x \right\} \right\}$$

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

**2.485 ODE No. 485**

$$axy(x) \left( \frac{d}{dx} y(x) \right)^2 - (a(y(x))^2 + bx^2 + c) \frac{d}{dx} y(x) + bxy(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

**2.486 ODE No. 486**

$$(y(x))^2 \left( \frac{d}{dx} y(x) \right)^2 + (y(x))^2 - a^2 = 0$$

**Mathematica:** cpu = 0.023503 (sec), leaf count = 117

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{a^2 - 2c_1x - c_1^2 - x^2} \right\}, \left\{ y(x) \rightarrow \sqrt{a^2 - 2c_1x - c_1^2 - x^2} \right\}, \left\{ y(x) \rightarrow -\sqrt{a^2 + 2c_1x - c_1^2 - x^2} \right\}, \left\{ y(x) \rightarrow \sqrt{a^2 + 2c_1x - c_1^2 - x^2} \right\} \right\}$$

**Maple:** cpu = 0.608 (sec), leaf count = 59

$$\left\{ y(x) = a, y(x) = \sqrt{-_C1^2 + 2\_C1 x + a^2 - x^2}, y(x) = -a, y(x) = -\sqrt{-_C1^2 + 2\_C1 x + a^2 - x^2} \right\}$$

**2.487 ODE No. 487**

$$(y(x))^2 \left( \frac{d}{dx} y(x) \right)^2 - 6x^3 \frac{d}{dx} y(x) + 4x^2 y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.858 (sec), leaf count = 114

$$\left\{ y(x) = \left( -\frac{\sqrt[3]{18}}{4} \sqrt[3]{x} - \frac{i}{4} \sqrt{3} \sqrt[3]{18} \sqrt[3]{x} \right) x, y(x) = \left( -\frac{\sqrt[3]{18}}{4} \sqrt[3]{x} + \frac{i}{4} \sqrt{3} \sqrt[3]{18} \sqrt[3]{x} \right) x, y(x) = \text{RootOf} \left( -\ln(x) \right) \right\}$$

**2.488 ODE No. 488**

$$(y(x))^2 \left( \frac{d}{dx} y(x) \right)^2 - 4ay(x) \frac{d}{dx} y(x) + (y(x))^2 - 4ax + 4a^2 = 0$$

**Mathematica:** cpu = 0.366546 (sec), leaf count = 85

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{16a^3x - 4a^2x^2 - 4ac_1x - c_1^2}}{2a} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{16a^3x - 4a^2x^2 - 4ac_1x - c_1^2}}{2a} \right\} \right\}$$

**Maple:** cpu = 0.905 (sec), leaf count = 113

$$\left\{ y(x) = -2\sqrt{ax}, y(x) = 2\sqrt{ax}, y(x) = -\frac{1}{4a} \sqrt{-16a^4 + 32a^3x - 16a^2x^2 + 8C_1a^2 + 8C_1ax - C_1^2} \right\}$$

**2.489 ODE No. 489**

$$(y(x))^2 \left( \frac{d}{dx} y(x) \right)^2 + 2xy(x) \frac{d}{dx} y(x) + a(y(x))^2 + bx + c = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 2.621 (sec), leaf count = 5525

**2.490 ODE No. 490**

$$(y(x))^2 \left( \frac{d}{dx} y(x) \right)^2 - 2xy(x) \frac{d}{dx} y(x) + 2(y(x))^2 - x^2 + a = 0$$

**Mathematica:** cpu = 0.601076 (sec), leaf count = 70

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{-a + 8c_1x - 4c_1^2 - 2x^2}}{\sqrt{2}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{-a + 8c_1x - 4c_1^2 - 2x^2}}{\sqrt{2}} \right\} \right\}$$

**Maple:** cpu = 0.920 (sec), leaf count = 145

$$\left\{ y(x) = \sqrt{-2\sqrt{a + 2C_1x - C_1} - x^2 - a}, y(x) = \sqrt{2\sqrt{a + 2C_1x - C_1} - x^2 - a}, y(x) = -\sqrt{-2\sqrt{a + 2C_1x - C_1} - x^2 - a} \right\}$$

**2.491 ODE No. 491**

$$\left( (y(x))^2 \left( \frac{d}{dx} y(x) \right)^2 + 2axy(x) \frac{d}{dx} y(x) + (1-a)(y(x))^2 + ax^2 + (a-1)b = 0 \right)$$

**Mathematica:** cpu = 1.033131 (sec), leaf count = 79

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{-2ac_1x + ac_1^2 + b + 2c_1x - c_1^2 - x^2} \right\}, \left\{ y(x) \rightarrow \sqrt{-2ac_1x + ac_1^2 + b + 2c_1x - c_1^2 - x^2} \right\} \right\}$$

**Maple:** cpu = 1.107 (sec), leaf count = 251

$$\left\{ y(x) = \sqrt{-ax^2 + b}, y(x) = \frac{1}{a} \sqrt{-a^2x^2 - 2a\sqrt{-C1a^2 - a^2b - C1a + abx} + C1a + a^2b - ab}, y(x) = \dots \right\}$$

**2.492 ODE No. 492**

$$\left( (y(x))^2 - a^2 \right) \left( \frac{d}{dx} y(x) \right)^2 + (y(x))^2 = 0$$

**Mathematica:** cpu = 0.282536 (sec), leaf count = 111

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \sqrt{a^2 - \#1^2} - a \log \left( a \sqrt{a^2 - \#1^2} + a^2 \right) + a \log(\#1) \right] [c_1 - x] \right\}, \left\{ y(x) \rightarrow \dots \right\} \right\}$$

**Maple:** cpu = 0.905 (sec), leaf count = 122

$$\left\{ x - \sqrt{a^2 - (y(x))^2} + a^2 \ln \left( \frac{1}{y(x)} \left( 2a^2 + 2\sqrt{a^2} \sqrt{a^2 - (y(x))^2} \right) \right) \frac{1}{\sqrt{a^2}} - C1 = 0, x + \sqrt{a^2 - (y(x))^2} \right\}$$

**2.493 ODE No. 493**

$$\left( (y(x))^2 - 2ax + a^2 \right) \left( \frac{d}{dx} y(x) \right)^2 + 2ay(x) \frac{d}{dx} y(x) + (y(x))^2 = 0$$

**Mathematica:** cpu = 8.600592 (sec), leaf count = 553

$$\left\{ \text{Solve} \left[ \left\{ y(x) = \frac{-\sqrt{-aK\$1287907^2 (aK\$1287907^2 - 2K\$1287907^2x - 2x)} - aK\$1287907}{K\$1287907^2 + 1}, x = \frac{ac_1^2K\$1287907^2}{K\$1287907^2 + 1} \right\} \right] \right\}$$

**Maple:** cpu = 1.341 (sec), leaf count = 124

$$\left\{ [x(T)] = \frac{1}{2a} \left( \left( \text{Artanh} \left( \frac{1}{\sqrt{-T^2 + 1}} \right) \right)^2 \sqrt{-T^2 + 1} a^2 - 2 \text{Artanh} \left( \frac{1}{\sqrt{-T^2 + 1}} \right) \sqrt{-T^2 + 1} C1 a \right) \right\}$$

**2.494 ODE No. 494**

$$\left( (y(x))^2 - a^2 x^2 \right) \left( \frac{d}{dx} y(x) \right)^2 + 2xy(x) \frac{d}{dx} y(x) + (-a^2 + 1)x^2 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.764 (sec), leaf count = 173

$$\left\{ y(x) = \sqrt{a^2 - 1}x, y(x) = \text{RootOf} \left( -\ln(x) + \int^{-Z} \frac{1}{-a^4 - a^2 a^2 + 2 a^2 - a^2 + 1} \left( -a^3 + a a^2 + \sqrt{-a} \right) \right) \right.$$

**2.495 ODE No. 495**

$$\left( (y(x))^2 + (1 - a)x^2 \right) \left( \frac{d}{dx} y(x) \right)^2 + 2axy(x) \frac{d}{dx} y(x) + (1 - a)(y(x))^2 + x^2 = 0$$

**Mathematica:** cpu = 0.110014 (sec), leaf count = 83

$$\left\{ \text{Solve} \left[ \sqrt{a - 1} \tan^{-1} \left( \frac{y(x)}{x} \right) - \frac{1}{2} \log \left( \frac{y(x)^2}{x^2} + 1 \right) = c_1 + \log(x), y(x) \right], \text{Solve} \left[ \sqrt{a - 1} \tan^{-1} \left( \frac{y(x)}{x} \right) + \right. \right.$$

**Maple:** cpu = 0.905 (sec), leaf count = 61

$$\left\{ y(x) = \tan \left( \text{RootOf} \left( -2 \sqrt{a - 1} - \ln \left( \frac{x^2}{(\cos(-Z))^2} \right) + 2 C1 \right) \right) x, y(x) = \tan \left( \text{RootOf} \left( 2 \sqrt{a - 1} \right) \right) x \right.$$

**2.496 ODE No. 496**

$$(y(x) - x)^2 \left( \left( \frac{d}{dx} y(x) \right)^2 + 1 \right) - a^2 \left( \frac{d}{dx} y(x) + 1 \right)^2 = 0$$

**Mathematica:** cpu = 95.092075 (sec), leaf count = 65

$$\left\{ \left\{ y(x) \rightarrow c_1 - \sqrt{a^2 + 2c_1x - c_1^2 - x^2} \right\}, \left\{ y(x) \rightarrow \sqrt{a^2 + 2c_1x - c_1^2 - x^2} + c_1 \right\} \right\}$$

**Maple:** cpu = 0.718 (sec), leaf count = 130

$$\left\{ y(x) = x - \sqrt{2}a, y(x) = x + \sqrt{2}a, y(x) = x + \text{RootOf} \left( -x + \int^{-Z} -\frac{1}{2 a^2 - 4 a^2} \left( -a^2 - 2 a^2 + \sqrt{-a} \right) \right) \right.$$

**2.497 ODE No. 497**

$$3(y(x))^2 \left(\frac{d}{dx}y(x)\right)^2 - 2xy(x) \frac{d}{dx}y(x) + 4(y(x))^2 - x^2 = 0$$

**Mathematica:** cpu = 0.174022 (sec), leaf count = 203

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{-4ix \sinh(3c_1) - 4ix \cosh(3c_1) + \sinh(6c_1) + \cosh(6c_1) - 3x^2}}{\sqrt{3}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{-4ix \sinh(3c_1) - 4ix \cosh(3c_1) + \sinh(6c_1) + \cosh(6c_1) - 3x^2}}{\sqrt{3}} \right\} \right.$$

**Maple:** cpu = 0.889 (sec), leaf count = 203

$$\left\{ \ln(x) - \frac{\sqrt{3}}{6} \sqrt{\frac{(\sqrt{3}x - 3y(x))(\sqrt{3}x + 3y(x))}{x^2}} + \frac{1}{2} \sqrt{\frac{x^2 - 3(y(x))^2}{x^2}} - \text{Arctanh}\left(\frac{1}{2} \sqrt{\frac{x^2 - 3(y(x))^2}{x^2}}\right) \right.$$

**2.498 ODE No. 498**

$$(3y(x) - 2) \left(\frac{d}{dx}y(x)\right)^2 - 4 + 4y(x) = 0$$

**Mathematica:** cpu = 0.103513 (sec), leaf count = 107

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction}\left[-\sqrt{1 - \#1} \sqrt{3\#1 - 2} - \frac{\sin^{-1}(\sqrt{3 - 3\#1})}{\sqrt{3}}\right] \& [c_1 - 2x] \right\}, \left\{ y(x) \rightarrow \text{InverseFunction}\left[\sqrt{1 - \#1} \sqrt{3\#1 - 2} - \frac{\sin^{-1}(\sqrt{3 - 3\#1})}{\sqrt{3}}\right] \& [c_1 - 2x] \right\} \right.$$

**Maple:** cpu = 0.749 (sec), leaf count = 99

$$\left\{ y(x) = 1, y(x) = \frac{\sin(\text{RootOf}(-8\sqrt{3}_C1_Z + 8\sqrt{3}x_Z - (\cos(_Z))^2 + 48_C1^2 - 96_C1x + 48x^2))}{6} \right.$$

**2.499 ODE No. 499**

$$(-a^2 + 1)(y(x))^2 \left(\frac{d}{dx}y(x)\right)^2 - 2a^2xy(x) \frac{d}{dx}y(x) + (y(x))^2 - a^2x^2 = 0$$

**Mathematica:** cpu = 0.333542 (sec), leaf count = 212

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{a^6(-x^2) + 3a^4x^2 + 2a^2xe^{a^2c_1 - c_1} - 2xe^{a^2c_1 - c_1} + e^{2a^2c_1 - 2c_1} - 3a^2x^2 + x^2}}{\sqrt{a^6 - 3a^4 + 3a^2 - 1}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{a^6(-x^2) + 3a^4x^2 + 2a^2xe^{a^2c_1 - c_1} - 2xe^{a^2c_1 - c_1} + e^{2a^2c_1 - 2c_1} - 3a^2x^2 + x^2}}{\sqrt{a^6 - 3a^4 + 3a^2 - 1}} \right\} \right.$$

**Maple:** cpu = 0.702 (sec), leaf count = 201

$$\left\{ y(x) = \text{RootOf}\left(-\ln(x) + \int^{-Z} \frac{-a}{a^2_a^4 - _a^4 + 2_a^2a^2 - _a^2 + a^2} \left(-_a^2a^2 + _a^2 - a^2 + \sqrt{-a^2a^2 - 2a^2a^2 + a^4}\right) dz\right) \right.$$

## 2.500 ODE No. 500

$$(a - b)(y(x))^2 \left( \frac{d}{dx} y(x) \right)^2 - 2bxy(x) \frac{d}{dx} y(x) + a(y(x))^2 - bx^2 - ab = 0$$

**Mathematica:** cpu = 1.322668 (sec), leaf count = 100

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{-ab - 2ac_1x + ac_1^2 + ax^2 + b^2 - bx^2}}{\sqrt{b - a}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{-ab - 2ac_1x + ac_1^2 + ax^2 + b^2 - bx^2}}{\sqrt{b - a}} \right\} \right.$$

**Maple:** cpu = 1.232 (sec), leaf count = 260

$$\left\{ y(x) = \frac{1}{b} \sqrt{-C1 ab + C1 b^2 - b^2 x^2 - 2b \sqrt{-C1 ab - ab^2 x + ab^2}}, y(x) = \frac{1}{b} \sqrt{-C1 ab + C1 b^2 - b^2 x^2 - 2b \sqrt{-C1 ab - ab^2 x + ab^2}} \right.$$

## 2.501 ODE No. 501

$$(a(y(x))^2 + bx + c) \left( \frac{d}{dx} y(x) \right)^2 - by(x) \frac{d}{dx} y(x) + d(y(x))^2 = 0$$

**Mathematica:** cpu = 33.600767 (sec), leaf count = 913

$$\left\{ \text{Solve} \left[ \left\{ y(x) = \frac{b \sqrt{-K\$1419264 - \sqrt{-K\$1419264^2 (-b^2 + 4aK\$1419264^2 xb + 4dxb + 4acK\$1419264^2 + 4d)}}{2(aK\$1419264^2 + d)} \right\} \right] \right.$$

**Maple:** cpu = 4.259 (sec), leaf count = 287

$$\left\{ [x(_T) = -\frac{1}{4bd} \left( (\ln(2))^2 \sqrt{-T^2 a + db^2} + 2 \ln(2) \ln \left( \frac{\sqrt{d} \sqrt{-T^2 a + d} + d}{-T} \right) \sqrt{-T^2 a + db^2} + 4 \ln(2) \right) \right.$$

## 2.502 ODE No. 502

$$(ay(x) - bx)^2 \left( a^2 \left( \frac{d}{dx} y(x) \right)^2 + b^2 \right) - c^2 \left( a \frac{d}{dx} y(x) + b \right)^2 = 0$$

**Mathematica:** cpu = 1.717718 (sec), leaf count = 100

$$\left\{ \left\{ y(x) \rightarrow \frac{bc_1}{a} - \frac{\sqrt{2b^2c_1x - b^2c_1^2 + b^2(-x^2) + c^2}}{a} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{2b^2c_1x - b^2c_1^2 + b^2(-x^2) + c^2}}{a} + \frac{bc_1}{a} \right\} \right.$$

**Maple:** cpu = 0.890 (sec), leaf count = 195

$$\left\{ y(x) = \frac{bx - \sqrt{2}c}{a}, y(x) = \frac{bx + \sqrt{2}c}{a}, y(x) = \frac{1}{a} \left( \text{RootOf} \left( -x + \int^{-z} \frac{a}{(2a^2a^2 - 4c^2)b} (-a^2a^2 + 2c^2 - \dots) \right) \right.$$

**2.503 ODE No. 503**

$$(b_2 y(x) + a_2 x + c_2)^2 \left( \frac{d}{dx} y(x) \right)^2 + (a_1 x + b_1 y(x) + c_1) \frac{d}{dx} y(x) + b_0 y(x) + a_0 + c_0 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 33.103 (sec), leaf count = 0

could not solve

**2.504 ODE No. 504**

$$x(y(x))^2 \left( \frac{d}{dx} y(x) \right)^2 - ((y(x))^3 + x^3 - a) \frac{d}{dx} y(x) + x^2 y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 1.201 (sec), leaf count = 303

$$\left\{ \int_{-b}^{y(x)} -a^2 \frac{1}{\sqrt{-a^6 + (-2x^3 - 2a)_a^3 + (-x^3 + a)^2}} dx - \frac{\ln(x)}{2} - C1 = 0, \int_{-b}^{y(x)} -a^2 \frac{1}{\sqrt{-a^6 + (-2x^3 - 2a)_a^3 + (-x^3 + a)^2}} dx - \frac{\ln(x)}{2} - C1 = 0 \right\}$$

**2.505 ODE No. 505**

$$x(y(x))^2 \left( \frac{d}{dx} y(x) \right)^2 - 2(y(x))^3 \frac{d}{dx} y(x) + 2x(y(x))^2 - x^3 = 0$$

**Mathematica:** cpu = 0.013002 (sec), leaf count = 73

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{2c_1 + x^2} \right\}, \left\{ y(x) \rightarrow \sqrt{2c_1 + x^2} \right\}, \left\{ y(x) \rightarrow -\sqrt{c_1 x^4 + x^2} \right\}, \left\{ y(x) \rightarrow \sqrt{c_1 x^4 + x^2} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 52

$$\left\{ y(x) = \sqrt{x^2 + C1}, y(x) = \sqrt{x^2 - C1 + 1x}, y(x) = -\sqrt{x^2 + C1}, y(x) = -\sqrt{x^2 - C1 + 1x} \right\}$$



**2.506 ODE No. 506**

$$x^2(x(y(x))^2 - 1) \left(\frac{d}{dx}y(x)\right)^2 + 2x^2(y(x))^2(y(x) - x) \frac{d}{dx}y(x) - (y(x))^2(x^2y(x) - 1) = 0$$

**Mathematica:** cpu = 47.848076 (sec), leaf count = 58

DSolve[ $2x^2(y(x) - x)y(x)^2y'(x) + x^2(xy(x)^2 - 1)y'(x)^2 - (x^2y(x) - 1)y(x)^2 = 0, y(x), x]$

**Maple:** cpu = 1.310 (sec), leaf count = 0

could not solve

**2.507 ODE No. 507**

$$((y(x))^4 - a^2x^2) \left(\frac{d}{dx}y(x)\right)^2 + 2a^2xy(x) \frac{d}{dx}y(x) + (y(x))^2((y(x))^2 - a^2) = 0$$

**Mathematica:** cpu = 29.710773 (sec), leaf count = 443

$$\left\{ \text{Solve} \left[ \left[ x = \frac{a^2\sqrt{1432838}y(\sqrt{1432838}) - \sqrt{a^2\sqrt{1432838}^2 (\sqrt{1432838}^2 + 1) y(\sqrt{1432838})^4}}{a^2\sqrt{1432838}^2}, y(x) = \right. \right. \right.$$

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

**2.508 ODE No. 508**

$$((y(x))^4 + x^2(y(x))^2 - x^2) \left(\frac{d}{dx}y(x)\right)^2 + 2xy(x) \frac{d}{dx}y(x) - (y(x))^2 = 0$$

**Mathematica:** cpu = 55.171506 (sec), leaf count = 47

DSolve[ $(x^2y(x)^2 - x^2 + y(x)^4)y'(x)^2 + 2xy(x)y'(x) - y(x)^2 = 0, y(x), x]$

**Maple:** cpu = 2.122 (sec), leaf count = 60

$$\{y(x) = -ix, y(x) = ix, y(x) = -\text{Artanh}(\text{RootOf}((\text{Artanh}(\_Z))^2 \_Z^2 - 2 \text{Artanh}(\_Z) \_C1 \_Z^2 + \_C2))\}$$

**2.509 ODE No. 509**

$$9(y(x))^4(x^2 - 1)\left(\frac{d}{dx}y(x)\right)^2 - 6x(y(x))^5\frac{d}{dx}y(x) - 4x^2 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 1.622 (sec), leaf count = 245

$$\left\{ y(x) = \sqrt[6]{-4x^2 + 4}, y(x) = \left(-\frac{1}{2} - \frac{i}{2}\sqrt{3}\right)\sqrt[6]{-4x^2 + 4}, y(x) = \left(-\frac{1}{2} + \frac{i}{2}\sqrt{3}\right)\sqrt[6]{-4x^2 + 4}, y(x) = \left(\frac{1}{2}\right)\sqrt[6]{-4x^2 + 4} \right.$$

**2.510 ODE No. 510**

$$x^2(x^2(y(x))^4 - 1)\left(\frac{d}{dx}y(x)\right)^2 + 2x^3(y(x))^3((y(x))^2 - x^2)\frac{d}{dx}y(x) - (y(x))^2(x^4(y(x))^2 - 1) = 0$$

**Mathematica:** cpu = 60.566191 (sec), leaf count = 66

$$\text{DSolve}\left[-(x^4y(x)^2 - 1)y(x)^2 + x^2(x^2y(x)^4 - 1)y'(x)^2 + 2x^3(y(x)^2 - x^2)y(x)^3y'(x) = 0, y(x), x\right]$$

**Maple:** cpu = 2.730 (sec), leaf count = 0

could not solve

**2.511 ODE No. 511**

$$\left(a^2\sqrt{(y(x))^2 + x^2 - x^2}\right)\left(\frac{d}{dx}y(x)\right)^2 + 2xy(x)\frac{d}{dx}y(x) + a^2\sqrt{(y(x))^2 + x^2} - (y(x))^2 = 0$$

**Mathematica:** cpu = 1.555697 (sec), leaf count = 229

$$\left\{ \text{Solve}\left[\tan^{-1}\left(\frac{x}{y(x)}\right) - \frac{2\sqrt{a^2(x^2 + y(x)^2)}\left(\sqrt{x^2 + y(x)^2} - a^2\right)\tan^{-1}\left(\frac{\sqrt{\sqrt{x^2 + y(x)^2} - a^2}}{a}\right)}{a\sqrt{x^2 + y(x)^2}\sqrt{\sqrt{x^2 + y(x)^2} - a^2}} = c_1, y(x)\right], S \right.$$

Maple: cpu = 8.112 (sec), leaf count = 199

$$\left\{ \arctan\left(\frac{x}{y(x)}\right) - 2 \frac{\sqrt{a^2((y(x))^2 + x^2)} \left(-a^2 + \sqrt{(y(x))^2 + x^2}\right)}{a\sqrt{(y(x))^2 + x^2} \sqrt{-a^2 + \sqrt{(y(x))^2 + x^2}}} \arctan\left(\frac{\sqrt{-a^2 + \sqrt{(y(x))^2 + x^2}}}{a}\right) \right\}$$

## 2.512 ODE No. 512

$$\left( a((y(x))^2 + x^2)^{3/2} - x^2 \right) \left( \frac{d}{dx} y(x) \right)^2 + 2xy(x) \frac{d}{dx} y(x) + a((y(x))^2 + x^2)^{3/2} - (y(x))^2 = 0$$

Mathematica: cpu = 4.686095 (sec), leaf count = 725

$$\left\{ \text{Solve} \left[ \tan^{-1}\left(\frac{x}{y(x)}\right) - \frac{i\sqrt{a}(x^2 + y(x)^2) \sqrt{\sqrt{x^2 + y(x)^2} - a(x^2 + y(x)^2)}}{\sqrt{2} \left( \log\left(\frac{a^{3/2}(3i\sqrt{2}a\sqrt{x^2 + y(x)})}{\dots}\right) \right)} \right] \right\}$$

Maple: cpu = 40.935 (sec), leaf count = 135

$$\left\{ y(x) = x \left( \tan \left( \text{RootOf} \left( -Z + \int \frac{x^2((\tan(Z))^2 + 1)}{(\tan(Z))^2} \right) - \frac{1}{2a^2(a^2 - 1)} (\sqrt{-aa} + 1) \sqrt{-a^{\frac{5}{2}}a(\sqrt{-aa} - \dots)} \right) \right) \right\}$$

## 2.513 ODE No. 513

$$\left( \frac{d}{dx} y(x) \right)^2 \sin(y(x)) + 2x \left( \frac{d}{dx} y(x) \right) (\cos(y(x)))^3 - \sin(y(x)) (\cos(y(x)))^4 = 0$$

Mathematica: cpu = 0 (sec), leaf count = 0

Hanged

Maple: cpu = 1.748 (sec), leaf count = 2402

$$\left\{ [x(T)] = -\frac{1}{8T} \left( 16T^2 \sin \left( 1/2 \arctan \left( \frac{-C1^2 T^2 - 2T C1 \sqrt[3]{-C1^3 T^3 + 54T C1 + 6}}{\sqrt[3]{-C1}} \right) \right) \right) \right\}$$

**2.514 ODE No. 514**

$$\left( \frac{d}{dx} y(x) \right)^2 (a \cos(y(x)) + b) - c \cos(y(x)) + d = 0$$

**Mathematica:** cpu = 15.435460 (sec), leaf count = 605

$$\left\{ \left\{ \begin{array}{l} y(x) \rightarrow \text{InverseFunction} \left[ \frac{4 \sin^2\left(\frac{\#1}{2}\right) \csc(\#1) \sqrt{a \cos(\#1) + b} \sqrt{\frac{\cot^2\left(\frac{\#1}{2}\right)(c-d)}{c+d}} \sqrt{\frac{\csc^2\left(\frac{\#1}{2}\right)(a+b)(d-c \cos(\#1))}{ad+bc}} \right] \end{array} \right. \right.$$

**Maple:** cpu = 0.140 (sec), leaf count = 87

$$\left\{ x - \int^{y(x)} (a \cos(\_a) + b) \frac{1}{\sqrt{(a \cos(\_a) + b)(c \cos(\_a) - d)}} d\_a - \_C1 = 0, x - \int^{y(x)} -(a \cos(\_a) +$$

**2.515 ODE No. 515**

$$f((y(x))^2 + x^2) \left( \left( \frac{d}{dx} y(x) \right)^2 + 1 \right) - \left( x \frac{d}{dx} y(x) - y(x) \right)^2 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 1.888 (sec), leaf count = 113

$$\left\{ y(x) = x \left( \tan \left( \text{RootOf} \left( -\_Z + \int \frac{x^2 ((\tan(\_Z))^2 + 1)}{(\tan(\_Z))^2} - \frac{1}{2\_a (f(\_a) - \_a)} \sqrt{-(f(\_a) - \_a) f(\_a) d\_a} \right) \right) \right)$$

**2.516 ODE No. 516**

$$\left( (y(x))^2 + x^2 \right) f\left(\frac{x}{\sqrt{(y(x))^2 + x^2}}\right) \left( \left(\frac{d}{dx}y(x)\right)^2 + 1 \right) - \left( x \frac{d}{dx}y(x) - y(x) \right)^2 = 0$$

**Mathematica:** cpu = 2.612332 (sec), leaf count = 251

$$\left\{ \text{Solve} \left[ \int_1^{\frac{y(x)}{x}} \frac{K[1]^2 f\left(\frac{1}{\sqrt{K[1]^2+1}}\right) + f\left(\frac{1}{\sqrt{K[1]^2+1}}\right) - 1}{(K[1] - i)(K[1] + i) \sqrt{f\left(\frac{1}{\sqrt{K[1]^2+1}}\right) \left( K[1] \sqrt{f\left(\frac{1}{\sqrt{K[1]^2+1}}\right) + i \sqrt{f\left(\frac{1}{\sqrt{K[1]^2+1}}\right) - 1} \right)}} dK[1] \right. \right.$$

**Maple:** cpu = 0.827 (sec), leaf count = 141

$$\left\{ y(x) = \text{RootOf} \left( -\ln(x) + \int^{-Z} -\frac{1}{-a^2+1} \left( -a f\left(\frac{1}{\sqrt{-a^2+1}}\right) - \sqrt{-\left(f\left(\frac{1}{\sqrt{-a^2+1}}\right)\right)^2 + f\left(\frac{1}{\sqrt{-a^2+1}}\right)} \right) \right. \right.$$

**2.517 ODE No. 517**

$$\left( (y(x))^2 + x^2 \right) f\left(\frac{y(x)}{\sqrt{(y(x))^2 + x^2}}\right) \left( \left(\frac{d}{dx}y(x)\right)^2 + 1 \right) - \left( x \frac{d}{dx}y(x) - y(x) \right)^2 = 0$$

**Mathematica:** cpu = 2.738848 (sec), leaf count = 281

$$\left\{ \text{Solve} \left[ \int_1^{\frac{y(x)}{x}} \frac{K[1]^2 f\left(\frac{K[1]}{\sqrt{K[1]^2+1}}\right) + f\left(\frac{K[1]}{\sqrt{K[1]^2+1}}\right) - 1}{(K[1] - i)(K[1] + i) \sqrt{f\left(\frac{K[1]}{\sqrt{K[1]^2+1}}\right) \left( K[1] \sqrt{f\left(\frac{K[1]}{\sqrt{K[1]^2+1}}\right) + i \sqrt{f\left(\frac{K[1]}{\sqrt{K[1]^2+1}}\right) - 1} \right)}} dK[1] \right. \right.$$

**Maple:** cpu = 0.812 (sec), leaf count = 78

$$\left\{ y(x) = \text{RootOf} \left( -\ln(x) + \int^{-Z} -\frac{1}{-a^2+1} \left( -a f\left(-a \frac{1}{\sqrt{-a^2+1}}\right) + \sqrt{-\left(f\left(-a \frac{1}{\sqrt{-a^2+1}}\right)\right)^2 + f\left(-a \frac{1}{\sqrt{-a^2+1}}\right)} \right) \right. \right.$$

**2.518 ODE No. 518**

$$\left( \frac{d}{dx} y(x) \right)^3 - (y(x) - a)^2 (y(x) - b)^2 = 0$$

**Mathematica:** cpu = 0.801102 (sec), leaf count = 236

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\frac{3\sqrt[3]{a - \#1} \left( \frac{\#1 - b}{a - b} \right)^{2/3} {}_2F_1 \left( \frac{1}{3}, \frac{2}{3}; \frac{4}{3}; \frac{a - \#1}{a - b} \right)}{(b - \#1)^{2/3}} \& \right] [c_1 + x] \right\}, \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \frac{3\sqrt[3]{a - \#1} \left( \frac{\#1 - b}{a - b} \right)^{2/3} {}_2F_1 \left( \frac{1}{3}, \frac{2}{3}; \frac{4}{3}; \frac{a - \#1}{a - b} \right)}{(b - \#1)^{2/3}} \& \right] [c_1 + x] \right\} \right.$$

**Maple:** cpu = 0.156 (sec), leaf count = 126

$$\left\{ x - \int^{y(x)} \frac{1}{\sqrt[3]{(a - a)^2 (-b + a)^2}} d_a - C1 = 0, x - \int^{y(x)} \frac{1}{(i\sqrt{3} - 1) \sqrt[3]{(a - a)^2 (-b + a)^2}} d_a - C2 = 0 \right.$$

**2.519 ODE No. 519**

$$\left( \frac{d}{dx} y(x) \right)^3 - f(x) (a(y(x))^2 + by(x) + c)^2 = 0$$

**Mathematica:** cpu = 1.827732 (sec), leaf count = 473

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \frac{3(2\#1a - \sqrt{b^2 - 4ac} + b) \left( \frac{2\#1a + \sqrt{b^2 - 4ac} + b}{\sqrt{b^2 - 4ac}} \right)^{2/3} {}_2F_1 \left( \frac{1}{3}, \frac{2}{3}; \frac{4}{3}; \frac{-b - 2a\#1 + \sqrt{b^2 - 4ac}}{2\sqrt{b^2 - 4ac}} \right)}{2 \cdot 2^{2/3} a (\#1(\#1a + b) + c)^{2/3}} \& \right] [c_1 + x] \right\}, \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \frac{3(2\#1a - \sqrt{b^2 - 4ac} + b) \left( \frac{2\#1a + \sqrt{b^2 - 4ac} + b}{\sqrt{b^2 - 4ac}} \right)^{2/3} {}_2F_1 \left( \frac{1}{3}, \frac{2}{3}; \frac{4}{3}; \frac{-b - 2a\#1 + \sqrt{b^2 - 4ac}}{2\sqrt{b^2 - 4ac}} \right)}{2 \cdot 2^{2/3} a (\#1(\#1a + b) + c)^{2/3}} \& \right] [c_1 + x] \right\} \right.$$

**Maple:** cpu = 0.250 (sec), leaf count = 197

$$\left\{ \int^{y(x)} (a^2 a + a b + c)^{-2/3} d_a + \int^x -1 \sqrt[3]{f(a) (a(y(x))^2 + by(x) + c)^2} (a(y(x))^2 + by(x) + c)^{-2/3} d_x - C1 = 0, \int^{y(x)} (a^2 a + a b + c)^{-2/3} d_a + \int^x -1 \sqrt[3]{f(a) (a(y(x))^2 + by(x) + c)^2} (a(y(x))^2 + by(x) + c)^{-2/3} d_x - C2 = 0 \right.$$

**2.520 ODE No. 520**

$$\left( \frac{d}{dx} y(x) \right)^3 + \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 151.472735 (sec), leaf count = 3323

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \frac{\left( 243\#1^2 - 27\sqrt{81\#1^2 + 12\#1} - 24\sqrt[3]{2}\sqrt[6]{3} \tan^{-1} \left( \frac{1}{\sqrt{3}} - \left( \frac{2}{3} \right)^{2/3} \sqrt[3]{\sqrt{81\#1^2 + 12\#1}} \right)}{\dots} \right. \right. \right.$$

**Maple:** cpu = 0.062 (sec), leaf count = 245

$$\left\{ x - \int^{y(x)} 6 \frac{\sqrt[3]{108\_a + 12\sqrt{81\_a^2 + 12}}}{(108\_a + 12\sqrt{81\_a^2 + 12})^{2/3} - 12} d\_a - \_C1 = 0, x - \int^{y(x)} 12 \frac{\dots}{(i\sqrt{3} - 1) \left( \sqrt[3]{108\_a + \dots} \right)} \dots \right.$$

**2.521 ODE No. 521**

$$\left( \frac{d}{dx} y(x) \right)^3 + x \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.003500 (sec), leaf count = 14

$$\{ \{ y(x) \rightarrow c_1 x + c_1^3 \} \}$$

**Maple:** cpu = 0.031 (sec), leaf count = 33

$$\left\{ y(x) = -\frac{2x}{9} \sqrt{-3x}, y(x) = \frac{2x}{9} \sqrt{-3x}, y(x) = \_C1^3 + \_C1 x \right\}$$

**2.522 ODE No. 522**

$$\left( \frac{d}{dx} y(x) \right)^3 - (x + 5) \frac{d}{dx} y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.003501 (sec), leaf count = 20

$$\{ \{ y(x) \rightarrow c_1 x - c_1^3 + 5c_1 \} \}$$

**Maple:** cpu = 0.047 (sec), leaf count = 46

$$\left\{ y(x) = -\frac{2x + 10}{9} \sqrt{3x + 15}, y(x) = \frac{2x + 10}{9} \sqrt{3x + 15}, y(x) = -\_C1^3 + \_C1 x + 5\_C1 \right\}$$

**2.523 ODE No. 523**

$$\left(\frac{d}{dx}y(x)\right)^3 - ax\frac{d}{dx}y(x) + x^3 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.046 (sec), leaf count = 299

$$\left\{y(x) = \int -\frac{i}{12} \left(\sqrt{3}(-108x^3 + 12\sqrt{-3x^3(4a^3 - 27x^3)})\right)^{\frac{2}{3}} - 12\sqrt{3}ax - i(-108x^3 + 12\sqrt{-3x^3(4a^3 - 27x^3)})\right\}$$

**2.524 ODE No. 524**

$$\left(\frac{d}{dx}y(x)\right)^3 - 2y(x)\frac{d}{dx}y(x) + (y(x))^2 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.047 (sec), leaf count = 295

$$\left\{x - \int^{y(x)} 6 \frac{\sqrt[3]{-108a^2 + 12\sqrt{3}\sqrt{-a^3(27a - 32)}}}{(-108a^2 + 12\sqrt{3}\sqrt{-a^3(27a - 32)})^{2/3} + 24a} da - C1 = 0, x - \int^{y(x)} 24 \frac{1}{(i\sqrt{3} - \dots)}\right\}$$

**2.525 ODE No. 525**

$$\left(\frac{d}{dx}y(x)\right)^2 - axy(x)\frac{d}{dx}y(x) + 2a(y(x))^2 = 0$$

**Mathematica:** cpu = 0.063008 (sec), leaf count = 135

$$\left\{\left\{y(x) \rightarrow c_1 \exp\left(\frac{1}{2}\left(\frac{ax^2}{2} + \frac{1}{2}\sqrt{ax}\sqrt{ax^2 - 8} - 4 \log\left(\sqrt{ax}\sqrt{ax^2 - 8} + ax\right)\right)\right)\right\}, \left\{y(x) \rightarrow c_1 \exp\left(\frac{1}{2}\left(\frac{ax^2}{2} + \frac{1}{2}\sqrt{ax}\sqrt{ax^2 - 8} - 4 \log\left(\sqrt{ax}\sqrt{ax^2 - 8} + ax\right)\right)\right)\right\}\right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 125

$$\left\{y(x) = C1 \left(a^2x\frac{1}{\sqrt{a^2}} + \sqrt{a^2x^2 - 8a}\right)^{-2\frac{a}{\sqrt{a^2}}} e^{\frac{ax^2}{4} + \frac{x}{4}\sqrt{a^2x^2 - 8a}}, y(x) = C1 \left(a^2x\frac{1}{\sqrt{a^2}} + \sqrt{a^2x^2 - 8a}\right)^2\right\}$$



**2.526 ODE No. 526**

$$\left( \frac{d}{dx} y(x) \right)^3 - ((y(x))^2 + xy(x) + x^2) \left( \frac{d}{dx} y(x) \right)^2 + (x(y(x))^3 + x^2(y(x))^2 + x^3 y(x)) \frac{d}{dx} y(x) - x^3 (y(x))$$

**Mathematica:** cpu = 0.009501 (sec), leaf count = 45

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{-c_1 - x} \right\}, \left\{ y(x) \rightarrow c_1 e^{\frac{x^2}{2}} \right\}, \left\{ y(x) \rightarrow c_1 + \frac{x^3}{3} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 32

$$\left\{ y(x) = (-x + \_C1)^{-1}, y(x) = e^{\frac{x^2}{2}} \_C1, y(x) = \frac{x^3}{3} + \_C1 \right\}$$

**2.527 ODE No. 527**

$$\left( \frac{d}{dx} y(x) \right)^3 - x(y(x))^4 \frac{d}{dx} y(x) - (y(x))^5 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.671 (sec), leaf count = 43

$$\left\{ y(x) = \_C1 \sqrt{\frac{\_C1^{10}}{(\_C1^4 x - 1)^2}}, y(x) = -\frac{3\sqrt{3}}{2} x^{-\frac{3}{2}}, y(x) = \frac{3\sqrt{3}}{2} x^{-\frac{3}{2}} \right\}$$

**2.528 ODE No. 528**

$$\left( \frac{d}{dx} y(x) \right)^3 + a \left( \frac{d}{dx} y(x) \right)^2 + by(x) + abx = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.078 (sec), leaf count = 95

$$\left\{ y(x) = -ax - \frac{a \left( e^{\text{RootOf}(-2a^2\_Z - 3e^2 - Z + 8ae^{-Z} + 2\_C1 b - 5a^2 - 2bx)} - a \right)^2 + \left( e^{\text{RootOf}(-2a^2\_Z - 3e^2 - Z + 8ae^{-Z} + 2\_C1 b - 5a^2 - 2bx)} - a \right)}{b} \right\}$$

**2.529 ODE No. 529**

$$\left( \frac{d}{dx}y(x) \right)^3 + x \left( \frac{d}{dx}y(x) \right)^2 - y(x) = 0$$

**Mathematica:** cpu = 52.151622 (sec), leaf count = 1758

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( \frac{4 \cdot 2^{2/3} x^4}{3 \left( -16x^3 - 72x^2 - 108x + 216c_1 + \sqrt{4(-4x^2 - 12x - 9)^3 + (-16x^3 - 72x^2 - 108x + 216c_1)^2} \right)} \right) \right. \right.$$

**Maple:** cpu = 0.031 (sec), leaf count = 1473

$$\left\{ y(x) = 0, y(x) = \left( \frac{1}{6} \sqrt[3]{-36x^2 - 54x + 108\_C1 - 8x^3 + 27 + 6\sqrt{-48\_C1x^3 - 216x^2\_C1 - 24x^3}} \right) \right.$$

**2.530 ODE No. 530**

$$\left( \frac{d}{dx}y(x) \right)^3 - y(x) \left( \frac{d}{dx}y(x) \right)^2 + (y(x))^2 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.094 (sec), leaf count = 421

$$\left\{ x - \int^{y(x)} 6 \frac{\sqrt[3]{-108\_a^2 + 8\_a^3 + 12\sqrt{-3\_a^4(4\_a - 27)}}}{4\_a^2 + 2\_a \sqrt[3]{-108\_a^2 + 8\_a^3 + 12\sqrt{-3\_a^4(4\_a - 27)}} + (-108\_a^2 + 8\_a^3 + 12\sqrt{-3\_a^4(4\_a - 27)}}} \right.$$

**2.531 ODE No. 531**

$$\left( \frac{d}{dx}y(x) \right)^2 - ((y(x))^4 + x(y(x))^2 + x^2) \left( \frac{d}{dx}y(x) \right)^2 + (x(y(x))^6 + x^2(y(x))^4 + x^3(y(x))^2) \frac{d}{dx}y(x) - x^3$$

**Mathematica:** cpu = 73.501334 (sec), leaf count = 72

DSolve[-x^3 y(x)^6 - (x^2 + y(x)^4 + x y(x)^2) y'(x)^2 + (x^3 y(x)^2 + x^2 y(x)^4 + x y(x)^6) y'(x) + y'(x)^2 = 0, y(x)

**Maple:** cpu = 1.935 (sec), leaf count = 0

could not solve

**2.532 ODE No. 532**

$$a \left( \frac{d}{dx}y(x) \right)^3 + b \left( \frac{d}{dx}y(x) \right)^2 + c \frac{d}{dx}y(x) - y(x) - d = 0$$

**Mathematica:** cpu = 3505.56 (sec), leaf count = 1258

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \int_1^{\#1} \frac{\sqrt[3]{2b^3 - 9ac}}{2b \sqrt[3]{2b^3 - 9acb - 27a^2d - 27a^2K[1]} + \sqrt{4(3ac - b^2)^3 + (2b^3 - 9acb - 27a^2d - 27a^2K[1])^2}} dx \right] \right. \right.$$

**Maple:** cpu = 0.125 (sec), leaf count = 1211

$$\left\{ x - \int^{y(x)} \frac{6 \sqrt[3]{108 - a^2}}{(108 - a^2 + 12 \sqrt{3} \sqrt{27 - a^2} a^2 + 54 - a a^2 d + 18 - a abc - 4 - a b^3 + 27 a^2 d^2 + 18 abcd + 4 acd^2)} dy \right.$$

**2.533 ODE No. 533**

$$x \left( \frac{d}{dx}y(x) \right)^3 - y(x) \left( \frac{d}{dx}y(x) \right)^2 + a = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.032 (sec), leaf count = 92

$$\left\{ y(x) = \frac{3 \sqrt[3]{2}}{2} \sqrt[3]{ax^2}, y(x) = -\frac{3 \sqrt[3]{2}}{4} \sqrt[3]{ax^2} - \frac{3i}{4} \sqrt{3 \sqrt[3]{2} \sqrt[3]{ax^2}}, y(x) = -\frac{3 \sqrt[3]{2}}{4} \sqrt[3]{ax^2} + \frac{3i}{4} \sqrt{3 \sqrt[3]{2} \sqrt[3]{ax^2}}, y(x) = \right.$$

**2.534 ODE No. 534**

$$4x \left( \frac{d}{dx} y(x) \right)^3 - 6y(x) \left( \frac{d}{dx} y(x) \right)^2 + 3y(x) - x = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.062 (sec), leaf count = 102

$$\left\{ y(x) = x, y(x) = \left( -\frac{1}{2} - \frac{\sqrt{3}}{2} \right) x, y(x) = \left( \frac{\sqrt{3}}{2} - \frac{1}{2} \right) x, y(x) = x \left( -\frac{(x + \_C1)\sqrt{2}}{\_C1^2} \sqrt{\_C1(x + \_C1)} \right) \right\}$$

**2.535 ODE No. 535**

$$8x \left( \frac{d}{dx} y(x) \right)^3 - 12y(x) \left( \frac{d}{dx} y(x) \right)^2 + 9y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.046 (sec), leaf count = 80

$$\left\{ y(x) = 0, y(x) = \frac{x}{\_C1^3} (\_C1(3\_C1 + x))^{\frac{3}{2}} \left( -3 \frac{3\_C1 + x}{\_C1} + 9 \right)^{-1}, y(x) = -\frac{3x}{2}, y(x) = \frac{3x}{2}, y(x) = \dots \right\}$$

**2.536 ODE No. 536**

$$(-a^2 + x^2) \left( \frac{d}{dx} y(x) \right)^3 + bx(-a^2 + x^2) \left( \frac{d}{dx} y(x) \right)^2 + \frac{d}{dx} y(x) + bx = 0$$

**Mathematica:** cpu = 0.023503 (sec), leaf count = 86

$$\left\{ \left\{ y(x) \rightarrow c_1 - \frac{bx^2}{2} \right\}, \left\{ y(x) \rightarrow c_1 - \tan^{-1} \left( \frac{x\sqrt{a^2 - x^2}}{x^2 - a^2} \right) \right\}, \left\{ y(x) \rightarrow \tan^{-1} \left( \frac{x\sqrt{a^2 - x^2}}{x^2 - a^2} \right) + c_1 \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 52

$$\left\{ y(x) = -\frac{bx^2}{2} + \_C1, y(x) = -\arctan \left( x \frac{1}{\sqrt{a^2 - x^2}} \right) + \_C1, y(x) = \arctan \left( x \frac{1}{\sqrt{a^2 - x^2}} \right) + \_C1 \right\}$$

**2.537 ODE No. 537**

$$x^3 \left( \frac{d}{dx} y(x) \right)^3 - 3x^2 y(x) \left( \frac{d}{dx} y(x) \right)^2 + (3x(y(x))^2 + x^6) \frac{d}{dx} y(x) - (y(x))^3 - 2x^5 y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

**2.538 ODE No. 538**

$$2 \left( x \frac{d}{dx} y(x) + y(x) \right)^3 - y(x) \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.608 (sec), leaf count = 3181

$$\left\{ \int_{-b}^x -\frac{1}{-a} \left( 6^{\frac{2}{3}} \left( y(x) \left( \sqrt{3} \sqrt{\frac{y(x)(27 - a y(x) - 2)}{-a}} - 9 y(x) \right) - a^2 \right)^{\frac{2}{3}} - 6 y(x) - a \sqrt[3]{6} \sqrt[3]{y(x) \left( \sqrt{3} \sqrt{\frac{y(x)(27 - a y(x) - 2)}{-a}} - 9 y(x) \right)} \right) dx \right.$$

**2.539 ODE No. 539**

$$\left( \frac{d}{dx} y(x) \right)^3 \sin(x) - (y(x) \sin(x) - (\cos(x))^2) \left( \frac{d}{dx} y(x) \right)^2 - (y(x) (\cos(x))^2 + \sin(x)) \frac{d}{dx} y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.026503 (sec), leaf count = 45

$$\left\{ \{y(x) \rightarrow c_1 e^x\}, \{y(x) \rightarrow c_1 - \cos(x)\}, \left\{ y(x) \rightarrow c_1 - \log \left( \sin \left( \frac{x}{2} \right) \right) + \log \left( \cos \left( \frac{x}{2} \right) \right) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 32

$$y(x) = \_C1 e^x, y(x) = -\cos(x) + \_C1, y(x) = -\ln(\csc(x) - \cot(x)) + \_C1$$

**2.540 ODE No. 540**

$$2y(x) \left( \frac{d}{dx} y(x) \right)^3 - y(x) \left( \frac{d}{dx} y(x) \right)^2 + 2x \frac{d}{dx} y(x) - x = 0$$

**Mathematica:** cpu = 0.019502 (sec), leaf count = 69

$$\left\{ \left\{ y(x) \rightarrow c_1 + \frac{x}{2} \right\}, \left\{ y(x) \rightarrow \frac{(3c_1 - 2ix^{3/2})^{2/3}}{2^{2/3}} \right\}, \left\{ y(x) \rightarrow \frac{(3c_1 + 2ix^{3/2})^{2/3}}{2^{2/3}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 109

$$\left\{ x + \frac{C1 x}{y(x)} \left( \frac{1}{y(x)} \left( -\sqrt{-xy(x)} + y(x) \right) \right)^{-\frac{2}{3}} \left( \frac{1}{y(x)} \left( -x + \sqrt{-xy(x)} + y(x) \right) \right)^{-\frac{2}{3}} = 0, x + \frac{C1 x}{y(x)} \left( \frac{1}{y(x)} \left( \sqrt{-xy(x)} + y(x) \right) \right)^{-\frac{2}{3}} \left( \frac{1}{y(x)} \left( x + \sqrt{-xy(x)} + y(x) \right) \right)^{-\frac{2}{3}} = 0 \right\}$$

**2.541 ODE No. 541**

$$(y(x))^2 \left( \frac{d}{dx} y(x) \right)^3 + 2x \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.499 (sec), leaf count = 103

$$\left\{ y(x) = \sqrt{-C1^3 + 2\_C1 x}, y(x) = -\frac{2i}{3} \sqrt[4]{2} \sqrt[4]{3} \sqrt[4]{-x^3}, y(x) = \frac{2i}{3} \sqrt[4]{2} \sqrt[4]{3} \sqrt[4]{-x^3}, y(x) = -\sqrt{-C1^3 + 2\_C1 x} \right\}$$

**2.542 ODE No. 542**

$$16(y(x))^2 \left( \frac{d}{dx} y(x) \right)^3 + 2x \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.500 (sec), leaf count = 107

$$\left\{ y(x) = \sqrt{16\_C1^3 + 2\_C1 x}, y(x) = -\frac{i}{3} \sqrt[4]{2} \sqrt[4]{3} \sqrt[4]{-x^3}, y(x) = \frac{i}{3} \sqrt[4]{2} \sqrt[4]{3} \sqrt[4]{-x^3}, y(x) = -\sqrt{16\_C1^3 + 2\_C1 x} \right\}$$

**2.543 ODE No. 543**

$$x(y(x))^2 \left(\frac{d}{dx}y(x)\right)^3 - (y(x))^3 \left(\frac{d}{dx}y(x)\right)^2 + x(x^2 + 1) \frac{d}{dx}y(x) - x^2y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 1.060 (sec), leaf count = 325

$$\left\{ y(x) = -\frac{i}{2} \sqrt[4]{-16x^4 + 40x^2 + 2 - 2\sqrt{-512x^6 + 192x^4 - 24x^2 + 1}}, y(x) = -\frac{i}{2} \sqrt[4]{-16x^4 + 40x^2 + 2 + 2\sqrt{-512x^6 + 192x^4 - 24x^2 + 1}} \right.$$

**2.544 ODE No. 544**

$$x^7(y(x))^2 \left(\frac{d}{dx}y(x)\right)^3 - (3x^6(y(x))^3 - 1) \left(\frac{d}{dx}y(x)\right)^2 + 3x^5(y(x))^4 \frac{d}{dx}y(x) - x^4(y(x))^5 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.686 (sec), leaf count = 7860

**2.545 ODE No. 545**

$$\left(\frac{d}{dx}y(x)\right)^4 - (y(x) - a)^3 (y(x) - b)^2 = 0$$

**Mathematica:** cpu = 0.701589 (sec), leaf count = 383

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\frac{\sqrt[4]{a - \#1} \sqrt{\frac{\#1 - b}{a - b}} B_{\frac{a - \#1}{a - b}} \left( \frac{1}{4}, \frac{1}{2} \right)}{\sqrt{b - \#1} \sqrt[4]{\frac{a - \#1}{a - b}}} \& \right] [c_1 - \sqrt[4]{-1x}] \right\}, \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \frac{\sqrt[4]{a - \#1} \sqrt{\frac{\#1 - b}{a - b}} B_{\frac{a - \#1}{a - b}} \left( \frac{1}{4}, \frac{1}{2} \right)}{\sqrt{b - \#1} \sqrt[4]{\frac{a - \#1}{a - b}}} \& \right] [c_1 + \sqrt[4]{-1x}] \right\} \right.$$

**Maple:** cpu = 0.140 (sec), leaf count = 141

$$\left\{ x - \int^{y(x)} \frac{1}{\sqrt[4]{(a - a)^3 (-b + a)^2}} da - C1 = 0, x - \int^{y(x)} -i \frac{1}{\sqrt[4]{(a - a)^3 (-b + a)^2}} da - C1 = 0 \right.$$

**2.546 ODE No. 546**

$$\left(\frac{d}{dx}y(x)\right)^4 + 3(x-1)\left(\frac{d}{dx}y(x)\right)^2 - 3(2y(x)-1)\frac{d}{dx}y(x) + 3x = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.125 (sec), leaf count = 245

$$\left\{ y(x) = -x + \frac{5}{6}, y(x) = x + \frac{1}{6}, y(x) = \frac{x}{6} \left( 3 \left( -C1/2 - 1/2 \sqrt{-C1^2 + 4x} \right)^2 + 3 \right) \left( -\frac{C1}{2} - \frac{1}{2} \sqrt{-C1^2 + 4x} \right) \right.$$

**2.547 ODE No. 547**

$$\left(\frac{d}{dx}y(x)\right)^4 - 4y(x)\left(x\frac{d}{dx}y(x) - 2y(x)\right)^2 = 0$$

**Mathematica:** cpu = 1.233157 (sec), leaf count = 490

$$\left\{ \text{Solve} \left[ \frac{\sqrt{(x^2 - 4\sqrt{y(x)})y(x)} \log\left(\sqrt{x^2 - 4\sqrt{y(x)}} + x\right)}{\sqrt{x^2 - 4\sqrt{y(x)}}\sqrt{y(x)}} - \frac{\sqrt{x^2 - 4\sqrt{y(x)}}\sqrt{y(x)} \log(y(x))}{4\sqrt{(x^2 - 4\sqrt{y(x)})y(x)}} + \frac{1}{4} \log(y(x)) \right] \right.$$

**Maple:** cpu = 0.171 (sec), leaf count = 118

$$\left\{ 1\sqrt{y(x)}\left(\sqrt{x^2 - 4\sqrt{y(x)}} + x\right)^{1\sqrt{x^2y(x)-4(y(x))}^{3/2}} \frac{1}{\sqrt{x^2-4\sqrt{y(x)}}\sqrt{y(x)}} \left( \left(\sqrt{x^2 - 4\sqrt{y(x)}} - x\right)^{1\sqrt{x^2y(x)-4(y(x))}^{3/2}} \right) \right.$$

**2.548 ODE No. 548**

$$\left(\frac{d}{dx}y(x)\right)^6 - (y(x)-a)^4(y(x)-b)^3 = 0$$

**Mathematica:** cpu = 1.005628 (sec), leaf count = 569

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\frac{\sqrt[3]{a-\#1}\sqrt{\frac{\#1-b}{a-b}}B_{\frac{a-\#1}{a-b}}\left(\frac{1}{3}, \frac{1}{2}\right)}{\sqrt{b-\#1}\sqrt[3]{\frac{a-\#1}{a-b}}} \& \right] [c_1 - ix] \right\}, \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \dots \right] \right. \right.$$



**Maple:** cpu = 0.234 (sec), leaf count = 241

$$\left\{ x - \int^{y(x)} \frac{1}{\sqrt[6]{(-a-a)^4(-b+a)^3}} da - C1 = 0, x - \int^{y(x)} \frac{-2i}{\sqrt{3}-i} \frac{1}{\sqrt[6]{(-a-a)^4(-b+a)^3}} da - \right.$$

## 2.549 ODE No. 549

$$x^2 \left( \left( \frac{d}{dx} y(x) \right)^2 + 1 \right)^3 - a^2 = 0$$

**Mathematica:** cpu = 0.246031 (sec), leaf count = 406

$$\left\{ \left\{ y(x) \rightarrow c_1 - \frac{\sqrt[3]{x}(2x^{2/3} + (1 + i\sqrt{3})a^{2/3}) \sqrt{\frac{-2x^{2/3} + (-1 - i\sqrt{3})a^{2/3}}{x^{2/3}}}}{2\sqrt{2}} \right\}, \left\{ y(x) \rightarrow c_1 + \frac{\sqrt[3]{x} \sqrt{\frac{-2x^{2/3} + (-1 - i\sqrt{3})a^{2/3}}{x^{2/3}}}}{2\sqrt{2}} \right\} \right.$$

**Maple:** cpu = 0.140 (sec), leaf count = 552

$$\left\{ y(x) = -1 \sqrt{-\frac{1}{a^4} (a^2 x)^{\frac{4}{3}} \left( (a^2 x)^{\frac{2}{3}} - a^2 \right) \left( (a^2 x)^{\frac{2}{3}} - a^2 \right) (a^2 x)^{-\frac{2}{3}} + C1}, y(x) = 1 \sqrt{-\frac{1}{a^4} (a^2 x)^{\frac{4}{3}} \left( (a^2 x)^{\frac{2}{3}} - a^2 \right) \left( (a^2 x)^{\frac{2}{3}} - a^2 \right) (a^2 x)^{-\frac{2}{3}} + C1} \right.$$

## 2.550 ODE No. 550

$$\left( \frac{d}{dx} y(x) \right)^r - a(y(x))^s - bx^{\frac{rs}{r-s}} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.203 (sec), leaf count = 61

$$\left\{ - \int_{-b}^{y(x)} \left( x(r-s) \sqrt[r]{a a^s + b x^{\frac{rs}{r-s}}} - r a \right)^{-1} da(r-s) + \ln(x) - C1 = 0 \right\}$$

**2.551 ODE No. 551**

$$\left( \frac{d}{dx} y(x) \right)^n - (f(x))^n (y(x) - a)^{n+1} (y(x) - b)^{n-1} = 0$$

**Mathematica:** cpu = 0.381048 (sec), leaf count = 84

$$\left\{ \left\{ y(x) \rightarrow \frac{-a(a-b)^n \left( \int_1^x (-1)^{\frac{1}{n}+1} f(K[1]) dK[1] + c_1 \right)^n - bn^n}{-(a-b)^n \left( \int_1^x (-1)^{\frac{1}{n}+1} f(K[1]) dK[1] + c_1 \right)^n - n^n} \right\} \right\}$$

**Maple:** cpu = 0.297 (sec), leaf count = 127

$$\left\{ y(x) = -a \left( \frac{n}{-C1 a + C1 b - a \int f(x) dx + b \int f(x) dx} \right)^n \left( -1 + \left( \frac{n}{-C1 a + C1 b - a \int f(x) dx} \right)^n \right) \right\}$$

**2.552 ODE No. 552**

$$\left( \frac{d}{dx} y(x) \right)^n - f(x) g(y(x)) = 0$$

**Mathematica:** cpu = 0.164021 (sec), leaf count = 39

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \int_1^{\#1} g(K[1])^{-1/n} dK[1] \& \right] \left[ \int_1^x f(K[2])^{\frac{1}{n}} dK[2] + c_1 \right] \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 43

$$\left\{ \int^{y(x)} (g(a))^{-n-1} da + \int^x -\frac{\sqrt[n]{f(a)g(y(x))}}{\sqrt[n]{g(y(x))}} da + C1 = 0 \right\}$$

**2.553 ODE No. 553**

$$a \left( \frac{d}{dx} y(x) \right)^m + b \left( \frac{d}{dx} y(x) \right)^n - y(x) = 0$$

**Mathematica:** cpu = 0.120015 (sec), leaf count = 51

$$\text{Solve} \left\{ \left\{ x = \frac{amK\$1483716^{m-1}}{m-1} + \frac{bnK\$1483716^{n-1}}{n-1} + c_1, y(x) = aK\$1483716^m + bK\$1483716^n \right\}, \{y(x)\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 36

$$\left\{ x - \int^{y(x)} (\text{RootOf}(-a_Z^m - b_Z^n + a))^{-1} da - C1 = 0, y(x) = 0 \right\}$$

**2.554 ODE No. 554**

$$x^{n-1} \left( \frac{d}{dx} y(x) \right)^n - nx \frac{d}{dx} y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.075010 (sec), leaf count = 49

Solve  $\left\{ y(x) = \frac{K\$1483865nx^2 - K\$1483865^n x^n}{x}, x = c_1(K\$1483865 - K\$1483865n)^{\frac{n}{1-n}} \right\}, \{y(x), K\$1483865\}$

**Maple:** cpu = 0.266 (sec), leaf count = 29

$$\left\{ y(x) = -C1 \sqrt[n]{\frac{x}{-C1}} n - \frac{(-C1^{-1})^{-n}}{-C1} \right\}$$

**2.555 ODE No. 555**

$$\sqrt{\left( \frac{d}{dx} y(x) \right)^2 + 1} + x \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.015 (sec), leaf count = 15

$$\left\{ y(x) = \sqrt{-C1^2 + 1} + -C1 x \right\}$$

**2.556 ODE No. 556**

$$\sqrt{\left( \frac{d}{dx} y(x) \right)^2 + 1} + x \left( \frac{d}{dx} y(x) \right)^2 + y(x) = 0$$

**Mathematica:** cpu = 6.600838 (sec), leaf count = 60

Solve  $\left\{ x = \frac{c_1}{(K\$1484035 + 1)^2} + \frac{-\sqrt{K\$1484035^2 + 1} - \sinh^{-1}(K\$1484035)}{(K\$1484035 + 1)^2}, y(x) = K\$1484035^2(-x) - \dots \right\}$

**Maple:** cpu = 0.156 (sec), leaf count = 581

$$\left\{ x^2 - C1 \left( \sqrt{-4xy(x) + 2 + 2\sqrt{4x^2 - 4xy(x) + 1}} - 2x \right)^{-2} + x + 2 \frac{x^2}{\left( \sqrt{-4xy(x) + 2 + 2\sqrt{4x^2 - 4xy(x) + 1}} \right)^2} \right\}$$

**2.557 ODE No. 557**

$$x \left( \sqrt{\left( \frac{d}{dx} y(x) \right)^2 + 1} + \frac{d}{dx} y(x) \right) - y(x) = 0$$

**Mathematica:** cpu = 0.016002 (sec), leaf count = 39

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{c_1 x - x^2} \right\}, \left\{ y(x) \rightarrow \sqrt{c_1 x - x^2} \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 78

$$\left\{ -C1 \frac{1}{\sqrt{\frac{(y(x))^2 + x^2}{x^2 (y(x))^2}}} \left( -\frac{x^2 - (y(x))^2}{2xy(x)} + \frac{1}{2} \sqrt{\frac{x^4 + 2x^2(y(x))^2 + (y(x))^4}{x^2(y(x))^2}} \right)^{-1} + x = 0 \right\}$$

**2.558 ODE No. 558**

$$ax \sqrt{\left( \frac{d}{dx} y(x) \right)^2 + 1} + x \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.586574 (sec), leaf count = 395

$$\left\{ \text{Solve} \left[ \frac{a \left( -\log \left( \frac{(a^2-1) \left( a \sqrt{a^2 - \frac{y(x)^2}{x^2} - 1} + a^2 - \frac{iy(x)}{x} - 1 \right)}{a^3 \left( \frac{y(x)}{x} - i \right)} \right) + \log \left( -\frac{(a^2-1) \left( a \sqrt{a^2 - \frac{y(x)^2}{x^2} - 1} + a^2 + \frac{iy(x)}{x} - 1 \right)}{a^3 \left( \frac{y(x)}{x} + i \right)} \right) + \log \left( \frac{y(x)}{x} \right)}{2(a^2 - 1)} \right] \right\}$$

**Maple:** cpu = 0.140 (sec), leaf count = 223

$$\left\{ x - C1 e^{\frac{1}{a} \text{Arcsinh} \left( \frac{1}{(a^2-1)x} \left( \sqrt{-a^2 x^2 + x^2 + (y(x))^2} a + y(x) \right) \right)} \frac{1}{\sqrt{\frac{1}{(a^2-1)^2 x^2} \left( -a^2 x^2 + a^2 (y(x))^2 + 2 \sqrt{-a^2 x^2 + x^2 + (y(x))^2} \right)}} \right\}$$

**2.559 ODE No. 559**

$$y(x) \sqrt{\left(\frac{d}{dx}y(x)\right)^2 + 1} - ay(x) \frac{d}{dx}y(x) - ax = 0$$

**Mathematica:** cpu = 0.351045 (sec), leaf count = 212

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{a^6(-x^2) + 3a^4x^2 + 2a^2xe^{a^2c_1-c_1} - 2xe^{a^2c_1-c_1} + e^{2a^2c_1-2c_1} - 3a^2x^2 + x^2}}{\sqrt{a^6 - 3a^4 + 3a^2 - 1}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{a^6}}{\dots} \right\} \right\}$$

**Maple:** cpu = 0.234 (sec), leaf count = 223

$$\left\{ x - e^{\int \frac{1}{(a^2-1)y(x)} (-a^2x + \sqrt{a^2x^2 + a^2(y(x))^2 - (y(x))^2})} a(a\sqrt{-a^2+1} - a) \frac{1}{\sqrt{-a^2+1}} (-_a a + \sqrt{-a^2+1})^{-1} (-_a^2 a + \sqrt{-a^2+1} - a - a)^{-1} d\_a \dots \right\}$$

**2.560 ODE No. 560**

$$ay(x) \sqrt{\left(\frac{d}{dx}y(x)\right)^2 + 1} - 2xy(x) \frac{d}{dx}y(x) + (y(x))^2 - x^2 = 0$$

**Mathematica:** cpu = 21.646749 (sec), leaf count = 110

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{a^2c_1^2(-x^2) - 4a^2c_1x - 4a^2 + 4x^2}}{\sqrt{a^2c_1^2 - 4}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{a^2c_1^2(-x^2) - 4a^2c_1x - 4a^2 + 4x^2}}{\sqrt{a^2c_1^2 - 4}} \right\} \right\}$$

**Maple:** cpu = 0.671 (sec), leaf count = 1512

$$\left\{ \int_{-b}^x 1 \left( 2\_a^3 - 2\_a(y(x))^2 + \sqrt{a^2(-a^4 + 2\_a^2(y(x))^2 - a^2(y(x))^2 + (y(x))^4)} \right) \left( -2a^2\_a(y(x))^2 + \dots \right) \right\}$$

**2.561 ODE No. 561**

$$f((y(x))^2 + x^2) \sqrt{\left(\frac{d}{dx}y(x)\right)^2 + 1} - x \frac{d}{dx}y(x) + y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 1.919 (sec), leaf count = 50

$$\left\{ y(x) = x \left( \tan \left( \text{RootOf} \left( -2\_Z + \int \frac{x^2((\tan(\_Z))^2+1)}{(\tan(\_Z))^2} \frac{f(\_a)}{-a} \frac{1}{\sqrt{-(f(\_a))^2 + \_a}} d\_a + 2\_C1 \right) \right) \right)^{-1} \right\}$$

## 2.562 ODE No. 562

$$a \sqrt[3]{\left(\frac{d}{dx}y(x)\right)^3 + 1} + bx \frac{d}{dx}y(x) - y(x) = 0$$

**Mathematica:** cpu = 264.371071 (sec), leaf count = 119

$$\text{Solve} \left[ \left\{ x = \frac{a(b-1) \sqrt[3]{(K\$1486420^3 (K\$1486420 - bK\$1486420)^{\frac{b}{1-b} + \frac{1}{b-1}})}{3b-2} {}_2F_1\left(\frac{2}{3}, \frac{2-3b}{3-3b}, \frac{5-6b}{3-3b}, -K\$1486420^3\right) \right\} + \right.$$

**Maple:** cpu = 0.094 (sec), leaf count = 3961

$$\left\{ x - \left( \frac{1}{2b^3x^3 + 2a^3} \left( 2b^2x^2y(x) \sqrt[3]{-4b^6x^6 - 8a^3b^3x^3 - 4b^3x^3(y(x))^3} + 4\sqrt{b^6x^6 + 2a^3b^3x^3 + 2b^3x^3(y(x))^3} \right) \right) \right\}$$

## 2.563 ODE No. 563

$$\ln\left(\frac{d}{dx}y(x)\right) + x \frac{d}{dx}y(x) + ay(x) + b = 0$$

**Mathematica:** cpu = 0.108514 (sec), leaf count = 59

$$\text{Solve} \left[ a \left( \frac{(a+1) \log(1 - aW(xe^{-ay(x)-b}))}{a^2} + \frac{W(xe^{-ay(x)-b})}{a} \right) + ay(x) = c_1, y(x) \right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 66

$$\left\{ -\left(e^{-ay(x)-\text{lambertW}(xe^{-ay(x)-b})-b}\right)^{-(a+1)^{-1}} -C1 + x - \frac{e^{ay(x)+\text{lambertW}(xe^{-ay(x)-b})+b}}{a} = 0 \right\}$$

**2.564 ODE No. 564**

$$\ln\left(\frac{d}{dx}y(x)\right) + a\left(x\frac{d}{dx}y(x) - y(x)\right) = 0$$

**Mathematica:** cpu = 0.042005 (sec), leaf count = 28

$$\left\{ \left\{ y(x) \rightarrow -\frac{e^{-c_1}(e^{c_1}c_1 - ax)}{a} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 36

$$\left\{ y(x) = -C1 x + \frac{\ln(-C1)}{a}, y(x) = \frac{1}{a} \ln\left(-\frac{1}{ax}\right) - a^{-1} \right\}$$

**2.565 ODE No. 565**

$$y(x) \ln\left(\frac{d}{dx}y(x)\right) + \frac{d}{dx}y(x) - y(x) \ln(y(x)) - xy(x) = 0$$

**Mathematica:** cpu = 0.011501 (sec), leaf count = 25

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{1}{2}W(e^x)^2 + W(e^x)} \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 17

$$\left\{ y(x) = -C1 e^{\frac{\text{lambertW}(e^x)(\text{lambertW}(e^x)+2)}{2}} \right\}$$

**2.566 ODE No. 566**

$$\sin\left(\frac{d}{dx}y(x)\right) + \frac{d}{dx}y(x) - x = 0$$

**Mathematica:** cpu = 0.010001 (sec), leaf count = 19

$$\text{DSolve}[y'(x) + \sin(y'(x)) - x = 0, y(x), x]$$

**Maple:** cpu = 0.031 (sec), leaf count = 16

$$\left\{ y(x) = \int \text{RootOf}(-Z + \sin(-Z) - x) dx + -C1 \right\}$$

**2.567 ODE No. 567**

$$a \cos \left( \frac{d}{dx} y(x) \right) + b \frac{d}{dx} y(x) + x = 0$$

**Mathematica:** cpu = 0.011001 (sec), leaf count = 21

$$\text{DSolve}[a \cos (y'(x)) + b y'(x) + x = 0, y(x), x]$$

**Maple:** cpu = 0.031 (sec), leaf count = 18

$$\left\{ y(x) = \int \text{RootOf}(a \cos (_Z) + _Z b + x) dx + _C1 \right\}$$

**2.568 ODE No. 568**

$$\left( \frac{d}{dx} y(x) \right)^2 \sin \left( \frac{d}{dx} y(x) \right) - y(x) = 0$$

**Mathematica:** cpu = 0.036505 (sec), leaf count = 28

Solve[ $\{x = c_1 + K\$1487319 \sin(K\$1487319) - \cos(K\$1487319), y(x) = K\$1487319^2 \sin(K\$1487319)\}$ , {

**Maple:** cpu = 0.047 (sec), leaf count = 32

$$\left\{ x - \int^{y(x)} (\text{RootOf}(\sin (_Z) _Z^2 - _a))^{-1} d_a - _C1 = 0, y(x) = 0 \right\}$$

**2.569 ODE No. 569**

$$\left( \left( \frac{d}{dx} y(x) \right)^2 + 1 \right) \left( \sin \left( x \frac{d}{dx} y(x) - y(x) \right) \right)^2 - 1 = 0$$

**Mathematica:** cpu = 0.040505 (sec), leaf count = 59

$$\left\{ \left\{ y(x) \rightarrow c_1 x - \frac{1}{2} \cos^{-1} \left( \frac{c_1^2 - 1}{c_1^2 + 1} \right) \right\}, \left\{ y(x) \rightarrow c_1 x + \frac{1}{2} \cos^{-1} \left( \frac{c_1^2 - 1}{c_1^2 + 1} \right) \right\} \right\}$$

**Maple:** cpu = 0.358 (sec), leaf count = 147

$$\left\{ y(x) = _C1 x - \arcsin \left( \frac{1}{\sqrt{-C1^2 + 1}} \right), y(x) = _C1 x + \arcsin \left( \frac{1}{\sqrt{-C1^2 + 1}} \right), y(x) = -\sqrt{1 - x} \sqrt{x} \right\}$$



**2.570 ODE No. 570**

$$\left( \left( \frac{d}{dx} y(x) \right)^2 + 1 \right) \left( \arctan \left( \frac{d}{dx} y(x) \right) + ax \right) + \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.108514 (sec), leaf count = 29

$$\text{DSolve}[(y'(x)^2 + 1) (ax + \tan^{-1}(y'(x))) + y'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.047 (sec), leaf count = 30

$$\left\{ y(x) = \int \tan(\text{RootOf}(ax(\tan(_Z))^2 + (\tan(_Z))^2 _Z + ax + \tan(_Z) + _Z)) dx + _C1 \right\}$$

**2.571 ODE No. 571**

$$ax^n f \left( \frac{d}{dx} y(x) \right) + x \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.102013 (sec), leaf count = 114

$$\text{Solve} \left[ \left\{ y(x) = af(K\$1487621)x^n + K\$1487621x, x = \left( nf(K\$1487621) \right)^{\frac{1}{n}-1} \left( \int_1^{K\$1487621} \frac{f(K[1])^{\frac{n-1}{n}-1}}{an} \right) \right. \right.$$

**Maple:** cpu = 0.203 (sec), leaf count = 199

$$\left\{ [y(_T) = a \left( \left( -\frac{1}{af(_T)n} \left( -_C1 an + \int (f(_T))^{-n-1} d_T n - \int (f(_T))^{-n-1} d_T \right) \right)^{(n-1)^{-1}} (f \right. \right.$$

**2.572 ODE No. 572**

$$\left( x \frac{d}{dx} y(x) - y(x) \right)^n f \left( \frac{d}{dx} y(x) \right) + y(x) g \left( \frac{d}{dx} y(x) \right) + xh \left( \frac{d}{dx} y(x) \right) = 0$$

**Mathematica:** cpu = 0.030504 (sec), leaf count = 41

$$\text{DSolve}[f(y'(x)) (xy'(x) - y(x))^n + y(x)g(y'(x)) + xh(y'(x)) = 0, y(x), x]$$

**Maple:** cpu = 0.905 (sec), leaf count = 0

could not solve

**2.573 ODE No. 573**

$$f\left(x\left(\frac{d}{dx}y(x)\right)^2\right) + 2x\frac{d}{dx}y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.012002 (sec), leaf count = 42

$$\left\{ \left\{ y(x) \rightarrow f(c_1) - 2\sqrt{c_1}\sqrt{x}, y(x) \rightarrow f(c_1) + 2\sqrt{c_1}\sqrt{x} \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 16

$$\left\{ y(x) = f\left(\frac{-C1^2}{4}\right) + \_C1 \sqrt{x} \right\}$$

**2.574 ODE No. 574**

$$f\left(x - 3/2\left(\frac{d}{dx}y(x)\right)^2\right) + \left(\frac{d}{dx}y(x)\right)^3 - y(x) = 0$$

**Mathematica:** cpu = 0.014502 (sec), leaf count = 102

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{9}\left(9f(c_1) + 2\sqrt{6}x\sqrt{x-c_1} - 2\sqrt{6}c_1\sqrt{x-c_1}\right), y(x) \rightarrow \frac{1}{9}\left(9f(c_1) - 2\sqrt{6}x\sqrt{x-c_1} + 2\sqrt{6}c_1\sqrt{x-c_1}\right) \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 67

$$\left\{ y(x) = f(\_C1) - \frac{2}{9}\sqrt{-6\_C1^3 + 18\_C1^2x - 18x^2\_C1 + 6x^3}, y(x) = f(\_C1) + \frac{2}{9}\sqrt{-6\_C1^3 + 18\_C1^2x - 18x^2\_C1 + 6x^3} \right\}$$

**2.575 ODE No. 575**

$$\left(\frac{d}{dx}y(x)\right) f\left(xy(x)\frac{d}{dx}y(x) - (y(x))^2\right) - x^2\frac{d}{dx}y(x) + xy(x) = 0$$

**Mathematica:** cpu = 0.017002 (sec), leaf count = 41

$$\text{DSolve}\left[y'(x)f(xy(x)y'(x) - y(x)^2) + x^2(-y'(x)) + xy(x) = 0, y(x), x\right]$$

**Maple:** cpu = 0.452 (sec), leaf count = 0

could not solve

**2.576 ODE No. 576**

$$\phi\left(f\left(x, y(x), \frac{d}{dx}y(x)\right), g\left(x, y(x), \frac{d}{dx}y(x)\right)\right) = 0$$

**Mathematica:** cpu = 0.007001 (sec), leaf count = 23

$$\text{DSolve}[\phi(f(x, y(x), y'(x)), g(x, y(x), y'(x))) = 0, y(x), x]$$

**Maple:** cpu = 0.016 (sec), leaf count = 0

could not solve

**2.577 ODE No. 577**

$$\frac{d}{dx}y(x) = F\left(\frac{y(x)}{x+a}\right) = 0$$

**Mathematica:** cpu = 12.111538 (sec), leaf count = 240

$$\text{Solve}\left[\int_1^{y(x)} \left(\frac{1}{-aF\left(\frac{K[2]}{a+x}\right) - xF\left(\frac{K[2]}{a+x}\right) + K[2]} - \int_1^x \left(\frac{F'\left(\frac{K[2]}{K[1]+a}\right)}{(K[1]+a)\left(aF\left(\frac{K[2]}{K[1]+a}\right) + K[1]F\left(\frac{K[2]}{K[1]+a}\right) - K[2]\right)}\right) dK[1] + 1\right) dK[2] + \int_1^x \left(\frac{2K[1]}{F(y(x) - K[1]^2) + 1}\right) dK[1]\right]$$

**Maple:** cpu = 0.031 (sec), leaf count = 28

$$\left\{y(x) = -\text{RootOf}\left(\int^{-Z} (F(-_a) + _a)^{-1} d_a + \ln(x+a) + _C1\right) (x+a)\right\}$$

**2.578 ODE No. 578**

$$\frac{d}{dx}y(x) = 2x + F(y(x) - x^2) = 0$$

**Mathematica:** cpu = 16.413084 (sec), leaf count = 97

$$\text{Solve}\left[\int_1^{y(x)} -\frac{F(K[2] - x^2) \int_1^x -\frac{2K[1]F'(K[2]-K[1]^2)}{F(K[2]-K[1]^2)^2} dK[1] + 1}{F(K[2] - x^2)} dK[2] + \int_1^x \left(\frac{2K[1]}{F(y(x) - K[1]^2) + 1}\right) dK[1]\right]$$

**Maple:** cpu = 0.031 (sec), leaf count = 22

$$\left\{y(x) = x^2 + \text{RootOf}\left(-x + \int^{-Z} (F(_a))^{-1} d_a + _C1\right)\right\}$$

**2.579 ODE No. 579**

$$\frac{d}{dx}y(x) = -1/2 ax + F(y(x) + 1/4 ax^2 + 1/2 bx) = 0$$

**Mathematica:** cpu = 13.258184 (sec), leaf count = 510

$$\text{Solve} \left[ \int_1^{y(x)} \frac{2F\left(K[2] + \frac{ax^2}{4} + \frac{bx}{2}\right) \int_1^x \left( \frac{2aK[1]F'\left(\frac{1}{4}aK[1]^2 + \frac{1}{2}bK[1] + K[2]\right)}{\left(2F\left(\frac{1}{4}aK[1]^2 + \frac{1}{2}bK[1] + K[2]\right) + b\right)^2} + \frac{2F'\left(\frac{1}{4}aK[1]^2 + \frac{1}{2}bK[1] + K[2]\right)}{2F\left(\frac{1}{4}aK[1]^2 + \frac{1}{2}bK[1] + K[2]\right) + b} - \frac{4F\left(\frac{1}{4}aK[1]^2 + \frac{1}{2}bK[1] + K[2]\right)}{\left(2F\left(\frac{1}{4}aK[1]^2 + \frac{1}{2}bK[1] + K[2]\right) + b\right)^2} \right) dx}{\dots} \right]$$

**Maple:** cpu = 0.031 (sec), leaf count = 35

$$\left\{ y(x) = -\frac{ax^2}{4} - \frac{bx}{2} + \text{RootOf}\left(-x + 2 \int^{-Z} (2F(_a) + b)^{-1} d_a + _C1\right) \right\}$$

**2.580 ODE No. 580**

$$\frac{d}{dx}y(x) = F(y(x) e^{-bx}) e^{bx} = 0$$

**Mathematica:** cpu = 24.434103 (sec), leaf count = 200

$$\text{Solve} \left[ \int_1^{y(x)} \left( \frac{1}{bK[2] - e^{bx}F(e^{-bx}K[2])} - \int_1^x \left( \frac{F'(K[2]e^{-bK[1]})}{e^{bK[1]}F(K[2]e^{-bK[1]}) - bK[2]} - \frac{e^{bK[1]}F(K[2]e^{-bK[1]}) (F'(K[2]e^{-bK[1]}))}{(e^{bK[1]}F(K[2]e^{-bK[1]}) - bK[2])^2} \right) dx \right) \right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 31

$$\left\{ y(x) = \frac{\text{RootOf}\left(-x + \int^{-Z} (F(_a) - _ab)^{-1} d_a + _C1\right)}{e^{-bx}} \right\}$$

**2.581 ODE No. 581**

$$\frac{d}{dx}y(x) = 1/2 \frac{1}{x^3} \left( 1 + 2 F\left(1/4 \frac{4x^2y(x) + 1}{x^2}\right) x \right) = 0$$

**Mathematica:** cpu = 40.986705 (sec), leaf count = 141

$$\text{Solve} \left[ \int_1^{y(x)} \frac{F\left(\frac{x^2K[2] + \frac{1}{4}}{x^2}\right) \int_1^x \frac{F'\left(\frac{K[2]K[1]^2 + \frac{1}{4}}{K[1]^2}\right)}{2K[1]^3 F\left(\frac{K[2]K[1]^2 + \frac{1}{4}}{K[1]^2}\right)} dK[1] + 1}{F\left(\frac{x^2K[2] + \frac{1}{4}}{x^2}\right)} dK[2] + \int_1^x \left( \frac{1}{2K[1]^3 F\left(\frac{y(x)K[1]^2 + \frac{1}{4}}{K[1]^2}\right)} + \dots \right) dx \right]$$

**Maple:** cpu = 0.093 (sec), leaf count = 32

$$\left\{ y(x) = \frac{4 \operatorname{RootOf}\left(\int^{-Z} (F(-a))^{-1} d_a a x + \_C1 x + 1\right) x^2 - 1}{4 x^2} \right\}$$

## 2.582 ODE No. 582

$$\frac{d}{dx} y(x) = \frac{1}{ax^2} \left( 1 + F\left(\frac{axy(x) + 1}{ax}\right) ax^2 \right) = 0$$

**Mathematica:** cpu = 16.699621 (sec), leaf count = 139

$$\text{Solve} \left[ \int_1^{y(x)} \frac{F\left(\frac{axK[2]+1}{ax}\right) \int_1^x \frac{F'\left(\frac{aK[1]K[2]+1}{aK[1]}\right)}{aK[1]^2 F\left(\frac{aK[1]K[2]+1}{aK[1]}\right)^2} dK[1] - 1}{F\left(\frac{axK[2]+1}{ax}\right)} dK[2] + \int_1^x \left( -\frac{1}{aK[1]^2 F\left(\frac{ay(x)K[1]+1}{aK[1]}\right)} - 1 \right) \right]$$

**Maple:** cpu = 0.156 (sec), leaf count = 30

$$\left\{ y(x) = \frac{\operatorname{RootOf}\left(-x + \int^{-Z} (F(-a))^{-1} d_a a + \_C1\right) ax - 1}{ax} \right\}$$

## 2.583 ODE No. 583

$$\frac{d}{dx} y(x) = -1/2 (ax^2 - 2F(y(x) + 1/8 ax^4)) x = 0$$

**Mathematica:** cpu = 41.455764 (sec), leaf count = 123

$$\text{Solve} \left[ \int_1^{y(x)} \frac{F\left(K[2] + \frac{ax^4}{8}\right) \int_1^x \frac{aK[1]^3 F'\left(\frac{1}{8}aK[1]^4 + K[2]\right)}{2F\left(\frac{1}{8}aK[1]^4 + K[2]\right)^2} dK[1] + 1}{F\left(K[2] + \frac{ax^4}{8}\right)} dK[2] + \int_1^x \left( K[1] - \frac{aK[1]^3}{2F\left(\frac{1}{8}aK[1]^4 + y(x)\right)} \right) \right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 31

$$\left\{ y(x) = -\frac{ax^4}{8} + \operatorname{RootOf}\left(-x^2 + 2 \int^{-Z} (F(-a))^{-1} d_a a + 2 \_C1\right) \right\}$$

**2.584 ODE No. 584**

$$\frac{d}{dx}y(x) = 2 \frac{a}{y(x) + 2F((y(x))^2 - 4ax)a} = 0$$

**Mathematica:** cpu = 18.981910 (sec), leaf count = 112

$$\text{Solve} \left[ \int_1^{y(x)} \left( \frac{K[2]}{4a^2F(K[2]^2 - 4ax)} - \frac{2a \int_1^x \frac{K[2]F'(K[2]^2 - 4aK[1])}{aF(K[2]^2 - 4aK[1])^2} dK[1] - 1}{2a} \right) dK[2] + \int_1^x -\frac{1}{2aF(y(x)^2 - 4ax)} dx \right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 35

$$\left\{ \frac{y(x)}{2a} + \frac{\int^{(y(x))^2 - 4ax} (F(_a))^{-1} d_a}{8a^2} - C1 = 0 \right\}$$

**2.585 ODE No. 585**

$$\frac{d}{dx}y(x) = F(\ln(\ln(y(x))) - \ln(x))y(x) = 0$$

**Mathematica:** cpu = 123.303658 (sec), leaf count = 202

$$\text{Solve} \left[ \int_1^{y(x)} \left( \frac{1}{K[2](xF(\log(\log(K[2])) - \log(x)) - \log(K[2]))} - \int_1^x \left( \frac{F(\log(\log(K[2])) - \log(K[1]))}{(K[1]F(\log(\log(K[2])) - \log(K[1]))} \right) dx \right) \right]$$

**Maple:** cpu = 0.406 (sec), leaf count = 163

$$\left\{ \int_{-b}^x \frac{F(\ln(\ln(y(x))) - \ln(_a))}{_a F(\ln(\ln(y(x))) - \ln(_a)) + \ln(y(x))} d_a + \int^{y(x)} -\frac{1}{_f(-xF(\ln(\ln(_f)) - \ln(x)) + \ln(_f))} dx \right\}$$

**2.586 ODE No. 586**

$$\frac{d}{dx}y(x) = \frac{x}{\sqrt{x^2 + 1}} F\left(\frac{y(x)}{\sqrt{x^2 + 1}}\right) = 0$$

**Mathematica:** cpu = 143.313198 (sec), leaf count = 972

$$\text{Solve} \left[ \int_1^{y(x)} \left( \frac{\sqrt{x^2+1} F\left(\frac{K[2]}{\sqrt{x^2+1}}\right)}{-x^2 F\left(\frac{K[2]}{\sqrt{x^2+1}}\right)^2 - F\left(\frac{K[2]}{\sqrt{x^2+1}}\right)^2 + K[2]^2} - \int_1^x \left( \frac{K[1] \sqrt{K[1]^2+1} \left( \frac{2F\left(\frac{K[2]}{\sqrt{K[1]^2+1}}\right) F'\left(\frac{K[2]}{\sqrt{K[1]^2+1}}\right)}{\sqrt{K[1]^2+1}} \right)}{K[2] \left( K[1]^2 F\left(\frac{K[2]}{\sqrt{K[1]^2+1}}\right) \right)} \right) \right] \right]$$

**Maple:** cpu = 0.203 (sec), leaf count = 39

$$\left\{ y(x) = \text{RootOf} \left( -\ln(x^2+1) + 2 \int^{-z} (F(_a) - _a)^{-1} d_a + 2\_C1 \right) \sqrt{x^2+1} \right\}$$

## 2.587 ODE No. 587

$$\frac{d}{dx} y(x) = 1/2 (x^{3/2} + 2 F(y(x) - 1/6 x^3)) \sqrt{x} = 0$$

**Mathematica:** cpu = 44.026091 (sec), leaf count = 120

$$\text{Solve} \left[ \int_1^{y(x)} \frac{F\left(K[2] - \frac{x^3}{6}\right) \int_1^x -\frac{K[1]^2 F'\left(K[2] - \frac{K[1]^3}{6}\right)}{2F\left(K[2] - \frac{K[1]^3}{6}\right)^2} dK[1] + 1}{F\left(K[2] - \frac{x^3}{6}\right)} dK[2] + \int_1^x \left( \frac{K[1]^2}{2F\left(y(x) - \frac{K[1]^3}{6}\right)} + \sqrt{K[1]} \right) dK[1] \right]$$

**Maple:** cpu = 0.109 (sec), leaf count = 29

$$\left\{ \int_{-b}^{y(x)} \left( F\left(-a - \frac{x^3}{6}\right) \right)^{-1} d_a - \frac{2}{3} x^{\frac{3}{2}} - _C1 = 0 \right\}$$

## 2.588 ODE No. 588

$$\frac{d}{dx} y(x) = \frac{x + F(-(x - y(x))(y(x) + x))}{y(x)} = 0$$

**Mathematica:** cpu = 31.940556 (sec), leaf count = 106

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x -\frac{2K[1]K[2]F'((K[2] - K[1])(K[1] + K[2]))}{F((K[2] - K[1])(K[1] + K[2]))^2} dK[1] - \frac{K[2]}{F((K[2] - x)(K[2] + x))} \right) dK[2] \right]$$

Maple: cpu = 0.109 (sec), leaf count = 53

$$\left\{ y(x) = \sqrt{x^2 + \text{RootOf} \left( -2x + \int^{-Z} (F(-a))^{-1} d_a + 2_{C1} \right)}, y(x) = -\sqrt{x^2 + \text{RootOf} \left( -2x + \int^{-Z} (F(-a))^{-1} d_a + 2_{C1} \right)} \right.$$

**2.589 ODE No. 589**

$$\boxed{\frac{d}{dx}y(x) = \frac{(y(x))^2}{x} F\left(-\frac{-1 + y(x) \ln(x)}{y(x)}\right) = 0}$$

Mathematica: cpu = 19.556483 (sec), leaf count = 242

$$\text{Solve} \left[ \int_1^{y(x)} \left( \frac{1}{K[2]^2 \left( -F\left(\frac{1 - \log(x)K[2]}{K[2]}\right) - 1 \right)} - \int_1^x \left( \frac{\left( -\frac{\log(K[1])}{K[2]} - \frac{1 - K[2] \log(K[1])}{K[2]^2} \right) F'\left(\frac{1 - K[2] \log(K[1])}{K[2]}\right)}{K[1] \left( F\left(\frac{1 - K[2] \log(K[1])}{K[2]}\right) + 1 \right)} - \right. \right.$$

Maple: cpu = 0.124 (sec), leaf count = 38

$$\left\{ \int_{-b}^{y(x)} \frac{1}{-a^2} \left( F\left(\frac{1 - a \ln(x)}{-a}\right) + 1 \right)^{-1} d_a - \ln(x) - C1 = 0 \right\}$$

**2.590 ODE No. 590**

$$\boxed{\frac{d}{dx}y(x) = \frac{x}{-y(x) + F((y(x))^2 + x^2)} = 0}$$

Mathematica: cpu = 30.943929 (sec), leaf count = 91

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x \frac{2K[1]K[2]F'(K[1]^2 + K[2]^2)}{F(K[1]^2 + K[2]^2)^2} dK[1] - \frac{K[2]}{F(K[2]^2 + x^2)} + 1 \right) dK[2] + \int_1^x -\frac{K[1]}{F(K[1]^2 + x^2)} dK[1] - \right.$$

Maple: cpu = 0.125 (sec), leaf count = 28

$$\left\{ -y(x) + \frac{\int^{(y(x))^2 + x^2} (F(-a))^{-1} d_a}{2} - C1 = 0 \right\}$$



**2.591 ODE No. 591**

$$\frac{d}{dx}y(x) = \frac{x}{\sqrt{a}y(x)} F\left(\frac{a(y(x))^2 + bx^2}{a}\right) = 0$$

**Mathematica:** cpu = 18.189310 (sec), leaf count = 250

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x \left( \frac{2bK[1]K[2]F'\left(\frac{aK[2]^2+bK[1]^2}{a}\right)}{\sqrt{a}\left(\sqrt{a}F\left(\frac{aK[2]^2+bK[1]^2}{a}\right) + b\right)} - \frac{2bK[1]K[2]F\left(\frac{aK[2]^2+bK[1]^2}{a}\right) F'\left(\frac{aK[2]^2+bK[1]^2}{a}\right)}{\left(\sqrt{a}F\left(\frac{aK[2]^2+bK[1]^2}{a}\right) + b\right)^2} \right) \right) \right]$$

**Maple:** cpu = 0.140 (sec), leaf count = 108

$$\left\{ y(x) = \frac{1}{a} \sqrt{a \left( -bx^2 + \text{RootOf} \left( \int^{-Z} (\sqrt{ab} + F(-a)a)^{-1} d_a a a^{\frac{3}{2}} b - bx^2 + 2\_C1 a \right) a \right)}, y(x) = -\frac{1}{a} \sqrt{\dots} \right\}$$

**2.592 ODE No. 592**

$$\frac{d}{dx}y(x) = 1/5 \frac{6x^3 + 5\sqrt{x} + 5F(y(x) - 2/5x^3 - 2\sqrt{x})}{x} = 0$$

**Mathematica:** cpu = 248.171514 (sec), leaf count = 238

$$\text{Solve} \left[ \int_1^{y(x)} \frac{F\left(K[2] - \frac{2x^3}{5} - 2\sqrt{x}\right) \int_1^x \left( -\frac{6K[1]^2 F'\left(-\frac{2}{5}K[1]^3 - 2\sqrt{K[1]} + K[2]\right)}{5F\left(-\frac{2}{5}K[1]^3 - 2\sqrt{K[1]} + K[2]\right)^2} - \frac{F'\left(-\frac{2}{5}K[1]^3 - 2\sqrt{K[1]} + K[2]\right)}{\sqrt{K[1]}F\left(-\frac{2}{5}K[1]^3 - 2\sqrt{K[1]} + K[2]\right)^2} \right)}{F\left(K[2] - \frac{2x^3}{5} - 2\sqrt{x}\right)} \right]$$

**Maple:** cpu = 0.156 (sec), leaf count = 33

$$\left\{ \int_{-b}^{y(x)} \left( F\left(-a - \frac{2x^3}{5} - 2\sqrt{x}\right) \right)^{-1} d_a a - \ln(x) - \_C1 = 0 \right\}$$

**2.593 ODE No. 593**

$$\frac{d}{dx}y(x) = \frac{F\left((y(x))^{3/2} - 3/2 e^x\right) e^x}{\sqrt{y(x)}} = 0$$

**Mathematica:** cpu = 62.104386 (sec), leaf count = 218

$$\text{Solve} \left[ \int_1^{y(x)} \left( \frac{\sqrt{K[2]}}{F\left(K[2]^{3/2} - \frac{3e^x}{2}\right) - 1} - \int_1^x \left( \frac{3e^{K[1]}\sqrt{K[2]}F\left(K[2]^{3/2} - \frac{3e^{K[1]}}{2}\right) F'\left(K[2]^{3/2} - \frac{3e^{K[1]}}{2}\right)}{2\left(F\left(K[2]^{3/2} - \frac{3e^{K[1]}}{2}\right) - 1\right)^2} - \frac{3e^{K[1]}}{2} \right) \right] \right]$$

**Maple:** cpu = 0.265 (sec), leaf count = 35

$$\left\{ \int_{-b}^{y(x)} 1\sqrt{-a} \left( F\left(-a^{\frac{3}{2}} - \frac{3e^x}{2}\right) - 1 \right)^{-1} d_a - e^x - \_C1 = 0 \right\}$$

**2.594 ODE No. 594**

$$\frac{d}{dx}y(x) = \frac{x}{y(x)} F\left(-\frac{(y(x))^2 + b}{x^2}\right) = 0$$

**Mathematica:** cpu = 17.877770 (sec), leaf count = 233

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x \left( \frac{K[1]F\left(\frac{K[2]^2-b}{K[1]^2}\right) \left( 2K[2]F'\left(\frac{K[2]^2-b}{K[1]^2}\right) - 2K[2] \right)}{\left( K[1]^2F\left(\frac{K[2]^2-b}{K[1]^2}\right) - K[2]^2 + b \right)^2} - \frac{2K[2]F'\left(\frac{K[2]^2-b}{K[1]^2}\right)}{K[1] \left( K[1]^2F\left(\frac{K[2]^2-b}{K[1]^2}\right) - K[2]^2 \right)} \right) \right] \right]$$

**Maple:** cpu = 0.140 (sec), leaf count = 67

$$\left\{ y(x) = \sqrt{\text{RootOf}\left(-2 \ln(x) + \int^{-Z} (F(-a) - a)^{-1} d_a + 2\_C1\right) x^2 + b}, y(x) = -\sqrt{\text{RootOf}\left(-2 \ln(x) + \int^{-Z} (F(-a) - a)^{-1} d_a + 2\_C1\right) x^2 + b} \right\}$$

**2.595 ODE No. 595**

$$\frac{d}{dx}y(x) = \frac{1}{x^2y(x)}F\left(\frac{x(y(x))^2 + 1}{x}\right) = 0$$

**Mathematica:** cpu = 19.349457 (sec), leaf count = 201

$$\text{Solve} \left[ \int_1^{y(x)} \left( \frac{K[2]}{2F\left(\frac{xK[2]^2+1}{x}\right) - 1} - \int_1^x \left( \frac{4K[2]F\left(\frac{K[1]K[2]^2+1}{K[1]}\right) F'\left(\frac{K[1]K[2]^2+1}{K[1]}\right)}{K[1]^2 \left(2F\left(\frac{K[1]K[2]^2+1}{K[1]}\right) - 1\right)^2} - \frac{2K[2]F'\left(\frac{K[1]K[2]^2+1}{K[1]}\right)}{K[1]^2 \left(2F\left(\frac{K[1]K[2]^2+1}{K[1]}\right) - 1\right)} \right) dx \right]$$

**Maple:** cpu = 0.124 (sec), leaf count = 72

$$\left\{ y(x) = \frac{1}{x} \sqrt{x \left( \text{RootOf} \left( \int^{-Z} (-1 + 2F(_a))^{-1} d_a x + \_C1 x + 1 \right) x - 1 \right)}, y(x) = -\frac{1}{x} \sqrt{x \left( \text{RootOf} \left( \int^{-Z} (-1 + 2F(_a))^{-1} d_a x + \_C1 x + 1 \right) x - 1 \right)} \right\}$$

**2.596 ODE No. 596**

$$\frac{d}{dx}y(x) = \frac{-2x^2 + x + F(y(x) + x^2 - x)}{x} = 0$$

**Mathematica:** cpu = 49.763319 (sec), leaf count = 153

$$\text{Solve} \left[ \int_1^{y(x)} \frac{F(K[2] + x^2 - x) \int_1^x \left( \frac{2K[1]F'(K[1]^2 - K[1] + K[2])}{F(K[1]^2 - K[1] + K[2])^2} - \frac{F'(K[1]^2 - K[1] + K[2])}{F(K[1]^2 - K[1] + K[2])^2} \right) dK[1] + 1}{F(K[2] + x^2 - x)} dK[2] + \int_1^x \dots \right]$$

**Maple:** cpu = 0.093 (sec), leaf count = 26

$$\left\{ y(x) = -x^2 + \text{RootOf} \left( -\ln(x) + \int^{-Z} (F(_a))^{-1} d_a + \_C1 \right) + x \right\}$$

**2.597 ODE No. 597**

$$\frac{d}{dx}y(x) = 2 \frac{a}{x^2} \left( -y(x) + 2F\left(\frac{x(y(x))^2 - 4a}{x}\right)a \right)^{-1} = 0$$

**Mathematica:** cpu = 27.163949 (sec), leaf count = 127

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x \frac{2K[2]F' \left( \frac{K[1]K[2]^2 - 4a}{K[1]} \right)}{K[1]^2 F \left( \frac{K[1]K[2]^2 - 4a}{K[1]} \right)^2} dK[1] - \frac{K[2]}{2aF \left( \frac{xK[2]^2 - 4a}{x} \right)} + 1 \right) dK[2] + \int_1^x - \frac{1}{K[1]^2 F \left( \frac{y(x)}{K[1]} \right)} \right]$$

**Maple:** cpu = 0.296 (sec), leaf count = 37

$$\left\{ -\frac{y(x)}{2a} + \frac{1}{8a^2} \int^{(y(x))^2 - 4\frac{a}{x}} (F(-a))^{-1} d_a - C1 = 0 \right\}$$

## 2.598 ODE No. 598

$$\frac{d}{dx} y(x) = \frac{1}{x-1} \left( y(x) + F \left( \frac{y(x)}{x} \right) \right) = 0$$

**Mathematica:** cpu = 0.077010 (sec), leaf count = 36

$$\text{Solve} \left[ \int_1^{\frac{y(x)}{x}} \frac{1}{F(K[1]) + K[1]} dK[1] = c_1 + \log(1-x) - \log(x), y(x) \right]$$

**Maple:** cpu = 0.032 (sec), leaf count = 29

$$\left\{ y(x) = \text{RootOf} \left( - \int^{-Z} (F(-a) + a)^{-1} d_a - \ln(x) + \ln(x-1) + C1 \right) x \right\}$$

## 2.599 ODE No. 599

$$\frac{d}{dx} y(x) = \frac{-x + F((y(x))^2 + x^2)}{y(x)} = 0$$

**Mathematica:** cpu = 22.629374 (sec), leaf count = 92

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x \frac{2K[1]K[2]F'(K[1]^2 + K[2]^2)}{F(K[1]^2 + K[2]^2)^2} dK[1] - \frac{K[2]}{F(K[2]^2 + x^2)} \right) dK[2] + \int_1^x \left( 1 - \frac{K[1]}{F(K[1]^2 + x^2)} \right) dK[1] \right]$$

**Maple:** cpu = 0.093 (sec), leaf count = 57

$$\left\{ y(x) = \sqrt{-x^2 + \text{RootOf} \left( -2x + \int^{-Z} (F(-a))^{-1} d_a + 2C1 \right)}, y(x) = -\sqrt{-x^2 + \text{RootOf} \left( -2x + \int^{-Z} (F(-a))^{-1} d_a + 2C1 \right)} \right\}$$

**2.600 ODE No. 600**

$$\frac{d}{dx}y(x) = \frac{(y(x))^2}{x} F\left(-\frac{2y(x)\ln(x)-1}{y(x)}\right) = 0$$

**Mathematica:** cpu = 24.086559 (sec), leaf count = 243

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x \left( \frac{2\left(-\frac{2\log(K[1])}{K[2]} - \frac{1-2K[2]\log(K[1])}{K[2]^2}\right) F'\left(\frac{1-2K[2]\log(K[1])}{K[2]}\right)}{K[1] \left(F\left(\frac{1-2K[2]\log(K[1])}{K[2]}\right) + 2\right)} - \frac{2\left(-\frac{2\log(K[1])}{K[2]} - \frac{1-2K[2]\log(K[1])}{K[2]^2}\right)}{K[1] \left(F\left(\frac{1-2K[2]\log(K[1])}{K[2]}\right) + 2\right)} \right) dK[1] \right]$$

**Maple:** cpu = 0.141 (sec), leaf count = 38

$$\left\{ \int_{-b}^{y(x)} \frac{1}{-a^2} \left( F\left(\frac{-2-a\ln(x)+1}{-a}\right) + 2 \right)^{-1} d_a - \ln(x) - C1 = 0 \right\}$$

**2.601 ODE No. 601**

$$\frac{d}{dx}y(x) = \frac{F(-(x-y(x))(y(x)+x))x}{y(x)} = 0$$

**Mathematica:** cpu = 32.152083 (sec), leaf count = 179

$$\text{Solve} \left[ \int_1^{y(x)} \left( \frac{K[2]}{F((K[2]-x)(K[2]+x))-1} - \int_1^x \left( \frac{2K[1]K[2]F((K[2]-K[1])(K[1]+K[2]))F'((K[2]-K[1])(K[1]+K[2]))}{(F((K[2]-K[1])(K[1]+K[2]))-1)^2} \right) dK[1] \right) dK[2] \right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 61

$$\left\{ y(x) = \sqrt{x^2 + \text{RootOf}\left(-x^2 + \int^{-Z} (F(-a) - 1)^{-1} d_a + 2_C1\right)}, y(x) = -\sqrt{x^2 + \text{RootOf}\left(-x^2 + \int^{-Z} (F(-a) - 1)^{-1} d_a + 2_C1\right)} \right\}$$

**2.602 ODE No. 602**

$$\frac{d}{dx}y(x) = \frac{(y(x))^2}{x^3} \left( 2 + F\left(\frac{x^2-y(x)}{x^2y(x)}\right)x^2 \right) = 0$$

**Mathematica:** cpu = 46.096854 (sec), leaf count = 164

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x \frac{2\left(-\frac{K[1]^2-K[2]}{K[1]^2K[2]^2} - \frac{1}{K[1]^2K[2]}\right) F'\left(\frac{K[1]^2-K[2]}{K[1]^2K[2]}\right)}{K[1]^3 F\left(\frac{K[1]^2-K[2]}{K[1]^2K[2]}\right)^2} dK[1] - \frac{1}{K[2]^2 F\left(\frac{x^2-K[2]}{x^2K[2]}\right)} \right) dK[2] + \int_1^x \frac{1}{K[2]^2 F\left(\frac{x^2-K[2]}{x^2K[2]}\right)} dK[2] \right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 33

$$\left\{ y(x) = \frac{x^2}{\text{RootOf}\left(-\ln(x) - \int^{-Z} (F(-a))^{-1} d_a + \_C1\right) x^2 + 1} \right\}$$

### 2.603 ODE No. 603

$$\frac{d}{dx} y(x) = \frac{2 F(y(x) + \ln(2x + 1)) x + F(y(x) + \ln(2x + 1)) - 2}{2x + 1} = 0$$

**Mathematica:** cpu = 17.469218 (sec), leaf count = 114

$$\text{Solve} \left[ \int_1^{y(x)} - \frac{F(K[2] + \log(2x + 1)) \int_1^x - \frac{2F'(K[2] + \log(2K[1] + 1))}{(2K[1] + 1)F(K[2] + \log(2K[1] + 1))^2} dK[1] - 1}{F(K[2] + \log(2x + 1))} dK[2] + \int_1^x \left( \frac{1}{(2K[1] + 1)} \right) dK[1] \right]$$

**Maple:** cpu = 0.124 (sec), leaf count = 27

$$\left\{ y(x) = -\ln(2x + 1) + \text{RootOf}\left(-x + \int^{-Z} (F(-a))^{-1} d_a + \_C1\right) \right\}$$

### 2.604 ODE No. 604

$$\frac{d}{dx} y(x) = 2 (y(x))^3 \left( 1 + 2 F\left(\frac{1 + 4x(y(x))^2}{(y(x))^2}\right) y(x) \right)^{-1} = 0$$

**Mathematica:** cpu = 26.277337 (sec), leaf count = 140

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x \frac{\left( \frac{8K[1]}{K[2]} - \frac{2(4K[1]K[2]^2 + 1)}{K[2]^3} \right) F'\left(\frac{4K[1]K[2]^2 + 1}{K[2]^2}\right)}{F\left(\frac{4K[1]K[2]^2 + 1}{K[2]^2}\right)^2} dK[1] + \frac{1}{2K[2]^3 F\left(\frac{4xK[2]^2 + 1}{K[2]^2}\right)} + \frac{1}{K[2]^2} \right) dK[2] \right]$$

**Maple:** cpu = 0.141 (sec), leaf count = 30

$$\left\{ -\_C1 - (y(x))^{-1} - \frac{\int^{4x+(y(x))^{-2}} (F(-a))^{-1} d_a}{4} = 0 \right\}$$

**2.605 ODE No. 605**

$$\frac{d}{dx}y(x) = -1/4 \frac{(y(x))^2}{x} \left( 2x - F\left(-1/2 \frac{xy(x) - 2}{y(x)}\right) \right) = 0$$

**Mathematica:** cpu = 28.541624 (sec), leaf count = 142

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x \frac{2 \left( -\frac{K[1]}{2K[2]} - \frac{1-\frac{1}{2}K[1]K[2]}{K[2]^2} \right) F' \left( \frac{1-\frac{1}{2}K[1]K[2]}{K[2]} \right)}{F \left( \frac{1-\frac{1}{2}K[1]K[2]}{K[2]} \right)^2} dK[1] - \frac{4}{K[2]^2 F \left( \frac{1-\frac{1}{2}xK[2]}{K[2]} \right)} \right) dK[2] + \int_1^x \dots \right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 29

$$\left\{ y(x) = 2 \left( 2 \text{RootOf} \left( -\ln(x) - 4 \int^{-Z} (F(_a))^{-1} d_a + _C1 \right) + x \right)^{-1} \right\}$$

**2.606 ODE No. 606**

$$\frac{d}{dx}y(x) = - \left( -e^{-x^2} + x^2 e^{-x^2} - F\left(y(x) - 1/2 x^2 e^{-x^2}\right) \right) x = 0$$

**Mathematica:** cpu = 64.106640 (sec), leaf count = 358

$$\text{Solve} \left[ \int_1^{y(x)} \frac{F \left( K[2] - \frac{1}{2} e^{-x^2} x^2 \right) \int_1^x \left( \frac{e^{-K[1]^2} K[1]^3 F' \left( K[2] - \frac{1}{2} e^{-K[1]^2} K[1]^2 \right)}{F \left( K[2] - \frac{1}{2} e^{-K[1]^2} K[1]^2 \right)^2} - \frac{e^{-K[1]^2} K[1] \left( e^{K[1]^2} F \left( K[2] - \frac{1}{2} e^{-K[1]^2} K[1]^2 \right) \right)}{F \left( K[2] - \frac{1}{2} e^{-K[1]^2} K[1]^2 \right)} \right) dK[1]}{F \left( K[2] - \frac{1}{2} e^{-x^2} x^2 \right)} \right]$$

**Maple:** cpu = 0.655 (sec), leaf count = 34

$$\left\{ y(x) = \frac{x^2 e^{-x^2}}{2} + \text{RootOf} \left( x^2 - 2 \int^{-Z} (F(_a))^{-1} d_a + 2 _C1 \right) \right\}$$

**2.607 ODE No. 607**

$$\frac{d}{dx}y(x) = \frac{1}{x} \left( 2y(x) + F\left(\frac{y(x)}{x^2}\right) x^3 \right) = 0$$

**Mathematica:** cpu = 739.416394 (sec), leaf count = 118

$$\text{Solve} \left[ \int_1^{y(x)} \frac{x^2 F\left(\frac{K[2]}{x^2}\right) \left( \int_1^x \left( \frac{2}{K[1]^3 F\left(\frac{K[2]}{K[1]^2}\right)} - \frac{2K[2]F'\left(\frac{K[2]}{K[1]^2}\right)}{K[1]^5 F\left(\frac{K[2]}{K[1]^2}\right)^2} \right) dK[1] \right) + 1}{x^2 F\left(\frac{K[2]}{x^2}\right)} dK[2] + \int_1^x \left( \frac{2y(x)}{K[1]^3 F\left(\frac{y(x)}{K[1]^2}\right)} \right) \right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 22

$$\left\{ y(x) = \text{RootOf} \left( -x + \int^{-Z} (F(_a))^{-1} d_a + _C1 \right) x^2 \right\}$$

**2.608 ODE No. 608**

$$\frac{d}{dx}y(x) = \sqrt{y(x)} \left( \sqrt{y(x)} + F\left(\frac{x-y(x)}{\sqrt{y(x)}}\right) \right)^{-1} = 0$$

**Mathematica:** cpu = 284.310103 (sec), leaf count = 271

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x \frac{-2 \left( -\frac{K[1]-K[2]}{2K[2]^{3/2}} - \frac{1}{\sqrt{K[2]}} \right) \sqrt{K[2]} F'\left(\frac{K[1]-K[2]}{\sqrt{K[2]}}\right) - \frac{F\left(\frac{K[1]-K[2]}{\sqrt{K[2]}}\right)}{\sqrt{K[2]}} - 1}{\left( -2\sqrt{K[2]} F\left(\frac{K[1]-K[2]}{\sqrt{K[2]}}\right) + K[1] - K[2] \right)^2} dK[1] - \frac{F\left(\frac{x-K[1]}{\sqrt{K[2]}}\right)}{x\sqrt{K[2]}} \right) \right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 40

$$\left\{ \frac{\ln(y(x))}{2} - \int^{x \frac{1}{\sqrt{y(x)}} - \sqrt{y(x)}} (2F(_a) - _a)^{-1} d_a - _C1 = 0 \right\}$$



**2.609 ODE No. 609**

$$\frac{d}{dx}y(x) = \frac{-3x^2y(x) + F(x^3y(x))}{x^3} = 0$$

**Mathematica:** cpu = 51.408028 (sec), leaf count = 114

$$\text{Solve} \left[ \int_1^{y(x)} - \frac{F(x^3K[2]) \int_1^x \left( \frac{3K[1]^5K[2]F'(K[1]^3K[2])}{F(K[1]^3K[2])^2} - \frac{3K[1]^2}{F(K[1]^3K[2])} \right) dK[1] + x^3}{F(x^3K[2])} dK[2] + \int_1^x \left( 1 - \frac{3y(x)K}{F(y(x)K)} \right) dK[2] \right]$$

**Maple:** cpu = 0.140 (sec), leaf count = 22

$$\left\{ y(x) = \frac{\text{RootOf} \left( x - \int^{-Z} (F(_a))^{-1} d_a + _C1 \right)}{x^3} \right\}$$

**2.610 ODE No. 610**

$$\frac{d}{dx}y(x) = \frac{1}{x} \left( y(x) + F\left(\frac{y(x)}{x}\right) x^2 \right) = 0$$

**Mathematica:** cpu = 0.062508 (sec), leaf count = 24

$$\text{Solve} \left[ \int_1^{\frac{y(x)}{x}} \frac{1}{F(K[1])} dK[1] = c_1 + x, y(x) \right]$$

**Maple:** cpu = 0.016 (sec), leaf count = 20

$$\left\{ y(x) = \text{RootOf} \left( x - \int^{-Z} (F(_a))^{-1} d_a + _C1 \right) x \right\}$$

**2.611 ODE No. 611**

$$\frac{d}{dx}y(x) = \frac{-2x - y(x) + F(x(y(x) + x))}{x} = 0$$

**Mathematica:** cpu = 39.069461 (sec), leaf count = 188

$$\text{Solve} \left[ \int_1^{y(x)} - \frac{F(x(K[2] + x)) \int_1^x \left( \frac{2K[1]^2F'(K[1](K[1]+K[2]))}{F(K[1](K[1]+K[2]))^2} + \frac{K[1](K[2]-F(K[1](K[1]+K[2])))F'(K[1](K[1]+K[2]))}{F(K[1](K[1]+K[2]))^2} \right) dK[1] - 1}{F(x(K[2] + x))} dK[2] \right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 28

$$\left\{ y(x) = \frac{-x^2 + \text{RootOf}\left(-x + \int^{-Z} (F(_a))^{-1} d_a + \_C1\right)}{x} \right\}$$

## 2.612 ODE No. 612

$$\frac{d}{dx}y(x) = 1/2 \left( y(x) e^{-1/4x^2} x + 2 F\left(y(x) e^{-1/4x^2}\right) \right) e^{1/4x^2} = 0$$

**Mathematica:** cpu = 49.253254 (sec), leaf count = 196

$$\text{Solve} \left[ \int_1^{y(x)} \frac{e^{-\frac{x^2}{4}} \left( e^{\frac{x^2}{4}} F\left(e^{-\frac{x^2}{4}} K[2]\right) \int_1^x \left( \frac{e^{-\frac{1}{4}K[1]^2} K[1]}{2F\left(e^{-\frac{1}{4}K[1]^2} K[2]\right)} - \frac{e^{-\frac{1}{2}K[1]^2} K[1]K[2]F'\left(e^{-\frac{1}{4}K[1]^2} K[2]\right)}{2F\left(e^{-\frac{1}{4}K[1]^2} K[2]\right)^2} \right) dK[1] + 1}{F\left(e^{-\frac{x^2}{4}} K[2]\right)} \right]$$

**Maple:** cpu = 0.110 (sec), leaf count = 27

$$\left\{ y(x) = \text{RootOf}\left(-x + \int^{-Z} (F(_a))^{-1} d_a + \_C1\right) \left(e^{-\frac{x^2}{4}}\right)^{-1} \right\}$$

## 2.613 ODE No. 613

$$\frac{d}{dx}y(x) = \frac{1}{x} \left( x + y(x) + F\left(-\frac{y(x) + x \ln(x)}{x}\right) x^2 \right) = 0$$

**Mathematica:** cpu = 818.937492 (sec), leaf count = 223

$$\text{Solve} \left[ \int_1^{y(x)} \frac{x F\left(\frac{K[2]-x \log(x)}{x}\right) \int_1^x \left( -\frac{K[2]F'\left(\frac{K[2]-K[1] \log(K[1])}{K[1]}\right)}{K[1]^3 F\left(\frac{K[2]-K[1] \log(K[1])}{K[1]}\right)^2} - \frac{F'\left(\frac{K[2]-K[1] \log(K[1])}{K[1]}\right)}{K[1]^2 F\left(\frac{K[2]-K[1] \log(K[1])}{K[1]}\right)^2} + \frac{1}{K[1]^2 F\left(\frac{K[2]-K[1] \log(K[1])}{K[1]}\right)} \right)}{x F\left(\frac{K[2]-x \log(x)}{x}\right)} \right]$$

**Maple:** cpu = 0.093 (sec), leaf count = 23

$$\left\{ y(x) = \left( \ln(x) + \text{RootOf}\left(-x + \int^{-Z} (F(_a))^{-1} d_a + \_C1\right) \right) x \right\}$$

**2.614 ODE No. 614**

$$\frac{d}{dx}y(x) = \frac{x(a-1)(a+1)}{y(x) + F(1/2(y(x))^2 - 1/2a^2x^2 + 1/2x^2)a^2 - F(1/2(y(x))^2 - 1/2a^2x^2 + 1/2x^2)} = 0$$

**Mathematica:** cpu = 72.937762 (sec), leaf count = 171

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x \frac{K[1]K[2]F'(-\frac{1}{2}a^2K[1]^2 + \frac{K[1]^2}{2} + \frac{K[2]^2}{2})}{F(-\frac{1}{2}a^2K[1]^2 + \frac{K[1]^2}{2} + \frac{K[2]^2}{2})^2} dK[1] + \frac{K[2]}{(a^2-1)F(\frac{K[2]^2}{2} - \frac{1}{2}a^2x^2 + \frac{x^2}{2})} \right) \right]$$

**Maple:** cpu = 0.328 (sec), leaf count = 59

$$\left\{ \frac{y(x)}{(a-1)(a+1)} + \frac{1}{2a^4 - 4a^2 + 2} \int^{-a^2x^2 + x^2 + (y(x))^2} \left( F\left(\frac{-a}{2}\right) \right)^{-1} d_a - C1 = 0 \right\}$$

**2.615 ODE No. 615**

$$\frac{d}{dx}y(x) = \frac{y(x)}{x(-1 + F(xy(x))y(x))} = 0$$

**Mathematica:** cpu = 17.029162 (sec), leaf count = 74

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x \frac{F'(K[1]K[2])}{F(K[1]K[2])^2} dK[1] - \frac{1}{K[2]F(xK[2])} + 1 \right) dK[2] + \int_1^x - \frac{1}{K[1]F(y(x)K[1])} dK[1] \right]$$

**Maple:** cpu = 0.109 (sec), leaf count = 26

$$\left\{ -y(x) + \int^{xy(x)} \frac{1}{F(-a)-a} d_a - C1 = 0 \right\}$$

**2.616 ODE No. 616**

$$\frac{d}{dx}y(x) = - \frac{-x^2 + 2x^3y(x) - F((xy(x) - 1)x)}{x^4} = 0$$

**Mathematica:** cpu = 52.212630 (sec), leaf count = 174

$$\text{Solve} \left[ \int_1^{y(x)} - \frac{F(x(xK[2] - 1)) \int_1^x \left( \frac{2K[2]K[1]^3F'(K[1](K[1]K[2]-1))}{F(K[1](K[1]K[2]-1))^2} - \frac{K[1]^2F'(K[1](K[1]K[2]-1))}{F(K[1](K[1]K[2]-1))^2} - \frac{2K[1]}{F(K[1](K[1]K[2]-1))} \right)}{F(x(xK[2] - 1))} \right]$$

Maple: cpu = 0.093 (sec), leaf count = 26

$$\left\{ y(x) = \frac{\text{RootOf}\left(\int^{-Z}(F(_a))^{-1} d_a x + _C1 x + 1\right) + x}{x^2} \right\}$$

## 2.617 ODE No. 617

$$\frac{d}{dx}y(x) = 1/9 \frac{x(y(x))^2 e^{3x^2}}{e^{9/2x^2}} F\left(1/3 \frac{(3+y(x))e^{3/2x^2}}{y(x)}\right) = 0$$

Mathematica: cpu = 67.610585 (sec), leaf count = 612

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x \left( \frac{K[2] \left( \frac{e^{\frac{3K[1]^2}{2}}}{3K[2]} - \frac{e^{\frac{3K[1]^2}{2}}(K[2]+3)}{3K[2]^2} \right) K[1]F' \left( \frac{e^{\frac{3K[1]^2}{2}}(K[2]+3)}{3K[2]} \right)}{K[2]F \left( \frac{e^{\frac{3K[1]^2}{2}}(K[2]+3)}{3K[2]} \right) - 9e^{\frac{3K[1]^2}{2}} K[2] - 27e^{\frac{3K[1]^2}{2}}} \right) + \frac{K[2]K[1]F \left( \frac{e^{\frac{3K[1]^2}{2}}(K[2]+3)}{3K[2]} \right)}{K[2]F \left( \frac{e^{\frac{3K[1]^2}{2}}(K[2]+3)}{3K[2]} \right) - 9e^{\frac{3K[1]^2}{2}} K[2] - 27e^{\frac{3K[1]^2}{2}}} \right) \right]$$

Maple: cpu = 0.234 (sec), leaf count = 47

$$\left\{ y(x) = -3 \frac{e^{3/2x^2}}{e^{3/2x^2} - 3 \text{RootOf}\left(-x^2 - 18 \int^{-Z}(F(_a) - 27_a)^{-1} d_a + 2_C1\right)} \right\}$$

## 2.618 ODE No. 618

$$\frac{d}{dx}y(x) = \frac{(1+y(x))((y(x) - \ln(1+y(x)) - \ln(x))x + 1)}{xy(x)} = 0$$

Mathematica: cpu = 0.103513 (sec), leaf count = 25

$$\left\{ \left\{ y(x) \rightarrow -W\left(-\frac{e^{c_1 e^x - 1}}{x}\right) - 1 \right\} \right\}$$

Maple: cpu = 0.312 (sec), leaf count = 34

$$\left\{ y(x) = \frac{1}{x} \left( e^{-\text{lambertW}\left(-\frac{e^{e^x - C1 - 1}}{x}\right) + e^x - C1 - 1} - x \right) \right\}$$

**2.619 ODE No. 619**

$$\frac{d}{dx}y(x) = 6 \frac{y(x)}{8 (y(x))^4 + 9 (y(x))^3 + 12 (y(x))^2 + 6 y(x) - F(-1/3 (y(x))^4 - 1/2 (y(x))^3 - (y(x))^2 -$$

**Mathematica:** cpu = 60.581193 (sec), leaf count = 327

$$\text{Solve} \left[ \int_1^{y(x)} \left( \frac{F\left(-\frac{1}{3}K[2]^4 - \frac{K[2]^3}{2} - K[2]^2 - K[2] + x\right) \int_1^x - \frac{6\left(-\frac{4}{3}K[2]^3 - \frac{3K[2]^2}{2} - 2K[2] - 1\right) F'\left(-\frac{1}{3}K[2]^4 - \frac{K[2]^3}{2} - K[2]^2 - K[2] + x\right)}{F\left(-\frac{1}{3}K[2]^4 - \frac{K[2]^3}{2} - K[2]^2 - K[2] + x\right)} dx \right) \right]$$

**Maple:** cpu = 0.359 (sec), leaf count = 81

$$\left\{ \int_{-b}^{y(x)} \frac{1}{-a} \left( -8_a^4 - 9_a^3 - 12_a^2 + F\left(-\frac{a^4}{3} - \frac{a^3}{2} - a^2 - a + x\right) - 6_a \right) \left( F\left(-\frac{a^4}{3} - \frac{a^3}{2} - a^2 - a + x\right) \right) dx \right\}$$

**2.620 ODE No. 620**

$$\frac{d}{dx}y(x) = \frac{(y(x))^2 + 2xy(x) + x^2 + e^{2F(-(x-y(x))(y(x)+x))}}{(y(x))^2 + 2xy(x) + x^2 - e^{2F(-(x-y(x))(y(x)+x))}} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.156 (sec), leaf count = 37

$$\left\{ y(x) = e^{\text{RootOf}\left(-_Z + \int (e^{-Z})^2 - 2_x e^{-Z} (e^{2F(-a)+_a})^{-1} d_{-a} +_{-C1}\right)} - x \right\}$$

**2.621 ODE No. 621**

$$\frac{d}{dx}y(x) = (y(x) + \sqrt{x})^{-1} = 0$$

**Mathematica:** cpu = 0.098513 (sec), leaf count = 445

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{\text{Root}\left[\#1^6 (16e^{12c_1} + 16x^3) - 24\#1^4 x^2 + 8\#1^3 x^{3/2} + 9\#1^2 x - 6\#1\sqrt{x} + 1\&, 1\right]} - \sqrt{x} \right\}, \left\{ y \right\} \right\}$$

**Maple:** cpu = 0.234 (sec), leaf count = 59

$$\left\{ y(x) = 1 \left( \sqrt{x} (\text{RootOf}(-Z^{18} - C1 - 9xZ^6 - 6\sqrt{x}Z^3 - 1))^3 + 1 \right) (\text{RootOf}(-Z^{18} - C1 - 9xZ^6 - 6\sqrt{x}Z^3 - 1)) \right\}$$

## 2.622 ODE No. 622

$$\boxed{\frac{d}{dx}y(x) = \left( y(x) + 2 + \sqrt{3x+1} \right)^{-1} = 0}$$

**Mathematica:** cpu = 0.449057 (sec), leaf count = 134

$$\text{Solve} \left[ 44c_1 + 6\sqrt{33} \tanh^{-1} \left( \frac{3y(x) + 7\sqrt{3x+1} + 6}{\sqrt{33} (y(x) + \sqrt{3x+1} + 2)} \right) = 33 \left( \log \left( \left( y(x) + \sqrt{3x+1} + 2 \right)^2 \left( \frac{1}{y(x) + \sqrt{3x+1} + 2} \right) \right) \right) \right]$$

**Maple:** cpu = 0.172 (sec), leaf count = 83

$$\left\{ \ln \left( 3\sqrt{3x+1}y(x) + 3(y(x))^2 + 6\sqrt{3x+1} - 6x + 12y(x) + 10 \right) - 6 \frac{\sqrt{3x+1}}{\sqrt{99x+33}} \text{Artanh} \left( \frac{3\sqrt{3x+1}}{\sqrt{99x+33}} \right) \right\}$$

## 2.623 ODE No. 623

$$\boxed{\frac{d}{dx}y(x) = \frac{x^2}{y(x) + x^{3/2}} = 0}$$

**Mathematica:** cpu = 0.176522 (sec), leaf count = 77

$$\text{Solve} \left[ 44c_1 + 6\sqrt{33} \tanh^{-1} \left( \frac{7x^{3/2} + 3y(x)}{\sqrt{33} (x^{3/2} + y(x))} \right) = 33 \left( \log \left( -\frac{3y(x)}{2x^{3/2}} - \frac{3y(x)^2}{2x^3} + 1 \right) + 3 \log(x) \right), y(x) \right]$$

**Maple:** cpu = 0.172 (sec), leaf count = 51

$$\left\{ \ln \left( 3x^{3/2}y(x) - 2x^3 + 3(y(x))^2 \right) - \frac{2\sqrt{33}}{11} \text{Artanh} \left( \frac{\sqrt{33}}{33} (3x^{3/2} + 6y(x)) x^{-3/2} \right) - C1 = 0 \right\}$$

**2.624 ODE No. 624**

$$\frac{d}{dx}y(x) = \frac{x^{5/3}}{y(x) + x^{4/3}} = 0$$

**Mathematica:** cpu = 0.951621 (sec), leaf count = 9837

**Maple:** cpu = 0.858 (sec), leaf count = 46

$$\left\{ y(x) = \frac{1}{2} \left( \text{RootOf}(-Z^{192} + 12x^{4/3}Z^{176} + 48x^{8/3}Z^{160} + 64x^4Z^{144} - C1) \right)^{16} + \frac{1}{2}x^{4/3} \right\}$$

**2.625 ODE No. 625**

$$\frac{d}{dx}y(x) = i/2x^2 \left( i - 2\sqrt{-x^3 + 6y(x)} \right) = 0$$

**Mathematica:** cpu = 0.209527 (sec), leaf count = 76

$$\text{Solve} \left[ -y(x) + \frac{1}{12} \left( 2i\sqrt{6y(x) - x^3} - \log(-x^3 + 6y(x) + 1) - 2i \tan^{-1} \left( \sqrt{6y(x) - x^3} \right) - 2x^3 + 12y(x) \right) \right]$$

**Maple:** cpu = 0.156 (sec), leaf count = 53

$$\left\{ -2i\sqrt{-x^3 + 6y(x)} + 2i \arctan \left( \sqrt{-x^3 + 6y(x)} \right) + \ln(x^3 - 6y(x) - 1) + 2x^3 - C1 = 0 \right\}$$

**2.626 ODE No. 626**

$$\frac{d}{dx}y(x) = \frac{x}{y(x) + \sqrt{x^2 + 1}} = 0$$

**Mathematica:** cpu = 0.195525 (sec), leaf count = 104

$$\text{Solve} \left[ \frac{1}{2} \left( \log \left( \frac{-\sqrt{x^2 + 1}y(x)^2 - (x^2 + 1)y(x) + (x^2 + 1)^{3/2}}{(x^2 + 1)^{3/2}} \right) + \log(x^2 + 1) \right) = c_1 + \frac{\tanh^{-1} \left( \frac{3\sqrt{x^2 + 1}}{\sqrt{5}(\sqrt{x^2 + 1} + 1)} \right)}{\sqrt{5}} \right]$$

**Maple:** cpu = 0.359 (sec), leaf count = 112

$$\left\{ -\frac{4}{3} \ln \left( 36 \frac{\sqrt{x^2 + 1}}{y(x) + \sqrt{x^2 + 1}} \right) + \frac{2}{3} \ln \left( -\frac{1296}{11} (y(x) \sqrt{x^2 + 1} - x^2 + (y(x))^2 - 1) (y(x) + \sqrt{x^2 + 1})^{-2} \right) \right\}$$

**2.627 ODE No. 627**

$$\frac{d}{dx}y(x) = \frac{(-1 + y(x) \ln(x))^2}{x} = 0$$

**Mathematica:** cpu = 0.753596 (sec), leaf count = 25

$$\left\{ \left\{ y(x) \rightarrow \frac{\tan(c_1 + \log(x))}{\log(x) \tan(c_1 + \log(x)) + 1} \right\} \right\}$$

**Maple:** cpu = 0.141 (sec), leaf count = 39

$$\left\{ y(x) = \frac{\sin(\ln(x)) \_C1 + \cos(\ln(x))}{(\sin(\ln(x)) \_C1 + \cos(\ln(x))) \ln(x) + \cos(\ln(x)) \_C1 - \sin(\ln(x))} \right\}$$

**2.628 ODE No. 628**

$$\frac{d}{dx}y(x) = 1/3 x (-2 + 3 \sqrt{x^2 + 3 y(x)}) = 0$$

**Mathematica:** cpu = 0.085511 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{48} (-54c_1x^2 + 81c_1^2 + 9x^4 - 16x^2) \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 23

$$\left\{ -C1 + \frac{3x^2}{4} + \frac{2}{3} - \sqrt{x^2 + 3y(x)} = 0 \right\}$$



**2.629 ODE No. 629**

$$\frac{d}{dx}y(x) = \frac{(2y(x)\ln(x) - 1)^2}{x} = 0$$

**Mathematica:** cpu = 0.780599 (sec), leaf count = 47

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{\sqrt{2}(\sqrt{2}\log(x) - \tan(\frac{1}{2}(\sqrt{2}c_1 + 2\sqrt{2}\log(x))))} \right\} \right\}$$

**Maple:** cpu = 0.172 (sec), leaf count = 72

$$\left\{ y(x) = \frac{\sin(\sqrt{2}\ln(x)) - C1 + \cos(\sqrt{2}\ln(x))}{(2\sin(\sqrt{2}\ln(x)) - C1 + 2\cos(\sqrt{2}\ln(x)))\ln(x) + \sqrt{2}\cos(\sqrt{2}\ln(x)) - C1 - \sqrt{2}\sin(\sqrt{2}\ln(x))} \right\}$$

**2.630 ODE No. 630**

$$\frac{d}{dx}y(x) = \frac{e^{bx}}{y(x)e^{-bx} + 1} = 0$$

**Mathematica:** cpu = 0.566572 (sec), leaf count = 101

$$\text{Solve} \left[ \frac{1}{2}b(\log(-be^{-2bx}y(x)^2 - be^{-bx}y(x) + 1) + 2bx) = \frac{b \tan^{-1}\left(\frac{(b+2)(-e^{bx}) - by(x)}{b\sqrt{-\frac{b+4}{b}}(e^{bx} + y(x))}\right)}{\sqrt{-\frac{b+4}{b}}} + c_1, y(x) \right]$$

**Maple:** cpu = 0.249 (sec), leaf count = 98

$$\left\{ y(x) = \frac{1}{e^{-bx}} \text{RootOf} \left( -e^{\text{RootOf} \left( \left( \tanh \left( \frac{2 - C1 b - 2bx - Z \sqrt{b^2 + 4b}}{2b} \right) \right)^2 b + 4 \left( \tanh \left( \frac{1}{2} \frac{\sqrt{b^2 + 4b} (2 - C1 b - 2bx - Z)}{b} \right) \right)^2 - 4 e^{-Z - b - 4} \right)} \right)$$

**2.631 ODE No. 631**

$$\frac{d}{dx}y(x) = 1/2 x^2 (1 + 2 \sqrt{x^3 - 6y(x)}) = 0$$

**Mathematica:** cpu = 0.096512 (sec), leaf count = 31

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{6}(-12c_1x^3 - 36c_1^2 - x^6 + x^3) \right\} \right\}$$

**Maple:** cpu = 0.172 (sec), leaf count = 23

$$\left\{ -C1 - x^3 - \frac{1}{2} - \sqrt{x^3 - 6y(x)} = 0 \right\}$$

**2.632 ODE No. 632**

$$\frac{d}{dx}y(x) = \frac{e^x}{y(x)e^{-x} + 1} = 0$$

**Mathematica:** cpu = 0.168521 (sec), leaf count = 65

$$\text{Solve} \left[ \frac{1}{2} \log(-e^{-2x}y(x)^2 - e^{-x}y(x) + 1) + x = c_1 + \frac{\tanh^{-1}\left(\frac{y(x)+3e^x}{\sqrt{5}(y(x)+e^x)}\right)}{\sqrt{5}}, y(x) \right]$$

**Maple:** cpu = 0.203 (sec), leaf count = 52

$$\left\{ x + \frac{\ln\left((y(x))^2(e^{-x})^2 + y(x)e^{-x} - 1\right)}{2} - \frac{\sqrt{5}}{5} \text{Artanh}\left(\frac{(1 + 2y(x)e^{-x})\sqrt{5}}{5}\right) - C1 = 0 \right\}$$

**2.633 ODE No. 633**

$$\frac{d}{dx}y(x) = \frac{e^{2/3x}}{y(x)e^{-2/3x} + 1} = 0$$

**Mathematica:** cpu = 0.191024 (sec), leaf count = 85

$$\text{Solve} \left[ 7 \left( -9c_1 + 3 \log \left( -\frac{2}{3} e^{-4x/3} y(x)^2 - \frac{2}{3} e^{-2x/3} y(x) + 1 \right) + 4x \right) = 6\sqrt{7} \tanh^{-1} \left( \frac{y(x) + 4e^{2x/3}}{\sqrt{7}(y(x) + e^{2x/3})} \right), \right]$$

**Maple:** cpu = 0.686 (sec), leaf count = 52

$$\left\{ y(x) = 1 \text{RootOf} \left( -e^{\text{RootOf}(-343(\tanh(1/6(4C1-4x-3Z)\sqrt{7}))^2 + 343 + 98e^{-Z})} - 3 + 2Z + 2Z^2 \right) \left( e^{-\frac{2x}{3}} \right)^{-1} \right\}$$

**2.634 ODE No. 634**

$$\frac{d}{dx}y(x) = \frac{1}{2} \frac{1 + 2x^5 \sqrt{4x^2y(x) + 1}}{x^3} = 0$$

**Mathematica:** cpu = 0.184523 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow \frac{-8c_1x^6 + 16c_1^2x^2 + x^{10} - 4}{16x^2} \right\} \right\}$$

**Maple:** cpu = 0.187 (sec), leaf count = 26

$$\left\{ -C1 - \frac{1}{x} \sqrt{4x^2y(x) + 1} + \frac{x^4}{2} = 0 \right\}$$

**2.635 ODE No. 635**

$$\frac{d}{dx}y(x) = 1/2 x(x + 2\sqrt{x^3 - 6y(x)}) = 0$$

**Mathematica:** cpu = 0.125016 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{24}(36c_1x^2 - 36c_1^2 - 9x^4 + 4x^3) \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 22

$$\left\{ -C1 - \frac{3x^2}{2} - \sqrt{x^3 - 6y(x)} = 0 \right\}$$

**2.636 ODE No. 636**

$$\frac{d}{dx}y(x) = (-\ln(y(x)) + x^2)y(x) = 0$$

**Mathematica:** cpu = 0.055007 (sec), leaf count = 24

$$\left\{ \left\{ y(x) \rightarrow e^{-2c_1e^{-x}+x^2-2x+2} \right\} \right\}$$

**Maple:** cpu = 0.140 (sec), leaf count = 19

$$\left\{ y(x) = e^{\frac{-C1}{e^x}+x^2-2x+2} \right\}$$

**2.637 ODE No. 637**

$$\frac{d}{dx}y(x) = \frac{xe^{-x^2}}{y(x)e^{x^2} + 1} = 0$$

**Mathematica:** cpu = 9.663227 (sec), leaf count = 59

$$\text{Solve} \left[ -\frac{1}{4} \log \left( 2e^{2x^2}y(x)^2 + 2e^{x^2}y(x) + 1 \right) - \frac{1}{2} \tan^{-1} \left( 2e^{x^2}y(x) + 1 \right) + \frac{x^2}{2} = c_1, y(x) \right]$$

**Maple:** cpu = 1.482 (sec), leaf count = 84

$$\left\{ y(x) = -\frac{1}{e^{x^2}} \tan \left( \text{RootOf} \left( 2x^2 - \ln \left( \frac{81(\tan(\_Z))^2}{10} + \frac{81}{10} \right) + 2 \ln(9/2 \tan(\_Z) - 9/2) + 6\_C1 - \right. \right. \right.$$

**2.638 ODE No. 638**

$$\frac{d}{dx}y(x) = -(-\ln(\ln(y(x))) + \ln(x))y(x) = 0$$

**Mathematica:** cpu = 2.786354 (sec), leaf count = 21

$$\text{DSolve}[y'(x) = y(x)(\log(\log(y(x))) - \log(x)), y(x), x]$$

**Maple:** cpu = 0.124 (sec), leaf count = 35

$$\left\{ \int_{-b}^{y(x)} \frac{1}{-a(x \ln(x) - \ln(\ln(-a))x + \ln(-a))} d_{-a} + \ln(x) - \_C1 = 0 \right\}$$

**2.639 ODE No. 639**

$$\frac{d}{dx}y(x) = (-\ln(\ln(y(x))) + \ln(x))^2 y(x) = 0$$

**Mathematica:** cpu = 0.363546 (sec), leaf count = 23

$$\text{DSolve}[y'(x) = y(x)(\log(x) - \log(\log(y(x))))^2, y(x), x]$$

**Maple:** cpu = 0.172 (sec), leaf count = 50

$$\left\{ \int_{-b}^{y(x)} \frac{1}{-a(x(\ln(x))^2 - 2\ln(x)\ln(\ln(-a))x + (\ln(\ln(-a)))^2x - \ln(-a))} d_{-a} - \ln(x) - \_C1 = 0 \right\}$$

**2.640 ODE No. 640**

$$\frac{d}{dx}y(x) = \frac{y(x)}{\ln(\ln(y(x))) - \ln(x) + 1} = 0$$

**Mathematica:** cpu = 3.865991 (sec), leaf count = 24

$$\text{DSolve}\left[y'(x) = \frac{y(x)}{\log(\log(y(x))) - \log(x) + 1}, y(x), x\right]$$

**Maple:** cpu = 0.203 (sec), leaf count = 45

$$\left\{ \int_{-b}^{y(x)} \frac{-\ln(\ln(-a)) + \ln(x) - 1}{-a(-\ln(-a)\ln(\ln(-a)) + (\ln(x) - 1)\ln(-a) + x)} d_{-a} - \_C1 = 0 \right\}$$

**2.641 ODE No. 641**

$$\frac{d}{dx}y(x) = 1/2 \frac{1 + 2\sqrt{4x^2y(x) + 1x^4}}{x^3} = 0$$

**Mathematica:** cpu = 0.177022 (sec), leaf count = 35

$$\left\{ \left\{ y(x) \rightarrow \frac{-24c_1x^5 + 36c_1^2x^2 + 4x^8 - 9}{36x^2} \right\} \right\}$$

**Maple:** cpu = 0.172 (sec), leaf count = 26

$$\left\{ -C1 - \frac{1}{x}\sqrt{4x^2y(x) + 1} + \frac{2x^3}{3} = 0 \right\}$$

**2.642 ODE No. 642**

$$\frac{d}{dx}y(x) = \frac{(-(y(x))^2 + 4ax)^2}{y(x)} = 0$$

**Mathematica:** cpu = 0.145018 (sec), leaf count = 105

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{4ax - \sqrt{2}\sqrt{a} \tanh\left(\frac{2\sqrt{2}ax - \sqrt{2}c_1}{\sqrt{a}}\right)} \right\}, \left\{ y(x) \rightarrow \sqrt{4ax - \sqrt{2}\sqrt{a} \tanh\left(\frac{2\sqrt{2}ax - \sqrt{2}c_1}{\sqrt{a}}\right)} \right\} \right\}$$

**Maple:** cpu = 0.187 (sec), leaf count = 286

$$\left\{ y(x) = \sqrt{4} \sqrt{\left(-C1 e^{2x(\sqrt{2}\sqrt{a}-2ax)} + e^{-2x(\sqrt{2}\sqrt{a}+2ax)}\right) \left(-C1 \left(ax - \frac{\sqrt{2}}{4}\sqrt{a}\right) e^{2x(\sqrt{2}\sqrt{a}-2ax)} + e^{-2x(\sqrt{2}\sqrt{a}+2ax)}\right)} \right\}$$

**2.643 ODE No. 643**

$$\frac{d}{dx}y(x) = 1/3 x \left(-2 + 3x\sqrt{x^2 + 3y(x)}\right) = 0$$

**Mathematica:** cpu = 0.118515 (sec), leaf count = 31

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{12}(-6c_1x^3 + 9c_1^2 + x^6 - 4x^2) \right\} \right\}$$

**Maple:** cpu = 0.172 (sec), leaf count = 22

$$\left\{ -C1 + \frac{x^3}{2} - \sqrt{x^2 + 3y(x)} = 0 \right\}$$

**2.644 ODE No. 644**

$$\frac{d}{dx}y(x) = -1/2 x^2 \left( ax - 2 \sqrt{a(ax^4 + 8y(x))} \right) = 0$$

**Mathematica:** cpu = 0.274535 (sec), leaf count = 34

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{72} a (-96c_1 x^3 + 144c_1^2 + 16x^6 - 9x^4) \right\} \right\}$$

**Maple:** cpu = 0.265 (sec), leaf count = 27

$$\left\{ -C1 + \frac{4ax^3}{3} - \sqrt{a(ax^4 + 8y(x))} = 0 \right\}$$

**2.645 ODE No. 645**

$$\frac{d}{dx}y(x) = (-\ln(y(x)) + x)y(x) = 0$$

**Mathematica:** cpu = 0.038505 (sec), leaf count = 20

$$\left\{ \left\{ y(x) \rightarrow e^{-e^{c_1 - x} + x - 1} \right\} \right\}$$

**Maple:** cpu = 0.110 (sec), leaf count = 14

$$\left\{ y(x) = e^{\frac{C1}{e^x} - 1 + x} \right\}$$

**2.646 ODE No. 646**

$$\frac{d}{dx}y(x) = 1/2 \frac{x^3 + x^2 + 2 \sqrt{x^3 - 6y(x)}}{1 + x} = 0$$

**Mathematica:** cpu = 0.180523 (sec), leaf count = 35

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{6} (18c_1 \log(x + 1) - 9c_1^2 + x^3 - 9 \log^2(x + 1)) \right\} \right\}$$

**Maple:** cpu = 0.202 (sec), leaf count = 23

$$\left\{ -C1 - 3 \ln(1 + x) - \sqrt{x^3 - 6y(x)} = 0 \right\}$$

**2.647 ODE No. 647**

$$\frac{d}{dx}y(x) = \frac{(a(y(x))^2 + bx^2)^2 x}{a^{5/2}y(x)} = 0$$

**Mathematica:** cpu = 0.422554 (sec), leaf count = 115

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{\frac{\sqrt{b} \tan\left(\frac{a^{3/2}bx^2+2c_1}{a^{9/4}\sqrt{b}}\right) - bx^2}{\sqrt[4]{a}}} \right\}, \left\{ y(x) \rightarrow \sqrt{\frac{\sqrt{b} \tan\left(\frac{a^{3/2}bx^2+2c_1}{a^{9/4}\sqrt{b}}\right) - bx^2}{\sqrt[4]{a}}} \right\} \right\}$$

**Maple:** cpu = 0.218 (sec), leaf count = 460

$$\left\{ y(x) = \frac{1}{a} \sqrt{-\left(\left(bx^2 - a^{\frac{3}{2}} \sqrt{-ba^{-\frac{3}{2}}}\right) e^{\frac{x^2}{2}(-2a^{3/2} \sqrt{-\frac{b}{a^{3/2}}+bx^2})a^{-\frac{3}{2}}} + \_C1 \left(a^{\frac{3}{2}} \sqrt{-ba^{-\frac{3}{2}} + bx^2}\right) e^{\frac{x^2}{2}(2a^{3/2} \sqrt{-\frac{b}{a^{3/2}}+bx^2})}\right)}$$

**2.648 ODE No. 648**

$$\frac{d}{dx}y(x) = -1/2 \frac{x^3 (\sqrt{ax} + \sqrt{a} - 2 \sqrt{ax^4 + 8y(x)}) \sqrt{a}}{1+x} = 0$$

**Mathematica:** cpu = 0.351044 (sec), leaf count = 128

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{72} (-96ac_1x^3 + 144ac_1x^2 - 288ac_1x + 288ac_1 \log(x+1) + 144ac_1^2 - 432ac_1 + 16ax^6 - 48ax^5) \right\} \right\}$$

**Maple:** cpu = 0.437 (sec), leaf count = 41

$$\left\{ \frac{1}{4} \sqrt{ax^4 + 8y(x)} \frac{1}{\sqrt{a}} - \frac{x^3}{3} + \frac{x^2}{2} - x + \ln(1+x) - \_C1 = 0 \right\}$$

**2.649 ODE No. 649**

$$\frac{d}{dx}y(x) = -x/4 + 1/4 + x \sqrt{x^2 - 2x + 1 + 8y(x)} = 0$$

**Mathematica:** cpu = 0.180523 (sec), leaf count = 37

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{8} (-16c_1x^2 + 16c_1^2 + 4x^4 - x^2 + 2x - 1) \right\} \right\}$$

**Maple:** cpu = 0.187 (sec), leaf count = 27

$$\left\{ -C1 + 2x^2 + \frac{1}{4} - \sqrt{x^2 - 2x + 1 + 8y(x)} = 0 \right\}$$

**2.650 ODE No. 650**

$$\frac{d}{dx}y(x) = -x/2 - a/2 + x\sqrt{x^2 + 2ax + a^2 + 4y(x)} = 0$$

**Mathematica:** cpu = 0.245531 (sec), leaf count = 40

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4}(-a^2 - 2ax - 4c_1x^2 + 4c_1^2 + x^4 - x^2) \right\} \right\}$$

**Maple:** cpu = 0.187 (sec), leaf count = 28

$$\left\{ -C1 + x^2 + \frac{1}{2} - \sqrt{x^2 + 2ax + a^2 + 4y(x)} = 0 \right\}$$

**2.651 ODE No. 651**

$$\frac{d}{dx}y(x) = \frac{(\ln(y(x)) + x^2)y(x)}{x} = 0$$

**Mathematica:** cpu = 0.037505 (sec), leaf count = 16

$$\left\{ \left\{ y(x) \rightarrow e^{2c_1x+x^2} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 13

$$\left\{ y(x) = e^{-C1x}e^{x^2} \right\}$$

**2.652 ODE No. 652**

$$\frac{d}{dx}y(x) = \frac{2a + x\sqrt{-(y(x))^2 + 4ax}}{y(x)} = 0$$

**Mathematica:** cpu = 1.924244 (sec), leaf count = 101

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{4096a^5x - 256a^4x^4 + 32a^2e^{c_1x^2} - e^{2c_1}}}{32a^2} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{4096a^5x - 256a^4x^4 + 32a^2e^{c_1x^2} - e^{2c_1}}}{32a^2} \right\} \right\}$$

**Maple:** cpu = 0.124 (sec), leaf count = 27

$$\left\{ -\sqrt{-(y(x))^2 + 4ax} - \frac{x^2}{2} - C1 = 0 \right\}$$



**2.653 ODE No. 653**

$$\frac{d}{dx}y(x) = -x/2 + 1 + x\sqrt{x^2 - 4x + 4y(x)} = 0$$

**Mathematica:** cpu = 0.182023 (sec), leaf count = 34

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4}(-4c_1x^2 + 4c_1^2 + x^4 - x^2 + 4x) \right\} \right\}$$

**Maple:** cpu = 0.172 (sec), leaf count = 24

$$\left\{ -C1 + x^2 + \frac{1}{2} - \sqrt{x^2 - 4x + 4y(x)} = 0 \right\}$$

**2.654 ODE No. 654**

$$\frac{d}{dx}y(x) = -1/3 \frac{2x^2 + 2x - 3\sqrt{x^2 + 3y(x)}}{1+x} = 0$$

**Mathematica:** cpu = 0.165021 (sec), leaf count = 37

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{12}(-18c_1 \log(x+1) + 9c_1^2 - 4x^2 + 9 \log^2(x+1)) \right\} \right\}$$

**Maple:** cpu = 0.203 (sec), leaf count = 23

$$\left\{ -C1 + \frac{3 \ln(1+x)}{2} - \sqrt{x^2 + 3y(x)} = 0 \right\}$$

**2.655 ODE No. 655**

$$\frac{d}{dx}y(x) = \frac{(y(x))^3 e^{-4/3x}}{y(x) e^{-2/3x} + 1} = 0$$

**Mathematica:** cpu = 11.358942 (sec), leaf count = 82

$$\text{Solve} \left[ \frac{3}{2} \log(y(x)) + \frac{1}{28} \left( -21 \log(-3y(x)^2 + 2e^{2x/3}y(x) + 2e^{4x/3}) + 6\sqrt{7} \tanh^{-1} \left( \frac{y(x) + 2e^{2x/3}}{\sqrt{7}y(x)} \right) + 28x \right) \right]$$

**Maple:** cpu = 0.920 (sec), leaf count = 64

$$\left\{ x + \frac{3}{2} \ln \left( y(x) e^{-\frac{2x}{3}} \right) - \frac{3}{4} \ln \left( 3(y(x))^2 (e^{-2/3x})^2 - 2y(x) e^{-2/3x} - 2 \right) + \frac{3\sqrt{7}}{14} \text{Artanh} \left( \frac{\sqrt{7}}{14} (6y(x) e^{-2/3x}) \right) \right\}$$

**2.656 ODE No. 656**

$$\frac{d}{dx}y(x) = \frac{(\ln(y(x)) + x^3)y(x)}{x} = 0$$

**Mathematica:** cpu = 0.042505 (sec), leaf count = 20

$$\left\{ \left\{ y(x) \rightarrow e^{3c_1x + \frac{x^3}{2}} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 15

$$\left\{ y(x) = e^{\frac{x^3}{2}} e^{-C1 x} \right\}$$

**2.657 ODE No. 657**

$$\frac{d}{dx}y(x) = -x/4 + 1/4 + x^2\sqrt{x^2 - 2x + 1 + 8y(x)} = 0$$

**Mathematica:** cpu = 0.190024 (sec), leaf count = 37

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{72}(-96c_1x^3 + 144c_1^2 + 16x^6 - 9x^2 + 18x - 9) \right\} \right\}$$

**Maple:** cpu = 0.171 (sec), leaf count = 26

$$\left\{ -C1 + \frac{4x^3}{3} - \sqrt{x^2 - 2x + 1 + 8y(x)} = 0 \right\}$$

**2.658 ODE No. 658**

$$\frac{d}{dx}y(x) = -1/4 \frac{x^2 - 1 - 4\sqrt{x^2 - 2x + 1 + 8y(x)}}{1 + x} = 0$$

**Mathematica:** cpu = 0.247531 (sec), leaf count = 45

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{8}(-32c_1 \log(4(x+1)) + 16c_1^2 - x^2 + 2x + 16 \log^2(4(x+1)) - 1) \right\} \right\}$$

**Maple:** cpu = 0.218 (sec), leaf count = 28

$$\left\{ -C1 + 4 \ln(1 + x) - \frac{1}{4} - \sqrt{x^2 - 2x + 1 + 8y(x)} = 0 \right\}$$

**2.659 ODE No. 659**

$$\frac{d}{dx}y(x) = -1/2 ax - b/2 + x\sqrt{a^2x^2 + 2 abx + b^2 + 4 ay(x) - 4 c} = 0$$

**Mathematica:** cpu = 0.440556 (sec), leaf count = 60

$$\left\{ \left\{ y(x) \rightarrow \frac{-4a^2c_1x^2 + 4a^2c_1^2 + a^2x^4 - a^2x^2 - 2abx - b^2 + 4c}{4a} \right\} \right\}$$

**Maple:** cpu = 0.187 (sec), leaf count = 41

$$\left\{ -C1 + ax^2 + \frac{a}{2} - \sqrt{a^2x^2 + 2 abx + b^2 + 4 ay(x) - 4 c} = 0 \right\}$$

**2.660 ODE No. 660**

$$\frac{d}{dx}y(x) = -x/2 - a/2 + x^2\sqrt{x^2 + 2 ax + a^2 + 4 y(x)} = 0$$

**Mathematica:** cpu = 0.265034 (sec), leaf count = 42

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{36}(-9a^2 - 18ax - 24c_1x^3 + 36c_1^2 + 4x^6 - 9x^2) \right\} \right\}$$

**Maple:** cpu = 0.188 (sec), leaf count = 29

$$\left\{ -C1 + \frac{2x^3}{3} - \sqrt{x^2 + 2 ax + a^2 + 4 y(x)} = 0 \right\}$$

**2.661 ODE No. 661**

$$\frac{d}{dx}y(x) = -1/2 ax - b/2 + x^2\sqrt{a^2x^2 + 2 abx + b^2 + 4 ay(x) - 4 c} = 0$$

**Mathematica:** cpu = 0.420553 (sec), leaf count = 61

$$\left\{ \left\{ y(x) \rightarrow \frac{-24a^2c_1x^3 + 36a^2c_1^2 + 4a^2x^6 - 9a^2x^2 - 18abx - 9b^2 + 36c}{36a} \right\} \right\}$$

**Maple:** cpu = 0.218 (sec), leaf count = 39

$$\left\{ -C1 + \frac{2ax^3}{3} - \sqrt{a^2x^2 + 2 abx + b^2 + 4 ay(x) - 4 c} = 0 \right\}$$

**2.662 ODE No. 662**

$$\frac{d}{dx}y(x) = x/2 + 1/2 + x^2\sqrt{x^2 + 2x + 1 - 4y(x)} = 0$$

**Mathematica:** cpu = 0.196525 (sec), leaf count = 37

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{36}(24c_1x^3 - 36c_1^2 - 4x^6 + 9x^2 + 18x + 9) \right\} \right\}$$

**Maple:** cpu = 0.188 (sec), leaf count = 26

$$\left\{ -C1 - \frac{2x^3}{3} - \sqrt{x^2 + 2x + 1 - 4y(x)} = 0 \right\}$$

**2.663 ODE No. 663**

$$\frac{d}{dx}y(x) = \frac{2a + x^2\sqrt{-(y(x))^2 + 4ax}}{y(x)} = 0$$

**Mathematica:** cpu = 2.294291 (sec), leaf count = 101

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{147456a^7x - 4096a^6x^6 + 128a^3e^{c_1}x^3 - e^{2c_1}}}{192a^3} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{147456a^7x - 4096a^6x^6 + 128a^3e^{c_1}x^3 - e^{2c_1}}}{192a^3} \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 27

$$\left\{ -\sqrt{-(y(x))^2 + 4ax} - \frac{x^3}{3} - C1 = 0 \right\}$$

**2.664 ODE No. 664**

$$\frac{d}{dx}y(x) = -x/2 + 1 + x^2\sqrt{x^2 - 4x + 4y(x)} = 0$$

**Mathematica:** cpu = 0.191024 (sec), leaf count = 36

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{36}(-24c_1x^3 + 36c_1^2 + 4x^6 - 9x^2 + 36x) \right\} \right\}$$

**Maple:** cpu = 0.171 (sec), leaf count = 25

$$\left\{ -C1 + \frac{2x^3}{3} - \sqrt{x^2 - 4x + 4y(x)} = 0 \right\}$$

**2.665 ODE No. 665**

$$\frac{d}{dx}y(x) = -1/2 \frac{(\sqrt{ax^4 + \sqrt{a}x^3 - 2\sqrt{ax^4 + 8y(x)})\sqrt{a}}}{1+x} = 0$$

**Mathematica:** cpu = 0.272035 (sec), leaf count = 41

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{8}(-32ac_1 \log(x+1) + 16ac_1^2 - ax^4 + 16a \log^2(x+1)) \right\} \right\}$$

**Maple:** cpu = 0.343 (sec), leaf count = 28

$$\left\{ -\frac{1}{4}\sqrt{ax^4 + 8y(x)}\frac{1}{\sqrt{a}} + \ln(1+x) - \_C1 = 0 \right\}$$

**2.666 ODE No. 666**

$$\frac{d}{dx}y(x) = (-\ln(y(x)) + 1 + x^2 + x^3)y(x) = 0$$

**Mathematica:** cpu = 0.075510 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow e^{-c_1 e^{-x+x^3-2x^2+4x-3}} \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 24

$$\left\{ y(x) = e^{\frac{-C1}{e^x} + x^3 - 2x^2 + 4x - 3} \right\}$$

**2.667 ODE No. 667**

$$\frac{d}{dx}y(x) = \frac{(y(x))^3 e^{-2bx}}{y(x) e^{-bx} + 1} = 0$$

**Mathematica:** cpu = 1.021630 (sec), leaf count = 90

$$\text{Solve} \left[ \frac{\log(y(x))}{b} + \frac{1}{2} \left( -\frac{\log(y(x)^2 - be^{bx}(e^{bx} + y(x)))}{b} + \frac{2 \tanh^{-1} \left( \frac{\sqrt{\frac{b}{b+4}}(2e^{bx} + y(x))}{y(x)} \right)}{\sqrt{b}\sqrt{b+4}} + 2x \right) = c_1, y(x) \right]$$

**Maple:** cpu = 0.172 (sec), leaf count = 83

$$\left\{ bx + b \text{Artanh} \left( (2y(x) e^{-bx} - b) \frac{1}{\sqrt{b^2 + 4b}} \right) \frac{1}{\sqrt{b^2 + 4b}} + \ln(y(x) e^{-bx}) - \frac{\ln(-by(x) e^{-bx} + (y(x))^2 (e^{-b} \right. \right.$$

**2.668 ODE No. 668**

$$\frac{d}{dx}y(x) = \frac{(y(x))^3 e^{-2x}}{y(x) e^{-x} + 1} = 0$$

**Mathematica:** cpu = 0.536568 (sec), leaf count = 78

$$\text{Solve} \left[ \log(y(x)) + y(x)^2 \left( \frac{x}{y(x)^2} - \frac{\log(-y(x)^2 + e^x y(x) + e^{2x})}{2y(x)^2} + \frac{\tanh^{-1}\left(\frac{y(x)+2e^x}{\sqrt{5}y(x)}\right)}{\sqrt{5}y(x)^2} \right) = c_1, y(x) \right]$$

**Maple:** cpu = 0.546 (sec), leaf count = 58

$$\left\{ y(x) = e^{\text{RootOf}\left(2\sqrt{5}\text{Artanh}\left(\frac{1}{5}\frac{(e^x-2e^{-Z})\sqrt{5}}{e^x}\right) + 5\ln((e^{-Z})^2 - e^{x+Z} - (e^x)^2) + 10\_C1 - 10\_Z - 10x\right)} \right\}$$

**2.669 ODE No. 669**

$$\frac{d}{dx}y(x) = 1/4 \frac{(-2(y(x))^{3/2} + 3e^x)^2 e^x}{\sqrt{y(x)}} = 0$$

**Mathematica:** cpu = 0.884112 (sec), leaf count = 264

$$\left\{ \left\{ y(x) \rightarrow \frac{(3e^{3c_1+x} + 2e^{3c_1} - 2e^{3e^x} + 3e^{x+3e^x})^{2/3}}{\sqrt[3]{8e^{3c_1+3e^x} + 4e^{6c_1} + 4e^{6e^x}}} \right\}, \left\{ y(x) \rightarrow -\frac{\sqrt[3]{-1}(3e^{3c_1+x} + 2e^{3c_1} - 2e^{3e^x} + 3e^{x+3e^x})}{\sqrt[3]{8e^{3c_1+3e^x} + 4e^{6c_1} + 4e^{6e^x}}} \right\} \right\}$$

**Maple:** cpu = 0.203 (sec), leaf count = 72

$$\left\{ -C1 + 1e^{-\frac{3e^x}{2} - \frac{9e^{2x}}{8}} \left( 2(y(x))^{3/2} e^x - 2e^x - 3e^{2x} \right) \left( e^{\frac{3e^x}{2} - \frac{9e^{2x}}{8}} \right)^{-1} \left( 2(y(x))^{3/2} e^x + 2e^x - 3e^{2x} \right)^{-1} = 0 \right\}$$

**2.670 ODE No. 670**

$$\frac{d}{dx}y(x) = i/2x \left( i - 2\sqrt{-x^2 + 4\ln(a) + 4\ln(y(x))} \right) y(x) = 0$$

**Mathematica:** cpu = 0.370047 (sec), leaf count = 99

$$\text{Solve} \left[ -\log(y(x)) + \frac{1}{4} \left( -\frac{1}{2} \log(4\log(a) - x^2 + 4\log(y(x)) + 1) + i\sqrt{4\log(a) - x^2 + 4\log(y(x))} - i \tan^{-1} \left( \frac{x}{\sqrt{4\log(a) - x^2 + 4\log(y(x))}} \right) \right) = c_1, y(x) \right]$$

**Maple:** cpu = 0.250 (sec), leaf count = 70

$$\left\{ \frac{1}{2} \sqrt{-x^2 + 4\ln(a) + 4\ln(y(x))} - \frac{1}{2} \arctan \left( \sqrt{-x^2 + 4\ln(a) + 4\ln(y(x))} \right) + \frac{i}{4} \ln(x^2 - 4\ln(a) - 4) = c_1, y(x) \right\}$$

**2.671 ODE No. 671**

$$\frac{d}{dx}y(x) = \frac{(x(y(x))^2 + 1)^2}{y(x)x^4} = 0$$

**Mathematica:** cpu = 0.426054 (sec), leaf count = 192

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{\sqrt{2}e^{\frac{2\sqrt{2}(c_1x+1)}{x}} - \frac{2e^{\frac{2\sqrt{2}(c_1x+1)}{x}}}{x} - \frac{2}{x} - \sqrt{2}}}}{\sqrt{2e^{\frac{2\sqrt{2}(c_1x+1)}{x}} + 2}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{\sqrt{2}e^{\frac{2\sqrt{2}(c_1x+1)}{x}} - \frac{2e^{\frac{2\sqrt{2}(c_1x+1)}{x}}}{x} - \frac{2}{x} - \sqrt{2}}}}{\sqrt{2e^{\frac{2\sqrt{2}(c_1x+1)}{x}} + 2}} \right\} \right.$$

**Maple:** cpu = 0.156 (sec), leaf count = 237

$$\left\{ y(x) = -\frac{\sqrt{2}}{2x} \sqrt{-\left(-C1 e^{\frac{-1-\sqrt{2}x}{x^2}} + e^{\frac{-1+\sqrt{2}x}{x^2}}\right) \left(-C1 \left(\sqrt{2}x + 2\right) e^{\frac{-1-\sqrt{2}x}{x^2}} + \left(2 - \sqrt{2}x\right) e^{\frac{-1+\sqrt{2}x}{x^2}}\right) x \left(-C1 e^{\frac{-1-\sqrt{2}x}{x^2}} + e^{\frac{-1+\sqrt{2}x}{x^2}}\right)}{\dots} \right.$$

**2.672 ODE No. 672**

$$\frac{d}{dx}y(x) = \frac{x^2 \left( 3x + \sqrt{-9x^4 + 4(y(x))^3} \right)}{(y(x))^2} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.156 (sec), leaf count = 36

$$\left\{ \int_{-b}^{y(x)} -a^2 \frac{1}{\sqrt{-9x^4 + 4a^3}} da - \frac{x^3}{3} - C1 = 0 \right\}$$

**2.673 ODE No. 673**

$$\frac{d}{dx}y(x) = 1/2 \frac{-\sin(2y(x)) + \cos(2y(x))x^2 + x^2}{x} = 0$$

**Mathematica:** cpu = 0.084011 (sec), leaf count = 23

$$\left\{ \left\{ y(x) \rightarrow \tan^{-1} \left( \frac{3c_1 + 2x^3}{6x} \right) \right\} \right\}$$

**Maple:** cpu = 0.359 (sec), leaf count = 17

$$\left\{ y(x) = \arctan \left( \frac{x^3 + 6C1}{3x} \right) \right\}$$

**2.674 ODE No. 674**

$$\frac{d}{dx}y(x) = -1/2 \frac{x^2 - x - 2 - 2\sqrt{x^2 - 4x + 4y(x)}}{1 + x} = 0$$

**Mathematica:** cpu = 0.233530 (sec), leaf count = 40

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4}(-8c_1 \log(x + 1) + 4c_1^2 - x^2 + 4x + 4 \log^2(x + 1)) \right\} \right\}$$

**Maple:** cpu = 0.234 (sec), leaf count = 27

$$\left\{ -C1 + 2 \ln(1 + x) - 1 - \sqrt{x^2 - 4x + 4y(x)} = 0 \right\}$$

**2.675 ODE No. 675**

$$\frac{d}{dx}y(x) = \frac{y(x) + x^3 a e^x + a x^4 + a x^3 - x(y(x))^2 e^x - x^2(y(x))^2 - x(y(x))^2}{x} = 0$$

**Mathematica:** cpu = 0.057007 (sec), leaf count = 48

$$\left\{ \left\{ y(x) \rightarrow \sqrt{ax} \tanh \left( \frac{1}{6} \sqrt{a} (6c_1 + 2x^3 + 3x^2 + 6e^x x - 6e^x) \right) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 46

$$\left\{ y(x) = \tanh \left( \frac{x^3}{3} \sqrt{a} + x e^x \sqrt{a} + \frac{x^2}{2} \sqrt{a} - e^x \sqrt{a} + -C1 \sqrt{a} \right) x \sqrt{a} \right\}$$

**2.676 ODE No. 676**

$$\frac{d}{dx}y(x) = 1/2 \frac{x + 1 + 2x^6 \sqrt{4x^2 y(x) + 1}}{x^3(1 + x)} = 0$$

**Mathematica:** cpu = 0.323541 (sec), leaf count = 144

$$\left\{ \left\{ y(x) \rightarrow \frac{-72c_1 x^6 + 96c_1 x^5 - 144c_1 x^4 + 288c_1 x^3 + 144c_1^2 x^2 - 288c_1 x^2 \log(x + 1) + 9x^{10} - 24x^9 + 52x^8}{x^3(1 + x)} \right\} \right\}$$

**Maple:** cpu = 0.374 (sec), leaf count = 43

$$\left\{ -C1 + 2 \ln(1 + x) - 2x + x^2 - \frac{2x^3}{3} + \frac{x^4}{2} - \frac{1}{x} \sqrt{4x^2 y(x) + 1} = 0 \right\}$$



**2.677 ODE No. 677**

$$\frac{d}{dx}y(x) = \frac{y(x) + x^3 a \ln(1+x) + ax^4 + ax^3 - x(y(x))^2 \ln(1+x) - x^2(y(x))^2 - x(y(x))^2}{x} = 0$$

**Mathematica:** cpu = 0.037505 (sec), leaf count = 80

$$\left\{ \left\{ y(x) \rightarrow \sqrt{ax} \tanh \left( \frac{1}{12} (12\sqrt{ac_1} + 4\sqrt{ax^3} + 3\sqrt{ax^2} + 6\sqrt{ax^2} \log(x+1) + 6\sqrt{ax} - 6\sqrt{a} \log(x+1)) \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 64

$$\left\{ y(x) = \tanh \left( \frac{\ln(1+x)x^2}{2} \sqrt{a} + \frac{x^3}{3} \sqrt{a} + \frac{x^2}{4} \sqrt{a} - \frac{\ln(1+x)}{2} \sqrt{a} + \_C1 \sqrt{a} + \frac{x}{2} \sqrt{a} + \frac{3}{4} \sqrt{a} \right) x \sqrt{a} \right\}$$

**2.678 ODE No. 678**

$$\frac{d}{dx}y(x) = 1/2 \frac{x^2(x+1+2x\sqrt{x^3-6y(x)})}{1+x} = 0$$

**Mathematica:** cpu = 0.250532 (sec), leaf count = 101

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{24} (24c_1x^3 - 36c_1x^2 + 72c_1x - 72c_1 \log(x+1) - 36c_1^2 - 4x^6 + 12x^5 - 33x^4 + 40x^3 + 24x^3 \log(x+1)) \right\} \right\}$$

**Maple:** cpu = 0.234 (sec), leaf count = 37

$$\left\{ \left\{ -C1 - x^3 + \frac{3x^2}{2} - 3x + 3 \ln(1+x) - \frac{1}{2} - \sqrt{x^3 - 6y(x)} = 0 \right\} \right\}$$

**2.679 ODE No. 679**

$$\frac{d}{dx}y(x) = \frac{y(x) + x^3 \ln(x) + x^4 + x^3 + 7x(y(x))^2 \ln(x) + 7x^2(y(x))^2 + 7x(y(x))^2}{x} = 0$$

**Mathematica:** cpu = 0.035505 (sec), leaf count = 59

$$\left\{ \left\{ y(x) \rightarrow \frac{x \tan \left( \frac{1}{12} (12\sqrt{7}c_1 + 4\sqrt{7}x^3 + 3\sqrt{7}x^2 + 6\sqrt{7}x^2 \log(x)) \right)}{\sqrt{7}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 37

$$\left\{ y(x) = \frac{x\sqrt{7}}{7} \tan \left( \frac{(6x^2 \ln(x) + 4x^3 + 3x^2 + 12\_C1) \sqrt{7}}{12} \right) \right\}$$

**2.680 ODE No. 680**

$$\frac{d}{dx}y(x) = 1/2 \frac{x^2 + 2x + 1 + 2\sqrt{x^2 + 2x + 1 - 4y(x)}}{1 + x} = 0$$

**Mathematica:** cpu = 0.235530 (sec), leaf count = 39

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4}(8c_1 \log(x + 1) - 4c_1^2 + x^2 + 2x - 4 \log^2(x + 1) + 1) \right\} \right\}$$

**Maple:** cpu = 0.218 (sec), leaf count = 28

$$\left\{ -C1 - 2 \ln(1 + x) - \frac{1}{2} - \sqrt{x^2 + 2x + 1 - 4y(x)} = 0 \right\}$$

**2.681 ODE No. 681**

$$\frac{d}{dx}y(x) = \frac{y(x) + x^3b \ln(x^{-1}) + x^4b + bx^3 + xa(y(x))^2 \ln(x^{-1}) + ax^2(y(x))^2 + ax(y(x))^2}{x} = 0$$

**Mathematica:** cpu = 0.045006 (sec), leaf count = 84

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt{bx} \tan\left(\frac{1}{12}\left(12\sqrt{a}\sqrt{bc_1} + 4\sqrt{a}\sqrt{bx^3} + 9\sqrt{a}\sqrt{bx^2} - 6\sqrt{a}\sqrt{bx^2} \log(x)\right)\right)}{\sqrt{a}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 57

$$\left\{ y(x) = \frac{x}{a} \tan\left(\frac{x^2 \ln(x^{-1})}{2} \sqrt{ab} + \frac{x^3}{3} \sqrt{ab} + \frac{3x^2}{4} \sqrt{ab} + -C1 \sqrt{ab}\right) \sqrt{ab} \right\}$$

**2.682 ODE No. 682**

$$\frac{d}{dx}y(x) = 2 \frac{a}{x(-xy(x) + 2ax(y(x))^2 - 8a^2)} = 0$$

**Mathematica:** cpu = 0.091012 (sec), leaf count = 39

$$\text{Solve}\left[\frac{y(x)^2 e^{-4ay(x)}}{8a} - \frac{e^{-4ay(x)}}{2x} = c_1, y(x)\right]$$

**Maple:** cpu = 0.218 (sec), leaf count = 28

$$\left\{ -C1 + \frac{-x(y(x))^2 + 4a}{e^{4ay(x)}x} = 0 \right\}$$

**2.683 ODE No. 683**

$$\frac{d}{dx}y(x) = \frac{y(x)(-1 + \ln(x(1+x)))y(x)x^4 - \ln(x(1+x))x^3}{x} = 0$$

**Mathematica:** cpu = 0.361046 (sec), leaf count = 84

$$\left\{ \left\{ y(x) \rightarrow \frac{e^{\frac{2x^3}{9} + \frac{x}{3}}}{c_1 e^{\frac{x^2}{6}} x \sqrt[3]{x+1} (x(x+1))^{\frac{x^3}{3}} + e^{\frac{x^2}{6} + \frac{1}{18}(4x^2-3x+6)x} x} \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 166

$$\left\{ y(x) = \frac{1}{x} (x(1+x))^{-\frac{x^3}{3}} e^{\frac{2x^3}{9}} e^{-\frac{x^2}{6}} e^{\frac{x}{3}} \left( x^{-\frac{x^3}{3}} (1+x)^{-\frac{x^3}{3}} e^{\frac{x(3ix^2(\operatorname{csgn}(ix(1+x)))^3 \pi - 3ix^2(\operatorname{csgn}(ix(1+x))))^2 \operatorname{csgn}(ix) \pi - 3ix^2(\operatorname{csgn}(ix(1+x)))^3 \pi - 3ix^2(\operatorname{csgn}(ix(1+x)))^3 \pi - 3ix^2(\operatorname{csgn}(ix(1+x)))^3 \pi}} \right) \right\}$$

**2.684 ODE No. 684**

$$\frac{d}{dx}y(x) = \frac{y(x) + \sqrt{(y(x))^2 + x^2 x^2}}{x} = 0$$

**Mathematica:** cpu = 0.027003 (sec), leaf count = 20

$$\left\{ \left\{ y(x) \rightarrow x \sinh \left( \frac{1}{2} (2c_1 + x^2) \right) \right\} \right\}$$

**Maple:** cpu = 0.920 (sec), leaf count = 30

$$\left\{ \ln \left( \sqrt{(y(x))^2 + x^2} + y(x) \right) - \frac{x^2}{2} - \ln(x) - \_C1 = 0 \right\}$$

**2.685 ODE No. 685**

$$\frac{d}{dx}y(x) = \frac{y(x) + \ln((1+x)(x-1))x^3 + 7 \ln((1+x)(x-1))x(y(x))^2}{x} = 0$$

**Mathematica:** cpu = 0.039005 (sec), leaf count = 87

$$\left\{ \left\{ y(x) \rightarrow \frac{x \tan \left( \frac{1}{2} (2\sqrt{7}c_1 - \sqrt{7}x^2 + \sqrt{7}x^2 \log(x-1) + \sqrt{7}x^2 \log(x+1) - \sqrt{7} \log(1-x) - \sqrt{7} \log(x+1)) \right)}{\sqrt{7}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 48

$$\left\{ y(x) = \frac{x\sqrt{7}}{7} \tan \left( \frac{(x^2 \ln((1+x)(x-1)) - x^2 - \ln((1+x)(x-1)) + 2\_C1 + 1)\sqrt{7}}{2} \right) \right\}$$

**2.686 ODE No. 686**

$$\frac{d}{dx}y(x) = \frac{x(y(x))^3 e^{2x^2}}{y(x) e^{x^2} + 1} = 0$$

**Mathematica:** cpu = 9.256675 (sec), leaf count = 68

$$\text{Solve} \left[ \log(y(x)) - 2y(x)^2 \left( \frac{\log(e^{2x^2}y(x)^2 + 2e^{x^2}y(x) + 2)}{4y(x)^2} - \frac{\tan^{-1}(e^{x^2}y(x) + 1)}{2y(x)^2} \right) = c_1, y(x) \right]$$

**Maple:** cpu = 1.482 (sec), leaf count = 85

$$\left\{ y(x) = \frac{1}{e^{x^2}} \left( -\tan \left( \text{RootOf} \left( -2x^2 - \ln \left( \frac{81(\tan(\_Z))^2}{10} + \frac{81}{10} \right) + 2 \ln(9/2 \tan(\_Z) - 9/2) + 6\_C \right) \right) \right)$$

**2.687 ODE No. 687**

$$\frac{d}{dx}y(x) = \frac{1}{x} \left( y(x) - \ln \left( \frac{1+x}{x-1} \right) x^3 + \ln \left( \frac{1+x}{x-1} \right) x(y(x))^2 \right) = 0$$

**Mathematica:** cpu = 0.064008 (sec), leaf count = 130

$$\left\{ \left\{ y(x) \rightarrow \frac{-x^2(x+1)^{x^2} e^{2c_1+2x} + x(x+1)^{x^2} e^{2c_1+2x} - x^2(x-1)^{x^2} - x(x-1)^{x^2}}{-(x+1)^{x^2} e^{2c_1+2x} + x(x+1)^{x^2} e^{2c_1+2x} - x(x-1)^{x^2} - (x-1)^{x^2}} \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 39

$$\left\{ y(x) = -\tanh \left( \frac{x^2}{2} \ln \left( \frac{1+x}{x-1} \right) - \frac{1}{2} \ln \left( \frac{1+x}{x-1} \right) + \_C1 + x - 1 \right) x \right\}$$

**2.688 ODE No. 688**

$$\frac{d}{dx}y(x) = \frac{1}{x} \left( y(x) + e^{\frac{1+x}{x-1}} x^3 + e^{\frac{1+x}{x-1}} x(y(x))^2 \right) = 0$$

**Mathematica:** cpu = 0.116515 (sec), leaf count = 78

$$\left\{ \left\{ y(x) \rightarrow x \tan \left( \frac{1}{2} \left( 2c_1 - 8e\text{Ei} \left( \frac{2}{x-1} \right) + e^{\frac{x}{x-1} + \frac{1}{x-1}} x^2 + 2e^{\frac{x}{x-1} + \frac{1}{x-1}} x - 3e^{\frac{2}{x-1} + 1} \right) \right) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 61

$$\left\{ y(x) = \tan \left( \frac{x^2}{2} e^{\frac{1+x}{x-1}} + x e^{\frac{1+x}{x-1}} + 4e\text{Ei}(1, -2(x-1)^{-1}) - \frac{3}{2} e^{\frac{1+x}{x-1}} + \_C1 \right) x \right\}$$

**2.689 ODE No. 689**

$$\frac{d}{dx}y(x) = \frac{xy(x) - y(x) - e^{1+x}x^3 + e^{1+x}x(y(x))^2}{x(x-1)} = 0$$

**Mathematica:** cpu = 0.075010 (sec), leaf count = 60

$$\left\{ \left\{ y(x) \rightarrow -\frac{x \left( e^{2c_1 + 2e^2 \text{Ei}(x-1) + 2e^{x+1}} - 1 \right)}{e^{2c_1 + 2e^2 \text{Ei}(x-1) + 2e^{x+1}} + 1} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 25

$$\{y(x) = -\tanh(e^{1+x} - e^2 \text{Ei}(1, 1-x) + \_C1)x\}$$

**2.690 ODE No. 690**

$$\frac{d}{dx}y(x) = 1/4 \frac{-x^2 + 1 + 4x^3 \sqrt{x^2 - 2x + 1 + 8y(x)}}{1+x} = 0$$

**Mathematica:** cpu = 0.319041 (sec), leaf count = 127

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{72} (-96c_1x^3 + 144c_1x^2 - 288c_1x + 288c_1 \log(4x+4) + 144c_1^2 - 528c_1 + 16x^6 - 48x^5 + 132x^4) \right\} \right\}$$

**Maple:** cpu = 0.265 (sec), leaf count = 40

$$\left\{ \_C1 + \frac{4x^3}{3} - 2x^2 + 4x - 4 \ln(1+x) - \sqrt{x^2 - 2x + 1 + 8y(x)} = 0 \right\}$$

**2.691 ODE No. 691**

$$\frac{d}{dx}y(x) = 1/2 \frac{-\sin(2y(x)) + \cos(2y(x))x^3 + x^3}{x} = 0$$

**Mathematica:** cpu = 0.080010 (sec), leaf count = 21

$$\left\{ \left\{ y(x) \rightarrow \tan^{-1} \left( \frac{2c_1 + x^4}{4x} \right) \right\} \right\}$$

**Maple:** cpu = 0.499 (sec), leaf count = 17

$$\left\{ y(x) = \arctan \left( \frac{x^4 + 8\_C1}{4x} \right) \right\}$$

**2.692 ODE No. 692**

$$\frac{d}{dx}y(x) = \frac{y(x) + x^3\sqrt{(y(x))^2 + x^2}}{x} = 0$$

**Mathematica:** cpu = 0.027003 (sec), leaf count = 20

$$\left\{ \left\{ y(x) \rightarrow x \sinh \left( \frac{1}{3}(3c_1 + x^3) \right) \right\} \right\}$$

**Maple:** cpu = 1.186 (sec), leaf count = 30

$$\left\{ \ln \left( \sqrt{(y(x))^2 + x^2} + y(x) \right) - \frac{x^3}{3} - \ln(x) - \_C1 = 0 \right\}$$

**2.693 ODE No. 693**

$$\frac{d}{dx}y(x) = (1 + (y(x))^2 e^{-2bx} + (y(x))^3 e^{-3bx}) e^{bx} = 0$$

**Mathematica:** cpu = 0.173022 (sec), leaf count = 146

$$\text{Solve} \left[ -\frac{1}{3}(9b + 29)^{2/3} \text{RootSum} \left[ \#1^3(9b + 29)^{2/3} - 9\#1b - 3\#1 + (9b + 29)^{2/3} \&, \frac{\log \left( \frac{3e^{-2bx}y(x)+e^{-bx}}{\sqrt[3]{(9b+29)e^{-3bx}}} \right) - \#1^2(- (9b + 29)^{2/3}) + \right. \right. \right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 40

$$\left\{ y(x) = \frac{1}{e^{-bx}} \text{RootOf} \left( -x - \int^{-Z} -(-a^3 + a^2 - ab + 1)^{-1} da + \_C1 \right) \right\}$$

**2.694 ODE No. 694**

$$\frac{d}{dx}y(x) = 1/2 \frac{x + 1 + 2\sqrt{4x^2y(x) + 1}x^3}{x^3(1+x)} = 0$$

**Mathematica:** cpu = 0.299538 (sec), leaf count = 66

$$\left\{ \left\{ y(x) \rightarrow \frac{-8c_1x^3 + 4c_1^2x^2 + 8c_1x^2 \log(x + 1) + 4x^4 - 8x^3 \log(x + 1) + 4x^2 \log^2(x + 1) - 1}{4x^2} \right\} \right\}$$

**Maple:** cpu = 0.234 (sec), leaf count = 30

$$\left\{ -2 \ln(1 + x) + 2x - \frac{1}{x} \sqrt{4x^2y(x) + 1} + \_C1 = 0 \right\}$$

**2.695 ODE No. 695**

$$\frac{d}{dx}y(x) = \frac{y(x) \ln(x-1) + x^4 + x^3 + x^2(y(x))^2 + x(y(x))^2}{\ln(x-1)x} = 0$$

**Mathematica:** cpu = 0.052007 (sec), leaf count = 34

$$\{ \{y(x) \rightarrow x \tan(c_1 + 2\text{Ei}(\log(x-1)) + 3\text{Ei}(2 \log(x-1)) + \text{Ei}(3 \log(x-1)))\} \}$$

**Maple:** cpu = 0.047 (sec), leaf count = 39

$$\{y(x) = \tan(-\text{Ei}(1, -3 \ln(x-1)) - 3 \text{Ei}(1, -2 \ln(x-1)) - 2 \text{Ei}(1, -\ln(x-1)) + \_C1) x\}$$

**2.696 ODE No. 696**

$$\frac{d}{dx}y(x) = \frac{y(x) \ln(x-1) + e^{1+x}x^3 + 7e^{1+x}x(y(x))^2}{\ln(x-1)x} = 0$$

**Mathematica:** cpu = 121.909981 (sec), leaf count = 50

$$\left\{ \left\{ y(x) \rightarrow \frac{x \tan\left(\sqrt{7} \int_1^x \frac{e^{K[1]+1} K[1]}{\log(K[1]-1)} dK[1] + \sqrt{7}c_1\right)}{\sqrt{7}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 32

$$\left\{ y(x) = \frac{x\sqrt{7}}{7} \tan\left(\left(e \int \frac{xe^x}{\ln(x-1)} dx + \_C1\right) \sqrt{7}\right) \right\}$$

**2.697 ODE No. 697**

$$\frac{d}{dx}y(x) = (1 + (y(x))^2)e^{-4/3x} + (y(x))^3e^{-2x}e^{2/3x} = 0$$

**Mathematica:** cpu = 0.129016 (sec), leaf count = 114

$$\text{Solve}\left[-\frac{35}{3}\text{RootSum}\left[-35\#1^3 + 9\sqrt{35}\#1 - 35\&, \frac{\log\left(\frac{3e^{-4x/3}y(x)+e^{-2x/3}}{\sqrt[3]{35}\sqrt[3]{e^{-2x}}}-\#1\right)}{3\sqrt[3]{35}-35\#1^2}\&\right], c_1 + \frac{1}{9}35^{2/3}e^{4x/3}(e^{-2x/3})^{-1}\right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 40

$$\left\{ y(x) = \text{RootOf}\left(-x + 3 \int^{-Z} (3\_a^3 + 3\_a^2 - 2\_a + 3)^{-1} d\_a + \_C1\right) \left(e^{-\frac{2x}{3}}\right)^{-1} \right\}$$

**2.698 ODE No. 698**

$$\frac{d}{dx}y(x) = (1 + (y(x))^2 e^{-2x} + (y(x))^3 e^{-3x}) e^x = 0$$

**Mathematica:** cpu = 0.132517 (sec), leaf count = 108

$$\text{Solve} \left[ -\frac{19}{3} \text{RootSum} \left[ -19\#1^3 + 6\sqrt[3]{38}\#1 - 19\&, \frac{\log \left( \frac{3e^{-2x}y(x)+e^{-x}}{\sqrt[3]{38}\sqrt[3]{e^{-3x}}} - \#1 \right)}{2\sqrt[3]{38} - 19\#1^2} \& \right] = c_1 + \frac{1}{9} 38^{2/3} e^{2x} (e^{-3x})^{2/3} \right]$$

**Maple:** cpu = 0.062 (sec), leaf count = 34

$$\left\{ y(x) = \frac{\text{RootOf} \left( -x + \int^{-Z} (_a^3 + _a^2 - _a + 1)^{-1} d_a + _C1 \right)}{e^{-x}} \right\}$$

**2.699 ODE No. 699**

$$\frac{d}{dx}y(x) = 1/3 \frac{x(-2x - 2 + 3x^2 \sqrt{x^2 + 3y(x)})}{1+x} = 0$$

**Mathematica:** cpu = 0.243531 (sec), leaf count = 101

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{48} (-24c_1x^3 + 36c_1x^2 - 72c_1x + 72c_1 \log(x+1) + 36c_1^2 + 4x^6 - 12x^5 + 33x^4 - 36x^3 - 24x^3 \log(x+1)) \right\} \right\}$$

**Maple:** cpu = 0.265 (sec), leaf count = 36

$$\left\{ -C1 + \frac{x^3}{2} - \frac{3x^2}{4} + \frac{3x}{2} - \frac{3 \ln(1+x)}{2} - \sqrt{x^2 + 3y(x)} = 0 \right\}$$

**2.700 ODE No. 700**

$$\frac{d}{dx}y(x) = \frac{1}{x(x(y(x))^2 + 1 + x)y(x)} = 0$$

**Mathematica:** cpu = 0.071009 (sec), leaf count = 76

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{2xW \left( c_1 e^{\frac{1}{2x} - \frac{1}{2}} \right) + x - 1}}{\sqrt{x}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{2xW \left( c_1 e^{\frac{1}{2x} - \frac{1}{2}} \right) + x - 1}}{\sqrt{x}} \right\} \right\}$$



**Maple:** cpu = 0.094 (sec), leaf count = 62

$$\left\{ y(x) = \frac{1}{x} \sqrt{x \left( 2 \operatorname{lambertW} \left( \frac{1}{2} \_C1 e^{-1/2 \frac{x-1}{x}} \right) x + x - 1 \right)}, y(x) = -\frac{1}{x} \sqrt{x \left( 2 \operatorname{lambertW} \left( \frac{1}{2} \_C1 e^{-1} \right)} \right)} \right.$$

## 2.701 ODE No. 701

$$\frac{d}{dx} y(x) = \frac{2 x e^x - 2 x - \ln(x) - 1 + x^4 \ln(x) + x^4 - 2 y(x) x^2 \ln(x) - 2 x^2 y(x) + (y(x))^2 \ln(x) + (y(x))}{e^x - 1}$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 4.727 (sec), leaf count = 100

$$\left\{ y(x) = 1 \left( x^2 \_C1 \left( e^{\int \left( \frac{e^x}{\ln(x)+1} - (\ln(x)+1)^{-1} \right) dx} \right)^{-2} - x^2 + \_C1 \left( e^{\int \left( \frac{e^x}{\ln(x)+1} - (\ln(x)+1)^{-1} \right) dx} \right)^{-2} + 1 \right) \left( \_C1 \right. \right.$$

## 2.702 ODE No. 702

$$\frac{d}{dx} y(x) = \frac{-y(x) e^x + x y(x) - x^3 \ln(x) - x^3 - x(y(x))^2 \ln(x) - x(y(x))^2}{(-e^x + x) x} = 0$$

**Mathematica:** cpu = 197.340559 (sec), leaf count = 36

$$\left\{ \left\{ y(x) \rightarrow x \tan \left( \int_1^x \frac{K[1](\log(K[1]) + 1)}{e^{K[1]} - K[1]} dK[1] + c_1 \right) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 35

$$\left\{ y(x) = \tan \left( \int \frac{x \ln(x)}{e^x - x} dx + \int \frac{x}{e^x - x} dx + \_C1 \right) x \right\}$$

**2.703 ODE No. 703**

$$\frac{d}{dx}y(x) = \frac{y(x)(1-x+y(x)x^2\ln(x)+x^3y(x)-x\ln(x)-x^2)}{(x-1)x} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.172 (sec), leaf count = 68

$$\left\{ y(x) = \frac{e^{dilog(x)}}{xe^x} \left( \int -\frac{e^{dilog(x)}(x+\ln(x))}{e^x(x-1)^2} dx + \_C1 x - \int -\frac{e^{dilog(x)}(x+\ln(x))}{e^x(x-1)^2} dx - \_C1 \right)^{-1} \right\}$$

**2.704 ODE No. 704**

$$\frac{d}{dx}y(x) = \frac{y(x)\ln(x)x - y(x) + 2x^5b + 2x^3a(y(x))^2}{(x\ln(x)-1)x} = 0$$

**Mathematica:** cpu = 240.336019 (sec), leaf count = 65

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt{b}x \tan\left(\sqrt{a}\sqrt{b} \int_1^x \frac{2K[1]^3}{K[1]\log(K[1])-1} dK[1] + \sqrt{a}\sqrt{b}c_1\right)}{\sqrt{a}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 45

$$\left\{ y(x) = \frac{x}{a} \tan\left(2 \int \frac{x^3}{x\ln(x)-1} dx \sqrt{ab} + 2\_C1 \sqrt{ab}\right) \sqrt{ab} \right\}$$

**2.705 ODE No. 705**

$$\frac{d}{dx}y(x) = \frac{(\ln(y(x)) + x + x^3 + x^4)y(x)}{x} = 0$$

**Mathematica:** cpu = 0.061508 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow x^x e^{c_1 x + \frac{x^4}{3} + \frac{x^3}{2}} \right\} \right\}$$

**Maple:** cpu = 0.172 (sec), leaf count = 24

$$\left\{ y(x) = e^{\frac{x^4}{3}} e^{\frac{x^3}{2}} e^{-C1 x} x^x \right\}$$

**2.706 ODE No. 706**

$$\frac{d}{dx}y(x) = -1/8(-\ln(-1 + y(x)) + \ln(1 + y(x)) + 2 \ln(x)) x(1 + y(x))^2 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.405 (sec), leaf count = 65

$$\left\{ \int_{-b}^{y(x)} \frac{1}{2-a+2} \left( -\frac{x^2(-a+1) \ln(-a-1)}{2} + \frac{x^2(-a+1) \ln(-a+1)}{2} + x^2(-a+1) \ln(x) + 4-a-4 \right) dx \right\}^{-1}$$

**2.707 ODE No. 707**

$$\frac{d}{dx}y(x) = 1/16(-\ln(-1 + y(x)) + \ln(1 + y(x)) + 2 \ln(x))^2 x(1 + y(x))^2 = 0$$

**Mathematica:** cpu = 480.133469 (sec), leaf count = 334

$$\text{Solve} \left[ \int_1^{y(x)} \left( \frac{1}{2(K[2] + 1)} + \frac{-\log^2(K[2] - 1) - \log^2(K[2] + 1)}{2(\log^2(K[2] - 1) + \log^2(K[2] + 1) + K[2](\log^2(K[2] - 1) + \log^2(K[2] + 1)))} \right) dx \right]$$

**Maple:** cpu = 0.468 (sec), leaf count = 105

$$\left\{ \int_{-b}^{y(x)} \frac{1}{4-a+4} \left( \frac{x^2(-a+1)(\ln(-a-1))^2}{4} - \left( \ln(x) + \frac{\ln(-a+1)}{2} \right) x^2(-a+1) \ln(-a-1) + \frac{x^2(-a+1)}{4} \right) dx \right\}$$

**2.708 ODE No. 708**

$$\frac{d}{dx}y(x) = \frac{-(y(x))^2 + 4ax)^3}{(-(y(x))^2 + 4ax - 1)y(x)} = 0$$

**Mathematica:** cpu = 0.299038 (sec), leaf count = 89

$$\text{Solve} \left[ 2a \left( x - \frac{\text{RootSum} \left[ -\#1^3 + 2\#1a - 2a\&, \frac{\#1a \log(-\#1 + 4ax - y(x)^2) - a \log(-\#1 + 4ax - y(x)^2)}{2a - 3\#1^2} \& \right]}{2a} \right) \right] = c_1, y(x)$$

**Maple:** cpu = 0.656 (sec), leaf count = 308

$$\left\{ \int_{-b}^x \frac{(4aa - (y(x))^2)^3}{64a^3a^3 - 48a^2a^2(y(x))^2 + 12aa(y(x))^4 - (y(x))^6 - 8aa^2 + 2a(y(x))^2 + 2a} dx \right\}$$

**2.709 ODE No. 709**

$$\frac{d}{dx}y(x) = \frac{2ax + 2a + x^3\sqrt{-(y(x))^2 + 4ax}}{(1+x)y(x)} = 0$$

**Mathematica:** cpu = 5.563707 (sec), leaf count = 217

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{6}\sqrt{144ax - 24c_1x^3 + 36c_1x^2 - 72c_1x + 72c_1\log(x+1) - 36c_1^2 - 4x^6 + 12x^5 - 33x^4 + 36x^3} \right\} \right\}$$

**Maple:** cpu = 0.203 (sec), leaf count = 39

$$\left\{ -\sqrt{-(y(x))^2 + 4ax} - \frac{x^3}{3} + \frac{x^2}{2} - x + \ln(1+x) - \_C1 = 0 \right\}$$

**2.710 ODE No. 710**

$$\frac{d}{dx}y(x) = \frac{-\ln(x) + e^{x-1} + 4x^2y(x) + 2x + 2x(y(x))^2 + 2x^3}{\ln(x) - e^{x-1}} = 0$$

**Mathematica:** cpu = 1910.257572 (sec), leaf count = 37

$$\left\{ \left\{ y(x) \rightarrow \tan \left( \int_1^x \frac{2K[5]}{e^{\frac{1}{K[5]}} - \log(K[5])} dK[5] + c_1 \right) - x \right\} \right\}$$

**Maple:** cpu = 1.685 (sec), leaf count = 35

$$\left\{ y(x) = -x + \tan \left( 2\_C1 - 2 \int \left( -\frac{\ln(x)}{x} + \frac{e^{x-1}}{x} \right)^{-1} dx \right) \right\}$$

**2.711 ODE No. 711**

$$\frac{d}{dx}y(x) = -\frac{(\ln(y(x))x + \ln(y(x)) - 1)y(x)}{1+x} = 0$$

**Mathematica:** cpu = 0.073509 (sec), leaf count = 28

$$\left\{ \left\{ y(x) \rightarrow e^{c_1e^{-x} + e^{-x-1}\text{Ei}(x+1)} \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 31

$$\left\{ y(x) = 1e^{\frac{C1}{e^x}} \left( e^{\frac{\text{Ei}(1, -1-x)}{e^x e}} \right)^{-1} \right\}$$

## 2.712 ODE No. 712

$$\frac{d}{dx}y(x) = 1/2 \frac{x^2 + 2x + 1 + 2x^3\sqrt{x^2 + 2x + 1} - 4y(x)}{1 + x} = 0$$

**Mathematica:** cpu = 0.296038 (sec), leaf count = 115

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{36} (24c_1x^3 - 36c_1x^2 + 72c_1x - 72c_1 \log(x + 1) - 36c_1^2 + 132c_1 - 4x^6 + 12x^5 - 33x^4 - 8x^3 + 2 \right. \right.$$

**Maple:** cpu = 0.265 (sec), leaf count = 38

$$\left\{ -C1 - \frac{2x^3}{3} + x^2 - 2x + 2 \ln(1 + x) - \sqrt{x^2 + 2x + 1} - 4y(x) = 0 \right\}$$

## 2.713 ODE No. 713

$$\frac{d}{dx}y(x) = \frac{-by(x)a + b^2 + ab + b^2x - ba\sqrt{x} - a^2}{a(-ay(x) + b + a + bx - a\sqrt{x})} = 0$$

**Mathematica:** cpu = 0.134517 (sec), leaf count = 649

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{a^2 \text{Root} \left[ \#1^6 (16e^{12c_1} + 16x^3) - \frac{24\#1^4x^2}{a^4} + \frac{8\#1^3x^{3/2}}{a^6} + \frac{9\#1^2x}{a^8} - \frac{6\#1\sqrt{x}}{a^{10}} + \frac{1}{a^{12}} \& , 1 \right]} - \frac{a\sqrt{x} - a -}{a} \right. \right.$$

**Maple:** cpu = 0.297 (sec), leaf count = 86

$$\left\{ y(x) = \frac{1}{2a} \left( 3 \tanh \left( \text{RootOf} \left( 729x^3(\tanh(\_Z))^6 a^6 - 2187x^3(\tanh(\_Z))^4 a^6 + 2187x^3(\tanh(\_Z))^2 a^6 \right. \right. \right.$$

## 2.714 ODE No. 714

$$\frac{d}{dx}y(x) = -\frac{y(x)(-\ln(x^{-1}) + e^x + y(x)x^2 \ln(x) + x^3y(x) - x \ln(x) - x^2)}{(-\ln(x^{-1}) + e^x)x} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.327 (sec), leaf count = 104

$$\left\{ y(x) = 1e^{\int -\frac{-x \ln(x) - x^2 + e^x - \ln(x^{-1})}{(-\ln(x^{-1}) + e^x)x} dx} \left( \int \frac{x(x + \ln(x))}{-\ln(x^{-1}) + e^x} e^{\int -\frac{-x \ln(x) - x^2 + e^x - \ln(x^{-1})}{(-\ln(x^{-1}) + e^x)x} dx} dx + \_C1 \right)^{-1} \right\}$$

**2.715 ODE No. 715**

$$\frac{d}{dx}y(x) = 1/2 \frac{-x^2 + x + 2 + 2x^3\sqrt{x^2 - 4x + 4y(x)}}{1+x} = 0$$

**Mathematica:** cpu = 0.273035 (sec), leaf count = 104

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{36}(-24c_1x^3 + 36c_1x^2 - 72c_1x + 72c_1 \log(x+1) + 36c_1^2 + 4x^6 - 12x^5 + 33x^4 - 36x^3 - 24x^3 \log(x+1)) \right\} \right\}$$

**Maple:** cpu = 0.249 (sec), leaf count = 39

$$\left\{ -C1 + \frac{2x^3}{3} - x^2 + 2x - 2 \ln(1+x) - \sqrt{x^2 - 4x + 4y(x)} = 0 \right\}$$

**2.716 ODE No. 716**

$$\frac{d}{dx}y(x) = \frac{3x^4 + 3x^3 + \sqrt{9x^4 - 4(y(x))^3}}{(1+x)(y(x))^2} = 0$$

**Mathematica:** cpu = 5.769733 (sec), leaf count = 133

$$\left\{ \left\{ y(x) \rightarrow \left(-\frac{3}{2}\right)^{2/3} \sqrt[3]{8c_1 \log(x+1) - 4c_1^2 + x^4 - 4 \log^2(x+1)} \right\}, \left\{ y(x) \rightarrow \left(\frac{3}{2}\right)^{2/3} \sqrt[3]{8c_1 \log(x+1) - 4c_1^2 + x^4 - 4 \log^2(x+1)} \right\} \right\}$$

**Maple:** cpu = 0.249 (sec), leaf count = 37

$$\left\{ \int_b^{y(x)} -a^2 \frac{1}{\sqrt{9x^4 - 4a^3}} da - \ln(1+x) - C1 = 0 \right\}$$

**2.717 ODE No. 717**

$$\frac{d}{dx}y(x) = -1/2 \frac{x^2 + x + ax + a - 2\sqrt{x^2 + 2ax + a^2 + 4y(x)}}{1+x} = 0$$

**Mathematica:** cpu = 0.337543 (sec), leaf count = 46

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4}(-a^2 - 2ax - 8c_1 \log(x+1) + 4c_1^2 - x^2 + 4 \log^2(x+1)) \right\} \right\}$$

**Maple:** cpu = 0.281 (sec), leaf count = 33

$$\left\{ -C1 + \frac{a}{2} + 2 \ln(1+x) - \sqrt{x^2 + 2ax + a^2 + 4y(x)} = 0 \right\}$$

**2.718 ODE No. 718**

$$\frac{d}{dx}y(x) = \left(1 + (y(x))^2 e^{2x^2} + (y(x))^3 e^{3x^2}\right) e^{-x^2} x = 0$$

**Mathematica:** cpu = 0.129517 (sec), leaf count = 127

$$\text{Solve} \left[ \frac{11}{3} \text{RootSum} \left[ 11\#1^3 + 15\sqrt[3]{11}\#1 + 11\&, \frac{\log \left( \frac{3e^{2x^2}xy(x)+e^{x^2}x}{\sqrt[3]{11}\sqrt[3]{e^{3x^2}x^3}} - \#1 \right)}{11\#1^2 + 5\sqrt[3]{11}} \& \right] = c_1 + \frac{11^{2/3}e^{x^2}x^3}{18\sqrt[3]{e^{3x^2}x^3}}, y(x) \right]$$

**Maple:** cpu = 0.063 (sec), leaf count = 44

$$\left\{ y(x) = -\frac{11 \text{RootOf} \left( -5x^2 + 20250 \int^{-Z} (121\_a^3 + 3375\_a - 3375)^{-1} d\_a + 6\_C1 \right) + 15}{45 e^{x^2}} \right\}$$

**2.719 ODE No. 719**

$$\frac{d}{dx}y(x) = \frac{y(x) (-e^x + \ln(2x) x^2 y(x) - \ln(2x) x)}{x e^x} = 0$$

**Mathematica:** cpu = 0.100013 (sec), leaf count = 49

$$\left\{ \left\{ y(x) \rightarrow \frac{2^{e^{-x}} x^{e^{-x}-1}}{c_1 e^{\text{Ei}(-x)} + 2^{e^{-x}} x^{e^{-x}}} \right\} \right\}$$

**Maple:** cpu = 0.110 (sec), leaf count = 57

$$\left\{ y(x) = -\frac{x^{e^{-x}} 2^{e^{-x}} e^{\text{Ei}(1,x)}}{x \left( \int x^{e^{-x}} 2^{e^{-x}} e^{\text{Ei}(1,x)} e^{-x} (\ln(2) + \ln(x)) dx + \_C1 \right)} \right\}$$

**2.720 ODE No. 720**

$$\frac{d}{dx}y(x) = \frac{x^3 \left( 3x + 3 + \sqrt{9x^4 - 4(y(x))^3} \right)}{(1+x)(y(x))^2} = 0$$

**Mathematica:** cpu = 6.127778 (sec), leaf count = 314

$$\left\{ \left\{ y(x) \rightarrow \sqrt[3]{6c_1x^3 - 9c_1x^2 + 18c_1x - 18c_1 \log(x+1) - 9c_1^2 - x^6 + 3x^5 - 6x^4 + 9x^3 + 6x^3 \log(x+1) - 9} \right\} \right\}$$

Maple: cpu = 0.171 (sec), leaf count = 48

$$\left\{ \int_{-b}^{y(x)} -a^2 \frac{1}{\sqrt{9x^4 - 4a^3}} da - \frac{x^3}{3} + \frac{x^2}{2} - x + \ln(1+x) - C1 = 0 \right\}$$

## 2.721 ODE No. 721

$$\frac{d}{dx}y(x) = 1/36 (18x^{3/2} + 36(y(x))^2 - 12x^3y(x) + x^6) \sqrt{x} = 0$$

Mathematica: cpu = 0.021003 (sec), leaf count = 27

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{c_1 - \frac{2x^{3/2}}{3}} + \frac{x^3}{6} \right\} \right\}$$

Maple: cpu = 0.062 (sec), leaf count = 19

$$\left\{ y(x) = \frac{x^3}{6} + \left( -C1 - \frac{2}{3}x^{\frac{3}{2}} \right)^{-1} \right\}$$

## 2.722 ODE No. 722

$$\frac{d}{dx}y(x) = -\frac{(y(x))^3}{(-1 + 2y(x)\ln(x) - y(x))x} = 0$$

Mathematica: cpu = 63.894114 (sec), leaf count = 491

$$\text{Solve} \left[ \sqrt[3]{-2} \left( (-2)^{2/3} - \frac{(1-2\log(x))^2 \left( -\frac{1}{(2\log(x)-1)^3} \right)^{2/3} (y(x)(5-4\log(x))+2)}{2\sqrt[3]{2}(y(x)(2\log(x)-1)-1)} \right) \left( \frac{y(x)(4\log(x)-5)-2}{\sqrt[3]{2}\sqrt[3]{-\frac{1}{(2\log(x)-1)^3}(2\log(x)-1)(y(x)(2\log(x)-1)-1)}} \right) \right]$$

Maple: cpu = 0.281 (sec), leaf count = 96

$$\left\{ y(x) = 1e^{\text{RootOf}\left(-e^{-Z}\ln\left(\frac{e^{-Z}+2}{2x^4}\right)+3e^{-Z}-C1+Ze^{-Z}+2\right)} \left( 2e^{\text{RootOf}\left(-e^{-Z}\ln\left(1/2\frac{e^{-Z}+2}{x^4}\right)+3e^{-Z}-C1+Ze^{-Z}+2\right)} \ln(x) \right) \right\}$$



**2.723 ODE No. 723**

$$\frac{d}{dx}y(x) = 2 \frac{a}{y(x) + 2a(y(x))^4 - 16a^2x(y(x))^2 + 32a^3x^2} = 0$$

**Mathematica:** cpu = 0.064508 (sec), leaf count = 663

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt[3]{-1024a^6c_1^3 + 9216a^5c_1x - 432a^2} + \sqrt{4(-64a^4c_1^2 - 192a^3x)^3 + (-1024a^6c_1^3 + 9216a^5c_1x)}}{12\sqrt[3]{2}a} \right. \right.$$

**Maple:** cpu = 0.046 (sec), leaf count = 864

$$\left\{ y(x) = \frac{1}{6a} \sqrt[3]{\left(64 - C1^3a^4 - 576 - C1 a^3x + 3 \sqrt{-12288 - C1^4a^7x + 24576 - C1^2a^6x^2 - 12288 a^5x^3 + 3}\right)} \right.$$

**2.724 ODE No. 724**

$$\frac{d}{dx}y(x) = -\frac{(y(x))^3}{(-1 + y(x) \ln(x) - y(x))x} = 0$$

**Mathematica:** cpu = 64.507191 (sec), leaf count = 420

$$\text{Solve} \left[ \frac{\sqrt[3]{-2} \left( \frac{1-y(x)(\log(x)-4)}{\sqrt[3]{2} \sqrt[3]{-\frac{1}{(\log(x)-1)^3} (\log(x)-1)(y(x)(\log(x)-1)-1)}} + (-2)^{2/3} \right)}{\left( \frac{2^{2/3}(y(x)(\log(x)-4)-1)}{\sqrt[3]{-\frac{1}{(\log(x)-1)^3} (\log(x)-1)(y(x)(\log(x)-1)-1)}} + (-2)^{2/3} \right)} \right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 18

$$\left\{ y(x) = (-\text{lambertW}(-C1 e^{-2}x) + \ln(x) - 2)^{-1} \right\}$$

**2.725 ODE No. 725**

$$\frac{d}{dx}y(x) = \frac{-\ln(x) + 2 \ln(2x)xy(x) + \ln(2x) + \ln(2x)(y(x))^2 + \ln(2x)x^2}{\ln(x)} = 0$$

**Mathematica:** cpu = 0.265034 (sec), leaf count = 19

$$\{ \{ y(x) \rightarrow \tan(c_1 + \log(2)\text{li}(x) + x) - x \} \}$$

**Maple:** cpu = 0.561 (sec), leaf count = 25

$$\{ y(x) = -x - \tan(\ln(2) Ei(1, -\ln(x)) + \_C1 - x) \}$$

**2.726 ODE No. 726**

$$\frac{d}{dx}y(x) = -\frac{by(x)a - bc + b^2x + ba\sqrt{x} - a^2}{a(ay(x) - c + bx + a\sqrt{x})} = 0$$

**Mathematica:** cpu = 0.082010 (sec), leaf count = 625

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{a^2 \text{Root} \left[ \#1^6 (16e^{12c_1} + 16x^3) - \frac{24\#1^4 x^2}{a^4} + \frac{8\#1^3 x^{3/2}}{a^6} + \frac{9\#1^2 x}{a^8} - \frac{6\#1\sqrt{x}}{a^{10}} + \frac{1}{a^{12}} \&x, 1 \right]} - \frac{a\sqrt{x} + bx}{a} \right. \right.$$

**Maple:** cpu = 0.202 (sec), leaf count = 83

$$\left\{ y(x) = \frac{1}{2a} \left( 3 \tanh \left( \text{RootOf} \left( -729 x^3 (\tanh(\_Z))^6 a^6 + 2187 x^3 (\tanh(\_Z))^4 a^6 - 2187 x^3 (\tanh(\_Z))^2 \right) \right) \right. \right.$$

**2.727 ODE No. 727**

$$\frac{d}{dx}y(x) = \frac{(2x + 2 + y(x))y(x)}{(\ln(y(x)) + 2x - 1)(1 + x)} = 0$$

**Mathematica:** cpu = 0.495063 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow \frac{W(e^{-2x}(c_1 + \log(x+1)))}{c_1 + \log(x+1)} \right\} \right\}$$

**Maple:** cpu = 0.187 (sec), leaf count = 25

$$\left\{ y(x) = e^{-\text{lambertW}((\ln(1+x) - \_C1)e^{-2x}) - 2x} \right\}$$

**2.728 ODE No. 728**

$$\frac{d}{dx}y(x) = \frac{(x^3 + 3(y(x))^2)y(x)}{(6(y(x))^2 + x)x} = 0$$

**Mathematica:** cpu = 0.434555 (sec), leaf count = 72

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{x}\sqrt{W\left(\frac{6e^{2c_1+x^2}}{x}\right)}}{\sqrt{6}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{x}\sqrt{W\left(\frac{6e^{2c_1+x^2}}{x}\right)}}{\sqrt{6}} \right\} \right\}$$

**Maple:** cpu = 0.234 (sec), leaf count = 50

$$\left\{ \left( (y(x))^{-2} + 6x^{-1} \right)^{-1} = \frac{x}{54} \left( e^{\text{RootOf}\left(e^{-Z}x^2 - e^{-Z} \ln\left(\frac{e^{-Z}+9}{2}\right) + 3e^{-Z} - C1 + Z e^{-Z} + 9\right)} + 9 \right) \right\}$$

**2.729 ODE No. 729**

$$\frac{d}{dx}y(x) = \frac{y(x)(x-y(x))}{x(x-(y(x))^3)} = 0$$

**Mathematica:** cpu = 0.355045 (sec), leaf count = 327

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{2}(6c_1 - 6 \log(x))}{3\sqrt[3]{\sqrt{4(6c_1 - 6 \log(x))^3 + 2916x^2} + 54x}} - \frac{\sqrt[3]{\sqrt{4(6c_1 - 6 \log(x))^3 + 2916x^2} + 54x}}{3\sqrt[3]{2}} \right\}, \left\{ y(x) \rightarrow \dots \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 497

$$\left\{ y(x) = \frac{1}{3} \sqrt[3]{-27x + 3\sqrt{-24(\ln(x))^3 + 72(\ln(x))^2 - C1 - 72\ln(x) - C1^2 + 24 - C1^3 + 81x^2} - 3} - \dots \right\}$$

**2.730 ODE No. 730**

$$\frac{d}{dx}y(x) = 1/4 \frac{\left(2(y(x))^{3/2} - 3e^x\right)^3 e^x}{\left(2(y(x))^{3/2} - 3e^x + 2\right) \sqrt{y(x)}} = 0$$

**Mathematica:** cpu = 33.979315 (sec), leaf count = 55

$$\text{DSolve}\left[y'(x) = \frac{e^x(2y(x)^{3/2} - 3e^x)^3}{4\sqrt{y(x)}(2y(x)^{3/2} - 3e^x + 2)}, y(x), x\right]$$

**Maple:** cpu = 1.342 (sec), leaf count = 49

$$\left\{ e^x - \int^{(y(x))^{3/2} - \frac{3e^x}{2}} \frac{2\_a}{3\_a^3 - 3\_a - 3} + \frac{2}{3\_a^3 - 3\_a - 3} d\_a - \_C1 = 0 \right\}$$

**2.731 ODE No. 731**

$$\frac{d}{dx}y(x) = \frac{1 + 2y(x)}{x(-2 + x(y(x))^2 + 2x(y(x))^3)} = 0$$

**Mathematica:** cpu = 0.197525 (sec), leaf count = 47

$$\text{Solve}\left[\frac{1}{64}(-4y(x)^2 + 4y(x) - 2\log(8y(x) + 4) + 3) - \frac{1}{4x(2y(x) + 1)} = c_1, y(x)\right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 42

$$\left\{ y(x) = \frac{e^{\text{RootOf}(x(e^{-Z})^3 - 4x(e^{-Z})^2 + 16\_C1xe^{-Z} + 2\_Zxe^{-Z} + 3xe^{-Z} + 16)}}{2} - \frac{1}{2} \right\}$$

**2.732 ODE No. 732**

$$\frac{d}{dx}y(x) = 1/2 \frac{-x^2 - x - ax - a + 2x^3\sqrt{x^2 + 2ax + a^2} + 4y(x)}{1 + x} = 0$$

**Mathematica:** cpu = 0.497563 (sec), leaf count = 110

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{36}(-9a^2 - 18ax - 24c_1x^3 + 36c_1x^2 - 72c_1x + 72c_1\log(x + 1) + 36c_1^2 + 4x^6 - 12x^5 + 33x^4 - \right. \right.$$

**Maple:** cpu = 0.281 (sec), leaf count = 43

$$\left\{ \_C1 + \frac{2x^3}{3} - x^2 + 2x - 2\ln(1 + x) - \sqrt{x^2 + 2ax + a^2} + 4y(x) = 0 \right\}$$

**2.733 ODE No. 733**

$$\frac{d}{dx}y(x) = \frac{2x \sin(x) - \ln(2x) + \ln(2x)x^4 - 2\ln(2x)x^2y(x) + \ln(2x)(y(x))^2}{\sin(x)} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

**2.734 ODE No. 734**

$$\frac{d}{dx}y(x) = \frac{(-\ln(y(x))x - \ln(y(x)) + x^3)y(x)}{1+x} = 0$$

**Mathematica:** cpu = 0.121515 (sec), leaf count = 37

$$\left\{ \left\{ y(x) \rightarrow \exp(-c_1 e^{-x} - e^{-x-1} \text{Ei}(x+1) + x^2 - 3x + 4) \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 39

$$\left\{ y(x) = \frac{e^{x^2} e^4}{(e^x)^3} e^{-\frac{C1}{e^x}} e^{\frac{\text{Ei}(1, -1-x)}{e^x e}} \right\}$$

**2.735 ODE No. 735**

$$\frac{d}{dx}y(x) = \frac{(2y(x)\ln(x) - 1)^3}{(-1 + 2y(x)\ln(x) - y(x))x} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.062 (sec), leaf count = 104

$$\left\{ y(x) = \frac{71 \text{RootOf}(-82944 \int^{-Z}(5041\_a^3 - 27648\_a + 27648)^{-1} d\_a - 16 \ln(x) + 3\_C1)}{142 \ln(x) \text{RootOf}(-82944 \int^{-Z}(5041\_a^3 - 27648\_a + 27648)^{-1} d\_a - 16 \ln(x) + 3\_C1)} \right\}$$

**2.736 ODE No. 736**

$$\frac{d}{dx}y(x) = \frac{2x^2 + 2x + x^4 - 2x^2y(x) - 1 + (y(x))^2}{1+x} = 0$$

**Mathematica:** cpu = 0.106514 (sec), leaf count = 31

$$\left\{ \left\{ y(x) \rightarrow \frac{(x+1)^2}{c_1 - \frac{x^2}{2} - x} + x^2 + 1 \right\} \right\}$$

**Maple:** cpu = 0.140 (sec), leaf count = 47

$$\left\{ y(x) = \frac{-C1 x^4 + 2\_C1 x^3 - x^2\_C1 - 2\_C1 x + x^2 - 2\_C1 + 1}{x^2\_C1 + 2\_C1 x + 1} \right\}$$

**2.737 ODE No. 737**

$$\frac{d}{dx}y(x) = \frac{x(-1 + x - 2xy(x) + 2x^3)}{x^2 - y(x)} = 0$$

**Mathematica:** cpu = 0.033504 (sec), leaf count = 36

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( W \left( -e^{c_1 + \frac{4x^3}{3} - 2x^2 - 1} \right) + 1 \right) + x^2 \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 29

$$\left\{ y(x) = x^2 + \frac{1}{2} \text{lambertW} \left( -2 \frac{e^{4/3 x^3} - C1 e^{-1}}{(e^{x^2})^2} \right) + \frac{1}{2} \right\}$$

**2.738 ODE No. 738**

$$\frac{d}{dx}y(x) = 2 \frac{a}{-x^2y(x) + 2a(y(x))^4 x^2 - 16a^2x(y(x))^2 + 32a^3} = 0$$

**Mathematica:** cpu = 0.515566 (sec), leaf count = 1347

$$\left\{ \left\{ y(x) \rightarrow -\frac{4a + e^{c_1}}{12a} + \sqrt[3]{\frac{4608x^2a^4 - 128x^3a^3 + 1152e^{c_1}x^2a^3 - 96e^{c_1}x^3a^2 - 432x^3a^2 - 24e^{2c_1}x^3a - 2e^{3c_1}}{12a^3}} \right\} \right\}$$

**Maple:** cpu = 0.561 (sec), leaf count = 1096

$$\left\{ y(x) = \frac{1}{12\_C1\ ax} \sqrt[3]{\left(-216\_C1^3 a^2 x + 576 a^3\_C1^2 + 12 \sqrt{-\frac{49152\_C1^4 a^7 - 324\_C1^4 a^2 x^3 + 1728}{\dots}}}\right)} \right.$$

**2.739 ODE No. 739**

$$\frac{d}{dx} y(x) = \frac{1 + 2y(x)}{x(-2 + xy(x) + 2x(y(x))^2)} = 0$$

**Mathematica:** cpu = 0.131517 (sec), leaf count = 39

$$\text{Solve}\left[\frac{1}{8}(-2y(x) + \log(4y(x) + 2) - 1) - \frac{1}{2x(2y(x) + 1)} = c_1, y(x)\right]$$

**Maple:** cpu = 0.140 (sec), leaf count = 35

$$\left\{ y(x) = \frac{e^{\text{RootOf}(x(e^{-z})^2 + 2\_C1 x e^{-z} - z x e^{-z} - x e^{-z} + 4)}}{2} - \frac{1}{2} \right\}$$

**2.740 ODE No. 740**

$$\frac{d}{dx} y(x) = \frac{x + (y(x))^4 - 2x^2(y(x))^2 + x^4}{y(x)} = 0$$

**Mathematica:** cpu = 0.067509 (sec), leaf count = 74

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{2c_1 x^2 + 2x^3 - 1}}{\sqrt{2}\sqrt{c_1 + x}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{2c_1 x^2 + 2x^3 - 1}}{\sqrt{2}\sqrt{c_1 + x}} \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 72

$$\left\{ y(x) = \frac{\sqrt{2}}{2x + 2\_C1} \sqrt{(x +\_C1)(2x^2\_C1 + 2x^3 - 1)}, y(x) = -\frac{\sqrt{2}}{2x + 2\_C1} \sqrt{(x +\_C1)(2x^2\_C1 - \dots)} \right.$$

**2.741 ODE No. 741**

$$\frac{d}{dx}y(x) = \frac{(a(y(x))^2 + bx^2)^3 x}{a^{5/2} (a(y(x))^2 + bx^2 + a) y(x)} = 0$$

**Mathematica:** cpu = 3.705971 (sec), leaf count = 175

$$\text{Solve}\left[\frac{1}{2}\left(x^2 - a^{3/2}\text{RootSum}\left[\#1^3b^3 + 3\#1^2ab^2y(x)^2 + \#1a^{3/2}b^2 + 3\#1a^2by(x)^4 + a^{5/2}by(x)^2 + a^{5/2}b + a\right]\right)\right]$$

**Maple:** cpu = 0.749 (sec), leaf count = 400

$$\left\{ \int_{-b}^x \frac{(b - a^2 + a(y(x))^2)^3 - a}{a^3} \left( (y(x))^6 a^3 + 3 a^2 b - a^2 (y(x))^4 + 3 a b^2 - a^4 (y(x))^2 + b^3 - a^6 + a^{5/2} b (y(x))^2 + a^{3/2} \right) dx \right\}$$

**2.742 ODE No. 742**

$$\frac{d}{dx}y(x) = -\frac{\cos(y(x))(x - \cos(y(x)) + 1)}{(x \sin(y(x)) - 1)(1 + x)} = 0$$

**Mathematica:** cpu = 5.755231 (sec), leaf count = 3913

$$\left\{ \left\{ y(x) \rightarrow -\sec^{-1} \left( \frac{c_1 x^3}{x^2 - 1} + \frac{\log(x + 1)x^3}{x^2 - 1} - \frac{c_1^3 x^3}{(x^2 - 1)(c_1^2 + 2 \log(x + 1)c_1 + \log^2(x + 1) + 1)} - \frac{1}{x^2 - 1} \right) \right\} \right\}$$

**Maple:** cpu = 1.185 (sec), leaf count = 259

$$\left\{ y(x) = \arctan \left( -\frac{-\ln(1 + x) + C1}{-C1^2 - 2 C1 \ln(1 + x) + (\ln(1 + x))^2 + 1} \left( -\ln(1 + x)x + C1 x + \sqrt{(\ln(1 + x))^2 + 1} \right) \right) \right\}$$

**2.743 ODE No. 743**

$$\frac{d}{dx}y(x) = \frac{-i/32(8ix + 16(y(x))^4 + 8x^2(y(x))^2 + x^4)}{y(x)} = 0$$

**Mathematica:** cpu = 32.841170 (sec), leaf count = 43

$$\text{DSolve}\left[y'(x) = -\frac{i(x^4 + 8x^2y(x)^2 + 16y(x)^4 + 8ix)}{32y(x)}, y(x), x\right]$$

**Maple:** cpu = 0.328 (sec), leaf count = 269

$$\left\{ y(x) = -i \sqrt{-i \left( -2 \left( -\sqrt{3} + i \right) -C1 \text{Ai}^{(1)} \left( -1/2 \left( \sqrt{3} - i \right) x \right) + \left( -2i + 2\sqrt{3} \right) \text{Bi}^{(1)} \left( -\frac{(\sqrt{3} - i)x}{2} \right) \right)} \right\}$$



**2.744 ODE No. 744**

$$\frac{d}{dx}y(x) = \frac{x}{-y(x) + x^4 + 2x^2(y(x))^2 + (y(x))^4} = 0$$

**Mathematica:** cpu = 0.043006 (sec), leaf count = 510

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{144c_1x^2 + \sqrt{4(12x^2 - 4c_1^2)^3 + (144c_1x^2 + 16c_1^3 - 108)^2 + 16c_1^3 - 108}}}{6\sqrt[3]{2}} - \frac{1}{3 \cdot 2^{2/3} \sqrt[3]{144c_1x^2 - \dots}} \right. \right.$$

**Maple:** cpu = 0.156 (sec), leaf count = 621

$$\left\{ y(x) = \frac{1}{12} \left( -2\_C1 \sqrt[3]{-36x^2\_C1 - 54 -\_C1^3} + 6 \sqrt{48x^6 + 24x^4\_C1^2 + (3\_C1^4 + 108\_C1)x^2 - \dots} \right) \right.$$

**2.745 ODE No. 745**

$$\frac{d}{dx}y(x) = \frac{(-1 + y(x) \ln(x))^3}{(-1 + y(x) \ln(x) - y(x))x} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.063 (sec), leaf count = 104

$$\left\{ y(x) = \frac{47 \text{RootOf}(-27783 \int^{-Z} (2209\_a^3 - 9261\_a - 9261) d\_a - 7 \ln(x) + 3\_C1)}{47 \ln(x) \text{RootOf}(-27783 \int^{-Z} (2209\_a^3 - 9261\_a + 9261) d\_a - 7 \ln(x) + 3\_C1)} - 84 \right.$$

**2.746 ODE No. 746**

$$\frac{d}{dx}y(x) = \frac{-i(ix + x^4 + 2x^2(y(x))^2 + (y(x))^4)}{y(x)} = 0$$

**Mathematica:** cpu = 31.239967 (sec), leaf count = 39

$$\text{DSolve}\left[y'(x) = -\frac{i(x^4 + 2x^2y(x)^2 + y(x)^4 + ix)}{y(x)}, y(x), x\right]$$

**Maple:** cpu = 0.312 (sec), leaf count = 243

$$\left\{ y(x) = \frac{-i\sqrt{2}}{2 \operatorname{Ai}(-\sqrt[3]{-8ix})_C1 + 2 \operatorname{Bi}(-\sqrt[3]{-8ix})} \sqrt{-2i \left( \operatorname{Ai}(-\sqrt[3]{-8ix})_C1 + \operatorname{Bi}(-\sqrt[3]{-8ix}) \right)} \left( -\dots \right) \right\}$$

**2.747 ODE No. 747**

$$\frac{d}{dx} y(x) = -\frac{y(x) (\tan(x) + \ln(2x)x - \ln(2x)x^2 y(x))}{x \tan(x)} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.281 (sec), leaf count = 69

$$\left\{ y(x) = 1e^{\int -\frac{x \ln(x) + x \ln(2) + \tan(x)}{x \tan(x)} dx} \left( \int -\frac{x(\ln(2) + \ln(x))}{\tan(x)} e^{\int -\frac{x \ln(x) + x \ln(2) + \tan(x)}{x \tan(x)} dx} dx + C1 \right)^{-1} \right\}$$

**2.748 ODE No. 748**

$$\frac{d}{dx} y(x) = \frac{y(x) (y(x) + x)}{x (x + (y(x))^3)} = 0$$

**Mathematica:** cpu = 0.382549 (sec), leaf count = 285

$$\left\{ \left\{ y(x) \rightarrow \frac{2\sqrt[3]{2}(c_1 + \log(x))}{\sqrt[3]{\sqrt{2916x^2 - 864(c_1 + \log(x))^3 + 54x}}} + \frac{\sqrt[3]{\sqrt{2916x^2 - 864(c_1 + \log(x))^3 + 54x}}}{3\sqrt[3]{2}} \right\}, \left\{ y(x) \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 497

$$\left\{ y(x) = \frac{1}{3} \sqrt[3]{27x + 3 \sqrt{-24 C1^3 - 72 \ln(x) C1^2 - 72 (\ln(x))^2 C1 - 24 (\ln(x))^3 + 81x^2}} - 3 \sqrt[3]{27} \right\}$$

**2.749 ODE No. 749**

$$\frac{d}{dx}y(x) = \frac{(x - y(x))^2 (y(x) + x)^2 x}{y(x)} = 0$$

**Mathematica:** cpu = 0.106013 (sec), leaf count = 126

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{x^2 e^{4c_1+2x^2} - e^{4c_1+2x^2} + x^2 + 1}}{\sqrt{e^{4c_1+2x^2} + 1}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{x^2 e^{4c_1+2x^2} - e^{4c_1+2x^2} + x^2 + 1}}{\sqrt{e^{4c_1+2x^2} + 1}} \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 192

$$\left\{ y(x) = 1 \sqrt{\left( -C1 e^{-\frac{x^2(x^2-2)}{2}} + e^{-\frac{x^2(x^2+2)}{2}} \right) \left( (x^2+1) e^{-\frac{x^2(x^2+2)}{2}} + -C1 (x^2-1) e^{-\frac{x^2(x^2-2)}{2}} \right) \left( -C1 e^{-\frac{x^2}{2}} \right)} \right\}$$

**2.750 ODE No. 750**

$$\frac{d}{dx}y(x) = \frac{(x^2 + 3(y(x))^2) y(x)}{(6(y(x))^2 + x)x} = 0$$

**Mathematica:** cpu = 0.422554 (sec), leaf count = 72

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{x} \sqrt{W\left(\frac{6e^{2c_1+2x}}{x}\right)}}{\sqrt{6}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{x} \sqrt{W\left(\frac{6e^{2c_1+2x}}{x}\right)}}{\sqrt{6}} \right\} \right\}$$

**Maple:** cpu = 0.234 (sec), leaf count = 49

$$\left\{ \left( (y(x))^{-2} + 6x^{-1} \right)^{-1} = \frac{x}{54} \left( e^{\text{RootOf}\left(-e^{-Z} \ln\left(\frac{(e^{-Z}+9)x}{2}\right) + 3e^{-Z} - C1 + -Ze^{-Z} + 2xe^{-Z} + 9\right)} + 9 \right) \right\}$$

**2.751 ODE No. 751**

$$\frac{d}{dx}y(x) = \frac{(\ln(y(x))x + \ln(y(x)) + x^4)y(x)}{x(1+x)} = 0$$

**Mathematica:** cpu = 0.078010 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow (x+1)^x e^{c_1 x + \frac{x^3}{2} - x^2} \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 26

$$\left\{ y(x) = \frac{(1+x)^x e^{-C_1 x} e^{\frac{x^3}{2}}}{e^{x^2}} \right\}$$

## 2.752 ODE No. 752

$$\frac{d}{dx} y(x) = \frac{\cos(y(x)) (\cos(y(x)) x^3 - x - 1)}{(x \sin(y(x)) - 1) (1 + x)} = 0$$

**Mathematica:** cpu = 19.954034 (sec), leaf count = 39

$$\text{DSolve}\left[ y'(x) = \frac{\cos(y(x)) (x^3 \cos(y(x)) - x - 1)}{(x + 1)(x \sin(y(x)) - 1)}, y(x), x \right]$$

**Maple:** cpu = 1.060 (sec), leaf count = 874

$$\left\{ y(x) = \arctan \left( -\frac{-2x^3 + 3x^2 - 4x^6 - 12x^5 + 24C_1x^3 + 33x^4 - 24 \ln(1+x)x^3 - 36x^2C_1 - 36x^3 + 36 \ln(1+x)}{4x^6 - 12x^5 + 24C_1x^3 + 33x^4 - 24 \ln(1+x)x^3 - 36x^2C_1 - 36x^3 + 36 \ln(1+x)} \right) \right\}$$

## 2.753 ODE No. 753

$$\frac{d}{dx} y(x) = \frac{(x + 1 + x^4 \ln(y(x))) y(x) \ln(y(x))}{x(1+x)} = 0$$

**Mathematica:** cpu = 0.109014 (sec), leaf count = 41

$$\left\{ \left\{ y(x) \rightarrow \exp \left( -\frac{12x}{-12c_1 + 3x^4 - 4x^3 + 6x^2 - 12x + 12 \log(x+1)} \right) \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 38

$$\left\{ y(x) = e^{-12 \frac{x}{3x^4 - 4x^3 + 6x^2 + 12 \ln(1+x) - 12C_1 - 12x}} \right\}$$

**2.754 ODE No. 754**

$$\frac{d}{dx}y(x) = \frac{xy(x) + x^3 + x(y(x))^2 + (y(x))^3}{x^2} = 0$$

**Mathematica:** cpu = 0.027003 (sec), leaf count = 47

$$\text{Solve} \left[ \text{RootSum} \left[ \#1^3 + \#1^2 + 1 \&, \frac{\log\left(\frac{y(x)}{x} - \#1\right)}{3\#1^2 + 2\#1} \& \right] = c_1 + x, y(x) \right]$$

**Maple:** cpu = 0.016 (sec), leaf count = 26

$$\left\{ y(x) = \text{RootOf} \left( - \int^{-Z} (-a^3 + -a^2 + 1)^{-1} d_a + x + -C1 \right) x \right\}$$

**2.755 ODE No. 755**

$$\frac{d}{dx}y(x) = \frac{(y(x))^{3/2}}{(y(x))^{3/2} + x^2 - 2xy(x) + (y(x))^2} = 0$$

**Mathematica:** cpu = 0.178023 (sec), leaf count = 2633

$$\left\{ \left\{ y(x) \rightarrow \frac{2}{3}(x + e^{c_1} + 2e^{2c_1}) - \frac{1}{3}\sqrt[3]{x^3 + 3e^{c_1}x^2 - 12e^{2c_1}x^2 + 3e^{2c_1}x + 12e^{3c_1}x + 48e^{4c_1}x + e^{3c_1} - 30e^{4c_1}} \right. \right.$$

**Maple:** cpu = 0.094 (sec), leaf count = 44

$$\left\{ 2 \frac{\sqrt{y(x)}}{y(x) - x} + (y(x) - x)^{-1} - 2 \frac{x}{\sqrt{y(x)}(y(x) - x)} - C1 = 0 \right\}$$

**2.756 ODE No. 756**

$$\frac{d}{dx}y(x) = \frac{2x^3y(x) + x^6 + x^2(y(x))^2 + (y(x))^3}{x^4} = 0$$

**Mathematica:** cpu = 0.080010 (sec), leaf count = 95

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29 \&, \frac{\log\left(\frac{\frac{3y(x)}{x^4} + \frac{1}{x^2}}{\sqrt[3]{29}\sqrt[3]{\frac{1}{x^6}}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2} \& \right] = c_1 + \frac{1}{9}29^{2/3} \left(\frac{1}{x^6}\right)^{2/3} x^5, y(x) \right]$$

**Maple:** cpu = 0.031 (sec), leaf count = 37

$$\left\{ y(x) = \frac{\left(-3 + 29 \operatorname{RootOf}\left(-81 \int^{-Z} (841_a^3 - 27_a + 27)^{-1} d_a + x + 3_{C1}\right)\right) x^2}{9} \right\}$$

## 2.757 ODE No. 757

$$\frac{d}{dx} y(x) = \frac{-4xy(x) + x^3 + 2x^2 - 4x - 8}{-8y(x) + 2x^2 + 4x - 8} = 0$$

**Mathematica:** cpu = 0.030004 (sec), leaf count = 36

$$\left\{ \left\{ y(x) \rightarrow 2(W(-e^{c_1 - \frac{x}{4}}) + 1) + \frac{1}{4}(x^2 + 2x - 4) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 26

$$\left\{ y(x) = \frac{x^2}{4} + 2 \operatorname{lambertW}\left(\frac{1}{2} C_1 e^{-x/4} e^{-1/2}\right) + \frac{x}{2} + 1 \right\}$$

## 2.758 ODE No. 758

$$\frac{d}{dx} y(x) = \frac{(2x + 2 + x^3 y(x)) y(x)}{(\ln(y(x)) + 2x - 1)(1 + x)} = 0$$

**Mathematica:** cpu = 1.093639 (sec), leaf count = 459

$$\left\{ \left\{ y(x) \rightarrow \frac{6W\left(-\frac{1}{6} \sqrt[6]{e^{-12x} (6c_1 + 2x^3 - 3x^2 + 6x - 6 \log(x+1))^6}\right)}{6c_1 + 2x^3 - 3x^2 + 6x - 6 \log(x+1)} \right\}, \left\{ y(x) \rightarrow \frac{6W\left(\frac{1}{6} \sqrt[6]{e^{-12x} (6c_1 + 2x^3 - 3x^2 + 6x - 6 \log(x+1))^6}\right)}{6c_1 + 2x^3 - 3x^2 + 6x - 6 \log(x+1)} \right\} \right\}$$

**Maple:** cpu = 0.187 (sec), leaf count = 41

$$\left\{ y(x) = e^{-\operatorname{lambertW}\left(-\frac{(-2x^3 + 3x^2 + 6 \ln(1+x) + 6_{C1} - 6x)e^{-2x}}{6}\right) - 2x} \right\}$$

**2.759 ODE No. 759**

$$\frac{d}{dx}y(x) = \frac{-\frac{i}{243}(54ix^2 + 81(y(x))^4 + 18x^4(y(x))^2 + x^8)x}{y(x)} = 0$$

**Mathematica:** cpu = 40.967202 (sec), leaf count = 46

$$\text{DSolve}\left[y'(x) = -\frac{ix(x^8 + 18x^4y(x)^2 + 54ix^2 + 81y(x)^4)}{243y(x)}, y(x), x\right]$$

**Maple:** cpu = 0.452 (sec), leaf count = 315

$$\left\{y(x) = \frac{-\frac{1}{6} - \frac{i}{6}}{x} \sqrt{(1-i) \left( J_{\frac{1}{3}} \left( \left( \frac{2}{27} - \frac{2i}{27} \right) \sqrt{6}x^3 \right) - C1 + Y_{\frac{1}{3}} \left( \left( \frac{2}{27} - \frac{2i}{27} \right) \sqrt{6}x^3 \right) \right)} \left( -C1 (-27 - 27i) \right) \right\}$$

**2.760 ODE No. 760**

$$\frac{d}{dx}y(x) = \frac{(x(y(x))^2 + 1)^3}{x^4(x(y(x))^2 + 1 + x)y(x)} = 0$$

**Mathematica:** cpu = 1.559198 (sec), leaf count = 112

$$\text{Solve}\left[2\left(\frac{1}{10}\log(2x^2y(x)^4 + 2x^2y(x)^2 + x^2 + 4xy(x)^2 + 2x + 2) - \frac{1}{5}\log(xy(x)^2 - x + 1) - \frac{1}{10}\tan^{-1}(2x)\right)\right]$$

**Maple:** cpu = 1.685 (sec), leaf count = 475

$$\left\{\frac{\ln(x(y(x))^2 - x + 1)(y(x))^2}{5(y(x))^2 - 5} - \frac{\ln(x(y(x))^2 - x + 1)}{5(y(x))^2 - 5} + \frac{1}{2x} - \frac{\ln(2x^2(y(x))^4 + 2x^2(y(x))^2 + 4x(y(x)))}{10(y(x))^4 + 10(y(x))}\right\}$$

**2.761 ODE No. 761**

$$\frac{d}{dx}y(x) = \frac{-4xy(x) - x^3 + 4x^2 - 4x + 8}{8y(x) + 2x^2 - 8x + 8} = 0$$

**Mathematica:** cpu = 0.027504 (sec), leaf count = 33

$$\left\{\left\{y(x) \rightarrow W(-e^{c1-x-1}) + \frac{1}{4}(-x^2 + 4x - 4) + 1\right\}\right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 18

$$\left\{y(x) = -\frac{x^2}{4} + \text{lambertW}\left(\frac{-C1}{e^x}\right) + x\right\}$$

**2.762 ODE No. 762**

$$\frac{d}{dx}y(x) = -\frac{(\ln(y(x))x + \ln(y(x)) - x)y(x)}{x(1+x)} = 0$$

**Mathematica:** cpu = 0.060508 (sec), leaf count = 26

$$\left\{ \left\{ y(x) \rightarrow (x+1)^{-1/x} e^{1-\frac{c_1}{x}} \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 22

$$\left\{ y(x) = \frac{e}{\sqrt[x]{1+x}} e^{-\frac{C1}{x}} \right\}$$

**2.763 ODE No. 763**

$$\frac{d}{dx}y(x) = \frac{(\ln(y(x))x + \ln(y(x)) + x)y(x)}{x(1+x)} = 0$$

**Mathematica:** cpu = 0.063508 (sec), leaf count = 22

$$\left\{ \left\{ y(x) \rightarrow x^x (x+1)^{-x} e^{c_1 x} \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 14

$$\left\{ y(x) = \left( \frac{C1 x}{1+x} \right)^x \right\}$$

**2.764 ODE No. 764**

$$\frac{d}{dx}y(x) = \frac{(-\ln(y(x))x - \ln(y(x)) + x^4)y(x)}{x(1+x)} = 0$$

**Mathematica:** cpu = 0.104013 (sec), leaf count = 50

$$\left\{ \left\{ y(x) \rightarrow (x+1)^{\frac{1}{x}} e^{-\frac{c_1}{x} + \frac{x^3}{4} - \frac{x^2}{3} + \frac{x}{2} - \frac{25}{12x} - 1} \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 36

$$\left\{ y(x) = e^{\frac{x^3}{4}} e^{-\frac{x^2}{3}} e^{\frac{x}{2}} \sqrt{1+x} e^{-\frac{C1}{x}} e^{-1} \right\}$$



**2.765 ODE No. 765**

$$\frac{d}{dx}y(x) = \frac{y(x)}{x} \left( -1 - \ln \left( \frac{(1+x)(x-1)}{x} \right) + \ln \left( \frac{(1+x)(x-1)}{x} \right) xy(x) \right) = 0$$

**Mathematica:** cpu = 135.603219 (sec), leaf count = 128

$$\left\{ \left\{ y(x) \rightarrow \frac{e^{\text{Li}_2(-x)+\text{Li}_2(x)} x^{\log(1-x)-\frac{\log(x)}{2}+\log(x+1)-\log(x)}}{c_1 - \int_1^x \log \left( \frac{(K[1]-1)(K[1]+1)}{K[1]} \right) \exp \left( \text{Li}_2(-K[1]) + \text{Li}_2(K[1]) - \frac{1}{2} \log(K[1]) \left( -2 \log(1 - K[1]) + \dots \right) \right)} \right. \right.$$

**Maple:** cpu = 0.110 (sec), leaf count = 106

$$\left\{ y(x) = \frac{e^{\text{dilog}(1+x)} x^{\ln(1+x)}}{e^{\text{dilog}(x)} x} e^{-\frac{(\ln(x))^2}{2}} \left( \int -\frac{e^{\text{dilog}(1+x)} x^{\ln(1+x)}}{e^{\text{dilog}(x)} x} e^{-\frac{(\ln(x))^2}{2}} \ln \left( \frac{(1+x)(x-1)}{x} \right) \left( x^{\ln \left( \frac{(1+x)(x-1)}{x} \right)} \right) \right)$$

**2.766 ODE No. 766**

$$\frac{d}{dx}y(x) = \frac{y(x)}{x \ln(x)} \left( -\ln(x) - x \ln \left( \frac{(1+x)(x-1)}{x} \right) + \ln \left( \frac{(1+x)(x-1)}{x} \right) x^2 y(x) \right) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.234 (sec), leaf count = 85

$$\left\{ y(x) = 1 e^{\int -\frac{1}{x \ln(x)} \left( x \ln \left( \frac{(1+x)(x-1)}{x} \right) + \ln(x) \right) dx} \left( \int -\frac{x}{\ln(x)} e^{\int -\frac{1}{x \ln(x)} \left( x \ln \left( \frac{(1+x)(x-1)}{x} \right) + \ln(x) \right) dx} \ln \left( \frac{(1+x)(x-1)}{x} \right) dx \right)$$

**2.767 ODE No. 767**

$$\frac{d}{dx}y(x) = \frac{-8xy(x) - x^3 + 2x^2 - 8x + 32}{32y(x) + 4x^2 - 8x + 32} = 0$$

**Mathematica:** cpu = 0.753096 (sec), leaf count = 38

$$\left\{ \left\{ y(x) \rightarrow 4(W(-e^{c_1 - \frac{x}{16}}) - 1) + \frac{1}{8}(-x^2 + 2x - 8) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 26

$$\left\{ y(x) = -\frac{x^2}{8} + 4 \text{lambertW}(1/4\_C1 e^{-x/16} e^{-3/4}) + \frac{x}{4} + 3 \right\}$$

**2.768 ODE No. 768**

$$\frac{d}{dx}y(x) = \frac{y(x)(1+y(x))}{x(-y(x)-1+xy(x))} = 0$$

**Mathematica:** cpu = 0.977124 (sec), leaf count = 70

$$\text{Solve} \left[ -\frac{2^{2/3} \left( xy(x) \left( \log \left( \frac{xy(x)}{(x-1)y(x)-1} \right) - \log \left( \frac{y(x)+1}{-xy(x)+y(x)+1} \right) - \log(x) - 1 + \log(2) \right) + 1 \right)}{9xy(x)} = c_1, y(x) \right]$$

**Maple:** cpu = 0.062 (sec), leaf count = 26

$$\left\{ y(x) = - \left( x \text{lambertW} \left( \frac{1}{x - C1 e^{x-1}} \right) + 1 \right)^{-1} \right\}$$

**2.769 ODE No. 769**

$$\frac{d}{dx}y(x) = \frac{-i/32(16ix^2 + 16(y(x))^4 + 8x^4(y(x))^2 + x^8)x}{y(x)} = 0$$

**Mathematica:** cpu = 42.445390 (sec), leaf count = 46

$$\text{DSolve} \left[ y'(x) = -\frac{ix(x^8 + 8x^4y(x)^2 + 16ix^2 + 16y(x)^4)}{32y(x)}, y(x), x \right]$$

**Maple:** cpu = 0.359 (sec), leaf count = 251

$$\left\{ y(x) = -\frac{\sqrt{4}}{2x} \sqrt{\left( -2(1/8x^6 + i) - C1 J_{1/3}((1/3 - i/3)x^3) + \left( -\frac{x^6}{4} - 2i \right) Y_{1/3} \left( \left( \frac{1}{3} - \frac{i}{3} \right) x^3 \right) + (1 + i) \right)} \right\}$$

**2.770 ODE No. 770**

$$\frac{d}{dx}y(x) = 2 \frac{(y(x))^6}{(y(x))^3 + 2 + 16x(y(x))^2 + 32x^2(y(x))^4} = 0$$

**Mathematica:** cpu = 0.105513 (sec), leaf count = 705

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{18432c_1^2x^2 + \sqrt{4(192c_1^2x - 12c_1 - 256x^2)^3 + (18432c_1^2x^2 - 2880c_1x + 8192x^3 + 108)^2} - 2}}{3\sqrt[3]{2}(1 - 16c_1x)} \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 1345

$$\left\{ y(x) = \frac{1}{3 \_C1 + 48 x} \sqrt[3]{4096 \_C1^3 x^3 + 6 \sqrt{3} \sqrt{4096 \_C1^4 x^3 + 27 \_C1^4 + 576 x \_C1^3 + 2048 \_C1^2 x^2}} \right.$$

## 2.771 ODE No. 771

$$\frac{d}{dx} y(x) = \frac{-4axy(x) - a^2x^3 - 2ax^2b - 4ax + 8}{8y(x) + 2ax^2 + 4bx + 8} = 0$$

**Mathematica:** cpu = 0.053007 (sec), leaf count = 46

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4}(-ax^2 - 2bx - 4) - \frac{2\left(W\left(-e^{-\frac{b^2x}{4} + c_1 - 1}\right) + 1\right)}{b} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 84

$$\left\{ y(x) = \frac{1}{4b} \left( -ax^2b - 2b^2x - 4b + 4e^{-1/4 \frac{1}{a} \left( ab^2x + 2 \_C1 b^2 + 4 \text{lambertW} \left( -1/2 e^{-1/4 b^2 x} e^{-1/2 \frac{-C1 b^2}{a}} e^{-b/2 e^{-1}} \right) \right)} \right) \right.$$

## 2.772 ODE No. 772

$$\frac{d}{dx} y(x) = \frac{(x + 1 + \ln(y(x)) x) \ln(y(x)) y(x)}{x(1 + x)} = 0$$

**Mathematica:** cpu = 0.108514 (sec), leaf count = 21

$$\left\{ \left\{ y(x) \rightarrow e^{\frac{x}{c_1 - x + \log(x+1)}} \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 18

$$\left\{ y(x) = e^{\frac{x}{\ln(1+x) + \_C1 - x}} \right\}$$

**2.773 ODE No. 773**

$$\frac{d}{dx}y(x) = \frac{xy(x) + x + (y(x))^2}{(x-1)(y(x)+x)} = 0$$

**Mathematica:** cpu = 0.053007 (sec), leaf count = 61

$$\text{Solve} \left[ \frac{1}{2} \log \left( \frac{y(x)^2}{x^2} + \frac{y(x)}{x} + 1 \right) + \frac{\tan^{-1} \left( \frac{2y(x)+1}{\sqrt{3}} \right)}{\sqrt{3}} = c_1 + \log(1-x) - \log(x), y(x) \right]$$

**Maple:** cpu = 0.218 (sec), leaf count = 48

$$\left\{ y(x) = \frac{\sqrt{3}x}{2} \tan \left( \text{RootOf} \left( -\sqrt{3} \ln \left( \frac{3x^2((\tan(_Z))^2 + 1)}{4(x-1)^2} \right) + 2\sqrt{3}_C1 - 2_Z \right) \right) - \frac{x}{2} \right\}$$

**2.774 ODE No. 774**

$$\frac{d}{dx}y(x) = \frac{-4xy(x) - x^3 - 2ax^2 - 4x + 8}{8y(x) + 2x^2 + 4ax + 8} = 0$$

**Mathematica:** cpu = 0.027003 (sec), leaf count = 45

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4}(-2ax - x^2 - 4) - \frac{2(W(-e^{-\frac{a^2x}{4} + c_1 - 1}) + 1))}{a} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 50

$$\left\{ y(x) = -\frac{1}{4a} \left( 2a^2x + ax^2 + 8 \text{lambertW} \left( -1/2 e^{-1/4 a^2 x} e^{-a/2} e^{-1} e^{1/4 - C1 a^2} \right) + 4a + 8 \right) \right\}$$

**2.775 ODE No. 775**

$$\frac{d}{dx}y(x) = \frac{x - y(x) + \sqrt{y(x)}}{x - y(x) + \sqrt{y(x)} + 1} = 0$$

**Mathematica:** cpu = 0.094512 (sec), leaf count = 943

$$\left\{ \left\{ y(x) \rightarrow \text{Root} \left[ x^6 - 2e^{3c_1}x^3 + e^{6c_1} + \#1^6 + (-6x - 6)\#1^5 + (15x^2 + 24x + 9)\#1^4 + (-20x^3 - 36x^2 - \dots \right] \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 60

$$\left\{ \sqrt{y(x) - 2\sqrt{y(x)} - xy(x)} + \sqrt{y(x) - 2\sqrt{y(x)} - x\sqrt{y(x)}} - \sqrt{y(x) - 2\sqrt{y(x)} - xx - C1} = 0 \right\}$$

**2.776 ODE No. 776**

$$\frac{d}{dx}y(x) = \frac{y(x)}{x \ln(x^{-1})} \left( -\ln(x^{-1}) - \ln\left(\frac{x^2+1}{x}\right) x + \ln\left(\frac{x^2+1}{x}\right) x^2 y(x) \right) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.234 (sec), leaf count = 92

$$\left\{ y(x) = 1 e^{\int -\frac{1}{x \ln(x^{-1})} \left( \ln\left(\frac{x^2+1}{x}\right) x + \ln(x^{-1}) \right) dx} \left( \int -\frac{x}{\ln(x^{-1})} e^{\int -\frac{1}{x \ln(x^{-1})} \left( \ln\left(\frac{x^2+1}{x}\right) x + \ln(x^{-1}) \right) dx} \ln\left(\frac{x^2+1}{x}\right) dx + \right. \right.$$

**2.777 ODE No. 777**

$$\frac{d}{dx}y(x) = \frac{y(x)(1+y(x))}{x(-y(x)-1+x(y(x))^4)} = 0$$

**Mathematica:** cpu = 0.086011 (sec), leaf count = 39

$$\text{Solve} \left[ -\frac{1}{2}(y(x)+1)^2 + 2(y(x)+1) - \frac{1}{xy(x)} - \log(y(x)+1) = c_1, y(x) \right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 51

$$\left\{ y(x) = e^{\text{RootOf}(x(e^{-Z})^3 - 5x(e^{-Z})^2 + 2\_C1 x e^{-Z} + 2\_Z x e^{-Z} + 7x e^{-Z} - 2\_C1 x - 2x\_Z - 3x + 2)} - 1 \right\}$$

**2.778 ODE No. 778**

$$\frac{d}{dx}y(x) = \frac{-3x^2y(x) + 1 + x^6(y(x))^2 + (y(x))^3 x^9}{x^3} = 0$$

**Mathematica:** cpu = 0.063008 (sec), leaf count = 95

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{3x^6y(x)+x^3}{\sqrt[3]{29}\sqrt[3]{x^9}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2} \& \right] = c_1 + \frac{29^{2/3}(x^9)^{2/3}}{9x^5}, y(x) \right]$$

**Maple:** cpu = 0.031 (sec), leaf count = 37

$$\left\{ y(x) = \frac{-3 + 29 \text{RootOf}\left(-81 \int^{-Z} (841\_a^3 - 27\_a + 27)^{-1} d\_a + x + 3\_C1\right)}{9x^3} \right\}$$

**2.779 ODE No. 779**

$$\frac{d}{dx}y(x) = \frac{x^3y(x) + x^3 + x(y(x))^2 + (y(x))^3}{(x-1)x^3} = 0$$

**Mathematica:** cpu = 0.028504 (sec), leaf count = 57

$$\text{Solve}\left[-\frac{1}{4}\log\left(\frac{y(x)^2}{x^2} + 1\right) + \frac{1}{2}\log\left(\frac{y(x)}{x} + 1\right) + \frac{1}{2}\tan^{-1}\left(\frac{y(x)}{x}\right) = c_1 + \log(1-x) - \log(x), y(x)\right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 50

$$\left\{\frac{1}{2}\ln\left(\frac{y(x)+x}{x}\right) - \frac{1}{4}\ln\left(\frac{(y(x))^2+x^2}{x^2}\right) + \frac{1}{2}\arctan\left(\frac{y(x)}{x}\right) + \ln(x) - \ln(x-1) - C1 = 0\right\}$$

**2.780 ODE No. 780**

$$\frac{d}{dx}y(x) = \frac{xy(x) + y(x) + x\sqrt{(y(x))^2 + x^2}}{x(1+x)} = 0$$

**Mathematica:** cpu = 0.023003 (sec), leaf count = 15

$$\{\{y(x) \rightarrow x \sinh(c_1 + \log(x+1))\}\}$$

**Maple:** cpu = 0.280 (sec), leaf count = 27

$$\left\{-C1 + \frac{1}{x(1+x)}\left(\sqrt{(y(x))^2 + x^2} + y(x)\right) = 0\right\}$$

**2.781 ODE No. 781**

$$\frac{d}{dx}y(x) = \frac{(x^4 + x^3 + x + 3(y(x))^2)y(x)}{(6(y(x))^2 + x)x} = 0$$

**Mathematica:** cpu = 0.495563 (sec), leaf count = 82

$$\left\{\left\{y(x) \rightarrow -\frac{\sqrt{x}\sqrt{W\left(6xe^{2c_1+\frac{2x^3}{3}+x^2}\right)}}{\sqrt{6}}\right\}, \left\{y(x) \rightarrow \frac{\sqrt{x}\sqrt{W\left(6xe^{2c_1+\frac{2x^3}{3}+x^2}\right)}}{\sqrt{6}}\right\}\right\}$$

**Maple:** cpu = 0.249 (sec), leaf count = 61

$$\left\{\left((y(x))^{-2} + 6x^{-1}\right)^{-1} = \frac{x}{54}\left(e^{\text{RootOf}\left(2x^3e^{-Z}+3e^{-Z}x^2-3e^{-Z}\ln\left(1/2\frac{e^{-Z}+9}{x}\right)+9e^{-Z}-C1+3-Ze^{-Z}+27\right)} + 9\right)\right\}$$

**2.782 ODE No. 782**

$$\frac{d}{dx}y(x) = \frac{y(x)}{x \tanh(x^{-1})} \left( -\tanh(x^{-1}) - \ln\left(\frac{x^2+1}{x}\right)x + \ln\left(\frac{x^2+1}{x}\right)x^2y(x) \right) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.530 (sec), leaf count = 92

$$\left\{ y(x) = 1e^{\int -\frac{1}{x \tanh(x^{-1})} (\ln(\frac{x^2+1}{x})x + \tanh(x^{-1})) dx} \left( \int -\frac{x}{\tanh(x^{-1})} e^{\int -\frac{1}{x \tanh(x^{-1})} (\ln(\frac{x^2+1}{x})x + \tanh(x^{-1})) dx} \ln\left(\frac{x^2+1}{x}\right) dx + C1 \right) \right\}$$

**2.783 ODE No. 783**

$$\frac{d}{dx}y(x) = -\frac{y(x) (\tanh(x) + \ln(2x)x - \ln(2x)x^2y(x))}{x \tanh(x)} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.203 (sec), leaf count = 69

$$\left\{ y(x) = 1e^{\int -\frac{x \ln(x) + x \ln(2) + \tanh(x)}{x \tanh(x)} dx} \left( \int -\frac{x (\ln(2) + \ln(x))}{\tanh(x)} e^{\int -\frac{x \ln(x) + x \ln(2) + \tanh(x)}{x \tanh(x)} dx} dx + C1 \right)^{-1} \right\}$$

**2.784 ODE No. 784**

$$\frac{d}{dx}y(x) = \frac{-\sinh(x) + x^2 \ln(x) + 2y(x) \ln(x)x + \ln(x) + (y(x))^2 \ln(x)}{\sinh(x)} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 26.208 (sec), leaf count = 24

$$\left\{ y(x) = -x - \tan\left(-C1 - \int \frac{\ln(x)}{\sinh(x)} dx\right) \right\}$$

**2.785 ODE No. 785**

$$\frac{d}{dx}y(x) = -\frac{\ln(x) - \sinh(x)x^2 - 2\sinh(x)xy(x) - \sinh(x) - \sinh(x)(y(x))^2}{\ln(x)} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 96.767 (sec), leaf count = 24

$$\left\{ y(x) = -x - \tan\left(-C1 - \int \frac{\sinh(x)}{\ln(x)} dx\right) \right\}$$

**2.786 ODE No. 786**

$$\frac{d}{dx}y(x) = \frac{y(x)\ln(x) + \cosh(x)xa(y(x))^2 + \cosh(x)x^3b}{x\ln(x)} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.047 (sec), leaf count = 39

$$\left\{ y(x) = \frac{x}{a} \tan\left(\int \frac{x \cosh(x)}{\ln(x)} dx \sqrt{ab} + -C1 \sqrt{ab}\right) \sqrt{ab} \right\}$$

**2.787 ODE No. 787**

$$\frac{d}{dx}y(x) = \frac{x(-x-1+x^2-2x^2y(x)+2x^4)}{(x^2-y(x))(1+x)} = 0$$

**Mathematica:** cpu = 19.683499 (sec), leaf count = 487

Solve  $\left[ \begin{array}{l} 2 \cdot 2^{2/3} \left( 2 - \frac{x(x^2-x-1)(2x^2-2y(x)+3)}{\sqrt[3]{x^3(x^2-x-1)^3(x^2-y(x))}} \right) \left( \frac{x(x^2-x-1)(2x^2-2y(x)+3)}{\sqrt[3]{x^3(x^2-x-1)^3(x^2-y(x))}} + 4 \right) \left( \left( 1 - \frac{x(x^2-x-1)(2x^2-2y(x)+3)}{2\sqrt[3]{x^3(x^2-x-1)^3(x^2-y(x))}} \right) \ln\left( \frac{x(x^2-x-1)(2x^2-2y(x)+3)}{\sqrt[3]{x^3(x^2-x-1)^3(x^2-y(x))}} + 4 \right) \right) \\ \hline 9 \left( -\frac{(2x^2-2y(x)+3)^3}{(x^2-y(x))^3} + \frac{12x(x^2-x-1)}{\sqrt[3]{x^3}} \right) \end{array} \right]$



**Maple:** cpu = 0.437 (sec), leaf count = 191

$$\left\{ y(x) = 1 \left( 4 x^2 e^{\text{RootOf} \left( 8 x^3 e^{-Z} - 24 e^{-Z} x^2 - 36 x^3 + 6 \ln \left( \frac{2 e^{-Z} - 9}{(1+x)^4} \right) \right) e^{-Z} + 18 - C1 e^{-Z} - 6 - Z e^{-Z} + 24 x e^{-Z} + 108 x^2 - 27 \ln \left( \frac{2 e^{-Z} - 9}{(1+x)^4} \right)} \right) \right.$$

## 2.788 ODE No. 788

$$\frac{d}{dx} y(x) = - \frac{y(x) (\ln(x-1) + \coth(1+x)x - \coth(1+x)x^2 y(x))}{\ln(x-1)x} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

## 2.789 ODE No. 789

$$\frac{d}{dx} y(x) = - \frac{\ln(x-1) - \coth(1+x)x^2 - 2 \coth(1+x)xy(x) - \coth(1+x) - \coth(1+x)(y(x))^2}{\ln(x-1)} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

## 2.790 ODE No. 790

$$\frac{d}{dx} y(x) = \frac{1}{\ln((x-1)^{-1})} \left( 2x \ln((x-1)^{-1}) - \coth\left(\frac{1+x}{x-1}\right) + \coth\left(\frac{1+x}{x-1}\right) (y(x))^2 - 2 \coth\left(\frac{1+x}{x-1}\right) \right)$$

**Mathematica:** cpu = 1267.680975 (sec), leaf count = 95

$$\left\{ \left\{ y(x) \rightarrow \frac{\exp\left(\int_1^x \frac{2 \coth\left(\frac{K[5]}{K[5]-1} + \frac{1}{K[5]-1}\right)}{\log\left(\frac{1}{K[5]-1}\right)} dK[5]\right)}{c_1 - \frac{1}{2} \exp\left(\text{Integrate}\left[\frac{2 \coth\left(\frac{K[5]}{K[5]-1} + \frac{1}{K[5]-1}\right)}{\log\left(\frac{1}{K[5]-1}\right)}, \{K[5], 1, x\}, \text{Assumptions} \rightarrow \text{True}\right]\right)} + x^2 + 1 \right\} \right.$$

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

**2.791 ODE No. 791**

$$\frac{d}{dx}y(x) = \frac{2x^2 \cosh((x-1)^{-1}) - 2x \cosh((x-1)^{-1}) - 1 + (y(x))^2 - 2x^2y(x) + x^4 - x + x(y(x))^2 - 2}{(x-1) \cosh((x-1)^{-1})}$$

**Mathematica:** cpu = 1670.398114 (sec), leaf count = 87

$$\left\{ \left\{ y(x) \rightarrow \frac{\exp\left(\int_1^x \frac{2(K[5]+1)\operatorname{sech}\left(\frac{1}{K[5]-1}\right)}{K[5]-1} dK[5]\right)}{c_1 - \frac{1}{2} \exp\left(\operatorname{Integrate}\left[\frac{2(K[5]+1)\operatorname{sech}\left(\frac{1}{K[5]-1}\right)}{K[5]-1}, \{K[5], 1, x\}, \text{Assumptions} \rightarrow \text{True}\right]\right)}\right\} + \frac{x^3 + x^2}{x + 1} + \dots \right.$$

**Maple:** cpu = 12.699 (sec), leaf count = 634

$$\left\{ y(x) = 1 \left( x^2 \left( e^{\frac{-C_1}{(e^{(x-1)^{-1}})^2 + 1}} e^{2(x-1)^{-1}} \right)^4 \left( e^{\frac{-C_1}{(e^{(x-1)^{-1}})^2 + 1}} \right)^4 \left( e^{\frac{1}{(e^{(x-1)^{-1}})^2 + 1}} \int \left( \frac{e^{(x-1)^{-1}}}{1+x} x + \frac{x}{e^{(x-1)^{-1}}(1+x)} - \frac{e^{(x-1)^{-1}}}{1+x} \right) dx \right) \right.$$

**2.792 ODE No. 792**

$$\frac{d}{dx}y(x) = \frac{y(x) (-\cosh((1+x)^{-1})x + \cosh((1+x)^{-1}) - x + x^2y(x) - x^2 + x^3y(x))}{(x-1)x \cosh((1+x)^{-1})} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

can not solve

**Maple:** cpu = 0.312 (sec), leaf count = 114

$$\left\{ y(x) = 1 e^{\int -\frac{\cosh((1+x)^{-1})x + x^2 - \cosh((1+x)^{-1}) + x}{x(x-1) \cosh((1+x)^{-1})} dx} \left( \int -\frac{x(1+x)}{(x-1) \cosh((1+x)^{-1})} e^{\int -\frac{\cosh((1+x)^{-1})x + x^2 - \cosh((1+x)^{-1})}{x(x-1) \cosh((1+x)^{-1})} dx} \right)$$

**2.793 ODE No. 793**

$$\frac{d}{dx}y(x) = -\frac{y(x)(xy(x)+1)}{x(xy(x)+1-y(x))} = 0$$

**Mathematica:** cpu = 13.841758 (sec), leaf count = 397

Solve  $\left[ \sqrt[3]{-2} \left( \frac{2^{2/3}((x-1)y(x)-2)}{\sqrt[3]{-\frac{1}{(x-1)^3}(x-1)((x-1)y(x)+1)}} + (-2)^{2/3} \right) \left( \frac{-xy(x)+y(x)+2}{\sqrt[3]{2} \sqrt[3]{-\frac{1}{(x-1)^3}(x-1)((x-1)y(x)+1)}} + (-2)^{2/3} \right) \left( \left( \frac{\sqrt[3]{-1}(-}{\sqrt[3]{-\frac{1}{(x-1)^3}(x-1)((x-1)y(x)+1)}} \right) \right) \right]$

**Maple:** cpu = 0.078 (sec), leaf count = 32

$$\left\{ y(x) = -2 \frac{1}{x} e^{-\text{lambertW}\left(-2 \frac{(x-1)(e^{-C1})^3 e^{-1}}{x}\right) + 3 C1 - 1} \right\}$$

**2.794 ODE No. 794**

$$\frac{d}{dx}y(x) = \frac{y(x)}{x(-1+y(x)+x^2(y(x))^3+(y(x))^4 x^3)} = 0$$

**Mathematica:** cpu = 0.091512 (sec), leaf count = 67

Solve  $\left[ \text{RootSum}\left[\#1^3 y(x)^3 + \#1^2 y(x)^2 + 1 \&, \frac{\#1 y(x) \log(x - \#1) + \log(x - \#1)}{3 \#1 y(x) + 2} \&\right] + y(x) - \log(x) = 0 \right]$

**Maple:** cpu = 0.390 (sec), leaf count = 32

$$\left\{ -y(x) + \int^{xy(x)} \frac{1}{-a(-a^3 + -a^2 + 1)} d_a - C1 = 0 \right\}$$

**2.795 ODE No. 795**

$$\frac{d}{dx}y(x) = \frac{x^3 + 3ax^2 + 3a^2x + a^3 + x(y(x))^2 + a(y(x))^2 + (y(x))^3}{(x+a)^3} = 0$$

**Mathematica:** cpu = 0.156520 (sec), leaf count = 111

$$\text{Solve} \left[ -\frac{19}{3} \text{RootSum} \left[ -19\#1^3 + 6\sqrt{38}\#1 - 19\&, \frac{\log \left( \frac{\frac{3y(x)}{(a+x)^3} + \frac{1}{(a+x)^2}}{\sqrt[3]{38}\sqrt{\frac{1}{(a+x)^6}}} - \#1 \right)}{2\sqrt[3]{38} - 19\#1^2} \& \right] = \frac{1}{9} 38^{2/3} \left( \frac{1}{(a+x)^6} \right)^{2/3} \right]$$

**Maple:** cpu = 0.032 (sec), leaf count = 37

$$\left\{ y(x) = -\text{RootOf} \left( -\int^{-Z} (\_a^3 - \_a^2 - \_a - 1)^{-1} d\_a + \ln(x+a) + \_C1 \right) (x+a) \right\}$$

## 2.796 ODE No. 796

$$\frac{d}{dx} y(x) = 1/3 \frac{x(y(x))^3 e^{3x^2}}{(3e^{3/2x^2} + e^{3/2x^2} y(x) + 3y(x)) e^{9/2x^2}} = 0$$

**Mathematica:** cpu = 9.404194 (sec), leaf count = 102

$$\text{Solve} \left[ \frac{1}{62} \left( -31 \log \left( 9e^{\frac{3x^2}{2}} (y(x) + 3)y(x) + 3e^{3x^2} (y(x) + 3)^2 - y(x)^2 \right) + 6\sqrt{93} \tanh^{-1} \left( \frac{\sqrt{\frac{3}{31}} \left( 2e^{\frac{3x^2}{2}} (y(x) + 3) \right)}{y(x)} \right) \right) \right]$$

**Maple:** cpu = 1.155 (sec), leaf count = 143

$$\left\{ y(x) = \text{RootOf} \left( \left( 7e^{3x^2 + \text{RootOf} \left( (e^{3/2x^2})^2 (42\sqrt{93} \tanh \left( \frac{(-C1-5-Z)\sqrt{93}}{90} \right) e^{3x^2 - Z} + 217 \left( \tanh \left( \frac{(-C1-5-Z)\sqrt{93}}{90} \right) \right)^2 e^{3x^2 - Z} + 1 \right)} \right) \right) \right\}$$

## 2.797 ODE No. 797

$$\frac{d}{dx} y(x) = \frac{y(x)}{x} \left( -1 - \cosh \left( \frac{1+x}{x-1} \right) x + \cosh \left( \frac{1+x}{x-1} \right) x^2 y(x) - \cosh \left( \frac{1+x}{x-1} \right) x^2 + \cosh \left( \frac{1+x}{x-1} \right) x^3 y(x) \right)$$

**Mathematica:** cpu = 2.027757 (sec), leaf count = 349

$$\left\{ \left\{ y(x) \rightarrow \frac{\exp \left( \frac{(3e^2-1)\text{Chi} \left( \frac{2}{x-1} \right)}{e} + \frac{(1+3e^2)\text{Shi} \left( \frac{2}{x-1} \right)}{e} - \frac{1}{4} e x^2 \sinh \left( \frac{2}{x-1} \right) + \frac{x^2 \sinh \left( \frac{2}{x-1} \right)}{4e} - \frac{1}{4} e x^2 \cosh \left( \frac{2}{x-1} \right) - \frac{x^2}{4} \right)}{x \left( c_1 \exp \left( \frac{(x-1)(-x+e^2)}{2} \right) \right)} \right. \right\}$$

**Maple:** cpu = 0.141 (sec), leaf count = 281

$$\left\{ y(x) = \frac{1}{x} e^{-\frac{ex^2}{4}} e^{2(x-1)^{-1}} e^{\frac{5e}{4} e^{2(x-1)^{-1}}} e^{-\frac{e^{-1}x^2}{4}} e^{-2(x-1)^{-1}} e^{\frac{e^{-1}}{4}} e^{-2(x-1)^{-1}} e^{-1} \text{Ei} \left( 1, 2(x-1)^{-1} \right) \left( e^{e^{2(x-1)^{-1}} x} \right)^{-1} \left( e^{e \text{Ei} \left( 1, 2(x-1)^{-1} \right)} \right)^{-1} \right\}$$

**2.798 ODE No. 798**

$$\frac{d}{dx}y(x) = \frac{(x + y(x) + 1)y(x)}{(2(y(x))^3 + y(x) + x)(1 + x)} = 0$$

**Mathematica:** cpu = 0.552070 (sec), leaf count = 27

$$\text{Solve}\left[y(x)^2 - \frac{x}{y(x)} + \log(y(x)) - \log(x + 1) = c_1, y(x)\right]$$

**Maple:** cpu = 0.109 (sec), leaf count = 30

$$\left\{y(x) = e^{\text{RootOf}\left(-\left(e^{-Z}\right)^3 + \ln(1+x)e^{-Z} + C1 e^{-Z} - Z e^{-Z+x}\right)}\right\}$$

**2.799 ODE No. 799**

$$\frac{d}{dx}y(x) = \frac{y(x)}{x} \left(-1 - x e^{\frac{1+x}{x-1}} + x^2 e^{\frac{1+x}{x-1}} y(x) - x^2 e^{\frac{1+x}{x-1}} + x^3 e^{\frac{1+x}{x-1}} y(x)\right) = 0$$

**Mathematica:** cpu = 0.300538 (sec), leaf count = 70

$$\left\{\left\{y(x) \rightarrow \frac{e^{6e\text{Ei}\left(\frac{2}{x-1}\right)}}{x \left(c_1 e^{\frac{1}{2}e^{\frac{x}{x-1}} + \frac{1}{x-1}(x^2+4x-5)} + e^{6e\text{Ei}\left(\frac{2}{x-1}\right)}\right)}\right\}\right\}$$

**Maple:** cpu = 0.234 (sec), leaf count = 147

$$\left\{y(x) = \frac{1}{x} e^{\frac{5}{2}e^{\frac{1+x}{x-1}}} e^{-\frac{x^2}{2}e^{\frac{1+x}{x-1}}} \left(e^{e\text{Ei}(1, -2(x-1)^{-1})}\right)^{-6} \left(e^{xe^{\frac{1+x}{x-1}}}\right)^{-2} \left(\int -(1+x)e^{\frac{1+x}{x-1}} e^{\frac{5}{2}e^{\frac{1+x}{x-1}}} e^{-\frac{x^2}{2}e^{\frac{1+x}{x-1}}} \left(e^{e\text{Ei}(1, -2(x-1)^{-1})}\right)^{-2} dx\right)$$

**2.800 ODE No. 800**

$$\frac{d}{dx}y(x) = \frac{-b^3 + 6b^2x - 12bx^2 + 8x^3 - 4b(y(x))^2 + 8x(y(x))^2 + 8(y(x))^3}{(2x - b)^3} = 0$$

**Mathematica:** cpu = 0.176022 (sec), leaf count = 128

$$\text{Solve}\left[-\frac{19}{3}\text{RootSum}\left[-19\#1^3 + 6\sqrt{38}\#1 - 19\&, \frac{\log\left(\frac{4}{(b-2x)^2} - \frac{24y(x)}{(b-2x)^3} - \#1\right)}{2\sqrt{38} - 19\#1^2}\&\right] = \frac{1}{9}38^{2/3}\left(\frac{1}{(b-2x)^6}\right)^2\right]$$

**Maple:** cpu = 0.015 (sec), leaf count = 41

$$\left\{ y(x) = \frac{\text{RootOf}\left(-\int^{-Z}(\_a^3 - \_a^2 - \_a - 1)^{-1} d\_a + \ln(-2x + b) + \_C1\right)(-2x + b)}{2} \right\}$$

## 2.801 ODE No. 801

$$\frac{d}{dx}y(x) = 1/2 \left( y(x) e^{-1/4x^2} x + 2 + 2(y(x))^2 e^{-1/2x^2} + 2(y(x))^3 e^{-3/4x^2} \right) e^{1/4x^2} = 0$$

**Mathematica:** cpu = 0.101013 (sec), leaf count = 126

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{3e^{-\frac{x^2}{2}}y(x)+e^{-\frac{x^2}{4}}}{\sqrt[3]{29}\sqrt[3]{e^{-\frac{3x^2}{4}}}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2} \& \right] = c_1 + \frac{1}{9} 29^{2/3} e^{\frac{x^2}{2}} \left( e^{-\frac{3x^2}{4}} \right) \right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 63

$$\left\{ y(x) = -\frac{1}{9} \left( 3e^{-1/4x^2} e^{1/4x^2} - 29 \text{RootOf}\left(-81 \int^{-Z} (841\_a^3 - 27\_a + 27)^{-1} d\_a + x + 3\_C1\right) \right) \right\} (e^{-\frac{3x^2}{4}})$$

## 2.802 ODE No. 802

$$\frac{d}{dx}y(x) = -\frac{1}{x}(-x^{-1} - \_F1(y(x) + x^{-1})) = 0$$

**Mathematica:** cpu = 0.075510 (sec), leaf count = 98

$$\text{Solve} \left[ \int_1^{y(x)} \frac{\_F1(K[2] + \frac{1}{x}) \left( \int_1^x -\frac{\_F1'(K[2] + \frac{1}{K[1]})}{K[1]^2 (\_F1(K[2] + \frac{1}{K[1]})^2)} dK[1] \right) + 1}{\_F1(K[2] + \frac{1}{x})} dK[2] + \int_1^x \left( \frac{1}{K[1]^2 \_F1\left(\frac{1}{K[1]} + \frac{1}{x}\right)} \right) dK[1] \right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 27

$$\left\{ y(x) = \frac{\text{RootOf}\left(-\ln(x) + \int^{-Z}(\_F1(\_a))^{-1} d\_a + \_C1\right)x - 1}{x} \right\}$$

### 2.803 ODE No. 803

$$\frac{d}{dx}y(x) = \frac{-F1((y(x))^2 - 2 \ln(x))}{\sqrt{(y(x))^2 x}} = 0$$

**Mathematica:** cpu = 0.080010 (sec), leaf count = 386

$$\text{Solve} \left[ \int_1^{y(x)} \left( - \int_1^x \left( \frac{4K[2] (-F1(K[2]^2 - 2 \log(K[1]))^3 - F1'(K[2]^2 - 2 \log(K[1]))}{K[1] ((-F1(K[2]^2 - 2 \log(K[1])))^2 - 1)^2} + \frac{4\sqrt{K[2]^2}(-F1(K[2]^2 - 2 \log(K[1]))}{K[1]}} \right) dx \right) dy(x) = 0 \right]$$

**Maple:** cpu = 0.327 (sec), leaf count = 65

$$\left\{ y(x) = \sqrt{2 \ln(x) + 2 \text{RootOf} \left( \ln(x) - \int^{-Z} (-F1(2\_a) - 1)^{-1} d\_a + \_C1 \right)}, y(x) = -\sqrt{2 \ln(x) + 2 \text{RootOf} \left( \ln(x) - \int^{-Z} (-F1(2\_a) - 1)^{-1} d\_a + \_C1 \right)} \right\}$$

### 2.804 ODE No. 804

$$\frac{d}{dx}y(x) = 1/2 \frac{-\sin(2y(x))x - \sin(2y(x)) + \cos(2y(x))x^4 + x^4}{x(1+x)} = 0$$

**Mathematica:** cpu = 0.493063 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow \tan^{-1} \left( \frac{-12c_1 + 3x^4 - 4x^3 + 6x^2 - 12x + 12 \log(x+1) - 25}{12x} \right) \right\} \right\}$$

**Maple:** cpu = 0.827 (sec), leaf count = 38

$$\left\{ y(x) = \arctan \left( \frac{3x^4 - 4x^3 + 6x^2 + 12 \ln(1+x) - 12\_C1 - 12x}{12x} \right) \right\}$$

### 2.805 ODE No. 805

$$\frac{d}{dx}y(x) = \frac{xy(x) + y(x) + x^4 \sqrt{(y(x))^2 + x^2}}{x(1+x)} = 0$$

**Mathematica:** cpu = 0.055507 (sec), leaf count = 37

$$\left\{ \left\{ y(x) \rightarrow x \sinh \left( \frac{1}{6} (6c_1 + 2x^3 - 3x^2 + 6x - 6 \log(x+1) + 11) \right) \right\} \right\}$$

**Maple:** cpu = 0.422 (sec), leaf count = 42

$$\left\{ \ln \left( y(x) + \sqrt{(y(x))^2 + x^2} \right) - \frac{x^3}{3} + \frac{x^2}{2} - x - \ln(x) + \ln(1+x) - \_C1 = 0 \right\}$$

**2.806 ODE No. 806**

$$\frac{d}{dx}y(x) = 1/2 \frac{-\sin(2y(x))x - \sin(2y(x)) + x\cos(2y(x)) + x}{x(1+x)} = 0$$

**Mathematica:** cpu = 0.269534 (sec), leaf count = 23

$$\left\{ \left\{ y(x) \rightarrow \tan^{-1} \left( \frac{-c_1 + x - \log(x+1) + 1}{x} \right) \right\} \right\}$$

**Maple:** cpu = 0.468 (sec), leaf count = 22

$$\left\{ y(x) = -\arctan \left( \frac{\ln(1+x) - x - C1}{x} \right) \right\}$$

**2.807 ODE No. 807**

$$\frac{d}{dx}y(x) = -(-x - F1(y(x) - \ln(x))y(x)e^{y(x)})^{-1} = 0$$

**Mathematica:** cpu = 1.852735 (sec), leaf count = 34

$$\text{DSolve} \left[ y'(x) = -\frac{1}{-e^{y(x)}y(x)F1(y(x) - \log(x)) - x}, y(x), x \right]$$

**Maple:** cpu = 0.468 (sec), leaf count = 43

$$\left\{ \frac{(\ln(x))^2}{2} - y(x)\ln(x) - \int^{y(x)-\ln(x)} \frac{F1(-a) - a + e^{-a}}{F1(-a)} da + C1 = 0 \right\}$$

**2.808 ODE No. 808**

$$\frac{d}{dx}y(x) = \frac{(1+2y(x))(1+y(x))}{x(-2y(x)-2+x+2xy(x))} = 0$$

**Mathematica:** cpu = 1.137644 (sec), leaf count = 127

$$\text{Solve} \left[ \frac{2^{2/3} \left( x \log \left( -\frac{y(x)+1}{2(x-1)y(x)+x-2} \right) - x \log \left( \frac{2xy(x)+x}{2(x-1)y(x)+x-2} \right) + 2xy(x) \left( \log \left( -\frac{y(x)+1}{2(x-1)y(x)+x-2} \right) - \log \left( \frac{2xy(x)+x}{2(x-1)y(x)+x-2} \right) \right) \right)}{9(2xy(x)+x)} \right]$$

**Maple:** cpu = 0.062 (sec), leaf count = 44

$$\left\{ y(x) = -\frac{1}{2} \left( x \text{lambertW} \left( \frac{1}{xe^{x-1}C1} \right) + 2 \right) \left( x \text{lambertW} \left( \frac{1}{xe^{x-1}C1} \right) + 1 \right)^{-1} \right\}$$



## 2.809 ODE No. 809

$$\frac{d}{dx}y(x) = \frac{-125 + 300x - 240x^2 + 64x^3 - 80(y(x))^2 + 64x(y(x))^2 + 64(y(x))^3}{(4x - 5)^3} = 0$$

**Mathematica:** cpu = 0.153020 (sec), leaf count = 128

$$\text{Solve} \left[ -\frac{19}{3} \text{RootSum} \left[ -19\#1^3 + 6\sqrt[3]{38}\#1 - 19\&, \frac{\log \left( \frac{\frac{192y(x)}{(4x-5)^3} + \frac{16}{(4x-5)^2} - \#1 \right)}{2\sqrt[3]{38} - 19\#1^2} \& \right] = c_1 + \frac{1}{9} 38^{2/3} \left( \frac{1}{(5-4x)} \right) \right]$$

**Maple:** cpu = 0.015 (sec), leaf count = 41

$$\left\{ y(x) = -\frac{\text{RootOf} \left( -\int^{-Z} (\_a^3 - \_a^2 - \_a - 1)^{-1} d\_a + \ln(4x - 5) + \_C1 \right) (4x - 5)}{4} \right\}$$

## 2.810 ODE No. 810

$$\frac{d}{dx}y(x) = \frac{x + y(x) + (y(x))^2 - 2y(x) \ln(x) x + x^2(\ln(x))^2}{x} = 0$$

**Mathematica:** cpu = 0.015002 (sec), leaf count = 40

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{\frac{c_1}{x} - 1} - \frac{1}{2} x^2 \left( \frac{1 - 2x \log(x)}{x^2} - \frac{1}{x^2} \right) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 16

$$\{y(x) = (\ln(x) + (\_C1 - x)^{-1}) x\}$$

## 2.811 ODE No. 811

$$\frac{d}{dx}y(x) = \frac{x^3 e^{y(x)} + x^4 + e^{y(x)} y(x) - e^{y(x)} \ln(e^{y(x)} + x) + x y(x) - \ln(e^{y(x)} + x) x + x}{x^2} = 0$$

**Mathematica:** cpu = 2.217281 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow -\log \left( \frac{e^{-c_1 x - \frac{x^3}{2}}}{x} - \frac{1}{x} \right) \right\} \right\}$$

**Maple:** cpu = 1.544 (sec), leaf count = 32

$$\left\{ y(x) = \frac{x^3}{2} + x\_C1 + \ln \left( -x \left( -1 + e^{\frac{x^3}{2}} e^{x\_C1} \right)^{-1} \right) \right\}$$

## 2.812 ODE No. 812

$$\frac{d}{dx}y(x) = 1/2 x^2 + \sqrt{x^3 - 6y(x)} + x^2 \sqrt{x^3 - 6y(x)} + x^3 \sqrt{x^3 - 6y(x)} = 0$$

**Mathematica:** cpu = 0.326541 (sec), leaf count = 70

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{96} (72c_1x^4 + 96c_1x^3 + 288c_1x - 144c_1^2 - 9x^8 - 24x^7 - 16x^6 - 72x^5 - 96x^4 + 16x^3 - 144x^2) \right\} \right\}$$

**Maple:** cpu = 0.312 (sec), leaf count = 32

$$\left\{ -\frac{1}{3} \sqrt{x^3 - 6y(x)} - \frac{x^4}{4} - \frac{x^3}{3} - x - \_C1 = 0 \right\}$$

## 2.813 ODE No. 813

$$\frac{d}{dx}y(x) = 1/2 \left( -\sqrt{ax^3} + 2 \sqrt{ax^4 + 8y(x)} + 2x^2 \sqrt{ax^4 + 8y(x)} + 2x^3 \sqrt{ax^4 + 8y(x)} \right) \sqrt{a} = 0$$

**Mathematica:** cpu = 0.493063 (sec), leaf count = 66

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{72} a (-72c_1x^4 - 96c_1x^3 - 288c_1x + 144c_1^2 + 9x^8 + 24x^7 + 16x^6 + 72x^5 + 87x^4 + 144x^2) \right\} \right\}$$

**Maple:** cpu = 0.327 (sec), leaf count = 38

$$\left\{ \frac{1}{4} \sqrt{ax^4 + 8y(x)} - \sqrt{a} \left( \frac{x^4}{4} + \frac{x^3}{3} + x \right) - \_C1 = 0 \right\}$$

## 2.814 ODE No. 814

$$\frac{d}{dx}y(x) = \frac{y(x) (-3x^3y(x) - 3 + (y(x))^2 x^7)}{x(x^3y(x) + 1)} = 0$$

**Mathematica:** cpu = 0.013502 (sec), leaf count = 72

$$\left\{ \left\{ y(x) \rightarrow \frac{x}{\frac{\sqrt{x(c_1-2x)+x}}{\sqrt{\frac{1}{x^7}}} - x^4} \right\}, \left\{ y(x) \rightarrow -\frac{x}{\frac{\sqrt{x(c_1-2x)+x}}{\sqrt{\frac{1}{x^7}}} + x^4} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 38

$$\left\{ y(x) = \frac{1}{x^3} \left( \sqrt{-C1 - 2x - 1} \right)^{-1}, y(x) = -\frac{1}{x^3} \left( \sqrt{-C1 - 2x + 1} \right)^{-1} \right\}$$

**2.815 ODE No. 815**

$$\frac{d}{dx}y(x) = \frac{(3 + y(x))^3 e^{9/2x^2} x e^{3/2x^2}}{(243 e^{3/2x^2} + 81 e^{3/2x^2} y(x) + 243 y(x)) e^{3x^2}} = 0$$

**Mathematica:** cpu = 10.172792 (sec), leaf count = 103

$$\text{Solve} \left[ \frac{1}{186} \left( 31 \log \left( -81 e^{\frac{3x^2}{2}} (y(x) + 3) y(x) + e^{3x^2} (y(x) + 3)^2 - 243 y(x)^2 \right) - 6\sqrt{93} \tanh^{-1} \left( \frac{2e^{\frac{3x^2}{2}} (y(x) + 3)}{9\sqrt{93}} \right) \right) \right]$$

**Maple:** cpu = 1.326 (sec), leaf count = 202

$$\left\{ 5 \ln \left( \frac{100 (e^{3/2x^2})^2 (y(x))^2 + 600 (e^{3/2x^2})^2 y(x) - 8100 (y(x))^2 e^{3/2x^2} + 900 (e^{3/2x^2})^2 - 24300 e^{3/2x^2} y(x)}{189 (3 e^{3/2x^2} + e^{3/2x^2} y(x) + 3 y(x))^2} \right) \right\}$$

**2.816 ODE No. 816**

$$\frac{d}{dx}y(x) = \frac{(x - y(x))^3 (y(x) + x)^3 x}{(-(y(x))^2 + x^2 - 1) y(x)} = 0$$

**Mathematica:** cpu = 0.141018 (sec), leaf count = 74

$$\text{Solve} \left[ \frac{1}{2} \left( \text{RootSum} \left[ \#1^3 - \#1 + 1 \&, \frac{\#1 \log(-\#1 + x^2 - y(x)^2) - \log(-\#1 + x^2 - y(x)^2)}{3\#1^2 - 1} \& \right] + x^2 \right) \right] =$$

**Maple:** cpu = 0.624 (sec), leaf count = 307

$$\left\{ \int_{-b}^x \frac{(-a - y(x))^3 (y(x) + a)^3 a}{a^6 - 3 a^4 (y(x))^2 + 3 a^2 (y(x))^4 - (y(x))^6 - a^2 + (y(x))^2 + 1} d_a + \int^{y(x)} \frac{(-f^6 + 3 f^4 x)}{(-f^6 + 3 f^4 x)} d_{-f} \right\}$$

**2.817 ODE No. 817**

$$\frac{d}{dx}y(x) = 1/2 \frac{-2 \cos(y(x)) + x^3 \cos(2y(x)) \ln(x) + x^3 \ln(x)}{\sin(y(x)) \ln(x) x} = 0$$

**Mathematica:** cpu = 0.384049 (sec), leaf count = 63

$$\left\{ \left\{ y(x) \rightarrow -\sec^{-1} \left( \frac{-9c_1 - x^3 + 3x^3 \log(x)}{9 \log(x)} \right) \right\}, \left\{ y(x) \rightarrow \sec^{-1} \left( \frac{-9c_1 - x^3 + 3x^3 \log(x)}{9 \log(x)} \right) \right\} \right\}$$

**Maple:** cpu = 0.500 (sec), leaf count = 27

$$\left\{ y(x) = \arccos \left( 9 \frac{\ln(x)}{3x^3 \ln(x) - x^3 + 9 C1} \right) \right\}$$

**2.818 ODE No. 818**

$$\frac{d}{dx}y(x) = \frac{y(x)}{x(-1 + xy(x) + x(y(x))^3 + x(y(x))^4)} = 0$$

**Mathematica:** cpu = 0.047006 (sec), leaf count = 34

$$\text{Solve}\left[\frac{y(x)^3}{3} + \frac{y(x)^2}{2} + \frac{1}{xy(x)} + \log(y(x)) = c_1, y(x)\right]$$

**Maple:** cpu = 0.109 (sec), leaf count = 34

$$\left\{y(x) = e^{\text{RootOf}(-2x(e^{-Z})^4 - 3x(e^{-Z})^3 + 6\_C1 e^{-Z}x - 6e^{-Z} - Zx - 6)}\right\}$$

**2.819 ODE No. 819**

$$\frac{d}{dx}y(x) = -2/3x + \sqrt{x^2 + 3y(x)} + x^2\sqrt{x^2 + 3y(x)} + x^3\sqrt{x^2 + 3y(x)} = 0$$

**Mathematica:** cpu = 0.230029 (sec), leaf count = 65

$$\left\{\left\{y(x) \rightarrow \frac{1}{192}(-72c_1x^4 - 96c_1x^3 - 288c_1x + 144c_1^2 + 9x^8 + 24x^7 + 16x^6 + 72x^5 + 96x^4 + 80x^2)\right\}\right\}$$

**Maple:** cpu = 0.265 (sec), leaf count = 32

$$\left\{\frac{2}{3}\sqrt{x^2 + 3y(x)} - \frac{x^4}{4} - \frac{x^3}{3} - x - \_C1 = 0\right\}$$

**2.820 ODE No. 820**

$$\frac{d}{dx}y(x) = 1/2 \frac{-2 \cos(y(x)) + x^2 \cos(2y(x)) \ln(x) + x^2 \ln(x)}{\sin(y(x)) \ln(x) x} = 0$$

**Mathematica:** cpu = 0.340543 (sec), leaf count = 63

$$\left\{\left\{y(x) \rightarrow -\sec^{-1}\left(\frac{-4c_1 - x^2 + 2x^2 \log(x)}{4 \log(x)}\right)\right\}, \left\{y(x) \rightarrow \sec^{-1}\left(\frac{-4c_1 - x^2 + 2x^2 \log(x)}{4 \log(x)}\right)\right\}\right\}$$

**Maple:** cpu = 0.530 (sec), leaf count = 27

$$\left\{y(x) = \arccos\left(4 \frac{\ln(x)}{2x^2 \ln(x) - x^2 + 4\_C1}\right)\right\}$$

**2.821 ODE No. 821**

$$\frac{d}{dx}y(x) = \frac{y(x)(xy(x)+1)}{x(-xy(x)-1+(y(x))^4x^3)} = 0$$

**Mathematica:** cpu = 0.034004 (sec), leaf count = 2093

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{4} - \frac{1}{2} \sqrt{\frac{c_1^2}{4} + \frac{\sqrt[3]{1944c_1^2x^6 + 1458x^5 + \sqrt{(1944c_1^2x^6 + 1458x^5)^2 - 4(54c_1x^4 + 144x^3)^3}}{18\sqrt[3]{2x^3}}}} \right\} \right.$$

**Maple:** cpu = 0.124 (sec), leaf count = 27

$$\left\{ -\frac{1}{2x^2(y(x))^2} - \frac{1}{3x^3(y(x))^3} - y(x) + \_C1 = 0 \right\}$$

**2.822 ODE No. 822**

$$\frac{d}{dx}y(x) = 1/4 \left( 4e^{-x^2} - 4x^2e^{-x^2} + 4(y(x))^2 - 4x^2e^{-x^2}y(x) + x^4(e^{-x^2})^2 \right) x = 0$$

**Mathematica:** cpu = 0.042005 (sec), leaf count = 32

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{c_1 - \frac{x^2}{2}} + \frac{1}{2}e^{-x^2}x^2 \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 25

$$\left\{ y(x) = \frac{x^2e^{-x^2}}{2} + \left( -C1 - \frac{x^2}{2} \right)^{-1} \right\}$$

**2.823 ODE No. 823**

$$\frac{d}{dx}y(x) = \frac{y(x)(y(x)+x)}{x(x+y(x)+(y(x))^3+(y(x))^4)} = 0$$

**Mathematica:** cpu = 0.383049 (sec), leaf count = 39

$$\text{Solve}\left[\frac{y(x)^3}{3} + \frac{y(x)^2}{2} + \log(y(x)) - \frac{y(x)\log(x)+x}{y(x)} = c_1, y(x)\right]$$

**Maple:** cpu = 0.109 (sec), leaf count = 38

$$\left\{y(x) = e^{\text{RootOf}(-2(e^{-z})^4 - 3(e^{-z})^3 + 6\ln(x)e^{-z} + 6 - C1e^{-z} - 6ze^{-z} + 6x)}\right\}$$

**2.824 ODE No. 824**

$$\frac{d}{dx}y(x) = \frac{y(x)(x^3 + x^2y(x) + (y(x))^2)}{x^2(x-1)(y(x)+x)} = 0$$

**Mathematica:** cpu = 0.055007 (sec), leaf count = 68

$$\text{Solve}\left[-\frac{1}{2}\log\left(\frac{y(x)^2}{x^2} + \frac{y(x)}{x} + 1\right) + \log\left(\frac{y(x)}{x}\right) + \frac{\tan^{-1}\left(\frac{\frac{2y(x)+1}{x}}{\sqrt{3}}\right)}{\sqrt{3}} = c_1 + \log(1-x) - \log(x), y(x)\right]$$

**Maple:** cpu = 0.280 (sec), leaf count = 61

$$\left\{\ln\left(\frac{y(x)}{x}\right) - \frac{1}{2}\ln\left(\frac{(y(x))^2 + xy(x) + x^2}{x^2}\right) + \frac{\sqrt{3}}{3}\arctan\left(\frac{(x+2y(x))\sqrt{3}}{3x}\right) + \ln(x) - \ln(x-1) - \dots\right\}$$

**2.825 ODE No. 825**

$$\frac{d}{dx}y(x) = \frac{\left((x^2+1)^{3/2}x^2 + (x^2+1)^{3/2} + (y(x))^2(x^2+1)^{3/2} + x^2(y(x))^3 + (y(x))^3\right)x}{(x^2+1)^3} = 0$$

**Mathematica:** cpu = 0.183023 (sec), leaf count = 148

$$\text{Solve} \left[ -\frac{19}{3} \text{RootSum} \left[ -19\#1^3 + 6\sqrt[3]{38}\#1 - 19\&, \frac{\log \left( \frac{\frac{3xy(x)}{(x^2+1)^2} + \frac{x}{(x^2+1)^{3/2}}}{\sqrt[3]{38} \sqrt[3]{\frac{x^3}{(x^2+1)^{9/2}}} - \#1} \right)}{2\sqrt[3]{38} - 19\#1^2} \& \right] = c_1 + \frac{19^{2/3} \left( \frac{x^3}{(x^2+1)^9} \right)^{1/3}}{18} \right]$$

**Maple:** cpu = 0.062 (sec), leaf count = 89

$$\left\{ y(x) = \frac{19 \text{RootOf} \left( -1296 \int^{-Z} (361\_a^3 - 432\_a + 432)^{-1} d\_a + 2 \ln(x^2 + 1) + 3\_C1 \right) x^2 - 6x^2 + 1}{18} \right\}$$

## 2.826 ODE No. 826

$$\frac{d}{dx} y(x) = \frac{(3x(y(x))^2 + x + 3(y(x))^2)y(x)}{(6(y(x))^2 + x)x(1+x)} = 0$$

**Mathematica:** cpu = 0.570072 (sec), leaf count = 70

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{x} \sqrt{W \left( \frac{6e^{2c_1}x}{(x+1)^2} \right)}}{\sqrt{6}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{x} \sqrt{W \left( \frac{6e^{2c_1}x}{(x+1)^2} \right)}}{\sqrt{6}} \right\} \right\}$$

**Maple:** cpu = 0.234 (sec), leaf count = 51

$$\left\{ \left( (y(x))^{-2} + 6x^{-1} \right)^{-1} = \frac{x}{54} \left( e^{\text{RootOf} \left( -e^{-Z} \ln \left( \frac{(1+x)^2 (e^{-Z}+9)}{2x} \right) + 3\_C1 e^{-Z} + \_Z e^{-Z} + 9 \right)} + 9 \right) \right\}$$

## 2.827 ODE No. 827

$$\frac{d}{dx} y(x) = -\frac{-y(x) + x^3 \sqrt{(y(x))^2 + x^2} - x^2 \sqrt{(y(x))^2 + x^2 y(x)}}{x} = 0$$

**Mathematica:** cpu = 0.124516 (sec), leaf count = 111

$$\left\{ \left\{ y(x) \rightarrow \frac{x \left( -2e^{\sqrt{2}c_1 + \frac{\sqrt{2}x^3}{3}} + e^{2\sqrt{2}c_1 + \frac{2\sqrt{2}x^3}{3}} - 1 \right)}{2e^{\sqrt{2}c_1 + \frac{\sqrt{2}x^3}{3}} + e^{2\sqrt{2}c_1 + \frac{2\sqrt{2}x^3}{3}} - 1} \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 49

$$\left\{ \ln \left( 2 \frac{x \left( \sqrt{2 (y(x))^2 + 2x^2 + y(x) + x} \right)}{y(x) - x} \right) + \frac{\sqrt{2}x^3}{3} - \ln(x) - C1 = 0 \right\}$$

## 2.828 ODE No. 828

$$\frac{d}{dx}y(x) = \frac{(1 + 2y(x))(1 + y(x))}{x(-2y(x) - 2 + x(y(x))^3 + 2x(y(x))^4)} = 0$$

**Mathematica:** cpu = 0.208027 (sec), leaf count = 56

$$\text{Solve} \left[ -\frac{1}{8}y(x)^2 + \frac{3y(x)}{8} - \frac{1}{2x(2y(x)+1)} - \frac{1}{2} \log(y(x)+1) + \frac{1}{16} \log(2y(x)+1) = c_1, y(x) \right]$$

**Maple:** cpu = 0.202 (sec), leaf count = 54

$$\left\{ y(x) = \frac{1}{2} e^{\text{RootOf}(x(e^{-z})^3 - 8x(e^{-z})^2 + 16 \ln(1/2 e^{-z} + 1/2) x e^{-z} + 16 - C1 e^{-z} x - 2e^{-z} - z x + 7 x e^{-z} + 16)} - \frac{1}{2} \right\}$$

## 2.829 ODE No. 829

$$\frac{d}{dx}y(x) = 1/2 \frac{1 + 2 \sqrt{4x^2y(x) + 1}x^3 + 2x^5 \sqrt{4x^2y(x) + 1} + 2x^6 \sqrt{4x^2y(x) + 1}}{x^3} = 0$$

**Mathematica:** cpu = 0.388549 (sec), leaf count = 74

$$\left\{ \left\{ y(x) \rightarrow \frac{-160c_1x^7 - 200c_1x^6 - 400c_1x^4 + 400c_1^2x^2 + 16x^{12} + 40x^{11} + 25x^{10} + 80x^9 + 100x^8 + 100x^6}{400x^2} \right. \right.$$

**Maple:** cpu = 0.297 (sec), leaf count = 40

$$\left\{ -C1 + \frac{1}{x} \left( -4x^6 - 5x^5 - 10x^3 + 10 \sqrt{4x^2y(x) + 1} \right) = 0 \right\}$$



**2.830 ODE No. 830**

$$\frac{d}{dx}y(x) = \frac{y(x)(x - y(x))}{x(x - y(x) - (y(x))^3 - (y(x))^4)} = 0$$

**Mathematica:** cpu = 0.433555 (sec), leaf count = 37

$$\text{Solve} \left[ -\frac{1}{3}y(x)^3 - \frac{y(x)^2}{2} - \frac{x}{y(x)} - \log(y(x)) + \log(x) = c_1, y(x) \right]$$

**Maple:** cpu = 0.109 (sec), leaf count = 38

$$\left\{ y(x) = e^{\text{RootOf}(2(e^{-Z})^4 + 3(e^{-Z})^3 - 6 \ln(x)e^{-Z} + 6\_C1 e^{-Z} + 6\_Z e^{-Z} + 6x)} \right\}$$

**2.831 ODE No. 831**

$$\frac{d}{dx}y(x) = \frac{2a + \sqrt{-(y(x))^2 + 4ax} + x^2\sqrt{-(y(x))^2 + 4ax} + x^3\sqrt{-(y(x))^2 + 4ax}}{y(x)} = 0$$

**Mathematica:** cpu = 4.434063 (sec), leaf count = 145

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{12}\sqrt{576ax - 72c_1x^4 - 96c_1x^3 - 288c_1x - 144c_1^2 - 9x^8 - 24x^7 - 16x^6 - 72x^5 - 96x^4 - 144x^3 - 144x^2 - 144x - 144c_1} \right\} \right.$$

**Maple:** cpu = 0.234 (sec), leaf count = 35

$$\left\{ -\sqrt{-(y(x))^2 + 4ax} - \frac{x^4}{4} - \frac{x^3}{3} - x - \_C1 = 0 \right\}$$

**2.832 ODE No. 832**

$$\frac{d}{dx}y(x) = \frac{(x + y(x) + 1)y(x)}{((y(x))^4 + (y(x))^3 + (y(x))^2 + x)(1 + x)} = 0$$

**Mathematica:** cpu = 0.580574 (sec), leaf count = 2497

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{2}\sqrt{\frac{3\sqrt[3]{2}(-8x + 3c_1)}{\sqrt[3]{1944(c_1 + \log(x + 1))^2 + 972(c_1 + \log(x + 1)) + 3726x} + \sqrt{(1944(c_1 + \log(x + 1))}} \right\} \right.$$

Maple: cpu = 0.125 (sec), leaf count = 31

$$\left\{ \ln(1+x) + \frac{x}{y(x)} - \frac{(y(x))^3}{3} - \frac{(y(x))^2}{2} - y(x) + C1 = 0 \right\}$$

### 2.833 ODE No. 833

$$\frac{d}{dx}y(x) = -\frac{-y(x) + x^4\sqrt{(y(x))^2 + x^2} - x^3\sqrt{(y(x))^2 + x^2}y(x)}{x} = 0$$

Mathematica: cpu = 0.119015 (sec), leaf count = 105

$$\left\{ \left\{ y(x) \rightarrow \frac{x \left( -2e^{\sqrt{2}c_1 + \frac{x^4}{2\sqrt{2}}} + e^{2\sqrt{2}c_1 + \frac{x^4}{\sqrt{2}}} - 1 \right)}{2e^{\sqrt{2}c_1 + \frac{x^4}{2\sqrt{2}}} + e^{2\sqrt{2}c_1 + \frac{x^4}{\sqrt{2}}} - 1} \right\} \right\}$$

Maple: cpu = 0.125 (sec), leaf count = 49

$$\left\{ \ln \left( 2 \frac{x \left( \sqrt{2} (y(x))^2 + 2x^2 + y(x) + x \right)}{y(x) - x} \right) + \frac{\sqrt{2}x^4}{4} - \ln(x) - C1 = 0 \right\}$$

### 2.834 ODE No. 834

$$\frac{d}{dx}y(x) = \frac{(x^4 + 3x(y(x))^2 + 3(y(x))^2)y(x)}{(6(y(x))^2 + x)x(1+x)} = 0$$

Mathematica: cpu = 0.696088 (sec), leaf count = 90

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{x}\sqrt{W\left(\frac{6(x+1)^2e^{2c_1+x^2-2x-3}}{x}\right)}}{\sqrt{6}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{x}\sqrt{W\left(\frac{6(x+1)^2e^{2c_1+x^2-2x-3}}{x}\right)}}{\sqrt{6}} \right\} \right\}$$

Maple: cpu = 0.234 (sec), leaf count = 60

$$\left\{ \left( (y(x))^{-2} + 6x^{-1} \right)^{-1} = \frac{x}{54} \left( e^{\text{RootOf}\left(e^{-Zx^2 - e^{-Z}\ln\left(\frac{x(e^{-Z}+9)}{2(1+x)^2}\right)} + 3C1e^{-Z} + Ze^{-Z} - 2xe^{-Z} + 9\right)} + 9 \right) \right\}$$

**2.835 ODE No. 835**

$$\frac{d}{dx}y(x) = -\left(-((y(x))^3)^{2/3}x - {}_2F1((y(x))^3 - 3 \ln(x)) \sqrt[3]{(y(x))^3x}\right)^{-1} = 0$$

**Mathematica:** cpu = 2.560325 (sec), leaf count = 47

$$\text{DSolve}\left[y'(x) = -\frac{1}{x\left(-\sqrt[3]{y(x)^3}\right) {}_2F1(y(x)^3 - 3 \log(x)) - x(y(x)^3)^{2/3}}, y(x), x\right]$$

**Maple:** cpu = 1.638 (sec), leaf count = 0

could not solve

**2.836 ODE No. 836**

$$\frac{d}{dx}y(x) = \frac{y(x)(x - y(x))(1 + y(x))}{x(xy(x) + x - y(x))} = 0$$

**Mathematica:** cpu = 12.338567 (sec), leaf count = 386

$$\text{Solve}\left[\frac{2^{2/3}(x-1)^2\left(\frac{x^6}{(x-1)^3}\right)^{2/3}}{9x^3} = c_1 + \frac{2^{2/3}\left(1 - \frac{(x-1)^2\left(\frac{x^6}{(x-1)^3}\right)^{2/3}((x+2)y(x)+x)}{x^4((x-1)y(x)+x)}\right)\left(\frac{\left(\frac{x^6}{(x-1)^3}\right)^{2/3}(x-1)^2((x+2)y(x)+x)}{x^4((x-1)y(x)+x)}\right)}{9x^3}\right]$$

**Maple:** cpu = 0.156 (sec), leaf count = 102

$$\left\{y(x) = -xe^{\text{RootOf}\left(-\ln\left(\frac{e^{-Z}}{2} + \frac{9}{2}\right)e^{-Z} + 3\_C1 e^{-Z} +\_Z e^{-Z} - xe^{-Z} + 9\right)}\left(e^{\text{RootOf}\left(-\ln\left(\frac{e^{-Z}}{2} + \frac{9}{2}\right)e^{-Z} + 3\_C1 e^{-Z} +\_Z e^{-Z} - xe^{-Z} + 9\right)}\right)\right.$$

**2.837 ODE No. 837**

$$\frac{d}{dx}y(x) = -\left(-\ln(x) ((y(x))^3)^{2/3} - {}_2F1((y(x))^3 + 3 Ei(1, -\ln(x))) \ln(x) \sqrt[3]{(y(x))^3}\right)^{-1} = 0$$

**Mathematica:** cpu = 3.085892 (sec), leaf count = 52

$$\text{DSolve}\left[y'(x) = -\frac{1}{-\sqrt[3]{y(x)^3} \log(x) {}_2F1(3Ei(-\log(x)) + y(x)^3) - (y(x)^3)^{2/3} \log(x)}, y(x), x\right]$$

**Maple:** cpu = 1.700 (sec), leaf count = 0

could not solve

**2.838 ODE No. 838**

$$\frac{d}{dx}y(x) = 1/25 \frac{30x^3 + 25\sqrt{x} + 25(y(x))^2 - 20x^3y(x) - 100y(x)\sqrt{x} + 4x^6 + 40x^{7/2} + 100x}{x} = 0$$

**Mathematica:** cpu = 0.027003 (sec), leaf count = 31

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{c_1 - \log(x)} + \frac{2}{5} \sqrt{x} (x^{5/2} + 5) \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 27

$$\left\{ y(x) = -\frac{x}{2} \left( -\frac{4x^2}{5} - 4\frac{1}{\sqrt{x}} \right) + (_C1 - \ln(x))^{-1} \right\}$$

**2.839 ODE No. 839**

$$\frac{d}{dx}y(x) = \frac{1}{x} \left( e^{-\frac{y(x)}{x}} y(x) + e^{-\frac{y(x)}{x}} x + x^2 \right) e^{\frac{y(x)}{x}} = 0$$

**Mathematica:** cpu = 0.068009 (sec), leaf count = 28

$$\left\{ \left\{ y(x) \rightarrow -x \log\left(\frac{e^{2c_1}}{2x} - \frac{x}{2}\right) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 19

$$\left\{ y(x) = \ln\left(2 \frac{x}{-x^2 + _C1}\right) x \right\}$$

**2.840 ODE No. 840**

$$\frac{d}{dx}y(x) = \frac{1}{x} \left( e^{-\frac{y(x)}{x}} y(x) + e^{-\frac{y(x)}{x}} x + x^3 \right) e^{\frac{y(x)}{x}} = 0$$

**Mathematica:** cpu = 0.096012 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow -x \log \left( \frac{e^{3c_1}}{3x} - \frac{x^2}{3} \right) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 19

$$\left\{ y(x) = \ln \left( 3 \frac{x}{-x^3 + \_C1} \right) x \right\}$$

**2.841 ODE No. 841**

$$\frac{d}{dx}y(x) = \frac{bx^3 + c^2\sqrt{a} - 2cbx^2\sqrt{a} + 2c(y(x))^2 a^{3/2} + b^2x^4\sqrt{a} - 2(y(x))^2 a^{3/2}bx^2 + a^{5/2}(y(x))^4}{ax^2y(x)} = 0$$

**Mathematica:** cpu = 1.255659 (sec), leaf count = 236

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{2a^{5/2}bx^2 - 2a^{5/2}c + 4a^3b^2x^3 - 4a^3bcx + a^2x + 4\sqrt{ab^2}c_1x^2 - 4\sqrt{ab}cc_1 + 2bc_1x}}{\sqrt{2}\sqrt{2a^{3/2}bc_1 + a^{7/2} + 2a^4bx}} \right\}, \left\{ y(x) \rightarrow \dots \right\} \right.$$

**Maple:** cpu = 0.234 (sec), leaf count = 97

$$\left\{ y(x) = \frac{1}{x\_C1 + 1} \sqrt{\left( (x\_C1 + 1)(bx^2 - c)\sqrt{a} + \frac{x}{2} \right) (x\_C1 + 1) a^{\frac{3}{2}} a^{-\frac{3}{2}}}, y(x) = -2 \frac{\sqrt{\left( (x\_C1 + 1)(bx^2 - c)\sqrt{a} + \frac{x}{2} \right) (x\_C1 + 1) a^{\frac{3}{2}} a^{-\frac{3}{2}}}}{\dots} \right.$$

**2.842 ODE No. 842**

$$\frac{d}{dx}y(x) = \frac{y(x) + x^2(\ln(x))^3 + 2x^2(\ln(x))^2 y(x) + x^2 \ln(x) (y(x))^2}{x \ln(x)} = 0$$

**Mathematica:** cpu = 0.122015 (sec), leaf count = 186

$$\left\{ \left\{ y(x) \rightarrow -\frac{c_1 e^{\frac{1}{4}x^2(2\log(x)-1)} \left( \frac{x}{2} + \frac{1}{2}x(2\log(x)-1) \right) + \frac{1}{4}x^2 e^{\frac{1}{4}x^2(2\log(x)-1)} (2\log(x)-1) \left( \frac{x}{2} + \frac{1}{2}x(2\log(x)-1) \right)}{x \left( c_1 e^{\frac{1}{4}x^2(2\log(x)-1)} + \frac{1}{4}x^2 e^{\frac{1}{4}x^2(2\log(x)-1)} (2\log(x)-1) \right)} \right\} \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 43

$$\left\{ y(x) = -\frac{\ln(x) (2x^2 \ln(x) - x^2 + 2\_C1 + 4)}{2x^2 \ln(x) - x^2 + 2\_C1} \right\}$$

**2.843 ODE No. 843**

$$\frac{d}{dx}y(x) = \frac{y(x) + x^3(\ln(x))^3 + 2x^3(\ln(x))^2 y(x) + x^3 \ln(x)(y(x))^2}{x \ln(x)} = 0$$

**Mathematica:** cpu = 0.124016 (sec), leaf count = 198

$$\left\{ \left\{ y(x) \rightarrow -\frac{c_1 e^{\frac{1}{9}x^3(3\log(x)-1)} \left( \frac{x^2}{3} + \frac{1}{3}x^2(3\log(x)-1) \right) + \frac{1}{9}x^3 e^{\frac{1}{9}x^3(3\log(x)-1)}(3\log(x)-1) \left( \frac{x^2}{3} + \frac{1}{3}x^2(3\log(x)-1) \right)}{x^2 \left( c_1 e^{\frac{1}{9}x^3(3\log(x)-1)} + \frac{1}{9}x^3 e^{\frac{1}{9}x^3(3\log(x)-1)}(3\log(x)-1) \right)} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 43

$$\left\{ y(x) = -\frac{\ln(x)(6x^3 \ln(x) - 2x^3 + 9\_C1 + 18)}{6x^3 \ln(x) - 2x^3 + 9\_C1} \right\}$$

**2.844 ODE No. 844**

$$\frac{d}{dx}y(x) = \frac{y(x)(y(x)+x)(1+y(x))}{x(xy(x)+x+y(x))} = 0$$

**Mathematica:** cpu = 16.574105 (sec), leaf count = 386

$$\text{Solve} \left[ \frac{2^{2/3} \left( 1 - \frac{\left( \frac{x^6}{(x+1)^3} \right)^{2/3} (x+1)^2 ((x-2)y(x)+x)}{x^4((x+1)y(x)+x)} \right) \left( \frac{\left( \frac{x^6}{(x+1)^3} \right)^{2/3} (x+1)^2 ((x-2)y(x)+x)}{x^4((x+1)y(x)+x)} + 2 \right) \left( \left( 1 - \frac{\left( \frac{x^6}{(x+1)^3} \right)^{2/3} (x+1)^2 ((x-2)y(x)+x)}{x^4((x+1)y(x)+x)} \right) \right)}{9 \left( \frac{3}{\dots} \right)} \right]$$

**Maple:** cpu = 0.140 (sec), leaf count = 97

$$\left\{ y(x) = -x e^{\text{RootOf}\left(-\ln\left(\frac{e^{-Z}}{2} + \frac{9}{2}\right)\right) e^{-Z} + 3\_C1 e^{-Z} +\_Z e^{-Z} + x e^{-Z} + 9} \left( e^{\text{RootOf}\left(-\ln\left(\frac{e^{-Z}}{2} + \frac{9}{2}\right)\right) e^{-Z} + 3\_C1 e^{-Z} +\_Z e^{-Z} + x e^{-Z} + 9} \right) \right\}$$

## 2.845 ODE No. 845

$$\frac{d}{dx}y(x) = \frac{3x^3 + \sqrt{-9x^4 + 4(y(x))^3} + x^2\sqrt{-9x^4 + 4(y(x))^3} + x^3\sqrt{-9x^4 + 4(y(x))^3}}{(y(x))^2} = 0$$

**Mathematica:** cpu = 4.914124 (sec), leaf count = 227

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{2} \sqrt[3]{-\frac{1}{2} \sqrt[3]{72c_1x^4 + 96c_1x^3 + 288c_1x + 144c_1^2 + 9x^8 + 24x^7 + 16x^6 + 72x^5 + 132x^4 + 144x^2}} \right\} \right\}$$

**Maple:** cpu = 0.187 (sec), leaf count = 44

$$\left\{ \int_{-b}^{y(x)} -a^2 \frac{1}{\sqrt{-9x^4 + 4a^3}} d_a - \frac{x^4}{4} - \frac{x^3}{3} - x - C1 = 0 \right\}$$

## 2.846 ODE No. 846

$$\frac{d}{dx}y(x) = (-x + ((y(x))^{-1} + 1)x + \_F1(((y(x))^{-1} + 1)x)x^2 - \_F1(((y(x))^{-1} + 1)x)x^2((y(x))^{-1} + 1) + \dots)$$

**Mathematica:** cpu = 1.356672 (sec), leaf count = 362

$$\text{Solve} \left[ \int_1^{y(x)} \left( \frac{x\_F1\left(x\left(\frac{1}{K[2]} + 1\right)\right) - 1}{xK[2]\_F1\left(x\left(\frac{1}{K[2]} + 1\right)\right) + x\_F1\left(x\left(\frac{1}{K[2]} + 1\right)\right) - K[2]} - \int_1^x \left( \frac{-\frac{K[1]\_F1'\left(K[1]\left(\frac{1}{K[2]} + 1\right)\right)}{K[2]}}{K[1]\left(K[2]\_F1\left(K[1]\left(\frac{1}{K[2]} + 1\right)\right)\right)} \right) \right]$$

**Maple:** cpu = 0.141 (sec), leaf count = 40

$$\left\{ y(x) = e^{\text{RootOf}\left(-Z - \int \frac{x e^{-Z}}{e^{-Z} - 1} \frac{1}{(\_F1(-a) - a - 1) - a} d_a + C1\right)} - 1 \right\}$$

**2.847 ODE No. 847**

$$\frac{d}{dx}y(x) = x/2 + 1/2 + \sqrt{x^2 + 2x + 1 - 4y(x)} + x^2\sqrt{x^2 + 2x + 1 - 4y(x)} + x^3\sqrt{x^2 + 2x + 1 - 4y(x)}$$

**Mathematica:** cpu = 0.365046 (sec), leaf count = 69

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{144} (72c_1x^4 + 96c_1x^3 + 288c_1x - 144c_1^2 - 9x^8 - 24x^7 - 16x^6 - 72x^5 - 96x^4 - 108x^2 + 72x + \dots \right. \right.$$

**Maple:** cpu = 0.265 (sec), leaf count = 36

$$\left\{ -\frac{1}{2}\sqrt{x^2 + 2x + 1 - 4y(x)} - \frac{x^4}{4} - \frac{x^3}{3} - x - C1 = 0 \right\}$$

**2.848 ODE No. 848**

$$\frac{d}{dx}y(x) = \frac{\cosh(x)}{\sinh(x)} + {}_2F1(y(x) - \ln(\sinh(x))) = 0$$

**Mathematica:** cpu = 0.109014 (sec), leaf count = 154

$$\text{Solve} \left[ \int_1^{y(x)} \frac{{}_2F1(K[2] - \log(\sinh(x))) \left( \int_1^x \left( \frac{{}_2F1'(K[2] - \log(\sinh(K[1]))}({}_2F1(K[2] - \log(\sinh(K[1])) + \coth(K[1]))}({}_2F1(K[2] - \log(\sinh(K[1])))^2)} \right) dx - \frac{{}_2F1(K[2] - \log(\sinh(x)))}{{}_2F1(K[2] - \log(\sinh(x)))} \right)}{{}_2F1(K[2] - \log(\sinh(x)))} \right]$$

**Maple:** cpu = 0.405 (sec), leaf count = 27

$$\left\{ \int_{-b}^{y(x)} ({}_2F1(a - \ln(\sinh(x))))^{-1} da - x - C1 = 0 \right\}$$

**2.849 ODE No. 849**

$$\frac{d}{dx}y(x) = -x/2 + 1 + \sqrt{x^2 - 4x + 4y(x)} + x^2\sqrt{x^2 - 4x + 4y(x)} + x^3\sqrt{x^2 - 4x + 4y(x)} = 0$$

**Mathematica:** cpu = 0.323541 (sec), leaf count = 68

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{144} (-72c_1x^4 - 96c_1x^3 - 288c_1x + 144c_1^2 + 9x^8 + 24x^7 + 16x^6 + 72x^5 + 96x^4 + 108x^2 + 144x + \dots \right. \right.$$

**Maple:** cpu = 0.265 (sec), leaf count = 35

$$\left\{ \frac{1}{2}\sqrt{x^2 - 4x + 4y(x)} - \frac{x^4}{4} - \frac{x^3}{3} - x - C1 = 0 \right\}$$



**2.850 ODE No. 850**

$$\frac{d}{dx}y(x) = (\sin(x))^{-1} + \_F1(y(x) - \ln(\sin(x)) + \ln(\cos(x) + 1)) = 0$$

**Mathematica:** cpu = 0.197025 (sec), leaf count = 1478

Solve  $\left[ \int_1^{y(x)} \frac{\sin(x) \left( \left( \int_1^x \left( \frac{(\cot^2(K[1]) + \csc(K[1]) \cot(K[1]) + 1) \sin(K[1]) (\csc(K[1]) + \_F1(K[2] + \log(\cos(K[1]) + 1) - \log(\sin(K[1])))}{(-\cot^2(K[1]) + \_F1(K[2] + \log(\cos(K[1]) + 1) - \log(\sin(K[1]))) \cot(K[1]))} \right) dx \right) \right)}{\sin(x)} dx \right]$

**Maple:** cpu = 0.795 (sec), leaf count = 32

$$\left\{ \int_{-b}^{y(x)} (\_F1(\_a - \ln(\sin(x)) + \ln(\cos(x) + 1)))^{-1} d\_a - x - \_C1 = 0 \right\}$$

**2.851 ODE No. 851**

$$\frac{d}{dx}y(x) = \frac{b^3 + (y(x))^2 b^3 + 2y(x) b^2 a x + x^2 b a^2 + (y(x))^3 b^3 + 3(y(x))^2 b^2 a x + 3y(x) b a^2 x^2 + a^3 x^3}{b^3} = 0$$

**Mathematica:** cpu = 0.155520 (sec), leaf count = 145

Solve  $\left[ -\frac{1}{3}(27a + 29b)^{2/3} \text{RootSum} \left[ \#1^3(27a + 29b)^{2/3} - 3\#1b^{2/3} + (27a + 29b)^{2/3} \&x, \frac{\log\left(\frac{3ax+b+3y(x)}{\sqrt[3]{\frac{27a+29b}{b}}}\right)}{b^{2/3} - \#1^2(27a + 29b)^{2/3}} \right] \right]$

**Maple:** cpu = 0.047 (sec), leaf count = 42

$$\left\{ y(x) = \frac{\text{RootOf}\left(\int^{-Z} (\_a^3 b + \_a^2 b + a + b)^{-1} d\_a b - x + \_C1\right) b - a x}{b} \right\}$$

**2.852 ODE No. 852**

$$\frac{d}{dx}y(x) = \frac{\alpha^3 + (y(x))^2 \alpha^3 + 2y(x) \alpha^2 \beta x + \alpha \beta^2 x^2 + (y(x))^3 \alpha^3 + 3(y(x))^2 \alpha^2 \beta x + 3y(x) \alpha \beta^2 x^2 + \beta^3 x^3}{\alpha^3}$$

**Mathematica:** cpu = 0.149019 (sec), leaf count = 145

$$\text{Solve} \left[ -\frac{1}{3}(29\alpha + 27\beta)^{2/3} \text{RootSum} \left[ \#1^3(29\alpha + 27\beta)^{2/3} - 3\#1\alpha^{2/3} + (29\alpha + 27\beta)^{2/3}\& \right], \frac{\log \left( \frac{\alpha + 3\beta x + 3y(x)}{\sqrt[3]{\frac{29\alpha + 27\beta}{\alpha}}} \right)}{\alpha^{2/3} - \#1^2(29\alpha + 27\beta)^{2/3}} \right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 42

$$\left\{ y(x) = \frac{\text{RootOf} \left( \int^{-Z} (_a^3 \alpha + _a^2 \alpha + \alpha + \beta)^{-1} d_a \alpha - x + _C1 \right) \alpha - \beta x}{\alpha} \right\}$$

## 2.853 ODE No. 853

$$\frac{d}{dx} y(x) = \frac{14xy(x) + 12 + 2x + x^3(y(x))^3 + 6x^2(y(x))^2}{x^2(xy(x) + 2 + x)} = 0$$

**Mathematica:** cpu = 0.016502 (sec), leaf count = 76

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{x^3 \left( \frac{1}{x^3} - \frac{1}{x^3 \sqrt{c_1 - 2x}} \right)} - \frac{x + 2}{x} \right\}, \left\{ y(x) \rightarrow \frac{1}{x^3 \left( \frac{1}{x^3 \sqrt{c_1 - 2x}} + \frac{1}{x^3} \right)} - \frac{x + 2}{x} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 65

$$\left\{ y(x) = -\frac{1}{x} \left( 2 \sqrt{-C1 - 2x} - x - 2 \right) \left( \sqrt{-C1 - 2x} - 1 \right)^{-1}, y(x) = -\frac{1}{x} \left( 2 \sqrt{-C1 - 2x} + x + 2 \right) \left( \sqrt{-C1 - 2x} + 1 \right)^{-1} \right\}$$

## 2.854 ODE No. 854

$$\frac{d}{dx} y(x) = \frac{y(x) (\ln(x) + \ln(y(x)) - 1 + x^2(\ln(x))^2 + 2x^2 \ln(y(x)) \ln(x) + x^2(\ln(y(x)))^2)}{x} = 0$$

**Mathematica:** cpu = 0.623579 (sec), leaf count = 49

$$\text{DSolve} \left[ y'(x) = \frac{y(x) (x^2 \log^2(y(x)) + 2x^2 \log(x) \log(y(x)) + x^2 \log^2(x) + \log(y(x)) + \log(x) - 1)}{x}, y(x), x \right]$$

**Maple:** cpu = 0.156 (sec), leaf count = 51

$$\left\{ y(x) = 1 \left( x^{\frac{x^3}{x^3+3-C1}} \right)^{-1} \left( x^{\frac{C1}{x^3+3-C1}} \right)^{-3} \left( e^{\frac{x}{x^3+3-C1}} \right)^{-3} \right\}$$

**2.855 ODE No. 855**

$$\frac{d}{dx}y(x) = \frac{y(x) (\ln(y(x)) - 1 + \ln(x) + x^3(\ln(x))^2 + 2x^3 \ln(y(x)) \ln(x) + x^3(\ln(y(x)))^2)}{x} = 0$$

**Mathematica:** cpu = 0.671585 (sec), leaf count = 49

$$\text{DSolve}\left[y'(x) = \frac{y(x) (x^3 \log^2(y(x)) + 2x^3 \log(x) \log(y(x)) + x^3 \log^2(x) + \log(y(x)) + \log(x) - 1)}{x}, y(x), x\right]$$

**Maple:** cpu = 0.156 (sec), leaf count = 51

$$\left\{ y(x) = 1 \left( x^{\frac{x^4}{x^4+4-C1}} \right)^{-1} \left( x^{\frac{C1}{x^4+4-C1}} \right)^{-4} \left( e^{\frac{x}{x^4+4-C1}} \right)^{-4} \right\}$$

**2.856 ODE No. 856**

$$\frac{d}{dx}y(x) = -\frac{x}{\sqrt{(y(x))^2}} (-x^{-1} - \_F1((y(x))^2 - 2x)) = 0$$

**Mathematica:** cpu = 0.894114 (sec), leaf count = 100

$$\text{Solve}\left[\int_1^{y(x)} \left( \frac{\sqrt{K[2]^2}}{\_F1(K[2]^2 - 2x)} - \int_1^x \frac{2K[2]\_F1'(K[2]^2 - 2K[1])}{(\_F1(K[2]^2 - 2K[1]))^2} dK[1] \right) dK[2] + \int_1^x \left( -\frac{1}{\_F1(y(x)^2 - 2x)} \right) dx = 0 \right]$$

**Maple:** cpu = 0.218 (sec), leaf count = 65

$$\left\{ y(x) = \sqrt{2 \text{RootOf}\left(x^2 - 2 \int^{-Z} (\_F1(2\_a))^{-1} d\_a + 4\_C1\right)} + 2x, y(x) = -\sqrt{2 \text{RootOf}\left(x^2 - 2 \int^{-Z} (\_F1(2\_a))^{-1} d\_a + 4\_C1\right)} + 2x \right\}$$

**2.857 ODE No. 857**

$$\frac{d}{dx}y(x) = -x/4 + 1/4 + \sqrt{x^2 - 2x + 1 + 8y(x)} + x^2 \sqrt{x^2 - 2x + 1 + 8y(x)} + x^3 \sqrt{x^2 - 2x + 1 + 8y(x)}$$

**Mathematica:** cpu = 0.341543 (sec), leaf count = 69

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{72} (-72c_1x^4 - 96c_1x^3 - 288c_1x + 144c_1^2 + 9x^8 + 24x^7 + 16x^6 + 72x^5 + 96x^4 + 135x^2 + 18x - 72c_1) \right\} \right\}$$

**Maple:** cpu = 0.265 (sec), leaf count = 36

$$\left\{ \frac{1}{4} \sqrt{x^2 - 2x + 1 + 8y(x)} - \frac{x^4}{4} - \frac{x^3}{3} - x - \_C1 = 0 \right\}$$

**2.858 ODE No. 858**

$$\frac{d}{dx}y(x) = \frac{a^3 + (y(x))^2 a^3 + 2 y(x) a^2 b x + a b^2 x^2 + (y(x))^3 a^3 + 3 (y(x))^2 a^2 b x + 3 y(x) a b^2 x^2 + b^3 x^3}{a^3} = 0$$

**Mathematica:** cpu = 0.160520 (sec), leaf count = 145

$$\text{Solve} \left[ -\frac{1}{3}(29a + 27b)^{2/3} \text{RootSum} \left[ \#1^3(29a + 27b)^{2/3} - 3\#1a^{2/3} + (29a + 27b)^{2/3} \&, \frac{\log \left( \frac{a+3bx+3y(x)}{\sqrt[3]{29a+27b}} - \dots \right)}{a^{2/3} - \#1^2(29a + 27b)^{2/3}} \right] \right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 42

$$\left\{ y(x) = \frac{\text{RootOf} \left( \int^{-Z} (_{a^3}a + _{a^2}a + a + b)^{-1} d_{aa} - x + _{C1} \right) a - bx}{a} \right\}$$

**2.859 ODE No. 859**

$$\frac{d}{dx}y(x) = -\frac{-x - \_F1((y(x))^2 - 2x)}{\sqrt{(y(x))^2 x}} = 0$$

**Mathematica:** cpu = 1.297665 (sec), leaf count = 102

$$\text{Solve} \left[ \int_1^{y(x)} \left( \frac{\sqrt{K[2]^2}}{\_F1(K[2]^2 - 2x)} - \int_1^x \frac{2K[2]\_F1'(K[2]^2 - 2K[1])}{(\_F1(K[2]^2 - 2K[1]))^2} dK[1] \right) dK[2] + \int_1^x \left( -\frac{1}{\_F1(y(x)^2 - 2x)} \right) dx \right]$$

**Maple:** cpu = 0.218 (sec), leaf count = 63

$$\left\{ y(x) = \sqrt{2 \text{RootOf} \left( \ln(x) - \int^{-Z} (\_F1(2\_a))^{-1} d\_a + 2\_C1 \right) + 2x}, y(x) = -\sqrt{2 \text{RootOf} \left( \ln(x) - \int^{-Z} (\_F1(2\_a))^{-1} d\_a + 2\_C1 \right) + 2x} \right\}$$

**2.860 ODE No. 860**

$$\frac{d}{dx}y(x) = 1/2 \frac{-\sin(2y(x)) + x \cos(2y(x)) + \cos(2y(x))x^3 + \cos(2y(x))x^4 + x + x^3 + x^4}{x} = 0$$

**Mathematica:** cpu = 0.150519 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow \tan^{-1} \left( \frac{10c_1 + 4x^5 + 5x^4 + 10x^2}{20x} \right) \right\} \right\}$$

**Maple:** cpu = 1.669 (sec), leaf count = 29

$$\left\{ y(x) = \arctan \left( \frac{4x^5 + 5x^4 + 10x^2 + 40\_C1}{20x} \right) \right\}$$

**2.861 ODE No. 861**

$$\frac{d}{dx}y(x) = -\frac{1}{x} \left( -\frac{y(x)}{x} (e^{-x^{-1}})^{-1} - {}_2F1 \left( y(x) (e^{-x^{-1}})^{-1} \right) \right) e^{-x^{-1}} = 0$$

**Mathematica:** cpu = 1.815230 (sec), leaf count = 155

$$\text{Solve} \left[ \int_1^{y(x)} \frac{{}_2F1 \left( e^{\frac{1}{x}} K[2] \right) \left( \int_1^x \left( \frac{e^{\frac{1}{K[1]}}}{K[1]^2 {}_2F1 \left( e^{\frac{1}{K[1]} K[2]} \right)} - \frac{e^{\frac{2}{K[1]} K[2]} {}_2F1' \left( e^{\frac{1}{K[1]} K[2]} \right)}{K[1]^2 \left( {}_2F1 \left( e^{\frac{1}{K[1]} K[2]} \right) \right)^2} \right) dK[1]}{{}_2F1 \left( e^{\frac{1}{x}} K[2] \right)} + e^{\frac{1}{x}}}{dK[2]} \right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 26

$$\left\{ y(x) = \frac{\text{RootOf} \left( -\ln(x) + \int^{-Z} ({}_2F1(\_a))^{-1} d\_a + \_C1 \right)}{e^{x^{-1}}} \right\}$$

**2.862 ODE No. 862**

$$\frac{d}{dx}y(x) = -\left(\frac{\text{Ei}(1, -\ln(-1 + y(x)))}{x} - \_F1(x)\right) \ln(-1 + y(x)) = 0$$

**Mathematica:** cpu = 1.114141 (sec), leaf count = 32

$$\text{DSolve}\left[y'(x) = \log(y(x) - 1) \left(\_F1(x) - \frac{\text{Ei}(-\log(y(x) - 1))}{x}\right), y(x), x\right]$$

**Maple:** cpu = 0.172 (sec), leaf count = 27

$$\left\{y(x) = e^{\text{RootOf}\left(\int \frac{-F1(x)}{x} dx + x\_C1 + \text{Ei}(1, -Z)\right)} + 1\right\}$$

**2.863 ODE No. 863**

$$\frac{d}{dx}y(x) = \frac{y(x) + x\sqrt{(y(x))^2 + x^2} + x^3\sqrt{(y(x))^2 + x^2} + x^4\sqrt{(y(x))^2 + x^2}}{x} = 0$$

**Mathematica:** cpu = 0.034504 (sec), leaf count = 30

$$\left\{\left\{y(x) \rightarrow x \sinh\left(\frac{1}{12}(12c_1 + 3x^4 + 4x^3 + 12x)\right)\right\}\right\}$$

**Maple:** cpu = 2.355 (sec), leaf count = 38

$$\left\{\ln\left(y(x) + \sqrt{(y(x))^2 + x^2}\right) - \frac{x^4}{4} - \frac{x^3}{3} - x - \ln(x) - \_C1 = 0\right\}$$

**2.864 ODE No. 864**

$$\frac{d}{dx}y(x) = \frac{y(x) \left( \left( e^{-1/4x^2} \right)^2 xy(x) + e^{-1/4x^2} x + 2(y(x))^2 e^{-3/4x^2} \right) e^{1/4x^2}}{2y(x) e^{-1/4x^2} + 2} = 0$$

**Mathematica:** cpu = 0.041005 (sec), leaf count = 137

$$\left\{\left\{y(x) \rightarrow \frac{2e^{\frac{x^2}{2}}}{\sqrt{2}\sqrt{2e^{\frac{x^2}{2}}(c_1 - 2x) + 2e^{\frac{x^2}{2}} - 2e^{\frac{x^2}{4}}}}\right\}, \left\{y(x) \rightarrow -\frac{2e^{\frac{x^2}{2}}}{\sqrt{2}\sqrt{2e^{\frac{x^2}{2}}(c_1 - 2x) + 2e^{\frac{x^2}{2}} + 2e^{\frac{x^2}{4}}}}\right\}\right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 186

$$\left\{y(x) = 1\left(e^{-\frac{x^2}{4}}\sqrt{\_C1 - 2xe^{\frac{x^2}{2}}} - e^{-\frac{x^2}{4}}e^{\frac{x^2}{2}} - e^{\frac{x^2}{4}}\sqrt{\_C1 - 2x}\right)\left(e^{-\frac{x^2}{4}}\right)^{-1}\left(e^{-\frac{x^2}{4}}e^{\frac{x^2}{2}} + e^{\frac{x^2}{4}}\sqrt{\_C1 - 2x}\right)\right\}$$

**2.865 ODE No. 865**

$$\frac{d}{dx}y(x) = \left( \frac{\ln(-1+y(x))y(x)}{(1-y(x))\ln(x)x} - \frac{\ln(-1+y(x))}{(1-y(x))\ln(x)x} - f(x) \right) (1-y(x)) = 0$$

**Mathematica:** cpu = 150.792648 (sec), leaf count = 84

Solve  $\left[ \int_1^x \left( -\frac{f(K[1])}{\log(K[1])} - \frac{\log(y(x)-1)}{K[1]\log^2(K[1])} \right) dK[1] + \int_1^{y(x)} \left( \frac{1}{\log(x)(K[2]-1)} - \int_1^x \frac{1}{K[1](K[2]-1)} \log(x) dx \right) dK[2] \right]$

**Maple:** cpu = 0.156 (sec), leaf count = 23

$$\left\{ y(x) = e^{\int \frac{f(x)}{\ln(x)} dx \ln(x)} x^{-C1} + 1 \right\}$$

**2.866 ODE No. 866**

$$\frac{d}{dx}y(x) = -x/2 - a/2 + \sqrt{x^2 + 2ax + a^2 + 4y(x)} + x^2\sqrt{x^2 + 2ax + a^2 + 4y(x)} + x^3\sqrt{x^2 + 2ax + a^2 + 4y(x)}$$

**Mathematica:** cpu = 0.500063 (sec), leaf count = 74

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{144}(-36a^2 - 72ax - 72c_1x^4 - 96c_1x^3 - 288c_1x + 144c_1^2 + 9x^8 + 24x^7 + 16x^6 + 72x^5 + 96x^4) \right\} \right\}$$

**Maple:** cpu = 0.437 (sec), leaf count = 39

$$\left\{ \frac{1}{2}\sqrt{x^2 + 2ax + a^2 + 4y(x)} - \frac{x^4}{4} - \frac{x^3}{3} - x - \_C1 = 0 \right\}$$

**2.867 ODE No. 867**

$$\frac{d}{dx}y(x) = -2/3x + 1 + (y(x))^2 + 2/3x^2y(x) + 1/9x^4 + (y(x))^3 + x^2(y(x))^2 + 1/3y(x)x^4 + 1/27x^6$$

**Mathematica:** cpu = 0.059508 (sec), leaf count = 77

Solve  $\left[ -\frac{29}{3}\text{RootSum}\left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{x^2+3y(x)+1}{\sqrt[3]{29}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2}\& \right] = c_1 + \frac{1}{9}29^{2/3}x, y(x) \right]$

**Maple:** cpu = 0.046 (sec), leaf count = 30

$$\left\{ y(x) = -\frac{x^2}{3} + \text{RootOf}\left( -x + \int^{-Z} (-a^3 + a^2 + 1)^{-1} da + \_C1 \right) \right\}$$

**2.868 ODE No. 868**

$$\frac{d}{dx}y(x) = 2x + 1 + (y(x))^2 - 2x^2y(x) + x^4 + (y(x))^3 - 3x^2(y(x))^2 + 3y(x)x^4 - x^6 = 0$$

**Mathematica:** cpu = 0.042005 (sec), leaf count = 79

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log \left( \frac{-3x^2 + 3y(x) + 1}{\sqrt[3]{29}} - \#1 \right)}{\sqrt[3]{29} - 29\#1^2} \& \right] = c_1 + \frac{1}{9} 29^{2/3} x, y(x) \right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 28

$$\left\{ y(x) = x^2 + \text{RootOf} \left( -x + \int^{-Z} (_a^3 + _a^2 + 1)^{-1} d_a + _C1 \right) \right\}$$

**2.869 ODE No. 869**

$$\frac{d}{dx}y(x) = \frac{-x + 1 - 2y(x) + 3x^2 - 2x^2y(x) + 2x^4 + x^3 - 2x^3y(x) + 2x^5}{x^2 - y(x)} = 0$$

**Mathematica:** cpu = 0.035005 (sec), leaf count = 42

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( W \left( -e^{c_1 + x^4 + \frac{4x^3}{3} - 2x^2 + 4x - 1} \right) + 1 \right) + x^2 \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 37

$$\left\{ y(x) = x^2 + \frac{1}{2} \text{lambertW} \left( -2 \frac{e^{x^4} e^{4/3 x^3} - C1 (e^x)^4 e^{-1}}{(e^{x^2})^2} \right) + \frac{1}{2} \right\}$$

**2.870 ODE No. 870**

$$\frac{d}{dx}y(x) = \frac{1}{x} \left( e^{-\frac{y(x)}{x}} y(x) + e^{-\frac{y(x)}{x}} x + x + x^3 + x^4 \right) e^{\frac{y(x)}{x}} = 0$$

**Mathematica:** cpu = 1.681213 (sec), leaf count = 35

$$\left\{ \left\{ y(x) \rightarrow -x \log \left( \frac{-c_1 - \frac{x^4}{4} - \frac{x^3}{3} - x}{x} \right) \right\} \right\}$$

**Maple:** cpu = 0.702 (sec), leaf count = 30

$$\left\{ y(x) = -\ln \left( -\frac{3x^4 + 4x^3 + 12 - C1 + 12x}{12x} \right) x \right\}$$



**2.871 ODE No. 871**

$$\frac{d}{dx}y(x) = \frac{2x(y(x))^2 + 4y(x)\ln(2x+1)x + 2(\ln(2x+1))^2x + (y(x))^2 - 2 + (\ln(2x+1))^2 + 2y(x)}{2x+1}$$

**Mathematica:** cpu = 0.022503 (sec), leaf count = 22

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{c_1 - x} - \log(2x + 1) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 66

$$\left\{ y(x) = -\frac{1}{2} \left( 4 \frac{\ln(2x+1)x}{2x+1} + 2 \frac{\ln(2x+1)}{2x+1} \right) \left( 2 \frac{x}{2x+1} + (2x+1)^{-1} \right)^{-1} + (-C1 - x)^{-1} \right\}$$

**2.872 ODE No. 872**

$$\frac{d}{dx}y(x) = 1/5 \frac{-30x^3y(x) + 12x^6 + 70x^{7/2} - 30x^3 - 25y(x)\sqrt{x} + 50x - 25\sqrt{x} - 25}{(-5y(x) + 2x^3 + 10\sqrt{x} - 5)x} = 0$$

**Mathematica:** cpu = 0.045506 (sec), leaf count = 215

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{5}(2x^3 + 10\sqrt{x} - 5) - \frac{\sqrt{-25c_1x - x(2x^3 + 10\sqrt{x} - 5)^2 - 50x \left( -\frac{4x^{7/2}}{5} - \frac{2x^6}{25} + \frac{2x^3}{5} - 2x + 2 \right)}}{5\sqrt{-\frac{1}{x}x}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 49

$$\left\{ y(x) = \frac{2x^3}{5} - \sqrt{-C1 + 2\ln(x)} + 2\sqrt{x} - 1, y(x) = \frac{2x^3}{5} + \sqrt{-C1 + 2\ln(x)} + 2\sqrt{x} - 1 \right\}$$

**2.873 ODE No. 873**

$$\frac{d}{dx}y(x) = \frac{1 + 2y(x)}{x(-2 + x + x(y(x))^2 + 3x(y(x))^3 + 2xy(x) + 2x(y(x))^4)} = 0$$

**Mathematica:** cpu = 0.345044 (sec), leaf count = 53

$$\text{Solve} \left[ \frac{1}{192}(-16y(x)^3 - 12y(x)^2 + 12y(x) - 54\log(4y(x) + 2) + 7) - \frac{1}{2x(2y(x) + 1)} = c_1, y(x) \right]$$

**Maple:** cpu = 0.187 (sec), leaf count = 50

$$\left\{ y(x) = \frac{e^{\text{RootOf}(2x(e^{-Z})^4 - 3x(e^{-Z})^3 - 6x(e^{-Z})^2 + 48-C1e^{-Z}x + 54e^{-Z} - Zx + 7xe^{-Z} + 96)}}{2} - \frac{1}{2} \right\}$$

**2.874 ODE No. 874**

$$\frac{d}{dx}y(x) = \frac{(-256ax^2 + 512 + 512(y(x))^2 + 128y(x)ax^4 + 8a^2x^8 + 512(y(x))^3 + 192x^4a(y(x))^2 + 24y(x)^4)}{512}$$

**Mathematica:** cpu = 0.067509 (sec), leaf count = 101

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log \left( \frac{\frac{1}{8}(3ax^5+8x)+3xy(x)}{\sqrt[3]{29}\sqrt[3]{x^3}} - \#1 \right)}{\sqrt[3]{29} - 29\#1^2} \& \right] = c_1 + \frac{1}{18} 29^{2/3} (x^3)^{2/3} \right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 40

$$\left\{ y(x) = -\frac{ax^4}{8} - \frac{1}{3} + \frac{29 \text{RootOf} \left( x^2 - 162 \int^{-Z} (841\_a^3 - 27\_a + 27)^{-1} d\_a + 6\_C1 \right)}{9} \right\}$$

**2.875 ODE No. 875**

$$\frac{d}{dx}y(x) = -\frac{-xy(x) - y(x) + x^5\sqrt{(y(x))^2 + x^2} - x^4\sqrt{(y(x))^2 + x^2}y(x)}{x(1+x)} = 0$$

**Mathematica:** cpu = 0.293537 (sec), leaf count = 285

$$\left\{ \left\{ y(x) \rightarrow \frac{x \left( 2(x+1)^{\sqrt{2}} \exp \left( \sqrt{2}c_1 + \frac{x^4}{2\sqrt{2}} + \frac{x^2}{\sqrt{2}} + \frac{1}{3}\sqrt{2}(x^2+3)x + \frac{25}{6\sqrt{2}} \right) + (x+1)^{2\sqrt{2}} \left( -e^{2\sqrt{2}c_1 + \frac{x^4}{\sqrt{2}} + \sqrt{2}x^2} \right)}{-2(x+1)^{\sqrt{2}} \exp \left( \sqrt{2}c_1 + \frac{x^4}{2\sqrt{2}} + \frac{x^2}{\sqrt{2}} + \frac{1}{3}\sqrt{2}(x^2+3)x + \frac{25}{6\sqrt{2}} \right) + (x+1)^{2\sqrt{2}} \left( -e^{2\sqrt{2}c_1 + \frac{x^4}{\sqrt{2}} + \sqrt{2}x^2} \right)} \right. \right.$$

**Maple:** cpu = 0.187 (sec), leaf count = 79

$$\left\{ \ln \left( 2 \frac{x \left( \sqrt{2} (y(x))^2 + 2x^2 + y(x) + x \right)}{y(x) - x} \right) + \frac{\sqrt{2}x^4}{4} - \frac{\sqrt{2}x^3}{3} + \frac{\sqrt{2}x^2}{2} - x\sqrt{2} - \ln(x) + \sqrt{2} \ln(1+x) \right\}$$

**2.876 ODE No. 876**

$$\frac{d}{dx}y(x) = -1/2 \frac{(y(x))^2 (x^2y(x) - 2x - 2xy(x) + y(x))}{(-2 + xy(x) - 2y(x))x} = 0$$

**Mathematica:** cpu = 0.017002 (sec), leaf count = 135

$$\left\{ \left\{ y(x) \rightarrow -\frac{4x}{\frac{2\sqrt{-4x\left(c_1-2\left(\frac{x^2}{8}-\frac{x}{2}+\frac{\log(x)}{4}\right)\right)-x(x-2)^2}}{\sqrt{-\frac{1}{x}}}-2(x-2)x} \right\}, \left\{ y(x) \rightarrow \frac{4x}{\frac{2\sqrt{-4x\left(c_1-2\left(\frac{x^2}{8}-\frac{x}{2}+\frac{\log(x)}{4}\right)\right)-x(x-2)^2}}{\sqrt{-\frac{1}{x}}}-2(x-2)x} \right\} \right.$$

**Maple:** cpu = 0.031 (sec), leaf count = 41

$$\left\{ y(x) = -4 \left( \sqrt{-C1 - 8 \ln(x)} - 2x + 4 \right)^{-1}, y(x) = 4 \left( \sqrt{-C1 - 8 \ln(x)} + 2x - 4 \right)^{-1} \right\}$$

**2.877 ODE No. 877**

$$\frac{d}{dx}y(x) = \frac{-2xy(x) + 2x^3 - 2x - (y(x))^3 + 3x^2(y(x))^2 - 3y(x)x^4 + x^6}{-y(x) + x^2 - 1} = 0$$

**Mathematica:** cpu = 0.016502 (sec), leaf count = 49

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{1 - \frac{1}{\sqrt{c_1-2x}}} + x^2 - 1 \right\}, \left\{ y(x) \rightarrow \frac{1}{\frac{1}{\sqrt{c_1-2x}} + 1} + x^2 - 1 \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 71

$$\left\{ y(x) = -\frac{1}{-2x + 2\_C1} \left( -2\_C1 x^2 + 2x^3 + \sqrt{2\_C1 - 2x + 1} - 1 \right), y(x) = \frac{1}{-2x + 2\_C1} \left( 2\_C1 x \right. \right.$$

**2.878 ODE No. 878**

$$\frac{d}{dx}y(x) = \frac{1 + (y(x))^4 - 8ax(y(x))^2 + 16a^2x^2 + (y(x))^6 - 12(y(x))^4ax + 48(y(x))^2a^2x^2 - 64a^3x^3}{y(x)} = 0$$

**Mathematica:** cpu = 0.262533 (sec), leaf count = 130

Solve  $\left[ 2a \left( x - \frac{1}{2} \text{RootSum} \left[ 64\#1^3a^3 - 48\#1^2a^2y(x)^2 - 16\#1^2a^2 + 12\#1ay(x)^4 + 8\#1ay(x)^2 + 2a - y(x) \right] \right) \right]$

Maple: cpu = 0.359 (sec), leaf count = 75

$$\left\{ \int_{-b}^{y(x)} \frac{-a}{-a^6 + 12a^4ax - 48a^2a^2x^2 + 64a^3x^3 - a^4 + 8a^2ax - 16a^2x^2 + 2a - 1} d_a + x - C1 \right.$$

## 2.879 ODE No. 879

$$\frac{d}{dx}y(x) = -\frac{-xy(x) - y(x) + \sqrt{(y(x))^2 + x^2x^2} - x\sqrt{(y(x))^2 + x^2}y(x)}{x(1+x)} = 0$$

Mathematica: cpu = 0.152519 (sec), leaf count = 135

$$\left\{ \left\{ y(x) \rightarrow \frac{x(-2(x+1)^{\sqrt{2}}e^{\sqrt{2}c_1+\sqrt{2}x} + e^{2\sqrt{2}c_1+2\sqrt{2}x} - (x+1)^{2\sqrt{2}})}{2(x+1)^{\sqrt{2}}e^{\sqrt{2}c_1+\sqrt{2}x} + e^{2\sqrt{2}c_1+2\sqrt{2}x} - (x+1)^{2\sqrt{2}}} \right\} \right\}$$

Maple: cpu = 0.172 (sec), leaf count = 55

$$\left\{ \ln \left( 2 \frac{x \left( \sqrt{2} (y(x))^2 + 2x^2 + y(x) + x \right)}{y(x) - x} \right) + x\sqrt{2} - \ln(x) - \sqrt{2} \ln(1+x) - C1 = 0 \right\}$$

## 2.880 ODE No. 880

$$\frac{d}{dx}y(x) = -2 \frac{a}{-y(x) - 2a - 2a(y(x))^4 + 16a^2x(y(x))^2 - 32a^3x^2 - 2a(y(x))^6 + 24(y(x))^4a^2x - 96}$$

Mathematica: cpu = 0.127516 (sec), leaf count = 131

$$\text{Solve} \left[ \frac{\text{RootSum} \left[ -64\#1^3a^3 + 48\#1^2a^2y(x)^2 + 16\#1^2a^2 - 12\#1ay(x)^4 - 8\#1ay(x)^2 + y(x)^6 + y(x)^4 + 1 \right]}{8a^2} \right]$$

Maple: cpu = 0.063 (sec), leaf count = 41

$$\left\{ \frac{y(x)}{2a} + \frac{\int^{(y(x))^2-4ax} (-a^3 + a^2 + 1)^{-1} d_a}{8a^2} - C1 = 0 \right\}$$

**2.881 ODE No. 881**

$$\frac{d}{dx}y(x) = \frac{-18xy(x) - 6x^3 - 18x + 27(y(x))^3 + 27x^2(y(x))^2 + 9y(x)x^4 + x^6}{27y(x) + 9x^2 + 27} = 0$$

**Mathematica:** cpu = 0.017502 (sec), leaf count = 75

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{27 \left( \frac{1}{27} - \frac{1}{\sqrt{c_1 - 1458x}} \right)} + \frac{1}{3}(-x^2 - 3) \right\}, \left\{ y(x) \rightarrow \frac{1}{27 \left( \frac{1}{\sqrt{c_1 - 1458x}} + \frac{1}{27} \right)} + \frac{1}{3}(-x^2 - 3) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 75

$$\left\{ y(x) = \frac{1}{-6x + 6\_C1} \left( -2\_C1 x^2 + 2x^3 + 3\sqrt{2\_C1 - 2x + 1} + 3 \right), y(x) = -\frac{1}{-6x + 6\_C1} \left( 2\_C1 \right) \right\}$$

**2.882 ODE No. 882**

$$\frac{d}{dx}y(x) = -\frac{(-108x^{3/2} - 216 - 216(y(x))^2 + 72x^3y(x) - 6x^6 - 216(y(x))^3 + 108x^3(y(x))^2 - 18y(x))}{216}$$

**Mathematica:** cpu = 0.068009 (sec), leaf count = 119

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log \left( \frac{\frac{1}{2}(2\sqrt{x} - x^{7/2}) + 3\sqrt{x}y(x)}{\sqrt[3]{29}\sqrt[3]{x^{3/2}}} - \#1 \right)}{\sqrt[3]{29} - 29\#1^2} \& \right] = c_1 + \frac{2}{27} 29^{2/3} \sqrt{x} \right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 41

$$\left\{ y(x) = \frac{x^3}{6} - \frac{1}{3} + \frac{29}{9} \text{RootOf} \left( 2x^{3/2} - 243 \int^{-Z} (841\_a^3 - 27\_a + 27)^{-1} d\_a + 9\_C1 \right) \right\}$$

**2.883 ODE No. 883**

$$\frac{d}{dx}y(x) = \frac{(a^3 + (y(x))^4 a^3 + 2(y(x))^2 a^2 b x^2 + a x^4 b^2 + (y(x))^6 a^3 + 3(y(x))^4 a^2 b x^2 + 3(y(x))^2 a b^2 x^4 + b^3)}{a^{7/2} y(x)}$$

**Mathematica:** cpu = 1.403178 (sec), leaf count = 164

$$\text{Solve} \left[ \frac{x^2}{2} - \frac{1}{2} a^{5/2} \text{RootSum} \left[ \#1^3 b^3 + 3\#1^2 a b^2 y(x)^2 + \#1^2 a b^2 + 3\#1 a^2 b y(x)^4 + 2\#1 a^2 b y(x)^2 + a^{5/2} b + a^3 \right] \right]$$

**Maple:** cpu = 0.592 (sec), leaf count = 595

$$\left\{ \int_{-b}^x (b^3\_a^6 + 3(y(x))^2 a b^2\_a^4 + 3(y(x))^4 a^2 b\_a^2 + (y(x))^6 a^3 + a\_a^4 b^2 + 2(y(x))^2 a^2 b\_a^2 + (y(x))^4 a^3) \right.$$

## 2.884 ODE No. 884

$$\frac{d}{dx}y(x) = -\frac{(-1 - (y(x))^4 + 2x^2(y(x))^2 - x^4 - (y(x))^6 + 3x^2(y(x))^4 - 3x^4(y(x))^2 + x^6)x}{y(x)} = 0$$

**Mathematica:** cpu = 0.364546 (sec), leaf count = 71

$$\text{Solve}\left[\frac{1}{4}\left(2\log(-x^2 + y(x)^2 + 1) - 2x^2 - \frac{1}{y(x)(y(x) + x)} + \frac{1}{xy(x) - y(x)^2} - 2\log(x - y(x)) - 2\log(y(x))\right), y(x)\right]$$

**Maple:** cpu = 0.265 (sec), leaf count = 107

$$\left\{ y(x) = e^{\text{RootOf}\left(-3x^2(e^{-Z})^2 + 6x^3e^{-Z} + 3(e^{-Z})^2 \ln\left(\frac{(e^{-Z})^2 - 2xe^{-Z} + 1}{e^{-Z} - 2x}\right) - 2\_C1(e^{-Z})^2 - 3\_Z(e^{-Z})^2 - 6e^{-Z} \ln\left(\frac{(e^{-Z})^2 - 2xe^{-Z} + 1}{e^{-Z} - 2x}\right)\right)} \right\}$$

## 2.885 ODE No. 885

$$\frac{d}{dx}y(x) = \frac{-\frac{i}{128}(32ix + 64 + 64(y(x))^4 + 32x^2(y(x))^2 + 4x^4 + 64(y(x))^6 + 48x^2(y(x))^4 + 12x^4(y(x))^2)}{y(x)}$$

**Mathematica:** cpu = 40.741674 (sec), leaf count = 73

$$\text{DSolve}\left[y'(x) = -\frac{i(x^6 + 12x^4y(x)^2 + 4x^4 + 48x^2y(x)^4 + 32x^2y(x)^2 + 64y(x)^6 + 64y(x)^4 + 32ix + 64)}{128y(x)}, y(x)\right]$$

**Maple:** cpu = 0.858 (sec), leaf count = 0

could not solve

## 2.886 ODE No. 886

$$\frac{d}{dx}y(x) = \frac{2x^2 - 4x^3y(x) + 1 + x^4(y(x))^2 + x^6(y(x))^3 - 3(y(x))^2x^5 + 3y(x)x^4 - x^3}{x^4} = 0$$

**Mathematica:** cpu = 0.054507 (sec), leaf count = 82

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{3x^2y(x) - 3x + 1}{\sqrt[3]{29}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2}\&\right] = c_1 - \frac{29^{2/3}}{9x}, y(x)\right]$$

**Maple:** cpu = 0.016 (sec), leaf count = 42

$$\left\{ y(x) = \frac{9x - 3 + 29\text{RootOf}\left(-81\int^{-Z}(841\_a^3 - 27\_a + 27)^{-1}d\_ax + 3x\_C1 - 1\right)}{9x^2} \right\}$$

**2.887 ODE No. 887**

$$\frac{d}{dx}y(x) = \frac{y(x)a^2x + a + a^2x + (y(x))^3 a^3x^3 + 3(y(x))^2 a^2x^2 + 3axy(x) + 1}{a^2x^2 (axy(x) + 1 + ax)} = 0$$

**Mathematica:** cpu = 0.049006 (sec), leaf count = 106

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{a^3x^3 \left( \frac{1}{a^3x^3} - \frac{1}{x^3\sqrt{c_1-2a^6x}} \right)} - \frac{ax+1}{ax} \right\}, \left\{ y(x) \rightarrow \frac{1}{a^3x^3 \left( \frac{1}{x^3\sqrt{c_1-2a^6x}} + \frac{1}{a^3x^3} \right)} - \frac{ax+1}{ax} \right\} \right\}$$

**Maple:** cpu = 0.046 (sec), leaf count = 70

$$\left\{ y(x) = -\frac{1}{ax} \left( -ax + \sqrt{-C1 - 2x} - 1 \right) \left( \sqrt{-C1 - 2x} - 1 \right)^{-1}, y(x) = -\frac{1}{ax} \left( ax + \sqrt{-C1 - 2x} + 1 \right) \left( \sqrt{-C1 - 2x} + 1 \right)^{-1} \right\}$$

**2.888 ODE No. 888**

$$\frac{d}{dx}y(x) = \frac{6x^2y(x) - 2x + 1 - 5x^3(y(x))^2 - 2xy(x) + (y(x))^3 x^4}{x^2 (x^2y(x) - x + 1)} = 0$$

**Mathematica:** cpu = 0.020003 (sec), leaf count = 78

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{x^4 \left( \frac{1}{x^2} - \frac{1}{x^2\sqrt{c_1+\frac{2}{x}}} \right)} + \frac{x-1}{x^2} \right\}, \left\{ y(x) \rightarrow \frac{1}{x^4 \left( \frac{1}{x^2\sqrt{c_1+\frac{2}{x}}} + \frac{1}{x^2} \right)} + \frac{x-1}{x^2} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 79

$$\left\{ y(x) = \frac{1}{x^2} \left( \sqrt{\frac{x-C1+2}{x}} x - x + 1 \right) \left( \sqrt{\frac{x-C1+2}{x}} - 1 \right)^{-1}, y(x) = \frac{1}{x^2} \left( \sqrt{\frac{x-C1+2}{x}} x + x - 1 \right) \left( \sqrt{\frac{x-C1+2}{x}} + 1 \right)^{-1} \right\}$$

**2.889 ODE No. 889**

$$\frac{d}{dx}y(x) = -1/8 \frac{\left( -8 - 8(y(x))^3 + 24(y(x))^{3/2} e^x - 18(e^x)^2 - 8(y(x))^{9/2} + 36(y(x))^3 e^x - 54(y(x))^{3/2} \right)}{\sqrt{y(x)}}$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.858 (sec), leaf count = 47

$$\left\{ e^x + \frac{2}{3} \ln \left( (y(x))^{\frac{3}{2}} - \frac{3e^x}{2} \right) + \frac{2}{3} \left( (y(x))^{\frac{3}{2}} - \frac{3e^x}{2} \right)^{-1} - \frac{2}{3} \ln \left( (y(x))^{\frac{3}{2}} - \frac{3e^x}{2} + 1 \right) - C1 = 0 \right\}$$

## 2.890 ODE No. 890

$$\frac{d}{dx} y(x) = \frac{x}{-y(x) + 1 + (y(x))^4 + 2x^2(y(x))^2 + x^4 + (y(x))^6 + 3x^2(y(x))^4 + 3x^4(y(x))^2 + x^6} = 0$$

**Mathematica:** cpu = 0.140518 (sec), leaf count = 103

$$\text{Solve} \left[ y(x) - \frac{1}{2} \text{RootSum} \left[ \#1^3 + 3\#1^2 y(x)^2 + \#1^2 + 3\#1 y(x)^4 + 2\#1 y(x)^2 + y(x)^6 + y(x)^4 + 1 \&, \frac{\#1}{3\#1^2} \right], \frac{1}{3\#1^2} \right]$$

**Maple:** cpu = 0.686 (sec), leaf count = 34

$$\left\{ -y(x) + \frac{\int^{(y(x))^2+x^2} (-a^3 + a^2 + 1)^{-1} da}{2} - C1 = 0 \right\}$$

## 2.891 ODE No. 891

$$\frac{d}{dx} y(x) = \frac{(y(x))^2 (-2y(x) + 2x^2 + 2x^2 y(x) + y(x)x^4)}{x^3 (x^2 - y(x) + x^2 y(x))} = 0$$

**Mathematica:** cpu = 0.020503 (sec), leaf count = 135

$$\left\{ \left\{ y(x) \rightarrow \frac{x^5}{\frac{\sqrt{x^5 (c_1 - 2(\frac{1}{2x^4} - \frac{1}{x^2} + \log(x))) + (x^2 - 1)^2 x}}{\sqrt{\frac{1}{x^5}}} - x^3 (x^2 - 1)} \right\}, \left\{ y(x) \rightarrow -\frac{x^5}{\frac{\sqrt{x^5 (c_1 - 2(\frac{1}{2x^4} - \frac{1}{x^2} + \log(x))) + (x^2 - 1)^2 x}}{\sqrt{\frac{1}{x^5}}}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 56

$$\left\{ y(x) = x^2 \left( \sqrt{-C1 - 2 \ln(x)x^2 - x^2 + 1} \right)^{-1}, y(x) = -x^2 \left( \sqrt{-C1 - 2 \ln(x)x^2 + x^2 - 1} \right)^{-1} \right\}$$



**2.892 ODE No. 892**

$$\frac{d}{dx}y(x) = 1 \left( (y(x))^2 + 2xy(x) + x^2 + e^{-2(-(y(x))^2+x^2-1)} \right) \left( (y(x))^2 + 2xy(x) + x^2 - e^{-2(-(y(x))^2+x^2-1)} \right)$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.452 (sec), leaf count = 40

$$\left\{ y(x) = e^{\text{RootOf}\left(-Z + \int (e^{-Z})^2 - 2xe^{-Z} (e^2(-a+1)^{-1} + a)^{-1} d_a + C1\right)} - x \right\}$$

**2.893 ODE No. 893**

$$\frac{d}{dx}y(x) = \frac{6x + x^3 + x^3(y(x))^2 + 4x^2y(x) + x^3(y(x))^3 + 6x^2(y(x))^2 + 12xy(x) + 8}{x^3} = 0$$

**Mathematica:** cpu = 0.048006 (sec), leaf count = 80

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{3y(x)+\frac{x+6}{\sqrt[3]{29}}}{\sqrt[3]{29}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2} \& \right] = c_1 + \frac{1}{9} 29^{2/3} x, y(x) \right]$$

**Maple:** cpu = 0.031 (sec), leaf count = 41

$$\left\{ y(x) = \frac{29 \text{RootOf}\left(-81 \int^{-Z} (841 - a^3 - 27 - a + 27)^{-1} d_a + x + 3 - C1\right) x - 3x - 18}{9x} \right\}$$

**2.894 ODE No. 894**

$$\frac{d}{dx}y(x) = \frac{-i(ix + 1 + x^4 + 2x^2(y(x))^2 + (y(x))^4 + x^6 + 3x^4(y(x))^2 + 3x^2(y(x))^4 + (y(x))^6)}{y(x)} = 0$$

**Mathematica:** cpu = 40.654663 (sec), leaf count = 65

$$\text{DSolve} \left[ y'(x) = -\frac{i(x^6 + 3x^4y(x)^2 + x^4 + 3x^2y(x)^4 + 2x^2y(x)^2 + y(x)^6 + y(x)^4 + ix + 1)}{y(x)}, y(x), x \right]$$

**Maple:** cpu = 0.734 (sec), leaf count = 0

could not solve

**2.895 ODE No. 895**

$$\frac{d}{dx}y(x) = \frac{(-256ax^2y(x) - 32a^2x^6 - 256ax^2 + 512(y(x))^3 + 192x^4a(y(x))^2 + 24y(x)a^2x^8 + a^3x^{12})x}{512y(x) + 64ax^4 + 512}$$

**Mathematica:** cpu = 0.022503 (sec), leaf count = 81

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{8}(-ax^4 - 8) + \frac{1}{512 \left( \frac{1}{512} - \frac{1}{\sqrt{c_1 - 262144x^2}} \right)} \right\}, \left\{ y(x) \rightarrow \frac{1}{8}(-ax^4 - 8) + \frac{1}{512 \left( \frac{1}{\sqrt{c_1 - 262144x^2}} + \frac{1}{512} \right)} \right\} \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 80

$$\left\{ y(x) = -\frac{1}{8} \left( \sqrt{-x^2 + \_C1ax^4 - ax^4 - 8} \right) \left( -1 + \sqrt{-x^2 + \_C1} \right)^{-1}, y(x) = -\frac{1}{8} \left( \sqrt{-x^2 + \_C1ax^4 + a} \right) \right.$$

**2.896 ODE No. 896**

$$\frac{d}{dx}y(x) = \frac{x + 1 + (y(x))^4 - 2x^2(y(x))^2 + x^4 + (y(x))^6 - 3x^2(y(x))^4 + 3x^4(y(x))^2 - x^6}{y(x)} = 0$$

**Mathematica:** cpu = 0.201026 (sec), leaf count = 106

Solve  $\left[ \frac{1}{2} \text{RootSum} \left[ -\#1^3 + 3\#1^2y(x)^2 + \#1^2 - 3\#1y(x)^4 - 2\#1y(x)^2 + y(x)^6 + y(x)^4 + 1\&, \frac{1}{3\#1^2 - 6\#} \right] \right]$

**Maple:** cpu = 0.296 (sec), leaf count = 63

$$\left\{ \int_{-b}^{y(x)} \frac{-a}{-a^6 + 3a^4x^2 - 3a^2x^4 + x^6 - a^4 + 2a^2x^2 - x^4 - 1} d_a + x - \_C1 = 0 \right\}$$

**2.897 ODE No. 897**

$$\frac{d}{dx}y(x) = \frac{(-108x^{3/2}y(x) + 18x^{9/2} - 108x^{3/2} - 216(y(x))^3 + 108x^3(y(x))^2 - 18y(x)x^6 + x^9)\sqrt{x}}{-216y(x) + 36x^3 - 216} = 0$$

**Mathematica:** cpu = 0.027003 (sec), leaf count = 79

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{6}(x^3 - 6) - \frac{1}{216 \left( -\frac{1}{\sqrt{c_1 - 62208x^{3/2}}} - \frac{1}{216} \right)} \right\}, \left\{ y(x) \rightarrow \frac{1}{6}(x^3 - 6) - \frac{1}{216 \left( \frac{1}{\sqrt{c_1 - 62208x^{3/2}}} - \frac{1}{216} \right)} \right\} \right.$$

**Maple:** cpu = 0.062 (sec), leaf count = 85

$$\left\{ y(x) = \frac{1}{6} \left( \sqrt{9\_C1 - 12x^{3/2}x^3 - 3x^3 + 18} \right) \left( -3 + \sqrt{9\_C1 - 12x^{3/2}} \right)^{-1}, y(x) = \frac{1}{6} \left( \sqrt{9\_C1 - 12x^{3/2}} \right) \right.$$

**2.898 ODE No. 898**

$$\frac{d}{dx}y(x) = 1/16 \frac{32 x^5 y(x) + 8 x^3 + 32 x^5 + 64 x^6 (y(x))^3 + 48 x^4 (y(x))^2 + 12 x^2 y(x) + 1}{x^6 (4 x^2 y(x) + 1 + 4 x^2)} = 0$$

**Mathematica:** cpu = 0.021503 (sec), leaf count = 106

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{64x^8 \left( \frac{1}{64x^8} - \frac{1}{x^8 \sqrt{c_1 + \frac{8192}{x}}} \right)} - \frac{4x^2 + 1}{4x^2} \right\}, \left\{ y(x) \rightarrow \frac{1}{64x^8 \left( \frac{1}{x^8 \sqrt{c_1 + \frac{8192}{x}}} + \frac{1}{64x^8} \right)} - \frac{4x^2 + 1}{4x^2} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 83

$$\left\{ y(x) = -\frac{1}{4x^2} \left( -4x^2 + \sqrt{\frac{x-C1+2}{x}} - 1 \right) \left( \sqrt{\frac{x-C1+2}{x}} - 1 \right)^{-1}, y(x) = -\frac{1}{4x^2} \left( 4x^2 + \sqrt{\frac{x-C1+2}{x}} - 1 \right) \left( \sqrt{\frac{x-C1+2}{x}} - 1 \right)^{-1} \right\}$$

**2.899 ODE No. 899**

$$\frac{d}{dx}y(x) = \frac{32 x^5 + 64 x^6 + 64 x^6 (y(x))^2 + 32 y(x) x^4 + 4 x^2 + 64 x^6 (y(x))^3 + 48 x^4 (y(x))^2 + 12 x^2 y(x) + 1}{64 x^8}$$

**Mathematica:** cpu = 0.062008 (sec), leaf count = 106

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log \left( \frac{\frac{3y(x)}{x^2} + \frac{4x^2+3}{4x^4}}{\sqrt[3]{29}\sqrt[3]{\frac{1}{x^6}}} - \#1 \right)}{\sqrt[3]{29} - 29\#1^2} \& \right] = c_1 - \frac{1}{9} 29^{2/3} \left( \frac{1}{x^6} \right)^{2/3} x^3, \right]$$

**Maple:** cpu = 0.015 (sec), leaf count = 47

$$\left\{ y(x) = \frac{116 \text{RootOf} \left( -81 \int^{-Z} (841 \_a^3 - 27 \_a + 27)^{-1} d\_ax + 3x\_C1 - 1 \right) x^2 - 12x^2 - 9}{36x^2} \right\}$$

## 2.900 ODE No. 900

$$\frac{d}{dx}y(x) = 2 \frac{a(-(y(x))^2 + 4ax - 1)}{-(y(x))^3 + 4axy(x) - y(x) - 2a(y(x))^6 + 24(y(x))^4 a^2 x - 96(y(x))^2 a^3 x^2 + 128a^4 x^3}$$

**Mathematica:** cpu = 0.091011 (sec), leaf count = 381

$$\left\{ \left\{ y(x) \rightarrow \text{Root} \left[ 8\#1^5 a - 16\#1^4 a^2 c_1 - 64\#1^3 a^2 x + \#1^2 (128a^3 c_1 x - 2) + 128\#1 a^3 x^2 - 256a^4 c_1 x^2 + 8ax^3 \right] \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 46

$$\left\{ \frac{y(x)}{2a} - \frac{1}{8a^2((y(x))^2 - 4ax)} - \frac{1}{16a^2((y(x))^2 - 4ax)^2} - C1 = 0 \right\}$$

## 2.901 ODE No. 901

$$\frac{d}{dx}y(x) = \frac{(y(x) - a \ln(y(x))x + x^2)y(x)}{(-y(x) \ln(y(x)) - y(x) \ln(x) - y(x) + ax)x} = 0$$

**Mathematica:** cpu = 0.089511 (sec), leaf count = 33

$$\text{Solve} \left[ ax \log(y(x)) - \frac{x^2}{2} - y(x) \log(x) - y(x) \log(y(x)) = c_1, y(x) \right]$$

**Maple:** cpu = 0.343 (sec), leaf count = 30

$$\left\{ y(x) = e^{\text{RootOf}(-2\_Zax + 2 \ln(x)e^{-Z} + 2\_Ze^{-Z} + 2\_C1 a + x^2)} \right\}$$

## 2.902 ODE No. 902

$$\frac{d}{dx}y(x) = \frac{-x(y(x))^2 + x^3 - x - (y(x))^6 + 3x^2(y(x))^4 - 3x^4(y(x))^2 + x^6}{(-(y(x))^2 + x^2 - 1)y(x)} = 0$$

**Mathematica:** cpu = 0.109514 (sec), leaf count = 295

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{2} \sqrt{\frac{4x^3}{x-c_1} - \frac{4c_1 x^2}{x-c_1} - \frac{\sqrt{4c_1 - 4x + 1}}{x-c_1} - \frac{1}{x-c_1}} \right\}, \left\{ y(x) \rightarrow \frac{1}{2} \sqrt{\frac{4x^3}{x-c_1} - \frac{4c_1 x^2}{x-c_1} - \frac{\sqrt{4c_1}}{x-c_1}} \right\} \right\}$$

**Maple:** cpu = 0.171 (sec), leaf count = 175

$$\left\{ y(x) = -\frac{1}{2\_C1 + 6x} \sqrt{(-C1 + 3x) \left( 4\_C1 x^2 + 12x^3 + \sqrt{-12\_C1 - 36x + 9} - 3 \right)}, y(x) = \frac{1}{2\_C1}$$

### 2.903 ODE No. 903

$$\frac{d}{dx}y(x) = 1/2 \frac{1}{x} \sin\left(\frac{y(x)}{x}\right) \left(y(x) + 2x^2 \sin\left(1/2 \frac{y(x)}{x}\right) \cos\left(1/2 \frac{y(x)}{x}\right)\right) \left(\sin\left(1/2 \frac{y(x)}{x}\right)\right)^{-1} \left(\cos\left(1/2 \frac{y(x)}{x}\right)\right)$$

**Mathematica:** cpu = 0.050006 (sec), leaf count = 19

$$\left\{ \left\{ y(x) \rightarrow 2x \cot^{-1}\left(e^{-c_1-x}\right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 48

$$\left\{ y(x) = \arctan\left(2 \frac{-C1 e^x}{-C1^2 (e^x)^2 + 1}, -\frac{-C1^2 (e^x)^2 - 1}{-C1^2 (e^x)^2 + 1}\right) x \right\}$$

### 2.904 ODE No. 904

$$\frac{d}{dx}y(x) = 1/2 \frac{1}{x} \sin\left(\frac{y(x)}{x}\right) \left(y(x) + 2x^3 \cos\left(1/2 \frac{y(x)}{x}\right) \sin\left(1/2 \frac{y(x)}{x}\right)\right) \left(\sin\left(1/2 \frac{y(x)}{x}\right)\right)^{-1} \left(\cos\left(1/2 \frac{y(x)}{x}\right)\right)$$

**Mathematica:** cpu = 0.051506 (sec), leaf count = 23

$$\left\{ \left\{ y(x) \rightarrow 2x \cot^{-1}\left(e^{-c_1 - \frac{x^2}{2}}\right) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 64

$$\left\{ y(x) = \arctan\left(2 \frac{e^{1/2 x^2} - C1}{(e^{1/2 x^2})^2 - C1^2 + 1}, -1 \left( \left( e^{\frac{x^2}{2}} \right)^2 - C1^2 - 1 \right) \left( \left( e^{\frac{x^2}{2}} \right)^2 - C1^2 + 1 \right)^{-1} \right) x \right\}$$

### 2.905 ODE No. 905

$$\frac{d}{dx}y(x) = \frac{a^2 x + a^3 x^3 + a^3 x^3 (y(x))^2 + 2 a^2 x^2 y(x) + a x + (y(x))^3 a^3 x^3 + 3 (y(x))^2 a^2 x^2 + 3 a x y(x) + 1}{a^3 x^3}$$

**Mathematica:** cpu = 0.060508 (sec), leaf count = 85

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29 \#1^3 + 3 \sqrt[3]{29} \#1 - 29 \&, \frac{\log\left(\frac{ax+3+3y(x)}{\sqrt[3]{29}} - \#1\right)}{\sqrt[3]{29 - 29\#1^2}} \& \right] = c_1 + \frac{1}{9} 29^{2/3} x, y(x) \right]$$

**Maple:** cpu = 0.031 (sec), leaf count = 46

$$\left\{ y(x) = \frac{29 \text{RootOf}\left(-81 \int^{-Z} (841 \_a^3 - 27 \_a + 27)^{-1} d\_a + x + 3 \_C1\right) ax - 3 ax - 9}{9 ax} \right\}$$

**2.906 ODE No. 906**

$$\frac{d}{dx}y(x) = \frac{x(x^2 + (y(x))^2 + 1)}{-(y(x))^3 - x^2y(x) - y(x) + (y(x))^6 + 3x^2(y(x))^4 + 3x^4(y(x))^2 + x^6} = 0$$

**Mathematica:** cpu = 0.055007 (sec), leaf count = 326

$$\left\{ \left\{ y(x) \rightarrow \text{Root} \left[ 4\#1^5 - 4\#1^4c_1 + 8\#1^3x^2 + \#1^2(2 - 8c_1x^2) + 4\#1x^4 - 4c_1x^4 + 2x^2 + 1\&, 1 \right] \right\}, \left\{ y(x) \right.$$

**Maple:** cpu = 0.249 (sec), leaf count = 33

$$\left\{ -\frac{1}{4((y(x))^2 + x^2)^2} - \frac{1}{2(y(x))^2 + 2x^2} - y(x) + \_C1 = 0 \right\}$$

**2.907 ODE No. 907**

$$\frac{d}{dx}y(x) = 1/2 \frac{-2 \cos(x) x + 2 x^2 \sin(x) + 2 x + 2 (y(x))^2 + 4 y(x) \cos(x) x - 4 x y(x) + x^2 \cos(2 x) + 3}{x}$$

**Mathematica:** cpu = 0.052507 (sec), leaf count = 22

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{c_1 - \log(x)} - x(\cos(x) - 1) \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 22

$$\left\{ y(x) = -\frac{(2 \cos(x) - 2) x}{2} + (\_C1 - \ln(x))^{-1} \right\}$$

**2.908 ODE No. 908**

$$\frac{d}{dx}y(x) = 4 \frac{x(a-1)(a+1)}{4y(x) + a^2(y(x))^4 - 2a^4(y(x))^2x^2 + 4(y(x))^2a^2x^2 + a^6x^4 - 3a^4x^4 + 3a^2x^4 - (y(x))^4 - 1}$$

**Mathematica:** cpu = 1.364673 (sec), leaf count = 1278

$$\left\{ \left\{ y(x) \rightarrow -\frac{c_1}{3(1-a^2)} + \frac{\sqrt[3]{18x^2c_1a^6 - 54x^2c_1a^4 - 54a^4 + 54x^2c_1a^2 + 108a^2 - 2c_1^3 - 18x^2c_1 + \sqrt{4(3(1-a^2)^3c_1^2 - 4(1-a^2)(c_1^3 - 3c_1^2x^2 + 3c_1x^4 - x^6)}}}{3(1-a^2)} \right\} \right\}$$

**Maple:** cpu = 0.312 (sec), leaf count = 1742

$$\left\{ y(x) = -\frac{9^{\frac{2}{3}}}{54a^2 - 54} \left( (2\_C1 a^2 - 2\_C1) \sqrt[3]{9} \sqrt[3]{(a-1)^2 (a+1)^2} \left( \frac{1}{3} \sqrt{-3(a-1)^5 (a+1)^5 x^6 + 6\_C1} \right) \right) \right.$$

## 2.909 ODE No. 909

$$\frac{d}{dx} y(x) = \frac{x^3 + (y(x))^4 x^3 + 2x^2(y(x))^2 + x + x^3(y(x))^6 + 3x^2(y(x))^4 + 3x(y(x))^2 + 1}{x^5 y(x)} = 0$$

**Mathematica:** cpu = 40.683666 (sec), leaf count = 64

$$\text{DSolve} \left[ y'(x) = \frac{x^3 y(x)^6 + x^3 y(x)^4 + x^3 + 3x^2 y(x)^4 + 2x^2 y(x)^2 + 3x y(x)^2 + x + 1}{x^5 y(x)}, y(x), x \right]$$

**Maple:** cpu = 0.390 (sec), leaf count = 84

$$\left\{ y(x) = \frac{1}{x} \sqrt{x \left( \text{RootOf} \left( \int^{-Z} (2\_a^3 + 2\_a^2 + 1)^{-1} d\_a x + x\_C1 + 1 \right) x - 1 \right)}, y(x) = -\frac{1}{x} \sqrt{x \left( \text{RootOf} \right)} \right.$$

## 2.910 ODE No. 910

$$\frac{d}{dx} y(x) = \frac{-2x - y(x) + 1 + x^2(y(x))^2 + 2x^3 y(x) + x^4 + x^3(y(x))^3 + 3x^4(y(x))^2 + 3x^5 y(x) + x^6}{x} = 0$$

**Mathematica:** cpu = 0.057507 (sec), leaf count = 98

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log \left( \frac{3x^3 + 3x^2 y(x) + x}{\sqrt[3]{29} \sqrt[3]{x^3}} - \#1 \right)}{\sqrt[3]{29} - 29\#1^2} \& \right] = c_1 + \frac{29^{2/3} (x^3)^{2/3}}{9x}, y(x) \right]$$

**Maple:** cpu = 0.016 (sec), leaf count = 42

$$\left\{ y(x) = \frac{-9x^2 + 29 \text{RootOf} \left( -81 \int^{-Z} (841\_a^3 - 27\_a + 27)^{-1} d\_a + x + 3\_C1 \right) - 3}{9x} \right\}$$

**2.911 ODE No. 911**

$$\frac{d}{dx}y(x) = -\left(-\frac{\ln(y(x))}{x} + \frac{\cos(x)\ln(y(x))}{\sin(x)} - \frac{F1(x)}{K[1]}\right)y(x) = 0$$

**Mathematica:** cpu = 4.337551 (sec), leaf count = 56

$$\text{Solve}\left[\int_1^x \left(\frac{2\log(y(x))\sin(K[1])}{K[1]^2} - \frac{2(\log(y(x))\cos(K[1]) - \sin(K[1])F1(K[1]))}{K[1]}\right) dK[1] - 2\sin(1)\log(y(x))\right]$$

**Maple:** cpu = 0.374 (sec), leaf count = 30

$$\left\{y(x) = e^{\frac{x C1}{\sin(x)}} e^{\frac{x}{\sin(x)} \int \frac{-F1(x)\sin(x)}{x} dx}\right\}$$

**2.912 ODE No. 912**

$$\frac{d}{dx}y(x) = 2 \frac{ax}{-x^3y(x) + 2ax^3 + 2a(y(x))^4x^3 - 16(y(x))^2a^2x^2 + 32a^3x + 2a(y(x))^6x^3 - 24(y(x))^4a^2}$$

**Mathematica:** cpu = 1.400178 (sec), leaf count = 205

$$\text{Solve}\left[-\text{RootSum}\left[-\#1^3y(x)^6 - \#1^3y(x)^4 - \#1^3 + 12\#1^2ay(x)^4 + 8\#1^2ay(x)^2 - 48\#1a^2y(x)^2 - 16\#1a^2\right]\right]$$

**Maple:** cpu = 3.026 (sec), leaf count = 43

$$\left\{-\frac{y(x)}{2a} + \frac{1}{8a^2} \int^{(y(x))^2 - 4\frac{a}{x}} (-a^3 + a^2 + 1)^{-1} da - C1 = 0\right\}$$

**2.913 ODE No. 913**

$$\frac{d}{dx}y(x) = -\frac{-(y(x))^3 - y(x) + 2(y(x))^2\ln(x) - (\ln(x))^2(y(x))^3 - 1 + 3y(x)\ln(x) - 3(\ln(x))^2(y(x))^2)}{xy(x)}$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.047 (sec), leaf count = 43

$$\left\{y(x) = 9 \left(9 \ln(x) + 56 \text{RootOf}\left(-81 \int^{-Z} (3136 a^3 - 27 a + 27)^{-1} da - \ln(x) + 3 C1\right) - 3\right)^{-1}$$



**2.914 ODE No. 914**

$$\frac{d}{dx}y(x) = 2 \frac{a(x(y(x))^2 - 4a + x)}{-x^3(y(x))^3 + 4ax^2y(x) - x^3y(x) + 2a(y(x))^6x^3 - 24(y(x))^4a^2x^2 + 96(y(x))^2xa^3 - 1}$$

**Mathematica:** cpu = 1.504191 (sec), leaf count = 401

$$\{ \{y(x) \rightarrow \text{Root}[8\#1^5ax^2 - 8\#1^4ac_1x^2 - 64\#1^3a^2x + \#1^2(64a^2c_1x + 2x^2) + 128\#1a^3 - 128a^3c_1 - 8ax]$$

**Maple:** cpu = 2.247 (sec), leaf count = 77

$$\left\{ -\frac{1}{2a} \left( -\frac{(y(x))^2 + 1}{(y(x))^4(x(y(x))^2 - 4a)} - 2 \frac{a}{(y(x))^4(x(y(x))^2 - 4a)^2} \right) + \frac{1}{4a^2} \left( 2ay(x) + \frac{1}{2(y(x))^2} + \frac{1}{4(y(x))^4} \right) \right\}$$

**2.915 ODE No. 915**

$$\frac{d}{dx}y(x) = -\frac{-(y(x))^3 - y(x) + 4(y(x))^2 \ln(x) - 4(\ln(x))^2(y(x))^3 - 1 + 6y(x) \ln(x) - 12(\ln(x))^2(y(x)))}{xy(x)}$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.046 (sec), leaf count = 43

$$\left\{ y(x) = 9 \left( 18 \ln(x) + 83 \text{RootOf} \left( -81 \int^{-Z} (6889\_a^3 - 27\_a + 27)^{-1} d\_a - \ln(x) + 3\_C1 \right) - 3 \right) \right\}$$

**2.916 ODE No. 916**

$$\frac{d}{dx}y(x) = \frac{y(x) (\ln(y(x))x + \ln(y(x)) - x - 1 + x \ln(x) + \ln(x) + x^4(\ln(x))^2 + 2x^4 \ln(y(x)) \ln(x) + x^4 \ln^2(y(x)))}{x(1+x)}$$

**Mathematica:** cpu = 2.069763 (sec), leaf count = 66

$$\text{DSolve} \left[ y'(x) = \frac{y(x) (x^4 \log^2(y(x)) + 2x^4 \log(x) \log(y(x)) + x^4 \log^2(x) + x \log(y(x)) + \log(y(x)) - x + x^4 \ln^2(y(x)))}{x(x+1)} \right]$$

**Maple:** cpu = 0.219 (sec), leaf count = 80

$$\left\{ y(x) = e^{-\frac{3x^4 \ln(x) - 4x^3 \ln(x) + 6x^2 \ln(x) + 12 \ln(1+x) \ln(x) - 12\_C1 \ln(x) - 12x \ln(x) + 12x}{3x^4 - 4x^3 + 6x^2 + 12 \ln(1+x) - 12\_C1 - 12x}} \right\}$$

**2.917 ODE No. 917**

$$\frac{d}{dx}y(x) = \frac{y(x) (x \ln(x) + \ln(x) + \ln(y(x)) x + \ln(y(x)) - x - 1 + x(\ln(x))^2 + 2x \ln(y(x)) \ln(x) + x)}{x(1+x)}$$

**Mathematica:** cpu = 1.226656 (sec), leaf count = 60

$$\text{DSolve} \left[ y'(x) = \frac{y(x) (x \log^2(y(x)) + 2x \log(x) \log(y(x)) + x \log(y(x)) + \log(y(x)) - x + x \log^2(x) + x \log(x))}{x(x+1)} \right]$$

**Maple:** cpu = 0.172 (sec), leaf count = 38

$$\left\{ y(x) = e^{-\frac{\ln(1+x) \ln(x) + C1 \ln(x) - x \ln(x) - x}{\ln(1+x) + C1 - x}} \right\}$$

**2.918 ODE No. 918**

$$\frac{d}{dx}y(x) = 2 \frac{(y(x))^8}{(y(x))^5 + 2(y(x))^6 + 2(y(x))^2 + 16x(y(x))^4 + 32(y(x))^6 x^2 + 2 + 24x(y(x))^2 + 96x^2}$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.858 (sec), leaf count = 41

$$\left\{ x - \text{RootOf} \left( \int^{-Z} (64_a^3 + 16_a^2 + 1)^{-1} d_ay(x) + y(x) - C1 + 1 \right) + \frac{1}{4(y(x))^2} = 0 \right\}$$

**2.919 ODE No. 919**

$$\frac{d}{dx}y(x) = \frac{(y(x))^{3/2} (x - y(x) + \sqrt{y(x)})}{(y(x))^{3/2} x - (y(x))^{5/2} + (y(x))^2 + x^3 - 3x^2y(x) + 3x(y(x))^2 - (y(x))^3} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.140 (sec), leaf count = 120

$$\left\{ 2 \frac{(y(x))^{3/2}}{(y(x) - x)^3} + 3 \frac{y(x)}{(y(x) - x)^3} - 6 \frac{\sqrt{y(x)}x}{(y(x) - x)^3} - 6 \frac{x}{(y(x) - x)^3} + 6 \frac{x^2}{\sqrt{y(x)}(y(x) - x)^3} - (y(x) - x) \right\}$$

**2.920 ODE No. 920**

$$\frac{d}{dx}y(x) = 2 \frac{(y(x))^6 (1 + 4x(y(x))^2 + (y(x))^2)}{(y(x))^3 + 4(y(x))^5 x + (y(x))^5 + 2 + 24x(y(x))^2 + 96x^2(y(x))^4 + 128x^3(y(x))^6} = 0$$

**Mathematica:** cpu = 0.244531 (sec), leaf count = 301

$$\{ \{y(x) \rightarrow \text{Root}[\#1^5(128c_1x^2 - 8x - 1) + 128\#1^4x^2 + \#1^3(64c_1x - 2) + 64\#1^2x + 8\#1c_1 + 8\&, 1]\} \}, \{ \}$$

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

**2.921 ODE No. 921**

$$\frac{d}{dx}y(x) = - \left( -\frac{\ln(y(x))}{x} + \frac{\ln(y(x))}{x \ln(x)} - F1(x) \right) y(x) = 0$$

**Mathematica:** cpu = 2.718845 (sec), leaf count = 52

$$\text{Solve} \left[ \text{ConditionalExpression} \left[ \int_1^x \left( \frac{\log(y(x)) - \log(y(x)) \log(K[1])}{K[1]^2} - \frac{\log(K[1])_F1(K[1])}{K[1]} \right) dK[1] = c_1 \right] \right]$$

**Maple:** cpu = 0.093 (sec), leaf count = 30

$$\left\{ y(x) = e^{\frac{x \cdot C1}{\ln(x)}} e^{\frac{x}{\ln(x)} \int \frac{-F1(x) \ln(x)}{x} dx} \right\}$$

**2.922 ODE No. 922**

$$\frac{d}{dx}y(x) = \frac{(y(x))^2}{(y(x))^2 + (y(x))^{3/2} + \sqrt{y(x)}x^2 - 2(y(x))^{3/2}x + (y(x))^{5/2} + x^3 - 3x^2y(x) + 3x(y(x))^2 -}$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.110 (sec), leaf count = 47

$$\left\{ \frac{\ln(y(x))}{2} - \int^{x \frac{1}{\sqrt{y(x)}} - \sqrt{y(x)}} (2_a^3 + 2_a^2 - a + 2)^{-1} d_a - C1 = 0 \right\}$$

## 2.923 ODE No. 923

$$\frac{d}{dx}y(x) = \frac{(y(x))^2 + 2xy(x) + x^2 + e^{-2(x-y(x))(y(x)+x)}}{(y(x))^2 + 2xy(x) + x^2 - e^{-2(x-y(x))(y(x)+x)}} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.156 (sec), leaf count = 36

$$\left\{ y(x) = e^{\text{RootOf}\left(-Z + \int (e^{-Z})^2 - 2xe^{-Z} (e^2 - a + a)^{-1} d_a + C1\right)} - x \right\}$$

## 2.924 ODE No. 924

$$\frac{d}{dx}y(x) = -\frac{y(x)}{\ln(y(x))} \left( -1/2 \frac{(\ln(y(x)))^2}{x} - F1(x) \right) = 0$$

**Mathematica:** cpu = 0.800602 (sec), leaf count = 55

Solve[ConditionalExpression[ $\int_1^x \left( -\frac{F1(K[1])}{K[1]} - \frac{\log^2(y(x))}{2K[1]^2} \right) dK[1] + \frac{1}{2} \log^2(y(x)) = c_1, \Re(x) > 0 \vee \dots$ ]

**Maple:** cpu = 0.094 (sec), leaf count = 47

$$\left\{ y(x) = e^{\sqrt{2 \int \frac{F1(x)}{x} dx + 2x - C1}}, y(x) = e^{-\sqrt{2 \int \frac{F1(x)}{x} dx + 2x - C1}} \right\}$$

## 2.925 ODE No. 925

$$\frac{d}{dx}y(x) = \frac{(y(x))^2 + 2xy(x) + x^2 + e^{2(x-y(x))^2(y(x)+x)^2}}{(y(x))^2 + 2xy(x) + x^2 - e^{2(x-y(x))^2(y(x)+x)^2}} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.188 (sec), leaf count = 38

$$\left\{ y(x) = e^{\text{RootOf}\left(-Z + \int (e^{-Z})^2 - 2xe^{-Z} (e^2 - a^2 + a)^{-1} d_a + C1\right)} - x \right\}$$

**2.926 ODE No. 926**

$$\frac{d}{dx}y(x) = 1/16 \frac{-8x^2(y(x))^3 + 16x(y(x))^2 + 16x(y(x))^3 - 8 + 12xy(x) - 6x^2(y(x))^2 + x^3(y(x))^3}{(-2 + xy(x) - 2y(x))x} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.032 (sec), leaf count = 65

$$\left\{ y(x) = 2 \frac{\sqrt{-C1 + 8 \ln(x)} - 4}{x \sqrt{-C1 + 8 \ln(x)} - 4x + 8}, y(x) = 2 \frac{\sqrt{-C1 + 8 \ln(x)} + 4}{x \sqrt{-C1 + 8 \ln(x)} + 4x - 8} \right\}$$

**2.927 ODE No. 927**

$$\frac{d}{dx}y(x) = -1/8 \left( -8e^{-x^2} + 8x^2e^{-x^2} - 8 - 8(y(x))^2 + 8x^2e^{-x^2}y(x) - 2x^4(e^{-x^2})^2 - 8(y(x))^3 + 12x^2e^{-x^2}y(x) \right)$$

**Mathematica:** cpu = 0.139518 (sec), leaf count = 112

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log \left( \frac{\frac{1}{2}e^{-x^2}x(2e^{x^2}-3x^2)+3xy(x)}{\sqrt[3]{29}\sqrt[3]{x^3}} - \#1 \right)}{\sqrt[3]{29} - 29\#1^2} \& \right] = c_1 + \frac{1}{18}29^{2/3} \right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 72

$$\left\{ y(x) = -\frac{-9x^2e^{-x^2} + 6e^{-x^2}e^{x^2} - 58 \text{RootOf} \left( x^2 - 162 \int^{-Z} (841\_a^3 - 27\_a + 27)^{-1} d\_a + 6\_C1 \right)}{18e^{-x^2}e^{x^2}} \right\}$$

**2.928 ODE No. 928**

$$\frac{d}{dx}y(x) = \frac{1}{x(1+x)} \left( e^{-\frac{y(x)}{x}} y(x) x + e^{-\frac{y(x)}{x}} y(x) + e^{-\frac{y(x)}{x}} x^2 + e^{-\frac{y(x)}{x}} x + x \right) e^{\frac{y(x)}{x}} = 0$$

**Mathematica:** cpu = 1.365673 (sec), leaf count = 23

$$\left\{ \left\{ y(x) \rightarrow -x \log \left( -\frac{\log(x+1) - c_1}{x} \right) \right\} \right\}$$

**Maple:** cpu = 0.265 (sec), leaf count = 21

$$\left\{ y(x) = -\ln \left( -\frac{\ln(1+x) - C1}{x} \right) x \right\}$$

**2.929 ODE No. 929**

$$\frac{d}{dx}y(x) = -1/32 \frac{16x(y(x))^3 - 8(y(x))^3 - 8y(x) + 8x(y(x))^2 - 2x^2(y(x))^3 - 8 + 12xy(x) - 6x^2(y(x))}{xy(x)}$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.031 (sec), leaf count = 42

$$\left\{ y(x) = 18 \left( 58 \operatorname{RootOf} \left( -324 \int^{-Z} (841\_a^3 - 27\_a + 27)^{-1} d\_a - \ln(x) + 12\_C1 \right) + 9x - 6 \right)^{-1} \right\}$$

**2.930 ODE No. 930**

$$\frac{d}{dx}y(x) = \frac{1}{x(1+x)} \left( e^{-\frac{y(x)}{x}} y(x) x + e^{-\frac{y(x)}{x}} y(x) + e^{-\frac{y(x)}{x}} x^2 + e^{-\frac{y(x)}{x}} x + x^4 \right) e^{\frac{y(x)}{x}} = 0$$

**Mathematica:** cpu = 1.567699 (sec), leaf count = 39

$$\left\{ \left\{ y(x) \rightarrow -x \log \left( \frac{-c_1 - \frac{x^3}{3} + \frac{x^2}{2} - x + \log(x+1)}{x} \right) \right\} \right\}$$

**Maple:** cpu = 0.436 (sec), leaf count = 36

$$\left\{ y(x) = -\ln \left( \frac{-2x^3 + 3x^2 + 6 \ln(1+x) - 6\_C1 - 6x}{6x} \right) x \right\}$$

**2.931 ODE No. 931**

$$\frac{d}{dx}y(x) = \frac{-3x^2y(x) - 2x^3 - 2x - x(y(x))^2 - y(x) + x^3(y(x))^3 + 3x^4(y(x))^2 + 3x^5y(x) + x^6}{x(xy(x) + x^2 + 1)} = 0$$

**Mathematica:** cpu = 0.027003 (sec), leaf count = 80

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{x^2 \left( \frac{1}{x} - \frac{1}{x\sqrt{c_1-2x}} \right)} - \frac{x^2+1}{x} \right\}, \left\{ y(x) \rightarrow \frac{1}{x^2 \left( \frac{1}{x\sqrt{c_1-2x}} + \frac{1}{x} \right)} - \frac{x^2+1}{x} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 73

$$\left\{ y(x) = -\frac{1}{x} \left( \sqrt{-C1 - 2xx^2 - x^2 - 1} \right) \left( \sqrt{-C1 - 2x - 1} \right)^{-1}, y(x) = -\frac{1}{x} \left( \sqrt{-C1 - 2xx^2 + x^2 + 1} \right) \right\}$$

**2.932 ODE No. 932**

$$\frac{d}{dx}y(x) = \frac{(27(y(x))^3 + 27e^{3x^2}y(x) + 18e^{3x^2}(y(x))^2 + 3(y(x))^3e^{3x^2} + 27e^{9/2x^2} + 27e^{9/2x^2}y(x) + 9e^{9/2x^2})}{243e^{9/2x^2}y(x)}$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.109 (sec), leaf count = 54

$$\left\{ y(x) = -369 \frac{e^{3/2x^2}}{123 + 123e^{3/2x^2} - 136 \operatorname{RootOf}\left(-41x^2 - 50243409 \int^{-Z}(9248\_a^3 - 1860867\_a + 1860867)\right)} \right\}$$

**2.933 ODE No. 933**

$$\frac{d}{dx}y(x) = -\frac{-x^2 - xy(x) - x^3 - x(y(x))^2 + 2y(x)x^2 \ln(x) - x^3(\ln(x))^2 - (y(x))^3 + 3x(y(x))^2 \ln(x)}{x^2}$$

**Mathematica:** cpu = 0.061008 (sec), leaf count = 99

$$\operatorname{Solve}\left[-\frac{29}{3}\operatorname{RootSum}\left[-29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{\frac{3y(x)}{x^2} + \frac{1-3\log(x)}{x}}{\sqrt[3]{29}\sqrt[3]{\frac{1}{x^3}}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2}\&\right] = c_1 + \frac{29^{2/3}}{9\sqrt[3]{\frac{1}{x^3}}}, y(x)\right]$$

**Maple:** cpu = 0.031 (sec), leaf count = 39

$$\left\{ y(x) = \frac{x\left(9 \ln(x) - 3 + 29 \operatorname{RootOf}\left(-81 \int^{-Z}(841\_a^3 - 27\_a + 27)^{-1} d\_a + x + 3\_C1\right)\right)}{9} \right\}$$

**2.934 ODE No. 934**

$$\frac{d}{dx}y(x) = x/2 + 1 + (y(x))^2 + 1/4x^2y(x) - xy(x) - 1/8x^4 + 1/8x^3 + 1/4x^2 + (y(x))^3 - 3/4x^2(y(x))^2$$

**Mathematica:** cpu = 0.099513 (sec), leaf count = 102

$$\operatorname{Solve}\left[-\frac{31}{3}\operatorname{RootSum}\left[-31\#1^3 + 3 \cdot 2^{2/3}\sqrt[3]{31}\#1 - 31\&, \frac{\log\left(\sqrt[3]{\frac{2}{31}}\left(\frac{1}{4}(-3x^2 - 6x + 4) + 3y(x)\right) - \#1\right)}{2^{2/3}\sqrt[3]{31} - 31\#1^2}\&\right]$$

**Maple:** cpu = 0.063 (sec), leaf count = 39

$$\left\{ y(x) = \frac{x^2}{4} + \frac{x}{2} + \text{RootOf} \left( -x + 2 \int^{-Z} (2_a^3 + 2_a^2 + 1)^{-1} d_a + _C1 \right) \right\}$$

## 2.935 ODE No. 935

$$\frac{d}{dx}y(x) = -x/2 + 1 + (y(x))^2 + 7/2 x^2 y(x) - 2xy(x) + \frac{13x^4}{16} - 3/2 x^3 + x^2 + (y(x))^3 + 3/4 x^2 (y(x))^2 -$$

**Mathematica:** cpu = 49.448279 (sec), leaf count = 246

$$\text{Solve} \left[ -\frac{\sqrt[3]{2} \left( \frac{\frac{1}{4}(3x^2 - 12x + 4) + 3y(x)}{\sqrt[3]{2}} + 2^{2/3} \right) \left( 2^{2/3} - 2^{2/3} \left( \frac{1}{4}(3x^2 - 12x + 4) + 3y(x) \right) \right) \left( \left( \frac{1}{4}(-3x^2 + 12x - 4) - \right)}{9 \left( - \left( \frac{1}{4}(3x^2 - 12x + \right)} \right)} \right)}{9 \left( - \left( \frac{1}{4}(3x^2 - 12x + \right)} \right)} \right]$$

**Maple:** cpu = 0.156 (sec), leaf count = 55

$$\left\{ y(x) = \frac{e^{\text{RootOf}(\ln(e^{-Z}-4)e^{-Z}+_C1 e^{-Z}-_Z e^{-Z}+x e^{-Z}-4 \ln(e^{-Z}-4)-4 _C1+4 _Z-4 x+4)}}{4} - 1 - \frac{x^2}{4} + x \right\}$$

## 2.936 ODE No. 936

$$\frac{d}{dx}y(x) = -x/4 + 1 + (y(x))^2 + \frac{7x^2 y(x)}{16} - 1/2 xy(x) + \frac{5x^4}{128} - \frac{5x^3}{64} + 1/16 x^2 + (y(x))^3 + 3/8 x^2 (y(x))^2 -$$

**Mathematica:** cpu = 0.094012 (sec), leaf count = 99

$$\text{Solve} \left[ -\frac{89}{3} \text{RootSum} \left[ -89\#1^3 + 6\sqrt[3]{178}\#1 - 89\&, \frac{\log \left( \frac{2^{2/3} \left( \frac{1}{8}(3x^2 - 6x + 8) + 3y(x) \right)}{\sqrt[3]{89}} - \#1 \right)}{2\sqrt[3]{178} - 89\#1^2} \right] \& \right] = c_1 + \frac{89^{2/3} x}{18\sqrt[3]{2}},$$

**Maple:** cpu = 0.046 (sec), leaf count = 39

$$\left\{ y(x) = -\frac{x^2}{8} + \frac{x}{4} + \text{RootOf} \left( -x + 4 \int^{-Z} (4_a^3 + 4_a^2 + 3)^{-1} d_a + _C1 \right) \right\}$$



**2.937 ODE No. 937**

$$\frac{d}{dx}y(x) = \frac{-2y(x) - 2 \ln(2x + 1) - 2 + 2x(y(x))^3 + (y(x))^3 + 6(y(x))^2 \ln(2x + 1)x + 3(y(x))^2 \ln(2x + 1)}{(2x + 1)(y(x) + 1)}$$

**Mathematica:** cpu = 0.054007 (sec), leaf count = 124

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{(2x + 1) \left( \frac{2x+1}{4x^2+4x+1} - \frac{1}{(2x+1)\sqrt{c_1-2x}} \right)} - \log(2x + 1) - 1 \right\}, \left\{ y(x) \rightarrow \frac{1}{(2x + 1) \left( \frac{1}{(2x+1)\sqrt{c_1-2x}} + \right)} \right\} \right.$$

**Maple:** cpu = 0.046 (sec), leaf count = 79

$$\left\{ y(x) = -1 \left( \sqrt{-C1 - 2x} \ln(2x + 1) - \ln(2x + 1) - 1 \right) \left( \sqrt{-C1 - 2x} - 1 \right)^{-1}, y(x) = -1 \left( \sqrt{-C1 - 2x} - 1 \right)^{-1} \right.$$

**2.938 ODE No. 938**

$$\frac{d}{dx}y(x) = \frac{-x^2 + x + 1 + (y(x))^2 + 5x^2y(x) - 2xy(x) + 4x^4 - 3x^3 + (y(x))^3 + 3x^2(y(x))^2 - 3x(y(x))}{x}$$

**Mathematica:** cpu = 0.063008 (sec), leaf count = 108

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log \left( \frac{3x^2-3x+1+3y(x)}{x\sqrt[3]{29}\sqrt[3]{\frac{1}{x^3}}} - \#1 \right)}{\sqrt[3]{29} - 29\#1^2} \& \right] = c_1 + \frac{1}{9} 29^{2/3} \left( \frac{1}{x^3} \right)^{2/3} \right.$$

**Maple:** cpu = 0.031 (sec), leaf count = 39

$$\left\{ y(x) = -x^2 + x - \frac{1}{3} + \frac{29 \text{RootOf} \left( -81 \int^{-Z} (841\_a^3 - 27\_a + 27)^{-1} d\_a + \ln(x) + 3\_C1 \right)}{9} \right\}$$

**2.939 ODE No. 939**

$$\frac{d}{dx}y(x) = \frac{-32xy(x) + 16x^3 + 16x^2 - 32x - 64(y(x))^3 + 48x^2(y(x))^2 + 96x(y(x))^2 - 12y(x)x^4 - 48}{-64y(x) + 16x^2 + 32x - 64}$$

**Mathematica:** cpu = 0.380548 (sec), leaf count = 136

$$\text{Solve} \left[ \frac{2}{5} \text{RootSum} \left[ \#1^4 + 4\#1^3 - 8\#1^2y(x) - 16\#1y(x) - 8\#1 + 16y(x)^2 + 16y(x) + 8\&, \frac{\#1^2(-\log(x) - 1)}{5} \right] \right.$$

**Maple:** cpu = 0.094 (sec), leaf count = 70

$$\left\{ x + \frac{2}{5} \ln \left( 2 (y(x) - 1/4 x^2 - x/2)^2 + 2y(x) - \frac{x^2}{2} - x + 1 \right) - \frac{2}{5} \arctan \left( -1 - 2y(x) + \frac{x^2}{2} + x \right) - \frac{4}{5} \ln \right.$$

## 2.940 ODE No. 940

$$\frac{d}{dx} y(x) = \frac{y(x) \ln(x) x + x^2 \ln(x) - 2xy(x) - x^2 - (y(x))^2 - (y(x))^3 + 3x(y(x))^2 \ln(x) - 3x^2(\ln(x))^2}{x(-y(x) + x \ln(x) - x)}$$

**Mathematica:** cpu = 0.022003 (sec), leaf count = 80

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{x \left( -\frac{1}{x^2 \sqrt{c_1 - 2x}} - \frac{1}{x^2} \right)} - x + x \log(x) \right\}, \left\{ y(x) \rightarrow -\frac{1}{x \left( \frac{1}{x^2 \sqrt{c_1 - 2x}} - \frac{1}{x^2} \right)} - x + x \log(x) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 63

$$\left\{ y(x) = x \left( \ln(x) \sqrt{-C1 - 2x} - \ln(x) + 1 \right) \left( \sqrt{-C1 - 2x} - 1 \right)^{-1}, y(x) = x \left( \ln(x) \sqrt{-C1 - 2x} + \ln(x) \right) \right.$$

## 2.941 ODE No. 941

$$\frac{d}{dx} y(x) = \frac{-32xy(x) - 72x^3 + 32x^2 - 32x + 64(y(x))^3 + 48x^2(y(x))^2 - 192x(y(x))^2 + 12y(x)x^4 - 9}{64y(x) + 16x^2 - 64x + 64}$$

**Mathematica:** cpu = 0.372047 (sec), leaf count = 53

Solve[x - 8RootSum[11776#1^3 - 40#1 - 1&, #1 log(17664#1^2 - 1472#1 + 11x^2 + 44y(x) - 44x - 40

**Maple:** cpu = 0.047 (sec), leaf count = 35

$$\left\{ y(x) = -\frac{x^2}{4} + x + \text{RootOf} \left( -x + \int^{-z} \frac{-a+1}{-a^3 - a - 1} d_{-a} + -C1 \right) \right\}$$

**2.942 ODE No. 942**

$$\frac{d}{dx}y(x) = -1 \left( (y(x))^2 + 2xy(x) + x^2 + e^{2 \frac{(x-y(x))^3(y(x)+x)^3}{-(y(x))^2+x^2-1}} \right) \left( -(y(x))^2 - 2xy(x) - x^2 + e^{2 \frac{(x-y(x))^3(y(x)+x)^3}{-(y(x))^2+x^2-1}} \right)$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.390 (sec), leaf count = 43

$$\left\{ y(x) = e^{\text{RootOf}\left(-Z + \int (e^{-Z})^2 - 2xe^{-Z} \left( e^{2 \frac{a^3}{-a+1} + a} \right)^{-1} d_a + C1 \right)} - x \right\}$$

**2.943 ODE No. 943**

$$\frac{d}{dx}y(x) = \frac{-128xy(x) - 24x^3 + 32x^2 - 128x + 512(y(x))^3 + 192x^2(y(x))^2 - 384x(y(x))^2 + 24y(x)x^3}{512y(x) + 64x^2 - 128x + 512}$$

**Mathematica:** cpu = 0.394550 (sec), leaf count = 53

Solve[x - 16RootSum[6656#1^3 - 23#1 - 1&, #1 log(79872#1^2 - 18304#1 + 181x^2 + 1448y(x) - 362x^3)]]

**Maple:** cpu = 0.047 (sec), leaf count = 40

$$\left\{ y(x) = -\frac{x^2}{8} + \frac{x}{4} + \text{RootOf}\left(-x + \int^{-Z} 4 \frac{-a+1}{4-a^3-a-1} d_a + C1 \right) \right\}$$

**2.944 ODE No. 944**

$$\frac{d}{dx}y(x) = \frac{-32axy(x) - 8a^2x^3 - 16ax^2b - 32ax + 64(y(x))^3 + 48ax^2(y(x))^2 + 96(y(x))^2bx + 12y(x)x^3}{64y(x) + 16ax^2 + 32bx}$$

**Mathematica:** cpu = 1.613205 (sec), leaf count = 233

Solve[x - 4RootSum[#1^6a^3 + 6#1^5a^2b + 12#1^4a^2y(x) + 12#1^4ab^2 + 48#1^3aby(x) + 8#1^3b^3 + 8#1^2ab^2]]

**Maple:** cpu = 0.062 (sec), leaf count = 47

$$\left\{ y(x) = -\frac{ax^2}{4} - \frac{bx}{2} + \text{RootOf}\left(bx + 2 \int^{-Z} -\frac{b(-a+1)}{2-a^3-ab+b} d_a + 2C1 \right) \right\}$$

## 2.945 ODE No. 945

$$\frac{d}{dx}y(x) = \frac{-32xy(x) - 8x^3 - 16ax^2 - 32x + 64(y(x))^3 + 48x^2(y(x))^2 + 96ax(y(x))^2 + 12y(x)x^4 + 4}{64y(x) + 16x^2 + 32ax + 64}$$

**Mathematica:** cpu = 1.213154 (sec), leaf count = 213

$$\text{Solve}\left[x - 4\text{RootSum}\left[\#1^6 + 6\#1^5a + 12\#1^4a^2 + 12\#1^4y(x) + 8\#1^3a^3 + 48\#1^3ay(x) + 48\#1^2a^2y(x) + \dots\right]\right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 41

$$\left\{y(x) = -\frac{x^2}{4} - \frac{ax}{2} + \text{RootOf}\left(-x + \int^{-Z} 2 \frac{-a+1}{2-a^3+aa+a} d_a + \_C1\right)\right\}$$

## 2.946 ODE No. 946

$$\frac{d}{dx}y(x) = \frac{\left(-8e^{-x^2}y(x) + 4x^2(e^{-x^2})^2 - 8e^{-x^2} + 8x^2e^{-x^2}y(x) - 4x^4(e^{-x^2})^2 + 8x^2e^{-x^2} - 8(y(x))^3 + \dots\right)}{-8y(x) + 4x^2e^{-x^2} - 8}$$

**Mathematica:** cpu = 0.081510 (sec), leaf count = 150

$$\left\{\left\{y(x) \rightarrow \frac{e^{-3x^2}}{8\left(\frac{1}{8}e^{-3x^2} - \frac{e^{-3x^2}}{\sqrt{c_1-64x^2}}\right)} - \frac{1}{2}e^{-x^2}(2e^{x^2} - x^2)\right\}, \left\{y(x) \rightarrow \frac{e^{-3x^2}}{8\left(\frac{e^{-3x^2}}{\sqrt{c_1-64x^2}} + \frac{1}{8}e^{-3x^2}\right)} - \frac{1}{2}e^{-x^2}(2e^{x^2} - x^2)\right\}\right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 100

$$\left\{y(x) = \frac{1}{2}\left(e^{-x^2}\sqrt{-x^2 + \_C1x^2} - x^2e^{-x^2} + 2\right)\left(-1 + \sqrt{-x^2 + \_C1}\right)^{-1}, y(x) = \frac{1}{2}\left(e^{-x^2}\sqrt{-x^2 + \_C1x^2} + x^2e^{-x^2} - 2\right)\left(-1 + \sqrt{-x^2 + \_C1}\right)^{-1}\right\}$$

## 2.947 ODE No. 947

$$\frac{d}{dx}y(x) = 1/2 \frac{2x^2 \cos(x) + 2 \sin(x)x^3 - 2x \sin(x) + 2x + 2x^2(y(x))^2 - 4y(x) \sin(x)x + 4y(x) \cos(x)}{x^5}$$

**Mathematica:** cpu = 0.108014 (sec), leaf count = 30

$$\left\{\left\{y(x) \rightarrow \frac{1}{c_1 - \log(x)} - \frac{-\sin(x) + x \cos(x) + 1}{x}\right\}\right\}$$

**Maple:** cpu = 0.171 (sec), leaf count = 36

$$\left\{y(x) = -\frac{x}{2}\left(2\frac{\cos(x)}{x} - 2\frac{\sin(x)}{x^2} + 2x^{-2}\right) + (\_C1 - \ln(x))^{-1}\right\}$$

**2.948 ODE No. 948**

$$\frac{d}{dx}y(x) = -216 \frac{y(x)}{-216 (y(x))^4 - 252 (y(x))^3 - 396 (y(x))^2 - 216 y(x) + 36 x^2 - 72 xy(x) + 60 (y(x))}$$

**Mathematica:** cpu = 0.259033 (sec), leaf count = 39

$$\text{Solve} \left[ \frac{36}{y(x) (2y(x)^3 + 3y(x)^2 + 6y(x) + 6) - 6x} + \log(y(x)) = c_1, y(x) \right]$$

**Maple:** cpu = 0.140 (sec), leaf count = 68

$$\left\{ y(x) = e^{\text{RootOf}(-12\_C1 (e^{-Z})^4 - 2 (e^{-Z})^4 - Z - 18\_C1 (e^{-Z})^3 - 3 (e^{-Z})^3 - Z - 36\_C1 (e^{-Z})^2 - 6\_Z (e^{-Z})^2 - 36\_C1 e^{-Z} - 6\_Z e^{-Z} + 36)} \right\}$$

**2.949 ODE No. 949**

$$\frac{d}{dx}y(x) = \frac{x^2 y(x) + x^4 + 2x^3 - 3x^2 + xy(x) + x + (y(x))^3 + 3x^2(y(x))^2 - 3x(y(x))^2 + 3y(x)x^4 - 6x^3}{x(y(x) + x^2 - x + 1)}$$

**Mathematica:** cpu = 0.021003 (sec), leaf count = 76

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{x \left( \frac{1}{x} - \frac{1}{x\sqrt{c_1 - 2 \log(x)}} \right)} - x^2 + x - 1 \right\}, \left\{ y(x) \rightarrow \frac{1}{x \left( \frac{1}{x\sqrt{c_1 - 2 \log(x)}} + \frac{1}{x} \right)} - x^2 + x - 1 \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 97

$$\left\{ y(x) = -1 \left( \sqrt{-C1 - 2 \ln(x)} x^2 - \sqrt{-C1 - 2 \ln(x)} x - x^2 + x - 1 \right) \left( -1 + \sqrt{-C1 - 2 \ln(x)} \right)^{-1}, y(x) \right\}$$

**2.950 ODE No. 950**

$$\frac{d}{dx}y(x) = -1/2 ax + 1 + (y(x))^2 + 1/2 ax^2 y(x) + bxy(x) + 1/16 a^2 x^4 + 1/4 ax^3 b + 1/4 b^2 x^2 + (y(x))^3 +$$

**Mathematica:** cpu = 0.167521 (sec), leaf count = 141

$$\text{Solve} \left[ -\frac{1}{3} (27b + 58)^{2/3} \text{RootSum} \left[ \#1^3 (27b + 58)^{2/3} - 3 \cdot 2^{2/3} \#1 + (27b + 58)^{2/3} \&, \frac{\log \left( \frac{\sqrt[3]{2} (\frac{1}{4} (3ax^2 + 6bx + 4) + 3)}{\sqrt[3]{27b + 58}} \right)}{2^{2/3} - \#1^2 (27b + 58)^{2/3}} \right] \right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 42

$$\left\{ y(x) = -\frac{ax^2}{4} - \frac{bx}{2} + \text{RootOf} \left( -x + 2 \int^{-Z} (2\_a^3 + 2\_a^2 + b + 2)^{-1} d\_a + -C1 \right) \right\}$$

**2.951 ODE No. 951**

$$\frac{d}{dx}y(x) = -x/2 + 1 + (y(x))^2 + 1/2 x^2 y(x) + axy(x) + 1/16 x^4 + 1/4 ax^3 + 1/4 a^2 x^2 + (y(x))^3 + 3/4 x^5$$

**Mathematica:** cpu = 0.144018 (sec), leaf count = 140

$$\text{Solve} \left[ -\frac{1}{3}(27a + 58)^{2/3} \text{RootSum} \left[ \#1^3(27a + 58)^{2/3} - 3 \cdot 2^{2/3} \#1 + (27a + 58)^{2/3} \&, \frac{\log \left( \frac{\sqrt[3]{2}(\frac{1}{4}(6ax+3x^2+4))+3}{\sqrt[3]{27a+58}} \right)}{2^{2/3} - \#1^2(27a + 58)^{2/3}} \right] \right]$$

**Maple:** cpu = 0.062 (sec), leaf count = 41

$$\left\{ y(x) = -\frac{x^2}{4} - \frac{ax}{2} + \text{RootOf} \left( -x + 2 \int^{-Z} (2\_a^3 + 2\_a^2 + a + 2)^{-1} d\_a + \_C1 \right) \right\}$$

**2.952 ODE No. 952**

$$\frac{d}{dx}y(x) = -\frac{-y(x) + \sqrt{(y(x))^2 + x^2 x^2} - x \sqrt{(y(x))^2 + x^2 y(x)} + x^4 \sqrt{(y(x))^2 + x^2} - x^3 \sqrt{(y(x))^2 + x^2}}{x}$$

**Mathematica:** cpu = 0.139018 (sec), leaf count = 189

$$\left\{ \left\{ y(x) \rightarrow \frac{x \left( -2e^{\sqrt{2}c_1 + \frac{\sqrt{2}x^5}{5} + \frac{x^4}{2\sqrt{2}} + \frac{x^2}{\sqrt{2}}} + e^{2\sqrt{2}c_1 + \frac{2\sqrt{2}x^5}{5} + \frac{x^4}{\sqrt{2}} + \sqrt{2}x^2} - 1 \right)}{2e^{\sqrt{2}c_1 + \frac{\sqrt{2}x^5}{5} + \frac{x^4}{2\sqrt{2}} + \frac{x^2}{\sqrt{2}}} + e^{2\sqrt{2}c_1 + \frac{2\sqrt{2}x^5}{5} + \frac{x^4}{\sqrt{2}} + \sqrt{2}x^2} - 1 \right\} \right\}$$

**Maple:** cpu = 0.202 (sec), leaf count = 65

$$\left\{ \ln \left( 2 \frac{x \left( \sqrt{2} (y(x))^2 + 2x^2 + y(x) + x \right)}{y(x) - x} \right) + \frac{\sqrt{2}x^5}{5} + \frac{\sqrt{2}x^4}{4} + \frac{\sqrt{2}x^2}{2} - \ln(x) - \_C1 = 0 \right\}$$

**2.953 ODE No. 953**

$$\frac{d}{dx}y(x) = \frac{y(x) (\ln(x) + \ln(y(x)) - 1 + x(\ln(x))^2 + 2x \ln(y(x)) \ln(x) + x(\ln(y(x)))^2 + x^3(\ln(x))^2 + 2x^3 \ln(y(x)) \ln(x))}{x}$$

**Mathematica:** cpu = 1.521193 (sec), leaf count = 97

$$\text{DSolve} \left[ y'(x) = \frac{y(x) (x^4 \log^2(y(x)) + 2x^4 \log(x) \log(y(x)) + x^4 \log^2(x) + x^3 \log^2(y(x)) + 2x^3 \log(x) \log(y(x)))}{x}, y(x) \right]$$

**Maple:** cpu = 0.281 (sec), leaf count = 145

$$\left\{ y(x) = 1 \left( \frac{x^5}{x^{4x^5+5x^4+10x^2+20} - C1} \right)^{-4} \left( \frac{x^4}{x^{4x^5+5x^4+10x^2+20} - C1} \right)^{-5} \left( \frac{x^2}{x^{4x^5+5x^4+10x^2+20} - C1} \right)^{-10} \left( \frac{C1}{x^{4x^5+5x^4+10x^2+20} - C1} \right)^{-10} \right.$$

**2.954 ODE No. 954**

$$\frac{d}{dx}y(x) = \frac{150x^3 + 125\sqrt{x} + 125 + 125(y(x))^2 - 100x^3y(x) - 500y(x)\sqrt{x} + 20x^6 + 200x^{7/2} + 500x - 125y(x)^3}{x}$$

**Mathematica:** cpu = 0.087511 (sec), leaf count = 115

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log \left( \frac{-6x^3 - 30\sqrt{x} + 5 + \frac{3y(x)}{x}}{\sqrt[3]{29}\sqrt[3]{\frac{1}{x^3}}} - \#1 \right)}{\sqrt[3]{29} - 29\#1^2} \& \right] = c_1 + \frac{1}{9} 29^{2/3} \left( \frac{1}{x^3} \right) \right]$$

**Maple:** cpu = 0.031 (sec), leaf count = 53

$$\left\{ y(x) = \frac{1}{45} \left( 18x^{7/2} + 145 \text{RootOf} \left( -81 \int^{-Z} (841\_a^3 - 27\_a + 27)^{-1} d\_a + \ln(x) + 3\_C1 \right) \sqrt{x} - 1 \right) \right.$$

**2.955 ODE No. 955**

$$\frac{d}{dx}y(x) = \frac{1}{25} \frac{-150x^3y(x) + 60x^6 + 350x^{7/2} - 150x^3 - 125y(x)\sqrt{x} + 250x - 125\sqrt{x} - 125(y(x))^3}{x}$$

**Mathematica:** cpu = 0.043006 (sec), leaf count = 112

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{5} (2x^3 + 10\sqrt{x} - 5) - \frac{1}{125x \left( -\frac{1}{x\sqrt{c_1 - 31250 \log(x)}} - \frac{1}{125x} \right)} \right\}, \left\{ y(x) \rightarrow \frac{1}{5} (2x^3 + 10\sqrt{x} - 5) - \frac{1}{125x \left( \frac{1}{x\sqrt{c_1 - 31250 \log(x)}} + \frac{1}{125x} \right)} \right\} \right.$$

**Maple:** cpu = 0.078 (sec), leaf count = 111

$$\left\{ y(x) = \frac{1}{5} \left( 2 \sqrt{-C1 - 2 \ln(x)} x^3 - 2 x^3 + 10 \sqrt{x} \sqrt{-C1 - 2 \ln(x)} - 10 \sqrt{x} + 5 \right) \left( -1 + \sqrt{-C1 - 2 \ln(x)} \right) \right.$$

## 2.956 ODE No. 956

$$\frac{d}{dx} y(x) = \frac{y(x)}{(\ln(x) + 1) x} \left( -1 - x^{2(\ln(x)+1)^{-1}} e^{2 \frac{(\ln(x))^2}{\ln(x)+1}} x^2 - x^{2(\ln(x)+1)^{-1}} e^{2 \frac{(\ln(x))^2}{\ln(x)+1}} x^2 \ln(x) + x^{2(\ln(x)+1)^{-1}} e^{2 \frac{(\ln(x))^2}{\ln(x)+1}} \right)$$

**Mathematica:** cpu = 0.210527 (sec), leaf count = 28

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{\left( c_1 e^{\frac{x^4}{4}} + 1 \right) (\log(x) + 1)} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 197

$$\left\{ y(x) = 1 e^{-\frac{x^4}{4}} \left( (\ln(x))^2 e^{\frac{-x^4 \ln(x) - x^4 + 8 (\ln(x))^2 - 4 \ln(\ln(x)+1) \ln(x) - 4 \ln(\ln(x)+1)}{4 \ln(x)+4}} x^{-2 \frac{\ln(x)}{\ln(x)+1}} + 2 \ln(x) e^{1/4 \frac{-x^4 \ln(x) - x^4 + 8 (\ln(x))^2 - 4 \ln(\ln(x)+1) \ln(x) - 4 \ln(\ln(x)+1)}{4 \ln(x)+4}} \right) \right.$$

## 2.957 ODE No. 957

$$\frac{d}{dx} y(x) = \frac{y(x)}{(\ln(x) + 1) x} \left( -1 - x^3 x^{2(\ln(x)+1)^{-1}} e^{2 \frac{(\ln(x))^2}{\ln(x)+1}} - x^3 x^{2(\ln(x)+1)^{-1}} e^{2 \frac{(\ln(x))^2}{\ln(x)+1}} \ln(x) + x^3 x^{2(\ln(x)+1)^{-1}} e^{2 \frac{(\ln(x))^2}{\ln(x)+1}} \right)$$

**Mathematica:** cpu = 0.198525 (sec), leaf count = 28

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{\left( c_1 e^{\frac{x^5}{5}} + 1 \right) (\log(x) + 1)} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 197

$$\left\{ y(x) = 1 e^{-\frac{x^5}{5}} \left( (\ln(x))^2 e^{\frac{-x^5 \ln(x) - x^5 + 10 (\ln(x))^2 - 5 \ln(\ln(x)+1) \ln(x) - 5 \ln(\ln(x)+1)}{5 \ln(x)+5}} x^{-2 \frac{\ln(x)}{\ln(x)+1}} + 2 \ln(x) e^{1/5 \frac{-x^5 \ln(x) - x^5 + 10 (\ln(x))^2 - 5 \ln(\ln(x)+1) \ln(x) - 5 \ln(\ln(x)+1)}{5 \ln(x)+5}} \right) \right.$$



**2.958 ODE No. 958**

$$\frac{d}{dx}y(x) = \frac{2x + 4y(x) \ln(2x + 1)x + 6(y(x))^2 \ln(2x + 1)x + 6y(x) (\ln(2x + 1))^2 x + 2(\ln(2x + 1))^3}{1}$$

**Mathematica:** cpu = 0.060508 (sec), leaf count = 82

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log \left( \frac{3y(x)+3\log(2x+1)+1}{\sqrt[3]{29}} - \#1 \right)}{\sqrt[3]{29} - 29\#1^2} \& \right] = c_1 + \frac{1}{9} 29^{2/3} x, y(x) \right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 40

$$\left\{ y(x) = -\ln(2x + 1) - \frac{1}{3} + \frac{29 \text{RootOf} \left( -81 \int^{-Z} (841\_a^3 - 27\_a + 27)^{-1} d\_a + x + 3\_C1 \right)}{9} \right\}$$

**2.959 ODE No. 959**

$$\frac{d}{dx}y(x) = 1/2 \frac{1}{x} \left( -y(x) \sin \left( \frac{y(x)}{x} \right) + y(x) \sin \left( 3/2 \frac{y(x)}{x} \right) \cos \left( 1/2 \frac{y(x)}{x} \right) + y(x) \cos \left( 1/2 \frac{y(x)}{x} \right) \sin \left( \frac{y(x)}{x} \right) \right)$$

**Mathematica:** cpu = 0.045506 (sec), leaf count = 20

$$\left\{ \left\{ y(x) \rightarrow x \sin^{-1} \left( e^{c_1 + \frac{x^2}{2}} \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 16

$$\left\{ y(x) = \frac{\arccos \left( e^{x^2} \_C1 + 1 \right) x}{2} \right\}$$

**2.960 ODE No. 960**

$$\frac{d}{dx}y(x) = 1/2 \frac{1}{x} \left( -y(x) \sin \left( \frac{y(x)}{x} \right) + y(x) \sin \left( 3/2 \frac{y(x)}{x} \right) \cos \left( 1/2 \frac{y(x)}{x} \right) + y(x) \cos \left( 1/2 \frac{y(x)}{x} \right) \sin \left( \frac{y(x)}{x} \right) \right)$$

**Mathematica:** cpu = 0.035505 (sec), leaf count = 14

$$\left\{ \left\{ y(x) \rightarrow x \sin^{-1} \left( e^{c_1 + x} \right) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 16

$$\left\{ y(x) = \frac{\arccos \left( \_C1 (e^x)^2 + 1 \right) x}{2} \right\}$$

**2.961 ODE No. 961**

$$\frac{d}{dx}y(x) = \frac{(y(x))^2 + 2xy(x) + x^2 + e^{2+2(y(x))^4-4x^2(y(x))^2+2x^4+2(y(x))^6-6x^2(y(x))^4+6x^4(y(x))^2-2x^6}}{(y(x))^2 + 2xy(x) + x^2 - e^{2+2(y(x))^4-4x^2(y(x))^2+2x^4+2(y(x))^6-6x^2(y(x))^4+6x^4(y(x))^2-2x^6}} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.312 (sec), leaf count = 45

$$\left\{ y(x) = e^{\text{RootOf}\left(-Z + \int (e^{-Z})^{-2xe^{-Z}} (e^2 - a^3 + 2 - a^2 + 2 + -a)^{-1} d_a + -C1\right)} - x \right\}$$

**2.962 ODE No. 962**

$$\frac{d}{dx}y(x) = 4 \frac{x}{-4(y(x))^3 + 4a^2x^2y(x) - 4x^2y(x) - 8y(x) - a^2(y(x))^6 + 3a^4(y(x))^4x^2 - 6(y(x))^4a^2}$$

**Mathematica:** cpu = 5.355180 (sec), leaf count = 1191

$$\{ \{ y(x) \rightarrow \text{Root}[2x^4a^8 - 8x^4a^6 + e^{c1}x^4a^4 + 11x^4a^4 - 2e^{c1}x^4a^2 - 6x^4a^2 + 4x^2a^2 + (2a^2 - 2)\#1^5 + e^{c1}x^4 - \dots]$$

**Maple:** cpu = 1.092 (sec), leaf count = 79

$$\left\{ -\frac{y(x)}{(a-1)(a+1)} + 2 \frac{1}{(a^2-1)^2(a^2x^2-x^2-(y(x))^2)^2} - 2 \frac{1}{(a^2-1)^2(a^2x^2-x^2-(y(x))^2)} + -C1 = 0 \right\}$$

**2.963 ODE No. 963**

$$\frac{d}{dx}y(x) = 1/4 \frac{-4 \cos(x)x + 4x^2 \sin(x) + 4x + 4 + 4(y(x))^2 + 8y(x) \cos(x)x - 8xy(x) + 2x^2 \cos(2x)}{}$$

**Mathematica:** cpu = 0.112014 (sec), leaf count = 108

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{3y(x) + -3x + 3x \cos(x) + 1}{\sqrt[3]{29} \sqrt[3]{\frac{1}{x^3}}}\right) - \#1}{\sqrt[3]{29} - 29\#1^2} \& \right] = c_1 + \frac{1}{9} 29^{2/3} \left( \frac{1}{x^3} \right) \right]$$

**Maple:** cpu = 0.156 (sec), leaf count = 39

$$\left\{ y(x) = -\cos(x)x + x - \frac{1}{3} + \frac{29 \text{RootOf}\left(-81 \int^{-Z} (841 - a^3 - 27 - a + 27)^{-1} d_a + \ln(x) + 3 - C1\right)}{9} \right\}$$

**2.964 ODE No. 964**

$$\frac{d}{dx}y(x) = -8 \frac{1}{8 - 8y(x) + 2x^4 + 3x^4(y(x))^2 + 4x^2(y(x))^2 + 2(y(x))^4 + 3a^4(y(x))^4 x^2 - 3a^6(y(x))}$$

**Mathematica:** cpu = 4.810111 (sec), leaf count = 264

$$\text{Solve} \left[ \frac{y(x)}{(a-1)(a+1)} - \frac{8\text{RootSum}[-\#1^3 a^6 + 3\#1^3 a^4 - 3\#1^3 a^2 + \#1^3 + 3\#1^2 a^4 y(x)^2 + 2\#1^2 a^4 - 6\#1^2 a^2 y(x) + 2\#1^2 a^2 y(x)^2 - 6\#1^2 a^2 y(x)^2 + 2\#1^2 a^2 y(x)^2 - 6\#1^2 a^2 y(x)^2]}{(a-1)(a+1)} \right]$$

**Maple:** cpu = 2.012 (sec), leaf count = 80

$$\left\{ \frac{y(x)}{(a-1)(a+1)} + 4 \frac{1}{a^4 - 2a^2 + 1} \sum_{-R=\text{RootOf}(-Z^3+2-Z^2+8)} \frac{\ln(-a^2 x^2 + x^2 + (y(x))^2 - R)}{3R^2 + 4R} - C1 = 0 \right\}$$

**2.965 ODE No. 965**

$$\frac{d}{dx}y(x) = 1/2 \frac{1}{x} \left( -y(x) \sin\left(\frac{y(x)}{x}\right) + y(x) \sin\left(3/2 \frac{y(x)}{x}\right) \cos\left(1/2 \frac{y(x)}{x}\right) + y(x) \cos\left(1/2 \frac{y(x)}{x}\right) \sin\left(\frac{y(x)}{x}\right) \right)$$

**Mathematica:** cpu = 0.056007 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow x \sin^{-1} \left( x e^{c_1 + \frac{x^3}{3} + \frac{x^2}{2}} \right) \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 25

$$\left\{ y(x) = \frac{x}{2} \arccos \left( e^{\frac{2x^3}{3}} e^{x^2} C1 x^2 + 1 \right) \right\}$$

**2.966 ODE No. 966**

$$\frac{d}{dx}y(x) = -1296 \frac{1}{216 - 432xy(x) - 648x^2y(x) + 216x(y(x))^2 - 1296y(x) + 216x^3 + 216x^2 - 2376}$$

**Mathematica:** cpu = 0.439556 (sec), leaf count = 292

$$\text{Solve} \left[ 72\text{RootSum} \left[ -216\#1^3 + 216\#1^2 y(x)^4 + 324\#1^2 y(x)^3 + 648\#1^2 y(x)^2 + 648\#1^2 y(x) - 216\#1^2 \right] \right]$$

**Maple:** cpu = 0.484 (sec), leaf count = 50

$$\left\{ y(x) = e^{\text{RootOf} \left( -Z - 6 \int x^{-1/3} (e^{-Z})^4 - 1/2 (e^{-Z})^3 - (e^{-Z})^2 - e^{-Z} (-a^3 + a^2 + 1)^{-1} d_a - C1 \right)} \right\}$$

**2.967 ODE No. 967**

$$\frac{d}{dx}y(x) = -\frac{x(-513 - 432x - 594x^2y(x) + 720x^3y(x) - 378y(x) - 864x^4 - 756x^3 - 1134x^2 - 540(y(x)^2 + 1))}{x^2 + 1}$$

**Mathematica:** cpu = 0.128516 (sec), leaf count = 151

$$\text{Solve} \left[ -\frac{29}{3} \text{RootSum} \left[ -29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log \left( \frac{\frac{3xy(x) + -4x^4 + 2x^3 + 5x}{x^2 + 1}}{2(x^2 + 1)^2} - \#1 \right)}{\sqrt[3]{29} \sqrt[3]{\frac{x^3}{(x^2 + 1)^3}}} \right] \&, \right] = c_1 + \frac{29^{2/3} \left( \frac{x^3}{(x^2 + 1)^2} \right)}{18x^2 + 18}$$

**Maple:** cpu = 0.062 (sec), leaf count = 90

$$\left\{ y(x) = \frac{58 \text{RootOf} \left( -162 \int^{-Z} (841\_a^3 - 27\_a + 27)^{-1} d\_a + \ln(x^2 + 1) + 6\_C1 \right) x^2 + 12x^3 - 6x^2}{18x^2 + 18} \right\}$$

**2.968 ODE No. 968**

$$\frac{d}{dx}y(x) = 1/2 \frac{1}{x(1+x)} \left( -\sin \left( \frac{y(x)}{x} \right) y(x) x - y(x) \sin \left( \frac{y(x)}{x} \right) + y(x) \sin \left( 3/2 \frac{y(x)}{x} \right) \cos \left( 1/2 \frac{y(x)}{x} \right) \right)$$

**Mathematica:** cpu = 0.084511 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow x \sin^{-1} \left( (x + 1)e^{c_1 + \frac{x^2}{2} - x - \frac{3}{2}} \right) \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 45

$$\left\{ y(x) = \frac{x}{2} \arccos \left( \frac{e^{x^2} - C1 x^2}{(e^x)^2} + 2 \frac{e^{x^2} - C1 x}{(e^x)^2} + \frac{e^{x^2} - C1}{(e^x)^2} + 1 \right) \right\}$$

**2.969 ODE No. 969**

$$\frac{d}{dx}y(x) = 1/2 \frac{1}{x(1+x)} \left( y(x) \sin \left( 3/2 \frac{y(x)}{x} \right) \cos \left( 1/2 \frac{y(x)}{x} \right) x + y(x) \sin \left( 3/2 \frac{y(x)}{x} \right) \cos \left( 1/2 \frac{y(x)}{x} \right) \right)$$

**Mathematica:** cpu = 0.058507 (sec), leaf count = 19

$$\left\{ \left\{ y(x) \rightarrow x \sin^{-1} \left( \frac{e^{c_1} x}{x+1} \right) \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 27

$$\left\{ y(x) = \frac{x}{2} \arccos \left( \frac{-C1 x^2 + x^2 + 2x + 1}{(1+x)^2} \right) \right\}$$

**2.970 ODE No. 970**

$$\frac{d}{dx}y(x) = -216 \frac{1}{-1296 xy(x) - 648 x^2 y(x) - 1944 x (y(x))^2 - 1296 y(x) + 216 x^3 - 1296 (y(x))^2 + 17}$$

**Mathematica:** cpu = 0.475060 (sec), leaf count = 66

$$\text{Solve} \left[ \frac{36(2y(x)^4 + 3y(x)^3 + 6y(x)^2 + 6y(x) - 6x - 3)}{(y(x)(2y(x)^3 + 3y(x)^2 + 6y(x) + 6) - 6x)^2} + \log(y(x)) = c_1, y(x) \right]$$

**Maple:** cpu = 0.562 (sec), leaf count = 183

$$\left\{ x - \frac{1}{-6\_C1 + 6 \ln(y(x))} \left( 2 \ln(y(x)) (y(x))^4 - 2\_C1 (y(x))^4 + 3 \ln(y(x)) (y(x))^3 - 3\_C1 (y(x))^3 + \dots \right) \right\}$$

**2.971 ODE No. 971**

$$\frac{d}{dx}y(x) = \frac{(xy(x) + 1)^3}{x^5} = 0$$

**Mathematica:** cpu = 0.101013 (sec), leaf count = 157

$$\text{Solve} \left[ \frac{1}{3} \log \left( \frac{\frac{3}{x^3} + \frac{3y(x)}{x^2}}{3 \sqrt[3]{-\frac{1}{x^6}}} + 1 \right) - \frac{1}{6} \log \left( \frac{\left( \frac{3}{x^3} + \frac{3y(x)}{x^2} \right)^2}{9 \left( -\frac{1}{x^6} \right)^{2/3}} - \frac{\frac{3}{x^3} + \frac{3y(x)}{x^2}}{3 \sqrt[3]{-\frac{1}{x^6}}} + 1 \right) + \frac{\tan^{-1} \left( \frac{2 \left( \frac{3}{x^3} + \frac{3y(x)}{x^2} \right) - 1}{\frac{3 \sqrt[3]{-\frac{1}{x^6}}}{\sqrt{3}}}}{\sqrt{3}} \right)}{\sqrt{3}} = c \right]$$

**Maple:** cpu = 0.187 (sec), leaf count = 88

$$\left\{ y(x) = \frac{\sqrt{3}}{6x} \left( \sqrt{3} \sqrt[3]{-x^{-6}x^3} + 3 \tan \left( \text{RootOf} \left( -18x^3(-x^{-6})^{2/3} - 6\_Z \sqrt{3} - \ln \left( \frac{(\sqrt{3} + \tan(\_Z))^6}{((\tan(\_Z))^2 + 1)^3} \right) \right) \right) \right.$$

## 2.972 ODE No. 972

$$\frac{d}{dx}y(x) = \frac{x(-x^2 + 2x^2y(x) - 2x^4 + 1)}{y(x) - x^2} = 0$$

**Mathematica:** cpu = 0.032004 (sec), leaf count = 32

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( W \left( -e^{c_1 + x^4 - 2x^2 - 1} \right) + 1 \right) + x^2 \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 27

$$\left\{ y(x) = x^2 + \frac{1}{2} \text{lambertW} \left( -2 \frac{e^{x^4} - C_1 e^{-1}}{(e^{x^2})^2} \right) + \frac{1}{2} \right\}$$

## 2.973 ODE No. 973

$$\frac{d}{dx}y(x) = \frac{y(x) \left( (y(x))^2 + y(x) e^{bx} + (e^{bx})^2 \right)}{(e^{bx})^2} = 0$$

**Mathematica:** cpu = 0.163521 (sec), leaf count = 146

$$\text{Solve} \left[ -\frac{1}{3}(9b-7)^{2/3} \text{RootSum} \left[ \#1^3(9b-7)^{2/3} - 9\#1b + 6\#1 + (9b-7)^{2/3} \&, \frac{\log \left( \frac{3e^{-2bx}y(x)+e^{-bx}}{\sqrt[3]{(9b-7)e^{-3bx}}} - \#1 \right)}{\#1^2(-(9b-7)^{2/3})+3b} \right] \right]$$

**Maple:** cpu = 0.234 (sec), leaf count = 136

$$\left\{ y(x) = \frac{1}{2} \tan \left( \text{RootOf} \left( -2\_Z e^{bx} - \ln \left( -(4(\tan(\_Z))^2 b - 3(\tan(\_Z))^2 + 4b - 3) \left( -\tan(\_Z) \sqrt{\dots} \right) \right) \right) \right)$$

**2.974 ODE No. 974**

$$\frac{d}{dx}y(x) = (y(x))^3 - 3x^2(y(x))^2 + 3y(x)x^4 - x^6 + 2x = 0$$

**Mathematica:** cpu = 0.010001 (sec), leaf count = 39

$$\left\{ \left\{ y(x) \rightarrow x^2 - \frac{1}{\sqrt{c_1 - 2x}} \right\}, \left\{ y(x) \rightarrow \frac{1}{\sqrt{c_1 - 2x}} + x^2 \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 57

$$\left\{ y(x) = 1 \left( x^2 \sqrt{2\_C1 - 2x} - 1 \right) \frac{1}{\sqrt{2\_C1 - 2x}}, y(x) = 1 \left( x^2 \sqrt{2\_C1 - 2x} + 1 \right) \frac{1}{\sqrt{2\_C1 - 2x}} \right\}$$

**2.975 ODE No. 975**

$$\frac{d}{dx}y(x) = (y(x))^3 + x^2(y(x))^2 + 1/3y(x)x^4 + 1/27x^6 - 2/3x = 0$$

**Mathematica:** cpu = 0.011501 (sec), leaf count = 47

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{\sqrt{c_1 - 2x}} - \frac{x^2}{3} \right\}, \left\{ y(x) \rightarrow \frac{1}{\sqrt{c_1 - 2x}} - \frac{x^2}{3} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 59

$$\left\{ y(x) = -\frac{1}{3} \left( x^2 \sqrt{-54\_C1 - 2x} - 3 \right) \frac{1}{\sqrt{-54\_C1 - 2x}}, y(x) = -\frac{1}{3} \left( x^2 \sqrt{-54\_C1 - 2x} + 3 \right) \frac{1}{\sqrt{-54\_C1 - 2x}} \right\}$$

**2.976 ODE No. 976**

$$\frac{d}{dx}y(x) = \frac{y(x) \left( (y(x))^2 x^7 + y(x)x^4 + x - 3 \right)}{x} = 0$$

**Mathematica:** cpu = 0.076010 (sec), leaf count = 101

$$\text{Solve} \left[ -\frac{7}{3} \text{RootSum} \left[ -7\#1^3 + 6\sqrt{-7}\#1 - 7\&, \frac{\log \left( \frac{3x^6y(x)+x^3}{\sqrt[3]{7}\sqrt[3]{-x^9}} - \#1 \right)}{2\sqrt[3]{-7} - 7\#1^2} \& \right] = c_1 + \frac{7^{2/3}(-x^9)^{2/3}}{9x^5}, y(x) \right]$$

**Maple:** cpu = 0.172 (sec), leaf count = 57

$$\left\{ y(x) = \frac{1}{2x^3} \left( \sqrt{3} \tan \left( \text{RootOf} \left( -\sqrt{3} \ln \left( \frac{9(\tan(_Z))^2 + 9}{7(-3 \tan(_Z) + \sqrt{3})^2} \right) + 3\sqrt{3\_C1} - 2\sqrt{3}x - 2\_Z \right) \right) \right) \right\}$$

**2.977 ODE No. 977**

$$\frac{d}{dx}y(x) = \frac{y(x) \left( (y(x))^2 + e^{-x^2} y(x) + (e^{-x^2})^2 \right) x}{(e^{-x^2})^2} = 0$$

**Mathematica:** cpu = 0.171522 (sec), leaf count = 139

$$\text{Solve} \left[ -\frac{25}{3} \text{RootSum} \left[ -25\#1^3 + 24\sqrt[3]{-15^{2/3}}\#1 - 25\&, \frac{\log \left( \frac{3e^{2x^2}xy(x)+e^{x^2}x}{5^{2/3}\sqrt[3]{-e^{3x^2}x^3}} - \#1 \right)}{8\sqrt[3]{-15^{2/3}} - 25\#1^2} \& \right] = c_1 - \frac{5\sqrt[3]{5}e^{x^2}x^3}{18\sqrt[3]{-e^{3x^2}x^3}} \right]$$

**Maple:** cpu = 0.141 (sec), leaf count = 122

$$\left\{ y(x) = \frac{1}{2e^{x^2}} \left( \sqrt{11} \tan \left( \text{RootOf} \left( -4\sqrt{11}x^2 + 8\sqrt{11} \ln \left( -\frac{36\sqrt{11}}{11} + 36 \tan(_Z) \right) \right) - 4\sqrt{11} \ln \left( \frac{2592}{\dots} \right) \right) \right.$$

**2.978 ODE No. 978**

$$\frac{d}{dx}y(x) = \frac{y(x) \left( (y(x))^2 + xy(x) + x^2 + x \right)}{x^2} = 0$$

**Mathematica:** cpu = 0.048006 (sec), leaf count = 60

$$\text{Solve} \left[ -\frac{1}{2} \log \left( \frac{y(x)^2}{x^2} + \frac{y(x)}{x} + 1 \right) + \log \left( \frac{y(x)}{x} \right) - \frac{\tan^{-1} \left( \frac{2y(x)+1}{\sqrt{3}} \right)}{\sqrt{3}} = c_1 + x, y(x) \right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 71

$$\left\{ y(x) = \frac{\sqrt{3}x}{2} \tan \left( \text{RootOf} \left( -\sqrt{3} \ln(3) - \sqrt{3} \ln \left( \frac{4}{3 + 3(\tan(_Z))^2} \right) \right) - 2\sqrt{3} \ln \left( -1/6\sqrt{3} + 1/2 \tan(_Z) \right) \right) \right.$$



**2.979 ODE No. 979**

$$\frac{d}{dx}y(x) = \frac{(y(x))^3 - 3x(y(x))^2 + 3x^2y(x) - x^3 + x}{x} = 0$$

**Mathematica:** cpu = 0.011001 (sec), leaf count = 37

$$\left\{ \left\{ y(x) \rightarrow x - \frac{1}{\sqrt{c_1 - 2 \log(x)}} \right\}, \left\{ y(x) \rightarrow \frac{1}{\sqrt{c_1 - 2 \log(x)}} + x \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 57

$$\left\{ y(x) = 1 \left( x \sqrt{2\_C1 - 2 \ln(x)} - 1 \right) \frac{1}{\sqrt{2\_C1 - 2 \ln(x)}}, y(x) = 1 \left( x \sqrt{2\_C1 - 2 \ln(x)} + 1 \right) \frac{1}{\sqrt{2\_C1 - 2 \ln(x)}} \right\}$$

**2.980 ODE No. 980**

$$\frac{d}{dx}y(x) = \frac{x^3(y(x))^3 + 6x^2(y(x))^2 + 12xy(x) + 8 + 2x}{x^3} = 0$$

**Mathematica:** cpu = 0.012002 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{\sqrt{c_1 - 2x}} - \frac{2}{x} \right\}, \left\{ y(x) \rightarrow \frac{1}{\sqrt{c_1 - 2x}} - \frac{2}{x} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 35

$$\left\{ y(x) = -\frac{1}{\sqrt{-C1 - 2x}} - 2x^{-1}, y(x) = \frac{1}{\sqrt{-C1 - 2x}} - 2x^{-1} \right\}$$

**2.981 ODE No. 981**

$$\frac{d}{dx}y(x) = \frac{(y(x))^3 a^3 x^3 + 3(y(x))^2 a^2 x^2 + 3axy(x) + 1 + a^2 x}{a^3 x^3} = 0$$

**Mathematica:** cpu = 0.017502 (sec), leaf count = 49

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{ax} - \frac{1}{\sqrt{c_1 - 2x}} \right\}, \left\{ y(x) \rightarrow \frac{1}{\sqrt{c_1 - 2x}} - \frac{1}{ax} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 41

$$\left\{ y(x) = -\frac{1}{\sqrt{-C1 - 2x}} - \frac{1}{ax}, y(x) = \frac{1}{\sqrt{-C1 - 2x}} - \frac{1}{ax} \right\}$$

**2.982 ODE No. 982**

$$\frac{d}{dx} y(x) = 1/2 \frac{y(x) \left( 2 (y(x))^2 + 2 y(x) e^{1/4 x^2} + 2 \left( e^{1/4 x^2} \right)^2 + x \left( e^{1/4 x^2} \right)^2 \right)}{\left( e^{1/4 x^2} \right)^2} = 0$$

**Mathematica:** cpu = 0.104513 (sec), leaf count = 132

$$\text{Solve} \left[ -\frac{7}{3} \text{RootSum} \left[ -7\#1^3 + 6\sqrt[3]{-7}\#1 - 7\&, \frac{\log \left( \frac{3e^{-\frac{x^2}{2}} y(x) + e^{-\frac{x^2}{4}}}{\sqrt[3]{7} \sqrt[3]{-e^{-\frac{3x^2}{4}}}} - \#1 \right)}{2\sqrt[3]{-7} - 7\#1^2} \& \right] = c_1 + \frac{1}{9} 7^{2/3} e^{\frac{x^2}{2}} \left( -e^{-\frac{3x^2}{4}} \right) \right]$$

**Maple:** cpu = 0.312 (sec), leaf count = 187

$$\left\{ -\frac{2}{3} \ln \left( 18 y(x) e^{-1/2 x^2} e^{1/4 x^2} + 6 e^{-1/4 x^2} e^{1/4 x^2} - 6 \right) + \frac{1}{3} \ln \left( \frac{324 (y(x))^2}{7} \left( e^{-\frac{x^2}{2}} \right)^2 \left( e^{\frac{x^2}{4}} \right)^2 + \frac{216 y(x)}{7} e^{-\frac{x^2}{2}} \right) \right\}$$

**2.983 ODE No. 983**

$$\frac{d}{dx} y(x) = \frac{(y(x))^3 - 3x(y(x))^2 + 3x^2 y(x) - x^3 + x^2}{(1+x)(x-1)} = 0$$

**Mathematica:** cpu = 0.255032 (sec), leaf count = 238

$$\text{Solve} \left[ \frac{1}{3} \log \left( \frac{\frac{3y(x)}{x^2-1} - \frac{3x}{x^2-1}}{3 \sqrt[3]{\frac{1}{(x-1)^3(x+1)^3}}} + 1 \right) - \frac{1}{6} \log \left( \frac{\left( \frac{3y(x)}{x^2-1} - \frac{3x}{x^2-1} \right)^2}{9 \left( \frac{1}{(x-1)^3(x+1)^3} \right)^{2/3}} - \frac{\frac{3y(x)}{x^2-1} - \frac{3x}{x^2-1}}{3 \sqrt[3]{\frac{1}{(x-1)^3(x+1)^3}}} + 1 \right) + \frac{\tan^{-1} \left( \frac{2 \left( \frac{3y(x)}{x^2-1} - \frac{3x}{x^2-1} \right)}{3 \sqrt[3]{\frac{1}{(x-1)^3(x+1)^3}}} \right)}{\sqrt{\frac{1}{(x-1)^3(x+1)^3}} \right]$$

**Maple:** cpu = 0.203 (sec), leaf count = 469

$$\left\{ y(x) = \frac{\sqrt{3}}{6} \left( \sqrt[3]{\frac{1}{(1+x)^3(x-1)^3}} \sqrt{3} x^2 + 3 \sqrt[3]{\frac{1}{(1+x)^3(x-1)^3}} \tan \left( \text{RootOf} \left( -18 \ln(1+x) \left( \frac{1}{(1+x)^3} \right) \right) \right) \right) \right\}$$

**2.984 ODE No. 984**

$$\frac{d}{dx}y(x) = \frac{y(x) (x^2(y(x))^2 + y(x) x e^x + (e^x)^2) (x - 1)}{x (e^x)^2} = 0$$

**Mathematica:** cpu = 3.039386 (sec), leaf count = 426

$$\text{Solve} \left[ -\frac{\sqrt[3]{2} \left( \frac{3e^{-2x} x(x-1)y(x)+e^{-x}(x-1)}{\sqrt[3]{2} \sqrt[3]{e^{-3x}(x-1)^3}} + 2^{2/3} \right) \left( 2^{2/3} - \frac{2^{2/3} (3e^{-2x} x(x-1)y(x)+e^{-x}(x-1))}{\sqrt[3]{e^{-3x}(x-1)^3}} \right)}{9 \left( -\frac{e^{3x} (3e^{-2x} x(x-1)y(x)+e^{-x}(x-1))}{(x-1)^3} \right)} \right]$$

**Maple:** cpu = 0.203 (sec), leaf count = 40

$$\left\{ y(x) = \frac{1}{9x} e^{\text{RootOf}\left(-e^{-Z} \ln\left(\frac{x(e^{-Z}+9)}{2}\right) + 3\_C1 e^{-Z} + \_Z e^{-Z} + x e^{-Z} + 9\right) + x} \right\}$$

**2.985 ODE No. 985**

$$\frac{d}{dx}y(x) = \frac{(xy(x) + 1) (x^2(y(x))^2 + x^2y(x) + 2xy(x) + 1 + x + x^2)}{x^5} = 0$$

**Mathematica:** cpu = 0.157520 (sec), leaf count = 103

$$\text{Solve} \left[ -\frac{17}{3} \text{RootSum} \left[ -17\#1^3 + 3\sqrt{-34}\#1 - 17\&, \frac{\log\left(\frac{\frac{x+3}{x^3} + \frac{3y(x)}{x^2}}{\sqrt[3]{34} \sqrt[3]{-\frac{1}{x^6}}} - \#1\right)}{\sqrt{-34} - 17\#1^2} \& \right] = c_1 - \frac{1}{9} 34^{2/3} \left( -\frac{1}{x^6} \right)^{2/3} \right]$$

**Maple:** cpu = 0.031 (sec), leaf count = 43

$$\left\{ y(x) = \frac{17 \text{RootOf}\left(162 \int^{-Z} (289\_a^3 + 54\_a - 54)^{-1} d\_ax + 3x\_C1 + 2\right) x - 3x - 9}{9x} \right\}$$

**2.986 ODE No. 986**

$$\frac{d}{dx}y(x) = \frac{(y(x))^3 - 3x(y(x))^2 \ln(x) + 3x^2(\ln(x))^2 y(x) - x^3(\ln(x))^3 + x^2 + xy(x)}{x^2} = 0$$

**Mathematica:** cpu = 0.014502 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow x \log(x) - \frac{x}{\sqrt{c_1 - 2x}} \right\}, \left\{ y(x) \rightarrow \frac{x}{\sqrt{c_1 - 2x}} + x \log(x) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 36

$$\left\{ y(x) = -x \frac{1}{\sqrt{-C1 - 2x}} + x \ln(x), y(x) = x \frac{1}{\sqrt{-C1 - 2x}} + x \ln(x) \right\}$$

**2.987 ODE No. 987**

$$\frac{d}{dx}y(x) = -F(x) (-ax^2 + (y(x))^2) + \frac{y(x)}{x} = 0$$

**Mathematica:** cpu = 0.099513 (sec), leaf count = 40

$$\left\{ \left\{ y(x) \rightarrow \sqrt{ax} \tanh \left( \sqrt{a} \int_1^x K[1] F(K[1]) dK[1] + \sqrt{ac_1} \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 26

$$\left\{ y(x) = \tanh \left( \int F(x) x dx \sqrt{a} + \_C1 \sqrt{a} \right) x \sqrt{a} \right\}$$

**2.988 ODE No. 988**

$$\frac{d}{dx}y(x) = -F(x) (-x^2 - 2xy(x) + (y(x))^2) + \frac{y(x)}{x} = 0$$

**Mathematica:** cpu = 0.365546 (sec), leaf count = 104

$$\left\{ \left\{ y(x) \rightarrow -\frac{x(-\exp(2\sqrt{2}(\int_1^x K[1](-F(K[1])) dK[1] + c_1)) + \sqrt{2} \exp(2\sqrt{2}(\int_1^x K[1](-F(K[1])) dK[1] + c_1))}{\exp(2\sqrt{2}(\int_1^x K[1](-F(K[1])) dK[1] + c_1)) + 1} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 29

$$\left\{ y(x) = \frac{x(\sqrt{2} + 2 \tanh((\int F(x) x dx + \_C1) \sqrt{2})) \sqrt{2}}{2} \right\}$$

**2.989 ODE No. 989**

$$\frac{d}{dx}y(x) = -F(x) (-a(y(x))^2 - bx^2) + \frac{y(x)}{x} = 0$$

**Mathematica:** cpu = 0.103513 (sec), leaf count = 55

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt{bx} \tan \left( \sqrt{a}\sqrt{b} \int_1^x K[1]F(K[1]) dK[1] + \sqrt{a}\sqrt{bc_1} \right)}{\sqrt{a}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 35

$$\left\{ y(x) = \frac{x}{a} \tan \left( \int F(x) x dx \sqrt{ab} + \_C1 \sqrt{ab} \right) \sqrt{ab} \right\}$$

**2.990 ODE No. 990**

$$\frac{d}{dx}y(x) = -F(x) (-(y(x))^2 + 2x^2y(x) + 1 - x^4) + 2x = 0$$

**Mathematica:** cpu = 0.474060 (sec), leaf count = 49

$$\left\{ \left\{ y(x) \rightarrow \frac{e^{\int_1^x 2F(K[5]) dK[5]}}{c_1 - \frac{1}{2} e^{\text{Integrate}[2F(K[5]),\{K[5],1,x\},\text{Assumptions}\rightarrow\text{True}]}} + x^2 + 1 \right\} \right\}$$

**Maple:** cpu = 0.359 (sec), leaf count = 46

$$\left\{ y(x) = 1 \left( \frac{-C1 x^2}{(e^{\int F(x) dx})^2} - x^2 + \frac{-C1}{(e^{\int F(x) dx})^2} + 1 \right) \left( \frac{-C1}{(e^{\int F(x) dx})^2} - 1 \right)^{-1} \right\}$$

**2.991 ODE No. 991**

$$\frac{d}{dx}y(x) = -F(x) (x^2 + 2xy(x) - (y(x))^2) + \frac{y(x)}{x} = 0$$

**Mathematica:** cpu = 0.306539 (sec), leaf count = 101

$$\left\{ \left\{ y(x) \rightarrow -\frac{x(-\exp(2\sqrt{2}(\int_1^x K[1]F(K[1]) dK[1] + c_1)) + \sqrt{2} \exp(2\sqrt{2}(\int_1^x K[1]F(K[1]) dK[1] + c_1)))}{\exp(2\sqrt{2}(\int_1^x K[1]F(K[1]) dK[1] + c_1)) + 1} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 31

$$\left\{ y(x) = -\frac{x(-\sqrt{2} + 2 \tanh((\int F(x) x dx + \_C1) \sqrt{2})) \sqrt{2}}{2} \right\}$$

**2.992 ODE No. 992**

$$\frac{d}{dx}y(x) = -F(x) (-7x(y(x))^2 - x^3) + \frac{y(x)}{x} = 0$$

**Mathematica:** cpu = 0.106513 (sec), leaf count = 42

$$\left\{ \left\{ y(x) \rightarrow \frac{x \tan(\sqrt{7} \int_1^x K[1]^2 F(K[1]) dK[1] + \sqrt{7}c_1)}{\sqrt{7}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 25

$$\left\{ y(x) = \frac{\tan\left(\left(\int_1^x F(x) x^2 dx + \_C1\right) \sqrt{7}\right) x \sqrt{7}}{7} \right\}$$

**2.993 ODE No. 993**

$$\frac{d}{dx}y(x) = -F(x) (-(y(x))^2 - 2y(x) \ln(x) - (\ln(x))^2) + \frac{y(x)}{x \ln(x)} = 0$$

**Mathematica:** cpu = 5232.495943 (sec), leaf count = 71

$$\left\{ \left\{ y(x) \rightarrow \frac{\int_1^x \frac{F(K[5])}{\sqrt{\frac{1}{\log^2(K[5])}}} dK[5] + c_1 - 1}{\sqrt{\frac{1}{\log^2(x)} \left( \int_1^x \frac{F(K[5])}{\sqrt{\frac{1}{\log^2(K[5])}}} dK[5] \right) + c_1 \sqrt{\frac{1}{\log^2(x)}}} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 35

$$\left\{ y(x) = -\frac{\ln(x) \left( \int -2 \ln(x) F(x) dx - \_C1 - 2 \right)}{\int -2 \ln(x) F(x) dx - \_C1} \right\}$$

**2.994 ODE No. 994**

$$\frac{d}{dx}y(x) = -x^3 (-(y(x))^2 - 2y(x) \ln(x) - (\ln(x))^2) + \frac{y(x)}{x \ln(x)} = 0$$

**Mathematica:** cpu = 0.122515 (sec), leaf count = 198

$$\left\{ \left\{ y(x) \rightarrow -\frac{c_1 e^{\frac{1}{16}x^4(4\log(x)-1)} \left( \frac{x^3}{4} + \frac{1}{4}x^3(4\log(x)-1) \right) + \frac{1}{16}x^4 e^{\frac{1}{16}x^4(4\log(x)-1)} (4\log(x)-1) \left( \frac{x^3}{4} + \frac{1}{4}x^3(4\log(x)-1) \right)}{x^3 \left( c_1 e^{\frac{1}{16}x^4(4\log(x)-1)} + \frac{1}{16}x^4 e^{\frac{1}{16}x^4(4\log(x)-1)} \right)} \right\} \right\}$$

Maple: cpu = 0.031 (sec), leaf count = 43

$$\left\{ y(x) = -\frac{\ln(x)(4x^4 \ln(x) - x^4 + 8\_C1 + 16)}{4x^4 \ln(x) - x^4 + 8\_C1} \right\}$$

## 2.995 ODE No. 995

$$\frac{d}{dx}y(x) = (y(x) - e^x)^2 + e^x = 0$$

Mathematica: cpu = 0.017002 (sec), leaf count = 17

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{c_1 - x} + e^x \right\} \right\}$$

Maple: cpu = 0.094 (sec), leaf count = 14

$$\{y(x) = e^x + (\_C1 - x)^{-1}\}$$

## 2.996 ODE No. 996

$$\frac{d}{dx}y(x) = \frac{(y(x) - Si(x))^2 + \sin(x)}{x} = 0$$

Mathematica: cpu = 56.731204 (sec), leaf count = 25

$$\text{DSolve}\left[y'(x) = \frac{(y(x) - \text{Si}(x))^2 + \sin(x)}{x}, y(x), x\right]$$

Maple: cpu = 0.047 (sec), leaf count = 15

$$\{y(x) = Si(x) + (\_C1 - \ln(x))^{-1}\}$$

## 2.997 ODE No. 997

$$\frac{d}{dx}y(x) = (y(x) + \cos(x))^2 + \sin(x) = 0$$

Mathematica: cpu = 0.029004 (sec), leaf count = 18

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{c_1 - x} - \cos(x) \right\} \right\}$$

Maple: cpu = 0.047 (sec), leaf count = 16

$$\{y(x) = -\cos(x) + (\_C1 - x)^{-1}\}$$

**2.998 ODE No. 998**

$$\frac{d}{dx}y(x) = \frac{(y(x) - \ln(x) - Ci(x))^2 + \cos(x)}{x} = 0$$

**Mathematica:** cpu = 0.472560 (sec), leaf count = 27

$$\left\{ \left\{ y(x) \rightarrow \frac{x^2}{c_1 - \frac{x^2}{2}} + Ci(x) + \log(x) + 1 \right\} \right\}$$

**Maple:** cpu = 0.281 (sec), leaf count = 27

$$\left\{ y(x) = \ln(x) + Ci(x) + \frac{-C1 x^2 + 1}{-C1 x^2 + 1} \right\}$$

**2.999 ODE No. 999**

$$\frac{d}{dx}y(x) = \frac{(y(x) - x + \ln(1+x))^2 + x}{1+x} = 0$$

**Mathematica:** cpu = 0.023503 (sec), leaf count = 24

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{c_1 - \log(x+1)} + x - \log(x+1) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 39

$$\left\{ y(x) = -\frac{(\ln(1+x))^2 + C1 \ln(1+x) - x \ln(1+x) - x C1 + 1}{\ln(1+x) + C1} \right\}$$

**2.1000 ODE No. 1000**

$$\frac{d}{dx}y(x) = \frac{2x^2y(x) + x^3 + y(x) \ln(x)x - (y(x))^2 - xy(x)}{x^2(x + \ln(x))} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.109 (sec), leaf count = 19

$$\left\{ y(x) = \frac{x(x - C1 - 1)}{-C1 \ln(x) + 1} \right\}$$



### 3 Kamke chapter 2. Linear second order

#### 3.1 ODE No. 1001

$$\frac{d^2}{dx^2}y(x) = 0$$

**Mathematica:** cpu = 0.003000 (sec), leaf count = 12

$$\{y(x) \rightarrow c_2x + c_1\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 9

$$\{y(x) = x\_C1 + \_C2\}$$

#### 3.2 ODE No. 1002

$$\frac{d^2}{dx^2}y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.004000 (sec), leaf count = 16

$$\{y(x) \rightarrow c_2 \sin(x) + c_1 \cos(x)\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 13

$$\{y(x) = \_C1 \sin(x) + \_C2 \cos(x)\}$$

#### 3.3 ODE No. 1003

$$\frac{d^2}{dx^2}y(x) + y(x) - \sin(nx) = 0$$

**Mathematica:** cpu = 0.115515 (sec), leaf count = 45

$$\left\{ \left\{ y(x) \rightarrow c_2 \sin(x) + c_1 \cos(x) + \frac{\cos^2(x)(-\sin(nx)) - \sin^2(x) \sin(nx)}{n^2 - 1} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 26

$$\left\{ y(x) = \sin(x) \_C2 + \cos(x) \_C1 - \frac{\sin(nx)}{n^2 - 1} \right\}$$

### 3.4 ODE No. 1004

$$\frac{d^2}{dx^2}y(x) + y(x) - a \cos(bx) = 0$$

**Mathematica:** cpu = 0.097012 (sec), leaf count = 47

$$\left\{ \left\{ y(x) \rightarrow \frac{-a \cos^2(x) \cos(bx) - a \sin^2(x) \cos(bx)}{b^2 - 1} + c_2 \sin(x) + c_1 \cos(x) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 27

$$\left\{ y(x) = \sin(x) \_C2 + \cos(x) \_C1 - \frac{a \cos(bx)}{b^2 - 1} \right\}$$

### 3.5 ODE No. 1005

$$\frac{d^2}{dx^2}y(x) + y(x) - \sin(ax) \sin(bx) = 0$$

**Mathematica:** cpu = 0.532068 (sec), leaf count = 1163

$$\left\{ \left\{ y(x) \rightarrow c_1 \cos(x) + c_2 \sin(x) + \frac{-\cos(x) \cos((a-b-1)x)a^3 + \cos(x) \cos((a-b+1)x)a^3 + \cos(x) \cos((a+b-1)x)a^3 + \cos(x) \cos((a+b+1)x)a^3}{2a^4 + (-4b^2 - 4)a^2 + 2b^4 - 4b^2 + 2} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 82

$$\left\{ y(x) = \sin(x) \_C2 + \cos(x) \_C1 + \frac{-(a+b+1)(a+b-1) \cos(x(a-b)) + \cos((a+b)x)(a-b+1) + \cos((a-b)x)(a+b+1) - (a+b-1)(a+b+1) \cos(x(a-b))}{2a^4 + (-4b^2 - 4)a^2 + 2b^4 - 4b^2 + 2} \right\}$$

### 3.6 ODE No. 1006

$$\frac{d^2}{dx^2}y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.003501 (sec), leaf count = 20

$$\left\{ \left\{ y(x) \rightarrow c_1 e^x + c_2 e^{-x} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 15

$$\left\{ y(x) = \_C1 e^{-x} + \_C2 e^x \right\}$$

### 3.7 ODE No. 1007

$$\frac{d^2}{dx^2}y(x) - 2y(x) - 4x^2e^{x^2} = 0$$

**Mathematica:** cpu = 0.057007 (sec), leaf count = 135

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\sqrt{2}x} + c_2 e^{-\sqrt{2}x} + \frac{e^{-\sqrt{2}x} \left( -2e^{x(x+\sqrt{2})} x + 2e^{(x-\sqrt{2})x+2\sqrt{2}x} x + \sqrt{2}e^{x(x+\sqrt{2})} + \sqrt{2}e^{(x-\sqrt{2})x+2\sqrt{2}x} \right)}{2\sqrt{2}} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 26

$$\left\{ y(x) = e^{x\sqrt{2}} \_C2 + e^{-x\sqrt{2}} \_C1 + e^{x^2} \right\}$$

### 3.8 ODE No. 1008

$$\frac{d^2}{dx^2}y(x) + a^2y(x) - \cot(ax) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.032 (sec), leaf count = 39

$$\left\{ y(x) = \sin(ax) \_C2 + \cos(ax) \_C1 + \frac{\sin(ax)}{a^2} \ln \left( \frac{\sin(ax)}{\cos(ax) + 1} \right) \right\}$$

### 3.9 ODE No. 1009

$$\frac{d^2}{dx^2}y(x) + ly(x) = 0$$

**Mathematica:** cpu = 0.004001 (sec), leaf count = 28

$$\left\{ \left\{ y(x) \rightarrow c_2 \sin(\sqrt{l}x) + c_1 \cos(\sqrt{l}x) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 21

$$\left\{ y(x) = \_C1 \sin(\sqrt{l}x) + \_C2 \cos(\sqrt{l}x) \right\}$$

### 3.10 ODE No. 1010

$$\frac{d^2}{dx^2}y(x) + (ax + b)y(x) = 0$$

**Mathematica:** cpu = 0.006001 (sec), leaf count = 46

$$\left\{ \left\{ y(x) \rightarrow c_1 \text{Ai} \left( \frac{-b - ax}{(-a)^{2/3}} \right) + c_2 \text{Bi} \left( \frac{-b - ax}{(-a)^{2/3}} \right) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 31

$$\left\{ y(x) = \_C1 \text{Ai} \left( -(ax + b)a^{-\frac{2}{3}} \right) + \_C2 \text{Bi} \left( -(ax + b)a^{-\frac{2}{3}} \right) \right\}$$

### 3.11 ODE No. 1011

$$\frac{d^2}{dx^2}y(x) - (x^2 + 1)y(x) = 0$$

**Mathematica:** cpu = 0.006001 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow c_1 D_{-1}(\sqrt{2}x) + c_2 D_0(i\sqrt{2}x) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 23

$$\left\{ y(x) = \_C1 e^{\frac{x^2}{2}} + \_C2 e^{\frac{x^2}{2}} \text{Erf}(x) \right\}$$

### 3.12 ODE No. 1012

$$\frac{d^2}{dx^2}y(x) - (x^2 + a)y(x) = 0$$

**Mathematica:** cpu = 0.007501 (sec), leaf count = 47

$$\left\{ \left\{ y(x) \rightarrow c_1 D_{\frac{1}{2}(-a-1)}(\sqrt{2}x) + c_2 D_{\frac{a-1}{2}}(i\sqrt{2}x) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 31

$$\left\{ y(x) = \_C1 M_{-\frac{a}{4}, \frac{1}{4}}(x^2) \frac{1}{\sqrt{x}} + \_C2 W_{-\frac{a}{4}, \frac{1}{4}}(x^2) \frac{1}{\sqrt{x}} \right\}$$

### 3.13 ODE No. 1013

$$\frac{d^2}{dx^2}y(x) - (a^2x^2 + a)y(x) = 0$$

**Mathematica:** cpu = 0.019502 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow c_1 D_{-1}(\sqrt{2}\sqrt{ax}) + c_2 D_0(i\sqrt{2}\sqrt{ax}) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 29

$$\left\{ y(x) = \_C1 e^{\frac{ax^2}{2}} + \_C2 e^{\frac{ax^2}{2}} \operatorname{Erf}(\sqrt{ax}) \right\}$$

### 3.14 ODE No. 1014

$$\frac{d^2}{dx^2}y(x) - cx^a y(x) = 0$$

**Mathematica:** cpu = 0.029004 (sec), leaf count = 170

$$\left\{ \left\{ y(x) \rightarrow (a+2)^{-\frac{1}{a+2}} c_1 c^{\frac{1}{2(a+2)}} x^{\frac{a+1}{a+2}} \Gamma\left(1 - \frac{1}{a+2}\right) I_{-\frac{1}{a+2}}\left(\frac{2\sqrt{cx}^{\frac{a+2}{2}}}{a+2}\right) + (-1)^{\frac{1}{a+2}} (a+2)^{-\frac{1}{a+2}} c_2 c^{\frac{1}{2(a+2)}} x^{1-\frac{1}{a+2}} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 65

$$\left\{ y(x) = \_C1 \sqrt{x} J_{(a+2)^{-1}}\left(2 \frac{\sqrt{-cx}^{a/2+1}}{a+2}\right) + \_C2 \sqrt{x} Y_{(a+2)^{-1}}\left(2 \frac{\sqrt{-cx}^{a/2+1}}{a+2}\right) \right\}$$

### 3.15 ODE No. 1015

$$\frac{d^2}{dx^2}y(x) - (a^2x^{2n} - 1)y(x) = 0$$

**Mathematica:** cpu = 0.344544 (sec), leaf count = 26

$$\text{DSolve}[y(x) (1 - a^2 x^{2n}) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.156 (sec), leaf count = 31

$$\left\{ y(x) = \text{DESol}\left(\left\{\frac{d^2}{dx^2} \_Y(x) + (-a^2 x^{2n} + 1) \_Y(x)\right\}, \{\_Y(x)\}\right) \right\}$$

### 3.16 ODE No. 1016

$$\frac{d^2}{dx^2}y(x) + (ax^{2c} + bx^{c-1})y(x) = 0$$

**Mathematica:** cpu = 0.126016 (sec), leaf count = 312

$$\left\{ \left\{ y(x) \rightarrow 2^{\frac{c}{2(c+1)}} c_1 (x^{c+1})^{\frac{c}{2(c+1)}} x^{-c/2} e^{-\frac{\sqrt{ax}^{c+1}}{\sqrt{-c^2-2c-1}}} U \left( \frac{\frac{\sqrt{acb}}{\sqrt{-(c+1)^2}} + \frac{\sqrt{ab}}{\sqrt{-(c+1)^2}} + ac}{2(ca+a)}, \frac{c}{c+1}, \frac{2\sqrt{ax}^{c+1}}{\sqrt{-c^2-2c-1}} \right) \right\} \right\}$$

**Maple:** cpu = 0.141 (sec), leaf count = 95

$$\left\{ y(x) = \_C1 x^{-\frac{c}{2}} M_{\frac{-ib}{2c+2}, \frac{1}{\sqrt{a}}, (2c+2)^{-1}} \left( \frac{2ix^{c+1}}{c+1} \sqrt{a} \right) + \_C2 x^{-\frac{c}{2}} W_{\frac{-ib}{2c+2}, \frac{1}{\sqrt{a}}, (2c+2)^{-1}} \left( \frac{2ix^{c+1}}{c+1} \sqrt{a} \right) \right\}$$

### 3.17 ODE No. 1017

$$\frac{d^2}{dx^2}y(x) + (e^{2x} - v^2)y(x) = 0$$

**Mathematica:** cpu = 0.027504 (sec), leaf count = 46

$$\left\{ \left\{ y(x) \rightarrow c_1 \Gamma(1-v) J_{-v}(\sqrt{e^{2x}}) + c_2 \Gamma(v+1) J_v(\sqrt{e^{2x}}) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 17

$$\{y(x) = \_C1 J_v(e^x) + \_C2 Y_v(e^x)\}$$

### 3.18 ODE No. 1018

$$\frac{d^2}{dx^2}y(x) + ae^{bx}y(x) = 0$$

**Mathematica:** cpu = 0.021503 (sec), leaf count = 55

$$\left\{ \left\{ y(x) \rightarrow c_1 J_0 \left( \frac{2\sqrt{a}\sqrt{e^{bx}}}{b} \right) + 2c_2 Y_0 \left( \frac{2\sqrt{a}\sqrt{e^{bx}}}{b} \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 39

$$\left\{ y(x) = \_C1 J_0 \left( 2 \frac{\sqrt{ae^{1/2bx}}}{b} \right) + \_C2 Y_0 \left( 2 \frac{\sqrt{ae^{1/2bx}}}{b} \right) \right\}$$

### 3.19 ODE No. 1019

$$\frac{d^2}{dx^2}y(x) - (4a^2b^2x^2e^{2bx^2} - 1)y(x) = 0$$

**Mathematica:** cpu = 0.780099 (sec), leaf count = 35

$$\text{DSolve}\left[y(x)\left(1 - 4a^2b^2x^2e^{2bx^2}\right) + y''(x) = 0, y(x), x\right]$$

**Maple:** cpu = 0.531 (sec), leaf count = 39

$$\left\{y(x) = \text{DESol}\left(\left\{\frac{d^2}{dx^2}Y(x) + (-4a^2b^2x^2e^{2bx^2} + 1)Y(x)\right\}, \{Y(x)\}\right)\right\}$$

### 3.20 ODE No. 1020

$$\frac{d^2}{dx^2}y(x) + (ae^{2x} + be^x + c)y(x) = 0$$

**Mathematica:** cpu = 0.680586 (sec), leaf count = 180

$$\left\{\left\{y(x) \rightarrow c_1 e^{i(\sqrt{c}\log(e^x) - \sqrt{a}e^x)} U\left(\frac{i(b - i\sqrt{a} + 2\sqrt{a}\sqrt{c})}{2\sqrt{a}}, 2i\sqrt{c} + 1, 2i\sqrt{a}e^x\right) + c_2 e^{i(\sqrt{c}\log(e^x) - \sqrt{a}e^x)} L_{-\frac{i(2\sqrt{a}\sqrt{c})}{2\sqrt{a}}}\right\}\right\}$$

**Maple:** cpu = 0.141 (sec), leaf count = 61

$$\left\{y(x) = \_C1 e^{-\frac{x}{2}} M_{-\frac{i}{2}b\frac{1}{\sqrt{a}}, i\sqrt{c}}(2i\sqrt{a}e^x) + \_C2 e^{-\frac{x}{2}} W_{-\frac{i}{2}b\frac{1}{\sqrt{a}}, i\sqrt{c}}(2i\sqrt{a}e^x)\right\}$$

### 3.21 ODE No. 1021

$$\frac{d^2}{dx^2}y(x) + (a(\cosh(x))^2 + b)y(x) = 0$$

**Mathematica:** cpu = 0.053507 (sec), leaf count = 44

$$\left\{\left\{y(x) \rightarrow c_1 \text{MathieuC}\left[\frac{1}{2}(a + 2b), -\frac{a}{4}, x\right] + c_2 \text{MathieuS}\left[\frac{1}{2}(a + 2b), -\frac{a}{4}, x\right]\right\}\right\}$$

**Maple:** cpu = 0.140 (sec), leaf count = 39

$$\left\{y(x) = \_C1 \text{MathieuC}\left(-\frac{a}{2} - b, \frac{a}{4}, ix\right) + \_C2 \text{MathieuS}\left(-\frac{a}{2} - b, \frac{a}{4}, ix\right)\right\}$$

### 3.22 ODE No. 1022

$$\frac{d^2}{dx^2}y(x) + (a \cos(2x) + b)y(x) = 0$$

**Mathematica:** cpu = 0.027003 (sec), leaf count = 28

$$\left\{ \left\{ y(x) \rightarrow c_1 \text{MathieuC}\left[b, -\frac{a}{2}, x\right] + c_2 \text{MathieuS}\left[b, -\frac{a}{2}, x\right] \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 21

$$\left\{ y(x) = \_C1 \text{MathieuC}\left(b, -\frac{a}{2}, x\right) + \_C2 \text{MathieuS}\left(b, -\frac{a}{2}, x\right) \right\}$$

### 3.23 ODE No. 1023

$$\frac{d^2}{dx^2}y(x) + (a(\cos(x))^2 + b)y(x) = 0$$

**Mathematica:** cpu = 0.014502 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow c_1 \text{MathieuC}\left[\frac{1}{2}(a+2b), -\frac{a}{4}, x\right] + c_2 \text{MathieuS}\left[\frac{1}{2}(a+2b), -\frac{a}{4}, x\right] \right\} \right\}$$

**Maple:** cpu = 0.141 (sec), leaf count = 29

$$\left\{ y(x) = \_C1 \text{MathieuC}\left(\frac{a}{2} + b, -\frac{a}{4}, x\right) + \_C2 \text{MathieuS}\left(\frac{a}{2} + b, -\frac{a}{4}, x\right) \right\}$$

### 3.24 ODE No. 1024

$$\frac{d^2}{dx^2}y(x) - (1 + 2(\tan(x))^2)y(x) = 0$$

**Mathematica:** cpu = 0.162021 (sec), leaf count = 84

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 \sqrt[4]{1 - \cos^2(x)} \sec(x)}{\sqrt[4]{\cos^2(x) - 1}} - \frac{c_2 \sqrt[4]{1 - \cos^2(x)} \sec(x) \left( \cos(x) \sqrt{1 - \cos^2(x)} - \sin^{-1}(\cos(x)) \right)}{2 \sqrt[4]{\cos^2(x) - 1}} \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 34

$$\left\{ y(x) = \frac{\_C1}{\cos(x)} + \frac{\_C2 (i \cos(x) \sin(x) + \ln(\cos(x) + i \sin(x)))}{\cos(x)} \right\}$$



### 3.25 ODE No. 1025

$$\frac{d^2}{dx^2}y(x) - \left( \frac{m(m-1)}{(\cos(x))^2} + \frac{n(n-1)}{(\sin(x))^2} + a \right) y(x) = 0$$

**Mathematica:** cpu = 0.954121 (sec), leaf count = 615

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 (-1)^{\frac{1}{2}(-2m-1)+1} \cos^2(x)^{\frac{1}{4}(-2m-1)+1} (\cos^2(x) - 1)^{\frac{1}{2} \left( \frac{4am+4\sqrt{-a}n^2+4an-4\sqrt{-a}n+4(-a)^{3/2}+8\sqrt{-a}a+\sqrt{-a}+4mn}{8a+8n^2-8n+2} \right)}}{c_1} \right. \right.$$

**Maple:** cpu = 0.140 (sec), leaf count = 105

$$\left\{ y(x) = \_C1 (\cos(x))^m (\sin(x))^n {}_2F_1\left(\frac{n}{2} + \frac{m}{2} + \frac{i}{2}\sqrt{a}, \frac{n}{2} + \frac{m}{2} - \frac{i}{2}\sqrt{a}; \frac{1}{2} + m; (\cos(x))^2\right) + \_C2 (\cos(x))^m (\sin(x))^n {}_2F_1\left(\frac{n}{2} + \frac{m}{2} - \frac{i}{2}\sqrt{a}, \frac{n}{2} + \frac{m}{2} + \frac{i}{2}\sqrt{a}; \frac{1}{2} + m; (\cos(x))^2\right) \right.$$

### 3.26 ODE No. 1026

$$\frac{d^2}{dx^2}y(x) - (n(n+1) \text{WeierstrassP}(x, g2, g3) + B) y(x) = 0$$

**Mathematica:** cpu = 0.184023 (sec), leaf count = 27

$$\text{DSolve}[y''(x) - y(x)(B + n(n+1)\wp(x; g2, g3)) = 0, y(x), x]$$

**Maple:** cpu = 0.280 (sec), leaf count = 33

$$\left\{ y(x) = \text{DESol}\left(\left\{ \frac{d^2}{dx^2} \_Y(x) + (-n(n+1) \text{WeierstrassP}(x, g2, g3) - B) \_Y(x) \right\}, \{\_Y(x)\} \right) \right.$$

### 3.27 ODE No. 1027

$$\frac{d^2}{dx^2}y(x) - (n(n+1)k^2(\text{JacobiSN}(x, k))^2 + b) y(x) = 0$$

**Mathematica:** cpu = 0.995126 (sec), leaf count = 23

$$\text{DSolve}[y(x) (asn(x|k)^2 + b) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.265 (sec), leaf count = 69

$$\left\{ y(x) = \_C1 \text{HeunG}\left(k^{-2}, \frac{b}{4k^2}, -\frac{n}{2}, \frac{n}{2} + \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, (\text{JacobiSN}(x, k))^2\right) + \_C2 \text{HeunG}\left(k^{-2}, \frac{k^2 + b + 1}{4k^2}, -\frac{n}{2}, \frac{n}{2} + \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, (\text{JacobiSN}(x, k))^2\right) \right.$$

### 3.28 ODE No. 1028

$$\frac{d^2}{dx^2}y(x) - \left(1/30 \frac{d^4}{dx^4}p(x) + 7/3 \frac{d^2}{dx^2}p(x) + ap(x) + b\right) y(x) = 0$$

**Mathematica:** cpu = 0.258033 (sec), leaf count = 37

$$\text{DSolve}\left[y''(x) - y(x) \left(ap(x) + b + \frac{p^4(x)}{30} + \frac{7p''(x)}{3}\right) = 0, y(x), x\right]$$

**Maple:** cpu = 0.172 (sec), leaf count = 48

$$\left\{y(x) = \text{DESol}\left(\left\{\frac{d^2}{dx^2}Y(x) + \left(-\frac{\frac{d^4}{dx^4}p(x)}{30} - \frac{7\frac{d^2}{dx^2}p(x)}{3} - ap(x) - b\right)Y(x)\right\}, \{-Y(x)\}\right)\right\}$$

### 3.29 ODE No. 1029

$$\frac{d^2}{dx^2}y(x) - \left((f(x))^2 + \frac{d}{dx}f(x)\right) y(x) = 0$$

**Mathematica:** cpu = 0.177022 (sec), leaf count = 24

$$\text{DSolve}[y''(x) - y(x) (f'(x) + f(x)^2) = 0, y(x), x]$$

**Maple:** cpu = 0.125 (sec), leaf count = 22

$$\left\{y(x) = \left(\int e^{\int -2f(x) dx} dx + \_C1\right) e^{\int f(x) dx} \_C2\right\}$$

### 3.30 ODE No. 1030

$$\frac{d^2}{dx^2}y(x) + (P(x) + l) y(x) = 0$$

**Mathematica:** cpu = 0.157020 (sec), leaf count = 18

$$\text{DSolve}[y(x)(l + P(x)) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.0 (sec), leaf count = 23

$$\left\{y(x) = \text{DESol}\left(\left\{(P(x) + l)Y(x) + \frac{d^2}{dx^2}Y(x)\right\}, \{-Y(x)\}\right)\right\}$$

### 3.31 ODE No. 1031

$$\frac{d^2}{dx^2}y(x) - f(x)y(x) = 0$$

**Mathematica:** cpu = 0.126516 (sec), leaf count = 17

$$\text{DSolve}[y''(x) - f(x)y(x) = 0, y(x), x]$$

**Maple:** cpu = 0.0 (sec), leaf count = 22

$$\left\{ y(x) = \text{DESol} \left( \left\{ -f(x) \_Y(x) + \frac{d^2}{dx^2} \_Y(x) \right\}, \{ \_Y(x) \} \right) \right\}$$

### 3.32 ODE No. 1032

$$\frac{d^2}{dx^2}y(x) + \left( 1/2 \frac{\frac{d^3}{dx^3}g(x)}{\frac{d}{dx}g(x)} - 3/4 \frac{\left(\frac{d^2}{dx^2}g(x)\right)^2}{\left(\frac{d}{dx}g(x)\right)^2} + \frac{(1/4 - v^2) \left(\frac{d}{dx}g(x)\right)^2}{g(x)} + \left(\frac{d}{dx}g(x)\right)^2 \right) y(x) = 0$$

**Mathematica:** cpu = 0.478061 (sec), leaf count = 71

$$\text{DSolve} \left[ y(x) \left( \frac{\left(\frac{1}{4} - v^2\right) g'(x)^2}{g(x)} + g'(x)^2 + \frac{g^3(x)}{2g'(x)} - \frac{3g''(x)^2}{4g'(x)^2} \right) + y''(x) = 0, y(x), x \right]$$

**Maple:** cpu = 0.156 (sec), leaf count = 53

$$\left\{ y(x) = \_C1 M_{\frac{i}{2}v^2 - \frac{i}{8}, \frac{1}{2}}(2ig(x)) \frac{1}{\sqrt{\frac{d}{dx}g(x)}} + \_C2 W_{\frac{i}{2}v^2 - \frac{i}{8}, \frac{1}{2}}(2ig(x)) \frac{1}{\sqrt{\frac{d}{dx}g(x)}} \right\}$$

### 3.33 ODE No. 1033

$$\frac{d^2}{dx^2}y(x) + \frac{d}{dx}y(x) + ae^{-2x}y(x) = 0$$

**Mathematica:** cpu = 0.016502 (sec), leaf count = 37

$$\left\{ \left\{ y(x) \rightarrow c_1 \cos(\sqrt{ae^{-x}}) - c_2 \sin(\sqrt{ae^{-x}}) \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 27

$$\left\{ y(x) = \_C1 \sin(e^{-x}\sqrt{a}) + \_C2 \cos(e^{-x}\sqrt{a}) \right\}$$

### 3.34 ODE No. 1034

$$\frac{d^2}{dx^2}y(x) - \frac{d}{dx}y(x) + e^{2x}y(x) = 0$$

**Mathematica:** cpu = 0.011001 (sec), leaf count = 20

$$\{ \{ y(x) \rightarrow c_2 \sin(e^x) + c_1 \cos(e^x) \} \}$$

**Maple:** cpu = 0.015 (sec), leaf count = 15

$$\{ y(x) = \_C1 \sin(e^x) + \_C2 \cos(e^x) \}$$

### 3.35 ODE No. 1035

$$\frac{d^2}{dx^2}y(x) + a \frac{d}{dx}y(x) + by(x) = 0$$

**Mathematica:** cpu = 0.004501 (sec), leaf count = 58

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{1}{2}x(-\sqrt{a^2-4b}-a)} + c_2 e^{\frac{1}{2}x(\sqrt{a^2-4b}-a)} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 45

$$\left\{ y(x) = \_C1 e^{(-\frac{a}{2} + \frac{1}{2}\sqrt{a^2-4b})x} + \_C2 e^{(-\frac{a}{2} - \frac{1}{2}\sqrt{a^2-4b})x} \right\}$$

### 3.36 ODE No. 1036

$$\frac{d^2}{dx^2}y(x) + a \frac{d}{dx}y(x) + by(x) - f(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

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**Maple:** cpu = 0.078 (sec), leaf count = 128

$$\left\{ y(x) = e^{(-\frac{a}{2} + \frac{1}{2}\sqrt{a^2-4b})x} \_C2 + e^{(-\frac{a}{2} - \frac{1}{2}\sqrt{a^2-4b})x} \_C1 + 1 \left( \int f(x) e^{-\frac{x}{2}(-a + \sqrt{a^2-4b})} dx e^{x\sqrt{a^2-4b}} - \int f(x) e^{x\sqrt{a^2-4b}} dx \right) \right\}$$

### 3.37 ODE No. 1037

$$\frac{d^2}{dx^2}y(x) + a\frac{d}{dx}y(x) - (b^2x^2 + c)y(x) = 0$$

**Mathematica:** cpu = 0.029504 (sec), leaf count = 101

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-\frac{ax}{2} - \frac{bx^2}{2}} H_{-\frac{a^2 - 4b - 4c}{8b}}(\sqrt{bx}) + c_2 e^{-\frac{ax}{2} - \frac{bx^2}{2}} {}_1F_1\left(-\frac{-a^2 - 4b - 4c}{16b}; \frac{1}{2}; bx^2\right) \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 73

$$\left\{ y(x) = {}_C1 M\left(\frac{a^2 + 12b + 4c}{16b}, \frac{3}{2}, bx^2\right) x e^{-\frac{x(bx+a)}{2}} + {}_C2 U\left(\frac{a^2 + 12b + 4c}{16b}, \frac{3}{2}, bx^2\right) x e^{-\frac{x(bx+a)}{2}} \right\}$$

### 3.38 ODE No. 1038

$$\frac{d^2}{dx^2}y(x) + 2a\frac{d}{dx}y(x) + f(x)y(x) = 0$$

**Mathematica:** cpu = 0.329542 (sec), leaf count = 23

$$\text{DSolve}[2ay'(x) + f(x)y(x) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.0 (sec), leaf count = 28

$$\left\{ y(x) = \text{DESol}\left(\left\{ f(x) {}_Y(x) + 2a\frac{d}{dx}{}_Y(x) + \frac{d^2}{dx^2}{}_Y(x) \right\}, \{ {}_Y(x) \} \right) \right\}$$

### 3.39 ODE No. 1039

$$\frac{d^2}{dx^2}y(x) + x\frac{d}{dx}y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.011501 (sec), leaf count = 47

$$\left\{ \left\{ y(x) \rightarrow \sqrt{\frac{\pi}{2}} c_1 e^{-\frac{x^2}{2}} \text{erfi}\left(\frac{x}{\sqrt{2}}\right) + c_2 e^{-\frac{x^2}{2}} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 33

$$\left\{ y(x) = \text{Erf}\left(\frac{i}{2}\sqrt{2}x\right) {}_C1 \left(e^{\frac{x^2}{2}}\right)^{-1} + {}_C2 \left(e^{\frac{x^2}{2}}\right)^{-1} \right\}$$

### 3.40 ODE No. 1040

$$\frac{d^2}{dx^2}y(x) + x \frac{d}{dx}y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.030004 (sec), leaf count = 53

$$\left\{ \left\{ y(x) \rightarrow c_1 x - \frac{1}{2} c_2 e^{-\frac{x^2}{2}} \left( \sqrt{2\pi} e^{\frac{x^2}{2}} \operatorname{erf}\left(\frac{x}{\sqrt{2}}\right) + 2 \right) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 34

$$\left\{ y(x) = x\_C1 + \_C2 \left( \pi \operatorname{Erf}\left(\frac{x\sqrt{2}}{2}\right) x + \sqrt{2}\sqrt{\pi} e^{-\frac{x^2}{2}} \right) \right\}$$

### 3.41 ODE No. 1041

$$\frac{d^2}{dx^2}y(x) + x \frac{d}{dx}y(x) + (n+1)y(x) = 0$$

**Mathematica:** cpu = 0.008501 (sec), leaf count = 55

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-\frac{x^2}{2}} H_n\left(\frac{x}{\sqrt{2}}\right) + c_2 e^{-\frac{x^2}{2}} {}_1F_1\left(-\frac{n}{2}; \frac{1}{2}; \frac{x^2}{2}\right) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 47

$$\left\{ y(x) = \_C1 e^{-\frac{x^2}{2}} M\left(-\frac{n}{2} + \frac{1}{2}, \frac{3}{2}, \frac{x^2}{2}\right) x + \_C2 e^{-\frac{x^2}{2}} U\left(-\frac{n}{2} + \frac{1}{2}, \frac{3}{2}, \frac{x^2}{2}\right) x \right\}$$

### 3.42 ODE No. 1042

$$\frac{d^2}{dx^2}y(x) + x \frac{d}{dx}y(x) - ny(x) = 0$$

**Mathematica:** cpu = 0.008001 (sec), leaf count = 61

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-\frac{x^2}{2}} H_{-n-1}\left(\frac{x}{\sqrt{2}}\right) + c_2 e^{-\frac{x^2}{2}} {}_1F_1\left(\frac{n+1}{2}; \frac{1}{2}; \frac{x^2}{2}\right) \right\} \right\}$$

**Maple:** cpu = 0.046 (sec), leaf count = 47

$$\left\{ y(x) = \_C1 e^{-\frac{x^2}{2}} M\left(\frac{n}{2} + 1, \frac{3}{2}, \frac{x^2}{2}\right) x + \_C2 e^{-\frac{x^2}{2}} U\left(\frac{n}{2} + 1, \frac{3}{2}, \frac{x^2}{2}\right) x \right\}$$

### 3.43 ODE No. 1043

$$\frac{d^2}{dx^2}y(x) - x \frac{d}{dx}y(x) + 2y(x) = 0$$

**Mathematica:** cpu = 0.044506 (sec), leaf count = 69

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4}c_2 \left( \sqrt{2\pi}x^2 \operatorname{erfi} \left( \frac{x}{\sqrt{2}} \right) - \sqrt{2\pi} \operatorname{erfi} \left( \frac{x}{\sqrt{2}} \right) - 2e^{\frac{x^2}{2}} x \right) + c_1(x^2 - 1) \right\} \right\}$$

**Maple:** cpu = 0.140 (sec), leaf count = 44

$$\left\{ y(x) = \_C1 \left( -2xe^{1/2x^2} + \operatorname{erfi} \left( \frac{x\sqrt{2}}{2} \right) \sqrt{\pi}\sqrt{2}(x-1)(1+x) \right) + \_C2(x^2 - 1) \right\}$$

### 3.44 ODE No. 1044

$$\frac{d^2}{dx^2}y(x) - x \frac{d}{dx}y(x) - ay(x) = 0$$

**Mathematica:** cpu = 0.008001 (sec), leaf count = 39

$$\left\{ \left\{ y(x) \rightarrow c_1 H_{-a} \left( \frac{x}{\sqrt{2}} \right) + c_2 {}_1F_1 \left( \frac{a}{2}; \frac{1}{2}; \frac{x^2}{2} \right) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 M \left( \frac{1}{2} + \frac{a}{2}, \frac{3}{2}, \frac{x^2}{2} \right) x + \_C2 U \left( \frac{1}{2} + \frac{a}{2}, \frac{3}{2}, \frac{x^2}{2} \right) x \right\}$$

### 3.45 ODE No. 1045

$$\frac{d^2}{dx^2}y(x) - x \frac{d}{dx}y(x) + (x-1)y(x) = 0$$

**Mathematica:** cpu = 0.021003 (sec), leaf count = 39

$$\left\{ \left\{ y(x) \rightarrow \sqrt{\frac{\pi}{2}}c_2 e^{x-2} \operatorname{erfi} \left( \frac{x-2}{\sqrt{2}} \right) + c_1 e^x \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 28

$$\left\{ y(x) = \operatorname{Erf} \left( \frac{i}{2}\sqrt{2}x - i\sqrt{2} \right) e^x \_C1 + \_C2 e^x \right\}$$

### 3.46 ODE No. 1046

$$\frac{d^2}{dx^2}y(x) - 2x \frac{d}{dx}y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.006501 (sec), leaf count = 31

$$\left\{ \left\{ y(x) \rightarrow c_1 H_{\frac{a}{2}}(x) + c_2 {}_1F_1\left(-\frac{a}{4}; \frac{1}{2}; x^2\right) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 31

$$\left\{ y(x) = -C1 M\left(\frac{1}{2} - \frac{a}{4}, \frac{3}{2}, x^2\right)x + -C2 U\left(\frac{1}{2} - \frac{a}{4}, \frac{3}{2}, x^2\right)x \right\}$$

### 3.47 ODE No. 1047

$$\frac{d^2}{dx^2}y(x) + 4x \frac{d}{dx}y(x) + (4x^2 + 2)y(x) = 0$$

**Mathematica:** cpu = 0.013502 (sec), leaf count = 27

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-x^2} + c_2 x e^{-x^2} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 22

$$\left\{ y(x) = -C1 e^{-x^2} + -C2 x e^{-x^2} \right\}$$

### 3.48 ODE No. 1048

$$\frac{d^2}{dx^2}y(x) - 4x \frac{d}{dx}y(x) + (3x^2 + 2n - 1)y(x) = 0$$

**Mathematica:** cpu = 0.010001 (sec), leaf count = 45

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{x^2}{2}} H_n(x) + c_2 e^{\frac{x^2}{2}} {}_1F_1\left(-\frac{n}{2}; \frac{1}{2}; x^2\right) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 43

$$\left\{ y(x) = -C1 e^{\frac{x^2}{2}} M\left(-\frac{n}{2} + \frac{1}{2}, \frac{3}{2}, x^2\right)x + -C2 e^{\frac{x^2}{2}} U\left(-\frac{n}{2} + \frac{1}{2}, \frac{3}{2}, x^2\right)x \right\}$$



### 3.49 ODE No. 1049

$$\frac{d^2}{dx^2}y(x) - 4x \frac{d}{dx}y(x) + (4x^2 - 1)y(x) - e^x = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.125 (sec), leaf count = 70

$$\left\{ y(x) = e^{x^2} \cos(x) \_C2 + e^{x^2} \sin(x) \_C1 - \frac{e^{x^2} \left( -e^{\frac{i}{2}} (i \cos(x) + \sin(x)) \operatorname{Erf}\left(x - \frac{1}{2} - \frac{i}{2}\right) + (i \cos(x) - \sin(x)) \operatorname{Erf}\left(x - \frac{1}{2} + \frac{i}{2}\right) \right)}{4} \right.$$

### 3.50 ODE No. 1050

$$\frac{d^2}{dx^2}y(x) - 4x \frac{d}{dx}y(x) + (4x^2 - 2)y(x) = 0$$

**Mathematica:** cpu = 0.012002 (sec), leaf count = 23

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{x^2} + c_2 e^{x^2} x \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 18

$$\left\{ y(x) = e^{x^2} \_C1 + \_C2 e^{x^2} x \right\}$$

### 3.51 ODE No. 1051

$$\frac{d^2}{dx^2}y(x) - 4x \frac{d}{dx}y(x) + (4x^2 - 3)y(x) - e^{x^2} = 0$$

**Mathematica:** cpu = 0.030004 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{(x-1)x} + \frac{1}{2} c_2 e^{(x-1)x+2x} - e^{(x-1)x+x} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 27

$$\left\{ y(x) = e^{x(1+x)} \_C2 + e^{x(x-1)} \_C1 - e^{x^2} \right\}$$

### 3.52 ODE No. 1052

$$\frac{d^2}{dx^2}y(x) + ax \frac{d}{dx}y(x) + by(x) = 0$$

**Mathematica:** cpu = 0.020503 (sec), leaf count = 78

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-\frac{ax^2}{2}} H_{\frac{b-a}{a}} \left( \frac{\sqrt{ax}}{\sqrt{2}} \right) + c_2 e^{-\frac{ax^2}{2}} {}_1F_1 \left( -\frac{b-a}{2a}; \frac{1}{2}; \frac{ax^2}{2} \right) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 65

$$\left\{ y(x) = \_C1 e^{-\frac{ax^2}{2}} M \left( \frac{2a-b}{2a}, \frac{3}{2}, \frac{ax^2}{2} \right) x + \_C2 e^{-\frac{ax^2}{2}} U \left( \frac{2a-b}{2a}, \frac{3}{2}, \frac{ax^2}{2} \right) x \right\}$$

### 3.53 ODE No. 1053

$$\frac{d^2}{dx^2}y(x) + 2ax \frac{d}{dx}y(x) + a^2x^2y(x) = 0$$

**Mathematica:** cpu = 0.029004 (sec), leaf count = 57

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-\frac{ax^2}{2} - \sqrt{ax}} + \frac{c_2 e^{\sqrt{ax} - \frac{ax^2}{2}}}{2\sqrt{a}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 e^{-\frac{x}{2}(ax-2\sqrt{a})} + \_C2 e^{-\frac{x}{2}(ax+2\sqrt{a})} \right\}$$

### 3.54 ODE No. 1054

$$\frac{d^2}{dx^2}y(x) + (ax+b) \frac{d}{dx}y(x) + (cx+d)y(x) = 0$$

**Mathematica:** cpu = 0.048006 (sec), leaf count = 172

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{cx}{a} - \frac{ax^2}{2} - bx} H_{-\frac{a^3+a^2d-abc+c^2}{a^3}} \left( \frac{ab-2c}{\sqrt{2}a^{3/2}} + \frac{\sqrt{ax}}{\sqrt{2}} \right) + c_2 e^{\frac{cx}{a} - \frac{ax^2}{2} - bx} {}_1F_1 \left( -\frac{-a^3+da^2-bca+c^2}{2a^3}; \frac{1}{2}; \frac{ax^2}{2} \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 105

$$\left\{ y(x) = \_C1 e^{-\frac{cx}{a}} M \left( \frac{da^2-abc+c^2}{2a^3}, \frac{1}{2}, -\frac{(a^2x+ab-2c)^2}{2a^3} \right) + \_C2 e^{-\frac{cx}{a}} U \left( \frac{da^2-abc+c^2}{2a^3}, \frac{1}{2}, -\frac{(a^2x+ab-2c)^2}{2a^3} \right) \right\}$$

### 3.55 ODE No. 1055

$$\frac{d^2}{dx^2}y(x) + (ax + b) \frac{d}{dx}y(x) + (a1 x^2 + b1 x + c1) y(x) = 0$$

**Mathematica:** cpu = 0.155020 (sec), leaf count = 421

$$\left\{ \left\{ y(x) \rightarrow c_1 \exp \left( \frac{-bx\sqrt{a^2 - 4a1} - \frac{1}{2}ax^2\sqrt{a^2 - 4a1} - \frac{1}{2}a^2x^2 - abx + 2a1x^2 + 2b1x}{2\sqrt{a^2 - 4a1}} \right) H_{-a^3 - a^2\sqrt{a^2 - 4a1} + 4a1} \right. \right.$$

**Maple:** cpu = 0.172 (sec), leaf count = 317

$$\left\{ y(x) = \_C1 {}_1F_1 \left( \frac{1}{4} \left( (a^2 - 4a1)^{\frac{3}{2}} + a^3 - 2a^2c1 + (2b1b - 4a1)a + (-2b^2 + 8c1)a1 - 2b1^2 \right) (a^2 - \right.$$

### 3.56 ODE No. 1056

$$\frac{d^2}{dx^2}y(x) - x^2 \frac{d}{dx}y(x) + xy(x) = 0$$

**Mathematica:** cpu = 0.036005 (sec), leaf count = 66

$$\left\{ \left\{ y(x) \rightarrow c_1 x - \frac{c_2 \left( 3e^{\frac{x^3}{3}} (-x^3)^{2/3} + 3^{2/3} x^3 \Gamma \left( \frac{2}{3}, -\frac{x^3}{3} \right) \right)}{3 (-x^3)^{2/3}} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 48

$$\left\{ y(x) = x\_C1 + \frac{\_C2}{x^2} \left( \sqrt[3]{3} e^{\frac{x^3}{3}} (-x^3)^{\frac{2}{3}} - x^3 \left( \Gamma \left( \frac{2}{3} \right) - \Gamma \left( \frac{2}{3}, -\frac{x^3}{3} \right) \right) \right) \right\}$$

### 3.57 ODE No. 1057

$$\frac{d^2}{dx^2}y(x) - x^2 \frac{d}{dx}y(x) - (1 + x)^2 y(x) = 0$$

**Mathematica:** cpu = 0.879612 (sec), leaf count = 55

$$\left\{ \left\{ y(x) \rightarrow c_2 e^{\frac{x^3}{3} + x} \int_1^x e^{-\frac{1}{3}K[1]^3 - 2K[1]} dK[1] + c_1 e^{\frac{x^3}{3} + x} \right\} \right\}$$

**Maple:** cpu = 0.110 (sec), leaf count = 50

$$\left\{ y(x) = \_C1 HeunT \left( 0, -3, 2\sqrt[3]{3}, \frac{3^{\frac{2}{3}}x}{3} \right) e^{-x} + \_C2 HeunT \left( 0, 3, 2\sqrt[3]{3}, -\frac{3^{\frac{2}{3}}x}{3} \right) e^{\frac{x(x^2+3)}{3}} \right\}$$

### 3.58 ODE No. 1058

$$\frac{d^2}{dx^2}y(x) - x^2(1+x) \frac{d}{dx}y(x) + x(x^4 - 2)y(x) = 0$$

**Mathematica:** cpu = 0.899614 (sec), leaf count = 55

$$\left\{ \left\{ y(x) \rightarrow c_2 e^{\frac{x^3}{3}} \int_1^x e^{\frac{K[1]^4}{4} - \frac{K[1]^3}{3}} dK[1] + c_1 e^{\frac{x^3}{3}} \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 e^{\frac{x^3}{3}} + \_C2 e^{\frac{x^3}{3}} \int e^{\frac{x^4}{4} - \frac{x^3}{3}} dx \right\}$$

### 3.59 ODE No. 1059

$$\frac{d^2}{dx^2}y(x) + x^4 \frac{d}{dx}y(x) - x^3 y(x) = 0$$

**Mathematica:** cpu = 0.052007 (sec), leaf count = 72

$$\left\{ \left\{ y(x) \rightarrow c_1 x - \frac{c_2 e^{-\frac{x^5}{5}} \left( 5(x^5)^{4/5} - 5^{4/5} e^{\frac{x^5}{5}} x^5 \Gamma\left(\frac{4}{5}, \frac{x^5}{5}\right) \right)}{5(x^5)^{4/5}} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 55

$$\left\{ y(x) = x \_C1 + \frac{\_C2}{x^7} e^{-\frac{x^5}{10}} \left( x^{10} M_{\frac{2}{5}, \frac{9}{10}}\left(\frac{x^5}{5}\right) + 9 M_{7/5, \frac{9}{10}}(1/5 x^5) x^5 + 36 M_{7/5, \frac{9}{10}}(1/5 x^5) \right) \right\}$$

### 3.60 ODE No. 1060

$$\frac{d^2}{dx^2}y(x) + ax^{q-1} \frac{d}{dx}y(x) + bx^{q-2}y(x) = 0$$

**Mathematica:** cpu = 0.037005 (sec), leaf count = 83

$$\left\{ \left\{ y(x) \rightarrow c_2 q^{-1/q} a^{\frac{1}{q}} (x^q)^{\frac{1}{q}} {}_1F_1\left(\frac{b}{aq} + \frac{1}{q}; 1 + \frac{1}{q}; -\frac{ax^q}{q}\right) + c_1 {}_1F_1\left(\frac{b}{aq}; 1 - \frac{1}{q}; -\frac{ax^q}{q}\right) \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 91

$$\left\{ y(x) = \_C1 e^{-\frac{ax^q}{q}} M\left(\frac{aq-b}{aq}, \frac{q+1}{q}, \frac{ax^q}{q}\right) x + \_C2 e^{-\frac{ax^q}{q}} U\left(\frac{aq-b}{aq}, \frac{q+1}{q}, \frac{ax^q}{q}\right) x \right\}$$

### 3.61 ODE No. 1061

$$\frac{d^2}{dx^2}y(x) + \left(\frac{d}{dx}y(x)\right)\sqrt{x} + \left(1/4 \frac{1}{\sqrt{x}} + x/4 - 9\right)y(x) - xe^{-1/3x^{3/2}} = 0$$

**Mathematica:** cpu = 0.076010 (sec), leaf count = 70

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-\frac{1}{3}(\sqrt{x}+9)x} + \frac{1}{6}c_2 e^{6x-\frac{1}{3}(\sqrt{x}+9)x} - \frac{1}{9}e^{3x-\frac{1}{3}(\sqrt{x}+9)x} x \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 38

$$\left\{ y(x) = e^{-\frac{1}{3}x^{\frac{3}{2}}} \sinh(3x) \_C2 + e^{-\frac{1}{3}x^{\frac{3}{2}}} \cosh(3x) \_C1 - \frac{x}{9} e^{-\frac{1}{3}x^{\frac{3}{2}}} \right\}$$

### 3.62 ODE No. 1062

$$\frac{d^2}{dx^2}y(x) - \frac{\frac{d}{dx}y(x)}{\sqrt{x}} + 1/4 \frac{(x + \sqrt{x} - 8)y(x)}{x^2} = 0$$

**Mathematica:** cpu = 0.028004 (sec), leaf count = 35

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{3}c_2 e^{\sqrt{x}} x^2 + \frac{c_1 e^{\sqrt{x}}}{x} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 23

$$\left\{ y(x) = \frac{\_C1}{x} e^{\sqrt{x}} + \_C2 e^{\sqrt{x}} x^2 \right\}$$

### 3.63 ODE No. 1063

$$\frac{d^2}{dx^2}y(x) - (2e^x + 1) \frac{d}{dx}y(x) + e^{2x}y(x) - e^{3x} = 0$$

**Mathematica:** cpu = 0.040505 (sec), leaf count = 28

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{e^x} + c_2 e^{e^x+e^x} + e^x + 2 \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 66

$$\left\{ y(x) = e^{e^x+\frac{x}{2}} \sinh\left(\frac{x}{2}\right) \_C2 + e^{e^x+\frac{x}{2}} \cosh\left(\frac{x}{2}\right) \_C1 + e^{\frac{x}{2}} \left( (e^{2x} + e^x + 1) \cosh\left(\frac{x}{2}\right) - 3(e^x + 1/3 e^{2x} + \dots) \right) \right\}$$

### 3.64 ODE No. 1064

$$\frac{d^2}{dx^2}y(x) + a \frac{d}{dx}y(x) + \tan(x) + by(x) = 0$$

**Mathematica:** cpu = 0.564072 (sec), leaf count = 1400

$$\left\{ \left\{ y(x) \rightarrow e^{\frac{1}{2}(-a-\sqrt{a^2-4b})x} c_1 + e^{\frac{1}{2}(\sqrt{a^2-4b}-a)x} c_2 + \frac{8(2 {}_2F_1(1, \frac{1}{4}i(\sqrt{a^2-4b}-a); \frac{1}{4}i(\sqrt{a^2-4b}-a) + 1; -\dots)}{\dots)} \right\} \right.$$

**Maple:** cpu = 0.203 (sec), leaf count = 129

$$\left\{ y(x) = e^{(-\frac{a}{2} + \frac{1}{2}\sqrt{a^2-4b})x} \_C2 + e^{(-\frac{a}{2} - \frac{1}{2}\sqrt{a^2-4b})x} \_C1 - 1 \left( \int \tan(x) e^{-\frac{x}{2}(-a+\sqrt{a^2-4b})} dx e^{x\sqrt{a^2-4b}} - \int \tan \right. \right.$$

### 3.65 ODE No. 1065

$$\frac{d^2}{dx^2}y(x) + 2n \left( \frac{d}{dx}y(x) \right) \cot(x) + (-a^2 + n^2) y(x) = 0$$

**Mathematica:** cpu = 0.163021 (sec), leaf count = 114

$$\left\{ \left\{ y(x) \rightarrow c_1 (\cos^2(x) - 1)^{\frac{1}{4}(1-2n)} P_{\frac{1}{2}(2n-1)}^{\frac{1}{2}(2\sqrt{2n^2-a^2}-1)}(\cos(x)) + c_2 (\cos^2(x) - 1)^{\frac{1}{4}(1-2n)} Q_{\frac{1}{2}(2n-1)}^{\frac{1}{2}(2\sqrt{2n^2-a^2}-1)}(\cos(x)) \right\} \right.$$

**Maple:** cpu = 0.171 (sec), leaf count = 67

$$\left\{ y(x) = \_C1 (\sin(x))^{-n+\frac{1}{2}} LegendreP\left(-\frac{1}{2} + \sqrt{-a^2 + 2n^2}, n - \frac{1}{2}, \cos(x)\right) + \_C2 (\sin(x))^{-n+\frac{1}{2}} LegendreQ\left(-\frac{1}{2} + \sqrt{-a^2 + 2n^2}, n - \frac{1}{2}, \cos(x)\right) \right.$$

### 3.66 ODE No. 1066

$$\frac{d^2}{dx^2}y(x) + \left( \frac{d}{dx}y(x) \right) \tan(x) + y(x) (\cos(x))^2 = 0$$

**Mathematica:** cpu = 0.035004 (sec), leaf count = 18

$$\left\{ \left\{ y(x) \rightarrow c_2 \sin(\sin(x)) + c_1 \cos(\sin(x)) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 15

$$\{y(x) = \_C1 \sin(\sin(x)) + \_C2 \cos(\sin(x))\}$$

### 3.67 ODE No. 1067

$$\frac{d^2}{dx^2}y(x) + \left(\frac{d}{dx}y(x)\right) \tan(x) - y(x) (\cos(x))^2 = 0$$

**Mathematica:** cpu = 0.032504 (sec), leaf count = 21

$$\{ \{y(x) \rightarrow c_1 \cosh(\sin(x)) + ic_2 \sinh(\sin(x))\} \}$$

**Maple:** cpu = 0.032 (sec), leaf count = 17

$$\{y(x) = \_C1 e^{\sin(x)} + \_C2 e^{-\sin(x)}\}$$

### 3.68 ODE No. 1068

$$\frac{d^2}{dx^2}y(x) + \left(\frac{d}{dx}y(x)\right) \cot(x) + v(v+1)y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.141 (sec), leaf count = 45

$$\left\{ y(x) = \_C1 {}_2F_1\left(-\frac{v}{2}, \frac{1}{2} + \frac{v}{2}; \frac{1}{2}; (\cos(x))^2\right) + \_C2 \cos(x) {}_2F_1\left(1 + \frac{v}{2}, \frac{1}{2} - \frac{v}{2}; \frac{3}{2}; (\cos(x))^2\right) \right\}$$

### 3.69 ODE No. 1069

$$\frac{d^2}{dx^2}y(x) - \left(\frac{d}{dx}y(x)\right) \cot(x) + y(x) (\sin(x))^2 = 0$$

**Mathematica:** cpu = 0.036005 (sec), leaf count = 19

$$\{ \{y(x) \rightarrow c_1 \cos(\cos(x)) - c_2 \sin(\cos(x))\} \}$$

**Maple:** cpu = 0.063 (sec), leaf count = 15

$$\{y(x) = \_C1 \sin(\cos(x)) + \_C2 \cos(\cos(x))\}$$

### 3.70 ODE No. 1070

$$\frac{d^2}{dx^2}y(x) + a\left(\frac{d}{dx}y(x)\right)\tan(x) + by(x) = 0$$

**Mathematica:** cpu = 0.317540 (sec), leaf count = 143

$$\left\{ \left\{ y(x) \rightarrow c_1 {}_2F_1\left(-\frac{a}{4} - \frac{1}{4}\sqrt{a^2 + 4b}, \frac{1}{4}\sqrt{a^2 + 4b} - \frac{a}{4}; \frac{1}{2} - \frac{a}{2}; \cos^2(x)\right) + i^{a+1}c_2 \cos^{a+1}(x) {}_2F_1\left(\frac{a}{4} - \frac{1}{4}\sqrt{a^2 + 4b}, \frac{1}{4}\sqrt{a^2 + 4b} - \frac{a}{4}; \frac{1}{2} - \frac{a}{2}; \cos^2(x)\right) \right\} \right.$$

**Maple:** cpu = 0.141 (sec), leaf count = 67

$$\left\{ y(x) = \_C1 (\cos(x))^{\frac{1}{2} + \frac{a}{2}} \text{LegendreP}\left(\frac{1}{2}\sqrt{a^2 + 4b} - \frac{1}{2}, \frac{1}{2} + \frac{a}{2}, \sin(x)\right) + \_C2 (\cos(x))^{\frac{1}{2} + \frac{a}{2}} \text{LegendreQ}\left(\frac{1}{2}\sqrt{a^2 + 4b} - \frac{1}{2}, \frac{1}{2} + \frac{a}{2}, \sin(x)\right) \right.$$

### 3.71 ODE No. 1071

$$\frac{d^2}{dx^2}y(x) + 2a\left(\frac{d}{dx}y(x)\right)\cot(ax) + (-a^2 + b^2)y(x) = 0$$

**Mathematica:** cpu = 0.106514 (sec), leaf count = 59

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-\sqrt{-b^2}x} \csc(ax) + \frac{c_2 e^{\sqrt{-b^2}x} \csc(ax)}{2\sqrt{-b^2}} \right\} \right.$$

**Maple:** cpu = 0.046 (sec), leaf count = 37

$$\left\{ y(x) = \_C1 \sin(bx) \frac{1}{\sqrt{(\cos(ax))^2 - 1}} + \_C2 \cos(bx) \frac{1}{\sqrt{(\cos(ax))^2 - 1}} \right.$$

### 3.72 ODE No. 1072

$$\frac{d^2}{dx^2}y(x) + a\left(\frac{d^2}{dx^2}p(x)\right)\frac{d}{dx}y(x) + (a + bp(x) - 4na(p(x))^2)y(x) = 0$$

**Mathematica:** cpu = 0.281536 (sec), leaf count = 38

$$\text{DSolve}[y(x) (-4anp(x)^2 + a + bp(x)) + ap''(x)y'(x) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.250 (sec), leaf count = 45

$$\left\{ y(x) = \text{DESol}\left(\left\{\frac{d^2}{dx^2}Y(x) + a\left(\frac{d^2}{dx^2}p(x)\right)\frac{d}{dx}Y(x) + (a + bp(x) - 4na(p(x))^2)Y(x)\right\}, \{Y(x)\}\right) \right.$$



### 3.73 ODE No. 1073

$$\frac{d^2}{dx^2}y(x) + \frac{(11 \text{ WeierstrassP}(x, a, b) \text{ WeierstrassPPrime}(x, a, b) - 6 (\text{WeierstrassP}(x, a, b))^2 + a/2) \frac{d}{dx}y}{\text{WeierstrassPPrime}(x, a, b) + (\text{WeierstrassP}(x, a, b))^2}$$

**Mathematica:** cpu = 1.365173 (sec), leaf count = 129

$$\text{DSolve} \left[ \frac{y'(x) (-\wp(x; a, b)\wp'(x; a, b) + \wp(x; a, b)^3 - 6\wp(x; a, b)^2 + \frac{a}{2})}{\wp'(x; a, b) - \wp(x; a, b)^2} + \frac{y(x) (\wp(x; a, b)^2(-\wp'(x; a, b)) - (6\wp(x; a, b)^3 - 6\wp(x; a, b)^2 + \frac{a}{2}))}{\wp(x; a, b)^2}, y(x) \right]$$

**Maple:** cpu = 2.511 (sec), leaf count = 109

$$\left\{ y(x) = \text{DESol} \left( \left\{ \frac{d^2}{dx^2} - Y(x) + \frac{\frac{d}{dx} - Y(x)}{\text{WeierstrassPPrime}(x, a, b) + (\text{WeierstrassP}(x, a, b))^2} \right\} (11 \text{ WeierstrassP}(x, a, b) \text{ WeierstrassPPrime}(x, a, b) - 6 (\text{WeierstrassP}(x, a, b))^2 + a/2) \right) \right\}$$

### 3.74 ODE No. 1074

$$\frac{d^2}{dx^2}y(x) + \frac{k^2 \text{JacobiSN}(x, k) \text{JacobiCN}(x, k) \frac{d}{dx}y(x)}{\text{JacobiDN}(x, k)} + n^2 y(x) (\text{JacobiDN}(x, k))^2 = 0$$

**Mathematica:** cpu = 26.455859 (sec), leaf count = 41

$$\text{DSolve} \left[ \frac{k^2 \text{cn}(x|k) \text{sn}(x|k) y'(x)}{\text{dn}(x|k)} + n^2 y(x) \text{dn}(x|k)^2 + y''(x) = 0, y(x), x \right]$$

**Maple:** cpu = 0.016 (sec), leaf count = 21

$$\{y(x) = \_C1 \sin(n \text{JacobiAM}(x, k)) + \_C2 \cos(n \text{JacobiAM}(x, k))\}$$

### 3.75 ODE No. 1075

$$\frac{d^2}{dx^2}y(x) + f(x) \frac{d}{dx}y(x) + g(x) y(x) = 0$$

**Mathematica:** cpu = 0.178523 (sec), leaf count = 23

$$\text{DSolve}[f(x)y'(x) + g(x)y(x) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.0 (sec), leaf count = 28

$$\left\{ y(x) = \text{DESol} \left( \left\{ g(x) \_Y(x) + f(x) \frac{d}{dx} \_Y(x) + \frac{d^2}{dx^2} \_Y(x) \right\}, \{ \_Y(x) \} \right) \right\}$$

### 3.76 ODE No. 1076

$$\frac{d^2}{dx^2}y(x) + f(x) \frac{d}{dx}y(x) + \left( \frac{d}{dx}f(x) + a \right) y(x) - g(x) = 0$$

**Mathematica:** cpu = 0.203026 (sec), leaf count = 31

$$\text{DSolve}[y(x) (a + f'(x)) + f(x)y'(x) - g(x) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.171 (sec), leaf count = 36

$$\left\{ y(x) = \text{DESol} \left( \left\{ \frac{d^2}{dx^2} Y(x) + f(x) \frac{d}{dx} Y(x) + \left( \frac{d}{dx} f(x) + a \right) Y(x) - g(x) \right\}, \{ Y(x) \} \right) \right\}$$

### 3.77 ODE No. 1077

$$\frac{d^2}{dx^2}y(x) + (af(x) + b) \frac{d}{dx}y(x) + (cf(x) + d) y(x) = 0$$

**Mathematica:** cpu = 0.320041 (sec), leaf count = 31

$$\text{DSolve}[y'(x)(af(x) + b) + y(x)(cf(x) + d) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.172 (sec), leaf count = 36

$$\left\{ y(x) = \text{DESol} \left( \left\{ \frac{d^2}{dx^2} Y(x) + (af(x) + b) \frac{d}{dx} Y(x) + (cf(x) + d) Y(x) \right\}, \{ Y(x) \} \right) \right\}$$

### 3.78 ODE No. 1078

$$\frac{d^2}{dx^2}y(x) + f(x) \frac{d}{dx}y(x) + \left( 1/4 (f(x))^2 + 1/2 \frac{d}{dx}f(x) + a \right) y(x) = 0$$

**Mathematica:** cpu = 0.073009 (sec), leaf count = 73

$$\left\{ \left\{ y(x) \rightarrow c_1 \exp \left( -\frac{1}{2} \int_1^x f(K[1]) dK[1] - \sqrt{-ax} \right) + \frac{c_2 e^{\sqrt{-ax} - \frac{1}{2} \int_1^x f(K[1]) dK[1]}}{2\sqrt{-a}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 39

$$\left\{ y(x) = \_C1 e^{-\frac{\int f(x) dx}{2}} \sinh(\sqrt{-ax}) + \_C2 e^{-\frac{\int f(x) dx}{2}} \cosh(\sqrt{-ax}) \right\}$$

### 3.79 ODE No. 1079

$$\frac{d^2}{dx^2}y(x) - \frac{a\left(\frac{d}{dx}f(x)\right)\frac{d}{dx}y(x)}{f(x)} + b(f(x))^{2a}y(x) = 0$$

**Mathematica:** cpu = 0.237530 (sec), leaf count = 135

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( e^{c_2 + \int_1^x -i\sqrt{b}f(K[1])^a dK[1]} - 2c_1 \exp \left( -c_2 - \int_1^x -i\sqrt{b}f(K[1])^a dK[1] \right) \right) \right\}, \left\{ y(x) \rightarrow \frac{1}{2} \left( e^{c_2 + \int_1^x i\sqrt{b}f(K[1])^a dK[1]} - 2c_1 \exp \left( -c_2 - \int_1^x i\sqrt{b}f(K[1])^a dK[1] \right) \right) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 37

$$\left\{ y(x) = \_C1 e^{\int i(f(x))^a \sqrt{b} dx} + \_C2 e^{-\int i(f(x))^a \sqrt{b} dx} \right\}$$

### 3.80 ODE No. 1080

$$\frac{d^2}{dx^2}y(x) - \left( \frac{\frac{d}{dx}f(x)}{f(x)} + 2a \right) \frac{d}{dx}y(x) + \left( \frac{a\frac{d}{dx}f(x)}{f(x)} + a^2 - b^2(f(x))^2 \right) y(x) = 0$$

**Mathematica:** cpu = 0.303038 (sec), leaf count = 56

$$\text{DSolve} \left[ y(x) \left( a^2 + \frac{af'(x)}{f(x)} - b^2 f(x)^2 \right) - y'(x) \left( 2a + \frac{f'(x)}{f(x)} \right) + y''(x) = 0, y(x), x \right]$$

**Maple:** cpu = 0.219 (sec), leaf count = 74

$$\left\{ y(x) = e^{\int -1 \left( \frac{f(x)(e^{-C1b})^{2b}}{(e^{\int f(x) dx b})^2} + bf(x) - \frac{(e^{-C1b})^{2a}}{(e^{\int f(x) dx b})^2} + a \right) \left( \frac{(e^{-C1b})^2}{(e^{\int f(x) dx b})^2} - 1 \right)^{-1} dx} \_C2 \right\}$$

### 3.81 ODE No. 1081

$$\frac{d^2}{dx^2}y(x) + \frac{f(x)\left(\frac{d^3}{dx^3}f(x)\right)\frac{d}{dx}y(x)}{(f(x))^2 + b^2} - \frac{a^2\left(\frac{d}{dx}f(x)\right)^2 y(x)}{(f(x))^2 + b^2} = 0$$

**Mathematica:** cpu = 0.810103 (sec), leaf count = 55

$$\text{DSolve} \left[ -\frac{a^2 y(x) f'(x)^2}{b^2 + f(x)^2} + \frac{f(x) f^3(x) y'(x)}{b^2 + f(x)^2} + y''(x) = 0, y(x), x \right]$$

**Maple:** cpu = 0.561 (sec), leaf count = 64

$$\left\{ y(x) = \text{DESol} \left( \left\{ \frac{d^2}{dx^2} Y(x) + \frac{f(x)\left(\frac{d^3}{dx^3}f(x)\right)\frac{d}{dx}Y(x)}{(f(x))^2 + b^2} - \frac{\left(\frac{d}{dx}f(x)\right)^2 a^2 Y(x)}{(f(x))^2 + b^2} \right\}, \{ \_Y(x) \} \right) \right\}$$

### 3.82 ODE No. 1082

$$\frac{d^2}{dx^2}y(x) - \left( \frac{\frac{d^2}{dx^2}g(x)}{\frac{d}{dx}g(x)} + \frac{(2m-1)\frac{d}{dx}g(x)}{g(x)} \right) \frac{d}{dx}y(x) + \left( \frac{(m^2-v^2)\left(\frac{d}{dx}g(x)\right)^2}{g(x)} + \left(\frac{d}{dx}g(x)\right)^2 \right) y(x) = 0$$

**Mathematica:** cpu = 0.548070 (sec), leaf count = 73

$$\text{DSolve}\left[y(x)\left(\frac{(m^2-v^2)g'(x)^2}{g(x)} + g'(x)^2\right) - y'(x)\left(\frac{(2m-1)g'(x)}{g(x)} + \frac{g''(x)}{g'(x)}\right) + y''(x) = 0, y(x), x\right]$$

**Maple:** cpu = 0.094 (sec), leaf count = 85

$$\left\{ y(x) = \_C1 e^{-ig(x)} M\left(\frac{i}{2}m^2 - \frac{i}{2}v^2 + m + \frac{1}{2}, 2m + 1, 2ig(x)\right) (g(x))^{2m} + \_C2 e^{-ig(x)} U\left(\frac{i}{2}m^2 - \frac{i}{2}v^2 + m + \frac{1}{2}, 2m + 1, 2ig(x)\right) (g(x))^{2m} \right\}$$

### 3.83 ODE No. 1083

$$\frac{d^2}{dx^2}y(x) - \frac{\left(\frac{d}{dx}f(x)\right)\frac{d}{dx}y(x)}{f(x)} + \left( 3/4 \frac{\left(\frac{d}{dx}f(x)\right)^2}{\left(f(x)\right)^2} - 1/2 \frac{\frac{d^2}{dx^2}f(x)}{f(x)} - 3/4 \frac{\left(\frac{d^2}{dx^2}g(x)\right)^2}{\left(\frac{d}{dx}g(x)\right)^2} + 1/2 \frac{\frac{d^3}{dx^3}g(x)}{\frac{d}{dx}g(x)} + \frac{(1/4)g''(x)}{g'(x)} \right) y(x) = 0$$

**Mathematica:** cpu = 0.823605 (sec), leaf count = 111

$$\text{DSolve}\left[-\frac{f'(x)y'(x)}{f(x)} + y(x)\left(-\frac{f''(x)}{2f(x)} + \frac{3f'(x)^2}{4f(x)^2} + \frac{(\frac{1}{4}-v^2)g'(x)^2}{g(x)^2} + g'(x)^2 + \frac{g^3(x)}{2g'(x)} - \frac{3g''(x)^2}{4g'(x)^2}\right) + y''(x) = 0, y(x), x\right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 43

$$\left\{ y(x) = \_C1 \sqrt{\frac{f(x)g(x)}{\frac{d}{dx}g(x)}} J_v(g(x)) + \_C2 \sqrt{\frac{f(x)g(x)}{\frac{d}{dx}g(x)}} Y_v(g(x)) \right\}$$

### 3.84 ODE No. 1084

$$\frac{d^2}{dx^2}y(x) - \left( 2 \frac{\frac{d}{dx}f(x)}{f(x)} + \frac{\frac{d^2}{dx^2}g(x)}{\frac{d}{dx}g(x)} - \frac{\frac{d}{dx}g(x)}{g(x)} \right) \frac{d}{dx}y(x) + \left( \frac{\frac{d}{dx}f(x)}{f(x)} \left( 2 \frac{\frac{d}{dx}f(x)}{f(x)} + \frac{\frac{d^2}{dx^2}g(x)}{\frac{d}{dx}g(x)} - \frac{\frac{d}{dx}g(x)}{g(x)} \right) - \frac{v^2 g'(x)^2}{g(x)^2} \right) y(x) = 0$$

**Mathematica:** cpu = 0.859609 (sec), leaf count = 125

$$\text{DSolve}\left[-y'(x)\left(\frac{2f'(x)}{f(x)} - \frac{g'(x)}{g(x)} + \frac{g''(x)}{g'(x)}\right) + y(x)\left(-\frac{f''(x)}{f(x)} + \frac{f'(x)\left(\frac{2f'(x)}{f(x)} - \frac{g'(x)}{g(x)} + \frac{g''(x)}{g'(x)}\right)}{f(x)} - \frac{v^2 g'(x)^2}{g(x)^2}\right) + y''(x) = 0, y(x), x\right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 21

$$\{y(x) = \_C1 J_v(g(x))f(x) + \_C2 Y_v(g(x))f(x)\}$$

### 3.85 ODE No. 1085

$$\frac{d^2}{dx^2}y(x) - \left( \frac{\frac{d^2}{dx^2}g(x)}{\frac{d}{dx}g(x)} + \frac{(2v-1)\frac{d}{dx}g(x)}{g(x)} + 2\frac{\frac{d}{dx}h(x)}{h(x)} \right) \frac{d}{dx}y(x) + \left( \frac{\frac{d}{dx}h(x)}{h(x)} \left( \frac{\frac{d^2}{dx^2}g(x)}{\frac{d}{dx}g(x)} + \frac{(2v-1)\frac{d}{dx}g(x)}{g(x)} \right) \right)$$

**Mathematica:** cpu = 0.922617 (sec), leaf count = 118

$$\text{DSolve} \left[ -y'(x) \left( \frac{(2v-1)g'(x)}{g(x)} + \frac{g''(x)}{g'(x)} + \frac{2h'(x)}{h(x)} \right) + y(x) \left( g'(x)^2 + \frac{h'(x) \left( \frac{(2v-1)g'(x)}{g(x)} + \frac{g''(x)}{g'(x)} + \frac{2h'(x)}{h(x)} \right)}{h(x)} \right) \right]$$

**Maple:** cpu = 0.062 (sec), leaf count = 29

$$\{y(x) = \_C1 J_v(g(x))h(x) (g(x))^v + \_C2 Y_v(g(x))h(x) (g(x))^v\}$$

### 3.86 ODE No. 1086

$$4 \frac{d^2}{dx^2}y(x) + 9xy(x) = 0$$

**Mathematica:** cpu = 0.004501 (sec), leaf count = 42

$$\left\{ \left\{ y(x) \rightarrow c_1 \text{Ai} \left( \sqrt[3]{-1} \left( \frac{3}{2} \right)^{2/3} x \right) + c_2 \text{Bi} \left( \sqrt[3]{-1} \left( \frac{3}{2} \right)^{2/3} x \right) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 29

$$\left\{ y(x) = \_C1 \text{Ai} \left( -\frac{3^{2/3} \sqrt[3]{2} x}{2} \right) + \_C2 \text{Bi} \left( -\frac{3^{2/3} \sqrt[3]{2} x}{2} \right) \right\}$$

### 3.87 ODE No. 1087

$$4 \frac{d^2}{dx^2}y(x) - (x^2 + a)y(x) = 0$$

**Mathematica:** cpu = 0.008001 (sec), leaf count = 36

$$\left\{ \left\{ y(x) \rightarrow c_1 D_{\frac{1}{4}(-a-2)}(x) + c_2 D_{\frac{a-2}{4}}(ix) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 M_{-\frac{a}{8}, \frac{1}{4}} \left( \frac{x^2}{2} \right) \frac{1}{\sqrt{x}} + \_C2 W_{-\frac{a}{8}, \frac{1}{4}} \left( \frac{x^2}{2} \right) \frac{1}{\sqrt{x}} \right\}$$

### 3.88 ODE No. 1088

$$4 \frac{d^2}{dx^2} y(x) + 4 \left( \frac{d}{dx} y(x) \right) \tan(x) - (5 (\tan(x))^2 + 2) y(x) = 0$$

**Mathematica:** cpu = 0.102513 (sec), leaf count = 180

$$\left\{ \left\{ y(x) \rightarrow -\frac{(-1)^{7/8} 2^{5/8} c_1}{\sqrt[8]{-8 \cos^2(2x) - 16 \cos(2x) - 8}} + \frac{3(-1)^{5/8} c_2 \left( 4\sqrt{-12}^{3/4} \sinh^{-1} \left( \frac{1}{2} \sqrt{-\frac{1}{2}} \sqrt{-8 \cos^2(2x) - 16 \cos(2x) - 8} \right) \right)}{\sqrt[8]{-8 \cos^2(2x) - 16 \cos(2x) - 8}} \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 36

$$\left\{ y(x) = -C1 \frac{1}{\sqrt{\cos(x)}} + -C2 (i \cos(x) \sin(x) - \ln(\sin(x) + i \cos(x))) \frac{1}{\sqrt{\cos(x)}} \right\}$$

### 3.89 ODE No. 1089

$$a \frac{d^2}{dx^2} y(x) - (ab + c + x) \frac{d}{dx} y(x) + (b(x + c) + d) y(x) = 0$$

**Mathematica:** cpu = 0.045006 (sec), leaf count = 99

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{bx} H_d \left( \frac{x}{\sqrt{2}\sqrt{a}} - \frac{ab - c}{\sqrt{2}\sqrt{a}} \right) + c_2 e^{bx} {}_1F_1 \left( -\frac{d}{2}; \frac{1}{2}; \left( \frac{x}{\sqrt{2}\sqrt{a}} - \frac{ab - c}{\sqrt{2}\sqrt{a}} \right)^2 \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 61

$$\left\{ y(x) = -C1 e^{bx} M \left( -\frac{d}{2}, \frac{1}{2}, \frac{(ab - c - x)^2}{2a} \right) + -C2 e^{bx} U \left( -\frac{d}{2}, \frac{1}{2}, \frac{(ab - c - x)^2}{2a} \right) \right\}$$

### 3.90 ODE No. 1090

$$a^2 \frac{d^2}{dx^2} y(x) + a(a^2 - 2be^{-ax}) \frac{d}{dx} y(x) + b^2 e^{-2ax} y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.032 (sec), leaf count = 59

$$\left\{ y(x) = -C1 e^{-\frac{a^3 x + 2be^{-ax}}{2a^2}} \sinh \left( \frac{ax}{2} \right) + -C2 e^{-\frac{a^3 x + 2be^{-ax}}{2a^2}} \cosh \left( \frac{ax}{2} \right) \right\}$$

### 3.91 ODE No. 1091

$$x \left( \frac{d^2}{dx^2} y(x) + y(x) \right) - \cos(x) = 0$$

**Mathematica:** cpu = 0.022503 (sec), leaf count = 41

$$\left\{ \left\{ y(x) \rightarrow c_2 \sin(x) + c_1 \cos(x) + \frac{1}{2} (\text{Ci}(2x) \sin(x) - \text{Si}(2x) \cos(x) + \log(x) \sin(x)) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 35

$$\left\{ y(x) = \sin(x) \_C2 + \cos(x) \_C1 + \frac{\sin(x) \text{Ci}(2x)}{2} + \frac{\sin(x) \ln(x)}{2} - \frac{\text{Si}(2x) \cos(x)}{2} \right\}$$

### 3.92 ODE No. 1092

$$x \frac{d^2}{dx^2} y(x) + (x + a) y(x) = 0$$

**Mathematica:** cpu = 0.096012 (sec), leaf count = 72

$$\left\{ \left\{ y(x) \rightarrow c_2 e^{-ix} x {}_1F_1 \left( 1 - \frac{1}{4} i (-2(a-2) - 4); 2; 2ix \right) + c_1 e^{-ix} x U \left( 1 - \frac{1}{4} i (-2(a-2) - 4), 2, 2ix \right) \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 29

$$\left\{ y(x) = \_C1 M_{-\frac{i}{2}a, \frac{1}{2}}(2ix) + \_C2 W_{-\frac{i}{2}a, \frac{1}{2}}(2ix) \right\}$$

### 3.93 ODE No. 1093

$$x \frac{d^2}{dx^2} y(x) + \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.004501 (sec), leaf count = 13

$$\left\{ \left\{ y(x) \rightarrow c_1 \log(x) + c_2 \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 10

$$\left\{ y(x) = \_C2 \ln(x) + \_C1 \right\}$$

### 3.94 ODE No. 1094

$$x \frac{d^2}{dx^2} y(x) + \frac{d}{dx} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.022003 (sec), leaf count = 41

$$\left\{ \left\{ y(x) \rightarrow c_1 J_0(2\sqrt{a}\sqrt{x}) + 2c_2 Y_0(2\sqrt{a}\sqrt{x}) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 29

$$\{y(x) = \_C1 J_0(2\sqrt{a}\sqrt{x}) + \_C2 Y_0(2\sqrt{a}\sqrt{x})\}$$

### 3.95 ODE No. 1095

$$x \frac{d^2}{dx^2} y(x) + \frac{d}{dx} y(x) + lxy(x) = 0$$

**Mathematica:** cpu = 0.008501 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow c_1 J_0(\sqrt{l}x) + c_2 Y_0(\sqrt{l}x) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 23

$$\{y(x) = \_C1 J_0(\sqrt{l}x) + \_C2 Y_0(\sqrt{l}x)\}$$

### 3.96 ODE No. 1096

$$x \frac{d^2}{dx^2} y(x) + \frac{d}{dx} y(x) + (x+a)y(x) = 0$$

**Mathematica:** cpu = 0.012002 (sec), leaf count = 61

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-ix} U\left(\frac{1}{2}i(a-i), 1, 2ix\right) + c_2 e^{-ix} L_{-\frac{1}{2}i(a-i)}(2ix) \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 43

$$\left\{ y(x) = \_C1 e^{-ix} M\left(\frac{1}{2} + \frac{i}{2}a, 1, 2ix\right) + \_C2 e^{-ix} U\left(\frac{1}{2} + \frac{i}{2}a, 1, 2ix\right) \right\}$$



### 3.97 ODE No. 1097

$$x \frac{d^2}{dx^2} y(x) - \frac{d}{dx} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.026003 (sec), leaf count = 46

$$\{ \{ y(x) \rightarrow 2ac_1 x J_2(2\sqrt{a}\sqrt{x}) - 2ac_2 x Y_2(2\sqrt{a}\sqrt{x}) \} \}$$

**Maple:** cpu = 0.016 (sec), leaf count = 31

$$\{ y(x) = \_C1 x J_2(2\sqrt{a}\sqrt{x}) + \_C2 x Y_2(2\sqrt{a}\sqrt{x}) \}$$

### 3.98 ODE No. 1098

$$x \frac{d^2}{dx^2} y(x) - \frac{d}{dx} y(x) - y(x) ax^3 = 0$$

**Mathematica:** cpu = 0.008501 (sec), leaf count = 41

$$\left\{ \left\{ y(x) \rightarrow c_1 \cosh\left(\frac{\sqrt{a}x^2}{2}\right) + ic_2 \sinh\left(\frac{\sqrt{a}x^2}{2}\right) \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 27

$$\left\{ y(x) = \_C1 \sinh\left(\frac{x^2}{2}\sqrt{a}\right) + \_C2 \cosh\left(\frac{x^2}{2}\sqrt{a}\right) \right\}$$

### 3.99 ODE No. 1099

$$x \frac{d^2}{dx^2} y(x) - \frac{d}{dx} y(x) + x^3(e^{x^2} - v^2) y(x) = 0$$

**Mathematica:** cpu = 1.065635 (sec), leaf count = 36

$$\text{DSolve}\left[x^3\left(e^{x^2} - v^2\right) y(x) + xy''(x) - y'(x) = 0, y(x), x\right]$$

**Maple:** cpu = 0.031 (sec), leaf count = 25

$$\left\{ y(x) = \_C1 J_v\left(e^{\frac{x^2}{2}}\right) + \_C2 Y_v\left(e^{\frac{x^2}{2}}\right) \right\}$$

### 3.100 ODE No. 1100

$$x \frac{d^2}{dx^2} y(x) + 2 \frac{d}{dx} y(x) - xy(x) - e^x = 0$$

**Mathematica:** cpu = 0.021503 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{-x}}{x} + \frac{c_2 e^x}{2x} + \frac{e^x(2x-1)}{4x} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 23

$$\left\{ y(x) = \frac{\sinh(x) - C2}{x} + \frac{\cosh(x) - C1}{x} + \frac{e^x}{2} \right\}$$

### 3.101 ODE No. 1101

$$x \frac{d^2}{dx^2} y(x) + 2 \frac{d}{dx} y(x) + axy(x) = 0$$

**Mathematica:** cpu = 0.025503 (sec), leaf count = 51

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{-\sqrt{-ax}}}{x} + \frac{c_2 e^{\sqrt{-ax}}}{2\sqrt{-ax}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 31

$$\left\{ y(x) = \frac{-C1}{x} \sinh(\sqrt{-ax}) + \frac{-C2}{x} \cosh(\sqrt{-ax}) \right\}$$

### 3.102 ODE No. 1102

$$x \frac{d^2}{dx^2} y(x) + 2 \frac{d}{dx} y(x) + ax^2 y(x) = 0$$

**Mathematica:** cpu = 0.006001 (sec), leaf count = 42

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 \text{Ai}\left(-\frac{ax}{(-a)^{2/3}}\right)}{x} + \frac{c_2 \text{Bi}\left(-\frac{ax}{(-a)^{2/3}}\right)}{x} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 35

$$\left\{ y(x) = -C1 J_{\frac{1}{3}}\left(\frac{2}{3}\sqrt{ax^{\frac{3}{2}}}\right) \frac{1}{\sqrt{x}} + -C2 Y_{\frac{1}{3}}\left(\frac{2}{3}\sqrt{ax^{\frac{3}{2}}}\right) \frac{1}{\sqrt{x}} \right\}$$

### 3.103 ODE No. 1103

$$x \frac{d^2}{dx^2} y(x) - 2 \frac{d}{dx} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.025503 (sec), leaf count = 64

$$\left\{ \left\{ y(x) \rightarrow 6a^{3/2} c_1 x^{3/2} J_3(2\sqrt{a}\sqrt{x}) - 2ia^{3/2} c_2 x^{3/2} Y_3(2\sqrt{a}\sqrt{x}) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 x^{\frac{3}{2}} J_3(2\sqrt{a}\sqrt{x}) + \_C2 x^{\frac{3}{2}} Y_3(2\sqrt{a}\sqrt{x}) \right\}$$

### 3.104 ODE No. 1104

$$x \frac{d^2}{dx^2} y(x) + v \frac{d}{dx} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.035505 (sec), leaf count = 104

$$\left\{ \left\{ y(x) \rightarrow c_2 a^{\frac{v-1}{2}-v+1} x^{\frac{v-1}{2}-v+1} \Gamma(2-v) J_{1-v}(2\sqrt{a}\sqrt{x}) + c_1 a^{\frac{1-v}{2}} x^{\frac{1-v}{2}} \Gamma(v) J_{v-1}(2\sqrt{a}\sqrt{x}) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 47

$$\left\{ y(x) = \_C1 x^{\frac{1}{2}-\frac{v}{2}} J_{v-1}(2\sqrt{a}\sqrt{x}) + \_C2 x^{\frac{1}{2}-\frac{v}{2}} Y_{v-1}(2\sqrt{a}\sqrt{x}) \right\}$$

### 3.105 ODE No. 1105

$$x \frac{d^2}{dx^2} y(x) + a \frac{d}{dx} y(x) + bxy(x) = 0$$

**Mathematica:** cpu = 0.021003 (sec), leaf count = 64

$$\left\{ \left\{ y(x) \rightarrow c_1 x^{\frac{1-a}{2}} J_{\frac{a-1}{2}}(\sqrt{bx}) + c_2 x^{\frac{1-a}{2}} Y_{\frac{a-1}{2}}(\sqrt{bx}) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 45

$$\left\{ y(x) = \_C1 x^{-\frac{a}{2}+\frac{1}{2}} J_{\frac{a}{2}-\frac{1}{2}}(\sqrt{bx}) + \_C2 x^{-\frac{a}{2}+\frac{1}{2}} Y_{\frac{a}{2}-\frac{1}{2}}(\sqrt{bx}) \right\}$$

### 3.106 ODE No. 1106

$$x \frac{d^2}{dx^2} y(x) + a \frac{d}{dx} y(x) + bx^{a1} y(x) = 0$$

**Mathematica:** cpu = 0.054507 (sec), leaf count = 447

$$\left\{ \left\{ y(x) \rightarrow c_1 \left( \frac{1}{a1} + 1 \right)^{\frac{a}{(\frac{1}{a1}+1)a1} - \frac{1}{(\frac{1}{a1}+1)a1}} a1^{\frac{a}{(\frac{1}{a1}+1)a1} - \frac{1}{(\frac{1}{a1}+1)a1}} b^{\frac{1}{2}} \left( \frac{1}{(\frac{1}{a1}+1)a1} - \frac{a}{(\frac{1}{a1}+1)a1} \right) (x^{a1})^{\left( \frac{1}{2a1} + \frac{1}{2} \right)} \left( \frac{1}{(\frac{1}{a1}+1)a1} - \frac{1}{(\frac{1}{a1}+1)a1} \right) \right. \right.$$

**Maple:** cpu = 0.062 (sec), leaf count = 77

$$\left\{ y(x) = \_C1 x^{-\frac{a}{2} + \frac{1}{2}} J_{\frac{a-1}{a1+1}} \left( 2 \frac{\sqrt{b} x^{a1/2+1/2}}{a1+1} \right) + \_C2 x^{-\frac{a}{2} + \frac{1}{2}} Y_{\frac{a-1}{a1+1}} \left( 2 \frac{\sqrt{b} x^{a1/2+1/2}}{a1+1} \right) \right\}$$

### 3.107 ODE No. 1107

$$x \frac{d^2}{dx^2} y(x) + (x + b) \frac{d}{dx} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.030504 (sec), leaf count = 40

$$\{ \{ y(x) \rightarrow c_1 e^{-x} U(b - a, b, x) + c_2 e^{-x} L_{a-b}^{b-1}(x) \} \}$$

**Maple:** cpu = 0.062 (sec), leaf count = 33

$$\{ y(x) = \_C1 e^{-x} M(-a + b, b, x) + \_C2 e^{-x} U(-a + b, b, x) \}$$

### 3.108 ODE No. 1108

$$x \frac{d^2}{dx^2} y(x) + (x + a + b) \frac{d}{dx} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.035004 (sec), leaf count = 37

$$\{ \{ y(x) \rightarrow c_1 e^{-x} U(b, a + b, x) + c_2 e^{-x} L_{-b}^{a+b-1}(x) \} \}$$

**Maple:** cpu = 0.062 (sec), leaf count = 29

$$\{ y(x) = \_C1 e^{-x} M(b, a + b, x) + \_C2 e^{-x} U(b, a + b, x) \}$$

### 3.109 ODE No. 1109

$$x \frac{d^2}{dx^2} y(x) - x \frac{d}{dx} y(x) - y(x) - x(1+x)e^x = 0$$

**Mathematica:** cpu = 0.052507 (sec), leaf count = 45

$$\left\{ \left\{ y(x) \rightarrow c_2(-e^x x \text{Ei}(-x) - 1) + c_1 e^x x + e^x(x^2 + x - x \log(-x) - 1) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 40

$$\{y(x) = (-\text{Ei}(1, x) x + e^{-x}) e^x \_C1 + e^x \_C2 x - (x \ln(x) - x^2 + 1) e^x\}$$

### 3.110 ODE No. 1110

$$x \frac{d^2}{dx^2} y(x) - x \frac{d}{dx} y(x) - ay(x) = 0$$

**Mathematica:** cpu = 0.040505 (sec), leaf count = 36

$$\left\{ \left\{ y(x) \rightarrow c_2 G_{1,2}^{2,0} \left( -x \left| \begin{array}{c} 1-a \\ 0, 1 \end{array} \right. \right) + c_1 x {}_1F_1(a+1; 2; x) \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 23

$$\{y(x) = \_C1 x M(a+1, 2, x) + \_C2 x U(a+1, 2, x)\}$$

### 3.111 ODE No. 1111

$$x \frac{d^2}{dx^2} y(x) - (1+x) \frac{d}{dx} y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.017502 (sec), leaf count = 20

$$\left\{ \left\{ y(x) \rightarrow c_1 e^x + c_2(-x-1) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 14

$$\{y(x) = \_C1 (1+x) + \_C2 e^x\}$$

### 3.112 ODE No. 1112

$$x \frac{d^2}{dx^2} y(x) - (1+x) \frac{d}{dx} y(x) - 2(x-1)y(x) = 0$$

**Mathematica:** cpu = 0.025003 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{2x} - \frac{1}{9} c_2 e^{-x} (3x+1) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 22

$$\{y(x) = \_C1 e^{2x} + \_C2 e^{-x} (3x+1)\}$$

### 3.113 ODE No. 1113

$$x \frac{d^2}{dx^2} y(x) + (b-x) \frac{d}{dx} y(x) - ay(x) = 0$$

**Mathematica:** cpu = 0.021503 (sec), leaf count = 24

$$\{ \{ y(x) \rightarrow c_1 U(a, b, x) + c_2 L_{-a}^{b-1}(x) \} \}$$

**Maple:** cpu = 0.063 (sec), leaf count = 17

$$\{y(x) = \_C1 M(a, b, x) + \_C2 U(a, b, x)\}$$

### 3.114 ODE No. 1114

$$x \frac{d^2}{dx^2} y(x) - 2(x-1) \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.049506 (sec), leaf count = 39

$$\left\{ \left\{ y(x) \rightarrow c_2 G_{1,2}^{2,0} \left( -2x \left| \begin{array}{c} \frac{1}{2} \\ -1, 0 \end{array} \right. \right) + c_1 e^x (I_0(x) - I_1(x)) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 35

$$\{y(x) = \_C1 e^x (I_0(x) - I_1(x)) + \_C2 e^x (-K_0(-x) + K_1(-x))\}$$

### 3.115 ODE No. 1115

$$x \frac{d^2}{dx^2} y(x) - (3x - 2) \frac{d}{dx} y(x) - (2x - 3) y(x) = 0$$

**Mathematica:** cpu = 0.069009 (sec), leaf count = 76

$$\left\{ \left\{ y(x) \rightarrow c_2 e^{-\frac{1}{2}(\sqrt{17}-3)x} {}_1F_1\left(1 - \frac{6}{\sqrt{17}}; 2; \sqrt{17}x\right) + c_1 e^{-\frac{1}{2}(\sqrt{17}-3)x} U\left(1 - \frac{6}{\sqrt{17}}, 2, \sqrt{17}x\right) \right\} \right\}$$

**Maple:** cpu = 0.140 (sec), leaf count = 55

$$\left\{ y(x) = {}_C1 M\left(1 - \frac{6\sqrt{17}}{17}, 2, \sqrt{17}x\right) e^{-\frac{x(-3+\sqrt{17})}{2}} + {}_C2 U\left(1 - \frac{6\sqrt{17}}{17}, 2, \sqrt{17}x\right) e^{-\frac{x(-3+\sqrt{17})}{2}} \right\}$$

### 3.116 ODE No. 1116

$$x \frac{d^2}{dx^2} y(x) + (ax + b + n) \frac{d}{dx} y(x) + nay(x) = 0$$

**Mathematica:** cpu = 0.053507 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-ax} U(b, b + n, ax) + c_2 e^{-ax} L_{-b}^{b+n-1}(ax) \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 35

$$\left\{ y(x) = {}_C1 e^{-ax} M(b, b + n, ax) + {}_C2 e^{-ax} U(b, b + n, ax) \right\}$$

### 3.117 ODE No. 1117

$$x \frac{d^2}{dx^2} y(x) - (a + b)(1 + x) \frac{d}{dx} y(x) + abxy(x) = 0$$

**Mathematica:** cpu = 0.097512 (sec), leaf count = 107

$$\left\{ \left\{ y(x) \rightarrow c_1 U\left(-\frac{-a^2 - ba - a + b}{a - b}, a + b + 2, (a - b)x\right) e^{(a+b+1)\log(x)+bx} + c_2 L_{\frac{-a^2 - ab - a + b}{a - b}}^{a+b+1}(x(a - b)) e^{(a+b+1)\log(x)+bx} \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 91

$$\left\{ y(x) = {}_C1 e^{bx} M\left(\frac{a^2 + ab + a - b}{a - b}, a + b + 2, x(a - b)\right) x^{a+b+1} + {}_C2 e^{bx} U\left(\frac{a^2 + ab + a - b}{a - b}, a + b + 2, x(a - b)\right) x^{a+b+1} \right\}$$

### 3.118 ODE No. 1118

$$x \frac{d^2}{dx^2} y(x) + ((a+b)x + m + n) \frac{d}{dx} y(x) + (abx + na + bm) y(x) = 0$$

**Mathematica:** cpu = 0.093012 (sec), leaf count = 51

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-ax} U(m, m+n, (a-b)x) + c_2 e^{-ax} L_{-m}^{m+n-1}(x(a-b)) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 43

$$\{y(x) = \_C1 e^{-ax} M(m, m+n, x(a-b)) + \_C2 e^{-ax} U(m, m+n, x(a-b))\}$$

### 3.119 ODE No. 1119

$$x \frac{d^2}{dx^2} y(x) - 2(ax+b) \frac{d}{dx} y(x) + (a^2x + 2ab) y(x) = 0$$

**Mathematica:** cpu = 0.174522 (sec), leaf count = 77

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{ax} x^{b-\frac{1}{2}\sqrt{(2b+1)^2+\frac{1}{2}}} + \frac{c_2 e^{ax} x^{b+\frac{1}{2}\sqrt{(2b+1)^2+\frac{1}{2}}}}{\sqrt{(2b+1)^2}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 24

$$\{y(x) = \_C1 e^{ax} + \_C2 x^{2b+1} e^{ax}\}$$

### 3.120 ODE No. 1120

$$x \frac{d^2}{dx^2} y(x) + (ax+b) \frac{d}{dx} y(x) + (cx+d) y(x) = 0$$

**Mathematica:** cpu = 0.065008 (sec), leaf count = 166

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{1}{2}x(-\sqrt{a^2-4c}-a)} U\left(-\frac{-ab-\sqrt{a^2-4c}b+2d}{2\sqrt{a^2-4c}}, b, \sqrt{a^2-4c}x\right) + c_2 e^{\frac{1}{2}x(-\sqrt{a^2-4c}-a)} L_{\frac{-b\sqrt{a^2-4c}-ab}{2\sqrt{a^2-4c}}}^{b-1}\right\} \right\}$$

**Maple:** cpu = 0.140 (sec), leaf count = 123

$$\{y(x) = \_C1 e^{-\frac{x}{2}(a+\sqrt{a^2-4c})} M\left(\frac{1}{2}(b\sqrt{a^2-4c}+ab-2d), \frac{1}{\sqrt{a^2-4c}}, b, \sqrt{a^2-4c}x\right) + \_C2 e^{-\frac{x}{2}(a+\sqrt{a^2-4c})}\}$$



### 3.121 ODE No. 1121

$$x \frac{d^2}{dx^2} y(x) - (x^2 - x) \frac{d}{dx} y(x) + (x - 1) y(x) = 0$$

**Mathematica:** cpu = 10.521836 (sec), leaf count = 40

$$\left\{ \left\{ y(x) \rightarrow c_2 x \int_1^x \frac{e^{\frac{K[1]^2}{2} - K[1]}}{K[1]^2} dK[1] + c_1 x \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 26

$$\left\{ y(x) = \left( \int \frac{1}{x^2} e^{\frac{x^2}{2} - x} dx \_C1 + \_C2 \right) x \right\}$$

### 3.122 ODE No. 1122

$$x \frac{d^2}{dx^2} y(x) - (x^2 - x - 2) \frac{d}{dx} y(x) - x(x + 3) y(x) = 0$$

**Mathematica:** cpu = 10.079280 (sec), leaf count = 56

$$\left\{ \left\{ y(x) \rightarrow c_2 e^{\frac{x^2}{2}} \int_1^x \frac{e^{-\frac{1}{2}K[1]^2 - K[1]}}{K[1]^2} dK[1] + c_1 e^{\frac{x^2}{2}} \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 34

$$\left\{ y(x) = \_C1 e^{\frac{x^2}{2}} + \_C2 e^{\frac{x^2}{2}} \int \frac{1}{x^2} e^{-\frac{x(x+2)}{2}} dx \right\}$$

### 3.123 ODE No. 1123

$$x \frac{d^2}{dx^2} y(x) - (2ax^2 + 1) \frac{d}{dx} y(x) + bx^3 y(x) = 0$$

**Mathematica:** cpu = 0.012002 (sec), leaf count = 91

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{1}{2}\sqrt{b}x^2 \left( \frac{a}{\sqrt{b}} - \frac{\sqrt{a^2-b}}{\sqrt{b}} \right)} + c_2 e^{\frac{1}{2}\sqrt{b}x^2 \left( \frac{\sqrt{a^2-b}}{\sqrt{b}} + \frac{a}{\sqrt{b}} \right)} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 45

$$\left\{ y(x) = \_C1 e^{\frac{x^2}{2}(\sqrt{a^2-b}+a)} + \_C2 e^{-\frac{x^2}{2}(\sqrt{a^2-b}-a)} \right\}$$

### 3.124 ODE No. 1124

$$x \frac{d^2}{dx^2} y(x) - 2(x^2 - a) \frac{d}{dx} y(x) + 2nxy(x) = 0$$

**Mathematica:** cpu = 0.063008 (sec), leaf count = 65

$$\left\{ \left\{ y(x) \rightarrow c_1 {}_1F_1\left(-\frac{n}{2}; a + \frac{1}{2}; x^2\right) + i^{1-2a} c_2 x^{1-2a} {}_1F_1\left(-a - \frac{n}{2} + \frac{1}{2}; \frac{3}{2} - a; x^2\right) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 29

$$\left\{ y(x) = \_C1 M\left(-\frac{n}{2}, \frac{1}{2} + a, x^2\right) + \_C2 U\left(-\frac{n}{2}, \frac{1}{2} + a, x^2\right) \right\}$$

### 3.125 ODE No. 1125

$$x \frac{d^2}{dx^2} y(x) + (4x^2 - 1) \frac{d}{dx} y(x) - 4x^3 y(x) - 4x^5 = 0$$

**Mathematica:** cpu = 0.129016 (sec), leaf count = 84

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-(1-\sqrt{2})x^2} + c_2 e^{-(1+\sqrt{2})x^2} - \frac{3\sqrt{2}x^2 + 4x^2 + 6\sqrt{2} + 8}{\sqrt{2}(3 + 2\sqrt{2})} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 36

$$\left\{ y(x) = e^{x^2(\sqrt{2}-1)} \_C2 + e^{-x^2(1+\sqrt{2})} \_C1 - x^2 - 2 \right\}$$

### 3.126 ODE No. 1126

$$x \frac{d^2}{dx^2} y(x) + (2ax^3 - 1) \frac{d}{dx} y(x) + (a^2x^3 + a) x^2 y(x) = 0$$

**Mathematica:** cpu = 1.204153 (sec), leaf count = 58

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{(a^2x^3 + a) y(x) + (2x^3a - 1) y'(x) + xy''(x) = 0, y(1) = c_1, y'(1) = c_2\}) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 26

$$\left\{ y(x) = \_C1 e^{-\frac{ax^3}{3}} + \_C2 e^{-\frac{ax^3}{3}} x^2 \right\}$$

**3.127 ODE No. 1127**

$$x \frac{d^2}{dx^2} y(x) + (2ax \ln(x) + 1) \frac{d}{dx} y(x) + (a^2 x (\ln(x))^2 + a \ln(x) + a) y(x) = 0$$

**Mathematica:** cpu = 0.038505 (sec), leaf count = 36

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{ax} x^{-ax} + c_2 e^{ax} x^{-ax} \log(x) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 31

$$\{y(x) = \_C1 x^{-ax} e^{ax} + \_C2 x^{-ax} e^{ax} \ln(x)\}$$

**3.128 ODE No. 1128**

$$x \frac{d^2}{dx^2} y(x) + (xf(x) + 2) \frac{d}{dx} y(x) + f(x) y(x) = 0$$

**Mathematica:** cpu = 0.244031 (sec), leaf count = 29

$$\text{DSolve}[(xf(x) + 2)y'(x) + f(x)y(x) + xy''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.156 (sec), leaf count = 35

$$\left\{ y(x) = \frac{-C1}{x} + \frac{-C2}{x} \int e^{\int \frac{-xf(x)-2}{x} dx} x^2 dx \right\}$$

**3.129 ODE No. 1129**

$$(x - 3) \frac{d^2}{dx^2} y(x) - (4x - 9) \frac{d}{dx} y(x) + (3x - 6) y(x) = 0$$

**Mathematica:** cpu = 0.037505 (sec), leaf count = 42

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{8} c_2 e^{3x-9} (4x^3 - 42x^2 + 150x - 183) + c_1 e^{x-3} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 30

$$\{y(x) = \_C1 e^x + \_C2 e^{3x} (4x^3 - 42x^2 + 150x - 183)\}$$

**3.130 ODE No. 1130**

$$2x \frac{d^2}{dx^2} y(x) + \frac{d}{dx} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.011501 (sec), leaf count = 46

$$\left\{ \left\{ y(x) \rightarrow c_2 \sin \left( \sqrt{2} \sqrt{a} \sqrt{x} \right) + c_1 \cos \left( \sqrt{2} \sqrt{a} \sqrt{x} \right) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 31

$$\left\{ y(x) = \_C1 \sin \left( \sqrt{x} \sqrt{2} \sqrt{a} \right) + \_C2 \cos \left( \sqrt{x} \sqrt{2} \sqrt{a} \right) \right\}$$

**3.131 ODE No. 1131**

$$2x \frac{d^2}{dx^2} y(x) - (x-1) \frac{d}{dx} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.010001 (sec), leaf count = 58

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt{x} U \left( \frac{1}{2} (1-2a), \frac{3}{2}, \frac{x}{2} \right) + c_2 \sqrt{x} L_{\frac{1}{2}(2a-1)}^{\frac{1}{2}} \left( \frac{x}{2} \right) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 \sqrt{x} M \left( -a + \frac{1}{2}, \frac{3}{2}, \frac{x}{2} \right) + \_C2 \sqrt{x} U \left( -a + \frac{1}{2}, \frac{3}{2}, \frac{x}{2} \right) \right\}$$

**3.132 ODE No. 1132**

$$2x \frac{d^2}{dx^2} y(x) - (2x-1) \frac{d}{dx} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.010501 (sec), leaf count = 48

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt{x} U \left( \frac{1-a}{2}, \frac{3}{2}, x \right) + c_2 \sqrt{x} L_{\frac{a-1}{2}}^{\frac{1}{2}} (x) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 31

$$\left\{ y(x) = \_C1 \sqrt{x} M \left( -\frac{a}{2} + \frac{1}{2}, \frac{3}{2}, x \right) + \_C2 \sqrt{x} U \left( -\frac{a}{2} + \frac{1}{2}, \frac{3}{2}, x \right) \right\}$$

### 3.133 ODE No. 1133

$$(2x - 1) \frac{d^2}{dx^2} y(x) - (3x - 4) \frac{d}{dx} y(x) + (x - 3) y(x) = 0$$

**Mathematica:** cpu = 0.091011 (sec), leaf count = 92

$$\left\{ \left\{ y(x) \rightarrow 2^{5/8} c_1 e^{x-\frac{1}{2}} + \frac{c_2 e^{\frac{x}{2}-\frac{1}{2}} (\sqrt{2} e^{x/2} \sqrt[4]{2x-1} \Gamma(\frac{3}{4}, \frac{1}{4}(2x-1)) - 2\sqrt[4]{e})}{2^{5/8} \sqrt[4]{2x-1}} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 47

$$\left\{ y(x) = -C1 e^{\frac{x}{2}} M\left(1, \frac{3}{4}, \frac{x}{2} - \frac{1}{4}\right) \frac{1}{\sqrt[4]{2x-1}} + -C2 e^{\frac{x}{2}} U\left(1, \frac{3}{4}, \frac{x}{2} - \frac{1}{4}\right) \frac{1}{\sqrt[4]{2x-1}} \right\}$$

### 3.134 ODE No. 1134

$$4x \frac{d^2}{dx^2} y(x) - (x + a) y(x) = 0$$

**Mathematica:** cpu = 0.094512 (sec), leaf count = 78

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4} c_2 e^{-x/2} x {}_1F_1\left(\frac{1}{128}(-32(-a-4i)-128i)+1; 2; x\right) + \frac{1}{4} c_1 e^{-x/2} x U\left(\frac{1}{128}(-32(-a-4i)-128i)+1; 2; x\right) \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 21

$$\left\{ y(x) = -C1 M_{-\frac{a}{4}, \frac{1}{2}}(x) + -C2 W_{-\frac{a}{4}, \frac{1}{2}}(x) \right\}$$

### 3.135 ODE No. 1135

$$4x \frac{d^2}{dx^2} y(x) + 2 \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.009501 (sec), leaf count = 27

$$\left\{ \left\{ y(x) \rightarrow c_1 \cosh(\sqrt{x}) + i c_2 \sinh(\sqrt{x}) \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 17

$$\left\{ y(x) = -C1 \sinh(\sqrt{x}) + -C2 \cosh(\sqrt{x}) \right\}$$

**3.136 ODE No. 1136**

$$4x \frac{d^2}{dx^2} y(x) + 4 \frac{d}{dx} y(x) - (x+2)y(x) = 0$$

**Mathematica:** cpu = 0.020503 (sec), leaf count = 30

$$\{ \{ y(x) \rightarrow c_2 e^{x/2} \text{Ei}(-x) + c_1 e^{x/2} \} \}$$

**Maple:** cpu = 0.031 (sec), leaf count = 20

$$\{ y(x) = \_C1 e^{\frac{x}{2}} + \_C2 e^{\frac{x}{2}} \text{Ei}(1, x) \}$$

**3.137 ODE No. 1137**

$$4x \frac{d^2}{dx^2} y(x) + 4y(x) - (x+2)y(x) + ly(x) = 0$$

**Mathematica:** cpu = 0.095512 (sec), leaf count = 74

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4} c_2 e^{-x/2} x {}_1F_1 \left( \frac{1}{128} (-32(l + (2 - 4i)) - 128i) + 1; 2; x \right) + \frac{1}{4} c_1 e^{-x/2} x U \left( \frac{1}{128} (-32(l + (2 - 4i)) - 128i) + 1; 2; x \right) \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 25

$$\{ y(x) = \_C1 M_{\frac{l}{4} + \frac{1}{2}, \frac{1}{2}}(x) + \_C2 W_{\frac{l}{4} + \frac{1}{2}, \frac{1}{2}}(x) \}$$

**3.138 ODE No. 1138**

$$4x \frac{d^2}{dx^2} y(x) + 4m \frac{d}{dx} y(x) - (x - 2m - 4n)y(x) = 0$$

**Mathematica:** cpu = 0.030504 (sec), leaf count = 38

$$\{ \{ y(x) \rightarrow c_1 e^{-x/2} U(-n, m, x) + c_2 e^{-x/2} L_n^{m-1}(x) \} \}$$

**Maple:** cpu = 0.062 (sec), leaf count = 29

$$\{ y(x) = \_C1 e^{-\frac{x}{2}} M(-n, m, x) + \_C2 e^{-\frac{x}{2}} U(-n, m, x) \}$$

### 3.139 ODE No. 1139

$$16x \frac{d^2}{dx^2} y(x) + 8 \frac{d}{dx} y(x) - (x+a)y(x) = 0$$

**Mathematica:** cpu = 0.012502 (sec), leaf count = 74

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{1}{4}(2\log(x)-x)} U\left(\frac{a+6}{8}, \frac{3}{2}, \frac{x}{2}\right) + c_2 e^{\frac{1}{4}(2\log(x)-x)} L_{\frac{1}{8}(-a-6)}\left(\frac{x}{2}\right) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 43

$$\left\{ y(x) = \_C1 \sqrt{x} e^{-\frac{x}{4}} M\left(\frac{a}{8} + \frac{3}{4}, \frac{3}{2}, \frac{x}{2}\right) + \_C2 \sqrt{x} e^{-\frac{x}{4}} U\left(\frac{a}{8} + \frac{3}{4}, \frac{3}{2}, \frac{x}{2}\right) \right\}$$

### 3.140 ODE No. 1140

$$ax \frac{d^2}{dx^2} y(x) + b \frac{d}{dx} y(x) + cy(x) = 0$$

**Mathematica:** cpu = 0.049006 (sec), leaf count = 190

$$\left\{ \left\{ y(x) \rightarrow c_1 a^{\frac{1}{2}(\frac{b}{a}-1)} c^{\frac{1}{2}(1-\frac{b}{a})} x^{\frac{1}{2}(1-\frac{b}{a})} \Gamma\left(\frac{b}{a}\right) J_{\frac{b}{a}-1}\left(\frac{2\sqrt{c}\sqrt{x}}{\sqrt{a}}\right) + c_2 a^{\frac{1}{2}(1-\frac{b}{a})-\frac{a-b}{a}} c^{\frac{a-b}{a}+\frac{1}{2}(\frac{b}{a}-1)} x^{\frac{a-b}{a}+\frac{1}{2}(\frac{b}{a}-1)} \Gamma\left(\frac{b}{a}\right) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 77

$$\left\{ y(x) = \_C1 x^{\frac{a-b}{2a}} J_{-\frac{a+b}{a}}\left(2\sqrt{\frac{c}{a}}\sqrt{x}\right) + \_C2 x^{\frac{a-b}{2a}} Y_{-\frac{a+b}{a}}\left(2\sqrt{\frac{c}{a}}\sqrt{x}\right) \right\}$$

### 3.141 ODE No. 1141

$$ax \frac{d^2}{dx^2} y(x) + (bx+3a) \frac{d}{dx} y(x) + 3by(x) = 0$$

**Mathematica:** cpu = 0.107514 (sec), leaf count = 70

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 e^{-\frac{bx}{a}} \left( b^2 x^2 \text{Ei}\left(\frac{bx}{a}\right) - a e^{\frac{bx}{a}} (a+bx) \right)}{2a^2 x^2} + c_1 e^{-\frac{bx}{a}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 49

$$\left\{ y(x) = \_C1 e^{-\frac{bx}{a}} + \_C2 \left( \frac{a(bx+a)}{x^2} + e^{-\frac{bx}{a}} \text{Ei}\left(1, -\frac{bx}{a}\right) b^2 \right) \right\}$$

### 3.142 ODE No. 1142

$$5(ax+b) \frac{d^2}{dx^2} y(x) + 8a \frac{d}{dx} y(x) + c\sqrt[5]{ax+b} y(x) = 0$$

**Mathematica:** cpu = 0.047006 (sec), leaf count = 108

$$\left\{ \left\{ y(x) \rightarrow \frac{3ac_2 \sin\left(\frac{\sqrt{5}\sqrt{c}(ax+b)^{3/5}}{3a}\right)}{\sqrt{5}\sqrt{c}(ax+b)^{3/5}} + \frac{6ac_1 \cos\left(\frac{\sqrt{5}\sqrt{c}(ax+b)^{3/5}}{3a}\right)}{\sqrt{5}\sqrt{c}(ax+b)^{3/5}} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 59

$$\left\{ y(x) = \_C1 \sinh\left(\frac{1}{3a}(ax+b)^{3/5} \sqrt{-5c}\right) (ax+b)^{-3/5} + \_C2 \cosh\left(\frac{1}{3a}(ax+b)^{3/5} \sqrt{-5c}\right) (ax+b)^{-3/5} \right\}$$

### 3.143 ODE No. 1143

$$2ax \frac{d^2}{dx^2} y(x) + (bx+a) \frac{d}{dx} y(x) + cy(x) = 0$$

**Mathematica:** cpu = 0.045006 (sec), leaf count = 93

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{a \log(x)-bx}{2a}} U\left(-\frac{c-b}{b}, \frac{3}{2}, \frac{bx}{2a}\right) + c_2 e^{\frac{a \log(x)-bx}{2a}} L_{\frac{c-b}{b}}^{\frac{1}{2}}\left(\frac{bx}{2a}\right) \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 67

$$\left\{ y(x) = \_C1 e^{-\frac{bx}{2a}} M\left(\frac{b-c}{b}, \frac{3}{2}, \frac{bx}{2a}\right) \sqrt{x} + \_C2 e^{-\frac{bx}{2a}} U\left(\frac{b-c}{b}, \frac{3}{2}, \frac{bx}{2a}\right) \sqrt{x} \right\}$$

### 3.144 ODE No. 1144

$$2ax \frac{d^2}{dx^2} y(x) + (bx+3a) \frac{d}{dx} y(x) + cy(x) = 0$$

**Mathematica:** cpu = 0.039505 (sec), leaf count = 88

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-\frac{bx}{2a}} U\left(-\frac{2c-3b}{2b}, \frac{3}{2}, \frac{bx}{2a}\right) + c_2 e^{-\frac{bx}{2a}} L_{\frac{2c-3b}{2b}}^{\frac{1}{2}}\left(\frac{bx}{2a}\right) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 67

$$\left\{ y(x) = \_C1 e^{-\frac{bx}{2a}} M\left(\frac{3b-2c}{2b}, \frac{3}{2}, \frac{bx}{2a}\right) + \_C2 e^{-\frac{bx}{2a}} U\left(\frac{3b-2c}{2b}, \frac{3}{2}, \frac{bx}{2a}\right) \right\}$$



### 3.145 ODE No. 1145

$$(a2 x + b2) \frac{d^2}{dx^2} y(x) + (a1 x + b1) \frac{d}{dx} y(x) + (a0 x + b0) y(x) = 0$$

**Mathematica:** cpu = 0.387049 (sec), leaf count = 398

$$\left\{ \left\{ y(x) \rightarrow c_1 U \left( -\frac{b2a1^2 - a2b1a1 - \sqrt{a1^2 - 4a0a2}b2a1 + 2a2^2b0 + a2\sqrt{a1^2 - 4a0a2}b1 - 2a0a2b2 - 2a2^2b0}{2a2^2\sqrt{a1^2 - 4a0a2}} \right) \right\} \right\}$$

**Maple:** cpu = 0.141 (sec), leaf count = 287

$$\left\{ y(x) = -C1 e^{-\frac{x}{2a2}(\sqrt{-4a0a2+a1^2}+a1)} M\left(\frac{1}{2a2^2}\left((a1b2+2a2^2-a2b1)\sqrt{-4a0a2+a1^2}-2a2^2b0\right)\right) \right\}$$

### 3.146 ODE No. 1146

$$x^2 \frac{d^2}{dx^2} y(x) - 6 y(x) = 0$$

**Mathematica:** cpu = 0.022503 (sec), leaf count = 18

$$\left\{ \left\{ y(x) \rightarrow c_1 x^3 + \frac{c_2}{x^2} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 15

$$\left\{ y(x) = \frac{-C1}{x^2} + -C2 x^3 \right\}$$

### 3.147 ODE No. 1147

$$x^2 \frac{d^2}{dx^2} y(x) - 12 y(x) = 0$$

**Mathematica:** cpu = 0.016002 (sec), leaf count = 18

$$\left\{ \left\{ y(x) \rightarrow c_1 x^4 + \frac{c_2}{x^3} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 15

$$\left\{ y(x) = -C1 x^4 + \frac{-C2}{x^3} \right\}$$

### 3.148 ODE No. 1148

$$x^2 \frac{d^2}{dx^2} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.009501 (sec), leaf count = 77

$$\left\{ \left\{ y(x) \rightarrow c_1 x^{\frac{1}{2} \left( \frac{1}{\sqrt{a}} - \frac{\sqrt{1-4a}}{\sqrt{a}} \right)} \sqrt{a} + c_2 x^{\frac{1}{2} \left( \frac{\sqrt{1-4a}}{\sqrt{a}} + \frac{1}{\sqrt{a}} \right)} \sqrt{a} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 x^{\frac{1}{2} + \frac{1}{2} \sqrt{1-4a}} + \_C2 x^{\frac{1}{2} - \frac{1}{2} \sqrt{1-4a}} \right\}$$

### 3.149 ODE No. 1149

$$x^2 \frac{d^2}{dx^2} y(x) + (ax + b) y(x) = 0$$

**Mathematica:** cpu = 0.075510 (sec), leaf count = 212

$$\left\{ \left\{ y(x) \rightarrow c_2 a^{\frac{1}{2}(\sqrt{1-4b}+1) - \frac{1}{2}\sqrt{1-4b}} x^{\frac{1}{2}(\sqrt{1-4b}+1) - \frac{1}{2}\sqrt{1-4b}} \Gamma(\sqrt{1-4b} + 1) J_{\sqrt{1-4b}}(2\sqrt{a}\sqrt{x}) + c_1 a^{\frac{1}{2}(1-\sqrt{1-4b}) + \frac{1}{2}\sqrt{1-4b}} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 47

$$\left\{ y(x) = \_C1 \sqrt{x} J_{\sqrt{1-4b}}(2\sqrt{a}\sqrt{x}) + \_C2 \sqrt{x} Y_{\sqrt{1-4b}}(2\sqrt{a}\sqrt{x}) \right\}$$

### 3.150 ODE No. 1150

$$x^2 \frac{d^2}{dx^2} y(x) + (x^2 - 2) y(x) = 0$$

**Mathematica:** cpu = 0.009001 (sec), leaf count = 53

$$\left\{ \left\{ y(x) \rightarrow \sqrt{\frac{2}{\pi}} c_2 \left( -\sin(x) - \frac{\cos(x)}{x} \right) + \sqrt{\frac{2}{\pi}} c_1 \left( \frac{\sin(x)}{x} - \cos(x) \right) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 31

$$\left\{ y(x) = \frac{\_C1 (\cos(x) x - \sin(x))}{x} + \frac{\_C2 (\cos(x) + x \sin(x))}{x} \right\}$$

**3.151 ODE No. 1151**

$$x^2 \frac{d^2}{dx^2} y(x) - (ax^2 + 2) y(x) = 0$$

**Mathematica:** cpu = 0.018002 (sec), leaf count = 129

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt{\frac{2}{\pi}} c_2 \sqrt{x} \left( i \sinh(\sqrt{ax}) - \frac{i \cosh(\sqrt{ax})}{\sqrt{ax}} \right)}{\sqrt{-i\sqrt{ax}}} + \frac{\sqrt{\frac{2}{\pi}} c_1 \sqrt{x} \left( \frac{\sinh(\sqrt{ax})}{\sqrt{ax}} - \cosh(\sqrt{ax}) \right)}{\sqrt{-i\sqrt{ax}}} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 43

$$\left\{ y(x) = \frac{C1}{x} e^{\sqrt{ax}} (-ax + \sqrt{a}) + \frac{C2}{x} e^{-\sqrt{ax}} (ax + \sqrt{a}) \right\}$$

**3.152 ODE No. 1152**

$$x^2 \frac{d^2}{dx^2} y(x) + (a^2 x^2 - 6) y(x) = 0$$

**Mathematica:** cpu = 0.018502 (sec), leaf count = 114

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt{\frac{2}{\pi}} c_1 \sqrt{x} \left( \frac{3 \sin(ax)}{a^2 x^2} - \sin(ax) - \frac{3 \cos(ax)}{ax} \right)}{\sqrt{ax}} + \frac{\sqrt{\frac{2}{\pi}} c_2 \sqrt{x} \left( -\frac{3 \cos(ax)}{a^2 x^2} - \frac{3 \sin(ax)}{ax} + \cos(ax) \right)}{\sqrt{ax}} \right\} \right\}$$

**Maple:** cpu = 0.171 (sec), leaf count = 67

$$\left\{ y(x) = \frac{-C1 (\cos(ax) a^2 x^2 - 3 \sin(ax) xa - 3 \cos(ax))}{x^2} + \frac{C2 (\sin(ax) a^2 x^2 + 3 \cos(ax) xa - 3 \sin(ax))}{x^2} \right\}$$

**3.153 ODE No. 1153**

$$x^2 \frac{d^2}{dx^2} y(x) + (ax^2 - v(v - 1)) y(x) = 0$$

**Mathematica:** cpu = 0.033504 (sec), leaf count = 56

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt{x} J_{\frac{1}{2}(2v-1)}(\sqrt{ax}) + c_2 \sqrt{x} Y_{\frac{1}{2}(2v-1)}(\sqrt{ax}) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 33

$$\left\{ y(x) = -C1 \sqrt{x} J_{v-\frac{1}{2}}(\sqrt{ax}) + -C2 \sqrt{x} Y_{v-\frac{1}{2}}(\sqrt{ax}) \right\}$$

### 3.154 ODE No. 1154

$$x^2 \frac{d^2}{dx^2} y(x) + (ax^2 + bx + c) y(x) = 0$$

**Mathematica:** cpu = 0.020002 (sec), leaf count = 88

$$\left\{ \left\{ y(x) \rightarrow c_1 M_{-\frac{ib}{2\sqrt{a}}, -\frac{1}{2}i\sqrt{4c-1}}(2i\sqrt{ax}) + c_2 W_{-\frac{ib}{2\sqrt{a}}, -\frac{1}{2}i\sqrt{4c-1}}(2i\sqrt{ax}) \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 57

$$\left\{ y(x) = \_C1 M_{-\frac{i}{2}b\frac{1}{\sqrt{a}}, \frac{1}{2}\sqrt{1-4c}}(2i\sqrt{ax}) + \_C2 W_{-\frac{i}{2}b\frac{1}{\sqrt{a}}, \frac{1}{2}\sqrt{1-4c}}(2i\sqrt{ax}) \right\}$$

### 3.155 ODE No. 1155

$$x^2 \frac{d^2}{dx^2} y(x) + (ax^k - b(b-1)) y(x) = 0$$

**Mathematica:** cpu = 0.052507 (sec), leaf count = 225

$$\left\{ \left\{ y(x) \rightarrow c_1 k^{-\frac{2(1-b)}{k} - \frac{2b}{k} + \frac{1}{k}} a^{\frac{1-b}{k} + \frac{1}{2}\left(\frac{2b}{k} - \frac{1}{k}\right)} (x^k)^{\frac{1-b}{k} + \frac{1}{2}\left(\frac{2b}{k} - \frac{1}{k}\right)} \Gamma\left(-\frac{2b}{k} + \frac{1}{k} + 1\right) J_{\frac{1-2b}{k}}\left(\frac{2\sqrt{a}\sqrt{x^k}}{k}\right) + c_2 k^{-1/k} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 69

$$\left\{ y(x) = \_C1 \sqrt{x} J_{\frac{1}{k}\sqrt{(2b-1)^2}}\left(2\frac{\sqrt{ax^{k/2}}}{k}\right) + \_C2 \sqrt{x} Y_{\frac{1}{k}\sqrt{(2b-1)^2}}\left(2\frac{\sqrt{ax^{k/2}}}{k}\right) \right\}$$

### 3.156 ODE No. 1156

$$x^2 \frac{d^2}{dx^2} y(x) + \frac{y(x)}{\ln(x)} - xe^x(2 + x \ln(x)) = 0$$

**Mathematica:** cpu = 0.207026 (sec), leaf count = 34

$$\text{DSolve}\left[x^2 y''(x) + \frac{y(x)}{\log(x)} - e^x x(x \log(x) + 2) = 0, y(x), x\right]$$

**Maple:** cpu = 0.093 (sec), leaf count = 73

$$\left\{ y(x) = \ln(x) \_C2 + (-Ei(1, -\ln(x)) \ln(x) - x) \_C1 - \left( - \int \frac{(Ei(1, -\ln(x)) \ln(x) + x) e^x (2 + x \ln(x))}{x} dx \right) \right\}$$

**3.157 ODE No. 1157**

$$x^2 \frac{d^2}{dx^2} y(x) + a \frac{d}{dx} y(x) - xy(x) = 0$$

**Mathematica:** cpu = 0.501564 (sec), leaf count = 46

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{y''(x)x^2 - y(x)x + ay'(x) = 0, y(1) = c_1, y'(1) = c_2\}) (x) \right\} \right\}$$

**Maple:** cpu = 0.140 (sec), leaf count = 32

$$\left\{ y(x) = \text{DESol} \left( \left\{ \frac{d^2}{dx^2} Y(x) + \frac{a \frac{d}{dx} Y(x)}{x^2} - \frac{Y(x)}{x} \right\}, \{ \_Y(x) \} \right) \right\}$$

**3.158 ODE No. 1158**

$$x^2 \frac{d^2}{dx^2} y(x) + a \frac{d}{dx} y(x) - (b^2 x^2 + ab) y(x) = 0$$

**Mathematica:** cpu = 8.381064 (sec), leaf count = 42

$$\left\{ \left\{ y(x) \rightarrow c_2 e^{bx} \int_1^x e^{\frac{a}{K[1]} - 2bK[1]} dK[1] + c_1 e^{bx} \right\} \right\}$$

**Maple:** cpu = 0.172 (sec), leaf count = 180

$$\left\{ y(x) = \_C1 e^{\frac{-bx^2+a}{x}} \text{HeunD} \left( 4\sqrt{2}\sqrt{ab}, -1 - 4\sqrt{2}\sqrt{ab}, 8\sqrt{2}\sqrt{ab}, -4\sqrt{2}\sqrt{ab} + 1, 1 \left( \sqrt{2}\sqrt{ab}x - a \right) \left( \sqrt{2}\sqrt{ab}x - a \right) \right) \right\}$$

**3.159 ODE No. 1159**

$$x^2 \frac{d^2}{dx^2} y(x) + x \frac{d}{dx} y(x) - y(x) - ax^2 = 0$$

**Mathematica:** cpu = 0.014502 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow \frac{ax^2}{3} + \frac{c_1(x^2 + 1)}{2x} + \frac{ic_2(x^2 - 1)}{2x} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 19

$$\left\{ y(x) = x\_C2 + \frac{ax^2}{3} + \frac{C1}{x} \right\}$$

**3.160 ODE No. 1160**

$$x^2 \frac{d^2}{dx^2} y(x) + x \frac{d}{dx} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.008501 (sec), leaf count = 30

$$\{ \{ y(x) \rightarrow c_2 \sin(\sqrt{a} \log(x)) + c_1 \cos(\sqrt{a} \log(x)) \} \}$$

**Maple:** cpu = 0.016 (sec), leaf count = 23

$$\{ y(x) = \_C1 \sin(\sqrt{a} \ln(x)) + \_C2 \cos(\sqrt{a} \ln(x)) \}$$

**3.161 ODE No. 1161**

$$x^2 \frac{d^2}{dx^2} y(x) + x \frac{d}{dx} y(x) - (x+a)y(x) = 0$$

**Mathematica:** cpu = 0.047506 (sec), leaf count = 78

$$\left\{ \left\{ y(x) \rightarrow (-1)^{-\sqrt{a}} c_1 \Gamma(1 - 2\sqrt{a}) I_{-2\sqrt{a}}(2\sqrt{x}) + (-1)^{\sqrt{a}} c_2 \Gamma(2\sqrt{a} + 1) I_{2\sqrt{a}}(2\sqrt{x}) \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 31

$$\{ y(x) = \_C1 I_{2\sqrt{a}}(2\sqrt{x}) + \_C2 K_{2\sqrt{a}}(2\sqrt{x}) \}$$

**3.162 ODE No. 1162**

$$x^2 \frac{d^2}{dx^2} y(x) + x \frac{d}{dx} y(x) + (-v^2 + x^2) y(x) = 0$$

**Mathematica:** cpu = 0.057007 (sec), leaf count = 18

$$\{ \{ y(x) \rightarrow c_1 J_v(x) + c_2 Y_v(x) \} \}$$

**Maple:** cpu = 0.0 (sec), leaf count = 15

$$\{ y(x) = \_C1 J_v(x) + \_C2 Y_v(x) \}$$

### 3.163 ODE No. 1163

$$x^2 \frac{d^2}{dx^2} y(x) + x \frac{d}{dx} y(x) + (-v^2 + x^2) y(x) - f(x) = 0$$

**Mathematica:** cpu = 0.353045 (sec), leaf count = 70

$$\left\{ \left\{ y(x) \rightarrow J_v(x) \int_1^x -\frac{\pi f(K[1]) Y_v(K[1])}{2K[1]} dK[1] + Y_v(x) \int_1^x \frac{\pi f(K[2]) J_v(K[2])}{2K[2]} dK[2] + c_1 J_v(x) + c_2 Y_v(x) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 50

$$\left\{ y(x) = J_v(x) \_C2 + Y_v(x) \_C1 - \frac{\pi}{2} \left( J_v(x) \int \frac{Y_v(x) f(x)}{x} dx - Y_v(x) \int \frac{J_v(x) f(x)}{x} dx \right) \right\}$$

### 3.164 ODE No. 1164

$$x^2 \frac{d^2}{dx^2} y(x) + x \frac{d}{dx} y(x) + (lx^2 - v^2) y(x) = 0$$

**Mathematica:** cpu = 0.028004 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow c_1 J_v(\sqrt{lx}) + c_2 Y_v(\sqrt{lx}) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 23

$$\left\{ y(x) = \_C1 J_v(\sqrt{lx}) + \_C2 Y_v(\sqrt{lx}) \right\}$$

### 3.165 ODE No. 1165

$$x^2 \frac{d^2}{dx^2} y(x) + (x + a) \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.054507 (sec), leaf count = 37

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1(a+x)}{a+1} - \frac{c_2 x e^{a/x}}{a^2(a+1)} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 19

$$\left\{ y(x) = (x+a) \_C1 + \_C2 x e^{\frac{a}{x}} \right\}$$

**3.166 ODE No. 1166**

$$x^2 \frac{d^2}{dx^2} y(x) - x \frac{d}{dx} y(x) + y(x) - 3x^3 = 0$$

**Mathematica:** cpu = 0.012502 (sec), leaf count = 23

$$\left\{ \left\{ y(x) \rightarrow c_1 x + c_2 x \log(x) + \frac{3x^3}{4} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 18

$$\left\{ y(x) = x\_C2 + x \ln(x) \_C1 + \frac{3x^3}{4} \right\}$$

**3.167 ODE No. 1167**

$$x^2 \frac{d^2}{dx^2} y(x) - x \frac{d}{dx} y(x) + (ax^m + b) y(x) = 0$$

**Mathematica:** cpu = 0.082010 (sec), leaf count = 326

$$\left\{ \left\{ y(x) \rightarrow c_1 m^{-\frac{2(m-i\sqrt{b-1}m)}{m^2} - \frac{2i\sqrt{b-1}}{m}} a^{\frac{m-i\sqrt{b-1}m}{m^2} + \frac{i\sqrt{b-1}}{m}} (x^m)^{\frac{m-i\sqrt{b-1}m}{m^2} + \frac{i\sqrt{b-1}}{m}} \Gamma\left(1 - \frac{2i\sqrt{b-1}}{m}\right) J_{-\frac{2i\sqrt{b-1}}{m}}\left(\frac{2\sqrt{a}x}{m}\right) \right. \right.$$

**Maple:** cpu = 0.031 (sec), leaf count = 63

$$\left. \left\{ y(x) = \_C1 x J_{\frac{\sqrt{1-b}}{m}}\left(2 \frac{\sqrt{a}x^{m/2}}{m}\right) + \_C2 x Y_{\frac{\sqrt{1-b}}{m}}\left(2 \frac{\sqrt{a}x^{m/2}}{m}\right) \right\} \right\}$$

**3.168 ODE No. 1168**

$$x^2 \frac{d^2}{dx^2} y(x) + 2x \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.004501 (sec), leaf count = 15

$$\left\{ \left\{ y(x) \rightarrow c_2 - \frac{c_1}{x} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 11

$$\left\{ y(x) = \_C1 + \frac{\_C2}{x} \right\}$$



### 3.169 ODE No. 1169

$$x^2 \frac{d^2}{dx^2} y(x) + 2x \frac{d}{dx} y(x) + (ax - b^2) y(x) = 0$$

**Mathematica:** cpu = 0.069509 (sec), leaf count = 236

$$\left\{ \left\{ y(x) \rightarrow c_1 a^{\frac{1}{2}(-\sqrt{4b^2+1}-1) + \frac{1}{2}\sqrt{4b^2+1}} x^{\frac{1}{2}(-\sqrt{4b^2+1}-1) + \frac{1}{2}\sqrt{4b^2+1}} \Gamma\left(1 - \sqrt{4b^2+1}\right) J_{-\sqrt{4b^2+1}}(2\sqrt{a}\sqrt{x}) + c_2 a^{\frac{1}{2}(\sqrt{4b^2+1}-1) + \frac{1}{2}\sqrt{4b^2+1}} x^{\frac{1}{2}(\sqrt{4b^2+1}-1) + \frac{1}{2}\sqrt{4b^2+1}} \Gamma\left(1 + \sqrt{4b^2+1}\right) Y_{-\sqrt{4b^2+1}}(2\sqrt{a}\sqrt{x}) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 51

$$\left\{ y(x) = -C1 J_{\sqrt{4b^2+1}}(2\sqrt{a}\sqrt{x}) \frac{1}{\sqrt{x}} + -C2 Y_{\sqrt{4b^2+1}}(2\sqrt{a}\sqrt{x}) \frac{1}{\sqrt{x}} \right\}$$

### 3.170 ODE No. 1170

$$x^2 \frac{d^2}{dx^2} y(x) + 2x \frac{d}{dx} y(x) + (ax^2 + b) y(x) = 0$$

**Mathematica:** cpu = 0.022503 (sec), leaf count = 58

$$\left\{ \left\{ y(x) \rightarrow c_1 j_{\frac{1}{2}(\sqrt{1-4b}-1)}(\sqrt{ax}) + c_2 y_{\frac{1}{2}(\sqrt{1-4b}-1)}(\sqrt{ax}) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 45

$$\left\{ y(x) = -C1 J_{\frac{1}{2}\sqrt{1-4b}}(\sqrt{ax}) \frac{1}{\sqrt{x}} + -C2 Y_{\frac{1}{2}\sqrt{1-4b}}(\sqrt{ax}) \frac{1}{\sqrt{x}} \right\}$$

### 3.171 ODE No. 1171

$$x^2 \frac{d^2}{dx^2} y(x) + 2x \frac{d}{dx} y(x) + (lx^2 + ax - n(n+1)) y(x) = 0$$

**Mathematica:** cpu = 0.054007 (sec), leaf count = 142

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{n \log(x) - i\sqrt{l}x} U\left(\frac{i(a - 2i\sqrt{l}n - 2i\sqrt{l})}{2\sqrt{l}}, 2n + 2, 2i\sqrt{l}x\right) + c_2 e^{n \log(x) - i\sqrt{l}x} L_{-\frac{i(a - 2i\sqrt{l}n - 2i\sqrt{l})}{2\sqrt{l}}}^{2n+1}(2i\sqrt{l}x) \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 51

$$\left\{ y(x) = \frac{-C1}{x} M_{-\frac{i}{2}a\frac{1}{\sqrt{l}}, n+\frac{1}{2}}(2i\sqrt{l}x) + \frac{-C2}{x} W_{-\frac{i}{2}a\frac{1}{\sqrt{l}}, n+\frac{1}{2}}(2i\sqrt{l}x) \right\}$$

### 3.172 ODE No. 1172

$$x^2 \frac{d^2}{dx^2} y(x) + 2(x-1) \frac{d}{dx} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.055007 (sec), leaf count = 158

$$\left\{ \left\{ y(x) \rightarrow 2^{\frac{1}{2}(1-\sqrt{1-4a})} c_1 \left(\frac{1}{x}\right)^{\frac{1}{2}(1-\sqrt{1-4a})} {}_1F_1\left(\frac{1}{2} - \frac{1}{2}\sqrt{1-4a}; 1 - \sqrt{1-4a}; -\frac{2}{x}\right) + 2^{\frac{1}{2}(\sqrt{1-4a}+1)} c_2 \left(\frac{1}{x}\right)^{\frac{1}{2}(\sqrt{1-4a}+1)} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 57

$$\left\{ y(x) = \_C1 e^{-x^{-1}} \sqrt{x^{-1}} I_{\frac{1}{2}\sqrt{1-4a}}(x^{-1}) + \_C2 e^{-x^{-1}} \sqrt{x^{-1}} K_{\frac{1}{2}\sqrt{1-4a}}(x^{-1}) \right\}$$

### 3.173 ODE No. 1173

$$x^2 \frac{d^2}{dx^2} y(x) + 2(x+a) \frac{d}{dx} y(x) - b(b-1)y(x) = 0$$

**Mathematica:** cpu = 0.060508 (sec), leaf count = 74

$$\left\{ \left\{ y(x) \rightarrow (-2)^{1-b} c_1 a^{1-b} \left(\frac{1}{x}\right)^{1-b} {}_1F_1\left(1-b; 2-2b; \frac{2a}{x}\right) + (-2)^b c_2 a^b \left(\frac{1}{x}\right)^b {}_1F_1\left(b; 2b; \frac{2a}{x}\right) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 45

$$\left\{ y(x) = \_C1 e^{\frac{a}{x}} I_{b-\frac{1}{2}}\left(\frac{a}{x}\right) \frac{1}{\sqrt{x}} + \_C2 e^{\frac{a}{x}} K_{b-\frac{1}{2}}\left(\frac{a}{x}\right) \frac{1}{\sqrt{x}} \right\}$$

### 3.174 ODE No. 1174

$$x^2 \frac{d^2}{dx^2} y(x) - 2x \frac{d}{dx} y(x) + 2y(x) - x^5 \ln(x) = 0$$

**Mathematica:** cpu = 0.018002 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow c_2 x^2 + c_1 x + \frac{1}{144} (12x^5 \log(x) - 7x^5) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 24

$$\left\{ y(x) = x \_C2 + \_C1 x^2 + \frac{x^5 (12 \ln(x) - 7)}{144} \right\}$$

### 3.175 ODE No. 1175

$$x^2 \frac{d^2}{dx^2} y(x) - 2x \frac{d}{dx} y(x) - 4y(x) - x \sin(x) - (ax^2 + 12a + 4) \cos(x) = 0$$

**Mathematica:** cpu = 0.157020 (sec), leaf count = 38

$$\left\{ \left\{ y(x) \rightarrow \frac{-2a \sin(x) - ax \cos(x) - \sin(x)}{x} + c_2 x^4 + \frac{c_1}{x} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 33

$$\left\{ y(x) = \frac{C1}{x} + x^4 C2 - \frac{ax \cos(x) + 2 \sin(x) a + \sin(x)}{x} \right\}$$

### 3.176 ODE No. 1176

$$x^2 \frac{d^2}{dx^2} y(x) - 2x \frac{d}{dx} y(x) + (x^2 + 2) y(x) = 0$$

**Mathematica:** cpu = 0.017502 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-ix} x - \frac{1}{2} i c_2 e^{ix} x \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 15

$$\{y(x) = \_C1 x \sin(x) + \_C2 \cos(x) x\}$$

### 3.177 ODE No. 1177

$$x^2 \frac{d^2}{dx^2} y(x) - 2x \frac{d}{dx} y(x) + (x^2 + 2) y(x) - \frac{x^2}{\cos(x)} = 0$$

**Mathematica:** cpu = 174.646177 (sec), leaf count = 136

$$\left\{ \left\{ y(x) \rightarrow c_2 \int_1^x e^{\frac{2}{K[1]} - K[1]} K[1]^2 dK[1] + \int_1^x \frac{e^{K[2] - \frac{2}{K[2]}} \sec(K[2]) \left( \int_1^{K[2]} e^{\frac{2}{K[1]} - K[1]} K[1]^2 dK[1] \right)}{K[2]^2} dK[2] \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 39

$$\left\{ y(x) = x \sin(x) \_C2 + \cos(x) x \_C1 + x \left( \ln(x) \sin(x) - \int \frac{\sin(x)}{\cos(x) x} dx \cos(x) \right) \right\}$$

**3.178 ODE No. 1178**

$$x^2 \frac{d^2}{dx^2} y(x) - 2x \frac{d}{dx} y(x) + (x^2 + 2) y(x) - \frac{x^3}{\cos(x)} = 0$$

**Mathematica:** cpu = 0.052507 (sec), leaf count = 74

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-ix} x - \frac{1}{2} i c_2 e^{ix} x + \frac{1}{2} e^{-ix} x (e^{2ix} \log(1 + e^{-2ix}) + \log(1 + e^{2ix})) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 28

$$\{y(x) = x \sin(x) \_C2 + \cos(x) x \_C1 + x(x \sin(x) + \ln(\cos(x)) \cos(x))\}$$

**3.179 ODE No. 1179**

$$x^2 \frac{d^2}{dx^2} y(x) - 2x \frac{d}{dx} y(x) + (a^2 x^2 + 2) y(x) = 0$$

**Mathematica:** cpu = 0.040005 (sec), leaf count = 53

$$\left\{ \left\{ y(x) \rightarrow c_1 x e^{-\sqrt{-a^2} x} + \frac{c_2 x e^{\sqrt{-a^2} x}}{2\sqrt{-a^2}} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 19

$$\{y(x) = \_C1 x \sin(ax) + \_C2 x \cos(ax)\}$$

**3.180 ODE No. 1180**

$$x^2 \frac{d^2}{dx^2} y(x) + 3x \frac{d}{dx} y(x) + (-v^2 + x^2 + 1) y(x) - f(x) = 0$$

**Mathematica:** cpu = 0.231029 (sec), leaf count = 73

$$\left\{ \left\{ y(x) \rightarrow \frac{J_v(x) \int_1^x -\frac{1}{2} \pi f(K[1]) Y_v(K[1]) dK[1] + Y_v(x) \int_1^x \frac{1}{2} \pi f(K[2]) J_v(K[2]) dK[2]}{x} + \frac{c_1 J_v(x)}{x} + \frac{c_2 Y_v(x)}{x} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 53

$$\left\{ y(x) = \frac{J_v(x) \_C2}{x} + \frac{Y_v(x) \_C1}{x} + \frac{\pi (Y_v(x) \int J_v(x) f(x) dx - J_v(x) \int Y_v(x) f(x) dx)}{2x} \right\}$$

**3.181 ODE No. 1181**

$$x^2 \frac{d^2}{dx^2} y(x) + (3x - 1) \frac{d}{dx} y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.028004 (sec), leaf count = 37

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{-1/x}}{x} - \frac{c_2 e^{-1/x} \text{Ei}\left(\frac{1}{x}\right)}{x} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 25

$$\left\{ y(x) = \frac{1}{x e^{x^{-1}}} (-C1 \text{Ei}(1, -x^{-1}) + -C2) \right\}$$

**3.182 ODE No. 1182**

$$x^2 \frac{d^2}{dx^2} y(x) - 3x \frac{d}{dx} y(x) + 4y(x) - 5x = 0$$

**Mathematica:** cpu = 0.015502 (sec), leaf count = 24

$$\left\{ \left\{ y(x) \rightarrow c_1 x^2 + 2c_2 x^2 \log(x) + 5x \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 20

$$\left\{ y(x) = x^2 -C2 + x^2 \ln(x) -C1 + 5x \right\}$$

**3.183 ODE No. 1183**

$$x^2 \frac{d^2}{dx^2} y(x) - 3x \frac{d}{dx} y(x) - 5y(x) - x^2 \ln(x) = 0$$

**Mathematica:** cpu = 0.024003 (sec), leaf count = 27

$$\left\{ \left\{ y(x) \rightarrow c_1 x^5 + \frac{c_2}{x} - \frac{1}{9} x^2 \log(x) \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 22

$$\left\{ y(x) = x^5 -C2 - \frac{x^2 \ln(x)}{9} + \frac{-C1}{x} \right\}$$

**3.184 ODE No. 1184**

$$x^2 \frac{d^2}{dx^2} y(x) - 4x \frac{d}{dx} y(x) + 6y(x) - x^4 + x^2 = 0$$

**Mathematica:** cpu = 0.018502 (sec), leaf count = 38

$$\left\{ \left\{ y(x) \rightarrow c_2 x^3 + c_1 x^2 + \frac{1}{2} (x^4 + 2x^2 + 2x^2 \log(x)) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 29

$$\left\{ y(x) = x^2 \_C2 + \_C1 x^3 + \frac{x^2(x^2 + 2 \ln(x) + 2)}{2} \right\}$$

**3.185 ODE No. 1185**

$$x^2 \frac{d^2}{dx^2} y(x) + 5x \frac{d}{dx} y(x) - (2x^3 - 4)y(x) = 0$$

**Mathematica:** cpu = 0.036005 (sec), leaf count = 67

$$\left\{ \left\{ y(x) \rightarrow \frac{3\sqrt[3]{6}c_2 K_0\left(\frac{2}{3}\sqrt{2}x^{3/2}\right)}{x^2} - \frac{3\sqrt[3]{-3}c_1 I_0\left(\frac{2}{3}\sqrt{2}x^{3/2}\right)}{2^{2/3}x^2} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 35

$$\left\{ y(x) = \frac{C1}{x^2} I_0\left(\frac{2\sqrt{2}}{3}x^{3/2}\right) + \frac{C2}{x^2} K_0\left(\frac{2\sqrt{2}}{3}x^{3/2}\right) \right\}$$

**3.186 ODE No. 1186**

$$x^2 \frac{d^2}{dx^2} y(x) - 5x \frac{d}{dx} y(x) + 8y(x) - \sin(x)x^3 = 0$$

**Mathematica:** cpu = 0.029504 (sec), leaf count = 42

$$\left\{ \left\{ y(x) \rightarrow c_2 x^4 + c_1 x^2 + \frac{1}{2} (x^4 \text{Ci}(x) - x^3 \sin(x) + x^2 \cos(x)) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 34

$$\left\{ y(x) = x^4 \_C2 + \_C1 x^2 + \frac{(\cos(x) + x(x \text{Ci}(x) - \sin(x))) x^2}{2} \right\}$$

**3.187 ODE No. 1187**

$$x^2 \frac{d^2}{dx^2} y(x) + ax \frac{d}{dx} y(x) + by(x) = 0$$

**Mathematica:** cpu = 0.011001 (sec), leaf count = 99

$$\left\{ \left\{ y(x) \rightarrow c_1 x^{\frac{1}{2} \sqrt{b} \left( -\frac{\sqrt{a^2 - 2a - 4b + 1} - \frac{a-1}{\sqrt{b}} \right)} + c_2 x^{\frac{1}{2} \sqrt{b} \left( \frac{\sqrt{a^2 - 2a - 4b + 1} - \frac{a-1}{\sqrt{b}} \right)} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 53

$$\left\{ y(x) = \_C1 x^{-\frac{a}{2} + \frac{1}{2} + \frac{1}{2} \sqrt{a^2 - 2a - 4b + 1}} + \_C2 x^{-\frac{a}{2} + \frac{1}{2} - \frac{1}{2} \sqrt{a^2 - 2a - 4b + 1}} \right\}$$

**3.188 ODE No. 1188**

$$x^2 \frac{d^2}{dx^2} y(x) + (ax + b) \frac{d}{dx} y(x) + cy(x) = 0$$

**Mathematica:** cpu = 0.082511 (sec), leaf count = 266

$$\left\{ \left\{ y(x) \rightarrow c_1 i^{-\sqrt{a^2 - 2a - 4c + 1} + a - 1} b^{\frac{1}{2} (-\sqrt{a^2 - 2a - 4c + 1} + a - 1)} \left( \frac{1}{x} \right)^{\frac{1}{2} (-\sqrt{a^2 - 2a - 4c + 1} + a - 1)} {}_1F_1 \left( \frac{a}{2} - \frac{1}{2} \sqrt{a^2 - 2a - 4c + 1}, \frac{b}{x} \right) + c_2 i^{\sqrt{a^2 - 2a - 4c + 1} + a - 1} b^{\frac{1}{2} (\sqrt{a^2 - 2a - 4c + 1} + a - 1)} \left( \frac{1}{x} \right)^{\frac{1}{2} (\sqrt{a^2 - 2a - 4c + 1} + a - 1)} {}_1F_1 \left( \frac{a}{2} + \frac{1}{2} \sqrt{a^2 - 2a - 4c + 1}, \frac{b}{x} \right) \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 135

$$\left\{ y(x) = \_C1 x^{-\frac{1}{2} \sqrt{a^2 - 2a - 4c + 1} - \frac{a}{2} + \frac{1}{2}} M \left( -\frac{1}{2} + \frac{1}{2} \sqrt{a^2 - 2a - 4c + 1} + \frac{a}{2}, 1 + \sqrt{a^2 - 2a - 4c + 1}, \frac{b}{x} \right) + \_C2 x^{-\frac{1}{2} \sqrt{a^2 - 2a - 4c + 1} - \frac{a}{2} + \frac{1}{2}} M \left( -\frac{1}{2} + \frac{1}{2} \sqrt{a^2 - 2a - 4c + 1} + \frac{a}{2}, 1 + \sqrt{a^2 - 2a - 4c + 1}, \frac{b}{x} \right) \right\}$$

**3.189 ODE No. 1189**

$$x^2 \frac{d^2}{dx^2} y(x) + ax \frac{d}{dx} y(x) + (bx^m + c) y(x) = 0$$

**Mathematica:** cpu = 0.069509 (sec), leaf count = 445

$$\left\{ \left\{ y(x) \rightarrow c_1 m^{-\frac{-\sqrt{a^2 - 2a - 4c + 1} - a + 1}{m} - \frac{\sqrt{a^2 - 2a - 4c + 1}}{m}} b^{\frac{-\sqrt{a^2 - 2a - 4c + 1} - a + 1}{2m} + \frac{\sqrt{a^2 - 2a - 4c + 1}}{2m}} (x^m)^{\frac{-\sqrt{a^2 - 2a - 4c + 1} - a + 1}{2m} + \frac{\sqrt{a^2 - 2a - 4c + 1}}{2m}} + c_2 m^{-\frac{-\sqrt{a^2 - 2a - 4c + 1} - a + 1}{m} - \frac{\sqrt{a^2 - 2a - 4c + 1}}{m}} b^{\frac{-\sqrt{a^2 - 2a - 4c + 1} - a + 1}{2m} - \frac{\sqrt{a^2 - 2a - 4c + 1}}{2m}} (x^m)^{\frac{-\sqrt{a^2 - 2a - 4c + 1} - a + 1}{2m} - \frac{\sqrt{a^2 - 2a - 4c + 1}}{2m}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 85

$$\left\{ y(x) = \_C1 x^{-\frac{a}{2} + \frac{1}{2}} J_{\frac{1}{m} \sqrt{a^2 - 2a - 4c + 1}} \left( 2 \frac{\sqrt{b} x^{m/2}}{m} \right) + \_C2 x^{-\frac{a}{2} + \frac{1}{2}} Y_{\frac{1}{m} \sqrt{a^2 - 2a - 4c + 1}} \left( 2 \frac{\sqrt{b} x^{m/2}}{m} \right) \right\}$$

### 3.190 ODE No. 1190

$$x^2 \frac{d^2}{dx^2} y(x) + x^2 \frac{d}{dx} y(x) + (ax + b) y(x) = 0$$

**Mathematica:** cpu = 0.030004 (sec), leaf count = 122

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{1}{2}((\sqrt{1-4b}+1) \log(x)-2x)} U\left(\frac{1}{2}(-2a + \sqrt{1-4b} + 1), \sqrt{1-4b} + 1, x\right) + c_2 e^{\frac{1}{2}((\sqrt{1-4b}+1) \log(x)-2x)} \right. \right.$$

**Maple:** cpu = 0.062 (sec), leaf count = 41

$$\left. \left\{ y(x) = \_C1 e^{-\frac{x}{2}} M_{a, \frac{1}{2}\sqrt{1-4b}}(x) + \_C2 e^{-\frac{x}{2}} W_{a, \frac{1}{2}\sqrt{1-4b}}(x) \right\} \right\}$$

### 3.191 ODE No. 1191

$$x^2 \frac{d^2}{dx^2} y(x) + x^2 \frac{d}{dx} y(x) - 2y(x) = 0$$

**Mathematica:** cpu = 0.008501 (sec), leaf count = 110

$$\left\{ \left\{ y(x) \rightarrow \frac{2c_2 e^{\frac{1}{2}(\log(x)-x)} \left( i \sinh\left(\frac{x}{2}\right) - \frac{2i \cosh\left(\frac{x}{2}\right)}{x} \right)}{\sqrt{\pi} \sqrt{-ix}} + \frac{2c_1 e^{\frac{1}{2}(\log(x)-x)} \left( \frac{2 \sinh\left(\frac{x}{2}\right)}{x} - \cosh\left(\frac{x}{2}\right) \right)}{\sqrt{\pi} \sqrt{-ix}} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 25

$$\left\{ y(x) = \frac{\_C1 (x-2)}{x} + \frac{\_C2 e^{-x} (x+2)}{x} \right\}$$

### 3.192 ODE No. 1192

$$x^2 \frac{d^2}{dx^2} y(x) + (x^2 - 1) \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 10.168291 (sec), leaf count = 39

$$\left\{ \left\{ y(x) \rightarrow c_2 e^{-x} \int_1^x e^{K[1] - \frac{1}{K[1]}} dK[1] + c_1 e^{-x} \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 53

$$\left\{ y(x) = \_C1 e^{-x} HeunD\left(4, 3, -8, 5, \frac{x-1}{1+x}\right) \sqrt{x} + \_C2 e^{-x^{-1}} HeunD\left(-4, 3, -8, 5, \frac{x-1}{1+x}\right) \sqrt{x} \right\}$$



### 3.193 ODE No. 1193

$$x^2 \frac{d^2}{dx^2} y(x) + x(1+x) \frac{d}{dx} y(x) + (x-9)y(x) = 0$$

**Mathematica:** cpu = 0.048506 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1((x-8)x+20)}{x^3} - \frac{c_2 e^{-x}(x^3+9x^2+36x+60)}{x^3} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 40

$$\left\{ y(x) = \frac{-C1(x^2-8x+20)}{x^3} + \frac{-C2 e^{-x}(x^3+9x^2+36x+60)}{x^3} \right\}$$

### 3.194 ODE No. 1194

$$x^2 \frac{d^2}{dx^2} y(x) + x(1+x) \frac{d}{dx} y(x) + (3x-1)y(x) = 0$$

**Mathematica:** cpu = 0.049506 (sec), leaf count = 65

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-x}(x-3)x - \frac{c_2 e^{-x}(x^3(-\text{Ei}(x)) + 3x^2 \text{Ei}(x) + e^x x^2 - 2e^x x - e^x)}{6x} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 44

$$\left\{ y(x) = -C1 x e^{-x}(x-3) + \frac{-C2(x^2 e^{-x}(x-3) \text{Ei}(1, -x) + x^2 - 2x - 1)}{x} \right\}$$

### 3.195 ODE No. 1195

$$x^2 \frac{d^2}{dx^2} y(x) + (x+3)x \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.028004 (sec), leaf count = 80

$$\left\{ \left\{ y(x) \rightarrow c_1 U\left(2 + \sqrt{2}, 1 + 2\sqrt{2}, x\right) e^{(\sqrt{2}-1) \log(x)-x} + c_2 L_{-2-\sqrt{2}}^{2\sqrt{2}}(x) e^{(\sqrt{2}-1) \log(x)-x} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 94

$$\left\{ y(x) = -C1 e^{-\frac{x}{2}} \left( (\sqrt{2} + x + 1) I_{-\frac{1}{2} + \sqrt{2}}\left(\frac{x}{2}\right) + (-\sqrt{2} + x + 1) I_{\frac{1}{2} + \sqrt{2}}\left(\frac{x}{2}\right) \right) \frac{1}{\sqrt{x}} + -C2 e^{-\frac{x}{2}} \left( (\sqrt{2} + x + \dots \right) \right\}$$

**3.196 ODE No. 1196**

$$x^2 \frac{d^2}{dx^2} y(x) - x(x-1) \frac{d}{dx} y(x) + (x-1)y(x) = 0$$

**Mathematica:** cpu = 0.025003 (sec), leaf count = 37

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2(x^2 \text{Ei}(x) - e^x x - e^x)}{2x} + c_1 x \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 27

$$\left\{ y(x) = x \_C1 + \_C2 \left( \frac{(1+x)e^x}{x} + x \text{Ei}(1, -x) \right) \right\}$$

**3.197 ODE No. 1197**

$$x^2 \frac{d^2}{dx^2} y(x) - (x^2 - 2x) \frac{d}{dx} y(x) - (x+a)y(x) = 0$$

**Mathematica:** cpu = 0.018002 (sec), leaf count = 78

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{1}{2}(x-\log(x))} J_{\frac{1}{2}\sqrt{4a+1}} \left( -\frac{ix}{2} \right) + c_2 e^{\frac{1}{2}(x-\log(x))} Y_{\frac{1}{2}\sqrt{4a+1}} \left( -\frac{ix}{2} \right) \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 49

$$\left\{ y(x) = \_C1 e^{\frac{x}{2}} I_{\frac{1}{2}\sqrt{4a+1}} \left( \frac{x}{2} \right) \frac{1}{\sqrt{x}} + \_C2 e^{\frac{x}{2}} K_{\frac{1}{2}\sqrt{4a+1}} \left( \frac{x}{2} \right) \frac{1}{\sqrt{x}} \right\}$$

**3.198 ODE No. 1198**

$$x^2 \frac{d^2}{dx^2} y(x) - (x^2 - 2x) \frac{d}{dx} y(x) - (3x+2)y(x) = 0$$

**Mathematica:** cpu = 0.029504 (sec), leaf count = 41

$$\left\{ \left\{ y(x) \rightarrow c_1 e^x x - \frac{c_2(e^x x^3 \text{Ei}(-x) + x^2 - x + 2)}{6x^2} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 33

$$\left\{ y(x) = \_C1 x e^x + \frac{\_C2 (-x^3 e^x \text{Ei}(1, x) + x^2 - x + 2)}{x^2} \right\}$$

**3.199 ODE No. 1199**

$$x^2 \frac{d^2}{dx^2} y(x) - x(x+4) \frac{d}{dx} y(x) + 4y(x) = 0$$

**Mathematica:** cpu = 0.012502 (sec), leaf count = 41

$$\left\{ \left\{ y(x) \rightarrow c_2 e^x x^4 - \frac{1}{6} c_1 x (e^x x^3 \text{Ei}(-x) + x^2 - x + 2) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 32

$$\{y(x) = \_C1 x^4 e^x + \_C2 x (x^3 e^x \text{Ei}(1, x) - x^2 + x - 2)\}$$

**3.200 ODE No. 1200**

$$x^2 \frac{d^2}{dx^2} y(x) + 2x^2 \frac{d}{dx} y(x) - v(v-1) y(x) = 0$$

**Mathematica:** cpu = 0.021503 (sec), leaf count = 62

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-x} \sqrt{x} J_{\frac{1}{2}(2v-1)}(-ix) + c_2 e^{-x} \sqrt{x} Y_{\frac{1}{2}(2v-1)}(-ix) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 33

$$\{y(x) = \_C1 e^{-x} \sqrt{x} I_{v-\frac{1}{2}}(x) + \_C2 e^{-x} \sqrt{x} K_{v-\frac{1}{2}}(x)\}$$

**3.201 ODE No. 1201**

$$x^2 \frac{d^2}{dx^2} y(x) + x(2x+1) \frac{d}{dx} y(x) - 4y(x) = 0$$

**Mathematica:** cpu = 0.054007 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{-2x} (2x+3)}{2x^2} + \frac{c_2 (2x^2 - 4x + 3)}{4x^2} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 34

$$\{y(x) = \frac{\_C1 (2x^2 - 4x + 3)}{x^2} + \frac{\_C2 e^{-2x} (2x + 3)}{x^2}\}$$

### 3.202 ODE No. 1202

$$x^2 \frac{d^2}{dx^2} y(x) - 2x(1+x) \frac{d}{dx} y(x) + 2(1+x)y(x) = 0$$

**Mathematica:** cpu = 0.014502 (sec), leaf count = 22

$$\left\{ \left\{ y(x) \rightarrow c_1 x + \frac{1}{2} c_2 e^{2x} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 15

$$\{y(x) = x\_C1 + \_C2 x e^{2x}\}$$

### 3.203 ODE No. 1203

$$x^2 \frac{d^2}{dx^2} y(x) + ax^2 \frac{d}{dx} y(x) - 2y(x) = 0$$

**Mathematica:** cpu = 0.021003 (sec), leaf count = 124

$$\left\{ \left\{ y(x) \rightarrow \frac{2c_2 e^{\frac{1}{2}(\log(x)-ax)} \left( i \sinh\left(\frac{ax}{2}\right) - \frac{2i \cosh\left(\frac{ax}{2}\right)}{ax} \right)}{\sqrt{\pi} \sqrt{-iax}} + \frac{2c_1 e^{\frac{1}{2}(\log(x)-ax)} \left( \frac{2 \sinh\left(\frac{ax}{2}\right)}{ax} - \cosh\left(\frac{ax}{2}\right) \right)}{\sqrt{\pi} \sqrt{-iax}} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 30

$$\left\{ y(x) = \frac{-C1(ax-2)}{x} + \frac{-C2 e^{-ax}(ax+2)}{x} \right\}$$

### 3.204 ODE No. 1204

$$x^2 \frac{d^2}{dx^2} y(x) + (a+2b)x^2 \frac{d}{dx} y(x) + ((a+b)bx^2 - 2)y(x) = 0$$

**Mathematica:** cpu = 0.019002 (sec), leaf count = 132

$$\left\{ \left\{ y(x) \rightarrow \frac{2c_2 e^{\frac{1}{2}(-ax-2bx+\log(x))} \left( i \sinh\left(\frac{ax}{2}\right) - \frac{2i \cosh\left(\frac{ax}{2}\right)}{ax} \right)}{\sqrt{\pi} \sqrt{-iax}} + \frac{2c_1 e^{\frac{1}{2}(-ax-2bx+\log(x))} \left( \frac{2 \sinh\left(\frac{ax}{2}\right)}{ax} - \cosh\left(\frac{ax}{2}\right) \right)}{\sqrt{\pi} \sqrt{-iax}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 37

$$\left\{ y(x) = \frac{-C1 e^{-bx}(ax-2)}{x} + \frac{-C2 e^{-(a+b)x}(ax+2)}{x} \right\}$$

### 3.205 ODE No. 1205

$$x^2 \frac{d^2}{dx^2} y(x) + ax^2 \frac{d}{dx} y(x) + f(x) y(x) = 0$$

**Mathematica:** cpu = 0.212527 (sec), leaf count = 29

$$\text{DSolve}[ax^2 y'(x) + f(x)y(x) + x^2 y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.0 (sec), leaf count = 30

$$\left\{ y(x) = \text{DESol} \left( \left\{ \frac{f(x) - Y(x)}{x^2} + a \frac{d}{dx} Y(x) + \frac{d^2}{dx^2} Y(x) \right\}, \{ -Y(x) \} \right) \right\}$$

### 3.206 ODE No. 1206

$$x^2 \frac{d^2}{dx^2} y(x) + (2ax + b)x \frac{d}{dx} y(x) + (abx + cx^2 + d)y(x) = 0$$

**Mathematica:** cpu = 0.114515 (sec), leaf count = 120

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{1}{2}(-2ax - (b-1)\log(x))} J_{\frac{1}{2}\sqrt{b^2 - 2b - 4d + 1}}(-i\sqrt{a^2 - cx}) + c_2 e^{\frac{1}{2}(-2ax - (b-1)\log(x))} Y_{\frac{1}{2}\sqrt{b^2 - 2b - 4d + 1}}(-i\sqrt{a^2 - cx}) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 87

$$\left\{ y(x) = \_C1 e^{-ax} x^{\frac{1}{2} - \frac{b}{2}} J_{\frac{1}{2}\sqrt{b^2 - 2b - 4d + 1}}(\sqrt{-a^2 + cx}) + \_C2 e^{-ax} x^{\frac{1}{2} - \frac{b}{2}} Y_{\frac{1}{2}\sqrt{b^2 - 2b - 4d + 1}}(\sqrt{-a^2 + cx}) \right\}$$

### 3.207 ODE No. 1207

$$x^2 \frac{d^2}{dx^2} y(x) + (ax + b) \left( \frac{d}{dx} y(x) \right) x + (a1 x^2 + b1 x + c1) y(x) = 0$$

**Mathematica:** cpu = 0.123516 (sec), leaf count = 294

$$\left\{ \left\{ y(x) \rightarrow c_1 U \left( -\frac{-ab + 2b1 - \sqrt{a^2 - 4a1} - \sqrt{a^2 - 4a1}\sqrt{b^2 - 2b - 4c1 + 1}}{2\sqrt{a^2 - 4a1}}, \sqrt{b^2 - 2b - 4c1 + 1} + 1, \sqrt{a^2 - 4a1} \right) \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 119

$$\left\{ y(x) = \_C1 e^{-\frac{ax}{2}} x^{-\frac{b}{2}} M_{-\frac{ab-2b1}{2}, \frac{1}{\sqrt{a^2-4a1}}, \frac{1}{2}\sqrt{b^2-2b-4c1+1}}(\sqrt{a^2-4a1}x) + \_C2 e^{-\frac{ax}{2}} x^{-\frac{b}{2}} W_{-\frac{ab-2b1}{2}, \frac{1}{\sqrt{a^2-4a1}}, \frac{1}{2}\sqrt{b^2-2b-4c1+1}}(\sqrt{a^2-4a1}x) \right\}$$

### 3.208 ODE No. 1208

$$x^2 \frac{d^2}{dx^2} y(x) + x^3 \frac{d}{dx} y(x) + (x^2 - 2) y(x) = 0$$

**Mathematica:** cpu = 0.037005 (sec), leaf count = 59

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 e^{-\frac{x^2}{2}} \left( \sqrt{2\pi} e^{\frac{x^2}{2}} \operatorname{erf}\left(\frac{x}{\sqrt{2}}\right) - 2x \right)}{2x} + \frac{c_1}{x} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 40

$$\left\{ y(x) = \frac{C1}{x} + \frac{C2}{x} \left( -\sqrt{\pi} \sqrt{2} \operatorname{Erf}\left(\frac{x\sqrt{2}}{2}\right) + 2x e^{-1/2 x^2} \right) \right\}$$

### 3.209 ODE No. 1209

$$x^2 \frac{d^2}{dx^2} y(x) + (x^2 + 2) x \frac{d}{dx} y(x) + (x^2 - 2) y(x) = 0$$

**Mathematica:** cpu = 0.020002 (sec), leaf count = 67

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{-\frac{x^2}{2}} \left( e^{\frac{x^2}{2}} x - \sqrt{\frac{\pi}{2}} \operatorname{erfi}\left(\frac{x}{\sqrt{2}}\right) \right)}{x^2} + \frac{c_2 e^{-\frac{x^2}{2}}}{x^2} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 48

$$\left\{ y(x) = \frac{C1}{x^2} e^{-\frac{x^2}{2}} + \frac{C2}{x^2} \left( -ix\sqrt{\pi}\sqrt{2} + e^{-\frac{x^2}{2}} \pi \operatorname{Erf}\left(\frac{i}{2}\sqrt{2}x\right) \right) \right\}$$

### 3.210 ODE No. 1210

$$x^2 \frac{d^2}{dx^2} y(x) - 2x(x^2 - a) \frac{d}{dx} y(x) + (2nx^2 + ((-1)^n - 1)a) y(x) = 0$$

**Mathematica:** cpu = 0.266034 (sec), leaf count = 252

$$\left\{ \left\{ y(x) \rightarrow c_1 (-1)^{\frac{1}{4}} \left( -\sqrt{4a^2 - 4a(-1)^{n+1} - 2a+1} \right)^{\frac{1}{4}} x^{\frac{1}{2}} \left( -\sqrt{4a^2 - 4a(-1)^{n+1} - 2a+1} \right) {}_1F_1\left(-\frac{a}{2} - \frac{n}{2} - \frac{1}{4} \sqrt{4a^2 - 4(-1)^n a + 1}, \frac{1}{4} \sqrt{4a^2 - 4(-1)^n a + 1}, x^2\right) + c_2 (-1)^{\frac{1}{4}} \left( -\sqrt{4a^2 - 4a(-1)^{n+1} - 2a+1} \right)^{\frac{1}{4}} x^{\frac{1}{2}} \left( -\sqrt{4a^2 - 4a(-1)^{n+1} - 2a+1} \right) {}_1F_1\left(-\frac{a}{2} - \frac{n}{2} - \frac{1}{4} \sqrt{4a^2 - 4(-1)^n a + 1}, \frac{1}{4} \sqrt{4a^2 - 4(-1)^n a + 1}, x^2\right) \right\} \right\}$$

**Maple:** cpu = 0.421 (sec), leaf count = 93

$$\left\{ y(x) = -C1 x^{-\frac{1}{2}-a} e^{\frac{x^2}{2}} M_{\frac{n}{2}+\frac{a}{2}+\frac{1}{4}, \frac{1}{4}\sqrt{1-4(-1)^n a+4a^2}}(x^2) + -C2 x^{-\frac{1}{2}-a} e^{\frac{x^2}{2}} W_{\frac{n}{2}+\frac{a}{2}+\frac{1}{4}, \frac{1}{4}\sqrt{1-4(-1)^n a+4a^2}}(x^2) \right\}$$

### 3.211 ODE No. 1211

$$x^2 \frac{d^2}{dx^2} y(x) + 4x^3 \frac{d}{dx} y(x) + (4x^4 + 2x^2 + 1) y(x) = 0$$

**Mathematica:** cpu = 0.055007 (sec), leaf count = 68

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-x^2} x^{\frac{1}{2} - \frac{i\sqrt{3}}{2}} - \frac{ic_2 e^{-x^2} x^{\frac{1}{2} + \frac{i\sqrt{3}}{2}}}{\sqrt{3}} \right\} \right\}$$

**Maple:** cpu = 0.046 (sec), leaf count = 41

$$\left\{ y(x) = \_C1 x^{\frac{1}{2} + \frac{i\sqrt{3}}{2}} e^{-x^2} + \_C2 x^{\frac{1}{2} - \frac{i\sqrt{3}}{2}} e^{-x^2} \right\}$$

### 3.212 ODE No. 1212

$$x^2 \frac{d^2}{dx^2} y(x) + (ax^2 + b) x \frac{d}{dx} y(x) + f(x) y(x) = 0$$

**Mathematica:** cpu = 0.375548 (sec), leaf count = 33

$$\text{DSolve}[x(ax^2 + b) y'(x) + f(x)y(x) + x^2 y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.016 (sec), leaf count = 39

$$\left\{ y(x) = \text{DESol} \left( \left\{ \frac{f(x) \_Y(x)}{x^2} + \frac{(ax^2 + b) \frac{d}{dx} \_Y(x)}{x} + \frac{d^2}{dx^2} \_Y(x) \right\}, \{ \_Y(x) \} \right) \right\}$$

### 3.213 ODE No. 1213

$$x^2 \frac{d^2}{dx^2} y(x) + (x^3 + 1) x \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.072009 (sec), leaf count = 54

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{3} c_1 {}_1F_1\left(-\frac{1}{3}; \frac{1}{3}; -\frac{x^3}{3}\right)}{x} + \frac{c_2 x {}_1F_1\left(\frac{1}{3}; \frac{5}{3}; -\frac{x^3}{3}\right)}{\sqrt[3]{3}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 59

$$\left\{ y(x) = \_C1 e^{-\frac{x^3}{6}} x^{\frac{3}{2}} \left( I_{\frac{5}{6}}\left(\frac{x^3}{6}\right) + I_{-\frac{1}{6}}\left(\frac{x^3}{6}\right) \right) + \_C2 e^{-\frac{x^3}{6}} x^{\frac{3}{2}} \left( K_{\frac{1}{6}}\left(\frac{x^3}{6}\right) - K_{\frac{5}{6}}\left(\frac{x^3}{6}\right) \right) \right\}$$

### 3.214 ODE No. 1214

$$x^2 \frac{d^2}{dx^2} y(x) + (-x^4 + (2n + 2a + 1)x^2 + (-1)^n a - a^2) y(x) = 0$$

**Mathematica:** cpu = 0.289037 (sec), leaf count = 260

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{-\frac{x^2}{2}} 2^{\frac{1}{4}} (\sqrt{4a^2 - 4a(-1)^{n+1} + 2}) (x^2)^{\frac{1}{4}} (\sqrt{4a^2 - 4a(-1)^{n+1} + 2}) U\left(\frac{1}{4}(-2a - 2n + \sqrt{4a^2 - 4(-1)^n a + 1})\right)}{\sqrt{x}} \right. \right.$$

**Maple:** cpu = 0.390 (sec), leaf count = 73

$$\left\{ y(x) = -C1 M_{\frac{n}{2} + \frac{a}{2} + \frac{1}{4}, \frac{1}{4} \sqrt{1 - 4(-1)^n a + 4a^2}}(x^2) \frac{1}{\sqrt{x}} + -C2 W_{\frac{n}{2} + \frac{a}{2} + \frac{1}{4}, \frac{1}{4} \sqrt{1 - 4(-1)^n a + 4a^2}}(x^2) \frac{1}{\sqrt{x}} \right\}$$

### 3.215 ODE No. 1215

$$x^2 \frac{d^2}{dx^2} y(x) + (ax^n + b) \left( \frac{d}{dx} y(x) \right) x + (a1 x^{2n} + b1 x^n + c1) y(x) = 0$$

**Mathematica:** cpu = 0.158020 (sec), leaf count = 664

$$\left\{ \left\{ y(x) \rightarrow c_1 x^{\frac{1-n}{2}} 2^{\frac{\sqrt{b^2 n^2 - 2bn^2 - 4c1n^2 + n^2}}{2n^2}} (x^n)^{\frac{\sqrt{b^2 n^2 - 2bn^2 - 4c1n^2 + n^2}}{2n^2}} \exp\left(\frac{1}{2}\left(-\frac{ax^n}{n} - b \log(x)\right) - \frac{\sqrt{a^2 - 4a}}{2n}\right) \right. \right.$$

**Maple:** cpu = 0.140 (sec), leaf count = 167

$$\left\{ y(x) = -C1 x^{-\frac{b}{2} - \frac{n}{2} + \frac{1}{2}} e^{-\frac{ax^n}{2n}} M_{-\frac{(b+n-1)a-2b1}{2n}, \frac{1}{\sqrt{a^2-4a1}}, \frac{1}{2n} \sqrt{b^2-2b-4c1+1}}\left(\frac{x^n}{n} \sqrt{a^2-4a1}\right) + -C2 x^{-\frac{b}{2} - \frac{n}{2} + \frac{1}{2}} e^{-\frac{ax^n}{2n}}$$

### 3.216 ODE No. 1216

$$x^2 \frac{d^2}{dx^2} y(x) + (ax^{a1} + b) x \frac{d}{dx} y(x) + (Ax^{2a1} + Bx^{a1} + Cx^{b1} + DD) y(x) = 0$$

**Mathematica:** cpu = 1.452184 (sec), leaf count = 50

$$\text{DSolve}[xy'(x) (ax^{a1} + b) + y(x) (Ax^{2a1} + Bx^{a1} + Cx^{b1} + DD) + x^2 y''(x) = 0, y(x), x]$$



**Maple:** cpu = 0.546 (sec), leaf count = 56

$$\left\{ y(x) = DESol \left( \left\{ \frac{d^2}{dx^2} Y(x) + \frac{(ax^{a1} + b) \frac{d}{dx} Y(x)}{x} + \frac{(Ax^{2a1} + Bx^{a1} + Cx^{b1} + DD) Y(x)}{x^2} \right\}, \{-Y(x)\} \right) \right\}$$

### 3.217 ODE No. 1217

$$x^2 \frac{d^2}{dx^2} y(x) - (2x^2 \tan(x) - x) \frac{d}{dx} y(x) - (x \tan(x) + a) y(x) = 0$$

**Mathematica:** cpu = 0.144018 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow c_1 \sec(x) J_{\sqrt{a}}(x) + c_2 \sec(x) Y_{\sqrt{a}}(x) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 27

$$\left\{ y(x) = \frac{-C1}{\cos(x)} J_{\sqrt{a}}(x) + \frac{-C2}{\cos(x)} Y_{\sqrt{a}}(x) \right\}$$

### 3.218 ODE No. 1218

$$x^2 \frac{d^2}{dx^2} y(x) + (2x^2 \cot(x) + x) \frac{d}{dx} y(x) + (x \cot(x) + a) y(x) = 0$$

**Mathematica:** cpu = 0.143518 (sec), leaf count = 38

$$\left\{ \left\{ y(x) \rightarrow c_1 \csc(x) J_{i\sqrt{a}}(x) + c_2 \csc(x) Y_{i\sqrt{a}}(x) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 33

$$\left\{ y(x) = \frac{-C1}{\sin(x)} J_{i\sqrt{a}}(x) + \frac{-C2}{\sin(x)} Y_{i\sqrt{a}}(x) \right\}$$

### 3.219 ODE No. 1219

$$x^2 \frac{d^2}{dx^2} y(x) + 2xf(x) \frac{d}{dx} y(x) + \left( x \frac{d}{dx} f(x) + (f(x))^2 - f(x) + ax^2 + bx + c \right) y(x) = 0$$

**Mathematica:** cpu = 23.116936 (sec), leaf count = 216

$$\left\{ \left\{ y(x) \rightarrow c_1 U \left( -\frac{-ib - \sqrt{a} - \sqrt{a}\sqrt{1-4c}}{2\sqrt{a}}, \sqrt{1-4c} + 1, 2i\sqrt{ax} \right) \exp \left( \int_1^x \frac{-2i\sqrt{a}K[1] - 2f(K[1]) + \sqrt{1-4c}}{2K[1]} dx \right) \right. \right.$$

**Maple:** cpu = 0.062 (sec), leaf count = 79

$$\left\{ y(x) = -C1 M_{-\frac{1}{2}b\frac{1}{\sqrt{a}}, \frac{1}{2}\sqrt{1-4c}}(2i\sqrt{ax}) e^{-\int \frac{f(x)}{x} dx} + -C2 W_{-\frac{1}{2}b\frac{1}{\sqrt{a}}, \frac{1}{2}\sqrt{1-4c}}(2i\sqrt{ax}) e^{-\int \frac{f(x)}{x} dx} \right\}$$

### 3.220 ODE No. 1220

$$x^2 \frac{d^2}{dx^2} y(x) + 2x^2 f(x) \frac{d}{dx} y(x) + \left( x^2 \left( \frac{d}{dx} f(x) + (f(x))^2 + a \right) - v(v-1) \right) y(x) = 0$$

**Mathematica:** cpu = 11.805499 (sec), leaf count = 96

$$\left\{ \left\{ y(x) \rightarrow c_1 J_{\frac{1}{2}(2v-1)}(\sqrt{ax}) \exp \left( \int_1^x \frac{1 - 2K[1]f(K[1])}{2K[1]} dK[1] \right) + c_2 Y_{\frac{1}{2}(2v-1)}(\sqrt{ax}) \exp \left( \int_1^x \frac{1 - 2K[1]f(K[1])}{2K[1]} dK[1] \right) \right. \right.$$

**Maple:** cpu = 0.015 (sec), leaf count = 51

$$\left\{ y(x) = \_C1 e^{-\frac{\int 2f(x) dx}{2}} \sqrt{x} J_{v-\frac{1}{2}}(\sqrt{ax}) + \_C2 e^{-\frac{\int 2f(x) dx}{2}} \sqrt{x} Y_{v-\frac{1}{2}}(\sqrt{ax}) \right\}$$

### 3.221 ODE No. 1221

$$x^2 \frac{d^2}{dx^2} y(x) + (x - 2x^2 f(x)) \frac{d}{dx} y(x) + \left( x^2 \left( 1 + (f(x))^2 - \frac{d}{dx} f(x) \right) - xf(x) - v^2 \right) y(x) = 0$$

**Mathematica:** cpu = 0.061508 (sec), leaf count = 40

$$\left\{ \left\{ y(x) \rightarrow c_1 J_v(x) e^{\int_1^x f(K[1]) dK[1]} + c_2 Y_v(x) e^{\int_1^x f(K[1]) dK[1]} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 53

$$\left\{ y(x) = \_C1 e^{-\frac{1}{2} \int \frac{-2xf(x)+1}{x} dx} \sqrt{x} J_v(x) + \_C2 e^{-\frac{1}{2} \int \frac{-2xf(x)+1}{x} dx} \sqrt{x} Y_v(x) \right\}$$

### 3.222 ODE No. 1222

$$(x^2 + 1) \frac{d^2}{dx^2} y(x) + x \frac{d}{dx} y(x) + 2y(x) = 0$$

**Mathematica:** cpu = 0.020003 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow c_2 \sin \left( \sqrt{2} \sinh^{-1}(x) \right) + c_1 \cos \left( \sqrt{2} \sinh^{-1}(x) \right) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 23

$$\left\{ y(x) = \_C1 \sin \left( \sqrt{2} \operatorname{Arcsinh}(x) \right) + \_C2 \cos \left( \sqrt{2} \operatorname{Arcsinh}(x) \right) \right\}$$

**3.223 ODE No. 1223**

$$(x^2 + 1) \frac{d^2}{dx^2} y(x) + x \frac{d}{dx} y(x) - 9 y(x) = 0$$

**Mathematica:** cpu = 0.019502 (sec), leaf count = 25

$$\left\{ \left\{ y(x) \rightarrow c_1 \cosh(3 \sinh^{-1}(x)) + i c_2 \sinh(3 \sinh^{-1}(x)) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 39

$$\left\{ y(x) = \_C1 \sin \left( 3 \arctan \left( \frac{x}{\sqrt{-x^2 - 1}} \right) \right) + \_C2 \cos \left( 3 \arctan \left( \frac{x}{\sqrt{-x^2 - 1}} \right) \right) \right\}$$

**3.224 ODE No. 1224**

$$(x^2 + 1) \frac{d^2}{dx^2} y(x) + x \frac{d}{dx} y(x) + a y(x) = 0$$

**Mathematica:** cpu = 0.018002 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow c_2 \sin(\sqrt{a} \sinh^{-1}(x)) + c_1 \cos(\sqrt{a} \sinh^{-1}(x)) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 23

$$\{ y(x) = \_C1 \sin(\sqrt{a} \operatorname{Arcsinh}(x)) + \_C2 \cos(\sqrt{a} \operatorname{Arcsinh}(x)) \}$$

**3.225 ODE No. 1225**

$$(x^2 + 1) \frac{d^2}{dx^2} y(x) - x \frac{d}{dx} y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.032004 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow c_2 \left( x \sinh^{-1}(x) - \sqrt{x^2 + 1} \right) + c_1 x \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 24

$$\{ y(x) = x \_C1 + \_C2 \left( \operatorname{Arcsinh}(x) x - \sqrt{x^2 + 1} \right) \}$$

### 3.226 ODE No. 1226

$$(x^2 + 1) \frac{d^2}{dx^2} y(x) + 2x \frac{d}{dx} y(x) - v(v-1) y(x) = 0$$

**Mathematica:** cpu = 0.018502 (sec), leaf count = 30

$$\{ \{ y(x) \rightarrow c_1 P_{v-1}(ix) + c_2 Q_{v-1}(ix) \} \}$$

**Maple:** cpu = 0.031 (sec), leaf count = 25

$$\{ y(x) = \_C1 \text{LegendreP}(v-1, ix) + \_C2 \text{LegendreQ}(v-1, ix) \}$$

### 3.227 ODE No. 1227

$$(x^2 + 1) \frac{d^2}{dx^2} y(x) - 2x \frac{d}{dx} y(x) + 2y(x) = 0$$

**Mathematica:** cpu = 0.036005 (sec), leaf count = 21

$$\{ \{ y(x) \rightarrow c_2 x - c_1 (x - i)^2 \} \}$$

**Maple:** cpu = 0.016 (sec), leaf count = 15

$$\{ y(x) = x \_C1 + \_C2 (x^2 - 1) \}$$

### 3.228 ODE No. 1228

$$(x^2 + 1) \frac{d^2}{dx^2} y(x) + 3x \frac{d}{dx} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.014502 (sec), leaf count = 82

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 P_{\frac{1}{2}(2\sqrt{1-a}-1)}(ix)}{\sqrt[4]{x^2+1}} + \frac{c_2 Q_{\frac{1}{2}(2\sqrt{1-a}-1)}(ix)}{\sqrt[4]{x^2+1}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 59

$$\left\{ y(x) = \_C1 (x + \sqrt{x^2+1})^{\sqrt{1-a}} \frac{1}{\sqrt{x^2+1}} + \_C2 (x + \sqrt{x^2+1})^{-\sqrt{1-a}} \frac{1}{\sqrt{x^2+1}} \right\}$$

**3.229 ODE No. 1229**

$$(x^2 + 1) \frac{d^2}{dx^2} y(x) + 4x \frac{d}{dx} y(x) + 2y(x) - 2 \cos(x) + 2x = 0$$

**Mathematica:** cpu = 0.040505 (sec), leaf count = 48

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{x^2 + 1} + \frac{c_2 x}{x^2 + 1} + \frac{-x^3 - 6 \cos(x)}{3(x^2 + 1)} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 41

$$\left\{ y(x) = \frac{x\_C1}{x^2 + 1} + \frac{\_C2}{x^2 + 1} - \frac{x^3 + 6 \cos(x)}{3x^2 + 3} \right\}$$

**3.230 ODE No. 1230**

$$(x^2 + 1) \frac{d^2}{dx^2} y(x) + ax \frac{d}{dx} y(x) + (a - 2) y(x) = 0$$

**Mathematica:** cpu = 0.025503 (sec), leaf count = 82

$$\left\{ \left\{ y(x) \rightarrow c_1 (x^2 + 1)^{\frac{2-a}{4}} P_{\frac{a-2}{2}}^{\frac{a-2}{2}}(ix) + c_2 (x^2 + 1)^{\frac{2-a}{4}} Q_{\frac{a-2}{2}}^{\frac{a-2}{2}}(ix) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 36

$$\left\{ y(x) = \_C1 (x^2 + 1)^{1-\frac{a}{2}} + \_C2 {}_2F_1\left(1, \frac{a}{2} - \frac{1}{2}; \frac{3}{2}; -x^2\right)x \right\}$$

**3.231 ODE No. 1231**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) - v(v + 1) y(x) = 0$$

**Mathematica:** cpu = 0.075010 (sec), leaf count = 58

$$\left\{ \left\{ y(x) \rightarrow c_1 {}_2F_1\left(-\frac{v}{2} - \frac{1}{2}, \frac{v}{2}; \frac{1}{2}; x^2\right) + ic_2 x {}_2F_1\left(\frac{v}{2} + \frac{1}{2}, -\frac{v}{2}; \frac{3}{2}; x^2\right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 57

$$\left\{ y(x) = \_C1 (-x^2 + 1) {}_2F_1\left(1 + \frac{v}{2}, \frac{1}{2} - \frac{v}{2}; \frac{1}{2}; x^2\right) + \_C2 (-x^3 + x) {}_2F_1\left(1 - \frac{v}{2}, \frac{3}{2} + \frac{v}{2}; \frac{3}{2}; x^2\right) \right\}$$

**3.232 ODE No. 1232**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) - n(n+1) y(x) + \frac{\partial}{\partial x} \text{Legendre}P(n, x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.141 (sec), leaf count = 418

$$\left\{ y(x) = (-x^2 + 1) {}_2F_1\left(\frac{n}{2} + 1, -\frac{n}{2} + \frac{1}{2}; \frac{1}{2}; x^2\right) C2 + (-x^3 + x) {}_2F_1\left(-\frac{n}{2} + 1, \frac{n}{2} + \frac{3}{2}; \frac{3}{2}; x^2\right) C1 - 3(n) \right.$$

**3.233 ODE No. 1233**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) - n(n+1) y(x) + \frac{\partial}{\partial x} \text{Legendre}Q(n, x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.109 (sec), leaf count = 418

$$\left\{ y(x) = (-x^2 + 1) {}_2F_1\left(\frac{n}{2} + 1, -\frac{n}{2} + \frac{1}{2}; \frac{1}{2}; x^2\right) C2 + (-x^3 + x) {}_2F_1\left(-\frac{n}{2} + 1, \frac{n}{2} + \frac{3}{2}; \frac{3}{2}; x^2\right) C1 - 3(n) \right.$$

**3.234 ODE No. 1234**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) + x \frac{d}{dx} y(x) + 2 = 0$$

**Mathematica:** cpu = 0.028004 (sec), leaf count = 38

$$\left\{ \left\{ y(x) \rightarrow \log\left(\sqrt{x^2 - 1} + x\right) \left(c_1 - \log\left(\sqrt{x^2 - 1} + x\right)\right) + c_2 \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 57

$$\left\{ y(x) = \int 1 \left( -2\sqrt{x^2 - 1} \ln\left(x + \sqrt{x^2 - 1}\right) \sqrt{x - 1} \sqrt{1 + x} + C1 x^2 - C1 \right) (1 + x)^{-\frac{3}{2}} (x - 1)^{-\frac{3}{2}} dx + \right.$$

**3.235 ODE No. 1235**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) + x \frac{d}{dx} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.026503 (sec), leaf count = 50

$$\left\{ \left\{ y(x) \rightarrow c_2 \sin \left( \sqrt{a} \log \left( \sqrt{x^2 - 1} + x \right) \right) + c_1 \cos \left( \sqrt{a} \log \left( \sqrt{x^2 - 1} + x \right) \right) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 43

$$\left\{ y(x) = -C1 \left( x + \sqrt{x^2 - 1} \right)^{i\sqrt{a}} + -C2 \left( \left( x + \sqrt{x^2 - 1} \right)^{i\sqrt{a}} \right)^{-1} \right\}$$

**3.236 ODE No. 1236**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) + x \frac{d}{dx} y(x) + f(x) y(x) = 0$$

**Mathematica:** cpu = 0.365046 (sec), leaf count = 28

$$\text{DSolve}[f(x)y(x) + (x^2 - 1) y''(x) + xy'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.0 (sec), leaf count = 41

$$\left\{ y(x) = \text{DESol} \left( \left\{ \frac{f(x) - Y(x)}{x^2 - 1} + \frac{x \frac{d}{dx} - Y(x)}{x^2 - 1} + \frac{d^2}{dx^2} - Y(x) \right\}, \{-Y(x)\} \right) \right\}$$

**3.237 ODE No. 1237**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) + 2x \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.010001 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow c_1 \left( \frac{1}{2} \log(1 - x) - \frac{1}{2} \log(x + 1) \right) + c_2 \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 21

$$\left\{ y(x) = -C1 + \left( -\frac{\ln(1 + x)}{2} + \frac{\ln(x - 1)}{2} \right) - C2 \right\}$$

**3.238 ODE No. 1238**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) + 2x \frac{d}{dx} y(x) - a = 0$$

**Mathematica:** cpu = 0.017502 (sec), leaf count = 36

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2}(a + c_1) \log(1 - x) + \frac{1}{2}(a - c_1) \log(x + 1) + c_2 \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 34

$$\left\{ y(x) = \frac{\ln(x - 1) \_C1}{2} + \frac{\ln(x - 1) a}{2} - \frac{\ln(1 + x) \_C1}{2} + \frac{\ln(1 + x) a}{2} + \_C2 \right\}$$

**3.239 ODE No. 1239**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) + 2x \frac{d}{dx} y(x) - ly(x) = 0$$

**Mathematica:** cpu = 0.014002 (sec), leaf count = 46

$$\left\{ \left\{ y(x) \rightarrow c_1 P_{\frac{1}{2}(\sqrt{4l+1}-1)}(x) + c_2 Q_{\frac{1}{2}(\sqrt{4l+1}-1)}(x) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 \text{LegendreP}\left(\frac{1}{2}\sqrt{1+4l} - \frac{1}{2}, x\right) + \_C2 \text{LegendreQ}\left(\frac{1}{2}\sqrt{1+4l} - \frac{1}{2}, x\right) \right\}$$

**3.240 ODE No. 1240**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) + 2x \frac{d}{dx} y(x) - v(v + 1) y(x) = 0$$

**Mathematica:** cpu = 0.017002 (sec), leaf count = 18

$$\left\{ \left\{ y(x) \rightarrow c_1 P_v(x) + c_2 Q_v(x) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 15

$$\left\{ y(x) = \_C1 \text{LegendreP}(v, x) + \_C2 \text{LegendreQ}(v, x) \right\}$$



**3.241 ODE No. 1241**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) - 2x \frac{d}{dx} y(x) - (v + 2)(v - 1) y(x) = 0$$

**Mathematica:** cpu = 0.015002 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow c_1 (x^2 - 1) P_v^2(x) + c_2 (x^2 - 1) Q_v^2(x) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 29

$$\{y(x) = \_C1 (x - 1) (1 + x) \text{LegendreP}(v, 2, x) + \_C2 (x - 1) (1 + x) \text{LegendreQ}(v, 2, x)\}$$

**3.242 ODE No. 1242**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) - (3x + 1) \frac{d}{dx} y(x) - (x^2 - x) y(x) = 0$$

**Mathematica:** cpu = 0.074509 (sec), leaf count = 68

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-x} (x + 1)^2 - c_2 e^{-x-2} (x^2 (-\text{Ei}(2(x + 1))) - 2x \text{Ei}(2(x + 1)) - \text{Ei}(2(x + 1)) + 2e^{2x+2}) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 42

$$\{y(x) = \_C1 e^{-x} (1 + x)^2 + \_C2 (e^{-2-x} (1 + x)^2 \text{Ei}(1, -2x - 2) + 2e^x)\}$$

**3.243 ODE No. 1243**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) + 4x \frac{d}{dx} y(x) + (x^2 + 1) y(x) = 0$$

**Mathematica:** cpu = 0.029004 (sec), leaf count = 45

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{-ix}}{x^2 - 1} - \frac{ic_2 e^{ix}}{2(x^2 - 1)} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 27

$$\left\{ y(x) = \frac{-C1 \sin(x)}{x^2 - 1} + \frac{-C2 \cos(x)}{x^2 - 1} \right\}$$

**3.244 ODE No. 1244**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) + 2(n + 1)x \frac{d}{dx} y(x) - (v + n + 1)(v - n)y(x) = 0$$

**Mathematica:** cpu = 0.026003 (sec), leaf count = 42

$$\left\{ \left\{ y(x) \rightarrow c_1 (x^2 - 1)^{-n/2} P_v^n(x) + c_2 (x^2 - 1)^{-n/2} Q_v^n(x) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 (x^2 - 1)^{-\frac{n}{2}} \text{LegendreP}(v, n, x) + \_C2 (x^2 - 1)^{-\frac{n}{2}} \text{LegendreQ}(v, n, x) \right\}$$

**3.245 ODE No. 1245**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) - 2(n - 1)x \frac{d}{dx} y(x) - (v - n + 1)(v + n)y(x) = 0$$

**Mathematica:** cpu = 0.021003 (sec), leaf count = 42

$$\left\{ \left\{ y(x) \rightarrow c_1 (x^2 - 1)^{n/2} P_v^n(x) + c_2 (x^2 - 1)^{n/2} Q_v^n(x) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 (x^2 - 1)^{\frac{n}{2}} \text{LegendreP}(v, n, x) + \_C2 (x^2 - 1)^{\frac{n}{2}} \text{LegendreQ}(v, n, x) \right\}$$

**3.246 ODE No. 1246**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) - 2(v - 1)x \frac{d}{dx} y(x) - 2vy(x) = 0$$

**Mathematica:** cpu = 0.021003 (sec), leaf count = 42

$$\left\{ \left\{ y(x) \rightarrow c_1 (x^2 - 1)^{v/2} P_v^v(x) + c_2 (x^2 - 1)^{v/2} Q_v^v(x) \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 (x^2 - 1)^v + \_C2 (x^2 - 1)^v x {}_2F_1\left(\frac{1}{2}, v + 1; \frac{3}{2}; x^2\right) \right\}$$

**3.247 ODE No. 1247**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) + 2ax \frac{d}{dx} y(x) + a(a - 1) y(x) = 0$$

**Mathematica:** cpu = 0.224528 (sec), leaf count = 97

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt{1 - x^2} (x^2 - 1)^{-a/2} e^{-\sqrt{(a-1)^2} \tanh^{-1}(x)} + \frac{c_2 \sqrt{1 - x^2} (x^2 - 1)^{-a/2} e^{\sqrt{(a-1)^2} \tanh^{-1}(x)}}{2\sqrt{(a-1)^2}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 27

$$\{y(x) = \_C1 (1 + x)^{1-a} + \_C2 (x - 1)^{1-a}\}$$

**3.248 ODE No. 1248**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) + ax \frac{d}{dx} y(x) + (bx^2 + cx + d) y(x) = 0$$

**Mathematica:** cpu = 2.122269 (sec), leaf count = 57

$$\{\{y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{(bx^2 + cx + d) y(x) + xay'(x) + (x^2 - 1) y''(x) = 0, y(0) = c_1, y'(0) = c_2\})\}\}$$

**Maple:** cpu = 0.172 (sec), leaf count = 150

$$\left\{ y(x) = \_C1 e^{\sqrt{-bx}} (x^2 - 1)^{-\frac{a}{4}} ((1 + x)(x - 1))^{\frac{a}{4}} \text{HeunC}\left(4\sqrt{-b}, \frac{a}{2} - 1, \frac{a}{2} - 1, 2c, d - c - \frac{a^2}{8} + b + \frac{1}{2}, \dots\right) \right\}$$

**3.249 ODE No. 1249**

$$(x^2 - 1) \frac{d^2}{dx^2} y(x) + (ax + b) \frac{d}{dx} y(x) + cy(x) = 0$$

**Mathematica:** cpu = 0.175022 (sec), leaf count = 193

$$\left\{ \left\{ y(x) \rightarrow c_2 2^{\frac{1}{2}(a+b-2)} (x - 1)^{\frac{1}{2}(-a-b+2)} {}_2F_1\left(-\frac{b}{2} - \frac{1}{2}\sqrt{a^2 - 2a - 4c + 1} + \frac{1}{2}, -\frac{b}{2} + \frac{1}{2}\sqrt{a^2 - 2a - 4c + 1} + \dots\right) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 134

$$\left\{ y(x) = \_C1 {}_2F_1\left(-\frac{1}{2} - \frac{1}{2}\sqrt{a^2 - 2a - 4c + 1} + \frac{a}{2}, -\frac{1}{2} + \frac{1}{2}\sqrt{a^2 - 2a - 4c + 1} + \frac{a}{2}; \frac{a}{2} - \frac{b}{2}; \frac{1}{2} + \frac{x}{2}\right) + \dots \right\}$$

**3.250 ODE No. 1250**

$$\boxed{(-a^2 + x^2) \frac{d^2}{dx^2}y(x) + 8x \frac{d}{dx}y(x) + 12y(x) = 0}$$

**Mathematica:** cpu = 0.047506 (sec), leaf count = 41

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2(a^2 + 3x^2)}{3(a-x)^3(a+x)^3} + \frac{c_1}{(a+x)^3} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 52

$$\left\{ y(x) = \frac{-C1(a^2 + 3x^2)}{(a-x)^3(x+a)^3} + \frac{-C2x(3a^2 + x^2)}{(a-x)^3(x+a)^3} \right\}$$

**3.251 ODE No. 1251**

$$\boxed{x(1+x) \frac{d^2}{dx^2}y(x) - (x-1) \frac{d}{dx}y(x) + y(x) = 0}$$

**Mathematica:** cpu = 0.035005 (sec), leaf count = 25

$$\{\{y(x) \rightarrow c_1(x-1) + c_2(x \log(x) - \log(x) - 4)\}\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 20

$$\{y(x) = \_C1(x-1) + \_C2(-4 + (x-1) \ln(x))\}$$

**3.252 ODE No. 1252**

$$\boxed{x(1+x) \frac{d^2}{dx^2}y(x) + (ax+b) \frac{d}{dx}y(x) + cy(x) = 0}$$

**Mathematica:** cpu = 0.161521 (sec), leaf count = 151

$$\left\{ \left\{ y(x) \rightarrow c_2 x^{1-b} {}_2F_1\left(\frac{a}{2} - b - \frac{1}{2}\sqrt{a^2 - 2a - 4c + 1} + \frac{1}{2}, \frac{a}{2} - b + \frac{1}{2}\sqrt{a^2 - 2a - 4c + 1} + \frac{1}{2}; 2 - b; -x\right) \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 124

$$\left\{ y(x) = \_C1 {}_2F_1\left(-\frac{1}{2} - \frac{1}{2}\sqrt{a^2 - 2a - 4c + 1} + \frac{a}{2}, -\frac{1}{2} + \frac{1}{2}\sqrt{a^2 - 2a - 4c + 1} + \frac{a}{2}; a - b; 1 + x\right) + \_C2 \dots \right\}$$

### 3.253 ODE No. 1253

$$x(1+x) \frac{d^2}{dx^2} y(x) + (3x+2) \frac{d}{dx} y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.025003 (sec), leaf count = 34

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt{2}c_1}{x} + \frac{c_2 \log(2x+2)}{\sqrt{2}x} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 16

$$\left\{ y(x) = \frac{\ln(1+x) \_C1 + \_C2}{x} \right\}$$

### 3.254 ODE No. 1254

$$(x^2 + x - 2) \frac{d^2}{dx^2} y(x) + (x^2 - x) \frac{d}{dx} y(x) - (6x^2 + 7x) y(x) = 0$$

**Mathematica:** cpu = 0.088511 (sec), leaf count = 69

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{5} c_2 e^{-3x-5} (195 e^{5x} x \text{Ei}(5-5x) - 195 e^{5x} \text{Ei}(5-5x) + e^5 x + 44 e^5) - c_1 e^{2x} (x-1) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 44

$$\left\{ y(x) = \_C1 e^{2x} (x-1) + \_C2 (195 e^{-5+2x} (x-1) \text{Ei}(1, 5x-5) - e^{-3x} (x+44)) \right\}$$

### 3.255 ODE No. 1255

$$x(x-1) \frac{d^2}{dx^2} y(x) + a \frac{d}{dx} y(x) - 2y(x) = 0$$

**Mathematica:** cpu = 0.204526 (sec), leaf count = 118

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1(a^2 + 2ax - a + 2x^2 - 2x)}{a^2 + 3a + 4} + \frac{c_2 x^{a+1} (a^2 + 2ax - a + 2x^2 - 2x) (1-x)^{1-a}}{(a-1)a(a+1)(a^2 + 3a + 4)(a^2 + a(2x-1) + 2(x-1)x)} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 42

$$\left\{ y(x) = (a^2 + 2ax + 2x^2 - a - 2x) \_C1 + \frac{\_C2 x^a x(x-1)}{(x-1)^a} \right\}$$

**3.256 ODE No. 1256**

$$x(x-1) \frac{d^2}{dx^2} y(x) + (2x-1) \frac{d}{dx} y(x) - v(v+1) y(x) = 0$$

**Mathematica:** cpu = 0.023003 (sec), leaf count = 26

$$\{ \{ y(x) \rightarrow c_1 P_v(2x-1) + c_2 Q_v(2x-1) \} \}$$

**Maple:** cpu = 0.078 (sec), leaf count = 51

$$\{ y(x) = \_C1 {}_2F_1(-v, -v; -2v; x^{-1}) x^v + \_C2 {}_2F_1(v+1, v+1; 2+2v; x^{-1}) x^{-v-1} \}$$

**3.257 ODE No. 1257**

$$x(x-1) \frac{d^2}{dx^2} y(x) + ((a+1)x+b) \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.045506 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 x^{b+1} {}_2F_1(b+1, a+b+1; b+2; x)}{b+1} + c_2 \right\} \right\}$$

**Maple:** cpu = 0.172 (sec), leaf count = 27

$$\{ y(x) = \_C1 + {}_2F_1(b+1, a+b+1; b+2; x) x^{b+1} \_C2 \}$$

**3.258 ODE No. 1258**

$$x(x-1) \frac{d^2}{dx^2} y(x) + (ax+b) \frac{d}{dx} y(x) + cy(x) = 0$$

**Mathematica:** cpu = 0.162021 (sec), leaf count = 146

$$\left\{ \left\{ y(x) \rightarrow (-1)^{b+1} c_2 x^{b+1} {}_2F_1\left(\frac{a}{2} + b - \frac{1}{2} \sqrt{a^2 - 2a - 4c + 1} + \frac{1}{2}, \frac{a}{2} + b + \frac{1}{2} \sqrt{a^2 - 2a - 4c + 1} + \frac{1}{2}; b + 2, x\right) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 110

$$\{ y(x) = \_C1 {}_2F_1\left(-\frac{1}{2} - \frac{1}{2} \sqrt{a^2 - 2a - 4c + 1} + \frac{a}{2}, -\frac{1}{2} + \frac{1}{2} \sqrt{a^2 - 2a - 4c + 1} + \frac{a}{2}; -b; x\right) + \_C2 x^{b+1} \}$$

### 3.259 ODE No. 1259

$$x(x-1) \frac{d^2}{dx^2} y(x) + ((a+1)x+b) \frac{d}{dx} y(x) - ly(x) = 0$$

**Mathematica:** cpu = 0.142018 (sec), leaf count = 120

$$\left\{ \left\{ y(x) \rightarrow (-1)^{b+1} c_2 x^{b+1} {}_2F_1\left(\frac{a}{2} + b - \frac{1}{2}\sqrt{a^2 + 4l} + 1, \frac{a}{2} + b + \frac{1}{2}\sqrt{a^2 + 4l} + 1; b + 2; x\right) + c_1 {}_2F_1\left(\frac{a}{2} - \frac{1}{2}\sqrt{a^2 + 4l} + 1, \frac{a}{2} + b + \frac{1}{2}\sqrt{a^2 + 4l} + 1; b + 2; x\right) \right. \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 92

$$\left\{ y(x) = -C1 {}_2F_1\left(\frac{a}{2} - \frac{1}{2}\sqrt{a^2 + 4l}, \frac{a}{2} + \frac{1}{2}\sqrt{a^2 + 4l}; -b; x\right) + -C2 x^{b+1} {}_2F_1\left(\frac{a}{2} - \frac{1}{2}\sqrt{a^2 + 4l} + b + 1, \frac{a}{2} + \frac{1}{2}\sqrt{a^2 + 4l} + b + 1; b + 2; x\right) \right.$$

### 3.260 ODE No. 1260

$$x(x-1) \frac{d^2}{dx^2} y(x) + ((a1+b1+1)x-d1) \frac{d}{dx} y(x) + a1 b1 d1 = 0$$

**Mathematica:** cpu = 0.160020 (sec), leaf count = 65

$$\left\{ \left\{ y(x) \rightarrow a1 b1 x \Gamma(d1 + 1) {}_3\tilde{F}_2(1, a1 + b1 + 1, 1; d1 + 1, 2; x) - \frac{c_1 x^{1-d1} {}_2F_1(1 - d1, a1 + b1 - d1 + 1; 2 - d1; x)}{d1 - 1} \right. \right.$$

**Maple:** cpu = 0.296 (sec), leaf count = 76

$$\left\{ y(x) = \int \left( -(\text{signum}(x-1))^{a1+b1-d1} (-\text{signum}(x-1))^{-a1-b1+d1} {}_2F_1(d1, -a1 - b1 + d1; 1 + d1; x) \right) dx \right.$$

### 3.261 ODE No. 1261

$$x(x+2) \frac{d^2}{dx^2} y(x) + 2(n+1 + (n+1-2l)x - lx^2) \frac{d}{dx} y(x) + (2l(p-n-1)x + 2pl+m)y(x) = 0$$

**Mathematica:** cpu = 2.666839 (sec), leaf count = 82

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{(-2xl - 2xnl + 2xpl + 2pl + m)y(x) + 2(-lx^2 - 2lx + nx + x + n)\}) \right. \right.$$

**Maple:** cpu = 0.171 (sec), leaf count = 124

$$\left\{ y(x) = -C1 \text{HeunC}\left(4l, n, n, -4pl, \frac{(4n+4p+4)l}{2} - \frac{n^2}{2} + m - n, -\frac{x}{2}\right) (x+2)^{-\frac{n}{2}-\frac{1}{2}} \left(-\frac{x}{2} - 1\right)^{\frac{n}{2}+\frac{1}{2}} \right.$$

**3.262 ODE No. 1262**

$$(1+x)^2 \frac{d^2}{dx^2} y(x) + (x^2+x-1) \frac{d}{dx} y(x) - (x+2)y(x) = 0$$

**Mathematica:** cpu = 38.898939 (sec), leaf count = 87

$$\left\{ \left\{ y(x) \rightarrow c_2 e^{-x} \int_1^x (K[1] + 1)^{\frac{K[1]}{K[1]+1} + \frac{1}{K[1]+1}} \exp\left(-\frac{K[1]^2}{K[1]+1} - \frac{K[1]}{K[1]+1} + 2K[1] - \frac{1}{K[1]+1}\right) dK[1] + c_1 \right\} \right.$$

**Maple:** cpu = 0.171 (sec), leaf count = 55

$$\left\{ y(x) = \_C1 e^{-x} HeunD\left(4, 4, -8, 12, \frac{x}{x+2}\right) (1+x) + \_C2 HeunD\left(-4, 4, -8, 12, \frac{x}{x+2}\right) (1+x) e^{\frac{x-1}{2x+1}} \right.$$

**3.263 ODE No. 1263**

$$x(x+3) \frac{d^2}{dx^2} y(x) + (3x-1) \frac{d}{dx} y(x) + y(x) - (20x+30)(x^2+3x)^{7/3} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

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**Maple:** cpu = 0.047 (sec), leaf count = 52

$$\left\{ y(x) = 1 \left( \_C2 + \int \frac{1}{x^2+3x} \left( \_C1 + 3(x^2+3x)^{7/3} x(x+3) \right) (x+3)^{7/3} x^{-4/3} dx \right) x^{4/3} (x+3)^{-7/3} \right\}$$

**3.264 ODE No. 1264**

$$(x^2+3x+4) \frac{d^2}{dx^2} y(x) + (x^2+x+1) \frac{d}{dx} y(x) - (2x+3)y(x) = 0$$

**Mathematica:** cpu = 0.064008 (sec), leaf count = 23

$$\left\{ \left\{ y(x) \rightarrow c_2(x^2+x+3) + c_1 e^{-x} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 19

$$\left\{ y(x) = \_C1 e^{-x} + \_C2 (x^2+x+3) \right\}$$



### 3.265 ODE No. 1265

$$(x-1)(x-2) \frac{d^2}{dx^2} y(x) - (2x-3) \frac{d}{dx} y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.042505 (sec), leaf count = 64

$$\left\{ \left\{ y(x) \rightarrow c_1 (x^2 - 3x + 2) P_{\frac{1}{2}}^2(-1+\sqrt{5})(2x-3) + c_2 (x^2 - 3x + 2) Q_{\frac{1}{2}}^2(-1+\sqrt{5})(2x-3) \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 97

$$\left\{ y(x) = -C1 {}_2F_1\left(\frac{1}{2} - \frac{\sqrt{5}}{2}, \frac{5}{2} - \frac{\sqrt{5}}{2}; -\sqrt{5} + 1; (x-1)^{-1}(x-2)^2(x-1)^{\frac{\sqrt{5}}{2}-\frac{1}{2}}\right) + -C2 {}_2F_1\left(\frac{1}{2} + \frac{\sqrt{5}}{2}, \frac{5}{2} + \frac{\sqrt{5}}{2}; -\sqrt{5} + 1; (x-1)^{-1}(x-2)^2(x-1)^{\frac{\sqrt{5}}{2}-\frac{1}{2}}\right) \right\}$$

### 3.266 ODE No. 1266

$$(x-2)^2 \frac{d^2}{dx^2} y(x) - (x-2) \frac{d}{dx} y(x) - 3y(x) = 0$$

**Mathematica:** cpu = 0.029504 (sec), leaf count = 22

$$\left\{ \left\{ y(x) \rightarrow c_1 (x-2)^3 + \frac{c_2}{x-2} \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 19

$$\left\{ y(x) = \frac{-C1}{x-2} + -C2 (x-2)^3 \right\}$$

### 3.267 ODE No. 1267

$$2x^2 \frac{d^2}{dx^2} y(x) - (2x^2 + l - 5x) \frac{d}{dx} y(x) - (4x-1)y(x) = 0$$

**Mathematica:** cpu = 34.197343 (sec), leaf count = 205

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt{\frac{\pi}{2}} c_2 l \left( e^{2\sqrt{2}\sqrt{-l}} \operatorname{erf}\left(\frac{\sqrt{-l}}{\sqrt{2}\sqrt{x}} + \sqrt{x}\right) + \operatorname{erf}\left(\frac{\sqrt{2}\sqrt{-l}-2x}{2\sqrt{x}}\right) + \operatorname{erf}\left(1 - \frac{\sqrt{-l}}{\sqrt{2}}\right) - e^{2\sqrt{2}\sqrt{-l}} \operatorname{erf}\left(\frac{\sqrt{-l}}{\sqrt{2}} + 1\right) \right)}{(-l)^{3/2}} \right\} \right\}$$

**Maple:** cpu = 0.046 (sec), leaf count = 41

$$\left\{ y(x) = e^x \left( -C1 \int \frac{1}{2e^x} e^{\frac{l}{2x}} x^{-\frac{3}{2}} dx + -C2 \right) \frac{1}{\sqrt{x}} \left( e^{\frac{l}{2x}} \right)^{-1} \right\}$$

**3.268 ODE No. 1268**

$$2x(x-1) \frac{d^2}{dx^2}y(x) + (2x-1) \frac{d}{dx}y(x) + (ax+b)y(x) = 0$$

**Mathematica:** cpu = 1.377675 (sec), leaf count = 55
$$\{ \{y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{(xa+b)y(x) + (2x-1)y'(x) + 2(x-1)xy''(x) = 0, y(2) = c_1, y'(2) = c_2\})\} \}$$
**Maple:** cpu = 0.078 (sec), leaf count = 39
$$\{y(x) = \_C1 \text{MathieuC}\left(-a - 2b, \frac{a}{2}, \arccos(\sqrt{x})\right) + \_C2 \text{MathieuS}\left(-a - 2b, \frac{a}{2}, \arccos(\sqrt{x})\right)\}$$
**3.269 ODE No. 1269**

$$2x(x-1) \frac{d^2}{dx^2}y(x) + ((2v+5)x - 2v - 3) \frac{d}{dx}y(x) + (v+1)y(x) = 0$$

**Mathematica:** cpu = 0.084511 (sec), leaf count = 60
$$\left\{ \left\{ y(x) \rightarrow c_1 {}_2F_1\left(\frac{1}{2}, v+1; v+\frac{3}{2}; x\right) + c_2 i^{-2v-1} x^{\frac{1}{2}(-2v-1)} {}_2F_1\left(\frac{1}{2}, -v; \frac{1}{2}-v; x\right) \right\} \right\}$$
**Maple:** cpu = 0.062 (sec), leaf count = 40
$$\left\{ y(x) = \_C1 {}_2F_1\left(\frac{1}{2}, v+1; \frac{3}{2}+v; x\right) + \_C2 x^{-\frac{1}{2}-v} {}_2F_1\left(\frac{1}{2}, -v; \frac{1}{2}-v; x\right) \right\}$$
**3.270 ODE No. 1270**

$$(2x^2 + 6x + 4) \frac{d^2}{dx^2}y(x) + (10x^2 + 21x + 8) \frac{d}{dx}y(x) + (12x^2 + 17x + 8)y(x) = 0$$

**Mathematica:** cpu = 162.565643 (sec), leaf count = 57
$$\left\{ \left\{ y(x) \rightarrow c_2 e^{-3x} (x+2)^4 \left( \int_1^x \frac{e^{K[1]} (K[1]+1)^{3/2}}{(K[1]+2)^5} dK[1] \right) + c_1 e^{-3x} (x+2)^4 \right\} \right\}$$
**Maple:** cpu = 0.125 (sec), leaf count = 54
$$\left\{ y(x) = \_C1 e^{-2x} (x+2)^4 \text{HeunC}\left(-1, -\frac{5}{2}, 4, -\frac{7}{4}, \frac{7}{2}, -1-x\right) + \_C2 e^{-2x} (x+2)^4 (1+x)^{\frac{5}{2}} \text{HeunC}\left(-\right)$$

**3.271 ODE No. 1271**

$$4x^2 \frac{d^2}{dx^2} y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.010501 (sec), leaf count = 27

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt{x} + \frac{1}{2} c_2 \sqrt{x} \log(x) \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 17

$$\{y(x) = \_C1 \sqrt{x} + \_C2 \sqrt{x} \ln(x)\}$$

**3.272 ODE No. 1272**

$$4x^2 \frac{d^2}{dx^2} y(x) + (4a^2 x^2 + 1) y(x) = 0$$

**Mathematica:** cpu = 0.012002 (sec), leaf count = 32

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt{x} J_0(ax) + c_2 \sqrt{x} Y_0(ax) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 25

$$\{y(x) = \_C1 \sqrt{x} J_0(ax) + \_C2 \sqrt{x} Y_0(ax)\}$$

**3.273 ODE No. 1273**

$$4x^2 \frac{d^2}{dx^2} y(x) - (-4kx + 4m^2 + x^2 - 1) y(x) = 0$$

**Mathematica:** cpu = 0.017002 (sec), leaf count = 20

$$\left\{ \left\{ y(x) \rightarrow c_1 M_{k,m}(x) + c_2 W_{k,m}(x) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 17

$$\{y(x) = \_C1 M_{k,m}(x) + \_C2 W_{k,m}(x)\}$$

### 3.274 ODE No. 1274

$$4x^2 \frac{d^2}{dx^2} y(x) + 4x \frac{d}{dx} y(x) + (-v^2 + x) y(x) = 0$$

**Mathematica:** cpu = 0.043506 (sec), leaf count = 38

$$\left\{ \left\{ y(x) \rightarrow c_1 \Gamma(1-v) J_{-v}(\sqrt{x}) + c_2 \Gamma(v+1) J_v(\sqrt{x}) \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 19

$$\left\{ y(x) = \_C1 J_v(\sqrt{x}) + \_C2 Y_v(\sqrt{x}) \right\}$$

### 3.275 ODE No. 1275

$$4x^2 \frac{d^2}{dx^2} y(x) + 4x \frac{d}{dx} y(x) + (-x^2 + 2(1-m+2l)x - m^2 + 1) y(x) = 0$$

**Mathematica:** cpu = 0.037005 (sec), leaf count = 120

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{1}{2}(\sqrt{m^2-1} \log(x)-x)} U\left(\frac{1}{2}(-2l+m+\sqrt{m^2-1}), \sqrt{m^2-1}+1, x\right) + c_2 e^{\frac{1}{2}(\sqrt{m^2-1} \log(x)-x)} L_{\frac{1}{2}}^{\sqrt{m^2-1}}\left(\frac{1}{2}(-2l+m+\sqrt{m^2-1})\right) \right\} \right\}$$

**Maple:** cpu = 0.110 (sec), leaf count = 55

$$\left\{ y(x) = \_C1 M_{l-\frac{m}{2}+\frac{1}{2}, \frac{1}{2}\sqrt{m-1}\sqrt{m+1}}(x) \frac{1}{\sqrt{x}} + \_C2 W_{l-\frac{m}{2}+\frac{1}{2}, \frac{1}{2}\sqrt{m-1}\sqrt{m+1}}(x) \frac{1}{\sqrt{x}} \right\}$$

### 3.276 ODE No. 1276

$$4x^2 \frac{d^2}{dx^2} y(x) + 4x \frac{d}{dx} y(x) - (4x^2 + 1) y(x) - 4\sqrt{x^3} e^x = 0$$

**Mathematica:** cpu = 0.046506 (sec), leaf count = 55

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{-x}}{\sqrt{x}} + \frac{c_2 e^x}{2\sqrt{x}} + \frac{e^x \sqrt{x^3} (2x-1)}{4x^2} \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 31

$$\left\{ y(x) = \sinh(x) \_C2 \frac{1}{\sqrt{x}} + \cosh(x) \_C1 \frac{1}{\sqrt{x}} + \frac{e^x}{2x} \sqrt{x^3} \right\}$$

**3.277 ODE No. 1277**

$$4x^2 \frac{d^2}{dx^2} y(x) + 4x \frac{d}{dx} y(x) - (ax^2 + 1) y(x) = 0$$

**Mathematica:** cpu = 0.028504 (sec), leaf count = 51

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{-\frac{\sqrt{ax}}{2}}}{\sqrt{x}} + \frac{c_2 e^{\frac{\sqrt{ax}}{2}}}{\sqrt{a}\sqrt{x}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 29

$$\left\{ y(x) = \_C1 \sinh\left(\frac{x}{2}\sqrt{a}\right) \frac{1}{\sqrt{x}} + \_C2 \cosh\left(\frac{x}{2}\sqrt{a}\right) \frac{1}{\sqrt{x}} \right\}$$

**3.278 ODE No. 1278**

$$4x^2 \frac{d^2}{dx^2} y(x) + 4x \frac{d}{dx} y(x) + f(x) y(x) = 0$$

**Mathematica:** cpu = 0.268034 (sec), leaf count = 28

$$\text{DSolve}[f(x)y(x) + 4x^2y''(x) + 4xy'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.0 (sec), leaf count = 33

$$\left\{ y(x) = \text{DESol}\left(\left\{ \frac{f(x) - Y(x)}{4x^2} + \frac{\frac{d}{dx} - Y(x)}{x} + \frac{d^2}{dx^2} - Y(x) \right\}, \{-Y(x)\}\right) \right\}$$

**3.279 ODE No. 1279**

$$4x^2 \frac{d^2}{dx^2} y(x) + 5x \frac{d}{dx} y(x) - y(x) - \ln(x) = 0$$

**Mathematica:** cpu = 0.163021 (sec), leaf count = 74

$$\left\{ \left\{ y(x) \rightarrow c_1 x^{\frac{1}{2}\left(\frac{\sqrt{17}}{4} - \frac{1}{4}\right)} + c_2 x^{\frac{1}{2}\left(-\frac{1}{4} - \frac{\sqrt{17}}{4}\right)} - \frac{256(\log(x) + 1)}{(\sqrt{17} - 1)^2 (1 + \sqrt{17})^2} \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 32

$$\left\{ y(x) = x^{-\frac{1}{8} + \frac{\sqrt{17}}{8}} \_C2 + x^{-\frac{1}{8} - \frac{\sqrt{17}}{8}} \_C1 - \ln(x) - 1 \right\}$$

**3.280 ODE No. 1280**

$$4x^2 \frac{d^2}{dx^2} y(x) + 8x \frac{d}{dx} y(x) - (4x^2 + 12x + 3) y(x) = 0$$

**Mathematica:** cpu = 0.039005 (sec), leaf count = 52

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 e^{-x} (4e^{2x} x^2 \text{Ei}(-2x) + 2x - 1)}{2x^{3/2}} + c_1 e^x \sqrt{x} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 41

$$\left\{ y(x) = \_C1 \sqrt{x} e^x + \_C2 (4x^2 e^x \text{Ei}(1, 2x) - 2e^{-x} x + e^{-x}) x^{-\frac{3}{2}} \right\}$$

**3.281 ODE No. 1281**

$$4x^2 \frac{d^2}{dx^2} y(x) - 4x(2x - 1) \frac{d}{dx} y(x) + (4x^2 - 4x - 1) y(x) = 0$$

**Mathematica:** cpu = 0.020503 (sec), leaf count = 28

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^x}{\sqrt{x}} + c_2 e^x \sqrt{x} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 19

$$\left\{ y(x) = \_C1 e^x \frac{1}{\sqrt{x}} + \_C2 \sqrt{x} e^x \right\}$$

**3.282 ODE No. 1282**

$$4x^2 \frac{d^2}{dx^2} y(x) + 4x^3 \frac{d}{dx} y(x) + (x^2 + 6)(x^2 - 4) y(x) = 0$$

**Mathematica:** cpu = 0.024003 (sec), leaf count = 39

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{-\frac{x^2}{4}}}{x^2} + \frac{1}{5} c_2 e^{-\frac{x^2}{4}} x^3 \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 27

$$\left\{ y(x) = \frac{C1}{x^2} e^{-\frac{x^2}{4}} + \_C2 x^3 e^{-\frac{x^2}{4}} \right\}$$

### 3.283 ODE No. 1283

$$4x^2 \frac{d^2}{dx^2} y(x) + 4x^2 \ln(x) \frac{d}{dx} y(x) + (x^2 (\ln(x))^2 + 2x - 8) y(x) - 4x^2 \sqrt{\frac{e^x}{x^x}} = 0$$

**Mathematica:** cpu = 0.098513 (sec), leaf count = 90

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{x/2} x^{-\frac{x}{2}-1} + \frac{1}{3} c_2 e^{x/2} x^{2-\frac{x}{2}} + \frac{1}{9} \left( 3x^2 \sqrt{e^x x^{-x}} \log(x) - x^2 \sqrt{e^x x^{-x}} \right) \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 52

$$\left\{ y(x) = x^{-\frac{x}{2}-1} e^{\frac{x}{2}} \_C2 + x^{-\frac{x}{2}+2} e^{\frac{x}{2}} \_C1 + \frac{x^2(3 \ln(x) - 1)}{9} \sqrt{x^{-x} e^x} \right\}$$

### 3.284 ODE No. 1284

$$(2x+1)^2 \frac{d^2}{dx^2} y(x) - 2(2x+1) \frac{d}{dx} y(x) - 12y(x) - 3x - 1 = 0$$

**Mathematica:** cpu = 0.044506 (sec), leaf count = 47

$$\left\{ \left\{ y(x) \rightarrow c_1 (2x+1)^3 + \frac{c_2}{2x+1} + \frac{-72x^2 - 56x - 7}{192(2x+1)} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 42

$$\left\{ y(x) = \frac{\_C1}{2x+1} + (2x+1)^3 \_C2 - \frac{72x^2 + 56x + 7}{384x + 192} \right\}$$

### 3.285 ODE No. 1285

$$x(4x-1) \frac{d^2}{dx^2} y(x) + ((4a+2)x-a) \frac{d}{dx} y(x) + a(a-1)y(x) = 0$$

**Mathematica:** cpu = 0.335543 (sec), leaf count = 134

$$\left\{ \left\{ y(x) \rightarrow \frac{2c_1 \sqrt[4]{4x-1} x^{\frac{1}{2}-\frac{a}{2}} e^{\sqrt{-(a-1)^2 \tan^{-1}(\sqrt{4x-1})}}}{\sqrt[4]{1-4x}} - \frac{c_2 \sqrt[4]{4x-1} x^{\frac{1}{2}-\frac{a}{2}} e^{-\sqrt{-(a-1)^2 \tan^{-1}(\sqrt{4x-1})}}}{2\sqrt{-(a-1)^2} \sqrt[4]{1-4x}} \right\} \right\}$$

**Maple:** cpu = 0.079 (sec), leaf count = 52

$$\left\{ y(x) = \_C1 {}_2F_1\left(\frac{a}{2}, \frac{a}{2} - \frac{1}{2}; a; 4x\right) + \_C2 x^{1-a} {}_2F_1\left(1 - \frac{a}{2}, -\frac{a}{2} + \frac{1}{2}; -a + 2; 4x\right) \right\}$$

### 3.286 ODE No. 1286

$$(3x - 1)^2 \frac{d^2}{dx^2} y(x) + 3(3x - 1) \frac{d}{dx} y(x) - 9y(x) - (\ln(3x - 1))^2 = 0$$

**Mathematica:** cpu = 0.103013 (sec), leaf count = 101

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1((1 - 3x)^2 + 1)}{2(1 - 3x)} + \frac{ic_2((1 - 3x)^2 - 1)}{2(1 - 3x)} + \frac{-6x - 3x \log^2(3x - 1) + \log^2(3x - 1) + \log(3x - 1)}{9(3x - 1)} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 32

$$\left\{ y(x) = \frac{-C1}{3x - 1} + (3x - 1) \_C2 - \frac{(\ln(3x - 1))^2}{9} - \frac{2}{9} \right\}$$

### 3.287 ODE No. 1287

$$9x(x - 1) \frac{d^2}{dx^2} y(x) + 3(2x - 1) \frac{d}{dx} y(x) - 20y(x) = 0$$

**Mathematica:** cpu = 0.018502 (sec), leaf count = 83

$$\left\{ \left\{ y(x) \rightarrow c_2 \sqrt[3]{1 - x} \sqrt[3]{x} Q_1^{\frac{2}{3}}(2x - 1) - \frac{c_1(2 - 2x)^{2/3} \sqrt[3]{1 - xx^{2/3}}(6x - 5)}{3 \cdot 2^{2/3}(x - 1)\Gamma\left(\frac{4}{3}\right)} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 27

$$\left\{ y(x) = \_C1 (6x - 5) x^{\frac{2}{3}} + \_C2 (6x - 1) (x - 1)^{\frac{2}{3}} \right\}$$

### 3.288 ODE No. 1288

$$16x^2 \frac{d^2}{dx^2} y(x) + (4x + 3)y(x) = 0$$

**Mathematica:** cpu = 0.038505 (sec), leaf count = 47

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{i\sqrt{x}} \sqrt[4]{x} + ic_2 e^{-i\sqrt{x}} \sqrt[4]{x} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 23

$$\left\{ y(x) = \_C1 \sin(\sqrt{x}) \sqrt[4]{x} + \_C2 \sqrt[4]{x} \cos(\sqrt{x}) \right\}$$



**3.289 ODE No. 1289**

$$16x^2 \frac{d^2}{dx^2}y(x) + 32x \frac{d}{dx}y(x) - (4x + 5)y(x) = 0$$

**Mathematica:** cpu = 0.079510 (sec), leaf count = 53

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 e^{-\sqrt{x}}(\sqrt{x} + 1)}{x^{5/4}} - \frac{c_1 e^{\sqrt{x}}(\sqrt{x} - 1)}{x^{5/4}} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 35

$$\left\{ y(x) = -C1 e^{\sqrt{x}}(\sqrt{x} - 1) x^{-5/4} + -C2 e^{-\sqrt{x}}(\sqrt{x} + 1) x^{-5/4} \right\}$$

**3.290 ODE No. 1290**

$$(27x^2 + 4) \frac{d^2}{dx^2}y(x) + 27x \frac{d}{dx}y(x) - 3y(x) = 0$$

**Mathematica:** cpu = 0.175022 (sec), leaf count = 103

$$\left\{ \left\{ y(x) \rightarrow c_1 \cosh \left( \frac{\sqrt{-27x^2 - 4} \tan^{-1} \left( \frac{3x}{\sqrt{-9x^2 - \frac{4}{3}}} \right)}{3\sqrt{27x^2 + 4}} \right) + ic_2 \sinh \left( \frac{\sqrt{-27x^2 - 4} \tan^{-1} \left( \frac{3x}{\sqrt{-9x^2 - \frac{4}{3}}} \right)}{3\sqrt{27x^2 + 4}} \right) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 47

$$\left\{ y(x) = -C1 \sin \left( \frac{1}{3} \arctan \left( 3 \frac{\sqrt{3}x}{\sqrt{-27x^2 - 4}} \right) \right) + -C2 \cos \left( \frac{1}{3} \arctan \left( 3 \frac{\sqrt{3}x}{\sqrt{-27x^2 - 4}} \right) \right) \right\}$$

**3.291 ODE No. 1291**

$$48x(x - 1) \frac{d^2}{dx^2}y(x) + (152x - 40) \frac{d}{dx}y(x) + 53y(x) = 0$$

**Mathematica:** cpu = 0.078010 (sec), leaf count = 92

$$\left\{ \left\{ y(x) \rightarrow c_1 {}_2F_1 \left( \frac{13}{12} - \frac{\sqrt{5}}{6}, \frac{13}{12} + \frac{\sqrt{5}}{6}; \frac{5}{6}; x \right) + \sqrt[6]{-1} c_2 \sqrt[6]{x} {}_2F_1 \left( \frac{5}{4} - \frac{\sqrt{5}}{6}, \frac{5}{4} + \frac{\sqrt{5}}{6}; \frac{7}{6}; x \right) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 62

$$\left\{ y(x) = -C1 {}_2F_1 \left( \frac{13}{12} - \frac{\sqrt{2}\sqrt{5}}{12}, \frac{13}{12} + \frac{\sqrt{2}\sqrt{5}}{12}; \frac{5}{6}; x \right) + -C2 \sqrt[6]{x} {}_2F_1 \left( \frac{5}{4} - \frac{\sqrt{2}\sqrt{5}}{12}, \frac{5}{4} + \frac{\sqrt{2}\sqrt{5}}{12}; \frac{7}{6}; x \right) \right\}$$

**3.292 ODE No. 1292**

$$50x(x-1) \frac{d^2}{dx^2}y(x) + 25(2x-1) \frac{d}{dx}y(x) - 2y(x) = 0$$

**Mathematica:** cpu = 0.041505 (sec), leaf count = 53

$$\left\{ \left\{ y(x) \rightarrow c_1 \cosh \left( \frac{2}{5} \log(\sqrt{x-1} + \sqrt{x}) \right) + ic_2 \sinh \left( \frac{2}{5} \log(\sqrt{x-1} + \sqrt{x}) \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 31

$$\left\{ y(x) = \_C1 (\sqrt{x} + \sqrt{x-1})^{\frac{2}{5}} + \_C2 (\sqrt{x} + \sqrt{x-1})^{-\frac{2}{5}} \right\}$$

**3.293 ODE No. 1293**

$$144x(x-1) \frac{d^2}{dx^2}y(x) + (120x-48) \frac{d}{dx}y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.341543 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow (-1)^{2/3} c_2 x^{2/3} {}_2F_1 \left( \frac{7}{12}, \frac{7}{12}; \frac{5}{3}; x \right) + c_1 {}_2F_1 \left( -\frac{1}{12}, -\frac{1}{12}; \frac{1}{3}; x \right) \right\} \right\}$$

**Maple:** cpu = 0.046 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 \sqrt[3]{x} \text{LegendreP} \left( -\frac{1}{2}, \frac{2}{3}, \sqrt{1-x} \right) + \_C2 \sqrt[3]{x} \text{LegendreQ} \left( -\frac{1}{2}, \frac{2}{3}, \sqrt{1-x} \right) \right\}$$

**3.294 ODE No. 1294**

$$144x(x-1) \frac{d^2}{dx^2}y(x) + (168x-96) \frac{d}{dx}y(x) + y(x) = 0$$

**Mathematica:** cpu = 0.070009 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow c_1 {}_2F_1 \left( \frac{1}{12}, \frac{1}{12}; \frac{2}{3}; x \right) + \sqrt[3]{-1} c_2 \sqrt[3]{x} {}_2F_1 \left( \frac{5}{12}, \frac{5}{12}; \frac{4}{3}; x \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 \sqrt[6]{x} \text{LegendreP} \left( -\frac{1}{2}, \frac{1}{3}, \sqrt{1-x} \right) + \_C2 \sqrt[6]{x} \text{LegendreQ} \left( -\frac{1}{2}, \frac{1}{3}, \sqrt{1-x} \right) \right\}$$

### 3.295 ODE No. 1295

$$ax^2 \frac{d^2}{dx^2}y(x) + bx \frac{d}{dx}y(x) + (cx^2 + dx + f)y(x) = 0$$

**Mathematica:** cpu = 0.287037 (sec), leaf count = 310

$$\left\{ \left\{ y(x) \rightarrow c_1 U \left( -\frac{-\sqrt{ca} - id\sqrt{a} - \sqrt{c}\sqrt{a^2 - 2ba - 4fa + b^2}}{2a\sqrt{c}}, \frac{\sqrt{a^2 - 2ba - 4fa + b^2}}{a} + 1, \frac{2i\sqrt{cx}}{\sqrt{a}} \right) \exp \left( \right. \right.$$

**Maple:** cpu = 0.218 (sec), leaf count = 113

$$\left\{ y(x) = -C1 x^{-\frac{b}{2a}} M_{-\frac{i}{2}d\frac{1}{\sqrt{c}}\frac{1}{\sqrt{a}}, \frac{1}{2a}\sqrt{a^2+(-2b-4f)a+b^2}} \left( 2ix\sqrt{c}\frac{1}{\sqrt{a}} \right) + -C2 x^{-\frac{b}{2a}} W_{-\frac{i}{2}d\frac{1}{\sqrt{c}}\frac{1}{\sqrt{a}}, \frac{1}{2a}\sqrt{a^2+(-2b-4f)a+b^2}} \right.$$

### 3.296 ODE No. 1296

$$a2 x^2 \frac{d^2}{dx^2}y(x) + (a1 x^2 + b1 x) \frac{d}{dx}y(x) + (a0 x^2 + b0 x + c0)y(x) = 0$$

**Mathematica:** cpu = 0.571573 (sec), leaf count = 356

$$\left\{ \left\{ y(x) \rightarrow c_1 U \left( -\frac{2b0a2 - \sqrt{a1^2 - 4a0a2}a2 - a1b1 - \sqrt{a1^2 - 4a0a2}\sqrt{a2^2 - 2b1a2 - 4c0a2 + b1^2}}{2a2\sqrt{a1^2 - 4a0a2}}, \frac{\sqrt{a2^2 - 2b1a2 - 4c0a2 + b1^2}}{\sqrt{a2^2 - 2b1a2 - 4c0a2 + b1^2}} \right) \right.$$

**Maple:** cpu = 0.218 (sec), leaf count = 165

$$\left\{ y(x) = -C1 x^{-\frac{b1}{2a2}} e^{-\frac{a1x}{2a2}} M_{-\frac{a1b1-2a2b0}{2a2}\frac{1}{\sqrt{-4a0a2+a1^2}}, \frac{1}{2a2}\sqrt{a2^2+(-2b1-4c0)a2+b1^2}} \left( \frac{x}{a2}\sqrt{-4a0a2+a1^2} \right) + -C2 \right.$$

### 3.297 ODE No. 1297

$$(ax^2 + 1) \frac{d^2}{dx^2}y(x) + ax \frac{d}{dx}y(x) + by(x) = 0$$

**Mathematica:** cpu = 0.033504 (sec), leaf count = 52

$$\left\{ \left\{ y(x) \rightarrow c_2 \sin \left( \frac{\sqrt{b} \sinh^{-1}(\sqrt{ax})}{\sqrt{a}} \right) + c_1 \cos \left( \frac{\sqrt{b} \sinh^{-1}(\sqrt{ax})}{\sqrt{a}} \right) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 61

$$\left\{ y(x) = -C1 \left( \sqrt{ax} + \sqrt{ax^2 + 1} \right)^{i\sqrt{b}\frac{1}{\sqrt{a}}} + -C2 \left( \left( \sqrt{ax} + \sqrt{ax^2 + 1} \right)^{i\sqrt{b}\frac{1}{\sqrt{a}}} \right)^{-1} \right\}$$

### 3.298 ODE No. 1298

$$(ax^2 + 1) \frac{d^2}{dx^2}y(x) + bx \frac{d}{dx}y(x) + cy(x) = 0$$

**Mathematica:** cpu = 0.079510 (sec), leaf count = 162

$$\left\{ \left\{ y(x) \rightarrow c_1 (ax^2 + 1)^{\frac{2a-b}{4a}} P_{\frac{b-2a}{2a}}^{\frac{b-2a}{2a}} \left( \frac{i\sqrt{ax}}{\sqrt{a^2 - 2ba - 4ca + b^2 - a}} \right) + c_2 (ax^2 + 1)^{\frac{2a-b}{4a}} Q_{\frac{b-2a}{2a}}^{\frac{b-2a}{2a}} \left( \frac{i\sqrt{ax}}{\sqrt{a^2 - 2ba - 4ca + b^2 - a}} \right) \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 143

$$\left\{ y(x) = \_C1 (ax^2 + 1)^{\frac{2a-b}{4a}} \text{LegendreP} \left( \frac{1}{2a} \left( \sqrt{a^2 + (-2b - 4c)a + b^2 - a} \right), \frac{2a-b}{2a}, \sqrt{-ax} \right) + \_C2 (ax^2 + 1)^{\frac{2a-b}{4a}} \text{LegendreQ} \left( \frac{1}{2a} \left( \sqrt{a^2 + (-2b - 4c)a + b^2 - a} \right), \frac{2a-b}{2a}, \sqrt{-ax} \right) \right\}$$

### 3.299 ODE No. 1299

$$(a^2x^2 - 1) \frac{d^2}{dx^2}y(x) + 2a^2x \frac{d}{dx}y(x) = 0$$

**Mathematica:** cpu = 0.014002 (sec), leaf count = 19

$$\left\{ \left\{ y(x) \rightarrow c_2 - \frac{c_1 \tanh^{-1}(ax)}{a} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 31

$$\left\{ y(x) = \_C1 + \left( \frac{\ln(ax - 1)}{2a} - \frac{\ln(ax + 1)}{2a} \right) \_C2 \right\}$$

### 3.300 ODE No. 1300

$$(a^2x^2 - 1) \frac{d^2}{dx^2}y(x) + 2a^2x \frac{d}{dx}y(x) - 2a^2y(x) = 0$$

**Mathematica:** cpu = 0.016002 (sec), leaf count = 41

$$\left\{ \left\{ y(x) \rightarrow ac_1x + c_2 \left( ax \left( \frac{1}{2} \log(ax + 1) - \frac{1}{2} \log(1 - ax) \right) - 1 \right) \right\} \right\}$$

**Maple:** cpu = 0.046 (sec), leaf count = 32

$$\left\{ y(x) = x\_C1 + \_C2 \left( \frac{a \ln(ax - 1)x}{2} - \frac{a \ln(ax + 1)x}{2} + 1 \right) \right\}$$

### 3.301 ODE No. 1301

$$(ax^2 + bx) \frac{d^2}{dx^2} y(x) + 2b \frac{d}{dx} y(x) - 2ay(x) = 0$$

**Mathematica:** cpu = 0.033004 (sec), leaf count = 31

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2(ax + b)^3}{3ax} + \frac{c_1}{x} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 22

$$\left\{ y(x) = \frac{-C1}{x} + \frac{-C2(ax + b)^3}{x} \right\}$$

### 3.302 ODE No. 1302

$$A2(ax + b)^2 \frac{d^2}{dx^2} y(x) + A1(ax + b) \frac{d}{dx} y(x) + A0(ax + b)y(x) = 0$$

**Mathematica:** cpu = 0.084011 (sec), leaf count = 243

$$\left\{ \left\{ y(x) \rightarrow c_1 \left( \frac{2b}{a} + 2x \right)^{\frac{A1}{2aA2}} (2aA2x + 2A2b)^{-\frac{A1}{2aA2}} \left( -\frac{A0 \left( \frac{b}{a} + x \right)}{aA2} \right)^{\frac{1}{2} - \frac{A1}{2aA2}} I_{\frac{A1}{aA2} - 1} \left( 2\sqrt{-\frac{A0 \left( \frac{b}{a} + x \right)}{aA2}} \right) + \right.$$

**Maple:** cpu = 0.046 (sec), leaf count = 117

$$\left. \left\{ y(x) = -C1(ax + b)^{-\frac{aA2 + A1}{2aA2}} J_{\frac{aA2 - A1}{aA2}} \left( 2\sqrt{A0} \sqrt{\frac{ax + b}{a^2 A2}} \right) + -C2(ax + b)^{-\frac{aA2 + A1}{2aA2}} Y_{\frac{aA2 - A1}{aA2}} \left( 2\sqrt{A0} \sqrt{\frac{ax + b}{a^2 A2}} \right) \right\}$$

### 3.303 ODE No. 1303

$$(ax^2 + bx + c) \frac{d^2}{dx^2} y(x) + (dx + f) \frac{d}{dx} y(x) + gy(x) = 0$$

**Mathematica:** cpu = 14.510843 (sec), leaf count = 56

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{gy(x) + (xd + f)y'(x) + (ax^2 + bx + c)y''(x) = 0, y(0) = c_1, y'(0) = c_2\}) \right\} \right\}$$

**Maple:** cpu = 0.140 (sec), leaf count = 501

$$\left\{ y(x) = -C1 {}_2F_1\left(\frac{1}{2a} \left( -a + d + \sqrt{a^2 + (-2d - 4g)a + d^2} \right), -\frac{1}{2a} \left( a - d + \sqrt{a^2 + (-2d - 4g)a + d^2} \right) \right) \right\}$$

### 3.304 ODE No. 1304

$$x^3 \frac{d^2}{dx^2} y(x) + x \frac{d}{dx} y(x) - (2x + 3) y(x) = 0$$

**Mathematica:** cpu = 0.034004 (sec), leaf count = 50

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 \left( e^{\frac{1}{x}} \text{Ei}\left(-\frac{1}{x}\right) + 2x^3 - x^2 + x \right) + c_1 e^{\frac{1}{x}}}{6x} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 41

$$\left\{ y(x) = \frac{C1 e^{x^{-1}}}{x} + \frac{-C2 \left( -2x^3 + e^{x^{-1}} \text{Ei}(1, x^{-1}) + x^2 - x \right)}{x} \right\}$$

### 3.305 ODE No. 1305

$$x^3 \frac{d^2}{dx^2} y(x) + 2x \frac{d}{dx} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.071009 (sec), leaf count = 47

$$\left\{ \left\{ y(x) \rightarrow c_2 G_{1,2}^{2,0} \left( -\frac{2}{x} \middle| \begin{matrix} \frac{1}{2} \\ -1, 0 \end{matrix} \right) + c_1 e^{\frac{1}{x}} \left( I_0 \left( \frac{1}{x} \right) - I_1 \left( \frac{1}{x} \right) \right) \right\} \right\}$$

**Maple:** cpu = 0.046 (sec), leaf count = 47

$$\left\{ y(x) = -C1 e^{x^{-1}} (I_0(x^{-1}) - I_1(x^{-1})) + -C2 e^{x^{-1}} (K_0(-x^{-1}) - K_1(-x^{-1})) \right\}$$

### 3.306 ODE No. 1306

$$x^3 \frac{d^2}{dx^2} y(x) + x^2 \frac{d}{dx} y(x) + (ax^2 + bx + a) y(x) = 0$$

**Mathematica:** cpu = 1.002127 (sec), leaf count = 56

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{y''(x)x^3 + y'(x)x^2 + (ax^2 + bx + a) y(x) = 0, y(1) = c_1, y'(1) = c_2\}) \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 95

$$\left\{ y(x) = -C1 \text{HeunD} \left( 0, 8a + 4b, 0, 8a - 4b, \frac{1+x}{x-1} \right) + -C2 \text{HeunD} \left( 0, 8a + 4b, 0, 8a - 4b, \frac{1+x}{x-1} \right) \right\}$$

### 3.307 ODE No. 1307

$$x^3 \frac{d^2}{dx^2} y(x) + x(1+x) \frac{d}{dx} y(x) - 2y(x) = 0$$

**Mathematica:** cpu = 0.085011 (sec), leaf count = 54

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{\frac{1}{x}} (x+1)}{x} - \frac{c_2 \left( e^{\frac{1}{x}} x \operatorname{Ei}\left(-\frac{1}{x}\right) + e^{\frac{1}{x}} \operatorname{Ei}\left(-\frac{1}{x}\right) + x \right)}{x} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 38

$$\left\{ y(x) = \frac{-C1 e^{x^{-1}} (1+x)}{x} + \frac{-C2 \left( -e^{x^{-1}} (1+x) \operatorname{Ei}(1, x^{-1}) + x \right)}{x} \right\}$$

### 3.308 ODE No. 1308

$$x^3 \frac{d^2}{dx^2} y(x) - x^2 \frac{d}{dx} y(x) + xy(x) - (\ln(x))^3 = 0$$

**Mathematica:** cpu = 0.018502 (sec), leaf count = 41

$$\left\{ \left\{ y(x) \rightarrow c_1 x + c_2 x \log(x) + \frac{2 \log^3(x) + 6 \log^2(x) + 9 \log(x) + 6}{8x} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 36

$$\left\{ y(x) = x_{-} C2 + x \ln(x)_{-} C1 + \frac{2 (\ln(x))^3 + 6 (\ln(x))^2 + 9 \ln(x) + 6}{8x} \right\}$$

### 3.309 ODE No. 1309

$$x^3 \frac{d^2}{dx^2} y(x) - (x^2 - 1) \frac{d}{dx} y(x) + xy(x) = 0$$

**Mathematica:** cpu = 0.081010 (sec), leaf count = 84

$$\left\{ \left\{ y(x) \rightarrow c_2 G_{1,2}^{2,0} \left( -\frac{1}{2x^2} \middle| \begin{matrix} 1 \\ -\frac{1}{2}, -\frac{1}{2} \end{matrix} \right) + \sqrt{2} c_1 e^{\frac{1}{4x^2}} x \left( \left( 1 - \frac{1}{2x^2} \right) I_0 \left( \frac{1}{4x^2} \right) + \frac{I_1 \left( \frac{1}{4x^2} \right)}{2x^2} \right) \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 73

$$\left\{ y(x) = \frac{-C1}{x} e^{\frac{1}{4x^2}} \left( (2x^2 - 1) I_0 \left( \frac{1}{4x^2} \right) + I_1 \left( \frac{1}{4x^2} \right) \right) + \frac{-C2}{x} e^{\frac{1}{4x^2}} \left( (2x^2 - 1) K_0 \left( -\frac{1}{4x^2} \right) + K_1 \left( -\frac{1}{4x^2} \right) \right) \right\}$$

### 3.310 ODE No. 1310

$$x^3 \frac{d^2}{dx^2} y(x) + 3x^2 \frac{d}{dx} y(x) + xy(x) - 1 = 0$$

**Mathematica:** cpu = 0.010001 (sec), leaf count = 31

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{x} + \frac{c_2 \log(x)}{x} + \frac{\log^2(x)}{2x} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 20

$$\left\{ y(x) = \frac{1}{x} \left( \frac{(\ln(x))^2}{2} + \_C1 \ln(x) + \_C2 \right) \right\}$$

### 3.311 ODE No. 1311

$$x(x^2 + 1) \frac{d^2}{dx^2} y(x) + (2x^2 + 1) \frac{d}{dx} y(x) - v(v + 1) xy(x) = 0$$

**Mathematica:** cpu = 0.134517 (sec), leaf count = 63

$$\left\{ \left\{ y(x) \rightarrow c_2 G_{2,2}^{2,0} \left( -x^2 \mid \begin{matrix} \frac{1-v}{2}, \frac{v+2}{2} \\ 0, 0 \end{matrix} \right) + c_1 {}_2F_1 \left( \frac{v}{2} + \frac{1}{2}, -\frac{v}{2}; 1; -x^2 \right) \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 52

$$\left\{ y(x) = \_C1 {}_2F_1 \left( -\frac{v}{2}, \frac{1}{2} + \frac{v}{2}; \frac{1}{2}; x^2 + 1 \right) + \_C2 \sqrt{x^2 + 1} {}_2F_1 \left( 1 + \frac{v}{2}, \frac{1}{2} - \frac{v}{2}; \frac{3}{2}; x^2 + 1 \right) \right\}$$

### 3.312 ODE No. 1312

$$x(x^2 + 1) \frac{d^2}{dx^2} y(x) + 2(x^2 - 1) \frac{d}{dx} y(x) - 2xy(x) = 0$$

**Mathematica:** cpu = 0.026003 (sec), leaf count = 32

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{x^2 + 1} + \frac{c_2 x^3}{3(x^2 + 1)} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 26

$$\left\{ y(x) = \frac{\_C1}{x^2 + 1} + \frac{\_C2 x^3}{x^2 + 1} \right\}$$



### 3.313 ODE No. 1313

$$x(x^2 + 1) \frac{d^2}{dx^2} y(x) + (2(n+1)x^2 + 2n+1) \frac{d}{dx} y(x) - (v-n)(v+n+1)xy(x) = 0$$

**Mathematica:** cpu = 0.211527 (sec), leaf count = 87

$$\left\{ \left\{ y(x) \rightarrow c_1 {}_2F_1\left(\frac{n}{2} - \frac{v}{2}, \frac{n}{2} + \frac{v}{2} + \frac{1}{2}; n+1; -x^2\right) + c_2 x^{-2n} {}_2F_1\left(-\frac{n}{2} - \frac{v}{2}, -\frac{n}{2} + \frac{v}{2} + \frac{1}{2}; 1-n; -x^2\right) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 39

$$\left\{ y(x) = \_C1 x^{-n} \text{LegendreP}\left(v, n, \sqrt{x^2 + 1}\right) + \_C2 x^{-n} \text{LegendreQ}\left(v, n, \sqrt{x^2 + 1}\right) \right\}$$

### 3.314 ODE No. 1314

$$x(x^2 + 1) \frac{d^2}{dx^2} y(x) - (2(n-1)x^2 + 2n-1) \frac{d}{dx} y(x) + (v+n)(-v+n-1)xy(x) = 0$$

**Mathematica:** cpu = 0.185024 (sec), leaf count = 87

$$\left\{ \left\{ y(x) \rightarrow c_1 {}_2F_1\left(-\frac{n}{2} - \frac{v}{2}, -\frac{n}{2} + \frac{v}{2} + \frac{1}{2}; 1-n; -x^2\right) + c_2 x^{2n} {}_2F_1\left(\frac{n}{2} - \frac{v}{2}, \frac{n}{2} + \frac{v}{2} + \frac{1}{2}; n+1; -x^2\right) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 x^n \text{LegendreP}\left(v, n, \sqrt{x^2 + 1}\right) + \_C2 x^n \text{LegendreQ}\left(v, n, \sqrt{x^2 + 1}\right) \right\}$$

### 3.315 ODE No. 1315

$$x(x^2 - 1) \frac{d^2}{dx^2} y(x) + \frac{d}{dx} y(x) + y(x) ax^3 = 0$$

**Mathematica:** cpu = 0.027503 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow c_2 \sin\left(\sqrt{a}\sqrt{x^2 - 1}\right) + c_1 \cos\left(\sqrt{a}\sqrt{x^2 - 1}\right) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 45

$$\left\{ y(x) = \_C1 \sin\left((1+x)(x-1)\sqrt{a}\frac{1}{\sqrt{x^2 - 1}}\right) + \_C2 \cos\left((1+x)(x-1)\sqrt{a}\frac{1}{\sqrt{x^2 - 1}}\right) \right\}$$

### 3.316 ODE No. 1316

$$x(x^2 - 1) \frac{d^2}{dx^2} y(x) + (x^2 - 1) \frac{d}{dx} y(x) - xy(x) = 0$$

**Mathematica:** cpu = 0.091512 (sec), leaf count = 38

$$\left\{ \left\{ y(x) \rightarrow c_2 G_{2,2}^{2,0} \left( x^2 \middle| \begin{matrix} \frac{1}{2}, \frac{3}{2} \\ 0, 0 \end{matrix} \right) + \frac{2c_1 E(x^2)}{\pi} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 18

$$\{y(x) = \_C1 \text{EllipticE}(x) + \_C2 (\text{EllipticCE}(x) - \text{EllipticCK}(x))\}$$

### 3.317 ODE No. 1317

$$x(x^2 - 1) \frac{d^2}{dx^2} y(x) + (3x^2 - 1) \frac{d}{dx} y(x) + xy(x) = 0$$

**Mathematica:** cpu = 0.115015 (sec), leaf count = 38

$$\left\{ \left\{ y(x) \rightarrow c_2 G_{2,2}^{2,0} \left( x^2 \middle| \begin{matrix} \frac{1}{2}, \frac{1}{2} \\ 0, 0 \end{matrix} \right) + \frac{2c_1 K(x^2)}{\pi} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 13

$$\{y(x) = \_C1 \text{EllipticK}(x) + \_C2 \text{EllipticCK}(x)\}$$

### 3.318 ODE No. 1318

$$x(x^2 - 1) \frac{d^2}{dx^2} y(x) + (ax^2 + b) \frac{d}{dx} y(x) + cxy(x) = 0$$

**Mathematica:** cpu = 0.293537 (sec), leaf count = 172

$$\left\{ \left\{ y(x) \rightarrow c_1 {}_2F_1 \left( \frac{a}{4} - \frac{1}{4} \sqrt{a^2 - 2a - 4c + 1} - \frac{1}{4}, \frac{a}{4} + \frac{1}{4} \sqrt{a^2 - 2a - 4c + 1} - \frac{1}{4}; \frac{1}{2} - \frac{b}{2}; x^2 \right) + i^{b+1} c_2 x^{b+1} \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 122

$$\left\{ y(x) = \_C1 {}_2F_1 \left( -\frac{1}{4} + \frac{a}{4} - \frac{1}{4} \sqrt{a^2 - 2a - 4c + 1}, -\frac{1}{4} + \frac{a}{4} + \frac{1}{4} \sqrt{a^2 - 2a - 4c + 1}; \frac{1}{2} - \frac{b}{2}; x^2 \right) + \_C2 x^{b+1} \right\}$$

**3.319 ODE No. 1319**

$$x(x^2 + 2) \frac{d^2}{dx^2}y(x) - \frac{d}{dx}y(x) - 6xy(x) = 0$$

**Mathematica:** cpu = 0.099513 (sec), leaf count = 118

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 \left( -2\sqrt[4]{2}x^2 {}_2F_1\left(\frac{1}{4}, \frac{3}{4}; \frac{5}{4}; -\frac{x^2}{2}\right) - \sqrt[4]{2}x^4 {}_2F_1\left(\frac{1}{4}, \frac{3}{4}; \frac{5}{4}; -\frac{x^2}{2}\right) - \sqrt{x^2 + 2}x^2 - \sqrt[4]{x^2 + 2} \right)}{3\sqrt[4]{x^2 + 2}} + c_1(x^2 + 2) \right\} \right.$$

**Maple:** cpu = 0.078 (sec), leaf count = 37

$$\left\{ y(x) = \_C1 x^{\frac{3}{2}}(x^2 + 2)^{\frac{3}{4}} + \_C2 (x^2 + 2)^{\frac{3}{4}} {}_2F_1\left(-\frac{3}{4}, \frac{7}{4}; \frac{1}{4}; -\frac{x^2}{2}\right) \right\}$$

**3.320 ODE No. 1320**

$$x(x^2 - 2) \frac{d^2}{dx^2}y(x) - (x^3 + 3x^2 - 2x - 2) \frac{d}{dx}y(x) + (x^2 + 4x + 2)y(x) = 0$$

**Mathematica:** cpu = 0.070009 (sec), leaf count = 21

$$\left\{ \left\{ y(x) \rightarrow c_1 e^x x^2 + c_2(x - 1) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 17

$$\left\{ y(x) = \_C1 (x - 1) + \_C2 e^x x^2 \right\}$$

**3.321 ODE No. 1321**

$$x^2(1 + x) \frac{d^2}{dx^2}y(x) - x(2x + 1) \frac{d}{dx}y(x) + (2x + 1)y(x) = 0$$

**Mathematica:** cpu = 0.026003 (sec), leaf count = 18

$$\left\{ \left\{ y(x) \rightarrow c_1 x + c_2 x(x + \log(x)) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 15

$$\left\{ y(x) = x\_C1 + \_C2 x(x + \ln(x)) \right\}$$

### 3.322 ODE No. 1322

$$x^2(1+x) \frac{d^2}{dx^2}y(x) + 2x(3x+2) \frac{d}{dx}y(x) = 0$$

**Mathematica:** cpu = 0.028504 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow c_1 \left( -\frac{1}{3x^3} + \frac{1}{x^2} - \frac{3}{x} - \frac{1}{x+1} - 4\log(x) + 4\log(x+1) \right) + c_2 \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 44

$$\left\{ y(x) = \_C1 + \left( -4 \ln(x) + 4 \ln(1+x) - \frac{12x^3 + 6x^2 - 2x + 1}{(3+3x)x^3} \right) - C2 \right\}$$

### 3.323 ODE No. 1323

$$\frac{d^2}{dx^2}y(x) = -2 \frac{(x-2) \frac{d}{dx}y(x)}{x(x-1)} + 2 \frac{(1+x)y(x)}{x^2(x-1)} = 0$$

**Mathematica:** cpu = 0.744094 (sec), leaf count = 54

$$\{ \{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{(-2x-2)y(x) + (2x-4)y'(x) + (x-1)xy''(x) = 0, y(2) = c_1, y'(2) = c_2\}) \}$$

**Maple:** cpu = 0.016 (sec), leaf count = 20

$$\left\{ y(x) = \frac{\_C1}{x^2} + \frac{\_C2(x-1)^3}{x^2} \right\}$$

### 3.324 ODE No. 1324

$$\frac{d^2}{dx^2}y(x) = \frac{(5x-4) \frac{d}{dx}y(x)}{x(x-1)} - \frac{(9x-6)y(x)}{x^2(x-1)} = 0$$

**Mathematica:** cpu = 0.029004 (sec), leaf count = 25

$$\{ \{ y(x) \rightarrow c_1x^3 - c_2x^2(x \log(x) + 1) \} \}$$

**Maple:** cpu = 0.047 (sec), leaf count = 21

$$\{ y(x) = \_C1 x^3 + \_C2 x^2(x \ln(x) + 1) \}$$

### 3.325 ODE No. 1325

$$\frac{d^2}{dx^2}y(x) = -\frac{((a+b+1)x + \alpha + \beta - 1)\frac{d}{dx}y(x)}{x(x-1)} - \frac{(abx - \alpha\beta)y(x)}{x^2(x-1)} = 0$$

**Mathematica:** cpu = 0.264534 (sec), leaf count = 52

$$\left\{ \left\{ y(x) \rightarrow (-1)^\alpha c_1 x^\alpha {}_2F_1(a + \alpha, \alpha + b; \alpha - \beta + 1; x) + (-1)^\beta c_2 x^\beta {}_2F_1(a + \beta, b + \beta; -\alpha + \beta + 1; x) \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 103

$$\left\{ y(x) = \_C1 x^\alpha (x-1)^{1-a-\alpha-b-\beta} {}_2F_1(1-b-\beta, 1-a-\beta; 1+\alpha-\beta; x) + \_C2 x^\beta (x-1)^{1-a-\alpha-b-\beta} {}_2F_1(1-b-\beta, 1-a-\beta; 1+\alpha-\beta; x) \right\}$$

### 3.326 ODE No. 1326

$$\frac{d^2}{dx^2}y(x) = -\frac{\frac{d}{dx}y(x)}{1+x} - \frac{y(x)}{x(1+x)^2} = 0$$

**Mathematica:** cpu = 0.028504 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 x}{x+1} + \frac{c_2 (x \log(x) - 1)}{x+1} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 26

$$\left\{ y(x) = \frac{x\_C1}{1+x} + \frac{\_C2 (x \ln(x) - 1)}{1+x} \right\}$$

### 3.327 ODE No. 1327

$$\frac{d^2}{dx^2}y(x) = 2\frac{\frac{d}{dx}y(x)}{x(x-2)} - \frac{y(x)}{x^2(x-2)} = 0$$

**Mathematica:** cpu = 0.167521 (sec), leaf count = 104

$$\left\{ \left\{ y(x) \rightarrow \left(-\frac{1}{2}\right)^{-\frac{1}{\sqrt{2}}} c_1 x^{-\frac{1}{\sqrt{2}}} {}_2F_1\left(-\frac{1}{\sqrt{2}}, -1 - \frac{1}{\sqrt{2}}; 1 - \sqrt{2}; \frac{x}{2}\right) + \left(-\frac{1}{2}\right)^{\frac{1}{\sqrt{2}}} c_2 x^{\frac{1}{\sqrt{2}}} {}_2F_1\left(\frac{1}{\sqrt{2}}, -1 + \frac{1}{\sqrt{2}}; 1 + \sqrt{2}; \frac{x}{2}\right) \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 85

$$\left\{ y(x) = \_C1 {}_2F_1\left(2 - \frac{\sqrt{2}}{2}, 1 - \frac{\sqrt{2}}{2}; 1 - \sqrt{2}; \frac{x}{2}\right) x^{-\frac{\sqrt{2}}{2}} (x-2)^2 + \_C2 {}_2F_1\left(2 + \frac{\sqrt{2}}{2}, 1 + \frac{\sqrt{2}}{2}; 1 + \sqrt{2}; \frac{x}{2}\right) x^{\frac{\sqrt{2}}{2}} (x-2)^2 \right\}$$

### 3.328 ODE No. 1328

$$\frac{d^2}{dx^2}y(x) = 2 \frac{y(x)}{x(x-1)^2} = 0$$

**Mathematica:** cpu = 0.022003 (sec), leaf count = 36

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2(-x^2 + 2x \log(x) + 1)}{x-1} - \frac{c_1x}{x-1} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 32

$$\left\{ y(x) = \frac{x-C1}{x-1} + \frac{-C2(2x \ln(x) - x^2 + 1)}{x-1} \right\}$$

### 3.329 ODE No. 1329

$$\frac{d^2}{dx^2}y(x) = -\frac{((\alpha + \beta + 1)x^2 - (\alpha + \beta + 1 + a(\gamma + 1) - \delta)x + a\gamma)y(x)}{x(x-1)(x-a)} - \frac{(\alpha\beta x - q)y(x)}{x(x-1)(x-a)} = 0$$

**Mathematica:** cpu = 6.409814 (sec), leaf count = 99

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{(x\alpha\beta - q)y(x) + (\alpha x^2 + \beta x^2 + x^2 - \alpha x - \beta x - a\delta x + \delta x - a\gamma)\}) \right\} \right\}$$

**Maple:** cpu = 0.234 (sec), leaf count = 64

$$\left\{ y(x) = \_C1 \text{HeunG}(a, q, \alpha, \beta, \gamma + 1, \delta, x) + \_C2 x^{1-\gamma} \text{HeunG}(a, q - (-1 + \gamma)(\delta(a-1) + \alpha + \beta - \gamma + 1), \alpha, \beta, \gamma, \delta, x) \right\}$$

### 3.330 ODE No. 1330

$$\frac{d^2}{dx^2}y(x) = -\frac{(Ax^2 + Bx + C) \frac{d}{dx}y(x)}{(x-a)(x-b)(x-c)} - \frac{(DDx + E)y(x)}{(x-a)(x-b)(x-c)} = 0$$

**Mathematica:** cpu = 135.163163 (sec), leaf count = 71

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{(xDD + e)y(x) + (Ax^2 + Bx + C)y'(x) - (a-x)(b-x)(c-x)y''(x)\}) \right\} \right\}$$

**Maple:** cpu = 0.780 (sec), leaf count = 1147

$$\left\{ y(x) = \_C1 \text{HeunG}\left(\frac{a-c}{a-b}, \frac{DDa + E}{a-b}, \frac{A}{2} - \frac{1}{2} + \frac{1}{2}\sqrt{A^2 - 2A - 4DD + 1}, 1, \left((A(b-c)a - Abc - Bc - \dots)\right)\right) \right\}$$

**3.331 ODE No. 1331**

$$\frac{d^2}{dx^2}y(x) = 1/2 \frac{(x-4) \frac{d}{dx}y(x)}{x(x-2)} - 1/2 \frac{(x-3)y(x)}{x^2(x-2)} = 0$$

**Mathematica:** cpu = 0.043006 (sec), leaf count = 55

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 \sqrt[4]{x-2} \sqrt{x}}{\sqrt[4]{2-x}} + \frac{2c_2 (x-2)^{3/4} \sqrt{x}}{\sqrt[4]{2-x}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 19

$$\left\{ y(x) = \_C1 \sqrt{x} + \_C2 \sqrt{x(x-2)} \right\}$$

**3.332 ODE No. 1332**

$$\frac{d^2}{dx^2}y(x) = \frac{\frac{d}{dx}y(x)}{1+x} - 1/4 \frac{(3x+1)y(x)}{x^2(1+x)} = 0$$

**Mathematica:** cpu = 0.023503 (sec), leaf count = 26

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt{x} + c_2 \sqrt{x}(x + \log(x)) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 19

$$\left\{ y(x) = \_C1 \sqrt{x} + \_C2 \sqrt{x}(x + \ln(x)) \right\}$$

**3.333 ODE No. 1333**

$$\frac{d^2}{dx^2}y(x) = -1/2 \frac{(3x-1) \frac{d}{dx}y(x)}{x(x-1)} + 1/4 \frac{v(v+1)y(x)}{x^2} = 0$$

**Mathematica:** cpu = 0.109014 (sec), leaf count = 70

$$\left\{ \left\{ y(x) \rightarrow c_1 i^{-v} x^{-v/2} {}_2F_1\left(\frac{1}{2}, -v; \frac{1}{2} - v; x\right) + c_2 i^{v+1} x^{\frac{v+1}{2}} {}_2F_1\left(\frac{1}{2}, v+1; v + \frac{3}{2}; x\right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 45

$$\left\{ y(x) = \_C1 x^{-\frac{v}{2}} {}_2F_1\left(\frac{1}{2}, -v; \frac{1}{2} - v; x\right) + \_C2 x^{\frac{1}{2} + \frac{v}{2}} {}_2F_1\left(\frac{1}{2}, v+1; \frac{3}{2} + v; x\right) \right\}$$

### 3.334 ODE No. 1334

$$\frac{d^2}{dx^2}y(x) = -\frac{((a+1)x-1)\frac{d}{dx}y(x)}{x(x-1)} - 1/4 \frac{((a^2-b^2)x+c^2)y(x)}{x^2(x-1)} = 0$$

**Mathematica:** cpu = 0.198525 (sec), leaf count = 114

$$\left\{ \left\{ y(x) \rightarrow i^{-c} c_1 x^{-c/2} {}_2F_1\left(\frac{a}{2} - \frac{b}{2} - \frac{c}{2}, \frac{a}{2} + \frac{b}{2} - \frac{c}{2}; 1 - c; x\right) + i^c c_2 x^{c/2} {}_2F_1\left(\frac{a}{2} - \frac{b}{2} + \frac{c}{2}, \frac{a}{2} + \frac{b}{2} + \frac{c}{2}; c + 1; x\right) \right. \right.$$

**Maple:** cpu = 0.062 (sec), leaf count = 97

$$\left\{ y(x) = \_C1 (x-1)^{1-a} x^{\frac{c}{2}} {}_2F_1\left(-\frac{a}{2} - \frac{b}{2} + \frac{c}{2} + 1, -\frac{a}{2} + \frac{b}{2} + \frac{c}{2} + 1; c + 1; x\right) + \_C2 (x-1)^{1-a} x^{-\frac{c}{2}} {}_2F_1\left(-\frac{a}{2} - \frac{b}{2} + \frac{c}{2} + 1, -\frac{a}{2} + \frac{b}{2} + \frac{c}{2} + 1; c + 1; x\right) \right.$$

### 3.335 ODE No. 1335

$$\frac{d^2}{dx^2}y(x) = -1/2 \frac{(3x-1)\frac{d}{dx}y(x)}{x(x-1)} - 1/4 \frac{(ax+b)y(x)}{x(x-1)^2} = 0$$

**Mathematica:** cpu = 0.305039 (sec), leaf count = 893

$$\left\{ \left\{ y(x) \rightarrow e^{\frac{1}{4}(-2\log(1-x)-\log(x))} \sqrt{x} c_1 {}_2F_1\left(\frac{1}{4}\left(\sqrt{-8a-4b-4\sqrt{4a^2+4ba-a-b}+1}+1\right), \frac{(-8a-4b-\sqrt{-8a-4b-4\sqrt{4a^2+4ba-a-b}+1})}{4}\right) \right. \right.$$

**Maple:** cpu = 0.031 (sec), leaf count = 57

$$\left\{ y(x) = \_C1 LegendreP\left(\frac{1}{2}\sqrt{1-4a} - \frac{1}{2}, \sqrt{-a-b}, \sqrt{x}\right) + \_C2 LegendreQ\left(\frac{1}{2}\sqrt{1-4a} - \frac{1}{2}, \sqrt{-a-b}, \sqrt{x}\right) \right.$$

### 3.336 ODE No. 1336

$$\frac{d^2}{dx^2}y(x) = -\frac{(-3x+1)y(x)}{(x-1)(2x-1)^2} = 0$$

**Mathematica:** cpu = 0.051007 (sec), leaf count = 70

$$\left\{ \left\{ y(x) \rightarrow c_2 \sqrt{1-2x}(2x \log(2(x-1)+1) - 2 \log(2(x-1)+1) - 2x \log(x-1) + 2 \log(x-1) - 1) - c_1 \right. \right.$$

**Maple:** cpu = 0.031 (sec), leaf count = 50

$$\left\{ y(x) = \_C1 \sqrt{2x-1}(x-1) + \_C2 ((2x-2) \ln(2x-1) - 1 + (-2x+2) \ln(x-1)) \sqrt{2x-1} \right\}$$



### 3.337 ODE No. 1337

$$\frac{d^2}{dx^2}y(x) = -1/2 \frac{(3x + a + 2b) \frac{d}{dx}y(x)}{(x + a)(x + b)} - 1/4 \frac{(a - b)y(x)}{(x + a)^2(x + b)} = 0$$

**Mathematica:** cpu = 0.081010 (sec), leaf count = 62

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{\sqrt{\frac{b+x}{a-b} + 1}} + \frac{c_2 \sqrt{b+x}}{\sqrt{a-b} \sqrt{\frac{b+x}{a-b} + 1}} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 44

$$\left\{ y(x) = \_C1 \sqrt{x+b} \frac{1}{\sqrt{1 + \frac{x+b}{a-b}}} + \_C2 \frac{1}{\sqrt{1 + \frac{x+b}{a-b}}} \right\}$$

### 3.338 ODE No. 1338

$$\frac{d^2}{dx^2}y(x) = 1/3 \frac{(6x - 1) \frac{d}{dx}y(x)}{x(x - 2)} + 1/3 \frac{y(x)}{x^2(x - 2)} = 0$$

**Mathematica:** cpu = 0.067008 (sec), leaf count = 40

$$\left\{ \left\{ y(x) \rightarrow \frac{3}{935} c_2 x (18x^2 - 102x + 187) + c_1 \sqrt[6]{x} (2 - x)^{17/6} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 31

$$\left\{ y(x) = \_C1 (18x^3 - 102x^2 + 187x) + \_C2 \sqrt[6]{x} (x - 2)^{\frac{17}{6}} \right\}$$

### 3.339 ODE No. 1339

$$\frac{d^2}{dx^2}y(x) = -\frac{(a(b+2)x^2 + (c-d+1)x) \frac{d}{dx}y(x)}{(ax+1)x^2} - \frac{(abx - cd)y(x)}{(ax+1)x^2} = 0$$

**Mathematica:** cpu = 0.263533 (sec), leaf count = 66

$$\left\{ \left\{ y(x) \rightarrow c_1 a^{-c} x^{-c} {}_2F_1(1 - c, b - c; -c - d + 1; -ax) + c_2 a^d x^d {}_2F_1(d + 1, b + d; c + d + 1; -ax) \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 89

$$\left\{ y(x) = \_C1 x^d (ax + 1)^{-b+c-d} {}_2F_1(c, 1 - b + c; 1 + d + c; -ax) + \_C2 x^{-c} (ax + 1)^{-b+c-d} {}_2F_1(-d, 1 - b + c; c + d + 1; -ax) \right\}$$

**3.340 ODE No. 1340**

$$\frac{d^2}{dx^2}y(x) = 2 \frac{(ax + 2b) \frac{d}{dx}y(x)}{x(ax + b)} - \frac{(2ax + 6b)y(x)}{(ax + b)x^2} = 0$$

**Mathematica:** cpu = 0.035005 (sec), leaf count = 32

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 x^3}{ax + b} + \frac{c_1 x^2}{ax + b} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 29

$$\left\{ y(x) = \frac{C1 x^2}{ax + b} + \frac{C2 x^3}{ax + b} \right\}$$

**3.341 ODE No. 1341**

$$\frac{d^2}{dx^2}y(x) = -\frac{(2ax + b) \frac{d}{dx}y(x)}{x(ax + b)} - \frac{(avx - b)y(x)}{(ax + b)x^2} + Ax = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.125 (sec), leaf count = 195

$$\left\{ y(x) = {}_2F_1\left(\frac{3}{2} - \frac{1}{2}\sqrt{1-4v}, -\frac{1}{2} - \frac{1}{2}\sqrt{1-4v}; 1 - \sqrt{1-4v}; -\frac{b}{ax}\right)x^{-\frac{1}{2} + \frac{1}{2}\sqrt{1-4v}} - C2 + {}_2F_1\left(\frac{3}{2} + \frac{1}{2}\sqrt{1-4v}, -\frac{1}{2} - \frac{1}{2}\sqrt{1-4v}; 1 - \sqrt{1-4v}; -\frac{b}{ax}\right)x^{-\frac{1}{2} - \frac{1}{2}\sqrt{1-4v}} - C2 \right\}$$

**3.342 ODE No. 1342**

$$\frac{d^2}{dx^2}y(x) = -\frac{ay(x)}{x^4} = 0$$

**Mathematica:** cpu = 0.041505 (sec), leaf count = 51

$$\left\{ \left\{ y(x) \rightarrow c_1 x e^{\frac{\sqrt{-a}}{x}} + \frac{c_2 x e^{-\frac{\sqrt{-a}}{x}}}{2\sqrt{-a}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 31

$$\left\{ y(x) = -C1 x \sinh\left(\frac{1}{x}\sqrt{-a}\right) + -C2 x \cosh\left(\frac{1}{x}\sqrt{-a}\right) \right\}$$

### 3.343 ODE No. 1343

$$\frac{d^2}{dx^2}y(x) = -\frac{(x^2a(1-a) - b(x+b))y(x)}{x^4} = 0$$

**Mathematica:** cpu = 0.665585 (sec), leaf count = 61

{ {y(x) → DifferentialRoot({y, x}, {y''(x)x^4 + (-a^2x^2 + ax^2 - bx - b^2)y(x) = 0, y(1) = c1, y'(1) = c2}) }

**Maple:** cpu = 0.094 (sec), leaf count = 62

$$\left\{ y(x) = \_C1 \left( (2ax + b) I_a \left( \frac{b}{x} \right) + I_{a+1} \left( \frac{b}{x} \right) b \right) + \_C2 \left( (2ax + b) K_a \left( \frac{b}{x} \right) - K_{a+1} \left( \frac{b}{x} \right) b \right) \right\}$$

### 3.344 ODE No. 1344

$$\frac{d^2}{dx^2}y(x) = -\frac{y(x)}{x^4} (e^{2x^{-1}} - v^2) = 0$$

**Mathematica:** cpu = 0.559571 (sec), leaf count = 173

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 2^{v+\frac{v+1}{2}} (e^{2/x})^{\frac{v+1}{2}-\frac{1}{2}} (-e^{2/x})^{\frac{1}{2}(-v-1)+\frac{1}{2}} I_v(\sqrt{-e^{2/x}})}{\log(e^{2/x})} + \frac{c_2 (-1)^{-v} 2^{v+\frac{v+1}{2}} (e^{2/x})^{\frac{v+1}{2}-\frac{1}{2}} (-e^{2/x})^{\frac{1}{2}(-v-1)+\frac{1}{2}} K_v(\sqrt{-e^{2/x}})}{\log(e^{2/x})} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 23

$$\left\{ y(x) = \_C1 x J_v(e^{x^{-1}}) + \_C2 x Y_v(e^{x^{-1}}) \right\}$$

### 3.345 ODE No. 1345

$$\frac{d^2}{dx^2}y(x) = -\frac{d}{dx}y(x) + 2\frac{y(x)}{x^4} = 0$$

**Mathematica:** cpu = 0.028504 (sec), leaf count = 52

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{1}{2x^2}} x - \sqrt{\frac{\pi}{2}} c_2 e^{\frac{1}{2x^2}} x \operatorname{erf}\left(\frac{1}{\sqrt{2x}}\right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 32

$$\left\{ y(x) = \_C1 x e^{\frac{1}{2x^2}} + \_C2 x e^{\frac{1}{2x^2}} \operatorname{Erf}\left(\frac{\sqrt{2}}{2x}\right) \right\}$$

**3.346 ODE No. 1346**

$$\frac{d^2}{dx^2}y(x) = \frac{(a+b)\frac{d}{dx}y(x)}{x^2} - \frac{((a+b)x+ab)y(x)}{x^4} = 0$$

**Mathematica:** cpu = 0.326541 (sec), leaf count = 87

$$\left\{ \left\{ y(x) \rightarrow c_1 x e^{-\frac{\sqrt{(a-b)^2+a+b}}{2x}} + \frac{c_2 x e^{-\frac{\sqrt{(a-b)^2-\frac{a}{2x}-\frac{b}{2x}}}{2x}}}{\sqrt{(a-b)^2}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 25

$$\{y(x) = \_C1 x e^{-\frac{a}{x}} + \_C2 x e^{-\frac{b}{x}}\}$$

**3.347 ODE No. 1347**

$$\frac{d^2}{dx^2}y(x) = -\frac{\frac{d}{dx}y(x)}{x} - \frac{y(x)}{x^4} = 0$$

**Mathematica:** cpu = 0.076510 (sec), leaf count = 31

$$\left\{ \left\{ y(x) \rightarrow c_2 J_0\left(\frac{1}{x}\right) + \frac{c_1 K_0\left(\frac{i}{x}\right)}{\sqrt{\pi}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 19

$$\{y(x) = \_C1 J_0(x^{-1}) + \_C2 Y_0(x^{-1})\}$$

**3.348 ODE No. 1348**

$$\frac{d^2}{dx^2}y(x) = -\frac{\frac{d}{dx}y(x)}{x} - \frac{(bx^2+a(x^4+1))y(x)}{x^4} = 0$$

**Mathematica:** cpu = 1.313167 (sec), leaf count = 58

$$\{\{y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{y''(x)x^4 + y'(x)x^3 + (ax^4 + bx^2 + a)y(x) = 0, y(1) = c_1, y'(1) = c_2\})\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 101

$$\left\{ y(x) = \_C1 \text{HeunD}\left(0, 2a+b, 0, 2a-b, \frac{x^2+1}{x^2-1}\right) + \_C2 \text{HeunD}\left(0, 2a+b, 0, 2a-b, \frac{x^2+1}{x^2-1}\right) \int \frac{1}{x} \left( \dots \right) \right\}$$

**3.349 ODE No. 1349**

$$\frac{d^2}{dx^2}y(x) = -\frac{(x^2 + 1) \frac{d}{dx}y(x)}{x^3} - \frac{y(x)}{x^4} = 0$$

**Mathematica:** cpu = 0.087011 (sec), leaf count = 76

$$\left\{ \left\{ y(x) \rightarrow c_2 G_{1,2}^{2,0} \left( -\frac{1}{2x^2} \middle| \begin{matrix} \frac{3}{2} \\ 0, 0 \end{matrix} \right) + c_1 e^{\frac{1}{4x^2}} \left( \left( 1 - \frac{1}{2x^2} \right) I_0 \left( \frac{1}{4x^2} \right) + \frac{I_1 \left( \frac{1}{4x^2} \right)}{2x^2} \right) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 73

$$\left\{ y(x) = \frac{-C1}{x^2} e^{\frac{1}{4x^2}} \left( (2x^2 - 1) I_0 \left( \frac{1}{4x^2} \right) + I_1 \left( \frac{1}{4x^2} \right) \right) + \frac{C2}{x^2} e^{\frac{1}{4x^2}} \left( (2x^2 - 1) K_0 \left( -\frac{1}{4x^2} \right) + K_1 \left( -\frac{1}{4x^2} \right) \right) \right\}$$

**3.350 ODE No. 1350**

$$\frac{d^2}{dx^2}y(x) = -2 \frac{\frac{d}{dx}y(x)}{x} - \frac{a^2 y(x)}{x^4} = 0$$

**Mathematica:** cpu = 0.009501 (sec), leaf count = 25

$$\left\{ \left\{ y(x) \rightarrow c_1 \cos \left( \frac{a}{x} \right) - c_2 \sin \left( \frac{a}{x} \right) \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 21

$$\left\{ y(x) = \_C1 \sin \left( \frac{a}{x} \right) + \_C2 \cos \left( \frac{a}{x} \right) \right\}$$

**3.351 ODE No. 1351**

$$\frac{d^2}{dx^2}y(x) = -\frac{(2x^2 + 1) \frac{d}{dx}y(x)}{x^3} + \frac{y(x)}{x^4} = 0$$

**Mathematica:** cpu = 0.024003 (sec), leaf count = 50

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{1}{2x^2}} - \sqrt{\frac{\pi}{2}} c_2 e^{\frac{1}{2x^2}} \operatorname{erf} \left( \frac{1}{\sqrt{2}x} \right) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 30

$$\left\{ y(x) = \_C1 e^{\frac{1}{2x^2}} + \_C2 e^{\frac{1}{2x^2}} \operatorname{Erf} \left( \frac{\sqrt{2}}{2x} \right) \right\}$$

### 3.352 ODE No. 1352

$$\frac{d^2}{dx^2}y(x) = -2 \frac{(x+a) \frac{d}{dx}y(x)}{x^2} - \frac{by(x)}{x^4} = 0$$

**Mathematica:** cpu = 0.013002 (sec), leaf count = 89

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-\frac{\sqrt{b} \left( -\frac{\sqrt{a^2-b}}{\sqrt{b}} - \frac{a}{\sqrt{b}} \right)}{x}} + c_2 e^{-\frac{\sqrt{b} \left( \frac{\sqrt{a^2-b}}{\sqrt{b}} - \frac{a}{\sqrt{b}} \right)}{x}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 43

$$\left\{ y(x) = \_C1 e^{\frac{1}{x}(a-\sqrt{a^2-b})} + \_C2 e^{\frac{1}{x}(\sqrt{a^2-b}+a)} \right\}$$

### 3.353 ODE No. 1353

$$\frac{d^2}{dx^2}y(x) = \frac{(2x^2-1) \frac{d}{dx}y(x)}{x^3} - \frac{y(x)}{x^4} = 0$$

**Mathematica:** cpu = 0.107514 (sec), leaf count = 119

$$\left\{ \left\{ y(x) \rightarrow c_1 \left( x^3 + 2x - \frac{1}{x} \right) - \frac{c_2 \left( \sqrt{2\pi} x^4 \operatorname{erfi} \left( \frac{1}{\sqrt{2x}} \right) + 2\sqrt{2\pi} x^2 \operatorname{erfi} \left( \frac{1}{\sqrt{2x}} \right) - \sqrt{2\pi} \operatorname{erfi} \left( \frac{1}{\sqrt{2x}} \right) + 2e^{\frac{1}{2x^2}} x - 2 \right)}{16x} \right\} \right\}$$

**Maple:** cpu = 0.141 (sec), leaf count = 68

$$\left\{ y(x) = \frac{\_C1}{x} \left( \sqrt{2}\sqrt{\pi}(x^4 + 2x^2 - 1) \operatorname{erfi} \left( \frac{\sqrt{2}}{2x} \right) + (-2x^3 + 2x) e^{\frac{1}{2x^2}} \right) + \frac{\_C2(x^4 + 2x^2 - 1)}{x} \right\}$$

### 3.354 ODE No. 1354

$$\frac{d^2}{dx^2}y(x) = \frac{(2x^2-1) \frac{d}{dx}y(x)}{x^3} - 2 \frac{y(x)}{x^4} = 0$$

**Mathematica:** cpu = 0.071009 (sec), leaf count = 108

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 \left( -5\sqrt{2\pi} x^2 \operatorname{erfi} \left( \frac{1}{\sqrt{2x}} \right) + \sqrt{2\pi} \operatorname{erfi} \left( \frac{1}{\sqrt{2x}} \right) - 2e^{\frac{1}{2x^2}} x + 4e^{\frac{1}{2x^2}} x^5 + 8e^{\frac{1}{2x^2}} x^3 \right)}{12x^2} + c_1 \left( 1 - \frac{1}{5x^2} \right) \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 32

$$\left\{ y(x) = \frac{\_C1(5x^2-1)}{x^2} + \_C2 {}_1F_1 \left( -\frac{5}{2}; -\frac{1}{2}; \frac{1}{2x^2} \right) x^3 \right\}$$

**3.355 ODE No. 1355**

$$\frac{d^2}{dx^2}y(x) = -\frac{(x^3 - 1) \frac{d}{dx}y(x)}{(x^3 + 1)x} + \frac{xy(x)}{x^3 + 1} = 0$$

**Mathematica:** cpu = 0.131517 (sec), leaf count = 59

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2}c_2 \left( 2x^2 - x^2 \sqrt[3]{x^3 + 1} {}_2F_1 \left( \frac{1}{3}, \frac{2}{3}; \frac{5}{3}; -x^3 \right) \right) + c_1 \sqrt[3]{x^3 + 1} \right\} \right\}$$

**Maple:** cpu = 0.110 (sec), leaf count = 37

$$\left\{ y(x) = \_C1 x^2 \sqrt[3]{x^3 + 1} {}_2F_1 \left( \frac{2}{3}, \frac{4}{3}; \frac{5}{3}; -x^3 \right) + \_C2 \sqrt[3]{x^3 + 1} \right\}$$

**3.356 ODE No. 1356**

$$\frac{d^2}{dx^2}y(x) = -\frac{(2x^2 + 1) \frac{d}{dx}y(x)}{x(x^2 + 1)} - \frac{(-v(v + 1)x^2 - n^2)y(x)}{x^2(x^2 + 1)} = 0$$

**Mathematica:** cpu = 0.287536 (sec), leaf count = 90

$$\left\{ \left\{ y(x) \rightarrow c_1 x^{-n} {}_2F_1 \left( -\frac{n}{2} - \frac{v}{2}, -\frac{n}{2} + \frac{v}{2} + \frac{1}{2}; 1 - n; -x^2 \right) + c_2 x^n {}_2F_1 \left( \frac{n}{2} - \frac{v}{2}, \frac{n}{2} + \frac{v}{2} + \frac{1}{2}; n + 1; -x^2 \right) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 29

$$\left\{ y(x) = \_C1 \text{LegendreP}(v, n, \sqrt{x^2 + 1}) + \_C2 \text{LegendreQ}(v, n, \sqrt{x^2 + 1}) \right\}$$

**3.357 ODE No. 1357**

$$\frac{d^2}{dx^2}y(x) = -\frac{(ax^2 + a - 1) \frac{d}{dx}y(x)}{x(x^2 + 1)} - \frac{(bx^2 + c)y(x)}{x^2(x^2 + 1)} = 0$$

**Mathematica:** cpu = 0.665585 (sec), leaf count = 288

$$\left\{ \left\{ y(x) \rightarrow c_1 x^{\frac{1}{2}(-\sqrt{a^2 - 4a - 4c + 4} - a + 2)} {}_2F_1 \left( -\frac{1}{4}\sqrt{a^2 - 2a - 4b + 1} - \frac{1}{4}\sqrt{a^2 - 4a - 4c + 4} + \frac{1}{4}, \frac{1}{4}\sqrt{a^2 - 2a - 4b + 1} - \frac{1}{4}\sqrt{a^2 - 4a - 4c + 4} + \frac{1}{4}; \frac{1}{2}\sqrt{a^2 - 2a - 4b + 1} - \frac{1}{2}\sqrt{a^2 - 4a - 4c + 4} + \frac{1}{2}; -x^2 \right) + c_2 x^{\frac{1}{2}(-\sqrt{a^2 - 4a - 4c + 4} + a + 2)} {}_2F_1 \left( -\frac{1}{4}\sqrt{a^2 - 2a - 4b + 1} + \frac{1}{4}\sqrt{a^2 - 4a - 4c + 4} + \frac{1}{4}, \frac{1}{4}\sqrt{a^2 - 2a - 4b + 1} + \frac{1}{4}\sqrt{a^2 - 4a - 4c + 4} + \frac{1}{4}; \frac{1}{2}\sqrt{a^2 - 2a - 4b + 1} + \frac{1}{2}\sqrt{a^2 - 4a - 4c + 4} + \frac{1}{2}; -x^2 \right) \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 103

$$\left\{ y(x) = \_C1 x^{1 - \frac{a}{2}} \text{LegendreP} \left( -\frac{1}{2} + \frac{1}{2}\sqrt{a^2 - 2a - 4b + 1}, \frac{1}{2}\sqrt{a^2 - 4a - 4c + 4}, \sqrt{x^2 + 1} \right) + \_C2 x^{1 - \frac{a}{2}} \text{LegendreQ} \left( -\frac{1}{2} + \frac{1}{2}\sqrt{a^2 - 2a - 4b + 1}, \frac{1}{2}\sqrt{a^2 - 4a - 4c + 4}, \sqrt{x^2 + 1} \right) \right\}$$

**3.358 ODE No. 1358**

$$\frac{d^2}{dx^2}y(x) = \frac{(x^2 - 2) \frac{d}{dx}y(x)}{x(x^2 - 1)} - \frac{(x^2 - 2)y(x)}{x^2(x^2 - 1)} = 0$$

**Mathematica:** cpu = 0.065008 (sec), leaf count = 66

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 x \sqrt[4]{x^2 - 1}}{\sqrt[4]{1 - x^2}} + \frac{c_2 x \sqrt[4]{x^2 - 1} \log(\sqrt{x^2 - 1} + x)}{\sqrt[4]{1 - x^2}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 21

$$\left\{ y(x) = x\_C1 + \_C2 x \ln(x + \sqrt{x^2 - 1}) \right\}$$

**3.359 ODE No. 1359**

$$\frac{d^2}{dx^2}y(x) = -2 \frac{x \frac{d}{dx}y(x)}{x^2 - 1} - \frac{v(v + 1)y(x)}{x^2(x^2 - 1)} = 0$$

**Mathematica:** cpu = 0.101513 (sec), leaf count = 86

$$\left\{ \left\{ y(x) \rightarrow c_1 i^{-v} x^{-v} {}_2F_1\left(\frac{1}{2} - \frac{v}{2}, -\frac{v}{2}; \frac{1}{2} - v; x^2\right) + c_2 i^{v+1} x^{v+1} {}_2F_1\left(\frac{v}{2} + \frac{1}{2}, \frac{v}{2} + 1; v + \frac{3}{2}; x^2\right) \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 57

$$\left\{ y(x) = \_C1 {}_2F_1\left(-\frac{v}{2}, \frac{1}{2} - \frac{v}{2}; \frac{1}{2} - v; x^2\right) x^{-v} + \_C2 {}_2F_1\left(1 + \frac{v}{2}, \frac{1}{2} + \frac{v}{2}; \frac{3}{2} + v; x^2\right) x^{v+1} \right\}$$

**3.360 ODE No. 1360**

$$\frac{d^2}{dx^2}y(x) = -2 \frac{x \frac{d}{dx}y(x)}{x^2 - 1} + \frac{v(v + 1)y(x)}{x^2} = 0$$

**Mathematica:** cpu = 0.091512 (sec), leaf count = 68

$$\left\{ \left\{ y(x) \rightarrow c_1 i^{-v} x^{-v} {}_2F_1\left(\frac{1}{2}, -v; \frac{1}{2} - v; x^2\right) + c_2 i^{v+1} x^{v+1} {}_2F_1\left(\frac{1}{2}, v + 1; v + \frac{3}{2}; x^2\right) \right\} \right\}$$

**Maple:** cpu = 0.046 (sec), leaf count = 47

$$\left\{ y(x) = \_C1 {}_2F_1\left(\frac{1}{2}, -v; \frac{1}{2} - v; x^2\right) x^{-v} + \_C2 {}_2F_1\left(\frac{1}{2}, v + 1; \frac{3}{2} + v; x^2\right) x^{v+1} \right\}$$



### 3.361 ODE No. 1361

$$\frac{d^2}{dx^2}y(x) = 2 \frac{x \frac{d}{dx}y(x)}{x^2 - 1} - \frac{(a(a+1) - ax^2(a+3))y(x)}{x^2(x^2 - 1)} = 0$$

**Mathematica:** cpu = 0.471560 (sec), leaf count = 38

$$\{ \{y(x) \rightarrow c_1 x^{-a} + c_2 (-2ax^2 + 2a - x^2 + 3) x^{a+1} \} \}$$

**Maple:** cpu = 0.015 (sec), leaf count = 33

$$\{y(x) = \_C1 x^{-a} + \_C2 x^{a+1} (2ax^2 + x^2 - 2a - 3)\}$$

### 3.362 ODE No. 1362

$$x^2(x^2 - 1) \frac{d^2}{dx^2}y(x) - 2x^3 \frac{d}{dx}y(x) - ((a - n)(a + n + 1)x^2(x^2 - 1) + 2ax^2 + n(n + 1)(x^2 - 1))y(x) = 0$$

**Mathematica:** cpu = 14.232807 (sec), leaf count = 115

$$\{ \{y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{-2y'(x)x^3 + (a^2x^4 - n^2x^4 + ax^4 - nx^4 - a^2x^2 + 2n^2x^2 + ax^2 + 2nx^2 - (a - n)(a + n + 1)x^2(x^2 - 1) + 2ax^2 + n(n + 1)(x^2 - 1))y(x)\}) \} \}$$

**Maple:** cpu = 0.172 (sec), leaf count = 109

$$\{y(x) = \_C1 \text{HeunC}\left(0, -n - \frac{1}{2}, -2, -\frac{a^2}{4} + \frac{n^2}{4} - \frac{a}{4} + \frac{n}{4}, -\frac{n^2}{4} - \frac{n}{4} + \frac{3}{4} + \frac{a^2}{4} - \frac{a}{4}, x^2\right) x^{-n} + \_C2 \text{HeunC}\left(0, -n - \frac{1}{2}, -2, -\frac{a^2}{4} + \frac{n^2}{4} - \frac{a}{4} + \frac{n}{4}, -\frac{n^2}{4} - \frac{n}{4} + \frac{3}{4} + \frac{a^2}{4} - \frac{a}{4}, x^2\right) x^{-n}\}$$

### 3.363 ODE No. 1363

$$\frac{d^2}{dx^2}y(x) = -\frac{(ax^2 + a - 2) \frac{d}{dx}y(x)}{x(x^2 - 1)} - \frac{by(x)}{x^2} = 0$$

**Mathematica:** cpu = 0.803102 (sec), leaf count = 236

$$\{ \{y(x) \rightarrow c_1 (-1)^{\frac{1}{4}(-\sqrt{a^2-2a-4b+1+a-1})} x^{\frac{1}{2}(-\sqrt{a^2-2a-4b+1+a-1})} {}_2F_1\left(\frac{a}{2} - \frac{1}{2}, \frac{a}{2} - \frac{1}{2}, \frac{1}{2}\sqrt{a^2 - 2a - 4b + 1} - \frac{1}{2}; 1\right) + c_2 (-1)^{\frac{1}{4}(\sqrt{a^2-2a-4b+1+a-1})} x^{\frac{1}{2}(\sqrt{a^2-2a-4b+1+a-1})} {}_2F_1\left(\frac{a}{2} + \frac{1}{2}, \frac{a}{2} + \frac{1}{2}, \frac{1}{2}\sqrt{a^2 - 2a - 4b + 1} + \frac{1}{2}; 1\right)\} \}$$

**Maple:** cpu = 0.109 (sec), leaf count = 171

$$\{y(x) = \_C1 x^{\frac{a}{2} - \frac{1}{2} + \frac{1}{2}\sqrt{a^2 - 2a - 4b + 1}} (x^2 - 1)^{-a+2} {}_2F_1\left(-\frac{a}{2} + \frac{3}{2}, -\frac{a}{2} + \frac{3}{2} + \frac{1}{2}\sqrt{a^2 - 2a - 4b + 1}; 1 + \frac{1}{2}\sqrt{a^2 - 2a - 4b + 1}\right) + \_C2 x^{\frac{a}{2} + \frac{1}{2} + \frac{1}{2}\sqrt{a^2 - 2a - 4b + 1}} (x^2 - 1)^{-a+2} {}_2F_1\left(-\frac{a}{2} + \frac{3}{2}, -\frac{a}{2} + \frac{3}{2} + \frac{1}{2}\sqrt{a^2 - 2a - 4b + 1}; 1 + \frac{1}{2}\sqrt{a^2 - 2a - 4b + 1}\right)\}$$

### 3.364 ODE No. 1364

$$\frac{d^2}{dx^2}y(x) = \frac{(2bcx^c(x^2 - 1) + 2(a - 1)x^2 - 2a) \frac{d}{dx}y(x)}{x(x^2 - 1)} - \frac{(b^2c^2x^{2c}(x^2 - 1) + bcx^{c+2}(2a - c - 1) - bcx^c)}{x(x^2 - 1)}$$

**Mathematica:** cpu = 0.171522 (sec), leaf count = 42

$$\left\{ \left\{ y(x) \rightarrow c_1 P_\nu(x) e^{a \log(x) + bx^c} + c_2 Q_\nu(x) e^{a \log(x) + bx^c} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 33

$$\{y(x) = \_C1 x^a e^{bx^c} \text{LegendreP}(\nu, x) + \_C2 x^a e^{bx^c} \text{LegendreQ}(\nu, x)\}$$

### 3.365 ODE No. 1365

$$\frac{d^2}{dx^2}y(x) = -\frac{ay(x)}{(x^2 + 1)^2} = 0$$

**Mathematica:** cpu = 0.093512 (sec), leaf count = 72

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt{x^2 + 1} e^{i\sqrt{a+1} \tan^{-1}(x)} + \frac{ic_2 \sqrt{x^2 + 1} e^{-i\sqrt{a+1} \tan^{-1}(x)}}{2\sqrt{a+1}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 65

$$\left\{ y(x) = \_C1 \sqrt{x^2 + 1} \left( \frac{x+i}{-x+i} \right)^{\frac{1}{2}\sqrt{a+1}} + \_C2 \sqrt{x^2 + 1} \left( \frac{x+i}{-x+i} \right)^{-\frac{1}{2}\sqrt{a+1}} \right\}$$

### 3.366 ODE No. 1366

$$\frac{d^2}{dx^2}y(x) = -2 \frac{x \frac{d}{dx}y(x)}{x^2 + 1} - \frac{y(x)}{(x^2 + 1)^2} = 0$$

**Mathematica:** cpu = 0.022503 (sec), leaf count = 31

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{\sqrt{x^2 + 1}} + \frac{c_2 x}{\sqrt{x^2 + 1}} \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 24

$$\left\{ y(x) = x \_C1 \frac{1}{\sqrt{x^2 + 1}} + \_C2 \frac{1}{\sqrt{x^2 + 1}} \right\}$$

### 3.367 ODE No. 1367

$$\frac{d^2}{dx^2}y(x) = -2 \frac{x \frac{d}{dx}y(x)}{x^2 + 1} - \frac{(a^2(x^2 + 1)^2 - n(n+1)(x^2 + 1) + m^2)y(x)}{(x^2 + 1)^2} = 0$$

**Mathematica:** cpu = 2.299792 (sec), leaf count = 98

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}\left(\{y, x\}, \left\{y''(x)(x^2 + 1)^2 + 2xy'(x)(x^2 + 1) + (a^2x^4 + 2a^2x^2 - n^2x^2 - nx^2 + m^2)y(x)\right\}\right) \right\} \right\}$$

**Maple:** cpu = 0.187 (sec), leaf count = 96

$$\left\{ y(x) = \_C1 (x^2 + 1)^{\frac{m}{2}} \text{HeunC}\left(0, -\frac{1}{2}, m, -\frac{a^2}{4}, \frac{1}{4} + \frac{a^2}{4} + \frac{m^2}{4} - \frac{n^2}{4} - \frac{n}{4}, -x^2\right) + \_C2 (x^2 + 1)^{\frac{m}{2}} x \text{HeunC}\left(0, -\frac{1}{2}, m, -\frac{a^2}{4}, \frac{1}{4} + \frac{a^2}{4} + \frac{m^2}{4} - \frac{n^2}{4} - \frac{n}{4}, -x^2\right) \right\}$$

### 3.368 ODE No. 1368

$$\frac{d^2}{dx^2}y(x) = -\frac{ax \frac{d}{dx}y(x)}{x^2 + 1} - \frac{by(x)}{(x^2 + 1)^2} = 0$$

**Mathematica:** cpu = 0.026503 (sec), leaf count = 106

$$\left\{ \left\{ y(x) \rightarrow c_1 (x^2 + 1)^{\frac{2-a}{4}} P_{\frac{a-2}{2}}^{\frac{1}{2}\sqrt{a^2-4a+4b+4}}(ix) + c_2 (x^2 + 1)^{\frac{2-a}{4}} Q_{\frac{a-2}{2}}^{\frac{1}{2}\sqrt{a^2-4a+4b+4}}(ix) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 81

$$\left\{ y(x) = \_C1 (x^2 + 1)^{\frac{1}{2}-\frac{a}{4}} \text{LegendreP}\left(\frac{a}{2} - 1, \frac{1}{2}\sqrt{a^2 - 4a + 4b + 4}, ix\right) + \_C2 (x^2 + 1)^{\frac{1}{2}-\frac{a}{4}} \text{LegendreQ}\left(\frac{a}{2} - 1, \frac{1}{2}\sqrt{a^2 - 4a + 4b + 4}, ix\right) \right\}$$

### 3.369 ODE No. 1369

$$\frac{d^2}{dx^2}y(x) = -\frac{ay(x)}{(x^2 - 1)^2} = 0$$

**Mathematica:** cpu = 0.102513 (sec), leaf count = 75

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt{1-x^2} e^{-\sqrt{1-a} \tanh^{-1}(x)} + \frac{c_2 \sqrt{1-x^2} e^{\sqrt{1-a} \tanh^{-1}(x)}}{2\sqrt{1-a}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 61

$$\left\{ y(x) = \_C1 \sqrt{x^2 - 1} \left(\frac{x-1}{1+x}\right)^{\frac{1}{2}\sqrt{1-a}} + \_C2 \sqrt{x^2 - 1} \left(\frac{x-1}{1+x}\right)^{-\frac{1}{2}\sqrt{1-a}} \right\}$$

**3.370 ODE No. 1370**

$$\frac{d^2}{dx^2}y(x) = -2 \frac{x \frac{d}{dx}y(x)}{x^2 - 1} + \frac{a^2 y(x)}{(x^2 - 1)^2} = 0$$

**Mathematica:** cpu = 0.028504 (sec), leaf count = 53

$$\left\{ \left\{ y(x) \rightarrow c_1 \cosh \left( \frac{1}{2} a (\log(1-x) - \log(x+1)) \right) + i c_2 \sinh \left( \frac{1}{2} a (\log(1-x) - \log(x+1)) \right) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 19

$$\{y(x) = \_C1 \sinh(a \operatorname{Artanh}(x)) + \_C2 \cosh(a \operatorname{Artanh}(x))\}$$

**3.371 ODE No. 1371**

$$\frac{d^2}{dx^2}y(x) = -2 \frac{x \frac{d}{dx}y(x)}{x^2 - 1} - \frac{(-a^2 - \lambda(x^2 - 1)) y(x)}{(x^2 - 1)^2} = 0$$

**Mathematica:** cpu = 0.021503 (sec), leaf count = 48

$$\left\{ \left\{ y(x) \rightarrow c_1 P_{\frac{1}{2}(\sqrt{4\lambda+1}-1)}^a(x) + c_2 Q_{\frac{1}{2}(\sqrt{4\lambda+1}-1)}^a(x) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 37

$$\left\{ y(x) = \_C1 \operatorname{LegendreP} \left( \frac{1}{2} \sqrt{1+4\lambda} - \frac{1}{2}, a, x \right) + \_C2 \operatorname{LegendreQ} \left( \frac{1}{2} \sqrt{1+4\lambda} - \frac{1}{2}, a, x \right) \right\}$$

**3.372 ODE No. 1372**

$$\frac{d^2}{dx^2}y(x) = -2 \frac{x \frac{d}{dx}y(x)}{x^2 - 1} - \frac{((x^2 - 1)(ax^2 + bx + c) - k^2) y(x)}{(x^2 - 1)^2} = 0$$

**Mathematica:** cpu = 4.812611 (sec), leaf count = 93

$$\left\{ \left\{ y(x) \rightarrow \operatorname{DifferentialRoot}(\{y, x\}, \{(ax^4 + bx^3 - ax^2 + cx^2 - bx - k^2 - c) y(x) + (2x^3 - 2x) y'(x) + (x^2 - 1) y''(x)\}) \right\} \right\}$$

**Maple:** cpu = 0.187 (sec), leaf count = 120

$$\left\{ y(x) = \_C1 e^{\sqrt{-ax}} \operatorname{HeunC} \left( 4\sqrt{-a}, k, k, 2b, \frac{k^2}{2} + a - b + c, \frac{1}{2} + \frac{x}{2} \right) (x^2 - 1)^{\frac{k}{2}} + \_C2 e^{\sqrt{-ax}} \operatorname{HeunC} \left( 4\sqrt{-a}, k, k, 2b, \frac{k^2}{2} + a - b + c, \frac{1}{2} + \frac{x}{2} \right) (x^2 - 1)^{\frac{k}{2}} \right\}$$

### 3.373 ODE No. 1373

$$\frac{d^2}{dx^2}y(x) = -2 \frac{x \frac{d}{dx}y(x)}{x^2 - 1} - \frac{(-a^2(x^2 - 1)^2 - n(n + 1)(x^2 - 1) - m^2)y(x)}{(x^2 - 1)^2} = 0$$

**Mathematica:** cpu = 2.321295 (sec), leaf count = 104

$$\{ \{y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{(-a^2x^4 + 2a^2x^2 - n^2x^2 - nx^2 - a^2 - m^2 + n^2 + n)y(x) + (2x^3 - 2$$

**Maple:** cpu = 0.156 (sec), leaf count = 92

$$\{y(x) = \_C1 (x^2 - 1)^{\frac{m}{2}} \text{HeunC}\left(0, -\frac{1}{2}, m, -\frac{a^2}{4}, \frac{1}{4} + \frac{a^2}{4} + \frac{m^2}{4} - \frac{n^2}{4} - \frac{n}{4}, x^2\right) + \_C2 (x^2 - 1)^{\frac{m}{2}} x \text{HeunC}$$

### 3.374 ODE No. 1374

$$\frac{d^2}{dx^2}y(x) = 2 \frac{x(2a - 1) \frac{d}{dx}y(x)}{x^2 - 1} - \frac{(x^2(2a(2a - 1) - v(v + 1)) + 2a + v(v + 1))y(x)}{(x^2 - 1)^2} = 0$$

**Mathematica:** cpu = 0.036005 (sec), leaf count = 32

$$\{ \{y(x) \rightarrow c_1(x^2 - 1)^a P_v(x) + c_2(x^2 - 1)^a Q_v(x)\} \}$$

**Maple:** cpu = 0.032 (sec), leaf count = 29

$$\{y(x) = \_C1 (x^2 - 1)^a \text{LegendreP}(v, x) + \_C2 (x^2 - 1)^a \text{LegendreQ}(v, x)\}$$

### 3.375 ODE No. 1375

$$\frac{d^2}{dx^2}y(x) = -2 \frac{x(n + 1 - 2a) \frac{d}{dx}y(x)}{x^2 - 1} - \frac{(4ax^2(a - n) - (x^2 - 1)(2a + (v - n)(v + n + 1)))y(x)}{(x^2 - 1)^2} = 0$$

**Mathematica:** cpu = 0.051506 (sec), leaf count = 54

$$\{ \{y(x) \rightarrow c_1(x^2 - 1)^{\frac{1}{2}(2a-n)} P_v^n(x) + c_2(x^2 - 1)^{\frac{1}{2}(2a-n)} Q_v^n(x)\} \}$$

**Maple:** cpu = 0.047 (sec), leaf count = 39

$$\{y(x) = \_C1 (x^2 - 1)^{a-\frac{n}{2}} \text{LegendreP}(v, n, x) + \_C2 (x^2 - 1)^{a-\frac{n}{2}} \text{LegendreQ}(v, n, x)\}$$

### 3.376 ODE No. 1376

$$\frac{d^2}{dx^2}y(x) = -\frac{(2x^2 + a)\frac{d}{dx}y(x)}{x(x^2 + a)} - \frac{by(x)}{x^2(x^2 + a)} = 0$$

**Mathematica:** cpu = 0.096512 (sec), leaf count = 82

$$\left\{ \left\{ y(x) \rightarrow c_2 \sin \left( \frac{\sqrt{b}(\log(x) - \log(\sqrt{a}\sqrt{a+x^2+a}))}{\sqrt{a}} \right) + c_1 \cos \left( \frac{\sqrt{b}(\log(x) - \log(\sqrt{a}\sqrt{a+x^2+a}))}{\sqrt{a}} \right) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 71

$$\left\{ y(x) = -C1 \left( \left( \frac{1}{x} (2a + 2\sqrt{a}\sqrt{x^2+a}) \right)^{i\sqrt{b}\frac{1}{\sqrt{a}}} \right)^{-1} + -C2 \left( \frac{1}{x} (2a + 2\sqrt{a}\sqrt{x^2+a}) \right)^{i\sqrt{b}\frac{1}{\sqrt{a}}} \right\}$$

### 3.377 ODE No. 1377

$$\frac{d^2}{dx^2}y(x) = -\frac{b^2y(x)}{(a^2 + x^2)^2} = 0$$

**Mathematica:** cpu = 0.236030 (sec), leaf count = 109

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt{a^2 + x^2} e^{i\sqrt{\frac{b^2}{a^2} + 1} \tan^{-1}\left(\frac{x}{a}\right)} + \frac{ic_2 \sqrt{a^2 + x^2} e^{-i\sqrt{\frac{a^2+b^2}{a^2}} \tan^{-1}\left(\frac{x}{a}\right)}}{2a\sqrt{\frac{a^2+b^2}{a^2}}} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 91

$$\left\{ y(x) = -C1 \sqrt{a^2 + x^2} \left( \frac{ix - a}{ix + a} \right)^{\frac{1}{2a}\sqrt{a^2+b^2}} + -C2 \sqrt{a^2 + x^2} \left( \frac{ix - a}{ix + a} \right)^{-\frac{1}{2a}\sqrt{a^2+b^2}} \right\}$$

### 3.378 ODE No. 1378

$$\frac{d^2}{dx^2}y(x) = -2\frac{(x^2 - 1)\frac{d}{dx}y(x)}{x(x-1)^2} - \frac{(-2x^2 + 2x + 2)y(x)}{x^2(x-1)^2} = 0$$

**Mathematica:** cpu = 0.049506 (sec), leaf count = 65

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 x^2}{1-x} + \frac{c_2 x(2x^2 \log(1-x) - 2x^2 \log(x) + 2x - 2x \log(1-x) + 2x \log(x) - 1)}{(x-1)^2} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 50

$$\left\{ y(x) = \frac{C1 x^2}{x-1} + \frac{-C2 x}{(x-1)^2} \left( (-x^2 + x) \ln(x-1) + (x^2 - x) \ln(x) - x + \frac{1}{2} \right) \right\}$$

**3.379 ODE No. 1379**

$$\frac{d^2}{dx^2}y(x) = 12 \frac{y(x)}{(1+x)^2(x^2+2x+3)} = 0$$

**Mathematica:** cpu = 0.077510 (sec), leaf count = 99

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 \left( 2x^3 + 4x^2 - 3\sqrt{2}x^2 \tan^{-1} \left( \frac{x+1}{\sqrt{2}} \right) + 8x - 6\sqrt{2}x \tan^{-1} \left( \frac{x+1}{\sqrt{2}} \right) - 9\sqrt{2} \tan^{-1} \left( \frac{x+1}{\sqrt{2}} \right) + 2 \right)}{2(x+1)^2} + c_1 \right\} \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 66

$$\left\{ y(x) = \frac{-C1(x^2+2x+3)}{(1+x)^2} + \frac{-C2}{(1+x)^2} \left( (3x^2+6x+9) \arctan \left( \frac{(1+x)\sqrt{2}}{2} \right) - \sqrt{2}(x^3+2x^2+4x+3) \right) \right.$$

**3.380 ODE No. 1380**

$$\frac{d^2}{dx^2}y(x) = -\frac{by(x)}{x^2(x-a)^2} = 0$$

**Mathematica:** cpu = 0.297038 (sec), leaf count = 132

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2(x-a)^{\frac{1}{2}}\sqrt{\frac{a^2-4b}{a^2}} + \frac{1}{2}x^{\frac{1}{2}-\frac{1}{2}}\sqrt{\frac{a^2-4b}{a^2}}}{a\sqrt{\frac{a^2-4b}{a^2}}} + c_1(x-a)^{\frac{1}{2}-\frac{1}{2}}\sqrt{1-\frac{4b}{a^2}}x^{\frac{1}{2}}\sqrt{1-\frac{4b}{a^2}+\frac{1}{2}} \right\} \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 75

$$\left\{ y(x) = -C1 \sqrt{x(a-x)} \left( \frac{a-x}{x} \right)^{\frac{1}{2a}\sqrt{a^2-4b}} + -C2 \sqrt{x(a-x)} \left( \frac{x}{a-x} \right)^{\frac{1}{2a}\sqrt{a^2-4b}} \right.$$

**3.381 ODE No. 1381**

$$\frac{d^2}{dx^2}y(x) = -\frac{by(x)}{x^2(x-a)^2} + c = 0$$

**Mathematica:** cpu = 0.626080 (sec), leaf count = 589

$$\left\{ \left\{ y(x) \rightarrow -\frac{2cx^2(a-x)(1-\frac{x}{a})^{-\frac{1}{2}}\sqrt{\frac{a^2-4b}{a^2}} \left( \sqrt{\frac{a^2-4b}{a^2}}(1-\frac{x}{a})\sqrt{\frac{a^2-4b}{a^2}} {}_2F_1 \left( \frac{1}{2}\sqrt{1-\frac{4b}{a^2}} - \frac{1}{2}, \frac{1}{2}\sqrt{1-\frac{4b}{a^2}} + \frac{3}{2}, \frac{1}{2} \right) \right)}{2} \right\} \right.$$

**Maple:** cpu = 0.109 (sec), leaf count = 219

$$\left\{ y(x) = \sqrt{x(a-x)} \left( \frac{a-x}{x} \right)^{\frac{1}{2a}\sqrt{a^2-4b}} \_C2 + \sqrt{x(a-x)} \left( \frac{x}{a-x} \right)^{\frac{1}{2a}\sqrt{a^2-4b}} \_C1 + c\sqrt{x(a-x)} \left( \left( \frac{x}{a-x} \right)^{\frac{1}{2a}\sqrt{a^2-4b}} \right) \right\}$$

### 3.382 ODE No. 1382

$$\frac{d^2}{dx^2}y(x) = \frac{cy(x)}{(x-a)^2(x-b)^2} = 0$$

**Mathematica:** cpu = 0.699089 (sec), leaf count = 154

$$\left\{ \left\{ y(x) \rightarrow c_1(x-a)^{\frac{1}{2}\left(\sqrt{\frac{4c}{(a-b)^2}+1}+1\right)}(x-b)^{\frac{1}{2}\left(1-\sqrt{\frac{4c}{(a-b)^2}+1}\right)} - \frac{c_2(x-a)^{\frac{1}{2}-\frac{1}{2}\sqrt{\frac{4c}{(a-b)^2}+1}}(x-b)^{\frac{1}{2}\sqrt{\frac{4c}{(a-b)^2}+1}+\frac{1}{2}}}{(a-b)\sqrt{\frac{4c}{(a-b)^2}+1}} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 116

$$\left\{ y(x) = \_C1 \sqrt{(a-x)(b-x)} \left( \frac{a-x}{b-x} \right)^{\frac{1}{2a-2b}\sqrt{a^2-2ab+b^2+4c}} + \_C2 \sqrt{(a-x)(b-x)} \left( \frac{a-x}{b-x} \right)^{-\frac{1}{2a-2b}\sqrt{a^2-2ab+b^2+4c}} \right\}$$

### 3.383 ODE No. 1383

$$\frac{d^2}{dx^2}y(x) = -\frac{((\alpha + \beta + 1)(x-a)^2(x-b) + (1 - \alpha - \beta)(x-b)^2(x-a)) \frac{d}{dx}y(x)}{(x-a)^2(x-b)^2} - \frac{\alpha\beta(a-b)^2 y(x)}{(x-a)^2(x-b)^2}$$

**Mathematica:** cpu = 0.138018 (sec), leaf count = 50

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\alpha(\log(x-a)-\log(x-b))} + c_2 e^{\beta(\log(x-a)-\log(x-b))} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 39

$$\left\{ y(x) = \_C1 \left( \frac{a-x}{b-x} \right)^\beta + \_C2 \left( \frac{a-x}{b-x} \right)^\alpha \right\}$$



**3.384 ODE No. 1384**

$$\frac{d^2}{dx^2}y(x) = -1/4 \frac{(-x^2(a^2 - 1) + 2(a + 3)bx - b^2)y(x)}{x^2} = 0$$

**Mathematica:** cpu = 0.033504 (sec), leaf count = 110

$$\left\{ \left\{ y(x) \rightarrow c_1 M_{\frac{(a+3)b}{2\sqrt{a^2-1}}, \frac{\sqrt{b(b^2+1)}}{2\sqrt{b}}}(\sqrt{a^2-1}x) + c_2 W_{\frac{(a+3)b}{2\sqrt{a^2-1}}, \frac{\sqrt{b(b^2+1)}}{2\sqrt{b}}}(\sqrt{a^2-1}x) \right\} \right\}$$

**Maple:** cpu = 0.187 (sec), leaf count = 73

$$\left\{ y(x) = -C1 M_{\frac{(a+3)b}{2}, \frac{1}{\sqrt{a^2-1}}, \frac{1}{2}\sqrt{b^2+1}}(\sqrt{a^2-1}x) + -C2 W_{\frac{(a+3)b}{2}, \frac{1}{\sqrt{a^2-1}}, \frac{1}{2}\sqrt{b^2+1}}(\sqrt{a^2-1}x) \right\}$$

**3.385 ODE No. 1385**

$$\frac{d^2}{dx^2}y(x) = -1/4 \frac{(ax^2 + a - 3)y(x)}{(x^2 + 1)^2} = 0$$

**Mathematica:** cpu = 0.019002 (sec), leaf count = 78

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt{x^2 + 1} P_{\frac{1}{2}(\sqrt{1-a}-1)}^{\frac{1}{2}}(ix) + c_2 \sqrt{x^2 + 1} Q_{\frac{1}{2}(\sqrt{1-a}-1)}^{\frac{1}{2}}(ix) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 61

$$\left\{ y(x) = -C1 \sqrt[4]{x^2 + 1} (x + \sqrt{x^2 + 1})^{\frac{1}{2}\sqrt{1-a}} + -C2 \sqrt[4]{x^2 + 1} (x + \sqrt{x^2 + 1})^{-\frac{1}{2}\sqrt{1-a}} \right\}$$

**3.386 ODE No. 1386**

$$\frac{d^2}{dx^2}y(x) = 18 \frac{y(x)}{(2x + 1)^2 (x^2 + x + 1)} = 0$$

**Mathematica:** cpu = 0.089011 (sec), leaf count = 108

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1(x^2 + x + 1)}{(2x + 1)^2} + \frac{c_2 \left( 16x^3 + 24x^2 - 12\sqrt{3}x^2 \tan^{-1}\left(\frac{2x+1}{\sqrt{3}}\right) + 30x - 12\sqrt{3}x \tan^{-1}\left(\frac{2x+1}{\sqrt{3}}\right) - 12 \right)}{(2x + 1)^2} \right\} \right\}$$

**Maple:** cpu = 0.046 (sec), leaf count = 68

$$\left\{ y(x) = \frac{-C1(x^2 + x + 1)}{(2x + 1)^2} + \frac{-C2}{(2x + 1)^2} \left( (36x^2 + 36x + 36) \arctan\left(\frac{(2x + 1)\sqrt{3}}{3}\right) - 16\sqrt{3}(x^3 + x^2 - \dots) \right) \right\}$$

**3.387 ODE No. 1387**

$$\frac{d^2}{dx^2}y(x) = 3/4 \frac{y(x)}{(x^2 + x + 1)^2} = 0$$

**Mathematica:** cpu = 0.038505 (sec), leaf count = 50

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt{x^2 + x + 1} + \frac{2c_2 \sqrt{x^2 + x + 1} \tan^{-1} \left( \frac{2x+1}{\sqrt{3}} \right)}{\sqrt{3}} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 36

$$\left\{ y(x) = \_C1 \sqrt{x^2 + x + 1} + \_C2 \arctan \left( \frac{(2x + 1) \sqrt{3}}{3} \right) \sqrt{x^2 + x + 1} \right\}$$

**3.388 ODE No. 1388**

$$\frac{d^2}{dx^2}y(x) = -1/2 \frac{(3x - 1) \frac{d}{dx}y(x)}{x(x - 1)} - 1/4 \frac{(v(v + 1)(x - 1) - a^2x)y(x)}{x^2(x - 1)^2} = 0$$

**Mathematica:** cpu = 0.291037 (sec), leaf count = 235

$$\left\{ \left\{ y(x) \rightarrow c_2 (-1)^{\frac{1}{2}(-2v-3)+1} x^{\frac{1}{4}(-2v-3)+1} e^{\frac{1}{4}(-2\log(1-x)-\log(x))} (x - 1)^{\frac{1}{2}(\frac{1}{2}(a+v+1)+\frac{1}{2}(a+v+2)+\frac{1}{2}(-2v-3)+1)} {}_2F_1 \left( \frac{1}{2} \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 82

$$\left\{ y(x) = \_C1 x^{-\frac{v}{2}}(x - 1)^{-\frac{a}{2}} {}_2F_1 \left( -\frac{v}{2} - \frac{a}{2}, \frac{1}{2} - \frac{v}{2} - \frac{a}{2}; \frac{1}{2} - v; x \right) + \_C2 x^{\frac{1}{2}+\frac{v}{2}}(x - 1)^{-\frac{a}{2}} {}_2F_1 \left( 1 + \frac{v}{2} - \frac{a}{2}, \frac{1}{2} \right) \right\}$$

**3.389 ODE No. 1389**

$$\frac{d^2}{dx^2}y(x) = -1/2 \frac{(3x - 1) \frac{d}{dx}y(x)}{x(x - 1)} - 1/4 \frac{(-v(v + 1)(x - 1)^2 - 4n^2x)y(x)}{x^2(x - 1)^2} = 0$$

**Mathematica:** cpu = 0.378548 (sec), leaf count = 217

$$\left\{ \left\{ y(x) \rightarrow c_2 (-1)^{\frac{1}{2}(-2v-3)+1} x^{\frac{1}{4}(-2v-3)+1} e^{\frac{1}{4}(-2\log(1-x)-\log(x))} (x - 1)^{\frac{1}{2}(n+\frac{1}{2}(2n+1)+\frac{1}{2}(-2v-3)+v+2)} {}_2F_1 \left( \frac{1}{2}(2n + 1) \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 74

$$\left\{ y(x) = \_C1 x^{-\frac{v}{2}}(x - 1)^{-n} {}_2F_1 \left( -v - n, -n + \frac{1}{2}; \frac{1}{2} - v; x \right) + \_C2 x^{\frac{1}{2}+\frac{v}{2}}(x - 1)^{-n} {}_2F_1 \left( v - n + 1, -n + \frac{1}{2} \right) \right\}$$

**3.390 ODE No. 1390**

$$\frac{d^2}{dx^2}y(x) = -3/16 \frac{y(x)}{x^2(x-1)^2} = 0$$

**Mathematica:** cpu = 0.041005 (sec), leaf count = 51

$$\left\{ \left\{ y(x) \rightarrow \frac{2c_2(1-x)^{3/4}x^{5/4}}{\sqrt{-(x-1)x}} + c_1(1-x)^{3/4}\sqrt[4]{x} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 25

$$\{y(x) = \_C1 x^{\frac{3}{4}}\sqrt[4]{x-1} + \_C2 \sqrt[4]{x}(x-1)^{\frac{3}{4}}\}$$

**3.391 ODE No. 1391**

$$\frac{d^2}{dx^2}y(x) = \frac{(7ax^2 + 5) \frac{d}{dx}y(x)}{x(ax^2 + 1)} - \frac{(15ax^2 + 5)y(x)}{x^2(ax^2 + 1)} = 0$$

**Mathematica:** cpu = 0.057507 (sec), leaf count = 27

$$\left\{ \left\{ y(x) \rightarrow c_1x^5 - \frac{1}{4}c_2x(2ax^2 + 1) \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 20

$$\{y(x) = \_C1 x^5 + \_C2 (2ax^3 + x)\}$$

**3.392 ODE No. 1392**

$$\frac{d^2}{dx^2}y(x) = -\frac{bx \frac{d}{dx}y(x)}{(x^2 - 1)a} - \frac{(cx^2 + dx + e)y(x)}{a(x^2 - 1)^2} = 0$$

**Mathematica:** cpu = 83.233069 (sec), leaf count = 1763961

Result too large for latex to process

**Maple:** cpu = 0.157 (sec), leaf count = 613

$$\left\{ y(x) = \_C1 \left( -\frac{1}{2} + \frac{x}{2} \right)^{\frac{1}{4a}(2a + \sqrt{4a^2 + (-4b - 4c - 4d - 4e)a + b^2})} (x^2 - 1)^{-\frac{b}{4a}} {}_2F_1\left(\frac{1}{4a}, \sqrt{4a^2 + (-4b - 4c - 4d - 4e)a + b^2}\right) \right\}$$

### 3.393 ODE No. 1393

$$\frac{d^2}{dx^2}y(x) = -\frac{(bx^2 + cx + d)y(x)}{ax^2(x-1)^2} = 0$$

**Mathematica:** cpu = 17.230188 (sec), leaf count = 413606

Result too large for latex to process

**Maple:** cpu = 0.110 (sec), leaf count = 299

$$\left\{ y(x) = \_C1 (x-1)^{-\frac{1}{2}(\sqrt{a-4b-4c-4d}-\sqrt{a})\frac{1}{\sqrt{a}}} x^{\frac{1}{2}(\sqrt{a}+\sqrt{a-4d})\frac{1}{\sqrt{a}}} {}_2F_1\left(-\frac{1}{2}\left(\sqrt{a-4b-4c-4d}-\sqrt{a}-\sqrt{a-4d}\right), \dots\right) \right.$$

### 3.394 ODE No. 1394

$$\frac{d^2}{dx^2}y(x) = -2\frac{\frac{d}{dx}y(x)}{x} - \frac{cy(x)}{x^2(ax+b)^2} = 0$$

**Mathematica:** cpu = 0.050506 (sec), leaf count = 115

$$\left\{ \left\{ y(x) \rightarrow c_1 \exp\left(\frac{\sqrt{c}\left(-\frac{\sqrt{b^2-4c}}{\sqrt{c}} - \frac{b}{\sqrt{c}}\right)(\log(x) - \log(ax+b))}{2b}\right) + c_2 \exp\left(\frac{\sqrt{c}\left(\frac{\sqrt{b^2-4c}}{\sqrt{c}} - \frac{b}{\sqrt{c}}\right)(\log(x) - \log(ax+b))}{2b}\right) \right. \right.$$

**Maple:** cpu = 0.078 (sec), leaf count = 89

$$\left\{ y(x) = \_C1 \sqrt{\frac{ax+b}{x}} \left(\frac{x}{ax+b}\right)^{\frac{a}{2b}\sqrt{\frac{b^2-4c}{a^2}}} + \_C2 \sqrt{\frac{ax+b}{x}} \left(\frac{x}{ax+b}\right)^{-\frac{a}{2b}\sqrt{\frac{b^2-4c}{a^2}}} \right\}$$

### 3.395 ODE No. 1395

$$\frac{d^2}{dx^2}y(x) = -\frac{y(x)}{(ax+b)^4} = 0$$

**Mathematica:** cpu = 0.160520 (sec), leaf count = 78

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{\sqrt{-\frac{1}{a^4}a}}{ax+b}}(ax+b) + \frac{c_2 e^{-\frac{\sqrt{-\frac{1}{a^4}a}}{ax+b}}(ax+b)}{2\sqrt{-\frac{1}{a^4}a^2}} \right. \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 43

$$\left\{ y(x) = \_C1 (ax+b) \sin\left(\frac{1}{a(ax+b)}\right) + \_C2 (ax+b) \cos\left(\frac{1}{a(ax+b)}\right) \right\}$$

**3.396 ODE No. 1396**

$$\frac{d^2}{dx^2}y(x) = -\frac{Ay(x)}{(ax^2 + bx + c)^2} = 0$$

**Mathematica:** cpu = 1.410179 (sec), leaf count = 211

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 \sqrt{ax^2 + bx + c} \exp\left(-\frac{\sqrt{4ac-b^2} \sqrt{1-\frac{4A}{b^2-4ac}} \tan^{-1}\left(\frac{2ax+b}{\sqrt{4ac-b^2}}\right)}{\sqrt{b^2-4ac}}\right)}{\sqrt{b^2-4ac} \sqrt{1-\frac{4A}{b^2-4ac}}} + c_1 \sqrt{x(ax+b)+c} \exp\left(\frac{\sqrt{4ac-b^2}}{\sqrt{b^2-4ac}}\right)} \right\} \right.$$

**Maple:** cpu = 0.109 (sec), leaf count = 189

$$\left\{ y(x) = \_C1 \sqrt{ax^2 + bx + c} \left(1 \left(i\sqrt{4ac - b^2} - 2ax - b\right) \left(2ax + b + i\sqrt{4ac - b^2}\right)^{-1}\right)^{\frac{a}{2} \sqrt{\frac{-4ac + b^2 - 4A}{a^2}} \frac{1}{\sqrt{-4ac - b^2}}}$$

**3.397 ODE No. 1397**

$$\frac{d^2}{dx^2}y(x) = -\frac{\frac{d}{dx}y(x)}{x^4} + \frac{y(x)}{x^5} = 0$$

**Mathematica:** cpu = 0.027003 (sec), leaf count = 38

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 \Gamma\left(\frac{1}{3}, -\frac{1}{3x^3}\right)}{3^{2/3} \sqrt[3]{-\frac{1}{x^3}}} + c_1 x \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 28

$$\left\{ y(x) = x\_C1 + \_C2 \left( \pi \sqrt{3} - \frac{3 \Gamma(2/3)}{2} \Gamma\left(\frac{1}{3}, -\frac{1}{3x^3}\right) \right) x \right\}$$

### 3.398 ODE No. 1398

$$\frac{d^2}{dx^2}y(x) = -\frac{(3x^2 - 1)\frac{d}{dx}y(x)}{x(x^2 - 1)} - \frac{(x^2 - 1 - (2v + 1)^2)y(x)}{(x^2 - 1)^2} = 0$$

**Mathematica:** cpu = 1.452684 (sec), leaf count = 88

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{x(x^2 - 4v^2 - 4v - 2)y(x) + (3x^4 - 4x^2 + 1)y'(x) + (x^5 - 2x^3 + x)\}) \right\} \right\}$$

**Maple:** cpu = 0.124 (sec), leaf count = 69

$$\left\{ y(x) = \_C1 (x^2 - 1)^{-\frac{1}{2}-v} {}_2F_1(-v, -v; -2v; -x^2 + 1) + \_C2 (x^2 - 1)^{v+\frac{1}{2}} {}_2F_1(v + 1, v + 1; 2 + 2v; -x^2 + 1) \right\}$$

### 3.399 ODE No. 1399

$$\frac{d^2}{dx^2}y(x) = \frac{(3x + 1)\frac{d}{dx}y(x)}{(1 + x)(x - 1)} - 36 \frac{(1 + x)^2 y(x)}{(x - 1)^2 (3x + 5)^2} = 0$$

**Mathematica:** cpu = 0.053507 (sec), leaf count = 72

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{1}{2}(3 \log(1-x) + \log(3x+5))} + \frac{1}{2} c_2 e^{\frac{1}{2}(3 \log(1-x) + \log(3x+5))} (3 \log(1-x) + \log(3x+5)) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 46

$$\left\{ y(x) = \_C1 \sqrt{3x + 5}(x - 1)^{\frac{3}{2}} + \_C2 \sqrt{3x + 5}(x - 1)^{\frac{3}{2}} (\ln(3x + 5) + 3 \ln(x - 1)) \right\}$$

### 3.400 ODE No. 1400

$$\frac{d^2}{dx^2}y(x) = \frac{\frac{d}{dx}y(x)}{x} - \frac{ay(x)}{x^6} = 0$$

**Mathematica:** cpu = 0.050506 (sec), leaf count = 60

$$\left\{ \left\{ y(x) \rightarrow c_1 x^2 e^{\frac{\sqrt{-a}}{2x^2}} + \frac{c_2 x^2 e^{-\frac{\sqrt{-a}}{2x^2}}}{2\sqrt{-a}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 37

$$\left\{ y(x) = \_C1 x^2 \sinh\left(\frac{1}{2x^2}\sqrt{-a}\right) + \_C2 x^2 \cosh\left(\frac{1}{2x^2}\sqrt{-a}\right) \right\}$$

### 3.401 ODE No. 1401

$$\frac{d^2}{dx^2}y(x) = -\frac{(3x^2 + a)\frac{d}{dx}y(x)}{x^3} - \frac{by(x)}{x^6} = 0$$

**Mathematica:** cpu = 0.013002 (sec), leaf count = 93

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-\frac{\sqrt{b}\left(-\frac{\sqrt{a^2-4b}}{\sqrt{b}} - \frac{a}{\sqrt{b}}\right)}{4x^2}} + c_2 e^{-\frac{\sqrt{b}\left(\frac{\sqrt{a^2-4b}}{\sqrt{b}} - \frac{a}{\sqrt{b}}\right)}{4x^2}} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 45

$$\left\{ y(x) = \_C1 e^{-\frac{1}{4x^2}(-a+\sqrt{a^2-4b})} + \_C2 e^{\frac{1}{4x^2}(a+\sqrt{a^2-4b})} \right\}$$

### 3.402 ODE No. 1402

$$\frac{d^2}{dx^2}y(x) = -\frac{((1-4a)x^2-1)\frac{d}{dx}y(x)}{x(x^2-1)} - \frac{\left((-v^2+x^2)(x^2-1)^2+4a(a+1)x^4-2ax^2(x^2-1)\right)y(x)}{x^2(x^2-1)^2} = 0$$

**Mathematica:** cpu = 4.464067 (sec), leaf count = 127

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{(x^6 + 4a^2x^4 - v^2x^4 + 2ax^4 - 2x^4 + 2v^2x^2 + 2ax^2 + x^2 - v^2)y(x) + \dots)\} \right\} \right\}$$

**Maple:** cpu = 0.218 (sec), leaf count = 69

$$\left\{ y(x) = \_C1 x^v (x^2 - 1)^a (x^2 - 1) \text{HeunC}\left(0, v, 1, \frac{1}{4}, \frac{a}{2} + \frac{1}{4}, x^2\right) + \_C2 x^{-v} (x^2 - 1)^a (x^2 - 1) \text{HeunC}\left(0, -v, 1, \frac{1}{4}, \frac{a}{2} + \frac{1}{4}, x^2\right) \right\}$$

### 3.403 ODE No. 1403

$$\frac{d^2}{dx^2}y(x) = -\left(\frac{1-a1-b1}{x-c1} + \frac{1-a2-b2}{x-c2} + \frac{1-a3-b3}{x-c3}\right)\frac{d}{dx}y(x) - \frac{y(x)}{(x-c1)(x-c2)(x-c3)}\left(\frac{a1}{x-c1} + \frac{a2}{x-c2} + \frac{a3}{x-c3}\right)$$

**Mathematica:** cpu = 97.102330 (sec), leaf count = 611

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{(c1-x)^2(c2-x)^2y''(x)(c3-x)^2 + (c1-x)(c2-x)(a1x^2 + a2x^2 + \dots)\} \right\} \right\}$$

**Maple:** cpu = 0.639 (sec), leaf count = 311

$$\left\{ y(x) = \_C1 \text{HeunG}\left(\frac{c1-c3}{c1-c2}, \frac{((-a3-2b1-b2+2)c1+(a3+b1-1)c2+c3(b1+b2-1))a1}{(c1-c2)}, \frac{c1-c3}{c1-c2}, x\right) \right\}$$

**3.404 ODE No. 1404**

$$\frac{d^2}{dx^2}y(x) = -\frac{(2x^2 + 1) \frac{d}{dx}y(x)}{x^3} - 1/4 \frac{(-2x^2 + 1)y(x)}{x^6} = 0$$

**Mathematica:** cpu = 0.023003 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{\frac{1}{4x^2}}}{x} + c_2 e^{\frac{1}{4x^2}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 24

$$\left\{ y(x) = \_C1 e^{\frac{1}{4x^2}} + \frac{\_C2}{x} e^{\frac{1}{4x^2}} \right\}$$

**3.405 ODE No. 1405**

$$\frac{d^2}{dx^2}y(x) = \frac{(2x^2 + 1) \frac{d}{dx}y(x)}{x^3} - 1/4 \frac{(ax^4 + 10x^2 + 1)y(x)}{x^6} = 0$$

**Mathematica:** cpu = 0.075510 (sec), leaf count = 77

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-\frac{1}{4x^2}} x^{\frac{3}{2} - \frac{\sqrt{9-a}}{2}} + \frac{c_2 e^{-\frac{1}{4x^2}} x^{\frac{\sqrt{9-a}}{2} + \frac{3}{2}}}{\sqrt{9-a}} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 47

$$\left\{ y(x) = \_C1 x^{\frac{3}{2} + \frac{1}{2}\sqrt{-a+9}} e^{-\frac{1}{4x^2}} + \_C2 x^{\frac{3}{2} - \frac{1}{2}\sqrt{-a+9}} e^{-\frac{1}{4x^2}} \right\}$$

**3.406 ODE No. 1406**

$$\frac{d^2}{dx^2}y(x) = -\frac{27xy(x)}{16(x^3 - 1)^2} = 0$$

**Mathematica:** cpu = 276.981672 (sec), leaf count = 257

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt{2}c_2(1-x)^{3/4} \sqrt[4]{x^2+x+1} \int_1^x \frac{\sqrt{\sqrt{3}K[1] + \sqrt{2K[1]-i\sqrt{3}+1}} \sqrt{2K[1]+i\sqrt{3}+1+\sqrt{3}}}{2(1-K[1])^{3/2} \sqrt{K[1]^2+K[1]+1}} dK[1]}{\sqrt[4]{\sqrt{3}x + \sqrt{2x - i\sqrt{3} + 1}} \sqrt{2x + i\sqrt{3} + 1 + \sqrt{3}}} + \frac{\sqrt{2}c_1}{\sqrt[4]{\sqrt{3}x + \sqrt{2x + i\sqrt{3} + 1 + \sqrt{3}}}} \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 53

$$\left\{ y(x) = \_C1 \sqrt{x} \sqrt[4]{x^3 - 1} \text{LegendreP}\left(-\frac{1}{6}, \frac{1}{3}, \sqrt{-x^3 + 1}\right) + \_C2 \sqrt{x} \sqrt[4]{x^3 - 1} \text{LegendreQ}\left(-\frac{1}{6}, \frac{1}{3}, \sqrt{-x^3 + 1}\right) \right\}$$



### 3.407 ODE No. 1407

$$\frac{d^2}{dx^2}y(x) = -\left(\frac{(1 - a1 - b1) b1}{b1 x - a1} + \frac{(1 - a2 - b2) b2}{b2 x - a2} + \frac{(1 - a3 - b3) b3}{b3 x - a3}\right) \frac{d}{dx}y(x) - \frac{1}{(b1 x - a1)(b2 x - a2)(b3 x - a3)}$$

**Mathematica:** cpu = 491.008850 (sec), leaf count = 842

{ {y(x) → DifferentialRoot({y, x}, {(a1 - xb1)<sup>2</sup>(a2 - xb2)<sup>2</sup>y''(x)(a3 - xb3)<sup>2</sup> + (a1 - xb1)(a2 - xb2)(a3 - xb3)}y'(x) - 1/((b1 x - a1)(b2 x - a2)(b3 x - a3))})

**Maple:** cpu = 2.074 (sec), leaf count = 2907

$$\left\{ y(x) = \_C1 \operatorname{HeunG}\left(\frac{b2(a1 b3 - a3 b1)}{b3(a1 b2 - b1 a2)}, -\frac{1}{4 b3(a1 b2 - b1 a2)}\left(\left((2 b2(a1 b3 - a3 b1) \sqrt{a1^2 + 6 a1 a2 + 6 a2^2} + 6 a1 a2 + 6 a2^2)\right)\right)\right)$$

### 3.408 ODE No. 1408

$$\frac{d^2}{dx^2}y(x) = -\frac{(x^2((x^2 - a1)(x^2 - a2) + (x^2 - a2)(x^2 - a3) + (x^2 - a3)(x^2 - a1)) - (x^2 - a1)(x^2 - a2)(x^2 - a3))}{x(x^2 - a1)(x^2 - a2)(x^2 - a3)}$$

**Mathematica:** cpu = 59.615570 (sec), leaf count = 98

{ {y(x) → DifferentialRoot({y, x}, {(A x<sup>2</sup> + B) y(x) + (2 x<sup>6</sup> - a1 x<sup>4</sup> - a2 x<sup>4</sup> - a3 x<sup>4</sup> + a1 a2 a3) y'(x) - x(a1 x<sup>2</sup> + a2 x<sup>2</sup> + a3 x<sup>2</sup>)})

**Maple:** cpu = 7.301 (sec), leaf count = 165

$$\left\{ y(x) = \operatorname{DESol}\left(\left(\frac{d^2}{dx^2} - Y(x) + \frac{(x^2((x^2 - a1)(x^2 - a2) + (x^2 - a2)(x^2 - a3) + (x^2 - a3)(x^2 - a1)) - (x^2 - a1)(x^2 - a2)(x^2 - a3))}{(x^2 - a1)(x^2 - a2)x(x^2 - a3)}\right)\right)$$

### 3.409 ODE No. 1409

$$\frac{d^2}{dx^2}y(x) = -\frac{ax^{2a-1} \frac{d}{dx}y(x)}{x^{2a}} - \frac{b^2 y(x)}{x^{2a}} = 0$$

**Mathematica:** cpu = 0.023003 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow c_1 \cos\left(\frac{bx^{1-a}}{a-1}\right) - c_2 \sin\left(\frac{bx^{1-a}}{a-1}\right) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 39

$$\left\{ y(x) = \_C1 \sin\left(\frac{x^{1-a}b}{a-1}\right) + \_C2 \cos\left(\frac{x^{1-a}b}{a-1}\right) \right\}$$

**3.410 ODE No. 1410**

$$\frac{d^2}{dx^2}y(x) = -\frac{(apx^b + q) \frac{d}{dx}y(x)}{x(ax^b - 1)} - \frac{(arx^b + s)y(x)}{x^2(ax^b - 1)} = 0$$

**Mathematica:** cpu = 0.132017 (sec), leaf count = 481

$$\left\{ \left\{ y(x) \rightarrow c_1 i^{-\frac{\sqrt{q^2+2q+4s+1}+q+1}{b}} a^{-\frac{\sqrt{q^2+2q+4s+1}+q+1}{2b}} (x^b)^{-\frac{\sqrt{q^2+2q+4s+1}+q+1}{2b}} {}_2F_1\left(\frac{p}{2b} + \frac{q}{2b} - \frac{\sqrt{p^2 - 2p - 4r + 1}}{2b} - \right. \right. \right.$$

**Maple:** cpu = 0.187 (sec), leaf count = 253

$$\left\{ y(x) = \_C1 {}_2F_1\left(\frac{1}{2b}\left(p + q + \sqrt{q^2 + 2q + 4s + 1} + \sqrt{p^2 - 2p - 4r + 1}\right), \frac{1}{2b}\left(p + q + \sqrt{q^2 + 2q + 4s + 1} + \sqrt{p^2 - 2p - 4r + 1}\right), \right.$$

**3.411 ODE No. 1411**

$$\frac{d^2}{dx^2}y(x) = \frac{y(x)}{e^x + 1} = 0$$

**Mathematica:** cpu = 0.333542 (sec), leaf count = 42

$$\left\{ \left\{ y(x) \rightarrow c_1(e^{-x} + 1) + c_2 e^{-x}(e^x \log(e^x + 1) + \log(e^x + 1) + 1) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 27

$$\left\{ y(x) = (((e^x + 1)^{-1} + \ln(e^x + 1)) \_C1 + \_C2) (1 + (e^x)^{-1}) \right\}$$

**3.412 ODE No. 1412**

$$\frac{d^2}{dx^2}y(x) = \frac{\frac{d}{dx}y(x)}{x \ln(x)} + (\ln(x))^2 y(x) = 0$$

**Mathematica:** cpu = 0.015502 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow c_1 \cosh(x(\log(x) - 1)) + ic_2 \sinh(x(\log(x) - 1)) \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 27

$$\left\{ y(x) = \_C1 \sinh(x \ln(x) - x) + \_C2 \cosh(x \ln(x) - x) \right\}$$

### 3.413 ODE No. 1413

$$\frac{d^2}{dx^2}y(x) = \frac{\frac{d}{dx}y(x)}{x(\ln(x)-1)} - \frac{y(x)}{x^2(\ln(x)-1)} = 0$$

**Mathematica:** cpu = 0.346544 (sec), leaf count = 37

$$\text{DSolve}\left[y''(x) = \frac{y'(x)}{x(\log(x)-1)} - \frac{y(x)}{x^2(\log(x)-1)}, y(x), x\right]$$

**Maple:** cpu = 0.047 (sec), leaf count = 12

$$\{y(x) = x\_C1 + \_C2 \ln(x)\}$$

### 3.414 ODE No. 1414

$$\frac{d^2}{dx^2}y(x) = -\frac{(-a^2(\sinh(x))^2 - n(n-1))y(x)}{(\sinh(x))^2} = 0$$

**Mathematica:** cpu = 1.132144 (sec), leaf count = 231

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2(-1)^{\frac{1}{2}(-2n-1)+1} \tanh^2(x)^{\frac{1}{4}(-2n-1)+1} (\tanh^2(x)-1)^{\frac{1}{2}(\frac{a+n}{2}+\frac{1}{2}(a+n+1)+\frac{1}{2}(-2n-1)+1)-\frac{1}{2}} {}_2F_1\left(\frac{1}{2}(-2n-1), \frac{1}{2}(-2n-1), \frac{3}{2}(-2n-1), \frac{1}{\sqrt{\tanh(x)}}\right)}{\sqrt{\tanh(x)}} \right. \right.$$

**Maple:** cpu = 0.187 (sec), leaf count = 97

$$\left\{ y(x) = \_C1 (\sinh(x))^n {}_2F_1\left(-\frac{a}{2} + \frac{n}{2}, \frac{a}{2} + \frac{n}{2}; \frac{1}{2}; \frac{\cosh(2x)}{2} + \frac{1}{2}\right) + \_C2 (\sinh(x))^n (2 \cosh(2x) + 2)^{\frac{3}{4}n} \right.$$

### 3.415 ODE No. 1415

$$\frac{d^2}{dx^2}y(x) = -2 \frac{n \cosh(x) \frac{d}{dx}y(x)}{\sinh(x)} - (-a^2 + n^2) y(x) = 0$$

**Mathematica:** cpu = 0.841107 (sec), leaf count = 273

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2(-1)^{\frac{1}{2}(-2n-1)+1} \tanh^2(x)^{\frac{1}{4}(-2n-1)+1} (\tanh^2(x)-1)^{\frac{1}{2}(\frac{a+n}{2}+\frac{1}{2}(a+n+1)+\frac{1}{2}(-2n-1)+1)} {}_2F_1\left(\frac{1}{2}(-2n-1), \frac{1}{2}(-2n-1), \frac{3}{2}(-2n-1), \frac{1}{\sqrt{\tanh(x)}}\right)}{\sqrt{\tanh(x)}} \right. \right.$$

**Maple:** cpu = 0.109 (sec), leaf count = 43

$$\left\{ y(x) = \_C1 (\sinh(x))^{-n+\frac{1}{2}} \text{LegendreP}\left(a - \frac{1}{2}, n - \frac{1}{2}, \cosh(x)\right) + \_C2 (\sinh(x))^{-n+\frac{1}{2}} \text{LegendreQ}\left(a - \frac{1}{2}, n - \frac{1}{2}, \cosh(x)\right) \right.$$

### 3.416 ODE No. 1416

$$\frac{d^2}{dx^2}y(x) = -\frac{(2n+1)\cos(x)\frac{d}{dx}y(x)}{\sin(x)} - (v+n+1)(v-n)y(x) = 0$$

**Mathematica:** cpu = 0.215027 (sec), leaf count = 46

$$\left\{ \left\{ y(x) \rightarrow c_1 (\cos^2(x) - 1)^{-n/2} P_v^n(\cos(x)) + c_2 (\cos^2(x) - 1)^{-n/2} Q_v^n(\cos(x)) \right\} \right\}$$

**Maple:** cpu = 0.141 (sec), leaf count = 31

$$\{y(x) = \_C1 (\sin(x))^{-n} \text{LegendreP}(v, n, \cos(x)) + \_C2 (\sin(x))^{-n} \text{LegendreQ}(v, n, \cos(x))\}$$

### 3.417 ODE No. 1417

$$\frac{d^2}{dx^2}y(x) = -\frac{((\sin(x))^2 - \cos(x))\frac{d}{dx}y(x)}{\sin(x)} - y(x)(\sin(x))^2 = 0$$

**Mathematica:** cpu = 0.141518 (sec), leaf count = 52

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{\cos(x)}{2}} \cos\left(\frac{1}{2}\sqrt{3}\cos(x)\right) + c_2 e^{\frac{\cos(x)}{2}} \sin\left(\frac{1}{2}\sqrt{3}\cos(x)\right) \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 e^{\frac{\cos(x)}{2}} \sin\left(\frac{\sqrt{3}\cos(x)}{2}\right) + \_C2 e^{\frac{\cos(x)}{2}} \cos\left(\frac{\sqrt{3}\cos(x)}{2}\right) \right\}$$

### 3.418 ODE No. 1418

$$\frac{d^2}{dx^2}y(x) = -\frac{x\sin(x)\frac{d}{dx}y(x)}{\cos(x)x - \sin(x)} + \frac{y(x)\sin(x)}{\cos(x)x - \sin(x)} = 0$$

**Mathematica:** cpu = 1.249159 (sec), leaf count = 46

$$\text{DSolve}\left[y''(x) = \frac{y(x)\sin(x)}{x\cos(x) - \sin(x)} - \frac{x\sin(x)y'(x)}{x\cos(x) - \sin(x)}, y(x), x\right]$$

**Maple:** cpu = 13.588 (sec), leaf count = 60

$$\left\{ y(x) = \_C1 \sin(x) + \_C2 \sin(x) \int e^{\int \frac{-2(\cos(x))^3 x + 3\sin(x)(\cos(x))^2 - \sin(x)}{(\sin(x)\cos(x)x + (\cos(x))^2 - 1)\cos(x)} dx} \cos(x) dx \right\}$$

### 3.419 ODE No. 1419

$$\frac{d^2}{dx^2}y(x) = -\frac{(x^2 \sin(x) - 2 \cos(x) x) \frac{d}{dx}y(x)}{x^2 \cos(x)} - \frac{(2 \cos(x) - x \sin(x)) y(x)}{x^2 \cos(x)} = 0$$

**Mathematica:** cpu = 1.177650 (sec), leaf count = 53

$$\text{DSolve}\left[y''(x) = -\frac{\sec(x)y'(x)(x^2 \sin(x) - 2x \cos(x))}{x^2} - \frac{y(x) \sec(x)(2x \cos(x) - x \sin(x))}{x^2}, y(x), x\right]$$

**Maple:** cpu = 0.219 (sec), leaf count = 13

$$\{y(x) = x\_C1 + \_C2 x \sin(x)\}$$

### 3.420 ODE No. 1420

$$(\cos(x))^2 \frac{d^2}{dx^2}y(x) - (a(\cos(x))^2 + n(n-1)) y(x) = 0$$

**Mathematica:** cpu = 0.435055 (sec), leaf count = 134

$$\left\{ \left\{ y(x) \rightarrow c_1 i^{1-n} \cos^{1-n}(x) {}_2F_1\left(-\frac{n}{2} - \frac{i\sqrt{a}}{2} + \frac{1}{2}, -\frac{n}{2} + \frac{i\sqrt{a}}{2} + \frac{1}{2}; \frac{3}{2} - n; \cos^2(x)\right) + c_2 i^n \cos^n(x) {}_2F_1\left(\frac{n}{2}\right. \right.$$

**Maple:** cpu = 0.218 (sec), leaf count = 123

$$\left. \left\{ y(x) = \_C1 \sin(2x) (\cos(x))^{-n} {}_2F_1\left(1 + \frac{i}{2}\sqrt{a} - \frac{n}{2}, 1 - \frac{i}{2}\sqrt{a} - \frac{n}{2}; \frac{3}{2} - n; \frac{\cos(2x)}{2} + \frac{1}{2}\right) + \_C2 (\cos(x))^n \right\} \right\}$$

### 3.421 ODE No. 1421

$$\frac{d^2}{dx^2}y(x) = -\frac{a(n-1) \sin(2ax) \frac{d}{dx}y(x)}{(\cos(ax))^2} - \frac{na^2((n-1) (\sin(ax))^2 + (\cos(ax))^2) y(x)}{(\cos(ax))^2} = 0$$

**Mathematica:** cpu = 0.248031 (sec), leaf count = 67

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-\sqrt{-a^2}x} \cos^{n-1}(ax) + \frac{c_2 e^{\sqrt{-a^2}x} \cos^{n-1}(ax)}{2\sqrt{-a^2}} \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 27

$$\{y(x) = \_C1 (\cos(ax))^n + \_C2 (\cos(ax))^{n-1} \sin(ax)\}$$

### 3.422 ODE No. 1422

$$\frac{d^2}{dx^2}y(x) = 2 \frac{y(x)}{(\sin(x))^2} = 0$$

**Mathematica:** cpu = 0.086011 (sec), leaf count = 64

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 \cos(x)}{\sqrt{\cos^2(x) - 1}} + \frac{c_2 \left( \cos(x) \log \left( \sqrt{\cos^2(x) - 1} + \cos(x) \right) - \sqrt{\cos^2(x) - 1} \right)}{\sqrt{\cos^2(x) - 1}} \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 57

$$\left\{ y(x) = \frac{-C1 \sin(2x)}{\cos(2x) - 1} + \frac{-C2 (-i \ln(\cos(2x) + i \sin(2x)) \sin(2x) + 2 \cos(2x) - 2)}{\cos(2x) - 1} \right\}$$

### 3.423 ODE No. 1423

$$\frac{d^2}{dx^2}y(x) = -\frac{ay(x)}{(\sin(x))^2} = 0$$

**Mathematica:** cpu = 0.072009 (sec), leaf count = 70

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt[4]{\cos^2(x) - 1} P_{-\frac{1}{2}}^{\frac{1}{2}\sqrt{1-4a}}(\cos(x)) + c_2 \sqrt[4]{\cos^2(x) - 1} Q_{-\frac{1}{2}}^{\frac{1}{2}\sqrt{1-4a}}(\cos(x)) \right\} \right\}$$

**Maple:** cpu = 0.203 (sec), leaf count = 165

$$\left\{ y(x) = -C1 \sqrt[4]{2 \cos(2x) + 2} {}_2F_1\left(\frac{1}{4}\sqrt{1-4a} + \frac{1}{4}, \frac{1}{4}\sqrt{1-4a} + \frac{1}{4}; \frac{1}{2}; \frac{\cos(2x)}{2} + \frac{1}{2}\right) \sqrt{-2 \cos(2x) + 2} \right\}$$

### 3.424 ODE No. 1424

$$(\sin(x))^2 \frac{d^2}{dx^2}y(x) - (a(\sin(x))^2 + n(n-1))y(x) = 0$$

**Mathematica:** cpu = 0.171022 (sec), leaf count = 90

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt[4]{\cos^2(x) - 1} P_{\frac{1}{2}(2n-1)}^{\frac{1}{2}(2n-1)}(\cos(x)) + c_2 \sqrt[4]{\cos^2(x) - 1} Q_{\frac{1}{2}(2n-1)}^{\frac{1}{2}(2n-1)}(\cos(x)) \right\} \right\}$$

**Maple:** cpu = 0.203 (sec), leaf count = 125

$$\left\{ y(x) = -C1 \left( \frac{\cos(2x)}{2} - \frac{1}{2} \right)^{\frac{n}{2}} {}_2F_1\left(\frac{n}{2} + \frac{i}{2}\sqrt{a}, \frac{n}{2} - \frac{i}{2}\sqrt{a}; \frac{1}{2}; \frac{\cos(2x)}{2} + \frac{1}{2}\right) + -C2 (2 \cos(2x) + 2)^{\frac{3}{4}} {}_2F_1\left(\frac{n}{2} + \frac{i}{2}\sqrt{a}, \frac{n}{2} - \frac{i}{2}\sqrt{a}; \frac{1}{2}; \frac{\cos(2x)}{2} + \frac{1}{2}\right) \right\}$$

**3.425 ODE No. 1425**

$$\frac{d^2}{dx^2}y(x) = -\frac{(-a^2(\cos(x))^2 - (3 - 2a)\cos(x) - 3 + 3a)y(x)}{(\sin(x))^2} = 0$$

**Mathematica:** cpu = 0.726092 (sec), leaf count = 232

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2(1 - \cos(x))^{\frac{1}{2}-a} \left( -\frac{(2a-1)(\cos(x)+1)}{-2a\cos(x)+\cos(x)+2} \right)^{a+\frac{1}{2}} (-2a\cos(x) + \cos(x) + 2) \left( \frac{(2a-1)(\cos(x)-1)}{(2a-1)\cos(x)-2} \right)^{a-\frac{1}{2}}}{\dots} \right. \right.$$

**Maple:** cpu = 0.312 (sec), leaf count = 99

$$\left\{ y(x) = \_C1 (-2 + (2a - 1)\cos(x)) \sqrt[4]{2\cos(x) + 2} (\sin(x))^{a-\frac{1}{2}} (-2\cos(x) + 2)^{-\frac{3}{4}} + \_C2 {}_2F_1\left(a - \frac{1}{2}, \dots\right) \right.$$

**3.426 ODE No. 1426**

$$(\sin(x))^2 \frac{d^2}{dx^2}y(x) - \left( a^2(\cos(x))^2 + b\cos(x) + \frac{b^2}{(2a-3)^2} + 3a + 2 \right) y(x) = 0$$

**Mathematica:** cpu = 6.105275 (sec), leaf count = 4128

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1(\cos(x) + 1)^{\frac{1}{2}} \left( -\frac{8a^2}{-16a^2+48a-36} + \frac{24a}{-16a^2+48a-36} + a - \frac{-32a^2+96a+\sqrt{(32a^2-96a+72)^2-4(-16a^2+48a-36)(16a^4+16ba^2-88a^2-36)}}{2(-16a^2+48a-36)} \right)}{\dots} \right. \right.$$

**Maple:** cpu = 0.390 (sec), leaf count = 599

$$\left\{ y(x) = \_C1 \left( \frac{\cos(x)}{2} - \frac{1}{2} \right)^{\frac{1}{8a-12}} \left( 4a-6+\sqrt{4b^2+16(a-3/2)^2b+16a^4-72a^2+81} \right) {}_2F_1\left(\frac{1}{8a-12}, \dots\right)$$

**3.427 ODE No. 1427**

$$\frac{d^2}{dx^2}y(x) = -\frac{-(a^2b^2 - (a+1)^2)(\sin(x))^2 - a(a+1)b\sin(2x) - a(a-1)y(x)}{(\sin(x))^2} = 0$$

**Mathematica:** cpu = 200.592472 (sec), leaf count = 57

DSolve[y''(x) = y(x) (-csc^2(x)) (-a^2b^2 - (a+1)^2) sin^2(x) - a(a+1)b sin(2x) + (1-a)a, y(x), x]

**Maple:** cpu = 1.107 (sec), leaf count = 262

$$\left\{ y(x) = \_C1 e^{\int \frac{1}{\sin(2x)(\sin(2x)b + \cos(2x)+1)} (2b((a+1)\cos(2x)+a+1/2)\sin(2x) - (\cos(2x)+1)((ab^2-a-2)\cos(2x)-ab^2-a+1)) dx} \sqrt{\sin(x)} \right\}$$

**3.428 ODE No. 1428**

$$\frac{d^2}{dx^2}y(x) = -\frac{(a(\cos(x))^2 + b(\sin(x))^2 + c)y(x)}{(\sin(x))^2} = 0$$

**Mathematica:** cpu = 0.392050 (sec), leaf count = 104

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt[4]{\cos^2(x) - 1} P_{\frac{1}{2}}^{\frac{1}{2}\sqrt{-4a-4c+1}}(\cos(x)) + c_2 \sqrt[4]{\cos^2(x) - 1} Q_{\frac{1}{2}}^{\frac{1}{2}\sqrt{-4a-4c+1}}(\cos(x)) \right\} \right\}$$

**Maple:** cpu = 0.218 (sec), leaf count = 219

$$\left\{ y(x) = \_C1 \sqrt[4]{2\cos(2x) + 2} {}_2F_1\left(\frac{1}{4}\sqrt{-4a+1-4c} + \frac{1}{2}\sqrt{-a+b} + \frac{1}{4}, \frac{1}{4}\sqrt{-4a+1-4c} - \frac{1}{2}\sqrt{-a+b} \right) \right\}$$

**3.429 ODE No. 1429**

$$\frac{d^2}{dx^2}y(x) = -\frac{\cos(x) \frac{d}{dx}y(x)}{\sin(x)} + \frac{y(x)}{(\sin(x))^2} = 0$$

**Mathematica:** cpu = 0.056507 (sec), leaf count = 51

$$\left\{ \left\{ y(x) \rightarrow c_1 \cosh\left(\log\left(\cos\left(\frac{x}{2}\right)\right) - \log\left(\sin\left(\frac{x}{2}\right)\right)\right) - ic_2 \sinh\left(\log\left(\cos\left(\frac{x}{2}\right)\right) - \log\left(\sin\left(\frac{x}{2}\right)\right)\right) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 25

$$\left\{ y(x) = \frac{\sin(x) \_C1}{-1 + \cos(x)} + \frac{(-1 + \cos(x)) \_C2}{\sin(x)} \right\}$$



**3.430 ODE No. 1430**

$$\frac{d^2}{dx^2}y(x) = -\frac{\cos(x) \frac{d}{dx}y(x)}{\sin(x)} - \frac{(v(v+1)(\sin(x))^2 - n^2)y(x)}{(\sin(x))^2} = 0$$

**Mathematica:** cpu = 0.452557 (sec), leaf count = 22

$$\{ \{ y(x) \rightarrow c_1 P_v^n(\cos(x)) + c_2 Q_v^n(\cos(x)) \} \}$$

**Maple:** cpu = 0.250 (sec), leaf count = 122

$$\left\{ y(x) = \_C1 \sin(2x) \left( \frac{\cos(2x)}{2} - \frac{1}{2} \right)^{\frac{n}{2}} {}_2F_1\left(1 + \frac{v}{2} + \frac{n}{2}, \frac{1}{2} - \frac{v}{2} + \frac{n}{2}; \frac{3}{2}; \frac{\cos(2x)}{2} + \frac{1}{2}\right) \frac{1}{\sqrt{1 - \cos(2x)}} + \right.$$

**3.431 ODE No. 1431**

$$\frac{d^2}{dx^2}y(x) = \frac{\cos(2x) \frac{d}{dx}y(x)}{\sin(2x)} - 2y(x) = 0$$

**Mathematica:** cpu = 0.202526 (sec), leaf count = 80

$$\left\{ \left\{ y(x) \rightarrow c_1 \left( \cos^2(x) - \frac{1}{2} \right) - \frac{2}{3} c_2 \cos^{\frac{3}{2}}(x) \left( 2 \cos^2(x) {}_2F_1\left(\frac{1}{4}, \frac{3}{4}; \frac{7}{4}; \cos^2(x)\right) - {}_2F_1\left(\frac{1}{4}, \frac{3}{4}; \frac{7}{4}; \cos^2(x)\right) \right) + \right.$$

**Maple:** cpu = 0.156 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 (\sin(2x))^{\frac{3}{4}} \text{LegendreP}\left(\frac{1}{4}, \frac{3}{4}, \cos(2x)\right) + \_C2 (\sin(2x))^{\frac{3}{4}} \text{LegendreQ}\left(\frac{1}{4}, \frac{3}{4}, \cos(2x)\right) \right\}$$

**3.432 ODE No. 1432**

$$\frac{d^2}{dx^2}y(x) = -\frac{\cos(x) \frac{d}{dx}y(x)}{\sin(x)} - 1/4 \frac{(-17(\sin(x))^2 - 1)y(x)}{(\sin(x))^2} = 0$$

**Mathematica:** cpu = 0.090511 (sec), leaf count = 37

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{-2x}}{\sqrt{\sin(x)}} + \frac{c_2 e^{2x}}{4\sqrt{\sin(x)}} \right\} \right\}$$

**Maple:** cpu = 0.046 (sec), leaf count = 25

$$\left\{ y(x) = \_C1 \sinh(2x) \frac{1}{\sqrt{\sin(x)}} + \_C2 \cosh(2x) \frac{1}{\sqrt{\sin(x)}} \right\}$$

### 3.433 ODE No. 1433

$$\frac{d^2}{dx^2}y(x) = -\frac{\sin(x) \frac{d}{dx}y(x)}{\cos(x)} - 1/4 \frac{(2x^2 + x^2(\sin(x))^2 - 24(\cos(x))^2) y(x)}{x^2(\cos(x))^2} + \sqrt{\cos(x)} = 0$$

**Mathematica:** cpu = 0.200525 (sec), leaf count = 46

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{5} c_2 x^3 \sqrt{\cos(x)} + \frac{c_1 \sqrt{\cos(x)}}{x^2} - \frac{1}{4} x^2 \sqrt{\cos(x)} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 32

$$\left\{ y(x) = \frac{C2}{x^2} \sqrt{\cos(x)} + \sqrt{\cos(x)} x^3 - C1 - \frac{x^2}{4} \sqrt{\cos(x)} \right\}$$

### 3.434 ODE No. 1434

$$\frac{d^2}{dx^2}y(x) = -\frac{b \cos(x) \frac{d}{dx}y(x)}{\sin(x) a} - \frac{(c(\cos(x))^2 + d \cos(x) + e) y(x)}{a(\sin(x))^2} = 0$$

**Mathematica:** cpu = 99.286108 (sec), leaf count = 1596424

Result too large for latex to process

**Maple:** cpu = 0.936 (sec), leaf count = 559

$$\left\{ y(x) = \_C1 (\sin(x))^{-\frac{a+b}{2a}} (\cos(x) + 1)^{\frac{1}{4a} (2a + \sqrt{a^2 + (-2b-4c-4d-4e)a+b^2})} (-1 + \cos(x))^{-\frac{1}{4a} (-2a + \sqrt{a^2 + (-2b-4c-4d-4e)a+b^2})} \right\}$$

### 3.435 ODE No. 1435

$$\frac{d^2}{dx^2}y(x) = -4 \frac{\sin(3x) y(x)}{(\sin(x))^3} = 0$$

**Mathematica:** cpu = 0.137517 (sec), leaf count = 70

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt[4]{\cos^2(x)} - 1 P_{-\frac{1}{2}+4i}^{\frac{i\sqrt{47}}{2}}(\cos(x)) + c_2 \sqrt[4]{\cos^2(x)} - 1 Q_{-\frac{1}{2}+4i}^{\frac{i\sqrt{47}}{2}}(\cos(x)) \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 41

$$\left\{ y(x) = \_C1 \sqrt{\sin(x)} LegendreP\left(-\frac{1}{2} + 4i, \frac{i}{2} \sqrt{47}, \cos(x)\right) + \_C2 \sqrt{\sin(x)} LegendreQ\left(-\frac{1}{2} + 4i, \frac{i}{2} \sqrt{47}, \cos(x)\right) \right\}$$

**3.436 ODE No. 1436**

$$\frac{d^2}{dx^2}y(x) = -1/4 \frac{(4v(v+1)(\sin(x))^2 - (\cos(x))^2 + 2 - 4n^2)y(x)}{(\sin(x))^2} = 0$$

**Mathematica:** cpu = 0.540069 (sec), leaf count = 42

$$\left\{ \left\{ y(x) \rightarrow c_1 \sqrt[4]{\cos^2(x) - 1} P_v^n(\cos(x)) + c_2 \sqrt[4]{\cos^2(x) - 1} Q_v^n(\cos(x)) \right\} \right\}$$

**Maple:** cpu = 0.203 (sec), leaf count = 140

$$\left\{ y(x) = \_C1 \sqrt[4]{2 \cos(2x) + 2} {}_2F_1\left(-\frac{v}{2} + \frac{n}{2}, \frac{1}{2} + \frac{v}{2} + \frac{n}{2}; \frac{1}{2}; \frac{\cos(2x)}{2} + \frac{1}{2}\right) \left(\frac{\cos(2x)}{2} - \frac{1}{2}\right)^{\frac{n}{2}} \sqrt{-2 \cos(2x)} \right\}$$

**3.437 ODE No. 1437**

$$\frac{d^2}{dx^2}y(x) = \frac{(3(\sin(x))^2 + 1) \frac{d}{dx}y(x)}{\cos(x) \sin(x)} + \frac{y(x) (\sin(x))^2}{(\cos(x))^2} = 0$$

**Mathematica:** cpu = 0.240531 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow c_1 \cos^{\frac{\sqrt{13}}{2} - \frac{3}{2}}(x) + c_2 \cos^{-\frac{3}{2} - \frac{\sqrt{13}}{2}}(x) \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 29

$$\left\{ y(x) = \_C1 (\cos(x))^{-\frac{3}{2} + \frac{\sqrt{13}}{2}} + \_C2 (\cos(x))^{-\frac{3}{2} - \frac{\sqrt{13}}{2}} \right\}$$

**3.438 ODE No. 1438**

$$\frac{d^2}{dx^2}y(x) = -\frac{(-a(\cos(x))^2 (\sin(x))^2 - m(m-1)(\sin(x))^2 - n(n-1)(\cos(x))^2)y(x)}{(\cos(x))^2 (\sin(x))^2} = 0$$

**Mathematica:** cpu = 0.940119 (sec), leaf count = 615

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 (-1)^{\frac{1}{2}(-2m-1)+1} \cos^2(x)^{\frac{1}{4}(-2m-1)+1} (\cos^2(x) - 1)^{\frac{1}{2} \left( \frac{4am+4\sqrt{-an^2+4an-4\sqrt{-an}+4(-a)^{3/2}+8\sqrt{-aa+\sqrt{-a}+4mn}}{8a+8n^2-8n+2} \right)}}{\dots} \right\} \right\}$$

**Maple:** cpu = 0.141 (sec), leaf count = 105

$$\left\{ y(x) = \_C1 (\cos(x))^m (\sin(x))^n {}_2F_1\left(\frac{n}{2} + \frac{m}{2} + \frac{i}{2}\sqrt{a}, \frac{n}{2} + \frac{m}{2} - \frac{i}{2}\sqrt{a}; \frac{1}{2} + m; (\cos(x))^2\right) + \_C2 (\cos(x)) \right\}$$

### 3.439 ODE No. 1439

$$\frac{d^2}{dx^2}y(x) = \frac{\left(\frac{d}{dx}\phi(x)\right) \frac{d}{dx}y(x)}{\phi(x) - \phi(a)} - \frac{(-n(n+1)(\phi(x) - \phi(a))^2 + (D^{(2)}(\phi)(a))y(x))}{\phi(x) - \phi(a)} = 0$$

**Mathematica:** cpu = 0.765097 (sec), leaf count = 61

$$\text{DSolve}\left[y''(x) = \frac{\phi'(x)y'(x)}{\phi(x) - \phi(a)} - \frac{y(x)(\phi''(a) - n(n+1)(\phi(x) - \phi(a))^2)}{\phi(x) - \phi(a)}, y(x), x\right]$$

**Maple:** cpu = 0.671 (sec), leaf count = 69

$$\left\{y(x) = \text{DESol}\left(\left\{\frac{d^2}{dx^2}Y(x) - \frac{\left(\frac{d}{dx}\phi(x)\right) \frac{d}{dx}Y(x)}{\phi(x) - \phi(a)} + \frac{(-n(n+1)(\phi(x) - \phi(a))^2 + \frac{d^2}{da^2}\phi(a))Y(x)}{\phi(x) - \phi(a)}\right\}\right)\right\}$$

### 3.440 ODE No. 1440

$$\frac{d^2}{dx^2}y(x) = -\frac{\left(\phi(x^3) - \phi(x)\frac{d}{dx}\phi(x) - \frac{d^2}{dx^2}\phi(x)\right) \frac{d}{dx}y(x)}{\frac{d}{dx}\phi(x) + (\phi(x))^2} - \frac{\left(\left(\frac{d}{dx}\phi(x)\right)^2 - (\phi(x))^2 \frac{d}{dx}\phi(x) - \phi(x) \frac{d^2}{dx^2}\phi(x)\right)}{\frac{d}{dx}\phi(x) + (\phi(x))^2}$$

**Mathematica:** cpu = 0.890613 (sec), leaf count = 86

$$\text{DSolve}\left[y''(x) = -\frac{y'(x)(-\phi''(x) - \phi(x)\phi'(x) + \phi(x^3))}{\phi'(x) + \phi(x)^2} - \frac{y(x)(-\phi(x)\phi''(x) + \phi(x)^2(-\phi'(x)) + \phi'(x)^2)}{\phi'(x) + \phi(x)^2}, y\right]$$

**Maple:** cpu = 0.0 (sec), leaf count = 94

$$\left\{y(x) = \text{DESol}\left(\left\{\frac{\left(\left(\frac{d}{dx}\phi(x)\right)^2 - (\phi(x))^2 \frac{d}{dx}\phi(x) - \phi(x) \frac{d^2}{dx^2}\phi(x)\right)Y(x)}{\frac{d}{dx}\phi(x) + (\phi(x))^2} + \frac{\left(\phi(x^3) - \phi(x)\frac{d}{dx}\phi(x) - \frac{d^2}{dx^2}\phi(x)\right)Y(x)}{\frac{d}{dx}\phi(x) + (\phi(x))^2}\right\}\right)\right\}$$

### 3.441 ODE No. 1441

$$\frac{d^2}{dx^2}y(x) = \frac{2 \text{JacobiSN}(x, k) \text{JacobiCN}(x, k) \text{JacobiDN}(x, k) \frac{d}{dx}y(x) - 2(1 - 2(k^2 + 1)) \text{JacobiSN}(a, k)}{(\text{JacobiSN}(x, k))^2 - \text{JacobiSN}(a, k)}$$

**Mathematica:** cpu = 1.467186 (sec), leaf count = 105

$$\text{DSolve}\left[y''(x) = -\frac{y'(x)(-\text{cn}(x|k)\text{dn}(x|k) - 2\text{sn}(x|k))}{\text{sn}(x|k)^2 - \text{sn}(a|k)^2} - \frac{y(x)(6k^2\text{sn}(a|k)^4 - 4(k^2 + 1)\text{sn}(a|k)^2 + 2)}{\text{sn}(x|k)^2 - \text{sn}(a|k)^2}, y\right]$$

**Maple:** cpu = 340.784 (sec), leaf count = 85

$$\left\{y(x) = \text{DESol}\left(\left\{\frac{d^2}{dx^2}Y(x) - 2 \frac{\text{JacobiSN}(x, k) \text{JacobiCN}(x, k) \text{JacobiDN}(x, k) \frac{d}{dx}Y(x)}{(\text{JacobiSN}(x, k))^2 - \text{JacobiSN}(a, k)} - \frac{(-2 + 4k^2\text{sn}(a|k)^4 - 4(k^2 + 1)\text{sn}(a|k)^2 + 2)Y(x)}{\text{sn}(x|k)^2 - \text{sn}(a|k)^2}\right\}\right)\right\}$$

**3.442 ODE No. 1442**

$$\frac{d^2}{dx^2}y(x) = -\frac{x \frac{d}{dx}y(x)}{f(x)} + \frac{y(x)}{f(x)} = 0$$

**Mathematica:** cpu = 0.213027 (sec), leaf count = 28

$$\text{DSolve}\left[y''(x) = \frac{y(x)}{f(x)} - \frac{xy'(x)}{f(x)}, y(x), x\right]$$

**Maple:** cpu = 0.063 (sec), leaf count = 31

$$\left\{y(x) = \_C1 \int e^{\int \frac{1}{x} \left(-2 - \frac{x^2}{f(x)}\right) dx} dx + \_C2 x\right\}$$

**3.443 ODE No. 1443**

$$\frac{d^2}{dx^2}y(x) = -1/2 \frac{\left(\frac{d}{dx}f(x)\right) \frac{d}{dx}y(x)}{f(x)} - \frac{g(x)y(x)}{f(x)} = 0$$

**Mathematica:** cpu = 0.266534 (sec), leaf count = 36

$$\text{DSolve}\left[y''(x) = -\frac{f'(x)y'(x)}{2f(x)} - \frac{g(x)y(x)}{f(x)}, y(x), x\right]$$

**Maple:** cpu = 0.016 (sec), leaf count = 39

$$\left\{y(x) = \text{DESol}\left(\left\{\frac{g(x) \_Y(x)}{f(x)} + \frac{\left(\frac{d}{dx}f(x)\right) \frac{d}{dx} \_Y(x)}{2f(x)} + \frac{d^2}{dx^2} \_Y(x)\right\}, \{\_Y(x)\}\right)\right\}$$

**3.444 ODE No. 1444**

$$\frac{d^2}{dx^2}y(x) = \frac{a \left(\frac{d}{dx}f(x)\right) \frac{d}{dx}y(x)}{f(x)} - \frac{b(f(x))^{2a+1} y(x)}{f(x)} = 0$$

**Mathematica:** cpu = 1.510692 (sec), leaf count = 36

$$\text{DSolve}\left[y''(x) = -by(x)f(x)^{2a} - \frac{af'(x)y'(x)}{f(x)}, y(x), x\right]$$

**Maple:** cpu = 0.016 (sec), leaf count = 37

$$\left\{y(x) = \_C1 e^{\int i(f(x))^a \sqrt{b} dx} + \_C2 e^{-\int i(f(x))^a \sqrt{b} dx}\right\}$$

### 3.445 ODE No. 1445

$$\frac{d^2}{dx^2}y(x) = -\frac{\left(2f(x)\left(\frac{d}{dx}g(x)\right)^2g(x) - ((g(x))^2 - 1)\left(f(x)\frac{d^2}{dx^2}g(x) + 2\left(\frac{d}{dx}f(x)\right)\frac{d}{dx}g(x)\right)\right)\frac{d}{dx}y(x)}{f(x)\left(\frac{d}{dx}g(x)\right)\left((g(x))^2 - 1\right)} - \left(\frac{d}{dx}f(x)\right)\frac{d}{dx}y(x)$$

**Mathematica:** cpu = 1.326669 (sec), leaf count = 169

$$\text{DSolve}\left[y''(x) = -\frac{y'(x)(2f(x)g(x)g'(x)^2 - (g(x)^2 - 1)(2f'(x)g'(x) + f(x)g''(x)))}{f(x)(g(x)^2 - 1)g'(x)} - \frac{y(x)((g(x)^2 - 1)(f'(x)g'(x) + 2f(x)g''(x))}{f(x)(g(x)^2 - 1)g'(x)}, y(x)\right]$$

**Maple:** cpu = 0.203 (sec), leaf count = 21

$$\{y(x) = \_C1 \text{LegendreP}(v, g(x)) f(x) + \_C2 \text{LegendreQ}(v, g(x)) f(x)\}$$

### 3.446 ODE No. 1446

$$\frac{d^2}{dx^2}y(x) = -\frac{\frac{d}{dx}y(x)}{x} - \frac{(x-1)y(x)}{x^4} = 0$$

**Mathematica:** cpu = 0.022003 (sec), leaf count = 33

$$\left\{\left\{y(x) \rightarrow c_1 e^{-1/x} - c_2 e^{-1/x} \text{Ei}\left(\frac{2}{x}\right)\right\}\right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 28

$$\{y(x) = \_C1 e^{-x^{-1}} + \_C2 e^{-x^{-1}} \text{Ei}(1, -2x^{-1})\}$$

### 3.447 ODE No. 1447

$$\frac{d^2}{dx^2}y(x) = -\frac{\frac{d}{dx}y(x)}{x} - \frac{(-1-x)y(x)}{x^4} = 0$$

**Mathematica:** cpu = 0.020002 (sec), leaf count = 29

$$\left\{\left\{y(x) \rightarrow c_1 e^{\frac{1}{x}} - c_2 e^{\frac{1}{x}} \text{Ei}\left(-\frac{2}{x}\right)\right\}\right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 24

$$\{y(x) = \_C1 e^{x^{-1}} + \_C2 e^{x^{-1}} \text{Ei}(1, 2x^{-1})\}$$

**3.448 ODE No. 1448**

$$\frac{d^2}{dx^2}y(x) = -\frac{b^2y(x)}{(-a^2 + x^2)^2} = 0$$

**Mathematica:** cpu = 0.323041 (sec), leaf count = 149

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1(x-a)^{\frac{1}{2}}\sqrt{1-\frac{b^2}{a^2}} + \frac{1}{2}(a+x)^{\frac{1}{2}-\frac{1}{2}}\sqrt{1-\frac{b^2}{a^2}} - c_2(x-a)^{\frac{1}{2}-\frac{1}{2}}\sqrt{\frac{a^2-b^2}{a^2}}(a+x)^{\frac{1}{2}}\sqrt{\frac{a^2-b^2}{a^2} + \frac{1}{2}}}{2a\sqrt{\frac{a^2-b^2}{a^2}}} \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 87

$$\left\{ y(x) = \_C1 \sqrt{(a-x)(x+a)} \left( \frac{a-x}{x+a} \right)^{\frac{1}{2a}\sqrt{a^2-b^2}} + \_C2 \sqrt{(a-x)(x+a)} \left( \frac{a-x}{x+a} \right)^{-\frac{1}{2a}\sqrt{a^2-b^2}} \right\}$$

## 4 Kamke chapter 3. Linear third order

### 4.1 ODE No. 1449

$$\frac{d^3}{dx^3}y(x) - \lambda y(x) = 0$$

**Mathematica:** cpu = 0.017002 (sec), leaf count = 53

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{(-1)^{2/3} \sqrt[3]{\lambda} x} + c_2 e^{-\sqrt[3]{-1} \sqrt[3]{\lambda} x} + c_3 e^{\sqrt[3]{\lambda} x} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 53

$$\left\{ y(x) = \_C1 e^{(-\frac{1}{2} \sqrt[3]{\lambda} - \frac{i}{2} \sqrt{3} \sqrt[3]{\lambda}) x} + \_C2 e^{(-\frac{1}{2} \sqrt[3]{\lambda} + \frac{i}{2} \sqrt{3} \sqrt[3]{\lambda}) x} + \_C3 e^{\sqrt[3]{\lambda} x} \right\}$$

### 4.2 ODE No. 1450

$$\frac{d^3}{dx^3}y(x) + y(x) ax^3 - bx = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.171 (sec), leaf count = 2294

$$\left\{ y(x) = \int 1401400 bx^3 \left( 8 x^6 {}_0F_2 \left( ; \frac{11}{6}, \frac{13}{6}; -\frac{x^6 a}{216} \right) {}_0F_2 \left( ; 7/6, 4/3; -\frac{x^6 a}{216} \right) - 5 {}_0F_2 \left( ; 5/6, 7/6; -\frac{x^6 a}{216} \right) x^6 \right. \right.$$

### 4.3 ODE No. 1451

$$\frac{d^3}{dx^3}y(x) - ax^b y(x) = 0$$

**Mathematica:** cpu = 0.019502 (sec), leaf count = 168

$$\left\{ \left\{ y(x) \rightarrow (-1)^{\frac{1}{b+3}} (b+3)^{-\frac{3}{b+3}} c_2 x a^{\frac{1}{b+3}} {}_0F_2 \left( ; 1 - \frac{1}{b+3}, 1 + \frac{1}{b+3}; \frac{ax^{b+3}}{(b+3)^3} \right) + (-1)^{\frac{2}{b+3}} (b+3)^{-\frac{6}{b+3}} c_3 x^2 a^{\frac{2}{b+3}} \right. \right.$$

**Maple:** cpu = 0.093 (sec), leaf count = 114

$$\left\{ y(x) = \_C1 {}_0F_2 \left( ; \frac{b+2}{b+3}, \frac{b+1}{b+3}; \frac{x^{b+3} a}{(b+3)^3} \right) + \_C2 x {}_0F_2 \left( ; \frac{b+4}{b+3}, \frac{b+2}{b+3}; \frac{x^{b+3} a}{(b+3)^3} \right) + \_C3 x^2 {}_0F_2 \left( ; \frac{b+5}{b+3}, \frac{b+4}{b+3}; \frac{x^{b+3} a}{(b+3)^3} \right) \right\}$$



#### 4.4 ODE No. 1452

$$\frac{d^3}{dx^3}y(x) + 3 \frac{d}{dx}y(x) - 4y(x) = 0$$

**Mathematica:** cpu = 0.006001 (sec), leaf count = 54

$$\left\{ \left\{ y(x) \rightarrow c_3 e^x + c_1 e^{-x/2} \sin\left(\frac{\sqrt{15}x}{2}\right) + c_2 e^{-x/2} \cos\left(\frac{\sqrt{15}x}{2}\right) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 e^x + \_C2 e^{-\frac{x}{2}} \sin\left(\frac{\sqrt{15}x}{2}\right) + \_C3 e^{-\frac{x}{2}} \cos\left(\frac{\sqrt{15}x}{2}\right) \right\}$$

#### 4.5 ODE No. 1453

$$\frac{d^3}{dx^3}y(x) - a^2 \frac{d}{dx}y(x) - e^{2ax}(\sin(x))^2 = 0$$

**Mathematica:** cpu = 0.593075 (sec), leaf count = 128

$$\left\{ \left\{ y(x) \rightarrow \frac{e^{-ax}(-9(a^2 - 4)a^4 e^{3ax} \cos(2x) - 3(11a^2 - 4)a^3 e^{3ax} \sin(2x) + (9a^6 + 49a^4 + 56a^2 + 16)(12a^2 - 12a^3(9a^6 + 49a^4 + 56a^2 + 16))}{12a^3(9a^6 + 49a^4 + 56a^2 + 16)} \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 230

$$\left\{ y(x) = \frac{108 e^{ax} \_C2 a^8 - 108 e^{-ax} \_C1 a^8 + 108 \_C3 a^9 - 9 a^6 e^{2ax} \cos(2x) + 588 e^{ax} \_C2 a^6 - 588 e^{-ax} \_C1 a^6}{108 e^{ax} \_C2 a^8 - 108 e^{-ax} \_C1 a^8 + 108 \_C3 a^9 - 9 a^6 e^{2ax} \cos(2x) + 588 e^{ax} \_C2 a^6 - 588 e^{-ax} \_C1 a^6} \right\}$$

#### 4.6 ODE No. 1454

$$\frac{d^3}{dx^3}y(x) + 2ax \frac{d}{dx}y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.009001 (sec), leaf count = 79

$$\left\{ \left\{ y(x) \rightarrow c_1 \text{Ai}\left(\sqrt[3]{-\frac{1}{2}\sqrt{ax}}\right)^2 + c_3 \text{Bi}\left(\sqrt[3]{-\frac{1}{2}\sqrt{ax}}\right)^2 + c_2 \text{Ai}\left(\sqrt[3]{-\frac{1}{2}\sqrt{ax}}\right) \text{Bi}\left(\sqrt[3]{-\frac{1}{2}\sqrt{ax}}\right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 55

$$\left\{ y(x) = \_C1 \left( \text{Ai}\left(-\frac{2^{\frac{2}{3}}x}{2}\sqrt[3]{a}\right) \right)^2 + \_C2 \left( \text{Bi}\left(-\frac{2^{\frac{2}{3}}x}{2}\sqrt[3]{a}\right) \right)^2 + \_C3 \text{Ai}\left(-\frac{2^{\frac{2}{3}}x}{2}\sqrt[3]{a}\right) \text{Bi}\left(-\frac{2^{\frac{2}{3}}x}{2}\sqrt[3]{a}\right) \right\}$$

#### 4.7 ODE No. 1455

$$\frac{d^3}{dx^3}y(x) - x^2 \frac{d^2}{dx^2}y(x) + (a + b - 1)x \frac{d}{dx}y(x) - by(x) = 0$$

**Mathematica:** cpu = 0.028004 (sec), leaf count = 127

$$\left\{ \left\{ y(x) \rightarrow \sqrt[3]{-\frac{1}{3}} c_2 x {}_2F_2\left(\frac{1}{3} - \frac{a}{3}, \frac{1}{3} - \frac{b}{3}; \frac{2}{3}, \frac{4}{3}; \frac{x^3}{3}\right) + c_1 {}_2F_2\left(-\frac{a}{3}, -\frac{b}{3}; \frac{1}{3}, \frac{2}{3}; \frac{x^3}{3}\right) + \left(-\frac{1}{3}\right)^{2/3} c_3 x^2 {}_2F_2\left(\frac{2}{3}, \frac{4}{3}; \frac{5}{3}, \frac{7}{3}; \frac{x^3}{3}\right) \right\} \right.$$

**Maple:** cpu = 0.110 (sec), leaf count = 71

$$\left\{ y(x) = -C1 {}_2F_2\left(-\frac{a}{3}, -\frac{b}{3}; \frac{1}{3}, \frac{2}{3}; \frac{x^3}{3}\right) + -C2 x {}_2F_2\left(\frac{1}{3} - \frac{a}{3}, \frac{1}{3} - \frac{b}{3}; \frac{2}{3}, \frac{4}{3}; \frac{x^3}{3}\right) + -C3 x^2 {}_2F_2\left(-\frac{a}{3} + \frac{2}{3}, -\frac{b}{3} + \frac{2}{3}; \frac{4}{3}, \frac{6}{3}; \frac{x^3}{3}\right) \right.$$

#### 4.8 ODE No. 1456

$$\frac{d^3}{dx^3}y(x) + x^{2c-2} \frac{d}{dx}y(x) + (c-1)x^{2c-3}y(x) = 0$$

**Mathematica:** cpu = 0.034004 (sec), leaf count = 183

$$\left\{ \left\{ y(x) \rightarrow c_1 {}_1F_2\left(\frac{1}{2} - \frac{1}{2c}; 1 - \frac{1}{c}, 1 - \frac{1}{2c}; -\frac{x^{2c}}{4c^2}\right) + 4^{-1/c} c_3 c^{-2/c} (x^{2c})^{1/c} {}_1F_2\left(\frac{1}{2} + \frac{1}{2c}; 1 + \frac{1}{2c}, 1 + \frac{1}{c}; -\frac{x^{2c}}{4c^2}\right) \right\} \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 74

$$\left\{ y(x) = -C1 x \left( J_{\frac{1}{2c}}\left(\frac{x^c}{2c}\right) \right)^2 + -C2 x \left( Y_{\frac{1}{2c}}\left(\frac{x^c}{2c}\right) \right)^2 + -C3 x J_{\frac{1}{2c}}\left(\frac{x^c}{2c}\right) Y_{\frac{1}{2c}}\left(\frac{x^c}{2c}\right) \right\}$$

#### 4.9 ODE No. 1457

$$\frac{d^3}{dx^3}y(x) - 3(2 \text{WeierstrassP}(x, g2, g3) + a) \frac{d}{dx}y(x) + by(x) = 0$$

**Mathematica:** cpu = 0.020003 (sec), leaf count = 30

$$\text{DSolve}[-3y'(x)(a + 2\wp(x; g2, g3)) + by(x) + y^{(3)}(x) = 0, y(x), x]$$

**Maple:** cpu = 0.203 (sec), leaf count = 37

$$\left\{ y(x) = \text{DESol}\left(\left\{ \frac{d^3}{dx^3} - Y(x) + (-6 \text{WeierstrassP}(x, g2, g3) - 3a) \frac{d}{dx} - Y(x) + b - Y(x) \right\}, \{-Y(x)\}\right) \right\}$$

#### 4.10 ODE No. 1458

$$\frac{d^3}{dx^3}y(x) + (-n^2 + 1) \text{WeierstrassP}(x, g2, g3) \frac{d}{dx}y(x) + 1/2 ((-n^2 + 1) \text{WeierstrassPPrime}(x, g2, g3))$$

**Mathematica:** cpu = 0.018502 (sec), leaf count = 51

$$\text{DSolve}\left[\frac{1}{2}y(x) \left((1 - n^2) \wp'(x; g2, g3) - a\right) + (1 - n^2) y'(x)\wp(x; g2, g3) + y^{(3)}(x) = 0, y(x), x\right]$$

**Maple:** cpu = 0.218 (sec), leaf count = 59

$$\left\{y(x) = \text{DESol}\left(\left\{\frac{d^3}{dx^3}Y(x) + (-n^2 \text{WeierstrassP}(x, g2, g3) + \text{WeierstrassP}(x, g2, g3)) \frac{d}{dx}Y(x) + \right.\right.\right.$$

#### 4.11 ODE No. 1459

$$\frac{d^3}{dx^3}y(x) - (4n(n+1) \text{WeierstrassP}(x, g2, g3) + a) \frac{d}{dx}y(x) - 2n(n+1) \text{WeierstrassPPrime}(x, g2, g3)$$

**Mathematica:** cpu = 0.018002 (sec), leaf count = 43

$$\text{DSolve}\left[-y'(x)(a + 4n(n+1)\wp(x; g2, g3)) - 2n(n+1)y(x)\wp'(x; g2, g3) + y^{(3)}(x) = 0, y(x), x\right]$$

**Maple:** cpu = 0.297 (sec), leaf count = 41

$$\left\{y(x) = \left(\text{DESol}\left(\left\{\frac{d^2}{dx^2}Y(x) + \left(-n^2 \text{WeierstrassP}(x, g2, g3) - n \text{WeierstrassP}(x, g2, g3) - \frac{a}{4}\right) Y(x)\right.\right.\right.\right.$$

#### 4.12 ODE No. 1460

$$\frac{d^3}{dx^3}y(x) + (A \text{WeierstrassP}(x, g2, g3) + a) \frac{d}{dx}y(x) + B \text{WeierstrassPPrime}(x, g2, g3) y(x) = 0$$

**Mathematica:** cpu = 0.012502 (sec), leaf count = 34

$$\text{DSolve}\left[y'(x)(a + A\wp(x; g2, g3)) + By(x)\wp'(x; g2, g3) + y^{(3)}(x) = 0, y(x), x\right]$$

**Maple:** cpu = 0.219 (sec), leaf count = 39

$$\left\{y(x) = \text{DESol}\left(\left\{\frac{d^3}{dx^3}Y(x) + (A \text{WeierstrassP}(x, g2, g3) + a) \frac{d}{dx}Y(x) + B \text{WeierstrassPPrime}(x, g2, g3) Y(x)\right.\right.\right.$$

#### 4.13 ODE No. 1461

$$\frac{d^3}{dx^3}y(x) - (3k^2(\text{JacobiSN}(z, x))^2 + a) \frac{d}{dx}y(x) + (b + c(\text{JacobiSN}(z, x))^2 - 3k^2 \text{JacobiSN}(z, x) \text{JacobiC}(\dots))$$

**Mathematica:** cpu = 0.029504 (sec), leaf count = 55

$$\text{DSolve}[-y'(x) (a + 3k^2 \text{sn}(z|x)^2) + y(x) (b + c \text{sn}(z|x)^2 - 3k^2 \text{cn}(z|x) \text{dn}(z|x) \text{sn}(z|x)) + y^{(3)}(x) = 0, y(x), x]$$

**Maple:** cpu = 1.154 (sec), leaf count = 63

$$\left\{ y(x) = \text{DESol} \left( \left\{ \frac{d^3}{dx^3} Y(x) + (-3k^2(\text{JacobiSN}(z, x))^2 - a) \frac{d}{dx} Y(x) + (b + c(\text{JacobiSN}(z, x))^2 - 3k^2 \text{cn}(z|x) \text{dn}(z|x) \text{sn}(z|x)) Y(x) \right\}, \{Y(x)\} \right) \right\}$$

#### 4.14 ODE No. 1462

$$\frac{d^3}{dx^3}y(x) - (6k^2(\sin(x))^2 + a) \frac{d}{dx}y(x) + by(x) = 0$$

**Mathematica:** cpu = 0.022003 (sec), leaf count = 32

$$\text{DSolve}[-y'(x) (a + 6k^2 \sin^2(x)) + by(x) + y^{(3)}(x) = 0, y(x), x]$$

**Maple:** cpu = 1.264 (sec), leaf count = 40

$$\left\{ y(x) = \text{DESol} \left( \left\{ \frac{d^3}{dx^3} Y(x) + (-6k^2(\sin(x))^2 - a) \frac{d}{dx} Y(x) + b Y(x) \right\}, \{Y(x)\} \right) \right\}$$

#### 4.15 ODE No. 1463

$$\frac{d^3}{dx^3}y(x) + 2f(x) \frac{d}{dx}y(x) + \left( \frac{d}{dx}f(x) \right) y(x) = 0$$

**Mathematica:** cpu = 0.072509 (sec), leaf count = 26

$$\text{DSolve}[y(x)f'(x) + 2f(x)y'(x) + y^{(3)}(x) = 0, y(x), x]$$

**Maple:** cpu = 0.063 (sec), leaf count = 24

$$\left\{ y(x) = \left( \text{DESol} \left( \left\{ \frac{d^2}{dx^2} Y(x) + \frac{f(x) Y(x)}{2} \right\}, \{Y(x)\} \right) \right)^2 \right\}$$

#### 4.16 ODE No. 1464

$$\frac{d^3}{dx^3}y(x) - 2 \frac{d^2}{dx^2}y(x) - 3 \frac{d}{dx}y(x) + 10 y(x) = 0$$

**Mathematica:** cpu = 0.005501 (sec), leaf count = 34

$$\left\{ \left\{ y(x) \rightarrow c_3 e^{-2x} + c_1 e^{2x} \sin(x) + c_2 e^{2x} \cos(x) \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 27

$$\left\{ y(x) = \_C1 e^{-2x} + \_C2 e^{2x} \sin(x) + \_C3 e^{2x} \cos(x) \right\}$$

#### 4.17 ODE No. 1465

$$\frac{d^3}{dx^3}y(x) - 2 \frac{d^2}{dx^2}y(x) - a^2 \frac{d}{dx}y(x) + 2 a^2 y(x) - \sinh(x) = 0$$

**Mathematica:** cpu = 0.081010 (sec), leaf count = 95

$$\left\{ \left\{ y(x) \rightarrow \frac{e^{-x}(3a^2 e^{2x} - a^2 - 3e^{2x} - 12e^x \sinh(x) - 6e^x \cosh(x) + 1)}{6(a-2)(a+2)(a^2-1)} + c_1 e^{-ax} + c_3 e^{ax} + c_2 e^{2x} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 467

$$\left\{ y(x) = -\frac{6 \cosh((a-1)x) e^{ax} - 6 \cosh((a-1)x) e^{-ax} - 6 \sinh((a+1)x) e^{ax} - 6 \sinh((a+1)x) e^{-ax}}{6(a-2)(a+2)(a^2-1)} \right\}$$

#### 4.18 ODE No. 1466

$$\frac{d^3}{dx^3}y(x) - 3a \frac{d^2}{dx^2}y(x) + 3a^2 \frac{d}{dx}y(x) - a^3 y(x) - e^{ax} = 0$$

**Mathematica:** cpu = 0.018002 (sec), leaf count = 46

$$\left\{ \left\{ y(x) \rightarrow c_3 x^2 e^{ax} + c_2 x e^{ax} + c_1 e^{ax} + \frac{1}{6} x^3 e^{ax} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 36

$$\left\{ y(x) = \frac{x^3 e^{ax}}{6} + \_C1 e^{ax} + \_C2 e^{ax} x + \_C3 e^{ax} x^2 \right\}$$

#### 4.19 ODE No. 1467

$$\frac{d^3}{dx^3}y(x) + a2 \frac{d^2}{dx^2}y(x) + a1 \frac{d}{dx}y(x) + a0 y(x) = 0$$

**Mathematica:** cpu = 0.005001 (sec), leaf count = 84

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{x \text{Root}[\#1^3 + \#1^2 a2 + \#1 a1 + a0 \&, 1]} + c_2 e^{x \text{Root}[\#1^3 + \#1^2 a2 + \#1 a1 + a0 \&, 2]} + c_3 e^{x \text{Root}[\#1^3 + \#1^2 a2 + \#1 a1 + a0 \&, 3]} \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 644

$$\left\{ y(x) = \_C1 e^{-\frac{x}{12} \left( i \left( 36 a1 a2 - 108 a0 - 8 a2^3 + 12 \sqrt{12 a0 a2^3 - 3 a1^2 a2^2 - 54 a1 a2 a0 + 12 a1^3 + 81 a0^2} \right)^{\frac{2}{3}} \sqrt{3} - 4 i \sqrt{3} a2^2 + 12 i \sqrt{3} a1 + \dots \right)} \right\}$$

#### 4.20 ODE No. 1468

$$\frac{d^3}{dx^3}y(x) - 6x \frac{d^2}{dx^2}y(x) + 2(4x^2 + 2a - 1) \frac{d}{dx}y(x) - 8axy(x) = 0$$

**Mathematica:** cpu = 0.087011 (sec), leaf count = 57

$$\left\{ \left\{ y(x) \rightarrow c_2 H_{\frac{a}{2}}(x) {}_1F_1\left(-\frac{a}{4}; \frac{1}{2}; x^2\right) + c_1 H_{\frac{a}{2}}(x)^2 + c_3 {}_1F_1\left(-\frac{a}{4}; \frac{1}{2}; x^2\right)^2 \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 64

$$\left\{ y(x) = \_C1 \left( M\left(\frac{1}{2} - \frac{a}{4}, \frac{3}{2}, x^2\right) \right)^2 x^2 + \_C2 \left( U\left(\frac{1}{2} - \frac{a}{4}, \frac{3}{2}, x^2\right) \right)^2 x^2 + \_C3 M\left(\frac{1}{2} - \frac{a}{4}, \frac{3}{2}, x^2\right) x^2 \right\}$$

#### 4.21 ODE No. 1469

$$\frac{d^3}{dx^3}y(x) + 3ax \frac{d^2}{dx^2}y(x) + 3a^2x^2 \frac{d}{dx}y(x) + a^3x^3y(x) = 0$$

**Mathematica:** cpu = 0.027003 (sec), leaf count = 72

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-\frac{ax^2}{2}} + c_2 e^{-\frac{ax^2}{2} - \sqrt{3}\sqrt{ax}} + c_3 e^{\sqrt{3}\sqrt{ax} - \frac{ax^2}{2}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 37

$$\left\{ y(x) = e^{-\frac{ax^2}{2}} \left( \_C1 + \_C2 e^{\sqrt{3}\sqrt{ax}} + \_C3 e^{-\sqrt{3}\sqrt{ax}} \right) \right\}$$

#### 4.22 ODE No. 1470

$$\frac{d^3}{dx^3}y(x) - \left(\frac{d^2}{dx^2}y(x)\right) \sin(x) - 2 \cos(x) \frac{d}{dx}y(x) + y(x) \sin(x) - \ln(x) = 0$$

**Mathematica:** cpu = 75.667609 (sec), leaf count = 63

$$\left\{ \left\{ y(x) \rightarrow e^{-\cos(x)} \int_1^x \frac{1}{4} e^{\cos(K[1])} (4c_1 K[1] - 3K[1]^2 + 2K[1]^2 \log(K[1]) + 4c_2) dK[1] + c_3 e^{-\cos(x)} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 36

$$\left\{ y(x) = \left( -C3 + \int \left( 2x\_C1 + \_C2 + \frac{x^2 \ln(x)}{2} - \frac{3x^2}{4} \right) e^{\cos(x)} dx \right) e^{-\cos(x)} \right\}$$

#### 4.23 ODE No. 1471

$$\frac{d^3}{dx^3}y(x) + f(x) \frac{d^2}{dx^2}y(x) + \frac{d}{dx}y(x) + f(x)y(x) = 0$$

**Mathematica:** cpu = 0.080010 (sec), leaf count = 27

$$\text{DSolve}[f(x)y''(x) + f(x)y(x) + y^{(3)}(x) + y'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.156 (sec), leaf count = 36

$$\left\{ y(x) = e^{ix} \left( \int e^{-2ix} \left( \int -C3 e^{f-f(x)+ix} dx + \_C2 \right) dx + \_C1 \right) \right\}$$

#### 4.24 ODE No. 1472

$$\frac{d^3}{dx^3}y(x) + f(x) \left( x^2 \frac{d^2}{dx^2}y(x) - 2x \frac{d}{dx}y(x) + 2y(x) \right) = 0$$

**Mathematica:** cpu = 0.081010 (sec), leaf count = 34

$$\text{DSolve}[f(x) (x^2 y''(x) - 2x y'(x) + 2y(x)) + y^{(3)}(x) = 0, y(x), x]$$

**Maple:** cpu = 0.141 (sec), leaf count = 33

$$\left\{ y(x) = \left( \int -C1 + \_C2 \int e^{-\int x^2 f(x) + 3x^{-1} dx} dx dx + \_C3 \right) x \right\}$$

#### 4.25 ODE No. 1473

$$\frac{d^3}{dx^3}y(x) + f(x) \frac{d^2}{dx^2}y(x) + g(x) \frac{d}{dx}y(x) + \left( f(x)g(x) + \frac{d}{dx}g(x) \right) y(x) = 0$$

**Mathematica:** cpu = 0.012002 (sec), leaf count = 38

$$\text{DSolve}[y(x) (f(x)g(x) + g'(x)) + f(x)y''(x) + g(x)y'(x) + y^{(3)}(x) = 0, y(x), x]$$

**Maple:** cpu = 0.046 (sec), leaf count = 47

$$\left\{ y(x) = \text{DESol} \left( \left\{ \frac{d^3}{dx^3} Y(x) + f(x) \frac{d^2}{dx^2} Y(x) + g(x) \frac{d}{dx} Y(x) + \left( f(x)g(x) + \frac{d}{dx}g(x) \right) Y(x) \right\}, \{ \_Y(x) \} \right) \right\}, \{ \_Y(x) \}$$

#### 4.26 ODE No. 1474

$$\frac{d^3}{dx^3}y(x) + 3f(x) \frac{d^2}{dx^2}y(x) + \left( \frac{d}{dx}f(x) + 2(f(x))^2 + 4g(x) \right) \frac{d}{dx}y(x) + \left( 4f(x)g(x) + 2 \frac{d}{dx}g(x) \right) y(x) = 0$$

**Mathematica:** cpu = 0.015002 (sec), leaf count = 55

$$\text{DSolve}[y'(x) (f'(x) + 2f(x)^2 + 4g(x)) + y(x) (4f(x)g(x) + 2g'(x)) + 3f(x)y''(x) + y^{(3)}(x) = 0, y(x), x]$$

**Maple:** cpu = 0.110 (sec), leaf count = 30

$$\left\{ y(x) = \left( \text{DESol} \left( \left\{ \frac{d^2}{dx^2} Y(x) + f(x) \frac{d}{dx} Y(x) + g(x) Y(x) \right\}, \{ \_Y(x) \} \right) \right)^2 \right\}$$

#### 4.27 ODE No. 1475

$$4 \frac{d^3}{dx^3}y(x) - 8 \frac{d^2}{dx^2}y(x) - 11 \frac{d}{dx}y(x) - 3y(x) + 18e^x = 0$$

**Mathematica:** cpu = 0.021503 (sec), leaf count = 38

$$\{ \{ y(x) \rightarrow c_1 e^{-x/2} + c_2 e^{-x/2} x + c_3 e^{3x} + e^x \} \}$$

**Maple:** cpu = 0.015 (sec), leaf count = 26

$$\{ y(x) = e^x + \_C1 e^{3x} + \_C2 e^{-\frac{x}{2}} + \_C3 e^{-\frac{x}{2}} x \}$$



#### 4.28 ODE No. 1476

$$27 \frac{d^3}{dx^3} y(x) - 36 n^2 \text{WeierstrassP}(x, g2, g3) \frac{d}{dx} y(x) - 2 n(n+3) (4n-3) \text{WeierstrassPPrime}(x, g2, g3)$$

**Mathematica:** cpu = 0.128516 (sec), leaf count = 44

$$\text{DSolve}[-36n^2 y'(x) \wp(x; g2, g3) - 2(n+3)(4n-3)ny(x)\wp'(x) + 27y^{(3)}(x) = 0, y(x), x]$$

**Maple:** cpu = 0.234 (sec), leaf count = 62

$$\left\{ y(x) = \text{DESol} \left( \left\{ 27 \frac{d^3}{dx^3} Y(x) - 36 n^2 \text{WeierstrassP}(x, g2, g3) \frac{d}{dx} Y(x) + (-8 \text{WeierstrassPPrime}(x, g2, g3)) \right\} \right) \right\}$$

#### 4.29 ODE No. 1477

$$x \frac{d^3}{dx^3} y(x) + 3 \frac{d^2}{dx^2} y(x) + xy(x) = 0$$

**Mathematica:** cpu = 0.170522 (sec), leaf count = 48

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{-x}}{x} + \frac{c_2 e^{\sqrt[3]{-1}x}}{x} + \frac{c_3 e^{-(-1)^{2/3}x}}{x} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 41

$$\left\{ y(x) = \frac{1}{x} \left( -C1 e^{-x} + -C2 e^{\frac{x}{2}} \sin \left( \frac{\sqrt{3}x}{2} \right) + -C3 e^{\frac{x}{2}} \cos \left( \frac{\sqrt{3}x}{2} \right) \right) \right\}$$

#### 4.30 ODE No. 1478

$$x \frac{d^3}{dx^3} y(x) + 3 \frac{d^2}{dx^2} y(x) - ax^2 y(x) = 0$$

**Mathematica:** cpu = 0.032004 (sec), leaf count = 104

$$\left\{ \left\{ y(x) \rightarrow -\frac{2(-1)^{3/4} \sqrt{2} c_1 {}_0F_2 \left( ; \frac{1}{2}, \frac{3}{4}; \frac{ax^4}{64} \right)}{\sqrt[4]{ax}} + c_2 {}_0F_2 \left( ; \frac{3}{4}, \frac{5}{4}; \frac{ax^4}{64} \right) + \frac{\sqrt[4]{-1} \sqrt[4]{a} c_3 x {}_0F_2 \left( ; \frac{5}{4}, \frac{3}{2}; \frac{ax^4}{64} \right)}{2\sqrt{2}} \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 48

$$\left\{ y(x) = -C1 {}_0F_2 \left( ; \frac{3}{4}, \frac{5}{4}; \frac{ax^4}{64} \right) + \frac{C2}{x} {}_0F_2 \left( ; \frac{1}{2}, \frac{3}{4}; \frac{ax^4}{64} \right) + -C3 x {}_0F_2 \left( ; \frac{5}{4}, \frac{3}{2}; \frac{ax^4}{64} \right) \right\}$$

### 4.31 ODE No. 1479

$$x \frac{d^3}{dx^3} y(x) + (a+b) \frac{d^2}{dx^2} y(x) - x \frac{d}{dx} y(x) - ay(x) = 0$$

**Mathematica:** cpu = 0.142518 (sec), leaf count = 153

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} i c_2 x {}_1F_2\left(\frac{a}{2} + \frac{1}{2}; \frac{3}{2}, \frac{a}{2} + \frac{b}{2} + \frac{1}{2}; \frac{x^2}{4}\right) + c_1 {}_1F_2\left(\frac{a}{2}; \frac{1}{2}, \frac{a}{2} + \frac{b}{2}; \frac{x^2}{4}\right) + c_3 \left(\frac{i}{2}\right)^{-a-b+2} x^{-a-b+2} {}_1F_2\left(\frac{a}{2}; \frac{1}{2}, \frac{a}{2} + \frac{b}{2}; \frac{x^2}{4}\right) \right\} \right.$$

**Maple:** cpu = 0.187 (sec), leaf count = 92

$$\left\{ y(x) = {}_1F_2\left(\frac{a}{2}; \frac{1}{2}, \frac{a}{2} + \frac{b}{2}; \frac{x^2}{4}\right) - C2 x {}_1F_2\left(\frac{1}{2} + \frac{a}{2}; \frac{3}{2}, \frac{a}{2} + \frac{b}{2} + \frac{1}{2}; \frac{x^2}{4}\right) - C3 x^{-a-b+2} {}_1F_2\left(1 - \frac{b}{2}; \frac{3}{2}, \frac{a}{2} + \frac{b}{2} + \frac{1}{2}; \frac{x^2}{4}\right) \right.$$

### 4.32 ODE No. 1480

$$x \frac{d^3}{dx^3} y(x) - (x+2v) \frac{d^2}{dx^2} y(x) - (x-2v-1) \frac{d}{dx} y(x) + (x-1)y(x) = 0$$

**Mathematica:** cpu = 0.210027 (sec), leaf count = 93

$$\left\{ \left\{ y(x) \rightarrow \frac{c_3 e^x x^{2v+2} \Gamma(v + \frac{3}{2}) {}_1\tilde{F}_1(v + \frac{3}{2}; 2v + 3; -2x)}{\Gamma(\frac{1}{2} - v)} + c_2 2^{-2v-2} e^x G_{2,3}^{2,1}\left(2x \left| \begin{matrix} 1, v + \frac{3}{2} \\ 1, 2(v+1), 0 \end{matrix} \right. \right) + c_1 e^x \right\} \right.$$

**Maple:** cpu = 0.219 (sec), leaf count = 35

$$\left\{ y(x) = {}_1F_2\left(\frac{a}{2}; \frac{1}{2}, \frac{a}{2} + \frac{b}{2}; \frac{x^2}{4}\right) - C2 x {}_1F_2\left(\frac{1}{2} + \frac{a}{2}; \frac{3}{2}, \frac{a}{2} + \frac{b}{2} + \frac{1}{2}; \frac{x^2}{4}\right) - C3 x^{-a-b+2} {}_1F_2\left(1 - \frac{b}{2}; \frac{3}{2}, \frac{a}{2} + \frac{b}{2} + \frac{1}{2}; \frac{x^2}{4}\right) \right.$$

### 4.33 ODE No. 1481

$$x \frac{d^3}{dx^3} y(x) + (x^2 - 3) \frac{d^2}{dx^2} y(x) + 4x \frac{d}{dx} y(x) + 2y(x) - f(x) = 0$$

**Mathematica:** cpu = 0.985125 (sec), leaf count = 431

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{240} e^{-\frac{x^2}{2}} \left( -240x^5 \left( \int_1^x \left( \frac{1}{15} \sqrt{\frac{\pi}{2}} K[1] \operatorname{erfi}\left(\frac{K[1]}{\sqrt{2}}\right) f(K[1]) - \frac{1}{240} \left( 15 \operatorname{Ei}\left(\frac{K[1]^2}{2}\right) + 16 e^{\frac{K[1]^2}{2}} \right) \right) \right) \right.$$

**Maple:** cpu = 0.031 (sec), leaf count = 44

$$\left\{ y(x) = \left( -C3 + \int \frac{2x - C1 - C2 - \iint -f(x) dx dx}{x^6} e^{\frac{x^2}{2}} dx \right) e^{-\frac{x^2}{2}} x^5 \right.$$

#### 4.34 ODE No. 1482

$$2x \frac{d^3}{dx^3} y(x) + 3 \frac{d^2}{dx^2} y(x) + axy(x) - b = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.219 (sec), leaf count = 2292

$$\left\{ y(x) = \int 350350 bx \left( 8x^3 {}_0F_2 \left( ; 7/6, 4/3; -\frac{ax^3}{54} \right) {}_0F_2 \left( ; \frac{11}{6}, \frac{13}{6}; -\frac{ax^3}{54} \right) a - 5x^3 {}_0F_2 \left( ; 5/6, 7/6; -\frac{ax^3}{54} \right) {}_0F_2 \left( ; \frac{11}{6}, \frac{13}{6}; -\frac{ax^3}{54} \right) \right.$$

#### 4.35 ODE No. 1483

$$2x \frac{d^3}{dx^3} y(x) - 4(x + \nu - 1) \frac{d^2}{dx^2} y(x) + (2x + 6\nu - 5) \frac{d}{dx} y(x) + (1 - 2\nu) y(x) = 0$$

**Mathematica:** cpu = 0.148519 (sec), leaf count = 112

$$\left\{ \left\{ y(x) \rightarrow \frac{c_3 e^x x \Gamma\left(\frac{5}{2} - 3\nu\right) \left( \frac{{}_2F_1\left(\frac{3}{2} - 3\nu; 1 - 2\nu; -x\right)}{3(2\nu - 1)x} + \frac{2}{3x\Gamma(2 - 2\nu)} \right)}{\Gamma\left(\frac{3}{2} - \nu\right)} + c_2 e^x G_{2,3}^{2,1} \left( x \left| \begin{matrix} 1, 3\nu - \frac{1}{2} \\ 1, 2\nu, 0 \end{matrix} \right. \right) + c_1 e^x \right\} \right\}$$

**Maple:** cpu = 0.218 (sec), leaf count = 37

$$\left\{ y(x) = \_C1 e^x + \_C2 e^{\frac{x}{2}} x^\nu I_\nu \left( \frac{x}{2} \right) + \_C3 e^{\frac{x}{2}} x^\nu K_\nu \left( \frac{x}{2} \right) \right\}$$

#### 4.36 ODE No. 1484

$$2x \frac{d^3}{dx^3} y(x) + 3(2ax + k) \frac{d^2}{dx^2} y(x) + 6(ak + bx) \frac{d}{dx} y(x) + (3bk + 2cx) y(x) = 0$$

**Mathematica:** cpu = 63.307539 (sec), leaf count = 80

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{(2xc + 3bk)y(x) + (6xb + 6ak)y'(x) + (6xa + 3k)y''(x) + 2xy^{(3)}(x) = 0\}) \right\} \right\}$$

**Maple:** cpu = 0.296 (sec), leaf count = 62

$$\left\{ y(x) = \text{DESol} \left( \left\{ (3bk + 2cx) \_Y(x) + (6ak + 6bx) \frac{d}{dx} \_Y(x) + (6ax + 3k) \frac{d^2}{dx^2} \_Y(x) + 2x \frac{d^3}{dx^3} \_Y(x) = 0 \right\} \right)$$

### 4.37 ODE No. 1485

$$(x-2)x \frac{d^3}{dx^3}y(x) - (x-2)x \frac{d^2}{dx^2}y(x) - 2 \frac{d}{dx}y(x) + 2y(x) = 0$$

**Mathematica:** cpu = 0.119015 (sec), leaf count = 66

$$\left\{ \left\{ y(x) \rightarrow -\frac{c_3(4e^x \text{Ei}(2-x) - e^2(x^2 \log(2-x) - x^2 \log(x) + 2x + 2))}{4e^2} + c_1x^2 + c_2e^x \right\} \right\}$$

**Maple:** cpu = 0.297 (sec), leaf count = 47

$$\left\{ y(x) = \_C1 x^2 + \_C2 e^x + \_C3 \left( -\frac{x^2 \ln(x)}{4} + \frac{x^2 \ln(x-2)}{4} + \text{Ei}(1, x-2) e^{x-2} + \frac{x}{2} + \frac{1}{2} \right) \right\}$$

### 4.38 ODE No. 1486

$$(2x-1) \frac{d^3}{dx^3}y(x) - 8x \frac{d}{dx}y(x) + 8y(x) = 0$$

**Mathematica:** cpu = 0.168021 (sec), leaf count = 65

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4}c_3x \left( \frac{e^{2x-2}\text{Ei}(2-4x)}{x} - \frac{2\text{Ei}(1-2x)}{e} - \frac{e^{-2x}}{x} \right) + c_1x - c_2e^{2x} \right\} \right\}$$

**Maple:** cpu = 0.187 (sec), leaf count = 50

$$\left\{ y(x) = x\_C1 + \_C2 e^{2x} + \_C3 \left( -\frac{xe^{-1}\text{Ei}(1, 2x-1)}{2} + \frac{\text{Ei}(1, -2+4x)e^{2x-2}}{4} + \frac{e^{-2x}}{4} \right) \right\}$$

### 4.39 ODE No. 1487

$$(2x-1) \frac{d^3}{dx^3}y(x) + (x+4) \frac{d^2}{dx^2}y(x) + 2 \frac{d}{dx}y(x) = 0$$

**Mathematica:** cpu = 114.051983 (sec), leaf count = 86

$$\left\{ \left\{ y(x) \rightarrow \int_1^x \left( c_2 e^{-\frac{K[1]}{2}} L_{-\frac{1}{4}}^{\frac{5}{4}} \left( \frac{K[1]}{2} - \frac{1}{4} \right) + \frac{c_1 e^{-\frac{K[1]}{2}} \left( \frac{1}{4 \left( \frac{K[1]}{2} - \frac{1}{4} \right)} + 1 \right)}{\sqrt[4]{\frac{K[1]}{2} - \frac{1}{4}}} \right) dK[1] + c_3 \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 38

$$\left\{ y(x) = 1 \left( \_C3 + \int (2x\_C1 + \_C2) e^{\frac{x}{2}} (2x-1)^{-\frac{3}{4}} dx \right) e^{-\frac{x}{2}} \frac{1}{\sqrt[4]{2x-1}} \right\}$$

#### 4.40 ODE No. 1488

$$x^2 \frac{d^3}{dx^3} y(x) - 6 \frac{d}{dx} y(x) + ax^2 y(x) = 0$$

**Mathematica:** cpu = 0.546069 (sec), leaf count = 102

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{-\sqrt[3]{ax}} (\sqrt[3]{ax} + 2)}{x} + \frac{c_2 e^{\sqrt[3]{-1} \sqrt[3]{ax}} (\sqrt[3]{ax} + 2(-1)^{2/3})}{x} + \frac{c_3 e^{-(-1)^{2/3} \sqrt[3]{ax}} (\sqrt[3]{ax} - 2\sqrt[3]{-1})}{x} \right\} \right\}$$

**Maple:** cpu = 0.390 (sec), leaf count = 151

$$\left\{ y(x) = \frac{-C1}{x} \left( a^3 x + 2(-a^4)^{2/3} \right) e^{\frac{x}{a} \sqrt[3]{-a^4}} + \frac{C2}{x} \left( (-a^4)^{\frac{2}{3}} \sqrt{3} - ia^3 x + i(-a^4)^{\frac{2}{3}} \right) e^{\frac{i}{2} \frac{(-\sqrt{3}+i)x}{a} \sqrt[3]{-a^4}} + \frac{C3}{x} \right\}$$

#### 4.41 ODE No. 1489

$$x^2 \frac{d^3}{dx^3} y(x) + (1+x) \frac{d^2}{dx^2} y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.799102 (sec), leaf count = 54

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{y^{(3)}(x)x^2 - y(x) + (x+1)y''(x) = 0, y(1) = c_1, y'(1) = c_2, y''(1) = c_3\}) \right\} \right\}$$

**Maple:** cpu = 0.218 (sec), leaf count = 36

$$\left\{ y(x) = \text{DESol} \left( \left\{ -_Y(x) + (1+x) \frac{d^2}{dx^2} _Y(x) + x^2 \frac{d^3}{dx^3} _Y(x) \right\}, \{ _Y(x) \} \right) \right\}$$

#### 4.42 ODE No. 1490

$$x^2 \frac{d^3}{dx^3} y(x) - x \frac{d^2}{dx^2} y(x) + (x^2 + 1) \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.018502 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} c_1 x^2 {}_0\tilde{F}_1 \left( ; 2; -\frac{x^2}{4} \right) + c_2 x Y_1(x) + c_3 \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 18

$$\{y(x) = \_C1 + \_C2 x J_1(x) + \_C3 x Y_1(x)\}$$

#### 4.43 ODE No. 1491

$$x^2 \frac{d^3}{dx^3} y(x) + 3x \frac{d^2}{dx^2} y(x) + (4a^2 x^{2a} + 1 - 4\nu^2 a^2) \frac{d}{dx} y(x) = 4a^3 x^{2a-1} y(x) = 0$$

**Mathematica:** cpu = 0.046006 (sec), leaf count = 102

$$\left\{ \left\{ y(x) \rightarrow c_2 (x^{2a})^{-\nu} {}_1F_2 \left( -\nu - \frac{1}{2}; 1 - 2\nu, 1 - \nu; -x^{2a} \right) + c_3 (x^{2a})^\nu {}_1F_2 \left( \nu - \frac{1}{2}; \nu + 1, 2\nu + 1; -x^{2a} \right) + \dots \right. \right.$$

**Maple:** cpu = 0.063 (sec), leaf count = 88

$$\left\{ y(x) = \_C1 {}_1F_2 \left( -\frac{1}{2}; \nu + 1, -\nu + 1; -x^{2a} \right) + \_C2 x^{-2a\nu} {}_1F_2 \left( -\frac{1}{2} - \nu; 1 - 2\nu, -\nu + 1; -x^{2a} \right) + \_C3 x \dots \right.$$

#### 4.44 ODE No. 1492

$$x^2 \frac{d^3}{dx^3} y(x) - 3(x - m) x \frac{d^2}{dx^2} y(x) + (2x^2 + 4(n - m)x + m(2m - 1)) \frac{d}{dx} y(x) - 2n(2x - 2m + 1) y(x) = 0$$

**Mathematica:** cpu = 0.403551 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow c_2 U(-n, m, x) L_n^{m-1}(x) + c_1 U(-n, m, x)^2 + c_3 L_n^{m-1}(x)^2 \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 39

$$\left\{ y(x) = \_C1 (M(-n, m, x))^2 + \_C2 (U(-n, m, x))^2 + \_C3 M(-n, m, x) U(-n, m, x) \right\}$$

#### 4.45 ODE No. 1493

$$x^2 \frac{d^3}{dx^3} y(x) + 4x \frac{d^2}{dx^2} y(x) + (x^2 + 2) \frac{d}{dx} y(x) + 3xy(x) - f(x) = 0$$

**Mathematica:** cpu = 7.185412 (sec), leaf count = 2582

$$\left\{ \left\{ y(x) \rightarrow J_0(x)c_1 + 2Y_0(x)c_2 + \frac{2c_3 {}_1F_2 \left( 1; \frac{1}{2}, \frac{1}{2}; -\frac{x^2}{4} \right)}{x} + \frac{x J_0(x) \int_1^x \left( \frac{-16J_1(K[1])Y_0(K[1])^2 f(K[1]) {}_1F_2 \left( 3; \frac{5}{2}, \frac{5}{2}; -\frac{1}{4}K \right)}{\dots} \right)}{\dots} \right. \right.$$

**Maple:** cpu = 0.265 (sec), leaf count = 1849

$$\left\{ y(x) = \frac{1}{x} \left( \int 9 \frac{\dots}{-4 {}_1F_2 \left( 3; 5/2, 5/2; -1/4 x^2 \right) J_1(x) G_{1,3}^{3,1} \left( 1/4 x^2 \left| \begin{matrix} -1/2 \\ 0,0,-1/2 \end{matrix} \right. \right) x^5 - 9 {}_1F_2 \left( 2; 3/2, 3/2; -1/4 x^2 \right)} \right. \right.$$

#### 4.46 ODE No. 1494

$$x^2 \frac{d^3}{dx^3} y(x) + 5x \frac{d^2}{dx^2} y(x) + 4 \frac{d}{dx} y(x) - \ln(x) = 0$$

**Mathematica:** cpu = 0.027003 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow -\frac{c_1}{x} - \frac{2c_2}{x} - \frac{2c_2 \log(x)}{x} + c_3 - \frac{x}{2} + \frac{1}{4} x \log(x) \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 25

$$\left\{ y(x) = -C1 + \frac{-C2 \ln(x)}{x} + \frac{-C3}{x} + \frac{x(\ln(x) - 2)}{4} \right\}$$

#### 4.47 ODE No. 1495

$$x^2 \frac{d^3}{dx^3} y(x) + 6x \frac{d^2}{dx^2} y(x) + 6 \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.018002 (sec), leaf count = 24

$$\left\{ \left\{ y(x) \rightarrow -\frac{c_2}{2x^2} - \frac{c_1}{x} + c_3 \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 16

$$\left\{ y(x) = -C1 + \frac{-C2}{x^2} + \frac{-C3}{x} \right\}$$

#### 4.48 ODE No. 1496

$$x^2 \frac{d^3}{dx^3} y(x) + 6x \frac{d^2}{dx^2} y(x) + 6 \frac{d}{dx} y(x) + ax^2 y(x) = 0$$

**Mathematica:** cpu = 0.273535 (sec), leaf count = 63

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{-\sqrt[3]{ax}}}{x^2} + \frac{c_2 e^{\sqrt[3]{-1} \sqrt[3]{ax}}}{x^2} + \frac{c_3 e^{-(-1)^{2/3} \sqrt[3]{ax}}}{x^2} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 67

$$\left\{ y(x) = \frac{1}{x^2} \left( -C1 e^{(-\frac{1}{2} \sqrt[3]{-a} + \frac{i}{2} \sqrt{3} \sqrt[3]{-a})x} + -C2 e^{(-\frac{1}{2} \sqrt[3]{-a} - \frac{i}{2} \sqrt{3} \sqrt[3]{-a})x} + -C3 e^{\sqrt[3]{-a}x} \right) \right\}$$

#### 4.49 ODE No. 1497

$$x^2 \frac{d^3}{dx^3} y(x) - 3(p+q)x \frac{d^2}{dx^2} y(x) + 3p(3q+1) \frac{d}{dx} y(x) - x^2 y(x) = 0$$

**Mathematica:** cpu = 0.499063 (sec), leaf count = 135

$$\left\{ \left\{ y(x) \rightarrow c_1 {}_0F_2\left(\left;\frac{2}{3}-p, \frac{1}{3}-q;\frac{x^3}{27}\right) + c_2 (-1)^{\frac{1}{3}(3p+1)} 3^{-3p-1} x^{3p+1} {}_0F_2\left(\left;p+\frac{4}{3}, p-q+\frac{2}{3};\frac{x^3}{27}\right) + c_3 (-1) \right\} \right.$$

**Maple:** cpu = 0.203 (sec), leaf count = 77

$$\left\{ y(x) = \_C1 {}_0F_2\left(\left;-q+\frac{1}{3}, -p+\frac{2}{3};\frac{x^3}{27}\right) + \_C2 x^{1+3p} {}_0F_2\left(\left;p+\frac{4}{3}, -q+\frac{2}{3}+p;\frac{x^3}{27}\right) + \_C3 x^{3q+2} {}_0F_2\left(\left;\right.\right) \right.$$

#### 4.50 ODE No. 1498

$$x^2 \frac{d^3}{dx^3} y(x) - 2(n+1)x \frac{d^2}{dx^2} y(x) + (ax^2 + 6n) \frac{d}{dx} y(x) - 2axy(x) = 0$$

**Mathematica:** cpu = 8.482077 (sec), leaf count = 584

$$\left\{ \left\{ y(x) \rightarrow -\frac{\pi c_3 2^{-n-\frac{3}{2}} x (\sqrt{ax})^{-n-\frac{1}{2}} \left( -a^{3/2} 2^{2n} x^3 \sec(\pi n) \Gamma\left(\frac{3}{2}-n\right) \Gamma\left(n+\frac{3}{2}\right) J_{\frac{1}{2}(2n+1)}(\sqrt{ax}) {}_1\tilde{F}_2\left(\frac{3}{2}-n; \frac{1}{2}, \frac{3}{2}\right) \right)}{\Gamma\left(\frac{3}{2}-n\right) \Gamma\left(n+\frac{3}{2}\right)} \right\} \right.$$

**Maple:** cpu = 0.234 (sec), leaf count = 53

$$\left\{ y(x) = \_C1 x^{n+\frac{1}{2}} J_{-n-\frac{1}{2}}(\sqrt{ax}) + \_C2 x^{n+\frac{1}{2}} Y_{-n-\frac{1}{2}}(\sqrt{ax}) + \_C3 (ax^2 + 4n - 2) \right\}$$

#### 4.51 ODE No. 1499

$$x^2 \frac{d^3}{dx^3} y(x) - (x^2 - 2x) \frac{d^2}{dx^2} y(x) - (x^2 + \nu^2 - 1/4) \frac{d}{dx} y(x) + (x^2 - 2x + \nu^2 - 1/4) y(x) = 0$$

**Mathematica:** cpu = 0.232530 (sec), leaf count = 97

$$\left\{ \left\{ y(x) \rightarrow \frac{c_3 e^x x^{\nu+\frac{1}{2}} \Gamma\left(\nu+\frac{1}{2}\right) {}_1\tilde{F}_1\left(\nu+\frac{1}{2}; 2\nu+1; -2x\right)}{\Gamma\left(\frac{3}{2}-\nu\right)} + c_2 2^{-\nu-\frac{1}{2}} e^x G_{2,3}^{2,1}\left(2x \left| \begin{matrix} 1, 0 \\ \frac{1}{2}-\nu, \nu+\frac{1}{2}, 0 \end{matrix} \right. \right) + c_1 e^x \right\} \right.$$

**Maple:** cpu = 0.218 (sec), leaf count = 25

$$\{ y(x) = \_C1 e^x + \_C2 \sqrt{x} I_\nu(x) + \_C3 \sqrt{x} K_\nu(x) \}$$



#### 4.52 ODE No. 1500

$$x^2 \frac{d^3}{dx^3} y(x) - (x + \nu) x \frac{d^2}{dx^2} y(x) + \nu(2x + 1) \frac{d}{dx} y(x) - \nu(1 + x) y(x) = 0$$

**Mathematica:** cpu = 47.362014 (sec), leaf count = 71

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{y^{(3)}(x)x^2 - (x + \nu)y''(x)x - (x + 1)\nu y(x) + (2x\nu + \nu)y'(x) = 0, y(1)\right\} \right\}$$

**Maple:** cpu = 0.172 (sec), leaf count = 55

$$\left\{ y(x) = \_C1 e^x + \_C2 x^{\frac{\nu}{2} + \frac{1}{2}} J_{-\nu-1}(2\sqrt{\nu}\sqrt{x}) + \_C3 x^{\frac{\nu}{2} + \frac{1}{2}} Y_{-\nu-1}(2\sqrt{\nu}\sqrt{x}) \right\}$$

#### 4.53 ODE No. 1501

$$x^2 \frac{d^3}{dx^3} y(x) - 2(x^2 - x) \frac{d^2}{dx^2} y(x) + (x^2 - 2x + 1/4 - \nu^2) \frac{d}{dx} y(x) + (\nu^2 - 1/4) y(x) = 0$$

**Mathematica:** cpu = 0.187024 (sec), leaf count = 86

$$\left\{ \left\{ y(x) \rightarrow \frac{c_3 e^x x^{\nu + \frac{1}{2}} \Gamma(\nu + \frac{1}{2}) {}_1\tilde{F}_1(\nu + \frac{1}{2}; 2\nu + 1; -x)}{\Gamma(\frac{3}{2} - \nu)} + c_2 e^x G_{2,3}^{2,1} \left( x \left| \begin{matrix} 1, 0 \\ \frac{1}{2} - \nu, \nu + \frac{1}{2}, 0 \end{matrix} \right. \right) + c_1 e^x \right\} \right\}$$

**Maple:** cpu = 0.203 (sec), leaf count = 37

$$\left\{ y(x) = \_C1 e^x + \_C2 e^{\frac{x}{2}} \sqrt{x} I_{\nu} \left( \frac{x}{2} \right) + \_C3 e^{\frac{x}{2}} \sqrt{x} K_{\nu} \left( \frac{x}{2} \right) \right\}$$

#### 4.54 ODE No. 1502

$$x^2 \frac{d^3}{dx^3} y(x) - (x^4 - 6x) \frac{d^2}{dx^2} y(x) - (2x^3 - 6) \frac{d}{dx} y(x) + 2x^2 y(x) = 0$$

**Mathematica:** cpu = 0.055007 (sec), leaf count = 98

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 \Gamma(\frac{1}{3}) {}_2F_2 \left( -\frac{2}{3}, \frac{1}{3}; \frac{2}{3}, \frac{4}{3}; \frac{x^3}{3} \right)}{3x \Gamma(\frac{4}{3})} + \frac{\sqrt[3]{-\frac{1}{3}} c_3 \Gamma(\frac{2}{3}) {}_2F_2 \left( -\frac{1}{3}, \frac{2}{3}; \frac{4}{3}, \frac{5}{3}; \frac{x^3}{3} \right)}{3\Gamma(\frac{5}{3})} + \frac{c_1}{x^2} \right\} \right\}$$

**Maple:** cpu = 0.328 (sec), leaf count = 109

$$\left\{ y(x) = \frac{C1}{x^2} + \frac{C2}{x^2} \int e^{\frac{x^3}{6}} \sqrt{x} \left( I_{\frac{1}{6}} \left( -\frac{x^3}{6} \right) x^3 + I_{-\frac{5}{6}} \left( -\frac{x^3}{6} \right) x^3 - 2 I_{1/6}(-1/6 x^3) \right) dx + \frac{C3}{x^2} \int e^{\frac{x^3}{6}} \sqrt{x} dx \right\}$$

#### 4.55 ODE No. 1503

$$(x^2 + 1) \frac{d^3}{dx^3} y(x) + 8x \frac{d^2}{dx^2} y(x) + 10 \frac{d}{dx} y(x) - 3 + x^{-2} - 2 \ln(x) = 0$$

**Mathematica:** cpu = 0.106013 (sec), leaf count = 62

$$\left\{ \left\{ y(x) \rightarrow c_3 - \frac{100(3c_2 - 1)x^3 + 900c_2x + 225c_1 + 36x^5 - 60(3x^4 + 10x^2 + 15)x \log(x)}{900(x^2 + 1)^2} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 86

$$\left\{ y(x) = \frac{x^2(x^2 + 2) \_C1}{(x^2 + 1)^2} + \frac{x(x^2 + 3) \_C2}{(x^2 + 1)^2} + \frac{\_C3}{(x^2 + 1)^2} + \frac{x(45x^4 \ln(x) - 9x^4 + 150x^2 \ln(x) - 50x^2 + 225)}{225(x^2 + 1)^2} \right\}$$

#### 4.56 ODE No. 1504

$$(x^2 + 2) \frac{d^3}{dx^3} y(x) - 2x \frac{d^2}{dx^2} y(x) + (x^2 + 2) \frac{d}{dx} y(x) - 2xy(x) = 0$$

**Mathematica:** cpu = 0.108014 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 x^2}{2} + \frac{1}{2} i c_2 e^{-ix} - \frac{1}{4} c_3 e^{ix} \right\} \right\}$$

**Maple:** cpu = 0.171 (sec), leaf count = 18

$$\{ y(x) = \_C1 x^2 + \_C2 \cos(x) + \_C3 \sin(x) \}$$

#### 4.57 ODE No. 1505

$$2x(x-1) \frac{d^3}{dx^3} y(x) + 3(2x-1) \frac{d^2}{dx^2} y(x) + (2ax+b) \frac{d}{dx} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 62.084884 (sec), leaf count = 69

$$\{ \{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{ay(x) + (2xa + b)y'(x) + (6x - 3)y''(x) + 2(x - 1)xy^{(3)}(x) = 0, y(2)$$

**Maple:** cpu = 0.125 (sec), leaf count = 79

$$\left\{ y(x) = \_C1 \left( \text{MathieuC} \left( -\frac{a}{2} - \frac{b}{2} + 1, \frac{a}{4}, \arccos(\sqrt{x}) \right) \right)^2 + \_C2 \left( \text{MathieuS} \left( -\frac{a}{2} - \frac{b}{2} + 1, \frac{a}{4}, \arccos(\sqrt{x}) \right) \right)^2 \right\}$$

#### 4.58 ODE No. 1506

$$4x^2 \frac{d^3}{dx^3} y(x) + (x^2 + 14x - 1) \frac{d^2}{dx^2} y(x) + 4(1+x) \frac{d}{dx} y(x) + 2y(x) = 0$$

**Mathematica:** cpu = 30.884422 (sec), leaf count = 208

$$\left\{ \left\{ y(x) \rightarrow c_2 \left( -\sqrt{e\pi} \operatorname{erfi} \left( \frac{x-1}{2\sqrt{x}} \right) + 3\sqrt{\frac{\pi}{e}} \operatorname{erfi} \left( \frac{x+1}{2\sqrt{x}} \right) - 3\sqrt{\frac{\pi}{e}} \operatorname{erfi}(1) - \frac{4e^{\frac{x^2+1}{4x}}}{\sqrt{x}} + 4\sqrt{e} \right) e^{\frac{1}{4}(-x-\frac{1}{x}+2\log(x))} \right. \right.$$

**Maple:** cpu = 0.031 (sec), leaf count = 43

$$\left\{ y(x) = \left( -C3 + \int \frac{2x-C1 + -C2}{4} e^{\frac{x}{4}} e^{\frac{1}{4x}} x^{-\frac{5}{2}} dx \right) e^{-\frac{x}{4}} \sqrt{x} e^{-\frac{1}{4x}} \right\}$$

#### 4.59 ODE No. 1507

$$(ax+b)x \frac{d^3}{dx^3} y(x) + (\alpha x + \beta) \frac{d^2}{dx^2} y(x) + x \frac{d}{dx} y(x) + y(x) - f(x) = 0$$

**Mathematica:** cpu = 2.446811 (sec), leaf count = 40

$$\text{DSolve}[xy^{(3)}(x)(ax+b) + (\alpha x + \beta)y''(x) - f(x) + xy'(x) + y(x) = 0, y(x), x]$$

**Maple:** cpu = 0.468 (sec), leaf count = 1421

$$\left\{ y(x) = \operatorname{HeunC} \left( 0, \frac{-2b+\beta}{b}, \frac{(2b+\beta)a-\alpha b}{ab}, -\frac{b}{a^2}, \frac{(4a-\alpha)b^2 - \alpha\beta b + a\beta^2}{2ab^2}, -\frac{ax}{b} \right) (ax+b)^{\frac{(2b+\beta)a-\alpha}{ab}} \right.$$

#### 4.60 ODE No. 1508

$$x^3 \frac{d^3}{dx^3} y(x) + (-\nu^2 + 1) x \frac{d}{dx} y(x) + (ax^3 + \nu^2 - 1) y(x) = 0$$

**Mathematica:** cpu = 0.777099 (sec), leaf count = 143

$$\left\{ \left\{ y(x) \rightarrow c_2 3^{\nu-1} a^{\frac{1-\nu}{3}} x^{1-\nu} {}_0F_2 \left( ; 1 - \frac{2\nu}{3}, 1 - \frac{\nu}{3}; -\frac{ax^3}{27} \right) + c_3 3^{-\nu-1} a^{\frac{\nu+1}{3}} x^{\nu+1} {}_0F_2 \left( ; \frac{\nu}{3} + 1, \frac{2\nu}{3} + 1; -\frac{ax^3}{27} \right) \right. \right.$$

**Maple:** cpu = 0.125 (sec), leaf count = 81

$$\left\{ y(x) = -C1 x {}_0F_2 \left( ; \frac{\nu}{3} + 1, -\frac{\nu}{3} + 1; -\frac{ax^3}{27} \right) + -C2 x^{-\nu+1} {}_0F_2 \left( ; 1 - \frac{2\nu}{3}, -\frac{\nu}{3} + 1; -\frac{ax^3}{27} \right) + -C3 x^{\nu+1} {}_0F_2 \left( ; \frac{\nu}{3} + 1, \frac{2\nu}{3} + 1; -\frac{ax^3}{27} \right) \right.$$

#### 4.61 ODE No. 1509

$$x^3 \frac{d^3}{dx^3} y(x) + (4x^3 + (-4\nu^2 + 1)x) \frac{d}{dx} y(x) + (4\nu^2 - 1)y(x) = 0$$

**Mathematica:** cpu = 0.010501 (sec), leaf count = 34

$$\left\{ \left\{ y(x) \rightarrow c_1 x J_\nu(x)^2 + c_3 x Y_\nu(x)^2 + c_2 x J_\nu(x) Y_\nu(x) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 30

$$\left\{ y(x) = \_C1 x (J_\nu(x))^2 + \_C2 x (Y_\nu(x))^2 + \_C3 x J_\nu(x) Y_\nu(x) \right\}$$

#### 4.62 ODE No. 1510

$$x^3 \frac{d^3}{dx^3} y(x) + (ax^{2\nu} + 1 - \nu^2) x \frac{d}{dx} y(x) + (bx^{3\nu} + a(\nu - 1)x^{2\nu} + \nu^2 - 1)y(x) = 0$$

**Mathematica:** cpu = 0.052007 (sec), leaf count = 60

DSolve[ $y(x) (a(\nu - 1)x^{2\nu} + bx^{3\nu} + \nu^2 - 1) + x(ax^{2\nu} - \nu^2 + 1) y'(x) + x^3 y^{(3)}(x) = 0, y(x), x]$

**Maple:** cpu = 0.078 (sec), leaf count = 74

$$\left\{ y(x) = DESol \left( \left\{ x^3 \frac{d^3}{dx^3} Y(x) + (x^{2\nu} a x - \nu^2 x + x) \frac{d}{dx} Y(x) + (x^{2\nu} a \nu - a x^{2\nu} + b x^{3\nu} + \nu^2 - 1) Y(x) \right\} \right) \right\}$$

#### 4.63 ODE No. 1511

$$x^3 \frac{d^3}{dx^3} y(x) + 3x^2 \frac{d^2}{dx^2} y(x) - 2x \frac{d}{dx} y(x) + 2y(x) - 6x^3(x-1) \ln(x) + x^3(x+8) = 0$$

**Mathematica:** cpu = 0.035505 (sec), leaf count = 51

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1}{x^2} + c_2 x + c_3 x \log(x) + \frac{1}{450} (-50x^4 + 50x^4 \log(x) - 18x^3 - 135x^3 \log(x)) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 37

$$\left\{ y(x) = \frac{x^3(50x \ln(x) - 135 \ln(x) - 50x - 18)}{450} + x\_C1 + \frac{\_C2}{x^2} + \_C3 x \ln(x) \right\}$$

#### 4.64 ODE No. 1512

$$x^3 \frac{d^3}{dx^3} y(x) + 3x^2 \frac{d^2}{dx^2} y(x) + (-a^2 + 1)x \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.038005 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow -\frac{c_1 x^{-a}}{a} + \frac{c_2 x^a}{a} + c_3 \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 18

$$\{y(x) = \_C1 + \_C2 x^{-a} + \_C3 x^a\}$$

#### 4.65 ODE No. 1513

$$x^3 \frac{d^3}{dx^3} y(x) - 4x^2 \frac{d^2}{dx^2} y(x) + (x^2 + 8)x \frac{d}{dx} y(x) - 2(x^2 + 4)y(x) = 0$$

**Mathematica:** cpu = 0.074509 (sec), leaf count = 25

$$\left\{ \left\{ y(x) \rightarrow c_1 x^2 - c_2 x \sin(x) + c_3 x \cos(x) \right\} \right\}$$

**Maple:** cpu = 0.171 (sec), leaf count = 20

$$\{y(x) = \_C1 x^2 + \_C2 x \sin(x) + \_C3 \cos(x) x\}$$

#### 4.66 ODE No. 1514

$$x^3 \frac{d^3}{dx^3} y(x) + 6x^2 \frac{d^2}{dx^2} y(x) + (ax^3 - 12)y(x) = 0$$

**Mathematica:** cpu = 0.717091 (sec), leaf count = 102

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 e^{-\sqrt[3]{ax}} (\sqrt[3]{ax} + 2)}{x^3} + \frac{c_2 e^{\sqrt[3]{-1} \sqrt[3]{ax}} (\sqrt[3]{ax} + 2(-1)^{2/3})}{x^3} + \frac{c_3 e^{-(-1)^{2/3} \sqrt[3]{ax}} (\sqrt[3]{ax} - 2\sqrt[3]{-1})}{x^3} \right\} \right\}$$

**Maple:** cpu = 0.390 (sec), leaf count = 151

$$\left\{ y(x) = \frac{C1}{x^3} \left( a^3 x + 2(-a^4)^{2/3} \right) e^{\frac{x}{a} \sqrt[3]{-a^4}} + \frac{C2}{x^3} \left( (-a^4)^{2/3} \sqrt{3} - ia^3 x + i(-a^4)^{2/3} \right) e^{\frac{i}{2} \frac{(-\sqrt{3}+i)x}{a} \sqrt[3]{-a^4}} + \frac{C3}{x^3} \right\}$$

#### 4.67 ODE No. 1515

$$x^3 \frac{d^3}{dx^3} y(x) + 3(1-a)x^2 \frac{d^2}{dx^2} y(x) + (4b^2c^2x^{2c+1} + 1 - 4\nu^2c^2 + 3a(a-1)x) \frac{d}{dx} y(x) + (4b^2c^2(c-a)x^2$$

**Mathematica:** cpu = 0.121015 (sec), leaf count = 104

**DSolve**[ $y(x) (a(4c^2\nu^2 - a^2) + 4b^2c^2(c-a)x^{2c}) + y'(x) (3(a-1)ax + 4b^2c^2x^{2c+1} - 4c^2\nu^2 + 1) + 3(1-a)y(x)$ ]

**Maple:** cpu = 0 (sec), leaf count = 0

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#### 4.68 ODE No. 1516

$$x^3 \frac{d^3}{dx^3} y(x) + (x+3)x^2 \frac{d^2}{dx^2} y(x) + 5(x-6)x \frac{d}{dx} y(x) + (4x+30)y(x) = 0$$

**Mathematica:** cpu = 434.677197 (sec), leaf count = 71

{ $y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{y^{(3)}(x)x^3 + (x+3)y''(x)x^2 + 5(x-6)y'(x)x + (4x+30)y(x) = 0, y(x)$ }

**Maple:** cpu = 0.359 (sec), leaf count = 263

$$\left\{ y(x) = \frac{-C1(x^4 - 84x^3 + 2016x^2 - 20160x + 75600)}{x^6} + \frac{-C2 e^{-x}(x^8 + 28x^7 + 450x^6 + 5100x^5 + 42900x^4 + 252000x^3 + 756000x^2 + 1209600x + 518400)}{x^6} \right.$$

#### 4.69 ODE No. 1517

$$x^3 \frac{d^3}{dx^3} y(x) + x^2 \frac{d^2}{dx^2} y(x) + \ln(x) + 2x \frac{d}{dx} y(x) - y(x) - 2x^3 = 0$$

**Mathematica:** cpu = 0.409052 (sec), leaf count = 30686

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**Maple:** cpu = 0.327 (sec), leaf count = 1770

$$\left\{ y(x) = - \int \frac{5 \left( x^{1/12} \sqrt[3]{44+12\sqrt{69}} + 2/3 + \frac{11(44+12\sqrt{69})^{2/3}}{1200} - \frac{\sqrt{69}(44+12\sqrt{69})^{2/3}}{400} \right)^2 \sqrt[3]{44+12\sqrt{69}} (\ln(x) - 2x^3)}{2x^3 (3\sqrt{23}\sqrt{3} + 11) (11\sqrt{23}\sqrt{3} - 207)} dx \right. \left. \left( 3 \right. \right.$$

#### 4.70 ODE No. 1518

$$(x^2 + 1) x \frac{d^3}{dx^3} y(x) + 3(2x^2 + 1) \frac{d^2}{dx^2} y(x) - 12y(x) = 0$$

**Mathematica:** cpu = 0.241531 (sec), leaf count = 106

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{3} c_1 (2x^2 + 1) + \frac{1}{3} c_2 x \sqrt{x^2 + 1} + \frac{c_3 (2x^2 + 1) (3x^2 + 3\sqrt{x^2 + 1} x^2 \log(x) - 3\sqrt{x^2 + 1} x^2 \log(\sqrt{x^2 + 1}))}{6(2x^3 + x)} \right\} \right\}$$

**Maple:** cpu = 0.374 (sec), leaf count = 56

$$\left\{ y(x) = \_C1 x \sqrt{x^2 + 1} + \frac{\_C2}{x} \left( 3x^2 \sqrt{x^2 + 1} \operatorname{Artanh} \left( \frac{1}{\sqrt{x^2 + 1}} \right) - 3x^2 - 1 \right) + \_C3 (2x^2 + 1) \right\}$$

#### 4.71 ODE No. 1519

$$(x + 3) x^2 \frac{d^3}{dx^3} y(x) - 3x(x + 2) \frac{d^2}{dx^2} y(x) + 6(1 + x) \frac{d}{dx} y(x) - 6y(x) = 0$$

**Mathematica:** cpu = 0.030004 (sec), leaf count = 65

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4} c_1 (x^3 - 3x^2 + 3x + 3) + \frac{1}{2} c_2 (-x^3 + 3x^2 - x - 1) + \frac{1}{8} c_3 (3x^3 - 5x^2 + x + 1) \right\} \right\}$$

**Maple:** cpu = 0.124 (sec), leaf count = 20

$$\{y(x) = \_C1 x^2 + x^3 \_C2 + \_C3 (1 + x)\}$$

#### 4.72 ODE No. 1520

$$2(x - a1)(x - a2)(x - a3) \frac{d^3}{dx^3} y(x) + (9x^2 - 6(a1 + a2 + a3)x + 3a1a2 + 3a1a3 + 3a2a3) \frac{d^2}{dx^2} y(x) + (3x^2 - 2a1x - 2a2) y'(x) - 3y(x) = 0$$

**Mathematica:** cpu = 72.774241 (sec), leaf count = 167

$$\left\{ \left\{ y(x) \rightarrow \operatorname{DifferentialRoot}(\{y, x\}, \{-n(n + 1)y(x) - 2(xn^2 + xn - 3x + b) y'(x) + 3(3x^2 - 2a1x - 2a2) y(x) - 3y(x)\}) \right\} \right\}$$

**Maple:** cpu = 0.374 (sec), leaf count = 279

$$\left\{ y(x) = \_C1 \left( \operatorname{HeunG} \left( \frac{-a3 + a1}{-a2 + a1}, -\frac{a1n^2 + a1n - a1 - a2 - a3 + b}{-4a2 + 4a1}, -\frac{n}{2}, \frac{n}{2}, \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{-x + a1}{-a2 + a1} \right) \right) \right\}$$

#### 4.73 ODE No. 1521

$$(1+x)x^3 \frac{d^3}{dx^3}y(x) - (4x+2)x^2 \frac{d^2}{dx^2}y(x) + (10x+4)x \frac{d}{dx}y(x) - 4(3x+1)y(x) = 0$$

**Mathematica:** cpu = 0.065008 (sec), leaf count = 35

$$\left\{ \left\{ y(x) \rightarrow c_1 x^2 + c_3 x^2 \left( x + \frac{1}{x} + \log^2(x) \right) + c_2 x^2 \log(x) \right\} \right\}$$

**Maple:** cpu = 0.358 (sec), leaf count = 31

$$\{y(x) = \_C1 x^2 + \_C2 x^2 \ln(x) + \_C3 (x(\ln(x))^2 + x^2 + 1) x\}$$

#### 4.74 ODE No. 1522

$$4x^4 \frac{d^3}{dx^3}y(x) - 4x^3 \frac{d^2}{dx^2}y(x) + 4x^2 \frac{d}{dx}y(x) - 1 = 0$$

**Mathematica:** cpu = 0.019502 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1 x^2}{2} - \frac{c_2 x^2}{4} + \frac{1}{2} c_2 x^2 \log(x) + c_3 - \frac{1}{36x} \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 31

$$\left\{ y(x) = \frac{x^2 \_C1 \ln(x)}{2} - \frac{\_C1 x^2}{4} + \frac{x^2 \_C2}{2} - \frac{1}{36x} + \_C3 \right\}$$

#### 4.75 ODE No. 1523

$$(x^2+1)x^3 \frac{d^3}{dx^3}y(x) - (4x^2+2)x^2 \frac{d^2}{dx^2}y(x) + (10x^2+4)x \frac{d}{dx}y(x) - 4(3x^2+1)y(x) = 0$$

**Mathematica:** cpu = 0.118515 (sec), leaf count = 74

$$\left\{ \left\{ y(x) \rightarrow c_1(-x^3 + 3x^2 - x) + \frac{1}{2} c_2(x^3 - 2x^2 + x) - \frac{c_3 x(-x^3 + 3x^2 - x)(\log(x) + 1)}{2(x^2 - 3x + 1)} \right\} \right\}$$

**Maple:** cpu = 0.359 (sec), leaf count = 26

$$\{y(x) = \_C1 x^2 + \_C2 x^2(\ln(x) + 1) + \_C3 (x^3 + x)\}$$



#### 4.76 ODE No. 1524

$$x^6 \frac{d^3}{dx^3} y(x) + x^2 \frac{d^2}{dx^2} y(x) - 2y(x) = 0$$

**Mathematica:** cpu = 0.143518 (sec), leaf count = 96

$$\left\{ \left\{ y(x) \rightarrow -\frac{\left(-\frac{1}{3}\right)^{2/3} c_2 x \Gamma\left(\frac{1}{3}\right) {}_2F_2\left(-\frac{2}{3}, \frac{1}{3}; \frac{2}{3}, \frac{4}{3}; \frac{1}{3x^3}\right)}{3\Gamma\left(\frac{4}{3}\right)} + \frac{c_3 \Gamma\left(\frac{2}{3}\right) {}_2F_2\left(-\frac{1}{3}, \frac{2}{3}; \frac{4}{3}, \frac{5}{3}; \frac{1}{3x^3}\right)}{9\Gamma\left(\frac{5}{3}\right)} + c_1 x^2 \right\} \right\}$$

**Maple:** cpu = 0.390 (sec), leaf count = 104

$$\left\{ y(x) = \_C1 x^2 + \_C2 \int 1 e^{\frac{1}{6x^3}} \left( 2x^3 I_{1/6}(-1/6 x^{-3}) - I_{1/6}\left(-\frac{1}{6x^3}\right) - I_{-5/6}\left(-\frac{1}{6x^3}\right) \right) x^{-11/2} dx x^2 + \_C3 \right\}$$

#### 4.77 ODE No. 1525

$$x^6 \frac{d^3}{dx^3} y(x) + 6x^5 \frac{d^2}{dx^2} y(x) + ay(x) = 0$$

**Mathematica:** cpu = 0.439556 (sec), leaf count = 102

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{\frac{\sqrt[3]{a}}{x}} (2x - \sqrt[3]{a}) + c_2 e^{\frac{(-1)^{2/3} \sqrt[3]{a}}{x}} \left( x - \frac{1}{2} (-1)^{2/3} \sqrt[3]{a} \right) + c_3 e^{-\frac{\sqrt[3]{-1} \sqrt[3]{a}}{x}} \left( \frac{1}{2} \sqrt[3]{-1} \sqrt[3]{a} + x \right) \right\} \right\}$$

**Maple:** cpu = 0.437 (sec), leaf count = 291

$$\left\{ y(x) = \_C1 (-8x^3 + a)^4 e^{-\frac{1}{ax} \sqrt[3]{-a^4}} \left( 2ax + \sqrt[3]{-a^4} \right)^{-3} \left( 4a^2 x^2 - 2x \sqrt[3]{-a^4} a + (-a^4)^{\frac{2}{3}} \right)^{-4} + \_C2 (-8x^3 + a)^4 e^{\frac{1}{ax} \sqrt[3]{-a^4}} \left( 2ax + \sqrt[3]{-a^4} \right)^{-3} \left( 4a^2 x^2 - 2x \sqrt[3]{-a^4} a + (-a^4)^{\frac{2}{3}} \right)^{-4} + \_C3 (-8x^3 + a)^4 e^{-\frac{1}{ax} \sqrt[3]{-a^4}} \left( 2ax + \sqrt[3]{-a^4} \right)^{-3} \left( 4a^2 x^2 - 2x \sqrt[3]{-a^4} a + (-a^4)^{\frac{2}{3}} \right)^{-4} \right\}$$

#### 4.78 ODE No. 1526

$$x^2(x^4 + 2x^2 + 2x + 1) \frac{d^3}{dx^3} y(x) - (2x^6 + 3x^4 - 6x^2 - 6x - 1) \frac{d^2}{dx^2} y(x) + (x^6 - 6x^3 - 15x^2 - 12x - 1) \frac{d}{dx} y(x) - (x^6 - 6x^3 - 15x^2 - 12x - 1) y(x) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

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**Maple:** cpu = 0.203 (sec), leaf count = 20

$$\left\{ y(x) = \_C1 e^x + \_C2 e^{x^{-1}} + \_C3 x e^x \right\}$$

#### 4.79 ODE No. 1527

$$(x - a)^3 (x - b)^3 \frac{d^3}{dx^3} y(x) - cy(x) = 0$$

**Mathematica:** cpu = 135.354688 (sec), leaf count = 58

$$\{ \{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{(a - x)^3 (b - x)^3 y^{(3)}(x) - cy(x) = 0, y(0) = c_1, y'(0) = c_2, y''(0) = c_3\}) \}$$

**Maple:** cpu = 0.421 (sec), leaf count = 500

$$\left\{ y(x) = \_C1 (x - a)^{-2 \frac{b}{a-b}} (x - b)^{2 \frac{a}{a-b}} (b - x)^{-\frac{\text{RootOf}(-Z^3 + (-3a - 3b)Z^2 + (2a^2 + 8ab + 2b^2)Z - 4ba^2 - 4ab^2 - c, \text{index}=1)}{a-b}} (a - \right.$$

#### 4.80 ODE No. 1528

$$\left( \frac{d^3}{dx^3} y(x) \right) \sin(x) + (2 \cos(x) + 1) \frac{d^2}{dx^2} y(x) - \sin(x) \frac{d}{dx} y(x) - \cos(x) = 0$$

**Mathematica:** cpu = 0.494563 (sec), leaf count = 72

$$\left\{ \left\{ y(x) \rightarrow \frac{\sin\left(\frac{x}{2}\right) \left( \sqrt{2} (c_2 x \sin\left(\frac{x}{2}\right) + \cos\left(\frac{x}{2}\right) (c_2 \log(2(\cos(x) + 1)) + 2c_1)) - 2 \cos\left(\frac{x}{2}\right) \sin^{-1}(\cos(x)) \right) + \right. \right.$$

**Maple:** cpu = 0.078 (sec), leaf count = 68

$$\left\{ y(x) = \frac{-C1}{-1 + \cos(x)} \left( \ln(\sin(x)) \sin(x) - \ln\left(-\frac{-1 + \cos(x)}{\sin(x)}\right) \sin(x) - \cos(x) x + x \right) + \_C2 + \frac{\sin(x)}{-1 + \cos(x)} \right.$$

#### 4.81 ODE No. 1529

$$(\sin(x) + x) \frac{d^3}{dx^3} y(x) + 3(\cos(x) + 1) \frac{d^2}{dx^2} y(x) - 3 \sin(x) \frac{d}{dx} y(x) - y(x) \cos(x) + \sin(x) = 0$$

**Mathematica:** cpu = 0.077010 (sec), leaf count = 42

$$\text{DSolve}[y^{(3)}(x)(x + \sin(x)) + 3(\cos(x) + 1)y''(x) - 3 \sin(x)y'(x) - y(x) \cos(x) + \sin(x) = 0, y(x), x]$$

**Maple:** cpu = 0.047 (sec), leaf count = 43

$$\left\{ y(x) = \frac{-C1 x^2}{\sin(x) + x} + \frac{-C2 x}{\sin(x) + x} - \frac{\cos(x)}{\sin(x) + x} + \frac{-C3}{\sin(x) + x} \right\}$$

#### 4.82 ODE No. 1530

$$\left( \frac{d^3}{dx^3} y(x) \right) (\sin(x))^2 + 3 \left( \frac{d^2}{dx^2} y(x) \right) \sin(x) \cos(x) + (\cos(2x) + 4\nu(\nu+1) (\sin(x))^2) \frac{d}{dx} y(x) + 2\nu(\nu+1) y(x) = 0$$

**Mathematica:** cpu = 0.112514 (sec), leaf count = 58

$$\text{DSolve}[y'(x) (4\nu(\nu+1) \sin^2(x) + \cos(2x)) + 2\nu(\nu+1)y(x) \sin(2x) + y^{(3)}(x) \sin^2(x) + 3 \sin(x) \cos(x) y''(x) + 2\nu(\nu+1) y(x) = 0, x]$$

**Maple:** cpu = 0.187 (sec), leaf count = 113

$$\left\{ y(x) = -C1 \left( {}_2F_1\left(-\frac{\nu}{2}, \frac{\nu}{2} + \frac{1}{2}; \frac{1}{2}; \frac{\cos(2x)}{2} + \frac{1}{2}\right) \right)^2 + -C2 (\cos(2x) + 1) \left( {}_2F_1\left(1 + \frac{\nu}{2}, \frac{1}{2} - \frac{\nu}{2}; \frac{3}{2}; \frac{\cos(2x)}{2}\right) \right) \right\}$$

#### 4.83 ODE No. 1531

$$\left( \frac{d}{dx} f(x) \right) \frac{d^2}{dx^2} y(x) + f(x) \frac{d^3}{dx^3} y(x) + \left( \frac{d}{dx} g(x) \right) \frac{d}{dx} y(x) + g(x) \frac{d^2}{dx^2} y(x) + \left( \frac{d}{dx} h(x) \right) y(x) + h(x) \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.034004 (sec), leaf count = 76

$$\text{DSolve}[A(x) (f(x) y''(x) + g(x) y'(x) + h(x) y(x)) + f'(x) y''(x) + f(x) y^{(3)}(x) + g'(x) y'(x) + g(x) y''(x) + h(x) y(x) + h'(x) y(x) = 0, x]$$

**Maple:** cpu = 0.125 (sec), leaf count = 70

$$\left\{ y(x) = \text{DESol} \left( \left\{ f(x) \frac{d^3}{dx^3} - Y(x) + \left( \frac{d}{dx} f(x) + g(x) + A(x) f(x) \right) \frac{d^2}{dx^2} - Y(x) + \left( \frac{d}{dx} g(x) + h(x) + A(x) g(x) \right) \frac{d}{dx} - Y(x) \right\} \right) \right\}$$

#### 4.84 ODE No. 1532

$$\frac{d^3}{dx^3} y(x) + x \frac{d}{dx} y(x) + n y(x) = 0$$

**Mathematica:** cpu = 0.018502 (sec), leaf count = 103

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 x {}_1F_2\left(\frac{n}{3} + \frac{1}{3}; \frac{2}{3}, \frac{4}{3}; -\frac{x^3}{9}\right)}{3^{2/3}} + c_1 {}_1F_2\left(\frac{n}{3}; \frac{1}{3}, \frac{2}{3}; -\frac{x^3}{9}\right) + \frac{c_3 x^2 {}_1F_2\left(\frac{n}{3} + \frac{2}{3}; \frac{4}{3}, \frac{5}{3}; -\frac{x^3}{9}\right)}{3\sqrt{3}} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 58

$$\left\{ y(x) = -C1 {}_1F_2\left(\frac{n}{3}; \frac{1}{3}, \frac{2}{3}; -\frac{x^3}{9}\right) + -C2 x {}_1F_2\left(\frac{1}{3} + \frac{n}{3}; \frac{2}{3}, \frac{4}{3}; -\frac{x^3}{9}\right) + -C3 x^2 {}_1F_2\left(\frac{2}{3} + \frac{n}{3}; \frac{4}{3}, \frac{5}{3}; -\frac{x^3}{9}\right) \right\}$$

#### 4.85 ODE No. 1533

$$\frac{d^3}{dx^3}y(x) - x \frac{d}{dx}y(x) - ny(x) = 0$$

**Mathematica:** cpu = 0.017002 (sec), leaf count = 113

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[3]{-1}c_2 x {}_1F_2\left(\frac{n}{3} + \frac{1}{3}; \frac{2}{3}, \frac{4}{3}; \frac{x^3}{9}\right)}{3^{2/3}} + c_1 {}_1F_2\left(\frac{n}{3}; \frac{1}{3}, \frac{2}{3}; \frac{x^3}{9}\right) + \frac{(-1)^{2/3}c_3 x^2 {}_1F_2\left(\frac{n}{3} + \frac{2}{3}; \frac{4}{3}, \frac{5}{3}; \frac{x^3}{9}\right)}{3\sqrt[3]{3}} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 58

$$\left\{ y(x) = -C1 {}_1F_2\left(\frac{n}{3}; \frac{1}{3}, \frac{2}{3}; \frac{x^3}{9}\right) + -C2 x {}_1F_2\left(\frac{1}{3} + \frac{n}{3}; \frac{2}{3}, \frac{4}{3}; \frac{x^3}{9}\right) + -C3 x^2 {}_1F_2\left(\frac{2}{3} + \frac{n}{3}; \frac{4}{3}, \frac{5}{3}; \frac{x^3}{9}\right) \right\}$$

## 5 Kamke chapter 4. Linear fourth order

### 5.1 ODE No. 1534

$$d^4y(x) = 0$$

**Mathematica:** cpu = 0.003000 (sec), leaf count = 24

$$\left\{ \left\{ y(x) \rightarrow c_4 x^3 + c_3 x^2 + c_2 x + c_1 \right\} \right\}$$

**Maple:** cpu = 0.141 (sec), leaf count = 21

$$\left\{ y(x) = \frac{-C1 x^3}{6} + \frac{-C2 x^2}{2} + -C3 x + -C4 \right\}$$

### 5.2 ODE No. 1535

$$d^4y(x) + 4y(x) - f = 0$$

**Mathematica:** cpu = 1.373674 (sec), leaf count = 265

$$\left\{ \left\{ y(x) \rightarrow e^{-x} \left( \cos(x) \int_1^x \frac{1}{8} e^{K[1]} f(K[1]) \left( -\sin^3(K[1]) + \cos^3(K[1]) - \sin(K[1]) \cos^2(K[1]) + \sin^2(K[1]) \right) \right) \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 36

$$\left\{ y(x) = \frac{f}{4} + -C1 e^x \cos(x) + -C2 e^x \sin(x) + -C3 e^{-x} \cos(x) + -C4 e^{-x} \sin(x) \right\}$$

### 5.3 ODE No. 1536

$$d^4y(x) + \lambda y(x) = 0$$

**Mathematica:** cpu = 0.004000 (sec), leaf count = 76

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{(-1)^{3/4} \sqrt[4]{\lambda} x} + c_2 e^{-\sqrt[4]{-1} \sqrt[4]{\lambda} x} + c_3 e^{(-1)^{3/4} \sqrt[4]{\lambda} x} + c_4 e^{\sqrt[4]{-1} \sqrt[4]{\lambda} x} \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 50

$$\left\{ y(x) = -C1 e^{-i \sqrt[4]{-\lambda} x} + -C2 e^{-\sqrt[4]{-\lambda} x} + -C3 e^{i \sqrt[4]{-\lambda} x} + -C4 e^{\sqrt[4]{-\lambda} x} \right\}$$

## 5.4 ODE No. 1537

$$d_4y(x) - 12 \frac{d^2}{dx^2}y(x) + 12y(x) - 16x^4e^{x^2} = 0$$

**Mathematica:** cpu = 0.828605 (sec), leaf count = 1722

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{12} e^{-\left(\sqrt{2(3-\sqrt{6})}-x\right)x - \sqrt{2(3+\sqrt{6})}x - \sqrt{2(3-\sqrt{6})}x} \left( -2\sqrt{3+\sqrt{6}} e^{\sqrt{2(3+\sqrt{6})}x + 2\sqrt{2(3-\sqrt{6})}x} x^3 + 2\sqrt{3+\sqrt{6}} \right) \right. \right.$$

**Maple:** cpu = 0.141 (sec), leaf count = 67

$$\left\{ y(x) = e^{x^2} + \_C1 e^{\sqrt{6-2\sqrt{6}}x} + \_C2 e^{\sqrt{6+2\sqrt{6}}x} + \_C3 e^{-\sqrt{6-2\sqrt{6}}x} + \_C4 e^{-\sqrt{6+2\sqrt{6}}x} \right\}$$

## 5.5 ODE No. 1538

$$d_4y(x) + 2a^2 \frac{d^2}{dx^2}y(x) + a^4y(x) - \cosh(ax) = 0$$

**Mathematica:** cpu = 0.247531 (sec), leaf count = 66

$$\left\{ \left\{ y(x) \rightarrow \frac{\cos^2(ax) \cosh(ax) + \sin^2(ax) \cosh(ax)}{4a^4} + c_3 \sin(ax) + c_4 x \sin(ax) + c_1 \cos(ax) + c_2 x \cos(ax) \right\} \right\}$$

**Maple:** cpu = 0.250 (sec), leaf count = 46

$$\left\{ y(x) = \frac{e^{ax} + e^{-ax}}{8a^4} + \_C1 \cos(ax) + \_C2 \sin(ax) + \_C3 \cos(ax)x + \_C4 \sin(ax)x \right\}$$

## 5.6 ODE No. 1539

$$d_4y(x) + (\lambda + 1) a^2 \frac{d^2}{dx^2}y(x) + \lambda a^4y(x) = 0$$

**Mathematica:** cpu = 0.007001 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow c_2 \sin(a\sqrt{\lambda}x) + c_1 \cos(a\sqrt{\lambda}x) + c_4 \sin(ax) + c_3 \cos(ax) \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 35

$$\left\{ y(x) = \_C1 \sin(ax) + \_C2 \cos(ax) + \_C3 \sin(a\sqrt{\lambda}x) + \_C4 \cos(a\sqrt{\lambda}x) \right\}$$

## 5.7 ODE No. 1540

$$d^4y(x) + a(bx - 1) \frac{d^2}{dx^2}y(x) + ab \frac{d}{dx}y(x) + \lambda y(x) = 0$$

**Mathematica:** cpu = 0.429555 (sec), leaf count = 67

$$\{ \{y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{\lambda y(x) + aby'(x) + a(bx - 1)y''(x) + y^{(4)}(x) = 0, y(0) = c_1, y'(0) = c_2\}) \}$$

**Maple:** cpu = 0.094 (sec), leaf count = 44

$$\left\{ y(x) = \text{DESol} \left( \left\{ \lambda \_Y(x) + ab \frac{d}{dx} \_Y(x) + a(bx - 1) \frac{d^2}{dx^2} \_Y(x) + \frac{d^4}{dx^4} \_Y(x) \right\}, \{ \_Y(x) \} \right) \right\}$$

## 5.8 ODE No. 1541

$$d^4y(x) + (ax^2 + b\lambda + c) \frac{d^2}{dx^2}y(x) + (ax^2 + \beta\lambda + \gamma) y(x) = 0$$

**Mathematica:** cpu = 80.218186 (sec), leaf count = 73

$$\{ \{y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{(ax^2 + \beta\lambda + \gamma) y(x) + (ax^2 + c + b\lambda) y''(x) + y^{(4)}(x) = 0, y(0) = c_1\}) \}$$

**Maple:** cpu = 0.062 (sec), leaf count = 50

$$\left\{ y(x) = \text{DESol} \left( \left\{ (ax^2 + \beta\lambda + \gamma) \_Y(x) + (ax^2 + b\lambda + c) \frac{d^2}{dx^2} \_Y(x) + \frac{d^4}{dx^4} \_Y(x) \right\}, \{ \_Y(x) \} \right) \right\}$$

## 5.9 ODE No. 1542

$$d^4y(x) + a \text{WeierstrassP}(x, g2, g3) \frac{d^2}{dx^2}y(x) + b \text{WeierstrassPPrime}(x, g2, g3) \frac{d}{dx}y(x) + (c(6(\text{WeierstrassP}(x, g2, g3))^2 - \frac{g2}{2}) + d) y(x) = 0$$

**Mathematica:** cpu = 0.029004 (sec), leaf count = 55

$$\text{DSolve} \left[ ay''(x)\wp(x; g2, g3) + by'(x)\wp'(x; g2, g3) + y(x) \left( c \left( 6\wp(x; g2, g3)^2 - \frac{g2}{2} \right) + d \right) + y^{(4)}(x) = 0, y(x) \right]$$

**Maple:** cpu = 0.561 (sec), leaf count = 60

$$\left\{ y(x) = \text{DESol} \left( \left\{ \frac{d^4}{dx^4} \_Y(x) + a \text{WeierstrassP}(x, g2, g3) \frac{d^2}{dx^2} \_Y(x) + b \text{WeierstrassPPrime}(x, g2, g3) \frac{d}{dx} \_Y(x) + (c(6(\text{WeierstrassP}(x, g2, g3))^2 - \frac{g2}{2}) + d) \_Y(x) \right\}, \{ \_Y(x) \} \right) \right\}$$

## 5.10 ODE No. 1543

$$d^4y(x) - (12k^2(\text{JacobiSN}(z, x))^2 + a) \frac{d^2}{dx^2}y(x) + b \frac{d}{dx}y(x) + (\alpha(\text{JacobiSN}(z, x))^2 + \beta)y(x) = 0$$

**Mathematica:** cpu = 0.100013 (sec), leaf count = 47

$$\text{DSolve}[-y''(x)(a + 12k^2\text{sn}(z|x)^2) + y(x)(\alpha\text{sn}(z|x)^2 + \beta) + by'(x) + y^{(4)}(x) = 0, y(x), x]$$

**Maple:** cpu = 5.319 (sec), leaf count = 59

$$\left\{ y(x) = \text{DESol} \left( \left\{ \frac{d^4}{dx^4} Y(x) + (-12k^2(\text{JacobiSN}(z, x))^2 - a) \frac{d^2}{dx^2} Y(x) + b \frac{d}{dx} Y(x) + (\alpha(\text{JacobiSN}(z, x))^2 + \beta) Y(x) \right\} \right) \right.$$

## 5.11 ODE No. 1544

$$d^4y(x) + 10f \frac{d^2}{dx^2}y(x) + 10df \frac{d}{dx}y(x) + (3f^2 + 3ddf)y(x) = 0$$

**Mathematica:** cpu = 0.014502 (sec), leaf count = 45

$$\text{DSolve}[y(x)(3f''(x) + 3f(x)^2) + 10f'(x)y'(x) + 10f(x)y''(x) + y^{(4)}(x) = 0, y(x), x]$$

**Maple:** cpu = 0.0 (sec), leaf count = 41

$$\left\{ y(x) = \sum_{a=1}^4 e^{\text{RootOf}(-Z^4 + 10fZ^2 + 10dfZ + 3f^2 + 3ddf, \text{index}=_a)x} \_C_{_a} \right\}$$

## 5.12 ODE No. 1545

$$d^4y(x) + 2 \frac{d^3}{dx^3}y(x) - 3 \frac{d^2}{dx^2}y(x) - 4 \frac{d}{dx}y(x) + 4y(x) - 32 \sin(2x) + 24 \cos(2x) = 0$$

**Mathematica:** cpu = 0.164521 (sec), leaf count = 40

$$\left\{ \left\{ y(x) \rightarrow c_1 e^{-2x} + c_2 e^{-2x} x + c_3 e^x + c_4 e^x x + \sin(2x) \right\} \right\}$$

**Maple:** cpu = 0.046 (sec), leaf count = 31

$$\{y(x) = \sin(2x) + \_C1 e^x + \_C2 e^{-2x} + \_C3 x e^x + \_C4 e^{-2x} x\}$$



### 5.13 ODE No. 1546

$$d^4y(x) + 4ax \frac{d^3}{dx^3}y(x) + 6a^2x^2 \frac{d^2}{dx^2}y(x) + 4a^3x^3 \frac{d}{dx}y(x) + a^4x^4y(x) = 0$$

**Mathematica:** cpu = 0.649083 (sec), leaf count = 301

$$\left\{ \left\{ y(x) \rightarrow \frac{2(\sqrt{6}-3) \sqrt{-(\sqrt{6}-3)} ac_3 \exp\left(-\frac{ax^2}{2} - \sqrt{-(\sqrt{6}-3)} ax - \frac{(-3+\sqrt{3}+\sqrt{6})ax}{\sqrt{-(\sqrt{6}-3)a}}\right)}{(-3-\sqrt{3}+\sqrt{6})(-3+\sqrt{3}+\sqrt{6})a} + \dots \right. \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 81

$$\left\{ y(x) = e^{-\frac{ax^2}{2}} \left( \_C1 e^{-\sqrt{-a\sqrt{6}+3}ax} + \_C2 e^{\sqrt{-a\sqrt{6}+3}ax} + \_C3 e^{-\sqrt{a\sqrt{6}+3}ax} + \_C4 e^{\sqrt{a\sqrt{6}+3}ax} \right) \right\}$$

### 5.14 ODE No. 1547

$$d^4y(x) + 6f \frac{d^3}{dx^3}y(x) + (11f^2 + 4df + 10g) \frac{d^2}{dx^2}y(x) + (6f^3 + 7df^2 + 30fg +ddf + 10dg) \frac{d}{dx}y(x) + \dots$$

**Mathematica:** cpu = 0.034504 (sec), leaf count = 116

$$\text{DSolve}[3y(x) (2g(x)f'(x) + 5f(x)g'(x) + 6f(x)^2g(x) + g''(x) + 3g(x)^2) + y''(x) (4f'(x) + 11f(x)^2 + 10g$$

**Maple:** cpu = 0.015 (sec), leaf count = 87

$$\left\{ y(x) = \sum_{a=1}^4 e^{\text{RootOf}(\_Z^4+6f\_Z^3+(11f^2+4df+10g)\_Z^2+(6f^3+7df^2+30fg+ddf+10dg)\_Z+18f^2g+6dfg+15dgg+9g^2+3ddg, \_a=1)} \right\}$$

### 5.15 ODE No. 1548

$$4d^4y(x) - 12 \frac{d^3}{dx^3}y(x) + 11 \frac{d^2}{dx^2}y(x) - 3 \frac{d}{dx}y(x) - 4 \cos(x) = 0$$

**Mathematica:** cpu = 0.098513 (sec), leaf count = 50

$$\left\{ \left\{ y(x) \rightarrow 2c_1 e^{x/2} + \frac{2}{3} c_2 e^{3x/2} + c_3 e^x + c_4 + \frac{18 \sin(x)}{65} - \frac{14 \cos(x)}{65} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 32

$$\left\{ y(x) = -\frac{14 \cos(x)}{65} + \frac{18 \sin(x)}{65} + \_C1 e^x + 2 \_C2 e^{x/2} + \frac{2 \_C3}{3} e^{\frac{3x}{2}} + \_C4 \right\}$$

## 5.16 ODE No. 1549

$$x d^4 y(x) + 5 \frac{d^3}{dx^3} y(x) - 24 = 0$$

**Mathematica:** cpu = 0.012002 (sec), leaf count = 34

$$\left\{ \left\{ y(x) \rightarrow c_4 x^2 - \frac{c_1}{24 x^2} + c_3 x + c_2 + \frac{4 x^3}{5} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 26

$$\left\{ y(x) = -\frac{C1}{24 x^2} + \frac{4 x^3}{5} + \frac{C2 x^2}{2} + C3 x + C4 \right\}$$

## 5.17 ODE No. 1550

$$x d^4 y(x) - (6 x^2 + 1) \frac{d^3}{dx^3} y(x) + 12 x^3 \frac{d^2}{dx^2} y(x) - (9 x^2 - 7) x^2 \frac{d}{dx} y(x) + 2 (x^2 - 3) x^3 y(x) = 0$$

**Mathematica:** cpu = 7.686976 (sec), leaf count = 262

$$\left\{ \left\{ y(x) \rightarrow c_3 e^{\frac{x^2}{2}} \int_1^x \frac{e^{\frac{K[1]^2}{2}} K[1] \left( \int \frac{U\left(\frac{1}{20}(-5-9\sqrt{5}), -\frac{1}{2}, \frac{1}{2}\sqrt{5}K[1]^2\right) \exp\left(\frac{1}{2}(-\frac{1}{2}K[1]^2 - 2\log(K[1])) - \frac{1}{4}\sqrt{5}K[1]^2\right)}{\sqrt{K[1]} \sqrt[4]{K[1]^2}} dK[1]\right)}{dK[1]} dK[1]}{\sqrt[4]{2}} \right. \right\}$$

**Maple:** cpu = 0.390 (sec), leaf count = 159

$$\left\{ y(x) = C1 e^{x^2} + C2 e^{\frac{x^2}{2}} + C3 \left( -e^{x^2} \int 1 M_{\frac{9\sqrt{5}}{20}, \frac{3}{4}} \left( \frac{\sqrt{5}x^2}{2} \right) e^{-\frac{x^2}{4}} x^{-\frac{3}{2}} dx + \int 1 M_{\frac{9\sqrt{5}}{20}, \frac{3}{4}} \left( \frac{\sqrt{5}x^2}{2} \right) e^{\frac{x^2}{4}} dx \right) \right\}$$

## 5.18 ODE No. 1551

$$x^2 d^4 y(x) - 2(\nu^2 x^2 + 6) \frac{d^2}{dx^2} y(x) + \nu^2(\nu^2 x^2 + 4) y(x) = 0$$

**Mathematica:** cpu = 0.443556 (sec), leaf count = 110

$$\left\{ \left\{ y(x) \rightarrow \frac{c_3(1-x)e^{-\nu x}(\nu^2 x^2 + \nu^2 x + \nu^2 + 6\nu x + 6\nu + 15)}{x} + \frac{c_4(1-x)e^{\nu x}(\nu^2 x^2 + \nu^2 x + \nu^2 - 6\nu x - 6\nu)}{x} \right\} \right\}$$

**Maple:** cpu = 0.110 (sec), leaf count = 63

$$\left\{ y(x) = \frac{C1 e^{\nu x}}{x} + \frac{C2 e^{-\nu x}}{x} + C3 e^{\nu x}(\nu^2 x^2 - 6\nu x + 15) + C4 e^{-\nu x}(\nu^2 x^2 + 6\nu x + 15) \right\}$$

### 5.19 ODE No. 1552

$$x^2 d^4 y(x) + 2x \frac{d^3}{dx^3} y(x) + ay(x) - bx^2 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.047 (sec), leaf count = 89

$$\left\{ y(x) = \frac{bx^2}{a} + \_C1 \sqrt{x} J_1(2 \sqrt[4]{-a} \sqrt{x}) + \_C2 \sqrt{x} Y_1(2 \sqrt[4]{-a} \sqrt{x}) + \_C3 \sqrt{x} J_1\left(2 \sqrt{-\sqrt{-a} \sqrt{x}}\right) + \_C4 \right.$$

### 5.20 ODE No. 1553

$$x^2 d^4 y(x) + 4x \frac{d^3}{dx^3} y(x) + 2 \frac{d^2}{dx^2} y(x) = 0$$

**Mathematica:** cpu = 0.021503 (sec), leaf count = 29

$$\{ \{ y(x) \rightarrow c_1(-x) + c_4 x + c_1 x \log(x) - c_2 \log(x) + c_3 \} \}$$

**Maple:** cpu = 0.031 (sec), leaf count = 18

$$\{ y(x) = \_C1 x + \_C2 x \ln(x) + \_C3 + \_C4 \ln(x) \}$$

### 5.21 ODE No. 1554

$$x^2 d^4 y(x) + 6x \frac{d^3}{dx^3} y(x) + 6 \frac{d^2}{dx^2} y(x) = 0$$

**Mathematica:** cpu = 0.021503 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow c_4 x + \frac{1}{2} \left( \frac{c_2}{x} - 2c_1 \log(x) \right) + c_3 \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 18

$$\left\{ y(x) = \_C1 + \_C2 \ln(x) + \frac{\_C3}{x} + \_C4 x \right\}$$

## 5.22 ODE No. 1555

$$x^2 d_4 y(x) + 6x \frac{d^3}{dx^3} y(x) + 6 \frac{d^2}{dx^2} y(x) - \lambda^2 y(x) = 0$$

**Mathematica:** cpu = 0.060008 (sec), leaf count = 156

$$\left\{ \left\{ y(x) \rightarrow c_4 G_{0,4}^{2,0} \left( \frac{\lambda^2 x^2}{16} \mid -\frac{1}{2}, \frac{1}{2}, 0, 0 \right) + c_2 G_{0,4}^{2,0} \left( \frac{\lambda^2 x^2}{16} \mid 0, 0, -\frac{1}{2}, \frac{1}{2} \right) + \frac{c_1 \left( J_1(2\sqrt{\lambda}\sqrt{x}) + I_1(2\sqrt{\lambda}\sqrt{x}) \right)}{2\sqrt{\lambda}\sqrt{x}} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 69

$$\left\{ y(x) = -C1 J_1(2\sqrt{\lambda}\sqrt{x}) \frac{1}{\sqrt{x}} + -C2 Y_1(2\sqrt{\lambda}\sqrt{x}) \frac{1}{\sqrt{x}} + -C3 J_1(2\sqrt{-\lambda}\sqrt{x}) \frac{1}{\sqrt{x}} + -C4 Y_1(2\sqrt{-\lambda}\sqrt{x}) \frac{1}{\sqrt{x}} \right\}$$

## 5.23 ODE No. 1556

$$x^2 d_4 y(x) + 8x \frac{d^3}{dx^3} y(x) + 12 \frac{d^2}{dx^2} y(x) = 0$$

**Mathematica:** cpu = 0.020002 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{6} \left( \frac{c_1}{x^2} + \frac{3c_2}{x} \right) + c_4 x + c_3 \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 19

$$\left\{ y(x) = -C1 + \frac{-C2}{x} + \frac{-C3}{x^2} + -C4 x \right\}$$

## 5.24 ODE No. 1557

$$x^2 d_4 y(x) + 8x \frac{d^3}{dx^3} y(x) + 12 \frac{d^2}{dx^2} y(x) - \lambda^2 y(x) = 0$$

**Mathematica:** cpu = 0.063008 (sec), leaf count = 146

$$\left\{ \left\{ y(x) \rightarrow c_4 G_{0,4}^{2,0} \left( \frac{\lambda^2 x^2}{16} \mid -1, 0, -\frac{1}{2}, \frac{1}{2} \right) + c_2 G_{0,4}^{2,0} \left( \frac{\lambda^2 x^2}{16} \mid -\frac{1}{2}, \frac{1}{2}, -1, 0 \right) - \frac{3ic_1 \left( I_2(2\sqrt{\lambda}\sqrt{x}) - J_2(2\sqrt{\lambda}\sqrt{x}) \right)}{4\lambda x} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 69

$$\left\{ y(x) = \frac{-C1}{x} J_2(2\sqrt{\lambda}\sqrt{x}) + \frac{-C2}{x} Y_2(2\sqrt{\lambda}\sqrt{x}) + \frac{-C3}{x} J_2(2\sqrt{-\lambda}\sqrt{x}) + \frac{-C4}{x} Y_2(2\sqrt{-\lambda}\sqrt{x}) \right\}$$

## 5.25 ODE No. 1558

$$x^2 d_4 y(x) + (2n - 2\nu + 4) x \frac{d^3}{dx^3} y(x) + (n - \nu + 1)(n - \nu + 2) \frac{d^2}{dx^2} y(x) - 1/16 b^4 y(x) = 0$$

**Mathematica:** cpu = 0.160520 (sec), leaf count = 319

$$\left\{ \left\{ y(x) \rightarrow c_4 i^{-n+\nu+1} 2^{3n-3\nu-3} b^{2(-n+\nu+1)+n-\nu-2} x^{\frac{1}{2}(n-\nu-2)-n+\nu+1} \Gamma(-n+\nu+2) (I_{\nu-n}(b\sqrt{x}) - J_{\nu-n}(b\sqrt{x})) \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 93

$$\{y(x) = \_C1 x^{-\frac{n}{2}+\frac{\nu}{2}} I_{n-\nu}(b\sqrt{x}) + \_C2 x^{-\frac{n}{2}+\frac{\nu}{2}} J_{n-\nu}(b\sqrt{x}) + \_C3 x^{-\frac{n}{2}+\frac{\nu}{2}} K_{n-\nu}(b\sqrt{x}) + \_C4 x^{-\frac{n}{2}+\frac{\nu}{2}} Y_{n-\nu}\}$$

## 5.26 ODE No. 1559

$$x^3 d_4 y(x) + 2x^2 \frac{d^3}{dx^3} y(x) - x \frac{d^2}{dx^2} y(x) + \frac{d}{dx} y(x) - a^4 x^3 y(x) = 0$$

**Mathematica:** cpu = 0.264534 (sec), leaf count = 100

$$\left\{ \left\{ y(x) \rightarrow c_4 G_{0,4}^{2,0} \left( \frac{a^4 x^4}{256} \mid 0, 0, \frac{1}{2}, \frac{1}{2} \right) + c_2 G_{0,4}^{2,0} \left( \frac{a^4 x^4}{256} \mid \frac{1}{2}, \frac{1}{2}, 0, 0 \right) + \frac{1}{8} i c_1 (I_0(ax) - J_0(ax)) + \frac{1}{2} c_3 (J_0(ax) - Y_0(ax)) \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 33

$$\{y(x) = \_C1 I_0(ax) + \_C2 J_0(ax) + \_C3 K_0(ax) + \_C4 Y_0(ax)\}$$

## 5.27 ODE No. 1560

$$x^3 d_4 y(x) + 6x^2 \frac{d^3}{dx^3} y(x) + 6x \frac{d^2}{dx^2} y(x) = 0$$

**Mathematica:** cpu = 0.020003 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow c_4 x + \frac{1}{2} \left( \frac{c_2}{x} - 2c_1 \log(x) \right) + c_3 \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 18

$$\left\{ y(x) = \_C1 + \_C2 \ln(x) + \frac{\_C3}{x} + \_C4 x \right\}$$

## 5.28 ODE No. 1561

$$x^4 d^4 y(x) - 2n(n+1)x^2 \frac{d^2}{dx^2} y(x) + 4n(n+1)x \frac{d}{dx} y(x) + (ax^4 + n(n+1)(n+3)(n-2))y(x) = 0$$

**Mathematica:** cpu = 3.736975 (sec), leaf count = 400

$$\left\{ \left\{ y(x) \rightarrow c_1 \left( -2^{n-\frac{5}{2}} \right) \sqrt{x} a^{\frac{2-n}{4} + \frac{1}{4}(n-\frac{3}{2})} \Gamma\left(\frac{3}{2} - n\right) \left( \cos\left(\frac{3}{4}\pi\left(\frac{3}{2} - n\right)\right) \text{ber}_{-n-\frac{1}{2}}(\sqrt[4]{ax}) + \sin\left(\frac{3}{4}\pi\left(\frac{3}{2} - n\right)\right) \text{ber}_{-n-\frac{1}{2}}(\sqrt[4]{ax}) \right) \right. \right.$$

**Maple:** cpu = 0.140 (sec), leaf count = 77

$$\left\{ y(x) = \_C1 \sqrt{x} J_{n+\frac{1}{2}}(\sqrt[4]{-ax}) + \_C2 \sqrt{x} Y_{n+\frac{1}{2}}(\sqrt[4]{-ax}) + \_C3 \sqrt{x} J_{n+\frac{1}{2}}\left(\sqrt{-\sqrt{-ax}}\right) + \_C4 \sqrt{x} Y_{n+\frac{1}{2}}\left(\sqrt{-\sqrt{-ax}}\right) \right.$$

## 5.29 ODE No. 1562

$$x^4 d^4 y(x) + 4x^3 \frac{d^3}{dx^3} y(x) - (4n^2 - 1)x^2 \frac{d^2}{dx^2} y(x) + (4n^2 - 1)x \frac{d}{dx} y(x) - 4y(x)x^4 = 0$$

**Mathematica:** cpu = 1.107641 (sec), leaf count = 140

$$\left\{ \left\{ y(x) \rightarrow c_1 {}_0F_3\left(\frac{1}{2}, 1 - \frac{n}{2}, \frac{n}{2} + 1; \frac{x^4}{64}\right) + \frac{1}{8} i c_2 x^2 {}_0F_3\left(\frac{3}{2}, \frac{3}{2} - \frac{n}{2}, \frac{n}{2} + \frac{3}{2}; \frac{x^4}{64}\right) + c_3 \left(\frac{i}{2}\right)^{-n} \Gamma(1-n)^2 \right. \right.$$

**Maple:** cpu = 0.187 (sec), leaf count = 93

$$\left\{ y(x) = \_C1 J_n\left(\left(\frac{1}{2} - \frac{i}{2}\right)\sqrt{2x}\right) J_n\left(\left(\frac{1}{2} + \frac{i}{2}\right)\sqrt{2x}\right) + \_C2 J_n\left(\left(\frac{1}{2} - \frac{i}{2}\right)\sqrt{2x}\right) Y_n\left(\left(\frac{1}{2} + \frac{i}{2}\right)\sqrt{2x}\right) \right.$$

## 5.30 ODE No. 1563

$$x^4 d^4 y(x) + 4x^3 \frac{d^3}{dx^3} y(x) - (4n^2 - 1)x^2 \frac{d^2}{dx^2} y(x) - (4n^2 - 1)x \frac{d}{dx} y(x) + (-4x^4 + 4n^2 - 1)y(x) = 0$$

**Mathematica:** cpu = 1.852235 (sec), leaf count = 232

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt{-1} c_2 x {}_0F_3\left(\frac{3}{2}, 1 - \frac{n}{2}, \frac{n}{2} + 1; \frac{x^4}{64}\right)}{2\sqrt{2}} - \frac{2(-1)^{3/4} \sqrt{2} c_1 {}_0F_3\left(\frac{1}{2}, \frac{1}{2} - \frac{n}{2}, \frac{n}{2} + \frac{1}{2}; \frac{x^4}{64}\right)}{x} + c_3 (-1)^{\frac{1}{4}(1-2n)} \right. \right.$$

**Maple:** cpu = 0.110 (sec), leaf count = 83

$$\left\{ y(x) = \_C1 x((\text{ber}_n(x))^2 + (\text{bei}_n(x))^2) + \_C2 x((\text{ber}_{-n}(x))^2 + (\text{bei}_{-n}(x))^2) + \_C3 x {}_0F_3\left(\frac{3}{2}, 1 - \frac{n}{2}, \frac{n}{2} + 1; \frac{x^4}{64}\right) \right.$$

### 5.31 ODE No. 1564

$$x^4 d^4 y(x) + 4x^3 \frac{d^3}{dx^3} y(x) - (4n^2 + 3)x^2 \frac{d^2}{dx^2} y(x) + (12n^2 - 3)x \frac{d}{dx} y(x) - (4x^4 + 12n^2 - 3)y(x) = 0$$

**Mathematica:** cpu = 1.386176 (sec), leaf count = 230

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt[4]{-1} c_1 x {}_0F_3\left(\frac{1}{2}, \frac{3}{2} - \frac{n}{2}, \frac{n}{2} + \frac{3}{2}, \frac{x^4}{64}\right)}{2\sqrt{2}} + c_3 (-1)^{\frac{1}{4}(-2n-1)} 2^{2n+\frac{1}{2}(2n+1)+1} x^{-2n-1} {}_0F_3\left(1-n, \frac{1}{2} - \frac{n}{2}, \frac{n}{2}\right) \right. \right.$$

**Maple:** cpu = 0.156 (sec), leaf count = 156

$$\left\{ y(x) = \frac{-C1 ((\text{ber}_n(x))^2 + (\text{bei}_n(x))^2)}{x} + {}_2F_3\left(\frac{3}{2}, 2 - \frac{n}{2}, 2 + \frac{n}{2}; \frac{x^4}{64}\right) + {}_0F_3\left(\frac{1}{2}, \frac{3}{2} + \frac{n}{2}, \frac{n}{2}\right) \right.$$

### 5.32 ODE No. 1565

$$x^4 d^4 y(x) + 6x^3 \frac{d^3}{dx^3} y(x) + (4x^4 + (-\rho^2 - \sigma^2 + 7)x^2) \frac{d^2}{dx^2} y(x) + (16x^3 + (-\rho^2 - \sigma^2 + 1)x) \frac{d}{dx} y(x) +$$

**Mathematica:** cpu = 0.518066 (sec), leaf count = 242

$$\left\{ \left\{ y(x) \rightarrow c_1 x^{-\rho} {}_2F_3\left(\frac{1}{2} - \frac{\rho}{2}, 1 - \frac{\rho}{2}; 1 - \rho, -\frac{\rho}{2} - \frac{\sigma}{2} + 1, -\frac{\rho}{2} + \frac{\sigma}{2} + 1; -x^2\right) + c_3 x^{-\sigma} {}_2F_3\left(\frac{1}{2} - \frac{\sigma}{2}, 1 - \frac{\sigma}{2}; \right. \right.$$

**Maple:** cpu = 0.171 (sec), leaf count = 85

$$\left\{ y(x) = {}_2F_3\left(\frac{\rho}{2} + \frac{\sigma}{2}, \frac{\rho}{2} - \frac{\sigma}{2}; \right) + {}_2F_3\left(\frac{\rho}{2} + \frac{\sigma}{2}, \frac{\rho}{2} - \frac{\sigma}{2}; \right) + {}_2F_3\left(\frac{\rho}{2} + \frac{\sigma}{2}, \frac{\rho}{2} - \frac{\sigma}{2}; \right) + {}_2F_3\left(\frac{\rho}{2} + \frac{\sigma}{2}, \frac{\rho}{2} - \frac{\sigma}{2}; \right) \right.$$

### 5.33 ODE No. 1566

$$x^4 d^4 y(x) + 6x^3 \frac{d^3}{dx^3} y(x) + (4x^4 + (-2\mu^2 - 2\nu^2 + 7)x^2) \frac{d^2}{dx^2} y(x) + (16x^3 + (-2\mu^2 - 2\nu^2 + 1)x) \frac{d}{dx} y(x) +$$

**Mathematica:** cpu = 0.620079 (sec), leaf count = 238

$$\left\{ \left\{ y(x) \rightarrow c_1 x^{-\mu-\nu} {}_2F_3\left(-\frac{\mu}{2} - \frac{\nu}{2} + \frac{1}{2}, -\frac{\mu}{2} - \frac{\nu}{2} + 1; 1 - \mu, 1 - \nu, -\mu - \nu + 1; -x^2\right) + c_2 x^{\mu-\nu} {}_2F_3\left(\frac{\mu}{2} - \frac{\nu}{2}, \frac{\mu}{2} + \frac{\nu}{2}; \right. \right.$$

**Maple:** cpu = 0.156 (sec), leaf count = 37

$$\left\{ y(x) = {}_2F_3(\nu, \mu; \nu, \mu; x) + {}_2F_3(\nu, \mu; \nu, \mu; x) + {}_2F_3(\nu, \mu; \nu, \mu; x) + {}_2F_3(\nu, \mu; \nu, \mu; x) \right\}$$

### 5.34 ODE No. 1567

$$x^4 d^4 y(x) + 8 x^3 \frac{d^3}{dx^3} y(x) + 12 x^2 \frac{d^2}{dx^2} y(x) = 0$$

**Mathematica:** cpu = 0.020503 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{6} \left( \frac{c_1}{x^2} + \frac{3c_2}{x} \right) + c_4 x + c_3 \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 19

$$\left\{ y(x) = \_C1 + \frac{\_C2}{x} + \frac{\_C3}{x^2} + \_C4 x \right\}$$

### 5.35 ODE No. 1568

$$x^4 d^4 y(x) + 8 x^3 \frac{d^3}{dx^3} y(x) + 12 x^2 \frac{d^2}{dx^2} y(x) + a y(x) = 0$$

**Mathematica:** cpu = 0.157020 (sec), leaf count = 378

$$\left\{ \left\{ y(x) \rightarrow c_1 b^{\frac{a-c\mu-c\nu}{c}} (x^{2c})^{\frac{a-c\mu-c\nu}{2c}} {}_2F_3 \left( -\frac{\mu}{2} - \frac{\nu}{2} + \frac{1}{2}, -\frac{\mu}{2} - \frac{\nu}{2} + 1; 1 - \mu, 1 - \nu, -\mu - \nu + 1; -b^2 x^{2c} \right) + c_2 \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 89

$$\left\{ y(x) = \_C1 x^{-\frac{1}{2}-\frac{1}{2}\sqrt{5-4\sqrt{1-a}}} + \_C2 x^{-\frac{1}{2}+\frac{1}{2}\sqrt{5-4\sqrt{1-a}}} + \_C3 x^{-\frac{1}{2}-\frac{1}{2}\sqrt{5+4\sqrt{1-a}}} + \_C4 x^{-\frac{1}{2}+\frac{1}{2}\sqrt{5+4\sqrt{1-a}}} \right\}$$

### 5.36 ODE No. 1569

$$x^4 d^4 y(x) + (6 - 4a) x^3 \frac{d^3}{dx^3} y(x) + (4b^2 c^2 x^{2c} + 6(a - 1)^2 - 2c^2(\mu^2 + \nu^2) + 1) x^2 \frac{d^2}{dx^2} y(x) + (4(3c - 2a) - 2c^2(\mu^2 + \nu^2)) x \frac{d}{dx} y(x) + (2c^2(\mu^2 + \nu^2) - 2a) y(x) = 0$$

**Mathematica:** cpu = 0.152019 (sec), leaf count = 378

$$\left\{ \left\{ y(x) \rightarrow c_1 b^{\frac{a-c\mu-c\nu}{c}} (x^{2c})^{\frac{a-c\mu-c\nu}{2c}} {}_2F_3 \left( -\frac{\mu}{2} - \frac{\nu}{2} + \frac{1}{2}, -\frac{\mu}{2} - \frac{\nu}{2} + 1; 1 - \mu, 1 - \nu, -\mu - \nu + 1; -b^2 x^{2c} \right) + c_2 \right\} \right\}$$

**Maple:** cpu = 0.218 (sec), leaf count = 81

$$\{ y(x) = \_C1 x^a J_\mu(x^c b) Y_\nu(x^c b) + \_C2 x^a J_\nu(x^c b) Y_\mu(x^c b) + \_C3 x^a J_\nu(x^c b) Y_\mu(x^c b) + \_C4 x^a Y_\nu(x^c b) Y_\mu(x^c b) \}$$



### 5.37 ODE No. 1570

$$x^4 d^4 y(x) + (6 - 4a - 4c) x^3 \frac{d^3}{dx^3} y(x) + (-2\nu^2 c^2 + 2a^2 + 4(a+c-1)^2 + 4(a-1)(c-1) - 1) x^2 \frac{d^2}{dx^2} y(x) - 6ax \frac{d}{dx} y(x) + 6a^2 y(x) = 0$$

**Mathematica:** cpu = 0.154020 (sec), leaf count = 470

$$\left\{ \left\{ y(x) \rightarrow c_1 \Gamma(1-\nu) (-1)^{\frac{a-c\nu}{4c}} 2^{-\frac{2(a-c\nu)}{c}} -\nu-1 b^{\frac{a-c\nu}{c}+\nu} (x^{4c})^{\frac{a-c\nu}{4c}+\frac{\nu}{4}} \left( J_{-\nu} \left( b\sqrt[4]{x^{4c}} \right) + I_{-\nu} \left( b\sqrt[4]{x^{4c}} \right) \right) + c_2 \Gamma(2-\nu) (-1)^{\frac{a-c\nu}{4c}} 2^{-\frac{2(a-c\nu)}{c}} -\nu-1 b^{\frac{a-c\nu}{c}+\nu} (x^{4c})^{\frac{a-c\nu}{4c}+\frac{\nu}{4}} \left( J_{-\nu} \left( b\sqrt[4]{x^{4c}} \right) - I_{-\nu} \left( b\sqrt[4]{x^{4c}} \right) \right) \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 57

$$\{y(x) = \_C1 x^a J_\nu(x^c b) + \_C2 x^a Y_\nu(x^c b) + \_C3 x^a J_\nu(ibx^c) + \_C4 x^a Y_\nu(ibx^c)\}$$

### 5.38 ODE No. 1571

$$\nu^4 x^4 d^4 y(x) + (4\nu - 2) \nu^3 x^3 \frac{d^3}{dx^3} y(x) + (\nu - 1)(2\nu - 1) \nu^2 x^2 \frac{d^2}{dx^2} y(x) - 1/16 b^4 x^{2\nu-1} y(x) = 0$$

**Mathematica:** cpu = 0.094012 (sec), leaf count = 390

$$\left\{ \left\{ y(x) \rightarrow c_1 {}_0F_3 \left( ; 1 - \frac{\nu}{2}, 1 - \frac{\nu}{2\nu}, -\frac{\nu}{2\nu} - \frac{\nu}{2} + 1; \frac{b^4 \nu^4 x^{2/\nu}}{256 \nu^4} \right) + c_2 \left( \frac{i}{16} \right)^\nu v^{2\nu} b^{2\nu} \nu^{-2\nu} (x^{2/\nu})^{\nu/2} {}_0F_3 \left( ; \frac{\nu}{2} + 1, \frac{\nu}{2} + 1, \frac{\nu}{2} + 1; -\frac{b^4 \nu^4 x^{2/\nu}}{256 \nu^4} \right) \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 151

$$\left\{ y(x) = \_C1 \sqrt{x} J_{(\lfloor \nu^{-1} \rfloor)^{-1}} \left( \frac{1}{\lfloor \nu^{-1} \rfloor} \sqrt{\frac{b^2}{\nu^2}} x^{\frac{\lfloor \nu^{-1} \rfloor}{2}} \right) + \_C2 \sqrt{x} Y_{(\lfloor \nu^{-1} \rfloor)^{-1}} \left( \frac{1}{\lfloor \nu^{-1} \rfloor} \sqrt{\frac{b^2}{\nu^2}} x^{\frac{\lfloor \nu^{-1} \rfloor}{2}} \right) + \_C3 \sqrt{x} J_{(\lfloor \nu^{-1} \rfloor)^{-1}} \left( \frac{1}{\lfloor \nu^{-1} \rfloor} \sqrt{\frac{b^2}{\nu^2}} x^{\frac{\lfloor \nu^{-1} \rfloor}{2}} \right) + \_C4 \sqrt{x} Y_{(\lfloor \nu^{-1} \rfloor)^{-1}} \left( \frac{1}{\lfloor \nu^{-1} \rfloor} \sqrt{\frac{b^2}{\nu^2}} x^{\frac{\lfloor \nu^{-1} \rfloor}{2}} \right) \right\}$$

### 5.39 ODE No. 1572

$$(x^2 - 1)^2 d^4 y(x) + 10x(x^2 - 1) \frac{d^3}{dx^3} y(x) + (24x^2 - 8 - 2(\mu(\mu + 1) + \nu(\nu + 1))(x^2 - 1)) \frac{d^2}{dx^2} y(x) - 6x(\mu^2 + \mu + \nu^2 + \nu) \frac{d}{dx} y(x) + 6(\mu^2 + \mu + \nu^2 + \nu) y(x) = 0$$

**Mathematica:** cpu = 93.272844 (sec), leaf count = 174

$$\{ \{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{(\mu - \nu - 1)(\mu - \nu + 1)(\mu + \nu)(\mu + \nu + 2)y(x) - 6x(\mu^2 + \mu + \nu^2 + \nu) \frac{d}{dx} y(x) + 6(\mu^2 + \mu + \nu^2 + \nu) y(x)\}) \}$$

**Maple:** cpu = 0.203 (sec), leaf count = 37

$$\{y(x) = \_C1 \text{LegendreP}(\nu, x) \text{LegendreP}(\mu, x) + \_C2 \text{LegendreP}(\nu, x) \text{LegendreQ}(\mu, x) + \_C3 \text{LegendreQ}(\nu, x) \text{LegendreP}(\mu, x) + \_C4 \text{LegendreQ}(\nu, x) \text{LegendreQ}(\mu, x)\}$$

## 5.40 ODE No. 1573

$$(e^x + 2x) d^4y(x) + 4(e^x + 2) \frac{d^3}{dx^3}y(x) + 6e^x \frac{d^2}{dx^2}y(x) + 4e^x \frac{d}{dx}y(x) + y(x)e^x - x^{-5} = 0$$

**Mathematica:** cpu = 0.054507 (sec), leaf count = 59

$$\text{DSolve} \left[ -\frac{1}{x^5} + (2x + e^x) y^{(4)}(x) + 4(e^x + 2) y^{(3)}(x) + 6e^x y''(x) + 4e^x y'(x) + e^x y(x) = 0, y(x), x \right]$$

**Maple:** cpu = 0.016 (sec), leaf count = 65

$$\left\{ y(x) = \frac{-C_4}{e^x + 2x} + \frac{-C_1 x^3}{e^x + 2x} + \frac{-C_2 x^2}{e^x + 2x} + \frac{-C_3 x}{e^x + 2x} + \frac{1}{(24e^x + 48x)x} \right\}$$

## 6 Kamke chapter 5. Linear fifth and higher order

### 6.1 ODE No. 1574

$$d^4y(x) (\sin(x))^4 + 2 \left( \frac{d^3}{dx^3} y(x) \right) (\sin(x))^3 \cos(x) + \left( \frac{d^2}{dx^2} y(x) \right) (\sin(x))^2 ((\sin(x))^2 - 3) + \left( \frac{d}{dx} y(x) \right) (\sin(x)) - y(x) = 0$$

**Mathematica:** cpu = 0.206526 (sec), leaf count = 73

DSolve[y(x) (a^4 sin^4(x) - 3) + y^(4)(x) sin^4(x) + 2y^(3)(x) sin^3(x) cos(x) + (sin^2(x) - 3) sin^2(x)y''(x) + (2 sin(x) - y(x)) y'(x) - y(x) = 0, y(x), x]

**Maple:** cpu = 0.639 (sec), leaf count = 345

$$\left\{ y(x) = \_C1 \sin(x) {}_2F_1\left(\frac{3}{4} + \frac{1}{4} \sqrt{-i(-4\sqrt{a+i}\sqrt{a-i}\sqrt{a-1}\sqrt{a+1} + 5i)}, \frac{3}{4} - \frac{1}{4} \sqrt{-i(-4\sqrt{a+i}\sqrt{a-i}\sqrt{a-1}\sqrt{a+1} + 5i)}\right), \right.$$

### 6.2 ODE No. 1575

$$d^4y(x) (\sin(x))^6 + 4 \left( \frac{d^3}{dx^3} y(x) \right) (\sin(x))^5 \cos(x) - 6 \left( \frac{d^2}{dx^2} y(x) \right) (\sin(x))^6 - 4 \left( \frac{d}{dx} y(x) \right) (\sin(x))^5 \cos(x) - y(x) = 0$$

**Mathematica:** cpu = 0.067008 (sec), leaf count = 61

DSolve[-f(x) + y^(4)(x) sin^6(x) + 4y^(3)(x) sin^5(x) cos(x) - 6 sin^6(x)y''(x) - 4 sin^5(x) cos(x)y'(x) + y(x) = 0, y(x), x]

**Maple:** cpu = 0.265 (sec), leaf count = 1277

$$\left\{ y(x) = -\frac{f(-12 \cos(x) (\sin(x))^2 e^{6ix} x^3 + 80 (\sin(x))^4 \ln(1 + e^{ix}) e^{6ix} x - 80 (\sin(x))^4 \ln(1 - e^{ix}) e^{6ix} x)}{12 \cos(x) (\sin(x))^2 e^{6ix} x^3 + 80 (\sin(x))^4 \ln(1 + e^{ix}) e^{6ix} x - 80 (\sin(x))^4 \ln(1 - e^{ix}) e^{6ix} x} \right.$$

### 6.3 ODE No. 1576

$$f \left( d^4y(x) - 2a^2 \frac{d^2}{dx^2} y(x) + a^4 y(x) \right) + 2 df \left( \frac{d^3}{dx^3} y(x) - a^2 \frac{d}{dx} y(x) \right) = 0$$

**Mathematica:** cpu = 0.246031 (sec), leaf count = 50

DSolve[2f'(x) (y^(3)(x) - a^2 y'(x)) + f(x) (a^4 y(x) - 2a^2 y''(x) + y^(4)(x)) = 0, y(x), x]

**Maple:** cpu = 0.016 (sec), leaf count = 67

$$\left\{ y(x) = \_C1 e^{ax} + \_C2 e^{-ax} + \_C3 e^{\frac{x}{f}(-df + \sqrt{a^2 f^2 + df^2})} + \_C4 e^{-\frac{x}{f}(df + \sqrt{a^2 f^2 + df^2})} \right\}$$

## 6.4 ODE No. 1577

$$f \frac{d^4}{dx^4} y(x) = 0$$

**Mathematica:** cpu = 1.265661 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow \int_1^x \left( \int_1^{K[2]} \left( \frac{c_1}{f(K[1])} + \frac{c_2 K[1]}{f(K[1])} \right) dK[1] \right) dK[2] + c_4 x + c_3 \right\} \right\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 21

$$\left\{ y(x) = \frac{-C1 x^3}{6} + \frac{-C2 x^2}{2} + -C3 x + -C4 \right\}$$

## 6.5 ODE No. 1578

$$d4y(x) - 2a^2 \frac{d^2}{dx^2} y(x) + a^4 y(x) - \lambda(ax - b) \left( \frac{d^2}{dx^2} y(x) - a^2 y(x) \right) = 0$$

**Mathematica:** cpu = 438.074128 (sec), leaf count = 139

$$\left\{ \left\{ y(x) \rightarrow c_3 e^{-ax} \int_1^x 2ae^{2aK[1]} \int e^{-aK[1]} \text{Ai} \left( \frac{a^2 + \lambda K[1]a - b\lambda}{(a\lambda)^{2/3}} \right) dK[1] dK[1] + c_4 e^{-ax} \int_1^x 2ae^{2aK[2]} \int e^{-aK[2]} \text{Ai} \left( \frac{a^2 + \lambda K[2]a - b\lambda}{(a\lambda)^{2/3}} \right) dK[2] dK[2] \right\} \right\}$$

**Maple:** cpu = 0.764 (sec), leaf count = 92

$$\left\{ y(x) = e^{ax} \left( \int e^{-2ax} \left( \int -C3 e^{ax} \text{Ai} \left( -\frac{\lambda(ax - b) + a^2}{a\lambda} \sqrt[3]{-a\lambda} \right) dx \right) dx + -C4 e^{ax} \text{Bi} \left( -\frac{\lambda(ax - b) + a^2}{a\lambda} \sqrt[3]{-a\lambda} \right) \right) \right\}$$

## 6.6 ODE No. 1579

$$\frac{d^5}{dx^5} y(x) + 2 \frac{d^3}{dx^3} y(x) + \frac{d}{dx} y(x) - ax - b \sin(x) - c \cos(x) = 0$$

**Mathematica:** cpu = 0.621079 (sec), leaf count = 104

$$\left\{ \left\{ y(x) \rightarrow \frac{ax^2}{2} + \frac{1}{8}b(x^2 - 2) \cos(x) - \frac{3}{8}bx \sin(x) - \frac{5}{16}b \cos(x) - \frac{1}{8}c(x^2 - 2) \sin(x) + c_2 x \sin(x) + \frac{9}{16}c \sin(x) \right\} \right\}$$

**Maple:** cpu = 0.156 (sec), leaf count = 78

$$\left\{ y(x) = -\frac{\sin(x) bx}{2} - \frac{3 b \cos(x)}{4} - \frac{\cos(x) cx}{2} - \frac{\sin(x) cx^2}{8} + \frac{21 \sin(x) c}{32} + \frac{\cos(x) bx^2}{8} + \frac{ax^2}{2} + -C1 \sin(x) \right\}$$

## 6.7 ODE No. 1580

$$\frac{d^6}{dx^6}y(x) + y(x) - \sin(3/2x)\sin(x/2) = 0$$

**Mathematica:** cpu = 0.839106 (sec), leaf count = 234

$$\left\{ \left\{ y(x) \rightarrow c_4 e^{-\frac{\sqrt{3}x}{2}} \sin\left(\frac{x}{2}\right) + c_6 e^{\frac{\sqrt{3}x}{2}} \sin\left(\frac{x}{2}\right) + c_5 \sin(x) + c_1 e^{\frac{\sqrt{3}x}{2}} \cos\left(\frac{x}{2}\right) + c_3 e^{-\frac{\sqrt{3}x}{2}} \cos\left(\frac{x}{2}\right) + c_2 \cos(x) \right\} \right.$$

**Maple:** cpu = 0.375 (sec), leaf count = 164

$$\left\{ y(x) = \left( \frac{e^{\frac{i}{2}x}}{24} + \frac{e^{-\frac{i}{2}x}}{24} \right) \cos\left(\frac{x}{2}\right) + \left( \frac{e^{\frac{i}{2}x}}{56} + \frac{e^{-\frac{i}{2}x}}{56} \right) \cos\left(\frac{3x}{2}\right) + \left( \frac{i}{24} e^{\frac{i}{2}x} - \frac{i}{24} e^{-\frac{i}{2}x} \right) \sin\left(\frac{x}{2}\right) + \left( -\frac{11i}{168} e^{\frac{i}{2}x} + \frac{11i}{168} e^{-\frac{i}{2}x} \right) \sin\left(\frac{3x}{2}\right) \right.$$

## 6.8 ODE No. 1581

$$\frac{d^5}{dx^5}y(x) - axy(x) - b = 0$$

**Mathematica:** cpu = 0.152519 (sec), leaf count = 61

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{-b - xay(x) + y^{(5)}(x) = 0, y(0) = c_1, y'(0) = c_2, y''(0) = c_3, y^{(3)}(0) = c_4\}) \right\} \right.$$

**Maple:** cpu = 0 (sec), leaf count = 0

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## 6.9 ODE No. 1582

$$\frac{d^5}{dx^5}y(x) + ax^\nu \frac{d}{dx}y(x) + a\nu x^{\nu-1}y(x) = 0$$

**Mathematica:** cpu = 0.337543 (sec), leaf count = 787

$$\left\{ \left\{ y(x) \rightarrow c_5 \left( \frac{4}{\nu} + 1 \right)^{-\frac{16}{\nu+4}} \nu^{-\frac{16}{\nu+4}} a^{\frac{4}{\nu+4}} (x^\nu)^{\frac{4(\frac{4}{\nu}+1)}{\nu+4}} {}_1F_4 \left( \frac{4}{\nu(1+\frac{4}{\nu})} + \frac{1}{1+\frac{4}{\nu}}; 1 + \frac{1}{(1+\frac{4}{\nu})\nu}, 1 + \frac{2}{(1+\frac{4}{\nu})\nu}, 1 + \frac{3}{(1+\frac{4}{\nu})\nu}, 1 + \frac{4}{(1+\frac{4}{\nu})\nu} \right) \right\} \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 41

$$\left\{ y(x) = \text{DESol} \left( \left\{ \frac{d^5}{dx^5} Y(x) + ax^\nu \frac{d}{dx} Y(x) + a\nu x^{\nu-1} Y(x) \right\}, \{ \_Y(x) \} \right) \right\}$$

## 6.10 ODE No. 1583

$$\frac{d^5}{dx^5}y(x) + a\frac{d^4}{dx^4}y(x) - f = 0$$

**Mathematica:** cpu = 1218.103679 (sec), leaf count = 117

$$\{ \{y(x) \rightarrow (\text{Integrate}\$a\$3645023 - 1)(\text{Integrate}\$a\$3818055 - 1)(\text{Integrate}\$a\$3863942 - 1)(x - 1)e^{-ax} - C1\} \}$$

**Maple:** cpu = 0.015 (sec), leaf count = 40

$$\left\{ y(x) = \frac{e^{-ax} - C1}{a^4} + \frac{fx^4}{24a} + \frac{-C2x^3}{6} + \frac{-C3x^2}{2} + C4x + C5 \right\}$$

## 6.11 ODE No. 1584

$$x\frac{d^5}{dx^5}y(x) - 5m\frac{d^4}{dx^4}y(x) + axy(x) = 0$$

**Mathematica:** cpu = 2.837860 (sec), leaf count = 216

$$\left\{ \left\{ y(x) \rightarrow c_5 5^{-5m-4} a^{\frac{1}{5}(5m+4)} x^{5m+4} {}_0F_4\left( ; m + \frac{6}{5}, m + \frac{7}{5}, m + \frac{8}{5}, m + \frac{9}{5}; -\frac{ax^5}{3125} \right) + \frac{1}{125} a^{3/5} c_4 x^3 {}_0F_4\left( ; \frac{6}{5}, \frac{7}{5}, \frac{8}{5}, \frac{9}{5}; -\frac{ax^5}{3125} \right) \right. \right.$$

**Maple:** cpu = 0.124 (sec), leaf count = 118

$$\left\{ y(x) = -C1 {}_0F_4\left( ; \frac{2}{5}, \frac{3}{5}, \frac{4}{5}, \frac{1}{5} - m; -\frac{x^5 a}{3125} \right) - C2 x {}_0F_4\left( ; \frac{3}{5}, \frac{4}{5}, \frac{6}{5}, \frac{2}{5} - m; -\frac{x^5 a}{3125} \right) - C3 x^2 {}_0F_4\left( ; \frac{4}{5}, \frac{5}{5}, \frac{6}{5}, \frac{1}{5} - m; -\frac{x^5 a}{3125} \right) \right.$$

## 6.12 ODE No. 1585

$$x\left(a\frac{d}{dx}y(x) + b\frac{d^2}{dx^2}y(x) + c\frac{d^3}{dx^3}y(x) + ed_4y(x)\right)y(x) = 0$$

**Mathematica:** cpu = 0.247031 (sec), leaf count = 214

$$\left\{ \{y(x) \rightarrow 0\}, \left\{ y(x) \rightarrow \frac{c_1 e^{x \text{Root}\left[\#1^3 + \frac{\#1^2 c}{e} + \frac{\#1 b}{e} + \frac{a}{e}\&, 1\right]}}{\text{Root}\left[\#1^3 + \frac{\#1^2 c}{e} + \frac{\#1 b}{e} + \frac{a}{e}\&, 1\right]} + \frac{c_2 e^{x \text{Root}\left[\#1^3 + \frac{\#1^2 c}{e} + \frac{\#1 b}{e} + \frac{a}{e}\&, 2\right]}}{\text{Root}\left[\#1^3 + \frac{\#1^2 c}{e} + \frac{\#1 b}{e} + \frac{a}{e}\&, 2\right]} + \frac{c_3 e^{x \text{Root}\left[\#1^3 + \frac{\#1^2 c}{e} + \frac{\#1 b}{e} + \frac{a}{e}\&, 3\right]}}{\text{Root}\left[\#1^3 + \frac{\#1^2 c}{e} + \frac{\#1 b}{e} + \frac{a}{e}\&, 3\right]} \right. \right.$$

**Maple:** cpu = 0.016 (sec), leaf count = 806

$$\left\{ y(x) = 0, y(x) = -C1 + -C2 e^{-\frac{x}{12e}} \left( i \left( 12\sqrt{3}\sqrt{27a^2e^2 - 18abce + 4ac^3 + 4b^3e - b^2c^2}e - 108ae^2 + 36bce - 8c^3 \right)^{\frac{2}{3}} \sqrt{3} + 12i\sqrt{3}be - 4i \right) \right.$$

### 6.13 ODE No. 1586

$$x \frac{d^5}{dx^5} y(x) - (aA_1 - A_0)x - A_1 - ((aA_2 - A_1)x + A_2) \frac{d}{dx} y(x) - ((aA_3 - A_2)x + A_3) \frac{d^2}{dx^2} y(x) - ((aA_4 - A_3)x + A_4) \frac{d^3}{dx^3} y(x) - ((aA_5 - A_4)x + A_5) \frac{d^4}{dx^4} y(x) = 0$$

**Mathematica:** cpu = 84.450724 (sec), leaf count = 148

$$\left\{ \left\{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{xA(0) - xA(1) - A(1) + (xA(1) - xA(2) - A(2))y'(x) + (xA(2) - xA(3) - A(3))y''(x) + (xA(3) - xA(4) - A(4))y'''(x) + (xA(4) - xA(5) - A(5))y^{(4)}(x)\}) \right\} \right.$$

**Maple:** cpu = 0.124 (sec), leaf count = 119

$$\left\{ y(x) = \int \text{DESol} \left( \left\{ -\frac{(axA_2 - xA_1 + A_2)Y(x)}{x} - \frac{(axA_3 - xA_2 + A_3) \frac{d}{dx} Y(x)}{x} - \frac{(axA_4 - xA_3 + A_4) \frac{d^2}{dx^2} Y(x)}{x} - \frac{(axA_5 - xA_4 + A_5) \frac{d^3}{dx^3} Y(x)}{x} - \frac{(axA_6 - xA_5 + A_6) \frac{d^4}{dx^4} Y(x)}{x} \right\} \right) \right.$$

### 6.14 ODE No. 1587

$$x^5 \frac{d^{10}}{dx^{10}} y(x) - ay(x) = 0$$

**Mathematica:** cpu = 0.311540 (sec), leaf count = 492

$$\left\{ \left\{ y(x) \rightarrow \frac{(-1)^{4/5} a^{9/5} c_1 x^9 {}_0F_9 \left( ; \frac{6}{5}, \frac{7}{5}, \frac{8}{5}, \frac{9}{5}, 2, \frac{11}{5}, \frac{12}{5}, \frac{13}{5}, \frac{14}{5}; \frac{ax^5}{9765625} \right)}{3814697265625} + \frac{(-1)^{3/5} a^{8/5} c_3 x^8 {}_0F_9 \left( ; \frac{4}{5}, \frac{6}{5}, \frac{7}{5}, \frac{8}{5}, \frac{9}{5}, 2, \frac{11}{5}, \frac{12}{5}, \frac{13}{5}; \frac{ax^5}{9765625} \right)}{152587890625} \right\} \right.$$

**Maple:** cpu = 0.265 (sec), leaf count = 200

$$\left\{ y(x) = {}_C1 x^{\frac{5}{2}} I_5(2 a^{1/10} \sqrt{x}) + {}_C2 x^{\frac{5}{2}} Y_5(2 i a^{\frac{1}{10}} \sqrt{x}) + {}_C3 x^{\frac{5}{2}} I_5(2 e^{i/5\pi} a^{1/10} \sqrt{x}) + {}_C4 x^{\frac{5}{2}} I_5(2 e^{2/5\pi} a^{1/10} \sqrt{x}) \right.$$

### 6.15 ODE No. 1588

$$x^{10} \frac{d^5}{dx^5} y(x) - ay(x) = 0$$

**Mathematica:** cpu = 6.345306 (sec), leaf count = 114

$$\left\{ \left\{ y(x) \rightarrow c_1 x^4 e^{-\frac{\sqrt[5]{a}}{x}} + c_2 x^4 e^{\frac{\sqrt[5]{-1} \sqrt[5]{a}}{x}} + c_3 x^4 e^{-\frac{(-1)^{2/5} \sqrt[5]{a}}{x}} + c_4 x^4 e^{\frac{(-1)^{3/5} \sqrt[5]{a}}{x}} + c_5 x^4 e^{-\frac{(-1)^{4/5} \sqrt[5]{a}}{x}} \right\} \right.$$

**Maple:** cpu = 0.078 (sec), leaf count = 90

$$\left\{ y(x) = {}_C1 {}_0F_4 \left( ; \frac{6}{5}, \frac{7}{5}, \frac{8}{5}, \frac{9}{5}; -\frac{a}{3125 x^5} \right) + {}_C2 x {}_0F_4 \left( ; \frac{4}{5}, \frac{6}{5}, \frac{7}{5}, \frac{8}{5}; -\frac{a}{3125 x^5} \right) + {}_C3 x^2 {}_0F_4 \left( ; \frac{3}{5}, \frac{4}{5}, \frac{6}{5}, \frac{8}{5}; -\frac{a}{3125 x^5} \right) \right.$$

**6.16 ODE No. 1589**

$$x^{11/2} \frac{d^{11}}{dx^{11}} y(x) - ay(x) = 0$$

**Mathematica:** cpu = 0.040505 (sec), leaf count = 670

$$\left\{ \left\{ y(x) \rightarrow \frac{4}{121} (-1)^{2/11} a^{2/11} c_2 x {}_0F_{10} \left( ; -\frac{7}{11}, -\frac{5}{11}, -\frac{3}{11}, -\frac{1}{11}, \frac{1}{11}, \frac{3}{11}, \frac{5}{11}, \frac{7}{11}, \frac{9}{11}, \frac{13}{11}; \frac{2048ax^{11/2}}{285311670611} \right) \right\} \right.$$

**Maple:** cpu = 6.380 (sec), leaf count = 27500

Too large to display

**6.17 ODE No. 1590**

$$(x - a)^5 (x - b)^5 \frac{d^5}{dx^5} y(x) - cy(x) = 0$$

**Mathematica:** cpu = 343.290592 (sec), leaf count = 72

$$\{ \{ y(x) \rightarrow \text{DifferentialRoot}(\{y, x\}, \{(a - x)^5 (b - x)^5 y^{(5)}(x) - cy(x) = 0, y(0) = c_1, y'(0) = c_2, y''(0) = c_3$$

**Maple:** cpu = 1.794 (sec), leaf count = 1258

$$\left\{ y(x) = \text{ODESolStruc} \left( e^{\int \frac{(e^{\int -g(-f) d_f + -C1)a - (\int -g(-f) d_f + -C1)b}{e^{\int -g(-f) d_f + -C1} a - (\int -g(-f) d_f + -C1)b}^2 b^{-2} e^{\int -g(-f) d_f + -C1} a - (\int -g(-f) d_f + -C1)b}^2}{e^{\int -g(-f) d_f + -C1} a - (\int -g(-f) d_f + -C1)b}^2} \right)$$



## 7 Kamke chapter 6. Non-linear second order

### 7.1 ODE No. 1591

$$\frac{d^2}{dx^2}y(x) - (y(x))^2 = 0$$

**Mathematica:** cpu = 0.039005 (sec), leaf count = 26

$$\left\{ \left\{ y(x) \rightarrow \sqrt[3]{6} \wp \left( \frac{x + c_1}{\sqrt[3]{6}}; 0, c_2 \right) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 12

$$\{y(x) = 6 \text{ WeierstrassP}(x + \_C1, 0, \_C2)\}$$

### 7.2 ODE No. 1592

$$\frac{d^2}{dx^2}y(x) - 6(y(x))^2 = 0$$

**Mathematica:** cpu = 0.030004 (sec), leaf count = 14

$$\{\{y(x) \rightarrow \wp(x + c_1; 0, c_2)\}\}$$

**Maple:** cpu = 0.016 (sec), leaf count = 10

$$\{y(x) = \text{WeierstrassP}(x + \_C1, 0, \_C2)\}$$

### 7.3 ODE No. 1593

$$\frac{d^2}{dx^2}y(x) - 6(y(x))^2 - x = 0$$

**Mathematica:** cpu = 0.162021 (sec), leaf count = 20

$$\text{DSolve}[y''(x) - 6y(x)^2 - x = 0, y(x), x]$$

**Maple:** cpu = 0.094 (sec), leaf count = 0

could not solve

## 7.4 ODE No. 1594

$$\frac{d^2}{dx^2}y(x) - 6(y(x))^2 + 4y(x) = 0$$

**Mathematica:** cpu = 0.366546 (sec), leaf count = 373

$$\text{Solve} \left[ \frac{4(\text{Root}[4\#1^3 - 4\#1^2 + c_1\&, 2] - \text{Root}[4\#1^3 - 4\#1^2 + c_1\&, 3]) (y(x) - \text{Root}[4\#1^3 - 4\#1^2 + c_1\&, 2])}{(c_1 + 4y(x))^3 - 4y(x)^2} (\text{Root}[4\#1^3 - 4\#1^2 + c_1\&, 2] - \text{Root}[4\#1^3 - 4\#1^2 + c_1\&, 3])}{(c_1 + 4y(x))^3 - 4y(x)^2} (\text{Root}[4\#1^3 - 4\#1^2 + c_1\&, 2] - \text{Root}[4\#1^3 - 4\#1^2 + c_1\&, 3])} \right]$$

**Maple:** cpu = 0.110 (sec), leaf count = 59

$$\left\{ \int^{y(x)} \frac{1}{\sqrt{4a^3 - 4a^2 + C1}} da - x - C2 = 0, \int^{y(x)} -\frac{1}{\sqrt{4a^3 - 4a^2 + C1}} da - x - C2 = 0 \right.$$

## 7.5 ODE No. 1595

$$\frac{d^2}{dx^2}y(x) + a(y(x))^2 + bx + c = 0$$

**Mathematica:** cpu = 0.335543 (sec), leaf count = 21

$$\text{DSolve}[ay(x)^2 + bx + c + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.124 (sec), leaf count = 0

could not solve

## 7.6 ODE No. 1596

$$\frac{d^2}{dx^2}y(x) - 2(y(x))^3 - xy(x) + a = 0$$

**Mathematica:** cpu = 0.968123 (sec), leaf count = 23

$$\text{DSolve}[a + y''(x) - 2y(x)^3 - xy(x) = 0, y(x), x]$$

**Maple:** cpu = 0.187 (sec), leaf count = 0

could not solve

## 7.7 ODE No. 1597

$$\frac{d^2}{dx^2}y(x) - a(y(x))^3 = 0$$

**Mathematica:** cpu = 2.336797 (sec), leaf count = 242

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt[4]{2}\sqrt{c_1}\sqrt{\frac{i\sqrt{a}}{\sqrt{c_1}}}\operatorname{sn}\left(\frac{(-1)^{3/4}\sqrt{\sqrt{2}\sqrt{a}\sqrt{c_1}x^2+2\sqrt{2}\sqrt{a}\sqrt{c_1}c_2x+\sqrt{2}\sqrt{a}\sqrt{c_1}c_2^2}}{\sqrt{2}}\right)-1}{\sqrt{a}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt[4]{2}\sqrt{c_1}\sqrt{\frac{i\sqrt{a}}{\sqrt{c_1}}}}{\sqrt{a}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 21

$$\left\{ y(x) = \_C2 \operatorname{JacobiSN}\left(\left(\frac{x}{2}\sqrt{-2a} + \_C1\right) \_C2, i\right) \right\}$$

## 7.8 ODE No. 1598

$$\frac{d^2}{dx^2}y(x) - 2a^2(y(x))^3 + 2abxy(x) - b = 0$$

**Mathematica:** cpu = 3.346425 (sec), leaf count = 30

$$\text{DSolve}[-2a^2y(x)^3 + 2abxy(x) - b + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.234 (sec), leaf count = 0

could not solve

## 7.9 ODE No. 1599

$$\frac{d^2}{dx^2}y(x) + d + bxy(x) + cy(x) + a(y(x))^3 = 0$$

**Mathematica:** cpu = 2.855863 (sec), leaf count = 27

$$\text{DSolve}[ay(x)^3 + bxy(x) + cy(x) + d + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.250 (sec), leaf count = 0

could not solve

## 7.10 ODE No. 1600

$$\frac{d^2}{dx^2}y(x) + d + b(y(x))^2 + cy(x) + a(y(x))^3 = 0$$

**Mathematica:** cpu = 2.224782 (sec), leaf count = 1017

$$\text{Solve} \left[ 4F \left( \sin^{-1} \left( \sqrt{\frac{(\text{Root}[3a\#1^4+4b\#1^3+6c\#1^2+12d\#1-6c_1\&,2]-\text{Root}[3a\#1^4+4b\#1^3+6c\#1^2+12d\#1-6c_1\&,4])(y(x)-\text{Root}[3a\#1^4+4b\#1^3+6c\#1^2+12d\#1-6c_1\&,1]-\text{Root}[3a\#1^4+4b\#1^3+6c\#1^2+12d\#1-6c_1\&,4])}{(\text{Root}[3a\#1^4+4b\#1^3+6c\#1^2+12d\#1-6c_1\&,1]-\text{Root}[3a\#1^4+4b\#1^3+6c\#1^2+12d\#1-6c_1\&,4])(y(x)-\text{Root}[3a\#1^4+4b\#1^3+6c\#1^2+12d\#1-6c_1\&,1]-\text{Root}[3a\#1^4+4b\#1^3+6c\#1^2+12d\#1-6c_1\&,4])} \right)} \right]$$

**Maple:** cpu = 0.063 (sec), leaf count = 89

$$\left\{ \int^{y(x)} -6 \frac{1}{\sqrt{-18\_a^4a - 24b\_a^3 - 36c\_a^2 - 72d\_a + 36\_C1}} d\_a - x - \_C2 = 0, \int^{y(x)} 6 \frac{1}{\sqrt{-18\_a^4a - 24b\_a^3 - 36c\_a^2 - 72d\_a + 36\_C1}} d\_a - x - \_C2 = 0 \right\}$$

## 7.11 ODE No. 1601

$$\frac{d^2}{dx^2}y(x) + ax^r(y(x))^n = 0$$

**Mathematica:** cpu = 0.037505 (sec), leaf count = 20

$$\text{DSolve}[ax^r y(x)^n + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 3.479 (sec), leaf count = 184

$$\left\{ y(x) = \text{ODESolStruc} \left( \_a e^{\int -b(\_a) d\_a + \_C1}, \left[ \left\{ \frac{d}{d\_a} b(\_a) = \frac{(\_a^n a n^2 - 2 \_a^n a n + \_a r n + \_a r^2 + \_a r)}{(\_a^n a n^2 - 2 \_a^n a n + \_a r n + \_a r^2 + \_a r)} \right\} \right] \right)$$

## 7.12 ODE No. 1602

$$\frac{d^2}{dx^2}y(x) + (n+1)a^{2n}(y(x))^{2n+1} - y(x) = 0$$

**Mathematica:** cpu = 81.621865 (sec), leaf count = 46

$$\text{Solve} \left[ \left( \int_1^{y(x)} \frac{1}{\sqrt{c_1 - K[1]^2 (a^{2n} K[1]^{2n} - 1)}} dK[1] \right)^2 = (c_2 + x)^2, y(x) \right]$$

**Maple:** cpu = 0.125 (sec), leaf count = 73

$$\left\{ \int^{y(x)} \frac{1}{\sqrt{-a^{2n} \_a^{2n+2} + \_a^2 + \_C1}} d\_a - x - \_C2 = 0, \int^{y(x)} -\frac{1}{\sqrt{-a^{2n} \_a^{2n+2} + \_a^2 + \_C1}} d\_a - x - \_C2 = 0 \right\}$$

### 7.13 ODE No. 1603

$$\frac{d^2}{dx^2}y(x) - (a(y(x))^2 + bxy(x) + cx^2 + \alpha y(x) + \beta x + \gamma)^{-\frac{3}{2}} = 0$$

**Mathematica:** cpu = 60.655702 (sec), leaf count = 42

$$\text{DSolve}\left[y''(x) - \frac{1}{(ay(x)^2 + bxy(x) + cx^2 + dy(x) + ex + k)^{3/2}} = 0, y(x), x\right]$$

**Maple:** cpu = 59.530 (sec), leaf count = 13291

$$y(x) = \frac{1}{2} \left( \frac{4acx - b^2x + 2a\beta - \alpha b}{g^2a^3b^2c + 4g^2a^2b^4 + 16a^2c^2\sqrt{a^2b^2\beta^2 + b^4ac^2 + 16a^3c\alpha^2 + 16b^2g^2d^3\gamma - 4a^2g^2\alpha^2 - 8a^2g^2\alpha b^2}} \right) \frac{ac + \arctan\left(\frac{1/2}{g^2a^2b^2}\right)}{g^2a^2c^2 - 32a}$$

### 7.14 ODE No. 1604

$$\frac{d^2}{dx^2}y(x) - e^{y(x)} = 0$$

**Mathematica:** cpu = 0.060508 (sec), leaf count = 34

$$\left\{ \left\{ y(x) \rightarrow \log\left(\frac{1}{2}c_1\left(\tanh^2\left(\frac{1}{2}\sqrt{c_1(c_2+x)^2}\right) - 1\right)\right) \right\} \right\}$$

**Maple:** cpu = 0.281 (sec), leaf count = 23

$$\left\{ y(x) = \ln\left(\frac{1}{2-C1^2}\left(\left(\tan\left(\frac{-C2+x}{2-C1}\right)\right)^2 + 1\right)\right) \right\}$$

### 7.15 ODE No. 1605

$$\frac{d^2}{dx^2}y(x) + ae^x\sqrt{y(x)} = 0$$

**Mathematica:** cpu = 0.519566 (sec), leaf count = 22

$$\text{DSolve}\left[ae^x\sqrt{y(x)} + y''(x) = 0, y(x), x\right]$$

**Maple:** cpu = 0.811 (sec), leaf count = 109

$$y(x) = \text{ODESolStruc}\left(\frac{-a}{e^{-2\int b(-a) d_a - 2_C1}}, \left[\frac{d}{d_a} b(-a) = (\sqrt{-aa} + 4_a)(-b(-a))^3 + 4(-b(-a))\right]\right)$$

## 7.16 ODE No. 1606

$$\frac{d^2}{dx^2}y(x) + e^x \sin(y(x)) = 0$$

**Mathematica:** cpu = 1.086138 (sec), leaf count = 18

$$\text{DSolve}[y''(x) + e^x \sin(y(x)) = 0, y(x), x]$$

**Maple:** cpu = 0.733 (sec), leaf count = 0

could not solve

## 7.17 ODE No. 1607

$$\frac{d^2}{dx^2}y(x) + a \sin(y(x)) = 0$$

**Mathematica:** cpu = 0.108014 (sec), leaf count = 79

$$\left\{ \left\{ y(x) \rightarrow -2am \left( \frac{1}{2} \sqrt{(2a + c_1)(x + c_2)^2} \middle| \frac{4a}{2a + c_1} \right) \right\}, \left\{ y(x) \rightarrow 2am \left( \frac{1}{2} \sqrt{(2a + c_1)(x + c_2)^2} \middle| \frac{4a}{2a + c_1} \right) \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 49

$$\left\{ \int^{y(x)} \frac{1}{\sqrt{2a \cos(\_a) + \_C1}} d\_a - x - \_C2 = 0, \int^{y(x)} -\frac{1}{\sqrt{2a \cos(\_a) + \_C1}} d\_a - x - \_C2 = 0 \right\}$$

## 7.18 ODE No. 1608

$$\frac{d^2}{dx^2}y(x) + a^2 \sin(y(x)) - b \sin(x) = 0$$

**Mathematica:** cpu = 0.050006 (sec), leaf count = 23

$$\text{DSolve}[a^2 \sin(y(x)) - b \sin(x) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 1.248 (sec), leaf count = 0

could not solve

## 7.19 ODE No. 1609

$$\frac{d^2}{dx^2}y(x) + a^2 \sin(y(x)) - bf(x) = 0$$

**Mathematica:** cpu = 0.035004 (sec), leaf count = 23

$$\text{DSolve}[a^2 \sin(y(x)) - bf(x) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.624 (sec), leaf count = 0

could not solve

## 7.20 ODE No. 1610

$$\frac{d^2}{dx^2}y(x) - \frac{1}{x^{3/2}}h\left(\frac{y(x)}{\sqrt{x}}\right) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.203 (sec), leaf count = 92

$$\left\{ y(x) = \text{RootOf}\left(-\ln(x) - 2 \int^{-z} \frac{1}{\sqrt{-C1 + 8 \int h(\_g) d\_g + \_g^2}} d\_g + 2\_C2\right) \sqrt{x}, y(x) = \text{RootOf}\right.$$

## 7.21 ODE No. 1611

$$\frac{d^2}{dx^2}y(x) - 3 \frac{d}{dx}y(x) - (y(x))^2 - 2y(x) = 0$$

**Mathematica:** cpu = 5.239165 (sec), leaf count = 27

$$\text{DSolve}[y''(x) - 3y'(x) - y(x)^2 - 2y(x) = 0, y(x), x]$$

**Maple:** cpu = 0.359 (sec), leaf count = 57

$$\left\{ y(x) = \text{ODESolStruc}\left(-a, \left[\left(\frac{d}{d\_a}b(-a)\right) - b(-a) - 3\_b(-a) - \_a^2 - 2\_a = 0\right], \left\{-a = y(x), \dots\right.\right.\right.$$

## 7.22 ODE No. 1612

$$\frac{d^2}{dx^2}y(x) - 7 \frac{d}{dx}y(x) - (y(x))^{3/2} + 12y(x) = 0$$

**Mathematica:** cpu = 22.518860 (sec), leaf count = 29

$$\text{DSolve}[y''(x) - 7y'(x) - y(x)^{3/2} + 12y(x) = 0, y(x), x]$$

**Maple:** cpu = 0.811 (sec), leaf count = 57

$$\left\{ y(x) = \text{ODESolStruc}\left(-a, \left[ \left( \frac{d}{d\_a} b(-a) \right) - b(-a) - 7\_b(-a) - \_a^{\frac{3}{2}} + 12\_a = 0 \right], \left\{ -a = y(x), \right. \right. \right.$$

## 7.23 ODE No. 1613

$$\frac{d^2}{dx^2}y(x) + 5a \frac{d}{dx}y(x) - 6(y(x))^2 + 6a^2y(x) = 0$$

**Mathematica:** cpu = 2.182777 (sec), leaf count = 31

$$\text{DSolve}[6a^2y(x) + 5ay'(x) + y''(x) - 6y(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 0.016 (sec), leaf count = 27

$$\left\{ y(x) = \text{WeierstrassP}\left(-\frac{e^{-ax}}{a} + \_C1, 0, \_C2\right) (e^{-ax})^2 \right\}$$

## 7.24 ODE No. 1614

$$\frac{d^2}{dx^2}y(x) + 3a \frac{d}{dx}y(x) - 2(y(x))^3 + 2a^2y(x) = 0$$

**Mathematica:** cpu = 1.489689 (sec), leaf count = 31

$$\text{DSolve}[2a^2y(x) + 3ay'(x) + y''(x) - 2y(x)^3 = 0, y(x), x]$$

**Maple:** cpu = 0.047 (sec), leaf count = 33

$$\left\{ y(x) = \frac{\_C2}{e^{ax}} \text{JacobiSN}\left(\left(-\frac{1}{a}\sqrt{-e^{-2ax}} + \_C1\right) \_C2, i\right) \right\}$$



## 7.25 ODE No. 1615

$$\frac{d^2}{dx^2}y(x) - \frac{(3n+4)\frac{d}{dx}y(x)}{n} - 2\frac{(n+1)(n+2)y(x)}{n^2}\left((y(x))^{\frac{n}{n+1}} - 1\right) = 0$$

**Mathematica:** cpu = 118.097997 (sec), leaf count = 50

$$\text{DSolve}\left[-\frac{2(n+1)(n+2)y(x)\left(y(x)^{\frac{n}{n+1}} - 1\right)}{n^2} - \frac{(3n+4)y'(x)}{n} + y''(x) = 0, y(x), x\right]$$

**Maple:** cpu = 3.526 (sec), leaf count = 116

$$\left\{y(x) = \text{ODESolStruc}\left(-a, \left[\left(\frac{d}{d_a}b(-a)\right) - b(-a) - \frac{1}{n^2}\left(2_a^{\frac{n}{n+1}}_a n^2 + 3_b(-a)n^2 + 6_a^{\frac{n}{n+1}}_a\right)\right]\right)\right\}$$

## 7.26 ODE No. 1616

$$\frac{d^2}{dx^2}y(x) + a\frac{d}{dx}y(x) + b(y(x))^n + 1/4(a^2 - 1)y(x) = 0$$

**Mathematica:** cpu = 25.262208 (sec), leaf count = 34

$$\text{DSolve}\left[\frac{1}{4}(a^2 - 1)y(x) + ay'(x) + by(x)^n + y''(x) = 0, y(x), x\right]$$

**Maple:** cpu = 0.889 (sec), leaf count = 63

$$\left\{y(x) = \text{ODESolStruc}\left(-a, \left[\left(\frac{d}{d_a}b(-a)\right) - b(-a) + a_b(-a) + b_a^n + \frac{a a^2}{4} - \frac{a}{4} = 0\right]\right), \left\{-a = \dots\right\}\right\}$$

## 7.27 ODE No. 1617

$$\frac{d^2}{dx^2}y(x) + a\frac{d}{dx}y(x) + bx^r(y(x))^n = 0$$

**Mathematica:** cpu = 0.045006 (sec), leaf count = 26

$$\text{DSolve}[ay'(x) + bx^r y(x)^n + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.359 (sec), leaf count = 0

could not solve

**7.28 ODE No. 1618**

$$\frac{d^2}{dx^2}y(x) + a \frac{d}{dx}y(x) + be^{y(x)} - 2a = 0$$

**Mathematica:** cpu = 30.684396 (sec), leaf count = 26

$$\text{DSolve}[ay'(x) - 2a + be^{y(x)} + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 1.107 (sec), leaf count = 56

$$\left\{ y(x) = \text{ODESolStruc} \left( -a, \left[ \left( \frac{d}{d\_a} b(-a) \right) - b(-a) + a b(-a) + be^{-a} - 2a = 0 \right], \left\{ -a = y(x), \dots \right\} \right. \right.$$

**7.29 ODE No. 1619**

$$\frac{d^2}{dx^2}y(x) + a \frac{d}{dx}y(x) + f(x) \sin(y(x)) = 0$$

**Mathematica:** cpu = 0.055507 (sec), leaf count = 23

$$\text{DSolve}[ay'(x) + f(x) \sin(y(x)) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.593 (sec), leaf count = 0

could not solve

**7.30 ODE No. 1620**

$$\frac{d^2}{dx^2}y(x) + y(x) \frac{d}{dx}y(x) - (y(x))^3 = 0$$

**Mathematica:** cpu = 122.323033 (sec), leaf count = 24

$$\text{DSolve}[y''(x) + y(x)y'(x) - y(x)^3 = 0, y(x), x]$$

**Maple:** cpu = 0.078 (sec), leaf count = 253

$$\left\{ \int^{y(x)} \left( \frac{-a^2}{2} + \frac{1}{2} \left( \sqrt[3]{-C1 + \sqrt{-a^6 + -C1^2}} - a^2 \frac{1}{\sqrt[3]{-C1 + \sqrt{-a^6 + -C1^2}}} \right)^2 \right)^{-1} d\_a - x - \_C2 = \dots \right.$$

**7.31 ODE No. 1621**

$$\frac{d^2}{dx^2}y(x) + y(x) \frac{d}{dx}y(x) - (y(x))^3 + ay(x) = 0$$

**Mathematica:** cpu = 100.138216 (sec), leaf count = 28

$$\text{DSolve}[ay(x) + y''(x) + y(x)y'(x) - y(x)^3 = 0, y(x), x]$$

**Maple:** cpu = 0.967 (sec), leaf count = 8191

**7.32 ODE No. 1622**

$$\frac{d^2}{dx^2}y(x) + (y(x) + 3a) \frac{d}{dx}y(x) - (y(x))^3 + a(y(x))^2 + 2a^2y(x) = 0$$

**Mathematica:** cpu = 26.601378 (sec), leaf count = 41

$$\text{DSolve}[2a^2y(x) + (3a + y(x))y'(x) + ay(x)^2 + y''(x) - y(x)^3 = 0, y(x), x]$$

**Maple:** cpu = 0.219 (sec), leaf count = 775

$$\left\{ y(x) = \frac{1}{e^{ax}} \text{RootOf} \left( \int^{-z} \frac{1}{-f^6 + C1} \left( -f^8 - C1 f^2 + \left( -f^{12} + 2 C1 f^6 - C1^2 + \sqrt{\frac{-f^6}{-f^6}} \right) \right) \right)$$

**7.33 ODE No. 1623**

$$\frac{d^2}{dx^2}y(x) + (y(x) + 3f(x)) \frac{d}{dx}y(x) - (y(x))^3 + f(x) (y(x))^2 + y(x) \left( \frac{d}{dx}f(x) + 2(f(x))^2 \right) = 0$$

**Mathematica:** cpu = 0.445557 (sec), leaf count = 50

$$\text{DSolve}[y(x) (f'(x) + 2f(x)^2) + (3f(x) + y(x))y'(x) + f(x)y(x)^2 + y''(x) - y(x)^3 = 0, y(x), x]$$

**Maple:** cpu = 2.340 (sec), leaf count = 0

could not solve

### 7.34 ODE No. 1624

$$\frac{d^2}{dx^2}y(x) + y(x) \frac{d}{dx}y(x) - (y(x))^3 - \left( \frac{\frac{d}{dx}f(x)}{f(x)} + f(x) \right) \left( 3 \frac{d}{dx}y(x) + (y(x))^2 \right) + \left( a(f(x))^2 + 3 \frac{d}{dx}f(x) \right)$$

**Mathematica:** cpu = 1.426181 (sec), leaf count = 93

$$\text{DSolve}\left[ y(x) \left( a f(x)^2 - \frac{f''(x)}{f(x)} + 3 f'(x) + \frac{3 f'(x)^2}{f(x)^2} \right) + b f(x)^3 - \left( \frac{f'(x)}{f(x)} + f(x) \right) (3 y'(x) + y(x)^2) + y''(x) \right]$$

**Maple:** cpu = 1.263 (sec), leaf count = 135

$$\left\{ y(x) = \text{ODESolStruc} \left( f \left( \text{RootOf} \left( \int -b(-a) d\_a + \_C1 - \int^{-Z} f(-f) d\_f \right) \right) \_a, \left[ \left\{ \frac{d}{d\_a} - b(-a) = \right. \right. \right. \right.$$

### 7.35 ODE No. 1625

$$\frac{d^2}{dx^2}y(x) + \left( y(x) - 3/2 \frac{\frac{d}{dx}f(x)}{f(x)} \right) \frac{d}{dx}y(x) - (y(x))^3 - 1/2 \frac{\left( \frac{d}{dx}f(x) \right) (y(x))^2}{f(x)} + 1/2 \frac{y(x)}{f(x)} \left( f(x) + \frac{\left( \frac{d}{dx}f(x) \right)}{f(x)} \right)$$

**Mathematica:** cpu = 0.963122 (sec), leaf count = 82

$$\text{DSolve}\left[ y'(x) \left( y(x) - \frac{3 f'(x)}{2 f(x)} \right) - \frac{y(x)^2 f'(x)}{2 f(x)} + y(x) \left( -\frac{f''(x)}{2 f(x)} + \frac{f'(x)^2}{f(x)^2} + f(x) \right) + y''(x) - y(x)^3 = 0, y(x) \right]$$

**Maple:** cpu = 0.343 (sec), leaf count = 0

could not solve

### 7.36 ODE No. 1626

$$\frac{d^2}{dx^2}y(x) + 2 y(x) \frac{d}{dx}y(x) + f(x) \frac{d}{dx}y(x) + \left( \frac{d}{dx}f(x) \right) y(x) = 0$$

**Mathematica:** cpu = 52.088114 (sec), leaf count = 33

$$\text{DSolve}[y(x) f'(x) + f(x) y'(x) + y''(x) + 2 y(x) y'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.156 (sec), leaf count = 48

$$\left\{ y(x) = \text{ODESolStruc} \left( -b(-a), \left[ \left\{ \frac{d}{d\_a} - b(-a) = -(-b(-a))^2 - f(-a) - b(-a) - \_C1 \right\}, \{ \_a = x, \_t \right. \right. \right. \right.$$

**7.37 ODE No. 1627**

$$\frac{d^2}{dx^2}y(x) + 2y(x) \frac{d}{dx}y(x) + f(x) \left( \frac{d}{dx}y(x) + (y(x))^2 \right) - g(x) = 0$$

**Mathematica:** cpu = 0.325541 (sec), leaf count = 35

$$\text{DSolve}[f(x) (y'(x) + y(x)^2) - g(x) + y''(x) + 2y(x)y'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.609 (sec), leaf count = 63

$$\left\{ y(x) = \text{ODESolStruc} \left( \_b(\_a), \left[ \left\{ e^{\int f(\_a) d\_a} (\_b(\_a))^2 + e^{\int f(\_a) d\_a} \frac{d}{d\_a} \_b(\_a) - \int e^{\int f(\_a) d\_a} g(\_a) \right\} \right] \right) \right.$$

**7.38 ODE No. 1628**

$$\frac{d^2}{dx^2}y(x) + 3y(x) \frac{d}{dx}y(x) + (y(x))^3 + f(x)y(x) - g(x) = 0$$

**Mathematica:** cpu = 7.278424 (sec), leaf count = 32

$$\text{DSolve}[f(x)y(x) - g(x) + y''(x) + 3y(x)y'(x) + y(x)^3 = 0, y(x), x]$$

**Maple:** cpu = 0.0 (sec), leaf count = 63

$$\left\{ y(x) = \frac{\frac{d}{dx} \text{DESol} \left( \left\{ -g(x) \_Y(x) + f(x) \frac{d}{dx} \_Y(x) + \frac{d^3}{dx^3} \_Y(x) \right\}, \{ \_Y(x) \} \right)}{\text{DESol} \left( \left\{ -g(x) \_Y(x) + f(x) \frac{d}{dx} \_Y(x) + \frac{d^3}{dx^3} \_Y(x) \right\}, \{ \_Y(x) \} \right)} \right\}$$

**7.39 ODE No. 1629**

$$\frac{d^2}{dx^2}y(x) + (3y(x) + f(x)) \frac{d}{dx}y(x) + (y(x))^3 + f(x)(y(x))^2 = 0$$

**Mathematica:** cpu = 0.036505 (sec), leaf count = 34

$$\text{DSolve}[(f(x) + 3y(x))y'(x) + f(x)y(x)^2 + y''(x) + y(x)^3 = 0, y(x), x]$$

**Maple:** cpu = 0.015 (sec), leaf count = 38

$$\left\{ y(x) = \frac{\int \_C1 e^{-\int f(x) dx} dx + \_C2}{\iint \_C1 e^{-\int f(x) dx} dx dx + \_C2 x + 1} \right\}$$

**7.40 ODE No. 1630**

$$\frac{d^2}{dx^2}y(x) - 3y(x) \frac{d}{dx}y(x) - 3a(y(x))^2 - 4a^2y(x) - b = 0$$

**Mathematica:** cpu = 11.895010 (sec), leaf count = 3227

$$\left\{ \left\{ y(x) \rightarrow - \frac{2 \left( (-1)^{\frac{a^{3/2} \sqrt{4a^3 - 3b} - 2a^3}}{4a^3} + 1 \right) 2^{-\frac{3(a^{3/2} \sqrt{4a^3 - 3b} - 2a^3)}{4a^3}} + \frac{3\sqrt{4a^6 - 3a^3b} + 1}{4a^3} 3^{\frac{a^{3/2} \sqrt{4a^3 - 3b} - 2a^3}{4a^3}} - \frac{\sqrt{4a^6 - 3a^3b}}{4a^3} a - \frac{a^{3/2} \sqrt{4a^3 - 3b}}{2a^3}}{\dots} \right. \right.$$

**Maple:** cpu = 0.405 (sec), leaf count = 803

$$\left\{ \int^{y(x)} -6a^2 \left( -12_a a^3 - 9_a a^2 a^2 + \left( \text{RootOf} \left( 2 K_{1/2} \frac{4a^3 - 3b}{\sqrt{(4a^3 - 3b)aa}} \left( -1/2 \frac{Z}{a^2} \right) - C1 a^2 + 3 K_{1/2} \frac{4a^3 - 3b}{\sqrt{(4a^3 - 3b)aa}} \right) \right. \right.$$

**7.41 ODE No. 1631**

$$\frac{d^2}{dx^2}y(x) - (3y(x) + f(x)) \frac{d}{dx}y(x) + (y(x))^3 + f(x) (y(x))^2 = 0$$

**Mathematica:** cpu = 0.032004 (sec), leaf count = 35

$$\text{DSolve}[-(f(x) + 3y(x))y'(x) + f(x)y(x)^2 + y''(x) + y(x)^3 = 0, y(x), x]$$

**Maple:** cpu = 0.031 (sec), leaf count = 38

$$\left\{ y(x) = \frac{- \int -C1 e^{\int f(x) dx} dx - C2}{\iint -C1 e^{\int f(x) dx} dx dx + C2 x + 1} \right\}$$

## 7.42 ODE No. 1632

$$\frac{d^2}{dx^2}y(x) - 2ay(x) \frac{d}{dx}y(x) = 0$$

**Mathematica:** cpu = 0.065008 (sec), leaf count = 46

$$\left\{ \left\{ y(x) \rightarrow \frac{\sqrt{c_1} \tan(\sqrt{a}\sqrt{c_1}x + \sqrt{a}\sqrt{c_1}c_2)}{\sqrt{a}} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 29

$$\left\{ y(x) = \frac{1}{a} \tan\left(-C2 \sqrt{-C1 a} + x \sqrt{-C1 a}\right) \sqrt{-C1 a} \right\}$$

## 7.43 ODE No. 1633

$$\frac{d^2}{dx^2}y(x) + ay(x) \frac{d}{dx}y(x) + b(y(x))^3 = 0$$

**Mathematica:** cpu = 35.438000 (sec), leaf count = 25

$$\text{DSolve}[ay(x)y'(x) + by(x)^3 + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.188 (sec), leaf count = 97

$$\left\{ \int^{y(x)} \left( \text{RootOf} \left( -2a \_a^2 \text{Artanh} \left( \frac{-a^2a + 4\_Z}{\sqrt{-a^4(a^2 - 8b)}} \right) \right) - \ln(-a^4b + \_Z \_a^2a + 2\_Z^2) \sqrt{-a^4(a^2 - 8b)} \right) \right\}$$

## 7.44 ODE No. 1634

$$\frac{d^2}{dx^2}y(x) + h(x, y(x)) \frac{d}{dx}y(x) + j(x, y(x)) = 0$$

**Mathematica:** cpu = 0.162521 (sec), leaf count = 24

$$\text{DSolve}[y'(x)h(x, y(x)) + j(x, y(x)) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.0 (sec), leaf count = 0

could not solve

**7.45 ODE No. 1635**

$$\frac{d^2}{dx^2}y(x) + a\left(\frac{d}{dx}y(x)\right)^2 + by(x) = 0$$

**Mathematica:** cpu = 101.517891 (sec), leaf count = 23

$$\text{DSolve}[ay'(x)^2 + by(x) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.109 (sec), leaf count = 79

$$\left\{ \int^{y(x)} -2 \frac{a}{\sqrt{4e^{-2a} - C1 a^2 - 4ab + 2b}} d_{-a} - x - C2 = 0, \int^{y(x)} 2 \frac{a}{\sqrt{4e^{-2a} - C1 a^2 - 4ab + 2b}} d_{-a} - x - C2 = 0 \right\}$$

**7.46 ODE No. 1636**

$$\frac{d^2}{dx^2}y(x) + a\left(\frac{d}{dx}y(x)\right) \left| \frac{d}{dx}y(x) \right| + b\frac{d}{dx}y(x) + cy(x) = 0$$

**Mathematica:** cpu = 36.575645 (sec), leaf count = 32

$$\text{DSolve}[ay'(x) |y'(x)| + by'(x) + cy(x) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.531 (sec), leaf count = 59

$$\left\{ y(x) = \text{ODESolStruc}\left(-a, \left[ \left( \frac{d}{d_{-a}} b(-a) \right) - b(-a) + a b(-a) |b(-a)| + b(-a) b + c_{-a} = 0 \right] \right), \dots \right\}$$

**7.47 ODE No. 1637**

$$\frac{d^2}{dx^2}y(x) + a\left(\frac{d}{dx}y(x)\right)^2 + b\frac{d}{dx}y(x) + cy(x) = 0$$

**Mathematica:** cpu = 30.477870 (sec), leaf count = 29

$$\text{DSolve}[ay'(x)^2 + by'(x) + cy(x) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.359 (sec), leaf count = 58

$$\left\{ y(x) = \text{ODESolStruc}\left(-a, \left[ \left( \frac{d}{d_{-a}} b(-a) \right) - b(-a) + a (b(-a))^2 + b(-a) b + c_{-a} = 0 \right] \right), \left\{ -a = \dots \right\} \right\}$$



**7.48 ODE No. 1638**

$$\frac{d^2}{dx^2}y(x) + a\left(\frac{d}{dx}y(x)\right)^2 + b\sin(y(x)) = 0$$

**Mathematica:** cpu = 100.155218 (sec), leaf count = 24

$$\text{DSolve}[ay'(x)^2 + b\sin(y(x)) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.125 (sec), leaf count = 126

$$\left\{ \int^{y(x)} (4a^2 + 1) \frac{1}{\sqrt{(4a^2 + 1)(4e^{-2a-a} C1 a^2 - 4\sin(-a)ab + 2b\cos(-a) + e^{-2a-a} C1)}} d_{-a-x} - \dots \right.$$

**7.49 ODE No. 1639**

$$\frac{d^2}{dx^2}y(x) + a\left(\frac{d}{dx}y(x)\right) \left| \frac{d}{dx}y(x) \right| + b\sin(y(x)) = 0$$

**Mathematica:** cpu = 41.170228 (sec), leaf count = 27

$$\text{DSolve}[ay'(x)|y'(x)| + b\sin(y(x)) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 2.246 (sec), leaf count = 56

$$\left\{ y(x) = \text{ODESolStruc}\left(-a, \left[ \left( \frac{d}{d_{-a}} b(-a) \right) - b(-a) + a b(-a) |b(-a)| + b\sin(-a) = 0 \right], \left\{ -a = \dots \right. \right.$$

**7.50 ODE No. 1640**

$$\frac{d^2}{dx^2}y(x) + ay(x) \left(\frac{d}{dx}y(x)\right)^2 + by(x) = 0$$

**Mathematica:** cpu = 200.467956 (sec), leaf count = 25

$$\text{DSolve}[ay(x)y'(x)^2 + by(x) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.109 (sec), leaf count = 70

$$\left\{ \int^{y(x)} a \frac{1}{\sqrt{a(e^{-a^2a} C1 a - b)}} d_{-a-x} - C2 = 0, \int^{y(x)} -a \frac{1}{\sqrt{a(e^{-a^2a} C1 a - b)}} d_{-a-x} - C2 = \dots \right.$$

**7.51 ODE No. 1641**

$$\frac{d^2}{dx^2}y(x) + h(y(x)) \left( \frac{d}{dx}y(x) \right)^2 + g(x) \frac{d}{dx}y(x) = 0$$

**Mathematica:** cpu = 2.378802 (sec), leaf count = 57

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \int_1^{\#1} e^{-\int_1^{K[4]} -h(K[1]) dK[1]} dK[4] \& \right] \left[ \int_1^x c_1 \left( -e^{-\int_1^{K[5]} g(K[2]) dK[2]} \right) dK[5] + c_2 \right] \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 29

$$\left\{ \int^{y(x)} e^{\int h(-b) d_b} d_b - \_C1 \int e^{-\int g(x) dx} dx - \_C2 = 0 \right\}$$

**7.52 ODE No. 1642**

$$\frac{d^2}{dx^2}y(x) - \frac{j(y(x)) \left( \frac{d}{dx}y(x) \right)^2}{h(y(x))} + g(x) \frac{d}{dx}y(x) + f(x) h(y(x)) = 0$$

**Mathematica:** cpu = 1.082137 (sec), leaf count = 40

$$\text{DSolve} \left[ f(x)h(y(x)) + g(x)y'(x) - \frac{j(y(x))y'(x)^2}{h(y(x))} + y''(x) = 0, y(x), x \right]$$

**Maple:** cpu = 0.203 (sec), leaf count = 0

could not solve

**7.53 ODE No. 1643**

$$\frac{(1 - D(j)(y(x))) \left( \frac{d}{dx}y(x) \right)^2}{j(y(x))} + f(x) \frac{d}{dx}y(x) + \frac{d^2}{dx^2}y(x) + g(x) j(y(x)) = 0$$

**Mathematica:** cpu = 0.409552 (sec), leaf count = 34

$$\text{DSolve} [f(x)y'(x) + g(x)j(y(x)) + h(y(x))y'(x)^2 + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.265 (sec), leaf count = 0

could not solve

**7.54 ODE No. 1644**

$$\frac{d^2}{dx^2}y(x) + h(y(x)) \left( \frac{d}{dx}y(x) \right)^2 + j(y(x)) \frac{d}{dx}y(x) + k(y(x)) = 0$$

**Mathematica:** cpu = 62.318914 (sec), leaf count = 32

$$\text{DSolve}[h(y(x))y'(x)^2 + j(y(x))y'(x) + k(y(x)) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.374 (sec), leaf count = 59

$$\left\{ y(x) = \text{ODESolStruc} \left( \_a, \left[ \left( \frac{d}{d\_a} \_b(\_a) \right) \_b(\_a) + h(\_a) (\_b(\_a))^2 + j(\_a) \_b(\_a) + k(\_a) = 0 \right] \right) \right.$$

**7.55 ODE No. 1645**

$$\frac{d^2}{dx^2}y(x) + \left( \left( \frac{d}{dx}y(x) \right)^2 + 1 \right) \left( h(x, y(x)) \frac{d}{dx}y(x) + j(x, y(x)) \right) = 0$$

**Mathematica:** cpu = 0.172522 (sec), leaf count = 34

$$\text{DSolve}[(y'(x)^2 + 1) (y'(x)h(x, y(x)) + j(x, y(x))) + y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.0 (sec), leaf count = 0

could not solve

**7.56 ODE No. 1646**

$$\frac{d^2}{dx^2}y(x) + ay(x) \left( \left( \frac{d}{dx}y(x) \right)^2 + 1 \right)^2 = 0$$

**Mathematica:** cpu = 10.814373 (sec), leaf count = 262

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\frac{\sqrt{\frac{\#1^2(-a)+2c_1+1}{2c_1+1}} \sqrt{2\#1^2a - 4c_1} E \left( \sin^{-1} \left( \sqrt{\frac{a}{2c_1+1}} \#1 \right) \left| 1 + \frac{1}{2c_1} \right. \right)}{\sqrt{\frac{a}{2c_1+1}} \sqrt{\#1^2(-a) + 2c_1 + 1} \sqrt{2 - \frac{\#1^2a}{c_1}}} \right] \& \right] [c_2 + x$$

**Maple:** cpu = 0.187 (sec), leaf count = 94

$$\left\{ \int^{y(x)} a(\_a^2 + 2\_C1) \frac{1}{\sqrt{-a(\_a^2 + 2\_C1)(\_a^2a + 2\_C1a - 1)}} d\_a - x - \_C2 = 0, \int^{y(x)} -a(\_a^2$$

**7.57 ODE No. 1647**

$$\frac{d^2}{dx^2}y(x) - a\left(x\frac{d}{dx}y(x) - y(x)\right)^r = 0$$

**Mathematica:** cpu = 48.122611 (sec), leaf count = 59

$$\left\{ \left\{ y(x) \rightarrow x \left( \int_1^x \left( \frac{1}{2}aK[2]^{2r} - \frac{1}{2}arK[2]^{2r} + c_1K[2]^{2r-2} \right)^{\frac{1}{1-r}} dK[2] + c_2 \right) \right\} \right\}$$

**Maple:** cpu = 0.312 (sec), leaf count = 123

$$\left\{ y(x) = \left( \int -\frac{ar}{2}2^{\frac{r}{r-1}} \left( (-arx^2 + ax^2 + \_C1)^{-1} \right)^{\frac{r}{r-1}} + \frac{a}{2}2^{\frac{r}{r-1}} \left( (-arx^2 + ax^2 + \_C1)^{-1} \right)^{\frac{r}{r-1}} + \frac{C1}{2x^2}2^{\frac{r}{r-1}} \right) \right\}$$

**7.58 ODE No. 1648**

$$\frac{d^2}{dx^2}y(x) - kx^a(y(x))^b \left( \frac{d}{dx}y(x) \right)^c = 0$$

**Mathematica:** cpu = 0.086011 (sec), leaf count = 27

$$\text{DSolve}[y''(x) - kx^a y(x)^b y'(x)^c = 0, y(x), x]$$

**Maple:** cpu = 1.404 (sec), leaf count = 413

$$\left\{ y(x) = \text{ODESolStruc} \left( \_a e^{\int -b(\_a) d\_a + \_C1}, \left[ \left\{ \frac{d}{d\_a} \_b(\_a) = -\frac{(\_b(\_a))^3}{(a-c+2)^2} \left( -a^b \left( -\frac{(a-c+2)(\_a)}{\_b(\_a)(b+} \right) \right) \right. \right. \right.$$

**7.59 ODE No. 1649**

$$\frac{d^2}{dx^2}y(x) + \left( \frac{d}{dx}y(x) - \frac{y(x)}{x} \right)^a h(x, y(x)) = 0$$

**Mathematica:** cpu = 2.647336 (sec), leaf count = 30

$$\text{DSolve} \left[ h(x, y(x)) \left( y'(x) - \frac{y(x)}{x} \right)^a + y''(x) = 0, y(x), x \right]$$

**Maple:** cpu = 0.0 (sec), leaf count = 0

could not solve

**7.60 ODE No. 1650**

$$\frac{d^2}{dx^2}y(x) - a\sqrt{\left(\frac{d}{dx}y(x)\right)^2 + 1} = 0$$

**Mathematica:** cpu = 0.023503 (sec), leaf count = 30

$$\left\{ \left\{ y(x) \rightarrow \frac{\sinh(c_1) \sinh(ax)}{a} + \frac{\cosh(c_1) \cosh(ax)}{a} + c_2 \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 18

$$\left\{ y(x) = \frac{\cosh(-C1 a + ax)}{a} + -C2 \right\}$$

**7.61 ODE No. 1651**

$$\frac{d^2}{dx^2}y(x) - a\sqrt{\left(\frac{d}{dx}y(x)\right)^2 + 1 - b} = 0$$

**Mathematica:** cpu = 0.284036 (sec), leaf count = 414

$$\left\{ \left\{ y(x) \rightarrow \frac{a \operatorname{InverseFunction} \left[ \frac{b \tan^{-1} \left( \frac{\#1 b}{\sqrt{\#1^2 + 1} \sqrt{a^2 - b^2}} \right) - \frac{b \tan^{-1} \left( \frac{\#1 a}{\sqrt{a^2 - b^2}} \right) + \sinh^{-1}(\#1)}{a}} \right] \& [c_1 + x]^2 - b \operatorname{InverseFu} \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 31

$$\left\{ y(x) = \int \operatorname{RootOf} \left( x - \int^{-Z} \left( a \sqrt{-f^2 + 1 + b} \right)^{-1} d_f + -C1 \right) dx + -C2 \right\}$$

## 7.62 ODE No. 1652

$$\frac{d^2}{dx^2}y(x) - a\sqrt{b(y(x))^2 + \left(\frac{d}{dx}y(x)\right)^2} = 0$$

**Mathematica:** cpu = 0.834106 (sec), leaf count = 31

$$\text{DSolve}\left[y''(x) - a\sqrt{by(x)^2 + y'(x)^2} = 0, y(x), x\right]$$

**Maple:** cpu = 0.203 (sec), leaf count = 36

$$\left\{ y(x) = e^{\int \text{RootOf}\left(x - f^{-z}(-f^2 + a\sqrt{-f^2 + b})^{-1} d_f + C1\right) dx + C2} \right\}$$

## 7.63 ODE No. 1653

$$\frac{d^2}{dx^2}y(x) - a\left(\left(\frac{d}{dx}y(x)\right)^2 + 1\right)^{3/2} = 0$$

**Mathematica:** cpu = 0.071509 (sec), leaf count = 75

$$\left\{ \left\{ y(x) \rightarrow c_2 - \frac{i\sqrt{a^2x^2 + 2ac_1x + c_1^2 - 1}}{a} \right\}, \left\{ y(x) \rightarrow c_2 + \frac{i\sqrt{a^2x^2 + 2ac_1x + c_1^2 - 1}}{a} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 55

$$\left\{ y(x) = \frac{(-C1 a + ax - 1)(-C1 a + ax + 1)}{a} \sqrt{-(C1^2 a^2 + 2 C1 a^2 x + a^2 x^2 - 1)^{-1}} + C2 \right\}$$

## 7.64 ODE No. 1654

$$\frac{d^2}{dx^2}y(x) - 2ax\left(\left(\frac{d}{dx}y(x)\right)^2 + 1\right)^{3/2} = 0$$

**Mathematica:** cpu = 0.311540 (sec), leaf count = 308

$$\left\{ \left\{ y(x) \rightarrow c_2 - \frac{\sqrt{\frac{ax^2+c_1-1}{c_1-1}} \sqrt{\frac{ax^2+c_1+1}{c_1+1}} \left( F\left(i \sinh^{-1}\left(x \sqrt{\frac{a}{c_1+1}}\right) \middle| \frac{c_1+1}{c_1-1}\right) + (c_1 - 1) E\left(i \sinh^{-1}\left(x \sqrt{\frac{a}{c_1+1}}\right) \middle| \frac{c_1}{c_1-1}\right) \right)}{\sqrt{\frac{a}{c_1+1}} \sqrt{a^2x^4 + 2ac_1x^2 + c_1^2 - 1}} \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 49

$$\left\{ y(x) = \int \sqrt{-(a^2x^4 + 4 C1 a^2x^2 + 4 C1^2 a^2 - 1)^{-1}} a(x^2 + 2 C1) dx + C2 \right\}$$

**7.65 ODE No. 1655**

$$\frac{d^2}{dx^2}y(x) - ay(x) \left( \left( \frac{d}{dx}y(x) \right)^2 + 1 \right)^{3/2} = 0$$

**Mathematica:** cpu = 0.887113 (sec), leaf count = 350

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\frac{\sqrt{\frac{\#1^2 a + 2c_1 - 2}{c_1 - 1}} \sqrt{\frac{\#1^2 a + 2c_1 + 2}{c_1 + 1}} \left( F \left( i \sinh^{-1} \left( \sqrt{\frac{a}{2c_1 + 2}} \#1 \right) \mid \frac{c_1 + 1}{c_1 - 1} \right) + (c_1 - 1) E \left( \sqrt{\frac{a}{2c_1 + 2}} \sqrt{\#1^4 a^2 + 4\#1^2 a c_1 + 4c_1^2 - 4} \right) \right)}{\sqrt{\frac{a}{2c_1 + 2}} \sqrt{\#1^4 a^2 + 4\#1^2 a c_1 + 4c_1^2 - 4}} \right] \right\} \right\}$$

**Maple:** cpu = 0.140 (sec), leaf count = 106

$$\left\{ \int^{y(x)} a(-a^2 + 2\_C1) \frac{1}{\sqrt{-_a^4 a^2 - 4\_C1\_a^2 a^2 - 4\_C1^2 a^2 + 4}} d\_a - x - \_C2 = 0, \int^{y(x)} -a(-a^2 -$$

**7.66 ODE No. 1656**

$$\frac{d^2}{dx^2}y(x) - a(c + bx + y(x)) \left( \left( \frac{d}{dx}y(x) \right)^2 + 1 \right)^{3/2} = 0$$

**Mathematica:** cpu = 100.341242 (sec), leaf count = 33

$$\text{DSolve} \left[ y''(x) - a(y'(x)^2 + 1)^{3/2} (bx + c + y(x)) = 0, y(x), x \right]$$

**Maple:** cpu = 0.499 (sec), leaf count = 771

$$\left\{ y(x) = -bx + \text{RootOf} \left( -x + \int^{-Z} \frac{1}{(\_f^4 a^2 + 4\_f^3 a^2 c + 4\_f^2 a^2 c^2 - 4\_C1\_f^2 a^2 - 8\_C1\_f a^2 c + 4$$

**7.67 ODE No. 1657**

$$\frac{d^2}{dx^2}y(x) + (y(x))^3 \frac{d}{dx}y(x) - y(x) \left( \frac{d}{dx}y(x) \right) \sqrt{(y(x))^4 + 4 \frac{d}{dx}y(x)} = 0$$

**Mathematica:** cpu = 0.152019 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow \sqrt{2} e^{c_1} \tan \left( 2\sqrt{2} e^{3c_1} (c_2 + x) \right) \right\} \right\}$$

**Maple:** cpu = 0.187 (sec), leaf count = 47

$$\left\{ y(x) = \frac{1}{\_C1} \tan \left( \_C2 (\_C1^{-2})^{\frac{3}{2}} + x (\_C1^{-2})^{\frac{3}{2}} \right), y(x) = \frac{1}{\_C1} \tanh \left( \_C2 (\_C1^{-2})^{\frac{3}{2}} + x (\_C1^{-2})^{\frac{3}{2}} \right) \right\}$$

**7.68 ODE No. 1658**

$$\frac{d^2}{dx^2}y(x) - h\left(\frac{d}{dx}y(x), ax + by(x)\right) = 0$$

**Mathematica:** cpu = 0.130517 (sec), leaf count = 26

$$\text{DSolve}[y''(x) - h(y'(x), ax + by(x)) = 0, y(x), x]$$

**Maple:** cpu = 0.094 (sec), leaf count = 117

$$\left\{ y(x) = \text{ODESolStruc}\left(-\frac{a(\int -b(-a) d_a + -C1) - b_a}{b}, \left[\left\{\frac{d}{d_a} - b(-a) = -h\left(-\frac{a_b(-a) - b}{-b(-a)b}, b_a\right)\right\}\right.\right.\right.$$

**7.69 ODE No. 1659**

$$\frac{d^2}{dx^2}y(x) - y(x)h\left(x, \frac{d}{dx}y(x)\right) = 0$$

**Mathematica:** cpu = 12.591099 (sec), leaf count = 26

$$\text{DSolve}\left[y''(x) - y(x)h\left(x, \frac{y'(x)}{y(x)}\right) = 0, y(x), x\right]$$

**Maple:** cpu = 0.063 (sec), leaf count = 60

$$\left\{ y(x) = \text{ODESolStruc}\left(e^{\int -b(-a) d_a + -C1}, \left[\left\{\frac{d}{d_a} - b(-a) = -(-b(-a))^2 + h(-a, -b(-a))\right\}, \left\{-a = x,\right.\right.\right.$$

**7.70 ODE No. 1660**

$$\frac{d^2}{dx^2}y(x) - x^{n-2}h\left(\frac{y(x)}{x^n}, \frac{d}{dx}y(x)\right) = 0$$

**Mathematica:** cpu = 3.899495 (sec), leaf count = 39

$$\text{DSolve}[y''(x) - x^{n-2}h(x^{-n}y(x), x^{1-n}y'(x)) = 0, y(x), x]$$

**Maple:** cpu = 0.640 (sec), leaf count = 132

$$\left\{ y(x) = \text{ODESolStruc}\left(\frac{-a}{e^{-(\int -b(-a) d_a + -C1)^n}}, \left[\left\{\frac{d}{d_a} - b(-a) = \left(-a n^2 - -a n - h\left(-a, \frac{-b(-a) - a n}{-b(-a)}\right)\right\}\right.\right.\right.$$



### 7.71 ODE No. 1661

$$8 \frac{d^2}{dx^2} y(x) + 9 \left( \frac{d}{dx} y(x) \right)^4 = 0$$

**Mathematica:** cpu = 0.034004 (sec), leaf count = 92

$$\left\{ \left\{ y(x) \rightarrow c_2 - \frac{1}{3} \sqrt[3]{-\frac{1}{3}(9x - 8c_1)^{2/3}} \right\}, \left\{ y(x) \rightarrow \frac{(9x - 8c_1)^{2/3}}{3\sqrt[3]{3}} + c_2 \right\}, \left\{ y(x) \rightarrow \frac{(-1)^{2/3}(9x - 8c_1)^{2/3}}{3\sqrt[3]{3}} \right\} \right.$$

**Maple:** cpu = 0.062 (sec), leaf count = 51

$$\left\{ y(x) = (_C1 + x)^{\frac{2}{3}} + _C2, y(x) = \frac{i\sqrt{3} - 1}{2} (_C1 + x)^{\frac{2}{3}} + _C2, y(x) = -\frac{i\sqrt{3} + 1}{2} (_C1 + x)^{\frac{2}{3}} + _C2 \right.$$

### 7.72 ODE No. 1662

$$a \frac{d^2}{dx^2} y(x) + h \left( \frac{d}{dx} y(x) \right) + cy(x) = 0$$

**Mathematica:** cpu = 1.537195 (sec), leaf count = 22

$$\text{DSolve}[ay''(x) + cy(x) + h(y'(x)) = 0, y(x), x]$$

**Maple:** cpu = 0.266 (sec), leaf count = 56

$$\left\{ y(x) = \text{ODESolStruc} \left( -a, \left[ \left( \frac{d}{d\_a} b(-a) \right) - b(-a) + \frac{h(-b(-a)) + c\_a}{a} = 0 \right], \left\{ -a = y(x), -b(-a) \right. \right.$$

### 7.73 ODE No. 1663

$$x \frac{d^2}{dx^2} y(x) + 2 \frac{d}{dx} y(x) - x(y(x))^n = 0$$

**Mathematica:** cpu = 0.037005 (sec), leaf count = 26

$$\text{DSolve}[-xy(x)^n + xy''(x) + 2y'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.593 (sec), leaf count = 151

$$\left\{ y(x) = \text{ODESolStruc} \left( -a e^{\int -b(-a) d\_a + _C1}, \left[ \frac{d}{d\_a} b(-a) = \left( -\frac{a^n n^2}{4} + \frac{a^n n}{2} - \frac{a n}{2} - \frac{a^n}{4} + \frac{3}{2} \right. \right. \right.$$

**7.74 ODE No. 1664**

$$x \frac{d^2}{dx^2} y(x) + 2 \frac{d}{dx} y(x) + ax^m (y(x))^n = 0$$

**Mathematica:** cpu = 0.537568 (sec), leaf count = 28

$$\text{DSolve}[ax^m y(x)^n + xy''(x) + 2y'(x) = 0, y(x), x]$$

**Maple:** cpu = 2.355 (sec), leaf count = 185

$$\left\{ y(x) = \text{ODESolStruc} \left( \_a e^{\int \_b(\_a) d\_a + \_C1}, \left[ \left\{ \frac{d}{d\_a} \_b(\_a) = \frac{(\_a^n a n^2 - 2 \_a^n a n + \_a m^2 - \_a m n + \dots)}{(m \dots)} \right. \right. \right. \right.$$

**7.75 ODE No. 1665**

$$x \frac{d^2}{dx^2} y(x) + 2 \frac{d}{dx} y(x) + x e^{y(x)} = 0$$

**Mathematica:** cpu = 0.400051 (sec), leaf count = 25

$$\text{DSolve}[xy''(x) + 2y'(x) + x e^{y(x)} = 0, y(x), x]$$

**Maple:** cpu = 0.405 (sec), leaf count = 84

$$\left\{ y(x) = \text{ODESolStruc} \left( \_a - 2 \int \_b(\_a) d\_a - 2 \_C1, \left[ \left\{ \frac{d}{d\_a} \_b(\_a) = (e^{-a} - 2) (\_b(\_a))^3 + (\_b(\_a)) \dots \right. \right. \right. \right.$$

**7.76 ODE No. 1666**

$$x \frac{d^2}{dx^2} y(x) + a \frac{d}{dx} y(x) + b x e^{y(x)} = 0$$

**Mathematica:** cpu = 0.593575 (sec), leaf count = 26

$$\text{DSolve}[ay'(x) + b x e^{y(x)} + xy''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.608 (sec), leaf count = 93

$$\left\{ y(x) = \text{ODESolStruc} \left( \_a - 2 \int \_b(\_a) d\_a - 2 \_C1, \left[ \left\{ \frac{d}{d\_a} \_b(\_a) = (b e^{-a} - 2 a + 2) (\_b(\_a))^3 - \dots \right. \right. \right. \right.$$

**7.77 ODE No. 1667**

$$x \frac{d^2}{dx^2} y(x) + a \frac{d}{dx} y(x) + bx^{5-2a} e^{y(x)} = 0$$

**Mathematica:** cpu = 0.640581 (sec), leaf count = 32

$$\text{DSolve}[bx^{5-2a} e^{y(x)} + ay'(x) + xy''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.983 (sec), leaf count = 124

$$\left\{ y(x) = \text{ODESolStruc} \left( \_a + 2a \left( \int \_b(\_a) d\_a + \_C1 \right) - 6 \int \_b(\_a) d\_a - 6 \_C1, \left[ \frac{d}{d\_a} \_b(\_a) \right] \right) \right\}$$

**7.78 ODE No. 1668**

$$x \frac{d^2}{dx^2} y(x) - (1 - y(x)) \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.082010 (sec), leaf count = 60

$$\left\{ \left\{ y(x) \rightarrow \sqrt{2} \sqrt{c_1 + 2} \tanh \left( \frac{1}{2} \left( \sqrt{2} \sqrt{c_1 + 2} \log(x) - 2\sqrt{2} \sqrt{c_1 + 2} c_2 \right) \right) + 2 \right\} \right\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 24

$$\left\{ y(x) = \frac{1}{\_C1} \left( 2 \_C1 + \tanh \left( \frac{\ln(x) - \_C2}{2 \_C1} \right) \right) \right\}$$

**7.79 ODE No. 1669**

$$x \frac{d^2}{dx^2} y(x) - x^2 \left( \frac{d}{dx} y(x) \right)^2 + 2 \frac{d}{dx} y(x) + (y(x))^2 = 0$$

**Mathematica:** cpu = 103.487141 (sec), leaf count = 126

$$\text{Solve} \left[ \int_1^{y(x)} -\frac{x}{c_1 e^{xK[1]} + 2xK[1] + 1} dK[1] - \int_1^x \left( -\frac{y(x)}{c_1 e^{y(x)K[2]} + 2y(x)K[2] + 1} - \frac{c_1 e^{y(x)K[2]} + y(x)}{K[2] (c_1 e^{y(x)K[2]} + 2y(x)K[2] + 1)} \right) dx \right]$$

**Maple:** cpu = 0.094 (sec), leaf count = 32

$$\left\{ y(x) = \frac{1}{x} \text{RootOf} \left( -\ln(x) + \_C2 + \int^{-Z} -(e^{-f} \_C1 - 2 \_f - 1)^{-1} d\_f \right) \right\}$$

**7.80 ODE No. 1670**

$$x \frac{d^2}{dx^2} y(x) + a \left( x \frac{d}{dx} y(x) - y(x) \right)^2 - b = 0$$

**Mathematica:** cpu = 90.651011 (sec), leaf count = 50

$$\left\{ \left\{ y(x) \rightarrow x \left( \int_1^x \frac{\sqrt{-\frac{b}{a}} \tan \left( c_1 - a \sqrt{-\frac{b}{a}} K[2] \right)}{K[2]^2} dK[2] + c_2 \right) \right\} \right\}$$

**Maple:** cpu = 0.281 (sec), leaf count = 35

$$\left\{ y(x) = \left( \int \frac{i}{x^2} \tan \left( -i\sqrt{a}\sqrt{bx} + \_C1 \right) \sqrt{b} \frac{1}{\sqrt{a}} dx + \_C2 \right) x \right\}$$

**7.81 ODE No. 1671**

$$2x \frac{d^2}{dx^2} y(x) + \left( \frac{d}{dx} y(x) \right)^3 + \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.042505 (sec), leaf count = 59

$$\left\{ \left\{ y(x) \rightarrow c_2 - 2ie^{c_1} \sqrt{e^{2c_1} - x} \right\}, \left\{ y(x) \rightarrow c_2 + 2ie^{c_1} \sqrt{e^{2c_1} - x} \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 35

$$\left\{ y(x) = -2 \frac{\sqrt{-C1 x - 1}}{-C1} + \_C2, y(x) = 2 \frac{\sqrt{-C1 x - 1}}{-C1} + \_C2 \right\}$$

**7.82 ODE No. 1672**

$$x^2 \frac{d^2}{dx^2} y(x) - a((y(x))^n - y(x)) = 0$$

**Mathematica:** cpu = 19.524479 (sec), leaf count = 27

$$\text{DSolve}[x^2 y''(x) - a(y(x)^n - y(x)) = 0, y(x), x]$$

**Maple:** cpu = 0.702 (sec), leaf count = 67

$$\left\{ y(x) = \text{ODESolStruc} \left( -a, \left[ \left\{ \frac{d}{d\_a} b(-a) = (-\_a^n a + a\_a) (-b(-a))^3 - (-b(-a))^2 \right\}, \left\{ -a = y(x), \right. \right. \right.$$

### 7.83 ODE No. 1673

$$x^2 \frac{d^2}{dx^2} y(x) + a(e^{y(x)} - 1) = 0$$

**Mathematica:** cpu = 35.890057 (sec), leaf count = 23

$$\text{DSolve}[a(e^{y(x)} - 1) + x^2 y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.514 (sec), leaf count = 65

$$\left\{ y(x) = \text{ODESolStruc} \left( \_a, \left[ \left\{ \frac{d}{d\_a} \_b(\_a) = (ae^{-a} - a) (\_b(\_a))^3 - (\_b(\_a))^2 \right\} \right], \left\{ \_a = y(x), \_b(\_a) \right\} \right) \right\}$$

### 7.84 ODE No. 1674

$$x^2 \frac{d^2}{dx^2} y(x) - (2a + b - 1) x \frac{d}{dx} y(x) + (c^2 b^2 x^{2b} + a(a + b)) y(x) = 0$$

**Mathematica:** cpu = 0.066008 (sec), leaf count = 106

$$\left\{ \left\{ y(x) \rightarrow c_2 2^{-\frac{a+b}{b}} c^{\frac{a+b}{b}-1} (x^{2b})^{\frac{a+b}{2b}-\frac{1}{2}} \sin \left( c\sqrt{x^{2b}} \right) + c_1 2^{-\frac{a}{b}} c^{a/b} (x^{2b})^{\frac{a}{2b}} \cos \left( c\sqrt{x^{2b}} \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 27

$$\{ y(x) = \_C1 \sin(x^b c) x^a + \_C2 \cos(x^b c) x^a \}$$

### 7.85 ODE No. 1675

$$x^2 \frac{d^2}{dx^2} y(x) + (a + 1) x \frac{d}{dx} y(x) - x^k h \left( x^k y(x), x \frac{d}{dx} y(x) + k y(x) \right) = 0$$

**Mathematica:** cpu = 3.448438 (sec), leaf count = 47

$$\text{DSolve}[x^k (-h(x^k y(x), ky(x) + xy'(x))) + (a + 1)xy'(x) + x^2 y''(x) = 0, y(x), x]$$

**Maple:** cpu = 1.638 (sec), leaf count = 0

could not solve

**7.86 ODE No. 1676**

$$x^2 \frac{d^2}{dx^2} y(x) + a \left( x \frac{d}{dx} y(x) - y(x) \right)^2 - bx^2 = 0$$

**Mathematica:** cpu = 54.698946 (sec), leaf count = 133

$$\left\{ \left\{ y(x) \rightarrow x \left( c_2 + \int_1^x \frac{i\sqrt{a}\sqrt{b}Y_1(-i\sqrt{a}\sqrt{b}K[2]) - i\sqrt{a}\sqrt{b}c_1J_1(i\sqrt{a}\sqrt{b}K[2])}{aK[2](c_1J_0(i\sqrt{a}\sqrt{b}K[2]) + Y_0(-i\sqrt{a}\sqrt{b}K[2]))} dK[2] \right) \right\} \right\}$$

**Maple:** cpu = 0.920 (sec), leaf count = 110

$$\left\{ y(x) = \left( \int -\frac{C1}{ax} Y_1(\sqrt{-abx}) \sqrt{-ab} (-C1 Y_0(\sqrt{-abx}) + J_0(\sqrt{-abx}))^{-1} - \frac{1}{ax} J_1(\sqrt{-abx}) \sqrt{-ab} \right) \right\}$$

**7.87 ODE No. 1677**

$$x^2 \frac{d^2}{dx^2} y(x) + ay(x) \left( \frac{d}{dx} y(x) \right)^2 + bx = 0$$

**Mathematica:** cpu = 46.986967 (sec), leaf count = 28

$$\text{DSolve}[ay(x)y'(x)^2 + bx + x^2y''(x) = 0, y(x), x]$$

**Maple:** cpu = 2.309 (sec), leaf count = 101

$$\left\{ y(x) = \text{ODESolStruc} \left( -a e^{\int -b(-a) d_a + C1}, \left[ \left\{ \frac{d}{d_a} -b(-a) = (a_a^3 + b) (-b(-a))^3 + (2_a^2 a + 1) \right. \right. \right. \right)$$

**7.88 ODE No. 1678**

$$x^2 \frac{d^2}{dx^2} y(x) - \sqrt{ax^2 \left( \frac{d}{dx} y(x) \right)^2 + b(y(x))^2} = 0$$

**Mathematica:** cpu = 1.836733 (sec), leaf count = 39

$$\text{DSolve}[x^2y''(x) - \sqrt{ax^2y'(x)^2 + by(x)^2} = 0, y(x), x]$$

**Maple:** cpu = 1.622 (sec), leaf count = 60

$$\left\{ y(x) - e^{\int^{\ln(x)} \text{RootOf} \left( \int^{-z} -y(x) \left( -a^2y(x) - a y(x) - \sqrt{(y(x))^2(-a^2a+b)} \right)^{-1} d_a - b + C1 \right) d_b + C2} = 0 \right\}$$

**7.89 ODE No. 1679**

$$(x^2 + 1) \frac{d^2}{dx^2} y(x) + \left( \frac{d}{dx} y(x) \right)^2 + 1 = 0$$

**Mathematica:** cpu = 0.042005 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \rightarrow -x \cot(c_1) + \csc^2(c_1) \log(-x \sin(c_1) - \cos(c_1)) + c_2 \right\} \right\}$$

**Maple:** cpu = 0.826 (sec), leaf count = 27

$$\left\{ y(x) = \frac{x}{-C1} + \ln(x - C1 - 1) + \frac{\ln(x - C1 - 1)}{-C1^2} + -C2 \right\}$$

**7.90 ODE No. 1680**

$$4x^2 \frac{d^2}{dx^2} y(x) - x^4 \left( \frac{d}{dx} y(x) \right)^2 + 4y(x) = 0$$

**Mathematica:** cpu = 10.873881 (sec), leaf count = 31

$$\text{DSolve}[x^4(-y'(x)^2) + 4x^2y''(x) + 4y(x) = 0, y(x), x]$$

**Maple:** cpu = 1.092 (sec), leaf count = 103

$$\left\{ y(x) = \text{ODESolStruc} \left( \frac{-a}{(e^{f-b(a)d-a+C1})^2}, \left[ \left\{ \frac{d}{d_a} -b(-a) = (-a^2 + 7-a) (-b(-a))^3 + (-a - 5) (- \right. \right. \right.$$

**7.91 ODE No. 1681**

$$9x^2 \frac{d^2}{dx^2} y(x) + a(y(x))^3 + 2y(x) = 0$$

**Mathematica:** cpu = 3.482442 (sec), leaf count = 26

$$\text{DSolve}[ay(x)^3 + 9x^2y''(x) + 2y(x) = 0, y(x), x]$$

**Maple:** cpu = 0.780 (sec), leaf count = 31

$$\left\{ y(x) = -C2 \text{JacobiSN} \left( \left( \frac{\sqrt{2}}{2x^3} \sqrt{x^{\frac{20}{3}} a + -C1} \right) -C2, i \right) \sqrt[3]{x} \right\}$$

### 7.92 ODE No. 1682

$$x^3 \left( \frac{d^2}{dx^2} y(x) + y(x) \frac{d}{dx} y(x) - (y(x))^3 \right) + 12xy(x) + 24 = 0$$

**Mathematica:** cpu = 22.595369 (sec), leaf count = 35

$$\text{DSolve}[x^3(y''(x) + y(x)y'(x) - y(x)^3) + 12xy(x) + 24 = 0, y(x), x]$$

**Maple:** cpu = 1.186 (sec), leaf count = 102

$$\left\{ y(x) = \text{ODESolStruc} \left( \_a e^{\int \_b(\_a) d\_a + \_C1}, \left[ \left\{ \frac{d}{d\_a} \_b(\_a) = (-\_a^3 - \_a^2 + 14\_a + 24) (\_b(\_a))^3 \right. \right. \right. \right.$$

### 7.93 ODE No. 1683

$$x^3 \frac{d^2}{dx^2} y(x) - a \left( x \frac{d}{dx} y(x) - y(x) \right)^2 = 0$$

**Mathematica:** cpu = 0.068509 (sec), leaf count = 26

$$\left\{ \left\{ y(x) \rightarrow -\frac{x \log(a(-\frac{c_1}{x} - c_2))}{a} \right\} \right\}$$

**Maple:** cpu = 0.796 (sec), leaf count = 23

$$\left\{ y(x) = -\frac{x}{a} \ln \left( \frac{a(\_C1 x - \_C2)}{x} \right) \right\}$$

### 7.94 ODE No. 1684

$$2x^3 \frac{d^2}{dx^2} y(x) + x^2(9 + 2xy(x)) \frac{d}{dx} y(x) + b + xy(x)(a + 3xy(x) - 2x^2(y(x))^2) = 0$$

**Mathematica:** cpu = 53.614308 (sec), leaf count = 52

$$\text{DSolve}[xy(x)(a - 2x^2y(x)^2 + 3xy(x)) + b + 2x^3y''(x) + x^2(2xy(x) + 9)y'(x) = 0, y(x), x]$$

**Maple:** cpu = 1.810 (sec), leaf count = 108

$$\left\{ y(x) = \text{ODESolStruc} \left( \_a e^{\int \_b(\_a) d\_a + \_C1}, \left[ \left\{ \frac{d}{d\_a} \_b(\_a) = \left( -\_a^3 + \frac{\_a^2}{2} + \frac{\_a\_a}{2} - \frac{5\_a}{2} + \frac{b}{2} \right) (\_b(\_a)) \right. \right. \right. \right.$$



### 7.95 ODE No. 1685

$$2(-x^k + 4x^3) \left( \frac{d^2}{dx^2} y(x) + y(x) \frac{d}{dx} y(x) - (y(x))^3 \right) - (kx^{k-1} - 12x^2) \left( 3 \frac{d}{dx} y(x) + (y(x))^2 \right) + axy(x)$$

**Mathematica:** cpu = 4.994134 (sec), leaf count = 70

$$\text{DSolve}[axy(x) + b - (kx^{k-1} - 12x^2) (3y'(x) + y(x)^2) + 2(4x^3 - x^k) (y''(x) + y(x)y'(x) - y(x)^3) = 0, y(x), x]$$

**Maple:** cpu = 3.650 (sec), leaf count = 0

could not solve

### 7.96 ODE No. 1686

$$x^4 \frac{d^2}{dx^2} y(x) + a^2 (y(x))^n = 0$$

**Mathematica:** cpu = 0.032504 (sec), leaf count = 23

$$\text{DSolve}[a^2 y(x)^n + x^4 y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.764 (sec), leaf count = 160

$$\left\{ y(x) = \text{ODESolStruc} \left( \_a e^{\int \_b(\_a) d\_a + \_C1}, \left[ \left\{ \frac{d}{d\_a} \_b(\_a) = \left( \frac{-a^n n^2 a^2}{4} - \frac{a^n n a^2}{2} + \frac{a^n a^2}{4} - \frac{a n}{2} \right) \right. \right. \right.$$

### 7.97 ODE No. 1687

$$x^4 \frac{d^2}{dx^2} y(x) - x(x^2 + 2y(x)) \frac{d}{dx} y(x) + 4(y(x))^2 = 0$$

**Mathematica:** cpu = 0.069509 (sec), leaf count = 262

$$\left\{ \left\{ y(x) \rightarrow \frac{x^3 \left( i \left( -\frac{\sqrt{-c_1-1}}{\sqrt{c_1}} + \frac{i}{\sqrt{c_1}} \right) \sqrt{c_1} c_2 x^{-1+i \left( -\frac{\sqrt{-c_1-1}}{\sqrt{c_1}} + \frac{i}{\sqrt{c_1}} \right) \sqrt{c_1}} + i \left( \frac{\sqrt{-c_1-1}}{\sqrt{c_1}} + \frac{i}{\sqrt{c_1}} \right) \sqrt{c_1} x^{-1+i \left( \frac{\sqrt{-c_1-1}}{\sqrt{c_1}} + \frac{i}{\sqrt{c_1}} \right) \sqrt{c_1}}}{c_2 x^{i \left( -\frac{\sqrt{-c_1-1}}{\sqrt{c_1}} + \frac{i}{\sqrt{c_1}} \right) \sqrt{c_1}} + x^{i \left( \frac{\sqrt{-c_1-1}}{\sqrt{c_1}} + \frac{i}{\sqrt{c_1}} \right) \sqrt{c_1}}} \right. \right.$$

**Maple:** cpu = 1.544 (sec), leaf count = 23

$$\{y(x) = \tanh(-\ln(x) \_C1 + \_C2 \_C1) x^2 \_C1 + x^2\}$$

**7.98 ODE No. 1688**

$$x^4 \frac{d^2}{dx^2} y(x) - x^2 \left( x + \frac{d}{dx} y(x) \right) \frac{d}{dx} y(x) + 4(y(x))^2 = 0$$

**Mathematica:** cpu = 283.320477 (sec), leaf count = 166

$$\text{Solve} \left[ \int_1^{y(x)} \frac{1}{c_1 x^2 \left( -e^{\frac{K[1]}{x^2}} \right) + 4K[1] + 2x^2} dK[1] - \int_1^x \left( \frac{K[2] \left( c_1 e^{\frac{y(x)}{K[2]^2}} + 2 \left( -\frac{y(x)}{K[2]^2} - 1 \right) \right)}{c_1 K[2]^2 \left( -e^{\frac{y(x)}{K[2]^2}} \right) + 2K[2]^2 + 4y(x)} \right) + 2 \left( \frac{1}{K[2]} \right) \right]$$

**Maple:** cpu = 1.638 (sec), leaf count = 32

$$\left\{ y(x) = \text{RootOf} \left( -\ln(x) + \_C2 - \int^{-z} (e^{-f} \_C1 + 4\_f + 2)^{-1} d\_f \right) x^2 \right\}$$

**7.99 ODE No. 1689**

$$x^4 \frac{d^2}{dx^2} y(x) + \left( x \frac{d}{dx} y(x) - y(x) \right)^3 = 0$$

**Mathematica:** cpu = 0.642582 (sec), leaf count = 329

$$\left\{ \left\{ y(x) \rightarrow -ix \log \left( -\frac{\sqrt{-8ic_1 x^2 - \sinh(2c_2) - \cosh(2c_2)}}{4c_1 x} - \frac{i \sinh(c_2)}{4c_1 x} - \frac{i \cosh(c_2)}{4c_1 x} \right) \right\}, \left\{ y(x) \rightarrow -ix \right\} \right\}$$

**Maple:** cpu = 1.623 (sec), leaf count = 37

$$\left\{ y(x) = \left( -\arctan \left( \frac{1}{\sqrt{\_C1 x^2 - 1}} \right) + \_C2 \right) x, y(x) = \left( \arctan \left( \frac{1}{\sqrt{\_C1 x^2 - 1}} \right) + \_C2 \right) x \right\}$$

**7.100 ODE No. 1690**

$$\left( \frac{d^2}{dx^2} y(x) \right) \sqrt{x} - (y(x))^{3/2} = 0$$

**Mathematica:** cpu = 22.744388 (sec), leaf count = 25

$$\text{DSolve}[\sqrt{x} y''(x) - y(x)^{3/2} = 0, y(x), x]$$

**Maple:** cpu = 3.479 (sec), leaf count = 97

$$\left\{ y(x) = \text{ODESolStruc} \left( \frac{-a}{(e^{f\_b(-a)} d\_a + \_C1)^3}, \left[ \left\{ \frac{d}{d\_a} b(-a) = \left( -\_a^{\frac{3}{2}} + 12\_a \right) (\_b(-a))^3 - 7(\_b(-a) \right) \right\} \right] \right)$$

**7.101 ODE No. 1691**

$$(ax^2 + bx + c)^{3/2} \frac{d^2}{dx^2} y(x) - F\left(\frac{y(x)}{\sqrt{ax^2 + bx + c}}\right) = 0$$

**Mathematica:** cpu = 61.997373 (sec), leaf count = 46

$$\text{DSolve}\left[y''(x) (ax^2 + bx + c)^{3/2} - f\left(\frac{y(x)}{\sqrt{ax^2 + bx + c}}\right) = 0, y(x), x\right]$$

**Maple:** cpu = 0.795 (sec), leaf count = 254

$$\left\{ y(x) = \text{RootOf}\left(-2a \arctan\left(\frac{2ax + b}{\sqrt{4ac - b^2}}\right) - 2 \int^{-z} \frac{a}{\sqrt{4C1a^2 - 4c_g^2a + b^2_g^2 + 8 \int F(_g) d_g}} \right.$$

**7.102 ODE No. 1692**

$$x^{\frac{n}{n+1}} \frac{d^2}{dx^2} y(x) - (y(x))^{\frac{2n+1}{n+1}} = 0$$

**Mathematica:** cpu = 0.083011 (sec), leaf count = 37

$$\text{DSolve}\left[x^{\frac{n}{n+1}} y''(x) - y(x)^{\frac{2n+1}{n+1}} = 0, y(x), x\right]$$

**Maple:** cpu = 3.370 (sec), leaf count = 165

$$\left\{ y(x) = \text{ODESolStruc}\left(-a \left(e^{\frac{(f-b(_a) d_{-a} - C1)(n+2)}{n}}\right)^{-1}, \left[\left\{ \frac{d}{d_{-a}} b(_a) = -\frac{(b(_a))^3}{n^2} \left(-a^{\frac{2n+1}{n+1}} n^2 - 2_{-a} n\right.\right.\right.\right.$$

**7.103 ODE No. 1693**

$$(f(x))^2 \frac{d^2}{dx^2} y(x) + f(x) \left(\frac{d}{dx} f(x)\right) \frac{d}{dx} y(x) - h\left(y(x), f(x) \frac{d}{dx} y(x)\right) = 0$$

**Mathematica:** cpu = 0.952121 (sec), leaf count = 39

$$\text{DSolve}\left[-h(y(x), f(x)y'(x)) + f(x)f'(x)y'(x) + f(x)^2y''(x) = 0, y(x), x\right]$$

**Maple:** cpu = 0.218 (sec), leaf count = 68

$$\left\{ y(x) = \text{ODESolStruc}\left(-a, \left[\left\{ \frac{d}{d_{-a}} b(_a) = -h(_a, (b(_a))^{-1}) (b(_a))^3 \right\}, \left\{ -a = y(x), -b(_a) \right.\right.\right.\right.$$

**7.104 ODE No. 1694**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) - a = 0$$

**Mathematica:** cpu = 0.196025 (sec), leaf count = 115

$$\left\{ \left\{ y(x) \rightarrow \exp \left( \frac{-c_1 - 2a \operatorname{erf}^{-1} \left( -i \sqrt{\frac{2}{\pi}} \sqrt{a e^{\frac{c_1}{a}} (c_2 + x)^2} \right)^2}{2a} \right) \right\} \right\}, \left\{ y(x) \rightarrow \exp \left( \frac{-c_1 - 2a \operatorname{erf}^{-1} \left( i \sqrt{\frac{2}{\pi}} \sqrt{a e^{\frac{c_1}{a}} (c_2 + x)^2} \right)^2}{2a} \right) \right\}$$

**Maple:** cpu = 1.669 (sec), leaf count = 55

$$\left\{ \int^{y(x)} \frac{1}{\sqrt{2 a \ln(-a) - 2 C1 a}} d_{-a} - x - C2 = 0, \int^{y(x)} -\frac{1}{\sqrt{2 a \ln(-a) - 2 C1 a}} d_{-a} - x - C2 = 0 \right.$$

**7.105 ODE No. 1695**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) - ax = 0$$

**Mathematica:** cpu = 25.610752 (sec), leaf count = 18

$$\text{DSolve}[y(x)y''(x) - ax = 0, y(x), x]$$

**Maple:** cpu = 2.090 (sec), leaf count = 103

$$\left\{ y(x) = \text{ODESolStruc} \left( -a \left( e^{\int -b(-a) d_{-a} + C1} \right)^{\frac{3}{2}}, \left[ \frac{d}{d_{-a}} - b(-a) = \frac{(3_{-a}^2 - 4a) (_b(-a))^3}{4_{-a}} + 2(_b(-a)) \right] \right.$$

**7.106 ODE No. 1696**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) - ax^2 = 0$$

**Mathematica:** cpu = 24.305086 (sec), leaf count = 20

$$\text{DSolve}[y(x)y''(x) - ax^2 = 0, y(x), x]$$

**Maple:** cpu = 1.856 (sec), leaf count = 102

$$\left\{ y(x) = \text{ODESolStruc} \left( -a \left( e^{\int -b(-a) d_{-a} + C1} \right)^2, \left[ \frac{d}{d_{-a}} - b(-a) = \frac{(2_{-a}^2 - a) (_b(-a))^3}{-a} + 3(_b(-a)) \right] \right.$$

**7.107 ODE No. 1697**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) + \left( \frac{d}{dx} y(x) \right)^2 - a = 0$$

**Mathematica:** cpu = 0.062508 (sec), leaf count = 94

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{2a^2c_2x + a^2c_2^2 + a^2x^2 - e^{2c_1}}}{\sqrt{a}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{2a^2c_2x + a^2c_2^2 + a^2x^2 - e^{2c_1}}}{\sqrt{a}} \right\} \right\}$$

**Maple:** cpu = 1.669 (sec), leaf count = 39

$$\left\{ y(x) = \sqrt{ax^2 - 2\_C1x + 2\_C2}, y(x) = -\sqrt{ax^2 - 2\_C1x + 2\_C2} \right\}$$

**7.108 ODE No. 1698**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) + (y(x))^2 - ax - b = 0$$

**Mathematica:** cpu = 0.039505 (sec), leaf count = 72

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{ax^3 + 3bx^2 + 3c_2x + 6c_1}}{\sqrt{3}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{ax^3 + 3bx^2 + 3c_2x + 6c_1}}{\sqrt{3}} \right\} \right\}$$

**Maple:** cpu = 1.669 (sec), leaf count = 0

could not solve

**7.109 ODE No. 1699**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) + \left( \frac{d}{dx} y(x) \right)^2 - \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.037505 (sec), leaf count = 40

$$\left\{ \left\{ y(x) \rightarrow c_1 \left( -W \left( -\frac{e^{-\frac{x}{c_1} - \frac{c_2}{c_1} - 1}}{c_1} \right) \right) - c_1 \right\} \right\}$$

**Maple:** cpu = 1.622 (sec), leaf count = 33

$$\left\{ y(x) = -\_C1 \left( \text{lambertW} \left( -\frac{e^{-1}}{-\_C1} \left( e^{-\frac{C2}{C1}} \right)^{-1} \left( e^{-\frac{x}{C1}} \right)^{-1} \right) + 1 \right) \right\}$$

**7.110 ODE No. 1700**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 + 1 = 0$$

**Mathematica:** cpu = 0.073009 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow -e^{-c_1} \sinh(e^{c_1}(c_2 + x)) \right\}, \left\{ y(x) \rightarrow e^{-c_1} \sinh(e^{c_1}(c_2 + x)) \right\} \right\}$$

**Maple:** cpu = 1.669 (sec), leaf count = 79

$$\left\{ y(x) = \frac{-C1}{2} \left( 1 \left( e^{-\frac{C2}{C1}} \right)^{-2} \left( e^{-\frac{x}{C1}} \right)^{-2} - 1 \right) e^{-\frac{C2}{C1}} e^{-\frac{x}{C1}}, y(x) = \frac{C1}{2} \left( \left( e^{-\frac{C2}{C1}} \right)^2 \left( e^{-\frac{x}{C1}} \right)^2 - 1 \right) \left( e^{-\frac{C2}{C1}} \right)^{-1} \left( e^{-\frac{x}{C1}} \right)^{-1} \right\}$$

**7.111 ODE No. 1701**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 - 1 = 0$$

**Mathematica:** cpu = 0.180523 (sec), leaf count = 97

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} e^{-e^{c_1} x - 2c_1 - e^{c_1} c_2} \left( e^{2e^{c_1}(c_2+x)} + e^{2c_1} \right) \right\}, \left\{ y(x) \rightarrow \frac{1}{2} \left( e^{-e^{c_1} x - 2c_1 - e^{c_1} c_2} + e^{e^{c_1} x + e^{c_1} c_2} \right) \right\} \right\}$$

**Maple:** cpu = 1.654 (sec), leaf count = 79

$$\left\{ y(x) = \frac{-C1}{2} \left( 1 \left( e^{-\frac{C2}{C1}} \right)^{-2} \left( e^{-\frac{x}{C1}} \right)^{-2} + 1 \right) e^{-\frac{C2}{C1}} e^{-\frac{x}{C1}}, y(x) = \frac{C1}{2} \left( \left( e^{-\frac{C2}{C1}} \right)^2 \left( e^{-\frac{x}{C1}} \right)^2 + 1 \right) \left( e^{-\frac{C2}{C1}} \right)^{-1} \left( e^{-\frac{x}{C1}} \right)^{-1} \right\}$$

**7.112 ODE No. 1702**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 + e^x y(x) (c(y(x))^2 + d) + e^{2x} (b + a(y(x))^4) = 0$$

**Mathematica:** cpu = 5.336178 (sec), leaf count = 50

$$\text{DSolve}[e^{2x} (ay(x)^4 + b) + e^x y(x) (cy(x)^2 + d) + y(x)y''(x) - y'(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 3.448 (sec), leaf count = 0

could not solve

**7.113 ODE No. 1703**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 - (y(x))^2 \ln(y(x)) = 0$$

**Mathematica:** cpu = 0.094512 (sec), leaf count = 63

$$\left\{ \left\{ y(x) \rightarrow e^{\frac{1}{2}(e^{c_2+x} - c_1 e^{-c_2-x})} \right\}, \left\{ y(x) \rightarrow e^{\frac{1}{2}(e^{-c_2-x} - c_1 e^{c_2+x})} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 25

$$\left\{ y(x) = e^{-\frac{e^{2x} c_1}{2 e^x}} e^{\frac{c_2}{2 e^x}} \right\}$$

**7.114 ODE No. 1704**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 - \frac{d}{dx} y(x) + f(x) (y(x))^3 + (y(x))^2 \left( \frac{\frac{d^2}{dx^2} f(x)}{f(x)} - \frac{\left( \frac{d}{dx} f(x) \right)^2}{(f(x))^2} \right) = 0$$

**Mathematica:** cpu = 41.261240 (sec), leaf count = 62

$$\text{DSolve} \left[ y(x)^2 \left( \frac{f''(x)}{f(x)} - \frac{f'(x)^2}{f(x)^2} \right) + f(x) y(x)^3 + y(x) y''(x) - y'(x)^2 - y'(x) = 0, y(x), x \right]$$

**Maple:** cpu = 0.390 (sec), leaf count = 0

could not solve

**7.115 ODE No. 1705**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 + f(x) \frac{d}{dx} y(x) - \left( \frac{d}{dx} f(x) \right) y(x) - (y(x))^3 = 0$$

**Mathematica:** cpu = 0.244531 (sec), leaf count = 43

$$\text{DSolve}[-y(x)f'(x) + f(x)y'(x) + y(x)y''(x) - y'(x)^2 - y(x)^3 = 0, y(x), x]$$

**Maple:** cpu = 0.375 (sec), leaf count = 0

could not solve

**7.116 ODE No. 1706**

$$\left(\frac{d^2}{dx^2}y(x)\right)y(x) - \left(\frac{d}{dx}y(x)\right)^2 + \left(\frac{d}{dx}f(x)\right)\frac{d}{dx}y(x) - \left(\frac{d^2}{dx^2}f(x)\right)y(x) + f(x)(y(x))^3 - (y(x))^4 = 0$$

**Mathematica:** cpu = 0.482561 (sec), leaf count = 52

DSolve[-y(x)f''(x) + f'(x)y'(x) + f(x)y(x)^3 + y(x)y''(x) - y'(x)^2 - y(x)^4 = 0, y(x), x]

**Maple:** cpu = 0.390 (sec), leaf count = 0

could not solve

**7.117 ODE No. 1707**

$$\left(\frac{d^2}{dx^2}y(x)\right)y(x) - \left(\frac{d}{dx}y(x)\right)^2 + ay(x)\frac{d}{dx}y(x) + b(y(x))^2 = 0$$

**Mathematica:** cpu = 0.072509 (sec), leaf count = 31

$$\left\{ \left\{ y(x) \rightarrow c_2 e^{-\frac{bx}{a} - \frac{c_1 e^{-ax}}{a}} \right\} \right\}$$

**Maple:** cpu = 1.545 (sec), leaf count = 39

$$\left\{ y(x) = 1 e^{\frac{e^{-ax} C_1}{a}} e^{\frac{b}{a^2}} \left(e^{\frac{bx}{a}}\right)^{-1} \left(e^{-\frac{C_2}{a}}\right)^{-1} \right\}$$

**7.118 ODE No. 1708**

$$\left(\frac{d^2}{dx^2}y(x)\right)y(x) - \left(\frac{d}{dx}y(x)\right)^2 + ay(x)\frac{d}{dx}y(x) - 2a(y(x))^2 + b(y(x))^3 = 0$$

**Mathematica:** cpu = 46.194866 (sec), leaf count = 43

DSolve[ay(x)y'(x) - 2ay(x)^2 + by(x)^3 + y(x)y''(x) - y'(x)^2 = 0, y(x), x]

**Maple:** cpu = 2.106 (sec), leaf count = 73

$$\left\{ y(x) = ODESolStruc\left(-a, \left[ \left(\frac{d}{dx} - b(-a)\right) - b(-a) - \frac{(-b(-a))^2 - a - b(-a)a - b(-a)^3 + 2(-a)^2 a}{-a} \right] \right)$$



**7.119 ODE No. 1709**

$$\left(\frac{d^2}{dx^2}y(x)\right)y(x) - \left(\frac{d}{dx}y(x)\right)^2 - (-1 + ay(x))\frac{d}{dx}y(x) + 2a^2(y(x))^2 - 2b^2(y(x))^3 + ay(x) = 0$$

**Mathematica:** cpu = 61.278281 (sec), leaf count = 56

$$\text{DSolve}[2a^2y(x)^2 - (ay(x) - 1)y'(x) + ay(x) - 2b^2y(x)^3 + y(x)y''(x) - y'(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 2.792 (sec), leaf count = 84

$$\left\{y(x) = \text{ODESolStruc}\left(-a, \left[\left(\frac{d}{d\_a}b(-a)\right) - b(-a) - \frac{2b^2\_a^3 - 2\_a^2a^2 + \_a\_b(-a)a + (-b(-a))}{\_a}\right]\right)\right.$$

**7.120 ODE No. 1710**

$$\left(\frac{d^2}{dx^2}y(x)\right)y(x) - \left(\frac{d}{dx}y(x)\right)^2 + (-1 + ay(x))\frac{d}{dx}y(x) - y(x)(1 + y(x))(b^2(y(x))^2 - a^2) = 0$$

**Mathematica:** cpu = 104.391256 (sec), leaf count = 55

$$\text{DSolve}[-y(x)(y(x) + 1)(b^2y(x)^2 - a^2) + (ay(x) - 1)y'(x) + y(x)y''(x) - y'(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 4.383 (sec), leaf count = 91

$$\left\{y(x) = \text{ODESolStruc}\left(-a, \left[\left(\frac{d}{d\_a}b(-a)\right) - b(-a) - \frac{-a^4b^2 + b^2\_a^3 - \_a^2a^2 - \_a\_b(-a)a - \_a}{\_a}\right]\right)\right.$$

**7.121 ODE No. 1711**

$$\left(\frac{d^2}{dx^2}y(x)\right)y(x) - \left(\frac{d}{dx}y(x)\right)^2 + (\tan(x) + \cot(x))y(x)\frac{d}{dx}y(x) + ((\cos(x))^2 - n^2(\cot(x))^2)(y(x))^2 = 0$$

**Mathematica:** cpu = 635.571707 (sec), leaf count = 915

$$\left\{y(x) \rightarrow e^e\right.$$

**Maple:** cpu = 0.390 (sec), leaf count = 81

$$\left\{ y(x) = 1 e^{\frac{Y_n(\sin(x))_{-C2}}{\sin(x)(J_n(\sin(x))Y_{n+1}(\sin(x)) - J_{n+1}(\sin(x))Y_n(\sin(x)))}} \left( e^{\frac{J_n(\sin(x))_{-C1}}{\sin(x)(J_n(\sin(x))Y_{n+1}(\sin(x)) - J_{n+1}(\sin(x))Y_n(\sin(x)))}} \right)^{-1} \right\}$$

### 7.122 ODE No. 1712

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 - f(x) y(x) \frac{d}{dx} y(x) - g(x) (y(x))^2 = 0$$

**Mathematica:** cpu = 10.804372 (sec), leaf count = 70

$$\left\{ \left\{ y(x) \rightarrow c_2 \exp \left( \int_1^x \left( c_1 e^{\int_1^{K[3]} f(K[1]) dK[1]} + e^{\int_1^{K[3]} f(K[1]) dK[1]} \int_1^{K[2]} g(K[2]) e^{-\int_1^{K[2]} f(K[1]) dK[1]} dK[2] \right) dK \right) \right\} \right.$$

**Maple:** cpu = 0.063 (sec), leaf count = 61

$$\left\{ y(x) = \frac{-C2}{e^{-C1} \int e^{\int f(x) dx} dx} e^{\int e^{\int f(x) dx} dx \int \frac{g(x)}{e^{\int f(x) dx}} dx} \left( e^{\int \frac{e^{\int f(x) dx} dx g(x)}{e^{\int f(x) dx}} dx} \right)^{-1} \right\}$$

### 7.123 ODE No. 1713

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 + (g(x) + f(x) (y(x))^2) \frac{d}{dx} y(x) - y(x) \left( \frac{d}{dx} g(x) - \left( \frac{d}{dx} f(x) \right) (y(x))^2 \right) = 0$$

**Mathematica:** cpu = 21.002667 (sec), leaf count = 56

$$\text{DSolve}[-y(x) (g'(x) - y(x)^2 f'(x)) + y'(x) (f(x) y(x)^2 + g(x)) + y(x) y''(x) - y'(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 0.234 (sec), leaf count = 60

$$\left\{ y(x) = \text{ODESolStruc} \left( -b(-a), \left[ \left\{ \frac{\frac{d}{da} b(-a)}{-b(-a)} + \frac{f(-a) (-b(-a))^2 + -C1 b(-a) - g(-a)}{-b(-a)} = 0 \right\}, \{ \right. \right.$$

**7.124 ODE No. 1714**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) - 3 \left( \frac{d}{dx} y(x) \right)^2 + 3 y(x) \frac{d}{dx} y(x) - (y(x))^2 = 0$$

**Mathematica:** cpu = 0.060508 (sec), leaf count = 25

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 e^x}{\sqrt{1 - 2e^{c_1 + x}}} \right\} \right\}$$

**Maple:** cpu = 1.513 (sec), leaf count = 67

$$\left\{ y(x) = -\frac{\sqrt{2}}{2\_C1 e^x - 2\_C2} \sqrt{(-C1 e^x - C2) e^{2x}}, y(x) = \frac{\sqrt{2}}{2\_C1 e^x - 2\_C2} \sqrt{(-C1 e^x - C2) e^{2x}} \right\}$$

**7.125 ODE No. 1715**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) - a \left( \frac{d}{dx} y(x) \right)^2 = 0$$

**Mathematica:** cpu = 0.034504 (sec), leaf count = 26

$$\left\{ \left\{ y(x) \rightarrow c_2 (-ax - c_1 + x)^{\frac{1}{1-a}} \right\} \right\}$$

**Maple:** cpu = 1.638 (sec), leaf count = 25

$$\left\{ y(x) = \left( \frac{1}{(1-a)(-C1 x + C2)} \right)^{(a-1)^{-1}} \right\}$$

**7.126 ODE No. 1716**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) + a \left( \left( \frac{d}{dx} y(x) \right)^2 + 1 \right) = 0$$

**Mathematica:** cpu = 0.645082 (sec), leaf count = 172

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\frac{\#1 \sqrt{1 - e^{2c_1} \#1^{-2a}} {}_2F_1\left(\frac{1}{2}, -\frac{1}{2a}; 1 - \frac{1}{2a}; e^{2c_1} \#1^{-2a}\right)}{\sqrt{e^{2c_1} \#1^{-2a} - 1}} \& \right] [c_2 + x] \right\}, \left\{ y(x) \rightarrow \dots \right\} \right\}$$

**Maple:** cpu = 1.622 (sec), leaf count = 68

$$\left\{ \int^{y(x)} \frac{1}{-a^{-a} \sqrt{-a^{2a} + C1}} d_{-a-x-C2} = 0, \int^{y(x)} -\frac{1}{-a^{-a} \sqrt{-a^{2a} + C1}} d_{-a-x-C2} = 0 \right\}$$

**7.127 ODE No. 1717**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) + a \left( \frac{d}{dx} y(x) \right)^2 + b(y(x))^3 = 0$$

**Mathematica:** cpu = 1.553697 (sec), leaf count = 290

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\frac{\sqrt{2a+3} \#1^{a+1} \sqrt{\frac{-2b\#1^{2a+3} + 2ac_1 + 3c_1}{(2a+3)c_1}} {}_2F_1\left(\frac{1}{2}, \frac{a+1}{2a+3}; \frac{a+1}{2a+3} + 1; \frac{2b\#1^{2a+3}}{2ac_1 + 3c_1}\right)}{(a+1)\sqrt{-2b\#1^{2a+3} + 2ac_1 + 3c_1}} \& \right] \right\} \right\} [c_2]$$

**Maple:** cpu = 1.716 (sec), leaf count = 108

$$\left\{ \int^{y(x)} (2a+3) a^{2a} \frac{1}{\sqrt{-(2a+3) a^{2a} (2 a^{2a+3} b - C1)}} da - x - C2 = 0, \int^{y(x)} -(2a+3) a^{2a}$$

**7.128 ODE No. 1718**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) + a \left( \frac{d}{dx} y(x) \right)^2 + b y(x) \frac{d}{dx} y(x) + c(y(x))^2 + d(y(x))^{1-a} = 0$$

**Mathematica:** cpu = 1.508191 (sec), leaf count = 744

$$\left\{ \left\{ y(x) \rightarrow \left( -\frac{ad \exp\left(\frac{1}{2}x(\sqrt{-4ac+b^2-4c}+b)\right) - \frac{x(b\sqrt{-4ac+b^2-4c}-4(a+1)c+b^2)}{\sqrt{-4ac+b^2-4c+b}} - \frac{2(a+1)cx}{\sqrt{-4ac+b^2-4c+b}}}{(a+1)c} \right) \right\} \right\} d \exp$$

**Maple:** cpu = 0.187 (sec), leaf count = 158

$$\left\{ y(x) = 1 \left( c^2(-4ac+b^2-4c) \left( -C2 ce^{-\frac{x}{2}(-b+\sqrt{-4ac+b^2-4c})} a - e^{\frac{x}{2}(b+\sqrt{-4ac+b^2-4c})} -C1 ac + -C2 ce^{-\frac{x}{2}}$$

**7.129 ODE No. 1719**

$$\left(\frac{d^2}{dx^2}y(x)\right)y(x) + a\left(\frac{d}{dx}y(x)\right)^2 + f(x)y(x)\frac{d}{dx}y(x) + g(x)(y(x))^2 = 0$$

**Mathematica:** cpu = 41.860316 (sec), leaf count = 38

$$\text{DSolve}[ay'(x)^2 + f(x)y(x)y'(x) + g(x)y(x)^2 + y(x)y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.374 (sec), leaf count = 70

$$\left\{y(x) = \text{ODESolStruc}\left(e^{\int -b(-a)d\_a + -C1}, \left[\frac{d}{d\_a} - b(-a) = (-a - 1)(-b(-a))^2 - f(-a)_-b(-a) - g(-a)\right]\right)\right.$$

**7.130 ODE No. 1720**

$$\left(\frac{d^2}{dx^2}y(x)\right)y(x) + a\left(\frac{d}{dx}y(x)\right)^2 + b(y(x))^2\frac{d}{dx}y(x) + c(y(x))^4 = 0$$

**Mathematica:** cpu = 89.226830 (sec), leaf count = 38

$$\text{DSolve}[ay'(x)^2 + by(x)^2y'(x) + cy(x)^4 + y(x)y''(x) = 0, y(x), x]$$

**Maple:** cpu = 1.747 (sec), leaf count = 174

$$\left\{\int^{y(x)} (2a + 4) \left(\tan\left(\text{RootOf}\left(2\_Zb\_a^2 - 2a \ln(\_a) \sqrt{-a^4(4ac - b^2 + 8c)} - \ln\left(\frac{-a^4(4ac(\tan(\_Z))}{\dots}\right)\right)\right)\right)\right.$$

**7.131 ODE No. 1721**

$$\left(\frac{d^2}{dx^2}y(x)\right)y(x) - \frac{(a-1)\left(\frac{d}{dx}y(x)\right)^2}{a} - f(x)(y(x))^2\frac{d}{dx}y(x) + \frac{af(x)^2(y(x))^4}{(a+2)^2} - \frac{a\left(\frac{d}{dx}f(x)\right)(y(x))^3}{a+2} = 0$$

**Mathematica:** cpu = 0.927618 (sec), leaf count = 71

$$\text{DSolve}\left[-\frac{ay(x)^3f'(x)}{a+2} + \frac{af(x)^2y(x)^4}{(a+2)^2} - \frac{(a-1)y'(x)^2}{a} - f(x)y(x)^2y'(x) + y(x)y''(x) = 0, y(x), x\right]$$

**Maple:** cpu = 1.856 (sec), leaf count = 0

could not solve

**7.132 ODE No. 1722**

$$\left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 - 1 - 2ay(x) \left( \left( \frac{d}{dx} y(x) \right)^2 + 1 \right)^{3/2} = 0$$

**Mathematica:** cpu = 1.926745 (sec), leaf count = 797

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\frac{\left( (4c_1 a^2 + \sqrt{8c_1 a^2 + 1} + 1) E\left( i \sinh^{-1} \left( \sqrt{2} \sqrt{\frac{a^2}{-4c_1 a^2 + \sqrt{8c_1 a^2 + 1} - 1}} \right) \right) \right) \frac{4c_1 a^2}{4c_1 a^2}} \right]} \right\} \right.$$

**Maple:** cpu = 3.339 (sec), leaf count = 98

$$\left\{ \int^{y(x)} (-a^2 a + \_C1) \frac{1}{\sqrt{-a^4 a^2 - 2\_C1 - a^2 a - \_C1^2 + \_a^2}} d\_a - x - \_C2 = 0, \int^{y(x)} -(\_a^2 a + \_C1) \frac{1}{\sqrt{-a^4 a^2 - 2\_C1 - a^2 a - \_C1^2 + \_a^2}} d\_a - x - \_C2 = 0 \right\}$$

**7.133 ODE No. 1723**

$$\left( \frac{d^2}{dx^2} y(x) \right) (y(x) + x) + \left( \frac{d}{dx} y(x) \right)^2 - \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 1.971750 (sec), leaf count = 1033

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{2} e^{-c_1} (2e^{c_1} x - 1) + \frac{\sqrt{-4e^{2c_1} x^2 - 4x^2 + 4e^{-c_1} x + 4e^{c_1} x + e^{-2c_1} - 4e^{-c_1} c_2^2 + 4e^{c_1} c_2^2 + 1}}{2\sqrt{2}} - \frac{1}{2} \right\} \right.$$

**Maple:** cpu = 1.591 (sec), leaf count = 16

$$\left\{ y(x) = \sqrt{\_C1 + 2x\_C2} + \_C1 + x \right\}$$

**7.134 ODE No. 1724**

$$\left( \frac{d^2}{dx^2} y(x) \right) (x - y(x)) + 2 \left( \frac{d}{dx} y(x) \right) \left( \frac{d}{dx} y(x) + 1 \right) = 0$$

**Mathematica:** cpu = 0.198525 (sec), leaf count = 38

$$\left\{ \left\{ y(x) \rightarrow -\frac{e^{-c_1} (e^{c_1} c_2 x + e^{c_1} c_2^2 + 1)}{c_2 + x} \right\} \right\}$$

**Maple:** cpu = 1.919 (sec), leaf count = 21

$$\left\{ y(x) = \frac{\_C2^2 - \_C2 x + \_C1}{\_C2 - x} \right\}$$

**7.135 ODE No. 1725**

$$\left( \frac{d^2}{dx^2} y(x) \right) (x - y(x)) - \left( \frac{d}{dx} y(x) + 1 \right) \left( \left( \frac{d}{dx} y(x) \right)^2 + 1 \right) = 0$$

**Mathematica:** cpu = 0.327042 (sec), leaf count = 75

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{-2c_2x + e^{2c_1} - c_2^2 - x^2 - c_2} \right\}, \left\{ y(x) \rightarrow \sqrt{-2c_2x + e^{2c_1} - c_2^2 - x^2 - c_2} \right\} \right\}$$

**Maple:** cpu = 1.997 (sec), leaf count = 105

$$\left\{ y(x) = x + \text{RootOf} \left( -x + \int^{-Z} (-C1^2 f^2 - 1) \left( -C1^2 f^2 + C1 \sqrt{-C1^2 f^2 + 2f + 2} \right)^{-1} d_f \right) \right\}$$

**7.136 ODE No. 1726**

$$\left( \frac{d^2}{dx^2} y(x) \right) (x - y(x)) - h \left( \frac{d}{dx} y(x) \right) = 0$$

**Mathematica:** cpu = 0.753596 (sec), leaf count = 75

$$\text{Solve} \left[ \left\{ x = \int \frac{\exp \left( -\int_1^{K\$6747475} \frac{K[3]-1}{h(K[3])} dK[3] - c_1 \right)}{h(K\$6747475)} dK\$6747475 + c_2, y(x) = x - \exp \left( -\int_1^{K\$6747475} \frac{K}{h} \right) \right\} \right]$$

**Maple:** cpu = 0.078 (sec), leaf count = 39

$$\left\{ y(x) = x + \text{RootOf} \left( -x + \int^{-Z} \left( -1 + \text{RootOf} \left( \int^{-Z} \frac{a-1}{h(-a)} d_a + \ln(-g) + C1 \right) \right)^{-1} d_g + C2 \right) \right\}$$

**7.137 ODE No. 1727**

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) + \left( \frac{d}{dx} y(x) \right)^2 + 1 = 0$$

**Mathematica:** cpu = 0.172522 (sec), leaf count = 129

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ e^{2c_1} \tan^{-1} \left( \frac{\sqrt{\#1}}{\sqrt{e^{2c_1} - \#1}} \right) - \sqrt{\#1} \sqrt{e^{2c_1} - \#1} \right] [c_2 + x] \right\}, \left\{ y(x) \rightarrow \text{InverseFunction} \left[ e^{2c_1} \tan^{-1} \left( \frac{\sqrt{\#1}}{\sqrt{e^{2c_1} - \#1}} \right) + \sqrt{\#1} \sqrt{e^{2c_1} - \#1} \right] [c_2 + x] \right\} \right\}$$

**Maple:** cpu = 1.716 (sec), leaf count = 95

$$\left\{ -\sqrt{-C1 y(x) - (y(x))^2} + \frac{C1}{2} \arctan \left( 1 \left( y(x) - \frac{C1}{2} \right) \frac{1}{\sqrt{-C1 y(x) - (y(x))^2}} \right) - x - C2 = 0, \right.$$

**7.138 ODE No. 1728**

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 + a = 0$$

**Mathematica:** cpu = 0.005501 (sec), leaf count = 31

$$\left\{ \left\{ y(x) \rightarrow \frac{x^2(c_1^2 - a)}{4c_2} + c_1x + c_2 \right\} \right\}$$

**Maple:** cpu = 1.622 (sec), leaf count = 24

$$\left\{ y(x) = \frac{(-C1^2 - a)x^2}{4-C2} + -C1x + -C2 \right\}$$

**7.139 ODE No. 1729**

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 + f(x) (y(x))^2 + a = 0$$

**Mathematica:** cpu = 0.022503 (sec), leaf count = 31

$$\text{DSolve}[a + f(x)y(x)^2 + 2y(x)y''(x) - y'(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 0.359 (sec), leaf count = 0

could not solve

**7.140 ODE No. 1730**

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 - 8(y(x))^3 = 0$$

**Mathematica:** cpu = 0.483061 (sec), leaf count = 127

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{2}i\sqrt{c_1}\text{ns} \left( \frac{1}{2} \left( -(-1)^{3/4}\sqrt{2}\sqrt[4]{c_1}x - (-1)^{3/4}\sqrt{2}\sqrt[4]{c_1}c_2 \right) \middle| -1 \right)^2 \right\}, \left\{ y(x) \rightarrow -\frac{1}{2}i\sqrt{c_1}\text{ns} \left( \frac{1}{2} \left( -(-1)^{3/4}\sqrt{2}\sqrt[4]{c_1}x - (-1)^{3/4}\sqrt{2}\sqrt[4]{c_1}c_2 \right) \middle| -1 \right)^2 \right\} \right\}$$

**Maple:** cpu = 1.669 (sec), leaf count = 53

$$\left\{ \int^{y(x)} \frac{1}{\sqrt{4-a^3 + -C1-a}} d_{-a-x} - -C2 = 0, \int^{y(x)} -\frac{1}{\sqrt{4-a^3 + -C1-a}} d_{-a-x} - -C2 = 0 \right\}$$



**7.141 ODE No. 1731**

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 - 8 (y(x))^3 - 4 (y(x))^2 = 0$$

**Mathematica:** cpu = 1.403178 (sec), leaf count = 359

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \frac{2i\#1 \sqrt{\frac{c_1}{\#1(2-2\sqrt{1-c_1})}} + 1 \sqrt{\frac{c_1}{\#1(2\sqrt{1-c_1}+2)}} + 1 F \left( i \sinh^{-1} \left( \frac{\sqrt{\frac{c_1}{2\sqrt{1-c_1}+2}}}{\sqrt{\#1}} \right) \right) \right] \right. \right.$$

**Maple:** cpu = 1.653 (sec), leaf count = 63

$$\left\{ \int^{y(x)} \frac{1}{\sqrt{4a^3 + aC1 + 4a^2}} da - x - C2 = 0, \int^{y(x)} -\frac{1}{\sqrt{4a^3 + aC1 + 4a^2}} da - x - \dots \right.$$

**7.142 ODE No. 1732**

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 - 4 (x + 2 y(x)) (y(x))^2 = 0$$

**Mathematica:** cpu = 1.657711 (sec), leaf count = 35

$$\text{DSolve}[2y(x)y''(x) - y'(x)^2 - 4(2y(x) + x)y(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 1.825 (sec), leaf count = 0

could not solve

**7.143 ODE No. 1733**

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 + (ay(x) + b) (y(x))^2 = 0$$

**Mathematica:** cpu = 2.552324 (sec), leaf count = 437

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \frac{i\sqrt{2}\#1^{3/2} \sqrt{\frac{4c_1}{\#1(\sqrt{2ac_1+b^2-b})}} + 2 \sqrt{1 - \frac{2c_1}{\#1(\sqrt{2ac_1+b^2+b})}} F \left( i \sinh^{-1} \left( \frac{\sqrt{2}\sqrt{\frac{b^2}{\sqrt{2ac_1+b^2-b}}}}{\sqrt{\#1}} \right) \right) \right. \right. \right.$$

Maple: cpu = 1.560 (sec), leaf count = 71

$$\left\{ \int^{y(x)} -2 \frac{1}{\sqrt{-2a_a^3 - 4b_a^2 + 4_a_C1}} d_a - x - _C2 = 0, \int^{y(x)} 2 \frac{1}{\sqrt{-2a_a^3 - 4b_a^2 + 4_a_C1}} d_a - x - _C2 = 0 \right.$$

### 7.144 ODE No. 1734

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 + 1 + 2x(y(x))^2 + a(y(x))^3 = 0$$

Mathematica: cpu = 1.481688 (sec), leaf count = 37

$$\text{DSolve}[ay(x)^3 + 2y(x)y''(x) - y'(x)^2 + 2xy(x)^2 + 1 = 0, y(x), x]$$

Maple: cpu = 1.841 (sec), leaf count = 0

could not solve

### 7.145 ODE No. 1735

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 + (ay(x) + bx)(y(x))^2 = 0$$

Mathematica: cpu = 1.244158 (sec), leaf count = 36

$$\text{DSolve}[y(x)^2(ay(x) + bx) + 2y(x)y''(x) - y'(x)^2 = 0, y(x), x]$$

Maple: cpu = 1.638 (sec), leaf count = 0

could not solve

### 7.146 ODE No. 1736

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 - 3(y(x))^4 = 0$$

Mathematica: cpu = 8.595591 (sec), leaf count = 285

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \frac{2i\#1^{3/2} \sqrt{(-1)^{5/6} \left( \frac{\sqrt[3]{-c_1}}{\#1} - 1 \right) \sqrt{\frac{(-c_1)^{2/3}}{\#1^2} + \frac{\sqrt[3]{-c_1}}{\#1}} + 1F \left( \sin^{-1} \left( \frac{\sqrt{-\frac{i\sqrt[3]{-c_1}}{\#1}}}{\sqrt[4]{3}} \right)}{\sqrt[4]{3} \sqrt{-c_1} \sqrt{\#1^3 + c_1}} \right)} \right. \right. \right.$$

**Maple:** cpu = 1.654 (sec), leaf count = 49

$$\left\{ \int^{y(x)} \frac{1}{\sqrt{-a^4 + a - C1}} d_{-a - x - C2} = 0, \int^{y(x)} -\frac{1}{\sqrt{-a^4 + a - C1}} d_{-a - x - C2} = 0 \right\}$$

### 7.147 ODE No. 1737

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 + b - 4(x^2 + a)(y(x))^2 - 8x(y(x))^3 - 3(y(x))^4 = 0$$

**Mathematica:** cpu = 1.182650 (sec), leaf count = 48

$$\text{DSolve}[-4(a + x^2)y(x)^2 + b + 2y(x)y''(x) - y'(x)^2 - 3y(x)^4 - 8xy(x)^3 = 0, y(x), x]$$

**Maple:** cpu = 1.779 (sec), leaf count = 0

could not solve

### 7.148 ODE No. 1738

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 + 3f(x)y(x) \frac{d}{dx} y(x) + 2 \left( (f(x))^2 + \frac{d}{dx} f(x) \right) (y(x))^2 - 8(y(x))^3 = 0$$

**Mathematica:** cpu = 0.550070 (sec), leaf count = 54

$$\text{DSolve}[2y(x)^2 (f'(x) + f(x)^2) + 3f(x)y(x)y'(x) + 2y(x)y''(x) - y'(x)^2 - 8y(x)^3 = 0, y(x), x]$$

**Maple:** cpu = 1.217 (sec), leaf count = 0

could not solve

### 7.149 ODE No. 1739

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 + 4(y(x))^2 \frac{d}{dx} y(x) + 1 + f(x)(y(x))^2 + (y(x))^4 = 0$$

**Mathematica:** cpu = 0.050506 (sec), leaf count = 45

$$\text{DSolve}[f(x)y(x)^2 + 2y(x)y''(x) + 4y(x)^2y'(x) - y'(x)^2 + y(x)^4 + 1 = 0, y(x), x]$$

**Maple:** cpu = 0.265 (sec), leaf count = 0

could not solve

**7.150 ODE No. 1740**

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - 3 \left( \frac{d}{dx} y(x) \right)^2 = 0$$

**Mathematica:** cpu = 0.026503 (sec), leaf count = 16

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2}{(2c_1 + x)^2} \right\} \right\}$$

**Maple:** cpu = 1.513 (sec), leaf count = 13

$$\{y(x) = 4(-C1 x + -C2)^{-2}\}$$

**7.151 ODE No. 1741**

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - 3 \left( \frac{d}{dx} y(x) \right)^2 - 4 (y(x))^2 = 0$$

**Mathematica:** cpu = 0.092012 (sec), leaf count = 17

$$\{ \{ y(x) \rightarrow c_2 \sec^2(2c_1 + x) \} \}$$

**Maple:** cpu = 1.638 (sec), leaf count = 37

$$\{y(x) = 4(-C1^2(\sin(x))^2 - C2^2(\sin(x))^2 - 2-C1-C2 \sin(x) \cos(x) + -C2^2)^{-1}\}$$

**7.152 ODE No. 1742**

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - 3 \left( \frac{d}{dx} y(x) \right)^2 + f(x) (y(x))^2 = 0$$

**Mathematica:** cpu = 11.134414 (sec), leaf count = 30

$$\text{DSolve}[f(x)y(x)^2 + 2y(x)y''(x) - 3y'(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 0.140 (sec), leaf count = 60

$$\left\{ y(x) = \text{ODESolStruc} \left( e^{f(-b(-a))d_{-a} + -C1}, \left[ \left\{ \frac{d}{d_{-a}} b(-a) = \frac{(-b(-a))^2}{2} - \frac{f(-a)}{2} \right\}, \left\{ -a = x, -b(-a) = \right. \right. \right. \right.$$

**7.153 ODE No. 1743**

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - 6 \left( \frac{d}{dx} y(x) \right)^2 + (1 + a(y(x))^3) (y(x))^2 = 0$$

**Mathematica:** cpu = 18.186309 (sec), leaf count = 2761

$$\left\{ \text{Solve} \left[ \frac{4 \left( F \left( \sin^{-1} \left( \sqrt{\frac{(\text{Root}[4c_1 \#1^4 + 4a \#1^3 + 1 \&, 2] - \text{Root}[4c_1 \#1^4 + 4a \#1^3 + 1 \&, 4]) (y(x) - \text{Root}[4c_1 \#1^4 + 4a \#1^3 + 1 \&, 1])}{(\text{Root}[4c_1 \#1^4 + 4a \#1^3 + 1 \&, 1] - \text{Root}[4c_1 \#1^4 + 4a \#1^3 + 1 \&, 4]) (y(x) - \text{Root}[4c_1 \#1^4 + 4a \#1^3 + 1 \&, 2])} \right)} \right)} \right]} \right]$$

**Maple:** cpu = 1.638 (sec), leaf count = 71

$$\left\{ \int^{y(x)} -2 \frac{1}{\sqrt{4 \_C1 \_a^4 + 4 a \_a^3 + 1 \_a}} d\_a - x - \_C2 = 0, \int^{y(x)} 2 \frac{1}{\sqrt{4 \_C1 \_a^4 + 4 a \_a^3 + 1 \_a}} d\_a \right.$$

**7.154 ODE No. 1744**

$$2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 \left( \left( \frac{d}{dx} y(x) \right)^2 + 1 \right) = 0$$

**Mathematica:** cpu = 0.974624 (sec), leaf count = 173

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -ie^{-c_1} \left( \sqrt{\#1} \sqrt{\#1 e^{2c_1} - 1} - e^{-c_1} \log \left( \sqrt{\#1} e^{2c_1} + e^{c_1} \sqrt{\#1 e^{2c_1} - 1} \right) \right) \& \right] [c_2 \right.$$

**Maple:** cpu = 1.670 (sec), leaf count = 95

$$\left\{ -\frac{C1}{2} \arctan \left( 1 \left( y(x) - \frac{C1}{2} \right) \frac{1}{\sqrt{-C1 y(x) - (y(x))^2}} \right) - \sqrt{-C1 y(x) - (y(x))^2} - x - C2 = 0, \right.$$

**7.155 ODE No. 1745**

$$2(y(x) - a) \frac{d^2}{dx^2} y(x) + \left( \frac{d}{dx} y(x) \right)^2 + 1 = 0$$

**Mathematica:** cpu = 0.294537 (sec), leaf count = 204

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\sqrt{2} \left( \frac{1}{2} \sqrt{a - \#1} \sqrt{e^{2c_1} - 2(a - \#1)} - \frac{e^{2c_1} \tan^{-1} \left( \frac{\sqrt{2} \sqrt{a - \#1}}{\sqrt{e^{2c_1} - 2(a - \#1)}} \right)}{2\sqrt{2}} \right) \right] [c_2 \right.$$

**Maple:** cpu = 1.763 (sec), leaf count = 293

$$\left\{ -\sqrt{-(y(x))^2 + (2a - C1)y(x) - a(-C1 + a)} + \arctan\left(1\left(y(x) - a - \frac{C1}{2}\right)\frac{1}{\sqrt{-(y(x))^2 + (2a - C1)y(x) - a(-C1 + a)}}\right) \right.$$

**7.156 ODE No. 1746**

$$3\left(\frac{d^2}{dx^2}y(x)\right)y(x) - 2\left(\frac{d}{dx}y(x)\right)^2 - ax^2 - bx - c = 0$$

**Mathematica:** cpu = 0.040505 (sec), leaf count = 36

$$\text{DSolve}[-ax^2 - bx - c + 3y(x)y''(x) - 2y'(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 1.903 (sec), leaf count = 207

$$\left\{ y(x) = \text{RootOf}\left(-2\arctan\left(\frac{2ax + b}{\sqrt{4ac - b^2}}\right)b - 2\int^{-z} \frac{b}{\sqrt{4f^{4/3} - C1b^2 - 36cf^2a + 9b^2f^2 - 2}} d_f\sqrt{\dots}\right) \right.$$

**7.157 ODE No. 1747**

$$3\left(\frac{d^2}{dx^2}y(x)\right)y(x) - 5\left(\frac{d}{dx}y(x)\right)^2 = 0$$

**Mathematica:** cpu = 0.027504 (sec), leaf count = 20

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2}{(3c_1 + 2x)^{3/2}} \right\} \right\}$$

**Maple:** cpu = 1.576 (sec), leaf count = 17

$$\left\{ -\frac{3}{2}(y(x))^{-\frac{2}{3}} - C1x - C2 = 0 \right\}$$

**7.158 ODE No. 1748**

$$4 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - 3 \left( \frac{d}{dx} y(x) \right)^2 + 4 y(x) = 0$$

**Mathematica:** cpu = 0.093512 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow \frac{(c_1^2 x^2 + 2c_2 c_1^2 x + c_2^2 c_1^2 - 64)^2}{256 c_1^2} \right\} \right\}$$

**Maple:** cpu = 1.654 (sec), leaf count = 67

$$\left\{ -4 \frac{\sqrt{-C1 (y(x))^{3/2} + 4 y(x)}}{\sqrt{y(x)}_C1} - x - _C2 = 0, 4 \frac{\sqrt{-C1 (y(x))^{3/2} + 4 y(x)}}{\sqrt{y(x)}_C1} - x - _C2 = 0, y(x) = 0 \right\}$$

**7.159 ODE No. 1749**

$$4 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - 3 \left( \frac{d}{dx} y(x) \right)^2 - 12 (y(x))^3 = 0$$

**Mathematica:** cpu = 0.547069 (sec), leaf count = 181

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\frac{4 \sqrt{\frac{4 \#1^{3/2}}{c_1} + 1} \sqrt{\#1^{3/2} c_1 + 4 \#1^3} {}_2F_1 \left( \frac{1}{6}, \frac{1}{2}, \frac{7}{6}; -\frac{4 \#1^{3/2}}{c_1} \right)}{4 \#1^2 + \sqrt{\#1} c_1} \right] \& [c_2 + x] \right\}, \left\{ y(x) \right\} \right\}$$

**Maple:** cpu = 1.684 (sec), leaf count = 57

$$\left\{ \int^{y(x)} \frac{1}{\sqrt{-C1 _a^{\frac{3}{2}} + 4 _a^3}} d_a - x - _C2 = 0, \int^{y(x)} -\frac{1}{\sqrt{-C1 _a^{\frac{3}{2}} + 4 _a^3}} d_a - x - _C2 = 0 \right\}$$

**7.160 ODE No. 1750**

$$4 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - 3 \left( \frac{d}{dx} y(x) \right)^2 + a(y(x))^3 + b(y(x))^2 + cy(x) = 0$$

**Mathematica:** cpu = 3.890994 (sec), leaf count = 2281

$$\left\{ \text{Solve} \left[ \frac{4F \left( \sin^{-1} \left( \sqrt{\frac{(\text{Root}[a \#1^4 + 3b \#1^2 - 3c_1 \#1 - 3c \&, 2] - \text{Root}[a \#1^4 + 3b \#1^2 - 3c_1 \#1 - 3c \&, 4]) (\sqrt{y(x)} - \text{Root}[a \#1^4 + 3b \#1^2 - 3c_1 \#1 - 3c \&, 1])}{(\text{Root}[a \#1^4 + 3b \#1^2 - 3c_1 \#1 - 3c \&, 1] - \text{Root}[a \#1^4 + 3b \#1^2 - 3c_1 \#1 - 3c \&, 4]) (\sqrt{y(x)} - \text{Root}[a \#1^4 + 3b \#1^2 - 3c_1 \#1 - 3c \&, 1])} \right)} \right)} \right]$$

**Maple:** cpu = 1.716 (sec), leaf count = 87

$$\left\{ \int^{y(x)} -3 \frac{1}{\sqrt{9 - C1 - a^{3/2} - 3a - a^3 - 9b - a^2 + 9c - a}} da - x - C2 = 0, \int^{y(x)} 3 \frac{1}{\sqrt{9 - C1 - a^{3/2} - 3a - a^3 - 9b - a^2 + 9c - a}} da - x - C2 = 0 \right.$$

### 7.161 ODE No. 1751

$$4 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - 3 \left( \frac{d}{dx} y(x) \right)^2 + \left( 6 (y(x))^2 - 2 \frac{\left( \frac{d}{dx} f(x) \right) y(x)}{f(x)} \right) \frac{d}{dx} y(x) + (y(x))^4 - 2 (y(x))^2 \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.742594 (sec), leaf count = 73

$$\text{DSolve} \left[ y'(x) \left( 6y(x)^2 - \frac{2y(x)f'(x)}{f(x)} \right) + f(x)y(x) + g(x)y(x)^2 + 4y(x)y''(x) - 2y(x)^2y'(x) - 3y'(x)^2 + y(x)^4 - 2y(x)^2 \frac{d}{dx} y(x) = 0 \right]$$

**Maple:** cpu = 0.483 (sec), leaf count = 0

could not solve

### 7.162 ODE No. 1752

$$4 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - 5 \left( \frac{d}{dx} y(x) \right)^2 + a(y(x))^2 = 0$$

**Mathematica:** cpu = 0.129016 (sec), leaf count = 26

$$\left\{ \left\{ y(x) \rightarrow c_2 \operatorname{sech}^4 \left( \frac{1}{4} \sqrt{a} (x - 4c_1) \right) \right\} \right\}$$

**Maple:** cpu = 1.575 (sec), leaf count = 33

$$\left\{ y(x) = 16 \frac{(e^{1/4 \sqrt{ax}})^4 a^2}{(e^{1/2 \sqrt{ax}} - C1 - C2)^4} \right\}$$



**7.163 ODE No. 1753**

$$12 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - 15 \left( \frac{d}{dx} y(x) \right)^2 + 8 (y(x))^3 = 0$$

**Mathematica:** cpu = 0.321041 (sec), leaf count = 43

$$\left\{ \left\{ y(x) \rightarrow \frac{2304c_1^2}{(3c_1^2x^2 + 6c_2c_1^2x + 3c_2^2c_1^2 + 128)^2} \right\} \right\}$$

**Maple:** cpu = 1.575 (sec), leaf count = 147

$$\left\{ -12 \frac{y(x) \left( 8 \sqrt{y(x)} - \_C1 \right) \sqrt{8y(x) - \_C1} \sqrt{y(x)}}{\sqrt{-24 (y(x))^3 + 3 \_C1 (y(x))^{5/2} - \_C1} \sqrt{\sqrt{y(x)} \left( 8 \sqrt{y(x)} - \_C1 \right)}} - x - \_C2 = 0, 12 \frac{\dots}{\sqrt{-24 (y(x))^3 + 3 \_C1 (y(x))^{5/2} - \_C1} \sqrt{\sqrt{y(x)} \left( 8 \sqrt{y(x)} - \_C1 \right)}} - x - \_C2 = 0 \right\}$$

**7.164 ODE No. 1754**

$$ny(x) \frac{d^2}{dx^2} y(x) - (n-1) \left( \frac{d}{dx} y(x) \right)^2 = 0$$

**Mathematica:** cpu = 0.033504 (sec), leaf count = 17

$$\{ \{ y(x) \rightarrow c_2(x - c_1n)^n \} \}$$

**Maple:** cpu = 1.544 (sec), leaf count = 15

$$\left\{ y(x) = \left( \frac{-C1 x + -C2}{n} \right)^n \right\}$$

**7.165 ODE No. 1755**

$$ay(x) \frac{d^2}{dx^2} y(x) + b \left( \frac{d}{dx} y(x) \right)^2 + c_4 (y(x))^4 + c_3 (y(x))^3 + c_2 (y(x))^2 + c_1 y(x) + c_0 = 0$$

**Mathematica:** cpu = 104.001206 (sec), leaf count = 46

**DSolve**[ $ay(x)y''(x) + by'(x)^2 + c_0 + c_1y(x) + c_2y(x)^2 + c_3y(x)^3 + c_4y(x)^4 = 0, y(x), x$ ]

**Maple:** cpu = 1.810 (sec), leaf count = 1028

$$\left\{ \int^{y(x)} b(6a^4 + 25a^3b + 35a^2b^2 + 20ab^3 + 4b^4) - a^2 \frac{b}{a} \sqrt{-a^2 \frac{b}{a} b(6a^4 + 25a^3b + 35a^2b^2 + 20ab^3 + 4b^4)} \right\}$$

**7.166 ODE No. 1756**

$$ay(x) \frac{d^2}{dx^2}y(x) + b \left( \frac{d}{dx}y(x) \right)^2 - \frac{y(x) \frac{d}{dx}y(x)}{\sqrt{c^2 + x^2}} = 0$$

**Mathematica:** cpu = 0.662084 (sec), leaf count = 126

$$\left\{ \left\{ y(x) \rightarrow c_2 \left( -a^2 \left( x \left( \sqrt{c^2 + x^2} + x \right)^{\frac{1}{a}} + c_1 \right) + a \left( \sqrt{c^2 + x^2} + x \right)^{\frac{1}{a}} \left( \sqrt{c^2 + x^2} - bx \right) + b \sqrt{c^2 + x^2} \left( \sqrt{c^2 + x^2} \right) \right) \right\} \right\}$$

**Maple:** cpu = 3.074 (sec), leaf count = 79

$$\left\{ y(x) = \left( \left( \frac{a}{a+b} \left( -C1 \sqrt[2]{x^{a-1+1}} {}_2F_1 \left( -\frac{1}{2a}, -\frac{1}{2a} - \frac{1}{2}; 1 - a^{-1}; -\frac{c^2}{x^2} \right) (-a^{-1} - 1)^{-1} + C2 \right)^{-1} \right)^{\frac{a}{a+b}} \right)$$

**7.167 ODE No. 1757**

$$ay(x) \frac{d^2}{dx^2}y(x) - (a-1) \left( \frac{d}{dx}y(x) \right)^2 + (a+2) f(x) (y(x))^2 \frac{d}{dx}y(x) + (f(x))^2 (y(x))^4 + a \left( \frac{d}{dx}f(x) \right) (y(x))$$

**Mathematica:** cpu = 0.827105 (sec), leaf count = 59

$$\text{DSolve}[(a+2)f(x)y(x)^2y'(x) + ay(x)y''(x) + ay(x)^3y'(x) - (a-1)y'(x)^2 + f(x)^2y(x)^4 = 0, y(x), x]$$

**Maple:** cpu = 1.123 (sec), leaf count = 0

could not solve

**7.168 ODE No. 1758**

$$(ay(x) + b) \frac{d^2}{dx^2}y(x) + c \left( \frac{d}{dx}y(x) \right)^2 = 0$$

**Mathematica:** cpu = 0.062008 (sec), leaf count = 36

$$\left\{ \left\{ y(x) \rightarrow \frac{(c_1(-a+c))(-c_2-x)^{\frac{a}{a+c}} - b}{a} \right\} \right\}$$

**Maple:** cpu = 1.529 (sec), leaf count = 88

$$\left\{ y(x) = -\frac{1}{a} \left( -C1 ax - C1 xc + b \left( \left( \frac{1}{(a+c)(-C1 x - C2)} \right)^{\frac{c}{a}(1+\frac{c}{a})^{-1}} - C2 a - C2 c \right) \right)$$

**7.169 ODE No. 1759**

$$xy(x) \frac{d^2}{dx^2}y(x) + x \left( \frac{d}{dx}y(x) \right)^2 - y(x) \frac{d}{dx}y(x) = 0$$

**Mathematica:** cpu = 0.036505 (sec), leaf count = 18

$$\left\{ \left\{ y(x) \rightarrow c_2 \sqrt{c_1 + x^2} \right\} \right\}$$

**Maple:** cpu = 1.498 (sec), leaf count = 31

$$\left\{ y(x) = \sqrt{-C1 x^2 + 2\_C2}, y(x) = -\sqrt{-C1 x^2 + 2\_C2} \right\}$$

**7.170 ODE No. 1760**

$$xy(x) \frac{d^2}{dx^2}y(x) + x \left( \frac{d}{dx}y(x) \right)^2 + ay(x) \frac{d}{dx}y(x) + f(x) = 0$$

**Mathematica:** cpu = 11.966520 (sec), leaf count = 104

$$\left\{ \left\{ y(x) \rightarrow -\sqrt{2} \sqrt{\int_1^x K[2]^{-a} \left( - \left( \int_1^{K[2]} K[1]^{a-1} f(K[1]) dK[1] + c_1 \right) \right) dK[2] + c_2} \right\}, \left\{ y(x) \rightarrow \sqrt{2} \sqrt{\int_1^x K[2]^{-a} \left( - \left( \int_1^{K[2]} K[1]^{a-1} f(K[1]) dK[1] + c_1 \right) \right) dK[2] + c_2} \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 114

$$\left\{ y(x) = \frac{\sqrt{2}}{a-1} \sqrt{(a-1) \left( x^{1-a} \int \frac{x^a f(x)}{x} dx + x^{1-a} \_C1 - \int f(x) dx - \_C2 \right)}, y(x) = -\frac{\sqrt{2}}{a-1} \sqrt{(a-1) \left( x^{1-a} \int \frac{x^a f(x)}{x} dx + x^{1-a} \_C1 - \int f(x) dx - \_C2 \right)} \right\}$$

**7.171 ODE No. 1761**

$$xy(x) \frac{d^2}{dx^2}y(x) - x \left( \frac{d}{dx}y(x) \right)^2 + y(x) \frac{d}{dx}y(x) + x(d + a(y(x))^4) + y(x) (c + b(y(x))^2) = 0$$

**Mathematica:** cpu = 1.733720 (sec), leaf count = 52

`DSolve[x(ay(x)^4 + d) + y(x) (by(x)^2 + c) + xy(x)y''(x) - xy'(x)^2 + y(x)y'(x) = 0, y(x), x]`

**Maple:** cpu = 2.184 (sec), leaf count = 0

could not solve

**7.172 ODE No. 1762**

$$xy(x) \frac{d^2}{dx^2}y(x) - x \left( \frac{d}{dx}y(x) \right)^2 + ay(x) \frac{d}{dx}y(x) + bx(y(x))^3 = 0$$

**Mathematica:** cpu = 52.685690 (sec), leaf count = 39

$$\text{DSolve}[ay(x)y'(x) + bxy(x)^3 + xy(x)y''(x) - xy'(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 2.215 (sec), leaf count = 106

$$\left\{ y(x) = \text{ODESolStruc} \left( \frac{-a}{(e^{f_{-b(-a)d_{-a}+_{-C1}}})^2}, \left[ \left\{ \frac{d}{d_{-a}} b_{(-a)} = -a(b_{-a} - 2a + 2)(-b_{(-a)})^3 + (a - 1) \right\} \right] \right) \right\}$$

**7.173 ODE No. 1763**

$$xy(x) \frac{d^2}{dx^2}y(x) + 2x \left( \frac{d}{dx}y(x) \right)^2 + ay(x) \frac{d}{dx}y(x) = 0$$

**Mathematica:** cpu = 0.139018 (sec), leaf count = 35

$$\left\{ \left\{ y(x) \rightarrow c_2 \exp \left( \frac{1}{3} (\log(3x - (a - 1)c_1x^a) - a \log(x)) \right) \right\} \right\}$$

**Maple:** cpu = 1.560 (sec), leaf count = 234

$$\left\{ y(x) = \frac{1}{(a - 1)x^a} \sqrt[3]{(3_{-C2}x^aa - 3_{-C2}x^a - 3_{-C1}x)(a - 1)^2(x^a)^2}, y(x) = -\frac{1}{(-2 + 2a)x^a} \sqrt[3]{(3_{-C2}x^aa - 3_{-C2}x^a - 3_{-C1}x)(a - 1)^2(x^a)^2} \right\}$$

**7.174 ODE No. 1764**

$$xy(x) \frac{d^2}{dx^2}y(x) - 2x \left( \frac{d}{dx}y(x) \right)^2 + (1 + y(x)) \frac{d}{dx}y(x) = 0$$

**Mathematica:** cpu = 0.064508 (sec), leaf count = 52

$$\left\{ \left\{ y(x) \rightarrow \frac{\tan \left( \frac{1}{2} (\sqrt{2}\sqrt{c_1} \log(x) - \sqrt{2}\sqrt{c_1}c_2) \right)}{\sqrt{2}\sqrt{c_1}} \right\} \right\}$$

**Maple:** cpu = 1.638 (sec), leaf count = 18

$$\left\{ y(x) = -C1 \tanh \left( \frac{\ln(x) - C2}{2_{-C1}} \right) \right\}$$

**7.175 ODE No. 1765**

$$xy(x) \frac{d^2}{dx^2}y(x) - 2x \left( \frac{d}{dx}y(x) \right)^2 + ay(x) \frac{d}{dx}y(x) = 0$$

**Mathematica:** cpu = 0.127516 (sec), leaf count = 24

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 x^a}{(a-1)c_1 x^a + x} \right\} \right\}$$

**Maple:** cpu = 1.513 (sec), leaf count = 31

$$\left\{ y(x) = -\frac{(a-1)x^a}{-C2 x^a a - C2 x^a - C1 x} \right\}$$

**7.176 ODE No. 1766**

$$xy(x) \frac{d^2}{dx^2}y(x) - 4x \left( \frac{d}{dx}y(x) \right)^2 + 4y(x) \frac{d}{dx}y(x) = 0$$

**Mathematica:** cpu = 0.046506 (sec), leaf count = 21

$$\left\{ \left\{ y(x) \rightarrow \frac{c_2 x}{\sqrt[3]{c_1 x^3 + 1}} \right\} \right\}$$

**Maple:** cpu = 1.529 (sec), leaf count = 84

$$\left\{ y(x) = \left( -\frac{1}{2} \frac{1}{\sqrt[3]{-3 C2 x^3 + C1}} - \frac{i}{2} \sqrt{3} \frac{1}{\sqrt[3]{-3 C2 x^3 + C1}} \right) x, y(x) = \left( -\frac{1}{2} \frac{1}{\sqrt[3]{-3 C2 x^3 + C1}} + \frac{i}{2} \sqrt{3} \frac{1}{\sqrt[3]{-3 C2 x^3 + C1}} \right) x \right\}$$

**7.177 ODE No. 1767**

$$xy(x) \frac{d^2}{dx^2}y(x) + \left( \frac{ax}{\sqrt{b^2 - x^2}} - x \right) \left( \frac{d}{dx}y(x) \right)^2 - y(x) \frac{d}{dx}y(x) = 0$$

**Mathematica:** cpu = 0.075510 (sec), leaf count = 55

$$\left\{ \left\{ y(x) \rightarrow c_2 \exp \left( \frac{c_1 \log(a\sqrt{b^2 - x^2} - c_1)}{a^2} + \frac{\sqrt{b^2 - x^2}}{a} \right) \right\} \right\}$$

**Maple:** cpu = 3.182 (sec), leaf count = 50

$$\left\{ y(x) = -C2 e^{\int -x\sqrt{b^2-x^2}(ab^2-ax^2+C1\sqrt{b^2-x^2})^{-1} dx} \right\}$$

**7.178 ODE No. 1768**

$$x(y(x) + x) \frac{d^2}{dx^2}y(x) + x \left( \frac{d}{dx}y(x) \right)^2 + (x - y(x)) \frac{d}{dx}y(x) - y(x) = 0$$

**Mathematica:** cpu = 0.113014 (sec), leaf count = 87

$$\left\{ \left\{ y(x) \rightarrow -x - \sqrt{-e^{2c_2}x^2 - 2ic_1x^2 + e^{2c_2} + x^2} \right\}, \left\{ y(x) \rightarrow -x + \sqrt{-e^{2c_2}x^2 - 2ic_1x^2 + e^{2c_2} + x^2} \right\} \right\}$$

**Maple:** cpu = 1.544 (sec), leaf count = 43

$$\left\{ y(x) = -x - \sqrt{-C2 x^2 + x^2 + C1}, y(x) = -x + \sqrt{-C2 x^2 + x^2 + C1} \right\}$$

**7.179 ODE No. 1769**

$$2xy(x) \frac{d^2}{dx^2}y(x) - x \left( \frac{d}{dx}y(x) \right)^2 + y(x) \frac{d}{dx}y(x) = 0$$

**Mathematica:** cpu = 0.045506 (sec), leaf count = 18

$$\left\{ \left\{ y(x) \rightarrow c_2(c_1 + \sqrt{x})^2 \right\} \right\}$$

**Maple:** cpu = 1.575 (sec), leaf count = 21

$$\left\{ y(x) = C1 \sqrt{x} C2 + C1^2 x + \frac{C2^2}{4} \right\}$$

**7.180 ODE No. 1770**

$$x^2(-1 + y(x)) \frac{d^2}{dx^2}y(x) - 2x^2 \left( \frac{d}{dx}y(x) \right)^2 - 2x(-1 + y(x)) \frac{d}{dx}y(x) - 2y(x)(-1 + y(x))^2 = 0$$

**Mathematica:** cpu = 0.792101 (sec), leaf count = 28

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{x^2 \left( -\frac{c_1}{x} + c_2 - \frac{1}{x^2} \right)} + 1 \right\} \right\}$$

**Maple:** cpu = 1.560 (sec), leaf count = 26

$$\left\{ y(x) = \frac{x(C1 x - C2)}{C1 x^2 - C2 x - 1} \right\}$$

**7.181 ODE No. 1771**

$$x^2(y(x) + x) \frac{d^2}{dx^2}y(x) - \left(x \frac{d}{dx}y(x) - y(x)\right)^2 = 0$$

**Mathematica:** cpu = 0.082010 (sec), leaf count = 21

$$\left\{ \left\{ y(x) \rightarrow c_2 x e^{\frac{c_1}{x}} - x \right\} \right\}$$

**Maple:** cpu = 1.685 (sec), leaf count = 21

$$\left\{ y(x) = \frac{x e^{-1}}{-C1} e^{-\frac{C2}{x}} - x \right\}$$

**7.182 ODE No. 1772**

$$x^2(x - y(x)) \frac{d^2}{dx^2}y(x) + a \left(x \frac{d}{dx}y(x) - y(x)\right)^2 = 0$$

**Mathematica:** cpu = 0.866110 (sec), leaf count = 37

$$\left\{ \left\{ y(x) \rightarrow x \left( \left( (a-1) \left( \frac{(-1)^{a+1} c_1}{x} - c_2 \right) \right)^{\frac{1}{1-a}} + 1 \right) \right\} \right\}$$

**Maple:** cpu = 1.670 (sec), leaf count = 47

$$\{ -C1 + (ax - x) -C2 - x^a y(x) (x - y(x))^{-a} + x^{a+1} (x - y(x))^{-a} = 0 \}$$

**7.183 ODE No. 1773**

$$2x^2 y(x) \frac{d^2}{dx^2}y(x) - x^2 \left( \left( \frac{d}{dx}y(x) \right)^2 + 1 \right) + (y(x))^2 = 0$$

**Mathematica:** cpu = 0.189524 (sec), leaf count = 44

$$\left\{ \left\{ y(x) \rightarrow \frac{x(c_1^2 \log^2(x) - 2c_2 c_1^2 \log(x) + c_2^2 c_1^2 + 4)}{4c_1} \right\} \right\}$$

**Maple:** cpu = 1.638 (sec), leaf count = 28

$$\left\{ y(x) = \frac{(-C1^2 + 1)x}{4-C2} + -C1 x \ln(x) + -C2 x (\ln(x))^2 \right\}$$

**7.184 ODE No. 1774**

$$ax^2y(x) \frac{d^2}{dx^2}y(x) + bx^2 \left( \frac{d}{dx}y(x) \right)^2 + cxy(x) \frac{d}{dx}y(x) + d(y(x))^2 = 0$$

**Mathematica:** cpu = 1.339670 (sec), leaf count = 93

$$\left\{ \left\{ y(x) \rightarrow c_2 \exp \left( - \frac{\log(x) \left( a \sqrt{\frac{a^2 - 2ac - 4ad - 4bd + c^2}{a^2}} - a + c \right) - 2a \log \left( x \sqrt{\frac{a^2 - 2ac - 4ad - 4bd + c^2}{a^2}} + c_1 \right)}{2(a + b)} \right) \right\} \right\}$$

**Maple:** cpu = 1.653 (sec), leaf count = 155

$$\left\{ y(x) = x^{-\frac{1}{2a+2b} \sqrt{a^2 - 2ac - 4ad - 4bd + c^2}} x^{\frac{a}{2a+2b}} x^{-\frac{c}{2a+2b}} \left( (a^2 - 2ac - 4ad - 4bd + c^2) \left( x^{\frac{1}{a} \sqrt{a^2 - 2ac - 4ad - 4bd + c^2}} \right) \right) \right\}$$

**7.185 ODE No. 1775**

$$x(1+x)^2 y(x) \frac{d^2}{dx^2}y(x) - x(1+x)^2 \left( \frac{d}{dx}y(x) \right)^2 + 2(1+x)^2 y(x) \frac{d}{dx}y(x) - a(x+2)(y(x))^2 = 0$$

**Mathematica:** cpu = 0.135017 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow c_2 e^{\frac{-a-c_1}{x} + a \log(x+1)} \right\} \right\}$$

**Maple:** cpu = 1.544 (sec), leaf count = 31

$$\left\{ y(x) = \frac{(1+x)^a}{-C1 e^a} e^{-\frac{C2}{x}} (e^{\frac{a}{x}})^{-1} \right\}$$

**7.186 ODE No. 1776**

$$8(-x^3+1)y(x) \frac{d^2}{dx^2}y(x) - 4(-x^3+1) \left( \frac{d}{dx}y(x) \right)^2 - 12x^2y(x) \frac{d}{dx}y(x) + 3x(y(x))^2 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 1.825 (sec), leaf count = 88

$$\left\{ y(x) = \frac{-C2^2 x}{4 - C1} \left( LegendreP \left( -\frac{1}{6}, \frac{1}{3}, \sqrt{-(x-1)(x^2+x+1)} \right) \right)^2 + -C1 \left( LegendreQ \left( -\frac{1}{6}, \frac{1}{3}, \sqrt{-(x-1)(x^2+x+1)} \right) \right)^2 \right\}$$



**7.187 ODE No. 1777**

$$f_0(x)y(x)\frac{d^2}{dx^2}y(x) + f_1(x)\left(\frac{d}{dx}y(x)\right)^2 + f_2(x)y(x)\frac{d}{dx}y(x) + f_3(x)(y(x))^2 = 0$$

**Mathematica:** cpu = 49.431277 (sec), leaf count = 41

$$\text{DSolve}[f_0(x)y(x)y''(x) + f_1(x)y'(x)^2 + f_2(x)y(x)y'(x) + f_3(x)y(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 0.530 (sec), leaf count = 83

$$\left\{ y(x) = \text{ODESolStruc}\left(e^{\int -b(-a)dx - C_1}, \left[\frac{d}{dx} - b(-a) = -\frac{(f_1(-a) + f_0(-a))(-b(-a))^2}{f_0(-a)} - \frac{f_2(-a)}{f_0(-a)}\right]\right)\right.$$

**7.188 ODE No. 1778**

$$(y(x))^2 \frac{d^2}{dx^2}y(x) - a = 0$$

**Mathematica:** cpu = 0.537568 (sec), leaf count = 75

$$\text{Solve}\left[\left(\frac{y(x)\sqrt{c_1 - \frac{2a}{y(x)}}}{c_1} + \frac{a \log\left(\sqrt{c_1}y(x)\sqrt{c_1 - \frac{2a}{y(x)}} - a + c_1y(x)\right)}{c_1^{3/2}}\right)^2 = (c_2 + x)^2, y(x)\right]$$

**Maple:** cpu = 1.950 (sec), leaf count = 369

$$\left\{ y(x) = \frac{-C_1\left(-C_1^2a^2 + 2-C_1ae^{\text{RootOf}(csgn(-C_1^{-1})-C_1^4a^2-2-Z-C_1^3ae^{-Z}-csgn(-C_1^{-1})(e^{-Z})^2-C_1^2-2csgn(-C_1^{-1})}\right)}}{2e^{\text{RootOf}(csgn(-C_1^{-1})-C_1^4a^2-2-Z-C_1^3ae^{-Z}-csgn(-C_1^{-1})(e^{-Z})^2-C_1^2-2csgn(-C_1^{-1})}}}\right.$$

**7.189 ODE No. 1779**

$$(y(x))^2 \frac{d^2}{dx^2}y(x) + y(x)\left(\frac{d}{dx}y(x)\right)^2 + ax = 0$$

**Mathematica:** cpu = 3.996008 (sec), leaf count = 28

$$\text{DSolve}[ax + y(x)^2y''(x) + y(x)y'(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 1.872 (sec), leaf count = 130

$$\left\{ \ln(x) - \int \frac{y(x)}{x} \frac{1}{2\sqrt{3}g^3 + 2\sqrt{3}a} \left(3-g^2\sqrt[3]{\frac{a}{-g^3}} \tan\left(\text{RootOf}\left(-2-Z\sqrt{3} + \ln\left(\frac{(\tan(-Z))^2 + (3+2\sqrt{3}\tan(-Z)) + (\tan(-Z))^2}{3+2\sqrt{3}\tan(-Z)}\right)\right)\right)\right.\right.$$

**7.190 ODE No. 1780**

$$(y(x))^2 \frac{d^2}{dx^2} y(x) + y(x) \left( \frac{d}{dx} y(x) \right)^2 - ax - b = 0$$

**Mathematica:** cpu = 0.488562 (sec), leaf count = 32

$$\text{DSolve}[-ax - b + y(x)^2 y''(x) + y(x) y'(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 2.012 (sec), leaf count = 172

$$\left\{ \frac{b \ln(ax + b)}{a} - \int^{\frac{y(x)}{ax+b}} \frac{1}{2\sqrt{3} \sqrt{-g^3 a^2 - 2\sqrt{3}}} \left( 3b^2 - g^2 \sqrt[3]{-\frac{a}{-g^3 b^3}} \tan \left( \text{RootOf} \left( 6b^2 \int \frac{-g^2}{-g^3 a^2 - 1} \left( -\frac{a}{-g^3 b^3} \right) \right) \right) \right. \right.$$

**7.191 ODE No. 1781**

$$((y(x))^2 + 1) \frac{d^2}{dx^2} y(x) + (1 - 2y(x)) \left( \frac{d}{dx} y(x) \right)^2 = 0$$

**Mathematica:** cpu = 0.085011 (sec), leaf count = 19

$$\{ \{ y(x) \rightarrow \tan(\log(-c_1(-c_2 - x))) \} \}$$

**Maple:** cpu = 1.528 (sec), leaf count = 11

$$\{ y(x) = \tan(\ln(_C1 x + _C2)) \}$$

**7.192 ODE No. 1782**

$$((y(x))^2 + 1) \frac{d^2}{dx^2} y(x) - 3y(x) \left( \frac{d}{dx} y(x) \right)^2 = 0$$

**Mathematica:** cpu = 0.088011 (sec), leaf count = 93

$$\left\{ \left\{ y(x) \rightarrow -\frac{ic_1(c_2 + x)}{\sqrt{c_1^2 x^2 + 2c_2 c_1^2 x + c_2^2 c_1^2 - 1}} \right\}, \left\{ y(x) \rightarrow \frac{ic_1(c_2 + x)}{\sqrt{c_1^2 x^2 + 2c_2 c_1^2 x + c_2^2 c_1^2 - 1}} \right\} \right\}$$

**Maple:** cpu = 1.638 (sec), leaf count = 56

$$\left\{ y(x) = _C1 x \sqrt{-( _C1^2 x^2 + 2 _C1 _C2 x + _C2^2 - 1)^{-1}} + _C2 \sqrt{-( _C1^2 x^2 + 2 _C1 _C2 x + _C2^2 - 1)^{-1}} \right\}$$

**7.193 ODE No. 1783**

$$(x + (y(x))^2) \frac{d^2}{dx^2} y(x) - 2(x - (y(x))^2) \left( \frac{d}{dx} y(x) \right)^3 + \left( \frac{d}{dx} y(x) \right) \left( 1 + 4y(x) \frac{d}{dx} y(x) \right) = 0$$

**Mathematica:** cpu = 1.423181 (sec), leaf count = 26

$$\text{Solve} \left[ x = c_2 e^{e^{-c_1} y(x)} - y(x)^2, y(x) \right]$$

**Maple:** cpu = 1.670 (sec), leaf count = 23

$$\left\{ \frac{-C1 y(x) + \ln(x + (y(x))^2) + C2 + 2}{y(x)} = 0 \right\}$$

**7.194 ODE No. 1784**

$$((y(x))^2 + x^2) \frac{d^2}{dx^2} y(x) - \left( \left( \frac{d}{dx} y(x) \right)^2 + 1 \right) \left( x \frac{d}{dx} y(x) - y(x) \right) = 0$$

**Mathematica:** cpu = 0.264034 (sec), leaf count = 74

$$\text{Solve} \left[ \frac{1}{2} \left( i \cot(c_1) \left( \log \left( 1 - \frac{iy(x)}{x} \right) - \log \left( 1 + \frac{iy(x)}{x} \right) \right) + \log \left( 1 - \frac{iy(x)}{x} \right) + \log \left( 1 + \frac{iy(x)}{x} \right) \right) = c_2 \right]$$

**Maple:** cpu = 2.324 (sec), leaf count = 52

$$\left\{ y(x) = \frac{x \left( i_{C1} + i - e^{\text{RootOf}(\ln(x)_{C1} + C2_{C1} + Z_{C1} - \ln((2i_{C1} + 2i - e^{-Z})x) - C2)} \right)}{-C1 + 1} \right\}$$

**7.195 ODE No. 1785**

$$((y(x))^2 + x^2) \frac{d^2}{dx^2} y(x) - 2 \left( \left( \frac{d}{dx} y(x) \right)^2 + 1 \right) \left( x \frac{d}{dx} y(x) - y(x) \right) = 0$$

**Mathematica:** cpu = 0.363546 (sec), leaf count = 95

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} \left( -\sqrt{4x(e^{c_2} - x) + e^{2c_2} \cot^2(c_1)} - e^{c_2} \cot(c_1) \right) \right\}, \left\{ y(x) \rightarrow \frac{1}{2} \left( \sqrt{4x(e^{c_2} - x) + e^{2c_2} \cot^2(c_1)} \right) \right\} \right\}$$

**Maple:** cpu = 1.810 (sec), leaf count = 83

$$\left\{ y(x) = \frac{1}{4_{C2}} \left( -C1 + 1 - \sqrt{8i_{C2}_{C1} x - 16_{C2}^2 x^2 + C1^2 - 8i_{C2} x + 2_{C1} + 1} \right), y(x) = \dots \right\}$$

**7.196 ODE No. 1786**

$$2y(x)(1-y(x))\frac{d^2}{dx^2}y(x) - (1-2y(x))\left(\frac{d}{dx}y(x)\right)^2 + y(x)(1-y(x))\left(\frac{d}{dx}y(x)\right)f(x) = 0$$

**Mathematica:** cpu = 1.028631 (sec), leaf count = 95

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4} \exp\left(-i \int_1^x c_1 \left(-e^{-\int_1^{K[3]} \frac{1}{2} f(K[1]) dK[1]}\right) dK[3] - ic_2\right) \left(1 + \exp\left(i \int_1^x c_1 \left(-e^{-\int_1^{K[3]} \frac{1}{2} f(K[1]) dK[1]}\right) dK[3] - ic_2\right)\right)^{-1} \right. \right.$$

**Maple:** cpu = 0.094 (sec), leaf count = 59

$$\left\{ y(x) = \frac{1}{8\_C2} \left( 4 \left( e^{-C1 \int e^{-1/2} \int f(x) dx dx} \right)^2 - C2^2 + 4 e^{-C1 \int e^{-1/2} \int f(x) dx dx} - C2 + 1 \right) \left( e^{-C1 \int e^{-\frac{f(x) dx}{2}} dx} \right)^{-1} \right.$$

**7.197 ODE No. 1787**

$$2y(x)(1-y(x))\frac{d^2}{dx^2}y(x) - (1-3y(x))\left(\frac{d}{dx}y(x)\right)^2 + h(y(x)) = 0$$

**Mathematica:** cpu = 36.216099 (sec), leaf count = 166

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \int_1^{\#1} \frac{1}{(K[2]-1)\sqrt{K[2]}\sqrt{2 \int_1^{K[2]} \frac{h(K[1])e^{-2(\log(1-K[1])+\frac{1}{2}\log(K[1])}{2(K[1]-1)K[1]} dK[1] + c_1}} dK[2]} \right. \right. \right.$$

**Maple:** cpu = 0.187 (sec), leaf count = 84

$$\left\{ \int^{y(x)} \frac{1}{-b-1} \frac{1}{\sqrt{\int \frac{h(-b)}{-b^2(-b-1)^3} d\_b\_b +\_C1\_b}} d\_b\_b - x -\_C2 = 0, \int^{y(x)} \frac{1}{-b-1} \frac{1}{\sqrt{\int \frac{h(-b)}{-b^2(-b-1)^3} d\_b\_b}} d\_b\_b \right.$$

**7.198 ODE No. 1788**

$$2y(x)(-1+y(x))\frac{d^2}{dx^2}y(x) - (3y(x)-1)\left(\frac{d}{dx}y(x)\right)^2 + 4y(x)\left(\frac{d}{dx}y(x)\right)(f(x)y(x)+g(x)) + 4(y(x))$$

**Mathematica:** cpu = 1.564699 (sec), leaf count = 85

$$\text{DSolve}[-4(1-y(x))y(x)^2(-f'(x)-f(x)^2-g'(x)+g(x)^2)+4y(x)y'(x)(f(x)y(x)+g(x))-2(1-y(x))$$

**Maple:** cpu = 0.219 (sec), leaf count = 113

$$\left\{ \sqrt{y(x)} - 2 \frac{\frac{\partial}{\partial x} \text{DESol}\left(\left\{-1/4 e^{-2 \int f(x) dx + 2 \int g(x) dx} - C1^2 - Y(x) - 2 g(x) \frac{d}{dx} - Y(x) + \frac{d^2}{dx^2} - Y(x)\right\}\right)}{\text{DESol}\left(\left\{-1/4 e^{-2 \int f(x) dx + 2 \int g(x) dx} - C1^2 - Y(x) - 2 g(x) \frac{d}{dx} - Y(x) + \frac{d^2}{dx^2} - Y(x)\right\}\right)}, \{-Y(x)\}$$

**7.199 ODE No. 1789**

$$-2 y(x) (1 - y(x)) \frac{d^2}{dx^2} y(x) + (1 - 3 y(x)) \left(\frac{d}{dx} y(x)\right)^2 - 4 y(x) \left(\frac{d}{dx} y(x)\right) (f(x) y(x) + g(x)) + (1 - y(x))^3$$

**Mathematica:** cpu = 8.823120 (sec), leaf count = 110

$$\text{DSolve}[4y(x)^2(1 - y(x)) (-f'(x) + f(x)^2 - g'(x) - g(x)^2) - 4y(x)y'(x)(f(x)y(x) + g(x)) + (1 - y(x))^3$$

**Maple:** cpu = 11.169 (sec), leaf count = 0

could not solve

**7.200 ODE No. 1790**

$$3 y(x) (1 - y(x)) \frac{d^2}{dx^2} y(x) - 2 (1 - 2 y(x)) \left(\frac{d}{dx} y(x)\right)^2 - h(y(x)) = 0$$

**Mathematica:** cpu = 21.362213 (sec), leaf count = 182

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \int_1^{\#1} - \frac{1}{(1 - K[2])^{2/3} K[2]^{2/3} \sqrt{2 \int_1^{K[2]} - \frac{h(K[1]) \exp(-2(\frac{2}{3} \log(1 - K[1]) + \frac{2}{3} \log(K[1]))}{3(K[1] - 1)K[1]} d \right.} \right. \right.$$

**Maple:** cpu = 0.171 (sec), leaf count = 219

$$\left\{ \int^{y(x)} -3 \frac{1}{\sqrt{-6 - b^2 \sqrt[3]{-b} (-b - 1)} \int \frac{h(-b)}{(-b^2 - b)^{4/3} - b(-b - 1)} d - b + 9 - b^2 \sqrt[3]{-b} (-b - 1) - C1 + 6 - b \sqrt[3]{-b} (-b - 1)} \right.$$

**7.201 ODE No. 1791**

$$(1 - y(x)) \frac{d^2}{dx^2} y(x) - 3(1 - 2y(x)) \left( \frac{d}{dx} y(x) \right)^2 - h(y(x)) = 0$$

**Mathematica:** cpu = 20.225068 (sec), leaf count = 164

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \int_1^{\#1} - \frac{e^{\frac{1}{2}(12-12K[2])}}}{(K[2] - 1)^3 \sqrt{2 \int_1^{K[2]} - \frac{h(K[1]) \exp(-2(6(K[1]-1)+3 \log(K[1]-1))}{K[1]-1}} dK[1] + c_1}} \right. \right. \right.$$

**Maple:** cpu = 0.249 (sec), leaf count = 90

$$\left\{ \int^{y(x)} \frac{1}{(\_b - 1)^3 (e^{-b})^6} \frac{1}{\sqrt{-2 \int \frac{h(\_b)}{(e^{-b})^{12} (\_b - 1)^7} d\_b + \_C1}} d\_b - x - \_C2 = 0, \int^{y(x)} - \frac{1}{(\_b - 1)^3 (e^{-b})^6} \right.$$

**7.202 ODE No. 1792**

$$ay(x)(-1 + y(x)) \frac{d^2}{dx^2} y(x) + (by(x) + c) \left( \frac{d}{dx} y(x) \right)^2 + h(y(x)) = 0$$

**Mathematica:** cpu = 25.014176 (sec), leaf count = 222

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \int_1^{\#1} - \frac{K[2]^{-\frac{c}{a}} (1 - K[2])^{\frac{1}{2} \left( \frac{2b}{a} + \frac{2c}{a} \right)}}{\sqrt{2 \int_1^{K[2]} - \frac{h(K[1]) \exp\left( \frac{-2(c \log(K[1]) - (b+c) \log(1-K[1]))}{a} \right)}{a(K[1]-1)K[1]} dK[1] + c_1}} dK[2] \& \right. \right. \right.$$

**Maple:** cpu = 0.562 (sec), leaf count = 192

$$\left\{ \int^{y(x)} a \frac{1}{\sqrt{-a \left( -\_C1 a + 2 \int \frac{h(\_b)}{\_b (\_b - 1)} \left( (\_b - 1)^{\frac{b}{a}} \right)^2 \left( (\_b - 1)^{\frac{c}{a}} \right)^2 \left( \_b^{\frac{c}{a}} \right)^{-2} d\_b \right)}} \left( \_b^{\frac{c}{a}} \right)^{-1} \left( (\_b - 1) \right.$$

**7.203 ODE No. 1793**

$$ay(x)(-1+y(x))\frac{d^2}{dx^2}y(x) - (a-1)(2y(x)-1)\left(\frac{d}{dx}y(x)\right)^2 + fy(x)(-1+y(x))\frac{d}{dx}y(x) = 0$$

**Mathematica:** cpu = 1.371674 (sec), leaf count = 113

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\frac{a(1-\#1)^{-1/a}(-\#1-1)\#1^{\frac{1}{a}}((a+1) {}_2F_1(-\frac{1}{a}, \frac{1}{a}; 1 + \frac{1}{a}; \#1) + \#1 {}_2F_1(1 + \frac{1}{a}, \frac{1}{a}; 2 + \frac{1}{a}; \#1))}{a+1} \right] \right\} \right.$$

**Maple:** cpu = 1.747 (sec), leaf count = 40

$$\left\{ -C1 e^{-\frac{fx}{a}} - C2 + \int^{y(x)} \frac{\sqrt{-a(-a-1)}}{-a(-a-1)} d_a = 0 \right\}$$

**7.204 ODE No. 1794**

$$aby(x)(-1+y(x))\frac{d^2}{dx^2}y(x) - ((2ab-a-b)y(x) + (1-a)b)\left(\frac{d}{dx}y(x)\right)^2 + fy(x)(-1+y(x))\frac{d}{dx}y(x)$$

**Mathematica:** cpu = 1.296165 (sec), leaf count = 98

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ -\frac{a\#1^{\frac{1}{a}}((a+1) {}_2F_1(\frac{1}{a}, -\frac{1}{b}; 1 + \frac{1}{a}; \#1) + \#1 {}_2F_1(1 + \frac{1}{a}, \frac{b-1}{b}; 2 + \frac{1}{a}; \#1))}{a+1} \right] \& \right\} \right.$$

**Maple:** cpu = 1.669 (sec), leaf count = 46

$$\left\{ -C1 e^{-\frac{fx}{ab}} - C2 + \int^{y(x)} \frac{\sqrt{-a^b(-a-1)}}{-a(-a-1)} d_a = 0 \right\}$$

**7.205 ODE No. 1795**

$$x(y(x))^2 \frac{d^2}{dx^2}y(x) - a = 0$$

**Mathematica:** cpu = 0.259533 (sec), leaf count = 116

$$\text{Solve} \left[ \frac{\sqrt{-\frac{2ay(x)}{x} - \frac{2c_1y(x)^2}{x^2}}}{2c_1} - \frac{a \tan^{-1} \left( \frac{\sqrt{2}\sqrt{c_1} \left( \frac{a+y(x)}{2c_1} + \frac{y(x)}{x} \right)}{\sqrt{-\frac{2ay(x)}{x} - \frac{2c_1y(x)^2}{x^2}}} \right)}{2\sqrt{2}c_1^{3/2}} - c_2 - \frac{1}{x} = 0, y(x) \right]$$

**Maple:** cpu = 2.262 (sec), leaf count = 793

$$\left\{ y(x) = \frac{-C1 x \left( 81 - C1^2 a^2 + 18 a - C1 e^{\text{RootOf}(243 \text{csgn}(-C1^{-1}) - C1^4 a^2 x - 54 - Z e^{-Z} a x - C1^3 - 3 \text{csgn}(-C1^{-1}) (e^{-Z})^2 - C1^2)} \right)}{2 e^{\text{RootOf}(243 \text{csgn}(-C1^{-1}) - C1^4 a^2 x - 54 - Z e^{-Z} a x - C1^3 - 3 \text{csgn}(-C1^{-1}) (e^{-Z})^2 - C1^2)}} \right.$$

**7.206 ODE No. 1796**

$$(a^2 - x^2) (a^2 - (y(x))^2) \frac{d^2}{dx^2} y(x) + (a^2 - x^2) y(x) \left( \frac{d}{dx} y(x) \right)^2 - x (a^2 - (y(x))^2) \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.340043 (sec), leaf count = 66

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{2} e^{-c_2} \left( \sqrt{x^2 - a^2} + x \right)^{-c_1} \left( a^2 \left( \sqrt{x^2 - a^2} + x \right)^{2c_1} + e^{2c_2} \right) \right\} \right\}$$

**Maple:** cpu = 1.732 (sec), leaf count = 51

$$\left\{ y(x) = \frac{1}{2 - C2} \left( \left( \left( x + \sqrt{-a^2 + x^2} \right)^{-C1} \right)^2 - C2^2 + a^2 \right) \left( \left( x + \sqrt{-a^2 + x^2} \right)^{-C1} \right)^{-1} \right\}$$

**7.207 ODE No. 1797**

$$2 x^2 y(x) (-1 + y(x)) \frac{d^2}{dx^2} y(x) - x^2 (3 y(x) - 1) \left( \frac{d}{dx} y(x) \right)^2 + 2 x y(x) (-1 + y(x)) \frac{d}{dx} y(x) + (a(y(x))^2 + b) y(x) = 0$$

**Mathematica:** cpu = 23.559992 (sec), leaf count = 91

$$\text{DSolve}[(y(x) - 1)^3 (a y(x)^2 + b) + c x y(x)^2 (y(x) - 1) + d x^2 y(x)^2 (y(x) + 1) + 2 x^2 y(x) (y(x) - 1) y''(x) - x^2 y(x) y'(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 5.881 (sec), leaf count = 0

could not solve



**7.208 ODE No. 1798**

$$x^3(y(x))^2 \frac{d^2}{dx^2}y(x) + (y(x) + x) \left( x \frac{d}{dx}y(x) - y(x) \right)^3 = 0$$

**Mathematica:** cpu = 38.092837 (sec), leaf count = 37

$$\text{DSolve}\left[x^3y(x)^2y''(x) + (y(x) + x)(xy'(x) - y(x))^3 = 0, y(x), x\right]$$

**Maple:** cpu = 1.716 (sec), leaf count = 166

$$\left\{ y(x) = \text{RootOf}\left(-2 \ln(x) - \int^{-Z} 1\left(i\sqrt{3}Y_{i\sqrt{3}}\left(2\sqrt{-f}\right) - C1\sqrt{-f} + i\sqrt{3}J_{i\sqrt{3}}\left(2\sqrt{-f}\right)\sqrt{-f} + Y_{i\sqrt{3}}\left(2\sqrt{-f}\right)\right) dz, x\right\}$$

**7.209 ODE No. 1799**

$$(y(x))^3 \frac{d^2}{dx^2}y(x) - a = 0$$

**Mathematica:** cpu = 1.945247 (sec), leaf count = 88

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{a + c_1^2x^2 + 2c_2c_1^2x + c_2^2c_1^2}}{\sqrt{c_1}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{a + c_1^2x^2 + 2c_2c_1^2x + c_2^2c_1^2}}{\sqrt{c_1}} \right\} \right\}$$

**Maple:** cpu = 1.762 (sec), leaf count = 70

$$\left\{ y(x) = \frac{1}{-C1} \sqrt{-C1 (-C1^2 - C2^2 + 2 - C1^2 - C2 x + -C1^2x^2 + a)}, y(x) = -\frac{1}{-C1} \sqrt{-C1 (-C1^2 - C2^2 + 2 - C1^2 - C2 x + -C1^2x^2 + a)} \right\}$$

**7.210 ODE No. 1800**

$$y(x) ((y(x))^2 + 1) \frac{d^2}{dx^2}y(x) + (1 - 3(y(x))^2) \left( \frac{d}{dx}y(x) \right)^2 = 0$$

**Mathematica:** cpu = 0.521066 (sec), leaf count = 84

$$\left\{ \left\{ y(x) \rightarrow -\frac{\sqrt{-2c_1x - 2c_2c_1 - 1}}{\sqrt{2}\sqrt{c_1x + c_2c_1}} \right\}, \left\{ y(x) \rightarrow \frac{\sqrt{-2c_1x - 2c_2c_1 - 1}}{\sqrt{2}\sqrt{c_1x + c_2c_1}} \right\} \right\}$$

**Maple:** cpu = 1.607 (sec), leaf count = 67

$$\left\{ y(x) = -\frac{1}{2 - C1 x + 2 - C2} \sqrt{-(2 - C1 x + 2 - C2)(2 - C1 x + 2 - C2 + 1)}, y(x) = \frac{1}{2 - C1 x + 2 - C2} \sqrt{-(2 - C1 x + 2 - C2)(2 - C1 x + 2 - C2 + 1)} \right\}$$

**7.211 ODE No. 1801**

$$2(y(x))^3 \frac{d^2}{dx^2}y(x) + (y(x))^4 - a^2x(y(x))^2 - 1 = 0$$

**Mathematica:** cpu = 20.022043 (sec), leaf count = 32

$$\text{DSolve}[-a^2xy(x)^2 + 2y(x)^3y''(x) + y(x)^4 - 1 = 0, y(x), x]$$

**Maple:** cpu = 1.794 (sec), leaf count = 0

could not solve

**7.212 ODE No. 1802**

$$2(y(x))^3 \frac{d^2}{dx^2}y(x) + (y(x))^2 \left(\frac{d}{dx}y(x)\right)^2 - ax^2 - bx - c = 0$$

**Mathematica:** cpu = 0.357545 (sec), leaf count = 41

$$\text{DSolve}[-ax^2 - bx - c + 2y(x)^3y''(x) + y(x)^2y'(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 1.903 (sec), leaf count = 0

could not solve

**7.213 ODE No. 1803**

$$2(c - y(x))(-y(x) + b)(-y(x) + a) \frac{d^2}{dx^2}y(x) + ((-y(x) + a)(-y(x) + b) + (c - y(x))(-y(x) + a) + (-$$

**Mathematica:** cpu = 18.332328 (sec), leaf count = 10387

$$\left\{ \text{Solve} \left[ \frac{2F \left( \sin^{-1} \left( \sqrt{\frac{(\text{Root}[a_0\#1^4 + (-aa_0 - ba_0 - ca_0 - c_1)\#1^3 + (-a_1 - a_2 - a_3 + aa_0b + aa_0c + a_0bc + ac_1 + bc_1 + cc_1)\#1^2 + (aa_2 + ca_2 + \dots)}{(\text{Root}[a_0\#1^4 + (-aa_0 - ba_0 - ca_0 - c_1)\#1^3 + (-a_1 - a_2 - a_3 + aa_0b + aa_0c + a_0bc + ac_1 + bc_1 + cc_1)\#1^2 + (aa_2 + ca_2 + \dots}} \right)} \right)}{\dots} \right] \right.$$

**Maple:** cpu = 5.288 (sec), leaf count = 230971

Result too large for latex to process

**7.214 ODE No. 1804**

$$(4(y(x))^3 - ay(x) - b) \frac{d^2}{dx^2}y(x) - (6(y(x))^2 - a/2) \left(\frac{d}{dx}y(x)\right)^2 = 0$$

**Mathematica:** cpu = 2.998381 (sec), leaf count = 415

Solve  $\left[ \frac{2\sqrt{\frac{y(x)-\text{Root}[4\#1^3-\#1a-b\&,1]}{\text{Root}[4\#1^3-\#1a-b\&,3]-\text{Root}[4\#1^3-\#1a-b\&,1]}}\sqrt{\frac{y(x)-\text{Root}[4\#1^3-\#1a-b\&,2]}{\text{Root}[4\#1^3-\#1a-b\&,3]-\text{Root}[4\#1^3-\#1a-b\&,2]}}(y(x) - \text{Root}[4\#1^3-\#1a-b\&,2])}{c_1\sqrt{2ay(x) + 2b - 8y(x)^3}} \right]$

**Maple:** cpu = 0.031 (sec), leaf count = 31

$$\left\{ \int^{y(x)} \frac{1}{\sqrt{4a^3 - a_a - b}} d_a - C1 x - C2 = 0 \right\}$$

**7.215 ODE No. 1805**

$$(4(y(x))^3 - ay(x) - b) \left(\frac{d^2}{dx^2}y(x) + f \frac{d}{dx}y(x)\right) - (6(y(x))^2 - a/2) \left(\frac{d}{dx}y(x)\right)^2 = 0$$

**Mathematica:** cpu = 1.882239 (sec), leaf count = 436

Solve  $\left[ \frac{2\sqrt{\frac{y(x)-\text{Root}[4\#1^3-\#1a-b\&,1]}{\text{Root}[4\#1^3-\#1a-b\&,3]-\text{Root}[4\#1^3-\#1a-b\&,1]}}\sqrt{\frac{y(x)-\text{Root}[4\#1^3-\#1a-b\&,2]}{\text{Root}[4\#1^3-\#1a-b\&,3]-\text{Root}[4\#1^3-\#1a-b\&,2]}}(y(x) - \text{Root}[4\#1^3-\#1a-b\&,2])}{\sqrt{ay(x) + b - 4y(x)^3}} \right]$

**Maple:** cpu = 0.031 (sec), leaf count = 34

$$\left\{ -C1 e^{-fx} - C2 + \int^{y(x)} \frac{1}{\sqrt{4a^3 - a_a - b}} d_a = 0 \right\}$$

**7.216 ODE No. 1806**

$$-2xy(x)(1-x)(1-y(x))(x-y(x))\frac{d^2}{dx^2}y(x) + x(1-x)(x-2xy(x)-2y(x)+3(y(x))^2)\left(\frac{d}{dx}y(x)\right)$$

**Mathematica:** cpu = 18.424840 (sec), leaf count = 123

$$\text{DSolve}[-f(x)((y(x)-1)y(x)(y(x)-x))^{3/2} + 2(1-y(x))(x^2-2xy(x)+y(x))y(x)y'(x) - 2(1-x)x(1$$

**Maple:** cpu = 3.073 (sec), leaf count = 916

$$\left\{ \left( \frac{3}{4} \int \frac{1}{x-1} e^{\int \frac{1}{x(x-1)} \text{EllipticE}(\sqrt{x}) (\text{EllipticK}(\sqrt{x}))^{-1} dx} \int x^{\frac{3}{2}} \int^{y(x)} \frac{1}{(-a+x)^2 \sqrt{-a^3 - a^2x - a^2 + ax}} d \right. \right.$$

**7.217 ODE No. 1807**

$$2x^2y(x)(1-x)^2(1-y(x))(x-y(x))\frac{d^2}{dx^2}y(x) - x^2(1-x)^2(x-2xy(x)-2y(x)+3(y(x))^2)\left(\frac{d}{dx}y(x)\right)$$

**Mathematica:** cpu = 33.961813 (sec), leaf count = 185

$$\text{DSolve}[a(1-y(x))^2(x-y(x))^2y(x)^2 + bx(1-y(x))^2(x-y(x))^2 - c(1-x)(x-y(x))^2y(x)^2 - d(1-x)x$$

**Maple:** cpu = 136.267 (sec), leaf count = 0

could not solve

**7.218 ODE No. 1808**

$$((y(x))^2 - 1)(a^2(y(x))^2 - 1)\frac{d^2}{dx^2}y(x) + b\sqrt{(1-(y(x))^2)(1-a^2(y(x))^2)}\left(\frac{d}{dx}y(x)\right)^2 + (1+a^2-2a^2$$

**Mathematica:** cpu = 103.724671 (sec), leaf count = 172

$$\text{Solve} \left[ \log(x) - b \left( \frac{\log \left( bc_1 \sqrt{1-y(x)^2} \sqrt{1-a^2y(x)^2} + \sqrt{y(x)^2-1} \sqrt{a^2y(x)^2-1} \exp \left( \frac{b\sqrt{1-y(x)^2}\sqrt{1-a^2y(x)^2}}{\sqrt{y(x)^2-1}\sqrt{a^2y(x)^2-1}} \right)}{b} \right. \right.$$

**Maple:** cpu = 0.110 (sec), leaf count = 72

$$\left\{ \int^{y(x)} e^{\int \frac{1}{(-b^2-1)(-b^2a^2-1)} \left( -2-b^3a^2 - b a^2 + b \sqrt{(-b^2-1)(-b^2a^2-1)} + b \right) d_b} d_b - C1 x - C2 = 0 \right\}$$

**7.219 ODE No. 1809**

$$(c + 2bx + ax^2 + (y(x))^2)^2 \frac{d^2}{dx^2}y(x) + dy(x) = 0$$

**Mathematica:** cpu = 43.116975 (sec), leaf count = 33

$$\text{DSolve}\left[y''(x) (ax^2 + 2bx + c + y(x)^2)^2 + dy(x) = 0, y(x), x\right]$$

**Maple:** cpu = 0.437 (sec), leaf count = 382

$$\left\{ y(x) = \text{RootOf}\left(-\int^{-Z} \frac{a}{-f^4ac + f^4b^2 + C1 f^2a^2 - c f^2a + b^2 f^2 + C1 a^2 + d} \sqrt{-f^6ac + f^6b^2 + C1 f^4a^2 - c f^4a + b^2 f^4 + C1 a^4 + d} \right)\right.$$

**7.220 ODE No. 1810**

$$\sqrt{y(x)} \frac{d^2}{dx^2}y(x) - a = 0$$

**Mathematica:** cpu = 0.060008 (sec), leaf count = 1677

$$\left\{ \left\{ y(x) \rightarrow \frac{3c_1^2}{16a^2} + \sqrt[3]{-\frac{221184c_1^6}{a^6} + \frac{159252480x^2c_1^3}{a^2} + \frac{159252480c_2^2c_1^3}{a^2} + \frac{318504960xc_2c_1^3}{a^2} + 2293235712a^2x^4 + 2293235712a^2x^2 + 2293235712a^2} \right\} \right.$$

**Maple:** cpu = 0.109 (sec), leaf count = 55

$$\left\{ \int^{y(x)} \frac{1}{\sqrt{4\sqrt{-aa} - C1}} d_a - x - C2 = 0, \int^{y(x)} -\frac{1}{\sqrt{4\sqrt{-aa} - C1}} d_a - x - C2 = 0 \right\}$$

**7.221 ODE No. 1811**

$$\sqrt{(y(x))^2 + x^2} \frac{d^2}{dx^2}y(x) - a \left( \left( \frac{d}{dx}y(x) \right)^2 + 1 \right)^{3/2} = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 3.026 (sec), leaf count = 1864

$$\left\{ y(x) = \text{RootOf} \left( -\ln(x) + \int^{-z} \frac{1}{-g^2 + 1} \left( \text{RootOf} \left( \arctan(-g) + \int^{-z} \frac{1}{(-f^2 a^2 + a^2 - 1)(-f^2 + 1)} \right) \right) \right) \right\}$$

### 7.222 ODE No. 1812

$$y(x) (1 - \ln(y(x))) \frac{d^2}{dx^2} y(x) + (1 + \ln(y(x))) \left( \frac{d}{dx} y(x) \right)^2 = 0$$

**Mathematica:** cpu = 0.027003 (sec), leaf count = 29

$$\left\{ \left\{ y(x) \rightarrow e^{\frac{c_1 x + c_2 c_1 - 1}{c_1 (c_2 + x)}} \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 19

$$\left\{ y(x) = e^{\frac{C1 x + C2 - 1}{-C1 x - C2}} \right\}$$

### 7.223 ODE No. 1813

$$(b + a(\sin(y(x)))^2) \frac{d^2}{dx^2} y(x) + a \left( \frac{d}{dx} y(x) \right)^2 \cos(y(x)) \sin(y(x)) + Ay(x) (c + a(\sin(y(x)))^2) = 0$$

**Mathematica:** cpu = 100.860808 (sec), leaf count = 48

$$\text{DSolve}[Ay(x) (a \sin^2(y(x)) + c) + y''(x) (a \sin^2(y(x)) + b) + ay'(x)^2 \sin(y(x)) \cos(y(x)) = 0, y(x), x]$$

**Maple:** cpu = 0.265 (sec), leaf count = 146

$$\left\{ \int^{y(x)} \sqrt{2} (b + a(\sin(-a))^2) \frac{1}{\sqrt{(b + a(\sin(-a))^2) (2 A a - a \cos(-a) \sin(-a) - A a (\sin(-a))^2 - A a - a^2)}} \right\}$$

**7.224 ODE No. 1814**

$$h(y(x)) \frac{d^2}{dx^2} y(x) + aD(h)(y(x)) \left( \frac{d}{dx} y(x) \right)^2 + j(y(x)) = 0$$

**Mathematica:** cpu = 13.253683 (sec), leaf count = 116

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \int_1^{\#1} \frac{e^{aK[2]}}{\sqrt{2 \int_1^{K[2]} - \frac{e^{2aK[1]} j(K[1])}{h(K[1])} dK[1] + c_1}} dK[2] \& \right] [c_2 + x] \right\}, \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \int_1^{\#1} \frac{e^{aK[2]}}{\sqrt{2 \int_1^{K[2]} - \frac{e^{2aK[1]} j(K[1])}{h(K[1])} dK[1] + c_1}} dK[2] \& \right] [c_2 + x] \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 90

$$\left\{ \int^{y(x)} \frac{1}{(h(-b))^{-a}} \frac{1}{\sqrt{-2 \int \frac{((h(-b))^a)^2 j(-b)}{h(-b)} d_-b + _C1}} d_-b - x - _C2 = 0, \int^{y(x)} - \frac{1}{(h(-b))^{-a}} \frac{1}{\sqrt{-2 \int \frac{((h(-b))^a)^2 j(-b)}{h(-b)} d_-b + _C1}} d_-b - x - _C2 = 0 \right\}$$

**7.225 ODE No. 1815**

$$h(y(x)) \frac{d^2}{dx^2} y(x) - D(h)(y(x)) \left( \frac{d}{dx} y(x) \right)^2 - (h(y(x)))^2 j \left( x, \frac{\frac{d}{dx} y(x)}{h(y(x))} \right) = 0$$

**Mathematica:** cpu = 1.169649 (sec), leaf count = 45

$$\text{DSolve} \left[ h(y(x))^2 \left( -j \left( x, \frac{y'(x)}{h(y(x))} \right) \right) + h(y(x)) y''(x) - h(y(x)) y'(x)^2 = 0, y(x), x \right]$$

**Maple:** cpu = 0.780 (sec), leaf count = 74

$$\left\{ y(x) = \text{ODESolStruc} \left( \text{RootOf} \left( \int -b(-a) d_-a + _C1 - \int^{-Z} (h(-f))^{-1} d_-f \right), \left[ \left\{ \frac{d}{d_-a} -b(-a) = j(-a) \right\} \right] \right)$$

**7.226 ODE No. 1816**

$$\left( \frac{d}{dx} y(x) \right) \frac{d^2}{dx^2} y(x) - x^2 y(x) \frac{d}{dx} y(x) - x(y(x))^2 = 0$$

**Mathematica:** cpu = 63.610077 (sec), leaf count = 34

$$\text{DSolve} [x^2(-y(x))y'(x) + y'(x)y''(x) - xy(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 0.874 (sec), leaf count = 46

$$\left\{ y(x) = \text{ODESolStruc} \left( -b(-a), \left[ \left\{ -(-b(-a))^2 -a^2 + \left( \frac{d}{d_-a} -b(-a) \right)^2 + _C1 = 0 \right\} \right], \{ _a = x, -b(-a) \} \right)$$

**7.227 ODE No. 1817**

$$\left( x \frac{d}{dx} y(x) - y(x) \right) \frac{d^2}{dx^2} y(x) + 4 \left( \frac{d}{dx} y(x) \right)^2 = 0$$

**Mathematica:** cpu = 14.420831 (sec), leaf count = 31

$$\text{DSolve}[4y'(x)^2 + (xy'(x) - y(x))y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.156 (sec), leaf count = 40

$$\left\{ y(x) = e^{\int \ln(x) dx} e^{\text{RootOf}(\ln(e^{-Z} - 1)e^{-Z} + C1 e^{-Z} - Z e^{-Z} - b e^{-Z} + 2) - 1d - b + C2} \right\}$$

**7.228 ODE No. 1818**

$$\left( x \frac{d}{dx} y(x) - y(x) \right) \frac{d^2}{dx^2} y(x) - \left( \left( \frac{d}{dx} y(x) \right)^2 + 1 \right)^2 = 0$$

**Mathematica:** cpu = 1.402678 (sec), leaf count = 35

$$\text{DSolve}[(xy'(x) - y(x))y''(x) - (y'(x)^2 + 1)^2 = 0, y(x), x]$$

**Maple:** cpu = 0.265 (sec), leaf count = 66

$$\left\{ y(x) = \text{RootOf} \left( -\ln(x) + \int^{-Z} \frac{-f + \text{RootOf}(-\tan(-Z^{-1}) - C1 - Z + f - C1 \tan(-Z^{-1}) + \tan(-Z^{-1})}{-f^2 + \dots} dx \right) \right\}$$

**7.229 ODE No. 1819**

$$ax^3 \left( \frac{d}{dx} y(x) \right) \frac{d^2}{dx^2} y(x) + b(y(x))^2 = 0$$

**Mathematica:** cpu = 90.744523 (sec), leaf count = 26

$$\text{DSolve}[ax^3y'(x)y''(x) + by(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 0.047 (sec), leaf count = 42

$$\left\{ y(x) = e^{\int \ln(x) dx} \text{RootOf} \left( -f^{-Z} \frac{a-a}{a-a^3-a^2a+b} d - a - b + C1 \right) d - b + C2 \right\}$$



**7.230 ODE No. 1820**

$$\left( f1 \frac{d}{dx} y(x) + f2 y(x) \right) \frac{d^2}{dx^2} y(x) + f3 \left( \frac{d}{dx} y(x) \right)^2 + f4(x) y(x) \frac{d}{dx} y(x) + f5(x) (y(x))^2 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.780 (sec), leaf count = 81

$$\left\{ y(x) = ODESolStruc \left( e^{\int -b(-a) dx - C1}, \left[ \frac{d}{dx} b(-a) = -\frac{(-b(-a))^3 f1 + (f2 + f3) (-b(-a))^2 + f4(-a)}{-b(-a) f1 + f2} \right] \right) \right.$$

**7.231 ODE No. 1821**

$$\left( 2 (y(x))^2 \frac{d}{dx} y(x) + x^2 \right) \frac{d^2}{dx^2} y(x) + 2 y(x) \left( \frac{d}{dx} y(x) \right)^3 + 3 x \frac{d}{dx} y(x) + y(x) = 0$$

**Mathematica:** cpu = 42.477894 (sec), leaf count = 45

$$\text{DSolve}[(x^2 + 2y(x)^2 y'(x)) y''(x) + 2y(x) y'(x)^3 + 3x y'(x) + y(x) = 0, y(x), x]$$

**Maple:** cpu = 1.529 (sec), leaf count = 54

$$\left\{ y(x) = ODESolStruc \left( -b(-a), \left[ (-b(-a))^2 \left( \frac{d}{dx} b(-a) \right)^2 + -a^2 \frac{d}{dx} b(-a) + -a b(-a) + -C \right] \right) \right.$$

**7.232 ODE No. 1822**

$$\left( \left( \frac{d}{dx} y(x) \right)^2 + (y(x))^2 \right) \frac{d^2}{dx^2} y(x) + (y(x))^3 = 0$$

**Mathematica:** cpu = 1.083138 (sec), leaf count = 371

$$\left\{ \left\{ y(x) \rightarrow c_2 \exp \left( \frac{1}{12} \left( -2\sqrt{3} \tan^{-1} \left( \frac{1 + 2 \text{InverseFunction} \left[ \frac{(\sqrt{3}-i) \tan^{-1} \left( \frac{\#1}{\sqrt{\frac{1}{2}(1-i\sqrt{3})}} \right)}{\sqrt{6(1-i\sqrt{3})}} \right) + \frac{(\sqrt{3}+i) \tan^{-1} \left( \frac{\#1}{\sqrt{\frac{1}{2}(1+i\sqrt{3})}} \right)}{\sqrt{6(1+i\sqrt{3})}} \right)}{\sqrt{3}} \right) \right) \right. \right.$$

**Maple:** cpu = 0.842 (sec), leaf count = 295

$$\left\{ y(x) = \_C2 \left( 1 + \left( \tan(\sqrt{3}x) \right)^2 \right)^{-\frac{C1^2}{4-C1^2+4}} \left( -C1 + \tan(\sqrt{3}x) \right)^{\frac{C1^2}{2-C1^2+2}} \left( 1 + \left( \tan(\sqrt{3}x) \right)^2 \right)^{-\frac{1}{4-C1^2+4}} \right.$$

### 7.233 ODE No. 1823

$$\left( \left( \frac{d}{dx} y(x) \right)^2 + a \left( x \frac{d}{dx} y(x) - y(x) \right) \right) \frac{d^2}{dx^2} y(x) - b = 0$$

**Mathematica:** cpu = 0.170022 (sec), leaf count = 35

$$\text{DSolve}[y''(x) (a(x)y'(x) - y(x)) + y'(x)^2 - b = 0, y(x), x]$$

**Maple:** cpu = 0.281 (sec), leaf count = 423

$$\left\{ y(x) = -\frac{ax^2}{4} + \text{RootOf} \left( -x - \int^{-Z} \frac{1}{-f^2 a^2 - 4\_f b + 2\_C1} \sqrt{-f^3 a^3 - 4 a\_f^2 b + 2 a\_f\_C1 - \sqrt{4\_f}} \right) \right.$$

### 7.234 ODE No. 1824

$$\left( a \sqrt{\left( \frac{d}{dx} y(x) \right)^2 + 1} - x \frac{d}{dx} y(x) \right) \frac{d^2}{dx^2} y(x) - \left( \frac{d}{dx} y(x) \right)^2 - 1 = 0$$

**Mathematica:** cpu = 0.352545 (sec), leaf count = 347

$$\left\{ \left\{ y(x) \rightarrow \frac{-2\sqrt{x^2(a^2 + c_1^2 - x^2)} + c_1 x \log \left( -c_1 \left( \sqrt{x^2(a^2 + c_1^2 - x^2)} + c_1 x \right) + a^2(-x) + ax^2 \right) + c_1 x \log \right. \right.$$

**Maple:** cpu = 0.717 (sec), leaf count = 99

$$\left\{ y(x) = \int \frac{1}{a(a^2 - x^2)} \left( -_C1 a^2 + x \sqrt{a^2 (-C1^2 + a^2 - x^2)} \right) dx + \_C2, y(x) = \int -\frac{1}{a(a^2 - x^2)} \left( -C1 \right.$$

**7.235 ODE No. 1825**

$$h\left(\frac{d}{dx}y(x)\right) \frac{d^2}{dx^2}y(x) + j(y(x)) \frac{d}{dx}y(x) + f = 0$$

**Mathematica:** cpu = 0.040505 (sec), leaf count = 27

$$\text{DSolve}[f(x) + y''(x)h(y'(x)) + j(y(x))y'(x) = 0, y(x), x]$$

**Maple:** cpu = 0.702 (sec), leaf count = 50

$$\left\{ y(x) = \text{ODESolStruc}\left(-f(-b), \left[\int^{-f(-b)} j(-a) d_a + \int^{\frac{d}{d-b}f(-b)} h(-a) d_a + -b f + -C1 = 0\right], \{ \right.$$

**7.236 ODE No. 1826**

$$\left(\frac{d^2}{dx^2}y(x)\right)^2 - ay(x) - b = 0$$

**Mathematica:** cpu = 0.773098 (sec), leaf count = 233

$$\left\{ \text{Solve}\left[\frac{3(ay(x) + b)^2 \left(3c_1 - \frac{4(ay(x)+b)^{3/2}}{a}\right) \left(1 - \frac{4(ay(x)+b)^{3/2}}{3ac_1}\right) {}_2F_1\left(\frac{1}{2}, \frac{2}{3}, \frac{5}{3}, \frac{4(b+ay(x))^{3/2}}{3ac_1}\right)^2}{(4(ay(x) + b)^{3/2} - 3ac_1)^2} = (c_2 + x)^2, y(x)\right.$$

**Maple:** cpu = 0.203 (sec), leaf count = 201

$$\left\{ \int^{y(x)} a\sqrt{3} \frac{1}{\sqrt{a(4_a \sqrt{a_a + ba} + 4b\sqrt{a_a + b} - C1)}} d_a - x - C2 = 0, \int^{y(x)} -3 \frac{1}{\sqrt{-3a(4_a \sqrt{a_a + ba} + 4b\sqrt{a_a + b} - C1)}} d_a - x - C2 = 0 \right.$$

**7.237 ODE No. 1827**

$$a^2 \left(\frac{d^2}{dx^2}y(x)\right)^2 - 2ax \frac{d^2}{dx^2}y(x) + \frac{d}{dx}y(x) = 0$$

**Mathematica:** cpu = 0.768097 (sec), leaf count = 29

$$\text{DSolve}[a^2 y''(x)^2 - 2axy''(x) + y'(x) = 0, y(x), x]$$

**Maple:** cpu = 2.169 (sec), leaf count = 81

$$\left\{ y(x) = \int \text{RootOf}\left(-\int_{-g}^{-Z} \left(x\sqrt{x^2 - f} - x^2 + 2a_f\right)^{-1} d_f + C1\right) dx + C2, y(x) = \int \text{RootOf}\left(\right.$$

**7.238 ODE No. 1828**

$$2(x^2 + 1) \left( \frac{d^2}{dx^2} y(x) \right)^2 - x \left( \frac{d^2}{dx^2} y(x) \right) \left( x + 4 \frac{d}{dx} y(x) \right) + 2 \left( x + \frac{d}{dx} y(x) \right) \frac{d}{dx} y(x) - 2y(x) = 0$$

**Mathematica:** cpu = 0.012502 (sec), leaf count = 32

$$\left\{ \left\{ y(x) \rightarrow -\frac{1}{2} \sqrt{c_2 - c_1^2 x^2 + c_1 x + c_2} \right\} \right\}$$

**Maple:** cpu = 1.045 (sec), leaf count = 20

$$\left\{ y(x) = \frac{-C1 x^2}{2} + \_C2 x + \_C1^2 + \_C2^2 \right\}$$

**7.239 ODE No. 1829**

$$3x^2 \left( \frac{d^2}{dx^2} y(x) \right)^2 - 2 \left( 3x \frac{d}{dx} y(x) + y(x) \right) \frac{d^2}{dx^2} y(x) + 4 \left( \frac{d}{dx} y(x) \right)^2 = 0$$

**Mathematica:** cpu = 0.006001 (sec), leaf count = 24

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1^2 x^2}{c_2} + c_1 x + c_2 \right\} \right\}$$

**Maple:** cpu = 0.234 (sec), leaf count = 32

$$\left\{ y(x) = x^{\frac{2\sqrt{3}}{3}} \_C1 x, y(x) = \frac{-C1^2 x^2}{\_C2} + \_C1 x + \_C2 \right\}$$

**7.240 ODE No. 1830**

$$x^2(2 - 9x) \left( \frac{d^2}{dx^2} y(x) \right)^2 - 6x(1 - 6x) \left( \frac{d}{dx} y(x) \right) \frac{d^2}{dx^2} y(x) + 6 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - 36x \left( \frac{d}{dx} y(x) \right)^2 = 0$$

**Mathematica:** cpu = 0.029004 (sec), leaf count = 24

$$\left\{ \left\{ y(x) \rightarrow \frac{c_1^2 x^3}{c_2} + c_1 x + c_2 \right\} \right\}$$

**Maple:** cpu = 0.390 (sec), leaf count = 312

$$\left\{ y(x) = 27 \_C1 \left( (9x - 1) \sqrt{9} + 9 \sqrt{9x^2 - 2x} \right)^{-2/9 \sqrt{9}} \left( (9x - 1) \sqrt{9} + 9 \sqrt{x(9x - 2)} \right)^{-\frac{5\sqrt{9}}{18}} \sqrt{1 \left( 1 + 1 \right)} \right\}$$

**7.241 ODE No. 1831**

$$(F_{1,1})(x) \left( \frac{d}{dx} y(x) \right)^2 + \left( ((F_{2,1})(x) + (F_{1,2})(x)) \frac{d^2}{dx^2} y(x) + y(x) ((F_{1,0})(x) + (F_{0,1})(x)) \right) \frac{d}{dx} y(x) + (F_{0,0})(x) y(x)$$

**Mathematica:** cpu = 230.453764 (sec), leaf count = 90

DSolve[y(x)(xF(0, 2) + xF(2, 0))y''(x) + xF(2, 2)y''(x)^2 + xF(1, 1)y''(x) + y'(x)((xF(1, 2) + xF(2, 1))y'(x) + (xF(0, 1) + xF(1, 0))y(x)) = 0, x]

**Maple:** cpu = 1.731 (sec), leaf count = 191

$$\left\{ y(x) = ODESolStruc \left( e^{\int -b(-a) dx + C1}, \left[ \frac{d}{dx} -b(-a) = -(-b(-a))^2 - \frac{((F_{2,1})(-a) + (F_{1,2})(-a))}{2(F_{2,2})(-a)} \right] \right) \right.$$

**7.242 ODE No. 1832**

$$y(x) \left( \frac{d^2}{dx^2} y(x) \right)^2 - ae^{2x} = 0$$

**Mathematica:** cpu = 0.682087 (sec), leaf count = 24

DSolve[y(x)y''(x)^2 - ae^{2x} = 0, y(x), x]

**Maple:** cpu = 0.608 (sec), leaf count = 117

$$\left\{ y(x) = ODESolStruc \left( -a \left( e^{-\frac{2 \int -b(-a) dx - \frac{2 C1}{3}}}{3} \right)^{-1}, \left[ \frac{d}{dx} -b(-a) = -\frac{(-b(-a))^3}{9-a} (-4-a^2 + 9\sqrt{a-a}) \right] \right) \right.$$

**7.243 ODE No. 1833**

$$(a^2(y(x))^2 - b^2) \left( \frac{d^2}{dx^2} y(x) \right)^2 - 2a^2y(x) \left( \frac{d}{dx} y(x) \right)^2 \frac{d^2}{dx^2} y(x) + \left( a^2 \left( \frac{d}{dx} y(x) \right)^2 - 1 \right) \left( \frac{d}{dx} y(x) \right)^2 = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 2.465 (sec), leaf count = 145

$$\left\{ y(x) = -C1, y(x) = b \left( e^{-\frac{C2+x}{b} \sqrt{-C1^2 a^2 - 1}} - -C1 \right) \frac{1}{\sqrt{-C1^2 a^2 - 1}}, y(x) = \frac{b}{a} \tan \left( \frac{-C1 - x \sqrt{a^2}}{ab} \right) \frac{1}{\sqrt{\tan^2 \left( \frac{-C1 - x \sqrt{a^2}}{ab} \right) + 1}}$$

**7.244 ODE No. 1834**

$$\left( (y(x))^2 - x^2 \left( \frac{d}{dx} y(x) \right)^2 + x^2 y(x) \frac{d^2}{dx^2} y(x) \right)^2 - 4xy(x) \left( x \frac{d}{dx} y(x) - y(x) \right)^3 = 0$$

**Mathematica:** cpu = 16.501095 (sec), leaf count = 53

$$\text{DSolve}\left[ (x^2 y(x) y''(x) + x^2 (-y'(x)^2) + y(x)^2)^2 - 4xy(x) (xy'(x) - y(x))^3 = 0, y(x), x \right]$$

**Maple:** cpu = 0.343 (sec), leaf count = 86

$$\left\{ y(x) = \text{ODESolStruc} \left( e^{\int -b(-a) dx - C1}, \left[ \frac{d}{d_a} b(-a) = 2 \frac{\sqrt{-a} (-a - b(-a) - 1) - b(-a)}{-a} - \frac{1}{-a^2} (2 \right. \right. \right.$$

**7.245 ODE No. 1835**

$$\left( 2 \left( \frac{d^2}{dx^2} y(x) \right) y(x) - \left( \frac{d}{dx} y(x) \right)^2 \right)^3 + 32 \left( \frac{d^2}{dx^2} y(x) \right) \left( x \frac{d^2}{dx^2} y(x) - \frac{d}{dx} y(x) \right)^3 = 0$$

**Mathematica:** cpu = 0.114015 (sec), leaf count = 143

$$\left\{ \left\{ y(x) \rightarrow \frac{1}{4} \left( -\frac{8c_1^3}{\sqrt[3]{3} \sqrt[3]{\sqrt{3} \sqrt{27c_1^{10} c_2^{10} - 64c_1^9 c_2^9 - 9c_1^5 c_2^5}}} + \frac{c_1^2}{c_2} - \frac{2 \sqrt[3]{\sqrt{3} \sqrt{27c_1^{10} c_2^{10} - 64c_1^9 c_2^9 - 9c_1^5 c_2^5}}}{3^{2/3} c_2^3} \right) x^2 + \right. \right.$$

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

**7.246 ODE No. 1836**

$$\sqrt{a \left( \frac{d^2}{dx^2} y(x) \right)^2 + b \left( \frac{d}{dx} y(x) \right)^2} + cy(x) \frac{d^2}{dx^2} y(x) + d \left( \frac{d}{dx} y(x) \right)^2 = 0$$

**Mathematica:** cpu = 14.719369 (sec), leaf count = 44

$$\text{DSolve}\left[ \sqrt{ay''(x)^2 + by'(x)^2} + cy(x)y''(x) + dy'(x)^2 = 0, y(x), x \right]$$

**Maple:** cpu = 0.297 (sec), leaf count = 94

$$\left\{ y(x) = \text{ODESolStruc} \left( -a, \left[ \left( \frac{d}{d_a} b(-a) \right) - b(-a) + \frac{-b(-a)}{c^2 - a^2 - a} \left( -a cd - b(-a) - \sqrt{-a^2 bc^2 + (-b} \right. \right. \right.$$

## 8 Kamke chapter 7. Non-linear third and higher order

### 8.1 ODE No. 1837

$$\frac{d^3}{dx^3}y(x) - a^2 \left( \left( \frac{d}{dx}y(x) \right)^5 + 2 \left( \frac{d}{dx}y(x) \right)^3 + \frac{d}{dx}y(x) \right) = 0$$

**Mathematica:** cpu = 10.857379 (sec), leaf count = 35

$$\text{DSolve}[y^{(3)}(x) - a^2(y'(x)^5 + 2y'(x)^3 + y'(x)) = 0, y(x), x]$$

**Maple:** cpu = 0.265 (sec), leaf count = 95

$$\left\{ y(x) = \int \text{RootOf} \left( -3 \int^{-z} \frac{1}{\sqrt{3-f^6 a^2 + 9-f^4 a^2 + 9-f^2 a^2 + 9-C1}} d_f + x + C2 \right) dx + C3, y(x) \right.$$

### 8.2 ODE No. 1838

$$\frac{d^3}{dx^3}y(x) + \left( \frac{d^2}{dx^2}y(x) \right) y(x) - \left( \frac{d}{dx}y(x) \right)^2 + 1 = 0$$

**Mathematica:** cpu = 0.032504 (sec), leaf count = 27

$$\text{DSolve}[y^{(3)}(x) + y(x)y''(x) - y'(x)^2 + 1 = 0, y(x), x]$$

**Maple:** cpu = 0.453 (sec), leaf count = 73

$$\left\{ y(x) = \text{ODESolStruc} \left( -a, \left[ \left( \frac{d^2}{d_a^2} b(-a) \right) (-b(-a))^2 + \left( \frac{d}{d_a} b(-a) \right)^2 - b(-a) + \left( \frac{d}{d_a} b(-a) \right) \right] \right.$$

### 8.3 ODE No. 1839

$$\frac{d^3}{dx^3}y(x) - \left( \frac{d^2}{dx^2}y(x) \right) y(x) + \left( \frac{d}{dx}y(x) \right)^2 = 0$$

**Mathematica:** cpu = 0.030004 (sec), leaf count = 25

$$\text{DSolve}[y^{(3)}(x) - y(x)y''(x) + y'(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 0.655 (sec), leaf count = 127

$$\left\{ y(x) = ODESolStruc \left( e^{\int -g(\_f) d\_f + C2}, \left[ \left\{ \frac{d}{d\_f} -g(\_f) = (6\_f - 1) (\_g(\_f))^3 + \frac{(7\_f - 1) (\_g(\_f))}{\_f} \right. \right. \right. \right.$$

#### 8.4 ODE No. 1840

$$\frac{d^3}{dx^3}y(x) + ay(x) \frac{d^2}{dx^2}y(x) = 0$$

**Mathematica:** cpu = 0.026503 (sec), leaf count = 19

$$\text{DSolve}[ay(x)y''(x) + y^{(3)}(x) = 0, y(x), x]$$

**Maple:** cpu = 0.655 (sec), leaf count = 129

$$\left\{ y(x) = ODESolStruc \left( e^{\int -g(\_f) d\_f + C2}, \left[ \left\{ \frac{d}{d\_f} -g(\_f) = (6\_f + 2a) (\_g(\_f))^3 + \frac{(7\_f + a) (\_g(\_f))}{\_f} \right. \right. \right. \right.$$

#### 8.5 ODE No. 1841

$$x^2 \frac{d^3}{dx^3}y(x) + x \frac{d^2}{dx^2}y(x) + (2xy(x) - 1) \frac{d}{dx}y(x) + (y(x))^2 - f(x) = 0$$

**Mathematica:** cpu = 0.087511 (sec), leaf count = 41

$$\text{DSolve}[-f(x) + x^2y^{(3)}(x) + xy''(x) + (2xy(x) - 1)y'(x) + y(x)^2 = 0, y(x), x]$$

**Maple:** cpu = 0.406 (sec), leaf count = 60

$$\left\{ y(x) = ODESolStruc \left( \_b(\_a), \left[ \left\{ \_a^2 \frac{d^2}{d\_a^2} \_b(\_a) + \_a (\_b(\_a))^2 - \_a \frac{d}{d\_a} \_b(\_a) - \int f(\_a) d\_a \right. \right. \right. \right.$$



## 8.6 ODE No. 1842

$$x^2 \frac{d^3}{dx^3} y(x) + x(-1 + y(x)) \frac{d^2}{dx^2} y(x) + x \left( \frac{d}{dx} y(x) \right)^2 + (1 - y(x)) \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 0.166521 (sec), leaf count = 286

$$\left\{ \left\{ y(x) \rightarrow \frac{2x \left( c_3 \left( J_{\frac{\sqrt{c_2+2}}{\sqrt{2}}} \left( -\frac{1}{2} i x \sqrt{c_1} \right) - \frac{1}{4} i \sqrt{c_1} x \left( J_{\frac{\sqrt{c_2+2}}{\sqrt{2}}-1} \left( -\frac{1}{2} i x \sqrt{c_1} \right) - J_{\frac{\sqrt{c_2+2}}{\sqrt{2}}+1} \left( -\frac{1}{2} i x \sqrt{c_1} \right) \right) \right) + Y_{\frac{\sqrt{c_2}}{\sqrt{2}}}}{c_3 x J_{\frac{\sqrt{c_2+2}}{\sqrt{2}}} \left( -\frac{1}{2} i x \sqrt{c_1} \right) + x Y_{\frac{\sqrt{c_2+2}}{\sqrt{2}}}} \right. \right.$$

**Maple:** cpu = 0.421 (sec), leaf count = 190

$$\left\{ \ln(x) + 2 \int^{y(x)} \left( 2 \left( \text{RootOf} \left( -2 Y_{1/2 \sqrt{4+CI}} \left( 1/2 \sqrt{2} Z \right) \sqrt{4+CI} C2 + 2 Y_{1/2 \sqrt{4+CI}} \left( 1/2 \sqrt{2} Z \right) \right) \right. \right.$$

## 8.7 ODE No. 1843

$$y(x) \frac{d^3}{dx^3} y(x) - \left( \frac{d}{dx} y(x) \right) \frac{d^2}{dx^2} y(x) + (y(x))^3 \frac{d}{dx} y(x) = 0$$

**Mathematica:** cpu = 2.969877 (sec), leaf count = 409

$$\left\{ \left\{ y(x) \rightarrow \text{InverseFunction} \left[ \frac{2i \sqrt{\frac{\#1^2}{2(\sqrt{c_2^2-c_1-c_2})} + 1} \sqrt{1 - \frac{\#1^2}{2(c_2 + \sqrt{c_2^2-c_1})}} F \left( i \sinh^{-1} \left( \frac{\sqrt{\frac{1}{\sqrt{c_2^2-c_1-c_2}} \#1}}{\sqrt{2}} \right) \right) \frac{c_2}{c_2}}{\sqrt{\frac{1}{\sqrt{c_2^2-c_1-c_2}}} \sqrt{-\frac{\#1^4}{2} + 2\#1^2 c_2 - 2c_1}} \right] \right. \right.$$

**Maple:** cpu = 0.234 (sec), leaf count = 77

$$\left\{ \int^{y(x)} -2 \frac{1}{\sqrt{-a^4 + 4C2_a^2 - 4C2^2 + 4C1}} d_a - x - C3 = 0, \int^{y(x)} 2 \frac{1}{\sqrt{-a^4 + 4C2_a^2}}$$

## 8.8 ODE No. 1844

$$4(y(x))^2 \frac{d^3}{dx^3}y(x) - 18y(x) \left(\frac{d}{dx}y(x)\right) \frac{d^2}{dx^2}y(x) + 15 \left(\frac{d}{dx}y(x)\right)^3 = 0$$

**Mathematica:** cpu = 0.075010 (sec), leaf count = 37

$$\text{DSolve}[4y(x)^2 y^{(3)}(x) + 15y'(x)^3 - 18y(x)y'(x)y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.203 (sec), leaf count = 26

$$\left\{ y(x) = \frac{-C3}{(-C2^2 - 2C2x - x^2 + 4C1)^2} \right\}$$

## 8.9 ODE No. 1845

$$9(y(x))^2 \frac{d^3}{dx^3}y(x) - 45y(x) \left(\frac{d}{dx}y(x)\right) \frac{d^2}{dx^2}y(x) + 40 \left(\frac{d}{dx}y(x)\right)^3 = 0$$

**Mathematica:** cpu = 0.074009 (sec), leaf count = 37

$$\text{DSolve}[9y(x)^2 y^{(3)}(x) + 40y'(x)^3 - 45y(x)y'(x)y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.187 (sec), leaf count = 22

$$\left\{ y(x) = -C3(-C2^2 + 2C2x + x^2 - 9C1)^{-\frac{3}{2}} \right\}$$

## 8.10 ODE No. 1846

$$2 \left(\frac{d}{dx}y(x)\right) \frac{d^3}{dx^3}y(x) - 3 \left(\frac{d}{dx}y(x)\right)^2 = 0$$

**Mathematica:** cpu = 0.040505 (sec), leaf count = 51

$$\left\{ \{y(x) \rightarrow c_1\}, \left\{ y(x) \rightarrow \sqrt{\frac{2}{3}} e^{-\sqrt{\frac{3}{2}}x} (c_1 e^{\sqrt{6}x} - c_2) + c_3 \right\} \right\}$$

**Maple:** cpu = 0.0 (sec), leaf count = 28

$$\left\{ y(x) = -C1, y(x) = -C1 + -C2 e^{\frac{\sqrt{6}x}{2}} + -C3 e^{-\frac{\sqrt{6}x}{2}} \right\}$$

### 8.11 ODE No. 1847

$$\left( \left( \frac{d}{dx} y(x) \right)^2 + 1 \right) \frac{d^3}{dx^3} y(x) - 3 \left( \frac{d}{dx} y(x) \right) \left( \frac{d^2}{dx^2} y(x) \right)^2 = 0$$

**Mathematica:** cpu = 0.124016 (sec), leaf count = 95

$$\left\{ \left\{ y(x) \rightarrow c_3 - \frac{i \sqrt{c_1^2 x^2 + 2c_2 c_1^2 x + c_2^2 c_1^2 - 1}}{c_1} \right\}, \left\{ y(x) \rightarrow c_3 + \frac{i \sqrt{c_1^2 x^2 + 2c_2 c_1^2 x + c_2^2 c_1^2 - 1}}{c_1} \right\} \right\}$$

**Maple:** cpu = 0.171 (sec), leaf count = 49

$$\left\{ y(x) = -\sqrt{-C2^2 - 2C2x - x^2 + C1} + C3, y(x) = \sqrt{-C2^2 - 2C2x - x^2 + C1} + C3 \right\}$$

### 8.12 ODE No. 1848

$$\left( \left( \frac{d}{dx} y(x) \right)^2 + 1 \right) \frac{d^3}{dx^3} y(x) - \left( 3 \frac{d}{dx} y(x) + a \right) \left( \frac{d^2}{dx^2} y(x) \right)^2 = 0$$

**Mathematica:** cpu = 594.052935 (sec), leaf count = 37

$$\text{DSolve}[y''(x)^2 (-a - 3y'(x)) + y^{(3)}(x) (y'(x)^2 + 1) = 0, y(x), x]$$

**Maple:** cpu = 0.843 (sec), leaf count = 789

$$\left\{ y(x) = \int \frac{\sin(\text{RootOf}(e^{2-Za} C1^2 C2^2 a^4 + 2e^{2-Za} C1^2 C2 a^4 x + e^{2-Za} C1^2 a^4 x^2 + 2e^{2-Za} C1))}{\cos(\text{RootOf}(e^{2-Za} C1^2 C2^2 a^4 + 2e^{2-Za} C1^2 C2 a^4 x + e^{2-Za} C1^2 a^4 x^2 + 2e^{2-Za} C1))} dx \right\}$$

### 8.13 ODE No. 1849

$$\left( \frac{d^2}{dx^2} y(x) \right) \frac{d^3}{dx^3} y(x) - a \sqrt{b^2 \left( \frac{d^2}{dx^2} y(x) \right)^2 + 1} = 0$$

**Mathematica:** cpu = 0.591575 (sec), leaf count = 426

$$\left\{ \left\{ y(x) \rightarrow \frac{\frac{(a^2 b^4 x^2 + 2ab^4 c_1 x + b^4 c_1^2 - 1)^{3/2}}{3ab^2} + \frac{\sqrt{a^2 b^4 x^2 + 2ab^4 c_1 x + b^4 c_1^2 - 1}}{ab^2} - \frac{c_1 \log(\sqrt{a^2 b^4 x^2 + 2ab^4 c_1 x + b^4 c_1^2 - 1} + ab^2 x + b^2 c_1)}{a}}{2ab^3} - x \right\} \right\}$$

**Maple:** cpu = 0.125 (sec), leaf count = 337

$$\left\{ y(x) = \int -\frac{x}{2b} \sqrt{-C1^2 a^2 b^4 + 2C1 a^2 b^4 x + a^2 b^4 x^2 - 1} - \frac{C1}{2b} \sqrt{-C1^2 a^2 b^4 + 2C1 a^2 b^4 x + a^2 b^4 x^2 - 1} dx \right\}$$

### 8.14 ODE No. 1850

$$\left(\frac{d}{dx}y(x)\right) d^4y(x) - \left(\frac{d^2}{dx^2}y(x)\right) \frac{d^3}{dx^3}y(x) + \left(\frac{d}{dx}y(x)\right)^3 \frac{d^3}{dx^3}y(x) = 0$$

**Mathematica:** cpu = 0.083511 (sec), leaf count = 37

$$\text{DSolve}[y^{(4)}(x)y'(x) - y^{(3)}(x)y''(x) + y^{(3)}(x)y'(x)^3 = 0, y(x), x]$$

**Maple:** cpu = 1.092 (sec), leaf count = 165

$$\left\{ y(x) = \text{ODESolStruc} \left( \int \frac{-j(-h)}{e^{f(-h)} d_{-h} + C2} d_{-h} + C3, \left[ \left\{ \frac{d}{d_{-h}} j(-h) = (12_{-h} + 3) (j(-h))^3 + \dots \right. \right. \right. \right.$$

### 8.15 ODE No. 1851

$$\left(\frac{d}{dx}y(x)\right) \left( \left(\frac{d^3}{dx^3}f(x)\right) \frac{d}{dx}y(x) + 3 \left(\frac{d^2}{dx^2}f(x)\right) \frac{d^2}{dx^2}y(x) + 3 \left(\frac{d}{dx}f(x)\right) \frac{d^3}{dx^3}y(x) + f(x) \frac{d^4}{dx^4}y(x) \right) -$$

**Mathematica:** cpu = 0.806102 (sec), leaf count = 141

$$\text{DSolve}[y'(x)^3 (f'(x)y'(x) + f(x)y''(x)) - y''(x) (f''(x)y'(x) + 2f'(x)y''(x) + f(x)y^{(3)}(x)) + y'(x) (f^{(3)}(x) + \dots)]$$

**Maple:** cpu = 2.589 (sec), leaf count = 0

could not solve

### 8.16 ODE No. 1852

$$3 \left(\frac{d^2}{dx^2}y(x)\right) d^4y(x) - 5 \left(\frac{d^3}{dx^3}y(x)\right)^2 = 0$$

**Mathematica:** cpu = 0.036505 (sec), leaf count = 28

$$\left\{ \left\{ y(x) \rightarrow c_2(-\sqrt{3c_1 + 2x}) + c_4x + c_3 \right\} \right\}$$

**Maple:** cpu = 0.203 (sec), leaf count = 30

$$\left\{ y(x) = 3(-C2 + x) \sqrt{6} C1^2 \sqrt{-\frac{-C1}{-C2 + x} + C3} x + C4 \right\}$$

**8.17 ODE No. 1853**

$$9 \left( \frac{d^2}{dx^2} y(x) \right)^2 \frac{d^5}{dx^5} y(x) - 45 \left( \frac{d^2}{dx^2} y(x) \right) \left( \frac{d^3}{dx^3} y(x) \right) \frac{d^4}{dx^4} y(x) + 40 \frac{d^3}{dx^3} y(x) = 0$$

**Mathematica:** cpu = 0.074009 (sec), leaf count = 41

$$\text{DSolve}[40y^{(3)}(x)^3 + 9y^{(5)}(x)y''(x)^2 - 45y^{(4)}(x)y^{(3)}(x)y''(x) = 0, y(x), x]$$

**Maple:** cpu = 0.515 (sec), leaf count = 110

$$\left\{ y(x) = \iint \text{RootOf} \left( - \int^{-Z} \left( \text{RootOf} \left( -20 \ln(\_f) + \int^{-Z} \_k \left( e^{\text{RootOf}(81\_k^2 e^{-Z} + 20 e^{-Z} \ln(e^{-Z} + 27)) - 40 e^{-Z} \ln(\_f)} \right) \right) \right) \right) \right.$$

**8.18 ODE No. 1854**

$$\frac{d^n}{dx^n} y(x) - f \left( \frac{d^{n-1}}{dx^{n-1}} y(x) \right) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 1

not solved

**Maple:** cpu = 0.515 (sec), leaf count = 0

could not solve

**8.19 ODE No. 1855**

$$\frac{d^n}{dx^n} y(x) = f \left( \frac{d^{n-2}}{dx^{n-2}} y(x) \right) = 0$$

**Mathematica:** cpu = 0 (sec), leaf count = 1

not solved

**Maple:** cpu = 0.515 (sec), leaf count = 0

could not solve

## 9 Kamke chapter 8. System of linear differential equations

### 9.1 ODE No. 1856

$$\left\{ \frac{d}{dt}x(t) = ax(t), \frac{d}{dt}y(t) = b \right\}$$

**Mathematica:** cpu = 0.005001 (sec), leaf count = 22

$$\left\{ \left\{ x(t) \rightarrow c_1 e^{at}, y(t) \rightarrow bt + c_2 \right\} \right\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 19

$$\left\{ \left\{ x(t) = \_C1 e^{at}, y(t) = bt + \_C2 \right\} \right\}$$

### 9.2 ODE No. 1857

$$\left\{ \frac{d}{dt}x(t) = ay(t), \frac{d}{dt}y(t) = -ax(t) \right\}$$

**Mathematica:** cpu = 0.039505 (sec), leaf count = 39

$$\left\{ \left\{ x(t) \rightarrow c_2 \sin(at) + c_1 \cos(at), y(t) \rightarrow c_2 \cos(at) - c_1 \sin(at) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 35

$$\left\{ \left\{ x(t) = \_C1 \sin(at) + \_C2 \cos(at), y(t) = \cos(at) \_C1 - \sin(at) \_C2 \right\} \right\}$$

### 9.3 ODE No. 1858

$$\left\{ \frac{d}{dt}x(t) = ay(t), \frac{d}{dt}y(t) = bx(t) \right\}$$

**Mathematica:** cpu = 0.010501 (sec), leaf count = 182

$$\left\{ \left\{ x(t) \rightarrow \frac{1}{2} c_1 e^{-\sqrt{a}\sqrt{bt}} \left( e^{2\sqrt{a}\sqrt{bt}} + 1 \right) + \frac{\sqrt{a} c_2 e^{-\sqrt{a}\sqrt{bt}} \left( e^{2\sqrt{a}\sqrt{bt}} - 1 \right)}{2\sqrt{b}}, y(t) \rightarrow \frac{\sqrt{b} c_1 e^{-\sqrt{a}\sqrt{bt}} \left( e^{2\sqrt{a}\sqrt{bt}} - 1 \right)}{2\sqrt{a}} + \dots \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 64

$$\left\{ \left\{ x(t) = \_C1 e^{\sqrt{a}\sqrt{bt}} + \_C2 e^{-\sqrt{a}\sqrt{bt}}, y(t) = 1\sqrt{b} \left( \_C1 e^{\sqrt{a}\sqrt{bt}} - \_C2 e^{-\sqrt{a}\sqrt{bt}} \right) \frac{1}{\sqrt{a}} \right\} \right\}$$

## 9.4 ODE No. 1859

$$\left\{ \frac{d}{dt}x(t) = ax(t) - y(t), \frac{d}{dt}y(t) = x(t) + ay(t) \right\}$$

**Mathematica:** cpu = 0.005001 (sec), leaf count = 51

$$\left\{ \left\{ x(t) \rightarrow c_1 e^{at} \cos(t) - c_2 e^{at} \sin(t), y(t) \rightarrow c_1 e^{at} \sin(t) + c_2 e^{at} \cos(t) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 37

$$\left\{ \left\{ x(t) = e^{at} (_C1 \sin(t) + _C2 \cos(t)), y(t) = e^{at} (\sin(t) _C2 - \cos(t) _C1) \right\} \right\}$$

## 9.5 ODE No. 1860

$$\left\{ \frac{d}{dt}x(t) = ax(t) + by(t), \frac{d}{dt}y(t) = cx(t) + by(t) \right\}$$

**Mathematica:** cpu = 0.045506 (sec), leaf count = 696

$$\left\{ \left\{ x(t) \rightarrow \frac{c_1 \left( a \left( -e^{\frac{1}{2}t(-\sqrt{a^2-2ab+b^2+4bc+a+b})} \right) + a e^{\frac{1}{2}t(\sqrt{a^2-2ab+b^2+4bc+a+b})} + b e^{\frac{1}{2}t(-\sqrt{a^2-2ab+b^2+4bc+a+b})} + \dots \right)}{\dots} \right\} \right\}$$

**Maple:** cpu = 0.046 (sec), leaf count = 237

$$\left\{ \left\{ x(t) = _C1 e^{\frac{t}{2}(a+b+\sqrt{a^2-2ab+b^2+4bc})} + _C2 e^{-\frac{t}{2}(-a-b+\sqrt{a^2-2ab+b^2+4bc})}, y(t) = \left( \frac{1}{2} + \frac{1}{b} \left( \frac{1}{2} \sqrt{a^2-2ab+b^2+4bc} \right) \right) \dots \right\} \right\}$$

## 9.6 ODE No. 1861

$$\left\{ a \frac{d}{dt}x(t) + b \frac{d}{dt}y(t) = \alpha x(t) + \beta y(t), b \frac{d}{dt}x(t) - a \frac{d}{dt}y(t) = \beta x(t) - \alpha y(t) \right\}$$

**Mathematica:** cpu = 0.011001 (sec), leaf count = 183

$$\left\{ \left\{ x(t) \rightarrow c_2 e^{\frac{t(a\alpha+b\beta)}{a^2+b^2}} \sin\left(\frac{t(a\beta-\alpha b)}{a^2+b^2}\right) + c_1 e^{\frac{t(a\alpha+b\beta)}{a^2+b^2}} \cos\left(\frac{t(a\beta-\alpha b)}{a^2+b^2}\right), y(t) \rightarrow c_2 e^{\frac{t(a\alpha+b\beta)}{a^2+b^2}} \cos\left(\frac{t(a\beta-\alpha b)}{a^2+b^2}\right) \dots \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 144

$$\left\{ \left\{ x(t) = _C1 e^{\frac{(i a \beta - i \alpha b + a \alpha + \beta b) t}{a^2 + b^2}} + _C2 e^{-\frac{(i a \beta - i \alpha b - a \alpha - \beta b) t}{a^2 + b^2}}, y(t) = i \left( _C1 e^{\frac{(i a \beta - i \alpha b + a \alpha + \beta b) t}{a^2 + b^2}} - _C2 e^{-\frac{(i a \beta - i \alpha b - a \alpha - \beta b) t}{a^2 + b^2}} \right) \dots \right\} \right\}$$

## 9.7 ODE No. 1862

$$\left\{ \frac{d}{dt}x(t) = -y(t), \frac{d}{dt}y(t) = 2x(t) + 2y(t) \right\}$$

**Mathematica:** cpu = 0.042005 (sec), leaf count = 52

$$\left\{ \left\{ x(t) \rightarrow c_1 e^t (\cos(t) - \sin(t)) - c_2 e^t \sin(t), y(t) \rightarrow 2c_1 e^t \sin(t) + c_2 e^t (\sin(t) + \cos(t)) \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 42

$$\left\{ \left\{ x(t) = e^t (\sin(t) \_C1 + \cos(t) \_C2), y(t) = -e^t (\sin(t) \_C1 - \sin(t) \_C2 + \cos(t) \_C1 + \cos(t) \_C2) \right\} \right\}$$

## 9.8 ODE No. 1863

$$\left\{ \frac{d}{dt}x(t) + 3x(t) + 4y(t) = 0, \frac{d}{dt}y(t) + 2x(t) + 5y(t) = 0 \right\}$$

**Mathematica:** cpu = 0.007001 (sec), leaf count = 84

$$\left\{ \left\{ x(t) \rightarrow \frac{1}{3}c_1 e^{-7t} (2e^{6t} + 1) - \frac{2}{3}c_2 e^{-7t} (e^{6t} - 1), y(t) \rightarrow \frac{1}{3}c_2 e^{-7t} (e^{6t} + 2) - \frac{1}{3}c_1 e^{-7t} (e^{6t} - 1) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 35

$$\left\{ \left\{ x(t) = \_C1 e^{-t} + \_C2 e^{-7t}, y(t) = -\frac{C1 e^{-t}}{2} + \_C2 e^{-7t} \right\} \right\}$$

## 9.9 ODE No. 1864

$$\left\{ \frac{d}{dt}x(t) = -5x(t) - 2y(t), \frac{d}{dt}y(t) = x(t) - 7y(t) \right\}$$

**Mathematica:** cpu = 0.013002 (sec), leaf count = 59

$$\left\{ \left\{ x(t) \rightarrow c_1 e^{-6t} (\sin(t) + \cos(t)) - 2c_2 e^{-6t} \sin(t), y(t) \rightarrow c_1 e^{-6t} \sin(t) + c_2 e^{-6t} (\cos(t) - \sin(t)) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 46

$$\left\{ \left\{ x(t) = e^{-6t} (\sin(t) \_C1 + \cos(t) \_C2), y(t) = \frac{e^{-6t} (\sin(t) \_C1 + \sin(t) \_C2 - \cos(t) \_C1 + \cos(t) \_C2)}{2} \right\} \right\}$$



### 9.10 ODE No. 1865

$$\left\{ \frac{d}{dt}x(t) = a1 x(t) + b1 y(t) + c1, \frac{d}{dt}y(t) = a2 x(t) + b2 y(t) + c2 \right\}$$

**Mathematica:** cpu = 1.201653 (sec), leaf count = 2062

$$\left\{ \left\{ x(t) \rightarrow -\frac{b1 e^{-\frac{1}{2}(a1+b2+\sqrt{a1^2-2b2a1+b2^2+4a2b1})} t \left( \frac{2((a1-b2+\sqrt{a1^2-2b2a1+b2^2+4a2b1})c2-2a2c1) e^{\sqrt{a1^2-2b2a1+b2^2+4a2b1}}}{-a1-b2+\sqrt{a1^2-2b2a1+b2^2+4a2b1}} \right) + \frac{c2}{a1} \right\}}{2(a1-b2+\sqrt{a1^2-2b2a1+b2^2+4a2b1})} \right\}$$

**Maple:** cpu = 0.172 (sec), leaf count = 334

$$\left\{ \left\{ x(t) = e^{\left(\frac{a1}{2} + \frac{b2}{2} + \frac{1}{2}\sqrt{a1^2 - 2a1b2 + 4a2b1 + b2^2}\right)t} \_C2 + e^{\left(\frac{a1}{2} + \frac{b2}{2} - \frac{1}{2}\sqrt{a1^2 - 2a1b2 + 4a2b1 + b2^2}\right)t} \_C1 + \frac{c2 b1 - b2}{a1 b2 - a2} \right\} \right\}$$

### 9.11 ODE No. 1866

$$\left\{ \frac{d}{dt}x(t) + 2y(t) = 3t, \frac{d}{dt}y(t) - 2x(t) = 4 \right\}$$

**Mathematica:** cpu = 0.027003 (sec), leaf count = 132

$$\left\{ \left\{ x(t) \rightarrow -c2 \sin(2t) + c1 \cos(2t) + \cos(2t) \left( \frac{3}{2}t \sin(2t) - \frac{5}{4} \cos(2t) \right) - \sin(2t) \left( \frac{5}{4} \sin(2t) + \frac{3}{2}t \cos(2t) \right) \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 39

$$\left\{ \left\{ x(t) = \sin(2t) \_C2 + \cos(2t) \_C1 - \frac{5}{4}, y(t) = -\cos(2t) \_C2 + \sin(2t) \_C1 + \frac{3t}{2} \right\} \right\}$$

### 9.12 ODE No. 1867

$$\left\{ \frac{d}{dt}y(t) - x(t) = -3t^2 + 3t + 1, \frac{d}{dt}x(t) + y(t) - t^2 + 6t + 1 = 0 \right\}$$

**Mathematica:** cpu = 0.075510 (sec), leaf count = 124

$$\left\{ \left\{ x(t) \rightarrow -c2 \sin(t) + c1 \cos(t) + \cos(t) ((3t^2 - t - 13) \cos(t) + (t - 12)t \sin(t)) - \sin(t) ((-3t^2 + t + 13) \cos(t) + (t - 12)t \sin(t)) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 42

$$\left\{ \left\{ x(t) = \sin(t) \_C2 + \cos(t) \_C1 + 3t^2 - t - 13, y(t) = t^2 - \cos(t) \_C2 + \sin(t) \_C1 - 12t \right\} \right\}$$

### 9.13 ODE No. 1868

$$\left\{ \frac{d}{dt}x(t) + 3x(t) - y(t) = e^{2t}, \frac{d}{dt}y(t) + x(t) + 5y(t) = e^t \right\}$$

**Mathematica:** cpu = 0.046006 (sec), leaf count = 162

$$\left\{ \left\{ x(t) \rightarrow c_1 e^{-4t}(t+1) + c_2 e^{-4t}t - e^t(t+1) \left( \frac{t}{5} + \frac{1}{36}e^t(6t-7) - \frac{1}{25} \right) + e^t t \left( \frac{t}{5} + \frac{1}{36}e^t(6t-1) + \frac{4}{25} \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 64

$$\left\{ \left\{ x(t) = e^{-4t} \_C2 + e^{-4t}t \_C1 + \frac{7e^{2t}}{36} + \frac{e^t}{25}, y(t) = -\frac{e^{2t}}{36} - e^{-4t} \_C2 - e^{-4t}t \_C1 + e^{-4t} \_C1 + \frac{4e^t}{25} \right\} \right\}$$

### 9.14 ODE No. 1869

$$\left\{ \frac{d}{dt}x(t) + \frac{d}{dt}y(t) - x(t) + 3y(t) = e^t - 1, \frac{d}{dt}x(t) + \frac{d}{dt}y(t) + 2x(t) + y(t) = e^{2t} + t \right\}$$

**Mathematica:** cpu = 0.087511 (sec), leaf count = 118

$$\left\{ \left\{ x(t) \rightarrow \frac{5}{72} \left( c_1 e^{-7t/5} + \frac{12(5712t + 833e^t + 2352e^{2t} - 5508)}{20825} \right) + \frac{1}{5}(t - e^t + e^{2t} + 1), y(t) \rightarrow \frac{5}{48} \left( c_1 e^{-7t/5} \right) \right\} \right\}$$

**Maple:** cpu = 0.031 (sec), leaf count = 51

$$\left\{ \left\{ x(t) = \frac{5e^{2t}}{17} - \frac{e^t}{6} + \frac{3t}{7} - \frac{1}{49} + e^{-\frac{7t}{5}} \_C1, y(t) = -\frac{e^{2t}}{17} + \frac{e^t}{4} + \frac{t}{7} - \frac{26}{49} + \frac{3\_C1}{2} e^{-\frac{7t}{5}} \right\} \right\}$$

### 9.15 ODE No. 1870

$$\left\{ \frac{d}{dt}x(t) + \frac{d}{dt}y(t) - y(t) = e^t, 2 \frac{d}{dt}x(t) + \frac{d}{dt}y(t) + 2y(t) = \cos(t) \right\}$$

**Mathematica:** cpu = 0.127016 (sec), leaf count = 122

$$\left\{ \left\{ x(t) \rightarrow -\frac{3}{4}c_2(e^{4t} - 1) + c_1 + \frac{1}{68}e^{-4t}(e^{4t} - 1)(34e^t + 3\sin(t) - 12\cos(t)) + \frac{1}{4} \left( 2e^{-3t} + 2e^t + \frac{3}{17}e^{-4t} \right) \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 47

$$\left\{ \left\{ x(t) = e^t + \frac{5\sin(t)}{17} - \frac{3\cos(t)}{17} + \frac{e^{4t} \_C1}{4} + \_C2, y(t) = -\frac{2e^t}{3} + \frac{4\cos(t)}{17} - \frac{\sin(t)}{17} - \frac{e^{4t} \_C1}{3} \right\} \right\}$$

## 9.16 ODE No. 1871

$$\left\{ 3 \frac{d}{dt} x(t) + 7 \frac{d}{dt} y(t) + x(t) + 24 y(t) = 3, 4 \frac{d}{dt} x(t) + 9 \frac{d}{dt} y(t) + 2 x(t) + 31 y(t) = e^t \right\}$$

**Mathematica:** cpu = 0.161521 (sec), leaf count = 180

$$\left\{ \left\{ x(t) \rightarrow -c_2 e^{-4t} \sin(t) + c_1 e^{-4t} (\cos(t) - \sin(t)) + \frac{1}{442} (3(153e^t - 754) \sin(t) + 31(17e^t - 78) \cos(t)) \right\} \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 71

$$\left\{ \left\{ x(t) = e^{-4t} \sin(t) \_C2 + e^{-4t} \cos(t) \_C1 - \frac{93}{17} + \frac{31 e^t}{26}, y(t) = -e^{-4t} \sin(t) \_C2 - e^{-4t} \cos(t) \_C2 \right\} \right.$$

## 9.17 ODE No. 1872

$$\left\{ 3 \frac{d}{dt} x(t) + 7 \frac{d}{dt} y(t) + 8 x(t) + 24 y(t) = e^{2t}, 4 \frac{d}{dt} x(t) + 9 \frac{d}{dt} y(t) + 11 x(t) + 31 y(t) = e^t \right\}$$

**Mathematica:** cpu = 0.059508 (sec), leaf count = 162

$$\left\{ \left\{ x(t) \rightarrow -c_1 e^{-4t} (t - 1) - c_2 e^{-4t} t - e^t t \left( -\frac{4t}{5} + \frac{1}{36} e^t (30t + 19) - \frac{11}{25} \right) - e^t (t - 1) \left( \frac{4t}{5} - \frac{1}{36} e^t (30t + 49) \right) \right\} \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 65

$$\left\{ \left\{ x(t) = e^{-4t} \_C2 + e^{-4t} t \_C1 - \frac{49 e^{2t}}{36} + \frac{31 e^t}{25}, y(t) = \frac{19 e^{2t}}{36} - e^{-4t} \_C2 - e^{-4t} t \_C1 - e^{-4t} \_C1 - 1 \right\} \right.$$

## 9.18 ODE No. 1873

$$\left\{ 3 \frac{d}{dt} x(t) + 7 \frac{d}{dt} y(t) + 34 x(t) + 38 y(t) = e^t, 4 \frac{d}{dt} x(t) + 9 \frac{d}{dt} y(t) + 44 x(t) + 49 y(t) = t \right\}$$

**Mathematica:** cpu = 0.045006 (sec), leaf count = 322

$$\left\{ \left\{ x(t) \rightarrow \frac{1}{5} c_1 e^{-6t} (4e^{5t} + 1) - \frac{1}{5} c_2 e^{-6t} (e^{5t} - 1) - \frac{1}{5} e^{-6t} (e^{5t} - 1) \left( \frac{16}{5} e^{6t} \left( \frac{t}{6} - \frac{1}{36} \right) + 4e^{2t} - \frac{4e^{7t}}{7} - \frac{31}{5} e^t \right) \right\} \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 52

$$\left\{ \left\{ x(t) = e^{-6t} \_C2 + \_C1 e^{-t} - \frac{56}{9} + \frac{19t}{3} - \frac{29 e^t}{7}, y(t) = 4e^{-6t} \_C2 - \_C1 e^{-t} + \frac{55}{9} + \frac{24 e^t}{7} - \frac{17t}{3} \right\} \right.$$

## 9.19 ODE No. 1874

$$\left\{ \frac{d}{dt}x(t) = x(t)f(t) + y(t)g(t), \frac{d}{dt}y(t) = -x(t)g(t) + y(t)f(t) \right\}$$

**Mathematica:** cpu = 0.062508 (sec), leaf count = 107

$$\left\{ \left\{ x(t) \rightarrow c_2 e^{\int_1^t f(K[2]) dK[2]} \sin \left( \int_1^t g(K[1]) dK[1] \right) + c_1 e^{\int_1^t f(K[2]) dK[2]} \cos \left( \int_1^t g(K[1]) dK[1] \right), y(t) \rightarrow c_2 \right. \right.$$

**Maple:** cpu = 0.296 (sec), leaf count = 57

$$\left\{ \left\{ x(t) = e^{\int \tan(-C1 - \int g(t) dt) g(t) + f(t) dt} \_C2, y(t) = \tan \left( -C1 - \int g(t) dt \right) e^{\int \tan(-C1 - \int g(t) dt) g(t) + f(t) dt} \_C2 \right. \right.$$

## 9.20 ODE No. 1875

$$\left\{ \frac{d}{dt}x(t) + (ax(t) + by(t))f(t) = g(t), \frac{d}{dt}y(t) + (cx(t) + dy(t))f(t) = h(t) \right\}$$

**Mathematica:** cpu = 0.007001 (sec), leaf count = 48

$$\text{DSolve}[\{f(t)(ax(t) + by(t)) + x'(t) = g(t), f(t)(cx(t) + dy(t)) + y'(t) = h(t)\}, \{x(t), y(t)\}, t]$$

**Maple:** cpu = 0.670 (sec), leaf count = 1633

$$\left\{ \left\{ x(t) = 1 \left( e^{\frac{1}{2da-2bc} \left( \sqrt{\frac{-a^2+2da-4bc-d^2}{da-bc}} (da-bc) + (a+d)\sqrt{-da+bc} \right) \int f(t)\sqrt{-da+bc} dt} \_C2 \sqrt{\frac{a^2 - 2da + 4bc + d^2}{da - bc}} \sqrt{-} \right. \right.$$

## 9.21 ODE No. 1876

$$\left\{ \frac{d}{dt}x(t) = x(t) \cos(t), \frac{d}{dt}y(t) = x(t) e^{-\sin(t)} \right\}$$

**Mathematica:** cpu = 0.074510 (sec), leaf count = 38

$$\left\{ \left\{ x(t) \rightarrow c_1 e^{\sin(t)}, y(t) \rightarrow c_1 \int_1^t e^{\sin(K[1]) - \sin(K[1])} dK[1] + c_2 \right\} \right\}$$

**Maple:** cpu = 0.093 (sec), leaf count = 18

$$\left\{ \left\{ x(t) = \_C2 e^{\sin(t)}, y(t) = t \_C2 + \_C1 \right\} \right\}$$

## 9.22 ODE No. 1877

$$\left\{ t \frac{d}{dt} x(t) + y(t) = 0, t \frac{d}{dt} y(t) + x(t) = 0 \right\}$$

**Mathematica:** cpu = 0.005001 (sec), leaf count = 31

$$\left\{ \left\{ x(t) \rightarrow c_1 t + \frac{c_2}{t}, y(t) \rightarrow \frac{c_2}{t} - c_1 t \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 31

$$\left\{ \left\{ x(t) = \frac{-C2 t^2 + _C1}{t}, y(t) = \frac{-C2 t^2 + _C1}{t} \right\} \right\}$$

## 9.23 ODE No. 1878

$$\left\{ t \frac{d}{dt} x(t) + 2x(t) = t, t \frac{d}{dt} y(t) - (t+2)x(t) - ty(t) = -t \right\}$$

**Mathematica:** cpu = 0.012502 (sec), leaf count = 39

$$\left\{ \left\{ x(t) \rightarrow \frac{c_1}{t^2} + \frac{t}{3}, y(t) \rightarrow -\frac{c_1}{t^2} + c_2 e^t - \frac{t}{3} \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 39

$$\left\{ \left\{ x(t) = \frac{t}{3} + \frac{-C2}{t^2}, y(t) = \frac{3 _C1 e^{t^2} - t^3 - 3 _C2}{3 t^2} \right\} \right\}$$

## 9.24 ODE No. 1879

$$\left\{ t \frac{d}{dt} x(t) + 2x(t) - 2y(t) = t, t \frac{d}{dt} y(t) + x(t) + 5y(t) = t^2 \right\}$$

**Mathematica:** cpu = 0.057507 (sec), leaf count = 58

$$\left\{ \left\{ x(t) \rightarrow \frac{c_1}{t^4} + \frac{c_2}{t^3} + \frac{1}{30} t(2t+9), y(t) \rightarrow -\frac{c_1}{t^4} - \frac{c_2}{2t^3} + \frac{1}{60} t(8t-3) \right\} \right\}$$

**Maple:** cpu = 0.046 (sec), leaf count = 54

$$\left\{ \left\{ x(t) = \frac{2t^6 + 9t^5 + 30t _C2 + 30 _C1}{30t^4}, y(t) = -\frac{-8t^6 + 3t^5 + 30t _C2 + 60 _C1}{60t^4} \right\} \right\}$$

## 9.25 ODE No. 1880

$$\left\{ t^2(1 - \sin(t)) \frac{d}{dt}x(t) = t(1 - 2 \sin(t))x(t) + t^2y(t), t^2(1 - \sin(t)) \frac{d}{dt}y(t) = (t \cos(t) - \sin(t))x(t) + ty(t) \right\}$$

**Mathematica:** cpu = 0.021503 (sec), leaf count = 79

DSolve[{t^2(1 - sin(t))x'(t) = t^2y(t) + tx(t)(1 - 2 sin(t)), t^2(1 - sin(t))y'(t) = x(t)(t cos(t) - sin(t)) + ty(t)}

**Maple:** cpu = 0 (sec), leaf count = 0

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## 9.26 ODE No. 1881

$$\left\{ \frac{d}{dt}x(t) + \frac{d}{dt}y(t) + y(t) = f(t), \frac{d^2}{dt^2}x(t) + \frac{d^2}{dt^2}y(t) + \frac{d}{dt}y(t) + x(t) + y(t) = g(t) \right\}$$

**Mathematica:** cpu = 0.058507 (sec), leaf count = 44

$$\{\{x(t) \rightarrow -f''(t) - f'(t) - f(t) + g'(t) + g(t), y(t) \rightarrow f''(t) + f(t) - g'(t)\}\}$$

**Maple:** cpu = 0.015 (sec), leaf count = 48

$$\left\{ \left\{ x(t) = -\frac{d}{dt}f(t) + g(t) - f(t) - \frac{d^2}{dt^2}f(t) + \frac{d}{dt}g(t), y(t) = f(t) + \frac{d^2}{dt^2}f(t) - \frac{d}{dt}g(t) \right\} \right\}$$

## 9.27 ODE No. 1882

$$\left\{ \frac{d^2}{dt^2}x(t) + \frac{d}{dt}y(t) - 2y(t) = e^{2t}, 2 \frac{d}{dt}x(t) + \frac{d}{dt}y(t) - 3x(t) = 0 \right\}$$

**Mathematica:** cpu = 0.419553 (sec), leaf count = 928

$$\left\{ \left\{ x(t) \rightarrow \frac{1}{46}e^{t/2}c_1 \left( 23 \cos \left( \frac{\sqrt{23}t}{2} \right) + 23e^{t/2} - 3\sqrt{23} \sin \left( \frac{\sqrt{23}t}{2} \right) \right) + \frac{e^{3t/2} \left( 23e^{t/2} \cos \left( \frac{\sqrt{23}t}{2} \right) - 7\sqrt{23}e^{t/2} \right)}{46} \right. \right.$$

**Maple:** cpu = 0.047 (sec), leaf count = 118

$$\left\{ \left\{ x(t) = \frac{e^{2t}}{4} + \_C1 e^t + \_C2 e^{\frac{t}{2}} \cos \left( \frac{\sqrt{23}t}{2} \right) + \_C3 e^{\frac{t}{2}} \sin \left( \frac{\sqrt{23}t}{2} \right), y(t) = -\frac{e^{2t}}{8} + \_C1 e^t - \frac{7\_C2}{4} \right. \right.$$

## 9.28 ODE No. 1883

$$\left\{ \frac{d}{dt}x(t) - \frac{d}{dt}y(t) + x(t) = 2t, \frac{d^2}{dt^2}x(t) + \frac{d}{dt}y(t) - 9x(t) + 3y(t) = \sin(2t) \right\}$$

**Mathematica:** cpu = 0.590075 (sec), leaf count = 614

$$\left\{ \left\{ x(t) \rightarrow \frac{1}{16}c_1e^{-3t}(20e^{4t}t + 7e^{4t} + 9) + \frac{1}{16}c_2e^{-3t}(4e^{4t}t + 3e^{4t} - 3) - \frac{3}{16}c_3e^{-3t}(4e^{4t}t - e^{4t} + 1) + \frac{e^{-4t}(2}{16} \right. \right.$$

**Maple:** cpu = 0.094 (sec), leaf count = 80

$$\left\{ \left\{ x(t) = -\frac{2 \cos(2t)}{325} + 4 - \frac{36 \sin(2t)}{325} + 2t + \_C1 e^t + \_C2 e^{-3t} + \_C3 e^t t, y(t) = \frac{16 \cos(2t)}{325} - \frac{37}{16} \right. \right.$$

## 9.29 ODE No. 1884

$$\left\{ \frac{d^2}{dt^2}x(t) - 2 \frac{d}{dt}y(t) = 2t - \cos(2t), \frac{d}{dt}x(t) - x(t) + 2y(t) = 0 \right\}$$

**Mathematica:** cpu = 0.180523 (sec), leaf count = 226

$$\left\{ \left\{ x(t) \rightarrow 7 \left( c_2 + t^2 - \frac{1}{2} \sin(2t) \right) + 8 \left( c_1 e^{t/2} + c_2 (e^{t/2} - 1) + \frac{1}{68} e^{-t/2} (e^{t/2} \cos(2t) - 2(17(2e^{t/2}t^2 + e^{t/2}t) \right) \right. \right.$$

**Maple:** cpu = 0.078 (sec), leaf count = 69

$$\left\{ \left\{ x(t) = \frac{\sin(2t)}{34} + \frac{2 \cos(2t)}{17} - t^2 + 2\_C1 e^{t/2} - 4t + \_C2, y(t) = \frac{\cos(2t)}{34} + \frac{9 \sin(2t)}{68} - t + \frac{\_C1}{2} e^{t/2} \right. \right.$$

## 9.30 ODE No. 1885

$$\left\{ t \frac{d^2}{dt^2}x(t) + 2 \frac{d}{dt}x(t) + tx(t) = 0, t \frac{d}{dt}x(t) - t \frac{d}{dt}y(t) - 2y(t) = 0 \right\}$$

**Mathematica:** cpu = 0.022503 (sec), leaf count = 47

$$\text{DSolve}[\{tx'(t) - ty'(t) - 2y(t) = 0, tx''(t) + 2x'(t) + tx(t) = 0\}, \{x(t), y(t)\}, t]$$

**Maple:** cpu = 0.078 (sec), leaf count = 47

$$\left\{ \left\{ x(t) = \frac{\sin(t) \_C2 + \_C3 \cos(t)}{t}, y(t) = \frac{\sin(t) \_C2 t + \cos(t) \_C3 t - 2 \_C3 \sin(t) + 2 \cos(t) \_C1}{t^2} \right. \right.$$

**9.31 ODE No. 1886**

$$\left\{ \frac{d^2}{dt^2}x(t) + ay(t) = 0, \frac{d^2}{dt^2}y(t) - a^2y(t) = 0 \right\}$$

**Mathematica:** cpu = 0.021003 (sec), leaf count = 115

$$\left\{ \left\{ x(t) \rightarrow -\frac{c_4 e^{-at}(-2ate^{at} + e^{2at} - 1)}{2a^2} - \frac{c_3 e^{-at}(e^{at} - 1)^2}{2a} + c_2 t + c_1, y(t) \rightarrow \frac{1}{2}c_3 e^{-at}(e^{2at} + 1) + \frac{c_4 e^{-at}}{2} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 50

$$\left\{ \left\{ x(t) = -\frac{-C1 ta + C3 e^{at} + C4 e^{-at} - C2 a}{a}, y(t) = C3 e^{at} + C4 e^{-at} \right\} \right\}$$

**9.32 ODE No. 1887**

$$\left\{ \frac{d^2}{dt^2}x(t) = ax(t) + by(t), \frac{d^2}{dt^2}y(t) = cx(t) + dy(t) \right\}$$

**Mathematica:** cpu = 0.480061 (sec), leaf count = 5748

$$\left\{ \left\{ x(t) \rightarrow \frac{e^{-\frac{\sqrt{a+d-\sqrt{a^2-2da+d^2+4bct}}}{\sqrt{2}}} - \frac{\sqrt{a+d+\sqrt{a^2-2da+d^2+4bct}}}{\sqrt{2}} \left( e^{\frac{\sqrt{a+d-\sqrt{a^2-2da+d^2+4bct}}}{\sqrt{2}}} a - e^{\frac{\sqrt{a+d+\sqrt{a^2-2da+d^2+4bct}}}{\sqrt{2}}} a - e^{\frac{\sqrt{a+d-\sqrt{a^2-2da+d^2+4bct}}}{\sqrt{2}}} \right)}{2} \right\} \right\}$$

**Maple:** cpu = 0.094 (sec), leaf count = 418

$$\left\{ \left\{ x(t) = C1 e^{-\frac{t}{2}\sqrt{-2\sqrt{a^2-2da+4bc+d^2}+2a+2d}} + C2 e^{\frac{t}{2}\sqrt{-2\sqrt{a^2-2da+4bc+d^2}+2a+2d}} + C3 e^{-\frac{t}{2}\sqrt{2\sqrt{a^2-2da+4bc+d^2}+2a+2d}} \right\} \right\}$$

**9.33 ODE No. 1888**

$$\left\{ \frac{d^2}{dt^2}x(t) = a1 x(t) + b1 y(t) + c1, \frac{d^2}{dt^2}y(t) = a2 x(t) + b2 y(t) + c2 \right\}$$

**Mathematica:** cpu = 25.510739 (sec), leaf count = 37858

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**Maple:** cpu = 0.171 (sec), leaf count = 634

$$\left\{ \left\{ x(t) = C4 e^{\frac{t}{2}\sqrt{2\sqrt{a1^2-2a1 b2+4a2 b1+b2^2}+2a1+2b2}} + C3 e^{-\frac{t}{2}\sqrt{2\sqrt{a1^2-2a1 b2+4a2 b1+b2^2}+2a1+2b2}} + C2 \right\} \right\}$$



### 9.34 ODE No. 1889

$$\left\{ \frac{d^2}{dt^2}x(t) + x(t) + y(t) = -5, \frac{d^2}{dt^2}y(t) - 4x(t) - 3y(t) = -3 \right\}$$

**Mathematica:** cpu = 0.103513 (sec), leaf count = 554

$$\left\{ \left\{ x(t) \rightarrow -\frac{1}{4}c_4e^{-t}(e^{2t}t + t - e^{2t} + 1) - \frac{1}{2}c_1e^{-t}(e^{2t}t - t - e^{2t} - 1) - \frac{1}{2}c_2e^{-t}(e^{2t}t + t - 2e^{2t} + 2) - \frac{1}{4}c_3e^{-t}(e^{2t}t + t - e^{2t} + 1) \right\} \right\}$$

**Maple:** cpu = 0.032 (sec), leaf count = 72

$$\left\{ \left\{ x(t) = 18 + \_C1 e^t + \_C2 e^{-t} + \_C3 e^t t + \_C4 e^{-t} t, y(t) = -2 \_C1 e^t - 2 \_C2 e^{-t} - 2 \_C3 e^t t - 2 \_C4 e^{-t} t \right\} \right\}$$

### 9.35 ODE No. 1890

$$\left\{ \frac{d^2}{dt^2}x(t) = (3(\cos(at+b))^2 - 1)c^2x(t) + 3/2c^2y(t)\sin(2atb), \frac{d^2}{dt^2}y(t) = (3(\sin(at+b))^2 - 1)c^2y(t) \right\}$$

**Mathematica:** cpu = 0.009501 (sec), leaf count = 86

$$\text{DSolve} \left[ \left\{ x''(t) = c^2x(t)(3\cos^2(at+b) - 1) + \frac{3}{2}c^2y(t)\sin(2abt), y''(t) = \frac{3}{2}c^2x(t)\sin(2abt) + c^2y(t)(3\sin^2(at+b) - 1) \right\} \right]$$

**Maple:** cpu = 13.666 (sec), leaf count = 1445

$$\left\{ \left\{ x(t) = \text{DESol} \left( \left( \frac{d^4}{dt^4} - Y(t) + \left( 2 \frac{\sin(atb)ab}{\cos(atb)} - 2 \frac{ab \cos(atb)}{\sin(atb)} \right) \frac{d^3}{dt^3} - Y(t) + \left( 2c^2 - 3(\sin(atb))^2 \right) c^2 \cos(atb) \right) \right\} \right\}$$

### 9.36 ODE No. 1891

$$\left\{ \frac{d^2}{dt^2}x(t) + 6x(t) + 7y(t) = 0, \frac{d^2}{dt^2}y(t) + 3x(t) + 2y(t) = 2t \right\}$$

**Mathematica:** cpu = 0.445557 (sec), leaf count = 766

$$\left\{ \left\{ x(t) \rightarrow -\frac{7}{60}c_4e^{-t}(3e^{2t} - 2e^t \sin(3t) - 3) + \frac{1}{60}c_2e^{-t}(9e^{2t} + 14e^t \sin(3t) - 9) - \frac{7}{20}c_3e^{-t}(e^{2t} - 2e^t \cos(3t) - 1) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 64

$$\left\{ \left\{ x(t) = \frac{14t}{9} + \_C1 e^t + \_C2 \cos(3t) + \_C3 e^{-t} + \_C4 \sin(3t), y(t) = -\_C1 e^t + \frac{3\_C2 \cos(3t)}{7} \right\} \right\}$$

**9.37 ODE No. 1892**

$$\left\{ \frac{d^2}{dt^2}x(t) - a\frac{d}{dt}y(t) + bx(t) = 0, \frac{d^2}{dt^2}y(t) + a\frac{d}{dt}x(t) + by(t) = 0 \right\}$$

**Mathematica:** cpu = 0.370547 (sec), leaf count = 4815

$$\left\{ \left\{ x(t) \rightarrow \frac{e^{-\frac{\sqrt{-a^2-2b-\sqrt{a^2(a^2+4b)}}t}} - \frac{\sqrt{-a^2-2b+\sqrt{a^2(a^2+4b)}}t}}{\sqrt{2}} \left( e^{\frac{\sqrt{-a^2-2b-\sqrt{a^2(a^2+4b)}}t}} a^2 - e^{\frac{\sqrt{-a^2-2b+\sqrt{a^2(a^2+4b)}}t}} a^2 - e^{\sqrt{2}t} \right) \right. \right.$$

**Maple:** cpu = 0.094 (sec), leaf count = 868

$$\left\{ \left\{ x(t) = \_C1 e^{-\frac{t}{2}\sqrt{-2a^2-2\sqrt{a^2(a^2+4b)}-4b}} + \_C2 e^{\frac{t}{2}\sqrt{-2a^2-2\sqrt{a^2(a^2+4b)}-4b}} + \_C3 e^{-\frac{t}{2}\sqrt{-2a^2+2\sqrt{a^2(a^2+4b)}-4b}} \right. \right.$$

**9.38 ODE No. 1893**

$$\left\{ a1 \frac{d^2}{dt^2}x(t) + b1 \frac{d}{dt}x(t) + c1 x(t) - A \frac{d}{dt}y(t) = B e^{i\omega t}, a2 \frac{d^2}{dt^2}y(t) + b2 \frac{d}{dt}y(t) + c2 y(t) + A \frac{d}{dt}x(t) = 0 \right\}$$

**Mathematica:** cpu = 369.474917 (sec), leaf count = 5538

**Maple:** cpu = 0.858 (sec), leaf count = 4516

### 9.39 ODE No. 1894

$$\left\{ \frac{d^2}{dt^2}x(t) + a \left( \frac{d}{dt}x(t) - \frac{d}{dt}y(t) \right) + b1 x(t) = c1 e^{i\omega t}, \frac{d^2}{dt^2}y(t) + a \left( \frac{d}{dt}y(t) - \frac{d}{dt}x(t) \right) + b2 y(t) = c2 e^{i\omega t} \right\}$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.671 (sec), leaf count = 2511

$$\left\{ \left\{ x(t) = \frac{ie^{i\omega t}ac1\omega + ie^{i\omega t}ac2\omega - e^{i\omega t}c1\omega^2 + e^{i\omega t}b2c1}{-2ia\omega^3 + iab1\omega + iab2\omega + \omega^4 - b1\omega^2 - b2\omega^2 + b2b1} + \_C1 e^{RootOf(-Z^4+2a\_Z^3+(b1+b2)\_Z^2} \right. \right.$$

### 9.40 ODE No. 1895

$$\left\{ a11 \frac{d^2}{dt^2}x(t) + b11 \frac{d}{dt}x(t) + c11 x(t) + a12 \frac{d^2}{dt^2}y(t) + b12 \frac{d}{dt}y(t) + c12 y(t) = 0, a21 \frac{d^2}{dt^2}x(t) + b21 \frac{d}{dt}x(t) + c21 x(t) + a22 \frac{d^2}{dt^2}y(t) + b22 \frac{d}{dt}y(t) + c22 y(t) = 0 \right\}$$

**Mathematica:** cpu = 0.449557 (sec), leaf count = 7517

Result too large for latex to process

**Maple:** cpu = 0.156 (sec), leaf count = 1187

$$\left\{ \left\{ x(t) = \sum_{a=1}^4 e^{RootOf((a22 a11 - a12 a21)\_Z^4 + (a11 b22 - a12 b21 - a21 b12 + a22 b11)\_Z^3 + (a11 c22 - a12 c21 - a21 c12 + a22 c11 + \dots} \right. \right.$$

### 9.41 ODE No. 1896

$$\left\{ \frac{d^3}{dt^3}y(t) - \frac{d^2}{dt^2}y(t) + 2 \frac{d}{dt}x(t) - x(t) = t, \frac{d^2}{dt^2}x(t) - 2 \frac{d}{dt}x(t) - \frac{d}{dt}y(t) + y(t) = 0 \right\}$$

**Mathematica:** cpu = 0.197525 (sec), leaf count = 1132

$$\left\{ \left\{ x(t) \rightarrow \frac{1}{64}e^{-t}(2e^{2t}t^2 - 6e^{2t}t + 7e^{2t} + 1) (e^t(1-t) + e^{-t}(-2t^3 - 8t^2 - 17t - 17)) + \frac{1}{64}e^{-t}(2e^{2t}t^2 + 6e^{2t}t + 7e^{2t} + 1) \right. \right.$$

**Maple:** cpu = 0.031 (sec), leaf count = 75

$$\left\{ \left\{ x(t) = -2 - t - \_C3 e^t - 6 \_C5 e^t - \frac{2 \_C2 e^{-t}}{3} - 2 \_C4 e^t t - 3 \_C5 e^t t^2, y(t) = -2 + \_C1 e^t + \_C2 e^{-t} \right. \right.$$

### 9.42 ODE No. 1897

$$\left\{ 2 \frac{d^2}{dt^2} x(t) + \frac{d^2}{dt^2} y(t) = 2t, \frac{d^2}{dt^2} x(t) + \frac{d^2}{dt^2} y(t) + \frac{d}{dt} y(t) = \sinh(2t) \right\}$$

**Mathematica:** cpu = 0.114015 (sec), leaf count = 284

$$\left\{ \left\{ x(t) \rightarrow \frac{1}{4} c_4 e^{-2t} (2e^{2t} t - e^{2t} + 1) + c_2 t + c_1 + t \left( \frac{t^2}{2} + \frac{t}{2} - \frac{e^{4t}}{8} + e^{2t} \left( \frac{t}{2} - \frac{1}{4} \right) \right) + \frac{1}{48} e^{-2t} (-4e^{2t} (4t^2 - 3) \right. \right.$$

**Maple:** cpu = 0.110 (sec), leaf count = 98

$$\left\{ \left\{ x(t) = -\frac{\sinh(2t)}{16} - \frac{\cosh(2t)}{16} - \frac{5e^{-2t}}{16} - \frac{e^{-2t}t}{4} + \frac{t^3}{6} + \frac{e^{-2t}C2}{4} + \frac{t^2}{4} + C3t + C4, y(t) = \frac{3 \cos}{16} \right. \right.$$

### 9.43 ODE No. 1898

$$\left\{ \frac{d^2}{dt^2} x(t) + \frac{d^2}{dt^2} y(t) - x(t) = 0, \frac{d^2}{dt^2} x(t) - \frac{d}{dt} x(t) + \frac{d}{dt} y(t) = 0 \right\}$$

**Mathematica:** cpu = 0.037505 (sec), leaf count = 420

$$\left\{ \left\{ x(t) \rightarrow -\frac{1}{5} c_1 e^{\frac{t}{2} - \frac{\sqrt{5}t}{2}} \left( \sqrt{5} e^{\sqrt{5}t} - 5e^{\frac{\sqrt{5}t}{2} + \frac{t}{2}} - \sqrt{5} \right) + \frac{c_2 e^{\frac{t}{2} - \frac{\sqrt{5}t}{2}} \left( e^{\sqrt{5}t} - 1 \right)}{\sqrt{5}} - \frac{1}{10} c_4 e^{\frac{t}{2} - \frac{\sqrt{5}t}{2}} \left( 5e^{\sqrt{5}t} + \sqrt{5} e^{\sqrt{5}t} \right) \right. \right.$$

**Maple:** cpu = 0.063 (sec), leaf count = 73

$$\left\{ \left\{ x(t) = \left( -\frac{1}{2} - \frac{\sqrt{5}}{2} \right) C3 e^{\frac{(\sqrt{5}+1)t}{2}} + \left( \frac{\sqrt{5}}{2} - \frac{1}{2} \right) C4 e^{-\frac{(\sqrt{5}-1)t}{2}} + C1 e^t, y(t) = C2 + C3 e^{\frac{(\sqrt{5}+1)t}{2}} \right. \right.$$

### 9.44 ODE No. 1899

$$\left\{ \frac{d}{dt} x(t) = 2x(t), \frac{d}{dt} y(t) = 3x(t) - 2y(t), \frac{d}{dt} z(t) = 2y(t) + 3z(t) \right\}$$

**Mathematica:** cpu = 0.010501 (sec), leaf count = 112

$$\left\{ \left\{ x(t) \rightarrow c_1 e^{2t}, y(t) \rightarrow \frac{3}{4} c_1 e^{-2t} (e^{4t} - 1) + c_2 e^{-2t}, z(t) \rightarrow \frac{3}{10} c_1 e^{-2t} (2e^t + 3e^{2t} + 4e^{3t} + 1) (e^t - 1)^2 + \frac{2}{5} c_2 \right. \right.$$

**Maple:** cpu = 0.078 (sec), leaf count = 52

$$\left\{ \left\{ x(t) = C3 e^{2t}, y(t) = \frac{3C3 e^{2t}}{4} + e^{-2t} C2, z(t) = C1 e^{3t} - \frac{3C3 e^{2t}}{2} - \frac{2e^{-2t} C2}{5} \right. \right\}$$

### 9.45 ODE No. 1900

$$\left\{ \frac{d}{dt}x(t) = 4x(t), \frac{d}{dt}y(t) = x(t) - 2y(t), \frac{d}{dt}z(t) = x(t) - 4y(t) + z(t) \right\}$$

**Mathematica:** cpu = 0.009501 (sec), leaf count = 94

$$\left\{ \left\{ x(t) \rightarrow c_1 e^{4t}, y(t) \rightarrow \frac{1}{6} c_1 e^{-2t} (e^{6t} - 1) + c_2 e^{-2t}, z(t) \rightarrow \frac{1}{9} c_1 e^{-2t} (e^{3t} + e^{6t} - 2) - \frac{4}{3} c_2 e^{-2t} (e^{3t} - 1) + c_3 \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 50

$$\left\{ \left\{ x(t) = \_C3 e^{4t}, y(t) = \frac{\_C3 e^{4t}}{6} + e^{-2t} \_C2, z(t) = \frac{\_C3 e^{4t}}{9} + \_C1 e^t + \frac{4 e^{-2t} \_C2}{3} \right\} \right\}$$

### 9.46 ODE No. 1901

$$\left\{ \frac{d}{dt}x(t) = y(t) - z(t), \frac{d}{dt}y(t) = x(t) + y(t), \frac{d}{dt}z(t) = x(t) + z(t) \right\}$$

**Mathematica:** cpu = 0.010001 (sec), leaf count = 105

$$\left\{ \left\{ x(t) \rightarrow c_2 (e^t - 1) + c_3 (1 - e^t) + c_1, y(t) \rightarrow c_1 (e^t - 1) + c_2 (e^t t + 1) + c_3 (-e^t t + e^t - 1), z(t) \rightarrow c_1 (e^t - 1) + c_2 (e^t t + 1) + c_3 (-e^t t + e^t - 1) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 48

$$\left\{ \left\{ x(t) = \_C2 + \_C3 e^t, y(t) = \_C3 e^t t + \_C1 e^t - \_C2, z(t) = \_C3 e^t t + \_C1 e^t - \_C3 e^t - \_C2 \right\} \right\}$$

### 9.47 ODE No. 1902

$$\left\{ \frac{d}{dt}x(t) - y(t) + z(t) = 0, \frac{d}{dt}y(t) - x(t) - y(t) = t, \frac{d}{dt}z(t) - x(t) - z(t) = t \right\}$$

**Mathematica:** cpu = 0.014002 (sec), leaf count = 226

$$\left\{ \left\{ x(t) \rightarrow c_2 (e^t - 1) + c_3 (1 - e^t) + c_1 + e^{-t} (1 - e^t) (-t - 1) + e^{-t} (e^t - 1) (-t - 1), y(t) \rightarrow c_3 (-e^t t + e^t) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 56

$$\left\{ \left\{ x(t) = \_C2 + \_C3 e^t, y(t) = \_C3 e^t t + \_C1 e^t - \_C2 - t - 1, z(t) = \_C3 e^t t + \_C1 e^t - \_C3 e^t - t - 1 \right\} \right\}$$

### 9.48 ODE No. 1903

$$\left\{ a \frac{d}{dt} x(t) = bc(y(t) - z(t)), b \frac{d}{dt} y(t) = ca(z(t) - x(t)), c \frac{d}{dt} z(t) = ab(x(t) - y(t)) \right\}$$

**Mathematica:** cpu = 0.090011 (sec), leaf count = 1304

$$\left\{ \left\{ x(t) \rightarrow \frac{e^{-i\sqrt{a^2+b^2+c^2}t} \left( 2e^{i\sqrt{a^2+b^2+c^2}t} a^2 + b^2 e^{2i\sqrt{a^2+b^2+c^2}t} + c^2 e^{2i\sqrt{a^2+b^2+c^2}t} + b^2 + c^2 \right) c_1 - b e^{-i\sqrt{a^2+b^2+c^2}t}}{2(a^2 + b^2 + c^2)} \right. \right.$$

**Maple:** cpu = 0.109 (sec), leaf count = 312

$$\left\{ \left\{ x(t) = \_C1 + \_C2 \sin(\sqrt{a^2 + b^2 + c^2}t) + \_C3 \cos(\sqrt{a^2 + b^2 + c^2}t), y(t) = -\frac{1}{b(b^2 + c^2)} \left( \sin(\sqrt{a^2 + b^2 + c^2}t) \right) \right. \right.$$

### 9.49 ODE No. 1904

$$\left\{ \frac{d}{dt} x(t) = cy(t) - bz(t), \frac{d}{dt} y(t) = az(t) - cx(t), \frac{d}{dt} z(t) = bx(t) - ay(t) \right\}$$

**Mathematica:** cpu = 0.065008 (sec), leaf count = 1445

$$\left\{ \left\{ x(t) \rightarrow \frac{e^{-\sqrt{-a^2-b^2-c^2}t} \left( 2e^{\sqrt{-a^2-b^2-c^2}t} a^2 + b^2 e^{2\sqrt{-a^2-b^2-c^2}t} + c^2 e^{2\sqrt{-a^2-b^2-c^2}t} + b^2 + c^2 \right) c_1 - e^{-\sqrt{-a^2-b^2-c^2}t}}{2(a^2 + b^2 + c^2)} \right. \right.$$

**Maple:** cpu = 0.062 (sec), leaf count = 312

$$\left\{ \left\{ x(t) = \_C1 + \_C2 \sin(\sqrt{a^2 + b^2 + c^2}t) + \_C3 \cos(\sqrt{a^2 + b^2 + c^2}t), y(t) = -\frac{1}{a(b^2 + c^2)} \left( \sin(\sqrt{a^2 + b^2 + c^2}t) \right) \right. \right.$$

### 9.50 ODE No. 1905

$$\left\{ \frac{d}{dt} x(t) = h(t)y(t) - g(t)z(t), \frac{d}{dt} y(t) = f(t)z(t) - h(t)x(t), \frac{d}{dt} z(t) = x(t)g(t) - y(t)f(t) \right\}$$

**Mathematica:** cpu = 0.006501 (sec), leaf count = 61

`DSolve[{x'(t) = h(t)y(t) - g(t)z(t), y'(t) = f(t)z(t) - h(t)x(t), z'(t) = g(t)x(t) - f(t)y(t)}, {x(t), y(t), z(t)}`

**Maple:** cpu = 0.530 (sec), leaf count = 2014

$$\left\{ \left\{ x(t) = DESol \left( \left\{ \frac{d^3}{dt^3} Y(t) + \left( \frac{\left( \frac{d}{dt} f(t) \right) \left( g(t) \right)^2}{-(h(t))^2 f(t) - f(t) \left( g(t) \right)^2 + h(t) \frac{d}{dt} g(t) - \left( \frac{d}{dt} h(t) \right) g(t)} \right) + \dots \right. \right.$$

### 9.51 ODE No. 1906

$$\left\{ \frac{d}{dt}x(t) = x(t) + y(t) - z(t), \frac{d}{dt}y(t) = y(t) + z(t) - x(t), \frac{d}{dt}z(t) = z(t) + x(t) - y(t) \right\}$$

**Mathematica:** cpu = 0.052007 (sec), leaf count = 278

$$\left\{ \left\{ x(t) \rightarrow \frac{1}{3}c_1 e^t \left( 2 \cos(\sqrt{3}t) + 1 \right) - \frac{1}{3}c_2 e^t \left( -\sqrt{3} \sin(\sqrt{3}t) + \cos(\sqrt{3}t) - 1 \right) - \frac{1}{3}c_3 e^t \left( \sqrt{3} \sin(\sqrt{3}t) + \cos(\sqrt{3}t) - 1 \right) \right. \right.$$

**Maple:** cpu = 0.063 (sec), leaf count = 128

$$\left\{ \left\{ x(t) = e^t \left( \sin(\sqrt{3}t) \_C2 + \cos(\sqrt{3}t) \_C3 + \_C1 \right), y(t) = -\frac{e^t \left( \sin(\sqrt{3}t) \sqrt{3} \_C3 - \cos(\sqrt{3}t) \sqrt{3} \right)}{3} \right. \right.$$

### 9.52 ODE No. 1907

$$\left\{ \frac{d}{dt}x(t) = -3x(t) + 48y(t) - 28z(t), \frac{d}{dt}y(t) = -4x(t) + 40y(t) - 22z(t), \frac{d}{dt}z(t) = -6x(t) + 57y(t) \right\}$$

**Mathematica:** cpu = 0.009501 (sec), leaf count = 179

$$\left\{ \left\{ x(t) \rightarrow c_1 (-e^t) (2e^{2t} - 3) + 6c_2 e^t (2e^t + 3e^{2t} - 5) - 2c_3 e^t (4e^t + 5e^{2t} - 9), y(t) \rightarrow -2c_1 e^t (e^{2t} - 1) + c_2 (e^{2t} - 3) + c_3 (e^{2t} - 3) \right. \right.$$

**Maple:** cpu = 0.046 (sec), leaf count = 66

$$\left\{ \left\{ x(t) = \_C1 e^{3t} + \_C2 e^{2t} + \_C3 e^t, y(t) = \_C1 e^{3t} + \frac{\_C2 e^{2t}}{4} + \frac{2 \_C3 e^t}{3}, z(t) = \frac{3 \_C1 e^{3t}}{2} + \frac{\_C2 e^{2t}}{2} + \frac{\_C3 e^t}{2} \right. \right.$$

### 9.53 ODE No. 1908

$$\left\{ \frac{d}{dt}x(t) = 6x(t) - 72y(t) + 44z(t), \frac{d}{dt}y(t) = 4x(t) - 4y(t) + 26z(t), \frac{d}{dt}z(t) = 6x(t) - 63y(t) + 38z(t) \right\}$$

**Mathematica:** cpu = 0.019502 (sec), leaf count = 551

Result too large for latex to process

**Maple:** cpu = 0.468 (sec), leaf count = 3207

### 9.54 ODE No. 1909

$$\left\{ \frac{d}{dt}x(t) = ax(t) + gy(t) + \beta z(t), \frac{d}{dt}y(t) = gx(t) + by(t) + \alpha z(t), \frac{d}{dt}z(t) = \beta x(t) + \alpha y(t) + cz(t) \right\}$$

**Mathematica:** cpu = 0.060008 (sec), leaf count = 1630

$$\left\{ \left\{ x(t) \rightarrow -c_2 \text{RootSum} \left[ \#1^3 - a\#1^2 - b\#1^2 - c\#1^2 - \alpha^2\#1 - \beta^2\#1 - g^2\#1 + ab\#1 + ac\#1 + bc\#1 \right] \right\} \right\}$$

**Maple:** cpu = 23.774 (sec), leaf count = 33085

Result too large for latex to process

### 9.55 ODE No. 1910

$$\left\{ t \frac{d}{dt}x(t) = 2x(t) - t, t^3 \frac{d}{dt}y(t) = -x(t) + t^2y(t) + t, t^4 \frac{d}{dt}z(t) = -x(t) - t^2y(t) + t^3z(t) + t \right\}$$

**Mathematica:** cpu = 0.009501 (sec), leaf count = 39

$$\left\{ \left\{ x(t) \rightarrow c_3 t^2 + t, y(t) \rightarrow c_2 t + c_3, z(t) \rightarrow c_1 t + \frac{c_3}{t} + c_2 \right\} \right\}$$

**Maple:** cpu = 0.063 (sec), leaf count = 37

$$\left\{ \left\{ x(t) = \_C3 t^2 + t, y(t) = t\_C2 + \_C3, z(t) = \frac{\_C1 t^2 + t\_C2 + \_C3}{t} \right\} \right\}$$

### 9.56 ODE No. 1911

$$\left\{ at \frac{d}{dt}x(t) = bc(y(t) - z(t)), bt \frac{d}{dt}y(t) = ca(z(t) - x(t)), ct \frac{d}{dt}z(t) = ab(x(t) - y(t)) \right\}$$

**Mathematica:** cpu = 0.037505 (sec), leaf count = 64

`DSolve[{atx'(t) = bc(y(t) - z(t)), bty'(t) = ac(z(t) - x(t)), ctz'(t) = ab(x(t) - y(t))}, {x(t), y(t), z(t)}, t]`

**Maple:** cpu = 0.110 (sec), leaf count = 322

$$\left\{ \left\{ x(t) = \_C1 + \_C2 \sin \left( \sqrt{a^2 + b^2 + c^2} \ln(t) \right) + \_C3 \cos \left( \sqrt{a^2 + b^2 + c^2} \ln(t) \right), y(t) = \frac{1}{b(b^2 + c^2)} \left( c \right) \right\} \right\}$$



**9.57 ODE No. 1912**

$$\left\{ \begin{array}{l} \frac{d}{dt}x_1(t) = ax_2(t) + bx_3(t) \cos(ct) + bx_4(t) \sin(ct), \\ \frac{d}{dt}x_2(t) = -ax_1(t) + bx_3(t) \sin(ct) - bx_4(t) \cos(ct) \end{array} \right.$$

**Mathematica:** cpu = 0.011001 (sec), leaf count = 122

`DSolve[{x1'(t) = ax2(t) + bx3(t) cos(ct) + bx4(t) sin(ct), x2'(t) = -ax1(t) + bx3(t) sin(ct) - bx4(t) cos(ct)}`

**Maple:** cpu = 1.716 (sec), leaf count = 11399

## 10 Kamke chapter 9. System of non-linear differential equations

### 10.1 ODE No. 1913

$$\left\{ \frac{d}{dt}x(t) = -x(t)(x(t) + y(t)), \frac{d}{dt}y(t) = y(t)(x(t) + y(t)) \right\}$$

**Mathematica:** cpu = 0.032004 (sec), leaf count = 64

$$\{\{y(t) \rightarrow -\sqrt{c_1} \cot(\sqrt{c_1}t - \sqrt{c_1}c_2), x(t) \rightarrow -\sqrt{c_1} \tan(\sqrt{c_1}t - \sqrt{c_1}c_2)\}\}$$

**Maple:** cpu = 0.109 (sec), leaf count = 54

$$\left\{ [\{x(t) = 0\}, \{y(t) = (-C1 - t)^{-1}\}], \left[ \left\{ x(t) = \frac{1}{-C1} \tanh\left(\frac{-C2 + t}{-C1}\right) \right\}, \left\{ y(t) = -\frac{(x(t))^2 + \frac{d}{dt}x(t)}{x(t)} \right\} \right] \right\}$$

### 10.2 ODE No. 1914

$$\left\{ \frac{d}{dt}x(t) = (ay(t) + b)x(t), \frac{d}{dt}y(t) = (cx(t) + d)y(t) \right\}$$

**Mathematica:** cpu = 0.508065 (sec), leaf count = 201

$$\left\{ \left\{ \begin{array}{l} \left( \begin{array}{l} a \text{InverseFunction} \left[ \int_1^{\#1} \frac{1}{K[1] \left( W \left( \frac{cK[1]}{ae} + \frac{c_1}{b} K[1] \frac{d}{b} \right) + 1 \right)} dK[1] \& [bt+c_2] \frac{d}{b} \exp \right. \end{array} \right. \\ \left. \left. \begin{array}{l} c \text{InverseFunction} \left[ \int_1^{\#1} \frac{1}{K[1] \left( W \left( \frac{cK[1]}{ae} \right) + 1 \right)} \right. \end{array} \right. \\ \left. \left. \begin{array}{l} bW \\ b \end{array} \right. \end{array} \right\} \right\} y(t) \rightarrow \left. \right\} a$$

**Maple:** cpu = 0.250 (sec), leaf count = 92

$$\left\{ \left\{ \{x(t) = 0\}, \{y(t) = -C1 e^{dt}\} \right\}, \left\{ x(t) = \text{RootOf} \left( - \int^{-Z} \frac{1}{b-a} \left( \text{lambertW} \left( \frac{e^{-1}}{b} e^{\frac{c-a}{b}} - a \frac{d}{b} e^{-\frac{C1}{b}} \right) + 1 \right) \right)^{-1} \right\} \right\}$$

### 10.3 ODE No. 1915

$$\left\{ \frac{d}{dt}x(t) = x(t) (a(px(t) + qy(t)) + \alpha), \frac{d}{dt}y(t) = y(t) (\beta + b(px(t) + qy(t))) \right\}$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 13.791 (sec), leaf count = 181

$$\left\{ \left[ \{x(t) = 0\}, \left\{ y(t) = \frac{\beta}{e^{-\beta t} - C1 \beta - bq} \right\} \right], \left[ \left\{ x(t) = ODESolStruc \left( -b(-a), \left[ \left( -b(-a) \right)^{-\frac{a+b}{a}} e^{-\frac{a(a\beta - \alpha b)}{a}} \right] \right) \right\} \right] \right\}$$

### 10.4 ODE No. 1916

$$\left\{ \frac{d}{dt}x(t) = h(a - x(t)) (c - x(t) - y(t)), \frac{d}{dt}y(t) = k(b - y(t)) (c - x(t) - y(t)) \right\}$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0.359 (sec), leaf count = 237

$$\left\{ \left[ \{x(t) = a\}, \left\{ y(t) = -\frac{ae^{-C1 ka + C1 kb - C1 kc + akt + bkt - ckt} - ce^{-C1 ka + C1 kb - C1 kc + akt + bkt - ckt} + b}{-1 + e^{-C1 ka + C1 kb - C1 kc + akt + bkt - ckt}} \right\} \right], \left[ \{x(t) = \dots\} \right] \right\}$$

### 10.5 ODE No. 1917

$$\left\{ \frac{d}{dt}x(t) = (y(t))^2 - \cos(x(t)), \frac{d}{dt}y(t) = -y(t) \sin(x(t)) \right\}$$

**Mathematica:** cpu = 250.096758 (sec), leaf count = 35

$$\text{DSolve}[\{x'(t) = y(t)^2 - \cos(x(t)), y'(t) = y(t)(-\sin(x(t)))\}, \{x(t), y(t)\}, t]$$

**Maple:** cpu = 0.593 (sec), leaf count = 109

$$\left\{ \left[ \left\{ x(t) = \text{RootOf} \left( 2 \int^{-Z} \left( \tan \left( \text{RootOf} \left( -3 \sqrt{-(\cos(\_f))^2} \ln \left( 9/4 \frac{(\cos(\_f))^2}{(\cos(\_Z))^2} \right) + 3 - C1 \sqrt{-(\cos(\_f))^2} \right) \right) \right) \right\} \right] \right\}$$

## 10.6 ODE No. 1918

$$\left\{ \frac{d}{dt}x(t) = -x(t)(y(t))^2 + x(t) + y(t), \frac{d}{dt}y(t) = (x(t))^2 y(t) - x(t) - y(t) \right\}$$

**Mathematica:** cpu = 0.090511 (sec), leaf count = 47

DSolve[{x'(t) = -x(t)y(t)^2 + x(t) + y(t), y'(t) = x(t)^2 y(t) - x(t) - y(t)}, {x(t), y(t)}, t]

**Maple:** cpu = 1.373 (sec), leaf count = 245

$$\left\{ [x(t) = 0], [y(t) = 0], [x(t) = ODESolStruc\left(-a, \left[ \left( \frac{d}{d\_a} b(-a) \right) - b(-a) - \frac{1}{2\_a^2} \left( 4\_b(-a) \right) \right] \right) \right\}$$

## 10.7 ODE No. 1919

$$\left\{ \frac{d}{dt}x(t) = x(t) + y(t) - x(t)((x(t))^2 + (y(t))^2), \frac{d}{dt}y(t) = -x(t) + y(t) - y(t)((x(t))^2 + (y(t))^2) \right\}$$

**Mathematica:** cpu = 0.107014 (sec), leaf count = 56

DSolve[{x'(t) = x(t)(-(x(t)^2 + y(t)^2)) + x(t) + y(t), y'(t) = -y(t)(x(t)^2 + y(t)^2) - x(t) + y(t)}, {x(t), y(t)}, t]

**Maple:** cpu = 2.278 (sec), leaf count = 249

$$\left\{ [x(t) = 0], [y(t) = 0], [x(t) = ODESolStruc\left(-a, \left[ \left( \frac{d}{d\_a} b(-a) \right) - b(-a) - \frac{1}{2\_a^3} \left( 6\_b(-a) \right) \right] \right) \right\}$$

## 10.8 ODE No. 1920

$$\left\{ \frac{d}{dt}x(t) = -y(t) + x(t)((x(t))^2 + (y(t))^2 - 1), \frac{d}{dt}y(t) = x(t) + y(t)((x(t))^2 + (y(t))^2 - 1) \right\}$$

**Mathematica:** cpu = 0.081510 (sec), leaf count = 52

DSolve[{x'(t) = x(t)(x(t)^2 + y(t)^2 - 1) - y(t), y'(t) = y(t)(x(t)^2 + y(t)^2 - 1) + x(t)}, {x(t), y(t)}, t]

**Maple:** cpu = 2.294 (sec), leaf count = 250

$$\left\{ [x(t) = 0], [y(t) = 0], [x(t) = ODESolStruc\left(-a, \left[ \left( \frac{d}{d\_a} b(-a) \right) - b(-a) - \frac{1}{2\_a^3} \left( 6\_b(-a) \right) \right] \right) \right\}$$

### 10.9 ODE No. 1921

$$\left\{ \begin{array}{l} \frac{d}{dt}x(t) = -y(t) ((x(t))^2 + (y(t))^2), \frac{d}{dt}y(t) = \begin{cases} (x(t))^2 + (y(t))^2 & 2x(t) \leq 0 \\ \left(1/2 x(t) - 1/2 \frac{(y(t))^2}{x(t)}\right) ((x(t))^2 + (y(t))^2) & \text{otherwise} \end{cases} \end{array} \right.$$

**Mathematica:** cpu = 2.354299 (sec), leaf count = 86

$$\text{DSolve} \left[ \left\{ \begin{array}{l} x'(t) = -y(t) (x(t)^2 + y(t)^2), y'(t) = \begin{cases} x(t)^2 + y(t)^2 & x(t)^2 + y(t)^2 \geq 2x(t) \\ (x(t)^2 + y(t)^2) \left(\frac{x(t)}{2} - \frac{y(t)^2}{2x(t)}\right) & \text{True} \end{cases} \end{array} \right. \right]$$

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

### 10.10 ODE No. 1922

$$\left\{ \begin{array}{l} \frac{d}{dt}x(t) = -y(t) + \begin{cases} x(t) ((x(t))^2 + (y(t))^2 - 1) \sin \left( ((x(t))^2 + (y(t))^2)^{-1} \right) & (x(t))^2 + (y(t))^2 \neq 1 \\ 0 & \text{otherwise} \end{cases} \end{array} \right., \frac{d}{dt}y(t) = \dots$$

**Mathematica:** cpu = 11.112911 (sec), leaf count = 106

$$\text{DSolve} \left[ \left\{ \begin{array}{l} x'(t) = \begin{cases} \sin \left( \frac{1}{x(t)^2 + y(t)^2} \right) x(t) (x(t)^2 + y(t)^2 - 1) & x(t)^2 + y(t)^2 \neq 1 \\ 0 & \text{True} \end{cases} \end{array} \right. \right] - y(t), y'(t) = \dots$$

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

### 10.11 ODE No. 1923

$$\left\{ (t^2 + 1) \frac{d}{dt}x(t) = -tx(t) + y(t), (t^2 + 1) \frac{d}{dt}y(t) = -x(t) - ty(t) \right\}$$

**Mathematica:** cpu = 0.685587 (sec), leaf count = 53

$$\left\{ \left\{ x(t) \rightarrow \frac{c_1}{t^2 + 1} + \frac{c_2 t}{t^2 + 1}, y(t) \rightarrow \frac{c_2}{t^2 + 1} - \frac{c_1 t}{t^2 + 1} \right\} \right\}$$

**Maple:** cpu = 0.062 (sec), leaf count = 35

$$\left\{ \left\{ x(t) = \frac{-C1 t + -C2}{t^2 + 1}, y(t) = \frac{-t - C2 + -C1}{t^2 + 1} \right\} \right\}$$

### 10.12 ODE No. 1924

$$\left\{ \left( (x(t))^2 + (y(t))^2 - t^2 \right) \frac{d}{dt} x(t) = -2tx(t), \left( (x(t))^2 + (y(t))^2 - t^2 \right) \frac{d}{dt} y(t) = -2ty(t) \right\}$$

**Mathematica:** cpu = 0.071009 (sec), leaf count = 191

$$\left\{ \left\{ y(t) \rightarrow \frac{c_1 \left( e^{c_2} - \sqrt{-4c_1^2 t^2 + e^{2c_2} - 4t^2} \right)}{2(c_1^2 + 1)}, x(t) \rightarrow \frac{e^{c_2} - \sqrt{-4c_1^2 t^2 + e^{2c_2} - 4t^2}}{2(c_1^2 + 1)} \right\}, \left\{ y(t) \rightarrow \frac{c_1 \left( \sqrt{-4c_1^2 t^2 + e^{2c_2} - 4t^2} \right)}{2(c_1^2 + 1)}, x(t) \rightarrow \frac{e^{c_2} - \sqrt{-4c_1^2 t^2 + e^{2c_2} - 4t^2}}{2(c_1^2 + 1)} \right\} \right\}$$

**Maple:** cpu = 0.234 (sec), leaf count = 186

$$\left\{ \left[ \{x(t) = 0\}, \left\{ y(t) = \frac{1}{2\_C1} \left( 1 + \sqrt{-4\_C1^2 t^2 + 1} \right), y(t) = -\frac{1}{2\_C1} \left( -1 + \sqrt{-4\_C1^2 t^2 + 1} \right) \right\} \right], \left[ \{x(t) = \frac{1}{2\_C1} \left( 1 + \sqrt{-4\_C1^2 t^2 + 1} \right), y(t) = \frac{1}{2\_C1} \left( -1 + \sqrt{-4\_C1^2 t^2 + 1} \right)\}, \{x(t) = -\frac{1}{2\_C1} \left( 1 + \sqrt{-4\_C1^2 t^2 + 1} \right), y(t) = -\frac{1}{2\_C1} \left( -1 + \sqrt{-4\_C1^2 t^2 + 1} \right)\} \right] \right\}$$

### 10.13 ODE No. 1925

$$\left\{ \left( \frac{d}{dt} x(t) \right) \frac{d}{dt} y(t) + t \frac{d}{dt} y(t) - y(t) = 0, \left( \frac{d}{dt} x(t) \right)^2 + t \frac{d}{dt} x(t) + a \frac{d}{dt} y(t) - x(t) = 0 \right\}$$

**Mathematica:** cpu = 8.399567 (sec), leaf count = 55

$$\text{DSolve}[\{ay'(t) + tx'(t) - x(t) + y'(t)^2 = 0, x'(t)y'(t) + ty'(t) - y(t) = 0\}, \{x(t), y(t)\}, t]$$

**Maple:** cpu = 0.219 (sec), leaf count = 226

$$\left\{ \left[ \left\{ x(t) = -\frac{t^2}{3} \right\}, \left\{ y(t) = -\frac{t^3}{27a} \right\} \right], \left[ \{x(t) = \_C1 t + \_C2\}, \left\{ y(t) = \frac{-\left(\frac{d}{dt} x(t)\right)^3 - 2\left(\frac{d}{dt} x(t)\right)^2 t - \left(\frac{d}{dt} x(t)\right)}{a} \right\} \right] \right\}$$

### 10.14 ODE No. 1926

$$\left\{ x(t) = t \frac{d}{dt} x(t) + f\left(\frac{d}{dt} x(t), \frac{d}{dt} y(t)\right), y(t) = t \frac{d}{dt} y(t) + g\left(\frac{d}{dt} x(t), \frac{d}{dt} y(t)\right) \right\}$$

**Mathematica:** cpu = 0.005501 (sec), leaf count = 46

$$\text{DSolve}[\{x(t) = f(x'(t), y'(t)) + tx'(t), y(t) = g(x'(t), y'(t)) + ty'(t)\}, \{x(t), y(t)\}, t]$$

**Maple:** cpu = 0.078 (sec), leaf count = 96

$$\left\{ \left[ \int \text{RootOf}\left(t \frac{d}{dt} y(t) + g\left(-Z, \frac{d}{dt} y(t)\right) - y(t)\right) dt + \_C1 = t \text{RootOf}\left(t \frac{d}{dt} y(t) + g\left(-Z, \frac{d}{dt} y(t)\right) - y(t)\right) \right] \right\}$$

### 10.15 ODE No. 1927

$$\left\{ \frac{d^2}{dt^2}x(t) = ae^{2x(t)} - e^{-x(t)} + e^{-2x(t)}(\cos(y(t)))^2, \frac{d^2}{dt^2}y(t) = e^{-2x(t)} \sin(y(t)) \cos(y(t)) - \frac{\sin(y(t))}{(\cos(y(t)))^3} \right\}$$

**Mathematica:** cpu = 0 (sec), leaf count = 0

Hanged

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

### 10.16 ODE No. 1928

$$\left\{ \frac{d^2}{dt^2}x(t) = \frac{kx(t)}{((x(t))^2 + (y(t))^2)^{3/2}}, \frac{d^2}{dt^2}y(t) = \frac{ky(t)}{((x(t))^2 + (y(t))^2)^{3/2}} \right\}$$

**Mathematica:** cpu = 0.007001 (sec), leaf count = 52

$$\text{DSolve} \left[ \left\{ x''(t) = \frac{kx(t)}{(x(t)^2 + y(t)^2)^{3/2}}, y''(t) = \frac{ky(t)}{(x(t)^2 + y(t)^2)^{3/2}} \right\}, \{x(t), y(t)\}, t \right]$$

**Maple:** cpu = 0 (sec), leaf count = 0

hanged

### 10.17 ODE No. 1929

$$\left\{ \frac{d^2}{dt^2}x(t) = -\frac{C(y(t)) f\left(\sqrt{\left(\frac{d}{dt}y(t)\right)^2}\right) \frac{d}{dt}x(t)}{\sqrt{\left(\frac{d}{dt}y(t)\right)^2}}, \frac{d^2}{dt^2}y(t) = -\frac{C(y(t)) f\left(\sqrt{\left(\frac{d}{dt}y(t)\right)^2}\right) \frac{d}{dt}y(t)}{\sqrt{\left(\frac{d}{dt}y(t)\right)^2}} - g \right\}$$

**Mathematica:** cpu = 0.008001 (sec), leaf count = 110

$$\text{DSolve} \left[ \left\{ x''(t) = -\frac{cy(t)x'(t)f\left(\sqrt{x'(t)^2 + y'(t)^2}\right)}{\sqrt{x'(t)^2 + y'(t)^2}}, y''(t) = -\frac{cy(t)y'(t)f\left(\sqrt{x'(t)^2 + y'(t)^2}\right)}{\sqrt{x'(t)^2 + y'(t)^2}} - g \right\}, \{x(t), y(t)\}, t \right]$$

**Maple:** cpu = 2.247 (sec), leaf count = 116

$$\left\{ \left[ \left\{ y(t) = \text{ODESolStruc} \left( -a, \left[ \left( \frac{d}{d\_a} b(-a) \right) - b(-a) + 1 \left( C(-a) f \left( \sqrt{(-b(-a))^2} \right) - b(-a) + g \sqrt{\dots} \right) \right] \right) \right. \right. \right.$$



**10.18 ODE No. 1930**

$$\left\{ \frac{d}{dt}x(t) = y(t) - z(t), \frac{d}{dt}y(t) = (x(t))^2 + y(t), \frac{d}{dt}z(t) = (x(t))^2 + z(t) \right\}$$

**Mathematica:** cpu = 0.052507 (sec), leaf count = 308

$$\left\{ \left\{ x(t) \rightarrow e^{-c_3} (e^{c_3} c_1 + e^t), y(t) \rightarrow c_2 (e^{-c_3} (e^{c_3} c_1 + e^t) - c_1) + (e^{-c_3} (e^{c_3} c_1 + e^t) - c_1) \left( -\frac{c_1^2}{e^{-c_3} (e^{c_3} c_1 + e^t)} \right) \right\} \right\}$$

**Maple:** cpu = 0.047 (sec), leaf count = 45

$$\left\{ \left[ \left\{ x(t) = \_C2 + \_C3 e^t \right\}, \left\{ y(t) = \left( \int (x(t))^2 e^{-t} dt + \_C1 \right) e^t \right\}, \left\{ z(t) = -\frac{d}{dt}x(t) + y(t) \right\} \right] \right\}$$

**10.19 ODE No. 1931**

$$\left\{ a \frac{d}{dt}x(t) = (b - c) y(t) z(t), b \frac{d}{dt}y(t) = (c - a) z(t) x(t), c \frac{d}{dt}z(t) = (a - b) x(t) y(t) \right\}$$

**Mathematica:** cpu = 6.037767 (sec), leaf count = 10101

$$\left\{ \left\{ x(t) \rightarrow \frac{\sqrt{2}b^2 \sqrt{a(a-c)}c_1 \operatorname{sn} \left( \frac{\sqrt{2}\sqrt{a}\sqrt{a-c}\sqrt{c_2}t - \sqrt{2}\sqrt{a}\sqrt{b}\sqrt{a-c}\sqrt{c_2}t - \frac{\sqrt{2}\sqrt{a}\sqrt{a-c}\sqrt{c_2}c_3}{a} + \frac{\sqrt{2}\sqrt{a}\sqrt{b}\sqrt{a-c}\sqrt{c_2}c_3}{\sqrt{b-c}} \right) - \frac{(a-b)bc_1}{(a-c)cc_2}}{(a-c)\sqrt{b(b-c)}c_1} \right\} \right\}$$

**Maple:** cpu = 0.514 (sec), leaf count = 1356

$$\left\{ \left[ \left\{ x(t) = 0 \right\}, \left\{ y(t) = 0 \right\}, \left\{ z(t) = \_C1 \right\} \right], \left[ \left\{ x(t) = 0 \right\}, \left\{ y(t) = \_C1 \right\}, \left\{ z(t) = 0 \right\} \right], \left[ \left\{ x(t) = \_C1 \right\}, \left\{ y(t) = 0 \right\}, \left\{ z(t) = 0 \right\} \right] \right\}$$

## 10.20 ODE No. 1932

$$\left\{ \frac{d}{dt}x(t) = x(t)(y(t) - z(t)), \frac{d}{dt}y(t) = y(t)(z(t) - x(t)), \frac{d}{dt}z(t) = z(t)(x(t) - y(t)) \right\}$$

**Mathematica:** cpu = 2.251786 (sec), leaf count = 55

DSolve[{x'(t) = x(t)(y(t) - z(t)), y'(t) = y(t)(z(t) - x(t)), z'(t) = z(t)(x(t) - y(t))}, {x(t), y(t), z(t)}, t]

**Maple:** cpu = 0.686 (sec), leaf count = 393

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## 10.21 ODE No. 1933

$$\left\{ \frac{d}{dt}x(t) + \frac{d}{dt}y(t) = x(t)y(t), \frac{d}{dt}x(t) + \frac{d}{dt}z(t) = x(t)z(t), \frac{d}{dt}y(t) + \frac{d}{dt}z(t) = y(t)z(t) \right\}$$

**Mathematica:** cpu = 126.589075 (sec), leaf count = 55

DSolve[{x'(t) + y'(t) = x(t)y(t), y'(t) + z'(t) = y(t)z(t), x'(t) + z'(t) = x(t)z(t)}, {x(t), y(t), z(t)}, t]

**Maple:** cpu = 1.529 (sec), leaf count = 17743

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## 10.22 ODE No. 1934

$$\left\{ \frac{d}{dt}x(t) = 1/2(x(t))^2 - 1/24y(t), \frac{d}{dt}y(t) = 2x(t)y(t) - 3z(t), \frac{d}{dt}z(t) = 3x(t)z(t) - 1/6(y(t))^2 \right\}$$

**Mathematica:** cpu = 72.632223 (sec), leaf count = 66

DSolve[{x'(t) = x(t)^2/2 - y(t)/24, y'(t) = 2x(t)y(t) - 3z(t), z'(t) = 3x(t)z(t) - y(t)^2/6}, {x(t), y(t), z(t)}, t]

**Maple:** cpu = 0.904 (sec), leaf count = 376

$$\left\{ \{y(t) = 0\}, \{x(t) = 2(2\_C1 - t)^{-1}\}, \{z(t) = 0\}, \{y(t) = 256(\_C1 t + \_C2)^{-4}\}, \left\{ x(t) = \frac{1}{2y(t)} \right\} \right\}$$

### 10.23 ODE No. 1935

$$\left\{ \frac{d}{dt}x(t) = x(t) ((y(t))^2 - (z(t))^2), \frac{d}{dt}y(t) = y(t) ((z(t))^2 - (x(t))^2), \frac{d}{dt}z(t) = z(t) ((x(t))^2 - (y(t))^2) \right\}$$

**Mathematica:** cpu = 0.050506 (sec), leaf count = 67

DSolve[{x'(t) = x(t) (y(t)^2 - z(t)^2), y'(t) = y(t) (z(t)^2 - x(t)^2), z'(t) = z(t) (x(t)^2 - y(t)^2)}, {x(t), y(t)}

**Maple:** cpu = 1.357 (sec), leaf count = 741

$$\left\{ \{x(t) = 0\}, \{y(t) = 0\}, \{z(t) = \_C1\}, [\{x(t) = 0\}], \left\{ y(t) = \frac{1}{(e^{-C2-C1})^2 (e^{-C1t})^2 - 1} \sqrt{((e^{-C2-C1})^2)} \right\} \right.$$

### 10.24 ODE No. 1936

$$\left\{ \frac{d}{dt}x(t) = x(t) ((y(t))^2 - (z(t))^2), \frac{d}{dt}y(t) = -y(t) ((z(t))^2 + (x(t))^2), \frac{d}{dt}z(t) = z(t) ((x(t))^2 + (y(t))^2) \right\}$$

**Mathematica:** cpu = 0.048006 (sec), leaf count = 64

DSolve[{x'(t) = x(t) (y(t)^2 - z(t)^2), y'(t) = -y(t) (x(t)^2 + z(t)^2), z'(t) = z(t) (x(t)^2 + y(t)^2)}, {x(t), y(t)}

**Maple:** cpu = 0.531 (sec), leaf count = 704

$$\left\{ \{x(t) = 0\}, \{y(t) = 0\}, \{z(t) = \_C1\}, [\{x(t) = 0\}], \left\{ y(t) = \frac{1}{(e^{-C2-C1})^2 (e^{-C1t})^2 - 1} \sqrt{-((e^{-C2-C1})^2)} \right\} \right.$$

### 10.25 ODE No. 1937

$$\begin{aligned} x'(t) &= -x(t)y(t)^2 + x(t) + y(t) \\ y'(t) &= x(t)^2y(t) - x(t) - y(t) \\ z'(t) &= y(t)^2 - x(t)^2 \end{aligned}$$

**Mathematica:** cpu = 0.266534 (sec), leaf count = 65

DSolve[{x'(t) = -x(t)y(t)^2 + x(t) + y(t), y'(t) = x(t)^2y(t) - x(t) - y(t), z'(t) = y(t)^2 - x(t)^2}, {x(t), y(t)}

**Maple:** cpu = 0.608 (sec), leaf count = 304

$$\left\{ \left[ \{x(t) = 0\}, \{y(t) = 0\}, \{z(t) = \_C1\} \right], \left[ x(t) = \text{ODESolStruc} \left( \_a, \left[ \left( \frac{d}{d\_a} \_b(\_a) \right) \_b(\_a) - \frac{1}{2} \right] \right) \right] \right\}$$

## 10.26 ODE No. 1938

$$\begin{aligned} x''(t) &= \frac{\partial F}{\partial x} \\ y''(t) &= \frac{\partial F}{\partial y} \\ z''(t) &= \frac{\partial F}{\partial z} \end{aligned}$$

Where  $F = F(r)$  and  $r = \sqrt{x(t)^2 + y(t)^2 + z(t)^2}$

**Mathematica:** cpu = 0.011001 (sec), leaf count = 137

$$\left\{ \left\{ x(t) \rightarrow c_1 e^{-\frac{t\sqrt{f'(r)}}{\sqrt{r}}} + c_2 e^{\frac{t\sqrt{f'(r)}}{\sqrt{r}}}, y(t) \rightarrow c_3 e^{-\frac{t\sqrt{f'(r)}}{\sqrt{r}}} + c_4 e^{\frac{t\sqrt{f'(r)}}{\sqrt{r}}}, z(t) \rightarrow c_5 e^{-\frac{t\sqrt{f'(r)}}{\sqrt{r}}} + c_6 e^{\frac{t\sqrt{f'(r)}}{\sqrt{r}}} \right\} \right\}$$

**Maple:** cpu = 0.078 (sec), leaf count = 101

$$\left\{ \left\{ x(t) = \_C5 e^{t\sqrt{\frac{d}{dr}F(r)}\frac{1}{\sqrt{r}}} + \_C6 e^{-t\sqrt{\frac{d}{dr}F(r)}\frac{1}{\sqrt{r}}}, y(t) = \_C3 e^{t\sqrt{\frac{d}{dr}F(r)}\frac{1}{\sqrt{r}}} + \_C4 e^{-t\sqrt{\frac{d}{dr}F(r)}\frac{1}{\sqrt{r}}}, z(t) = \_C1 \right\} \right\}$$

## 10.27 ODE No. 1939

$$\begin{aligned} (x(t) - y(t))(x(t) - z(t))x'(t) &= f(t) \\ (y(t) - x(t))(y(t) - z(t))y'(t) &= f(t) \\ (z(t) - x(t))(z(t) - y(t))z'(t) &= f(t) \end{aligned}$$

**Mathematica:** cpu = 0.011501 (sec), leaf count = 76

DSolve[{(x(t) - y(t))(x(t) - z(t))x'(t) = f(t), (y(t) - x(t))(y(t) - z(t))y'(t) = f(t), (z(t) - x(t))(z(t) - y(t))z'(t) = f(t)}, {x[t], y[t], z[t]}, t]

**Maple:** cpu = 1.030 (sec), leaf count = 1121

$$\left\{ \left\{ x(t) = \int 6 \frac{f(t)}{\_C1^3 + 11664 \_C2^2 - 23328 \_C2 \int f(t) dt + 11664 (\int f(t) dt)^2} \left( -C1^4 + 11664 \left( \int f(t) dt \right)^2 \right) dt \right\} \right\}$$

**10.28 ODE No. 1940**

$$\begin{aligned}x_1'(t) \sin(x_2(t)) &= x_4(t) \sin(x_3(t)) + x_5(t) \cos(x_3(t)) \\x_2'(t) &= x_4(t) \cos(x_3(t)) - x_5(t) \sin(x_3(t)) \\x_1'(t) \cos(x_2(t)) + x_3'(t) &= a \\x_4'(t) - a(1 - \lambda)x_5(t) &= -m \sin(x_2(t)) \cos(x_3(t)) \\a(1 - \lambda)x_4(t) + x_5'(t) &= m \sin(x_2(t)) \sin(x_3(t))\end{aligned}$$

**Mathematica:** cpu = 0.007001 (sec), leaf count = 118

`DSolve[{x1'(t) sin(x2(t)) = x4(t) sin(x3(t)) + x5(t) cos(x3(t)), x2'(t) = x4(t) cos(x3(t)) - x5(t) sin(x3(t))`

**Maple:** cpu = 0 (sec), leaf count = 0

hanged