

Computer algebra independent integration tests

8-Special-functions/8.4-Trig-integral-functions

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3.22	$\int \frac{\text{Si}(a+bx)}{x} dx$	94
3.23	$\int \frac{\text{Si}(a+bx)}{x^2} dx$	96
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3.44	$\int x^2 \sin(bx)\text{Si}(bx) dx$	158
3.45	$\int x^3 \sin(bx)\text{Si}(bx) dx$	162
3.46	$\int \frac{\cos(bx)\text{Si}(bx)}{x^3} dx$	166
3.47	$\int \frac{\cos(bx)\text{Si}(bx)}{x^2} dx$	169
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3.57	$\int \sin(a + bx)\text{Si}(a + bx) dx$	201
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3.59	$\int x^2 \cos(a + bx)\text{Si}(a + bx) dx$	206
3.60	$\int x \cos(a + bx)\text{Si}(a + bx) dx$	210
3.61	$\int \cos(a + bx)\text{Si}(a + bx) dx$	214
3.62	$\int \frac{\cos(a+bx)\text{Si}(a+bx)}{x} dx$	217
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3.77	$\int x^m \text{CosIntegral}(bx)^2 dx$	272
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3.79	$\int x^2 \text{CosIntegral}(bx)^2 dx$	278
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3.81	$\int \text{CosIntegral}(bx)^2 dx$	285
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3.85	$\int x^m \text{CosIntegral}(a + bx) dx$	294
3.86	$\int x^3 \text{CosIntegral}(a + bx) dx$	296
3.87	$\int x^2 \text{CosIntegral}(a + bx) dx$	299
3.88	$\int x \text{CosIntegral}(a + bx) dx$	302
3.89	$\int \text{CosIntegral}(a + bx) dx$	305
3.90	$\int \frac{\text{CosIntegral}(a+bx)}{x} dx$	307
3.91	$\int \frac{\text{CosIntegral}(a+bx)}{x^2} dx$	309
3.92	$\int \frac{\text{CosIntegral}(a+bx)}{x^3} dx$	312
3.93	$\int x^m \text{CosIntegral}(a + bx)^2 dx$	316
3.94	$\int x^2 \text{CosIntegral}(a + bx)^2 dx$	318
3.95	$\int x \text{CosIntegral}(a + bx)^2 dx$	323
3.96	$\int \text{CosIntegral}(a + bx)^2 dx$	327
3.97	$\int \frac{\text{CosIntegral}(a+bx)^2}{x} dx$	330
3.98	$\int \frac{\text{CosIntegral}(a+bx)^2}{x^2} dx$	332
3.99	$\int \frac{\text{CosIntegral}(a+bx)^2}{x^3} dx$	334
3.100	$\int x^2 \text{CosIntegral}(d(a + b \log(cx^n))) dx$	336
3.101	$\int x \text{CosIntegral}(d(a + b \log(cx^n))) dx$	339
3.102	$\int \text{CosIntegral}(d(a + b \log(cx^n))) dx$	342
3.103	$\int \frac{\text{CosIntegral}(d(a+b \log(cx^n)))}{x} dx$	345
3.104	$\int \frac{\text{CosIntegral}(d(a+b \log(cx^n)))}{x^2} dx$	348
3.105	$\int \frac{\text{CosIntegral}(d(a+b \log(cx^n)))}{x^3} dx$	351
3.106	$\int (ex)^m \text{CosIntegral}(d(a + b \log(cx^n))) dx$	354
3.107	$\int \frac{\text{CosIntegral}(bx) \sin(bx)}{x^3} dx$	357
3.108	$\int \frac{\text{CosIntegral}(bx) \sin(bx)}{x^2} dx$	360
3.109	$\int \frac{\text{CosIntegral}(bx) \sin(bx)}{x} dx$	363
3.110	$\int \text{CosIntegral}(bx) \sin(bx) dx$	365
3.111	$\int x \text{CosIntegral}(bx) \sin(bx) dx$	368
3.112	$\int x^2 \text{CosIntegral}(bx) \sin(bx) dx$	371
3.113	$\int x^3 \text{CosIntegral}(bx) \sin(bx) dx$	375
3.114	$\int \frac{\cos(bx)\text{CosIntegral}(bx)}{x^3} dx$	379
3.115	$\int \frac{\cos(bx)\text{CosIntegral}(bx)}{x^2} dx$	383

3.116	$\int \frac{\cos(bx)\text{CosIntegral}(bx)}{x} dx$	385
3.117	$\int \cos(bx)\text{CosIntegral}(bx) dx$	387
3.118	$\int x \cos(bx)\text{CosIntegral}(bx) dx$	390
3.119	$\int x^2 \cos(bx)\text{CosIntegral}(bx) dx$	393
3.120	$\int x^3 \cos(bx)\text{CosIntegral}(bx) dx$	397
3.121	$\int \text{CosIntegral}(2x) \sin(5x) dx$	401
3.122	$\int \cos(5x)\text{CosIntegral}(2x) dx$	404
3.123	$\int x^2 \text{CosIntegral}(a + bx) \sin(a + bx) dx$	407
3.124	$\int x \text{CosIntegral}(a + bx) \sin(a + bx) dx$	411
3.125	$\int \text{CosIntegral}(a + bx) \sin(a + bx) dx$	415
3.126	$\int \frac{\text{CosIntegral}(a+bx) \sin(a+bx)}{x} dx$	418
3.127	$\int x^2 \cos(a + bx)\text{CosIntegral}(a + bx) dx$	420
3.128	$\int x \cos(a + bx)\text{CosIntegral}(a + bx) dx$	424
3.129	$\int \cos(a + bx)\text{CosIntegral}(a + bx) dx$	427
3.130	$\int \frac{\cos(a+bx)\text{CosIntegral}(a+bx)}{x} dx$	430
3.131	$\int x \text{CosIntegral}(c + dx) \sin(a + bx) dx$	432
3.132	$\int \text{CosIntegral}(c + dx) \sin(a + bx) dx$	437
3.133	$\int \frac{\text{CosIntegral}(c+dx) \sin(a+bx)}{x} dx$	445
3.134	$\int x \cos(a + bx)\text{CosIntegral}(c + dx) dx$	447
3.135	$\int \cos(a + bx)\text{CosIntegral}(c + dx) dx$	452
3.136	$\int \frac{\cos(a+bx)\text{CosIntegral}(c+dx)}{x} dx$	460

4 Listing of Grading functions

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Chapter 1

Introduction

This report gives the result of running the computer algebra independent integration problems. The listing of the problems are maintained by and can be downloaded from <https://rulebasedintegration.org>

The number of integrals in this report is [136]. This is test number [206].

1.1 Listing of CAS systems tested

The following systems were tested at this time.

1. Mathematica 12.1 (64 bit) on windows 10.
2. Rubi 4.16.1 in Mathematica 12 on windows 10.
3. Maple 2020 (64 bit) on windows 10.
4. Maxima 5.43 on Linux. (via sagemath 8.9)
5. Fricas 1.3.6 on Linux (via sagemath 9.0)
6. Sympy 1.5 under Python 3.7.3 using Anaconda distribution.
7. Giac/Xcas 1.5 on Linux. (via sagemath 8.9)

Maxima, Fricas and Giac/Xcas were called from inside SageMath. This was done using SageMath integrate command by changing the name of the algorithm to use the different CAS systems.

Sympy was called directly using Python.

1.2 Results

Important note: A number of problems in this test suite have no antiderivative in closed form. This means the antiderivative of these integrals can not be expressed in terms of elementary, special functions or Hypergeometric2F1 functions. RootSum and RootOf are not allowed.

If a CAS returns the above integral unevaluated within the time limit, then the result is counted as passed and assigned an A grade.

However, if CAS times out, then it is assigned an F grade even if the integral is not integrable, as this implies CAS could not determine that the integral is not integrable in the time limit.

If a CAS returns an antiderivative to such an integral, it is assigned an A grade automatically and this special result is listed in the introduction section of each individual test report to make it easy to identify as this can be important result to investigate.

The results given in in the table below reflects the above.

System	solved	Failed
Rubi	% 100. (136)	% 0. (0)
Mathematica	% 98.53 (134)	% 1.47 (2)
Maple	% 86.76 (118)	% 13.24 (18)
Maxima	% 25. (34)	% 75. (102)
Fricas	% 25. (34)	% 75. (102)
Sympy	% 36.76 (50)	% 63.24 (86)
Giac	% 77.94 (106)	% 22.06 (30)

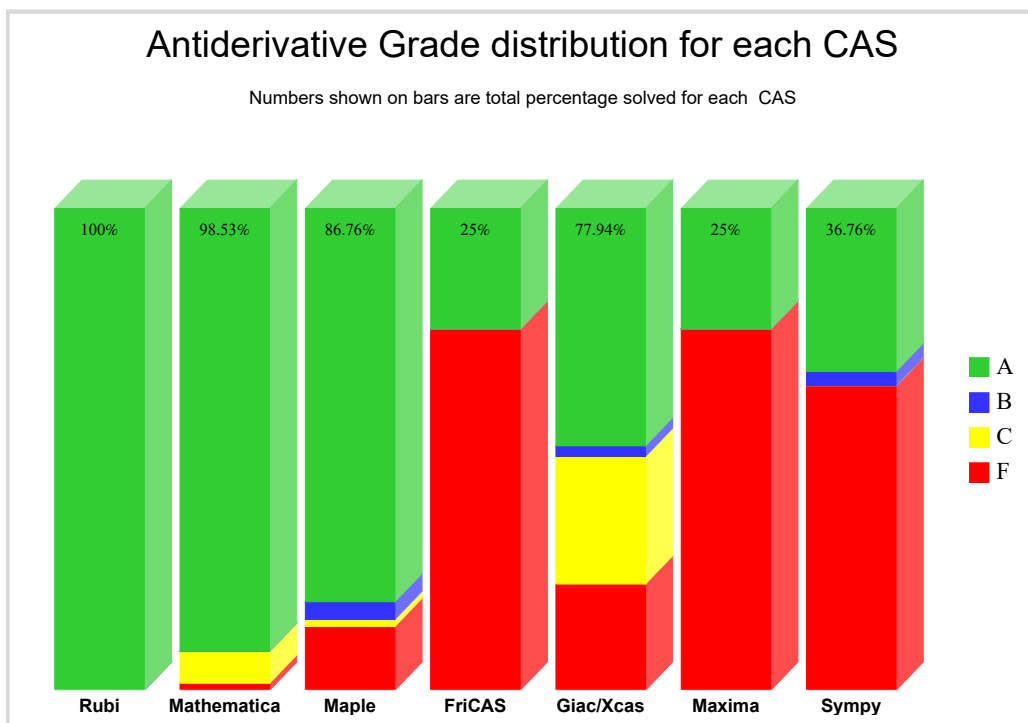
The table below gives additional break down of the grading of quality of the antiderivatives generated by each CAS. The grading is given using the letters A,B,C and F with A being the best quality. The grading is accomplished by comparing the antiderivative generated with the optimal antiderivatives included in the test suite. The following table describes the meaning of these grades.

grade	description
A	Integral was solved and antiderivative is optimal in quality and leaf size.
B	Integral was solved and antiderivative is optimal in quality but leaf size is larger than twice the optimal antiderivatives leaf size.
C	Integral was solved and antiderivative is non-optimal in quality. This can be due to one or more of the following reasons <ol style="list-style-type: none"> 1. antiderivative contains a hypergeometric function and the optimal antiderivative does not. 2. antiderivative contains a special function and the optimal antiderivative does not. 3. antiderivative contains the imaginary unit and the optimal antiderivative does not.
F	Integral was not solved. Either the integral was returned unevaluated within the time limit, or it timed out, or CAS hanged or crashed or an exception was raised.

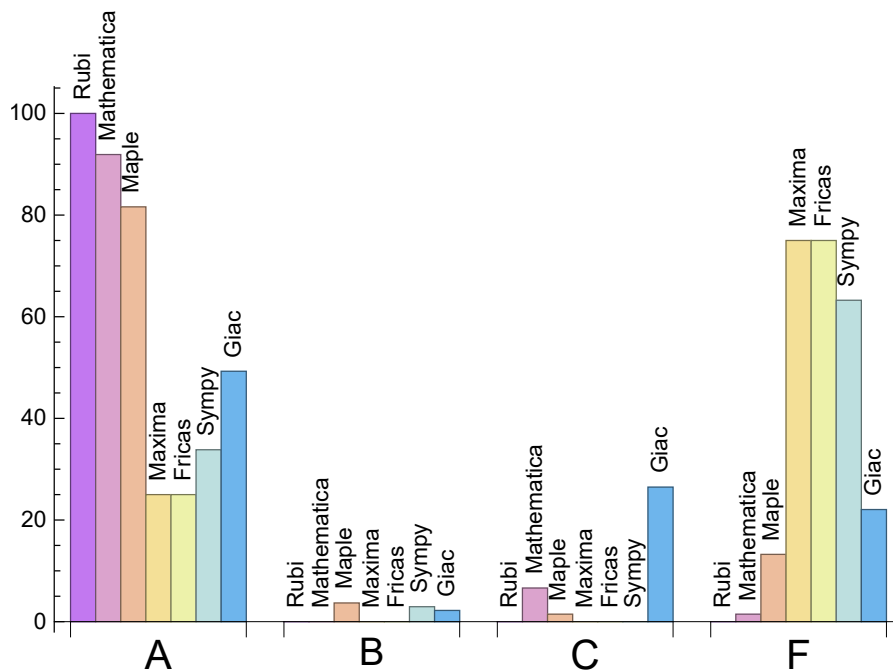
Grading is implemented for all CAS systems. Based on the above, the following table summarizes the grading for this test suite.

System	% A grade	% B grade	% C grade	% F grade
Rubi	100.	0.	0.	0.
Mathematica	91.91	0.	6.62	1.47
Maple	81.62	3.68	1.47	13.24
Maxima	25.	0.	0.	75.
Fricas	25.	0.	0.	75.
Sympy	33.82	2.94	0.	63.24
Giac	49.26	2.21	26.47	22.06

The following is a Bar chart illustration of the data in the above table.



The figure below compares the CAS systems for each grade level.



1.3 Performance

The table below summarizes the performance of each CAS system in terms of CPU time and leaf size of results.

System	Mean time (sec)	Mean size	Normalized mean	Median size	Normalized median
Rubi	0.19	78.26	0.75	49.	1.
Mathematica	1.65	62.69	0.65	44.	0.72
Maple	0.07	97.07	0.78	43.	0.88
Maxima	0.	0.	0.	0.	0.
Fricas	0.	0.	0.	0.	0.
Sympy	0.5	26.14	0.5	0.	0.
Giac	0.86	555.75	4.24	62.	1.02

1.4 list of integrals that has no closed form antiderivative

{9, 14, 15, 16, 17, 22, 25, 29, 30, 31, 40, 46, 48, 58, 62, 65, 68, 77, 82, 83, 84, 85, 90, 93, 97, 98, 99, 107, 109, 115, 126, 130, 133, 136}

1.5 list of integrals solved by CAS but has no known antiderivative

Rubi {}

Mathematica {}

Maple {}

Maxima {}

Fricas {}

Sympy {}

Giac {}

1.6 list of integrals solved by CAS but failed verification

The following are integrals solved by CAS but the verification phase failed to verify the anti-derivative produced is correct. This does not mean necessarily that the anti-derivative is wrong, as additional methods of verification might be needed, or more time is needed (3 minutes time limit was used). These integrals are listed here to make it easier to do further investigation to determine why it was not possible to verify the result produced.

Rubi {}

Mathematica {41, 49, 63, 64, 66, 67}

Maple Verification phase not implemented yet.

Maxima Verification phase not implemented yet.

Fricas Verification phase not implemented yet.

Sympy Verification phase not implemented yet.

Giac Verification phase not implemented yet.

1.7 Timing

The command `AboluteTiming[]` was used in Mathematica to obtain the elapsed time for each integrate call. In Maple, the command `Usage` was used as in the following example

```
cpu_time := Usage(assign ('result_of _int',int(expr,x)),output='realtime')
```

For all other CAS systems, the elapsed time to complete each integral was found by taking the difference between the time after the call has completed from the time before the call was made. This was done using Python's `time.time()` call.

All elapsed times shown are in seconds. A time limit of 3 minutes was used for each integral. If the integrate command did not complete within this time limit, the integral was aborted and considered to have failed and assigned an F grade. The time used by failed integrals due to time out is not counted in the final statistics.

1.8 Verification

A verification phase was applied on the result of integration for Rubi and Mathematica. Future version of this report will implement verification for the other CAS systems. For the integrals whose result was not run through a verification phase, it is assumed that the antiderivative produced was correct.

Verification phase has 3 minutes time out. An integral whose result was not verified could still be correct. Further investigation is needed on those integrals which failed verifications. Such integrals are marked in the summary table below and also in each integral separate section so they are easy to identify and locate.

1.9 Important notes about some of the results

1.9.1 Important note about Maxima results

Since these integrals are run in a batch mode, using an automated script, and by using `sagemath` (SageMath uses Maxima), then any integral where Maxima needs an interactive response from the user to answer a question during evaluation of the integral in order to complete the integration, will fail and is counted as failed.

The exception raised is `ValueError`. Therefore Maxima result below is lower than what could result if Maxima was run directly and each question Maxima asks was answered correctly.

The percentage of such failures were not counted for each test file, but for an example, for the Timofeev test file, there were about 30 such integrals out of total 705, or about 4 percent. This pecentage can be higher or lower depending on the specific input test file.

Such integrals can be indentified by looking at the output of the integration in each section for Maxima. If the output was an exception `ValueError` then this is most likely due to this reason.

Maxima integrate was run using SageMath with the following settings set by default

```
'besselexpand : true'
'display2d : false'
'domain : complex'
'keepfloat : true'
'load(to_poly_solve)'
'load(simplify_sum)'
'load(abs_integrate)' 'load(diag)'
```

SageMath loading of Maxima `abs_integrate` was found to cause some problem. So the following code was added to disable this effect.

```
from sage.interfaces.maxima_lib import maxima_lib
maxima_lib.set('extra_definite_integration_methods', '[]')
maxima_lib.set('extra_integration_methods', '[]')
```

See <https://ask.sagemath.org/question/43088/integrate-results-that-are-different-from-using-maxima/> for reference.

1.9.2 Important note about FriCAS and Giac/X-CAS results

There are Few integrals which failed due to SageMath not able to translate the result back to SageMath syntax and not because these CAS system were not able to do the integrations.

These will fail With error Exception raised: NotImplementedError

The number of such cases seems to be very small. About 1 or 2 percent of all integrals.

Hopefully the next version of SageMath will have complete translation of FriCAS and XCAS syntax and I will re-run all the tests again when this happens.

1.9.3 Important note about finding leaf size of antiderivative

For Mathematica, Rubi and Maple, the builtin system function LeafSize is used to find the leaf size of each antiderivative.

The other CAS systems (SageMath and Sympy) do not have special builtin function for this purpose at this time. Therefore the leaf size is determined as follows.

For Fricas, Giac and Maxima (all called via sagemath) the following code is used

#see <https://stackoverflow.com/questions/25202346/how-to-obtain-leaf-count-expression-size-in->

```
def tree(expr):
    if expr.operator() is None:
        return expr
    else:
        return [expr.operator()+map(tree, expr.operands())

try:
    # 1.35 is a fudge factor since this estimate of leaf count is bit lower than
    #what it should be compared to Mathematica's
    leafCount = round(1.35*len(flatten(tree(anti))))
except Exception as ee:
    leafCount =1
```

For Sympy, called directly from Python, the following code is used

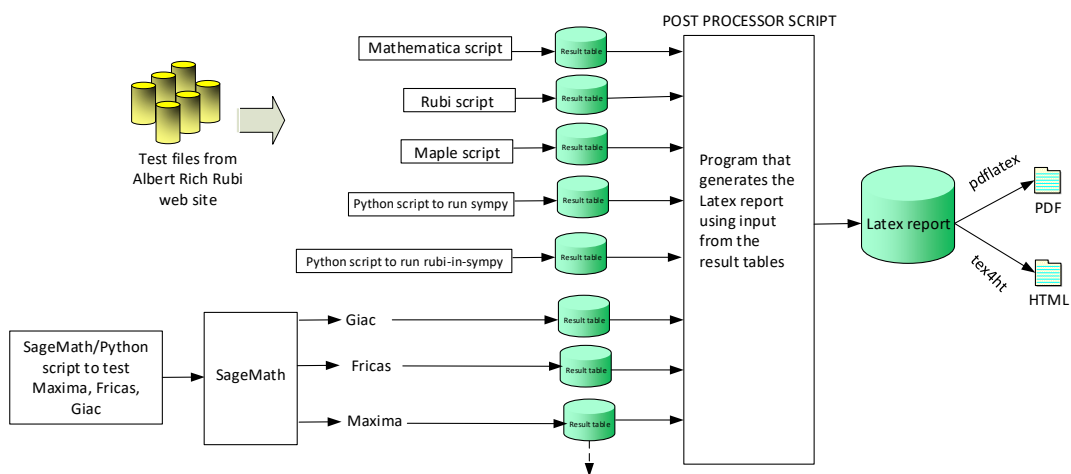
```
try:
    # 1.7 is a fudge factor since it is low side from actual leaf count
    leafCount = round(1.7*count_ops(anti))

except Exception as ee:
    leafCount =1
```

When these cas systems have a builtin function to find the leaf size of expressions, it will be used instead, and these tests run again.

1.10 Design of the test system

The following diagram gives a high level view of the current test build system.



One record (line) per one integral result. The line is CSV comma separated. It contains 13 fields. This is description of each record (line)

1. integer, the problem number.
2. integer. 0 or 1 for failed or passed. (this is not the grade field)
3. integer. Leaf size of result.
4. integer. Leaf size of the optimal antiderivative.
5. number. CPU time used to solve this integral. 0 if failed.
6. string. The integral in Latex format
7. string. The input used in CAS own syntax.
8. string. The result (antiderivative) produced by CAS in Latex format
9. string. The optimal antiderivative in Latex format.
10. integer. 0 or 1. Indicates if problem has known antiderivative or not
11. String. The result (antiderivative) in CAS own syntax.
12. String. The grade of the antiderivative. Can be "A", "B", "C", or "F"
13. String. The optimal antiderivative in CAS own syntax.

High level overview of the CAS independent integration test build system

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June 22, 2018

Chapter 2

detailed summary tables of results

2.1 List of integrals sorted by grade for each CAS

2.1.1 Rubi

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136 }

B grade: { }

C grade: { }

F grade: { }

2.1.2 Mathematica

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 40, 42, 43, 44, 45, 46, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 65, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 133, 136 }

B grade: { }

C grade: { 41, 63, 64, 66, 67, 131, 132, 134, 135 }

F grade: { 39, 47 }

2.1.3 Maple

A grade: { 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 27, 28, 29, 30, 31, 35, 40, 41, 42, 43, 44, 45, 46, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 64, 65, 67, 68, 70, 71, 72, 73, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 95, 96, 97, 98, 99, 103, 107, 109, 110, 111, 112, 113, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 132, 133, 135, 136 }

B grade: { 63, 66, 74, 131, 134 }

C grade: { 1, 69 }

F grade: { 26, 32, 33, 34, 36, 37, 38, 39, 47, 94, 100, 101, 102, 104, 105, 106, 108, 114 }

2.1.4 Maxima

A grade: { 9, 14, 15, 16, 17, 22, 25, 29, 30, 31, 40, 46, 48, 58, 62, 65, 68, 77, 82, 83, 84, 85, 90, 93, 97, 98, 99, 107, 109, 115, 126, 130, 133, 136 }

B grade: { }

C grade: { }

F grade: { 1, 2, 3, 4, 5, 6, 7, 8, 10, 11, 12, 13, 18, 19, 20, 21, 23, 24, 26, 27, 28, 32, 33, 34, 35, 36, 37, 38, 39, 41, 42, 43, 44, 45, 47, 49, 50, 51, 52, 53, 54, 55, 56, 57, 59, 60, 61, 63, 64, 66, 67, 69, 70, 71, 72, 73, 74, 75, 76, 78, 79, 80, 81, 86, 87, 88, 89, 91, 92, 94, 95, 96, 100, 101, 102, 103, 104, 105, 106, 108, 110, 111, 112, 113, 114, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 127, 128, 129, 131, 132, 134, 135 }

2.1.5 FriCAS

A grade: { 9, 14, 15, 16, 17, 22, 25, 29, 30, 31, 40, 46, 48, 58, 62, 65, 68, 77, 82, 83, 84, 85, 90, 93, 97, 98, 99, 107, 109, 115, 126, 130, 133, 136 }

B grade: { }

C grade: { }

F grade: { 1, 2, 3, 4, 5, 6, 7, 8, 10, 11, 12, 13, 18, 19, 20, 21, 23, 24, 26, 27, 28, 32, 33, 34, 35, 36, 37, 38, 39, 41, 42, 43, 44, 45, 47, 49, 50, 51, 52, 53, 54, 55, 56, 57, 59, 60, 61, 63, 64, 66, 67, 69, 70, 71, 72, 73, 74, 75, 76, 78, 79, 80, 81, 86, 87, 88, 89, 91, 92, 94, 95, 96, 100, 101, 102, 103, 104, 105, 106, 108, 110, 111, 112, 113, 114, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 127, 128, 129, 131, 132, 134, 135 }

2.1.6 SymPy

A grade: { 1, 2, 3, 4, 5, 7, 8, 9, 14, 15, 16, 17, 22, 25, 29, 30, 31, 40, 41, 46, 48, 58, 62, 65, 68, 70, 71, 72, 77, 82, 83, 84, 85, 90, 93, 97, 98, 99, 107, 109, 115, 116, 126, 130, 133, 136 }

B grade: { 69, 73, 75, 76 }

C grade: { }

F grade: { 6, 10, 11, 12, 13, 18, 19, 20, 21, 23, 24, 26, 27, 28, 32, 33, 34, 35, 36, 37, 38, 39, 42, 43, 44, 45, 47, 49, 50, 51, 52, 53, 54, 55, 56, 57, 59, 60, 61, 63, 64, 66, 67, 74, 78, 79, 80, 81, 86, 87, 88, 89, 91, 92, 94, 95, 96, 100, 101, 102, 103, 104, 105, 106, 108, 110, 111, 112, 113, 114, 117, 118, 119, 120, 121, 122, 123, 124, 125, 127, 128, 129, 131, 132, 134, 135 }

2.1.7 Giac

A grade: { 2, 3, 4, 5, 7, 9, 10, 12, 14, 15, 16, 17, 22, 25, 29, 30, 31, 35, 40, 41, 43, 45, 46, 48, 49, 51, 53, 54, 58, 62, 65, 68, 70, 71, 72, 73, 76, 77, 78, 80, 82, 83, 84, 85, 86, 87, 88, 90, 93, 97, 98, 99, 103, 107, 109, 110, 112, 115, 116, 118, 120, 121, 122, 126, 130, 133, 136 }

B grade: { 61, 89, 125 }

C grade: { 8, 11, 13, 18, 19, 20, 21, 23, 24, 42, 44, 50, 52, 55, 56, 57, 59, 60, 64, 67, 75, 79, 81, 91, 92, 111, 113, 117, 119, 123, 124, 127, 128, 129, 132, 135 }

F grade: { 1, 6, 26, 27, 28, 32, 33, 34, 36, 37, 38, 39, 47, 63, 66, 69, 74, 94, 95, 96, 100, 101, 102, 104, 105, 106, 108, 114, 131, 134 }

2.2 Detailed conclusion table per each integral for all CAS systems

Detailed conclusion table per each integral is given by table below. The elapsed time is in seconds. For failed result it is given as F(-1) if the failure was due to timeout. It is given as F(-2) if the failure was due to an exception being raised, which could indicate a bug in the system. If the failure was due to integral not being evaluated within the time limit, then it is given just an F.

In this table, the column **normalized size** is defined as $\frac{\text{antiderivative leaf size}}{\text{optimal antiderivative leaf size}}$

Problem 1	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	C	F	F	A	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	86	86	82	37	0	0	46	0
normalized size	1	1.	0.95	0.43	0.	0.	0.53	0.
time (sec)	N/A	0.074	0.054	0.171	0.	0.	0.958	0.

Problem 2	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	63	63	50	56	0	0	61	66
normalized size	1	1.	0.79	0.89	0.	0.	0.97	1.05
time (sec)	N/A	0.068	0.036	0.056	0.	0.	1.272	1.295

Problem 3	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	49	49	41	44	0	0	46	51
normalized size	1	1.	0.84	0.9	0.	0.	0.94	1.04
time (sec)	N/A	0.046	0.027	0.054	0.	0.	1.474	1.287

Problem 4	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	35	35	35	32	0	0	29	39
normalized size	1	1.	1.	0.91	0.	0.	0.83	1.11
time (sec)	N/A	0.023	0.006	0.05	0.	0.	0.743	1.305

Problem 5	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	15	15	15	17	0	0	12	20
normalized size	1	1.	1.	1.13	0.	0.	0.8	1.33
time (sec)	N/A	0.004	0.001	0.05	0.	0.	0.802	1.251

Problem 6	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	43	43	43	20	0	0	0	0
normalized size	1	1.	1.	0.47	0.	0.	0.	0.
time (sec)	N/A	0.02	0.004	0.069	0.	0.	0.	0.

Problem 7	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	25	25	25	32	0	0	36	50
normalized size	1	1.	1.	1.28	0.	0.	1.44	2.
time (sec)	N/A	0.045	0.01	0.054	0.	0.	1.169	1.203

Problem 8	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	A	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	46	46	46	48	0	0	41	201
normalized size	1	1.	1.	1.04	0.	0.	0.89	4.37
time (sec)	N/A	0.065	0.013	0.052	0.	0.	0.891	1.353

Problem 9	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.031	2.513	0.059	0.	0.	0.	0.

Problem 10	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	149	149	107	149	0	0	0	119
normalized size	1	1.	0.72	1.	0.	0.	0.	0.8
time (sec)	N/A	0.216	0.13	0.069	0.	0.	0.	1.287

Problem 11	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	112	112	78	84	0	0	0	105
normalized size	1	1.	0.7	0.75	0.	0.	0.	0.94
time (sec)	N/A	0.135	0.073	0.149	0.	0.	0.	1.281

Problem 12	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	74	74	58	69	0	0	0	76
normalized size	1	1.	0.78	0.93	0.	0.	0.	1.03
time (sec)	N/A	0.095	0.053	0.058	0.	0.	0.	1.325

Problem 13	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	32	32	32	32	0	0	0	66
normalized size	1	1.	1.	1.	0.	0.	0.	2.06
time (sec)	N/A	0.051	0.008	0.05	0.	0.	0.	1.34

Problem 14	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.023	0.424	0.053	0.	0.	0.	0.

Problem 15	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.024	0.469	0.056	0.	0.	0.	0.

Problem 16	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.025	0.501	0.054	0.	0.	0.	0.

Problem 17	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	47	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.295	4.095	0.185	0.	0.	0.	0.

Problem 18	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	184	184	96	157	0	0	0	74
normalized size	1	1.	0.52	0.85	0.	0.	0.	0.4
time (sec)	N/A	0.368	0.197	0.049	0.	0.	0.	1.286

Problem 19	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	118	118	63	99	0	0	0	74
normalized size	1	1.	0.53	0.84	0.	0.	0.	0.63
time (sec)	N/A	0.277	0.141	0.053	0.	0.	0.	1.218

Problem 20	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	71	71	50	61	0	0	0	74
normalized size	1	1.	0.7	0.86	0.	0.	0.	1.04
time (sec)	N/A	0.206	0.1	0.051	0.	0.	0.	1.264

Problem 21	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	26	26	41	24	0	0	0	62
normalized size	1	1.	1.58	0.92	0.	0.	0.	2.38
time (sec)	N/A	0.005	0.036	0.049	0.	0.	0.	1.345

Problem 22	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.024	0.655	0.061	0.	0.	0.	0.

Problem 23	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	46	46	39	48	0	0	0	244
normalized size	1	1.	0.85	1.04	0.	0.	0.	5.3
time (sec)	N/A	0.232	0.073	0.057	0.	0.	0.	1.318

Problem 24	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	111	111	84	86	0	0	0	1092
normalized size	1	1.	0.76	0.77	0.	0.	0.	9.84
time (sec)	N/A	0.325	0.331	0.06	0.	0.	0.	1.337

Problem 25	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.044	5.25	0.148	0.	0.	0.	0.

Problem 26	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	329	329	158	0	0	0	0	0
normalized size	1	1.	0.48	0.	0.	0.	0.	0.
time (sec)	N/A	1.495	1.711	0.056	0.	0.	0.	0.

Problem 27	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	154	154	95	135	0	0	0	0
normalized size	1	1.	0.62	0.88	0.	0.	0.	0.
time (sec)	N/A	0.333	0.28	0.066	0.	0.	0.	0.

Problem 28	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	49	49	43	45	0	0	0	0
normalized size	1	1.	0.88	0.92	0.	0.	0.	0.
time (sec)	N/A	0.065	0.009	0.049	0.	0.	0.	0.

Problem 29	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.034	3.302	0.051	0.	0.	0.	0.

Problem 30	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.034	5.059	0.056	0.	0.	0.	0.

Problem 31	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.034	2.753	0.059	0.	0.	0.	0.

Problem 32	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F(-1)
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	137	137	106	0	0	0	0	0
normalized size	1	1.	0.77	0.	0.	0.	0.	0.
time (sec)	N/A	0.276	1.726	0.097	0.	0.	0.	0.

Problem 33	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F(-1)
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	137	137	106	0	0	0	0	0
normalized size	1	1.	0.77	0.	0.	0.	0.	0.
time (sec)	N/A	0.263	1.694	0.095	0.	0.	0.	0.

Problem 34	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F(-1)
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	128	128	102	0	0	0	0	0
normalized size	1	1.	0.8	0.	0.	0.	0.	0.
time (sec)	N/A	0.238	1.642	0.069	0.	0.	0.	0.

Problem 35	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	54	54	95	72	0	0	0	80
normalized size	1	1.	1.76	1.33	0.	0.	0.	1.48
time (sec)	N/A	0.031	0.064	0.075	0.	0.	0.	1.571

Problem 36	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F(-1)
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	131	131	107	0	0	0	0	0
normalized size	1	1.	0.82	0.	0.	0.	0.	0.
time (sec)	N/A	0.254	1.684	0.092	0.	0.	0.	0.

Problem 37	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F(-1)
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	139	139	111	0	0	0	0	0
normalized size	1	1.	0.8	0.	0.	0.	0.	0.
time (sec)	N/A	0.251	1.698	0.092	0.	0.	0.	0.

Problem 38	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F(-1)
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	176	176	128	0	0	0	0	0
normalized size	1	1.	0.73	0.	0.	0.	0.	0.
time (sec)	N/A	0.315	3.02	0.093	0.	0.	0.	0.

Problem 39	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	F	F	F	F	F	F
verified	N/A	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	96	96	0	0	0	0	0	0
normalized size	1	1.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.203	1.004	0.056	0.	0.	0.	0.

Problem 40	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	48	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.152	0.821	0.057	0.	0.	0.	0.

Problem 41	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F	F	A	A
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	10	10	26	9	0	0	7	11
normalized size	1	1.	2.6	0.9	0.	0.	0.7	1.1
time (sec)	N/A	0.021	0.014	0.041	0.	0.	1.06	1.146

Problem 42	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	26	26	26	23	0	0	0	55
normalized size	1	1.	1.	0.88	0.	0.	0.	2.12
time (sec)	N/A	0.046	0.011	0.05	0.	0.	0.	1.224

Problem 43	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	61	61	44	58	0	0	0	62
normalized size	1	1.	0.72	0.95	0.	0.	0.	1.02
time (sec)	N/A	0.081	0.079	0.062	0.	0.	0.	1.164

Problem 44	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	91	91	64	69	0	0	0	89
normalized size	1	1.	0.7	0.76	0.	0.	0.	0.98
time (sec)	N/A	0.111	0.104	0.059	0.	0.	0.	1.161

Problem 45	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	126	126	93	138	0	0	0	104
normalized size	1	1.	0.74	1.1	0.	0.	0.	0.83
time (sec)	N/A	0.194	0.177	0.059	0.	0.	0.	1.177

Problem 46	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	102	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.188	0.829	0.084	0.	0.	0.	0.

Problem 47	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	F	F	F	F	F	F
verified	N/A	Yes	N/A	TBD	TBD	TBD	TBD	TBD
size	44	44	0	0	0	0	0	0
normalized size	1	1.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.095	0.617	0.062	0.	0.	0.	0.

Problem 48	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.026	0.954	0.056	0.	0.	0.	0.

Problem 49	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	34	34	36	33	0	0	0	45
normalized size	1	1.	1.06	0.97	0.	0.	0.	1.32
time (sec)	N/A	0.058	0.013	0.053	0.	0.	0.	1.182

Problem 50	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	61	61	42	44	0	0	0	74
normalized size	1	1.	0.69	0.72	0.	0.	0.	1.21
time (sec)	N/A	0.066	0.049	0.056	0.	0.	0.	1.177

Problem 51	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	98	98	72	105	0	0	0	88
normalized size	1	1.	0.73	1.07	0.	0.	0.	0.9
time (sec)	N/A	0.123	0.097	0.065	0.	0.	0.	1.172

Problem 52	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	128	128	94	111	0	0	0	115
normalized size	1	1.	0.73	0.87	0.	0.	0.	0.9
time (sec)	N/A	0.179	0.105	0.078	0.	0.	0.	1.19

Problem 53	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F(-2)	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	29	29	25	24	0	0	0	31
normalized size	1	1.	0.86	0.83	0.	0.	0.	1.07
time (sec)	N/A	0.055	0.026	0.124	0.	0.	0.	1.201

Problem 54	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F(-2)	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	29	29	25	24	0	0	0	31
normalized size	1	1.	0.86	0.83	0.	0.	0.	1.07
time (sec)	N/A	0.056	0.026	0.131	0.	0.	0.	1.182

Problem 55	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F(-1)	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	187	187	123	171	0	0	0	223
normalized size	1	1.	0.66	0.91	0.	0.	0.	1.19
time (sec)	N/A	0.708	0.326	0.063	0.	0.	0.	1.229

Problem 56	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	97	97	71	89	0	0	0	146
normalized size	1	1.	0.73	0.92	0.	0.	0.	1.51
time (sec)	N/A	0.275	0.238	0.057	0.	0.	0.	1.19

Problem 57	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	34	34	33	31	0	0	0	77
normalized size	1	1.	0.97	0.91	0.	0.	0.	2.26
time (sec)	N/A	0.054	0.017	0.049	0.	0.	0.	1.199

Problem 58	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.123	4.921	0.081	0.	0.	0.	0.

Problem 59	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F(-1)	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	218	218	134	209	0	0	0	231
normalized size	1	1.	0.61	0.96	0.	0.	0.	1.06
time (sec)	N/A	0.66	0.343	0.068	0.	0.	0.	1.218

Problem 60	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	108	108	74	105	0	0	0	144
normalized size	1	1.	0.69	0.97	0.	0.	0.	1.33
time (sec)	N/A	0.232	0.198	0.061	0.	0.	0.	1.202

Problem 61	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	46	46	45	43	0	0	0	128
normalized size	1	1.	0.98	0.93	0.	0.	0.	2.78
time (sec)	N/A	0.075	0.021	0.055	0.	0.	0.	1.173

Problem 62	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.125	2.614	0.086	0.	0.	0.	0.

Problem 63	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	B	F	F	F	F(-1)
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	371	371	345	1212	0	0	0	0
normalized size	1	1.	0.93	3.27	0.	0.	0.	0.
time (sec)	N/A	0.92	5.313	0.108	0.	0.	0.	0.

Problem 64	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F	F	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	154	154	168	282	0	0	0	12880
normalized size	1	1.	1.09	1.83	0.	0.	0.	83.64
time (sec)	N/A	0.228	1.971	0.072	0.	0.	0.	2.034

Problem 65	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.142	28.787	0.088	0.	0.	0.	0.

Problem 66	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	B	F	F	F	F(-1)
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	370	370	393	1208	0	0	0	0
normalized size	1	1.	1.06	3.26	0.	0.	0.	0.
time (sec)	N/A	1.24	4.214	0.107	0.	0.	0.	0.

Problem 67	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F	F	F	C
verified	N/A	Yes	NO	TBD	TBD	TBD	TBD	TBD
size	153	153	164	280	0	0	0	12439
normalized size	1	1.	1.07	1.83	0.	0.	0.	81.3
time (sec)	N/A	0.223	1.745	0.079	0.	0.	0.	1.97

Problem 68	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.107	13.115	0.093	0.	0.	0.	0.

Problem 69	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	C	F	F	B	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	90	90	78	124	0	0	654	0
normalized size	1	1.	0.87	1.38	0.	0.	7.27	0.
time (sec)	N/A	0.082	0.076	0.099	0.	0.	2.174	0.

Problem 70	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	63	63	53	56	0	0	85	66
normalized size	1	1.	0.84	0.89	0.	0.	1.35	1.05
time (sec)	N/A	0.071	0.04	0.048	0.	0.	2.905	1.195

Problem 71	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	49	49	44	44	0	0	70	51
normalized size	1	1.	0.9	0.9	0.	0.	1.43	1.04
time (sec)	N/A	0.048	0.029	0.05	0.	0.	2.435	1.171

Problem 72	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	35	35	35	32	0	0	53	39
normalized size	1	1.	1.	0.91	0.	0.	1.51	1.11
time (sec)	N/A	0.024	0.008	0.05	0.	0.	1.749	1.165

Problem 73	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	B	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	16	16	16	19	0	0	31	22
normalized size	1	1.	1.	1.19	0.	0.	1.94	1.38
time (sec)	N/A	0.004	0.001	0.045	0.	0.	1.684	1.191

Problem 74	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	B	F	F	F(-2)	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	61	61	94	158	0	0	0	0
normalized size	1	1.	1.54	2.59	0.	0.	0.	0.
time (sec)	N/A	0.023	0.039	0.091	0.	0.	0.	0.

Problem 75	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	B	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	26	26	26	34	0	0	42	147
normalized size	1	1.	1.	1.31	0.	0.	1.62	5.65
time (sec)	N/A	0.048	0.011	0.047	0.	0.	1.384	1.205

Problem 76	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	B	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	46	46	46	48	0	0	87	72
normalized size	1	1.	1.	1.04	0.	0.	1.89	1.57
time (sec)	N/A	0.068	0.014	0.053	0.	0.	3.134	1.161

Problem 77	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.033	2.707	0.056	0.	0.	0.	0.

Problem 78	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	163	163	108	148	0	0	0	119
normalized size	1	1.	0.66	0.91	0.	0.	0.	0.73
time (sec)	N/A	0.229	0.116	0.069	0.	0.	0.	1.183

Problem 79	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	112	112	78	84	0	0	0	104
normalized size	1	1.	0.7	0.75	0.	0.	0.	0.93
time (sec)	N/A	0.138	0.081	0.073	0.	0.	0.	1.221

Problem 80	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	75	75	58	70	0	0	0	76
normalized size	1	1.	0.77	0.93	0.	0.	0.	1.01
time (sec)	N/A	0.091	0.049	0.059	0.	0.	0.	1.298

Problem 81	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	31	31	31	30	0	0	0	66
normalized size	1	1.	1.	0.97	0.	0.	0.	2.13
time (sec)	N/A	0.054	0.008	0.047	0.	0.	0.	1.283

Problem 82	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.022	0.401	0.047	0.	0.	0.	0.

Problem 83	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.025	0.485	0.055	0.	0.	0.	0.

Problem 84	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.026	0.5	0.052	0.	0.	0.	0.

Problem 85	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	47	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.316	3.607	0.155	0.	0.	0.	0.

Problem 86	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	184	184	95	154	0	0	0	108
normalized size	1	1.	0.52	0.84	0.	0.	0.	0.59
time (sec)	N/A	0.374	0.218	0.052	0.	0.	0.	1.209

Problem 87	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	118	118	64	99	0	0	0	108
normalized size	1	1.	0.54	0.84	0.	0.	0.	0.92
time (sec)	N/A	0.272	0.15	0.049	0.	0.	0.	1.177

Problem 88	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	71	71	49	60	0	0	0	108
normalized size	1	1.	0.69	0.85	0.	0.	0.	1.52
time (sec)	N/A	0.207	0.105	0.049	0.	0.	0.	1.147

Problem 89	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	27	27	42	26	0	0	0	93
normalized size	1	1.	1.56	0.96	0.	0.	0.	3.44
time (sec)	N/A	0.006	0.036	0.043	0.	0.	0.	1.134

Problem 90	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	12	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.021	0.612	0.056	0.	0.	0.	0.

Problem 91	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	47	47	40	49	0	0	0	201
normalized size	1	1.	0.85	1.04	0.	0.	0.	4.28
time (sec)	N/A	0.222	0.08	0.057	0.	0.	0.	1.227

Problem 92	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	111	111	76	88	0	0	0	1010
normalized size	1	1.	0.68	0.79	0.	0.	0.	9.1
time (sec)	N/A	0.327	0.399	0.056	0.	0.	0.	1.232

Problem 93	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.042	5.273	0.142	0.	0.	0.	0.

Problem 94	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	329	329	159	0	0	0	0	0
normalized size	1	1.	0.48	0.	0.	0.	0.	0.
time (sec)	N/A	1.322	1.216	0.053	0.	0.	0.	0.

Problem 95	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	155	155	96	136	0	0	0	0
normalized size	1	1.	0.62	0.88	0.	0.	0.	0.
time (sec)	N/A	0.338	0.327	0.061	0.	0.	0.	0.

Problem 96	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	48	48	41	43	0	0	0	0
normalized size	1	1.	0.85	0.9	0.	0.	0.	0.
time (sec)	N/A	0.065	0.011	0.046	0.	0.	0.	0.

Problem 97	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.03	1.315	0.049	0.	0.	0.	0.

Problem 98	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.036	2.179	0.059	0.	0.	0.	0.

Problem 99	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.035	2.52	0.066	0.	0.	0.	0.

Problem 100	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F(-1)
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	133	133	102	0	0	0	0	0
normalized size	1	1.	0.77	0.	0.	0.	0.	0.
time (sec)	N/A	0.251	1.743	0.096	0.	0.	0.	0.

Problem 101	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F(-1)
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	133	133	102	0	0	0	0	0
normalized size	1	1.	0.77	0.	0.	0.	0.	0.
time (sec)	N/A	0.247	1.716	0.092	0.	0.	0.	0.

Problem 102	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F(-1)
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	124	124	98	0	0	0	0	0
normalized size	1	1.	0.79	0.	0.	0.	0.	0.
time (sec)	N/A	0.228	1.658	0.073	0.	0.	0.	0.

Problem 103	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	55	55	96	73	0	0	0	82
normalized size	1	1.	1.75	1.33	0.	0.	0.	1.49
time (sec)	N/A	0.035	0.079	0.07	0.	0.	0.	1.336

Problem 104	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F(-1)
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	127	127	102	0	0	0	0	0
normalized size	1	1.	0.8	0.	0.	0.	0.	0.
time (sec)	N/A	0.247	1.701	0.096	0.	0.	0.	0.

Problem 105	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F(-1)
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	135	135	105	0	0	0	0	0
normalized size	1	1.	0.78	0.	0.	0.	0.	0.
time (sec)	N/A	0.239	1.713	0.097	0.	0.	0.	0.

Problem 106	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F(-1)
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	172	172	124	0	0	0	0	0
normalized size	1	1.	0.72	0.	0.	0.	0.	0.
time (sec)	N/A	0.295	3.042	0.082	0.	0.	0.	0.

Problem 107	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	102	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.251	1.466	0.056	0.	0.	0.	0.

Problem 108	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	44	44	44	0	0	0	0	0
normalized size	1	1.	1.	0.	0.	0.	0.	0.
time (sec)	N/A	0.103	0.01	0.059	0.	0.	0.	0.

Problem 109	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	14	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.027	2.051	0.057	0.	0.	0.	0.

Problem 110	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	35	35	37	34	0	0	0	46
normalized size	1	1.	1.06	0.97	0.	0.	0.	1.31
time (sec)	N/A	0.061	0.013	0.052	0.	0.	0.	1.168

Problem 111	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	62	62	44	45	0	0	0	77
normalized size	1	1.	0.71	0.73	0.	0.	0.	1.24
time (sec)	N/A	0.069	0.05	0.057	0.	0.	0.	1.178

Problem 112	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	111	111	72	107	0	0	0	89
normalized size	1	1.	0.65	0.96	0.	0.	0.	0.8
time (sec)	N/A	0.128	0.086	0.062	0.	0.	0.	1.153

Problem 113	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	147	147	94	111	0	0	0	116
normalized size	1	1.	0.64	0.76	0.	0.	0.	0.79
time (sec)	N/A	0.183	0.107	0.076	0.	0.	0.	1.237

Problem 114	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	97	97	97	0	0	0	0	0
normalized size	1	1.	1.	0.	0.	0.	0.	0.
time (sec)	N/A	0.199	0.014	0.082	0.	0.	0.	0.

Problem 115	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	50	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.093	0.444	0.057	0.	0.	0.	0.

Problem 116	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	A	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	10	10	10	9	0	0	7	11
normalized size	1	1.	1.	0.9	0.	0.	0.7	1.1
time (sec)	N/A	0.02	0.003	0.046	0.	0.	1.068	1.243

Problem 117	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	25	25	25	22	0	0	0	54
normalized size	1	1.	1.	0.88	0.	0.	0.	2.16
time (sec)	N/A	0.043	0.012	0.049	0.	0.	0.	1.255

Problem 118	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	60	60	42	57	0	0	0	59
normalized size	1	1.	0.7	0.95	0.	0.	0.	0.98
time (sec)	N/A	0.08	0.046	0.059	0.	0.	0.	1.194

Problem 119	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	89	89	64	66	0	0	0	88
normalized size	1	1.	0.72	0.74	0.	0.	0.	0.99
time (sec)	N/A	0.113	0.081	0.073	0.	0.	0.	1.2

Problem 120	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	142	142	93	136	0	0	0	103
normalized size	1	1.	0.65	0.96	0.	0.	0.	0.73
time (sec)	N/A	0.19	0.105	0.065	0.	0.	0.	1.263

Problem 121	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F(-2)	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	29	29	23	24	0	0	0	31
normalized size	1	1.	0.79	0.83	0.	0.	0.	1.07
time (sec)	N/A	0.056	0.026	0.104	0.	0.	0.	1.218

Problem 122	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F(-2)	F	A
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	29	29	27	24	0	0	0	31
normalized size	1	1.	0.93	0.83	0.	0.	0.	1.07
time (sec)	N/A	0.053	0.024	0.095	0.	0.	0.	1.245

Problem 123	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	220	220	134	211	0	0	0	230
normalized size	1	1.	0.61	0.96	0.	0.	0.	1.05
time (sec)	N/A	0.72	0.322	0.066	0.	0.	0.	1.319

Problem 124	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	109	109	76	106	0	0	0	150
normalized size	1	1.	0.7	0.97	0.	0.	0.	1.38
time (sec)	N/A	0.229	0.182	0.062	0.	0.	0.	1.214

Problem 125	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	47	47	46	44	0	0	0	130
normalized size	1	1.	0.98	0.94	0.	0.	0.	2.77
time (sec)	N/A	0.076	0.024	0.052	0.	0.	0.	1.191

Problem 126	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.131	6.969	0.085	0.	0.	0.	0.

Problem 127	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	185	185	123	168	0	0	0	221
normalized size	1	1.	0.66	0.91	0.	0.	0.	1.19
time (sec)	N/A	0.586	0.301	0.083	0.	0.	0.	1.208

Problem 128	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	96	96	69	88	0	0	0	143
normalized size	1	1.	0.72	0.92	0.	0.	0.	1.49
time (sec)	N/A	0.252	0.158	0.062	0.	0.	0.	1.178

Problem 129	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	A	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	33	33	32	30	0	0	0	76
normalized size	1	1.	0.97	0.91	0.	0.	0.	2.3
time (sec)	N/A	0.056	0.019	0.053	0.	0.	0.	1.165

Problem 130	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.075	3.237	0.085	0.	0.	0.	0.

Problem 131	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	371	371	328	1208	0	0	0	0
normalized size	1	1.	0.88	3.26	0.	0.	0.	0.
time (sec)	N/A	1.019	6.403	0.102	0.	0.	0.	0.

Problem 132	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	154	154	144	280	0	0	0	12438
normalized size	1	1.	0.94	1.82	0.	0.	0.	80.77
time (sec)	N/A	0.222	1.387	0.078	0.	0.	0.	1.886

Problem 133	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.138	31.069	0.088	0.	0.	0.	0.

Problem 134	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	B	F	F	F	F(-1)
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	370	370	433	1212	0	0	0	0
normalized size	1	1.	1.17	3.28	0.	0.	0.	0.
time (sec)	N/A	0.801	4.406	0.105	0.	0.	0.	0.

Problem 135	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	A	A	C	A	F	F	F	C
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD
size	153	153	153	282	0	0	0	12879
normalized size	1	1.	1.	1.84	0.	0.	0.	84.18
time (sec)	N/A	0.217	1.577	0.074	0.	0.	0.	1.94

Problem 136	Optimal	Rubi	Mathematica	Maple	Maxima	Fricas	Sympy	Giac
grade	N/A	A	A	A	A	A	A	A
verified	N/A	N/A	N/A	TBD	TBD	TBD	TBD	TBD
size	18	0	0	0	0	0	0	0
normalized size	1	0.	0.	0.	0.	0.	0.	0.
time (sec)	N/A	0.092	18.706	0.089	0.	0.	0.	0.

2.3 Detailed conclusion table specific for Rubi results

The following table is specific to Rubi. It gives additional statistics for each integral. the column **steps** is the number of steps used by Rubi to obtain the antiderivative. The **rules** column is the number of unique rules used. The **integrand size** column is the leaf size of the integrand. Finally the ratio $\frac{\text{number of rules}}{\text{integrand size}}$ is given. The larger this ratio is, the harder the integral was to solve. In this test, problem number [26] had the largest ratio of [1.583]

Table 2.1: Rubi specific breakdown of results for each integral

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1	A	5	4	1.	8	0.5
2	A	6	4	1.	8	0.5
3	A	5	4	1.	8	0.5
4	A	4	4	1.	6	0.667
5	A	1	1	1.	4	0.25
6	A	1	1	1.	8	0.125
7	A	4	4	1.	8	0.5
8	A	5	4	1.	8	0.5
9	A	0	0	0.	0	0.
10	A	19	11	1.	10	1.1
11	A	15	10	1.	10	1.
12	A	10	8	1.	8	1.
13	A	6	5	1.	6	0.833
14	A	0	0	0.	0	0.
15	A	0	0	0.	0	0.
16	A	0	0	0.	0	0.
17	A	0	0	0.	0	0.
18	A	14	6	1.	10	0.6
19	A	10	6	1.	10	0.6
20	A	7	6	1.	8	0.75
21	A	1	1	1.	6	0.167
22	A	0	0	0.	0	0.
23	A	7	5	1.	10	0.5
24	A	11	6	1.	10	0.6
25	A	0	0	0.	0	0.
26	A	39	19	1.	12	1.583
27	A	17	14	1.	10	1.4
28	A	5	5	1.	8	0.625
29	A	0	0	0.	0	0.
30	A	0	0	0.	0	0.
31	A	0	0	0.	0	0.
32	A	7	5	1.	17	0.294
33	A	7	5	1.	15	0.333
34	A	7	5	1.	13	0.385
35	A	3	1	1.	17	0.059
36	A	7	5	1.	17	0.294
37	A	7	5	1.	17	0.294
38	A	7	5	1.	19	0.263
39	A	14	10	1.	12	0.833
40	A	0	0	0.	0	0.
41	A	1	1	1.	12	0.083
42	A	5	4	1.	9	0.444
43	A	9	7	1.	10	0.7

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
44	A	14	9	1.	12	0.75
45	A	18	10	1.	12	0.833
46	A	0	0	0.	0	0.
47	A	7	6	1.	12	0.5
48	A	0	0	0.	0	0.
49	A	5	4	1.	9	0.444
50	A	9	7	1.	10	0.7
51	A	13	9	1.	12	0.75
52	A	20	11	1.	12	0.917
53	A	6	4	1.	9	0.444
54	A	6	4	1.	9	0.444
55	A	21	16	1.	16	1.
56	A	11	9	1.	14	0.643
57	A	4	4	1.	13	0.308
58	A	0	0	0.	0	0.
59	A	21	14	1.	16	0.875
60	A	12	10	1.	14	0.714
61	A	4	3	1.	13	0.231
62	A	0	0	0.	0	0.
63	A	24	10	1.	14	0.714
64	A	9	5	1.	13	0.385
65	A	0	0	0.	0	0.
66	A	24	9	1.	14	0.643
67	A	9	5	1.	13	0.385
68	A	0	0	0.	0	0.
69	A	5	4	1.	8	0.5
70	A	6	4	1.	8	0.5
71	A	5	4	1.	8	0.5
72	A	4	4	1.	6	0.667
73	A	1	1	1.	4	0.25
74	A	1	1	1.	8	0.125
75	A	4	4	1.	8	0.5
76	A	5	4	1.	8	0.5
77	A	0	0	0.	0	0.
78	A	19	11	1.	10	1.1
79	A	15	10	1.	10	1.
80	A	10	8	1.	8	1.
81	A	6	5	1.	6	0.833
82	A	0	0	0.	0	0.
83	A	0	0	0.	0	0.
84	A	0	0	0.	0	0.
85	A	0	0	0.	0	0.
86	A	14	6	1.	10	0.6
87	A	10	6	1.	10	0.6

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
88	A	7	6	1.	8	0.75
89	A	1	1	1.	6	0.167
90	A	0	0	0.	0	0.
91	A	7	5	1.	10	0.5
92	A	11	6	1.	10	0.6
93	A	0	0	0.	0	0.
94	A	39	19	1.	12	1.583
95	A	17	14	1.	10	1.4
96	A	5	5	1.	8	0.625
97	A	0	0	0.	0	0.
98	A	0	0	0.	0	0.
99	A	0	0	0.	0	0.
100	A	7	5	1.	17	0.294
101	A	7	5	1.	15	0.333
102	A	7	5	1.	13	0.385
103	A	3	1	1.	17	0.059
104	A	7	5	1.	17	0.294
105	A	7	5	1.	17	0.294
106	A	7	5	1.	19	0.263
107	A	0	0	0.	0	0.
108	A	7	6	1.	12	0.5
109	A	0	0	0.	0	0.
110	A	5	4	1.	9	0.444
111	A	9	7	1.	10	0.7
112	A	13	9	1.	12	0.75
113	A	20	11	1.	12	0.917
114	A	14	10	1.	12	0.833
115	A	0	0	0.	0	0.
116	A	1	1	1.	12	0.083
117	A	5	4	1.	9	0.444
118	A	9	7	1.	10	0.7
119	A	14	9	1.	12	0.75
120	A	18	10	1.	12	0.833
121	A	6	4	1.	9	0.444
122	A	6	4	1.	9	0.444
123	A	21	14	1.	16	0.875
124	A	12	10	1.	14	0.714
125	A	4	3	1.	13	0.231
126	A	0	0	0.	0	0.
127	A	21	16	1.	16	1.
128	A	11	9	1.	14	0.643
129	A	4	4	1.	13	0.308
130	A	0	0	0.	0	0.
131	A	24	9	1.	14	0.643

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Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
132	A	9	5	1.	13	0.385
133	A	0	0	0.	0	0.
134	A	24	10	1.	14	0.714
135	A	9	5	1.	13	0.385
136	A	0	0	0.	0	0.

Chapter 3

Listing of integrals

3.1 $\int x^m \text{Si}(bx) dx$

Optimal. Leaf size=86

$$\frac{x^m(-ibx)^{-m}\Gamma(m+1,-ibx)}{2b(m+1)} + \frac{x^m(ibx)^{-m}\Gamma(m+1,ibx)}{2b(m+1)} + \frac{x^{m+1}\text{Si}(bx)}{m+1}$$

[Out] $(x^m \Gamma[1+m, (-I)*b*x]) / (2*b*(1+m)*((-I)*b*x)^m + (x^m \Gamma[1+m, I*b*x]) / (2*b*(1+m)*(I*b*x)^m) + (x^{(1+m)} \text{SinIntegral}[b*x]) / (1+m)$

Rubi [A] time = 0.073956, antiderivative size = 86, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {6503, 12, 3308, 2181}

$$\frac{x^m(-ibx)^{-m}\Gamma(m+1,-ibx)}{2b(m+1)} + \frac{x^m(ibx)^{-m}\Gamma(m+1,ibx)}{2b(m+1)} + \frac{x^{m+1}\text{Si}(bx)}{m+1}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^m \text{SinIntegral}[b*x], x]$

[Out] $(x^m \Gamma[1+m, (-I)*b*x]) / (2*b*(1+m)*((-I)*b*x)^m + (x^m \Gamma[1+m, I*b*x]) / (2*b*(1+m)*(I*b*x)^m) + (x^{(1+m)} \text{SinIntegral}[b*x]) / (1+m)$

Rule 6503

$\text{Int}[(c + d*x)^m \text{SinIntegral}[a + b*x], x_Symbol] :> \text{Simp}[(c + d*x)^{m+1} \text{SinIntegral}[a + b*x] / (d*(m+1)), x] - \text{Dist}[b / (d*(m+1)), \text{Int}[(c + d*x)^{m+1} \text{Sin}[a + b*x] / (a + b*x), x], x] /;$ FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]

Rule 12

$\text{Int}[(a)*u, x_Symbol] :> \text{Dist}[a, \text{Int}[u, x], x] /;$ FreeQ[a, x] && !MatchQ[u, (b)*(v)] /; FreeQ[b, x]

Rule 3308

$\text{Int}[(c + d*x)^m \sin[(e + f*x)], x_Symbol] :> \text{Dist}[I/2, \text{Int}[(c + d*x)^m / E^{I*(e + f*x)}, x], x] - \text{Dist}[I/2, \text{Int}[(c + d*x)^m * E^{I*(e + f*x)}, x], x] /;$ FreeQ[{c, d, e, f, m}, x]

Rule 2181

```
Int[(F_)^((g_)*(e_) + (f_)*(x_))*((c_) + (d_)*(x_))^(m_), x_Symbol]
:> -Simp[(F^(g*(e - (c*f)/d))*(c + d*x)^FracPart[m]*Gamma[m + 1, (-((f*g*Log[F])/d))*(c + d*x])]/(d*(-((f*g*Log[F])/d))^(IntPart[m] + 1)*(-((f*g*Log[F])*(c + d*x))/d))^FracPart[m]), x] /; FreeQ[{F, c, d, e, f, g, m}, x] && !IntegerQ[m]
```

Rubi steps

$$\begin{aligned} \int x^m \text{Si}(bx) dx &= \frac{x^{1+m} \text{Si}(bx)}{1+m} - \frac{b \int \frac{x^m \sin(bx)}{b} dx}{1+m} \\ &= \frac{x^{1+m} \text{Si}(bx)}{1+m} - \frac{\int x^m \sin(bx) dx}{1+m} \\ &= \frac{x^{1+m} \text{Si}(bx)}{1+m} - \frac{i \int e^{-ibx} x^m dx}{2(1+m)} + \frac{i \int e^{ibx} x^m dx}{2(1+m)} \\ &= \frac{x^m (-ibx)^{-m} \Gamma(1+m, -ibx)}{2b(1+m)} + \frac{x^m (ibx)^{-m} \Gamma(1+m, ibx)}{2b(1+m)} + \frac{x^{1+m} \text{Si}(bx)}{1+m} \end{aligned}$$

Mathematica [A] time = 0.0539509, size = 82, normalized size = 0.95

$$\frac{x^m (b^2 x^2)^{-m} \left((-ibx)^m \Gamma(m+1, ibx) + (ibx)^m \Gamma(m+1, -ibx) + 2bx (b^2 x^2)^m \text{Si}(bx) \right)}{2b(m+1)}$$

Antiderivative was successfully verified.

[In] Integrate[x^m*SinIntegral[b*x],x]

[Out] (x^m*((I*b*x)^m*Gamma[1+m, (-I)*b*x] + ((-I)*b*x)^m*Gamma[1+m, I*b*x] + 2*b*x*(b^2*x^2)^m*SinIntegral[b*x]))/(2*b*(1+m)*(b^2*x^2)^m)

Maple [C] time = 0.171, size = 37, normalized size = 0.4

$$\frac{bx^{2+m}}{2+m} {}_2F_3\left(\frac{1}{2}, 1 + \frac{m}{2}; \frac{3}{2}, \frac{3}{2}, 2 + \frac{m}{2}; -\frac{b^2 x^2}{4}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*Si(b*x),x)

[Out] b/(2+m)*x^(2+m)*hypergeom([1/2, 1+1/2*m], [3/2, 3/2, 2+1/2*m], -1/4*b^2*x^2)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^m \text{Si}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Si(b*x),x, algorithm="maxima")

[Out] integrate(x^m*Si(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^m \text{Si}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Si(b*x),x, algorithm="fricas")

[Out] integral(x^m*sin_integral(b*x), x)

Sympy [A] time = 0.957741, size = 46, normalized size = 0.53

$$\frac{bx^2 x^m \Gamma\left(\frac{m}{2} + 1\right) {}_2F_3\left(\frac{1}{2}, \frac{m}{2} + 1 \mid -\frac{b^2 x^2}{4}\right)}{2\Gamma\left(\frac{m}{2} + 2\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m*Si(b*x),x)

[Out] b*x**2*x**m*gamma(m/2 + 1)*hyper((1/2, m/2 + 1), (3/2, 3/2, m/2 + 2), -b**2*x**2/4)/(2*gamma(m/2 + 2))

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int x^m \text{Si}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Si(b*x),x, algorithm="giac")

[Out] integrate(x^m*Si(b*x), x)

3.2 $\int x^3 \text{Si}(bx) dx$

Optimal. Leaf size=63

$$-\frac{3x^2 \sin(bx)}{4b^2} + \frac{3 \sin(bx)}{2b^4} - \frac{3x \cos(bx)}{2b^3} + \frac{1}{4}x^4 \text{Si}(bx) + \frac{x^3 \cos(bx)}{4b}$$

[Out] $(-3*x*\text{Cos}[b*x])/(2*b^3) + (x^3*\text{Cos}[b*x])/(4*b) + (3*\text{Sin}[b*x])/(2*b^4) - (3*x^2*\text{Sin}[b*x])/(4*b^2) + (x^4*\text{SinIntegral}[b*x])/4$

Rubi [A] time = 0.0684778, antiderivative size = 63, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {6503, 12, 3296, 2637}

$$-\frac{3x^2 \sin(bx)}{4b^2} + \frac{3 \sin(bx)}{2b^4} - \frac{3x \cos(bx)}{2b^3} + \frac{1}{4}x^4 \text{Si}(bx) + \frac{x^3 \cos(bx)}{4b}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^3*\text{SinIntegral}[b*x], x]$

[Out] $(-3*x*\text{Cos}[b*x])/(2*b^3) + (x^3*\text{Cos}[b*x])/(4*b) + (3*\text{Sin}[b*x])/(2*b^4) - (3*x^2*\text{Sin}[b*x])/(4*b^2) + (x^4*\text{SinIntegral}[b*x])/4$

Rule 6503

$\text{Int}[\{(c_.) + (d_.)*(x_)\}^{(m_.)}*\text{SinIntegral}[(a_.) + (b_.)*(x_)], x_Symbol] :$
 $> \text{Simp}[\{(c + d*x)^{(m + 1)}*\text{SinIntegral}[a + b*x]\}/(d*(m + 1)), x] - \text{Dist}[b/(d*(m + 1)), \text{Int}[\{(c + d*x)^{(m + 1)}*\text{Sin}[a + b*x]\}/(a + b*x), x], x] /;$ FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]

Rule 12

$\text{Int}[(a_)*(u_), x_Symbol] := \text{Dist}[a, \text{Int}[u, x], x] /;$ FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 3296

$\text{Int}[\{(c_.) + (d_.)*(x_)\}^{(m_.)}*\sin[(e_.) + (f_.)*(x_)], x_Symbol] := -\text{Simp}[\{(c + d*x)^m*\text{Cos}[e + f*x]\}/f, x] + \text{Dist}[(d*m)/f, \text{Int}[\{(c + d*x)^{(m - 1)}*\text{Cos}[e + f*x], x], x] /;$ FreeQ[{c, d, e, f}, x] && GtQ[m, 0]

Rule 2637

$\text{Int}[\sin[\text{Pi}/2 + (c_.) + (d_.)*(x_)], x_Symbol] := \text{Simp}[\text{Sin}[c + d*x]/d, x] /;$ FreeQ[{c, d}, x]

Rubi steps

$$\begin{aligned}
\int x^3 \text{Si}(bx) dx &= \frac{1}{4} x^4 \text{Si}(bx) - \frac{1}{4} b \int \frac{x^3 \sin(bx)}{b} dx \\
&= \frac{1}{4} x^4 \text{Si}(bx) - \frac{1}{4} \int x^3 \sin(bx) dx \\
&= \frac{x^3 \cos(bx)}{4b} + \frac{1}{4} x^4 \text{Si}(bx) - \frac{3 \int x^2 \cos(bx) dx}{4b} \\
&= \frac{x^3 \cos(bx)}{4b} - \frac{3x^2 \sin(bx)}{4b^2} + \frac{1}{4} x^4 \text{Si}(bx) + \frac{3 \int x \sin(bx) dx}{2b^2} \\
&= -\frac{3x \cos(bx)}{2b^3} + \frac{x^3 \cos(bx)}{4b} - \frac{3x^2 \sin(bx)}{4b^2} + \frac{1}{4} x^4 \text{Si}(bx) + \frac{3 \int \cos(bx) dx}{2b^3} \\
&= -\frac{3x \cos(bx)}{2b^3} + \frac{x^3 \cos(bx)}{4b} + \frac{3 \sin(bx)}{2b^4} - \frac{3x^2 \sin(bx)}{4b^2} + \frac{1}{4} x^4 \text{Si}(bx)
\end{aligned}$$

Mathematica [A] time = 0.0364487, size = 50, normalized size = 0.79

$$\frac{b^4 x^4 \text{Si}(bx) - 3(b^2 x^2 - 2) \sin(bx) + bx(b^2 x^2 - 6) \cos(bx)}{4b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*SinIntegral[b*x],x]

[Out] (b*x*(-6 + b^2*x^2)*Cos[b*x] - 3*(-2 + b^2*x^2)*Sin[b*x] + b^4*x^4*SinIntegral[b*x])/(4*b^4)

Maple [A] time = 0.056, size = 56, normalized size = 0.9

$$\frac{1}{b^4} \left(\frac{b^4 x^4 \text{Si}(bx)}{4} + \frac{b^3 x^3 \cos(bx)}{4} - \frac{3 b^2 x^2 \sin(bx)}{4} + \frac{3 \sin(bx)}{2} - \frac{3 b x \cos(bx)}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*Si(b*x),x)

[Out] 1/b^4*(1/4*b^4*x^4*Si(b*x)+1/4*b^3*x^3*cos(b*x)-3/4*b^2*x^2*sin(b*x)+3/2*sin(b*x)-3/2*b*x*cos(b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \text{Si}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Si(b*x),x, algorithm="maxima")

[Out] integrate(x^3*Si(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^3 \text{Si}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Si(b*x),x, algorithm="fricas")

[Out] integral(x^3*sin_integral(b*x), x)

Sympy [A] time = 1.27236, size = 61, normalized size = 0.97

$$\frac{x^4 \text{Si}(bx)}{4} + \frac{x^3 \cos(bx)}{4b} - \frac{3x^2 \sin(bx)}{4b^2} - \frac{3x \cos(bx)}{2b^3} + \frac{3 \sin(bx)}{2b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*Si(b*x),x)

[Out] x**4*Si(b*x)/4 + x**3*cos(b*x)/(4*b) - 3*x**2*sin(b*x)/(4*b**2) - 3*x*cos(b*x)/(2*b**3) + 3*sin(b*x)/(2*b**4)

Giac [A] time = 1.29534, size = 66, normalized size = 1.05

$$\frac{1}{4} x^4 \text{Si}(bx) + \frac{(b^3 x^3 - 6bx) \cos(bx)}{4b^4} - \frac{3(b^2 x^2 - 2) \sin(bx)}{4b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Si(b*x),x, algorithm="giac")

[Out] 1/4*x^4*sin_integral(b*x) + 1/4*(b^3*x^3 - 6*b*x)*cos(b*x)/b^4 - 3/4*(b^2*x^2 - 2)*sin(b*x)/b^4

3.3 $\int x^2 \mathbf{Si}(bx) dx$

Optimal. Leaf size=49

$$-\frac{2x \sin(bx)}{3b^2} - \frac{2 \cos(bx)}{3b^3} + \frac{1}{3}x^3 \mathbf{Si}(bx) + \frac{x^2 \cos(bx)}{3b}$$

[Out] $(-2*\text{Cos}[b*x])/(3*b^3) + (x^2*\text{Cos}[b*x])/(3*b) - (2*x*\text{Sin}[b*x])/(3*b^2) + (x^3*\text{SinIntegral}[b*x])/3$

Rubi [A] time = 0.0461829, antiderivative size = 49, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {6503, 12, 3296, 2638}

$$-\frac{2x \sin(bx)}{3b^2} - \frac{2 \cos(bx)}{3b^3} + \frac{1}{3}x^3 \mathbf{Si}(bx) + \frac{x^2 \cos(bx)}{3b}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2*\text{SinIntegral}[b*x], x]$

[Out] $(-2*\text{Cos}[b*x])/(3*b^3) + (x^2*\text{Cos}[b*x])/(3*b) - (2*x*\text{Sin}[b*x])/(3*b^2) + (x^3*\text{SinIntegral}[b*x])/3$

Rule 6503

$\text{Int}[(c + d*x)^m * \text{SinIntegral}[a + b*x], x_Symbol] :> \text{Simp}[(c + d*x)^{m+1} * \text{SinIntegral}[a + b*x] / (d*(m+1)), x] - \text{Dist}[b/(d*(m+1)), \text{Int}[(c + d*x)^{m+1} * \text{Sin}[a + b*x] / (a + b*x), x], x] /;$ FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]

Rule 12

$\text{Int}[a*(u), x_Symbol] :> \text{Dist}[a, \text{Int}[u, x], x] /;$ FreeQ[a, x] && !MatchQ[u, (b)*(v)] /;

 FreeQ[b, x]

Rule 3296

$\text{Int}[(c + d*x)^m * \sin[e + f*x], x_Symbol] :> -\text{Simp}[(c + d*x)^m * \text{Cos}[e + f*x] / f, x] + \text{Dist}[(d*m)/f, \text{Int}[(c + d*x)^{m-1} * \text{Cos}[e + f*x], x], x] /;$ FreeQ[{c, d, e, f}, x] && GtQ[m, 0]

Rule 2638

$\text{Int}[\sin[c + d*x], x_Symbol] :> -\text{Simp}[\text{Cos}[c + d*x] / d, x] /;$ FreeQ[{c, d}, x]

Rubi steps

$$\begin{aligned}
\int x^2 \text{Si}(bx) dx &= \frac{1}{3} x^3 \text{Si}(bx) - \frac{1}{3} b \int \frac{x^2 \sin(bx)}{b} dx \\
&= \frac{1}{3} x^3 \text{Si}(bx) - \frac{1}{3} \int x^2 \sin(bx) dx \\
&= \frac{x^2 \cos(bx)}{3b} + \frac{1}{3} x^3 \text{Si}(bx) - \frac{2 \int x \cos(bx) dx}{3b} \\
&= \frac{x^2 \cos(bx)}{3b} - \frac{2x \sin(bx)}{3b^2} + \frac{1}{3} x^3 \text{Si}(bx) + \frac{2 \int \sin(bx) dx}{3b^2} \\
&= -\frac{2 \cos(bx)}{3b^3} + \frac{x^2 \cos(bx)}{3b} - \frac{2x \sin(bx)}{3b^2} + \frac{1}{3} x^3 \text{Si}(bx)
\end{aligned}$$

Mathematica [A] time = 0.0271712, size = 41, normalized size = 0.84

$$\frac{b^3 x^3 \text{Si}(bx) + (b^2 x^2 - 2) \cos(bx) - 2bx \sin(bx)}{3b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*SinIntegral[b*x],x]

[Out] ((-2 + b^2*x^2)*Cos[b*x] - 2*b*x*Sin[b*x] + b^3*x^3*SinIntegral[b*x])/(3*b^3)

Maple [A] time = 0.054, size = 44, normalized size = 0.9

$$\frac{1}{b^3} \left(\frac{b^3 x^3 \text{Si}(bx)}{3} + \frac{b^2 x^2 \cos(bx)}{3} - \frac{2 \cos(bx)}{3} - \frac{2 \sin(bx) bx}{3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*Si(b*x),x)

[Out] 1/b^3*(1/3*b^3*x^3*Si(b*x)+1/3*b^2*x^2*cos(b*x)-2/3*cos(b*x)-2/3*sin(b*x)*b*x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Si}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Si(b*x),x, algorithm="maxima")

[Out] integrate(x^2*Si(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^2 \text{Si}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Si(b*x),x, algorithm="fricas")

[Out] integral(x^2*sin_integral(b*x), x)

Sympy [A] time = 1.47372, size = 46, normalized size = 0.94

$$\frac{x^3 \operatorname{Si}(bx)}{3} + \frac{x^2 \cos(bx)}{3b} - \frac{2x \sin(bx)}{3b^2} - \frac{2 \cos(bx)}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*Si(b*x),x)

[Out] x**3*Si(b*x)/3 + x**2*cos(b*x)/(3*b) - 2*x*sin(b*x)/(3*b**2) - 2*cos(b*x)/(3*b**3)

Giac [A] time = 1.28744, size = 51, normalized size = 1.04

$$\frac{1}{3} x^3 \operatorname{Si}(bx) - \frac{2x \sin(bx)}{3b^2} + \frac{(b^2 x^2 - 2) \cos(bx)}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Si(b*x),x, algorithm="giac")

[Out] 1/3*x^3*sin_integral(b*x) - 2/3*x*sin(b*x)/b^2 + 1/3*(b^2*x^2 - 2)*cos(b*x)/b^3

3.4 $\int x\text{Si}(bx) dx$

Optimal. Leaf size=35

$$-\frac{\sin(bx)}{2b^2} + \frac{1}{2}x^2\text{Si}(bx) + \frac{x \cos(bx)}{2b}$$

[Out] (x*Cos[b*x])/(2*b) - Sin[b*x]/(2*b^2) + (x^2*SinIntegral[b*x])/2

Rubi [A] time = 0.0227732, antiderivative size = 35, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.667$, Rules used = {6503, 12, 3296, 2637}

$$-\frac{\sin(bx)}{2b^2} + \frac{1}{2}x^2\text{Si}(bx) + \frac{x \cos(bx)}{2b}$$

Antiderivative was successfully verified.

[In] Int[x*SinIntegral[b*x], x]

[Out] (x*Cos[b*x])/(2*b) - Sin[b*x]/(2*b^2) + (x^2*SinIntegral[b*x])/2

Rule 6503

Int[((c_.) + (d_.)*(x_))^(m_.)*SinIntegral[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[((c + d*x)^(m + 1)*SinIntegral[a + b*x])/(d*(m + 1)), x] - Dist[b/(d*(m + 1)), Int[((c + d*x)^(m + 1)*Sin[a + b*x])/(a + b*x), x], x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 3296

Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)], x_Symbol] :> -Simp[((c + d*x)^m*Cos[e + f*x])/f, x] + Dist[(d*m)/f, Int[(c + d*x)^(m - 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && GtQ[m, 0]

Rule 2637

Int[sin[Pi/2 + (c_.) + (d_.)*(x_)], x_Symbol] :> Simp[Sin[c + d*x]/d, x] /; FreeQ[{c, d}, x]

Rubi steps

$$\begin{aligned} \int x\text{Si}(bx) dx &= \frac{1}{2}x^2\text{Si}(bx) - \frac{1}{2}b \int \frac{x \sin(bx)}{b} dx \\ &= \frac{1}{2}x^2\text{Si}(bx) - \frac{1}{2} \int x \sin(bx) dx \\ &= \frac{x \cos(bx)}{2b} + \frac{1}{2}x^2\text{Si}(bx) - \frac{\int \cos(bx) dx}{2b} \\ &= \frac{x \cos(bx)}{2b} - \frac{\sin(bx)}{2b^2} + \frac{1}{2}x^2\text{Si}(bx) \end{aligned}$$

Mathematica [A] time = 0.0063835, size = 35, normalized size = 1.

$$-\frac{\sin(bx)}{2b^2} + \frac{1}{2}x^2\text{Si}(bx) + \frac{x \cos(bx)}{2b}$$

Antiderivative was successfully verified.

[In] Integrate[x*SinIntegral[b*x],x]

[Out] (x*Cos[b*x])/(2*b) - Sin[b*x]/(2*b^2) + (x^2*SinIntegral[b*x])/2

Maple [A] time = 0.05, size = 32, normalized size = 0.9

$$\frac{1}{b^2} \left(\frac{b^2 x^2 \text{Si}(bx)}{2} + \frac{bx \cos(bx)}{2} - \frac{\sin(bx)}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*Si(b*x),x)

[Out] 1/b^2*(1/2*b^2*x^2*Si(b*x)+1/2*b*x*cos(b*x)-1/2*sin(b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \text{Si}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(b*x),x, algorithm="maxima")

[Out] integrate(x*Si(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x \text{Si}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(b*x),x, algorithm="fricas")

[Out] integral(x*sin_integral(b*x), x)

Sympy [A] time = 0.743066, size = 29, normalized size = 0.83

$$\frac{x^2 \text{Si}(bx)}{2} + \frac{x \cos(bx)}{2b} - \frac{\sin(bx)}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*Si(b*x),x)
```

```
[Out] x**2*Si(b*x)/2 + x*cos(b*x)/(2*b) - sin(b*x)/(2*b**2)
```

Giac [A] time = 1.30504, size = 39, normalized size = 1.11

$$\frac{1}{2}x^2 \operatorname{Si}(bx) + \frac{x \cos(bx)}{2b} - \frac{\sin(bx)}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*Si(b*x),x, algorithm="giac")
```

```
[Out] 1/2*x^2*sin_integral(b*x) + 1/2*x*cos(b*x)/b - 1/2*sin(b*x)/b^2
```

3.5 $\int \text{Si}(bx) dx$

Optimal. Leaf size=15

$$x\text{Si}(bx) + \frac{\cos(bx)}{b}$$

[Out] Cos[b*x]/b + x*SinIntegral[b*x]

Rubi [A] time = 0.0038514, antiderivative size = 15, normalized size of antiderivative = 1., number of steps used = 1, number of rules used = 1, integrand size = 4, $\frac{\text{number of rules}}{\text{integrand size}} = 0.25$, Rules used = {6499}

$$x\text{Si}(bx) + \frac{\cos(bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[SinIntegral[b*x],x]

[Out] Cos[b*x]/b + x*SinIntegral[b*x]

Rule 6499

Int[SinIntegral[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[((a + b*x)*SinIntegral[a + b*x])/b, x] + Simp[Cos[a + b*x]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\int \text{Si}(bx) dx = \frac{\cos(bx)}{b} + x\text{Si}(bx)$$

Mathematica [A] time = 0.0014557, size = 15, normalized size = 1.

$$x\text{Si}(bx) + \frac{\cos(bx)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[SinIntegral[b*x],x]

[Out] Cos[b*x]/b + x*SinIntegral[b*x]

Maple [A] time = 0.05, size = 17, normalized size = 1.1

$$\frac{bx\text{Si}(bx) + \cos(bx)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x),x)

[Out] $1/b*(b*x*Si(b*x)+cos(b*x))$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int Si(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x),x, algorithm="maxima")`

[Out] `integrate(Si(b*x), x)`

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(Si(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x),x, algorithm="fricas")`

[Out] `integral(sin_integral(b*x), x)`

Sympy [A] time = 0.802061, size = 12, normalized size = 0.8

$$x Si(bx) + \frac{\cos(bx)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x),x)`

[Out] `x*Si(b*x) + cos(b*x)/b`

Giac [A] time = 1.25101, size = 20, normalized size = 1.33

$$x Si(bx) + \frac{\cos(bx)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x),x, algorithm="giac")`

[Out] `x*sin_integral(b*x) + cos(b*x)/b`

3.6 $\int \frac{\text{Si}(bx)}{x} dx$

Optimal. Leaf size=43

$$\frac{1}{2}bx\text{HypergeometricPFQ}(\{1,1,1\},\{2,2,2\},-ibx) + \frac{1}{2}bx\text{HypergeometricPFQ}(\{1,1,1\},\{2,2,2\},ibx)$$

[Out] (b*x*HypergeometricPFQ[{1, 1, 1}, {2, 2, 2}, (-I)*b*x])/2 + (b*x*HypergeometricPFQ[{1, 1, 1}, {2, 2, 2}, I*b*x])/2

Rubi [A] time = 0.0200348, antiderivative size = 43, normalized size of antiderivative = 1., number of steps used = 1, number of rules used = 1, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {6501}

$$\frac{1}{2}bx {}_3F_3(1,1,1;2,2,2;-ibx) + \frac{1}{2}bx {}_3F_3(1,1,1;2,2,2;ibx)$$

Antiderivative was successfully verified.

[In] Int[SinIntegral[b*x]/x,x]

[Out] (b*x*HypergeometricPFQ[{1, 1, 1}, {2, 2, 2}, (-I)*b*x])/2 + (b*x*HypergeometricPFQ[{1, 1, 1}, {2, 2, 2}, I*b*x])/2

Rule 6501

Int[SinIntegral[(b_.)*(x_)]/(x_), x_Symbol] :> Simp[(1*b*x*HypergeometricPFQ[{1, 1, 1}, {2, 2, 2}, -(I*b*x)])/2, x] + Simp[(1*b*x*HypergeometricPFQ[{1, 1, 1}, {2, 2, 2}, I*b*x])/2, x] /; FreeQ[b, x]

Rubi steps

$$\int \frac{\text{Si}(bx)}{x} dx = \frac{1}{2}bx {}_3F_3(1,1,1;2,2,2;-ibx) + \frac{1}{2}bx {}_3F_3(1,1,1;2,2,2;ibx)$$

Mathematica [A] time = 0.0042725, size = 43, normalized size = 1.

$$\frac{1}{2}bx\text{HypergeometricPFQ}(\{1,1,1\},\{2,2,2\},-ibx) + \frac{1}{2}bx\text{HypergeometricPFQ}(\{1,1,1\},\{2,2,2\},ibx)$$

Antiderivative was successfully verified.

[In] Integrate[SinIntegral[b*x]/x,x]

[Out] (b*x*HypergeometricPFQ[{1, 1, 1}, {2, 2, 2}, (-I)*b*x])/2 + (b*x*HypergeometricPFQ[{1, 1, 1}, {2, 2, 2}, I*b*x])/2

Maple [A] time = 0.069, size = 20, normalized size = 0.5

$$bx {}_2F_3\left(\frac{1}{2}, \frac{1}{2}; \frac{3}{2}, \frac{3}{2}, \frac{3}{2}; -\frac{b^2x^2}{4}\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(Si(b*x)/x,x)`

[Out] `b*x*hypergeom([1/2,1/2],[3/2,3/2,3/2],-1/4*b^2*x^2)`

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x)/x,x, algorithm="maxima")`

[Out] `integrate(Si(b*x)/x, x)`

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Si}(bx)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x)/x,x, algorithm="fricas")`

[Out] `integral(sin_integral(b*x)/x, x)`

Sympy [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: AttributeError

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x)/x,x)`

[Out] Exception raised: AttributeError

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x)/x,x, algorithm="giac")`

[Out] `integrate(Si(b*x)/x, x)`

3.7 $\int \frac{\text{Si}(bx)}{x^2} dx$

Optimal. Leaf size=25

$$b\text{CosIntegral}(bx) - \frac{\text{Si}(bx)}{x} - \frac{\sin(bx)}{x}$$

[Out] b*CosIntegral[b*x] - Sin[b*x]/x - SinIntegral[b*x]/x

Rubi [A] time = 0.0452787, antiderivative size = 25, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {6503, 12, 3297, 3302}

$$b\text{CosIntegral}(bx) - \frac{\text{Si}(bx)}{x} - \frac{\sin(bx)}{x}$$

Antiderivative was successfully verified.

[In] Int[SinIntegral[b*x]/x^2,x]

[Out] b*CosIntegral[b*x] - Sin[b*x]/x - SinIntegral[b*x]/x

Rule 6503

Int[((c_.) + (d_.)*(x_))^(m_.)*SinIntegral[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[((c + d*x)^(m + 1)*SinIntegral[a + b*x])/(d*(m + 1)), x] - Dist[b/(d*(m + 1)), Int[((c + d*x)^(m + 1)*Sin[a + b*x])/(a + b*x), x], x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 3297

Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)], x_Symbol] :> Simp[((c + d*x)^(m + 1)*Sin[e + f*x])/(d*(m + 1)), x] - Dist[f/(d*(m + 1)), Int[(c + d*x)^(m + 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && LtQ[m, -1]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned}
\int \frac{\text{Si}(bx)}{x^2} dx &= -\frac{\text{Si}(bx)}{x} + b \int \frac{\sin(bx)}{bx^2} dx \\
&= -\frac{\text{Si}(bx)}{x} + \int \frac{\sin(bx)}{x^2} dx \\
&= -\frac{\sin(bx)}{x} - \frac{\text{Si}(bx)}{x} + b \int \frac{\cos(bx)}{x} dx \\
&= b\text{Ci}(bx) - \frac{\sin(bx)}{x} - \frac{\text{Si}(bx)}{x}
\end{aligned}$$

Mathematica [A] time = 0.009746, size = 25, normalized size = 1.

$$b\text{CosIntegral}(bx) - \frac{\text{Si}(bx)}{x} - \frac{\sin(bx)}{x}$$

Antiderivative was successfully verified.

[In] Integrate[SinIntegral[b*x]/x^2,x]

[Out] b*CosIntegral[b*x] - Sin[b*x]/x - SinIntegral[b*x]/x

Maple [A] time = 0.054, size = 32, normalized size = 1.3

$$b \left(-\frac{\text{Si}(bx)}{bx} - \frac{\sin(bx)}{bx} + \text{Ci}(bx) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x)/x^2,x)

[Out] b*(-Si(b*x)/b/x-sin(b*x)/b/x+Ci(b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)/x^2,x, algorithm="maxima")

[Out] integrate(Si(b*x)/x^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Si}(bx)}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)/x^2,x, algorithm="fricas")

[Out] integral(sin_integral(b*x)/x^2, x)

Sympy [A] time = 1.16882, size = 36, normalized size = 1.44

$$-\frac{b^3 x^2 {}_3F_4\left(1, 1, \frac{3}{2} \middle| \frac{b^2 x^2}{4}\right)}{36} + \frac{b \log(b^2 x^2)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)/x**2,x)

[Out] -b**3*x**2*hyper((1, 1, 3/2), (2, 2, 5/2, 5/2), -b**2*x**2/4)/36 + b*log(b*x**2*x**2)/2

Giac [A] time = 1.20313, size = 50, normalized size = 2.

$$\frac{bx \operatorname{Ci}(bx) + bx \operatorname{Ci}(-bx) - 2 \sin(bx)}{2x} - \frac{\operatorname{Si}(bx)}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)/x^2,x, algorithm="giac")

[Out] 1/2*(b*x*cos_integral(b*x) + b*x*cos_integral(-b*x) - 2*sin(b*x))/x - sin_integral(b*x)/x

3.8 $\int \frac{\text{Si}(bx)}{x^3} dx$

Optimal. Leaf size=46

$$-\frac{1}{4}b^2\text{Si}(bx) - \frac{\text{Si}(bx)}{2x^2} - \frac{\sin(bx)}{4x^2} - \frac{b \cos(bx)}{4x}$$

[Out] $-(b*\text{Cos}[b*x])/(4*x) - \text{Sin}[b*x]/(4*x^2) - (b^2*\text{SinIntegral}[b*x])/4 - \text{SinIntegral}[b*x]/(2*x^2)$

Rubi [A] time = 0.0646036, antiderivative size = 46, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {6503, 12, 3297, 3299}

$$-\frac{1}{4}b^2\text{Si}(bx) - \frac{\text{Si}(bx)}{2x^2} - \frac{\sin(bx)}{4x^2} - \frac{b \cos(bx)}{4x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{SinIntegral}[b*x]/x^3, x]$

[Out] $-(b*\text{Cos}[b*x])/(4*x) - \text{Sin}[b*x]/(4*x^2) - (b^2*\text{SinIntegral}[b*x])/4 - \text{SinIntegral}[b*x]/(2*x^2)$

Rule 6503

```
Int[((c_.) + (d_.)*(x_))^(m_.)*SinIntegral[(a_.) + (b_.)*(x_)], x_Symbol] :
> Simp[((c + d*x)^(m + 1)*SinIntegral[a + b*x])/(d*(m + 1)), x] - Dist[b/(d
*(m + 1)), Int[((c + d*x)^(m + 1)*Sin[a + b*x])/(a + b*x), x], x] /; FreeQ[
{a, b, c, d, m}, x] && NeQ[m, -1]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !Match
Q[u, (b_)*(v_)] /; FreeQ[b, x]
```

Rule 3297

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)], x_Symbol] :> Simp[((
c + d*x)^(m + 1)*Sin[e + f*x])/(d*(m + 1)), x] - Dist[f/(d*(m + 1)), Int[(c
+ d*x)^(m + 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && LtQ[m, -1
]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{\text{Si}(bx)}{x^3} dx &= -\frac{\text{Si}(bx)}{2x^2} + \frac{1}{2}b \int \frac{\sin(bx)}{bx^3} dx \\
&= -\frac{\text{Si}(bx)}{2x^2} + \frac{1}{2} \int \frac{\sin(bx)}{x^3} dx \\
&= -\frac{\sin(bx)}{4x^2} - \frac{\text{Si}(bx)}{2x^2} + \frac{1}{4}b \int \frac{\cos(bx)}{x^2} dx \\
&= -\frac{b \cos(bx)}{4x} - \frac{\sin(bx)}{4x^2} - \frac{\text{Si}(bx)}{2x^2} - \frac{1}{4}b^2 \int \frac{\sin(bx)}{x} dx \\
&= -\frac{b \cos(bx)}{4x} - \frac{\sin(bx)}{4x^2} - \frac{1}{4}b^2 \text{Si}(bx) - \frac{\text{Si}(bx)}{2x^2}
\end{aligned}$$

Mathematica [A] time = 0.0130357, size = 46, normalized size = 1.

$$-\frac{1}{4}b^2 \text{Si}(bx) - \frac{\text{Si}(bx)}{2x^2} - \frac{\sin(bx)}{4x^2} - \frac{b \cos(bx)}{4x}$$

Antiderivative was successfully verified.

[In] Integrate[SinIntegral[b*x]/x^3,x]

[Out] -(b*Cos[b*x])/(4*x) - Sin[b*x]/(4*x^2) - (b^2*SinIntegral[b*x])/4 - SinIntegral[b*x]/(2*x^2)

Maple [A] time = 0.052, size = 48, normalized size = 1.

$$b^2 \left(-\frac{\text{Si}(bx)}{2b^2x^2} - \frac{\sin(bx)}{4b^2x^2} - \frac{\cos(bx)}{4bx} - \frac{\text{Si}(bx)}{4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x)/x^3,x)

[Out] b^2*(-1/2*Si(b*x)/b^2/x^2-1/4*sin(b*x)/b^2/x^2-1/4*cos(b*x)/b/x-1/4*Si(b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)/x^3,x, algorithm="maxima")

[Out] integrate(Si(b*x)/x^3, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Si}(bx)}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)/x^3,x, algorithm="fricas")

[Out] integral(sin_integral(b*x)/x^3, x)

Sympy [A] time = 0.891122, size = 41, normalized size = 0.89

$$-\frac{b^2 \operatorname{Si}(bx)}{4} - \frac{b \cos(bx)}{4x} - \frac{\sin(bx)}{4x^2} - \frac{\operatorname{Si}(bx)}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)/x**3,x)

[Out] -b**2*Si(b*x)/4 - b*cos(b*x)/(4*x) - sin(b*x)/(4*x**2) - Si(b*x)/(2*x**2)

Giac [C] time = 1.35264, size = 201, normalized size = 4.37

$$\frac{b^2 x^2 \Im(\operatorname{Ci}(bx)) \tan\left(\frac{1}{2} bx\right)^2 - b^2 x^2 \Im(\operatorname{Ci}(-bx)) \tan\left(\frac{1}{2} bx\right)^2 + 2 b^2 x^2 \operatorname{Si}(bx) \tan\left(\frac{1}{2} bx\right)^2 + b^2 x^2 \Im(\operatorname{Ci}(bx)) - b^2 x^2 \Im(\operatorname{Ci}(-bx))}{8 \left(x^2 \tan\left(\frac{1}{2} bx\right)^2 + x^2 \right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)/x^3,x, algorithm="giac")

[Out] -1/8*(b^2*x^2*imag_part(cos_integral(b*x))*tan(1/2*b*x)^2 - b^2*x^2*imag_part(cos_integral(-b*x))*tan(1/2*b*x)^2 + 2*b^2*x^2*sin_integral(b*x)*tan(1/2*b*x)^2 + b^2*x^2*imag_part(cos_integral(b*x)) - b^2*x^2*imag_part(cos_integral(-b*x)) + 2*b^2*x^2*sin_integral(b*x) - 2*b*x*tan(1/2*b*x)^2 + 2*b*x + 4*tan(1/2*b*x))/(x^2*tan(1/2*b*x)^2 + x^2) - 1/2*sin_integral(b*x)/x^2

3.9 $\int x^m \mathbf{Si}(bx)^2 dx$

Optimal. Leaf size=12

CannotIntegrate($x^m \mathbf{Si}(bx)^2, x$)

[Out] CannotIntegrate[x^m*SinIntegral[b*x]², x]

Rubi [A] time = 0.0310492, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int x^m \mathbf{Si}(bx)^2 dx$$

Verification is Not applicable to the result.

[In] Int[x^m*SinIntegral[b*x]², x]

[Out] Defer[Int][x^m*SinIntegral[b*x]², x]

Rubi steps

$$\int x^m \mathbf{Si}(bx)^2 dx = \int x^m \mathbf{Si}(bx)^2 dx$$

Mathematica [A] time = 2.51324, size = 0, normalized size = 0.

$$\int x^m \mathbf{Si}(bx)^2 dx$$

Verification is Not applicable to the result.

[In] Integrate[x^m*SinIntegral[b*x]², x]

[Out] Integrate[x^m*SinIntegral[b*x]², x]

Maple [A] time = 0.059, size = 0, normalized size = 0.

$$\int x^m (\mathbf{Si}(bx))^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*Si(b*x)², x)

[Out] int(x^m*Si(b*x)², x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \mathbf{Si}(bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Si(b*x)²,x, algorithm="maxima")

[Out] integrate(x^m*Si(b*x)², x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^m \text{Si}(bx)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Si(b*x)²,x, algorithm="fricas")

[Out] integral(x^m*sin_integral(b*x)², x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \text{Si}^2(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m*Si(b*x)**2,x)

[Out] Integral(x**m*Si(b*x)**2, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \text{Si}(bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Si(b*x)²,x, algorithm="giac")

[Out] integrate(x^m*Si(b*x)², x)

3.10 $\int x^3 \text{Si}(bx)^2 dx$

Optimal. Leaf size=149

$$\frac{3\text{CosIntegral}(2bx)}{2b^4} - \frac{3x^2\text{Si}(bx)\sin(bx)}{2b^2} + \frac{3\text{Si}(bx)\sin(bx)}{b^4} - \frac{3x\text{Si}(bx)\cos(bx)}{b^3} + \frac{x^2}{2b^2} - \frac{x^2\sin^2(bx)}{4b^2} - \frac{3\log(x)}{2b^4} + \frac{2\text{Si}(bx)^2}{b^4}$$

[Out] $x^2/(2*b^2) + (3*\text{CosIntegral}[2*b*x])/(2*b^4) - (3*\text{Log}[x])/(2*b^4) - (x*\text{Cos}[b*x]*\text{Sin}[b*x])/b^3 + (2*\text{Sin}[b*x]^2)/b^4 - (x^2*\text{Sin}[b*x]^2)/(4*b^2) - (3*x*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b^3 + (x^3*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/(2*b) + (3*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b^4 - (3*x^2*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/(2*b^2) + (x^4*\text{SinIntegral}[b*x]^2)/4$

Rubi [A] time = 0.215849, antiderivative size = 149, normalized size of antiderivative = 1., number of steps used = 19, number of rules used = 11, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 1.1$, Rules used = {6507, 6513, 12, 3443, 3310, 30, 6519, 2564, 6517, 3312, 3302}

$$\frac{3\text{CosIntegral}(2bx)}{2b^4} - \frac{3x^2\text{Si}(bx)\sin(bx)}{2b^2} + \frac{3\text{Si}(bx)\sin(bx)}{b^4} - \frac{3x\text{Si}(bx)\cos(bx)}{b^3} + \frac{x^2}{2b^2} - \frac{x^2\sin^2(bx)}{4b^2} - \frac{3\log(x)}{2b^4} + \frac{2\text{Si}(bx)^2}{b^4}$$

Antiderivative was successfully verified.

[In] Int[x^3*SinIntegral[b*x]^2,x]

[Out] $x^2/(2*b^2) + (3*\text{CosIntegral}[2*b*x])/(2*b^4) - (3*\text{Log}[x])/(2*b^4) - (x*\text{Cos}[b*x]*\text{Sin}[b*x])/b^3 + (2*\text{Sin}[b*x]^2)/b^4 - (x^2*\text{Sin}[b*x]^2)/(4*b^2) - (3*x*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b^3 + (x^3*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/(2*b) + (3*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b^4 - (3*x^2*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/(2*b^2) + (x^4*\text{SinIntegral}[b*x]^2)/4$

Rule 6507

Int[(x_)^(m_)*SinIntegral[(b_)*(x_)]^2, x_Symbol] :> Simp[(x^(m + 1)*SinIntegral[b*x]^2)/(m + 1), x] - Dist[2/(m + 1), Int[x^m*Sin[b*x]*SinIntegral[b*x], x], x] /; FreeQ[b, x] && IGtQ[m, 0]

Rule 6513

Int[((e_) + (f_)*(x_))^(m_)*Sin[(a_) + (b_)*(x_)]*SinIntegral[(c_) + (d_)*(x_)], x_Symbol] :> -Simp[((e + f*x)^m*Cos[a + b*x]*SinIntegral[c + d*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*Cos[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Cos[a + b*x]*SinIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 3443

Int[Cos[(a_) + (b_)*(x_)^(n_)]*(x_)^(m_)*Sin[(a_) + (b_)*(x_)^(n_)]^(p_), x_Symbol] :> Simp[(x^(m - n + 1)*Sin[a + b*x^n]^(p + 1))/(b*n*(p + 1)), x] - Dist[(m - n + 1)/(b*n*(p + 1)), Int[x^(m - n)*Sin[a + b*x^n]^(p + 1), x], x] /; FreeQ[{a, b, p}, x] && LtQ[0, n, m + 1] && NeQ[p, -1]

Rule 3310

```
Int[((c_.) + (d_.)*(x_))*((b_.)*sin[(e_.) + (f_.)*(x_)])^(n_), x_Symbol] :=
  Simp[(d*(b*SIN[e + f*x])^n)/(f^2*n^2), x] + (Dist[(b^2*(n - 1))/n, Int[(c
+ d*x)*(b*SIN[e + f*x])^(n - 2), x], x] - Simp[(b*(c + d*x)*Cos[e + f*x]*(b
*SIN[e + f*x])^(n - 1))/(f*n), x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1
]
```

Rule 30

```
Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6519

```
Int[Cos[(a_.) + (b_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_)*SinIntegral[(c_.) +
(d_.)*(x_)], x_Symbol] := Simp[((e + f*x)^m*SIN[a + b*x]*SinIntegral[c + d*
x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*SIN[a + b*x]*Sin[c + d*x])/(c + d*
x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*SIN[a + b*x]*SinIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 2564

```
Int[cos[(e_.) + (f_.)*(x_)]^(n_)*((a_.)*sin[(e_.) + (f_.)*(x_)])^(m_), x_
Symbol] := Dist[1/(a*f), Subst[Int[x^m*(1 - x^2/a^2)^((n - 1)/2), x], x, a*
SIN[e + f*x]], x] /; FreeQ[{a, e, f, m}, x] && IntegerQ[(n - 1)/2] && !(In
tegerQ[(m - 1)/2] && LtQ[0, m, n])
```

Rule 6517

```
Int[Cos[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := S
imp[(SIN[a + b*x]*SinIntegral[c + d*x])/b, x] - Dist[d/b, Int[(SIN[a + b*x]
*SIN[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 3312

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := In
t[ExpandTrigReduce[(c + d*x)^m, SIN[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f
, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int x^3 \text{Si}(bx)^2 dx &= \frac{1}{4}x^4 \text{Si}(bx)^2 - \frac{1}{2} \int x^3 \sin(bx) \text{Si}(bx) dx \\
&= \frac{x^3 \cos(bx) \text{Si}(bx)}{2b} + \frac{1}{4}x^4 \text{Si}(bx)^2 - \frac{1}{2} \int \frac{x^2 \cos(bx) \sin(bx)}{b} dx - \frac{3 \int x^2 \cos(bx) \text{Si}(bx) dx}{2b} \\
&= \frac{x^3 \cos(bx) \text{Si}(bx)}{2b} - \frac{3x^2 \sin(bx) \text{Si}(bx)}{2b^2} + \frac{1}{4}x^4 \text{Si}(bx)^2 + \frac{3 \int x \sin(bx) \text{Si}(bx) dx}{b^2} - \frac{\int x^2 \cos(bx) \sin(bx) dx}{2b} \\
&= -\frac{x^2 \sin^2(bx)}{4b^2} - \frac{3x \cos(bx) \text{Si}(bx)}{b^3} + \frac{x^3 \cos(bx) \text{Si}(bx)}{2b} - \frac{3x^2 \sin(bx) \text{Si}(bx)}{2b^2} + \frac{1}{4}x^4 \text{Si}(bx)^2 + \frac{3 \int \cos(bx) \text{Si}(bx) dx}{b^4} \\
&= -\frac{x \cos(bx) \sin(bx)}{b^3} + \frac{\sin^2(bx)}{2b^4} - \frac{x^2 \sin^2(bx)}{4b^2} - \frac{3x \cos(bx) \text{Si}(bx)}{b^3} + \frac{x^3 \cos(bx) \text{Si}(bx)}{2b} + \frac{3 \sin(bx) \text{Si}(bx)}{b^4} \\
&= \frac{x^2}{2b^2} - \frac{x \cos(bx) \sin(bx)}{b^3} + \frac{\sin^2(bx)}{2b^4} - \frac{x^2 \sin^2(bx)}{4b^2} - \frac{3x \cos(bx) \text{Si}(bx)}{b^3} + \frac{x^3 \cos(bx) \text{Si}(bx)}{2b} + \frac{3 \sin(bx) \text{Si}(bx)}{b^4} \\
&= \frac{x^2}{2b^2} - \frac{x \cos(bx) \sin(bx)}{b^3} + \frac{2 \sin^2(bx)}{b^4} - \frac{x^2 \sin^2(bx)}{4b^2} - \frac{3x \cos(bx) \text{Si}(bx)}{b^3} + \frac{x^3 \cos(bx) \text{Si}(bx)}{2b} + \frac{3 \sin(bx) \text{Si}(bx)}{b^4} \\
&= \frac{x^2}{2b^2} - \frac{3 \log(x)}{2b^4} - \frac{x \cos(bx) \sin(bx)}{b^3} + \frac{2 \sin^2(bx)}{b^4} - \frac{x^2 \sin^2(bx)}{4b^2} - \frac{3x \cos(bx) \text{Si}(bx)}{b^3} + \frac{x^3 \cos(bx) \text{Si}(bx)}{2b} + \frac{3 \sin(bx) \text{Si}(bx)}{b^4} \\
&= \frac{x^2}{2b^2} + \frac{3 \text{Ci}(2bx)}{2b^4} - \frac{3 \log(x)}{2b^4} - \frac{x \cos(bx) \sin(bx)}{b^3} + \frac{2 \sin^2(bx)}{b^4} - \frac{x^2 \sin^2(bx)}{4b^2} - \frac{3x \cos(bx) \text{Si}(bx)}{b^3} + \frac{x^3 \cos(bx) \text{Si}(bx)}{2b} + \frac{3 \sin(bx) \text{Si}(bx)}{b^4}
\end{aligned}$$

Mathematica [A] time = 0.129789, size = 107, normalized size = 0.72

$$\frac{2b^4 x^4 \text{Si}(bx)^2 + 4 \text{Si}(bx) (bx (b^2 x^2 - 6) \cos(bx) - 3 (b^2 x^2 - 2) \sin(bx)) + 3b^2 x^2 + b^2 x^2 \cos(2bx) + 12 \text{CosIntegral}(2bx)}{8b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*SinIntegral[b*x]^2,x]

[Out] (3*b^2*x^2 - 8*Cos[2*b*x] + b^2*x^2*Cos[2*b*x] + 12*CosIntegral[2*b*x] - 12*Log[x] - 4*b*x*Sin[2*b*x] + 4*(b*x*(-6 + b^2*x^2)*Cos[b*x] - 3*(-2 + b^2*x^2)*Sin[b*x]))*SinIntegral[b*x] + 2*b^4*x^4*SinIntegral[b*x]^2)/(8*b^4)

Maple [A] time = 0.069, size = 149, normalized size = 1.

$$\frac{x^4 (\text{Si}(bx))^2}{4} + \frac{x^3 \cos(bx) \text{Si}(bx)}{2b} - \frac{3x^2 \text{Si}(bx) \sin(bx)}{2b^2} + 3 \frac{\text{Si}(bx) \sin(bx)}{b^4} - 3 \frac{x \cos(bx) \text{Si}(bx)}{b^3} + \frac{x^2 (\cos(bx))^2}{4b^2} - \frac{x^2 \sin^2(bx)}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*Si(b*x)^2,x)

[Out] 1/4*x^4*Si(b*x)^2+1/2*x^3*cos(b*x)*Si(b*x)/b-3/2*x^2*Si(b*x)*sin(b*x)/b^2+3*Si(b*x)*sin(b*x)/b^4-3*x*cos(b*x)*Si(b*x)/b^3+1/4/b^2*x^2*cos(b*x)^2-x*cos(b*x)*sin(b*x)/b^3+1/4*x^2/b^2+1/2*sin(b*x)^2/b^4-3/2*cos(b*x)^2/b^4-3/2/b^4*ln(b*x)+3/2*Ci(2*b*x)/b^4

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \text{Si}(bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Si(b*x)^2,x, algorithm="maxima")

[Out] integrate(x^3*Si(b*x)^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^3 \text{Si}(bx)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Si(b*x)^2,x, algorithm="fricas")

[Out] integral(x^3*sin_integral(b*x)^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \text{Si}^2(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*Si(b*x)**2,x)

[Out] Integral(x**3*Si(b*x)**2, x)

Giac [A] time = 1.28656, size = 119, normalized size = 0.8

$$\frac{1}{4} x^4 \text{Si}(bx)^2 + \frac{1}{2} \left(\frac{(b^3 x^3 - 6bx) \cos(bx)}{b^4} - \frac{3(b^2 x^2 - 2) \sin(bx)}{b^4} \right) \text{Si}(bx) + \frac{3(b^2 x^2 + 2 \text{Ci}(2bx) + 2 \text{Ci}(-2bx) - 4 \log(x))}{8b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Si(b*x)^2,x, algorithm="giac")

[Out] 1/4*x^4*sin_integral(b*x)^2 + 1/2*((b^3*x^3 - 6*b*x)*cos(b*x)/b^4 - 3*(b^2*x^2 - 2)*sin(b*x)/b^4)*sin_integral(b*x) + 3/8*(b^2*x^2 + 2*cos_integral(2*b*x) + 2*cos_integral(-2*b*x) - 4*log(x))/b^4

3.11 $\int x^2 \text{Si}(bx)^2 dx$

Optimal. Leaf size=112

$$\frac{2\text{Si}(2bx)}{3b^3} - \frac{4x\text{Si}(bx)\sin(bx)}{3b^2} - \frac{4\text{Si}(bx)\cos(bx)}{3b^3} + \frac{5x}{6b^2} - \frac{x\sin^2(bx)}{3b^2} - \frac{5\sin(bx)\cos(bx)}{6b^3} + \frac{1}{3}x^3\text{Si}(bx)^2 + \frac{2x^2\text{Si}(bx)\cos(bx)}{3b}$$

```
[Out] (5*x)/(6*b^2) - (5*Cos[b*x]*Sin[b*x])/(6*b^3) - (x*Sin[b*x]^2)/(3*b^2) - (4*Cos[b*x]*SinIntegral[b*x])/(3*b^3) + (2*x^2*Cos[b*x]*SinIntegral[b*x])/(3*b) - (4*x*Sin[b*x]*SinIntegral[b*x])/(3*b^2) + (x^3*SinIntegral[b*x]^2)/3 + (2*SinIntegral[2*b*x])/(3*b^3)
```

Rubi [A] time = 0.134827, antiderivative size = 112, normalized size of antiderivative = 1., number of steps used = 15, number of rules used = 10, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 1.$, Rules used = {6507, 6513, 12, 3443, 2635, 8, 6519, 6511, 4406, 3299}

$$\frac{2\text{Si}(2bx)}{3b^3} - \frac{4x\text{Si}(bx)\sin(bx)}{3b^2} - \frac{4\text{Si}(bx)\cos(bx)}{3b^3} + \frac{5x}{6b^2} - \frac{x\sin^2(bx)}{3b^2} - \frac{5\sin(bx)\cos(bx)}{6b^3} + \frac{1}{3}x^3\text{Si}(bx)^2 + \frac{2x^2\text{Si}(bx)\cos(bx)}{3b}$$

Antiderivative was successfully verified.

```
[In] Int[x^2*SinIntegral[b*x]^2,x]
```

```
[Out] (5*x)/(6*b^2) - (5*Cos[b*x]*Sin[b*x])/(6*b^3) - (x*Sin[b*x]^2)/(3*b^2) - (4*Cos[b*x]*SinIntegral[b*x])/(3*b^3) + (2*x^2*Cos[b*x]*SinIntegral[b*x])/(3*b) - (4*x*Sin[b*x]*SinIntegral[b*x])/(3*b^2) + (x^3*SinIntegral[b*x]^2)/3 + (2*SinIntegral[2*b*x])/(3*b^3)
```

Rule 6507

```
Int[(x_)^(m_)*SinIntegral[(b_)*(x_)]^2, x_Symbol] := Simp[(x^(m + 1)*SinIntegral[b*x]^2)/(m + 1), x] - Dist[2/(m + 1), Int[x^m*Sin[b*x]*SinIntegral[b*x], x], x] /; FreeQ[b, x] && IGtQ[m, 0]
```

Rule 6513

```
Int[((e_)+(f_)*(x_))^(m_)*Sin[(a_)+(b_)*(x_)]*SinIntegral[(c_)+(d_)*(x_)], x_Symbol] := -Simp[((e+f*x)^m*Cos[a+b*x]*SinIntegral[c+d*x])/b, x] + (Dist[d/b, Int[((e+f*x)^m*Cos[a+b*x]*Sin[c+d*x])/(c+d*x), x], x] + Dist[(f*m)/b, Int[(e+f*x)^(m-1)*Cos[a+b*x]*SinIntegral[c+d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]
```

Rule 3443

```
Int[Cos[(a_)+(b_)*(x_)^(n_)]*(x_)^(m_)*Sin[(a_)+(b_)*(x_)^(n_)]^(p_), x_Symbol] := Simp[(x^(m-n+1)*Sin[a+b*x^n]^(p+1))/(b*n*(p+1)), x] - Dist[(m-n+1)/(b*n*(p+1)), Int[x^(m-n)*Sin[a+b*x^n]^(p+1), x], x] /; FreeQ[{a, b, p}, x] && LtQ[0, n, m+1] && NeQ[p, -1]
```

Rule 2635

```
Int[((b_)*sin[(c_)+(d_)*(x_)])^(n_), x_Symbol] := -Simp[(b*Cos[c+d*x])*(b*Sin[c+d*x])^(n-1)/(d*n), x] + Dist[(b^2*(n-1))/n, Int[(b*Sin[c
```

+ d*x])^(n - 2), x], x] /; FreeQ[{b, c, d}, x] && GtQ[n, 1] && IntegerQ[2*n]

Rule 8

Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]

Rule 6519

Int[Cos[(a_.) + (b_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.)*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := Simp[((e + f*x)^m*Sin[a + b*x]*SinIntegral[c + d*x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*Sin[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Sin[a + b*x]*SinIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]

Rule 6511

Int[Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := -Simp[(Cos[a + b*x]*SinIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^(n)*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned}
 \int x^2 \text{Si}(bx)^2 dx &= \frac{1}{3} x^3 \text{Si}(bx)^2 - \frac{2}{3} \int x^2 \sin(bx) \text{Si}(bx) dx \\
 &= \frac{2x^2 \cos(bx) \text{Si}(bx)}{3b} + \frac{1}{3} x^3 \text{Si}(bx)^2 - \frac{2}{3} \int \frac{x \cos(bx) \sin(bx)}{b} dx - \frac{4 \int x \cos(bx) \text{Si}(bx) dx}{3b} \\
 &= \frac{2x^2 \cos(bx) \text{Si}(bx)}{3b} - \frac{4x \sin(bx) \text{Si}(bx)}{3b^2} + \frac{1}{3} x^3 \text{Si}(bx)^2 + \frac{4 \int \sin(bx) \text{Si}(bx) dx}{3b^2} - \frac{2 \int x \cos(bx) \sin(bx) dx}{3b} \\
 &= -\frac{x \sin^2(bx)}{3b^2} - \frac{4 \cos(bx) \text{Si}(bx)}{3b^3} + \frac{2x^2 \cos(bx) \text{Si}(bx)}{3b} - \frac{4x \sin(bx) \text{Si}(bx)}{3b^2} + \frac{1}{3} x^3 \text{Si}(bx)^2 + \frac{\int \sin^2(bx) dx}{3b^2} \\
 &= -\frac{5 \cos(bx) \sin(bx)}{6b^3} - \frac{x \sin^2(bx)}{3b^2} - \frac{4 \cos(bx) \text{Si}(bx)}{3b^3} + \frac{2x^2 \cos(bx) \text{Si}(bx)}{3b} - \frac{4x \sin(bx) \text{Si}(bx)}{3b^2} + \frac{1}{3} x^3 \text{Si}(bx)^2 \\
 &= \frac{5x}{6b^2} - \frac{5 \cos(bx) \sin(bx)}{6b^3} - \frac{x \sin^2(bx)}{3b^2} - \frac{4 \cos(bx) \text{Si}(bx)}{3b^3} + \frac{2x^2 \cos(bx) \text{Si}(bx)}{3b} - \frac{4x \sin(bx) \text{Si}(bx)}{3b^2} + \frac{1}{3} x^3 \text{Si}(bx)^2 \\
 &= \frac{5x}{6b^2} - \frac{5 \cos(bx) \sin(bx)}{6b^3} - \frac{x \sin^2(bx)}{3b^2} - \frac{4 \cos(bx) \text{Si}(bx)}{3b^3} + \frac{2x^2 \cos(bx) \text{Si}(bx)}{3b} - \frac{4x \sin(bx) \text{Si}(bx)}{3b^2} + \frac{1}{3} x^3 \text{Si}(bx)^2 \\
 &= \frac{5x}{6b^2} - \frac{5 \cos(bx) \sin(bx)}{6b^3} - \frac{x \sin^2(bx)}{3b^2} - \frac{4 \cos(bx) \text{Si}(bx)}{3b^3} + \frac{2x^2 \cos(bx) \text{Si}(bx)}{3b} - \frac{4x \sin(bx) \text{Si}(bx)}{3b^2} + \frac{1}{3} x^3 \text{Si}(bx)^2
 \end{aligned}$$

Mathematica [A] time = 0.0725869, size = 78, normalized size = 0.7

$$\frac{4b^3x^3\text{Si}(bx)^2 + 8\text{Si}(bx)\left((b^2x^2 - 2)\cos(bx) - 2bx\sin(bx)\right) + 8\text{Si}(2bx) + 8bx - 5\sin(2bx) + 2bx\cos(2bx)}{12b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*SinIntegral[b*x]^2,x]

[Out] (8*b*x + 2*b*x*Cos[2*b*x] - 5*Sin[2*b*x] + 8*((-2 + b^2*x^2)*Cos[b*x] - 2*b*x*Sin[b*x])*SinIntegral[b*x] + 4*b^3*x^3*SinIntegral[b*x]^2 + 8*SinIntegral[2*b*x])/(12*b^3)

Maple [A] time = 0.149, size = 84, normalized size = 0.8

$$\frac{1}{b^3} \left(\frac{b^3 x^3 (\text{Si}(bx))^2}{3} - 2 \text{Si}(bx) \left(-\frac{1}{3} b^2 x^2 \cos(bx) + \frac{2}{3} \cos(bx) + \frac{2}{3} \sin(bx) bx \right) + \frac{bx (\cos(bx))^2}{3} - \frac{5 \sin(bx) \cos(bx)}{6} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*Si(b*x)^2,x)

[Out] 1/b^3*(1/3*b^3*x^3*Si(b*x)^2-2*Si(b*x)*(-1/3*b^2*x^2*cos(b*x)+2/3*cos(b*x)+2/3*sin(b*x)*b*x)+1/3*b*x*cos(b*x)^2-5/6*sin(b*x)*cos(b*x)+1/2*b*x+2/3*Si(2*b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Si}(bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Si(b*x)^2,x, algorithm="maxima")

[Out] integrate(x^2*Si(b*x)^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^2 \text{Si}(bx)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Si(b*x)^2,x, algorithm="fricas")

[Out] integral(x^2*sin_integral(b*x)^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Si}^2(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*Si(b*x)**2,x)

[Out] Integral(x**2*Si(b*x)**2, x)

Giac [C] time = 1.28072, size = 105, normalized size = 0.94

$$\frac{1}{3}x^3 \operatorname{Si}(bx)^2 - \frac{2}{3} \left(\frac{2x \sin(bx)}{b^2} - \frac{(b^2x^2 - 2) \cos(bx)}{b^3} \right) \operatorname{Si}(bx) + \frac{2bx + \Im(\operatorname{Ci}(2bx)) - \Im(\operatorname{Ci}(-2bx)) + 2 \operatorname{Si}(2bx)}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Si(b*x)^2,x, algorithm="giac")

[Out] 1/3*x^3*sin_integral(b*x)^2 - 2/3*(2*x*sin(b*x)/b^2 - (b^2*x^2 - 2)*cos(b*x)/b^3)*sin_integral(b*x) + 1/3*(2*b*x + imag_part(cos_integral(2*b*x)) - imag_part(cos_integral(-2*b*x)) + 2*sin_integral(2*b*x))/b^3

3.12 $\int x \text{Si}(bx)^2 dx$

Optimal. Leaf size=74

$$-\frac{\text{CosIntegral}(2bx)}{2b^2} - \frac{\text{Si}(bx) \sin(bx)}{b^2} + \frac{\log(x)}{2b^2} - \frac{\sin^2(bx)}{2b^2} + \frac{1}{2}x^2\text{Si}(bx)^2 + \frac{x\text{Si}(bx) \cos(bx)}{b}$$

```
[Out] -CosIntegral[2*b*x]/(2*b^2) + Log[x]/(2*b^2) - Sin[b*x]^2/(2*b^2) + (x*Cos[
b*x]*SinIntegral[b*x])/b - (Sin[b*x]*SinIntegral[b*x])/b^2 + (x^2*SinIntegr
al[b*x]^2)/2
```

Rubi [A] time = 0.0952158, antiderivative size = 74, normalized size of antiderivative = 1., number of steps used = 10, number of rules used = 8, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 1.$, Rules used = {6507, 6513, 12, 2564, 30, 6517, 3312, 3302}

$$-\frac{\text{CosIntegral}(2bx)}{2b^2} - \frac{\text{Si}(bx) \sin(bx)}{b^2} + \frac{\log(x)}{2b^2} - \frac{\sin^2(bx)}{2b^2} + \frac{1}{2}x^2\text{Si}(bx)^2 + \frac{x\text{Si}(bx) \cos(bx)}{b}$$

Antiderivative was successfully verified.

```
[In] Int[x*SinIntegral[b*x]^2,x]
```

```
[Out] -CosIntegral[2*b*x]/(2*b^2) + Log[x]/(2*b^2) - Sin[b*x]^2/(2*b^2) + (x*Cos[
b*x]*SinIntegral[b*x])/b - (Sin[b*x]*SinIntegral[b*x])/b^2 + (x^2*SinIntegr
al[b*x]^2)/2
```

Rule 6507

```
Int[(x_)^(m_)*SinIntegral[(b_)*(x_)]^2, x_Symbol] := Simp[(x^(m + 1)*SinI
ntegral[b*x]^2)/(m + 1), x] - Dist[2/(m + 1), Int[x^m*Sin[b*x]*SinIntegral[
b*x], x], x] /; FreeQ[b, x] && IGtQ[m, 0]
```

Rule 6513

```
Int[((e_) + (f_)*(x_))^(m_)*Sin[(a_) + (b_)*(x_)]*SinIntegral[(c_) +
(d_)*(x_)], x_Symbol] := -Simp[((e + f*x)^m*Cos[a + b*x]*SinIntegral[c + d
*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*Cos[a + b*x]*Sin[c + d*x])/(c + d*
x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Cos[a + b*x]*SinIntegral[c
+ d*x], x], x)) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !Match
Q[u, (b_)*(v_)] /; FreeQ[b, x]
```

Rule 2564

```
Int[cos[(e_) + (f_)*(x_)]^(n_)*((a_)*sin[(e_) + (f_)*(x_)]^(m_), x_
Symbol] := Dist[1/(a*f), Subst[Int[x^m*(1 - x^2/a^2)^(n - 1)/2], x], x, a*
Sin[e + f*x]], x] /; FreeQ[{a, e, f, m}, x] && IntegerQ[(n - 1)/2] && !(In
tegerQ[(m - 1)/2] && LtQ[0, m, n])
```

Rule 30

```
Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6517

```
Int[Cos[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := S
imp[(Sin[a + b*x]*SinIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]
*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 3312

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := In
t[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f
, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int x \operatorname{Si}(bx)^2 dx &= \frac{1}{2}x^2 \operatorname{Si}(bx)^2 - \int x \sin(bx) \operatorname{Si}(bx) dx \\
&= \frac{x \cos(bx) \operatorname{Si}(bx)}{b} + \frac{1}{2}x^2 \operatorname{Si}(bx)^2 - \frac{\int \cos(bx) \operatorname{Si}(bx) dx}{b} - \int \frac{\cos(bx) \sin(bx)}{b} dx \\
&= \frac{x \cos(bx) \operatorname{Si}(bx)}{b} - \frac{\sin(bx) \operatorname{Si}(bx)}{b^2} + \frac{1}{2}x^2 \operatorname{Si}(bx)^2 - \frac{\int \cos(bx) \sin(bx) dx}{b} + \frac{\int \frac{\sin^2(bx)}{bx} dx}{b} \\
&= \frac{x \cos(bx) \operatorname{Si}(bx)}{b} - \frac{\sin(bx) \operatorname{Si}(bx)}{b^2} + \frac{1}{2}x^2 \operatorname{Si}(bx)^2 + \frac{\int \frac{\sin^2(bx)}{x} dx}{b^2} - \frac{\operatorname{Subst}\left(\int x dx, x, \sin(bx)\right)}{b^2} \\
&= -\frac{\sin^2(bx)}{2b^2} + \frac{x \cos(bx) \operatorname{Si}(bx)}{b} - \frac{\sin(bx) \operatorname{Si}(bx)}{b^2} + \frac{1}{2}x^2 \operatorname{Si}(bx)^2 + \frac{\int \left(\frac{1}{2x} - \frac{\cos(2bx)}{2x}\right) dx}{b^2} \\
&= \frac{\log(x)}{2b^2} - \frac{\sin^2(bx)}{2b^2} + \frac{x \cos(bx) \operatorname{Si}(bx)}{b} - \frac{\sin(bx) \operatorname{Si}(bx)}{b^2} + \frac{1}{2}x^2 \operatorname{Si}(bx)^2 - \frac{\int \frac{\cos(2bx)}{x} dx}{2b^2} \\
&= -\frac{\operatorname{Ci}(2bx)}{2b^2} + \frac{\log(x)}{2b^2} - \frac{\sin^2(bx)}{2b^2} + \frac{x \cos(bx) \operatorname{Si}(bx)}{b} - \frac{\sin(bx) \operatorname{Si}(bx)}{b^2} + \frac{1}{2}x^2 \operatorname{Si}(bx)^2
\end{aligned}$$

Mathematica [A] time = 0.0533695, size = 58, normalized size = 0.78

$$\frac{2b^2x^2\operatorname{Si}(bx)^2 - 2\operatorname{CosIntegral}(2bx) + 4\operatorname{Si}(bx)(bx\cos(bx) - \sin(bx)) + \cos(2bx) + 2\log(x)}{4b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*SinIntegral[b*x]^2,x]

[Out] (Cos[2*b*x] - 2*CosIntegral[2*b*x] + 2*Log[x] + 4*(b*x*cos[b*x] - Sin[b*x]) *SinIntegral[b*x] + 2*b^2*x^2*SinIntegral[b*x]^2)/(4*b^2)

Maple [A] time = 0.058, size = 69, normalized size = 0.9

$$\frac{x^2 (\operatorname{Si}(bx))^2}{2} + \frac{x \cos(bx) \operatorname{Si}(bx)}{b} - \frac{\operatorname{Si}(bx) \sin(bx)}{b^2} + \frac{(\cos(bx))^2}{2b^2} + \frac{\ln(bx)}{2b^2} - \frac{\operatorname{Ci}(2bx)}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*Si(b*x)^2,x)`

[Out] $\frac{1}{2}x^2\text{Si}(bx)^2 + x\cos(bx)\text{Si}(bx)/b - \text{Si}(bx)\sin(bx)/b^2 + \frac{1}{2}/b^2\cos(bx)^2 + \frac{1}{2}/b^2\ln(bx) - \frac{1}{2}\text{Ci}(2bx)/b^2$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x\text{Si}(bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Si(b*x)^2,x, algorithm="maxima")`

[Out] `integrate(x*Si(b*x)^2, x)`

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x\text{Si}(bx)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Si(b*x)^2,x, algorithm="fricas")`

[Out] `integral(x*sin_integral(b*x)^2, x)`

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x\text{Si}^2(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Si(b*x)**2,x)`

[Out] `Integral(x*Si(b*x)**2, x)`

Giac [A] time = 1.32525, size = 76, normalized size = 1.03

$$\frac{1}{2}x^2\text{Si}(bx)^2 + \left(\frac{x\cos(bx)}{b} - \frac{\sin(bx)}{b^2}\right)\text{Si}(bx) - \frac{\text{Ci}(2bx) + \text{Ci}(-2bx) - 2\log(x)}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Si(b*x)^2,x, algorithm="giac")`

[Out] $\frac{1}{2}x^2\sin_integral(bx)^2 + (x\cos(bx)/b - \sin(bx)/b^2)\sin_integral(bx) - \frac{1}{4}(\cos_integral(2bx) + \cos_integral(-2bx) - 2\log(x))/b^2$

3.13 $\int \text{Si}(bx)^2 dx$

Optimal. Leaf size=32

$$x\text{Si}(bx)^2 - \frac{\text{Si}(2bx)}{b} + \frac{2\text{Si}(bx)\cos(bx)}{b}$$

[Out] (2*Cos[b*x]*SinIntegral[b*x])/b + x*SinIntegral[b*x]^2 - SinIntegral[2*b*x]/b

Rubi [A] time = 0.0508099, antiderivative size = 32, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 5, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.833$, Rules used = {6505, 6511, 12, 4406, 3299}

$$x\text{Si}(bx)^2 - \frac{\text{Si}(2bx)}{b} + \frac{2\text{Si}(bx)\cos(bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[SinIntegral[b*x]^2,x]

[Out] (2*Cos[b*x]*SinIntegral[b*x])/b + x*SinIntegral[b*x]^2 - SinIntegral[2*b*x]/b

Rule 6505

Int[SinIntegral[(a_.) + (b_.)*(x_)]^2, x_Symbol] := Simp[((a + b*x)*SinIntegral[a + b*x]^2)/b, x] - Dist[2, Int[Sin[a + b*x]*SinIntegral[a + b*x], x], x] /; FreeQ[{a, b}, x]

Rule 6511

Int[Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := -Simp[(Cos[a + b*x]*SinIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_.)*(v_)] /; FreeQ[b, x]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned}
\int \operatorname{Si}(bx)^2 dx &= x\operatorname{Si}(bx)^2 - 2 \int \sin(bx)\operatorname{Si}(bx) dx \\
&= \frac{2 \cos(bx)\operatorname{Si}(bx)}{b} + x\operatorname{Si}(bx)^2 - 2 \int \frac{\cos(bx) \sin(bx)}{bx} dx \\
&= \frac{2 \cos(bx)\operatorname{Si}(bx)}{b} + x\operatorname{Si}(bx)^2 - \frac{2 \int \frac{\cos(bx) \sin(bx)}{x} dx}{b} \\
&= \frac{2 \cos(bx)\operatorname{Si}(bx)}{b} + x\operatorname{Si}(bx)^2 - \frac{2 \int \frac{\sin(2bx)}{2x} dx}{b} \\
&= \frac{2 \cos(bx)\operatorname{Si}(bx)}{b} + x\operatorname{Si}(bx)^2 - \frac{\int \frac{\sin(2bx)}{x} dx}{b} \\
&= \frac{2 \cos(bx)\operatorname{Si}(bx)}{b} + x\operatorname{Si}(bx)^2 - \frac{\operatorname{Si}(2bx)}{b}
\end{aligned}$$

Mathematica [A] time = 0.0075411, size = 32, normalized size = 1.

$$x\operatorname{Si}(bx)^2 - \frac{\operatorname{Si}(2bx)}{b} + \frac{2\operatorname{Si}(bx) \cos(bx)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[SinIntegral[b*x]^2,x]

[Out] (2*Cos[b*x]*SinIntegral[b*x])/b + x*SinIntegral[b*x]^2 - SinIntegral[2*b*x]/b

Maple [A] time = 0.05, size = 32, normalized size = 1.

$$\frac{bx (\operatorname{Si}(bx))^2 + 2 \cos(bx) \operatorname{Si}(bx) - \operatorname{Si}(2bx)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x)^2,x)

[Out] 1/b*(b*x*Si(b*x)^2+2*cos(b*x)*Si(b*x)-Si(2*b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \operatorname{Si}(bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)^2,x, algorithm="maxima")

[Out] integrate(Si(b*x)^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}(\operatorname{Si}(bx)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)^2,x, algorithm="fricas")

[Out] integral(sin_integral(b*x)^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \operatorname{Si}^2(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)**2,x)

[Out] Integral(Si(b*x)**2, x)

Giac [C] time = 1.33996, size = 66, normalized size = 2.06

$$x \operatorname{Si}(bx)^2 + \frac{2 \cos(bx) \operatorname{Si}(bx)}{b} - \frac{\Im(\operatorname{Ci}(2bx)) - \Im(\operatorname{Ci}(-2bx)) + 2 \operatorname{Si}(2bx)}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)^2,x, algorithm="giac")

[Out] x*sin_integral(b*x)^2 + 2*cos(b*x)*sin_integral(b*x)/b - 1/2*(imag_part(cos_integral(2*b*x)) - imag_part(cos_integral(-2*b*x)) + 2*sin_integral(2*b*x))/b

$$3.14 \quad \int \frac{\text{Si}(bx)^2}{x} dx$$

Optimal. Leaf size=12

CannotIntegrate $\left(\frac{\text{Si}(bx)^2}{x}, x\right)$

[Out] CannotIntegrate[SinIntegral[b*x]^2/x, x]

Rubi [A] time = 0.022994, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{Si}(bx)^2}{x} dx$$

Verification is Not applicable to the result.

[In] Int[SinIntegral[b*x]^2/x, x]

[Out] Defer[Int][SinIntegral[b*x]^2/x, x]

Rubi steps

$$\int \frac{\text{Si}(bx)^2}{x} dx = \int \frac{\text{Si}(bx)^2}{x} dx$$

Mathematica [A] time = 0.423825, size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)^2}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[SinIntegral[b*x]^2/x, x]

[Out] Integrate[SinIntegral[b*x]^2/x, x]

Maple [A] time = 0.053, size = 0, normalized size = 0.

$$\int \frac{(\text{Si}(bx))^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x)^2/x, x)

[Out] int(Si(b*x)^2/x, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)^2/x,x, algorithm="maxima")

[Out] integrate(Si(b*x)^2/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Si}(bx)^2}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)^2/x,x, algorithm="fricas")

[Out] integral(sin_integral(b*x)^2/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}^2(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)**2/x,x)

[Out] Integral(Si(b*x)**2/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)^2/x,x, algorithm="giac")

[Out] integrate(Si(b*x)^2/x, x)

$$3.15 \quad \int \frac{\text{Si}(bx)^2}{x^2} dx$$

Optimal. Leaf size=12

CannotIntegrate $\left(\frac{\text{Si}(bx)^2}{x^2}, x\right)$

[Out] CannotIntegrate[SinIntegral[b*x]^2/x^2, x]

Rubi [A] time = 0.0244746, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{Si}(bx)^2}{x^2} dx$$

Verification is Not applicable to the result.

[In] Int[SinIntegral[b*x]^2/x^2, x]

[Out] Defer[Int][SinIntegral[b*x]^2/x^2, x]

Rubi steps

$$\int \frac{\text{Si}(bx)^2}{x^2} dx = \int \frac{\text{Si}(bx)^2}{x^2} dx$$

Mathematica [A] time = 0.468781, size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)^2}{x^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[SinIntegral[b*x]^2/x^2, x]

[Out] Integrate[SinIntegral[b*x]^2/x^2, x]

Maple [A] time = 0.056, size = 0, normalized size = 0.

$$\int \frac{(\text{Si}(bx))^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x)^2/x^2, x)

[Out] int(Si(b*x)^2/x^2, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)^2/x^2,x, algorithm="maxima")

[Out] integrate(Si(b*x)^2/x^2, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Si}(bx)^2}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)^2/x^2,x, algorithm="fricas")

[Out] integral(sin_integral(b*x)^2/x^2, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}^2(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)**2/x**2,x)

[Out] Integral(Si(b*x)**2/x**2, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)^2/x^2,x, algorithm="giac")

[Out] integrate(Si(b*x)^2/x^2, x)

$$3.16 \quad \int \frac{\text{Si}(bx)^2}{x^3} dx$$

Optimal. Leaf size=12

$$\text{CannotIntegrate}\left(\frac{\text{Si}(bx)^2}{x^3}, x\right)$$

[Out] CannotIntegrate[SinIntegral[b*x]^2/x^3, x]

Rubi [A] time = 0.02474, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{Si}(bx)^2}{x^3} dx$$

Verification is Not applicable to the result.

[In] Int[SinIntegral[b*x]^2/x^3, x]

[Out] Defer[Int][SinIntegral[b*x]^2/x^3, x]

Rubi steps

$$\int \frac{\text{Si}(bx)^2}{x^3} dx = \int \frac{\text{Si}(bx)^2}{x^3} dx$$

Mathematica [A] time = 0.501191, size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)^2}{x^3} dx$$

Verification is Not applicable to the result.

[In] Integrate[SinIntegral[b*x]^2/x^3, x]

[Out] Integrate[SinIntegral[b*x]^2/x^3, x]

Maple [A] time = 0.054, size = 0, normalized size = 0.

$$\int \frac{(\text{Si}(bx))^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x)^2/x^3, x)

[Out] int(Si(b*x)^2/x^3, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)^2/x^3,x, algorithm="maxima")

[Out] integrate(Si(b*x)^2/x^3, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Si}(bx)^2}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)^2/x^3,x, algorithm="fricas")

[Out] integral(sin_integral(b*x)^2/x^3, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}^2(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)**2/x**3,x)

[Out] Integral(Si(b*x)**2/x**3, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)^2/x^3,x, algorithm="giac")

[Out] integrate(Si(b*x)^2/x^3, x)

3.17 $\int x^m \text{Si}(a + bx) dx$

Optimal. Leaf size=47

$$\frac{x^{m+1} \text{Si}(a + bx)}{m + 1} - \frac{b \text{CannotIntegrate}\left(\frac{x^{m+1} \sin(a+bx)}{a+bx}, x\right)}{m + 1}$$

[Out] $-\left(\frac{b \text{CannotIntegrate}[(x^{1+m}) \sin[a + b*x]]}{(a + b*x)}, x\right)/(1 + m) + (x^{1+m}) \text{SinIntegral}[a + b*x]/(1 + m)$

Rubi [A] time = 0.294585, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int x^m \text{Si}(a + bx) dx$$

Verification is Not applicable to the result.

[In] Int[x^m*SinIntegral[a + b*x],x]

[Out] $(x^{1+m}) \text{SinIntegral}[a + b*x]/(1 + m) - (b \text{Defer}[\text{Int}][(x^{1+m}) \sin[a + b*x]]/(a + b*x), x)/(1 + m)$

Rubi steps

$$\int x^m \text{Si}(a + bx) dx = \frac{x^{1+m} \text{Si}(a + bx)}{1 + m} - \frac{b \int \frac{x^{1+m} \sin(a+bx)}{a+bx} dx}{1 + m}$$

Mathematica [A] time = 4.09459, size = 0, normalized size = 0.

$$\int x^m \text{Si}(a + bx) dx$$

Verification is Not applicable to the result.

[In] Integrate[x^m*SinIntegral[a + b*x],x]

[Out] Integrate[x^m*SinIntegral[a + b*x], x]

Maple [A] time = 0.185, size = 0, normalized size = 0.

$$\int x^m \text{Si}(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*Si(b*x+a),x)

[Out] int(x^m*Si(b*x+a),x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \operatorname{Si}(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Si(b*x+a),x, algorithm="maxima")

[Out] integrate(x^m*Si(b*x + a), x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}(x^m \operatorname{Si}(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Si(b*x+a),x, algorithm="fricas")

[Out] integral(x^m*sin_integral(b*x + a), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \operatorname{Si}(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m*Si(b*x+a),x)

[Out] Integral(x**m*Si(a + b*x), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \operatorname{Si}(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Si(b*x+a),x, algorithm="giac")

[Out] integrate(x^m*Si(b*x + a), x)

3.18 $\int x^3 \text{Si}(a + bx) dx$

Optimal. Leaf size=184

$$\frac{a^4 \text{Si}(a + bx)}{4b^4} - \frac{a^2 \sin(a + bx)}{4b^4} - \frac{a^3 \cos(a + bx)}{4b^4} + \frac{a^2 x \cos(a + bx)}{4b^3} - \frac{3x^2 \sin(a + bx)}{4b^2} - \frac{ax^2 \cos(a + bx)}{4b^2} + \frac{ax \sin(a + bx)}{2b^3}$$

[Out] (a*cos[a + b*x])/(2*b^4) - (a^3*cos[a + b*x])/(4*b^4) - (3*x*cos[a + b*x])/(2*b^3) + (a^2*x*cos[a + b*x])/(4*b^3) - (a*x^2*cos[a + b*x])/(4*b^2) + (x^3*cos[a + b*x])/(4*b) + (3*sin[a + b*x])/(2*b^4) - (a^2*sin[a + b*x])/(4*b^4) + (a*x*sin[a + b*x])/(2*b^3) - (3*x^2*sin[a + b*x])/(4*b^2) - (a^4*sinIntegral[a + b*x])/(4*b^4) + (x^4*sinIntegral[a + b*x])/4

Rubi [A] time = 0.36786, antiderivative size = 184, normalized size of antiderivative = 1., number of steps used = 14, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.6$, Rules used = {6503, 6742, 2638, 3296, 2637, 3299}

$$\frac{a^4 \text{Si}(a + bx)}{4b^4} - \frac{a^2 \sin(a + bx)}{4b^4} - \frac{a^3 \cos(a + bx)}{4b^4} + \frac{a^2 x \cos(a + bx)}{4b^3} - \frac{3x^2 \sin(a + bx)}{4b^2} - \frac{ax^2 \cos(a + bx)}{4b^2} + \frac{ax \sin(a + bx)}{2b^3}$$

Antiderivative was successfully verified.

[In] Int[x^3*SinIntegral[a + b*x],x]

[Out] (a*cos[a + b*x])/(2*b^4) - (a^3*cos[a + b*x])/(4*b^4) - (3*x*cos[a + b*x])/(2*b^3) + (a^2*x*cos[a + b*x])/(4*b^3) - (a*x^2*cos[a + b*x])/(4*b^2) + (x^3*cos[a + b*x])/(4*b) + (3*sin[a + b*x])/(2*b^4) - (a^2*sin[a + b*x])/(4*b^4) + (a*x*sin[a + b*x])/(2*b^3) - (3*x^2*sin[a + b*x])/(4*b^2) - (a^4*sinIntegral[a + b*x])/(4*b^4) + (x^4*sinIntegral[a + b*x])/4

Rule 6503

Int[((c_.) + (d_.)*(x_))^(m_.)*SinIntegral[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[((c + d*x)^(m + 1)*SinIntegral[a + b*x])/(d*(m + 1)), x] - Dist[b/(d*(m + 1)), Int[((c + d*x)^(m + 1)*Sin[a + b*x])/(a + b*x), x], x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]

Rule 6742

Int[u_, x_Symbol] :> With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]]

Rule 2638

Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] :> -Simp[Cos[c + d*x]/d, x] /; FreeQ[{c, d}, x]

Rule 3296

Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)], x_Symbol] :> -Simp[((c + d*x)^m*cos[e + f*x])/f, x] + Dist[(d*m)/f, Int[(c + d*x)^(m - 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && GtQ[m, 0]

Rule 2637

Int[sin[Pi/2 + (c_.) + (d_.)*(x_)], x_Symbol] :> Simp[Sin[c + d*x]/d, x] /; FreeQ[{c, d}, x]

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int x^3 \text{Si}(a + bx) dx &= \frac{1}{4} x^4 \text{Si}(a + bx) - \frac{1}{4} b \int \frac{x^4 \sin(a + bx)}{a + bx} dx \\
&= \frac{1}{4} x^4 \text{Si}(a + bx) - \frac{1}{4} b \int \left(-\frac{a^3 \sin(a + bx)}{b^4} + \frac{a^2 x \sin(a + bx)}{b^3} - \frac{a x^2 \sin(a + bx)}{b^2} + \frac{x^3 \sin(a + bx)}{b} + \frac{a^4 \sin(a + bx)}{b^4} \right) dx \\
&= \frac{1}{4} x^4 \text{Si}(a + bx) - \frac{1}{4} \int x^3 \sin(a + bx) dx + \frac{a^3 \int \sin(a + bx) dx}{4b^3} - \frac{a^4 \int \frac{\sin(a + bx)}{a + bx} dx}{4b^3} - \frac{a^2 \int x \sin(a + bx) dx}{4b^2} \\
&= -\frac{a^3 \cos(a + bx)}{4b^4} + \frac{a^2 x \cos(a + bx)}{4b^3} - \frac{a x^2 \cos(a + bx)}{4b^2} + \frac{x^3 \cos(a + bx)}{4b} - \frac{a^4 \text{Si}(a + bx)}{4b^4} + \frac{1}{4} x^4 \text{Si}(a + bx) \\
&= -\frac{a^3 \cos(a + bx)}{4b^4} + \frac{a^2 x \cos(a + bx)}{4b^3} - \frac{a x^2 \cos(a + bx)}{4b^2} + \frac{x^3 \cos(a + bx)}{4b} - \frac{a^2 \sin(a + bx)}{4b^4} + \frac{a x \sin(a + bx)}{2b^3} \\
&= \frac{a \cos(a + bx)}{2b^4} - \frac{a^3 \cos(a + bx)}{4b^4} - \frac{3x \cos(a + bx)}{2b^3} + \frac{a^2 x \cos(a + bx)}{4b^3} - \frac{a x^2 \cos(a + bx)}{4b^2} + \frac{x^3 \cos(a + bx)}{4b} \\
&= \frac{a \cos(a + bx)}{2b^4} - \frac{a^3 \cos(a + bx)}{4b^4} - \frac{3x \cos(a + bx)}{2b^3} + \frac{a^2 x \cos(a + bx)}{4b^3} - \frac{a x^2 \cos(a + bx)}{4b^2} + \frac{x^3 \cos(a + bx)}{4b}
\end{aligned}$$

Mathematica [A] time = 0.196839, size = 96, normalized size = 0.52

$$\frac{(b^4 x^4 - a^4) \text{Si}(a + bx) - (a^2 - 2abx + 3b^2 x^2 - 6) \sin(a + bx) + (a^2 bx - a^3 - ab^2 x^2 + 2a + b^3 x^3 - 6bx) \cos(a + bx)}{4b^4}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^3*SinIntegral[a + b*x], x]
```

```
[Out] ((2*a - a^3 - 6*b*x + a^2*b*x - a*b^2*x^2 + b^3*x^3)*Cos[a + b*x] - (-6 + a^2 - 2*a*b*x + 3*b^2*x^2)*Sin[a + b*x] + (-a^4 + b^4*x^4)*SinIntegral[a + b*x])/(4*b^4)
```

Maple [A] time = 0.049, size = 157, normalized size = 0.9

$$\frac{1}{b^4} \left(\frac{\text{Si}(bx + a) b^4 x^4}{4} + \frac{(bx + a)^3 \cos(bx + a)}{4} - \frac{3(bx + a)^2 \sin(bx + a)}{4} + \frac{3 \sin(bx + a)}{2} - \frac{(3bx + 3a) \cos(bx + a)}{2} + a \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^3*Si(b*x+a), x)
```

```
[Out] 1/b^4*(1/4*Si(b*x+a)*b^4*x^4+1/4*(b*x+a)^3*cos(b*x+a)-3/4*(b*x+a)^2*sin(b*x+a)+3/2*sin(b*x+a)-3/2*(b*x+a)*cos(b*x+a)+a*(-(b*x+a)^2*cos(b*x+a)+2*cos(b*x+a)+2*sin(b*x+a)*(b*x+a))-3/2*a^2*(-(b*x+a)*cos(b*x+a)+sin(b*x+a))-a^3*cos(b*x+a)-1/4*a^4*Si(b*x+a))
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \text{Si}(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Si(b*x+a),x, algorithm="maxima")

[Out] integrate(x^3*Si(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^3 \text{Si}(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Si(b*x+a),x, algorithm="fricas")

[Out] integral(x^3*sin_integral(b*x + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \text{Si}(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*Si(b*x+a),x)

[Out] Integral(x**3*Si(a + b*x), x)

Giac [C] time = 1.28597, size = 74, normalized size = 0.4

$$\frac{1}{4} x^4 \text{Si}(bx + a) - \frac{a^4 \Im(\text{Ci}(bx + a)) - a^4 \Im(\text{Ci}(-bx - a)) + 2 a^4 \text{Si}(bx + a)}{8 b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Si(b*x+a),x, algorithm="giac")

[Out] 1/4*x^4*sin_integral(b*x + a) - 1/8*(a^4*imag_part(cos_integral(b*x + a)) - a^4*imag_part(cos_integral(-b*x - a)) + 2*a^4*sin_integral(b*x + a))/b^4

3.19 $\int x^2 \text{Si}(a + bx) dx$

Optimal. Leaf size=118

$$\frac{a^3 \text{Si}(a + bx)}{3b^3} + \frac{a^2 \cos(a + bx)}{3b^3} + \frac{a \sin(a + bx)}{3b^3} - \frac{2x \sin(a + bx)}{3b^2} - \frac{ax \cos(a + bx)}{3b^2} - \frac{2 \cos(a + bx)}{3b^3} + \frac{1}{3} x^3 \text{Si}(a + bx) + \frac{x^2}{3}$$

[Out] $(-2*\text{Cos}[a + b*x])/(3*b^3) + (a^2*\text{Cos}[a + b*x])/(3*b^3) - (a*x*\text{Cos}[a + b*x])/(3*b^2) + (x^2*\text{Cos}[a + b*x])/(3*b) + (a*\text{Sin}[a + b*x])/(3*b^3) - (2*x*\text{Sin}[a + b*x])/(3*b^2) + (a^3*\text{SinIntegral}[a + b*x])/(3*b^3) + (x^3*\text{SinIntegral}[a + b*x])/3$

Rubi [A] time = 0.276629, antiderivative size = 118, normalized size of antiderivative = 1., number of steps used = 10, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.6$, Rules used = {6503, 6742, 2638, 3296, 2637, 3299}

$$\frac{a^3 \text{Si}(a + bx)}{3b^3} + \frac{a^2 \cos(a + bx)}{3b^3} + \frac{a \sin(a + bx)}{3b^3} - \frac{2x \sin(a + bx)}{3b^2} - \frac{ax \cos(a + bx)}{3b^2} - \frac{2 \cos(a + bx)}{3b^3} + \frac{1}{3} x^3 \text{Si}(a + bx) + \frac{x^2}{3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2*\text{SinIntegral}[a + b*x], x]$

[Out] $(-2*\text{Cos}[a + b*x])/(3*b^3) + (a^2*\text{Cos}[a + b*x])/(3*b^3) - (a*x*\text{Cos}[a + b*x])/(3*b^2) + (x^2*\text{Cos}[a + b*x])/(3*b) + (a*\text{Sin}[a + b*x])/(3*b^3) - (2*x*\text{Sin}[a + b*x])/(3*b^2) + (a^3*\text{SinIntegral}[a + b*x])/(3*b^3) + (x^3*\text{SinIntegral}[a + b*x])/3$

Rule 6503

$\text{Int}[(c + d*x)^m * \text{SinIntegral}[a + b*x], x_Symbol] :> \text{Simp}[(c + d*x)^{m+1} * \text{SinIntegral}[a + b*x] / (d*(m+1)), x] - \text{Dist}[b / (d*(m+1)), \text{Int}[(c + d*x)^{m+1} * \text{Sin}[a + b*x] / (a + b*x), x], x] /;$ FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]

Rule 6742

$\text{Int}[u, x_Symbol] :> \text{With}[\{v = \text{ExpandIntegrand}[u, x]\}, \text{Int}[v, x] /;$ SumQ[v]

Rule 2638

$\text{Int}[\sin[c + d*x], x_Symbol] :> -\text{Simp}[\cos[c + d*x] / d, x] /;$ FreeQ[{c, d}, x]

Rule 3296

$\text{Int}[(c + d*x)^m * \sin[e + f*x], x_Symbol] :> -\text{Simp}[(c + d*x)^m * \cos[e + f*x] / f, x] + \text{Dist}[(d*m) / f, \text{Int}[(c + d*x)^{m-1} * \cos[e + f*x], x], x] /;$ FreeQ[{c, d, e, f}, x] && GtQ[m, 0]

Rule 2637

$\text{Int}[\sin[\pi/2 + c + d*x], x_Symbol] :> \text{Simp}[\sin[c + d*x] / d, x] /;$ FreeQ[{c, d}, x]

Rule 3299

`Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]`

Rubi steps

$$\begin{aligned}
 \int x^2 \text{Si}(a+bx) dx &= \frac{1}{3} x^3 \text{Si}(a+bx) - \frac{1}{3} b \int \frac{x^3 \sin(a+bx)}{a+bx} dx \\
 &= \frac{1}{3} x^3 \text{Si}(a+bx) - \frac{1}{3} b \int \left(\frac{a^2 \sin(a+bx)}{b^3} - \frac{ax \sin(a+bx)}{b^2} + \frac{x^2 \sin(a+bx)}{b} - \frac{a^3 \sin(a+bx)}{b^3(a+bx)} \right) dx \\
 &= \frac{1}{3} x^3 \text{Si}(a+bx) - \frac{1}{3} \int x^2 \sin(a+bx) dx - \frac{a^2 \int \sin(a+bx) dx}{3b^2} + \frac{a^3 \int \frac{\sin(a+bx)}{a+bx} dx}{3b^2} + \frac{a \int x \sin(a+bx) dx}{3b} \\
 &= \frac{a^2 \cos(a+bx)}{3b^3} - \frac{ax \cos(a+bx)}{3b^2} + \frac{x^2 \cos(a+bx)}{3b} + \frac{a^3 \text{Si}(a+bx)}{3b^3} + \frac{1}{3} x^3 \text{Si}(a+bx) + \frac{a \int \cos(a+bx) dx}{3b^2} \\
 &= \frac{a^2 \cos(a+bx)}{3b^3} - \frac{ax \cos(a+bx)}{3b^2} + \frac{x^2 \cos(a+bx)}{3b} + \frac{a \sin(a+bx)}{3b^3} - \frac{2x \sin(a+bx)}{3b^2} + \frac{a^3 \text{Si}(a+bx)}{3b^3} \\
 &= -\frac{2 \cos(a+bx)}{3b^3} + \frac{a^2 \cos(a+bx)}{3b^3} - \frac{ax \cos(a+bx)}{3b^2} + \frac{x^2 \cos(a+bx)}{3b} + \frac{a \sin(a+bx)}{3b^3} - \frac{2x \sin(a+bx)}{3b^2}
 \end{aligned}$$

Mathematica [A] time = 0.141367, size = 63, normalized size = 0.53

$$\frac{(a^3 + b^3 x^3) \text{Si}(a+bx) + (a^2 - abx + b^2 x^2 - 2) \cos(a+bx) + (a - 2bx) \sin(a+bx)}{3b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*SinIntegral[a + b*x], x]

[Out] $((-2 + a^2 - a*b*x + b^2*x^2)*\text{Cos}[a + b*x] + (a - 2*b*x)*\text{Sin}[a + b*x] + (a^3 + b^3*x^3)*\text{SinIntegral}[a + b*x]) / (3*b^3)$

Maple [A] time = 0.053, size = 99, normalized size = 0.8

$$\frac{1}{b^3} \left(\frac{b^3 x^3 \text{Si}(bx+a)}{3} + \frac{(bx+a)^2 \cos(bx+a)}{3} - \frac{2 \cos(bx+a)}{3} - \frac{2 \sin(bx+a)(bx+a)}{3} + a(-bx+a) \cos(bx+a) + \dots \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*Si(b*x+a), x)

[Out] $1/b^3*(1/3*b^3*x^3*Si(b*x+a)+1/3*(b*x+a)^2*cos(b*x+a)-2/3*cos(b*x+a)-2/3*sin(b*x+a)*(b*x+a)+a*(-(b*x+a)*cos(b*x+a)+sin(b*x+a))+a^2*cos(b*x+a)+1/3*a^3*Si(b*x+a))$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Si}(bx+a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Si(b*x+a), x, algorithm="maxima")

[Out] integrate(x²*Si(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^2 \text{Si}(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x²*Si(b*x+a),x, algorithm="fricas")

[Out] integral(x²*sin_integral(b*x + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Si}(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*Si(b*x+a),x)

[Out] Integral(x**2*Si(a + b*x), x)

Giac [C] time = 1.21799, size = 74, normalized size = 0.63

$$\frac{1}{3} x^3 \text{Si}(bx + a) + \frac{a^3 \Im(\text{Ci}(bx + a)) - a^3 \Im(\text{Ci}(-bx - a)) + 2 a^3 \text{Si}(bx + a)}{6 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x²*Si(b*x+a),x, algorithm="giac")

[Out] 1/3*x³*sin_integral(b*x + a) + 1/6*(a³*imag_part(cos_integral(b*x + a)) - a³*imag_part(cos_integral(-b*x - a)) + 2*a³*sin_integral(b*x + a))/b³

3.20 $\int x \text{Si}(a + bx) dx$

Optimal. Leaf size=71

$$-\frac{a^2 \text{Si}(a + bx)}{2b^2} - \frac{\sin(a + bx)}{2b^2} - \frac{a \cos(a + bx)}{2b^2} + \frac{1}{2} x^2 \text{Si}(a + bx) + \frac{x \cos(a + bx)}{2b}$$

[Out] $-(a \cdot \text{Cos}[a + b \cdot x]) / (2 \cdot b^2) + (x \cdot \text{Cos}[a + b \cdot x]) / (2 \cdot b) - \text{Sin}[a + b \cdot x] / (2 \cdot b^2) - (a^2 \cdot \text{SinIntegral}[a + b \cdot x]) / (2 \cdot b^2) + (x^2 \cdot \text{SinIntegral}[a + b \cdot x]) / 2$

Rubi [A] time = 0.206409, antiderivative size = 71, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 6, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.75$, Rules used = {6503, 6742, 2638, 3296, 2637, 3299}

$$-\frac{a^2 \text{Si}(a + bx)}{2b^2} - \frac{\sin(a + bx)}{2b^2} - \frac{a \cos(a + bx)}{2b^2} + \frac{1}{2} x^2 \text{Si}(a + bx) + \frac{x \cos(a + bx)}{2b}$$

Antiderivative was successfully verified.

[In] Int[x*SinIntegral[a + b*x],x]

[Out] $-(a \cdot \text{Cos}[a + b \cdot x]) / (2 \cdot b^2) + (x \cdot \text{Cos}[a + b \cdot x]) / (2 \cdot b) - \text{Sin}[a + b \cdot x] / (2 \cdot b^2) - (a^2 \cdot \text{SinIntegral}[a + b \cdot x]) / (2 \cdot b^2) + (x^2 \cdot \text{SinIntegral}[a + b \cdot x]) / 2$

Rule 6503

Int[((c_.) + (d_.)*(x_))^(m_.)*SinIntegral[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[((c + d*x)^(m + 1)*SinIntegral[a + b*x]) / (d*(m + 1)), x] - Dist[b / (d*(m + 1)), Int[((c + d*x)^(m + 1)*Sin[a + b*x]) / (a + b*x), x], x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]

Rule 6742

Int[u_, x_Symbol] :> With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]]

Rule 2638

Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] :> -Simp[Cos[c + d*x] / d, x] /; FreeQ[{c, d}, x]

Rule 3296

Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)], x_Symbol] :> -Simp[((c + d*x)^m * Cos[e + f*x]) / f, x] + Dist[(d*m) / f, Int[(c + d*x)^(m - 1) * Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && GtQ[m, 0]

Rule 2637

Int[sin[Pi/2 + (c_.) + (d_.)*(x_)], x_Symbol] :> Simp[Sin[c + d*x] / d, x] /; FreeQ[{c, d}, x]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_) / ((c_.) + (d_.)*(x_))], x_Symbol] :> Simp[SinIntegral[e + f*x] / d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned}
\int x\text{Si}(a+bx) dx &= \frac{1}{2}x^2\text{Si}(a+bx) - \frac{1}{2}b \int \frac{x^2 \sin(a+bx)}{a+bx} dx \\
&= \frac{1}{2}x^2\text{Si}(a+bx) - \frac{1}{2}b \int \left(-\frac{a \sin(a+bx)}{b^2} + \frac{x \sin(a+bx)}{b} + \frac{a^2 \sin(a+bx)}{b^2(a+bx)} \right) dx \\
&= \frac{1}{2}x^2\text{Si}(a+bx) - \frac{1}{2} \int x \sin(a+bx) dx + \frac{a \int \sin(a+bx) dx}{2b} - \frac{a^2 \int \frac{\sin(a+bx)}{a+bx} dx}{2b} \\
&= -\frac{a \cos(a+bx)}{2b^2} + \frac{x \cos(a+bx)}{2b} - \frac{a^2\text{Si}(a+bx)}{2b^2} + \frac{1}{2}x^2\text{Si}(a+bx) - \frac{\int \cos(a+bx) dx}{2b} \\
&= -\frac{a \cos(a+bx)}{2b^2} + \frac{x \cos(a+bx)}{2b} - \frac{\sin(a+bx)}{2b^2} - \frac{a^2\text{Si}(a+bx)}{2b^2} + \frac{1}{2}x^2\text{Si}(a+bx)
\end{aligned}$$

Mathematica [A] time = 0.0998636, size = 50, normalized size = 0.7

$$\frac{(b^2x^2 - a^2) \text{Si}(a+bx) - \sin(a+bx) + (bx-a) \cos(a+bx)}{2b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*SinIntegral[a + b*x], x]

[Out] ((-a + b*x)*Cos[a + b*x] - Sin[a + b*x] + (-a^2 + b^2*x^2)*SinIntegral[a + b*x])/(2*b^2)

Maple [A] time = 0.051, size = 61, normalized size = 0.9

$$\frac{1}{b^2} \left(\text{Si}(bx+a) \left(\frac{(bx+a)^2}{2} - a(bx+a) \right) + \frac{(bx+a) \cos(bx+a)}{2} - \frac{\sin(bx+a)}{2} - a \cos(bx+a) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*Si(b*x+a), x)

[Out] 1/b^2*(Si(b*x+a)*(1/2*(b*x+a)^2-a*(b*x+a))+1/2*(b*x+a)*cos(b*x+a)-1/2*sin(b*x+a)-a*cos(b*x+a))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x\text{Si}(bx+a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(b*x+a), x, algorithm="maxima")

[Out] integrate(x*Si(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x \text{Si}(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(b*x+a),x, algorithm="fricas")

[Out] integral(x*sin_integral(b*x + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \text{Si}(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(b*x+a),x)

[Out] Integral(x*Si(a + b*x), x)

Giac [C] time = 1.26429, size = 74, normalized size = 1.04

$$\frac{1}{2} x^2 \text{Si}(bx + a) - \frac{a^2 \Im(\text{Ci}(bx + a)) - a^2 \Im(\text{Ci}(-bx - a)) + 2 a^2 \text{Si}(bx + a)}{4 b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(b*x+a),x, algorithm="giac")

[Out] 1/2*x^2*sin_integral(b*x + a) - 1/4*(a^2*imag_part(cos_integral(b*x + a)) - a^2*imag_part(cos_integral(-b*x - a)) + 2*a^2*sin_integral(b*x + a))/b^2

3.21 $\int \text{Si}(a + bx) dx$

Optimal. Leaf size=26

$$\frac{(a + bx)\text{Si}(a + bx)}{b} + \frac{\cos(a + bx)}{b}$$

[Out] Cos[a + b*x]/b + ((a + b*x)*SinIntegral[a + b*x])/b

Rubi [A] time = 0.0054842, antiderivative size = 26, normalized size of antiderivative = 1., number of steps used = 1, number of rules used = 1, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.167$, Rules used = {6499}

$$\frac{(a + bx)\text{Si}(a + bx)}{b} + \frac{\cos(a + bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[SinIntegral[a + b*x], x]

[Out] Cos[a + b*x]/b + ((a + b*x)*SinIntegral[a + b*x])/b

Rule 6499

Int[SinIntegral[(a_.) + (b_.)*(x_.)], x_Symbol] := Simp[((a + b*x)*SinIntegral[a + b*x])/b, x] + Simp[Cos[a + b*x]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\int \text{Si}(a + bx) dx = \frac{\cos(a + bx)}{b} + \frac{(a + bx)\text{Si}(a + bx)}{b}$$

Mathematica [A] time = 0.0359392, size = 41, normalized size = 1.58

$$x\text{Si}(a + bx) + \frac{a\text{Si}(a + bx)}{b} - \frac{\sin(a)\sin(bx)}{b} + \frac{\cos(a)\cos(bx)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[SinIntegral[a + b*x], x]

[Out] (Cos[a]*Cos[b*x])/b - (Sin[a]*Sin[b*x])/b + (a*SineIntegral[a + b*x])/b + x*SineIntegral[a + b*x]

Maple [A] time = 0.049, size = 24, normalized size = 0.9

$$\frac{(bx + a)\text{Si}(bx + a) + \cos(bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x+a), x)

[Out] $1/b*((b*x+a)*\text{Si}(b*x+a)+\cos(b*x+a))$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Si}(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x+a),x, algorithm="maxima")`

[Out] `integrate(Si(b*x + a), x)`

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(\text{Si}(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x+a),x, algorithm="fricas")`

[Out] `integral(sin_integral(b*x + a), x)`

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Si}(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x+a),x)`

[Out] `Integral(Si(a + b*x), x)`

Giac [C] time = 1.34509, size = 62, normalized size = 2.38

$$x \text{Si}(bx + a) + \frac{a \Im(\text{Ci}(bx + a)) - a \Im(\text{Ci}(-bx - a)) + 2a \text{Si}(bx + a)}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x+a),x, algorithm="giac")`

[Out] `x*sin_integral(b*x + a) + 1/2*(a*imag_part(cos_integral(b*x + a)) - a*imag_part(cos_integral(-b*x - a)) + 2*a*sin_integral(b*x + a))/b`

$$3.22 \quad \int \frac{\text{Si}(a+bx)}{x} dx$$

Optimal. Leaf size=12

$$\text{CannotIntegrate}\left(\frac{\text{Si}(a+bx)}{x}, x\right)$$

[Out] CannotIntegrate[SinIntegral[a + b*x]/x, x]

Rubi [A] time = 0.0235792, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{Si}(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Int[SinIntegral[a + b*x]/x, x]

[Out] Defer[Int][SinIntegral[a + b*x]/x, x]

Rubi steps

$$\int \frac{\text{Si}(a+bx)}{x} dx = \int \frac{\text{Si}(a+bx)}{x} dx$$

Mathematica [A] time = 0.654852, size = 0, normalized size = 0.

$$\int \frac{\text{Si}(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[SinIntegral[a + b*x]/x, x]

[Out] Integrate[SinIntegral[a + b*x]/x, x]

Maple [A] time = 0.061, size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx+a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x+a)/x, x)

[Out] int(Si(b*x+a)/x, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)/x,x, algorithm="maxima")

[Out] integrate(Si(b*x + a)/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Si}(bx + a)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)/x,x, algorithm="fricas")

[Out] integral(sin_integral(b*x + a)/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(a + bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)/x,x)

[Out] Integral(Si(a + b*x)/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)/x,x, algorithm="giac")

[Out] integrate(Si(b*x + a)/x, x)

3.23 $\int \frac{\text{Si}(a+bx)}{x^2} dx$

Optimal. Leaf size=46

$$\frac{b \sin(a) \text{CosIntegral}(bx)}{a} - \frac{b \text{Si}(a+bx)}{a} - \frac{\text{Si}(a+bx)}{x} + \frac{b \cos(a) \text{Si}(bx)}{a}$$

[Out] (b*CosIntegral[b*x]*Sin[a])/a + (b*Cos[a]*SinIntegral[b*x])/a - (b*SIntegral[a + b*x])/a - SinIntegral[a + b*x]/x

Rubi [A] time = 0.232405, antiderivative size = 46, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {6503, 6742, 3303, 3299, 3302}

$$\frac{b \sin(a) \text{CosIntegral}(bx)}{a} - \frac{b \text{Si}(a+bx)}{a} - \frac{\text{Si}(a+bx)}{x} + \frac{b \cos(a) \text{Si}(bx)}{a}$$

Antiderivative was successfully verified.

[In] Int[SinIntegral[a + b*x]/x^2,x]

[Out] (b*CosIntegral[b*x]*Sin[a])/a + (b*Cos[a]*SinIntegral[b*x])/a - (b*SIntegral[a + b*x])/a - SinIntegral[a + b*x]/x

Rule 6503

```
Int[((c_.) + (d_.)*(x_))^(m_.)*SinIntegral[(a_.) + (b_.)*(x_)], x_Symbol] :
> Simp[((c + d*x)^(m + 1)*SinIntegral[a + b*x])/(d*(m + 1)), x] - Dist[b/(d
*(m + 1)), Int[((c + d*x)^(m + 1)*Sin[a + b*x])/(a + b*x), x], x] /; FreeQ[
{a, b, c, d, m}, x] && NeQ[m, -1]
```

Rule 6742

```
Int[u_, x_Symbol] :=> With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]
]
```

Rule 3303

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :=> Dist[Cos[(d*
e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f
)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] &&
NeQ[d*e - c*f, 0]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :=> Simp[SinInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :=> Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{\text{Si}(a+bx)}{x^2} dx &= -\frac{\text{Si}(a+bx)}{x} + b \int \frac{\sin(a+bx)}{x(a+bx)} dx \\
&= -\frac{\text{Si}(a+bx)}{x} + b \int \left(\frac{\sin(a+bx)}{ax} - \frac{b \sin(a+bx)}{a(a+bx)} \right) dx \\
&= -\frac{\text{Si}(a+bx)}{x} + \frac{b \int \frac{\sin(a+bx)}{x} dx}{a} - \frac{b^2 \int \frac{\sin(a+bx)}{a+bx} dx}{a} \\
&= -\frac{b \text{Si}(a+bx)}{a} - \frac{\text{Si}(a+bx)}{x} + \frac{(b \cos(a)) \int \frac{\sin(bx)}{x} dx}{a} + \frac{(b \sin(a)) \int \frac{\cos(bx)}{x} dx}{a} \\
&= \frac{b \text{Ci}(bx) \sin(a)}{a} + \frac{b \cos(a) \text{Si}(bx)}{a} - \frac{b \text{Si}(a+bx)}{a} - \frac{\text{Si}(a+bx)}{x}
\end{aligned}$$

Mathematica [A] time = 0.0732792, size = 39, normalized size = 0.85

$$\frac{bx \sin(a) \text{CosIntegral}(bx) - (a+bx) \text{Si}(a+bx) + bx \cos(a) \text{Si}(bx)}{ax}$$

Antiderivative was successfully verified.

[In] Integrate[SinIntegral[a + b*x]/x^2,x]

[Out] (b*x*CosIntegral[b*x]*Sin[a] + b*x*Cos[a]*SinIntegral[b*x] - (a + b*x)*SinIntegral[a + b*x])/(a*x)

Maple [A] time = 0.057, size = 48, normalized size = 1.

$$b \left(-\frac{\text{Si}(bx+a)}{bx} - \frac{\text{Si}(bx+a)}{a} + \frac{\text{Si}(bx) \cos(a) + \text{Ci}(bx) \sin(a)}{a} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x+a)/x^2,x)

[Out] b*(-Si(b*x+a)/b/x-1/a*Si(b*x+a)+1/a*(Si(b*x)*cos(a)+Ci(b*x)*sin(a)))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx+a)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)/x^2,x, algorithm="maxima")

[Out] integrate(Si(b*x + a)/x^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Si}(bx+a)}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)/x^2,x, algorithm="fricas")

[Out] integral(sin_integral(b*x + a)/x^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(a + bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)/x**2,x)

[Out] Integral(Si(a + b*x)/x**2, x)

Giac [C] time = 1.31766, size = 244, normalized size = 5.3

$$\left(\Im(\text{Ci}(bx + a)) \tan\left(\frac{1}{2}a\right)^2 + \Im(\text{Ci}(bx)) \tan\left(\frac{1}{2}a\right)^2 - \Im(\text{Ci}(-bx - a)) \tan\left(\frac{1}{2}a\right)^2 - \Im(\text{Ci}(-bx)) \tan\left(\frac{1}{2}a\right)^2 + 2 \text{Si}(bx + a) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)/x^2,x, algorithm="giac")

[Out] -1/2*(imag_part(cos_integral(b*x + a))*tan(1/2*a)^2 + imag_part(cos_integral(b*x))*tan(1/2*a)^2 - imag_part(cos_integral(-b*x - a))*tan(1/2*a)^2 - imag_part(cos_integral(-b*x))*tan(1/2*a)^2 + 2*sin_integral(b*x + a)*tan(1/2*a)^2 + 2*sin_integral(b*x)*tan(1/2*a)^2 - 2*real_part(cos_integral(b*x))*tan(1/2*a) - 2*real_part(cos_integral(-b*x))*tan(1/2*a) + imag_part(cos_integral(b*x + a)) - imag_part(cos_integral(b*x)) - imag_part(cos_integral(-b*x - a)) + imag_part(cos_integral(-b*x)) + 2*sin_integral(b*x + a) - 2*sin_integral(b*x))*b/(a*tan(1/2*a)^2 + a) - sin_integral(b*x + a)/x

3.24 $\int \frac{\text{Si}(a+bx)}{x^3} dx$

Optimal. Leaf size=111

$$-\frac{b^2 \sin(a) \text{CosIntegral}(bx)}{2a^2} + \frac{b^2 \text{Si}(a+bx)}{2a^2} - \frac{b^2 \cos(a) \text{Si}(bx)}{2a^2} + \frac{b^2 \cos(a) \text{CosIntegral}(bx)}{2a} - \frac{b^2 \sin(a) \text{Si}(bx)}{2a} - \frac{\text{Si}(a)}{2}$$

[Out] (b^2*cos[a]*CosIntegral[b*x])/(2*a) - (b^2*cosIntegral[b*x]*Sin[a])/(2*a^2) - (b*SIN[a + b*x])/(2*a*x) - (b^2*cos[a]*SinIntegral[b*x])/(2*a^2) - (b^2*SIN[a]*SinIntegral[b*x])/(2*a) + (b^2*SINIntegral[a + b*x])/(2*a^2) - SinIntegral[a + b*x]/(2*x^2)

Rubi [A] time = 0.325046, antiderivative size = 111, normalized size of antiderivative = 1., number of steps used = 11, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.6$, Rules used = {6503, 6742, 3297, 3303, 3299, 3302}

$$-\frac{b^2 \sin(a) \text{CosIntegral}(bx)}{2a^2} + \frac{b^2 \text{Si}(a+bx)}{2a^2} - \frac{b^2 \cos(a) \text{Si}(bx)}{2a^2} + \frac{b^2 \cos(a) \text{CosIntegral}(bx)}{2a} - \frac{b^2 \sin(a) \text{Si}(bx)}{2a} - \frac{\text{Si}(a)}{2}$$

Antiderivative was successfully verified.

[In] Int[SINIntegral[a + b*x]/x^3,x]

[Out] (b^2*cos[a]*CosIntegral[b*x])/(2*a) - (b^2*cosIntegral[b*x]*Sin[a])/(2*a^2) - (b*SIN[a + b*x])/(2*a*x) - (b^2*cos[a]*SinIntegral[b*x])/(2*a^2) - (b^2*SIN[a]*SinIntegral[b*x])/(2*a) + (b^2*SINIntegral[a + b*x])/(2*a^2) - SinIntegral[a + b*x]/(2*x^2)

Rule 6503

Int[((c_.) + (d_.)*(x_))^(m_.)*SinIntegral[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[((c + d*x)^(m + 1)*SinIntegral[a + b*x])/(d*(m + 1)), x] - Dist[b/(d*(m + 1)), Int[((c + d*x)^(m + 1)*Sin[a + b*x])/(a + b*x), x], x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]

Rule 6742

Int[u_, x_Symbol] :> With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]]

Rule 3297

Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)], x_Symbol] :> Simp[((c + d*x)^(m + 1)*Sin[e + f*x])/(d*(m + 1)), x] - Dist[f/(d*(m + 1)), Int[(c + d*x)^(m + 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && LtQ[m, -1]

Rule 3303

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Dist[Cos[(d*e - c*f)/d], Int[SIN[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[SIN[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rubi steps

$$\begin{aligned}
 \int \frac{\text{Si}(a+bx)}{x^3} dx &= -\frac{\text{Si}(a+bx)}{2x^2} + \frac{1}{2}b \int \frac{\sin(a+bx)}{x^2(a+bx)} dx \\
 &= -\frac{\text{Si}(a+bx)}{2x^2} + \frac{1}{2}b \int \left(\frac{\sin(a+bx)}{ax^2} - \frac{b \sin(a+bx)}{a^2x} + \frac{b^2 \sin(a+bx)}{a^2(a+bx)} \right) dx \\
 &= -\frac{\text{Si}(a+bx)}{2x^2} + \frac{b \int \frac{\sin(a+bx)}{x^2} dx}{2a} - \frac{b^2 \int \frac{\sin(a+bx)}{x} dx}{2a^2} + \frac{b^3 \int \frac{\sin(a+bx)}{a+bx} dx}{2a^2} \\
 &= -\frac{b \sin(a+bx)}{2ax} + \frac{b^2 \text{Si}(a+bx)}{2a^2} - \frac{\text{Si}(a+bx)}{2x^2} + \frac{b^2 \int \frac{\cos(a+bx)}{x} dx}{2a} - \frac{(b^2 \cos(a)) \int \frac{\sin(bx)}{x} dx}{2a^2} - \frac{(b^2 \sin(a)) \int \frac{\cos(bx)}{x} dx}{2a^2} \\
 &= -\frac{b^2 \text{Ci}(bx) \sin(a)}{2a^2} - \frac{b \sin(a+bx)}{2ax} - \frac{b^2 \cos(a) \text{Si}(bx)}{2a^2} + \frac{b^2 \text{Si}(a+bx)}{2a^2} - \frac{\text{Si}(a+bx)}{2x^2} + \frac{(b^2 \cos(a)) \int \frac{\cos(bx)}{x} dx}{2a} \\
 &= \frac{b^2 \cos(a) \text{Ci}(bx)}{2a} - \frac{b^2 \text{Ci}(bx) \sin(a)}{2a^2} - \frac{b \sin(a+bx)}{2ax} - \frac{b^2 \cos(a) \text{Si}(bx)}{2a^2} - \frac{b^2 \sin(a) \text{Si}(bx)}{2a} + \frac{b^2 \text{Si}(a+bx)}{2a^2}
 \end{aligned}$$

Mathematica [A] time = 0.331378, size = 84, normalized size = 0.76

$$\frac{a^2 \text{Si}(a+bx) - b^2 x^2 (a \cos(a) - \sin(a)) \text{CosIntegral}(bx) - b^2 x^2 \text{Si}(a+bx) + b^2 x^2 (a \sin(a) + \cos(a)) \text{Si}(bx) + abx \sin(a) + b^2 \text{Si}(a+bx)}{2a^2 x^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[SinIntegral[a + b*x]/x^3, x]
```

```
[Out] -(-(b^2*x^2*CosIntegral[b*x]*(a*Cos[a] - Sin[a])) + a*b*x*Sin[a + b*x] + b^2*x^2*(Cos[a] + a*Sin[a])*SinIntegral[b*x] + a^2*SinIntegral[a + b*x] - b^2*x^2*SinIntegral[a + b*x])/(2*a^2*x^2)
```

Maple [A] time = 0.06, size = 86, normalized size = 0.8

$$b^2 \left(-\frac{\text{Si}(bx+a)}{2b^2x^2} + \frac{\text{Si}(bx+a)}{2a^2} + \frac{1}{2a} \left(-\frac{\sin(bx+a)}{bx} - \text{Si}(bx) \sin(a) + \text{Ci}(bx) \cos(a) \right) - \frac{\text{Si}(bx) \cos(a) + \text{Ci}(bx) \sin(a)}{2a^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(Si(b*x+a)/x^3, x)
```

```
[Out] b^2*(-1/2*Si(b*x+a)/b^2/x^2+1/2/a^2*Si(b*x+a)+1/2/a*(-sin(b*x+a)/b/x-Si(b*x)*sin(a)+Ci(b*x)*cos(a))-1/2/a^2*(Si(b*x)*cos(a)+Ci(b*x)*sin(a))
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx + a)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)/x^3,x, algorithm="maxima")

[Out] integrate(Si(b*x + a)/x^3, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Si}(bx + a)}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)/x^3,x, algorithm="fricas")

[Out] integral(sin_integral(b*x + a)/x^3, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(a + bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)/x**3,x)

[Out] Integral(Si(a + b*x)/x**3, x)

Giac [C] time = 1.33659, size = 1092, normalized size = 9.84

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)/x^3,x, algorithm="giac")

[Out]
$$\begin{aligned} & -1/4*(a*b*x*\text{real_part}(\text{cos_integral}(b*x))*\tan(1/2*b*x)^2*\tan(1/2*a)^2 + a*b*x*\text{real_part}(\text{cos_integral}(-b*x))*\tan(1/2*b*x)^2*\tan(1/2*a)^2 + 2*a*b*x*\text{imag_part}(\text{cos_integral}(b*x))*\tan(1/2*b*x)^2*\tan(1/2*a) - 2*a*b*x*\text{imag_part}(\text{cos_integral}(-b*x))*\tan(1/2*b*x)^2*\tan(1/2*a) + 4*a*b*x*\text{sin_integral}(b*x)*\tan(1/2*b*x)^2*\tan(1/2*a) - b*x*\text{imag_part}(\text{cos_integral}(b*x + a))*\tan(1/2*b*x)^2*\tan(1/2*a)^2 - b*x*\text{imag_part}(\text{cos_integral}(b*x))*\tan(1/2*b*x)^2*\tan(1/2*a)^2 + b*x*\text{imag_part}(\text{cos_integral}(-b*x - a))*\tan(1/2*b*x)^2*\tan(1/2*a)^2 + b*x*\text{imag_part}(\text{cos_integral}(-b*x))*\tan(1/2*b*x)^2*\tan(1/2*a)^2 - 2*b*x*\text{sin_integral}(b*x + a)*\tan(1/2*b*x)^2*\tan(1/2*a)^2 - 2*b*x*\text{sin_integral}(b*x)*\tan(1/2*b*x)^2*\tan(1/2*a)^2 - a*b*x*\text{real_part}(\text{cos_integral}(b*x))*\tan(1/2*b*x)^2 - a*b*x*\text{real_part}(\text{cos_integral}(-b*x))*\tan(1/2*b*x)^2 + 2*b*x*\text{real_part}(\text{cos_inte} \end{aligned}$$

```

gral(b*x))*tan(1/2*b*x)^2*tan(1/2*a) + 2*b*x*real_part(cos_integral(-b*x))*
tan(1/2*b*x)^2*tan(1/2*a) + a*b*x*real_part(cos_integral(b*x))*tan(1/2*a)^2
+ a*b*x*real_part(cos_integral(-b*x))*tan(1/2*a)^2 - b*x*imag_part(cos_int
egral(b*x + a))*tan(1/2*b*x)^2 + b*x*imag_part(cos_integral(b*x))*tan(1/2*b
*x)^2 + b*x*imag_part(cos_integral(-b*x - a))*tan(1/2*b*x)^2 - b*x*imag_par
t(cos_integral(-b*x))*tan(1/2*b*x)^2 - 2*b*x*sin_integral(b*x + a)*tan(1/2*
b*x)^2 + 2*b*x*sin_integral(b*x)*tan(1/2*b*x)^2 + 2*a*b*x*imag_part(cos_int
egral(b*x))*tan(1/2*a) - 2*a*b*x*imag_part(cos_integral(-b*x))*tan(1/2*a) +
4*a*b*x*sin_integral(b*x)*tan(1/2*a) - b*x*imag_part(cos_integral(b*x + a)
)*tan(1/2*a)^2 - b*x*imag_part(cos_integral(b*x))*tan(1/2*a)^2 + b*x*imag_p
art(cos_integral(-b*x - a))*tan(1/2*a)^2 + b*x*imag_part(cos_integral(-b*x)
)*tan(1/2*a)^2 - 2*b*x*sin_integral(b*x + a)*tan(1/2*a)^2 - 2*b*x*sin_integ
ral(b*x)*tan(1/2*a)^2 - a*b*x*real_part(cos_integral(b*x)) - a*b*x*real_par
t(cos_integral(-b*x)) + 2*b*x*real_part(cos_integral(b*x))*tan(1/2*a) + 2*b
*x*real_part(cos_integral(-b*x))*tan(1/2*a) - 4*a*tan(1/2*b*x)^2*tan(1/2*a)
- 4*a*tan(1/2*b*x)*tan(1/2*a)^2 - b*x*imag_part(cos_integral(b*x + a)) + b
*x*imag_part(cos_integral(b*x)) + b*x*imag_part(cos_integral(-b*x - a)) - b
*x*imag_part(cos_integral(-b*x)) - 2*b*x*sin_integral(b*x + a) + 2*b*x*sin_
integral(b*x) + 4*a*tan(1/2*b*x) + 4*a*tan(1/2*a))*b/(a^2*x*tan(1/2*b*x)^2*
tan(1/2*a)^2 + a^2*x*tan(1/2*b*x)^2 + a^2*x*tan(1/2*a)^2 + a^2*x) - 1/2*sin
_integral(b*x + a)/x^2

```


3.25 $\int x^m \mathbf{Si}(a + bx)^2 dx$

Optimal. Leaf size=14

$$\text{CannotIntegrate}(x^m \text{Si}(a + bx)^2, x)$$

[Out] CannotIntegrate[x^m*SinIntegral[a + b*x]^2, x]

Rubi [A] time = 0.0437283, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int x^m \text{Si}(a + bx)^2 dx$$

Verification is Not applicable to the result.

[In] Int[x^m*SinIntegral[a + b*x]^2,x]

[Out] Defer[Int][x^m*SinIntegral[a + b*x]^2, x]

Rubi steps

$$\int x^m \text{Si}(a + bx)^2 dx = \int x^m \text{Si}(a + bx)^2 dx$$

Mathematica [A] time = 5.25018, size = 0, normalized size = 0.

$$\int x^m \text{Si}(a + bx)^2 dx$$

Verification is Not applicable to the result.

[In] Integrate[x^m*SinIntegral[a + b*x]^2,x]

[Out] Integrate[x^m*SinIntegral[a + b*x]^2, x]

Maple [A] time = 0.148, size = 0, normalized size = 0.

$$\int x^m (\text{Si}(bx + a))^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*Si(b*x+a)^2,x)

[Out] int(x^m*Si(b*x+a)^2,x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \text{Si}(bx + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Si(b*x+a)²,x, algorithm="maxima")

[Out] integrate(x^m*Si(b*x + a)², x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^m \text{Si}(bx + a)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Si(b*x+a)²,x, algorithm="fricas")

[Out] integral(x^m*sin_integral(b*x + a)², x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \text{Si}^2(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m*Si(b*x+a)**2,x)

[Out] Integral(x**m*Si(a + b*x)**2, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \text{Si}(bx + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Si(b*x+a)²,x, algorithm="giac")

[Out] integrate(x^m*Si(b*x + a)², x)

3.26 $\int x^2 \text{Si}(a + bx)^2 dx$

Optimal. Leaf size=329

$$\frac{a^2(a + bx)\text{Si}(a + bx)^2}{3b^3} - \frac{a^2\text{Si}(2a + 2bx)}{b^3} + \frac{2a^2\text{Si}(a + bx)\cos(a + bx)}{3b^3} + \frac{a\text{CosIntegral}(2a + 2bx)}{b^3} - \frac{ax(a + bx)\text{Si}(a + bx)}{3b^2}$$

```
[Out] (2*x)/(3*b^2) - (a*cos[2*a + 2*b*x])/(3*b^3) + (x*cos[2*a + 2*b*x])/(6*b^2)
+ (a*cosIntegral[2*a + 2*b*x])/b^3 - (a*log[a + b*x])/b^3 - (2*cos[a + b*x]
)*sin[a + b*x])/(3*b^3) - sin[2*a + 2*b*x]/(12*b^3) - (4*cos[a + b*x]*sinIn
tegral[a + b*x])/(3*b^3) + (2*a^2*cos[a + b*x]*sinIntegral[a + b*x])/(3*b^3
) - (2*a*x*cos[a + b*x]*sinIntegral[a + b*x])/(3*b^2) + (2*x^2*cos[a + b*x]
*sinIntegral[a + b*x])/(3*b) + (2*a*sin[a + b*x]*sinIntegral[a + b*x])/(3*b
^3) - (4*x*sin[a + b*x]*sinIntegral[a + b*x])/(3*b^2) + (a^2*(a + b*x)*sinI
ntegral[a + b*x]^2)/(3*b^3) - (a*x*(a + b*x)*sinIntegral[a + b*x]^2)/(3*b^2
) + (x^2*(a + b*x)*sinIntegral[a + b*x]^2)/(3*b) + (2*sinIntegral[2*a + 2*b
*x])/(3*b^3) - (a^2*sinIntegral[2*a + 2*b*x])/b^3
```

Rubi [A] time = 1.49501, antiderivative size = 329, normalized size of antiderivative = 1., number of steps used = 39, number of rules used = 19, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 1.583$, Rules used = {6509, 6513, 4573, 6741, 6742, 2638, 3296, 2637, 3299, 6519, 2635, 8, 3312, 3302, 6511, 4406, 12, 6517, 6505}

$$\frac{a^2(a + bx)\text{Si}(a + bx)^2}{3b^3} - \frac{a^2\text{Si}(2a + 2bx)}{b^3} + \frac{2a^2\text{Si}(a + bx)\cos(a + bx)}{3b^3} + \frac{a\text{CosIntegral}(2a + 2bx)}{b^3} - \frac{ax(a + bx)\text{Si}(a + bx)}{3b^2}$$

Antiderivative was successfully verified.

```
[In] Int[x^2*SinIntegral[a + b*x]^2,x]
```

```
[Out] (2*x)/(3*b^2) - (a*cos[2*a + 2*b*x])/(3*b^3) + (x*cos[2*a + 2*b*x])/(6*b^2)
+ (a*cosIntegral[2*a + 2*b*x])/b^3 - (a*log[a + b*x])/b^3 - (2*cos[a + b*x]
)*sin[a + b*x])/(3*b^3) - sin[2*a + 2*b*x]/(12*b^3) - (4*cos[a + b*x]*sinIn
tegral[a + b*x])/(3*b^3) + (2*a^2*cos[a + b*x]*sinIntegral[a + b*x])/(3*b^3
) - (2*a*x*cos[a + b*x]*sinIntegral[a + b*x])/(3*b^2) + (2*x^2*cos[a + b*x]
*sinIntegral[a + b*x])/(3*b) + (2*a*sin[a + b*x]*sinIntegral[a + b*x])/(3*b
^3) - (4*x*sin[a + b*x]*sinIntegral[a + b*x])/(3*b^2) + (a^2*(a + b*x)*sinI
ntegral[a + b*x]^2)/(3*b^3) - (a*x*(a + b*x)*sinIntegral[a + b*x]^2)/(3*b^2
) + (x^2*(a + b*x)*sinIntegral[a + b*x]^2)/(3*b) + (2*sinIntegral[2*a + 2*b
*x])/(3*b^3) - (a^2*sinIntegral[2*a + 2*b*x])/b^3
```

Rule 6509

```
Int[((c_.) + (d_.)*(x_))^(m_.)*SinIntegral[(a_.) + (b_.)*(x_)]^2, x_Symbol]
:> Simp[((a + b*x)*(c + d*x)^m*sinIntegral[a + b*x]^2)/(b*(m + 1)), x] + (-
Dist[2/(m + 1), Int[(c + d*x)^m*sin[a + b*x]*sinIntegral[a + b*x], x], x] +
Dist[((b*c - a*d)*m)/(b*(m + 1)), Int[(c + d*x)^(m - 1)*sinIntegral[a + b*
x]^2, x], x]) /; FreeQ[{a, b, c, d}, x] && IGtQ[m, 0]
```

Rule 6513

```
Int[((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) +
(d_.)*(x_)], x_Symbol] :> -Simp[((e + f*x)^m*cos[a + b*x]*sinIntegral[c + d
*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*cos[a + b*x]*sin[c + d*x])/(c + d*
x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*cos[a + b*x]*sinIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 4573

$\text{Int}[\text{Cos}[w_]^{(p_)} * (u_) * \text{Sin}[v_]^{(p_)}, x_ \text{Symbol}] \text{ :> } \text{Dist}[1/2^p, \text{Int}[u * \text{Sin}[2 * v]^{(p)}, x], x] \text{ /; } \text{EqQ}[w, v] \ \&\& \ \text{IntegerQ}[p]$

Rule 6741

$\text{Int}[u_ , x_ \text{Symbol}] \text{ :> } \text{With}[\{v = \text{NormalizeIntegrand}[u, x]\}, \text{Int}[v, x] \text{ /; } v \neq u]$

Rule 6742

$\text{Int}[u_ , x_ \text{Symbol}] \text{ :> } \text{With}[\{v = \text{ExpandIntegrand}[u, x]\}, \text{Int}[v, x] \text{ /; } \text{SumQ}[v]$
]

Rule 2638

$\text{Int}[\text{sin}[(c_) + (d_) * (x_)], x_ \text{Symbol}] \text{ :> } -\text{Simp}[\text{Cos}[c + d * x] / d, x] \text{ /; } \text{FreeQ}[\{c, d\}, x]$

Rule 3296

$\text{Int}[((c_) + (d_) * (x_))^{(m_)} * \text{sin}[(e_) + (f_) * (x_)], x_ \text{Symbol}] \text{ :> } -\text{Simp}[(c + d * x)^m * \text{Cos}[e + f * x] / f, x] + \text{Dist}[(d * m) / f, \text{Int}[(c + d * x)^{(m - 1)} * \text{Cos}[e + f * x], x], x] \text{ /; } \text{FreeQ}[\{c, d, e, f\}, x] \ \&\& \ \text{GtQ}[m, 0]$

Rule 2637

$\text{Int}[\text{sin}[\text{Pi}/2 + (c_) + (d_) * (x_)], x_ \text{Symbol}] \text{ :> } \text{Simp}[\text{Sin}[c + d * x] / d, x] \text{ /; } \text{FreeQ}[\{c, d\}, x]$

Rule 3299

$\text{Int}[\text{sin}[(e_) + (f_) * (x_)] / ((c_) + (d_) * (x_)), x_ \text{Symbol}] \text{ :> } \text{Simp}[\text{SinIntegral}[e + f * x] / d, x] \text{ /; } \text{FreeQ}[\{c, d, e, f\}, x] \ \&\& \ \text{EqQ}[d * e - c * f, 0]$

Rule 6519

$\text{Int}[\text{Cos}[(a_) + (b_) * (x_)] * ((e_) + (f_) * (x_))^{(m_)} * \text{SinIntegral}[(c_) + (d_) * (x_)], x_ \text{Symbol}] \text{ :> } \text{Simp}[(e + f * x)^m * \text{Sin}[a + b * x] * \text{SinIntegral}[c + d * x] / b, x] + (-\text{Dist}[d / b, \text{Int}[(e + f * x)^m * \text{Sin}[a + b * x] * \text{Sin}[c + d * x] / (c + d * x), x], x] - \text{Dist}[(f * m) / b, \text{Int}[(e + f * x)^{(m - 1)} * \text{Sin}[a + b * x] * \text{SinIntegral}[c + d * x], x], x]) \text{ /; } \text{FreeQ}[\{a, b, c, d, e, f\}, x] \ \&\& \ \text{IGtQ}[m, 0]$

Rule 2635

$\text{Int}[((b_) * \text{sin}[(c_) + (d_) * (x_)])^{(n_)}, x_ \text{Symbol}] \text{ :> } -\text{Simp}[(b * \text{Cos}[c + d * x] * (b * \text{Sin}[c + d * x])^{(n - 1)}) / (d * n), x] + \text{Dist}[(b^2 * (n - 1)) / n, \text{Int}[(b * \text{Sin}[c + d * x])^{(n - 2)}, x], x] \text{ /; } \text{FreeQ}[\{b, c, d\}, x] \ \&\& \ \text{GtQ}[n, 1] \ \&\& \ \text{IntegerQ}[2 * n]$
]

Rule 8

$\text{Int}[a_ , x_ \text{Symbol}] \text{ :> } \text{Simp}[a * x, x] \text{ /; } \text{FreeQ}[a, x]$

Rule 3312

$\text{Int}[((c_) + (d_) * (x_))^{(m_)} * \text{sin}[(e_) + (f_) * (x_)]^{(n_)}, x_ \text{Symbol}] \text{ :> } \text{Int}[\text{ExpandTrigReduce}[(c + d * x)^m, \text{Sin}[e + f * x]^{(n)}, x], x] \text{ /; } \text{FreeQ}[\{c, d, e, f$

, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rule 6511

Int[Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := -Simp[(Cos[a + b*x]*SinIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 6517

Int[Cos[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := Simp[(Sin[a + b*x]*SinIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 6505

Int[SinIntegral[(a_.) + (b_.)*(x_)]^2, x_Symbol] := Simp[((a + b*x)*SinIntegral[a + b*x]^2)/b, x] - Dist[2, Int[Sin[a + b*x]*SinIntegral[a + b*x], x], x] /; FreeQ[{a, b}, x]

Rubi steps

$$\begin{aligned}
\int x^2 \text{Si}(a+bx)^2 dx &= \frac{x^2(a+bx)\text{Si}(a+bx)^2}{3b} - \frac{2}{3} \int x^2 \sin(a+bx)\text{Si}(a+bx) dx - \frac{(2a) \int x\text{Si}(a+bx)^2 dx}{3b} \\
&= \frac{2x^2 \cos(a+bx)\text{Si}(a+bx)}{3b} - \frac{ax(a+bx)\text{Si}(a+bx)^2}{3b^2} + \frac{x^2(a+bx)\text{Si}(a+bx)^2}{3b} - \frac{2}{3} \int \frac{x^2 \cos(a+bx)}{a+bx} dx \\
&= -\frac{2ax \cos(a+bx)\text{Si}(a+bx)}{3b^2} + \frac{2x^2 \cos(a+bx)\text{Si}(a+bx)}{3b} - \frac{4x \sin(a+bx)\text{Si}(a+bx)}{3b^2} + \frac{a^2(a+bx)\text{Si}(a+bx)}{3b} \\
&= -\frac{4 \cos(a+bx)\text{Si}(a+bx)}{3b^3} + \frac{2a^2 \cos(a+bx)\text{Si}(a+bx)}{3b^3} - \frac{2ax \cos(a+bx)\text{Si}(a+bx)}{3b^2} + \frac{2x^2 \cos(a+bx)}{3b} \\
&= -\frac{4 \cos(a+bx)\text{Si}(a+bx)}{3b^3} + \frac{2a^2 \cos(a+bx)\text{Si}(a+bx)}{3b^3} - \frac{2ax \cos(a+bx)\text{Si}(a+bx)}{3b^2} + \frac{2x^2 \cos(a+bx)}{3b} \\
&= -\frac{a \log(a+bx)}{3b^3} - \frac{2 \cos(a+bx) \sin(a+bx)}{3b^3} - \frac{4 \cos(a+bx)\text{Si}(a+bx)}{3b^3} + \frac{2a^2 \cos(a+bx)\text{Si}(a+bx)}{3b^3} \\
&= \frac{2x}{3b^2} - \frac{a \cos(2a+2bx)}{6b^3} + \frac{x \cos(2a+2bx)}{6b^2} + \frac{a\text{Ci}(2a+2bx)}{3b^3} - \frac{a \log(a+bx)}{b^3} - \frac{2 \cos(a+bx) \sin(a+bx)}{3b^3} \\
&= \frac{2x}{3b^2} - \frac{a \cos(2a+2bx)}{3b^3} + \frac{x \cos(2a+2bx)}{6b^2} + \frac{a\text{Ci}(2a+2bx)}{b^3} - \frac{a \log(a+bx)}{b^3} - \frac{2 \cos(a+bx) \sin(a+bx)}{3b^3}
\end{aligned}$$

Mathematica [A] time = 1.71065, size = 158, normalized size = 0.48

$$4(a^3 + b^3x^3) \text{Si}(a+bx)^2 + 8\text{Si}(a+bx) \left((a^2 - abx + b^2x^2 - 2) \cos(a+bx) + (a - 2bx) \sin(a+bx) \right) - 12a^2 \text{Si}(2(a+bx)) +$$

Antiderivative was successfully verified.

[In] Integrate[x^2*SinIntegral[a + b*x]^2,x]

[Out] (8*a + 8*b*x - 4*a*Cos[2*(a + b*x)] + 2*b*x*Cos[2*(a + b*x)] + 12*a*CosIntegral[2*(a + b*x)] - 12*a*Log[a + b*x] - 5*Sin[2*(a + b*x)] + 8*((-2 + a^2 - a*b*x + b^2*x^2)*Cos[a + b*x] + (a - 2*b*x)*Sin[a + b*x])*SinIntegral[a + b*x] + 4*(a^3 + b^3*x^3)*SinIntegral[a + b*x]^2 + 8*SinIntegral[2*(a + b*x)] - 12*a^2*SinIntegral[2*(a + b*x)])/(12*b^3)

Maple [F] time = 0.056, size = 0, normalized size = 0.

$$\int x^2 (\text{Si}(bx+a))^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*Si(b*x+a)^2,x)

[Out] int(x^2*Si(b*x+a)^2,x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Si}(bx+a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Si(b*x+a)^2,x, algorithm="maxima")

[Out] integrate(x^2*Si(b*x + a)^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^2 \text{Si}(bx + a)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Si(b*x+a)^2,x, algorithm="fricas")

[Out] integral(x^2*sin_integral(b*x + a)^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Si}^2(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*Si(b*x+a)**2,x)

[Out] Integral(x**2*Si(a + b*x)**2, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Si}(bx + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Si(b*x+a)^2,x, algorithm="giac")

[Out] integrate(x^2*Si(b*x+ a)^2, x)

3.27 $\int x \text{Si}(a + bx)^2 dx$

Optimal. Leaf size=154

$$-\frac{\text{CosIntegral}(2a + 2bx)}{2b^2} - \frac{a(a + bx)\text{Si}(a + bx)^2}{2b^2} + \frac{a\text{Si}(2a + 2bx)}{b^2} - \frac{\text{Si}(a + bx)\sin(a + bx)}{b^2} - \frac{a\text{Si}(a + bx)\cos(a + bx)}{b^2} +$$

```
[Out] Cos[2*a + 2*b*x]/(4*b^2) - CosIntegral[2*a + 2*b*x]/(2*b^2) + Log[a + b*x]/
(2*b^2) - (a*Cos[a + b*x]*SinIntegral[a + b*x])/b^2 + (x*Cos[a + b*x]*SinIn
tegral[a + b*x])/b - (Sin[a + b*x]*SinIntegral[a + b*x])/b^2 - (a*(a + b*x)
*SinIntegral[a + b*x]^2)/(2*b^2) + (x*(a + b*x)*SinIntegral[a + b*x]^2)/(2*
b) + (a*SinIntegral[2*a + 2*b*x])/b^2
```

Rubi [A] time = 0.333002, antiderivative size = 154, normalized size of antiderivative = 1., number of steps used = 17, number of rules used = 14, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}}$ = 1.4, Rules used = {6509, 6513, 4573, 6741, 6742, 2638, 3299, 6517, 3312, 3302, 6505, 6511, 4406, 12}

$$-\frac{\text{CosIntegral}(2a + 2bx)}{2b^2} - \frac{a(a + bx)\text{Si}(a + bx)^2}{2b^2} + \frac{a\text{Si}(2a + 2bx)}{b^2} - \frac{\text{Si}(a + bx)\sin(a + bx)}{b^2} - \frac{a\text{Si}(a + bx)\cos(a + bx)}{b^2} +$$

Antiderivative was successfully verified.

```
[In] Int[x*SinIntegral[a + b*x]^2,x]
```

```
[Out] Cos[2*a + 2*b*x]/(4*b^2) - CosIntegral[2*a + 2*b*x]/(2*b^2) + Log[a + b*x]/
(2*b^2) - (a*Cos[a + b*x]*SinIntegral[a + b*x])/b^2 + (x*Cos[a + b*x]*SinIn
tegral[a + b*x])/b - (Sin[a + b*x]*SinIntegral[a + b*x])/b^2 - (a*(a + b*x)
*SinIntegral[a + b*x]^2)/(2*b^2) + (x*(a + b*x)*SinIntegral[a + b*x]^2)/(2*
b) + (a*SinIntegral[2*a + 2*b*x])/b^2
```

Rule 6509

```
Int[((c_.) + (d_.)*(x_))^(m_.)*SinIntegral[(a_) + (b_.)*(x_)]^2, x_Symbol]
:> Simp[((a + b*x)*(c + d*x)^m*SinIntegral[a + b*x]^2)/(b*(m + 1)), x] + (-
Dist[2/(m + 1), Int[(c + d*x)^m*Sin[a + b*x]*SinIntegral[a + b*x], x], x] +
Dist[((b*c - a*d)*m)/(b*(m + 1)), Int[(c + d*x)^(m - 1)*SinIntegral[a + b*
x]^2, x], x]) /; FreeQ[{a, b, c, d}, x] && IGtQ[m, 0]
```

Rule 6513

```
Int[((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) +
(d_.)*(x_)], x_Symbol] :> -Simp[((e + f*x)^m*Cos[a + b*x]*SinIntegral[c + d
*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*Cos[a + b*x]*Sin[c + d*x])/(c + d*
x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Cos[a + b*x]*SinIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 4573

```
Int[Cos[w_]^(p_.)*(u_.)*Sin[v_]^(p_.), x_Symbol] :> Dist[1/2^p, Int[u*Sin[2
*v]^p, x], x] /; EqQ[w, v] && IntegerQ[p]
```

Rule 6741

```
Int[u_, x_Symbol] :> With[{v = NormalizeIntegrand[u, x]}, Int[v, x] /; v !=
= u]
```


Rule 6742

Int[u_, x_Symbol] :=> With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]
]

Rule 2638

Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] :=> -Simp[Cos[c + d*x]/d, x] /; FreeQ
[{c, d}, x]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :=> Simp[SinInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 6517

Int[Cos[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :=> S
imp[(Sin[a + b*x]*SinIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]
*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 3312

Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] :=> In
t[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f
, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :=> Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]

Rule 6505

Int[SinIntegral[(a_.) + (b_.)*(x_)]^2, x_Symbol] :=> Simp[((a + b*x)*SinInte
gral[a + b*x]^2)/b, x] - Dist[2, Int[Sin[a + b*x]*SinIntegral[a + b*x], x],
x] /; FreeQ[{a, b}, x]

Rule 6511

Int[Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :=> -
Simp[(Cos[a + b*x]*SinIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]
*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b
.)*(x)]^(n_.), x_Symbol] :=> Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x
]^(n)*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IG
tQ[p, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] :=> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !Match
Q[u, (b_)*(v_)] /; FreeQ[b, x]

Rubi steps

$$\begin{aligned}
\int x \operatorname{Si}(a+bx)^2 dx &= \frac{x(a+bx)\operatorname{Si}(a+bx)^2}{2b} - \frac{a \int \operatorname{Si}(a+bx)^2 dx}{2b} - \int x \sin(a+bx)\operatorname{Si}(a+bx) dx \\
&= \frac{x \cos(a+bx)\operatorname{Si}(a+bx)}{b} - \frac{a(a+bx)\operatorname{Si}(a+bx)^2}{2b^2} + \frac{x(a+bx)\operatorname{Si}(a+bx)^2}{2b} - \frac{\int \cos(a+bx)\operatorname{Si}(a+bx) dx}{b} \\
&= -\frac{a \cos(a+bx)\operatorname{Si}(a+bx)}{b^2} + \frac{x \cos(a+bx)\operatorname{Si}(a+bx)}{b} - \frac{\sin(a+bx)\operatorname{Si}(a+bx)}{b^2} - \frac{a(a+bx)\operatorname{Si}(a+bx)^2}{2b^2} \\
&= -\frac{a \cos(a+bx)\operatorname{Si}(a+bx)}{b^2} + \frac{x \cos(a+bx)\operatorname{Si}(a+bx)}{b} - \frac{\sin(a+bx)\operatorname{Si}(a+bx)}{b^2} - \frac{a(a+bx)\operatorname{Si}(a+bx)^2}{2b^2} \\
&= \frac{\log(a+bx)}{2b^2} - \frac{a \cos(a+bx)\operatorname{Si}(a+bx)}{b^2} + \frac{x \cos(a+bx)\operatorname{Si}(a+bx)}{b} - \frac{\sin(a+bx)\operatorname{Si}(a+bx)}{b^2} - \frac{a(a+bx)\operatorname{Si}(a+bx)^2}{2b^2} \\
&= -\frac{\operatorname{Ci}(2a+2bx)}{2b^2} + \frac{\log(a+bx)}{2b^2} - \frac{a \cos(a+bx)\operatorname{Si}(a+bx)}{b^2} + \frac{x \cos(a+bx)\operatorname{Si}(a+bx)}{b} - \frac{\sin(a+bx)\operatorname{Si}(a+bx)}{b^2} \\
&= \frac{\cos(2a+2bx)}{4b^2} - \frac{\operatorname{Ci}(2a+2bx)}{2b^2} + \frac{\log(a+bx)}{2b^2} - \frac{a \cos(a+bx)\operatorname{Si}(a+bx)}{b^2} + \frac{x \cos(a+bx)\operatorname{Si}(a+bx)}{b} - \frac{\sin(a+bx)\operatorname{Si}(a+bx)}{b^2}
\end{aligned}$$

Mathematica [A] time = 0.280375, size = 95, normalized size = 0.62

$$\frac{-2(a^2 - b^2x^2)\operatorname{Si}(a+bx)^2 - 2\operatorname{CosIntegral}(2(a+bx)) + 4a\operatorname{Si}(2(a+bx)) - 4\operatorname{Si}(a+bx)(\sin(a+bx) + (a-bx)\cos(a+bx))}{4b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*SinIntegral[a + b*x]^2,x]

[Out] (Cos[2*(a + b*x)] - 2*CosIntegral[2*(a + b*x)] + 2*Log[a + b*x] - 4*((a - b*x)*Cos[a + b*x] + Sin[a + b*x])*SinIntegral[a + b*x] - 2*(a^2 - b^2*x^2)*SinIntegral[a + b*x]^2 + 4*a*SinIntegral[2*(a + b*x)])/(4*b^2)

Maple [A] time = 0.066, size = 135, normalized size = 0.9

$$\frac{x^2(\operatorname{Si}(bx+a))^2}{2} - \frac{(\operatorname{Si}(bx+a))^2 a^2}{2b^2} + \frac{x \cos(bx+a)\operatorname{Si}(bx+a)}{b} - \frac{a \cos(bx+a)\operatorname{Si}(bx+a)}{b^2} - \frac{\operatorname{Si}(bx+a)\sin(bx+a)}{b^2} + \dots$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*Si(b*x+a)^2,x)

[Out] 1/2*x^2*Si(b*x+a)^2-1/2/b^2*Si(b*x+a)^2*a^2+x*cos(b*x+a)*Si(b*x+a)/b-a*cos(b*x+a)*Si(b*x+a)/b^2-Si(b*x+a)*sin(b*x+a)/b^2+1/2/b^2*cos(b*x+a)^2+1/2*ln(b*x+a)/b^2-1/2*Ci(2*b*x+2*a)/b^2+a*Si(2*b*x+2*a)/b^2

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \operatorname{Si}(bx+a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(b*x+a)^2,x, algorithm="maxima")

[Out] integrate(x*Si(b*x + a)^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x \text{Si}(bx + a)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(b*x+a)^2,x, algorithm="fricas")

[Out] integral(x*sin_integral(b*x + a)^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \text{Si}^2(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(b*x+a)**2,x)

[Out] Integral(x*Si(a + b*x)**2, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int x \text{Si}(bx + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(b*x+a)^2,x, algorithm="giac")

[Out] integrate(x*Si(b*x + a)^2, x)

3.28 $\int \text{Si}(a + bx)^2 dx$

Optimal. Leaf size=49

$$\frac{(a + bx)\text{Si}(a + bx)^2}{b} - \frac{\text{Si}(2a + 2bx)}{b} + \frac{2\text{Si}(a + bx)\cos(a + bx)}{b}$$

[Out] (2*Cos[a + b*x]*SinIntegral[a + b*x])/b + ((a + b*x)*SinIntegral[a + b*x]^2)/b - SinIntegral[2*a + 2*b*x]/b

Rubi [A] time = 0.0646836, antiderivative size = 49, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 5, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {6505, 6511, 4406, 12, 3299}

$$\frac{(a + bx)\text{Si}(a + bx)^2}{b} - \frac{\text{Si}(2a + 2bx)}{b} + \frac{2\text{Si}(a + bx)\cos(a + bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[SinIntegral[a + b*x]^2,x]

[Out] (2*Cos[a + b*x]*SinIntegral[a + b*x])/b + ((a + b*x)*SinIntegral[a + b*x]^2)/b - SinIntegral[2*a + 2*b*x]/b

Rule 6505

Int[SinIntegral[(a_.) + (b_.)*(x_)]^2, x_Symbol] := Simp[((a + b*x)*SinIntegral[a + b*x]^2)/b, x] - Dist[2, Int[Sin[a + b*x]*SinIntegral[a + b*x], x], x] /; FreeQ[{a, b}, x]

Rule 6511

Int[Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := -Simp[(Cos[a + b*x]*SinIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_.)*(v_)] /; FreeQ[b, x]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned}
\int \text{Si}(a + bx)^2 dx &= \frac{(a + bx)\text{Si}(a + bx)^2}{b} - 2 \int \sin(a + bx)\text{Si}(a + bx) dx \\
&= \frac{2 \cos(a + bx)\text{Si}(a + bx)}{b} + \frac{(a + bx)\text{Si}(a + bx)^2}{b} - 2 \int \frac{\cos(a + bx) \sin(a + bx)}{a + bx} dx \\
&= \frac{2 \cos(a + bx)\text{Si}(a + bx)}{b} + \frac{(a + bx)\text{Si}(a + bx)^2}{b} - 2 \int \frac{\sin(2a + 2bx)}{2(a + bx)} dx \\
&= \frac{2 \cos(a + bx)\text{Si}(a + bx)}{b} + \frac{(a + bx)\text{Si}(a + bx)^2}{b} - \int \frac{\sin(2a + 2bx)}{a + bx} dx \\
&= \frac{2 \cos(a + bx)\text{Si}(a + bx)}{b} + \frac{(a + bx)\text{Si}(a + bx)^2}{b} - \frac{\text{Si}(2a + 2bx)}{b}
\end{aligned}$$

Mathematica [A] time = 0.0089927, size = 43, normalized size = 0.88

$$\frac{(a + bx)\text{Si}(a + bx)^2 - \text{Si}(2(a + bx)) + 2\text{Si}(a + bx) \cos(a + bx)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[SinIntegral[a + b*x]^2,x]

[Out] (2*Cos[a + b*x]*SinIntegral[a + b*x] + (a + b*x)*SinIntegral[a + b*x]^2 - SinIntegral[2*(a + b*x)])/b

Maple [A] time = 0.049, size = 45, normalized size = 0.9

$$\frac{(bx + a) (\text{Si}(bx + a))^2 + 2 \cos(bx + a) \text{Si}(bx + a) - \text{Si}(2bx + 2a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x+a)^2,x)

[Out] 1/b*((b*x+a)*Si(b*x+a)^2+2*cos(b*x+a)*Si(b*x+a)-Si(2*b*x+2*a))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Si}(bx + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)^2,x, algorithm="maxima")

[Out] integrate(Si(b*x + a)^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(\text{Si}(bx + a)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Si(b*x+a)^2,x, algorithm="fricas")
```

```
[Out] integral(sin_integral(b*x + a)^2, x)
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Si}^2(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Si(b*x+a)**2,x)
```

```
[Out] Integral(Si(a + b*x)**2, x)
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Si}(bx + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Si(b*x+a)^2,x, algorithm="giac")
```

```
[Out] integrate(Si(b*x + a)^2, x)
```

$$3.29 \quad \int \frac{\text{Si}(a+bx)^2}{x} dx$$

Optimal. Leaf size=14

$$\text{CannotIntegrate}\left(\frac{\text{Si}(a+bx)^2}{x}, x\right)$$

[Out] CannotIntegrate[SinIntegral[a + b*x]^2/x, x]

Rubi [A] time = 0.0341303, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{Si}(a+bx)^2}{x} dx$$

Verification is Not applicable to the result.

[In] Int[SinIntegral[a + b*x]^2/x, x]

[Out] Defer[Int][SinIntegral[a + b*x]^2/x, x]

Rubi steps

$$\int \frac{\text{Si}(a+bx)^2}{x} dx = \int \frac{\text{Si}(a+bx)^2}{x} dx$$

Mathematica [A] time = 3.30173, size = 0, normalized size = 0.

$$\int \frac{\text{Si}(a+bx)^2}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[SinIntegral[a + b*x]^2/x, x]

[Out] Integrate[SinIntegral[a + b*x]^2/x, x]

Maple [A] time = 0.051, size = 0, normalized size = 0.

$$\int \frac{(\text{Si}(bx+a))^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x+a)^2/x, x)

[Out] int(Si(b*x+a)^2/x, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx + a)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)^2/x,x, algorithm="maxima")

[Out] integrate(Si(b*x + a)^2/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Si}(bx + a)^2}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)^2/x,x, algorithm="fricas")

[Out] integral(sin_integral(b*x + a)^2/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}^2(a + bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)**2/x,x)

[Out] Integral(Si(a + b*x)**2/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx + a)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)^2/x,x, algorithm="giac")

[Out] integrate(Si(b*x + a)^2/x, x)

$$3.30 \quad \int \frac{\text{Si}(a+bx)^2}{x^2} dx$$

Optimal. Leaf size=14

$$\text{CannotIntegrate}\left(\frac{\text{Si}(a+bx)^2}{x^2}, x\right)$$

[Out] CannotIntegrate[SinIntegral[a + b*x]^2/x^2, x]

Rubi [A] time = 0.0338769, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{Si}(a+bx)^2}{x^2} dx$$

Verification is Not applicable to the result.

[In] Int[SinIntegral[a + b*x]^2/x^2, x]

[Out] Defer[Int][SinIntegral[a + b*x]^2/x^2, x]

Rubi steps

$$\int \frac{\text{Si}(a+bx)^2}{x^2} dx = \int \frac{\text{Si}(a+bx)^2}{x^2} dx$$

Mathematica [A] time = 5.05896, size = 0, normalized size = 0.

$$\int \frac{\text{Si}(a+bx)^2}{x^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[SinIntegral[a + b*x]^2/x^2, x]

[Out] Integrate[SinIntegral[a + b*x]^2/x^2, x]

Maple [A] time = 0.056, size = 0, normalized size = 0.

$$\int \frac{(\text{Si}(bx+a))^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x+a)^2/x^2, x)

[Out] int(Si(b*x+a)^2/x^2, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx + a)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)^2/x^2,x, algorithm="maxima")

[Out] integrate(Si(b*x + a)^2/x^2, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Si}(bx + a)^2}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)^2/x^2,x, algorithm="fricas")

[Out] integral(sin_integral(b*x + a)^2/x^2, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}^2(a + bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)**2/x**2,x)

[Out] Integral(Si(a + b*x)**2/x**2, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx + a)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)^2/x^2,x, algorithm="giac")

[Out] integrate(Si(b*x + a)^2/x^2, x)

$$3.31 \quad \int \frac{\text{Si}(a+bx)^2}{x^3} dx$$

Optimal. Leaf size=14

$$\text{CannotIntegrate}\left(\frac{\text{Si}(a+bx)^2}{x^3}, x\right)$$

[Out] CannotIntegrate[SinIntegral[a + b*x]^2/x^3, x]

Rubi [A] time = 0.0344856, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{Si}(a+bx)^2}{x^3} dx$$

Verification is Not applicable to the result.

[In] Int[SinIntegral[a + b*x]^2/x^3, x]

[Out] Defer[Int][SinIntegral[a + b*x]^2/x^3, x]

Rubi steps

$$\int \frac{\text{Si}(a+bx)^2}{x^3} dx = \int \frac{\text{Si}(a+bx)^2}{x^3} dx$$

Mathematica [A] time = 2.75319, size = 0, normalized size = 0.

$$\int \frac{\text{Si}(a+bx)^2}{x^3} dx$$

Verification is Not applicable to the result.

[In] Integrate[SinIntegral[a + b*x]^2/x^3, x]

[Out] Integrate[SinIntegral[a + b*x]^2/x^3, x]

Maple [A] time = 0.059, size = 0, normalized size = 0.

$$\int \frac{(\text{Si}(bx+a))^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x+a)^2/x^3, x)

[Out] int(Si(b*x+a)^2/x^3, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx + a)^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)^2/x^3,x, algorithm="maxima")

[Out] integrate(Si(b*x + a)^2/x^3, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Si}(bx + a)^2}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)^2/x^3,x, algorithm="fricas")

[Out] integral(sin_integral(b*x + a)^2/x^3, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}^2(a + bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)**2/x**3,x)

[Out] Integral(Si(a + b*x)**2/x**3, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx + a)^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)^2/x^3,x, algorithm="giac")

[Out] integrate(Si(b*x + a)^2/x^3, x)

3.32 $\int x^2 \text{Si}(d(a + b \log(cx^n))) dx$

Optimal. Leaf size=137

$$-\frac{1}{6}ix^3e^{-\frac{3a}{bn}}(cx^n)^{-3/n}\text{ExpIntegralEi}\left(\frac{(3-ibdn)(a+b\log(cx^n))}{bn}\right)+\frac{1}{6}ix^3e^{-\frac{3a}{bn}}(cx^n)^{-3/n}\text{ExpIntegralEi}\left(\frac{(3+ibdn)(a+b\log(cx^n))}{bn}\right)$$

```
[Out] ((-I/6)*x^3*ExpIntegralEi[((3 - I*b*d*n)*(a + b*Log[c*x^n]))/(b*n)])/(E^((3*a)/(b*n))*(c*x^n)^(3/n)) + ((I/6)*x^3*ExpIntegralEi[((3 + I*b*d*n)*(a + b*Log[c*x^n]))/(b*n)])/(E^((3*a)/(b*n))*(c*x^n)^(3/n)) + (x^3*SinIntegral[d*(a + b*Log[c*x^n])])/3
```

Rubi [A] time = 0.276316, antiderivative size = 137, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.294$, Rules used = {6526, 12, 4497, 2310, 2178}

$$-\frac{1}{6}ix^3e^{-\frac{3a}{bn}}(cx^n)^{-3/n}\text{Ei}\left(\frac{(3-ibdn)(a+b\log(cx^n))}{bn}\right)+\frac{1}{6}ix^3e^{-\frac{3a}{bn}}(cx^n)^{-3/n}\text{Ei}\left(\frac{(ibdn+3)(a+b\log(cx^n))}{bn}\right)+\frac{1}{3}x^3\text{Si}(d(a+b\log(cx^n)))$$

Antiderivative was successfully verified.

```
[In] Int[x^2*SinIntegral[d*(a + b*Log[c*x^n])], x]
```

```
[Out] ((-I/6)*x^3*ExpIntegralEi[((3 - I*b*d*n)*(a + b*Log[c*x^n]))/(b*n)])/(E^((3*a)/(b*n))*(c*x^n)^(3/n)) + ((I/6)*x^3*ExpIntegralEi[((3 + I*b*d*n)*(a + b*Log[c*x^n]))/(b*n)])/(E^((3*a)/(b*n))*(c*x^n)^(3/n)) + (x^3*SinIntegral[d*(a + b*Log[c*x^n])])/3
```

Rule 6526

```
Int[((e_.)*(x_))^(m_.)*SinIntegral[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)], x_Symbol] := Simp[((e*x)^(m + 1)*SinIntegral[d*(a + b*Log[c*x^n])])/(e*(m + 1)), x] - Dist[(b*d*n)/(m + 1), Int[((e*x)^m*Sin[d*(a + b*Log[c*x^n])])/(d*(a + b*Log[c*x^n])], x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 4497

```
Int[((e_.) + Log[(g_.)*(x_)^(m_.)]*(f_.))*(h_.))^(q_.)*((i_.)*(x_)^(r_.))*Sin[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)], x_Symbol] := Dist[(I*(i*x)^r)/(E^(I*a*d)*(c*x^n)^(I*b*d)*(2*x^(r - I*b*d*n))), Int[x^(r - I*b*d*n)*(h*(e + f*Log[g*x^m]))^q, x], x] - Dist[(I*E^(I*a*d)*(i*x)^r*(c*x^n)^(I*b*d))/(2*x^(r + I*b*d*n)), Int[x^(r + I*b*d*n)*(h*(e + f*Log[g*x^m]))^q, x], x] /; FreeQ[{a, b, c, d, e, f, g, h, i, m, n, q, r}, x]
```

Rule 2310

```
Int[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))^(p_.)*((d_.)*(x_)^(m_.), x_Symbol] := Dist[(d*x)^(m + 1)/(d*n*(c*x^n)^((m + 1)/n)), Subst[Int[E^((m + 1)*x/n)*(a + b*x)^p, x], x, Log[c*x^n]], x] /; FreeQ[{a, b, c, d, m, n, p}, x]
```

Rule 2178

```
Int[(F_)^((g_.)*(e_.) + (f_.)*(x_)))/((c_.) + (d_.)*(x_)), x_Symbol] := Si
mp[(F^(g*(e - (c*f)/d))*ExpIntegralEi[(f*g*(c + d*x)*Log[F])/d])/d, x] /; F
reeQ[{F, c, d, e, f, g}, x] && !$UseGamma == True
```

Rubi steps

$$\begin{aligned} \int x^2 \operatorname{Si}(d(a + b \log(cx^n))) dx &= \frac{1}{3} x^3 \operatorname{Si}(d(a + b \log(cx^n))) - \frac{1}{3} (bdn) \int \frac{x^2 \sin(d(a + b \log(cx^n)))}{d(a + b \log(cx^n))} dx \\ &= \frac{1}{3} x^3 \operatorname{Si}(d(a + b \log(cx^n))) - \frac{1}{3} (bn) \int \frac{x^2 \sin(d(a + b \log(cx^n)))}{a + b \log(cx^n)} dx \\ &= \frac{1}{3} x^3 \operatorname{Si}(d(a + b \log(cx^n))) - \frac{1}{6} \left(i b e^{-iad} n x^{ibdn} (cx^n)^{-ibd} \right) \int \frac{x^{2-ibdn}}{a + b \log(cx^n)} dx + \frac{1}{6} \left(i b e^{iad} n \right) \int \frac{x^{2-ibdn}}{a + b \log(cx^n)} dx \\ &= \frac{1}{3} x^3 \operatorname{Si}(d(a + b \log(cx^n))) - \frac{1}{6} \left(i b e^{-iad} x^3 (cx^n)^{-ibd - \frac{3-ibdn}{n}} \right) \operatorname{Subst} \left(\int \frac{e^{\frac{(3-ibdn)x}{n}}}{a + bx} dx, x, \log(cx^n) \right) \\ &= -\frac{1}{6} i e^{-\frac{3a}{bn}} x^3 (cx^n)^{-3/n} \operatorname{Ei} \left(\frac{(3-ibdn)(a + b \log(cx^n))}{bn} \right) + \frac{1}{6} i e^{-\frac{3a}{bn}} x^3 (cx^n)^{-3/n} \operatorname{Ei} \left(\frac{(3+ibdn)(a + b \log(cx^n))}{bn} \right) \end{aligned}$$

Mathematica [A] time = 1.72639, size = 106, normalized size = 0.77

$$\frac{1}{6} x^3 \left(2 \operatorname{Si}(d(a + b \log(cx^n))) - i e^{-\frac{3a}{bn}} (cx^n)^{-3/n} \left(\operatorname{ExpIntegralEi} \left(\frac{(3-ibdn)(a + b \log(cx^n))}{bn} \right) - \operatorname{ExpIntegralEi} \left(\frac{(3+ibdn)(a + b \log(cx^n))}{bn} \right) \right) \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*SinIntegral[d*(a + b*Log[c*x^n])],x]
```

```
[Out] (x^3*((( -I)*(ExpIntegralEi[((3 - I*b*d*n)*(a + b*Log[c*x^n])]/(b*n)) - ExpIntegralEi[((3 + I*b*d*n)*(a + b*Log[c*x^n])]/(b*n)))]/(E^((3*a)/(b*n))*(c*x^n)^(3/n)) + 2*SinIntegral[d*(a + b*Log[c*x^n])]))/6
```

Maple [F] time = 0.097, size = 0, normalized size = 0.

$$\int x^2 \operatorname{Si}(d(a + b \ln(cx^n))) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*Si(d*(a+b*ln(c*x^n))),x)
```

```
[Out] int(x^2*Si(d*(a+b*ln(c*x^n))),x)
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \operatorname{Si}((b \log(cx^n) + a)d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*Si(d*(a+b*log(c*x^n))),x, algorithm="maxima")
```

[Out] integrate(x^2*Si((b*log(c*x^n) + a)*d), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^2 \text{Si}(bd \log(cx^n) + ad), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Si(d*(a+b*log(c*x^n))),x, algorithm="fricas")

[Out] integral(x^2*sin_integral(b*d*log(c*x^n) + a*d), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Si}(ad + bd \log(cx^n)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*Si(d*(a+b*ln(c*x**n))),x)

[Out] Integral(x**2*Si(a*d + b*d*log(c*x**n)), x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Si(d*(a+b*log(c*x^n))),x, algorithm="giac")

[Out] Timed out

3.33 $\int x \mathbf{Si}(d(a + b \log(cx^n))) dx$

Optimal. Leaf size=137

$$-\frac{1}{4}ix^2e^{-\frac{2a}{bn}}(cx^n)^{-2/n}\text{ExpIntegralEi}\left(\frac{(2-ibdn)(a+b\log(cx^n))}{bn}\right) + \frac{1}{4}ix^2e^{-\frac{2a}{bn}}(cx^n)^{-2/n}\text{ExpIntegralEi}\left(\frac{(2+ibdn)(a+b\log(cx^n))}{bn}\right)$$

[Out] $((-I/4)*x^2*\text{ExpIntegralEi}[(2 - I*b*d*n)*(a + b*\text{Log}[c*x^n])]/(b*n))/(\text{E}^{((2*a)/(b*n))*(c*x^n)^{(2/n)}}) + ((I/4)*x^2*\text{ExpIntegralEi}[(2 + I*b*d*n)*(a + b*\text{Log}[c*x^n])]/(b*n))/(\text{E}^{((2*a)/(b*n))*(c*x^n)^{(2/n)}}) + (x^2*\text{SinIntegral}[d*(a + b*\text{Log}[c*x^n])])/2$

Rubi [A] time = 0.263112, antiderivative size = 137, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {6526, 12, 4497, 2310, 2178}

$$-\frac{1}{4}ix^2e^{-\frac{2a}{bn}}(cx^n)^{-2/n}\text{Ei}\left(\frac{(2-ibdn)(a+b\log(cx^n))}{bn}\right) + \frac{1}{4}ix^2e^{-\frac{2a}{bn}}(cx^n)^{-2/n}\text{Ei}\left(\frac{(ibdn+2)(a+b\log(cx^n))}{bn}\right) + \frac{1}{2}x^2\mathbf{Si}(d(a + b \log(cx^n)))$$

Antiderivative was successfully verified.

[In] $\text{Int}[x*\text{SinIntegral}[d*(a + b*\text{Log}[c*x^n])], x]$

[Out] $((-I/4)*x^2*\text{ExpIntegralEi}[(2 - I*b*d*n)*(a + b*\text{Log}[c*x^n])]/(b*n))/(\text{E}^{((2*a)/(b*n))*(c*x^n)^{(2/n)}}) + ((I/4)*x^2*\text{ExpIntegralEi}[(2 + I*b*d*n)*(a + b*\text{Log}[c*x^n])]/(b*n))/(\text{E}^{((2*a)/(b*n))*(c*x^n)^{(2/n)}}) + (x^2*\text{SinIntegral}[d*(a + b*\text{Log}[c*x^n])])/2$

Rule 6526

$\text{Int}[(e^x)^m(x)^n*\text{SinIntegral}[(a + \text{Log}[c*(x)^n])*(b)], x_Symbol] \rightarrow \text{Simp}[(e^{x+1})^m*\text{SinIntegral}[d*(a + b*\text{Log}[c*x^n])]/(e^{m+1}), x] - \text{Dist}[(b*d*n)/(m+1), \text{Int}[(e^x)^m*\text{Sin}[d*(a + b*\text{Log}[c*x^n])]]/(d*(a + b*\text{Log}[c*x^n])), x, x] /;$ FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]

Rule 12

$\text{Int}[(a)*(u), x_Symbol] \rightarrow \text{Dist}[a, \text{Int}[u, x], x] /;$ FreeQ[a, x] && !MatchQ[u, (b)*(v)] /; FreeQ[b, x]

Rule 4497

$\text{Int}[(e^x + \text{Log}[g*(x)^m])*(f)*(h)^q*(i*(x))^r, x_Symbol] \rightarrow \text{Dist}[(I*(i*x)^r)/(\text{E}^{(I*a*d)*(c*x^n)^{(I*b*d)*(2*x^{(r-I*b*d*n)})})}, \text{Int}[x^{(r-I*b*d*n)}*(h*(e + f*\text{Log}[g*x^m]))^q, x], x] - \text{Dist}[(I*\text{E}^{(I*a*d)}*(i*x)^r*(c*x^n)^{(I*b*d)}]/(2*x^{(r+I*b*d*n)}), \text{Int}[x^{(r+I*b*d*n)}*(h*(e + f*\text{Log}[g*x^m]))^q, x], x] /;$ FreeQ[{a, b, c, d, e, f, g, h, i, m, n, q, r}, x]

Rule 2310

$\text{Int}[(a + \text{Log}[c*(x)^n])*(b)^p*((d)*(x))^m, x_Symbol] \rightarrow \text{Dist}[(d*x)^{(m+1)}/(d*n*(c*x^n)^{(m+1)/n}), \text{Subst}[\text{Int}[\text{E}^{((m+1)*x)/n}*(a + b*x)^p, x], x, \text{Log}[c*x^n], x] /;$ FreeQ[{a, b, c, d, m, n, p}, x]

Rule 2178

```
Int[(F_)^((g_)*(e_) + (f_)*(x_))/((c_) + (d_)*(x_)), x_Symbol] := Si
mp[(F^(g*(e - (c*f)/d))*ExpIntegralEi[(f*g*(c + d*x)*Log[F])/d])/d, x] /; F
reeQ[{F, c, d, e, f, g}, x] && !$UseGamma == True
```

Rubi steps

$$\begin{aligned}
\int x \operatorname{Si}(d(a + b \log(cx^n))) dx &= \frac{1}{2} x^2 \operatorname{Si}(d(a + b \log(cx^n))) - \frac{1}{2} (bdn) \int \frac{x \sin(d(a + b \log(cx^n)))}{d(a + b \log(cx^n))} dx \\
&= \frac{1}{2} x^2 \operatorname{Si}(d(a + b \log(cx^n))) - \frac{1}{2} (bn) \int \frac{x \sin(d(a + b \log(cx^n)))}{a + b \log(cx^n)} dx \\
&= \frac{1}{2} x^2 \operatorname{Si}(d(a + b \log(cx^n))) - \frac{1}{4} \left(i b e^{-iad} n x^{ibdn} (cx^n)^{-ibd} \right) \int \frac{x^{1-ibdn}}{a + b \log(cx^n)} dx + \frac{1}{4} \left(i b e^{iad} n x^{-ibdn} (cx^n)^{ibd} \right) \int \frac{x^{1-ibdn}}{a + b \log(cx^n)} dx \\
&= \frac{1}{2} x^2 \operatorname{Si}(d(a + b \log(cx^n))) - \frac{1}{4} \left(i b e^{-iad} x^2 (cx^n)^{-ibd - \frac{2-ibdn}{n}} \right) \operatorname{Subst} \left(\int \frac{e^{\frac{(2-ibdn)x}{n}}}{a + bx} dx, x, \log(cx^n) \right) \\
&= -\frac{1}{4} i e^{-\frac{2a}{bn}} x^2 (cx^n)^{-2/n} \operatorname{Ei} \left(\frac{(2-ibdn)(a + b \log(cx^n))}{bn} \right) + \frac{1}{4} i e^{-\frac{2a}{bn}} x^2 (cx^n)^{-2/n} \operatorname{Ei} \left(\frac{(2+ibdn)(a + b \log(cx^n))}{bn} \right)
\end{aligned}$$

Mathematica [A] time = 1.6937, size = 106, normalized size = 0.77

$$\frac{1}{4} x^2 \left(2 \operatorname{Si}(d(a + b \log(cx^n))) - i e^{-\frac{2a}{bn}} (cx^n)^{-2/n} \left(\operatorname{ExpIntegralEi} \left(\frac{(2-ibdn)(a + b \log(cx^n))}{bn} \right) - \operatorname{ExpIntegralEi} \left(\frac{(2+ibdn)(a + b \log(cx^n))}{bn} \right) \right) \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x*SinIntegral[d*(a + b*Log[c*x^n])], x]
```

```
[Out] (x^2*(((-I)*(ExpIntegralEi[((2 - I*b*d*n)*(a + b*Log[c*x^n])]/(b*n))] - ExpIntegralEi[((2 + I*b*d*n)*(a + b*Log[c*x^n])]/(b*n)]))/(E^((2*a)/(b*n))*(c*x^n)^(2/n)) + 2*SinIntegral[d*(a + b*Log[c*x^n])])/4
```

Maple [F] time = 0.095, size = 0, normalized size = 0.

$$\int x \operatorname{Si}(d(a + b \ln(cx^n))) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*Si(d*(a+b*ln(c*x^n))), x)
```

```
[Out] int(x*Si(d*(a+b*ln(c*x^n))), x)
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \operatorname{Si}((b \log(cx^n) + a)d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*Si(d*(a+b*log(c*x^n))), x, algorithm="maxima")
```

[Out] integrate(x*Si((b*log(c*x^n) + a)*d), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x \text{Si}(bd \log(cx^n) + ad), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(d*(a+b*log(c*x^n))),x, algorithm="fricas")

[Out] integral(x*sin_integral(b*d*log(c*x^n) + a*d), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \text{Si}(ad + bd \log(cx^n)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(d*(a+b*ln(c*x**n))),x)

[Out] Integral(x*Si(a*d + b*d*log(c*x**n)), x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(d*(a+b*log(c*x^n))),x, algorithm="giac")

[Out] Timed out

3.34 $\int \text{Si}(d(a + b \log(cx^n))) dx$

Optimal. Leaf size=128

$$-\frac{1}{2}ixe^{-\frac{a}{bn}}(cx^n)^{-1/n} \text{ExpIntegralEi}\left(\frac{(1-ibdn)(a+b \log(cx^n))}{bn}\right) + \frac{1}{2}ixe^{-\frac{a}{bn}}(cx^n)^{-1/n} \text{ExpIntegralEi}\left(\frac{(1+ibdn)(a+b \log(cx^n))}{bn}\right)$$

[Out] $((-I/2)*x*\text{ExpIntegralEi}[\frac{((1 - I*b*d*n)*(a + b*\text{Log}[c*x^n])}{(b*n))}]/(E^{(a/(b*n))}*(c*x^n)^n)^{-1}) + ((I/2)*x*\text{ExpIntegralEi}[\frac{((1 + I*b*d*n)*(a + b*\text{Log}[c*x^n])}{(b*n))}]/(E^{(a/(b*n))}*(c*x^n)^n)^{-1}) + x*\text{SinIntegral}[d*(a + b*\text{Log}[c*x^n])]$

Rubi [A] time = 0.238001, antiderivative size = 128, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {6523, 12, 4495, 2310, 2178}

$$-\frac{1}{2}ixe^{-\frac{a}{bn}}(cx^n)^{-1/n} \text{Ei}\left(\frac{(1-ibdn)(a+b \log(cx^n))}{bn}\right) + \frac{1}{2}ixe^{-\frac{a}{bn}}(cx^n)^{-1/n} \text{Ei}\left(\frac{(ibdn+1)(a+b \log(cx^n))}{bn}\right) + x\text{Si}(d(a + b \log(cx^n)))$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{SinIntegral}[d*(a + b*\text{Log}[c*x^n])], x]$

[Out] $((-I/2)*x*\text{ExpIntegralEi}[\frac{((1 - I*b*d*n)*(a + b*\text{Log}[c*x^n])}{(b*n))}]/(E^{(a/(b*n))}*(c*x^n)^n)^{-1}) + ((I/2)*x*\text{ExpIntegralEi}[\frac{((1 + I*b*d*n)*(a + b*\text{Log}[c*x^n])}{(b*n))}]/(E^{(a/(b*n))}*(c*x^n)^n)^{-1}) + x*\text{SinIntegral}[d*(a + b*\text{Log}[c*x^n])]$

Rule 6523

$\text{Int}[\text{SinIntegral}[\frac{((a_.) + \text{Log}[(c_.)*(x_.)^{(n_.)}])*(b_.)}{(d_.)}], x_Symbol] \rightarrow \text{Simp}[x*\text{SinIntegral}[d*(a + b*\text{Log}[c*x^n])], x] - \text{Dist}[b*d*n, \text{Int}[\text{Sin}[d*(a + b*\text{Log}[c*x^n])]/(d*(a + b*\text{Log}[c*x^n])], x], x] /; \text{FreeQ}\{a, b, c, d, n\}, x]$

Rule 12

$\text{Int}[(a_)*(u_), x_Symbol] \rightarrow \text{Dist}[a, \text{Int}[u, x], x] /; \text{FreeQ}[a, x] \&\& \text{!MatchQ}[u, (b_)*(v_)] /; \text{FreeQ}[b, x]$

Rule 4495

$\text{Int}[\frac{((e_.) + \text{Log}[(g_.)*(x_.)^{(m_.)}])*(f_.)*(h_.)^{(q_.)}*\text{Sin}[\frac{((a_.) + \text{Log}[(c_.)*(x_.)^{(n_.)}])*(b_.)}{(d_.)}])}{(d_.)}, x_Symbol] \rightarrow \text{Dist}[I/(E^{(I*a*d)}*(c*x^n)^{(I*b*d)}*(2/x^{(I*b*d*n)})), \text{Int}[(h*(e + f*\text{Log}[g*x^m]))^q/x^{(I*b*d*n)}, x], x] - \text{Dist}[(I*E^{(I*a*d)}*(c*x^n)^{(I*b*d)})/(2*x^{(I*b*d*n)}), \text{Int}[x^{(I*b*d*n)}*(h*(e + f*\text{Log}[g*x^m]))^q, x], x] /; \text{FreeQ}\{a, b, c, d, e, f, g, h, m, n, q\}, x]$

Rule 2310

$\text{Int}[\frac{((a_.) + \text{Log}[(c_.)*(x_.)^{(n_.)}])*(b_.)^{(p_.)}*(d_.)*(x_.)^{(m_.)}}{(d*x)^{(m+1)}/(d*n*(c*x^n)^{((m+1)/n)})}, x_Symbol] \rightarrow \text{Dist}[(d*x)^{(m+1)}/(d*n*(c*x^n)^{((m+1)/n)}), \text{Subst}[\text{Int}[E^{((m+1)*x/n)}*(a + b*x)^p, x], x, \text{Log}[c*x^n]], x] /; \text{FreeQ}\{a, b, c, d, m, n, p\}, x]$

Rule 2178

$\text{Int}[(F_.)^{((g_.)*((e_.) + (f_.)*(x_)))}/((c_.) + (d_.)*(x_)), x_Symbol] \rightarrow \text{Simp}[(F^{(g*(e - (c*f)/d)})*\text{ExpIntegralEi}[\frac{(f*g*(c + d*x)*\text{Log}[F]}{d})]/d], x] /; \text{FreeQ}\{c, d, f, g\}, x]$

```
reeQ[{F, c, d, e, f, g}, x] && !$UseGamma == True
```

Rubi steps

$$\begin{aligned}
 \int \text{Si}(d(a + b \log(cx^n))) dx &= x \text{Si}(d(a + b \log(cx^n))) - (bdn) \int \frac{\sin(d(a + b \log(cx^n)))}{d(a + b \log(cx^n))} dx \\
 &= x \text{Si}(d(a + b \log(cx^n))) - (bn) \int \frac{\sin(d(a + b \log(cx^n)))}{a + b \log(cx^n)} dx \\
 &= x \text{Si}(d(a + b \log(cx^n))) - \frac{1}{2} \left(i b e^{-iad} n x^{ibdn} (cx^n)^{-ibd} \right) \int \frac{x^{-ibdn}}{a + b \log(cx^n)} dx + \frac{1}{2} \left(i b e^{iad} n x^{-ibdn} \right) \int \frac{x^{-ibdn}}{a + b \log(cx^n)} dx \\
 &= x \text{Si}(d(a + b \log(cx^n))) - \frac{1}{2} \left(i b e^{-iad} x (cx^n)^{-ibd - \frac{1-ibdn}{n}} \right) \text{Subst} \left(\int \frac{e^{\frac{(1-ibdn)x}{n}}}{a + bx} dx, x, \log(cx^n) \right) + \frac{1}{2} \left(i b e^{iad} x (cx^n)^{-ibd - \frac{1-ibdn}{n}} \right) \text{Subst} \left(\int \frac{e^{\frac{(1+ibdn)x}{n}}}{a + bx} dx, x, \log(cx^n) \right) \\
 &= -\frac{1}{2} i e^{-\frac{a}{bn}} x (cx^n)^{-1/n} \text{Ei} \left(\frac{(1-ibdn)(a + b \log(cx^n))}{bn} \right) + \frac{1}{2} i e^{-\frac{a}{bn}} x (cx^n)^{-1/n} \text{Ei} \left(\frac{(1+ibdn)(a + b \log(cx^n))}{bn} \right)
 \end{aligned}$$

Mathematica [A] time = 1.6419, size = 102, normalized size = 0.8

$$x \text{Si}(d(a + b \log(cx^n))) - \frac{1}{2} i x e^{-\frac{a}{bn}} (cx^n)^{-1/n} \left(\text{ExpIntegralEi} \left(\frac{(1-ibdn)(a + b \log(cx^n))}{bn} \right) - \text{ExpIntegralEi} \left(\frac{(1+ibdn)(a + b \log(cx^n))}{bn} \right) \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[SinIntegral[d*(a + b*Log[c*x^n]), x]
```

```
[Out] ((-I/2)*x*(ExpIntegralEi[((1 - I*b*d*n)*(a + b*Log[c*x^n])/(b*n)] - ExpIntegralEi[((1 + I*b*d*n)*(a + b*Log[c*x^n])/(b*n)])))/(E^(a/(b*n))*(c*x^n)^n^(-1)) + x*SinIntegral[d*(a + b*Log[c*x^n])]
```

Maple [F] time = 0.069, size = 0, normalized size = 0.

$$\int \text{Si}(d(a + b \ln(cx^n))) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(Si(d*(a+b*ln(c*x^n))), x)
```

```
[Out] int(Si(d*(a+b*ln(c*x^n))), x)
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Si}((b \log(cx^n) + a)d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Si(d*(a+b*log(c*x^n))), x, algorithm="maxima")
```

```
[Out] integrate(Si((b*log(c*x^n) + a)*d), x)
```

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(\text{Si}(bd \log(cx^n) + ad), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*(a+b*log(c*x^n))),x, algorithm="fricas")

[Out] integral(sin_integral(b*d*log(c*x^n) + a*d), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Si}(d(a + b \log(cx^n))) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*(a+b*ln(c*x**n))),x)

[Out] Integral(Si(d*(a + b*log(c*x**n))), x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*(a+b*log(c*x^n))),x, algorithm="giac")

[Out] Timed out

$$3.35 \quad \int \frac{\text{Si}(d(a+b \log(cx^n)))}{x} dx$$

Optimal. Leaf size=54

$$\frac{(a + b \log(cx^n)) \text{Si}(d(a + b \log(cx^n)))}{bn} + \frac{\cos(d(a + b \log(cx^n)))}{bdn}$$

[Out] Cos[d*(a + b*Log[c*x^n])]/(b*d*n) + ((a + b*Log[c*x^n])*SinIntegral[d*(a + b*Log[c*x^n]))]/(b*n)

Rubi [A] time = 0.0309975, antiderivative size = 54, normalized size of antiderivative = 1., number of steps used = 3, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {6499}

$$\frac{(a + b \log(cx^n)) \text{Si}(d(a + b \log(cx^n)))}{bn} + \frac{\cos(d(a + b \log(cx^n)))}{bdn}$$

Antiderivative was successfully verified.

[In] Int[SinIntegral[d*(a + b*Log[c*x^n])]/x,x]

[Out] Cos[d*(a + b*Log[c*x^n])]/(b*d*n) + ((a + b*Log[c*x^n])*SinIntegral[d*(a + b*Log[c*x^n]))]/(b*n)

Rule 6499

Int[SinIntegral[(a_.) + (b_.)*(x_)], x_Symbol] := Simp[((a + b*x)*SinIntegral[a + b*x])/b, x] + Simp[Cos[a + b*x]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\begin{aligned} \int \frac{\text{Si}(d(a + b \log(cx^n)))}{x} dx &= \frac{\text{Subst}\left(\int \text{Si}(d(a + bx)) dx, x, \log(cx^n)\right)}{n} \\ &= \frac{\text{Subst}\left(\int \text{Si}(x) dx, x, ad + bd \log(cx^n)\right)}{bdn} \\ &= \frac{\cos(ad + bd \log(cx^n))}{bdn} + \frac{(a + b \log(cx^n)) \text{Si}(ad + bd \log(cx^n))}{bn} \end{aligned}$$

Mathematica [A] time = 0.0638797, size = 95, normalized size = 1.76

$$\frac{\log(cx^n) \text{Si}(d(a + b \log(cx^n)))}{n} + \frac{a \text{Si}(ad + b \log(cx^n) d)}{bn} - \frac{\sin(ad) \sin(bd \log(cx^n))}{bdn} + \frac{\cos(ad) \cos(bd \log(cx^n))}{bdn}$$

Antiderivative was successfully verified.

[In] Integrate[SinIntegral[d*(a + b*Log[c*x^n])]/x,x]

[Out] (Cos[a*d]*Cos[b*d*Log[c*x^n]])/(b*d*n) - (Sin[a*d]*Sin[b*d*Log[c*x^n]])/(b*d*n) + (Log[c*x^n]*SinIntegral[d*(a + b*Log[c*x^n])])/n + (a*SinIntegral[a*d + b*d*Log[c*x^n]])/(b*n)

Maple [A] time = 0.075, size = 72, normalized size = 1.3

$$\frac{\ln(cx^n) \operatorname{Si}(ad + bd \ln(cx^n))}{n} + \frac{\operatorname{Si}(ad + bd \ln(cx^n)) a}{bn} + \frac{\cos(ad + bd \ln(cx^n))}{bdn}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(d*(a+b*ln(c*x^n)))/x,x)

[Out] 1/n*ln(c*x^n)*Si(a*d+b*d*ln(c*x^n))+1/n/b*Si(a*d+b*d*ln(c*x^n))*a+1/n/b/d*cos(a*d+b*d*ln(c*x^n))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{Si}((b \log(cx^n) + a)d)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*(a+b*log(c*x^n)))/x,x, algorithm="maxima")

[Out] integrate(Si((b*log(c*x^n) + a)*d)/x, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}\left(\frac{\operatorname{Si}(bd \log(cx^n) + ad)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*(a+b*log(c*x^n)))/x,x, algorithm="fricas")

[Out] integral(sin_integral(b*d*log(c*x^n) + a*d)/x, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{Si}(ad + bd \log(cx^n))}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*(a+b*ln(c*x**n)))/x,x)

[Out] Integral(Si(a*d + b*d*log(c*x**n))/x, x)

Giac [A] time = 1.57132, size = 80, normalized size = 1.48

$$\frac{(bdn \log(x) + bd \log(c) + ad) \operatorname{Si}(bdn \log(x) + bd \log(c) + ad) + \cos(bdn \log(x) + bd \log(c) + ad)}{bdn}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Si(d*(a+b*log(c*x^n)))/x,x, algorithm="giac")
```

```
[Out] ((b*d*n*log(x) + b*d*log(c) + a*d)*sin_integral(b*d*n*log(x) + b*d*log(c) +  
a*d) + cos(b*d*n*log(x) + b*d*log(c) + a*d))/(b*d*n)
```


$$3.36 \quad \int \frac{\text{Si}(d(a+b \log(cx^n)))}{x^2} dx$$

Optimal. Leaf size=131

$$\frac{ie^{\frac{a}{bn}} (cx^n)^{\frac{1}{n}} \text{ExpIntegralEi}\left(-\frac{(1-ibdn)(a+b \log(cx^n))}{bn}\right)}{2x} + \frac{ie^{\frac{a}{bn}} (cx^n)^{\frac{1}{n}} \text{ExpIntegralEi}\left(-\frac{(1+ibdn)(a+b \log(cx^n))}{bn}\right)}{2x} - \frac{\text{Si}(d(a+b \log(cx^n)))}{x}$$

[Out] $((-I/2)*E^{(a/(b*n))}*(c*x^n)^n^{(-1)}*\text{ExpIntegralEi}[-(((1 - I*b*d*n)*(a + b*\text{Log}[c*x^n]))/(b*n))])/x + ((I/2)*E^{(a/(b*n))}*(c*x^n)^n^{(-1)}*\text{ExpIntegralEi}[-(((1 + I*b*d*n)*(a + b*\text{Log}[c*x^n]))/(b*n))])/x - \text{SinIntegral}[d*(a + b*\text{Log}[c*x^n])]/x$

Rubi [A] time = 0.25396, antiderivative size = 131, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.294$, Rules used = {6526, 12, 4497, 2310, 2178}

$$\frac{ie^{\frac{a}{bn}} (cx^n)^{\frac{1}{n}} \text{Ei}\left(-\frac{(1-ibdn)(a+b \log(cx^n))}{bn}\right)}{2x} + \frac{ie^{\frac{a}{bn}} (cx^n)^{\frac{1}{n}} \text{Ei}\left(-\frac{(1+ibdn)(a+b \log(cx^n))}{bn}\right)}{2x} - \frac{\text{Si}(d(a+b \log(cx^n)))}{x}$$

Antiderivative was successfully verified.

[In] Int[SinIntegral[d*(a + b*Log[c*x^n])]/x^2, x]

[Out] $((-I/2)*E^{(a/(b*n))}*(c*x^n)^n^{(-1)}*\text{ExpIntegralEi}[-(((1 - I*b*d*n)*(a + b*\text{Log}[c*x^n]))/(b*n))])/x + ((I/2)*E^{(a/(b*n))}*(c*x^n)^n^{(-1)}*\text{ExpIntegralEi}[-(((1 + I*b*d*n)*(a + b*\text{Log}[c*x^n]))/(b*n))])/x - \text{SinIntegral}[d*(a + b*\text{Log}[c*x^n])]/x$

Rule 6526

Int[((e_.)*(x_))^(m_.)*SinIntegral[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)], x_Symbol] := Simp[((e*x)^(m + 1)*SinIntegral[d*(a + b*Log[c*x^n])])/(e*(m + 1)), x] - Dist[(b*d*n)/(m + 1), Int[((e*x)^m * Sin[d*(a + b*Log[c*x^n])])/(d*(a + b*Log[c*x^n])), x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 4497

Int[((e_.) + Log[(g_.)*(x_)^(m_.)]*(f_.))*(h_.))^(q_.)*((i_.)*(x_))^(r_.)*Sin[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)], x_Symbol] := Dist[(I*(i*x)^r)/(E^(I*a*d)*(c*x^n)^(I*b*d)*(2*x^(r - I*b*d*n))), Int[x^(r - I*b*d*n)*(h*(e + f*Log[g*x^m]))^q, x], x] - Dist[(I*E^(I*a*d)*(i*x)^r*(c*x^n)^(I*b*d))/(2*x^(r + I*b*d*n)), Int[x^(r + I*b*d*n)*(h*(e + f*Log[g*x^m]))^q, x], x] /; FreeQ[{a, b, c, d, e, f, g, h, i, m, n, q, r}, x]

Rule 2310

Int[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))^(p_.)*((d_.)*(x_))^(m_.), x_Symbol] := Dist[(d*x)^(m + 1)/(d*n*(c*x^n)^((m + 1)/n)), Subst[Int[E^(((m + 1)*x)/n)*(a + b*x)^p, x], x, Log[c*x^n]], x] /; FreeQ[{a, b, c, d, m, n, p}, x]

Rule 2178

```
Int[(F_)^((g_.)*(e_.) + (f_.)*(x_)))/((c_.) + (d_.)*(x_)), x_Symbol] := Si
mp[(F^(g*(e - (c*f)/d))*ExpIntegralEi[(f*g*(c + d*x)*Log[F])/d])/d, x] /; F
reeQ[{F, c, d, e, f, g}, x] && !$UseGamma == True
```

Rubi steps

$$\begin{aligned} \int \frac{\text{Si}(d(a + b \log(cx^n)))}{x^2} dx &= -\frac{\text{Si}(d(a + b \log(cx^n)))}{x} + (bdn) \int \frac{\sin(d(a + b \log(cx^n)))}{dx^2(a + b \log(cx^n))} dx \\ &= -\frac{\text{Si}(d(a + b \log(cx^n)))}{x} + (bn) \int \frac{\sin(d(a + b \log(cx^n)))}{x^2(a + b \log(cx^n))} dx \\ &= -\frac{\text{Si}(d(a + b \log(cx^n)))}{x} + \frac{1}{2} \left(ibe^{-iad} n x^{ibdn} (cx^n)^{-ibd} \int \frac{x^{-2-ibdn}}{a + b \log(cx^n)} dx - \frac{1}{2} \left(ibe^{iad} n x^{-ibdn} \right. \right. \\ &= -\frac{\text{Si}(d(a + b \log(cx^n)))}{x} + \frac{\left(ibe^{-iad} (cx^n)^{-ibd - \frac{-1-ibdn}{n}} \right) \text{Subst} \left(\int \frac{e^{\frac{(-1-ibdn)x}{a+bx}}}{a+bx} dx, x, \log(cx^n) \right)}{2x} \\ &= -\frac{ie^{\frac{a}{bn}} (cx^n)^{\frac{1}{n}} \text{Ei} \left(-\frac{(1-ibdn)(a+b \log(cx^n))}{bn} \right)}{2x} + \frac{ie^{\frac{a}{bn}} (cx^n)^{\frac{1}{n}} \text{Ei} \left(-\frac{(1+ibdn)(a+b \log(cx^n))}{bn} \right)}{2x} - \frac{\text{Si}(d(a + b \log(cx^n)))}{x} \end{aligned}$$

Mathematica [A] time = 1.68398, size = 107, normalized size = 0.82

$$\frac{-2\text{Si}(d(a + b \log(cx^n))) + ie^{\frac{a}{bn}} (cx^n)^{\frac{1}{n}} \left(\text{ExpIntegralEi} \left(-\frac{i(bdn-i)(a+b \log(cx^n))}{bn} \right) - \text{ExpIntegralEi} \left(\frac{i(bdn+i)(a+b \log(cx^n))}{bn} \right) \right)}{2x}$$

Antiderivative was successfully verified.

```
[In] Integrate[SinIntegral[d*(a + b*Log[c*x^n])]/x^2,x]
```

```
[Out] (I*E^(a/(b*n))*(c*x^n)^n^(-1)*(ExpIntegralEi[((-I)*(-I + b*d*n)*(a + b*Log[c*x^n])]/(b*n)] - ExpIntegralEi[(I*(I + b*d*n)*(a + b*Log[c*x^n])]/(b*n)]) - 2*SinIntegral[d*(a + b*Log[c*x^n])])/(2*x)
```

Maple [F] time = 0.092, size = 0, normalized size = 0.

$$\int \frac{\text{Si}(d(a + b \ln(cx^n)))}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(Si(d*(a+b*ln(c*x^n)))/x^2,x)
```

```
[Out] int(Si(d*(a+b*ln(c*x^n)))/x^2,x)
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}((b \log(cx^n) + a)d)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*(a+b*log(c*x^n)))/x^2,x, algorithm="maxima")

[Out] integrate(Si((b*log(c*x^n) + a)*d)/x^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Si}(bd \log(cx^n) + ad)}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*(a+b*log(c*x^n)))/x^2,x, algorithm="fricas")

[Out] integral(sin_integral(b*d*log(c*x^n) + a*d)/x^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(ad + bd \log(cx^n))}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*(a+b*ln(c*x**n)))/x**2,x)

[Out] Integral(Si(a*d + b*d*log(c*x**n))/x**2, x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*(a+b*log(c*x^n)))/x^2,x, algorithm="giac")

[Out] Timed out

$$3.37 \quad \int \frac{\text{Si}(d(a+b \log(cx^n)))}{x^3} dx$$

Optimal. Leaf size=139

$$\frac{i e^{\frac{2a}{bn}} (cx^n)^{2/n} \text{ExpIntegralEi}\left(-\frac{(2-ibdn)(a+b \log(cx^n))}{bn}\right)}{4x^2} + \frac{i e^{\frac{2a}{bn}} (cx^n)^{2/n} \text{ExpIntegralEi}\left(-\frac{(2+ibdn)(a+b \log(cx^n))}{bn}\right)}{4x^2} - \frac{\text{Si}(d(a+b \log(cx^n)))}{2x^2}$$

[Out] $((-I/4)*E^{((2*a)/(b*n))*(c*x^n)^{(2/n)}*ExpIntegralEi[-(((2 - I*b*d*n)*(a + b*Log[c*x^n]))/(b*n))])/x^2 + ((I/4)*E^{((2*a)/(b*n))*(c*x^n)^{(2/n)}*ExpIntegralEi[-(((2 + I*b*d*n)*(a + b*Log[c*x^n]))/(b*n))])/x^2 - SinIntegral[d*(a + b*Log[c*x^n])]/(2*x^2)$

Rubi [A] time = 0.251442, antiderivative size = 139, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.294$, Rules used = {6526, 12, 4497, 2310, 2178}

$$\frac{i e^{\frac{2a}{bn}} (cx^n)^{2/n} \text{Ei}\left(-\frac{(2-ibdn)(a+b \log(cx^n))}{bn}\right)}{4x^2} + \frac{i e^{\frac{2a}{bn}} (cx^n)^{2/n} \text{Ei}\left(-\frac{(2+ibdn)(a+b \log(cx^n))}{bn}\right)}{4x^2} - \frac{\text{Si}(d(a+b \log(cx^n)))}{2x^2}$$

Antiderivative was successfully verified.

[In] Int[SinIntegral[d*(a + b*Log[c*x^n])]/x^3,x]

[Out] $((-I/4)*E^{((2*a)/(b*n))*(c*x^n)^{(2/n)}*ExpIntegralEi[-(((2 - I*b*d*n)*(a + b*Log[c*x^n]))/(b*n))])/x^2 + ((I/4)*E^{((2*a)/(b*n))*(c*x^n)^{(2/n)}*ExpIntegralEi[-(((2 + I*b*d*n)*(a + b*Log[c*x^n]))/(b*n))])/x^2 - SinIntegral[d*(a + b*Log[c*x^n])]/(2*x^2)$

Rule 6526

Int[((e_.)*(x_))^(m_.)*SinIntegral[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)], x_Symbol] := Simp[((e*x)^(m + 1)*SinIntegral[d*(a + b*Log[c*x^n])]/(e*(m + 1)), x] - Dist[(b*d*n)/(m + 1), Int[((e*x)^m*Sin[d*(a + b*Log[c*x^n])])]/(d*(a + b*Log[c*x^n])), x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 4497

Int[(((e_.) + Log[(g_.)*(x_)^(m_.)]*(f_.))*(h_.))^(q_.)*((i_.)*(x_)^(r_.))*Sin[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)], x_Symbol] := Dist[(I*(i*x)^r)/(E^(I*a*d)*(c*x^n)^(I*b*d)*(2*x^(r - I*b*d*n))), Int[x^(r - I*b*d*n)*(h*(e + f*Log[g*x^m]))^q, x], x] - Dist[(I*E^(I*a*d)*(i*x)^r*(c*x^n)^(I*b*d))/(2*x^(r + I*b*d*n)), Int[x^(r + I*b*d*n)*(h*(e + f*Log[g*x^m]))^q, x], x] /; FreeQ[{a, b, c, d, e, f, g, h, i, m, n, q, r}, x]

Rule 2310

Int[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))^(p_.)*((d_.)*(x_)^(m_.)), x_Symbol] := Dist[(d*x)^(m + 1)/(d*n*(c*x^n)^((m + 1)/n)), Subst[Int[E^(((m + 1)*x)/n)*(a + b*x)^p, x], x, Log[c*x^n]], x] /; FreeQ[{a, b, c, d, m, n, p}, x]

Rule 2178

```
Int[(F_)^((g_.)*((e_.) + (f_.)*(x_)))/((c_.) + (d_.)*(x_)), x_Symbol] := Si
mp[(F^(g*(e - (c*f)/d))*ExpIntegralEi[(f*g*(c + d*x)*Log[F])/d])/d, x] /; F
reeQ[{F, c, d, e, f, g}, x] && !$UseGamma == True
```

Rubi steps

$$\begin{aligned}
\int \frac{\text{Si}(d(a + b \log(cx^n)))}{x^3} dx &= -\frac{\text{Si}(d(a + b \log(cx^n)))}{2x^2} + \frac{1}{2}(bdn) \int \frac{\sin(d(a + b \log(cx^n)))}{dx^3(a + b \log(cx^n))} dx \\
&= -\frac{\text{Si}(d(a + b \log(cx^n)))}{2x^2} + \frac{1}{2}(bn) \int \frac{\sin(d(a + b \log(cx^n)))}{x^3(a + b \log(cx^n))} dx \\
&= -\frac{\text{Si}(d(a + b \log(cx^n)))}{2x^2} + \frac{1}{4} \left(ibe^{-iad} n x^{ibdn} (cx^n)^{-ibd} \right) \int \frac{x^{-3-ibdn}}{a + b \log(cx^n)} dx - \frac{1}{4} \left(ibe^{iad} n x \right) \\
&= -\frac{\text{Si}(d(a + b \log(cx^n)))}{2x^2} + \frac{\left(ibe^{-iad} (cx^n)^{-ibd-\frac{-2-ibdn}{n}} \right) \text{Subst} \left(\int \frac{e^{\frac{(-2-ibdn)x}{a+bx}}}{a+bx} dx, x, \log(cx^n) \right)}{4x^2} \\
&= -\frac{ie^{\frac{2a}{bn}} (cx^n)^{2/n} \text{Ei} \left(-\frac{(2-ibdn)(a+b \log(cx^n))}{bn} \right)}{4x^2} + \frac{ie^{\frac{2a}{bn}} (cx^n)^{2/n} \text{Ei} \left(-\frac{(2+ibdn)(a+b \log(cx^n))}{bn} \right)}{4x^2} - \frac{\text{Si}(d(a + b \log(cx^n)))}{4x^2}
\end{aligned}$$

Mathematica [A] time = 1.6982, size = 111, normalized size = 0.8

$$\frac{i \left(e^{\frac{2a}{bn}} (cx^n)^{2/n} \left(\text{ExpIntegralEi} \left(-\frac{i(bdn-2i)(a+b \log(cx^n))}{bn} \right) - \text{ExpIntegralEi} \left(\frac{i(bdn+2i)(a+b \log(cx^n))}{bn} \right) \right) + 2i \text{Si}(d(a + b \log(cx^n))) \right)}{4x^2}$$

Antiderivative was successfully verified.

[In] Integrate[SinIntegral[d*(a + b*Log[c*x^n])]/x^3,x]

[Out] ((I/4)*(E^((2*a)/(b*n))*(c*x^n)^(2/n)*(ExpIntegralEi[((-I)*(-2*I + b*d*n)*(a + b*Log[c*x^n])]/(b*n)) - ExpIntegralEi[(I*(2*I + b*d*n)*(a + b*Log[c*x^n])]/(b*n)])) + (2*I)*SinIntegral[d*(a + b*Log[c*x^n])])/x^2

Maple [F] time = 0.092, size = 0, normalized size = 0.

$$\int \frac{\text{Si}(d(a + b \ln(cx^n)))}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(d*(a+b*ln(c*x^n)))/x^3,x)

[Out] int(Si(d*(a+b*ln(c*x^n)))/x^3,x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}((b \log(cx^n) + a)d)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*(a+b*log(c*x^n)))/x^3,x, algorithm="maxima")

[Out] integrate(Si((b*log(c*x^n) + a)*d)/x^3, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Si}(bd \log(cx^n) + ad)}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*(a+b*log(c*x^n)))/x^3,x, algorithm="fricas")

[Out] integral(sin_integral(b*d*log(c*x^n) + a*d)/x^3, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(ad + bd \log(cx^n))}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*(a+b*ln(c*x**n)))/x**3,x)

[Out] Integral(Si(a*d + b*d*log(c*x**n))/x**3, x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*(a+b*log(c*x^n)))/x^3,x, algorithm="giac")

[Out] Timed out

3.38 $\int (ex)^m \mathbf{Si}(d(a + b \log(cx^n))) dx$

Optimal. Leaf size=176

$$\frac{ix(ex)^m e^{-\frac{a(m+1)}{bn}} (cx^n)^{-\frac{m+1}{n}} \text{ExpIntegralEi}\left(\frac{(-ibdn+m+1)(a+b \log(cx^n))}{bn}\right)}{2(m+1)} + \frac{ix(ex)^m e^{-\frac{a(m+1)}{bn}} (cx^n)^{-\frac{m+1}{n}} \text{ExpIntegralEi}\left(\frac{(ibdn-m-1)(a+b \log(cx^n))}{bn}\right)}{2(m+1)}$$

[Out] $((-I/2)*x*(e*x)^m*\text{ExpIntegralEi}[\frac{((1+m-I*b*d*n)*(a+b*\text{Log}[c*x^n])}{(b*n)})]/(E^((a*(1+m))/(b*n))*(1+m)*(c*x^n)^((1+m)/n)) + ((I/2)*x*(e*x)^m*\text{ExpIntegralEi}[\frac{((1+m+I*b*d*n)*(a+b*\text{Log}[c*x^n])}{(b*n)})]/(E^((a*(1+m))/(b*n))*(1+m)*(c*x^n)^((1+m)/n)) + ((e*x)^(1+m)*\text{SinIntegral}[d*(a+b*\text{Log}[c*x^n])])/(e*(1+m)))$

Rubi [A] time = 0.314787, antiderivative size = 176, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {6526, 12, 4497, 2310, 2178}

$$\frac{ix(ex)^m e^{-\frac{a(m+1)}{bn}} (cx^n)^{-\frac{m+1}{n}} \text{Ei}\left(\frac{(m-ibdn+1)(a+b \log(cx^n))}{bn}\right)}{2(m+1)} + \frac{ix(ex)^m e^{-\frac{a(m+1)}{bn}} (cx^n)^{-\frac{m+1}{n}} \text{Ei}\left(\frac{(m+ibdn+1)(a+b \log(cx^n))}{bn}\right)}{2(m+1)} + \frac{(ex)^{m+1}}{e}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(e*x)^m*\text{SinIntegral}[d*(a + b*\text{Log}[c*x^n])], x]$

[Out] $((-I/2)*x*(e*x)^m*\text{ExpIntegralEi}[\frac{((1+m-I*b*d*n)*(a+b*\text{Log}[c*x^n])}{(b*n)})]/(E^((a*(1+m))/(b*n))*(1+m)*(c*x^n)^((1+m)/n)) + ((I/2)*x*(e*x)^m*\text{ExpIntegralEi}[\frac{((1+m+I*b*d*n)*(a+b*\text{Log}[c*x^n])}{(b*n)})]/(E^((a*(1+m))/(b*n))*(1+m)*(c*x^n)^((1+m)/n)) + ((e*x)^(1+m)*\text{SinIntegral}[d*(a+b*\text{Log}[c*x^n])])/(e*(1+m)))$

Rule 6526

$\text{Int}[\frac{(e^x)^m \text{SinIntegral}[(a + \text{Log}[c*x^n])*(b)]}{(e^{m+1})}, x] - \text{Dist}[\frac{b*d*n}{m+1}, \text{Int}[\frac{(e^x)^m \text{Sin}[d*(a + b*\text{Log}[c*x^n])]}{d*(a + b*\text{Log}[c*x^n])}, x], x] /;$ FreeQ[{a, b, c, d, e, m, n}, x] && Ne Q[m, -1]

Rule 12

$\text{Int}[(a)*(u), x_Symbol] := \text{Dist}[a, \text{Int}[u, x], x] /;$ FreeQ[a, x] && !Match Q[u, (b)*(v)] /; FreeQ[b, x]

Rule 4497

$\text{Int}[\frac{((e^x)^m + \text{Log}[g*x^m])*(f*x^r)*(h*x^q)}{\text{Sin}[(a + \text{Log}[c*x^n])*(b)]}, x_Symbol] := \text{Dist}[\frac{(I*(i*x)^r)}{E^{(I*a*d)*(c*x^n)^{(I*b*d)*(2*x^r - I*b*d*n)}}}, \text{Int}[x^{(r - I*b*d*n)}*(h*(e + f*\text{Log}[g*x^m]))^q, x], x] - \text{Dist}[\frac{(I*E^{(I*a*d)}*(i*x)^r*(c*x^n)^{(I*b*d)})}{(2*x^{(r + I*b*d*n)})}, \text{Int}[x^{(r + I*b*d*n)}*(h*(e + f*\text{Log}[g*x^m]))^q, x], x] /;$ FreeQ[{a, b, c, d, e, f, g, h, i, m, n, q, r}, x]

Rule 2310

$\text{Int}[\frac{(a + \text{Log}[c*x^n])*(b)^p*(d*x^m)}{(d*x)^{(m+1)/(d*n*(c*x^n)^{(m+1)/n})}}, x_Symbol] := \text{Dist}[(d*x)^{(m+1)/(d*n*(c*x^n)^{(m+1)/n})}, \text{Subst}[\text{Int}[E^{((m+1)*x}$

$/n)^m(a + b*x)^p, x], x, \text{Log}[c*x^n], x] /; \text{FreeQ}[\{a, b, c, d, m, n, p\}, x]$

Rule 2178

$\text{Int}[(F_)^g((g_.)*((e_.) + (f_.)*(x_)))/((c_.) + (d_.)*(x_)), x_Symbol] :> \text{Simp}[(F^g*(e - (c*f)/d))*\text{ExpIntegralEi}[(f*g*(c + d*x)*\text{Log}[F])/d]/d, x] /; \text{FreeQ}[\{F, c, d, e, f, g\}, x] \&\amp; \text{\$UseGamma} == \text{True}$

Rubi steps

$$\begin{aligned} \int (ex)^m \text{Si}(d(a + b \log(cx^n))) dx &= \frac{(ex)^{1+m} \text{Si}(d(a + b \log(cx^n)))}{e(1+m)} - \frac{(bdn) \int \frac{(ex)^m \sin(d(a+b \log(cx^n)))}{d(a+b \log(cx^n))} dx}{1+m} \\ &= \frac{(ex)^{1+m} \text{Si}(d(a + b \log(cx^n)))}{e(1+m)} - \frac{(bn) \int \frac{(ex)^m \sin(d(a+b \log(cx^n)))}{a+b \log(cx^n)} dx}{1+m} \\ &= \frac{(ex)^{1+m} \text{Si}(d(a + b \log(cx^n)))}{e(1+m)} - \frac{(ibe^{-iad} nx^{-m+ibdn} (ex)^m (cx^n)^{-ibd}) \int \frac{x^{m-ibdn}}{a+b \log(cx^n)} dx}{2(1+m)} + \dots \\ &= \frac{(ex)^{1+m} \text{Si}(d(a + b \log(cx^n)))}{e(1+m)} - \frac{(ibe^{-iad} x (ex)^m (cx^n)^{-ibd - \frac{1+m-ibdn}{n}}) \text{Subst}\left(\int \frac{e^{\frac{(1+m-ibdn)x}{a+bx}}}{a+bx} dx\right)}{2(1+m)} \\ &= -\frac{ie^{-\frac{a(1+m)}{bn}} x (ex)^m (cx^n)^{-\frac{1+m}{n}} \text{Ei}\left(\frac{(1+m-ibdn)(a+b \log(cx^n))}{bn}\right)}{2(1+m)} + \frac{ie^{-\frac{a(1+m)}{bn}} x (ex)^m (cx^n)^{-\frac{1+m}{n}} \text{Ei}\left(\dots\right)}{2(1+m)} \end{aligned}$$

Mathematica [A] time = 3.01977, size = 128, normalized size = 0.73

$$\frac{(ex)^m \left(2x \text{Si}(d(a + b \log(cx^n))) - ix^{-m} \exp\left(-\frac{(m+1)(a+b \log(cx^n)-bn \log(x))}{bn}\right) \left(\text{ExpIntegralEi}\left(\frac{(-ibdn+m+1)(a+b \log(cx^n))}{bn}\right) - \text{ExpIntegralEi}\left(\frac{(1+m-ibdn)(a+b \log(cx^n))}{bn}\right) \right) \right)}{2(m+1)}$$

Antiderivative was successfully verified.

[In] Integrate[(e*x)^m*SinIntegral[d*(a + b*Log[c*x^n]), x]

[Out] ((e*x)^m*(((1+m - I*b*d*n)*(a + b*Log[c*x^n]))/(b*n)) - ExpIntegralEi[(((1+m + I*b*d*n)*(a + b*Log[c*x^n]))/(b*n))])/(E^(((1+m)*(a - b*n*Log[x] + b*Log[c*x^n]))/(b*n))*x^m) + 2*x*SinIntegral[d*(a + b*Log[c*x^n])])/(2*(1+m))

Maple [F] time = 0.093, size = 0, normalized size = 0.

$$\int (ex)^m \text{Si}(d(a + b \ln(cx^n))) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e*x)^m*Si(d*(a+b*ln(c*x^n))), x)

[Out] int((e*x)^m*Si(d*(a+b*ln(c*x^n))), x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int (ex)^m \operatorname{Si}((b \log(cx^n) + a)d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e*x)^m*Si(d*(a+b*log(c*x^n))),x, algorithm="maxima")

[Out] integrate((e*x)^m*Si((b*log(c*x^n) + a)*d), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}\left((ex)^m \operatorname{Si}(bd \log(cx^n) + ad), x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e*x)^m*Si(d*(a+b*log(c*x^n))),x, algorithm="fricas")

[Out] integral((e*x)^m*sin_integral(b*d*log(c*x^n) + a*d), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int (ex)^m \operatorname{Si}(ad + bd \log(cx^n)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e*x)**m*Si(d*(a+b*ln(c*x**n))),x)

[Out] Integral((e*x)**m*Si(a*d + b*d*log(c*x**n)), x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e*x)^m*Si(d*(a+b*log(c*x^n))),x, algorithm="giac")

[Out] Timed out

3.39 $\int \frac{\sin(bx)\text{Si}(bx)}{x^3} dx$

Optimal. Leaf size=96

$$b^2\text{CosIntegral}(2bx) - \frac{1}{4}b^2\text{Si}(bx)^2 - \frac{\text{Si}(bx)\sin(bx)}{2x^2} - \frac{b\text{Si}(bx)\cos(bx)}{2x} - \frac{\sin^2(bx)}{4x^2} - \frac{b\sin(2bx)}{4x} - \frac{b\sin(bx)\cos(bx)}{2x}$$

[Out] $b^2\text{CosIntegral}[2*b*x] - (b*\text{Cos}[b*x]*\text{Sin}[b*x])/(2*x) - \text{Sin}[b*x]^2/(4*x^2) - (b*\text{Sin}[2*b*x])/(4*x) - (b*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/(2*x) - (\text{Sin}[b*x]*\text{SinIntegral}[b*x])/(2*x^2) - (b^2*\text{SinIntegral}[b*x]^2)/4$

Rubi [A] time = 0.203468, antiderivative size = 96, normalized size of antiderivative = 1., number of steps used = 14, number of rules used = 10, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.833$, Rules used = {6515, 6521, 6686, 12, 4406, 3297, 3302, 3314, 29, 3312}

$$b^2\text{CosIntegral}(2bx) - \frac{1}{4}b^2\text{Si}(bx)^2 - \frac{\text{Si}(bx)\sin(bx)}{2x^2} - \frac{b\text{Si}(bx)\cos(bx)}{2x} - \frac{\sin^2(bx)}{4x^2} - \frac{b\sin(2bx)}{4x} - \frac{b\sin(bx)\cos(bx)}{2x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(\text{Sin}[b*x]*\text{SinIntegral}[b*x])/x^3, x]$

[Out] $b^2\text{CosIntegral}[2*b*x] - (b*\text{Cos}[b*x]*\text{Sin}[b*x])/(2*x) - \text{Sin}[b*x]^2/(4*x^2) - (b*\text{Sin}[2*b*x])/(4*x) - (b*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/(2*x) - (\text{Sin}[b*x]*\text{SinIntegral}[b*x])/(2*x^2) - (b^2*\text{SinIntegral}[b*x]^2)/4$

Rule 6515

$\text{Int}[(e + f*x)^m * \text{Sin}[a + b*x] * \text{SinIntegral}[c + d*x], x_Symbol] :> \text{Simp}[(e + f*x)^{m+1} * \text{Sin}[a + b*x] * \text{SinIntegral}[c + d*x] / (f*(m+1)), x] + (-\text{Dist}[b/(f*(m+1)), \text{Int}[(e + f*x)^{m+1} * \text{Cos}[a + b*x] * \text{SinIntegral}[c + d*x], x], x] - \text{Dist}[d/(f*(m+1)), \text{Int}[(e + f*x)^{m+1} * \text{Sin}[a + b*x] * \text{Sin}[c + d*x] / (c + d*x), x], x]) /; \text{FreeQ}\{a, b, c, d, e, f\}, x \&\& \text{ILtQ}[m, -1]$

Rule 6521

$\text{Int}[\text{Cos}[a + b*x] * (e + f*x)^m * \text{SinIntegral}[c + d*x], x_Symbol] :> \text{Simp}[(e + f*x)^{m+1} * \text{Cos}[a + b*x] * \text{SinIntegral}[c + d*x] / (f*(m+1)), x] + (\text{Dist}[b/(f*(m+1)), \text{Int}[(e + f*x)^{m+1} * \text{Sin}[a + b*x] * \text{SinIntegral}[c + d*x], x], x] - \text{Dist}[d/(f*(m+1)), \text{Int}[(e + f*x)^{m+1} * \text{Cos}[a + b*x] * \text{Sin}[c + d*x] / (c + d*x), x], x]) /; \text{FreeQ}\{a, b, c, d, e, f\}, x \&\& \text{ILtQ}[m, -1]$

Rule 6686

$\text{Int}[u * (y)^m, x_Symbol] :> \text{With}\{q = \text{DerivativeDivides}[y, u, x]\}, \text{Simp}[q*y^{m+1} / (m+1), x] /; \text{!FalseQ}[q] /; \text{FreeQ}[m, x] \&\& \text{NeQ}[m, -1]$

Rule 12

$\text{Int}[a * u, x_Symbol] :> \text{Dist}[a, \text{Int}[u, x], x] /; \text{FreeQ}[a, x] \&\& \text{!MatchQ}[u, (b)*(v)] /; \text{FreeQ}[b, x]$

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 3297

```
Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)], x_Symbol] := Simp[((c + d*x)^(m + 1)*Sin[e + f*x])/(d*(m + 1)), x] - Dist[f/(d*(m + 1)), Int[(c + d*x)^(m + 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && LtQ[m, -1]
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rule 3314

```
Int[((c_.) + (d_.)*(x_))^(m_.)*((b_.)*sin[(e_.) + (f_.)*(x_)])^(n_.), x_Symbol] := Simp[((c + d*x)^(m + 1)*(b*Sine[e + f*x])^n)/(d*(m + 1)), x] + (Dist[(b^2*f^2*n*(n - 1))/(d^2*(m + 1)*(m + 2)), Int[(c + d*x)^(m + 2)*(b*Sine[e + f*x])^(n - 2), x], x] - Dist[(f^2*n^2)/(d^2*(m + 1)*(m + 2)), Int[(c + d*x)^(m + 2)*(b*Sine[e + f*x])^n, x], x] - Simp[(b*f*n*(c + d*x)^(m + 2)*Cos[e + f*x]*(b*Sine[e + f*x])^(n - 1))/(d^2*(m + 1)*(m + 2)), x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && LtQ[m, -2]
```

Rule 29

```
Int[(x_)^(-1), x_Symbol] := Simp[Log[x], x]
```

Rule 3312

```
Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rubi steps

$$\begin{aligned}
 \int \frac{\sin(bx)\text{Si}(bx)}{x^3} dx &= -\frac{\sin(bx)\text{Si}(bx)}{2x^2} + \frac{1}{2}b \int \frac{\sin^2(bx)}{bx^3} dx + \frac{1}{2}b \int \frac{\cos(bx)\text{Si}(bx)}{x^2} dx \\
 &= -\frac{b \cos(bx)\text{Si}(bx)}{2x} - \frac{\sin(bx)\text{Si}(bx)}{2x^2} + \frac{1}{2} \int \frac{\sin^2(bx)}{x^3} dx + \frac{1}{2}b^2 \int \frac{\cos(bx) \sin(bx)}{bx^2} dx - \frac{1}{2}b^2 \int \frac{\sin^2(bx)}{bx^2} dx \\
 &= -\frac{b \cos(bx) \sin(bx)}{2x} - \frac{\sin^2(bx)}{4x^2} - \frac{b \cos(bx)\text{Si}(bx)}{2x} - \frac{\sin(bx)\text{Si}(bx)}{2x^2} - \frac{1}{4}b^2\text{Si}(bx)^2 + \frac{1}{2}b \int \frac{\cos(bx) \sin(bx)}{bx^2} dx \\
 &= \frac{1}{2}b^2 \log(x) - \frac{b \cos(bx) \sin(bx)}{2x} - \frac{\sin^2(bx)}{4x^2} - \frac{b \cos(bx)\text{Si}(bx)}{2x} - \frac{\sin(bx)\text{Si}(bx)}{2x^2} - \frac{1}{4}b^2\text{Si}(bx)^2 + \frac{1}{2}b \int \frac{\cos(bx) \sin(bx)}{bx^2} dx \\
 &= -\frac{b \cos(bx) \sin(bx)}{2x} - \frac{\sin^2(bx)}{4x^2} - \frac{b \cos(bx)\text{Si}(bx)}{2x} - \frac{\sin(bx)\text{Si}(bx)}{2x^2} - \frac{1}{4}b^2\text{Si}(bx)^2 + \frac{1}{4}b \int \frac{\sin(2bx)}{x^2} dx \\
 &= \frac{1}{2}b^2\text{Ci}(2bx) - \frac{b \cos(bx) \sin(bx)}{2x} - \frac{\sin^2(bx)}{4x^2} - \frac{b \sin(2bx)}{4x} - \frac{b \cos(bx)\text{Si}(bx)}{2x} - \frac{\sin(bx)\text{Si}(bx)}{2x^2} - \frac{1}{4}b^2\text{Si}(bx)^2 \\
 &= b^2\text{Ci}(2bx) - \frac{b \cos(bx) \sin(bx)}{2x} - \frac{\sin^2(bx)}{4x^2} - \frac{b \sin(2bx)}{4x} - \frac{b \cos(bx)\text{Si}(bx)}{2x} - \frac{\sin(bx)\text{Si}(bx)}{2x^2} - \frac{1}{4}b^2\text{Si}(bx)^2
 \end{aligned}$$

Mathematica [F] time = 1.00412, size = 0, normalized size = 0.

$$\int \frac{\sin(bx)\text{Si}(bx)}{x^3} dx$$

Verification is Not applicable to the result.

[In] Integrate[(Sin[b*x]*SinIntegral[b*x])/x^3,x]

[Out] Integrate[(Sin[b*x]*SinIntegral[b*x])/x^3, x]

Maple [F] time = 0.056, size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx) \sin(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x)*sin(b*x)/x^3,x)

[Out] int(Si(b*x)*sin(b*x)/x^3,x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx) \sin(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)*sin(b*x)/x^3,x, algorithm="maxima")

[Out] integrate(Si(b*x)*sin(b*x)/x^3, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\sin(bx)\text{Si}(bx)}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)*sin(b*x)/x^3,x, algorithm="fricas")

[Out] integral(sin(b*x)*sin_integral(b*x)/x^3, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sin(bx)\text{Si}(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Si(b*x)*sin(b*x)/x**3,x)
```

```
[Out] Integral(sin(b*x)*Si(b*x)/x**3, x)
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx) \sin(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Si(b*x)*sin(b*x)/x^3,x, algorithm="giac")
```

```
[Out] integrate(Si(b*x)*sin(b*x)/x^3, x)
```

3.40 $\int \frac{\sin(bx)\text{Si}(bx)}{x^2} dx$

Optimal. Leaf size=48

$$b\text{CannotIntegrate}\left(\frac{\text{Si}(bx)\cos(bx)}{x}, x\right) + b\text{Si}(2bx) - \frac{\text{Si}(bx)\sin(bx)}{x} - \frac{\sin^2(bx)}{x}$$

[Out] b*CannotIntegrate[(Cos[b*x]*SinIntegral[b*x])/x, x] - Sin[b*x]^2/x - (Sin[b*x]*SinIntegral[b*x])/x + b*SinIntegral[2*b*x]

Rubi [A] time = 0.151637, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\sin(bx)\text{Si}(bx)}{x^2} dx$$

Verification is Not applicable to the result.

[In] Int[(Sin[b*x]*SinIntegral[b*x])/x^2, x]

[Out] -(Sin[b*x]^2/x) - (Sin[b*x]*SinIntegral[b*x])/x + b*SinIntegral[2*b*x] + b*Defer[Int][(Cos[b*x]*SinIntegral[b*x])/x, x]

Rubi steps

$$\begin{aligned} \int \frac{\sin(bx)\text{Si}(bx)}{x^2} dx &= -\frac{\sin(bx)\text{Si}(bx)}{x} + b \int \frac{\sin^2(bx)}{bx^2} dx + b \int \frac{\cos(bx)\text{Si}(bx)}{x} dx \\ &= -\frac{\sin(bx)\text{Si}(bx)}{x} + b \int \frac{\cos(bx)\text{Si}(bx)}{x} dx + \int \frac{\sin^2(bx)}{x^2} dx \\ &= -\frac{\sin^2(bx)}{x} - \frac{\sin(bx)\text{Si}(bx)}{x} + b \int \frac{\cos(bx)\text{Si}(bx)}{x} dx + (2b) \int \frac{\sin(2bx)}{2x} dx \\ &= -\frac{\sin^2(bx)}{x} - \frac{\sin(bx)\text{Si}(bx)}{x} + b \int \frac{\sin(2bx)}{x} dx + b \int \frac{\cos(bx)\text{Si}(bx)}{x} dx \\ &= -\frac{\sin^2(bx)}{x} - \frac{\sin(bx)\text{Si}(bx)}{x} + b\text{Si}(2bx) + b \int \frac{\cos(bx)\text{Si}(bx)}{x} dx \end{aligned}$$

Mathematica [A] time = 0.82105, size = 0, normalized size = 0.

$$\int \frac{\sin(bx)\text{Si}(bx)}{x^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[(Sin[b*x]*SinIntegral[b*x])/x^2, x]

[Out] Integrate[(Sin[b*x]*SinIntegral[b*x])/x^2, x]

Maple [A] time = 0.057, size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)\sin(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(Si(b*x)*sin(b*x)/x^2,x)`

[Out] `int(Si(b*x)*sin(b*x)/x^2,x)`

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx) \sin(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x)*sin(b*x)/x^2,x, algorithm="maxima")`

[Out] `integrate(Si(b*x)*sin(b*x)/x^2, x)`

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\sin(bx) \text{Si}(bx)}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x)*sin(b*x)/x^2,x, algorithm="fricas")`

[Out] `integral(sin(b*x)*sin_integral(b*x)/x^2, x)`

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sin(bx) \text{Si}(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x)*sin(b*x)/x**2,x)`

[Out] `Integral(sin(b*x)*Si(b*x)/x**2, x)`

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx) \sin(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x)*sin(b*x)/x^2,x, algorithm="giac")`

[Out] `integrate(Si(b*x)*sin(b*x)/x^2, x)`

$$3.41 \quad \int \frac{\sin(bx)\text{Si}(bx)}{x} dx$$

Optimal. Leaf size=10

$$\frac{\text{Si}(bx)^2}{2}$$

[Out] SinIntegral[b*x]^2/2

Rubi [A] time = 0.020708, antiderivative size = 10, normalized size of antiderivative = 1., number of steps used = 1, number of rules used = 1, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.083$, Rules used = {6686}

$$\frac{\text{Si}(bx)^2}{2}$$

Antiderivative was successfully verified.

[In] Int[(Sin[b*x]*SinIntegral[b*x])/x,x]

[Out] SinIntegral[b*x]^2/2

Rule 6686

Int[(u_)*(y_)^(m_.), x_Symbol] := With[{q = DerivativeDivides[y, u, x]}, Si mp[(q*y^(m + 1))/(m + 1), x] /; !FalseQ[q]] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{\sin(bx)\text{Si}(bx)}{x} dx = \frac{\text{Si}(bx)^2}{2}$$

Mathematica [C] time = 0.0142256, size = 26, normalized size = 2.6

$$\frac{\text{Si}(bx)^2 \sin(bx)}{2bx \text{sinc}(bx)}$$

Warning: Unable to verify antiderivative.

[In] Integrate[(Sin[b*x]*SinIntegral[b*x])/x,x]

[Out] (Sin[b*x]*SinIntegral[b*x]^2)/(2*b*x*Sinc[b*x])

Maple [A] time = 0.041, size = 9, normalized size = 0.9

$$\frac{(\text{Si}(bx))^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x)*sin(b*x)/x,x)

[Out] $1/2*\text{Si}(b*x)^2$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx) \sin(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x)*sin(b*x)/x,x, algorithm="maxima")`

[Out] `integrate(Si(b*x)*sin(b*x)/x, x)`

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\sin(bx) \text{Si}(bx)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x)*sin(b*x)/x,x, algorithm="fricas")`

[Out] `integral(sin(b*x)*sin_integral(b*x)/x, x)`

Sympy [A] time = 1.06016, size = 7, normalized size = 0.7

$$\frac{\text{Si}^2(bx)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x)*sin(b*x)/x,x)`

[Out] `Si(b*x)**2/2`

Giac [A] time = 1.14573, size = 11, normalized size = 1.1

$$\frac{1}{2} \text{Si}(bx)^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Si(b*x)*sin(b*x)/x,x, algorithm="giac")`

[Out] `1/2*sin_integral(b*x)^2`

3.42 $\int \sin(bx) \mathbf{Si}(bx) dx$

Optimal. Leaf size=26

$$\frac{\mathbf{Si}(2bx)}{2b} - \frac{\mathbf{Si}(bx) \cos(bx)}{b}$$

[Out] $-\left(\frac{\cos[bx] \text{SinIntegral}[bx]}{b}\right) + \frac{\text{SinIntegral}[2bx]}{2b}$

Rubi [A] time = 0.0461413, antiderivative size = 26, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 4, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.444$, Rules used = {6511, 12, 4406, 3299}

$$\frac{\mathbf{Si}(2bx)}{2b} - \frac{\mathbf{Si}(bx) \cos(bx)}{b}$$

Antiderivative was successfully verified.

[In] `Int[Sin[b*x]*SinIntegral[b*x],x]`

[Out] $-\left(\frac{\cos[bx] \text{SinIntegral}[bx]}{b}\right) + \frac{\text{SinIntegral}[2bx]}{2b}$

Rule 6511

```
Int[Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :> -
Simp[(Cos[a + b*x]*SinIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]
]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !Match
Q[u, (b_)*(v_)] /; FreeQ[b, x]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b
_.)*(x_)]^(n_.), x_Symbol] :> Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x
]^(n)*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IG
tQ[p, 0]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int \sin(bx) \operatorname{Si}(bx) dx &= -\frac{\cos(bx) \operatorname{Si}(bx)}{b} + \int \frac{\cos(bx) \sin(bx)}{bx} dx \\
&= -\frac{\cos(bx) \operatorname{Si}(bx)}{b} + \frac{\int \frac{\cos(bx) \sin(bx)}{x} dx}{b} \\
&= -\frac{\cos(bx) \operatorname{Si}(bx)}{b} + \frac{\int \frac{\sin(2bx)}{2x} dx}{b} \\
&= -\frac{\cos(bx) \operatorname{Si}(bx)}{b} + \frac{\int \frac{\sin(2bx)}{x} dx}{2b} \\
&= -\frac{\cos(bx) \operatorname{Si}(bx)}{b} + \frac{\operatorname{Si}(2bx)}{2b}
\end{aligned}$$

Mathematica [A] time = 0.0114716, size = 26, normalized size = 1.

$$\frac{\operatorname{Si}(2bx)}{2b} - \frac{\operatorname{Si}(bx) \cos(bx)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[Sin[b*x]*SinIntegral[b*x],x]

[Out] -((Cos[b*x]*SinIntegral[b*x])/b) + SinIntegral[2*b*x]/(2*b)

Maple [A] time = 0.05, size = 23, normalized size = 0.9

$$\frac{1}{b} \left(-\cos(bx) \operatorname{Si}(bx) + \frac{\operatorname{Si}(2bx)}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x)*sin(b*x),x)

[Out] 1/b*(-cos(b*x)*Si(b*x)+1/2*Si(2*b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \operatorname{Si}(bx) \sin(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x)*sin(b*x),x, algorithm="maxima")

[Out] integrate(Si(b*x)*sin(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}(\sin(bx) \operatorname{Si}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Si(b*x)*sin(b*x),x, algorithm="fricas")
```

```
[Out] integral(sin(b*x)*sin_integral(b*x), x)
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \sin(bx) \operatorname{Si}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Si(b*x)*sin(b*x),x)
```

```
[Out] Integral(sin(b*x)*Si(b*x), x)
```

Giac [C] time = 1.22423, size = 55, normalized size = 2.12

$$-\frac{\cos(bx) \operatorname{Si}(bx)}{b} + \frac{\Im(\operatorname{Ci}(2bx)) - \Im(\operatorname{Ci}(-2bx)) + 2 \operatorname{Si}(2bx)}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Si(b*x)*sin(b*x),x, algorithm="giac")
```

```
[Out] -cos(b*x)*sin_integral(b*x)/b + 1/4*(imag_part(cos_integral(2*b*x)) - imag_
part(cos_integral(-2*b*x)) + 2*sin_integral(2*b*x))/b
```

3.43 $\int x \sin(bx) \mathbf{Si}(bx) dx$

Optimal. Leaf size=61

$$\frac{\text{CosIntegral}(2bx)}{2b^2} + \frac{\text{Si}(bx) \sin(bx)}{b^2} - \frac{\log(x)}{2b^2} + \frac{\sin^2(bx)}{2b^2} - \frac{x \text{Si}(bx) \cos(bx)}{b}$$

[Out] CosIntegral[2*b*x]/(2*b^2) - Log[x]/(2*b^2) + Sin[b*x]^2/(2*b^2) - (x*Cos[b*x]*SinIntegral[b*x])/b + (Sin[b*x]*SinIntegral[b*x])/b^2

Rubi [A] time = 0.0812445, antiderivative size = 61, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 7, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.7$, Rules used = {6513, 12, 2564, 30, 6517, 3312, 3302}

$$\frac{\text{CosIntegral}(2bx)}{2b^2} + \frac{\text{Si}(bx) \sin(bx)}{b^2} - \frac{\log(x)}{2b^2} + \frac{\sin^2(bx)}{2b^2} - \frac{x \text{Si}(bx) \cos(bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[x*Sin[b*x]*SinIntegral[b*x], x]

[Out] CosIntegral[2*b*x]/(2*b^2) - Log[x]/(2*b^2) + Sin[b*x]^2/(2*b^2) - (x*Cos[b*x]*SinIntegral[b*x])/b + (Sin[b*x]*SinIntegral[b*x])/b^2

Rule 6513

Int[((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :> -Simp[((e + f*x)^m*Cos[a + b*x]*SinIntegral[c + d*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*Cos[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Cos[a + b*x]*SinIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 2564

Int[cos[(e_.) + (f_.)*(x_)]^(n_.)*((a_.)*sin[(e_.) + (f_.)*(x_)])^(m_.), x_Symbol] :> Dist[1/(a*f), Subst[Int[x^m*(1 - x^2/a^2)^((n - 1)/2), x], x, a*Sin[e + f*x]], x] /; FreeQ[{a, e, f, m}, x] && IntegerQ[(n - 1)/2] && !(IntegerQ[(m - 1)/2] && LtQ[0, m, n])

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 6517

Int[Cos[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :> Simp[(Sin[a + b*x]*SinIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 3312

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := Int
t[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f
, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int x \sin(bx) \operatorname{Si}(bx) dx &= -\frac{x \cos(bx) \operatorname{Si}(bx)}{b} + \frac{\int \cos(bx) \operatorname{Si}(bx) dx}{b} + \int \frac{\cos(bx) \sin(bx)}{b} dx \\
&= -\frac{x \cos(bx) \operatorname{Si}(bx)}{b} + \frac{\sin(bx) \operatorname{Si}(bx)}{b^2} + \frac{\int \cos(bx) \sin(bx) dx}{b} - \frac{\int \frac{\sin^2(bx)}{bx} dx}{b} \\
&= -\frac{x \cos(bx) \operatorname{Si}(bx)}{b} + \frac{\sin(bx) \operatorname{Si}(bx)}{b^2} - \frac{\int \frac{\sin^2(bx)}{x} dx}{b^2} + \frac{\operatorname{Subst}(\int x dx, x, \sin(bx))}{b^2} \\
&= \frac{\sin^2(bx)}{2b^2} - \frac{x \cos(bx) \operatorname{Si}(bx)}{b} + \frac{\sin(bx) \operatorname{Si}(bx)}{b^2} - \frac{\int \left(\frac{1}{2x} - \frac{\cos(2bx)}{2x} \right) dx}{b^2} \\
&= -\frac{\log(x)}{2b^2} + \frac{\sin^2(bx)}{2b^2} - \frac{x \cos(bx) \operatorname{Si}(bx)}{b} + \frac{\sin(bx) \operatorname{Si}(bx)}{b^2} + \frac{\int \frac{\cos(2bx)}{x} dx}{2b^2} \\
&= \frac{\operatorname{Ci}(2bx)}{2b^2} - \frac{\log(x)}{2b^2} + \frac{\sin^2(bx)}{2b^2} - \frac{x \cos(bx) \operatorname{Si}(bx)}{b} + \frac{\sin(bx) \operatorname{Si}(bx)}{b^2}
\end{aligned}$$

Mathematica [A] time = 0.0789173, size = 44, normalized size = 0.72

$$-\frac{-2\operatorname{CosIntegral}(2bx) + 4\operatorname{Si}(bx)(bx \cos(bx) - \sin(bx)) + \cos(2bx) + 2 \log(x)}{4b^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[x*Sin[b*x]*SinIntegral[b*x], x]
```

```
[Out] -(Cos[2*b*x] - 2*CosIntegral[2*b*x] + 2*Log[x] + 4*(b*x*Cos[b*x] - Sin[b*x])
)*SinIntegral[b*x])/(4*b^2)
```

Maple [A] time = 0.062, size = 58, normalized size = 1.

$$-\frac{x \cos(bx) \operatorname{Si}(bx)}{b} + \frac{\operatorname{Si}(bx) \sin(bx)}{b^2} - \frac{(\cos(bx))^2}{2b^2} - \frac{\ln(bx)}{2b^2} + \frac{\operatorname{Ci}(2bx)}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*Si(b*x)*sin(b*x), x)
```

```
[Out] -x*cos(b*x)*Si(b*x)/b+Si(b*x)*sin(b*x)/b^2-1/2/b^2*cos(b*x)^2-1/2/b^2*ln(b*
x)+1/2*Ci(2*b*x)/b^2
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \operatorname{Si}(bx) \sin(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(b*x)*sin(b*x),x, algorithm="maxima")

[Out] integrate(x*Si(b*x)*sin(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}(x \sin(bx) \operatorname{Si}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(b*x)*sin(b*x),x, algorithm="fricas")

[Out] integral(x*sin(b*x)*sin_integral(b*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \sin(bx) \operatorname{Si}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(b*x)*sin(b*x),x)

[Out] Integral(x*sin(b*x)*Si(b*x), x)

Giac [A] time = 1.16351, size = 62, normalized size = 1.02

$$-\left(\frac{x \cos(bx)}{b} - \frac{\sin(bx)}{b^2}\right) \operatorname{Si}(bx) + \frac{\operatorname{Ci}(2bx) + \operatorname{Ci}(-2bx) - 2 \log(x)}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(b*x)*sin(b*x),x, algorithm="giac")

[Out] -(x*cos(b*x)/b - sin(b*x)/b^2)*sin_integral(b*x) + 1/4*(cos_integral(2*b*x) + cos_integral(-2*b*x) - 2*log(x))/b^2

3.44 $\int x^2 \sin(bx) \text{Si}(bx) dx$

Optimal. Leaf size=91

$$-\frac{\text{Si}(2bx)}{b^3} + \frac{2x\text{Si}(bx)\sin(bx)}{b^2} + \frac{2\text{Si}(bx)\cos(bx)}{b^3} - \frac{5x}{4b^2} + \frac{x\sin^2(bx)}{2b^2} + \frac{5\sin(bx)\cos(bx)}{4b^3} - \frac{x^2\text{Si}(bx)\cos(bx)}{b}$$

[Out] $(-5*x)/(4*b^2) + (5*\text{Cos}[b*x]*\text{Sin}[b*x])/(4*b^3) + (x*\text{Sin}[b*x]^2)/(2*b^2) + (2*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b^3 - (x^2*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b + (2*x*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b^2 - \text{SinIntegral}[2*b*x]/b^3$

Rubi [A] time = 0.111096, antiderivative size = 91, normalized size of antiderivative = 1., number of steps used = 14, number of rules used = 9, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.75$, Rules used = {6513, 12, 3443, 2635, 8, 6519, 6511, 4406, 3299}

$$-\frac{\text{Si}(2bx)}{b^3} + \frac{2x\text{Si}(bx)\sin(bx)}{b^2} + \frac{2\text{Si}(bx)\cos(bx)}{b^3} - \frac{5x}{4b^2} + \frac{x\sin^2(bx)}{2b^2} + \frac{5\sin(bx)\cos(bx)}{4b^3} - \frac{x^2\text{Si}(bx)\cos(bx)}{b}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2*\text{Sin}[b*x]*\text{SinIntegral}[b*x], x]$

[Out] $(-5*x)/(4*b^2) + (5*\text{Cos}[b*x]*\text{Sin}[b*x])/(4*b^3) + (x*\text{Sin}[b*x]^2)/(2*b^2) + (2*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b^3 - (x^2*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b + (2*x*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b^2 - \text{SinIntegral}[2*b*x]/b^3$

Rule 6513

$\text{Int}[(e_.) + (f_.)*(x_.)]^{(m_.)}*\text{Sin}[(a_.) + (b_.)*(x_.)]*\text{SinIntegral}[(c_.) + (d_.)*(x_.)], x_Symbol] \rightarrow -\text{Simp}[(e + f*x)^m*\text{Cos}[a + b*x]*\text{SinIntegral}[c + d*x])/b, x] + (\text{Dist}[d/b, \text{Int}[(e + f*x)^m*\text{Cos}[a + b*x]*\text{Sin}[c + d*x]]/(c + d*x), x], x] + \text{Dist}[(f*m)/b, \text{Int}[(e + f*x)^{m-1}*\text{Cos}[a + b*x]*\text{SinIntegral}[c + d*x], x], x] /; \text{FreeQ}\{a, b, c, d, e, f\}, x] \&\& \text{IGtQ}[m, 0]$

Rule 12

$\text{Int}[(a_)*(u_), x_Symbol] \rightarrow \text{Dist}[a, \text{Int}[u, x], x] /; \text{FreeQ}[a, x] \&\& !\text{MatchQ}[u, (b_)*(v_)] /; \text{FreeQ}[b, x]$

Rule 3443

$\text{Int}[\text{Cos}[(a_.) + (b_.)*(x_.)]^{(n_.)}*(x_.)^{(m_.)}*\text{Sin}[(a_.) + (b_.)*(x_.)]^{(p_.)}, x_Symbol] \rightarrow \text{Simp}[(x^{m-n+1}*\text{Sin}[a + b*x^n]^{p+1})/(b*n*(p+1)), x] - \text{Dist}[(m-n+1)/(b*n*(p+1)), \text{Int}[x^{m-n}*\text{Sin}[a + b*x^n]^{p+1}], x], x] /; \text{FreeQ}\{a, b, p\}, x] \&\& \text{LtQ}[0, n, m+1] \&\& \text{NeQ}[p, -1]$

Rule 2635

$\text{Int}[(b_.)*\text{sin}[(c_.) + (d_.)*(x_.)]^{(n_.)}, x_Symbol] \rightarrow -\text{Simp}[(b*\text{Cos}[c + d*x] * (b*\text{Sin}[c + d*x])^{n-1})/(d*n), x] + \text{Dist}[(b^2*(n-1))/n, \text{Int}[(b*\text{Sin}[c + d*x])^{n-2}], x], x] /; \text{FreeQ}\{b, c, d\}, x] \&\& \text{GtQ}[n, 1] \&\& \text{IntegerQ}[2*n]$

Rule 8

$\text{Int}[a_, x_Symbol] \rightarrow \text{Simp}[a*x, x] /; \text{FreeQ}[a, x]$

Rule 6519

```
Int[Cos[(a_.) + (b_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.)*SinIntegral[(c_.) +
(d_.)*(x_)], x_Symbol] := Simp[((e + f*x)^m*Sin[a + b*x]*SinIntegral[c + d*
x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*Sin[a + b*x]*Sin[c + d*x])/(c + d*
x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Sin[a + b*x]*SinIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 6511

```
Int[Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := -
Simp[(Cos[a + b*x]*SinIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x
]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b
_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x
]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IG
tQ[p, 0]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int x^2 \sin(bx) \text{Si}(bx) dx &= -\frac{x^2 \cos(bx) \text{Si}(bx)}{b} + \frac{2 \int x \cos(bx) \text{Si}(bx) dx}{b} + \int \frac{x \cos(bx) \sin(bx)}{b} dx \\
&= -\frac{x^2 \cos(bx) \text{Si}(bx)}{b} + \frac{2x \sin(bx) \text{Si}(bx)}{b^2} - \frac{2 \int \sin(bx) \text{Si}(bx) dx}{b^2} + \frac{\int x \cos(bx) \sin(bx) dx}{b} - \frac{2 \int \sin^2(bx) dx}{b^2} \\
&= \frac{x \sin^2(bx)}{2b^2} + \frac{2 \cos(bx) \text{Si}(bx)}{b^3} - \frac{x^2 \cos(bx) \text{Si}(bx)}{b} + \frac{2x \sin(bx) \text{Si}(bx)}{b^2} - \frac{\int \sin^2(bx) dx}{2b^2} - \frac{2 \int \sin(bx) \text{Si}(bx) dx}{b^2} \\
&= \frac{5 \cos(bx) \sin(bx)}{4b^3} + \frac{x \sin^2(bx)}{2b^2} + \frac{2 \cos(bx) \text{Si}(bx)}{b^3} - \frac{x^2 \cos(bx) \text{Si}(bx)}{b} + \frac{2x \sin(bx) \text{Si}(bx)}{b^2} - \frac{2 \int \sin(bx) \text{Si}(bx) dx}{b^2} \\
&= -\frac{5x}{4b^2} + \frac{5 \cos(bx) \sin(bx)}{4b^3} + \frac{x \sin^2(bx)}{2b^2} + \frac{2 \cos(bx) \text{Si}(bx)}{b^3} - \frac{x^2 \cos(bx) \text{Si}(bx)}{b} + \frac{2x \sin(bx) \text{Si}(bx)}{b^2} \\
&= -\frac{5x}{4b^2} + \frac{5 \cos(bx) \sin(bx)}{4b^3} + \frac{x \sin^2(bx)}{2b^2} + \frac{2 \cos(bx) \text{Si}(bx)}{b^3} - \frac{x^2 \cos(bx) \text{Si}(bx)}{b} + \frac{2x \sin(bx) \text{Si}(bx)}{b^2} \\
&= -\frac{5x}{4b^2} + \frac{5 \cos(bx) \sin(bx)}{4b^3} + \frac{x \sin^2(bx)}{2b^2} + \frac{2 \cos(bx) \text{Si}(bx)}{b^3} - \frac{x^2 \cos(bx) \text{Si}(bx)}{b} + \frac{2x \sin(bx) \text{Si}(bx)}{b^2}
\end{aligned}$$

Mathematica [A] time = 0.103689, size = 64, normalized size = 0.7

$$\frac{8\text{Si}(bx) \left((b^2 x^2 - 2) \cos(bx) - 2bx \sin(bx) \right) + 8\text{Si}(2bx) + 8bx - 5 \sin(2bx) + 2bx \cos(2bx)}{8b^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*Sin[b*x]*SinIntegral[b*x],x]
```

```
[Out] -(8*b*x + 2*b*x*Cos[2*b*x] - 5*Sin[2*b*x] + 8*((-2 + b^2*x^2)*Cos[b*x] - 2*
b*x*Sin[b*x])*SinIntegral[b*x] + 8*SinIntegral[2*b*x])/(8*b^3)
```

Maple [A] time = 0.059, size = 69, normalized size = 0.8

$$\frac{1}{b^3} \left(\text{Si}(bx) \left(-b^2 x^2 \cos(bx) + 2 \cos(bx) + 2 \sin(bx) bx \right) - \frac{bx (\cos(bx))^2}{2} + \frac{5 \sin(bx) \cos(bx)}{4} - \frac{3bx}{4} - \text{Si}(2bx) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*Si(b*x)*sin(b*x), x)

[Out] 1/b^3*(Si(b*x)*(-b^2*x^2*cos(b*x)+2*cos(b*x)+2*sin(b*x)*b*x)-1/2*b*x*cos(b*x)^2+5/4*sin(b*x)*cos(b*x)-3/4*b*x-Si(2*b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Si}(bx) \sin(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Si(b*x)*sin(b*x), x, algorithm="maxima")

[Out] integrate(x^2*Si(b*x)*sin(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^2 \sin(bx) \text{Si}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Si(b*x)*sin(b*x), x, algorithm="fricas")

[Out] integral(x^2*sin(b*x)*sin_integral(b*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \sin(bx) \text{Si}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*Si(b*x)*sin(b*x), x)

[Out] Integral(x**2*sin(b*x)*Si(b*x), x)

Giac [C] time = 1.16074, size = 89, normalized size = 0.98

$$\left(\frac{2x \sin(bx)}{b^2} - \frac{(b^2 x^2 - 2) \cos(bx)}{b^3} \right) \text{Si}(bx) - \frac{2bx + \Im(\text{Ci}(2bx)) - \Im(\text{Ci}(-2bx)) + 2 \text{Si}(2bx)}{2b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*Si(b*x)*sin(b*x),x, algorithm="giac")
```

```
[Out] (2*x*sin(b*x)/b^2 - (b^2*x^2 - 2)*cos(b*x)/b^3)*sin_integral(b*x) - 1/2*(2*  
b*x + imag_part(cos_integral(2*b*x)) - imag_part(cos_integral(-2*b*x)) + 2*  
sin_integral(2*b*x))/b^3
```

3.45 $\int x^3 \sin(bx) \mathbf{Si}(bx) dx$

Optimal. Leaf size=126

$$-\frac{3\text{CosIntegral}(2bx)}{b^4} + \frac{3x^2\text{Si}(bx)\sin(bx)}{b^2} - \frac{6\text{Si}(bx)\sin(bx)}{b^4} + \frac{6x\text{Si}(bx)\cos(bx)}{b^3} - \frac{x^2}{b^2} + \frac{x^2\sin^2(bx)}{2b^2} + \frac{3\log(x)}{b^4} - \frac{4\sin^2}{b^4}$$

[Out] $-(x^2/b^2) - (3*\text{CosIntegral}[2*b*x])/b^4 + (3*\text{Log}[x])/b^4 + (2*x*\text{Cos}[b*x]*\text{Sin}[b*x])/b^3 - (4*\text{Sin}[b*x]^2)/b^4 + (x^2*\text{Sin}[b*x]^2)/(2*b^2) + (6*x*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b^3 - (x^3*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b - (6*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b^4 + (3*x^2*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b^2$

Rubi [A] time = 0.193518, antiderivative size = 126, normalized size of antiderivative = 1., number of steps used = 18, number of rules used = 10, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.833$, Rules used = {6513, 12, 3443, 3310, 30, 6519, 2564, 6517, 3312, 3302}

$$-\frac{3\text{CosIntegral}(2bx)}{b^4} + \frac{3x^2\text{Si}(bx)\sin(bx)}{b^2} - \frac{6\text{Si}(bx)\sin(bx)}{b^4} + \frac{6x\text{Si}(bx)\cos(bx)}{b^3} - \frac{x^2}{b^2} + \frac{x^2\sin^2(bx)}{2b^2} + \frac{3\log(x)}{b^4} - \frac{4\sin^2}{b^4}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^3*\text{Sin}[b*x]*\text{SinIntegral}[b*x], x]$

[Out] $-(x^2/b^2) - (3*\text{CosIntegral}[2*b*x])/b^4 + (3*\text{Log}[x])/b^4 + (2*x*\text{Cos}[b*x]*\text{Sin}[b*x])/b^3 - (4*\text{Sin}[b*x]^2)/b^4 + (x^2*\text{Sin}[b*x]^2)/(2*b^2) + (6*x*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b^3 - (x^3*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b - (6*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b^4 + (3*x^2*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b^2$

Rule 6513

$\text{Int}[(e_. + (f_.)*(x_.))^(m_.)*\text{Sin}[(a_.) + (b_.)*(x_.)]*\text{SinIntegral}[(c_.) + (d_.)*(x_.)], x_Symbol] \rightarrow -\text{Simp}[(e + f*x)^m*\text{Cos}[a + b*x]*\text{SinIntegral}[c + d*x])/b, x] + (\text{Dist}[d/b, \text{Int}[(e + f*x)^m*\text{Cos}[a + b*x]*\text{Sin}[c + d*x]]/(c + d*x), x], x] + \text{Dist}[(f*m)/b, \text{Int}[(e + f*x)^(m - 1)*\text{Cos}[a + b*x]*\text{SinIntegral}[c + d*x], x], x] /; \text{FreeQ}\{a, b, c, d, e, f\}, x] \&\& \text{IGtQ}[m, 0]$

Rule 12

$\text{Int}[(a_)*(u_), x_Symbol] \rightarrow \text{Dist}[a, \text{Int}[u, x], x] /; \text{FreeQ}[a, x] \&\& !\text{MatchQ}[u, (b_)*(v_)] /; \text{FreeQ}[b, x]$

Rule 3443

$\text{Int}[\text{Cos}[(a_.) + (b_.)*(x_.)^(n_.)]*(x_.)^(m_.)*\text{Sin}[(a_.) + (b_.)*(x_.)^(n_.)]^(p_.), x_Symbol] \rightarrow \text{Simp}[(x^(m - n + 1)*\text{Sin}[a + b*x^n]^(p + 1))/(b*n*(p + 1)), x] - \text{Dist}[(m - n + 1)/(b*n*(p + 1)), \text{Int}[x^(m - n)*\text{Sin}[a + b*x^n]^(p + 1), x], x] /; \text{FreeQ}\{a, b, p\}, x] \&\& \text{LtQ}[0, n, m + 1] \&\& \text{NeQ}[p, -1]$

Rule 3310

$\text{Int}[(c_. + (d_.)*(x_.))*((b_.)*\text{sin}[(e_.) + (f_.)*(x_.)])^(n_), x_Symbol] \rightarrow \text{Simp}[(d*(b*\text{Sin}[e + f*x])^n)/(f^2*n^2), x] + (\text{Dist}[(b^2*(n - 1))/n, \text{Int}[(c + d*x)*(b*\text{Sin}[e + f*x])^(n - 2), x], x] - \text{Simp}[(b*(c + d*x)*\text{Cos}[e + f*x]*(b*\text{Sin}[e + f*x])^(n - 1))/(f*n), x]) /; \text{FreeQ}\{b, c, d, e, f\}, x] \&\& \text{GtQ}[n, 1]$

Rule 30

Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 6519

Int[Cos[(a_) + (b_)*(x_)]*((e_) + (f_)*(x_))^(m_)*SinIntegral[(c_) + (d_)*(x_)], x_Symbol] := Simp[((e + f*x)^m*Sin[a + b*x]*SinIntegral[c + d*x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*Sin[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Sin[a + b*x]*SinIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]

Rule 2564

Int[cos[(e_) + (f_)*(x_)]^(n_)*((a_)*sin[(e_) + (f_)*(x_)])^(m_), x_Symbol] := Dist[1/(a*f), Subst[Int[x^m*(1 - x^2/a^2)^((n - 1)/2), x], x, a*Sin[e + f*x]], x] /; FreeQ[{a, e, f, m}, x] && IntegerQ[(n - 1)/2] && !(IntegerQ[(m - 1)/2] && LtQ[0, m, n])

Rule 6517

Int[Cos[(a_) + (b_)*(x_)]*SinIntegral[(c_) + (d_)*(x_)], x_Symbol] := Simp[(Sin[a + b*x]*SinIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 3312

Int[((c_) + (d_)*(x_))^(m_)*sin[(e_) + (f_)*(x_)]^(n_), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3302

Int[sin[(e_) + (f_)*(x_)]/((c_) + (d_)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned}
 \int x^3 \sin(bx) \text{Si}(bx) dx &= -\frac{x^3 \cos(bx) \text{Si}(bx)}{b} + \frac{3 \int x^2 \cos(bx) \text{Si}(bx) dx}{b} + \int \frac{x^2 \cos(bx) \sin(bx)}{b} dx \\
 &= -\frac{x^3 \cos(bx) \text{Si}(bx)}{b} + \frac{3x^2 \sin(bx) \text{Si}(bx)}{b^2} - \frac{6 \int x \sin(bx) \text{Si}(bx) dx}{b^2} + \frac{\int x^2 \cos(bx) \sin(bx) dx}{b} \\
 &= \frac{x^2 \sin^2(bx)}{2b^2} + \frac{6x \cos(bx) \text{Si}(bx)}{b^3} - \frac{x^3 \cos(bx) \text{Si}(bx)}{b} + \frac{3x^2 \sin(bx) \text{Si}(bx)}{b^2} - \frac{6 \int \cos(bx) \text{Si}(bx) dx}{b^3} \\
 &= \frac{2x \cos(bx) \sin(bx)}{b^3} - \frac{\sin^2(bx)}{b^4} + \frac{x^2 \sin^2(bx)}{2b^2} + \frac{6x \cos(bx) \text{Si}(bx)}{b^3} - \frac{x^3 \cos(bx) \text{Si}(bx)}{b} - \frac{6 \sin(bx) \text{Si}(bx)}{b} \\
 &= -\frac{x^2}{b^2} + \frac{2x \cos(bx) \sin(bx)}{b^3} - \frac{\sin^2(bx)}{b^4} + \frac{x^2 \sin^2(bx)}{2b^2} + \frac{6x \cos(bx) \text{Si}(bx)}{b^3} - \frac{x^3 \cos(bx) \text{Si}(bx)}{b} \\
 &= -\frac{x^2}{b^2} + \frac{2x \cos(bx) \sin(bx)}{b^3} - \frac{4 \sin^2(bx)}{b^4} + \frac{x^2 \sin^2(bx)}{2b^2} + \frac{6x \cos(bx) \text{Si}(bx)}{b^3} - \frac{x^3 \cos(bx) \text{Si}(bx)}{b} \\
 &= -\frac{x^2}{b^2} + \frac{3 \log(x)}{b^4} + \frac{2x \cos(bx) \sin(bx)}{b^3} - \frac{4 \sin^2(bx)}{b^4} + \frac{x^2 \sin^2(bx)}{2b^2} + \frac{6x \cos(bx) \text{Si}(bx)}{b^3} - \frac{x^3 \cos(bx) \text{Si}(bx)}{b} \\
 &= -\frac{x^2}{b^2} - \frac{3 \text{Ci}(2bx)}{b^4} + \frac{3 \log(x)}{b^4} + \frac{2x \cos(bx) \sin(bx)}{b^3} - \frac{4 \sin^2(bx)}{b^4} + \frac{x^2 \sin^2(bx)}{2b^2} + \frac{6x \cos(bx) \text{Si}(bx)}{b^3} - \frac{x^3 \cos(bx) \text{Si}(bx)}{b}
 \end{aligned}$$

Mathematica [A] time = 0.176824, size = 93, normalized size = 0.74

$$\frac{4\text{Si}(bx) \left(bx (b^2x^2 - 6) \cos(bx) - 3 (b^2x^2 - 2) \sin(bx) \right) + 3b^2x^2 + b^2x^2 \cos(2bx) + 12\text{CosIntegral}(2bx) - 4bx \sin(2bx) - 2\text{Log}[x] - 4bx \sin(2bx) + 4(bx(-6 + b^2x^2)\cos[bx] - 3(-2 + b^2x^2)\sin[bx])\text{SinIntegral}[bx]}{4b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*Sin[b*x]*SinIntegral[b*x],x]

[Out] $-(3b^2x^2 - 8\text{Cos}[2bx] + b^2x^2\text{Cos}[2bx] + 12\text{CosIntegral}[2bx] - 12\text{Log}[x] - 4bx\sin(2bx) + 4(bx(-6 + b^2x^2)\cos[bx] - 3(-2 + b^2x^2)\sin[bx])\text{SinIntegral}[bx])/(4b^4)$

Maple [A] time = 0.059, size = 138, normalized size = 1.1

$$-\frac{x^3 \cos(bx) \text{Si}(bx)}{b} + 3 \frac{x^2 \text{Si}(bx) \sin(bx)}{b^2} + 6 \frac{x \cos(bx) \text{Si}(bx)}{b^3} - 6 \frac{\text{Si}(bx) \sin(bx)}{b^4} - \frac{x^2 (\cos(bx))^2}{2b^2} + 2 \frac{x \cos(bx) \sin(bx)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*Si(b*x)*sin(b*x),x)

[Out] $-x^3 \cos(bx) \text{Si}(bx)/b + 3x^2 \text{Si}(bx) \sin(bx)/b^2 + 6x \cos(bx) \text{Si}(bx)/b^3 - 6 \text{Si}(bx) \sin(bx)/b^4 - 1/2 \cdot x^2 \cos^2(bx)/b^2 + x \cos(bx) \sin(bx)/b^3 - 1/2 \cdot x^2 \sin^2(bx)/b^2 + 3 \cos^2(bx)/b^4 + 3/b^4 \ln(bx) - 3 \text{Ci}(2bx)/b^4$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \text{Si}(bx) \sin(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Si(b*x)*sin(b*x),x, algorithm="maxima")

[Out] integrate(x^3*Si(b*x)*sin(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^3 \sin(bx) \text{Si}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Si(b*x)*sin(b*x),x, algorithm="fricas")

[Out] integral(x^3*sin(b*x)*sin_integral(b*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \sin(bx) \text{Si}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*Si(b*x)*sin(b*x), x)

[Out] Integral(x**3*sin(b*x)*Si(b*x), x)

Giac [A] time = 1.17674, size = 104, normalized size = 0.83

$$-\left(\frac{(b^3x^3 - 6bx)\cos(bx)}{b^4} - \frac{3(b^2x^2 - 2)\sin(bx)}{b^4}\right)\text{Si}(bx) - \frac{3(b^2x^2 + 2\text{Ci}(2bx) + 2\text{Ci}(-2bx) - 4\log(x))}{4b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Si(b*x)*sin(b*x), x, algorithm="giac")

[Out] -((b^3*x^3 - 6*b*x)*cos(b*x)/b^4 - 3*(b^2*x^2 - 2)*sin(b*x)/b^4)*sin_integr
al(b*x) - 3/4*(b^2*x^2 + 2*cos_integral(2*b*x) + 2*cos_integral(-2*b*x) - 4
*log(x))/b^4

3.46 $\int \frac{\cos(bx)\text{Si}(bx)}{x^3} dx$

Optimal. Leaf size=102

$$-\frac{1}{2}b^2\text{CannotIntegrate}\left(\frac{\text{Si}(bx)\cos(bx)}{x}, x\right) - b^2\text{Si}(2bx) - \frac{\text{Si}(bx)\cos(bx)}{2x^2} + \frac{b\text{Si}(bx)\sin(bx)}{2x} - \frac{\sin(2bx)}{8x^2} + \frac{b\sin^2(bx)}{2x} - \frac{b}{2}$$

[Out] $-(b^2*\text{CannotIntegrate}[(\text{Cos}[b*x]*\text{SinIntegral}[b*x])/x, x])/2 - (b*\text{Cos}[2*b*x])/(4*x) + (b*\text{Sin}[b*x]^2)/(2*x) - \text{Sin}[2*b*x]/(8*x^2) - (\text{Cos}[b*x]*\text{SinIntegral}[b*x])/(2*x^2) + (b*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/(2*x) - b^2*\text{SinIntegral}[2*b*x]$

Rubi [A] time = 0.188222, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\cos(bx)\text{Si}(bx)}{x^3} dx$$

Verification is Not applicable to the result.

[In] $\text{Int}[(\text{Cos}[b*x]*\text{SinIntegral}[b*x])/x^3, x]$

[Out] $-(b*\text{Cos}[2*b*x])/(4*x) + (b*\text{Sin}[b*x]^2)/(2*x) - \text{Sin}[2*b*x]/(8*x^2) - (\text{Cos}[b*x]*\text{SinIntegral}[b*x])/(2*x^2) + (b*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/(2*x) - b^2*\text{SinIntegral}[2*b*x] - (b^2*\text{Defer}[\text{Int}[(\text{Cos}[b*x]*\text{SinIntegral}[b*x])/x, x])/2$

Rubi steps

$$\begin{aligned} \int \frac{\cos(bx)\text{Si}(bx)}{x^3} dx &= -\frac{\cos(bx)\text{Si}(bx)}{2x^2} + \frac{1}{2}b \int \frac{\cos(bx)\sin(bx)}{bx^3} dx - \frac{1}{2}b \int \frac{\sin(bx)\text{Si}(bx)}{x^2} dx \\ &= -\frac{\cos(bx)\text{Si}(bx)}{2x^2} + \frac{b\sin(bx)\text{Si}(bx)}{2x} + \frac{1}{2} \int \frac{\cos(bx)\sin(bx)}{x^3} dx - \frac{1}{2}b^2 \int \frac{\sin^2(bx)}{bx^2} dx - \frac{1}{2}b^2 \int \frac{\cos(bx)\text{Si}(bx)}{x} dx \\ &= -\frac{\cos(bx)\text{Si}(bx)}{2x^2} + \frac{b\sin(bx)\text{Si}(bx)}{2x} + \frac{1}{2} \int \frac{\sin(2bx)}{2x^3} dx - \frac{1}{2}b \int \frac{\sin^2(bx)}{x^2} dx - \frac{1}{2}b^2 \int \frac{\cos(bx)\text{Si}(bx)}{x} dx \\ &= \frac{b\sin^2(bx)}{2x} - \frac{\cos(bx)\text{Si}(bx)}{2x^2} + \frac{b\sin(bx)\text{Si}(bx)}{2x} + \frac{1}{4} \int \frac{\sin(2bx)}{x^3} dx - \frac{1}{2}b^2 \int \frac{\cos(bx)\text{Si}(bx)}{x} dx - b^2 \int \frac{\sin^2(bx)}{2x} dx \\ &= \frac{b\sin^2(bx)}{2x} - \frac{\sin(2bx)}{8x^2} - \frac{\cos(bx)\text{Si}(bx)}{2x^2} + \frac{b\sin(bx)\text{Si}(bx)}{2x} + \frac{1}{4}b \int \frac{\cos(2bx)}{x^2} dx - \frac{1}{2}b^2 \int \frac{\sin(2bx)}{x} dx \\ &= -\frac{b\cos(2bx)}{4x} + \frac{b\sin^2(bx)}{2x} - \frac{\sin(2bx)}{8x^2} - \frac{\cos(bx)\text{Si}(bx)}{2x^2} + \frac{b\sin(bx)\text{Si}(bx)}{2x} - \frac{1}{2}b^2\text{Si}(2bx) - \frac{1}{2}b^2 \int \frac{\sin(2bx)}{x} dx \\ &= -\frac{b\cos(2bx)}{4x} + \frac{b\sin^2(bx)}{2x} - \frac{\sin(2bx)}{8x^2} - \frac{\cos(bx)\text{Si}(bx)}{2x^2} + \frac{b\sin(bx)\text{Si}(bx)}{2x} - b^2\text{Si}(2bx) - \frac{1}{2}b^2 \int \frac{\cos(2bx)}{x} dx \end{aligned}$$

Mathematica [A] time = 0.828828, size = 0, normalized size = 0.

$$\int \frac{\cos(bx)\text{Si}(bx)}{x^3} dx$$

Verification is Not applicable to the result.

[In] $\text{Integrate}[(\text{Cos}[b*x]*\text{SinIntegral}[b*x])/x^3, x]$

[Out] Integrate[(Cos[b*x]*SinIntegral[b*x])/x^3, x]

Maple [A] time = 0.084, size = 0, normalized size = 0.

$$\int \frac{\cos(bx) \operatorname{Si}(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(b*x)*Si(b*x)/x^3,x)

[Out] int(cos(b*x)*Si(b*x)/x^3,x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{Si}(bx) \cos(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x)*Si(b*x)/x^3,x, algorithm="maxima")

[Out] integrate(Si(b*x)*cos(b*x)/x^3, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}\left(\frac{\cos(bx) \operatorname{Si}(bx)}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x)*Si(b*x)/x^3,x, algorithm="fricas")

[Out] integral(cos(b*x)*sin_integral(b*x)/x^3, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\cos(bx) \operatorname{Si}(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x)*Si(b*x)/x**3,x)

[Out] Integral(cos(b*x)*Si(b*x)/x**3, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{Si}(bx) \cos(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(b*x)*Si(b*x)/x^3,x, algorithm="giac")
```

```
[Out] integrate(Si(b*x)*cos(b*x)/x^3, x)
```

$$3.47 \quad \int \frac{\cos(bx)\text{Si}(bx)}{x^2} dx$$

Optimal. Leaf size=44

$$b\text{CosIntegral}(2bx) - \frac{1}{2}b\text{Si}(bx)^2 - \frac{\text{Si}(bx)\cos(bx)}{x} - \frac{\sin(2bx)}{2x}$$

[Out] b*CosIntegral[2*b*x] - Sin[2*b*x]/(2*x) - (Cos[b*x]*SinIntegral[b*x])/x - (b*SinIntegral[b*x]^2)/2

Rubi [A] time = 0.0946792, antiderivative size = 44, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 6, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {6521, 6686, 12, 4406, 3297, 3302}

$$b\text{CosIntegral}(2bx) - \frac{1}{2}b\text{Si}(bx)^2 - \frac{\text{Si}(bx)\cos(bx)}{x} - \frac{\sin(2bx)}{2x}$$

Antiderivative was successfully verified.

[In] Int[(Cos[b*x]*SinIntegral[b*x])/x^2,x]

[Out] b*CosIntegral[2*b*x] - Sin[2*b*x]/(2*x) - (Cos[b*x]*SinIntegral[b*x])/x - (b*SinIntegral[b*x]^2)/2

Rule 6521

```
Int[Cos[(a_.) + (b_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.)*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := Simp[((e + f*x)^(m + 1)*Cos[a + b*x]*SinIntegral[c + d*x])/(f*(m + 1)), x] + (Dist[b/(f*(m + 1)), Int[(e + f*x)^(m + 1)*Sin[a + b*x]*SinIntegral[c + d*x], x], x] - Dist[d/(f*(m + 1)), Int[((e + f*x)^(m + 1)*Cos[a + b*x]*Sin[c + d*x])/(c + d*x), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && ILtQ[m, -1]
```

Rule 6686

```
Int[(u_)*(y_)^(m_.), x_Symbol] := With[{q = DerivativeDivides[y, u, x]}, Simp[(q*y^(m + 1))/(m + 1), x] /; !FalseQ[q]] /; FreeQ[m, x] && NeQ[m, -1]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 3297

```
Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)], x_Symbol] := Simp[((c + d*x)^(m + 1)*Sin[e + f*x])/(d*(m + 1)), x] - Dist[f/(d*(m + 1)), Int[(c + d*x)^(m + 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && LtQ[m, -1]
```

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned}
 \int \frac{\cos(bx)\text{Si}(bx)}{x^2} dx &= -\frac{\cos(bx)\text{Si}(bx)}{x} + b \int \frac{\cos(bx)\sin(bx)}{bx^2} dx - b \int \frac{\sin(bx)\text{Si}(bx)}{x} dx \\
 &= -\frac{\cos(bx)\text{Si}(bx)}{x} - \frac{1}{2}b\text{Si}(bx)^2 + \int \frac{\cos(bx)\sin(bx)}{x^2} dx \\
 &= -\frac{\cos(bx)\text{Si}(bx)}{x} - \frac{1}{2}b\text{Si}(bx)^2 + \int \frac{\sin(2bx)}{2x^2} dx \\
 &= -\frac{\cos(bx)\text{Si}(bx)}{x} - \frac{1}{2}b\text{Si}(bx)^2 + \frac{1}{2} \int \frac{\sin(2bx)}{x^2} dx \\
 &= -\frac{\sin(2bx)}{2x} - \frac{\cos(bx)\text{Si}(bx)}{x} - \frac{1}{2}b\text{Si}(bx)^2 + b \int \frac{\cos(2bx)}{x} dx \\
 &= b\text{Ci}(2bx) - \frac{\sin(2bx)}{2x} - \frac{\cos(bx)\text{Si}(bx)}{x} - \frac{1}{2}b\text{Si}(bx)^2
 \end{aligned}$$

Mathematica [F] time = 0.617386, size = 0, normalized size = 0.

$$\int \frac{\cos(bx)\text{Si}(bx)}{x^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[(Cos[b*x]*SinIntegral[b*x])/x^2,x]

[Out] Integrate[(Cos[b*x]*SinIntegral[b*x])/x^2, x]

Maple [F] time = 0.062, size = 0, normalized size = 0.

$$\int \frac{\cos(bx)\text{Si}(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(b*x)*Si(b*x)/x^2,x)

[Out] int(cos(b*x)*Si(b*x)/x^2,x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)\cos(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x)*Si(b*x)/x^2,x, algorithm="maxima")

[Out] integrate(Si(b*x)*cos(b*x)/x^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\cos(bx)\text{Si}(bx)}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x)*Si(b*x)/x^2,x, algorithm="fricas")

[Out] integral(cos(b*x)*sin_integral(b*x)/x^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\cos(bx)\text{Si}(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x)*Si(b*x)/x**2,x)

[Out] Integral(cos(b*x)*Si(b*x)/x**2, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx)\cos(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x)*Si(b*x)/x^2,x, algorithm="giac")

[Out] integrate(Si(b*x)*cos(b*x)/x^2, x)

$$3.48 \quad \int \frac{\cos(bx)\text{Si}(bx)}{x} dx$$

Optimal. Leaf size=14

$$\text{CannotIntegrate}\left(\frac{\text{Si}(bx)\cos(bx)}{x}, x\right)$$

[Out] CannotIntegrate[(Cos[b*x]*SinIntegral[b*x])/x, x]

Rubi [A] time = 0.0258647, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\cos(bx)\text{Si}(bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Int[(Cos[b*x]*SinIntegral[b*x])/x, x]

[Out] Defer[Int] [(Cos[b*x]*SinIntegral[b*x])/x, x]

Rubi steps

$$\int \frac{\cos(bx)\text{Si}(bx)}{x} dx = \int \frac{\cos(bx)\text{Si}(bx)}{x} dx$$

Mathematica [A] time = 0.953999, size = 0, normalized size = 0.

$$\int \frac{\cos(bx)\text{Si}(bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[(Cos[b*x]*SinIntegral[b*x])/x, x]

[Out] Integrate[(Cos[b*x]*SinIntegral[b*x])/x, x]

Maple [A] time = 0.056, size = 0, normalized size = 0.

$$\int \frac{\cos(bx)\text{Si}(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(b*x)*Si(b*x)/x, x)

[Out] int(cos(b*x)*Si(b*x)/x, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx) \cos(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x)*Si(b*x)/x,x, algorithm="maxima")

[Out] integrate(Si(b*x)*cos(b*x)/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\cos(bx) \text{Si}(bx)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x)*Si(b*x)/x,x, algorithm="fricas")

[Out] integral(cos(b*x)*sin_integral(b*x)/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\cos(bx) \text{Si}(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x)*Si(b*x)/x,x)

[Out] Integral(cos(b*x)*Si(b*x)/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx) \cos(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x)*Si(b*x)/x,x, algorithm="giac")

[Out] integrate(Si(b*x)*cos(b*x)/x, x)

3.49 $\int \cos(bx)\mathbf{Si}(bx) dx$

Optimal. Leaf size=34

$$\frac{\text{CosIntegral}(2bx)}{2b} + \frac{\text{Si}(bx)\sin(bx)}{b} - \frac{\log(x)}{2b}$$

[Out] CosIntegral[2*b*x]/(2*b) - Log[x]/(2*b) + (Sin[b*x]*SinIntegral[b*x])/b

Rubi [A] time = 0.0577979, antiderivative size = 34, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 4, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.444$, Rules used = {6517, 12, 3312, 3302}

$$\frac{\text{CosIntegral}(2bx)}{2b} + \frac{\text{Si}(bx)\sin(bx)}{b} - \frac{\log(x)}{2b}$$

Antiderivative was successfully verified.

[In] Int[Cos[b*x]*SinIntegral[b*x],x]

[Out] CosIntegral[2*b*x]/(2*b) - Log[x]/(2*b) + (Sin[b*x]*SinIntegral[b*x])/b

Rule 6517

Int[Cos[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :> Simp[Imp[(Sin[a + b*x]*SinIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 3312

Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] :> Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned}
\int \cos(bx)\text{Si}(bx) dx &= \frac{\sin(bx)\text{Si}(bx)}{b} - \int \frac{\sin^2(bx)}{bx} dx \\
&= \frac{\sin(bx)\text{Si}(bx)}{b} - \frac{\int \frac{\sin^2(bx)}{x} dx}{b} \\
&= \frac{\sin(bx)\text{Si}(bx)}{b} - \frac{\int \left(\frac{1}{2x} - \frac{\cos(2bx)}{2x} \right) dx}{b} \\
&= -\frac{\log(x)}{2b} + \frac{\sin(bx)\text{Si}(bx)}{b} + \frac{\int \frac{\cos(2bx)}{x} dx}{2b} \\
&= \frac{\text{Ci}(2bx)}{2b} - \frac{\log(x)}{2b} + \frac{\sin(bx)\text{Si}(bx)}{b}
\end{aligned}$$

Mathematica [A] time = 0.0129354, size = 36, normalized size = 1.06

$$\frac{\text{CosIntegral}(2bx)}{2b} + \frac{\text{Si}(bx) \sin(bx)}{b} - \frac{\log(bx)}{2b}$$

Warning: Unable to verify antiderivative.

[In] Integrate[Cos[b*x]*SinIntegral[b*x],x]

[Out] CosIntegral[2*b*x]/(2*b) - Log[b*x]/(2*b) + (Sin[b*x]*SinIntegral[b*x])/b

Maple [A] time = 0.053, size = 33, normalized size = 1.

$$\frac{\text{Si}(bx) \sin(bx)}{b} - \frac{\ln(bx)}{2b} + \frac{\text{Ci}(2bx)}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(b*x)*Si(b*x),x)

[Out] Si(b*x)*sin(b*x)/b-1/2/b*ln(b*x)+1/2*Ci(2*b*x)/b

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Si}(bx) \cos(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x)*Si(b*x),x, algorithm="maxima")

[Out] integrate(Si(b*x)*cos(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(\cos(bx) \text{Si}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(b*x)*Si(b*x),x, algorithm="fricas")
```

```
[Out] integral(cos(b*x)*sin_integral(b*x), x)
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \cos(bx) \operatorname{Si}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(b*x)*Si(b*x),x)
```

```
[Out] Integral(cos(b*x)*Si(b*x), x)
```

Giac [A] time = 1.18222, size = 45, normalized size = 1.32

$$\frac{\sin(bx) \operatorname{Si}(bx)}{b} + \frac{\operatorname{Ci}(2bx) + \operatorname{Ci}(-2bx) - 2 \log(x)}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(b*x)*Si(b*x),x, algorithm="giac")
```

```
[Out] sin(b*x)*sin_integral(b*x)/b + 1/4*(cos_integral(2*b*x) + cos_integral(-2*b*x) - 2*log(x))/b
```

3.50 $\int x \cos(bx) \mathbf{Si}(bx) dx$

Optimal. Leaf size=61

$$-\frac{\text{Si}(2bx)}{2b^2} + \frac{\text{Si}(bx) \cos(bx)}{b^2} + \frac{\sin(bx) \cos(bx)}{2b^2} + \frac{x \text{Si}(bx) \sin(bx)}{b} - \frac{x}{2b}$$

[Out] $-x/(2*b) + (\text{Cos}[b*x]*\text{Sin}[b*x])/(2*b^2) + (\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b^2 + (x*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b - \text{SinIntegral}[2*b*x]/(2*b^2)$

Rubi [A] time = 0.0659373, antiderivative size = 61, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 7, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.7$, Rules used = {6519, 12, 2635, 8, 6511, 4406, 3299}

$$-\frac{\text{Si}(2bx)}{2b^2} + \frac{\text{Si}(bx) \cos(bx)}{b^2} + \frac{\sin(bx) \cos(bx)}{2b^2} + \frac{x \text{Si}(bx) \sin(bx)}{b} - \frac{x}{2b}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x*\text{Cos}[b*x]*\text{SinIntegral}[b*x], x]$

[Out] $-x/(2*b) + (\text{Cos}[b*x]*\text{Sin}[b*x])/(2*b^2) + (\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b^2 + (x*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b - \text{SinIntegral}[2*b*x]/(2*b^2)$

Rule 6519

$\text{Int}[\text{Cos}[(a_.) + (b_.)*(x_.)]*((e_.) + (f_.)*(x_.))^{(m_.)}*\text{SinIntegral}[(c_.) + (d_.)*(x_.)], x_Symbol] := \text{Simp}[(e + f*x)^m*\text{Sin}[a + b*x]*\text{SinIntegral}[c + d*x]/b, x] + (-\text{Dist}[d/b, \text{Int}[(e + f*x)^m*\text{Sin}[a + b*x]*\text{Sin}[c + d*x]/(c + d*x), x], x] - \text{Dist}[(f*m)/b, \text{Int}[(e + f*x)^{(m-1)}*\text{Sin}[a + b*x]*\text{SinIntegral}[c + d*x], x], x]) /; \text{FreeQ}\{a, b, c, d, e, f\}, x] \&\& \text{IGtQ}[m, 0]$

Rule 12

$\text{Int}[(a_)*(u_), x_Symbol] := \text{Dist}[a, \text{Int}[u, x], x] /; \text{FreeQ}[a, x] \&\& !\text{MatchQ}[u, (b_)*(v_)] /; \text{FreeQ}[b, x]$

Rule 2635

$\text{Int}[(b_.)*\sin[(c_.) + (d_.)*(x_.)]^{(n_.)}, x_Symbol] := -\text{Simp}[(b*\text{Cos}[c + d*x])*(b*\text{Sin}[c + d*x])^{(n-1)})/(d*n), x] + \text{Dist}[(b^2*(n-1))/n, \text{Int}[(b*\text{Sin}[c + d*x])^{(n-2)}, x], x] /; \text{FreeQ}\{b, c, d\}, x] \&\& \text{GtQ}[n, 1] \&\& \text{IntegerQ}[2*n]$

Rule 8

$\text{Int}[a_, x_Symbol] := \text{Simp}[a*x, x] /; \text{FreeQ}[a, x]$

Rule 6511

$\text{Int}[\text{Sin}[(a_.) + (b_.)*(x_.)]*\text{SinIntegral}[(c_.) + (d_.)*(x_.)], x_Symbol] := -\text{Simp}[(\text{Cos}[a + b*x]*\text{SinIntegral}[c + d*x])/b, x] + \text{Dist}[d/b, \text{Int}[(\text{Cos}[a + b*x]*\text{Sin}[c + d*x])/(c + d*x), x], x] /; \text{FreeQ}\{a, b, c, d\}, x]$

Rule 4406

$\text{Int}[\text{Cos}[(a_.) + (b_.)*(x_.)]^{(p_.)}*((c_.) + (d_.)*(x_.))^{(m_.)}*\text{Sin}[(a_.) + (b_.)*(x_.)]^{(n_.)}, x_Symbol] := \text{Int}[\text{ExpandTrigReduce}[(c + d*x)^m, \text{Sin}[a + b*x$

$]^n \cos[a + b*x]^p, x] /; \text{FreeQ}\{a, b, c, d, m\}, x\} \&\& \text{IGtQ}[n, 0] \&\& \text{IGtQ}[p, 0]$

Rule 3299

$\text{Int}[\sin[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] \text{:>} \text{Simp}[\text{SinIntegral}[e + f*x]/d, x] /; \text{FreeQ}\{c, d, e, f\}, x\} \&\& \text{EqQ}[d*e - c*f, 0]$

Rubi steps

$$\begin{aligned} \int x \cos(bx) \text{Si}(bx) dx &= \frac{x \sin(bx) \text{Si}(bx)}{b} - \frac{\int \sin(bx) \text{Si}(bx) dx}{b} - \int \frac{\sin^2(bx)}{b} dx \\ &= \frac{\cos(bx) \text{Si}(bx)}{b^2} + \frac{x \sin(bx) \text{Si}(bx)}{b} - \frac{\int \frac{\cos(bx) \sin(bx)}{bx} dx}{b} - \frac{\int \sin^2(bx) dx}{b} \\ &= \frac{\cos(bx) \sin(bx)}{2b^2} + \frac{\cos(bx) \text{Si}(bx)}{b^2} + \frac{x \sin(bx) \text{Si}(bx)}{b} - \frac{\int \frac{\cos(bx) \sin(bx)}{x} dx}{b^2} - \frac{\int 1 dx}{2b} \\ &= -\frac{x}{2b} + \frac{\cos(bx) \sin(bx)}{2b^2} + \frac{\cos(bx) \text{Si}(bx)}{b^2} + \frac{x \sin(bx) \text{Si}(bx)}{b} - \frac{\int \frac{\sin(2bx)}{2x} dx}{b^2} \\ &= -\frac{x}{2b} + \frac{\cos(bx) \sin(bx)}{2b^2} + \frac{\cos(bx) \text{Si}(bx)}{b^2} + \frac{x \sin(bx) \text{Si}(bx)}{b} - \frac{\int \frac{\sin(2bx)}{x} dx}{2b^2} \\ &= -\frac{x}{2b} + \frac{\cos(bx) \sin(bx)}{2b^2} + \frac{\cos(bx) \text{Si}(bx)}{b^2} + \frac{x \sin(bx) \text{Si}(bx)}{b} - \frac{\text{Si}(2bx)}{2b^2} \end{aligned}$$

Mathematica [A] time = 0.0492865, size = 42, normalized size = 0.69

$$\frac{-2\text{Si}(2bx) + 4\text{Si}(bx)(bx \sin(bx) + \cos(bx)) - 2bx + \sin(2bx)}{4b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*cos[b*x]*SinIntegral[b*x],x]

[Out] $(-2*b*x + \text{Sin}[2*b*x] + 4*(\text{Cos}[b*x] + b*x*\text{Sin}[b*x]))*\text{SinIntegral}[b*x] - 2*\text{SinIntegral}[2*b*x])/(4*b^2)$

Maple [A] time = 0.056, size = 44, normalized size = 0.7

$$\frac{1}{b^2} \left(\text{Si}(bx) (\sin(bx) bx + \cos(bx)) + \frac{\sin(bx) \cos(bx)}{2} - \frac{bx}{2} - \frac{\text{Si}(2bx)}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*cos(b*x)*Si(b*x),x)

[Out] $1/b^2*(\text{Si}(b*x)*(\sin(b*x)*b*x+\cos(b*x))+1/2*\sin(b*x)*\cos(b*x)-1/2*b*x-1/2*\text{Si}(2*b*x))$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \text{Si}(bx) \cos(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*cos(b*x)*Si(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x*Si(b*x)*cos(b*x), x)
```

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x \cos(bx) \text{Si}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*cos(b*x)*Si(b*x),x, algorithm="fricas")
```

```
[Out] integral(x*cos(b*x)*sin_integral(b*x), x)
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \cos(bx) \text{Si}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*cos(b*x)*Si(b*x),x)
```

```
[Out] Integral(x*cos(b*x)*Si(b*x), x)
```

Giac [C] time = 1.1768, size = 74, normalized size = 1.21

$$\left(\frac{x \sin(bx)}{b} + \frac{\cos(bx)}{b^2} \right) \text{Si}(bx) - \frac{2bx + \Im(\text{Ci}(2bx)) - \Im(\text{Ci}(-2bx)) + 2 \text{Si}(2bx)}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*cos(b*x)*Si(b*x),x, algorithm="giac")
```

```
[Out] (x*sin(b*x)/b + cos(b*x)/b^2)*sin_integral(b*x) - 1/4*(2*b*x + imag_part(cos_integral(2*b*x)) - imag_part(cos_integral(-2*b*x)) + 2*sin_integral(2*b*x))/b^2
```

3.51 $\int x^2 \cos(bx) \text{Si}(bx) dx$

Optimal. Leaf size=98

$$-\frac{\text{CosIntegral}(2bx)}{b^3} - \frac{2\text{Si}(bx) \sin(bx)}{b^3} + \frac{2x\text{Si}(bx) \cos(bx)}{b^2} + \frac{\log(x)}{b^3} - \frac{5 \sin^2(bx)}{4b^3} + \frac{x \sin(bx) \cos(bx)}{2b^2} + \frac{x^2 \text{Si}(bx) \sin(bx)}{b}$$

[Out] $-x^2/(4*b) - \text{CosIntegral}[2*b*x]/b^3 + \text{Log}[x]/b^3 + (x*\text{Cos}[b*x]*\text{Sin}[b*x])/(2*b^2) - (5*\text{Sin}[b*x]^2)/(4*b^3) + (2*x*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b^2 - (2*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b^3 + (x^2*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b$

Rubi [A] time = 0.122718, antiderivative size = 98, normalized size of antiderivative = 1., number of steps used = 13, number of rules used = 9, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.75$, Rules used = {6519, 12, 3310, 30, 6513, 2564, 6517, 3312, 3302}

$$-\frac{\text{CosIntegral}(2bx)}{b^3} - \frac{2\text{Si}(bx) \sin(bx)}{b^3} + \frac{2x\text{Si}(bx) \cos(bx)}{b^2} + \frac{\log(x)}{b^3} - \frac{5 \sin^2(bx)}{4b^3} + \frac{x \sin(bx) \cos(bx)}{2b^2} + \frac{x^2 \text{Si}(bx) \sin(bx)}{b}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2*\text{Cos}[b*x]*\text{SinIntegral}[b*x], x]$

[Out] $-x^2/(4*b) - \text{CosIntegral}[2*b*x]/b^3 + \text{Log}[x]/b^3 + (x*\text{Cos}[b*x]*\text{Sin}[b*x])/(2*b^2) - (5*\text{Sin}[b*x]^2)/(4*b^3) + (2*x*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b^2 - (2*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b^3 + (x^2*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b$

Rule 6519

$\text{Int}[\text{Cos}[(a_.) + (b_.)*(x_.)]*((e_.) + (f_.)*(x_.))^{(m_.)*\text{SinIntegral}[(c_.) + (d_.)*(x_.)]}, x_Symbol] \rightarrow \text{Simp}[(e + f*x)^m*\text{Sin}[a + b*x]*\text{SinIntegral}[c + d*x])/b, x] + (-\text{Dist}[d/b, \text{Int}[(e + f*x)^m*\text{Sin}[a + b*x]*\text{Sin}[c + d*x]]/(c + d*x), x], x] - \text{Dist}[(f*m)/b, \text{Int}[(e + f*x)^{m-1}*\text{Sin}[a + b*x]*\text{SinIntegral}[c + d*x], x], x] /; \text{FreeQ}\{a, b, c, d, e, f\}, x] \&\& \text{IGtQ}[m, 0]$

Rule 12

$\text{Int}[(a_)*(u_), x_Symbol] \rightarrow \text{Dist}[a, \text{Int}[u, x], x] /; \text{FreeQ}[a, x] \&\& !\text{MatchQ}[u, (b_)*(v_)] /; \text{FreeQ}[b, x]$

Rule 3310

$\text{Int}[(c_.) + (d_.)*(x_.)]*((b_.)*\text{sin}[(e_.) + (f_.)*(x_.)])^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(d*(b*\text{Sin}[e + f*x])^n)/(f^2*n^2), x] + (\text{Dist}[(b^2*(n-1))/n, \text{Int}[(c + d*x)*(b*\text{Sin}[e + f*x])^{n-2}], x], x] - \text{Simp}[(b*(c + d*x)*\text{Cos}[e + f*x]*(b*\text{Sin}[e + f*x])^{n-1})/(f*n), x]) /; \text{FreeQ}\{b, c, d, e, f\}, x] \&\& \text{GtQ}[n, 1]$

Rule 30

$\text{Int}[(x_)^{(m_.)}, x_Symbol] \rightarrow \text{Simp}[x^{(m+1)}/(m+1), x] /; \text{FreeQ}[m, x] \&\& \text{NeQ}[m, -1]$

Rule 6513

$\text{Int}[(e_.) + (f_.)*(x_.)]^{(m_.)*\text{Sin}[(a_.) + (b_.)*(x_.)]*\text{SinIntegral}[(c_.) + (d_.)*(x_.)], x_Symbol] \rightarrow -\text{Simp}[(e + f*x)^m*\text{Cos}[a + b*x]*\text{SinIntegral}[c + d*x])/b, x] + (\text{Dist}[d/b, \text{Int}[(e + f*x)^m*\text{Cos}[a + b*x]*\text{Sin}[c + d*x]]/(c + d*x), x], x]$

$x), x], x] + \text{Dist}[(f*m)/b, \text{Int}[(e + f*x)^{(m-1)}*\text{Cos}[a + b*x]*\text{SinIntegral}[c + d*x], x], x]) /; \text{FreeQ}[\{a, b, c, d, e, f\}, x] \ \&\& \ \text{IGtQ}[m, 0]$

Rule 2564

$\text{Int}[\text{Cos}[(e_.) + (f_.)*(x_.)]^{(n_.)}*((a_.)*\text{sin}[(e_.) + (f_.)*(x_.)])^{(m_.)}, x_Symbol] \rightarrow \text{Dist}[1/(a*f), \text{Subst}[\text{Int}[x^m*(1 - x^2/a^2)^{(n-1)/2}], x], x, a*\text{Sin}[e + f*x]], x] /; \text{FreeQ}[\{a, e, f, m\}, x] \ \&\& \ \text{IntegerQ}[(n-1)/2] \ \&\& \ !(\text{IntegerQ}[(m-1)/2] \ \&\& \ \text{LtQ}[0, m, n])$

Rule 6517

$\text{Int}[\text{Cos}[(a_.) + (b_.)*(x_.)]*\text{SinIntegral}[(c_.) + (d_.)*(x_.)], x_Symbol] \rightarrow \text{Simp}[(\text{Sin}[a + b*x]*\text{SinIntegral}[c + d*x])/b, x] - \text{Dist}[d/b, \text{Int}[(\text{Sin}[a + b*x]*\text{Sin}[c + d*x])/(c + d*x), x], x] /; \text{FreeQ}[\{a, b, c, d\}, x]$

Rule 3312

$\text{Int}[(c_.) + (d_.)*(x_.)]^{(m_.)}*\text{sin}[(e_.) + (f_.)*(x_.)]^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandTrigReduce}[(c + d*x)^m, \text{Sin}[e + f*x]^n, x], x] /; \text{FreeQ}[\{c, d, e, f, m\}, x] \ \&\& \ \text{IGtQ}[n, 1] \ \&\& \ (!\text{RationalQ}[m] \ || \ (\text{GeQ}[m, -1] \ \&\& \ \text{LtQ}[m, 1]))$

Rule 3302

$\text{Int}[\text{sin}[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] \rightarrow \text{Simp}[\text{CosIntegral}[e - \text{Pi}/2 + f*x]/d, x] /; \text{FreeQ}[\{c, d, e, f\}, x] \ \&\& \ \text{EqQ}[d*(e - \text{Pi}/2) - c*f, 0]$

Rubi steps

$$\begin{aligned} \int x^2 \cos(bx) \text{Si}(bx) dx &= \frac{x^2 \sin(bx) \text{Si}(bx)}{b} - \frac{2 \int x \sin(bx) \text{Si}(bx) dx}{b} - \int \frac{x \sin^2(bx)}{b} dx \\ &= \frac{2x \cos(bx) \text{Si}(bx)}{b^2} + \frac{x^2 \sin(bx) \text{Si}(bx)}{b} - \frac{2 \int \cos(bx) \text{Si}(bx) dx}{b^2} - \frac{\int x \sin^2(bx) dx}{b} - \frac{2 \int \frac{\cos(bx) \text{Si}(bx)}{b} dx}{b} \\ &= \frac{x \cos(bx) \sin(bx)}{2b^2} - \frac{\sin^2(bx)}{4b^3} + \frac{2x \cos(bx) \text{Si}(bx)}{b^2} - \frac{2 \sin(bx) \text{Si}(bx)}{b^3} + \frac{x^2 \sin(bx) \text{Si}(bx)}{b} - \frac{2 \int \frac{\cos(bx) \text{Si}(bx)}{b} dx}{b} \\ &= -\frac{x^2}{4b} + \frac{x \cos(bx) \sin(bx)}{2b^2} - \frac{\sin^2(bx)}{4b^3} + \frac{2x \cos(bx) \text{Si}(bx)}{b^2} - \frac{2 \sin(bx) \text{Si}(bx)}{b^3} + \frac{x^2 \sin(bx) \text{Si}(bx)}{b} \\ &= -\frac{x^2}{4b} + \frac{x \cos(bx) \sin(bx)}{2b^2} - \frac{5 \sin^2(bx)}{4b^3} + \frac{2x \cos(bx) \text{Si}(bx)}{b^2} - \frac{2 \sin(bx) \text{Si}(bx)}{b^3} + \frac{x^2 \sin(bx) \text{Si}(bx)}{b} \\ &= -\frac{x^2}{4b} + \frac{\log(x)}{b^3} + \frac{x \cos(bx) \sin(bx)}{2b^2} - \frac{5 \sin^2(bx)}{4b^3} + \frac{2x \cos(bx) \text{Si}(bx)}{b^2} - \frac{2 \sin(bx) \text{Si}(bx)}{b^3} + \frac{x^2 \sin(bx) \text{Si}(bx)}{b} \\ &= -\frac{x^2}{4b} - \frac{\text{Ci}(2bx)}{b^3} + \frac{\log(x)}{b^3} + \frac{x \cos(bx) \sin(bx)}{2b^2} - \frac{5 \sin^2(bx)}{4b^3} + \frac{2x \cos(bx) \text{Si}(bx)}{b^2} - \frac{2 \sin(bx) \text{Si}(bx)}{b^3} \end{aligned}$$

Mathematica [A] time = 0.0967561, size = 72, normalized size = 0.73

$$\frac{8\text{Si}(bx) \left((b^2 x^2 - 2) \sin(bx) + 2bx \cos(bx) \right) - 2b^2 x^2 - 8\text{CosIntegral}(2bx) + 2bx \sin(2bx) + 5 \cos(2bx) + 8 \log(x)}{8b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*Cos[b*x]*SinIntegral[b*x],x]

[Out] $(-2b^2x^2 + 5\cos[2bx] - 8\text{CosIntegral}[2bx] + 8\log[x] + 2bx\sin[2bx] + 8(2bx\cos[bx] + (-2 + b^2x^2)\sin[bx])\text{SinIntegral}[bx])/(8b^3)$

Maple [A] time = 0.065, size = 105, normalized size = 1.1

$$\frac{x^2\text{Si}(bx)\sin(bx)}{b} + 2\frac{x\cos(bx)\text{Si}(bx)}{b^2} - 2\frac{\text{Si}(bx)\sin(bx)}{b^3} + \frac{x\cos(bx)\sin(bx)}{2b^2} - \frac{x^2}{4b} - \frac{(\sin(bx))^2}{4b^3} + \frac{\ln(bx)}{b^3} - \frac{\text{Ci}(2bx)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x^2*cos(b*x)*Si(b*x),x)`

[Out] $x^2\text{Si}(bx)\sin(bx)/b + 2x\cos(bx)\text{Si}(bx)/b^2 - 2\text{Si}(bx)\sin(bx)/b^3 + 1/2x\cos(bx)\sin(bx)/b^2 - 1/4x^2/b - 1/4\sin(bx)^2/b^3 + 1/b^3\ln(bx) - \text{Ci}(2bx)/b^3 + \cos(bx)^2/b^3$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2\text{Si}(bx)\cos(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*cos(b*x)*Si(b*x),x, algorithm="maxima")`

[Out] `integrate(x^2*Si(b*x)*cos(b*x), x)`

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^2\cos(bx)\text{Si}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*cos(b*x)*Si(b*x),x, algorithm="fricas")`

[Out] `integral(x^2*cos(b*x)*sin_integral(b*x), x)`

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2\cos(bx)\text{Si}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2*cos(b*x)*Si(b*x),x)`

[Out] `Integral(x**2*cos(b*x)*Si(b*x), x)`

Giac [A] time = 1.17171, size = 88, normalized size = 0.9

$$\left(\frac{2x \cos(bx)}{b^2} + \frac{(b^2x^2 - 2) \sin(bx)}{b^3} \right) \text{Si}(bx) - \frac{b^2x^2 + 2 \text{Ci}(2bx) + 2 \text{Ci}(-2bx) - 4 \log(x)}{4b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*cos(b*x)*Si(b*x),x, algorithm="giac")

[Out] (2*x*cos(b*x)/b^2 + (b^2*x^2 - 2)*sin(b*x)/b^3)*sin_integral(b*x) - 1/4*(b^2*x^2 + 2*cos_integral(2*b*x) + 2*cos_integral(-2*b*x) - 4*log(x))/b^3

3.52 $\int x^3 \cos(bx) \text{Si}(bx) dx$

Optimal. Leaf size=128

$$\frac{3x^2 \text{Si}(bx) \cos(bx)}{b^2} + \frac{3 \text{Si}(2bx)}{b^4} - \frac{6x \text{Si}(bx) \sin(bx)}{b^3} - \frac{6 \text{Si}(bx) \cos(bx)}{b^4} + \frac{x^2 \sin(bx) \cos(bx)}{2b^2} + \frac{4x}{b^3} - \frac{2x \sin^2(bx)}{b^3} - \frac{4 \sin(bx)}{b^3}$$

[Out] $(4*x)/b^3 - x^3/(6*b) - (4*\text{Cos}[b*x]*\text{Sin}[b*x])/b^4 + (x^2*\text{Cos}[b*x]*\text{Sin}[b*x])/(2*b^2) - (2*x*\text{Sin}[b*x]^2)/b^3 - (6*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b^4 + (3*x^2*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b^2 - (6*x*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b^3 + (x^3*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b + (3*\text{SinIntegral}[2*b*x])/b^4$

Rubi [A] time = 0.179184, antiderivative size = 128, normalized size of antiderivative = 1., number of steps used = 20, number of rules used = 11, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.917$, Rules used = {6519, 12, 3311, 30, 2635, 8, 6513, 3443, 6511, 4406, 3299}

$$\frac{3x^2 \text{Si}(bx) \cos(bx)}{b^2} + \frac{3 \text{Si}(2bx)}{b^4} - \frac{6x \text{Si}(bx) \sin(bx)}{b^3} - \frac{6 \text{Si}(bx) \cos(bx)}{b^4} + \frac{x^2 \sin(bx) \cos(bx)}{2b^2} + \frac{4x}{b^3} - \frac{2x \sin^2(bx)}{b^3} - \frac{4 \sin(bx)}{b^3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^3*\text{Cos}[b*x]*\text{SinIntegral}[b*x], x]$

[Out] $(4*x)/b^3 - x^3/(6*b) - (4*\text{Cos}[b*x]*\text{Sin}[b*x])/b^4 + (x^2*\text{Cos}[b*x]*\text{Sin}[b*x])/(2*b^2) - (2*x*\text{Sin}[b*x]^2)/b^3 - (6*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b^4 + (3*x^2*\text{Cos}[b*x]*\text{SinIntegral}[b*x])/b^2 - (6*x*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b^3 + (x^3*\text{Sin}[b*x]*\text{SinIntegral}[b*x])/b + (3*\text{SinIntegral}[2*b*x])/b^4$

Rule 6519

$\text{Int}[\text{Cos}[(a_.) + (b_.)*(x_.)]*((e_.) + (f_.)*(x_.))^{(m_.)}*\text{SinIntegral}[(c_.) + (d_.)*(x_.)], x_Symbol] \rightarrow \text{Simp}[(e + f*x)^m*\text{Sin}[a + b*x]*\text{SinIntegral}[c + d*x]/b, x] + (-\text{Dist}[d/b, \text{Int}[(e + f*x)^m*\text{Sin}[a + b*x]*\text{Sin}[c + d*x]/(c + d*x), x], x] - \text{Dist}[(f*m)/b, \text{Int}[(e + f*x)^{m-1}*\text{Sin}[a + b*x]*\text{SinIntegral}[c + d*x], x], x]) /; \text{FreeQ}\{a, b, c, d, e, f\}, x \ \&\& \ \text{IGtQ}[m, 0]$

Rule 12

$\text{Int}[(a_)*(u_), x_Symbol] \rightarrow \text{Dist}[a, \text{Int}[u, x], x] /; \text{FreeQ}[a, x] \ \&\& \ !\text{MatchQ}[u, (b_)*(v_)] /; \text{FreeQ}[b, x]$

Rule 3311

$\text{Int}[(c_.) + (d_.)*(x_.))^{(m_.)}*((b_.)*\text{sin}[(e_.) + (f_.)*(x_.)])^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(d*m*(c + d*x)^{m-1}*(b*\text{Sin}[e + f*x])^n)/(f^2*n^2), x] + (\text{Dist}[(b^2*(n-1))/n, \text{Int}[(c + d*x)^m*(b*\text{Sin}[e + f*x])^{n-2}, x], x] - \text{Dist}[(d^2*m*(m-1))/(f^2*n^2), \text{Int}[(c + d*x)^{m-2}*(b*\text{Sin}[e + f*x])^n, x], x] - \text{Simp}[(b*(c + d*x)^m*\text{Cos}[e + f*x]*(b*\text{Sin}[e + f*x])^{n-1})/(f*n), x]) /; \text{FreeQ}\{b, c, d, e, f\}, x \ \&\& \ \text{GtQ}[n, 1] \ \&\& \ \text{GtQ}[m, 1]$

Rule 30

$\text{Int}[(x_)^{(m_.)}, x_Symbol] \rightarrow \text{Simp}[x^{m+1}/(m+1), x] /; \text{FreeQ}[m, x] \ \&\& \ \text{NeQ}[m, -1]$

Rule 2635

```
Int[((b_.)*sin[(c_.) + (d_.)*(x_)])^(n_), x_Symbol] := -Simp[(b*Cos[c + d*x]
)*(b*Sin[c + d*x])^(n - 1))/(d*n), x] + Dist[(b^2*(n - 1))/n, Int[(b*Sin[c
+ d*x])^(n - 2), x], x] /; FreeQ[{b, c, d}, x] && GtQ[n, 1] && IntegerQ[2*n
]
```

Rule 8

```
Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]
```

Rule 6513

```
Int[((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) +
(d_.)*(x_)], x_Symbol] := -Simp[((e + f*x)^m*Cos[a + b*x]*SinIntegral[c + d
*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*Cos[a + b*x]*Sin[c + d*x])/(c + d*
x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Cos[a + b*x]*SinIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 3443

```
Int[Cos[(a_.) + (b_.)*(x_)^(n_.)]*(x_)^(m_.)*Sin[(a_.) + (b_.)*(x_)^(n_.)]^(
p_.), x_Symbol] := Simp[(x^(m - n + 1)*Sin[a + b*x^n]^(p + 1))/(b*n*(p + 1
)), x] - Dist[(m - n + 1)/(b*n*(p + 1)), Int[x^(m - n)*Sin[a + b*x^n]^(p +
1), x], x] /; FreeQ[{a, b, p}, x] && LtQ[0, n, m + 1] && NeQ[p, -1]
```

Rule 6511

```
Int[Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := -
Simp[(Cos[a + b*x]*SinIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x
]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b
_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x
]^(n)*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IG
tQ[p, 0]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int x^3 \cos(bx) \text{Si}(bx) dx &= \frac{x^3 \sin(bx) \text{Si}(bx)}{b} - \frac{3 \int x^2 \sin(bx) \text{Si}(bx) dx}{b} - \int \frac{x^2 \sin^2(bx)}{b} dx \\
&= \frac{3x^2 \cos(bx) \text{Si}(bx)}{b^2} + \frac{x^3 \sin(bx) \text{Si}(bx)}{b} - \frac{6 \int x \cos(bx) \text{Si}(bx) dx}{b^2} - \frac{\int x^2 \sin^2(bx) dx}{b} - \frac{3 \int \frac{x \cos(bx)}{b} dx}{b} \\
&= \frac{x^2 \cos(bx) \sin(bx)}{2b^2} - \frac{x \sin^2(bx)}{2b^3} + \frac{3x^2 \cos(bx) \text{Si}(bx)}{b^2} - \frac{6x \sin(bx) \text{Si}(bx)}{b^3} + \frac{x^3 \sin(bx) \text{Si}(bx)}{b} + \frac{3x^2 \cos(bx) \text{Si}(bx)}{b^2} \\
&= -\frac{x^3}{6b} - \frac{\cos(bx) \sin(bx)}{4b^4} + \frac{x^2 \cos(bx) \sin(bx)}{2b^2} - \frac{2x \sin^2(bx)}{b^3} - \frac{6 \cos(bx) \text{Si}(bx)}{b^4} + \frac{3x^2 \cos(bx) \text{Si}(bx)}{b^2} \\
&= \frac{x}{4b^3} - \frac{x^3}{6b} - \frac{4 \cos(bx) \sin(bx)}{b^4} + \frac{x^2 \cos(bx) \sin(bx)}{2b^2} - \frac{2x \sin^2(bx)}{b^3} - \frac{6 \cos(bx) \text{Si}(bx)}{b^4} + \frac{3x^2 \cos(bx) \text{Si}(bx)}{b^2} \\
&= \frac{4x}{b^3} - \frac{x^3}{6b} - \frac{4 \cos(bx) \sin(bx)}{b^4} + \frac{x^2 \cos(bx) \sin(bx)}{2b^2} - \frac{2x \sin^2(bx)}{b^3} - \frac{6 \cos(bx) \text{Si}(bx)}{b^4} + \frac{3x^2 \cos(bx) \text{Si}(bx)}{b^2} \\
&= \frac{4x}{b^3} - \frac{x^3}{6b} - \frac{4 \cos(bx) \sin(bx)}{b^4} + \frac{x^2 \cos(bx) \sin(bx)}{2b^2} - \frac{2x \sin^2(bx)}{b^3} - \frac{6 \cos(bx) \text{Si}(bx)}{b^4} + \frac{3x^2 \cos(bx) \text{Si}(bx)}{b^2}
\end{aligned}$$

Mathematica [A] time = 0.104526, size = 94, normalized size = 0.73

$$\frac{12\text{Si}(bx) \left(bx \left(b^2 x^2 - 6 \right) \sin(bx) + 3 \left(b^2 x^2 - 2 \right) \cos(bx) \right) - 2b^3 x^3 + 3b^2 x^2 \sin(2bx) + 36\text{Si}(2bx) + 36bx - 24 \sin(2bx) + 12b^4}{12b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*Cos[b*x]*SinIntegral[b*x],x]

[Out] (36*b*x - 2*b^3*x^3 + 12*b*x*Cos[2*b*x] - 24*Sin[2*b*x] + 3*b^2*x^2*Sin[2*b*x] + 12*(3*(-2 + b^2*x^2)*Cos[b*x] + b*x*(-6 + b^2*x^2)*Sin[b*x])*SinIntegral[b*x] + 36*SinIntegral[2*b*x])/(12*b^4)

Maple [A] time = 0.078, size = 111, normalized size = 0.9

$$\frac{1}{b^4} \left(\text{Si}(bx) \left(\sin(bx) b^3 x^3 + 3 b^2 x^2 \cos(bx) - 6 \cos(bx) - 6 \sin(bx) bx \right) - b^2 x^2 \left(-\frac{\sin(bx) \cos(bx)}{2} + \frac{bx}{2} \right) + 2 bx \cos(bx) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*cos(b*x)*Si(b*x),x)

[Out] 1/b^4*(Si(b*x)*(sin(b*x)*b^3*x^3+3*b^2*x^2*cos(b*x)-6*cos(b*x)-6*sin(b*x)*b*x)-b^2*x^2*(-1/2*sin(b*x)*cos(b*x)+1/2*b*x)+2*b*x*cos(b*x)^2-4*sin(b*x)*cos(b*x)+2*b*x+1/3*x^3*b^3+3*Si(2*b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \text{Si}(bx) \cos(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*cos(b*x)*Si(b*x),x, algorithm="maxima")

[Out] integrate(x^3*Si(b*x)*cos(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^3 \cos(bx) \text{Si}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*cos(b*x)*Si(b*x),x, algorithm="fricas")

[Out] integral(x^3*cos(b*x)*sin_integral(b*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \cos(bx) \text{Si}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*cos(b*x)*Si(b*x),x)

[Out] Integral(x**3*cos(b*x)*Si(b*x), x)

Giac [C] time = 1.19029, size = 115, normalized size = 0.9

$$\left(\frac{3(b^2x^2 - 2)\cos(bx)}{b^4} + \frac{(b^3x^3 - 6bx)\sin(bx)}{b^4} \right) \text{Si}(bx) - \frac{b^3x^3 - 18bx - 9\Im(\text{Ci}(2bx)) + 9\Im(\text{Ci}(-2bx)) - 18\text{Si}(2bx)}{6b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*cos(b*x)*Si(b*x),x, algorithm="giac")

[Out] (3*(b^2*x^2 - 2)*cos(b*x)/b^4 + (b^3*x^3 - 6*b*x)*sin(b*x)/b^4)*sin_integra
l(b*x) - 1/6*(b^3*x^3 - 18*b*x - 9*imag_part(cos_integral(2*b*x)) + 9*imag_
part(cos_integral(-2*b*x)) - 18*sin_integral(2*b*x))/b^4

3.53 $\int \sin(5x)\text{Si}(2x) dx$

Optimal. Leaf size=29

$$-\frac{\text{Si}(3x)}{10} + \frac{\text{Si}(7x)}{10} - \frac{1}{5}\text{Si}(2x)\cos(5x)$$

[Out] $-(\text{Cos}[5*x]*\text{SinIntegral}[2*x])/5 - \text{SinIntegral}[3*x]/10 + \text{SinIntegral}[7*x]/10$

Rubi [A] time = 0.0550338, antiderivative size = 29, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 4, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.444$, Rules used = {6511, 12, 4430, 3299}

$$-\frac{\text{Si}(3x)}{10} + \frac{\text{Si}(7x)}{10} - \frac{1}{5}\text{Si}(2x)\cos(5x)$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{Sin}[5*x]*\text{SinIntegral}[2*x], x]$

[Out] $-(\text{Cos}[5*x]*\text{SinIntegral}[2*x])/5 - \text{SinIntegral}[3*x]/10 + \text{SinIntegral}[7*x]/10$

Rule 6511

$\text{Int}[\text{Sin}[(a_.) + (b_.)*(x_.)]*\text{SinIntegral}[(c_.) + (d_.)*(x_.)], x_Symbol] \text{ :> } -\text{Simp}[(\text{Cos}[a + b*x]*\text{SinIntegral}[c + d*x])/b, x] + \text{Dist}[d/b, \text{Int}[(\text{Cos}[a + b*x]*\text{Sin}[c + d*x])/(c + d*x), x], x] \text{ /; FreeQ}\{a, b, c, d\}, x]$

Rule 12

$\text{Int}[(a_)*(u_), x_Symbol] \text{ :> } \text{Dist}[a, \text{Int}[u, x], x] \text{ /; FreeQ}[a, x] \ \&\& \ !\text{Match} Q[u, (b_)*(v_)] \text{ /; FreeQ}[b, x]$

Rule 4430

$\text{Int}[\text{Cos}[(c_.) + (d_.)*(x_.)]^{(q_.)}*((e_.) + (f_.)*(x_.))^{(m_.)}*\text{Sin}[(a_.) + (b_.)*(x_.)]^{(p_.)}, x_Symbol] \text{ :> } \text{Int}[\text{ExpandTrigReduce}[(e + f*x)^m, \text{Sin}[a + b*x]^{p*}\text{Cos}[c + d*x]^q, x], x] \text{ /; FreeQ}\{a, b, c, d, e, f, m\}, x] \ \&\& \ \text{IGtQ}[p, 0] \ \&\& \ \text{IGtQ}[q, 0]$

Rule 3299

$\text{Int}[\text{sin}[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] \text{ :> } \text{Simp}[\text{SinIntegral}[e + f*x]/d, x] \text{ /; FreeQ}\{c, d, e, f\}, x] \ \&\& \ \text{EqQ}[d*e - c*f, 0]$

Rubi steps

$$\begin{aligned}
\int \sin(5x)\text{Si}(2x) dx &= -\frac{1}{5} \cos(5x)\text{Si}(2x) + \frac{2}{5} \int \frac{\cos(5x) \sin(2x)}{2x} dx \\
&= -\frac{1}{5} \cos(5x)\text{Si}(2x) + \frac{1}{5} \int \frac{\cos(5x) \sin(2x)}{x} dx \\
&= -\frac{1}{5} \cos(5x)\text{Si}(2x) + \frac{1}{5} \int \left(-\frac{\sin(3x)}{2x} + \frac{\sin(7x)}{2x} \right) dx \\
&= -\frac{1}{5} \cos(5x)\text{Si}(2x) - \frac{1}{10} \int \frac{\sin(3x)}{x} dx + \frac{1}{10} \int \frac{\sin(7x)}{x} dx \\
&= -\frac{1}{5} \cos(5x)\text{Si}(2x) - \frac{\text{Si}(3x)}{10} + \frac{\text{Si}(7x)}{10}
\end{aligned}$$

Mathematica [A] time = 0.0260674, size = 25, normalized size = 0.86

$$\frac{1}{10}(-\text{Si}(3x) + \text{Si}(7x) - 2\text{Si}(2x) \cos(5x))$$

Antiderivative was successfully verified.

[In] Integrate[Sin[5*x]*SinIntegral[2*x],x]

[Out] (-2*Cos[5*x]*SinIntegral[2*x] - SinIntegral[3*x] + SinIntegral[7*x])/10

Maple [A] time = 0.124, size = 24, normalized size = 0.8

$$-\frac{\cos(5x) \text{Si}(2x)}{5} - \frac{\text{Si}(3x)}{10} + \frac{\text{Si}(7x)}{10}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(2*x)*sin(5*x),x)

[Out] -1/5*cos(5*x)*Si(2*x)-1/10*Si(3*x)+1/10*Si(7*x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Si}(2x) \sin(5x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(2*x)*sin(5*x),x, algorithm="maxima")

[Out] integrate(Si(2*x)*sin(5*x), x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Si(2*x)*sin(5*x),x, algorithm="fricas")
```

```
[Out] Exception raised: UnboundLocalError
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \sin(5x) \operatorname{Si}(2x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Si(2*x)*sin(5*x),x)
```

```
[Out] Integral(sin(5*x)*Si(2*x), x)
```

Giac [A] time = 1.20063, size = 31, normalized size = 1.07

$$-\frac{1}{5} \cos(5x) \operatorname{Si}(2x) + \frac{1}{10} \operatorname{Si}(7x) - \frac{1}{10} \operatorname{Si}(3x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Si(2*x)*sin(5*x),x, algorithm="giac")
```

```
[Out] -1/5*cos(5*x)*sin_integral(2*x) + 1/10*sin_integral(7*x) - 1/10*sin_integra
1(3*x)
```


3.54 $\int \cos(5x)\mathbf{Si}(2x) dx$

Optimal. Leaf size=29

$$-\frac{1}{10}\text{CosIntegral}(3x) + \frac{1}{10}\text{CosIntegral}(7x) + \frac{1}{5}\text{Si}(2x)\sin(5x)$$

[Out] -CosIntegral[3*x]/10 + CosIntegral[7*x]/10 + (Sin[5*x]*SinIntegral[2*x])/5

Rubi [A] time = 0.0556862, antiderivative size = 29, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 4, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.444$, Rules used = {6517, 12, 4428, 3302}

$$-\frac{1}{10}\text{CosIntegral}(3x) + \frac{1}{10}\text{CosIntegral}(7x) + \frac{1}{5}\text{Si}(2x)\sin(5x)$$

Antiderivative was successfully verified.

[In] Int[Cos[5*x]*SinIntegral[2*x],x]

[Out] -CosIntegral[3*x]/10 + CosIntegral[7*x]/10 + (Sin[5*x]*SinIntegral[2*x])/5

Rule 6517

Int[Cos[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :> Simp[(Sin[a + b*x]*SinIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 4428

Int[((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(p_.)*Sin[(c_.) + (d_.)*(x_)]^(q_.), x_Symbol] :> Int[ExpandTrigReduce[(e + f*x)^m, Sin[a + b*x]^p*Sin[c + d*x]^q, x], x] /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[p, 0] && IGtQ[q, 0] && IntegerQ[m]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned}
\int \cos(5x)\text{Si}(2x) dx &= \frac{1}{5} \sin(5x)\text{Si}(2x) - \frac{2}{5} \int \frac{\sin(2x)\sin(5x)}{2x} dx \\
&= \frac{1}{5} \sin(5x)\text{Si}(2x) - \frac{1}{5} \int \frac{\sin(2x)\sin(5x)}{x} dx \\
&= \frac{1}{5} \sin(5x)\text{Si}(2x) - \frac{1}{5} \int \left(\frac{\cos(3x)}{2x} - \frac{\cos(7x)}{2x} \right) dx \\
&= \frac{1}{5} \sin(5x)\text{Si}(2x) - \frac{1}{10} \int \frac{\cos(3x)}{x} dx + \frac{1}{10} \int \frac{\cos(7x)}{x} dx \\
&= -\frac{\text{Ci}(3x)}{10} + \frac{\text{Ci}(7x)}{10} + \frac{1}{5} \sin(5x)\text{Si}(2x)
\end{aligned}$$

Mathematica [A] time = 0.0258747, size = 25, normalized size = 0.86

$$\frac{1}{10}(-\text{CosIntegral}(3x) + \text{CosIntegral}(7x) + 2\text{Si}(2x)\sin(5x))$$

Antiderivative was successfully verified.

[In] Integrate[Cos[5*x]*SinIntegral[2*x],x]

[Out] (-CosIntegral[3*x] + CosIntegral[7*x] + 2*Sin[5*x]*SinIntegral[2*x])/10

Maple [A] time = 0.131, size = 24, normalized size = 0.8

$$-\frac{\text{Ci}(3x)}{10} + \frac{\text{Ci}(7x)}{10} + \frac{\text{Si}(2x)\sin(5x)}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(5*x)*Si(2*x),x)

[Out] -1/10*Ci(3*x)+1/10*Ci(7*x)+1/5*Si(2*x)*sin(5*x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Si}(2x)\cos(5x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(5*x)*Si(2*x),x, algorithm="maxima")

[Out] integrate(Si(2*x)*cos(5*x), x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(5*x)*Si(2*x),x, algorithm="fricas")
```

```
[Out] Exception raised: UnboundLocalError
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \cos(5x) \operatorname{Si}(2x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(5*x)*Si(2*x),x)
```

```
[Out] Integral(cos(5*x)*Si(2*x), x)
```

Giac [A] time = 1.18164, size = 31, normalized size = 1.07

$$\frac{1}{5} \sin(5x) \operatorname{Si}(2x) + \frac{1}{10} \operatorname{Ci}(7x) - \frac{1}{10} \operatorname{Ci}(3x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(cos(5*x)*Si(2*x),x, algorithm="giac")
```

```
[Out] 1/5*sin(5*x)*sin_integral(2*x) + 1/10*cos_integral(7*x) - 1/10*cos_integral(3*x)
```

3.55 $\int x^2 \sin(a + bx) \mathbf{Si}(a + bx) dx$

Optimal. Leaf size=187

$$\frac{a^2 \text{Si}(2a + 2bx)}{2b^3} - \frac{a \text{CosIntegral}(2a + 2bx)}{b^3} - \frac{\text{Si}(2a + 2bx)}{b^3} + \frac{2x \text{Si}(a + bx) \sin(a + bx)}{b^2} + \frac{2 \text{Si}(a + bx) \cos(a + bx)}{b^3} + \frac{a \log}{b^3}$$

[Out] $-(x/b^2) + (a \text{Cos}[2a + 2b*x])/(4*b^3) - (x \text{Cos}[2a + 2b*x])/(4*b^2) - (a \text{CosIntegral}[2a + 2b*x])/b^3 + (a \text{Log}[a + b*x])/b^3 + (\text{Cos}[a + b*x] \text{Sin}[a + b*x])/b^3 + \text{Sin}[2a + 2b*x]/(8*b^3) + (2 \text{Cos}[a + b*x] \text{SinIntegral}[a + b*x])/b^3 - (x^2 \text{Cos}[a + b*x] \text{SinIntegral}[a + b*x])/b + (2*x \text{Sin}[a + b*x] \text{SinIntegral}[a + b*x])/b^2 - \text{SinIntegral}[2a + 2b*x]/b^3 + (a^2 \text{SinIntegral}[2a + 2b*x])/(2*b^3)$

Rubi [A] time = 0.708193, antiderivative size = 187, normalized size of antiderivative = 1., number of steps used = 21, number of rules used = 16, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 1.$, Rules used = {6513, 4573, 6741, 6742, 2638, 3296, 2637, 3299, 6519, 2635, 8, 3312, 3302, 6511, 4406, 12}

$$\frac{a^2 \text{Si}(2a + 2bx)}{2b^3} - \frac{a \text{CosIntegral}(2a + 2bx)}{b^3} - \frac{\text{Si}(2a + 2bx)}{b^3} + \frac{2x \text{Si}(a + bx) \sin(a + bx)}{b^2} + \frac{2 \text{Si}(a + bx) \cos(a + bx)}{b^3} + \frac{a \log}{b^3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2 \text{Sin}[a + b*x] \text{SinIntegral}[a + b*x], x]$

[Out] $-(x/b^2) + (a \text{Cos}[2a + 2b*x])/(4*b^3) - (x \text{Cos}[2a + 2b*x])/(4*b^2) - (a \text{CosIntegral}[2a + 2b*x])/b^3 + (a \text{Log}[a + b*x])/b^3 + (\text{Cos}[a + b*x] \text{Sin}[a + b*x])/b^3 + \text{Sin}[2a + 2b*x]/(8*b^3) + (2 \text{Cos}[a + b*x] \text{SinIntegral}[a + b*x])/b^3 - (x^2 \text{Cos}[a + b*x] \text{SinIntegral}[a + b*x])/b + (2*x \text{Sin}[a + b*x] \text{SinIntegral}[a + b*x])/b^2 - \text{SinIntegral}[2a + 2b*x]/b^3 + (a^2 \text{SinIntegral}[2a + 2b*x])/(2*b^3)$

Rule 6513

$\text{Int}[(e_.) + (f_.)(x_)^{(m_.)} \text{Sin}[(a_.) + (b_.)(x_)] \text{SinIntegral}[(c_.) + (d_.)(x_)], x_Symbol] \rightarrow -\text{Simp}[(e + f*x)^m \text{Cos}[a + b*x] \text{SinIntegral}[c + d*x])/b, x] + (\text{Dist}[d/b, \text{Int}[(e + f*x)^m \text{Cos}[a + b*x] \text{Sin}[c + d*x]]/(c + d*x), x], x] + \text{Dist}[(f*m)/b, \text{Int}[(e + f*x)^{m-1} \text{Cos}[a + b*x] \text{SinIntegral}[c + d*x], x], x) /; \text{FreeQ}\{a, b, c, d, e, f\}, x] \&\& \text{IGtQ}[m, 0]$

Rule 4573

$\text{Int}[\text{Cos}[w_]^{(p_.)}(u_) \text{Sin}[v_]^{(p_.)}, x_Symbol] \rightarrow \text{Dist}[1/2^p, \text{Int}[u \text{Sin}[2*v]^p, x], x] /; \text{EqQ}[w, v] \&\& \text{IntegerQ}[p]$

Rule 6741

$\text{Int}[u_, x_Symbol] \rightarrow \text{With}\{v = \text{NormalizeIntegrand}[u, x]\}, \text{Int}[v, x] /; v \neq u]$

Rule 6742

$\text{Int}[u_, x_Symbol] \rightarrow \text{With}\{v = \text{ExpandIntegrand}[u, x]\}, \text{Int}[v, x] /; \text{SumQ}[v]$

Rule 2638

Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] := -Simp[Cos[c + d*x]/d, x] /; FreeQ[{c, d}, x]

Rule 3296

Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)], x_Symbol] := -Simp[((c + d*x)^m*cos[e + f*x])/f, x] + Dist[(d*m)/f, Int[(c + d*x)^(m - 1)*cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && GtQ[m, 0]

Rule 2637

Int[sin[Pi/2 + (c_.) + (d_.)*(x_)], x_Symbol] := Simp[Sin[c + d*x]/d, x] /; FreeQ[{c, d}, x]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 6519

Int[Cos[(a_.) + (b_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.)*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := Simp[((e + f*x)^m*sin[a + b*x]*SinIntegral[c + d*x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*sin[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*sin[a + b*x]*SinIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]

Rule 2635

Int[((b_.)*sin[(c_.) + (d_.)*(x_)])^(n_), x_Symbol] := -Simp[(b*cos[c + d*x]*(b*sin[c + d*x])^(n - 1))/(d*n), x] + Dist[(b^2*(n - 1))/n, Int[(b*sin[c + d*x])^(n - 2), x], x] /; FreeQ[{b, c, d}, x] && GtQ[n, 1] && IntegerQ[2*n]

Rule 8

Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]

Rule 3312

Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rule 6511

Int[Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := -Simp[(Cos[a + b*x]*SinIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_.)]^(p_.)*((c_.) + (d_.)*(x_.))^(m_.)*Sin[(a_.) + (b_.)*(x_.)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^(n)*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rubi steps

$$\begin{aligned}
 \int x^2 \sin(a + bx) \operatorname{Si}(a + bx) dx &= -\frac{x^2 \cos(a + bx) \operatorname{Si}(a + bx)}{b} + \frac{2 \int x \cos(a + bx) \operatorname{Si}(a + bx) dx}{b} + \int \frac{x^2 \cos(a + bx) \sin(a + bx)}{a + bx} dx \\
 &= -\frac{x^2 \cos(a + bx) \operatorname{Si}(a + bx)}{b} + \frac{2x \sin(a + bx) \operatorname{Si}(a + bx)}{b^2} + \frac{1}{2} \int \frac{x^2 \sin(2(a + bx))}{a + bx} dx - \frac{2 \int x \cos(a + bx) \operatorname{Si}(a + bx) dx}{b} \\
 &= \frac{2 \cos(a + bx) \operatorname{Si}(a + bx)}{b^3} - \frac{x^2 \cos(a + bx) \operatorname{Si}(a + bx)}{b} + \frac{2x \sin(a + bx) \operatorname{Si}(a + bx)}{b^2} + \frac{1}{2} \int \frac{x^2 \sin(2(a + bx))}{a + bx} dx \\
 &= \frac{2 \cos(a + bx) \operatorname{Si}(a + bx)}{b^3} - \frac{x^2 \cos(a + bx) \operatorname{Si}(a + bx)}{b} + \frac{2x \sin(a + bx) \operatorname{Si}(a + bx)}{b^2} + \frac{1}{2} \int \frac{x^2 \sin(2(a + bx))}{a + bx} dx \\
 &= \frac{\cos(a + bx) \sin(a + bx)}{b^3} + \frac{2 \cos(a + bx) \operatorname{Si}(a + bx)}{b^3} - \frac{x^2 \cos(a + bx) \operatorname{Si}(a + bx)}{b} + \frac{2x \sin(a + bx) \operatorname{Si}(a + bx)}{b^2} \\
 &= -\frac{x}{b^2} + \frac{a \cos(2a + 2bx)}{4b^3} - \frac{x \cos(2a + 2bx)}{4b^2} + \frac{a \log(a + bx)}{b^3} + \frac{\cos(a + bx) \sin(a + bx)}{b^3} + \frac{2x \sin(a + bx) \operatorname{Si}(a + bx)}{b^2} \\
 &= -\frac{x}{b^2} + \frac{a \cos(2a + 2bx)}{4b^3} - \frac{x \cos(2a + 2bx)}{4b^2} - \frac{a \operatorname{Ci}(2a + 2bx)}{b^3} + \frac{a \log(a + bx)}{b^3} + \frac{\cos(a + bx) \sin(a + bx)}{b^3}
 \end{aligned}$$

Mathematica [A] time = 0.326212, size = 123, normalized size = 0.66

$$\frac{4a^2 \operatorname{Si}(2(a + bx)) - 8 \operatorname{Si}(a + bx) \left((b^2 x^2 - 2) \cos(a + bx) - 2bx \sin(a + bx) \right) - 8a \operatorname{CosIntegral}(2(a + bx)) - 8 \operatorname{Si}(2(a + bx))}{8b^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*Sin[a + b*x]*SinIntegral[a + b*x],x]
```

```
[Out] (-8*b*x + 2*a*Cos[2*(a + b*x)] - 2*b*x*Cos[2*(a + b*x)] - 8*a*CosIntegral[2*(a + b*x)] + 8*a*Log[a + b*x] + 5*Sin[2*(a + b*x)] - 8*((-2 + b^2*x^2)*Cos[a + b*x] - 2*b*x*Sin[a + b*x])*SinIntegral[a + b*x] - 8*SinIntegral[2*(a + b*x)] + 4*a^2*SinIntegral[2*(a + b*x)])/(8*b^3)
```

Maple [A] time = 0.063, size = 171, normalized size = 0.9

$$-\frac{x^2 \cos(bx + a) \operatorname{Si}(bx + a)}{b} + 2 \frac{x \operatorname{Si}(bx + a) \sin(bx + a)}{b^2} + 2 \frac{\cos(bx + a) \operatorname{Si}(bx + a)}{b^3} - \frac{(\cos(bx + a))^2 x}{2b^2} + \frac{a \cos(bx + a)}{2b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*Si(b*x+a)*sin(b*x+a),x)
```

[Out] $-x^2 \cos(bx+a) \operatorname{Si}(bx+a) / b^2 + x \operatorname{Si}(bx+a) \sin(bx+a) / b^2 + 2 \cos(bx+a) \operatorname{Si}(bx+a) / b^3 - 1/2 / b^2 \cos(bx+a)^2 + x + 1/2 / b^3 a \cos(bx+a)^2 + 5/4 \cos(bx+a) \sin(bx+a) / b^3 - 3/4 x / b^2 - 3/4 / b^3 a + 1/2 a^2 \operatorname{Si}(2bx+2a) / b^3 - a \operatorname{Ci}(2bx+2a) / b^3 + a \ln(bx+a) / b^3 - \operatorname{Si}(2bx+2a) / b^3$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \operatorname{Si}(bx+a) \sin(bx+a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*Si(b*x+a)*sin(b*x+a),x, algorithm="maxima")`

[Out] `integrate(x^2*Si(b*x + a)*sin(b*x + a), x)`

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}(x^2 \sin(bx+a) \operatorname{Si}(bx+a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*Si(b*x+a)*sin(b*x+a),x, algorithm="fricas")`

[Out] `integral(x^2*sin(b*x + a)*sin_integral(b*x + a), x)`

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x**2*Si(b*x+a)*sin(b*x+a),x)`

[Out] Timed out

Giac [C] time = 1.22913, size = 223, normalized size = 1.19

$$\left(\frac{2x \sin(bx+a)}{b^2} - \frac{(b^2x^2 - 2) \cos(bx+a)}{b^3} \right) \operatorname{Si}(bx+a) + \frac{a^2 \Im(\operatorname{Ci}(2bx+2a)) - a^2 \Im(\operatorname{Ci}(-2bx-2a)) + 2a^2 \operatorname{Si}(2bx-2a)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x^2*Si(b*x+a)*sin(b*x+a),x, algorithm="giac")`

[Out] $(2*x*\sin(b*x + a)/b^2 - (b^2*x^2 - 2)*\cos(b*x + a)/b^3)*\sin_integral(b*x + a) + 1/4*(a^2*\operatorname{imag_part}(\cos_integral(2*b*x + 2*a)) - a^2*\operatorname{imag_part}(\cos_integral(-2*b*x - 2*a)) + 2*a^2*\sin_integral(2*b*x + 2*a) - 4*b*x + 4*a*\log(\operatorname{abs}(b*x + a)) - 2*a*\operatorname{real_part}(\cos_integral(2*b*x + 2*a)) - 2*a*\operatorname{real_part}(\cos_integral(-2*b*x - 2*a)) - 2*\operatorname{imag_part}(\cos_integral(2*b*x + 2*a)) + 2*\operatorname{imag_part}(\cos_integral(-2*b*x - 2*a)) - 4*\sin_integral(2*b*x + 2*a))/b^3$

3.56 $\int x \sin(a + bx) \mathbf{Si}(a + bx) dx$

Optimal. Leaf size=97

$$\frac{\text{CosIntegral}(2a + 2bx)}{2b^2} - \frac{a\text{Si}(2a + 2bx)}{2b^2} + \frac{\text{Si}(a + bx)\sin(a + bx)}{b^2} - \frac{\log(a + bx)}{2b^2} - \frac{\cos(2a + 2bx)}{4b^2} - \frac{x\text{Si}(a + bx)\cos(a + bx)}{b}$$

```
[Out] -Cos[2*a + 2*b*x]/(4*b^2) + CosIntegral[2*a + 2*b*x]/(2*b^2) - Log[a + b*x]
/(2*b^2) - (x*Cos[a + b*x]*SinIntegral[a + b*x])/b + (Sin[a + b*x]*SinInteg
ral[a + b*x])/b^2 - (a*SinIntegral[2*a + 2*b*x])/(2*b^2)
```

Rubi [A] time = 0.274699, antiderivative size = 97, normalized size of antiderivative = 1., number of steps used = 11, number of rules used = 9, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.643$, Rules used = {6513, 4573, 6741, 6742, 2638, 3299, 6517, 3312, 3302}

$$\frac{\text{CosIntegral}(2a + 2bx)}{2b^2} - \frac{a\text{Si}(2a + 2bx)}{2b^2} + \frac{\text{Si}(a + bx)\sin(a + bx)}{b^2} - \frac{\log(a + bx)}{2b^2} - \frac{\cos(2a + 2bx)}{4b^2} - \frac{x\text{Si}(a + bx)\cos(a + bx)}{b}$$

Antiderivative was successfully verified.

```
[In] Int[x*Sin[a + b*x]*SinIntegral[a + b*x],x]
```

```
[Out] -Cos[2*a + 2*b*x]/(4*b^2) + CosIntegral[2*a + 2*b*x]/(2*b^2) - Log[a + b*x]
/(2*b^2) - (x*Cos[a + b*x]*SinIntegral[a + b*x])/b + (Sin[a + b*x]*SinInteg
ral[a + b*x])/b^2 - (a*SinIntegral[2*a + 2*b*x])/(2*b^2)
```

Rule 6513

```
Int[((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) +
(d_.)*(x_)], x_Symbol] := -Simp[((e + f*x)^m*Cos[a + b*x]*SinIntegral[c + d
*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*Cos[a + b*x]*Sin[c + d*x])/(c + d*
x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Cos[a + b*x]*SinIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 4573

```
Int[Cos[w_]^(p_.)*(u_.)*Sin[v_]^(p_.), x_Symbol] := Dist[1/2^p, Int[u*Sin[2
*v]^(p, x), x] /; EqQ[w, v] && IntegerQ[p]
```

Rule 6741

```
Int[u_, x_Symbol] := With[{v = NormalizeIntegrand[u, x]}, Int[v, x] /; v !=
= u]
```

Rule 6742

```
Int[u_, x_Symbol] := With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]
]
```

Rule 2638

```
Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] := -Simp[Cos[c + d*x]/d, x] /; FreeQ
[{c, d}, x]
```

Rule 3299


```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 6517

```
Int[Cos[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := Simp[(Sin[a + b*x]*SinIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 3312

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rubi steps

$$\begin{aligned} \int x \sin(a + bx) \text{Si}(a + bx) dx &= -\frac{x \cos(a + bx) \text{Si}(a + bx)}{b} + \frac{\int \cos(a + bx) \text{Si}(a + bx) dx}{b} + \int \frac{x \cos(a + bx) \sin(a + bx)}{a + bx} \\ &= -\frac{x \cos(a + bx) \text{Si}(a + bx)}{b} + \frac{\sin(a + bx) \text{Si}(a + bx)}{b^2} + \frac{1}{2} \int \frac{x \sin(2(a + bx))}{a + bx} dx - \frac{\int \frac{\sin^2}{a}}{a} \\ &= -\frac{x \cos(a + bx) \text{Si}(a + bx)}{b} + \frac{\sin(a + bx) \text{Si}(a + bx)}{b^2} + \frac{1}{2} \int \frac{x \sin(2a + 2bx)}{a + bx} dx - \frac{\int \left(\frac{\sin^2}{2a}\right)}{2a} \\ &= -\frac{\log(a + bx)}{2b^2} - \frac{x \cos(a + bx) \text{Si}(a + bx)}{b} + \frac{\sin(a + bx) \text{Si}(a + bx)}{b^2} + \frac{1}{2} \int \left(\frac{\sin(2a + 2bx)}{b}\right) \\ &= \frac{\text{Ci}(2a + 2bx)}{2b^2} - \frac{\log(a + bx)}{2b^2} - \frac{x \cos(a + bx) \text{Si}(a + bx)}{b} + \frac{\sin(a + bx) \text{Si}(a + bx)}{b^2} + \frac{\int \sin}{b} \\ &= -\frac{\cos(2a + 2bx)}{4b^2} + \frac{\text{Ci}(2a + 2bx)}{2b^2} - \frac{\log(a + bx)}{2b^2} - \frac{x \cos(a + bx) \text{Si}(a + bx)}{b} + \frac{\sin(a + bx) \text{Si}(a + bx)}{b^2} \end{aligned}$$

Mathematica [A] time = 0.237806, size = 71, normalized size = 0.73

$$\frac{-2\text{CosIntegral}(2(a + bx)) + 2a\text{Si}(2(a + bx)) + 4\text{Si}(a + bx)(bx \cos(a + bx) - \sin(a + bx)) + 2\log(a + bx) + \cos(2(a + bx))}{4b^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[x*Sin[a + b*x]*SinIntegral[a + b*x], x]
```

```
[Out] -(Cos[2*(a + b*x)] - 2*CosIntegral[2*(a + b*x)] + 2*Log[a + b*x] + 4*(b*x*Cos[a + b*x] - Sin[a + b*x])*SinIntegral[a + b*x] + 2*a*SinIntegral[2*(a + b*x)])/(4*b^2)
```

Maple [A] time = 0.057, size = 89, normalized size = 0.9

$$-\frac{x \cos(bx + a) \text{Si}(bx + a)}{b} + \frac{\text{Si}(bx + a) \sin(bx + a)}{b^2} - \frac{(\cos(bx + a))^2}{2b^2} - \frac{a \text{Si}(2bx + 2a)}{2b^2} - \frac{\ln(bx + a)}{2b^2} + \frac{\text{Ci}(2bx + 2a)}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*Si(b*x+a)*sin(b*x+a),x)`

[Out] $-x\cos(bx+a)\text{Si}(bx+a)/b + \text{Si}(bx+a)\sin(bx+a)/b^{2-1/2}/b^{2}\cos(bx+a)^{2-1/2} + a\text{Si}(2bx+2a)/b^{2-1/2}\ln(bx+a)/b^{2+1/2} + \text{Ci}(2bx+2a)/b^2$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x\text{Si}(bx+a)\sin(bx+a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Si(b*x+a)*sin(b*x+a),x, algorithm="maxima")`

[Out] `integrate(x*Si(b*x + a)*sin(b*x + a), x)`

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x\sin(bx+a)\text{Si}(bx+a),x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Si(b*x+a)*sin(b*x+a),x, algorithm="fricas")`

[Out] `integral(x*sin(b*x + a)*sin_integral(b*x + a), x)`

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x\sin(a+bx)\text{Si}(a+bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Si(b*x+a)*sin(b*x+a),x)`

[Out] `Integral(x*sin(a + b*x)*Si(a + b*x), x)`

Giac [C] time = 1.18991, size = 146, normalized size = 1.51

$$-\left(\frac{x\cos(bx+a)}{b} - \frac{\sin(bx+a)}{b^2}\right)\text{Si}(bx+a) - \frac{a\Im(\text{Ci}(2bx+2a)) - a\Im(\text{Ci}(-2bx-2a)) + 2a\text{Si}(2bx+2a) + 2\log(|bx+a|)}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Si(b*x+a)*sin(b*x+a),x, algorithm="giac")`

[Out] $-(x\cos(bx+a)/b - \sin(bx+a)/b^2)\text{sin_integral}(bx+a) - 1/4*(a\text{imag_part}(\cos_integral(2bx+2a)) - a\text{imag_part}(\cos_integral(-2bx-2a)) + 2a\text{sin_integral}(2bx+2a) + 2\log(\text{abs}(bx+a)) - \text{real_part}(\cos_integral(2bx+2a)) - \text{real_part}(\cos_integral(-2bx-2a)))/b^2$

3.57 $\int \sin(a + bx) \text{Si}(a + bx) dx$

Optimal. Leaf size=34

$$\frac{\text{Si}(2a + 2bx)}{2b} - \frac{\text{Si}(a + bx) \cos(a + bx)}{b}$$

[Out] -((Cos[a + b*x]*SinIntegral[a + b*x])/b) + SinIntegral[2*a + 2*b*x]/(2*b)

Rubi [A] time = 0.0541703, antiderivative size = 34, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {6511, 4406, 12, 3299}

$$\frac{\text{Si}(2a + 2bx)}{2b} - \frac{\text{Si}(a + bx) \cos(a + bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[Sin[a + b*x]*SinIntegral[a + b*x], x]

[Out] -((Cos[a + b*x]*SinIntegral[a + b*x])/b) + SinIntegral[2*a + 2*b*x]/(2*b)

Rule 6511

Int[Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :> -Simp[(Cos[a + b*x]*SinIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] :> Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 12

Int[(a_.)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_.)*(v_) /; FreeQ[b, x]]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned} \int \sin(a + bx) \text{Si}(a + bx) dx &= -\frac{\cos(a + bx) \text{Si}(a + bx)}{b} + \int \frac{\cos(a + bx) \sin(a + bx)}{a + bx} dx \\ &= -\frac{\cos(a + bx) \text{Si}(a + bx)}{b} + \int \frac{\sin(2a + 2bx)}{2(a + bx)} dx \\ &= -\frac{\cos(a + bx) \text{Si}(a + bx)}{b} + \frac{1}{2} \int \frac{\sin(2a + 2bx)}{a + bx} dx \\ &= -\frac{\cos(a + bx) \text{Si}(a + bx)}{b} + \frac{\text{Si}(2a + 2bx)}{2b} \end{aligned}$$

Mathematica [A] time = 0.01693, size = 33, normalized size = 0.97

$$\frac{\text{Si}(2(a + bx))}{2b} - \frac{\text{Si}(a + bx) \cos(a + bx)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[Sin[a + b*x]*SinIntegral[a + b*x],x]

[Out] -((Cos[a + b*x]*SinIntegral[a + b*x])/b) + SinIntegral[2*(a + b*x)]/(2*b)

Maple [A] time = 0.049, size = 31, normalized size = 0.9

$$\frac{1}{b} \left(-\cos(bx + a) \text{Si}(bx + a) + \frac{\text{Si}(2bx + 2a)}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x+a)*sin(b*x+a),x)

[Out] 1/b*(-cos(b*x+a)*Si(b*x+a)+1/2*Si(2*b*x+2*a))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Si}(bx + a) \sin(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)*sin(b*x+a),x, algorithm="maxima")

[Out] integrate(Si(b*x + a)*sin(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(\sin(bx + a) \text{Si}(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)*sin(b*x+a),x, algorithm="fricas")

[Out] integral(sin(b*x + a)*sin_integral(b*x + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \sin(a + bx) \text{Si}(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Si(b*x+a)*sin(b*x+a),x)
```

```
[Out] Integral(sin(a + b*x)*Si(a + b*x), x)
```

Giac [C] time = 1.19919, size = 77, normalized size = 2.26

$$-\frac{\cos(bx + a)\operatorname{Si}(bx + a)}{b} + \frac{\Im(\operatorname{Ci}(2bx + 2a)) - \Im(\operatorname{Ci}(-2bx - 2a)) + 2\operatorname{Si}(2bx + 2a)}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Si(b*x+a)*sin(b*x+a),x, algorithm="giac")
```

```
[Out] -cos(b*x + a)*sin_integral(b*x + a)/b + 1/4*(imag_part(cos_integral(2*b*x +
2*a)) - imag_part(cos_integral(-2*b*x - 2*a)) + 2*sin_integral(2*b*x + 2*a
))/b
```

$$3.58 \quad \int \frac{\sin(a+bx)\text{Si}(a+bx)}{x} dx$$

Optimal. Leaf size=18

$$\text{CannotIntegrate}\left(\frac{\text{Si}(a+bx)\sin(a+bx)}{x}, x\right)$$

[Out] CannotIntegrate[(Sin[a + b*x]*SinIntegral[a + b*x])/x, x]

Rubi [A] time = 0.122967, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\sin(a+bx)\text{Si}(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Int[(Sin[a + b*x]*SinIntegral[a + b*x])/x,x]

[Out] Defer[Int] [(Sin[a + b*x]*SinIntegral[a + b*x])/x, x]

Rubi steps

$$\int \frac{\sin(a+bx)\text{Si}(a+bx)}{x} dx = \int \frac{\sin(a+bx)\text{Si}(a+bx)}{x} dx$$

Mathematica [A] time = 4.92098, size = 0, normalized size = 0.

$$\int \frac{\sin(a+bx)\text{Si}(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[(Sin[a + b*x]*SinIntegral[a + b*x])/x,x]

[Out] Integrate[(Sin[a + b*x]*SinIntegral[a + b*x])/x, x]

Maple [A] time = 0.081, size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx+a)\sin(bx+a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(b*x+a)*sin(b*x+a)/x,x)

[Out] int(Si(b*x+a)*sin(b*x+a)/x,x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx + a) \sin(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)*sin(b*x+a)/x,x, algorithm="maxima")

[Out] integrate(Si(b*x + a)*sin(b*x + a)/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\sin(bx + a) \text{Si}(bx + a)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)*sin(b*x+a)/x,x, algorithm="fricas")

[Out] integral(sin(b*x + a)*sin_integral(b*x + a)/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sin(a + bx) \text{Si}(a + bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)*sin(b*x+a)/x,x)

[Out] Integral(sin(a + b*x)*Si(a + b*x)/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx + a) \sin(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(b*x+a)*sin(b*x+a)/x,x, algorithm="giac")

[Out] integrate(Si(b*x + a)*sin(b*x + a)/x, x)

3.59 $\int x^2 \cos(a + bx) \mathbf{Si}(a + bx) dx$

Optimal. Leaf size=218

$$\frac{a^2 \text{CosIntegral}(2a + 2bx)}{2b^3} - \frac{a^2 \log(a + bx)}{2b^3} - \frac{\text{CosIntegral}(2a + 2bx)}{b^3} + \frac{a \text{Si}(2a + 2bx)}{b^3} - \frac{2 \text{Si}(a + bx) \sin(a + bx)}{b^3} + \frac{2x \text{Si}(a + bx)}{b^3}$$

[Out] (a*x)/(2*b^2) - x^2/(4*b) + Cos[2*a + 2*b*x]/(2*b^3) - CosIntegral[2*a + 2*b*x]/b^3 + (a^2*CosIntegral[2*a + 2*b*x])/(2*b^3) + Log[a + b*x]/b^3 - (a^2*Log[a + b*x])/(2*b^3) - (a*Cos[a + b*x]*Sin[a + b*x])/(2*b^3) + (x*Cos[a + b*x]*Sin[a + b*x])/(2*b^2) - Sin[a + b*x]^2/(4*b^3) + (2*x*Cos[a + b*x]*SinIntegral[a + b*x])/b^2 - (2*SIN[a + b*x]*SinIntegral[a + b*x])/b^3 + (x^2*SIN[a + b*x]*SinIntegral[a + b*x])/b + (a*SINIntegral[2*a + 2*b*x])/b^3

Rubi [A] time = 0.659721, antiderivative size = 218, normalized size of antiderivative = 1., number of steps used = 21, number of rules used = 14, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.875$, Rules used = {6519, 6742, 2635, 8, 3310, 30, 3312, 3302, 6513, 4573, 6741, 2638, 3299, 6517}

$$\frac{a^2 \text{CosIntegral}(2a + 2bx)}{2b^3} - \frac{a^2 \log(a + bx)}{2b^3} - \frac{\text{CosIntegral}(2a + 2bx)}{b^3} + \frac{a \text{Si}(2a + 2bx)}{b^3} - \frac{2 \text{Si}(a + bx) \sin(a + bx)}{b^3} + \frac{2x \text{Si}(a + bx)}{b^3}$$

Antiderivative was successfully verified.

[In] Int[x^2*Cos[a + b*x]*SinIntegral[a + b*x],x]

[Out] (a*x)/(2*b^2) - x^2/(4*b) + Cos[2*a + 2*b*x]/(2*b^3) - CosIntegral[2*a + 2*b*x]/b^3 + (a^2*CosIntegral[2*a + 2*b*x])/(2*b^3) + Log[a + b*x]/b^3 - (a^2*Log[a + b*x])/(2*b^3) - (a*Cos[a + b*x]*Sin[a + b*x])/(2*b^3) + (x*Cos[a + b*x]*Sin[a + b*x])/(2*b^2) - Sin[a + b*x]^2/(4*b^3) + (2*x*Cos[a + b*x]*SinIntegral[a + b*x])/b^2 - (2*SIN[a + b*x]*SinIntegral[a + b*x])/b^3 + (x^2*SIN[a + b*x]*SinIntegral[a + b*x])/b + (a*SINIntegral[2*a + 2*b*x])/b^3

Rule 6519

Int[Cos[(a_.) + (b_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.)*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := Simp[((e + f*x)^m*SIN[a + b*x]*SinIntegral[c + d*x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*SIN[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*SIN[a + b*x]*SinIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]

Rule 6742

Int[u_, x_Symbol] := With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]]

Rule 2635

Int[((b_.)*sin[(c_.) + (d_.)*(x_)])^(n_), x_Symbol] := -Simp[(b*Cos[c + d*x]*(b*SIN[c + d*x])^(n - 1))/(d*n), x] + Dist[(b^2*(n - 1))/n, Int[(b*SIN[c + d*x])^(n - 2), x], x] /; FreeQ[{b, c, d}, x] && GtQ[n, 1] && IntegerQ[2*n]

Rule 8

Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]

Rule 3310

```
Int[((c_.) + (d_.)*(x_))*((b_.)*sin[(e_.) + (f_.)*(x_)])^(n_), x_Symbol] :=
  Simp[(d*(b*SIN[e + f*x])^n)/(f^2*n^2), x] + (Dist[(b^2*(n - 1))/n, Int[(c
+ d*x)*(b*SIN[e + f*x])^(n - 2), x], x] - Simp[(b*(c + d*x)*Cos[e + f*x]*(b
*SIN[e + f*x])^(n - 1))/(f*n), x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1
]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 3312

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := In
t[ExpandTrigReduce[(c + d*x)^m, SIN[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f
, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rule 6513

```
Int[((e_.) + (f_.)*(x_))^(m_)*Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) +
(d_.)*(x_)], x_Symbol] := -Simp[((e + f*x)^m*cos[a + b*x]*SinIntegral[c + d
*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*cos[a + b*x]*Sin[c + d*x])/(c + d*
x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*cos[a + b*x]*SinIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 4573

```
Int[Cos[w_]^(p_.)*(u_.)*Sin[v_]^(p_.), x_Symbol] := Dist[1/2^p, Int[u*SIN[2
*v]^p, x], x] /; EqQ[w, v] && IntegerQ[p]
```

Rule 6741

```
Int[u_, x_Symbol] := With[{v = NormalizeIntegrand[u, x]}, Int[v, x] /; v !=
= u]
```

Rule 2638

```
Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] := -Simp[Cos[c + d*x]/d, x] /; FreeQ
[{c, d}, x]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SINInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 6517

```
Int[Cos[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := S
imp[(SIN[a + b*x]*SinIntegral[c + d*x])/b, x] - Dist[d/b, Int[(SIN[a + b*x]
*SIN[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\begin{aligned}
\int x^2 \cos(a + bx) \operatorname{Si}(a + bx) dx &= \frac{x^2 \sin(a + bx) \operatorname{Si}(a + bx)}{b} - \frac{2 \int x \sin(a + bx) \operatorname{Si}(a + bx) dx}{b} - \int \frac{x^2 \sin^2(a + bx)}{a + bx} dx \\
&= \frac{2x \cos(a + bx) \operatorname{Si}(a + bx)}{b^2} + \frac{x^2 \sin(a + bx) \operatorname{Si}(a + bx)}{b} - \frac{2 \int \cos(a + bx) \operatorname{Si}(a + bx) dx}{b^2} - \frac{2 \int \frac{x^2 \sin^2(a + bx)}{a + bx} dx}{b^2} \\
&= \frac{2x \cos(a + bx) \operatorname{Si}(a + bx)}{b^2} - \frac{2 \sin(a + bx) \operatorname{Si}(a + bx)}{b^3} + \frac{x^2 \sin(a + bx) \operatorname{Si}(a + bx)}{b} + \frac{2 \int \frac{x^2 \sin^2(a + bx)}{a + bx} dx}{b^2} \\
&= -\frac{a \cos(a + bx) \sin(a + bx)}{2b^3} + \frac{x \cos(a + bx) \sin(a + bx)}{2b^2} - \frac{\sin^2(a + bx)}{4b^3} + \frac{2x \cos(a + bx) \operatorname{Si}(a + bx)}{b^2} \\
&= \frac{ax}{2b^2} - \frac{x^2}{4b} + \frac{\log(a + bx)}{b^3} - \frac{a^2 \log(a + bx)}{2b^3} - \frac{a \cos(a + bx) \sin(a + bx)}{2b^3} + \frac{x \cos(a + bx) \operatorname{Si}(a + bx)}{2b^2} \\
&= \frac{ax}{2b^2} - \frac{x^2}{4b} - \frac{\operatorname{Ci}(2a + 2bx)}{b^3} + \frac{a^2 \operatorname{Ci}(2a + 2bx)}{2b^3} + \frac{\log(a + bx)}{b^3} - \frac{a^2 \log(a + bx)}{2b^3} - \frac{a \cos(a + bx) \sin(a + bx)}{2b^3} \\
&= \frac{ax}{2b^2} - \frac{x^2}{4b} + \frac{\cos(2a + 2bx)}{2b^3} - \frac{\operatorname{Ci}(2a + 2bx)}{b^3} + \frac{a^2 \operatorname{Ci}(2a + 2bx)}{2b^3} + \frac{\log(a + bx)}{b^3} - \frac{a^2 \log(a + bx)}{2b^3}
\end{aligned}$$

Mathematica [A] time = 0.343218, size = 134, normalized size = 0.61

$$\frac{4(a^2 - 2) \operatorname{CosIntegral}(2(a + bx)) - 4a^2 \log(a + bx) + 8 \operatorname{Si}(a + bx) \left((b^2 x^2 - 2) \sin(a + bx) + 2bx \cos(a + bx) \right) + 8a \operatorname{Si}(2(a + bx))}{8b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*Cos[a + b*x]*SinIntegral[a + b*x],x]

[Out] (4*a*b*x - 2*b^2*x^2 + 5*Cos[2*(a + b*x)] + 4*(-2 + a^2)*CosIntegral[2*(a + b*x)] + 8*Log[a + b*x] - 4*a^2*Log[a + b*x] - 2*a*Sin[2*(a + b*x)] + 2*b*x*Sin[2*(a + b*x)] + 8*(2*b*x*Cos[a + b*x] + (-2 + b^2*x^2)*Sin[a + b*x])*SinIntegral[a + b*x] + 8*a*SinIntegral[2*(a + b*x)])/(8*b^3)

Maple [A] time = 0.068, size = 209, normalized size = 1.

$$\frac{x^2 \operatorname{Si}(bx + a) \sin(bx + a)}{b} + 2 \frac{x \cos(bx + a) \operatorname{Si}(bx + a)}{b^2} - 2 \frac{\operatorname{Si}(bx + a) \sin(bx + a)}{b^3} + \frac{x \cos(bx + a) \sin(bx + a)}{2b^2} - \frac{a \cos(bx + a) \operatorname{Si}(bx + a)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*cos(b*x+a)*Si(b*x+a),x)

[Out] x^2*Si(b*x+a)*sin(b*x+a)/b+2*x*cos(b*x+a)*Si(b*x+a)/b^2-2*Si(b*x+a)*sin(b*x+a)/b^3+1/2*x*cos(b*x+a)*sin(b*x+a)/b^2-1/2*a*cos(b*x+a)*sin(b*x+a)/b^3-1/4*x^2/b+1/2*a*x/b^2+3/4/b^3*a^2-1/4*sin(b*x+a)^2/b^3-1/2*a^2*ln(b*x+a)/b^3+1/2*a^2*Ci(2*b*x+2*a)/b^3+cos(b*x+a)^2/b^3+a*Si(2*b*x+2*a)/b^3+ln(b*x+a)/b^3-Ci(2*b*x+2*a)/b^3

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \operatorname{Si}(bx + a) \cos(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*cos(b*x+a)*Si(b*x+a),x, algorithm="maxima")

[Out] integrate(x^2*Si(b*x + a)*cos(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^2 \cos(bx + a) \text{Si}(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*cos(b*x+a)*Si(b*x+a),x, algorithm="fricas")

[Out] integral(x^2*cos(b*x + a)*sin_integral(b*x + a), x)

Sympy [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*cos(b*x+a)*Si(b*x+a),x)

[Out] Timed out

Giac [C] time = 1.21811, size = 231, normalized size = 1.06

$$\left(\frac{2x \cos(bx + a)}{b^2} + \frac{(b^2x^2 - 2) \sin(bx + a)}{b^3} \right) \text{Si}(bx + a) - \frac{b^2x^2 - 2abx + 2a^2 \log(|bx + a|) - a^2 \Re(\text{Ci}(2bx + 2a)) - a^2}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*cos(b*x+a)*Si(b*x+a),x, algorithm="giac")

[Out] (2*x*cos(b*x + a)/b^2 + (b^2*x^2 - 2)*sin(b*x + a)/b^3)*sin_integral(b*x + a) - 1/4*(b^2*x^2 - 2*a*b*x + 2*a^2*log(abs(b*x + a)) - a^2*real_part(cos_integral(2*b*x + 2*a)) - a^2*real_part(cos_integral(-2*b*x - 2*a)) - 2*a*imag_part(cos_integral(2*b*x + 2*a)) + 2*a*imag_part(cos_integral(-2*b*x - 2*a))) - 4*a*sin_integral(2*b*x + 2*a) - 4*log(abs(b*x + a)) + 2*real_part(cos_integral(2*b*x + 2*a)) + 2*real_part(cos_integral(-2*b*x - 2*a)))/b^3

3.60 $\int x \cos(a + bx) \text{Si}(a + bx) dx$

Optimal. Leaf size=108

$$-\frac{a \text{CosIntegral}(2a + 2bx)}{2b^2} - \frac{\text{Si}(2a + 2bx)}{2b^2} + \frac{\text{Si}(a + bx) \cos(a + bx)}{b^2} + \frac{a \log(a + bx)}{2b^2} + \frac{\sin(a + bx) \cos(a + bx)}{2b^2} + \frac{x \text{Si}(a + bx)}{b}$$

```
[Out] -x/(2*b) - (a*CosIntegral[2*a + 2*b*x])/(2*b^2) + (a*Log[a + b*x])/(2*b^2)
+ (Cos[a + b*x]*Sin[a + b*x])/(2*b^2) + (Cos[a + b*x]*SinIntegral[a + b*x])
/b^2 + (x*Sin[a + b*x]*SinIntegral[a + b*x])/b - SinIntegral[2*a + 2*b*x]/(
2*b^2)
```

Rubi [A] time = 0.231651, antiderivative size = 108, normalized size of antiderivative = 1., number of steps used = 12, number of rules used = 10, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.714$, Rules used = {6519, 6742, 2635, 8, 3312, 3302, 6511, 4406, 12, 3299}

$$-\frac{a \text{CosIntegral}(2a + 2bx)}{2b^2} - \frac{\text{Si}(2a + 2bx)}{2b^2} + \frac{\text{Si}(a + bx) \cos(a + bx)}{b^2} + \frac{a \log(a + bx)}{2b^2} + \frac{\sin(a + bx) \cos(a + bx)}{2b^2} + \frac{x \text{Si}(a + bx)}{b}$$

Antiderivative was successfully verified.

```
[In] Int[x*Cos[a + b*x]*SinIntegral[a + b*x],x]
```

```
[Out] -x/(2*b) - (a*CosIntegral[2*a + 2*b*x])/(2*b^2) + (a*Log[a + b*x])/(2*b^2)
+ (Cos[a + b*x]*Sin[a + b*x])/(2*b^2) + (Cos[a + b*x]*SinIntegral[a + b*x])
/b^2 + (x*Sin[a + b*x]*SinIntegral[a + b*x])/b - SinIntegral[2*a + 2*b*x]/(
2*b^2)
```

Rule 6519

```
Int[Cos[(a_.) + (b_.)*(x_.)]*((e_.) + (f_.)*(x_.))^(m_.)*SinIntegral[(c_.) +
(d_.)*(x_.)], x_Symbol] := Simp[((e + f*x)^m*Sin[a + b*x]*SinIntegral[c + d*
x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*Sin[a + b*x]*Sin[c + d*x])/(c + d*
x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Sin[a + b*x]*SinIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 6742

```
Int[u_, x_Symbol] := With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]
]
```

Rule 2635

```
Int[((b_.)*sin[(c_.) + (d_.)*(x_.)])^(n_), x_Symbol] := -Simp[(b*Cos[c + d*x]
)*(b*Sin[c + d*x])^(n - 1))/(d*n), x] + Dist[(b^2*(n - 1))/n, Int[(b*Sin[c
+ d*x])^(n - 2), x], x] /; FreeQ[{b, c, d}, x] && GtQ[n, 1] && IntegerQ[2*n]
]
```

Rule 8

```
Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]
```

Rule 3312

```
Int[((c_.) + (d_.)*(x_.))^(m_.)*sin[(e_.) + (f_.)*(x_.)]^(n_), x_Symbol] := In
t[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f
, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rule 6511

```
Int[Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := -Simp[(Cos[a + b*x]*SinIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int x \cos(a + bx) \operatorname{Si}(a + bx) dx &= \frac{x \sin(a + bx) \operatorname{Si}(a + bx)}{b} - \frac{\int \sin(a + bx) \operatorname{Si}(a + bx) dx}{b} - \int \frac{x \sin^2(a + bx)}{a + bx} dx \\
&= \frac{\cos(a + bx) \operatorname{Si}(a + bx)}{b^2} + \frac{x \sin(a + bx) \operatorname{Si}(a + bx)}{b} - \frac{\int \frac{\cos(a + bx) \sin(a + bx)}{a + bx} dx}{b} - \int \left(\frac{\sin^2(a + bx)}{a + bx} \right) dx \\
&= \frac{\cos(a + bx) \operatorname{Si}(a + bx)}{b^2} + \frac{x \sin(a + bx) \operatorname{Si}(a + bx)}{b} - \frac{\int \sin^2(a + bx) dx}{b} - \frac{\int \frac{\sin(2a + 2bx)}{2(a + bx)} dx}{b} \\
&= \frac{\cos(a + bx) \sin(a + bx)}{2b^2} + \frac{\cos(a + bx) \operatorname{Si}(a + bx)}{b^2} + \frac{x \sin(a + bx) \operatorname{Si}(a + bx)}{b} - \frac{\int 1 dx}{2b} \\
&= -\frac{x}{2b} + \frac{a \log(a + bx)}{2b^2} + \frac{\cos(a + bx) \sin(a + bx)}{2b^2} + \frac{\cos(a + bx) \operatorname{Si}(a + bx)}{b^2} + \frac{x \sin(a + bx) \operatorname{Si}(a + bx)}{b} \\
&= -\frac{x}{2b} - \frac{a \operatorname{Ci}(2a + 2bx)}{2b^2} + \frac{a \log(a + bx)}{2b^2} + \frac{\cos(a + bx) \sin(a + bx)}{2b^2} + \frac{\cos(a + bx) \operatorname{Si}(a + bx)}{b^2}
\end{aligned}$$

Mathematica [A] time = 0.198282, size = 74, normalized size = 0.69

$$\frac{-2a \operatorname{CosIntegral}(2(a + bx)) - 2 \operatorname{Si}(2(a + bx)) + 4 \operatorname{Si}(a + bx)(bx \sin(a + bx) + \cos(a + bx)) + 2a \log(a + bx) + \sin(2(a + bx))}{4b^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[x*Cos[a + b*x]*SinIntegral[a + b*x], x]
```

```
[Out] (-2*b*x - 2*a*CosIntegral[2*(a + b*x)] + 2*a*Log[a + b*x] + Sin[2*(a + b*x)] + 4*(Cos[a + b*x] + b*x*Sin[a + b*x])*SinIntegral[a + b*x] - 2*SinIntegral[a + b*x])
```

$1[2*(a + b*x)]/(4*b^2)$

Maple [A] time = 0.061, size = 105, normalized size = 1.

$$\frac{x\text{Si}(bx+a)\sin(bx+a)}{b} + \frac{\cos(bx+a)\text{Si}(bx+a)}{b^2} + \frac{\cos(bx+a)\sin(bx+a)}{2b^2} - \frac{x}{2b} - \frac{a}{2b^2} - \frac{\text{Si}(2bx+2a)}{2b^2} + \frac{a\ln(bx+a)}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*cos(b*x+a)*Si(b*x+a),x)`

[Out] `x*Si(b*x+a)*sin(b*x+a)/b+cos(b*x+a)*Si(b*x+a)/b^2+1/2*cos(b*x+a)*sin(b*x+a)/b^2-1/2*x/b-1/2/b^2*a-1/2*Si(2*b*x+2*a)/b^2+1/2*a*ln(b*x+a)/b^2-1/2*a*Ci(2*b*x+2*a)/b^2`

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x\text{Si}(bx+a)\cos(bx+a)dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*cos(b*x+a)*Si(b*x+a),x, algorithm="maxima")`

[Out] `integrate(x*Si(b*x + a)*cos(b*x + a), x)`

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x\cos(bx+a)\text{Si}(bx+a),x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*cos(b*x+a)*Si(b*x+a),x, algorithm="fricas")`

[Out] `integral(x*cos(b*x + a)*sin_integral(b*x + a), x)`

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x\cos(a+bx)\text{Si}(a+bx)dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*cos(b*x+a)*Si(b*x+a),x)`

[Out] `Integral(x*cos(a + b*x)*Si(a + b*x), x)`

Giac [C] time = 1.20177, size = 144, normalized size = 1.33

$$\left(\frac{x \sin(bx + a)}{b} + \frac{\cos(bx + a)}{b^2}\right) \text{Si}(bx + a) - \frac{2bx - 2a \log(|bx + a|) + a\Re(\text{Ci}(2bx + 2a)) + a\Re(\text{Ci}(-2bx - 2a)) + 2a\Im(\text{Ci}(2bx + 2a)) + 2a\Im(\text{Ci}(-2bx - 2a))}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*cos(b*x+a)*Si(b*x+a),x, algorithm="giac")

[Out] (x*sin(b*x + a)/b + cos(b*x + a)/b^2)*sin_integral(b*x + a) - 1/4*(2*b*x - 2*a*log(abs(b*x + a)) + a*real_part(cos_integral(2*b*x + 2*a)) + a*real_part(cos_integral(-2*b*x - 2*a)) + imag_part(cos_integral(2*b*x + 2*a)) - imag_part(cos_integral(-2*b*x - 2*a)) + 2*sin_integral(2*b*x + 2*a))/b^2

3.61 $\int \cos(a + bx)\text{Si}(a + bx) dx$

Optimal. Leaf size=46

$$\frac{\text{CosIntegral}(2a + 2bx)}{2b} + \frac{\text{Si}(a + bx)\sin(a + bx)}{b} - \frac{\log(a + bx)}{2b}$$

[Out] CosIntegral[2*a + 2*b*x]/(2*b) - Log[a + b*x]/(2*b) + (Sin[a + b*x]*SinIntegral[a + b*x])/b

Rubi [A] time = 0.074803, antiderivative size = 46, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {6517, 3312, 3302}

$$\frac{\text{CosIntegral}(2a + 2bx)}{2b} + \frac{\text{Si}(a + bx)\sin(a + bx)}{b} - \frac{\log(a + bx)}{2b}$$

Antiderivative was successfully verified.

[In] Int[Cos[a + b*x]*SinIntegral[a + b*x],x]

[Out] CosIntegral[2*a + 2*b*x]/(2*b) - Log[a + b*x]/(2*b) + (Sin[a + b*x]*SinIntegral[a + b*x])/b

Rule 6517

Int[Cos[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :> Simp[(Sin[a + b*x]*SinIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 3312

Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] :> Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned} \int \cos(a + bx)\text{Si}(a + bx) dx &= \frac{\sin(a + bx)\text{Si}(a + bx)}{b} - \int \frac{\sin^2(a + bx)}{a + bx} dx \\ &= \frac{\sin(a + bx)\text{Si}(a + bx)}{b} - \int \left(\frac{1}{2(a + bx)} - \frac{\cos(2a + 2bx)}{2(a + bx)} \right) dx \\ &= -\frac{\log(a + bx)}{2b} + \frac{\sin(a + bx)\text{Si}(a + bx)}{b} + \frac{1}{2} \int \frac{\cos(2a + 2bx)}{a + bx} dx \\ &= \frac{\text{Ci}(2a + 2bx)}{2b} - \frac{\log(a + bx)}{2b} + \frac{\sin(a + bx)\text{Si}(a + bx)}{b} \end{aligned}$$

Mathematica [A] time = 0.020974, size = 45, normalized size = 0.98

$$\frac{\text{CosIntegral}(2(a + bx))}{2b} + \frac{\text{Si}(a + bx) \sin(a + bx)}{b} - \frac{\log(a + bx)}{2b}$$

Antiderivative was successfully verified.

[In] Integrate[Cos[a + b*x]*SinIntegral[a + b*x], x]

[Out] CosIntegral[2*(a + b*x)]/(2*b) - Log[a + b*x]/(2*b) + (Sin[a + b*x]*SinIntegral[a + b*x])/b

Maple [A] time = 0.055, size = 43, normalized size = 0.9

$$\frac{\text{Ci}(2bx + 2a)}{2b} - \frac{\ln(bx + a)}{2b} + \frac{\text{Si}(bx + a) \sin(bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(b*x+a)*Si(b*x+a), x)

[Out] 1/2*Ci(2*b*x+2*a)/b-1/2*ln(b*x+a)/b+Si(b*x+a)*sin(b*x+a)/b

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Si}(bx + a) \cos(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(b*x+a), x, algorithm="maxima")

[Out] integrate(Si(b*x + a)*cos(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(\cos(bx + a) \text{Si}(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(b*x+a), x, algorithm="fricas")

[Out] integral(cos(b*x + a)*sin_integral(b*x + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \cos(a + bx) \text{Si}(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(b*x+a),x)

[Out] Integral(cos(a + b*x)*Si(a + b*x), x)

Giac [B] time = 1.17286, size = 128, normalized size = 2.78

$$\frac{\sin(bx + a) \operatorname{Si}(bx + a)}{b} + \frac{\cos(2a)^2 \operatorname{Ci}(2bx + 2a) + \cos(2a)^2 \operatorname{Ci}(-2bx - 2a) + \operatorname{Ci}(2bx + 2a) \sin(2a)^2 + \operatorname{Ci}(-2bx - 2a) \sin(2a)^2}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(b*x+a),x, algorithm="giac")

[Out] sin(b*x + a)*sin_integral(b*x + a)/b + 1/4*(cos(2*a)^2*cos_integral(2*b*x + 2*a) + cos(2*a)^2*cos_integral(-2*b*x - 2*a) + cos_integral(2*b*x + 2*a)*sin(2*a)^2 + cos_integral(-2*b*x - 2*a)*sin(2*a)^2 - 2*log(b*x + a))/b

$$3.62 \quad \int \frac{\cos(a+bx)\text{Si}(a+bx)}{x} dx$$

Optimal. Leaf size=18

$$\text{CannotIntegrate}\left(\frac{\text{Si}(a+bx)\cos(a+bx)}{x}, x\right)$$

[Out] CannotIntegrate[(Cos[a + b*x]*SinIntegral[a + b*x])/x, x]

Rubi [A] time = 0.124983, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\cos(a+bx)\text{Si}(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Int[(Cos[a + b*x]*SinIntegral[a + b*x])/x,x]

[Out] Defer[Int] [(Cos[a + b*x]*SinIntegral[a + b*x])/x, x]

Rubi steps

$$\int \frac{\cos(a+bx)\text{Si}(a+bx)}{x} dx = \int \frac{\cos(a+bx)\text{Si}(a+bx)}{x} dx$$

Mathematica [A] time = 2.61414, size = 0, normalized size = 0.

$$\int \frac{\cos(a+bx)\text{Si}(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[(Cos[a + b*x]*SinIntegral[a + b*x])/x,x]

[Out] Integrate[(Cos[a + b*x]*SinIntegral[a + b*x])/x, x]

Maple [A] time = 0.086, size = 0, normalized size = 0.

$$\int \frac{\cos(bx+a)\text{Si}(bx+a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(b*x+a)*Si(b*x+a)/x,x)

[Out] int(cos(b*x+a)*Si(b*x+a)/x,x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx + a) \cos(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(b*x+a)/x,x, algorithm="maxima")

[Out] integrate(Si(b*x + a)*cos(b*x + a)/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\cos(bx + a) \text{Si}(bx + a)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(b*x+a)/x,x, algorithm="fricas")

[Out] integral(cos(b*x + a)*sin_integral(b*x + a)/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\cos(a + bx) \text{Si}(a + bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(b*x+a)/x,x)

[Out] Integral(cos(a + b*x)*Si(a + b*x)/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(bx + a) \cos(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(b*x+a)/x,x, algorithm="giac")

[Out] integrate(Si(b*x + a)*cos(b*x + a)/x, x)

3.63 $\int x \sin(a + bx) \text{Si}(c + dx) dx$

Optimal. Leaf size=371

$$\frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b^2} + \frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b+d)}{d} + x(b+d)\right)}{2b^2} + \frac{\sin\left(a - \frac{bc}{d}\right) \text{Si}\left(x(b-d)\right)}{2b^2}$$

```
[Out] Cos[a - c + (b - d)*x]/(2*b*(b - d)) - Cos[a + c + (b + d)*x]/(2*b*(b + d))
- (Cos[a - (b*c)/d]*CosIntegral[(c*(b - d))/d + (b - d)*x])/(2*b^2) + (Cos
[a - (b*c)/d]*CosIntegral[(c*(b + d))/d + (b + d)*x])/(2*b^2) + (c*CosInteg
ral[(c*(b - d))/d + (b - d)*x]*Sin[a - (b*c)/d])/(2*b*d) - (c*CosIntegral[(c
*(b + d))/d + (b + d)*x]*Sin[a - (b*c)/d])/(2*b*d) + (c*Cos[a - (b*c)/d]*S
inIntegral[(c*(b - d))/d + (b - d)*x])/(2*b*d) + (Sin[a - (b*c)/d]*SinInteg
ral[(c*(b - d))/d + (b - d)*x])/(2*b^2) - (x*Cos[a + b*x]*SinIntegral[c + d
*x])/b + (Sin[a + b*x]*SinIntegral[c + d*x])/b^2 - (c*Cos[a - (b*c)/d]*SinI
ntegral[(c*(b + d))/d + (b + d)*x])/(2*b*d) - (Sin[a - (b*c)/d]*SinIntegral
[(c*(b + d))/d + (b + d)*x])/(2*b^2)
```

Rubi [A] time = 0.920128, antiderivative size = 371, normalized size of antiderivative = 1., number of steps used = 24, number of rules used = 10, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.714$, Rules used = {6513, 6742, 4574, 2638, 4430, 3303, 3299, 3302, 6517, 4428}

$$\frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b^2} + \frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b+d)}{d} + x(b+d)\right)}{2b^2} + \frac{\sin\left(a - \frac{bc}{d}\right) \text{Si}\left(x(b-d)\right)}{2b^2}$$

Antiderivative was successfully verified.

```
[In] Int[x*Sin[a + b*x]*SinIntegral[c + d*x],x]
```

```
[Out] Cos[a - c + (b - d)*x]/(2*b*(b - d)) - Cos[a + c + (b + d)*x]/(2*b*(b + d))
- (Cos[a - (b*c)/d]*CosIntegral[(c*(b - d))/d + (b - d)*x])/(2*b^2) + (Cos
[a - (b*c)/d]*CosIntegral[(c*(b + d))/d + (b + d)*x])/(2*b^2) + (c*CosInteg
ral[(c*(b - d))/d + (b - d)*x]*Sin[a - (b*c)/d])/(2*b*d) - (c*CosIntegral[(c
*(b + d))/d + (b + d)*x]*Sin[a - (b*c)/d])/(2*b*d) + (c*Cos[a - (b*c)/d]*S
inIntegral[(c*(b - d))/d + (b - d)*x])/(2*b*d) + (Sin[a - (b*c)/d]*SinInteg
ral[(c*(b - d))/d + (b - d)*x])/(2*b^2) - (x*Cos[a + b*x]*SinIntegral[c + d
*x])/b + (Sin[a + b*x]*SinIntegral[c + d*x])/b^2 - (c*Cos[a - (b*c)/d]*SinI
ntegral[(c*(b + d))/d + (b + d)*x])/(2*b*d) - (Sin[a - (b*c)/d]*SinIntegral
[(c*(b + d))/d + (b + d)*x])/(2*b^2)
```

Rule 6513

```
Int[((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) +
(d_.)*(x_)], x_Symbol] := -Simp[((e + f*x)^m*Cos[a + b*x]*SinIntegral[c + d
*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*Cos[a + b*x]*Sin[c + d*x])/(c + d*
x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Cos[a + b*x]*SinIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 6742

```
Int[u_, x_Symbol] := With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]
]
```

Rule 4574

```
Int[Cos[w_]^(q_.)*Sin[v_]^(p_.), x_Symbol] := Int[ExpandTrigReduce[Sin[v]^p
*Cos[w]^q, x], x] /; IGtQ[p, 0] && IGtQ[q, 0] && ((PolynomialQ[v, x] && Pol
ynomialQ[w, x]) || (BinomialQ[{v, w}, x] && IndependentQ[Cancel[v/w], x]))
```

Rule 2638

```
Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] := -Simp[Cos[c + d*x]/d, x] /; FreeQ
[{c, d}, x]
```

Rule 4430

```
Int[Cos[(c_.) + (d_.)*(x_)]^(q_.)*((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b
_.)*(x_)]^(p_.), x_Symbol] := Int[ExpandTrigReduce[(e + f*x)^m, Sin[a + b*x
]^p*Cos[c + d*x]^q, x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[p, 0]
&& IGtQ[q, 0]
```

Rule 3303

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Dist[Cos[(d*
e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f
)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] &&
NeQ[d*e - c*f, 0]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rule 6517

```
Int[Cos[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := S
imp[(Sin[a + b*x]*SinIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]
*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 4428

```
Int[((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(p_.)*Sin[(c_.) + (d
_.)*(x_)]^(q_.), x_Symbol] := Int[ExpandTrigReduce[(e + f*x)^m, Sin[a + b*x
]^p*Sin[c + d*x]^q, x], x] /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[p, 0] &&
IGtQ[q, 0] && IntegerQ[m]
```

Rubi steps

$$\begin{aligned}
\int x \sin(a + bx) \operatorname{Si}(c + dx) dx &= -\frac{x \cos(a + bx) \operatorname{Si}(c + dx)}{b} + \frac{\int \cos(a + bx) \operatorname{Si}(c + dx) dx}{b} + \frac{d \int \frac{x \cos(a + bx) \sin(c + dx)}{c + dx} dx}{b} \\
&= -\frac{x \cos(a + bx) \operatorname{Si}(c + dx)}{b} + \frac{\sin(a + bx) \operatorname{Si}(c + dx)}{b^2} - \frac{d \int \frac{\sin(a + bx) \sin(c + dx)}{c + dx} dx}{b^2} + \frac{d \int \left(\frac{\cos(a + bx) \sin(c + dx)}{c + dx} \right) dx}{b^2} \\
&= -\frac{x \cos(a + bx) \operatorname{Si}(c + dx)}{b} + \frac{\sin(a + bx) \operatorname{Si}(c + dx)}{b^2} + \frac{\int \cos(a + bx) \sin(c + dx) dx}{b} - \frac{d \int \frac{\sin(a + bx) \sin(c + dx)}{c + dx} dx}{b^2} \\
&= -\frac{x \cos(a + bx) \operatorname{Si}(c + dx)}{b} + \frac{\sin(a + bx) \operatorname{Si}(c + dx)}{b^2} + \frac{\int \left(-\frac{1}{2} \sin(a - c + (b - d)x) + \frac{1}{2} \sin(a + c + (b + d)x) \right) dx}{b} \\
&= -\frac{x \cos(a + bx) \operatorname{Si}(c + dx)}{b} + \frac{\sin(a + bx) \operatorname{Si}(c + dx)}{b^2} - \frac{\int \sin(a - c + (b - d)x) dx}{2b} + \frac{\int \sin(a + c + (b + d)x) dx}{2b} \\
&= \frac{\cos(a - c + (b - d)x)}{2b(b - d)} - \frac{\cos(a + c + (b + d)x)}{2b(b + d)} - \frac{\cos\left(a - \frac{bc}{d}\right) \operatorname{Ci}\left(\frac{c(b - d)}{d} + (b - d)x\right)}{2b^2} + \frac{\cos\left(a + \frac{bc}{d}\right) \operatorname{Ci}\left(\frac{c(b + d)}{d} + (b + d)x\right)}{2b^2} \\
&= \frac{\cos(a - c + (b - d)x)}{2b(b - d)} - \frac{\cos(a + c + (b + d)x)}{2b(b + d)} - \frac{\cos\left(a - \frac{bc}{d}\right) \operatorname{Ci}\left(\frac{c(b - d)}{d} + (b - d)x\right)}{2b^2} + \frac{\cos\left(a + \frac{bc}{d}\right) \operatorname{Ci}\left(\frac{c(b + d)}{d} + (b + d)x\right)}{2b^2}
\end{aligned}$$

Mathematica [C] time = 5.31338, size = 345, normalized size = 0.93

$$\frac{e^{-i(a+c)} \left(-i(bc - id) e^{\frac{i(d(2a+c)-bc)}{d}} \operatorname{ExpIntegralEi}\left(\frac{i(b-d)(c+dx)}{d}\right) + bd \left(\frac{e^{i(2a+bx-dx)}}{b-d} - \frac{e^{-ix(b+d)}}{b+d} \right) + (d - ibc) e^{\frac{ic(b+d)}{d}} \operatorname{ExpIntegralEi}\left(\frac{ic(b+d)}{d}\right) \right)}{4b^2d}$$

Warning: Unable to verify antiderivative.

[In] Integrate[x*Sin[a + b*x]*SinIntegral[c + d*x], x]

[Out] (b*d*(-1/((b + d)*E^(I*(b + d)*x))) + E^(I*(2*a + b*x - d*x))/(b - d)) - I*(b*c - I*d)*E^((I*(-(b*c) + (2*a + c)*d))/d)*ExpIntegralEi[(I*(b - d)*(c + d*x))/d] + ((-I)*b*c + d)*E^((I*c*(b + d))/d)*ExpIntegralEi[((-I)*(b + d)*(c + d*x))/d]/(4*b^2*d*E^(I*(a + c))) + (b*d*(1/((b - d)*E^(I*(b - d)*x)) - E^(I*(2*a + (b + d)*x))/(b + d)) + I*(b*c + I*d)*E^((I*c*(b - d))/d)*ExpIntegralEi[((-I)*(b - d)*(c + d*x))/d] + ((I*b*c + d)*ExpIntegralEi[(I*(b + d)*(c + d*x))/d])/E^((I*(b*c - 2*a*d + c*d))/d)/(4*b^2*d*E^(I*(a - c))) - ((b*x*Cos[a + b*x] - Sin[a + b*x])*SinIntegral[c + d*x])/b^2

Maple [B] time = 0.108, size = 1212, normalized size = 3.3

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*Si(d*x+c)*sin(b*x+a), x)

[Out] (Si(d*x+c)/b*(1/b*d*(-(b/d*(d*x+c)+(a*d-b*c)/d)*cos(b/d*(d*x+c)+(a*d-b*c)/d)+sin(b/d*(d*x+c)+(a*d-b*c)/d))+a*d/b*cos(b/d*(d*x+c)+(a*d-b*c)/d)-1/b*(-1/2/(b-d)*d*cos((b-d)/d*(d*x+c)+(a*d-b*c)/d)+1/2*(a*d-b*c)*d/(b-d)*(Si((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*cos((-a*d+b*c)/d)/d-Ci((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*sin((-a*d+b*c)/d)/d)-1/2/(b-d)*d^2*a*(Si((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*cos((-a*d+b*c)/d)/d-Ci((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*sin((-a*d+b*c)/d)/d)

```

a*d-b*c)/d+(-a*d+b*c)/d)*sin((-a*d+b*c)/d)/d)+1/2/(b-d)*c*d^2*(Si((b-d)/d*(
d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*cos((-a*d+b*c)/d)/d-Ci((b-d)/d*(d*x+c)+(a*
d-b*c)/d+(-a*d+b*c)/d)*sin((-a*d+b*c)/d)/d)+1/2/(b+d)*d*cos((b+d)/d*(d*x+c)
+(a*d-b*c)/d)-1/2*(a*d-b*c)*d/(b+d)*(Si((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b
*c)/d)*cos((-a*d+b*c)/d)/d-Ci((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*sin(
((-a*d+b*c)/d)/d)+1/2/(b+d)*d^2*a*(Si((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)
)/d)*cos((-a*d+b*c)/d)/d-Ci((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*sin((
-a*d+b*c)/d)/d)+1/2/(b+d)*c*d^2*(Si((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/
d)*cos((-a*d+b*c)/d)/d-Ci((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*sin((-a
*d+b*c)/d)/d)+1/2/b*d^2*(Si((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*sin((
-a*d+b*c)/d)/d+Ci((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*cos((-a*d+b*c)/
d)/d)-1/2/b*d^2*(Si((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*sin((-a*d+b*c)
)/d)/d+Ci((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*cos((-a*d+b*c)/d)/d)))/
d

```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \operatorname{Si}(dx + c) \sin(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(d*x+c)*sin(b*x+a),x, algorithm="maxima")

[Out] integrate(x*Si(d*x + c)*sin(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}(x \sin(bx + a) \operatorname{Si}(dx + c), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(d*x+c)*sin(b*x+a),x, algorithm="fricas")

[Out] integral(x*sin(b*x + a)*sin_integral(d*x + c), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \sin(a + bx) \operatorname{Si}(c + dx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Si(d*x+c)*sin(b*x+a),x)

[Out] Integral(x*sin(a + b*x)*Si(c + d*x), x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*Si(d*x+c)*sin(b*x+a),x, algorithm="giac")
```

```
[Out] Timed out
```

3.64 $\int \sin(a + bx)\mathbf{Si}(c + dx) dx$

Optimal. Leaf size=154

$$-\frac{\sin\left(a - \frac{bc}{d}\right)\text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b} + \frac{\sin\left(a - \frac{bc}{d}\right)\text{CosIntegral}\left(\frac{c(b+d)}{d} + x(b+d)\right)}{2b} - \frac{\cos\left(a - \frac{bc}{d}\right)\mathbf{Si}\left(x(b-d)\right)}{2b}$$

[Out] `-(CosIntegral[(c*(b - d))/d + (b - d)*x]*Sin[a - (b*c)/d])/(2*b) + (CosIntegral[(c*(b + d))/d + (b + d)*x]*Sin[a - (b*c)/d])/(2*b) - (Cos[a - (b*c)/d]*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b) - (Cos[a + b*x]*SinIntegral[c + d*x])/b + (Cos[a - (b*c)/d]*SinIntegral[(c*(b + d))/d + (b + d)*x])/(2*b)`

Rubi [A] time = 0.228481, antiderivative size = 154, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {6511, 4430, 3303, 3299, 3302}

$$-\frac{\sin\left(a - \frac{bc}{d}\right)\text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b} + \frac{\sin\left(a - \frac{bc}{d}\right)\text{CosIntegral}\left(\frac{c(b+d)}{d} + x(b+d)\right)}{2b} - \frac{\cos\left(a - \frac{bc}{d}\right)\mathbf{Si}\left(x(b-d)\right)}{2b}$$

Antiderivative was successfully verified.

[In] `Int[Sin[a + b*x]*SinIntegral[c + d*x], x]`

[Out] `-(CosIntegral[(c*(b - d))/d + (b - d)*x]*Sin[a - (b*c)/d])/(2*b) + (CosIntegral[(c*(b + d))/d + (b + d)*x]*Sin[a - (b*c)/d])/(2*b) - (Cos[a - (b*c)/d]*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b) - (Cos[a + b*x]*SinIntegral[c + d*x])/b + (Cos[a - (b*c)/d]*SinIntegral[(c*(b + d))/d + (b + d)*x])/(2*b)`

Rule 6511

`Int[Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :> Simp[(Cos[a + b*x]*SinIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]`

Rule 4430

`Int[Cos[(c_.) + (d_.)*(x_)]^(q_.)*((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(p_.), x_Symbol] :> Int[ExpandTrigReduce[(e + f*x)^m, Sin[a + b*x]^(p)*Cos[c + d*x]^q, x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[p, 0] && IGtQ[q, 0]`

Rule 3303

`Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]`

Rule 3299

`Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]`

Rule 3302

Int[sin[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned} \int \sin(a + bx)\text{Si}(c + dx) dx &= -\frac{\cos(a + bx)\text{Si}(c + dx)}{b} + \frac{d \int \frac{\cos(a+bx)\sin(c+dx)}{c+dx} dx}{b} \\ &= -\frac{\cos(a + bx)\text{Si}(c + dx)}{b} + \frac{d \int \left(-\frac{\sin(a-c+(b-d)x)}{2(c+dx)} + \frac{\sin(a+c+(b+d)x)}{2(c+dx)} \right) dx}{b} \\ &= -\frac{\cos(a + bx)\text{Si}(c + dx)}{b} - \frac{d \int \frac{\sin(a-c+(b-d)x)}{c+dx} dx}{2b} + \frac{d \int \frac{\sin(a+c+(b+d)x)}{c+dx} dx}{2b} \\ &= -\frac{\cos(a + bx)\text{Si}(c + dx)}{b} - \frac{\left(d \cos\left(a - \frac{bc}{d}\right) \right) \int \frac{\sin\left(\frac{c(b-d)}{d} + (b-d)x\right)}{c+dx} dx}{2b} + \frac{\left(d \cos\left(a - \frac{bc}{d}\right) \right) \int \frac{\sin\left(\frac{c(b+d)}{d} + (b+d)x\right)}{c+dx} dx}{2b} \\ &= -\frac{\text{Ci}\left(\frac{c(b-d)}{d} + (b-d)x\right) \sin\left(a - \frac{bc}{d}\right)}{2b} + \frac{\text{Ci}\left(\frac{c(b+d)}{d} + (b+d)x\right) \sin\left(a - \frac{bc}{d}\right)}{2b} - \frac{\cos\left(a - \frac{bc}{d}\right)}{2b} \end{aligned}$$

Mathematica [C] time = 1.9715, size = 168, normalized size = 1.09

$$\frac{i e^{-\frac{i(ad+bc)}{d}} \left(e^{2ia} \text{ExpIntegralEi}\left(\frac{i(b-d)(c+dx)}{d}\right) - e^{2ia} \text{ExpIntegralEi}\left(\frac{i(b+d)(c+dx)}{d}\right) + 4i e^{\frac{i(ad+bc)}{d}} \cos(a + bx) \text{Si}(c + dx) - e^{\frac{2ibc}{d}} \right)}{4b}$$

Warning: Unable to verify antiderivative.

[In] Integrate[Sin[a + b*x]*SinIntegral[c + d*x],x]

[Out] ((I/4)*(-(E^(((2*I)*b*c)/d)*ExpIntegralEi[(-(I)*(b - d)*(c + d*x))/d]) + E^(((2*I)*a)*ExpIntegralEi[(I*(b - d)*(c + d*x))/d] + E^(((2*I)*b*c)/d)*ExpIntegralEi[(-(I)*(b + d)*(c + d*x))/d] - E^(((2*I)*a)*ExpIntegralEi[(I*(b + d)*(c + d*x))/d] + (4*I)*E^((I*(b*c + a*d))/d)*Cos[a + b*x]*SinIntegral[c + d*x]))/(b*E^((I*(b*c + a*d))/d))

Maple [A] time = 0.072, size = 282, normalized size = 1.8

$$\frac{1}{d} \left(-\frac{\text{Si}(dx + c)d}{b} \cos\left(\frac{b(dx + c)}{d} + \frac{ad - bc}{d}\right) + \frac{d}{b} \left(-\frac{d}{2} \left(\frac{1}{d} \text{Si}\left(\frac{(b-d)(dx + c)}{d} + \frac{ad - bc}{d} + \frac{-ad + bc}{d}\right) \cos\left(\frac{-ad + bc}{d}\right) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(d*x+c)*sin(b*x+a),x)

[Out] (-Si(d*x+c)/b*d*cos(b/d*(d*x+c)+(a*d-b*c)/d)+1/b*d*(-1/2*d*(Si((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*cos((-a*d+b*c)/d)/d-Ci((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*sin((-a*d+b*c)/d)/d+1/2*d*(Si((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*cos((-a*d+b*c)/d)/d-Ci((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*sin((-a*d+b*c)/d)/d))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \operatorname{Si}(dx + c) \sin(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*x+c)*sin(b*x+a),x, algorithm="maxima")

[Out] integrate(Si(d*x + c)*sin(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}(\sin(bx + a) \operatorname{Si}(dx + c), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*x+c)*sin(b*x+a),x, algorithm="fricas")

[Out] integral(sin(b*x + a)*sin_integral(d*x + c), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \sin(a + bx) \operatorname{Si}(c + dx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*x+c)*sin(b*x+a),x)

[Out] Integral(sin(a + b*x)*Si(c + d*x), x)

Giac [C] time = 2.03416, size = 12880, normalized size = 83.64

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*x+c)*sin(b*x+a),x, algorithm="giac")

[Out] $\frac{1}{4} * (\operatorname{imag_part}(\cos_integral(b*x + d*x + c + b*c/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d)^2 - \operatorname{imag_part}(\cos_integral(b*x - d*x - c + b*c/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d)^2 + \operatorname{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d)^2 - \operatorname{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d)^2 + 2 * \sin_integral((b*d*x + d^2*x + b*c + c*d)/d) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d)^2 - 2 * \sin_integral((b*d*x - d^2*x + b*c - c*d)/d) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d)^2 - 2 * \operatorname{real_part}(\cos_integral(b*x - d*x - c + b*c/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d)^2$

$$\begin{aligned}
& d)^2 + 2*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*a + 1/2*c)^2* \\
& \tan(1/2*(b*c + c*d)/d)^2 - 2*\sin_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan \\
& (1/2*a + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 - \text{imag_part}(\cos_integral(b*x + d \\
& *x + c + b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 + \text{imag_part}(\\
& \cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c* \\
& d)/d)^2 - \text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a - 1/2*c \\
&)^2*\tan(1/2*(b*c + c*d)/d)^2 + \text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/ \\
& d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 - 2*\sin_integral((b*d*x + \\
& d^2*x + b*c + c*d)/d)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 + 2*si \\
& n_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c \\
& + c*d)/d)^2 - 4*\text{imag_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*a + \\
& 1/2*c)^2*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c - c*d)/d) + 4*\text{imag_part}(\cos_integ \\
& ral(-b*x + d*x + c - b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)*\tan(1/ \\
& 2*(b*c - c*d)/d) - 8*\sin_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a \\
& + 1/2*c)^2*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c - c*d)/d) - 4*\text{imag_part}(\cos_inte \\
& gral(b*x - d*x - c + b*c/d))*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2*ta \\
& n(1/2*(b*c - c*d)/d) + 4*\text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d))*ta \\
& n(1/2*a - 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) - 8*\sin_in \\
& tegral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c + c*d \\
&)/d)^2*\tan(1/2*(b*c - c*d)/d) - \text{imag_part}(\cos_integral(b*x + d*x + c + b*c/ \\
& d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 + \text{imag_part}(\cos_integral(\\
& b*x - d*x - c + b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 - ima \\
& g_part(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(\\
& b*c - c*d)/d)^2 + \text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a \\
& + 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 - 2*\sin_integral((b*d*x + d^2*x + b*c \\
& + c*d)/d)*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 + 2*\sin_integral((b \\
& *d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 \\
& + \text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1 \\
& /2*(b*c - c*d)/d)^2 - \text{imag_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/ \\
& 2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 + \text{imag_part}(\cos_integral(-b*x + d*x \\
& + c - b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 - \text{imag_part}(co \\
& s_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d \\
&)/d)^2 + 2*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*a - 1/2*c)^2 \\
& *\tan(1/2*(b*c - c*d)/d)^2 - 2*\sin_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan \\
& (1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 + 4*\text{imag_part}(\cos_integral(b*x \\
& + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*(b*c + c*d)/d)*\tan(1/2*(b*c \\
& - c*d)/d)^2 - 4*\text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a \\
& + 1/2*c)*\tan(1/2*(b*c + c*d)/d)*\tan(1/2*(b*c - c*d)/d)^2 + 8*\sin_integral((\\
& b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*a + 1/2*c)*\tan(1/2*(b*c + c*d)/d)*\tan \\
& (1/2*(b*c - c*d)/d)^2 - \text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(\\
& 1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 + \text{imag_part}(\cos_integral(b*x \\
& - d*x - c + b*c/d))*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 - ima \\
& g_part(\cos_integral(-b*x +d*x + c - b*c/d))*\tan(1/2*(b*c + c*d)/d)^2*\tan(1 \\
& /2*(b*c - c*d)/d)^2 + \text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1 \\
& /2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 - 2*\sin_integral((b*d*x + d^2* \\
& x + b*c + c*d)/d)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 + 2*\sin \\
& _integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(\\
& b*c - c*d)/d)^2 - 2*\text{real_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2* \\
& a + 1/2*c)^2*\tan(1/2*a - 1/2*c) - 2*\text{real_part}(\cos_integral(-b*x + d*x + c - \\
& b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c) + 2*\text{real_part}(\cos_integral \\
& (b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*a - 1/2*c)^2 + 2*\text{real_p} \\
& art(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*a - 1/ \\
& 2*c)^2 + 2*\text{real_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c \\
&)^2*\tan(1/2*(b*c + c*d)/d) + 2*\text{real_part}(\cos_integral(-b*x - d*x - c - b*c/ \\
& d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d) - 2*\text{real_part}(\cos_integral(\\
& b*x + d*x + c + b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d) - 2*rea \\
& l_part(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(\\
& b*c + c*d)/d) - 2*\text{real_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a \\
& + 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2 - 2*\text{real_part}(\cos_integral(-b*x - d*x - c
\end{aligned}$$

$$\begin{aligned}
& - b*c/d)) * \tan(1/2*a + 1/2*c) * \tan(1/2*(b*c + c*d)/d)^2 - 2*\text{real_part}(\cos_in \\
& \text{tegral}(b*x - d*x - c + b*c/d)) * \tan(1/2*a - 1/2*c) * \tan(1/2*(b*c + c*d)/d)^2 \\
& - 2*\text{real_part}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2*a - 1/2*c) * \tan(\\
& 1/2*(b*c + c*d)/d)^2 + 2*\text{real_part}(\cos_integral(b*x - d*x - c + b*c/d)) * \tan \\
& (1/2*a + 1/2*c)^2 * \tan(1/2*(b*c - c*d)/d) + 2*\text{real_part}(\cos_integral(-b*x + \\
& d*x + c - b*c/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*(b*c - c*d)/d) - 2*\text{real_part} \\
& (\cos_integral(b*x - d*x - c + b*c/d)) * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(b*c - c \\
& *d)/d) - 2*\text{real_part}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2*a - 1/2* \\
& c)^2 * \tan(1/2*(b*c - c*d)/d) + 2*\text{real_part}(\cos_integral(b*x - d*x - c + b*c/ \\
& d)) * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d) + 2*\text{real_part}(\cos_integ \\
& ral(-b*x + d*x + c - b*c/d)) * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d) \\
&) + 2*\text{real_part}(\cos_integral(b*x + d*x + c + b*c/d)) * \tan(1/2*a + 1/2*c) * \tan \\
& (1/2*(b*c - c*d)/d)^2 + 2*\text{real_part}(\cos_integral(-b*x - d*x - c - b*c/d)) * \tan \\
& (1/2*a + 1/2*c) * \tan(1/2*(b*c - c*d)/d)^2 + 2*\text{real_part}(\cos_integral(b*x - \\
& d*x - c + b*c/d)) * \tan(1/2*a - 1/2*c) * \tan(1/2*(b*c - c*d)/d)^2 + 2*\text{real_par} \\
& t(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2*a - 1/2*c) * \tan(1/2*(b*c - c \\
& *d)/d)^2 - 2*\text{real_part}(\cos_integral(b*x + d*x + c + b*c/d)) * \tan(1/2*(b*c + \\
& c*d)/d) * \tan(1/2*(b*c - c*d)/d)^2 - 2*\text{real_part}(\cos_integral(-b*x - d*x - c \\
& - b*c/d)) * \tan(1/2*(b*c + c*d)/d) * \tan(1/2*(b*c - c*d)/d)^2 - \text{imag_part}(\cos_i \\
& ntegral(b*x + d*x + c + b*c/d)) * \tan(1/2*a + 1/2*c)^2 - \text{imag_part}(\cos_integr \\
& al(b*x - d*x - c + b*c/d)) * \tan(1/2*a + 1/2*c)^2 + \text{imag_part}(\cos_integral(-b \\
& *x + d*x + c - b*c/d)) * \tan(1/2*a + 1/2*c)^2 + \text{imag_part}(\cos_integral(-b*x - \\
& d*x - c - b*c/d)) * \tan(1/2*a + 1/2*c)^2 - 2*\text{sin_integral}((b*d*x + d^2*x + b \\
& *c + c*d)/d) * \tan(1/2*a + 1/2*c)^2 - 2*\text{sin_integral}((b*d*x - d^2*x + b*c - c \\
& *d)/d) * \tan(1/2*a + 1/2*c)^2 + \text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d) \\
&) * \tan(1/2*a - 1/2*c)^2 + \text{imag_part}(\cos_integral(b*x - d*x - c + b*c/d)) * \tan \\
& (1/2*a - 1/2*c)^2 - \text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2 \\
& *a - 1/2*c)^2 - \text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d)) * \tan(1/2*a - \\
& 1/2*c)^2 + 2*\text{sin_integral}((b*d*x + d^2*x + b*c + c*d)/d) * \tan(1/2*a - 1/2*c \\
&)^2 + 2*\text{sin_integral}((b*d*x - d^2*x + b*c - c*d)/d) * \tan(1/2*a - 1/2*c)^2 + \\
& 4*\text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d)) * \tan(1/2*a + 1/2*c) * \tan(1/2 \\
& *(b*c + c*d)/d) - 4*\text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d)) * \tan(1/2 \\
& *a + 1/2*c) * \tan(1/2*(b*c + c*d)/d) + 8*\text{sin_integral}((b*d*x + d^2*x + b*c + \\
& c*d)/d) * \tan(1/2*a + 1/2*c) * \tan(1/2*(b*c + c*d)/d) - \text{imag_part}(\cos_integral(\\
& b*x + d*x + c + b*c/d)) * \tan(1/2*(b*c + c*d)/d)^2 - \text{imag_part}(\cos_integral(b \\
& *x - d*x - c + b*c/d)) * \tan(1/2*(b*c + c*d)/d)^2 + \text{imag_part}(\cos_integral(-b \\
& *x + d*x + c - b*c/d)) * \tan(1/2*(b*c + c*d)/d)^2 + \text{imag_part}(\cos_integral(-b \\
& *x - d*x - c - b*c/d)) * \tan(1/2*(b*c + c*d)/d)^2 - 2*\text{sin_integral}((b*d*x + d \\
& ^2*x + b*c + c*d)/d) * \tan(1/2*(b*c + c*d)/d)^2 - 2*\text{sin_integral}((b*d*x - d^2 \\
& *x + b*c - c*d)/d) * \tan(1/2*(b*c + c*d)/d)^2 - 4*\text{imag_part}(\cos_integral(b*x \\
& - d*x - c + b*c/d)) * \tan(1/2*a - 1/2*c) * \tan(1/2*(b*c - c*d)/d) + 4*\text{imag_part} \\
& (\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2*a - 1/2*c) * \tan(1/2*(b*c - c* \\
& d)/d) - 8*\text{sin_integral}((b*d*x - d^2*x + b*c - c*d)/d) * \tan(1/2*a - 1/2*c) * \tan \\
& (1/2*(b*c - c*d)/d) + \text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d)) * \tan(1 \\
& /2*(b*c - c*d)/d)^2 + \text{imag_part}(\cos_integral(b*x - d*x - c + b*c/d)) * \tan(1/ \\
& 2*(b*c - c*d)/d)^2 - \text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/ \\
& 2*(b*c - c*d)/d)^2 - \text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d)) * \tan(1/ \\
& 2*(b*c - c*d)/d)^2 + 2*\text{sin_integral}((b*d*x + d^2*x + b*c + c*d)/d) * \tan(1/2* \\
& (b*c - c*d)/d)^2 + 2*\text{sin_integral}((b*d*x - d^2*x + b*c - c*d)/d) * \tan(1/2*(b \\
& *c - c*d)/d)^2 + 2*\text{real_part}(\cos_integral(b*x + d*x + c + b*c/d)) * \tan(1/2*a \\
& + 1/2*c) + 2*\text{real_part}(\cos_integral(-b*x - d*x - c - b*c/d)) * \tan(1/2*a + 1 \\
& /2*c) - 2*\text{real_part}(\cos_integral(b*x - d*x - c + b*c/d)) * \tan(1/2*a - 1/2*c) \\
& - 2*\text{real_part}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2*a - 1/2*c) - 2 \\
& *\text{real_part}(\cos_integral(b*x + d*x + c + b*c/d)) * \tan(1/2*(b*c + c*d)/d) - 2* \\
& \text{real_part}(\cos_integral(-b*x - d*x - c - b*c/d)) * \tan(1/2*(b*c + c*d)/d) + 2* \\
& \text{real_part}(\cos_integral(b*x - d*x - c + b*c/d)) * \tan(1/2*(b*c - c*d)/d) + 2*r \\
& eal_part(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2*(b*c - c*d)/d) + \text{ima} \\
& g_part(\cos_integral(b*x + d*x + c + b*c/d)) - \text{imag_part}(\cos_integral(b*x - \\
& d*x - c + b*c/d)) + \text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d)) - \text{imag_}
\end{aligned}$$


```

part(cos_integral(-b*x - d*x - c - b*c/d)) + 2*sin_integral((b*d*x + d^2*x
+ b*c + c*d)/d) - 2*sin_integral((b*d*x - d^2*x + b*c - c*d)/d))*d/(b*d*tan
(1/2*a + 1/2*c)^2*tan(1/2*a - 1/2*c)^2*tan(1/2*(b*c + c*d)/d)^2*tan(1/2*(b*
c - c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2*tan(1/2*a - 1/2*c)^2*tan(1/2*(b*c
+ c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2*tan(1/2*a - 1/2*c)^2*tan(1/2*(b*c -
c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2*tan(1/2*(b*c + c*d)/d)^2*tan(1/2*(b*c
- c*d)/d)^2 + b*d*tan(1/2*a - 1/2*c)^2*tan(1/2*(b*c + c*d)/d)^2*tan(1/2*(b*
c - c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2*tan(1/2*a - 1/2*c)^2 + b*d*tan(1/2
*a + 1/2*c)^2*tan(1/2*(b*c + c*d)/d)^2 + b*d*tan(1/2*a - 1/2*c)^2*tan(1/2*(
b*c + c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2*tan(1/2*(b*c - c*d)/d)^2 + b*d*t
an(1/2*a - 1/2*c)^2*tan(1/2*(b*c - c*d)/d)^2 + b*d*tan(1/2*(b*c + c*d)/d)^2
*tan(1/2*(b*c - c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2 + b*d*tan(1/2*a - 1/2*
c)^2 + b*d*tan(1/2*(b*c + c*d)/d)^2 + b*d*tan(1/2*(b*c - c*d)/d)^2 + b*d) -
cos(b*x + a)*sin_integral(d*x + c)/b

```

$$3.65 \quad \int \frac{\sin(a+bx)\text{Si}(c+dx)}{x} dx$$

Optimal. Leaf size=18

$$\text{CannotIntegrate}\left(\frac{\sin(a+bx)\text{Si}(c+dx)}{x}, x\right)$$

[Out] CannotIntegrate[(Sin[a + b*x]*SinIntegral[c + d*x])/x, x]

Rubi [A] time = 0.142027, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\sin(a+bx)\text{Si}(c+dx)}{x} dx$$

Verification is Not applicable to the result.

[In] Int[(Sin[a + b*x]*SinIntegral[c + d*x])/x,x]

[Out] Defer[Int] [(Sin[a + b*x]*SinIntegral[c + d*x])/x, x]

Rubi steps

$$\int \frac{\sin(a+bx)\text{Si}(c+dx)}{x} dx = \int \frac{\sin(a+bx)\text{Si}(c+dx)}{x} dx$$

Mathematica [A] time = 28.787, size = 0, normalized size = 0.

$$\int \frac{\sin(a+bx)\text{Si}(c+dx)}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[(Sin[a + b*x]*SinIntegral[c + d*x])/x,x]

[Out] Integrate[(Sin[a + b*x]*SinIntegral[c + d*x])/x, x]

Maple [A] time = 0.088, size = 0, normalized size = 0.

$$\int \frac{\text{Si}(dx+c)\sin(bx+a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Si(d*x+c)*sin(b*x+a)/x,x)

[Out] int(Si(d*x+c)*sin(b*x+a)/x,x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(dx + c) \sin(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*x+c)*sin(b*x+a)/x,x, algorithm="maxima")

[Out] integrate(Si(d*x + c)*sin(b*x + a)/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\sin(bx + a) \text{Si}(dx + c)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*x+c)*sin(b*x+a)/x,x, algorithm="fricas")

[Out] integral(sin(b*x + a)*sin_integral(d*x + c)/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sin(a + bx) \text{Si}(c + dx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*x+c)*sin(b*x+a)/x,x)

[Out] Integral(sin(a + b*x)*Si(c + d*x)/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(dx + c) \sin(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Si(d*x+c)*sin(b*x+a)/x,x, algorithm="giac")

[Out] integrate(Si(d*x + c)*sin(b*x + a)/x, x)

3.66 $\int x \cos(a + bx) \text{Si}(c + dx) dx$

Optimal. Leaf size=370

$$\frac{\sin\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b^2} - \frac{\sin\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b+d)}{d} + x(b+d)\right)}{2b^2} + \frac{\cos\left(a - \frac{bc}{d}\right) \text{Si}\left(x(b-d)\right)}{2b^2}$$

```
[Out] (c*cos[a - (b*c)/d]*CosIntegral[(c*(b - d))/d + (b - d)*x])/(2*b*d) - (c*cos[a - (b*c)/d]*CosIntegral[(c*(b + d))/d + (b + d)*x])/(2*b*d) + (CosIntegral[(c*(b - d))/d + (b - d)*x]*Sin[a - (b*c)/d])/(2*b^2) - (CosIntegral[(c*(b + d))/d + (b + d)*x]*Sin[a - (b*c)/d])/(2*b^2) - Sin[a - c + (b - d)*x]/(2*b*(b - d)) + Sin[a + c + (b + d)*x]/(2*b*(b + d)) + (Cos[a - (b*c)/d]*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b^2) - (c*sin[a - (b*c)/d]*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b*d) + (Cos[a + b*x]*SinIntegral[c + d*x])/b^2 + (x*sin[a + b*x]*SinIntegral[c + d*x])/b - (Cos[a - (b*c)/d]*SinIntegral[(c*(b + d))/d + (b + d)*x])/(2*b^2) + (c*sin[a - (b*c)/d]*SinIntegral[(c*(b + d))/d + (b + d)*x])/(2*b*d)
```

Rubi [A] time = 1.24023, antiderivative size = 370, normalized size of antiderivative = 1., number of steps used = 24, number of rules used = 9, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.643$, Rules used = {6519, 4608, 6742, 2637, 3303, 3299, 3302, 6511, 4430}

$$\frac{\sin\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b^2} - \frac{\sin\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b+d)}{d} + x(b+d)\right)}{2b^2} + \frac{\cos\left(a - \frac{bc}{d}\right) \text{Si}\left(x(b-d)\right)}{2b^2}$$

Antiderivative was successfully verified.

```
[In] Int[x*cos[a + b*x]*SinIntegral[c + d*x],x]
```

```
[Out] (c*cos[a - (b*c)/d]*CosIntegral[(c*(b - d))/d + (b - d)*x])/(2*b*d) - (c*cos[a - (b*c)/d]*CosIntegral[(c*(b + d))/d + (b + d)*x])/(2*b*d) + (CosIntegral[(c*(b - d))/d + (b - d)*x]*Sin[a - (b*c)/d])/(2*b^2) - (CosIntegral[(c*(b + d))/d + (b + d)*x]*Sin[a - (b*c)/d])/(2*b^2) - Sin[a - c + (b - d)*x]/(2*b*(b - d)) + Sin[a + c + (b + d)*x]/(2*b*(b + d)) + (Cos[a - (b*c)/d]*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b^2) - (c*sin[a - (b*c)/d]*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b*d) + (Cos[a + b*x]*SinIntegral[c + d*x])/b^2 + (x*sin[a + b*x]*SinIntegral[c + d*x])/b - (Cos[a - (b*c)/d]*SinIntegral[(c*(b + d))/d + (b + d)*x])/(2*b^2) + (c*sin[a - (b*c)/d]*SinIntegral[(c*(b + d))/d + (b + d)*x])/(2*b*d)
```

Rule 6519

```
Int[Cos[(a_.) + (b_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.)*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :> Simp[((e + f*x)^m*sin[a + b*x]*SinIntegral[c + d*x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*sin[a + b*x]*Sin[c + d*x])/(c + d*x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*sin[a + b*x]*SinIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 4608

```
Int[(u_.)*Sin[(a_.) + (b_.)*(x_)]^(m_.)*Sin[(c_.) + (d_.)*(x_)]^(n_.), x_Symbol] :> Int[ExpandTrigReduce[u, Sin[a + b*x]^m*sin[c + d*x]^n, x], x] /; FreeQ[{a, b, c, d}, x] && IGtQ[m, 0] && IGtQ[n, 0]
```

Rule 6742

```
Int[u_, x_Symbol] := With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]
]
```

Rule 2637

```
Int[sin[Pi/2 + (c_.) + (d_.)*(x_)], x_Symbol] := Simp[Sin[c + d*x]/d, x] /;
FreeQ[{c, d}, x]
```

Rule 3303

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Dist[Cos[(d*
e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f
)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] &&
NeQ[d*e - c*f, 0]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rule 6511

```
Int[Sin[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := -
Simp[(Cos[a + b*x]*SinIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x
]*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 4430

```
Int[Cos[(c_.) + (d_.)*(x_)]^(q_.)*((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b
_.)*(x_)]^(p_.), x_Symbol] := Int[ExpandTrigReduce[(e + f*x)^m, Sin[a + b*x
]^p*Cos[c + d*x]^q, x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[p, 0]
&& IGtQ[q, 0]
```

Rubi steps

$$\begin{aligned}
\int x \cos(a + bx) \text{Si}(c + dx) dx &= \frac{x \sin(a + bx) \text{Si}(c + dx)}{b} - \frac{\int \sin(a + bx) \text{Si}(c + dx) dx}{b} - \frac{d \int \frac{x \sin(a + bx) \sin(c + dx)}{c + dx} dx}{b} \\
&= \frac{\cos(a + bx) \text{Si}(c + dx)}{b^2} + \frac{x \sin(a + bx) \text{Si}(c + dx)}{b} - \frac{d \int \frac{\cos(a + bx) \sin(c + dx)}{c + dx} dx}{b^2} - \frac{d \int \left(\frac{x \cos(a - c + (b - d)x)}{2(c + dx)} \right) dx}{b^2} \\
&= \frac{\cos(a + bx) \text{Si}(c + dx)}{b^2} + \frac{x \sin(a + bx) \text{Si}(c + dx)}{b} - \frac{d \int \left(-\frac{\sin(a - c + (b - d)x)}{2(c + dx)} + \frac{\sin(a + c + (b + d)x)}{2(c + dx)} \right) dx}{b^2} \\
&= \frac{\cos(a + bx) \text{Si}(c + dx)}{b^2} + \frac{x \sin(a + bx) \text{Si}(c + dx)}{b} + \frac{d \int \frac{\sin(a - c + (b - d)x)}{c + dx} dx}{2b^2} - \frac{d \int \frac{\sin(a + c + (b + d)x)}{c + dx} dx}{2b^2} \\
&= \frac{\cos(a + bx) \text{Si}(c + dx)}{b^2} + \frac{x \sin(a + bx) \text{Si}(c + dx)}{b} - \frac{\int \cos(a - c + (b - d)x) dx}{2b} + \frac{\int \cos(a + c + (b + d)x) dx}{2b} \\
&= \frac{\text{Ci}\left(\frac{c(b-d)}{d} + (b-d)x\right) \sin\left(a - \frac{bc}{d}\right)}{2b^2} - \frac{\text{Ci}\left(\frac{c(b+d)}{d} + (b+d)x\right) \sin\left(a - \frac{bc}{d}\right)}{2b^2} - \frac{\sin(a - c + (b - d)x)}{2b(b - d)} + \frac{\sin(a + c + (b + d)x)}{2b(b + d)} \\
&= \frac{c \cos\left(a - \frac{bc}{d}\right) \text{Ci}\left(\frac{c(b-d)}{d} + (b-d)x\right)}{2bd} - \frac{c \cos\left(a - \frac{bc}{d}\right) \text{Ci}\left(\frac{c(b+d)}{d} + (b+d)x\right)}{2bd} + \frac{\text{Ci}\left(\frac{c(b-d)}{d} + (b-d)x\right)}{2b} - \frac{\text{Ci}\left(\frac{c(b+d)}{d} + (b+d)x\right)}{2b}
\end{aligned}$$

Mathematica [C] time = 4.21426, size = 393, normalized size = 1.06

$$e^{-\frac{i(d(a-dx)+b(c+dx))}{d}} \left(-(b^2 - d^2)(bc - id)e^{i(2a+x(b-d))} \text{ExpIntegralEi}\left(\frac{i(b+d)(c+dx)}{d}\right) - ibde^{\frac{ic(b+d)}{d}} (-de^{2i(a+bx)} + be^{2i(a+bx)} + b + d) \right)$$

$$4b^2d(b-d)(b+d)$$

Warning: Unable to verify antiderivative.

[In] Integrate[x*Cos[a + b*x]*SinIntegral[c + d*x], x]

[Out] $-\left((-I)*b*d*(1/((b + d)*E^{(I*(b + d)*x)}) + E^{(I*(2*a + (b - d)*x))}/(b - d)\right) + \left(- (b*c) + I*d\right)*E^{((I*(-(b*c) + (2*a + c)*d))/d)}*ExpIntegralEi[(I*(b - d)*(c + d*x))/d] + (b*c + I*d)*E^{((I*c*(b + d))/d)}*ExpIntegralEi[(-I)*(b + d)*(c + d*x)/d]/(4*b^2*d*E^{(I*(a + c))} + ((-I)*b*d*E^{((I*c*(b + d))/d)}*(b + d + b*E^{((2*I)*(a + b*x))} - d*E^{((2*I)*(a + b*x))}) + (b*c + I*d)*(b^2 - d^2)*E^{((-I)*d*x + I*b*((2*c)/d + x)}*ExpIntegralEi[(((-I)*(b - d)*(c + d*x))/d) - (b*c - I*d)*(b^2 - d^2)*E^{(I*(2*a + (b - d)*x))}*ExpIntegralEi[(I*(b + d)*(c + d*x))/d]/(4*b^2*(b - d)*d*(b + d)*E^{((I*(d*(a - d*x) + b*(c + d*x)))/d)} + ((Cos[a + b*x] + b*x*Sin[a + b*x])*SinIntegral[c + d*x])/b^2$

Maple [B] time = 0.107, size = 1208, normalized size = 3.3

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*cos(b*x+a)*Si(d*x+c), x)

[Out] $(\text{Si}(d*x+c)/b*(1/b*d*(\sin(b/d*(d*x+c)+(a*d-b*c)/d)*(b/d*(d*x+c)+(a*d-b*c)/d) + \cos(b/d*(d*x+c)+(a*d-b*c)/d)) - a*d/b*\sin(b/d*(d*x+c)+(a*d-b*c)/d) - 1/b*(1/2/(b-d)*d*\sin((b-d)/d*(d*x+c)+(a*d-b*c)/d) + 1/2*(a*d-b*c)*d/(b-d)*(\text{Si}((b-d)/d*(d*x+c)+(a*d-b*c)/d + (-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d + \text{Ci}((b-d)/d*(d*x+c) +$

$$\begin{aligned} & a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d)-1/2/(b-d)*d^2*a*(\text{Si}((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d+\text{Ci}((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d)+1/2/(b-d)*c*d^2*(\text{Si}((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d+\text{Ci}((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d)-1/2/(b+d)*d*\sin((b+d)/d*(d*x+c)+(a*d-b*c)/d)-1/2*(a*d-b*c)*d/(b+d)*(\text{Si}((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d+\text{Ci}((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d)+1/2/(b+d)*d^2*a*(\text{Si}((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d+\text{Ci}((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d)+1/2/(b+d)*c*d^2*(\text{Si}((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d+\text{Ci}((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d)-1/2/b*d^2*(\text{Si}((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d-\text{Ci}((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d)+1/2/b*d^2*(\text{Si}((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d-\text{Ci}((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d))/d \end{aligned}$$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \text{Si}(dx + c) \cos(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*cos(b*x+a)*Si(d*x+c),x, algorithm="maxima")

[Out] integrate(x*Si(d*x + c)*cos(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x \cos(bx + a) \text{Si}(dx + c), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*cos(b*x+a)*Si(d*x+c),x, algorithm="fricas")

[Out] integral(x*cos(b*x + a)*sin_integral(d*x + c), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \cos(a + bx) \text{Si}(c + dx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*cos(b*x+a)*Si(d*x+c),x)

[Out] Integral(x*cos(a + b*x)*Si(c + d*x), x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*cos(b*x+a)*Si(d*x+c),x, algorithm="giac")
```

```
[Out] Timed out
```


3.67 $\int \cos(a + bx) \text{Si}(c + dx) dx$

Optimal. Leaf size=153

$$\frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b} + \frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b+d)}{d} + x(b+d)\right)}{2b} + \frac{\sin\left(a - \frac{bc}{d}\right) \text{Si}\left(x(b-d)\right)}{2b}$$

```
[Out] -(Cos[a - (b*c)/d]*CosIntegral[(c*(b - d))/d + (b - d)*x])/(2*b) + (Cos[a -
(b*c)/d]*CosIntegral[(c*(b + d))/d + (b + d)*x])/(2*b) + (Sin[a - (b*c)/d]
*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b) + (Sin[a + b*x]*SinIntegral[
c + d*x])/b - (Sin[a - (b*c)/d]*SinIntegral[(c*(b + d))/d + (b + d)*x])/(2*
b)
```

Rubi [A] time = 0.222689, antiderivative size = 153, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {6517, 4428, 3303, 3299, 3302}

$$\frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b} + \frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b+d)}{d} + x(b+d)\right)}{2b} + \frac{\sin\left(a - \frac{bc}{d}\right) \text{Si}\left(x(b-d)\right)}{2b}$$

Antiderivative was successfully verified.

```
[In] Int[Cos[a + b*x]*SinIntegral[c + d*x], x]
```

```
[Out] -(Cos[a - (b*c)/d]*CosIntegral[(c*(b - d))/d + (b - d)*x])/(2*b) + (Cos[a -
(b*c)/d]*CosIntegral[(c*(b + d))/d + (b + d)*x])/(2*b) + (Sin[a - (b*c)/d]
*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b) + (Sin[a + b*x]*SinIntegral[
c + d*x])/b - (Sin[a - (b*c)/d]*SinIntegral[(c*(b + d))/d + (b + d)*x])/(2*
b)
```

Rule 6517

```
Int[Cos[(a_.) + (b_.)*(x_)]*SinIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := S
imp[(Sin[a + b*x]*SinIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]
*Sin[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 4428

```
Int[((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(p_.)*Sin[(c_.) + (
d_.)*(x_)]^(q_.), x_Symbol] := Int[ExpandTrigReduce[(e + f*x)^m, Sin[a + b*x]
]^p*SIN[c + d*x]^q, x] /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[p, 0] &&
IGtQ[q, 0] && IntegerQ[m]
```

Rule 3303

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Dist[Cos[(d*
e - c*f)/d], Int[SIN[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[SIN[(d*e - c*f
)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] &&
NeQ[d*e - c*f, 0]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SINte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned}
 \int \cos(a + bx)\text{Si}(c + dx) dx &= \frac{\sin(a + bx)\text{Si}(c + dx)}{b} - \frac{d \int \frac{\sin(a+bx)\sin(c+dx)}{c+dx} dx}{b} \\
 &= \frac{\sin(a + bx)\text{Si}(c + dx)}{b} - \frac{d \int \left(\frac{\cos(a-c+(b-d)x)}{2(c+dx)} - \frac{\cos(a+c+(b+d)x)}{2(c+dx)} \right) dx}{b} \\
 &= \frac{\sin(a + bx)\text{Si}(c + dx)}{b} - \frac{d \int \frac{\cos(a-c+(b-d)x)}{c+dx} dx}{2b} + \frac{d \int \frac{\cos(a+c+(b+d)x)}{c+dx} dx}{2b} \\
 &= \frac{\sin(a + bx)\text{Si}(c + dx)}{b} - \frac{\left(d \cos\left(a - \frac{bc}{d}\right) \right) \int \frac{\cos\left(\frac{c(b-d)}{d} + (b-d)x\right)}{c+dx} dx}{2b} + \frac{\left(d \cos\left(a - \frac{bc}{d}\right) \right) \int \frac{\cos\left(\frac{c(b+d)}{d} + (b+d)x\right)}{c+dx} dx}{2b} \\
 &= -\frac{\cos\left(a - \frac{bc}{d}\right) \text{Ci}\left(\frac{c(b-d)}{d} + (b-d)x\right)}{2b} + \frac{\cos\left(a - \frac{bc}{d}\right) \text{Ci}\left(\frac{c(b+d)}{d} + (b+d)x\right)}{2b} + \frac{\sin\left(a - \frac{bc}{d}\right) \text{Si}\left(\frac{c(b+d)}{d} + (b+d)x\right)}{2b}
 \end{aligned}$$

Mathematica [C] time = 1.74471, size = 164, normalized size = 1.07

$$\frac{e^{-\frac{i(ad+bc)}{d}} \left(-e^{2ia} \text{ExpIntegralEi}\left(\frac{i(b-d)(c+dx)}{d}\right) + e^{2ia} \text{ExpIntegralEi}\left(\frac{i(b+d)(c+dx)}{d}\right) + 4e^{\frac{i(ad+bc)}{d}} \sin(a + bx)\text{Si}(c + dx) - e^{\frac{2ibc}{d}} \text{ExpIntegralEi}\left(\frac{c(b+d)}{d} + (b+d)x\right) \right)}{4b}$$

Warning: Unable to verify antiderivative.

[In] Integrate[Cos[a + b*x]*SinIntegral[c + d*x], x]

[Out] $(-E^{((2*I)*b*c)/d} \text{ExpIntegralEi}[((-I)*(b-d)*(c+d*x))/d]) - E^{((2*I)*a) \text{ExpIntegralEi}[(I*(b-d)*(c+d*x))/d] + E^{((2*I)*b*c)/d} \text{ExpIntegralEi}[((-I)*(b+d)*(c+d*x))/d] + E^{((2*I)*a) \text{ExpIntegralEi}[(I*(b+d)*(c+d*x))/d] + 4*E^{((I*(b*c+a*d))/d)} \text{Sin}[a + b*x] \text{SinIntegral}[c + d*x] / (4*b*E^{((I*(b*c+a*d))/d)})$

Maple [A] time = 0.079, size = 280, normalized size = 1.8

$$\frac{1}{d} \left(\frac{\text{Si}(dx+c)d}{b} \sin\left(\frac{b(dx+c)}{d} + \frac{ad-bc}{d}\right) - \frac{d}{b} \left(\frac{1}{2} \frac{1}{d} \text{Si}\left(\frac{(b-d)(dx+c)}{d} + \frac{ad-bc}{d} + \frac{-ad+bc}{d}\right) \sin\left(\frac{-ad+bc}{d}\right) + \frac{1}{d} \text{Ci}\left(\frac{(b+d)(dx+c)}{d} + \frac{ad-bc}{d} + \frac{-ad+bc}{d}\right) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(b*x+a)*Si(d*x+c), x)

[Out] $(\text{Si}(d*x+c)/b*d*\sin(b/d*(d*x+c)+(a*d-b*c)/d)-1/b*d*(1/2*d*(\text{Si}((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d+\text{Ci}((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d-1/2*d*(\text{Si}((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d+\text{Ci}((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d)/d$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \operatorname{Si}(dx + c) \cos(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(d*x+c),x, algorithm="maxima")

[Out] integrate(Si(d*x + c)*cos(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}(\cos(bx + a) \operatorname{Si}(dx + c), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(d*x+c),x, algorithm="fricas")

[Out] integral(cos(b*x + a)*sin_integral(d*x + c), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \cos(a + bx) \operatorname{Si}(c + dx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(d*x+c),x)

[Out] Integral(cos(a + b*x)*Si(c + d*x), x)

Giac [C] time = 1.97024, size = 12439, normalized size = 81.3

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(d*x+c),x, algorithm="giac")

[Out] $\frac{1}{4} * (\operatorname{real_part}(\cos_integral(b*x + d*x + c + b*c/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d)^2 - \operatorname{real_part}(\cos_integral(b*x - d*x - c + b*c/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d)^2 - \operatorname{real_part}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d)^2 + \operatorname{real_part}(\cos_integral(-b*x - d*x - c - b*c/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d)^2 + 2 * \operatorname{imag_part}(\cos_integral(b*x - d*x - c + b*c/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d) - 2 * \operatorname{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d) + 4 * \sin_integral((b*d*x - d^2*x + b*c - c*d)/d) *$

$$\begin{aligned}
& c*d/d)*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2 + \\
& 2*\text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/ \\
& 2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 - 2*\text{imag_part}(\cos_integral(-b*x - d \\
& *x - c - b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d \\
&)/d)^2 + 4*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*a + 1/2*c)*\t \\
& an(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 + 2*\text{imag_part}(\cos_integral(b*x \\
& - d*x - c + b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c \\
& - c*d)/d) - 2*\text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a + \\
& 1/2*c)^2*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d) + 4*\sin_integral((b*d*x \\
& x - d^2*x + b*c - c*d)/d)*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2*\tan(1/2 \\
& *(b*c - c*d)/d) - 2*\text{imag_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*a \\
& + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) + 2*\text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) - 4*\sin_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) + 2*\text{imag_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) - 2*\text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) + 4*\sin_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) - 2*\text{imag_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c - c*d)/d)^2 + 2*\text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c - c*d)/d)^2 - 4*\sin_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c - c*d)/d)^2 - 2*\text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 - 4*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*a + 1/2*c)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 - 2*\text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)*\tan(1/2*(b*c - c*d)/d)^2 - 2*\text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)*\tan(1/2*(b*c - c*d)/d)^2 + 4*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)*\tan(1/2*(b*c - c*d)/d)^2 + 2*\text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)*\tan(1/2*(b*c - c*d)/d)^2 - 2*\text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 + 4*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*a + 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 - 2*\text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 + 4*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*a + 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 - 2*\text{imag_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 + 2*\text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 - 4*\sin_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 - \text{real_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2 + \text{real_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2 + \text{real_part}(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2 - \text{real_part}(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2 + 4*\text{real_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d) + 4*\text{real_part}(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d) + \text{real_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 - \text{real_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 - \text{real_part}(\cos_integral(-b*x + d
\end{aligned}$$

$$\begin{aligned}
& 1/2*c)^2*\tan(1/2*(b*c - c*d)/d) - 2*imag_part(\cos_integral(-b*x + d*x + c - \\
& b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d) + 4*\sin_integral((b*d*x \\
& x - d^2*x + b*c - c*d)/d)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d) - 2*i \\
& mag_part(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*(b*c + c*d)/d)^2*\tan(\\
& 1/2*(b*c - c*d)/d) + 2*imag_part(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(\\
& 1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) - 4*\sin_integral((b*d*x - d^2*x \\
& + b*c - c*d)/d)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) - 2*imag_p \\
& art(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*(b*c - \\
& c*d)/d)^2 + 2*imag_part(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1 \\
& /2*c)*\tan(1/2*(b*c - c*d)/d)^2 - 4*\sin_integral((b*d*x + d^2*x + b*c + c*d) \\
& /d)*\tan(1/2*a + 1/2*c)*\tan(1/2*(b*c - c*d)/d)^2 - 2*imag_part(\cos_integral(\\
& b*x - d*x - c + b*c/d))*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c - c*d)/d)^2 + 2*ima \\
& g_part(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a - 1/2*c)*\tan(1/2*(b* \\
& c - c*d)/d)^2 - 4*\sin_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a - 1 \\
& /2*c)*\tan(1/2*(b*c - c*d)/d)^2 + 2*imag_part(\cos_integral(b*x + d*x + c + b \\
& *c/d))*\tan(1/2*(b*c + c*d)/d)*\tan(1/2*(b*c - c*d)/d)^2 - 2*imag_part(\cos_in \\
& tegral(-b*x - d*x - c - b*c/d))*\tan(1/2*(b*c + c*d)/d)*\tan(1/2*(b*c - c*d)/ \\
& d)^2 + 4*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*(b*c + c*d)/d) \\
& *\tan(1/2*(b*c - c*d)/d)^2 - real_part(\cos_integral(b*x + d*x + c + b*c/d))* \\
& \tan(1/2*a + 1/2*c)^2 - real_part(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1 \\
& /2*a + 1/2*c)^2 - real_part(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a \\
& + 1/2*c)^2 - real_part(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1 \\
& /2*c)^2 + real_part(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a - 1/2*c) \\
& ^2 + real_part(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*a - 1/2*c)^2 + \\
& real_part(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a - 1/2*c)^2 + real \\
& _part(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a - 1/2*c)^2 + 4*real_p \\
& art(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*(b*c + \\
& c*d)/d) + 4*real_part(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1/2 \\
& *c)*\tan(1/2*(b*c + c*d)/d) - real_part(\cos_integral(b*x + d*x + c + b*c/d)) \\
& *\tan(1/2*(b*c + c*d)/d)^2 - real_part(\cos_integral(b*x - d*x - c + b*c/d))* \\
& \tan(1/2*(b*c + c*d)/d)^2 - real_part(\cos_integral(-b*x + d*x + c - b*c/d))* \\
& \tan(1/2*(b*c + c*d)/d)^2 - real_part(\cos_integral(-b*x - d*x - c - b*c/d))* \\
& \tan(1/2*(b*c + c*d)/d)^2 - 4*real_part(\cos_integral(b*x - d*x - c + b*c/d)) \\
& *\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c - c*d)/d) - 4*real_part(\cos_integral(-b*x \\
& + d*x + c - b*c/d))*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c - c*d)/d) + real_part(c \\
& os_integral(b*x + d*x + c + b*c/d))*\tan(1/2*(b*c - c*d)/d)^2 + real_part(co \\
& s_integral(b*x - d*x - c + b*c/d))*\tan(1/2*(b*c - c*d)/d)^2 + real_part(cos \\
& _integral(-b*x + d*x + c - b*c/d))*\tan(1/2*(b*c - c*d)/d)^2 + real_part(cos \\
& _integral(-b*x - d*x - c - b*c/d))*\tan(1/2*(b*c - c*d)/d)^2 - 2*imag_part(c \\
& os_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c) + 2*imag_part(cos_in \\
& tegral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1/2*c) - 4*\sin_integral((b*d*x \\
& + d^2*x + b*c + c*d)/d)*\tan(1/2*a + 1/2*c) + 2*imag_part(\cos_integral(b*x - \\
& d*x - c + b*c/d))*\tan(1/2*a - 1/2*c) - 2*imag_part(\cos_integral(-b*x + d*x \\
& + c - b*c/d))*\tan(1/2*a - 1/2*c) + 4*\sin_integral((b*d*x - d^2*x + b*c - c \\
& *d)/d)*\tan(1/2*a - 1/2*c) + 2*imag_part(\cos_integral(b*x + d*x + c + b*c/d) \\
&)*\tan(1/2*(b*c + c*d)/d) - 2*imag_part(\cos_integral(-b*x - d*x - c - b*c/d) \\
&)*\tan(1/2*(b*c + c*d)/d) + 4*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)* \\
& \tan(1/2*(b*c + c*d)/d) - 2*imag_part(\cos_integral(b*x - d*x - c + b*c/d))*\tan \\
& (1/2*(b*c - c*d)/d) + 2*imag_part(\cos_integral(-b*x + d*x + c - b*c/d))*\tan \\
& (1/2*(b*c - c*d)/d) - 4*\sin_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2 \\
& *(b*c - c*d)/d) + real_part(\cos_integral(b*x + d*x + c + b*c/d)) - real_par \\
& t(\cos_integral(b*x - d*x - c + b*c/d)) - real_part(\cos_integral(-b*x + d*x \\
& + c - b*c/d)) + real_part(\cos_integral(-b*x - d*x - c - b*c/d))*d/(b*d*\tan \\
& (1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b* \\
& c - c*d)/d)^2 + b*d*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c \\
& + c*d)/d)^2 + b*d*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - \\
& c*d)/d)^2 + b*d*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c \\
& - c*d)/d)^2 + b*d*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b* \\
& c - c*d)/d)^2 + b*d*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2 + b*d*\tan(1/2
\end{aligned}$$

```

*a + 1/2*c)^2*tan(1/2*(b*c + c*d)/d)^2 + b*d*tan(1/2*a - 1/2*c)^2*tan(1/2*(
b*c + c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2*tan(1/2*(b*c - c*d)/d)^2 + b*d*t
an(1/2*a - 1/2*c)^2*tan(1/2*(b*c - c*d)/d)^2 + b*d*tan(1/2*(b*c + c*d)/d)^2
*tan(1/2*(b*c - c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2 + b*d*tan(1/2*a - 1/2*
c)^2 + b*d*tan(1/2*(b*c + c*d)/d)^2 + b*d*tan(1/2*(b*c - c*d)/d)^2 + b*d) +
sin(b*x + a)*sin_integral(d*x + c)/b

```


$$3.68 \quad \int \frac{\cos(a+bx)\text{Si}(c+dx)}{x} dx$$

Optimal. Leaf size=18

$$\text{CannotIntegrate}\left(\frac{\cos(a+bx)\text{Si}(c+dx)}{x}, x\right)$$

[Out] CannotIntegrate[(Cos[a + b*x]*SinIntegral[c + d*x])/x, x]

Rubi [A] time = 0.106662, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\cos(a+bx)\text{Si}(c+dx)}{x} dx$$

Verification is Not applicable to the result.

[In] Int[(Cos[a + b*x]*SinIntegral[c + d*x])/x,x]

[Out] Defer[Int] [(Cos[a + b*x]*SinIntegral[c + d*x])/x, x]

Rubi steps

$$\int \frac{\cos(a+bx)\text{Si}(c+dx)}{x} dx = \int \frac{\cos(a+bx)\text{Si}(c+dx)}{x} dx$$

Mathematica [A] time = 13.115, size = 0, normalized size = 0.

$$\int \frac{\cos(a+bx)\text{Si}(c+dx)}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[(Cos[a + b*x]*SinIntegral[c + d*x])/x,x]

[Out] Integrate[(Cos[a + b*x]*SinIntegral[c + d*x])/x, x]

Maple [A] time = 0.093, size = 0, normalized size = 0.

$$\int \frac{\cos(bx+a)\text{Si}(dx+c)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(cos(b*x+a)*Si(d*x+c)/x,x)

[Out] int(cos(b*x+a)*Si(d*x+c)/x,x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(dx + c) \cos(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(d*x+c)/x,x, algorithm="maxima")

[Out] integrate(Si(d*x + c)*cos(b*x + a)/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\cos(bx + a) \text{Si}(dx + c)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(d*x+c)/x,x, algorithm="fricas")

[Out] integral(cos(b*x + a)*sin_integral(d*x + c)/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\cos(a + bx) \text{Si}(c + dx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(d*x+c)/x,x)

[Out] Integral(cos(a + b*x)*Si(c + d*x)/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Si}(dx + c) \cos(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(cos(b*x+a)*Si(d*x+c)/x,x, algorithm="giac")

[Out] integrate(Si(d*x + c)*cos(b*x + a)/x, x)

3.69 $\int x^m \text{CosIntegral}(bx) dx$

Optimal. Leaf size=90

$$\frac{ix^m(-ibx)^{-m}\Gamma(m+1,-ibx)}{2b(m+1)} - \frac{ix^m(ibx)^{-m}\Gamma(m+1,ibx)}{2b(m+1)} + \frac{x^{m+1}\text{CosIntegral}(bx)}{m+1}$$

[Out] $(x^{(1+m)}\text{CosIntegral}[b*x])/(1+m) + ((I/2)*x^m*\Gamma[1+m, (-I)*b*x])/(b*(1+m)*((-I)*b*x)^m) - ((I/2)*x^m*\Gamma[1+m, I*b*x])/(b*(1+m)*(I*b*x)^m)$

Rubi [A] time = 0.0823221, antiderivative size = 90, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {6504, 12, 3307, 2181}

$$\frac{ix^m(-ibx)^{-m}\Gamma(m+1,-ibx)}{2b(m+1)} - \frac{ix^m(ibx)^{-m}\Gamma(m+1,ibx)}{2b(m+1)} + \frac{x^{m+1}\text{CosIntegral}(bx)}{m+1}$$

Antiderivative was successfully verified.

[In] Int[x^m*CosIntegral[b*x],x]

[Out] $(x^{(1+m)}\text{CosIntegral}[b*x])/(1+m) + ((I/2)*x^m*\Gamma[1+m, (-I)*b*x])/(b*(1+m)*((-I)*b*x)^m) - ((I/2)*x^m*\Gamma[1+m, I*b*x])/(b*(1+m)*(I*b*x)^m)$

Rule 6504

Int[CosIntegral[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[((c + d*x)^(m + 1)*CosIntegral[a + b*x])/(d*(m + 1)), x] - Dist[b/(d*(m + 1)), Int[((c + d*x)^(m + 1)*Cos[a + b*x])/(a + b*x), x], x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]

Rule 12

Int[(a_)*(u_), x_Symbol] :=> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 3307

Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + Pi*(k_.) + (f_.)*(x_)], x_Symbol] :=> Dist[I/2, Int[(c + d*x)^m/(E^(I*k*Pi)*E^(I*(e + f*x))), x], x] - Dist[I/2, Int[(c + d*x)^m*E^(I*k*Pi)*E^(I*(e + f*x)), x], x] /; FreeQ[{c, d, e, f, m}, x] && IntegerQ[2*k]

Rule 2181

Int[(F_)^((g_.)*((e_.) + (f_.)*(x_)))*((c_.) + (d_.)*(x_))^(m_), x_Symbol] :=> -Simp[(F^(g*(e - (c*f)/d))*(c + d*x)^FracPart[m]*Gamma[m + 1, -(f*g*Log[F])/d])*(c + d*x)]/(d*(-(f*g*Log[F])/d)^(IntPart[m] + 1)*(-(f*g*Log[F])*(c + d*x)/d)^FracPart[m]), x] /; FreeQ[{F, c, d, e, f, g, m}, x] && !IntegerQ[m]

Rubi steps

$$\begin{aligned}
\int x^m \text{Ci}(bx) dx &= \frac{x^{1+m} \text{Ci}(bx)}{1+m} - \frac{b \int \frac{x^m \cos(bx)}{b} dx}{1+m} \\
&= \frac{x^{1+m} \text{Ci}(bx)}{1+m} - \frac{\int x^m \cos(bx) dx}{1+m} \\
&= \frac{x^{1+m} \text{Ci}(bx)}{1+m} - \frac{\int e^{-ibx} x^m dx}{2(1+m)} - \frac{\int e^{ibx} x^m dx}{2(1+m)} \\
&= \frac{x^{1+m} \text{Ci}(bx)}{1+m} + \frac{ix^m (-ibx)^{-m} \Gamma(1+m, -ibx)}{2b(1+m)} - \frac{ix^m (ibx)^{-m} \Gamma(1+m, ibx)}{2b(1+m)}
\end{aligned}$$

Mathematica [A] time = 0.0762758, size = 78, normalized size = 0.87

$$\frac{x^m \left(2x \text{CosIntegral}(bx) + \frac{i(b^2 x^2)^{-m} ((ibx)^m \Gamma(m+1, -ibx) - (-ibx)^m \Gamma(m+1, ibx))}{b} \right)}{2(m+1)}$$

Antiderivative was successfully verified.

[In] Integrate[x^m * CosIntegral[b*x], x]

[Out] (x^m * (2*x * CosIntegral[b*x] + (I * ((I*b*x)^m * Gamma[1 + m, (-I)*b*x] - ((-I)*b*x)^m * Gamma[1 + m, I*b*x]))) / (b * (b^2 * x^2)^m) / (2 * (1 + m))

Maple [C] time = 0.099, size = 124, normalized size = 1.4

$$2^{-1+m} b^{-1-m} \sqrt{\pi} \left(2 \frac{(\Psi(1/2 + m/2) + 2\gamma - \Psi(3/2 + m/2) + 2 \ln(x) + 2 \ln(b)) x^{1+m} 2^{-1-m} b^{1+m}}{\sqrt{\pi} (1+m)} - \frac{2^{-1-m} x^{3+m} b^{3+m}}{\sqrt{\pi} (3+m)} {}_3F_4(1, 1, 1; 3/2, 2, 2, 5/2 + 1/2 * m) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m * Ci(b*x), x)

[Out] 2^(-1+m) * b^(-1-m) * Pi^(1/2) * (2 * (Psi(1/2 + 1/2 * m) + 2 * gamma - Psi(3/2 + 1/2 * m) + 2 * ln(x) + 2 * ln(b)) / Pi^(1/2) * x^(1+m) * 2^(-1-m) * b^(1+m) / (1+m) - 2^(-1-m) / Pi^(1/2) / (3+m) * x^(3+m) * b^(3+m) * hypergeom([1, 1, 3/2 + 1/2 * m], [3/2, 2, 2, 5/2 + 1/2 * m], -1/4 * b^2 * x^2))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^m \text{Ci}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m * Ci(b*x), x, algorithm="maxima")

[Out] integrate(x^m * Ci(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^m \text{Ci}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Ci(b*x),x, algorithm="fricas")

[Out] integral(x^m*cos_integral(b*x), x)

Sympy [B] time = 2.17449, size = 654, normalized size = 7.27

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m*Ci(b*x),x)

[Out]
$$4*2**m*b**(-m)*m*x*\text{sqrt}(\text{exp}(-2*m*\log(2))*\text{exp}(m*\log(b**2*x**2)))*\log(b**2*x**2)*\text{gamma}(m/2 + 5/2)/(8*m**2*\text{gamma}(m/2 + 5/2) + 16*m*\text{gamma}(m/2 + 5/2) + 8*\text{gamma}(m/2 + 5/2)) + 8*2**m*\text{EulerGamma}*b**(-m)*m*x*\text{sqrt}(\text{exp}(-2*m*\log(2))*\text{exp}(m*\log(b**2*x**2)))*\text{gamma}(m/2 + 5/2)/(8*m**2*\text{gamma}(m/2 + 5/2) + 16*m*\text{gamma}(m/2 + 5/2) + 8*\text{gamma}(m/2 + 5/2)) + 4*2**m*b**(-m)*x*\text{sqrt}(\text{exp}(-2*m*\log(2))*\text{exp}(m*\log(b**2*x**2)))*\log(b**2*x**2)*\text{gamma}(m/2 + 5/2)/(8*m**2*\text{gamma}(m/2 + 5/2) + 16*m*\text{gamma}(m/2 + 5/2) + 8*\text{gamma}(m/2 + 5/2)) - 8*2**m*b**(-m)*x*\text{sqrt}(\text{exp}(-2*m*\log(2))*\text{exp}(m*\log(b**2*x**2)))*\text{gamma}(m/2 + 5/2)/(8*m**2*\text{gamma}(m/2 + 5/2) + 16*m*\text{gamma}(m/2 + 5/2) + 8*\text{gamma}(m/2 + 5/2)) + 8*2**m*\text{EulerGamma}*b**(-m)*x*\text{sqrt}(\text{exp}(-2*m*\log(2))*\text{exp}(m*\log(b**2*x**2)))*\text{gamma}(m/2 + 5/2)/(8*m**2*\text{gamma}(m/2 + 5/2) + 16*m*\text{gamma}(m/2 + 5/2) + 8*\text{gamma}(m/2 + 5/2)) - b**2*m**2*x**3*x**m*\text{gamma}(m/2 + 3/2)*\text{hyper}((1, 1, m/2 + 3/2), (3/2, 2, 2, m/2 + 5/2), -b**2*x**2/4)/(8*m**2*\text{gamma}(m/2 + 5/2) + 16*m*\text{gamma}(m/2 + 5/2) + 8*\text{gamma}(m/2 + 5/2)) - 2*b**2*m*x**3*x**m*\text{gamma}(m/2 + 3/2)*\text{hyper}((1, 1, m/2 + 3/2), (3/2, 2, 2, m/2 + 5/2), -b**2*x**2/4)/(8*m**2*\text{gamma}(m/2 + 5/2) + 16*m*\text{gamma}(m/2 + 5/2) + 8*\text{gamma}(m/2 + 5/2)) - b**2*x**3*x**m*\text{gamma}(m/2 + 3/2)*\text{hyper}((1, 1, m/2 + 3/2), (3/2, 2, 2, m/2 + 5/2), -b**2*x**2/4)/(8*m**2*\text{gamma}(m/2 + 5/2) + 16*m*\text{gamma}(m/2 + 5/2) + 8*\text{gamma}(m/2 + 5/2))$$

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int x^m \text{Ci}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Ci(b*x),x, algorithm="giac")

[Out] integrate(x^m*Ci(b*x), x)

3.70 $\int x^3 \text{CosIntegral}(bx) dx$

Optimal. Leaf size=63

$$-\frac{3x^2 \cos(bx)}{4b^2} + \frac{3x \sin(bx)}{2b^3} + \frac{3 \cos(bx)}{2b^4} + \frac{1}{4}x^4 \text{CosIntegral}(bx) - \frac{x^3 \sin(bx)}{4b}$$

[Out] (3*Cos[b*x])/(2*b^4) - (3*x^2*Cos[b*x])/(4*b^2) + (x^4*CosIntegral[b*x])/4 + (3*x*Sin[b*x])/(2*b^3) - (x^3*Sin[b*x])/(4*b)

Rubi [A] time = 0.0713873, antiderivative size = 63, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {6504, 12, 3296, 2638}

$$-\frac{3x^2 \cos(bx)}{4b^2} + \frac{3x \sin(bx)}{2b^3} + \frac{3 \cos(bx)}{2b^4} + \frac{1}{4}x^4 \text{CosIntegral}(bx) - \frac{x^3 \sin(bx)}{4b}$$

Antiderivative was successfully verified.

[In] Int[x^3*CosIntegral[b*x],x]

[Out] (3*Cos[b*x])/(2*b^4) - (3*x^2*Cos[b*x])/(4*b^2) + (x^4*CosIntegral[b*x])/4 + (3*x*Sin[b*x])/(2*b^3) - (x^3*Sin[b*x])/(4*b)

Rule 6504

```
Int[CosIntegral[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :
> Simp[((c + d*x)^(m + 1)*CosIntegral[a + b*x])/(d*(m + 1)), x] - Dist[b/(d
*(m + 1)), Int[((c + d*x)^(m + 1)*Cos[a + b*x])/(a + b*x), x], x] /; FreeQ[
{a, b, c, d, m}, x] && NeQ[m, -1]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !Match
Q[u, (b_.)*(v_)] /; FreeQ[b, x]
```

Rule 3296

```
Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)], x_Symbol] :> -Simp[
((c + d*x)^m*cos[e + f*x])/f, x] + Dist[(d*m)/f, Int[(c + d*x)^(m - 1)*Cos[
e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && GtQ[m, 0]
```

Rule 2638

```
Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] :> -Simp[Cos[c + d*x]/d, x] /; FreeQ
[{c, d}, x]
```

Rubi steps

$$\begin{aligned}
\int x^3 \text{Ci}(bx) dx &= \frac{1}{4} x^4 \text{Ci}(bx) - \frac{1}{4} b \int \frac{x^3 \cos(bx)}{b} dx \\
&= \frac{1}{4} x^4 \text{Ci}(bx) - \frac{1}{4} \int x^3 \cos(bx) dx \\
&= \frac{1}{4} x^4 \text{Ci}(bx) - \frac{x^3 \sin(bx)}{4b} + \frac{3 \int x^2 \sin(bx) dx}{4b} \\
&= -\frac{3x^2 \cos(bx)}{4b^2} + \frac{1}{4} x^4 \text{Ci}(bx) - \frac{x^3 \sin(bx)}{4b} + \frac{3 \int x \cos(bx) dx}{2b^2} \\
&= -\frac{3x^2 \cos(bx)}{4b^2} + \frac{1}{4} x^4 \text{Ci}(bx) + \frac{3x \sin(bx)}{2b^3} - \frac{x^3 \sin(bx)}{4b} - \frac{3 \int \sin(bx) dx}{2b^3} \\
&= \frac{3 \cos(bx)}{2b^4} - \frac{3x^2 \cos(bx)}{4b^2} + \frac{1}{4} x^4 \text{Ci}(bx) + \frac{3x \sin(bx)}{2b^3} - \frac{x^3 \sin(bx)}{4b}
\end{aligned}$$

Mathematica [A] time = 0.0398461, size = 53, normalized size = 0.84

$$-\frac{x(b^2x^2 - 6)\sin(bx)}{4b^3} - \frac{3(b^2x^2 - 2)\cos(bx)}{4b^4} + \frac{1}{4}x^4\text{CosIntegral}(bx)$$

Antiderivative was successfully verified.

[In] Integrate[x^3*CosIntegral[b*x],x]

[Out] (-3*(-2 + b^2*x^2)*Cos[b*x])/(4*b^4) + (x^4*CosIntegral[b*x])/4 - (x*(-6 + b^2*x^2)*Sin[b*x])/(4*b^3)

Maple [A] time = 0.048, size = 56, normalized size = 0.9

$$\frac{1}{b^4} \left(\frac{b^4 x^4 \text{Ci}(bx)}{4} - \frac{\sin(bx) b^3 x^3}{4} - \frac{3 b^2 x^2 \cos(bx)}{4} + \frac{3 \cos(bx)}{2} + \frac{3 \sin(bx) bx}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*Ci(b*x),x)

[Out] 1/b^4*(1/4*b^4*x^4*Ci(b*x)-1/4*sin(b*x)*b^3*x^3-3/4*b^2*x^2*cos(b*x)+3/2*cos(b*x)+3/2*sin(b*x)*b*x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \text{Ci}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Ci(b*x),x, algorithm="maxima")

[Out] integrate(x^3*Ci(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^3 \text{Ci}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Ci(b*x),x, algorithm="fricas")

[Out] integral(x^3*cos_integral(b*x), x)

Sympy [A] time = 2.9055, size = 85, normalized size = 1.35

$$-\frac{x^4 \log(bx)}{4} + \frac{x^4 \log(b^2 x^2)}{8} + \frac{x^4 \text{Ci}(bx)}{4} - \frac{x^3 \sin(bx)}{4b} - \frac{3x^2 \cos(bx)}{4b^2} + \frac{3x \sin(bx)}{2b^3} + \frac{3 \cos(bx)}{2b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*Ci(b*x),x)

[Out] -x**4*log(b*x)/4 + x**4*log(b**2*x**2)/8 + x**4*Ci(b*x)/4 - x**3*sin(b*x)/(4*b) - 3*x**2*cos(b*x)/(4*b**2) + 3*x*sin(b*x)/(2*b**3) + 3*cos(b*x)/(2*b**4)

Giac [A] time = 1.19487, size = 66, normalized size = 1.05

$$\frac{1}{4} x^4 \text{Ci}(bx) - \frac{3(b^2 x^2 - 2) \cos(bx)}{4b^4} - \frac{(b^3 x^3 - 6bx) \sin(bx)}{4b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Ci(b*x),x, algorithm="giac")

[Out] 1/4*x^4*cos_integral(b*x) - 3/4*(b^2*x^2 - 2)*cos(b*x)/b^4 - 1/4*(b^3*x^3 - 6*b*x)*sin(b*x)/b^4

3.71 $\int x^2 \text{CosIntegral}(bx) dx$

Optimal. Leaf size=49

$$\frac{2 \sin(bx)}{3b^3} - \frac{2x \cos(bx)}{3b^2} + \frac{1}{3}x^3 \text{CosIntegral}(bx) - \frac{x^2 \sin(bx)}{3b}$$

[Out] $(-2*x*\text{Cos}[b*x])/(3*b^2) + (x^3*\text{CosIntegral}[b*x])/3 + (2*\text{Sin}[b*x])/(3*b^3) - (x^2*\text{Sin}[b*x])/(3*b)$

Rubi [A] time = 0.0478551, antiderivative size = 49, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {6504, 12, 3296, 2637}

$$\frac{2 \sin(bx)}{3b^3} - \frac{2x \cos(bx)}{3b^2} + \frac{1}{3}x^3 \text{CosIntegral}(bx) - \frac{x^2 \sin(bx)}{3b}$$

Antiderivative was successfully verified.

[In] Int[x^2*CosIntegral[b*x], x]

[Out] $(-2*x*\text{Cos}[b*x])/(3*b^2) + (x^3*\text{CosIntegral}[b*x])/3 + (2*\text{Sin}[b*x])/(3*b^3) - (x^2*\text{Sin}[b*x])/(3*b)$

Rule 6504

Int[CosIntegral[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[((c + d*x)^(m + 1)*CosIntegral[a + b*x])/(d*(m + 1)), x] - Dist[b/(d*(m + 1)), Int[((c + d*x)^(m + 1)*Cos[a + b*x])/(a + b*x), x], x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 3296

Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)], x_Symbol] :> -Simp[((c + d*x)^m*cos[e + f*x])/f, x] + Dist[(d*m)/f, Int[(c + d*x)^(m - 1)*cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && GtQ[m, 0]

Rule 2637

Int[sin[Pi/2 + (c_.) + (d_.)*(x_)], x_Symbol] :> Simp[Sin[c + d*x]/d, x] /; FreeQ[{c, d}, x]

Rubi steps

$$\begin{aligned}
\int x^2 \text{Ci}(bx) dx &= \frac{1}{3} x^3 \text{Ci}(bx) - \frac{1}{3} b \int \frac{x^2 \cos(bx)}{b} dx \\
&= \frac{1}{3} x^3 \text{Ci}(bx) - \frac{1}{3} \int x^2 \cos(bx) dx \\
&= \frac{1}{3} x^3 \text{Ci}(bx) - \frac{x^2 \sin(bx)}{3b} + \frac{2 \int x \sin(bx) dx}{3b} \\
&= -\frac{2x \cos(bx)}{3b^2} + \frac{1}{3} x^3 \text{Ci}(bx) - \frac{x^2 \sin(bx)}{3b} + \frac{2 \int \cos(bx) dx}{3b^2} \\
&= -\frac{2x \cos(bx)}{3b^2} + \frac{1}{3} x^3 \text{Ci}(bx) + \frac{2 \sin(bx)}{3b^3} - \frac{x^2 \sin(bx)}{3b}
\end{aligned}$$

Mathematica [A] time = 0.0287376, size = 44, normalized size = 0.9

$$-\frac{(b^2 x^2 - 2) \sin(bx)}{3b^3} - \frac{2x \cos(bx)}{3b^2} + \frac{1}{3} x^3 \text{CosIntegral}(bx)$$

Antiderivative was successfully verified.

[In] Integrate[x^2*CosIntegral[b*x],x]

[Out] (-2*x*Cos[b*x])/(3*b^2) + (x^3*CosIntegral[b*x])/3 - ((-2 + b^2*x^2)*Sin[b*x])/(3*b^3)

Maple [A] time = 0.05, size = 44, normalized size = 0.9

$$\frac{1}{b^3} \left(\frac{b^3 x^3 \text{Ci}(bx)}{3} - \frac{b^2 x^2 \sin(bx)}{3} + \frac{2 \sin(bx)}{3} - \frac{2bx \cos(bx)}{3} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*Ci(b*x),x)

[Out] 1/b^3*(1/3*b^3*x^3*Ci(b*x)-1/3*b^2*x^2*sin(b*x)+2/3*sin(b*x)-2/3*b*x*cos(b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Ci}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x),x, algorithm="maxima")

[Out] integrate(x^2*Ci(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^2 \text{Ci}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*cos_integral(b*x),x, algorithm="fricas")

[Out] integral(x^2*cos_integral(b*x), x)

Sympy [A] time = 2.43547, size = 70, normalized size = 1.43

$$-\frac{x^3 \log(bx)}{3} + \frac{x^3 \log(b^2x^2)}{6} + \frac{x^3 \operatorname{Ci}(bx)}{3} - \frac{x^2 \sin(bx)}{3b} - \frac{2x \cos(bx)}{3b^2} + \frac{2 \sin(bx)}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*cos_integral(b*x),x)

[Out] -x**3*log(b*x)/3 + x**3*log(b**2*x**2)/6 + x**3*cos_integral(b*x)/3 - x**2*sin(b*x)/(3*b) - 2*x*cos(b*x)/(3*b**2) + 2*sin(b*x)/(3*b**3)

Giac [A] time = 1.17142, size = 51, normalized size = 1.04

$$\frac{1}{3} x^3 \operatorname{Ci}(bx) - \frac{2x \cos(bx)}{3b^2} - \frac{(b^2x^2 - 2) \sin(bx)}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*cos_integral(b*x),x, algorithm="giac")

[Out] 1/3*x^3*cos_integral(b*x) - 2/3*x*cos(b*x)/b^2 - 1/3*(b^2*x^2 - 2)*sin(b*x)/b^3

3.72 $\int x \text{CosIntegral}(bx) dx$

Optimal. Leaf size=35

$$-\frac{\cos(bx)}{2b^2} + \frac{1}{2}x^2 \text{CosIntegral}(bx) - \frac{x \sin(bx)}{2b}$$

[Out] $-\text{Cos}[b*x]/(2*b^2) + (x^2*\text{CosIntegral}[b*x])/2 - (x*\text{Sin}[b*x])/(2*b)$

Rubi [A] time = 0.0235583, antiderivative size = 35, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.667$, Rules used = {6504, 12, 3296, 2638}

$$-\frac{\cos(bx)}{2b^2} + \frac{1}{2}x^2 \text{CosIntegral}(bx) - \frac{x \sin(bx)}{2b}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x*\text{CosIntegral}[b*x], x]$

[Out] $-\text{Cos}[b*x]/(2*b^2) + (x^2*\text{CosIntegral}[b*x])/2 - (x*\text{Sin}[b*x])/(2*b)$

Rule 6504

$\text{Int}[\text{CosIntegral}[(a_.) + (b_.)*(x_.)]*((c_.) + (d_.)*(x_.))^{(m_.)}, x_Symbol] :> \text{Simp}[\frac{(c + d*x)^{(m + 1)}*\text{CosIntegral}[a + b*x]}{(d*(m + 1))}, x] - \text{Dist}[b/(d*(m + 1)), \text{Int}[\frac{(c + d*x)^{(m + 1)}*\text{Cos}[a + b*x]}{(a + b*x)}, x], x] /;$ $\text{FreeQ}[\{a, b, c, d, m\}, x] \ \&\& \ \text{NeQ}[m, -1]$

Rule 12

$\text{Int}[(a_)*(u_), x_Symbol] :> \text{Dist}[a, \text{Int}[u, x], x] /;$ $\text{FreeQ}[a, x] \ \&\& \ !\text{MatchQ}[u, (b_)*(v_)] /;$ $\text{FreeQ}[b, x]$

Rule 3296

$\text{Int}[\frac{(c_.) + (d_.)*(x_.))^{(m_.)}*\sin[(e_.) + (f_.)*(x_.)]}{f}, x_Symbol] :> -\text{Simp}[\frac{(c + d*x)^m*\text{Cos}[e + f*x]}{f}, x] + \text{Dist}[\frac{d*m}{f}, \text{Int}[\frac{(c + d*x)^{(m - 1)}*\text{Cos}[e + f*x]}{f}, x], x] /;$ $\text{FreeQ}[\{c, d, e, f\}, x] \ \&\& \ \text{GtQ}[m, 0]$

Rule 2638

$\text{Int}[\sin[(c_.) + (d_.)*(x_.)], x_Symbol] :> -\text{Simp}[\text{Cos}[c + d*x]/d, x] /;$ $\text{FreeQ}[\{c, d\}, x]$

Rubi steps

$$\begin{aligned} \int x \text{Ci}(bx) dx &= \frac{1}{2}x^2 \text{Ci}(bx) - \frac{1}{2}b \int \frac{x \cos(bx)}{b} dx \\ &= \frac{1}{2}x^2 \text{Ci}(bx) - \frac{1}{2} \int x \cos(bx) dx \\ &= \frac{1}{2}x^2 \text{Ci}(bx) - \frac{x \sin(bx)}{2b} + \frac{\int \sin(bx) dx}{2b} \\ &= -\frac{\cos(bx)}{2b^2} + \frac{1}{2}x^2 \text{Ci}(bx) - \frac{x \sin(bx)}{2b} \end{aligned}$$

Mathematica [A] time = 0.0079792, size = 35, normalized size = 1.

$$-\frac{\cos(bx)}{2b^2} + \frac{1}{2}x^2\text{CosIntegral}(bx) - \frac{x \sin(bx)}{2b}$$

Antiderivative was successfully verified.

[In] Integrate[x*CosIntegral[b*x],x]

[Out] -Cos[b*x]/(2*b^2) + (x^2*CosIntegral[b*x])/2 - (x*Sin[b*x])/(2*b)

Maple [A] time = 0.05, size = 32, normalized size = 0.9

$$\frac{1}{b^2} \left(\frac{b^2 x^2 \text{Ci}(bx)}{2} - \frac{\sin(bx) bx}{2} - \frac{\cos(bx)}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*Ci(b*x),x)

[Out] 1/b^2*(1/2*b^2*x^2*Ci(b*x)-1/2*sin(b*x)*b*x-1/2*cos(b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \text{Ci}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x),x, algorithm="maxima")

[Out] integrate(x*Ci(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x \text{Ci}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x),x, algorithm="fricas")

[Out] integral(x*cos_integral(b*x), x)

Sympy [A] time = 1.74918, size = 53, normalized size = 1.51

$$-\frac{x^2 \log(bx)}{2} + \frac{x^2 \log(b^2 x^2)}{4} + \frac{x^2 \text{Ci}(bx)}{2} - \frac{x \sin(bx)}{2b} - \frac{\cos(bx)}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*Ci(b*x),x)
```

```
[Out] -x**2*log(b*x)/2 + x**2*log(b**2*x**2)/4 + x**2*Ci(b*x)/2 - x*sin(b*x)/(2*b) - cos(b*x)/(2*b**2)
```

Giac [A] time = 1.16488, size = 39, normalized size = 1.11

$$\frac{1}{2}x^2 \operatorname{Ci}(bx) - \frac{x \sin(bx)}{2b} - \frac{\cos(bx)}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*Ci(b*x),x, algorithm="giac")
```

```
[Out] 1/2*x^2*cos_integral(b*x) - 1/2*x*sin(b*x)/b - 1/2*cos(b*x)/b^2
```

3.73 $\int \text{CosIntegral}(bx) dx$

Optimal. Leaf size=16

$$x\text{CosIntegral}(bx) - \frac{\sin(bx)}{b}$$

[Out] x*CosIntegral[b*x] - Sin[b*x]/b

Rubi [A] time = 0.0044011, antiderivative size = 16, normalized size of antiderivative = 1., number of steps used = 1, number of rules used = 1, integrand size = 4, $\frac{\text{number of rules}}{\text{integrand size}} = 0.25$, Rules used = {6500}

$$x\text{CosIntegral}(bx) - \frac{\sin(bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[CosIntegral[b*x],x]

[Out] x*CosIntegral[b*x] - Sin[b*x]/b

Rule 6500

Int[CosIntegral[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[((a + b*x)*CosIntegral[a + b*x])/b, x] - Simp[Sin[a + b*x]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\int \text{Ci}(bx) dx = x\text{Ci}(bx) - \frac{\sin(bx)}{b}$$

Mathematica [A] time = 0.0014589, size = 16, normalized size = 1.

$$x\text{CosIntegral}(bx) - \frac{\sin(bx)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[CosIntegral[b*x],x]

[Out] x*CosIntegral[b*x] - Sin[b*x]/b

Maple [A] time = 0.045, size = 19, normalized size = 1.2

$$\frac{bx\text{Ci}(bx) - \sin(bx)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x),x)

[Out] $1/b*(b*x*Ci(b*x)-\sin(b*x))$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int Ci(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x),x, algorithm="maxima")`

[Out] `integrate(Ci(b*x), x)`

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(Ci(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x),x, algorithm="fricas")`

[Out] `integral(cos_integral(b*x), x)`

Sympy [B] time = 1.68395, size = 31, normalized size = 1.94

$$-x \log(bx) + \frac{x \log(b^2 x^2)}{2} + x Ci(bx) - \frac{\sin(bx)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x),x)`

[Out] `-x*log(b*x) + x*log(b**2*x**2)/2 + x*Ci(b*x) - sin(b*x)/b`

Giac [A] time = 1.19137, size = 22, normalized size = 1.38

$$x Ci(bx) - \frac{\sin(bx)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x),x, algorithm="giac")`

[Out] `x*cos_integral(b*x) - sin(b*x)/b`

3.74 $\int \frac{\text{CosIntegral}(bx)}{x} dx$

Optimal. Leaf size=61

$$-\frac{1}{2}ibx\text{HypergeometricPFQ}(\{1,1,1\},\{2,2,2\},-ibx) + \frac{1}{2}ibx\text{HypergeometricPFQ}(\{1,1,1\},\{2,2,2\},ibx) + \frac{1}{2}\log^2(bx)$$

[Out] $(-I/2)*b*x*\text{HypergeometricPFQ}[\{1, 1, 1\}, \{2, 2, 2\}, (-I)*b*x] + (I/2)*b*x*\text{HypergeometricPFQ}[\{1, 1, 1\}, \{2, 2, 2\}, I*b*x] + \text{EulerGamma}*\text{Log}[x] + \text{Log}[b*x]^2/2$

Rubi [A] time = 0.02331, antiderivative size = 61, normalized size of antiderivative = 1., number of steps used = 1, number of rules used = 1, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.125$, Rules used = {6502}

$$-\frac{1}{2}ibx {}_3F_3(1,1,1;2,2,2;-ibx) + \frac{1}{2}ibx {}_3F_3(1,1,1;2,2,2;ibx) + \frac{1}{2}\log^2(bx) + \gamma \log(x)$$

Antiderivative was successfully verified.

[In] Int[CosIntegral[b*x]/x,x]

[Out] $(-I/2)*b*x*\text{HypergeometricPFQ}[\{1, 1, 1\}, \{2, 2, 2\}, (-I)*b*x] + (I/2)*b*x*\text{HypergeometricPFQ}[\{1, 1, 1\}, \{2, 2, 2\}, I*b*x] + \text{EulerGamma}*\text{Log}[x] + \text{Log}[b*x]^2/2$

Rule 6502

Int[CosIntegral[(b_.)*(x_)]/(x_), x_Symbol] :> -Simp[(I*b*x*HypergeometricPFQ[{1, 1, 1}, {2, 2, 2}, -(I*b*x)])/2, x] + (Simp[(1*I*b*x*HypergeometricPFQ[{1, 1, 1}, {2, 2, 2}, I*b*x])/2, x] + Simp[EulerGamma*Log[x], x] + Simp[(1*Log[b*x]^2)/2, x]) /; FreeQ[b, x]

Rubi steps

$$\int \frac{\text{Ci}(bx)}{x} dx = -\frac{1}{2}ibx {}_3F_3(1,1,1;2,2,2;-ibx) + \frac{1}{2}ibx {}_3F_3(1,1,1;2,2,2;ibx) + \gamma \log(x) + \frac{1}{2}\log^2(bx)$$

Mathematica [A] time = 0.039013, size = 94, normalized size = 1.54

$$\frac{1}{2}(-ibx\text{HypergeometricPFQ}(\{1,1,1\},\{2,2,2\},-ibx) + ibx\text{HypergeometricPFQ}(\{1,1,1\},\{2,2,2\},ibx) + \log(x)(\text{Gamma}[0, (-I)*b*x] + \text{Gamma}[0, I*b*x] - \text{Log}[x] + \text{Log}[(-I)*b*x] + \text{Log}[I*b*x]))/2$$

Antiderivative was successfully verified.

[In] Integrate[CosIntegral[b*x]/x,x]

[Out] $((-I)*b*x*\text{HypergeometricPFQ}[\{1, 1, 1\}, \{2, 2, 2\}, (-I)*b*x] + I*b*x*\text{HypergeometricPFQ}[\{1, 1, 1\}, \{2, 2, 2\}, I*b*x] + \text{Log}[x]*(2*\text{EulerGamma} + 2*\text{CosIntegral}[b*x] + \text{Gamma}[0, (-I)*b*x] + \text{Gamma}[0, I*b*x] - \text{Log}[x] + \text{Log}[(-I)*b*x] + \text{Log}[I*b*x]))/2$

Maple [B] time = 0.091, size = 158, normalized size = 2.6

$$\frac{\sqrt{\pi}}{4} \left(\frac{1}{2\sqrt{\pi}} \left(-\frac{\pi^2}{3} + 4 \ln(x)\gamma - 4 \ln(2)\gamma + 4 \ln(b)\gamma + (-\gamma - 2 \ln(2))^2 + 4 (\ln(2))^2 + 4 (\ln(b))^2 + 4 (\ln(x))^2 - 2\gamma \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x)/x,x)

[Out] $\frac{1}{4} \pi^{1/2} \left(\frac{1}{2} \left(-\frac{1}{3} \pi^2 + 4 \ln(x) \gamma - 4 \ln(2) \gamma + 4 \ln(b) \gamma + (-\gamma - 2 \ln(2))^2 + 4 (\ln(2))^2 + 4 (\ln(b))^2 + 4 (\ln(x))^2 - 2\gamma \right) \right) - \frac{1}{2} \pi^{1/2} \operatorname{hypergeom}([1, 1, 1], [3/2, 2, 2, 2], -1/4 b^2 x^2)$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{Ci}(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)/x,x, algorithm="maxima")

[Out] integrate(Ci(b*x)/x, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}\left(\frac{\operatorname{Ci}(bx)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)/x,x, algorithm="fricas")

[Out] integral(cos_integral(b*x)/x, x)

Sympy [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: AttributeError

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)/x,x)

[Out] Exception raised: AttributeError

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{Ci}(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x)/x,x, algorithm="giac")
```

```
[Out] integrate(Ci(b*x)/x, x)
```

3.75 $\int \frac{\text{CosIntegral}(bx)}{x^2} dx$

Optimal. Leaf size=26

$$-\frac{\text{CosIntegral}(bx)}{x} - b\text{Si}(bx) - \frac{\cos(bx)}{x}$$

[Out] -(Cos[b*x]/x) - CosIntegral[b*x]/x - b*SinIntegral[b*x]

Rubi [A] time = 0.0478876, antiderivative size = 26, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {6504, 12, 3297, 3299}

$$-\frac{\text{CosIntegral}(bx)}{x} - b\text{Si}(bx) - \frac{\cos(bx)}{x}$$

Antiderivative was successfully verified.

[In] Int[CosIntegral[b*x]/x^2,x]

[Out] -(Cos[b*x]/x) - CosIntegral[b*x]/x - b*SinIntegral[b*x]

Rule 6504

Int[CosIntegral[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[((c + d*x)^(m + 1)*CosIntegral[a + b*x])/(d*(m + 1)), x] - Dist[b/(d*(m + 1)), Int[((c + d*x)^(m + 1)*Cos[a + b*x])/(a + b*x), x], x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 3297

Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)], x_Symbol] :> Simp[((c + d*x)^(m + 1)*Sin[e + f*x])/(d*(m + 1)), x] - Dist[f/(d*(m + 1)), Int[(c + d*x)^(m + 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && LtQ[m, -1]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned} \int \frac{\text{Ci}(bx)}{x^2} dx &= -\frac{\text{Ci}(bx)}{x} + b \int \frac{\cos(bx)}{bx^2} dx \\ &= -\frac{\text{Ci}(bx)}{x} + \int \frac{\cos(bx)}{x^2} dx \\ &= -\frac{\cos(bx)}{x} - \frac{\text{Ci}(bx)}{x} - b \int \frac{\sin(bx)}{x} dx \\ &= -\frac{\cos(bx)}{x} - \frac{\text{Ci}(bx)}{x} - b\text{Si}(bx) \end{aligned}$$

Mathematica [A] time = 0.0108275, size = 26, normalized size = 1.

$$-\frac{\text{CosIntegral}(bx)}{x} - b\text{Si}(bx) - \frac{\cos(bx)}{x}$$

Antiderivative was successfully verified.

[In] Integrate[CosIntegral[b*x]/x^2,x]

[Out] -(Cos[b*x]/x) - CosIntegral[b*x]/x - b*SinIntegral[b*x]

Maple [A] time = 0.047, size = 34, normalized size = 1.3

$$b\left(-\frac{\text{Ci}(bx)}{bx} - \frac{\cos(bx)}{bx} - \text{Si}(bx)\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x)/x^2,x)

[Out] b*(-Ci(b*x)/b/x-cos(b*x)/b/x-Si(b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)/x^2,x, algorithm="maxima")

[Out] integrate(Ci(b*x)/x^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bx)}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)/x^2,x, algorithm="fricas")

[Out] integral(cos_integral(b*x)/x^2, x)

Sympy [B] time = 1.38407, size = 42, normalized size = 1.62

$$-\frac{b^2 x {}_3F_4\left(\frac{1}{2}, 1, 1 \mid \frac{b^2 x^2}{4}\right)}{4} - \frac{\log(b^2 x^2)}{2x} - \frac{1}{x} - \frac{\gamma}{x}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)/x**2,x)

[Out] $-b^{**2}x*\text{hyper}((1/2, 1, 1), (3/2, 3/2, 2, 2), -b^{**2}x^{**2}/4)/4 - \log(b^{**2}x^{**2})/(2*x) - 1/x - \text{EulerGamma}/x$

Giac [C] time = 1.20492, size = 147, normalized size = 5.65

$$\frac{bx\Im(Ci(bx))\tan\left(\frac{1}{2}bx\right)^2 - bx\Im(Ci(-bx))\tan\left(\frac{1}{2}bx\right)^2 + 2bx\text{Si}(bx)\tan\left(\frac{1}{2}bx\right)^2 + bx\Im(Ci(bx)) - bx\Im(Ci(-bx)) + 2bx}{2\left(x\tan\left(\frac{1}{2}bx\right)^2 + x\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)/x^2,x, algorithm="giac")

[Out] $-1/2*(b*x*\text{imag_part}(\text{cos_integral}(b*x))*\tan(1/2*b*x)^2 - b*x*\text{imag_part}(\text{cos_integral}(-b*x))*\tan(1/2*b*x)^2 + 2*b*x*\text{sin_integral}(b*x)*\tan(1/2*b*x)^2 + b*x*\text{imag_part}(\text{cos_integral}(b*x)) - b*x*\text{imag_part}(\text{cos_integral}(-b*x)) + 2*b*x*\text{sin_integral}(b*x) - 2*\tan(1/2*b*x)^2 + 2)/(x*\tan(1/2*b*x)^2 + x) - \text{cos_integral}(b*x)/x$

3.76 $\int \frac{\text{CosIntegral}(bx)}{x^3} dx$

Optimal. Leaf size=46

$$-\frac{1}{4}b^2\text{CosIntegral}(bx) - \frac{\text{CosIntegral}(bx)}{2x^2} - \frac{\cos(bx)}{4x^2} + \frac{b \sin(bx)}{4x}$$

[Out] $-\text{Cos}[b*x]/(4*x^2) - (b^2*\text{CosIntegral}[b*x])/4 - \text{CosIntegral}[b*x]/(2*x^2) + (b*\text{Sin}[b*x])/(4*x)$

Rubi [A] time = 0.0675109, antiderivative size = 46, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 4, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {6504, 12, 3297, 3302}

$$-\frac{1}{4}b^2\text{CosIntegral}(bx) - \frac{\text{CosIntegral}(bx)}{2x^2} - \frac{\cos(bx)}{4x^2} + \frac{b \sin(bx)}{4x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{CosIntegral}[b*x]/x^3, x]$

[Out] $-\text{Cos}[b*x]/(4*x^2) - (b^2*\text{CosIntegral}[b*x])/4 - \text{CosIntegral}[b*x]/(2*x^2) + (b*\text{Sin}[b*x])/(4*x)$

Rule 6504

$\text{Int}[\text{CosIntegral}[(a_.) + (b_.)*(x_.)]*((c_.) + (d_.)*(x_.))^{(m_.)}, x_Symbol] :> \text{Simp}[\frac{(c + d*x)^{(m + 1)}*\text{CosIntegral}[a + b*x]}{d*(m + 1)}, x] - \text{Dist}[b/(d*(m + 1)), \text{Int}[\frac{(c + d*x)^{(m + 1)}*\text{Cos}[a + b*x]}{a + b*x}, x], x] /;$ FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]

Rule 12

$\text{Int}[(a_)*(u_), x_Symbol] :> \text{Dist}[a, \text{Int}[u, x], x] /;$ FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 3297

$\text{Int}[\frac{(c_.) + (d_.)*(x_.))^{(m_.)}*\sin[(e_.) + (f_.)*(x_.)]}{x_Symbol} :> \text{Simp}[\frac{(c + d*x)^{(m + 1)}*\text{Sin}[e + f*x]}{d*(m + 1)}, x] - \text{Dist}[f/(d*(m + 1)), \text{Int}[\frac{(c + d*x)^{(m + 1)}*\text{Cos}[e + f*x]}{x}, x], x] /;$ FreeQ[{c, d, e, f}, x] && LtQ[m, -1]

Rule 3302

$\text{Int}[\frac{\sin[(e_.) + (f_.)*(x_.)]}{(c_.) + (d_.)*(x_.)}, x_Symbol] :> \text{Simp}[\text{CosIntegral}[e - \text{Pi}/2 + f*x]/d, x] /;$ FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned}
\int \frac{\text{Ci}(bx)}{x^3} dx &= -\frac{\text{Ci}(bx)}{2x^2} + \frac{1}{2}b \int \frac{\cos(bx)}{bx^3} dx \\
&= -\frac{\text{Ci}(bx)}{2x^2} + \frac{1}{2} \int \frac{\cos(bx)}{x^3} dx \\
&= -\frac{\cos(bx)}{4x^2} - \frac{\text{Ci}(bx)}{2x^2} - \frac{1}{4}b \int \frac{\sin(bx)}{x^2} dx \\
&= -\frac{\cos(bx)}{4x^2} - \frac{\text{Ci}(bx)}{2x^2} + \frac{b \sin(bx)}{4x} - \frac{1}{4}b^2 \int \frac{\cos(bx)}{x} dx \\
&= -\frac{\cos(bx)}{4x^2} - \frac{1}{4}b^2 \text{Ci}(bx) - \frac{\text{Ci}(bx)}{2x^2} + \frac{b \sin(bx)}{4x}
\end{aligned}$$

Mathematica [A] time = 0.0138352, size = 46, normalized size = 1.

$$-\frac{1}{4}b^2 \text{CosIntegral}(bx) - \frac{\text{CosIntegral}(bx)}{2x^2} - \frac{\cos(bx)}{4x^2} + \frac{b \sin(bx)}{4x}$$

Antiderivative was successfully verified.

[In] Integrate[CosIntegral[b*x]/x^3,x]

[Out] -Cos[b*x]/(4*x^2) - (b^2*CosIntegral[b*x])/4 - CosIntegral[b*x]/(2*x^2) + (b*Sin[b*x])/(4*x)

Maple [A] time = 0.053, size = 48, normalized size = 1.

$$b^2 \left(-\frac{\text{Ci}(bx)}{2b^2x^2} - \frac{\cos(bx)}{4b^2x^2} + \frac{\sin(bx)}{4bx} - \frac{\text{Ci}(bx)}{4} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x)/x^3,x)

[Out] b^2*(-1/2*Ci(b*x)/b^2/x^2-1/4*cos(b*x)/b^2/x^2+1/4*sin(b*x)/b/x-1/4*Ci(b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)/x^3,x, algorithm="maxima")

[Out] integrate(Ci(b*x)/x^3, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bx)}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)/x^3,x, algorithm="fricas")

[Out] integral(cos_integral(b*x)/x^3, x)

Sympy [B] time = 3.13406, size = 87, normalized size = 1.89

$$\frac{b^2 \log(bx)}{4} - \frac{b^2 \log(b^2x^2)}{8} - \frac{b^2 \operatorname{Ci}(bx)}{4} + \frac{b \sin(bx)}{4x} + \frac{\log(bx)}{2x^2} - \frac{\log(b^2x^2)}{4x^2} - \frac{\cos(bx)}{4x^2} - \frac{\operatorname{Ci}(bx)}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)/x**3,x)

[Out] b**2*log(b*x)/4 - b**2*log(b**2*x**2)/8 - b**2*Ci(b*x)/4 + b*sin(b*x)/(4*x) + log(b*x)/(2*x**2) - log(b**2*x**2)/(4*x**2) - cos(b*x)/(4*x**2) - Ci(b*x)/(2*x**2)

Giac [A] time = 1.16096, size = 72, normalized size = 1.57

$$-\frac{b^2x^2 \operatorname{Ci}(bx) + b^2x^2 \operatorname{Ci}(-bx) - 2bx \sin(bx) + 2 \cos(bx)}{8x^2} - \frac{\operatorname{Ci}(bx)}{2x^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)/x^3,x, algorithm="giac")

[Out] -1/8*(b^2*x^2*cos_integral(b*x) + b^2*x^2*cos_integral(-b*x) - 2*b*x*sin(b*x) + 2*cos(b*x))/x^2 - 1/2*cos_integral(b*x)/x^2

3.77 $\int x^m \mathbf{CosIntegral}(bx)^2 dx$

Optimal. Leaf size=12

CannotIntegrate($x^m \mathbf{CosIntegral}(bx)^2, x$)

[Out] CannotIntegrate[x^m*CosIntegral[b*x]², x]

Rubi [A] time = 0.0329213, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int x^m \mathbf{CosIntegral}(bx)^2 dx$$

Verification is Not applicable to the result.

[In] Int[x^m*CosIntegral[b*x]², x]

[Out] Defer[Int][x^m*CosIntegral[b*x]², x]

Rubi steps

$$\int x^m \mathbf{Ci}(bx)^2 dx = \int x^m \mathbf{Ci}(bx)^2 dx$$

Mathematica [A] time = 2.70721, size = 0, normalized size = 0.

$$\int x^m \mathbf{CosIntegral}(bx)^2 dx$$

Verification is Not applicable to the result.

[In] Integrate[x^m*CosIntegral[b*x]², x]

[Out] Integrate[x^m*CosIntegral[b*x]², x]

Maple [A] time = 0.056, size = 0, normalized size = 0.

$$\int x^m (\mathbf{Ci}(bx))^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*Ci(b*x)², x)

[Out] int(x^m*Ci(b*x)², x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \mathbf{Ci}(bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^m*Ci(b*x)^2,x, algorithm="maxima")
```

```
[Out] integrate(x^m*Ci(b*x)^2, x)
```

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^m \text{Ci}(bx)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^m*Ci(b*x)^2,x, algorithm="fricas")
```

```
[Out] integral(x^m*cos_integral(b*x)^2, x)
```

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \text{Ci}^2(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**m*Ci(b*x)**2,x)
```

```
[Out] Integral(x**m*Ci(b*x)**2, x)
```

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \text{Ci}(bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^m*Ci(b*x)^2,x, algorithm="giac")
```

```
[Out] integrate(x^m*Ci(b*x)^2, x)
```

3.78 $\int x^3 \text{CosIntegral}(bx)^2 dx$

Optimal. Leaf size=163

$$\frac{3x^2 \text{CosIntegral}(bx) \cos(bx)}{2b^2} - \frac{3 \text{CosIntegral}(2bx)}{2b^4} + \frac{3x \text{CosIntegral}(bx) \sin(bx)}{b^3} + \frac{3 \text{CosIntegral}(bx) \cos(bx)}{b^4} + \frac{x^2}{4b^2}$$

[Out] $x^2/(4*b^2) + (3*\text{Cos}[b*x]^2)/(8*b^4) + (3*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/b^4 - (3*x^2*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/(2*b^2) + (x^4*\text{CosIntegral}[b*x]^2)/4 - (3*\text{CosIntegral}[2*b*x])/(2*b^4) - (3*\text{Log}[x])/(2*b^4) + (x*\text{Cos}[b*x]*\text{Sin}[b*x])/b^3 + (3*x*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/b^3 - (x^3*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/(2*b) - (13*\text{Sin}[b*x]^2)/(8*b^4) + (x^2*\text{Sin}[b*x]^2)/(4*b^2)$

Rubi [A] time = 0.228525, antiderivative size = 163, normalized size of antiderivative = 1., number of steps used = 19, number of rules used = 11, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 1.1$, Rules used = {6508, 6514, 12, 3443, 3310, 30, 6520, 2564, 6518, 3312, 3302}

$$\frac{3x^2 \text{CosIntegral}(bx) \cos(bx)}{2b^2} - \frac{3 \text{CosIntegral}(2bx)}{2b^4} + \frac{3x \text{CosIntegral}(bx) \sin(bx)}{b^3} + \frac{3 \text{CosIntegral}(bx) \cos(bx)}{b^4} + \frac{x^2}{4b^2}$$

Antiderivative was successfully verified.

[In] Int[x^3*CosIntegral[b*x]^2,x]

[Out] $x^2/(4*b^2) + (3*\text{Cos}[b*x]^2)/(8*b^4) + (3*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/b^4 - (3*x^2*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/(2*b^2) + (x^4*\text{CosIntegral}[b*x]^2)/4 - (3*\text{CosIntegral}[2*b*x])/(2*b^4) - (3*\text{Log}[x])/(2*b^4) + (x*\text{Cos}[b*x]*\text{Sin}[b*x])/b^3 + (3*x*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/b^3 - (x^3*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/(2*b) - (13*\text{Sin}[b*x]^2)/(8*b^4) + (x^2*\text{Sin}[b*x]^2)/(4*b^2)$

Rule 6508

Int[CosIntegral[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[(x^(m + 1)*CosIntegral[b*x]^2)/(m + 1), x] - Dist[2/(m + 1), Int[x^m*Cos[b*x]*CosIntegral[b*x], x], x] /; FreeQ[b, x] && IGtQ[m, 0]

Rule 6514

Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.), x_Symbol] :> Simp[((e + f*x)^m*Sin[a + b*x]*CosIntegral[c + d*x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Sin[a + b*x]*CosIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 3443

Int[Cos[(a_.) + (b_.)*(x_)^(n_.)]*(x_)^(m_.)*Sin[(a_.) + (b_.)*(x_)^(n_.)]^(p_.), x_Symbol] :> Simp[(x^(m - n + 1)*Sin[a + b*x^n]^(p + 1))/(b*n*(p + 1)), x] - Dist[(m - n + 1)/(b*n*(p + 1)), Int[x^(m - n)*Sin[a + b*x^n]^(p + 1), x], x] /; FreeQ[{a, b, p}, x] && LtQ[0, n, m + 1] && NeQ[p, -1]

Rule 3310

```
Int[((c_.) + (d_.)*(x_))*((b_.)*sin[(e_.) + (f_.)*(x_)])^(n_), x_Symbol] :=
Simp[(d*(b*SIN[e + f*x])^n)/(f^2*n^2), x] + (Dist[(b^2*(n - 1))/n, Int[(c
+ d*x)*(b*SIN[e + f*x])^(n - 2), x], x] - Simp[(b*(c + d*x)*Cos[e + f*x]*(b
*SIN[e + f*x])^(n - 1))/(f*n), x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1
]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 6520

```
Int[CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) +
(b_.)*(x_)], x_Symbol] := -Simp[((e + f*x)^m*Cos[a + b*x]*CosIntegral[c + d
*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*Cos[a + b*x]*Cos[c + d*x])/(c + d*
x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Cos[a + b*x]*CosIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 2564

```
Int[cos[(e_.) + (f_.)*(x_)]^(n_.)*((a_.)*sin[(e_.) + (f_.)*(x_)])^(m_.), x_
Symbol] := Dist[1/(a*f), Subst[Int[x^m*(1 - x^2/a^2)^(n - 1)/2], x], x, a*
Sin[e + f*x], x] /; FreeQ[{a, e, f, m}, x] && IntegerQ[(n - 1)/2] && !(In
tegerQ[(m - 1)/2] && LtQ[0, m, n])
```

Rule 6518

```
Int[CosIntegral[(c_.) + (d_.)*(x_)]*Sin[(a_.) + (b_.)*(x_)], x_Symbol] := -
Simp[(Cos[a + b*x]*CosIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x
]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 3312

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := In
t[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f
, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int x^3 \text{Ci}(bx)^2 dx &= \frac{1}{4}x^4 \text{Ci}(bx)^2 - \frac{1}{2} \int x^3 \cos(bx) \text{Ci}(bx) dx \\
&= \frac{1}{4}x^4 \text{Ci}(bx)^2 - \frac{x^3 \text{Ci}(bx) \sin(bx)}{2b} + \frac{1}{2} \int \frac{x^2 \cos(bx) \sin(bx)}{b} dx + \frac{3 \int x^2 \text{Ci}(bx) \sin(bx) dx}{2b} \\
&= -\frac{3x^2 \cos(bx) \text{Ci}(bx)}{2b^2} + \frac{1}{4}x^4 \text{Ci}(bx)^2 - \frac{x^3 \text{Ci}(bx) \sin(bx)}{2b} + \frac{3 \int x \cos(bx) \text{Ci}(bx) dx}{b^2} + \frac{\int x^2 \cos(bx) \sin(bx) dx}{2b} \\
&= -\frac{3x^2 \cos(bx) \text{Ci}(bx)}{2b^2} + \frac{1}{4}x^4 \text{Ci}(bx)^2 + \frac{3x \text{Ci}(bx) \sin(bx)}{b^3} - \frac{x^3 \text{Ci}(bx) \sin(bx)}{2b} + \frac{x^2 \sin^2(bx)}{4b^2} - \frac{3 \int \text{Ci}(bx) dx}{b} \\
&= \frac{3 \cos^2(bx)}{8b^4} + \frac{3 \cos(bx) \text{Ci}(bx)}{b^4} - \frac{3x^2 \cos(bx) \text{Ci}(bx)}{2b^2} + \frac{1}{4}x^4 \text{Ci}(bx)^2 + \frac{x \cos(bx) \sin(bx)}{b^3} + \frac{3x \text{Ci}(bx) \sin(bx)}{b^3} \\
&= \frac{x^2}{4b^2} + \frac{3 \cos^2(bx)}{8b^4} + \frac{3 \cos(bx) \text{Ci}(bx)}{b^4} - \frac{3x^2 \cos(bx) \text{Ci}(bx)}{2b^2} + \frac{1}{4}x^4 \text{Ci}(bx)^2 + \frac{x \cos(bx) \sin(bx)}{b^3} + \frac{3x \text{Ci}(bx) \sin(bx)}{b^3} \\
&= \frac{x^2}{4b^2} + \frac{3 \cos^2(bx)}{8b^4} + \frac{3 \cos(bx) \text{Ci}(bx)}{b^4} - \frac{3x^2 \cos(bx) \text{Ci}(bx)}{2b^2} + \frac{1}{4}x^4 \text{Ci}(bx)^2 + \frac{x \cos(bx) \sin(bx)}{b^3} + \frac{3x \text{Ci}(bx) \sin(bx)}{b^3} \\
&= \frac{x^2}{4b^2} + \frac{3 \cos^2(bx)}{8b^4} + \frac{3 \cos(bx) \text{Ci}(bx)}{b^4} - \frac{3x^2 \cos(bx) \text{Ci}(bx)}{2b^2} + \frac{1}{4}x^4 \text{Ci}(bx)^2 - \frac{3 \log(x)}{2b^4} + \frac{x \cos(bx) \sin(bx)}{b^3} \\
&= \frac{x^2}{4b^2} + \frac{3 \cos^2(bx)}{8b^4} + \frac{3 \cos(bx) \text{Ci}(bx)}{b^4} - \frac{3x^2 \cos(bx) \text{Ci}(bx)}{2b^2} + \frac{1}{4}x^4 \text{Ci}(bx)^2 - \frac{3 \text{Ci}(2bx)}{2b^4} - \frac{3 \log(x)}{2b^4} + \frac{x \cos(bx) \sin(bx)}{b^3}
\end{aligned}$$

Mathematica [A] time = 0.115799, size = 108, normalized size = 0.66

$$\frac{2b^4 x^4 \text{CosIntegral}(bx)^2 - 4 \text{CosIntegral}(bx) (bx (b^2 x^2 - 6) \sin(bx) + 3 (b^2 x^2 - 2) \cos(bx)) + 3b^2 x^2 - b^2 x^2 \cos(2bx) - 12 \log(x)}{8b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*CosIntegral[b*x]^2,x]

[Out] (3*b^2*x^2 + 8*Cos[2*b*x] - b^2*x^2*Cos[2*b*x] + 2*b^4*x^4*CosIntegral[b*x]^2 - 12*CosIntegral[2*b*x] - 12*Log[x] - 4*CosIntegral[b*x]*(3*(-2 + b^2*x^2)*Cos[b*x] + b*x*(-6 + b^2*x^2)*Sin[b*x]) + 4*b*x*Sin[2*b*x])/(8*b^4)

Maple [A] time = 0.069, size = 148, normalized size = 0.9

$$\frac{x^4 (\text{Ci}(bx))^2}{4} - \frac{x^3 \text{Ci}(bx) \sin(bx)}{2b} - \frac{3x^2 \text{Ci}(bx) \cos(bx)}{2b^2} + 3 \frac{\text{Ci}(bx) \cos(bx)}{b^4} + 3 \frac{x \text{Ci}(bx) \sin(bx)}{b^3} - \frac{x^2 (\cos(bx))^2}{4b^2} + \frac{x \cos(bx) \sin(bx)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*Ci(b*x)^2,x)

[Out] 1/4*x^4*Ci(b*x)^2-1/2*x^3*Ci(b*x)*sin(b*x)/b-3/2*x^2*Ci(b*x)*cos(b*x)/b^2+3*x*Ci(b*x)*cos(b*x)/b^3+3*x^2*Ci(b*x)*sin(b*x)/b^2-1/4*b^2*x^2*cos(b*x)^2+x*cos(b*x)*sin(b*x)/b^3+1/2*x^2/b^2-1/2*sin(b*x)^2/b^4-3/2/b^4*ln(b*x)-3/2*Ci(2*b*x)/b^4+3/2*cos(b*x)^2/b^4

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \text{Ci}(bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Ci(b*x)^2,x, algorithm="maxima")

[Out] integrate(x^3*Ci(b*x)^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^3 \text{Ci}(bx)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Ci(b*x)^2,x, algorithm="fricas")

[Out] integral(x^3*cos_integral(b*x)^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \text{Ci}^2(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*Ci(b*x)**2,x)

[Out] Integral(x**3*Ci(b*x)**2, x)

Giac [A] time = 1.18327, size = 119, normalized size = 0.73

$$\frac{1}{4} x^4 \text{Ci}(bx)^2 - \frac{1}{2} \left(\frac{3(b^2 x^2 - 2) \cos(bx)}{b^4} + \frac{(b^3 x^3 - 6bx) \sin(bx)}{b^4} \right) \text{Ci}(bx) + \frac{3(b^2 x^2 - 2 \text{Ci}(2bx) - 2 \text{Ci}(-2bx) - 4 \log(x))}{8b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Ci(b*x)^2,x, algorithm="giac")

[Out] 1/4*x^4*cos_integral(b*x)^2 - 1/2*(3*(b^2*x^2 - 2)*cos(b*x)/b^4 + (b^3*x^3 - 6*b*x)*sin(b*x)/b^4)*cos_integral(b*x) + 3/8*(b^2*x^2 - 2*cos_integral(2*b*x) - 2*cos_integral(-2*b*x) - 4*log(x))/b^4

3.79 $\int x^2 \text{CosIntegral}(bx)^2 dx$

Optimal. Leaf size=112

$$\frac{4\text{CosIntegral}(bx) \sin(bx)}{3b^3} - \frac{4x\text{CosIntegral}(bx) \cos(bx)}{3b^2} - \frac{2\text{Si}(2bx)}{3b^3} + \frac{x}{2b^2} + \frac{x \sin^2(bx)}{3b^2} + \frac{5 \sin(bx) \cos(bx)}{6b^3} + \frac{1}{3}x^3 \text{CosIntegral}(bx)^2$$

[Out] $x/(2*b^2) - (4*x*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/(3*b^2) + (x^3*\text{CosIntegral}[b*x]^2)/3 + (5*\text{Cos}[b*x]*\text{Sin}[b*x])/(6*b^3) + (4*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/(3*b^3) - (2*x^2*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/(3*b) + (x*\text{Sin}[b*x]^2)/(3*b^2) - (2*\text{SinIntegral}[2*b*x])/(3*b^3)$

Rubi [A] time = 0.138129, antiderivative size = 112, normalized size of antiderivative = 1., number of steps used = 15, number of rules used = 10, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 1.$, Rules used = {6508, 6514, 12, 3443, 2635, 8, 6520, 6512, 4406, 3299}

$$\frac{4\text{CosIntegral}(bx) \sin(bx)}{3b^3} - \frac{4x\text{CosIntegral}(bx) \cos(bx)}{3b^2} - \frac{2\text{Si}(2bx)}{3b^3} + \frac{x}{2b^2} + \frac{x \sin^2(bx)}{3b^2} + \frac{5 \sin(bx) \cos(bx)}{6b^3} + \frac{1}{3}x^3 \text{CosIntegral}(bx)^2$$

Antiderivative was successfully verified.

[In] Int[x^2*CosIntegral[b*x]^2,x]

[Out] $x/(2*b^2) - (4*x*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/(3*b^2) + (x^3*\text{CosIntegral}[b*x]^2)/3 + (5*\text{Cos}[b*x]*\text{Sin}[b*x])/(6*b^3) + (4*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/(3*b^3) - (2*x^2*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/(3*b) + (x*\text{Sin}[b*x]^2)/(3*b^2) - (2*\text{SinIntegral}[2*b*x])/(3*b^3)$

Rule 6508

Int[CosIntegral[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] := Simp[(x^(m + 1)*CosIntegral[b*x]^2)/(m + 1), x] - Dist[2/(m + 1), Int[x^m*Cos[b*x]*CosIntegral[b*x], x], x] /; FreeQ[b, x] && IGtQ[m, 0]

Rule 6514

Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.), x_Symbol] := Simp[((e + f*x)^m*Sin[a + b*x]*CosIntegral[c + d*x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Sin[a + b*x]*CosIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 3443

Int[Cos[(a_.) + (b_.)*(x_)^(n_.)]*(x_)^(m_.)*Sin[(a_.) + (b_.)*(x_)^(n_.)]^(p_.), x_Symbol] := Simp[(x^(m - n + 1)*Sin[a + b*x^n]^(p + 1))/(b*n*(p + 1)), x] - Dist[(m - n + 1)/(b*n*(p + 1)), Int[x^(m - n)*Sin[a + b*x^n]^(p + 1), x], x] /; FreeQ[{a, b, p}, x] && LtQ[0, n, m + 1] && NeQ[p, -1]

Rule 2635

Int[((b_.)*sin[(c_.) + (d_.)*(x_)])^(n_), x_Symbol] := -Simp[(b*cos[c + d*x]*(b*sin[c + d*x])^(n - 1))/(d*n), x] + Dist[(b^2*(n - 1))/n, Int[(b*sin[c + d*x])^(n - 1), x], x]

+ d*x])^(n - 2), x], x] /; FreeQ[{b, c, d}, x] && GtQ[n, 1] && IntegerQ[2*n]

Rule 8

Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]

Rule 6520

Int[CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)], x_Symbol] := -Simp[((e + f*x)^m*Cos[a + b*x]*CosIntegral[c + d*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*Cos[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Cos[a + b*x]*CosIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]

Rule 6512

Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := Simp[(Sin[a + b*x]*CosIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^(n)*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned}
 \int x^2 \text{Ci}(bx)^2 dx &= \frac{1}{3} x^3 \text{Ci}(bx)^2 - \frac{2}{3} \int x^2 \cos(bx) \text{Ci}(bx) dx \\
 &= \frac{1}{3} x^3 \text{Ci}(bx)^2 - \frac{2x^2 \text{Ci}(bx) \sin(bx)}{3b} + \frac{2}{3} \int \frac{x \cos(bx) \sin(bx)}{b} dx + \frac{4 \int x \text{Ci}(bx) \sin(bx) dx}{3b} \\
 &= -\frac{4x \cos(bx) \text{Ci}(bx)}{3b^2} + \frac{1}{3} x^3 \text{Ci}(bx)^2 - \frac{2x^2 \text{Ci}(bx) \sin(bx)}{3b} + \frac{4 \int \cos(bx) \text{Ci}(bx) dx}{3b^2} + \frac{2 \int x \cos(bx) \sin(bx) dx}{3b} \\
 &= -\frac{4x \cos(bx) \text{Ci}(bx)}{3b^2} + \frac{1}{3} x^3 \text{Ci}(bx)^2 + \frac{4 \text{Ci}(bx) \sin(bx)}{3b^3} - \frac{2x^2 \text{Ci}(bx) \sin(bx)}{3b} + \frac{x \sin^2(bx)}{3b^2} - \frac{\int \sin^2(bx) dx}{3b^2} \\
 &= -\frac{4x \cos(bx) \text{Ci}(bx)}{3b^2} + \frac{1}{3} x^3 \text{Ci}(bx)^2 + \frac{5 \cos(bx) \sin(bx)}{6b^3} + \frac{4 \text{Ci}(bx) \sin(bx)}{3b^3} - \frac{2x^2 \text{Ci}(bx) \sin(bx)}{3b} + \frac{x \sin^2(bx)}{3b^2} \\
 &= \frac{x}{2b^2} - \frac{4x \cos(bx) \text{Ci}(bx)}{3b^2} + \frac{1}{3} x^3 \text{Ci}(bx)^2 + \frac{5 \cos(bx) \sin(bx)}{6b^3} + \frac{4 \text{Ci}(bx) \sin(bx)}{3b^3} - \frac{2x^2 \text{Ci}(bx) \sin(bx)}{3b} \\
 &= \frac{x}{2b^2} - \frac{4x \cos(bx) \text{Ci}(bx)}{3b^2} + \frac{1}{3} x^3 \text{Ci}(bx)^2 + \frac{5 \cos(bx) \sin(bx)}{6b^3} + \frac{4 \text{Ci}(bx) \sin(bx)}{3b^3} - \frac{2x^2 \text{Ci}(bx) \sin(bx)}{3b} \\
 &= \frac{x}{2b^2} - \frac{4x \cos(bx) \text{Ci}(bx)}{3b^2} + \frac{1}{3} x^3 \text{Ci}(bx)^2 + \frac{5 \cos(bx) \sin(bx)}{6b^3} + \frac{4 \text{Ci}(bx) \sin(bx)}{3b^3} - \frac{2x^2 \text{Ci}(bx) \sin(bx)}{3b}
 \end{aligned}$$

Mathematica [A] time = 0.0805696, size = 78, normalized size = 0.7

$$\frac{4b^3 x^3 \text{CosIntegral}(bx)^2 - 8 \text{CosIntegral}(bx) \left((b^2 x^2 - 2) \sin(bx) + 2bx \cos(bx) \right) - 8 \text{Si}(2bx) + 8bx + 5 \sin(2bx) - 2bx}{12b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*CosIntegral[b*x]^2,x]

[Out] (8*b*x - 2*b*x*Cos[2*b*x] + 4*b^3*x^3*CosIntegral[b*x]^2 - 8*CosIntegral[b*x]*(2*b*x*Cos[b*x] + (-2 + b^2*x^2)*Sin[b*x]) + 5*Sin[2*b*x] - 8*SinIntegral[2*b*x])/(12*b^3)

Maple [A] time = 0.073, size = 84, normalized size = 0.8

$$\frac{1}{b^3} \left(\frac{b^3 x^3 (\text{Ci}(bx))^2}{3} - 2 \text{Ci}(bx) \left(\frac{1}{3} b^2 x^2 \sin(bx) - \frac{2}{3} \sin(bx) + \frac{2}{3} bx \cos(bx) \right) - \frac{bx (\cos(bx))^2}{3} + \frac{5 \sin(bx) \cos(bx)}{6} \right) +$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*Ci(b*x)^2,x)

[Out] 1/b^3*(1/3*b^3*x^3*Ci(b*x)^2-2*Ci(b*x)*(1/3*b^2*x^2*sin(b*x)-2/3*sin(b*x)+2/3*b*x*cos(b*x))-1/3*b*x*cos(b*x)^2+5/6*sin(b*x)*cos(b*x)+5/6*b*x-2/3*Si(2*b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Ci}(bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x)^2,x, algorithm="maxima")

[Out] integrate(x^2*Ci(b*x)^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^2 \text{Ci}(bx)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x)^2,x, algorithm="fricas")

[Out] integral(x^2*cos_integral(b*x)^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Ci}^2(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*Ci(b*x)**2,x)

[Out] Integral(x**2*Ci(b*x)**2, x)

Giac [C] time = 1.22111, size = 104, normalized size = 0.93

$$\frac{1}{3} x^3 \operatorname{Ci}(bx)^2 - \frac{2}{3} \left(\frac{2x \cos(bx)}{b^2} + \frac{(b^2 x^2 - 2) \sin(bx)}{b^3} \right) \operatorname{Ci}(bx) + \frac{2bx - \Im(\operatorname{Ci}(2bx)) + \Im(\operatorname{Ci}(-2bx)) - 2 \operatorname{Si}(2bx)}{3b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x)^2,x, algorithm="giac")

[Out] 1/3*x^3*cos_integral(b*x)^2 - 2/3*(2*x*cos(b*x)/b^2 + (b^2*x^2 - 2)*sin(b*x)/b^3)*cos_integral(b*x) + 1/3*(2*b*x - imag_part(cos_integral(2*b*x)) + imag_part(cos_integral(-2*b*x)) - 2*sin_integral(2*b*x))/b^3

3.80 $\int x \text{CosIntegral}(bx)^2 dx$

Optimal. Leaf size=75

$$\frac{\text{CosIntegral}(2bx)}{2b^2} - \frac{\text{CosIntegral}(bx) \cos(bx)}{b^2} + \frac{\log(x)}{2b^2} + \frac{\sin^2(bx)}{2b^2} + \frac{1}{2}x^2 \text{CosIntegral}(bx)^2 - \frac{x \text{CosIntegral}(bx) \sin(bx)}{b}$$

[Out] -((Cos[b*x]*CosIntegral[b*x])/b^2) + (x^2*CosIntegral[b*x]^2)/2 + CosIntegral[2*b*x]/(2*b^2) + Log[x]/(2*b^2) - (x*CosIntegral[b*x]*Sin[b*x])/b + Sin[b*x]^2/(2*b^2)

Rubi [A] time = 0.0906658, antiderivative size = 75, normalized size of antiderivative = 1., number of steps used = 10, number of rules used = 8, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 1.$, Rules used = {6508, 6514, 12, 2564, 30, 6518, 3312, 3302}

$$\frac{\text{CosIntegral}(2bx)}{2b^2} - \frac{\text{CosIntegral}(bx) \cos(bx)}{b^2} + \frac{\log(x)}{2b^2} + \frac{\sin^2(bx)}{2b^2} + \frac{1}{2}x^2 \text{CosIntegral}(bx)^2 - \frac{x \text{CosIntegral}(bx) \sin(bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[x*CosIntegral[b*x]^2,x]

[Out] -((Cos[b*x]*CosIntegral[b*x])/b^2) + (x^2*CosIntegral[b*x]^2)/2 + CosIntegral[2*b*x]/(2*b^2) + Log[x]/(2*b^2) - (x*CosIntegral[b*x]*Sin[b*x])/b + Sin[b*x]^2/(2*b^2)

Rule 6508

Int[CosIntegral[(b_.)*(x_)]^2*(x_)^(m_.), x_Symbol] :> Simp[(x^(m + 1)*CosIntegral[b*x]^2)/(m + 1), x] - Dist[2/(m + 1), Int[x^m*Cos[b*x]*CosIntegral[b*x], x], x] /; FreeQ[b, x] && IGtQ[m, 0]

Rule 6514

Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.), x_Symbol] :> Simp[((e + f*x)^m*Sin[a + b*x]*CosIntegral[c + d*x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Sin[a + b*x]*CosIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 2564

Int[cos[(e_.) + (f_.)*(x_)]^(n_.)*((a_.)*sin[(e_.) + (f_.)*(x_)]^(m_.), x_Symbol] :> Dist[1/(a*f), Subst[Int[x^m*(1 - x^2/a^2)^((n - 1)/2), x], x, a*Sin[e + f*x], x] /; FreeQ[{a, e, f, m}, x] && IntegerQ[(n - 1)/2] && !(IntegerQ[(m - 1)/2] && LtQ[0, m, n])

Rule 30

Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 6518

```
Int[CosIntegral[(c_.) + (d_.)*(x_)]*Sin[(a_.) + (b_.)*(x_)], x_Symbol] := -
Simp[(Cos[a + b*x]*CosIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]
]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 3312

```
Int[((c_.) + (d_.)*(x_)^(m_))*sin[(e_.) + (f_.)*(x_)^(n_)], x_Symbol] := In
t[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f
, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int x \operatorname{Ci}(bx)^2 dx &= \frac{1}{2} x^2 \operatorname{Ci}(bx)^2 - \int x \cos(bx) \operatorname{Ci}(bx) dx \\
&= \frac{1}{2} x^2 \operatorname{Ci}(bx)^2 - \frac{x \operatorname{Ci}(bx) \sin(bx)}{b} + \frac{\int \operatorname{Ci}(bx) \sin(bx) dx}{b} + \int \frac{\cos(bx) \sin(bx)}{b} dx \\
&= -\frac{\cos(bx) \operatorname{Ci}(bx)}{b^2} + \frac{1}{2} x^2 \operatorname{Ci}(bx)^2 - \frac{x \operatorname{Ci}(bx) \sin(bx)}{b} + \frac{\int \frac{\cos^2(bx)}{bx} dx}{b} + \frac{\int \cos(bx) \sin(bx) dx}{b} \\
&= -\frac{\cos(bx) \operatorname{Ci}(bx)}{b^2} + \frac{1}{2} x^2 \operatorname{Ci}(bx)^2 - \frac{x \operatorname{Ci}(bx) \sin(bx)}{b} + \frac{\int \frac{\cos^2(bx)}{x} dx}{b^2} + \frac{\operatorname{Subst}(\int x dx, x, \sin(bx))}{b^2} \\
&= -\frac{\cos(bx) \operatorname{Ci}(bx)}{b^2} + \frac{1}{2} x^2 \operatorname{Ci}(bx)^2 - \frac{x \operatorname{Ci}(bx) \sin(bx)}{b} + \frac{\sin^2(bx)}{2b^2} + \frac{\int \left(\frac{1}{2x} + \frac{\cos(2bx)}{2x} \right) dx}{b^2} \\
&= -\frac{\cos(bx) \operatorname{Ci}(bx)}{b^2} + \frac{1}{2} x^2 \operatorname{Ci}(bx)^2 + \frac{\log(x)}{2b^2} - \frac{x \operatorname{Ci}(bx) \sin(bx)}{b} + \frac{\sin^2(bx)}{2b^2} + \frac{\int \frac{\cos(2bx)}{x} dx}{2b^2} \\
&= -\frac{\cos(bx) \operatorname{Ci}(bx)}{b^2} + \frac{1}{2} x^2 \operatorname{Ci}(bx)^2 + \frac{\operatorname{Ci}(2bx)}{2b^2} + \frac{\log(x)}{2b^2} - \frac{x \operatorname{Ci}(bx) \sin(bx)}{b} + \frac{\sin^2(bx)}{2b^2}
\end{aligned}$$

Mathematica [A] time = 0.0489505, size = 58, normalized size = 0.77

$$\frac{2b^2 x^2 \operatorname{CosIntegral}(bx)^2 + 2 \operatorname{CosIntegral}(2bx) - 4 \operatorname{CosIntegral}(bx)(bx \sin(bx) + \cos(bx)) - \cos(2bx) + 2 \log(x)}{4b^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[x*CosIntegral[b*x]^2,x]
```

```
[Out] (-Cos[2*b*x] + 2*b^2*x^2*CosIntegral[b*x]^2 + 2*CosIntegral[2*b*x] + 2*Log[x]
- 4*CosIntegral[b*x]*(Cos[b*x] + b*x*Sin[b*x]))/(4*b^2)
```

Maple [A] time = 0.059, size = 70, normalized size = 0.9

$$\frac{x^2 (\operatorname{Ci}(bx))^2}{2} - \frac{x \operatorname{Ci}(bx) \sin(bx)}{b} - \frac{\operatorname{Ci}(bx) \cos(bx)}{b^2} - \frac{(\cos(bx))^2}{2b^2} + \frac{\ln(bx)}{2b^2} + \frac{\operatorname{Ci}(2bx)}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*Ci(b*x)^2,x)`

[Out] $\frac{1}{2}x^2Ci(bx)^2 - xCi(bx)\sin(bx)/b - Ci(bx)\cos(bx)/b^2 - \frac{1}{2}b^{-2}\cos(bx)^2 + \frac{1}{2}b^{-2}\ln(bx) + \frac{1}{2}Ci(2bx)/b^2$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int xCi(bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Ci(b*x)^2,x, algorithm="maxima")`

[Out] `integrate(x*Ci(b*x)^2, x)`

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x Ci(bx)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Ci(b*x)^2,x, algorithm="fricas")`

[Out] `integral(x*cos_integral(b*x)^2, x)`

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x Ci^2(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Ci(b*x)**2,x)`

[Out] `Integral(x*Ci(b*x)**2, x)`

Giac [A] time = 1.29807, size = 76, normalized size = 1.01

$$\frac{1}{2}x^2 Ci(bx)^2 - \left(\frac{x \sin(bx)}{b} + \frac{\cos(bx)}{b^2} \right) Ci(bx) + \frac{Ci(2bx) + Ci(-2bx) + 2 \log(x)}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Ci(b*x)^2,x, algorithm="giac")`

[Out] $\frac{1}{2}x^2\cos_integral(bx)^2 - (x\sin(bx)/b + \cos(bx)/b^2)\cos_integral(bx) + \frac{1}{4}(\cos_integral(2bx) + \cos_integral(-2bx) + 2\log(x))/b^2$

3.81 $\int \text{CosIntegral}(bx)^2 dx$

Optimal. Leaf size=31

$$x\text{CosIntegral}(bx)^2 - \frac{2\text{CosIntegral}(bx)\sin(bx)}{b} + \frac{\text{Si}(2bx)}{b}$$

[Out] x*CosIntegral[b*x]^2 - (2*CosIntegral[b*x]*Sin[b*x])/b + SinIntegral[2*b*x]/b

Rubi [A] time = 0.0537311, antiderivative size = 31, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 5, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.833$, Rules used = {6506, 6512, 12, 4406, 3299}

$$x\text{CosIntegral}(bx)^2 - \frac{2\text{CosIntegral}(bx)\sin(bx)}{b} + \frac{\text{Si}(2bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[CosIntegral[b*x]^2,x]

[Out] x*CosIntegral[b*x]^2 - (2*CosIntegral[b*x]*Sin[b*x])/b + SinIntegral[2*b*x]/b

Rule 6506

Int[CosIntegral[(a_.) + (b_.)*(x_)]^2, x_Symbol] := Simp[((a + b*x)*CosIntegral[a + b*x]^2)/b, x] - Dist[2, Int[Cos[a + b*x]*CosIntegral[a + b*x], x], x] /; FreeQ[{a, b}, x]

Rule 6512

Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := Simp[(Sin[a + b*x]*CosIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned}
\int \text{Ci}(bx)^2 dx &= x\text{Ci}(bx)^2 - 2 \int \cos(bx)\text{Ci}(bx) dx \\
&= x\text{Ci}(bx)^2 - \frac{2\text{Ci}(bx) \sin(bx)}{b} + 2 \int \frac{\cos(bx) \sin(bx)}{bx} dx \\
&= x\text{Ci}(bx)^2 - \frac{2\text{Ci}(bx) \sin(bx)}{b} + \frac{2 \int \frac{\cos(bx) \sin(bx)}{x} dx}{b} \\
&= x\text{Ci}(bx)^2 - \frac{2\text{Ci}(bx) \sin(bx)}{b} + \frac{2 \int \frac{\sin(2bx)}{2x} dx}{b} \\
&= x\text{Ci}(bx)^2 - \frac{2\text{Ci}(bx) \sin(bx)}{b} + \frac{\int \frac{\sin(2bx)}{x} dx}{b} \\
&= x\text{Ci}(bx)^2 - \frac{2\text{Ci}(bx) \sin(bx)}{b} + \frac{\text{Si}(2bx)}{b}
\end{aligned}$$

Mathematica [A] time = 0.0076127, size = 31, normalized size = 1.

$$x\text{CosIntegral}(bx)^2 - \frac{2\text{CosIntegral}(bx) \sin(bx)}{b} + \frac{\text{Si}(2bx)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[CosIntegral[b*x]^2, x]

[Out] x*CosIntegral[b*x]^2 - (2*CosIntegral[b*x]*Sin[b*x])/b + SinIntegral[2*b*x]/b

Maple [A] time = 0.047, size = 30, normalized size = 1.

$$\frac{bx (\text{Ci}(bx))^2 - 2 \text{Ci}(bx) \sin(bx) + \text{Si}(2bx)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x)^2, x)

[Out] 1/b*(b*x*Ci(b*x)^2-2*Ci(b*x)*sin(b*x)+Si(2*b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Ci}(bx)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)^2, x, algorithm="maxima")

[Out] integrate(Ci(b*x)^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(\text{Ci}(bx)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x)^2,x, algorithm="fricas")
```

```
[Out] integral(cos_integral(b*x)^2, x)
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \operatorname{Ci}^2(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x)**2,x)
```

```
[Out] Integral(Ci(b*x)**2, x)
```

Giac [C] time = 1.28276, size = 66, normalized size = 2.13

$$x \operatorname{Ci}(bx)^2 - \frac{2 \operatorname{Ci}(bx) \sin(bx)}{b} + \frac{\Im(\operatorname{Ci}(2bx)) - \Im(\operatorname{Ci}(-2bx)) + 2 \operatorname{Si}(2bx)}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x)^2,x, algorithm="giac")
```

```
[Out] x*cos_integral(b*x)^2 - 2*cos_integral(b*x)*sin(b*x)/b + 1/2*(imag_part(cos
_integral(2*b*x)) - imag_part(cos_integral(-2*b*x)) + 2*sin_integral(2*b*x)
)/b
```

$$3.82 \quad \int \frac{\text{CosIntegral}(bx)^2}{x} dx$$

Optimal. Leaf size=12

$$\text{CannotIntegrate}\left(\frac{\text{CosIntegral}(bx)^2}{x}, x\right)$$

[Out] CannotIntegrate[CosIntegral[b*x]^2/x, x]

Rubi [A] time = 0.0217906, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{CosIntegral}(bx)^2}{x} dx$$

Verification is Not applicable to the result.

[In] Int[CosIntegral[b*x]^2/x, x]

[Out] Defer[Int][CosIntegral[b*x]^2/x, x]

Rubi steps

$$\int \frac{\text{Ci}(bx)^2}{x} dx = \int \frac{\text{Ci}(bx)^2}{x} dx$$

Mathematica [A] time = 0.400944, size = 0, normalized size = 0.

$$\int \frac{\text{CosIntegral}(bx)^2}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[CosIntegral[b*x]^2/x, x]

[Out] Integrate[CosIntegral[b*x]^2/x, x]

Maple [A] time = 0.047, size = 0, normalized size = 0.

$$\int \frac{(\text{Ci}(bx))^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x)^2/x, x)

[Out] int(Ci(b*x)^2/x, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)^2/x,x, algorithm="maxima")

[Out] integrate(Ci(b*x)^2/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bx)^2}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)^2/x,x, algorithm="fricas")

[Out] integral(cos_integral(b*x)^2/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}^2(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)**2/x,x)

[Out] Integral(Ci(b*x)**2/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)^2/x,x, algorithm="giac")

[Out] integrate(Ci(b*x)^2/x, x)

$$3.83 \quad \int \frac{\text{CosIntegral}(bx)^2}{x^2} dx$$

Optimal. Leaf size=12

$$\text{CannotIntegrate}\left(\frac{\text{CosIntegral}(bx)^2}{x^2}, x\right)$$

[Out] CannotIntegrate[CosIntegral[b*x]^2/x^2, x]

Rubi [A] time = 0.0251882, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{CosIntegral}(bx)^2}{x^2} dx$$

Verification is Not applicable to the result.

[In] Int[CosIntegral[b*x]^2/x^2, x]

[Out] Defer[Int][CosIntegral[b*x]^2/x^2, x]

Rubi steps

$$\int \frac{\text{Ci}(bx)^2}{x^2} dx = \int \frac{\text{Ci}(bx)^2}{x^2} dx$$

Mathematica [A] time = 0.484829, size = 0, normalized size = 0.

$$\int \frac{\text{CosIntegral}(bx)^2}{x^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[CosIntegral[b*x]^2/x^2, x]

[Out] Integrate[CosIntegral[b*x]^2/x^2, x]

Maple [A] time = 0.055, size = 0, normalized size = 0.

$$\int \frac{(\text{Ci}(bx))^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x)^2/x^2, x)

[Out] int(Ci(b*x)^2/x^2, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)^2/x^2,x, algorithm="maxima")

[Out] integrate(Ci(b*x)^2/x^2, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bx)^2}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)^2/x^2,x, algorithm="fricas")

[Out] integral(cos_integral(b*x)^2/x^2, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}^2(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)**2/x**2,x)

[Out] Integral(Ci(b*x)**2/x**2, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)^2/x^2,x, algorithm="giac")

[Out] integrate(Ci(b*x)^2/x^2, x)

$$3.84 \quad \int \frac{\text{CosIntegral}(bx)^2}{x^3} dx$$

Optimal. Leaf size=12

$$\text{CannotIntegrate}\left(\frac{\text{CosIntegral}(bx)^2}{x^3}, x\right)$$

[Out] CannotIntegrate[CosIntegral[b*x]^2/x^3, x]

Rubi [A] time = 0.0256739, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{CosIntegral}(bx)^2}{x^3} dx$$

Verification is Not applicable to the result.

[In] Int[CosIntegral[b*x]^2/x^3, x]

[Out] Defer[Int][CosIntegral[b*x]^2/x^3, x]

Rubi steps

$$\int \frac{\text{Ci}(bx)^2}{x^3} dx = \int \frac{\text{Ci}(bx)^2}{x^3} dx$$

Mathematica [A] time = 0.499957, size = 0, normalized size = 0.

$$\int \frac{\text{CosIntegral}(bx)^2}{x^3} dx$$

Verification is Not applicable to the result.

[In] Integrate[CosIntegral[b*x]^2/x^3, x]

[Out] Integrate[CosIntegral[b*x]^2/x^3, x]

Maple [A] time = 0.052, size = 0, normalized size = 0.

$$\int \frac{(\text{Ci}(bx))^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x)^2/x^3, x)

[Out] int(Ci(b*x)^2/x^3, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx)^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)^2/x^3,x, algorithm="maxima")

[Out] integrate(Ci(b*x)^2/x^3, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bx)^2}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)^2/x^3,x, algorithm="fricas")

[Out] integral(cos_integral(b*x)^2/x^3, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}^2(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)**2/x**3,x)

[Out] Integral(Ci(b*x)**2/x**3, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx)^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)^2/x^3,x, algorithm="giac")

[Out] integrate(Ci(b*x)^2/x^3, x)

3.85 $\int x^m \text{CosIntegral}(a + bx) dx$

Optimal. Leaf size=47

$$\frac{x^{m+1} \text{CosIntegral}(a + bx)}{m + 1} - \frac{b \text{CannotIntegrate}\left(\frac{x^{m+1} \cos(a+bx)}{a+bx}, x\right)}{m + 1}$$

[Out] $-\left(\frac{b \text{CannotIntegrate}[(x^{1+m}) \cos[a + b*x]]}{(a + b*x)}, x\right) / (1 + m) + (x^{1+m}) \text{CosIntegral}[a + b*x] / (1 + m)$

Rubi [A] time = 0.315771, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int x^m \text{CosIntegral}(a + bx) dx$$

Verification is Not applicable to the result.

[In] Int[x^m*CosIntegral[a + b*x], x]

[Out] $(x^{1+m}) \text{CosIntegral}[a + b*x] / (1 + m) - (b \text{Defer}[\text{Int}][(x^{1+m}) \cos[a + b*x]] / (a + b*x), x) / (1 + m)$

Rubi steps

$$\int x^m \text{Ci}(a + bx) dx = \frac{x^{1+m} \text{Ci}(a + bx)}{1 + m} - \frac{b \int \frac{x^{1+m} \cos(a+bx)}{a+bx} dx}{1 + m}$$

Mathematica [A] time = 3.60651, size = 0, normalized size = 0.

$$\int x^m \text{CosIntegral}(a + bx) dx$$

Verification is Not applicable to the result.

[In] Integrate[x^m*CosIntegral[a + b*x], x]

[Out] Integrate[x^m*CosIntegral[a + b*x], x]

Maple [A] time = 0.155, size = 0, normalized size = 0.

$$\int x^m \text{Ci}(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*Ci(b*x+a), x)

[Out] int(x^m*Ci(b*x+a), x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \operatorname{Ci}(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Ci(b*x+a),x, algorithm="maxima")

[Out] integrate(x^m*Ci(b*x + a), x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}(x^m \operatorname{Ci}(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Ci(b*x+a),x, algorithm="fricas")

[Out] integral(x^m*cos_integral(b*x + a), x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \operatorname{Ci}(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**m*Ci(b*x+a),x)

[Out] Integral(x**m*Ci(a + b*x), x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \operatorname{Ci}(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^m*Ci(b*x+a),x, algorithm="giac")

[Out] integrate(x^m*Ci(b*x + a), x)

3.86 $\int x^3 \text{CosIntegral}(a + bx) dx$

Optimal. Leaf size=184

$$-\frac{a^4 \text{CosIntegral}(a + bx)}{4b^4} + \frac{a^3 \sin(a + bx)}{4b^4} - \frac{a^2 x \sin(a + bx)}{4b^3} - \frac{a^2 \cos(a + bx)}{4b^4} + \frac{ax^2 \sin(a + bx)}{4b^2} - \frac{3x^2 \cos(a + bx)}{4b^2} - \frac{ax^3 \sin(a + bx)}{4b}$$

```
[Out] (3*Cos[a + b*x])/(2*b^4) - (a^2*Cos[a + b*x])/(4*b^4) + (a*x*Cos[a + b*x])/(2*b^3) - (3*x^2*Cos[a + b*x])/(4*b^2) - (a^4*CosIntegral[a + b*x])/(4*b^4) + (x^4*CosIntegral[a + b*x])/4 - (a*Sin[a + b*x])/(2*b^4) + (a^3*Sin[a + b*x])/(4*b^4) + (3*x*Sin[a + b*x])/(2*b^3) - (a^2*x*Sin[a + b*x])/(4*b^3) + (a*x^2*Sin[a + b*x])/(4*b^2) - (x^3*Sin[a + b*x])/(4*b)
```

Rubi [A] time = 0.374411, antiderivative size = 184, normalized size of antiderivative = 1., number of steps used = 14, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.6$, Rules used = {6504, 6742, 2637, 3296, 2638, 3302}

$$-\frac{a^4 \text{CosIntegral}(a + bx)}{4b^4} + \frac{a^3 \sin(a + bx)}{4b^4} - \frac{a^2 x \sin(a + bx)}{4b^3} - \frac{a^2 \cos(a + bx)}{4b^4} + \frac{ax^2 \sin(a + bx)}{4b^2} - \frac{3x^2 \cos(a + bx)}{4b^2} - \frac{ax^3 \sin(a + bx)}{4b}$$

Antiderivative was successfully verified.

```
[In] Int[x^3*CosIntegral[a + b*x],x]
```

```
[Out] (3*Cos[a + b*x])/(2*b^4) - (a^2*Cos[a + b*x])/(4*b^4) + (a*x*Cos[a + b*x])/(2*b^3) - (3*x^2*Cos[a + b*x])/(4*b^2) - (a^4*CosIntegral[a + b*x])/(4*b^4) + (x^4*CosIntegral[a + b*x])/4 - (a*Sin[a + b*x])/(2*b^4) + (a^3*Sin[a + b*x])/(4*b^4) + (3*x*Sin[a + b*x])/(2*b^3) - (a^2*x*Sin[a + b*x])/(4*b^3) + (a*x^2*Sin[a + b*x])/(4*b^2) - (x^3*Sin[a + b*x])/(4*b)
```

Rule 6504

```
Int[CosIntegral[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_)^(m_.), x_Symbol] :> Simp[((c + d*x)^(m + 1)*CosIntegral[a + b*x])/(d*(m + 1)), x] - Dist[b/(d*(m + 1)), Int[((c + d*x)^(m + 1)*Cos[a + b*x])/(a + b*x), x], x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]
```

Rule 6742

```
Int[u_, x_Symbol] :=> With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]]
```

Rule 2637

```
Int[sin[Pi/2 + (c_.) + (d_.)*(x_)], x_Symbol] :=> Simp[Sin[c + d*x]/d, x] /; FreeQ[{c, d}, x]
```

Rule 3296

```
Int[((c_.) + (d_.)*(x_)^(m_.))*sin[(e_.) + (f_.)*(x_)], x_Symbol] :=> -Simp[((c + d*x)^m*Cos[e + f*x])/f, x] + Dist[(d*m)/f, Int[(c + d*x)^(m - 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && GtQ[m, 0]
```

Rule 2638

```
Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] :=> -Simp[Cos[c + d*x]/d, x] /; FreeQ[{c, d}, x]
```

Rule 3302

`Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]`

Rubi steps

$$\begin{aligned}
 \int x^3 \text{Ci}(a + bx) dx &= \frac{1}{4} x^4 \text{Ci}(a + bx) - \frac{1}{4} b \int \frac{x^4 \cos(a + bx)}{a + bx} dx \\
 &= \frac{1}{4} x^4 \text{Ci}(a + bx) - \frac{1}{4} b \int \left(-\frac{a^3 \cos(a + bx)}{b^4} + \frac{a^2 x \cos(a + bx)}{b^3} - \frac{a x^2 \cos(a + bx)}{b^2} + \frac{x^3 \cos(a + bx)}{b} \right) dx \\
 &= \frac{1}{4} x^4 \text{Ci}(a + bx) - \frac{1}{4} \int x^3 \cos(a + bx) dx + \frac{a^3 \int \cos(a + bx) dx}{4b^3} - \frac{a^4 \int \frac{\cos(a+bx)}{a+bx} dx}{4b^3} - \frac{a^2 \int x \cos(a+bx) dx}{4b^2} \\
 &= -\frac{a^4 \text{Ci}(a + bx)}{4b^4} + \frac{1}{4} x^4 \text{Ci}(a + bx) + \frac{a^3 \sin(a + bx)}{4b^4} - \frac{a^2 x \sin(a + bx)}{4b^3} + \frac{a x^2 \sin(a + bx)}{4b^2} - \frac{x^3 \sin(a + bx)}{4b} \\
 &= -\frac{a^2 \cos(a + bx)}{4b^4} + \frac{a x \cos(a + bx)}{2b^3} - \frac{3x^2 \cos(a + bx)}{4b^2} - \frac{a^4 \text{Ci}(a + bx)}{4b^4} + \frac{1}{4} x^4 \text{Ci}(a + bx) + \frac{a^3 \sin(a + bx)}{4b^4} \\
 &= -\frac{a^2 \cos(a + bx)}{4b^4} + \frac{a x \cos(a + bx)}{2b^3} - \frac{3x^2 \cos(a + bx)}{4b^2} - \frac{a^4 \text{Ci}(a + bx)}{4b^4} + \frac{1}{4} x^4 \text{Ci}(a + bx) - \frac{a \sin(a + bx)}{2b} \\
 &= \frac{3 \cos(a + bx)}{2b^4} - \frac{a^2 \cos(a + bx)}{4b^4} + \frac{a x \cos(a + bx)}{2b^3} - \frac{3x^2 \cos(a + bx)}{4b^2} - \frac{a^4 \text{Ci}(a + bx)}{4b^4} + \frac{1}{4} x^4 \text{Ci}(a + bx)
 \end{aligned}$$

Mathematica [A] time = 0.217777, size = 95, normalized size = 0.52

$$\frac{(b^4 x^4 - a^4) \text{CosIntegral}(a + bx) + (-a^2 b x + a^3 + a b^2 x^2 - 2a - b^3 x^3 + 6bx) \sin(a + bx) - (a^2 - 2abx + 3b^2 x^2 - 6) \cos(a + bx)}{4b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*CosIntegral[a + b*x], x]

[Out] $(-((-6 + a^2 - 2*a*b*x + 3*b^2*x^2)*\text{Cos}[a + b*x]) + (-a^4 + b^4*x^4)*\text{CosIntegral}[a + b*x] + (-2*a + a^3 + 6*b*x - a^2*b*x + a*b^2*x^2 - b^3*x^3)*\text{Sin}[a + b*x])/(4*b^4)$

Maple [A] time = 0.052, size = 154, normalized size = 0.8

$$\frac{1}{b^4} \left(\frac{\text{Ci}(bx + a) b^4 x^4}{4} - \frac{\sin(bx + a) (bx + a)^3}{4} - \frac{3 (bx + a)^2 \cos(bx + a)}{4} + \frac{3 \cos(bx + a)}{2} + \frac{3 \sin(bx + a) (bx + a)}{2} + \dots \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*Ci(b*x+a), x)

[Out] $1/b^4*(1/4*Ci(b*x+a)*b^4*x^4-1/4*\sin(b*x+a)*(b*x+a)^3-3/4*(b*x+a)^2*\cos(b*x+a)+3/2*\cos(b*x+a)+3/2*\sin(b*x+a)*(b*x+a)+a*((b*x+a)^2*\sin(b*x+a)-2*\sin(b*x+a)+2*(b*x+a)*\cos(b*x+a))-3/2*a^2*(\sin(b*x+a)*(b*x+a)+\cos(b*x+a))+a^3*\sin(b*x+a)-1/4*a^4*Ci(b*x+a))$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \text{Ci}(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Ci(b*x+a),x, algorithm="maxima")

[Out] integrate(x^3*Ci(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^3 \text{Ci}(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Ci(b*x+a),x, algorithm="fricas")

[Out] integral(x^3*cos_integral(b*x + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \text{Ci}(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*Ci(b*x+a),x)

[Out] Integral(x**3*Ci(a + b*x), x)

Giac [A] time = 1.20939, size = 108, normalized size = 0.59

$$\frac{1}{4} x^4 \text{Ci}(bx + a) - \frac{a^4 \cos(a)^2 \text{Ci}(bx + a) + a^4 \cos(a)^2 \text{Ci}(-bx - a) + a^4 \text{Ci}(bx + a) \sin(a)^2 + a^4 \text{Ci}(-bx - a) \sin(a)^2}{8b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Ci(b*x+a),x, algorithm="giac")

[Out] 1/4*x^4*cos_integral(b*x + a) - 1/8*(a^4*cos(a)^2*cos_integral(b*x + a) + a^4*cos(a)^2*cos_integral(-b*x - a) + a^4*cos_integral(b*x + a)*sin(a)^2 + a^4*cos_integral(-b*x - a)*sin(a)^2)/b^4

3.87 $\int x^2 \text{CosIntegral}(a + bx) dx$

Optimal. Leaf size=118

$$\frac{a^3 \text{CosIntegral}(a + bx)}{3b^3} - \frac{a^2 \sin(a + bx)}{3b^3} + \frac{ax \sin(a + bx)}{3b^2} + \frac{2 \sin(a + bx)}{3b^3} + \frac{a \cos(a + bx)}{3b^3} - \frac{2x \cos(a + bx)}{3b^2} + \frac{1}{3}x^3 C$$

```
[Out] (a*Cos[a + b*x])/(3*b^3) - (2*x*Cos[a + b*x])/(3*b^2) + (a^3*CosIntegral[a + b*x])/(3*b^3) + (x^3*CosIntegral[a + b*x])/3 + (2*Sin[a + b*x])/(3*b^3) - (a^2*Sin[a + b*x])/(3*b^3) + (a*x*Sin[a + b*x])/(3*b^2) - (x^2*Sin[a + b*x])/(3*b)
```

Rubi [A] time = 0.272134, antiderivative size = 118, normalized size of antiderivative = 1., number of steps used = 10, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.6$, Rules used = {6504, 6742, 2637, 3296, 2638, 3302}

$$\frac{a^3 \text{CosIntegral}(a + bx)}{3b^3} - \frac{a^2 \sin(a + bx)}{3b^3} + \frac{ax \sin(a + bx)}{3b^2} + \frac{2 \sin(a + bx)}{3b^3} + \frac{a \cos(a + bx)}{3b^3} - \frac{2x \cos(a + bx)}{3b^2} + \frac{1}{3}x^3 C$$

Antiderivative was successfully verified.

```
[In] Int[x^2*CosIntegral[a + b*x],x]
```

```
[Out] (a*Cos[a + b*x])/(3*b^3) - (2*x*Cos[a + b*x])/(3*b^2) + (a^3*CosIntegral[a + b*x])/(3*b^3) + (x^3*CosIntegral[a + b*x])/3 + (2*Sin[a + b*x])/(3*b^3) - (a^2*Sin[a + b*x])/(3*b^3) + (a*x*Sin[a + b*x])/(3*b^2) - (x^2*Sin[a + b*x])/(3*b)
```

Rule 6504

```
Int[CosIntegral[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[((c + d*x)^(m + 1)*CosIntegral[a + b*x])/(d*(m + 1)), x] - Dist[b/(d*(m + 1)), Int[((c + d*x)^(m + 1)*Cos[a + b*x])/(a + b*x), x], x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]
```

Rule 6742

```
Int[u_, x_Symbol] :> With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]]
```

Rule 2637

```
Int[sin[Pi/2 + (c_.) + (d_.)*(x_)], x_Symbol] :> Simp[Sin[c + d*x]/d, x] /; FreeQ[{c, d}, x]
```

Rule 3296

```
Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)], x_Symbol] :> -Simp[((c + d*x)^m*Cos[e + f*x])/f, x] + Dist[(d*m)/f, Int[(c + d*x)^(m - 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && GtQ[m, 0]
```

Rule 2638

```
Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] :> -Simp[Cos[c + d*x]/d, x] /; FreeQ[{c, d}, x]
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rubi steps

$$\begin{aligned}
 \int x^2 \text{Ci}(a + bx) dx &= \frac{1}{3} x^3 \text{Ci}(a + bx) - \frac{1}{3} b \int \frac{x^3 \cos(a + bx)}{a + bx} dx \\
 &= \frac{1}{3} x^3 \text{Ci}(a + bx) - \frac{1}{3} b \int \left(\frac{a^2 \cos(a + bx)}{b^3} - \frac{ax \cos(a + bx)}{b^2} + \frac{x^2 \cos(a + bx)}{b} - \frac{a^3 \cos(a + bx)}{b^3(a + bx)} \right) dx \\
 &= \frac{1}{3} x^3 \text{Ci}(a + bx) - \frac{1}{3} \int x^2 \cos(a + bx) dx - \frac{a^2 \int \cos(a + bx) dx}{3b^2} + \frac{a^3 \int \frac{\cos(a + bx)}{a + bx} dx}{3b^2} + \frac{a \int x \cos(a + bx) dx}{3b} \\
 &= \frac{a^3 \text{Ci}(a + bx)}{3b^3} + \frac{1}{3} x^3 \text{Ci}(a + bx) - \frac{a^2 \sin(a + bx)}{3b^3} + \frac{ax \sin(a + bx)}{3b^2} - \frac{x^2 \sin(a + bx)}{3b} - \frac{a \int \sin(a + bx) dx}{3b^2} \\
 &= \frac{a \cos(a + bx)}{3b^3} - \frac{2x \cos(a + bx)}{3b^2} + \frac{a^3 \text{Ci}(a + bx)}{3b^3} + \frac{1}{3} x^3 \text{Ci}(a + bx) - \frac{a^2 \sin(a + bx)}{3b^3} + \frac{ax \sin(a + bx)}{3b^2} \\
 &= \frac{a \cos(a + bx)}{3b^3} - \frac{2x \cos(a + bx)}{3b^2} + \frac{a^3 \text{Ci}(a + bx)}{3b^3} + \frac{1}{3} x^3 \text{Ci}(a + bx) + \frac{2 \sin(a + bx)}{3b^3} - \frac{a^2 \sin(a + bx)}{3b^3}
 \end{aligned}$$

Mathematica [A] time = 0.149831, size = 64, normalized size = 0.54

$$\frac{(a^3 + b^3 x^3) \text{CosIntegral}(a + bx) - (a^2 - abx + b^2 x^2 - 2) \sin(a + bx) + (a - 2bx) \cos(a + bx)}{3b^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*CosIntegral[a + b*x], x]
```

```
[Out] ((a - 2*b*x)*Cos[a + b*x] + (a^3 + b^3*x^3)*CosIntegral[a + b*x] - (-2 + a^2 - a*b*x + b^2*x^2)*Sin[a + b*x])/(3*b^3)
```

Maple [A] time = 0.049, size = 99, normalized size = 0.8

$$\frac{1}{b^3} \left(\frac{b^3 x^3 \text{Ci}(bx + a)}{3} - \frac{(bx + a)^2 \sin(bx + a)}{3} + \frac{2 \sin(bx + a)}{3} - \frac{(2bx + 2a) \cos(bx + a)}{3} + a(\sin(bx + a)(bx + a) + \cos(bx + a)) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*Ci(b*x+a), x)
```

```
[Out] 1/b^3*(1/3*b^3*x^3*Ci(b*x+a)-1/3*(b*x+a)^2*sin(b*x+a)+2/3*sin(b*x+a)-2/3*(b*x+a)*cos(b*x+a)+a*(sin(b*x+a)*(b*x+a)+cos(b*x+a))-a^2*sin(b*x+a)+1/3*a^3*Ci(b*x+a))
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Ci}(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x+a),x, algorithm="maxima")

[Out] integrate(x^2*Ci(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^2 \text{Ci}(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x+a),x, algorithm="fricas")

[Out] integral(x^2*cos_integral(b*x + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Ci}(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*Ci(b*x+a),x)

[Out] Integral(x**2*Ci(a + b*x), x)

Giac [A] time = 1.17672, size = 108, normalized size = 0.92

$$\frac{1}{3} x^3 \text{Ci}(bx + a) + \frac{a^3 \cos(a)^2 \text{Ci}(bx + a) + a^3 \cos(a)^2 \text{Ci}(-bx - a) + a^3 \text{Ci}(bx + a) \sin(a)^2 + a^3 \text{Ci}(-bx - a) \sin(a)^2}{6 b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x+a),x, algorithm="giac")

[Out] 1/3*x^3*cos_integral(b*x + a) + 1/6*(a^3*cos(a)^2*cos_integral(b*x + a) + a^3*cos(a)^2*cos_integral(-b*x - a) + a^3*cos_integral(b*x + a)*sin(a)^2 + a^3*cos_integral(-b*x - a)*sin(a)^2)/b^3

3.88 $\int x \text{CosIntegral}(a + bx) dx$

Optimal. Leaf size=71

$$-\frac{a^2 \text{CosIntegral}(a + bx)}{2b^2} + \frac{a \sin(a + bx)}{2b^2} - \frac{\cos(a + bx)}{2b^2} + \frac{1}{2} x^2 \text{CosIntegral}(a + bx) - \frac{x \sin(a + bx)}{2b}$$

[Out] $-\text{Cos}[a + b*x]/(2*b^2) - (a^2*\text{CosIntegral}[a + b*x])/(2*b^2) + (x^2*\text{CosIntegral}[a + b*x])/2 + (a*\text{Sin}[a + b*x])/(2*b^2) - (x*\text{Sin}[a + b*x])/(2*b)$

Rubi [A] time = 0.20677, antiderivative size = 71, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 6, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.75$, Rules used = {6504, 6742, 2637, 3296, 2638, 3302}

$$-\frac{a^2 \text{CosIntegral}(a + bx)}{2b^2} + \frac{a \sin(a + bx)}{2b^2} - \frac{\cos(a + bx)}{2b^2} + \frac{1}{2} x^2 \text{CosIntegral}(a + bx) - \frac{x \sin(a + bx)}{2b}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x*\text{CosIntegral}[a + b*x], x]$

[Out] $-\text{Cos}[a + b*x]/(2*b^2) - (a^2*\text{CosIntegral}[a + b*x])/(2*b^2) + (x^2*\text{CosIntegral}[a + b*x])/2 + (a*\text{Sin}[a + b*x])/(2*b^2) - (x*\text{Sin}[a + b*x])/(2*b)$

Rule 6504

$\text{Int}[\text{CosIntegral}[(a_.) + (b_.)*(x_.)]*((c_.) + (d_.)*(x_.))^{(m_.)}, x_Symbol] :> \text{Simp}[(c + d*x)^{(m + 1)}*\text{CosIntegral}[a + b*x]/(d*(m + 1)), x] - \text{Dist}[b/(d*(m + 1)), \text{Int}[(c + d*x)^{(m + 1)}*\text{Cos}[a + b*x]/(a + b*x), x], x] /; \text{FreeQ}[\{a, b, c, d, m\}, x] \&\& \text{NeQ}[m, -1]$

Rule 6742

$\text{Int}[u_, x_Symbol] :> \text{With}[\{v = \text{ExpandIntegrand}[u, x]\}, \text{Int}[v, x] /; \text{SumQ}[v]]$

Rule 2637

$\text{Int}[\sin[\text{Pi}/2 + (c_.) + (d_.)*(x_.)], x_Symbol] :> \text{Simp}[\text{Sin}[c + d*x]/d, x] /; \text{FreeQ}[\{c, d\}, x]$

Rule 3296

$\text{Int}[(c_.) + (d_.)*(x_.))^{(m_.)}*\sin[(e_.) + (f_.)*(x_.)], x_Symbol] :> -\text{Simp}[(c + d*x)^m*\text{Cos}[e + f*x]/f, x] + \text{Dist}[(d*m)/f, \text{Int}[(c + d*x)^{(m - 1)}*\text{Cos}[e + f*x], x], x] /; \text{FreeQ}[\{c, d, e, f\}, x] \&\& \text{GtQ}[m, 0]$

Rule 2638

$\text{Int}[\sin[(c_.) + (d_.)*(x_.)], x_Symbol] :> -\text{Simp}[\text{Cos}[c + d*x]/d, x] /; \text{FreeQ}[\{c, d\}, x]$

Rule 3302

$\text{Int}[\sin[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] :> \text{Simp}[\text{CosIntegral}[e - \text{Pi}/2 + f*x]/d, x] /; \text{FreeQ}[\{c, d, e, f\}, x] \&\& \text{EqQ}[d*(e - \text{Pi}/2) -$

c*f, 0]

Rubi steps

$$\begin{aligned}
\int x \operatorname{Ci}(a+bx) dx &= \frac{1}{2} x^2 \operatorname{Ci}(a+bx) - \frac{1}{2} b \int \frac{x^2 \cos(a+bx)}{a+bx} dx \\
&= \frac{1}{2} x^2 \operatorname{Ci}(a+bx) - \frac{1}{2} b \int \left(-\frac{a \cos(a+bx)}{b^2} + \frac{x \cos(a+bx)}{b} + \frac{a^2 \cos(a+bx)}{b^2(a+bx)} \right) dx \\
&= \frac{1}{2} x^2 \operatorname{Ci}(a+bx) - \frac{1}{2} \int x \cos(a+bx) dx + \frac{a \int \cos(a+bx) dx}{2b} - \frac{a^2 \int \frac{\cos(a+bx)}{a+bx} dx}{2b} \\
&= -\frac{a^2 \operatorname{Ci}(a+bx)}{2b^2} + \frac{1}{2} x^2 \operatorname{Ci}(a+bx) + \frac{a \sin(a+bx)}{2b^2} - \frac{x \sin(a+bx)}{2b} + \frac{\int \sin(a+bx) dx}{2b} \\
&= -\frac{\cos(a+bx)}{2b^2} - \frac{a^2 \operatorname{Ci}(a+bx)}{2b^2} + \frac{1}{2} x^2 \operatorname{Ci}(a+bx) + \frac{a \sin(a+bx)}{2b^2} - \frac{x \sin(a+bx)}{2b}
\end{aligned}$$

Mathematica [A] time = 0.105331, size = 49, normalized size = 0.69

$$\frac{(b^2 x^2 - a^2) \operatorname{CosIntegral}(a+bx) + (a-bx) \sin(a+bx) - \cos(a+bx)}{2b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*CosIntegral[a + b*x], x]

[Out] (-Cos[a + b*x] + (-a^2 + b^2*x^2)*CosIntegral[a + b*x] + (a - b*x)*Sin[a + b*x])/(2*b^2)

Maple [A] time = 0.049, size = 60, normalized size = 0.9

$$\frac{1}{b^2} \left(\operatorname{Ci}(bx+a) \left(\frac{(bx+a)^2}{2} - a(bx+a) \right) - \frac{\sin(bx+a)(bx+a)}{2} - \frac{\cos(bx+a)}{2} + a \sin(bx+a) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*Ci(b*x+a), x)

[Out] 1/b^2*(Ci(b*x+a)*(1/2*(b*x+a)^2-a*(b*x+a))-1/2*sin(b*x+a)*(b*x+a)-1/2*cos(b*x+a)+a*sin(b*x+a))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \operatorname{Ci}(bx+a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x+a), x, algorithm="maxima")

[Out] integrate(x*Ci(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x \text{Ci}(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x+a),x, algorithm="fricas")

[Out] integral(x*cos_integral(b*x + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \text{Ci}(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x+a),x)

[Out] Integral(x*Ci(a + b*x), x)

Giac [A] time = 1.14683, size = 108, normalized size = 1.52

$$\frac{1}{2} x^2 \text{Ci}(bx + a) - \frac{a^2 \cos(a)^2 \text{Ci}(bx + a) + a^2 \cos(a)^2 \text{Ci}(-bx - a) + a^2 \text{Ci}(bx + a) \sin(a)^2 + a^2 \text{Ci}(-bx - a) \sin(a)^2}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x+a),x, algorithm="giac")

[Out] 1/2*x^2*cos_integral(b*x + a) - 1/4*(a^2*cos(a)^2*cos_integral(b*x + a) + a^2*cos(a)^2*cos_integral(-b*x - a) + a^2*cos_integral(b*x + a)*sin(a)^2 + a^2*cos_integral(-b*x - a)*sin(a)^2)/b^2

3.89 $\int \text{CosIntegral}(a + bx) dx$

Optimal. Leaf size=27

$$\frac{(a + bx)\text{CosIntegral}(a + bx)}{b} - \frac{\sin(a + bx)}{b}$$

[Out] ((a + b*x)*CosIntegral[a + b*x])/b - Sin[a + b*x]/b

Rubi [A] time = 0.0056449, antiderivative size = 27, normalized size of antiderivative = 1., number of steps used = 1, number of rules used = 1, integrand size = 6, $\frac{\text{number of rules}}{\text{integrand size}} = 0.167$, Rules used = {6500}

$$\frac{(a + bx)\text{CosIntegral}(a + bx)}{b} - \frac{\sin(a + bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[CosIntegral[a + b*x], x]

[Out] ((a + b*x)*CosIntegral[a + b*x])/b - Sin[a + b*x]/b

Rule 6500

Int[CosIntegral[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[((a + b*x)*CosIntegral[a + b*x])/b, x] - Simp[Sin[a + b*x]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\int \text{Ci}(a + bx) dx = \frac{(a + bx)\text{Ci}(a + bx)}{b} - \frac{\sin(a + bx)}{b}$$

Mathematica [A] time = 0.0363525, size = 42, normalized size = 1.56

$$x\text{CosIntegral}(a + bx) + \frac{a\text{CosIntegral}(a + bx)}{b} - \frac{\sin(a) \cos(bx)}{b} - \frac{\cos(a) \sin(bx)}{b}$$

Antiderivative was successfully verified.

[In] Integrate[CosIntegral[a + b*x], x]

[Out] (a*CosIntegral[a + b*x])/b + x*CosIntegral[a + b*x] - (Cos[b*x]*Sin[a])/b - (Cos[a]*Sin[b*x])/b

Maple [A] time = 0.043, size = 26, normalized size = 1.

$$\frac{(bx + a) \text{Ci}(bx + a) - \sin(bx + a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x+a), x)

[Out] $1/b*((b*x+a)*Ci(b*x+a)-\sin(b*x+a))$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int Ci(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x+a),x, algorithm="maxima")`

[Out] `integrate(Ci(b*x + a), x)`

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(Ci(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x+a),x, algorithm="fricas")`

[Out] `integral(cos_integral(b*x + a), x)`

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int Ci(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x+a),x)`

[Out] `Integral(Ci(a + b*x), x)`

Giac [B] time = 1.13353, size = 93, normalized size = 3.44

$$x Ci(bx + a) + \frac{a \cos(a)^2 Ci(bx + a) + a \cos(a)^2 Ci(-bx - a) + a Ci(bx + a) \sin(a)^2 + a Ci(-bx - a) \sin(a)^2}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x+a),x, algorithm="giac")`

[Out] `x*cos_integral(b*x + a) + 1/2*(a*cos(a)^2*cos_integral(b*x + a) + a*cos(a)^2*cos_integral(-b*x - a) + a*cos_integral(b*x + a)*sin(a)^2 + a*cos_integral(-b*x - a)*sin(a)^2)/b`

$$3.90 \quad \int \frac{\text{CosIntegral}(a+bx)}{x} dx$$

Optimal. Leaf size=12

$$\text{CannotIntegrate}\left(\frac{\text{CosIntegral}(a+bx)}{x}, x\right)$$

[Out] CannotIntegrate[CosIntegral[a + b*x]/x, x]

Rubi [A] time = 0.0207117, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{CosIntegral}(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Int[CosIntegral[a + b*x]/x, x]

[Out] Defer[Int][CosIntegral[a + b*x]/x, x]

Rubi steps

$$\int \frac{\text{Ci}(a+bx)}{x} dx = \int \frac{\text{Ci}(a+bx)}{x} dx$$

Mathematica [A] time = 0.612036, size = 0, normalized size = 0.

$$\int \frac{\text{CosIntegral}(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[CosIntegral[a + b*x]/x, x]

[Out] Integrate[CosIntegral[a + b*x]/x, x]

Maple [A] time = 0.056, size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx+a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x+a)/x, x)

[Out] int(Ci(b*x+a)/x, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)/x,x, algorithm="maxima")

[Out] integrate(Ci(b*x + a)/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bx + a)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)/x,x, algorithm="fricas")

[Out] integral(cos_integral(b*x + a)/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(a + bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)/x,x)

[Out] Integral(Ci(a + b*x)/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)/x,x, algorithm="giac")

[Out] integrate(Ci(b*x + a)/x, x)

3.91 $\int \frac{\text{CosIntegral}(a+bx)}{x^2} dx$

Optimal. Leaf size=47

$$-\frac{b\text{CosIntegral}(a+bx)}{a} - \frac{\text{CosIntegral}(a+bx)}{x} + \frac{b\cos(a)\text{CosIntegral}(bx)}{a} - \frac{b\sin(a)\text{Si}(bx)}{a}$$

[Out] (b*Cos[a]*CosIntegral[b*x])/a - (b*CosIntegral[a + b*x])/a - CosIntegral[a + b*x]/x - (b*Sin[a]*SinIntegral[b*x])/a

Rubi [A] time = 0.221595, antiderivative size = 47, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {6504, 6742, 3303, 3299, 3302}

$$-\frac{b\text{CosIntegral}(a+bx)}{a} - \frac{\text{CosIntegral}(a+bx)}{x} + \frac{b\cos(a)\text{CosIntegral}(bx)}{a} - \frac{b\sin(a)\text{Si}(bx)}{a}$$

Antiderivative was successfully verified.

[In] Int[CosIntegral[a + b*x]/x^2,x]

[Out] (b*Cos[a]*CosIntegral[b*x])/a - (b*CosIntegral[a + b*x])/a - CosIntegral[a + b*x]/x - (b*Sin[a]*SinIntegral[b*x])/a

Rule 6504

Int[CosIntegral[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[((c + d*x)^(m + 1)*CosIntegral[a + b*x])/(d*(m + 1)), x] - Dist[b/(d*(m + 1)), Int[((c + d*x)^(m + 1)*Cos[a + b*x])/(a + b*x), x], x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]

Rule 6742

Int[u_, x_Symbol] :> With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]]

Rule 3303

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned}
\int \frac{\text{Ci}(a+bx)}{x^2} dx &= -\frac{\text{Ci}(a+bx)}{x} + b \int \frac{\cos(a+bx)}{x(a+bx)} dx \\
&= -\frac{\text{Ci}(a+bx)}{x} + b \int \left(\frac{\cos(a+bx)}{ax} - \frac{b \cos(a+bx)}{a(a+bx)} \right) dx \\
&= -\frac{\text{Ci}(a+bx)}{x} + \frac{b \int \frac{\cos(a+bx)}{x} dx}{a} - \frac{b^2 \int \frac{\cos(a+bx)}{a+bx} dx}{a} \\
&= -\frac{b \text{Ci}(a+bx)}{a} - \frac{\text{Ci}(a+bx)}{x} + \frac{(b \cos(a)) \int \frac{\cos(bx)}{x} dx}{a} - \frac{(b \sin(a)) \int \frac{\sin(bx)}{x} dx}{a} \\
&= \frac{b \cos(a) \text{Ci}(bx)}{a} - \frac{b \text{Ci}(a+bx)}{a} - \frac{\text{Ci}(a+bx)}{x} - \frac{b \sin(a) \text{Si}(bx)}{a}
\end{aligned}$$

Mathematica [A] time = 0.0796085, size = 40, normalized size = 0.85

$$\frac{-(a+bx)\text{CosIntegral}(a+bx) + bx \cos(a)\text{CosIntegral}(bx) - bx \sin(a)\text{Si}(bx)}{ax}$$

Antiderivative was successfully verified.

[In] Integrate[CosIntegral[a + b*x]/x^2,x]

[Out] (b*x*Cos[a]*CosIntegral[b*x] - (a + b*x)*CosIntegral[a + b*x] - b*x*Sin[a]*SinIntegral[b*x])/(a*x)

Maple [A] time = 0.057, size = 49, normalized size = 1.

$$b \left(-\frac{\text{Ci}(bx+a)}{bx} - \frac{\text{Ci}(bx+a)}{a} + \frac{-\text{Si}(bx) \sin(a) + \text{Ci}(bx) \cos(a)}{a} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x+a)/x^2,x)

[Out] b*(-Ci(b*x+a)/b/x-1/a*Ci(b*x+a)+1/a*(-Si(b*x)*sin(a)+Ci(b*x)*cos(a)))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx+a)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)/x^2,x, algorithm="maxima")

[Out] integrate(Ci(b*x + a)/x^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bx+a)}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x+a)/x^2,x, algorithm="fricas")
```

```
[Out] integral(cos_integral(b*x + a)/x^2, x)
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{Ci}(a + bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x+a)/x**2,x)
```

```
[Out] Integral(Ci(a + b*x)/x**2, x)
```

Giac [C] time = 1.22721, size = 201, normalized size = 4.28

$$\left(\Re(\operatorname{Ci}(bx + a)) \tan\left(\frac{1}{2}a\right)^2 + \Re(\operatorname{Ci}(bx)) \tan\left(\frac{1}{2}a\right)^2 + \Re(\operatorname{Ci}(-bx - a)) \tan\left(\frac{1}{2}a\right)^2 + \Re(\operatorname{Ci}(-bx)) \tan\left(\frac{1}{2}a\right)^2 + 2 \Im(\operatorname{Ci}(bx + a)) \tan\left(\frac{1}{2}a\right) \right) / x^2$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x+a)/x^2,x, algorithm="giac")
```

```
[Out] -1/2*(real_part(cos_integral(b*x + a))*tan(1/2*a)^2 + real_part(cos_integra
l(b*x))*tan(1/2*a)^2 + real_part(cos_integral(-b*x - a))*tan(1/2*a)^2 + rea
l_part(cos_integral(-b*x))*tan(1/2*a)^2 + 2*imag_part(cos_integral(b*x))*ta
n(1/2*a) - 2*imag_part(cos_integral(-b*x))*tan(1/2*a) + 4*sin_integral(b*x)
*tan(1/2*a) + real_part(cos_integral(b*x + a)) - real_part(cos_integral(b*x
)) + real_part(cos_integral(-b*x - a)) - real_part(cos_integral(-b*x)))*b/(
a*tan(1/2*a)^2 + a) - cos_integral(b*x + a)/x
```

3.92 $\int \frac{\text{CosIntegral}(a+bx)}{x^3} dx$

Optimal. Leaf size=111

$$\frac{b^2 \text{CosIntegral}(a+bx)}{2a^2} - \frac{b^2 \cos(a) \text{CosIntegral}(bx)}{2a^2} + \frac{b^2 \sin(a) \text{Si}(bx)}{2a^2} - \frac{b^2 \sin(a) \text{CosIntegral}(bx)}{2a} - \frac{b^2 \cos(a) \text{Si}(bx)}{2a}$$

[Out] $-(b \cdot \text{Cos}[a + b \cdot x]) / (2 \cdot a \cdot x) - (b^2 \cdot \text{Cos}[a] \cdot \text{CosIntegral}[b \cdot x]) / (2 \cdot a^2) + (b^2 \cdot \text{CosIntegral}[a + b \cdot x]) / (2 \cdot a^2) - \text{CosIntegral}[a + b \cdot x] / (2 \cdot x^2) - (b^2 \cdot \text{CosIntegral}[b \cdot x] \cdot \text{Sin}[a]) / (2 \cdot a) - (b^2 \cdot \text{Cos}[a] \cdot \text{SinIntegral}[b \cdot x]) / (2 \cdot a) + (b^2 \cdot \text{Sin}[a] \cdot \text{SinIntegral}[b \cdot x]) / (2 \cdot a^2)$

Rubi [A] time = 0.326721, antiderivative size = 111, normalized size of antiderivative = 1., number of steps used = 11, number of rules used = 6, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.6$, Rules used = {6504, 6742, 3297, 3303, 3299, 3302}

$$\frac{b^2 \text{CosIntegral}(a+bx)}{2a^2} - \frac{b^2 \cos(a) \text{CosIntegral}(bx)}{2a^2} + \frac{b^2 \sin(a) \text{Si}(bx)}{2a^2} - \frac{b^2 \sin(a) \text{CosIntegral}(bx)}{2a} - \frac{b^2 \cos(a) \text{Si}(bx)}{2a}$$

Antiderivative was successfully verified.

[In] Int[CosIntegral[a + b*x]/x^3, x]

[Out] $-(b \cdot \text{Cos}[a + b \cdot x]) / (2 \cdot a \cdot x) - (b^2 \cdot \text{Cos}[a] \cdot \text{CosIntegral}[b \cdot x]) / (2 \cdot a^2) + (b^2 \cdot \text{CosIntegral}[a + b \cdot x]) / (2 \cdot a^2) - \text{CosIntegral}[a + b \cdot x] / (2 \cdot x^2) - (b^2 \cdot \text{CosIntegral}[b \cdot x] \cdot \text{Sin}[a]) / (2 \cdot a) - (b^2 \cdot \text{Cos}[a] \cdot \text{SinIntegral}[b \cdot x]) / (2 \cdot a) + (b^2 \cdot \text{Sin}[a] \cdot \text{SinIntegral}[b \cdot x]) / (2 \cdot a^2)$

Rule 6504

Int[CosIntegral[(a_.) + (b_.)*(x_)]*((c_.) + (d_.)*(x_))^(m_.), x_Symbol] :> Simp[((c + d*x)^(m + 1)*CosIntegral[a + b*x]) / (d*(m + 1)), x] - Dist[b / (d*(m + 1)), Int[((c + d*x)^(m + 1)*Cos[a + b*x]) / (a + b*x), x], x] /; FreeQ[{a, b, c, d, m}, x] && NeQ[m, -1]

Rule 6742

Int[u_, x_Symbol] :> With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]]

Rule 3297

Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)], x_Symbol] :> Simp[((c + d*x)^(m + 1)*Sin[e + f*x]) / (d*(m + 1)), x] - Dist[f / (d*(m + 1)), Int[(c + d*x)^(m + 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && LtQ[m, -1]

Rule 3303

Int[sin[(e_.) + (f_.)*(x_)] / ((c_.) + (d_.)*(x_)), x_Symbol] :> Dist[Cos[(d*e - c*f) / d], Int[Sin[(c*f) / d + f*x] / (c + d*x), x], x] + Dist[Sin[(d*e - c*f) / d], Int[Cos[(c*f) / d + f*x] / (c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int \frac{\text{Ci}(a+bx)}{x^3} dx &= -\frac{\text{Ci}(a+bx)}{2x^2} + \frac{1}{2}b \int \frac{\cos(a+bx)}{x^2(a+bx)} dx \\
&= -\frac{\text{Ci}(a+bx)}{2x^2} + \frac{1}{2}b \int \left(\frac{\cos(a+bx)}{ax^2} - \frac{b \cos(a+bx)}{a^2x} + \frac{b^2 \cos(a+bx)}{a^2(a+bx)} \right) dx \\
&= -\frac{\text{Ci}(a+bx)}{2x^2} + \frac{b \int \frac{\cos(a+bx)}{x^2} dx}{2a} - \frac{b^2 \int \frac{\cos(a+bx)}{x} dx}{2a^2} + \frac{b^3 \int \frac{\cos(a+bx)}{a+bx} dx}{2a^2} \\
&= -\frac{b \cos(a+bx)}{2ax} + \frac{b^2 \text{Ci}(a+bx)}{2a^2} - \frac{\text{Ci}(a+bx)}{2x^2} - \frac{b^2 \int \frac{\sin(a+bx)}{x} dx}{2a} - \frac{(b^2 \cos(a)) \int \frac{\cos(bx)}{x} dx}{2a^2} + \frac{(b^2 \sin(a)) \int \frac{\sin(bx)}{x} dx}{2a^2} \\
&= -\frac{b \cos(a+bx)}{2ax} - \frac{b^2 \cos(a) \text{Ci}(bx)}{2a^2} + \frac{b^2 \text{Ci}(a+bx)}{2a^2} - \frac{\text{Ci}(a+bx)}{2x^2} + \frac{b^2 \sin(a) \text{Si}(bx)}{2a^2} - \frac{(b^2 \cos(a)) \int \frac{\cos(bx)}{x} dx}{2a} \\
&= -\frac{b \cos(a+bx)}{2ax} - \frac{b^2 \cos(a) \text{Ci}(bx)}{2a^2} + \frac{b^2 \text{Ci}(a+bx)}{2a^2} - \frac{\text{Ci}(a+bx)}{2x^2} - \frac{b^2 \text{Ci}(bx) \sin(a)}{2a} - \frac{b^2 \cos(a) \text{Si}(bx)}{2a}
\end{aligned}$$

Mathematica [A] time = 0.398744, size = 76, normalized size = 0.68

$$\frac{(a^2 - b^2x^2) \text{CosIntegral}(a+bx) + b^2x^2(a \sin(a) + \cos(a)) \text{CosIntegral}(bx) + bx(bx(a \cos(a) - \sin(a))) \text{Si}(bx) + a \cos(a) \text{Si}(bx)}{2a^2x^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[CosIntegral[a + b*x]/x^3, x]
```

```
[Out] -((a^2 - b^2*x^2)*CosIntegral[a + b*x] + b^2*x^2*CosIntegral[b*x]*(Cos[a] +
a*Sin[a]) + b*x*(a*Cos[a + b*x] + b*x*(a*Cos[a] - Sin[a])*SinIntegral[b*x]
))/ (2*a^2*x^2)
```

Maple [A] time = 0.056, size = 88, normalized size = 0.8

$$b^2 \left(-\frac{\text{Ci}(bx+a)}{2b^2x^2} + \frac{\text{Ci}(bx+a)}{2a^2} + \frac{1}{2a} \left(-\frac{\cos(bx+a)}{bx} - \text{Si}(bx) \cos(a) - \text{Ci}(bx) \sin(a) \right) - \frac{-\text{Si}(bx) \sin(a) + \text{Ci}(bx) \cos(a)}{2a^2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(Ci(b*x+a)/x^3, x)
```

```
[Out] b^2*(-1/2*Ci(b*x+a)/b^2/x^2+1/2/a^2*Ci(b*x+a)+1/2/a*(-cos(b*x+a)/b/x-Si(b*x)
)*cos(a)-Ci(b*x)*sin(a))-1/2/a^2*(-Si(b*x)*sin(a)+Ci(b*x)*cos(a))
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx + a)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)/x^3,x, algorithm="maxima")

[Out] integrate(Ci(b*x + a)/x^3, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bx + a)}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)/x^3,x, algorithm="fricas")

[Out] integral(cos_integral(b*x + a)/x^3, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(a + bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)/x**3,x)

[Out] Integral(Ci(a + b*x)/x**3, x)

Giac [C] time = 1.23233, size = 1010, normalized size = 9.1

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)/x^3,x, algorithm="giac")

[Out] 1/4*(a*b*x*imag_part(cos_integral(b*x))*tan(1/2*b*x)^2*tan(1/2*a)^2 - a*b*x*imag_part(cos_integral(-b*x))*tan(1/2*b*x)^2*tan(1/2*a)^2 + 2*a*b*x*sin_integral(b*x)*tan(1/2*b*x)^2*tan(1/2*a)^2 - 2*a*b*x*real_part(cos_integral(b*x))*tan(1/2*b*x)^2*tan(1/2*a) - 2*a*b*x*real_part(cos_integral(-b*x))*tan(1/2*b*x)^2*tan(1/2*a) + b*x*real_part(cos_integral(b*x + a))*tan(1/2*b*x)^2*tan(1/2*a)^2 + b*x*real_part(cos_integral(b*x))*tan(1/2*b*x)^2*tan(1/2*a)^2 + b*x*real_part(cos_integral(-b*x - a))*tan(1/2*b*x)^2*tan(1/2*a)^2 + b*x*real_part(cos_integral(-b*x))*tan(1/2*b*x)^2*tan(1/2*a)^2 - a*b*x*imag_part(cos_integral(b*x))*tan(1/2*b*x)^2 + a*b*x*imag_part(cos_integral(-b*x))*tan(1/2*b*x)^2 - 2*a*b*x*sin_integral(b*x)*tan(1/2*b*x)^2 + 2*b*x*imag_part(cos_integral(b*x))*tan(1/2*b*x)^2*tan(1/2*a) - 2*b*x*imag_part(cos_integral(-b*x))*tan(1/2*b*x)^2*tan(1/2*a) + 2*b*x*real_part(cos_integral(b*x))*tan(1/2*b*x)^2*tan(1/2*a) - 2*b*x*real_part(cos_integral(-b*x))*tan(1/2*b*x)^2*tan(1/2*a)

$$\begin{aligned}
& -b*x)) * \tan(1/2*b*x)^2 * \tan(1/2*a) + 4*b*x * \sin_integral(b*x) * \tan(1/2*b*x)^2 * \\
& \tan(1/2*a) + a*b*x * \operatorname{imag_part}(\cos_integral(b*x)) * \tan(1/2*a)^2 - a*b*x * \operatorname{imag_part} \\
& \operatorname{part}(\cos_integral(-b*x)) * \tan(1/2*a)^2 + 2*a*b*x * \sin_integral(b*x) * \tan(1/2*a)^2 \\
& + b*x * \operatorname{real_part}(\cos_integral(b*x + a)) * \tan(1/2*b*x)^2 - b*x * \operatorname{real_part}(\cos \\
& _integral(b*x)) * \tan(1/2*b*x)^2 + b*x * \operatorname{real_part}(\cos_integral(-b*x - a)) * \tan(\\
& 1/2*b*x)^2 - b*x * \operatorname{real_part}(\cos_integral(-b*x)) * \tan(1/2*b*x)^2 - 2*a*b*x * \operatorname{rea} \\
& \operatorname{l_part}(\cos_integral(b*x)) * \tan(1/2*a) - 2*a*b*x * \operatorname{real_part}(\cos_integral(-b*x) \\
&) * \tan(1/2*a) + b*x * \operatorname{real_part}(\cos_integral(b*x + a)) * \tan(1/2*a)^2 + b*x * \operatorname{real} \\
& _part(\cos_integral(b*x)) * \tan(1/2*a)^2 + b*x * \operatorname{real_part}(\cos_integral(-b*x - a \\
&)) * \tan(1/2*a)^2 + b*x * \operatorname{real_part}(\cos_integral(-b*x)) * \tan(1/2*a)^2 - 2*a * \tan(\\
& 1/2*b*x)^2 * \tan(1/2*a)^2 - a*b*x * \operatorname{imag_part}(\cos_integral(b*x)) + a*b*x * \operatorname{imag_p} \\
& \operatorname{art}(\cos_integral(-b*x)) - 2*a*b*x * \sin_integral(b*x) + 2*b*x * \operatorname{imag_part}(\cos_i \\
& \operatorname{ntegral}(b*x)) * \tan(1/2*a) - 2*b*x * \operatorname{imag_part}(\cos_integral(-b*x)) * \tan(1/2*a) + \\
& 4*b*x * \sin_integral(b*x) * \tan(1/2*a) + b*x * \operatorname{real_part}(\cos_integral(b*x + a)) \\
& - b*x * \operatorname{real_part}(\cos_integral(b*x)) + b*x * \operatorname{real_part}(\cos_integral(-b*x - a)) \\
& - b*x * \operatorname{real_part}(\cos_integral(-b*x)) + 2*a * \tan(1/2*b*x)^2 + 8*a * \tan(1/2*b*x) \\
& * \tan(1/2*a) + 2*a * \tan(1/2*a)^2 - 2*a) * b / (a^2 * x * \tan(1/2*b*x)^2 * \tan(1/2*a)^2 \\
& + a^2 * x * \tan(1/2*b*x)^2 + a^2 * x * \tan(1/2*a)^2 + a^2 * x) - 1/2 * \cos_integral(b*x \\
& + a) / x^2
\end{aligned}$$

3.93 $\int x^m \text{CosIntegral}(a + bx)^2 dx$

Optimal. Leaf size=14

CannotIntegrate($x^m \text{CosIntegral}(a + bx)^2, x$)

[Out] CannotIntegrate[x^m*CosIntegral[a + b*x]², x]

Rubi [A] time = 0.0424156, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int x^m \text{CosIntegral}(a + bx)^2 dx$$

Verification is Not applicable to the result.

[In] Int[x^m*CosIntegral[a + b*x]²,x]

[Out] Defer[Int][x^m*CosIntegral[a + b*x]², x]

Rubi steps

$$\int x^m \text{Ci}(a + bx)^2 dx = \int x^m \text{Ci}(a + bx)^2 dx$$

Mathematica [A] time = 5.27344, size = 0, normalized size = 0.

$$\int x^m \text{CosIntegral}(a + bx)^2 dx$$

Verification is Not applicable to the result.

[In] Integrate[x^m*CosIntegral[a + b*x]²,x]

[Out] Integrate[x^m*CosIntegral[a + b*x]², x]

Maple [A] time = 0.142, size = 0, normalized size = 0.

$$\int x^m (\text{Ci}(bx + a))^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^m*Ci(b*x+a)²,x)

[Out] int(x^m*Ci(b*x+a)²,x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \text{Ci}(bx + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^m*Ci(b*x+a)^2,x, algorithm="maxima")
```

```
[Out] integrate(x^m*Ci(b*x + a)^2, x)
```

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^m \text{Ci}(bx + a)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^m*Ci(b*x+a)^2,x, algorithm="fricas")
```

```
[Out] integral(x^m*cos_integral(b*x + a)^2, x)
```

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \text{Ci}^2(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**m*Ci(b*x+a)**2,x)
```

```
[Out] Integral(x**m*Ci(a + b*x)**2, x)
```

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int x^m \text{Ci}(bx + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^m*Ci(b*x+a)^2,x, algorithm="giac")
```

```
[Out] integrate(x^m*Ci(b*x + a)^2, x)
```

3.94 $\int x^2 \text{CosIntegral}(a + bx)^2 dx$

Optimal. Leaf size=329

$$\frac{a^2(a + bx)\text{CosIntegral}(a + bx)^2}{3b^3} - \frac{2a^2\text{CosIntegral}(a + bx)\sin(a + bx)}{3b^3} + \frac{a^2\text{Si}(2a + 2bx)}{b^3} - \frac{ax(a + bx)\text{CosIntegral}(a + bx)}{3b^2}$$

```
[Out] (2*x)/(3*b^2) + (a*cos[2*a + 2*b*x])/(3*b^3) - (x*cos[2*a + 2*b*x])/(6*b^2)
+ (2*a*cos[a + b*x]*cosIntegral[a + b*x])/(3*b^3) - (4*x*cos[a + b*x]*cosIntegral[a + b*x])/(3*b^2)
+ (a^2*(a + b*x)*cosIntegral[a + b*x]^2)/(3*b^3) - (a*x*(a + b*x)*cosIntegral[a + b*x]^2)/(3*b^2)
+ (x^2*(a + b*x)*cosIntegral[a + b*x]^2)/(3*b) - (a*cosIntegral[2*a + 2*b*x])/b^3 - (a*log[a + b*x])/b^3
+ (2*cos[a + b*x]*sin[a + b*x])/(3*b^3) + (4*cosIntegral[a + b*x]*sin[a + b*x])/(3*b^3) - (2*a^2*cosIntegral[a + b*x]*sin[a + b*x])/(3*b^3)
+ (2*a*x*cosIntegral[a + b*x]*sin[a + b*x])/(3*b^2) - (2*x^2*cosIntegral[a + b*x]*sin[a + b*x])/(3*b)
+ sin[2*a + 2*b*x]/(12*b^3) - (2*sinIntegral[2*a + 2*b*x])/(3*b^3) + (a^2*sinIntegral[2*a + 2*b*x])/b^3
```

Rubi [A] time = 1.32241, antiderivative size = 329, normalized size of antiderivative = 1., number of steps used = 39, number of rules used = 19, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 1.583$, Rules used = {6510, 6514, 4573, 6741, 6742, 2638, 3296, 2637, 3299, 6520, 2635, 8, 3312, 3302, 6512, 4406, 12, 6518, 6506}

$$\frac{a^2(a + bx)\text{CosIntegral}(a + bx)^2}{3b^3} - \frac{2a^2\text{CosIntegral}(a + bx)\sin(a + bx)}{3b^3} + \frac{a^2\text{Si}(2a + 2bx)}{b^3} - \frac{ax(a + bx)\text{CosIntegral}(a + bx)}{3b^2}$$

Antiderivative was successfully verified.

```
[In] Int[x^2*cosIntegral[a + b*x]^2,x]
```

```
[Out] (2*x)/(3*b^2) + (a*cos[2*a + 2*b*x])/(3*b^3) - (x*cos[2*a + 2*b*x])/(6*b^2)
+ (2*a*cos[a + b*x]*cosIntegral[a + b*x])/(3*b^3) - (4*x*cos[a + b*x]*cosIntegral[a + b*x])/(3*b^2)
+ (a^2*(a + b*x)*cosIntegral[a + b*x]^2)/(3*b^3) - (a*x*(a + b*x)*cosIntegral[a + b*x]^2)/(3*b^2)
+ (x^2*(a + b*x)*cosIntegral[a + b*x]^2)/(3*b) - (a*cosIntegral[2*a + 2*b*x])/b^3 - (a*log[a + b*x])/b^3
+ (2*cos[a + b*x]*sin[a + b*x])/(3*b^3) + (4*cosIntegral[a + b*x]*sin[a + b*x])/(3*b^3) - (2*a^2*cosIntegral[a + b*x]*sin[a + b*x])/(3*b^3)
+ (2*a*x*cosIntegral[a + b*x]*sin[a + b*x])/(3*b^2) - (2*x^2*cosIntegral[a + b*x]*sin[a + b*x])/(3*b)
+ sin[2*a + 2*b*x]/(12*b^3) - (2*sinIntegral[2*a + 2*b*x])/(3*b^3) + (a^2*sinIntegral[2*a + 2*b*x])/b^3
```

Rule 6510

```
Int[CosIntegral[(a_) + (b_)*(x_)]^2*((c_) + (d_)*(x_))^(m_), x_Symbol]
:> Simp[((a + b*x)*(c + d*x)^m*cosIntegral[a + b*x]^2)/(b*(m + 1)), x] + (-Dist[2/(m + 1), Int[(c + d*x)^m*cos[a + b*x]*cosIntegral[a + b*x], x], x] + Dist[((b*c - a*d)*m)/(b*(m + 1)), Int[(c + d*x)^(m - 1)*cosIntegral[a + b*x]^2, x], x]) /; FreeQ[{a, b, c, d}, x] && IGtQ[m, 0]
```

Rule 6514

```
Int[Cos[(a_) + (b_)*(x_)]*cosIntegral[(c_) + (d_)*(x_)]*((e_) + (f_)*(x_))^(m_), x_Symbol]
:> Simp[((e + f*x)^m*sin[a + b*x]*cosIntegral[c + d*x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*sin[a + b*x]*cos[c + d*x])/(c + d*x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*sin[a + b*x]*cosIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```


Rule 4573

$\text{Int}[\text{Cos}[w_]^{(p_)} * (u_) * \text{Sin}[v_]^{(p_)}, x_ \text{Symbol}] \text{ :> Dist}[1/2^p, \text{Int}[u * \text{Sin}[2 * v]^p, x], x] \text{ /; EqQ}[w, v] \ \&\& \ \text{IntegerQ}[p]$

Rule 6741

$\text{Int}[u_ , x_ \text{Symbol}] \text{ :> With}[\{v = \text{NormalizeIntegrand}[u, x]\}, \text{Int}[v, x] \text{ /; } v \neq u]$

Rule 6742

$\text{Int}[u_ , x_ \text{Symbol}] \text{ :> With}[\{v = \text{ExpandIntegrand}[u, x]\}, \text{Int}[v, x] \text{ /; SumQ}[v]$

Rule 2638

$\text{Int}[\text{sin}[(c_) + (d_) * (x_)], x_ \text{Symbol}] \text{ :> -Simp}[\text{Cos}[c + d * x] / d, x] \text{ /; FreeQ}[\{c, d\}, x]$

Rule 3296

$\text{Int}[((c_) + (d_) * (x_))^{(m_)} * \text{sin}[(e_) + (f_) * (x_)], x_ \text{Symbol}] \text{ :> -Simp}[\text{((c + d * x)}^m * \text{Cos}[e + f * x]) / f, x] + \text{Dist}[(d * m) / f, \text{Int}[(c + d * x)^{(m - 1)} * \text{Cos}[e + f * x], x], x] \text{ /; FreeQ}[\{c, d, e, f\}, x] \ \&\& \ \text{GtQ}[m, 0]$

Rule 2637

$\text{Int}[\text{sin}[\text{Pi}/2 + (c_) + (d_) * (x_)], x_ \text{Symbol}] \text{ :> Simp}[\text{Sin}[c + d * x] / d, x] \text{ /; FreeQ}[\{c, d\}, x]$

Rule 3299

$\text{Int}[\text{sin}[(e_) + (f_) * (x_)] / ((c_) + (d_) * (x_)), x_ \text{Symbol}] \text{ :> Simp}[\text{SinIntegral}[e + f * x] / d, x] \text{ /; FreeQ}[\{c, d, e, f\}, x] \ \&\& \ \text{EqQ}[d * e - c * f, 0]$

Rule 6520

$\text{Int}[\text{CosIntegral}[(c_) + (d_) * (x_)] * ((e_) + (f_) * (x_))^{(m_)} * \text{Sin}[(a_) + (b_) * (x_)], x_ \text{Symbol}] \text{ :> -Simp}[\text{((e + f * x)}^m * \text{Cos}[a + b * x] * \text{CosIntegral}[c + d * x]) / b, x] + (\text{Dist}[d / b, \text{Int}[\text{((e + f * x)}^m * \text{Cos}[a + b * x] * \text{Cos}[c + d * x]) / (c + d * x), x], x] + \text{Dist}[(f * m) / b, \text{Int}[(e + f * x)^{(m - 1)} * \text{Cos}[a + b * x] * \text{CosIntegral}[c + d * x], x], x]) \text{ /; FreeQ}[\{a, b, c, d, e, f\}, x] \ \&\& \ \text{IGtQ}[m, 0]$

Rule 2635

$\text{Int}[((b_) * \text{sin}[(c_) + (d_) * (x_)])^{(n_)}, x_ \text{Symbol}] \text{ :> -Simp}[(b * \text{Cos}[c + d * x] * (b * \text{Sin}[c + d * x])^{(n - 1)}) / (d * n), x] + \text{Dist}[(b^2 * (n - 1)) / n, \text{Int}[(b * \text{Sin}[c + d * x])^{(n - 2)}, x], x] \text{ /; FreeQ}[\{b, c, d\}, x] \ \&\& \ \text{GtQ}[n, 1] \ \&\& \ \text{IntegerQ}[2 * n]$

Rule 8

$\text{Int}[a_ , x_ \text{Symbol}] \text{ :> Simp}[a * x, x] \text{ /; FreeQ}[a, x]$

Rule 3312

$\text{Int}[((c_) + (d_) * (x_))^{(m_)} * \text{sin}[(e_) + (f_) * (x_)]^{(n_)}, x_ \text{Symbol}] \text{ :> Int}[\text{ExpandTrigReduce}[(c + d * x)^m, \text{Sin}[e + f * x]^n, x], x] \text{ /; FreeQ}[\{c, d, e, f$

, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rule 6512

Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :> Simp[(Sin[a + b*x]*CosIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] :> Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 6518

Int[CosIntegral[(c_.) + (d_.)*(x_)]*Sin[(a_.) + (b_.)*(x_)], x_Symbol] :> -Simp[(Cos[a + b*x]*CosIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 6506

Int[CosIntegral[(a_.) + (b_.)*(x_)]^2, x_Symbol] :> Simp[((a + b*x)*CosIntegral[a + b*x]^2)/b, x] - Dist[2, Int[Cos[a + b*x]*CosIntegral[a + b*x], x], x] /; FreeQ[{a, b}, x]

Rubi steps

$$\begin{aligned}
\int x^2 \text{Ci}(a+bx)^2 dx &= \frac{x^2(a+bx)\text{Ci}(a+bx)^2}{3b} - \frac{2}{3} \int x^2 \cos(a+bx)\text{Ci}(a+bx) dx - \frac{(2a) \int x\text{Ci}(a+bx)^2 dx}{3b} \\
&= -\frac{ax(a+bx)\text{Ci}(a+bx)^2}{3b^2} + \frac{x^2(a+bx)\text{Ci}(a+bx)^2}{3b} - \frac{2x^2\text{Ci}(a+bx)\sin(a+bx)}{3b} + \frac{2}{3} \int \frac{x^2 \cos(a+bx)\text{Ci}(a+bx)}{3b} dx \\
&= -\frac{4x \cos(a+bx)\text{Ci}(a+bx)}{3b^2} + \frac{a^2(a+bx)\text{Ci}(a+bx)^2}{3b^3} - \frac{ax(a+bx)\text{Ci}(a+bx)^2}{3b^2} + \frac{x^2(a+bx)\text{Ci}(a+bx)}{3b} \\
&= \frac{2a \cos(a+bx)\text{Ci}(a+bx)}{3b^3} - \frac{4x \cos(a+bx)\text{Ci}(a+bx)}{3b^2} + \frac{a^2(a+bx)\text{Ci}(a+bx)^2}{3b^3} - \frac{ax(a+bx)\text{Ci}(a+bx)^2}{3b^2} \\
&= \frac{2a \cos(a+bx)\text{Ci}(a+bx)}{3b^3} - \frac{4x \cos(a+bx)\text{Ci}(a+bx)}{3b^2} + \frac{a^2(a+bx)\text{Ci}(a+bx)^2}{3b^3} - \frac{ax(a+bx)\text{Ci}(a+bx)^2}{3b^2} \\
&= \frac{2a \cos(a+bx)\text{Ci}(a+bx)}{3b^3} - \frac{4x \cos(a+bx)\text{Ci}(a+bx)}{3b^2} + \frac{a^2(a+bx)\text{Ci}(a+bx)^2}{3b^3} - \frac{ax(a+bx)\text{Ci}(a+bx)^2}{3b^2} \\
&= \frac{2x}{3b^2} + \frac{a \cos(2a+2bx)}{6b^3} - \frac{x \cos(2a+2bx)}{6b^2} + \frac{2a \cos(a+bx)\text{Ci}(a+bx)}{3b^3} - \frac{4x \cos(a+bx)\text{Ci}(a+bx)}{3b^2} \\
&= \frac{2x}{3b^2} + \frac{a \cos(2a+2bx)}{3b^3} - \frac{x \cos(2a+2bx)}{6b^2} + \frac{2a \cos(a+bx)\text{Ci}(a+bx)}{3b^3} - \frac{4x \cos(a+bx)\text{Ci}(a+bx)}{3b^2}
\end{aligned}$$

Mathematica [A] time = 1.21594, size = 159, normalized size = 0.48

$$4(a^3 + b^3 x^3) \text{CosIntegral}(a+bx)^2 - 8 \text{CosIntegral}(a+bx) \left((a^2 - abx + b^2 x^2 - 2) \sin(a+bx) - (a - 2bx) \cos(a+bx) \right)$$

Antiderivative was successfully verified.

[In] Integrate[x^2*CosIntegral[a + b*x]^2,x]

[Out] (8*a + 8*b*x + 4*a*cos[2*(a + b*x)] - 2*b*x*cos[2*(a + b*x)] + 4*(a^3 + b^3*x^3)*CosIntegral[a + b*x]^2 - 12*a*cosIntegral[2*(a + b*x)] - 12*a*Log[a + b*x] - 8*cosIntegral[a + b*x]*(-(a - 2*b*x)*Cos[a + b*x]) + (-2 + a^2 - a*b*x + b^2*x^2)*Sin[a + b*x]) + 5*Sin[2*(a + b*x)] - 8*SinIntegral[2*(a + b*x)] + 12*a^2*SinIntegral[2*(a + b*x)]/(12*b^3)

Maple [F] time = 0.053, size = 0, normalized size = 0.

$$\int x^2 (\text{Ci}(bx+a))^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*Ci(b*x+a)^2,x)

[Out] int(x^2*Ci(b*x+a)^2,x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Ci}(bx+a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x+a)^2,x, algorithm="maxima")

[Out] integrate(x^2*Ci(b*x + a)^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^2 \text{Ci}(bx + a)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x+a)^2,x, algorithm="fricas")

[Out] integral(x^2*cos_integral(b*x + a)^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Ci}^2(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*Ci(b*x+a)**2,x)

[Out] Integral(x**2*Ci(a + b*x)**2, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Ci}(bx + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x+a)^2,x, algorithm="giac")

[Out] integrate(x^2*Ci(b*x + a)^2, x)

3.95 $\int x \text{CosIntegral}(a + bx)^2 dx$

Optimal. Leaf size=155

$$-\frac{a(a+bx)\text{CosIntegral}(a+bx)^2}{2b^2} + \frac{\text{CosIntegral}(2a+2bx)}{2b^2} + \frac{a\text{CosIntegral}(a+bx)\sin(a+bx)}{b^2} - \frac{\text{CosIntegral}(a+bx)}{b}$$

```
[Out] -Cos[2*a + 2*b*x]/(4*b^2) - (Cos[a + b*x]*CosIntegral[a + b*x])/b^2 - (a*(a
+ b*x)*CosIntegral[a + b*x]^2)/(2*b^2) + (x*(a + b*x)*CosIntegral[a + b*x]
^2)/(2*b) + CosIntegral[2*a + 2*b*x]/(2*b^2) + Log[a + b*x]/(2*b^2) + (a*Co
sIntegral[a + b*x]*Sin[a + b*x])/b^2 - (x*CosIntegral[a + b*x]*Sin[a + b*x]
)/b - (a*SinIntegral[2*a + 2*b*x])/b^2
```

Rubi [A] time = 0.337556, antiderivative size = 155, normalized size of antiderivative = 1., number of steps used = 17, number of rules used = 14, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 1.4$, Rules used = {6510, 6514, 4573, 6741, 6742, 2638, 3299, 6518, 3312, 3302, 6506, 6512, 4406, 12}

$$-\frac{a(a+bx)\text{CosIntegral}(a+bx)^2}{2b^2} + \frac{\text{CosIntegral}(2a+2bx)}{2b^2} + \frac{a\text{CosIntegral}(a+bx)\sin(a+bx)}{b^2} - \frac{\text{CosIntegral}(a+bx)}{b}$$

Antiderivative was successfully verified.

```
[In] Int[x*CosIntegral[a + b*x]^2,x]
```

```
[Out] -Cos[2*a + 2*b*x]/(4*b^2) - (Cos[a + b*x]*CosIntegral[a + b*x])/b^2 - (a*(a
+ b*x)*CosIntegral[a + b*x]^2)/(2*b^2) + (x*(a + b*x)*CosIntegral[a + b*x]
^2)/(2*b) + CosIntegral[2*a + 2*b*x]/(2*b^2) + Log[a + b*x]/(2*b^2) + (a*Co
sIntegral[a + b*x]*Sin[a + b*x])/b^2 - (x*CosIntegral[a + b*x]*Sin[a + b*x]
)/b - (a*SinIntegral[2*a + 2*b*x])/b^2
```

Rule 6510

```
Int[CosIntegral[(a_) + (b_.)*(x_)]^2*((c_.) + (d_.)*(x_))^(m_.), x_Symbol]
:> Simp[((a + b*x)*(c + d*x)^m*CosIntegral[a + b*x]^2)/(b*(m + 1)), x] + (-
Dist[2/(m + 1), Int[(c + d*x)^m*Cos[a + b*x]*CosIntegral[a + b*x], x], x] +
Dist[((b*c - a*d)*m)/(b*(m + 1)), Int[(c + d*x)^(m - 1)*CosIntegral[a + b*
x]^2, x], x]) /; FreeQ[{a, b, c, d}, x] && IGtQ[m, 0]
```

Rule 6514

```
Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*
(x_))^(m_.), x_Symbol] :> Simp[((e + f*x)^m*Sin[a + b*x]*CosIntegral[c + d*
x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*Sin[a + b*x]*Cos[c + d*x])/(c + d*
x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Sin[a + b*x]*CosIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 4573

```
Int[Cos[w_]^(p_.)*(u_.)*Sin[v_]^(p_.), x_Symbol] :> Dist[1/2^p, Int[u*Sin[2
*v]^p, x], x] /; EqQ[w, v] && IntegerQ[p]
```

Rule 6741

```
Int[u_, x_Symbol] :> With[{v = NormalizeIntegrand[u, x]}, Int[v, x] /; v !=
= u]
```

Rule 6742

```
Int[u_, x_Symbol] :=> With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]
]
```

Rule 2638

```
Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] :=> -Simp[Cos[c + d*x]/d, x] /; FreeQ
[{c, d}, x]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :=> Simp[SinInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 6518

```
Int[CosIntegral[(c_.) + (d_.)*(x_)]*Sin[(a_.) + (b_.)*(x_)], x_Symbol] :=> -
Simp[(Cos[a + b*x]*CosIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]
]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 3312

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] :=> In
t[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f
, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :=> Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rule 6506

```
Int[CosIntegral[(a_.) + (b_.)*(x_)]^2, x_Symbol] :=> Simp[((a + b*x)*CosInte
gral[a + b*x]^2)/b, x] - Dist[2, Int[Cos[a + b*x]*CosIntegral[a + b*x], x],
x] /; FreeQ[{a, b}, x]
```

Rule 6512

```
Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :=> S
imp[(Sin[a + b*x]*CosIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]
)*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b
_.)*(x_)]^(n_.), x_Symbol] :=> Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]
]^(n)*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IG
tQ[p, 0]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :=> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !Match
Q[u, (b_)*(v_)] /; FreeQ[b, x]
```

Rubi steps

$$\begin{aligned}
\int x \operatorname{Ci}(a+bx)^2 dx &= \frac{x(a+bx)\operatorname{Ci}(a+bx)^2}{2b} - \frac{a \int \operatorname{Ci}(a+bx)^2 dx}{2b} - \int x \cos(a+bx)\operatorname{Ci}(a+bx) dx \\
&= -\frac{a(a+bx)\operatorname{Ci}(a+bx)^2}{2b^2} + \frac{x(a+bx)\operatorname{Ci}(a+bx)^2}{2b} - \frac{x\operatorname{Ci}(a+bx)\sin(a+bx)}{b} + \frac{\int \operatorname{Ci}(a+bx)\sin(a+bx) dx}{b} \\
&= -\frac{\cos(a+bx)\operatorname{Ci}(a+bx)}{b^2} - \frac{a(a+bx)\operatorname{Ci}(a+bx)^2}{2b^2} + \frac{x(a+bx)\operatorname{Ci}(a+bx)^2}{2b} + \frac{a\operatorname{Ci}(a+bx)\sin(a+bx)}{b^2} \\
&= -\frac{\cos(a+bx)\operatorname{Ci}(a+bx)}{b^2} - \frac{a(a+bx)\operatorname{Ci}(a+bx)^2}{2b^2} + \frac{x(a+bx)\operatorname{Ci}(a+bx)^2}{2b} + \frac{a\operatorname{Ci}(a+bx)\sin(a+bx)}{b^2} \\
&= -\frac{\cos(a+bx)\operatorname{Ci}(a+bx)}{b^2} - \frac{a(a+bx)\operatorname{Ci}(a+bx)^2}{2b^2} + \frac{x(a+bx)\operatorname{Ci}(a+bx)^2}{2b} + \frac{\log(a+bx)}{2b^2} + \frac{a\operatorname{Ci}(a+bx)\sin(a+bx)}{b^2} \\
&= -\frac{\cos(a+bx)\operatorname{Ci}(a+bx)}{b^2} - \frac{a(a+bx)\operatorname{Ci}(a+bx)^2}{2b^2} + \frac{x(a+bx)\operatorname{Ci}(a+bx)^2}{2b} + \frac{\operatorname{Ci}(2a+2bx)}{2b^2} + \frac{\log(a+bx)}{2b^2} \\
&= -\frac{\cos(2a+2bx)}{4b^2} - \frac{\cos(a+bx)\operatorname{Ci}(a+bx)}{b^2} - \frac{a(a+bx)\operatorname{Ci}(a+bx)^2}{2b^2} + \frac{x(a+bx)\operatorname{Ci}(a+bx)^2}{2b} + \frac{\operatorname{Ci}(2a+2bx)}{2b^2} + \frac{\log(a+bx)}{2b^2}
\end{aligned}$$

Mathematica [A] time = 0.327434, size = 96, normalized size = 0.62

$$\frac{2(a^2 - b^2x^2)\operatorname{CosIntegral}(a+bx)^2 - 2\operatorname{CosIntegral}(2(a+bx)) + 4\operatorname{CosIntegral}(a+bx)((bx-a)\sin(a+bx) + \cos(a+bx))}{4b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*CosIntegral[a + b*x]^2,x]

[Out] -(Cos[2*(a + b*x)] + 2*(a^2 - b^2*x^2)*CosIntegral[a + b*x]^2 - 2*CosIntegral[2*(a + b*x)] - 2*Log[a + b*x] + 4*CosIntegral[a + b*x]*(Cos[a + b*x] + (-a + b*x)*Sin[a + b*x])) + 4*a*SinIntegral[2*(a + b*x)]/(4*b^2)

Maple [A] time = 0.061, size = 136, normalized size = 0.9

$$\frac{x^2(\operatorname{Ci}(bx+a))^2}{2} - \frac{(\operatorname{Ci}(bx+a))^2 a^2}{2b^2} - \frac{x\operatorname{Ci}(bx+a)\sin(bx+a)}{b} + \frac{\operatorname{Ci}(bx+a)a\sin(bx+a)}{b^2} - \frac{\operatorname{Ci}(bx+a)\cos(bx+a)}{b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*Ci(b*x+a)^2,x)

[Out] 1/2*x^2*Ci(b*x+a)^2-1/2/b^2*Ci(b*x+a)^2*a^2-x*Ci(b*x+a)*sin(b*x+a)/b+a*Ci(b*x+a)*sin(b*x+a)/b^2-Ci(b*x+a)*cos(b*x+a)/b^2-1/2/b^2*cos(b*x+a)^2+1/2*ln(b*x+a)/b^2+1/2*Ci(2*b*x+2*a)/b^2-a*Si(2*b*x+2*a)/b^2

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \operatorname{Ci}(bx+a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x+a)^2,x, algorithm="maxima")

[Out] integrate(x*cos_integral(b*x + a)^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x \cos(bx + a)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*cos(b*x+a)^2,x, algorithm="fricas")

[Out] integral(x*cos_integral(b*x + a)^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \cos^2(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*cos(b*x+a)**2,x)

[Out] Integral(x*cos(a + b*x)**2, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int x \cos^2(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*cos(b*x+a)^2,x, algorithm="giac")

[Out] integrate(x*cos(b*x + a)^2, x)

3.96 $\int \text{CosIntegral}(a + bx)^2 dx$

Optimal. Leaf size=48

$$\frac{(a + bx)\text{CosIntegral}(a + bx)^2}{b} - \frac{2\text{CosIntegral}(a + bx)\sin(a + bx)}{b} + \frac{\text{Si}(2a + 2bx)}{b}$$

[Out] ((a + b*x)*CosIntegral[a + b*x]^2)/b - (2*CosIntegral[a + b*x]*Sin[a + b*x])/b + SinIntegral[2*a + 2*b*x]/b

Rubi [A] time = 0.0652635, antiderivative size = 48, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 5, integrand size = 8, $\frac{\text{number of rules}}{\text{integrand size}} = 0.625$, Rules used = {6506, 6512, 4406, 12, 3299}

$$\frac{(a + bx)\text{CosIntegral}(a + bx)^2}{b} - \frac{2\text{CosIntegral}(a + bx)\sin(a + bx)}{b} + \frac{\text{Si}(2a + 2bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[CosIntegral[a + b*x]^2,x]

[Out] ((a + b*x)*CosIntegral[a + b*x]^2)/b - (2*CosIntegral[a + b*x]*Sin[a + b*x])/b + SinIntegral[2*a + 2*b*x]/b

Rule 6506

Int[CosIntegral[(a_.) + (b_.)*(x_)]^2, x_Symbol] := Simp[((a + b*x)*CosIntegral[a + b*x]^2)/b, x] - Dist[2, Int[Cos[a + b*x]*CosIntegral[a + b*x], x], x] /; FreeQ[{a, b}, x]

Rule 6512

Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := Simp[(Sin[a + b*x]*CosIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_.)*(v_) /; FreeQ[b, x]]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned}
\int \text{Ci}(a+bx)^2 dx &= \frac{(a+bx)\text{Ci}(a+bx)^2}{b} - 2 \int \cos(a+bx)\text{Ci}(a+bx) dx \\
&= \frac{(a+bx)\text{Ci}(a+bx)^2}{b} - \frac{2\text{Ci}(a+bx)\sin(a+bx)}{b} + 2 \int \frac{\cos(a+bx)\sin(a+bx)}{a+bx} dx \\
&= \frac{(a+bx)\text{Ci}(a+bx)^2}{b} - \frac{2\text{Ci}(a+bx)\sin(a+bx)}{b} + 2 \int \frac{\sin(2a+2bx)}{2(a+bx)} dx \\
&= \frac{(a+bx)\text{Ci}(a+bx)^2}{b} - \frac{2\text{Ci}(a+bx)\sin(a+bx)}{b} + \int \frac{\sin(2a+2bx)}{a+bx} dx \\
&= \frac{(a+bx)\text{Ci}(a+bx)^2}{b} - \frac{2\text{Ci}(a+bx)\sin(a+bx)}{b} + \frac{\text{Si}(2a+2bx)}{b}
\end{aligned}$$

Mathematica [A] time = 0.0107419, size = 41, normalized size = 0.85

$$\frac{(a+bx)\text{CosIntegral}(a+bx)^2 - 2\text{CosIntegral}(a+bx)\sin(a+bx) + \text{Si}(2(a+bx))}{b}$$

Antiderivative was successfully verified.

[In] Integrate[CosIntegral[a + b*x]^2, x]

[Out] ((a + b*x)*CosIntegral[a + b*x]^2 - 2*CosIntegral[a + b*x]*Sin[a + b*x] + SinIntegral[2*(a + b*x)])/b

Maple [A] time = 0.046, size = 43, normalized size = 0.9

$$\frac{(bx+a)(\text{Ci}(bx+a))^2 - 2\text{Ci}(bx+a)\sin(bx+a) + \text{Si}(2bx+2a)}{b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x+a)^2, x)

[Out] 1/b*((b*x+a)*Ci(b*x+a)^2-2*Ci(b*x+a)*sin(b*x+a)+Si(2*b*x+2*a))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Ci}(bx+a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)^2, x, algorithm="maxima")

[Out] integrate(Ci(b*x + a)^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(\text{Ci}(bx+a)^2, x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x+a)^2,x, algorithm="fricas")
```

```
[Out] integral(cos_integral(b*x + a)^2, x)
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Ci}^2(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x+a)**2,x)
```

```
[Out] Integral(Ci(a + b*x)**2, x)
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Ci}(bx + a)^2 dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x+a)^2,x, algorithm="giac")
```

```
[Out] integrate(Ci(b*x + a)^2, x)
```

$$3.97 \quad \int \frac{\mathbf{CosIntegral}(a+bx)^2}{x} dx$$

Optimal. Leaf size=14

$$\text{CannotIntegrate}\left(\frac{\text{CosIntegral}(a+bx)^2}{x}, x\right)$$

[Out] CannotIntegrate[CosIntegral[a + b*x]^2/x, x]

Rubi [A] time = 0.0299319, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{CosIntegral}(a+bx)^2}{x} dx$$

Verification is Not applicable to the result.

[In] Int[CosIntegral[a + b*x]^2/x, x]

[Out] Defer[Int][CosIntegral[a + b*x]^2/x, x]

Rubi steps

$$\int \frac{\text{Ci}(a+bx)^2}{x} dx = \int \frac{\text{Ci}(a+bx)^2}{x} dx$$

Mathematica [A] time = 1.31549, size = 0, normalized size = 0.

$$\int \frac{\text{CosIntegral}(a+bx)^2}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[CosIntegral[a + b*x]^2/x, x]

[Out] Integrate[CosIntegral[a + b*x]^2/x, x]

Maple [A] time = 0.049, size = 0, normalized size = 0.

$$\int \frac{(\text{Ci}(bx+a))^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x+a)^2/x, x)

[Out] int(Ci(b*x+a)^2/x, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx + a)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)^2/x,x, algorithm="maxima")

[Out] integrate(Ci(b*x + a)^2/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bx + a)^2}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)^2/x,x, algorithm="fricas")

[Out] integral(cos_integral(b*x + a)^2/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}^2(a + bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)**2/x,x)

[Out] Integral(Ci(a + b*x)**2/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx + a)^2}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)^2/x,x, algorithm="giac")

[Out] integrate(Ci(b*x + a)^2/x, x)

$$3.98 \quad \int \frac{\text{CosIntegral}(a+bx)^2}{x^2} dx$$

Optimal. Leaf size=14

$$\text{CannotIntegrate}\left(\frac{\text{CosIntegral}(a+bx)^2}{x^2}, x\right)$$

[Out] CannotIntegrate[CosIntegral[a + b*x]^2/x^2, x]

Rubi [A] time = 0.0359025, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{CosIntegral}(a+bx)^2}{x^2} dx$$

Verification is Not applicable to the result.

[In] Int[CosIntegral[a + b*x]^2/x^2, x]

[Out] Defer[Int][CosIntegral[a + b*x]^2/x^2, x]

Rubi steps

$$\int \frac{\text{Ci}(a+bx)^2}{x^2} dx = \int \frac{\text{Ci}(a+bx)^2}{x^2} dx$$

Mathematica [A] time = 2.17928, size = 0, normalized size = 0.

$$\int \frac{\text{CosIntegral}(a+bx)^2}{x^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[CosIntegral[a + b*x]^2/x^2, x]

[Out] Integrate[CosIntegral[a + b*x]^2/x^2, x]

Maple [A] time = 0.059, size = 0, normalized size = 0.

$$\int \frac{(\text{Ci}(bx+a))^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x+a)^2/x^2, x)

[Out] int(Ci(b*x+a)^2/x^2, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx + a)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)^2/x^2,x, algorithm="maxima")

[Out] integrate(Ci(b*x + a)^2/x^2, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bx + a)^2}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)^2/x^2,x, algorithm="fricas")

[Out] integral(cos_integral(b*x + a)^2/x^2, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}^2(a + bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)**2/x**2,x)

[Out] Integral(Ci(a + b*x)**2/x**2, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx + a)^2}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)^2/x^2,x, algorithm="giac")

[Out] integrate(Ci(b*x + a)^2/x^2, x)

$$3.99 \quad \int \frac{\text{CosIntegral}(a+bx)^2}{x^3} dx$$

Optimal. Leaf size=14

$$\text{CannotIntegrate}\left(\frac{\text{CosIntegral}(a+bx)^2}{x^3}, x\right)$$

[Out] CannotIntegrate[CosIntegral[a + b*x]^2/x^3, x]

Rubi [A] time = 0.0347127, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{CosIntegral}(a+bx)^2}{x^3} dx$$

Verification is Not applicable to the result.

[In] Int[CosIntegral[a + b*x]^2/x^3, x]

[Out] Defer[Int][CosIntegral[a + b*x]^2/x^3, x]

Rubi steps

$$\int \frac{\text{Ci}(a+bx)^2}{x^3} dx = \int \frac{\text{Ci}(a+bx)^2}{x^3} dx$$

Mathematica [A] time = 2.52033, size = 0, normalized size = 0.

$$\int \frac{\text{CosIntegral}(a+bx)^2}{x^3} dx$$

Verification is Not applicable to the result.

[In] Integrate[CosIntegral[a + b*x]^2/x^3, x]

[Out] Integrate[CosIntegral[a + b*x]^2/x^3, x]

Maple [A] time = 0.066, size = 0, normalized size = 0.

$$\int \frac{(\text{Ci}(bx+a))^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x+a)^2/x^3, x)

[Out] int(Ci(b*x+a)^2/x^3, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{Ci}(bx + a)^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)^2/x^3,x, algorithm="maxima")

[Out] integrate(Ci(b*x + a)^2/x^3, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}\left(\frac{\operatorname{Ci}(bx + a)^2}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)^2/x^3,x, algorithm="fricas")

[Out] integral(cos_integral(b*x + a)^2/x^3, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{Ci}^2(a + bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)**2/x**3,x)

[Out] Integral(Ci(a + b*x)**2/x**3, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{Ci}(bx + a)^2}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)^2/x^3,x, algorithm="giac")

[Out] integrate(Ci(b*x + a)^2/x^3, x)

3.100 $\int x^2 \text{CosIntegral}(d(a + b \log(cx^n))) dx$

Optimal. Leaf size=133

$$\frac{1}{3}x^3 \text{CosIntegral}(d(a + b \log(cx^n))) - \frac{1}{6}x^3 e^{-\frac{3a}{bn}} (cx^n)^{-3/n} \text{ExpIntegralEi}\left(\frac{(3 - ibdn)(a + b \log(cx^n))}{bn}\right) - \frac{1}{6}x^3 e^{-\frac{3a}{bn}} (cx^n)^{-3/n}$$

[Out] (x^3*CosIntegral[d*(a + b*Log[c*x^n])])/3 - (x^3*ExpIntegralEi[((3 - I*b*d*n)*(a + b*Log[c*x^n])/(b*n))]/(6*E^((3*a)/(b*n))*(c*x^n)^(3/n)) - (x^3*ExpIntegralEi[((3 + I*b*d*n)*(a + b*Log[c*x^n])/(b*n))]/(6*E^((3*a)/(b*n))*(c*x^n)^(3/n))

Rubi [A] time = 0.251172, antiderivative size = 133, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.294$, Rules used = {6527, 12, 4498, 2310, 2178}

$$\frac{1}{3}x^3 \text{CosIntegral}(d(a + b \log(cx^n))) - \frac{1}{6}x^3 e^{-\frac{3a}{bn}} (cx^n)^{-3/n} \text{Ei}\left(\frac{(3 - ibdn)(a + b \log(cx^n))}{bn}\right) - \frac{1}{6}x^3 e^{-\frac{3a}{bn}} (cx^n)^{-3/n} \text{Ei}\left(\frac{(ibdn + 3)(a + b \log(cx^n))}{bn}\right)$$

Antiderivative was successfully verified.

[In] Int[x^2*CosIntegral[d*(a + b*Log[c*x^n]), x]

[Out] (x^3*CosIntegral[d*(a + b*Log[c*x^n])])/3 - (x^3*ExpIntegralEi[((3 - I*b*d*n)*(a + b*Log[c*x^n])/(b*n))]/(6*E^((3*a)/(b*n))*(c*x^n)^(3/n)) - (x^3*ExpIntegralEi[((3 + I*b*d*n)*(a + b*Log[c*x^n])/(b*n))]/(6*E^((3*a)/(b*n))*(c*x^n)^(3/n))

Rule 6527

Int[CosIntegral[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_)^(m_.), x_Symbol] := Simp[((e*x)^(m + 1)*CosIntegral[d*(a + b*Log[c*x^n])]/(e*(m + 1)), x] - Dist[(b*d*n)/(m + 1), Int[((e*x)^m*Cos[d*(a + b*Log[c*x^n])]/(d*(a + b*Log[c*x^n])), x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 4498

Int[Cos[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.) + Log[(g_.)*(x_)^(m_.)]*(f_.))*(h_.)^(q_.)*((i_.)*(x_)^(r_.), x_Symbol] := Dist[(i*x)^r/(E^(I*a*d)*(c*x^n)^(I*b*d)*(2*x^(r - I*b*d*n))), Int[x^(r - I*b*d*n)*(h*(e + f*Log[g*x^m]))^q, x], x] + Dist[(E^(I*a*d)*(i*x)^r*(c*x^n)^(I*b*d))/(2*x^(r + I*b*d*n)), Int[x^(r + I*b*d*n)*(h*(e + f*Log[g*x^m]))^q, x], x] /; FreeQ[{a, b, c, d, e, f, g, h, i, m, n, q, r}, x]

Rule 2310

Int[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))^(p_)*((d_.)*(x_)^(m_.), x_Symbol] := Dist[(d*x)^(m + 1)/(d*n*(c*x^n)^((m + 1)/n)), Subst[Int[E^(((m + 1)*x)/n)*(a + b*x)^p, x], x, Log[c*x^n]], x] /; FreeQ[{a, b, c, d, m, n, p}, x]

Rule 2178

```
Int[(F_)^((g_)*(e_) + (f_)*(x_))/((c_) + (d_)*(x_)), x_Symbol] := Si
mp[(F^(g*(e - (c*f)/d))*ExpIntegralEi[(f*g*(c + d*x)*Log[F])/d])/d, x] /; F
reeQ[{F, c, d, e, f, g}, x] && !$UseGamma == True
```

Rubi steps

$$\begin{aligned}
\int x^2 \text{Ci}(d(a + b \log(cx^n))) dx &= \frac{1}{3} x^3 \text{Ci}(d(a + b \log(cx^n))) - \frac{1}{3} (bdn) \int \frac{x^2 \cos(d(a + b \log(cx^n)))}{d(a + b \log(cx^n))} dx \\
&= \frac{1}{3} x^3 \text{Ci}(d(a + b \log(cx^n))) - \frac{1}{3} (bn) \int \frac{x^2 \cos(d(a + b \log(cx^n)))}{a + b \log(cx^n)} dx \\
&= \frac{1}{3} x^3 \text{Ci}(d(a + b \log(cx^n))) - \frac{1}{6} (be^{-iad} n x^{ibdn} (cx^n)^{-ibd}) \int \frac{x^{2-ibdn}}{a + b \log(cx^n)} dx - \frac{1}{6} (be^{i} \\
&= \frac{1}{3} x^3 \text{Ci}(d(a + b \log(cx^n))) - \frac{1}{6} (be^{-iad} x^3 (cx^n)^{-ibd - \frac{3-ibdn}{n}}) \text{Subst} \left(\int \frac{e^{\frac{(3-ibdn)x}{n}}}{a + bx} dx, x, \log \right) \\
&= \frac{1}{3} x^3 \text{Ci}(d(a + b \log(cx^n))) - \frac{1}{6} e^{-\frac{3a}{bn}} x^3 (cx^n)^{-3/n} \text{Ei} \left(\frac{(3-ibdn)(a + b \log(cx^n))}{bn} \right) - \frac{1}{6} e^{-\frac{3a}{bn}}
\end{aligned}$$

Mathematica [A] time = 1.74331, size = 102, normalized size = 0.77

$$\frac{1}{6} x^3 \left(2 \text{CosIntegral}(d(a + b \log(cx^n))) - e^{-\frac{3a}{bn}} (cx^n)^{-3/n} \left(\text{ExpIntegralEi} \left(\frac{(3-ibdn)(a + b \log(cx^n))}{bn} \right) + \text{ExpIntegralEi} \left(\frac{(3+ibdn)(a + b \log(cx^n))}{bn} \right) \right) \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*CosIntegral[d*(a + b*Log[c*x^n])], x]
```

```
[Out] (x^3*(2*CosIntegral[d*(a + b*Log[c*x^n])] - (ExpIntegralEi[((3 - I*b*d*n)*(a + b*Log[c*x^n])]/(b*n)) + ExpIntegralEi[((3 + I*b*d*n)*(a + b*Log[c*x^n])]/(b*n)))/(E^((3*a)/(b*n))*(c*x^n)^(3/n)))/6
```

Maple [F] time = 0.096, size = 0, normalized size = 0.

$$\int x^2 \text{Ci}(d(a + b \ln(cx^n))) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*Ci(d*(a+b*ln(c*x^n))), x)
```

```
[Out] int(x^2*Ci(d*(a+b*ln(c*x^n))), x)
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Ci}((b \log(cx^n) + a)d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*Ci(d*(a+b*log(c*x^n))), x, algorithm="maxima")
```

[Out] integrate(x^2*Ci((b*log(c*x^n) + a)*d), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(x^2 \text{Ci}(bd \log(cx^n) + ad), x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(d*(a+b*log(c*x^n))),x, algorithm="fricas")

[Out] integral(x^2*cos_integral(b*d*log(c*x^n) + a*d), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Ci}(ad + bd \log(cx^n)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*Ci(d*(a+b*ln(c*x**n))),x)

[Out] Integral(x**2*Ci(a*d + b*d*log(c*x**n)), x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(d*(a+b*log(c*x^n))),x, algorithm="giac")

[Out] Timed out

3.101 $\int x \text{CosIntegral}(d(a + b \log(cx^n))) dx$

Optimal. Leaf size=133

$$\frac{1}{2}x^2 \text{CosIntegral}(d(a + b \log(cx^n))) - \frac{1}{4}x^2 e^{-\frac{2a}{bn}} (cx^n)^{-2/n} \text{ExpIntegralEi}\left(\frac{(2 - ibdn)(a + b \log(cx^n))}{bn}\right) - \frac{1}{4}x^2 e^{-\frac{2a}{bn}} (cx^n)^{-2/n} \text{ExpIntegralEi}\left(\frac{(2 + ibdn)(a + b \log(cx^n))}{bn}\right)$$

[Out] (x^2*CosIntegral[d*(a + b*Log[c*x^n])])/2 - (x^2*ExpIntegralEi[((2 - I*b*d*n)*(a + b*Log[c*x^n])/(b*n))]/(4*E^((2*a)/(b*n))*(c*x^n)^(2/n)) - (x^2*ExpIntegralEi[((2 + I*b*d*n)*(a + b*Log[c*x^n])/(b*n))]/(4*E^((2*a)/(b*n))*(c*x^n)^(2/n))

Rubi [A] time = 0.247479, antiderivative size = 133, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 15, $\frac{\text{number of rules}}{\text{integrand size}} = 0.333$, Rules used = {6527, 12, 4498, 2310, 2178}

$$\frac{1}{2}x^2 \text{CosIntegral}(d(a + b \log(cx^n))) - \frac{1}{4}x^2 e^{-\frac{2a}{bn}} (cx^n)^{-2/n} \text{Ei}\left(\frac{(2 - ibdn)(a + b \log(cx^n))}{bn}\right) - \frac{1}{4}x^2 e^{-\frac{2a}{bn}} (cx^n)^{-2/n} \text{Ei}\left(\frac{(2 + ibdn)(a + b \log(cx^n))}{bn}\right)$$

Antiderivative was successfully verified.

[In] Int[x*CosIntegral[d*(a + b*Log[c*x^n]), x]

[Out] (x^2*CosIntegral[d*(a + b*Log[c*x^n])])/2 - (x^2*ExpIntegralEi[((2 - I*b*d*n)*(a + b*Log[c*x^n])/(b*n))]/(4*E^((2*a)/(b*n))*(c*x^n)^(2/n)) - (x^2*ExpIntegralEi[((2 + I*b*d*n)*(a + b*Log[c*x^n])/(b*n))]/(4*E^((2*a)/(b*n))*(c*x^n)^(2/n))

Rule 6527

Int[CosIntegral[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_)^(m_.), x_Symbol] :> Simp[((e*x)^(m + 1)*CosIntegral[d*(a + b*Log[c*x^n])]/(e*(m + 1)), x] - Dist[(b*d*n)/(m + 1), Int[((e*x)^m * Cos[d*(a + b*Log[c*x^n])])/(d*(a + b*Log[c*x^n])), x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[m, -1]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 4498

Int[Cos[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*(((e_.) + Log[(g_.)*(x_)^(m_.)]*(f_.))*(h_.))^(q_.)*((i_.)*(x_)^(r_.), x_Symbol] :> Dist[(i*x)^r / (E^(I*a*d)*(c*x^n)^(I*b*d)*(2*x^(r - I*b*d*n))), Int[x^(r - I*b*d*n)*(h*(e + f*Log[g*x^m]))^q, x], x] + Dist[(E^(I*a*d)*(i*x)^r*(c*x^n)^(I*b*d))/(2*x^(r + I*b*d*n)), Int[x^(r + I*b*d*n)*(h*(e + f*Log[g*x^m]))^q, x], x] /; FreeQ[{a, b, c, d, e, f, g, h, i, m, n, q, r}, x]

Rule 2310

Int[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))^(p_)*((d_.)*(x_)^(m_.), x_Symbol] :> Dist[(d*x)^(m + 1)/(d*n*(c*x^n)^((m + 1)/n)), Subst[Int[E^(((m + 1)*x)/n)*(a + b*x)^p, x], x, Log[c*x^n]], x] /; FreeQ[{a, b, c, d, m, n, p}, x]

Rule 2178

```
Int[(F_)^((g_.)*(e_.) + (f_.)*(x_)))/((c_.) + (d_.)*(x_)), x_Symbol] := Si
mp[(F^(g*(e - (c*f)/d))*ExpIntegralEi[(f*g*(c + d*x)*Log[F])/d])/d, x] /; F
reeQ[{F, c, d, e, f, g}, x] && !$UseGamma == True
```

Rubi steps

$$\begin{aligned}
\int x \operatorname{Ci}(d(a + b \log(cx^n))) dx &= \frac{1}{2} x^2 \operatorname{Ci}(d(a + b \log(cx^n))) - \frac{1}{2} (bdn) \int \frac{x \cos(d(a + b \log(cx^n)))}{d(a + b \log(cx^n))} dx \\
&= \frac{1}{2} x^2 \operatorname{Ci}(d(a + b \log(cx^n))) - \frac{1}{2} (bn) \int \frac{x \cos(d(a + b \log(cx^n)))}{a + b \log(cx^n)} dx \\
&= \frac{1}{2} x^2 \operatorname{Ci}(d(a + b \log(cx^n))) - \frac{1}{4} \left(b e^{-iad} n x^{ibdn} (cx^n)^{-ibd} \right) \int \frac{x^{1-ibdn}}{a + b \log(cx^n)} dx - \frac{1}{4} \left(b e^{iad} n x^{ibdn} (cx^n)^{-ibd} \right) \int \frac{x^{1-ibdn}}{a + b \log(cx^n)} dx \\
&= \frac{1}{2} x^2 \operatorname{Ci}(d(a + b \log(cx^n))) - \frac{1}{4} \left(b e^{-iad} x^2 (cx^n)^{-ibd - \frac{2-ibdn}{n}} \right) \operatorname{Subst} \left(\int \frac{e^{\frac{(2-ibdn)x}{n}}}{a + bx} dx, x, \log(cx^n) \right) \\
&= \frac{1}{2} x^2 \operatorname{Ci}(d(a + b \log(cx^n))) - \frac{1}{4} e^{-\frac{2a}{bn}} x^2 (cx^n)^{-2/n} \operatorname{Ei} \left(\frac{(2-ibdn)(a + b \log(cx^n))}{bn} \right) - \frac{1}{4} e^{-\frac{2a}{bn}} x^2 (cx^n)^{-2/n} \operatorname{Ei} \left(\frac{(2+ibdn)(a + b \log(cx^n))}{bn} \right)
\end{aligned}$$

Mathematica [A] time = 1.71581, size = 102, normalized size = 0.77

$$\frac{1}{4} x^2 \left(2 \operatorname{CosIntegral}(d(a + b \log(cx^n))) - e^{-\frac{2a}{bn}} (cx^n)^{-2/n} \left(\operatorname{ExpIntegralEi} \left(\frac{(2-ibdn)(a + b \log(cx^n))}{bn} \right) + \operatorname{ExpIntegralEi} \left(\frac{(2+ibdn)(a + b \log(cx^n))}{bn} \right) \right) \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[x*CosIntegral[d*(a + b*Log[c*x^n])], x]
```

```
[Out] (x^2*(2*CosIntegral[d*(a + b*Log[c*x^n])] - (ExpIntegralEi[((2 - I*b*d*n)*(a + b*Log[c*x^n])]/(b*n)] + ExpIntegralEi[((2 + I*b*d*n)*(a + b*Log[c*x^n])]/(b*n)]))/(E^((2*a)/(b*n))*(c*x^n)^(2/n)))/4
```

Maple [F] time = 0.092, size = 0, normalized size = 0.

$$\int x \operatorname{Ci}(d(a + b \ln(cx^n))) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*Ci(d*(a+b*ln(c*x^n))), x)
```

```
[Out] int(x*Ci(d*(a+b*ln(c*x^n))), x)
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \operatorname{Ci}((b \log(cx^n) + a)d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*Ci(d*(a+b*log(c*x^n))), x, algorithm="maxima")
```

[Out] integrate(x*Ci((b*log(c*x^n) + a)*d), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x \text{Ci}(bd \log(cx^n) + ad), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(d*(a+b*log(c*x^n))),x, algorithm="fricas")

[Out] integral(x*cos_integral(b*d*log(c*x^n) + a*d), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \text{Ci}(ad + bd \log(cx^n)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(d*(a+b*ln(c*x**n))),x)

[Out] Integral(x*Ci(a*d + b*d*log(c*x**n)), x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(d*(a+b*log(c*x^n))),x, algorithm="giac")

[Out] Timed out

3.102 $\int \text{CosIntegral}(d(a + b \log(cx^n))) dx$

Optimal. Leaf size=124

$$x \text{CosIntegral}(d(a + b \log(cx^n))) - \frac{1}{2} x e^{-\frac{a}{bn}} (cx^n)^{-1/n} \text{ExpIntegralEi}\left(\frac{(1 - ibdn)(a + b \log(cx^n))}{bn}\right) - \frac{1}{2} x e^{-\frac{a}{bn}} (cx^n)^{-1/n} \text{ExpIntegralEi}\left(\frac{(1 + ibdn)(a + b \log(cx^n))}{bn}\right)$$

[Out] x*CosIntegral[d*(a + b*Log[c*x^n])] - (x*ExpIntegralEi[((1 - I*b*d*n)*(a + b*Log[c*x^n]))/(b*n)])/(2*E^(a/(b*n))*(c*x^n)^n^(-1)) - (x*ExpIntegralEi[((1 + I*b*d*n)*(a + b*Log[c*x^n]))/(b*n)])/(2*E^(a/(b*n))*(c*x^n)^n^(-1))

Rubi [A] time = 0.228058, antiderivative size = 124, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {6524, 12, 4496, 2310, 2178}

$$x \text{CosIntegral}(d(a + b \log(cx^n))) - \frac{1}{2} x e^{-\frac{a}{bn}} (cx^n)^{-1/n} \text{Ei}\left(\frac{(1 - ibdn)(a + b \log(cx^n))}{bn}\right) - \frac{1}{2} x e^{-\frac{a}{bn}} (cx^n)^{-1/n} \text{Ei}\left(\frac{(ibdn + 1)(a + b \log(cx^n))}{bn}\right)$$

Antiderivative was successfully verified.

[In] Int[CosIntegral[d*(a + b*Log[c*x^n]),x]

[Out] x*CosIntegral[d*(a + b*Log[c*x^n])] - (x*ExpIntegralEi[((1 - I*b*d*n)*(a + b*Log[c*x^n]))/(b*n)])/(2*E^(a/(b*n))*(c*x^n)^n^(-1)) - (x*ExpIntegralEi[((1 + I*b*d*n)*(a + b*Log[c*x^n]))/(b*n)])/(2*E^(a/(b*n))*(c*x^n)^n^(-1))

Rule 6524

Int[CosIntegral[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)], x_Symbol] := Simp[x*CosIntegral[d*(a + b*Log[c*x^n]), x] - Dist[b*d*n, Int[Cos[d*(a + b*Log[c*x^n])]/(d*(a + b*Log[c*x^n]), x], x] /; FreeQ[{a, b, c, d, n}, x]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 4496

Int[Cos[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*(((e_.) + Log[(g_.)*(x_)^(m_.)]*(f_.))*(h_.))^(q_.), x_Symbol] := Dist[1/(E^(I*a*d)*(c*x^n)^(I*b*d)*(2/x^(I*b*d*n))), Int[(h*(e + f*Log[g*x^m]))^q/x^(I*b*d*n), x], x] + Dist[(E^(I*a*d)*(c*x^n)^(I*b*d))/(2*x^(I*b*d*n)), Int[x^(I*b*d*n)*(h*(e + f*Log[g*x^m]))^q, x], x] /; FreeQ[{a, b, c, d, e, f, g, h, m, n, q}, x]

Rule 2310

Int[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))^(p_)*((d_.)*(x_)^(m_.)), x_Symbol] := Dist[(d*x)^(m + 1)/(d*n*(c*x^n)^((m + 1)/n)), Subst[Int[E^(((m + 1)*x)/n)*(a + b*x)^p, x], x, Log[c*x^n]], x] /; FreeQ[{a, b, c, d, m, n, p}, x]

Rule 2178

Int[(F_)^((g_.)*((e_.) + (f_.)*(x_)))/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[(F^(g*(e - (c*f)/d))*ExpIntegralEi[(f*g*(c + d*x)*Log[F])/d])/d, x] /; FreeQ[{F, c, d, e, f, g}, x] && !\$UseGamma == True

Rubi steps

$$\begin{aligned}
\int \text{Ci}(d(a + b \log(cx^n))) dx &= x \text{Ci}(d(a + b \log(cx^n))) - (bdn) \int \frac{\cos(d(a + b \log(cx^n)))}{d(a + b \log(cx^n))} dx \\
&= x \text{Ci}(d(a + b \log(cx^n))) - (bn) \int \frac{\cos(d(a + b \log(cx^n)))}{a + b \log(cx^n)} dx \\
&= x \text{Ci}(d(a + b \log(cx^n))) - \frac{1}{2} (be^{-iad} n x^{ibdn} (cx^n)^{-ibd}) \int \frac{x^{-ibdn}}{a + b \log(cx^n)} dx - \frac{1}{2} (be^{iad} n x^{-ibdn}) \int \frac{x^{-ibdn}}{a + b \log(cx^n)} dx \\
&= x \text{Ci}(d(a + b \log(cx^n))) - \frac{1}{2} (be^{-iad} x (cx^n)^{-ibd - \frac{1-ibdn}{n}}) \text{Subst} \left(\int \frac{e^{\frac{(1-ibdn)x}{n}}}{a + bx} dx, x, \log(cx^n) \right) \\
&= x \text{Ci}(d(a + b \log(cx^n))) - \frac{1}{2} e^{-\frac{a}{bn}} x (cx^n)^{-1/n} \text{Ei} \left(\frac{(1-ibdn)(a + b \log(cx^n))}{bn} \right) - \frac{1}{2} e^{-\frac{a}{bn}} x (cx^n)^{-1/n} \text{Ei} \left(\frac{(1+ibdn)(a + b \log(cx^n))}{bn} \right)
\end{aligned}$$

Mathematica [A] time = 1.65783, size = 98, normalized size = 0.79

$$x \text{CosIntegral}(d(a + b \log(cx^n))) - \frac{1}{2} x e^{-\frac{a}{bn}} (cx^n)^{-1/n} \left(\text{ExpIntegralEi} \left(\frac{(1-ibdn)(a + b \log(cx^n))}{bn} \right) + \text{ExpIntegralEi} \left(\frac{(1+ibdn)(a + b \log(cx^n))}{bn} \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[CosIntegral[d*(a + b*Log[c*x^n])], x]

[Out] x*CosIntegral[d*(a + b*Log[c*x^n])] - (x*(ExpIntegralEi[((1 - I*b*d*n)*(a + b*Log[c*x^n]))/(b*n)] + ExpIntegralEi[((1 + I*b*d*n)*(a + b*Log[c*x^n]))/(b*n)]))/(2*E^(a/(b*n))*(c*x^n)^n^(-1))

Maple [F] time = 0.073, size = 0, normalized size = 0.

$$\int \text{Ci}(d(a + b \ln(cx^n))) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(d*(a+b*ln(c*x^n))), x)

[Out] int(Ci(d*(a+b*ln(c*x^n))), x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Ci}((b \log(cx^n) + a)d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*(a+b*log(c*x^n))), x, algorithm="maxima")

[Out] integrate(Ci((b*log(c*x^n) + a)*d), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(\text{Ci}(bd \log(cx^n) + ad), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*(a+b*log(c*x^n))),x, algorithm="fricas")

[Out] integral(cos_integral(b*d*log(c*x^n) + a*d), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Ci}(d(a + b \log(cx^n))) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*(a+b*ln(c*x**n))),x)

[Out] Integral(Ci(d*(a + b*log(c*x**n))), x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*(a+b*log(c*x^n))),x, algorithm="giac")

[Out] Timed out

$$3.103 \quad \int \frac{\text{CosIntegral}(d(a+b \log(cx^n)))}{x} dx$$

Optimal. Leaf size=55

$$\frac{(a + b \log(cx^n)) \text{CosIntegral}(d(a + b \log(cx^n)))}{bn} - \frac{\sin(d(a + b \log(cx^n)))}{bdn}$$

[Out] (CosIntegral[d*(a + b*Log[c*x^n])]*(a + b*Log[c*x^n]))/(b*n) - Sin[d*(a + b*Log[c*x^n])]/(b*d*n)

Rubi [A] time = 0.0352144, antiderivative size = 55, normalized size of antiderivative = 1., number of steps used = 3, number of rules used = 1, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.059$, Rules used = {6500}

$$\frac{(a + b \log(cx^n)) \text{CosIntegral}(d(a + b \log(cx^n)))}{bn} - \frac{\sin(d(a + b \log(cx^n)))}{bdn}$$

Antiderivative was successfully verified.

[In] Int[CosIntegral[d*(a + b*Log[c*x^n])]/x,x]

[Out] (CosIntegral[d*(a + b*Log[c*x^n])]*(a + b*Log[c*x^n]))/(b*n) - Sin[d*(a + b*Log[c*x^n])]/(b*d*n)

Rule 6500

Int[CosIntegral[(a_.) + (b_.)*(x_)], x_Symbol] :> Simp[((a + b*x)*CosIntegral[a + b*x])/b, x] - Simp[Sin[a + b*x]/b, x] /; FreeQ[{a, b}, x]

Rubi steps

$$\begin{aligned} \int \frac{\text{Ci}(d(a + b \log(cx^n)))}{x} dx &= \frac{\text{Subst}\left(\int \text{Ci}(d(a + bx)) dx, x, \log(cx^n)\right)}{n} \\ &= \frac{\text{Subst}\left(\int \text{Ci}(x) dx, x, ad + bd \log(cx^n)\right)}{bdn} \\ &= \frac{\text{Ci}(ad + bd \log(cx^n))(a + b \log(cx^n))}{bn} - \frac{\sin(ad + bd \log(cx^n))}{bdn} \end{aligned}$$

Mathematica [A] time = 0.0786387, size = 96, normalized size = 1.75

$$\frac{a \text{CosIntegral}(ad + bd \log(cx^n))}{bn} + \frac{\log(cx^n) \text{CosIntegral}(d(a + b \log(cx^n)))}{n} - \frac{\sin(ad) \cos(bd \log(cx^n))}{bdn} - \frac{\cos(ad)}{bdn}$$

Antiderivative was successfully verified.

[In] Integrate[CosIntegral[d*(a + b*Log[c*x^n])]/x,x]

[Out] (a*CosIntegral[a*d + b*d*Log[c*x^n])]/(b*n) + (CosIntegral[d*(a + b*Log[c*x^n])]*Log[c*x^n])/n - (Cos[b*d*Log[c*x^n]]*Sin[a*d])/(b*d*n) - (Cos[a*d]*Sin[b*d*Log[c*x^n])]/(b*d*n)

Maple [A] time = 0.07, size = 73, normalized size = 1.3

$$\frac{\ln(cx^n) \operatorname{Ci}(ad + bd \ln(cx^n))}{n} + \frac{\operatorname{Ci}(ad + bd \ln(cx^n)) a}{bn} - \frac{\sin(ad + bd \ln(cx^n))}{bdn}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(d*(a+b*ln(c*x^n)))/x,x)

[Out] 1/n*ln(c*x^n)*Ci(a*d+b*d*ln(c*x^n))+1/n/b*Ci(a*d+b*d*ln(c*x^n))*a-1/n/b/d*sin(a*d+b*d*ln(c*x^n))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{Ci}((b \log(cx^n) + a)d)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*(a+b*log(c*x^n)))/x,x, algorithm="maxima")

[Out] integrate(Ci((b*log(c*x^n) + a)*d)/x, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}\left(\frac{\operatorname{Ci}(bd \log(cx^n) + ad)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*(a+b*log(c*x^n)))/x,x, algorithm="fricas")

[Out] integral(cos_integral(b*d*log(c*x^n) + a*d)/x, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{Ci}(ad + bd \log(cx^n))}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*(a+b*ln(c*x**n)))/x,x)

[Out] Integral(Ci(a*d + b*d*log(c*x**n))/x, x)

Giac [A] time = 1.33635, size = 82, normalized size = 1.49

$$\frac{(bdn \log(x) + bd \log(c) + ad) \operatorname{Ci}(bdn \log(x) + bd \log(c) + ad) - \sin(bdn \log(x) + bd \log(c) + ad)}{bdn}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(d*(a+b*log(c*x^n)))/x,x, algorithm="giac")
```

```
[Out] ((b*d*n*log(x) + b*d*log(c) + a*d)*cos_integral(b*d*n*log(x) + b*d*log(c) +  
a*d) - sin(b*d*n*log(x) + b*d*log(c) + a*d))/(b*d*n)
```

3.104 $\int \frac{\text{CosIntegral}(d(a+b \log(cx^n)))}{x^2} dx$

Optimal. Leaf size=127

$$-\frac{\text{CosIntegral}(d(a+b \log(cx^n)))}{x} + \frac{e^{\frac{a}{bn}}(cx^n)^{\frac{1}{n}} \text{ExpIntegralEi}\left(-\frac{(1-ibdn)(a+b \log(cx^n))}{bn}\right)}{2x} + \frac{e^{\frac{a}{bn}}(cx^n)^{\frac{1}{n}} \text{ExpIntegralEi}\left(-\frac{(1+ibdn)(a+b \log(cx^n))}{bn}\right)}{2x}$$

[Out] $-(\text{CosIntegral}[d*(a + b*\text{Log}[c*x^n]])/x) + (E^{(a/(b*n))}*(c*x^n)^n^{(-1)}*\text{ExpIntegralEi}[-(((1 - I*b*d*n)*(a + b*\text{Log}[c*x^n]))/(b*n))])/(2*x) + (E^{(a/(b*n))}*(c*x^n)^n^{(-1)}*\text{ExpIntegralEi}[-(((1 + I*b*d*n)*(a + b*\text{Log}[c*x^n]))/(b*n))])/(2*x)$

Rubi [A] time = 0.247361, antiderivative size = 127, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.294$, Rules used = {6527, 12, 4498, 2310, 2178}

$$-\frac{\text{CosIntegral}(d(a+b \log(cx^n)))}{x} + \frac{e^{\frac{a}{bn}}(cx^n)^{\frac{1}{n}} \text{Ei}\left(-\frac{(1-ibdn)(a+b \log(cx^n))}{bn}\right)}{2x} + \frac{e^{\frac{a}{bn}}(cx^n)^{\frac{1}{n}} \text{Ei}\left(-\frac{(1+ibdn)(a+b \log(cx^n))}{bn}\right)}{2x}$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{CosIntegral}[d*(a + b*\text{Log}[c*x^n])]/x^2, x]$

[Out] $-(\text{CosIntegral}[d*(a + b*\text{Log}[c*x^n]])/x) + (E^{(a/(b*n))}*(c*x^n)^n^{(-1)}*\text{ExpIntegralEi}[-(((1 - I*b*d*n)*(a + b*\text{Log}[c*x^n]))/(b*n))])/(2*x) + (E^{(a/(b*n))}*(c*x^n)^n^{(-1)}*\text{ExpIntegralEi}[-(((1 + I*b*d*n)*(a + b*\text{Log}[c*x^n]))/(b*n))])/(2*x)$

Rule 6527

$\text{Int}[\text{CosIntegral}[(a_.) + \text{Log}[(c_.)*(x_.)^{(n_.)}]*(b_.)]*(d_.)]*((e_.)*(x_.))^{(m_.)}, x_Symbol] := \text{Simp}[(e*x)^{(m+1)}*\text{CosIntegral}[d*(a + b*\text{Log}[c*x^n])]/(e*(m+1)), x] - \text{Dist}[(b*d*n)/(m+1), \text{Int}[(e*x)^m*\text{Cos}[d*(a + b*\text{Log}[c*x^n])]]/(d*(a + b*\text{Log}[c*x^n])), x], x] /; \text{FreeQ}\{a, b, c, d, e, m, n\}, x] \&\& \text{NeQ}[m, -1]$

Rule 12

$\text{Int}[(a_)*(u_), x_Symbol] := \text{Dist}[a, \text{Int}[u, x], x] /; \text{FreeQ}[a, x] \&\& !\text{MatchQ}[u, (b_)*(v_)] /; \text{FreeQ}[b, x]$

Rule 4498

$\text{Int}[\text{Cos}[(a_.) + \text{Log}[(c_.)*(x_.)^{(n_.)}]*(b_.)]*(d_.)]*((e_.) + \text{Log}[(g_.)*(x_.)^{(m_.)}]*(f_.))*(h_.)^{(q_.)}*((i_.)*(x_.))^{(r_.)}, x_Symbol] := \text{Dist}[(i*x)^r/(E^{(I*a*d)}*(c*x^n)^{(I*b*d)}*(2*x^{(r - I*b*d*n)})), \text{Int}[x^{(r - I*b*d*n)}*(h*(e + f*\text{Log}[g*x^m]))^q, x], x] + \text{Dist}[(E^{(I*a*d)}*(i*x)^r*(c*x^n)^{(I*b*d)})/(2*x^{(r + I*b*d*n)}), \text{Int}[x^{(r + I*b*d*n)}*(h*(e + f*\text{Log}[g*x^m]))^q, x], x] /; \text{FreeQ}\{a, b, c, d, e, f, g, h, i, m, n, q, r\}, x]$

Rule 2310

$\text{Int}[(a_.) + \text{Log}[(c_.)*(x_.)^{(n_.)}]*(b_.)]^{(p_.)}*((d_.)*(x_.))^{(m_.)}, x_Symbol] := \text{Dist}[(d*x)^{(m+1)}/(d*n*(c*x^n)^{((m+1)/n)}), \text{Subst}[\text{Int}[E^{((m+1)*x/n)}*(a + b*x)^p, x], x, \text{Log}[c*x^n]], x] /; \text{FreeQ}\{a, b, c, d, m, n, p\}, x]$

Rule 2178

```
Int[(F_)^((g_.)*(e_.) + (f_.)*(x_))/((c_.) + (d_.)*(x_)), x_Symbol] := Si
mp[(F^(g*(e - (c*f)/d))*ExpIntegralEi[(f*g*(c + d*x)*Log[F])/d])/d, x] /; F
reeQ[{F, c, d, e, f, g}, x] && !$UseGamma == True
```

Rubi steps

$$\begin{aligned} \int \frac{\text{Ci}(d(a + b \log(cx^n)))}{x^2} dx &= -\frac{\text{Ci}(d(a + b \log(cx^n)))}{x} + (bdn) \int \frac{\cos(d(a + b \log(cx^n)))}{dx^2(a + b \log(cx^n))} dx \\ &= -\frac{\text{Ci}(d(a + b \log(cx^n)))}{x} + (bn) \int \frac{\cos(d(a + b \log(cx^n)))}{x^2(a + b \log(cx^n))} dx \\ &= -\frac{\text{Ci}(d(a + b \log(cx^n)))}{x} + \frac{1}{2} (be^{-iad} nx^{ibdn} (cx^n)^{-ibd}) \int \frac{x^{-2-ibdn}}{a + b \log(cx^n)} dx + \frac{1}{2} (be^{iad} nx^{ibdn} (cx^n)^{-ibd}) \int \frac{x^{-2-ibdn}}{a + b \log(cx^n)} dx \\ &= -\frac{\text{Ci}(d(a + b \log(cx^n)))}{x} + \frac{(be^{-iad} (cx^n)^{-ibd-\frac{-1-ibdn}{n}}) \text{Subst}\left(\int \frac{e^{\frac{(-1-ibdn)x}{a+bx}}}{a+bx} dx, x, \log(cx^n)\right)}{2x} + \frac{(be^{iad} (cx^n)^{-ibd-\frac{-1-ibdn}{n}}) \text{Subst}\left(\int \frac{e^{\frac{(-1-ibdn)x}{a+bx}}}{a+bx} dx, x, \log(cx^n)\right)}{2x} \\ &= -\frac{\text{Ci}(d(a + b \log(cx^n)))}{x} + \frac{e^{\frac{a}{bn}} (cx^n)^{\frac{1}{n}} \text{Ei}\left(-\frac{(1-ibdn)(a+b \log(cx^n))}{bn}\right)}{2x} + \frac{e^{\frac{a}{bn}} (cx^n)^{\frac{1}{n}} \text{Ei}\left(-\frac{(1+ibdn)(a+b \log(cx^n))}{bn}\right)}{2x} \end{aligned}$$

Mathematica [A] time = 1.701, size = 102, normalized size = 0.8

$$\frac{-2\text{CosIntegral}(d(a + b \log(cx^n))) + e^{\frac{a}{bn}} (cx^n)^{\frac{1}{n}} \left(\text{ExpIntegralEi}\left(-\frac{i(bdn-i)(a+b \log(cx^n))}{bn}\right) + \text{ExpIntegralEi}\left(\frac{i(bdn+i)(a+b \log(cx^n))}{bn}\right) \right)}{2x}$$

Antiderivative was successfully verified.

[In] Integrate[CosIntegral[d*(a + b*Log[c*x^n])]/x^2,x]

[Out] (-2*CosIntegral[d*(a + b*Log[c*x^n])] + E^(a/(b*n))*(c*x^n)^n^(-1)*(ExpIntegralEi[((-I)*(-I + b*d*n)*(a + b*Log[c*x^n]))/(b*n)] + ExpIntegralEi[(I*(I + b*d*n)*(a + b*Log[c*x^n]))/(b*n)]))/(2*x)

Maple [F] time = 0.096, size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(d(a + b \ln(cx^n)))}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(d*(a+b*ln(c*x^n)))/x^2,x)

[Out] int(Ci(d*(a+b*ln(c*x^n)))/x^2,x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}((b \log(cx^n) + a)d)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*(a+b*log(c*x^n)))/x^2,x, algorithm="maxima")

[Out] integrate(Ci((b*log(c*x^n) + a)*d)/x^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bd \log(cx^n) + ad)}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*(a+b*log(c*x^n)))/x^2,x, algorithm="fricas")

[Out] integral(cos_integral(b*d*log(c*x^n) + a*d)/x^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(ad + bd \log(cx^n))}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*(a+b*ln(c*x**n)))/x**2,x)

[Out] Integral(Ci(a*d + b*d*log(c*x**n))/x**2, x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*(a+b*log(c*x^n)))/x^2,x, algorithm="giac")

[Out] Timed out

3.105 $\int \frac{\text{CosIntegral}(d(a+b \log(cx^n)))}{x^3} dx$

Optimal. Leaf size=135

$$\frac{\text{CosIntegral}(d(a+b \log(cx^n)))}{2x^2} + \frac{e^{\frac{2a}{bn}} (cx^n)^{2/n} \text{ExpIntegralEi}\left(-\frac{(2-ibdn)(a+b \log(cx^n))}{bn}\right)}{4x^2} + \frac{e^{\frac{2a}{bn}} (cx^n)^{2/n} \text{ExpIntegralEi}\left(\frac{(2+ibdn)(a+b \log(cx^n))}{bn}\right)}{4x^2}$$

```
[Out] -CosIntegral[d*(a + b*Log[c*x^n])]/(2*x^2) + (E^((2*a)/(b*n))*(c*x^n)^(2/n)
*ExpIntegralEi[-(((2 - I*b*d*n)*(a + b*Log[c*x^n]))/(b*n)))]/(4*x^2) + (E^
(2*a)/(b*n))*(c*x^n)^(2/n)*ExpIntegralEi[-(((2 + I*b*d*n)*(a + b*Log[c*x^n]
)))/(b*n))]/(4*x^2)
```

Rubi [A] time = 0.238982, antiderivative size = 135, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 17, $\frac{\text{number of rules}}{\text{integrand size}} = 0.294$, Rules used = {6527, 12, 4498, 2310, 2178}

$$\frac{\text{CosIntegral}(d(a+b \log(cx^n)))}{2x^2} + \frac{e^{\frac{2a}{bn}} (cx^n)^{2/n} \text{Ei}\left(-\frac{(2-ibdn)(a+b \log(cx^n))}{bn}\right)}{4x^2} + \frac{e^{\frac{2a}{bn}} (cx^n)^{2/n} \text{Ei}\left(-\frac{(ibdn+2)(a+b \log(cx^n))}{bn}\right)}{4x^2}$$

Antiderivative was successfully verified.

```
[In] Int[CosIntegral[d*(a + b*Log[c*x^n])]/x^3,x]
```

```
[Out] -CosIntegral[d*(a + b*Log[c*x^n])]/(2*x^2) + (E^((2*a)/(b*n))*(c*x^n)^(2/n)
*ExpIntegralEi[-(((2 - I*b*d*n)*(a + b*Log[c*x^n]))/(b*n)))]/(4*x^2) + (E^
(2*a)/(b*n))*(c*x^n)^(2/n)*ExpIntegralEi[-(((2 + I*b*d*n)*(a + b*Log[c*x^n]
)))/(b*n))]/(4*x^2)
```

Rule 6527

```
Int[CosIntegral[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.)*(x_)^(
m_.), x_Symbol] := Simp[((e*x)^(m + 1)*CosIntegral[d*(a + b*Log[c*x^n])]/(
e*(m + 1)), x] - Dist[(b*d*n)/(m + 1), Int[((e*x)^m*Cos[d*(a + b*Log[c*x^n]
)])/d*(a + b*Log[c*x^n]), x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && Ne
Q[m, -1]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !Match
Q[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 4498

```
Int[Cos[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))*(d_.)]*((e_.) + Log[(g_.)*(x
_)^(m_.)]*(f_.))*(h_.)^(q_.)*((i_.)*(x_)^(r_.), x_Symbol] := Dist[(i*x)^r
/(E^(I*a*d)*(c*x^n)^(I*b*d)*(2*x^(r - I*b*d*n))), Int[x^(r - I*b*d*n)*(h*(e
+ f*Log[g*x^m]))^q, x], x] + Dist[(E^(I*a*d)*(i*x)^r*(c*x^n)^(I*b*d))/(2*x
^(r + I*b*d*n)), Int[x^(r + I*b*d*n)*(h*(e + f*Log[g*x^m]))^q, x], x] /; Fr
eeQ[{a, b, c, d, e, f, g, h, i, m, n, q, r}, x]
```

Rule 2310

```
Int[((a_.) + Log[(c_.)*(x_)^(n_.)]*(b_.))^(p_.)*((d_.)*(x_)^(m_.), x_Symbol
] := Dist[(d*x)^(m + 1)/(d*n*(c*x^n)^((m + 1)/n)), Subst[Int[E^(((m + 1)*x)
/n)*(a + b*x)^p, x], x, Log[c*x^n]], x] /; FreeQ[{a, b, c, d, m, n, p}, x]
```

Rule 2178

```
Int[(F_)^((g_.)*(e_.) + (f_.)*(x_))/((c_.) + (d_.)*(x_)), x_Symbol] := Si
mp[(F^(g*(e - (c*f)/d))*ExpIntegralEi[(f*g*(c + d*x)*Log[F])/d])/d, x] /; F
reeQ[{F, c, d, e, f, g}, x] && !$UseGamma == True
```

Rubi steps

$$\begin{aligned}
\int \frac{\text{Ci}(d(a + b \log(cx^n)))}{x^3} dx &= -\frac{\text{Ci}(d(a + b \log(cx^n)))}{2x^2} + \frac{1}{2}(bdn) \int \frac{\cos(d(a + b \log(cx^n)))}{dx^3(a + b \log(cx^n))} dx \\
&= -\frac{\text{Ci}(d(a + b \log(cx^n)))}{2x^2} + \frac{1}{2}(bn) \int \frac{\cos(d(a + b \log(cx^n)))}{x^3(a + b \log(cx^n))} dx \\
&= -\frac{\text{Ci}(d(a + b \log(cx^n)))}{2x^2} + \frac{1}{4} \left(be^{-iad} n x^{ibd n} (cx^n)^{-ibd} \right) \int \frac{x^{-3-ibd n}}{a + b \log(cx^n)} dx + \frac{1}{4} \left(be^{iad} n x^{-ibd n} \right) \int \frac{x^{-3-ibd n}}{a + b \log(cx^n)} dx \\
&= -\frac{\text{Ci}(d(a + b \log(cx^n)))}{2x^2} + \frac{\left(be^{-iad} (cx^n)^{-ibd - \frac{-2-ibd n}{n}} \right) \text{Subst} \left(\int \frac{e^{\frac{(-2-ibd n)x}{a+bx}}}{a+bx} dx, x, \log(cx^n) \right)}{4x^2} + \frac{\left(be^{iad} (cx^n)^{-ibd - \frac{-2-ibd n}{n}} \right) \text{Subst} \left(\int \frac{e^{\frac{(-2-ibd n)x}{a+bx}}}{a+bx} dx, x, \log(cx^n) \right)}{4x^2} \\
&= -\frac{\text{Ci}(d(a + b \log(cx^n)))}{2x^2} + \frac{e^{\frac{2a}{bn}} (cx^n)^{2/n} \text{Ei} \left(-\frac{(2-ibd n)(a+b \log(cx^n))}{bn} \right)}{4x^2} + \frac{e^{\frac{2a}{bn}} (cx^n)^{2/n} \text{Ei} \left(-\frac{(2+ibd n)(a+b \log(cx^n))}{bn} \right)}{4x^2}
\end{aligned}$$

Mathematica [A] time = 1.71334, size = 105, normalized size = 0.78

$$\frac{-2\text{CosIntegral}(d(a + b \log(cx^n))) + e^{\frac{2a}{bn}} (cx^n)^{2/n} \left(\text{ExpIntegralEi} \left(-\frac{i(bdn-2i)(a+b \log(cx^n))}{bn} \right) + \text{ExpIntegralEi} \left(\frac{i(bdn+2i)(a+b \log(cx^n))}{bn} \right) \right)}{4x^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[CosIntegral[d*(a + b*Log[c*x^n])]/x^3, x]
```

```
[Out] (-2*CosIntegral[d*(a + b*Log[c*x^n])] + E^((2*a)/(b*n))*(c*x^n)^(2/n)*(ExpIntegralEi[(-I)*(-2*I + b*d*n)*(a + b*Log[c*x^n])/(b*n)] + ExpIntegralEi[(I*(2*I + b*d*n)*(a + b*Log[c*x^n])/(b*n))]))/(4*x^2)
```

Maple [F] time = 0.097, size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(d(a + b \ln(cx^n)))}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(Ci(d*(a+b*ln(c*x^n)))/x^3, x)
```

```
[Out] int(Ci(d*(a+b*ln(c*x^n)))/x^3, x)
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}((b \log(cx^n) + a)d)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*(a+b*log(c*x^n)))/x^3,x, algorithm="maxima")

[Out] integrate(Ci((b*log(c*x^n) + a)*d)/x^3, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bd \log(cx^n) + ad)}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*(a+b*log(c*x^n)))/x^3,x, algorithm="fricas")

[Out] integral(cos_integral(b*d*log(c*x^n) + a*d)/x^3, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(ad + bd \log(cx^n))}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*(a+b*ln(c*x**n)))/x**3,x)

[Out] Integral(Ci(a*d + b*d*log(c*x**n))/x**3, x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*(a+b*log(c*x^n)))/x^3,x, algorithm="giac")

[Out] Timed out

3.106 $\int (ex)^m \text{CosIntegral}(d(a + b \log(cx^n))) dx$

Optimal. Leaf size=172

$$\frac{(ex)^{m+1} \text{CosIntegral}(d(a + b \log(cx^n)))}{e(m+1)} - \frac{x(ex)^m e^{-\frac{a(m+1)}{bn}} (cx^n)^{-\frac{m+1}{n}} \text{ExpIntegralEi}\left(\frac{(-ibdn+m+1)(a+b \log(cx^n))}{bn}\right)}{2(m+1)} - \frac{x(ex)^m e^{-\frac{a(m+1)}{bn}} (cx^n)^{-\frac{m+1}{n}} \text{ExpIntegralEi}\left(\frac{(m-ibdn+1)(a+b \log(cx^n))}{bn}\right)}{2(m+1)}$$

[Out] $((e*x)^{(1+m)}*\text{CosIntegral}[d*(a + b*\text{Log}[c*x^n])])/(e*(1+m)) - (x*(e*x)^m*\text{ExpIntegralEi}[((1+m - I*b*d*n)*(a + b*\text{Log}[c*x^n]))/(b*n)])/ (2*E^{((a*(1+m))/(b*n))* (1+m)*(c*x^n)^{((1+m)/n)}} - (x*(e*x)^m*\text{ExpIntegralEi}[((1+m + I*b*d*n)*(a + b*\text{Log}[c*x^n]))/(b*n)])/ (2*E^{((a*(1+m))/(b*n))* (1+m)*(c*x^n)^{((1+m)/n)}})$

Rubi [A] time = 0.294702, antiderivative size = 172, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 5, integrand size = 19, $\frac{\text{number of rules}}{\text{integrand size}} = 0.263$, Rules used = {6527, 12, 4498, 2310, 2178}

$$\frac{(ex)^{m+1} \text{CosIntegral}(d(a + b \log(cx^n)))}{e(m+1)} - \frac{x(ex)^m e^{-\frac{a(m+1)}{bn}} (cx^n)^{-\frac{m+1}{n}} \text{Ei}\left(\frac{(m-ibdn+1)(a+b \log(cx^n))}{bn}\right)}{2(m+1)} - \frac{x(ex)^m e^{-\frac{a(m+1)}{bn}} (cx^n)^{-\frac{m+1}{n}} \text{Ei}\left(\frac{(m-ibdn+1)(a+b \log(cx^n))}{bn}\right)}{2(m+1)}$$

Antiderivative was successfully verified.

[In] $\text{Int}[(e*x)^m*\text{CosIntegral}[d*(a + b*\text{Log}[c*x^n])], x]$

[Out] $((e*x)^{(1+m)}*\text{CosIntegral}[d*(a + b*\text{Log}[c*x^n])])/(e*(1+m)) - (x*(e*x)^m*\text{ExpIntegralEi}[((1+m - I*b*d*n)*(a + b*\text{Log}[c*x^n]))/(b*n)])/ (2*E^{((a*(1+m))/(b*n))* (1+m)*(c*x^n)^{((1+m)/n)}} - (x*(e*x)^m*\text{ExpIntegralEi}[((1+m + I*b*d*n)*(a + b*\text{Log}[c*x^n]))/(b*n)])/ (2*E^{((a*(1+m))/(b*n))* (1+m)*(c*x^n)^{((1+m)/n)}})$

Rule 6527

$\text{Int}[\text{CosIntegral}[(a_.) + \text{Log}[(c_.)*(x_.)^{(n_.)}]*(b_.)]*(d_.)]*(e_.)*(x_.)^{(m_.)}, x_Symbol] :> \text{Simp}[(e*x)^{(m+1)}*\text{CosIntegral}[d*(a + b*\text{Log}[c*x^n])]/(e*(m+1)), x] - \text{Dist}[(b*d*n)/(m+1), \text{Int}[(e*x)^m*\text{Cos}[d*(a + b*\text{Log}[c*x^n])]]/(d*(a + b*\text{Log}[c*x^n])), x], x] /; \text{FreeQ}\{a, b, c, d, e, m, n, x\} \&\& \text{NeQ}[m, -1]$

Rule 12

$\text{Int}[(a_)*(u_), x_Symbol] :> \text{Dist}[a, \text{Int}[u, x], x] /; \text{FreeQ}[a, x] \&\& !\text{MatchQ}[u, (b_)*(v_)] /; \text{FreeQ}[b, x]$

Rule 4498

$\text{Int}[\text{Cos}[(a_.) + \text{Log}[(c_.)*(x_.)^{(n_.)}]*(b_.)]*(d_.)]*((e_.) + \text{Log}[(g_.)*(x_.)^{(m_.)}]*(f_.)]*(h_.)^{(q_.)}*((i_.)*(x_.)^{(r_.)}, x_Symbol] :> \text{Dist}[(i*x)^r/(E^{(I*a*d)*(c*x^n)^{(I*b*d)}*(2*x^{(r - I*b*d*n)})}), \text{Int}[x^{(r - I*b*d*n)}*(h*(e + f*\text{Log}[g*x^m]))^q, x], x] + \text{Dist}[(E^{(I*a*d)}*(i*x)^r*(c*x^n)^{(I*b*d)})/(2*x^{(r + I*b*d*n)}), \text{Int}[x^{(r + I*b*d*n)}*(h*(e + f*\text{Log}[g*x^m]))^q, x], x] /; \text{FreeQ}\{a, b, c, d, e, f, g, h, i, m, n, q, r, x\}$

Rule 2310

$\text{Int}[(a_.) + \text{Log}[(c_.)*(x_.)^{(n_.)}]*(b_.)]^{(p_.)}*((d_.)*(x_.)^{(m_.)}, x_Symbol] :> \text{Dist}[(d*x)^{(m+1)}/(d*n*(c*x^n)^{((m+1)/n)}), \text{Subst}[\text{Int}[E^{((m+1)*x}$

$/n)(a + b*x)^p, x], x, \text{Log}[c*x^n], x] /; \text{FreeQ}\{a, b, c, d, m, n, p\}, x]$

Rule 2178

$\text{Int}[(F_)^{(g_)*((e_)+(f_)*(x_))}/((c_)+(d_)*(x_)), x_Symbol] := \text{Simp}[(F^{(g*(e - (c*f)/d)})*\text{ExpIntegralEi}[(f*g*(c + d*x)*\text{Log}[F])/d])/d, x] /; \text{FreeQ}\{F, c, d, e, f, g\}, x] \&\& \text{!}\$UseGamma == \text{True}$

Rubi steps

$$\begin{aligned} \int (ex)^m \text{Ci}(d(a + b \log(cx^n))) dx &= \frac{(ex)^{1+m} \text{Ci}(d(a + b \log(cx^n)))}{e(1+m)} - \frac{(bdn) \int \frac{(ex)^m \cos(d(a+b \log(cx^n)))}{d(a+b \log(cx^n))} dx}{1+m} \\ &= \frac{(ex)^{1+m} \text{Ci}(d(a + b \log(cx^n)))}{e(1+m)} - \frac{(bn) \int \frac{(ex)^m \cos(d(a+b \log(cx^n)))}{a+b \log(cx^n)} dx}{1+m} \\ &= \frac{(ex)^{1+m} \text{Ci}(d(a + b \log(cx^n)))}{e(1+m)} - \frac{(be^{-iad} n x^{-m+ibdn} (ex)^m (cx^n)^{-ibd}) \int \frac{x^{m-ibdn}}{a+b \log(cx^n)} dx}{2(1+m)} \\ &= \frac{(ex)^{1+m} \text{Ci}(d(a + b \log(cx^n)))}{e(1+m)} - \frac{(be^{-iad} x (ex)^m (cx^n)^{-ibd - \frac{1+m-ibdn}{n}}) \text{Subst}\left(\int \frac{e^{\frac{(1+m-ibdn)x}{a+b \log(cx^n)}}}{a+b \log(cx^n)} dx\right)}{2(1+m)} \\ &= \frac{(ex)^{1+m} \text{Ci}(d(a + b \log(cx^n)))}{e(1+m)} - \frac{e^{-\frac{a(1+m)}{bn}} x (ex)^m (cx^n)^{-\frac{1+m}{n}} \text{Ei}\left(\frac{(1+m-ibdn)(a+b \log(cx^n))}{bn}\right)}{2(1+m)} \end{aligned}$$

Mathematica [A] time = 3.04162, size = 124, normalized size = 0.72

$$\frac{(ex)^m \left(2x \text{CosIntegral}(d(a + b \log(cx^n))) - x^{-m} \exp\left(-\frac{(m+1)(a+b \log(cx^n)) - bn \log(x)}{bn}\right) \right) \left(\text{ExpIntegralEi}\left(\frac{(-ibdn+m+1)(a+b \log(cx^n))}{bn}\right) \right)}{2(m+1)}$$

Antiderivative was successfully verified.

[In] Integrate[(e*x)^m * CosIntegral[d*(a + b*Log[c*x^n])], x]

[Out] ((e*x)^m * (2*x * CosIntegral[d*(a + b*Log[c*x^n])] - (ExpIntegralEi[((1 + m - I*b*d*n)*(a + b*Log[c*x^n])]/(b*n)] + ExpIntegralEi[((1 + m + I*b*d*n)*(a + b*Log[c*x^n])]/(b*n)])) / (E^(((1 + m)*(a - b*n*Log[x] + b*Log[c*x^n])) / (b*n)) * x^m)) / (2*(1 + m))

Maple [F] time = 0.082, size = 0, normalized size = 0.

$$\int (ex)^m \text{Ci}(d(a + b \ln(cx^n))) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e*x)^m * Ci(d*(a+b*ln(c*x^n))), x)

[Out] int((e*x)^m * Ci(d*(a+b*ln(c*x^n))), x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int (ex)^m \operatorname{Ci}((b \log(cx^n) + a)d) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e*x)^m*Ci(d*(a+b*log(c*x^n))),x, algorithm="maxima")

[Out] integrate((e*x)^m*Ci((b*log(c*x^n) + a)*d), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}\left((ex)^m \operatorname{Ci}(bd \log(cx^n) + ad), x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e*x)^m*Ci(d*(a+b*log(c*x^n))),x, algorithm="fricas")

[Out] integral((e*x)^m*cos_integral(b*d*log(c*x^n) + a*d), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int (ex)^m \operatorname{Ci}(ad + bd \log(cx^n)) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e*x)**m*Ci(d*(a+b*ln(c*x**n))),x)

[Out] Integral((e*x)**m*Ci(a*d + b*d*log(c*x**n)), x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e*x)^m*Ci(d*(a+b*log(c*x^n))),x, algorithm="giac")

[Out] Timed out

3.107 $\int \frac{\text{CosIntegral}(bx) \sin(bx)}{x^3} dx$

Optimal. Leaf size=102

$$-\frac{1}{2}b^2 \text{CannotIntegrate}\left(\frac{\text{CosIntegral}(bx) \sin(bx)}{x}, x\right) - b^2 \text{Si}(2bx) - \frac{\text{CosIntegral}(bx) \sin(bx)}{2x^2} - \frac{b \text{CosIntegral}(bx)}{2x}$$

[Out] $-(b^2 \text{CannotIntegrate}[(\text{CosIntegral}[b*x] * \text{Sin}[b*x])/x, x])/2 - (b * \text{Cos}[b*x]^2)/(2*x) - (b * \text{Cos}[2*b*x])/(4*x) - (b * \text{Cos}[b*x] * \text{CosIntegral}[b*x])/(2*x) - (\text{CosIntegral}[b*x] * \text{Sin}[b*x])/(2*x^2) - \text{Sin}[2*b*x]/(8*x^2) - b^2 * \text{SinIntegral}[2*b*x]$

Rubi [A] time = 0.250831, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{CosIntegral}(bx) \sin(bx)}{x^3} dx$$

Verification is Not applicable to the result.

[In] $\text{Int}[(\text{CosIntegral}[b*x] * \text{Sin}[b*x])/x^3, x]$

[Out] $-(b * \text{Cos}[b*x]^2)/(2*x) - (b * \text{Cos}[2*b*x])/(4*x) - (b * \text{Cos}[b*x] * \text{CosIntegral}[b*x])/(2*x) - (\text{CosIntegral}[b*x] * \text{Sin}[b*x])/(2*x^2) - \text{Sin}[2*b*x]/(8*x^2) - b^2 * \text{SinIntegral}[2*b*x] - (b^2 * \text{Defer}[\text{Int}[(\text{CosIntegral}[b*x] * \text{Sin}[b*x])/x, x])/2$

Rubi steps

$$\begin{aligned} \int \frac{\text{Ci}(bx) \sin(bx)}{x^3} dx &= -\frac{\text{Ci}(bx) \sin(bx)}{2x^2} + \frac{1}{2}b \int \frac{\cos(bx) \text{Ci}(bx)}{x^2} dx + \frac{1}{2}b \int \frac{\cos(bx) \sin(bx)}{bx^3} dx \\ &= -\frac{b \cos(bx) \text{Ci}(bx)}{2x} - \frac{\text{Ci}(bx) \sin(bx)}{2x^2} + \frac{1}{2} \int \frac{\cos(bx) \sin(bx)}{x^3} dx + \frac{1}{2}b^2 \int \frac{\cos^2(bx)}{bx^2} dx - \frac{1}{2}b^2 \int \frac{\cos(bx) \sin(bx)}{bx^3} dx \\ &= -\frac{b \cos(bx) \text{Ci}(bx)}{2x} - \frac{\text{Ci}(bx) \sin(bx)}{2x^2} + \frac{1}{2} \int \frac{\sin(2bx)}{2x^3} dx + \frac{1}{2}b \int \frac{\cos^2(bx)}{x^2} dx - \frac{1}{2}b^2 \int \frac{\text{Ci}(bx) \sin(bx)}{bx^3} dx \\ &= -\frac{b \cos^2(bx)}{2x} - \frac{b \cos(bx) \text{Ci}(bx)}{2x} - \frac{\text{Ci}(bx) \sin(bx)}{2x^2} + \frac{1}{4} \int \frac{\sin(2bx)}{x^3} dx - \frac{1}{2}b^2 \int \frac{\text{Ci}(bx) \sin(bx)}{x} dx \\ &= -\frac{b \cos^2(bx)}{2x} - \frac{b \cos(bx) \text{Ci}(bx)}{2x} - \frac{\text{Ci}(bx) \sin(bx)}{2x^2} - \frac{\sin(2bx)}{8x^2} + \frac{1}{4}b \int \frac{\cos(2bx)}{x^2} dx - \frac{1}{2}b^2 \int \frac{\text{Ci}(bx) \sin(bx)}{x} dx \\ &= -\frac{b \cos^2(bx)}{2x} - \frac{b \cos(2bx)}{4x} - \frac{b \cos(bx) \text{Ci}(bx)}{2x} - \frac{\text{Ci}(bx) \sin(bx)}{2x^2} - \frac{\sin(2bx)}{8x^2} - \frac{1}{2}b^2 \text{Si}(2bx) - \frac{1}{2}b^2 \int \frac{\text{Ci}(bx) \sin(bx)}{x} dx \\ &= -\frac{b \cos^2(bx)}{2x} - \frac{b \cos(2bx)}{4x} - \frac{b \cos(bx) \text{Ci}(bx)}{2x} - \frac{\text{Ci}(bx) \sin(bx)}{2x^2} - \frac{\sin(2bx)}{8x^2} - b^2 \text{Si}(2bx) - \frac{1}{2}b^2 \int \frac{\text{Ci}(bx) \sin(bx)}{x} dx \end{aligned}$$

Mathematica [A] time = 1.46596, size = 0, normalized size = 0.

$$\int \frac{\text{CosIntegral}(bx) \sin(bx)}{x^3} dx$$

Verification is Not applicable to the result.

[In] $\text{Integrate}[(\text{CosIntegral}[b*x] * \text{Sin}[b*x])/x^3, x]$

[Out] Integrate[(CosIntegral[b*x]*Sin[b*x])/x^3, x]

Maple [A] time = 0.056, size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx) \sin(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x)*sin(b*x)/x^3,x)

[Out] int(Ci(b*x)*sin(b*x)/x^3,x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx) \sin(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)*sin(b*x)/x^3,x, algorithm="maxima")

[Out] integrate(Ci(b*x)*sin(b*x)/x^3, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bx) \sin(bx)}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)*sin(b*x)/x^3,x, algorithm="fricas")

[Out] integral(cos_integral(b*x)*sin(b*x)/x^3, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sin(bx) \text{Ci}(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)*sin(b*x)/x**3,x)

[Out] Integral(sin(b*x)*Ci(b*x)/x**3, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx) \sin(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x)*sin(b*x)/x^3,x, algorithm="giac")
```

```
[Out] integrate(Ci(b*x)*sin(b*x)/x^3, x)
```

3.108 $\int \frac{\text{CosIntegral}(bx) \sin(bx)}{x^2} dx$

Optimal. Leaf size=44

$$\frac{1}{2}b\text{CosIntegral}(bx)^2 + b\text{CosIntegral}(2bx) - \frac{\text{CosIntegral}(bx) \sin(bx)}{x} - \frac{\sin(2bx)}{2x}$$

[Out] (b*CosIntegral[b*x]^2)/2 + b*CosIntegral[2*b*x] - (CosIntegral[b*x]*Sin[b*x])/x - Sin[2*b*x]/(2*x)

Rubi [A] time = 0.102781, antiderivative size = 44, normalized size of antiderivative = 1., number of steps used = 7, number of rules used = 6, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.5$, Rules used = {6522, 6686, 12, 4406, 3297, 3302}

$$\frac{1}{2}b\text{CosIntegral}(bx)^2 + b\text{CosIntegral}(2bx) - \frac{\text{CosIntegral}(bx) \sin(bx)}{x} - \frac{\sin(2bx)}{2x}$$

Antiderivative was successfully verified.

[In] Int[(CosIntegral[b*x]*Sin[b*x])/x^2,x]

[Out] (b*CosIntegral[b*x]^2)/2 + b*CosIntegral[2*b*x] - (CosIntegral[b*x]*Sin[b*x])/x - Sin[2*b*x]/(2*x)

Rule 6522

```
Int[CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_)*Sin[(a_.) + (b_.)*(x_)], x_Symbol] := Simp[((e + f*x)^(m + 1)*Sin[a + b*x]*CosIntegral[c + d*x])/(f*(m + 1)), x] + (-Dist[b/(f*(m + 1)), Int[(e + f*x)^(m + 1)*Cos[a + b*x]*CosIntegral[c + d*x], x], x] - Dist[d/(f*(m + 1)), Int[((e + f*x)^(m + 1)*Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && ILtQ[m, -1]
```

Rule 6686

```
Int[(u_)*(y_)^(m_.), x_Symbol] := With[{q = DerivativeDivides[y, u, x]}, Simp[(q*y^(m + 1))/(m + 1), x] /; !FalseQ[q]] /; FreeQ[m, x] && NeQ[m, -1]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 3297

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)], x_Symbol] := Simp[((c + d*x)^(m + 1)*Sin[e + f*x])/(d*(m + 1)), x] - Dist[f/(d*(m + 1)), Int[(c + d*x)^(m + 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && LtQ[m, -1]
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rubi steps

$$\begin{aligned}
 \int \frac{\text{Ci}(bx) \sin(bx)}{x^2} dx &= -\frac{\text{Ci}(bx) \sin(bx)}{x} + b \int \frac{\cos(bx) \text{Ci}(bx)}{x} dx + b \int \frac{\cos(bx) \sin(bx)}{bx^2} dx \\
 &= \frac{1}{2} b \text{Ci}(bx)^2 - \frac{\text{Ci}(bx) \sin(bx)}{x} + \int \frac{\cos(bx) \sin(bx)}{x^2} dx \\
 &= \frac{1}{2} b \text{Ci}(bx)^2 - \frac{\text{Ci}(bx) \sin(bx)}{x} + \int \frac{\sin(2bx)}{2x^2} dx \\
 &= \frac{1}{2} b \text{Ci}(bx)^2 - \frac{\text{Ci}(bx) \sin(bx)}{x} + \frac{1}{2} \int \frac{\sin(2bx)}{x^2} dx \\
 &= \frac{1}{2} b \text{Ci}(bx)^2 - \frac{\text{Ci}(bx) \sin(bx)}{x} - \frac{\sin(2bx)}{2x} + b \int \frac{\cos(2bx)}{x} dx \\
 &= \frac{1}{2} b \text{Ci}(bx)^2 + b \text{Ci}(2bx) - \frac{\text{Ci}(bx) \sin(bx)}{x} - \frac{\sin(2bx)}{2x}
 \end{aligned}$$

Mathematica [A] time = 0.0095825, size = 44, normalized size = 1.

$$\frac{1}{2} b \text{CosIntegral}(bx)^2 + b \text{CosIntegral}(2bx) - \frac{\text{CosIntegral}(bx) \sin(bx)}{x} - \frac{\sin(2bx)}{2x}$$

Antiderivative was successfully verified.

```
[In] Integrate[(CosIntegral[b*x]*Sin[b*x])/x^2,x]
```

```
[Out] (b*CosIntegral[b*x]^2)/2 + b*CosIntegral[2*b*x] - (CosIntegral[b*x]*Sin[b*x])/x - Sin[2*b*x]/(2*x)
```

Maple [F] time = 0.059, size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx) \sin(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(Ci(b*x)*sin(b*x)/x^2,x)
```

```
[Out] int(Ci(b*x)*sin(b*x)/x^2,x)
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx) \sin(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x)*sin(b*x)/x^2,x, algorithm="maxima")
```

[Out] integrate(Ci(b*x)*sin(b*x)/x^2, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bx)\sin(bx)}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)*sin(b*x)/x^2,x, algorithm="fricas")

[Out] integral(cos_integral(b*x)*sin(b*x)/x^2, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sin(bx)\text{Ci}(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)*sin(b*x)/x**2,x)

[Out] Integral(sin(b*x)*Ci(b*x)/x**2, x)

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx)\sin(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)*sin(b*x)/x^2,x, algorithm="giac")

[Out] integrate(Ci(b*x)*sin(b*x)/x^2, x)

$$3.109 \quad \int \frac{\text{CosIntegral}(bx) \sin(bx)}{x} dx$$

Optimal. Leaf size=14

$$\text{CannotIntegrate}\left(\frac{\text{CosIntegral}(bx) \sin(bx)}{x}, x\right)$$

[Out] CannotIntegrate[(CosIntegral[b*x]*Sin[b*x])/x, x]

Rubi [A] time = 0.0265349, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{CosIntegral}(bx) \sin(bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Int[(CosIntegral[b*x]*Sin[b*x])/x,x]

[Out] Defer[Int] [(CosIntegral[b*x]*Sin[b*x])/x, x]

Rubi steps

$$\int \frac{\text{Ci}(bx) \sin(bx)}{x} dx = \int \frac{\text{Ci}(bx) \sin(bx)}{x} dx$$

Mathematica [A] time = 2.05059, size = 0, normalized size = 0.

$$\int \frac{\text{CosIntegral}(bx) \sin(bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[(CosIntegral[b*x]*Sin[b*x])/x,x]

[Out] Integrate[(CosIntegral[b*x]*Sin[b*x])/x, x]

Maple [A] time = 0.057, size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx) \sin(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x)*sin(b*x)/x,x)

[Out] int(Ci(b*x)*sin(b*x)/x,x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx) \sin(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)*sin(b*x)/x,x, algorithm="maxima")

[Out] integrate(Ci(b*x)*sin(b*x)/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bx) \sin(bx)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)*sin(b*x)/x,x, algorithm="fricas")

[Out] integral(cos_integral(b*x)*sin(b*x)/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sin(bx) \text{Ci}(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)*sin(b*x)/x,x)

[Out] Integral(sin(b*x)*Ci(b*x)/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx) \sin(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)*sin(b*x)/x,x, algorithm="giac")

[Out] integrate(Ci(b*x)*sin(b*x)/x, x)

3.110 $\int \text{CosIntegral}(bx) \sin(bx) dx$

Optimal. Leaf size=35

$$\frac{\text{CosIntegral}(2bx)}{2b} - \frac{\text{CosIntegral}(bx) \cos(bx)}{b} + \frac{\log(x)}{2b}$$

[Out] $-\left(\frac{\text{Cos}[b*x]*\text{CosIntegral}[b*x]}{b}\right) + \frac{\text{CosIntegral}[2*b*x]}{(2*b)} + \frac{\text{Log}[x]}{(2*b)}$

Rubi [A] time = 0.0612325, antiderivative size = 35, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 4, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.444$, Rules used = {6518, 12, 3312, 3302}

$$\frac{\text{CosIntegral}(2bx)}{2b} - \frac{\text{CosIntegral}(bx) \cos(bx)}{b} + \frac{\log(x)}{2b}$$

Antiderivative was successfully verified.

[In] Int[CosIntegral[b*x]*Sin[b*x],x]

[Out] $-\left(\frac{\text{Cos}[b*x]*\text{CosIntegral}[b*x]}{b}\right) + \frac{\text{CosIntegral}[2*b*x]}{(2*b)} + \frac{\text{Log}[x]}{(2*b)}$

Rule 6518

Int[CosIntegral[(c_.) + (d_.)*(x_)]*Sin[(a_.) + (b_.)*(x_)], x_Symbol] := -Simp[(Cos[a + b*x]*CosIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 3312

Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned}
\int \text{Ci}(bx) \sin(bx) dx &= -\frac{\cos(bx)\text{Ci}(bx)}{b} + \int \frac{\cos^2(bx)}{bx} dx \\
&= -\frac{\cos(bx)\text{Ci}(bx)}{b} + \frac{\int \frac{\cos^2(bx)}{x} dx}{b} \\
&= -\frac{\cos(bx)\text{Ci}(bx)}{b} + \frac{\int \left(\frac{1}{2x} + \frac{\cos(2bx)}{2x}\right) dx}{b} \\
&= -\frac{\cos(bx)\text{Ci}(bx)}{b} + \frac{\log(x)}{2b} + \frac{\int \frac{\cos(2bx)}{x} dx}{2b} \\
&= -\frac{\cos(bx)\text{Ci}(bx)}{b} + \frac{\text{Ci}(2bx)}{2b} + \frac{\log(x)}{2b}
\end{aligned}$$

Mathematica [A] time = 0.0132629, size = 37, normalized size = 1.06

$$\frac{\text{CosIntegral}(2bx)}{2b} - \frac{\text{CosIntegral}(bx) \cos(bx)}{b} + \frac{\log(bx)}{2b}$$

Antiderivative was successfully verified.

[In] Integrate[CosIntegral[b*x]*Sin[b*x],x]

[Out] -((Cos[b*x]*CosIntegral[b*x])/b) + CosIntegral[2*b*x]/(2*b) + Log[b*x]/(2*b)

Maple [A] time = 0.052, size = 34, normalized size = 1.

$$-\frac{\text{Ci}(bx) \cos(bx)}{b} + \frac{\ln(bx)}{2b} + \frac{\text{Ci}(2bx)}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x)*sin(b*x),x)

[Out] -Ci(b*x)*cos(b*x)/b+1/2/b*ln(b*x)+1/2*Ci(2*b*x)/b

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Ci}(bx) \sin(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)*sin(b*x),x, algorithm="maxima")

[Out] integrate(Ci(b*x)*sin(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(\text{Ci}(bx) \sin(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x)*sin(b*x),x, algorithm="fricas")
```

```
[Out] integral(cos_integral(b*x)*sin(b*x), x)
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \sin(bx) \operatorname{Ci}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x)*sin(b*x),x)
```

```
[Out] Integral(sin(b*x)*Ci(b*x), x)
```

Giac [A] time = 1.16776, size = 46, normalized size = 1.31

$$-\frac{\cos(bx) \operatorname{Ci}(bx)}{b} + \frac{\operatorname{Ci}(2bx) + \operatorname{Ci}(-2bx) + 2 \log(x)}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x)*sin(b*x),x, algorithm="giac")
```

```
[Out] -cos(b*x)*cos_integral(b*x)/b + 1/4*(cos_integral(2*b*x) + cos_integral(-2*
b*x) + 2*log(x))/b
```

3.111 $\int x \text{CosIntegral}(bx) \sin(bx) dx$

Optimal. Leaf size=62

$$\frac{\text{CosIntegral}(bx) \sin(bx)}{b^2} - \frac{\text{Si}(2bx)}{2b^2} + \frac{\sin(bx) \cos(bx)}{2b^2} - \frac{x \text{CosIntegral}(bx) \cos(bx)}{b} + \frac{x}{2b}$$

[Out] $x/(2*b) - (x*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/b + (\text{Cos}[b*x]*\text{Sin}[b*x])/(2*b^2) + (\text{CosIntegral}[b*x]*\text{Sin}[b*x])/b^2 - \text{SinIntegral}[2*b*x]/(2*b^2)$

Rubi [A] time = 0.0691263, antiderivative size = 62, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 7, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.7$, Rules used = {6520, 12, 2635, 8, 6512, 4406, 3299}

$$\frac{\text{CosIntegral}(bx) \sin(bx)}{b^2} - \frac{\text{Si}(2bx)}{2b^2} + \frac{\sin(bx) \cos(bx)}{2b^2} - \frac{x \text{CosIntegral}(bx) \cos(bx)}{b} + \frac{x}{2b}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x*\text{CosIntegral}[b*x]*\text{Sin}[b*x], x]$

[Out] $x/(2*b) - (x*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/b + (\text{Cos}[b*x]*\text{Sin}[b*x])/(2*b^2) + (\text{CosIntegral}[b*x]*\text{Sin}[b*x])/b^2 - \text{SinIntegral}[2*b*x]/(2*b^2)$

Rule 6520

$\text{Int}[\text{CosIntegral}[(c_.) + (d_.)*(x_.)]*((e_.) + (f_.)*(x_.))^{(m_.)*\text{Sin}[(a_.) + (b_.)*(x_.)], x_Symbol] :> -\text{Simp}[(e + f*x)^m*\text{Cos}[a + b*x]*\text{CosIntegral}[c + d*x])/b, x] + (\text{Dist}[d/b, \text{Int}[(e + f*x)^m*\text{Cos}[a + b*x]*\text{Cos}[c + d*x]]/(c + d*x), x], x] + \text{Dist}[(f*m)/b, \text{Int}[(e + f*x)^{m-1}*\text{Cos}[a + b*x]*\text{CosIntegral}[c + d*x], x], x) /; \text{FreeQ}\{a, b, c, d, e, f\}, x] \&\& \text{IGtQ}[m, 0]$

Rule 12

$\text{Int}[(a_)*(u_), x_Symbol] :> \text{Dist}[a, \text{Int}[u, x], x] /; \text{FreeQ}[a, x] \&\& !\text{MatchQ}[u, (b_)*(v_)] /; \text{FreeQ}[b, x]$

Rule 2635

$\text{Int}[(b_.)*\text{sin}[(c_.) + (d_.)*(x_.)]^{(n_.)}, x_Symbol] :> -\text{Simp}[(b*\text{Cos}[c + d*x])*(b*\text{Sin}[c + d*x])^{(n-1)})/(d*n), x] + \text{Dist}[(b^2*(n-1))/n, \text{Int}[(b*\text{Sin}[c + d*x])^{(n-2)}, x], x] /; \text{FreeQ}\{b, c, d\}, x] \&\& \text{GtQ}[n, 1] \&\& \text{IntegerQ}[2*n]$

Rule 8

$\text{Int}[a_, x_Symbol] :> \text{Simp}[a*x, x] /; \text{FreeQ}[a, x]$

Rule 6512

$\text{Int}[\text{Cos}[(a_.) + (b_.)*(x_.)]*\text{CosIntegral}[(c_.) + (d_.)*(x_.)], x_Symbol] :> \text{Simp}[(\text{Sin}[a + b*x]*\text{CosIntegral}[c + d*x])/b, x] - \text{Dist}[d/b, \text{Int}[(\text{Sin}[a + b*x]*\text{Cos}[c + d*x])/(c + d*x), x], x] /; \text{FreeQ}\{a, b, c, d\}, x]$

Rule 4406

$\text{Int}[\text{Cos}[(a_.) + (b_.)*(x_.)]^{(p_.)}*((c_.) + (d_.)*(x_.))^{(m_.)*\text{Sin}[(a_.) + (b_.)*(x_.)]^{(n_.)}, x_Symbol] :> \text{Int}[\text{ExpandTrigReduce}[(c + d*x)^m, \text{Sin}[a + b*x$

$]^n \cos[a + b*x]^p, x] /; \text{FreeQ}\{a, b, c, d, m\}, x\} \&\& \text{IGtQ}[n, 0] \&\& \text{IGtQ}[p, 0]$

Rule 3299

$\text{Int}[\sin[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] \text{ :> } \text{Simp}[\text{SinIntegral}[e + f*x]/d, x] /; \text{FreeQ}\{c, d, e, f\}, x\} \&\& \text{EqQ}[d*e - c*f, 0]$

Rubi steps

$$\begin{aligned} \int x \text{Ci}(bx) \sin(bx) dx &= -\frac{x \cos(bx) \text{Ci}(bx)}{b} + \frac{\int \cos(bx) \text{Ci}(bx) dx}{b} + \int \frac{\cos^2(bx)}{b} dx \\ &= -\frac{x \cos(bx) \text{Ci}(bx)}{b} + \frac{\text{Ci}(bx) \sin(bx)}{b^2} + \frac{\int \cos^2(bx) dx}{b} - \frac{\int \frac{\cos(bx) \sin(bx)}{bx} dx}{b} \\ &= -\frac{x \cos(bx) \text{Ci}(bx)}{b} + \frac{\cos(bx) \sin(bx)}{2b^2} + \frac{\text{Ci}(bx) \sin(bx)}{b^2} - \frac{\int \frac{\cos(bx) \sin(bx)}{x} dx}{b^2} + \frac{\int 1 dx}{2b} \\ &= \frac{x}{2b} - \frac{x \cos(bx) \text{Ci}(bx)}{b} + \frac{\cos(bx) \sin(bx)}{2b^2} + \frac{\text{Ci}(bx) \sin(bx)}{b^2} - \frac{\int \frac{\sin(2bx)}{2x} dx}{b^2} \\ &= \frac{x}{2b} - \frac{x \cos(bx) \text{Ci}(bx)}{b} + \frac{\cos(bx) \sin(bx)}{2b^2} + \frac{\text{Ci}(bx) \sin(bx)}{b^2} - \frac{\int \frac{\sin(2bx)}{x} dx}{2b^2} \\ &= \frac{x}{2b} - \frac{x \cos(bx) \text{Ci}(bx)}{b} + \frac{\cos(bx) \sin(bx)}{2b^2} + \frac{\text{Ci}(bx) \sin(bx)}{b^2} - \frac{\text{Si}(2bx)}{2b^2} \end{aligned}$$

Mathematica [A] time = 0.0504018, size = 44, normalized size = 0.71

$$\frac{\text{CosIntegral}(bx)(4 \sin(bx) - 4bx \cos(bx)) - 2\text{Si}(2bx) + 2bx + \sin(2bx)}{4b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*CosIntegral[b*x]*Sin[b*x],x]

[Out] (2*b*x + CosIntegral[b*x]*(-4*b*x*cos[b*x] + 4*Sin[b*x])) + Sin[2*b*x] - 2*SinIntegral[2*b*x])/(4*b^2)

Maple [A] time = 0.057, size = 45, normalized size = 0.7

$$\frac{1}{b^2} \left(\text{Ci}(bx) (-bx \cos(bx) + \sin(bx)) + \frac{\sin(bx) \cos(bx)}{2} + \frac{bx}{2} - \frac{\text{Si}(2bx)}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*Ci(b*x)*sin(b*x),x)

[Out] 1/b^2*(Ci(b*x)*(-b*x*cos(b*x)+sin(b*x))+1/2*sin(b*x)*cos(b*x)+1/2*b*x-1/2*Si(2*b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \text{Ci}(bx) \sin(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x)*sin(b*x),x, algorithm="maxima")

[Out] integrate(x*Ci(b*x)*sin(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

integral(x Ci(bx) sin(bx), x)

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x)*sin(b*x),x, algorithm="fricas")

[Out] integral(x*cos_integral(b*x)*sin(b*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \sin(bx) \operatorname{Ci}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x)*sin(b*x),x)

[Out] Integral(x*sin(b*x)*Ci(b*x), x)

Giac [C] time = 1.17779, size = 77, normalized size = 1.24

$$-\left(\frac{x \cos(bx)}{b} - \frac{\sin(bx)}{b^2}\right) \operatorname{Ci}(bx) + \frac{2bx - \Im(\operatorname{Ci}(2bx)) + \Im(\operatorname{Ci}(-2bx)) - 2 \operatorname{Si}(2bx)}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x)*sin(b*x),x, algorithm="giac")

[Out] -(x*cos(b*x)/b - sin(b*x)/b^2)*cos_integral(b*x) + 1/4*(2*b*x - imag_part(cos_integral(2*b*x)) + imag_part(cos_integral(-2*b*x)) - 2*sin_integral(2*b*x))/b^2

3.112 $\int x^2 \text{CosIntegral}(bx) \sin(bx) dx$

Optimal. Leaf size=111

$$-\frac{\text{CosIntegral}(2bx)}{b^3} + \frac{2x\text{CosIntegral}(bx)\sin(bx)}{b^2} + \frac{2\text{CosIntegral}(bx)\cos(bx)}{b^3} - \frac{\log(x)}{b^3} - \frac{\sin^2(bx)}{b^3} + \frac{\cos^2(bx)}{4b^3} + \dots$$

[Out] $x^2/(4*b) + \text{Cos}[b*x]^2/(4*b^3) + (2*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/b^3 - (x^2*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/b - \text{CosIntegral}[2*b*x]/b^3 - \text{Log}[x]/b^3 + (x*\text{Cos}[b*x]*\text{Sin}[b*x])/(2*b^2) + (2*x*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/b^2 - \text{Sin}[b*x]^2/b^3$

Rubi [A] time = 0.12765, antiderivative size = 111, normalized size of antiderivative = 1., number of steps used = 13, number of rules used = 9, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.75$, Rules used = {6520, 12, 3310, 30, 6514, 2564, 6518, 3312, 3302}

$$-\frac{\text{CosIntegral}(2bx)}{b^3} + \frac{2x\text{CosIntegral}(bx)\sin(bx)}{b^2} + \frac{2\text{CosIntegral}(bx)\cos(bx)}{b^3} - \frac{\log(x)}{b^3} - \frac{\sin^2(bx)}{b^3} + \frac{\cos^2(bx)}{4b^3} + \dots$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2*\text{CosIntegral}[b*x]*\text{Sin}[b*x], x]$

[Out] $x^2/(4*b) + \text{Cos}[b*x]^2/(4*b^3) + (2*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/b^3 - (x^2*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/b - \text{CosIntegral}[2*b*x]/b^3 - \text{Log}[x]/b^3 + (x*\text{Cos}[b*x]*\text{Sin}[b*x])/(2*b^2) + (2*x*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/b^2 - \text{Sin}[b*x]^2/b^3$

Rule 6520

$\text{Int}[\text{CosIntegral}[(c_.) + (d_.)*(x_.)]*((e_.) + (f_.)*(x_.))^{(m_.)*\text{Sin}[(a_.) + (b_.)*(x_.)]}, x_Symbol] \rightarrow -\text{Simp}[(e + f*x)^m*\text{Cos}[a + b*x]*\text{CosIntegral}[c + d*x]/b, x] + (\text{Dist}[d/b, \text{Int}[(e + f*x)^m*\text{Cos}[a + b*x]*\text{Cos}[c + d*x]/(c + d*x), x], x] + \text{Dist}[(f*m)/b, \text{Int}[(e + f*x)^{(m-1)}*\text{Cos}[a + b*x]*\text{CosIntegral}[c + d*x], x], x]) /; \text{FreeQ}\{a, b, c, d, e, f\}, x] \&\& \text{IGtQ}[m, 0]$

Rule 12

$\text{Int}[(a_.)*(u_.), x_Symbol] \rightarrow \text{Dist}[a, \text{Int}[u, x], x] /; \text{FreeQ}[a, x] \&\& !\text{MatchQ}[u, (b_.)*(v_.) /; \text{FreeQ}[b, x]]$

Rule 3310

$\text{Int}[(c_.) + (d_.)*(x_.)]*((b_.)*\text{Sin}[(e_.) + (f_.)*(x_.)])^{(n_.)}, x_Symbol] \rightarrow \text{Simp}[(d*(b*\text{Sin}[e + f*x])^n)/(f^2*n^2), x] + (\text{Dist}[(b^2*(n-1))/n, \text{Int}[(c + d*x)*(b*\text{Sin}[e + f*x])^{(n-2)}, x], x] - \text{Simp}[(b*(c + d*x)*\text{Cos}[e + f*x]*(b*\text{Sin}[e + f*x])^{(n-1)})/(f*n), x]) /; \text{FreeQ}\{b, c, d, e, f\}, x] \&\& \text{GtQ}[n, 1]$

Rule 30

$\text{Int}[(x_.)^{(m_.)}, x_Symbol] \rightarrow \text{Simp}[x^{(m+1)}/(m+1), x] /; \text{FreeQ}[m, x] \&\& \text{NeQ}[m, -1]$

Rule 6514

$\text{Int}[\text{Cos}[(a_.) + (b_.)*(x_.)]*\text{CosIntegral}[(c_.) + (d_.)*(x_.)]*((e_.) + (f_.)*(x_.))^{(m_.)}, x_Symbol] \rightarrow \text{Simp}[(e + f*x)^m*\text{Sin}[a + b*x]*\text{CosIntegral}[c + d*x]$

$x])/b, x] + (-\text{Dist}[d/b, \text{Int}[(e + f*x)^m*\text{Sin}[a + b*x]*\text{Cos}[c + d*x]]/(c + d*x), x], x] - \text{Dist}[(f*m)/b, \text{Int}[(e + f*x)^{m-1}*\text{Sin}[a + b*x]*\text{CosIntegral}[c + d*x], x], x]) /; \text{FreeQ}\{a, b, c, d, e, f\}, x\} \&\& \text{IGtQ}[m, 0]$

Rule 2564

$\text{Int}[\text{Cos}[(e_.) + (f_.)*(x_.)]^{(n_.)}*((a_.)*\text{sin}[(e_.) + (f_.)*(x_.)])^{(m_.)}, x_ \text{Symbol}] \text{:>} \text{Dist}[1/(a*f), \text{Subst}[\text{Int}[x^m*(1 - x^2/a^2)^{(n-1)/2}], x], x, a*\text{Sin}[e + f*x]], x] /; \text{FreeQ}\{a, e, f, m\}, x\} \&\& \text{IntegerQ}[(n-1)/2] \&\& !(\text{IntegerQ}[(m-1)/2] \&\& \text{LtQ}[0, m, n])$

Rule 6518

$\text{Int}[\text{CosIntegral}[(c_.) + (d_.)*(x_.)]*\text{Sin}[(a_.) + (b_.)*(x_.)], x_ \text{Symbol}] \text{:>} - \text{Simp}[(\text{Cos}[a + b*x]*\text{CosIntegral}[c + d*x])/b, x] + \text{Dist}[d/b, \text{Int}[(\text{Cos}[a + b*x]*\text{Cos}[c + d*x])/(c + d*x), x], x] /; \text{FreeQ}\{a, b, c, d\}, x\}$

Rule 3312

$\text{Int}[(c_.) + (d_.)*(x_.)]^{(m_.)}*\text{sin}[(e_.) + (f_.)*(x_.)]^{(n_.)}, x_ \text{Symbol}] \text{:>} \text{Int}[\text{ExpandTrigReduce}[(c + d*x)^m, \text{Sin}[e + f*x]^n, x], x] /; \text{FreeQ}\{c, d, e, f, m\}, x\} \&\& \text{IGtQ}[n, 1] \&\& (!\text{RationalQ}[m] \|\| (\text{GeQ}[m, -1] \&\& \text{LtQ}[m, 1]))$

Rule 3302

$\text{Int}[\text{sin}[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_ \text{Symbol}] \text{:>} \text{Simp}[\text{CosIntegral}[e - \text{Pi}/2 + f*x]/d, x] /; \text{FreeQ}\{c, d, e, f\}, x\} \&\& \text{EqQ}[d*(e - \text{Pi}/2) - c*f, 0]$

Rubi steps

$$\begin{aligned} \int x^2 \text{Ci}(bx) \sin(bx) dx &= -\frac{x^2 \cos(bx) \text{Ci}(bx)}{b} + \frac{2 \int x \cos(bx) \text{Ci}(bx) dx}{b} + \int \frac{x \cos^2(bx)}{b} dx \\ &= -\frac{x^2 \cos(bx) \text{Ci}(bx)}{b} + \frac{2x \text{Ci}(bx) \sin(bx)}{b^2} - \frac{2 \int \text{Ci}(bx) \sin(bx) dx}{b^2} + \frac{\int x \cos^2(bx) dx}{b} - \frac{2 \int \frac{\cos(bx)}{b}}{b} \\ &= \frac{\cos^2(bx)}{4b^3} + \frac{2 \cos(bx) \text{Ci}(bx)}{b^3} - \frac{x^2 \cos(bx) \text{Ci}(bx)}{b} + \frac{x \cos(bx) \sin(bx)}{2b^2} + \frac{2x \text{Ci}(bx) \sin(bx)}{b^2} - \frac{2 \int \frac{\cos(bx)}{b}}{b} \\ &= \frac{x^2}{4b} + \frac{\cos^2(bx)}{4b^3} + \frac{2 \cos(bx) \text{Ci}(bx)}{b^3} - \frac{x^2 \cos(bx) \text{Ci}(bx)}{b} + \frac{x \cos(bx) \sin(bx)}{2b^2} + \frac{2x \text{Ci}(bx) \sin(bx)}{b^2} \\ &= \frac{x^2}{4b} + \frac{\cos^2(bx)}{4b^3} + \frac{2 \cos(bx) \text{Ci}(bx)}{b^3} - \frac{x^2 \cos(bx) \text{Ci}(bx)}{b} + \frac{x \cos(bx) \sin(bx)}{2b^2} + \frac{2x \text{Ci}(bx) \sin(bx)}{b^2} \\ &= \frac{x^2}{4b} + \frac{\cos^2(bx)}{4b^3} + \frac{2 \cos(bx) \text{Ci}(bx)}{b^3} - \frac{x^2 \cos(bx) \text{Ci}(bx)}{b} - \frac{\log(x)}{b^3} + \frac{x \cos(bx) \sin(bx)}{2b^2} + \frac{2x \text{Ci}(bx) \sin(bx)}{b^2} \\ &= \frac{x^2}{4b} + \frac{\cos^2(bx)}{4b^3} + \frac{2 \cos(bx) \text{Ci}(bx)}{b^3} - \frac{x^2 \cos(bx) \text{Ci}(bx)}{b} - \frac{\text{Ci}(2bx)}{b^3} - \frac{\log(x)}{b^3} + \frac{x \cos(bx) \sin(bx)}{2b^2} \end{aligned}$$

Mathematica [A] time = 0.0859148, size = 72, normalized size = 0.65

$$\frac{-8 \text{CosIntegral}(bx) \left((b^2 x^2 - 2) \cos(bx) - 2bx \sin(bx) \right) + 2b^2 x^2 - 8 \text{CosIntegral}(2bx) + 2bx \sin(2bx) + 5 \cos(2bx) - 8 \log(x)}{8b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*CosIntegral[b*x]*Sin[b*x],x]

```
[Out] (2*b^2*x^2 + 5*Cos[2*b*x] - 8*CosIntegral[2*b*x] - 8*Log[x] - 8*CosIntegral
[b*x]*((-2 + b^2*x^2)*Cos[b*x] - 2*b*x*Sin[b*x]) + 2*b*x*Sin[2*b*x])/(8*b^3
)
```

Maple [A] time = 0.062, size = 107, normalized size = 1.

$$-\frac{x^2 \operatorname{Ci}(bx) \cos(bx)}{b} + 2 \frac{x \operatorname{Ci}(bx) \sin(bx)}{b^2} + 2 \frac{\operatorname{Ci}(bx) \cos(bx)}{b^3} + \frac{x \cos(bx) \sin(bx)}{2b^2} + \frac{x^2}{4b} - \frac{(\sin(bx))^2}{4b^3} + \frac{(\cos(bx))^2}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2*Ci(b*x)*sin(b*x),x)
```

```
[Out] -x^2*Ci(b*x)*cos(b*x)/b+2*x*Ci(b*x)*sin(b*x)/b^2+2*Ci(b*x)*cos(b*x)/b^3+1/2
*x*cos(b*x)*sin(b*x)/b^2+1/4*x^2/b-1/4*sin(b*x)^2/b^3+cos(b*x)^2/b^3-1/b^3*
ln(b*x)-Ci(2*b*x)/b^3
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \operatorname{Ci}(bx) \sin(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*Ci(b*x)*sin(b*x),x, algorithm="maxima")
```

```
[Out] integrate(x^2*Ci(b*x)*sin(b*x), x)
```

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}(x^2 \operatorname{Ci}(bx) \sin(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*Ci(b*x)*sin(b*x),x, algorithm="fricas")
```

```
[Out] integral(x^2*cos_integral(b*x)*sin(b*x), x)
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \sin(bx) \operatorname{Ci}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*Ci(b*x)*sin(b*x),x)
```

```
[Out] Integral(x**2*sin(b*x)*Ci(b*x), x)
```

Giac [A] time = 1.15272, size = 89, normalized size = 0.8

$$\left(\frac{2x \sin(bx)}{b^2} - \frac{(b^2x^2 - 2) \cos(bx)}{b^3} \right) \text{Ci}(bx) + \frac{b^2x^2 - 2 \text{Ci}(2bx) - 2 \text{Ci}(-2bx) - 4 \log(x)}{4b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x)*sin(b*x),x, algorithm="giac")

[Out] (2*x*sin(b*x)/b^2 - (b^2*x^2 - 2)*cos(b*x)/b^3)*cos_integral(b*x) + 1/4*(b^2*x^2 - 2*cos_integral(2*b*x) - 2*cos_integral(-2*b*x) - 4*log(x))/b^3

3.113 $\int x^3 \text{CosIntegral}(bx) \sin(bx) dx$

Optimal. Leaf size=147

$$\frac{3x^2 \text{CosIntegral}(bx) \sin(bx)}{b^2} - \frac{6 \text{CosIntegral}(bx) \sin(bx)}{b^4} + \frac{6x \text{CosIntegral}(bx) \cos(bx)}{b^3} + \frac{3 \text{Si}(2bx)}{b^4} + \frac{x^2 \sin(bx) \cos(bx)}{2b^2}$$

```
[Out] (-5*x)/(2*b^3) + x^3/(6*b) + (x*cos[b*x]^2)/(2*b^3) + (6*x*cos[b*x]*CosIntegral[b*x])/b^3 - (x^3*cos[b*x]*CosIntegral[b*x])/b - (4*cos[b*x]*Sin[b*x])/b^4 + (x^2*cos[b*x]*Sin[b*x])/(2*b^2) - (6*cosIntegral[b*x]*Sin[b*x])/b^4 + (3*x^2*cosIntegral[b*x]*Sin[b*x])/b^2 - (3*x*sin[b*x]^2)/(2*b^3) + (3*SineIntegral[2*b*x])/b^4
```

Rubi [A] time = 0.182771, antiderivative size = 147, normalized size of antiderivative = 1., number of steps used = 20, number of rules used = 11, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.917$, Rules used = {6520, 12, 3311, 30, 2635, 8, 6514, 3443, 6512, 4406, 3299}

$$\frac{3x^2 \text{CosIntegral}(bx) \sin(bx)}{b^2} - \frac{6 \text{CosIntegral}(bx) \sin(bx)}{b^4} + \frac{6x \text{CosIntegral}(bx) \cos(bx)}{b^3} + \frac{3 \text{Si}(2bx)}{b^4} + \frac{x^2 \sin(bx) \cos(bx)}{2b^2}$$

Antiderivative was successfully verified.

```
[In] Int[x^3*CosIntegral[b*x]*Sin[b*x],x]
```

```
[Out] (-5*x)/(2*b^3) + x^3/(6*b) + (x*cos[b*x]^2)/(2*b^3) + (6*x*cos[b*x]*CosIntegral[b*x])/b^3 - (x^3*cos[b*x]*CosIntegral[b*x])/b - (4*cos[b*x]*Sin[b*x])/b^4 + (x^2*cos[b*x]*Sin[b*x])/(2*b^2) - (6*cosIntegral[b*x]*Sin[b*x])/b^4 + (3*x^2*cosIntegral[b*x]*Sin[b*x])/b^2 - (3*x*sin[b*x]^2)/(2*b^3) + (3*SineIntegral[2*b*x])/b^4
```

Rule 6520

```
Int[CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)], x_Symbol] := -Simp[((e + f*x)^m*cos[a + b*x]*CosIntegral[c + d*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*cos[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Cos[a + b*x]*CosIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 3311

```
Int[((c_.) + (d_.)*(x_))^(m_.)*((b_.)*sin[(e_.) + (f_.)*(x_)])^(n_.), x_Symbol] := Simp[(d*m*(c + d*x)^(m - 1)*(b*sin[e + f*x])^n)/(f^2*n^2), x] + (Dist[(b^2*(n - 1))/n, Int[(c + d*x)^m*(b*sin[e + f*x])^(n - 2), x], x] - Dist[(d^2*m*(m - 1))/(f^2*n^2), Int[(c + d*x)^(m - 2)*(b*sin[e + f*x])^n, x], x] - Simp[(b*(c + d*x)^m*cos[e + f*x]*(b*sin[e + f*x])^(n - 1))/(f*n), x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && GtQ[m, 1]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]
```

Rule 2635

```
Int[((b_.)*sin[(c_.) + (d_.)*(x_)])^(n_), x_Symbol] := -Simp[(b*Cos[c + d*x]
)*(b*Sin[c + d*x])^(n - 1))/(d*n), x] + Dist[(b^2*(n - 1))/n, Int[(b*Sin[c
+ d*x])^(n - 2), x], x] /; FreeQ[{b, c, d}, x] && GtQ[n, 1] && IntegerQ[2*n
]
```

Rule 8

```
Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]
```

Rule 6514

```
Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*
(x_))^(m_.), x_Symbol] := Simp[((e + f*x)^m*Sin[a + b*x]*CosIntegral[c + d*
x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*Sin[a + b*x]*Cos[c + d*x])/(c + d*
x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Sin[a + b*x]*CosIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 3443

```
Int[Cos[(a_.) + (b_.)*(x_)^(n_.)]*(x_)^(m_.)*Sin[(a_.) + (b_.)*(x_)^(n_.)]^(
p_.), x_Symbol] := Simp[(x^(m - n + 1)*Sin[a + b*x^n]^(p + 1))/(b*n*(p + 1
)), x] - Dist[(m - n + 1)/(b*n*(p + 1)), Int[x^(m - n)*Sin[a + b*x^n]^(p +
1), x], x] /; FreeQ[{a, b, p}, x] && LtQ[0, n, m + 1] && NeQ[p, -1]
```

Rule 6512

```
Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := S
imp[(Sin[a + b*x]*CosIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]
*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b
_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x
]^(n)*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IG
tQ[p, 0]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int x^3 \text{Ci}(bx) \sin(bx) dx &= -\frac{x^3 \cos(bx) \text{Ci}(bx)}{b} + \frac{3 \int x^2 \cos(bx) \text{Ci}(bx) dx}{b} + \int \frac{x^2 \cos^2(bx)}{b} dx \\
&= -\frac{x^3 \cos(bx) \text{Ci}(bx)}{b} + \frac{3x^2 \text{Ci}(bx) \sin(bx)}{b^2} - \frac{6 \int x \text{Ci}(bx) \sin(bx) dx}{b^2} + \frac{\int x^2 \cos^2(bx) dx}{b} - \frac{3 \int x \cos(bx) \sin(bx) dx}{b^2} \\
&= \frac{x \cos^2(bx)}{2b^3} + \frac{6x \cos(bx) \text{Ci}(bx)}{b^3} - \frac{x^3 \cos(bx) \text{Ci}(bx)}{b} + \frac{x^2 \cos(bx) \sin(bx)}{2b^2} + \frac{3x^2 \text{Ci}(bx) \sin(bx)}{b^2} \\
&= \frac{x^3}{6b} + \frac{x \cos^2(bx)}{2b^3} + \frac{6x \cos(bx) \text{Ci}(bx)}{b^3} - \frac{x^3 \cos(bx) \text{Ci}(bx)}{b} - \frac{\cos(bx) \sin(bx)}{4b^4} + \frac{x^2 \cos(bx) \sin(bx)}{2b^2} \\
&= -\frac{x}{4b^3} + \frac{x^3}{6b} + \frac{x \cos^2(bx)}{2b^3} + \frac{6x \cos(bx) \text{Ci}(bx)}{b^3} - \frac{x^3 \cos(bx) \text{Ci}(bx)}{b} - \frac{4 \cos(bx) \sin(bx)}{b^4} + \frac{x^2 \cos(bx) \sin(bx)}{2b^2} \\
&= -\frac{5x}{2b^3} + \frac{x^3}{6b} + \frac{x \cos^2(bx)}{2b^3} + \frac{6x \cos(bx) \text{Ci}(bx)}{b^3} - \frac{x^3 \cos(bx) \text{Ci}(bx)}{b} - \frac{4 \cos(bx) \sin(bx)}{b^4} + \frac{x^2 \cos(bx) \sin(bx)}{2b^2} \\
&= -\frac{5x}{2b^3} + \frac{x^3}{6b} + \frac{x \cos^2(bx)}{2b^3} + \frac{6x \cos(bx) \text{Ci}(bx)}{b^3} - \frac{x^3 \cos(bx) \text{Ci}(bx)}{b} - \frac{4 \cos(bx) \sin(bx)}{b^4} + \frac{x^2 \cos(bx) \sin(bx)}{2b^2}
\end{aligned}$$

Mathematica [A] time = 0.107106, size = 94, normalized size = 0.64

$$\frac{-12 \text{CosIntegral}(bx) (bx (b^2 x^2 - 6) \cos(bx) - 3 (b^2 x^2 - 2) \sin(bx)) + 2b^3 x^3 + 3b^2 x^2 \sin(2bx) + 36 \text{Si}(2bx) - 36bx - 24}{12b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3*CosIntegral[b*x]*Sin[b*x],x]

[Out] (-36*b*x + 2*b^3*x^3 + 12*b*x*Cos[2*b*x] - 12*CosIntegral[b*x]*(b*x*(-6 + b^2*x^2)*Cos[b*x] - 3*(-2 + b^2*x^2)*Sin[b*x]) - 24*Sin[2*b*x] + 3*b^2*x^2*SinIntegral[2*b*x])/(12*b^4)

Maple [A] time = 0.076, size = 111, normalized size = 0.8

$$\frac{1}{b^4} \left(\text{Ci}(bx) (-b^3 x^3 \cos(bx) + 3b^2 x^2 \sin(bx) - 6 \sin(bx) + 6bx \cos(bx)) + b^2 x^2 \left(\frac{\sin(bx) \cos(bx)}{2} + \frac{bx}{2} \right) + 2bx \cos(bx) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3*Ci(b*x)*sin(b*x),x)

[Out] 1/b^4*(Ci(b*x)*(-b^3*x^3*cos(b*x)+3*b^2*x^2*sin(b*x)-6*sin(b*x)+6*b*x*cos(b*x))+b^2*x^2*(1/2*sin(b*x)*cos(b*x)+1/2*b*x)+2*b*x*cos(b*x)-4*sin(b*x)*cos(b*x)-4*b*x-1/3*x^3*b^3+3*Si(2*b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \text{Ci}(bx) \sin(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Ci(b*x)*sin(b*x),x, algorithm="maxima")

[Out] integrate(x^3*Ci(b*x)*sin(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^3 \text{Ci}(bx) \sin(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Ci(b*x)*sin(b*x),x, algorithm="fricas")

[Out] integral(x^3*cos_integral(b*x)*sin(b*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \sin(bx) \text{Ci}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*Ci(b*x)*sin(b*x),x)

[Out] Integral(x**3*sin(b*x)*Ci(b*x), x)

Giac [C] time = 1.23702, size = 116, normalized size = 0.79

$$-\left(\frac{(b^3 x^3 - 6bx) \cos(bx)}{b^4} - \frac{3(b^2 x^2 - 2) \sin(bx)}{b^4}\right) \text{Ci}(bx) + \frac{b^3 x^3 - 18bx + 9 \Im(\text{Ci}(2bx)) - 9 \Im(\text{Ci}(-2bx)) + 18 \text{Si}(2bx)}{6b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Ci(b*x)*sin(b*x),x, algorithm="giac")

[Out] -((b^3*x^3 - 6*b*x)*cos(b*x)/b^4 - 3*(b^2*x^2 - 2)*sin(b*x)/b^4)*cos_integr
al(b*x) + 1/6*(b^3*x^3 - 18*b*x + 9*imag_part(cos_integral(2*b*x)) - 9*imag
_part(cos_integral(-2*b*x)) + 18*sin_integral(2*b*x))/b^4

$$3.114 \quad \int \frac{\cos(bx)\text{CosIntegral}(bx)}{x^3} dx$$

Optimal. Leaf size=97

$$-\frac{1}{4}b^2\text{CosIntegral}(bx)^2 - b^2\text{CosIntegral}(2bx) - \frac{\text{CosIntegral}(bx)\cos(bx)}{2x^2} + \frac{b\text{CosIntegral}(bx)\sin(bx)}{2x} - \frac{\cos^2(bx)}{4x^2}$$

[Out] -Cos[b*x]^2/(4*x^2) - (Cos[b*x]*CosIntegral[b*x])/(2*x^2) - (b^2*CosIntegral[b*x]^2)/4 - b^2*CosIntegral[2*b*x] + (b*Cos[b*x]*Sin[b*x])/(2*x) + (b*CosIntegral[b*x]*Sin[b*x])/(2*x) + (b*Sine[2*b*x])/(4*x)

Rubi [A] time = 0.198593, antiderivative size = 97, normalized size of antiderivative = 1., number of steps used = 14, number of rules used = 10, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.833$, Rules used = {6516, 6522, 6686, 12, 4406, 3297, 3302, 3314, 29, 3312}

$$-\frac{1}{4}b^2\text{CosIntegral}(bx)^2 - b^2\text{CosIntegral}(2bx) - \frac{\text{CosIntegral}(bx)\cos(bx)}{2x^2} + \frac{b\text{CosIntegral}(bx)\sin(bx)}{2x} - \frac{\cos^2(bx)}{4x^2}$$

Antiderivative was successfully verified.

[In] Int[(Cos[b*x]*CosIntegral[b*x])/x^3,x]

[Out] -Cos[b*x]^2/(4*x^2) - (Cos[b*x]*CosIntegral[b*x])/(2*x^2) - (b^2*CosIntegral[b*x]^2)/4 - b^2*CosIntegral[2*b*x] + (b*Cos[b*x]*Sin[b*x])/(2*x) + (b*CosIntegral[b*x]*Sin[b*x])/(2*x) + (b*Sine[2*b*x])/(4*x)

Rule 6516

Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.), x_Symbol] := Simp[((e + f*x)^(m + 1)*Cos[a + b*x]*CosIntegral[c + d*x])/(f*(m + 1)), x] + (Dist[b/(f*(m + 1)), Int[(e + f*x)^(m + 1)*Sin[a + b*x]*CosIntegral[c + d*x], x], x] - Dist[d/(f*(m + 1)), Int[((e + f*x)^(m + 1)*Cos[a + b*x]*Cos[c + d*x])/(c + d*x), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && ILtQ[m, -1]

Rule 6522

Int[CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_)*Sin[(a_.) + (b_.)*(x_)], x_Symbol] := Simp[((e + f*x)^(m + 1)*Sin[a + b*x]*CosIntegral[c + d*x])/(f*(m + 1)), x] + (-Dist[b/(f*(m + 1)), Int[(e + f*x)^(m + 1)*Cos[a + b*x]*CosIntegral[c + d*x], x], x] - Dist[d/(f*(m + 1)), Int[((e + f*x)^(m + 1)*Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && ILtQ[m, -1]

Rule 6686

Int[(u_)*(y_)^(m_.), x_Symbol] := With[{q = DerivativeDivides[y, u, x]}, Simp[(q*y^(m + 1))/(m + 1), x] /; !FalseQ[q]] /; FreeQ[m, x] && NeQ[m, -1]

Rule 12

Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_)] /; FreeQ[b, x]

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^(n)*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 3297

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)], x_Symbol] := Simp[((c + d*x)^(m + 1)*Sin[e + f*x]/(d*(m + 1)), x] - Dist[f/(d*(m + 1)), Int[(c + d*x)^(m + 1)*Cos[e + f*x], x], x] /; FreeQ[{c, d, e, f}, x] && LtQ[m, -1]
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rule 3314

```
Int[((c_.) + (d_.)*(x_))^(m_)*((b_.)*sin[(e_.) + (f_.)*(x_)])^(n_), x_Symbol] := Simp[((c + d*x)^(m + 1)*(b*Sine[e + f*x])^n)/(d*(m + 1)), x] + (Dist[(b^2*f^2*n*(n - 1))/(d^2*(m + 1)*(m + 2)), Int[(c + d*x)^(m + 2)*(b*Sine[e + f*x])^(n - 2), x], x] - Dist[(f^2*n^2)/(d^2*(m + 1)*(m + 2)), Int[(c + d*x)^(m + 2)*(b*Sine[e + f*x])^n, x], x] - Simp[(b*f*n*(c + d*x)^(m + 2)*Cos[e + f*x]*(b*Sine[e + f*x])^(n - 1))/(d^2*(m + 1)*(m + 2)), x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1] && LtQ[m, -2]
```

Rule 29

```
Int[(x_)^(-1), x_Symbol] := Simp[Log[x], x]
```

Rule 3312

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)^(n_)], x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rubi steps

$$\begin{aligned}
 \int \frac{\cos(bx)\text{Ci}(bx)}{x^3} dx &= -\frac{\cos(bx)\text{Ci}(bx)}{2x^2} + \frac{1}{2}b \int \frac{\cos^2(bx)}{bx^3} dx - \frac{1}{2}b \int \frac{\text{Ci}(bx) \sin(bx)}{x^2} dx \\
 &= -\frac{\cos(bx)\text{Ci}(bx)}{2x^2} + \frac{b\text{Ci}(bx) \sin(bx)}{2x} + \frac{1}{2} \int \frac{\cos^2(bx)}{x^3} dx - \frac{1}{2}b^2 \int \frac{\cos(bx)\text{Ci}(bx)}{x} dx - \frac{1}{2}b^2 \int \frac{\cos(bx)\text{Ci}(bx)}{x} dx \\
 &= -\frac{\cos^2(bx)}{4x^2} - \frac{\cos(bx)\text{Ci}(bx)}{2x^2} - \frac{1}{4}b^2\text{Ci}(bx)^2 + \frac{b \cos(bx) \sin(bx)}{2x} + \frac{b\text{Ci}(bx) \sin(bx)}{2x} - \frac{1}{2}b \int \frac{\cos(bx)\text{Ci}(bx)}{x} dx \\
 &= -\frac{\cos^2(bx)}{4x^2} - \frac{\cos(bx)\text{Ci}(bx)}{2x^2} - \frac{1}{4}b^2\text{Ci}(bx)^2 + \frac{1}{2}b^2 \log(x) + \frac{b \cos(bx) \sin(bx)}{2x} + \frac{b\text{Ci}(bx) \sin(bx)}{2x} - \frac{1}{2}b \int \frac{\cos(bx)\text{Ci}(bx)}{x} dx \\
 &= -\frac{\cos^2(bx)}{4x^2} - \frac{\cos(bx)\text{Ci}(bx)}{2x^2} - \frac{1}{4}b^2\text{Ci}(bx)^2 + \frac{b \cos(bx) \sin(bx)}{2x} + \frac{b\text{Ci}(bx) \sin(bx)}{2x} - \frac{1}{4}b \int \frac{\sin(2bx)}{x^2} dx \\
 &= -\frac{\cos^2(bx)}{4x^2} - \frac{\cos(bx)\text{Ci}(bx)}{2x^2} - \frac{1}{4}b^2\text{Ci}(bx)^2 - \frac{1}{2}b^2\text{Ci}(2bx) + \frac{b \cos(bx) \sin(bx)}{2x} + \frac{b\text{Ci}(bx) \sin(bx)}{2x} - \frac{1}{4}b \int \frac{\sin(2bx)}{x^2} dx \\
 &= -\frac{\cos^2(bx)}{4x^2} - \frac{\cos(bx)\text{Ci}(bx)}{2x^2} - \frac{1}{4}b^2\text{Ci}(bx)^2 - b^2\text{Ci}(2bx) + \frac{b \cos(bx) \sin(bx)}{2x} + \frac{b\text{Ci}(bx) \sin(bx)}{2x} - \frac{1}{4}b \int \frac{\sin(2bx)}{x^2} dx
 \end{aligned}$$

Mathematica [A] time = 0.0138336, size = 97, normalized size = 1.

$$-\frac{1}{4}b^2\text{CosIntegral}(bx)^2 - b^2\text{CosIntegral}(2bx) - \frac{\text{CosIntegral}(bx)\cos(bx)}{2x^2} + \frac{b\text{CosIntegral}(bx)\sin(bx)}{2x} - \frac{\cos^2(bx)}{4x^2}$$

Antiderivative was successfully verified.

[In] Integrate[(Cos[b*x]*CosIntegral[b*x])/x^3,x]

[Out] -Cos[b*x]^2/(4*x^2) - (Cos[b*x]*CosIntegral[b*x])/(2*x^2) - (b^2*CosIntegral[b*x]^2)/4 - b^2*CosIntegral[2*b*x] + (b*Cos[b*x]*Sin[b*x])/(2*x) + (b*CosIntegral[b*x]*Sin[b*x])/(2*x) + (b*Sine[2*b*x])/(4*x)

Maple [F] time = 0.082, size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx)\cos(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x)*cos(b*x)/x^3,x)

[Out] int(Ci(b*x)*cos(b*x)/x^3,x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx)\cos(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)*cos(b*x)/x^3,x, algorithm="maxima")

[Out] integrate(Ci(b*x)*cos(b*x)/x^3, x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\cos(bx)\text{Ci}(bx)}{x^3}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)*cos(b*x)/x^3,x, algorithm="fricas")

[Out] integral(cos(b*x)*cos_integral(b*x)/x^3, x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\cos(bx)\text{Ci}(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x)*cos(b*x)/x**3,x)
```

```
[Out] Integral(cos(b*x)*Ci(b*x)/x**3, x)
```

Giac [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx) \cos(bx)}{x^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x)*cos(b*x)/x^3,x, algorithm="giac")
```

```
[Out] integrate(Ci(b*x)*cos(b*x)/x^3, x)
```


$$3.115 \quad \int \frac{\cos(bx)\text{CosIntegral}(bx)}{x^2} dx$$

Optimal. Leaf size=50

$$-b\text{CannotIntegrate}\left(\frac{\text{CosIntegral}(bx)\sin(bx)}{x}, x\right) - \frac{\text{CosIntegral}(bx)\cos(bx)}{x} - b\text{Si}(2bx) - \frac{\cos^2(bx)}{x}$$

[Out] -(b*CannotIntegrate[(CosIntegral[b*x]*Sin[b*x])/x, x]) - Cos[b*x]^2/x - (Cos[b*x]*CosIntegral[b*x])/x - b*SinIntegral[2*b*x]

Rubi [A] time = 0.0930662, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\cos(bx)\text{CosIntegral}(bx)}{x^2} dx$$

Verification is Not applicable to the result.

[In] Int[(Cos[b*x]*CosIntegral[b*x])/x^2, x]

[Out] -(Cos[b*x]^2/x) - (Cos[b*x]*CosIntegral[b*x])/x - b*SinIntegral[2*b*x] - b*Defer[Int] [(CosIntegral[b*x]*Sin[b*x])/x, x]

Rubi steps

$$\begin{aligned} \int \frac{\cos(bx)\text{Ci}(bx)}{x^2} dx &= -\frac{\cos(bx)\text{Ci}(bx)}{x} + b \int \frac{\cos^2(bx)}{bx^2} dx - b \int \frac{\text{Ci}(bx)\sin(bx)}{x} dx \\ &= -\frac{\cos(bx)\text{Ci}(bx)}{x} - b \int \frac{\text{Ci}(bx)\sin(bx)}{x} dx + \int \frac{\cos^2(bx)}{x^2} dx \\ &= -\frac{\cos^2(bx)}{x} - \frac{\cos(bx)\text{Ci}(bx)}{x} - b \int \frac{\text{Ci}(bx)\sin(bx)}{x} dx + (2b) \int -\frac{\sin(2bx)}{2x} dx \\ &= -\frac{\cos^2(bx)}{x} - \frac{\cos(bx)\text{Ci}(bx)}{x} - b \int \frac{\text{Ci}(bx)\sin(bx)}{x} dx - b \int \frac{\sin(2bx)}{x} dx \\ &= -\frac{\cos^2(bx)}{x} - \frac{\cos(bx)\text{Ci}(bx)}{x} - b\text{Si}(2bx) - b \int \frac{\text{Ci}(bx)\sin(bx)}{x} dx \end{aligned}$$

Mathematica [A] time = 0.444453, size = 0, normalized size = 0.

$$\int \frac{\cos(bx)\text{CosIntegral}(bx)}{x^2} dx$$

Verification is Not applicable to the result.

[In] Integrate[(Cos[b*x]*CosIntegral[b*x])/x^2, x]

[Out] Integrate[(Cos[b*x]*CosIntegral[b*x])/x^2, x]

Maple [A] time = 0.057, size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx)\cos(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(Ci(b*x)*cos(b*x)/x^2,x)`

[Out] `int(Ci(b*x)*cos(b*x)/x^2,x)`

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{Ci}(bx) \cos(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x)*cos(b*x)/x^2,x, algorithm="maxima")`

[Out] `integrate(Ci(b*x)*cos(b*x)/x^2, x)`

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}\left(\frac{\cos(bx) \operatorname{Ci}(bx)}{x^2}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x)*cos(b*x)/x^2,x, algorithm="fricas")`

[Out] `integral(cos(b*x)*cos_integral(b*x)/x^2, x)`

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\cos(bx) \operatorname{Ci}(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x)*cos(b*x)/x**2,x)`

[Out] `Integral(cos(b*x)*Ci(b*x)/x**2, x)`

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\operatorname{Ci}(bx) \cos(bx)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x)*cos(b*x)/x^2,x, algorithm="giac")`

[Out] `integrate(Ci(b*x)*cos(b*x)/x^2, x)`

$$3.116 \quad \int \frac{\cos(bx)\text{CosIntegral}(bx)}{x} dx$$

Optimal. Leaf size=10

$$\frac{1}{2}\text{CosIntegral}(bx)^2$$

[Out] CosIntegral[b*x]^2/2

Rubi [A] time = 0.0197507, antiderivative size = 10, normalized size of antiderivative = 1., number of steps used = 1, number of rules used = 1, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.083$, Rules used = {6686}

$$\frac{1}{2}\text{CosIntegral}(bx)^2$$

Antiderivative was successfully verified.

[In] Int[(Cos[b*x]*CosIntegral[b*x])/x,x]

[Out] CosIntegral[b*x]^2/2

Rule 6686

Int[(u_)*(y_)^(m_.), x_Symbol] :> With[{q = DerivativeDivides[y, u, x]}, Simp[(q*y^(m + 1))/(m + 1), x] /; !FalseQ[q]] /; FreeQ[m, x] && NeQ[m, -1]

Rubi steps

$$\int \frac{\cos(bx)\text{Ci}(bx)}{x} dx = \frac{\text{Ci}(bx)^2}{2}$$

Mathematica [A] time = 0.0031494, size = 10, normalized size = 1.

$$\frac{1}{2}\text{CosIntegral}(bx)^2$$

Antiderivative was successfully verified.

[In] Integrate[(Cos[b*x]*CosIntegral[b*x])/x,x]

[Out] CosIntegral[b*x]^2/2

Maple [A] time = 0.046, size = 9, normalized size = 0.9

$$\frac{(\text{Ci}(bx))^2}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x)*cos(b*x)/x,x)

[Out] $1/2 * \text{Ci}(b*x)^2$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx) \cos(bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x)*cos(b*x)/x,x, algorithm="maxima")`

[Out] `integrate(Ci(b*x)*cos(b*x)/x, x)`

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\cos(bx) \text{Ci}(bx)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x)*cos(b*x)/x,x, algorithm="fricas")`

[Out] `integral(cos(b*x)*cos_integral(b*x)/x, x)`

Sympy [A] time = 1.06805, size = 7, normalized size = 0.7

$$\frac{\text{Ci}^2(bx)}{2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x)*cos(b*x)/x,x)`

[Out] `Ci(b*x)**2/2`

Giac [A] time = 1.24342, size = 11, normalized size = 1.1

$$\frac{1}{2} \text{Ci}(bx)^2$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(Ci(b*x)*cos(b*x)/x,x, algorithm="giac")`

[Out] `1/2*cos_integral(b*x)^2`

3.117 $\int \cos(bx) \mathbf{CosIntegral}(bx) dx$

Optimal. Leaf size=25

$$\frac{\mathbf{CosIntegral}(bx) \sin(bx)}{b} - \frac{\mathbf{Si}(2bx)}{2b}$$

[Out] (CosIntegral[b*x]*Sin[b*x])/b - SinIntegral[2*b*x]/(2*b)

Rubi [A] time = 0.043309, antiderivative size = 25, normalized size of antiderivative = 1., number of steps used = 5, number of rules used = 4, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.444$, Rules used = {6512, 12, 4406, 3299}

$$\frac{\mathbf{CosIntegral}(bx) \sin(bx)}{b} - \frac{\mathbf{Si}(2bx)}{2b}$$

Antiderivative was successfully verified.

[In] Int[Cos[b*x]*CosIntegral[b*x],x]

[Out] (CosIntegral[b*x]*Sin[b*x])/b - SinIntegral[2*b*x]/(2*b)

Rule 6512

Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :> Simp[(Sin[a + b*x]*CosIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] :> Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n * Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned}
\int \cos(bx) \operatorname{Ci}(bx) dx &= \frac{\operatorname{Ci}(bx) \sin(bx)}{b} - \int \frac{\cos(bx) \sin(bx)}{bx} dx \\
&= \frac{\operatorname{Ci}(bx) \sin(bx)}{b} - \frac{\int \frac{\cos(bx) \sin(bx)}{x} dx}{b} \\
&= \frac{\operatorname{Ci}(bx) \sin(bx)}{b} - \frac{\int \frac{\sin(2bx)}{2x} dx}{b} \\
&= \frac{\operatorname{Ci}(bx) \sin(bx)}{b} - \frac{\int \frac{\sin(2bx)}{x} dx}{2b} \\
&= \frac{\operatorname{Ci}(bx) \sin(bx)}{b} - \frac{\operatorname{Si}(2bx)}{2b}
\end{aligned}$$

Mathematica [A] time = 0.0115221, size = 25, normalized size = 1.

$$\frac{\operatorname{CosIntegral}(bx) \sin(bx)}{b} - \frac{\operatorname{Si}(2bx)}{2b}$$

Antiderivative was successfully verified.

[In] Integrate[Cos[b*x]*CosIntegral[b*x],x]

[Out] (CosIntegral[b*x]*Sin[b*x])/b - SinIntegral[2*b*x]/(2*b)

Maple [A] time = 0.049, size = 22, normalized size = 0.9

$$\frac{1}{b} \left(\operatorname{Ci}(bx) \sin(bx) - \frac{\operatorname{Si}(2bx)}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x)*cos(b*x),x)

[Out] 1/b*(Ci(b*x)*sin(b*x)-1/2*Si(2*b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \operatorname{Ci}(bx) \cos(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x)*cos(b*x),x, algorithm="maxima")

[Out] integrate(Ci(b*x)*cos(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}(\cos(bx) \operatorname{Ci}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x)*cos(b*x),x, algorithm="fricas")
```

```
[Out] integral(cos(b*x)*cos_integral(b*x), x)
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \cos(bx) \operatorname{Ci}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x)*cos(b*x),x)
```

```
[Out] Integral(cos(b*x)*Ci(b*x), x)
```

Giac [C] time = 1.25457, size = 54, normalized size = 2.16

$$\frac{\operatorname{Ci}(bx) \sin(bx)}{b} - \frac{\Im(\operatorname{Ci}(2bx)) - \Im(\operatorname{Ci}(-2bx)) + 2 \operatorname{Si}(2bx)}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x)*cos(b*x),x, algorithm="giac")
```

```
[Out] cos_integral(b*x)*sin(b*x)/b - 1/4*(imag_part(cos_integral(2*b*x)) - imag_p
art(cos_integral(-2*b*x)) + 2*sin_integral(2*b*x))/b
```

3.118 $\int x \cos(bx) \text{CosIntegral}(bx) dx$

Optimal. Leaf size=60

$$-\frac{\text{CosIntegral}(2bx)}{2b^2} + \frac{\text{CosIntegral}(bx) \cos(bx)}{b^2} - \frac{\log(x)}{2b^2} - \frac{\sin^2(bx)}{2b^2} + \frac{x \text{CosIntegral}(bx) \sin(bx)}{b}$$

[Out] (Cos[b*x]*CosIntegral[b*x])/b^2 - CosIntegral[2*b*x]/(2*b^2) - Log[x]/(2*b^2) + (x*CosIntegral[b*x]*Sin[b*x])/b - Sin[b*x]^2/(2*b^2)

Rubi [A] time = 0.0802722, antiderivative size = 60, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 7, integrand size = 10, $\frac{\text{number of rules}}{\text{integrand size}} = 0.7$, Rules used = {6514, 12, 2564, 30, 6518, 3312, 3302}

$$-\frac{\text{CosIntegral}(2bx)}{2b^2} + \frac{\text{CosIntegral}(bx) \cos(bx)}{b^2} - \frac{\log(x)}{2b^2} - \frac{\sin^2(bx)}{2b^2} + \frac{x \text{CosIntegral}(bx) \sin(bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[x*Cos[b*x]*CosIntegral[b*x],x]

[Out] (Cos[b*x]*CosIntegral[b*x])/b^2 - CosIntegral[2*b*x]/(2*b^2) - Log[x]/(2*b^2) + (x*CosIntegral[b*x]*Sin[b*x])/b - Sin[b*x]^2/(2*b^2)

Rule 6514

```
Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.), x_Symbol] :> Simp[((e + f*x)^m*Sin[a + b*x]*CosIntegral[c + d*x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Sin[a + b*x]*CosIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 2564

```
Int[cos[(e_.) + (f_.)*(x_)]^(n_.)*((a_.)*sin[(e_.) + (f_.)*(x_)])^(m_.), x_Symbol] :> Dist[1/(a*f), Subst[Int[x^m*(1 - x^2/a^2)^((n - 1)/2), x], x, a*Sin[e + f*x]], x] /; FreeQ[{a, e, f, m}, x] && IntegerQ[(n - 1)/2] && !(IntegerQ[(m - 1)/2] && LtQ[0, m, n])
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]
```

Rule 6518

```
Int[CosIntegral[(c_.) + (d_.)*(x_)]*Sin[(a_.) + (b_.)*(x_)], x_Symbol] :> -Simp[(Cos[a + b*x]*CosIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 3312


```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := Int
t[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f
, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int x \cos(bx) \operatorname{Ci}(bx) dx &= \frac{x \operatorname{Ci}(bx) \sin(bx)}{b} - \frac{\int \operatorname{Ci}(bx) \sin(bx) dx}{b} - \int \frac{\cos(bx) \sin(bx)}{b} dx \\
&= \frac{\cos(bx) \operatorname{Ci}(bx)}{b^2} + \frac{x \operatorname{Ci}(bx) \sin(bx)}{b} - \frac{\int \frac{\cos^2(bx)}{bx} dx}{b} - \frac{\int \cos(bx) \sin(bx) dx}{b} \\
&= \frac{\cos(bx) \operatorname{Ci}(bx)}{b^2} + \frac{x \operatorname{Ci}(bx) \sin(bx)}{b} - \frac{\int \frac{\cos^2(bx)}{x} dx}{b^2} - \frac{\operatorname{Subst}(\int x dx, x, \sin(bx))}{b^2} \\
&= \frac{\cos(bx) \operatorname{Ci}(bx)}{b^2} + \frac{x \operatorname{Ci}(bx) \sin(bx)}{b} - \frac{\sin^2(bx)}{2b^2} - \frac{\int \left(\frac{1}{2x} + \frac{\cos(2bx)}{2x} \right) dx}{b^2} \\
&= \frac{\cos(bx) \operatorname{Ci}(bx)}{b^2} - \frac{\log(x)}{2b^2} + \frac{x \operatorname{Ci}(bx) \sin(bx)}{b} - \frac{\sin^2(bx)}{2b^2} - \frac{\int \frac{\cos(2bx)}{x} dx}{2b^2} \\
&= \frac{\cos(bx) \operatorname{Ci}(bx)}{b^2} - \frac{\operatorname{Ci}(2bx)}{2b^2} - \frac{\log(x)}{2b^2} + \frac{x \operatorname{Ci}(bx) \sin(bx)}{b} - \frac{\sin^2(bx)}{2b^2}
\end{aligned}$$

Mathematica [A] time = 0.0458631, size = 42, normalized size = 0.7

$$\frac{-2\operatorname{CosIntegral}(2bx) + 4\operatorname{CosIntegral}(bx)(bx \sin(bx) + \cos(bx)) + \cos(2bx) - 2 \log(x)}{4b^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[x*Cos[b*x]*CosIntegral[b*x], x]
```

```
[Out] (Cos[2*b*x] - 2*CosIntegral[2*b*x] - 2*Log[x] + 4*CosIntegral[b*x]*(Cos[b*x]
+ b*x*Sin[b*x]))/(4*b^2)
```

Maple [A] time = 0.059, size = 57, normalized size = 1.

$$\frac{x \operatorname{Ci}(bx) \sin(bx)}{b} + \frac{\operatorname{Ci}(bx) \cos(bx)}{b^2} + \frac{(\cos(bx))^2}{2b^2} - \frac{\ln(bx)}{2b^2} - \frac{\operatorname{Ci}(2bx)}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x*Ci(b*x)*cos(b*x), x)
```

```
[Out] x*Ci(b*x)*sin(b*x)/b+Ci(b*x)*cos(b*x)/b^2+1/2/b^2*cos(b*x)^2-1/2/b^2*ln(b*x)
)-1/2*Ci(2*b*x)/b^2
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \operatorname{Ci}(bx) \cos(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x)*cos(b*x),x, algorithm="maxima")

[Out] integrate(x*Ci(b*x)*cos(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}(x \cos(bx) \operatorname{Ci}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x)*cos(b*x),x, algorithm="fricas")

[Out] integral(x*cos(b*x)*cos_integral(b*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \cos(bx) \operatorname{Ci}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x)*cos(b*x),x)

[Out] Integral(x*cos(b*x)*Ci(b*x), x)

Giac [A] time = 1.19351, size = 59, normalized size = 0.98

$$\left(\frac{x \sin(bx)}{b} + \frac{\cos(bx)}{b^2} \right) \operatorname{Ci}(bx) - \frac{\operatorname{Ci}(2bx) + \operatorname{Ci}(-2bx) + 2 \log(x)}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x)*cos(b*x),x, algorithm="giac")

[Out] (x*sin(b*x)/b + cos(b*x)/b^2)*cos_integral(b*x) - 1/4*(cos_integral(2*b*x) + cos_integral(-2*b*x) + 2*log(x))/b^2

3.119 $\int x^2 \cos(bx) \text{CosIntegral}(bx) dx$

Optimal. Leaf size=89

$$\frac{2\text{CosIntegral}(bx)\sin(bx)}{b^3} + \frac{2x\text{CosIntegral}(bx)\cos(bx)}{b^2} + \frac{\text{Si}(2bx)}{b^3} - \frac{3x}{4b^2} - \frac{x\sin^2(bx)}{2b^2} - \frac{5\sin(bx)\cos(bx)}{4b^3} + \frac{x^2\text{CosIntegral}(bx)}{b^3}$$

[Out] $(-3*x)/(4*b^2) + (2*x*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/b^2 - (5*\text{Cos}[b*x]*\text{Sin}[b*x])/(4*b^3) - (2*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/b^3 + (x^2*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/b - (x*\text{Sin}[b*x]^2)/(2*b^2) + \text{SinIntegral}[2*b*x]/b^3$

Rubi [A] time = 0.112837, antiderivative size = 89, normalized size of antiderivative = 1., number of steps used = 14, number of rules used = 9, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.75$, Rules used = {6514, 12, 3443, 2635, 8, 6520, 6512, 4406, 3299}

$$\frac{2\text{CosIntegral}(bx)\sin(bx)}{b^3} + \frac{2x\text{CosIntegral}(bx)\cos(bx)}{b^2} + \frac{\text{Si}(2bx)}{b^3} - \frac{3x}{4b^2} - \frac{x\sin^2(bx)}{2b^2} - \frac{5\sin(bx)\cos(bx)}{4b^3} + \frac{x^2\text{CosIntegral}(bx)}{b^3}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2*\text{Cos}[b*x]*\text{CosIntegral}[b*x], x]$

[Out] $(-3*x)/(4*b^2) + (2*x*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/b^2 - (5*\text{Cos}[b*x]*\text{Sin}[b*x])/(4*b^3) - (2*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/b^3 + (x^2*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/b - (x*\text{Sin}[b*x]^2)/(2*b^2) + \text{SinIntegral}[2*b*x]/b^3$

Rule 6514

$\text{Int}[\text{Cos}[(a_.) + (b_.)*(x_.)]*\text{CosIntegral}[(c_.) + (d_.)*(x_.)]*((e_.) + (f_.)*(x_.))^{(m_.)}, x_Symbol] :> \text{Simp}[\frac{(e + f*x)^m*\text{Sin}[a + b*x]*\text{CosIntegral}[c + d*x]}{b}, x] + (-\text{Dist}[d/b, \text{Int}[\frac{(e + f*x)^m*\text{Sin}[a + b*x]*\text{Cos}[c + d*x]}{c + d*x}, x], x] - \text{Dist}[(f*m)/b, \text{Int}[(e + f*x)^{m-1}*\text{Sin}[a + b*x]*\text{CosIntegral}[c + d*x], x], x]) /; \text{FreeQ}\{a, b, c, d, e, f, x\} \&\& \text{IGtQ}[m, 0]$

Rule 12

$\text{Int}[(a_)*(u_), x_Symbol] :> \text{Dist}[a, \text{Int}[u, x], x] /; \text{FreeQ}[a, x] \&\& !\text{MatchQ}[u, (b_)*(v_)] /; \text{FreeQ}[b, x]$

Rule 3443

$\text{Int}[\text{Cos}[(a_.) + (b_.)*(x_.)^{(n_.)}]*(x_.)^{(m_.)}*\text{Sin}[(a_.) + (b_.)*(x_.)^{(n_.)}]^{(p_.)}, x_Symbol] :> \text{Simp}[\frac{x^{(m-n+1)}*\text{Sin}[a + b*x^n]^{(p+1)}}{(b*n*(p+1))}, x] - \text{Dist}[(m-n+1)/(b*n*(p+1)), \text{Int}[x^{(m-n)}*\text{Sin}[a + b*x^n]^{(p+1)}, x], x] /; \text{FreeQ}\{a, b, p, x\} \&\& \text{LtQ}[0, n, m+1] \&\& \text{NeQ}[p, -1]$

Rule 2635

$\text{Int}[\frac{(b_.)*\text{sin}[(c_.) + (d_.)*(x_.)]^{(n_.)}}{b}, x_Symbol] :> -\text{Simp}[\frac{(b*\text{Cos}[c + d*x])*(b*\text{Sin}[c + d*x])^{(n-1)}}{(d*n)}, x] + \text{Dist}[\frac{b^2*(n-1)}{n}, \text{Int}[\frac{(b*\text{Sin}[c + d*x])^{(n-2)}}{b}, x], x] /; \text{FreeQ}\{b, c, d, x\} \&\& \text{GtQ}[n, 1] \&\& \text{IntegerQ}[2*n]$

Rule 8

$\text{Int}[a_, x_Symbol] :> \text{Simp}[a*x, x] /; \text{FreeQ}[a, x]$

Rule 6520

```
Int[CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) +
(b_.)*(x_)], x_Symbol] := -Simp[((e + f*x)^m*Cos[a + b*x]*CosIntegral[c + d
*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*Cos[a + b*x]*Cos[c + d*x])/(c + d*
x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Cos[a + b*x]*CosIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 6512

```
Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := S
imp[(Sin[a + b*x]*CosIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]
*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b
_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x
]^(n)*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IG
tQ[p, 0]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int x^2 \cos(bx) \operatorname{Ci}(bx) dx &= \frac{x^2 \operatorname{Ci}(bx) \sin(bx)}{b} - \frac{2 \int x \operatorname{Ci}(bx) \sin(bx) dx}{b} - \int \frac{x \cos(bx) \sin(bx)}{b} dx \\
&= \frac{2x \cos(bx) \operatorname{Ci}(bx)}{b^2} + \frac{x^2 \operatorname{Ci}(bx) \sin(bx)}{b} - \frac{2 \int \cos(bx) \operatorname{Ci}(bx) dx}{b^2} - \frac{\int x \cos(bx) \sin(bx) dx}{b} - \frac{2 \int \cos^2(bx) dx}{b} \\
&= \frac{2x \cos(bx) \operatorname{Ci}(bx)}{b^2} - \frac{2 \operatorname{Ci}(bx) \sin(bx)}{b^3} + \frac{x^2 \operatorname{Ci}(bx) \sin(bx)}{b} - \frac{x \sin^2(bx)}{2b^2} + \frac{\int \sin^2(bx) dx}{2b^2} - \frac{2 \int \cos^2(bx) dx}{b} \\
&= \frac{2x \cos(bx) \operatorname{Ci}(bx)}{b^2} - \frac{5 \cos(bx) \sin(bx)}{4b^3} - \frac{2 \operatorname{Ci}(bx) \sin(bx)}{b^3} + \frac{x^2 \operatorname{Ci}(bx) \sin(bx)}{b} - \frac{x \sin^2(bx)}{2b^2} + \frac{2 \int \sin^2(bx) dx}{b} \\
&= -\frac{3x}{4b^2} + \frac{2x \cos(bx) \operatorname{Ci}(bx)}{b^2} - \frac{5 \cos(bx) \sin(bx)}{4b^3} - \frac{2 \operatorname{Ci}(bx) \sin(bx)}{b^3} + \frac{x^2 \operatorname{Ci}(bx) \sin(bx)}{b} - \frac{x \sin^2(bx)}{2b^2} \\
&= -\frac{3x}{4b^2} + \frac{2x \cos(bx) \operatorname{Ci}(bx)}{b^2} - \frac{5 \cos(bx) \sin(bx)}{4b^3} - \frac{2 \operatorname{Ci}(bx) \sin(bx)}{b^3} + \frac{x^2 \operatorname{Ci}(bx) \sin(bx)}{b} - \frac{x \sin^2(bx)}{2b^2} \\
&= -\frac{3x}{4b^2} + \frac{2x \cos(bx) \operatorname{Ci}(bx)}{b^2} - \frac{5 \cos(bx) \sin(bx)}{4b^3} - \frac{2 \operatorname{Ci}(bx) \sin(bx)}{b^3} + \frac{x^2 \operatorname{Ci}(bx) \sin(bx)}{b} - \frac{x \sin^2(bx)}{2b^2}
\end{aligned}$$

Mathematica [A] time = 0.0809702, size = 64, normalized size = 0.72

$$\frac{8 \operatorname{CosIntegral}(bx) \left((b^2 x^2 - 2) \sin(bx) + 2bx \cos(bx) \right) + 8 \operatorname{Si}(2bx) - 8bx - 5 \sin(2bx) + 2bx \cos(2bx)}{8b^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2*Cos[b*x]*CosIntegral[b*x], x]
```

```
[Out] (-8*b*x + 2*b*x*Cos[2*b*x] + 8*CosIntegral[b*x]*(2*b*x*Cos[b*x] + (-2 + b^2
*x^2)*Sin[b*x]) - 5*Sin[2*b*x] + 8*SinIntegral[2*b*x])/(8*b^3)
```

Maple [A] time = 0.073, size = 66, normalized size = 0.7

$$\frac{1}{b^3} \left(\text{Ci}(bx) (b^2 x^2 \sin(bx) - 2 \sin(bx) + 2bx \cos(bx)) + \frac{bx (\cos(bx))^2}{2} - \frac{5 \sin(bx) \cos(bx)}{4} - \frac{5bx}{4} + \text{Si}(2bx) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*Ci(b*x)*cos(b*x), x)

[Out] 1/b^3*(Ci(b*x)*(b^2*x^2*sin(b*x)-2*sin(b*x)+2*b*x*cos(b*x))+1/2*b*x*cos(b*x)^2-5/4*sin(b*x)*cos(b*x)-5/4*b*x+Si(2*b*x))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Ci}(bx) \cos(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x)*cos(b*x), x, algorithm="maxima")

[Out] integrate(x^2*Ci(b*x)*cos(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^2 \cos(bx) \text{Ci}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x)*cos(b*x), x, algorithm="fricas")

[Out] integral(x^2*cos(b*x)*cos_integral(b*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \cos(bx) \text{Ci}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*Ci(b*x)*cos(b*x), x)

[Out] Integral(x**2*cos(b*x)*Ci(b*x), x)

Giac [C] time = 1.19961, size = 88, normalized size = 0.99

$$\left(\frac{2x \cos(bx)}{b^2} + \frac{(b^2 x^2 - 2) \sin(bx)}{b^3} \right) \text{Ci}(bx) - \frac{2bx - \Im(\text{Ci}(2bx)) + \Im(\text{Ci}(-2bx)) - 2 \text{Si}(2bx)}{2b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*Ci(b*x)*cos(b*x),x, algorithm="giac")
```

```
[Out] (2*x*cos(b*x)/b^2 + (b^2*x^2 - 2)*sin(b*x)/b^3)*cos_integral(b*x) - 1/2*(2*  
b*x - imag_part(cos_integral(2*b*x)) + imag_part(cos_integral(-2*b*x)) - 2*  
sin_integral(2*b*x))/b^3
```

3.120 $\int x^3 \cos(bx) \text{CosIntegral}(bx) dx$

Optimal. Leaf size=142

$$\frac{3x^2 \text{CosIntegral}(bx) \cos(bx)}{b^2} + \frac{3 \text{CosIntegral}(2bx)}{b^4} - \frac{6x \text{CosIntegral}(bx) \sin(bx)}{b^3} - \frac{6 \text{CosIntegral}(bx) \cos(bx)}{b^4} - \frac{x}{2}$$

[Out] $-x^2/(2*b^2) - (3*\text{Cos}[b*x]^2)/(4*b^4) - (6*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/b^4 + (3*x^2*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/b^2 + (3*\text{CosIntegral}[2*b*x])/b^4 + (3*\text{Log}[x])/b^4 - (2*x*\text{Cos}[b*x]*\text{Sin}[b*x])/b^3 - (6*x*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/b^3 + (x^3*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/b + (13*\text{Sin}[b*x]^2)/(4*b^4) - (x^2*\text{Sin}[b*x]^2)/(2*b^2)$

Rubi [A] time = 0.18973, antiderivative size = 142, normalized size of antiderivative = 1., number of steps used = 18, number of rules used = 10, integrand size = 12, $\frac{\text{number of rules}}{\text{integrand size}} = 0.833$, Rules used = {6514, 12, 3443, 3310, 30, 6520, 2564, 6518, 3312, 3302}

$$\frac{3x^2 \text{CosIntegral}(bx) \cos(bx)}{b^2} + \frac{3 \text{CosIntegral}(2bx)}{b^4} - \frac{6x \text{CosIntegral}(bx) \sin(bx)}{b^3} - \frac{6 \text{CosIntegral}(bx) \cos(bx)}{b^4} - \frac{x}{2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^3*\text{Cos}[b*x]*\text{CosIntegral}[b*x], x]$

[Out] $-x^2/(2*b^2) - (3*\text{Cos}[b*x]^2)/(4*b^4) - (6*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/b^4 + (3*x^2*\text{Cos}[b*x]*\text{CosIntegral}[b*x])/b^2 + (3*\text{CosIntegral}[2*b*x])/b^4 + (3*\text{Log}[x])/b^4 - (2*x*\text{Cos}[b*x]*\text{Sin}[b*x])/b^3 - (6*x*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/b^3 + (x^3*\text{CosIntegral}[b*x]*\text{Sin}[b*x])/b + (13*\text{Sin}[b*x]^2)/(4*b^4) - (x^2*\text{Sin}[b*x]^2)/(2*b^2)$

Rule 6514

$\text{Int}[\text{Cos}[(a_.) + (b_.)*(x_.)]*\text{CosIntegral}[(c_.) + (d_.)*(x_.)]*((e_.) + (f_.)*(x_.))^{(m_.)}, x_Symbol] := \text{Simp}[\frac{(e + f*x)^m*\text{Sin}[a + b*x]*\text{CosIntegral}[c + d*x]}{b}, x] + (-\text{Dist}[d/b, \text{Int}[\frac{(e + f*x)^m*\text{Sin}[a + b*x]*\text{Cos}[c + d*x]}{c + d*x}, x], x] - \text{Dist}[\frac{(f*m)}{b}, \text{Int}[(e + f*x)^{(m-1)}*\text{Sin}[a + b*x]*\text{CosIntegral}[c + d*x], x], x]) /; \text{FreeQ}\{a, b, c, d, e, f\}, x \ \&\& \ \text{IGtQ}[m, 0]$

Rule 12

$\text{Int}[(a_)*(u_), x_Symbol] := \text{Dist}[a, \text{Int}[u, x], x] /; \text{FreeQ}[a, x] \ \&\& \ !\text{MatchQ}[u, (b_)*(v_)] /; \text{FreeQ}[b, x]$

Rule 3443

$\text{Int}[\text{Cos}[(a_.) + (b_.)*(x_.)^{(n_.)}]*(x_.)^{(m_.)}*\text{Sin}[(a_.) + (b_.)*(x_.)^{(n_.)}]^{(p_.)}, x_Symbol] := \text{Simp}[\frac{x^{(m-n+1)}*\text{Sin}[a + b*x^n]^{(p+1)}}{(b*n*(p+1))}, x] - \text{Dist}[\frac{(m-n+1)}{(b*n*(p+1))}, \text{Int}[x^{(m-n)}*\text{Sin}[a + b*x^n]^{(p+1)}, x], x] /; \text{FreeQ}\{a, b, p\}, x \ \&\& \ \text{LtQ}[0, n, m+1] \ \&\& \ \text{NeQ}[p, -1]$

Rule 3310

$\text{Int}[\frac{((c_.) + (d_.)*(x_.))*((b_.)*\text{sin}[(e_.) + (f_.)*(x_.)])^{(n_.)}, x_Symbol] := \text{Simp}[\frac{d*(b*\text{Sin}[e + f*x])^n}{(f^2*n^2)}, x] + (\text{Dist}[\frac{(b^2*(n-1))}{n}, \text{Int}[(c + d*x)*(b*\text{Sin}[e + f*x])^{(n-2)}, x], x] - \text{Simp}[\frac{b*(c + d*x)*\text{Cos}[e + f*x]*(b*\text{Sin}[e + f*x])^{(n-1)}}{(f*n)}, x]) /; \text{FreeQ}\{b, c, d, e, f\}, x \ \&\& \ \text{GtQ}[n, 1]$

]

Rule 30

```
Int[(x_)^(m_), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]
```

Rule 6520

```
Int[CosIntegral[(c_) + (d_)*(x_)]*((e_) + (f_)*(x_))^(m_)*Sin[(a_) + (b_)*(x_)], x_Symbol] := -Simp[((e + f*x)^m*Cos[a + b*x]*CosIntegral[c + d*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*Cos[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Cos[a + b*x]*CosIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 2564

```
Int[cos[(e_) + (f_)*(x_)]^(n_)*((a_)*sin[(e_) + (f_)*(x_)])^(m_), x_Symbol] := Dist[1/(a*f), Subst[Int[x^m*(1 - x^2/a^2)^((n - 1)/2), x], x, a*Sin[e + f*x]], x] /; FreeQ[{a, e, f, m}, x] && IntegerQ[(n - 1)/2] && !(IntegerQ[(m - 1)/2] && LtQ[0, m, n])
```

Rule 6518

```
Int[CosIntegral[(c_) + (d_)*(x_)]*Sin[(a_) + (b_)*(x_)], x_Symbol] := -Simp[(Cos[a + b*x]*CosIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 3312

```
Int[((c_) + (d_)*(x_))^(m_)*sin[(e_) + (f_)*(x_)]^(n_), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3302

```
Int[sin[(e_) + (f_)*(x_)]/((c_) + (d_)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int x^3 \cos(bx) \text{Ci}(bx) dx &= \frac{x^3 \text{Ci}(bx) \sin(bx)}{b} - \frac{3 \int x^2 \text{Ci}(bx) \sin(bx) dx}{b} - \int \frac{x^2 \cos(bx) \sin(bx)}{b} dx \\
&= \frac{3x^2 \cos(bx) \text{Ci}(bx)}{b^2} + \frac{x^3 \text{Ci}(bx) \sin(bx)}{b} - \frac{6 \int x \cos(bx) \text{Ci}(bx) dx}{b^2} - \frac{\int x^2 \cos(bx) \sin(bx) dx}{b} \\
&= \frac{3x^2 \cos(bx) \text{Ci}(bx)}{b^2} - \frac{6x \text{Ci}(bx) \sin(bx)}{b^3} + \frac{x^3 \text{Ci}(bx) \sin(bx)}{b} - \frac{x^2 \sin^2(bx)}{2b^2} + \frac{6 \int \text{Ci}(bx) \sin(bx) dx}{b^3} \\
&= -\frac{3 \cos^2(bx)}{4b^4} - \frac{6 \cos(bx) \text{Ci}(bx)}{b^4} + \frac{3x^2 \cos(bx) \text{Ci}(bx)}{b^2} - \frac{2x \cos(bx) \sin(bx)}{b^3} - \frac{6x \text{Ci}(bx) \sin(bx)}{b^3} \\
&= -\frac{x^2}{2b^2} - \frac{3 \cos^2(bx)}{4b^4} - \frac{6 \cos(bx) \text{Ci}(bx)}{b^4} + \frac{3x^2 \cos(bx) \text{Ci}(bx)}{b^2} - \frac{2x \cos(bx) \sin(bx)}{b^3} - \frac{6x \text{Ci}(bx) \sin(bx)}{b^3} \\
&= -\frac{x^2}{2b^2} - \frac{3 \cos^2(bx)}{4b^4} - \frac{6 \cos(bx) \text{Ci}(bx)}{b^4} + \frac{3x^2 \cos(bx) \text{Ci}(bx)}{b^2} - \frac{2x \cos(bx) \sin(bx)}{b^3} - \frac{6x \text{Ci}(bx) \sin(bx)}{b^3} \\
&= -\frac{x^2}{2b^2} - \frac{3 \cos^2(bx)}{4b^4} - \frac{6 \cos(bx) \text{Ci}(bx)}{b^4} + \frac{3x^2 \cos(bx) \text{Ci}(bx)}{b^2} + \frac{3 \log(x)}{b^4} - \frac{2x \cos(bx) \sin(bx)}{b^3} \\
&= -\frac{x^2}{2b^2} - \frac{3 \cos^2(bx)}{4b^4} - \frac{6 \cos(bx) \text{Ci}(bx)}{b^4} + \frac{3x^2 \cos(bx) \text{Ci}(bx)}{b^2} + \frac{3 \text{Ci}(2bx)}{b^4} + \frac{3 \log(x)}{b^4} - \frac{2x \cos(bx) \sin(bx)}{b^3}
\end{aligned}$$

Mathematica [A] time = 0.105215, size = 93, normalized size = 0.65

$$\frac{4 \text{CosIntegral}(bx) (bx (b^2 x^2 - 6) \sin(bx) + 3 (b^2 x^2 - 2) \cos(bx)) - 3b^2 x^2 + b^2 x^2 \cos(2bx) + 12 \text{CosIntegral}(2bx) - 4b^4 \log(x)}{4b^4}$$

Antiderivative was successfully verified.

[In] Integrate[x^3 * Cos[b*x] * CosIntegral[b*x], x]

[Out] (-3*b^2*x^2 - 8*Cos[2*b*x] + b^2*x^2*Cos[2*b*x] + 12*CosIntegral[2*b*x] + 12*Log[x] + 4*CosIntegral[b*x]*(3*(-2 + b^2*x^2)*Cos[b*x] + b*x*(-6 + b^2*x^2)*Sin[b*x]) - 4*b*x*Sin[2*b*x])/(4*b^4)

Maple [A] time = 0.065, size = 136, normalized size = 1.

$$\frac{x^3 \text{Ci}(bx) \sin(bx)}{b} + 3 \frac{x^2 \text{Ci}(bx) \cos(bx)}{b^2} - 6 \frac{x \text{Ci}(bx) \sin(bx)}{b^3} - 6 \frac{\text{Ci}(bx) \cos(bx)}{b^4} + \frac{x^2 (\cos(bx))^2}{2b^2} - 2 \frac{x \cos(bx) \sin(bx)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^3 * Ci(b*x) * cos(b*x), x)

[Out] x^3 * Ci(b*x) * sin(b*x) / b + 3 * x^2 * Ci(b*x) * cos(b*x) / b^2 - 6 * x * Ci(b*x) * sin(b*x) / b^3 - 6 * Ci(b*x) * cos(b*x) / b^4 + 1/2 * b^2 * x^2 * cos(b*x)^2 - 2 * x * cos(b*x) * sin(b*x) / b^3 - x^2 / b^2 + sin(b*x)^2 / b^4 + 3 / b^4 * ln(b*x) + 3 * Ci(2 * b * x) / b^4 - 3 * cos(b*x)^2 / b^4

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \text{Ci}(bx) \cos(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Ci(b*x)*cos(b*x),x, algorithm="maxima")

[Out] integrate(x^3*Ci(b*x)*cos(b*x), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^3 \cos(bx) \text{Ci}(bx), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Ci(b*x)*cos(b*x),x, algorithm="fricas")

[Out] integral(x^3*cos(b*x)*cos_integral(b*x), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^3 \cos(bx) \text{Ci}(bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**3*Ci(b*x)*cos(b*x),x)

[Out] Integral(x**3*cos(b*x)*Ci(b*x), x)

Giac [A] time = 1.26308, size = 103, normalized size = 0.73

$$\left(\frac{3(b^2x^2 - 2)\cos(bx)}{b^4} + \frac{(b^3x^3 - 6bx)\sin(bx)}{b^4} \right) \text{Ci}(bx) - \frac{3(b^2x^2 - 2)\text{Ci}(2bx) - 2\text{Ci}(-2bx) - 4\log(x)}{4b^4}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^3*Ci(b*x)*cos(b*x),x, algorithm="giac")

[Out] (3*(b^2*x^2 - 2)*cos(b*x)/b^4 + (b^3*x^3 - 6*b*x)*sin(b*x)/b^4)*cos_integra
l(b*x) - 3/4*(b^2*x^2 - 2*cos_integral(2*b*x) - 2*cos_integral(-2*b*x) - 4*
log(x))/b^4

3.121 $\int \text{CosIntegral}(2x) \sin(5x) dx$

Optimal. Leaf size=29

$$\frac{1}{10}\text{CosIntegral}(3x) + \frac{1}{10}\text{CosIntegral}(7x) - \frac{1}{5}\text{CosIntegral}(2x) \cos(5x)$$

[Out] $-(\text{Cos}[5*x]*\text{CosIntegral}[2*x])/5 + \text{CosIntegral}[3*x]/10 + \text{CosIntegral}[7*x]/10$

Rubi [A] time = 0.0557009, antiderivative size = 29, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 4, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.444$, Rules used = {6518, 12, 4429, 3302}

$$\frac{1}{10}\text{CosIntegral}(3x) + \frac{1}{10}\text{CosIntegral}(7x) - \frac{1}{5}\text{CosIntegral}(2x) \cos(5x)$$

Antiderivative was successfully verified.

[In] $\text{Int}[\text{CosIntegral}[2*x]*\text{Sin}[5*x], x]$

[Out] $-(\text{Cos}[5*x]*\text{CosIntegral}[2*x])/5 + \text{CosIntegral}[3*x]/10 + \text{CosIntegral}[7*x]/10$

Rule 6518

$\text{Int}[\text{CosIntegral}[(c_.) + (d_.)*(x_.)]*\text{Sin}[(a_.) + (b_.)*(x_.)], x_Symbol] \text{ :> } -\text{Simp}[(\text{Cos}[a + b*x]*\text{CosIntegral}[c + d*x])/b, x] + \text{Dist}[d/b, \text{Int}[(\text{Cos}[a + b*x]*\text{Cos}[c + d*x])/(c + d*x), x], x] \text{ /; FreeQ}\{a, b, c, d\}, x]$

Rule 12

$\text{Int}[(a_.)*(u_), x_Symbol] \text{ :> } \text{Dist}[a, \text{Int}[u, x], x] \text{ /; FreeQ}\{a, x\} \ \&\& \ \text{!MatchQ}[u, (b_.)*(v_) \text{ /; FreeQ}\{b, x\}]$

Rule 4429

$\text{Int}[\text{Cos}[(a_.) + (b_.)*(x_.)]^{(p_.)}*\text{Cos}[(c_.) + (d_.)*(x_.)]^{(q_.)}*((e_.) + (f_.)*(x_.))^{(m_.)}, x_Symbol] \text{ :> } \text{Int}[\text{ExpandTrigReduce}[(e + f*x)^m, \text{Cos}[a + b*x]^{p*}\text{Cos}[c + d*x]^q, x], x] \text{ /; FreeQ}\{a, b, c, d, e, f\}, x\} \ \&\& \ \text{IGtQ}[p, 0] \ \&\& \ \text{IGtQ}[q, 0] \ \&\& \ \text{IntegerQ}[m]$

Rule 3302

$\text{Int}[\text{sin}[(e_.) + (f_.)*(x_.)]/((c_.) + (d_.)*(x_.)), x_Symbol] \text{ :> } \text{Simp}[\text{CosIntegral}[e - \text{Pi}/2 + f*x]/d, x] \text{ /; FreeQ}\{c, d, e, f\}, x\} \ \&\& \ \text{EqQ}[d*(e - \text{Pi}/2) - c*f, 0]$

Rubi steps

$$\begin{aligned}
\int \text{Ci}(2x) \sin(5x) dx &= -\frac{1}{5} \cos(5x) \text{Ci}(2x) + \frac{2}{5} \int \frac{\cos(2x) \cos(5x)}{2x} dx \\
&= -\frac{1}{5} \cos(5x) \text{Ci}(2x) + \frac{1}{5} \int \frac{\cos(2x) \cos(5x)}{x} dx \\
&= -\frac{1}{5} \cos(5x) \text{Ci}(2x) + \frac{1}{5} \int \left(\frac{\cos(3x)}{2x} + \frac{\cos(7x)}{2x} \right) dx \\
&= -\frac{1}{5} \cos(5x) \text{Ci}(2x) + \frac{1}{10} \int \frac{\cos(3x)}{x} dx + \frac{1}{10} \int \frac{\cos(7x)}{x} dx \\
&= -\frac{1}{5} \cos(5x) \text{Ci}(2x) + \frac{\text{Ci}(3x)}{10} + \frac{\text{Ci}(7x)}{10}
\end{aligned}$$

Mathematica [A] time = 0.0262833, size = 23, normalized size = 0.79

$$\frac{1}{10}(\text{CosIntegral}(3x) + \text{CosIntegral}(7x) - 2\text{CosIntegral}(2x) \cos(5x))$$

Antiderivative was successfully verified.

[In] Integrate[CosIntegral[2*x]*Sin[5*x],x]

[Out] (-2*Cos[5*x]*CosIntegral[2*x] + CosIntegral[3*x] + CosIntegral[7*x])/10

Maple [A] time = 0.104, size = 24, normalized size = 0.8

$$\frac{\text{Ci}(3x)}{10} + \frac{\text{Ci}(7x)}{10} - \frac{\text{Ci}(2x) \cos(5x)}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(2*x)*sin(5*x),x)

[Out] 1/10*Ci(3*x)+1/10*Ci(7*x)-1/5*Ci(2*x)*cos(5*x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Ci}(2x) \sin(5x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(2*x)*sin(5*x),x, algorithm="maxima")

[Out] integrate(Ci(2*x)*sin(5*x), x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(2*x)*sin(5*x),x, algorithm="fricas")
```

```
[Out] Exception raised: UnboundLocalError
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \sin(5x) \operatorname{Ci}(2x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(2*x)*sin(5*x),x)
```

```
[Out] Integral(sin(5*x)*Ci(2*x), x)
```

Giac [A] time = 1.21775, size = 31, normalized size = 1.07

$$-\frac{1}{5} \cos(5x) \operatorname{Ci}(2x) + \frac{1}{10} \operatorname{Ci}(7x) + \frac{1}{10} \operatorname{Ci}(3x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(2*x)*sin(5*x),x, algorithm="giac")
```

```
[Out] -1/5*cos(5*x)*cos_integral(2*x) + 1/10*cos_integral(7*x) + 1/10*cos_integra
1(3*x)
```

3.122 $\int \cos(5x)\mathbf{CosIntegral}(2x) dx$

Optimal. Leaf size=29

$$\frac{1}{5}\mathbf{CosIntegral}(2x)\sin(5x) - \frac{\mathbf{Si}(3x)}{10} - \frac{\mathbf{Si}(7x)}{10}$$

[Out] (CosIntegral[2*x]*Sin[5*x])/5 - SinIntegral[3*x]/10 - SinIntegral[7*x]/10

Rubi [A] time = 0.0534955, antiderivative size = 29, normalized size of antiderivative = 1., number of steps used = 6, number of rules used = 4, integrand size = 9, $\frac{\text{number of rules}}{\text{integrand size}} = 0.444$, Rules used = {6512, 12, 4430, 3299}

$$\frac{1}{5}\mathbf{CosIntegral}(2x)\sin(5x) - \frac{\mathbf{Si}(3x)}{10} - \frac{\mathbf{Si}(7x)}{10}$$

Antiderivative was successfully verified.

[In] Int[Cos[5*x]*CosIntegral[2*x],x]

[Out] (CosIntegral[2*x]*Sin[5*x])/5 - SinIntegral[3*x]/10 - SinIntegral[7*x]/10

Rule 6512

Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :> Simp[(Sin[a + b*x]*CosIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 12

Int[(a_)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]

Rule 4430

Int[Cos[(c_.) + (d_.)*(x_)]^(q_.)*((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(p_.), x_Symbol] :> Int[ExpandTrigReduce[(e + f*x)^m, Sin[a + b*x]^p*cos[c + d*x]^q, x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[p, 0] && IGtQ[q, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned}
\int \cos(5x) \operatorname{Ci}(2x) dx &= \frac{1}{5} \operatorname{Ci}(2x) \sin(5x) - \frac{2}{5} \int \frac{\cos(2x) \sin(5x)}{2x} dx \\
&= \frac{1}{5} \operatorname{Ci}(2x) \sin(5x) - \frac{1}{5} \int \frac{\cos(2x) \sin(5x)}{x} dx \\
&= \frac{1}{5} \operatorname{Ci}(2x) \sin(5x) - \frac{1}{5} \int \left(\frac{\sin(3x)}{2x} + \frac{\sin(7x)}{2x} \right) dx \\
&= \frac{1}{5} \operatorname{Ci}(2x) \sin(5x) - \frac{1}{10} \int \frac{\sin(3x)}{x} dx - \frac{1}{10} \int \frac{\sin(7x)}{x} dx \\
&= \frac{1}{5} \operatorname{Ci}(2x) \sin(5x) - \frac{\operatorname{Si}(3x)}{10} - \frac{\operatorname{Si}(7x)}{10}
\end{aligned}$$

Mathematica [A] time = 0.024018, size = 27, normalized size = 0.93

$$\frac{1}{10} (2 \operatorname{CosIntegral}(2x) \sin(5x) - \operatorname{Si}(3x) - \operatorname{Si}(7x))$$

Antiderivative was successfully verified.

[In] Integrate[Cos [5*x]*CosIntegral [2*x] , x]

[Out] (2*CosIntegral [2*x]*Sin [5*x] - SinIntegral [3*x] - SinIntegral [7*x])/10

Maple [A] time = 0.095, size = 24, normalized size = 0.8

$$-\frac{\operatorname{Si}(3x)}{10} - \frac{\operatorname{Si}(7x)}{10} + \frac{\operatorname{Ci}(2x) \sin(5x)}{5}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(2*x)*cos(5*x), x)

[Out] -1/10*Si(3*x)-1/10*Si(7*x)+1/5*Ci(2*x)*sin(5*x)

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \operatorname{Ci}(2x) \cos(5x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(2*x)*cos(5*x), x, algorithm="maxima")

[Out] integrate(Ci(2*x)*cos(5*x), x)

Fricas [F(-2)] time = 0., size = 0, normalized size = 0.

Exception raised: UnboundLocalError

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(2*x)*cos(5*x),x, algorithm="fricas")
```

```
[Out] Exception raised: UnboundLocalError
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \cos(5x) \operatorname{Ci}(2x) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(2*x)*cos(5*x),x)
```

```
[Out] Integral(cos(5*x)*Ci(2*x), x)
```

Giac [A] time = 1.2446, size = 31, normalized size = 1.07

$$\frac{1}{5} \operatorname{Ci}(2x) \sin(5x) - \frac{1}{10} \operatorname{Si}(7x) - \frac{1}{10} \operatorname{Si}(3x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(2*x)*cos(5*x),x, algorithm="giac")
```

```
[Out] 1/5*cos_integral(2*x)*sin(5*x) - 1/10*sin_integral(7*x) - 1/10*sin_integral(3*x)
```


3.123 $\int x^2 \text{CosIntegral}(a + bx) \sin(a + bx) dx$

Optimal. Leaf size=220

$$\frac{a^2 \text{CosIntegral}(2a + 2bx)}{2b^3} + \frac{a^2 \log(a + bx)}{2b^3} - \frac{\text{CosIntegral}(2a + 2bx)}{b^3} + \frac{2x \text{CosIntegral}(a + bx) \sin(a + bx)}{b^2} + \frac{2 \text{CosIntegral}(a + bx) \sin(a + bx)}{b}$$

[Out] $-(a*x)/(2*b^2) + x^2/(4*b) + \text{Cos}[a + b*x]^2/(4*b^3) + \text{Cos}[2*a + 2*b*x]/(2*b^3) + (2*\text{Cos}[a + b*x]*\text{CosIntegral}[a + b*x])/b^3 - (x^2*\text{Cos}[a + b*x]*\text{CosIntegral}[a + b*x])/b - \text{CosIntegral}[2*a + 2*b*x]/b^3 + (a^2*\text{CosIntegral}[2*a + 2*b*x])/(2*b^3) - \text{Log}[a + b*x]/b^3 + (a^2*\text{Log}[a + b*x])/(2*b^3) - (a*\text{Cos}[a + b*x]*\text{Sin}[a + b*x])/(2*b^3) + (x*\text{Cos}[a + b*x]*\text{Sin}[a + b*x])/(2*b^2) + (2*x*\text{CosIntegral}[a + b*x]*\text{Sin}[a + b*x])/b^2 + (a*\text{SinIntegral}[2*a + 2*b*x])/b^3$

Rubi [A] time = 0.719672, antiderivative size = 220, normalized size of antiderivative = 1., number of steps used = 21, number of rules used = 14, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 0.875$, Rules used = {6520, 6742, 2635, 8, 3310, 30, 3312, 3302, 6514, 4573, 6741, 2638, 3299, 6518}

$$\frac{a^2 \text{CosIntegral}(2a + 2bx)}{2b^3} + \frac{a^2 \log(a + bx)}{2b^3} - \frac{\text{CosIntegral}(2a + 2bx)}{b^3} + \frac{2x \text{CosIntegral}(a + bx) \sin(a + bx)}{b^2} + \frac{2 \text{CosIntegral}(a + bx) \sin(a + bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[x^2*CosIntegral[a + b*x]*Sin[a + b*x],x]

[Out] $-(a*x)/(2*b^2) + x^2/(4*b) + \text{Cos}[a + b*x]^2/(4*b^3) + \text{Cos}[2*a + 2*b*x]/(2*b^3) + (2*\text{Cos}[a + b*x]*\text{CosIntegral}[a + b*x])/b^3 - (x^2*\text{Cos}[a + b*x]*\text{CosIntegral}[a + b*x])/b - \text{CosIntegral}[2*a + 2*b*x]/b^3 + (a^2*\text{CosIntegral}[2*a + 2*b*x])/(2*b^3) - \text{Log}[a + b*x]/b^3 + (a^2*\text{Log}[a + b*x])/(2*b^3) - (a*\text{Cos}[a + b*x]*\text{Sin}[a + b*x])/(2*b^3) + (x*\text{Cos}[a + b*x]*\text{Sin}[a + b*x])/(2*b^2) + (2*x*\text{CosIntegral}[a + b*x]*\text{Sin}[a + b*x])/b^2 + (a*\text{SinIntegral}[2*a + 2*b*x])/b^3$

Rule 6520

Int[CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)], x_Symbol] := -Simp[((e + f*x)^m*Cos[a + b*x]*CosIntegral[c + d*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*Cos[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Cos[a + b*x]*CosIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]

Rule 6742

Int[u_, x_Symbol] := With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]]

Rule 2635

Int[((b_.)*sin[(c_.) + (d_.)*(x_)])^(n_), x_Symbol] := -Simp[(b*Cos[c + d*x]*(b*SIN[c + d*x])^(n - 1))/(d*n), x] + Dist[(b^2*(n - 1))/n, Int[(b*SIN[c + d*x])^(n - 2), x], x] /; FreeQ[{b, c, d}, x] && GtQ[n, 1] && IntegerQ[2*n]

Rule 8

Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]

Rule 3310

```
Int[((c_.) + (d_.)*(x_))*((b_.)*sin[(e_.) + (f_.)*(x_)])^(n_), x_Symbol] :=
  Simp[(d*(b*SIN[e + f*x])^n)/(f^2*n^2), x] + (Dist[(b^2*(n - 1))/n, Int[(c
+ d*x)*(b*SIN[e + f*x])^(n - 2), x], x] - Simp[(b*(c + d*x)*Cos[e + f*x]*(b
*SIN[e + f*x])^(n - 1))/(f*n), x]) /; FreeQ[{b, c, d, e, f}, x] && GtQ[n, 1
]
```

Rule 30

```
Int[(x_)^(m_.), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 3312

```
Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := In
t[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f
, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rule 6514

```
Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*
(x_))^(m_.), x_Symbol] := Simp[((e + f*x)^m*SIN[a + b*x]*CosIntegral[c + d*
x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*SIN[a + b*x]*Cos[c + d*x])/(c + d*
x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*SIN[a + b*x]*CosIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 4573

```
Int[Cos[w_]^(p_.)*(u_.)*Sin[v_]^(p_.), x_Symbol] := Dist[1/2^p, Int[u*SIN[2
*v]^p, x], x] /; EqQ[w, v] && IntegerQ[p]
```

Rule 6741

```
Int[u_, x_Symbol] := With[{v = NormalizeIntegrand[u, x]}, Int[v, x] /; v !=
= u]
```

Rule 2638

```
Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] := -Simp[Cos[c + d*x]/d, x] /; FreeQ
[{c, d}, x]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SINInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 6518

```
Int[CosIntegral[(c_.) + (d_.)*(x_)]*Sin[(a_.) + (b_.)*(x_)], x_Symbol] := -
Simp[(Cos[a + b*x]*CosIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x
]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rubi steps

$$\begin{aligned}
\int x^2 \text{Ci}(a+bx) \sin(a+bx) dx &= -\frac{x^2 \cos(a+bx) \text{Ci}(a+bx)}{b} + \frac{2 \int x \cos(a+bx) \text{Ci}(a+bx) dx}{b} + \int \frac{x^2 \cos^2(a+bx)}{a+bx} dx \\
&= -\frac{x^2 \cos(a+bx) \text{Ci}(a+bx)}{b} + \frac{2x \text{Ci}(a+bx) \sin(a+bx)}{b^2} - \frac{2 \int \text{Ci}(a+bx) \sin(a+bx) dx}{b^2} \\
&= \frac{2 \cos(a+bx) \text{Ci}(a+bx)}{b^3} - \frac{x^2 \cos(a+bx) \text{Ci}(a+bx)}{b} + \frac{2x \text{Ci}(a+bx) \sin(a+bx)}{b^2} - \frac{2 \int \text{Ci}(a+bx) \sin(a+bx) dx}{b^2} \\
&= \frac{\cos^2(a+bx)}{4b^3} + \frac{2 \cos(a+bx) \text{Ci}(a+bx)}{b^3} - \frac{x^2 \cos(a+bx) \text{Ci}(a+bx)}{b} - \frac{a \cos(a+bx)}{2b} \\
&= -\frac{ax}{2b^2} + \frac{x^2}{4b} + \frac{\cos^2(a+bx)}{4b^3} + \frac{2 \cos(a+bx) \text{Ci}(a+bx)}{b^3} - \frac{x^2 \cos(a+bx) \text{Ci}(a+bx)}{b} \\
&= -\frac{ax}{2b^2} + \frac{x^2}{4b} + \frac{\cos^2(a+bx)}{4b^3} + \frac{2 \cos(a+bx) \text{Ci}(a+bx)}{b^3} - \frac{x^2 \cos(a+bx) \text{Ci}(a+bx)}{b} \\
&= -\frac{ax}{2b^2} + \frac{x^2}{4b} + \frac{\cos^2(a+bx)}{4b^3} + \frac{\cos(2a+2bx)}{2b^3} + \frac{2 \cos(a+bx) \text{Ci}(a+bx)}{b^3} - \frac{x^2 \cos(a+bx) \text{Ci}(a+bx)}{b}
\end{aligned}$$

Mathematica [A] time = 0.321807, size = 134, normalized size = 0.61

$$\frac{4(a^2 - 2) \text{CosIntegral}(2(a+bx)) + 4a^2 \log(a+bx) - 8 \text{CosIntegral}(a+bx) \left((b^2 x^2 - 2) \cos(a+bx) - 2bx \sin(a+bx) \right)}{8b^3}$$

Antiderivative was successfully verified.

[In] Integrate[x^2*CosIntegral[a + b*x]*Sin[a + b*x],x]

[Out] $(-4*a*b*x + 2*b^2*x^2 + 5*\text{Cos}[2*(a + b*x)] + 4*(-2 + a^2)*\text{CosIntegral}[2*(a + b*x)] - 8*\text{Log}[a + b*x] + 4*a^2*\text{Log}[a + b*x] - 8*\text{CosIntegral}[a + b*x]*((-2 + b^2*x^2)*\text{Cos}[a + b*x] - 2*b*x*\text{Sin}[a + b*x]) - 2*a*\text{Sin}[2*(a + b*x)] + 2*b*x*\text{Sin}[2*(a + b*x)] + 8*a*\text{SinIntegral}[2*(a + b*x)])/(8*b^3)$

Maple [A] time = 0.066, size = 211, normalized size = 1.

$$-\frac{x^2 \text{Ci}(bx+a) \cos(bx+a)}{b} + 2 \frac{x \text{Ci}(bx+a) \sin(bx+a)}{b^2} + 2 \frac{\text{Ci}(bx+a) \cos(bx+a)}{b^3} + \frac{x \cos(bx+a) \sin(bx+a)}{2b^2} - \frac{a \cos(bx+a)}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x^2*Ci(b*x+a)*sin(b*x+a),x)

[Out] $-x^2 \text{Ci}(b*x+a) \cos(b*x+a)/b + 2*x \text{Ci}(b*x+a) \sin(b*x+a)/b^2 + 2 \text{Ci}(b*x+a) \cos(b*x+a)/b^3 + 1/2*x \cos(b*x+a) \sin(b*x+a)/b^2 - 1/2*a \cos(b*x+a) \sin(b*x+a)/b^3 + 1/4*x^2/b - 1/2*a*x/b^2 - 3/4/b^3*a^2 - 1/4*\sin(b*x+a)^2/b^3 + 1/2*a^2*\ln(b*x+a)/b^3 + 1/2*a^2*\text{Ci}(2*b*x+2*a)/b^3 + \cos(b*x+a)^2/b^3 + a*\text{Si}(2*b*x+2*a)/b^3 - \ln(b*x+a)/b^3 - \text{Ci}(2*b*x+2*a)/b^3$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Ci}(bx+a) \sin(bx+a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x+a)*sin(b*x+a),x, algorithm="maxima")

[Out] integrate(x^2*Ci(b*x + a)*sin(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(x^2 \text{Ci}(bx + a) \sin(bx + a), x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x+a)*sin(b*x+a),x, algorithm="fricas")

[Out] integral(x^2*cos_integral(b*x + a)*sin(b*x + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \sin(a + bx) \text{Ci}(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x**2*Ci(b*x+a)*sin(b*x+a),x)

[Out] Integral(x**2*sin(a + b*x)*Ci(a + b*x), x)

Giac [C] time = 1.31872, size = 230, normalized size = 1.05

$$\left(\frac{2x \sin(bx + a)}{b^2} - \frac{(b^2x^2 - 2) \cos(bx + a)}{b^3}\right) \text{Ci}(bx + a) + \frac{b^2x^2 - 2abx + 2a^2 \log(|bx + a|) + a^2 \Re(\text{Ci}(2bx + 2a)) + a^2 \Im(\text{Ci}(2bx + 2a))}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x^2*Ci(b*x+a)*sin(b*x+a),x, algorithm="giac")

[Out] (2*x*sin(b*x + a)/b^2 - (b^2*x^2 - 2)*cos(b*x + a)/b^3)*cos_integral(b*x + a) + 1/4*(b^2*x^2 - 2*a*b*x + 2*a^2*log(abs(b*x + a)) + a^2*real_part(cos_integral(2*b*x + 2*a)) + a^2*real_part(cos_integral(-2*b*x - 2*a)) + 2*a*imag_part(cos_integral(2*b*x + 2*a)) - 2*a*imag_part(cos_integral(-2*b*x - 2*a))) + 4*a*sin_integral(2*b*x + 2*a) - 4*log(abs(b*x + a)) - 2*real_part(cos_integral(2*b*x + 2*a)) - 2*real_part(cos_integral(-2*b*x - 2*a)))/b^3

3.124 $\int x \text{CosIntegral}(a + bx) \sin(a + bx) dx$

Optimal. Leaf size=109

$$\frac{a \text{CosIntegral}(2a + 2bx)}{2b^2} + \frac{\text{CosIntegral}(a + bx) \sin(a + bx)}{b^2} - \frac{\text{Si}(2a + 2bx)}{2b^2} - \frac{a \log(a + bx)}{2b^2} + \frac{\sin(a + bx) \cos(a + bx)}{2b^2}$$

```
[Out] x/(2*b) - (x*cos[a + b*x]*CosIntegral[a + b*x])/b - (a*cosIntegral[2*a + 2*
b*x])/(2*b^2) - (a*Log[a + b*x])/(2*b^2) + (Cos[a + b*x]*Sin[a + b*x])/(2*b
^2) + (CosIntegral[a + b*x]*Sin[a + b*x])/b^2 - SinIntegral[2*a + 2*b*x]/(2
*b^2)
```

Rubi [A] time = 0.229298, antiderivative size = 109, normalized size of antiderivative = 1., number of steps used = 12, number of rules used = 10, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.714$, Rules used = {6520, 6742, 2635, 8, 3312, 3302, 6512, 4406, 12, 3299}

$$\frac{a \text{CosIntegral}(2a + 2bx)}{2b^2} + \frac{\text{CosIntegral}(a + bx) \sin(a + bx)}{b^2} - \frac{\text{Si}(2a + 2bx)}{2b^2} - \frac{a \log(a + bx)}{2b^2} + \frac{\sin(a + bx) \cos(a + bx)}{2b^2}$$

Antiderivative was successfully verified.

```
[In] Int[x*cosIntegral[a + b*x]*Sin[a + b*x], x]
```

```
[Out] x/(2*b) - (x*cos[a + b*x]*CosIntegral[a + b*x])/b - (a*cosIntegral[2*a + 2*
b*x])/(2*b^2) - (a*Log[a + b*x])/(2*b^2) + (Cos[a + b*x]*Sin[a + b*x])/(2*b
^2) + (CosIntegral[a + b*x]*Sin[a + b*x])/b^2 - SinIntegral[2*a + 2*b*x]/(2
*b^2)
```

Rule 6520

```
Int[CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) +
(b_.)*(x_)], x_Symbol] := -Simp[((e + f*x)^m*cos[a + b*x]*CosIntegral[c + d
*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*cos[a + b*x]*Cos[c + d*x])/(c + d*
x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Cos[a + b*x]*CosIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 6742

```
Int[u_, x_Symbol] := With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]
]
```

Rule 2635

```
Int[((b_.)*sin[(c_.) + (d_.)*(x_)])^(n_), x_Symbol] := -Simp[(b*cos[c + d*x]
)*(b*sin[c + d*x])^(n - 1))/(d*n), x] + Dist[(b^2*(n - 1))/n, Int[(b*sin[c
+ d*x])^(n - 2), x], x] /; FreeQ[{b, c, d}, x] && GtQ[n, 1] && IntegerQ[2*n]
]
```

Rule 8

```
Int[a_, x_Symbol] := Simp[a*x, x] /; FreeQ[a, x]
```

Rule 3312

```
Int[((c_.) + (d_.)*(x_))^(m_.)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := In
t[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f
, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]
```

Rule 6512

```
Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := Simp[(Sin[a + b*x]*CosIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rubi steps

$$\begin{aligned}
\int x \operatorname{Ci}(a+bx) \sin(a+bx) dx &= -\frac{x \cos(a+bx) \operatorname{Ci}(a+bx)}{b} + \frac{\int \cos(a+bx) \operatorname{Ci}(a+bx) dx}{b} + \int \frac{x \cos^2(a+bx)}{a+bx} dx \\
&= -\frac{x \cos(a+bx) \operatorname{Ci}(a+bx)}{b} + \frac{\operatorname{Ci}(a+bx) \sin(a+bx)}{b^2} - \frac{\int \frac{\cos(a+bx) \sin(a+bx)}{a+bx} dx}{b} + \int \left(\frac{\cos^2(a+bx)}{a+bx} \right) dx \\
&= -\frac{x \cos(a+bx) \operatorname{Ci}(a+bx)}{b} + \frac{\operatorname{Ci}(a+bx) \sin(a+bx)}{b^2} + \frac{\int \cos^2(a+bx) dx}{b} - \frac{\int \frac{\sin(2a+2bx)}{2(a+bx)} dx}{b} \\
&= -\frac{x \cos(a+bx) \operatorname{Ci}(a+bx)}{b} + \frac{\cos(a+bx) \sin(a+bx)}{2b^2} + \frac{\operatorname{Ci}(a+bx) \sin(a+bx)}{b^2} + \frac{\int 1 dx}{2b} \\
&= \frac{x}{2b} - \frac{x \cos(a+bx) \operatorname{Ci}(a+bx)}{b} - \frac{a \log(a+bx)}{2b^2} + \frac{\cos(a+bx) \sin(a+bx)}{2b^2} + \frac{\operatorname{Ci}(a+bx) \sin(a+bx)}{b^2} \\
&= \frac{x}{2b} - \frac{x \cos(a+bx) \operatorname{Ci}(a+bx)}{b} - \frac{a \operatorname{Ci}(2a+2bx)}{2b^2} - \frac{a \log(a+bx)}{2b^2} + \frac{\cos(a+bx) \sin(a+bx)}{2b^2}
\end{aligned}$$

Mathematica [A] time = 0.181983, size = 76, normalized size = 0.7

$$\frac{-2a \operatorname{CosIntegral}(2(a+bx)) + \operatorname{CosIntegral}(a+bx)(4 \sin(a+bx) - 4bx \cos(a+bx)) - 2\operatorname{Si}(2(a+bx)) - 2a \log(a+bx)}{4b^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[x*CosIntegral[a + b*x]*Sin[a + b*x], x]
```

```
[Out] (2*b*x - 2*a*CosIntegral[2*(a + b*x)] - 2*a*Log[a + b*x] + CosIntegral[a + b*x]*(-4*b*x*Cos[a + b*x] + 4*Sin[a + b*x]) + Sin[2*(a + b*x)] - 2*SinInteg
```

ral[2*(a + b*x)]/(4*b^2)

Maple [A] time = 0.062, size = 106, normalized size = 1.

$$-\frac{x \operatorname{Ci}(bx+a) \cos(bx+a)}{b} + \frac{\operatorname{Ci}(bx+a) \sin(bx+a)}{b^2} + \frac{\cos(bx+a) \sin(bx+a)}{2b^2} + \frac{x}{2b} + \frac{a}{2b^2} - \frac{a \ln(bx+a)}{2b^2} - \frac{a \operatorname{Ci}(2bx+2a)}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*Ci(b*x+a)*sin(b*x+a),x)

[Out] -x*Ci(b*x+a)*cos(b*x+a)/b+Ci(b*x+a)*sin(b*x+a)/b^2+1/2*cos(b*x+a)*sin(b*x+a)/b^2+1/2*x/b+1/2/b^2*a-1/2*a*ln(b*x+a)/b^2-1/2*a*Ci(2*b*x+2*a)/b^2-1/2*Si(2*b*x+2*a)/b^2

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \operatorname{Ci}(bx+a) \sin(bx+a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x+a)*sin(b*x+a),x, algorithm="maxima")

[Out] integrate(x*Ci(b*x + a)*sin(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}(x \operatorname{Ci}(bx+a) \sin(bx+a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x+a)*sin(b*x+a),x, algorithm="fricas")

[Out] integral(x*cos_integral(b*x + a)*sin(b*x + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \sin(a+bx) \operatorname{Ci}(a+bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(b*x+a)*sin(b*x+a),x)

[Out] Integral(x*sin(a + b*x)*Ci(a + b*x), x)

Giac [C] time = 1.21399, size = 150, normalized size = 1.38

$$-\left(\frac{x \cos(bx + a)}{b} - \frac{\sin(bx + a)}{b^2}\right) \text{Ci}(bx + a) + \frac{2bx - 2a \log(|bx + a|) - a\Re(\text{Ci}(2bx + 2a)) - a\Re(\text{Ci}(-2bx - 2a)) - \Im(\text{Si}(2bx + 2a)) - \Im(\text{Si}(-2bx - 2a))}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*Ci(b*x+a)*sin(b*x+a),x, algorithm="giac")
```

```
[Out] -(x*cos(b*x + a)/b - sin(b*x + a)/b^2)*cos_integral(b*x + a) + 1/4*(2*b*x -
2*a*log(abs(b*x + a)) - a*real_part(cos_integral(2*b*x + 2*a)) - a*real_pa
rt(cos_integral(-2*b*x - 2*a)) - imag_part(cos_integral(2*b*x + 2*a)) + ima
g_part(cos_integral(-2*b*x - 2*a)) - 2*sin_integral(2*b*x + 2*a))/b^2
```


3.125 $\int \text{CosIntegral}(a + bx) \sin(a + bx) dx$

Optimal. Leaf size=47

$$\frac{\text{CosIntegral}(2a + 2bx)}{2b} - \frac{\text{CosIntegral}(a + bx) \cos(a + bx)}{b} + \frac{\log(a + bx)}{2b}$$

[Out] -((Cos[a + b*x]*CosIntegral[a + b*x])/b) + CosIntegral[2*a + 2*b*x]/(2*b) + Log[a + b*x]/(2*b)

Rubi [A] time = 0.076047, antiderivative size = 47, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 3, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.231$, Rules used = {6518, 3312, 3302}

$$\frac{\text{CosIntegral}(2a + 2bx)}{2b} - \frac{\text{CosIntegral}(a + bx) \cos(a + bx)}{b} + \frac{\log(a + bx)}{2b}$$

Antiderivative was successfully verified.

[In] Int[CosIntegral[a + b*x]*Sin[a + b*x], x]

[Out] -((Cos[a + b*x]*CosIntegral[a + b*x])/b) + CosIntegral[2*a + 2*b*x]/(2*b) + Log[a + b*x]/(2*b)

Rule 6518

Int[CosIntegral[(c_.) + (d_.)*(x_)]*Sin[(a_.) + (b_.)*(x_)], x_Symbol] := -Simp[(Cos[a + b*x]*CosIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 3312

Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned} \int \text{Ci}(a + bx) \sin(a + bx) dx &= -\frac{\cos(a + bx)\text{Ci}(a + bx)}{b} + \int \frac{\cos^2(a + bx)}{a + bx} dx \\ &= -\frac{\cos(a + bx)\text{Ci}(a + bx)}{b} + \int \left(\frac{1}{2(a + bx)} + \frac{\cos(2a + 2bx)}{2(a + bx)} \right) dx \\ &= -\frac{\cos(a + bx)\text{Ci}(a + bx)}{b} + \frac{\log(a + bx)}{2b} + \frac{1}{2} \int \frac{\cos(2a + 2bx)}{a + bx} dx \\ &= -\frac{\cos(a + bx)\text{Ci}(a + bx)}{b} + \frac{\text{Ci}(2a + 2bx)}{2b} + \frac{\log(a + bx)}{2b} \end{aligned}$$

Mathematica [A] time = 0.0241664, size = 46, normalized size = 0.98

$$\frac{\text{CosIntegral}(2(a + bx))}{2b} - \frac{\text{CosIntegral}(a + bx) \cos(a + bx)}{b} + \frac{\log(a + bx)}{2b}$$

Antiderivative was successfully verified.

[In] Integrate[CosIntegral[a + b*x]*Sin[a + b*x], x]

[Out] -((Cos[a + b*x]*CosIntegral[a + b*x])/b) + CosIntegral[2*(a + b*x)]/(2*b) + Log[a + b*x]/(2*b)

Maple [A] time = 0.052, size = 44, normalized size = 0.9

$$\frac{\text{Ci}(2bx + 2a)}{2b} - \frac{\text{Ci}(bx + a) \cos(bx + a)}{b} + \frac{\ln(bx + a)}{2b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x+a)*sin(b*x+a), x)

[Out] 1/2*Ci(2*b*x+2*a)/b-Ci(b*x+a)*cos(b*x+a)/b+1/2*ln(b*x+a)/b

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Ci}(bx + a) \sin(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)*sin(b*x+a), x, algorithm="maxima")

[Out] integrate(Ci(b*x + a)*sin(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(\text{Ci}(bx + a) \sin(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)*sin(b*x+a), x, algorithm="fricas")

[Out] integral(cos_integral(b*x + a)*sin(b*x + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \sin(a + bx) \text{Ci}(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)*sin(b*x+a),x)

[Out] Integral(sin(a + b*x)*Ci(a + b*x), x)

Giac [B] time = 1.19141, size = 130, normalized size = 2.77

$$-\frac{\cos(bx+a) \operatorname{Ci}(bx+a)}{b} + \frac{\cos(2a)^2 \operatorname{Ci}(2bx+2a) + \cos(2a)^2 \operatorname{Ci}(-2bx-2a) + \operatorname{Ci}(2bx+2a) \sin(2a)^2 + \operatorname{Ci}(-2bx-2a) \sin(2a)^2}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)*sin(b*x+a),x, algorithm="giac")

[Out] $-\cos(bx+a) \operatorname{cos_integral}(bx+a)/b + 1/4 * (\cos(2a)^2 \operatorname{cos_integral}(2bx+2a) + \cos(2a)^2 \operatorname{cos_integral}(-2bx-2a) + \operatorname{cos_integral}(2bx+2a) * \sin(2a)^2 + \operatorname{cos_integral}(-2bx-2a) * \sin(2a)^2 + 2 * \log(bx+a)) / b$

$$3.126 \quad \int \frac{\text{CosIntegral}(a+bx) \sin(a+bx)}{x} dx$$

Optimal. Leaf size=18

$$\text{CannotIntegrate}\left(\frac{\text{CosIntegral}(a+bx) \sin(a+bx)}{x}, x\right)$$

[Out] CannotIntegrate[(CosIntegral[a + b*x]*Sin[a + b*x])/x, x]

Rubi [A] time = 0.131469, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{CosIntegral}(a+bx) \sin(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Int[(CosIntegral[a + b*x]*Sin[a + b*x])/x,x]

[Out] Defer[Int] [(CosIntegral[a + b*x]*Sin[a + b*x])/x, x]

Rubi steps

$$\int \frac{\text{Ci}(a+bx) \sin(a+bx)}{x} dx = \int \frac{\text{Ci}(a+bx) \sin(a+bx)}{x} dx$$

Mathematica [A] time = 6.96945, size = 0, normalized size = 0.

$$\int \frac{\text{CosIntegral}(a+bx) \sin(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[(CosIntegral[a + b*x]*Sin[a + b*x])/x,x]

[Out] Integrate[(CosIntegral[a + b*x]*Sin[a + b*x])/x, x]

Maple [A] time = 0.085, size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx+a) \sin(bx+a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x+a)*sin(b*x+a)/x,x)

[Out] int(Ci(b*x+a)*sin(b*x+a)/x,x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx + a) \sin(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)*sin(b*x+a)/x,x, algorithm="maxima")

[Out] integrate(Ci(b*x + a)*sin(b*x + a)/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(bx + a) \sin(bx + a)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)*sin(b*x+a)/x,x, algorithm="fricas")

[Out] integral(cos_integral(b*x + a)*sin(b*x + a)/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sin(a + bx) \text{Ci}(a + bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)*sin(b*x+a)/x,x)

[Out] Integral(sin(a + b*x)*Ci(a + b*x)/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx + a) \sin(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)*sin(b*x+a)/x,x, algorithm="giac")

[Out] integrate(Ci(b*x + a)*sin(b*x + a)/x, x)

3.127 $\int x^2 \cos(a + bx) \text{CosIntegral}(a + bx) dx$

Optimal. Leaf size=185

$$-\frac{a^2 \text{Si}(2a + 2bx)}{2b^3} + \frac{a \text{CosIntegral}(2a + 2bx)}{b^3} - \frac{2 \text{CosIntegral}(a + bx) \sin(a + bx)}{b^3} + \frac{2x \text{CosIntegral}(a + bx) \cos(a + bx)}{b^2}$$

[Out] $-(x/b^2) - (a \cos[2a + 2bx])/(4b^3) + (x \cos[2a + 2bx])/(4b^2) + (2x \cos[a + bx] \text{CosIntegral}[a + bx])/b^2 + (a \text{CosIntegral}[2a + 2bx])/b^3 + (a \log[a + bx])/b^3 - (\cos[a + bx] \sin[a + bx])/b^3 - (2 \text{CosIntegral}[a + bx] \sin[a + bx])/b^3 + (x^2 \text{CosIntegral}[a + bx] \sin[a + bx])/b - \sin[2a + 2bx]/(8b^3) + \text{SinIntegral}[2a + 2bx]/b^3 - (a^2 \text{SinIntegral}[2a + 2bx])/(2b^3)$

Rubi [A] time = 0.585556, antiderivative size = 185, normalized size of antiderivative = 1., number of steps used = 21, number of rules used = 16, integrand size = 16, $\frac{\text{number of rules}}{\text{integrand size}} = 1.$, Rules used = {6514, 4573, 6741, 6742, 2638, 3296, 2637, 3299, 6520, 2635, 8, 3312, 3302, 6512, 4406, 12}

$$-\frac{a^2 \text{Si}(2a + 2bx)}{2b^3} + \frac{a \text{CosIntegral}(2a + 2bx)}{b^3} - \frac{2 \text{CosIntegral}(a + bx) \sin(a + bx)}{b^3} + \frac{2x \text{CosIntegral}(a + bx) \cos(a + bx)}{b^2}$$

Antiderivative was successfully verified.

[In] $\text{Int}[x^2 \cos[a + bx] \text{CosIntegral}[a + bx], x]$

[Out] $-(x/b^2) - (a \cos[2a + 2bx])/(4b^3) + (x \cos[2a + 2bx])/(4b^2) + (2x \cos[a + bx] \text{CosIntegral}[a + bx])/b^2 + (a \text{CosIntegral}[2a + 2bx])/b^3 + (a \log[a + bx])/b^3 - (\cos[a + bx] \sin[a + bx])/b^3 - (2 \text{CosIntegral}[a + bx] \sin[a + bx])/b^3 + (x^2 \text{CosIntegral}[a + bx] \sin[a + bx])/b - \sin[2a + 2bx]/(8b^3) + \text{SinIntegral}[2a + 2bx]/b^3 - (a^2 \text{SinIntegral}[2a + 2bx])/(2b^3)$

Rule 6514

$\text{Int}[\cos[(a_.) + (b_.)(x_.)] \text{CosIntegral}[(c_.) + (d_.)(x_.)] ((e_.) + (f_.)(x_.))^m, x_Symbol] \rightarrow \text{Simp}[(e + fx)^m \sin[a + bx] \text{CosIntegral}[c + dx]/b, x] + (-\text{Dist}[d/b, \text{Int}[(e + fx)^m \sin[a + bx] \text{Cos}[c + dx]/(c + dx), x], x] - \text{Dist}[(f m)/b, \text{Int}[(e + fx)^{m-1} \sin[a + bx] \text{CosIntegral}[c + dx], x], x]) /; \text{FreeQ}\{a, b, c, d, e, f\}, x \&\& \text{IGtQ}[m, 0]$

Rule 4573

$\text{Int}[\cos[w_]^{(p_.)}(u_.) \sin[v_]^{(p_.)}, x_Symbol] \rightarrow \text{Dist}[1/2^p, \text{Int}[u \sin[2*v]^p, x], x] /; \text{EqQ}[w, v] \&\& \text{IntegerQ}[p]$

Rule 6741

$\text{Int}[u_, x_Symbol] \rightarrow \text{With}\{v = \text{NormalizeIntegrand}[u, x]\}, \text{Int}[v, x] /; v \neq u]$

Rule 6742

$\text{Int}[u_, x_Symbol] \rightarrow \text{With}\{v = \text{ExpandIntegrand}[u, x]\}, \text{Int}[v, x] /; \text{SumQ}[v]$

Rule 2638

$\text{Int}[\sin[(c_.) + (d_.)(x_.)], x_Symbol] \rightarrow -\text{Simp}[\text{Cos}[c + d*x]/d, x] /; \text{FreeQ}[\{c, d\}, x]$

Rule 3296

$\text{Int}[(c_.) + (d_.)(x_.)]^{(m_.)} \sin[(e_.) + (f_.)(x_.)], x_Symbol] \rightarrow -\text{Simp}[(c + d*x)^m \text{Cos}[e + f*x]/f, x] + \text{Dist}[(d*m)/f, \text{Int}[(c + d*x)^{(m-1)} \text{Cos}[e + f*x], x], x] /; \text{FreeQ}[\{c, d, e, f\}, x] \&\& \text{GtQ}[m, 0]$

Rule 2637

$\text{Int}[\sin[\text{Pi}/2 + (c_.) + (d_.)(x_.)], x_Symbol] \rightarrow \text{Simp}[\text{Sin}[c + d*x]/d, x] /; \text{FreeQ}[\{c, d\}, x]$

Rule 3299

$\text{Int}[\sin[(e_.) + (f_.)(x_.)] / ((c_.) + (d_.)(x_.)), x_Symbol] \rightarrow \text{Simp}[\text{SinIntegral}[e + f*x]/d, x] /; \text{FreeQ}[\{c, d, e, f\}, x] \&\& \text{EqQ}[d*e - c*f, 0]$

Rule 6520

$\text{Int}[\text{CosIntegral}[(c_.) + (d_.)(x_.)] * ((e_.) + (f_.)(x_.))^{(m_.)} \text{Sin}[(a_.) + (b_.)(x_.)], x_Symbol] \rightarrow -\text{Simp}[(e + f*x)^m \text{Cos}[a + b*x] * \text{CosIntegral}[c + d*x]/b, x] + (\text{Dist}[d/b, \text{Int}[(e + f*x)^m \text{Cos}[a + b*x] * \text{Cos}[c + d*x]/(c + d*x), x], x] + \text{Dist}[(f*m)/b, \text{Int}[(e + f*x)^{(m-1)} \text{Cos}[a + b*x] * \text{CosIntegral}[c + d*x], x], x]) /; \text{FreeQ}[\{a, b, c, d, e, f\}, x] \&\& \text{IGtQ}[m, 0]$

Rule 2635

$\text{Int}[(b_.) \sin[(c_.) + (d_.)(x_.)]^{(n_.)}, x_Symbol] \rightarrow -\text{Simp}[(b * \text{Cos}[c + d*x] * (b * \text{Sin}[c + d*x])^{(n-1)}) / (d*n), x] + \text{Dist}[(b^2 * (n-1)) / n, \text{Int}[(b * \text{Sin}[c + d*x])^{(n-2)}, x], x] /; \text{FreeQ}[\{b, c, d\}, x] \&\& \text{GtQ}[n, 1] \&\& \text{IntegerQ}[2*n]$

Rule 8

$\text{Int}[a_, x_Symbol] \rightarrow \text{Simp}[a*x, x] /; \text{FreeQ}[a, x]$

Rule 3312

$\text{Int}[(c_.) + (d_.)(x_.)]^{(m_.)} \sin[(e_.) + (f_.)(x_.)]^{(n_.)}, x_Symbol] \rightarrow \text{Int}[\text{ExpandTrigReduce}[(c + d*x)^m, \text{Sin}[e + f*x]^n, x], x] /; \text{FreeQ}[\{c, d, e, f, m\}, x] \&\& \text{IGtQ}[n, 1] \&\& (!\text{RationalQ}[m] \mid\mid (\text{GeQ}[m, -1] \&\& \text{LtQ}[m, 1]))$

Rule 3302

$\text{Int}[\sin[(e_.) + (f_.)(x_.)] / ((c_.) + (d_.)(x_.)), x_Symbol] \rightarrow \text{Simp}[\text{CosIntegral}[e - \text{Pi}/2 + f*x]/d, x] /; \text{FreeQ}[\{c, d, e, f\}, x] \&\& \text{EqQ}[d*(e - \text{Pi}/2) - c*f, 0]$

Rule 6512

$\text{Int}[\text{Cos}[(a_.) + (b_.)(x_.)] * \text{CosIntegral}[(c_.) + (d_.)(x_.)], x_Symbol] \rightarrow \text{Simp}[(\text{Sin}[a + b*x] * \text{CosIntegral}[c + d*x]) / b, x] - \text{Dist}[d/b, \text{Int}[(\text{Sin}[a + b*x] * \text{Cos}[c + d*x]) / (c + d*x), x], x] /; \text{FreeQ}[\{a, b, c, d\}, x]$

Rule 4406

```
Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^(n)*Cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]
```

Rule 12

```
Int[(a_)*(u_), x_Symbol] := Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_)*(v_) /; FreeQ[b, x]]
```

Rubi steps

$$\begin{aligned}
 \int x^2 \cos(a + bx) \operatorname{Ci}(a + bx) dx &= \frac{x^2 \operatorname{Ci}(a + bx) \sin(a + bx)}{b} - \frac{2 \int x \operatorname{Ci}(a + bx) \sin(a + bx) dx}{b} - \int \frac{x^2 \cos(a + bx) \sin(a + bx)}{a + bx} dx \\
 &= \frac{2x \cos(a + bx) \operatorname{Ci}(a + bx)}{b^2} + \frac{x^2 \operatorname{Ci}(a + bx) \sin(a + bx)}{b} - \frac{1}{2} \int \frac{x^2 \sin(2(a + bx))}{a + bx} dx - \frac{2}{b} \int x \operatorname{Ci}(a + bx) \sin(a + bx) dx \\
 &= \frac{2x \cos(a + bx) \operatorname{Ci}(a + bx)}{b^2} - \frac{2 \operatorname{Ci}(a + bx) \sin(a + bx)}{b^3} + \frac{x^2 \operatorname{Ci}(a + bx) \sin(a + bx)}{b} - \frac{1}{2} \int \frac{x^2 \sin(2(a + bx))}{a + bx} dx \\
 &= \frac{2x \cos(a + bx) \operatorname{Ci}(a + bx)}{b^2} - \frac{2 \operatorname{Ci}(a + bx) \sin(a + bx)}{b^3} + \frac{x^2 \operatorname{Ci}(a + bx) \sin(a + bx)}{b} - \frac{1}{2} \int \frac{x^2 \sin(2(a + bx))}{a + bx} dx \\
 &= \frac{2x \cos(a + bx) \operatorname{Ci}(a + bx)}{b^2} - \frac{\cos(a + bx) \sin(a + bx)}{b^3} - \frac{2 \operatorname{Ci}(a + bx) \sin(a + bx)}{b^3} + \frac{x^2 \operatorname{Ci}(a + bx) \sin(a + bx)}{b} \\
 &= -\frac{x}{b^2} - \frac{a \cos(2a + 2bx)}{4b^3} + \frac{x \cos(2a + 2bx)}{4b^2} + \frac{2x \cos(a + bx) \operatorname{Ci}(a + bx)}{b^2} + \frac{a \log(a + bx)}{b^3} \\
 &= -\frac{x}{b^2} - \frac{a \cos(2a + 2bx)}{4b^3} + \frac{x \cos(2a + 2bx)}{4b^2} + \frac{2x \cos(a + bx) \operatorname{Ci}(a + bx)}{b^2} + \frac{a \operatorname{Ci}(2a + 2bx)}{b^3}
 \end{aligned}$$

Mathematica [A] time = 0.300744, size = 123, normalized size = 0.66

$$\frac{-4a^2 \operatorname{Si}(2(a + bx)) + 8 \operatorname{CosIntegral}(a + bx) \left((b^2 x^2 - 2) \sin(a + bx) + 2bx \cos(a + bx) \right) + 8a \operatorname{CosIntegral}(2(a + bx)) + 8 \operatorname{Si}(2(a + bx))}{8b^3}$$

Antiderivative was successfully verified.

```
[In] Integrate[x^2 * Cos[a + b*x] * CosIntegral[a + b*x], x]
```

```
[Out] (-8*b*x - 2*a * Cos[2*(a + b*x)] + 2*b*x * Cos[2*(a + b*x)] + 8*a * CosIntegral[2*(a + b*x)] + 8*a * Log[a + b*x] + 8 * CosIntegral[a + b*x] * (2*b*x * Cos[a + b*x] + (-2 + b^2*x^2) * Sin[a + b*x]) - 5 * Sin[2*(a + b*x)] + 8 * SinIntegral[2*(a + b*x)] - 4*a^2 * SinIntegral[2*(a + b*x)]) / (8*b^3)
```

Maple [A] time = 0.083, size = 168, normalized size = 0.9

$$\frac{x^2 \operatorname{Ci}(bx + a) \sin(bx + a)}{b} + 2 \frac{x \operatorname{Ci}(bx + a) \cos(bx + a)}{b^2} - 2 \frac{\operatorname{Ci}(bx + a) \sin(bx + a)}{b^3} + \frac{(\cos(bx + a))^2 x}{2b^2} - \frac{a \cos(bx + a)}{2b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(x^2 * Ci(b*x+a) * cos(b*x+a), x)
```



```
[Out] x^2*Ci(b*x+a)*sin(b*x+a)/b+2*x*Ci(b*x+a)*cos(b*x+a)/b^2-2*Ci(b*x+a)*sin(b*x+a)/b^3+1/2/b^2*cos(b*x+a)^2*x-1/2/b^3*a*cos(b*x+a)^2-5/4*cos(b*x+a)*sin(b*x+a)/b^3-5/4*x/b^2-5/4/b^3*a-1/2*a^2*Si(2*b*x+2*a)/b^3+a*ln(b*x+a)/b^3+a*Ci(2*b*x+2*a)/b^3+Si(2*b*x+2*a)/b^3
```

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \text{Ci}(bx + a) \cos(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*Ci(b*x+a)*cos(b*x+a),x, algorithm="maxima")
```

```
[Out] integrate(x^2*Ci(b*x + a)*cos(b*x + a), x)
```

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x^2 \cos(bx + a) \text{Ci}(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*Ci(b*x+a)*cos(b*x+a),x, algorithm="fricas")
```

```
[Out] integral(x^2*cos(b*x + a)*cos_integral(b*x + a), x)
```

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x^2 \cos(a + bx) \text{Ci}(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x**2*Ci(b*x+a)*cos(b*x+a),x)
```

```
[Out] Integral(x**2*cos(a + b*x)*Ci(a + b*x), x)
```

Giac [C] time = 1.20779, size = 221, normalized size = 1.19

$$\left(\frac{2x \cos(bx + a)}{b^2} + \frac{(b^2x^2 - 2) \sin(bx + a)}{b^3} \right) \text{Ci}(bx + a) - \frac{a^2 \Im(\text{Ci}(2bx + 2a)) - a^2 \Im(\text{Ci}(-2bx - 2a)) + 2a^2 \text{Si}(2bx + 2a)}{b^3}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x^2*Ci(b*x+a)*cos(b*x+a),x, algorithm="giac")
```

```
[Out] (2*x*cos(b*x + a)/b^2 + (b^2*x^2 - 2)*sin(b*x + a)/b^3)*cos_integral(b*x + a) - 1/4*(a^2*imag_part(cos_integral(2*b*x + 2*a)) - a^2*imag_part(cos_integral(-2*b*x - 2*a)) + 2*a^2*sin_integral(2*b*x + 2*a) + 4*b*x - 4*a*log(abs(b*x + a)) - 2*a*real_part(cos_integral(2*b*x + 2*a)) - 2*a*real_part(cos_integral(-2*b*x - 2*a)) - 2*imag_part(cos_integral(2*b*x + 2*a)) + 2*imag_part(cos_integral(-2*b*x - 2*a)) - 4*sin_integral(2*b*x + 2*a))/b^3
```

3.128 $\int x \cos(a + bx) \text{CosIntegral}(a + bx) dx$

Optimal. Leaf size=96

$$-\frac{\text{CosIntegral}(2a + 2bx)}{2b^2} + \frac{\text{CosIntegral}(a + bx) \cos(a + bx)}{b^2} + \frac{a \text{Si}(2a + 2bx)}{2b^2} - \frac{\log(a + bx)}{2b^2} + \frac{\cos(2a + 2bx)}{4b^2} + \frac{x \text{CosIntegral}(a + bx)}{b}$$

[Out] Cos[2*a + 2*b*x]/(4*b^2) + (Cos[a + b*x]*CosIntegral[a + b*x])/b^2 - CosIntegral[2*a + 2*b*x]/(2*b^2) - Log[a + b*x]/(2*b^2) + (x*CosIntegral[a + b*x]*Sin[a + b*x])/b + (a*SinIntegral[2*a + 2*b*x])/(2*b^2)

Rubi [A] time = 0.251984, antiderivative size = 96, normalized size of antiderivative = 1., number of steps used = 11, number of rules used = 9, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.643$, Rules used = {6514, 4573, 6741, 6742, 2638, 3299, 6518, 3312, 3302}

$$-\frac{\text{CosIntegral}(2a + 2bx)}{2b^2} + \frac{\text{CosIntegral}(a + bx) \cos(a + bx)}{b^2} + \frac{a \text{Si}(2a + 2bx)}{2b^2} - \frac{\log(a + bx)}{2b^2} + \frac{\cos(2a + 2bx)}{4b^2} + \frac{x \text{CosIntegral}(a + bx)}{b}$$

Antiderivative was successfully verified.

[In] Int[x*Cos[a + b*x]*CosIntegral[a + b*x],x]

[Out] Cos[2*a + 2*b*x]/(4*b^2) + (Cos[a + b*x]*CosIntegral[a + b*x])/b^2 - CosIntegral[2*a + 2*b*x]/(2*b^2) - Log[a + b*x]/(2*b^2) + (x*CosIntegral[a + b*x]*Sin[a + b*x])/b + (a*SinIntegral[2*a + 2*b*x])/(2*b^2)

Rule 6514

Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.), x_Symbol] :> Simp[((e + f*x)^m*Sin[a + b*x]*CosIntegral[c + d*x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Sin[a + b*x]*CosIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]

Rule 4573

Int[Cos[w_]^(p_.)*(u_.)*Sin[v_]^(p_.), x_Symbol] :> Dist[1/2^p, Int[u*Sin[2*v]^p, x], x] /; EqQ[w, v] && IntegerQ[p]

Rule 6741

Int[u_, x_Symbol] :> With[{v = NormalizeIntegrand[u, x]}, Int[v, x] /; v != u]

Rule 6742

Int[u_, x_Symbol] :> With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]]

Rule 2638

Int[sin[(c_.) + (d_.)*(x_)], x_Symbol] :> -Simp[Cos[c + d*x]/d, x] /; FreeQ[{c, d}, x]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 6518

Int[CosIntegral[(c_.) + (d_.)*(x_)]*Sin[(a_.) + (b_.)*(x_)], x_Symbol] := -Simp[(Cos[a + b*x]*CosIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 3312

Int[((c_.) + (d_.)*(x_))^(m_)*sin[(e_.) + (f_.)*(x_)]^(n_), x_Symbol] := Int[ExpandTrigReduce[(c + d*x)^m, Sin[e + f*x]^n, x], x] /; FreeQ[{c, d, e, f, m}, x] && IGtQ[n, 1] && (!RationalQ[m] || (GeQ[m, -1] && LtQ[m, 1]))

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned}
 \int x \cos(a + bx) \text{Ci}(a + bx) dx &= \frac{x \text{Ci}(a + bx) \sin(a + bx)}{b} - \frac{\int \text{Ci}(a + bx) \sin(a + bx) dx}{b} - \int \frac{x \cos(a + bx) \sin(a + bx)}{a + bx} \\
 &= \frac{\cos(a + bx) \text{Ci}(a + bx)}{b^2} + \frac{x \text{Ci}(a + bx) \sin(a + bx)}{b} - \frac{1}{2} \int \frac{x \sin(2(a + bx))}{a + bx} dx - \frac{\int \frac{\cos^2}{2(a + bx)}}{a} \\
 &= \frac{\cos(a + bx) \text{Ci}(a + bx)}{b^2} + \frac{x \text{Ci}(a + bx) \sin(a + bx)}{b} - \frac{1}{2} \int \frac{x \sin(2a + 2bx)}{a + bx} dx - \frac{\int \left(\frac{\cos^2}{2(a + bx)} \right)}{a} \\
 &= \frac{\cos(a + bx) \text{Ci}(a + bx)}{b^2} - \frac{\log(a + bx)}{2b^2} + \frac{x \text{Ci}(a + bx) \sin(a + bx)}{b} - \frac{1}{2} \int \left(\frac{\sin(2a + 2bx)}{b} \right) \\
 &= \frac{\cos(a + bx) \text{Ci}(a + bx)}{b^2} - \frac{\text{Ci}(2a + 2bx)}{2b^2} - \frac{\log(a + bx)}{2b^2} + \frac{x \text{Ci}(a + bx) \sin(a + bx)}{b} - \frac{\int \left(\frac{\sin(2a + 2bx)}{b} \right)}{a} \\
 &= \frac{\cos(2a + 2bx)}{4b^2} + \frac{\cos(a + bx) \text{Ci}(a + bx)}{b^2} - \frac{\text{Ci}(2a + 2bx)}{2b^2} - \frac{\log(a + bx)}{2b^2} + \frac{x \text{Ci}(a + bx) \sin(a + bx)}{b}
 \end{aligned}$$

Mathematica [A] time = 0.157884, size = 69, normalized size = 0.72

$$\frac{-2\text{CosIntegral}(2(a + bx)) + 4\text{CosIntegral}(a + bx)(bx \sin(a + bx) + \cos(a + bx)) + 2a\text{Si}(2(a + bx)) - 2\log(a + bx)}{4b^2}$$

Antiderivative was successfully verified.

[In] Integrate[x*Cos[a + b*x]*CosIntegral[a + b*x],x]

[Out] (Cos[2*(a + b*x)] - 2*CosIntegral[2*(a + b*x)] - 2*Log[a + b*x] + 4*CosIntegral[a + b*x]*(Cos[a + b*x] + b*x*Sin[a + b*x]) + 2*a*SinIntegral[2*(a + b*x)])/(4*b^2)

Maple [A] time = 0.062, size = 88, normalized size = 0.9

$$\frac{x \text{Ci}(bx + a) \sin(bx + a)}{b} + \frac{\text{Ci}(bx + a) \cos(bx + a)}{b^2} + \frac{(\cos(bx + a))^2}{2b^2} - \frac{\ln(bx + a)}{2b^2} - \frac{\text{Ci}(2bx + 2a)}{2b^2} + \frac{a \text{Si}(2bx + 2a)}{2b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(x*Ci(b*x+a)*cos(b*x+a),x)`

[Out] $x\text{Ci}(b*x+a)*\sin(b*x+a)/b+\text{Ci}(b*x+a)*\cos(b*x+a)/b^2+1/2/b^2*\cos(b*x+a)^2-1/2*\ln(b*x+a)/b^2-1/2*\text{Ci}(2*b*x+2*a)/b^2+1/2*a*\text{Si}(2*b*x+2*a)/b^2$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x\text{Ci}(bx+a)\cos(bx+a)dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Ci(b*x+a)*cos(b*x+a),x, algorithm="maxima")`

[Out] `integrate(x*Ci(b*x + a)*cos(b*x + a), x)`

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x\cos(bx+a)\text{Ci}(bx+a),x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Ci(b*x+a)*cos(b*x+a),x, algorithm="fricas")`

[Out] `integral(x*cos(b*x + a)*cos_integral(b*x + a), x)`

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x\cos(a+bx)\text{Ci}(a+bx)dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Ci(b*x+a)*cos(b*x+a),x)`

[Out] `Integral(x*cos(a + b*x)*Ci(a + b*x), x)`

Giac [C] time = 1.17762, size = 143, normalized size = 1.49

$$\left(\frac{x\sin(bx+a)}{b} + \frac{\cos(bx+a)}{b^2}\right)\text{Ci}(bx+a) + \frac{a\Im(\text{Ci}(2bx+2a)) - a\Im(\text{Ci}(-2bx-2a)) + 2a\text{Si}(2bx+2a) - 2\log(|bx+a|)}{4b^2}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate(x*Ci(b*x+a)*cos(b*x+a),x, algorithm="giac")`

[Out] $(x*\sin(b*x + a)/b + \cos(b*x + a)/b^2)*\cos_integral(b*x + a) + 1/4*(a*\text{imag_part}(\cos_integral(2*b*x + 2*a)) - a*\text{imag_part}(\cos_integral(-2*b*x - 2*a)) + 2*a*\sin_integral(2*b*x + 2*a) - 2*\log(\text{abs}(b*x + a)) - \text{real_part}(\cos_integral(2*b*x + 2*a)) - \text{real_part}(\cos_integral(-2*b*x - 2*a)))/b^2$

3.129 $\int \cos(a + bx) \mathbf{CosIntegral}(a + bx) dx$

Optimal. Leaf size=33

$$\frac{\mathbf{CosIntegral}(a + bx) \sin(a + bx)}{b} - \frac{\mathbf{Si}(2a + 2bx)}{2b}$$

[Out] (CosIntegral[a + b*x]*Sin[a + b*x])/b - SinIntegral[2*a + 2*b*x]/(2*b)

Rubi [A] time = 0.0562818, antiderivative size = 33, normalized size of antiderivative = 1., number of steps used = 4, number of rules used = 4, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.308$, Rules used = {6512, 4406, 12, 3299}

$$\frac{\mathbf{CosIntegral}(a + bx) \sin(a + bx)}{b} - \frac{\mathbf{Si}(2a + 2bx)}{2b}$$

Antiderivative was successfully verified.

[In] Int[Cos[a + b*x]*CosIntegral[a + b*x], x]

[Out] (CosIntegral[a + b*x]*Sin[a + b*x])/b - SinIntegral[2*a + 2*b*x]/(2*b)

Rule 6512

Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :> Simp[(Sin[a + b*x]*CosIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 4406

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*((c_.) + (d_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(n_.), x_Symbol] :> Int[ExpandTrigReduce[(c + d*x)^m, Sin[a + b*x]^n*cos[a + b*x]^p, x], x] /; FreeQ[{a, b, c, d, m}, x] && IGtQ[n, 0] && IGtQ[p, 0]

Rule 12

Int[(a_.)*(u_), x_Symbol] :> Dist[a, Int[u, x], x] /; FreeQ[a, x] && !MatchQ[u, (b_.)*(v_) /; FreeQ[b, x]]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rubi steps

$$\begin{aligned} \int \cos(a + bx) \mathbf{Ci}(a + bx) dx &= \frac{\mathbf{Ci}(a + bx) \sin(a + bx)}{b} - \int \frac{\cos(a + bx) \sin(a + bx)}{a + bx} dx \\ &= \frac{\mathbf{Ci}(a + bx) \sin(a + bx)}{b} - \int \frac{\sin(2a + 2bx)}{2(a + bx)} dx \\ &= \frac{\mathbf{Ci}(a + bx) \sin(a + bx)}{b} - \frac{1}{2} \int \frac{\sin(2a + 2bx)}{a + bx} dx \\ &= \frac{\mathbf{Ci}(a + bx) \sin(a + bx)}{b} - \frac{\mathbf{Si}(2a + 2bx)}{2b} \end{aligned}$$

Mathematica [A] time = 0.0187926, size = 32, normalized size = 0.97

$$\frac{\text{CosIntegral}(a + bx) \sin(a + bx)}{b} - \frac{\text{Si}(2(a + bx))}{2b}$$

Antiderivative was successfully verified.

[In] Integrate[Cos[a + b*x]*CosIntegral[a + b*x],x]

[Out] (CosIntegral[a + b*x]*Sin[a + b*x])/b - SinIntegral[2*(a + b*x)]/(2*b)

Maple [A] time = 0.053, size = 30, normalized size = 0.9

$$\frac{1}{b} \left(\text{Ci}(bx + a) \sin(bx + a) - \frac{\text{Si}(2bx + 2a)}{2} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x+a)*cos(b*x+a),x)

[Out] 1/b*(Ci(b*x+a)*sin(b*x+a)-1/2*Si(2*b*x+2*a))

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Ci}(bx + a) \cos(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)*cos(b*x+a),x, algorithm="maxima")

[Out] integrate(Ci(b*x + a)*cos(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(\cos(bx + a) \text{Ci}(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)*cos(b*x+a),x, algorithm="fricas")

[Out] integral(cos(b*x + a)*cos_integral(b*x + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \cos(a + bx) \text{Ci}(a + bx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x+a)*cos(b*x+a),x)
```

```
[Out] Integral(cos(a + b*x)*Ci(a + b*x), x)
```

Giac [C] time = 1.16471, size = 76, normalized size = 2.3

$$\frac{\operatorname{Ci}(bx+a)\sin(bx+a)}{b} - \frac{\Im(\operatorname{Ci}(2bx+2a)) - \Im(\operatorname{Ci}(-2bx-2a)) + 2\operatorname{Si}(2bx+2a)}{4b}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(Ci(b*x+a)*cos(b*x+a),x, algorithm="giac")
```

```
[Out] cos_integral(b*x + a)*sin(b*x + a)/b - 1/4*(imag_part(cos_integral(2*b*x +
2*a)) - imag_part(cos_integral(-2*b*x - 2*a)) + 2*sin_integral(2*b*x + 2*a)
)/b
```

$$3.130 \quad \int \frac{\cos(a+bx)\text{CosIntegral}(a+bx)}{x} dx$$

Optimal. Leaf size=18

$$\text{CannotIntegrate}\left(\frac{\text{CosIntegral}(a+bx)\cos(a+bx)}{x}, x\right)$$

[Out] CannotIntegrate[(Cos[a + b*x]*CosIntegral[a + b*x])/x, x]

Rubi [A] time = 0.07491, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\cos(a+bx)\text{CosIntegral}(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Int[(Cos[a + b*x]*CosIntegral[a + b*x])/x, x]

[Out] Defer[Int] [(Cos[a + b*x]*CosIntegral[a + b*x])/x, x]

Rubi steps

$$\int \frac{\cos(a+bx)\text{Ci}(a+bx)}{x} dx = \int \frac{\cos(a+bx)\text{Ci}(a+bx)}{x} dx$$

Mathematica [A] time = 3.23689, size = 0, normalized size = 0.

$$\int \frac{\cos(a+bx)\text{CosIntegral}(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[(Cos[a + b*x]*CosIntegral[a + b*x])/x, x]

[Out] Integrate[(Cos[a + b*x]*CosIntegral[a + b*x])/x, x]

Maple [A] time = 0.085, size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx+a)\cos(bx+a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(b*x+a)*cos(b*x+a)/x, x)

[Out] int(Ci(b*x+a)*cos(b*x+a)/x, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx + a) \cos(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)*cos(b*x+a)/x,x, algorithm="maxima")

[Out] integrate(Ci(b*x + a)*cos(b*x + a)/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\cos(bx + a) \text{Ci}(bx + a)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)*cos(b*x+a)/x,x, algorithm="fricas")

[Out] integral(cos(b*x + a)*cos_integral(b*x + a)/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\cos(a + bx) \text{Ci}(a + bx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)*cos(b*x+a)/x,x)

[Out] Integral(cos(a + b*x)*Ci(a + b*x)/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(bx + a) \cos(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(b*x+a)*cos(b*x+a)/x,x, algorithm="giac")

[Out] integrate(Ci(b*x + a)*cos(b*x + a)/x, x)

3.131 $\int x \text{CosIntegral}(c + dx) \sin(a + bx) dx$

Optimal. Leaf size=371

$$\frac{\sin\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b^2} - \frac{\sin\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b+d)}{d} + x(b+d)\right)}{2b^2} + \frac{\sin(a + bx) \text{CosIntegral}(c + dx)}{b^2}$$

```
[Out] -(c*cos[a - (b*c)/d]*CosIntegral[(c*(b - d))/d + (b - d)*x])/(2*b*d) - (x*cos[a + b*x]*CosIntegral[c + d*x])/b - (c*cos[a - (b*c)/d]*CosIntegral[(c*(b + d))/d + (b + d)*x])/(2*b*d) - (CosIntegral[(c*(b - d))/d + (b - d)*x]*Sin[a - (b*c)/d])/(2*b^2) - (CosIntegral[(c*(b + d))/d + (b + d)*x]*Sin[a - (b*c)/d])/(2*b^2) + (CosIntegral[c + d*x]*Sin[a + b*x])/b^2 + Sin[a - c + (b - d)*x]/(2*b*(b - d)) + Sin[a + c + (b + d)*x]/(2*b*(b + d)) - (Cos[a - (b*c)/d]*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b^2) + (c*sin[a - (b*c)/d]*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b*d) - (Cos[a - (b*c)/d]*SinIntegral[(c*(b + d))/d + (b + d)*x])/(2*b^2) + (c*sin[a - (b*c)/d]*SinIntegral[(c*(b + d))/d + (b + d)*x])/(2*b*d)
```

Rubi [A] time = 1.01904, antiderivative size = 371, normalized size of antiderivative = 1., number of steps used = 24, number of rules used = 9, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.643$, Rules used = {6520, 4609, 6742, 2637, 3303, 3299, 3302, 6512, 4430}

$$\frac{\sin\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b^2} - \frac{\sin\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b+d)}{d} + x(b+d)\right)}{2b^2} + \frac{\sin(a + bx) \text{CosIntegral}(c + dx)}{b^2}$$

Antiderivative was successfully verified.

```
[In] Int[x*CosIntegral[c + d*x]*Sin[a + b*x],x]
```

```
[Out] -(c*cos[a - (b*c)/d]*CosIntegral[(c*(b - d))/d + (b - d)*x])/(2*b*d) - (x*cos[a + b*x]*CosIntegral[c + d*x])/b - (c*cos[a - (b*c)/d]*CosIntegral[(c*(b + d))/d + (b + d)*x])/(2*b*d) - (CosIntegral[(c*(b - d))/d + (b - d)*x]*Sin[a - (b*c)/d])/(2*b^2) - (CosIntegral[(c*(b + d))/d + (b + d)*x]*Sin[a - (b*c)/d])/(2*b^2) + (CosIntegral[c + d*x]*Sin[a + b*x])/b^2 + Sin[a - c + (b - d)*x]/(2*b*(b - d)) + Sin[a + c + (b + d)*x]/(2*b*(b + d)) - (Cos[a - (b*c)/d]*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b^2) + (c*sin[a - (b*c)/d]*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b*d) - (Cos[a - (b*c)/d]*SinIntegral[(c*(b + d))/d + (b + d)*x])/(2*b^2) + (c*sin[a - (b*c)/d]*SinIntegral[(c*(b + d))/d + (b + d)*x])/(2*b*d)
```

Rule 6520

```
Int[CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)], x_Symbol] :> -Simp[((e + f*x)^m*cos[a + b*x]*CosIntegral[c + d*x])/b, x] + (Dist[d/b, Int[((e + f*x)^m*cos[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] + Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*cos[a + b*x]*CosIntegral[c + d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 4609

```
Int[Cos[(a_.) + (b_.)*(x_)]^(m_.)*Cos[(c_.) + (d_.)*(x_)]^(n_.)*(u_.), x_Symbol] :> Int[ExpandTrigReduce[u, Cos[a + b*x]^m*cos[c + d*x]^n, x], x] /; FreeQ[{a, b, c, d}, x] && IGtQ[m, 0] && IGtQ[n, 0]
```

Rule 6742

```
Int[u_, x_Symbol] := With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]
]
```

Rule 2637

```
Int[sin[Pi/2 + (c_.) + (d_.)*(x_)], x_Symbol] := Simp[Sin[c + d*x]/d, x] /;
FreeQ[{c, d}, x]
```

Rule 3303

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Dist[Cos[(d*
e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f
)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] &&
NeQ[d*e - c*f, 0]
```

Rule 3299

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 3302

```
Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rule 6512

```
Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)], x_Symbol] := S
imp[(Sin[a + b*x]*CosIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]
*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 4430

```
Int[Cos[(c_.) + (d_.)*(x_)]^(q_.)*((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b
_.)*(x_)]^(p_.), x_Symbol] := Int[ExpandTrigReduce[(e + f*x)^m, Sin[a + b*x
]^p*Cos[c + d*x]^q, x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[p, 0]
&& IGtQ[q, 0]
```

Rubi steps

$$\begin{aligned}
\int x \operatorname{Ci}(c+dx) \sin(a+bx) dx &= -\frac{x \cos(a+bx) \operatorname{Ci}(c+dx)}{b} + \frac{\int \cos(a+bx) \operatorname{Ci}(c+dx) dx}{b} + \frac{d \int \frac{x \cos(a+bx) \cos(c+dx)}{c+dx} dx}{b} \\
&= -\frac{x \cos(a+bx) \operatorname{Ci}(c+dx)}{b} + \frac{\operatorname{Ci}(c+dx) \sin(a+bx)}{b^2} - \frac{d \int \frac{\cos(c+dx) \sin(a+bx)}{c+dx} dx}{b^2} + \frac{d \int \left(\frac{x \cos(a+bx) \cos(c+dx)}{c+dx} \right) dx}{b^2} \\
&= -\frac{x \cos(a+bx) \operatorname{Ci}(c+dx)}{b} + \frac{\operatorname{Ci}(c+dx) \sin(a+bx)}{b^2} - \frac{d \int \left(\frac{\sin(a-c+(b-d)x}{2(c+dx)} + \frac{\sin(a+c+(b+d)x}{2(c+dx)} \right) dx}{b^2} \\
&= -\frac{x \cos(a+bx) \operatorname{Ci}(c+dx)}{b} + \frac{\operatorname{Ci}(c+dx) \sin(a+bx)}{b^2} - \frac{d \int \frac{\sin(a-c+(b-d)x}{c+dx} dx}{2b^2} - \frac{d \int \frac{\sin(a+c+(b+d)x}{c+dx} dx}{2b^2} \\
&= -\frac{x \cos(a+bx) \operatorname{Ci}(c+dx)}{b} + \frac{\operatorname{Ci}(c+dx) \sin(a+bx)}{b^2} + \frac{\int \cos(a-c+(b-d)x) dx}{2b} + \frac{\int \cos(a+c+(b+d)x) dx}{2b} \\
&= -\frac{x \cos(a+bx) \operatorname{Ci}(c+dx)}{b} - \frac{\operatorname{Ci}\left(\frac{c(b-d)}{d} + (b-d)x\right) \sin\left(a - \frac{bc}{d}\right)}{2b^2} - \frac{\operatorname{Ci}\left(\frac{c(b+d)}{d} + (b+d)x\right) \sin\left(a + \frac{bc}{d}\right)}{2b^2} \\
&= -\frac{c \cos\left(a - \frac{bc}{d}\right) \operatorname{Ci}\left(\frac{c(b-d)}{d} + (b-d)x\right)}{2bd} - \frac{x \cos(a+bx) \operatorname{Ci}(c+dx)}{b} - \frac{c \cos\left(a + \frac{bc}{d}\right) \operatorname{Ci}\left(\frac{c(b+d)}{d} + (b+d)x\right)}{2bd}
\end{aligned}$$

Mathematica [C] time = 6.40292, size = 328, normalized size = 0.88

$$-4 \operatorname{CosIntegral}(c+dx)(bx \cos(a+bx) - \sin(a+bx)) + \frac{e^{-ia} \left(-(bc+id)e^{\frac{ibc}{d}} \operatorname{ExpIntegralEi}\left(-\frac{i(b-d)(c+dx)}{d}\right) - (bc+id)e^{\frac{ibc}{d}} \operatorname{ExpIntegralEi}\left(-\frac{i(b+d)(c+dx)}{d}\right) \right)}{d}$$

Antiderivative was successfully verified.

[In] Integrate[x*CosIntegral[c + d*x]*Sin[a + b*x], x]

[Out] (((I*b*d*(1/((b + d)*E^(I*(b + d)*x)) + E^(I*(2*c - b*x + d*x))/(b - d)))/E^(I*c) - (b*c + I*d)*E^((I*b*c)/d)*ExpIntegralEi[(-I)*(b - d)*(c + d*x))/d] - (b*c + I*d)*E^((I*b*c)/d)*ExpIntegralEi[(-I)*(b + d)*(c + d*x))/d])/(d * E^(I*a)) - (E^(I*(a - c))*(I*b*d*(E^(I*(b - d)*x)/(b - d) + E^(I*(2*c + (b + d)*x))/(b + d)) + ((b*c - I*d)*ExpIntegralEi[(I*(b - d)*(c + d*x))/d])/E^((I*c*(b - d))/d) + ((b*c - I*d)*ExpIntegralEi[(I*(b + d)*(c + d*x))/d])/E^((I*c*(b - d))/d))/d - 4*CosIntegral[c + d*x]*(b*x*Cos[a + b*x] - Sin[a + b*x]))/(4*b^2)

Maple [B] time = 0.102, size = 1208, normalized size = 3.3

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*Ci(d*x+c)*sin(b*x+a), x)

[Out] (Ci(d*x+c)/b*(1/b*d*(-(b/d*(d*x+c)+(a*d-b*c)/d)*cos(b/d*(d*x+c)+(a*d-b*c)/d)+sin(b/d*(d*x+c)+(a*d-b*c)/d))+a*d/b*cos(b/d*(d*x+c)+(a*d-b*c)/d)-1/b*(-1/2/(b-d)*d*sin((b-d)/d*(d*x+c)+(a*d-b*c)/d)-1/2*(a*d-b*c)*d/(b-d)*(Si((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*sin((-a*d+b*c)/d)/d+Ci((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*cos((-a*d+b*c)/d)/d)+1/2/(b-d)*d^2*a*(Si((b-d)/d

$$\begin{aligned} & * (d*x+c) + (a*d-b*c)/d + (-a*d+b*c)/d * \sin((-a*d+b*c)/d)/d + \text{Ci}((b-d)/d*(d*x+c) + \\ & a*d-b*c)/d + (-a*d+b*c)/d * \cos((-a*d+b*c)/d)/d - 1/2/(b-d)*c*d^2*(\text{Si}((b-d)/d*(d*x+c) + \\ & (a*d-b*c)/d + (-a*d+b*c)/d) * \sin((-a*d+b*c)/d)/d + \text{Ci}((b-d)/d*(d*x+c) + (a*d-b*c)/d + \\ & (-a*d+b*c)/d) * \cos((-a*d+b*c)/d)/d - 1/2/(b+d)*d*\sin((b+d)/d*(d*x+c) + (a*d-b*c)/d + \\ & (-a*d+b*c)/d) - 1/2*(a*d-b*c)*d/(b+d)*(\text{Si}((b+d)/d*(d*x+c) + (a*d-b*c)/d + (-a*d+b*c)/d) * \\ & \sin((-a*d+b*c)/d)/d + \text{Ci}((b+d)/d*(d*x+c) + (a*d-b*c)/d + (-a*d+b*c)/d) * \cos((-a*d+b*c)/d)/d \\ & + 1/2/(b+d)*d^2*a*(\text{Si}((b+d)/d*(d*x+c) + (a*d-b*c)/d + (-a*d+b*c)/d) * \sin((-a*d+b*c)/d)/d + \\ & \text{Ci}((b+d)/d*(d*x+c) + (a*d-b*c)/d + (-a*d+b*c)/d) * \cos((-a*d+b*c)/d)/d + 1/2/(b+d)*c*d^2*(\text{Si}((b+d)/d*(d*x+c) + \\ & (a*d-b*c)/d + (-a*d+b*c)/d) * \sin((-a*d+b*c)/d)/d + \text{Ci}((b+d)/d*(d*x+c) + (a*d-b*c)/d + (-a*d+b*c)/d) * \\ & \cos((-a*d+b*c)/d)/d + 1/2/b*d^2*(\text{Si}((b-d)/d*(d*x+c) + (a*d-b*c)/d + (-a*d+b*c)/d) * \cos((-a*d+b*c)/d)/d \\ & - \text{Ci}((b-d)/d*(d*x+c) + (a*d-b*c)/d + (-a*d+b*c)/d) * \sin((-a*d+b*c)/d)/d + 1/2/b*d^2*(\text{Si}((b+d)/d*(d*x+c) + \\ & (a*d-b*c)/d + (-a*d+b*c)/d) * \cos((-a*d+b*c)/d)/d - \text{Ci}((b+d)/d*(d*x+c) + (a*d-b*c)/d + (-a*d+b*c)/d) * \\ & \sin((-a*d+b*c)/d)/d) \end{aligned}$$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \text{Ci}(dx + c) \sin(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(d*x+c)*sin(b*x+a), x, algorithm="maxima")

[Out] integrate(x*Ci(d*x + c)*sin(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(x \text{Ci}(dx + c) \sin(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(d*x+c)*sin(b*x+a), x, algorithm="fricas")

[Out] integral(x*cos_integral(d*x + c)*sin(b*x + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \sin(a + bx) \text{Ci}(c + dx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(d*x+c)*sin(b*x+a), x)

[Out] Integral(x*sin(a + b*x)*Ci(c + d*x), x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*Ci(d*x+c)*sin(b*x+a),x, algorithm="giac")
```

```
[Out] Timed out
```

3.132 $\int \text{CosIntegral}(c + dx) \sin(a + bx) dx$

Optimal. Leaf size=154

$$\frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b} - \frac{\cos(a + bx) \text{CosIntegral}(c + dx)}{b} + \frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b+d)}{d}\right)}{2b}$$

[Out] (Cos[a - (b*c)/d]*CosIntegral[(c*(b - d))/d + (b - d)*x])/(2*b) - (Cos[a + b*x]*CosIntegral[c + d*x])/b + (Cos[a - (b*c)/d]*CosIntegral[(c*(b + d))/d + (b + d)*x])/(2*b) - (Sin[a - (b*c)/d]*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b) - (Sin[a - (b*c)/d]*SinIntegral[(c*(b + d))/d + (b + d)*x])/(2*b)

Rubi [A] time = 0.221602, antiderivative size = 154, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {6518, 4429, 3303, 3299, 3302}

$$\frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b} - \frac{\cos(a + bx) \text{CosIntegral}(c + dx)}{b} + \frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b+d)}{d}\right)}{2b}$$

Antiderivative was successfully verified.

[In] Int[CosIntegral[c + d*x]*Sin[a + b*x], x]

[Out] (Cos[a - (b*c)/d]*CosIntegral[(c*(b - d))/d + (b - d)*x])/(2*b) - (Cos[a + b*x]*CosIntegral[c + d*x])/b + (Cos[a - (b*c)/d]*CosIntegral[(c*(b + d))/d + (b + d)*x])/(2*b) - (Sin[a - (b*c)/d]*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b) - (Sin[a - (b*c)/d]*SinIntegral[(c*(b + d))/d + (b + d)*x])/(2*b)

Rule 6518

Int[CosIntegral[(c_.) + (d_.)*(x_)]*Sin[(a_.) + (b_.)*(x_)], x_Symbol] := -Simp[(Cos[a + b*x]*CosIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 4429

Int[Cos[(a_.) + (b_.)*(x_)]^(p_.)*Cos[(c_.) + (d_.)*(x_)]^(q_.)*((e_.) + (f_.)*(x_))^(m_.), x_Symbol] := Int[ExpandTrigReduce[(e + f*x)^m, Cos[a + b*x]^p*Cos[c + d*x]^q, x], x] /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[p, 0] && IGtQ[q, 0] && IntegerQ[m]

Rule 3303

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned} \int \text{Ci}(c+dx) \sin(a+bx) dx &= -\frac{\cos(a+bx)\text{Ci}(c+dx)}{b} + \frac{d \int \frac{\cos(a+bx)\cos(c+dx)}{c+dx} dx}{b} \\ &= -\frac{\cos(a+bx)\text{Ci}(c+dx)}{b} + \frac{d \int \left(\frac{\cos(a-c+(b-d)x)}{2(c+dx)} + \frac{\cos(a+c+(b+d)x)}{2(c+dx)} \right) dx}{b} \\ &= -\frac{\cos(a+bx)\text{Ci}(c+dx)}{b} + \frac{d \int \frac{\cos(a-c+(b-d)x)}{c+dx} dx}{2b} + \frac{d \int \frac{\cos(a+c+(b+d)x)}{c+dx} dx}{2b} \\ &= -\frac{\cos(a+bx)\text{Ci}(c+dx)}{b} + \frac{\left(d \cos\left(a - \frac{bc}{d}\right) \right) \int \frac{\cos\left(\frac{c(b-d)}{d} + (b-d)x\right)}{c+dx} dx}{2b} + \frac{\left(d \cos\left(a - \frac{bc}{d}\right) \right) \int \frac{\cos\left(\frac{c(b+d)}{d} + (b+d)x\right)}{c+dx} dx}{2b} \\ &= \frac{\cos\left(a - \frac{bc}{d}\right) \text{Ci}\left(\frac{c(b-d)}{d} + (b-d)x\right)}{2b} - \frac{\cos(a+bx)\text{Ci}(c+dx)}{b} + \frac{\cos\left(a - \frac{bc}{d}\right) \text{Ci}\left(\frac{c(b+d)}{d} + (b+d)x\right)}{2b} \end{aligned}$$

Mathematica [C] time = 1.38716, size = 144, normalized size = 0.94

$$\frac{-4 \cos(a+bx) \text{CosIntegral}(c+dx) + \left(\text{ExpIntegralEi}\left(-\frac{i(b-d)(c+dx)}{d}\right) + \text{ExpIntegralEi}\left(-\frac{i(b+d)(c+dx)}{d}\right) \right) \left(\cos\left(a - \frac{bc}{d}\right) - i \sin\left(a - \frac{bc}{d}\right) \right)}{4b}$$

Antiderivative was successfully verified.

[In] Integrate[CosIntegral[c + d*x]*Sin[a + b*x], x]

[Out] (-4*Cos[a + b*x]*CosIntegral[c + d*x] + (ExpIntegralEi[(-I)*(b - d)*(c + d*x)/d] + ExpIntegralEi[(-I)*(b + d)*(c + d*x)/d])*(Cos[a - (b*c)/d] - I*Sin[a - (b*c)/d]) + (ExpIntegralEi[(I*(b - d)*(c + d*x))/d] + ExpIntegralEi[(I*(b + d)*(c + d*x))/d])*(Cos[a - (b*c)/d] + I*Sin[a - (b*c)/d]))/(4*b)

Maple [A] time = 0.078, size = 280, normalized size = 1.8

$$\frac{1}{d} \left(-\frac{\text{Ci}(dx+c)d}{b} \cos\left(\frac{b(dx+c)}{d} + \frac{ad-bc}{d}\right) + \frac{d}{b} \left(\frac{1}{2} \left(\frac{\text{Si}\left(\frac{(b-d)(dx+c)}{d} + \frac{ad-bc}{d} + \frac{-ad+bc}{d}\right)}{d} \sin\left(\frac{-ad+bc}{d}\right) + \frac{1}{d} \text{Ci}\left(\frac{(b-d)(dx+c)}{d} + \frac{ad-bc}{d} + \frac{-ad+bc}{d}\right) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(d*x+c)*sin(b*x+a), x)

[Out] (-Ci(d*x+c)/b*d*cos(b/d*(d*x+c)+(a*d-b*c)/d)+1/b*d*(1/2*d*(Si((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*sin((-a*d+b*c)/d)/d+Ci((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*cos((-a*d+b*c)/d)/d+1/2*d*(Si((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*sin((-a*d+b*c)/d)/d+Ci((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*cos((-a*d+b*c)/d)/d)))/d

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \text{Ci}(dx + c) \sin(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*sin(b*x+a),x, algorithm="maxima")

[Out] integrate(Ci(d*x + c)*sin(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\text{integral}(\text{Ci}(dx + c) \sin(bx + a), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*sin(b*x+a),x, algorithm="fricas")

[Out] integral(cos_integral(d*x + c)*sin(b*x + a), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \sin(a + bx) \text{Ci}(c + dx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*sin(b*x+a),x)

[Out] Integral(sin(a + b*x)*Ci(c + d*x), x)

Giac [C] time = 1.88639, size = 12438, normalized size = 80.77

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*sin(b*x+a),x, algorithm="giac")

[Out] $\frac{1}{4} * (\text{real_part}(\text{cos_integral}(bx + dx + c + bc/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(bc + cd)/d)^2 * \tan(1/2*(bc - cd)/d)^2 + \text{real_part}(\text{cos_integral}(bx - dx - c + bc/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(bc + cd)/d)^2 * \tan(1/2*(bc - cd)/d)^2 + \text{real_part}(\text{cos_integral}(-bx + dx + c - bc/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(bc + cd)/d)^2 * \tan(1/2*(bc - cd)/d)^2 + \text{real_part}(\text{cos_integral}(-bx - dx - c - bc/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(bc + cd)/d)^2 * \tan(1/2*(bc - cd)/d)^2 - 2 * \text{imag_part}(\text{cos_integral}(bx - dx - c + bc/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(bc + cd)/d)^2 * \tan(1/2*(bc - cd)/d) + 2 * \text{imag_part}(\text{cos_integral}(-bx + dx + c - bc/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(bc + cd)/d)^2 * \tan(1/2*(bc - cd)/d) - 4 * \text{sin_integral}((b*dx - d^2*x + bc - cd)/d) *$

$$\begin{aligned}
& c*d/d)*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2 + \\
& 2*\text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/ \\
& 2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 - 2*\text{imag_part}(\cos_integral(-b*x - d \\
& *x - c - b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d \\
&)/d)^2 + 4*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*a + 1/2*c)*\tan \\
& (1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 - 2*\text{imag_part}(\cos_integral(b*x \\
& - d*x - c + b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c \\
& - c*d)/d) + 2*\text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a + \\
& 1/2*c)^2*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d) - 4*\sin_integral((b*d*x \\
& x - d^2*x + b*c - c*d)/d)*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2*\tan(1/2 \\
& *(b*c - c*d)/d) + 2*\text{imag_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*a \\
& + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) - 2*\text{imag_part}(\cos_integral \\
& (-b*x + d*x + c - b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c + c \\
& *d)/d)^2*\tan(1/2*(b*c - c*d)/d) + 4*\sin_integral((b*d*x - d^2*x + b*c - c*d \\
&)/d)*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) - \\
& 2*\text{imag_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(\\
& 1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) + 2*\text{imag_part}(\cos_integral(-b*x \\
& + d*x + c - b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2* \\
& (b*c - c*d)/d) - 4*\sin_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a - \\
& 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) + 2*\text{imag_part}(\cos_ \\
& integral(b*x - d*x - c + b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)*\tan \\
& (1/2*(b*c - c*d)/d)^2 - 2*\text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d))*\tan \\
& (1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c - c*d)/d)^2 + 4*\sin_in \\
& tegral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2* \\
& c)*\tan(1/2*(b*c - c*d)/d)^2 - 2*\text{imag_part}(\cos_integral(b*x + d*x + c + b*c/ \\
& d))*\tan(1/2*a + 1/2*c)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 + 2*\text{im} \\
& ag_part(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*a \\
& - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 - 4*\sin_integral((b*d*x + d^2*x + b*c + \\
& c*d)/d)*\tan(1/2*a + 1/2*c)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 - \\
& 2*\text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(\\
& 1/2*(b*c + c*d)/d)*\tan(1/2*(b*c - c*d)/d)^2 + 2*\text{imag_part}(\cos_integral(-b*x \\
& - d*x - c - b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)*\tan(1/2*(b \\
& *c - c*d)/d)^2 - 4*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*a + \\
& 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)*\tan(1/2*(b*c - c*d)/d)^2 + 2*\text{imag_part}(\cos_ \\
& integral(b*x + d*x + c + b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d \\
&)*\tan(1/2*(b*c - c*d)/d)^2 - 2*\text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/ \\
& d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)*\tan(1/2*(b*c - c*d)/d)^2 + \\
& 4*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*a - 1/2*c)^2*\tan(1/2* \\
& (b*c + c*d)/d)*\tan(1/2*(b*c - c*d)/d)^2 + 2*\text{imag_part}(\cos_integral(b*x + d* \\
& x + c + b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - \\
& c*d)/d)^2 - 2*\text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1 \\
& /2*c)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 + 4*\sin_integral((b \\
& *d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*a + 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2*\tan \\
& (1/2*(b*c - c*d)/d)^2 + 2*\text{imag_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan \\
& (1/2*a - 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 - 2*\text{ima} \\
& g_part(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a - 1/2*c)*\tan(1/2*(b* \\
& c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 + 4*\sin_integral((b*d*x - d^2*x + b* \\
& c - c*d)/d)*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d) \\
& /d)^2 - \text{real_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)^2 \\
& *\tan(1/2*a - 1/2*c)^2 - \text{real_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(\\
& 1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2 - \text{real_part}(\cos_integral(-b*x + d*x + \\
& c - b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2 - \text{real_part}(\cos_inte \\
& gral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2 + 4 \\
& *real_part(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2* \\
& a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d) + 4*real_part(\cos_integral(-b*x - d*x - \\
& c - b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d) \\
& + \text{real_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(\\
& 1/2*(b*c + c*d)/d)^2 + \text{real_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1 \\
& /2*a + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 + \text{real_part}(\cos_integral(-b*x + d
\end{aligned}$$

$$\begin{aligned}
& 1/2*c)^2*\tan(1/2*(b*c - c*d)/d) + 2*imag_part(\cos_integral(-b*x + d*x + c - \\
& b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d) - 4*\sin_integral((b*d*x \\
& x - d^2*x + b*c - c*d)/d)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d) + 2*i \\
& mag_part(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*(b*c + c*d)/d)^2*\tan(\\
& 1/2*(b*c - c*d)/d) - 2*imag_part(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(\\
& 1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) + 4*\sin_integral((b*d*x - d^2*x \\
& + b*c - c*d)/d)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) - 2*imag_p \\
& art(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*(b*c - \\
& c*d)/d)^2 + 2*imag_part(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1 \\
& /2*c)*\tan(1/2*(b*c - c*d)/d)^2 - 4*\sin_integral((b*d*x + d^2*x + b*c + c*d) \\
& /d)*\tan(1/2*a + 1/2*c)*\tan(1/2*(b*c - c*d)/d)^2 + 2*imag_part(\cos_integral(\\
& b*x - d*x - c + b*c/d))*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c - c*d)/d)^2 - 2*ima \\
& g_part(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a - 1/2*c)*\tan(1/2*(b* \\
& c - c*d)/d)^2 + 4*\sin_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a - 1 \\
& /2*c)*\tan(1/2*(b*c - c*d)/d)^2 + 2*imag_part(\cos_integral(b*x + d*x + c + b \\
& *c/d))*\tan(1/2*(b*c + c*d)/d)*\tan(1/2*(b*c - c*d)/d)^2 - 2*imag_part(\cos_in \\
& tegral(-b*x - d*x - c - b*c/d))*\tan(1/2*(b*c + c*d)/d)*\tan(1/2*(b*c - c*d)/ \\
& d)^2 + 4*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*(b*c + c*d)/d) \\
& *\tan(1/2*(b*c - c*d)/d)^2 - \text{real_part}(\cos_integral(b*x + d*x + c + b*c/d))* \\
& \tan(1/2*a + 1/2*c)^2 + \text{real_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1 \\
& /2*a + 1/2*c)^2 + \text{real_part}(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a \\
& + 1/2*c)^2 - \text{real_part}(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1 \\
& /2*c)^2 + \text{real_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a - 1/2*c) \\
& ^2 - \text{real_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*a - 1/2*c)^2 - \\
& \text{real_part}(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a - 1/2*c)^2 + \text{real} \\
& _part(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a - 1/2*c)^2 + 4*\text{real_p} \\
& art(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*(b*c + \\
& c*d)/d) + 4*\text{real_part}(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1/2 \\
& *c)*\tan(1/2*(b*c + c*d)/d) - \text{real_part}(\cos_integral(b*x + d*x + c + b*c/d)) \\
& *\tan(1/2*(b*c + c*d)/d)^2 + \text{real_part}(\cos_integral(b*x - d*x - c + b*c/d))* \\
& \tan(1/2*(b*c + c*d)/d)^2 + \text{real_part}(\cos_integral(-b*x + d*x + c - b*c/d))* \\
& \tan(1/2*(b*c + c*d)/d)^2 - \text{real_part}(\cos_integral(-b*x - d*x - c - b*c/d))* \\
& \tan(1/2*(b*c + c*d)/d)^2 + 4*\text{real_part}(\cos_integral(b*x - d*x - c + b*c/d)) \\
& *\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c - c*d)/d) + 4*\text{real_part}(\cos_integral(-b*x \\
& + d*x + c - b*c/d))*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c - c*d)/d) + \text{real_part}(c \\
& os_integral(b*x + d*x + c + b*c/d))*\tan(1/2*(b*c - c*d)/d)^2 - \text{real_part}(co \\
& s_integral(b*x - d*x - c + b*c/d))*\tan(1/2*(b*c - c*d)/d)^2 - \text{real_part}(\cos \\
& _integral(-b*x + d*x + c - b*c/d))*\tan(1/2*(b*c - c*d)/d)^2 + \text{real_part}(\cos \\
& _integral(-b*x - d*x - c - b*c/d))*\tan(1/2*(b*c - c*d)/d)^2 - 2*imag_part(c \\
& os_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c) + 2*imag_part(\cos_in \\
& tegral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1/2*c) - 4*\sin_integral((b*d*x \\
& + d^2*x + b*c + c*d)/d)*\tan(1/2*a + 1/2*c) - 2*imag_part(\cos_integral(b*x - \\
& d*x - c + b*c/d))*\tan(1/2*a - 1/2*c) + 2*imag_part(\cos_integral(-b*x + d*x \\
& + c - b*c/d))*\tan(1/2*a - 1/2*c) - 4*\sin_integral((b*d*x - d^2*x + b*c - c \\
& *d)/d)*\tan(1/2*a - 1/2*c) + 2*imag_part(\cos_integral(b*x + d*x + c + b*c/d) \\
&)*\tan(1/2*(b*c + c*d)/d) - 2*imag_part(\cos_integral(-b*x - d*x - c - b*c/d) \\
&)*\tan(1/2*(b*c + c*d)/d) + 4*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)*ta \\
& n(1/2*(b*c + c*d)/d) + 2*imag_part(\cos_integral(b*x - d*x - c + b*c/d))*\tan \\
& (1/2*(b*c - c*d)/d) - 2*imag_part(\cos_integral(-b*x + d*x + c - b*c/d))*\tan \\
& (1/2*(b*c - c*d)/d) + 4*\sin_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2 \\
& *(b*c - c*d)/d) + \text{real_part}(\cos_integral(b*x + d*x + c + b*c/d)) + \text{real_par} \\
& t(\cos_integral(b*x - d*x - c + b*c/d)) + \text{real_part}(\cos_integral(-b*x + d*x \\
& + c - b*c/d)) + \text{real_part}(\cos_integral(-b*x - d*x - c - b*c/d)))*d/(b*d*\tan \\
& (1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b* \\
& c - c*d)/d)^2 + b*d*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c \\
& + c*d)/d)^2 + b*d*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - \\
& c*d)/d)^2 + b*d*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c \\
& - c*d)/d)^2 + b*d*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b* \\
& c - c*d)/d)^2 + b*d*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2 + b*d*\tan(1/2
\end{aligned}$$

```

*a + 1/2*c)^2*tan(1/2*(b*c + c*d)/d)^2 + b*d*tan(1/2*a - 1/2*c)^2*tan(1/2*(
b*c + c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2*tan(1/2*(b*c - c*d)/d)^2 + b*d*t
an(1/2*a - 1/2*c)^2*tan(1/2*(b*c - c*d)/d)^2 + b*d*tan(1/2*(b*c + c*d)/d)^2
*tan(1/2*(b*c - c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2 + b*d*tan(1/2*a - 1/2*
c)^2 + b*d*tan(1/2*(b*c + c*d)/d)^2 + b*d*tan(1/2*(b*c - c*d)/d)^2 + b*d) -
cos(b*x + a)*cos_integral(d*x + c)/b

```

$$3.133 \quad \int \frac{\text{CosIntegral}(c+dx) \sin(a+bx)}{x} dx$$

Optimal. Leaf size=18

$$\text{CannotIntegrate}\left(\frac{\sin(a+bx)\text{CosIntegral}(c+dx)}{x}, x\right)$$

[Out] CannotIntegrate[(CosIntegral[c + d*x]*Sin[a + b*x])/x, x]

Rubi [A] time = 0.137741, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\text{CosIntegral}(c+dx) \sin(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Int[(CosIntegral[c + d*x]*Sin[a + b*x])/x,x]

[Out] Defer[Int] [(CosIntegral[c + d*x]*Sin[a + b*x])/x, x]

Rubi steps

$$\int \frac{\text{Ci}(c+dx) \sin(a+bx)}{x} dx = \int \frac{\text{Ci}(c+dx) \sin(a+bx)}{x} dx$$

Mathematica [A] time = 31.0695, size = 0, normalized size = 0.

$$\int \frac{\text{CosIntegral}(c+dx) \sin(a+bx)}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[(CosIntegral[c + d*x]*Sin[a + b*x])/x,x]

[Out] Integrate[(CosIntegral[c + d*x]*Sin[a + b*x])/x, x]

Maple [A] time = 0.088, size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(dx+c) \sin(bx+a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(d*x+c)*sin(b*x+a)/x,x)

[Out] int(Ci(d*x+c)*sin(b*x+a)/x,x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(dx + c) \sin(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*sin(b*x+a)/x,x, algorithm="maxima")

[Out] integrate(Ci(d*x + c)*sin(b*x + a)/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\text{Ci}(dx + c) \sin(bx + a)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*sin(b*x+a)/x,x, algorithm="fricas")

[Out] integral(cos_integral(d*x + c)*sin(b*x + a)/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\sin(a + bx) \text{Ci}(c + dx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*sin(b*x+a)/x,x)

[Out] Integral(sin(a + b*x)*Ci(c + d*x)/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(dx + c) \sin(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*sin(b*x+a)/x,x, algorithm="giac")

[Out] integrate(Ci(d*x + c)*sin(b*x + a)/x, x)

3.134 $\int x \cos(a + bx) \text{CosIntegral}(c + dx) dx$

Optimal. Leaf size=370

$$\frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b^2} + \frac{\cos(a + bx) \text{CosIntegral}(c + dx)}{b^2} - \frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b+d)}{d}\right)}{2b^2}$$

```
[Out] Cos[a - c + (b - d)*x]/(2*b*(b - d)) + Cos[a + c + (b + d)*x]/(2*b*(b + d))
- (Cos[a - (b*c)/d]*CosIntegral[(c*(b - d))/d + (b - d)*x])/(2*b^2) + (Cos
[a + b*x]*CosIntegral[c + d*x])/b^2 - (Cos[a - (b*c)/d]*CosIntegral[(c*(b +
d))/d + (b + d)*x])/(2*b^2) + (c*CosIntegral[(c*(b - d))/d + (b - d)*x]*Si
n[a - (b*c)/d])/(2*b*d) + (c*CosIntegral[(c*(b + d))/d + (b + d)*x]*Sin[a -
(b*c)/d])/(2*b*d) + (x*CosIntegral[c + d*x]*Sin[a + b*x])/b + (c*Cos[a - (
b*c)/d]*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b*d) + (Sin[a - (b*c)/d]
*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b^2) + (c*Cos[a - (b*c)/d]*SinI
ntegral[(c*(b + d))/d + (b + d)*x])/(2*b*d) + (Sin[a - (b*c)/d]*SinIntegral
[(c*(b + d))/d + (b + d)*x])/(2*b^2)
```

Rubi [A] time = 0.801469, antiderivative size = 370, normalized size of antiderivative = 1., number of steps used = 24, number of rules used = 10, integrand size = 14, $\frac{\text{number of rules}}{\text{integrand size}} = 0.714$, Rules used = {6514, 6742, 4574, 2638, 4430, 3303, 3299, 3302, 6518, 4429}

$$\frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b^2} + \frac{\cos(a + bx) \text{CosIntegral}(c + dx)}{b^2} - \frac{\cos\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b+d)}{d}\right)}{2b^2}$$

Antiderivative was successfully verified.

```
[In] Int[x*Cos[a + b*x]*CosIntegral[c + d*x],x]
```

```
[Out] Cos[a - c + (b - d)*x]/(2*b*(b - d)) + Cos[a + c + (b + d)*x]/(2*b*(b + d))
- (Cos[a - (b*c)/d]*CosIntegral[(c*(b - d))/d + (b - d)*x])/(2*b^2) + (Cos
[a + b*x]*CosIntegral[c + d*x])/b^2 - (Cos[a - (b*c)/d]*CosIntegral[(c*(b +
d))/d + (b + d)*x])/(2*b^2) + (c*CosIntegral[(c*(b - d))/d + (b - d)*x]*Si
n[a - (b*c)/d])/(2*b*d) + (c*CosIntegral[(c*(b + d))/d + (b + d)*x]*Sin[a -
(b*c)/d])/(2*b*d) + (x*CosIntegral[c + d*x]*Sin[a + b*x])/b + (c*Cos[a - (
b*c)/d]*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b*d) + (Sin[a - (b*c)/d]
*SinIntegral[(c*(b - d))/d + (b - d)*x])/(2*b^2) + (c*Cos[a - (b*c)/d]*SinI
ntegral[(c*(b + d))/d + (b + d)*x])/(2*b*d) + (Sin[a - (b*c)/d]*SinIntegral
[(c*(b + d))/d + (b + d)*x])/(2*b^2)
```

Rule 6514

```
Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)]*((e_.) + (f_.)*
(x_)^(m_.), x_Symbol] := Simp[((e + f*x)^m*Sin[a + b*x]*CosIntegral[c + d*
x])/b, x] + (-Dist[d/b, Int[((e + f*x)^m*Sin[a + b*x]*Cos[c + d*x])/(c + d*
x), x], x] - Dist[(f*m)/b, Int[(e + f*x)^(m - 1)*Sin[a + b*x]*CosIntegral[c
+ d*x], x], x]) /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[m, 0]
```

Rule 6742

```
Int[u_, x_Symbol] := With[{v = ExpandIntegrand[u, x]}, Int[v, x] /; SumQ[v]
]
```

Rule 4574

```
Int[Cos[w_]^(q_)*Sin[v_]^(p_), x_Symbol] := Int[ExpandTrigReduce[Sin[v]^p
*Cos[w]^q, x], x] /; IGtQ[p, 0] && IGtQ[q, 0] && ((PolynomialQ[v, x] && Pol
ynomialQ[w, x]) || (BinomialQ[{v, w}, x] && IndependentQ[Cancel[v/w], x]))
```

Rule 2638

```
Int[sin[(c_) + (d_)*(x_)], x_Symbol] := -Simp[Cos[c + d*x]/d, x] /; FreeQ
[{c, d}, x]
```

Rule 4430

```
Int[Cos[(c_) + (d_)*(x_)]^(q_)*((e_) + (f_)*(x_))^(m_)*Sin[(a_) + (b
_)*(x_)]^(p_), x_Symbol] := Int[ExpandTrigReduce[(e + f*x)^m, Sin[a + b*x
]^p*Cos[c + d*x]^q, x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[p, 0]
&& IGtQ[q, 0]
```

Rule 3303

```
Int[sin[(e_) + (f_)*(x_)]/((c_) + (d_)*(x_)), x_Symbol] := Dist[Cos[(d*
e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f
)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] &&
NeQ[d*e - c*f, 0]
```

Rule 3299

```
Int[sin[(e_) + (f_)*(x_)]/((c_) + (d_)*(x_)), x_Symbol] := Simp[SinInte
gral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]
```

Rule 3302

```
Int[sin[(e_) + (f_)*(x_)]/((c_) + (d_)*(x_)), x_Symbol] := Simp[CosInte
gral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) -
c*f, 0]
```

Rule 6518

```
Int[CosIntegral[(c_) + (d_)*(x_)]*Sin[(a_) + (b_)*(x_)], x_Symbol] := -
Simp[(Cos[a + b*x]*CosIntegral[c + d*x])/b, x] + Dist[d/b, Int[(Cos[a + b*x
]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]
```

Rule 4429

```
Int[Cos[(a_) + (b_)*(x_)]^(p_)*Cos[(c_) + (d_)*(x_)]^(q_)*((e_) + (f
_)*(x_))^(m_), x_Symbol] := Int[ExpandTrigReduce[(e + f*x)^m, Cos[a + b*x
]^p*Cos[c + d*x]^q, x], x] /; FreeQ[{a, b, c, d, e, f}, x] && IGtQ[p, 0] &&
IGtQ[q, 0] && IntegerQ[m]
```

Rubi steps

$$\begin{aligned}
\int x \cos(a + bx) \text{Ci}(c + dx) dx &= \frac{x \text{Ci}(c + dx) \sin(a + bx)}{b} - \frac{\int \text{Ci}(c + dx) \sin(a + bx) dx}{b} - \frac{d \int \frac{x \cos(c+dx) \sin(a+bx)}{c+dx} dx}{b} \\
&= \frac{\cos(a + bx) \text{Ci}(c + dx)}{b^2} + \frac{x \text{Ci}(c + dx) \sin(a + bx)}{b} - \frac{d \int \frac{\cos(a+bx) \cos(c+dx)}{c+dx} dx}{b^2} - \frac{d \int \left(\frac{\cos(a+bx) \sin(c+dx)}{c+dx} \right) dx}{b^2} \\
&= \frac{\cos(a + bx) \text{Ci}(c + dx)}{b^2} + \frac{x \text{Ci}(c + dx) \sin(a + bx)}{b} - \frac{\int \cos(c + dx) \sin(a + bx) dx}{b} + \frac{\int \cos(a + bx) \sin(c + dx) dx}{b} \\
&= \frac{\cos(a + bx) \text{Ci}(c + dx)}{b^2} + \frac{x \text{Ci}(c + dx) \sin(a + bx)}{b} - \frac{\int \left(\frac{1}{2} \sin(a - c + (b - d)x) + \frac{1}{2} \sin(a + c + (b + d)x) \right) dx}{b} \\
&= \frac{\cos(a + bx) \text{Ci}(c + dx)}{b^2} + \frac{x \text{Ci}(c + dx) \sin(a + bx)}{b} - \frac{\int \sin(a - c + (b - d)x) dx}{2b} - \frac{\int \sin(a + c + (b + d)x) dx}{2b} \\
&= \frac{\cos(a - c + (b - d)x)}{2b(b - d)} + \frac{\cos(a + c + (b + d)x)}{2b(b + d)} - \frac{\cos\left(a - \frac{bc}{d}\right) \text{Ci}\left(\frac{c(b-d)}{d} + (b-d)x\right)}{2b^2} + \frac{\cos\left(a + \frac{bc}{d}\right) \text{Ci}\left(\frac{c(b+d)}{d} + (b+d)x\right)}{2b^2} \\
&= \frac{\cos(a - c + (b - d)x)}{2b(b - d)} + \frac{\cos(a + c + (b + d)x)}{2b(b + d)} - \frac{\cos\left(a - \frac{bc}{d}\right) \text{Ci}\left(\frac{c(b-d)}{d} + (b-d)x\right)}{2b^2} + \frac{\cos\left(a + \frac{bc}{d}\right) \text{Ci}\left(\frac{c(b+d)}{d} + (b+d)x\right)}{2b^2}
\end{aligned}$$

Mathematica [C] time = 4.40565, size = 433, normalized size = 1.17

$$-i \exp\left(-\frac{i(d(a+c+dx)+b(c+dx))}{d}\right) \left((b^2 - d^2)(bc - id)e^{i(2a+x(b+d)+c)} \text{ExpIntegralEi}\left(\frac{i(b-d)(c+dx)}{d}\right) + e^{\frac{ibc}{d}} \left(ibd(d(-1 + e^{2i(a+bx)}) \right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[x*Cos[a + b*x]*CosIntegral[c + d*x],x]

[Out] (((-I)*((b*c - I*d)*(b^2 - d^2)*E^(I*(2*a + c + (b + d)*x))*ExpIntegralEi[(I*(b - d)*(c + d*x))/d] + E^((I*b*c)/d)*(I*b*d*(d*(-1 + E^((2*I)*(a + b*x))) + b*(1 + E^((2*I)*(a + b*x)))) - (b*c + I*d)*(b^2 - d^2)*E^((I*(b + d)*(c + d*x))/d)*ExpIntegralEi[(-I)*(b + d)*(c + d*x)/d]))/E^((I*(b*(c + d*x) + d*(a + c + d*x))/d) - (I*(I*b*d*E^((I*c*(b + d))/d)*(b + d + b*E^((2*I)*(a + b*x)) - d*E^((2*I)*(a + b*x))) - (b*c + I*d)*(b^2 - d^2)*E^((-I)*d*x + I*b*((2*c)/d + x))*ExpIntegralEi[(-I)*(b - d)*(c + d*x)/d] + (b*c - I*d)*(b^2 - d^2)*E^(I*(2*a + (b - d)*x))*ExpIntegralEi[(I*(b + d)*(c + d*x))/d]))/E^((I*(d*(a - d*x) + b*(c + d*x))/d) + 4*(b - d)*d*(b + d)*CosIntegral[c + d*x]*(Cos[a + b*x] + b*x*Sin[a + b*x]))/(4*b^2*(b - d)*d*(b + d))

Maple [B] time = 0.105, size = 1212, normalized size = 3.3

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] int(x*Ci(d*x+c)*cos(b*x+a),x)

[Out] (Ci(d*x+c)/b*(1/b*d*(sin(b/d*(d*x+c)+(a*d-b*c)/d)*(b/d*(d*x+c)+(a*d-b*c)/d) + cos(b/d*(d*x+c)+(a*d-b*c)/d) - a*d/b*sin(b/d*(d*x+c)+(a*d-b*c)/d) - 1/b*(-1/2/(b-d)*d*cos((b-d)/d*(d*x+c)+(a*d-b*c)/d) + 1/2*(a*d-b*c)*d/(b-d)*(Si((b-d)/

$$d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d*\cos((-a*d+b*c)/d)/d-Ci((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d-1/2/(b-d)*d^2*a*(Si((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d-Ci((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d)+1/2/(b-d)*c*d^2*(Si((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d-Ci((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d)-1/2/(b+d)*d*\cos((b+d)/d*(d*x+c)+(a*d-b*c)/d)+1/2*(a*d-b*c)*d/(b+d)*(Si((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d-Ci((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d)-1/2/(b+d)*d^2*a*(Si((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d-Ci((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d)-1/2/(b+d)*c*d^2*(Si((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d-Ci((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d)+1/2/b*d^2*(Si((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d+Ci((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d)+1/2/b*d^2*(Si((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\sin((-a*d+b*c)/d)/d+Ci((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*\cos((-a*d+b*c)/d)/d))/d$$

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int x \operatorname{Ci}(dx + c) \cos(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(d*x+c)*cos(b*x+a),x, algorithm="maxima")

[Out] integrate(x*Ci(d*x + c)*cos(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}(x \cos(bx + a) \operatorname{Ci}(dx + c), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(d*x+c)*cos(b*x+a),x, algorithm="fricas")

[Out] integral(x*cos(b*x + a)*cos_integral(d*x + c), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int x \cos(a + bx) \operatorname{Ci}(c + dx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(x*Ci(d*x+c)*cos(b*x+a),x)

[Out] Integral(x*cos(a + b*x)*Ci(c + d*x), x)

Giac [F(-1)] time = 0., size = 0, normalized size = 0.

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate(x*Ci(d*x+c)*cos(b*x+a),x, algorithm="giac")
```

```
[Out] Timed out
```

3.135 $\int \cos(a + bx) \text{CosIntegral}(c + dx) dx$

Optimal. Leaf size=153

$$-\frac{\sin\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b} - \frac{\sin\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b+d)}{d} + x(b+d)\right)}{2b} + \frac{\sin(a + bx) \text{CosIntegral}(c + dx)}{b}$$

[Out] $-(\text{CosIntegral}[(c*(b - d))/d + (b - d)*x]*\text{Sin}[a - (b*c)/d])/(2*b) - (\text{CosIntegral}[(c*(b + d))/d + (b + d)*x]*\text{Sin}[a - (b*c)/d])/(2*b) + (\text{CosIntegral}[c + d*x]*\text{Sin}[a + b*x])/b - (\text{Cos}[a - (b*c)/d]*\text{SinIntegral}[(c*(b - d))/d + (b - d)*x])/(2*b) - (\text{Cos}[a - (b*c)/d]*\text{SinIntegral}[(c*(b + d))/d + (b + d)*x])/(2*b)$

Rubi [A] time = 0.216809, antiderivative size = 153, normalized size of antiderivative = 1., number of steps used = 9, number of rules used = 5, integrand size = 13, $\frac{\text{number of rules}}{\text{integrand size}} = 0.385$, Rules used = {6512, 4430, 3303, 3299, 3302}

$$-\frac{\sin\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b-d)}{d} + x(b-d)\right)}{2b} - \frac{\sin\left(a - \frac{bc}{d}\right) \text{CosIntegral}\left(\frac{c(b+d)}{d} + x(b+d)\right)}{2b} + \frac{\sin(a + bx) \text{CosIntegral}(c + dx)}{b}$$

Antiderivative was successfully verified.

[In] Int[Cos[a + b*x]*CosIntegral[c + d*x], x]

[Out] $-(\text{CosIntegral}[(c*(b - d))/d + (b - d)*x]*\text{Sin}[a - (b*c)/d])/(2*b) - (\text{CosIntegral}[(c*(b + d))/d + (b + d)*x]*\text{Sin}[a - (b*c)/d])/(2*b) + (\text{CosIntegral}[c + d*x]*\text{Sin}[a + b*x])/b - (\text{Cos}[a - (b*c)/d]*\text{SinIntegral}[(c*(b - d))/d + (b - d)*x])/(2*b) - (\text{Cos}[a - (b*c)/d]*\text{SinIntegral}[(c*(b + d))/d + (b + d)*x])/(2*b)$

Rule 6512

Int[Cos[(a_.) + (b_.)*(x_)]*CosIntegral[(c_.) + (d_.)*(x_)], x_Symbol] :> Simp[(Sin[a + b*x]*CosIntegral[c + d*x])/b, x] - Dist[d/b, Int[(Sin[a + b*x]*Cos[c + d*x])/(c + d*x), x], x] /; FreeQ[{a, b, c, d}, x]

Rule 4430

Int[Cos[(c_.) + (d_.)*(x_)]^(q_.)*((e_.) + (f_.)*(x_))^(m_.)*Sin[(a_.) + (b_.)*(x_)]^(p_.), x_Symbol] :> Int[ExpandTrigReduce[(e + f*x)^m, Sin[a + b*x]^(p)*Cos[c + d*x]^q, x], x] /; FreeQ[{a, b, c, d, e, f, m}, x] && IGtQ[p, 0] && IGtQ[q, 0]

Rule 3303

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Dist[Cos[(d*e - c*f)/d], Int[Sin[(c*f)/d + f*x]/(c + d*x), x], x] + Dist[Sin[(d*e - c*f)/d], Int[Cos[(c*f)/d + f*x]/(c + d*x), x], x] /; FreeQ[{c, d, e, f}, x] && NeQ[d*e - c*f, 0]

Rule 3299

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] :> Simp[SinIntegral[e + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*e - c*f, 0]

Rule 3302

Int[sin[(e_.) + (f_.)*(x_)]/((c_.) + (d_.)*(x_)), x_Symbol] := Simp[CosIntegral[e - Pi/2 + f*x]/d, x] /; FreeQ[{c, d, e, f}, x] && EqQ[d*(e - Pi/2) - c*f, 0]

Rubi steps

$$\begin{aligned}
 \int \cos(a + bx) \operatorname{Ci}(c + dx) dx &= \frac{\operatorname{Ci}(c + dx) \sin(a + bx)}{b} - \frac{d \int \frac{\cos(c+dx) \sin(a+bx)}{c+dx} dx}{b} \\
 &= \frac{\operatorname{Ci}(c + dx) \sin(a + bx)}{b} - \frac{d \int \left(\frac{\sin(a-c+(b-d)x)}{2(c+dx)} + \frac{\sin(a+c+(b+d)x)}{2(c+dx)} \right) dx}{b} \\
 &= \frac{\operatorname{Ci}(c + dx) \sin(a + bx)}{b} - \frac{d \int \frac{\sin(a-c+(b-d)x)}{c+dx} dx}{2b} - \frac{d \int \frac{\sin(a+c+(b+d)x)}{c+dx} dx}{2b} \\
 &= \frac{\operatorname{Ci}(c + dx) \sin(a + bx)}{b} - \frac{\left(d \cos\left(a - \frac{bc}{d}\right) \right) \int \frac{\sin\left(\frac{c(b-d)}{d} + (b-d)x\right)}{c+dx} dx}{2b} - \frac{\left(d \cos\left(a - \frac{bc}{d}\right) \right) \int \frac{\sin\left(\frac{c(b+d)}{d} + (b+d)x\right)}{c+dx} dx}{2b} \\
 &= -\frac{\operatorname{Ci}\left(\frac{c(b-d)}{d} + (b-d)x\right) \sin\left(a - \frac{bc}{d}\right)}{2b} - \frac{\operatorname{Ci}\left(\frac{c(b+d)}{d} + (b+d)x\right) \sin\left(a - \frac{bc}{d}\right)}{2b} + \frac{\operatorname{Ci}(c + dx) \sin(a + bx)}{b}
 \end{aligned}$$

Mathematica [C] time = 1.57664, size = 153, normalized size = 1.

$$\frac{4 \sin(a + bx) \operatorname{CosIntegral}(c + dx) + ie^{-\frac{i(ad+bc)}{d}} \left(e^{2ia} \operatorname{ExpIntegralEi}\left(\frac{i(b-d)(c+dx)}{d}\right) + e^{2ia} \operatorname{ExpIntegralEi}\left(\frac{i(b+d)(c+dx)}{d}\right) - e^{2ia} \right)}{4b}$$

Antiderivative was successfully verified.

[In] Integrate[Cos[a + b*x]*CosIntegral[c + d*x], x]

[Out] ((I*(-(E^(((2*I)*b*c)/d)*ExpIntegralEi[((-I)*(b-d)*(c+d*x))/d])) + E^(((2*I)*a)*ExpIntegralEi[(I*(b-d)*(c+d*x))/d] - E^(((2*I)*b*c)/d)*ExpIntegralEi[((-I)*(b+d)*(c+d*x))/d] + E^(((2*I)*a)*ExpIntegralEi[(I*(b+d)*(c+d*x))/d])))/E^((I*(b*c+a*d))/d) + 4*CosIntegral[c + d*x]*Sin[a + b*x])/(4*b)

Maple [A] time = 0.074, size = 282, normalized size = 1.8

$$\frac{1}{d} \left(\frac{\operatorname{Ci}(dx + c)d}{b} \sin\left(\frac{b(dx + c)}{d} + \frac{ad - bc}{d}\right) - \frac{d}{b} \left(\frac{d}{2} \left(\frac{1}{d} \operatorname{Si}\left(\frac{(b-d)(dx + c)}{d} + \frac{ad - bc}{d} + \frac{-ad + bc}{d}\right) \cos\left(\frac{-ad + bc}{d}\right) - \frac{1}{d} \right) \right) \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(d*x+c)*cos(b*x+a), x)

[Out] (Ci(d*x+c)/b*d*sin(b/d*(d*x+c)+(a*d-b*c)/d)-1/b*d*(1/2*d*(Si((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*cos((-a*d+b*c)/d)/d-Ci((b-d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*sin((-a*d+b*c)/d)/d+1/2*d*(Si((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*cos((-a*d+b*c)/d)/d-Ci((b+d)/d*(d*x+c)+(a*d-b*c)/d+(-a*d+b*c)/d)*sin((-a*d+b*c)/d)/d)))/d

Maxima [F] time = 0., size = 0, normalized size = 0.

$$\int \operatorname{Ci}(dx + c) \cos(bx + a) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*cos(b*x+a),x, algorithm="maxima")

[Out] integrate(Ci(d*x + c)*cos(b*x + a), x)

Fricas [F] time = 0., size = 0, normalized size = 0.

$$\operatorname{integral}(\cos(bx + a) \operatorname{Ci}(dx + c), x)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*cos(b*x+a),x, algorithm="fricas")

[Out] integral(cos(b*x + a)*cos_integral(d*x + c), x)

Sympy [F] time = 0., size = 0, normalized size = 0.

$$\int \cos(a + bx) \operatorname{Ci}(c + dx) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*cos(b*x+a),x)

[Out] Integral(cos(a + b*x)*Ci(c + d*x), x)

Giac [C] time = 1.93965, size = 12879, normalized size = 84.18

result too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*cos(b*x+a),x, algorithm="giac")

[Out]
$$\begin{aligned} & -1/4*(\operatorname{imag_part}(\operatorname{cos_integral}(bx + dx + c + b*c/d))*\tan(1/2*a + 1/2*c)^2* \\ & \operatorname{an}(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 + \operatorname{ima} \\ & \operatorname{g_part}(\operatorname{cos_integral}(bx - dx - c + b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a \\ & - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 - \operatorname{imag_part}(\operatorname{co} \\ & \operatorname{s_integral}(-bx + dx + c - b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c) \\ & ^2*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 - \operatorname{imag_part}(\operatorname{cos_integr} \\ & \operatorname{al}(-bx - dx - c - b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2*\tan(1 \\ & /2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 + 2*\operatorname{sin_integral}((b*d*x + d^2* \\ & x + b*c + c*d)/d)*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + \\ & c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 + 2*\operatorname{sin_integral}((b*d*x - d^2*x + b*c - \\ & c*d)/d)*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2* \\ & \tan(1/2*(b*c - c*d)/d)^2 + 2*\operatorname{real_part}(\operatorname{cos_integral}(bx - dx - c + b*c/d)) \end{aligned}$$

$$\begin{aligned}
& /d)^2 + 2*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*a + 1/2*c)^2* \\
& \tan(1/2*(b*c + c*d)/d)^2 + 2*\sin_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan \\
& (1/2*a + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 - \text{imag_part}(\cos_integral(b*x + \\
& d*x + c + b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 - \text{imag_part} \\
& (\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c \\
& *d)/d)^2 + \text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a - 1/2* \\
& c)^2*\tan(1/2*(b*c + c*d)/d)^2 + \text{imag_part}(\cos_integral(-b*x - d*x - c - b*c \\
& /d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 - 2*\sin_integral((b*d*x \\
& + d^2*x + b*c + c*d)/d)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d)^2 - 2*s \\
& in_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b* \\
& c + c*d)/d)^2 + 4*\text{imag_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2*a \\
& + 1/2*c)^2*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c - c*d)/d) - 4*\text{imag_part}(\cos_inte \\
& gral(-b*x + d*x + c - b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c)*\tan(1 \\
& /2*(b*c - c*d)/d) + 8*\sin_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a \\
& + 1/2*c)^2*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c - c*d)/d) + 4*\text{imag_part}(\cos_int \\
& egral(b*x - d*x - c + b*c/d))*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2*t \\
& an(1/2*(b*c - c*d)/d) - 4*\text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d))*t \\
& an(1/2*a - 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d) + 8*\sin_i \\
& ntegral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a - 1/2*c)*\tan(1/2*(b*c + c* \\
& d)/d)^2*\tan(1/2*(b*c - c*d)/d) - \text{imag_part}(\cos_integral(b*x + d*x + c + b*c \\
& /d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 - \text{imag_part}(\cos_integral \\
& (b*x - d*x - c + b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 + \text{im} \\
& ag_part(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2* \\
& (b*c - c*d)/d)^2 + \text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2* \\
& a + 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 - 2*\sin_integral((b*d*x + d^2*x + b*c \\
& + c*d)/d)*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 - 2*\sin_integral((\\
& b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 \\
& + \text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(\\
& 1/2*(b*c - c*d)/d)^2 + \text{imag_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1 \\
& /2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 - \text{imag_part}(\cos_integral(-b*x + d* \\
& x + c - b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 - \text{imag_part}(c \\
& os_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c* \\
& d)/d)^2 + 2*\sin_integral((b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*a - 1/2*c)^ \\
& 2*\tan(1/2*(b*c - c*d)/d)^2 + 2*\sin_integral((b*d*x - d^2*x + b*c - c*d)/d)* \\
& \tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c - c*d)/d)^2 + 4*\text{imag_part}(\cos_integral(b* \\
& x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*(b*c + c*d)/d)*\tan(1/2*(b* \\
& c - c*d)/d)^2 - 4*\text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a \\
& + 1/2*c)*\tan(1/2*(b*c + c*d)/d)*\tan(1/2*(b*c - c*d)/d)^2 + 8*\sin_integral(\\
& (b*d*x + d^2*x + b*c + c*d)/d)*\tan(1/2*a + 1/2*c)*\tan(1/2*(b*c + c*d)/d)*\tan \\
& (1/2*(b*c - c*d)/d)^2 - \text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan \\
& (1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 - \text{imag_part}(\cos_integral(b*x \\
& - d*x - c + b*c/d))*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 + \text{im} \\
& ag_part(\cos_integral(-b*x + d*x + c - b*c/d))*\tan(1/2*(b*c + c*d)/d)^2*\tan(\\
& 1/2*(b*c - c*d)/d)^2 + \text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(\\
& 1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 - 2*\sin_integral((b*d*x + d^2 \\
& *x + b*c + c*d)/d)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2*(b*c - c*d)/d)^2 - 2*s \\
& in_integral((b*d*x - d^2*x + b*c - c*d)/d)*\tan(1/2*(b*c + c*d)/d)^2*\tan(1/2* \\
& (b*c - c*d)/d)^2 + 2*\text{real_part}(\cos_integral(b*x - d*x - c + b*c/d))*\tan(1/2 \\
& *a + 1/2*c)^2*\tan(1/2*a - 1/2*c) + 2*\text{real_part}(\cos_integral(-b*x + d*x + c \\
& - b*c/d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*a - 1/2*c) + 2*\text{real_part}(\cos_integra \\
& l(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*a - 1/2*c)^2 + 2*\text{real_} \\
& part(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a + 1/2*c)*\tan(1/2*a - 1 \\
& /2*c)^2 + 2*\text{real_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a + 1/2* \\
& c)^2*\tan(1/2*(b*c + c*d)/d) + 2*\text{real_part}(\cos_integral(-b*x - d*x - c - b*c \\
& /d))*\tan(1/2*a + 1/2*c)^2*\tan(1/2*(b*c + c*d)/d) - 2*\text{real_part}(\cos_integral \\
& (b*x + d*x + c + b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2*(b*c + c*d)/d) - 2*\text{re} \\
& al_part(\cos_integral(-b*x - d*x - c - b*c/d))*\tan(1/2*a - 1/2*c)^2*\tan(1/2* \\
& (b*c + c*d)/d) - 2*\text{real_part}(\cos_integral(b*x + d*x + c + b*c/d))*\tan(1/2*a \\
& + 1/2*c)*\tan(1/2*(b*c + c*d)/d)^2 - 2*\text{real_part}(\cos_integral(-b*x - d*x -
\end{aligned}$$

$$\begin{aligned}
& c - b*c/d)) * \tan(1/2*a + 1/2*c) * \tan(1/2*(b*c + c*d)/d)^2 + 2*\text{real_part}(\cos_i \\
& \text{ntegral}(b*x - d*x - c + b*c/d)) * \tan(1/2*a - 1/2*c) * \tan(1/2*(b*c + c*d)/d)^2 \\
& + 2*\text{real_part}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2*a - 1/2*c) * \tan \\
& (1/2*(b*c + c*d)/d)^2 - 2*\text{real_part}(\cos_integral(b*x - d*x - c + b*c/d)) * \tan \\
& (1/2*a + 1/2*c)^2 * \tan(1/2*(b*c - c*d)/d) - 2*\text{real_part}(\cos_integral(-b*x + \\
& d*x + c - b*c/d)) * \tan(1/2*a + 1/2*c)^2 * \tan(1/2*(b*c - c*d)/d) + 2*\text{real_par} \\
& \text{t}(\cos_integral(b*x - d*x - c + b*c/d)) * \tan(1/2*a - 1/2*c)^2 * \tan(1/2*(b*c - \\
& c*d)/d) + 2*\text{real_part}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2*a - 1/2 \\
& *c)^2 * \tan(1/2*(b*c - c*d)/d) - 2*\text{real_part}(\cos_integral(b*x - d*x - c + b*c \\
& /d)) * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/d) - 2*\text{real_part}(\cos_inte \\
& \text{gral}(-b*x + d*x + c - b*c/d)) * \tan(1/2*(b*c + c*d)/d)^2 * \tan(1/2*(b*c - c*d)/ \\
& d) + 2*\text{real_part}(\cos_integral(b*x + d*x + c + b*c/d)) * \tan(1/2*a + 1/2*c) * \tan \\
& (1/2*(b*c - c*d)/d)^2 + 2*\text{real_part}(\cos_integral(-b*x - d*x - c - b*c/d)) * \\
& \tan(1/2*a + 1/2*c) * \tan(1/2*(b*c - c*d)/d)^2 - 2*\text{real_part}(\cos_integral(b*x \\
& - d*x - c + b*c/d)) * \tan(1/2*a - 1/2*c) * \tan(1/2*(b*c - c*d)/d)^2 - 2*\text{real_pa} \\
& \text{rt}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2*a - 1/2*c) * \tan(1/2*(b*c - \\
& c*d)/d)^2 - 2*\text{real_part}(\cos_integral(b*x + d*x + c + b*c/d)) * \tan(1/2*(b*c + \\
& c*d)/d) * \tan(1/2*(b*c - c*d)/d)^2 - 2*\text{real_part}(\cos_integral(-b*x - d*x - c \\
& - b*c/d)) * \tan(1/2*(b*c + c*d)/d) * \tan(1/2*(b*c - c*d)/d)^2 - \text{imag_part}(\cos_ \\
& \text{integral}(b*x + d*x + c + b*c/d)) * \tan(1/2*a + 1/2*c)^2 + \text{imag_part}(\cos_integ \\
& \text{ral}(b*x - d*x - c + b*c/d)) * \tan(1/2*a + 1/2*c)^2 - \text{imag_part}(\cos_integral(- \\
& b*x + d*x + c - b*c/d)) * \tan(1/2*a + 1/2*c)^2 + \text{imag_part}(\cos_integral(-b*x \\
& - d*x - c - b*c/d)) * \tan(1/2*a + 1/2*c)^2 - 2*\text{sin_integral}((b*d*x + d^2*x + \\
& b*c + c*d)/d) * \tan(1/2*a + 1/2*c)^2 + 2*\text{sin_integral}((b*d*x - d^2*x + b*c - \\
& c*d)/d) * \tan(1/2*a + 1/2*c)^2 + \text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d \\
&)) * \tan(1/2*a - 1/2*c)^2 - \text{imag_part}(\cos_integral(b*x - d*x - c + b*c/d)) * \tan \\
& (1/2*a - 1/2*c)^2 + \text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/ \\
& 2*a - 1/2*c)^2 - \text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d)) * \tan(1/2*a \\
& - 1/2*c)^2 + 2*\text{sin_integral}((b*d*x + d^2*x + b*c + c*d)/d) * \tan(1/2*a - 1/2* \\
& c)^2 - 2*\text{sin_integral}((b*d*x - d^2*x + b*c - c*d)/d) * \tan(1/2*a - 1/2*c)^2 + \\
& 4*\text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d)) * \tan(1/2*a + 1/2*c) * \tan(1/ \\
& 2*(b*c + c*d)/d) - 4*\text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d)) * \tan(1/ \\
& 2*a + 1/2*c) * \tan(1/2*(b*c + c*d)/d) + 8*\text{sin_integral}((b*d*x + d^2*x + b*c + \\
& c*d)/d) * \tan(1/2*a + 1/2*c) * \tan(1/2*(b*c + c*d)/d) - \text{imag_part}(\cos_integral \\
& (b*x + d*x + c + b*c/d)) * \tan(1/2*(b*c + c*d)/d)^2 + \text{imag_part}(\cos_integral(\\
& b*x - d*x - c + b*c/d)) * \tan(1/2*(b*c + c*d)/d)^2 - \text{imag_part}(\cos_integral(- \\
& b*x + d*x + c - b*c/d)) * \tan(1/2*(b*c + c*d)/d)^2 + \text{imag_part}(\cos_integral(- \\
& b*x - d*x - c - b*c/d)) * \tan(1/2*(b*c + c*d)/d)^2 - 2*\text{sin_integral}((b*d*x + \\
& d^2*x + b*c + c*d)/d) * \tan(1/2*(b*c + c*d)/d)^2 + 2*\text{sin_integral}((b*d*x - d^ \\
& 2*x + b*c - c*d)/d) * \tan(1/2*(b*c + c*d)/d)^2 + 4*\text{imag_part}(\cos_integral(b*x \\
& - d*x - c + b*c/d)) * \tan(1/2*a - 1/2*c) * \tan(1/2*(b*c - c*d)/d) - 4*\text{imag_par} \\
& \text{t}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2*a - 1/2*c) * \tan(1/2*(b*c - c \\
& *d)/d) + 8*\text{sin_integral}((b*d*x - d^2*x + b*c - c*d)/d) * \tan(1/2*a - 1/2*c) * \tan \\
& (1/2*(b*c - c*d)/d) + \text{imag_part}(\cos_integral(b*x + d*x + c + b*c/d)) * \tan(\\
& 1/2*(b*c - c*d)/d)^2 - \text{imag_part}(\cos_integral(b*x - d*x - c + b*c/d)) * \tan(1 \\
& /2*(b*c - c*d)/d)^2 + \text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1 \\
& /2*(b*c - c*d)/d)^2 - \text{imag_part}(\cos_integral(-b*x - d*x - c - b*c/d)) * \tan(1 \\
& /2*(b*c - c*d)/d)^2 + 2*\text{sin_integral}((b*d*x + d^2*x + b*c + c*d)/d) * \tan(1/2 \\
& *(b*c - c*d)/d)^2 - 2*\text{sin_integral}((b*d*x - d^2*x + b*c - c*d)/d) * \tan(1/2*(\\
& b*c - c*d)/d)^2 + 2*\text{real_part}(\cos_integral(b*x + d*x + c + b*c/d)) * \tan(1/2* \\
& a + 1/2*c) + 2*\text{real_part}(\cos_integral(-b*x - d*x - c - b*c/d)) * \tan(1/2*a + \\
& 1/2*c) + 2*\text{real_part}(\cos_integral(b*x - d*x - c + b*c/d)) * \tan(1/2*a - 1/2*c) \\
&) + 2*\text{real_part}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2*a - 1/2*c) - \\
& 2*\text{real_part}(\cos_integral(b*x + d*x + c + b*c/d)) * \tan(1/2*(b*c + c*d)/d) - 2 \\
& * \text{real_part}(\cos_integral(-b*x - d*x - c - b*c/d)) * \tan(1/2*(b*c + c*d)/d) - 2 \\
& * \text{real_part}(\cos_integral(b*x - d*x - c + b*c/d)) * \tan(1/2*(b*c - c*d)/d) - 2* \\
& \text{real_part}(\cos_integral(-b*x + d*x + c - b*c/d)) * \tan(1/2*(b*c - c*d)/d) + \text{im} \\
& \text{ag_part}(\cos_integral(b*x + d*x + c + b*c/d)) + \text{imag_part}(\cos_integral(b*x - \\
& d*x - c + b*c/d)) - \text{imag_part}(\cos_integral(-b*x + d*x + c - b*c/d)) - \text{imag}
\end{aligned}$$

```

_part(cos_integral(-b*x - d*x - c - b*c/d)) + 2*sin_integral((b*d*x + d^2*x
+ b*c + c*d)/d) + 2*sin_integral((b*d*x - d^2*x + b*c - c*d)/d))*d/(b*d*tan
(1/2*a + 1/2*c)^2*tan(1/2*a - 1/2*c)^2*tan(1/2*(b*c + c*d)/d)^2*tan(1/2*(b
*c - c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2*tan(1/2*a - 1/2*c)^2*tan(1/2*(b*c
+ c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2*tan(1/2*a - 1/2*c)^2*tan(1/2*(b*c -
c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2*tan(1/2*(b*c + c*d)/d)^2*tan(1/2*(b*c
- c*d)/d)^2 + b*d*tan(1/2*a - 1/2*c)^2*tan(1/2*(b*c + c*d)/d)^2*tan(1/2*(b
*c - c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2*tan(1/2*a - 1/2*c)^2 + b*d*tan(1/
2*a + 1/2*c)^2*tan(1/2*(b*c + c*d)/d)^2 + b*d*tan(1/2*a - 1/2*c)^2*tan(1/2*
(b*c + c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2*tan(1/2*(b*c - c*d)/d)^2 + b*d*
tan(1/2*a - 1/2*c)^2*tan(1/2*(b*c - c*d)/d)^2 + b*d*tan(1/2*(b*c + c*d)/d)^
2*tan(1/2*(b*c - c*d)/d)^2 + b*d*tan(1/2*a + 1/2*c)^2 + b*d*tan(1/2*a - 1/2
*c)^2 + b*d*tan(1/2*(b*c + c*d)/d)^2 + b*d*tan(1/2*(b*c - c*d)/d)^2 + b*d)
+ cos_integral(d*x + c)*sin(b*x + a)/b

```

$$3.136 \quad \int \frac{\cos(a+bx)\mathbf{CosIntegral}(c+dx)}{x} dx$$

Optimal. Leaf size=18

$$\text{CannotIntegrate}\left(\frac{\cos(a+bx)\mathbf{CosIntegral}(c+dx)}{x}, x\right)$$

[Out] CannotIntegrate[(Cos[a + b*x]*CosIntegral[c + d*x])/x, x]

Rubi [A] time = 0.0921269, antiderivative size = 0, normalized size of antiderivative = 0., number of steps used = 0, number of rules used = 0, integrand size = 0, $\frac{\text{number of rules}}{\text{integrand size}} = 0.$, Rules used = {}

$$\int \frac{\cos(a+bx)\mathbf{CosIntegral}(c+dx)}{x} dx$$

Verification is Not applicable to the result.

[In] Int[(Cos[a + b*x]*CosIntegral[c + d*x])/x, x]

[Out] Defer[Int] [(Cos[a + b*x]*CosIntegral[c + d*x])/x, x]

Rubi steps

$$\int \frac{\cos(a+bx)\mathbf{Ci}(c+dx)}{x} dx = \int \frac{\cos(a+bx)\mathbf{Ci}(c+dx)}{x} dx$$

Mathematica [A] time = 18.7056, size = 0, normalized size = 0.

$$\int \frac{\cos(a+bx)\mathbf{CosIntegral}(c+dx)}{x} dx$$

Verification is Not applicable to the result.

[In] Integrate[(Cos[a + b*x]*CosIntegral[c + d*x])/x, x]

[Out] Integrate[(Cos[a + b*x]*CosIntegral[c + d*x])/x, x]

Maple [A] time = 0.089, size = 0, normalized size = 0.

$$\int \frac{\mathbf{Ci}(dx+c)\cos(bx+a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(Ci(d*x+c)*cos(b*x+a)/x, x)

[Out] int(Ci(d*x+c)*cos(b*x+a)/x, x)

Maxima [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(dx + c) \cos(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*cos(b*x+a)/x,x, algorithm="maxima")

[Out] integrate(Ci(d*x + c)*cos(b*x + a)/x, x)

Fricas [A] time = 0., size = 0, normalized size = 0.

$$\text{integral}\left(\frac{\cos(bx + a) \text{Ci}(dx + c)}{x}, x\right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*cos(b*x+a)/x,x, algorithm="fricas")

[Out] integral(cos(b*x + a)*cos_integral(d*x + c)/x, x)

Sympy [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\cos(a + bx) \text{Ci}(c + dx)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*cos(b*x+a)/x,x)

[Out] Integral(cos(a + b*x)*Ci(c + d*x)/x, x)

Giac [A] time = 0., size = 0, normalized size = 0.

$$\int \frac{\text{Ci}(dx + c) \cos(bx + a)}{x} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate(Ci(d*x+c)*cos(b*x+a)/x,x, algorithm="giac")

[Out] integrate(Ci(d*x + c)*cos(b*x + a)/x, x)

Chapter 4

Listing of Grading functions

The following are the current version of the grading functions used for grading the quality of the antiderivative with reference to the optimal antiderivative included in the test suite.

There is a version for Maple and for Mathematica/Rubi. There is a version for grading Sympy and version for use with Sagemath.

The following are links to the current source code.

The following are the listings of source code of the grading functions.

4.0.1 Mathematica and Rubi grading function

```
1 (* Original version thanks to Albert Rich emailed on 03/21/2017 *)
2 (* ::Package:: *)
3
4 (* ::Subsection:: *)
5 (*GradeAntiderivative[result,optimal]*)
6
7
8 (* ::Text:: *)
9 (*If result and optimal are mathematical expressions, *)
10 (*      GradeAntiderivative[result,optimal] returns*)
11 (* "F" if the result fails to integrate an expression that*)
12 (*   is integrable*)
13 (* "C" if result involves higher level functions than necessary*)
14 (* "B" if result is more than twice the size of the optimal*)
15 (*   antiderivative*)
16 (* "A" if result can be considered optimal*)
17
18
19 GradeAntiderivative[result_,optimal_] :=
20   If[ExpnType[result]<=ExpnType[optimal],
21     If[FreeQ[result,Complex] || Not[FreeQ[optimal,Complex]],
22       If[LeafCount[result]<=2*LeafCount[optimal],
23         "A",
24         "B"],
25       "C"],
26     If[FreeQ[result,Integrate] && FreeQ[result,Int],
27       "C",
28       "F"]]
29
30
31 (* ::Text:: *)
32 (*The following summarizes the type number assigned an *)
33 (*expression based on the functions it involves*)
34 (*1 = rational function*)
35 (*2 = algebraic function*)
36 (*3 = elementary function*)
37 (*4 = special function*)
```



```

101 AppellFunctionQ[func_] :=
102   MemberQ[{AppellF1},func]

```

4.0.2 Maple grading function

```

1 # File: GradeAntiderivative.mpl
2 # Original version thanks to Albert Rich emailed on 03/21/2017
3
4 #Nasser 03/22/2017 Use Maple leaf count instead since buildin
5 #Nasser 03/23/2017 missing 'ln' for ElementaryFunctionQ added
6 #Nasser 03/24/2017 corrected the check for complex result
7 #Nasser 10/27/2017 check for leafsize and do not call ExpnType()
8 # if leaf size is "too large". Set at 500,000
9 #Nasser 12/22/2019 Added debug flag, added 'dilog' to special functions
10 # see problem 156, file Apostol_Problems
11
12 GradeAntiderivative := proc(result,optimal)
13 local leaf_count_result, leaf_count_optimal,ExpnType_result,ExpnType_optimal,
14     debug:=false;
15
16     leaf_count_result:=leafcount(result);
17     #do NOT call ExpnType() if leaf size is too large. Recursion problem
18     if leaf_count_result > 500000 then
19         return "B";
20     fi;
21
22     leaf_count_optimal:=leafcount(optimal);
23
24     ExpnType_result:=ExpnType(result);
25     ExpnType_optimal:=ExpnType(optimal);
26
27     if debug then
28         print("ExpnType_result",ExpnType_result," ExpnType_optimal=",
29             ExpnType_optimal);
30     fi;
31
32 # If result and optimal are mathematical expressions,
33 # GradeAntiderivative[result,optimal] returns
34 # "F" if the result fails to integrate an expression that
35 # is integrable
36 # "C" if result involves higher level functions than necessary
37 # "B" if result is more than twice the size of the optimal
38 # antiderivative
39 # "A" if result can be considered optimal
40
41 #This check below actually is not needed, since I only
42 #call this grading only for passed integrals. i.e. I check
43 #for "F" before calling this. But no harm of keeping it here.
44 #just in case.
45
46 if not type(result,freeof('int')) then
47     return "F";
48 end if;
49
50 if ExpnType_result<=ExpnType_optimal then
51     if debug then
52         print("ExpnType_result<=ExpnType_optimal");
53     fi;
54     if is_contains_complex(result) then
55         if is_contains_complex(optimal) then
56             if debug then

```

```

57         print("both result and optimal complex");
58         fi;
59         #both result and optimal complex
60         if leaf_count_result<=2*leaf_count_optimal then
61             return "A";
62         else
63             return "B";
64         end if
65     else #result contains complex but optimal is not
66         if debug then
67             print("result contains complex but optimal is not");
68         fi;
69         return "C";
70     end if
71 else # result do not contain complex
72     # this assumes optimal do not as well
73     if debug then
74         print("result do not contain complex, this assumes optimal do
not as well");
75     fi;
76     if leaf_count_result<=2*leaf_count_optimal then
77         if debug then
78             print("leaf_count_result<=2*leaf_count_optimal");
79         fi;
80         return "A";
81     else
82         if debug then
83             print("leaf_count_result>2*leaf_count_optimal");
84         fi;
85         return "B";
86     end if
87 end if
88 else #ExpnType(result) > ExpnType(optimal)
89     if debug then
90         print("ExpnType(result) > ExpnType(optimal)");
91     fi;
92     return "C";
93 end if
94
95 end proc:
96
97 #
98 # is_contains_complex(result)
99 # takes expressions and returns true if it contains "I" else false
100 #
101 #Nasser 032417
102 is_contains_complex:= proc(expression)
103     return (has(expression,I));
104 end proc:
105
106 # The following summarizes the type number assigned an expression
107 # based on the functions it involves
108 # 1 = rational function
109 # 2 = algebraic function
110 # 3 = elementary function
111 # 4 = special function
112 # 5 = hyperpergeometric function
113 # 6 = appell function
114 # 7 = rootsum function
115 # 8 = integrate function
116 # 9 = unknown function
117
118 ExpnType := proc(expn)

```

```

119   if type(expn,'atomic') then
120       1
121   elif type(expn,'list') then
122       apply(max,map(ExpnType,expn))
123   elif type(expn,'sqrt') then
124       if type(op(1,expn),'rational') then
125           1
126       else
127           max(2,ExpnType(op(1,expn)))
128       end if
129   elif type(expn,'^^') then
130       if type(op(2,expn),'integer') then
131           ExpnType(op(1,expn))
132       elif type(op(2,expn),'rational') then
133           if type(op(1,expn),'rational') then
134               1
135           else
136               max(2,ExpnType(op(1,expn)))
137           end if
138       else
139           max(3,ExpnType(op(1,expn)),ExpnType(op(2,expn)))
140       end if
141   elif type(expn,'+`') or type(expn,'*`') then
142       max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
143   elif ElementaryFunctionQ(op(0,expn)) then
144       max(3,ExpnType(op(1,expn)))
145   elif SpecialFunctionQ(op(0,expn)) then
146       max(4,apply(max,map(ExpnType,[op(expn)])))
147   elif HypergeometricFunctionQ(op(0,expn)) then
148       max(5,apply(max,map(ExpnType,[op(expn)])))
149   elif AppellFunctionQ(op(0,expn)) then
150       max(6,apply(max,map(ExpnType,[op(expn)])))
151   elif op(0,expn)='int' then
152       max(8,apply(max,map(ExpnType,[op(expn)]))) else
153       9
154   end if
155 end proc:
156
157
158 ElementaryFunctionQ := proc(func)
159     member(func,[
160         exp,log,ln,
161         sin,cos,tan,cot,sec,csc,
162         arcsin,arccos,arctan,arccot,arcsec,arccsc,
163         sinh,cosh,tanh,coth,sech,csch,
164         arcsinh,arccosh,arctanh,arccoth,arcsech,arccsch])
165 end proc:
166
167 SpecialFunctionQ := proc(func)
168     member(func,[
169         erf,erfc,erfi,
170         FresnelS,FresnelC,
171         Ei,Ei,Li,Si,Ci,Shi,Chi,
172         GAMMA,lnGAMMA,Psi,Zeta,polylog,dilog,LambertW,
173         EllipticF,EllipticE,EllipticPi])
174 end proc:
175
176 HypergeometricFunctionQ := proc(func)
177     member(func,[Hypergeometric1F1,hypergeom,HypergeometricPFQ])
178 end proc:
179
180 AppellFunctionQ := proc(func)
181     member(func,[AppellF1])

```

```

182 end proc:
183
184 # u is a sum or product. rest(u) returns all but the
185 # first term or factor of u.
186 rest := proc(u) local v;
187     if nops(u)=2 then
188         op(2,u)
189     else
190         apply(op(0,u),op(2..nops(u),u))
191     end if
192 end proc:
193
194 #leafcount(u) returns the number of nodes in u.
195 #Nasser 3/23/17 Replaced by build-in leafCount from package in Maple
196 leafcount := proc(u)
197     MmaTranslator[Mma][LeafCount](u);
198 end proc:

```

4.0.3 Sympy grading function

```

1 #Dec 24, 2019. Nasser M. Abbasi:
2 #           Port of original Maple grading function by
3 #           Albert Rich to use with Sympy/Python
4 #Dec 27, 2019 Nasser. Added `RootSum`. See problem 177, Timofeev file
5 #           added 'exp_polar'
6 from sympy import *
7
8 def leaf_count(expr):
9     #sympy do not have leaf count function. This is approximation
10    return round(1.7*count_ops(expr))
11
12 def is_sqrt(expr):
13     if isinstance(expr,Pow):
14         if expr.args[1] == Rational(1,2):
15             return True
16         else:
17             return False
18     else:
19         return False
20
21 def is_elementary_function(func):
22     return func in [exp,log,ln,sin,cos,tan,cot,sec,csc,
23                    asin,acos,atan,acot,asec,acsc,sinh,cosh,tanh,coth,sech,csch,
24                    asinh,acosh,atanh,acoth,asech,acsch
25                    ]
26
27 def is_special_function(func):
28     return func in [ erf,erfc,erfi,
29                    fresnels,fresnelc,Ei,Ei,Li,Si,Ci,Shi,Chi,
30                    gamma,loggamma,digamma,zeta,polylog,LambertW,
31                    elliptic_f,elliptic_e,elliptic_pi,exp_polar
32                    ]
33
34 def is_hypergeometric_function(func):
35     return func in [hyper]
36
37 def is_appell_function(func):
38     return func in [appellf1]
39
40 def is_atom(expn):
41     try:
42         if expn.isAtom or isinstance(expn,int) or isinstance(expn,float):
43             return True

```

```

44     else:
45         return False
46
47     except AttributeError as error:
48         return False
49
50 def expnType(expn):
51     debug=False
52     if debug:
53         print("expn=",expn,"type(expn)=",type(expn))
54
55     if is_atom(expn):
56         return 1
57     elif isinstance(expn,list):
58         return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
59     elif is_sqrt(expn):
60         if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
61             return 1
62         else:
63             return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn)))
64     elif isinstance(expn,Pow): #type(expn,``^`)
65         if isinstance(expn.args[1],Integer): #type(op(2,expn),'integer')
66             return expnType(expn.args[0]) #ExpnType(op(1,expn))
67         elif isinstance(expn.args[1],Rational): #type(op(2,expn),'rational')
68             if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
69                 return 1
70             else:
71                 return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn
72 )))
73     else:
74         return max(3,expnType(expn.args[0]),expnType(expn.args[1])) #max(3,
75 ExpnType(op(1,expn)),ExpnType(op(2,expn)))
76     elif isinstance(expn,Add) or isinstance(expn,Mul): #type(expn,``+`) or
77 type(expn,``*`)
78     m1 = expnType(expn.args[0])
79     m2 = expnType(list(expn.args[1:]))
80     return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
81     elif is_elementary_function(expn.func): #ElementaryFunctionQ(op(0,expn))
82     return max(3,expnType(expn.args[0])) #max(3,ExpnType(op(1,expn)))
83     elif is_special_function(expn.func): #SpecialFunctionQ(op(0,expn))
84     m1 = max(map(expnType, list(expn.args)))
85     return max(4,m1) #max(4,apply(max,map(ExpnType,[op(expn)])))
86     elif is_hypergeometric_function(expn.func): #HypergeometricFunctionQ(op(0,
87 expn))
88     m1 = max(map(expnType, list(expn.args)))
89     return max(5,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
90     elif is_appell_function(expn.func):
91     m1 = max(map(expnType, list(expn.args)))
92     return max(6,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
93     elif isinstance(expn,RootSum):
94     m1 = max(map(expnType, list(expn.args))) #Apply[Max,Append[Map[ExpnType
95 ,Apply[List,expn]],7]],
96     return max(7,m1)
97     elif str(expn).find("Integral") != -1:
98     m1 = max(map(expnType, list(expn.args)))
99     return max(8,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
100     else:
101     return 9
102
103 #main function
104 def grade_antiderivative(result,optimal):
105
106     leaf_count_result = leaf_count(result)

```

```

102 leaf_count_optimal = leaf_count(optimal)
103
104 expnType_result = expnType(result)
105 expnType_optimal = expnType(optimal)
106
107 if str(result).find("Integral") != -1:
108     return "F"
109
110 if expnType_result <= expnType_optimal:
111     if result.has(I):
112         if optimal.has(I): #both result and optimal complex
113             if leaf_count_result <= 2*leaf_count_optimal:
114                 return "A"
115             else:
116                 return "B"
117         else: #result contains complex but optimal is not
118             return "C"
119     else: # result do not contain complex, this assumes optimal do not as
well
120         if leaf_count_result <= 2*leaf_count_optimal:
121             return "A"
122         else:
123             return "B"
124     else:
125         return "C"

```

4.0.4 SageMath grading function

```

1 #Dec 24, 2019. Nasser: Ported original Maple grading function by
2 #     Albert Rich to use with Sagemath. This is used to
3 #     grade Fracas, Giac and Maxima results.
4 #Dec 24, 2019. Nasser: Added 'exp_integral_e' and 'sng', 'sin_integral'
5 #     'arctan2','floor','abs','log_integral'
6
7 from sage.all import *
8 from sage.symbolic.operators import add_vararg, mul_vararg
9
10 def tree(expr):
11     debug=False;
12     if debug:
13         print ("Enter tree(expr), expr=",expr)
14         print ("expr.operator()=",expr.operator())
15         print ("expr.operands()=",expr.operands())
16         print ("map(tree, expr.operands()=",map(tree, expr.operands()))
17
18     if expr.operator() is None:
19         return expr
20     else:
21         return [expr.operator()+list(map(tree, expr.operands()))
22
23 def leaf_count(anti):
24     debug=False;
25
26     if debug: print ("Enter leaf_count, anti=", anti, " len(anti)=", len(anti))
27
28     if len(anti) == 0: #special check for optimal being 0 for some test cases.
29         if debug: print ("len(anti) == 0")
30         return 1
31     else:
32         if debug: print ("round(1.35*len(flatten(tree(anti))))=",round(1.35*len
(flatten(tree(anti))))
33         return round(1.35*len(flatten(tree(anti)))) #fudge factor
34             #since this estimate of leaf count is bit lower than

```



```

35         #what it should be compared to Mathematica's
36
37 def is_sqrt(expr):
38     debug=False;
39     if expr.operator() == operator.pow: #isinstance(expr,Pow):
40         if expr.operands()[1]==1/2: #expr.args[1] == Rational(1,2):
41             if debug: print ("expr is sqrt")
42             return True
43         else:
44             return False
45     else:
46         return False
47
48 def is_elementary_function(func):
49     debug = False
50
51     m = func.name() in ['exp','log','ln',
52         'sin','cos','tan','cot','sec','csc',
53         'arcsin','arccos','arctan','arccot','arcsec','arccsc',
54         'sinh','cosh','tanh','coth','sech','csch',
55         'arcsinh','arccosh','arctanh','arccoth','arcsech','arccsch','sgn',
56         'arctan2','floor','abs'
57     ]
58     if debug:
59         if m:
60             print ("func ", func , " is elementary_function")
61         else:
62             print ("func ", func , " is NOT elementary_function")
63
64
65     return m
66
67 def is_special_function(func):
68     debug = False
69
70     if debug: print ("type(func)=", type(func))
71
72     m= func.name() in ['erf','erfc','erfi','fresnel_sin','fresnel_cos','Ei',
73         'Ei','Li','Si','sin_integral','Ci','cos_integral','Shi','
74     sinh_integral'
75         'Chi','cosh_integral','gamma','log_gamma','psi,zeta',
76         'polylog','lambert_w','elliptic_f','elliptic_e',
77         'elliptic_pi','exp_integral_e','log_integral']
78
79     if debug:
80         print ("m=",m)
81         if m:
82             print ("func ", func , " is special_function")
83         else:
84             print ("func ", func , " is NOT special_function")
85
86     return m
87
88
89 def is_hypergeometric_function(func):
90     return func.name() in ['hypergeometric','hypergeometric_M','
91     hypergeometric_U']
92
93 def is_appell_function(func):
94     return func.name() in ['hypergeometric'] #[appellf1] can't find this in
95     sagemath

```

```

95 def is_atom(expn):
96
97     #thanks to answer at https://ask.sagemath.org/question/49179/what-is-
sagemath-equivalent-to-atomic-type-in-maple/
98     try:
99         if expn.parent() is SR:
100             return expn.operator() is None
101         if expn.parent() in (ZZ, QQ, AA, QQbar):
102             return expn in expn.parent() # Should always return True
103         if hasattr(expn.parent(),"base_ring") and hasattr(expn.parent(),"gens")
:
104             return expn in expn.parent().base_ring() or expn in expn.parent().
gens()
105         return False
106
107     except AttributeError as error:
108         return False
109
110
111 def expnType(expn):
112     debug=False
113
114     if debug:
115         print(">>>>Enter expnType, expn=", expn)
116         print(">>>>is_atom(expn)=", is_atom(expn))
117
118     if is_atom(expn):
119         return 1
120     elif type(expn)==list: #instance(expn,list):
121         return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
122     elif is_sqrt(expn):
123         if type(expn.operands()[0])==Rational: #type(instance(expn.args[0],
Rational):
124             return 1
125         else:
126             return max(2,expnType(expn.operands()[0])) #max(2,expnType(expn.
args[0]))
127     elif expn.operator() == operator.pow: #instance(expn,Pow)
128         if type(expn.operands()[1])==Integer: #instance(expn.args[1],Integer
)
129             return expnType(expn.operands()[0]) #expnType(expn.args[0])
130         elif type(expn.operands()[1])==Rational: #instance(expn.args[1],
Rational)
131             if type(expn.operands()[0])==Rational: #instance(expn.args[0],
Rational)
132                 return 1
133             else:
134                 return max(2,expnType(expn.operands()[0])) #max(2,expnType(
expn.args[0]))
135         else:
136             return max(3,expnType(expn.operands()[0]),expnType(expn.operands()
[1])) #max(3,expnType(expn.operands()[0]),expnType(expn.operands()[1]))
137     elif expn.operator() == add_vararg or expn.operator() == mul_vararg: #
instance(expn,Add) or instance(expn,Mul)
138         m1 = expnType(expn.operands()[0]) #expnType(expn.args[0])
139         m2 = expnType(expn.operands()[1:]) #expnType(list(expn.args[1:]))
140         return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn)))
141     elif is_elementary_function(expn.operator()): #is_elementary_function(expn
.func)
142         return max(3,expnType(expn.operands()[0]))
143     elif is_special_function(expn.operator()): #is_special_function(expn.func)
144         m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(
expn.args)))

```

```

145     return max(4,m1)    #max(4,m1)
146     elif is_hypergeometric_function(expn.operator()): #
is_hypergeometric_function(expn.func)
147         m1 = max(map(expnType, expn.operands()))    #max(map(expnType, list(
expn.args)))
148         return max(5,m1)    #max(5,m1)
149     elif is_appell_function(expn.operator()):
150         m1 = max(map(expnType, expn.operands()))    #max(map(expnType, list(
expn.args)))
151         return max(6,m1)    #max(6,m1)
152     elif str(expn).find("Integral") != -1: #this will never happen, since it
153         #is checked before calling the grading function that is passed.
154         #but kept it here.
155         m1 = max(map(expnType, expn.operands()))    #max(map(expnType, list(
expn.args)))
156         return max(8,m1)    #max(5,apply(max,map(ExpnType,[op(expn)])))
157     else:
158         return 9
159
160 #main function
161 def grade_antiderivative(result,optimal):
162     debug = False;
163
164     if debug: print ("Enter grade_antiderivative for sagemath")
165
166     leaf_count_result = leaf_count(result)
167     leaf_count_optimal = leaf_count(optimal)
168
169     if debug: print ("leaf_count_result=", leaf_count_result, "
leaf_count_optimal=",leaf_count_optimal)
170
171
172     expnType_result = expnType(result)
173     expnType_optimal = expnType(optimal)
174
175     if debug: print ("expnType_result=", expnType_result, "expnType_optimal=",
expnType_optimal)
176
177     if expnType_result <= expnType_optimal:
178         if result.has(I):
179             if optimal.has(I): #both result and optimal complex
180                 if leaf_count_result <= 2*leaf_count_optimal:
181                     return "A"
182                 else:
183                     return "B"
184             else: #result contains complex but optimal is not
185                 return "C"
186         else: # result do not contain complex, this assumes optimal do not as
well
187             if leaf_count_result <= 2*leaf_count_optimal:
188                 return "A"
189             else:
190                 return "B"
191     else:
192         return "C"

```