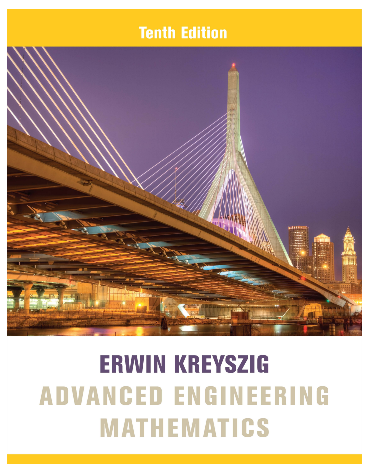
A Solution Manual For

ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011



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October 12, 2023

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1 Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.1. page 174

1.1 problem 6

Internal problem ID [4869]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.1. page 174
Problem number: 6.
ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type `[_separable]`

$$\boxed{y'(x+1) - y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 11

```
Order:=6;
dsolve((1+x)*diff(y(x),x)=y(x),y(x),type='series',x=0);
```

$$y(x) = y(0)(x+1)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 9

```
AsymptoticDSolveValue[(1+x)*y'[x]==y[x],y[x],{x,0,5}]
```

$$y(x) \to c_1(x+1)$$

1.2 problem 7

Internal problem ID [4870]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.1. page 174
Problem number: 7.
ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type `[_separable]`

$$\boxed{2xy + y' = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 21

```
Order:=6;
dsolve(diff(y(x),x)=-2*x*y(x),y(x),type='series',x=0);
```

$$y(x) = \left(1 - x^2 + \frac{1}{2}x^4\right) y(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 20

```
AsymptoticDSolveValue[y'[x]==-2*x*y[x],y[x],{x,0,5}]
```

$$y(x) \rightarrow c_1 \left(\frac{x^4}{2} - x^2 + 1\right)$$

1.3 problem 8

Internal problem ID [4871]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.1. page 174
Problem number: 8.
ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type `[_separable]`

$$\boxed{y'x - 3y - k = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 24

```
Order:=6;
dsolve(x*diff(y(x),x)-3*y(x)=k,y(x),type='series',x=0);
```

$$y(x) = c_1 x^3 (1 + O(x^6)) + \left(-\frac{k}{3} + O(x^6)\right)$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 15

```
AsymptoticDSolveValue[x*y'[x]-3*y[x]==k,y[x],{x,0,5}]
```

$$y(x) \to -\frac{k}{3} + c_1 x^3$$

1.4 problem 9

Internal problem ID [4872]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.1. page 174
Problem number: 9.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$\boxed{y'' + y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 34

```
Order:=6;
dsolve(diff(y(x),x$2)+y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \left(1 - \frac{1}{2}x^2 + \frac{1}{24}x^4\right) y(0) + \left(x - \frac{1}{6}x^3 + \frac{1}{120}x^5\right) D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 42

```
AsymptoticDSolveValue[y''[x]+y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2\left(\frac{x^5}{120} - \frac{x^3}{6} + x\right) + c_1\left(\frac{x^4}{24} - \frac{x^2}{2} + 1\right)$$

1.5 problem 10

Internal problem ID [4873]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.1. page 174
Problem number: 10.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{y'' - y' + xy = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 49

```
Order:=6;
dsolve(diff(y(x),x$2)-diff(y(x),x)+x*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \left(1 - \frac{1}{6}x^3 - \frac{1}{24}x^4 - \frac{1}{120}x^5\right) y(0) + \left(x + \frac{1}{2}x^2 + \frac{1}{6}x^3 - \frac{1}{24}x^4 - \frac{1}{30}x^5\right) D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 63

```
AsymptoticDSolveValue[y''[x]-y'[x]+x*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(-\frac{x^5}{120} - \frac{x^4}{24} - \frac{x^3}{6} + 1\right) + c_2\left(-\frac{x^5}{30} - \frac{x^4}{24} + \frac{x^3}{6} + \frac{x^2}{2} + x\right)$$

1.6 problem 11

Internal problem ID [4874]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.1. page 174
Problem number: 11.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{y'' - y' + x^2 y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 44

```
Order:=6;
dsolve(diff(y(x),x$2)-diff(y(x),x)+x^2*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \left(1 - \frac{1}{12}x^4 - \frac{1}{60}x^5\right) y(0) + \left(x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 - \frac{1}{24}x^5\right) D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 56

```
AsymptoticDSolveValue[y''[x]-y'[x]+x^2*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1 \left(-\frac{x^5}{60} - \frac{x^4}{12} + 1\right) + c_2 \left(-\frac{x^5}{24} + \frac{x^4}{24} + \frac{x^3}{6} + \frac{x^2}{2} + x\right)$$

1.7 problem 12

Internal problem ID [4875]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.1. page 174
Problem number: 12.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[_Gegenbauer]`

$$\boxed{(-x^2+1)\,y''-2y'x+2y=0}$$

With the expansion point for the power series method at $x=0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 24

```
Order:=6;
dsolve((1-x^2)*diff(y(x),x$2)-2*x*diff(y(x),x)+2*y(x)=0,y(x),type='series',x=0);
```

$$y(x)=\left(1-x^2-\frac{1}{3}x^4\right)y(0)+D(y)\,(0)\,x+O\left(x^6\right)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 25

```
AsymptoticDSolveValue[(1-x^2)*y''[x]-2*x*y'[x]+2*y[x]==0,y[x],{x,0,5}]
```

$$y(x)\to c_1\left(-\frac{x^4}{3}-x^2+1\right)+c_2x$$

1.8 problem 13

Internal problem ID [4876]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.1. page 174
Problem number: 13.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{y'' + y(x^2 + 1) = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 34

```
Order:=6;
dsolve(diff(y(x),x$2)+(1+x^2)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \left(1 - \frac{1}{2}x^2 - \frac{1}{24}x^4\right) y(0) + \left(x - \frac{1}{6}x^3 - \frac{1}{24}x^5\right) D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 42

```
AsymptoticDSolveValue[y''[x]+(1+x^2)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2\left(-\frac{x^5}{24} - \frac{x^3}{6} + x\right) + c_1\left(-\frac{x^4}{24} - \frac{x^2}{2} + 1\right)$$

1.9 problem 14

Internal problem ID [4877]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.1. page 174
Problem number: 14.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{y'' - 4y'x + (4x^2 - 2)\, y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 30

```
Order:=6;
dsolve(diff(y(x),x$2)-4*x*diff(y(x),x)+(4*x^2-2)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \left(1 + x^2 + \frac{1}{2}x^4\right) y(0) + \left(x + x^3 + \frac{1}{2}x^5\right) D(y)\,(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 34

```
AsymptoticDSolveValue[y''[x]-4*x*y'[x]+(4*x^2-2)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2\left(\frac{x^5}{2} + x^3 + x\right) + c_1\left(\frac{x^4}{2} + x^2 + 1\right)$$

1.10 problem 16

Internal problem ID [4878]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.1. page 174
Problem number: 16.
ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type `[_quadrature]`

$$\boxed{4y + y' - 1 = 0}$$

With initial conditions

$$\left[y(0) = \frac{5}{4}\right]$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 20

```
Order:=6;
dsolve([diff(y(x),x)+4*y(x)=1,y(0) = 5/4],y(x),type='series',x=0);
```

$$y(x) = \frac{5}{4} - 4x + 8x^2 - \frac{32}{3}x^3 + \frac{32}{3}x^4 - \frac{128}{15}x^5 + \mathrm{O}\left(x^6\right)$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 36

```
AsymptoticDSolveValue[{y'[x]+4*y[x]==1,{y[0]==125/100}},y[x],{x,0,5}]
```

$$y(x) \to -\frac{128x^5}{15} + \frac{32x^4}{3} - \frac{32x^3}{3} + 8x^2 - 4x + \frac{5}{4}$$

1.11 problem 17

Internal problem ID [4879]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.1. page 174
Problem number: 17.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{y'' + 3y'x + 2y = 0}$$

With initial conditions

$$[y(0) = 1, y'(0) = 1]$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 20

```
Order:=6;
dsolve([diff(y(x),x$2)+3*x*diff(y(x),x)+2*y(x)=0,y(0) = 1, D(y)(0) = 1],y(x),type='series',x=
```

$$y(x) = 1 + x - x^2 - \frac{5}{6}x^3 + \frac{2}{3}x^4 + \frac{11}{24}x^5 + \mathrm{O}\left(x^6\right)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 32

```
AsymptoticDSolveValue[{y''[x]+3*x*y'[x]+2*y[x]==0,{y[0]==1,y'[0]==1}},y[x],{x,0,5}]
```

$$y(x) \to \frac{11x^5}{24} + \frac{2x^4}{3} - \frac{5x^3}{6} - x^2 + x + 1$$

1.12 problem 18

Internal problem ID [4880]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.1. page 174
Problem number: 18.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[_Gegenbauer]`

$$\boxed{(-x^2+1)\,y''-2y'x+30y=0}$$

With initial conditions

$$\left[y(0)=0, y'(0)=\frac{15}{8}\right]$$

With the expansion point for the power series method at $x=0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 14

```
Order:=6;
dsolve([(1-x^2)*diff(y(x),x$2)-2*x*diff(y(x),x)+30*y(x)=0,y(0) = 0, D(y)(0) = 15/8],y(x),type
```

$$y(x)=\frac{15}{8}x-\frac{35}{4}x^3+\frac{63}{8}x^5+\mathrm{O}\left(x^6\right)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 23

```
AsymptoticDSolveValue[{(1-x^2)*y''[x]-2*x*y'[x]+30*y[x]==0,{y[0]==0,y'[0]==1875/1000}},y[x],{
```

$$y(x)\to\frac{63x^5}{8}-\frac{35x^3}{4}+\frac{15x}{8}$$

1.13 problem 19

Internal problem ID [4881]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.1. page 174
Problem number: 19.
ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type `[_separable]`

$$\boxed{(x-2)\,y'-xy=0}$$

With initial conditions

$$[y(0)=4]$$

With the expansion point for the power series method at $x=0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 16

```
Order:=6;
dsolve([(x-2)*diff(y(x),x)=x*y(x),y(0) = 4],y(x),type='series',x=0);
```

$$y(x)=4-x^2-\frac{1}{3}x^3+\frac{1}{30}x^5+\mathrm{O}\left(x^6\right)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 24

```
AsymptoticDSolveValue[{(x-2)*y'[x]==x*y[x],{y[0]==4}},y[x],{x,0,5}]
```

$$y(x)\to\frac{x^5}{30}-\frac{x^3}{3}-x^2+4$$

2 Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186

2.1 problem 2

Internal problem ID [4882]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 2.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _exact, _linear, _homogeneous]]`

$$\boxed{(x-2)^2 y'' + (2+x) y' - y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 44

```
Order:=6;
dsolve((x-2)^2*diff(y(x),x$2)+(x+2)*diff(y(x),x)-y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \left(1 + \frac{1}{8}x^2 + \frac{1}{48}x^3 - \frac{1}{480}x^5\right) y(0) + \left(x - \frac{1}{4}x^2 - \frac{1}{24}x^3 + \frac{1}{240}x^5\right) D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 56

```
AsymptoticDSolveValue[(x-2)^2*y''[x]+(x+2)*y'[x]-y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(-\frac{x^5}{480} + \frac{x^3}{48} + \frac{x^2}{8} + 1\right) + c_2\left(\frac{x^5}{240} - \frac{x^3}{24} - \frac{x^2}{4} + x\right)$$

2.2 problem 3

Internal problem ID [4883]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 3.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[_Lienard]`

$$\boxed{xy'' + 2y' + xy = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 32

```
Order:=6;
dsolve(x*diff(y(x),x$2)+2*diff(y(x),x)+x*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = c_1 \left(1 - \frac{1}{6}x^2 + \frac{1}{120}x^4 + \mathrm{O}\left(x^6\right)\right) + \frac{c_2\left(1 - \frac{1}{2}x^2 + \frac{1}{24}x^4 + \mathrm{O}\left(x^6\right)\right)}{x}$$

✓ Solution by Mathematica

Time used: 0.008 (sec). Leaf size: 42

```
AsymptoticDSolveValue[x*y''[x]+2*y'[x]+x*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1 \left(\frac{x^3}{24} - \frac{x}{2} + \frac{1}{x}\right) + c_2 \left(\frac{x^4}{120} - \frac{x^2}{6} + 1\right)$$

2.3 problem 4

Internal problem ID [4884]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 4.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler]]`

$$\boxed{xy'' + y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 58

```
Order:=6;
dsolve(x*diff(y(x),x$2)+y(x)=0,y(x),type='series',x=0);
```

$$y(x) = c_1 x\left(1 - \frac{1}{2}x + \frac{1}{12}x^2 - \frac{1}{144}x^3 + \frac{1}{2880}x^4 - \frac{1}{86400}x^5 + \mathrm{O}\left(x^6\right)\right) + c_2\left(\ln\left(x\right)\left(-x + \frac{1}{2}x^2 - \frac{1}{12}x^3 + \frac{1}{144}x^4 - \frac{1}{2880}x^5 + \mathrm{O}\left(x^6\right)\right) + \left(1 - \frac{3}{4}x^2 + \frac{7}{36}x^3 - \frac{35}{1728}x^4 + \frac{101}{86400}x^5 + \mathrm{O}\left(x^6\right)\right)\right)$$

✓ Solution by Mathematica

Time used: 0.016 (sec). Leaf size: 85

```
AsymptoticDSolveValue[x*y''[x]+y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(\frac{1}{144}x\left(x^3 - 12x^2 + 72x - 144\right)\log(x) + \frac{-47x^4 + 480x^3 - 2160x^2 + 1728x + 1728}{1728}\right) + c_2\left(\frac{x^5}{2880} - \frac{x^4}{144} + \frac{x^3}{12} - \frac{x^2}{2} + x\right)$$

2.4 problem 5

Internal problem ID [4885]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 5.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{xy'' + (1 + 2x)\, y' + (x + 1)\, y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 43

```
Order:=6;
dsolve(x*diff(y(x),x$2)+(2*x+1)*diff(y(x),x)+(x+1)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \left(1 - x + \frac{1}{2}x^2 - \frac{1}{6}x^3 + \frac{1}{24}x^4 - \frac{1}{120}x^5\right)(\ln(x)\, c_2 + c_1) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 78

```
AsymptoticDSolveValue[x*y''[x]+(2*x+1)*y'[x]+(x+1)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(-\frac{x^5}{120} + \frac{x^4}{24} - \frac{x^3}{6} + \frac{x^2}{2} - x + 1\right) + c_2\left(-\frac{x^5}{120} + \frac{x^4}{24} - \frac{x^3}{6} + \frac{x^2}{2} - x + 1\right)\log(x)$$

2.5 problem 6

Internal problem ID [4886]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 6.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{xy'' + 2x^3y' + (x^2-2)\,y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 58

```
Order:=6;
dsolve(x*diff(y(x),x$2)+2*x^3*diff(y(x),x)+(x^2-2)*y(x)=0,y(x),type='series',x=0);
```

$$\begin{aligned} y(x) = {} & c_1 x\left(1 + x + \frac{1}{3}x^2 - \frac{7}{36}x^3 - \frac{97}{360}x^4 - \frac{517}{5400}x^5 + \mathrm{O}\left(x^6\right)\right) \\ & + c_2\left(\ln(x)\left(2x + 2x^2 + \frac{2}{3}x^3 - \frac{7}{18}x^4 - \frac{97}{180}x^5 + \mathrm{O}\left(x^6\right)\right)\right. \\ & \left. + \left(1 - 3x^2 - \frac{31}{18}x^3 - \frac{85}{216}x^4 + \frac{4067}{5400}x^5 + \mathrm{O}\left(x^6\right)\right)\right) \end{aligned}$$

✓ Solution by Mathematica

Time used: 0.018 (sec). Leaf size: 83

```
AsymptoticDSolveValue[x*y''[x]+2*x^3*y'[x]+(x^2-2)*y[x]==0,y[x],{x,0,5}]
```

$$\begin{aligned} y(x) \to {} & c_1\left(\frac{1}{216}\left(-x^4 - 516x^3 - 1080x^2 - 432x + 216\right) - \frac{1}{18}x\left(7x^3 - 12x^2 - 36x - 36\right)\log(x)\right) \\ & + c_2\left(-\frac{97x^5}{360} - \frac{7x^4}{36} + \frac{x^3}{3} + x^2 + x\right) \end{aligned}$$

2.6 problem 7

Internal problem ID [4887]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 7.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{y'' + (x-1)\,y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 49

```
Order:=6;
dsolve(diff(y(x),x$2)+(x-1)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \left(1+\frac{1}{2}x^2-\frac{1}{6}x^3+\frac{1}{24}x^4-\frac{1}{30}x^5\right)y(0)+\left(x+\frac{1}{6}x^3-\frac{1}{12}x^4+\frac{1}{120}x^5\right)D(y)(0)+O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 63

```
AsymptoticDSolveValue[y''[x]+(x-1)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2\left(\frac{x^5}{120}-\frac{x^4}{12}+\frac{x^3}{6}+x\right)+c_1\left(-\frac{x^5}{30}+\frac{x^4}{24}-\frac{x^3}{6}+\frac{x^2}{2}+1\right)$$

2.7 problem 8

Internal problem ID [4888]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 8.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[_Lienard]`

$$\boxed{xy'' + y' + xy = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 41

```
Order:=6;
dsolve(x*diff(y(x),x$2)+diff(y(x),x)+x*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = (\ln(x)\, c_2 + c_1)\left(1 - \frac{1}{4}x^2 + \frac{1}{64}x^4 + \mathrm{O}\left(x^6\right)\right) + \left(\frac{1}{4}x^2 - \frac{3}{128}x^4 + \mathrm{O}\left(x^6\right)\right) c_2$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 60

```
AsymptoticDSolveValue[x*y''[x]+y'[x]+x*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(\frac{x^4}{64} - \frac{x^2}{4} + 1\right) + c_2\left(-\frac{3x^4}{128} + \frac{x^2}{4} + \left(\frac{x^4}{64} - \frac{x^2}{4} + 1\right)\log(x)\right)$$

2.8 problem 9

Internal problem ID [4889]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 9.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[_Jacobi]`

$$\boxed{2x(x-1)\,y''-y'(x+1)+y=0}$$

With the expansion point for the power series method at $x=0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 26

```
Order:=6;
dsolve(2*x*(x-1)*diff(y(x),x$2)-(x+1)*diff(y(x),x)+y(x)=0,y(x),type='series',x=0);
```

$$y(x)=c_1\sqrt{x}\left(1+\mathrm{O}\left(x^6\right)\right)+c_2\left(1+x+\mathrm{O}\left(x^6\right)\right)$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 18

```
AsymptoticDSolveValue[2*x*(x-1)*y''[x]-(x+1)*y'[x]+y[x]==0,y[x],{x,0,5}]
```

$$y(x)\to c_1\sqrt{x}+c_2(x+1)$$

2.9 problem 10

Internal problem ID [4890]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 10.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{xy'' + 2y' + 4xy = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 32

```
Order:=6;
dsolve(x*diff(y(x),x$2)+2*diff(y(x),x)+4*x*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = c_1\left(1 - \frac{2}{3}x^2 + \frac{2}{15}x^4 + \mathrm{O}\left(x^6\right)\right) + \frac{c_2\left(1 - 2x^2 + \frac{2}{3}x^4 + \mathrm{O}\left(x^6\right)\right)}{x}$$

✓ Solution by Mathematica

Time used: 0.008 (sec). Leaf size: 40

```
AsymptoticDSolveValue[x*y''[x]+2*y'[x]+4*x*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(\frac{2x^3}{3} - 2x + \frac{1}{x}\right) + c_2\left(\frac{2x^4}{15} - \frac{2x^2}{3} + 1\right)$$

2.10 problem 11

Internal problem ID [4891]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 11.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{xy'' + (2-2x)\,y' + (x-2)\,y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 44

```
Order:=6;
dsolve(x*diff(y(x),x$2)+(2-2*x)*diff(y(x),x)+(x-2)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = c_1\left(1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \frac{1}{120}x^5 + \mathrm{O}\left(x^6\right)\right) + \frac{c_2\left(1 + 2x + \frac{3}{2}x^2 + \frac{2}{3}x^3 + \frac{5}{24}x^4 + \frac{1}{20}x^5 + \mathrm{O}\left(x^6\right)\right)}{x}$$

✓ Solution by Mathematica

Time used: 0.023 (sec). Leaf size: 58

```
AsymptoticDSolveValue[x*y''[x]+(2-2*x)*y'[x]+(x-2)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(\frac{5x^3}{24} + \frac{2x^2}{3} + \frac{3x}{2} + \frac{1}{x} + 2\right) + c_2\left(\frac{x^4}{24} + \frac{x^3}{6} + \frac{x^2}{2} + x + 1\right)$$

2.11 problem 12

Internal problem ID [4892]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 12.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{x^2y'' + 6y'x + (4x^2 + 6)\, y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 35

```
Order:=6;
dsolve(x^2*diff(y(x),x$2)+6*x*diff(y(x),x)+(4*x^2+6)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \frac{c_1\left(1 - \frac{2}{3}x^2 + \frac{2}{15}x^4 + \mathrm{O}\left(x^6\right)\right) x + c_2\left(1 - 2x^2 + \frac{2}{3}x^4 + \mathrm{O}\left(x^6\right)\right)}{x^3}$$

✓ Solution by Mathematica

Time used: 0.009 (sec). Leaf size: 38

```
AsymptoticDSolveValue[x^2*y''[x]+6*x*y'[x]+(4*x^2+6)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(\frac{1}{x^3} + \frac{2x}{3} - \frac{2}{x}\right) + c_2\left(\frac{2x^2}{15} + \frac{1}{x^2} - \frac{2}{3}\right)$$

2.12 problem 13

Internal problem ID [4893]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 13.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$xy'' + (-2x + 1)\, y' + (x - 1)\, y = 0$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 43

```
Order:=6;
dsolve(x*diff(y(x),x$2)+(1-2*x)*diff(y(x),x)+(x-1)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = (\ln(x)\, c_2 + c_1)\left(1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \frac{1}{120}x^5\right) + O\left(x^6\right)$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 74

```
AsymptoticDSolveValue[x*y''[x]+(1-2*x)*y'[x]+(x-1)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(\frac{x^5}{120} + \frac{x^4}{24} + \frac{x^3}{6} + \frac{x^2}{2} + x + 1\right) + c_2\left(\frac{x^5}{120} + \frac{x^4}{24} + \frac{x^3}{6} + \frac{x^2}{2} + x + 1\right)\log(x)$$

2.13 problem 15

Internal problem ID [4894]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 15.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _exact, _linear, _homogeneous]]`

$$\boxed{2x(1-x)\,y''-(1+6x)\,y'-2y=0}$$

With the expansion point for the power series method at $x=0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 44

```
Order:=6;
dsolve(2*x*(1-x)*diff(y(x),x$2)-(1+6*x)*diff(y(x),x)-2*y(x)=0,y(x),type='series',x=0);
```

$$y(x)=c_1x^{\frac{3}{2}}\left(1+\frac{5}{2}x+\frac{35}{8}x^2+\frac{105}{16}x^3+\frac{1155}{128}x^4+\frac{3003}{256}x^5+\mathrm{O}\left(x^6\right)\right)+c_2\left(1-2x-8x^2-16x^3-\frac{128}{5}x^4-\frac{256}{7}x^5+\mathrm{O}\left(x^6\right)\right)$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 79

```
AsymptoticDSolveValue[2*x*(1-x)*y''[x]-(1+6*x)*y'[x]-2*y[x]==0,y[x],{x,0,5}]
```

$$y(x)\to c_2\left(-\frac{256x^5}{7}-\frac{128x^4}{5}-16x^3-8x^2-2x+1\right)+c_1\left(\frac{3003x^5}{256}+\frac{1155x^4}{128}+\frac{105x^3}{16}+\frac{35x^2}{8}+\frac{5x}{2}+1\right)x^{3/2}$$

2.14 problem 16

Internal problem ID [4895]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 16.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[_Jacobi]`

$$x(1-x)\,y''+\left(\frac{1}{2}+2x\right)y'-2y=0$$

With the expansion point for the power series method at $x=0$.

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 36

```
Order:=6;
dsolve(x*(1-x)*diff(y(x),x$2)+(1/2+2*x)*diff(y(x),x)-2*y(x)=0,y(x),type='series',x=0);
```

$$y(x)=c_1\sqrt{x}\left(1+\frac{1}{2}x-\frac{1}{40}x^2-\frac{1}{560}x^3-\frac{1}{2688}x^4-\frac{1}{8448}x^5+\mathrm{O}\left(x^6\right)\right)+c_2\left(1+4x+\mathrm{O}\left(x^6\right)\right)$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 55

```
AsymptoticDSolveValue[x*(1-x)*y''[x]+(1/2+2*x)*y'[x]-2*y[x]==0,y[x],{x,0,5}]
```

$$y(x)\to c_1\sqrt{x}\left(-\frac{x^5}{8448}-\frac{x^4}{2688}-\frac{x^3}{560}-\frac{x^2}{40}+\frac{x}{2}+1\right)+c_2(4x+1)$$

2.15 problem 17

Internal problem ID [4896]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 17.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler]]`

$$\boxed{4xy'' + y' + 8y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 44

```
Order:=6;
dsolve(4*x*diff(y(x),x$2)+diff(y(x),x)+8*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = c_1 x^{\frac{3}{4}} \left(1 - \frac{8}{7}x + \frac{32}{77}x^2 - \frac{256}{3465}x^3 + \frac{512}{65835}x^4 - \frac{4096}{7571025}x^5 + \mathrm{O}\left(x^6\right)\right) + c_2 \left(1 - 8x + \frac{32}{5}x^2 - \frac{256}{135}x^3 + \frac{512}{1755}x^4 - \frac{4096}{149175}x^5 + \mathrm{O}\left(x^6\right)\right)$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 83

```
AsymptoticDSolveValue[4*x*y''[x]+y'[x]+8*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2 \left(-\frac{4096x^5}{149175} + \frac{512x^4}{1755} - \frac{256x^3}{135} + \frac{32x^2}{5} - 8x + 1\right) + c_1 x^{3/4} \left(-\frac{4096x^5}{7571025} + \frac{512x^4}{65835} - \frac{256x^3}{3465} + \frac{32x^2}{77} - \frac{8x}{7} + 1\right)$$

2.16 problem 18

Internal problem ID [4897]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 18.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{4(t^2 - 3t + 2)\,y'' - 2y' + y = 0}$$

With the expansion point for the power series method at $t = 0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 54

```
Order:=6;
dsolve(4*(t^2-3*t+2)*diff(y(t),t$2)-2*diff(y(t),t)+y(t)=0,y(t),type='series',t=0);
```

$$y(t) = \left(1 - \frac{1}{16}t^2 - \frac{7}{192}t^3 - \frac{73}{3072}t^4 - \frac{1037}{61440}t^5\right) y(0) + \left(t + \frac{1}{8}t^2 + \frac{5}{96}t^3 + \frac{47}{1536}t^4 + \frac{643}{30720}t^5\right) D(y)(0) + O(t^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 70

```
AsymptoticDSolveValue[4*(t^2-3*t+2)*y''[t]-2*y'[t]+y[t]==0,y[t],{t,0,5}]
```

$$y(t) \to c_1\left(-\frac{1037t^5}{61440} - \frac{73t^4}{3072} - \frac{7t^3}{192} - \frac{t^2}{16} + 1\right) + c_2\left(\frac{643t^5}{30720} + \frac{47t^4}{1536} + \frac{5t^3}{96} + \frac{t^2}{8} + t\right)$$

2.17 problem 19

Internal problem ID [4898]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 19.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{2(t^2-5t+6)\,y''+(2t-3)\,y'-8y=0}$$

With the expansion point for the power series method at $t=0$.

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 54

```
Order:=6;
dsolve(2*(t^2-5*t+6)*diff(y(t),t$2)+(2*t-3)*diff(y(t),t)-8*y(t)=0,y(t),type='series',t=0);
```

$$y(t)=\left(1+\frac{1}{3}t^2+\frac{13}{108}t^3+\frac{299}{5184}t^4+\frac{923}{34560}t^5\right)y(0)+\left(t+\frac{1}{8}t^2+\frac{37}{288}t^3+\frac{851}{13824}t^4+\frac{2627}{92160}t^5\right)D(y)(0)+O(t^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 70

```
AsymptoticDSolveValue[2*(t^2-5*t+6)*y''[t]+(2*t-3)*y'[t]-8*y[t]==0,y[t],{t,0,5}]
```

$$y(t)\to c_1\left(\frac{923t^5}{34560}+\frac{299t^4}{5184}+\frac{13t^3}{108}+\frac{t^2}{3}+1\right)+c_2\left(\frac{2627t^5}{92160}+\frac{851t^4}{13824}+\frac{37t^3}{288}+\frac{t^2}{8}+t\right)$$

2.18 problem 20

Internal problem ID [4899]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.3. Extended Power Series Method: Frobenius Method page 186
Problem number: 20.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{3t(t+1)\,y''+ty'-y=0}$$

With the expansion point for the power series method at $t=0$.

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 42

```
Order:=6;
dsolve(3*t*(1+t)*diff(y(t),t$2)+t*diff(y(t),t)-y(t)=0,y(t),type='series',t=0);
```

$$y(t) = c_1 t\left(1+\mathrm{O}\left(t^6\right)\right)+\left(\frac{1}{3}t+\mathrm{O}\left(t^6\right)\right)\ln(t)\,c_2 + \left(1-\frac{1}{3}t-\frac{2}{9}t^2+\frac{7}{81}t^3-\frac{35}{729}t^4+\frac{91}{2916}t^5+\mathrm{O}\left(t^6\right)\right)c_2$$

✓ Solution by Mathematica

Time used: 0.049 (sec). Leaf size: 43

```
AsymptoticDSolveValue[3*t*(1+t)*y''[t]+t*y'[t]-y[t]==0,y[t],{t,0,5}]
```

$$y(t) \to c_1\left(\frac{1}{729}\left(-35t^4+63t^3-162t^2+243t+729\right)+\frac{1}{3}t\log(t)\right)+c_2 t$$

3 Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.4. Bessels Equation page 195

3.1 problem 2

Internal problem ID [4900]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.4. Bessels Equation page 195
Problem number: 2.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$x^2y'' + y'x + \left(x^2 - \frac{4}{49}\right) y = 0$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 35

```
Order:=6;
dsolve(x^2*diff(y(x),x$2)+x*diff(y(x),x)+(x^2-4/49)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \frac{c_2 x^{\frac{4}{7}} \left(1 - \frac{7}{36}x^2 + \frac{49}{4608}x^4 + \mathrm{O}\left(x^6\right)\right) + c_1 \left(1 - \frac{7}{20}x^2 + \frac{49}{1920}x^4 + \mathrm{O}\left(x^6\right)\right)}{x^{\frac{2}{7}}}$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 52

```
AsymptoticDSolveValue[x^2*y''[x]+x*y'[x]+(x^2-4/49)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1 x^{2/7} \left(\frac{49x^4}{4608} - \frac{7x^2}{36} + 1\right) + \frac{c_2 \left(\frac{49x^4}{1920} - \frac{7x^2}{20} + 1\right)}{x^{2/7}}$$

3.2 problem 3

Internal problem ID [4901]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.4. Bessels Equation page 195
Problem number: 3.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler]]`

$$xy'' + y' + \frac{y}{4} = 0$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 59

```
Order:=6;
dsolve(x*diff(y(x),x$2)+diff(y(x),x)+1/4*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = (\ln(x)\, c_2 + c_1)\left(1 - \frac{1}{4}x + \frac{1}{64}x^2 - \frac{1}{2304}x^3 + \frac{1}{147456}x^4 - \frac{1}{14745600}x^5 + \mathrm{O}\left(x^6\right)\right) + \left(\frac{1}{2}x - \frac{3}{64}x^2 + \frac{11}{6912}x^3 - \frac{25}{884736}x^4 + \frac{137}{442368000}x^5 + \mathrm{O}\left(x^6\right)\right) c_2$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 117

```
AsymptoticDSolveValue[x*y''[x]+y'[x]+1/4*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(-\frac{x^5}{14745600} + \frac{x^4}{147456} - \frac{x^3}{2304} + \frac{x^2}{64} - \frac{x}{4} + 1\right) + c_2\left(\frac{137x^5}{442368000} - \frac{25x^4}{884736} + \frac{11x^3}{6912} - \frac{3x^2}{64} + \left(-\frac{x^5}{14745600} + \frac{x^4}{147456} - \frac{x^3}{2304} + \frac{x^2}{64} - \frac{x}{4} + 1\right)\log(x) + \frac{x}{2}\right)$$

3.3 problem 4

Internal problem ID [4902]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.4. Bessels Equation page 195
Problem number: 4.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$y'' + \left(\mathrm{e}^{-2x} - \frac{1}{9}\right) y = 0$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 49

```
Order:=6;
dsolve(diff(y(x),x$2)+(exp(-2*x)-1/9)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \left(1-\frac{4}{9}x^2+\frac{1}{3}x^3-\frac{65}{486}x^4+\frac{1}{135}x^5\right) y(0)+\left(x-\frac{4}{27}x^3+\frac{1}{6}x^4-\frac{227}{2430}x^5\right) D(y)\,(0)+O\left(x^6\right)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 63

```
AsymptoticDSolveValue[y''[x]+(Exp[-2*x]-1/9)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2\left(-\frac{227x^5}{2430} + \frac{x^4}{6} - \frac{4x^3}{27} + x\right) + c_1\left(\frac{x^5}{135} - \frac{65x^4}{486} + \frac{x^3}{3} - \frac{4x^2}{9} + 1\right)$$

3.4 problem 6

Internal problem ID [4903]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.4. Bessels Equation page 195
Problem number: 6.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{x^2 y'' + \frac{\left(x+\frac{3}{4}\right) y}{4} = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 47

```
Order:=6;
dsolve(x^2*diff(y(x),x$2)+1/4*(x+3/4)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = c_1 x^{\frac{1}{4}} \left(1 - \frac{1}{2}x + \frac{1}{24}x^2 - \frac{1}{720}x^3 + \frac{1}{40320}x^4 - \frac{1}{3628800}x^5 + \mathrm{O}\left(x^6\right)\right) + c_2 x^{\frac{3}{4}} \left(1 - \frac{1}{6}x + \frac{1}{120}x^2 - \frac{1}{5040}x^3 + \frac{1}{362880}x^4 - \frac{1}{39916800}x^5 + \mathrm{O}\left(x^6\right)\right)$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 90

```
AsymptoticDSolveValue[x^2*y''[x]+1/4*(x+3/4)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2 \sqrt[4]{x}\left(-\frac{x^5}{3628800} + \frac{x^4}{40320} - \frac{x^3}{720} + \frac{x^2}{24} - \frac{x}{2} + 1\right) + c_1 x^{3/4}\left(-\frac{x^5}{39916800} + \frac{x^4}{362880} - \frac{x^3}{5040} + \frac{x^2}{120} - \frac{x}{6} + 1\right)$$

3.5 problem 7

Internal problem ID [4904]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.4. Bessels Equation page 195
Problem number: 7.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$x^2y'' + y'x + \frac{(x^2-1)\,y}{4} = 0$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 35

```
Order:=6;
dsolve(x^2*diff(y(x),x$2)+x*diff(y(x),x)+1/4*(x^2-1)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \frac{c_1x\left(1-\frac{1}{24}x^2+\frac{1}{1920}x^4+\mathrm{O}\left(x^6\right)\right)+c_2\left(1-\frac{1}{8}x^2+\frac{1}{384}x^4+\mathrm{O}\left(x^6\right)\right)}{\sqrt{x}}$$

✓ Solution by Mathematica

Time used: 0.009 (sec). Leaf size: 58

```
AsymptoticDSolveValue[x^2*y''[x]+x*y'[x]+1/4*(x^2-1)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(\frac{x^{7/2}}{384}-\frac{x^{3/2}}{8}+\frac{1}{\sqrt{x}}\right)+c_2\left(\frac{x^{9/2}}{1920}-\frac{x^{5/2}}{24}+\sqrt{x}\right)$$

3.6 problem 8

Internal problem ID [4905]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.4. Bessels Equation page 195
Problem number: 8.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$(1+2x)^2 y'' + 2(1+2x)\, y' + 16x(1+x)\, y = 0$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 49

```
Order:=6;
dsolve((2*x+1)^2*diff(y(x),x$2)+2*(2*x+1)*diff(y(x),x)+16*x*(x+1)*y(x)=0,y(x),type='series',x
```

$$y(x) = \left(1 - \frac{8}{3}x^3 + \frac{16}{3}x^4 - \frac{152}{15}x^5\right) y(0) + \left(x - x^2 + \frac{4}{3}x^3 - \frac{10}{3}x^4 + \frac{104}{15}x^5\right) D(y)\,(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 61

```
AsymptoticDSolveValue[(2*x+1)^2*y''[x]+2*(2*x+1)*y'[x]+16*x*(x+1)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(-\frac{152x^5}{15} + \frac{16x^4}{3} - \frac{8x^3}{3} + 1\right) + c_2\left(\frac{104x^5}{15} - \frac{10x^4}{3} + \frac{4x^3}{3} - x^2 + x\right)$$

4 Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.5. Bessel Functions Y(x). General Solution page 200

4.1 problem 1

Internal problem ID [4906]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.5. Bessel Functions Y(x). General Solution page 200
Problem number: 1.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[_Bessel]`

$$\boxed{x^2y'' + y'x + (x^2 - 6)\, y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 97

```
Order:=6;
dsolve(x^2*diff(y(x),x$2)+x*diff(y(x),x)+(x^2-6)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = c_1 x^{-\sqrt{6}} \left(1 + \frac{1}{-4 + 4\sqrt{6}} x^2 + \frac{1}{32} \frac{1}{(-2+\sqrt{6})\,(-1+\sqrt{6})} x^4 + \mathrm{O}\left(x^6\right)\right) + c_2 x^{\sqrt{6}} \left(1 - \frac{1}{4 + 4\sqrt{6}} x^2 + \frac{1}{32} \frac{1}{(2+\sqrt{6})\,(1+\sqrt{6})} x^4 + \mathrm{O}\left(x^6\right)\right)$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 210

```
AsymptoticDSolveValue[x^2*y''[x]+x*y'[x]+(x^2-6)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2\left(\frac{x^4}{\left(-4-\sqrt{6}+\left(1-\sqrt{6}\right)\left(2-\sqrt{6}\right)\right)\left(-2-\sqrt{6}+\left(3-\sqrt{6}\right)\left(4-\sqrt{6}\right)\right)} - \frac{x^2}{-4-\sqrt{6}+\left(1-\sqrt{6}\right)\left(2-\sqrt{6}\right)}+1\right)x^{-\sqrt{6}} + c_1\left(\frac{x^4}{\left(-4+\sqrt{6}+\left(1+\sqrt{6}\right)\left(2+\sqrt{6}\right)\right)\left(-2+\sqrt{6}+\left(3+\sqrt{6}\right)\left(4+\sqrt{6}\right)\right)} - \frac{x^2}{-4+\sqrt{6}+\left(1+\sqrt{6}\right)\left(2+\sqrt{6}\right)}+1\right)x^{\sqrt{6}}$$

4.2 problem 2

Internal problem ID [4907]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.5. Bessel Functions Y(x). General Solution page 200
Problem number: 2.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[_Lienard]`

$$\boxed{xy'' + 5y' + xy = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 44

```
Order:=6;
dsolve(x*diff(y(x),x$2)+5*diff(y(x),x)+x*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \frac{c_1 x^4 \left(1 - \frac{1}{12}x^2 + \frac{1}{384}x^4 + \mathrm{O}\left(x^6\right)\right) + c_2 \left(\ln\left(x\right)\left(9x^4 + \mathrm{O}\left(x^6\right)\right) + \left(-144 - 36x^2 + \mathrm{O}\left(x^6\right)\right)\right)}{x^4}$$

✓ Solution by Mathematica

Time used: 0.008 (sec). Leaf size: 47

```
AsymptoticDSolveValue[x*y''[x]+5*y'[x]+x*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2 \left(\frac{x^4}{384} - \frac{x^2}{12} + 1\right) + c_1 \left(\frac{\left(x^2+8\right)^2}{64x^4} - \frac{\log(x)}{16}\right)$$

4.3 problem 3

Internal problem ID [4908]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.5. Bessel Functions Y(x). General Solution page 200
Problem number: 3.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$9x^2y'' + 9y'x + (36x^4 - 16)\, y = 0$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 31

```
Order:=6;
dsolve(9*x^2*diff(y(x),x$2)+9*x*diff(y(x),x)+(36*x^4-16)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \frac{c_2 x^{\frac{8}{3}}\left(1 - \frac{3}{20}x^4 + \mathrm{O}\left(x^6\right)\right) + c_1\left(1 - \frac{3}{4}x^4 + \mathrm{O}\left(x^6\right)\right)}{x^{\frac{4}{3}}}$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 38

```
AsymptoticDSolveValue[9*x^2*y''[x]+9*x*y'[x]+(36*x^4-16)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(1 - \frac{3x^4}{20}\right)x^{4/3} + \frac{c_2\left(1 - \frac{3x^4}{4}\right)}{x^{4/3}}$$

4.4 problem 4

Internal problem ID [4909]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.5. Bessel Functions Y(x). General Solution page 200
Problem number: 4.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler]]`

$$\boxed{y'' + xy = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 24

```
Order:=6;
dsolve(diff(y(x),x$2)+x*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \left(1 - \frac{x^3}{6}\right) y(0) + \left(x - \frac{1}{12}x^4\right) D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 28

```
AsymptoticDSolveValue[y''[x]+x*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2\left(x - \frac{x^4}{12}\right) + c_1\left(1 - \frac{x^3}{6}\right)$$

4.5 problem 5

Internal problem ID [4910]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.5. Bessel Functions Y(x). General Solution page 200
Problem number: 5.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler]]`

$$\boxed{4xy'' + 4y' + y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 59

```
Order:=6;
dsolve(4*x*diff(y(x),x$2)+4*diff(y(x),x)+y(x)=0,y(x),type='series',x=0);
```

$$y(x) = (\ln(x)\, c_2 + c_1)\left(1 - \frac{1}{4}x + \frac{1}{64}x^2 - \frac{1}{2304}x^3 + \frac{1}{147456}x^4 - \frac{1}{14745600}x^5 + \mathrm{O}\left(x^6\right)\right) + \left(\frac{1}{2}x - \frac{3}{64}x^2 + \frac{11}{6912}x^3 - \frac{25}{884736}x^4 + \frac{137}{442368000}x^5 + \mathrm{O}\left(x^6\right)\right) c_2$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 117

```
AsymptoticDSolveValue[4*x*y''[x]+4*y'[x]+y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(-\frac{x^5}{14745600} + \frac{x^4}{147456} - \frac{x^3}{2304} + \frac{x^2}{64} - \frac{x}{4} + 1\right) + c_2\left(\frac{137x^5}{442368000} - \frac{25x^4}{884736} + \frac{11x^3}{6912} - \frac{3x^2}{64} + \left(-\frac{x^5}{14745600} + \frac{x^4}{147456} - \frac{x^3}{2304} + \frac{x^2}{64} - \frac{x}{4} + 1\right)\log(x) + \frac{x}{2}\right)$$

4.6 problem 6

Internal problem ID [4911]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.5. Bessel Functions Y(x). General Solution page 200
Problem number: 6.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler]]`

$$\boxed{xy'' + y' + 36y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 59

```
Order:=6;
dsolve(x*diff(y(x),x$2)+diff(y(x),x)+36*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = (\ln(x)\, c_2 + c_1)\left(1 - 36x + 324x^2 - 1296x^3 + 2916x^4 - \frac{104976}{25}x^5 + \mathrm{O}\left(x^6\right)\right) + \left(72x - 972x^2 + 4752x^3 - 12150x^4 + \frac{2396952}{125}x^5 + \mathrm{O}\left(x^6\right)\right) c_2$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 93

```
AsymptoticDSolveValue[x*y''[x]+y'[x]+36*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(-\frac{104976x^5}{25} + 2916x^4 - 1296x^3 + 324x^2 - 36x + 1\right) + c_2\left(\frac{2396952x^5}{125} - 12150x^4 + 4752x^3 - 972x^2 + \left(-\frac{104976x^5}{25} + 2916x^4 - 1296x^3 + 324x^2 - 36x + 1\right)\log(x) + 72x\right)$$

4.7 problem 7

Internal problem ID [4912]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.5. Bessel Functions Y(x). General Solution page 200
Problem number: 7.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler]]`

$$\boxed{y'' + k^2x^2y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 30

```
Order:=6;
dsolve(diff(y(x),x$2)+k^2*x^2*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \left(1 - \frac{k^2x^4}{12}\right)y(0) + \left(x - \frac{1}{20}k^2x^5\right)D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 34

```
AsymptoticDSolveValue[y''[x]+k^2*x^2*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2\left(x - \frac{k^2x^5}{20}\right) + c_1\left(1 - \frac{k^2x^4}{12}\right)$$

4.8 problem 8

Internal problem ID [4913]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.5. Bessel Functions Y(x). General Solution page 200
Problem number: 8.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler]]`

$$\boxed{y'' + x^4 k^2 y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 14

```
Order:=6;
dsolve(diff(y(x),x$2)+k^2*x^4*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = y(0) + D(y)(0)\,x + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 10

```
AsymptoticDSolveValue[y''[x]+k^2*x^4*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2 x + c_1$$

4.9 problem 9

Internal problem ID [4914]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. Special Functions. Problem set 5.5. Bessel Functions Y(x). General Solution page 200
Problem number: 9.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[_Lienard]`

$$\boxed{xy'' - 5y' + xy = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 32

```
Order:=6;
dsolve(x*diff(y(x),x$2)-5*diff(y(x),x)+x*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = c_1 x^6 \left(1 - \frac{1}{16}x^2 + \frac{1}{640}x^4 + \mathrm{O}\left(x^6\right)\right) + c_2\left(-86400 - 10800x^2 - 1350x^4 + \mathrm{O}\left(x^6\right)\right)$$

✓ Solution by Mathematica

Time used: 0.008 (sec). Leaf size: 44

```
AsymptoticDSolveValue[x*y''[x]-5*y'[x]+x*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(\frac{x^4}{64} + \frac{x^2}{8} + 1\right) + c_2\left(\frac{x^{10}}{640} - \frac{x^8}{16} + x^6\right)$$

5 Chapter 5. Series Solutions of ODEs. REVIEW QUESTIONS. page 201

5.1 problem 11

Internal problem ID [4915]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. REVIEW QUESTIONS. page 201
Problem number: 11.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$\boxed{y'' + 4y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 34

```
Order:=6;
dsolve(diff(y(x),x$2)+4*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \left(1 - 2x^2 + \frac{2}{3}x^4\right) y(0) + \left(x - \frac{2}{3}x^3 + \frac{2}{15}x^5\right) D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 40

```
AsymptoticDSolveValue[y''[x]+4*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2\left(\frac{2x^5}{15} - \frac{2x^3}{3} + x\right) + c_1\left(\frac{2x^4}{3} - 2x^2 + 1\right)$$

5.2 problem 12

Internal problem ID [4916]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. REVIEW QUESTIONS. page 201
Problem number: 12.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{xy'' + (-2x+1)\,y' + (x-1)\,y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 43

```
Order:=6;
dsolve(x*diff(y(x),x$2)+(1-2*x)*diff(y(x),x)+(x-1)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = (\ln(x)\,c_2 + c_1)\left(1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \frac{1}{120}x^5\right) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 74

```
AsymptoticDSolveValue[x*y''[x]+(1-2*x)*y'[x]+(x-1)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(\frac{x^5}{120} + \frac{x^4}{24} + \frac{x^3}{6} + \frac{x^2}{2} + x + 1\right) + c_2\left(\frac{x^5}{120} + \frac{x^4}{24} + \frac{x^3}{6} + \frac{x^2}{2} + x + 1\right)\log(x)$$

5.3 problem 13

Internal problem ID [4917]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. REVIEW QUESTIONS. page 201
Problem number: 13.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{(x-1)^2 y'' - (x-1) y' - 35y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 54

```
Order:=6;
dsolve((x-1)^2*diff(y(x),x$2)-(x-1)*diff(y(x),x)-35*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \left(1 + \frac{35}{2}x^2 + \frac{35}{6}x^3 + \frac{665}{12}x^4 + \frac{259}{4}x^5\right) y(0) + \left(x - \frac{1}{2}x^2 + \frac{35}{6}x^3 + \frac{35}{12}x^4 + \frac{49}{4}x^5\right) D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 70

```
AsymptoticDSolveValue[(x-1)^2*y''[x]-(x-1)*y'[x]-35*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1 \left(\frac{259x^5}{4} + \frac{665x^4}{12} + \frac{35x^3}{6} + \frac{35x^2}{2} + 1\right) + c_2 \left(\frac{49x^5}{4} + \frac{35x^4}{12} + \frac{35x^3}{6} - \frac{x^2}{2} + x\right)$$

5.4 problem 14

Internal problem ID [4918]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. REVIEW QUESTIONS. page 201
Problem number: 14.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler]]`

$$\boxed{16(1+x)^2 y'' + 3y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 49

```
Order:=6;
dsolve(16*(x+1)^2*diff(y(x),x$2)+3*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = \left(1 - \frac{3}{32}x^2 + \frac{1}{16}x^3 - \frac{93}{2048}x^4 + \frac{9}{256}x^5\right) y(0) + \left(x - \frac{1}{32}x^3 + \frac{1}{32}x^4 - \frac{57}{2048}x^5\right) D(y)(0) + O(x^6)$$

✓ Solution by Mathematica

Time used: 0.001 (sec). Leaf size: 63

```
AsymptoticDSolveValue[16*(x+1)^2*y''[x]+3*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2\left(-\frac{57x^5}{2048} + \frac{x^4}{32} - \frac{x^3}{32} + x\right) + c_1\left(\frac{9x^5}{256} - \frac{93x^4}{2048} + \frac{x^3}{16} - \frac{3x^2}{32} + 1\right)$$

5.5 problem 15

Internal problem ID [4919]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. REVIEW QUESTIONS. page 201
Problem number: 15.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[_Bessel]`

$$\boxed{x^2y'' + y'x + (x^2 - 5)\, y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 97

```
Order:=6;
dsolve(x^2*diff(y(x),x$2)+x*diff(y(x),x)+(x^2-5)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = c_1 x^{-\sqrt{5}} \left(1 + \frac{1}{-4 + 4\sqrt{5}} x^2 + \frac{1}{32} \frac{1}{\left(-2 + \sqrt{5}\right)\left(\sqrt{5} - 1\right)} x^4 + \mathrm{O}\left(x^6\right)\right) + c_2 x^{\sqrt{5}} \left(1 - \frac{1}{4 + 4\sqrt{5}} x^2 + \frac{1}{32} \frac{1}{\left(2 + \sqrt{5}\right)\left(\sqrt{5} + 1\right)} x^4 + \mathrm{O}\left(x^6\right)\right)$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 210

```
AsymptoticDSolveValue[x^2*y''[x]+x*y'[x]+(x^2-5)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2\left(\frac{x^4}{\left(-3-\sqrt{5}+\left(1-\sqrt{5}\right)\left(2-\sqrt{5}\right)\right)\left(-1-\sqrt{5}+\left(3-\sqrt{5}\right)\left(4-\sqrt{5}\right)\right)} - \frac{x^2}{-3-\sqrt{5}+\left(1-\sqrt{5}\right)\left(2-\sqrt{5}\right)}+1\right)x^{-\sqrt{5}} + c_1\left(\frac{x^4}{\left(-3+\sqrt{5}+\left(1+\sqrt{5}\right)\left(2+\sqrt{5}\right)\right)\left(-1+\sqrt{5}+\left(3+\sqrt{5}\right)\left(4+\sqrt{5}\right)\right)} - \frac{x^2}{-3+\sqrt{5}+\left(1+\sqrt{5}\right)\left(2+\sqrt{5}\right)}+1\right)x^{\sqrt{5}}$$

5.6 problem 16

Internal problem ID [4920]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. REVIEW QUESTIONS. page 201
Problem number: 16.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{x^2y'' + 2x^3y' + (x^2-2)\,y = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 35

```
Order:=6;
dsolve(x^2*diff(y(x),x$2)+2*x^3*diff(y(x),x)+(x^2-2)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = c_1x^2\left(1 - \frac{1}{2}x^2 + \frac{9}{56}x^4 + \mathrm{O}\left(x^6\right)\right) + \frac{c_2\left(12 - 6x^2 + \frac{9}{2}x^4 + \mathrm{O}\left(x^6\right)\right)}{x}$$

✓ Solution by Mathematica

Time used: 0.01 (sec). Leaf size: 44

```
AsymptoticDSolveValue[x^2*y''[x]+2*x^3*y'[x]+(x^2-2)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(\frac{3x^3}{8} - \frac{x}{2} + \frac{1}{x}\right) + c_2\left(\frac{9x^6}{56} - \frac{x^4}{2} + x^2\right)$$

5.7 problem 17

Internal problem ID [4921]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. REVIEW QUESTIONS. page 201
Problem number: 17.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[_Laguerre]`

$$xy'' - y'(1 + x) + y = 0$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 44

```
Order:=6;
dsolve(x*diff(y(x),x$2)-(x+1)*diff(y(x),x)+y(x)=0,y(x),type='series',x=0);
```

$$y(x) = c_1 x^2 \left(1 + \frac{1}{3}x + \frac{1}{12}x^2 + \frac{1}{60}x^3 + \frac{1}{360}x^4 + \frac{1}{2520}x^5 + \mathrm{O}\left(x^6\right)\right) + c_2\left(-2 - 2x - x^2 - \frac{1}{3}x^3 - \frac{1}{12}x^4 - \frac{1}{60}x^5 + \mathrm{O}\left(x^6\right)\right)$$

✓ Solution by Mathematica

Time used: 0.02 (sec). Leaf size: 66

```
AsymptoticDSolveValue[x*y''[x]-(x+1)*y'[x]+y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(\frac{x^4}{24} + \frac{x^3}{6} + \frac{x^2}{2} + x + 1\right) + c_2\left(\frac{x^6}{360} + \frac{x^5}{60} + \frac{x^4}{12} + \frac{x^3}{3} + x^2\right)$$

5.8 problem 18

Internal problem ID [4922]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. REVIEW QUESTIONS. page 201
Problem number: 18.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler]]`

$$\boxed{xy'' + 3y' + 4yx^3 = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 28

```
Order:=6;
dsolve(x*diff(y(x),x$2)+3*diff(y(x),x)+4*x^3*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = c_1\left(1 - \frac{1}{6}x^4 + \mathrm{O}\left(x^6\right)\right) + \frac{c_2(-2 + x^4 + \mathrm{O}\left(x^6\right))}{x^2}$$

✓ Solution by Mathematica

Time used: 0.007 (sec). Leaf size: 30

```
AsymptoticDSolveValue[x*y''[x]+3*y'[x]+4*x^3*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_2\left(1 - \frac{x^4}{6}\right) + c_1\left(\frac{1}{x^2} - \frac{x^2}{2}\right)$$

5.9 problem 19

Internal problem ID [4923]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. REVIEW QUESTIONS. page 201
Problem number: 19.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_Emden, _Fowler]]`

$$\boxed{y'' + \frac{y}{4x} = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 58

```
Order:=6;
dsolve(diff(y(x),x$2)+1/(4*x)*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = c_1 x\left(1 - \frac{1}{8}x + \frac{1}{192}x^2 - \frac{1}{9216}x^3 + \frac{1}{737280}x^4 - \frac{1}{88473600}x^5 + \mathrm{O}\left(x^6\right)\right) + c_2\left(\ln\left(x\right)\left(-\frac{1}{4}x + \frac{1}{32}x^2 - \frac{1}{768}x^3 + \frac{1}{36864}x^4 - \frac{1}{2949120}x^5 + \mathrm{O}\left(x^6\right)\right) + \left(1 - \frac{3}{64}x^2 + \frac{7}{2304}x^3 - \frac{35}{442368}x^4 + \frac{101}{88473600}x^5 + \mathrm{O}\left(x^6\right)\right)\right)$$

✓ Solution by Mathematica

Time used: 0.017 (sec). Leaf size: 85

```
AsymptoticDSolveValue[y''[x]+1/(4*x)*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(\frac{x(x^3 - 48x^2 + 1152x - 9216)\log(x)}{36864} + \frac{-47x^4 + 1920x^3 - 34560x^2 + 110592x + 442368}{442368}\right) + c_2\left(\frac{x^5}{737280} - \frac{x^4}{9216} + \frac{x^3}{192} - \frac{x^2}{8} + x\right)$$

5.10 problem 20

Internal problem ID [4924]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 5. Series Solutions of ODEs. REVIEW QUESTIONS. page 201
Problem number: 20.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{xy'' + y' - xy = 0}$$

With the expansion point for the power series method at $x = 0$.

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 41

```
Order:=6;
dsolve(x*diff(y(x),x$2)+diff(y(x),x)-x*y(x)=0,y(x),type='series',x=0);
```

$$y(x) = (\ln(x) c_2 + c_1)\left(1 + \frac{1}{4}x^2 + \frac{1}{64}x^4 + O(x^6)\right) + \left(-\frac{1}{4}x^2 - \frac{3}{128}x^4 + O(x^6)\right) c_2$$

✓ Solution by Mathematica

Time used: 0.002 (sec). Leaf size: 60

```
AsymptoticDSolveValue[x*y''[x]+y'[x]-x*y[x]==0,y[x],{x,0,5}]
```

$$y(x) \to c_1\left(\frac{x^4}{64} + \frac{x^2}{4} + 1\right) + c_2\left(-\frac{3x^4}{128} - \frac{x^2}{4} + \left(\frac{x^4}{64} + \frac{x^2}{4} + 1\right)\log(x)\right)$$

6 Chapter 6. Laplace Transforms. Problem set 6.2, page 216

6.1 problem 1

Internal problem ID [4925]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.2, page 216
Problem number: 1.
ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type `[[_linear, 'class A']]`

$$\boxed{y' + \frac{26y}{5} - \frac{97\sin(2t)}{5} = 0}$$

With initial conditions

$$[y(0) = 0]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 23

```
dsolve([diff(y(t),t)+52/10*y(t)=194/10*sin(2*t),y(0) = 0],y(t), singsol=all)
```

$$y(t) = -\frac{5\cos(2t)}{4} + \frac{13\sin(2t)}{4} + \frac{5\,e^{-\frac{26t}{5}}}{4}$$

✓ Solution by Mathematica

Time used: 0.092 (sec). Leaf size: 31

```
DSolve[{y'[t]+52/10*y[t]==194/10*Sin[2*t],{y[0]==0}},y[t],t,IncludeSingularSolutions -> True]
```

$$y(t) \to \frac{1}{4}\left(5e^{-26t/5} + 13\sin(2t) - 5\cos(2t)\right)$$

6.2 problem 2

Internal problem ID [4926]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.2, page 216
Problem number: 2.
ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type `[_quadrature]`

$$\boxed{2y + y' = 0}$$

With initial conditions

$$\left[y(0) = \frac{3}{2}\right]$$

✓ Solution by Maple

Time used: 0.0 (sec). Leaf size: 10

```
dsolve([diff(y(t),t)+2*y(t)=0,y(0) = 3/2],y(t), singsol=all)
```

$$y(t) = \frac{3\,\mathrm{e}^{-2t}}{2}$$

✓ Solution by Mathematica

Time used: 0.035 (sec). Leaf size: 31

```
DSolve[{y'[t]+52/10*y[t]==194/10*Sin[2*t],{y[0]==15/10}},y[t],t,IncludeSingularSolutions -> T
```

$$y(t) \to \frac{1}{4}\left(11e^{-26t/5} + 13\sin(2t) - 5\cos(2t)\right)$$

6.3 problem 3

Internal problem ID [4927]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.2, page 216
Problem number: 3.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$\boxed{y'' - y' - 6y = 0}$$

With initial conditions

$$[y(0) = 11, y'(0) = 28]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 15

```
dsolve([diff(y(t),t$2)-diff(y(t),t)-6*y(t)=0,y(0) = 11, D(y)(0) = 28],y(t), singsol=all)
```

$$y(t) = \left(10\,\mathrm{e}^{5t} + 1\right)\mathrm{e}^{-2t}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 18

```
DSolve[{y''[t]-y'[t]-6*y[t]==0,{y[0]==11,y'[0]==28}},y[t],t,IncludeSingularSolutions -> True]
```

$$y(t) \to e^{-2t} + 10e^{3t}$$

6.4 problem 4

Internal problem ID [4928]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.2, page 216
Problem number: 4.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{y'' + 9y - 10\,\mathrm{e}^{-t} = 0}$$

With initial conditions

$$[y(0) = 0, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 21

```
dsolve([diff(y(t),t$2)+9*y(t)=10*exp(-t),y(0) = 0, D(y)(0) = 0],y(t), singsol=all)
```

$$y(t) = \frac{\sin(3t)}{3} - \cos(3t) + \mathrm{e}^{-t}$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 25

```
DSolve[{y''[t]+9*y[t]==10*Exp[-t],{y[0]==0,y'[0]==0}},y[t],t,IncludeSingularSolutions -> True
```

$$y(t) \to e^{-t} + \frac{1}{3}\sin(3t) - \cos(3t)$$

6.5 problem 5

Internal problem ID [4929]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.2, page 216
Problem number: 5.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$\boxed{y'' - \frac{y}{4} = 0}$$

With initial conditions

$$[y(0) = 12, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 17

```
dsolve([diff(y(t),t$2)-1/4*y(t)=0,y(0) = 12, D(y)(0) = 0],y(t), singsol=all)
```

$$y(t) = 6\,\mathrm{e}^{-\frac{t}{2}} + 6\,\mathrm{e}^{\frac{t}{2}}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 13

```
DSolve[{y''[t]-1/4*y[t]==0,{y[0]==12,y'[0]==0}},y[t],t,IncludeSingularSolutions -> True]
```

$$y(t) \to 12\cosh\left(\frac{t}{2}\right)$$

6.6 problem 6

Internal problem ID [4930]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.2, page 216
Problem number: 6.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$\boxed{y'' - 6y' + 5y - 29\cos(2t) = 0}$$

With initial conditions

$$\left[y(0) = \frac{16}{5}, y'(0) = \frac{31}{5}\right]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 25

```
dsolve([diff(y(t),t$2)-6*diff(y(t),t)+5*y(t)=29*cos(2*t),y(0) = 16/5, D(y)(0) = 31/5],y(t), s
```

$$y(t) = 2\,e^{5t} + e^{t} + \frac{\cos(2t)}{5} - \frac{12\sin(2t)}{5}$$

✓ Solution by Mathematica

Time used: 0.006 (sec). Leaf size: 31

```
DSolve[{y''[t]-6*y'[t]+5*y[t]==29*Cos[2*t],{y[0]==32/10,y'[0]==62/10}},y[t],t,IncludeSingular
```

$$y(t) \to e^{t} + 2e^{5t} + \frac{1}{5}(\cos(2t) - 12\sin(2t))$$

6.7 problem 7

Internal problem ID [4931]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.2, page 216
Problem number: 7.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{y'' + 7y' + 12y - 21\,\mathrm{e}^{3t} = 0}$$

With initial conditions

$$\left[y(0) = \frac{7}{2}, y'(0) = -10\right]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 18

```
dsolve([diff(y(t),t$2)+7*diff(y(t),t)+12*y(t)=21*exp(3*t),y(0) = 7/2, D(y)(0) = -10],y(t), si
```

$$y(t) = \frac{(\mathrm{e}^{7t} + \mathrm{e}^{t} + 5)\,\mathrm{e}^{-4t}}{2}$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 28

```
DSolve[{y''[t]+7*y'[t]+12*y[t]==21*Exp[3*t],{y[0]==32/10,y'[0]==62/10}},y[t],t,IncludeSingula
```

$$y(t) \to \frac{1}{10}e^{-4t}\left(5e^{t}\left(e^{6t} + 31\right) - 128\right)$$

6.8 problem 8

Internal problem ID [4932]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.2, page 216
Problem number: 8.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$\boxed{y'' - 4y' + 4y = 0}$$

With initial conditions

$$\left[y(0) = \frac{81}{10}, y'(0) = \frac{39}{10}\right]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 15

```
dsolve([diff(y(t),t$2)-4*diff(y(t),t)+4*y(t)=0,y(0) = 81/10, D(y)(0) = 39/10],y(t), singsol=a
```

$$y(t) = -\frac{3\,e^{2t}(-27 + 41t)}{10}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 19

```
DSolve[{y''[t]-4*y'[t]+4*y[t]==0,{y[0]==81/10,y'[0]==39/10}},y[t],t,IncludeSingularSolutions
```

$$y(t) \to -\frac{3}{10}e^{2t}(41t - 27)$$

6.9 problem 9

Internal problem ID [4933]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.2, page 216
Problem number: 9.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{y'' - 4y' + 3y - 6t + 8 = 0}$$

With initial conditions

$$[y(0) = 0, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 16

```
dsolve([diff(y(t),t$2)-4*diff(y(t),t)+3*y(t)=6*t-8,y(0) = 0, D(y)(0) = 0],y(t), singsol=all)
```

$$y(t) = e^t - e^{3t} + 2t$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 19

```
DSolve[{y''[t]-4*y'[t]+3*y[t]==6*t-8,{y[0]==0,y'[0]==0}},y[t],t,IncludeSingularSolutions -> T
```

$$y(t) \to 2t + e^t - e^{3t}$$

6.10 problem 10

Internal problem ID [4934]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.2, page 216
Problem number: 10.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{y'' + \frac{y}{25} - \frac{t^2}{50} = 0}$$

With initial conditions

$$[y(0) = -25, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 11

```
dsolve([diff(y(t),t$2)+4/100*y(t)=2/100*t^2,y(0) = -25, D(y)(0) = 0],y(t), singsol=all)
```

$$y(t) = \frac{t^2}{2} - 25$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 14

```
DSolve[{y''[t]+4/100*y[t]==2/100*t^2,{y[0]==-25,y'[0]==0}},y[t],t,IncludeSingularSolutions ->
```

$$y(t) \to \frac{1}{2}(t^2 - 50)$$

6.11 problem 11

Internal problem ID [4935]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.2, page 216
Problem number: 11.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$\boxed{y'' + 3y' + \frac{9y}{4} - 9t^3 - 64 = 0}$$

With initial conditions

$$\left[y(0) = 1, y'(0) = \frac{63}{2}\right]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 28

```
dsolve([diff(y(t),t$2)+3*diff(y(t),t)+225/100*y(t)=9*t^3+64,y(0) = 1, D(y)(0) = 63/2],y(t), s
```

$$y(t) = \mathrm{e}^{-\frac{3t}{2}} + \mathrm{e}^{-\frac{3t}{2}}t + 4t^3 - 16t^2 + 32t$$

✓ Solution by Mathematica

Time used: 0.007 (sec). Leaf size: 27

```
DSolve[{y''[t]+3*y'[t]+225/100*y[t]==9*t^3+64,{y[0]==1,y'[0]==315/10}},y[t],t,IncludeSingular
```

$$y(t) \to e^{-3t/2}(t+1) + 4t((t-4)t+8)$$

6.12 problem 12

Internal problem ID [4936]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.2, page 216
Problem number: 12.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$\boxed{y'' - 2y' - 3y = 0}$$

With initial conditions

$$[y(4) = -3, y'(4) = -17]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 21

```
dsolve([diff(y(t),t$2)-2*diff(y(t),t)-3*y(t)=0,y(4) = -3, D(y)(4) = -17],y(t), singsol=all)
```

$$y(t) = 2\,\mathrm{e}^{4-t} - 5\,\mathrm{e}^{-12+3t}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 24

```
DSolve[{y''[t]-2*y'[t]-3*y[t]==0,{y[4]==-3,y'[4]==-17}},y[t],t,IncludeSingularSolutions -> Tr
```

$$y(t) \to 2e^{4-t} - 5e^{3(t-4)}$$

6.13 problem 13

Internal problem ID [4937]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.2, page 216
Problem number: 13.
ODE order: 1.
ODE degree: 1.

CAS Maple gives this as type `[_quadrature]`

$$\boxed{y' - 6y = 0}$$

With initial conditions

$$[y(-1) = 4]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 12

```
dsolve([diff(y(t),t)-6*y(t)=0,y(-1) = 4],y(t), singsol=all)
```

$$y(t) = 4\,\mathrm{e}^{6t+6}$$

✓ Solution by Mathematica

Time used: 0.021 (sec). Leaf size: 14

```
DSolve[{y'[t]-6*y[t]==0,{y[-1]==4}},y[t],t,IncludeSingularSolutions -> True]
```

$$y(t) \to 4e^{6t+6}$$

6.14 problem 14

Internal problem ID [4938]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.2, page 216
Problem number: 14.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{y'' + 2y' + 5y - 50t + 100 = 0}$$

With initial conditions

$$[y(2) = -4, y'(2) = 14]$$

✓ Solution by Maple

Time used: 0.062 (sec). Leaf size: 37

```
dsolve([diff(y(t),t$2)+2*diff(y(t),t)+5*y(t)=50*t-100,y(2) = -4, D(y)(2) = 14],y(t), singsol=
```

$$y(t) = 2\sin(2t)\cos(4)\,e^{-t+2} - 2\cos(2t)\sin(4)\,e^{-t+2} + 10t - 24$$

✓ Solution by Mathematica

Time used: 0.005 (sec). Leaf size: 25

```
DSolve[{y''[t]+2*y'[t]+5*y[t]==50*t-100,{y[2]==-4,y'[2]==14}},y[t],t,IncludeSingularSolutions
```

$$y(t) \to 10t - 2e^{2-t}\sin(4-2t) - 24$$

6.15 problem 15

Internal problem ID [4939]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.2, page 216
Problem number: 15.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{y'' + 3y' - 4y - 6\,\mathrm{e}^{2t-3} = 0}$$

With initial conditions

$$\left[y\left(\frac{3}{2}\right) = 4, y'\left(\frac{3}{2}\right) = 5\right]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 17

```
dsolve([diff(y(t),t$2)+3*diff(y(t),t)-4*y(t)=6*exp(2*t-3),y(3/2) = 4, D(y)(3/2) = 5],y(t), si
```

$$y(t) = 3\,\mathrm{e}^{t-\frac{3}{2}} + \mathrm{e}^{2t-3}$$

✓ Solution by Mathematica

Time used: 0.027 (sec). Leaf size: 22

```
DSolve[{y''[t]+3*y'[t]-4*y[t]==6*Exp[2*t-3],{y[15/10]==4,y'[15/10]==5}},y[t],t,IncludeSingula
```

$$y(t) \to 3e^{t-\frac{3}{2}} + e^{2t-3}$$

7 Chapter 6. Laplace Transforms. Problem set 6.3, page 224

7.1 problem 18

Internal problem ID [4940]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.3, page 224
Problem number: 18.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _missing_x]]`

$$\boxed{9y'' - 6y' + y = 0}$$

With initial conditions

$$[y(0) = 3, y'(0) = 1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 10

```
dsolve([9*diff(y(t),t$2)-6*diff(y(t),t)+y(t)=0,y(0) = 3, D(y)(0) = 1],y(t), singsol=all)
```

$$y(t) = 3\,e^{\frac{t}{3}}$$

✓ Solution by Mathematica

Time used: 0.003 (sec). Leaf size: 14

```
DSolve[{9*y''[t]-6*y'[t]+y[t]==0,{y[0]==3,y'[0]==1}},y[t],t,IncludeSingularSolutions -> True]
```

$$y(t) \to 3e^{t/3}$$

7.2 problem 19

Internal problem ID [4941]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.3, page 224
Problem number: 19.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$\boxed{y'' + 6y' + 8y - e^{-3t} + e^{-5t} = 0}$$

With initial conditions

$$[y(0) = 0, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 28

```
dsolve([diff(y(t),t$2)+6*diff(y(t),t)+8*y(t)=exp(-3*t)-exp(-5*t),y(0) = 0, D(y)(0) = 0],y(t),
```

$$y(t) = -\frac{(e^{-3t} - 3\,e^{-2t} + 3\,e^{-t} - 1)\,e^{-2t}}{3}$$

✓ Solution by Mathematica

Time used: 0.05 (sec). Leaf size: 21

```
DSolve[{y''[t]+6*y'[t]+8*y[t]==Exp[-3*t]-Exp[-5*t],{y[0]==0,y'[0]==0}},y[t],t,IncludeSingular
```

$$y(t) \to \frac{1}{3}e^{-5t}\left(e^t - 1\right)^3$$

7.3 problem 20

Internal problem ID [4942]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.3, page 224
Problem number: 20.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _with_linear_symmetries]]`

$$\boxed{y'' + 10y' + 24y - 144t^2 = 0}$$

With initial conditions

$$\left[y(0) = \frac{19}{12}, y'(0) = -5\right]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 14

```
dsolve([diff(y(t),t$2)+10*diff(y(t),t)+24*y(t)=144*t^2,y(0) = 19/12, D(y)(0) = -5],y(t), sing
```

$$y(t) = 6t^2 - 5t + \frac{19}{12}$$

✓ Solution by Mathematica

Time used: 0.004 (sec). Leaf size: 16

```
DSolve[{y''[t]+10*y'[t]+24*y[t]==144*t^2,{y[0]==19/12,y'[0]==-5}},y[t],t,IncludeSingularSolut
```

$$y(t) \rightarrow t(6t - 5) + \frac{19}{12}$$

7.4 problem 21

Internal problem ID [4943]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.3, page 224
Problem number: 21.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' + 9y - \left(\begin{cases} 8\sin(t) & 0 < t < \pi \\ 0 & \pi < t \end{cases} \right) = 0$$

With initial conditions

$$[y(0) = 0, y'(0) = 4]$$

✓ Solution by Maple

Time used: 0.141 (sec). Leaf size: 35

```
dsolve([diff(y(t),t$2)+9*y(t)=piecewise(0<t and t<Pi,8*sin(t),t>Pi,0),y(0) = 0, D(y)(0) = 4],
```

$$y(t) = 4 \left(\begin{cases} \frac{\sin(3t)}{3} & t < 0 \\ \sin(t)\cos(t)^2 & t < \pi \\ \frac{\sin(3t)}{3} & \pi \leq t \end{cases} \right)$$

✓ Solution by Mathematica

Time used: 0.01 (sec). Leaf size: 30

```
DSolve[{y''[t]+9*y[t]==Piecewise[{{8*Sin[t],0<t<Pi},{0,t>Pi}}],{y[0]==0,y'[0]==4}},y[t],t,Inc
```

$$y(t) \to \begin{cases} \frac{4}{3}\sin(3t) & t > \pi \lor t \leq 0 \\ \sin(t) + \sin(3t) & \text{True} \end{cases}$$

7.5 problem 22

Internal problem ID [4944]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.3, page 224
Problem number: 22.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' + 3y' + 2y - \left(\begin{cases} 4t & 0 < t < 1 \\ 8 & 1 < t \end{cases}\right) = 0$$

With initial conditions

$$[y(0) = 0, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.203 (sec). Leaf size: 62

```
dsolve([diff(y(t),t$2)+3*diff(y(t),t)+2*y(t)=piecewise(0<t and t<1,4*t,t>1,8),y(0) = 0, D(y)(
```

$$y(t) = \begin{cases} 0 & t < 0 \\ 2t - e^{-2t} - 3 + 4\,e^{-t} & t < 1 \\ 3\,e^{-2t+2} - 8\,e^{-t+1} - e^{-2t} + 4 + 4\,e^{-t} & 1 \leq t \end{cases}$$

✓ Solution by Mathematica

Time used: 0.01 (sec). Leaf size: 62

```
DSolve[{y''[t]+3*y'[t]+2*y[t]==Piecewise[{{4*t,0<t<1},{8,t>1}}],{y[0]==0,y'[0]==0}},y[t],t,In
```

$$y(t) \to \begin{cases} 0 & t \leq 0 \\ e^{-2t}(-1 + 4e^t) + 2t - 3 & 0 < t \leq 1 \\ e^{-2t}(-1 + 3e^2 - 4e^t(-1 + 2e)) + 4 & \text{True} \end{cases}$$

7.6 problem 23

Internal problem ID [4945]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.3, page 224
Problem number: 23.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' + y' - 2y - \left(\begin{cases} 3\sin(t) - \cos(t) & 0 < t < 2\pi \\ 3\sin(2t) - \cos(2t) & 2\pi < t \end{cases}\right) = 0$$

With initial conditions

$$[y(0) = 1, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.328 (sec). Leaf size: 48

```
dsolve([diff(y(t),t$2)+diff(y(t),t)-2*y(t)=piecewise(0<t and t<2*Pi,3*sin(t)-cos(t),t>2*Pi,3*
```

$$y(t) = \begin{cases} \frac{(2\,\mathrm{e}^{3t}+1)\,\mathrm{e}^{-2t}}{3} & t < 0 \\ \mathrm{e}^{t} - \sin(t) & t < 2\pi \\ \mathrm{e}^{t} - \sin(t)\cos(t) & 2\pi \leq t \end{cases}$$

✓ Solution by Mathematica

Time used: 0.019 (sec). Leaf size: 55

```
DSolve[{y''[t]+y'[t]-2*y[t]==Piecewise[{{3*Sin[t]-Cos[t],0<t<2*Pi},{3*Sin[2*t]-Cos[2*t],t>2*P
```

$$y(t) \to \begin{cases} \frac{e^{-2t}}{3} + \frac{2e^{t}}{3} & t \leq 0 \\ e^{t} - \sin(t) & 0 < t \leq 2\pi \\ e^{t} - \cos(t)\sin(t) & \text{True} \end{cases}$$

7.7 problem 24

Internal problem ID [4946]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.3, page 224
Problem number: 24.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' + 3y' + 2y - \left(\begin{cases} 1 & 0 < t < 1 \\ 0 & 1 < t \end{cases}\right) = 0$$

With initial conditions

$$[y(0) = 0, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.235 (sec). Leaf size: 56

```
dsolve([diff(y(t),t$2)+3*diff(y(t),t)+2*y(t)=piecewise(0<t and t<1,1,t>1,0),y(0) = 0, D(y)(0)
```

$$y(t) = \frac{\left(\begin{cases} 0 & t < 0 \\ 1 - 2\,\mathrm{e}^{-t} + \mathrm{e}^{-2t} & t < 1 \\ 2\,\mathrm{e}^{-t+1} - \mathrm{e}^{-2t+2} - 2\,\mathrm{e}^{-t} + \mathrm{e}^{-2t} & 1 \le t \end{cases}\right)}{2}$$

✓ Solution by Mathematica

Time used: 0.009 (sec). Leaf size: 57

```
DSolve[{y''[t]+3*y'[t]+2*y[t]==Piecewise[{{1,0<t<1},{0,t>1}}],{y[0]==0,y'[0]==0}},y[t],t,Incl
```

$$y(t) \to \begin{cases} 0 & t \le 0 \\ \frac{1}{2}e^{-2t}(-1 + e^t)^2 & 0 < t \le 1 \\ \frac{1}{2}(-1 + e)e^{-2t}(-1 - e + 2e^t) & \text{True} \end{cases}$$

7.8 problem 25

Internal problem ID [4947]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.3, page 224
Problem number: 25.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' + y - \left(\begin{cases} t & 0 < t < 1 \\ 0 & 1 < t \end{cases}\right) = 0$$

With initial conditions

$$[y(0) = 0, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.109 (sec). Leaf size: 34

```
dsolve([diff(y(t),t$2)+y(t)=piecewise(0<t and t<1,t,t>1,0),y(0) = 0, D(y)(0) = 0],y(t), sings
```

$$y(t) = \begin{cases} 0 & t < 0 \\ -\sin(t) + t & t < 1 \\ -\sin(t) + \cos(t-1) + \sin(t-1) & 1 \leq t \end{cases}$$

✓ Solution by Mathematica

Time used: 0.009 (sec). Leaf size: 45

```
DSolve[{y''[t]+y[t]==Piecewise[{{t,0<t<1},{0,t>1}}],{y[0]==0,y'[0]==0}},y[t],t,IncludeSingula
```

$$y(t) \to \begin{cases} t - \sin(t) & 0 < t \leq 1 \\ (\cos(1) - \sin(1))\cos(t) + (-1 + \cos(1) + \sin(1))\sin(t) & t > 1 \end{cases}$$

7.9 problem 26

Internal problem ID [4948]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.3, page 224
Problem number: 26.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' + 2y' + 5y - \left(\begin{cases} 10\sin(t) & 0 < t < 2\pi \\ 0 & 2\pi < t \end{cases}\right) = 0$$

With initial conditions

$$[y(\pi) = 1, y'(\pi) = 2\,\mathrm{e}^{-\pi} - 2]$$

✓ Solution by Maple

Time used: 0.594 (sec). Leaf size: 102

```
dsolve([diff(y(t),t$2)+2*diff(y(t),t)+5*y(t)=piecewise(0<t and t<2*Pi,10*sin(t),t>2*Pi,0),y(P
```

$$y(t) = \begin{cases} -\frac{\mathrm{e}^{-t}(2\cos(2t)-3\sin(2t))}{2} & t < 0 \\ 2\cos(t)\,\mathrm{e}^{-t}\sin(t) - \cos(t) + 2\sin(t) & t < 2\pi \\ 2\cos(t)\,\mathrm{e}^{-t}\sin(t) - 2\cos(t)^2\,\mathrm{e}^{2\pi-t} + \sin(t)\cos(t)\,\mathrm{e}^{2\pi-t} + \mathrm{e}^{2\pi-t} & 2\pi \leq t \end{cases}$$

✓ Solution by Mathematica

Time used: 0.013 (sec). Leaf size: 94

```
DSolve[{y''[t]+2*y'[t]+5*y[t]==Piecewise[{{10*Sin[t],0<t<2*Pi},{0,t>2*Pi}}],{y[Pi]==1,y'[Pi]=
```

$$y(t) \to \left\{ \begin{array}{cc} \frac{1}{2}e^{-t}(3\sin(2t) - 2\cos(2t)) & t \leq 0 \\ -\cos(t) + 2\sin(t) + e^{-t}\sin(2t) & 0 < t \leq 2\pi \\ \frac{1}{2}e^{-t}((2 + e^{2\pi})\sin(2t) - 2e^{2\pi}\cos(2t)) & \text{True} \end{array} \right.$$

7.10 problem 27

Internal problem ID [4949]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.3, page 224
Problem number: 27.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$y'' + 4y - \left(\begin{cases} 8t^2 & 0 < t < 5 \\ 0 & 5 < t \end{cases}\right) = 0$$

With initial conditions

$$[y(1) = 1 + \cos(2), y'(1) = 4 - 2\sin(2)]$$

✓ Solution by Maple

Time used: 0.14 (sec). Leaf size: 47

```
dsolve([diff(y(t),t$2)+4*y(t)=piecewise(0<t and t<5,8*t^2,t>5,0),y(1) = 1+cos(2), D(y)(1) = 4
```

$$y(t) = \begin{cases} 0 & t < 0 \\ 2t^2 - 1 + \cos(2t) & t < 5 \\ 49\cos(2t - 10) + 10\sin(2t - 10) + \cos(2t) & 5 \leq t \end{cases}$$

✓ Solution by Mathematica

Time used: 0.01 (sec). Leaf size: 51

```
DSolve[{y''[t]+4*y[t]==Piecewise[{{8*t^2,0<t<5},{0,t>5}}],{y[1]==1+Cos[2],y'[1]==4-2*Sin[2]}}
```

$$y(t) \to \{ \begin{array}{cc} 2t^2 + \cos(2t) - 1 & 0 < t \leq 5 \\ 49\cos(2(t-5)) + \cos(2t) - 10\sin(10 - 2t) & t > 5 \end{array}$$

8 Chapter 6. Laplace Transforms. Problem set 6.4, page 230

8.1 problem 3

Internal problem ID [4950]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.4, page 230
Problem number: 3.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$\boxed{y'' + 4y - (\delta(-\pi + t)) = 0}$$

With initial conditions

$$[y(0) = 8, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 23

```
dsolve([diff(y(t),t$2)+4*y(t)=Dirac(t-Pi),y(0) = 8, D(y)(0) = 0],y(t), singsol=all)
```

$$y(t) = 8\cos(2t) + \frac{\text{Heaviside}(-\pi + t)\sin(2t)}{2}$$

✓ Solution by Mathematica

Time used: 0.032 (sec). Leaf size: 23

```
DSolve[{y''[t]+4*y[t]==DiracDelta[t-Pi],{y[0]==8,y'[0]==0}},y[t],t,IncludeSingularSolutions -
```

$$y(t) \to \theta(t - \pi)\sin(t)\cos(t) + 8\cos(2t)$$

8.2 problem 4

Internal problem ID [4951]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.4, page 230
Problem number: 4.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$\boxed{y'' + 16y - 4(\delta(t - 3\pi)) = 0}$$

With initial conditions

$$[y(0) = 2, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 22

```
dsolve([diff(y(t),t$2)+16*y(t)=4*Dirac(t-3*Pi),y(0) = 2, D(y)(0) = 0],y(t), singsol=all)
```

$$y(t) = 2\cos(4t) + \text{Heaviside}(t - 3\pi)\sin(4t)$$

✓ Solution by Mathematica

Time used: 0.009 (sec). Leaf size: 23

```
DSolve[{y''[t]+16*y[t]==4*DiracDelta[t-3*Pi],{y[0]==2,y'[0]==0}},y[t],t,IncludeSingularSoluti
```

$$y(t) \to \theta(t - 3\pi)\sin(4t) + 2\cos(4t)$$

8.3 problem 5

Internal problem ID [4952]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.4, page 230
Problem number: 5.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$\boxed{y'' + y - (\delta(-\pi + t)) + \delta(-2\pi + t) = 0}$$

With initial conditions

$$[y(0) = 0, y'(0) = 1]$$

✓ Solution by Maple

Time used: 0.015 (sec). Leaf size: 22

```
dsolve([diff(y(t),t$2)+y(t)=Dirac(t-Pi)-Dirac(t-2*Pi),y(0) = 0, D(y)(0) = 1],y(t), singsol=al
```

$$y(t) = -\sin(t)\left(\text{Heaviside}\left(-\pi + t\right) + \text{Heaviside}\left(-2\pi + t\right) - 1\right)$$

✓ Solution by Mathematica

Time used: 0.016 (sec). Leaf size: 23

```
DSolve[{y''[t]+y[t]==DiracDelta[t-Pi]-DiracDelta[t-2*Pi],{y[0]==0,y'[0]==1}},y[t],t,IncludeSi
```

$$y(t) \to -((\theta(t - 2\pi) + \theta(t - \pi) - 1)\sin(t))$$

8.4 problem 6

Internal problem ID [4953]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.4, page 230
Problem number: 6.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$\boxed{y'' + 4y' + 5y - (\delta(t-1)) = 0}$$

With initial conditions

$$[y(0) = 0, y'(0) = 3]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 28

```
dsolve([diff(y(t),t$2)+4*diff(y(t),t)+5*y(t)=Dirac(t-1),y(0) = 0, D(y)(0) = 3],y(t), singsol=
```

$$y(t) = 3\,\mathrm{e}^{-2t}\sin(t) + \mathrm{Heaviside}(t-1)\,\mathrm{e}^{-2t+2}\sin(t-1)$$

✓ Solution by Mathematica

Time used: 0.014 (sec). Leaf size: 31

```
DSolve[{y''[t]+4*y'[t]+5*y[t]==DiracDelta[t-1],{y[0]==0,y'[0]==3}},y[t],t,IncludeSingularSolu
```

$$y(t) \to e^{-2t}\left(3\sin(t) - e^2\theta(t-1)\sin(1-t)\right)$$

8.5 problem 7

Internal problem ID [4954]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.4, page 230
Problem number: 7.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$\boxed{4y'' + 24y' + 37y - 17\,\mathrm{e}^{-t} - \left(\delta\left(t - \frac{1}{2}\right)\right) = 0}$$

With initial conditions

$$[y(0) = 1, y'(0) = 1]$$

✓ Solution by Maple

Time used: 0.031 (sec). Leaf size: 36

```
dsolve([4*diff(y(t),t$2)+24*diff(y(t),t)+37*y(t)=17*exp(-t)+Dirac(t-1/2),y(0) = 1, D(y)(0) =
```

$$y(t) = \frac{\mathrm{e}^{-3t}\left(\text{Heaviside}\left(t - \frac{1}{2}\right)\mathrm{e}^{\frac{3}{2}}\sin\left(-\frac{1}{4} + \frac{t}{2}\right) + 2\,\mathrm{e}^{2t} + 8\sin\left(\frac{t}{2}\right)\right)}{2}$$

✓ Solution by Mathematica

Time used: 0.046 (sec). Leaf size: 63

```
DSolve[{4*y''[t]+24*y'[t]+27*y[t]==17*Exp[-t]+DiracDelta[t-1/2],{y[0]==1,y'[0]==1}},y[t],t,In
```

$$y(t) \to \frac{1}{84}e^{-9t/2}\left(7e^{3/4}\left(e^{3t} - e^{3/2}\right)\theta(2t-1) + 12\left(-7e^{3t} + 17e^{7t/2} - 3\right)\right)$$

8.6 problem 8

Internal problem ID [4955]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.4, page 230
Problem number: 8.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$\boxed{y'' + 3y' + 2y - 10\sin(t) - 10(\delta(t-1)) = 0}$$

With initial conditions

$$[y(0) = 1, y'(0) = -1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 47

```
dsolve([diff(y(t),t$2)+3*diff(y(t),t)+2*y(t)=10*(sin(t)+Dirac(t-1)),y(0) = 1, D(y)(0) = -1],y
```

$$\begin{aligned} y(t) = &-10\,\mathrm{Heaviside}(t-1)\,\mathrm{e}^{-2t+2} + 10\,\mathrm{Heaviside}(t-1)\,\mathrm{e}^{-t+1} \\ &- 3\cos(t) + \sin(t) - 2\,\mathrm{e}^{-2t} + 6\,\mathrm{e}^{-t} \end{aligned}$$

✓ Solution by Mathematica

Time used: 0.072 (sec). Leaf size: 45

```
DSolve[{y''[t]+3*y'[t]+2*y[t]==10*(Sin[t]+DiracDelta[t-1]),{y[0]==1,y'[0]==-1}},y[t],t,Includ
```

$$y(t) \to e^{-2t}\left(10e\left(e^t - e\right)\theta(t-1) + 6e^t + e^{2t}(\sin(t) - 3\cos(t)) - 2\right)$$

8.7 problem 9

Internal problem ID [4956]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.4, page 230
Problem number: 9.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$\boxed{y'' + 4y' + 5y - (1 - \text{Heaviside}\,(-10 + t))\,e^{t} + e^{10}(\delta(-10 + t)) = 0}$$

With initial conditions

$$[y(0) = 0, y'(0) = 1]$$

✓ Solution by Maple

Time used: 0.047 (sec). Leaf size: 49

```
dsolve([diff(y(t),t$2)+4*diff(y(t),t)+5*y(t)=(1-Heaviside(t-10))*exp(t)-exp(10)*Dirac(t-10),y
```

$$y(t) = -\frac{e^{-2t}\left(\left(-e^{30}\cos(t-10) + 7\,e^{30}\sin(t-10) + e^{3t}\right)\text{Heaviside}\,(t-10) + \cos(t) - 7\sin(t) - e^{3t}\right)}{10}$$

✓ Solution by Mathematica

Time used: 0.414 (sec). Leaf size: 86

```
DSolve[{y''[t]+4*y'[t]+5*y[t]==(1-UnitStep[t-10])*Exp[t]-Exp[10]*DiracDelta[t-10],{y[0]==0,y'
```

$$y(t) \rightarrow \begin{cases} \frac{1}{10}e^{-2t}(-\cos(t) + e^{3t} + 10e^{30}\theta(t-10)\sin(10-t) + 7\sin(t)) & t \leq 10 \\ \frac{1}{10}e^{-2t}(-\cos(t) + e^{30}(\cos(10-t) + 7\sin(10-t)) + 7\sin(t)) & \text{True} \end{cases}$$

8.8 problem 10

Internal problem ID [4957]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.4, page 230
Problem number: 10.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$\boxed{y'' + 5y' + 6y - \left(\delta\left(t - \frac{\pi}{2}\right)\right) - \cos(t)\,\mathrm{Heaviside}(-\pi + t) = 0}$$

With initial conditions

$$[y(0) = 0, y'(0) = 0]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 79

```
dsolve([diff(y(t),t$2)+5*diff(y(t),t)+6*y(t)=Dirac(t-1/2*Pi)+Heaviside(t-Pi)*cos(t),y(0) = 0,
```

$$\begin{aligned} y(t) = &-\mathrm{Heaviside}\left(t - \frac{\pi}{2}\right)\mathrm{e}^{-3t+\frac{3\pi}{2}} - \frac{3\,\mathrm{Heaviside}(-\pi + t)\,\mathrm{e}^{-3t+3\pi}}{10} \\ &+ \frac{2\,\mathrm{Heaviside}(-\pi + t)\,\mathrm{e}^{-2t+2\pi}}{5} + \mathrm{Heaviside}\left(t - \frac{\pi}{2}\right)\mathrm{e}^{-2t+\pi} \\ &+ \frac{\mathrm{Heaviside}(-\pi + t)\,(\cos(t) + \sin(t))}{10} \end{aligned}$$

✓ Solution by Mathematica

Time used: 0.375 (sec). Leaf size: 79

```
DSolve[{y''[t]+5*y'[t]+6*y[t]==DiracDelta[t-1/2*Pi]+UnitStep[t-Pi]*Cos[t],{y[0]==0,y'[0]==0}}
```

$$y(t) \to \frac{1}{10}e^{-3t}\left((\theta(\pi - t) - 1)\left(-4e^{t+2\pi} - e^{3t}(\sin(t) + \cos(t)) + 3e^{3\pi}\right) - 10e^{\pi}\left(e^{\pi/2} - e^{t}\right)\theta(2t - \pi)\right)$$

8.9 problem 11

Internal problem ID [4958]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.4, page 230
Problem number: 11.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$\boxed{y'' + 5y' + 6y - \text{Heaviside}\,(t-1) - (\delta(t-2)) = 0}$$

With initial conditions

$$[y(0) = 0, y'(0) = 1]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 68

```
dsolve([diff(y(t),t$2)+5*diff(y(t),t)+6*y(t)=Heaviside(t-1)+Dirac(t-2),y(0) = 0, D(y)(0) = 1]
```

$$y(t) = e^{-2t} - e^{-3t} + \frac{\text{Heaviside}\,(t-1)}{6} - \frac{\text{Heaviside}\,(t-1)\, e^{-2t+2}}{2} + \text{Heaviside}\,(t-2)\, e^{-2t+4} + \frac{\text{Heaviside}\,(t-1)\, e^{-3t+3}}{3} - \text{Heaviside}\,(t-2)\, e^{-3t+6}$$

✓ Solution by Mathematica

Time used: 0.155 (sec). Leaf size: 71

```
DSolve[{y''[t]+5*y'[t]+6*y[t]==UnitStep[t-1]+DiracDelta[t-2],{y[0]==0,y'[0]==1}},y[t],t,Inclu
```

$$y(t) \to \begin{cases} e^{-3t}(-1+e^t) & t \leq 1 \\ \frac{1}{6}e^{-3t}(6e^4(-e^2+e^t)\,\theta(t-2) + e^{3t} - 3e^t(-2+e^2) + 2e^3 - 6) & \text{True} \end{cases}$$

8.10 problem 12

Internal problem ID [4959]

Book: ADVANCED ENGINEERING MATHEMATICS. ERWIN KREYSZIG, HERBERT KREYSZIG, EDWARD J. NORMINTON. 10th edition. John Wiley USA. 2011
Section: Chapter 6. Laplace Transforms. Problem set 6.4, page 230
Problem number: 12.
ODE order: 2.
ODE degree: 1.

CAS Maple gives this as type `[[_2nd_order, _linear, _nonhomogeneous]]`

$$\boxed{y'' + 2y' + 5y - 25t + 100(\delta(-\pi + t)) = 0}$$

With initial conditions

$$[y(0) = -2, y'(0) = 5]$$

✓ Solution by Maple

Time used: 0.016 (sec). Leaf size: 27

```
dsolve([diff(y(t),t$2)+2*diff(y(t),t)+5*y(t)=25*t-100*Dirac(t-Pi),y(0) = -2, D(y)(0) = 5],y(t
```

$$y(t) = -50 \operatorname{Heaviside}(-\pi + t) \sin(2t) e^{\pi - t} + 5t - 2$$

✓ Solution by Mathematica

Time used: 0.123 (sec). Leaf size: 29

```
DSolve[{y''[t]+2*y'[t]+5*y[t]==25*t-100*DiracDelta[t-Pi],{y[0]==-2,y'[0]==5}},y[t],t,IncludeS
```

$$y(t) \to -50e^{\pi - t}\theta(t - \pi)\sin(2t) + 5t - 2$$